

Title: Introduction to Complex Analysis/Computer Skills - Lecture 4C

Date: Sep 02, 2010 11:15 AM

URL: <http://pirsa.org/10090091>

Abstract:

$$\text{eqs} = \text{x}[\#] - \sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{\text{x}[\#] - \text{x}[k]}] \& /@ \text{Range}[M];$$

```
In[93]:= fr = FindRoot[eqs, vars];
```

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eqs /. fr // Chop; (* check of equations *)
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lp = { $\frac{\text{x}[\# + 1] + \text{x}[\#]}{2}$ ,  $\frac{1}{\text{x}[\# + 1] - \text{x}[\#]}$ } & /@ \text{Range}[M - 1] /. fr // ListPlot;
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lp = Table[{ $\frac{\text{x}[j + 1] + \text{x}[j]}{2}$ ,  $\frac{1}{\text{x}[j + 1] - \text{x}[j]}$ }, {j, 1, M - 1}] /. fr // ListPlot;
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```
In[99]:= p1 = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x, - $\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red]
```

```
In[100]:= Show[p1, lp]
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$$\text{eqs} = \text{x}[\#] - \sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{\text{x}[\#] - \text{x}[k]}] \& /@ \text{Range}[M];$$

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lp = Table[ $\left\{ \frac{\text{x}[j + 1] + \text{x}[j]}{2}, \frac{1}{\text{x}[j + 1] - \text{x}[j]} \right\}$ , {j, 1, M - 1}] /. fr // ListPlot;
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In[99]:= pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x, - $\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red]
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In[99]:= p1 = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red}$ ]
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$$\text{eqs} = \text{x}[\#] - \sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{\text{x}[\#] - \text{x}[k]}] \& /@ \text{Range}[M];$$

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In[101]:= lp = { $\frac{\text{x}[\# + 1] + \text{x}[\#]}{2}$ ,  $\frac{1}{\text{x}[\# + 1] - \text{x}[\#]}$ } & /@ \text{Range}[M - 1] /. fr // ListPlot;
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lp = Table[{ $\text{x}[j]$ ,  $\frac{1}{\text{x}[j + 1] - \text{x}[j]}$ }, {j, 1, M - 1}] /. fr // ListPlot;
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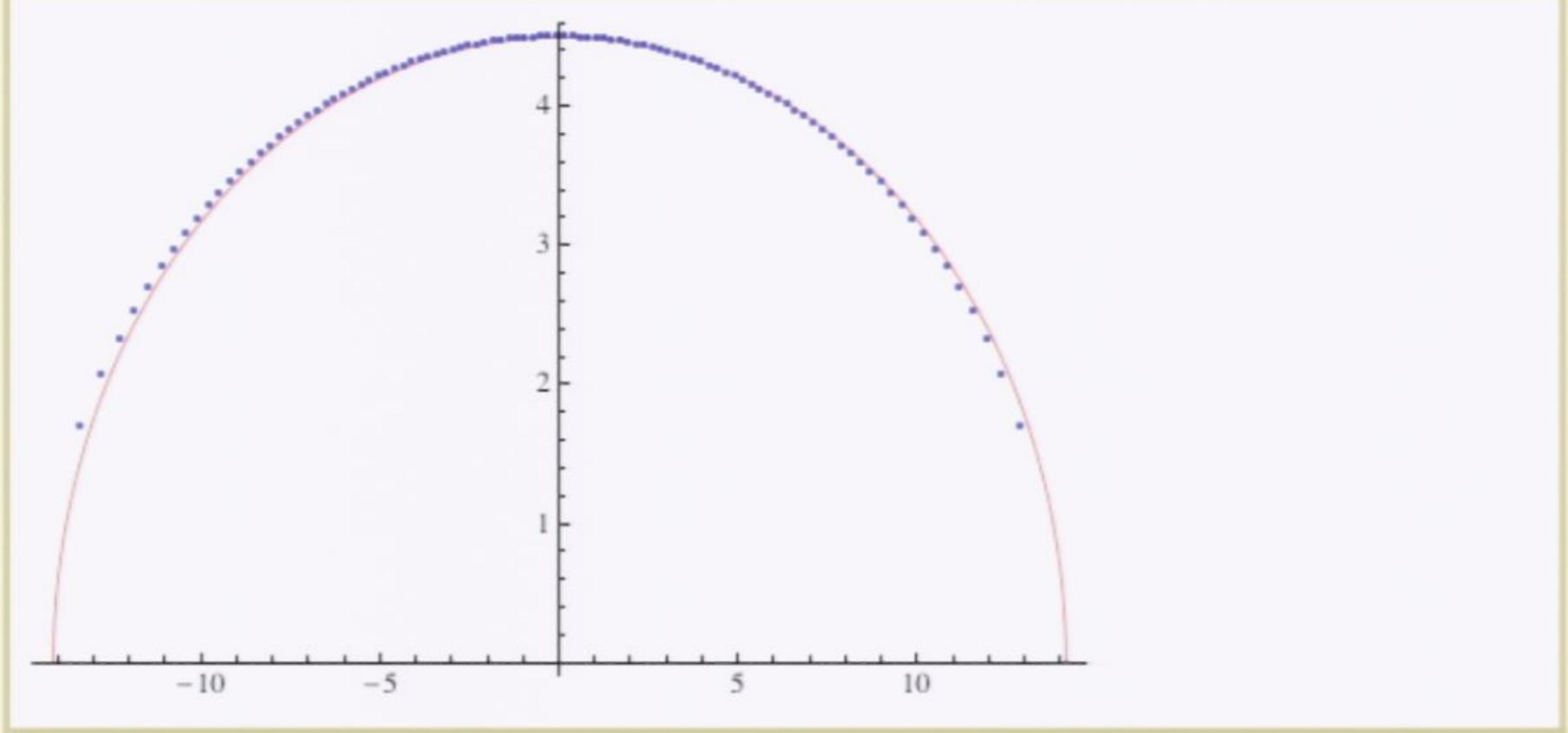
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```



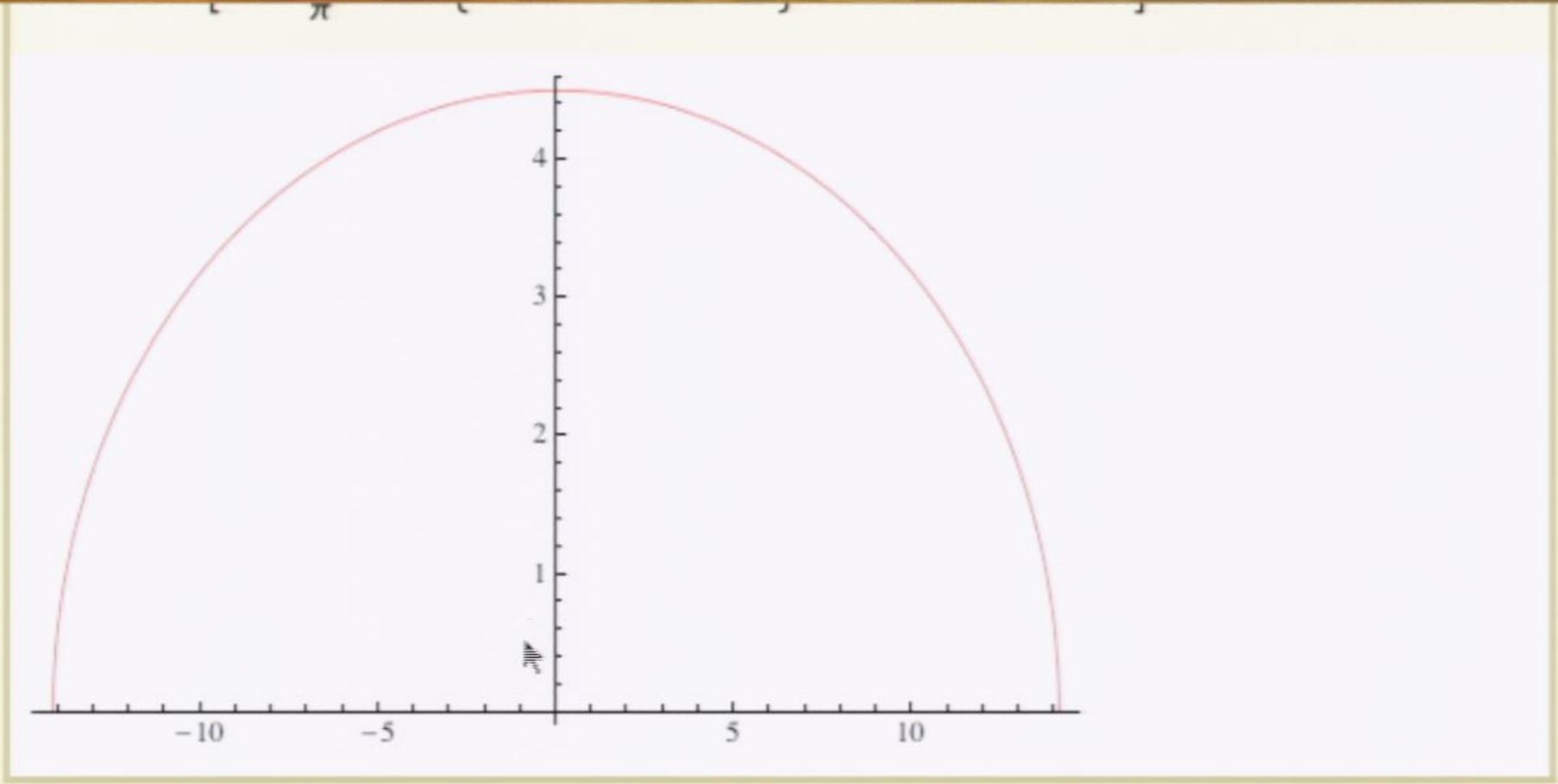


In[104]:= Show[pl, lp]



Out[104]=

In[103]:=



In[104]:=

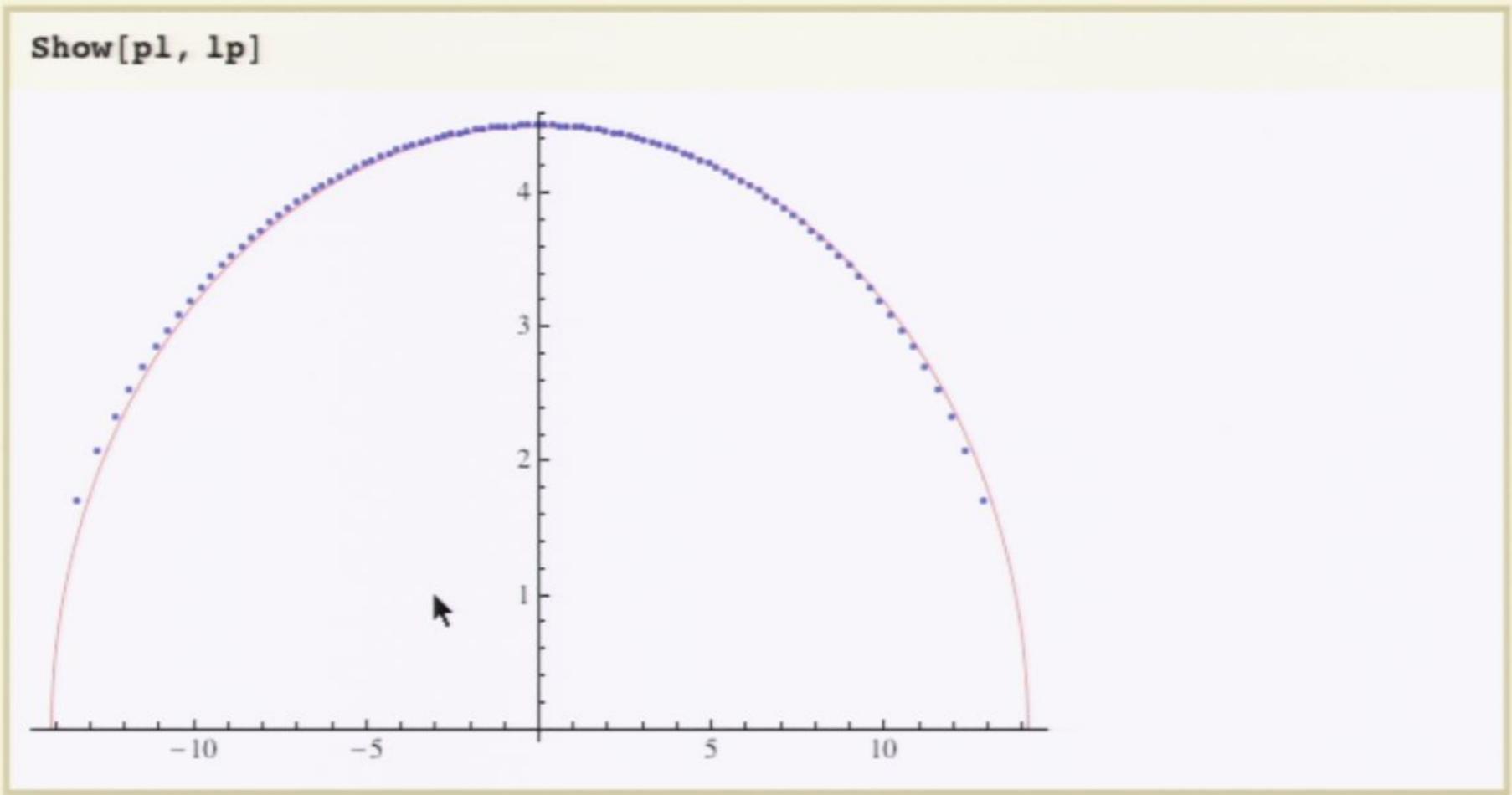
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In[103]:= pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x,  $-\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red]
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In[104]:= Show[pl, lp]
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$$\sum_{k=1}^{\dots} [\dots x[\#] - x[k]]$$

In[93]:= `fr = FindRoot[eqs, vars];`

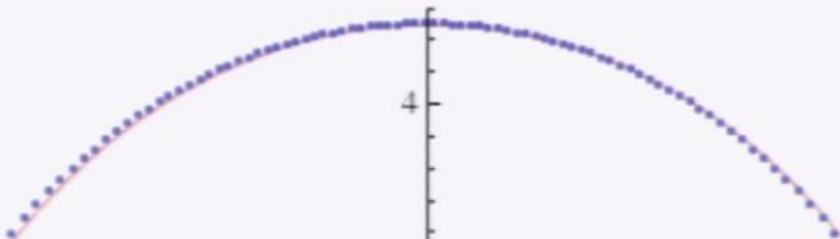
`eqs /. fr // Chop; (* check of equations *)`

In[101]:= `lp = { $\frac{x[\# + 1] + x[\#]}{2}$, $\frac{1}{x[\# + 1] - x[\#]}$ } & /@ Range[M - 1] /. fr // ListPlot;`

`lp = Table[{ $x[j]$, $\frac{1}{x[j + 1] - x[j]}$ }, {j, 1, M - 1}] /. fr // ListPlot;`

In[103]:= `p1 = Plot[$\frac{\sqrt{2M - x^2}}{\pi}$, {x, $-\sqrt{2M}$, $\sqrt{2M}$ }, PlotStyle -> Red]`

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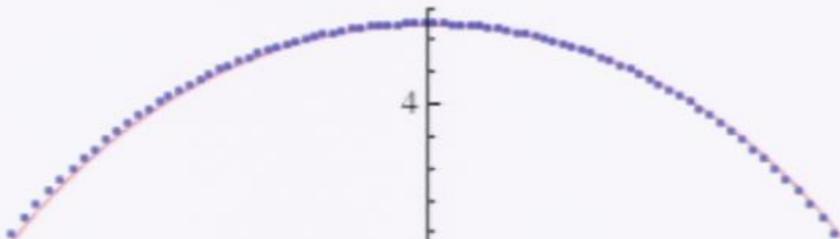
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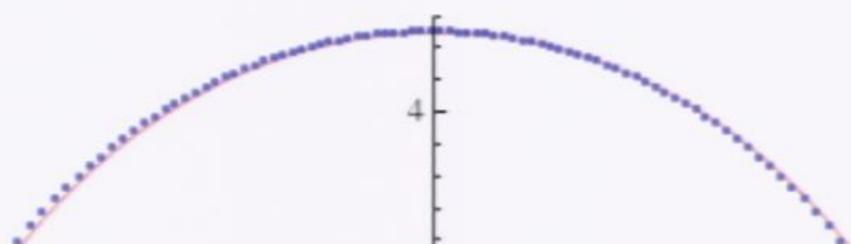
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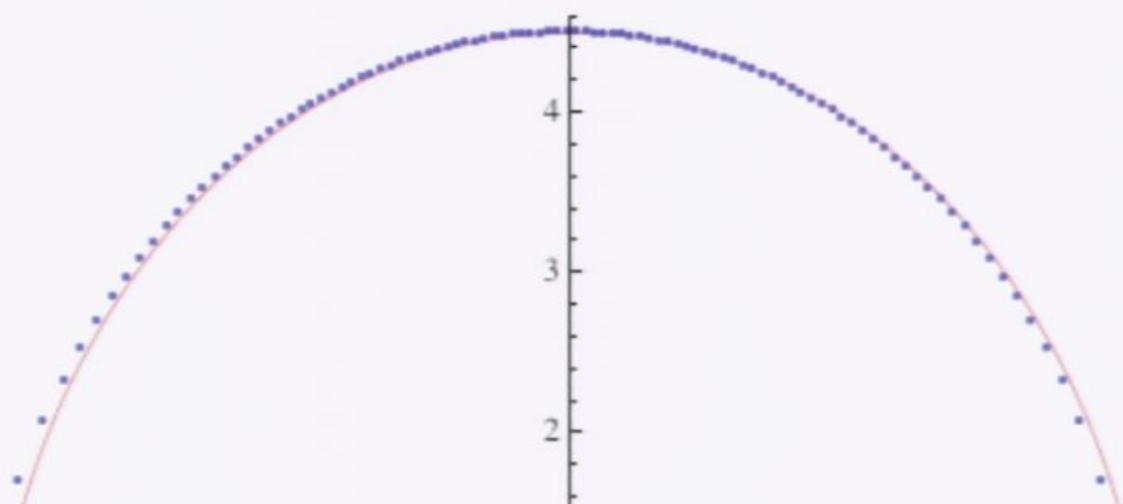
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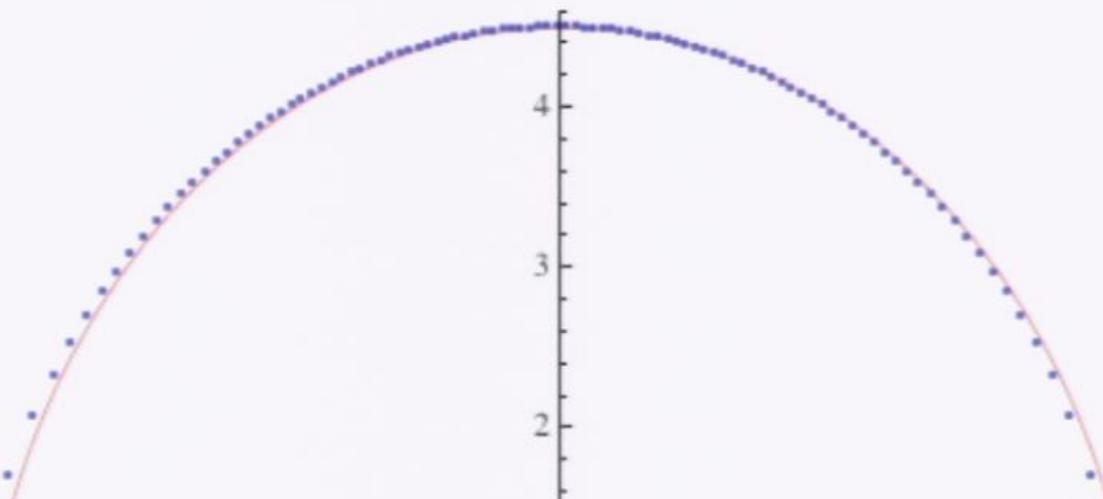


