

Title: Standard Model - Lecture 15

Date: Jan 21, 2011 09:00 AM

URL: <http://pirsa.org/11010018>

Abstract:



perimeter scholars
international

q_s q_w q

q_s q_w q

$2 \frac{ij}{s}$

$18 \times 3 \rightarrow$

α_s α_w α

λ_{ij}

$18 \times 3 \rightarrow$ masses,

4 CKM angles.

$\alpha_s \quad \alpha_w \quad \alpha$

α_s

$18 \times 3 \rightarrow \text{mucosa},$
12

$y \quad \bar{y} \quad \bar{y} \quad \bar{y} \quad \bar{y}$

m_h

4 CKM angles.

20

$\alpha_s \quad \alpha_w \quad \alpha$

γ_{ij}^f

$18 \times 3 \rightarrow \text{mesons},$
12

4 CKM angles.

m_h

20^{15}

$\bar{S} \bar{I} \bar{f} \cdot \phi$

$q_s \quad q_w \quad q$

λ_{ij}^{ν}

$18 \times 3 \rightarrow \text{measurements},$
12

4 CKM angles.

m_h

2015

$\bar{\psi} \psi \phi$

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

$q_s \quad q_w \quad q$

λ_{ij}

$18 \times 3 \rightarrow \text{measure, } 12$

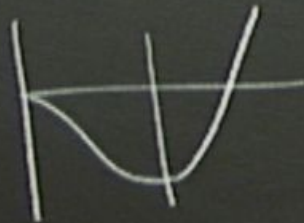
m_h

4 CKM angles.

2015

$\bar{\psi} \psi \phi$

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$v =$

$q_s \quad q_w \quad q$

λ_{ij}

$18 \times 3 \rightarrow \text{measurements},$
12

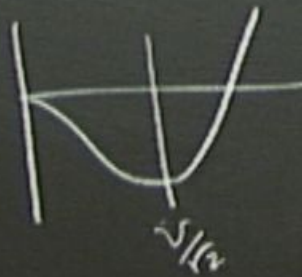
4 CKM angles.

m_h

2015

$\bar{\psi} \psi \phi$

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$v = \left(\frac{\mu^2}{\lambda} \right)^{1/2}$$

m_W

m_h

χ^2

$18 \times 3 \rightarrow \text{measured}$
12

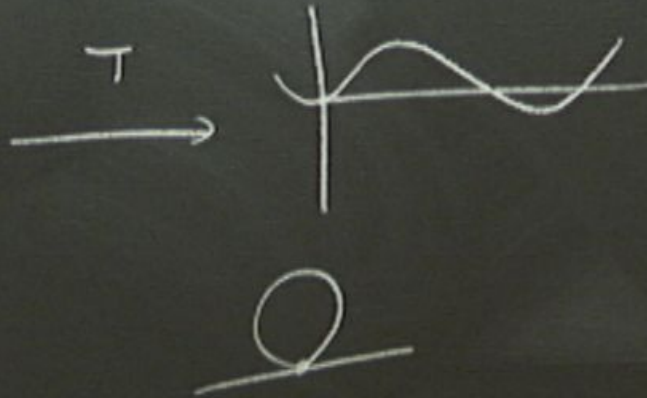
4 CKM angles.

