

Title: Physics as Information: Quantum Theory meets Relativity

Date: Nov 30, 2010 04:00 PM

URL: <http://pirsa.org/10110080>

Abstract: I will review some recent advances on the line of deriving quantum field theory from pure quantum information processing. The general idea is that there is only Quantum Theory (without quantization rules), and the whole Physics---including space-time and relativity---is emergent from the processing. And, since Quantum Theory itself is made with purely informational principles, the whole Physics must be reformulated in information-theoretical terms. Here's the TOC of the talk: a) Very short review of the informational axiomatization of Quantum Theory; b) How space-time and relativistic covariance emerge from the quantum computation; c) Special relativity without space: other ideas; d) Dirac equation derived as information flow (without the need of Lorentz covariance); e) Information-theoretical meaning of inertial mass and Planck constant; f) Observable consequences (at the Planck scale?); h) What about Gravity? Three alternatives as a start for a brainstorming.



**QUit**  
quantum information  
theory group

---

# PHYSICS AS INFORMATION: QUANTUM THEORY MEETS RELATIVITY

---

**Giacomo Mauro D'Ariano**

*Dipartimento di Fisica "A. Volta", Università di Pavia*

November 30th 2010, Perimeter Institute, Waterloo, Ontario, CA

EXPLORING THE POSSIBILITY THAT  
PURE INFORMATION MAY UNDERLIE  
ALL OF PHYSICS



EXPLORING THE POSSIBILITY THAT  
PURE INFORMATION MAY UNDERLIE  
ALL OF PHYSICS

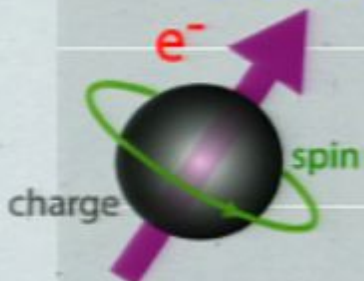
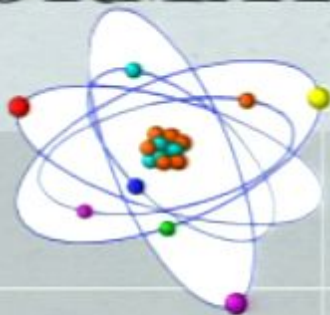
Such information should be made of *qubits!*



# OPERATIONALISM = INFORMATIONALISM

**PHYSICS**

**INFORMATION**



system

register

state

initialization

effect

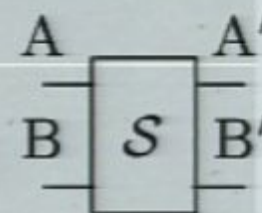
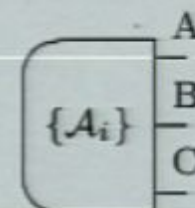
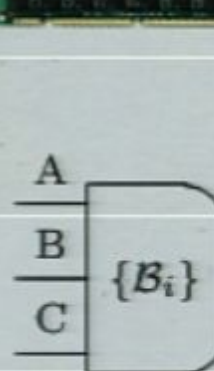
readout

transformation

processing

event

subroutine



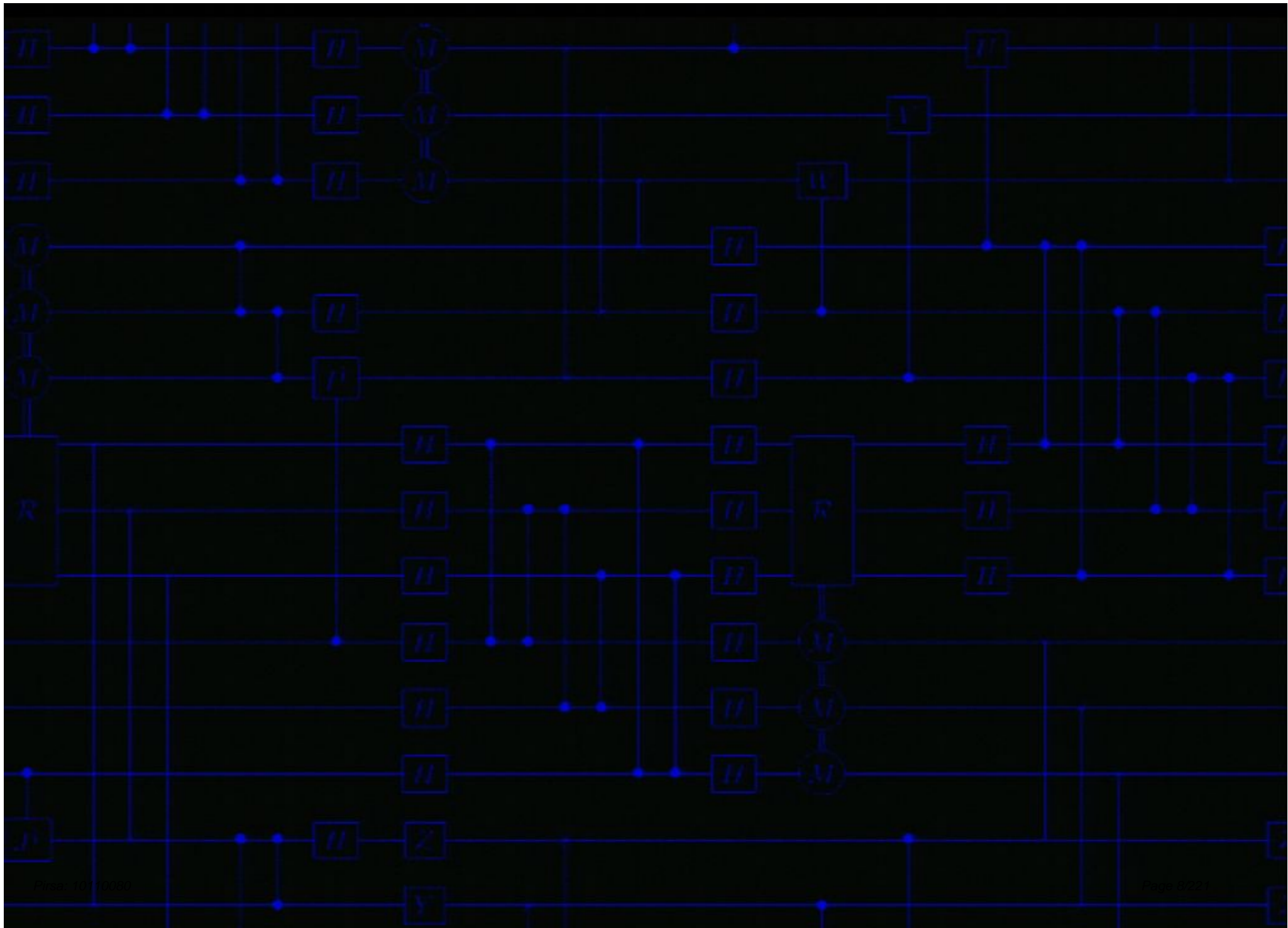
EXPLORING THE POSSIBILITY THAT  
PURE INFORMATION MAY UNDERLIE  
ALL OF PHYSICS

Such information should be made of *qubits!*

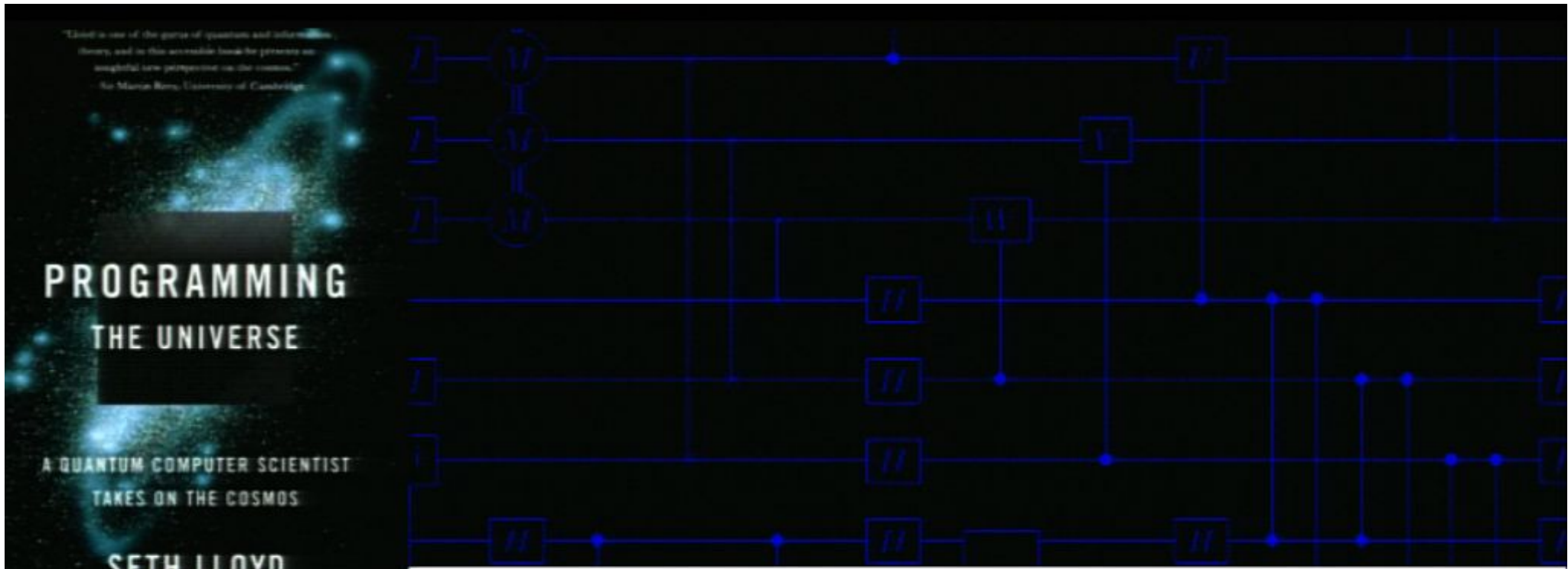


# EXPLORING THE POSSIBILITY THAT PURE INFORMATION MAY UNDERLIE ALL OF PHYSICS

Can we say that a quantum field is just a collection of (infinitely many) quantum systems (each at every “space point = Planck cell) unitarily interacting with a bunch of other systems?








THE UNIVERSE IS A HUGE COMPUTER



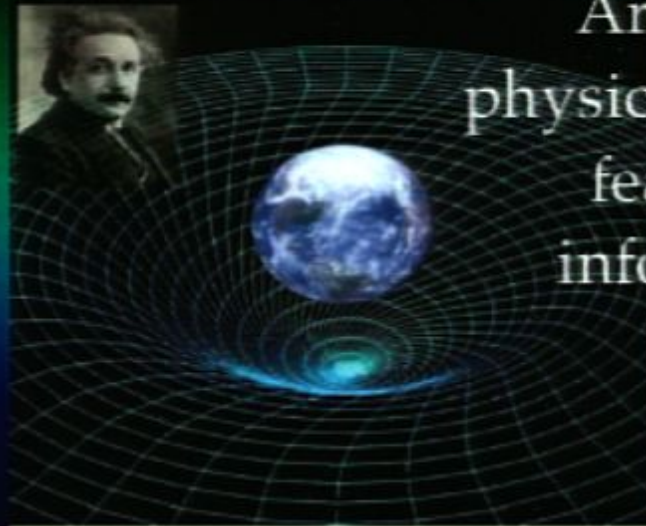
Does the continuum play a fundamental role, or it is only a mathematical idealization?



EXPLORING THE POSSIBILITY THAT  
PURE INFORMATION MAY UNDERLIE  
ALL OF PHYSICS

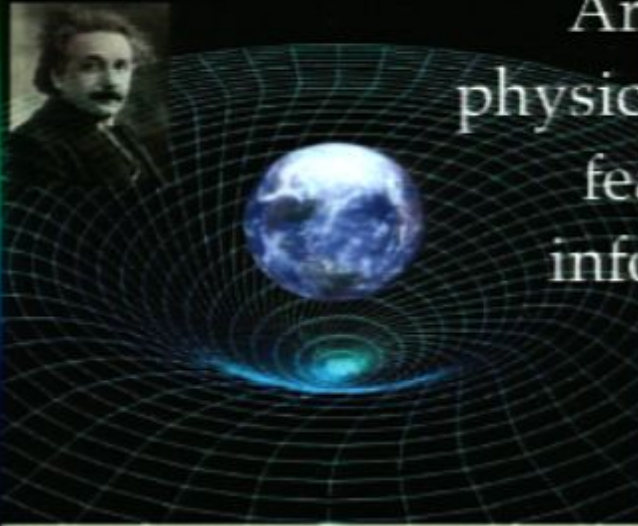
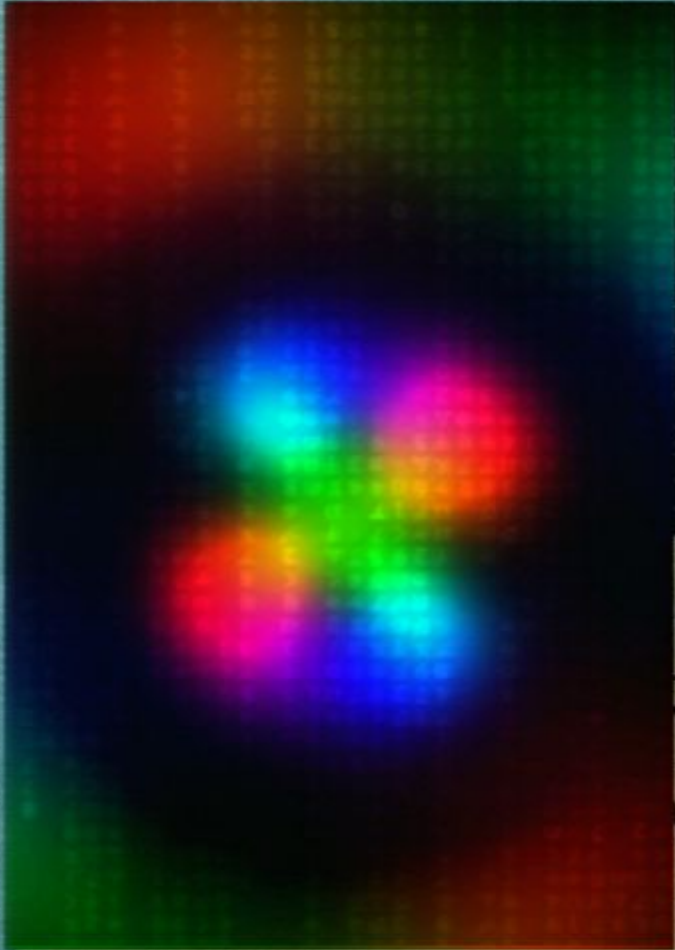


Are space, time, and all  
physical observables emergent  
features of a quantum  
information processing?



CONSIDERING THE POSSIBILITY THAT  
INFORMATION MAY UNDERLIE  
ALL OF PHYSICS





Are space, time, and all  
physical observables emergent  
features of a quantum  
information processing?

CONSIDERING THE POSSIBILITY THAT  
INFORMATION MAY UNDERLIE  
ALL OF PHYSICS



# Physics is Information

“It from  
Bit”



*“Information  
is physical”*

(Bit from It)



# Physics is Information

“It from  
QBit”

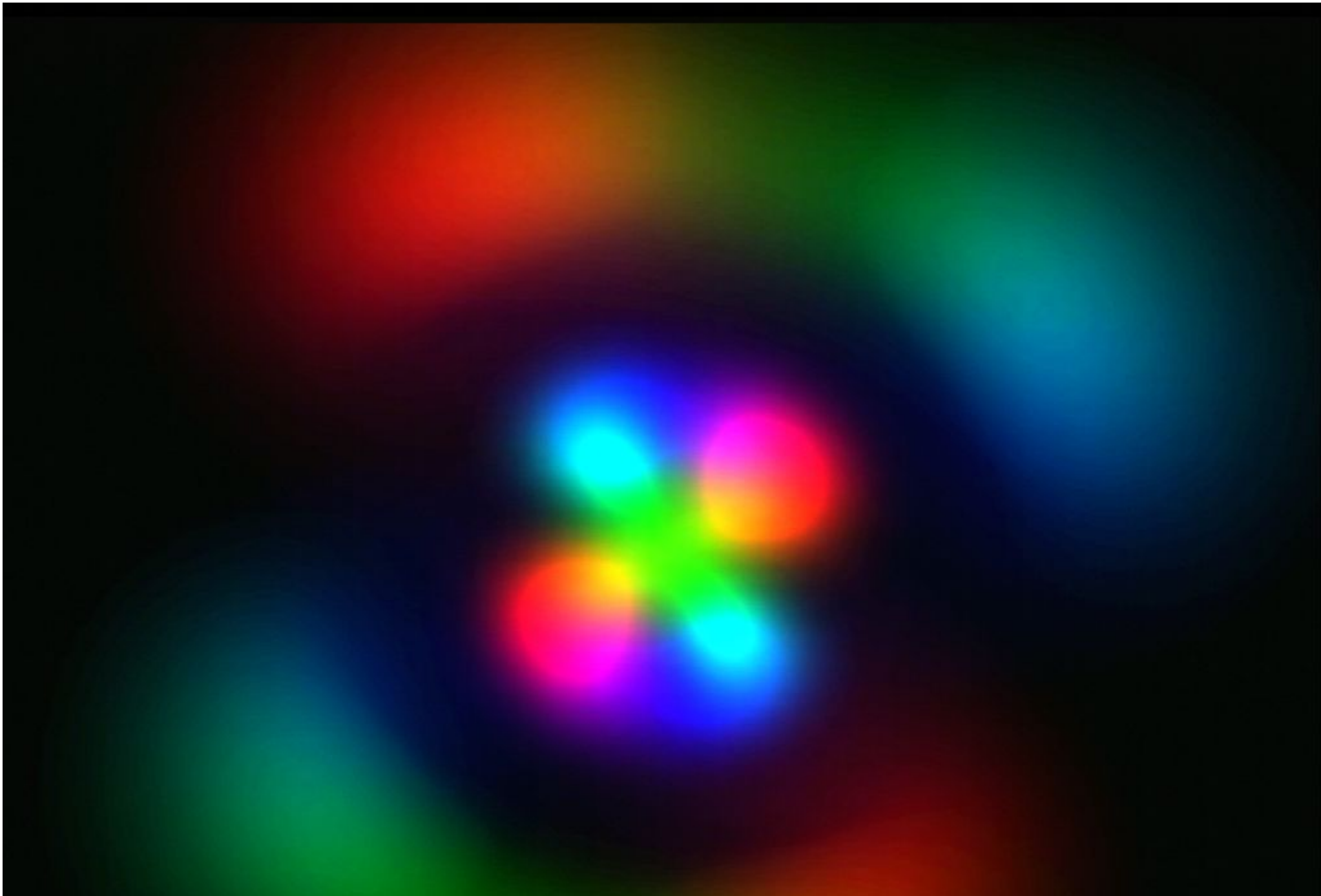


*“Information  
is physical”*

(QBit from It)











The informational paradigm: a huge change in ontology

The informational paradigm: a huge change in ontology

A very prominent hypothesis



# OUTLINE

- \* Very short review of the informational axiomatization of QT
- \* How space-time and relativistic covariance emerge from the quantum computation
- \* Special relativity without space and time: other ideas
- \* Dirac equation derived as information flow (without the need of Lorentz covariance)
- \* Information-theoretical meaning of inertial mass and Planck constant
- \* Observable consequences (at the Planck scale?)
- \* What about Gravity? Three alternatives as a start for a brainstorming

---

# HOW RELATIVITY EMERGES FROM THE COMPUTATION?

---

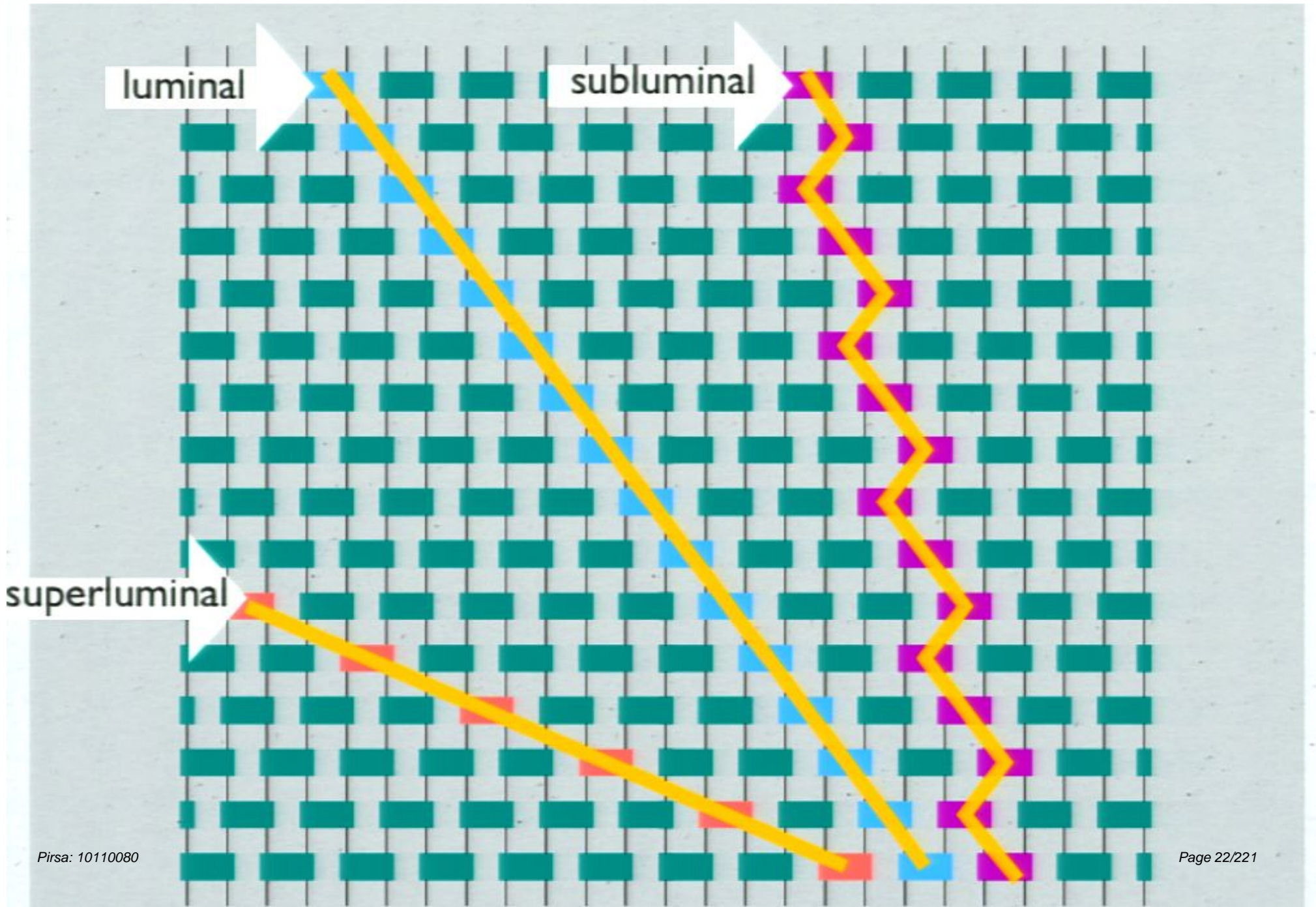


---

# HOW RELATIVITY EMERGES FROM THE COMPUTATION?

---

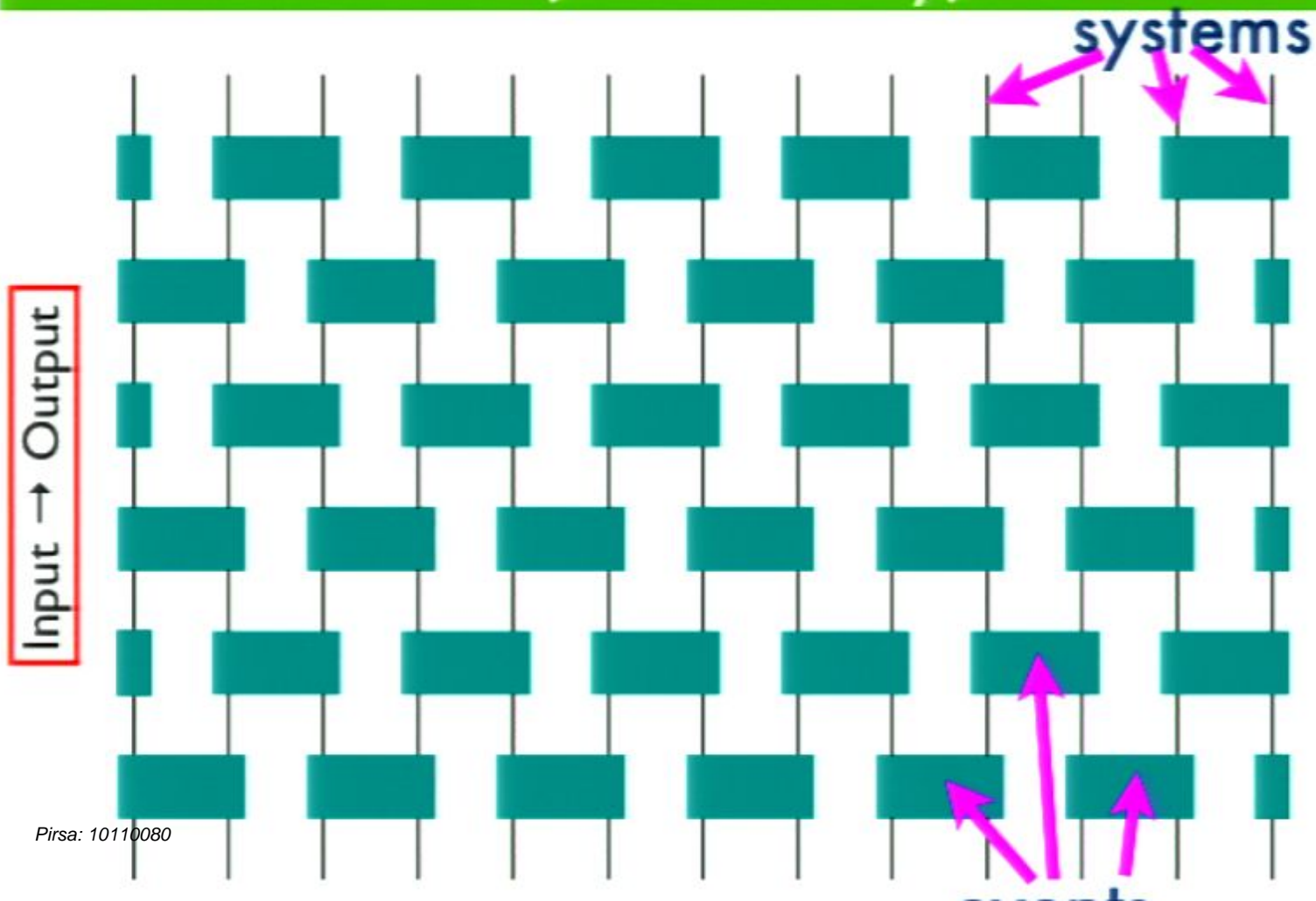
Informational description of reality:  
a causal network of events.





# Relativity from QT

(from causality)

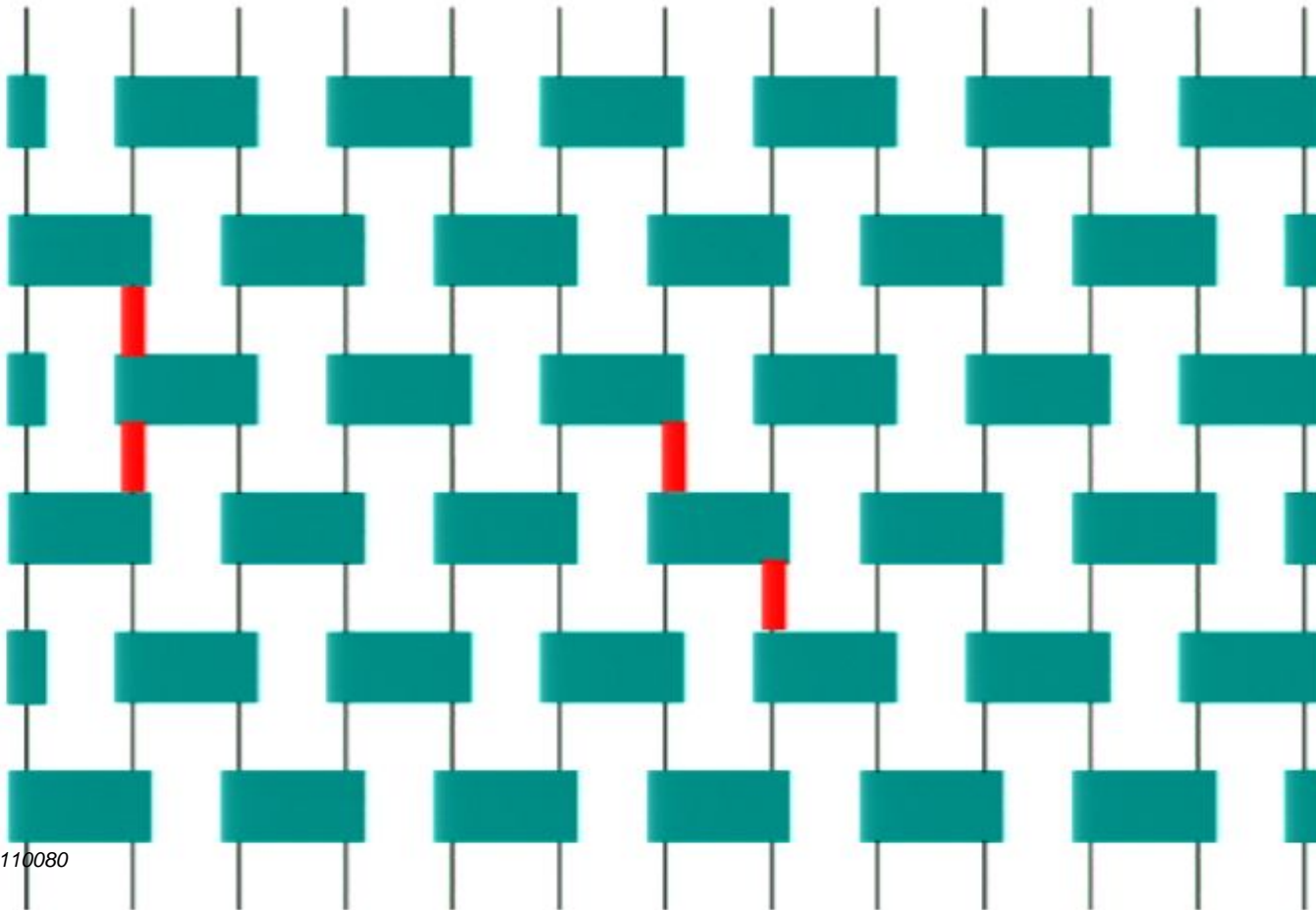


# Relativity from QT

(from causality)

causally  
connected  
systems

Input → Output

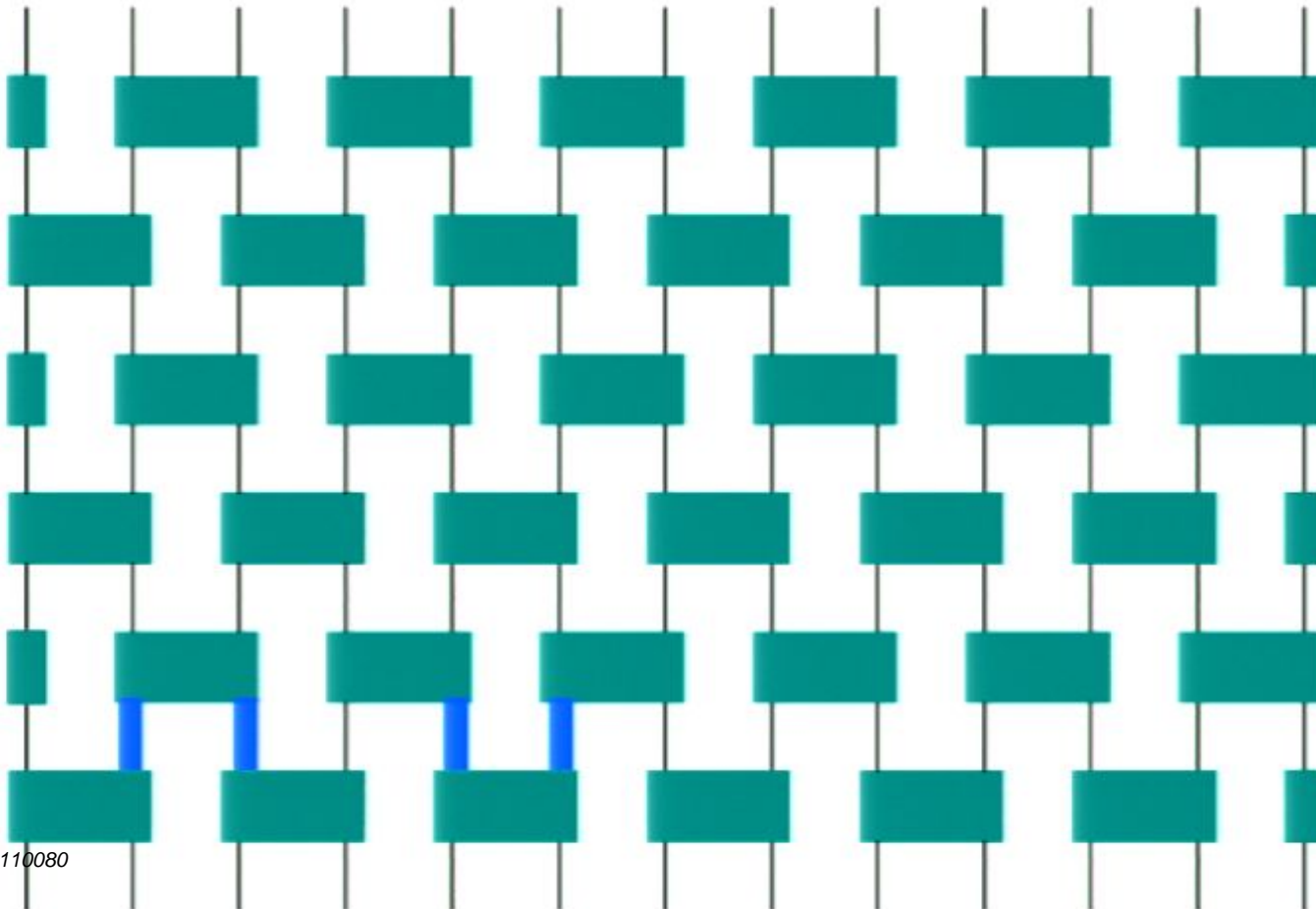




# Relativity from QT

(from causality)

Input → Output



independent  
systems

“slice”

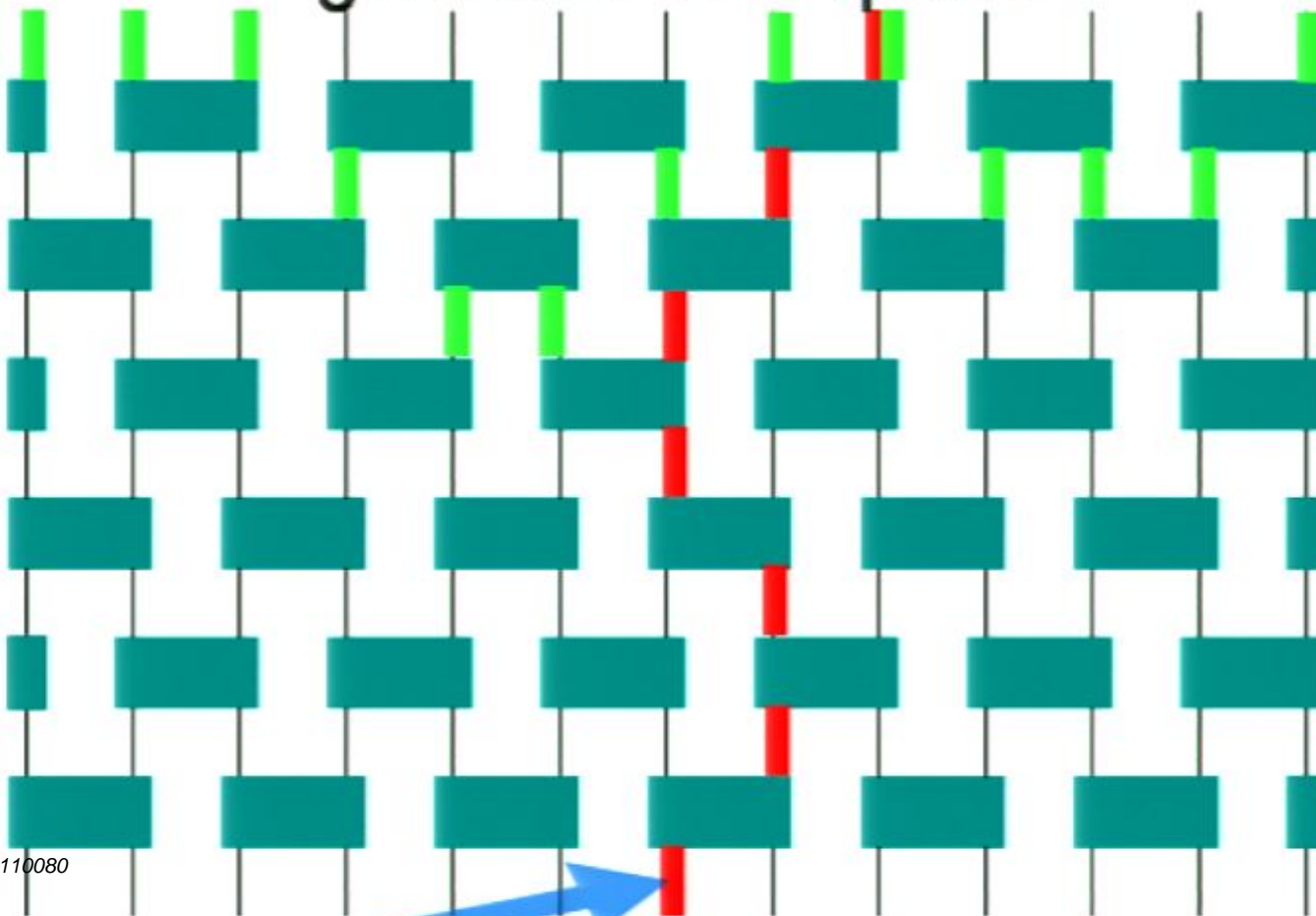
# Relativity from QT

(from causality)

topology  
(Alexandrov)

global slice = space

Input → Output





# Relativity from QT

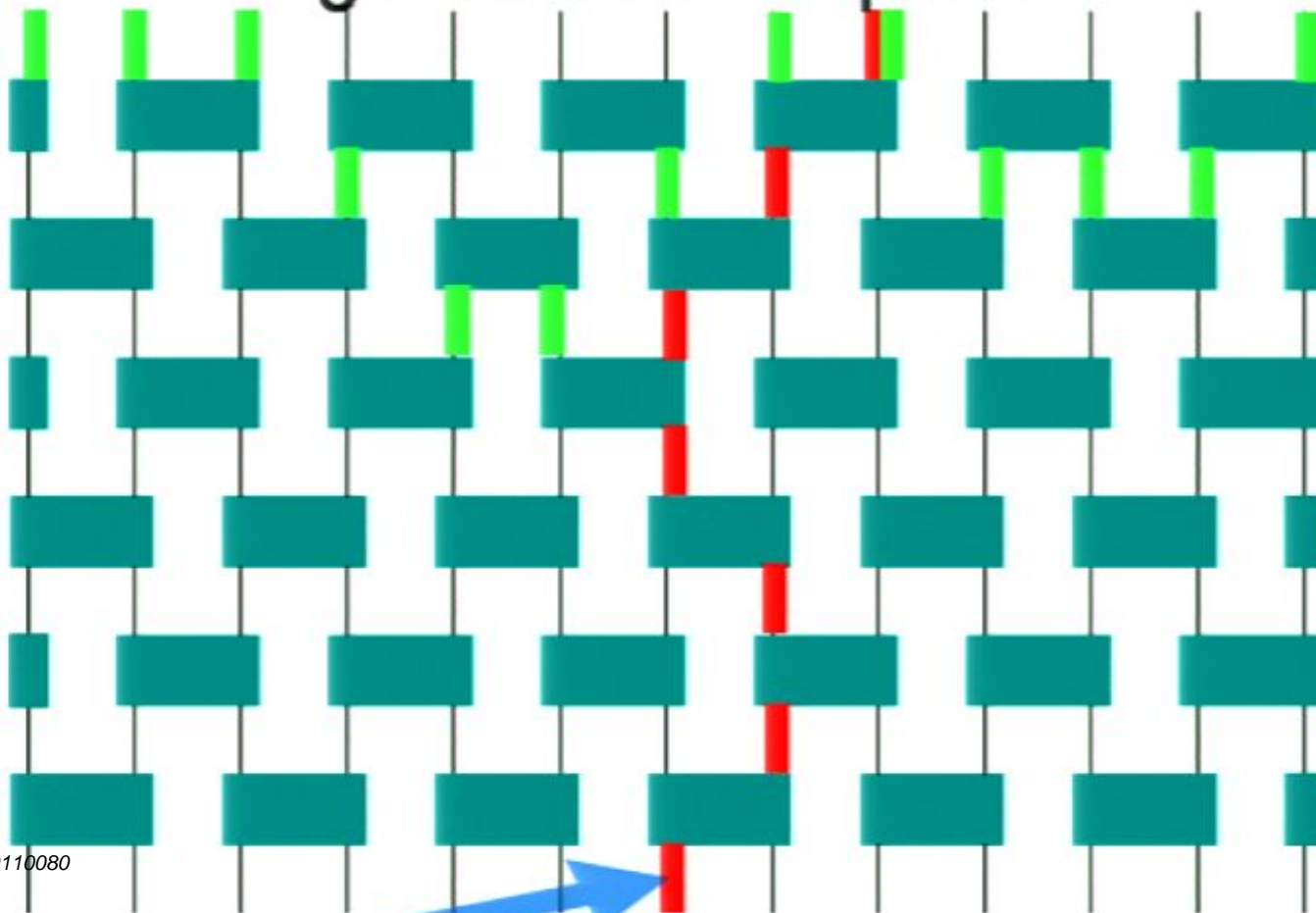
(from causality)

topology  
(Alexandrov)

metric =  
event-counting

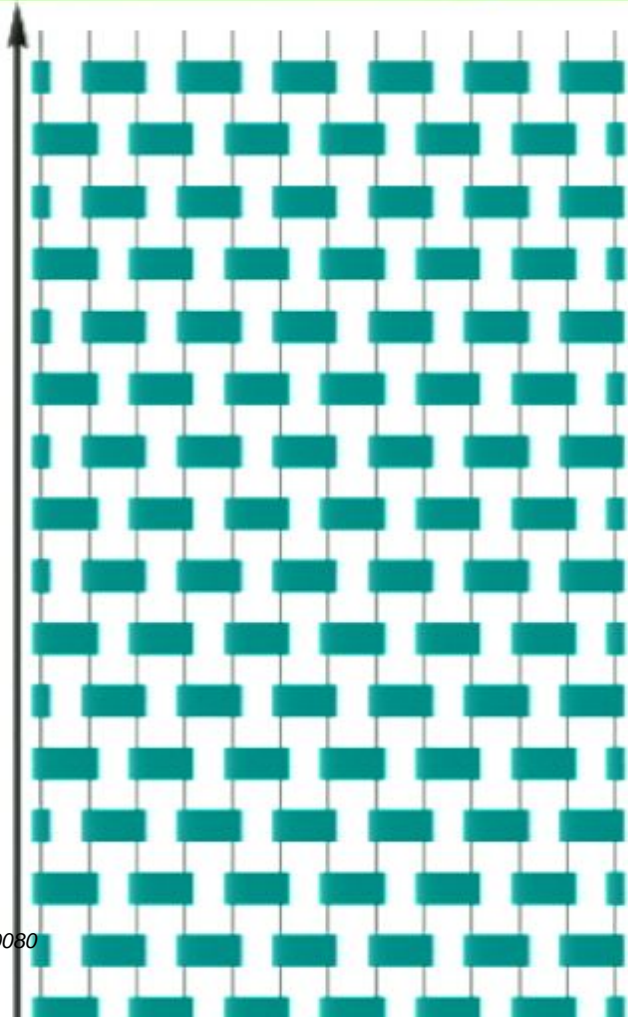
global slice = space

Input → Output



# Relativity from QT

(from causality)





# Relativity from QT

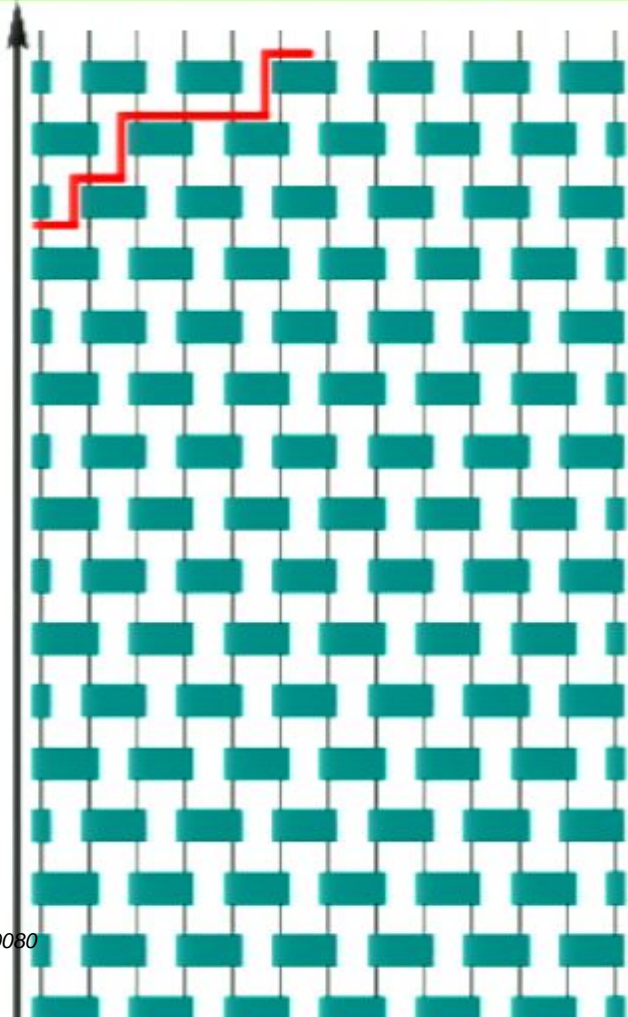
(from causality)

build a  
uniform  
foliation

# Relativity from QT

(from causality)

build a  
uniform  
foliation





# Relativity from QT

Operating  
Systems

R. Stockton Gaines  
Editor

## Time, Clocks, and the Ordering of Events in a Distributed System

Leslie Lamport  
Massachusetts Computer Associates, Inc.

The concept of one event happening before another in a distributed system is examined, and is shown to define a partial ordering of the events. A distributed algorithm is given for synchronizing a system of logical clocks which can be used to totally order the events. The use of the total ordering is illustrated with a method for solving synchronization problems. The algorithm is then specialized for synchronizing physical clocks, and a bound is derived on how far out of synchrony the clocks can become.

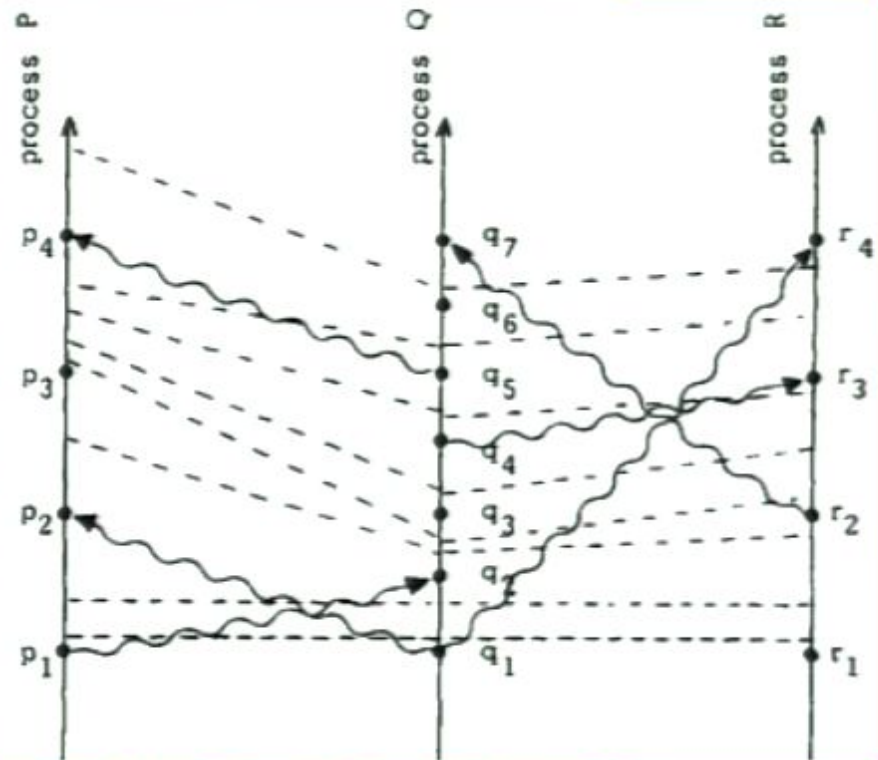
Key Words and Phrases: distributed systems, computer networks, clock synchronization, multiprocess

A distributed system consists of a collection of distinct processes which are spatially separated, and which communicate with one another by exchanging messages. A network of inter-

net, is a distributed control unit. channels are if the messages compared to the We will spatially separated remarks will tiprocessing lems similar the unpredictable occur.

