

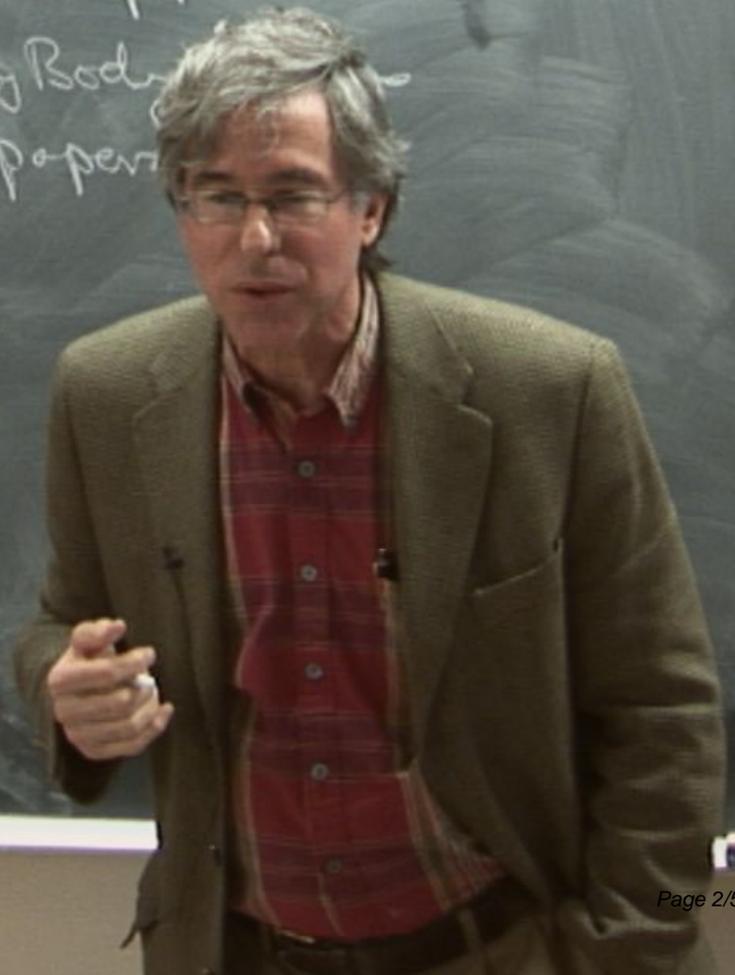
Title: Condensed Matter Review - Lecture 6

Date: Jan 10, 2011 10:15 AM

URL: <http://pirsa.org/11010028>

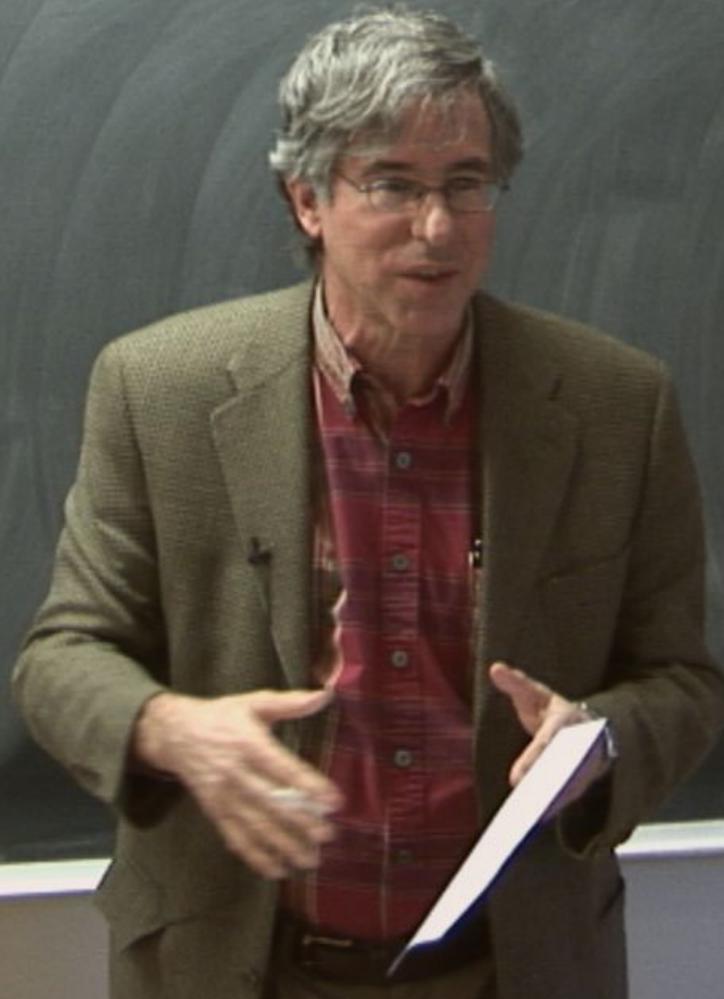
Abstract:

Landau's Fermi Liquid Theory
Refs: Piers Coleman's book - Chap 7
Tony Leggett's RMP article on ^3He
Bruus + Flensberg Chap 15
Wen QFT of Many Bodies
Landau - original papers



Landau's Fermi Liquid Theory
refs: Piers Coleman's book - Chap 7
Tony Leggett's RMP article on ^3He
Bruus + Flensberg Chap 15
Wen QFT of Many Body Systems
Landau - original paper

