Title: Some Ideas (not to try!) on Quantum Gravity Phenomenology

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Abstract:

SOME IDEAS

ON

QUANTUM GRAVITY PHENOMENOLOGY

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Adviser: Leonardo Modesto

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OUTLINE

- ## Quasi-Normal Modes
  - ### Classical Case
    - WKB method, Continuous fraction
    - Detection, Parameter estimation
  - ### Self-Dual Blackholes
    - The metric and the quantum correction
    - Connection with surface gravity
    - The present plots & possible phenomenology
- ## Dark Matter
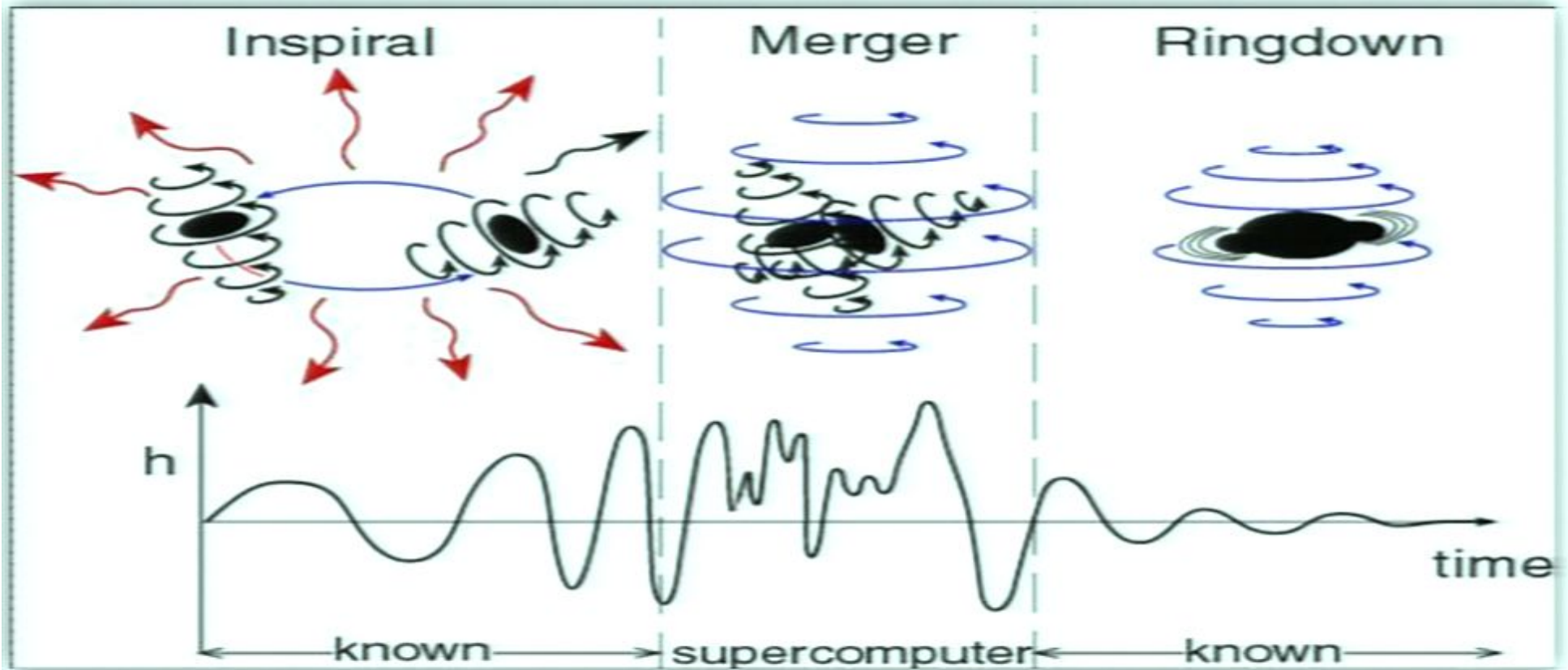 - Cosmic Rays, QNMs and structure formation
- ## Effective Lorentz Invariance Violation
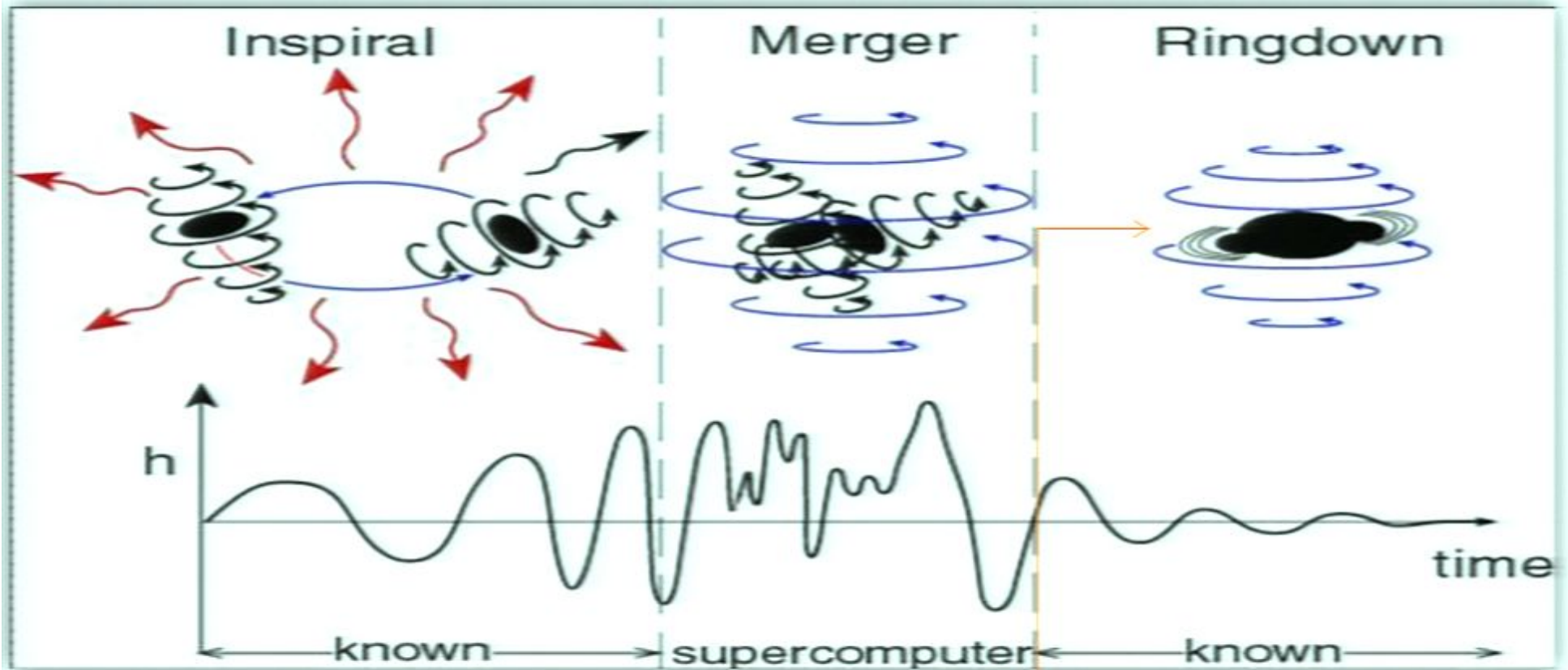 - ### GRBs
    - Neutrinos
    - Gravitons?
- ## Initial Orbital Configuration of LISA

THE LIFE OF A BLACK HOLE

THE LIFE OF A BLACK HOLE

| Inspiral | Merger | Ringdown |

h

time

known — supercomputer — known

Quasi-Normal Modes

- Exponential decay
- Perturbation of metric outside event horizon
- Directly connected to parameters of BH (mass, spin)

QNM FOR SCHWARZSCHILD BH

QNM for Schwarzschild BH

$$ds^2 = g^0_{\mu\nu}dx^\mu dx^\nu = -e^{v(r)}dt^2 + e^{\lambda(r)}dr^2 + r^2\left(d\theta^2 + \sin^2\theta d\phi^2\right)$$

Perturb the metric: $g_{\mu\nu} = g^0_{\mu\nu} + h_{\mu\nu}$

Leading to variation in Einstein equations: $\delta G_{\mu\nu} = 4\pi\delta T_{\mu\nu}$

QNM for Schwarzschild BH

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Assuming scalar decomposition of $\boldsymbol{h}$: $\chi(t, r, \theta, \phi) = \sum_{\ell m} \frac{\chi_{\ell m}(r, t)}{r} Y_{\ell m}(\theta, \phi)$

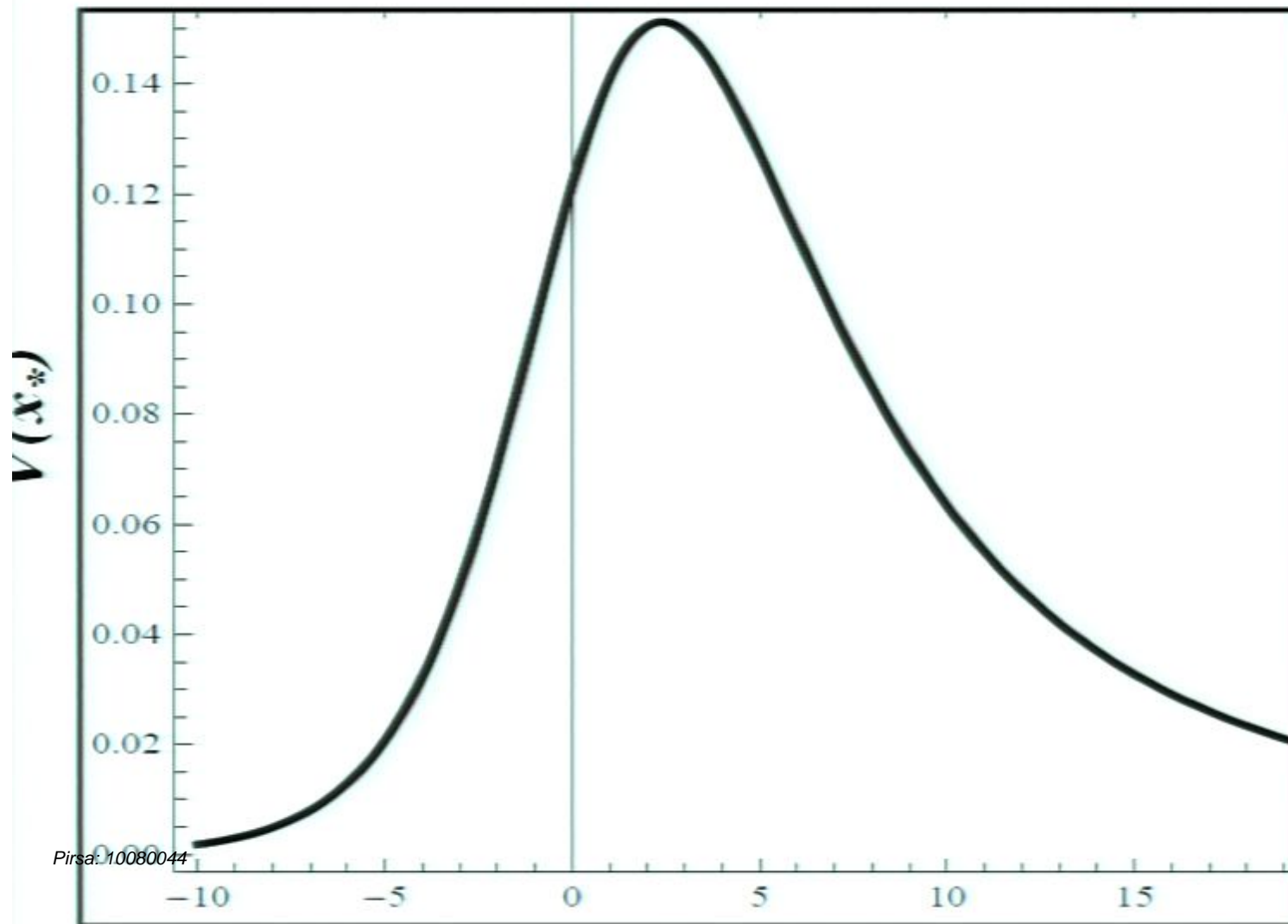For radial component of perturbation outside event horizon,

$$\frac{\partial^2 \chi_l}{\partial r_*^2} + \left(\omega^2 - V_l(r)\right) \chi_l = 0$$

where $\dfrac{\partial^2 \chi_l}{\partial t^2} = -\omega^2 \chi_l$, Tortoise radius: $r_* = r + 2M \log(r/2M - 1)$