In a distributed say that one "happened before" of the events often arise because and its implications

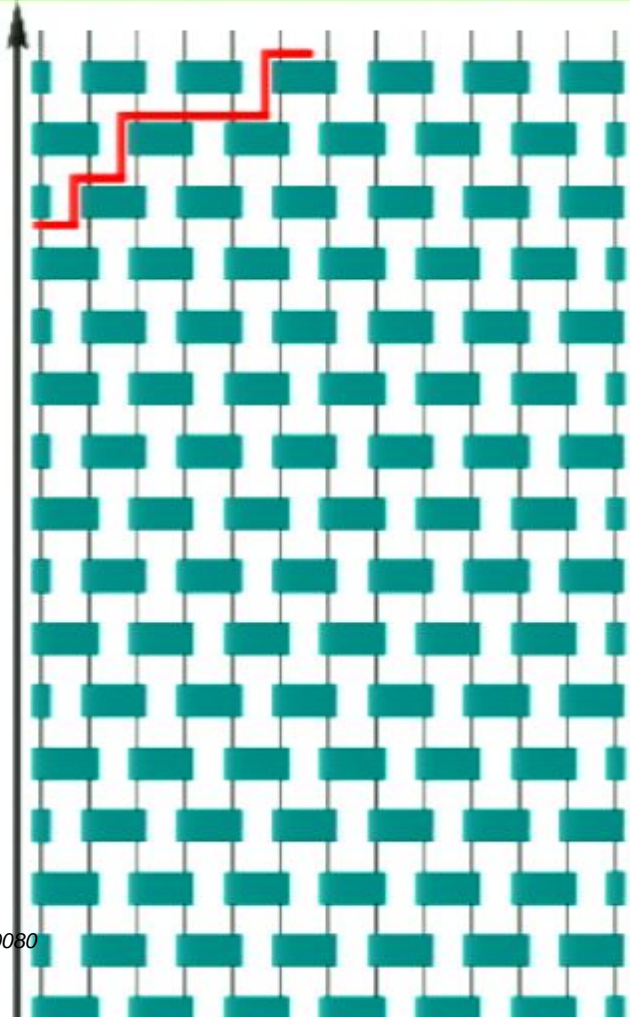
In this paper, we show the partial ordering defined by the "happened before" relation, and give a distributed algorithm for extending it to a consistent total ordering of all the events. This algorithm can provide a useful mechanism for implementing a distributed Communications illustrate its use with a simple method of



# Relativity from QT

(from causality)

build a  
uniform  
foliation

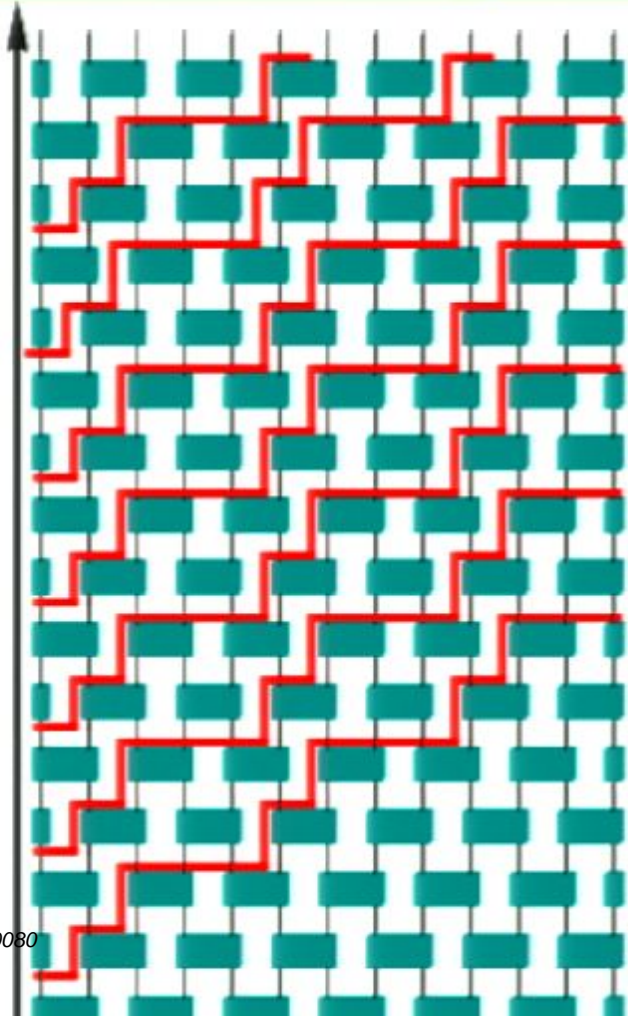




# Relativity from QT

(from causality)

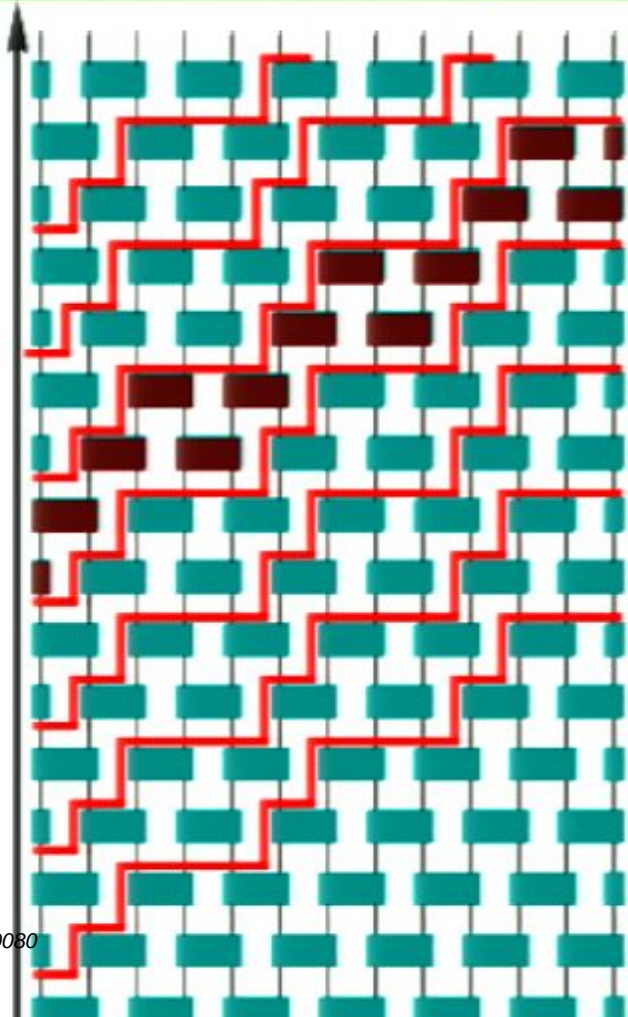
build a  
uniform  
foliation



# Relativity from QT

(from causality)

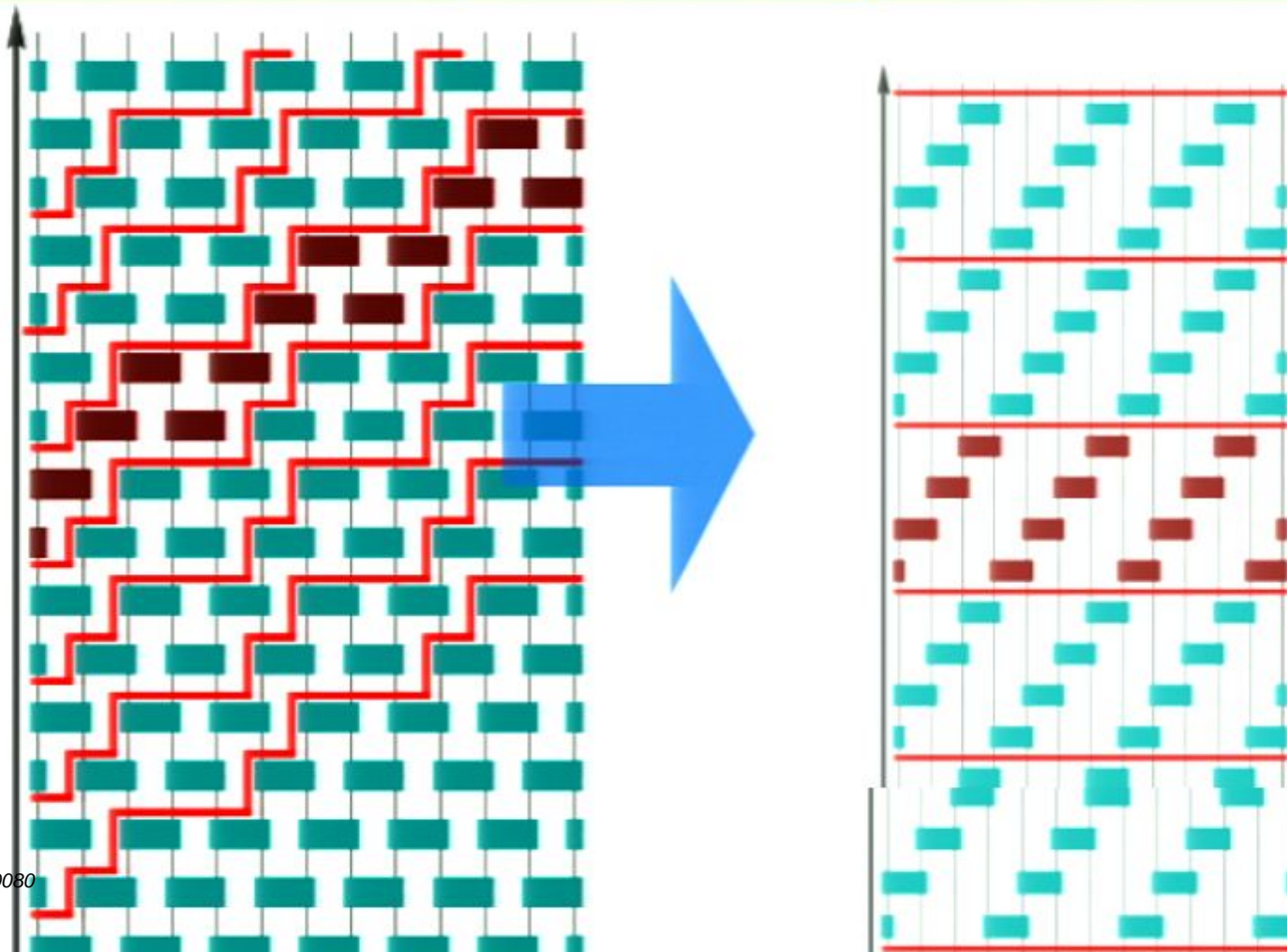
build a  
uniform  
foliation





# Relativity from QT

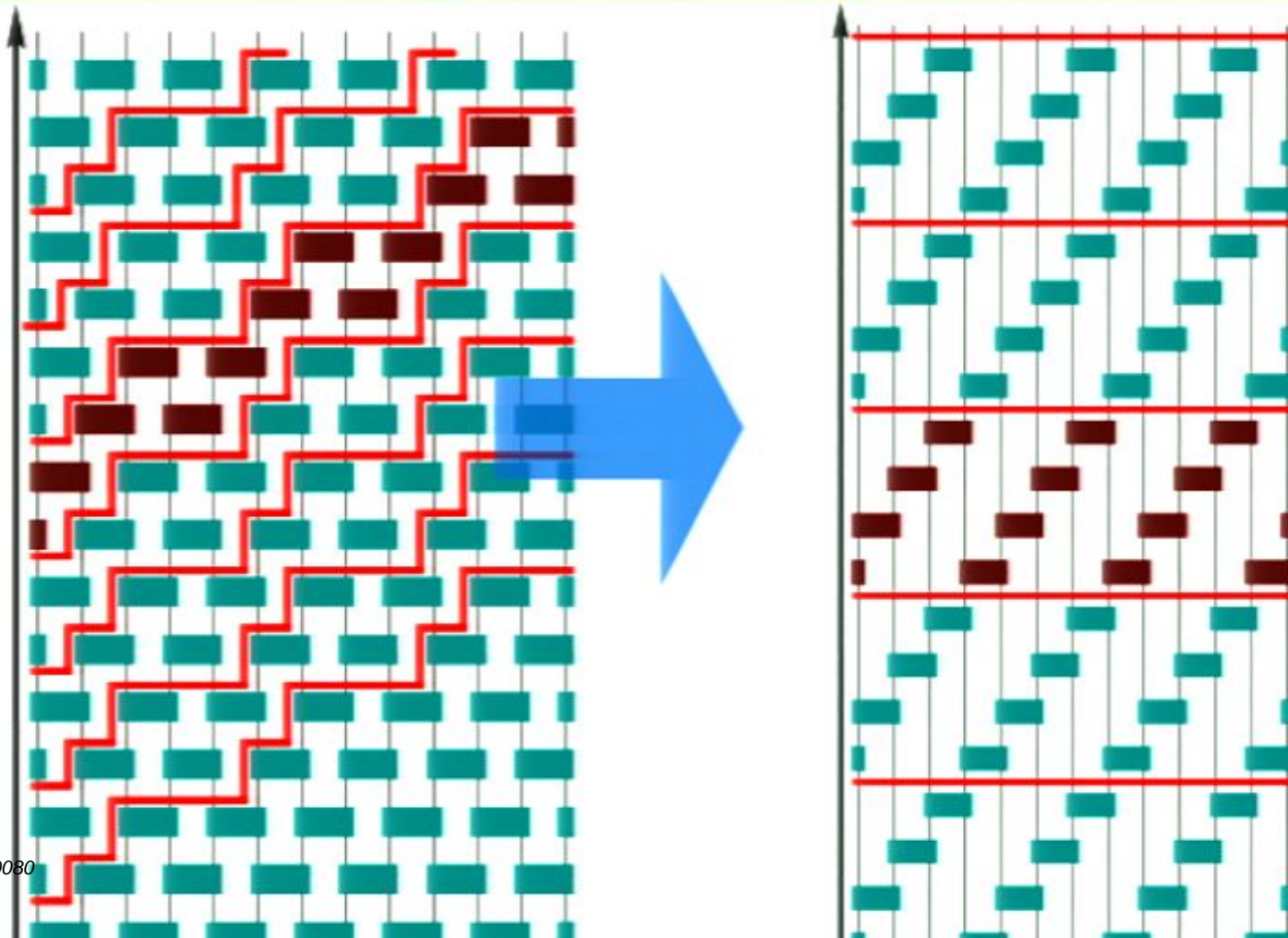
(from causality)



change  
reference

# Relativity from QT

(from causality)



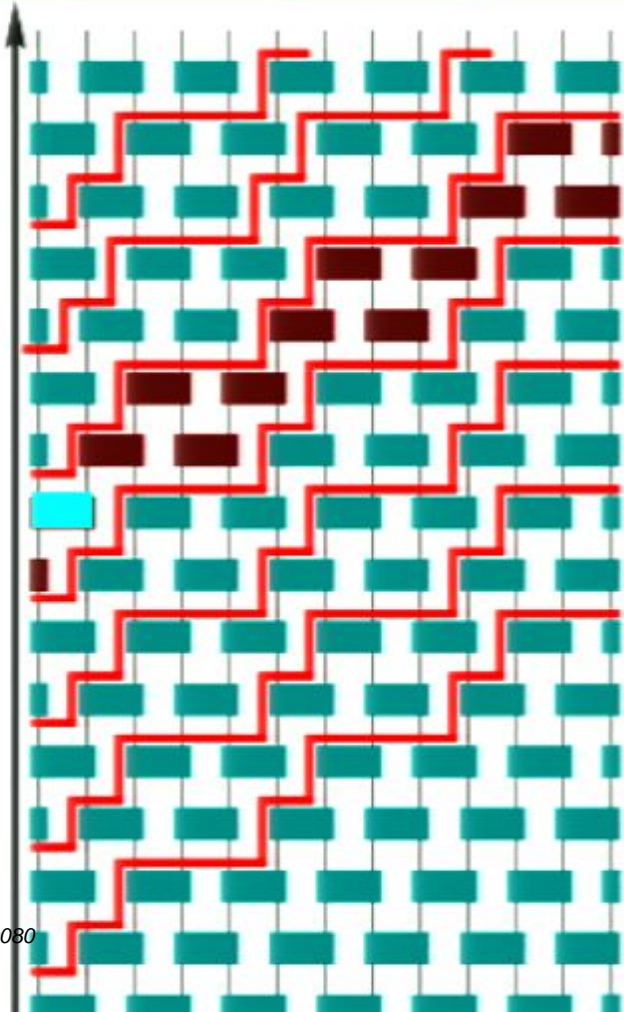
change  
reference



# Relativity from QT

(from causality)

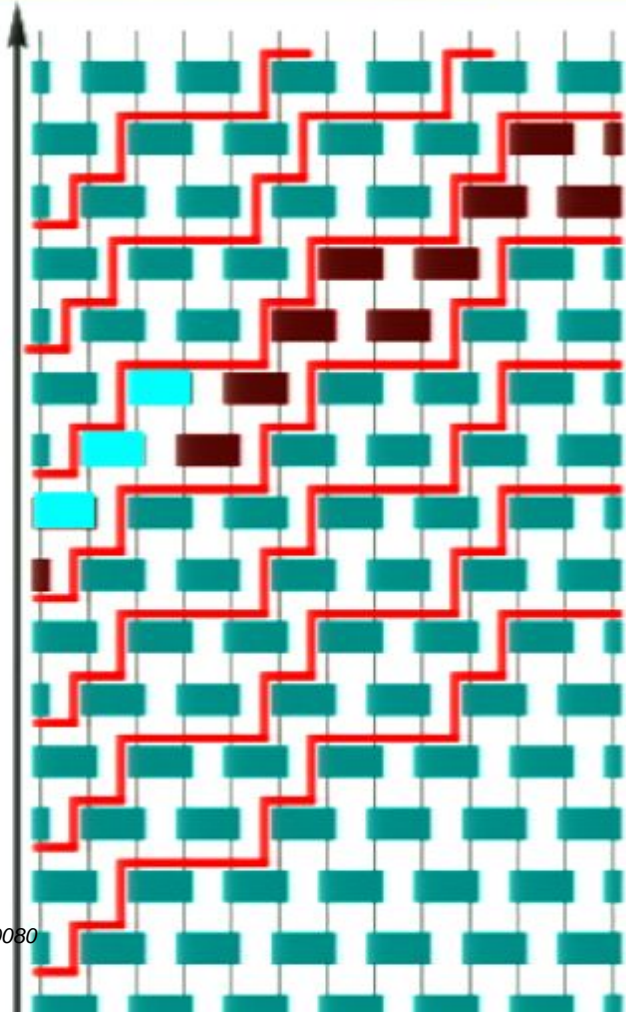
speed of  
light



# Relativity from QT

(from causality)

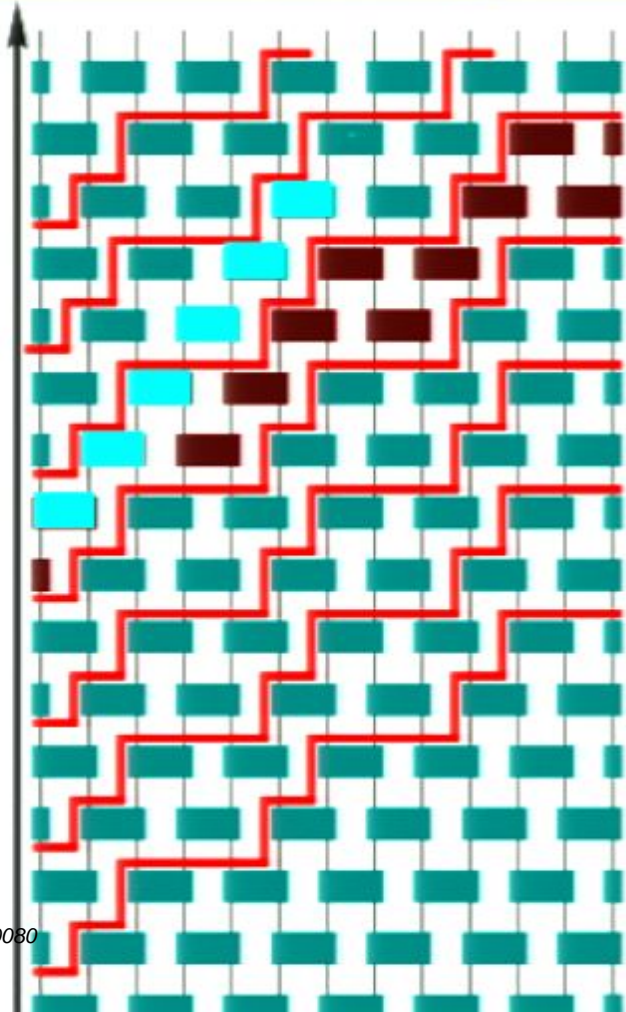
speed of  
light



# Relativity from QT

(from causality)

speed of  
light

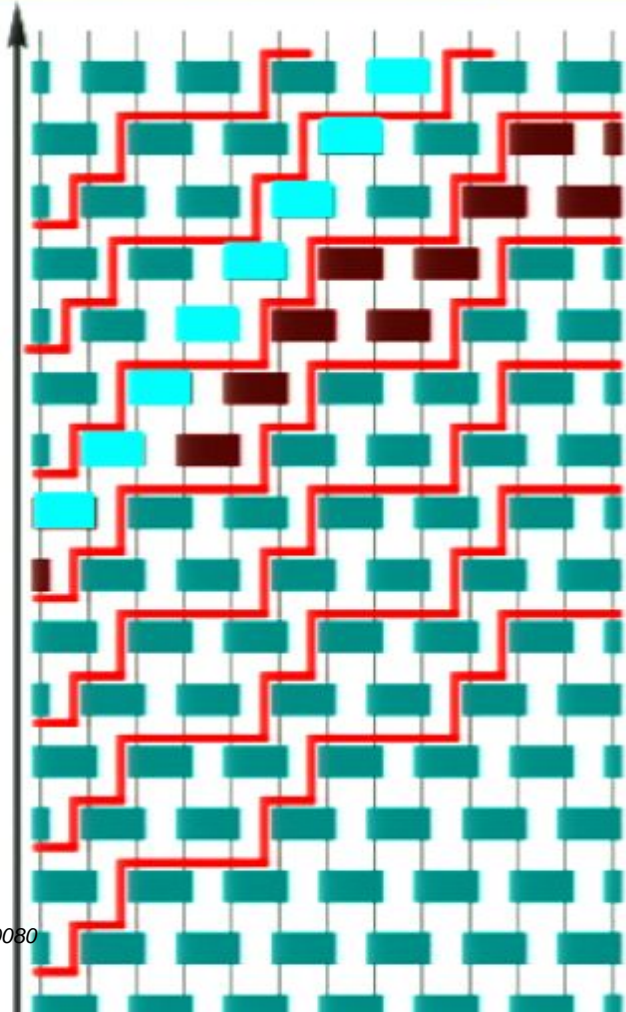




# Relativity from QT

(from causality)

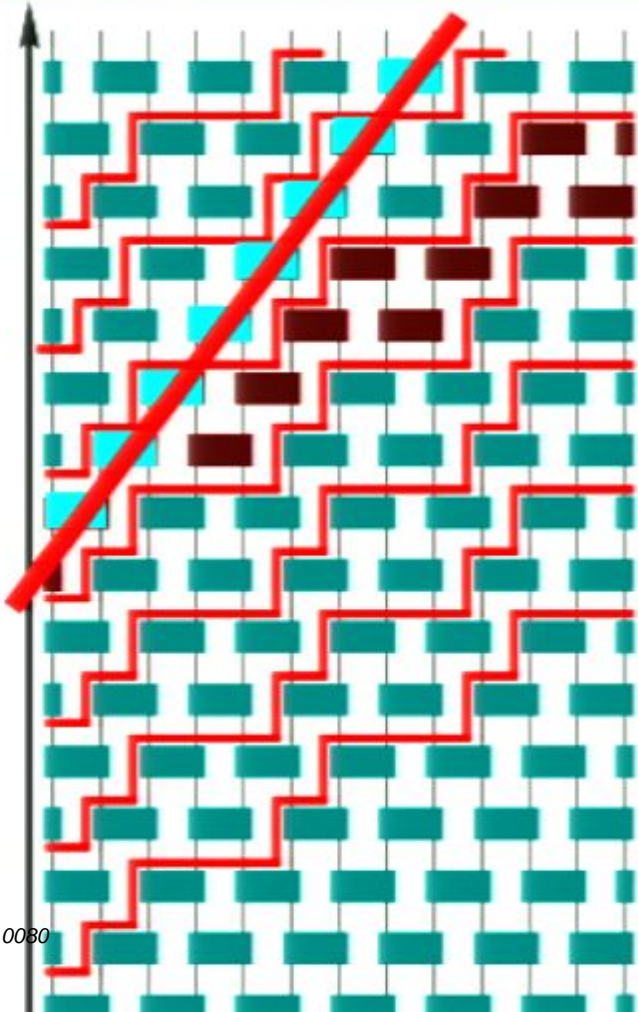
speed of  
light



# Relativity from QT

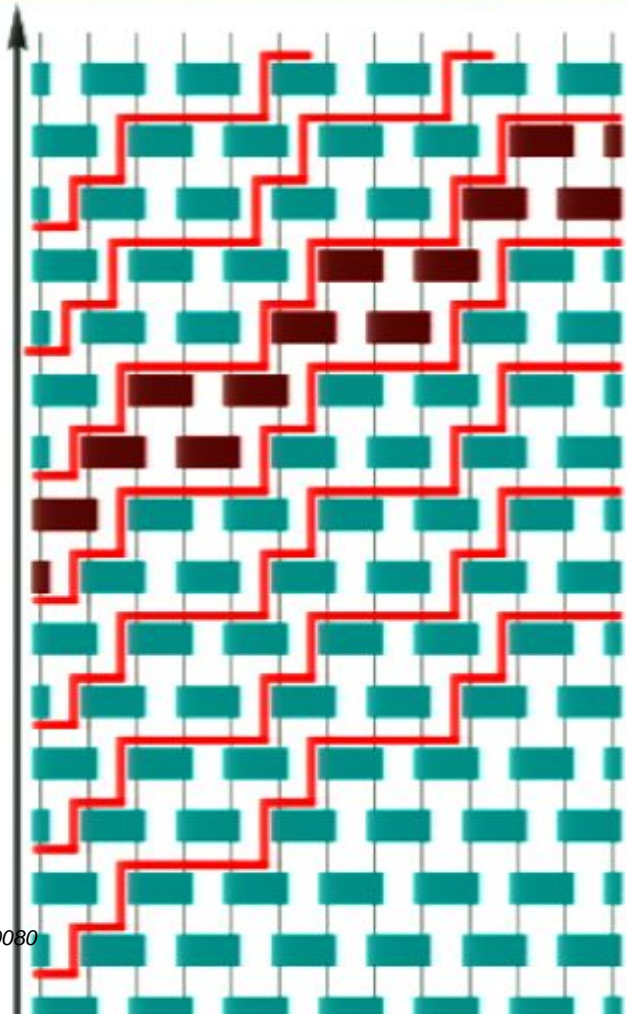
(from causality)

speed of  
light



# Relativity from QT

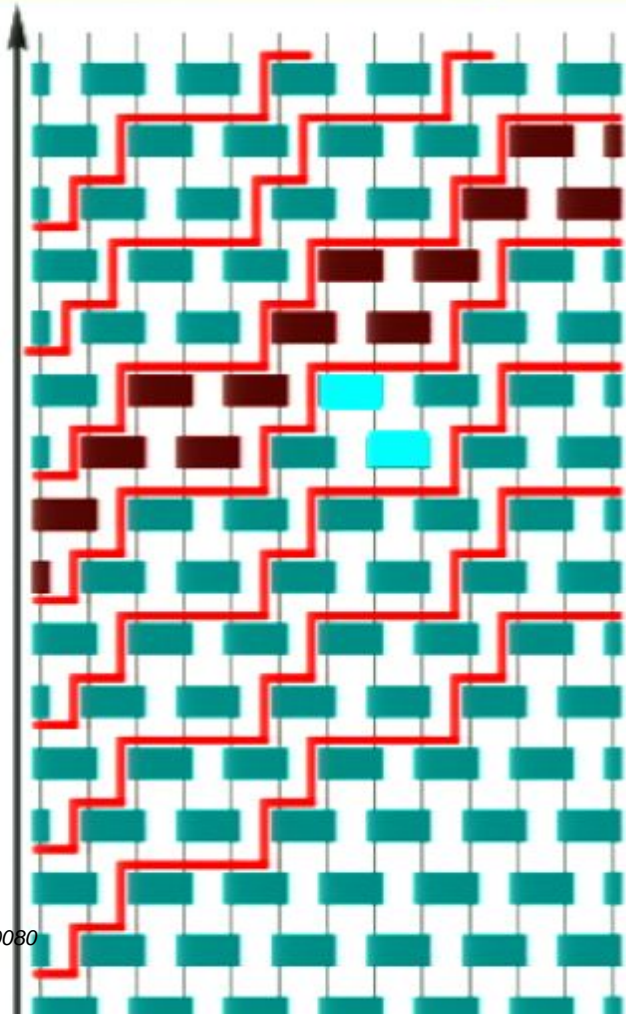
(from causality)





# Relativity from QT

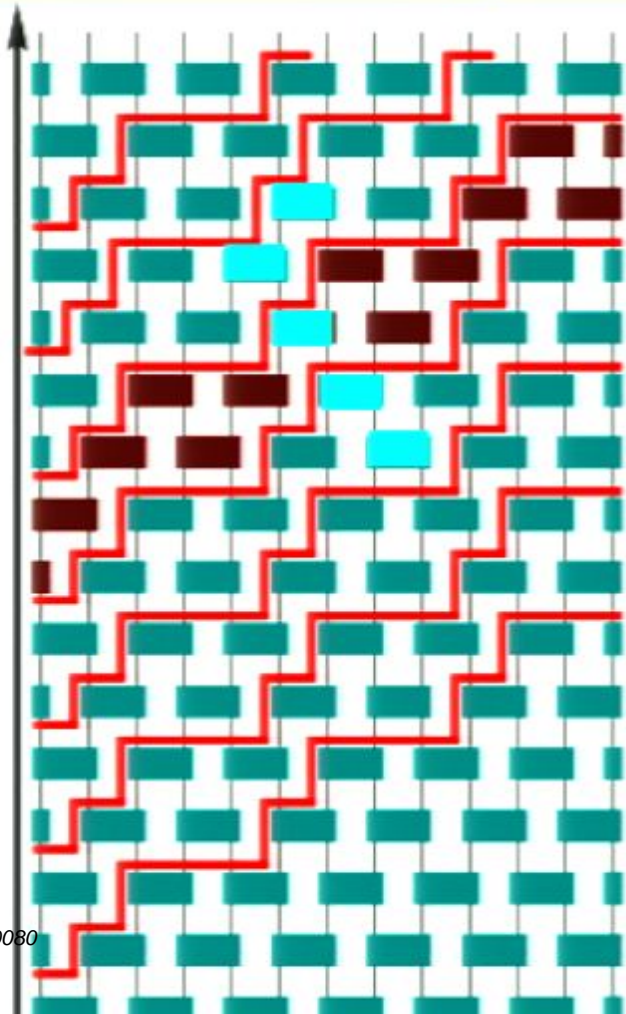
(from causality)



clock tic-tac

# Relativity from QT

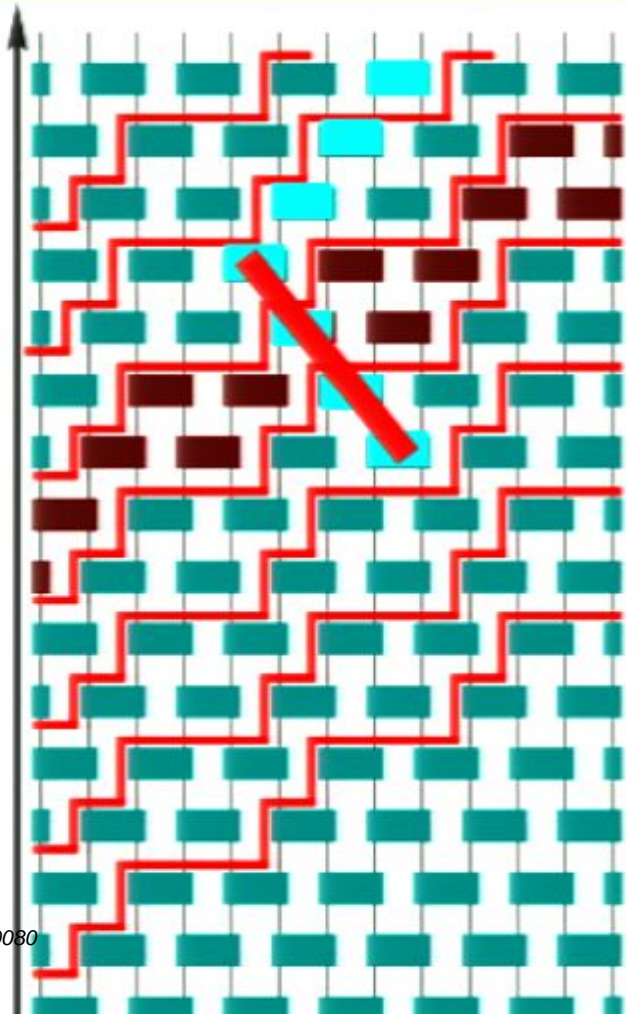
(from causality)



clock tic-tac

# Relativity from QT

(from causality)

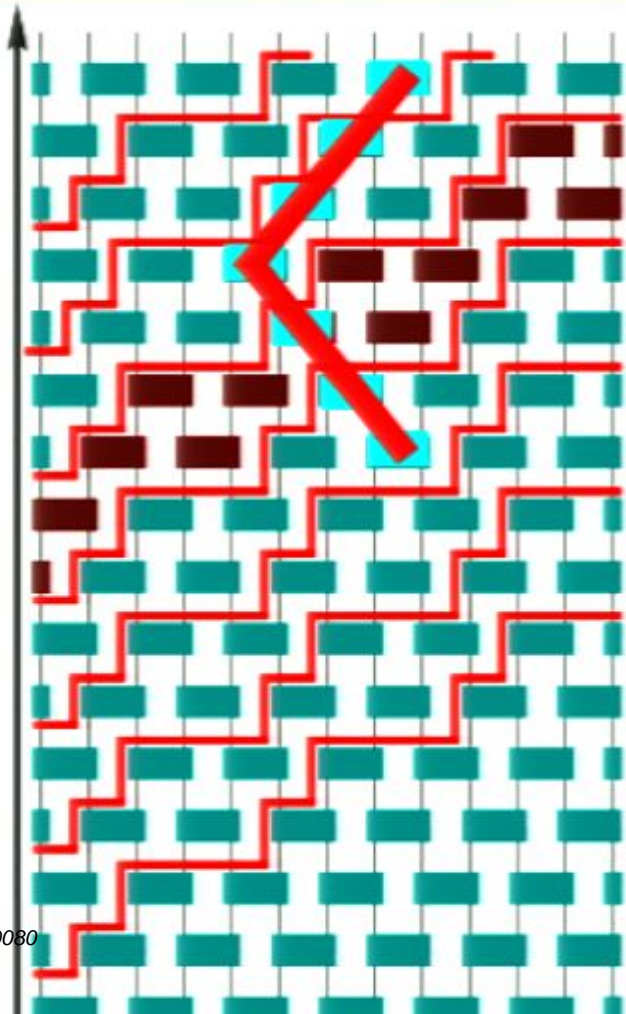


clock tic-tac

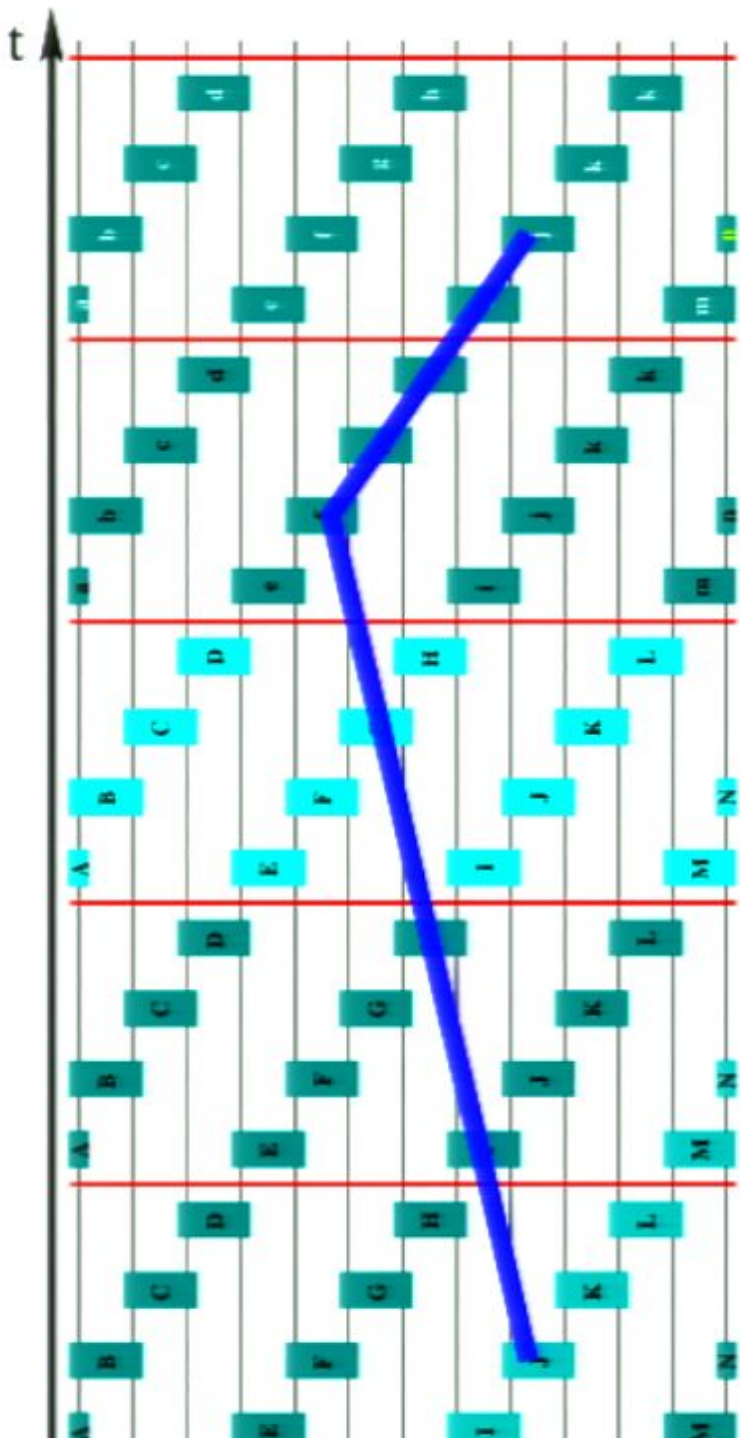
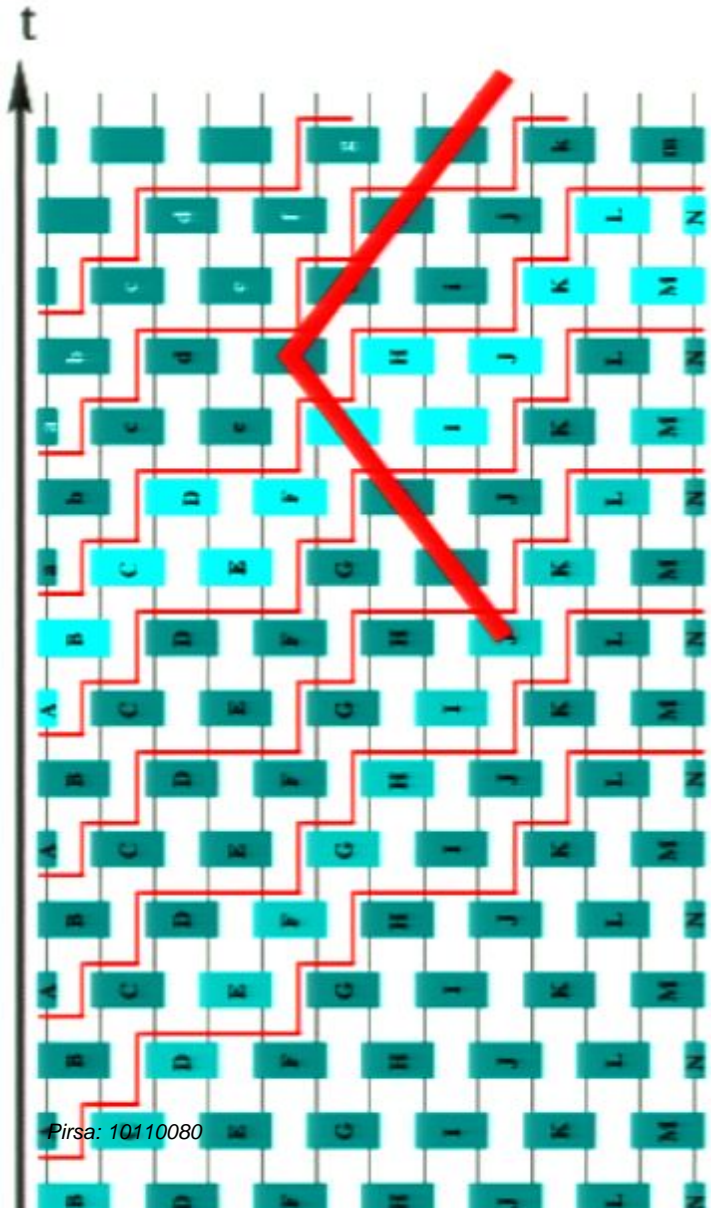


# Relativity from QT

(from causality)



clock tic-tac

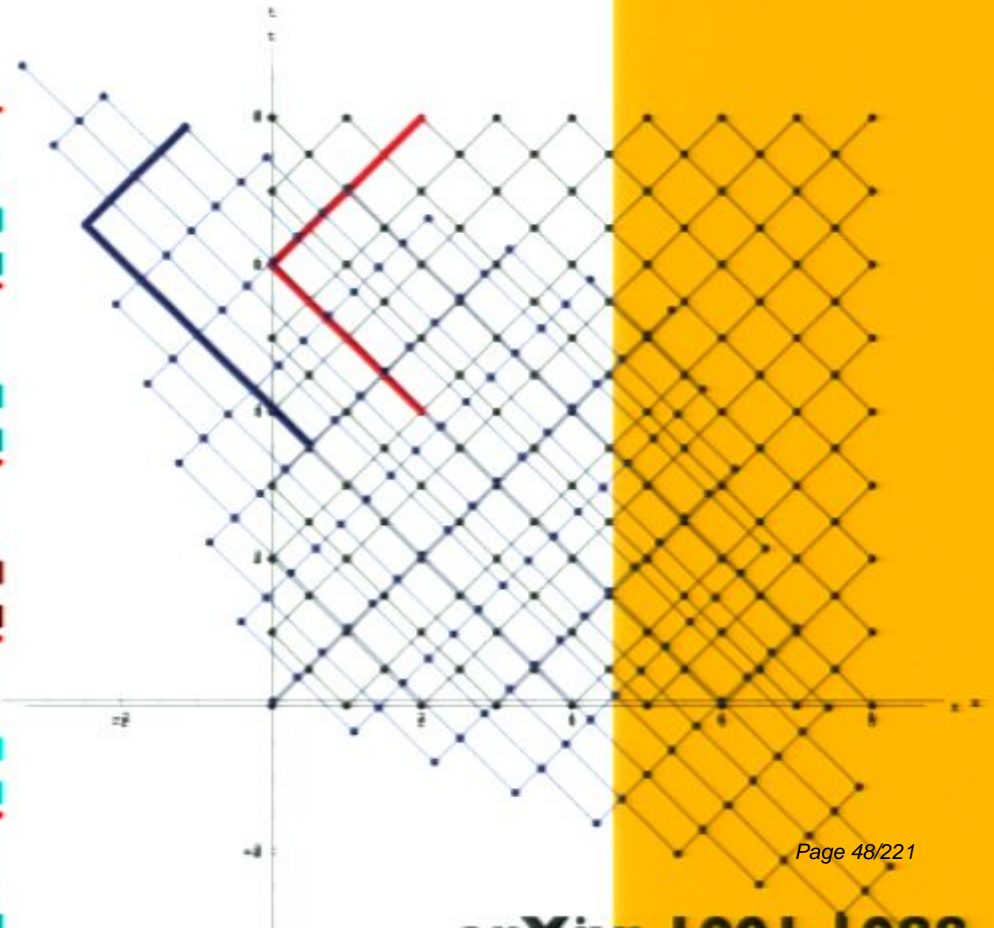
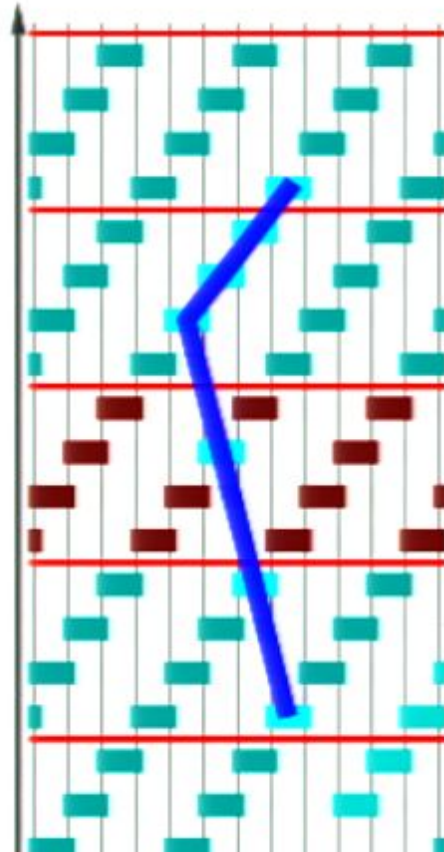
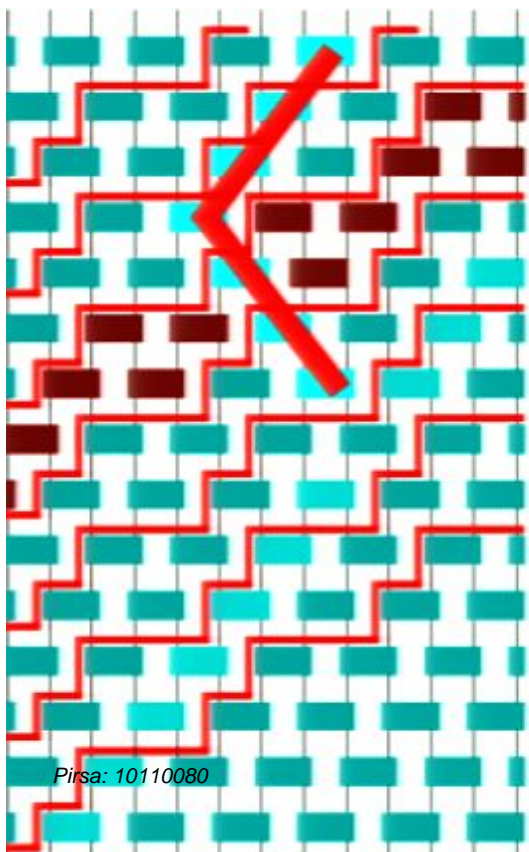


# Time dilation and space contraction



# Relativity from QT

(from causality)





---

---

FROM CAUSALITY WE GOT  
SPACE-TIME ENDOWED WITH  
RELATIVITY

---

---

# Relativity from QT

A theory of quantum gravity based on quantum computation

Seth Lloyd

Massachusetts Institute of Technology  
MIT 3-160, Cambridge, Mass. 02139 USA  
slloyd@mit.edu

Keywords: quantum computation, quantum gravity

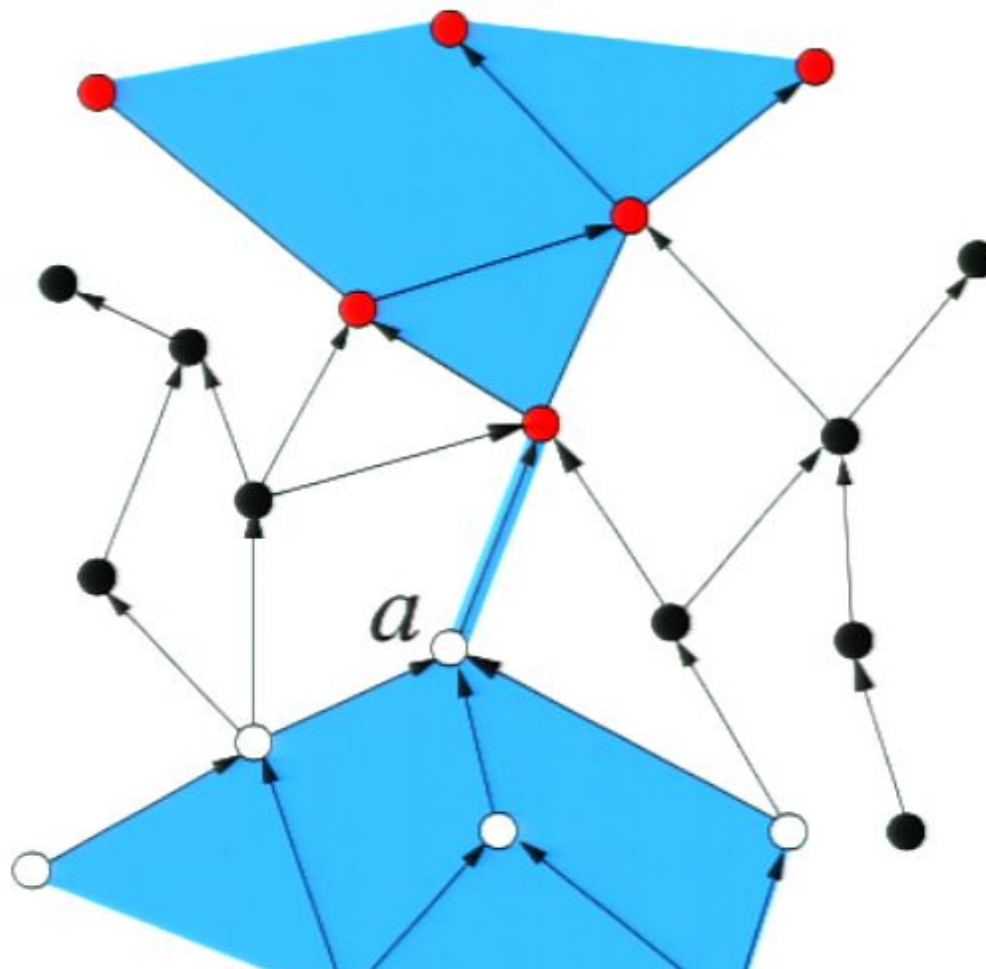
*Abstract:* This paper proposes a method of unifying quantum computation on quantum computation. In this theory, fundamental physics emerges from pairwise interactions between quantum degrees of freedom. Space-time is a construct, derived from the underlying quantum computation. Quantum computation gives rise to a superposition of four-dimensional geometries that obeys the Einstein-Regge equations. The theory predicts a reaction of the metric to computational 'matter,' but the details of this reaction are not yet known.