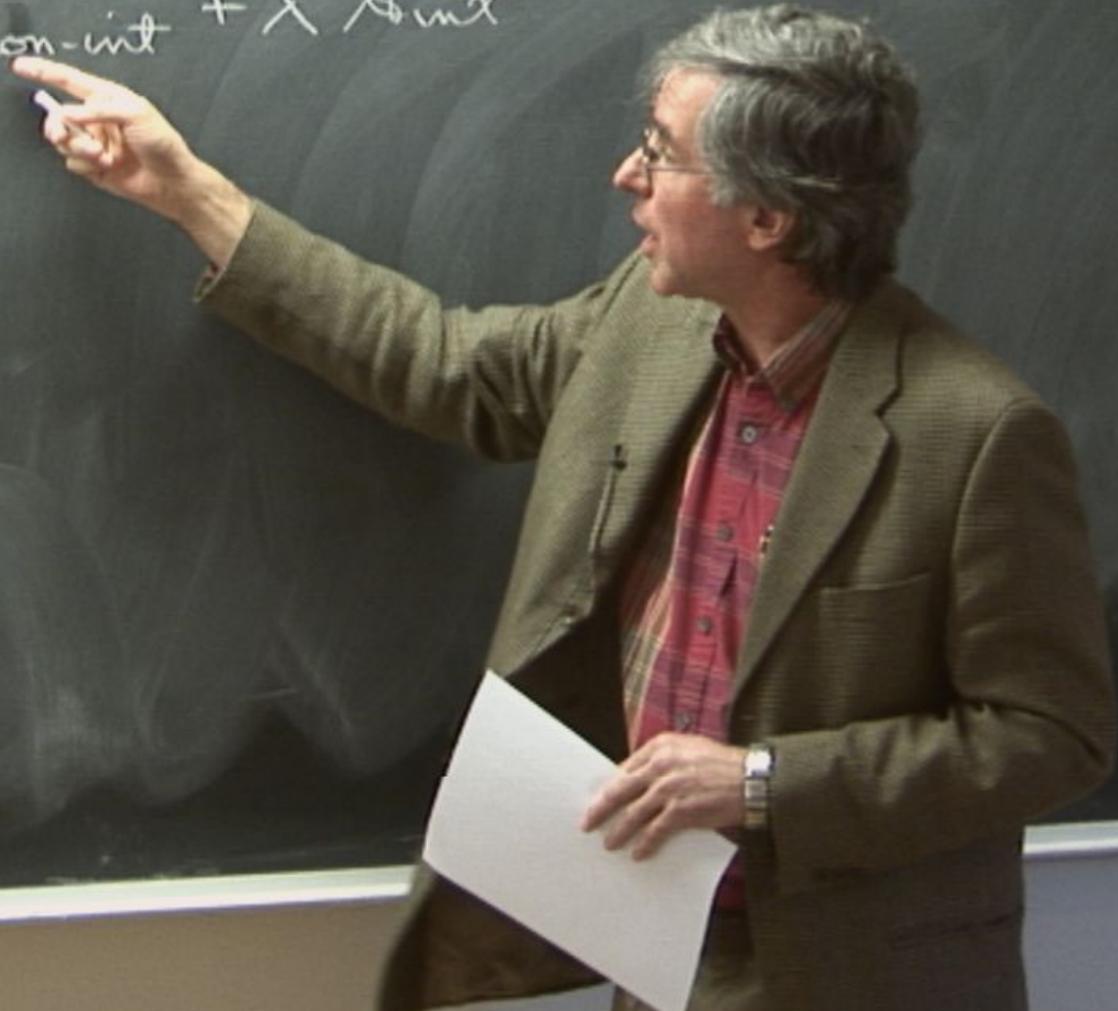
Adiabaticity



Adiabaticity

- effects of slowly turning
on el-el ints

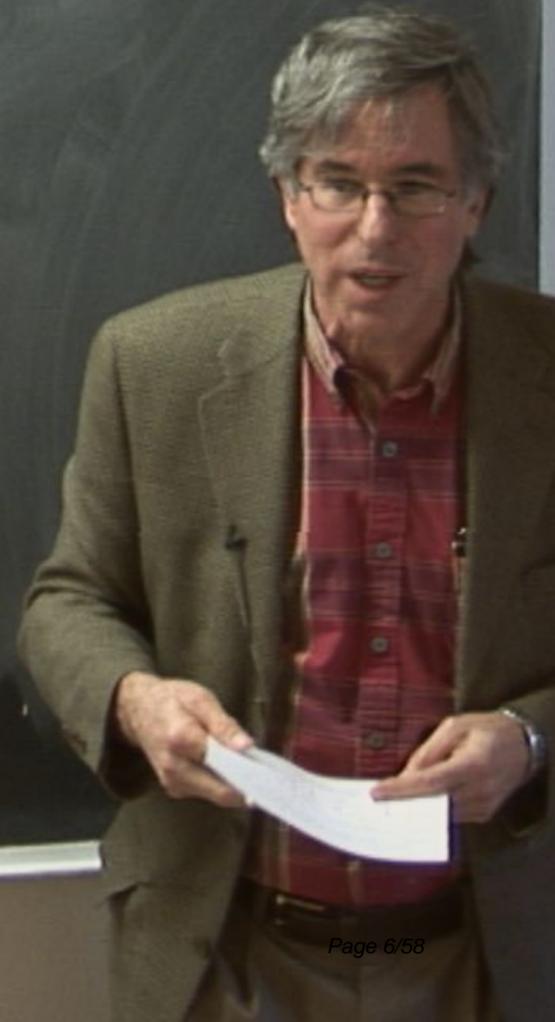
$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Adiabaticity

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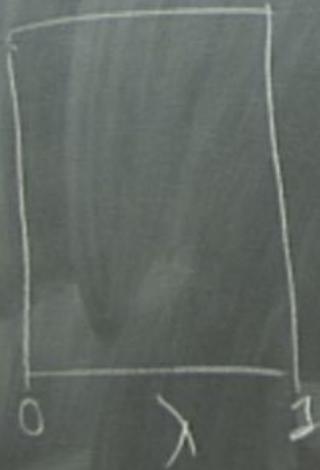
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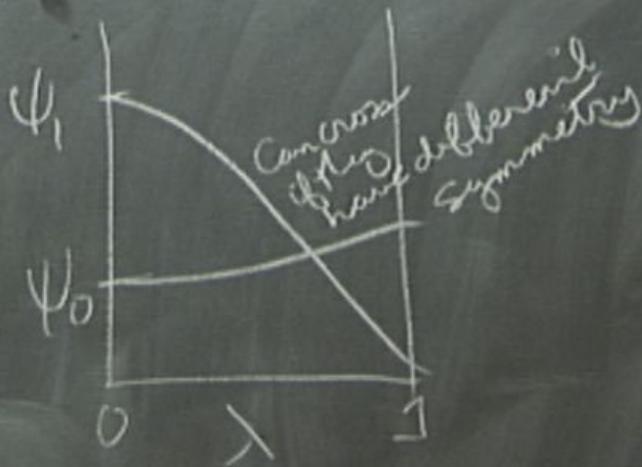
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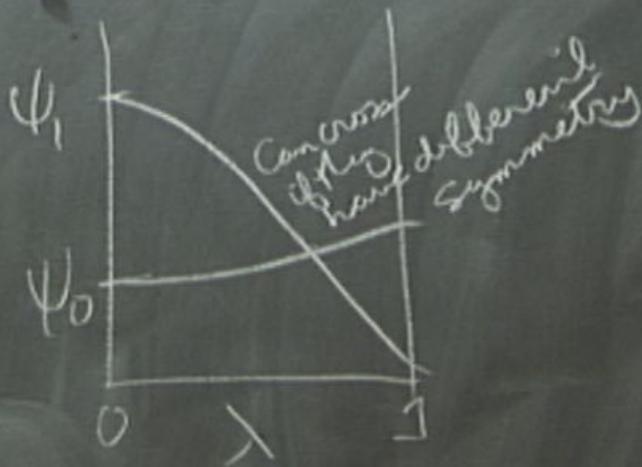
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Adiabaticity

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$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Phase Transition

Can cross if they
have different
symmetry

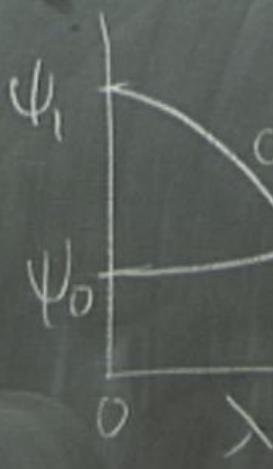
Adiabaticity

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$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$

Phase Transition

E
 E_1, E_2, E_3

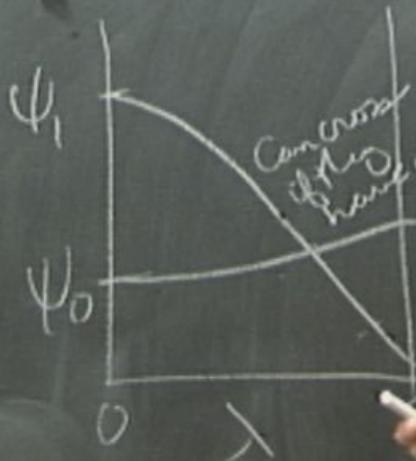
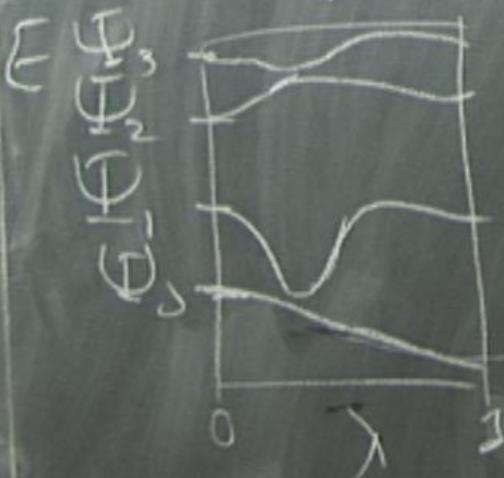


Concave
if they
have different
symmetry

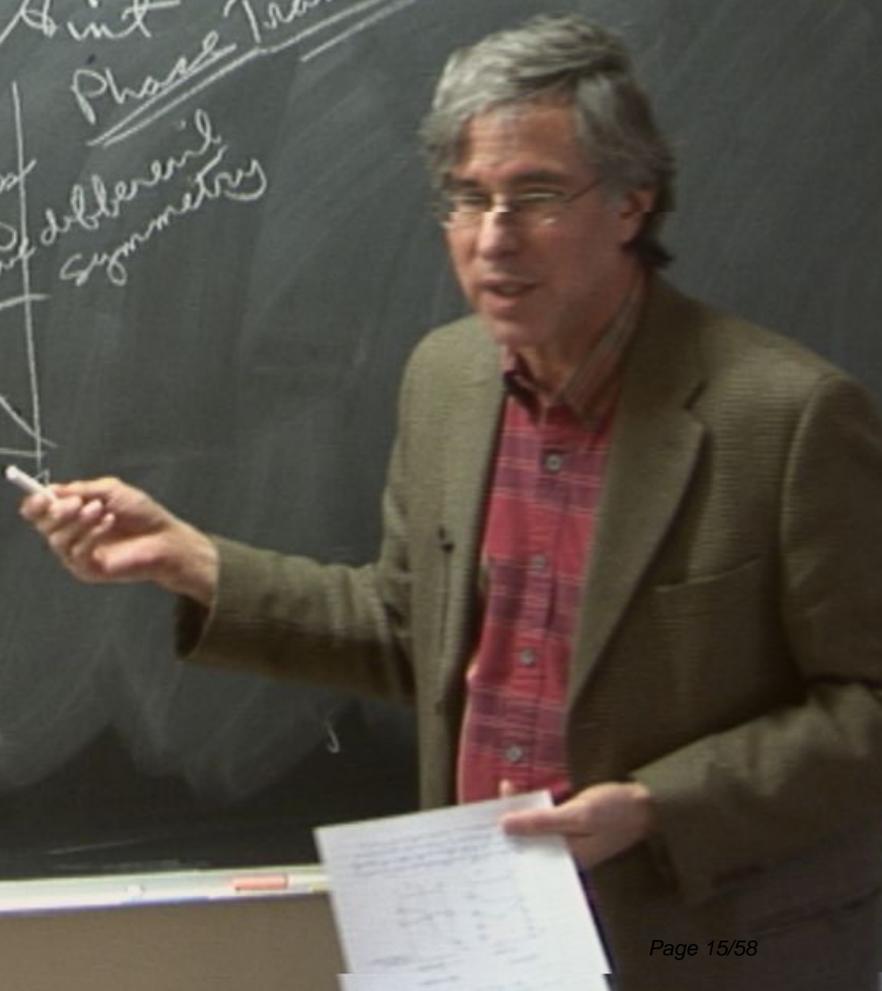
Adiabaticity

- effects of slowly turning
on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