& Regge-Wheeler Potential: $V_\ell(r) = \left(1 - \dfrac{2M}{r}\right)\left[\dfrac{\ell(\ell+1)}{r^2} + \dfrac{2\sigma M}{r^3}\right]$
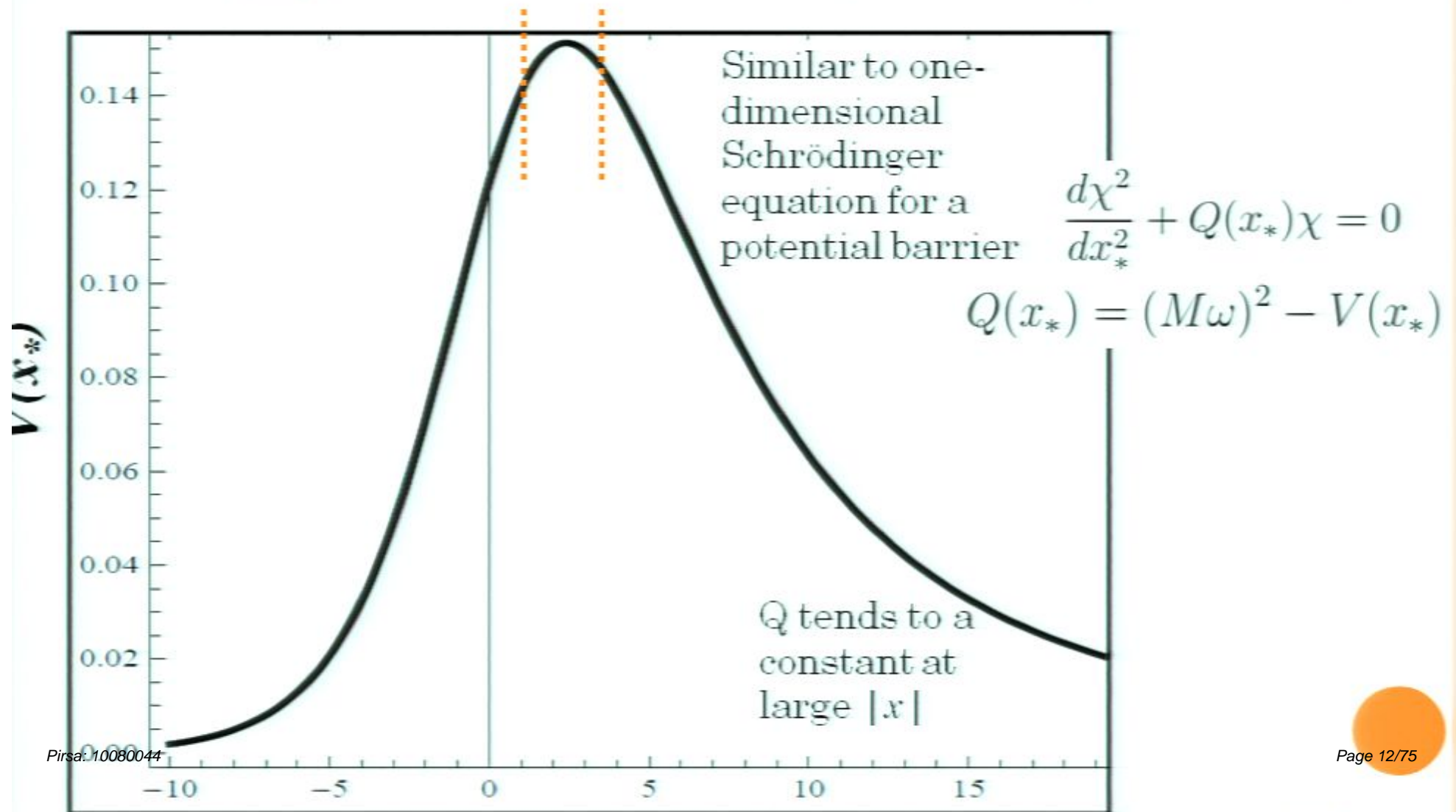
A CLOSER LOOK AT THE POTENTIAL

$M = 1\,\mathrm{M}_{\mathrm{Solar}},\ l = 2\ \&\ \sigma = 1 - s^2 = 1$ (for Scalar perturbation)

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$M = 1\,M_{Solar}$, $l = 2$ & $\sigma = 1 - s^2 = 1$ (for Scalar perturbation)

Similar to one-
dimensional
Schrödinger
equation for a
potential barrier

$$\frac{d\chi^2}{dx_*^2} + Q(x_*)\chi = 0$$

$$Q(x_*) = (M\omega)^2 - V(x_*)$$

Q tends to a
constant at
large $|x|$

WKB APPROXIMATION METHOD

Parabola to first order

χ_2

$\chi_1 \to e^{i\alpha x}$

$\chi_3 \to e^{-i\alpha x}$

Match WKB solutions at the turning points
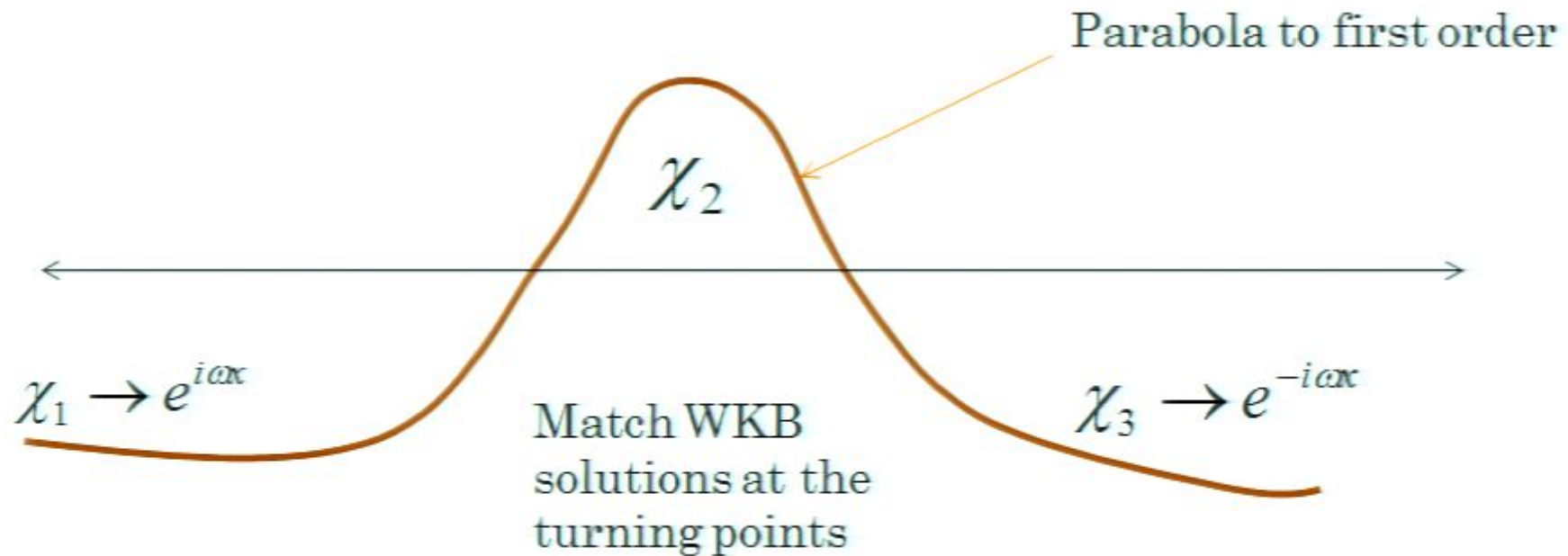
Condition for normal modes: $\dfrac{Q_0}{\sqrt{2Q_0''}} = i\left(n + \dfrac{1}{2}\right)$

$$(M\omega_n)^2 = V_\ell(r_0) - i\left(n + \frac{1}{2}\right)\left[-2\frac{d^2 V_\ell(r_0)}{dr_*^2}\right]^{1/2}$$

Schutz & Will (1985)

RHS Independent of M
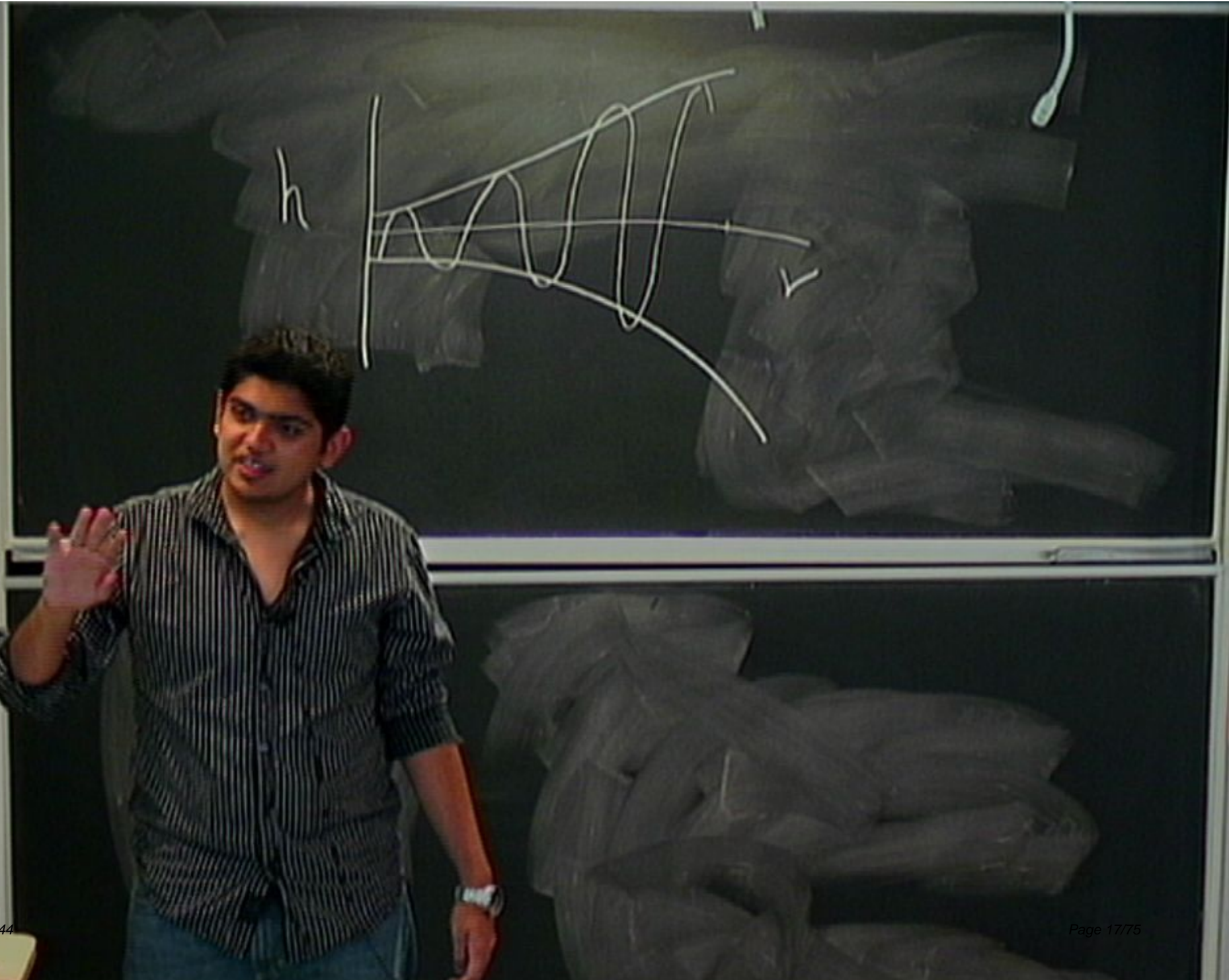
METHOD OF CONTINUED FRACTIONS