THE GEOMETRY OF  
SPACE-TIME IS A  
CONSTRUCT DERIVED  
FROM THE UNDERLYING  
QUANTUM INFORMATION  
PROCESSING



# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

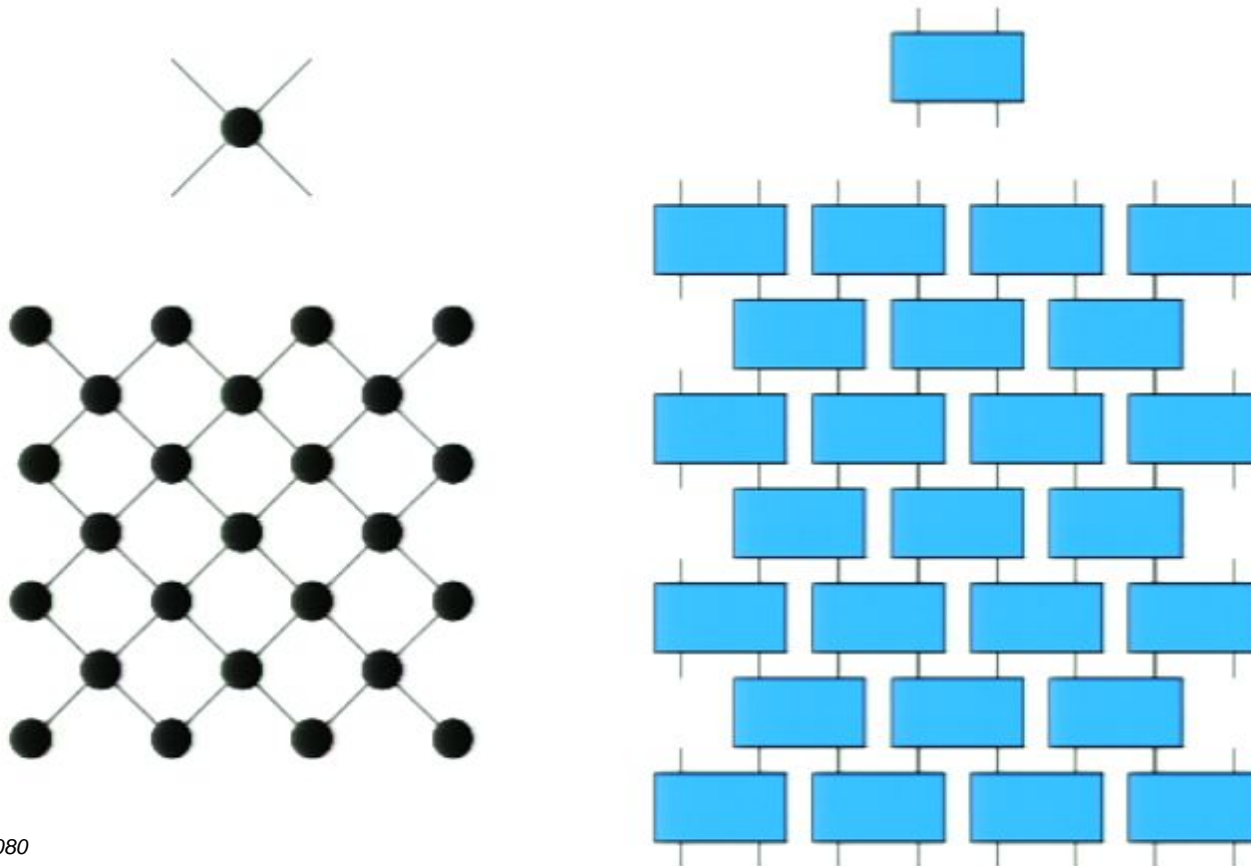


“Light” cones



# Lorentz transformations from causality and topological homogeneity

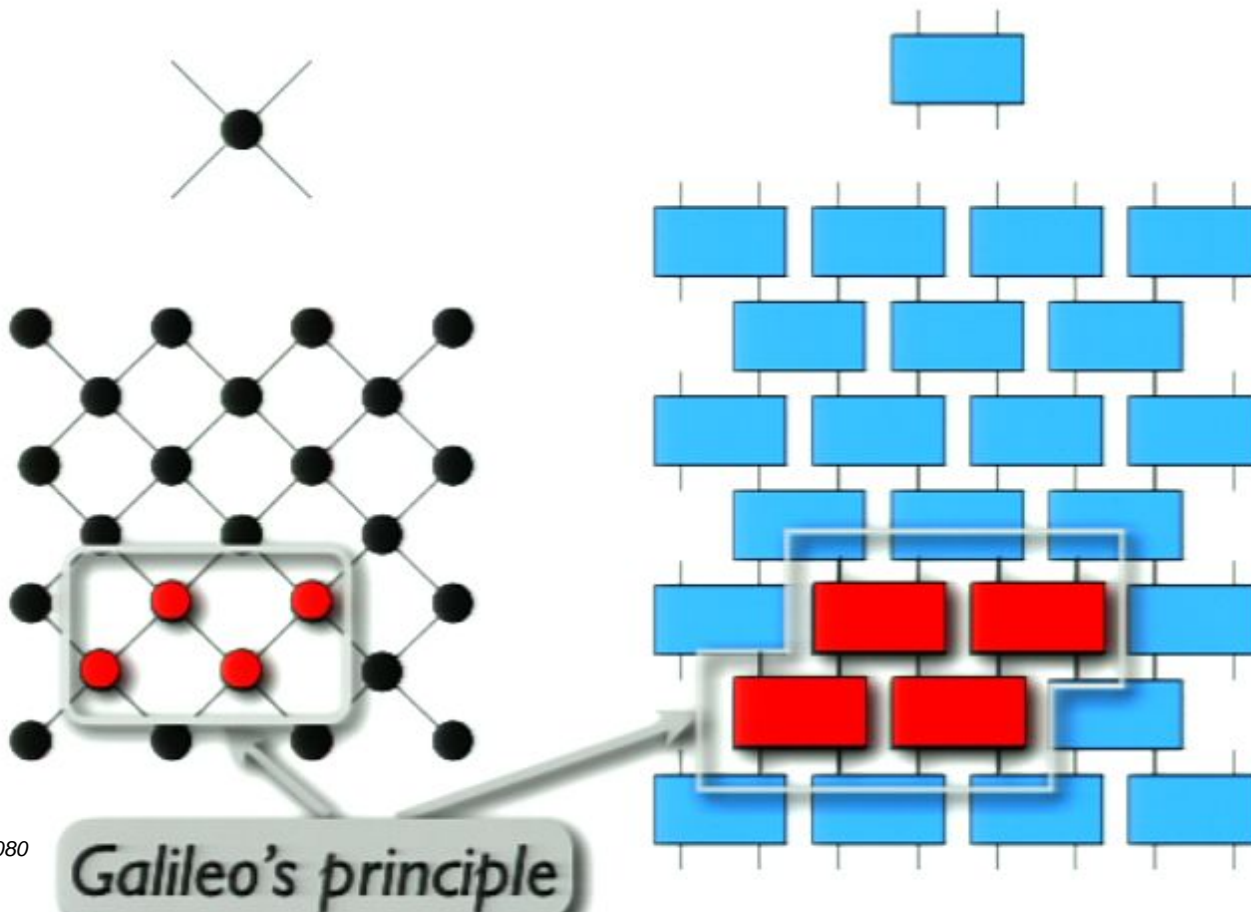
GMD and  
A. Tosini  
1008.4805



# Lorentz transformations from causality and topological homogeneity

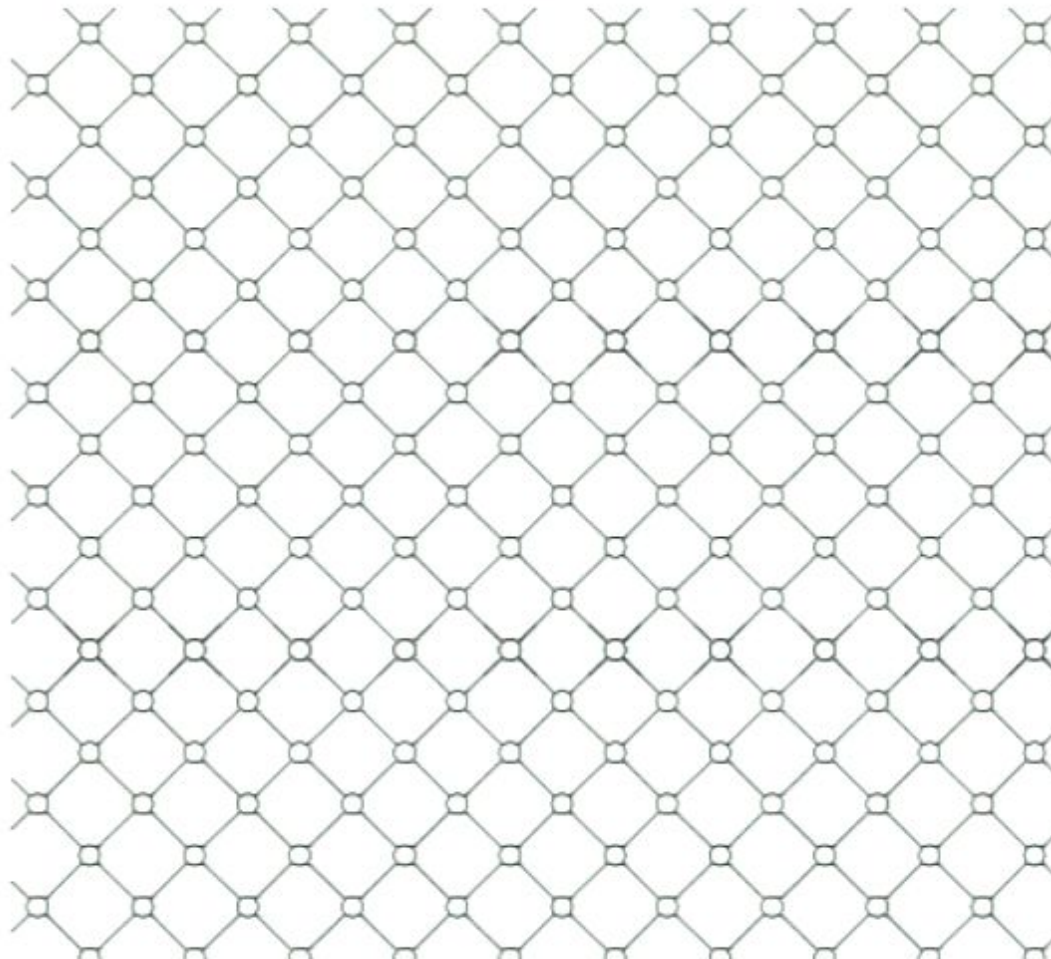
GMD and  
A. Tosini  
1008.4805

topological homogeneity



# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

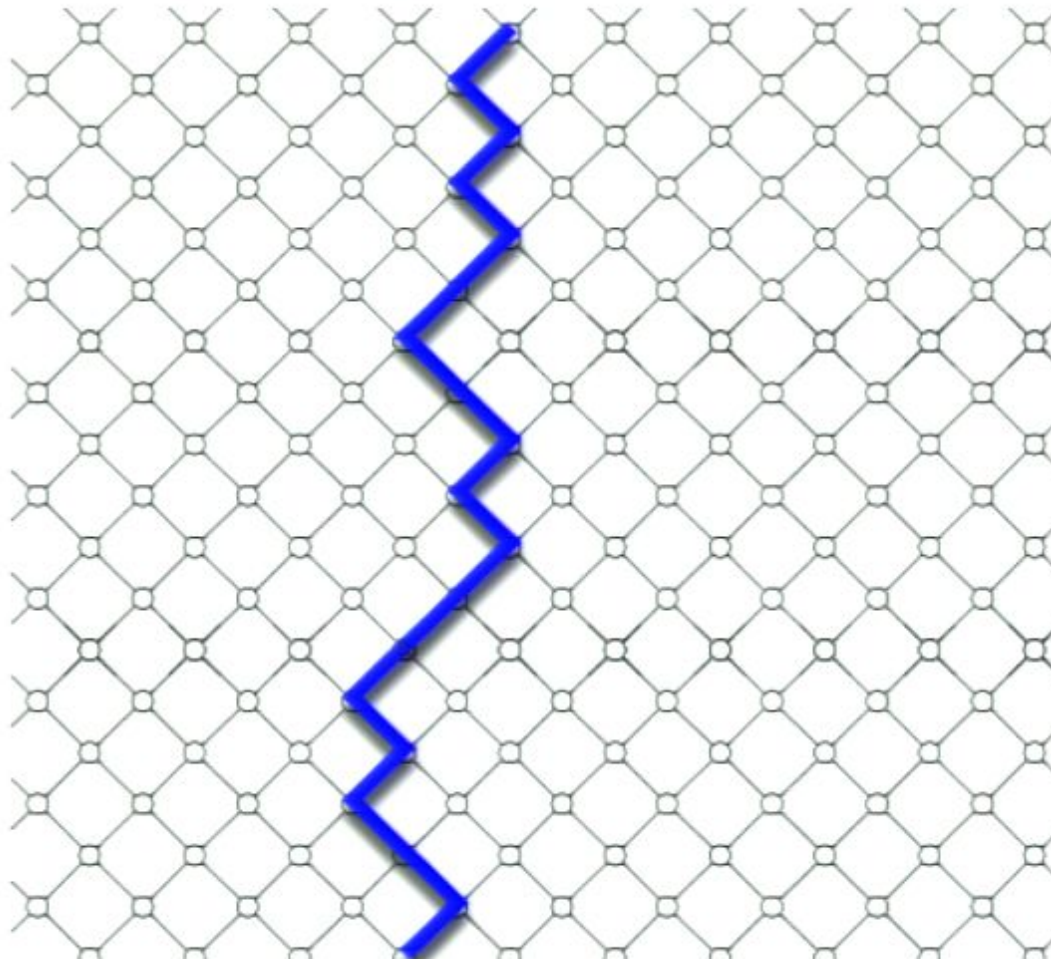


observer



# Lorentz transformations from causality and topological homogeneity

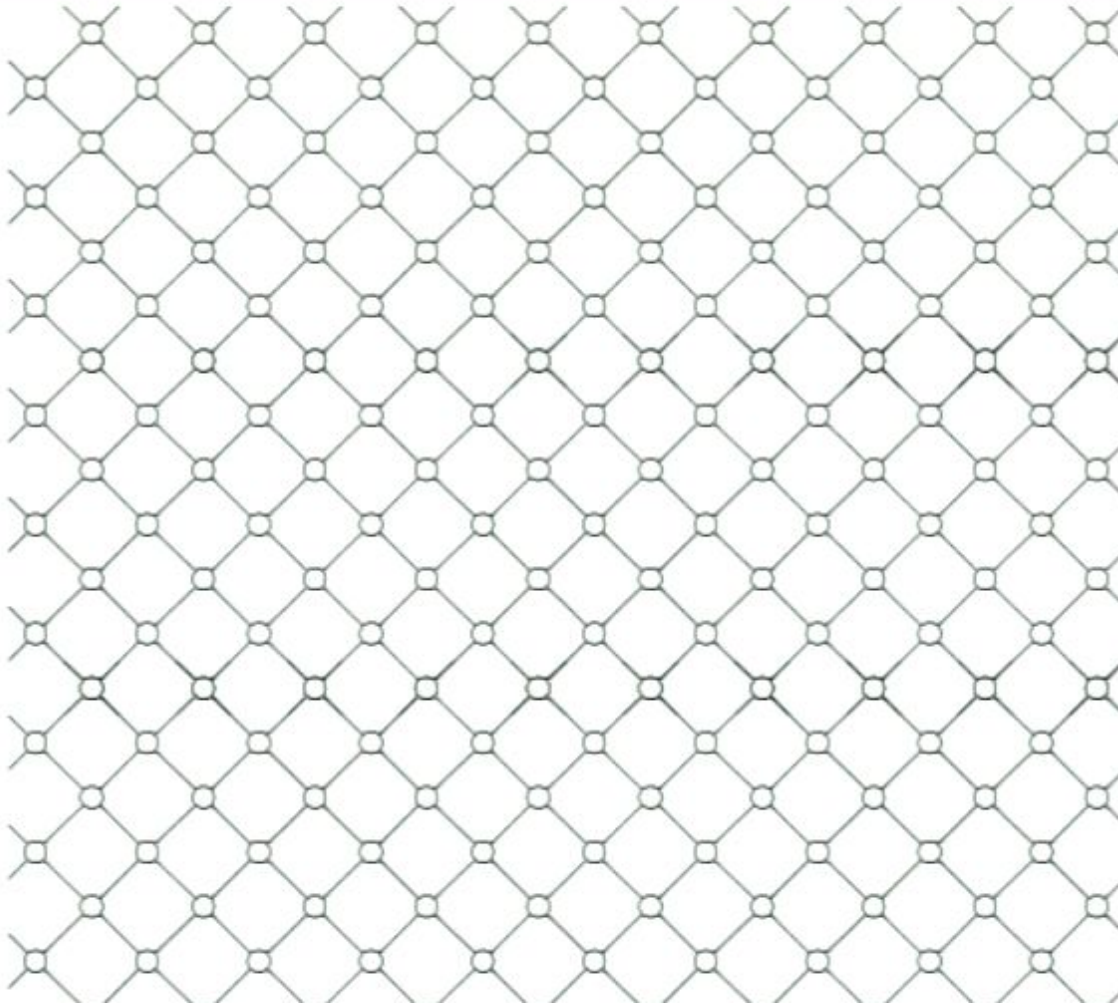
GMD and  
A. Tosini  
1008.4805



observer

# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805



Simultaneity



Build

Build In Build Out Action

Effect: None

Direction: Order

Delivery: Duration

More Options

Delete Skip Play Rehearse Record View Themes Masters Guides Smart Builds Text

B I U

Master Slides

Slide & Bullets - Left

Slide & Bullets - Right

to - Horizontal Slides

signed cardinality:  $|C(a, b)|_{\pm} := \sigma$

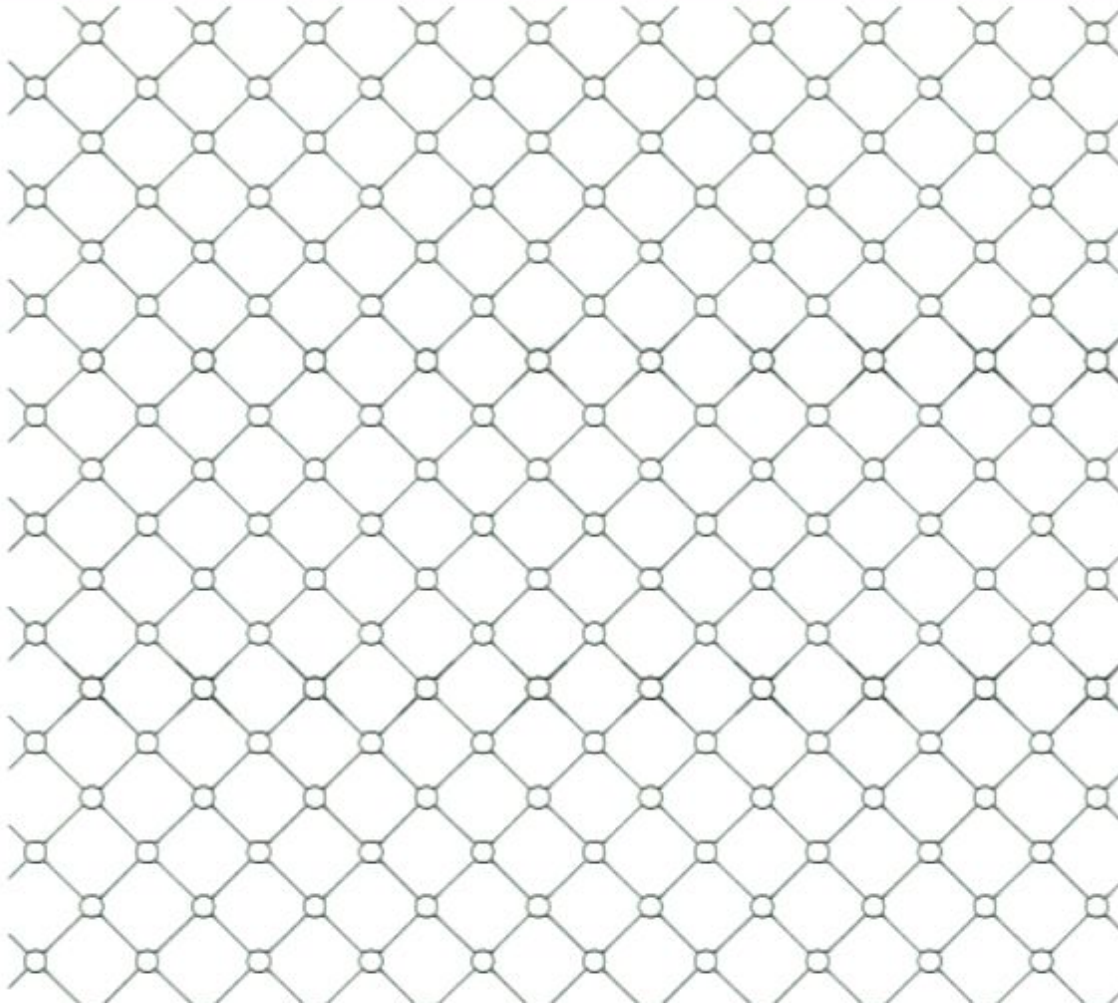
where  $\sigma = +$  for  $a < b$

The notion of simultaneity can be built by observers (clocks) shifted in different directions. We send a light signal and observe tick-tacks 1-2-3. If they are the same for general observers, and put the events on their worldlines, there do not exist synchronized clocks. Signed cardinality ...



# Lorentz transformations from causality and topological homogeneity

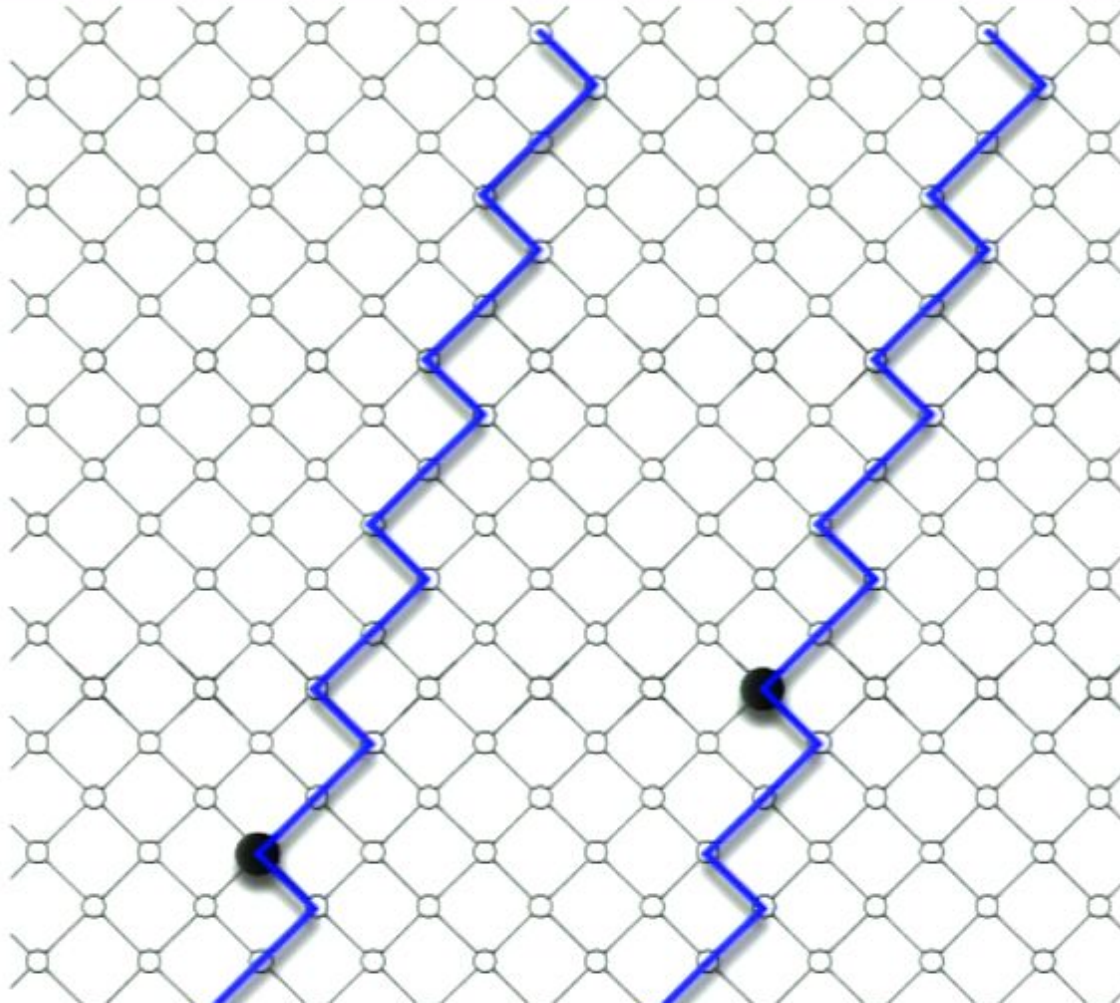
GMD and  
A. Tosini  
1008.4805



Simultaneity

# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

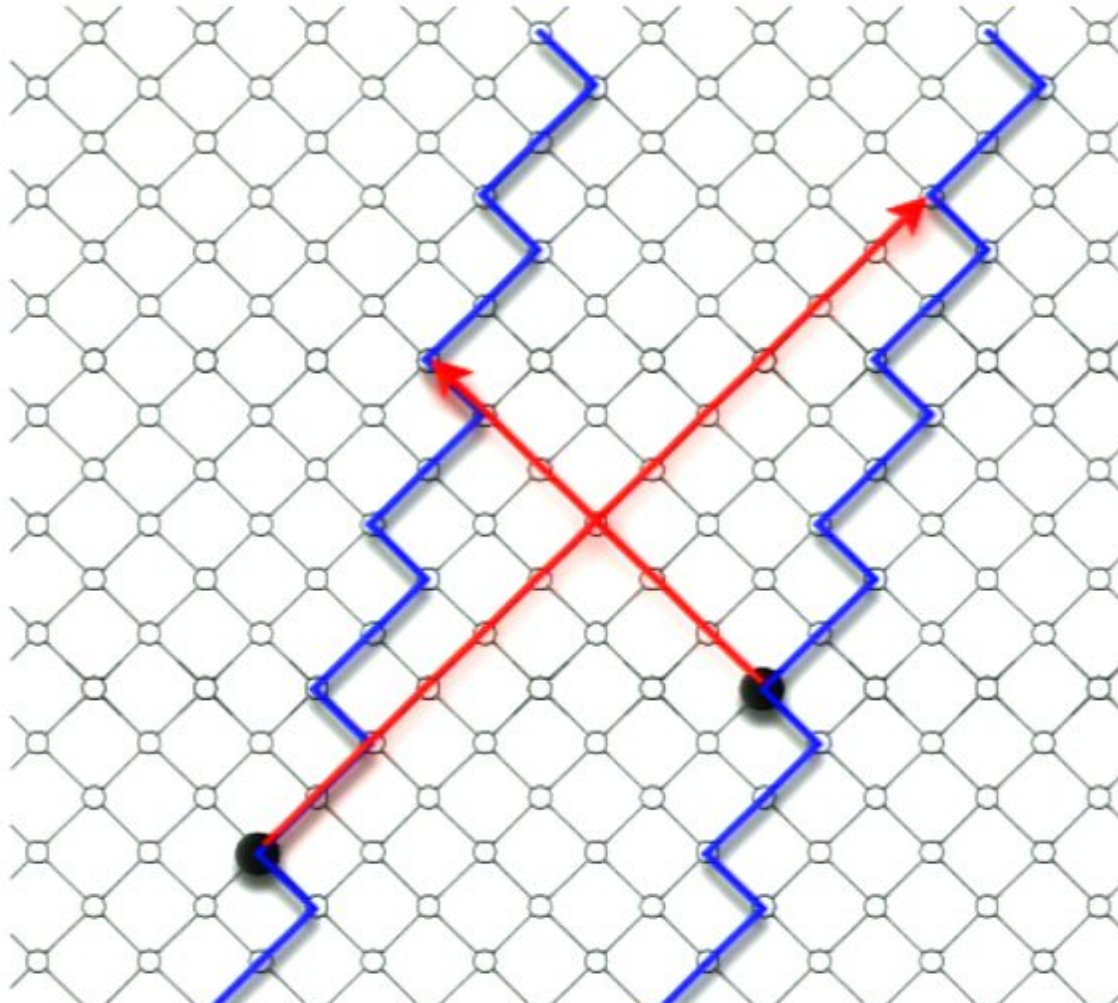


Simultaneity



# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805



Simultaneity



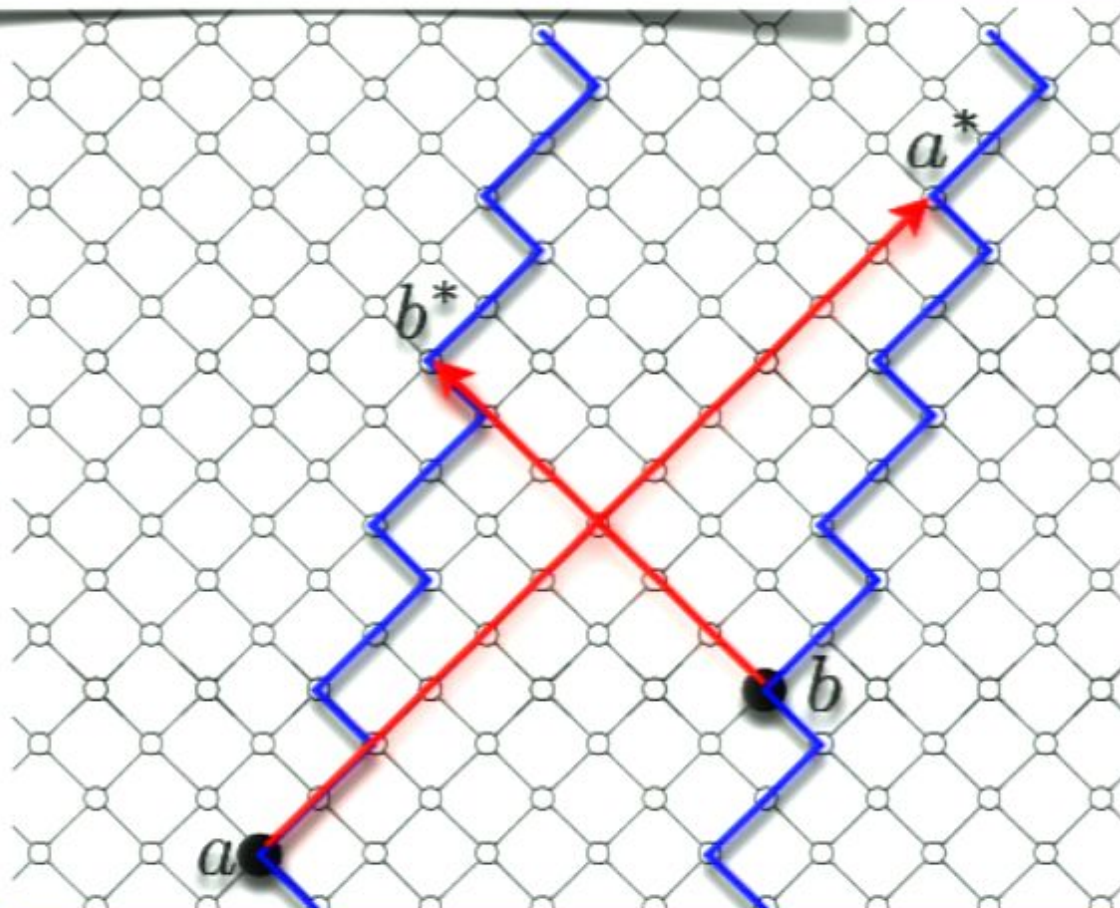
signed cardinality:  $|\mathcal{C}(a, b)|_{\pm} := \sigma |\mathcal{C}(a, b)|$

where  $\sigma = +$  for  $a \prec b$

$\sigma = -$  for  $b \prec a$

from causality  
eity

GMD and  
A. Tosini  
1008.4805



Simultaneity

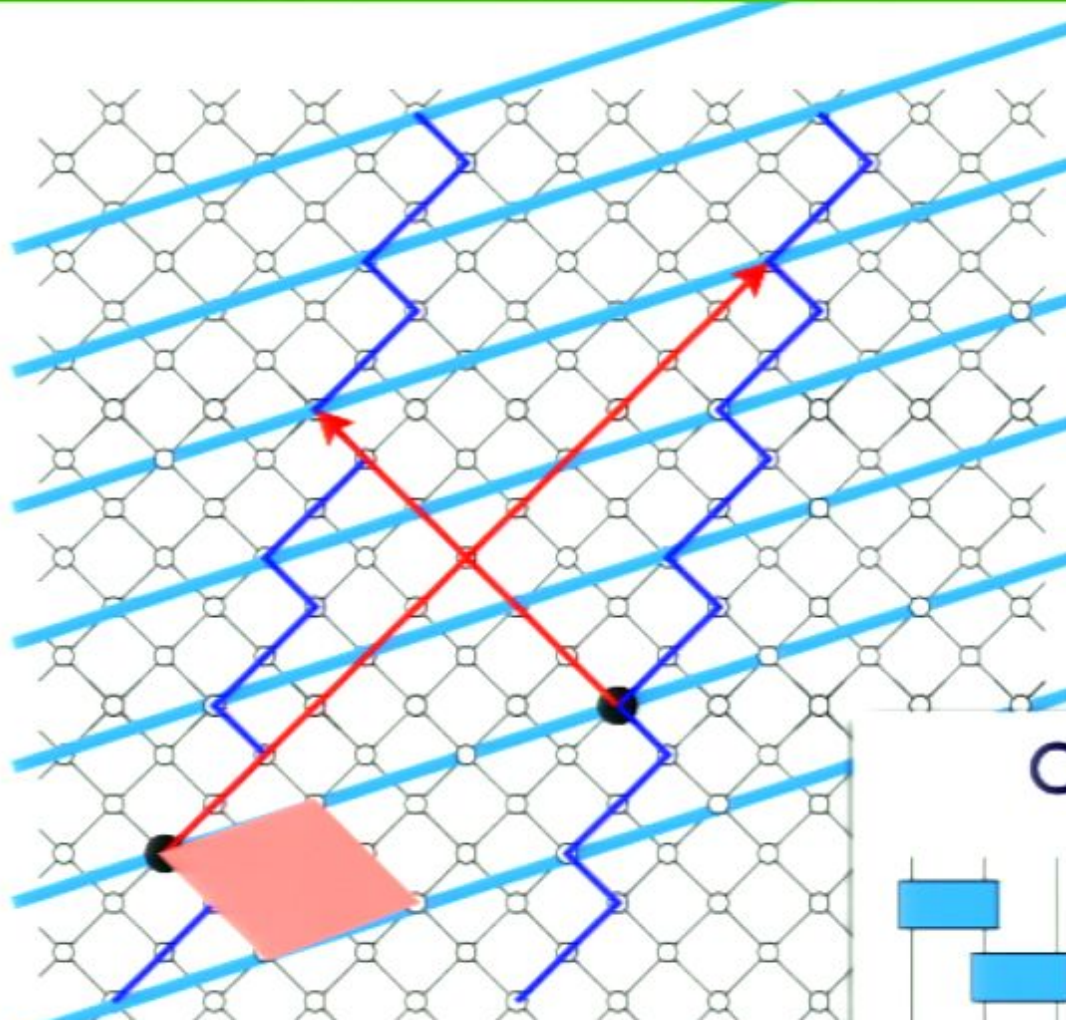
$$a \sim_0 b \Leftrightarrow \inf |O_a(a, b^*)|_{\pm} = \inf |O_b(b, a^*)|_{\pm}.$$





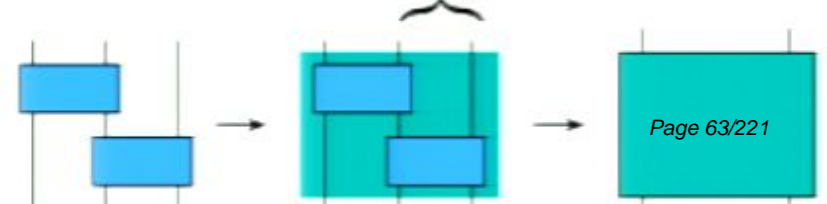
# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805



foliation

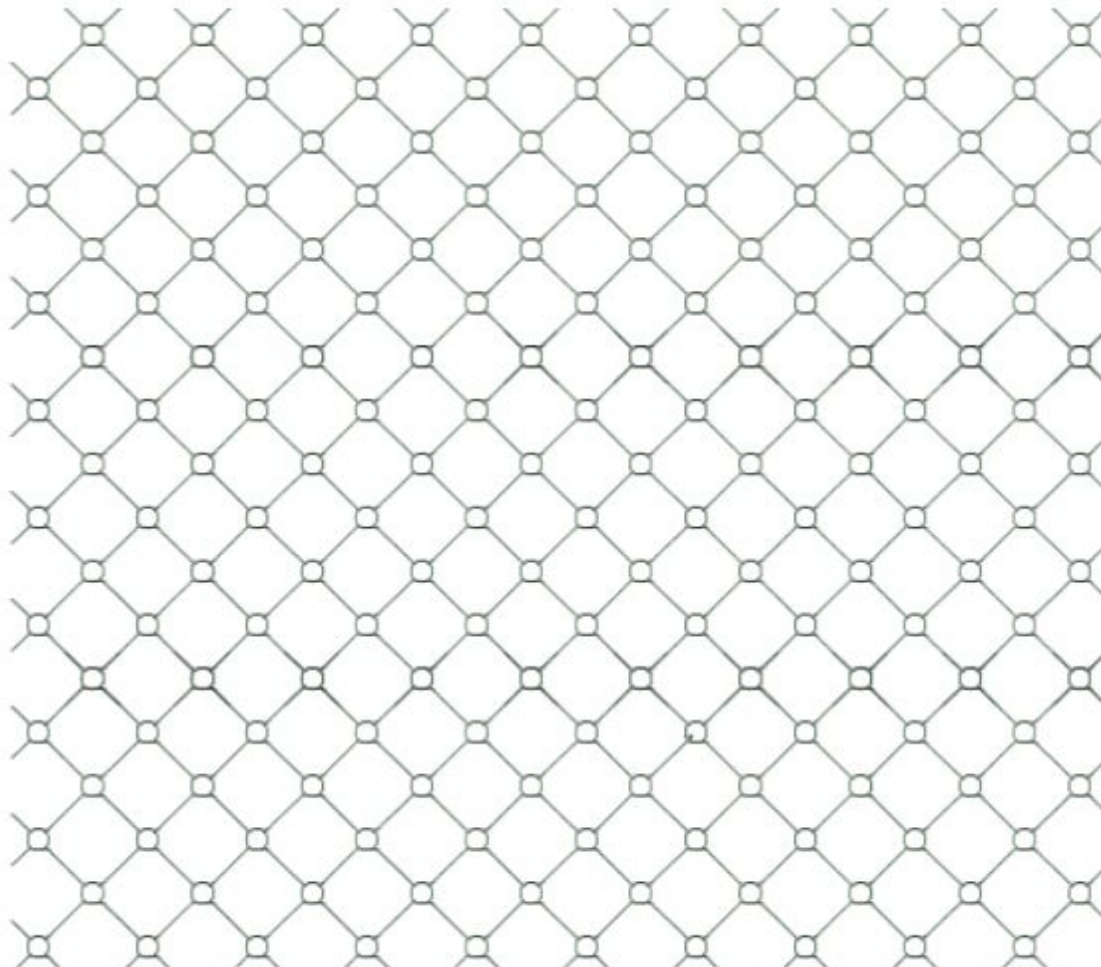
### Coarse-graining





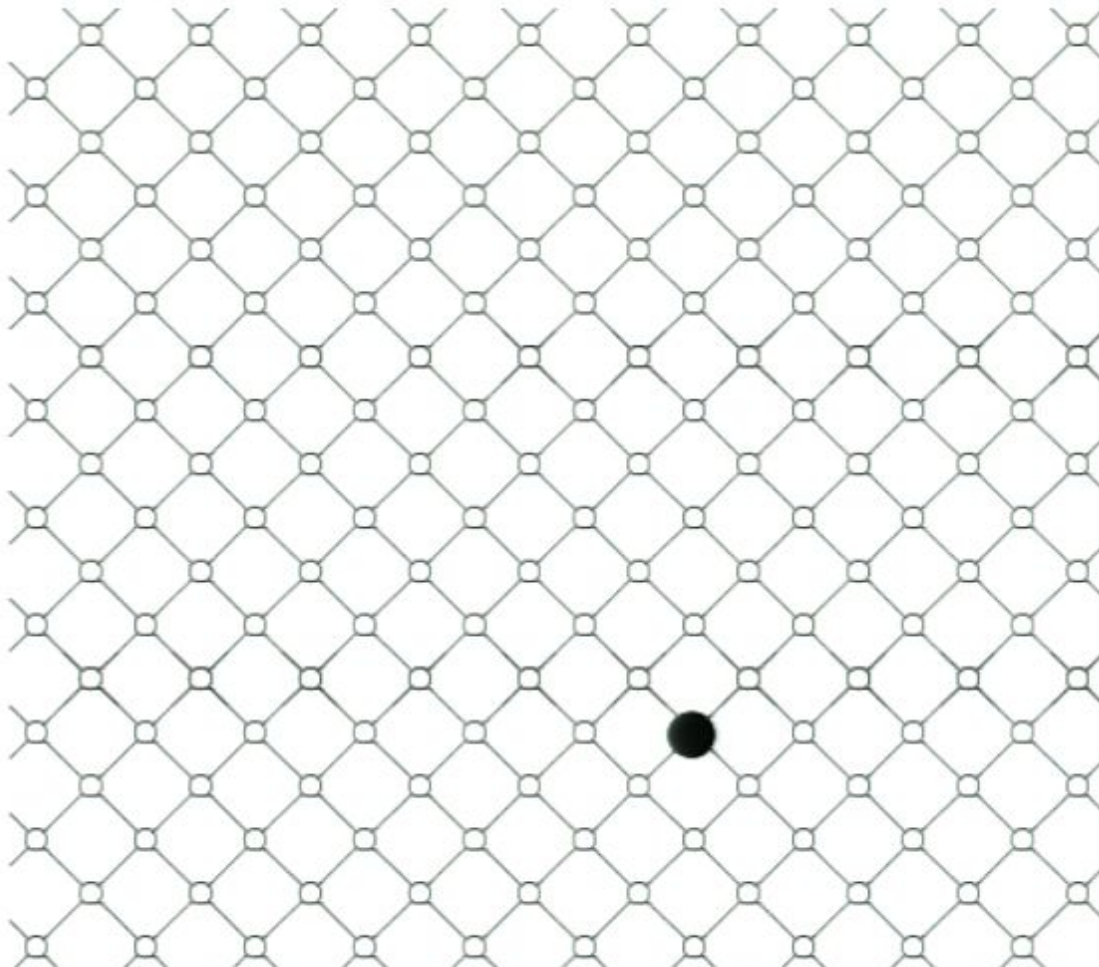
# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805



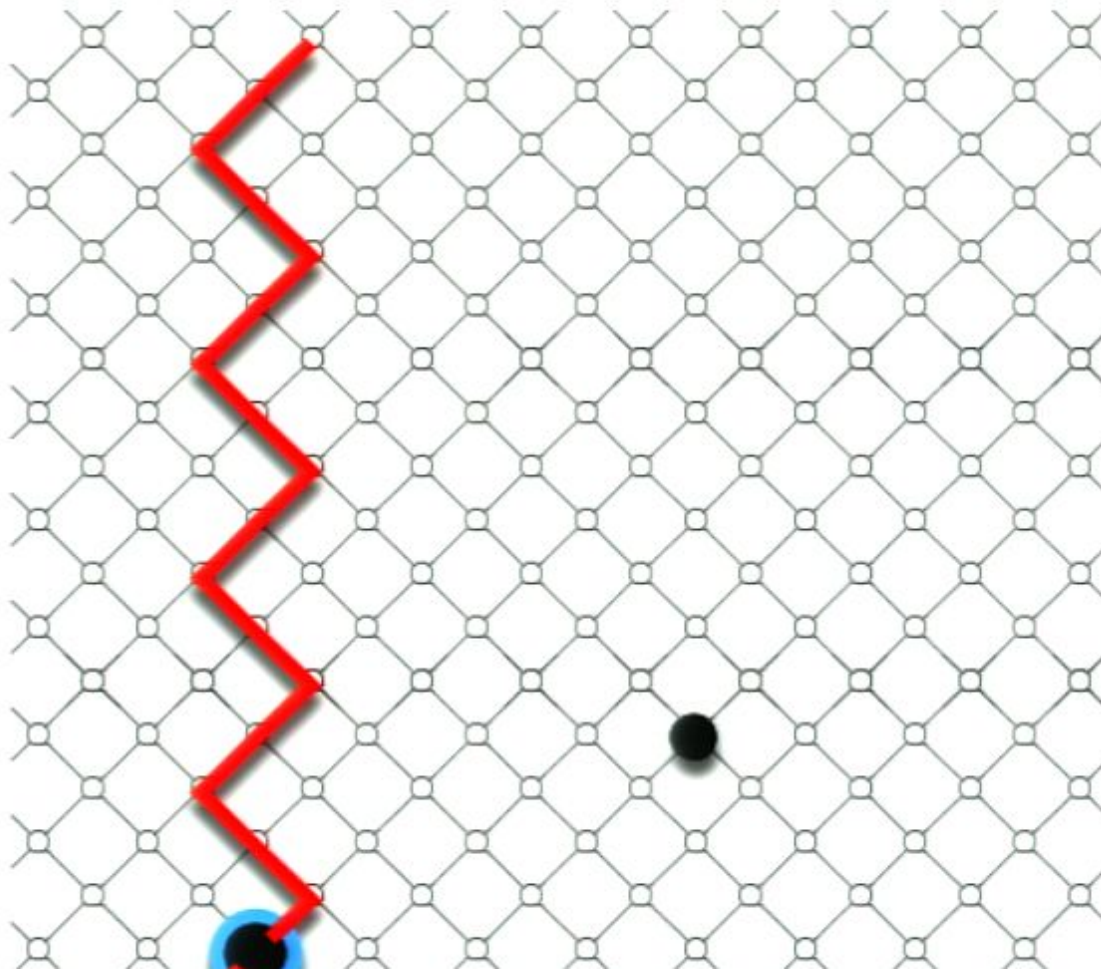
# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805



# Lorentz transformations from causality and topological homogeneity

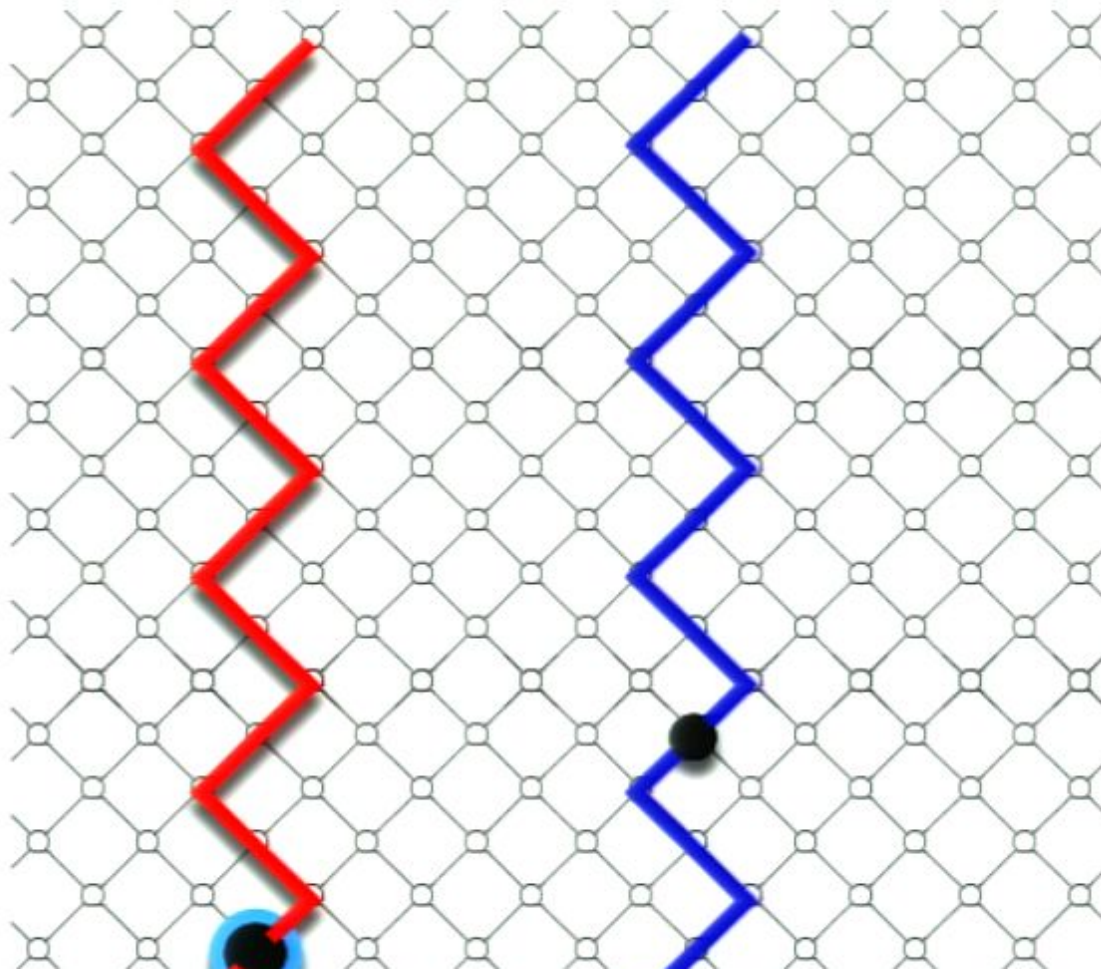
GMD and  
A. Tosini  
1008.4805





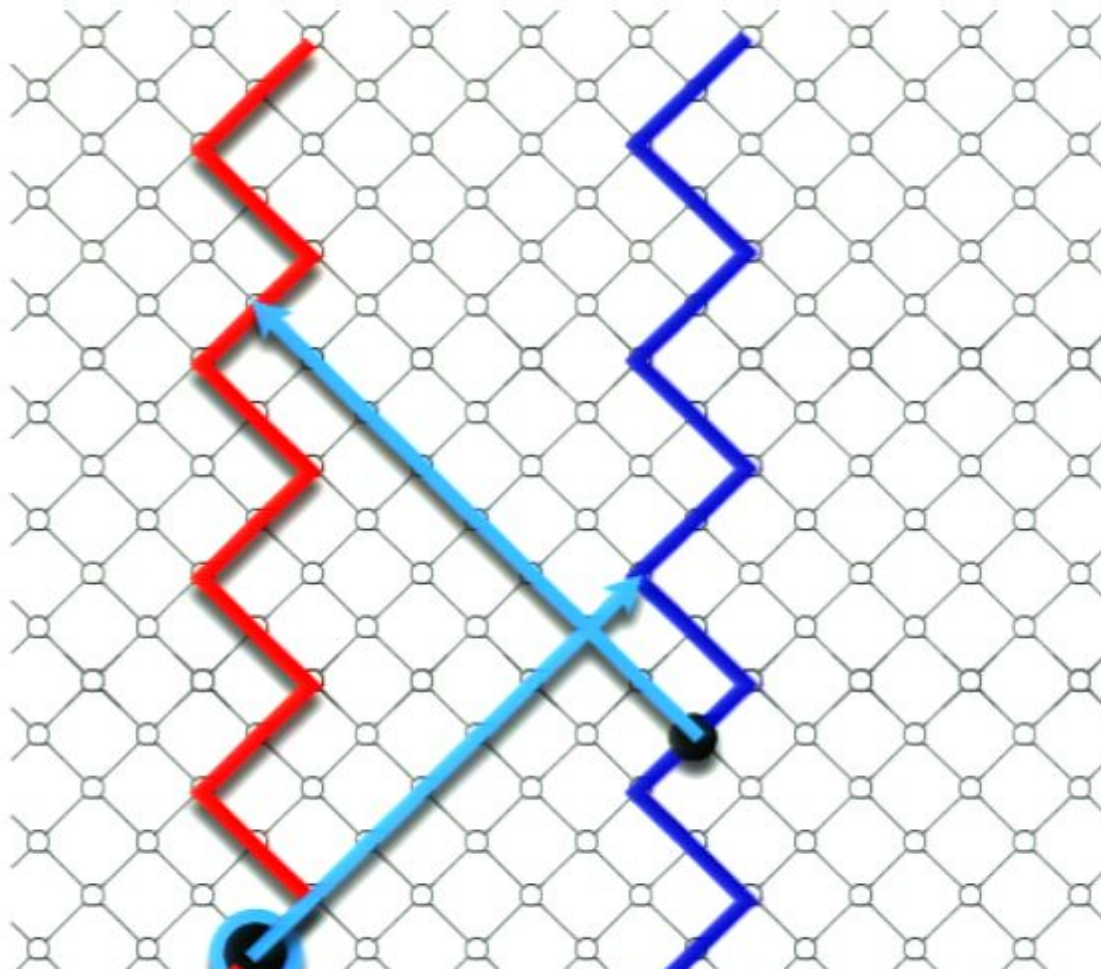
# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805



# Lorentz transformations from causality and topological homogeneity

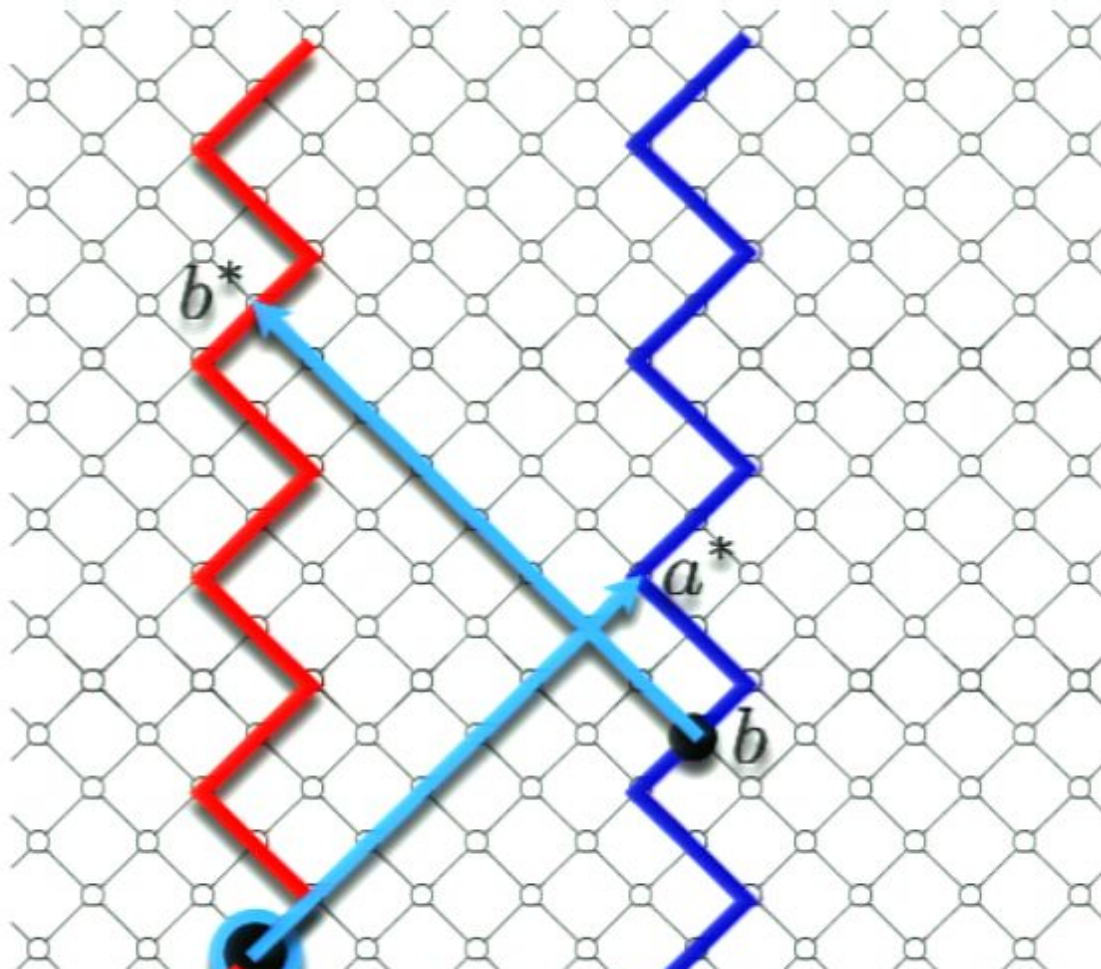
GMD and  
A. Tosini  
1008.4805





# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805





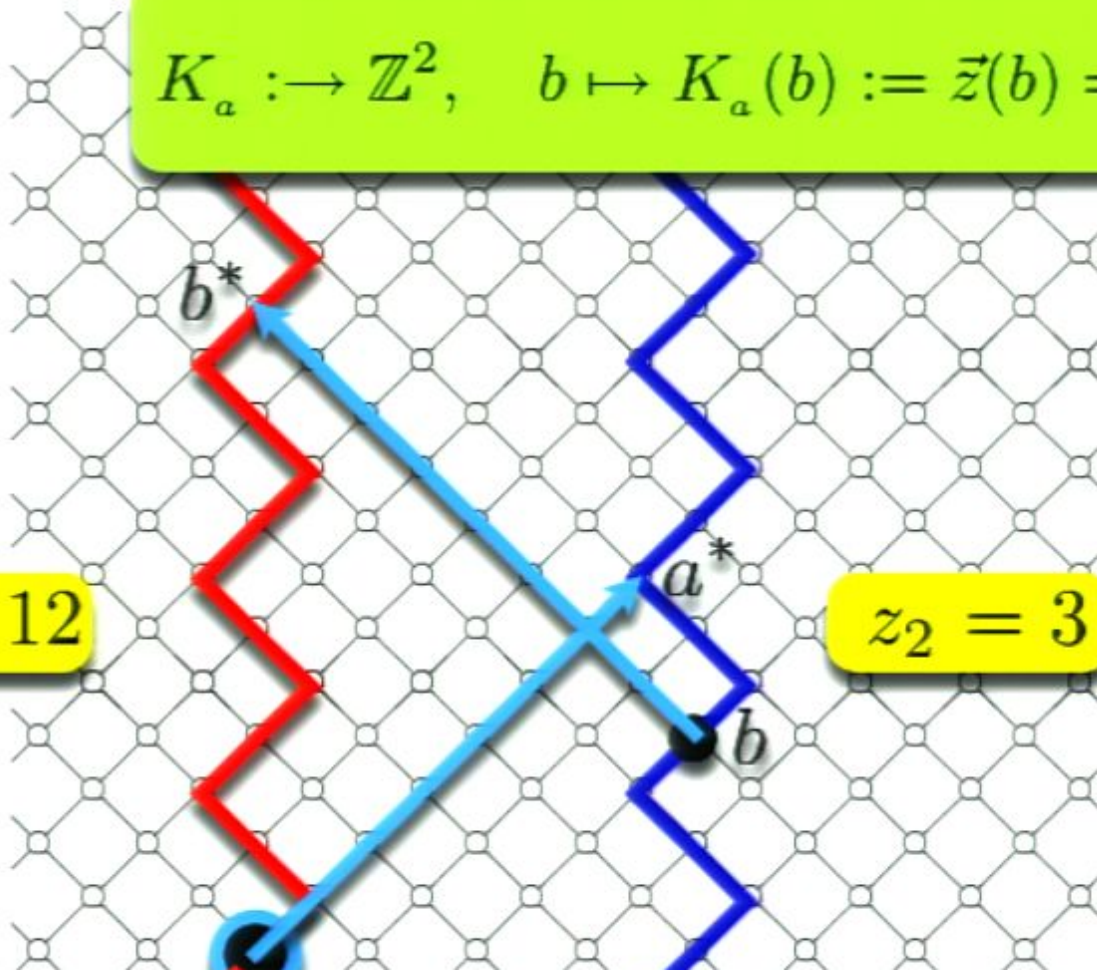
# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

$$K_a : \rightarrow \mathbb{Z}^2, \quad b \mapsto K_a(b) := \vec{z}(b) = \begin{bmatrix} z_1(b) \\ z_2(b) \end{bmatrix}$$

$$z_1 = 12$$

$$z_2 = 3$$



Coordinates

# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

**Lemma 1** *An event  $b \in \mathcal{L}(\mathcal{O}_a)$  belongs to the  $t$ -th leaf  $\mathcal{L}_t(\mathcal{O}_a)$  for  $t = (z_1 - z_2)/2$ , and the number of events on such leaf between  $b$  and  $\mathcal{O}_a$  is given by  $s = (z_1 + z_2)/2$ .*

According to the last Lemma the coordinates

$$\begin{bmatrix} t(b) \\ s(b) \end{bmatrix} := 2^{\frac{1}{2}} \mathbf{U}(\pi/4) \begin{bmatrix} z(b) \\ z(b) \end{bmatrix}, \quad (10)$$

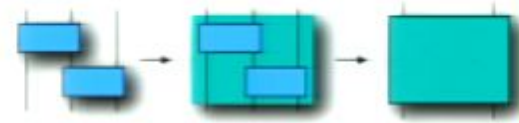
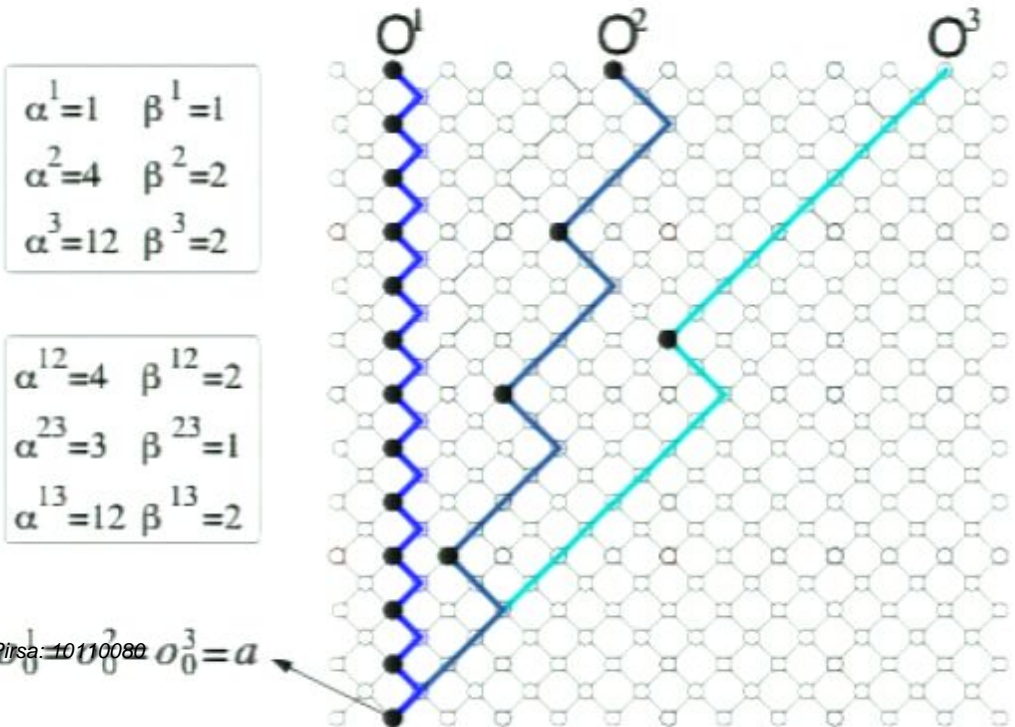
where  $\mathbf{U}(\theta)$  is the matrix performing a  $\theta$ -rotation, can be interpreted as the space-time coordinates of the event  $b$  in the frame  $\mathcal{L}(\mathcal{O}_a)$ .