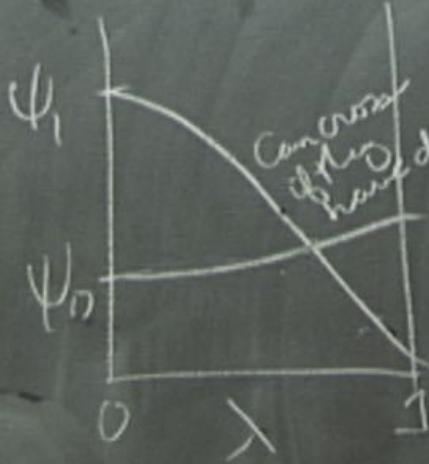
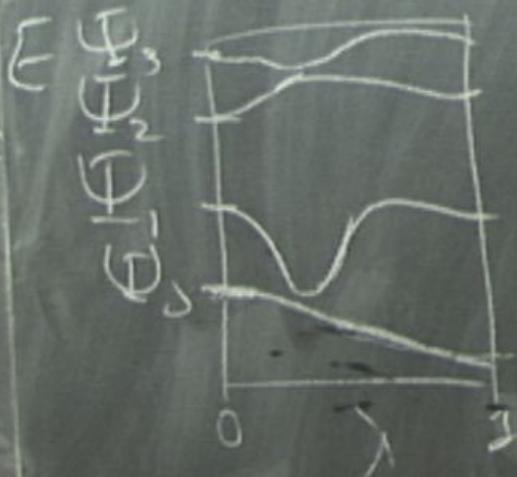
Phase Transition
Crossing if they have different symmetry



Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossed if they have different symmetry

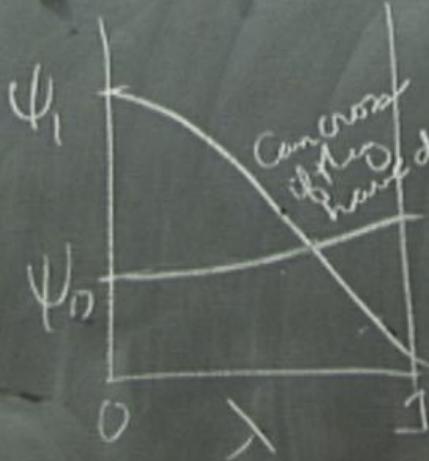
Phase Transition

$$\Psi_0^{\text{non-int}} (\{n_{p,\sigma}\}) \rightarrow \Psi_0^{\text{int}}$$

Adiabaticity

- effects of slowly turning
on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Phase Transition

$$\Psi_0^{\text{non-int}}(\{n_{p,\sigma}\})$$

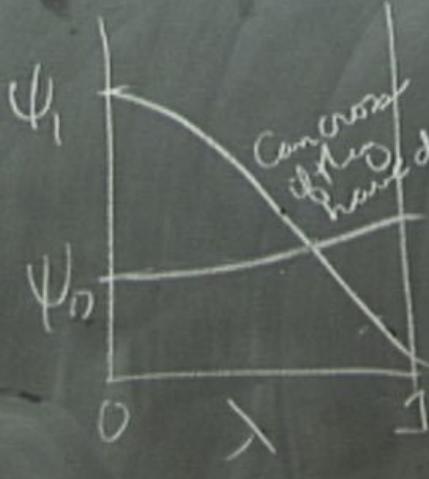
$$\Psi_0^{\text{int}}(\{n_{p,\sigma}\})$$

For fixed N_e

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Come across if they have different symmetry

Phase Transitions

$$\Psi_0^{\text{non-int}} (\{n_{p,\sigma}\})$$

$$\Psi_0^{\text{int}} (\{n_{p,\sigma}\})$$

$n_{p,\sigma} = \begin{cases} 1 & \text{for } |p| < p_F \\ 0 & \text{otherwise} \end{cases}$

For fixed N_{el}

Adiabaticity

- effects of slowly turning on el-el ints

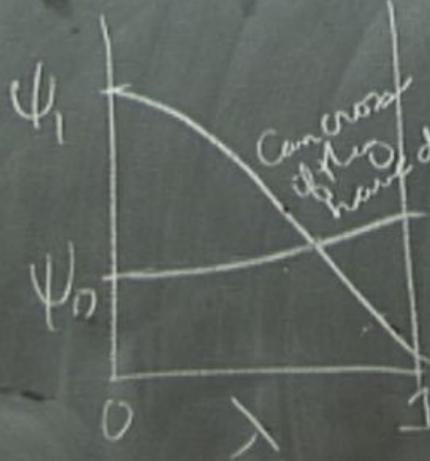
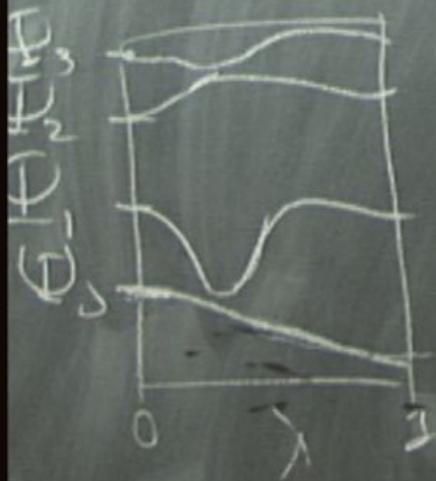
$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$

Assuming
Uniform
isotropic
liquid

$$N_{p,\sigma} \begin{cases} = 1 & \text{for } |p| < p_F \\ = 0 & \text{otherwise} \end{cases}$$

For fixed
Nee

Phase Transition



Crossing if they have different symmetry

$$\Psi_0^{\text{non-int}} (\{N_{p,\sigma}\})$$

$$\rightarrow \Psi_0^{\text{int}} (\{N_{p,\sigma}\})$$

Adiabaticity

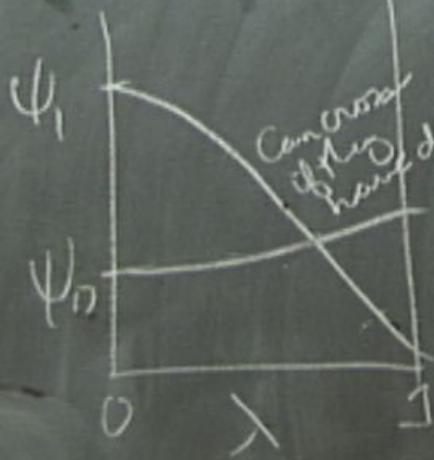
- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$

Assuming
Uniform
isotropic
liquid

$\eta_{\text{PF}} \begin{cases} = 1 & \text{for } |\rho| < \rho_F \\ = 0 & \text{otherwise} \end{cases}$
For fixed
Nee

Phase Transition



Concave
if they
have different
symmetry

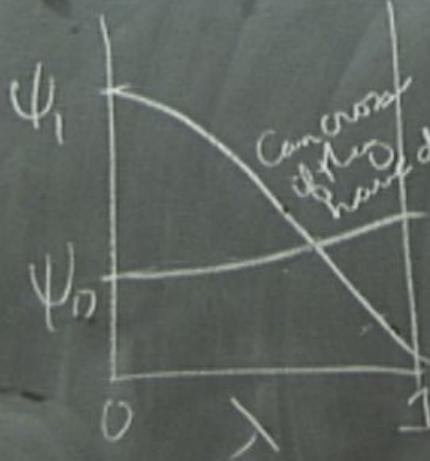
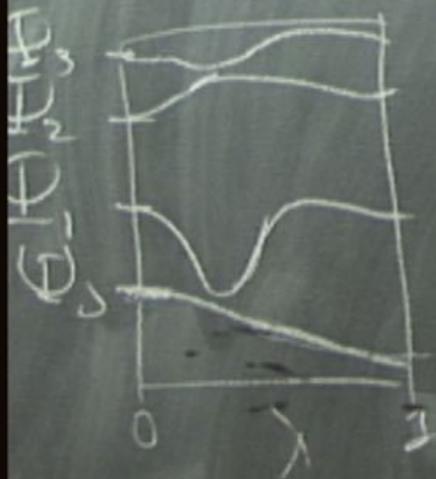
$$\Psi_0(\{\eta_{\text{PF}}\})$$

$$\Psi_0(\{\eta_{\text{PF}}\})$$

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossed if they have different symmetry

