Title: Research Skills - Lecture 3C

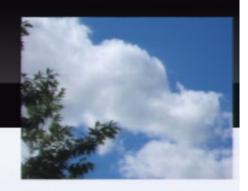
Date: Aug 20, 2010 01:30 PM

URL: http://pirsa.org/10080031

Abstract:

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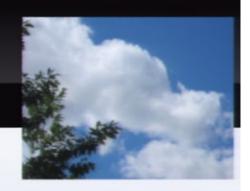
Outline



- Why are clouds white?
- Mie theory:
 - Mie's Work
 - Mie's Approch

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- Clouds are formed by small ice crystals or water droplets
- These scatter incident light
- Mie Scattering





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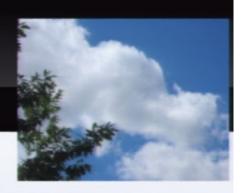




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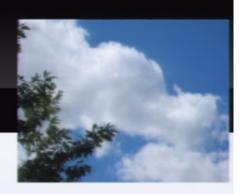
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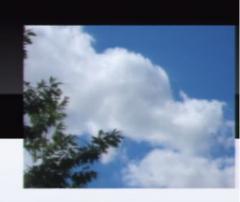
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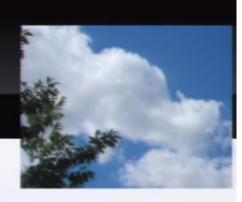
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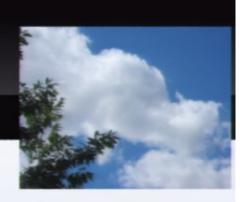
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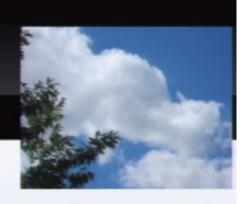
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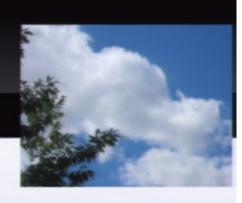
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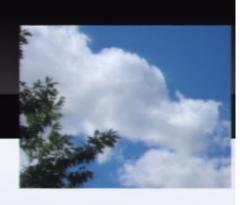
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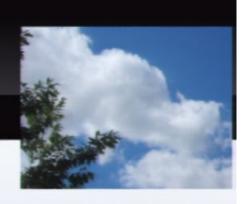
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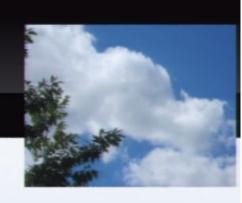
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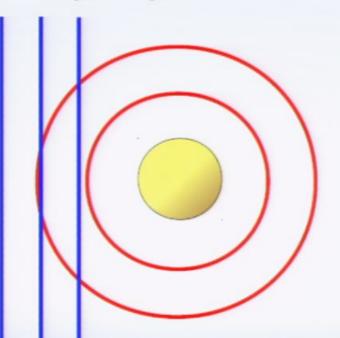
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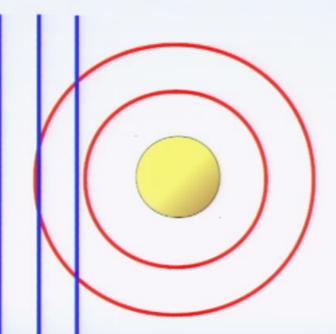
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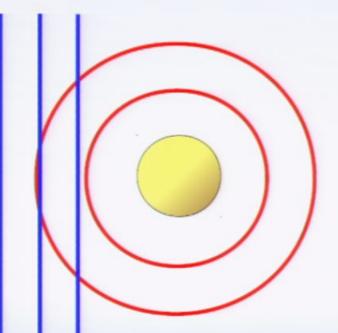
- Assumes colloidal particles are spheres
- Scattering of a electromagnetic plane wave by a sphere
- The medium has refractive index n_o and the particle has refractive index n (complex number in general)



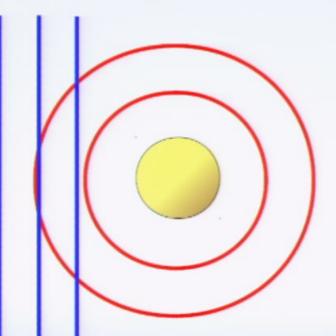
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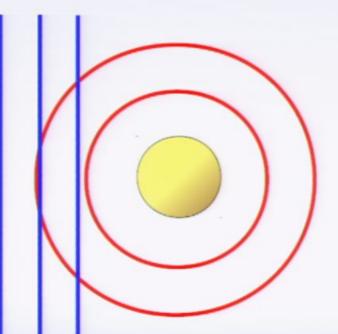
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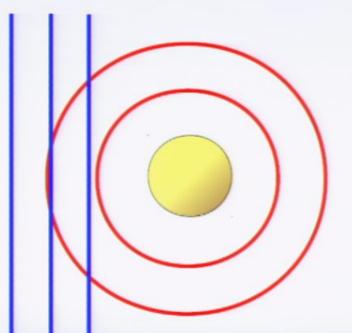
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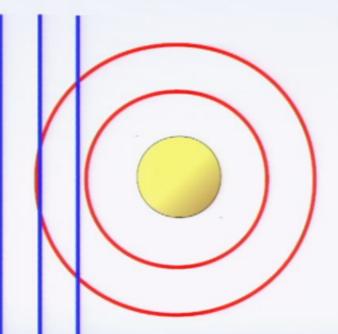
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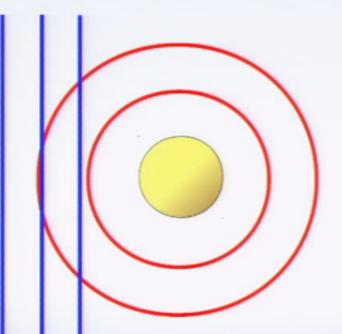
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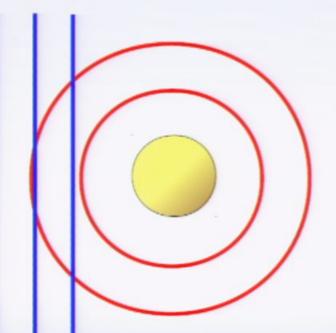
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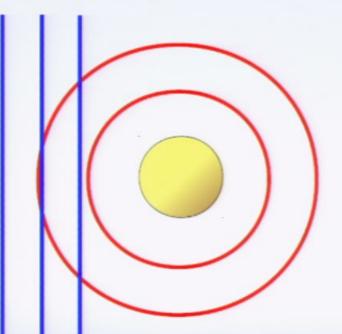
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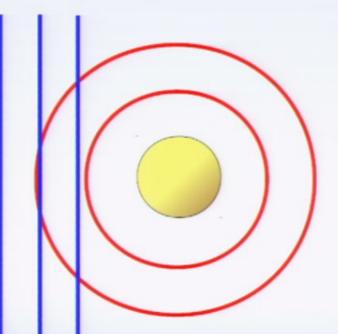
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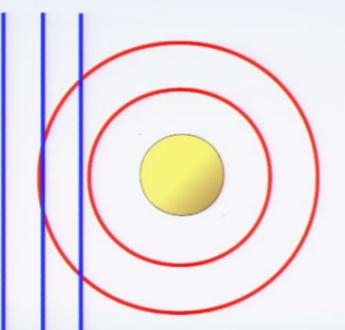
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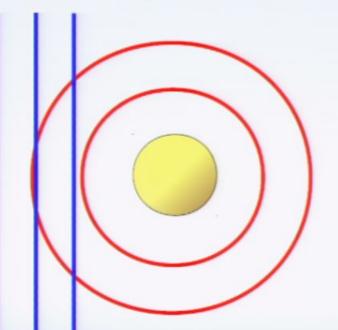


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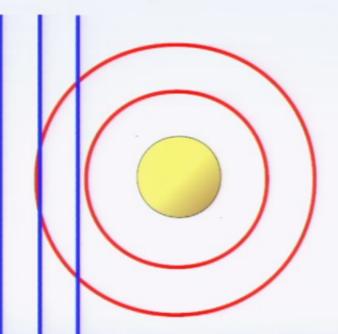


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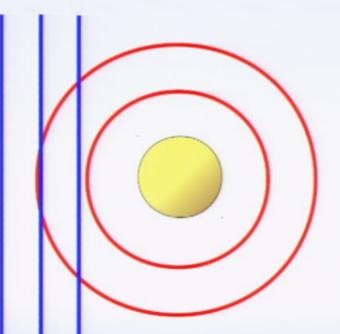




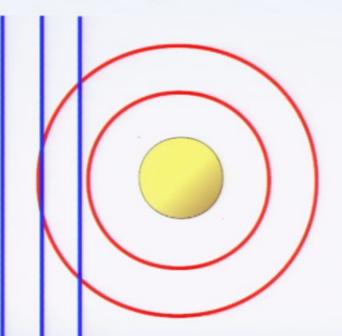
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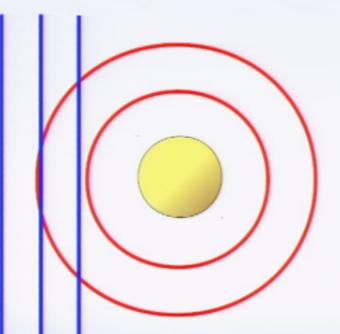
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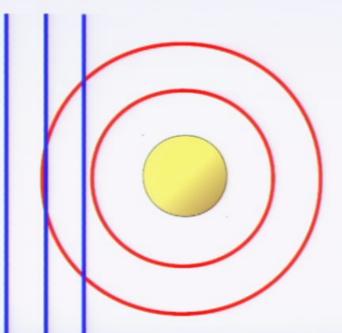
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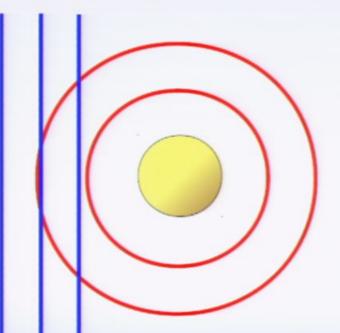
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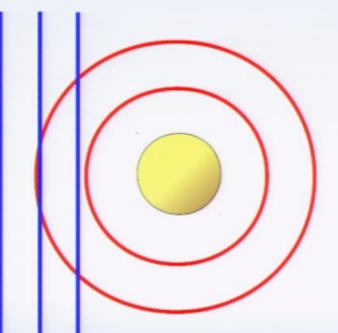
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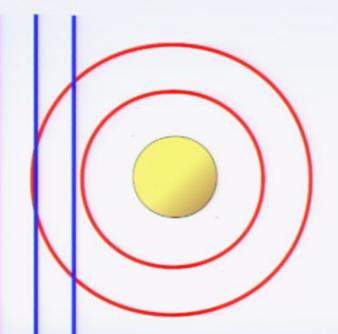
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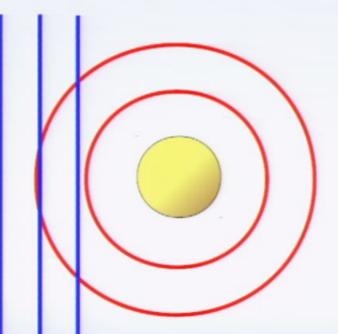
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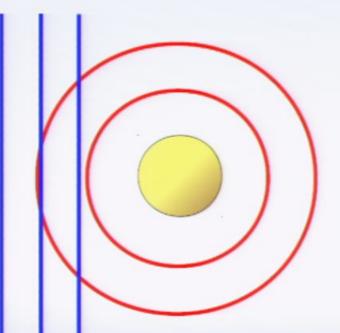
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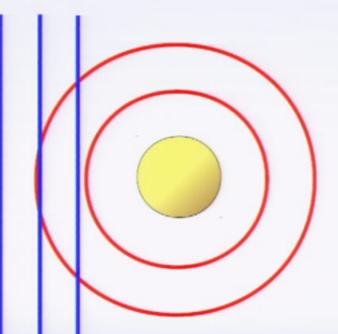
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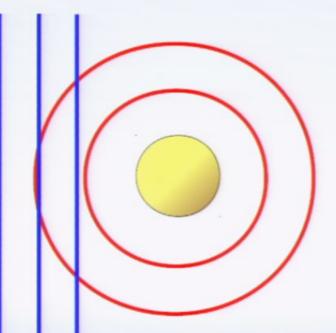
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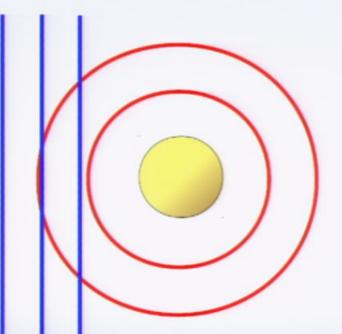
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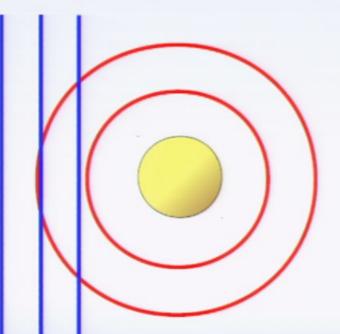
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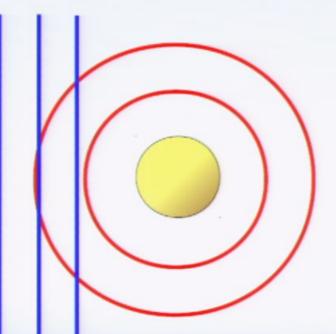
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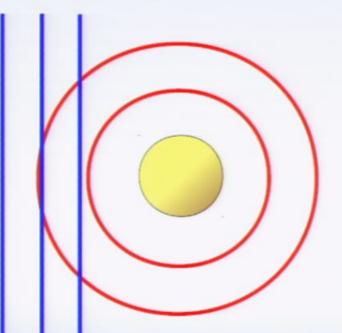
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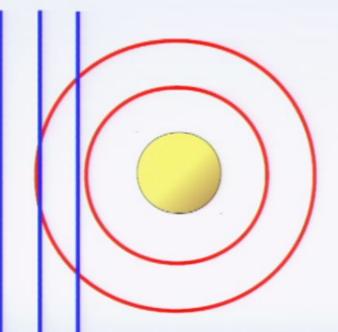
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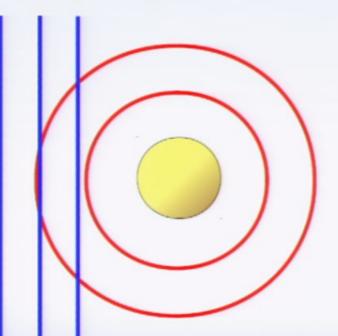
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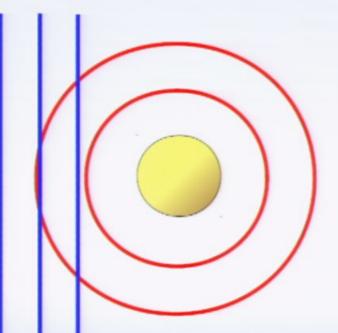
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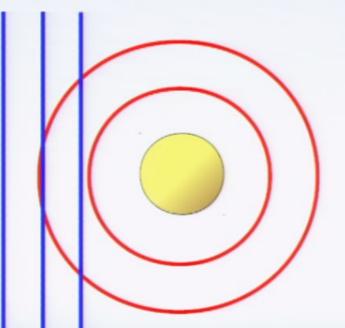
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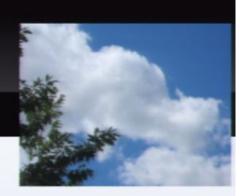


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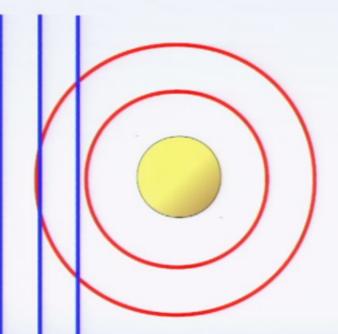


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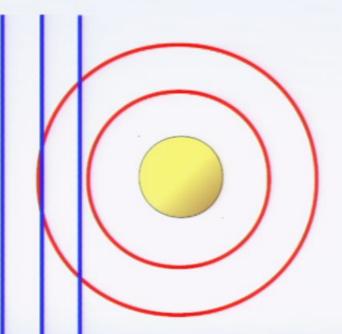




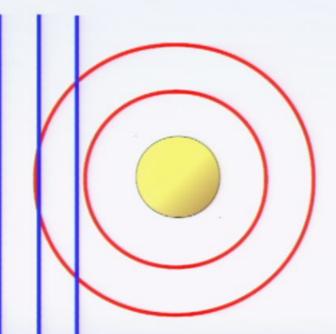
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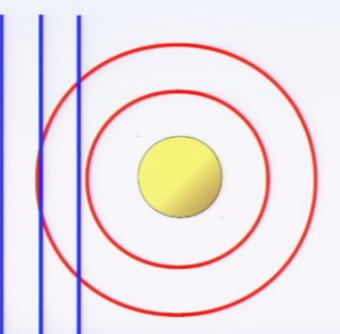
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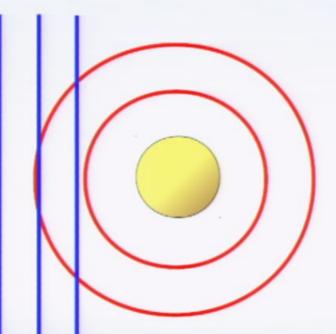
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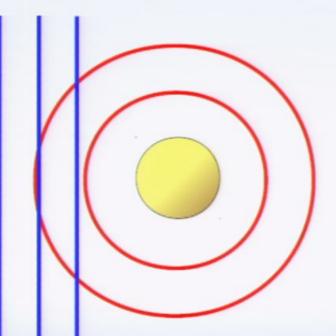
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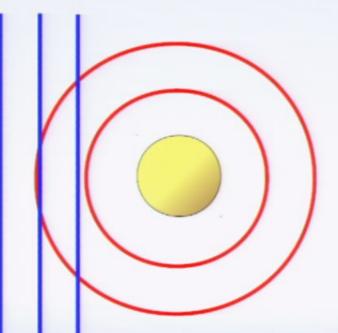
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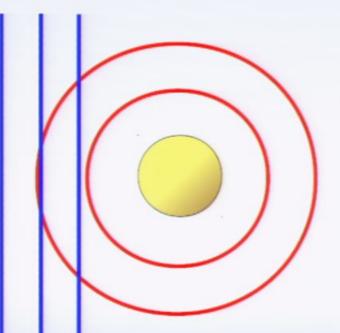
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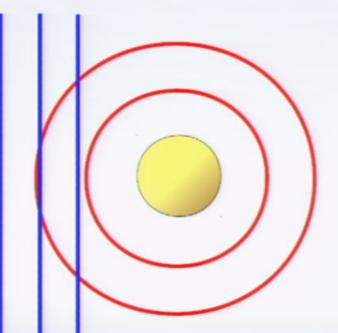
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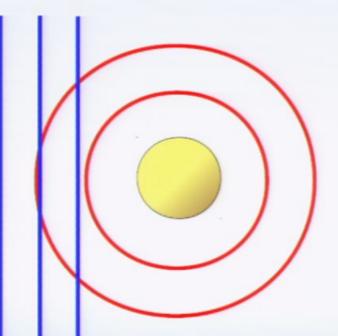
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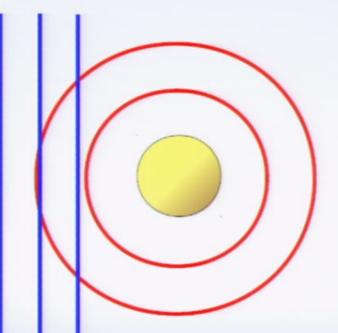
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
- Separation of variables
- Solution is given as series of Bessel functionS

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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
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- Starting point: Maxwell's equations
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- Starting point: Maxwell's equations
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- Starting point: Maxwell's equations
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- Separation of variables
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- Starting point: Maxwell's equations
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- Harmonic time dependance
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- Separation of variables
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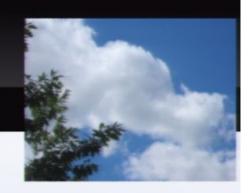
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- Starting point: Maxwell's equations
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- Harmonic time dependance
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- Starting point: Maxwell's equations
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- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
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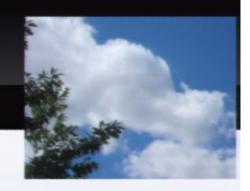
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- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
- Solution is given as series of Bessel functionS

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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
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Pirsa: 10080031



- Starting point: Maxwell's equations
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
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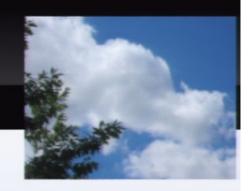
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
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Pirsa: 10080031



- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
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- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
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- Separation of variables
- Solution is given as series of Bessel functionS

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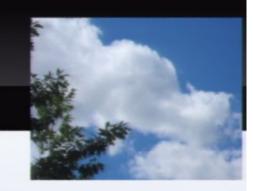
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Pirsa: 10080031 Page 142/662



- Starting point: Maxwell's equations
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- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
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- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strength fields
- Separation of variables
- Solution is given as series of Bessel functionS

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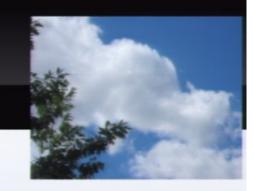


- Starting point: Maxwell's equations
- Spherical coordinates
- Harmonic time dependance
- Continuity conditions on the surface of the sphere for the electrical and magnetic strenght fields
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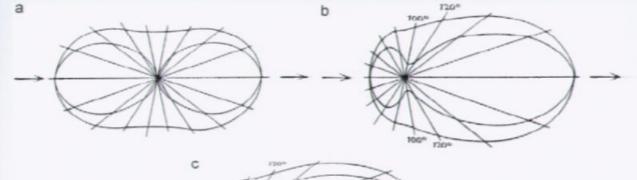
Pirsa: 10080031



- Point like particles $\Longrightarrow 1/\lambda^4$ Rayleigh law
- Particles greater than wavelenght: scattering depends only weakly on λ

Sun light is white, so clouds scatter white light!