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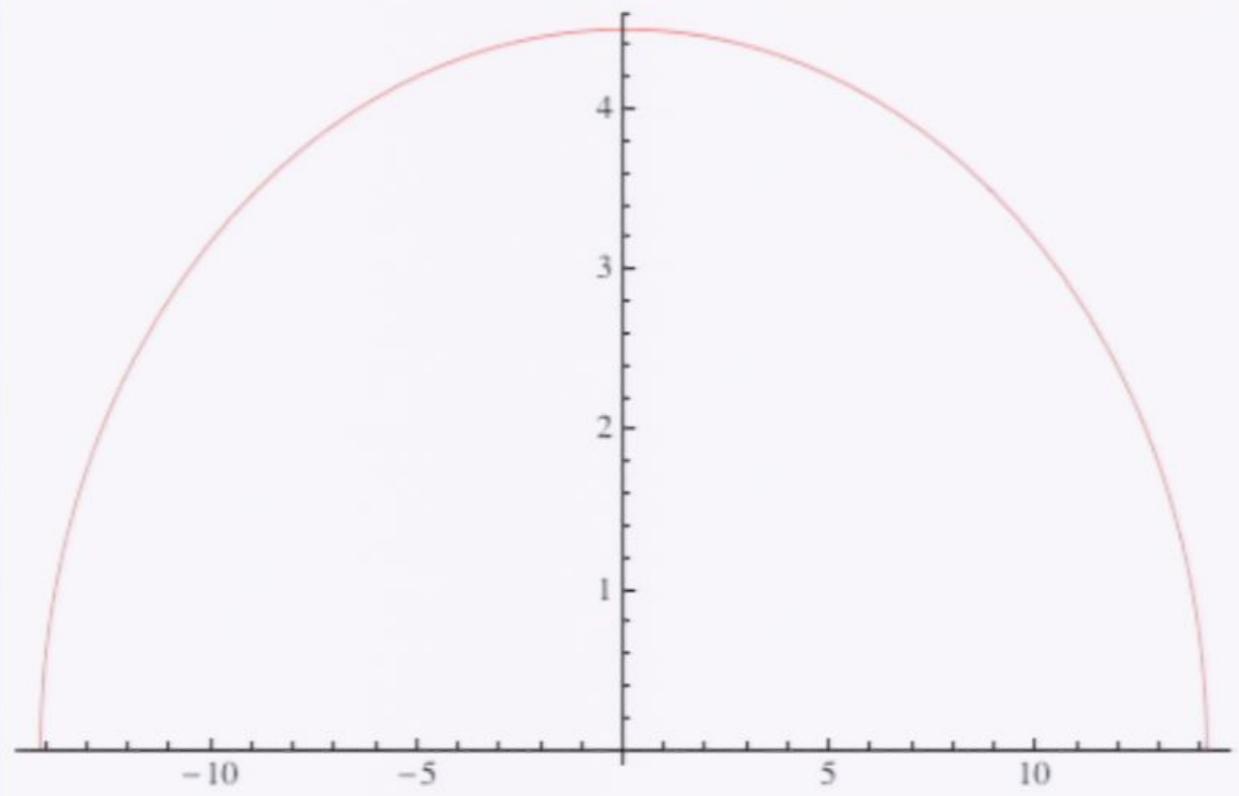
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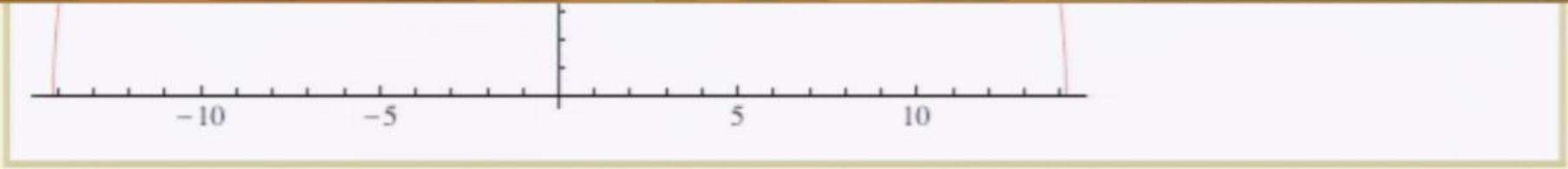
Out[107]=



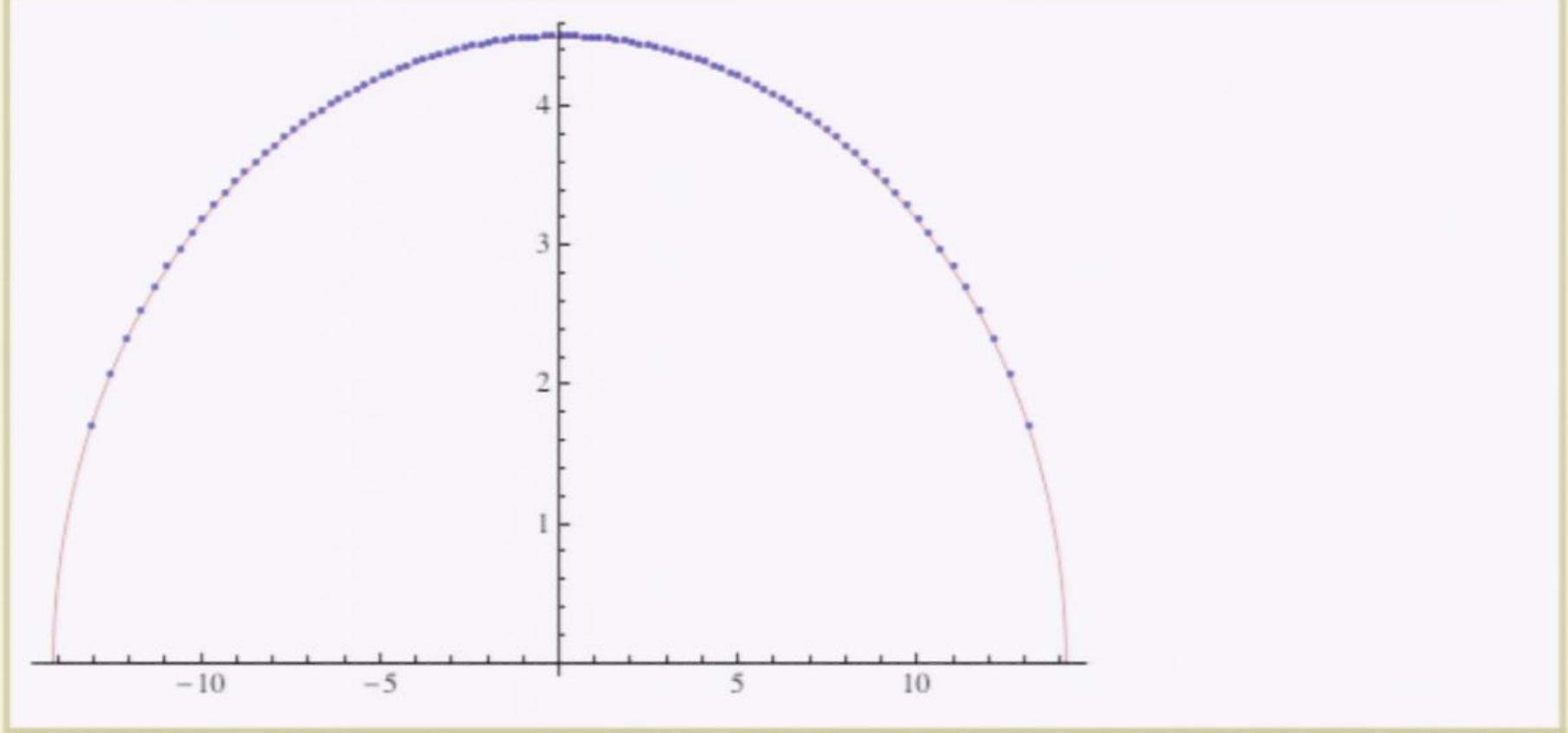
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In[108]:= Show[pl, lp]



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$$\text{eqs} = \mathbf{x}[\#] - \sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{\mathbf{x}[\#] - \mathbf{x}[k]}] \ \& \ /@ \text{Range}[M];$$

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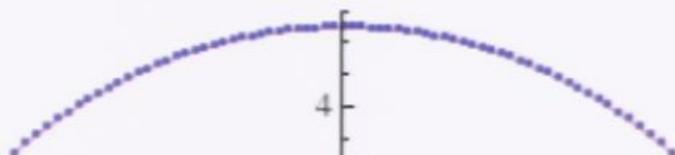
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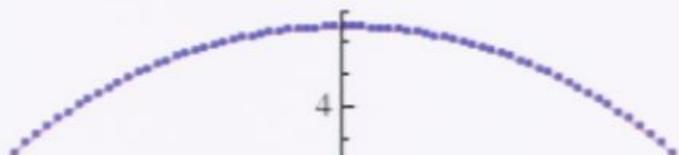
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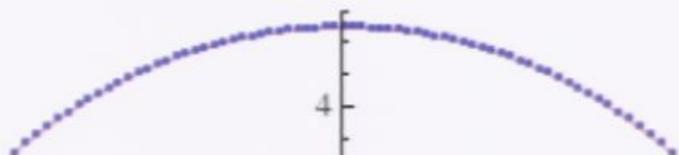
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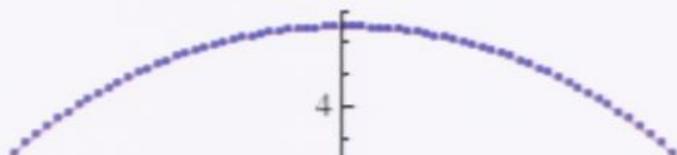
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■ Live version

In[88]:= `M = 100;`

In[89]:= `vars = Table[{x[j], j - M/2}, {j, M}];`
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`pl = Plot[$\frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red}];$`

In[109]:=

`M = 100;``vars = {x[#], # - M/2} & /@ Range[M];``eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];`

In[93]:=

`fr = FindRoot[eqs, vars];``eqs /. fr // Chop; (* check of equations *)`

In[105]:=

`lp = $\left\{ \frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]} \right\}$ & /@ Range[M - 1] /. fr // ListPlot;``lp = Table $\left[\left\{ \frac{x[j] + x[j + 1]}{2}, \frac{1}{x[j + 1] - x[j]} \right\}, \{j, 1, M - 1\} \right]$ /. fr // ListPlot;`

In[109]:= `M = 100;`

`vars = {x[#], # - M/2} & /@ Range[M];`

`eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];`

In[93]:= `fr = FindRoot[eqs, vars];`

`eqs /. fr // Chop; (* check of equations *)`

In[105]:= `lp = { $\frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]}}$ & /@ Range[M - 1] /. fr // ListPlot;`

`lp = Table[{ $\frac{x[j] + x[j + 1]}{2}, \frac{1}{x[j + 1] - x[j]}$ }, {j, 1, M - 1}] /. fr // ListPlot;`

`pl = Plot[$\frac{\sqrt{2M - x^2}}{\pi}$, {x, - $\sqrt{2M}$, $\sqrt{2M}$ }, PlotStyle -> Red];`

In[109]:= M = 100;

vars = {x[#], # - M/2} & /@ Range[M];

eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];

In[93]:= fr = FindRoot[eqs, vars];

eqs /. fr // Chop; (* check of equations *)

In[105]:= lp = $\left\{ \frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]} \right\}$ & /@ Range[M - 1] /. fr // ListPlot;

lp = Table $\left[\left\{ \frac{x[j] + x[j + 1]}{2}, \frac{1}{x[j + 1] - x[j]} \right\}, \{j, 1, M - 1\} \right]$ /. fr // ListPlot;

pl = Plot $\left[\frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red} \right];$

In[109]:= M = 100;

vars = {x[#], # - M/2} & /@ Range[M];

eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];

In[93]:= fr = FindRoot[eqs, vars];

eqs /. fr // Chop; (* check of equations *)

In[105]:= lp = $\left\{ \frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]} \right\}$ & /@ Range[M - 1] /. fr // ListPlot;

lp = Table $\left[\left\{ \frac{x[j] + x[j + 1]}{2}, \frac{1}{x[j + 1] - x[j]} \right\}, \{j, 1, M - 1\} \right]$ /. fr // ListPlot;

pl = Plot $\left[\frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red} \right];$

in[109]:= **M = 100;**

vars = {x[#], # - M/2} & /@ Range[M];

eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];

in[93]:= **fr = FindRoot[eqs, vars];**

in[110]:= **eqs /. fr // Chop; (* check of equations *)**

in[105]:= **lp = $\left\{ \frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]} \right\}$ & /@ Range[M - 1] /. fr // ListPlot;**

lp = Table $\left[\left\{ \frac{x[j] + x[j + 1]}{2}, \frac{1}{x[j + 1] - x[j]} \right\}, \{j, 1, M - 1\} \right]$ /. fr // ListPlot;

pl = Plot $\left[\frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red} \right];$

In[109]:= `M = 100;`

`vars = {x[#], # - M/2} & /@ Range[M];`

`eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];`

In[93]:= `fr = FindRoot[eqs, vars];`

In[110]:= `eqs /. fr // Chop; (* check of equations *)`

`lp = { $\frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]}}$ & /@ Range[M - 1] /. fr // ListPlot;`

`pl = Plot[$\frac{\sqrt{2M - x^2}}{\pi}$, {x, - $\sqrt{2M}$, $\sqrt{2M}$ }, PlotStyle -> Red];`

In[100]:= `Show[pl, lp]`

In[109]:= `M = 100;`

`vars = {x[#], # - M/2} & /@ Range[M];`

`eqs = x[#] - $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$ & /@ Range[M];`

In[93]:= `fr = FindRoot[eqs, vars];`

In[110]:= `eqs /. fr // Chop; (* check of equations *)`

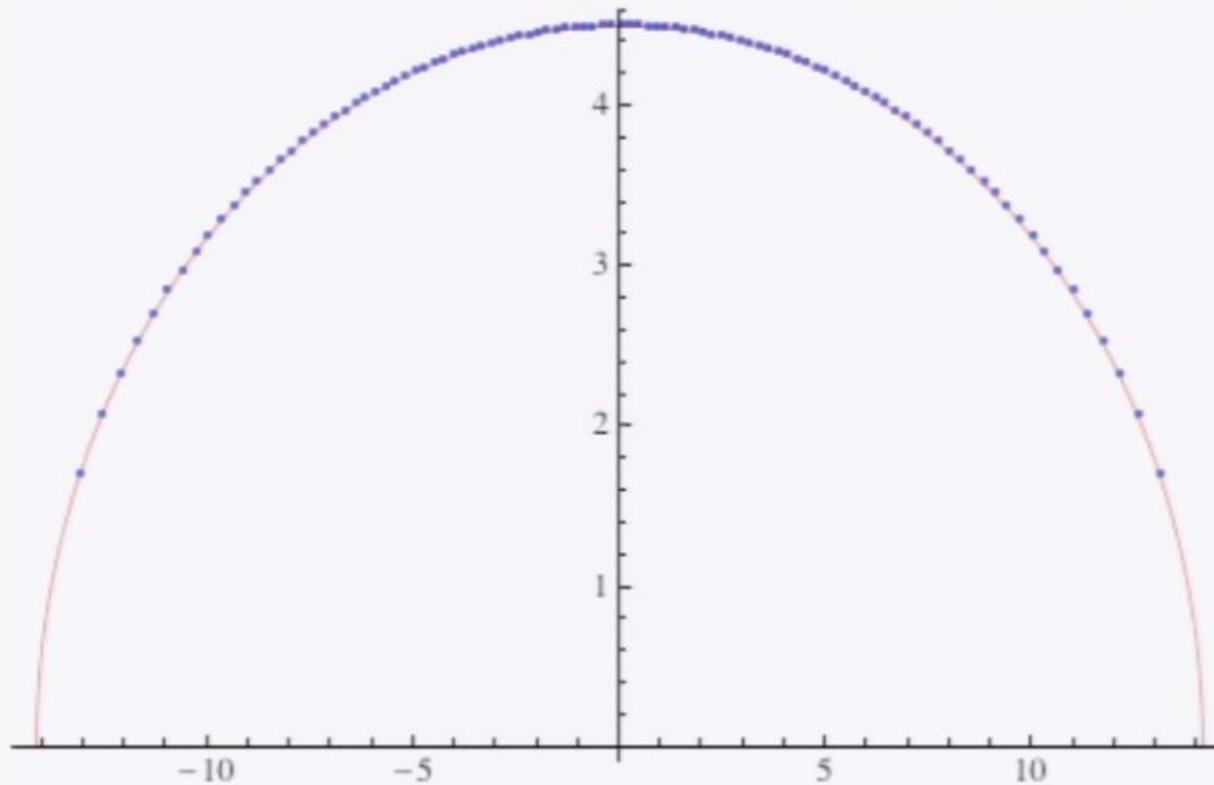
In[111]:= `lp = { $\frac{x[\# + 1] + x[\#]}{2}$, $\frac{1}{x[\# + 1] - x[\#]}$ } & /@ Range[M - 1] /. fr // ListPlot;`

`pl = Plot[$\frac{\sqrt{2M - x^2}}{\pi}$, {x, - $\sqrt{2M}$, $\sqrt{2M}$ }, PlotStyle -> Red];`

In[108]:= `Show[pl, lp]`

```
pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x,  $-\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red];
```

```
In[113]:= Show[pl, lp]
```



■ Live version

```
In[109]:= M = 100;
```

```
vars = {x[#], # - M/2} & /@ Range[M];
```

```
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[93]:= fr = FindRoot[eqs, vars];
```

```
In[110]:= eqs /. fr // Chop; (* check of equations *)
```

```
In[111]:= lp =  $\left\{ \frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]} \right\}$  & /@ Range[M - 1] /. fr // ListPlot;
```

```
p1 = Plot $\left[ \frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red} \right];$ 
```

```
In[113]:= Show[p1, lp]
```