Phase Transitions

Assuming Uniform isotropic liquid

$\eta_{p,0} \begin{cases} = 1 & \text{for } |p| < p_F \\ = 0 & \text{otherwise} \end{cases}$

For fixed N_{el}

$$\Psi_0^{\text{non-int}}(\{N_{p,\sigma}\})$$

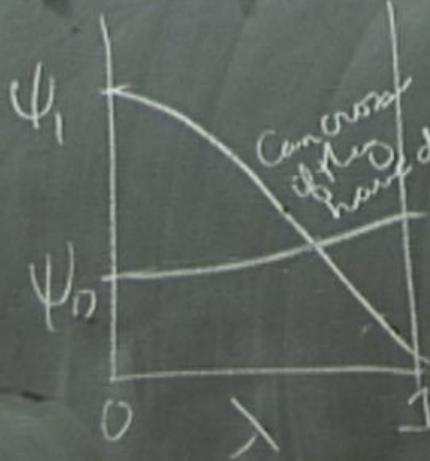
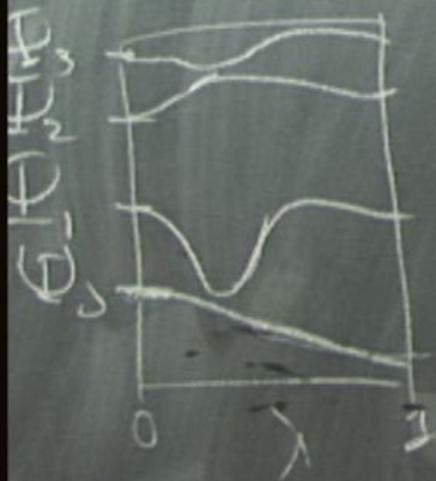
$$\Psi_0^{\text{int}}(\{N_{p,\sigma}\})$$

for both cases

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Assuming Uniform isotropic liquid

Phase Transitions

$$\Psi_0^{\text{non-int}} (\{N_{p,\sigma}\})$$

$\epsilon = 1$ for $|\vec{p}| < p_F$
 $\epsilon = 0$ otherwise

For fixed $N_{p,\sigma}$

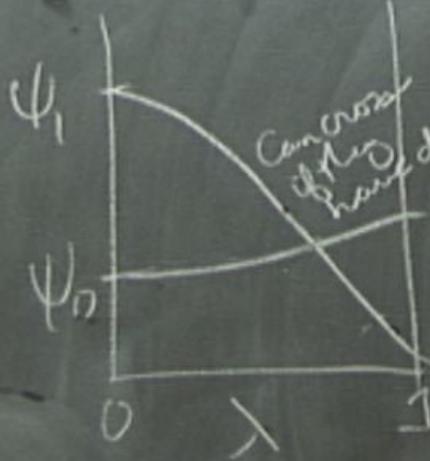
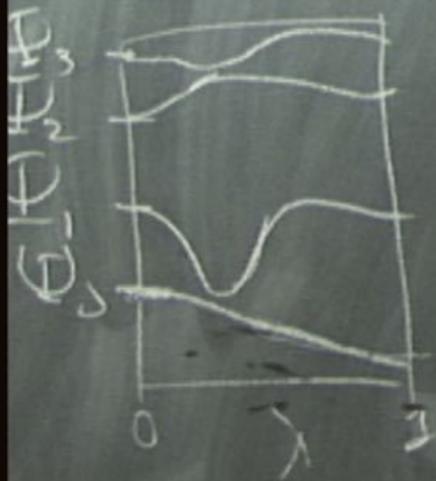
$$\Psi_0^{\text{int}} (\{N_{p,\sigma}\})$$

Need for both cases

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Assuming Uniform isotropic liquid

Phase Transition

$\Psi_{\vec{p}, \sigma} \in 1$ for $|\vec{p}| < p_F$
 $\in 0$ otherwise

For fixed N

$\Psi_{\vec{p}, \sigma}^{\text{non-int}}$

for both cases

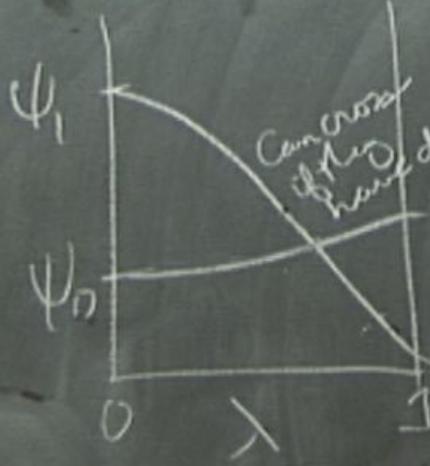
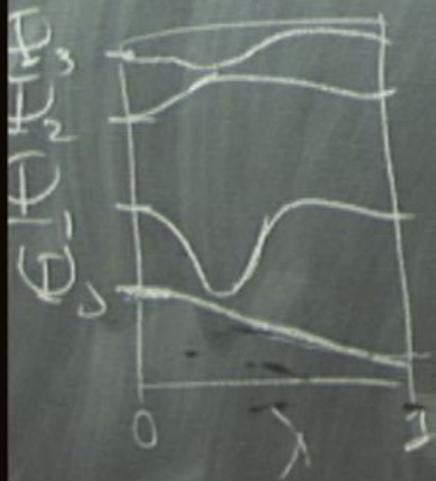
$\Psi_{\vec{p}, \sigma}^{\text{int}}$

The states labeled by \vec{p}, σ

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing of the levels
Phase Transition
different symmetry

Assuming
Uniform
isotropic
liquid

$\begin{cases} 1 & \text{for } |\vec{p}| < p_F \\ 0 & \text{otherwise} \end{cases}$

For fixed
Nee

Ψ_0 ($\{\vec{p}, \sigma\}$)
non-int

for both
cases

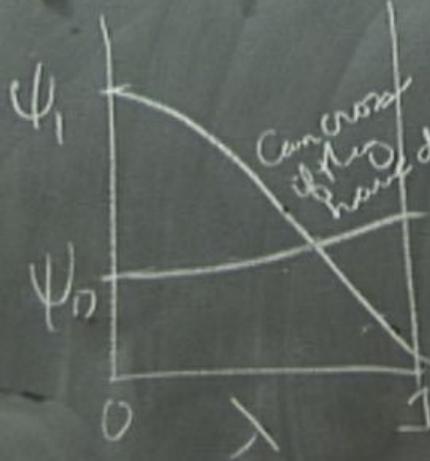
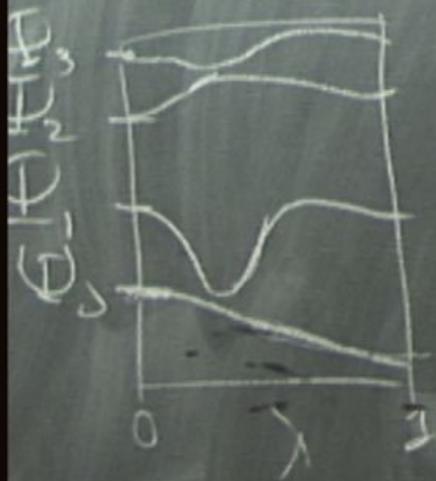
Ψ_0 ($\{\vec{p}, \sigma\}$)
int

The states labeled by \vec{p}, σ
Same \vec{p}, σ as for non-int case

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Phase Transition

Assuming Uniform isotropic liquid

$\epsilon = 1$ for $|\vec{p}| < p_F$
 $\epsilon = 0$ otherwise

For fixed N

Ψ_0 (non-int) $\{N_{\vec{p},\sigma}\}$

for both cases

Ψ_0 (int) $\{N_{\vec{p},\sigma}\}$

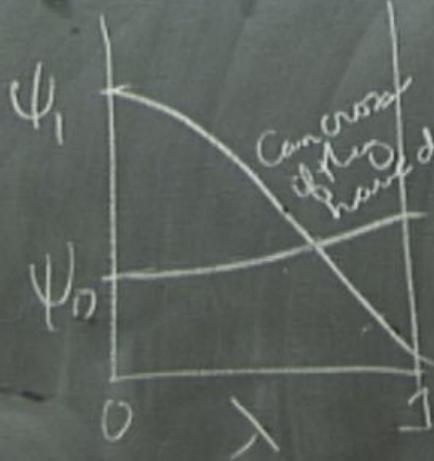
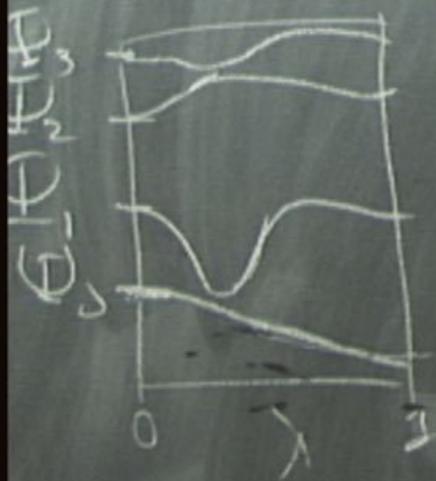
The states labeled by \vec{p}, σ
 Same \vec{p}, σ as for non-int case