Particle size increases forward scattering increases



Polar diagrams:

Incident light: $\lambda = 550 \text{ nm}$

Particle size:

- a) Point like
- b) 160nm
- c)180 nm

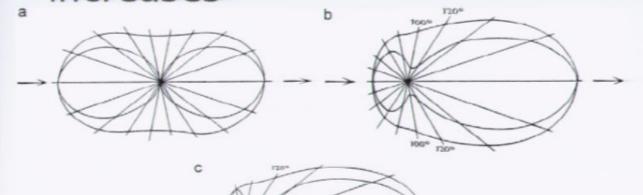
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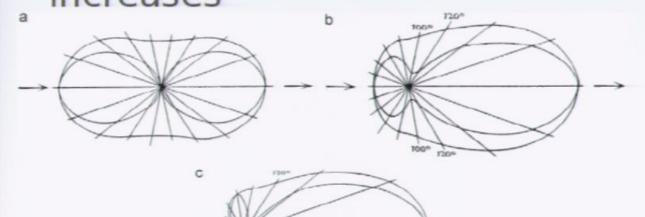
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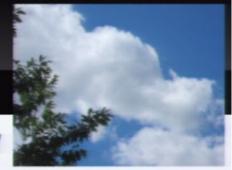
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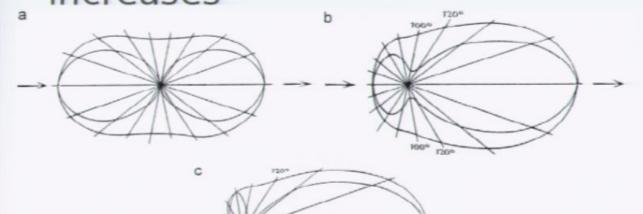
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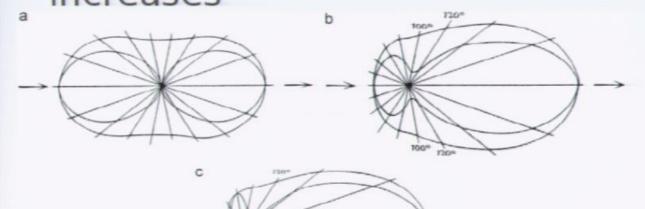
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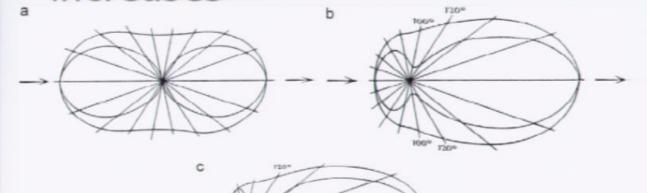
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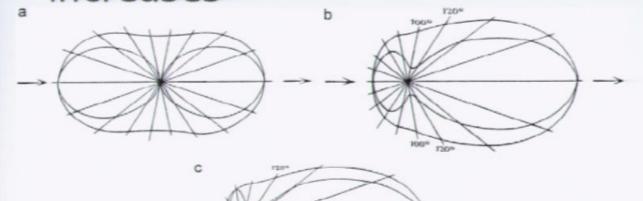
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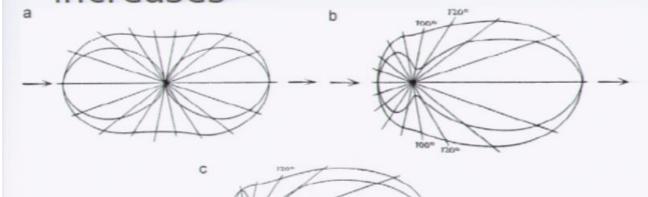
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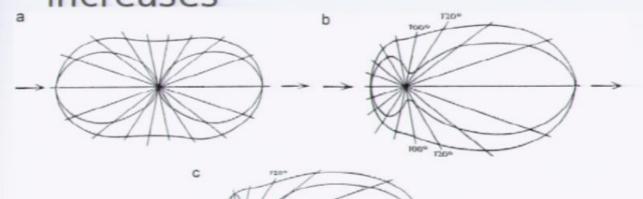
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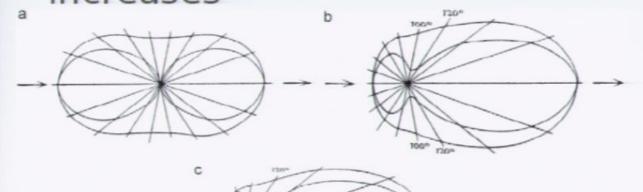
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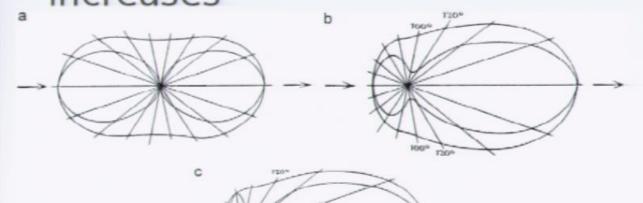
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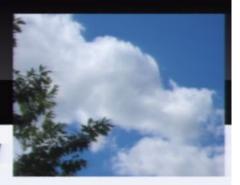
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Pirsa: 10080031



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b 100° 120°

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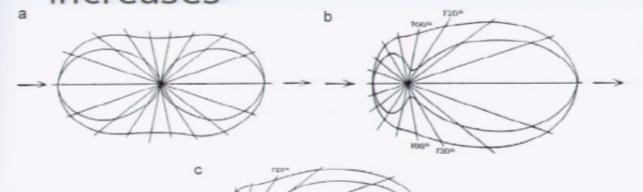
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Pirsa: 10080031

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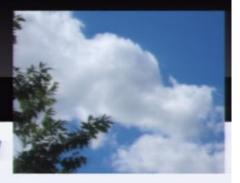
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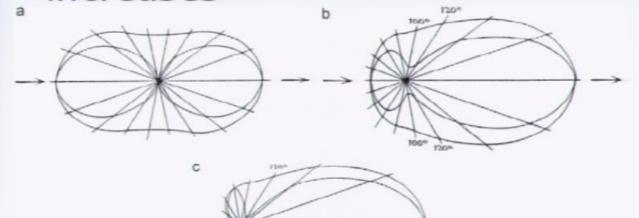
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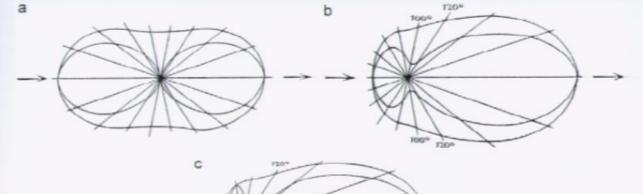
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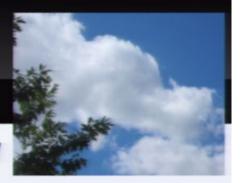
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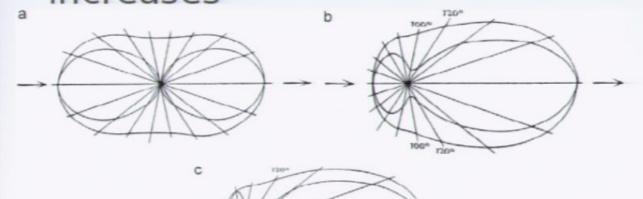
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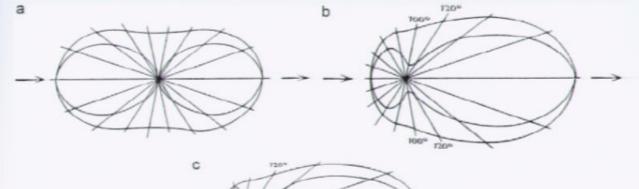
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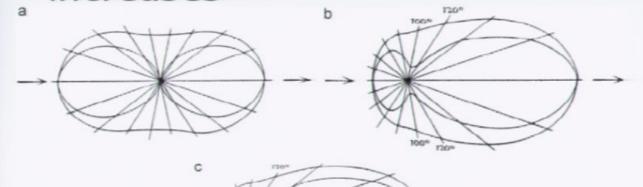
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Incident light: $\lambda = 550 \text{ nm}$

Particle size:

- a) Point like
- b) 160nm

c)180 nm

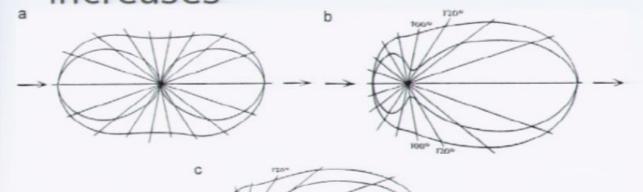
Page 210/662

Pirsa: 10080031

- Point like particles $\longrightarrow 1/\lambda^4$ Rayleigh law
- Particles greater than wavelenght: scattering depends only weakly on λ

Sun light is white, so clouds scatter white light!

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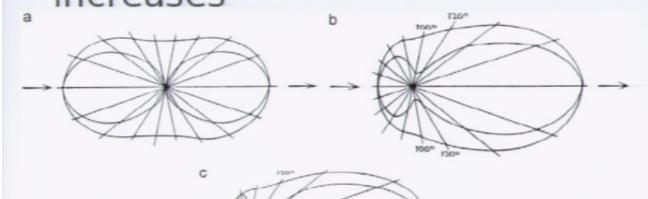
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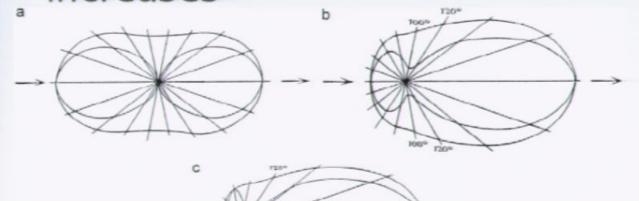
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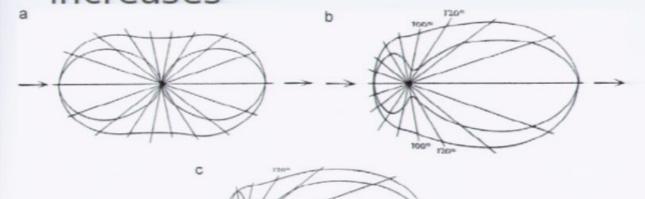
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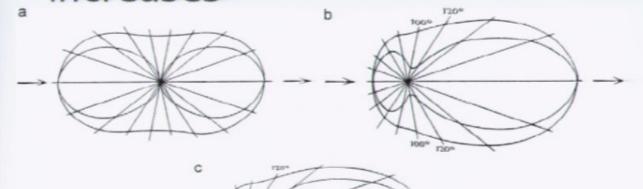
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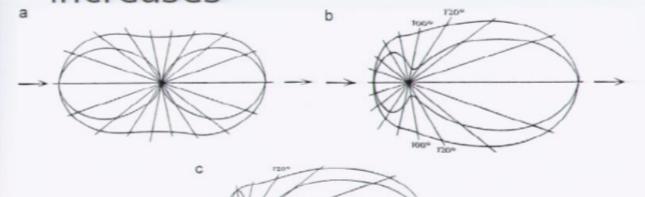
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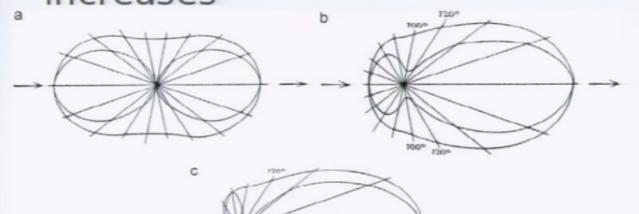
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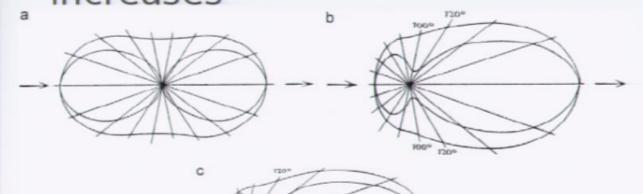
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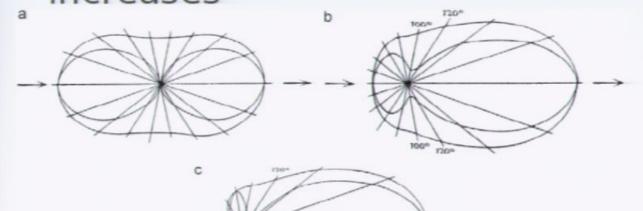
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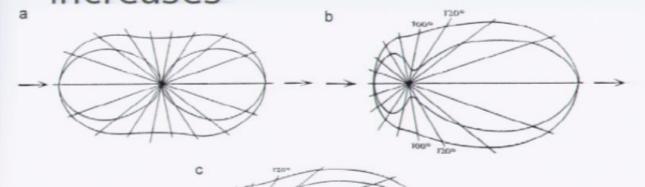
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b 150°

C 120°

C 120°

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Conclusions



- White colour of clouds is due to Mie scattering
- Mie theory treats scattering by spherical particles of any size
- Mie scattering depends weakly on wavelength, when the particle size is larger than wavelength
- For water droplets all light is scattered almost in the same



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Outline

- Stay-on-tab What it is and a little bit of history
- Leverage and levers The physics and examples of levers
- The scored lid Comments on the lid of a soda can
- Summary

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Invented by Dan Cudzik in 1975



Figure: The stay-on-tab

- Invented by Dan Cudzik in 1975
- Designed to replace the old pull tab which was an environmental problem



Figure: The pull-tab (Wikipedia)

- Invented by Dan Cudzik in 1975
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- Easy and safe to use no sharp edges



Figure: The stay-on-tab

- Invented by Dan Cudzik in 1975
- Designed to replace the old pull tab which was an environmental problem
- Easy and safe to use no sharp edges
- Simple desing cheap and easy to fabricate



Figure: The stay-on-tab

Leverage

"Give me a lever long enough and a fulcrum on which to place it, and I shall move the world"

- Archimedes

$$\tau = \mathsf{r} \times \mathsf{F}$$
 (1)

where au is the torque vector, ${\bf r}$ is the displacement vector and ${\bf F}$ is the force vector

Lever amplifies the force you excert on the can

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Classes of levers

Class 1: The fulcrum is located between the applied force and the load



Figure: Scissors (Wikipedia)

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Classes of levers

- Class 1: The fulcrum is located between the applied force and the load
- Class 2: The load is situated between the fulcrum and the force



Figure: Wheelbarrow (Wikipedia)

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Classes of levers

- Class 1: The fulcrum is located between the applied force and the load
- Class 2: The load is situated between the fulcrum and the force
- between the fulcrum and the load

 Davidovits, Paul (2008),

 Physics in Biology and

 Medicine, Third edition



Figure: Tweezers (Wikipedia)

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The stay-on-tab is a class 1 lever



Figure: The stay-on-tab

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- The stay-on-tab is a class 1 lever
- Lets assume that the force is perpendicular to the ring pull



Figure: The stay-on-tab

Pirsa: 10080031 Page 234/662

- The stay-on-tab is a class 1 lever
- Lets assume that the force is perpendicular to the ring pull
- $r_1 \approx 20 \text{ mm} \text{ and } r_2 \approx 5 \text{ mm}$ $\Rightarrow \text{ force is quadrupled}$
- But wait! There's more!



Figure: The stay-on-tab

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The lid is scored to make things easier



Figure: The scored lid (Wikipedia)

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- The lid is scored to make things easier
- The score has to be precise; not too deep and not too shallow



Figure: The scored lid (Wikipedia)

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- The lid is scored to make things easier
- The score has to be precise; not too deep and not too shallow
- The lid and the tab are manufactured separately



Figure: The scored lid (Wikipedia)

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- The lid is scored to make things easier
- The score has to be precise; not too deep and not too shallow
- The lid and the tab are manufactured separately
- The lid is made of a different alloy and is much thicker than the rest of the can



Figure: The scored lid (Wikipedia)

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- The stay-on-tab has taken us through:
 - Archimedes (lever)



Figure: The stay-on-tab

- The stay-on-tab has taken us through:
 - Archimedes (lever)
 - Clapeyron (ideal gas law)



Figure: The stay-on-tab

- The stay-on-tab has taken us through:
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 - Modern engineering



Figure: The stay-on-tab

- The stay-on-tab has taken us through:
 - Archimedes (lever)
 - Clapeyron (ideal gas law)
 - Modern engineering
- Above all: human curiosity and ingenuity



Pirsa: 10080031 Page 243/662

- The stay-on-tab has taken us through:
 - Archimedes (lever)
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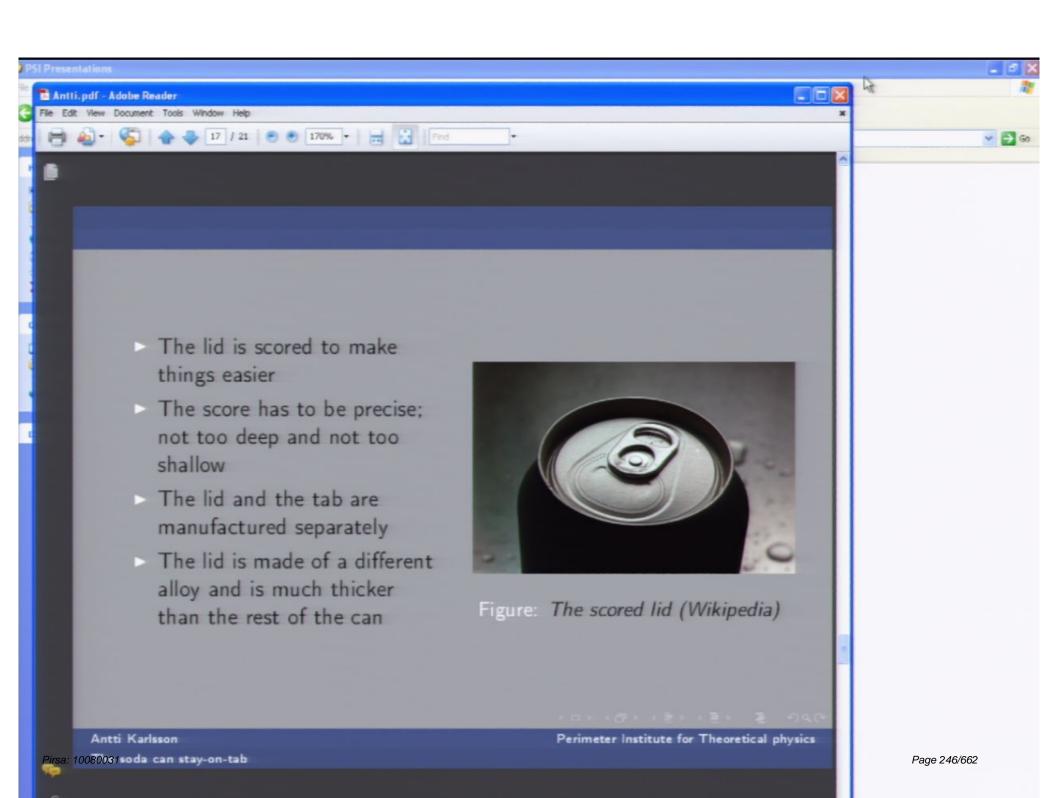
Figure: The stay-on-tab

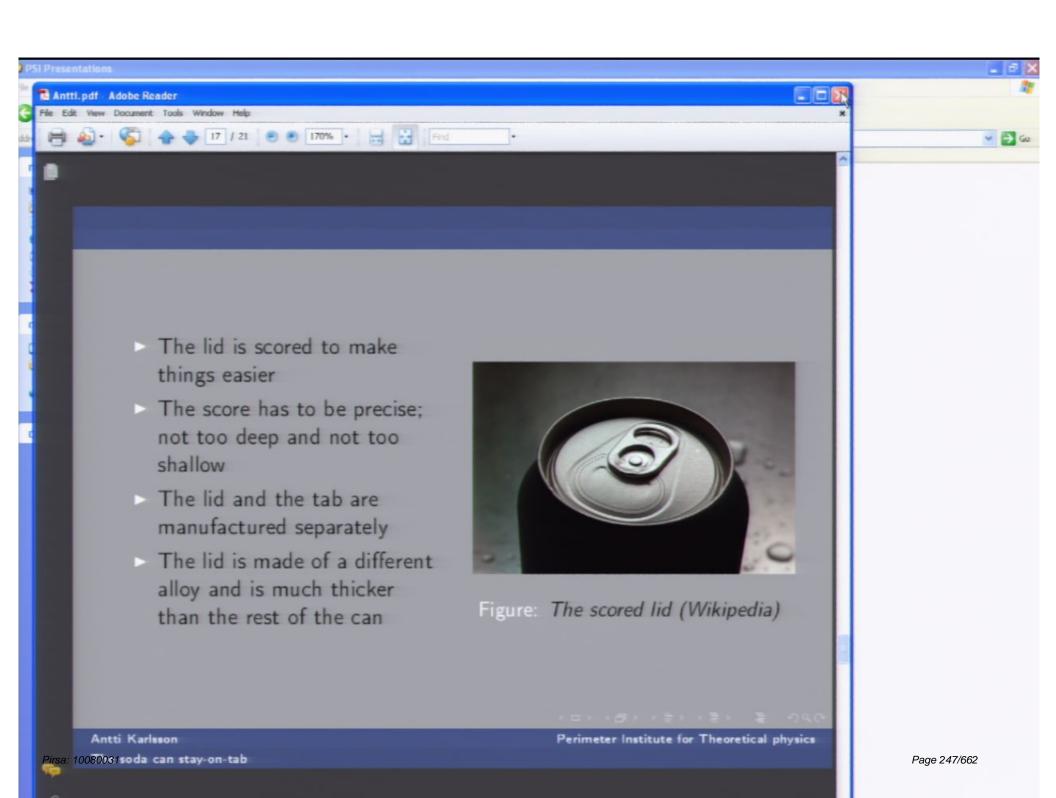
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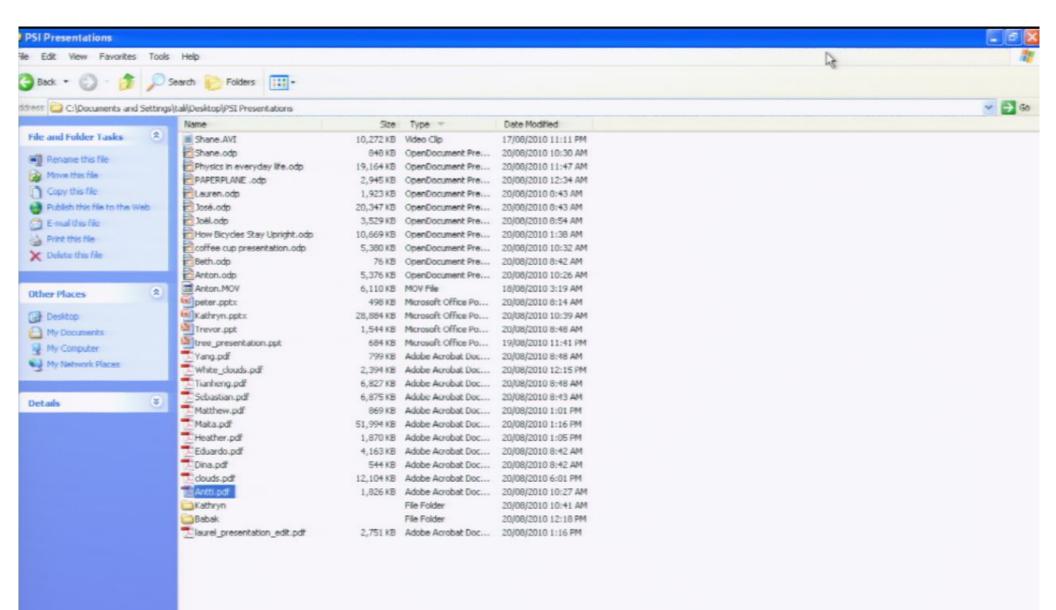