Live version

```
In[109]:= M = 100;
```

```
vars = {x[#], # - M/2} & /@ Range[M];
```

```
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

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In[93]:= fr = FindRoot[eqs, vars];
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```

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In[111]:= lp =  $\left\{ \frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]} \right\}$  & /@ Range[M - 1] /. fr // ListPlot;
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pl = Plot $\left[ \frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red} \right];$ 
```

```
In[112]:= Show[pl, lp]
```

Live version

```
In[109]:= M = 100;
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In[93]:= fr = FindRoot[eqs, vars];
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```
pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x, - $\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red];
```

Live version

■ Check of density

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In[109]:= M = 100;
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pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x, - $\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red];
```

Live version

- Check of density
- Harmonic Oscillator

}

Live version

- Check of density
-



Live version

- Check of density
- Hermite P|

Live version

- Check of density
- Hermite Polynomials|

Live version

■ Check of density

```
In[109]:= M = 100;
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Live version

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Live version

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M = 100;
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```

Live version

```
M = 100;
```

- Check of density
- Hermite Polynomials

```
M = 100;
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■ Check of density

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vars = {x[#], # - M/2} & /@ Range[M];
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p1 = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x, - $\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red];
```

```
In[113]:= Show[p1, lp]
```

```
M = 100;
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■ Check of density

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■ Check of density

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In[110]:= eqs /. fr // Chop; (* check of equations *)
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■ C|

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pl = Plot $\left[ \frac{\sqrt{2M - x^2}}{\pi}, \{x, -\sqrt{2M}, \sqrt{2M}\}, \text{PlotStyle} \rightarrow \text{Red} \right];$ 
```

```
M = 100;
```

■ S|

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```
M = 100;
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■ Solving th

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vars = {x[#], # - M/2} & /@ Range[M];
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M = 100;
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■ Solving the equation

```
vars = {x[#], # - M/2} & /@ Range[M];
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eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
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■ Check of density

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M = 100;
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■ Solving the equations

```
vars = {x[#], # - M/2} & /@ Range[M];
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eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
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In[93]:= fr = FindRoot[eqs, vars];
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In[111]:= lp = { $\frac{x[\# + 1] + x[\#]}{2}, \frac{1}{x[\# + 1] - x[\#]}}$  & /@ Range[M - 1] /. fr // ListPlot;
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pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x, - $\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red];
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M = 100;
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■ Solving the equations

```
vars = {x[#], # - M/2} & /@ Range[M];
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```
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[93]:= fr = FindRoot[eqs, vars];
```

```
In[110]:= eqs /. fr // Chop; (* check of equations *)
```

■ Check of density

■ Hermite Polynomials

Live version

```
M = 100;
```

- Solving the equations
- Check of density
- Hermite Polynomials

Live version

```
In[114]:= M = 100;
```

■ Solving the equations

```
vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[93]:= fr = FindRoot[eqs, vars];
```

```
In[110]:= eqs /. fr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials

Live version

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[110]:= eqs /. fr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials

Live version

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[118]:= eqs /. fr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials

```
in[117]:= fr = FindRoot[eqs, vars],
```

```
in[118]:= eqs /. fr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials

Live version

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[118]:= eqs /. fr // Chop; (* check of equations *)
```

■ Check of density

■ Hermite Polynomials

Live version

In[114]:= M = 100;

- Solving the equations
- Check of density
- Hermite Polynomials

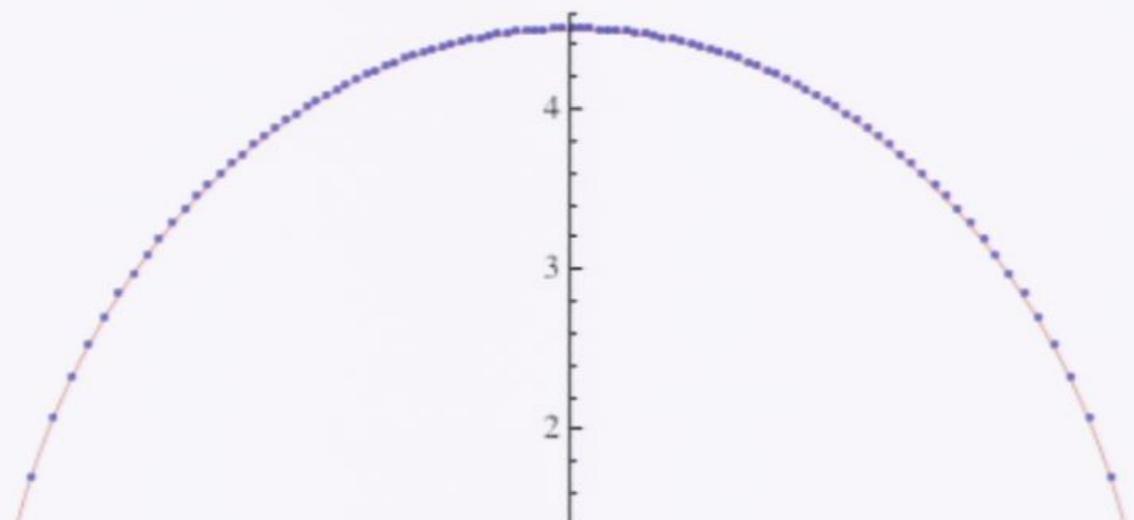
In[114]:= M = 100;

- Solving the equations
- Check of density

In[111]:= lp = { $\frac{x[\# + 1] + x[\#]}{2}$, $\frac{1}{x[\# + 1] - x[\#]}$ } & /@ Range[M - 1] /. fr // ListPlot;

p1 = Plot[$\frac{\sqrt{2M - x^2}}{\pi}$, {x, - $\sqrt{2M}$, $\sqrt{2M}$ }, PlotStyle -> Red];

In[113]:= Show[p1, lp]



```
pl = Plot[ $\frac{\sqrt{2M - x^2}}{\pi}$ , {x,  $-\sqrt{2M}$ ,  $\sqrt{2M}$ }, PlotStyle -> Red];
```

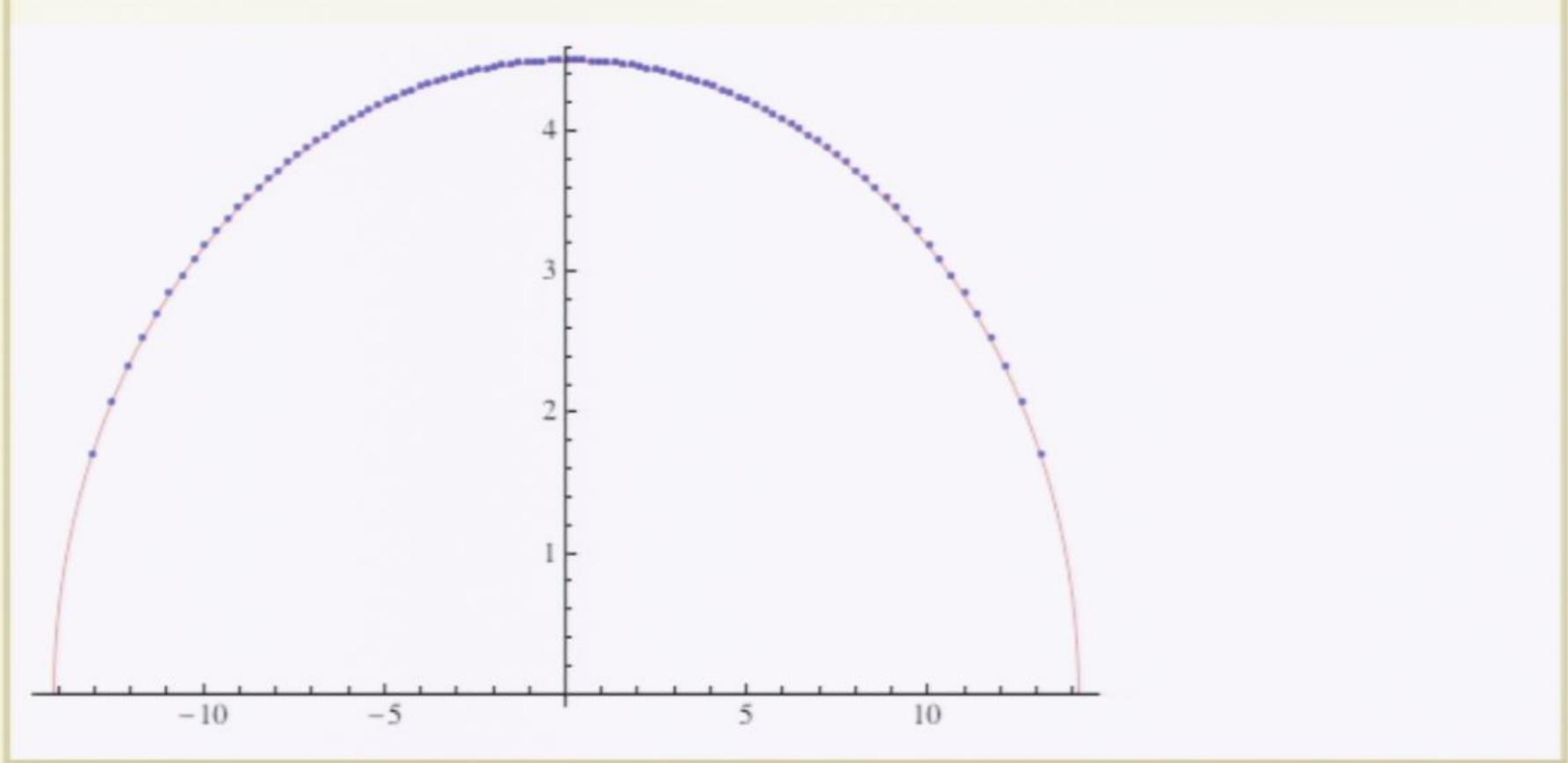
In[122]:=

```
Show[pl, lp]
```

Out[122]=

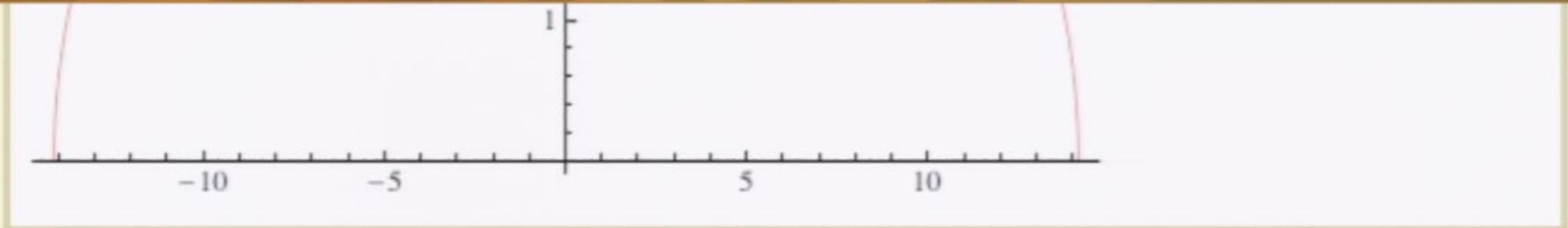


Out[122]=



```
In[58]:= g /@ {1, 2, 3}
g @ {1, 2, 3}
```

```
Out[58]= {g[1], g[2], g[3]}
```



```
In[58]:= g /@ {1, 2, 3}  
g@{1, 2, 3}
```

```
Out[58]= {g[1], g[2], g[3]}
```

```
Out[59]= g[{1, 2, 3}]
```

■ Hermite Polynomials



■ Hermite Polynomials

Live version

In[114]:= M = 100;

- Solving the equations
- Check of density
- Hermite Polynomials



Live version

In[114]:= `M = 100;`

- Solving the equations
- Check of density
- Hermite Polynomials

|

Live version

In[114]:= `M = 100;`

- Solving the equations
- Check of density
- Hermite Polynomials

`HermiteH[M, x]`

```
000 000 x72 -  
855 839 953 154 276 787 645 462 529 649 990 521 691 665 666 441 683 664 896 000 :  
000 x74 +  
7 807 662 730 530 244 378 520 009 042 420 966 162 801 160 465 783 780 802 560 000  
x76 -  
62 398 902 941 300 654 373 786 286 053 314 414 887 521 761 964 305 940 480 000  
x78 +  
434 422 741 996 396 960 830 157 687 712 948 458 077 683 152 916 054 016 000 x80 -  
2 616 216 452 853 941 347 968 429 314 742 237 025 460 302 035 025 920 000 x82 +  
13 508 862 923 514 327 097 943 696 978 014 993 246 782 970 920 960 000 x84 -  
59 135 925 246 574 345 709 192 654 349 723 636 648 023 949 312 000 x86 +  
216 275 588 676 081 724 119 304 378 499 511 732 777 517 056 000 x88 -  
648 016 745 096 874 079 758 215 366 290 671 858 509 414 400 x90 +  
1 548 057 202 811 452 651 118 526 914 215 651 835 904 000 x92 -  
2 833 323 638 181 565 135 883 828 715 105 288 192 000 x94 +  
3 728 057 418 659 954 126 162 932 519 875 379 200 x96 -  
3 137 435 235 564 867 768 704 340 433 305 600 x98 +  
1 267 650 600 228 229 401 496 703 205 376 x100
```

```

000 000 x72 -
855 839 953 154 276 787 645 462 529 649 990 521 691 665 666 441 683 664 896 000 :
000 x74 +
7 807 662 730 530 244 378 520 009 042 420 966 162 801 160 465 783 780 802 560 000
x76 -
62 398 902 941 300 654 373 786 286 053 314 414 887 521 761 964 305 940 480 000
x78 +
434 422 741 996 396 960 830 157 687 712 948 458 077 683 152 916 054 016 000 x80 -
2 616 216 452 853 941 347 968 429 314 742 237 025 460 302 035 025 920 000 x82 +
13 508 862 923 514 327 097 943 696 978 014 993 246 782 970 920 960 000 x84 -
59 135 925 246 574 345 709 192 654 349 723 636 648 023 949 312 000 x86 +
216 275 588 676 081 724 119 304 378 499 511 732 777 517 056 000 x88 -
648 016 745 096 874 079 758 215 366 290 671 858 509 414 400 x90 +
1 548 057 202 811 452 651 118 526 914 215 651 835 904 000 x92 -
2 833 323 638 181 565 135 883 828 715 105 288 192 000 x94 +
3 728 057 418 659 954 126 162 932 519 875 379 200 x96 -
3 137 435 235 564 867 768 704 340 433 305 600 x98 +
1 267 650 600 228 229 401 496 703 205 376 x100

```

Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```



- Check of density
- Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

Live version

```
In[114]:= M = 100;
```

- Solving the equations
- Check of density
- Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

Live version

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[118]:= eqs /. fr // Chop; (* check of equations *)
```

■ Check of density

■ Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[118]:= eqs /. fr // Chop; (* check of equations *)
```

■ Check of density

■ Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[118]:= eqs /. fr // Chop; (* check of equations *)
```

■ Check of density

■ Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
NSolve[H
```

```
In[114]:= M = 100;
```

■ Solving the equations

```
In[115]:= vars = {x[#], # - M/2} & /@ Range[M];  
eqs = x[#] -  $\sum_{k=1}^M \text{If}[\# == k, 0, \frac{1}{x[\#] - x[k]}]$  & /@ Range[M];
```

```
In[117]:= fr = FindRoot[eqs, vars];
```

```
In[118]:= eqs /. fr // Chop; (* check of equations *)
```

■ Check of density

■ Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
NSolve[HermiteH[M, x]]
```

```
{x → 1.88912 - 3.26509 × 10-8 i}, {x → 2.11295 + 1.62674 × 10-6 i},  
{x → 2.33733 - 0.0000194974 i}, {x → 2.5623 + 6.54176 × 10-7 i},  
{x → 2.788 - 3.53819 × 10-6 i}, {x → 3.01561 + 0.00364814 i},  
{x → 3.23443 + 0.00335743 i}, {x → 3.46756 + 0.158637 i},  
{x → 3.5597 - 0.164266 i}, {x → 3.77007 + 0.263802 i},  
{x → 3.9707 - 0.41326 i}, {x → 4.1282 + 0.419705 i},  
{x → 4.39816 - 0.60615 i}, {x → 4.47546 + 0.719175 i},  
{x → 4.6864 - 0.813229 i}, {x → 4.87914 + 0.994008 i},  
{x → 5.26176 + 1.03884 i}, {x → 5.27665 - 1.12554 i},  
{x → 5.42309 - 0.634532 i}, {x → 5.75579 + 1.4069 i},  
{x → 5.99028 - 1.30585 i}, {x → 6.06854 + 1.43692 i},  
{x → 6.57009 - 1.71242 i}, {x → 6.61592 + 1.65116 i},  
{x → 7.27034 - 1.75606 i}, {x → 7.31742 + 1.81212 i},  
{x → 7.96199 - 1.93226 i}, {x → 8.06244 + 1.90413 i},  
{x → 8.38372 - 2.01986 i}, {x → 8.85193 + 1.93964 i},  
{x → 9.22345 - 2.03044 i}, {x → 9.69597 + 1.89839 i},  
{x → 10.107 - 1.86676 i}, {x → 10.5887 + 1.67559 i},  
{x → 11.0388 - 1.73107 i}, {x → 11.5701 + 1.5409 i},  
{x → 11.9396 - 1.37923 i}, {x → 12.282 + 0.925798 i},  
{x → 12.5146 - 0.651076 i}, {x → 12.848 + 0.621395 i},  
{x → 13.0007 - 0.121423 i}, {x → 13.3897 + 0.0407832 i}
```

```
In[123]:= HermiteH[M, x]
```

```
In[124]:= NSolve[HermiteH[M, x] == 0, x]
```

Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
In[124]:= NSolve[HermiteH[M, x] == 0, x]
```

Hermite Polynomials

In[123]:=

```
HermiteH[M, x]
```

```
NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -1]
```

Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]
```

```
9.528965823390114804697065744307488780829168738449774517286045575:  
649936402309068284249526476544666858}, {x →  
9.832269807777969094355161531340931578094745392667077668701054067:  
094778754563657564781490827979714635}, {x →  
10.14450994129284546988858830144045594100473412126424677786447754:  
440810133919442229958708980901290237}, {x →  
10.46718542134281214178313316357805048536805919779128288455204873:  
296803629012201738135548914729525799}, {x →  
10.80226075368471459482166754925048490352246777012635158446582730:  
614467249911387252731247538215761284}, {x →  
11.15240438558512526489903525035673867121886647690732260455002788:  
401316875993099618797345238330084422}, {x →  
11.52141540078703024169421519361580678776230083373169929244322658:  
851144666468937682665399619490106780}, {x →  
11.91506194311416580198479791876277707078719271962430708269020433:  
754088327256838679816957056185944748}, {x →  
12.34296422285967429510274026687072750768421588599909694559654933:  
384204094405704233633165658160599804}, {x →  
12.82379974948780890633912881377721549748456726861033482492239296:  
918960235456168623348585269969198591}, {x →  
13.40648733814491013849801535865160714588975698129522505717205406:  
103979330879664050291316092727922929}}
```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540:
 6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929:
 6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493:
 3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043:
 3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265:
 8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278:
 8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273:
 0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487:
 3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775:
 4440810133919442229958708980901290237}, {x ->
-9.83226980777796909435516153134093157809474539266707766870105496:
 7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540 :
6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929 :
6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493 :
3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043 :
3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265 :
8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278 :
8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273 :
0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487 :
3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775 :
4440810133919442229958708980901290237}, {x ->
-9.83226980777796909435516153134093157809474539266707766870105486 :
7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[125]= {{x -> -13.40648733814491013849801535865160714588975698129522505717205406103979330879664050291316092727922929}, {x -> -12.82379974948780890633912881377721549748456726861033482492239296918960235456168623348585269969198591}, {x -> -12.34296422285967429510274026687072750768421588599909694559654933384204094405704233633165658160599804}, {x -> -11.91506194311416580198479791876277707078719271962430708269020433754088327256838679816957056185944748}, {x -> -11.52141540078703024169421519361580678776230083373169929244322658851144666468937682665399619490106780}, {x -> -11.15240438558512526489903525035673867121886647690732260455002788401316875993099618797345238330084422}, {x -> -10.80226075368471459482166754925048490352246777012635158446582730614467249911387252731247538215761284}, {x -> -10.46718542134281214178313316357805048536805919779128288455204873296803629012201738135548914729525799}, {x -> -10.14450994129284546988858830144045594100473412126424677786447754440810133919442229958708980901290237}, {x -> -9.832269807777969094355161531340931578094745392667077668701054967094778754563657564781490827979714635}, {x ->