Coordinates



Frames in standard configuration (boosted). Consider now two observers  $O_a^1 = \{o_i^1\}$  and  $O_a^2 = \{o_j^2\}$  sharing the same origin (homogeneity guarantees the existence of observers sharing the origin). We will shortly denote the two frames as  $\mathfrak{R}^1$  and  $\mathfrak{R}^2$ , and the corresponding coordinate maps as  $K^1$  and  $K^2$ . We will say that the two frames  $\mathfrak{R}^1$  and  $\mathfrak{R}^2$  are in *standard configuration* if there exist positive  $\alpha^{12}, \beta^{12}$ , such that  $\forall i \in \mathbb{Z}$

$$K^1(o_i^2) = \mathbf{D}^{12} K^2(o_i^2), \quad \mathbf{D}^{12} := \text{diag}(\alpha^{12}, \beta^{12}). \quad (11)$$



$$v^{12} = \frac{\alpha^{12} - \beta^{12}}{\alpha^{12} + \beta^{12}}$$

Boosts



# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

$$\rightarrow v^{13} = \frac{\alpha^{12}\alpha^{23} - \beta^{12}\beta^{23}}{\alpha^{12}\alpha^{23} + \beta^{12}\beta^{23}} = \frac{v_{12} + v_{23}}{1 + v_{12}v_{23}}$$

Coordinates

# Lorentz transformations from causality and topological homogeneity

GMD and  
A. Tosini  
1008.4805

$$\rightarrow v^{13} = \frac{\alpha^{12}\alpha^{23} - \beta^{12}\beta^{23}}{\alpha^{12}\alpha^{23} + \beta^{12}\beta^{23}} = \frac{v_{12} + v_{23}}{1 + v_{12}v_{23}}$$



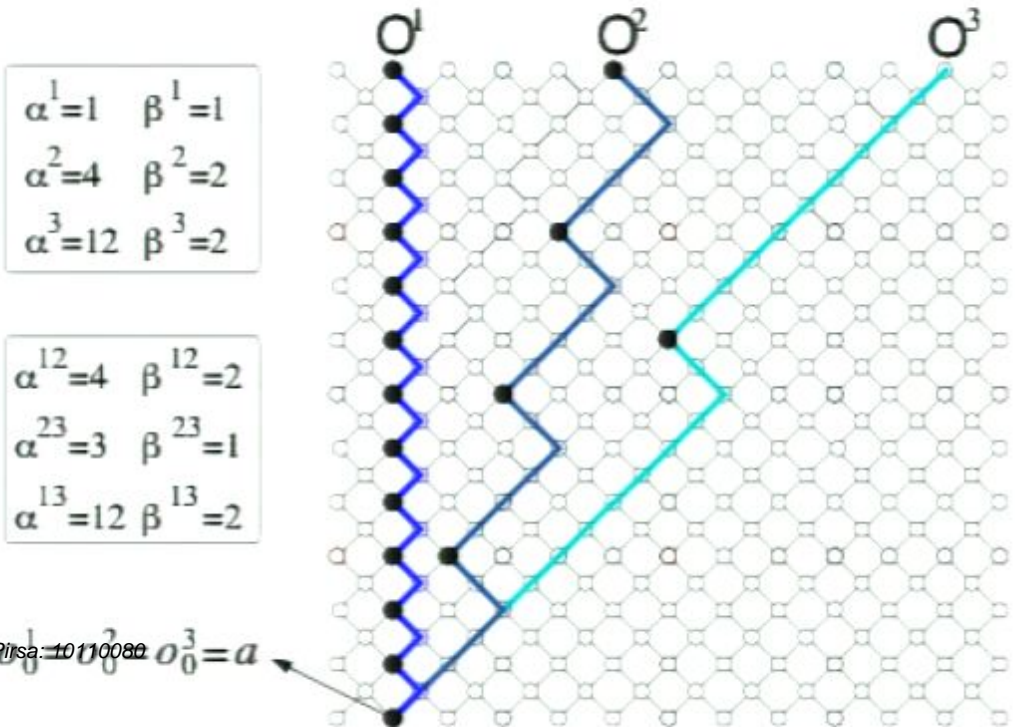
$$t^1 = \chi_{12} \frac{t^2 + v^{12}s^2}{\sqrt{1 - (v^{12})^2}}, \quad s^1 = \chi_{12} \frac{s^2 + v^{12}t^2}{\sqrt{1 - (v^{12})^2}},$$

$$\chi_{12} := \sqrt{\alpha^{12}\beta^{12}}$$

which differ from the Lorentz transformations only by the multiplicative factor  $\chi_{12}$ . The factor  $\chi_{12}$  can be removed by rescaling the coordinate map in Eq. (10) using the

Frames in standard configuration (boosted). Consider now two observers  $O_a^1 = \{o_i^1\}$  and  $O_a^2 = \{o_j^2\}$  sharing the same origin (homogeneity guarantees the existence of observers sharing the origin). We will shortly denote the two frames as  $\mathfrak{R}^1$  and  $\mathfrak{R}^2$ , and the corresponding coordinate maps as  $K^1$  and  $K^2$ . We will say that the two frames  $\mathfrak{R}^1$  and  $\mathfrak{R}^2$  are in *standard configuration* if there exist positive  $\alpha^{12}, \beta^{12}$ , such that  $\forall i \in \mathbb{Z}$

$$K^1(o_i^2) = \mathbf{D}^{12} K^2(o_i^2), \quad \mathbf{D}^{12} := \text{diag}(\alpha^{12}, \beta^{12}). \quad (11)$$



$$v^{12} = \frac{\alpha^{12} - \beta^{12}}{\alpha^{12} + \beta^{12}}$$

Boosts

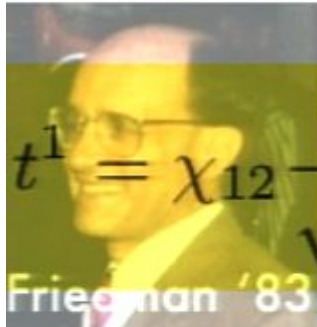


# Lorentz transformations from causality and topological homogeneity, ...

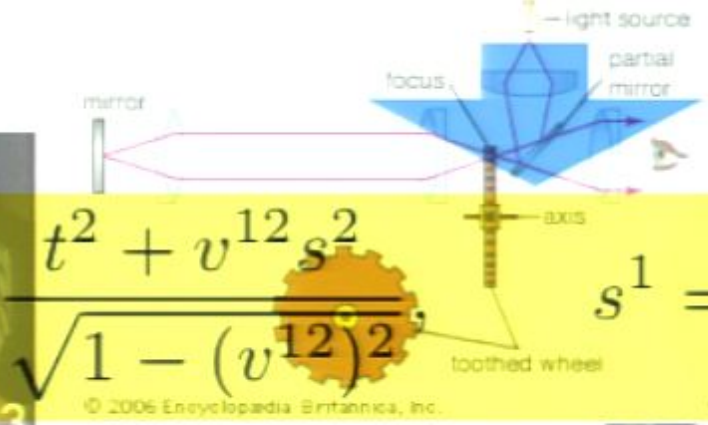
GMD and  
A. Tosini  
1008.4805

The causal network manifests the **conventionality of simultaneity**.

$$v_{13} = \frac{\alpha^{12}\alpha^{23} - \beta^{12}\beta^{23}}{\alpha^{12}\alpha^{23} + \beta^{12}\beta^{23}} = \frac{v_{12} + v_{23}}{1 + v_{12}v_{23}}$$



$$t^1 = \chi_{12} \frac{t^2 + v^{12}s^2}{\sqrt{1 - (v^{12})^2}}$$



To determine simultaneity of distant events we need to know a speed, to measure a speed we need to know simultaneity of different events'... We can only determine the two-way average speed of light ...

Come on  $\chi_{12} := \sqrt{\alpha^{12}\beta^{12}}$

which differ from the Lorentz transformations only by the multiplicative factor  $\chi_{12}$ . The factor  $\chi_{12}$  can be removed by rescaling the coordinate map in Eq. (10) using the

Coordinates

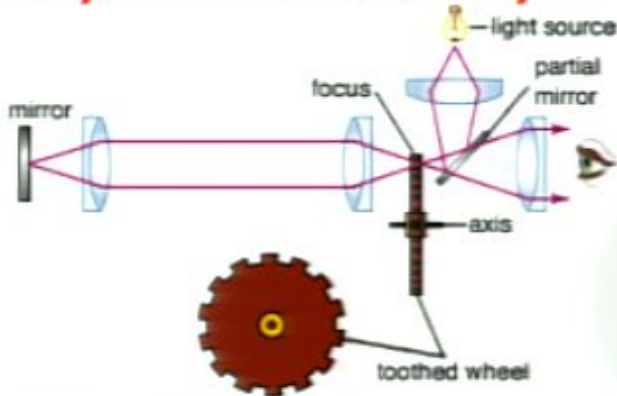
# Conventionality of simultaneity, homogeneity, ...



The causal network manifests the *conventionality of simultaneity*.

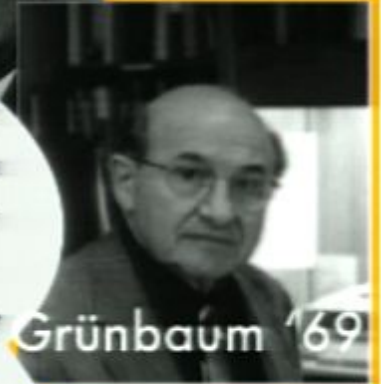


Bridgman '62



© 2006 Encyclopædia Britannica, Inc.

To determine simultaneity of distant events we need to know a speed, to measure a speed we need to know simultaneity of different events ... We can only determine the two-way average speed of light ...



Grünbaum '69



Friedman '83



Pensa: 10110080



Page 77/221





---

---

# SPECIAL RELATIVITY WITHOUT SPACE: OTHER IDEAS

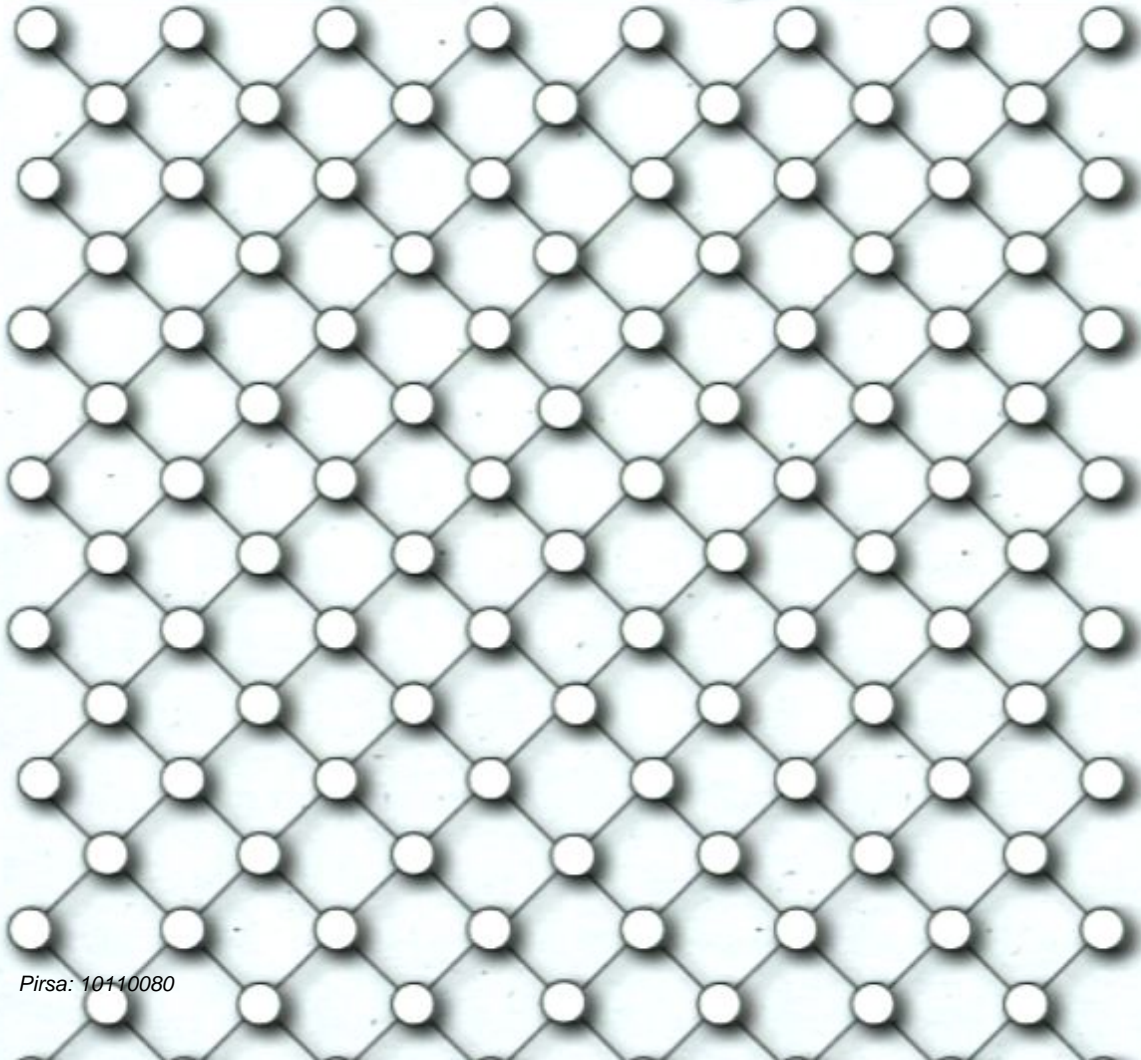
---

---



# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein, SLAC)

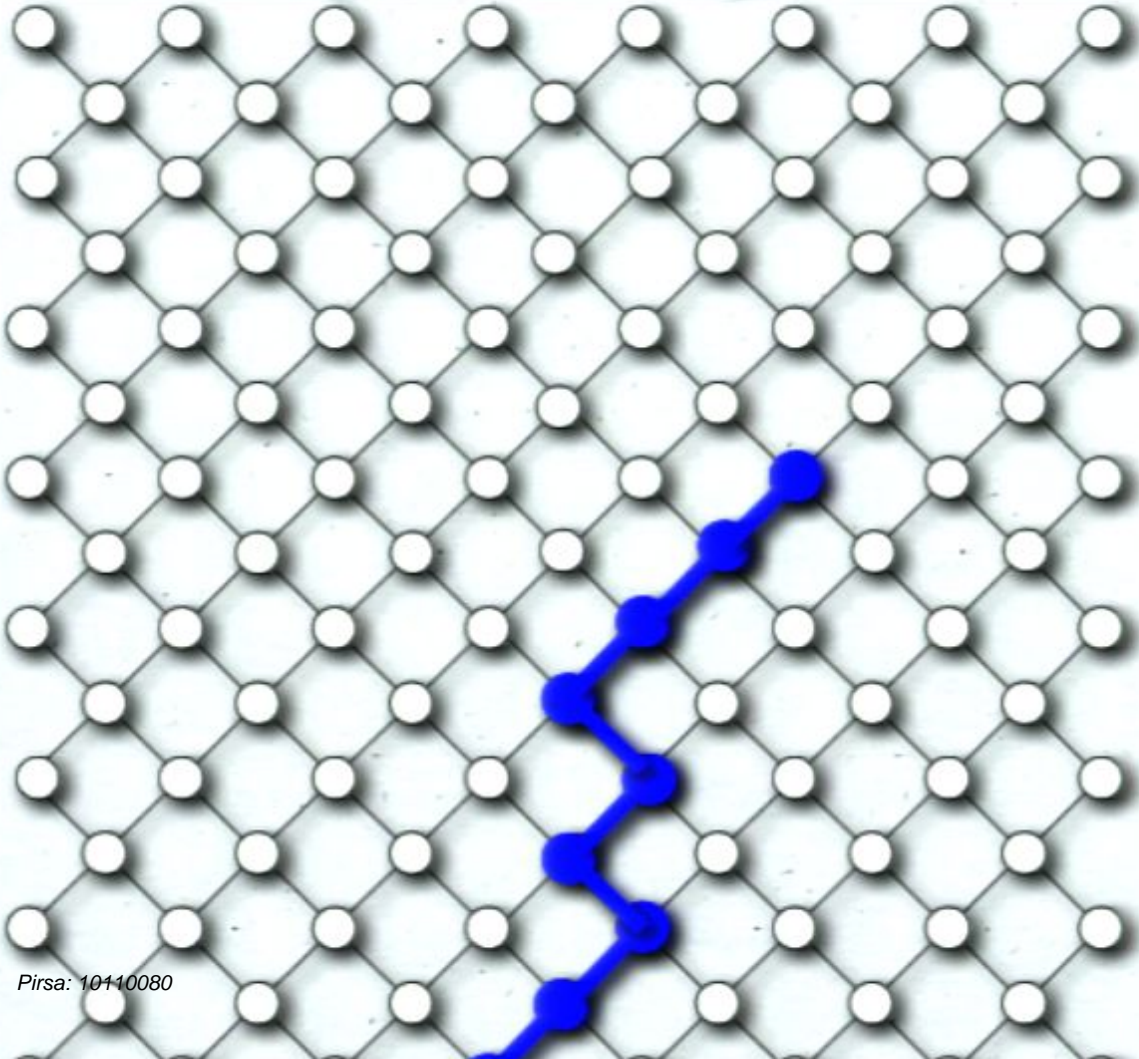


# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein, SLAC)

★ ★ ★ ★

★ ★ ★ ★



+ + - + - + + +

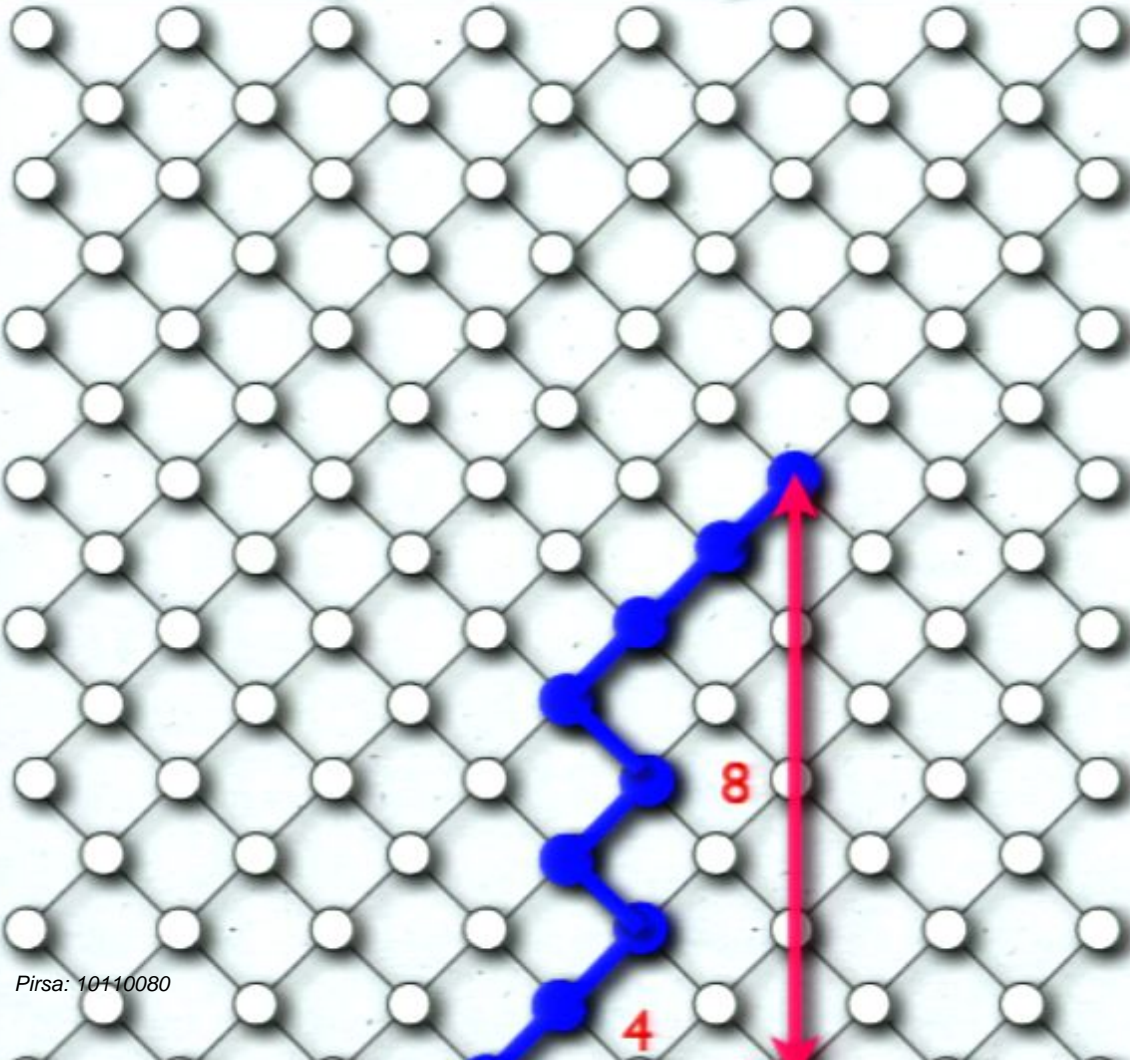


# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein, SLAC)

★★★★

★★★★



++-++

$$p = \frac{3}{4} \quad q = \frac{1}{4}$$

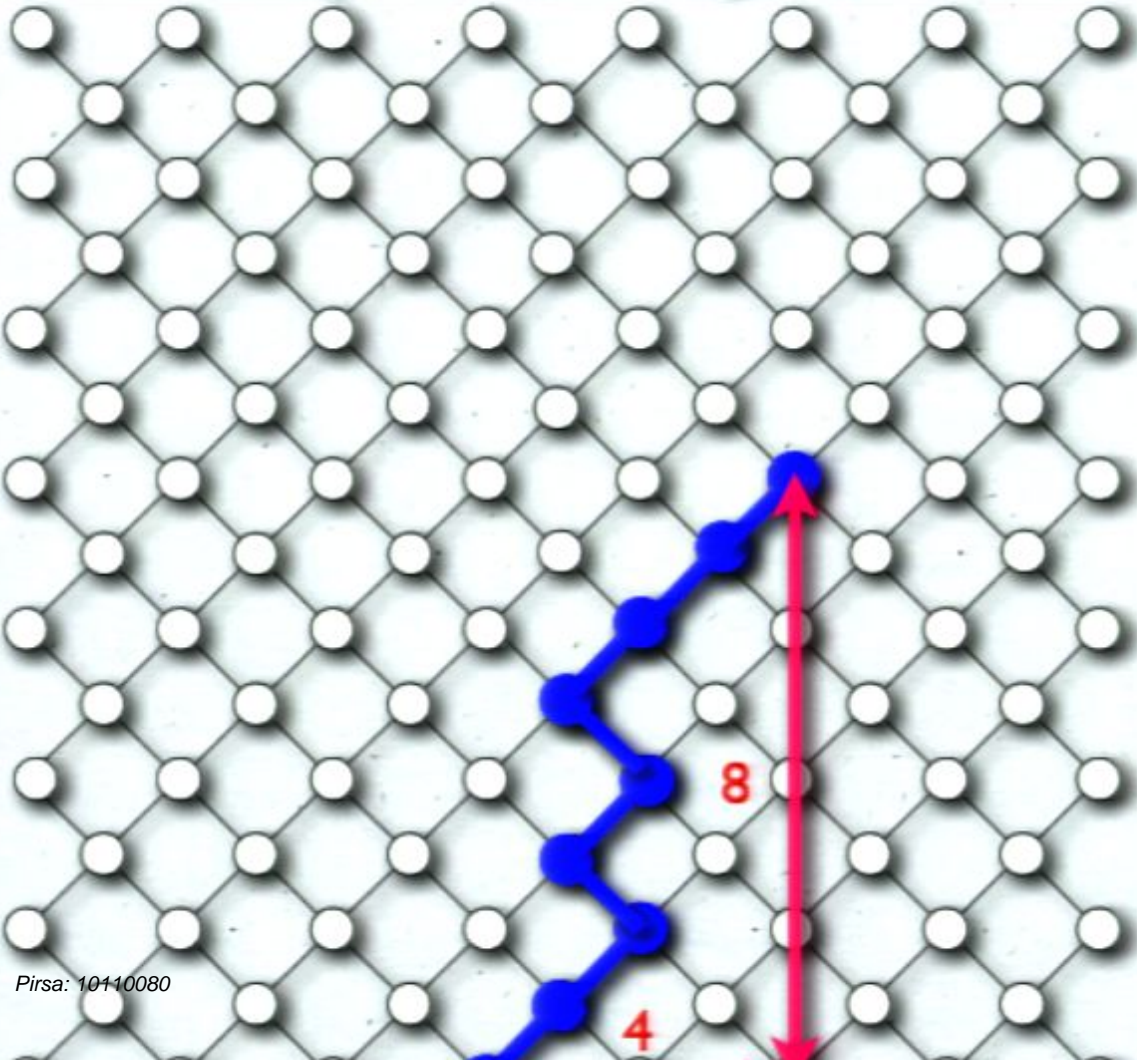
Average velocity:

$$v = p - q = \frac{1}{2}$$



# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein, SLAC)



++-++

$$p = \frac{3}{4} \quad q = \frac{1}{4}$$

Average velocity:

$$v = p - q = \frac{1}{2}$$

---

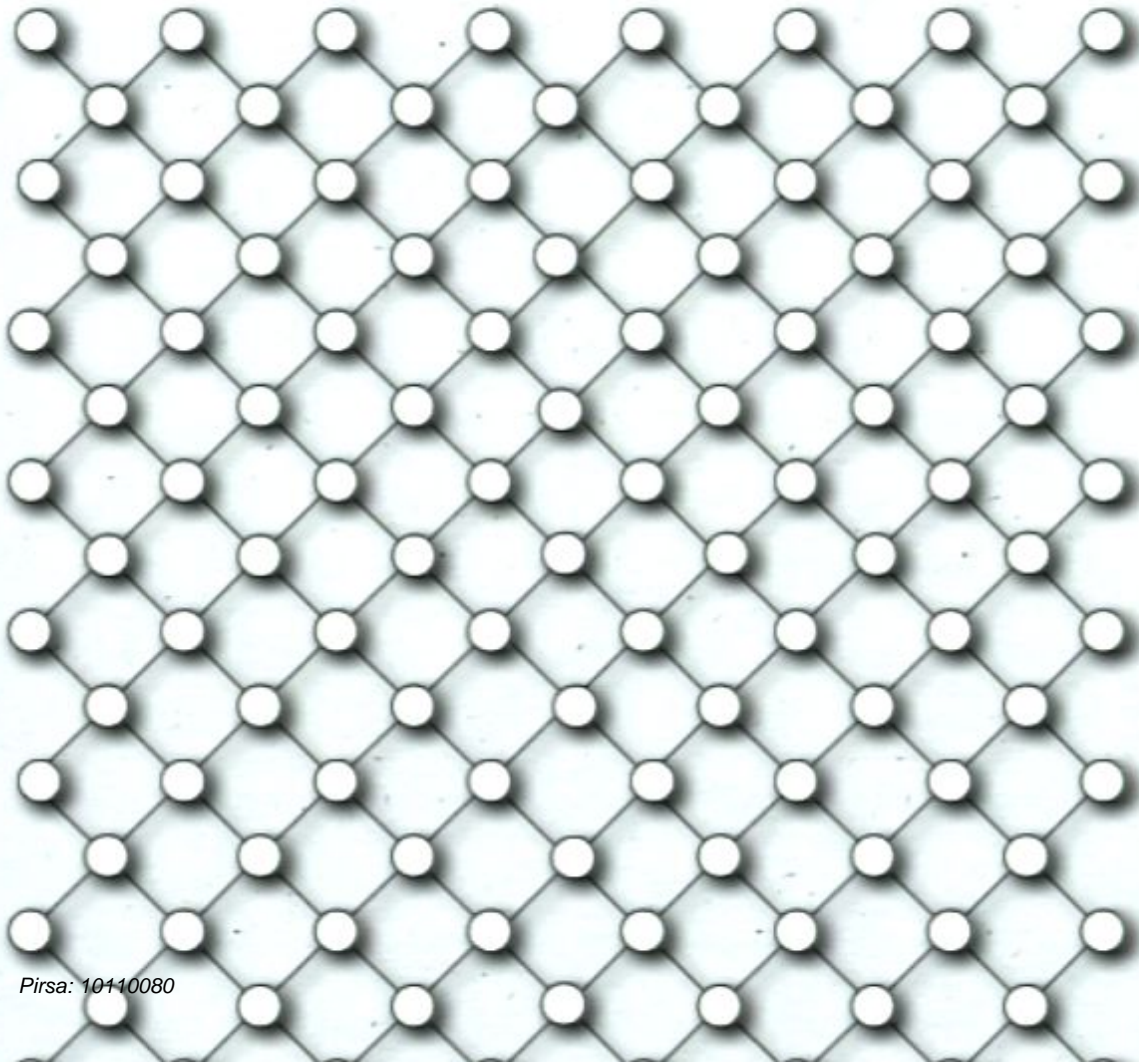
---

# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

★ ★ ★ ★

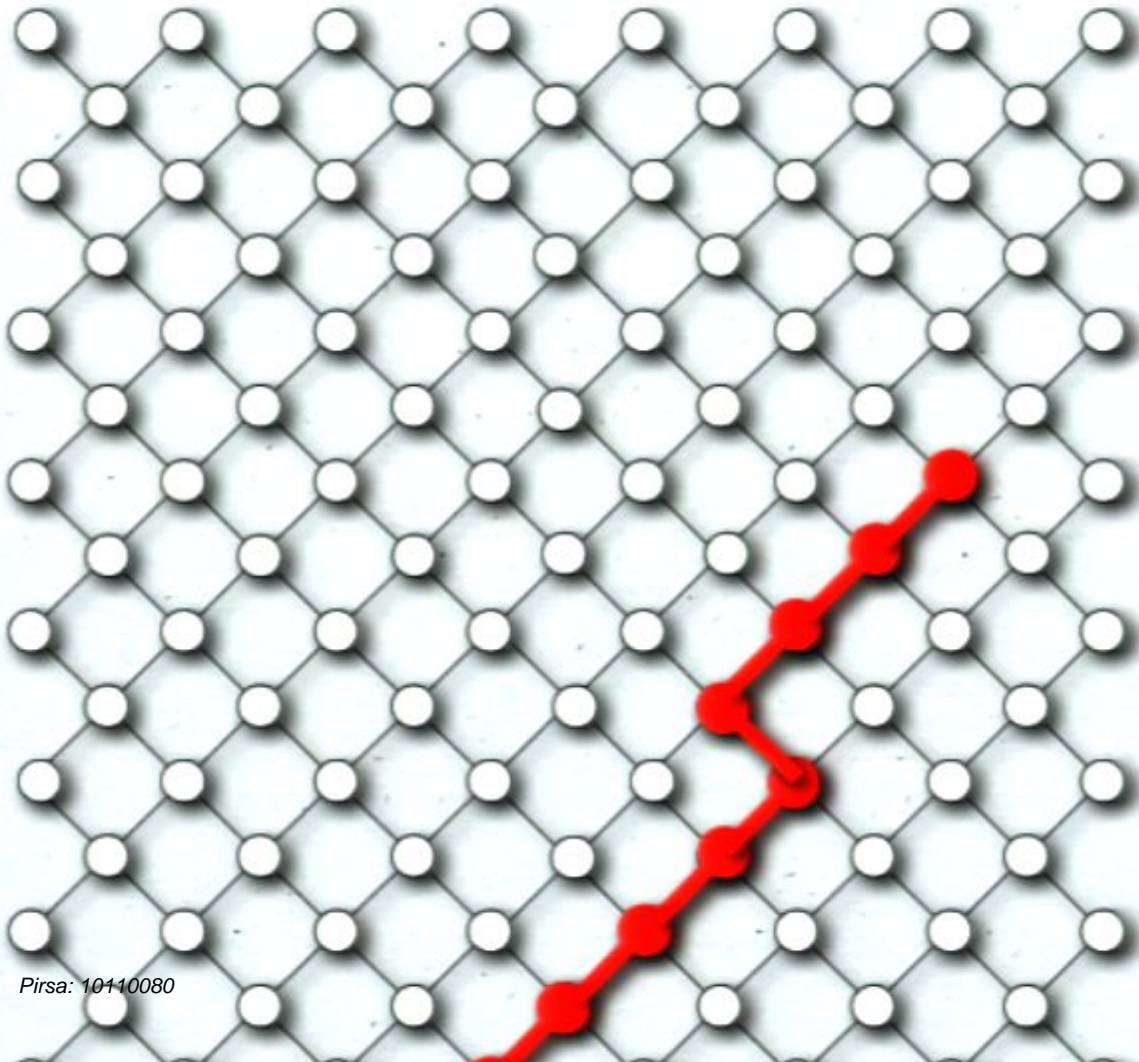
★ ★ ★ ★





# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)



+ + + + - + +

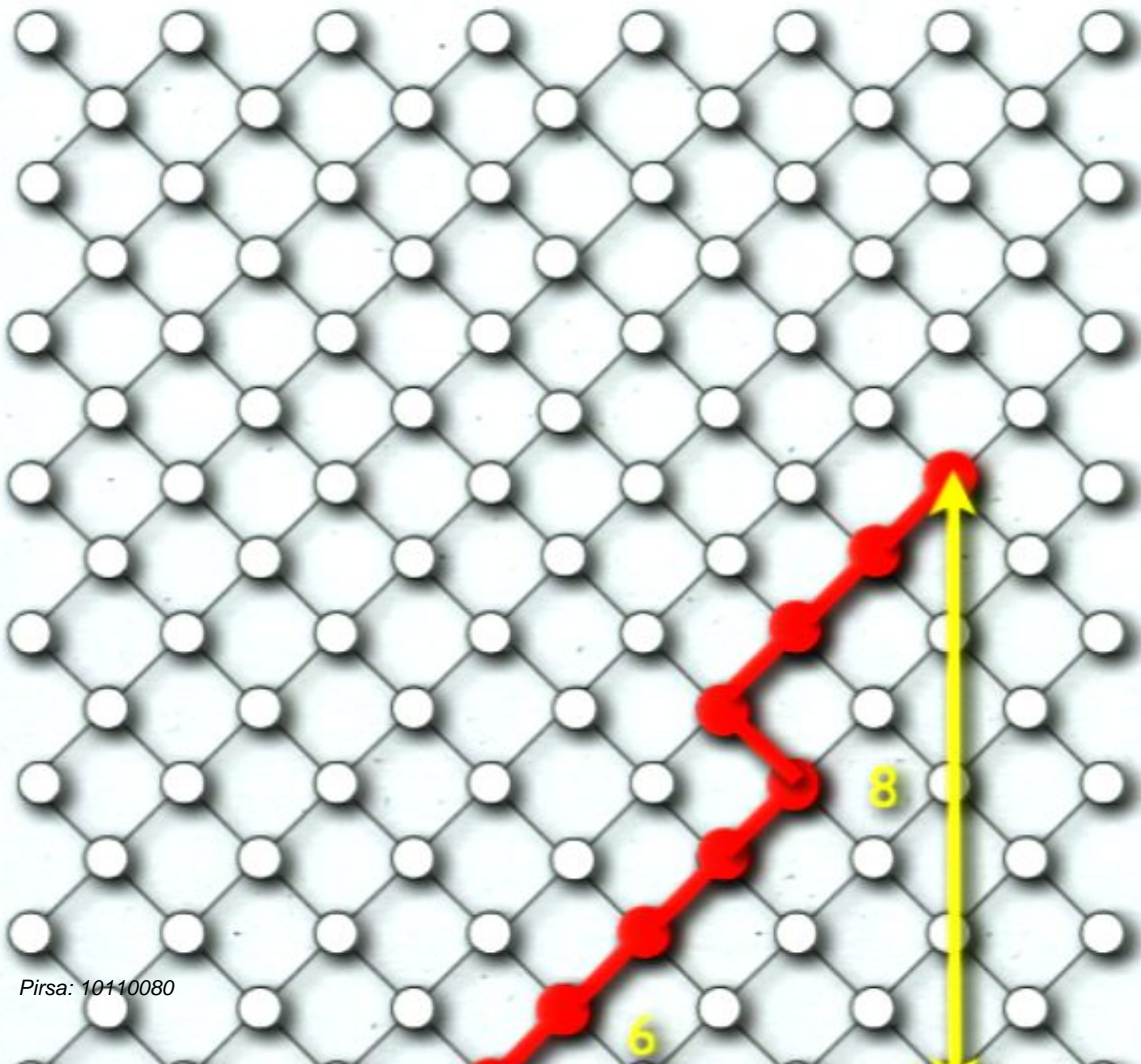


# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

★★★★

★★★★



++++-++++

$$p = \frac{7}{8} \quad q = \frac{1}{8}$$

Average velocity:

$$v = p - q = \frac{3}{4}$$



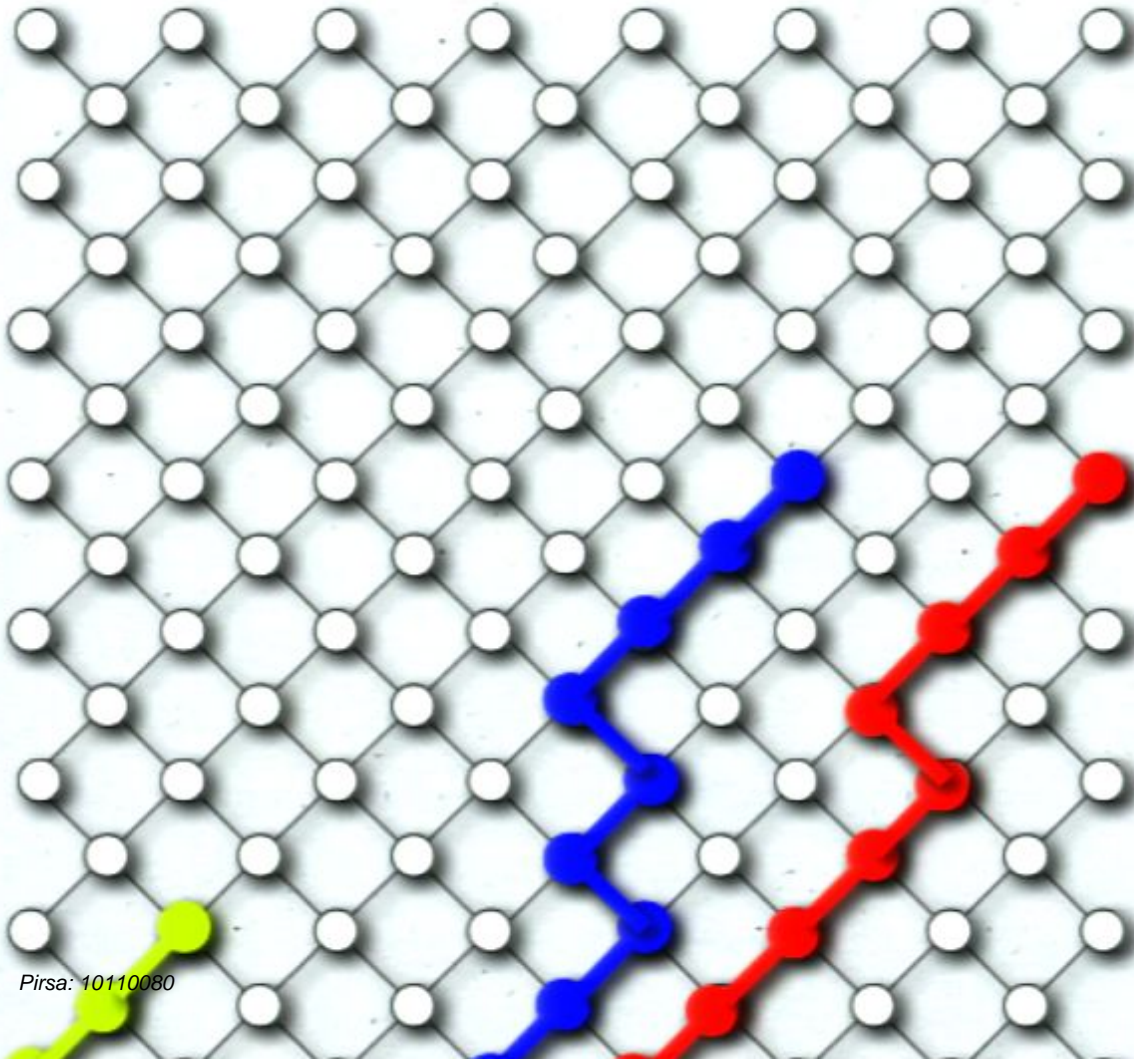


# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

★★★★

★★★★



++-+-+++

++++-++++

$$v_{12} = v_1 + v_2 = \frac{5}{4}$$

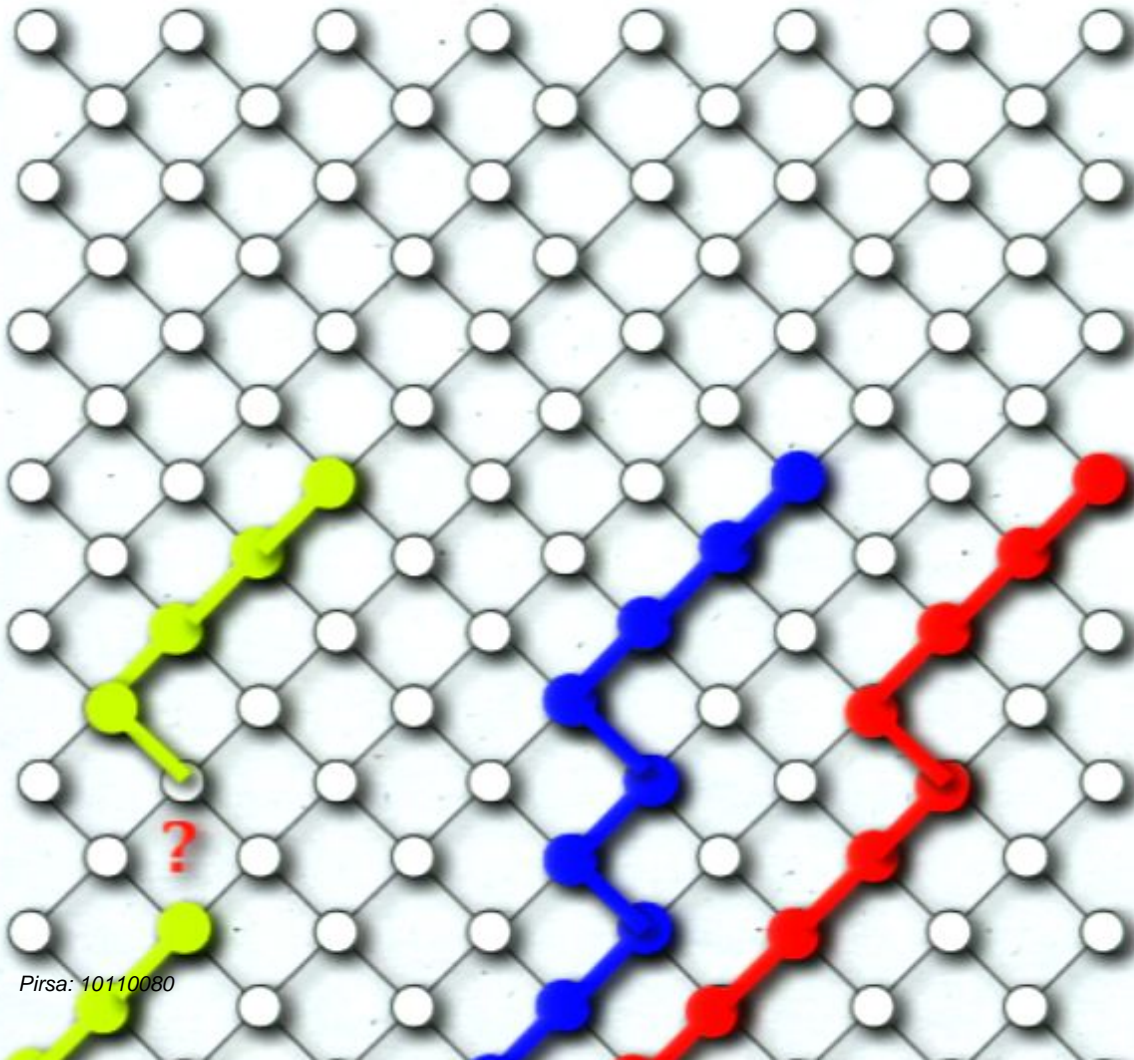


# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

★★★★

★★★★



+ + - + - + + +

+ + + + - + + +

.....

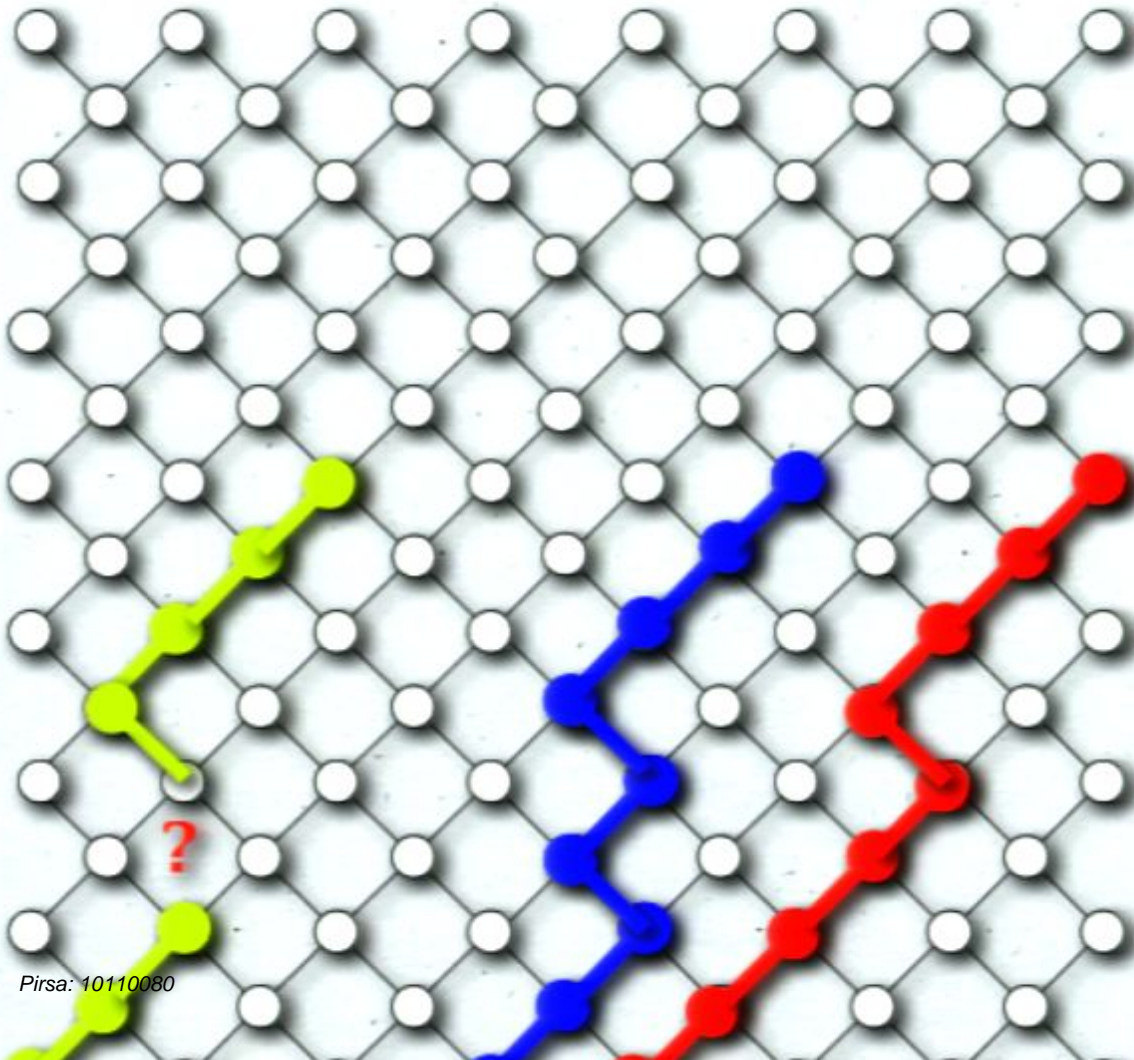
$$v_{12} = v_1 + v_2 = \frac{5}{4}$$

# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

★★★★

★★★★



+ + - + - + + +

+ + + + - + + +

+ + + - + + +

$$v_{12} = v_1 + v_2 = \frac{5}{4}$$

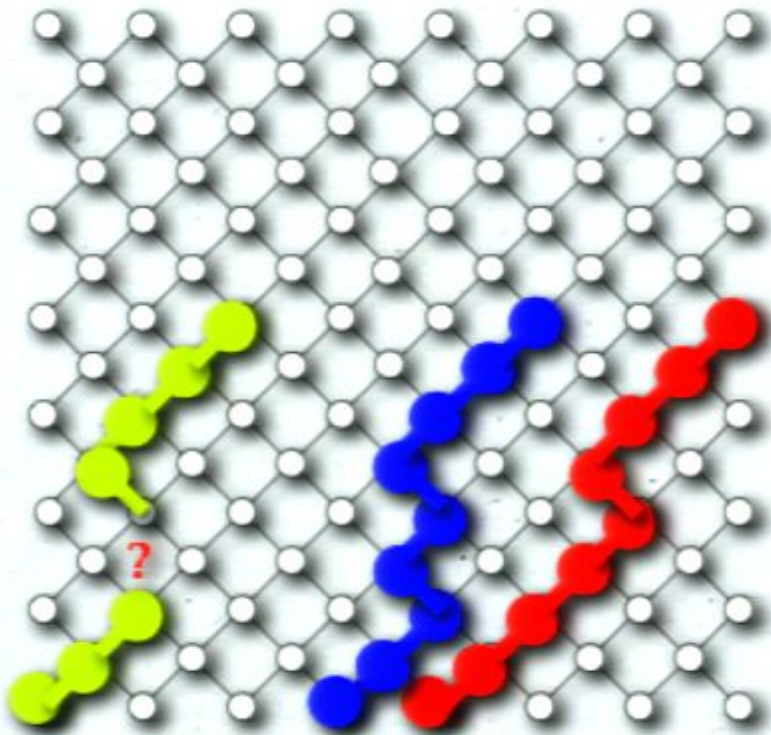


# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

★★★★

★★★★

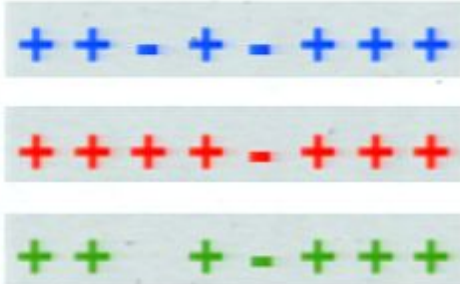
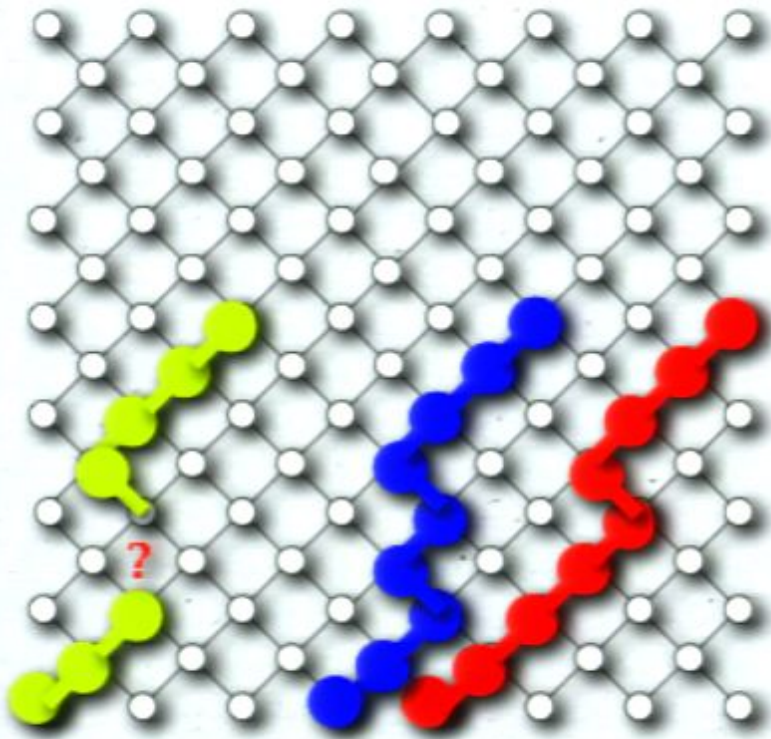


++-+-+++  
++++-+++  
++ +-++++



# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)

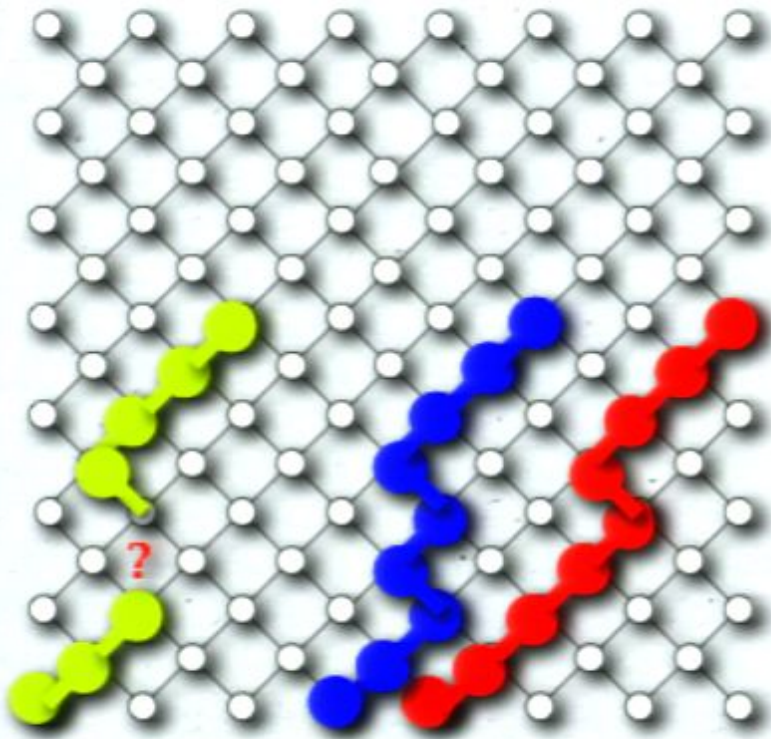


$$p_{12} = \frac{p_1 p_2}{p_1 p_2 + q_1 q_2}$$

$$q_{12} = \frac{q_1 q_2}{p_1 p_2 + q_1 q_2}$$

# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)



++-+-+++  
 ++++--+++  
 ++ +-+++

$$p_{12} = \frac{p_1 p_2}{p_1 p_2 + q_1 q_2}$$

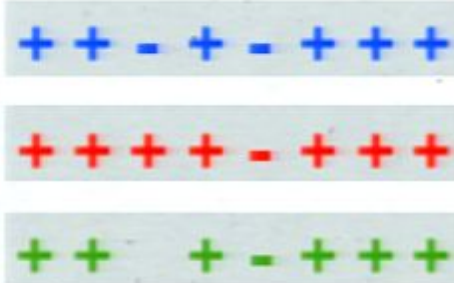
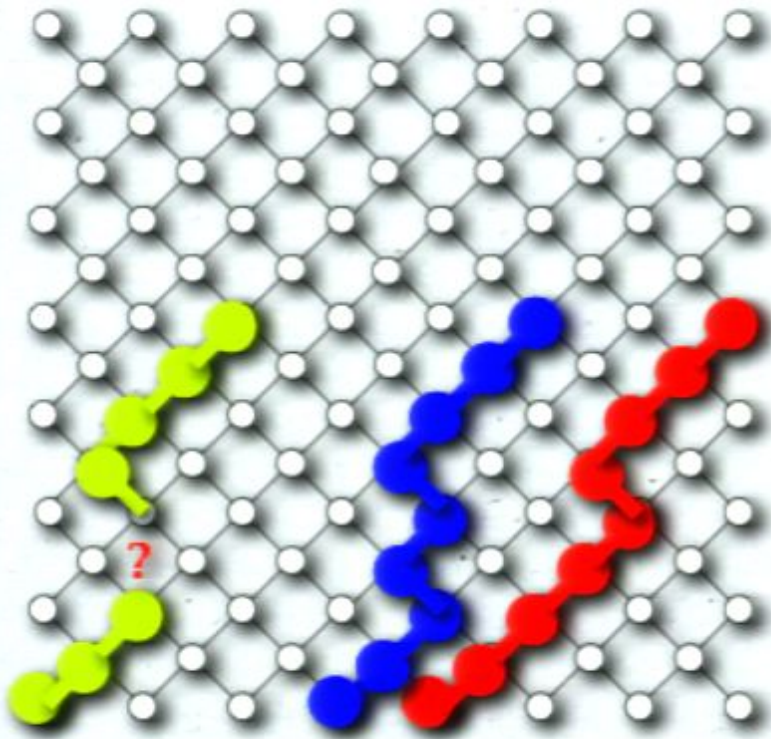
$$q_{12} = \frac{q_1 q_2}{p_1 p_2 + q_1 q_2}$$

$$v_{12} = p_{12} - q_{12} = \frac{p_1 p_2 - q_1 q_2}{p_1 p_2 + q_1 q_2}$$



# SPECIAL RELATIVITY FROM RANDOMNESS

(from Irving Stein)



$$p_{12} = \frac{p_1 p_2}{p_1 p_2 + q_1 q_2}$$

$$q_{12} = \frac{q_1 q_2}{p_1 p_2 + q_1 q_2}$$

$$v_{12} = p_{12} - q_{12} = \frac{p_1 p_2 - q_1 q_2}{p_1 p_2 + q_1 q_2}$$



$$v_{12} = \frac{v_1 + v_2}{1 + v_1 v_2}$$



---

---

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)



---

---

# SPECIAL RELATIVITY FROM RANDOMNESS

---

---

Kevin S. Brown (Kent, WA)

---

---

★ ★ ★ ★

★ ★ ★ ★

$p(v) = v^2$  a probability!