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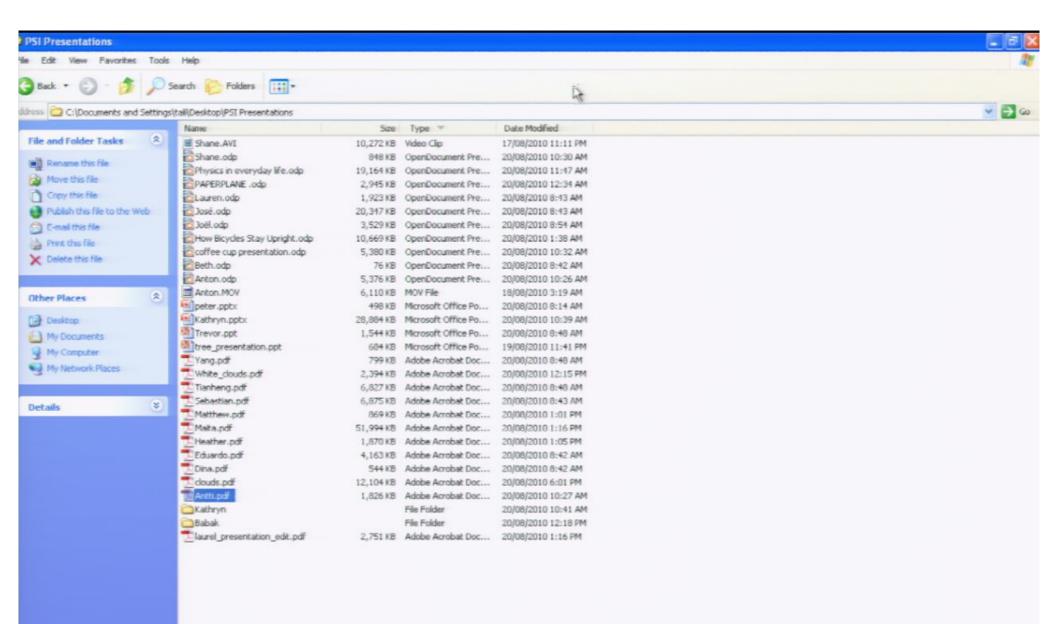
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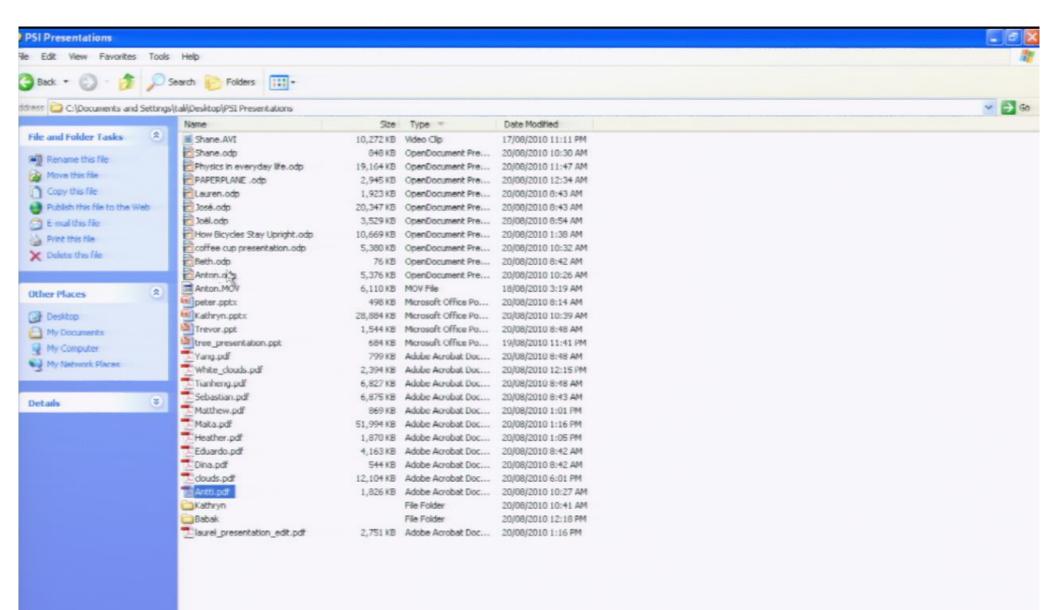




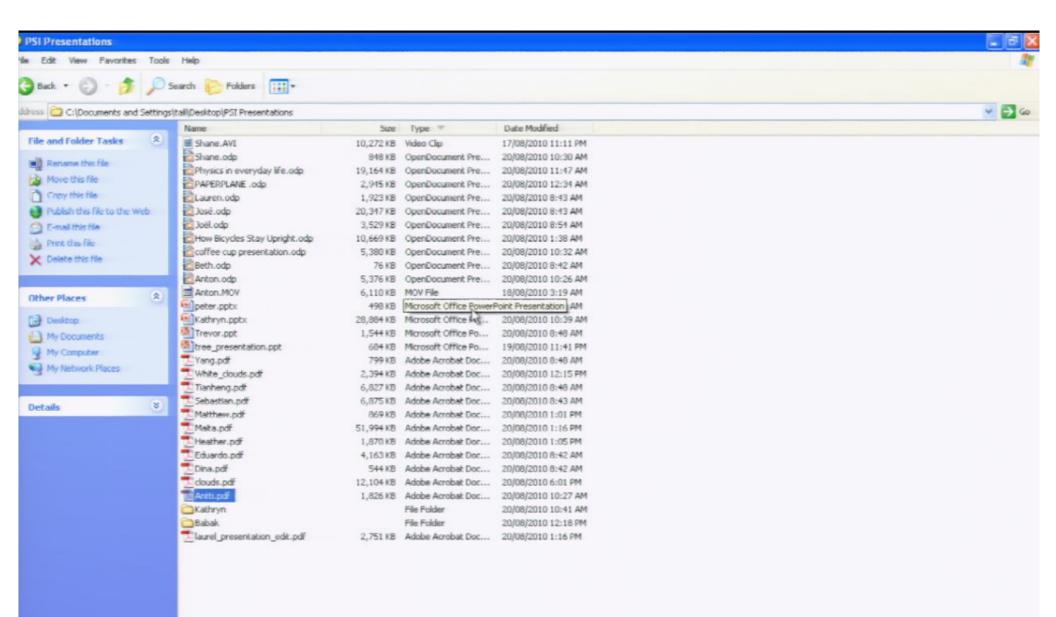
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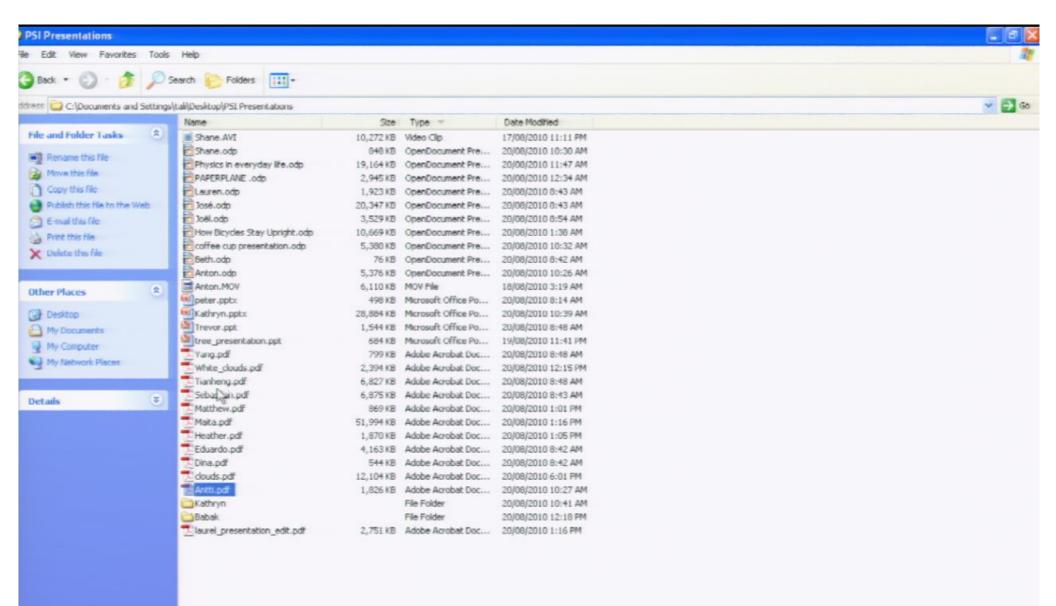
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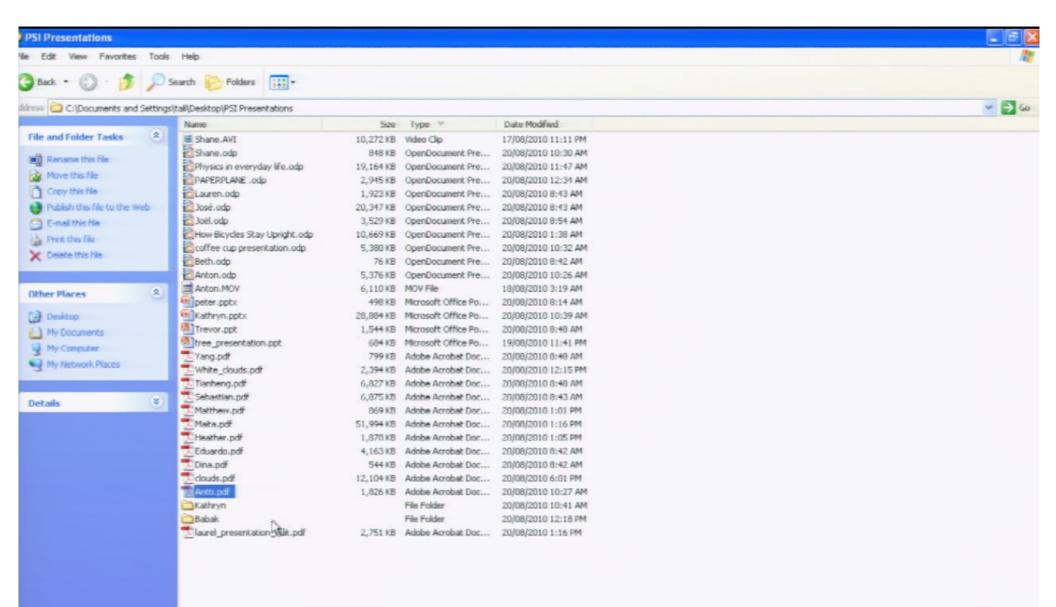
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How Bicycles Stay Upright

Maeve Manion-Fischer
Perimeter Scholars International

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Outline

Can you explain how a bicycle works?

Possible Explanations

Experimental Tests

Unexpected Effects

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Possible Explanations

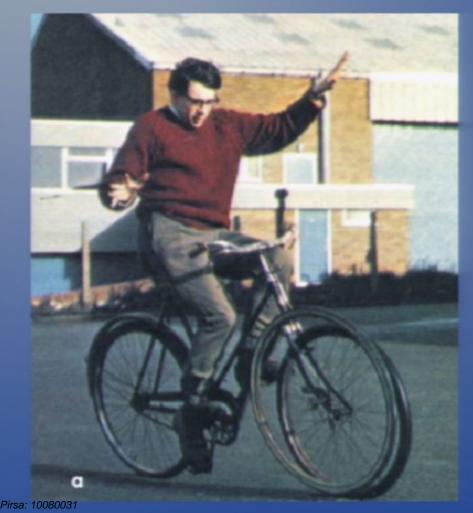
- Centrifugal force
- Gyroscopic Motion
- A rolling hoop stays upright because of gyroscopic forces, shouldn't a bicycle wheel be similar?



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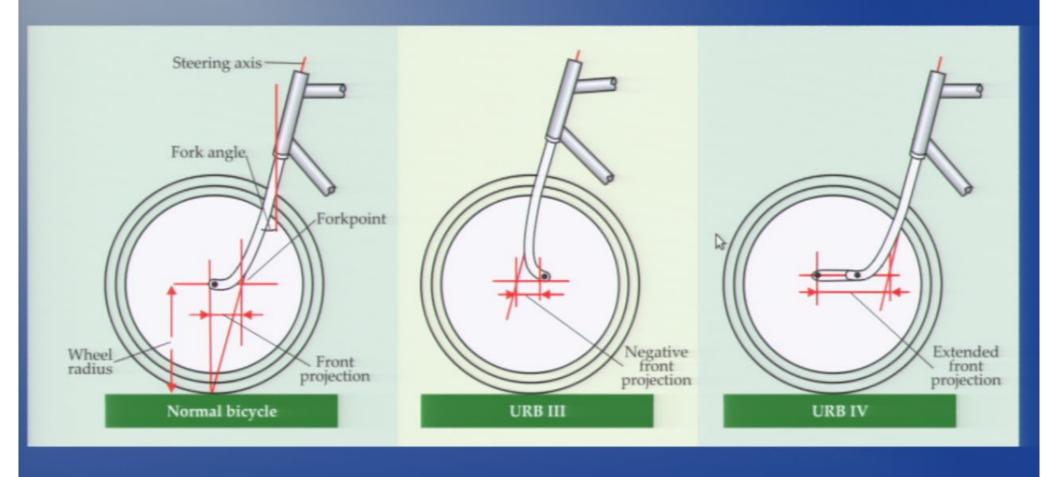
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Testing the Hypothesis



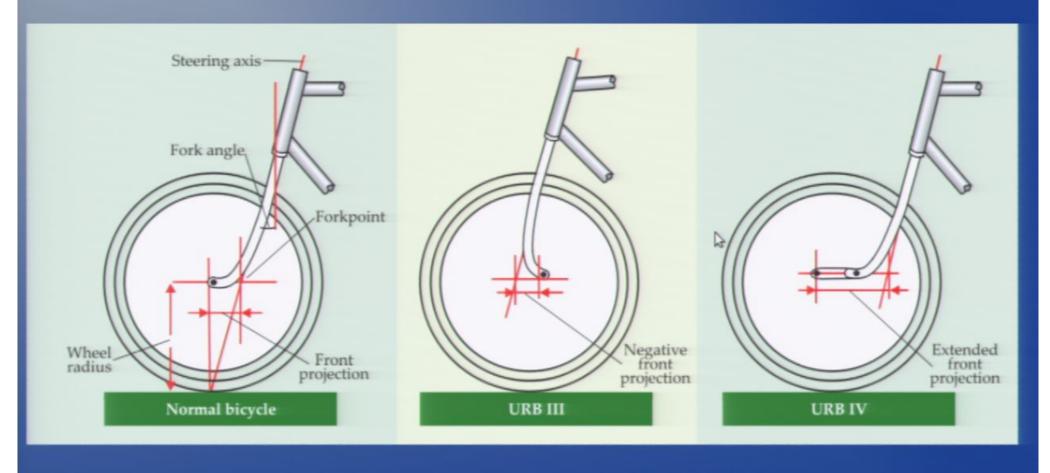
- Riderless normal bicycle will stay upright for awhile (centrifugal forces not enough to explain this)
- When riderless, this bicycle will fall over immediately.

The Effect of the Steering Mechanism



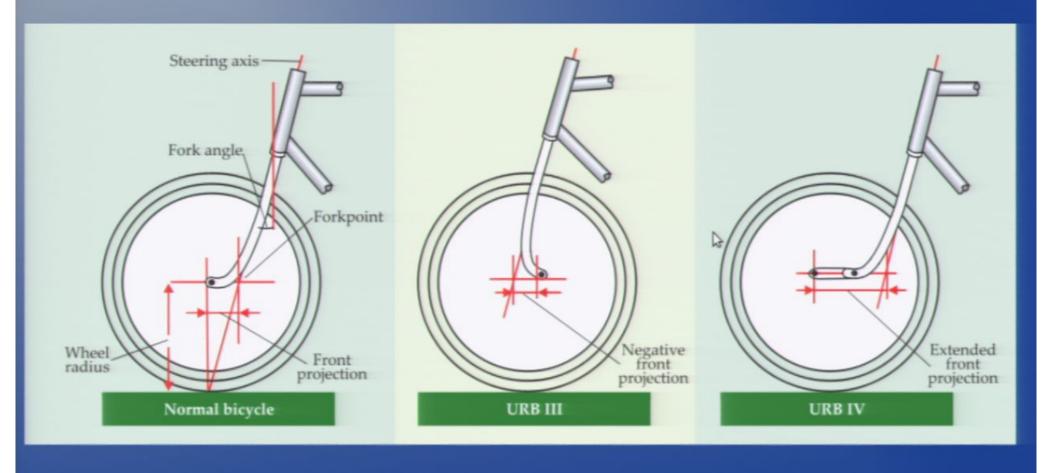
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The Effect of the Steering Mechanism



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The Effect of the Steering Mechanism



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Conclusions

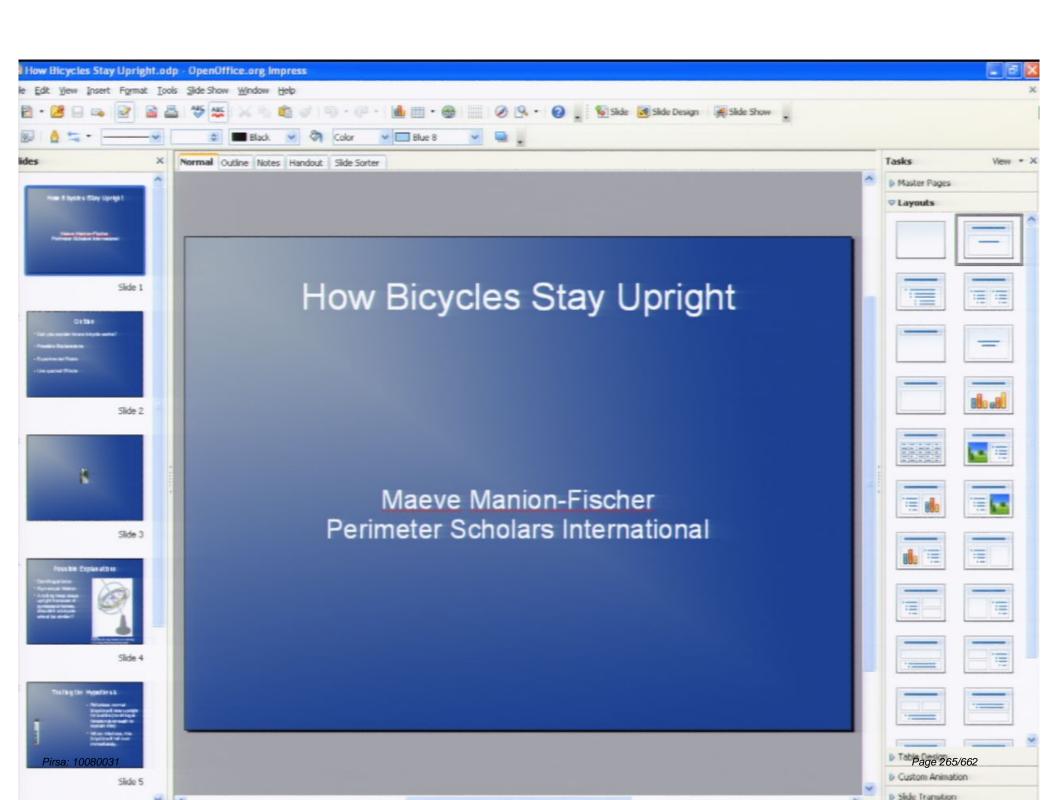
- Explanations that immediately come to mind do not explain the motion of a bicycle
- The stability of bicycles is best explained by both the structure of the steering mechanism and castoring forces.

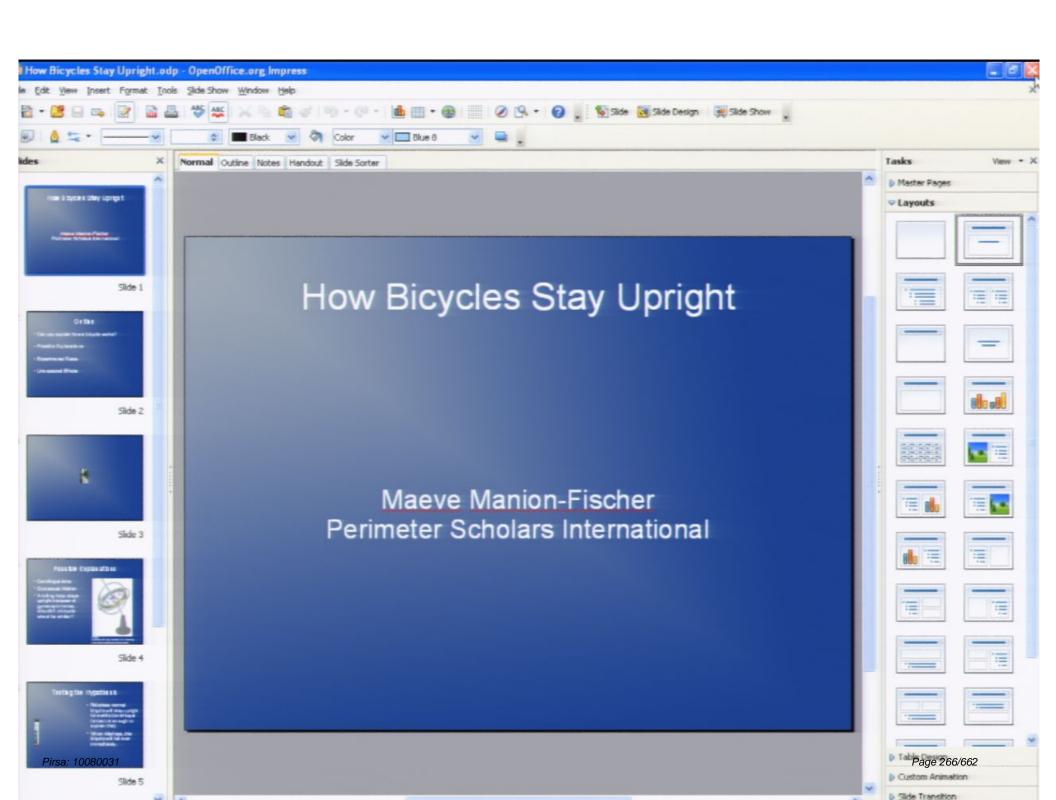
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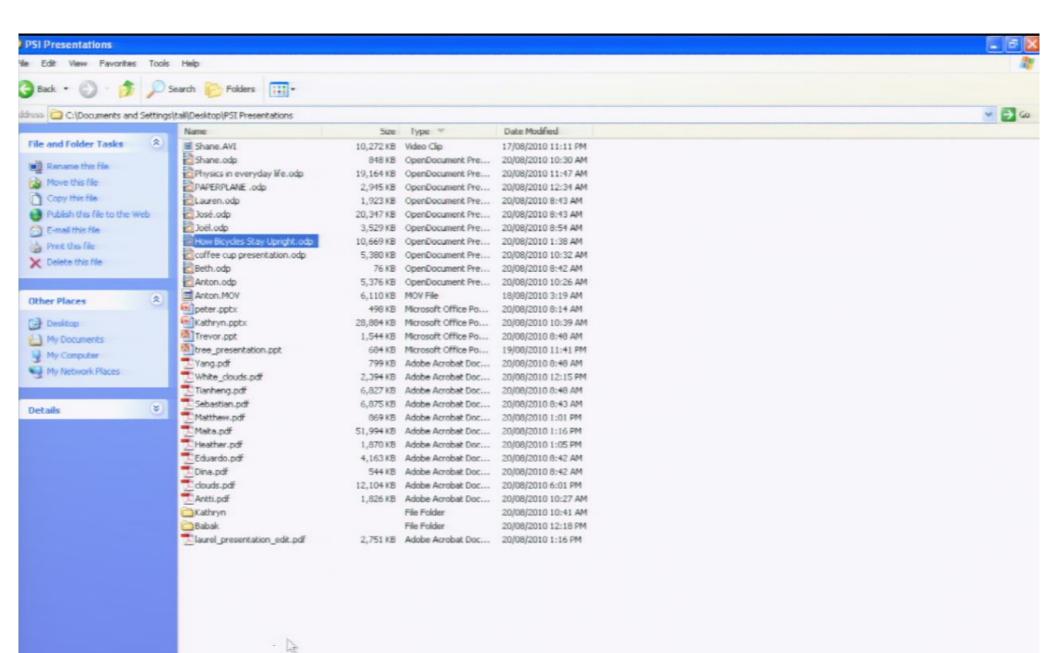
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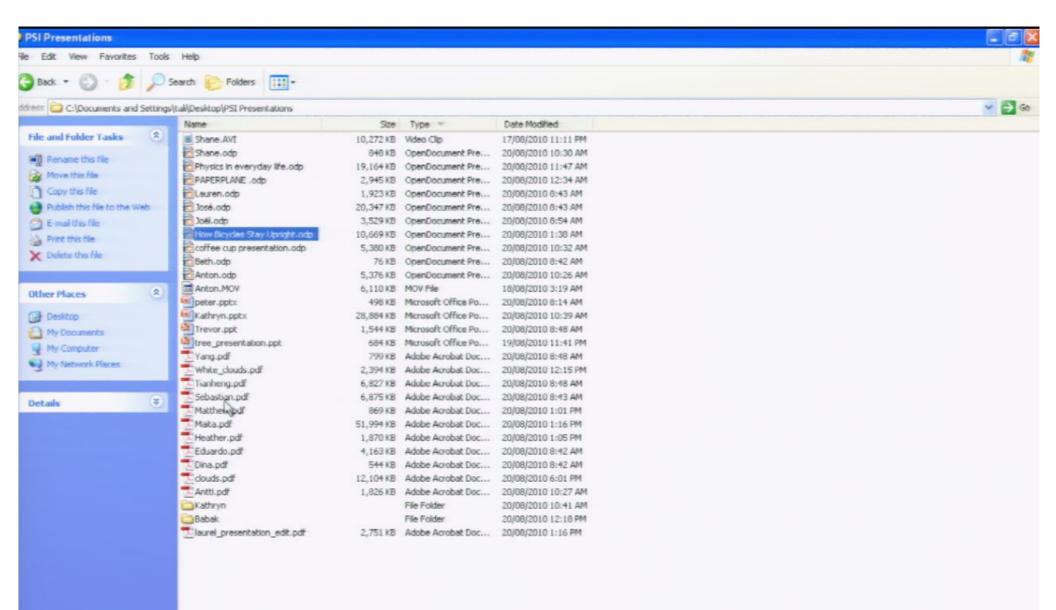