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540 :
6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929 :
6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493 :
3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043 :
3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265 :
8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278 :
8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273 :
0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487 :
3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775 :
4440810133919442229958708980901290237}, {x ->
-9.83226980777796909435516153134093157809474539266707766870105486 :
7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540:
 6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929:
 6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493:
 3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043:
 3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265:
 8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278:
 8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273:
 0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487:
 3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775:
 4440810133919442229958708980901290237}, {x ->
-9.83226980777796909435516153134093157809474539266707766870105496:
 7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[125]= {{x -> -13.40648733814491013849801535865160714588975698129522505717205406103979330879664050291316092727922929}, {x -> -12.82379974948780890633912881377721549748456726861033482492239296918960235456168623348585269969198591}, {x -> -12.34296422285967429510274026687072750768421588599909694559654933384204094405704233633165658160599804}, {x -> -11.91506194311416580198479791876277707078719271962430708269020433754088327256838679816957056185944748}, {x -> -11.52141540078703024169421519361580678776230083373169929244322658851144666468937682665399619490106780}, {x -> -11.15240438558512526489903525035673867121886647690732260455002788401316875993099618797345238330084422}, {x -> -10.80226075368471459482166754925048490352246777012635158446582730614467249911387252731247538215761284}, {x -> -10.46718542134281214178313316357805048536805919779128288455204873296803629012201738135548914729525799}, {x -> -10.14450994129284546988858830144045594100473412126424677786447754440810133919442229958708980901290237}, {x -> -9.832269807777969094355161531340931578094745392667077668701054967094778754563657564781490827979714635}, {x ->

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540 :
6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929 :
6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493 :
3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043 :
3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265 :
8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278 :
8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273 :
0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487 :
3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775 :
4440810133919442229958708980901290237}, {x ->
-9.83226980777796909435516153134093157809474539266707766870105496 :
7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540 :
6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929 :
6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493 :
3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043 :
3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265 :
8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278 :
8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273 :
0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487 :
3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775 :
4440810133919442229958708980901290237}, {x ->
-9.83226980777796909435516153134093157809474539266707766870105496 :
7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[125]= {{x -> -13.40648733814491013849801535865160714588975698129522505717205406103979330879664050291316092727922929}, {x -> -12.82379974948780890633912881377721549748456726861033482492239296918960235456168623348585269969198591}, {x -> -12.34296422285967429510274026687072750768421588599909694559654933384204094405704233633165658160599804}, {x -> -11.91506194311416580198479791876277707078719271962430708269020433754088327256838679816957056185944748}, {x -> -11.52141540078703024169421519361580678776230083373169929244322658851144666468937682665399619490106780}, {x -> -11.15240438558512526489903525035673867121886647690732260455002788401316875993099618797345238330084422}, {x -> -10.80226075368471459482166754925048490352246777012635158446582730614467249911387252731247538215761284}, {x -> -10.46718542134281214178313316357805048536805919779128288455204873296803629012201738135548914729525799}, {x -> -10.14450994129284546988858830144045594100473412126424677786447754440810133919442229958708980901290237}, {x -> -9.832269807777969094355161531340931578094745392667077668701054967094778754563657564781490827979714635}, {x ->

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
-13.4064873381449101384980153586516071458897569812952250571720540 :
 6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929 :
 6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493 :
 3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043 :
 3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265 :
 8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278 :
 8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273 :
 0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487 :
 3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775 :
 4440810133919442229958708980901290237}, {x ->
-9.832269807777969094355161531340931578094745392667077668701054 :
 7094778754563657564781490827979714635}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[125]= {{x -> -13.40648733814491013849801535865160714588975698129522505717205406103979330879664050291316092727922929}, {x -> -12.82379974948780890633912881377721549748456726861033482492239296918960235456168623348585269969198591}, {x -> -12.34296422285967429510274026687072750768421588599909694559654933384204094405704233633165658160599804}, {x -> -11.91506194311416580198479791876277707078719271962430708269020433754088327256838679816957056185944748}, {x -> -11.52141540078703024169421519361580678776230083373169929244322658851144666468937682665399619490106780}, {x -> -11.15240438558512526489903525035673867121886647690732260455002788401316875993099618797345238330084422}, {x -> -10.80226075368471459482166754925048490352246777012635158446582730614467249911387252731247538215761284}, {x -> -10.46718542134281214178313316357805048536805919779128288455204873296803629012201738135548914729525799}, {x -> -10.14450994129284546988858830144045594100473412126424677786447754440810133919442229958708980901290237}, {x -> -9.832269807777969094355161531340931578094745392667077668701054867094778754563657564781490827979714635}, {x ->

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[125]= {{x -> -13.40648733814491013849801535865160714588975698129522505717205406103979330879664050291316092727922929}, {x -> -12.82379974948780890633912881377721549748456726861033482492239296918960235456168623348585269969198591}, {x -> -12.34296422285967429510274026687072750768421588599909694559654933384204094405704233633165658160599804}, {x -> -11.91506194311416580198479791876277707078719271962430708269020433754088327256838679816957056185944748}, {x -> -11.52141540078703024169421519361580678776230083373169929244322658851144666468937682665399619490106780}, {x -> -11.15240438558512526489903525035673867121886647690732260455002788401316875993099618797345238330084422}, {x -> -10.80226075368471459482166754925048490352246777012635158446582730614467249911387252731247538215761284}, {x -> -10.46718542134281214178313316357805048536805919779128288455204873296803629012201738135548914729525799}, {x -> -10.14450994129284546988858830144045594100473412126424677786447754440810133919442229958708980901290237}, {x -> -9.832269807777969094355161531340931578094745392667077668701054067094778754563657564781490827979714635}, {x ->

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
  -13.4064873381449101384980153586516071458897569812952250571720540
  6103979330879664050291316092727922929}, {x ->
  -12.8237997494878089063391288137772154974845672686103348249223929
  6918960235456168623348585269969198591}, {x ->
  -12.3429642228596742951027402668707275076842158859990969455965493
  3384204094405704233633165658160599804}, {x ->
  -11.9150619431141658019847979187627770707871927196243070826902043
  3754088327256838679816957056185944748}, {x ->
  -11.5214154007870302416942151936158067877623008337316992924432265
  8851144666468937682665399619490106780}, {x ->
  -11.1524043855851252648990352503567386712188664769073226045500278
  8401316875993099618797345238330084422}, {x ->
  -10.8022607536847145948216675492504849035224677701263515844658273
  0614467249911387252731247538215761284}, {x ->
  -10.4671854213428121417831331635780504853680591977912828845520487
  3296803629012201738135548914729525799}, {x ->
  -10.1445099412928454698885883014404559410047341212642467778644775
  4440810133919442229958708980901290237}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
  -13.4064873381449101384980153586516071458897569812952250571720540
  6103979330879664050291316092727922929}, {x ->
  -12.8237997494878089063391288137772154974845672686103348249223929
  6918960235456168623348585269969198591}, {x ->
  -12.3429642228596742951027402668707275076842158859990969455965493
  3384204094405704233633165658160599804}, {x ->
  -11.9150619431141658019847979187627770707871927196243070826902043
  3754088327256838679816957056185944748}, {x ->
  -11.5214154007870302416942151936158067877623008337316992924432265
  8851144666468937682665399619490106780}, {x ->
  -11.1524043855851252648990352503567386712188664769073226045500278
  8401316875993099618797345238330084422}, {x ->
  -10.8022607536847145948216675492504849035224677701263515844658273
  0614467249911387252731247538215761284}, {x ->
  -10.4671854213428121417831331635780504853680591977912828845520487
  3296803629012201738135548914729525799}, {x ->
  -10.1445099412928454698885883014404559410047341212642467778644775
  4440810133919442229958708980901290237}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
  -13.4064873381449101384980153586516071458897569812952250571720540
  6103979330879664050291316092727922929}, {x ->
  -12.8237997494878089063391288137772154974845672686103348249223929
  6918960235456168623348585269969198591}, {x ->
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  3384204094405704233633165658160599804}, {x ->
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  3754088327256838679816957056185944748}, {x ->
  -11.5214154007870302416942151936158067877623008337316992924432265
  8851144666468937682665399619490106780}, {x ->
  -11.1524043855851252648990352503567386712188664769073226045500278
  8401316875993099618797345238330084422}, {x ->
  -10.8022607536847145948216675492504849035224677701263515844658273
  0614467249911387252731247538215761284}, {x ->
  -10.4671854213428121417831331635780504853680591977912828845520487
  3296803629012201738135548914729525799}, {x ->
  -10.1445099412928454698885883014404559410047341212642467778644775
  4440810133919442229958708980901290237}, {x ->

```

In[123]:= HermiteH[M, x]

In[125]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

```

Out[125]= {{x ->
  -13.4064873381449101384980153586516071458897569812952250571720540
  6103979330879664050291316092727922929}, {x ->
  -12.8237997494878089063391288137772154974845672686103348249223929
  6918960235456168623348585269969198591}, {x ->
  -12.3429642228596742951027402668707275076842158859990969455965493
  3384204094405704233633165658160599804}, {x ->
  -11.9150619431141658019847979187627770707871927196243070826902043
  3754088327256838679816957056185944748}, {x ->
  -11.5214154007870302416942151936158067877623008337316992924432265
  8851144666468937682665399619490106780}, {x ->
  -11.1524043855851252648990352503567386712188664769073226045500278
  8401316875993099618797345238330084422}, {x ->
  -10.8022607536847145948216675492504849035224677701263515844658273
  0614467249911387252731247538215761284}, {x ->
  -10.4671854213428121417831331635780504853680591977912828845520487
  3296803629012201738135548914729525799}, {x ->
  -10.1445099412928454698885883014404559410047341212642467778644775
  4440810133919442229958708980901290237}, {x ->

```

In[123]:= HermiteH[M, x]

NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] // N

Out[125]=

```
{ {x ->
-13.4064873381449101384980153586516071458897569812952250571720540
6103979330879664050291316092727922929}, {x ->
-12.8237997494878089063391288137772154974845672686103348249223929
6918960235456168623348585269969198591}, {x ->
-12.3429642228596742951027402668707275076842158859990969455965493
3384204094405704233633165658160599804}, {x ->
-11.9150619431141658019847979187627770707871927196243070826902043
3754088327256838679816957056185944748}, {x ->
-11.5214154007870302416942151936158067877623008337316992924432265
8851144666468937682665399619490106780}, {x ->
-11.1524043855851252648990352503567386712188664769073226045500278
8401316875993099618797345238330084422}, {x ->
-10.8022607536847145948216675492504849035224677701263515844658273
0614467249911387252731247538215761284}, {x ->
-10.4671854213428121417831331635780504853680591977912828845520487
3296803629012201738135548914729525799}, {x ->
-10.1445099412928454698885883014404559410047341212642467778644775
4440810133919442229958708980901290237}, {x ->
```

```
{x → -10.1445}, {x → -9.83227}, {x → -9.52897}, {x → -9.23342},  
{x → -8.94469}, {x → -8.662}, {x → -8.3847}, {x → -8.11225},  
{x → -7.84418}, {x → -7.5801}, {x → -7.31965}, {x → -7.06253},  
{x → -6.80846}, {x → -6.55721}, {x → -6.30854}, {x → -6.06228},  
{x → -5.81823}, {x → -5.57624}, {x → -5.33616}, {x → -5.09785},  
{x → -4.86118}, {x → -4.62603}, {x → -4.3923}, {x → -4.15989},  
{x → -3.92869}, {x → -3.69862}, {x → -3.46959}, {x → -3.24151},  
{x → -3.01432}, {x → -2.78794}, {x → -2.5623}, {x → -2.33732},  
{x → -2.11295}, {x → -1.88912}, {x → -1.66576}, {x → -1.44283},  
{x → -1.22025}, {x → -0.997977}, {x → -0.775951}, {x → -0.554115},  
{x → -0.332415}, {x → -0.110796}, {x → 0.110796}, {x → 0.332415},  
{x → 0.554115}, {x → 0.775951}, {x → 0.997977}, {x → 1.22025},  
{x → 1.44283}, {x → 1.66576}, {x → 1.88912}, {x → 2.11295},  
{x → 2.33732}, {x → 2.5623}, {x → 2.78794}, {x → 3.01432}, {x → 3.24151},  
{x → 3.46959}, {x → 3.69862}, {x → 3.92869}, {x → 4.15989}, {x → 4.3923},  
{x → 4.62603}, {x → 4.86118}, {x → 5.09785}, {x → 5.33616},  
{x → 5.57624}, {x → 5.81823}, {x → 6.06228}, {x → 6.30854},  
{x → 6.55721}, {x → 6.80846}, {x → 7.06253}, {x → 7.31965},  
{x → 7.5801}, {x → 7.84418}, {x → 8.11225}, {x → 8.3847}, {x → 8.662},  
{x → 8.94469}, {x → 9.23342}, {x → 9.52897}, {x → 9.83227},  
{x → 10.1445}, {x → 10.4672}, {x → 10.8023}, {x → 11.1524},  
{x → 11.5214}, {x → 11.9151}, {x → 12.343}, {x → 12.8238}, {x → 13.4065}
```

- Check of density
- Hermite Polynomials

In[123]:= HermiteH[M, x]

In[126]:= NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] // N

Out[126]=

```
{ {x -> -13.4065}, {x -> -12.8238}, {x -> -12.343}, {x -> -11.9151},  
  {x -> -11.5214}, {x -> -11.1524}, {x -> -10.8023}, {x -> -10.4672},  
  {x -> -10.1445}, {x -> -9.83227}, {x -> -9.52897}, {x -> -9.23342},  
  {x -> -8.94469}, {x -> -8.662}, {x -> -8.3847}, {x -> -8.11225},  
  {x -> -7.84418}, {x -> -7.5801}, {x -> -7.31965}, {x -> -7.06253},  
  {x -> -6.80846}, {x -> -6.55721}, {x -> -6.30854}, {x -> -6.06228},  
  {x -> -5.81823}, {x -> -5.57624}, {x -> -5.33616}, {x -> -5.09785},  
  {x -> -4.86118}, {x -> -4.62603}, {x -> -4.3923}, {x -> -4.15989},  
  {x -> -3.92869}, {x -> -3.69862}, {x -> -3.46959}, {x -> -3.24151},  
  {x -> -3.01432}, {x -> -2.78794}, {x -> -2.5623}, {x -> -2.33732},  
  {x -> -2.11295}, {x -> -1.88912}, {x -> -1.66576}, {x -> -1.44283},  
  {x -> -1.22025}, {x -> -0.997977}, {x -> -0.775951}, {x -> -0.554115},  
  {x -> -0.332415}, {x -> -0.110796}, {x -> 0.110796}, {x -> 0.332415},  
  {x -> 0.554115}, {x -> 0.775951}, {x -> 0.997977}, {x -> 1.22025},  
  {x -> 1.44283}, {x -> 1.66576}, {x -> 1.88912}, {x -> 2.11295},
```

- Check of density
- Hermite Polynomials

In[123]:=

```
HermiteH[M, x]
```

```
fr
```

Out[126]=

```
NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]
```

```
{ {x -> -13.4065}, {x -> -12.8238}, {x -> -12.343}, {x -> -11.9151},  
  {x -> -11.5214}, {x -> -11.1524}, {x -> -10.8023}, {x -> -10.4672},  
  {x -> -10.1445}, {x -> -9.83227}, {x -> -9.52897}, {x -> -9.23342},  
  {x -> -8.94469}, {x -> -8.662}, {x -> -8.3847}, {x -> -8.11225},  
  {x -> -7.84418}, {x -> -7.5801}, {x -> -7.31965}, {x -> -7.06253},  
  {x -> -6.80846}, {x -> -6.55721}, {x -> -6.30854}, {x -> -6.06228},  
  {x -> -5.81823}, {x -> -5.57624}, {x -> -5.33616}, {x -> -5.09785},  
  {x -> -4.86118}, {x -> -4.62603}, {x -> -4.3923}, {x -> -4.15989},  
  {x -> -3.92869}, {x -> -3.69862}, {x -> -3.46959}, {x -> -3.24151},  
  {x -> -3.01432}, {x -> -2.78794}, {x -> -2.5623}, {x -> -2.33732},  
  {x -> -2.11295}, {x -> -1.88912}, {x -> -1.66576}, {x -> -1.44283},  
  {x -> -1.22025}, {x -> -0.997977}, {x -> -0.775951}, {x -> -0.554115},  
  {x -> -0.332415}, {x -> -0.110796}, {x -> 0.110796}, {x -> 0.332415}
```