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Radial Equation: $r(r-1)\dfrac{d^2\chi_l}{dr^2} + \dfrac{d\chi_l}{dr} - \left(l(l+1) - \dfrac{\rho^2 r^3}{r-1} - \dfrac{\sigma}{r}\right)\chi_l = 0$

where $2M = 1$ & $\rho = i\omega$

Assume the following solution from boundary condition:

$$\chi_l(r) = (r-1)^\rho r^{-2\rho} e^{-\rho(r-1)} \sum_{n=0}^{\infty} a_n \left(\dfrac{r-1}{r}\right)^n$$
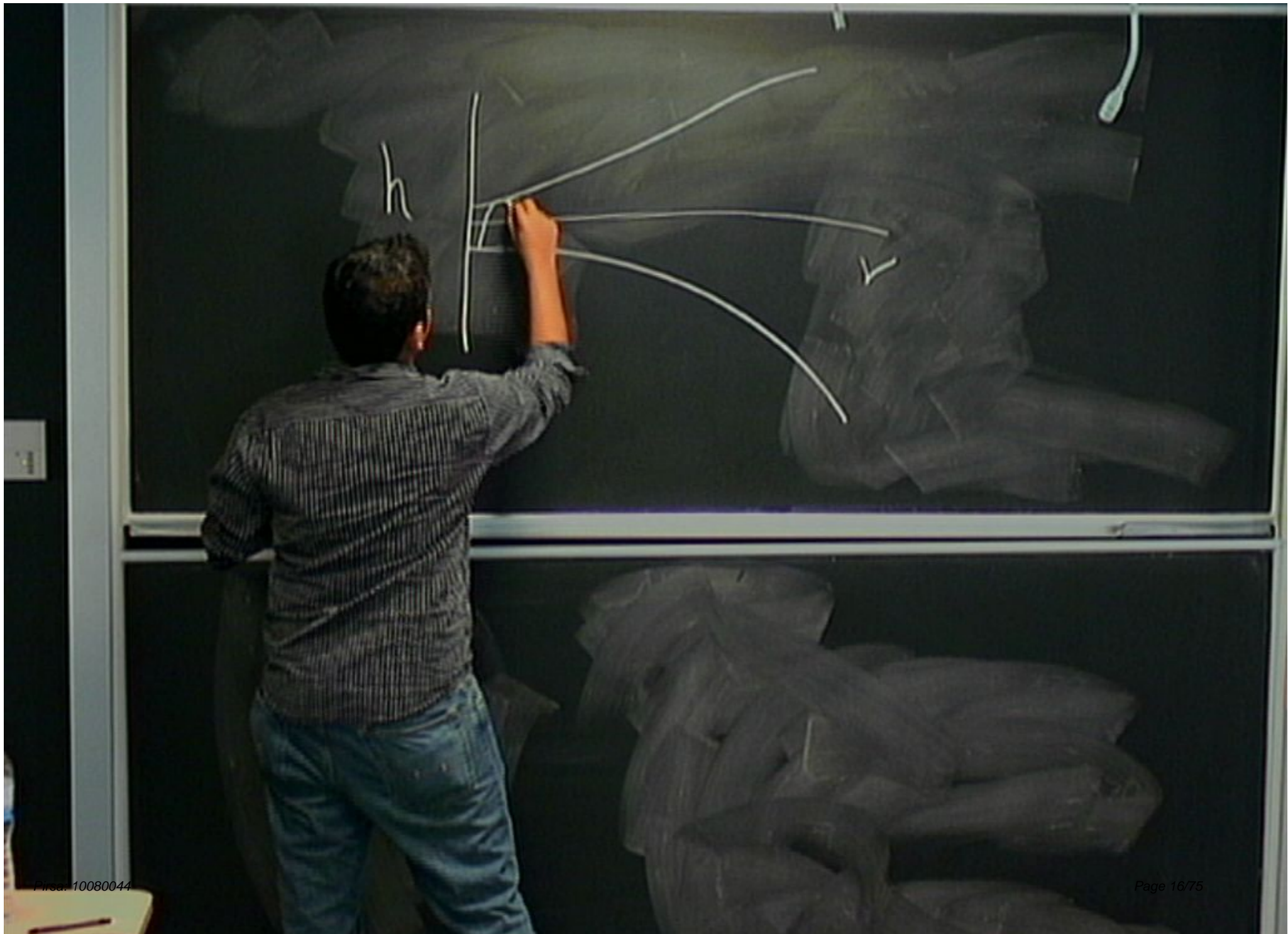
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$$\chi_l(r) = (r-1)^\rho r^{-2\rho} e^{-\rho(r-1)} \sum_{n=0}^{\infty} a_n \left(\dfrac{r-1}{r}\right)^n$$

Then we get the following relations:

$\alpha_0 a_1 + \beta_0 a_0 = 0, \quad \alpha_n a_{n+1} + \beta_n a_n + \gamma_n a_{n-1} = 0,$

where : $\alpha_n = n^2 + (2\rho+2)n + 2\rho + 1, \quad \gamma_n = n^2 + 4\rho n + 4\rho^2 - \sigma - 1$

$\beta_n = -(2n^2 + (8\rho+2)n + 8\rho^2 + 4\rho + l(l+1) - \sigma)$

DETECTION OF QNMS

- In physical units: $\omega = (\omega M) 2\pi\ (5142\ Hz) \dfrac{M_{solar}}{M}$

  - For LIGO ($\sim 10 - 10000$ Hz) : stellar BHs

  - For LISA ($\sim 0.1 - 0.00001$ Hz) : Super- Massive BHs

- Only first couple of modes 'n' observable (exponential damping)

- If QNM spectrums inconsistent with isolated BH then:

  - We are not observing isolated BH approaching equilibrium

  - It might be neutron star or some exotic Boson star (?) Thus, it could be used as a test for "no-hair" theorem

  - GR is not true in strong field regime

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DETERMINING PARAMETERS

Parameters (Kerr BH): n, *l* , *m* , *Mass (M)* , *Spin (a)*
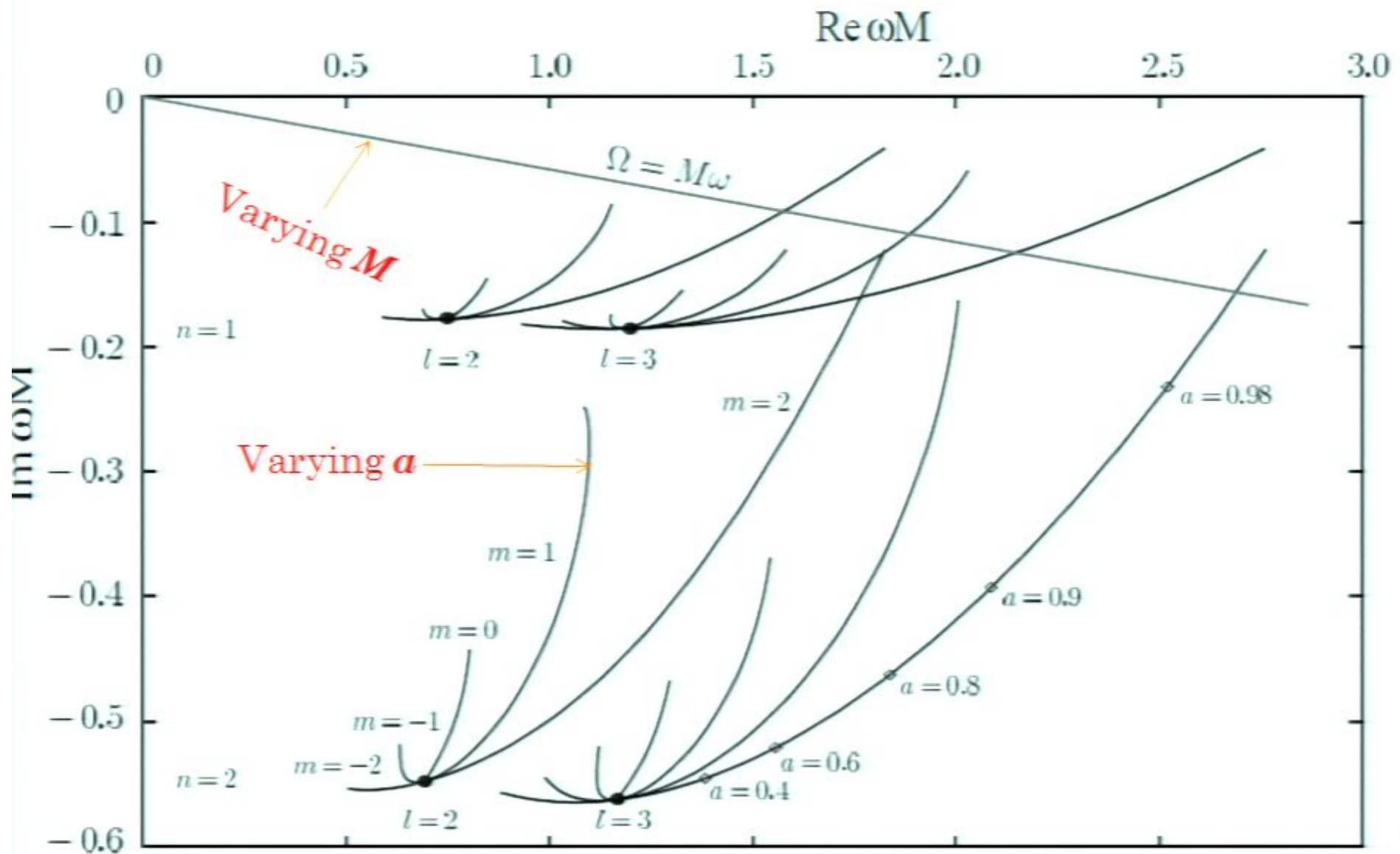
SELF-DUAL BHs

- Semi classical metric obtained from a classical analysis of the Loop Quantum BH

$$ds^2 = -G(r)dt^2 + \frac{dr^2}{F(r)} + H(r)d\Omega^{(2)}$$

$$d\Omega^{(2)} = d\theta^2 + \sin^2\theta d\phi^2$$

$$G(r) = \frac{(r - r_+)(r - r_-)(r + r_*)^2}{r^4 + a_o^2}$$

$$F(r) = \frac{(r - r_+)(r - r_-)r^4}{(r + r_*)^2(r^4 + a_o^2)},$$

$$H(r) = r^2 + \frac{a_o^2}{r^2}.$$

$$r_+ = 2m, \ r_- = 2mP^2$$

$$r_* = \sqrt{r_+ r_-} = 2mP.$$

$$P = (\sqrt{1 + \epsilon^2} - 1)/(\sqrt{1 + \epsilon^2} + 1)$$

$a_0 \propto A_{\min}$ (*Minimum Area in LQG*)

$\varepsilon \propto \gamma$ (*Immirzi Parameter*)

- Free from singularity & invariant under: $r \to a_0/r$

- Area of event horizon (X²) > Compton wavelength:

$$X = \sqrt{(2M)^2 + (\frac{a_0}{\ })^2} > \hbar/2M$$

QNM FOR SELF-DUAL BHS

Mass of scalar field

Wave-equation for a scalar field in a general spherical surface:

$$\frac{1}{\sqrt{-g}}\partial_\mu\left(g^{\mu\nu}\sqrt{-g}\partial_\nu\Phi\right) - m_\Phi^2\Phi = 0,$$

(As LQG is not developed to involve perturbation we assume this classical result)
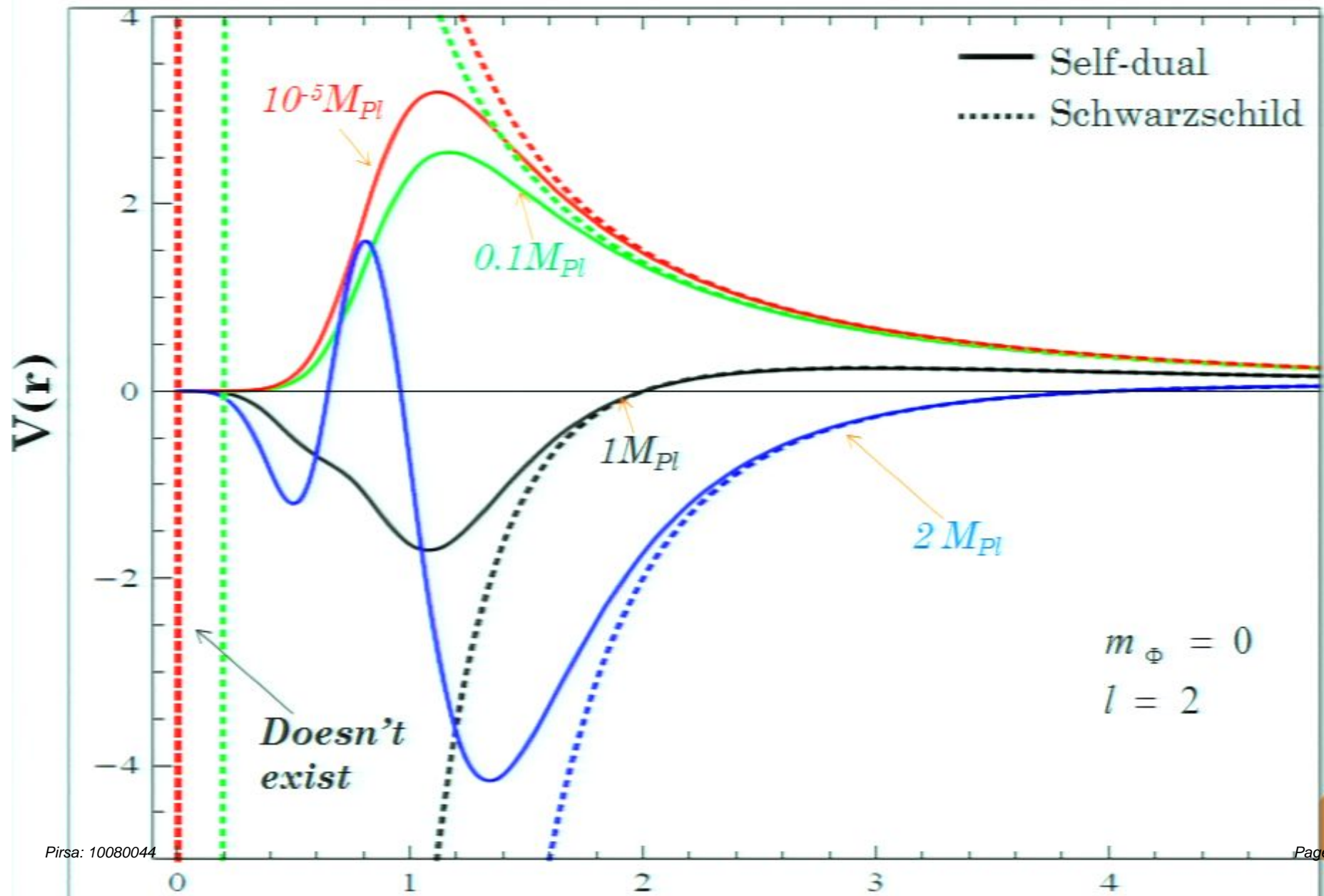
Assuming the scalar field:

$$\Phi(r,\theta,\phi,t) := T(t)\,\varphi(r)\,Y(\theta,\phi)$$

Radial Equation:

$$\left[\frac{\partial^2}{\partial r^{*2}} + \omega^2 - V(r(r^*))\right]\psi(r) = 0,$$

where, $r^* = \int \frac{1}{\sqrt{GF}}\,dr$

$$K^2 = l(l+1)$$

$$V(r) = G\left(m_\Phi^2 + \frac{K^2}{H}\right) + \frac{1}{2}\sqrt{\frac{GF}{H}}\left[\frac{\partial}{\partial r}\left(\sqrt{\frac{GF}{H}}\frac{\partial H}{\partial r}\right)\right]$$

POTENTIAL OF SELF-DUAL BH

SURFACE GRAVITY AND QNMs

SURFACE GRAVITY AND QNMS

Always
TRUE!

$$\omega_n = i\kappa\left(n + \frac{1}{2}\right) + \frac{\ln 3}{2\pi}\kappa + O[n^{-1/2}] \qquad \text{as} \qquad n \to \infty$$
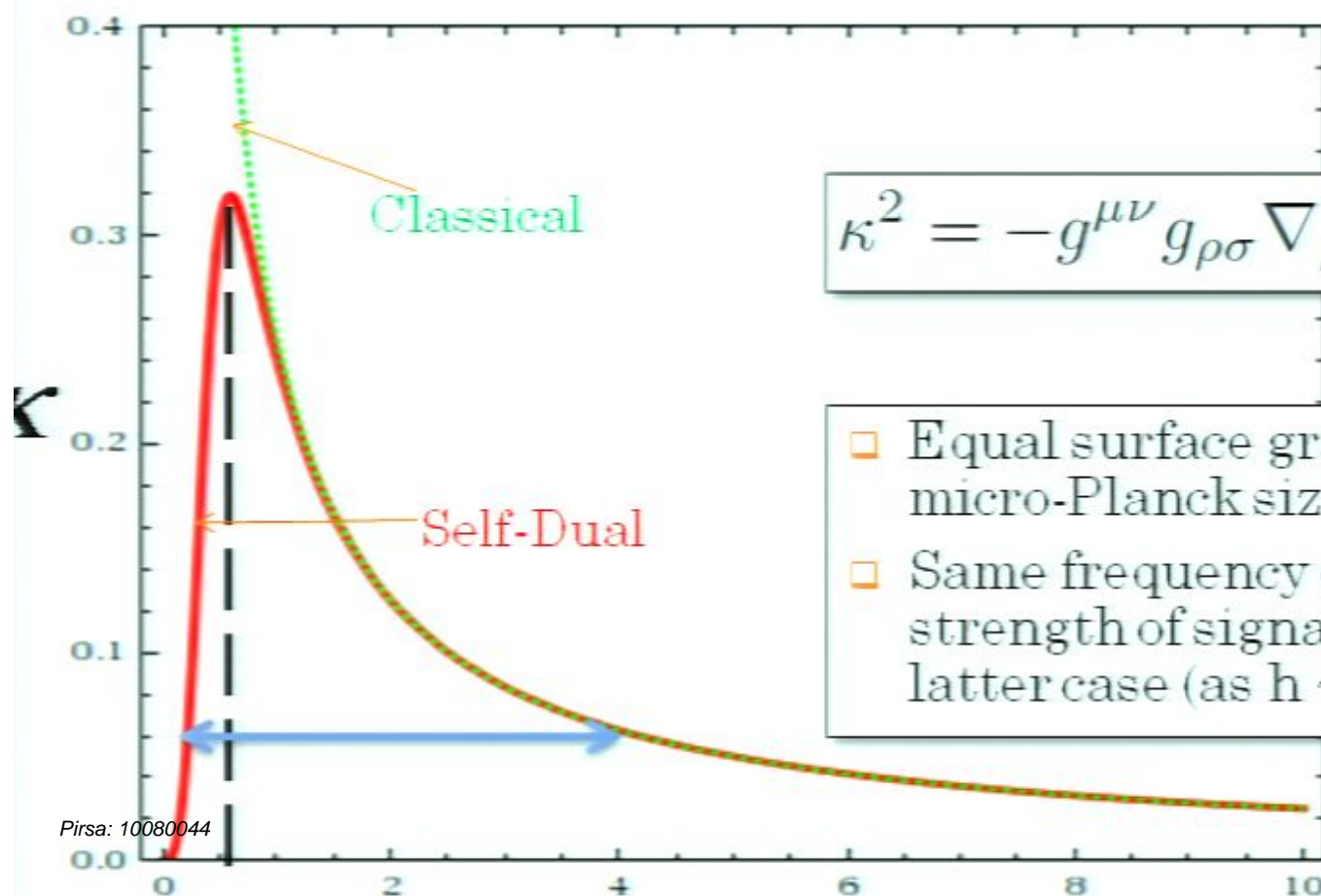
Nollert (1993)
Medved et al. (2003)

Surface Gravity and QNMs

Always TRUE!

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Medved et al. (2003)

$$\kappa^2 = -g^{\mu\nu}g_{\rho\sigma}\nabla_\mu\chi^\rho\nabla_\nu\chi^\sigma/2$$

Classical

Self-Dual

- ❑ Equal surface gravity for SMBH and micro-Planck size BH
- ❑ Same frequency of GW although strength of signal very weak in the latter case (as h ~ M/r)
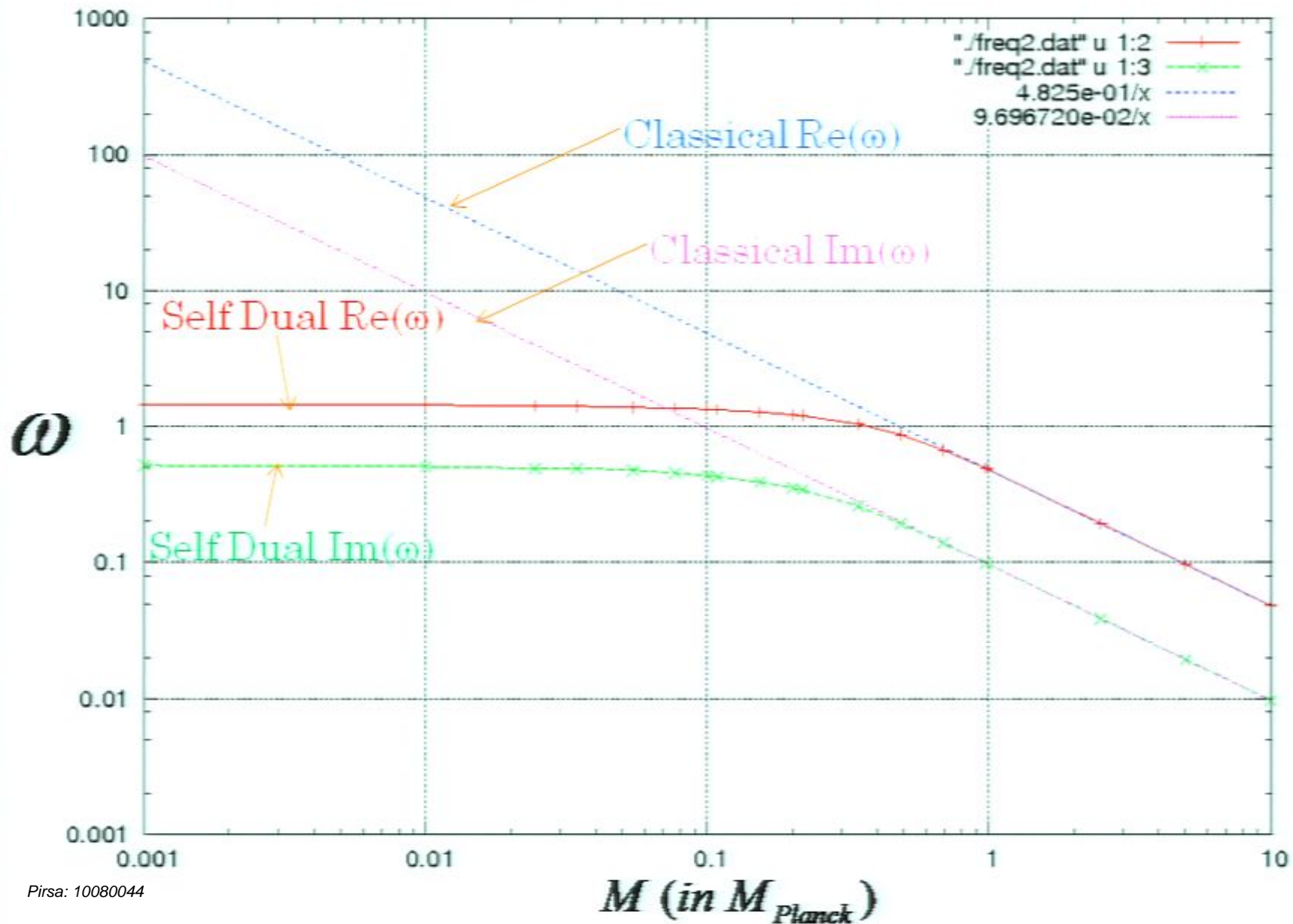
COMPUTING QNMS (FOR SMALL 'n')