---

---

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

★★★★

★★★★

$p(v) = v^2$  a probability!

$v_x$   $v_y$  (orthogonal = independent)



---

---

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

★★★★

★★★★

$p(v) = v^2$  a probability!

$v_x$   $v_y$  (orthogonal = independent)

$$p(a \cup b) = p(a) + p(b) - p(a \cap b) = p(a) + p(b) - p(a)p(b)$$

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

$$p(v) = v^2 \quad \text{a probability!}$$

$v_x$   $v_y$  (orthogonal = independent)

$$p(a \cup b) = p(a) + p(b) - p(a \cap b) = p(a) + p(b) - p(a)p(b)$$

$$p(v_x \cup v_y) = v_x^2 + v_y^2 - v_x^2 v_y^2 \quad \text{composition of orthogonal speeds in SR!}$$

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

★★★★

★★★★

$p(v) = v^2$  a probability!

$v_x$   $v_y$  (orthogonal = independent)

$$p(a \cup b) = p(a) + p(b) - p(a \cap b) = p(a) + p(b) - p(a)p(b)$$

$$p(v_x \cup v_y) = v_x^2 + v_y^2 \quad (\text{Galileo, disjoint events})$$



# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

$$p(v) = v^2 \quad \text{a probability!}$$

$v_x$   $v_y$  (orthogonal = independent)

$$p(a \cup b) = p(a) + p(b) - p(a \cap b) = p(a) + p(b) - p(a)p(b)$$

$$p(v_x \cup v_y) = v_x^2 + v_y^2 - v_x^2 v_y^2 \quad \text{composition of orthogonal speeds in SR!}$$

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

★★★★

★★★★

$$p(v) = v^2 \quad \text{a probability!}$$

$v_x$   $v_y$  (orthogonal = independent)

$$p(a \cup b) = p(a) + p(b) - p(a \cap b) = p(a) + p(b) - p(a)p(b)$$

$$p(v_x \cup v_y) = v_x^2 + v_y^2 - v_x^2 v_y^2 \quad \text{composition of orthogonal speeds in SR!}$$

$$1 - p(v_x \cup v_y) = [1 - p(v_x)][1 - p(v_y)]$$

$$\overline{v_x \cup v_y} = \overline{v_x} \cap \overline{v_y}$$

*de Morgan!*

# SPECIAL RELATIVITY FROM RANDOMNESS

Kevin S. Brown (Kent, WA)

★★★★

★★★★

$$p(v) = v^2 \quad \text{a probability!}$$

$v_x$   $v_y$  (orthogonal = independent)

$$p(a \cup b) = p(a) + p(b) - p(a \cap b) = p(a) + p(b) - p(a)p(b)$$

$$p(v_x \cup v_y) = v_x^2 + v_y^2 - v_x^2 v_y^2 \quad \text{composition of orthogonal speeds in SR!}$$

$$1 - p(v_x \cup v_y) = [1 - p(v_x)][1 - p(v_y)]$$

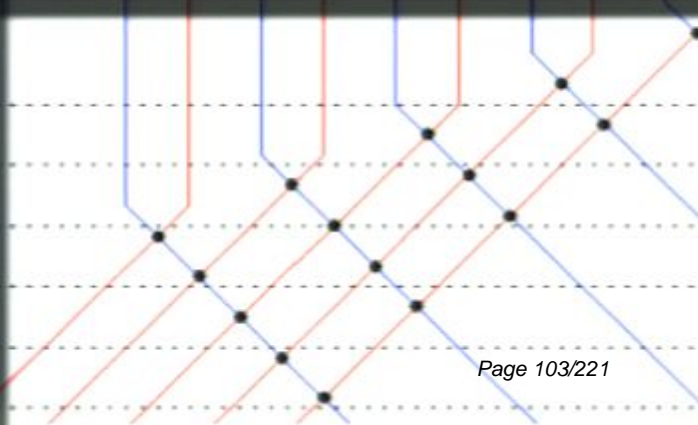
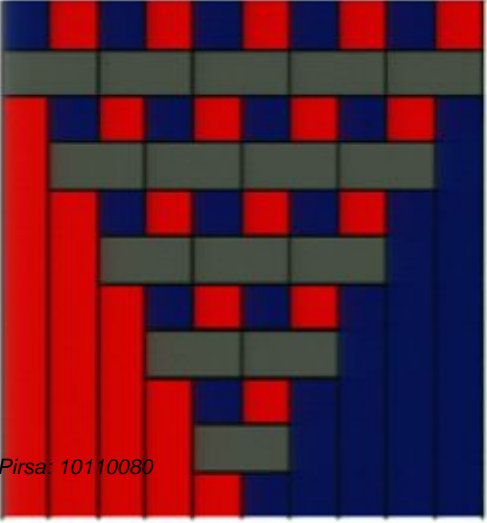
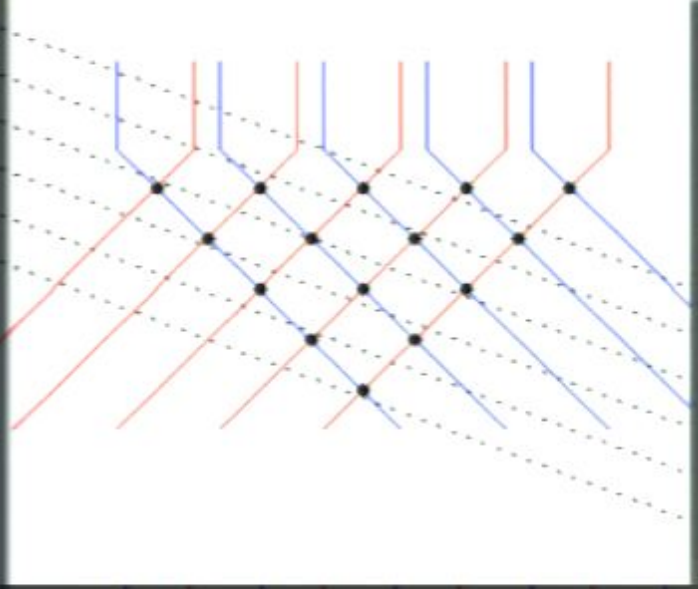
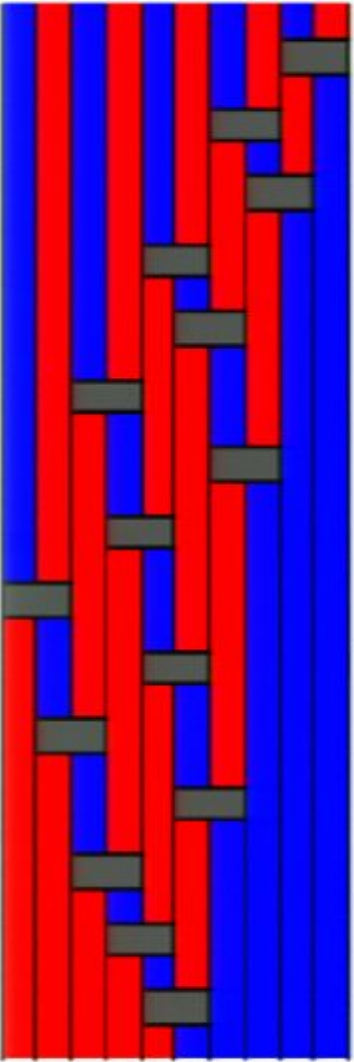
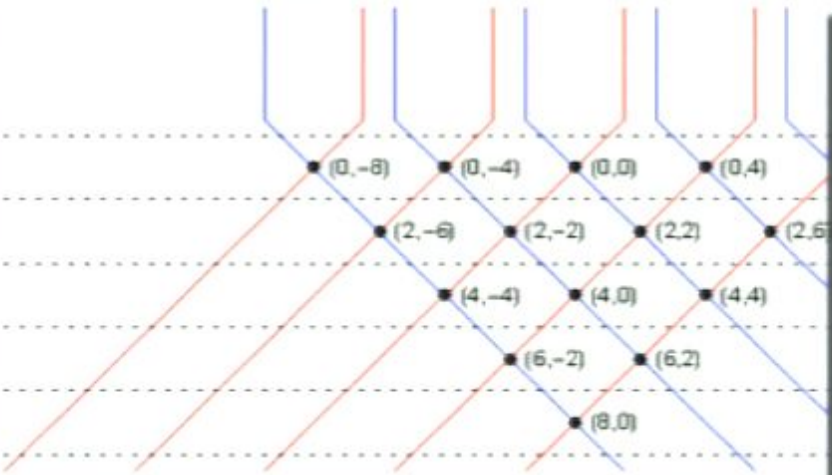
$$\overline{v_x \cup v_y} = \overline{v_x} \cap \overline{v_y}$$

**de Morgan!**



# SPECIAL RELATIVITY WITHOUT SPACE

Stephen Wolfram, *A New Kind of Science*



---

WHAT IS THE INFORMATIONAL MEANING  
OF INERTIAL MASS AND  $\hbar$   
AND HOW THE QUANTUM FIELD EMERGES

---

---

---

# THE INFORMATION FLOW

---

---

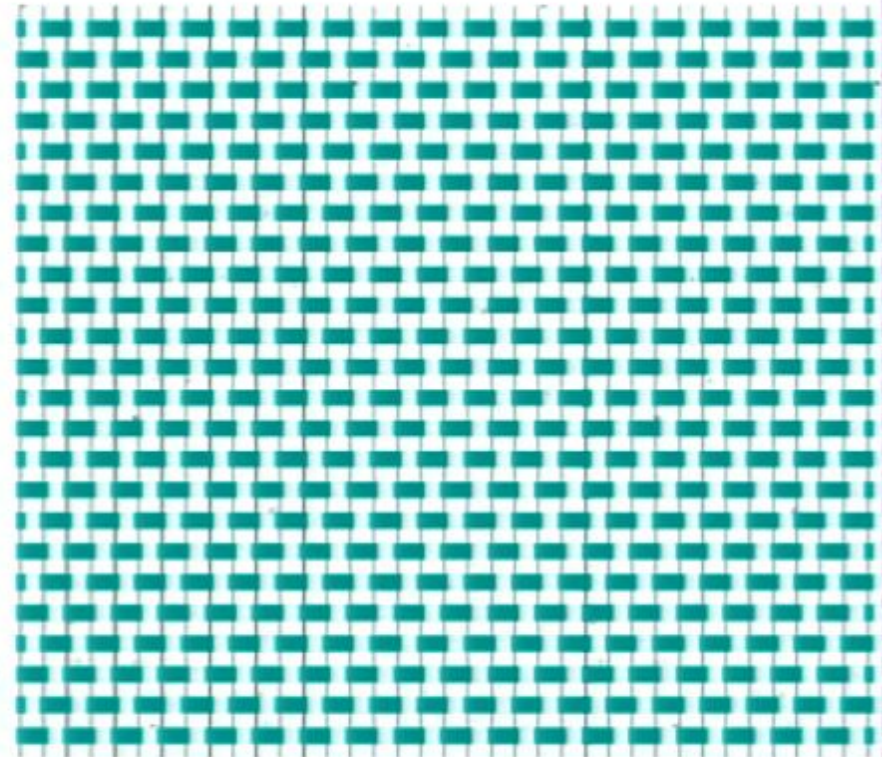
## ONE-DIMENSIONAL FLOW

---

---



Information can flow only in two directions





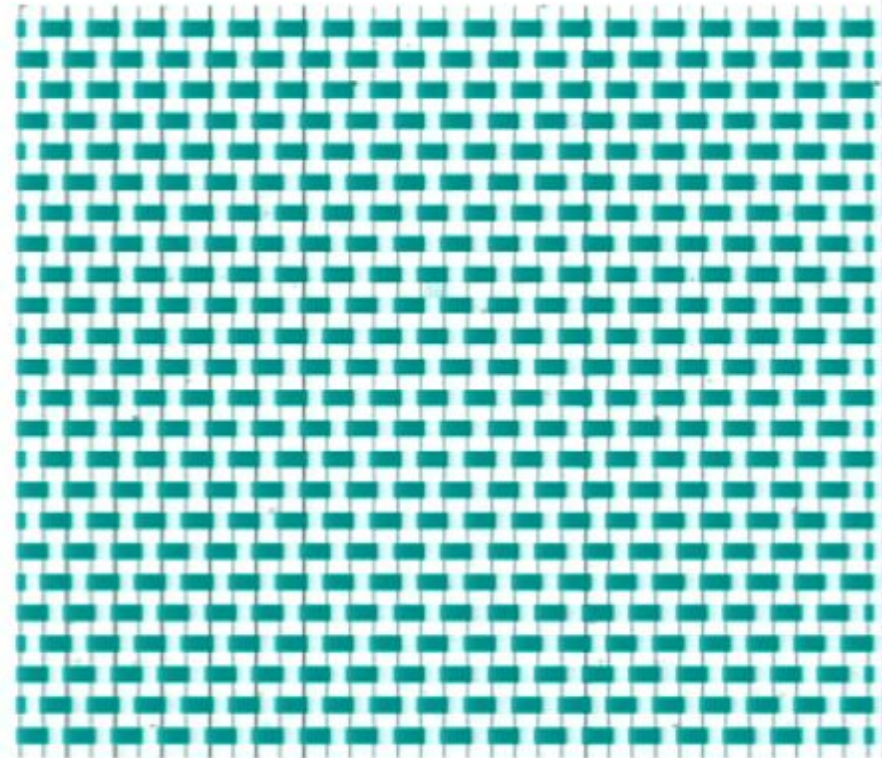
# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW



Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$



# THE INFORMATION FLOW

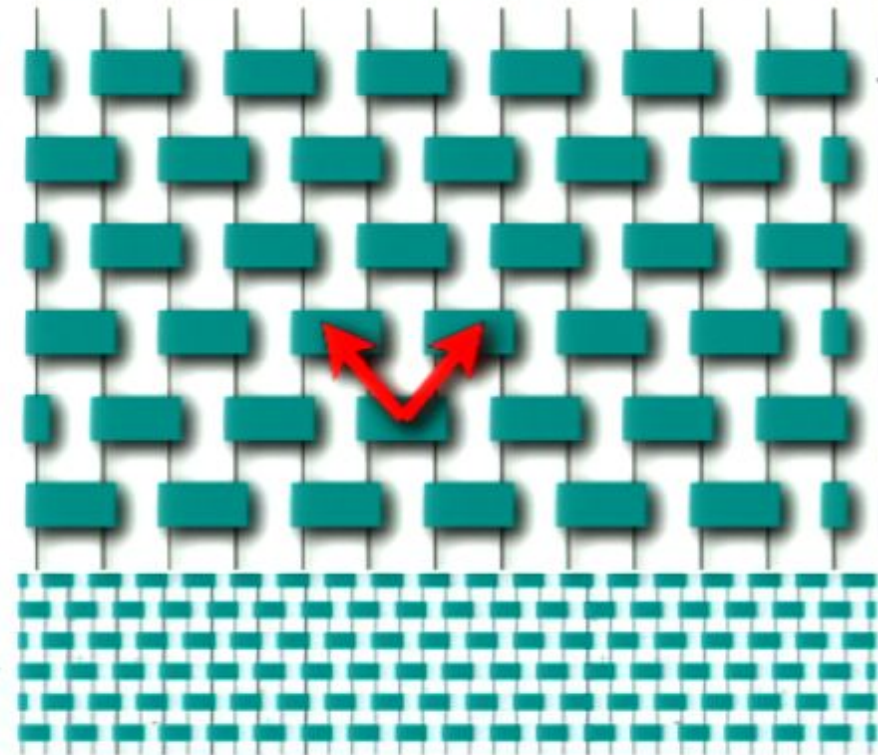
## ONE-DIMENSIONAL FLOW

★★★★

★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

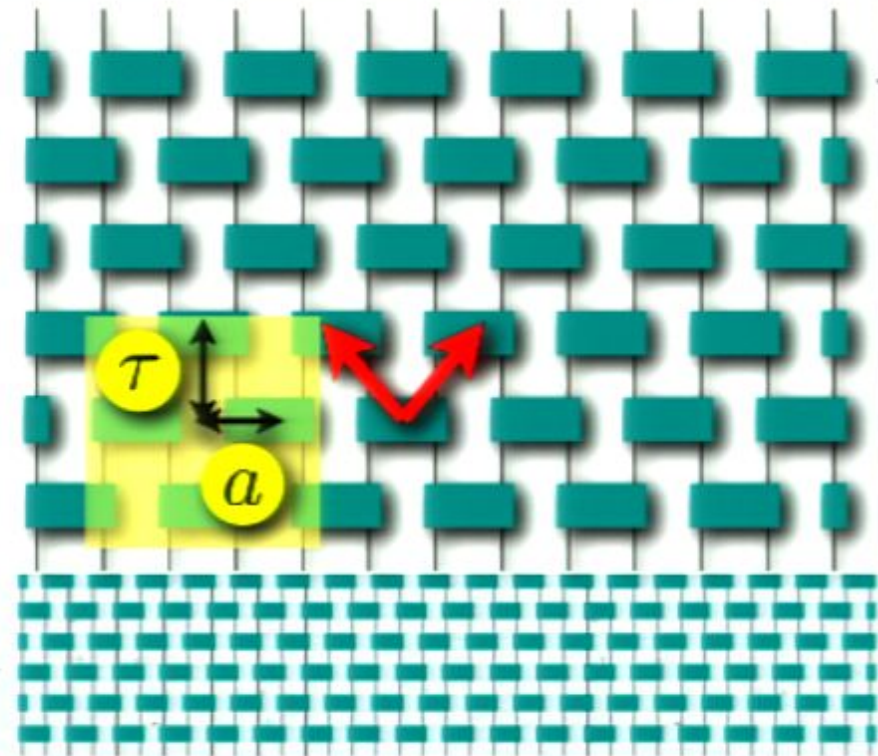
★★★★

★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

$$v = a/\tau$$





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

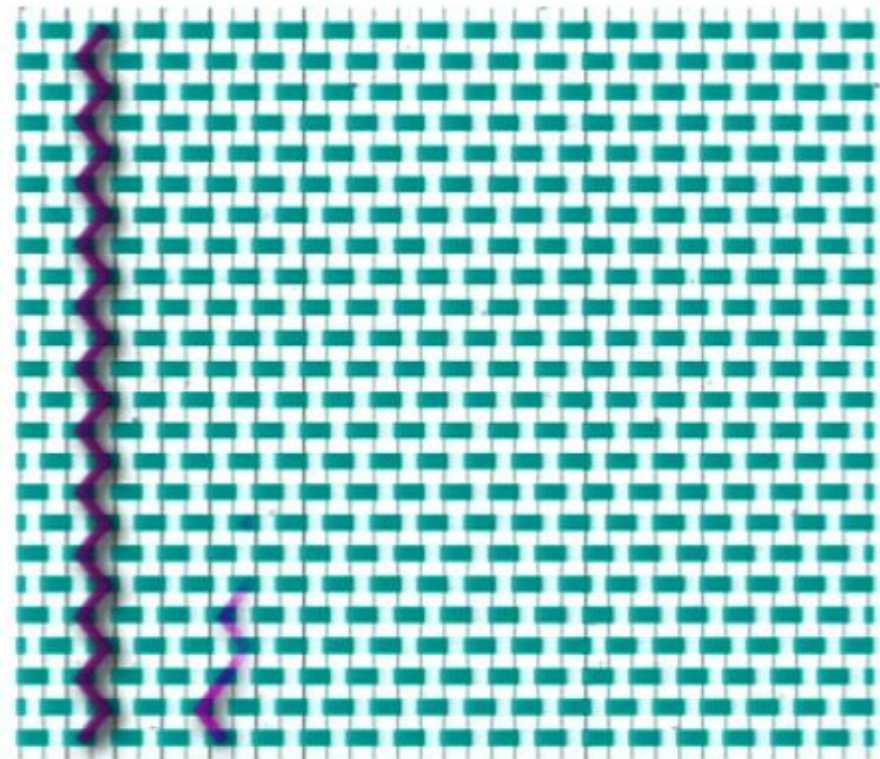
★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$



# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

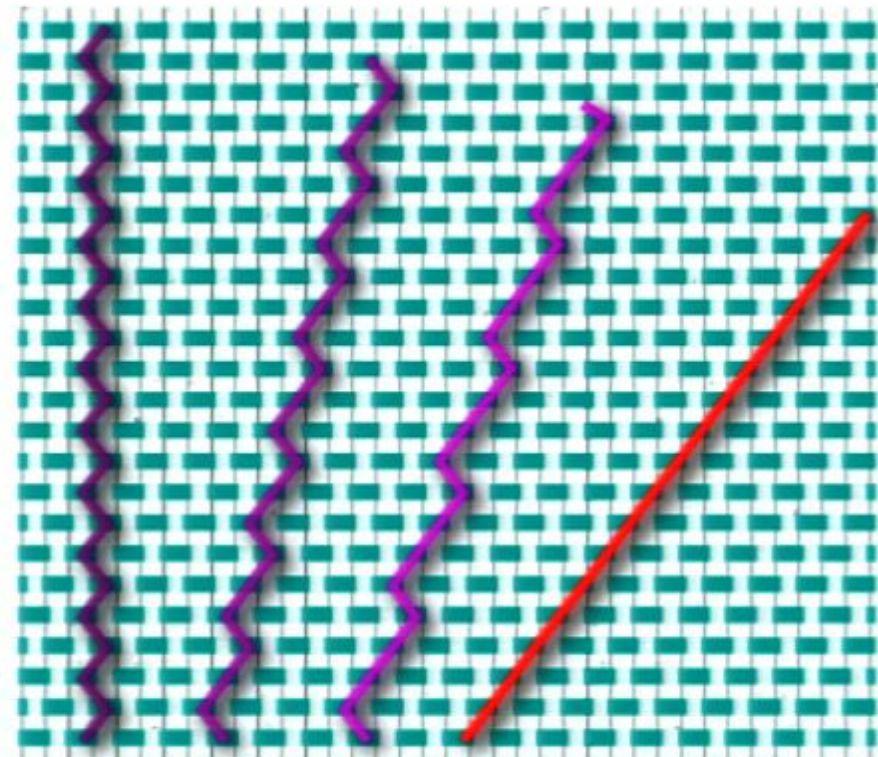
★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

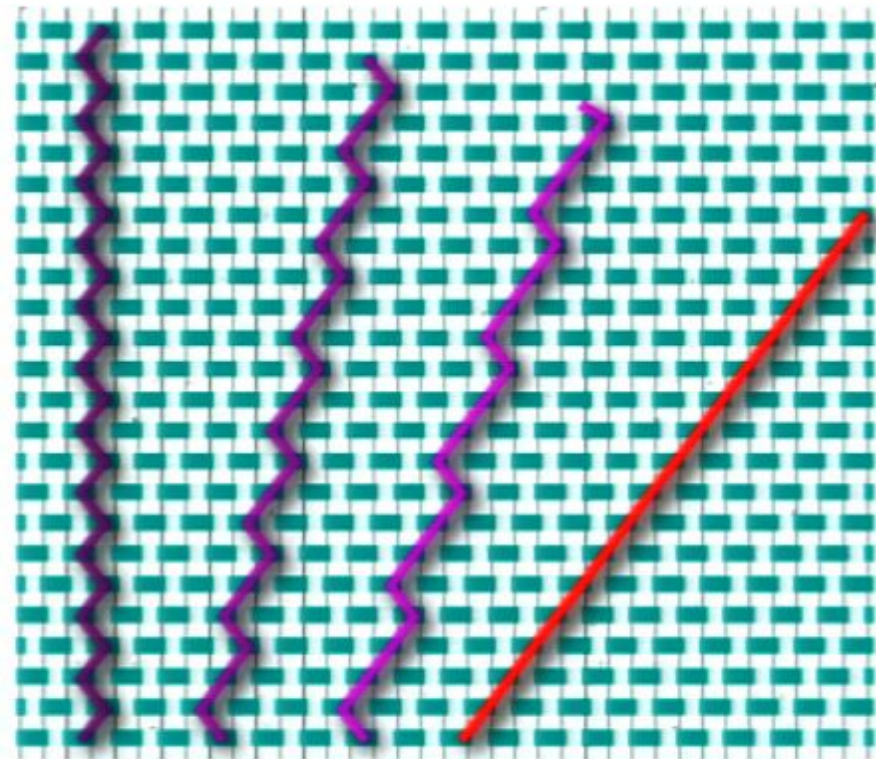
★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

★★★★

Information can flow only in two directions

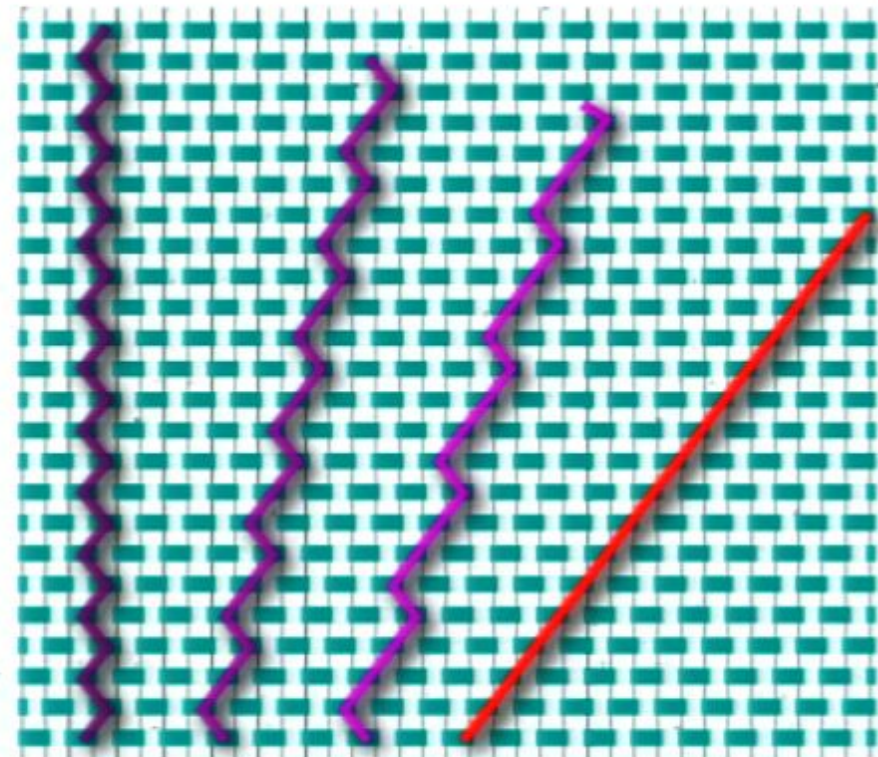
$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$



coupling between  $\phi^+$  and  $\phi^-$  with  
imaginary constant



# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

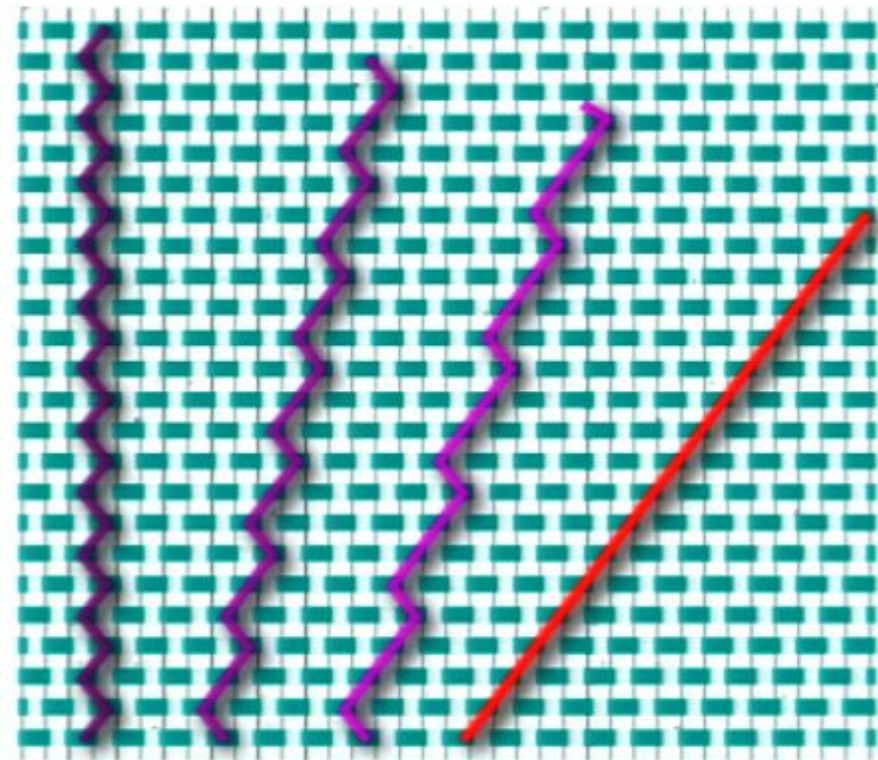
★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$



coupling between  $\phi^+$  and  $\phi^-$  with  
imaginary constant

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & -i\omega \\ -i\omega & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$



# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

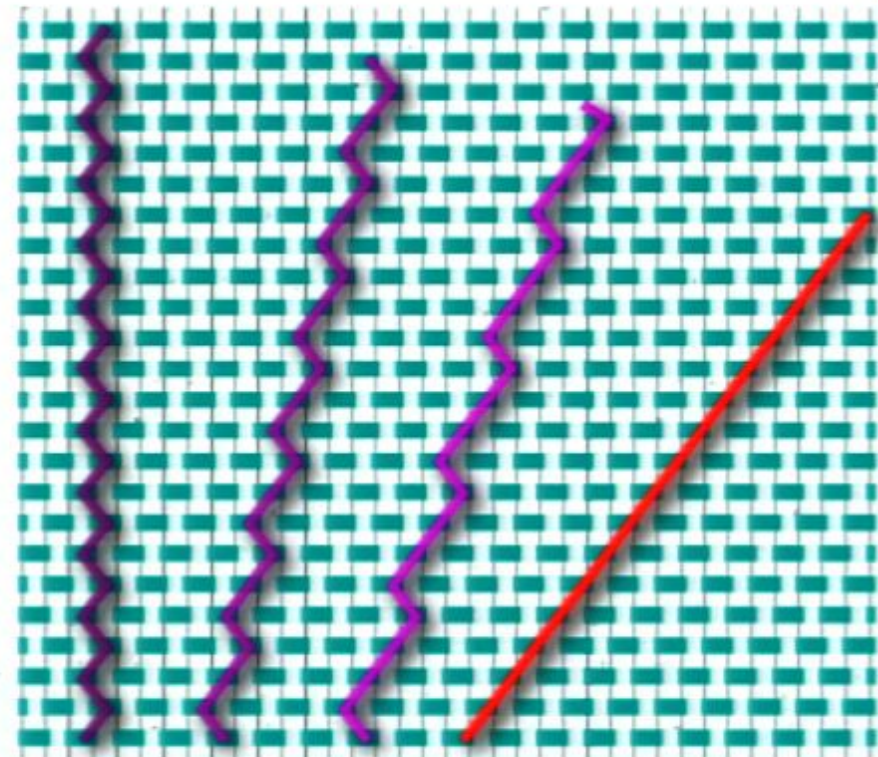
★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$



coupling between  $\phi^+$  and  $\phi^-$  with  
imaginary constant

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & -i\omega \\ -i\omega & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

(spinless) **Dirac equation!**



# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

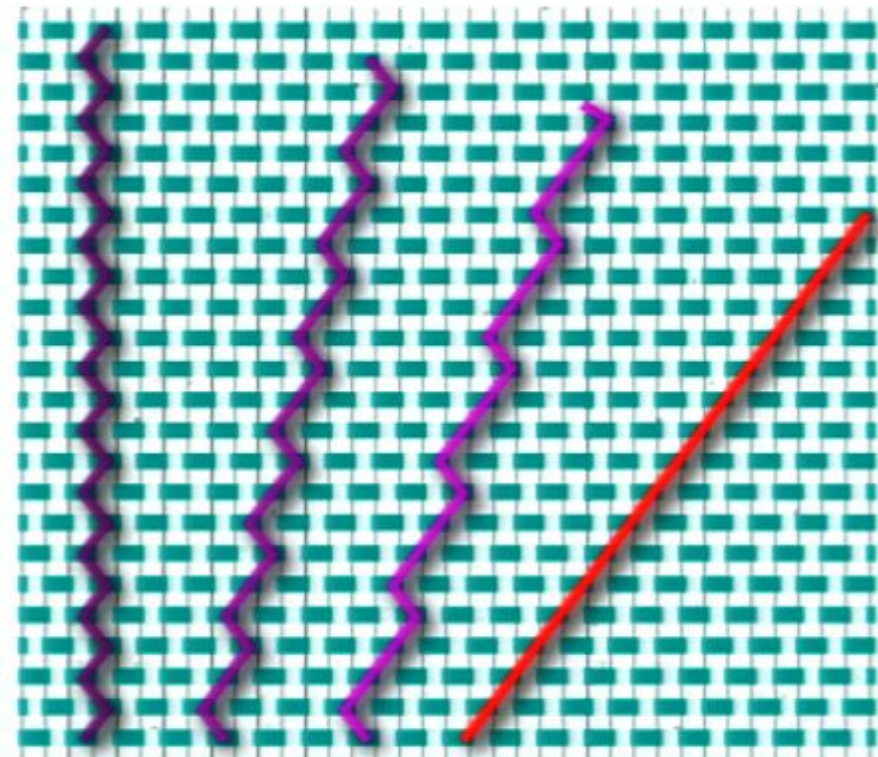
★★★★

★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction  $v = a/\tau$



coupling between  $\phi^+$  and  $\phi^-$  with  
imaginary constant

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & -i\omega \\ -i\omega & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

(spinless) **Dirac equation!**

No need of imposing

# WHAT IS $\hbar$ ?

$$i\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} i\nu\hat{\partial}_x & \omega \\ \omega & -i\nu\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

$$\omega = c\lambda^{-1}$$

$$\lambda = \frac{\hbar}{mc}$$

Compton  
wavelength

$m$

mass in Kg

$a$

topon

$T$

chronon

$(\omega)$

mass (informational) in  $s^{-1}$



---

---

# THE INFORMATION FLOW

---

---

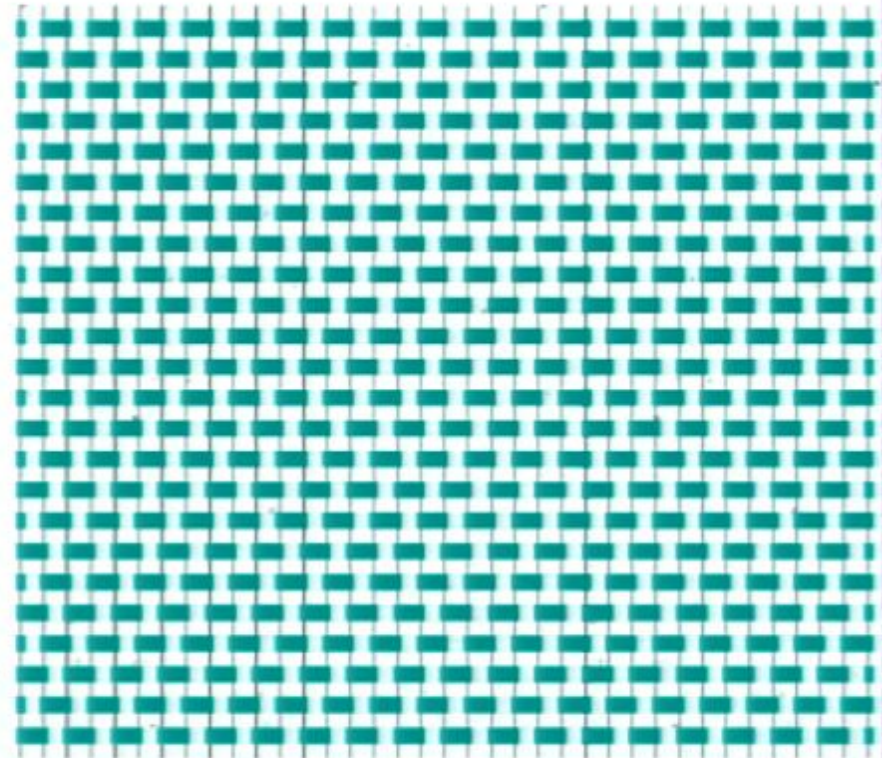
## ONE-DIMENSIONAL FLOW

---

---



Information can flow only in two directions





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

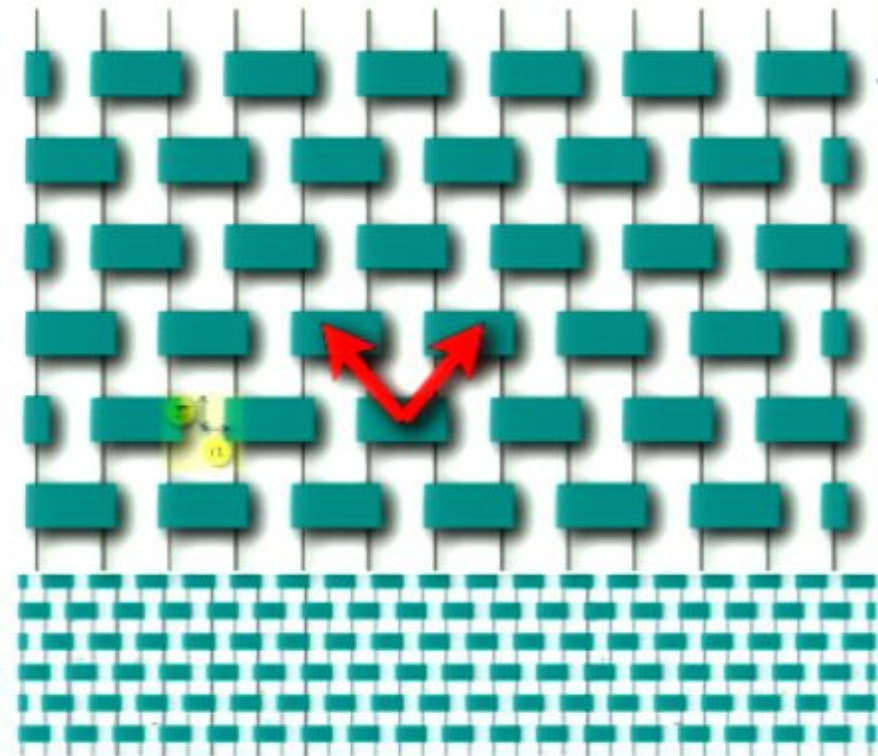
★★★★

★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

$$v = a/\tau$$



# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

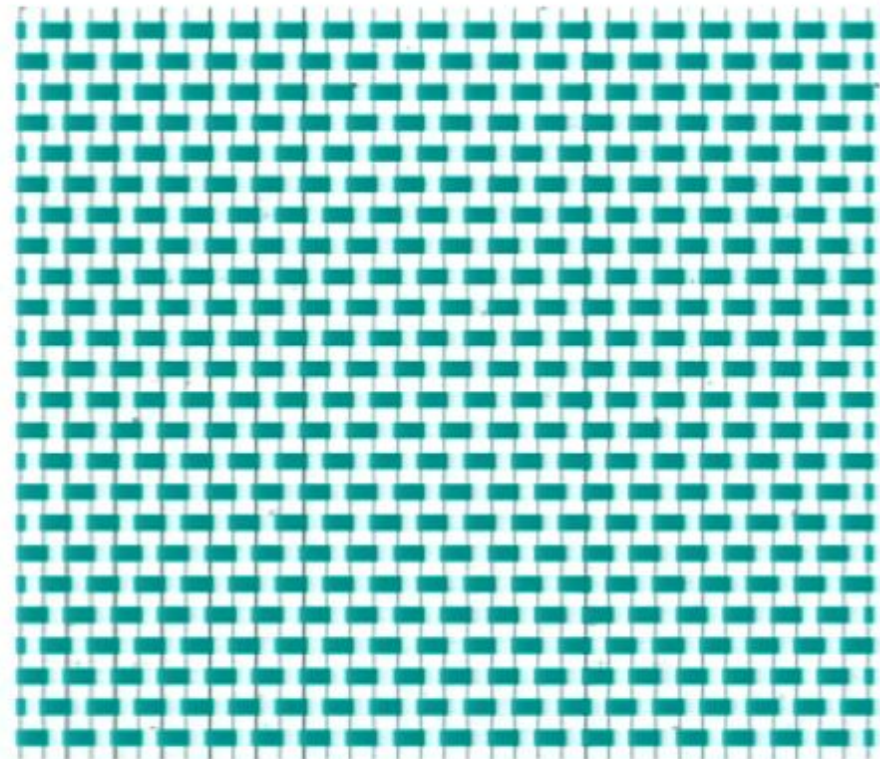
★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

★★★★

★★★★

Information can flow only in two directions

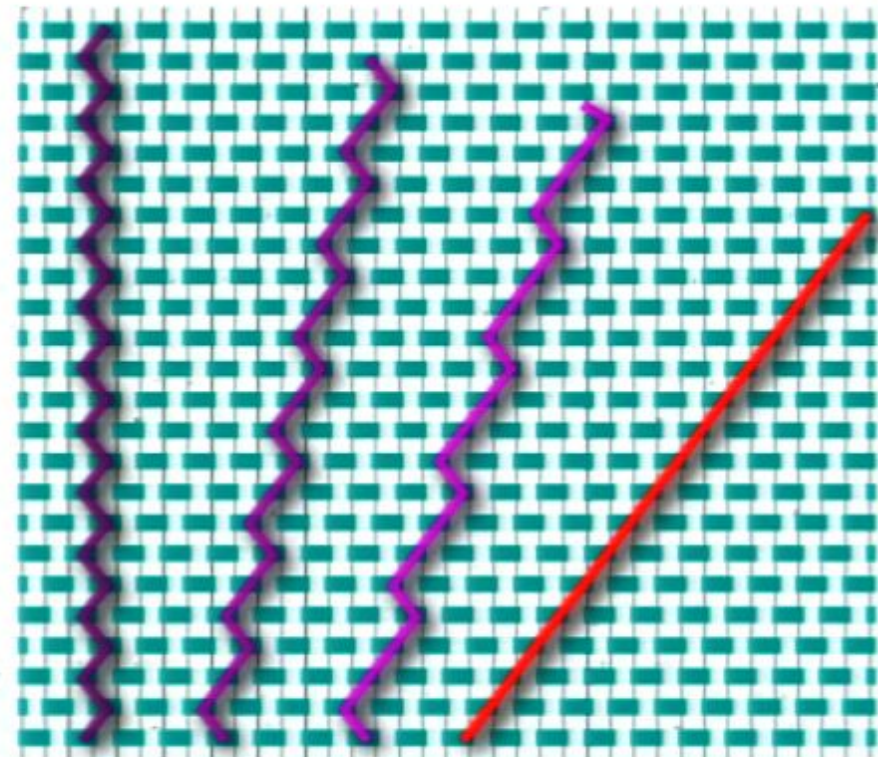
$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction

$$v = a/\tau$$



coupling between  $\phi^+$  and  $\phi^-$  with  
imaginary constant





# THE INFORMATION FLOW

## ONE-DIMENSIONAL FLOW

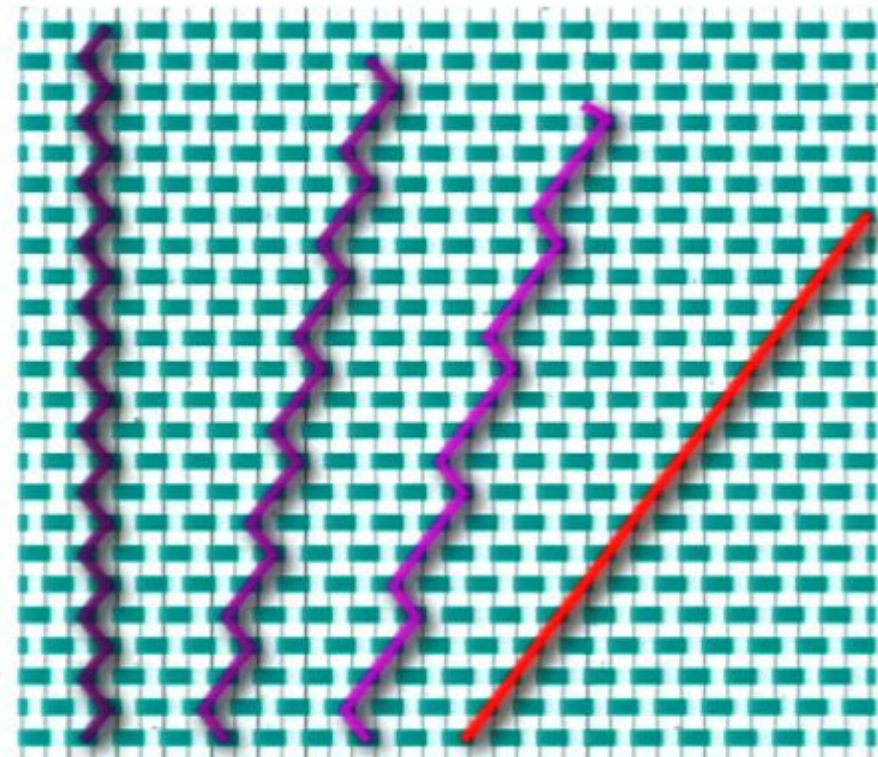
★★★★

★★★★

Information can flow only in two directions

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & 0 \\ 0 & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

Constant average speed:  
periodic change of direction  $v = a/\tau$



coupling between  $\phi^+$  and  $\phi^-$  with  
imaginary constant

$$\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} v\hat{\partial}_x & -i\omega \\ -i\omega & -v\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

# WHAT IS $\hbar$ ?

$$i\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} i\nu\hat{\partial}_x & \omega \\ \omega & -i\nu\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

$$\omega = c\lambda^{-1}$$

$\lambda = \frac{\hbar}{mc}$	Compton wavelength
$m$	mass in Kg
$a$	topon
$\tau$	chronon
$(\omega)$	mass (informational) in $s^{-1}$

# WHAT IS $\hbar$ ?

$$i\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} i\nu\hat{\partial}_x & \omega \\ \omega & -i\nu\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

$$\omega = c\lambda^{-1}$$

$$m = \frac{\tau^2}{a^2} \hbar\omega = \frac{1}{c^2} \hbar\omega$$

$$\lambda = \frac{\hbar}{mc}$$

Compton  
wavelength

$m$

mass in Kg

$a$

topon

$\tau$

chronon

$(\omega)$

mass (informational) in  $s^{-1}$



# WHAT IS $\hbar$ ?

$$i\hat{\partial}_t \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix} = \begin{bmatrix} i\nu\hat{\partial}_x & \omega \\ \omega & -i\nu\hat{\partial}_x \end{bmatrix} \begin{bmatrix} \phi^+ \\ \phi^- \end{bmatrix}$$

$$\omega = c\lambda^{-1}$$

$$m = \frac{\tau^2}{a^2} \hbar\omega = \frac{1}{c^2} \hbar\omega$$

$\hbar$ : conversion factor between the informational notion (in  $s^{-1}$ ) and the customary notion (in Kg) of the inertial mass

$$\lambda = \frac{\hbar}{mc}$$

Compton wavelength

$m$

mass in Kg

$a$

topon

$\tau$

chronon

$(\omega)$

mass (informational) in  $s^{-1}$

---

---

# THE INFORMATION FLOW

---

---

## SIMULATING A QUANTUM FIELD

---

---



Simulation of QFT with a quantum computer, with gates performing infinitesimal transformations:

---

---

# THE INFORMATION FLOW

---

---

## SIMULATING A QUANTUM FIELD

---

---



Simulation of QFT with a quantum computer, with gates performing infinitesimal transformations:



In order to have average speed equal to  $c$  you need infinite maximal speed.



---

---

# THE INFORMATION FLOW

---

---

## SIMULATING A QUANTUM FIELD

---

---



Simulation of QFT with a quantum computer, with gates performing infinitesimal transformations:



In order to have average speed equal to  $c$  you need infinite maximal speed.



Lorentz-covariance must be imposed as a constraint, and cannot be derived from QT causality!

# THE INFORMATION FLOW

## SIMULATING A QUANTUM FIELD

Simulation of QFT with a quantum computer, with gates performing infinitesimal transformations:



In order to have average speed equal to  $c$  you need infinite maximal speed.



Lorentz-covariance must be imposed as a constraint, and cannot be derived from QT causality!



Relativity is derived from the computational

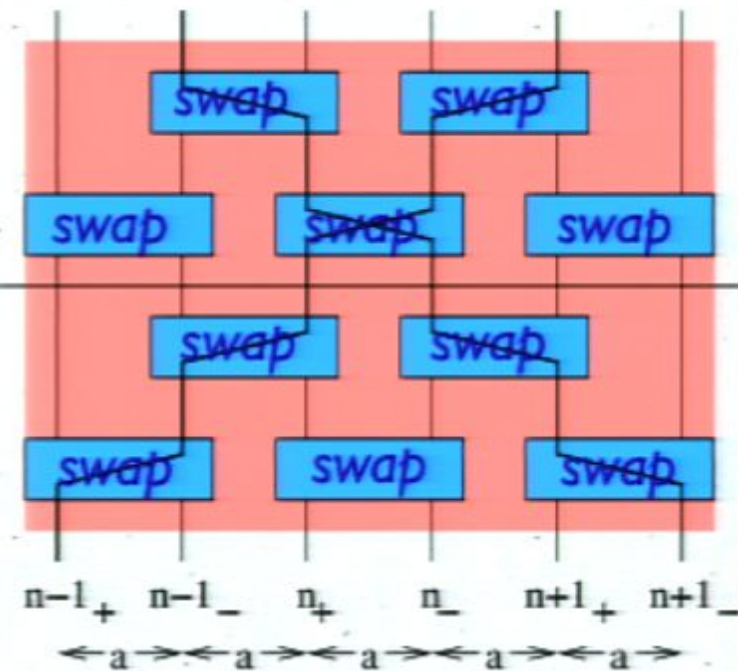
# THE INFORMATION FLOW

## SIMULATING A QUANTUM FIELD

Simulation of QFT with a quantum computer, with gates performing infinitesimal transformations:

In order to have average speed equal to  $c$  you need infinite maximal speed.

Lorentz-covariance must be imposed as a constraint, and cannot be derived from QT causality!