```
x[17] → -7.84418, x[18] → -7.5801, x[19] → -7.31965, x[20] → -7.06253,  
x[21] → -6.80846, x[22] → -6.55721, x[23] → -6.30854, x[24] → -6.06228,  
x[25] → -5.81823, x[26] → -5.57624, x[27] → -5.33616, x[28] → -5.09785,  
x[29] → -4.86118, x[30] → -4.62603, x[31] → -4.3923, x[32] → -4.15989,  
x[33] → -3.92869, x[34] → -3.69862, x[35] → -3.46959, x[36] → -3.24151,  
x[37] → -3.01432, x[38] → -2.78794, x[39] → -2.5623, x[40] → -2.33732,  
x[41] → -2.11295, x[42] → -1.88912, x[43] → -1.66576,  
x[44] → -1.44283, x[45] → -1.22025, x[46] → -0.997977,  
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,  
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,  
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,  
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,  
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,  
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,  
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,  
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,  
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,  
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
x[17] → -7.84418, x[18] → -7.5801, x[19] → -7.31965, x[20] → -7.06253,  
x[21] → -6.80846, x[22] → -6.55721, x[23] → -6.30854, x[24] → -6.06228,  
x[25] → -5.81823, x[26] → -5.57624, x[27] → -5.33616, x[28] → -5.09785,  
x[29] → -4.86118, x[30] → -4.62603, x[31] → -4.3923, x[32] → -4.15989,  
x[33] → -3.92869, x[34] → -3.69862, x[35] → -3.46959, x[36] → -3.24151,  
x[37] → -3.01432, x[38] → -2.78794, x[39] → -2.5623, x[40] → -2.33732,  
x[41] → -2.11295, x[42] → -1.88912, x[43] → -1.66576,  
x[44] → -1.44283, x[45] → -1.22025, x[46] → -0.997977,  
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,  
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,  
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,  
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,  
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,  
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,  
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,  
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,  
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,  
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
x[17] → -7.84418, x[18] → -7.5801, x[19] → -7.31965, x[20] → -7.06253,  
x[21] → -6.80846, x[22] → -6.55721, x[23] → -6.30854, x[24] → -6.06228,  
x[25] → -5.81823, x[26] → -5.57624, x[27] → -5.33616, x[28] → -5.09785,  
x[29] → -4.86118, x[30] → -4.62603, x[31] → -4.3923, x[32] → -4.15989,  
x[33] → -3.92869, x[34] → -3.69862, x[35] → -3.46959, x[36] → -3.24151,  
x[37] → -3.01432, x[38] → -2.78794, x[39] → -2.5623, x[40] → -2.33732,  
x[41] → -2.11295, x[42] → -1.88912, x[43] → -1.66576,  
x[44] → -1.44283, x[45] → -1.22025, x[46] → -0.997977,  
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,  
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,  
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,  
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,  
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,  
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,  
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,  
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,  
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,  
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```

x[47] → 0.775951, x[48] → 0.997977, x[49] → 0.997977,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

NSolve[HermiteH[M, x] = 0, x, WorkingPrecision → 100]

Out[126]=

```

{{x → -13.4065}, {x → -12.8238}, {x → -12.343}, {x → -11.9151},
{x → -11.5214}, {x → -11.1524}, {x → -10.8023}, {x → -10.4672},
{x → -10.1445}, {x → -9.83227}, {x → -9.52897}, {x → -9.23342},
{x → -8.94469}, {x → -8.662}, {x → -8.3847}, {x → -8.11225},
{x → -7.84418}, {x → -7.5801}, {x → -7.31965}, {x → -7.06253},
{x → -6.80846}, {x → -6.55721}, {x → -6.30854}, {x → -6.06228},
{x → -5.81823}, {x → -5.57624}, {x → -5.33616}, {x → -5.09785},
{x → -4.86118}, {x → -4.62603}, {x → -4.3923}, {x → -4.15989}

```

```
x[47] → 0.775951, x[48] → 0.997977, x[49] → 0.997977,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.94869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

NSolve[HermiteH[M, x] = 0, x, WorkingPrecision → 100]

Out[126]=

```
{ {x → -13.4065}, {x → -12.8238}, {x → -12.343}, {x → -11.9151},
{x → -11.5214}, {x → -11.1524}, {x → -10.8023}, {x → -10.4672},
{x → -10.1445}, {x → -9.83227}, {x → -9.52897}, {x → -9.23342},
{x → -8.94469}, {x → -8.662}, {x → -8.3847}, {x → -8.11225},
{x → -7.84418}, {x → -7.5801}, {x → -7.31965}, {x → -7.06253},
{x → -6.80846}, {x → -6.55721}, {x → -6.30854}, {x → -6.06228},
{x → -5.81823}, {x → -5.57624}, {x → -5.33616}, {x → -5.09785},
{x → -4.86118}, {x → -4.62603}, {x → -4.3923}, {x → -4.15989}
```

```

x[47] → 0.775951, x[48] → 0.997977, x[49] → 0.997977,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[126]=

```

{{x → -13.4065}, {x → -12.8238}, {x → -12.343}, {x → -11.9151},
{x → -11.5214}, {x → -11.1524}, {x → -10.8023}, {x → -10.4672},
{x → -10.1445}, {x → -9.83227}, {x → -9.52897}, {x → -9.23342},
{x → -8.94469}, {x → -8.662}, {x → -8.3847}, {x → -8.11225},
{x → -7.84418}, {x → -7.5801}, {x → -7.31965}, {x → -7.06253},
{x → -6.80846}, {x → -6.55721}, {x → -6.30854}, {x → -6.06228},
{x → -5.81823}, {x → -5.57624}, {x → -5.33616}, {x → -5.09785},
{x → -4.86118}, {x → -4.62603}, {x → -4.3923}, {x → -4.15989}

```

```

x[47] → 0.775951, x[48] → 0.997977, x[49] → 0.997977,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

In[128]:=

x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100]

Out[126]=

```

{{x → -13.4065}, {x → -12.8238}, {x → -12.343}, {x → -11.9151},
{x → -11.5214}, {x → -11.1524}, {x → -10.8023}, {x → -10.4672},
{x → -10.1445}, {x → -9.83227}, {x → -9.52897}, {x → -9.23342},
{x → -8.94469}, {x → -8.662}, {x → -8.3847}, {x → -8.11225},
{x → -7.84418}, {x → -7.5801}, {x → -7.31965}, {x → -7.06253},
{x → -6.80846}, {x → -6.55721}, {x → -6.30854}, {x → -6.06228},
{x → -5.81823}, {x → -5.57624}, {x → -5.33616}, {x → -5.09785},
{x → -4.86118}, {x → -4.62603}, {x → -4.3923}, {x → -4.15989}

```

```
-8.1122473111627919172116920138170293561681703167016002110428366159 :  
95643449519034803433351115564832876 ,  
-7.8441823844608211687920795305108108525882918227801973984098026886 :  
96483123253287653012197925024910694 ,  
-7.5801008078574888842858087147798508005952446740540945677192169554 :  
99454094723384429679188047826916118 ,  
-7.3196528223045353163320619830886983154201857246217903244639380132 :  
70029963215354749281782509383683749 ,  
-7.0625310602488654374655227313402111369558533713012115279611172061 :  
75481411893453880065565481885226214 ,  
-6.8084633528587964144789809043219887893673137842015956696475008783 :  
56591614372026262188517613471895696 ,  
-6.5572070319215393159801431092748363242153412136855770618561199942 :  
45582030766853218823315804264891038 ,  
-6.3085443611121351216388174153874158418899967897332704833362499453 :  
99391265891556418506625037381671838 ,  
-6.0622788326143026386651846010776852194050157282097797276233160767 :  
66214532866635695049747813875485102 ,  
-5.8182321352035170473622698170478695905988755193471267208205267205 :  
95032128490952679030803981090929310 ,  
-5.5762416493299241033034851100970939533372038220981612782295494301 :  
09408297513216467040525628532896982 ,  
-5.3361583601383604972771152654631793693757767432758103958972702926 :  
50749446911965097429110659719200096 ,  
-5.0978451050891362470000919393992882018148316917197696067898879805 :
```

```

x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

In[128]:=

x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100]

Out[128]=

```

{-13.406487338144910138498015358651607145889756981295225057172054061\
03979330879664050291316092727922929,
-12.823799749487808906339128813777215497484567268610334824922392969\
18960235456168623348585269969198591,
-12.342964222859674295102740266870727507684215885999096945596549333\
84204094405704233633165658160599804,
-11.915061943114165801984797918762777070787192719624307082690204337\

```

```

x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

SolHx /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100]

Out[128]=

```

{-13.406487338144910138498015358651607145889756981295225057172054061
03979330879664050291316092727922929,
-12.823799749487808906339128813777215497484567268610334824922392969
18960235456168623348585269969198591,
-12.342964222859674295102740266870727507684215885999096945596549333
84204094405704233633165658160599804,
-11.915061943114165801984797918762777070787192719624307082690204337

```

```

x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100]

In[128]=

```

{-13.406487338144910138498015358651607145889756981295225057172054061.
03979330879664050291316092727922929,
-12.823799749487808906339128813777215497484567268610334824922392969.
18960235456168623348585269969198591,
-12.342964222859674295102740266870727507684215885999096945596549333.
84204094405704233633165658160599804,
-11.915061943114165801984797918762777070787192719624307082690204337.

```

```

x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

```

SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];

```

In[128]=

```

{-13.406487338144910138498015358651607145889756981295225057172054061.
03979330879664050291316092727922929,
-12.823799749487808906339128813777215497484567268610334824922392969.
18960235456168623348585269969198591,
-12.342964222859674295102740266870727507684215885999096945596549333.
84204094405704233633165658160599804,
-11.915061943114165801984797918762777070787192719624307082690204337.

```

```

x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```

In[129]:= **SolHer** = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];

```

Out[128]= {-13.406487338144910138498015358651607145889756981295225057172054061
03979330879664050291316092727922929,
-12.823799749487808906339128813777215497484567268610334824922392969
18960235456168623348585269969198591,
-12.342964222859674295102740266870727507684215885999096945596549333
84204094405704233633165658160599804,
-11.915061943114165801984797918762777070787192719624307082690204337

```

```
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,  
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,  
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,  
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,  
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,  
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,  
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,  
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,  
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,  
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
```

```
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,  
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,  
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,  
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,  
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,  
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,  
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,  
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,  
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,  
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
```

```
x /@ Ra
```

```
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,  
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,  
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,  
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,  
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,  
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,  
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,  
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,  
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,  
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
```

```
x /@ Range[]
```

```
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,  
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,  
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,  
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,  
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
```

```
In[130]:= x /@ Range[M]
```

```
Out[130]= {x[1], x[2], x[3], x[4], x[5], x[6], x[7], x[8], x[9], x[10],  
x[11], x[12], x[13], x[14], x[15], x[16], x[17], x[18], x[19],  
x[20], x[21], x[22], x[23], x[24], x[25], x[26], x[27], x[28],  
x[29], x[30], x[31], x[32], x[33], x[34], x[35], x[36], x[37],  
x[38], x[39], x[40], x[41], x[42], x[43], x[44], x[45], x[46],  
x[47], x[48], x[49], x[50], x[51], x[52], x[53], x[54], x[55],  
x[56], x[57], x[58], x[59], x[60], x[61], x[62], x[63], x[64],  
x[65], x[66], x[67], x[68], x[69], x[70], x[71], x[72], x[73],  
x[74], x[75], x[76], x[77], x[78], x[79], x[80], x[81], x[82],  
x[83], x[84], x[85], x[86], x[87], x[88], x[89], x[90], x[91],  
x[92], x[93], x[94], x[95], x[96], x[97], x[98], x[99], x[100]}
```

`x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}`

`in[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];`

`in[131]:= x /@ Range[M] /. fr`

`Out[131]=`

```
{-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

```
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
```

```
In[131]:= x /@ Range[M] /. fr
```

```
Out[131]= {-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

In[129]:= **SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];**

Solx /@ Range[M] /. fr

Out[131]=

```
{-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

In[129]:= **SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];**

SolElx /@ Range[M] /. fr

Out[131]=

```
{-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

```
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[129]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
```

```
SolEl = x /@ Range[M] /. fr
```

```
Out[131]= {-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,  
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,  
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,  
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,  
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,  
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,  
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,  
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,  
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,  
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,  
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,  
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,  
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,  
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,  
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```
SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
SolEl = x /@ Range[M] /. fr;
```

In[131]=

```
{-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];  
SolEl = x /@ Range[M] /. fr;
```

```
Out[131]= {-13.4065, -12.8238, -12.343, -11.9151, -11.5214, -11.1524, -10.8023,  
-10.4672, -10.1445, -9.83227, -9.52897, -9.23342, -8.94469,  
-8.662, -8.3847, -8.11225, -7.84418, -7.5801, -7.31965, -7.06253,  
-6.80846, -6.55721, -6.30854, -6.06228, -5.81823, -5.57624,  
-5.33616, -5.09785, -4.86118, -4.62603, -4.3923, -4.15989,  
-3.92869, -3.69862, -3.46959, -3.24151, -3.01432, -2.78794,  
-2.5623, -2.33732, -2.11295, -1.88912, -1.66576, -1.44283,  
-1.22025, -0.997977, -0.775951, -0.554115, -0.332415, -0.110796,  
0.110796, 0.332415, 0.554115, 0.775951, 0.997977, 1.22025, 1.44283,  
1.66576, 1.88912, 2.11295, 2.33732, 2.5623, 2.78794, 3.01432,  
3.24151, 3.46959, 3.69862, 3.92869, 4.15989, 4.3923, 4.62603,  
4.86118, 5.09785, 5.33616, 5.57624, 5.81823, 6.06228, 6.30854,  
6.55721, 6.80846, 7.06253, 7.31965, 7.5801, 7.84418, 8.11225,  
8.3847, 8.662, 8.94469, 9.23342, 9.52897, 9.83227, 10.1445, 10.4672,  
10.8023, 11.1524, 11.5214, 11.9151, 12.343, 12.8238, 13.4065}
```

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];  
SolEl = x /@ Range[M] /. fr;
```

```
SolE|
```

```
Out[134]= {0., 0., 0., 0., 1.77636 × 10-15, 0., 0., 0., 0., 0., 0.,  
0., 0., 0., 0., 0., 0., 0., -8.88178 × 10-16, -8.88178 × 10-16,  
-8.88178 × 10-16, 0., 0., 0., -8.88178 × 10-16, 0., -8.88178 × 10-16,  
-8.88178 × 10-16, 0., -8.88178 × 10-16, 0., -8.88178 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -8.88178 × 10-16,  
-4.44089 × 10-16, -6.66134 × 10-16, -6.66134 × 10-16, -6.66134 × 10-16,  
-6.66134 × 10-16, -5.55112 × 10-16, -7.77156 × 10-16, -6.66134 × 10-16,  
-5.55112 × 10-16, -5.41234 × 10-16, -5.82867 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -3.33067 × 10-16, -5.55112 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -8.88178 × 10-16,  
0., -8.88178 × 10-16, 0., -8.88178 × 10-16, 0., 0., -8.88178 × 10-16,  
0., -8.88178 × 10-16, 0., 0., 0., 0., 0., -8.88178 × 10-16,  
-8.88178 × 10-16, 0., -1.77636 × 10-15, -1.77636 × 10-15,  
-1.77636 × 10-15, 0., 0., 0., 0., 0., -1.77636 × 10-15, -1.77636 × 10-15,  
0., -1.77636 × 10-15, 0., -1.77636 × 10-15, -1.77636 × 10-15}
```

In[134]:=

SolEl - SolHer

Out[134]=

```
{0., 0., 0., 0., -1.77636 × 10-15, 0., 0., 0., 0., 0., 0.,  
0., 0., 0., 0., 0., 0., 0., -8.88178 × 10-16, -8.88178 × 10-16,  
-8.88178 × 10-16, 0., 0., 0., -8.88178 × 10-16, 0., -8.88178 × 10-16,  
-8.88178 × 10-16, 0., -8.88178 × 10-16, 0., -8.88178 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -8.88178 × 10-16,  
-4.44089 × 10-16, -6.66134 × 10-16, -6.66134 × 10-16, -6.66134 × 10-16,  
-6.66134 × 10-16, -5.55112 × 10-16, -7.77156 × 10-16, -6.66134 × 10-16,  
-5.55112 × 10-16, -5.41234 × 10-16, -5.82867 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -3.33067 × 10-16, -5.55112 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16,  
-4.44089 × 10-16, -4.44089 × 10-16, -4.44089 × 10-16, -8.88178 × 10-16,  
0., -8.88178 × 10-16, 0., -8.88178 × 10-16, 0., 0., -8.88178 × 10-16,  
0., -8.88178 × 10-16, 0., 0., 0., 0., 0., -8.88178 × 10-16,  
-8.88178 × 10-16, 0., -1.77636 × 10-15, -1.77636 × 10-15,  
-1.77636 × 10-15, 0., 0., 0., 0., 0., -1.77636 × 10-15, -1.77636 × 10-15
```

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];  
SolEl = x /@ Range[M] /. fr;
```

```
SolEl - SolHer // C
```

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];  
SolEl = x /@ Range[M] /. fr;
```

```
In[135]:= SolEl - SolHer // Chop
```

```
Out[135]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

```
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,
x[81] → 7.06253, x[82] → 7.31965, x[83] → 7.5801, x[84] → 7.84418,
x[85] → 8.11225, x[86] → 8.3847, x[87] → 8.662, x[88] → 8.94469,
x[89] → 9.23342, x[90] → 9.52897, x[91] → 9.83227, x[92] → 10.1445,
x[93] → 10.4672, x[94] → 10.8023, x[95] → 11.1524, x[96] → 11.5214,
x[97] → 11.9151, x[98] → 12.343, x[99] → 12.8238, x[100] → 13.4065}
```

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision → 100];
SolEl = x /@ Range[M] /. fr;
```

```
In[135]:= SolEl - SolHer // Chop
```

```
Out[135]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

In[123]:= hermite[n, x]

In[127]:= fr

Out[127]= {x[1] → -13.4065, x[2] → -12.8238, x[3] → -12.343, x[4] → -11.9151,
x[5] → -11.5214, x[6] → -11.1524, x[7] → -10.8023, x[8] → -10.4672,
x[9] → -10.1445, x[10] → -9.83227, x[11] → -9.52897, x[12] → -9.23342,
x[13] → -8.94469, x[14] → -8.662, x[15] → -8.3847, x[16] → -8.11225,
x[17] → -7.84418, x[18] → -7.5801, x[19] → -7.31965, x[20] → -7.06253,
x[21] → -6.80846, x[22] → -6.55721, x[23] → -6.30854, x[24] → -6.06228,
x[25] → -5.81823, x[26] → -5.57624, x[27] → -5.33616, x[28] → -5.09785,
x[29] → -4.86118, x[30] → -4.62603, x[31] → -4.3923, x[32] → -4.15989,
x[33] → -3.92869, x[34] → -3.69862, x[35] → -3.46959, x[36] → -3.24151,
x[37] → -3.01432, x[38] → -2.78794, x[39] → -2.5623, x[40] → -2.33732,
x[41] → -2.11295, x[42] → -1.88912, x[43] → -1.66576,
x[44] → -1.44283, x[45] → -1.22025, x[46] → -0.997977,
x[47] → -0.775951, x[48] → -0.554115, x[49] → -0.332415,
x[50] → -0.110796, x[51] → 0.110796, x[52] → 0.332415,
x[53] → 0.554115, x[54] → 0.775951, x[55] → 0.997977, x[56] → 1.22025,
x[57] → 1.44283, x[58] → 1.66576, x[59] → 1.88912, x[60] → 2.11295,
x[61] → 2.33732, x[62] → 2.5623, x[63] → 2.78794, x[64] → 3.01432,
x[65] → 3.24151, x[66] → 3.46959, x[67] → 3.69862, x[68] → 3.92869,
x[69] → 4.15989, x[70] → 4.3923, x[71] → 4.62603, x[72] → 4.86118,
x[73] → 5.09785, x[74] → 5.33616, x[75] → 5.57624, x[76] → 5.81823,
x[77] → 6.06228, x[78] → 6.30854, x[79] → 6.55721, x[80] → 6.80846,

In[123]:= HermiteH[M, x]

In[127]:= fr

In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];
 SolEl = x /@ Range[M] /. fr;

In[135]:= SolEl - SolHer // Chop

Out[135]:= {0,
 0,
 0,
 0, 0}

Hermite Polynomials

```
In[123]:= HermiteH[M, x]
```

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];  
SolEl = x /@ Range[M] /. fr;
```