- Small 'n' is what we observe
  - In principle, easier to compute!
  - In the case of self-dual BHs – slightly non-trivial!
- WKB method **might** fail at $M < M_{planck}$
  - More than one turning points in the potential (doesn't have a peak at $r = 3M$!)
  - It **might** work at $M > M_{planck}$ as only $r = 3M$ dominates
    - *As consistency check, $a_\theta = 0 = P$ should match with Schwarzschild case*
- Continuous fraction – most reliable but extremely difficult to compute the expressions !
  - Should work for all M
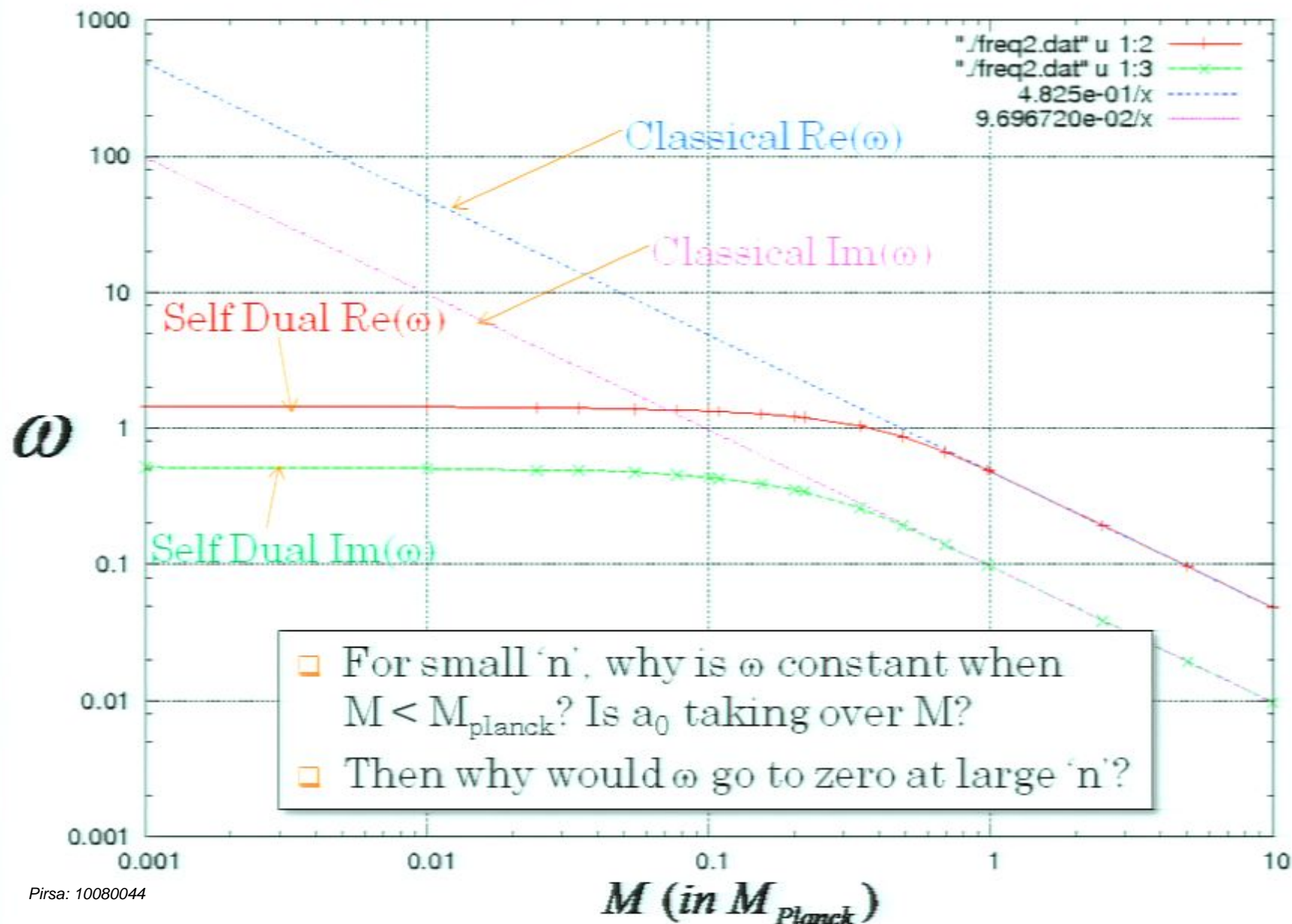- Evolving the time dependent wave equation

COMPUTING QNMs (FOR SMALL 'n')

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o **Evolving the time dependent wave equation**
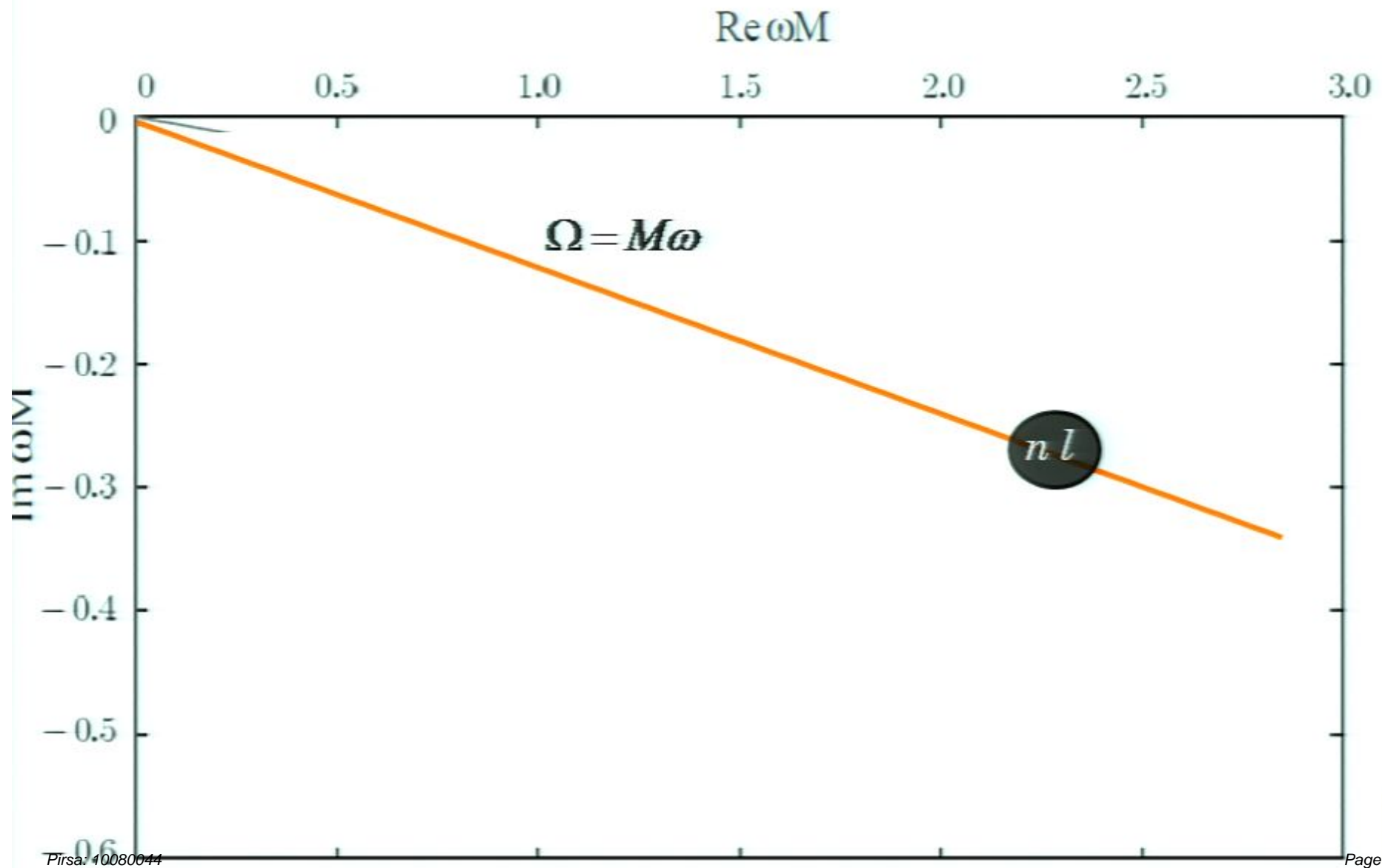
  - Works only for n=1
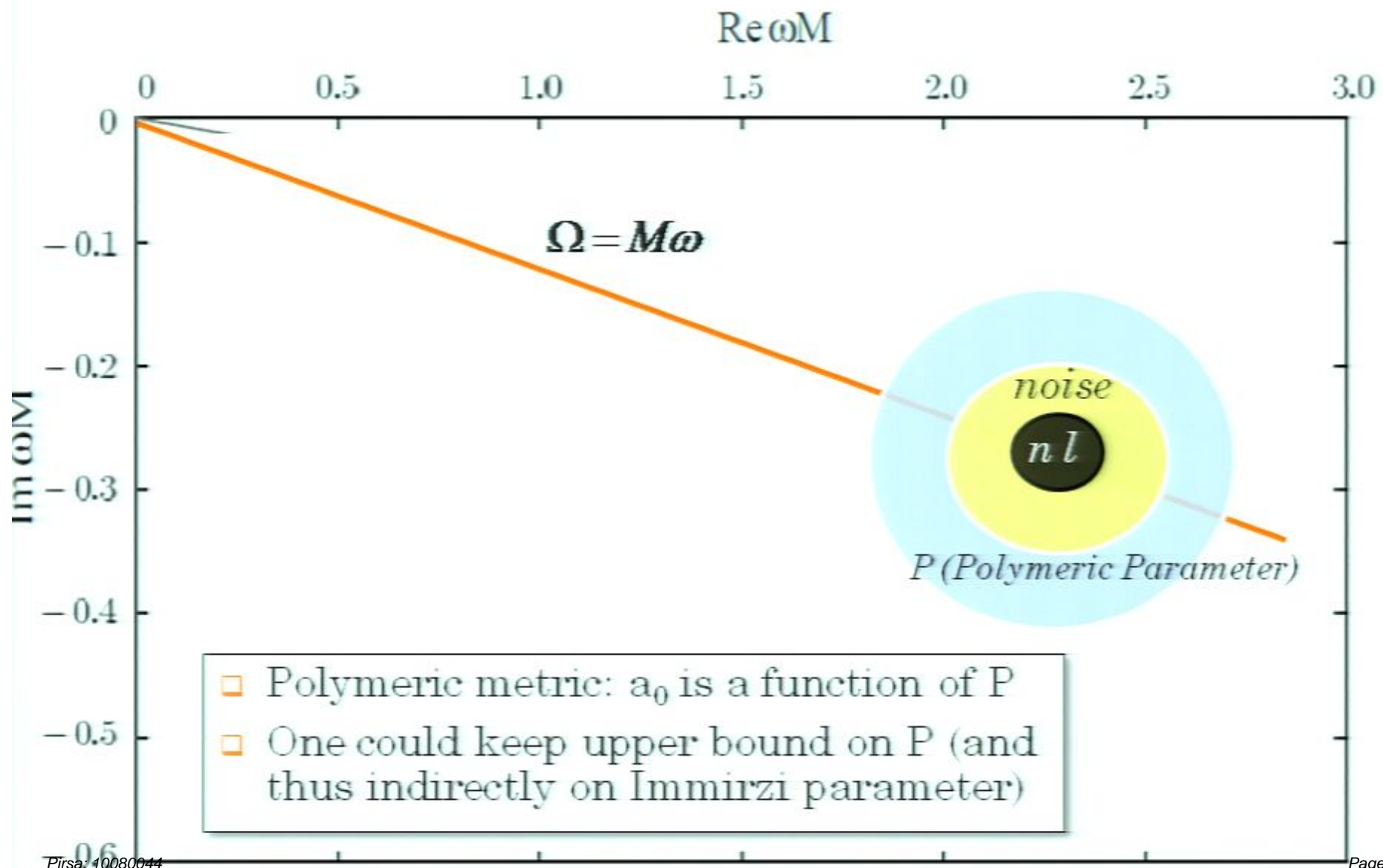
PLOTS OF QNM (FOR n = 1)

PLOTS OF QNM (FOR n = 1)

Plot legend:
- "./freq2.dat" u 1:2
- "./freq2.dat" u 1:3
- 4.825e-01/x
- 9.696720e-02/x

Plot labels: Classical Re(ω), Classical Im(ω), Self Dual Re(ω), Self Dual Im(ω)

Y-axis: ω (1000, 100, 10, 1, 0.1, 0.01, 0.001)

X-axis: M (in M_{Planck}) (0.001, 0.01, 0.1, 1, 10)

- For small 'n', why is ω constant when $M < M_{planck}$? Is a_0 taking over M?
- Then why would ω go to zero at large 'n'?