20^{15}

$$- \mu^2 |\phi|^2 + \lambda |\phi|^4$$

$$v = \left(\frac{\mu^2}{\lambda} \right)^{1/2}$$

m_W
 m_H



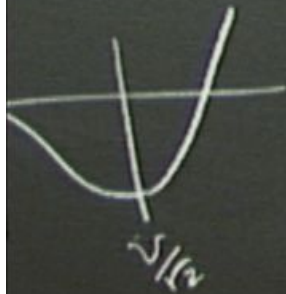
χ^2

$18 \times 3 \rightarrow \text{measured}$
12

4 CKM angles.

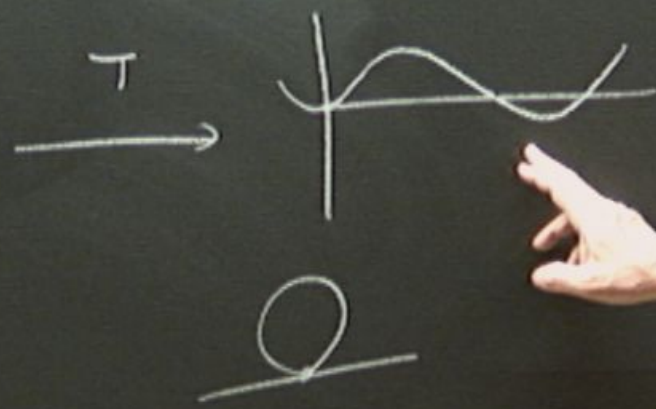
20^{15}

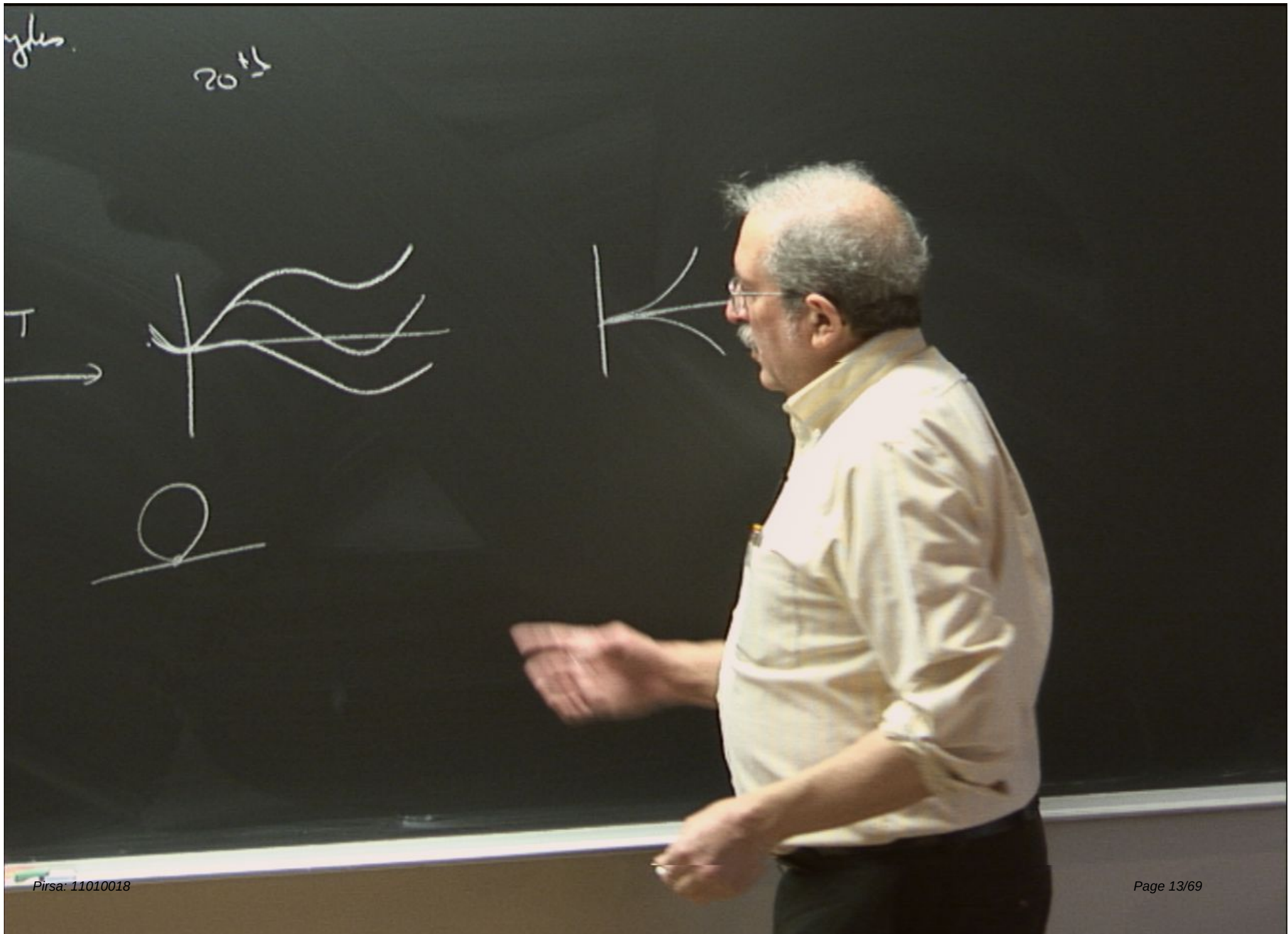
$$- \mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$v = \left(\frac{\mu^2}{\lambda} \right)^{1/2}$$

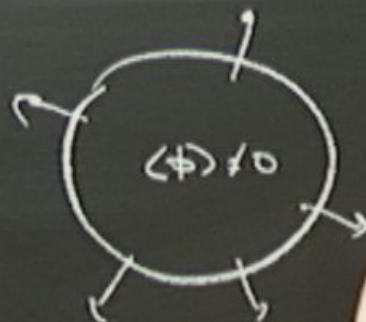
m_W
 m_h





m_h

20 ± 4



m_h

20 ± 4



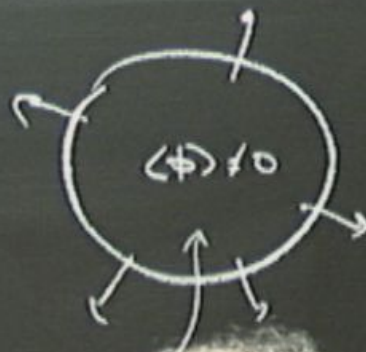
massive W, Z

massless
 W plasma
 $\langle \phi \rangle = 0$



m_h

20 ± 5



massless
W plasma.
 $\langle \phi \rangle = 0$

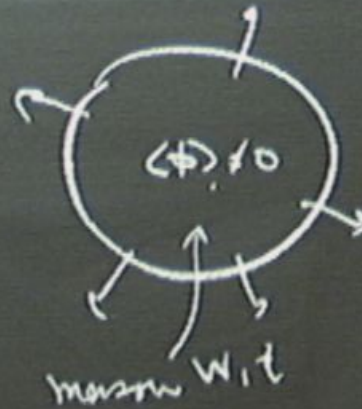
mass



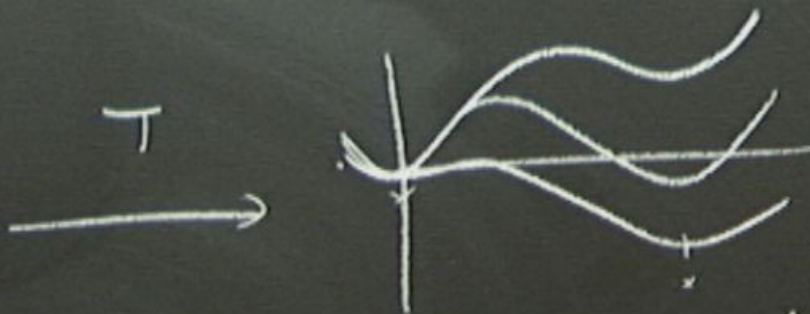
4 CKM angles.