```
In[135]:= SolEl - SolHer // Chop
```

```
Out[135]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check of density
- Hermite Polynomials

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];  

SolEl = x /@ Range[M] /. fr;
```

```
In[135]:= SolEl - SolHer // Chop
```

```
Out[135]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  

0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  

0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  

0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check of density

- Hermite Polynomials

```

In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];
           SolEl = x /@ Range[M] /. fr;
    
```

```

In[135]:= SolEl - SolHer // Chop
    
```

```

Out[135]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
           0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
           0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
           0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
    
```

- Check differential |

- Check of density
- Hermite Polynomials

```
In[132]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100];  
SolEl = x /@ Range[M] /. fr;
```

```
In[135]:= SolEl - SolHer // Chop
```

```
Out[135]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations|

- Check of density
- Hermite Polynomials

```
SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort|;  
SolEl = x /@ Range[M] /. fr;
```

In[135]:=

```
SolEl - SolHer // Chop
```

Out[135]=

```
{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[135]:= SolEl - SolHer // Chop
```

```
Out[135]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

- Check of density
- Hermite Polynomials

```
in[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
in[138]:= SolEl - SolHer // Chop
```

```
out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
q''
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

$$Q''[x] - 2xQ'[x] + 2MQ[x]$$

- Check of density
- Hermite Polynomials

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
          Sort;
          SolEl = x /@ Range[M] /. fr // Sort;
    
```

```

In[138]:= SolEl - SolHer // Chop
    
```

```

Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
           0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
           0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
           0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
    
```

- Check differential equations

```

Block[{Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0}
    
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
Block[{MQ''[x] - 2 x Q'[x] + 2 M Q[x] == 0
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
Block[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop  
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
In[139]:= Block[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0  
Out[139]= 200 Q[x] - 2 x Q'[x] + Q''[x] == 0
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
In[139]:= Block[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0]
```

```
Out[139]:= 200 Q[x] - 2 x Q'[x] + Q''[x] == 0
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
In[140]:= Module[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0]
```

```
Out[140]:= 2 M$334252 Q[x] - 2 x Q'[x] + Q''[x] == 0
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
a = 1|
```

```
In[140]:= Module[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0]
```

```
Out[140]:= 2 M$334252 Q[x] - 2 x Q'[x] + Q''[x] == 0
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
In[141]:= a = 1;
```

```
Block[[]
```

```
In[140]:= Module[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0]
```

- Check of density
- Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations

```
In[141]:= a = 1;
```

```
Block[{a}, a]
```

```
In[140]:= Module[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0]
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
In[141]:= a = 1;
```

```
In[142]:= Block[{a}, a]
```

```
Out[142]= 1
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
In[140]:= Module[{M}, Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0]
```

```
Out[140]= 2 M$334252 Q[x] - 2 x Q'[x] + Q''[x] == 0
```

■ Hermite Polynomials

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
    
```

```

In[138]:= SolEl - SolHer // Chop
    
```

```

Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
    
```

■ Check differential equations

```

Q''[x] - 2 x Q'[x] + 2 M Q[x] == 0
    
```

```

Out[140]= 2 M$334252 Q[x] - 2 x Q'[x] + Q''[x] == 0
    
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
 $Q''[x] - 2x Q'[x] + 2M Q[x] == 0$ 
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
∃
```

$$Q''[x] - 2x Q'[x] + 2M Q[x] == 0$$

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

$$Q''[x] - 2x Q'[x] + 2M Q[x] == 0$$

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
In[143]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0
```

```
Out[143]= 2 m Q[x] - 2 x Q'[x] + Q''[x] == 0
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
DSolve [Q'' [x] - 2 x Q' [x] + 2 m Q[x] == 0
```

```
Out[143]= 2 m Q[x] - 2 x Q'[x] + Q''[x] == 0
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0
```

```
Out[143]= 2 m Q[x] - 2 x Q'[x] + Q''[x] == 0
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0.]
```

Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

Check differential equations

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
```

```
Out[144]= {{Q -> Function[{x},  
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

Hermitic Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolE1 = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolE1 - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

Check differential equations

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
```

```
Out[144]:= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

Check differential equations

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
```

```
Out[144]= {{Q -> Function[{x},  
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

■ Hermite Polynomials

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
    
```

```

In[138]:= SolEl - SolHer // Chop
    
```

```

Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
    
```

■ Check differential equations

```

In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
    
```

```

Out[144]= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
    
```

■ Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
```

```
Out[144]= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

Hermite Polynomials

```
In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //  
Sort;  
SolEl = x /@ Range[M] /. fr // Sort;
```

```
In[138]:= SolEl - SolHer // Chop
```

```
Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

Check differential equations

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
```

```
Out[144]:= {{Q -> Function[{x},  
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;

```

```

In[138]:= SolEl - SolHer // Chop

```

```

Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}

```

Check differential equations

```

In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]

```

```

Out[144]:= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}

```

```

Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q

```

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
    
```

```

In[138]:= SolEl - SolHer // Chop
    
```

```

Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
    
```

■ Check differential equations

```

In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
    
```

```

Out[144]= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
    
```

```

Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_]
    
```

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;

```

```

In[138]:= SolEl - SolHer // Chop

```

```

Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}

```

■ Check differential equations

```

In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]

```

```

Out[144]:= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}

```

```

Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> Hermite[[]

```

```

In[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] //
Sort;
SolEl = x /@ Range[M] /. fr // Sort;
    
```

```

In[138]:= SolEl - SolHer // Chop
    
```

```

Out[138]:= {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
    
```

■ Check differential equations

```

In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
    
```

```

Out[144]:= {{Q -> Function[{x},
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
    
```

```

Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
    
```

In[138]:= **SolEl - SolHer // Chop**

Out[138]:= {0,
 0,
 0,
 0, 0}

■ Check differential equations

In[144]:= **DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]**

Out[144]:= {{Q → Function[{x},
 C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}

In[145]:= **Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] → HermiteH[m, x]**

Out[145]:= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]

In[138]:=

SolE1 - SolHer // Chop

Out[138]=

```
{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

In[144]:=

$$\mathbf{DSolve}[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]$$

Out[144]=

```
{ { { Q → Function[{x},
      C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2] ] ] } }
```

$$x^2 + |$$

In[145]:=

$$Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$$

Out[145]=

$$2 m \text{HermiteH}[m, x] - 2 x O'[x] + O''[x]$$

In[138]:=

`SolE1 - SolHer // Chop`

Out[138]=

```
{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

In[144]:=

`DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]`

Out[144]=

```
{ { Q -> Function[{x},  
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]] } }
```

In[146]:=

`x^2 + x^3 /. x^y -> f[y]`

Out[146]=

`f[2] + f[3]`

```
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

■ Check differential equations

In[144]:= `DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]`

Out[144]:= $\left\{ \left\{ Q \rightarrow \text{Function}\left[\{x\}, \right. \right. \right.$
 $\left. \left. \left. C[1] \text{ HermiteH}[m, x] + C[2] \text{ Hypergeometric1F1}\left[-\frac{m}{2}, \frac{1}{2}, x^2\right]\right] \right\} \right\}$

In[146]:= `x^2 + x^3 /. x^y -> f[y]`

Out[146]:= `f[2] + f[3]`

In[145]:= `Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]`

Out[145]:= `2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]`

■ Check differential equations

In[144]:= `DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]`

Out[144]:= $\left\{ \left\{ Q \rightarrow \text{Function} \left[\{x\}, \right. \right. \right.$
 $\left. \left. \left. C[1] \text{HermiteH}[m, x] + C[2] \text{Hypergeometric1F1} \left[-\frac{m}{2}, \frac{1}{2}, x^2 \right] \right] \right\} \right\}$

In[146]:= `x2 + x3 /. xy -> f[y]`

Out[146]:= `f[2] + f[3]`

In[145]:= `Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]`

Out[145]:= `2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]`

`Q'[x]`

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
Out[144]= {{Q -> Function[{x},
  C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

```
In[146]:= x^2 + x^3 /. x^y -> f[y]
Out[146]= f[2] + f[3]
```

```
In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
Out[145]= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]
```

```
In[147]:= Q'[x] // FullForm
Out[147]//FullForm= Derivative[1][Q][x]
```

```
In[144]:= DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]
Out[144]= {{Q -> Function[{x},
  C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
```

```
In[146]:= x^2 + x^3 /. x^y_ -> f[y]
Out[146]= f[2] + f[3]
```

```
In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
Out[145]= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]
```

```
In[147]:= Q'[x] // FullForm
Out[147]//FullForm= Derivative[1][Q][x]
```

```

In[144]:= {{Q -> Function[{x},
    C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
    
```

```

In[146]:= x^2 + x^3 /. x^y -> f[y]
Out[146]:= f[2] + f[3]
    
```

```

In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
Out[145]:= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]
    
```

```

In[147]:= Q'[x] // FullForm
Out[147]//FullForm=
    Derivative[1][Q][x]
    
```

```

In[ ]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
    
```

In[144]:= $\left\{ \left\{ Q \rightarrow \text{Function} \left[\{x\}, \right. \right. \right.$
 $\left. \left. C[1] \text{ HermiteH}[m, x] + C[2] \text{ Hypergeometric1F1} \left[-\frac{m}{2}, \frac{1}{2}, x^2 \right] \right] \right\} \right\}$

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm= $\text{Derivative}[1][Q][x]$

In[]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow [x_] \rightarrow \text{HermiteH}[m, x]$

```

In[144]:= {{Q -> Function[{x},
      C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}
    
```

```

In[146]:= x^2 + x^3 /. x^y -> f[y]
    
```

```

Out[146]= f[2] + f[3]
    
```

```

In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
    
```

```

Out[145]= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]
    
```

```

In[147]:= Q'[x] // FullForm
    
```

```

Out[147]//FullForm= Derivative[1][Q][x]
    
```

```

In[148]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> Her
    
```

```

In[144]:= {{Q -> Function[{x},
              C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]}}

```

```

In[146]:= x^2 + x^3 /. x^y_ -> f[y]

```

```

Out[146]:= f[2] + f[3]

```

```

In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]

```

```

Out[145]:= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]

```

```

In[147]:= Q'[x] // FullForm

```

```

Out[147]//FullForm=
Derivative[1][Q][x]

```

```

In[148]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> HermiteH[m, #] &

```

[2 2]]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[148]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&)$

Out[148]= $4 (-1 + m) m \text{HermiteH}[-2 + m, x] -$
 $4 x m \text{HermiteH}[-1 + m, x] + 2 m \text{HermiteH}[m, x]$

[2 2]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[149]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{Simplify}$

Out[149]= $2 m (2 (-1 + m) \text{HermiteH}[-2 + m, x] - 2 x \text{HermiteH}[-1 + m, x] + \text{HermiteH}[m, x])$

[2 2]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[150]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[150]= 0

[2 2]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[150]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[150]= 0

[2 2]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

$0 == |Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[150]= 0

[2 2]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[151]:= $0 == | Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[151]= True

[2 2]]]]

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

$f''[x] + |$

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

$f''[x] + \omega^2 f[x]$

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

$f''[x] + \omega^2 f[x] /. f \rightarrow A \text{Sin}[B \#] \&|$

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

$f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

In[146]:= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm= $\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

In[146]:= $f[2] + f[3]$

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

```
In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
```

```
Out[145]= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]
```

```
In[147]:= Q'[x] // FullForm
```

```
Out[147]//FullForm=
```

```
Derivative[1][Q][x]
```

```
In[152]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (HermiteH[m, #] &) // FullSimplify
```

```
Out[152]= 0
```

```
In[153]:= f''[x] + ω2 f[x] /. f -> (A Sin[B #] &)
```

```
Out[153]= -A B2 Sin[B x] + A ω2 Sin[B x]
```

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm= $\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

▣ About Simplify and FullSimplify

Simpoi

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

▣ About Simplify and FullSimplify

Simplify[Exp[]

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

▣ About Simplify and FullSimplify

$\text{Simplify}[\text{Exp}[I x] + \text{Exp}[-I x]]$

In[147]:= $Q'[x] // FullForm$

Out[147]//FullForm=

Derivative[1][Q][x]

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (HermiteH[m, \#] \&) // FullSimplify$

Out[152]=

0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \sin[B \#] \&)$

Out[153]=

$-A B^2 \sin[B x] + A \omega^2 \sin[B x]$

About Simplify and FullSimplify

In[154]:= $Simplify[\text{Exp}[I x] + \text{Exp}[-I x]]$

Out[154]=

$e^{-i x} + e^{i x}$

```
In[147]:= Q'[x] // FullForm
```

```
Out[147]//FullForm=
```

```
Derivative[1][Q][x]
```

```
In[152]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (HermiteH[m, #] &) // FullSimplify
```

```
Out[152]= 0
```

```
In[153]:= f''[x] +  $\omega^2$  f[x] /. f -> (A Sin[B #] &)
```

```
Out[153]= -A B2 Sin[B x] + A  $\omega^2$  Sin[B x]
```

▫ About Simplify and FullSimplify

```
In[155]:= FullSimplify[Exp[I x] + Exp[-I x]]
```

```
Out[155]= 2 Cos[x]
```

```
In[147]:= Q'[x] // FullForm
```

```
Out[147]//FullForm=
```

```
Derivative[1][Q][x]
```

```
In[152]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (HermiteH[m, #] &) // FullSimplify
```

```
Out[152]= 0
```

```
In[153]:= f''[x] +  $\omega^2$  f[x] /. f -> (A Sin[B #] &)
```

```
Out[153]= -A B2 Sin[B x] + A  $\omega^2$  Sin[B x]
```

▫ About Simplify and FullSimplify

```
In[155]:= FullSimplify[Exp[I x] + Exp[-I x]]
```

```
Out[155]= 2 Cos[x]
```

In[147]:= $Q'[x]$ // FullForm

Out[147]//FullForm=

Derivative[1][Q][x]

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x]$ /. $Q \rightarrow (\text{HermiteH}[m, \#] \&)$ // FullSimplify

Out[152]=

0

In[153]:= $f''[x] + \omega^2 f[x]$ /. $f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]=

$-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

About Simplify and FullSimplify

In[155]:= FullSimplify[Exp[I x] + Exp[-I x]]

Out[155]=

2 Cos[x]

Exp[I x] + Exp[-I x]

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

▫ About Simplify and FullSimplify

In[155]:= $\text{FullSimplify}[\text{Exp}[I x] + \text{Exp}[-I x]]$

Out[155]= $2 \text{Cos}[x]$

In[156]:= $\text{Exp}[I x] + \text{Exp}[-I x] // \text{FullForm}$

Out[156]/FullForm=

$\text{Plus}[\text{Power}[E, \text{Times}[\text{Complex}[0, -1], x]], \text{Power}[E, \text{Times}[\text{Complex}[0, 1], x]]]$

Out[152]=

0

In[153]:=

$f''[x] + \omega^2 f[x] /. f \rightarrow (A \sin[B \#] \&)$

Out[153]=

$-A B^2 \sin[B x] + A \omega^2 \sin[B x]$

□ About Simplify and FullSimplify

In[155]:=

`FullSimplify[Exp[I x] + Exp[-I x]]`

Out[155]=

$2 \cos[x]$

In[156]:=

`Exp[I x] + Exp[-I x] // FullForm`

Out[156]//FullForm=

`Plus[Power[E, Times[Complex[0, -1], x]],
Power[E, Times[Complex[0, 1], x]]]`

Out[152]=

0

In[153]:=

 $f''[x] + \omega^2 f[x] /. f \rightarrow (A \sin[B \#] \&)$

Out[153]=

 $-A B^2 \sin[B x] + A \omega^2 \sin[B x]$

□ About Simplify and FullSimplify

In[155]:=

`FullSimplify[Exp[I x] + Exp[-I x]]`

Out[155]=

2 Cos[x]

In[156]:=

`Exp[I x] + Exp[-I x] // FullForm`

Out[156]//FullForm=

```
Plus[Power[E, Times[Complex[0, -1], x]],  
      Power[E, Times[Complex[0, 1], x]]]
```