What changes is $\epsilon_{\vec{p},\sigma} \leftrightarrow m^*$

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Phase Transition

Assuming Uniform isotropic liquid

$$N_{\vec{p}, \sigma} = \begin{cases} 1 & \text{for } |\vec{p}| < p_F \\ 0 & \text{otherwise} \end{cases}$$

$$\Psi_0 (\{N_{\vec{p}, \sigma}\})_{\text{non-int}}$$

For fixed Nee for both cases

$$\Psi_0 (\{N_{\vec{p}, \sigma}\})_{\text{int}}$$

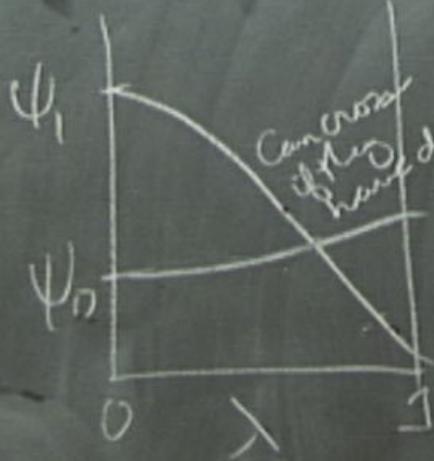
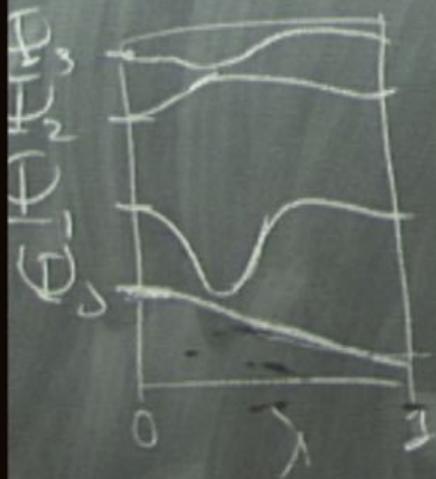
The states labeled by \vec{p}, σ
Same \vec{p}, σ as for non-int case

What changes is $\epsilon_{\vec{p}, \sigma} \leftrightarrow m^*$
and hence also $N^*(0)$

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Phase Transitions

Assuming Uniform isotropic liquid

$$N_{\vec{p}, \sigma} = \begin{cases} 1 & \text{for } |\vec{p}| < p_F \\ 0 & \text{otherwise} \end{cases}$$

For fixed $N_{\vec{p}, \sigma}$

$$\Psi_0(\{N_{\vec{p}, \sigma}\})_{\text{non-int}}$$

$$\Psi_0(\{N_{\vec{p}, \sigma}\})_{\text{int}}$$

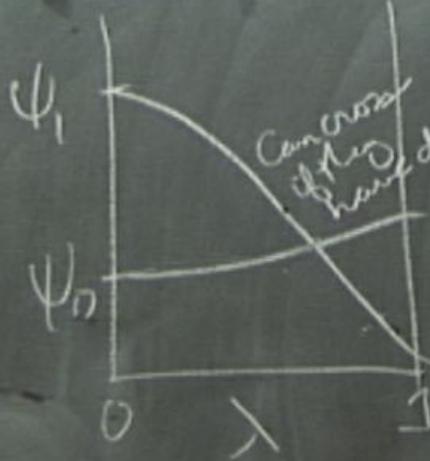
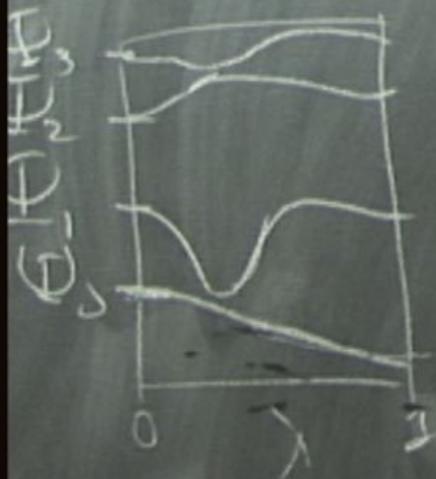
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$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Phase Transition

Assuming Uniform isotropic liquid

$$N_{\vec{p}, \sigma} = \begin{cases} 1 & \text{for } |\vec{p}| < p_F \\ 0 & \text{otherwise} \end{cases}$$

For fixed $N_{\vec{p}, \sigma}$

$$\Psi_0 (\{N_{\vec{p}, \sigma}\})_{\text{non-int}}$$

$$\rightarrow \Psi_0 (\{N_{\vec{p}, \sigma}\})_{\text{int}}$$

for both cases

The states labeled by \vec{p}, σ

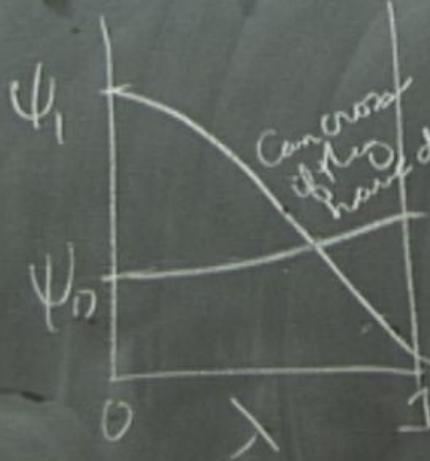
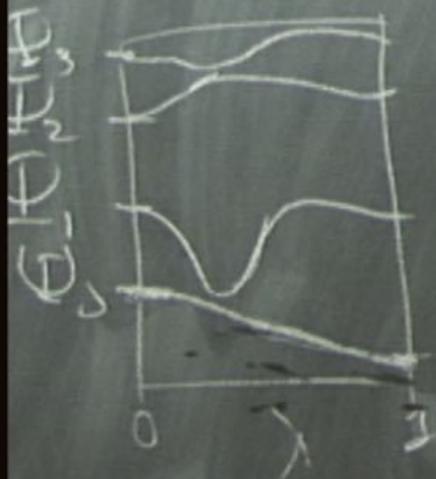
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Adiabaticity

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$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if they have different symmetry

Phase Transition

Assuming Uniform isotropic liquid

$$N_{\vec{p}, \sigma} = \begin{cases} 1 & \text{for } |\vec{p}| < p_F \\ 0 & \text{otherwise} \end{cases}$$

For fixed N

$$\Psi_0(\{N_{\vec{p}, \sigma}\})$$

$$\rightarrow \Psi_0(\{N_{\vec{p}, \sigma}\})$$

for both cases

The states labeled by \vec{p}, σ

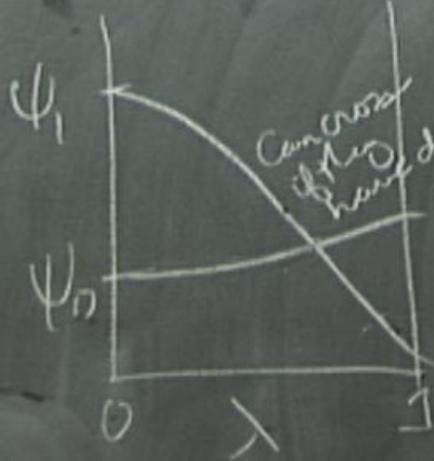
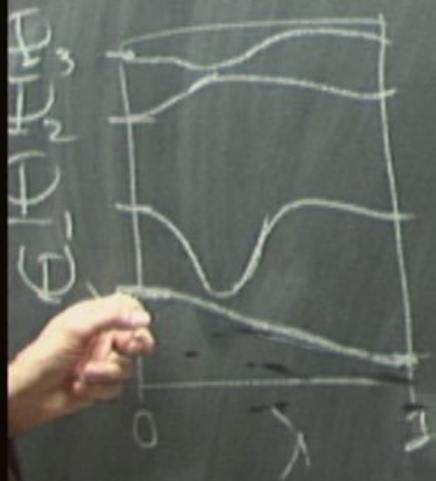
Same \vec{p}, σ as for non-int case