m_h

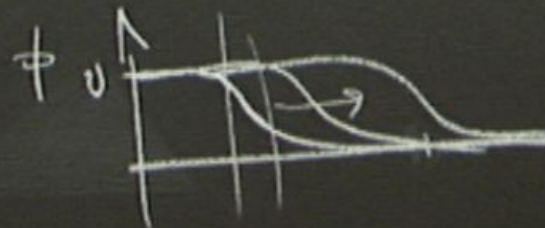
20^{+15}_{-10}



massless
W plasma.
 $\langle \phi \rangle = 0$



$(\sqrt{\phi})^2$



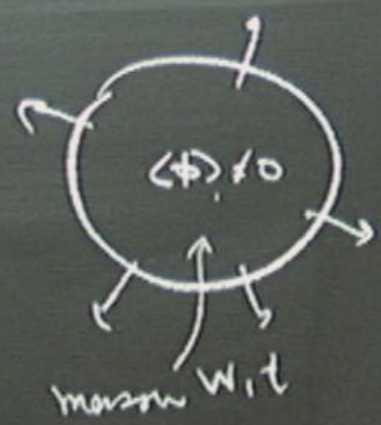
m_h

2013

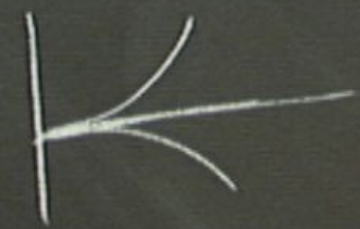
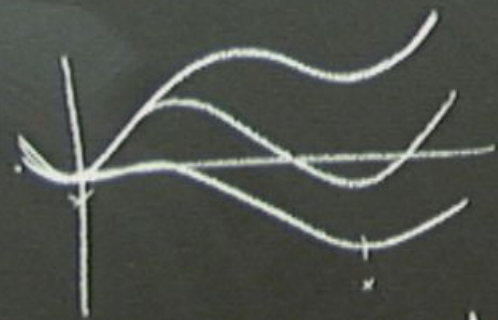
CKM angles.

e^{-1/α_w}

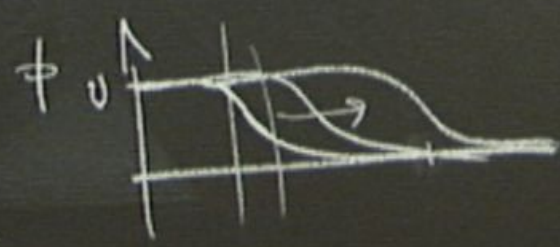
T



massless
W plasma.
 $\langle \phi \rangle = 0$



$(\vec{\nabla} \phi)^2$



$\alpha_s \quad \alpha_w \quad \alpha$

α_s

18×3



museas,

12

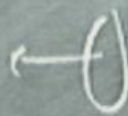
4 CKM axes.

e^{-1/α_w}

T



Pb



Pb.

$\alpha_s \quad \alpha_w \quad \alpha$

α_s

18x3



museas,

12

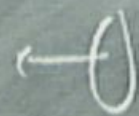
4 CKM axes.

e^{-1/α_w}

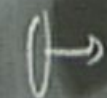
T



Pb



Pb.



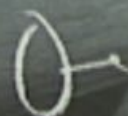
$\alpha_s \quad \alpha_w \quad \alpha$

λ_{ij}

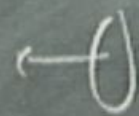
$18 \times 3 \rightarrow \text{masses},$
12

4 CKM angles.

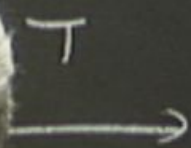
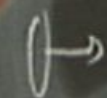
e^{-1/α_w}



P_b



P_b



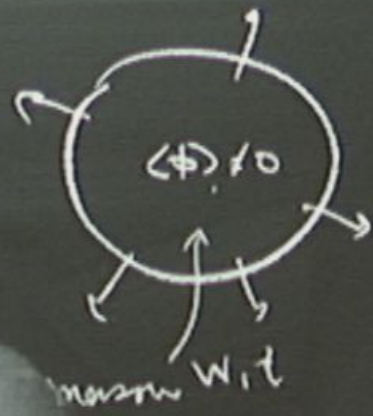
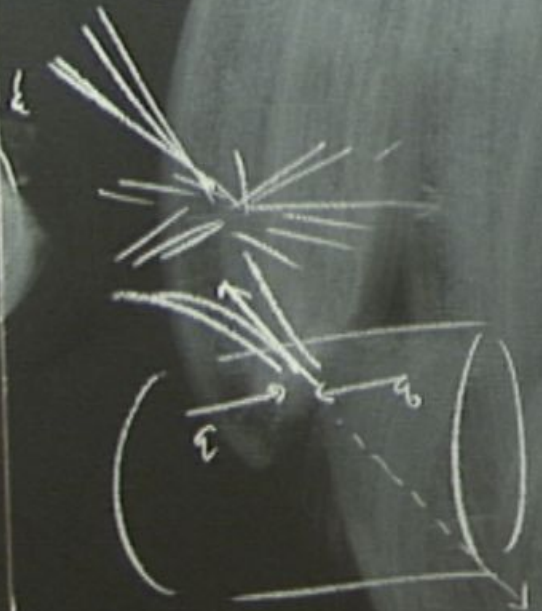
measured,
12

4 CKM angles

m_h

$m_{H^\pm}$

$P_1 \sim 100 \text{ GeV}$



massless
W plasma
 $\langle \phi \rangle = 0$



$$\phi = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$g_s \quad g_w \quad g$$

$$\lambda_{ij}$$

$$18 \times 3$$

$$\rightarrow$$

$$\text{masses,}$$

$$12$$

$$4$$

$$V = -\mu |\phi|^2 + \lambda |\phi|^4$$



$$v = \left| \frac{\mu}{\lambda} \right|^{1/2}$$

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

$$g_s \quad g_w \quad g$$

$$\lambda_{ij}$$

$$18 \times 3 \rightarrow \text{masses}, 12$$

4

$$V = -\mu |\phi|^2 + \lambda |\phi|^4$$



$$v = \sqrt{\frac{\mu^2}{\lambda}}$$

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

$$g_s \quad g_w \quad g$$

$$\lambda_{ij}$$

$$18 \times 3$$



massless,

$$12$$

$$4$$

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$v = \sqrt{\frac{\mu^2}{\lambda}}$$