Out[152]=

0

In[153]:=

$f''[x] + \omega^2 f[x] /. f \rightarrow (A \sin[B \#] \&)$

Out[153]=

$-A B^2 \sin[B x] + A \omega^2 \sin[B x]$

About Simplify and FullSimplify

In[155]:=

`FullSimplify[Exp[I x] + Exp[-I x]]`

Out[155]=

$2 \cos[x]$

In[156]:=

`Exp[I x] + Exp[-I x] // FullForm`

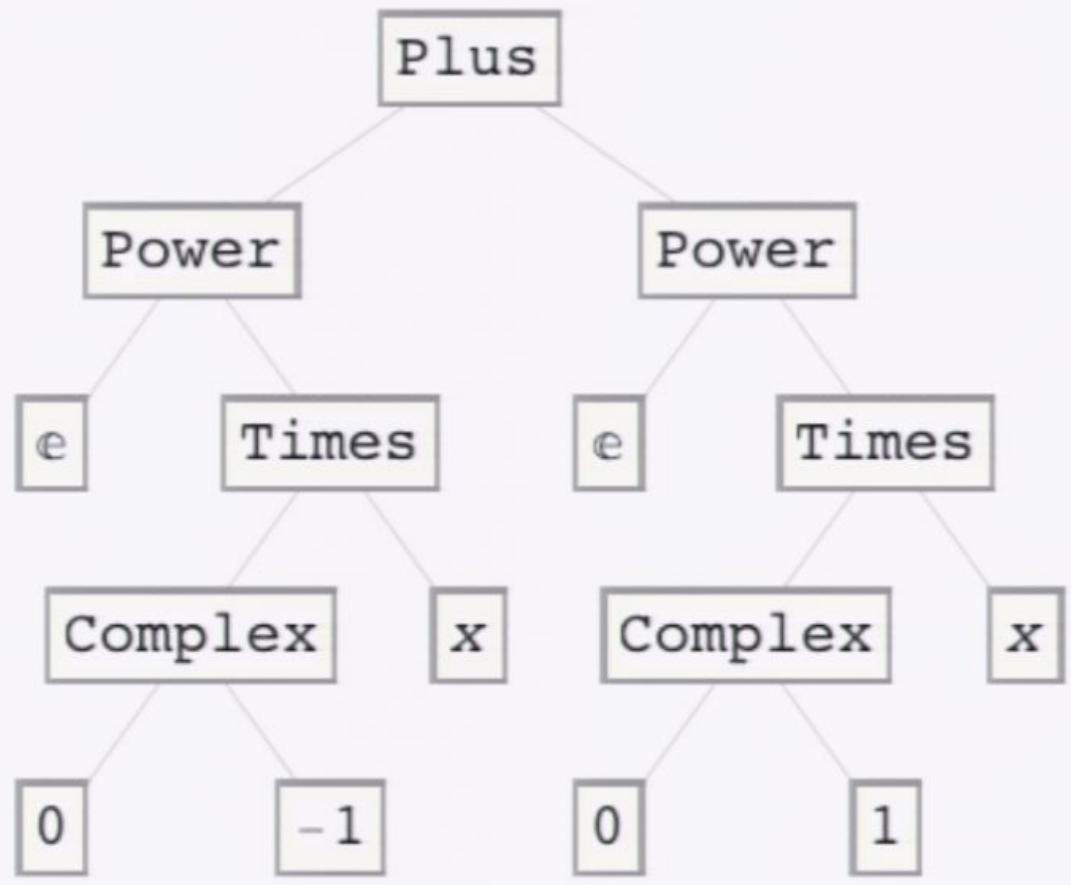
Out[156]//FullForm=

`Plus[Power[E, Times[Complex[0, -1], x]],
Power[E, Times[Complex[0, 1], x]]]`

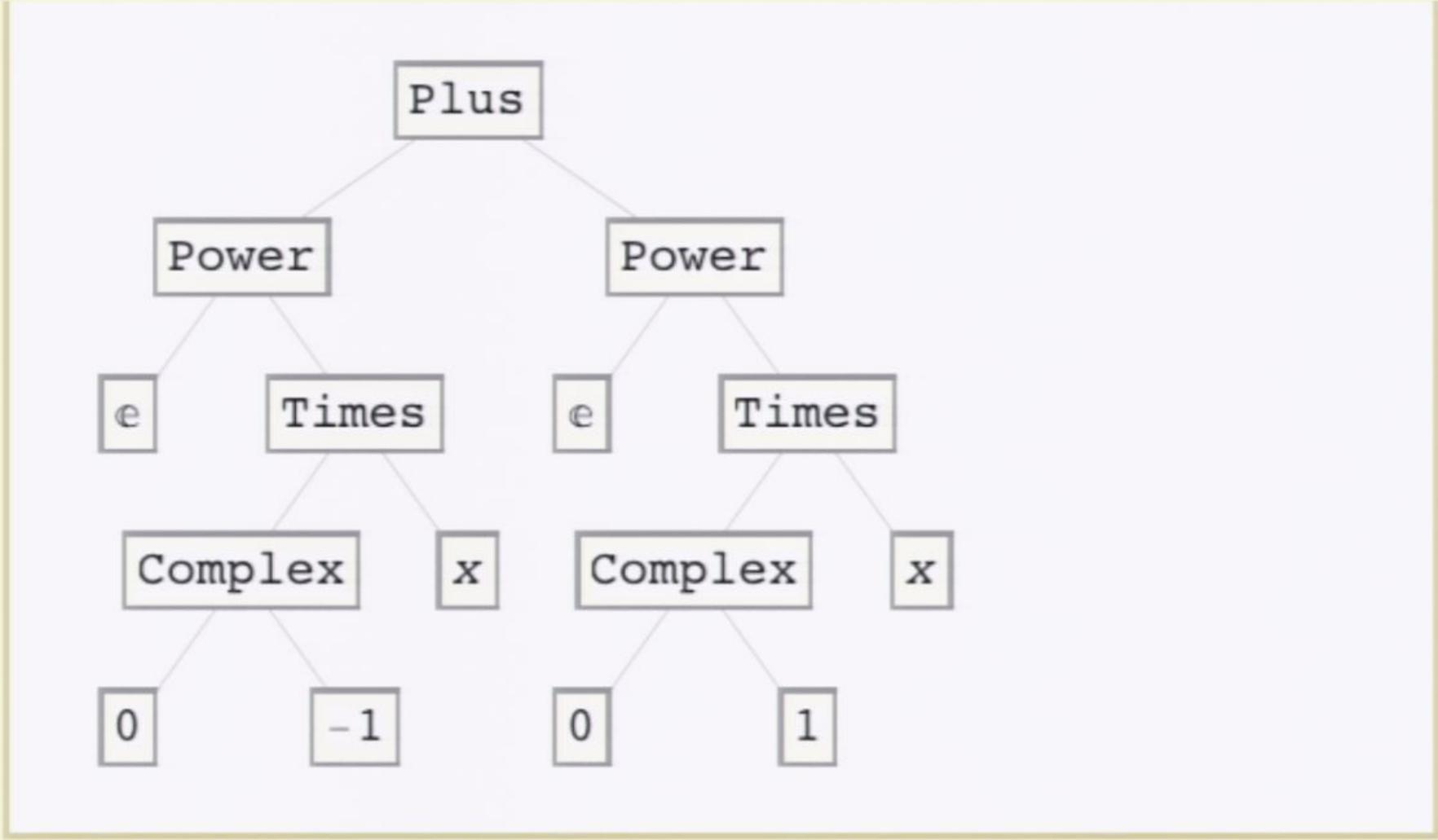
`Exp[I x] + Exp[-I x] // Tr`

In[157]:= Exp[I x] + Exp[-I x] // TreeForm

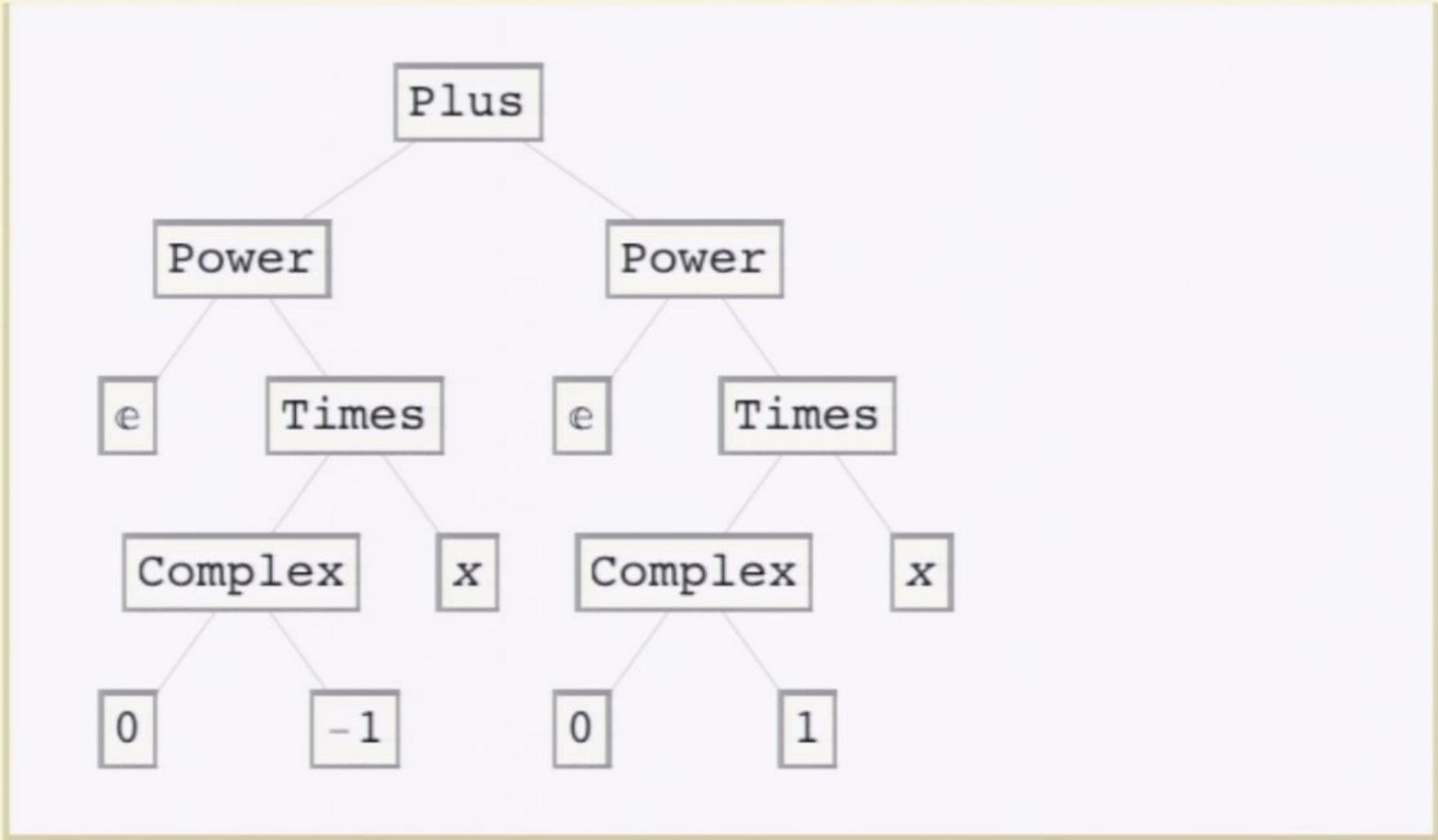
Out[157]//TreeForm=

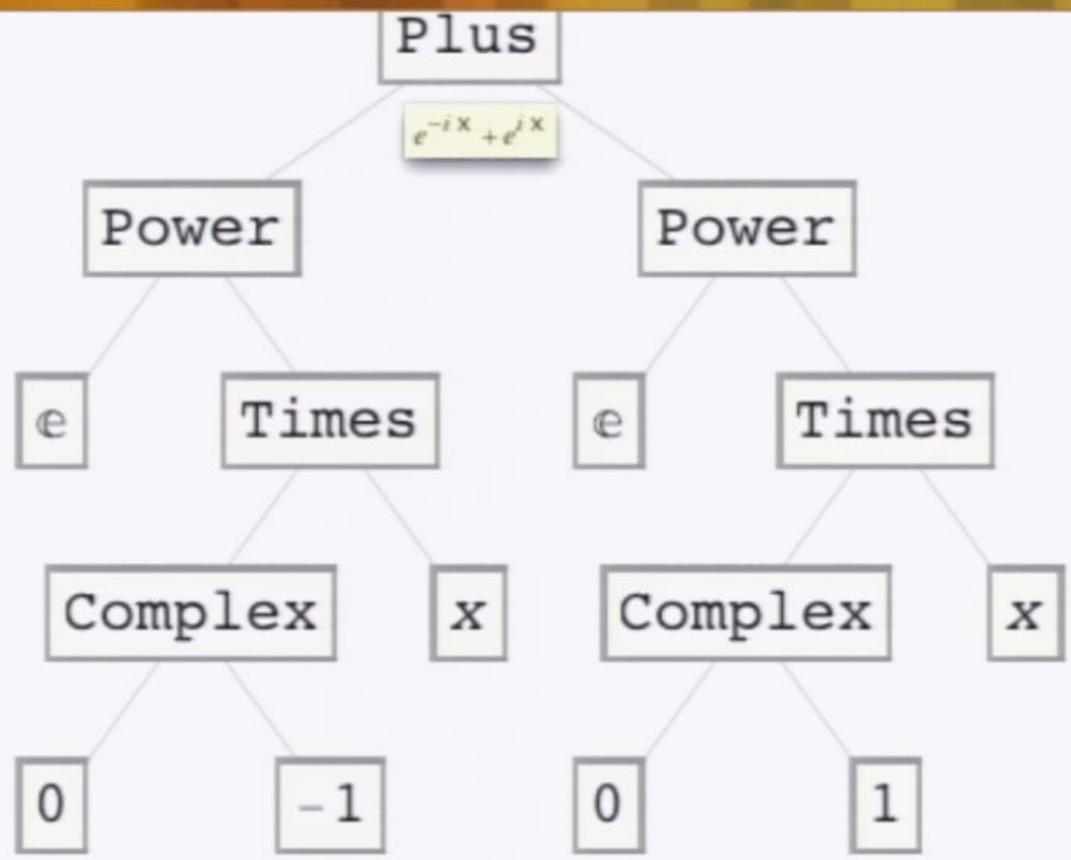


(157)/TreeForm=



In[157]/TreeForm=





```
In[158]:= FullSimplify[Exp[I x] + Exp[-I x]]
```

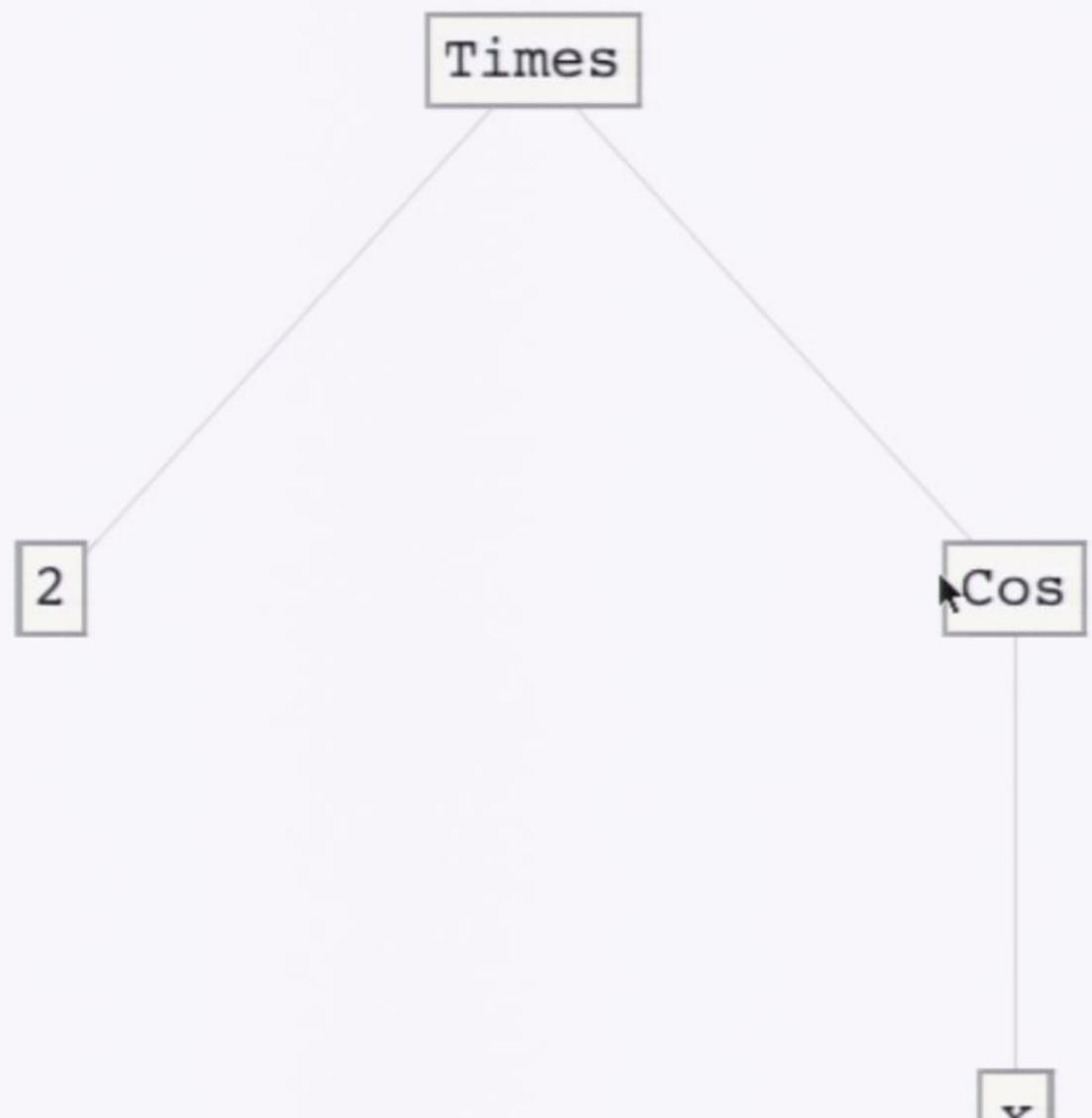
```
Out[158]= 2 Cos[x]
```

2

Cos

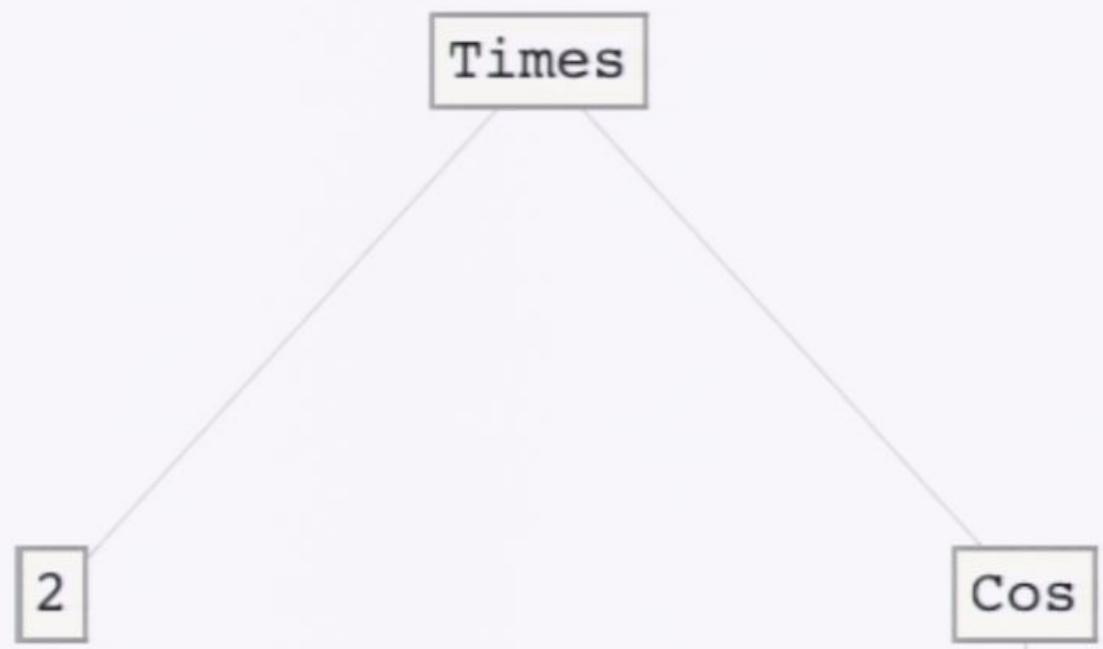
x

[159]/TreeForm=



```
In[159]:= FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm
```

Out[159]/TreeForm=

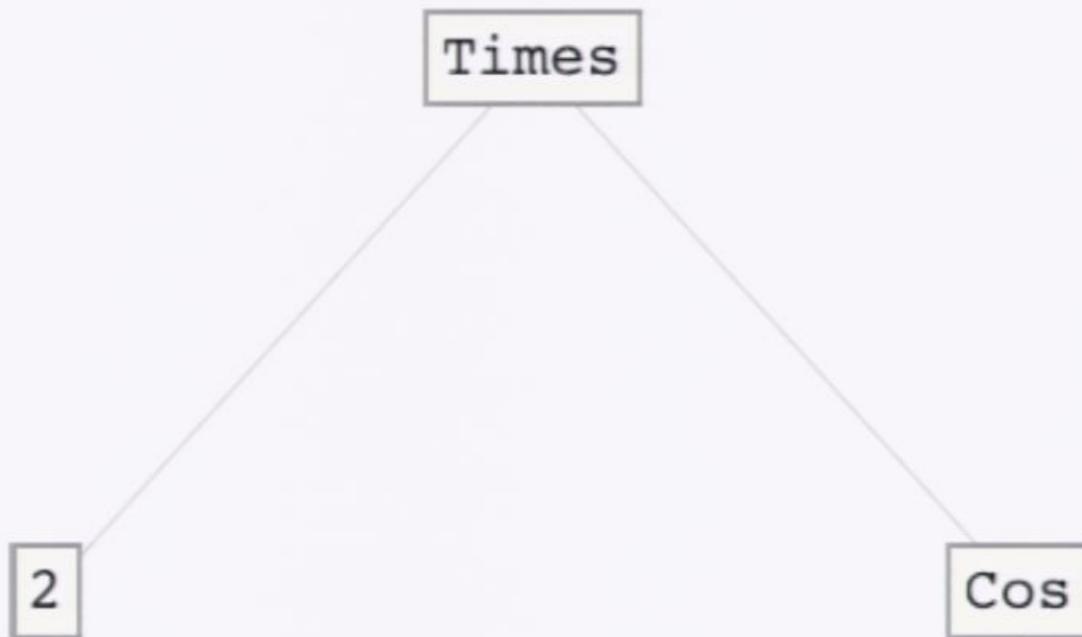


0 -1 0 1

```
FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm
```

```
In[159]:= FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm
```

```
Out[159]/TreeForm=
```