What changes is $\epsilon_{\vec{p}, \sigma} \leftrightarrow m^*$
 $\vec{v}_{\vec{p}, \sigma}$ and hence also $N^*(0)$

Adiabaticity

- effects of slowly turning on el-el ints

$$\mathcal{H} = \mathcal{H}_{\text{non-int}} + \lambda \mathcal{H}_{\text{int}}$$



Crossing if the two have different symmetry

Assuming Uniform isotropic liquid

Phase Transition

$$\Psi_0(\{\vec{p}, \sigma\})_{\text{non-int}}$$

$\epsilon = 1$ for $|\vec{p}| < p_F$
 $\epsilon = 0$ otherwise

For fixed N

Need for both cases

$$\Psi_0(\{\vec{p}, \sigma\})_{\text{int}}$$

The states labeled by \vec{p}, σ
Same \vec{p}, σ as for non-int case

What changes is $\epsilon_{\vec{p}, \sigma} \leftrightarrow m^*$
 $\vec{v}_{\vec{p}, \sigma}$ and hence also $N^*(0)$

Excitations:

Charged { Add an el with \vec{p}, σ ($|\vec{p}| > p_F$)
{ Remove el with \vec{p}', σ' ($|\vec{p}'| < p_F$)

Excitations

Charged Excitations

Add an el with \vec{p}, σ ($|\vec{p}| > p_F$)

Remove el with \vec{p}', σ' ($|\vec{p}'| < p_F$)

Both cost $|\epsilon_{\vec{p}, \sigma} - \mu| > 0$

$\vec{p}_i \rightarrow \vec{p}_i'$

Excitations

Charged Excitations

Add an el with \vec{p}, σ ($|\vec{p}| > p_F$)

(Remove el, with ^(hole) \vec{p}', σ' ($|\vec{p}'| < p_F$))

Both cost $|\epsilon_{\vec{p}, \sigma} - \mu| > 0$

$\vec{p} \rightarrow \vec{p}'$

Neutral Excitations — el-hole pair

Excitations

Charged Excitations

Add an el with \vec{p}, σ ($|\vec{p}| > p_F$)

(Remove el, with \vec{p}', σ' ($|\vec{p}'| < p_F$))

Both cost $|\epsilon_{\vec{p}, \sigma} - \mu| > 0$

$\vec{p} \rightarrow \vec{p}'$

Neutral Excitations — el-hole pair

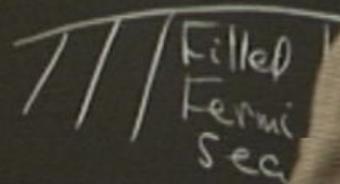
How stable are these excitations?

How stable are these excitations?
How quickly do they decay

How stable are these excitations?
How quickly do they decay
The decay rate $\frac{1}{\tau}$

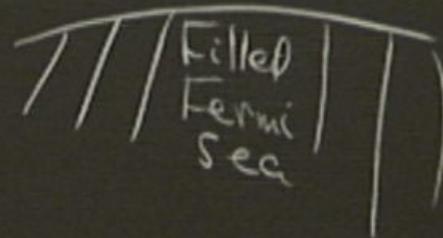
How stable are these excitations?
How quickly do they decay
The decay rate $\frac{1}{\tau} \sim \epsilon^2$

How stable are these excitations?
How quickly do they decay
The decay rate $\propto E^2$



How stable are these excitations?
How quickly do they decay

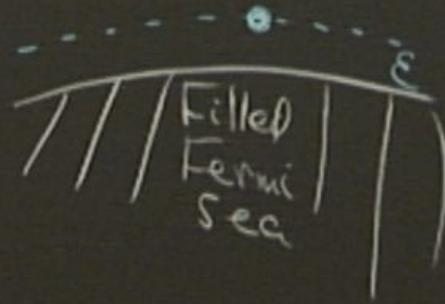
The decay rate $\frac{1}{\tau} \sim \epsilon^2$



How stable are these excitations?

How quickly do they decay

The decay rate $\frac{1}{\tau} \sim \epsilon^2$



How stable are these excitations?

How quickly do they decay

decay rate $\frac{1}{\tau} \sim \epsilon^2$



How stable are these excitations?
How quickly do they decay

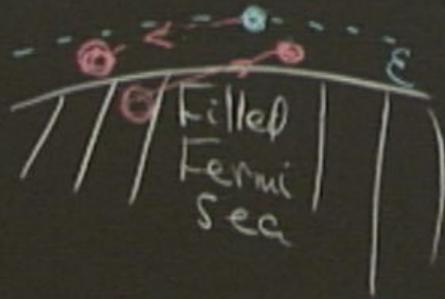
The decay rate $\frac{1}{\tau} \sim \epsilon^2$



How stable are these excitations?

How quickly do they decay

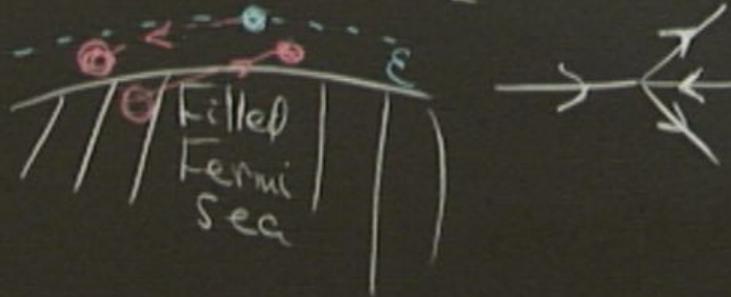
The decay rate $\frac{1}{\tau} \sim \epsilon^2$



How stable are these excitations?

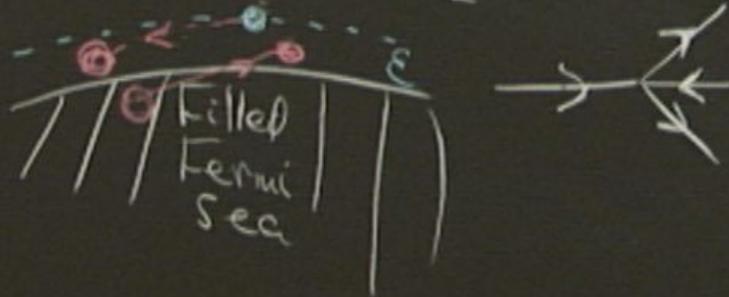
How quickly do they decay

The decay rate $\frac{1}{\tau} \sim \epsilon^2$



How stable are these excitations?
How quickly do they decay

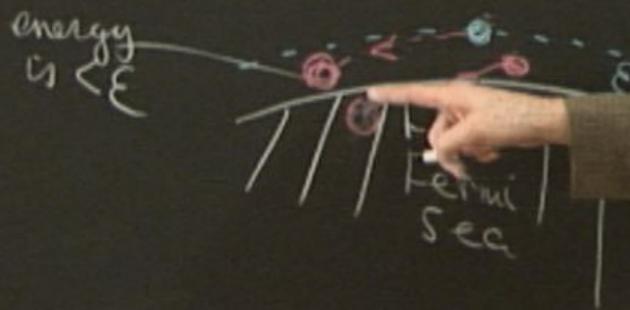
The decay rate $\frac{1}{\tau} \sim \epsilon^2$



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How stable are these excitations?