ReωM

Im ωM

$\Omega = M\omega$

noise

n l

P (Polymeric Parameter)

- Polymeric metric: a_0 is a function of P
- One could keep upper bound on P (and thus indirectly on Immirzi parameter)

Quantum BH as Dark Matter

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QUANTUM BH AS DARK MATTER

○ **Micro self-dual BHs : "neo − MACHOs"**

- Primordial − formed due to statistical thermal fluctuations at the end (during?) of inflation
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- Assuming they were created at the Teq ~ 10^{14} GeV
- Assuming they constitute ALL the observed DM

$$\int_0^\infty \frac{(a(t_i))^3 m_0(m_i)\rho_{max}(m_i)}{(a(t_0))^3} dm_i = 0.22\rho_{crit}$$

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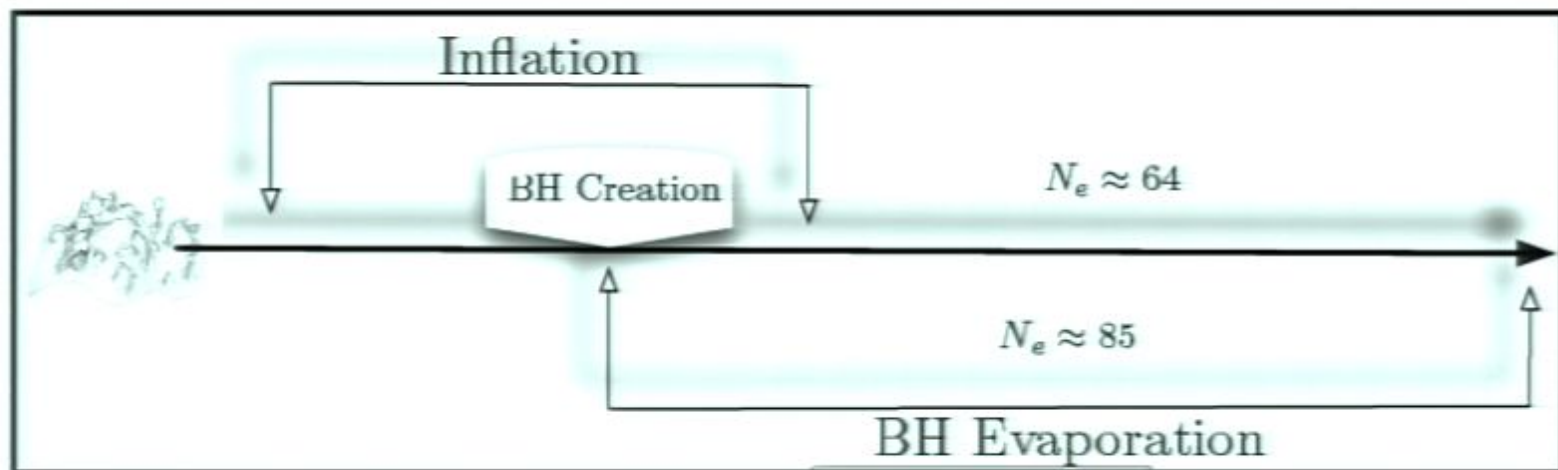- Assuming they constitute ALL the observed DM

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DM Phenomenology
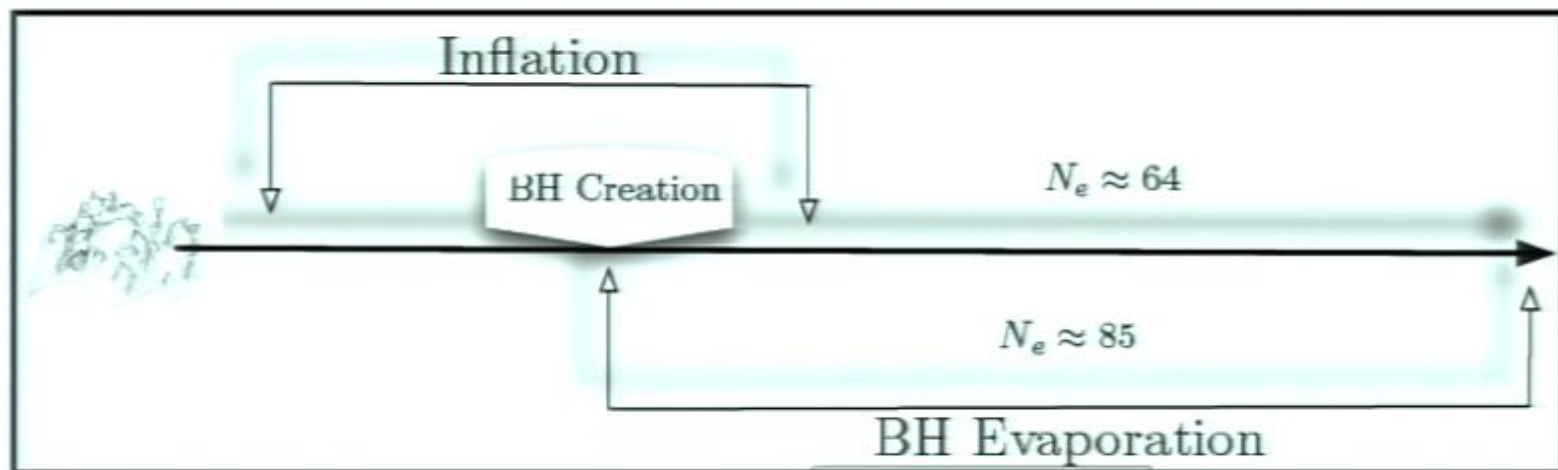
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Inflation

BH Creation

$N_e \approx 64$

$N_e \approx 85$

BH Evaporation

DM Phenomenology

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○ Ultra High Energy Cosmic Rays

- The issue of GZK cutoff

$$\sigma_{obs} \approx 10^{-37} \frac{\text{UHECR particles}}{\text{s m}^3}$$

- Invisible matter within 50 Mpc (?)

DM Phenomenology

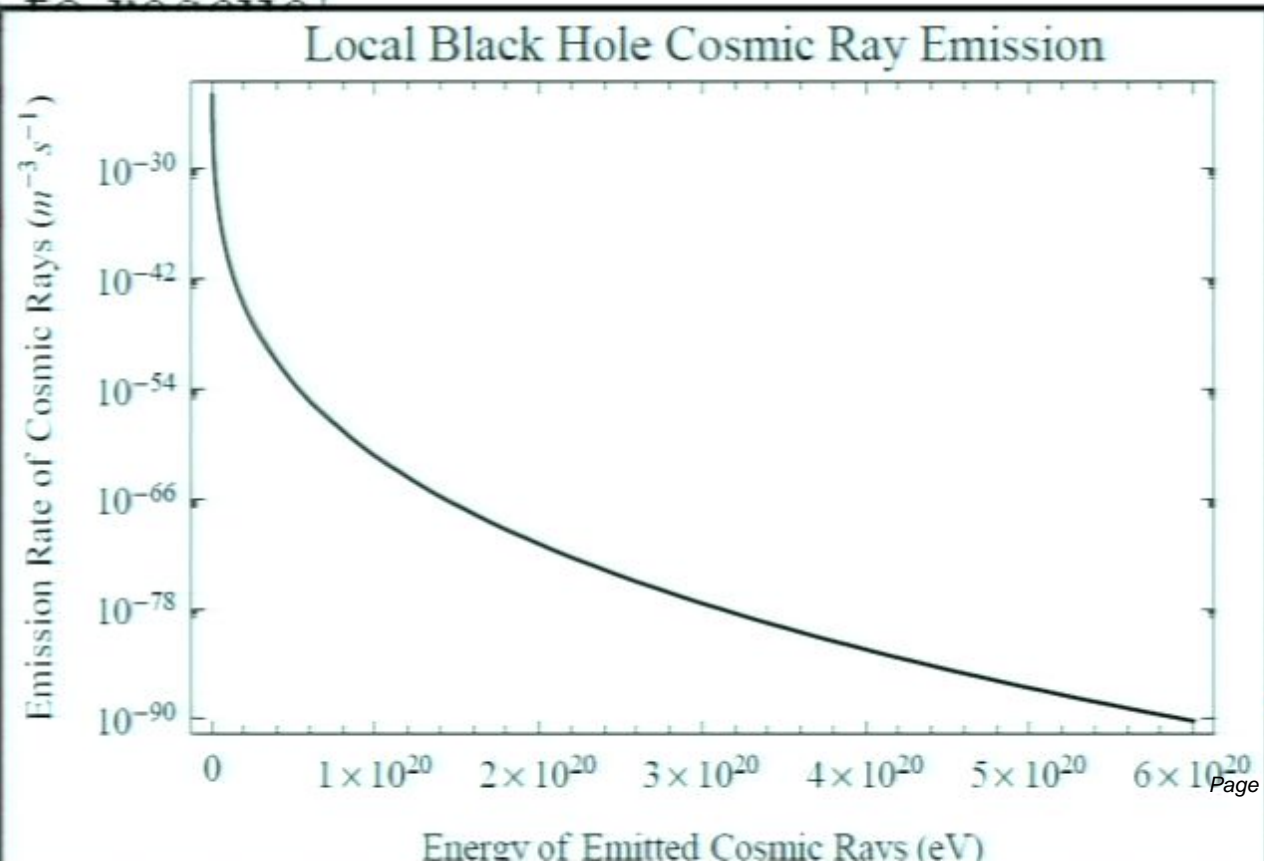o Ultra High Energy Cosmic Rays

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o Self-Dual BHs to rescue!

$$\sigma_{th} = \int_{m_0=0}^{\infty} \int_{6\times10^{19}\text{ eV}}^{m_0} \frac{2A_{min}\,\rho_{MWBH}(m_0)\,\nu^2}{\pi(e^{\frac{\nu}{T_{BH}(m_0)}} - 1)} d\nu$$

DM PHENOMENOLOGY

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Local Black Hole Cosmic Ray Emission

Pirsa: 10080044

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DM Phenomenology (Wild Idea No. 1)

○ Compute QNMs of micro quantum BHs
- Finding where the mass range where distribution peaks
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    - Asymptotic safety gravity BHs, Non-commutative BHs
  - If the frequency of GWs feasible then we know where to look (LIGO or LISA)
- Assuming all of the DM BHs haven't reached equilibrium (WHY?)
  - And also assuming their distribution is homogenous & isotropic & we assume a neat fraction of them in phase
  - Then, in principle, within solar system one could tune enough BHs to have a stochastic background noise in GW detectors

DM Phenomenology (WILD IDEA No. 2)

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- Evolution of the SMBH would depend on the propertied of DM halo

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- Different properties would predict different merger rate
- LISA could listen SMBH merger
  - Could test cosmological models

And thus could tell us something new about DM

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LORENTZ INVARIANCE VIOLATION

- Deformed Special Relativity:

$$m^2 = E^2 - p^2 + \Delta_{qg}(E, p^2; M_{QG})$$

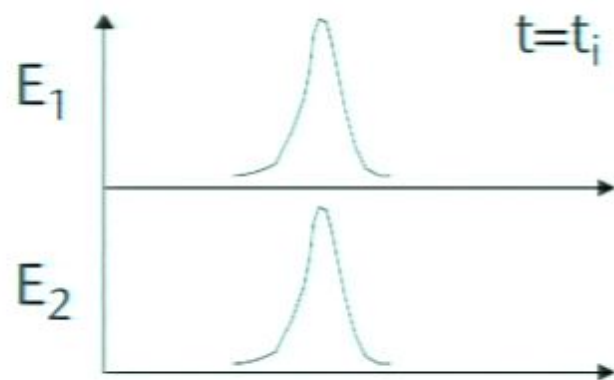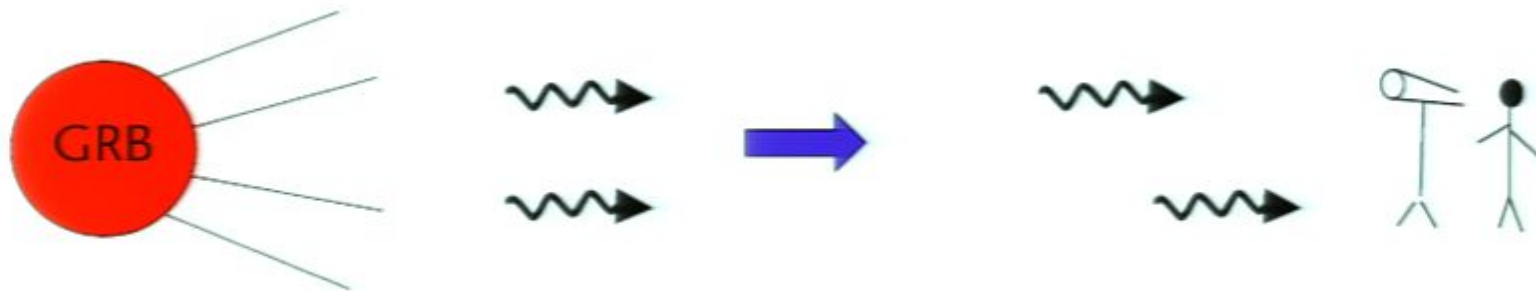- Vacuum has an energy dependent refractive index (?)