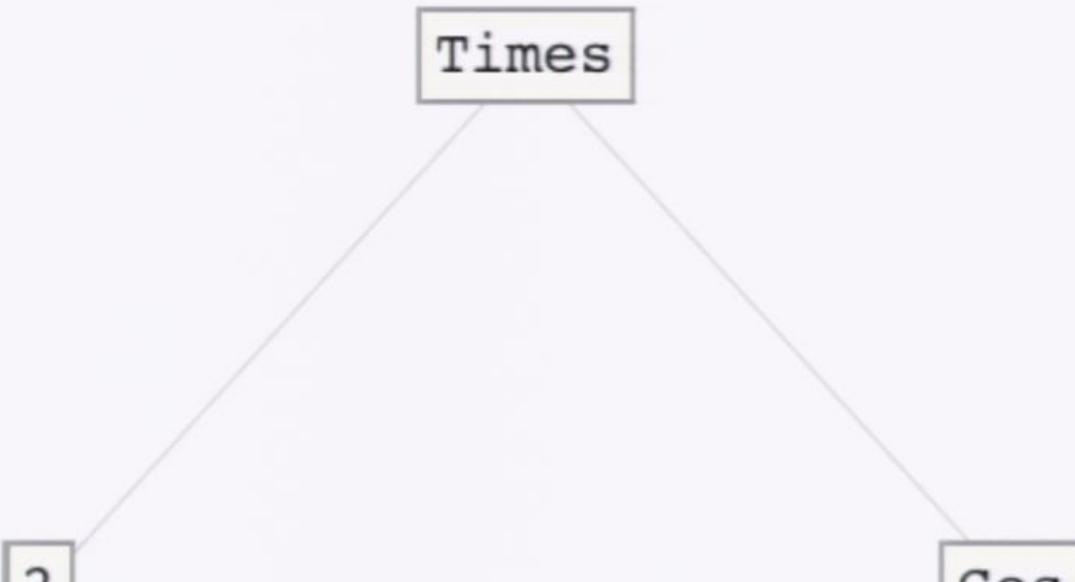
0 -1 0 1

In[160]:= FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount

Out[160]= 4

In[159]:= FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm

Out[159]//TreeForm=



```
Plus[Power[E, Times[Complex[0, -1], x]],  
      Power[E, Times[Complex[0, 1], x]]]
```



```
In[157]:= Exp[I x] + Exp[-I x] // TreeForm
```

```
In[160]:= FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount
```

```
Out[160]= 4
```

```
In[159]:= FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm
```

```
Out[159]//TreeForm=
```

Times

```
Plus[Power[E, Times[Complex[0, -1], x]],  
      Power[E, Times[Complex[0, 1], x]]]
```

In[157]:= **Exp[I x] + Exp[-I x] // TreeForm**

```
Exp[I x] + Exp[-I x] // Leaf
```

In[160]:= **FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount**

Out[160]= 4

In[159]:= **FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm**

Out[159]//TreeForm=

```
graph TD; Times[Times];
```

```
Plus[Power[E, Times[Complex[0, -1], x]],  
      Power[E, Times[Complex[0, 1], x]]]
```

In[157]:= **Exp[I x] + Exp[-I x] // TreeForm**

In[161]:= **Exp[I x] + Exp[-I x] // LeafCount**

Out[161]= 15

In[160]:= **FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount**

Out[160]= 4

In[159]:= **FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm**

Out[159]//TreeForm=

```
graph TD; Times[Times];
```

```
Plus[Power[E, Times[Complex[0, -1], x]],  
      Power[E, Times[Complex[0, 1], x]]]
```

```
In[157]:= Exp[I x] + Exp[-I x] // TreeForm
```

```
In[161]:= Exp[I x] + Exp[-I x] // LeafCount
```

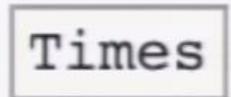
Out[161]= 15

```
In[160]:= FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount
```

Out[160]= 4

```
In[159]:= FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm
```

Out[159]//TreeForm=



```
Plus[Power[E, Times[Complex[0, -1], x]],
      Power[E, Times[Complex[0, 1], x]]]
```

In[157]:= **Exp[I x] + Exp[-I x] // TreeForm**

In[161]:= **Exp[I x] + Exp[-I x] // LeafCount**

Out[161]= 15

In[160]:= **FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount**

Out[160]= 4

$\sqrt{\square}$

In[159]:= **FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm**

Out[159]//TreeForm=

Times

```
Plus[Power[E, Times[Complex[0, -1], x]],  
      Power[E, Times[Complex[0, 1], x]]]
```

In[157]:= **Exp[I x] + Exp[-I x] // TreeForm**

In[161]:= **Exp[I x] + Exp[-I x] // LeafCount**

Out[161]= 15

In[160]:= **FullSimplify[Exp[I x] + Exp[-I x]] // LeafCount**

Out[160]= 4

In[159]:= **FullSimplify[Exp[I x] + Exp[-I x]] // TreeForm**

Out[159]//TreeForm=

Times

In[147]:= $Q'[x] // FullForm$

Out[147]/FullForm=

Derivative[1][Q][x]

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (HermiteH[m, \#] \&) // FullSimplify$

Out[152]=

0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \sin[B \#] \&)$

Out[153]= $-A B^2 \sin[B x] + A \omega^2 \sin[B x]$

▫ About Simplify and FullSimplify

In[155]:= $FullSimplify[Exp[I x] + Exp[-I x]]$

Out[155]= $2 \cos[x]$

In[156]:= $Exp[I x] + Exp[-I x] // FullForm$

In[147]:= $Q'[x]$ // FullForm

Out[147]/FullForm=

Derivative[1][Q][x]

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x]$ /. $Q \rightarrow (\text{HermiteH}[m, \#] \&)$ // FullSimplify

Out[152]=

0

In[153]:= $f''[x] + \omega^2 f[x]$ /. $f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

▢ About Simplify and FullSimplify

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2 m \text{HermiteH}[m, x] - 2 x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]=

0

In[155]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

In[146]:= $x^2 + x^3 /. x^y \rightarrow f[y]$

Out[146]= $f[2] + f[3]$

In[145]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2xQ'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$


```
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations
- From the equation |

```
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
```

- Check differential equations
- From the equation for $Q(x)$ to the equation |


```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for $Q(x)$ to the equation for $G(x)$

```
in[162]:= Q''[x] - 2 x Q'[x] + 2 m Q[x]
```

```
out[162]:= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

```
in[162]:= Q''[x] - 2 x Q'[x] + 2 m Q[x]    {
```

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

In[118]:= eqs /. rr // Chop; (* check of equations *)

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q - I$$
$$2 m Q[x] - 2 x Q'[x] + Q''[x]$$

Out[162]=

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}[\int]$$

$$\text{out[162]}= 2m Q[x] - 2x Q'[x] + Q''[x]$$

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}[\int$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
:int|
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}[\int]$$
$$\text{out[162]}= 2m Q[x] - 2x Q'[x] + Q''[x]$$

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

$$\int$$

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

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out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
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$$\int$$

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
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- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[163]:=  $\int^x G[y] dy$ 
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

$$\int G[y] dy$$

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[163]:= \int G[y] dy
```

```
out[163]= \int G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[163]:= \int G[y] dy
```

```
out[163]= \int G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

$$\int_{0|} G[y] dy$$

```
out[163]= \int G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

$$\int_0^a G[y] dy$$

```
out[163]= \int G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp}\left[\int G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[164]:= \int_0^x G[y] dy
```

```
out[164]= \int_0^x G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \text{Exp} \left[\int_0^x G[x_] \right]$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[164]:= \int_0^x G[y] dy
```

```
out[164]= \int_0^x G[y] dy
```

```
In[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow \text{Exp}\left[\int_0^x G[x_] \right]$$

```
Out[162]:= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
In[164]:= \int_0^x G[y] dy
```

```
Out[164]:= \int_0^x G[y] dy
```

```
In[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow \text{Exp} \left[\int_0^x G[y] dy \right]$$

```
Out[162]:= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
In[164]:= \int_0^x G[y] dy
```

```
Out[164]:= \int_0^x G[y] dy
```

```
In[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow \text{Exp}\left[\int_0^x G[y] dy\right]$$

```
Out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
In[164]:= \int_0^x G[y] dy
```

```
Out[164]= \int_0^x G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

$$Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow \left(\text{Exp} \left[\int_0^x G[y] dy \right] \& \right)$$

```
out[162]= 2 m Q[x] - 2 x Q'[x] + Q''[x]
```

```
in[164]:= \int_0^x G[y] dy
```

```
out[164]= \int_0^x G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

```
in[165]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (Exp[Integrate[G[y], {y, 0, x}] &) // FullSimplify
```

```
out[165]= e∫0x G[y] dy (2 m - 2 x G[x] + G[x]2 + G'[x])
```

```
in[164]:= Integrate[G[y], {y, 0, x}]
```

```
out[164]= ∫0x G[y] dy
```

```
in[118]:= eqs /. rr // Chop; (* check of equations *)
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

```
in[165]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (Exp[Integrate[G[y], y] &]) // FullSimplify
```

```
out[165]:= e∫0x G[y] dy (2 m - 2 x G[x] + G[x]2 + G'[x])
```

■ Solving the equations

```

In[115]:= vars = {x[#], # - M/2} & /@ Range[M];

eqs = x[#] - Sum[If[# == k, 0, 1/(x[#] - x[k])], {k, 1, M}] & /@ Range[M];
    
```

```

In[117]:= fr = FindRoot[eqs, vars];
    
```

```

In[118]:= eqs /. fr // Chop; (* check of equations *)
    
```

- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

```

In[165]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (Exp[Integrate[G[y], {y, 0, x}] &) // FullSimplify
    
```

$$e^{\int_0^x G[y] dy} (2m - 2xG[x] + G[x]^2 + G'[x])$$

In[114]:= M = 100;

- Solving the equations
- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

In[165]:= $Q''[x] - 2xQ'[x] + 2mQ[x] /. Q \rightarrow \left(\text{Exp}\left[\int_0^x G[y] dy\right] \& \right) // \text{FullSimplify}$

Out[165]= $e^{\int_0^x G[y] dy} (2m - 2xG[x] + G[x]^2 + G'[x])$

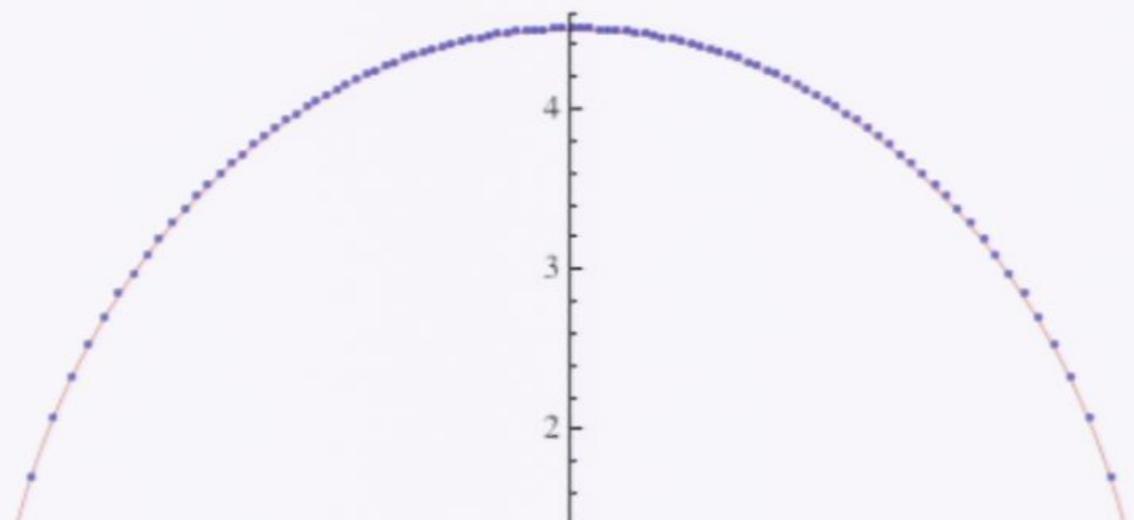
In[114]:= M = 100;

- Solving the equations
- Check of density

In[120]:= lp = { $\frac{x[\# + 1] + x[\#]}{2}$, $\frac{1}{x[\# + 1] - x[\#]}$ } & /@ Range[M - 1] /. fr // ListPlot;

p1 = Plot[$\frac{\sqrt{2M - x^2}}{\pi}$, {x, - $\sqrt{2M}$, $\sqrt{2M}$ }, PlotStyle -> Red];

In[122]:= Show[p1, lp]



In[114]:= M = 100;

- Solving the equations
- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

In[165]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \left(\text{Exp}\left[\int_0^x G[y] dy\right] \& \right) // \text{FullSimplify}$

Out[165]= $e^{\int_0^x G[y] dy} (2m - 2x G[x] + G[x]^2 + G'[x])$

in[114]:= M = 100;

- Solving the equations
- Check of density
- Hermite Polynomials

in[136]:= SolHer = x /. NSolve[HermiteH[M, x] == 0, x, WorkingPrecision -> 100] // Sort;
SolEl = x /@ Range[M] /. fr // Sort;

in[138]:= SolEl - SolHer // Chop

out[138]:= {0,
0,
0,
0, 0}

- Check differential equations
- From the equation for Q(x) to the equation for G(x)

In[114]:= M = 100;

- Solving the equations
- Check of density
- Hermite Polynomials
- Check differential equations
- From the equation for Q(x) to the equation for G(x)

In[165]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow \left(\text{Exp}\left[\int_0^x G[y] dy\right] \& \right) // \text{FullSimplify}$

Out[165]= $e^{\int_0^x G[y] dy} (2m - 2x G[x] + G[x]^2 + G'[x])$

- Check of density
- Hermite Polynomials
- Check differential equations

In[144]:= `DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]`

Out[144]:= $\left\{ \left\{ Q \rightarrow \text{Function} \left[\{x\}, \right. \right. \right.$
 $\left. \left. \left. C[1] \text{HermiteH}[m, x] + C[2] \text{Hypergeometric1F1} \left[-\frac{m}{2}, \frac{1}{2}, x^2 \right] \right] \right\} \right\}$

In[146]:= `x2 + x3 /. xy -> f[y]`

Out[146]:= `f[2] + f[3]`

In[145]:= `Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]`

Out[145]:= `2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]`

In[147]:= `Q'[x] // FullForm`

```
C[1] HermiteH[m, x] + C[2] Hypergeometric1F1[-m/2, 1/2, x^2]]]]}}
```

```
In[146]:= x^2 + x^3 /. x^y_ -> f[y]
```

```
Out[146]= f[2] + f[3]
```

```
In[145]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]
```

```
Out[145]= 2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]
```

```
In[147]:= Q'[x] // FullForm
```

```
Out[147]/FullForm=
```

```
Derivative[1][Q][x]
```

```
In[152]:= Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q -> (HermiteH[m, #] &) // FullSimplify
```

```
Out[152]= 0  
Pirsa: 10090091
```

Check differential equations

In[144]:= `DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]`

Out[144]:= $\left\{ \left\{ Q \rightarrow \text{Function} \left[\{x\}, \right. \right. \right.$
 $\left. \left. \left. C[1] \text{HermiteH}[m, x] + C[2] \text{Hypergeometric1F1} \left[-\frac{m}{2}, \frac{1}{2}, x^2 \right] \right] \right\} \right\}$

In[146]:= `x2 + x3 /. xy -> f[y]`

Out[146]:= `f[2] + f[3]`

In[145]:= `Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]`

Out[145]:= `2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]`

In[147]:= `Q'[x] // FullForm`

Out[147]//FullForm=

`Derivative[1][Q][x]`

Check differential equations

In[144]:= `DSolve[Q''[x] - 2 x Q'[x] + 2 m Q[x] == 0, Q, x]`

Out[144]:= $\left\{ \left\{ Q \rightarrow \text{Function}\left[\{x\}, C[1] \text{HermiteH}[m, x] + C[2] \text{Hypergeometric1F1}\left[-\frac{m}{2}, \frac{1}{2}, x^2\right]\right]\right\} \right\}$

In[146]:= `x2 + x3 /. xy -> f[y]`

Out[146]:= `f[2] + f[3]`

In[145]:= `Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q[x_] -> HermiteH[m, x]`

Out[145]:= `2 m HermiteH[m, x] - 2 x Q'[x] + Q''[x]`

In[147]:= `Q'[x] // FullForm`

Out[147]//FullForm=

`Derivative[1][Q][x]`

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]//FullForm=

$\text{Derivative}[1][Q][x]$

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&)$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

- Cut
- Copy
- Paste
- Copy As
- Merge Cells
- Ungroup Cells
- Open/Close Group
- Open All Subgroups
- Close All Subgroups
- Evaluate Cells

In[145]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q[x_] \rightarrow \text{HermiteH}[m, x]$

Out[145]= $2m \text{HermiteH}[m, x] - 2x Q'[x] + Q''[x]$

In[147]:= $Q'[x] // \text{FullForm}$

Out[147]/FullForm=

Derivative[1][Q][x]

In[152]:= $Q''[x] - 2x Q'[x] + 2m Q[x] /. Q \rightarrow (\text{HermiteH}[m, \#] \&) // \text{FullSimplify}$

Out[152]= 0

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

Out[153]= $-A B^2 \sin[B x] + A \omega^2 \sin[B x]$

▫ About Simplify and FullSimplify

■ From the equation for Q(x) to the equation for G(x)

In[165]:= $Q''[x] - 2 x Q'[x] + 2 m Q[x] /. Q \rightarrow \left(\text{Exp}\left[\int_0^x G[y] dy\right] \& \right) // \text{FullSimplify}$

Out[165]= $e^{\int_0^x G[y] dy} (2 m - 2 x G[x] + G[x]^2 + G'[x])$

}

In[153]:= $f''[x] + \omega^2 f[x] /. f \rightarrow (A \text{Sin}[B \#] \&)$

Out[153]= $-A B^2 \text{Sin}[B x] + A \omega^2 \text{Sin}[B x]$

▫ About Simplify and FullSimplify

■ From the equation for Q(x) to the equation for G(x)

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