Relativity is derived from the computational

We must have finite



# THE INFORMATION FLOW

## LINEAR FLOW

★★★★

★★★★

Each gate evolves the field linearly:

(anti)commutation  
relations are preserved

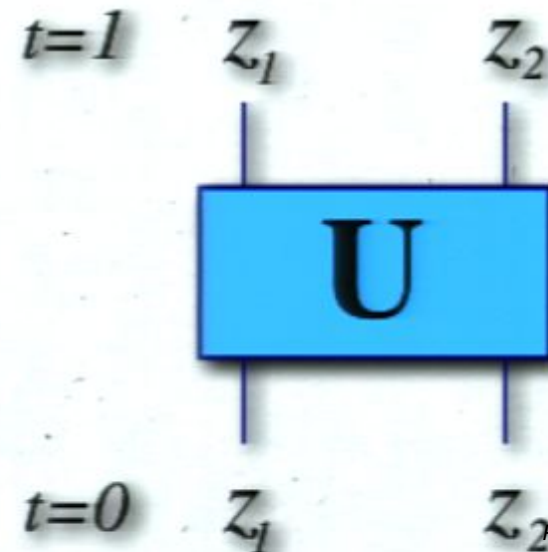
$$[z_i, z_j^\dagger]_{\pm} = \delta_{ij}$$

Evolution from bipartite gates:

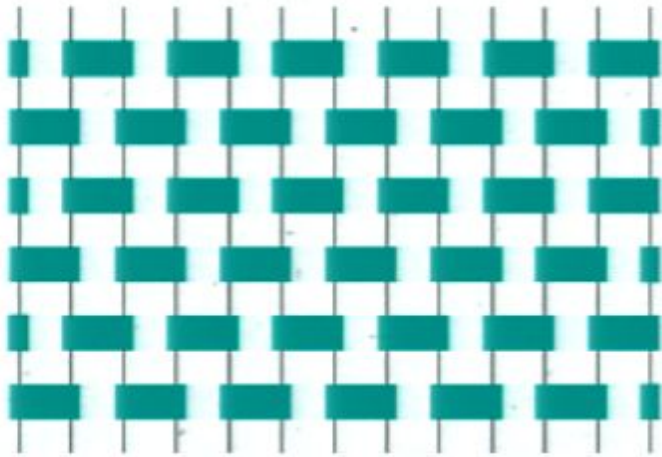
$$\begin{bmatrix} z_1 \\ z_2 \end{bmatrix}_{t=1} = U \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} U^\dagger = \mathbf{U} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix}$$

$$z_n(t=1) = U z_n U^\dagger = \sum_k U_{nk} z_k$$

$$\mathbf{U} := \|U_{ij}\| \quad \text{unitary matrix}$$



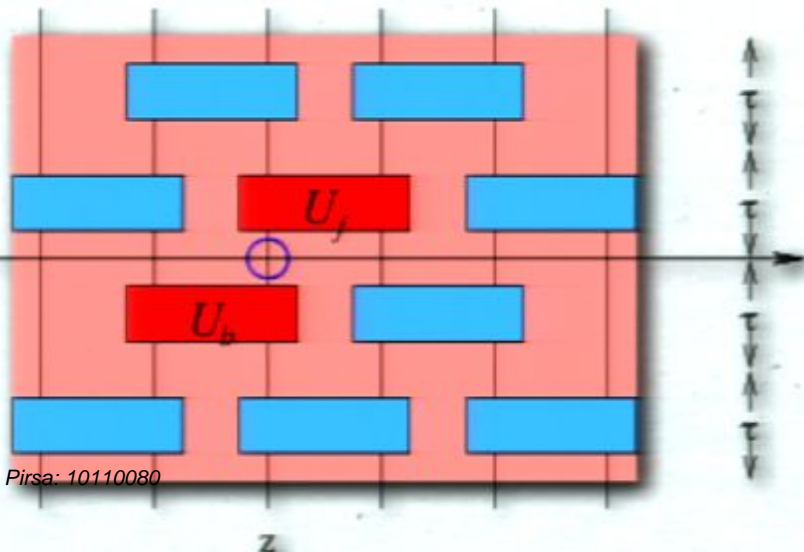
# QC SIMULATION OF QFT



Coarse-grained discrete **derivatives**:

$$\hat{\partial}_t z = \frac{1}{2k\tau} [z(k\tau) - z(-k\tau)]$$

$$\hat{\partial}_x = \frac{1}{4ka} (\delta_+^k - \delta_-^k)$$



**“HAMILTONIAN”**

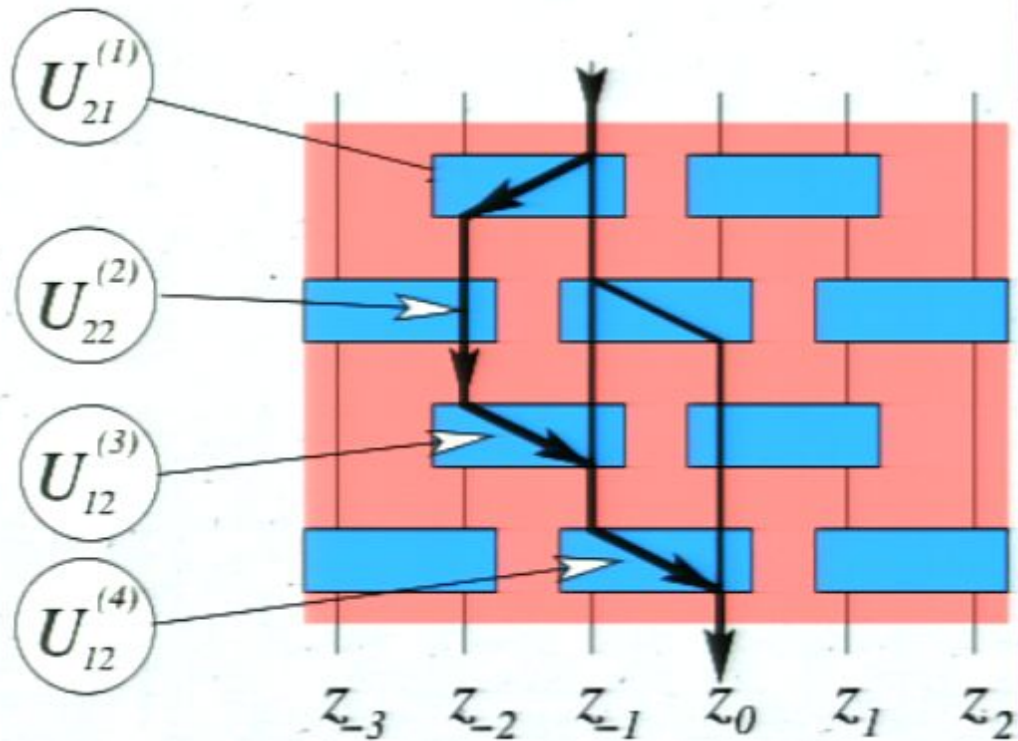
$$H_{\text{gate}}^{(2n)} z = \frac{i}{2n\tau} [z(n\tau) - z(-n\tau)] = i\hat{\partial}_t z$$

$$H_{\text{gate}}^{(2)} z = \frac{i}{2\tau} (U_f z U_f^\dagger - U_b^\dagger z U_b)$$

# QC SIMULATION OF QFT

We need to develop a *path-sum calculus* over the circuit:

1. Number all the input wires at each gate, from the leftmost to the rightmost one, and do the same for the output wires
2. We say that a wire  $l$  is in the past-cone of the wire  $k$  if there is a path from  $l$  to  $k$  passing through gates.
3. For any output wire  $k$  and any input wire  $l$  in its causal past cone, consider all paths connecting  $k$  with  $l$
4. The following linear expansion holds



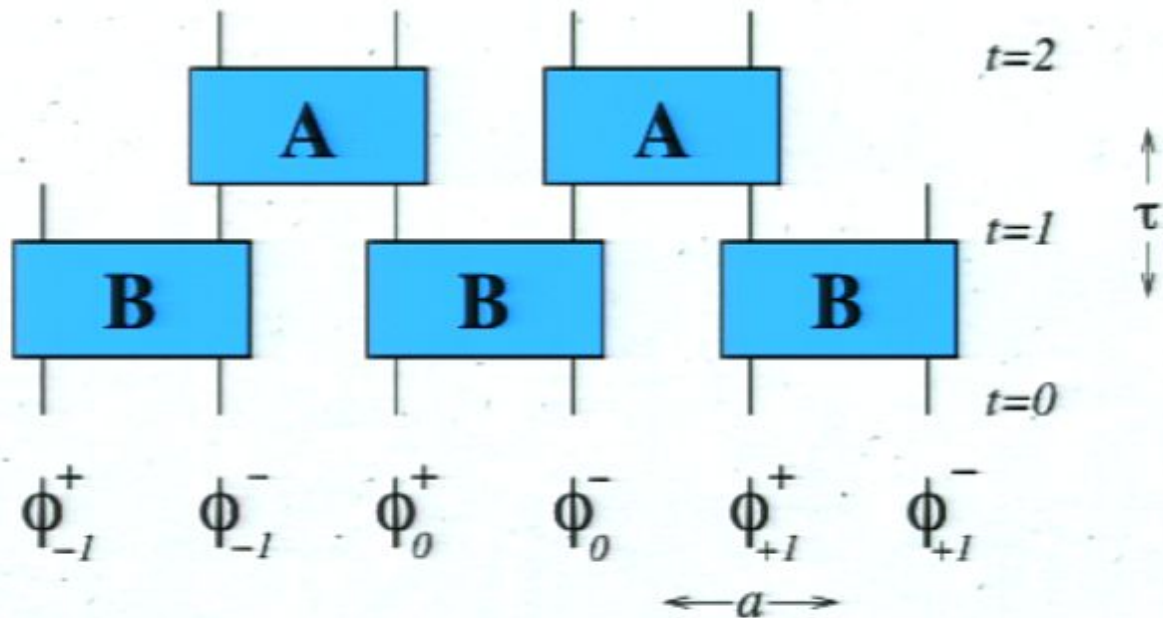
$$z_l(t) = \sum U_{i_1 i_2}^{(1)} U_{i_2 i_3}^{(2)} \cdots U_{i_n i_{n+1}}^{(n)} z_k(0)$$



# QC SIMULATION OF QFT

## “Hamiltonian”

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau} \begin{bmatrix} A_{21}B_{21}\delta_- - B_{12}^\dagger A_{12}^\dagger \delta_+ + A_{22}B_{11} - B_{11}^\dagger A_{22}^\dagger & (A_{21}B_{22} - B_{11}^\dagger A_{21}^\dagger)\delta_- + A_{22}B_{12} - B_{12}^\dagger A_{11}^\dagger \\ (A_{12}B_{11} - B_{22}^\dagger A_{12}^\dagger)\delta_+ + A_{11}B_{21} - B_{21}^\dagger A_{22}^\dagger & A_{12}B_{12}\delta_+ - B_{21}^\dagger A_{21}^\dagger \delta_- + A_{11}B_{22} - B_{22}^\dagger A_{11}^\dagger \end{bmatrix}$$



# QC SIMULATION OF QFT

## “Hamiltonian”

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau} \begin{bmatrix} A_{21}B_{21}\delta_- - B_{12}^\dagger A_{12}^\dagger \delta_+ + A_{22}B_{11} - B_{11}^\dagger A_{22}^\dagger & (A_{21}B_{22} - B_{11}^\dagger A_{21}^\dagger)\delta_- + A_{22}B_{12} - B_{12}^\dagger A_{11}^\dagger \\ (A_{12}B_{11} - B_{22}^\dagger A_{12}^\dagger)\delta_+ + A_{11}B_{21} - B_{21}^\dagger A_{22}^\dagger & A_{12}B_{12}\delta_+ - B_{21}^\dagger A_{21}^\dagger \delta_- + A_{11}B_{22} - B_{22}^\dagger A_{11}^\dagger \end{bmatrix}$$

Hermiticity is satisfied:

$$\langle \phi_n^\pm | H_{\text{gate}}^{(4)} | \phi_n^\pm \rangle = \langle \phi_n^\pm | H_{\text{gate}}^{(4)} | \phi_n^\pm \rangle^* \implies i(A_{aa}B_{bb} - A_{aa}^\dagger B_{bb}^\dagger) \in \mathbb{R},$$

$$\langle \phi_n^\pm | H_{\text{gate}}^{(4)} | \phi_n^\mp \rangle = \langle \phi_n^\mp | H_{\text{gate}}^{(4)} | \phi_n^\pm \rangle^* \implies (A_{22}B_{12} - A_{11}^\dagger B_{12}^\dagger) = -(A_{11}B_{21} - A_{22}^\dagger B_{21}^\dagger)^*,$$

$$\langle \phi_{n+1}^\pm | H_{\text{gate}}^{(4)} | \phi_n^\pm \rangle = \langle \phi_n^\pm | H_{\text{gate}}^{(4)} | \phi_{n+1}^\pm \rangle^* \implies A_{ab}^\dagger B_{ab}^\dagger = A_{ba}^* B_{ba}^*,$$

$$\langle \phi_n^+ | H_{\text{gate}}^{(4)} | \phi_{n-1}^- \rangle = \langle \phi_{n-1}^- | H_{\text{gate}}^{(4)} | \phi_n^+ \rangle^* \implies A_{21}B_{22} - A_{21}^\dagger B_{11}^\dagger = -(A_{12}B_{11} - A_{12}^\dagger B_{22}^\dagger)^*.$$

---

---

# OBSERVATIONAL CONSEQUENCES: MASS-DEPENDENT REFRACTION INDEX OF VACUUM

---

---



# QC SIMULATION OF QFT

## THE SPINLESS DIRAC EQUATION

Write the "Hamiltonian" as follows:

$$H_{\text{gate}}^{(4)} = c(\mathbf{H} + i\mathbf{K}\hat{\partial}_x) = ic\zeta\hat{\partial}_x + \omega\sigma_x, \quad \omega = c\lambda^{-1}$$

(inverse) refraction index



$$H_{11} = -\frac{1}{2a}\Im(A_{21}B_{21} + A_{22}B_{11}) = 0,$$

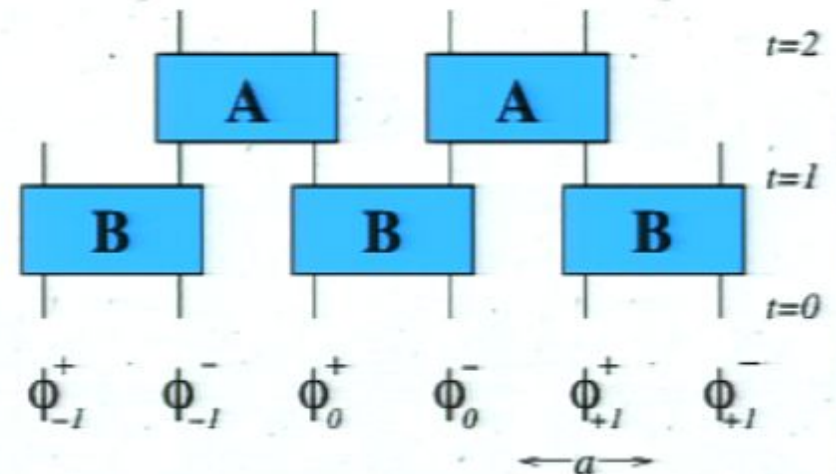
$$H_{12} = \frac{i}{4a}(A_{21}B_{22} - A_{12}^*B_{11}^* + A_{22}B_{12} - A_{11}^*B_{21}^*) = \lambda^{-1}$$

$$H_{22} = -\frac{1}{2a}\Im(A_{12}B_{12} + A_{11}B_{22}) = 0,$$

$$K_{11} = -\Re(A_{21}B_{21}) = \zeta,$$

$$K_{22} = \Re(A_{12}B_{12}) = -\zeta,$$

$$K_{12} = -\frac{1}{2}(A_{21}B_{22} - A_{12}^*B_{11}^*) = 0.$$



# QC SIMULATION OF QFT

## THE SPINLESS DIRAC EQUATION

Write the "Hamiltonian" as follows:

(inverse) refraction index

$$H_{\text{gate}}^{(4)} = c(\mathbf{H} + i\mathbf{K}\hat{\partial}_x) = ic\zeta\hat{\partial}_x + \omega\sigma_x, \quad \omega = c\lambda^{-1}$$



$$H_{11} = -\frac{1}{2a}\Im(A_{21}B_{21} + A_{22}B_{11}) = 0,$$

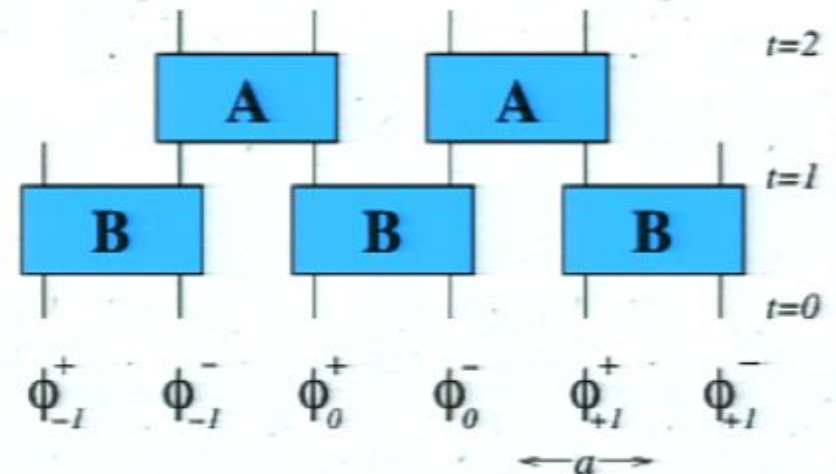
$$H_{12} = \frac{i}{4a}(A_{21}B_{22} - A_{12}^*B_{11}^* + A_{22}B_{12} - A_{11}^*B_{21}^*) = \lambda^{-1}$$

$$H_{22} = -\frac{1}{2a}\Im(A_{12}B_{12} + A_{11}B_{22}) = 0,$$

$$K_{11} = -\Re(A_{21}B_{21}) = \zeta,$$

$$K_{22} = \Re(A_{12}B_{12}) = -\zeta,$$

$$K_{12} = -\frac{1}{2}(A_{21}B_{22} - A_{12}^*B_{11}^*) = 0.$$



$$\mathbf{A} = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} 0 & ie^{i\phi} \end{bmatrix}$$

# QC SIMULATION OF QFT

## THE SPINLESS DIRAC EQUATION

Write the "Hamiltonian" as follows:

(inverse) refraction index

$$H_{\text{gate}}^{(4)} = c(\mathbf{H} + i\mathbf{K}\hat{\partial}_x) = ic\zeta\hat{\partial}_x + \omega\sigma_x, \quad \omega = c\lambda^{-1}$$



$$H_{11} = -\frac{1}{2a}\Im(A_{21}B_{21} + A_{22}B_{11}) = 0,$$

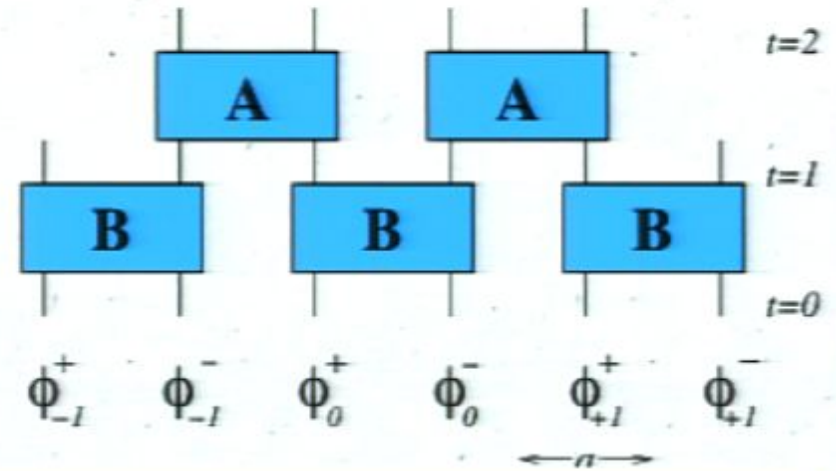
$$H_{12} = \frac{i}{4a}(A_{21}B_{22} - A_{12}^*B_{11}^* + A_{22}B_{12} - A_{11}^*B_{21}^*) = \lambda^{-1}$$

$$H_{22} = -\frac{1}{2a}\Im(A_{12}B_{12} + A_{11}B_{22}) = 0,$$

$$K_{11} = -\Re(A_{21}B_{21}) = \zeta,$$

$$K_{22} = \Re(A_{12}B_{12}) = -\zeta,$$

$$K_{12} = -\frac{1}{2}(A_{21}B_{22} - A_{12}^*B_{11}^*) = 0.$$



$$\mathbf{A} = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} 0 & ie^{i\phi} \end{bmatrix}$$

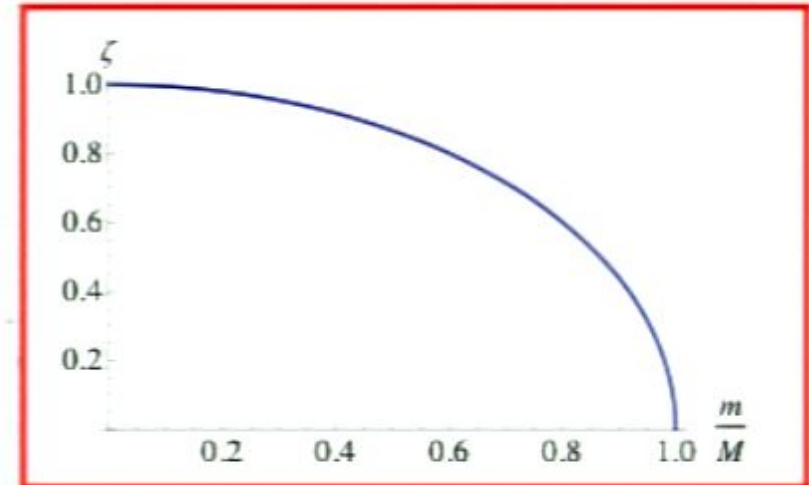
$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



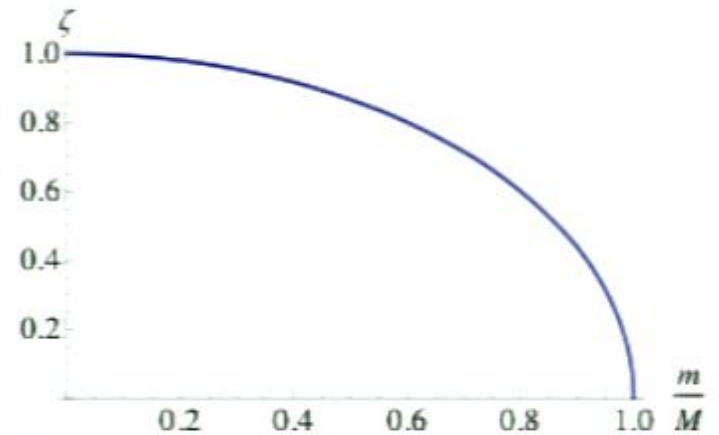
# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

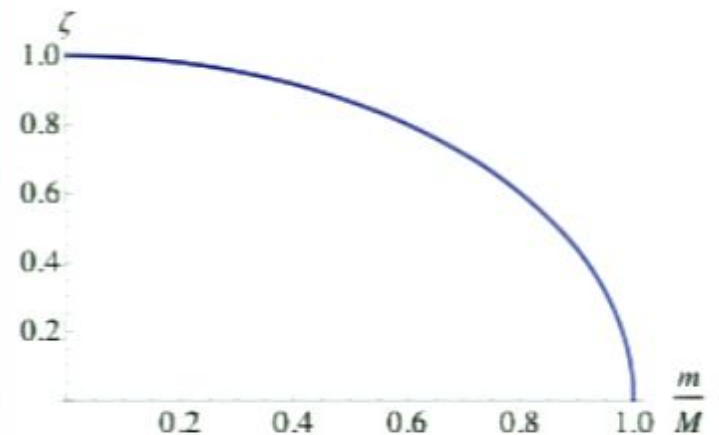
*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$





# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

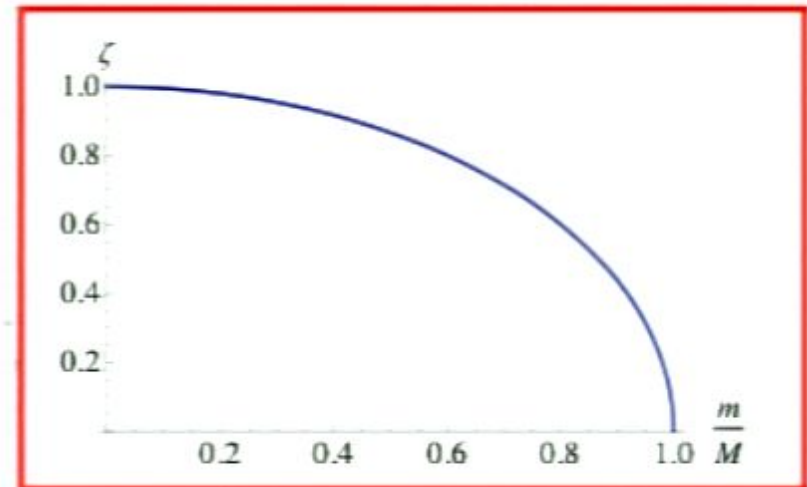
$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \blacksquare$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

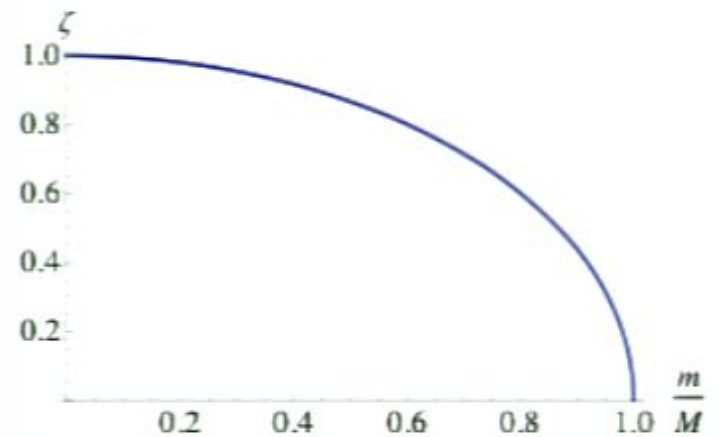
$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq \frac{1}{2\tau}$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

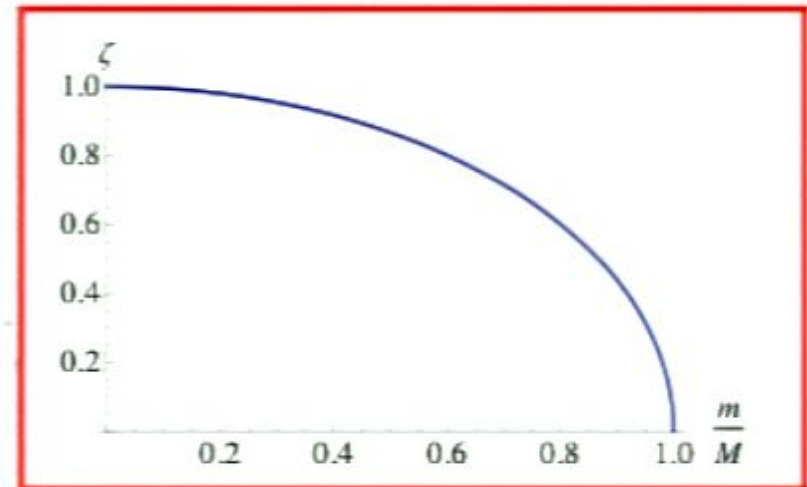
The Hamiltonian is Hermitian, whence:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq \frac{1}{2\tau}$$

The norm is obtained by FT at  $k = \frac{\pi}{2a}$

$$\frac{\sqrt{\zeta^2 + 4\tau^2\omega^2}}{2\tau} \leq \frac{1}{2\tau}$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$





# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

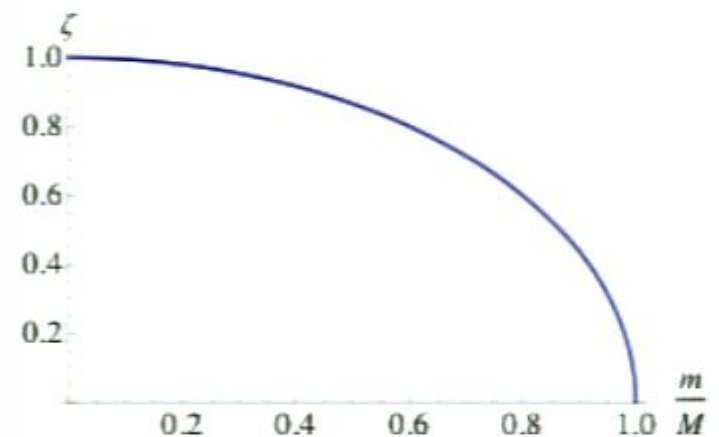
$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq \frac{1}{2\tau}$$

The norm is obtained by FT at  $k = \frac{\pi}{2a}$

$$\frac{\sqrt{\zeta^2 + 4\tau^2\omega^2}}{2\tau} \leq \frac{1}{2\tau}$$

namely for  $\omega = c\lambda^{-1}$  one has:

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$

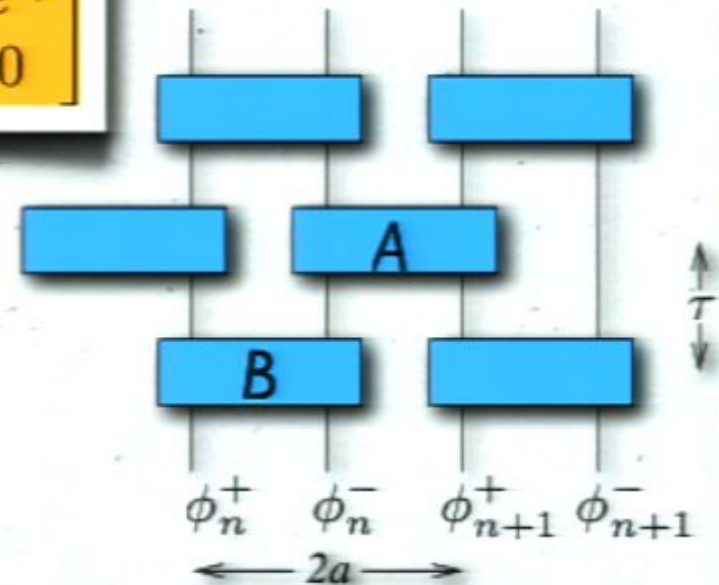


$$\zeta \leq \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$

# QC SIMULATION OF QFT

**SIMPLE SCALAR FIELD IN 1 SPACE DIM.**

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

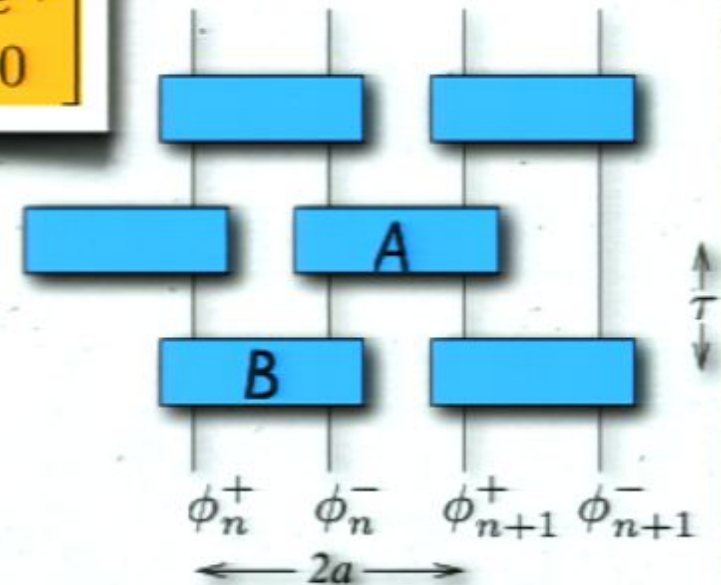


# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

W.l.g. fix  $\phi = 0$ ,  $\psi = -\pi/2$





# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

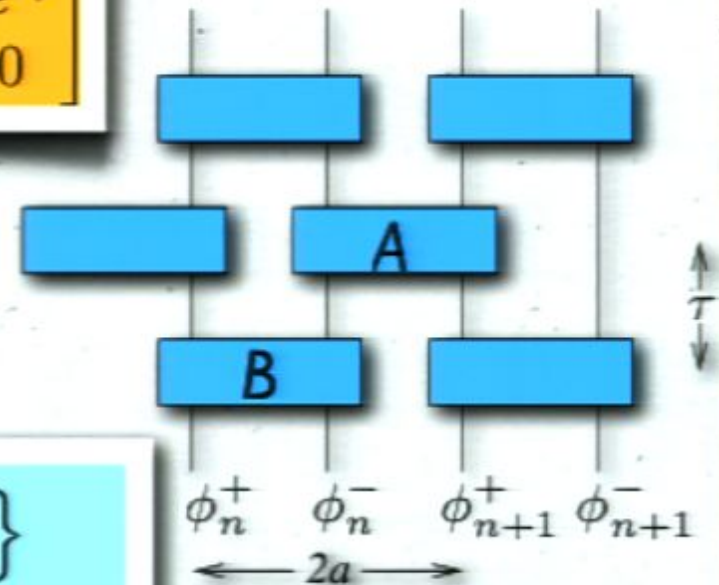
$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

W.l.g. fix  $\phi = 0$ ,  $\psi = -\pi/2$

For both Bose and Fermi fields one has:

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$



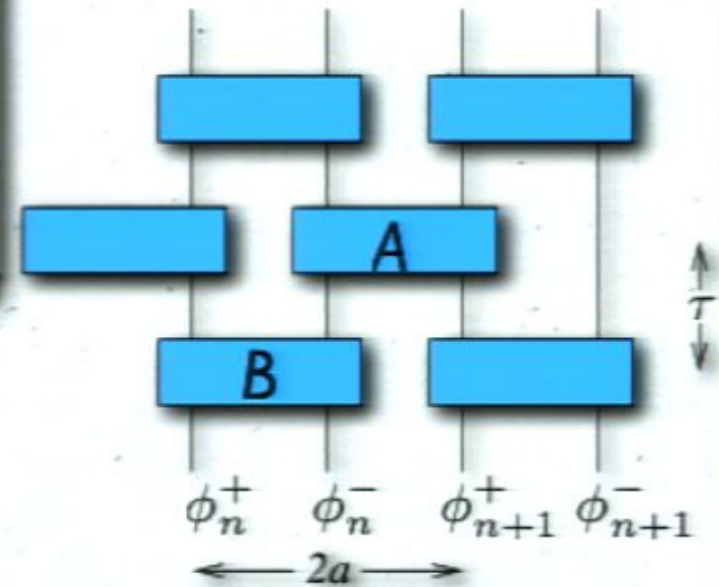
# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$

Commuting	Anticommuting
Harmonic oscillator	Clifford algebra
$[a_l, a_k^\dagger] = \delta_{lk}$	$\phi_n^+ = \sigma_{2n}^- \prod_{k=-\infty}^{n-1} \sigma_{2k+1}^z \sigma_{2k}^z$
$\phi_n^+ = a_{2n} \quad \phi_n^- = a_{2n+1}$	$\phi_n^- = \sigma_{2n+1}^- \sigma_{2n}^z \prod_{k=-\infty}^{n-1} \sigma_k^z$





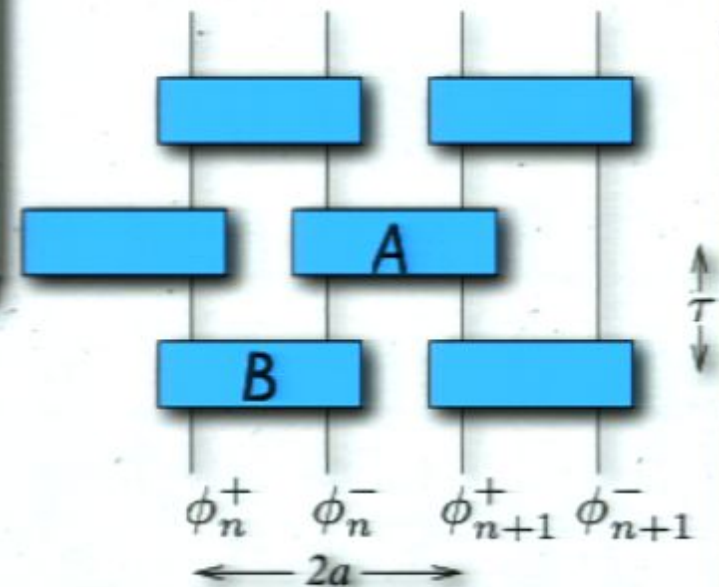
# QC SIMULATION OF QFT

**SIMPLE SCALAR FIELD IN 1 SPACE DIM.**

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^- \dagger \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^- \dagger \phi_n^+ \right] \right\}$$

Commuting	Anticommuting
Harmonic oscillator	Clifford algebra
$[a_l, a_k^\dagger] = \delta_{lk}$	$\phi_n^+ = \sigma_{2n}^- \prod_{k=-\infty}^{n-1} \sigma_{2k+1}^z \sigma_{2k}^z$
$\phi_n^+ = a_{2n} \quad \phi_n^- = a_{2n+1}$	$\phi_n^- = \sigma_{2n+1}^- \sigma_{2n}^z \prod_{k=-\infty}^{n-1} \sigma_k^z$



$$A = \exp \left[ -i\theta \left( \sigma_{2n-1}^- \sigma_{2n}^+ + \sigma_{2n-1}^+ \sigma_{2n}^- \right) \right]$$

$$B = \exp \left[ -i\frac{\pi}{2} \left( \sigma_{2n}^+ \sigma_{2n+1}^- + \sigma_{2n}^- \sigma_{2n+1}^+ \right) \right]$$

**Gates act on local algebras only!**



# QC SIMULATION OF QFT

## CONNECTION WITH THE USUAL QFT

★★★★

★★★★

Global field Hamiltonian, i. e. such that:  $[H, \phi_l] = H_{\text{gate}}^{(2n)} \phi_l$



$$H = - \sum_l \phi_l^\dagger H_{\text{gate}}^{(2n)} \phi_l \quad (*)$$

# QC SIMULATION OF QFT

## CONNECTION WITH THE USUAL QFT

★★★★

★★★★

Global field Hamiltonian, i. e. such that:  $[H, \phi_l] = H_{\text{gate}}^{(2n)} \phi_l$



$$H = - \sum_l \phi_l^\dagger H_{\text{gate}}^{(2n)} \phi_l \quad (*)$$

For a given field theory to be simulable by a homogeneous quantum computer in the discrete approximation  $\phi(la) = a^{-\frac{1}{2}} \phi_l$  one needs the field Hamiltonian that can be written in the form (\*) with the  $n \geq 1$  satisfying the bound

$$\|H_{\text{gate}}^{(2n)}\| \leq \frac{1}{n\tau}$$

# QC SIMULATION OF QFT

## CONNECTION WITH THE USUAL QFT

★★★★

★★★★

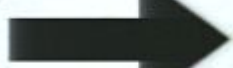
Global field Hamiltonian, i. e. such that:  $[H, \phi_l] = H_{\text{gate}}^{(2n)} \phi_l$



$$H = - \sum_l \phi_l^\dagger H_{\text{gate}}^{(2n)} \phi_l \quad (*)$$

For a given field theory to be simulable by a homogeneous quantum computer in the discrete approximation  $\phi(la) = a^{-\frac{1}{2}} \phi_l$  one needs the field Hamiltonian that can be written in the form (\*) with the  $n \geq 1$  satisfying the bound

$$\|H_{\text{gate}}^{(2n)}\| \leq \frac{1}{n\tau}$$



All known QFT are QC-simulable!



# FIRST QUANTIZATION

## EMERGENCE OF CCR



Constant of motion (number of “particles”)

$$N = \sum_n \phi_n^\dagger \phi_n = \sum_n \sigma_n^3$$

$$\text{or } N = \sum_n a_n^\dagger a_n$$

# FIRST QUANTIZATION

## EMERGENCE OF CCR

★★★★

★★★★

Constant of motion (number of “particles”)

$$N = \sum_n \phi_n^\dagger \phi_n = \sum_n \sigma_n^3 \quad \text{or} \quad N = \sum_n a_n^\dagger a_n$$

Vacuum state (invariant under processing):  $|\mathbf{0}\rangle = \prod_n |0\rangle_n$

# FIRST QUANTIZATION

## EMERGENCE OF CCR

★★★★

★★★★

Constant of motion (number of “particles”)

$$N = \sum_n \phi_n^\dagger \phi_n = \sum_n \sigma_n^3 \quad \text{or} \quad N = \sum_n a_n^\dagger a_n$$

Vacuum state (invariant under processing):  $|\mathbf{0}\rangle = \prod_n |0\rangle_n$

Single-particle states:  $|\phi_n^\alpha\rangle := \phi_n^{\alpha\dagger} |\mathbf{0}\rangle$  (ppm information encoding!)



# FIRST QUANTIZATION

## EMERGENCE OF CCR

★★★★

★★★★

Constant of motion (number of “particles”)

$$N = \sum_n \phi_n^\dagger \phi_n = \sum_n \sigma_n^3 \quad \text{or} \quad N = \sum_n a_n^\dagger a_n$$

Vacuum state (invariant under processing):  $|\mathbf{0}\rangle = \prod_n |0\rangle_n$

Single-particle states:  $|\phi_n^\alpha\rangle := \phi_n^{\alpha\dagger} |\mathbf{0}\rangle$  (ppm information encoding!)

$$P^\alpha = -i\hbar \sum_n |\phi_n^\alpha\rangle \hat{\partial}_x \langle \phi_n^\alpha|, \quad X^\alpha = 2a \sum_n |\phi_n^\alpha\rangle n \langle \phi_n^\alpha|.$$

# FIRST QUANTIZATION

## EMERGENCE OF CCR

★★★★

★★★★

Constant of motion (number of “particles”)

$$N = \sum_n \phi_n^\dagger \phi_n = \sum_n \sigma_n^3 \quad \text{or} \quad N = \sum_n a_n^\dagger a_n$$

Vacuum state (invariant under processing):  $|\mathbf{0}\rangle = \prod_n |0\rangle_n$

Single-particle states:  $|\phi_n^\alpha\rangle := \phi_n^{\alpha\dagger} |\mathbf{0}\rangle$  (ppm information encoding!)

$$P^\alpha = -i\hbar \sum_n |\phi_n^\alpha\rangle \hat{\partial}_x \langle \phi_n^\alpha|, \quad X^\alpha = 2a \sum_n |\phi_n^\alpha\rangle n \langle \phi_n^\alpha|.$$

$$[X^\alpha, P^\beta] = i\hbar \delta_{\alpha\beta} I_\alpha$$

# FIRST QUANTIZATION

Single-"particle" Schrödinger equation in ppm representation:

$$\Psi = \begin{bmatrix} \dots \\ \langle \phi_n^+ | \Psi \rangle \\ \langle \phi_n^- | \Psi \rangle \\ \langle \phi_{n+1}^+ | \Psi \rangle \\ \langle \phi_{n+1}^- | \Psi \rangle \\ \dots \end{bmatrix} \quad i\hat{\partial}_t \langle \phi_n^\alpha | \Psi \rangle = \langle \mathbf{0} | [\mathbf{H}_{\text{gate}}^{(4)} \phi_n]^\alpha | \Psi \rangle = \sum_{m\beta} H_{n\alpha, m\beta} \langle \phi_m^\beta | \Psi \rangle$$

$$H = c \begin{bmatrix} \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & 0 & \lambda & \frac{i\zeta}{4a} & 0 & 0 & 0 & \dots & \dots \\ \dots & \dots & \lambda & 0 & 0 & -\frac{i\zeta}{4a} & 0 & 0 & \dots & \dots \\ \dots & \dots & -\frac{i\zeta}{4a} & 0 & 0 & \lambda & \frac{i\zeta}{4a} & 0 & \dots & \dots \\ \dots & \dots & 0 & \frac{i\zeta}{4a} & \lambda & 0 & 0 & -\frac{i\zeta}{4a} & \dots & \dots \\ \dots & \dots & 0 & 0 & -\frac{i\zeta}{4a} & 0 & 0 & \lambda & \dots & \dots \\ \dots & \dots & 0 & 0 & 0 & \frac{i\zeta}{4a} & \lambda & 0 & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \end{bmatrix}$$

$$i\hat{\partial}_t \Psi = H\Psi$$

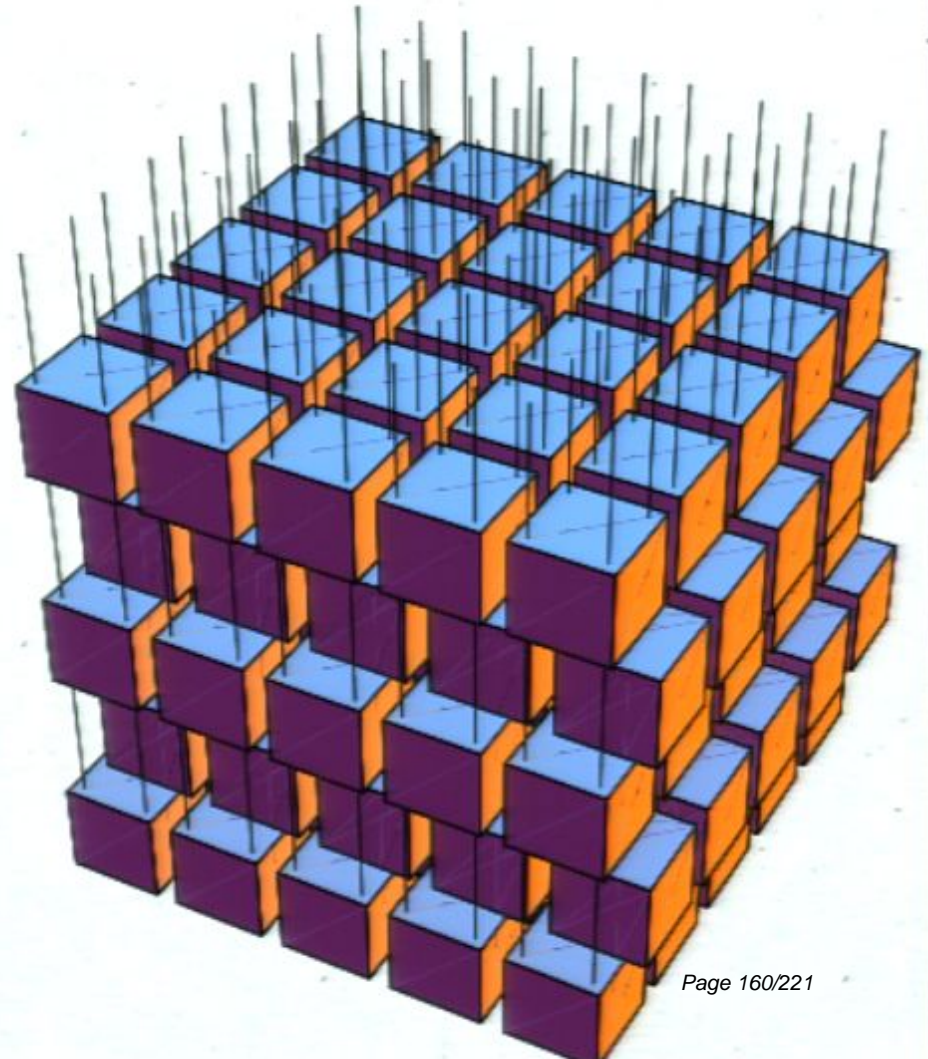


# QC SIMULATION OF QFT

QCFT FOR MORE THAN 1 SPACE DIM?



Need six space field operators...



# QC SIMULATION OF QFT

## QCFT FOR MORE THAN 1 SPACE DIM?

★★★★

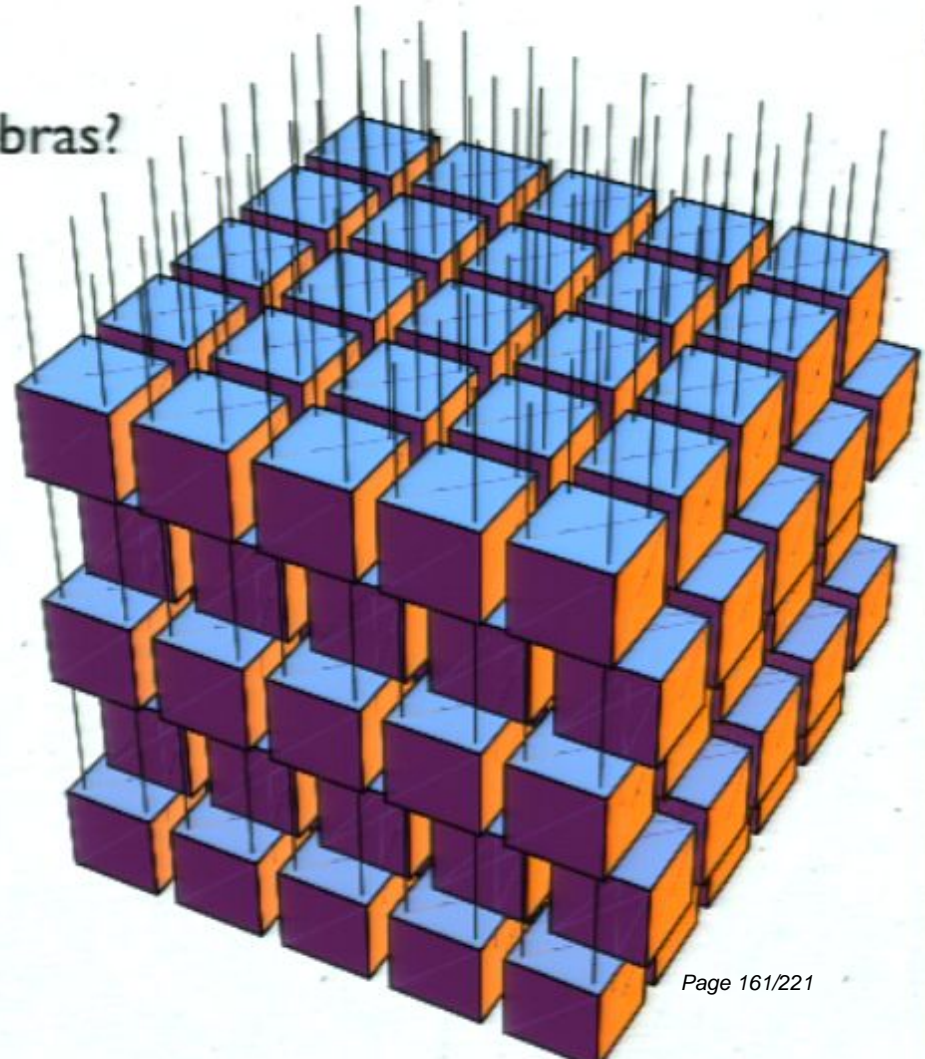
★★★★

Need six space field operators...

Anticommuting fields in terms of local algebras?

Do we really need anticommuting fields?  
(Grassman variables? Microcausality and  
parastatistics...)

*Do we need fields?*





# QC SIMUL

## QCFT FOR MORE THAN 1 SPACE DIM

★★★★

Need six space field operators...

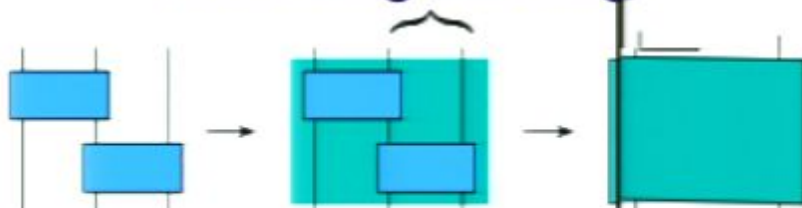
Anticommuting fields in terms of local algebras?

Do we really need anticommuting fields?  
(Grassman variables? Microcausality and parastatistics...)

**Do we need fields?**

**For having Lorentz covariance as manifest ...**

### Coarse-graining





---

---

# A NEW QCFT?

**COMPARE WITH THE USUAL QFT**

★ ★ ★ ★

★ ★ ★ ★

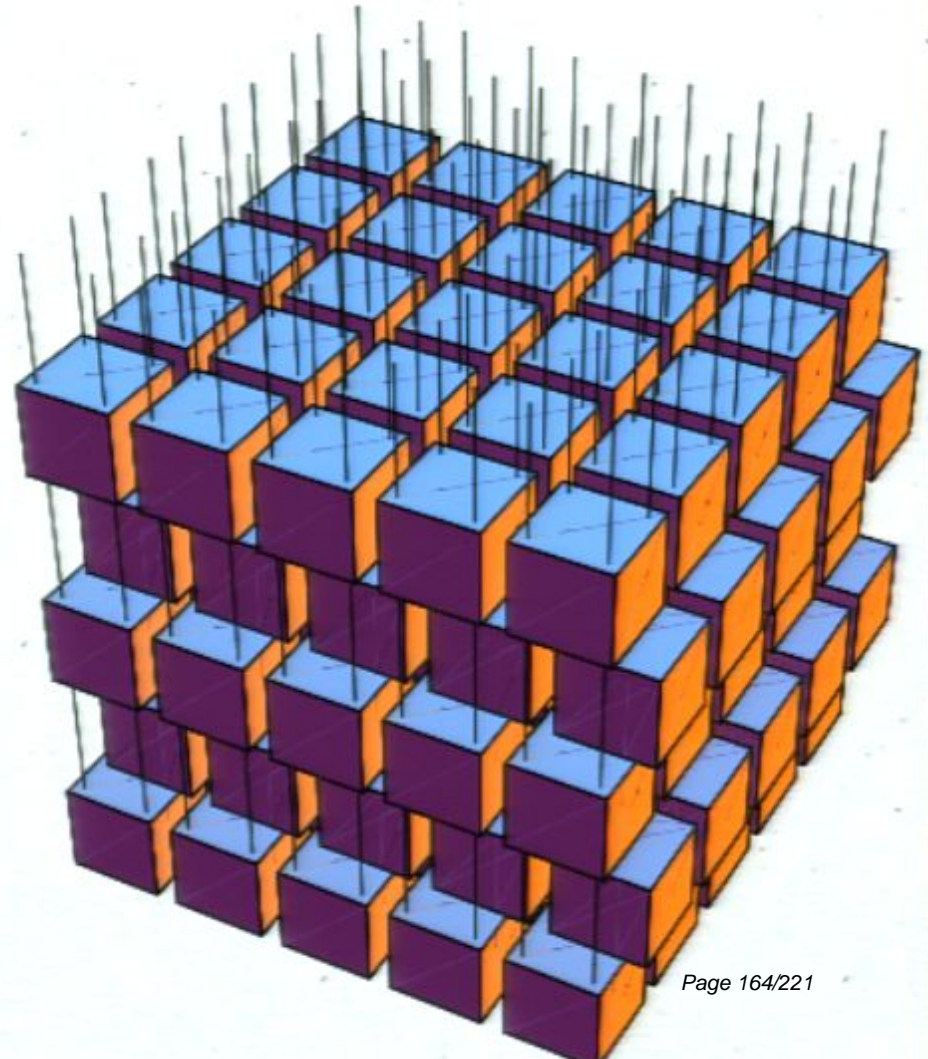
Regard the QCFT as the “true theory” at the Planck scale, and the usual QFT as an approximation for “mesoscopic” scale

# QC SIMULATION OF QFT

QCFT FOR MORE THAN 1 SPACE DIM?



Need six space field operators...



# QC SIMULATION OF QFT

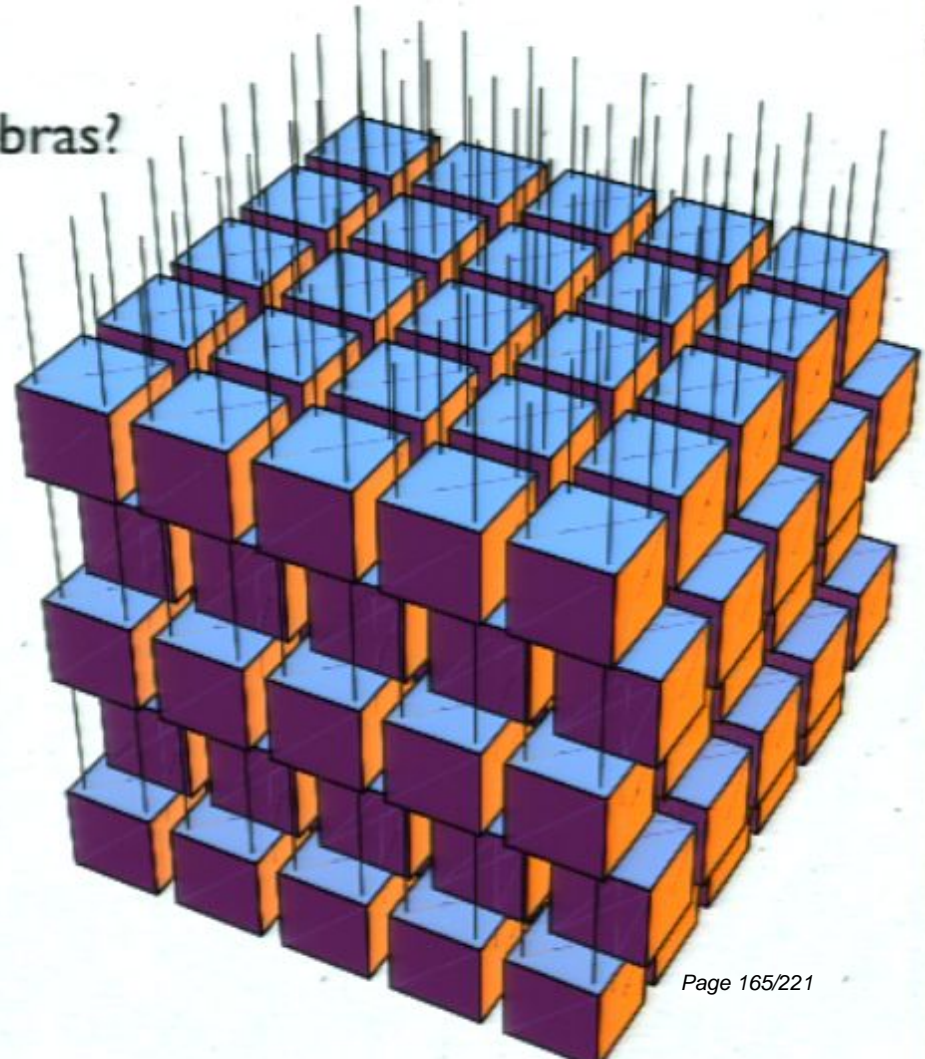
## QCFT FOR MORE THAN 1 SPACE DIM?