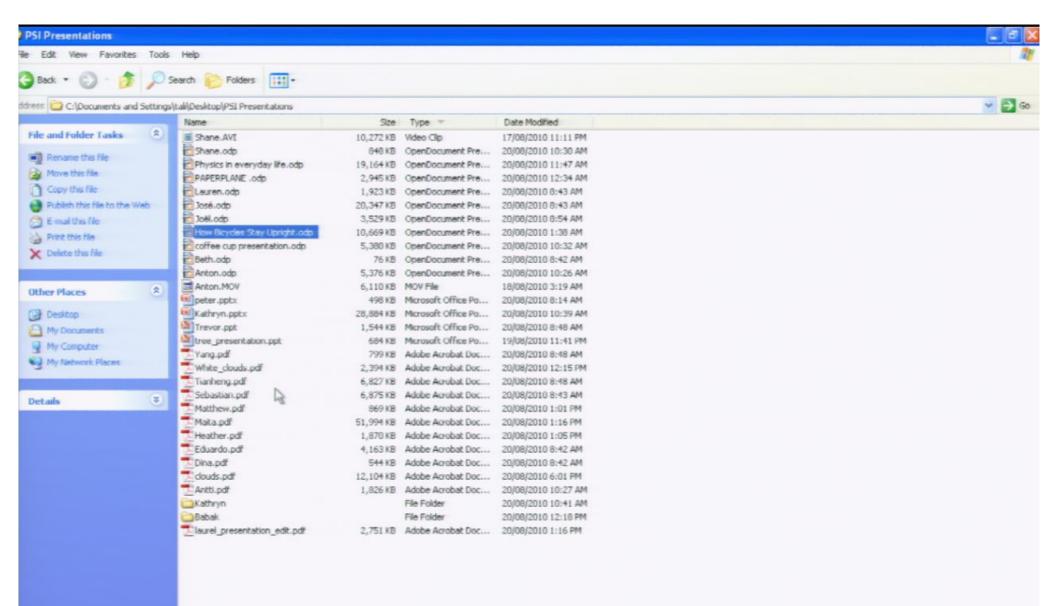




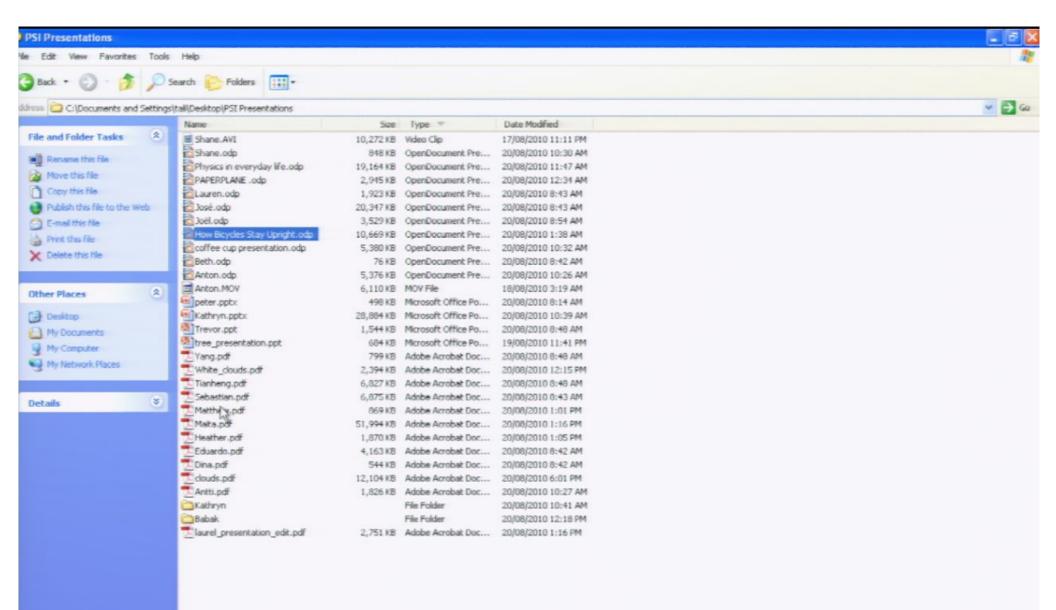
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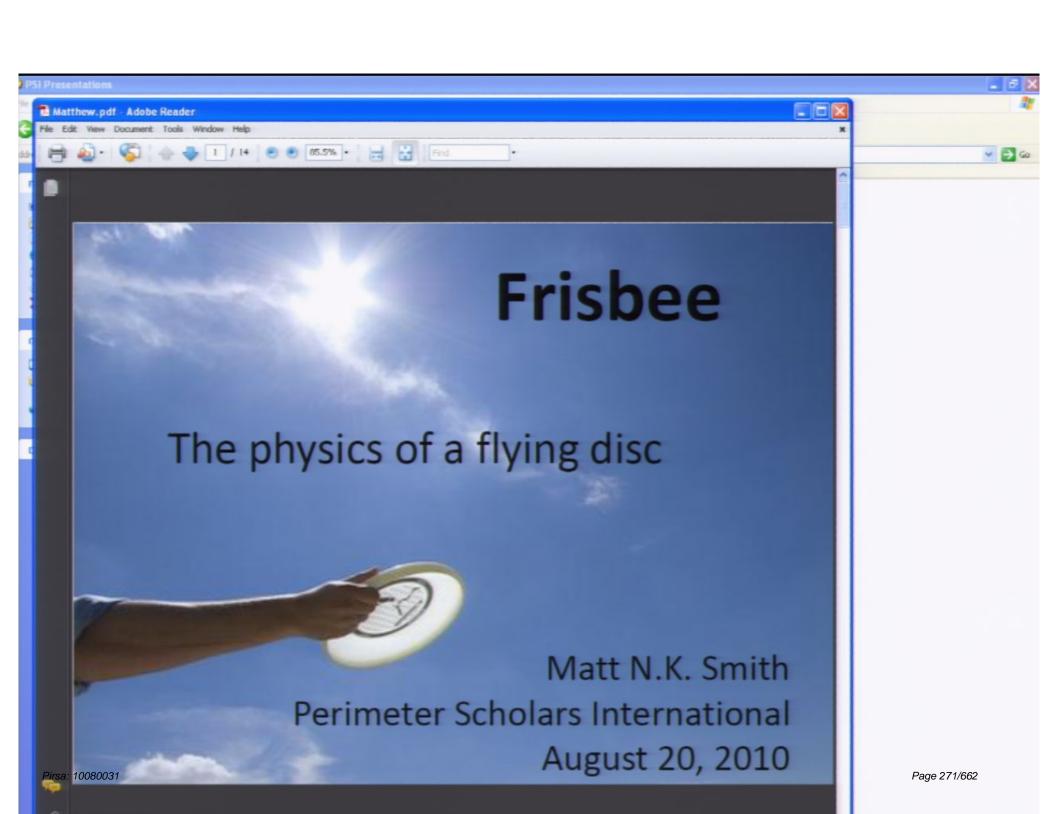
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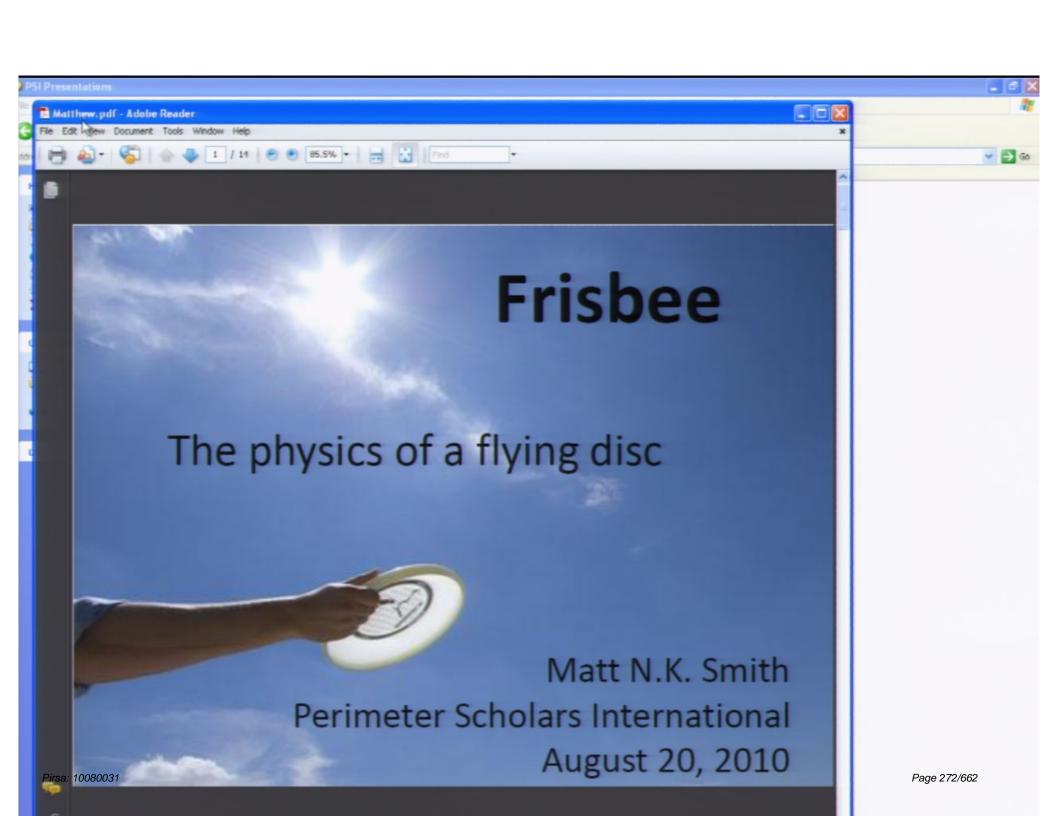


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Frisbee

The physics of a flying disc

Matt N.K. Smith
Perimeter Scholars International

Outline

- I. Why frisbee?
- Free body diagram
- III. Physics of a flying object
 - Drag
 - Lift
- IV. Physics of a rotating object
 - Angular momentum
 - Gyroscopic precession
- V. Conclusions

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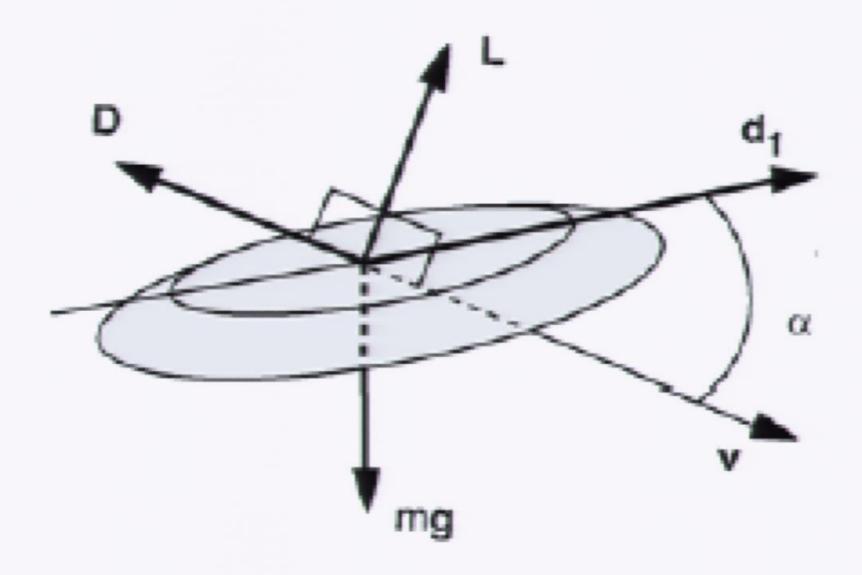
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- A thrown disc travels farther than a thrown ball
- The frisbee has high resistance to vertical velocity

Air resistance



- A thrown disc travels farther than a thrown ball
- The frisbee has high resistance to vertical velocity





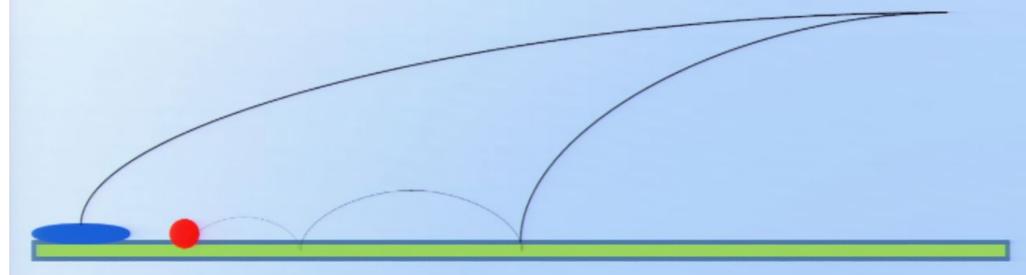
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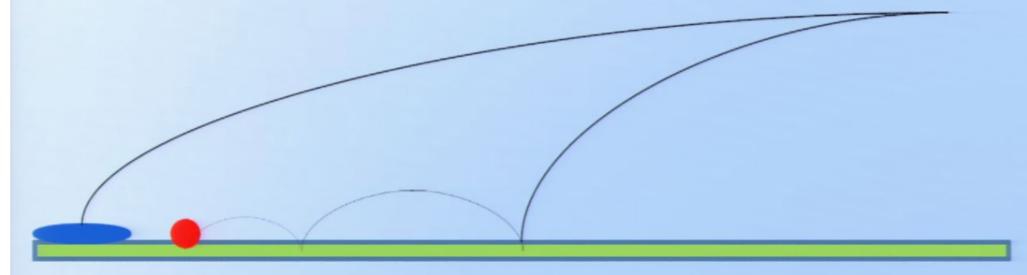
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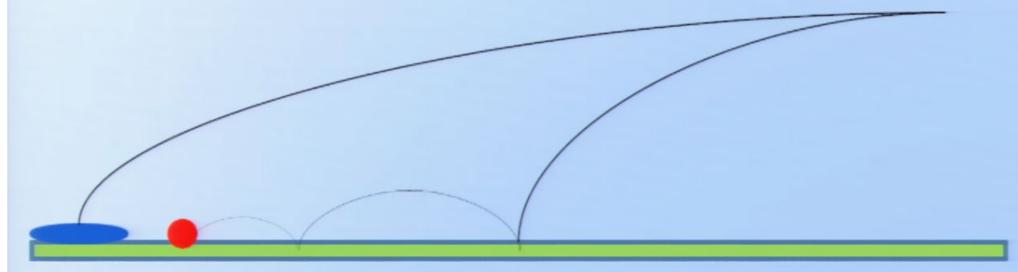
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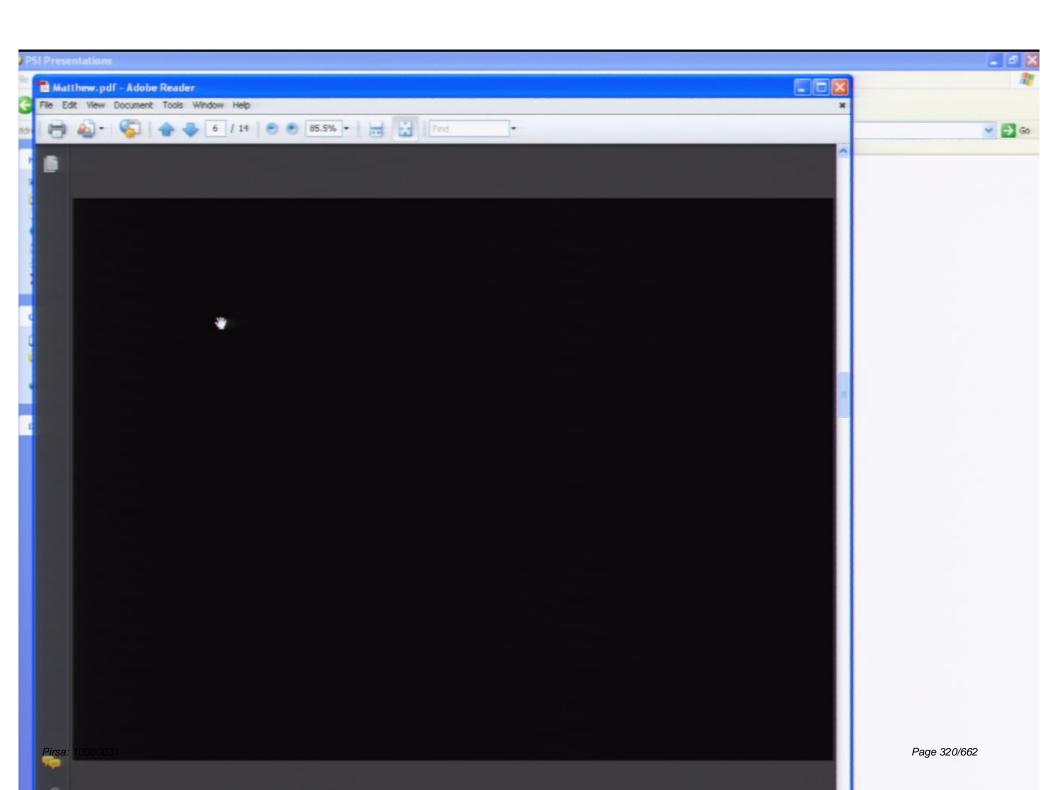


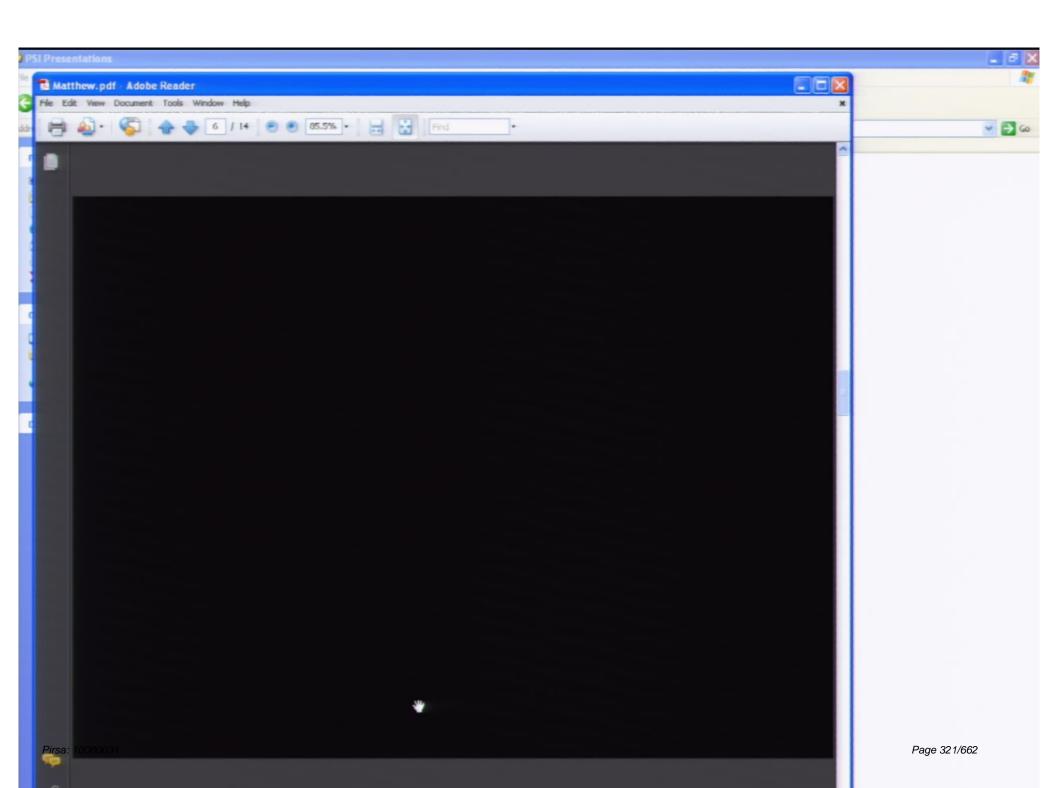
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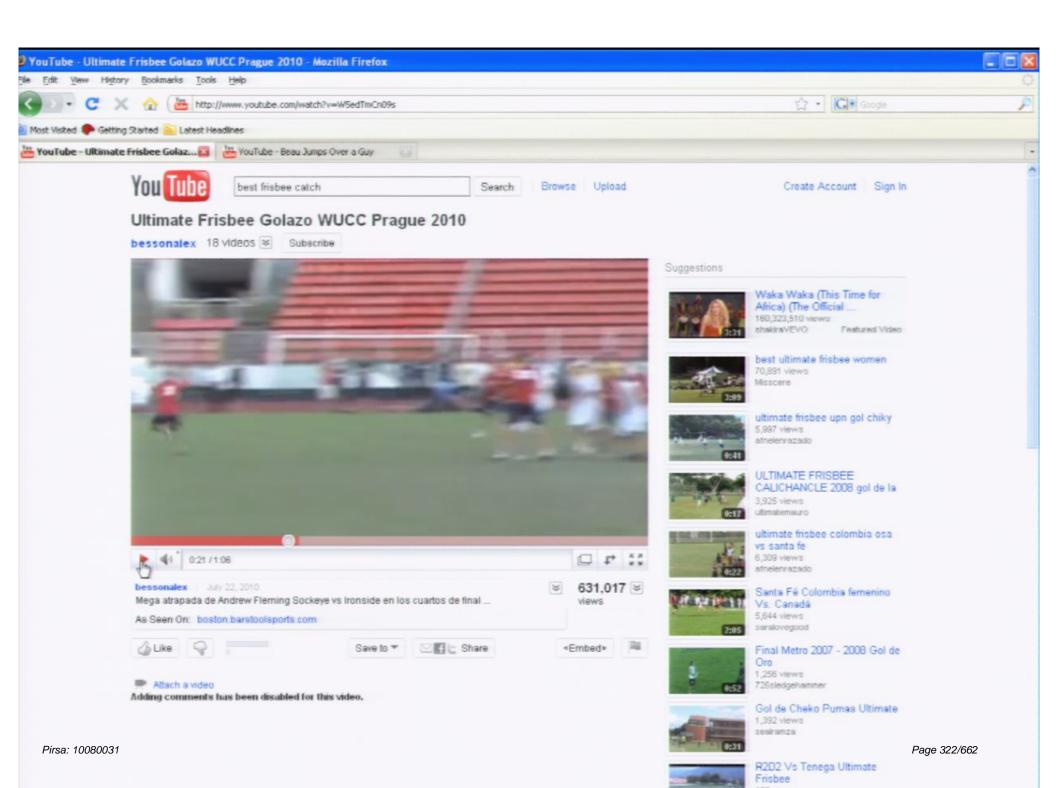
Air resistance