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

$$g_s \quad g_w \quad g$$

$$\lambda_{ij}$$

$$18 \times 3 \rightarrow \text{masses},$$

4

12

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$m_W = \frac{g v}{2}$$

$$v = \sqrt{\frac{\mu^2}{\lambda}}$$

250 GeV

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

$$g_s \quad g_w \quad g$$

$$\lambda_{ij}^{\nu}$$

$$18 \times 3 \rightarrow \text{masses}, 12$$

4

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$m_W = \frac{g v}{2}$$

$$v = \sqrt{\frac{\mu^2}{\lambda}}$$

250 GeV

$$\phi \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

$$g_s \quad g_w \quad g$$

$$\lambda_{ij}$$

$$18 \times 3 \rightarrow \text{masses,}$$

4

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

$$= \mu^2 h^2 +$$



$$m_W = \frac{gv}{2}$$

$$v = \sqrt{\frac{\mu^2}{\lambda}}$$

$$250 \text{ GeV}$$

$$\phi \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

λ_{ij}

$18 \times 3 \rightarrow$ masses,

12

$$\mu^2 h^2 +$$

$$\frac{\mu^2}{\lambda}$$

$v =$
 $\uparrow$
 250 GeV

$$m_h^2 =$$

$$2\mu^2$$

$$\frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h/\lambda \end{pmatrix}$$

m_h

4 CKM angles

h

18x3 → measure,

12

$$\lambda |\phi|^4$$

$$= \mu^2 h^2 +$$

$$v - \left| \frac{\mu^2}{\lambda} \right|^{1/2}$$

$$250 \text{ GeV}$$

$$\rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

$$m_h^2 =$$

$$2\mu^2$$

$$\lambda =$$

$$\frac{\lambda}{4\pi} =$$

$$\frac{1}{2} \frac{m_h^2}{v^2}$$

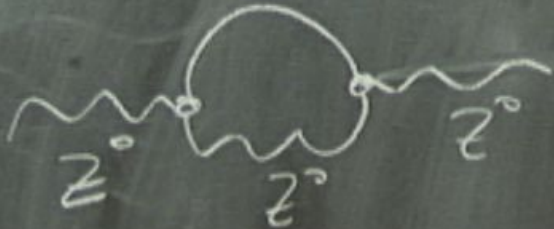
$$\frac{m^2}{8\pi v^2}$$

4 CKM angles.

15

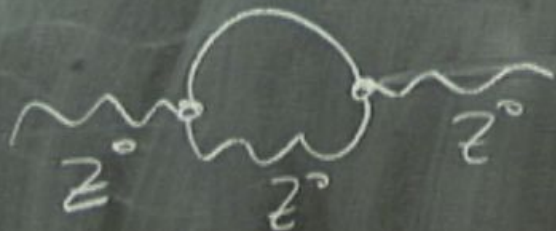
$$114 \text{ GeV} < m_h <$$

$$114 \text{ GeV} < m_h <$$



$$\frac{g^2 + g'^2}{2} v^2 Z^0$$

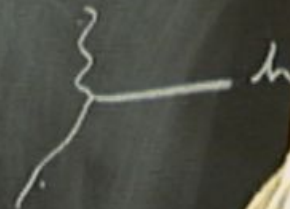
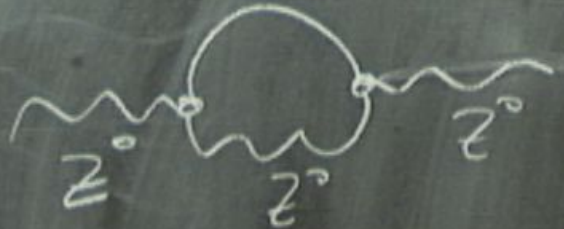
$$114 \text{ GeV} < m_h <$$



$$\frac{g^2 + g'^2}{2} \frac{v^2}{4} \frac{Z^0}{(v+h)^2}$$

$$114 \text{ GeV} < m_h <$$

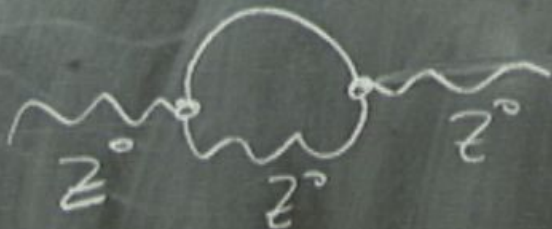
$$\frac{\alpha_W}{4\pi}$$



$$\frac{3+S'}{2} \frac{v^2}{4} Z^0 (v+h)^2$$

$$114 \text{ GeV} < m_h < 180 \text{ GeV}$$

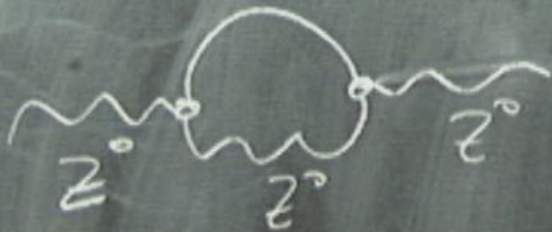
$$\frac{\alpha_W}{4\pi} \lesssim \frac{m_h^2}{m_Z^2}$$



$$\frac{3+S'}{2} \frac{v^2}{4} \frac{Z^0}{(v+h)^2}$$

$$114 \text{ GeV} < m_h < 180 \text{ GeV}$$

$$\frac{\alpha_W}{4\pi} \lesssim \frac{m_h^2}{m_Z^2}$$



$$\frac{g^2 + g'^2}{2} \frac{v^2}{4} \frac{Z^0}{(v+h)^2}$$

$$v \rightarrow v + h(x)$$

$$s \mid \vdash h = -i \frac{m_f}{v}$$

$$v \rightarrow v + h(x)$$

A Feynman diagram showing a fermion line (solid line) with a scalar loop (dashed line labeled h) and a fermion loop (solid line labeled f). The diagram is connected to a vertex on the left.

$$-i \frac{m_f}{v} \frac{1}{\epsilon}$$

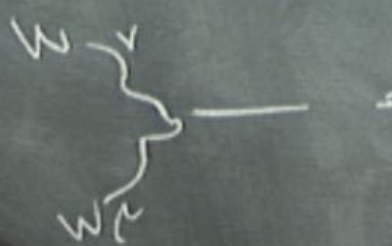
A Feynman diagram showing a fermion line (solid line) with a W boson loop (wavy line labeled W) and a W boson loop (wavy line labeled W). The diagram is connected to a vertex on the left.