Need six space field operators...

Anticommuting fields in terms of local algebras?

Do we really need anticommuting fields?  
(Grassman variables? Microcausality and  
parastatistics...)





# QC SIMULATION OF QFT

## QCFT FOR MORE THAN 1 SPACE DIM?

★★★★

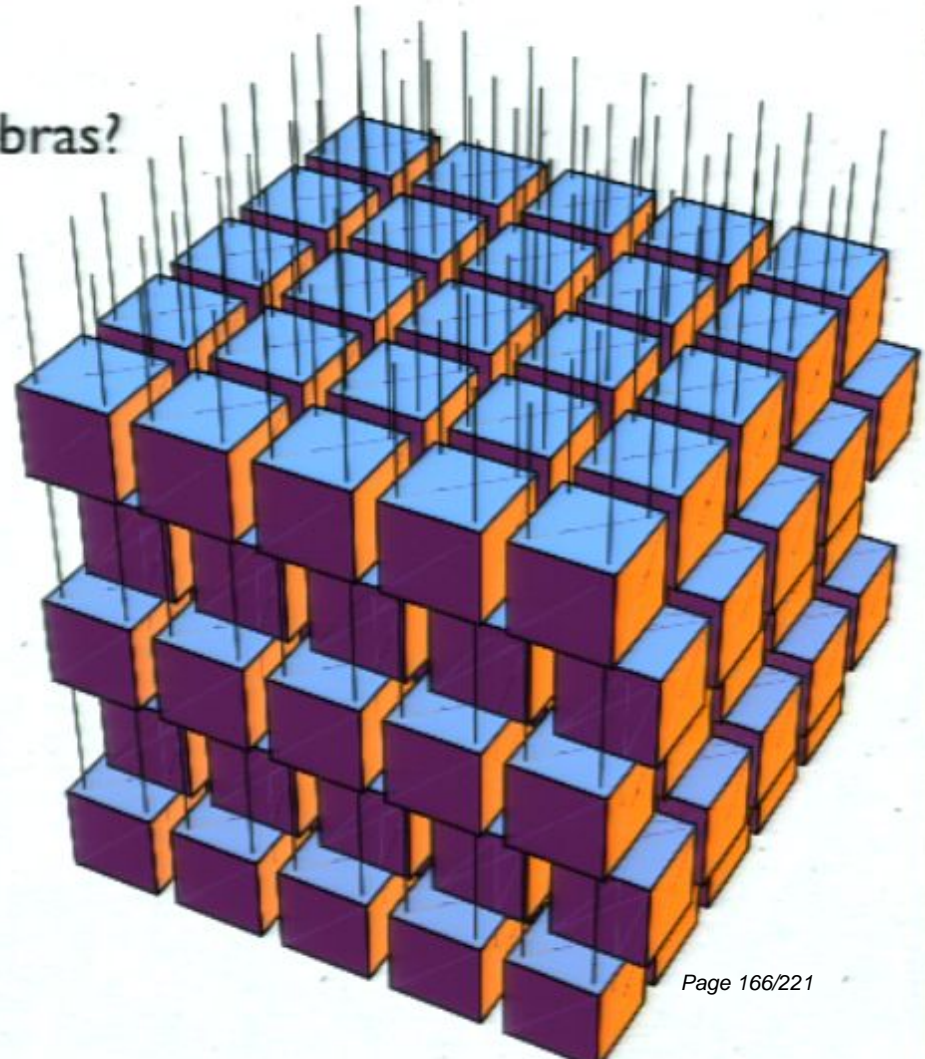
★★★★

Need six space field operators...

Anticommuting fields in terms of local algebras?

Do we really need anticommuting fields?  
(Grassman variables? Microcausality and parastatistics...)

***Do we need fields?***



# QC SIMULATION OF QFT

## QCFT FOR MORE THAN 1 SPACE DIM?

★★★★

★★★★

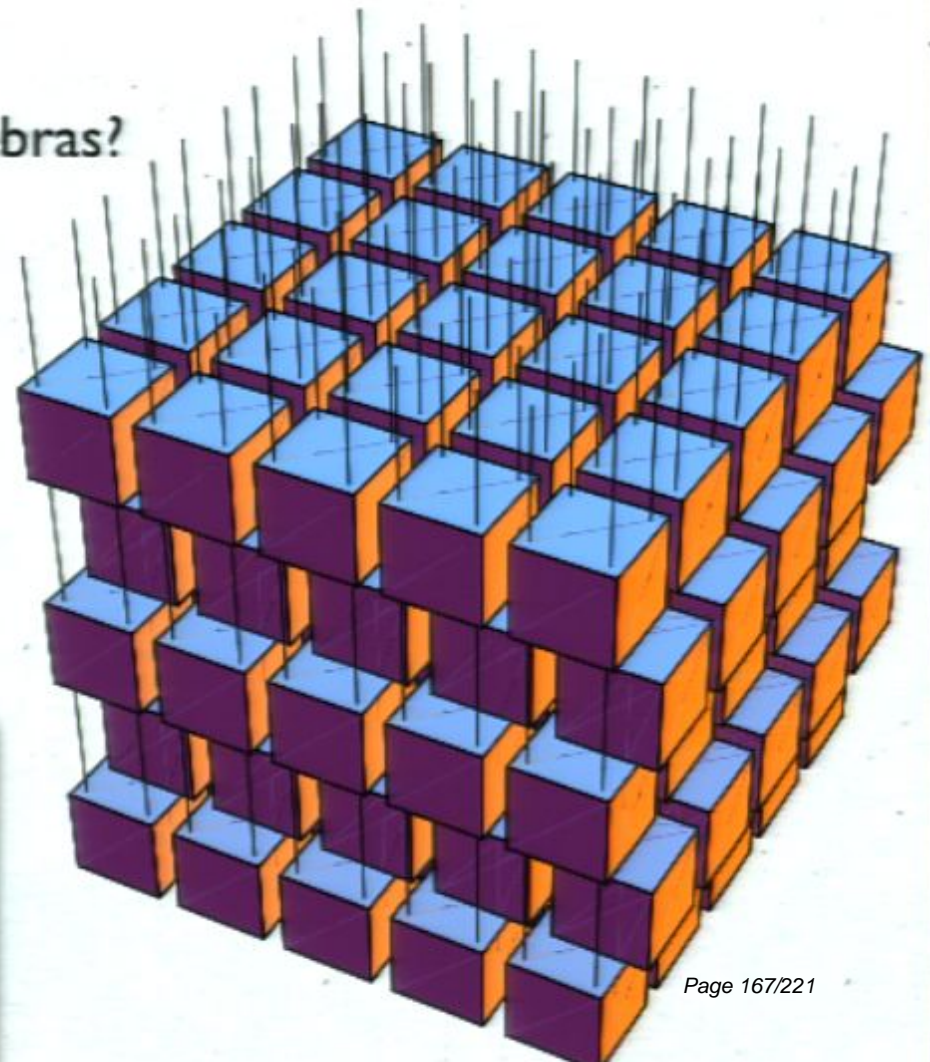
Need six space field operators...

Anticommuting fields in terms of local algebras?

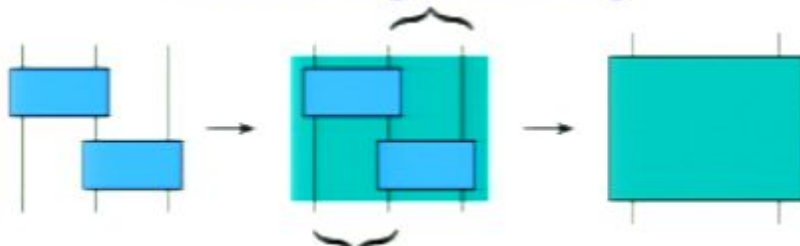
Do we really need anticommuting fields?  
(Grassman variables? Microcausality and parastatistics...)

**Do we need fields?**

**For having Lorentz covariance  
as manifest ...**



### Coarse-graining





---

---

# A NEW QCFT?

**COMPARE WITH THE USUAL QFT**

★ ★ ★ ★

★ ★ ★ ★

Regard the QCFT as the “true theory” at the Planck scale, and the usual QFT as an approximation for “mesoscopic” scale



# A NEW QCFT?

COMPARE WITH THE USUAL QFT

Regard the QCFT as the “true theory” at the Planck scale, and the usual QFT as an approximation for “mesoscopic” scale

QCFT solve many problems that plague QFT:

- \* Feynman's path integral
- \* u.v. renormalization
- \* no need of quantization rules (emergent)
- \* problems related to the continuous
- \* ...

---

---

# A NEW QCFT?

**COMPARE WITH THE USUAL QFT**



Regard the QCFT as the “true theory” at the Planck scale, and the usual QFT as an approximation for “mesoscopic” scale

# A NEW

COMPARE WITH

# QCFT?

THE USUAL QFT

and the QCFT as the "true theory" at the Planck scale  
usual QFT as an approximation

theory" at the Planck scale  
ation for "mesoscopic" scales

QCFT solve many problems that

that plague QFT:

Feynman's path integral

renormalization

need of quantization rules

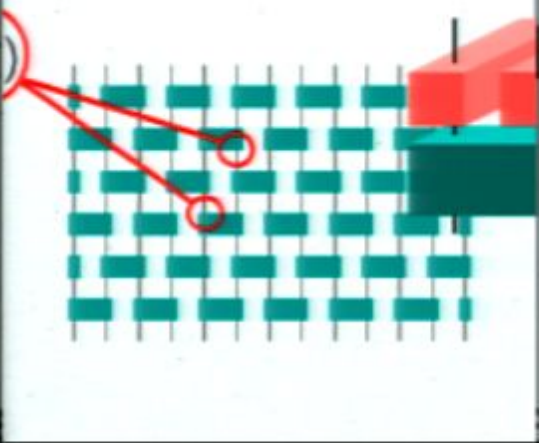
problems related to the continuous

scales (emergent)

continuous

## A NEW QCFT?

GAUGE INVARIANCE





---

---

# A NEW QCFT?

**COMPARE WITH THE USUAL QFT**

★ ★ ★ ★

★ ★ ★ ★

Regard the QCFT as the “true theory” at the Planck scale, and the usual QFT as an approximation for “mesoscopic” scale

# A NEW QCFT?

COMPARE WITH THE USUAL QFT

★★★★

★★★★

Regard the QCFT as the “true theory” at the Planck scale, and the usual QFT as an approximation for “mesoscopic” scale

QCFT solve many problems that plague QFT:

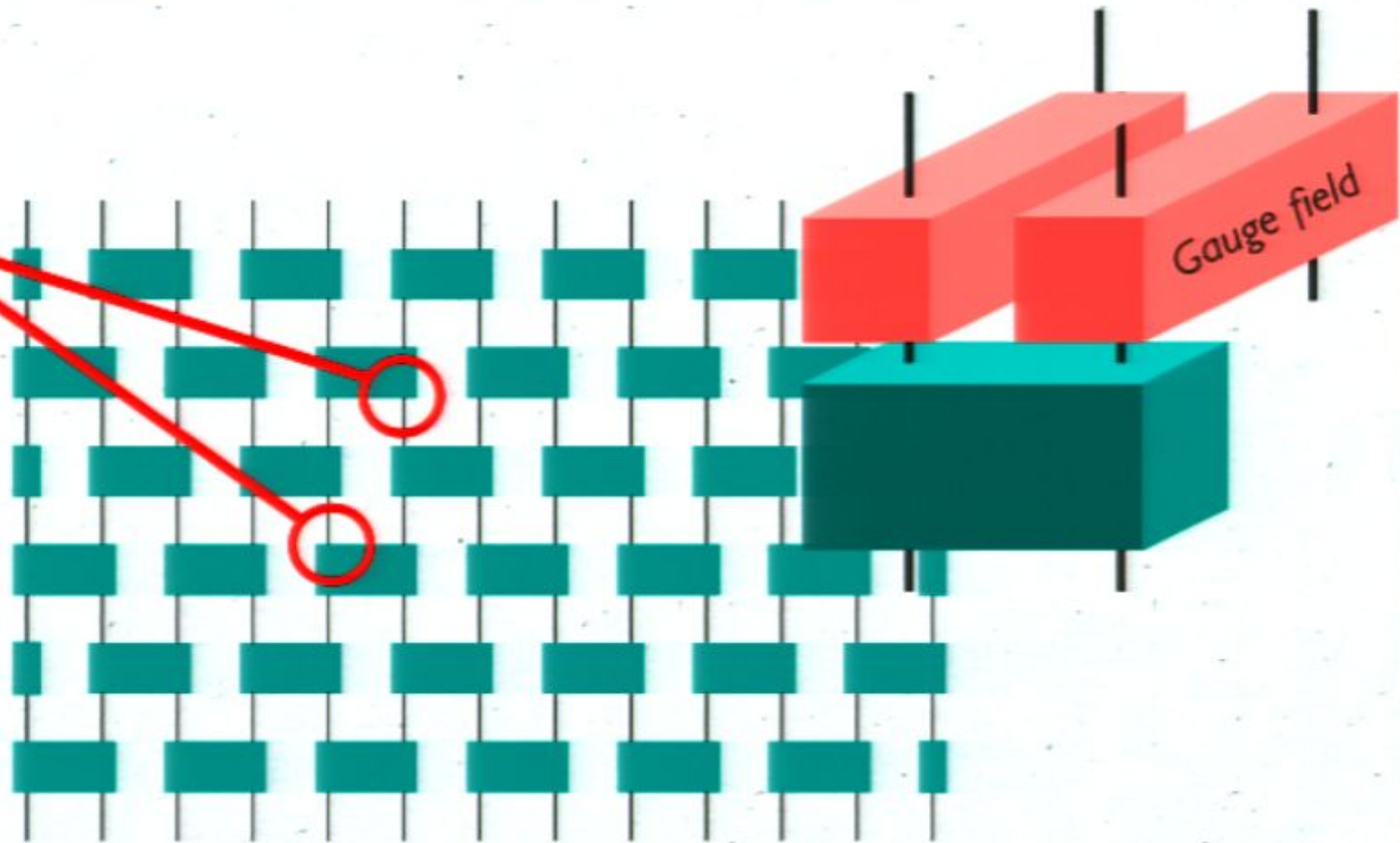
- \* Feynman's path integral
- \* u.v. renormalization
- \* no need of quantization rules (emergent)
- \* problems related to the continuous
- \* ...

# A NEW QCFT?

## GAUGE INVARIANCE



$U(x)$



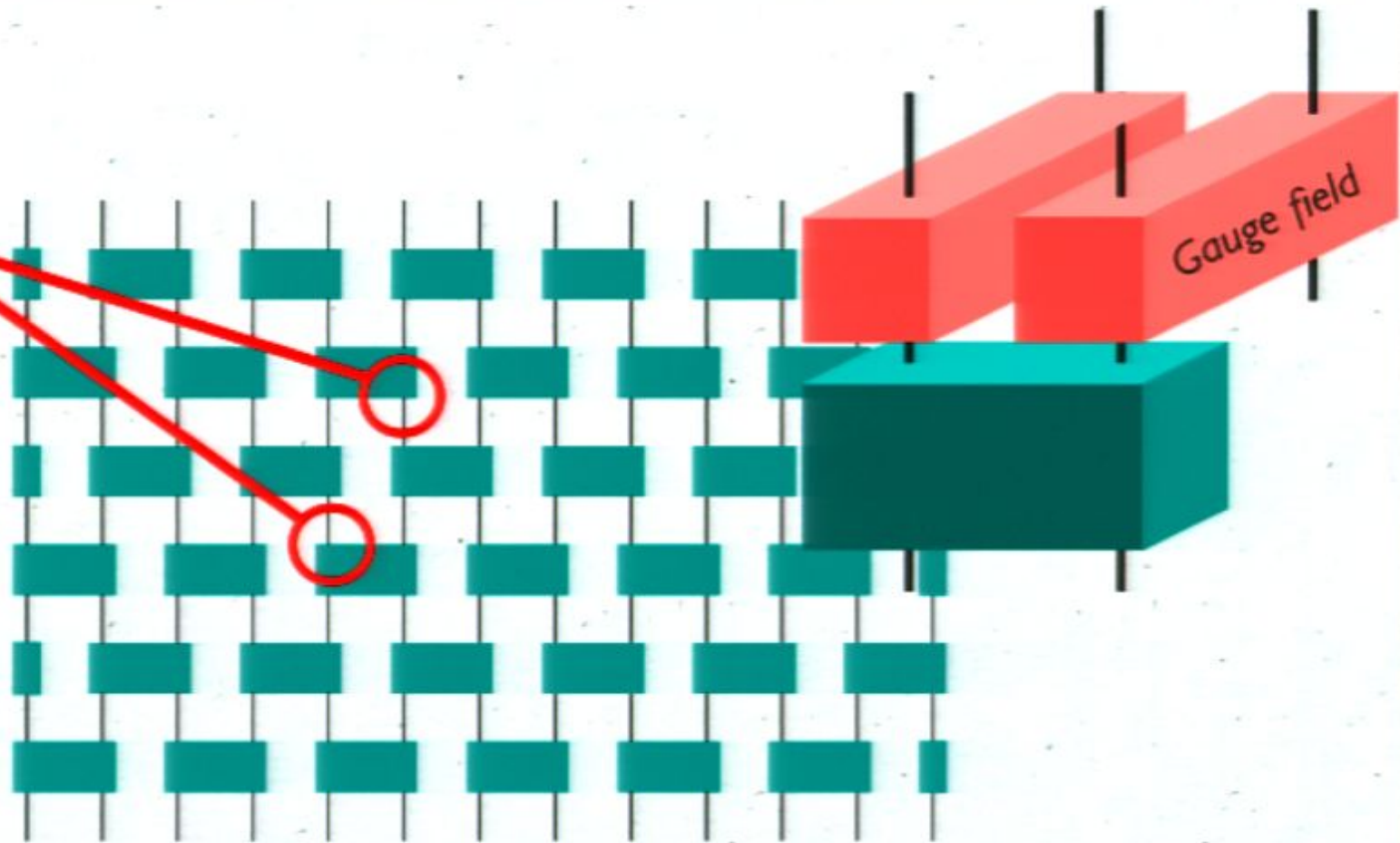


# A NEW QCFT?

GAUGE INVARIANCE



$U(x)$



**Native nonabelian Gauge theory!**  
and on ... foliation !!!



**Good for QGravity?**

---

---

# CONCLUSIONS

---

---

## PHYSICS IS INFORMATION

---

---



- \* Quantum Theory is an information theory
- \* Space-time and relativistic covariance emerge from the information processing
- \* Information flow is the free QFT
- \* Physics is emergent (inertial mass, Planck constant, quantization rules, ...)
- \* A new QCFT:
  - \* has no space-background (QG-ready)
  - \* doesn't need quantization
  - \* cures many problems that plague QFT
  - \* **opens a route to foundations of QFT**

# TODO SOON

## PHYSICS IS INFORMATION

- \* Quantization rules as emergent (needs interpretation) ✓
- \* General correspondence Lagrangian-gates ✓
- \* Build up a complete QCFT for Dirac in 3 space dimensions ✓
- \* Emergent unitary representation of the Lorentz group ✓
- \* The need of the field (anticommuting fields, parastatistics,...) ?
- \* Informational meaning of energy, gravitational mass,... ?
- \* Violations of Lorentz-covariance... ?



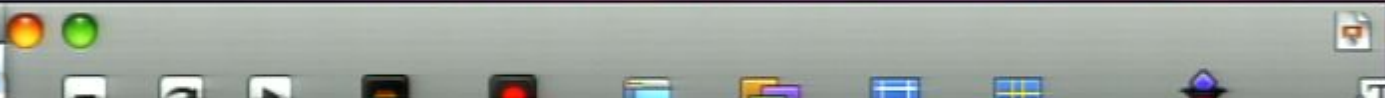
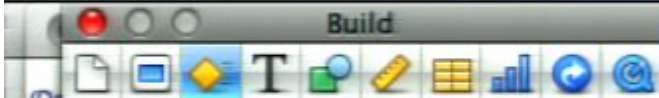
---

---

**THANK YOU**

---

---



THANK YOU

Build In Build Out Action

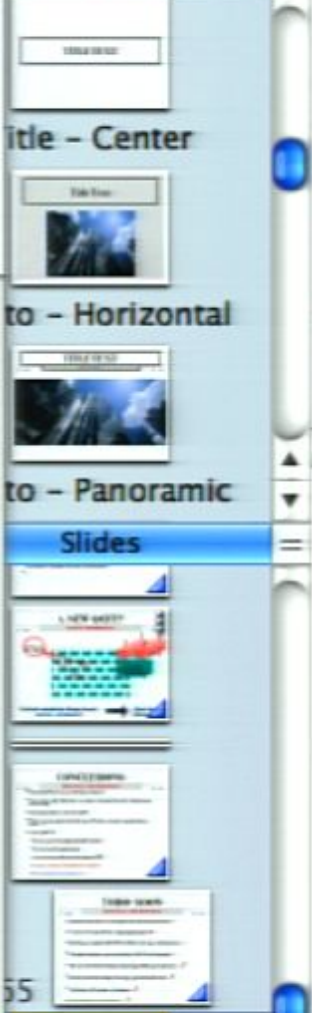
Effect  
None

Direction Order

Delivery Duration

More Options

Master Slides



THANK YOU

Build In Build Out Action

Effect  
None

Direction Order

Delivery Duration

More Options

Master Slides

- Table of Contents
- Title - Center
- Title - Top
- Title - Horizontal
- Title - Panoramic
- Slides



100%



Build

QC SIMULATION OF QFT

CONNECTION WITH THE USUAL QFT

Global field Hamiltonian, i.e. such that:  $[H, \phi] = H^{(2N)} \phi$

→  $H = - \sum_j \phi_j H_{\text{gate}}^{(2N)} \phi_j$  (\*)

For a given field theory to be simulable by a homogeneous quantum computer in the discrete approximation  $\phi(x) = a^{-1} \phi_j$  one needs the field Hamiltonian that can be written in the form (\*) with the  $N \gg 1$  satisfying the bound

$|H_{\text{gate}}^{(2N)}| < \frac{1}{2N}$

→ All known QFT are QC-simulable!

Build In Build Out Action

Effect: None

Direction: Order

Delivery: Duration

More Options

Delete Skip Play Rehearse Record View Themes Masters Guides Smart Builds Text

B I U

Master Slides

Title, Bullets & Photo

Title - Top

Slides

61

# QC SIMULATION

CONNECTION WITH THE USUAL QFT

★★★★

100%

It is worth noticing that for a given field theory to be simulable by a homogeneous quantum computer in the discrete approximation one needs the global field Hamiltonian that can be written in the form ....

This bound generally gives a renormalization of the





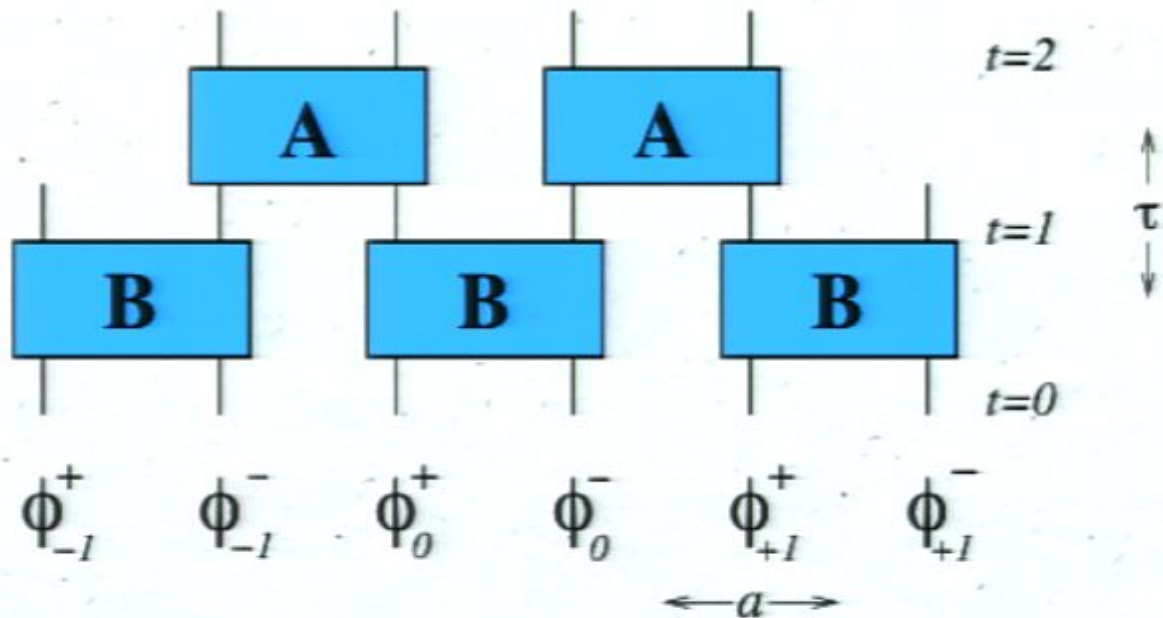




# QC SIMULATION OF QFT

## “Hamiltonian”

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau} \begin{bmatrix} A_{21}B_{21}\delta_- - B_{12}^\dagger A_{12}^\dagger\delta_+ + A_{22}B_{11} - B_{11}^\dagger A_{22}^\dagger & (A_{21}B_{22} - B_{11}^\dagger A_{21}^\dagger)\delta_- + A_{22}B_{12} - B_{12}^\dagger A_{11}^\dagger \\ (A_{12}B_{11} - B_{22}^\dagger A_{12}^\dagger)\delta_+ + A_{11}B_{21} - B_{21}^\dagger A_{22}^\dagger & A_{12}B_{12}\delta_+ - B_{21}^\dagger A_{21}^\dagger\delta_- + A_{11}B_{22} - B_{22}^\dagger A_{11}^\dagger \end{bmatrix}$$



# QC SIMULATION OF QFT

## THE SPINLESS DIRAC EQUATION

Write the "Hamiltonian" as follows:

(inverse) refraction index

$$H_{\text{gate}}^{(4)} = c(\mathbf{H} + i\mathbf{K}\hat{\partial}_x) = ic\zeta\hat{\partial}_x + \omega\sigma_x, \quad \omega = c\lambda^{-1}$$



$$H_{11} = -\frac{1}{2a}\Im(A_{21}B_{21} + A_{22}B_{11}) = 0,$$

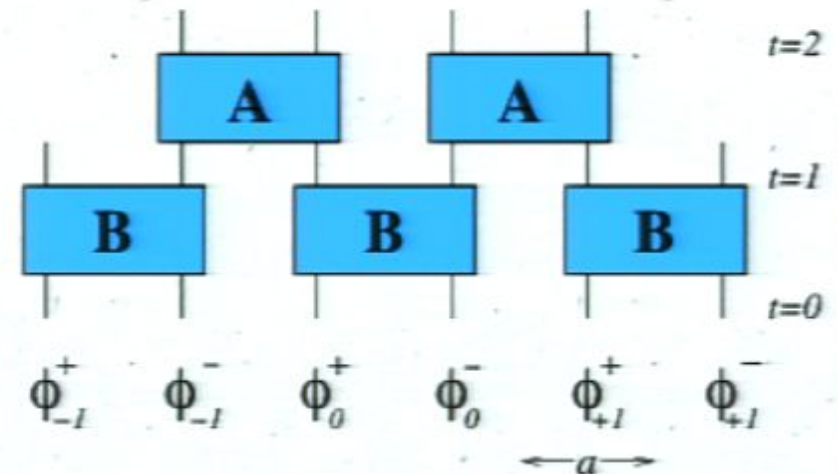
$$H_{12} = \frac{i}{4a}(A_{21}B_{22} - A_{12}^*B_{11}^* + A_{22}B_{12} - A_{11}^*B_{21}^*) = \lambda^{-1}$$

$$H_{22} = -\frac{1}{2a}\Im(A_{12}B_{12} + A_{11}B_{22}) = 0,$$

$$K_{11} = -\Re(A_{21}B_{21}) = \zeta,$$

$$K_{22} = \Re(A_{12}B_{12}) = -\zeta,$$

$$K_{12} = -\frac{1}{2}(A_{21}B_{22} - A_{12}^*B_{11}^*) = 0.$$



$$\mathbf{A} = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} 0 & ie^{i\phi} \\ & \end{bmatrix}$$

# QC SIMULATION OF QFT

## THE SPINLESS DIRAC EQUATION

Write the "Hamiltonian" as follows:

(inverse) refraction index

$$H_{\text{gate}}^{(4)} = c(\mathbf{H} + i\mathbf{K}\hat{\partial}_x) = ic\zeta\hat{\partial}_x + \omega\sigma_x, \quad \omega = c\lambda^{-1}$$



$$H_{11} = -\frac{1}{2a}\Im(A_{21}B_{21} + A_{22}B_{11}) = 0,$$

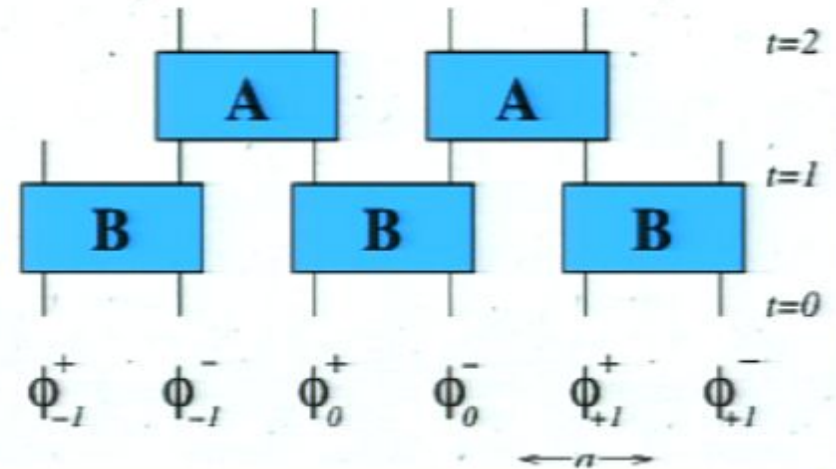
$$H_{12} = \frac{i}{4a}(A_{21}B_{22} - A_{12}^*B_{11}^* + A_{22}B_{12} - A_{11}^*B_{21}^*) = \lambda^{-1}$$

$$H_{22} = -\frac{1}{2a}\Im(A_{12}B_{12} + A_{11}B_{22}) = 0,$$

$$K_{11} = -\Re(A_{21}B_{21}) = \zeta,$$

$$K_{22} = \Re(A_{12}B_{12}) = -\zeta,$$

$$K_{12} = -\frac{1}{2}(A_{21}B_{22} - A_{12}^*B_{11}^*) = 0.$$



$$\mathbf{A} = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} 0 & ie^{i\phi} \end{bmatrix}$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



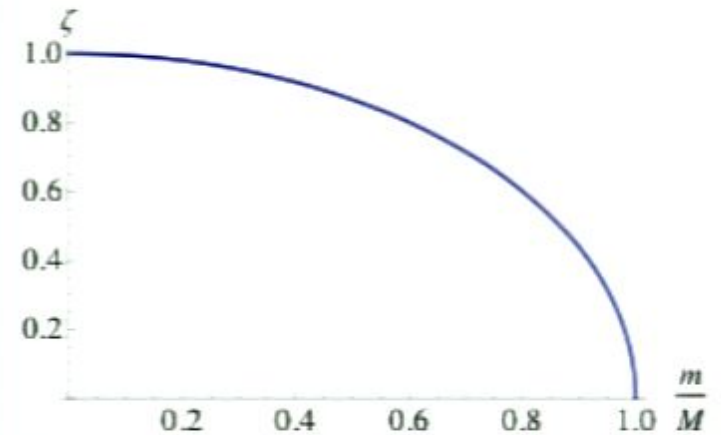
# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

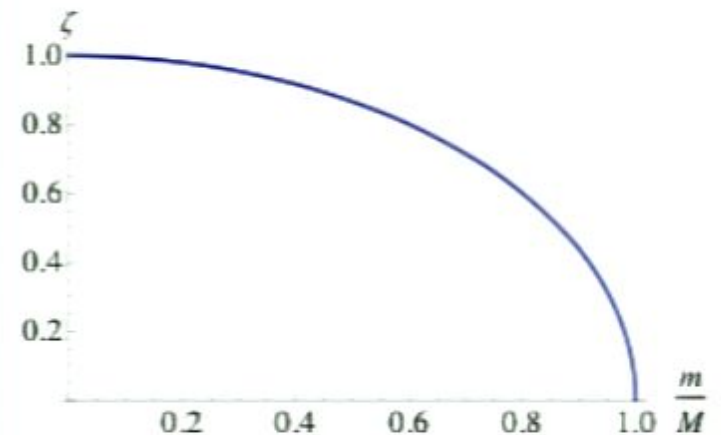
*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

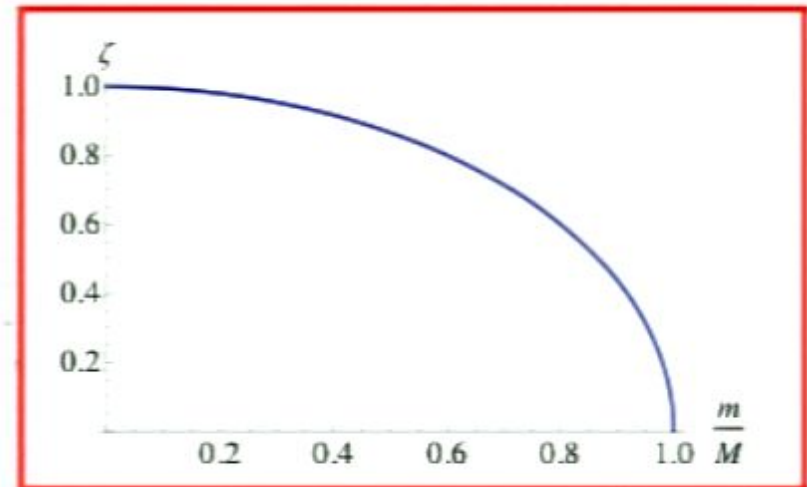
$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger)$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$





# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

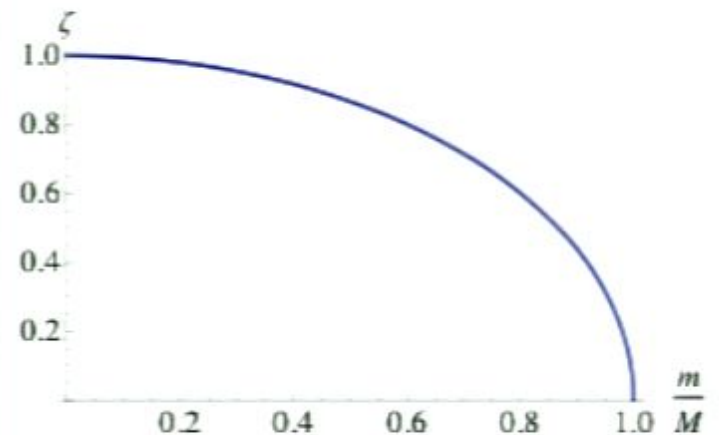
$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq \frac{1}{2\tau}$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

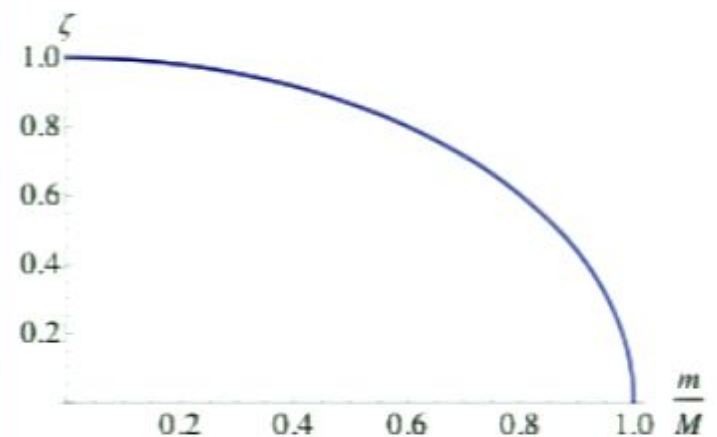
$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq \frac{1}{2\tau}$$

The norm is obtained by FT at  $k = \frac{\pi}{2a}$

$$\frac{\sqrt{\zeta^2 + 4\tau^2\omega^2}}{2\tau} \leq \frac{1}{2\tau}$$

namely for  $\omega = c\lambda^{-1}$  one has:

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$

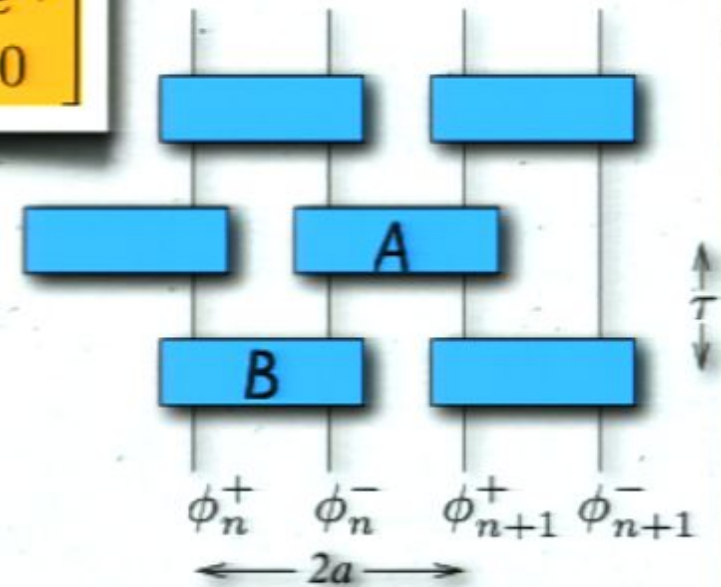


$$\zeta \leq \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$

# QC SIMULATION OF QFT

**SIMPLE SCALAR FIELD IN 1 SPACE DIM.**

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$



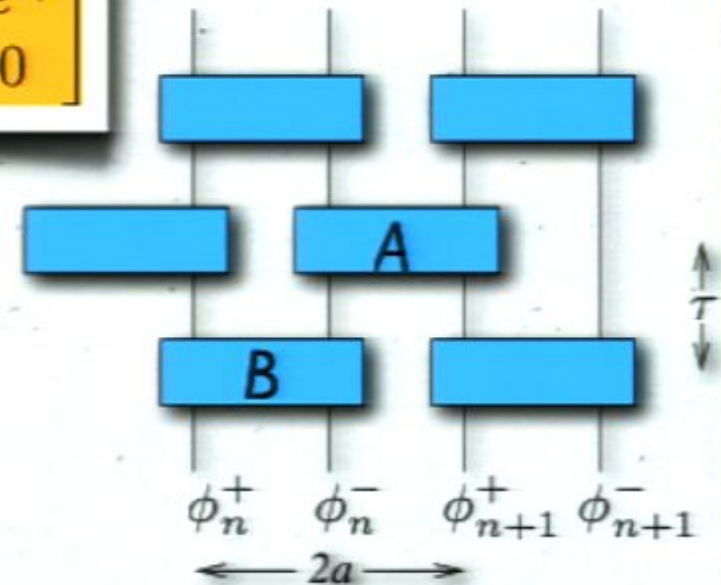


# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

W.l.g. fix  $\phi = 0$ ,  $\psi = -\pi/2$



# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

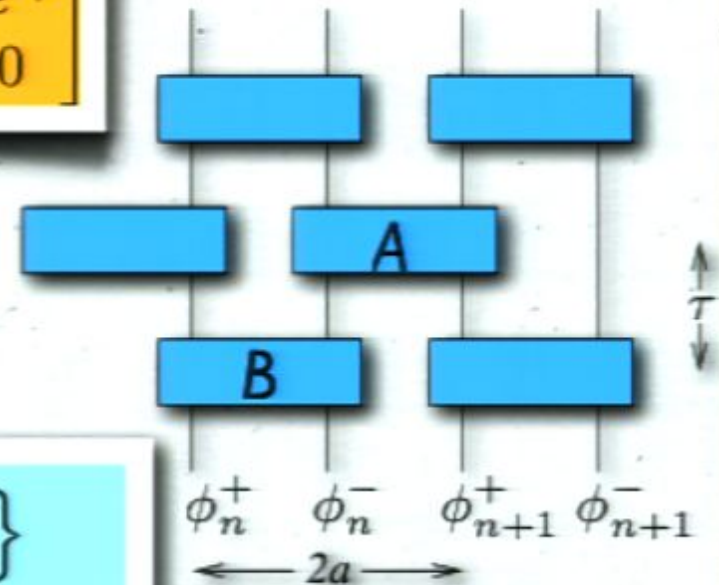
$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

W.l.g. fix  $\phi = 0$ ,  $\psi = -\pi/2$

For both Bose and Fermi fields one has:

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$



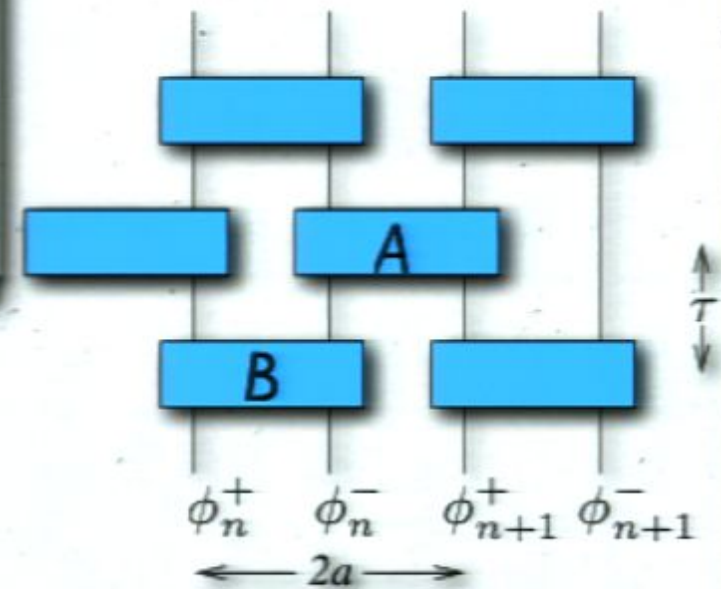
# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$

Commuting	Anticommuting
Harmonic oscillator	Clifford algebra
$[a_l, a_k^\dagger] = \delta_{lk}$	$\phi_n^+ = \sigma_{2n}^- \prod_{k=-\infty}^{n-1} \sigma_{2k+1}^z \sigma_{2k}^z$
$\phi_n^+ = a_{2n} \quad \phi_n^- = a_{2n+1}$	$\phi_n^- = \sigma_{2n+1}^- \sigma_{2n}^z \prod_{k=-\infty}^{n-1} \sigma_k^z$



A

B



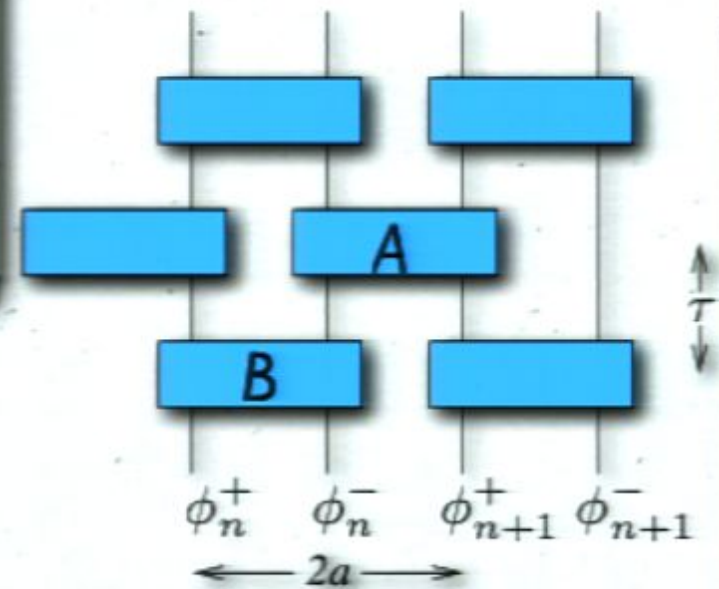
# QC SIMULATION OF QFT

**SIMPLE SCALAR FIELD IN 1 SPACE DIM.**

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$

Commuting	Anticommuting
Harmonic oscillator	Clifford algebra
$[a_l, a_k^\dagger] = \delta_{lk}$	$\phi_n^+ = \sigma_{2n}^- \prod_{k=-\infty}^{n-1} \sigma_{2k+1}^z \sigma_{2k}^z$
$\phi_n^+ = a_{2n} \quad \phi_n^- = a_{2n+1}$	$\phi_n^- = \sigma_{2n+1}^- \sigma_{2n}^z \prod_{k=-\infty}^{n-1} \sigma_k^z$



$$A = \exp \left[ -i\theta \left( \sigma_{2n-1}^- \sigma_{2n}^+ + \sigma_{2n-1}^+ \sigma_{2n}^- \right) \right]$$

$$B = \exp \left[ -i\frac{\pi}{2} \left( \sigma_{2n}^+ \sigma_{2n+1}^- + \sigma_{2n}^- \sigma_{2n+1}^+ \right) \right]$$

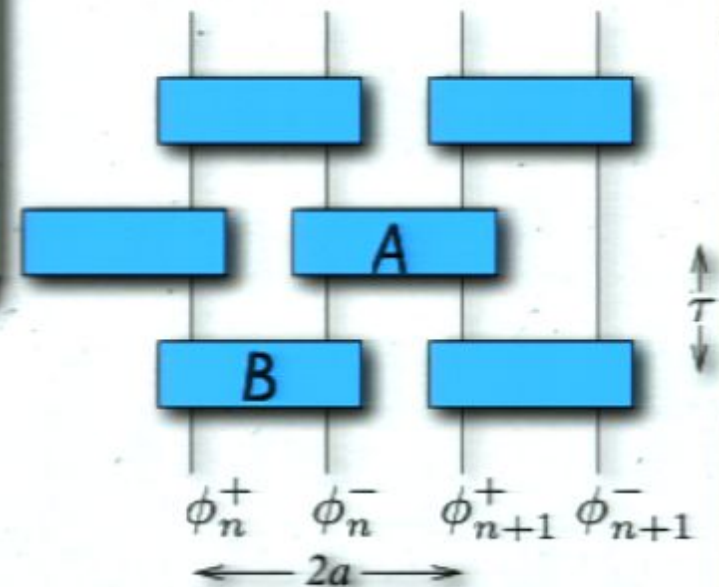
**Gates act on local algebras only!**

# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

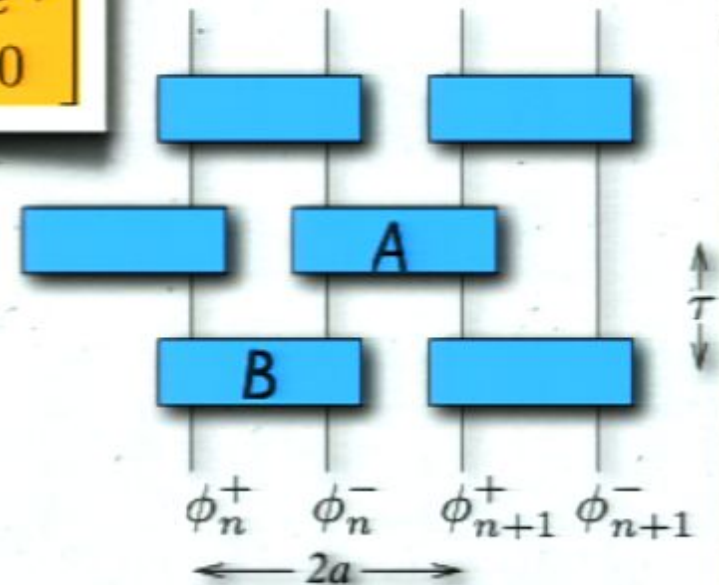
$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$



# QC SIMULATION OF QFT

**SIMPLE SCALAR FIELD IN 1 SPACE DIM.**

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

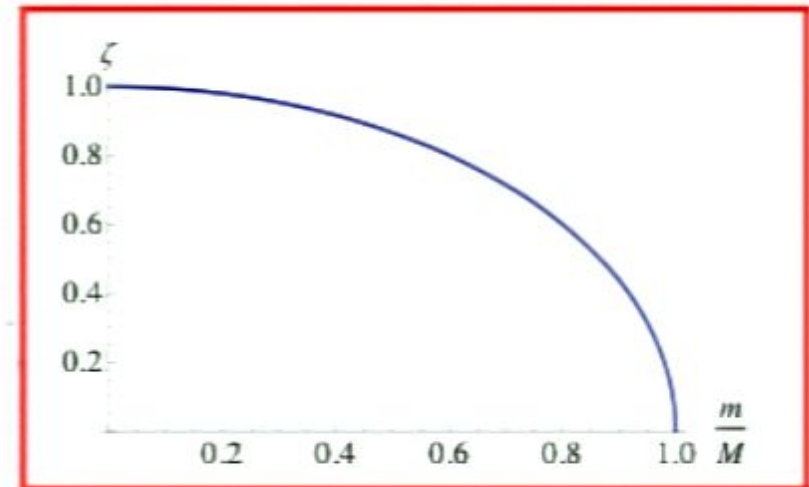




# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

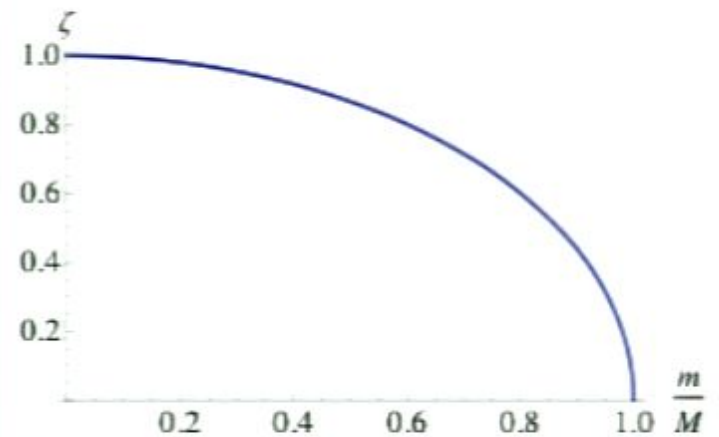
$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$



# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

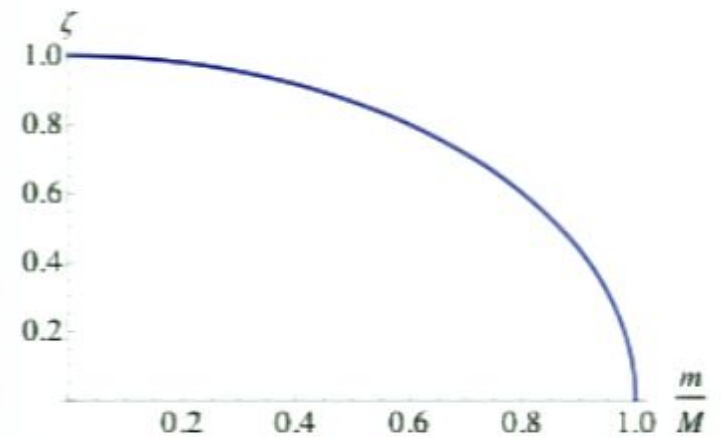
$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq$$

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$





# MASS-DEPENDENT REFRACTION INDEX OF VACUUM

*General phenomenon due to unitarity*

**Proof.** We need the gate-Hamiltonian:

$$H_{\text{gate}}^{(2n)} = ic\zeta\sigma_3\hat{\partial}_x + \omega\sigma_1$$

We must have the same number  $n$  of time-steps and of space-steps, and from the form of the Hamiltonian we get  $n=2$ .