- No longer invariant:

$$c(\varepsilon) = 1 - \zeta \frac{E}{E_{QG}} = 1 - \varepsilon \qquad ds^2(\varepsilon) \neq ds^2(\varepsilon')$$
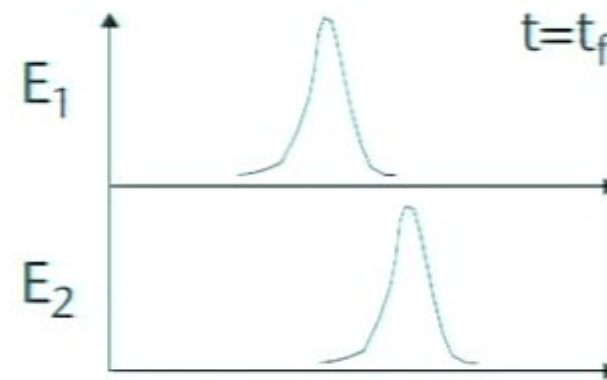
- Where is the relativity ?
  - Observers agree on E_{QG}
  - Observers agree on the wavelength of a color
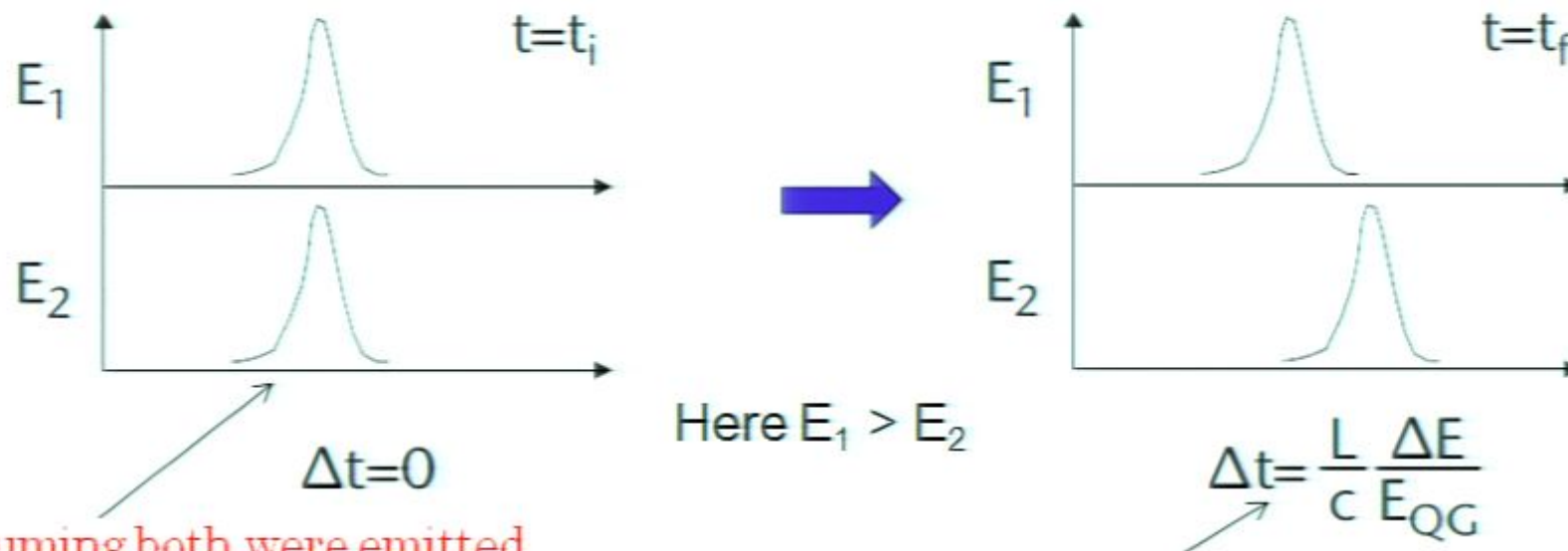
PHENOMENON OF TIME DELAY

$t=t_i$

E_1

E_2

$\Delta t = 0$

Here $E_1 > E_2$

$t=t_f$

E_1

E_2

$\Delta t = \dfrac{L}{c}\dfrac{\Delta E}{E_{QG}}$

PHENOMENON OF TIME DELAY

GRB

Assuming attenuation of gamma
photons has negligible effects

$t=t_i$

E_1

E_2

$\Delta t=0$

Here $E_1 > E_2$

$t=t_f$

E_1

E_2

$\Delta t= \dfrac{L}{c} \dfrac{\Delta E}{E_{QG}}$

Assuming both were emitted
at 'almost' same time

Assuming we know the distance
to the source pretty well

PHENOMENON OF TIME DELAY (CONT.)

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Flat FRW Metric: $ds^2 = -dt^2 + a(t)^2[d\chi^2 + \chi^2(d\theta^2 + \sin^2\theta d\phi^2)]$

PHENOMENON OF TIME DELAY (CONT.)

Flat FRW Metric: $ds^2 = -dt^2 + a(t)^2[d\chi^2 + \chi^2(d\theta^2 + \sin^2\theta d\phi^2)]$

Assume first order QG effect: $E \equiv \sqrt{m^2 + \dfrac{p_\chi^2}{a^2(t)}\left(1 - \zeta\dfrac{p_\chi}{a(t)\,E_{QG}}\right)}$

PHENOMENON OF TIME DELAY (CONT.)

Flat FRW Metric: $ds^2 = -dt^2 + a(t)^2[d\chi^2 + \chi^2(d\theta^2 + \sin^2\theta d\phi^2)]$

Assume first order QG effect: $E \equiv \sqrt{m^2 + \dfrac{p_\chi^2}{a^2(t)}\left(1 - \zeta\dfrac{p_\chi}{a(t)\,E_{QG}}\right)}$

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For $m = 0$ (QG phenomenology) | For $\zeta = 0$ (Bounding graviton mass)

$\Delta t = \dfrac{\zeta}{E_{QG}}D(f_e' - f_e)$

$\Delta t = \dfrac{m^2}{2}D\left(\dfrac{1}{f_e^2} - \dfrac{1}{f_{e'}^2}\right)$

$D \equiv \dfrac{1}{H}\int_0^z dz\dfrac{1+z}{\sqrt{\Omega_\Lambda + (1+z^3)\Omega_{Matter}}}$

$D \equiv (1+Z)^2\int_{t_e}^{t_a}\dfrac{a(t)}{a(t_a)}dt$

SOURCES FOR PHENOMENOLOGY OF LIV

○ **Gamma Ray Bursts**

- Distance ~Gpc, energy ~ GeV

  ○ *GRB 080916:* $z = 4.35$, $E_{max} = 13.2$ GeV, $E_{QG} \sim 0.1\, E_{Planck}$

  ○ *GRB 090510:* $z = 0.903$, $E_{max} = 31$ GeV, $E_{QG} \sim 10\, E_{Planck}$

○ **Active Galactic Nuclei**

- Distance ~0.1 z, total energy TeV

  ○ *PKS 2155-304:* $E_{QG} \sim 0.1\, E_{Planck}$

○ **Pulsars**

- Distance ~kpc, energy ~ 100 MeV but nano –second

  precision in pulsation

MULTI-MESSENGER PHENOMENOLOGY FOR LIV

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○ **Neutrinos**

  - GRB: $E > 10^2$ TeV

  - Detection probability for a short burst $\sim 10^{-2}$, so unlikely to have two neutrinos detected from same source

  - Comparison with low energy photon could be used (even if there is an intrinsic delay!)   U. Jacob & T. Piran (2007)
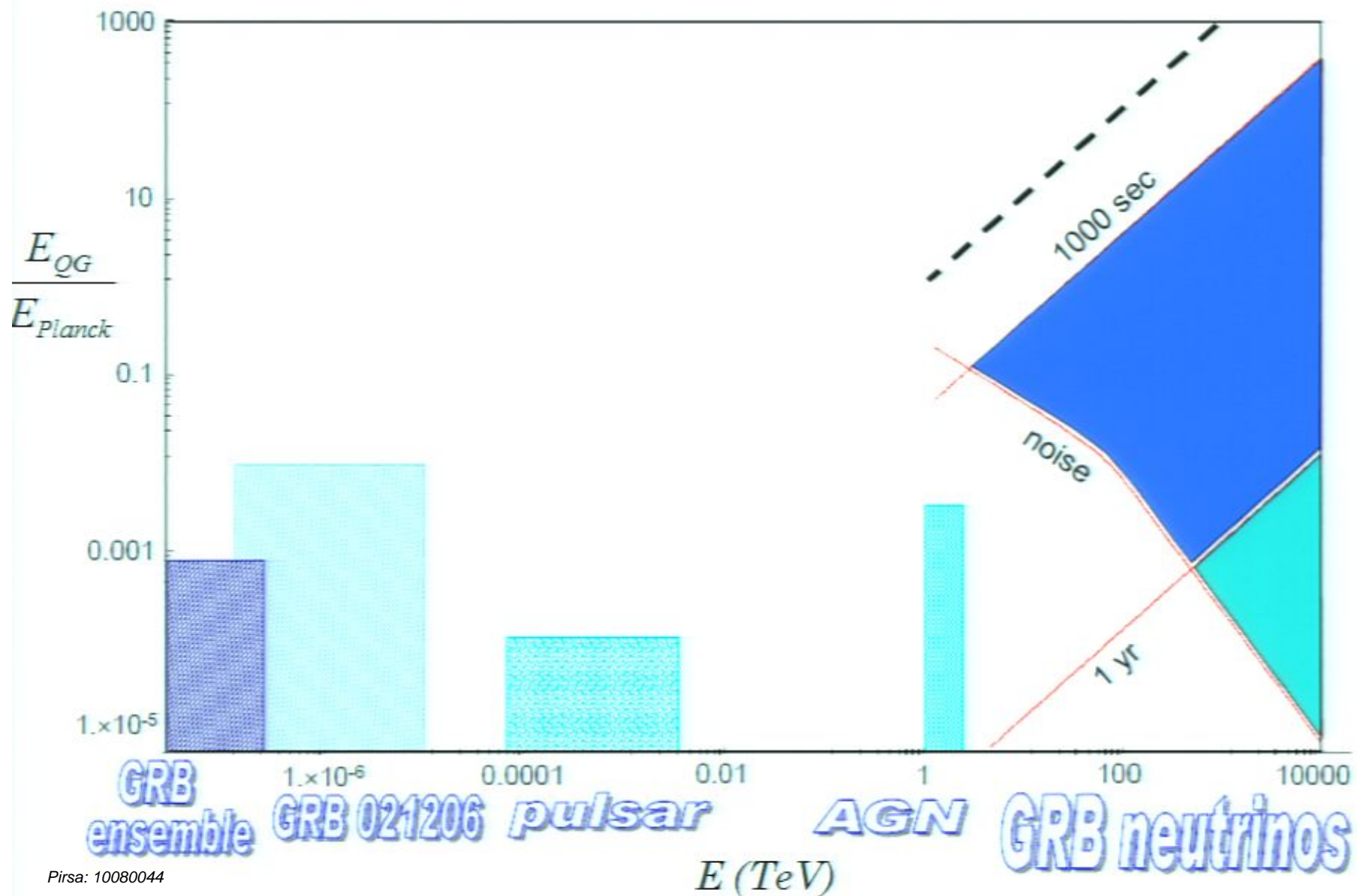
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  - Easier to model merging of SMBH + cosmological scale (entire universe) – energy to low ($\sim 10^{-3}$ Hz) = Almost unaffected by QG !
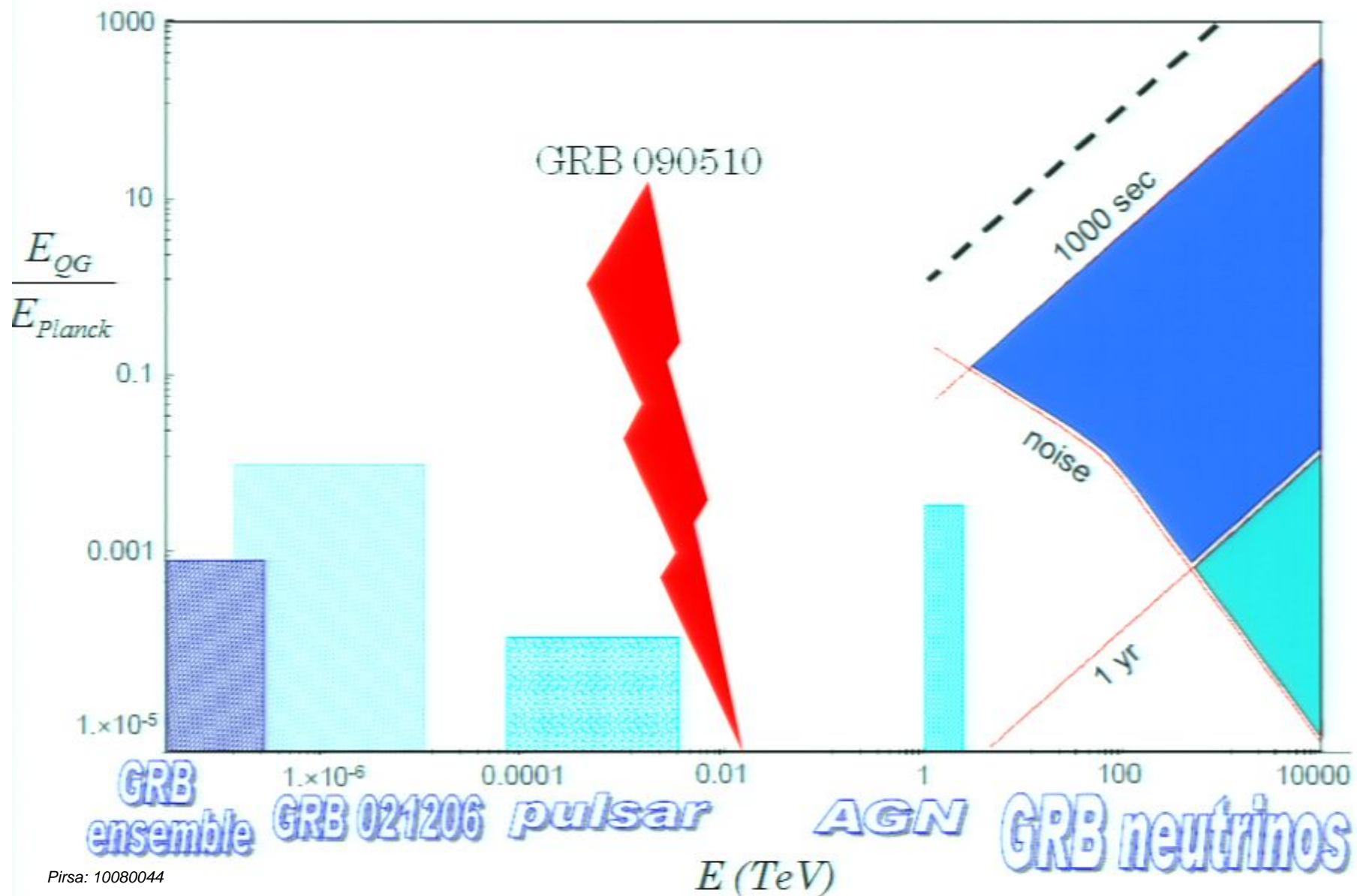 - EM signal during coalescence (accretion & transients of relativistic gas)   B. Kocsis et al. (2008)
    - Similar as keeping bound on mass of graviton, but here one favors graviton to have no delay (massless) !
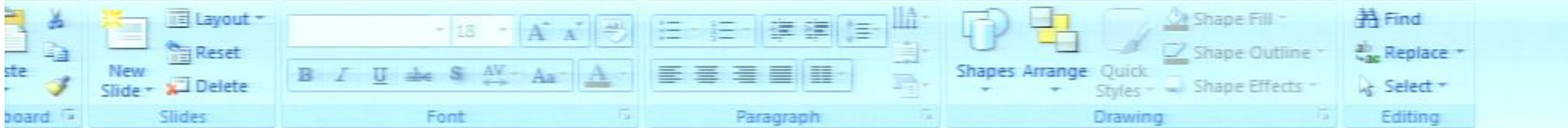
SUMMARIZING THE BOUNDS