$$i 2 \frac{m_W^2}{v} g^{\mu\nu}$$

$$v \rightarrow v + h(x)$$



$$= -i \frac{m_f}{v} \frac{1}{\cancel{}}$$



$$= i 2 \frac{m_W^2}{v} g^{\mu\nu}$$

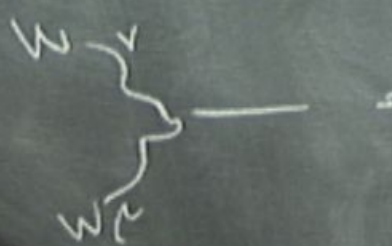


$$= -3i \frac{m_h^2}{v}$$

$$v \rightarrow v + h(x)$$



$$= -i \frac{m_f}{v} \frac{1}{\epsilon}$$



$$= i 2 \frac{m_W^2}{v} g^{ff}$$

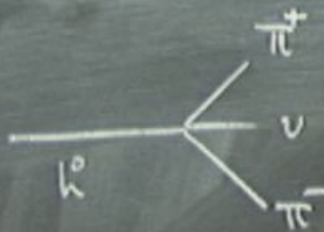


$$= -3i \frac{m_h^2}{v}$$

$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W}{16} m_h \left(\frac{m_h}{m_W} \right)^2$$

$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W m_h}{16} \left(\frac{m_h}{m_W} \right)^2 \left(1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^4}{m_h^4} \right) \left(1 - \frac{4m_W^2}{m_h^2} \right)^{\frac{1}{2}}$$

$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W m_h}{16} \left(\frac{m_h}{m_W} \right)^2 \left(1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^4}{m_h^4} \right) \left(1 - \frac{4m_W^2}{m_h^2} \right)^{\frac{1}{2}}$$



$$\alpha_W \left(\frac{m_L}{m_W} \right)^2 \sim \frac{2}{c_W^2}$$

$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W}{16} m_h \left(\frac{m_h}{m_W} \right)^2 \left(1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^4}{m_h^4} \right) \left(1 - \frac{4m_W^2}{m_h^2} \right)^{\frac{1}{2}}$$

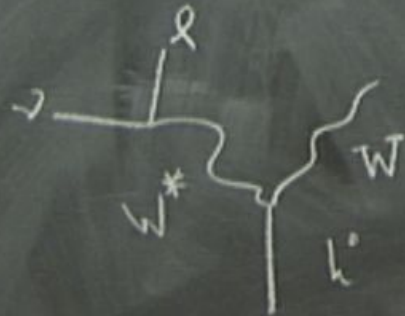
$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f \bar{f}) = \frac{\alpha_W}{8} m_h \left(\frac{m_f}{m_h} \right)^2 \left(1 - \frac{4m_f^2}{m_h^2} \right)^{\frac{3}{2}} \cdot N_c$$

10^{-3}

$$I(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W}{16} m_h \left(\frac{m_h}{m_W} \right)^2 \left(1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^4}{m_h^4} \right) \left(1 - \frac{4m_W^2}{m_h^2} \right)^{\frac{1}{2}}$$

$$I(h^0 \rightarrow f \bar{f}) = \frac{\alpha_W}{8} m_h \left(\frac{m_f}{m_h} \right)^2 \left(1 - \frac{4m_f^2}{m_h^2} \right)^{\frac{3}{2}} N_c$$



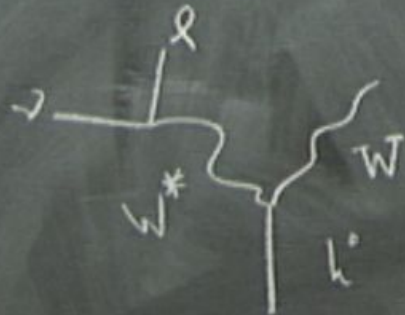
10^{-3}

$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W}{16} m_h \left(\frac{m_h}{m_W} \right)^2 \left(1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^4}{m_h^4} \right) \left(1 - \frac{4m_W^2}{m_h^2} \right)^{\frac{1}{2}}$$

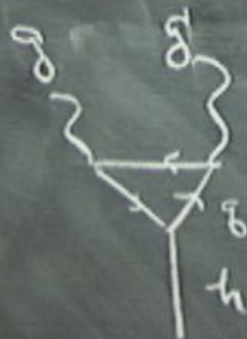
$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f \bar{f}) = \frac{\alpha_W}{8} m_h \left(\frac{m_f}{m_h} \right)^2 \left(1 - \frac{4m_f^2}{m_h^2} \right)^{\frac{3}{2}} N_c$$

10^{-3}

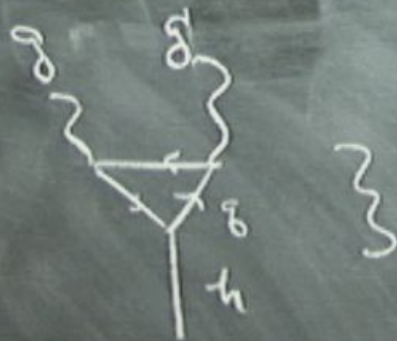


$$v \rightarrow v + h(x)$$

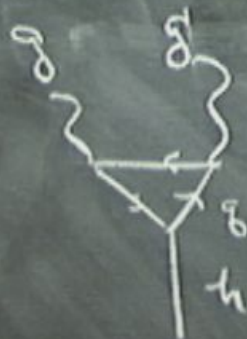


$$\int \frac{d^4 k}{(2\pi)} \frac{1}{[k^2]}$$

$$v \rightarrow v + h(x)$$



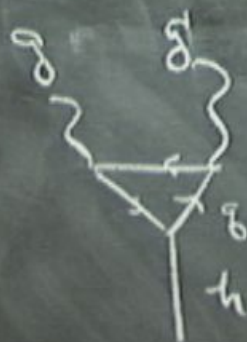
$$v \rightarrow v + h(x)$$



$$\left. \right\} \frac{1}{v} h(F_{\mu\nu} F^{\mu\nu})$$

m_f

$$v \rightarrow v + h(x)$$



$$\sim \frac{1}{v} h(F_{\mu\nu} F^{\mu\nu})$$

$$m_f \quad (\overline{m_f} \text{ a } m_h)$$

$$v \rightarrow v + h(x)$$



$$\left. \vphantom{\frac{1}{v}} \right\} \frac{1}{v} h(F_{\mu\nu} F^{\mu\nu})$$

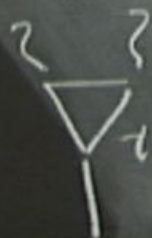
$$\frac{m_f}{v} \left(\overline{m_f} \text{ a } m_h \right)$$