The Hamiltonian is Hermitian, whence:

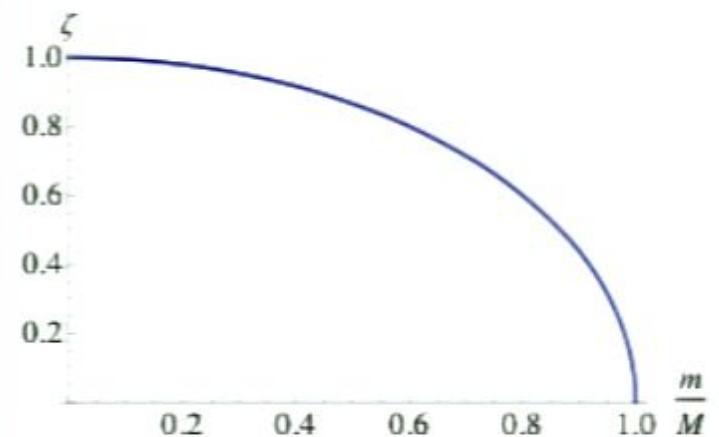
$$H_{\text{gate}}^{(4)} = \frac{i}{4\tau}(U_f - U_f^\dagger) \longrightarrow \|H_{\text{gate}}^{(4)}\| \leq \frac{1}{2\tau}$$

The norm is obtained by FT at  $k = \frac{\pi}{2a}$

$$\frac{\sqrt{\zeta^2 + 4\tau^2\omega^2}}{2\tau} \leq \frac{1}{2\tau}$$

namely for  $\omega = c\lambda^{-1}$  one has:

$$\sin \theta = \zeta = \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$

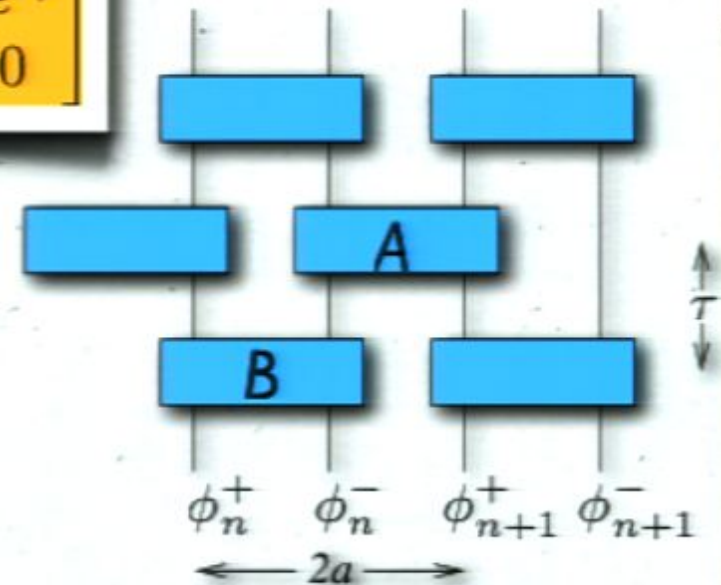


$$\zeta \leq \sqrt{1 - \left(\frac{2a}{\lambda}\right)^2}$$

# QC SIMULATION OF QFT

SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

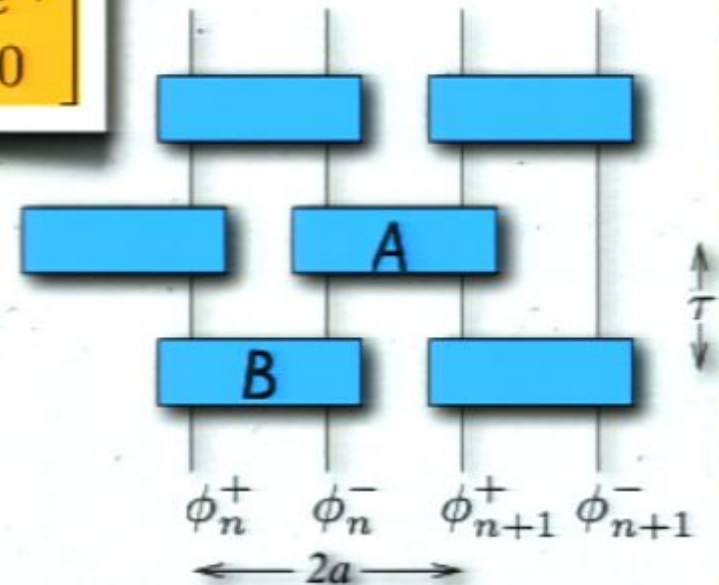


# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

W.l.g. fix  $\phi = 0$ ,  $\psi = -\pi/2$





# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

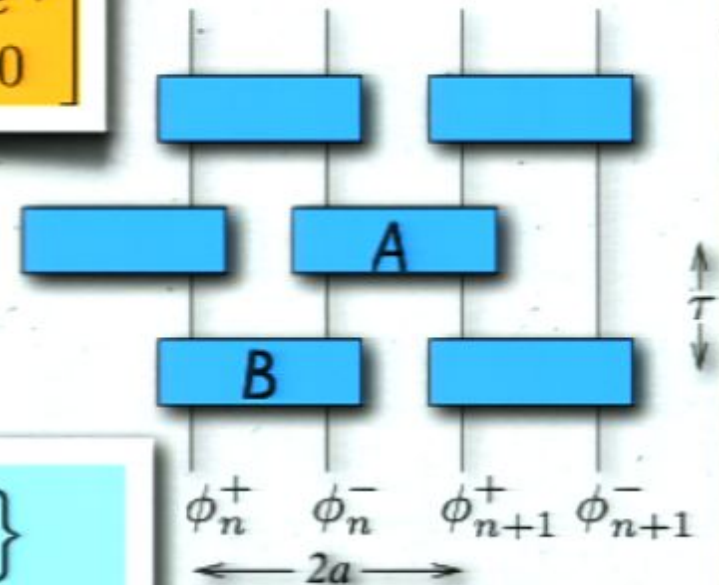
$$A = \begin{bmatrix} e^{i\phi} \cos \theta & e^{i\psi} \sin \theta \\ -e^{-i\psi} \sin \theta & e^{-i\phi} \cos \theta \end{bmatrix} \quad B = \begin{bmatrix} 0 & ie^{i\phi} \\ -ie^{-i\phi} & 0 \end{bmatrix}$$

W.l.g. fix  $\phi = 0$ ,  $\psi = -\pi/2$

For both Bose and Fermi fields one has:

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$



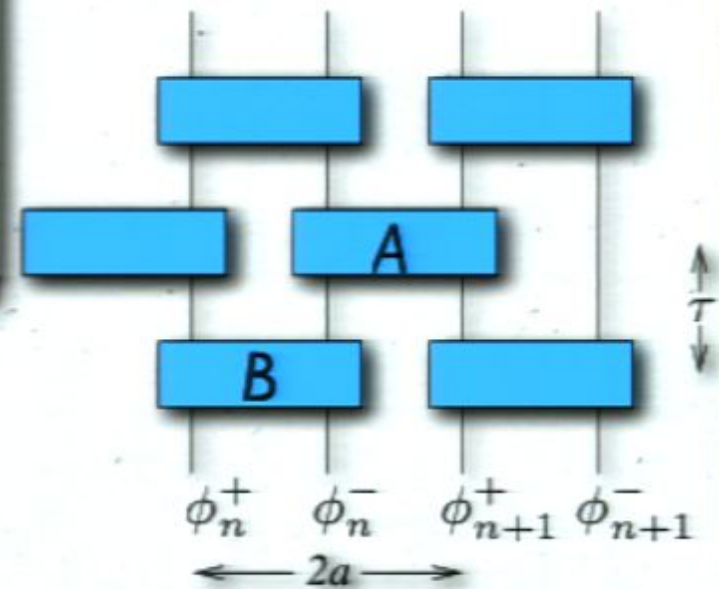
# QC SIMULATION OF QFT

## SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$

Commuting	Anticommuting
Harmonic oscillator	Clifford algebra
$[a_l, a_k^\dagger] = \delta_{lk}$	$\phi_n^+ = \sigma_{2n}^- \prod_{k=-\infty}^{n-1} \sigma_{2k+1}^z \sigma_{2k}^z$
$\phi_n^+ = a_{2n} \quad \phi_n^- = a_{2n+1}$	$\phi_n^- = \sigma_{2n+1}^- \sigma_{2n}^z \prod_{k=-\infty}^{n-1} \sigma_k^z$





# QC SIMULATION OF QFT

**SIMPLE SCALAR FIELD IN 1 SPACE DIM.**

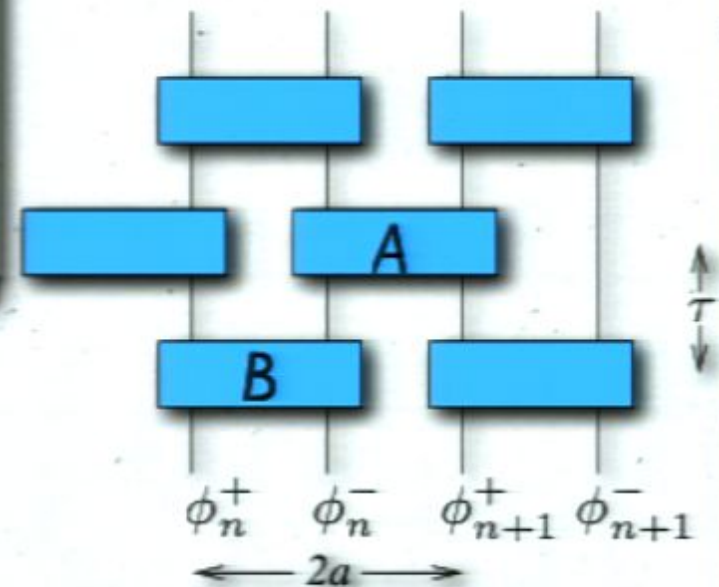
★★★★

★★★★

$$A = \exp \left\{ i\theta \left[ \phi_n^{+\dagger} \phi_{n-1}^- + \phi_{n-1}^{-\dagger} \phi_n^+ \right] \right\}$$

$$B = \exp \left\{ i\frac{\pi}{2} \left[ \phi_n^{+\dagger} \phi_n^- + \phi_n^{-\dagger} \phi_n^+ \right] \right\}$$

Commuting	Anticommuting
Harmonic oscillator	Clifford algebra
$[a_l, a_k^\dagger] = \delta_{lk}$	$\phi_n^+ = \sigma_{2n}^- \prod_{k=-\infty}^{n-1} \sigma_{2k+1}^z \sigma_{2k}^z$
$\phi_n^+ = a_{2n} \quad \phi_n^- = a_{2n+1}$	$\phi_n^- = \sigma_{2n+1}^- \sigma_{2n}^z \prod_{k=-\infty}^{n-1} \sigma_k^z$



$$A = \exp \left[ -i\theta \left( \sigma_{2n-1}^- \sigma_{2n}^+ + \sigma_{2n-1}^+ \sigma_{2n}^- \right) \right]$$

$$B = \exp \left[ -i\frac{\pi}{2} \left( \sigma_{2n}^+ \sigma_{2n+1}^- + \sigma_{2n}^- \sigma_{2n+1}^+ \right) \right]$$

**Gates act on local algebras only!**



Build

QC SIMULATION OF QFT  
SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$A = \exp\{i\theta [\hat{a}_1^\dagger \hat{a}_{2-1} + \hat{a}_{1-1}^\dagger \hat{a}_2]\}$   
 $B = \exp\{i\frac{\theta}{2} [\hat{a}_1^\dagger \hat{a}_2 + \hat{a}_1^\dagger \hat{a}_2^\dagger]\}$

Commuting	Anticommuting
Heisenberg oscillator	Clifford algebra
$[\hat{a}_1, \hat{a}_2] = i\hbar$	$\{\hat{c}_1, \hat{c}_2\} = \hbar$
$\hat{a}_1^\dagger \hat{a}_1 = \hat{N}_1$	$\hat{c}_1^\dagger \hat{c}_1 = \hat{N}_1$
$\hat{a}_2^\dagger \hat{a}_2 = \hat{N}_2$	$\hat{c}_2^\dagger \hat{c}_2 = \hat{N}_2$

→  $A = \exp[-i\theta (\hat{\sigma}_{2-1}^x \hat{\sigma}_2^z + \hat{\sigma}_{1-1}^x \hat{\sigma}_1^z)]$   
 $B = \exp[-i\frac{\theta}{2} (\hat{\sigma}_{2-1}^z \hat{\sigma}_{2+1}^z + \hat{\sigma}_{2-1}^z \hat{\sigma}_{2+1}^z)]$

Gates act on local algebras only!

Build In Build Out Action

Effect: None

Direction: Order

Delivery: Duration

More Options

Delete Skip Play Rehearse Record View Themes Masters Guides Smart Builds Text

B I U

Master Slides

Title, Bullets & Photo

Title - Top

Slides

# QC SIMU

SIMPLE SCA

★ ★ ★ ★

100%

We can obtain anticommuting field using the Cliff ordered in the same way as in the construction, i the unitary transformation of the local gates are f mess-up fields in different locations (for Bose field

Build

QC SIMULATION OF QFT  
SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$A = \exp\{i\theta[\sigma_{2n-1}^x \sigma_{2n-2}^z + \sigma_{2n-1}^z \sigma_{2n}^x]\}$   
 $B = \exp\{i\frac{\theta}{2}[\sigma_{2n}^z \sigma_{2n-1}^z + \sigma_{2n}^x \sigma_{2n+1}^x]\}$

Commuting	Anticommuting
Hermitian operator	Clifford algebra
$\sigma_{2n}^z \sigma_{2n-1}^z = \sigma_{2n-1}^z \sigma_{2n}^z$	$\sigma_{2n}^z \sigma_{2n-1}^z = -\sigma_{2n-1}^z \sigma_{2n}^z$
$\sigma_{2n}^x \sigma_{2n-1}^z = \sigma_{2n-1}^z \sigma_{2n}^x$	$\sigma_{2n}^x \sigma_{2n-1}^z = -\sigma_{2n-1}^z \sigma_{2n}^x$

→  $A = \exp[-i\theta(\sigma_{2n-1}^z \sigma_{2n}^x + \sigma_{2n-1}^x \sigma_{2n}^z)]$   
 $B = \exp[-i\frac{\theta}{2}(\sigma_{2n}^z \sigma_{2n+1}^z + \sigma_{2n}^x \sigma_{2n+1}^x)]$

Gates act on local algebras only!

Build In Build Out Action

Effect: None

Direction: Order

Delivery: Duration

More Options

Delete Skip Play Rehearse Record View Themes Masters Guides Smart Builds Text

B I U

Master Slides

Title, Bullets & Photo

Title - Top

Slides

# QC SIMU

SIMPLE SCA

★★★★

100%

We can obtain anticommuting field using the Clifford ordered in the same way as in the construction, if the unitary transformation of the local gates are f mess-up fields in different locations (for Bose field)



Build

QC SIMULATION OF QFT  
SIMPLE SCALAR FIELD IN 1 SPACE DIM.

$A = \exp\{i\theta [\hat{a}_1^\dagger \hat{a}_{2-1} + \hat{a}_{1-1}^\dagger \hat{a}_2]\}$   
 $B = \exp\{i\frac{\pi}{2} [\hat{a}_1^\dagger \hat{a}_2 + \hat{a}_1^\dagger \hat{a}_2]\}$

Commuting: Anticommuting  
 Heisenberg oscillator: Clifford algebra

$\hat{a}_1 \hat{a}_2 = \hat{a}_2 \hat{a}_1$      $\hat{a}_1 \hat{a}_2 = -\hat{a}_2 \hat{a}_1$      $\hat{a}_1^2 = \hat{a}_2^2 = 0$   
 $\hat{a}_1^\dagger \hat{a}_1 = \hat{a}_2^\dagger \hat{a}_2$      $\hat{a}_1^\dagger \hat{a}_2 = -\hat{a}_2^\dagger \hat{a}_1$      $\hat{a}_1^\dagger \hat{a}_1 + \hat{a}_2^\dagger \hat{a}_2 = \mathbb{I}$

$A = \exp[-i\theta (\hat{\sigma}_{2x-1} \hat{\sigma}_{2x} + \hat{\sigma}_{2x-1} \hat{\sigma}_{2x})]$   
 $B = \exp[-i\frac{\pi}{4} (\hat{\sigma}_{2x} \hat{\sigma}_{2x+1} + \hat{\sigma}_{2x} \hat{\sigma}_{2x+1})]$

Gates act on local algebras only!

Build In Build Out Action

Effect: None

Direction: Order

Delivery: Duration

More Options

Delete Skip Play Rehearse Record View Themes Masters Guides Smart Builds Text

B I U

Master Slides

Title, Bullets & Photo

Title - Top

Slides

# QC SIMU

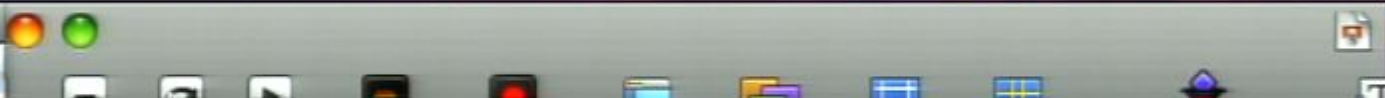
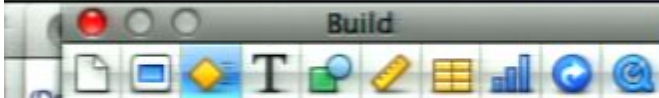
SIMPLE SCA

★★★★

100%

We can obtain anticommuting field using the Clifford ordered in the same way as in the construction, if the unitary transformation of the local gates are f mess-up fields in different locations (for Bose field)





### GRAVITATION?

**STRONG EQUIVALENCE PRINCIPLE**

gravitation = local mass distributions

Gravitation is a quantum effect

for possibility

Schwarzschild geometry

Build In Build Out Action

Effect  
None

Direction Order

Delivery Duration

More Options

#### Master Slides

- Blank
- to - Horizontal copy
- to - Panoramic
- Slides
- 5
- THANK YOU
- GRAVITATION
- GRAVITATION
- GRAVITATION
- GRAVITATION

# GRAVITATION

## STRONG EQUIVALENCE PRINCIPLE

★★★★

100%

# GRAVITATION?

## STRONG EQUIVALENCE PRINCIPLE

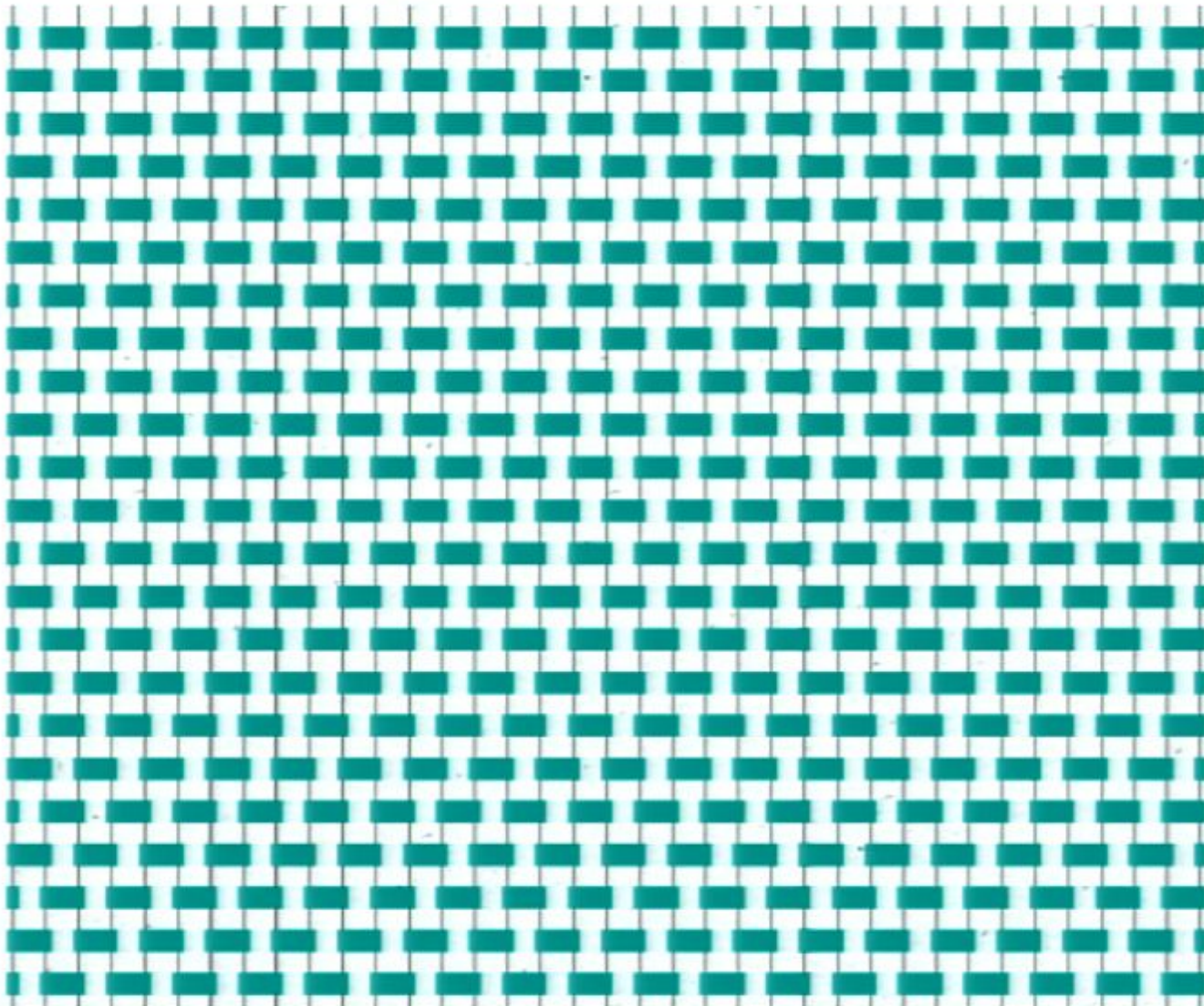
★ ★ ★ ★

★ ★ ★ ★

*gravitational =  
inertial mass  
informationally*

**Gravitation  
is a  
quantum  
effect**

**1st  
possibility**





# GRAVITATION?

## STRONG EQUIVALENCE PRINCIPLE

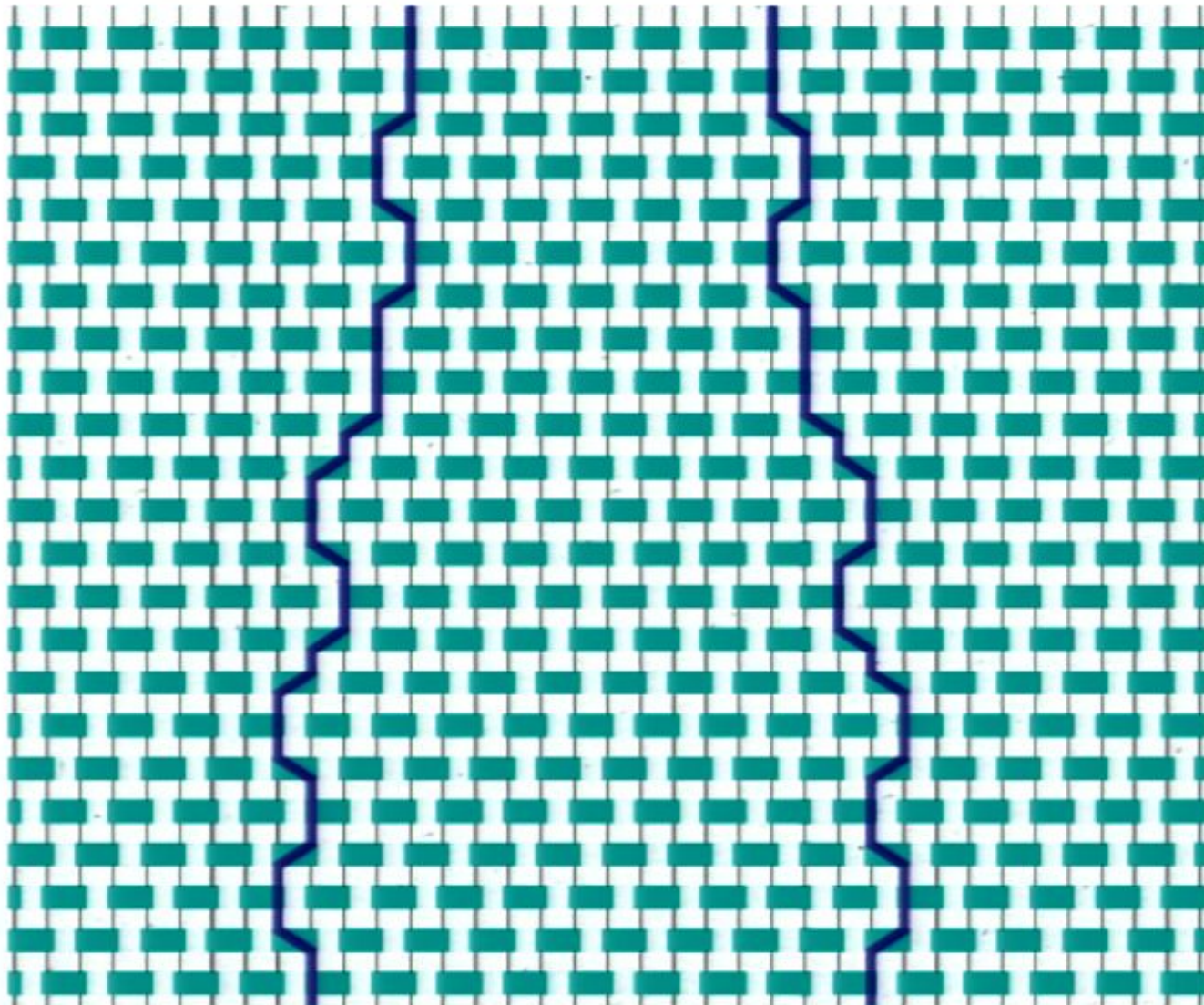
★ ★ ★ ★

★ ★ ★ ★

*gravitational =  
inertial mass  
informationally*

**Gravitation  
is a  
quantum  
effect**

**1st  
possibility**



**Sakharov  
induced  
gravity?**



# GRAVITATION?

## STRONG EQUIVALENCE PRINCIPLE

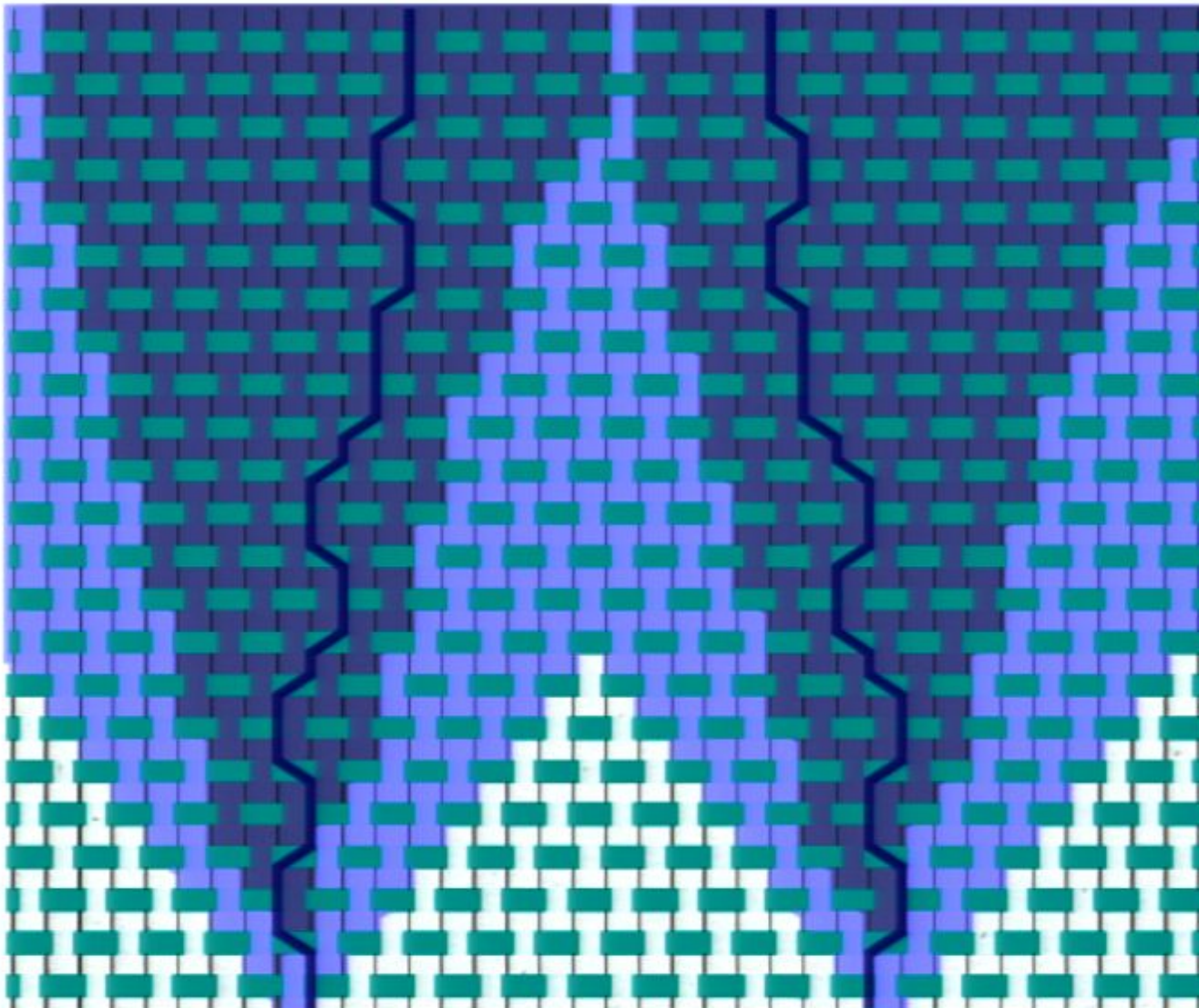
★ ★ ★ ★

★ ★ ★ ★

*gravitational =  
inertial mass  
informationally*

**1st  
possibility**

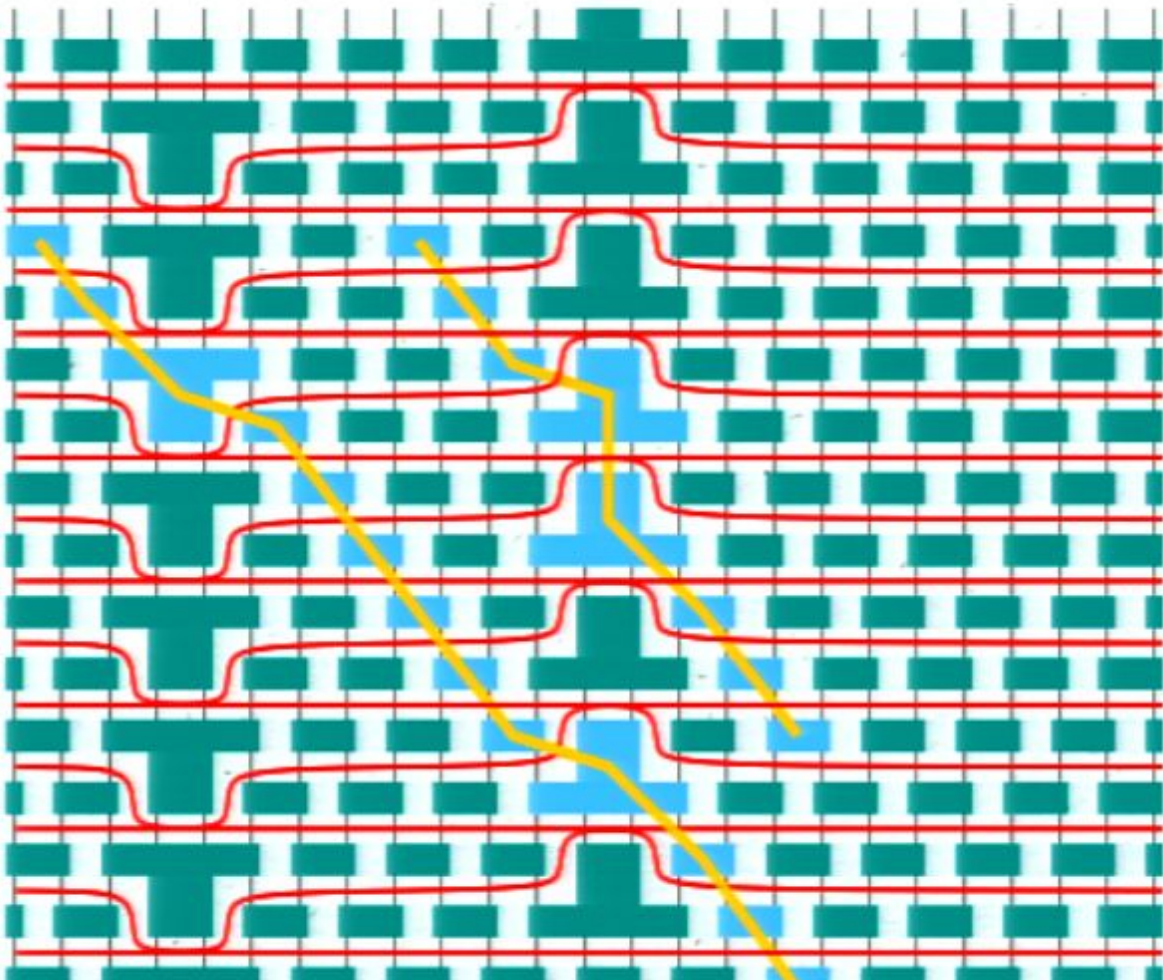
**Gravitation  
is a  
quantum  
effect**



Sakharov  
induced  
gravity?

# GRAVITATION?

MASS = EVENT



**2nd  
possibility**

*positive and  
negative masses*



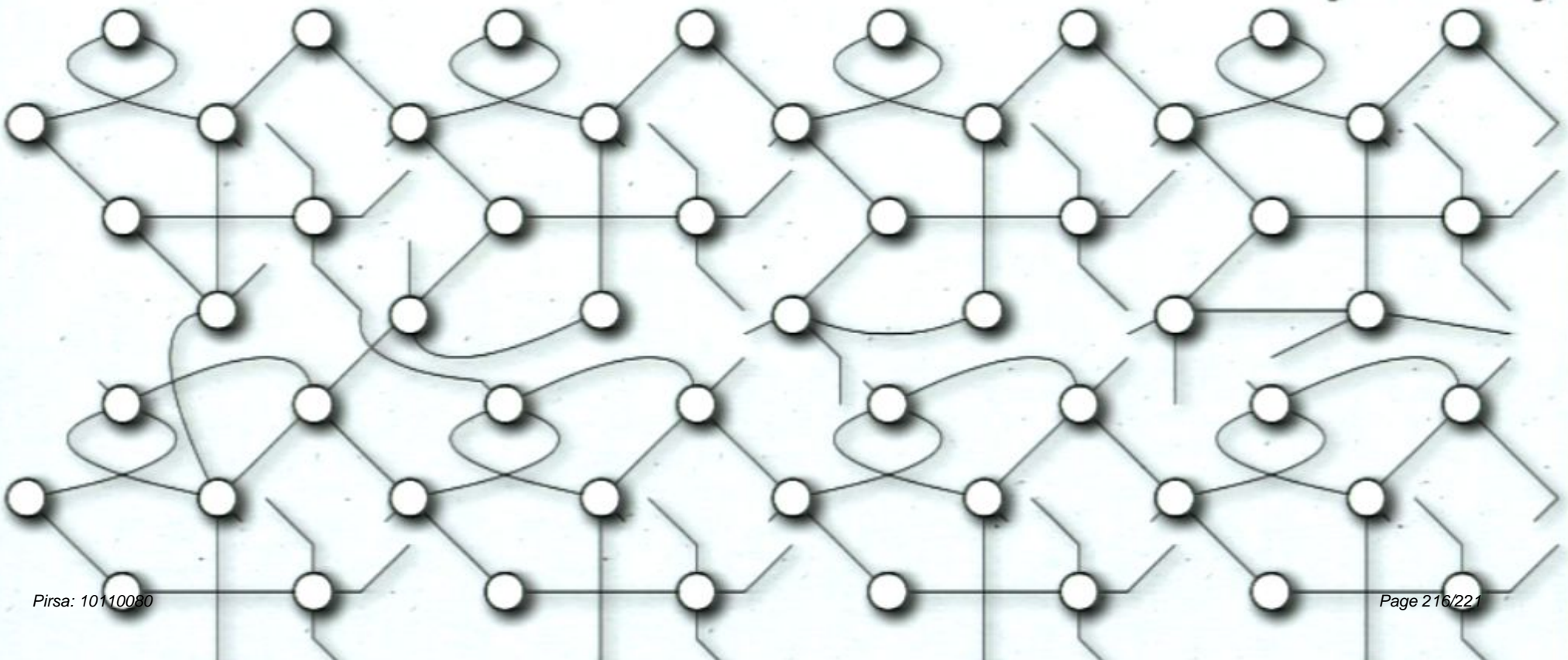


# GRAVITATION?

## THIRD QUANTIZATION?



**3rd  
possibility**





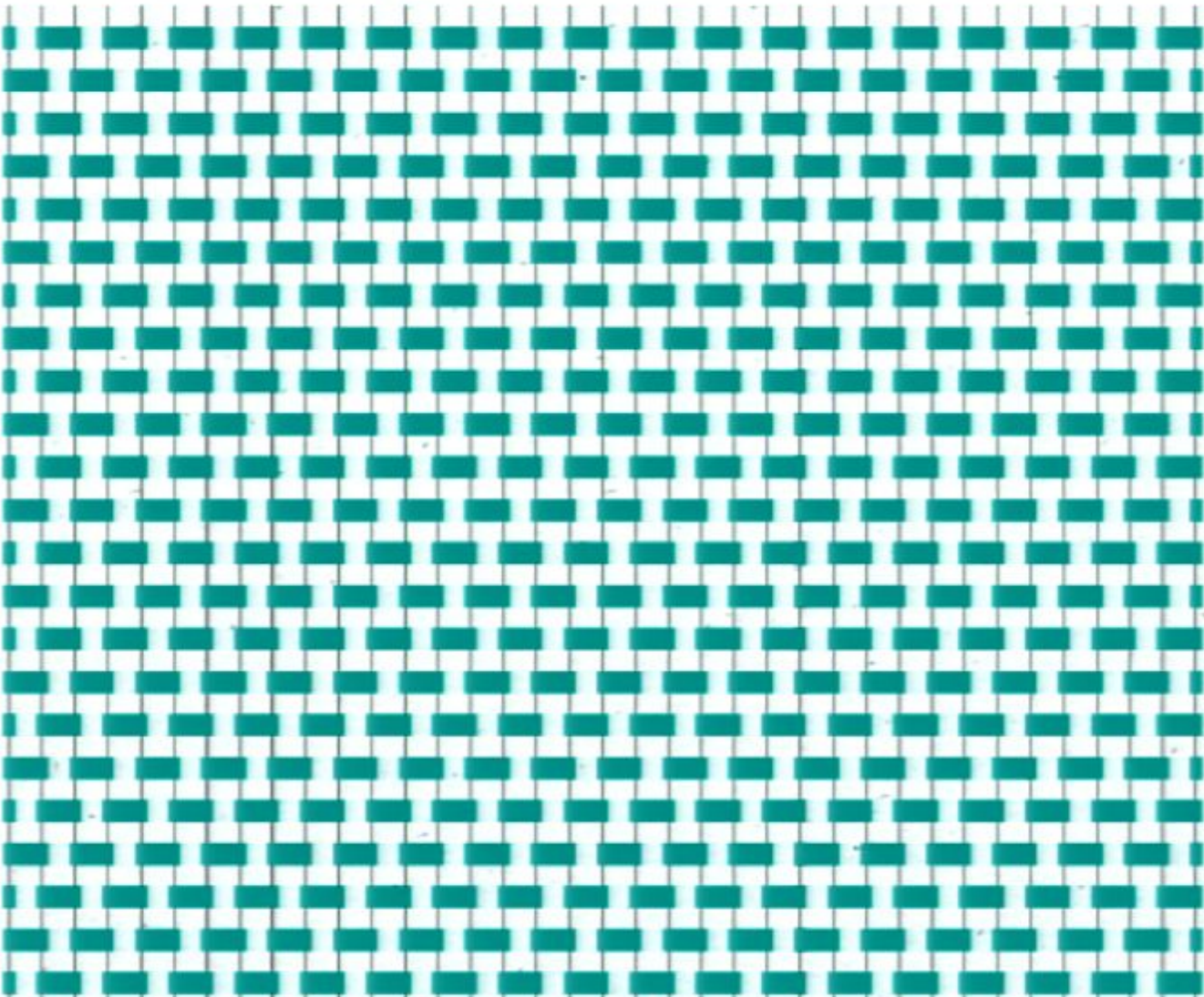
# GRAVITATION?

## STRONG EQUIVALENCE PRINCIPLE

★ ★ ★ ★

★ ★ ★ ★

*gravitational =  
inertial mass  
informationally*



**1st  
possibility**

**Gravitation  
is a  
quantum  
effect**

Sakharov  
induced  
gravity?



# GRAVITATION?

## STRONG EQUIVALENCE PRINCIPLE

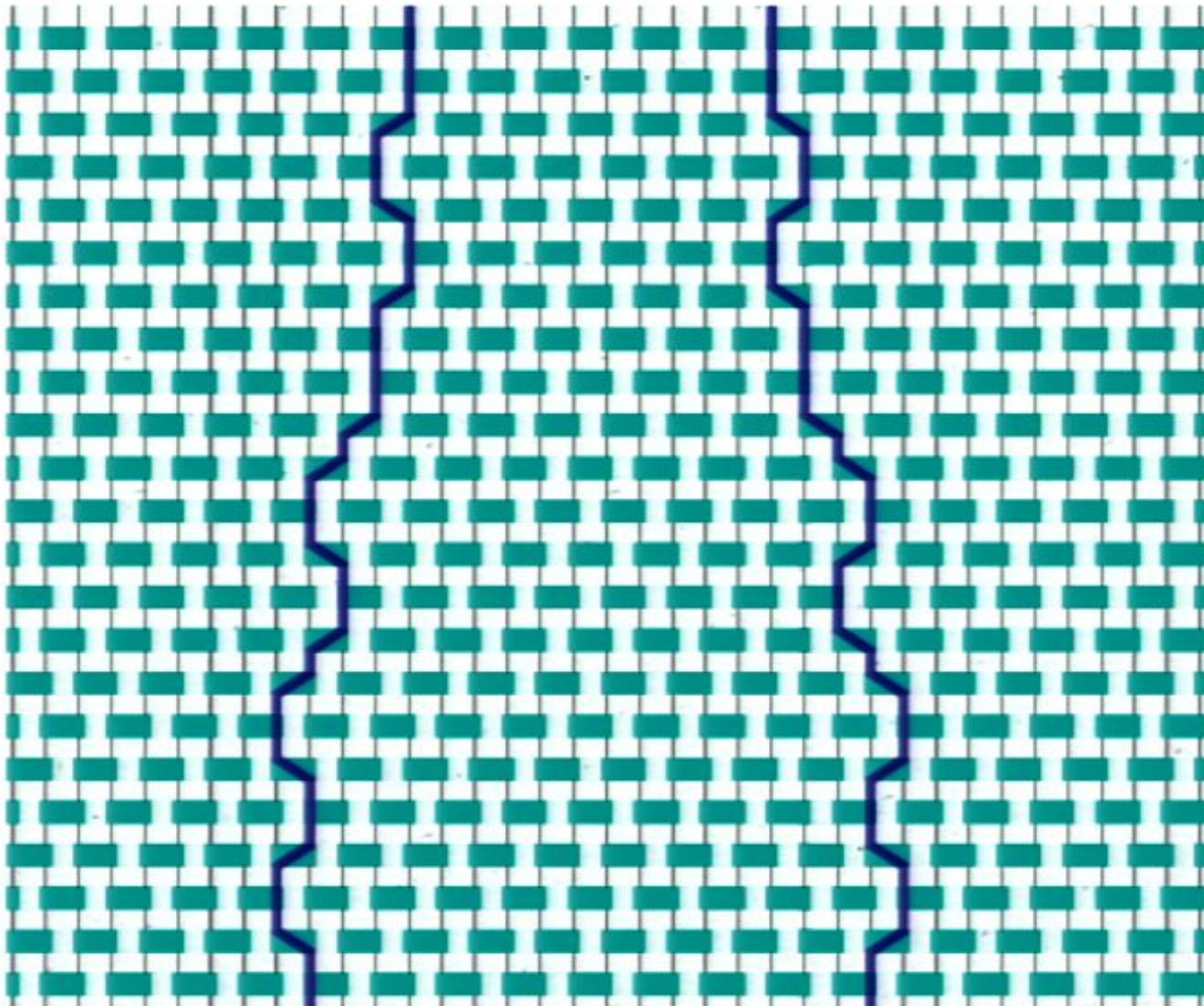
★ ★ ★ ★

★ ★ ★ ★

*gravitational =  
inertial mass  
informationally*

**Gravitation  
is a  
quantum  
effect**

**1st  
possibility**



**Sakharov  
induced  
gravity?**



# GRAVITATION?

## STRONG EQUIVALENCE PRINCIPLE

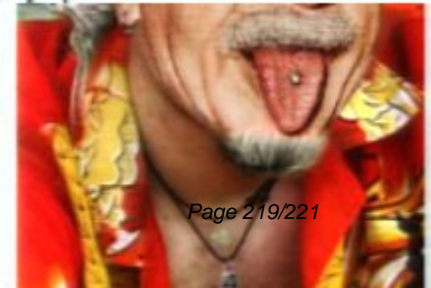
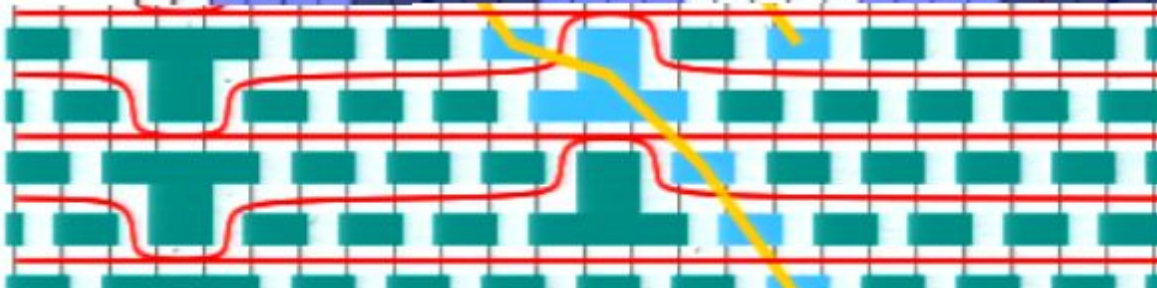
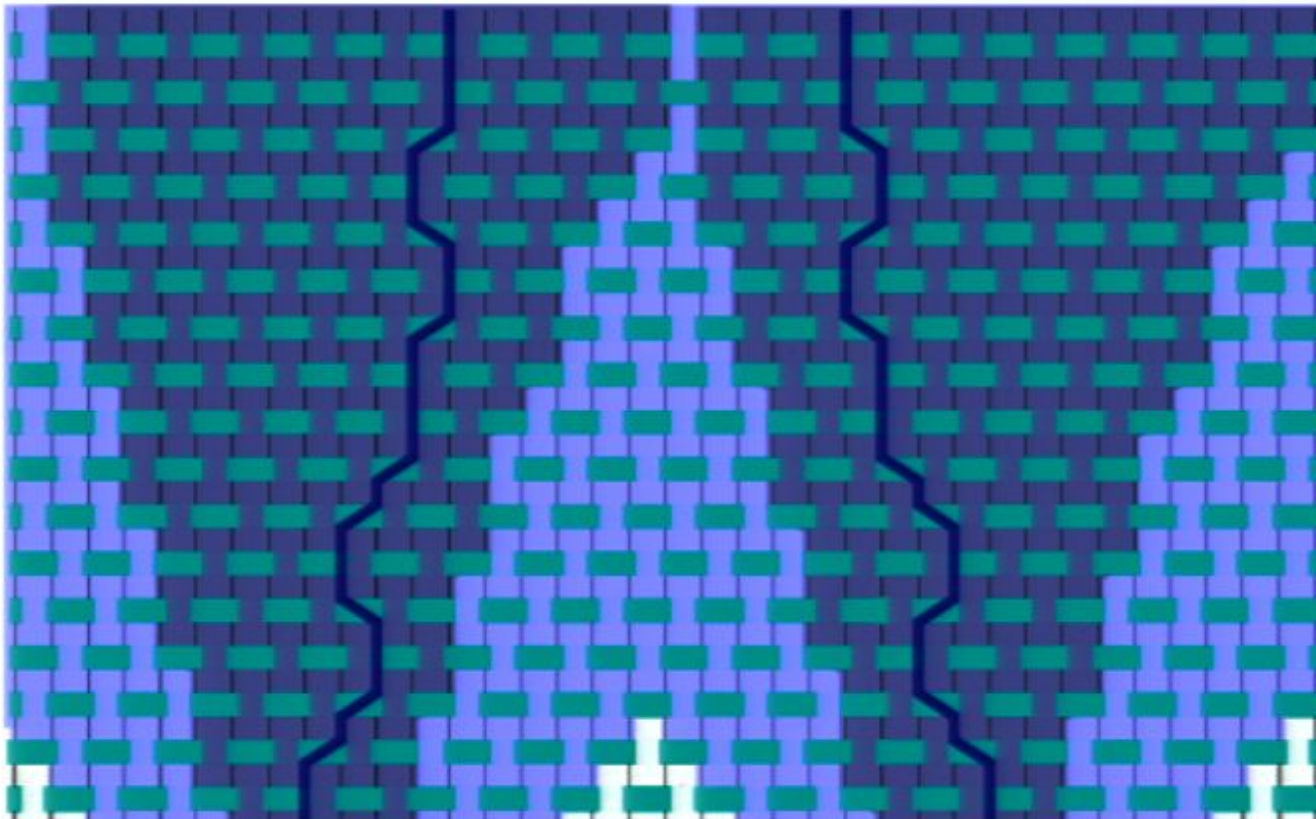
★★★★

★★★★

*gravitational =  
inertial mass  
informationally*

**1st  
possibility**

**Gravitation  
is a  
quantum  
effect**



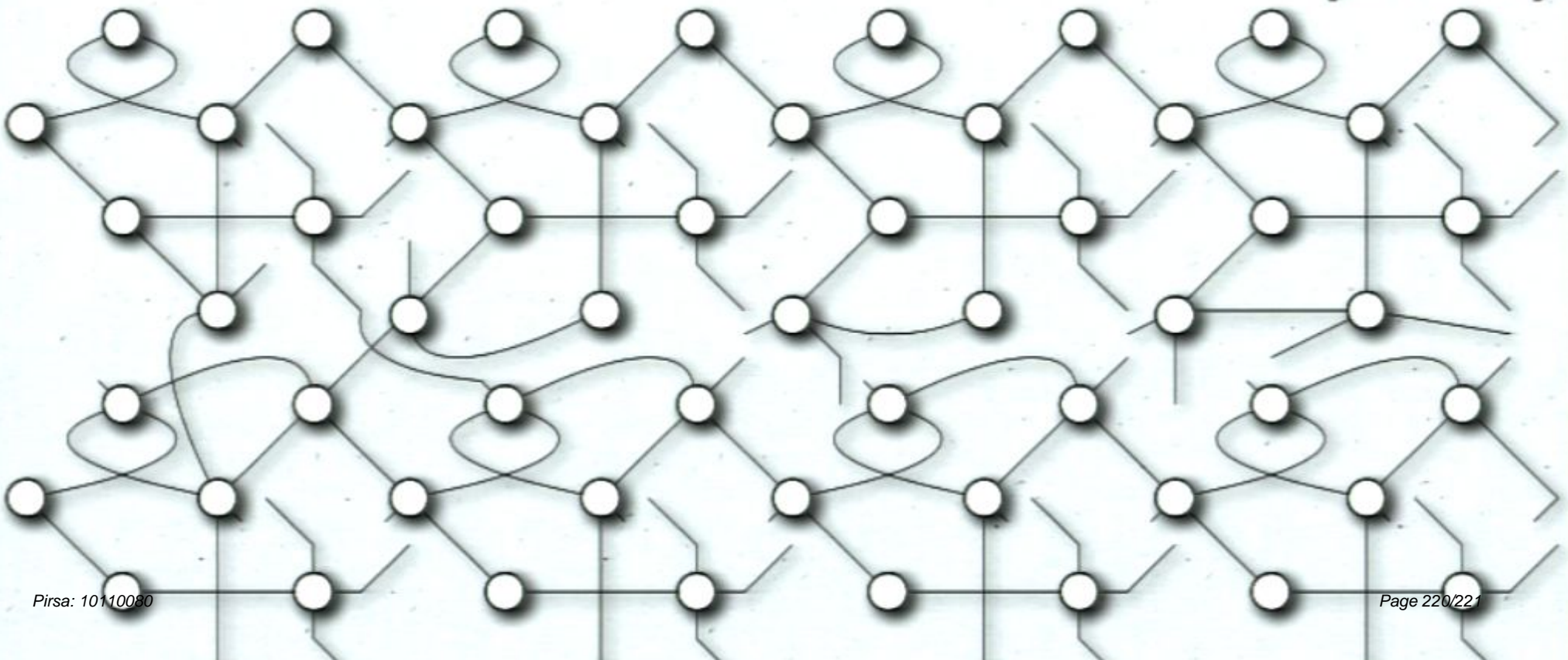


# GRAVITATION?

## THIRD QUANTIZATION?

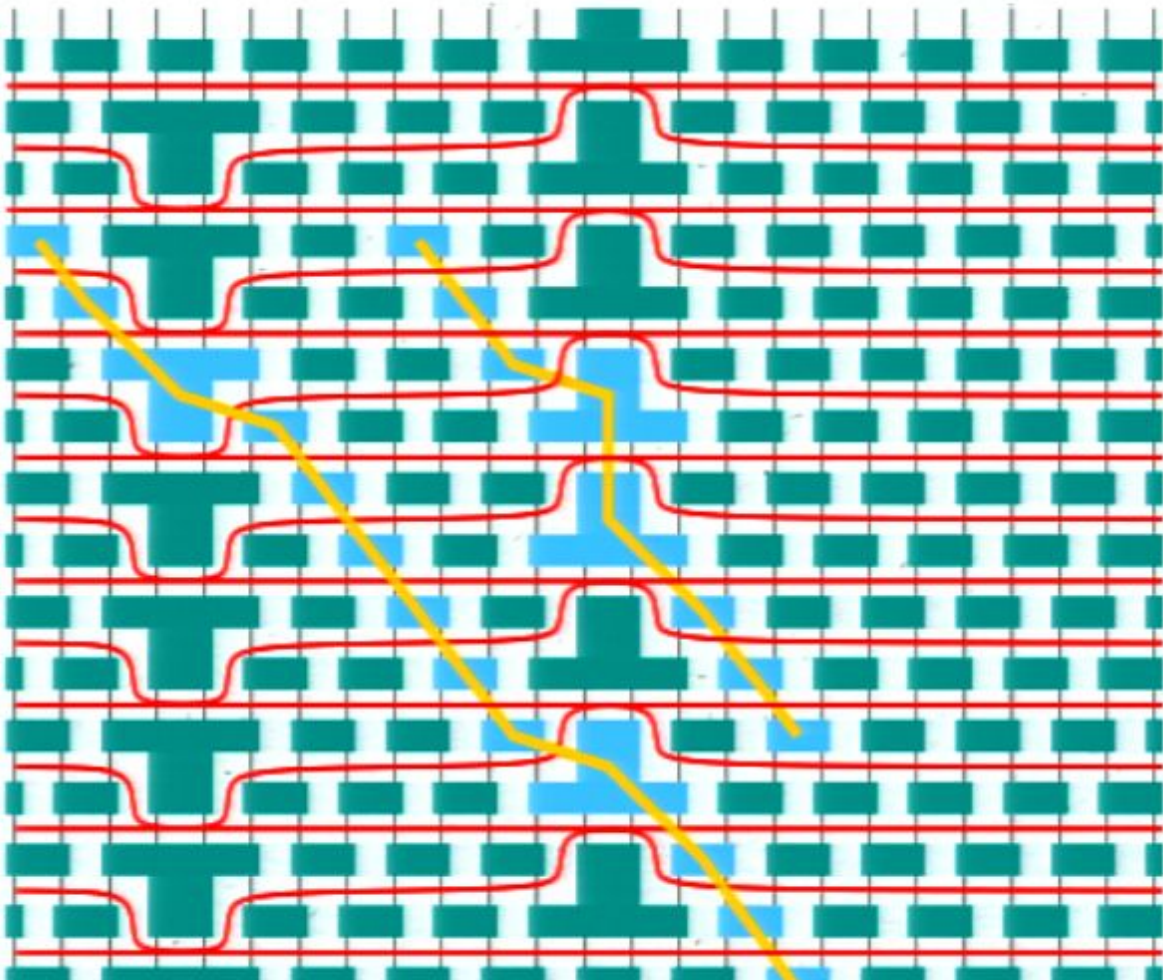


**3rd  
possibility**



# GRAVITATION?

MASS = EVENT



**2nd  
possibility**

positive and  
negative masses