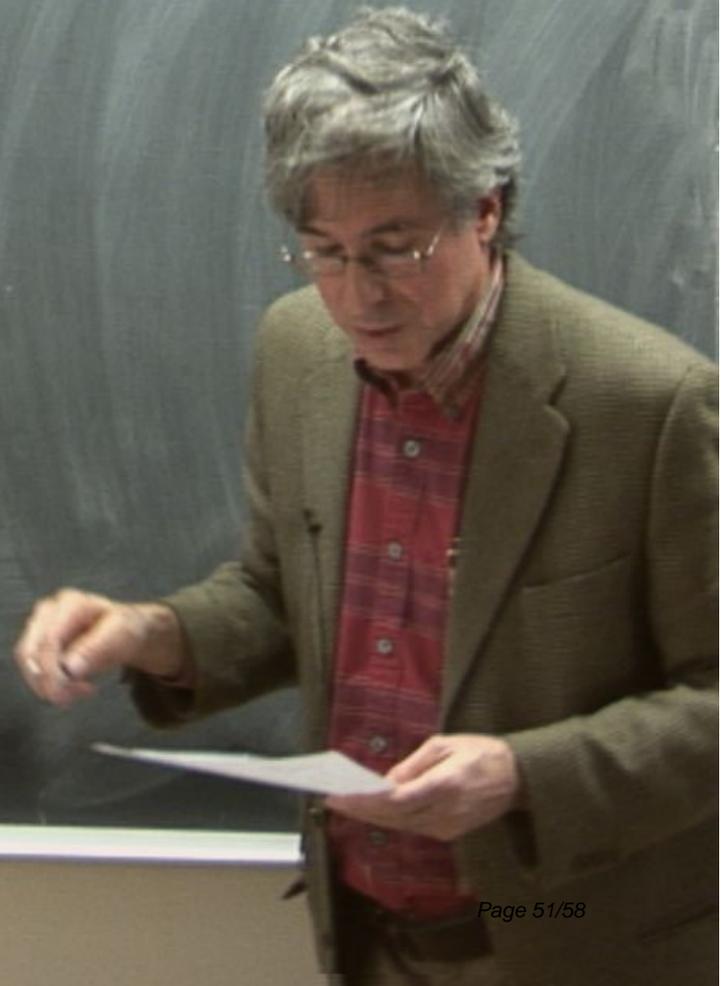
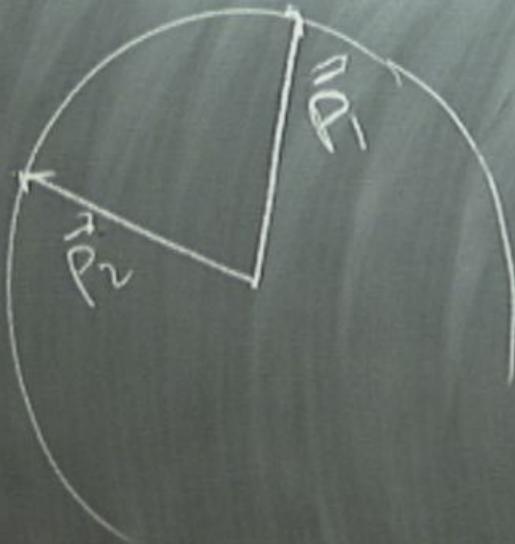
How quickly do they decay

The decay rate $\frac{1}{\tau} \sim \epsilon^2$

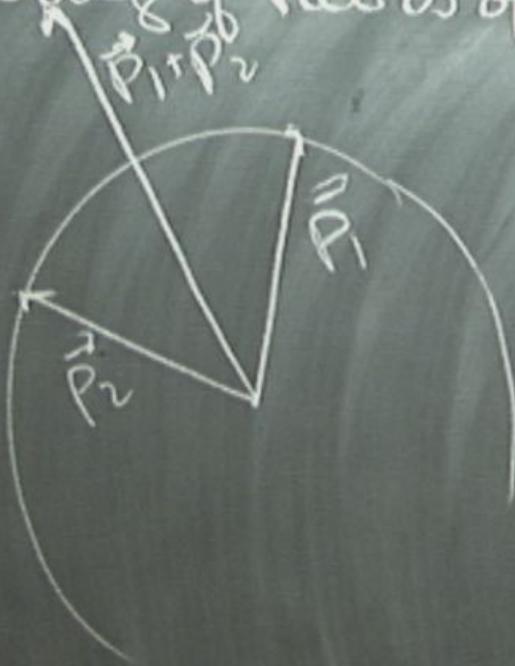


Scattering of Pairs of Quasiparticle

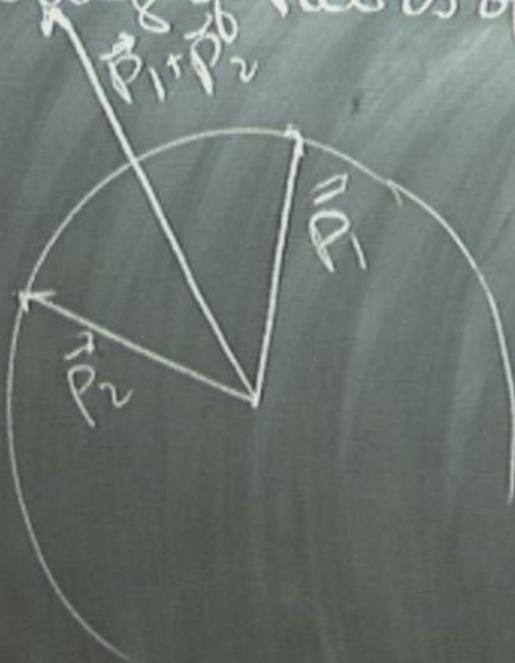
Scattering of Pairs of Quasiparticle



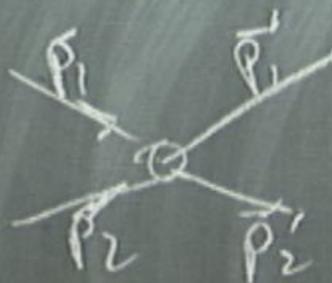
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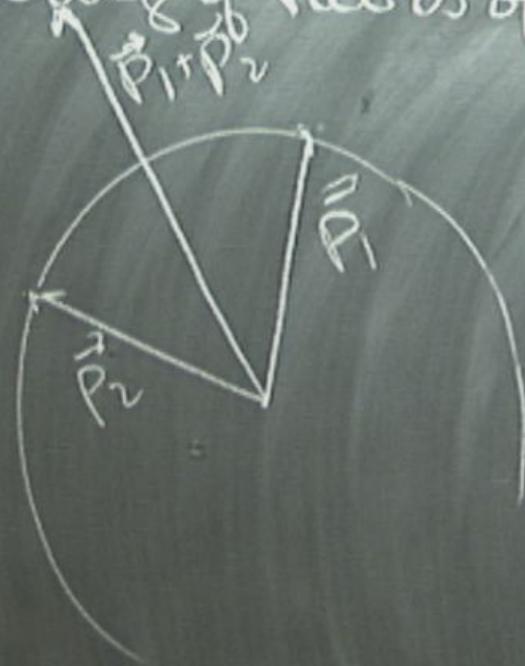
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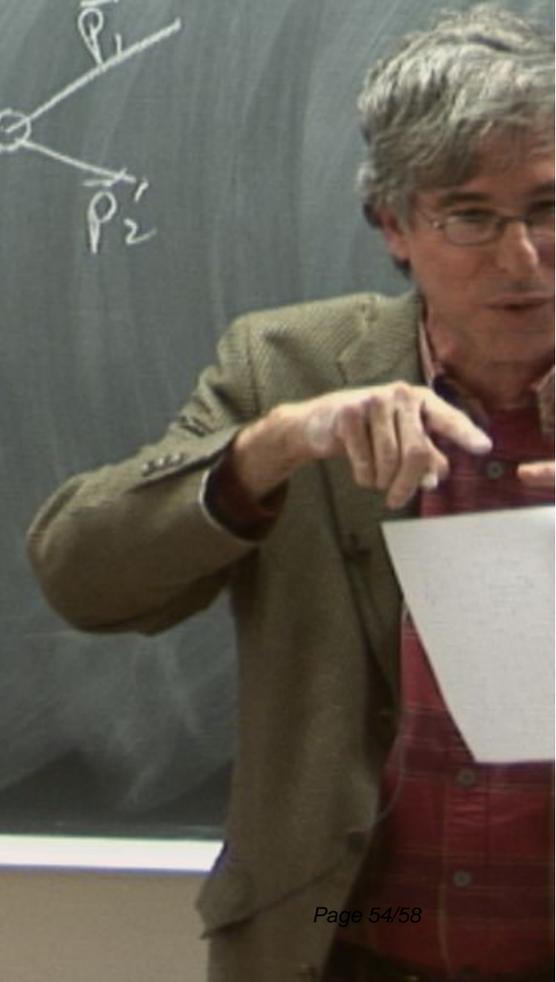
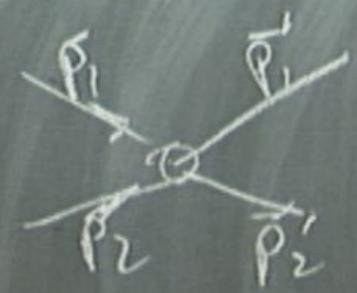
$$\vec{p}_1 + \vec{p}_2 = \vec{p}_1' + \vec{p}_2'$$



Scattering of Pairs of Quasiparticle



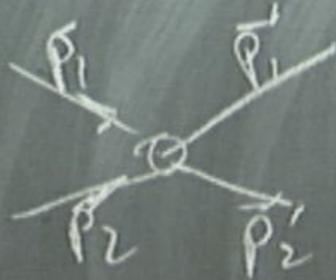
$$\vec{p}_1 + \vec{p}_2 = \vec{p}_1' + \vec{p}_2'$$