$$\nu \rightarrow \nu + h(x)$$



$$\sim \frac{1}{\nu} h(F_{\mu\nu} F^{\mu\nu})$$

$$\frac{m_f}{\nu} (m_f^2 \text{ a } m_h)$$



$$I = \frac{\alpha_w \alpha_s^2}{288\pi^2} \frac{m_h^3}{m_w^2}$$

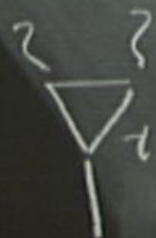
$$\nu \rightarrow \nu + h(x)$$



$$\sim \frac{1}{v} \text{tr}(F_{\mu\nu} F^{\mu\nu})$$



$$\frac{m_f}{v} \left(\frac{1}{m_f} + m_h \right)$$



$$\Gamma = \frac{\alpha_w \alpha_s^2}{288\pi^2} \frac{m_h^3}{m_t^2}$$

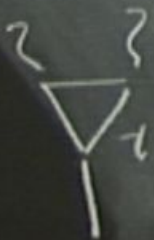
$$\nu \rightarrow \nu + h(x)$$



$$\sim \frac{1}{v} h(F_{\mu\nu} F^{\mu\nu})$$



$$\frac{m_f}{v} \frac{1}{(m_f^2 + m_h^2)}$$



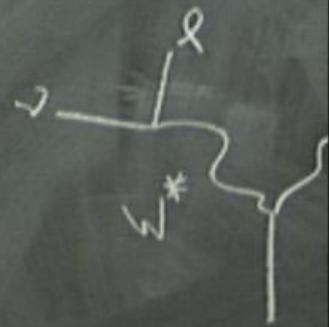
$$\Gamma = \frac{\alpha_W \alpha_S^2}{288\pi^2} \frac{m_h^3}{m_W^2}$$

$$BR \sim 2 \times 10^{-3}$$

$$\Gamma(h^0 \rightarrow W^+ W^-) =$$

$$m_h <$$

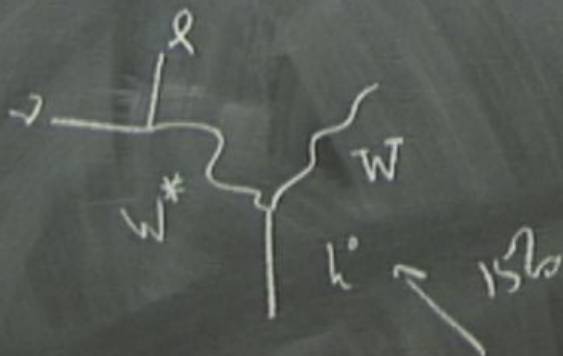
$$\Gamma(h^0 \rightarrow f \bar{f}) =$$



$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_w}{16} m_h \left(\frac{m_h}{m_W} \right)^2 \left(1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^4}{m_h^4} \right) \left(1 - \frac{4m_W^2}{m_h^2} \right)^{\frac{1}{2}}$$

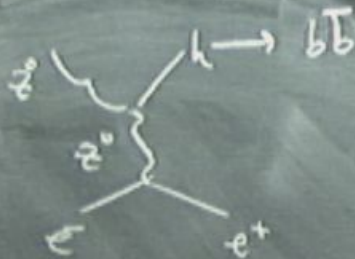
$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f \bar{f}) = \frac{\alpha_w}{8} m_h \left(\frac{m_f}{m_h} \right)^2 \left(1 - \frac{4m_f^2}{m_h^2} \right)^{\frac{3}{2}} N_c$$



10^{-3} $m_h = 120 \text{ GeV}$
 down

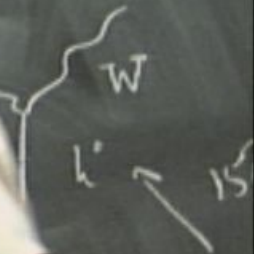
LEP



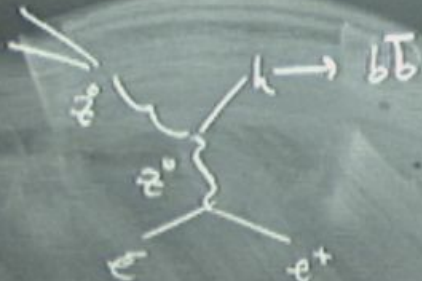
$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W m_h^2}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f \bar{f}) = \frac{\alpha_W}{8}$$



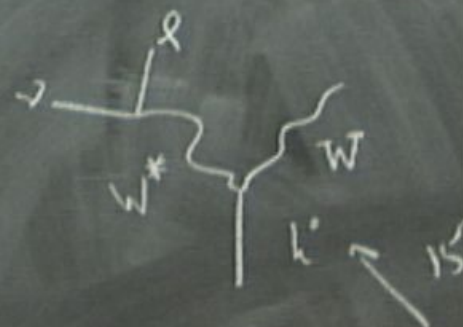
LEP



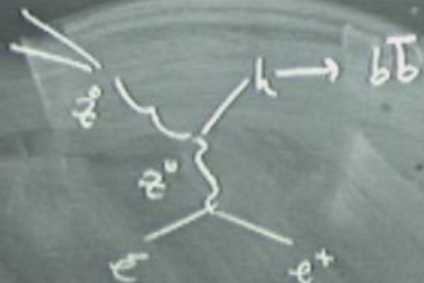
$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W m_h^2}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f \bar{f}) = \frac{\alpha_W}{8}$$



LEP



$$e^+e^- \rightarrow \gamma^* \gamma^* \rightarrow b\bar{b}$$

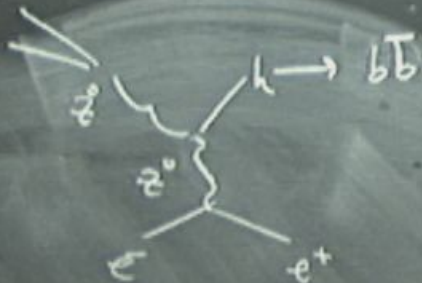
$$\Gamma(h^0 \rightarrow W^+W^-) = \frac{\alpha_W m_h^2}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f\bar{f}) = \frac{\alpha_W}{8}$$