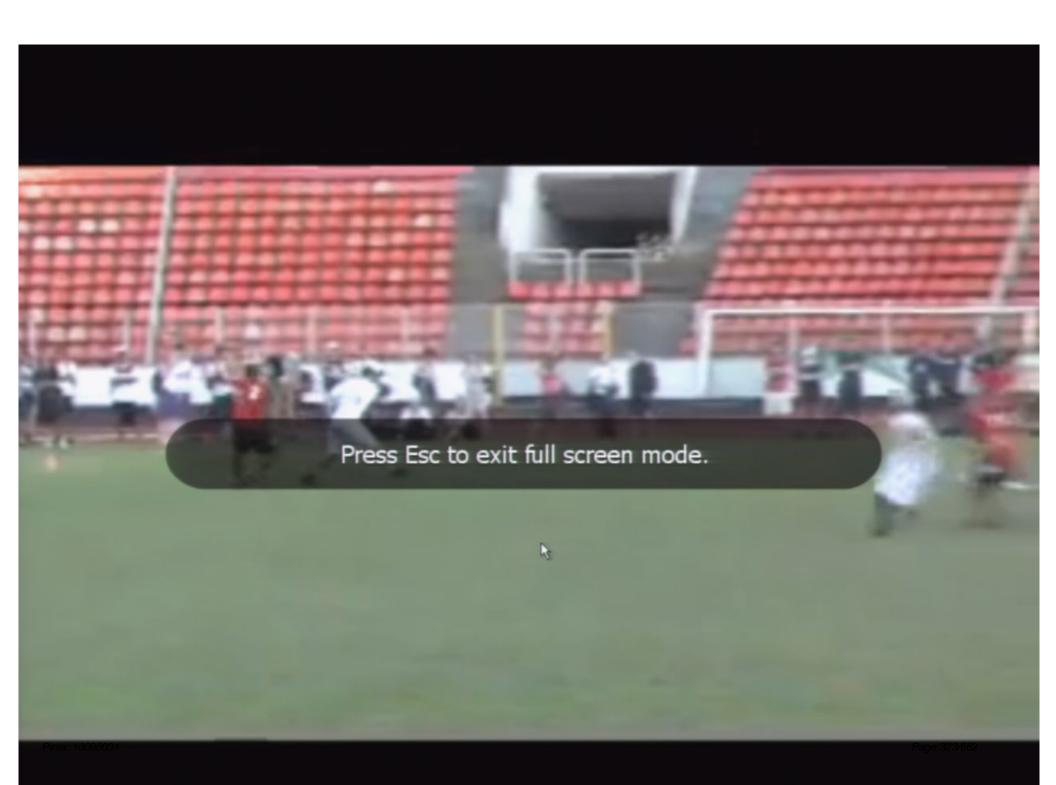


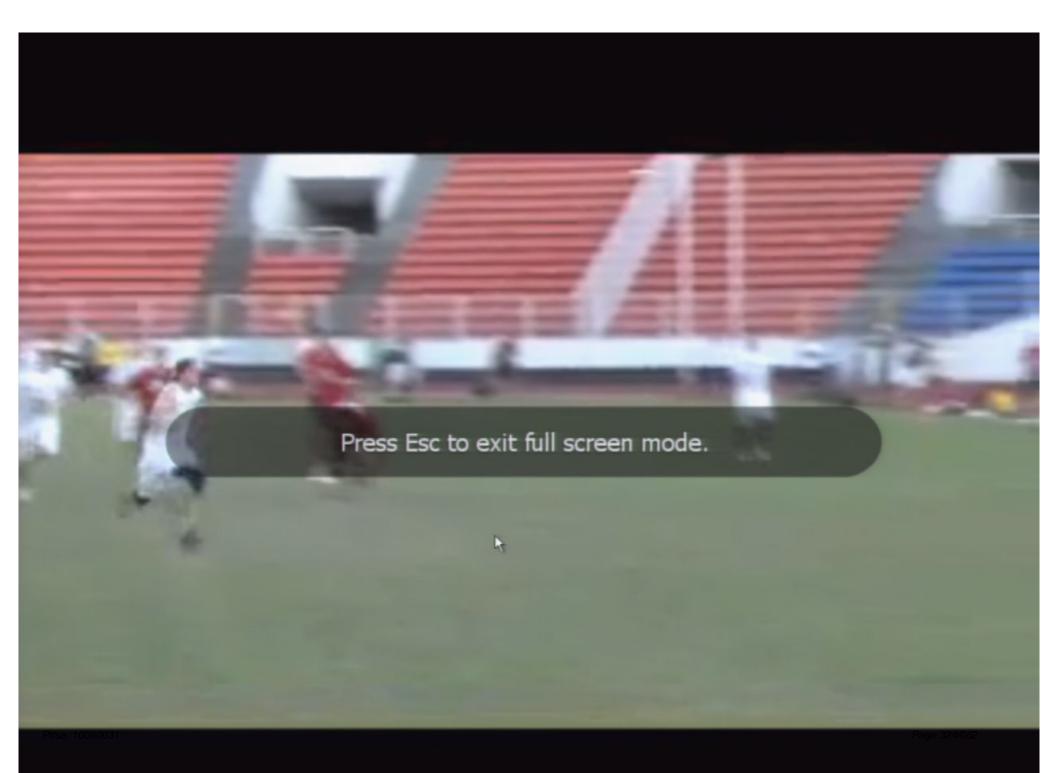
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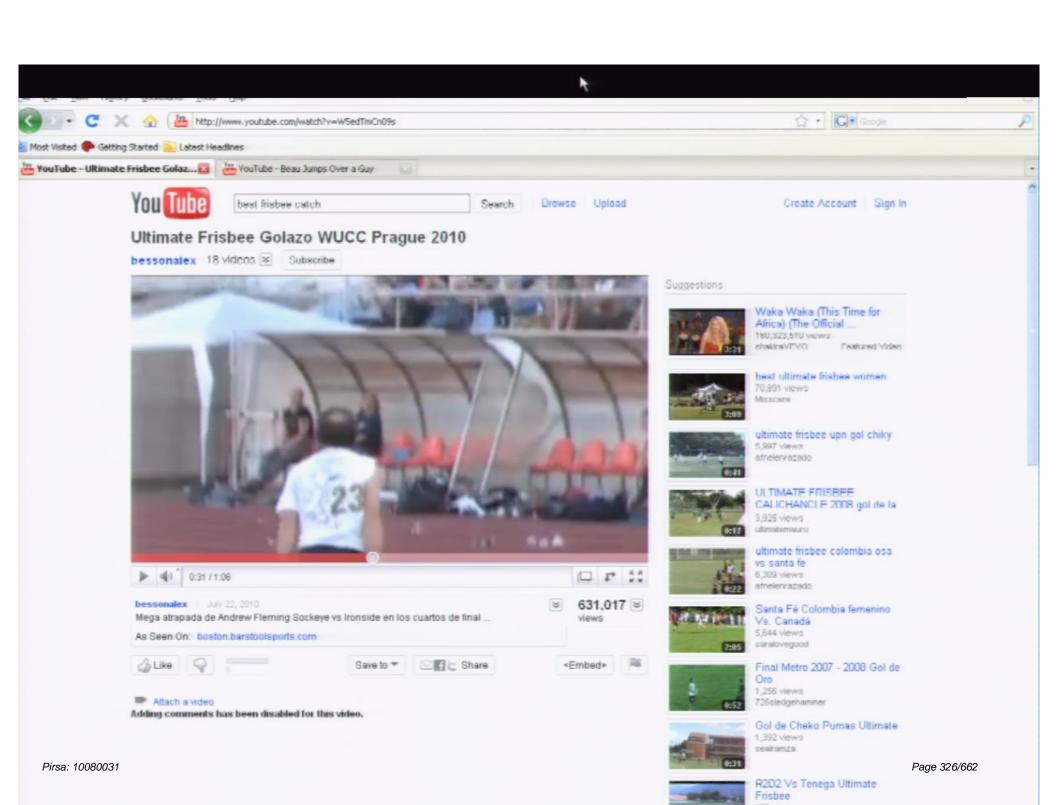


















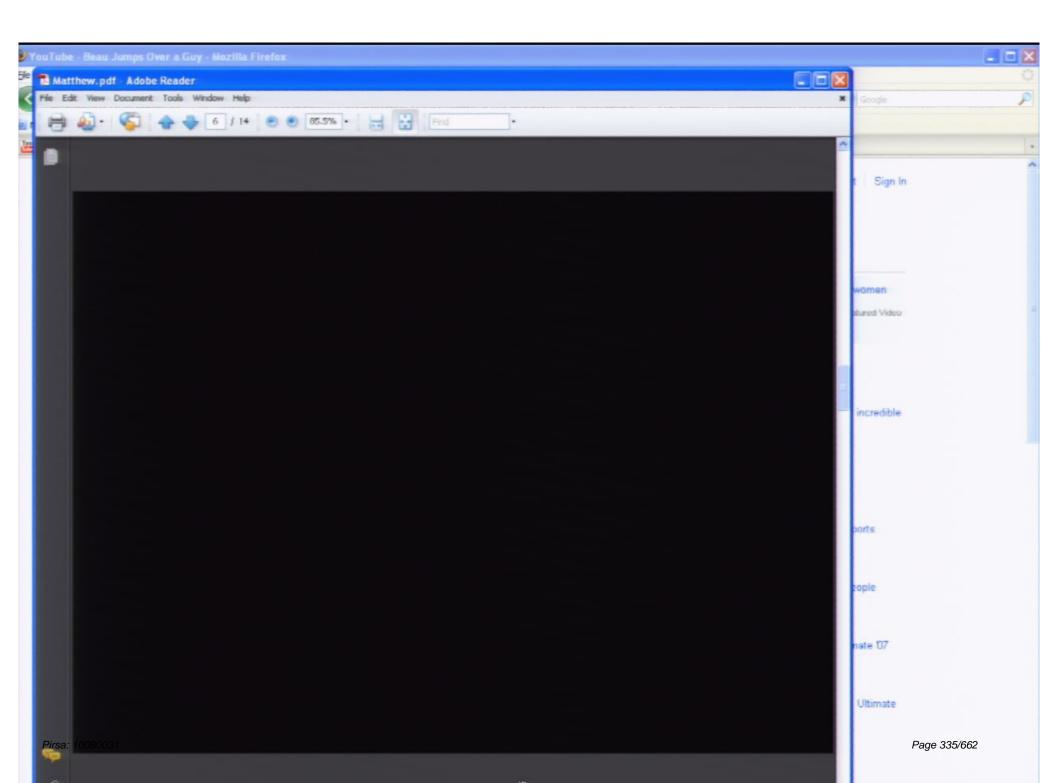












Pirsa: 10080031

Reynolds Number

$$R = \frac{\rho vd}{\eta} \approx 2.59 \cdot 10^5$$

Drag Force

$$F_D = \frac{1}{2} \rho A v^2 C_D$$

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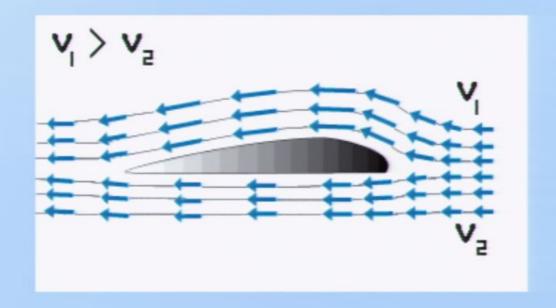
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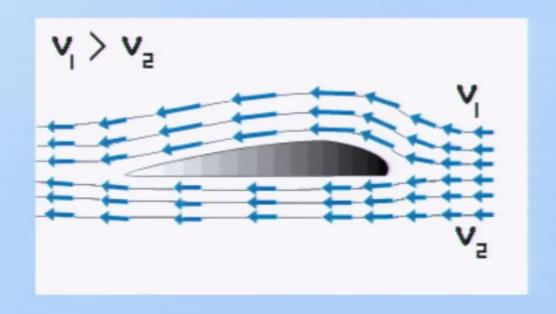
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- Air going over the frisbee moves faster than air traveling under
- So the pressure above the disc is lower than the pressure below it
- The result is a lift



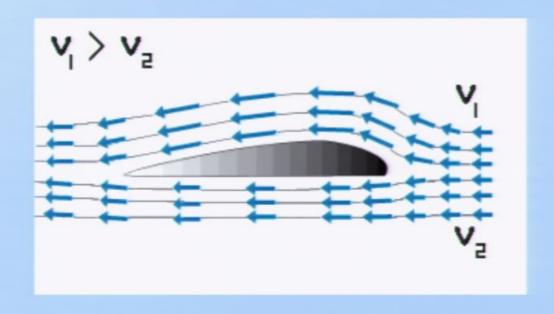
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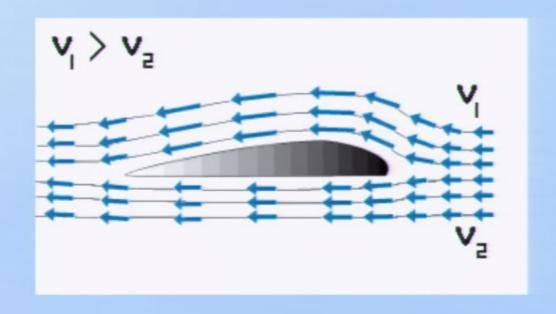
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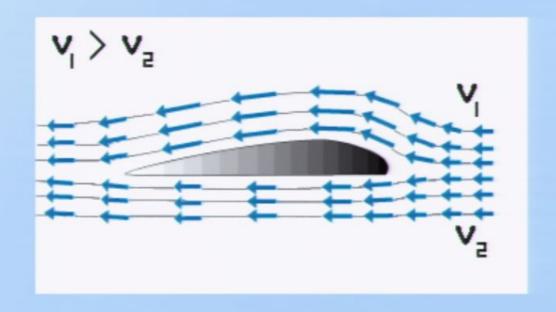
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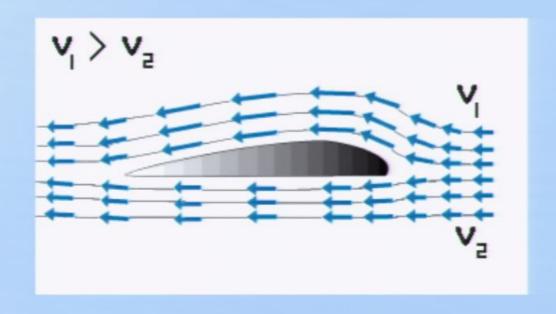
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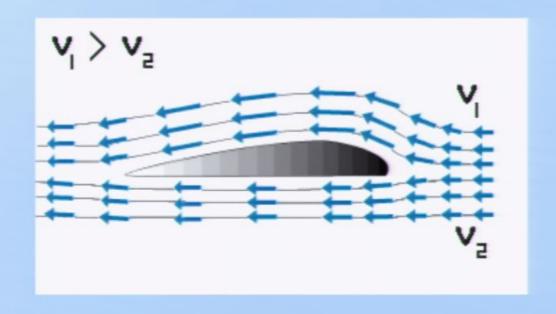
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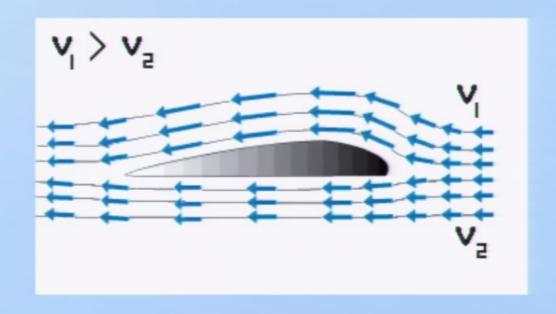
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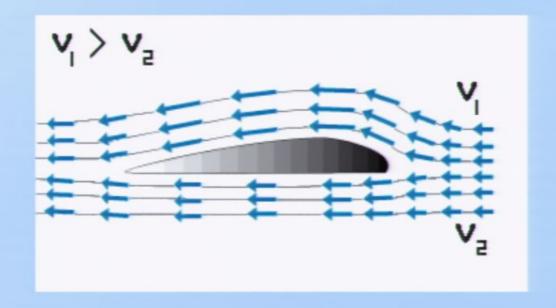
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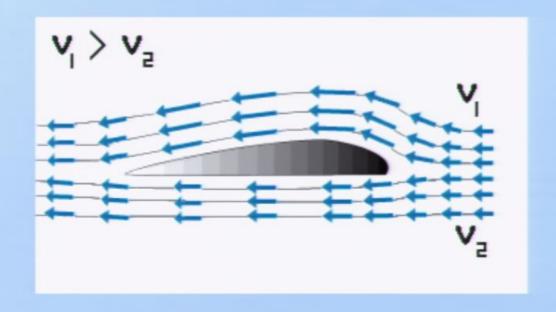
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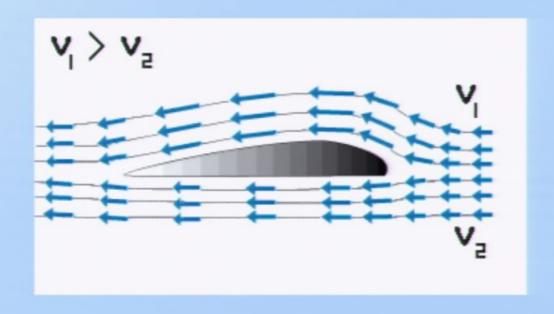
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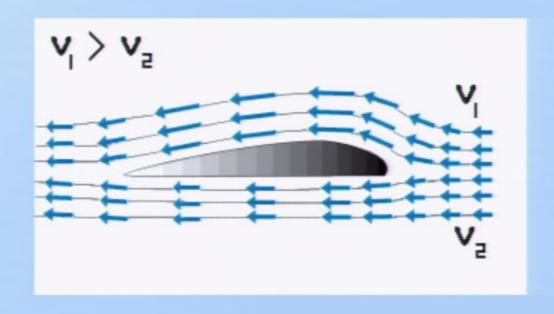
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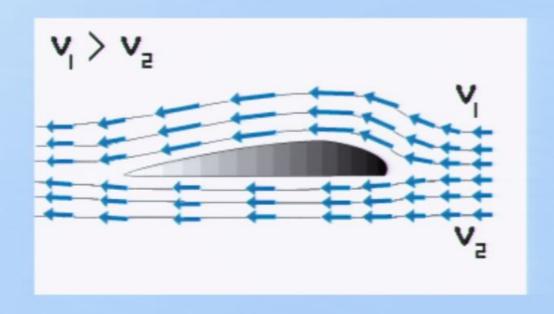
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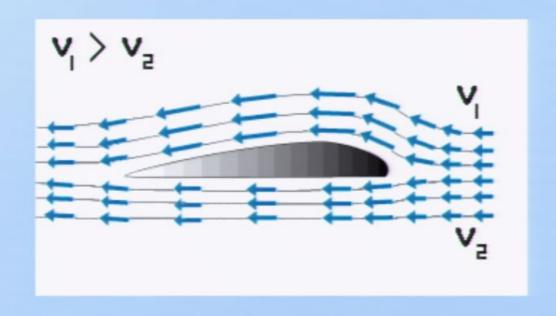
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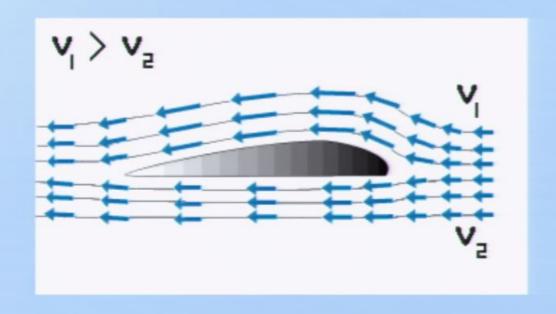
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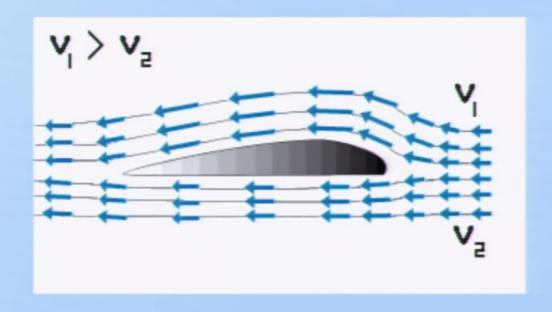
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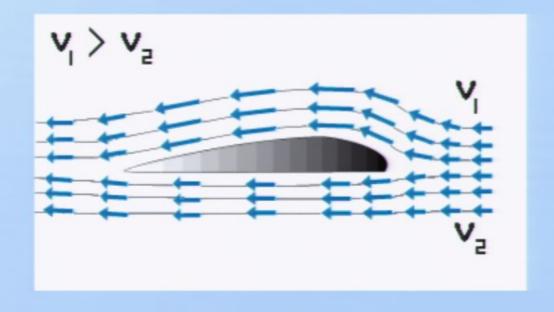
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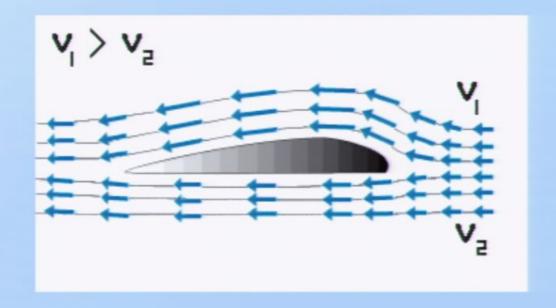
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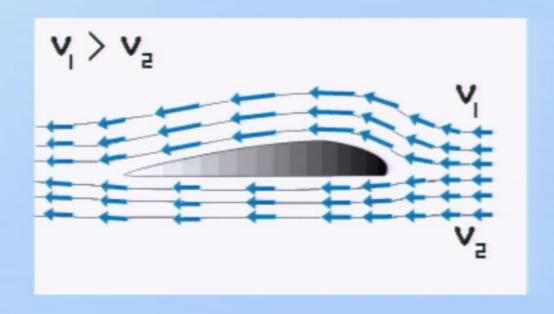
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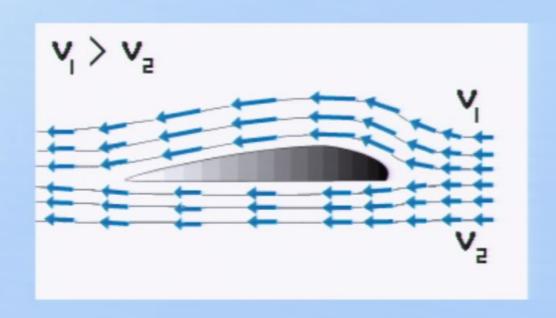
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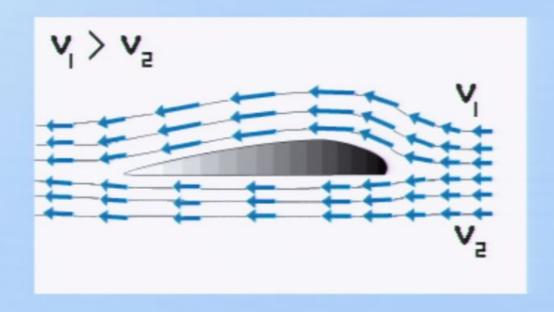
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orce upward