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"*THOUGH THE SOURCE BE OBSCURE, STILL THE STREAM FLOWS ON...*"

- Taken from *NUMBER – THE LANGUAGE OF SCIENE* by *Tobias Dantzig*

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- **GRB** (?) = Photons + Neutrinos + GWs

COMPUTING QNMS (FOR SMALL 'n')

- Small 'n' is what we observe
  - In principle, easier to compute!
  - In the case of self-dual BHs – slightly non-trivial!
- WKB method might fail at $M < M_{planck}$
  - More than one turning points in the potential (doesn't have a peak at $r = 3M$!)
  - It might work at $M > M_{planck}$ as only $r = 3M$ dominates
    - As consistency check, $a_0 = 0 = P$ should match with Schwarzschild case
- Continuous fraction – most reliable but extremely difficult to compute the expressions !
  - Should work for all M
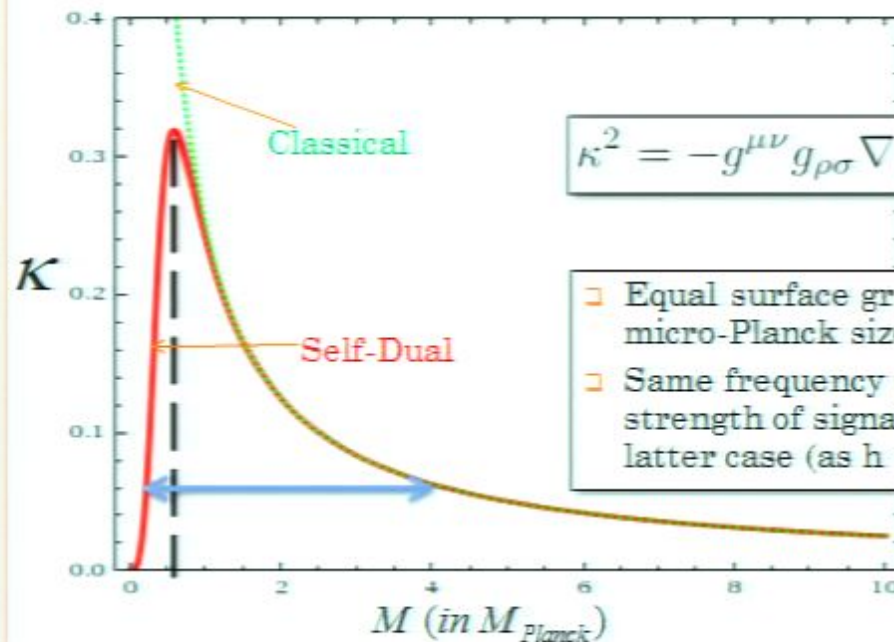- Evolving the time dependent wave equation
  - Works only for n=1

Work in progress!

SURFACE GRAVITY AND QNMs

Always TRUE!

$$\omega_n = i\kappa\left(n + \frac{1}{2}\right) + \frac{\ln 3}{2\pi}\kappa + O[n^{-1/2}] \qquad \text{as} \qquad n \to \infty$$
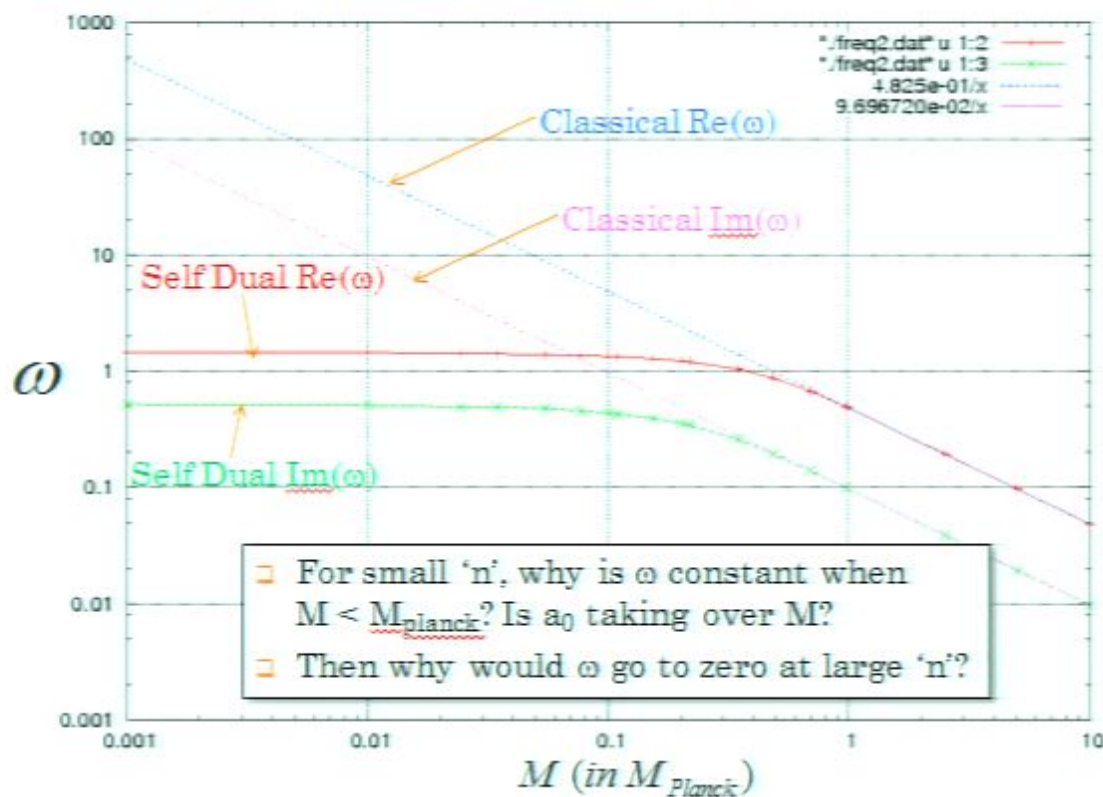
Nollert (1993)
Medved et al. (2003)

$$\kappa^2 = -g^{\mu\nu}g_{\rho\sigma}\nabla_\mu\chi^\rho\nabla_\nu\chi^\sigma/2$$

Classical

Self-Dual

- Equal surface gravity for SMBH and micro-Planck size BH
- Same frequency of GW although strength of signal very weak in the latter case (as h ~ M/r)

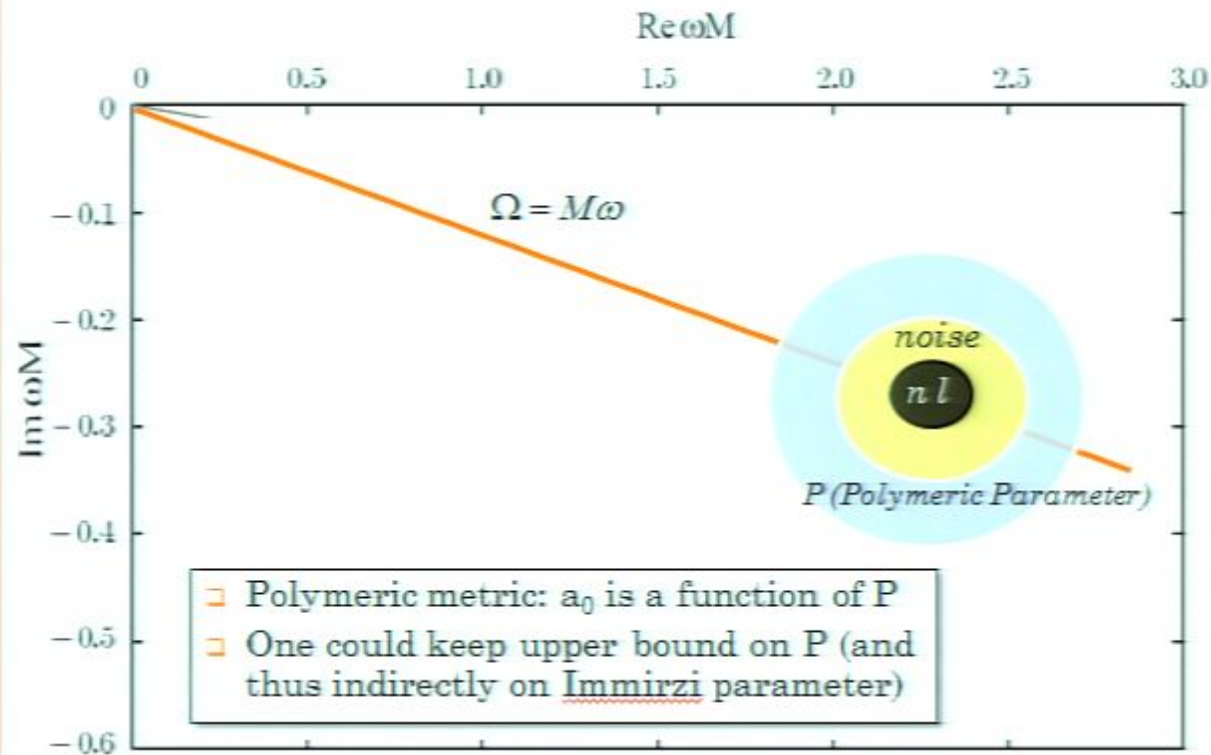M (in M_{Planck})

POSSIBLE PHENOMENOLOGY FOR ASTROPHYSICAL BHs

$\Omega = M\omega$

noise

$n\,l$

P (Polymeric Parameter)

❑ Polymeric metric: a_0 is a function of P
❑ One could keep upper bound on P (and thus indirectly on Immirzi parameter)

Work in progress!