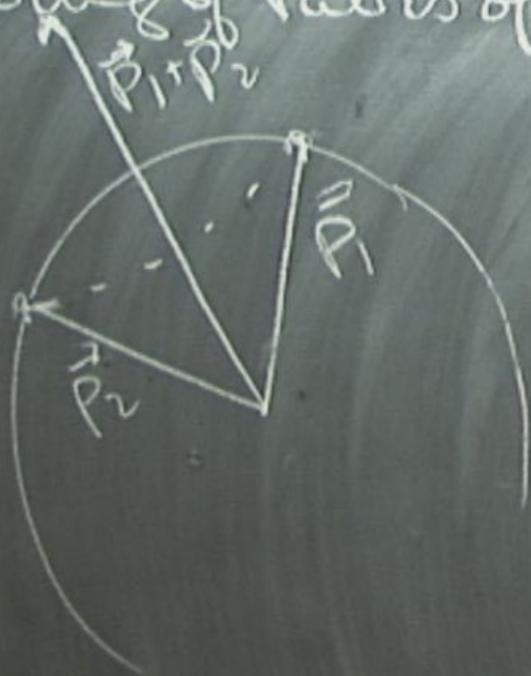
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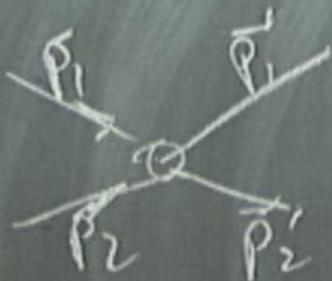
$$\vec{p}_1 + \vec{p}_2 = \vec{p}'_1 + \vec{p}_2$$



Scattering of Pairs of Quasiparticle



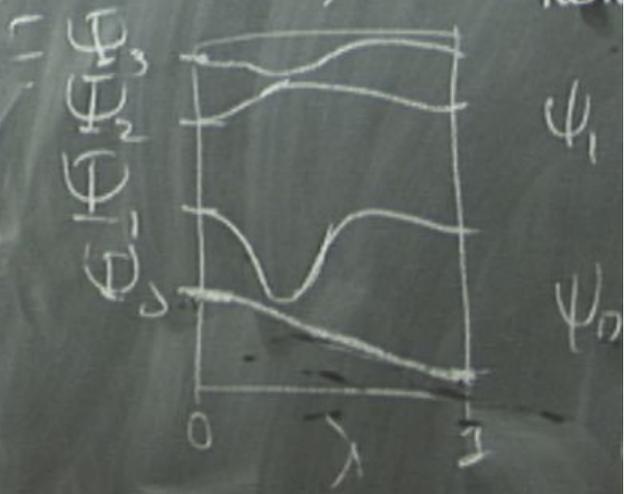
$$\vec{p}_1 + \vec{p}_2 = \vec{p}_1' + \vec{p}_2'$$



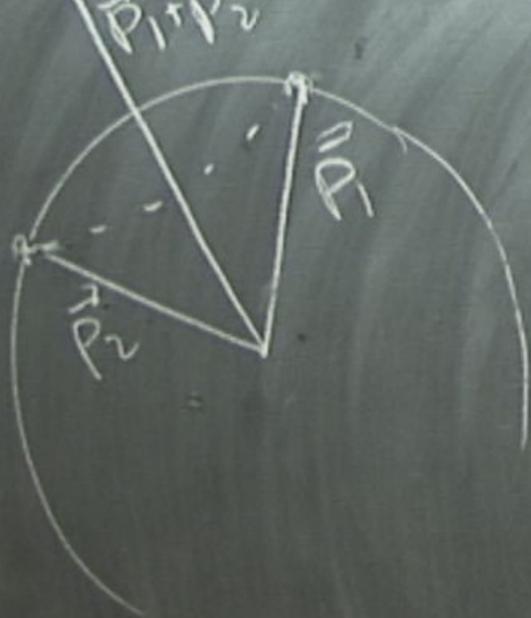
Adiabaticity

- effects of \dot{s} on el-e

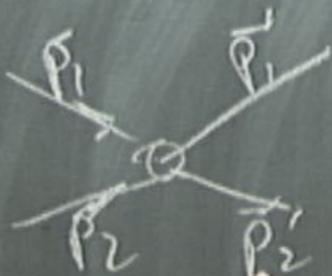
$$\mathcal{H} = \mathcal{H}_{\text{non}}$$



Scattering of Pairs of Quasiparticle



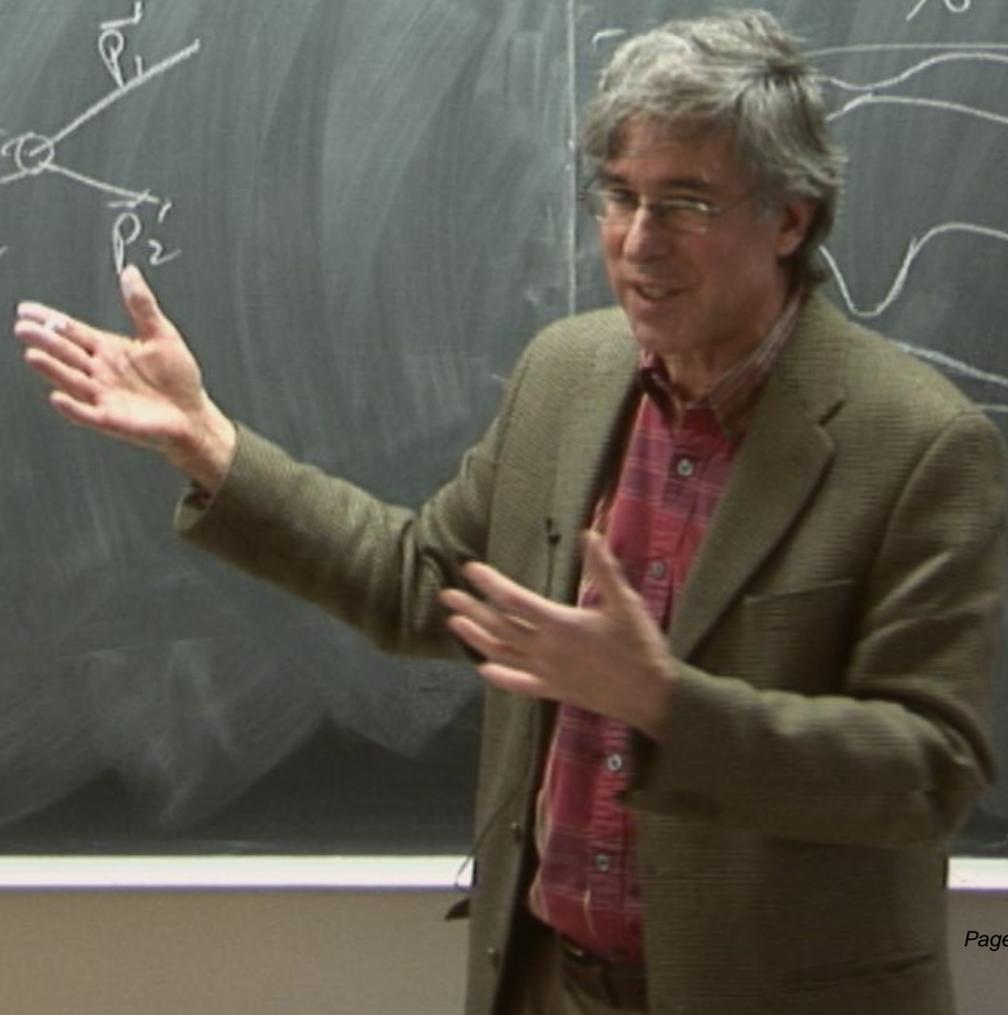
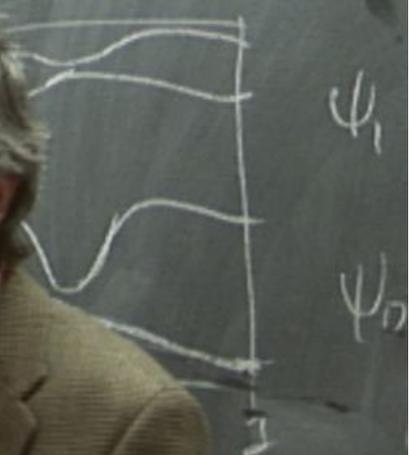
$$\vec{p}_1 + \vec{p}_2 = \vec{p}_1' + \vec{p}_2'$$

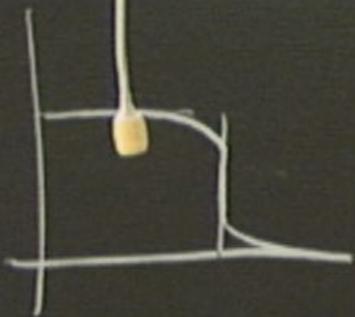


Adiabaticity

- effects of δ on el-e

$$\mathcal{H} = \mathcal{H}_{\text{non}}$$





How stable are these excitations?
 How quickly do they decay?

The decay rate $\frac{1}{\tau} \sim \epsilon^2 + T^2$