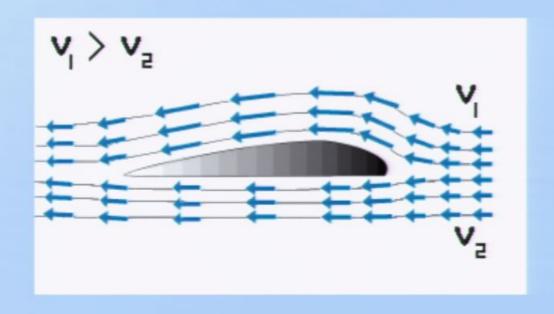
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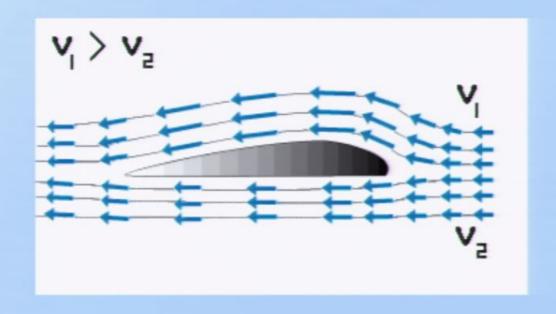
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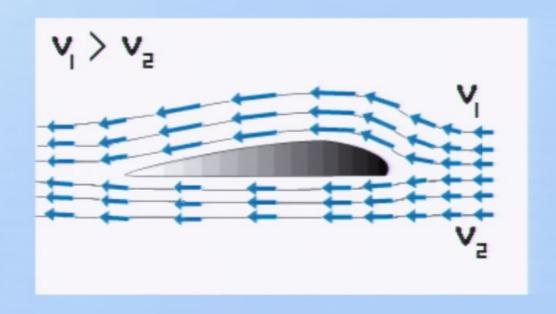
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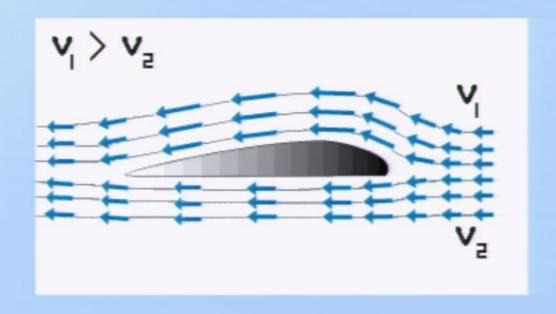
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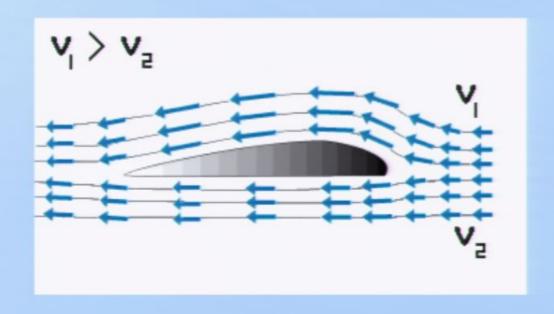
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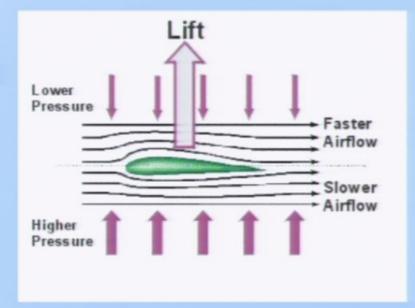


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 But why does the air above the frisbee move faster? Not trivial.

Kutta-Joukowski equation

$$F_L = \rho v \Gamma$$

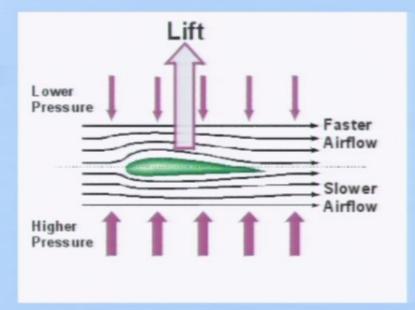


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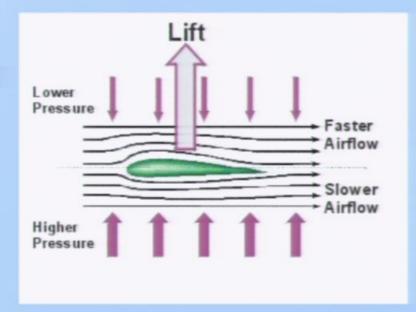


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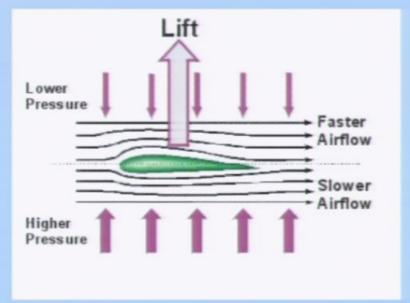
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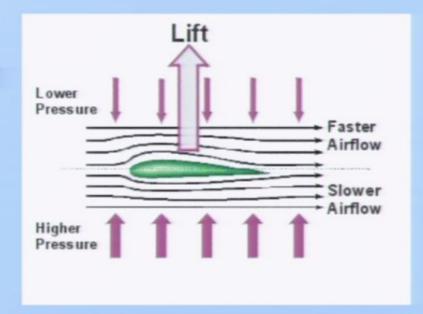


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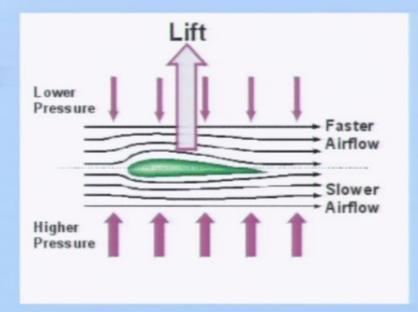


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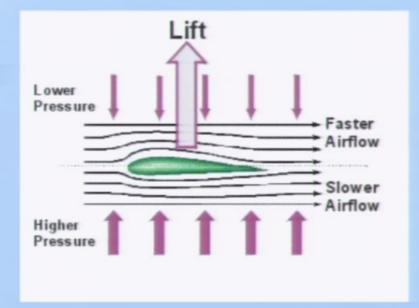
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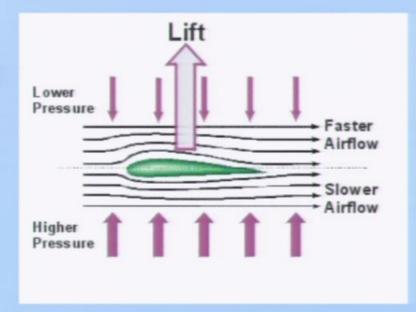


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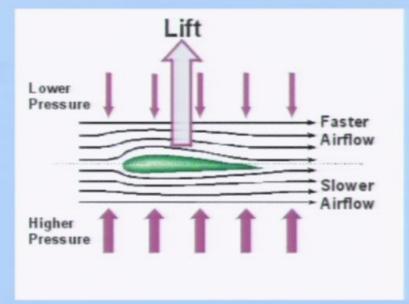


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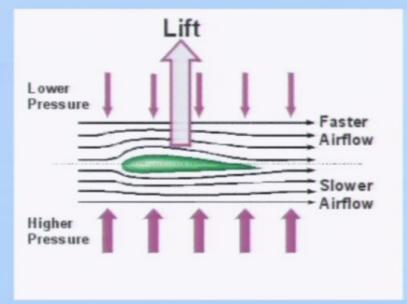
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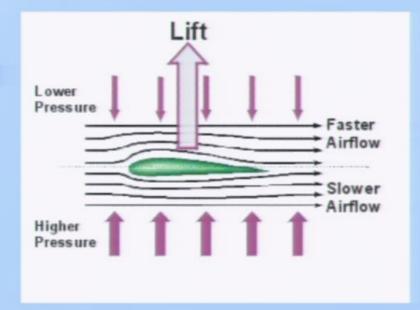
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Kutta-Joukowski equation

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• Where Γ , the circulation, is the line integral of the fluid velocity around the path of the

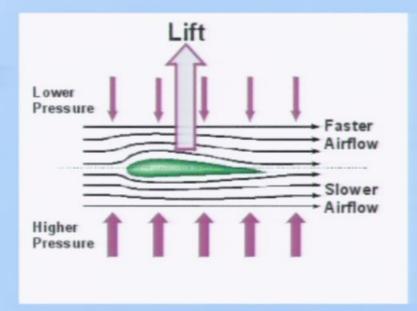
Pirsa: 10080031

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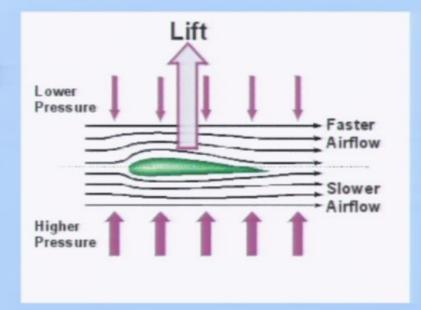


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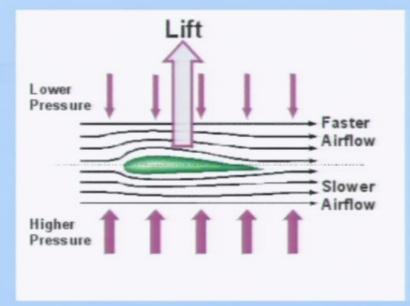
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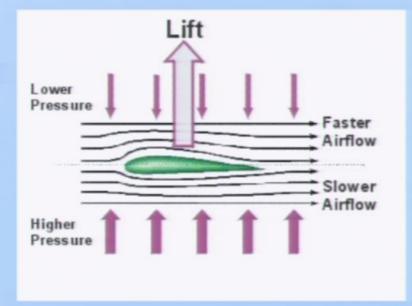
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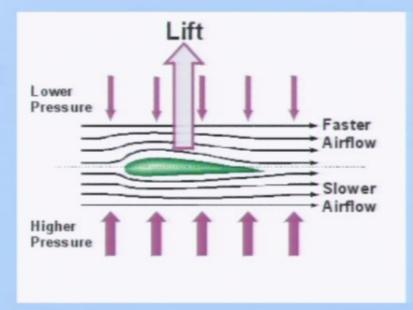


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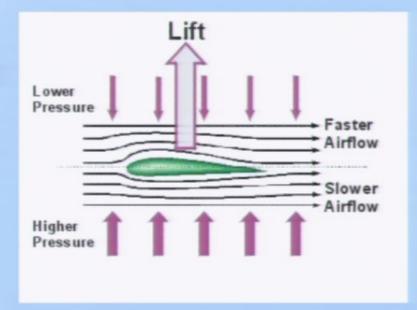


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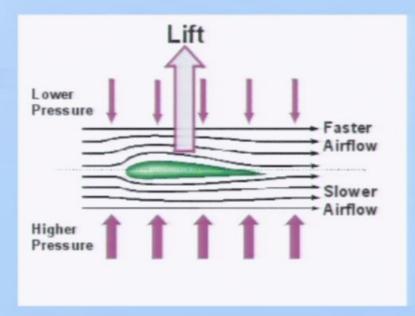


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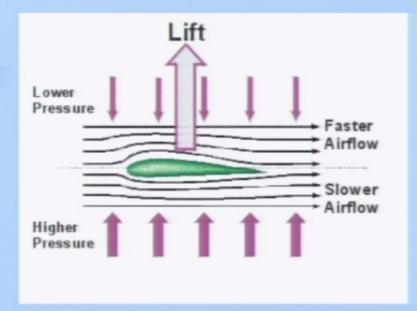


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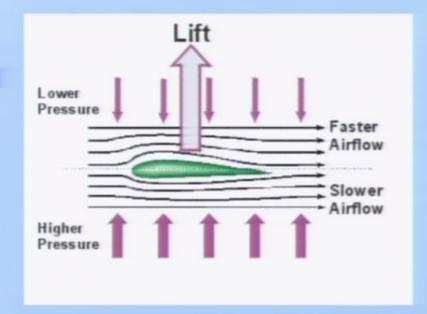


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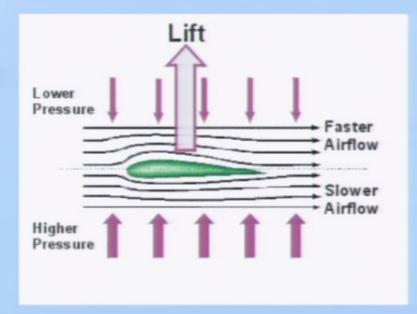


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faster? Not trivial.

Kutta-Joukowski equation

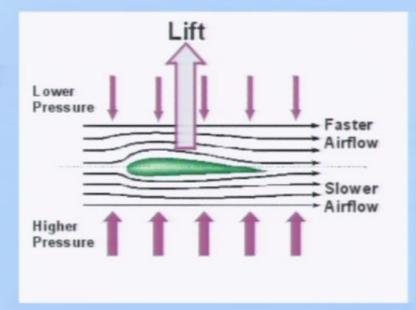
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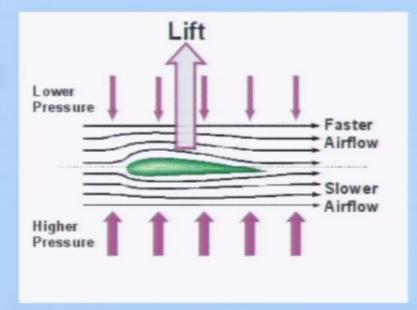


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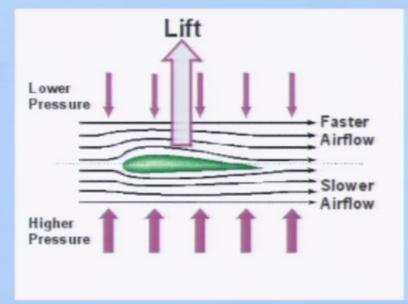
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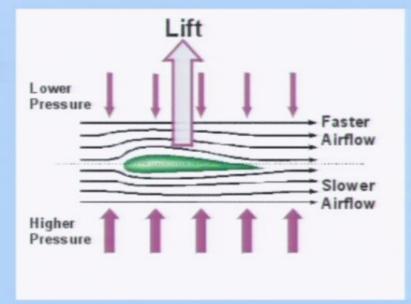
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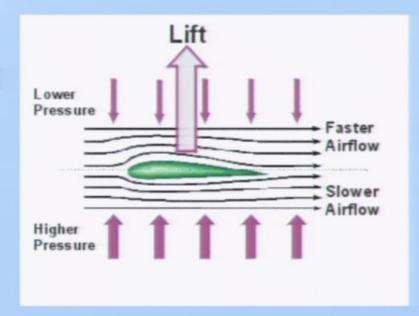


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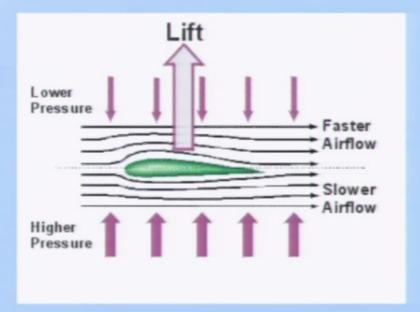


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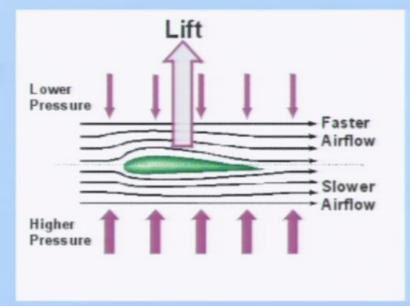
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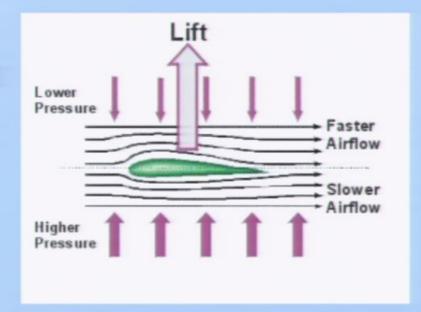


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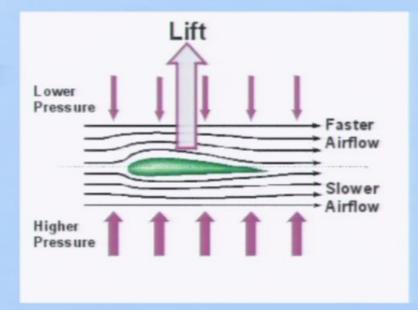
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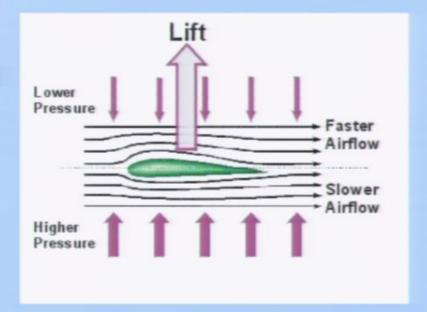
Pirsa: 10080031

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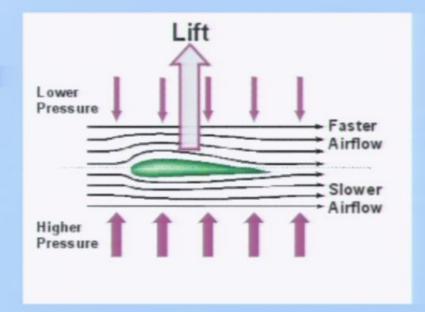


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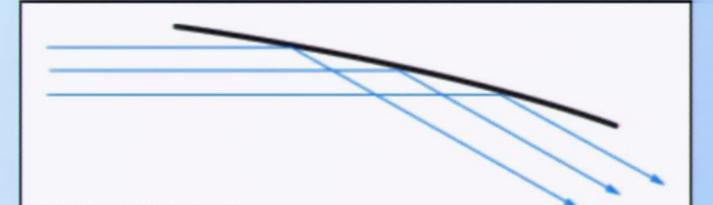
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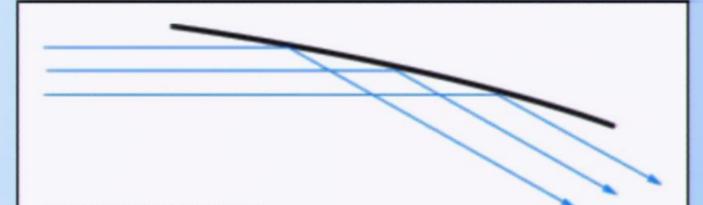
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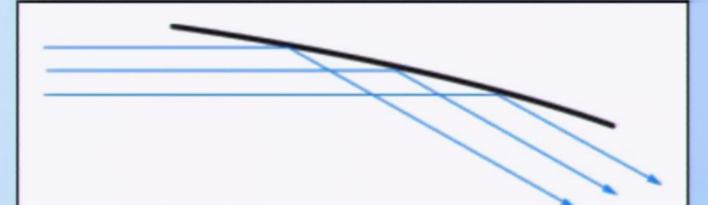
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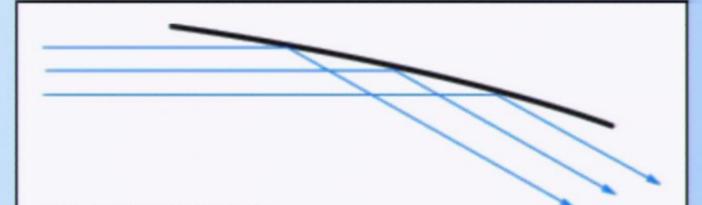
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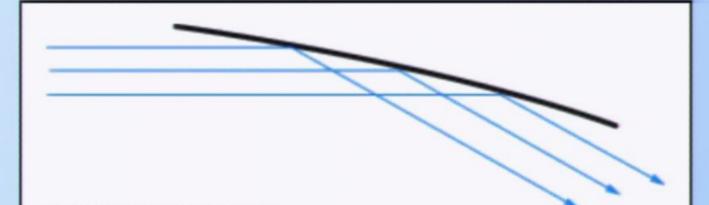
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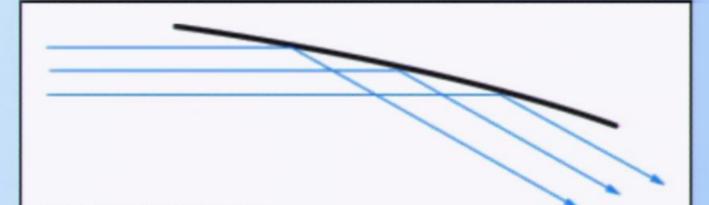
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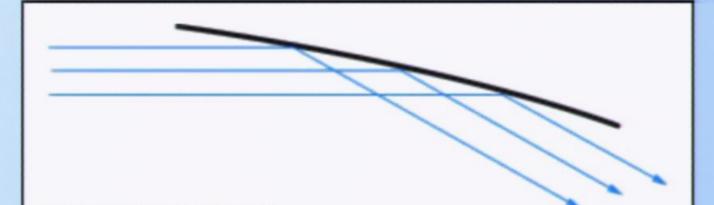
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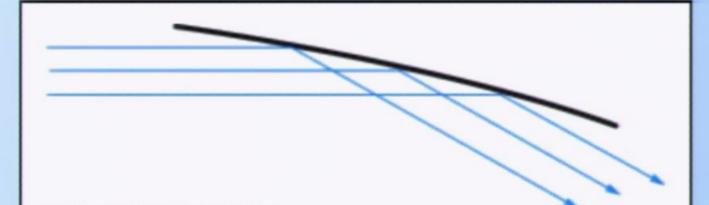
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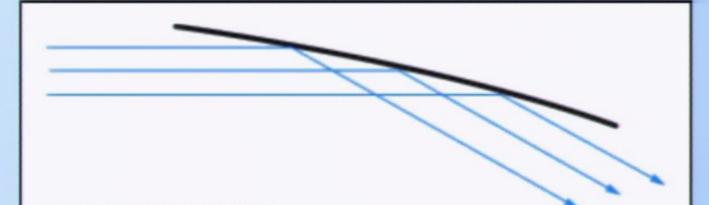
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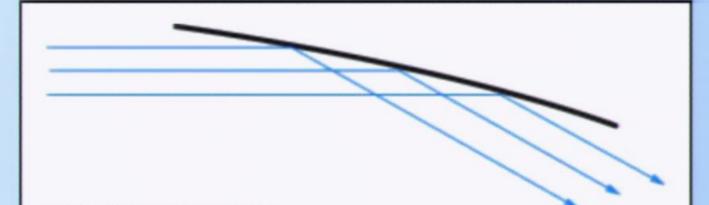
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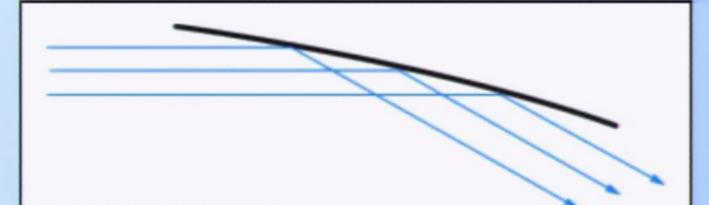
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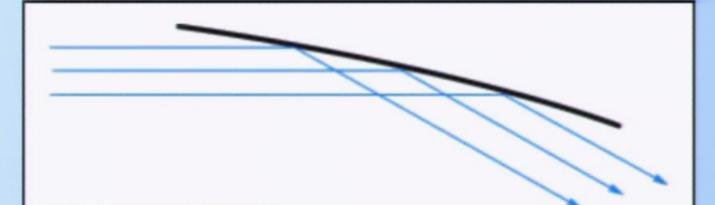
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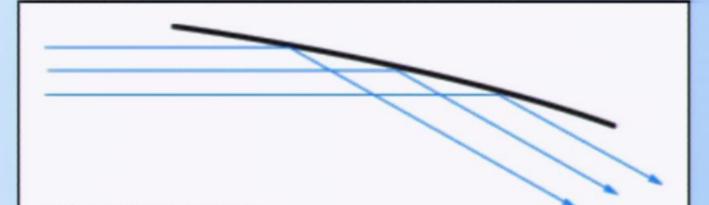
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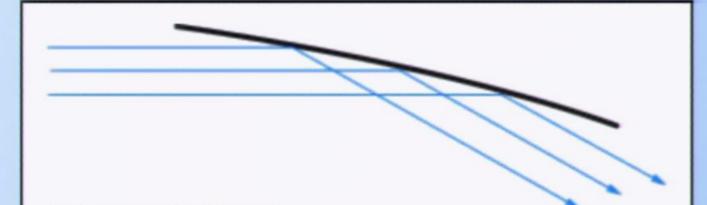
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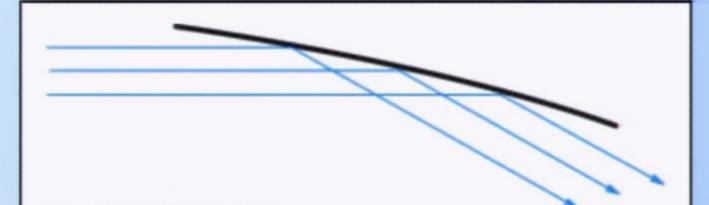
Pirsa: 10080031