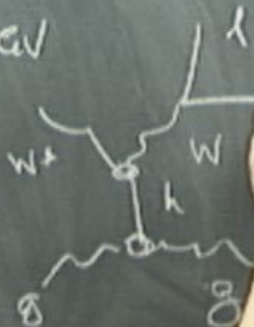
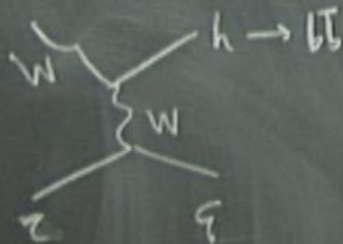
LEP



$$e^+e^- \rightarrow \gamma^* \gamma^* \rightarrow b\bar{b}$$

$$m_h > 114 \text{ GeV}$$

Tevatron

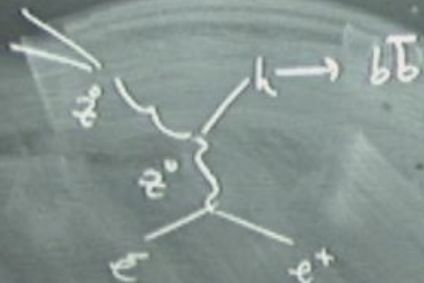


$$\Gamma(h^0 \rightarrow W^+W^-) = \frac{\alpha_W m}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow \gamma\gamma) = \frac{\alpha_W}{8}$$

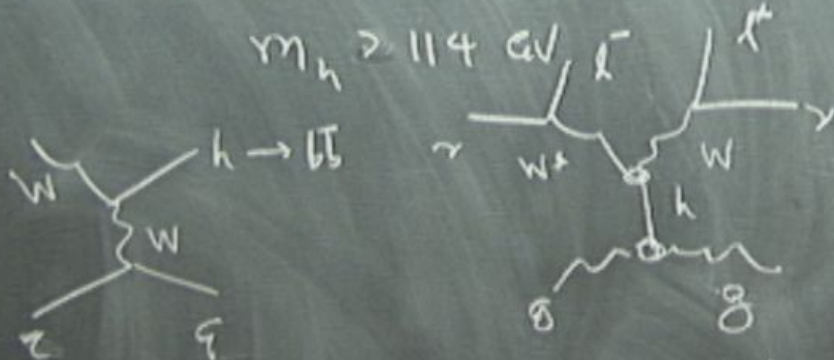
LEP



$$e^+e^- \rightarrow \gamma^* \gamma^* \rightarrow b\bar{b}$$

$$m_h > 114 \text{ GeV}$$

Tevatron

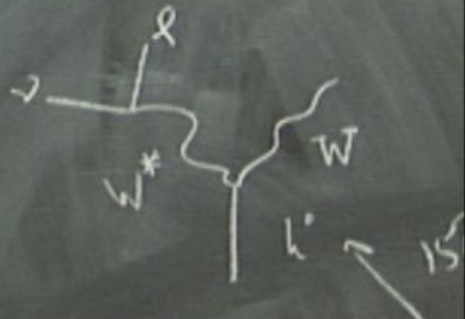


excluded around 160 GeV

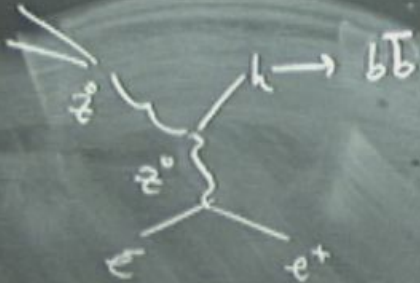
$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W m_h}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f\bar{f}) = \frac{\alpha_W}{8}$$



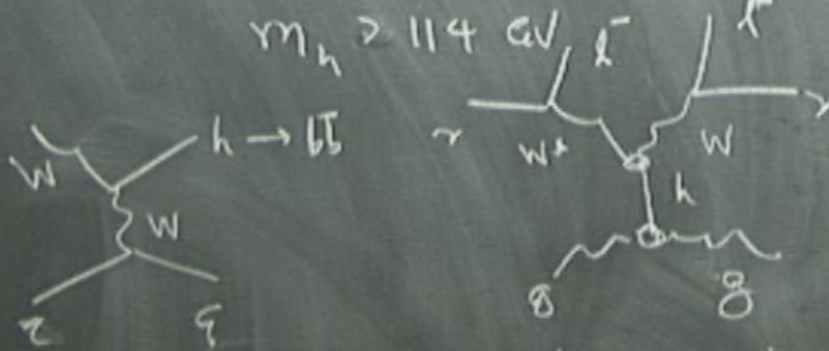
LEP



$$e^+e^- \rightarrow Z^0 Z^0 \rightarrow b\bar{b}$$

$$m_h > 114 \text{ GeV}$$

Tevatron



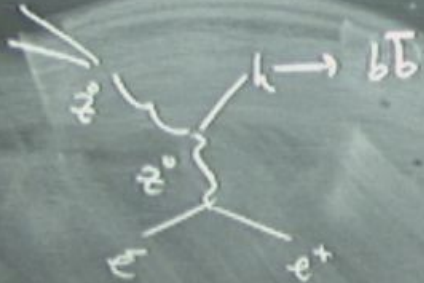
excluded
and
160 GeV

$$\Gamma(h^0 \rightarrow W^+W^-) = \frac{\alpha_W m_h}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f\bar{f}) = \frac{\alpha_W}{8}$$

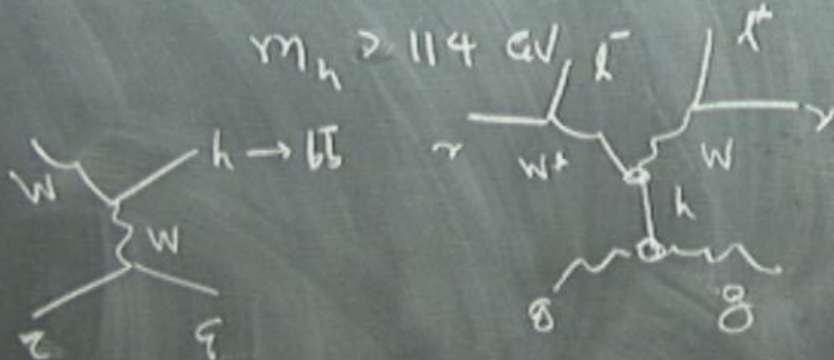
LEP



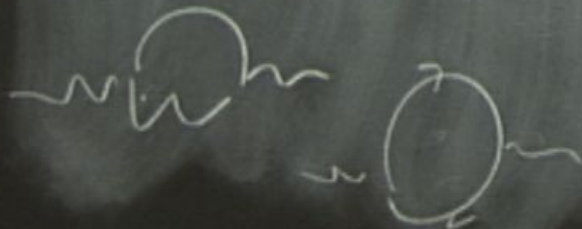
$$e^+e^- \rightarrow Z^0 Z^0 \rightarrow b\bar{b}$$

$$m_h > 114 \text{ GeV}$$

Tevatron



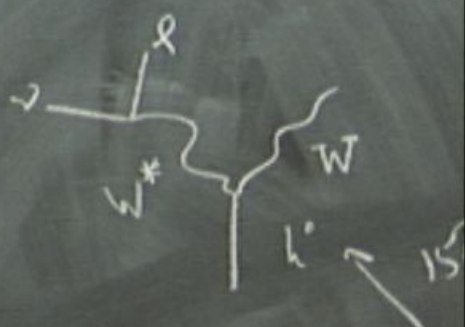
excluded and
160 GeV



$$\Gamma(h^0 \rightarrow W^+ W^-) = \frac{\alpha_W m}{16}$$

$$m_h < 2m_W$$

$$\Gamma(h^0 \rightarrow f\bar{f}) = \frac{\alpha_W}{8}$$



$$h \rightarrow W^+ W^- \rightarrow \bar{\tau} \tau^0 \rightarrow \ell^+ \ell^- \ell^+ \ell^-$$

$$h \rightarrow W^+ W^-$$

$$\rightarrow \tau^+ \tau^- \rightarrow$$

$$l^+ l^- l^+ l^-$$

$$h^0 \rightarrow b \bar{b}$$

discoupling



$$h \rightarrow W^+ W^- \rightarrow \tau^+ \tau^- \rightarrow \ell^+ \ell^- \ell^+ \ell^-$$

$$h^0 \rightarrow b \bar{b}$$

discovery

$$W, Z + h \rightarrow b \bar{b}$$

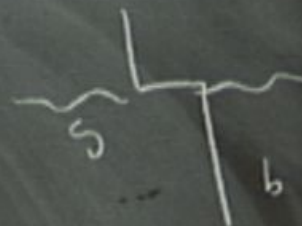
light boosted



$$h \rightarrow W^+ W^- \rightarrow \tau^+ \tau^- \rightarrow \ell^+ \ell^- \ell^+ \ell^-$$

$$h^0 \rightarrow b \bar{b}$$

discouraging

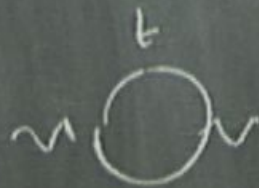
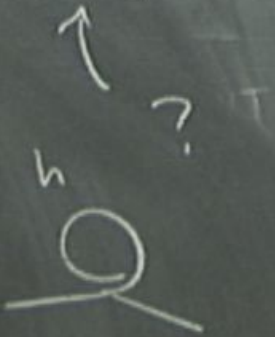


$$q \bar{q} \rightarrow W, Z + h \rightarrow b \bar{b}$$

light boosted

$$g S \rightarrow h \rightarrow \gamma \gamma$$

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



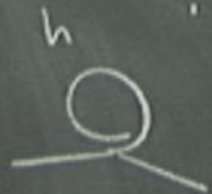
$$h \rightarrow W^+ W^- \rightarrow \tau^+ \tau^-$$

$$h \rightarrow b \bar{b}$$

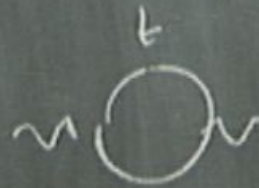
$$g_S \rightarrow$$

$$V = -\mu^2 |\phi|^2 + 2 |\phi|^4$$

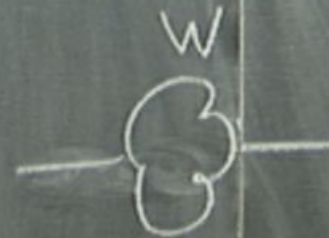
↑
?



$$+ \frac{\lambda}{(4\pi)^2} \Lambda^2$$



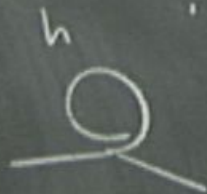
$$- \frac{\lambda_t}{(4\pi)^2} \Lambda^2$$



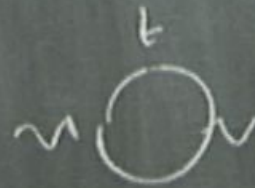
$$+ \frac{\alpha_W}{4\pi} \Lambda^2$$



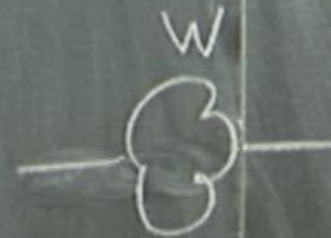
$$V = \underbrace{-\mu^2 |\phi|^2}_{\text{?}} + 2 |\phi|^4$$



$$+ \frac{\lambda}{(4\pi)^2} \Lambda^2$$



$$- \frac{\lambda_t}{(4\pi)^2} \Lambda^2$$



$$+ \frac{\alpha_W}{4\pi} \Lambda^2$$

$$\odot \Rightarrow \mu_{\text{ren}}^2 = \mu_b^2 + () \Lambda^2$$