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Lift: Alternative view

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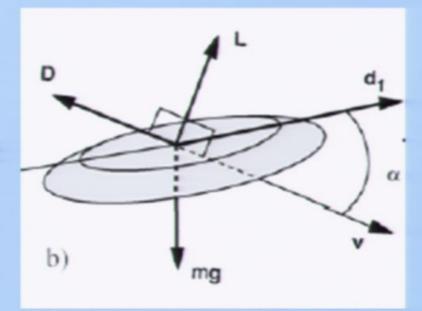


 Disc spinning clockwise, moving forward: left side moves faster than right side

 The resulting pressure difference delivers a torque tending the disc to skew from its

straight path

 Poorly thrown discs list clockwise

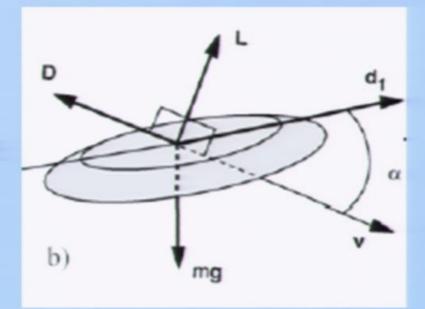


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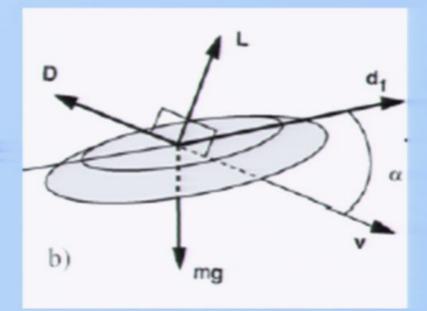


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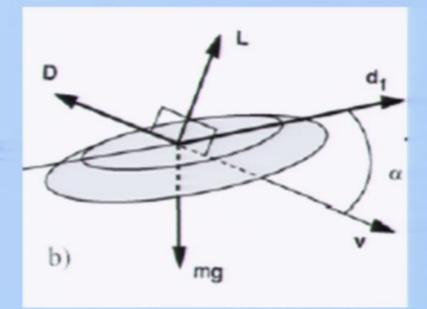


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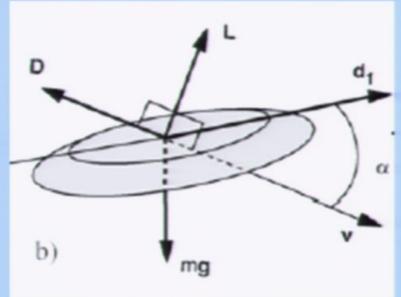


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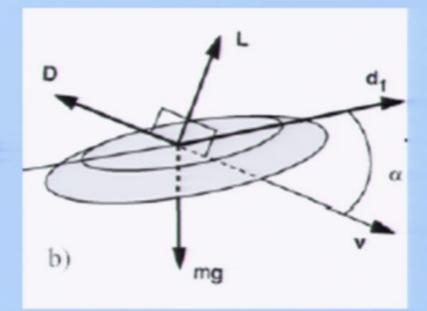


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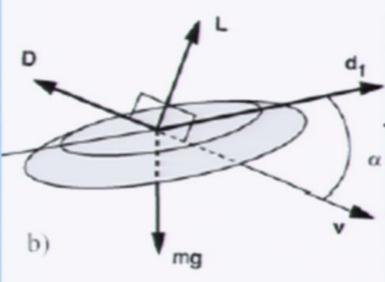


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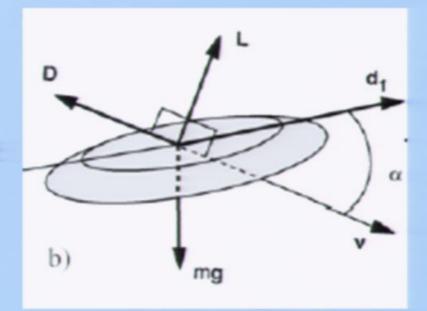


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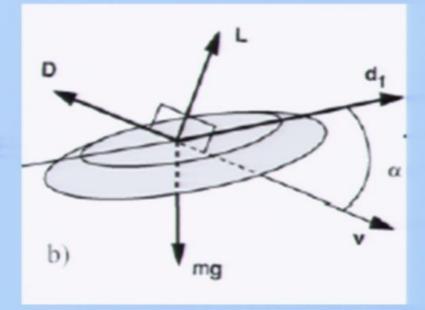


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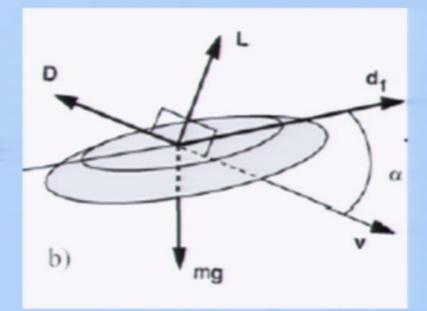


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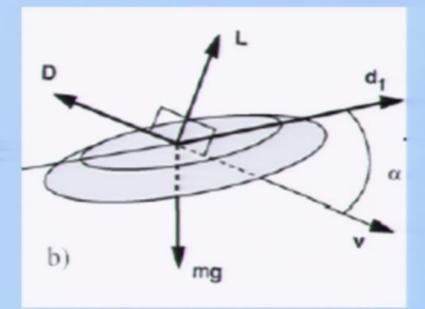


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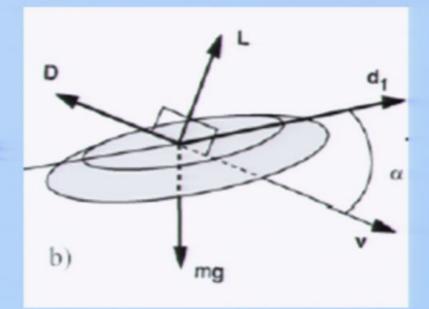


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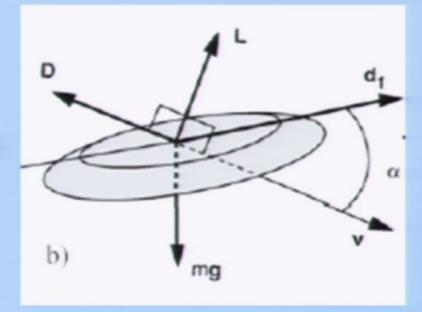


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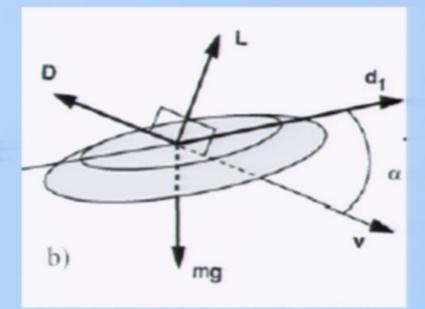


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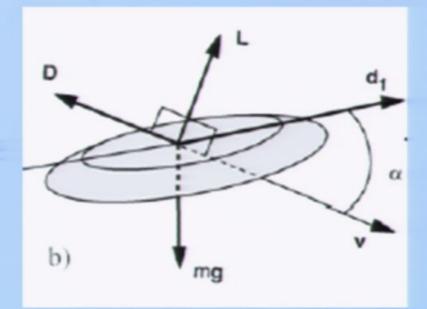


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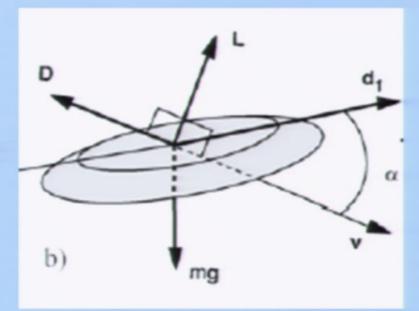


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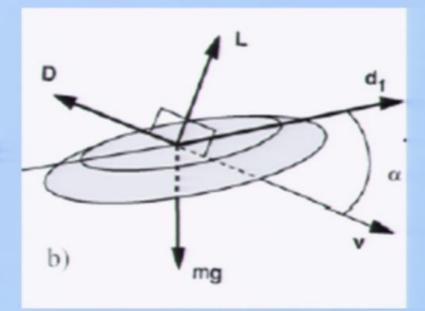


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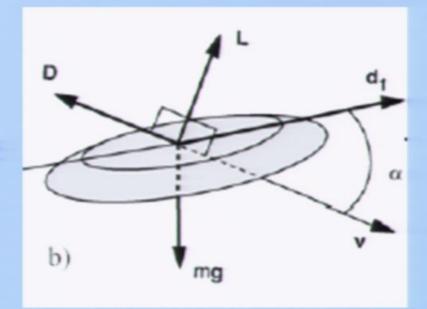


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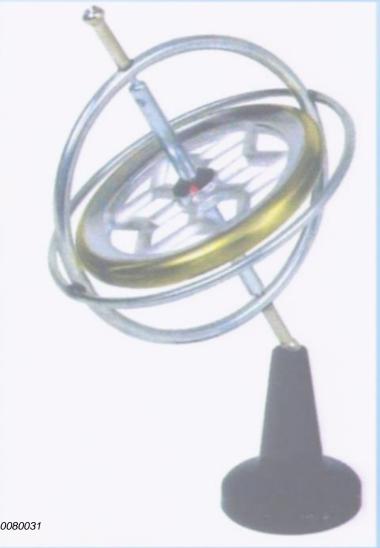
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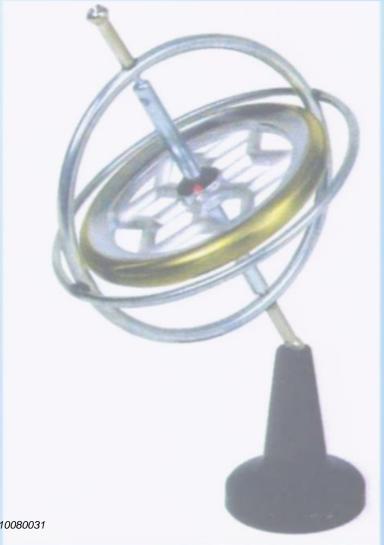


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- Gyroscopic inertia combats the tendency to skew to the side
- Greater spin = more stable flight

Pirsa: 10080031

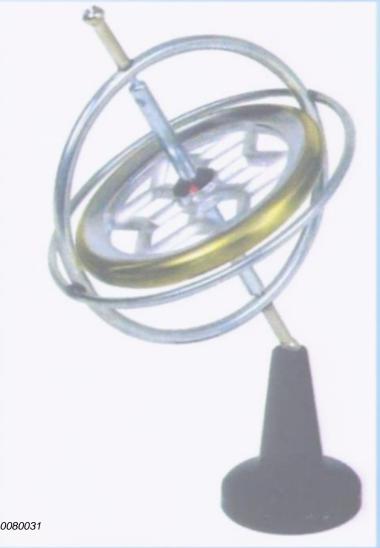


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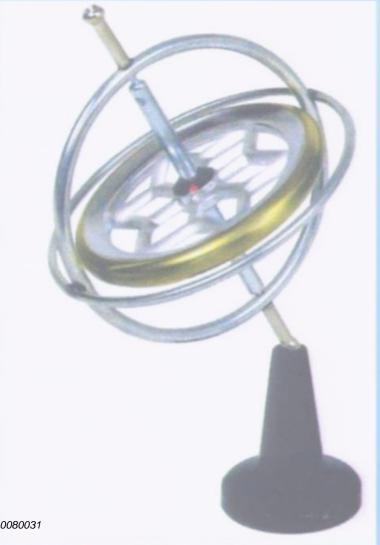
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Pirsa: 10080031

- A frisbee flies like a plane's wing
- But frisbees rely on gyroscopic precession for stable flight
- Distance flown depends most on initial velocity, angle of attack, and angular momentum.

Pirsa: 10080031 Page 462/662

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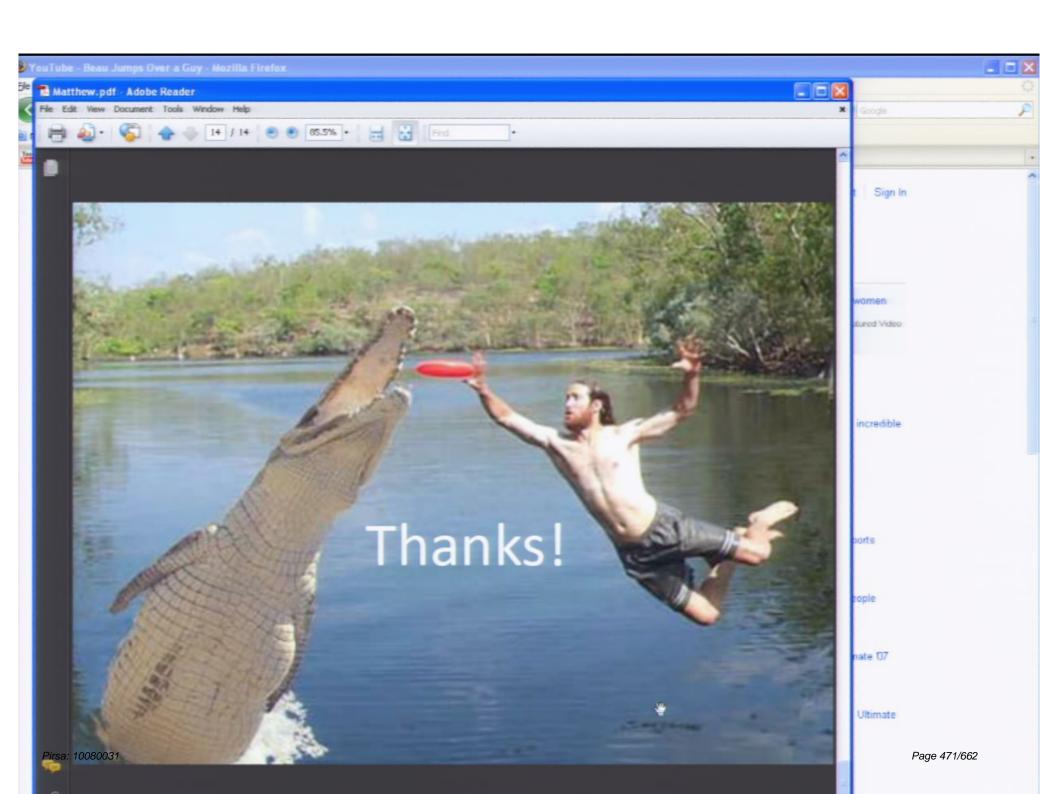
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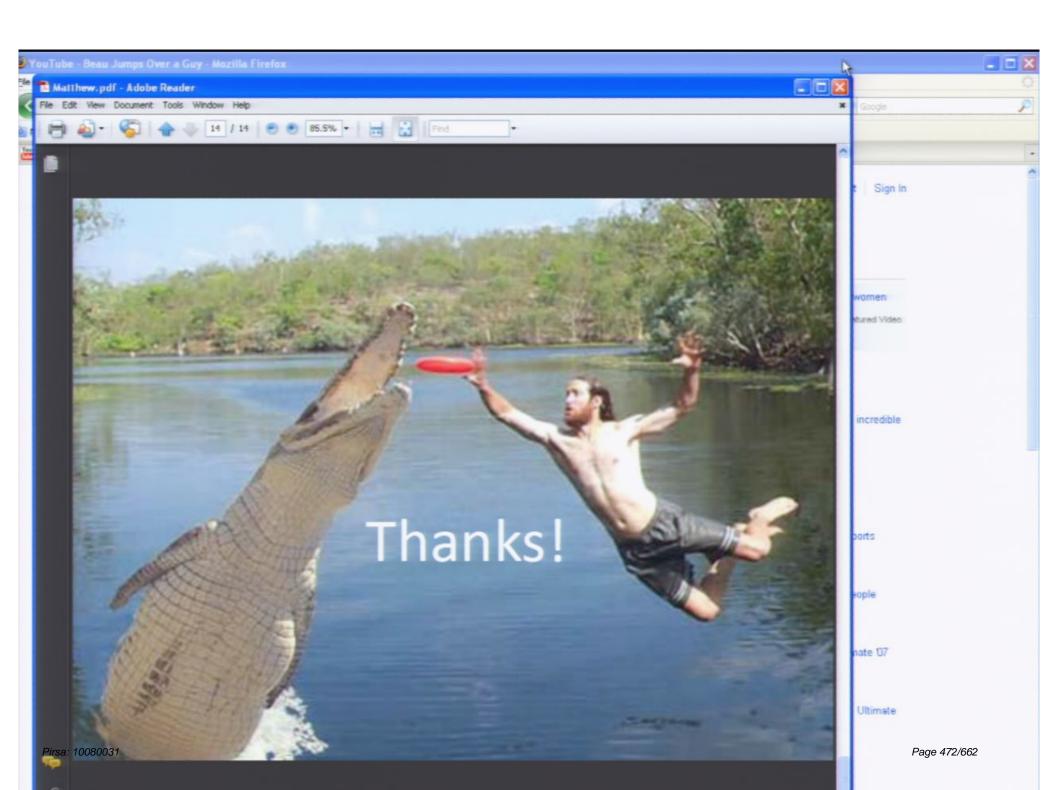
Conclusions

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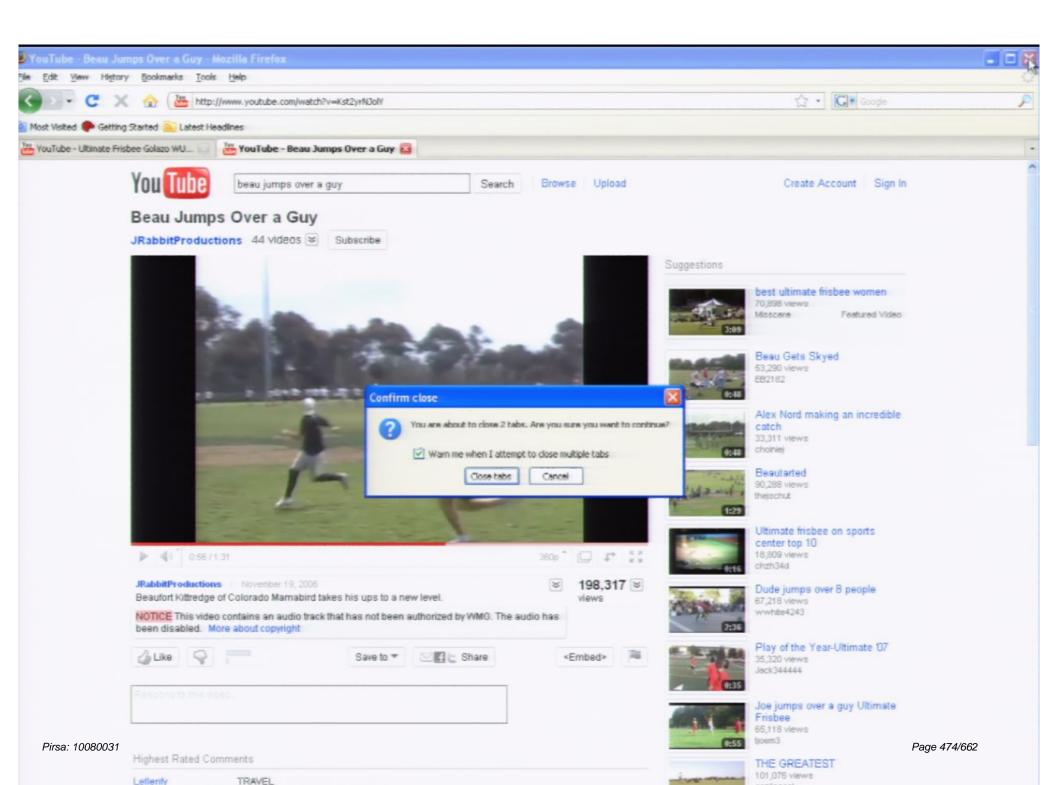
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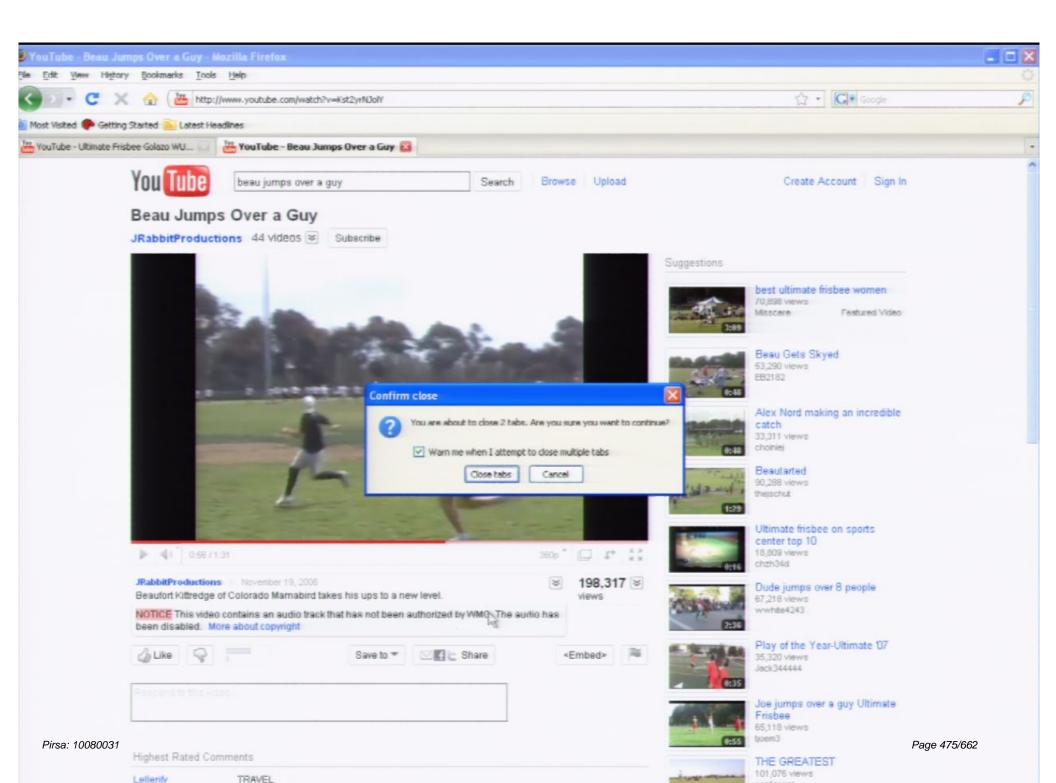


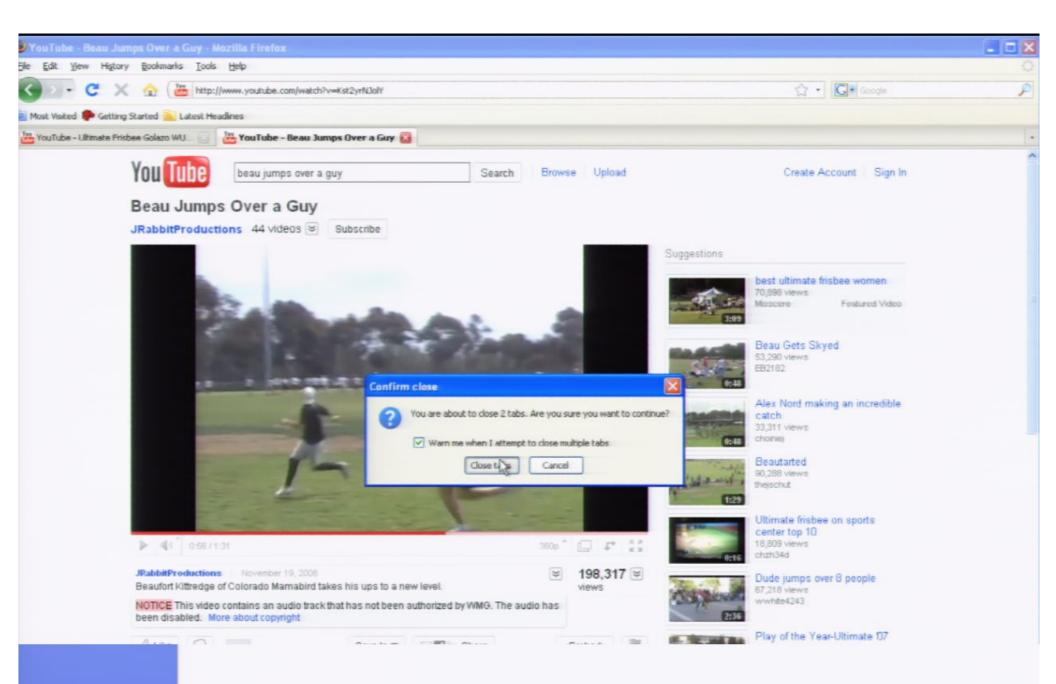












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Clouds?

Laura Piispanen

Theoretical physics University of Turku

August 20, 2010



Clouds?

Laura Piispanen

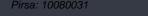
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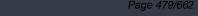
August 20, 2010



Contents

- Motivation
- Clouds?
- Why do they look that way?
- Clouds on other planets







A cloud is made of billows upon billows upon billows that look like clouds. As you come closer to a cloud you don't get something smooth, but irregularities at a smaller scale.

Benoit Mandelbrot



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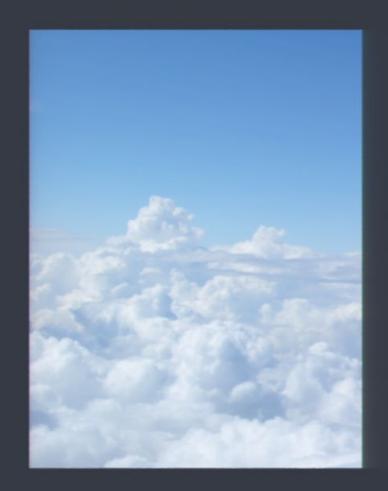
Benoit Mandelbrot







Huge white things on the sky

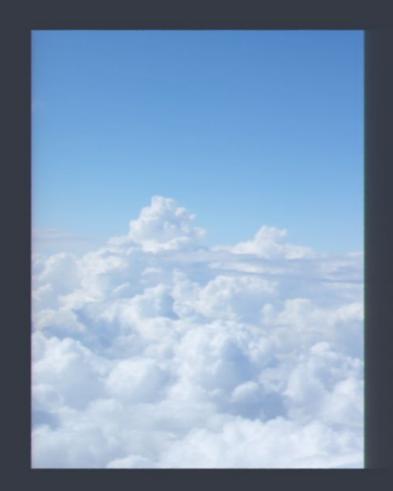








- Huge white things on the sky
- Can also appear as greyish

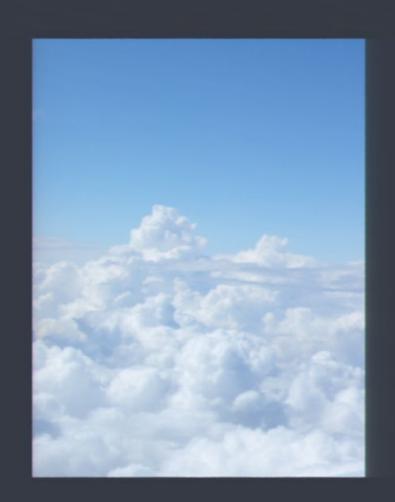


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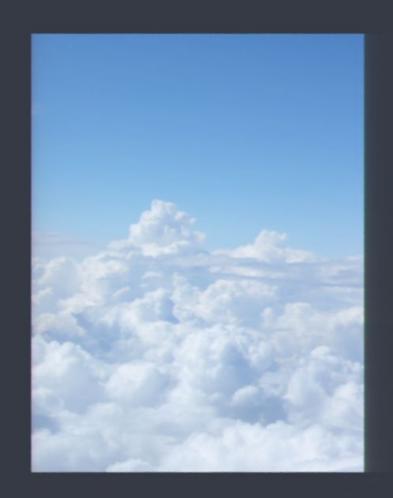


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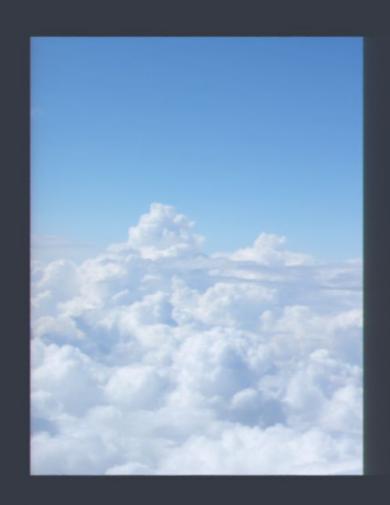


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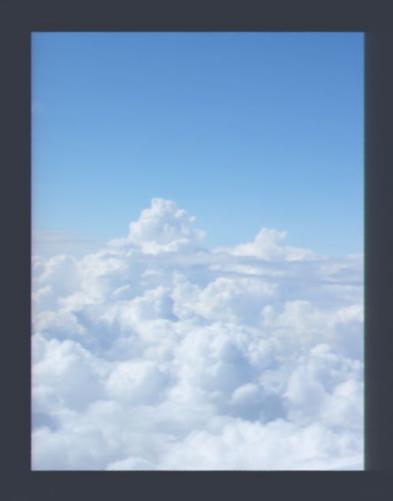
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 - small crystals of ice



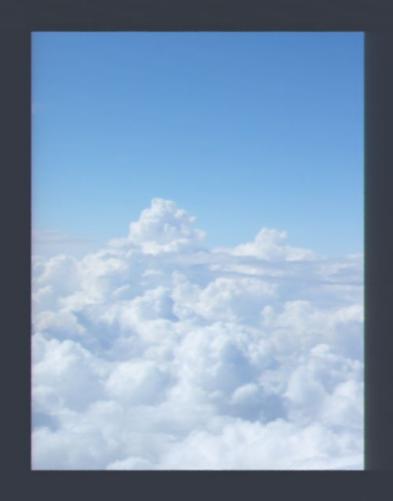




- Huge white things on the sky
- Can also appear as greyish
- Consist of a vast collection of
 - tiny droplets of liquid water
 - ("warm clouds")
 - small crystals of ice



- Huge white things on the sky
- Can also appear as greyish
- Consist of a vast collection of
 - tiny droplets of liquid water
 - ("warm clouds")
 - small crystals of ice
 - ("cold clouds")









sun warms water









- sun warms water
- water vaporizes into the air







- sun warms water
- water vaporizes into the air
- sun warms the humid air





- sun warms water
- water vaporizes into the air
- sun warms the humid air
- warm, humid air is lighter than cold air



Pirsa: 10080031

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- sun warms water
- water vaporizes into the air
- sun warms the humid air
- warm, humid air is lighter than cold air
- warm, humid air rises high and spreads

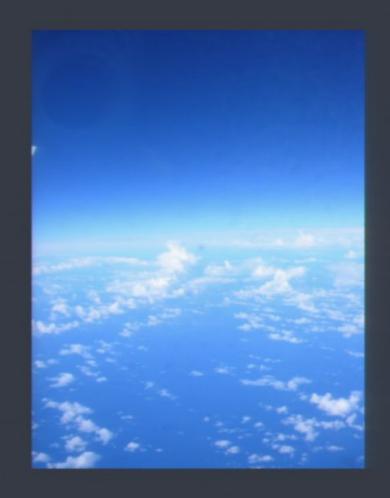


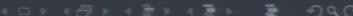
- sun warms water
- water vaporizes into the air
- sun warms the humid air
- warm, humid air is lighter than cold air
- warm, humid air rises high and spreads
- air cools and the vaporized water forms into dropplets



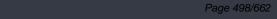


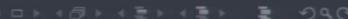
- sun warms water
- water vaporizes into the air
- sun warms the humid air
- warm, humid air is lighter than cold air
- warm, humid air rises high and spreads
- air cools and the vaporized water forms into dropplets
- we have a cloud!











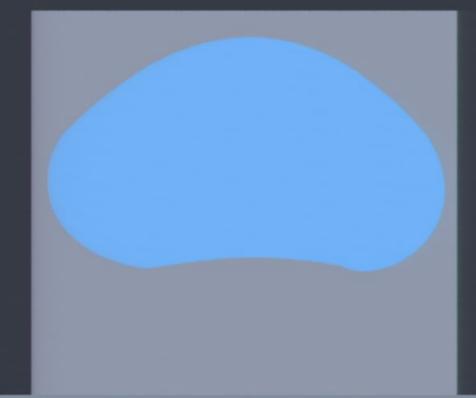
- They actually do
- Airflow that creates clouds, same time pushes them up

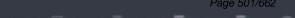
ㅁ > + 리 > + 분 > + 분 > 9 약 연

- They actually do
- Airflow that creates clouds, same time pushes them up
- This causes the waterdroplets to be this shape:



- They actually do
- Airflow that creates clouds, same time pushes them up
- This causes the waterdroplets to be this shape:





Why do clouds appear in different shapes?

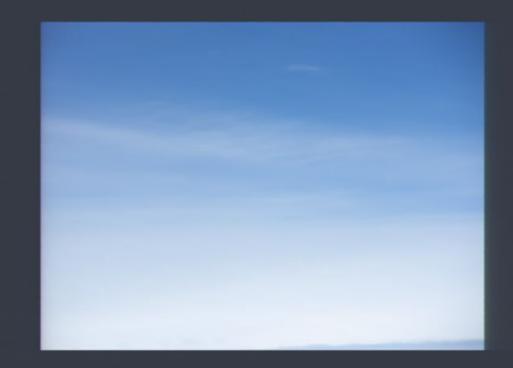




 Different kind of particles and temperature



- Different kind of particles and temperature
 - icy clouds appear tenuous

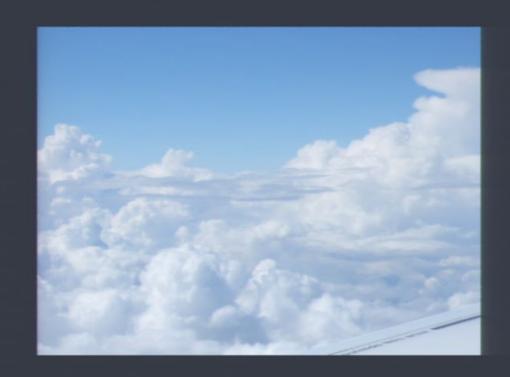






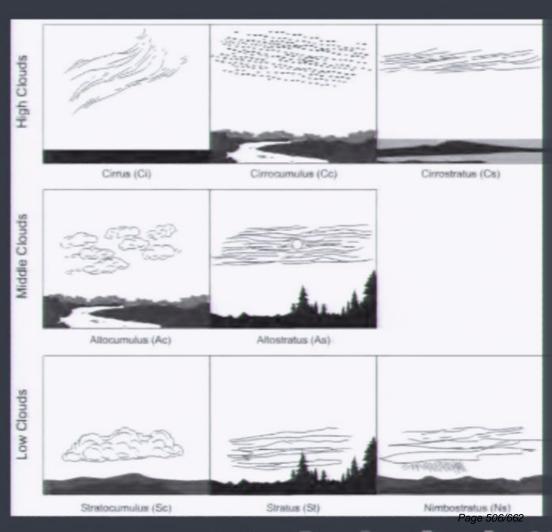


- Different kind of particles and temperature
 - icy clouds appear tenuous
 - warm clouds are softer-looking



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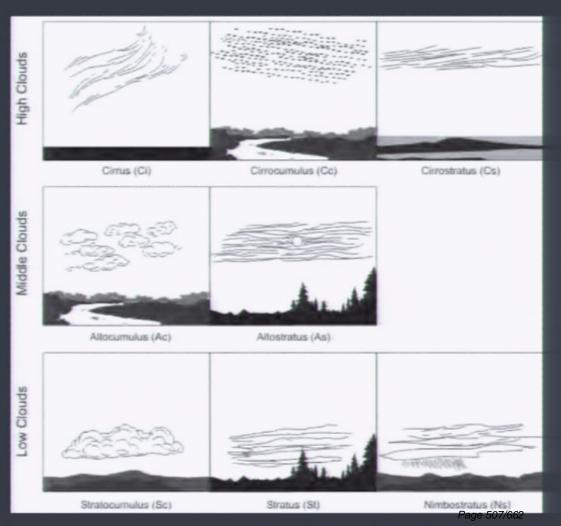
- Different kind of particles and temperature
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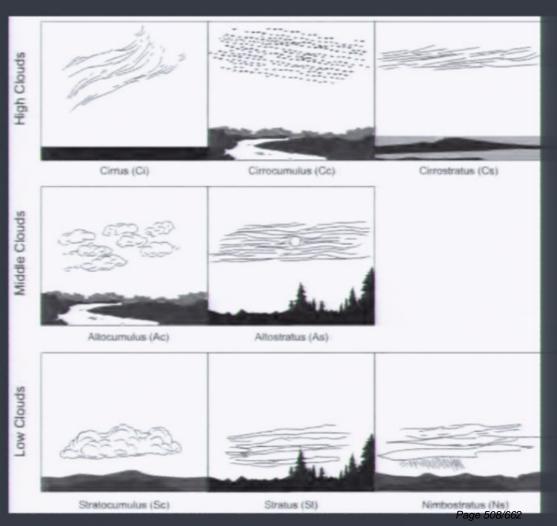
- Different kind of particles and temperature
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Pirea: 10080031



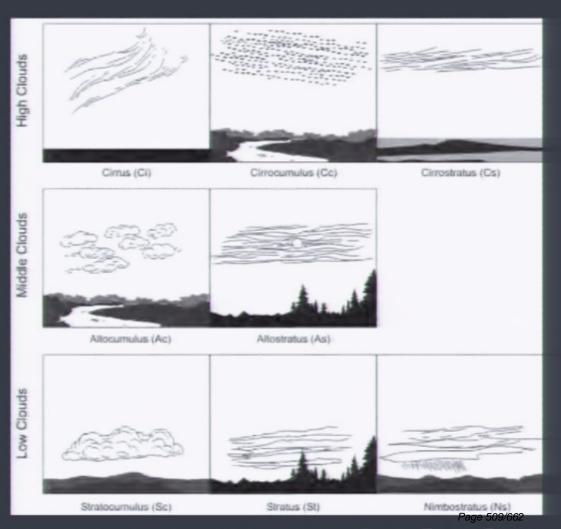
- Different kind of particles and temperature
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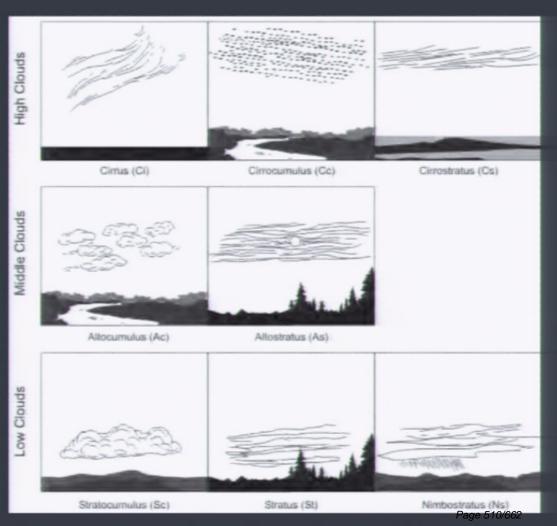
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Direa: 10080031



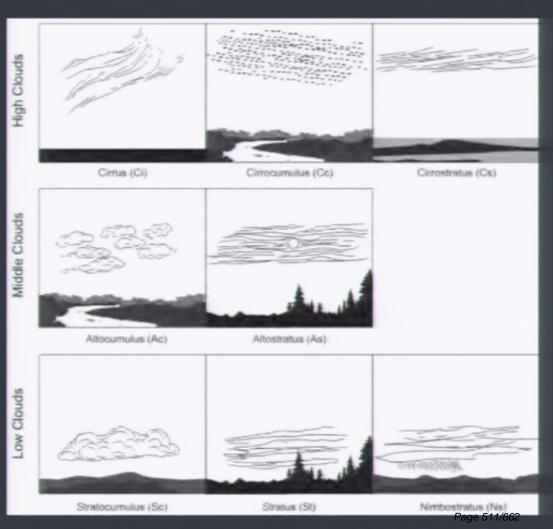
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Pirea: 10080031



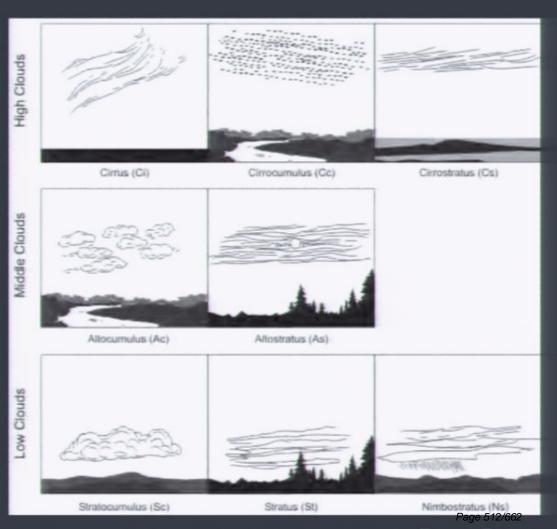
- Different kind of particles and temperature
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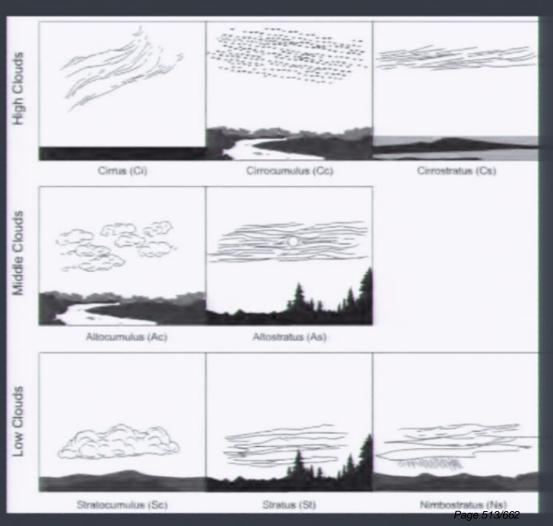
- Different kind of particles and temperature
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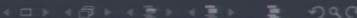




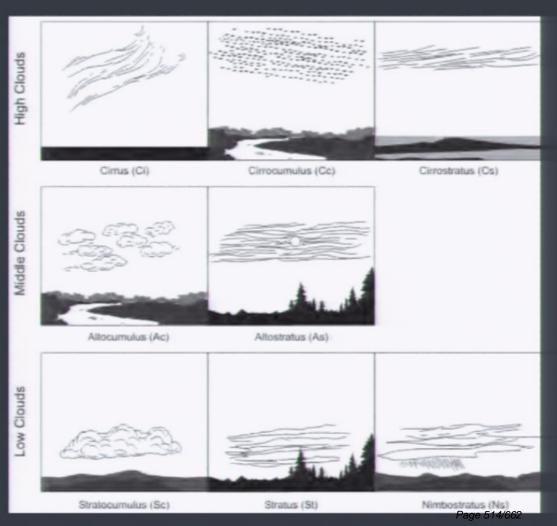
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Pirea: 10080031



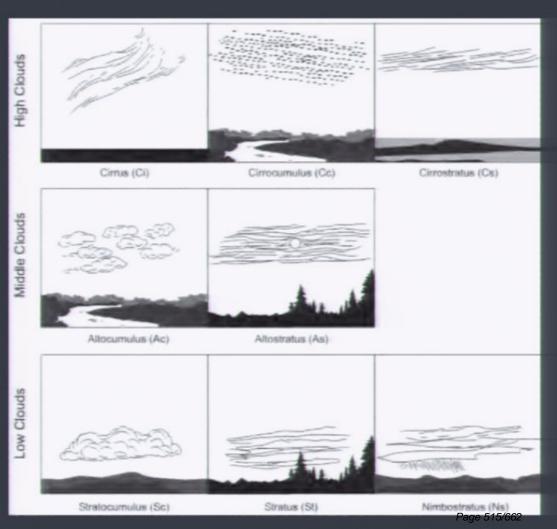
- Different kind of particles and temperature
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Pirsa: 10080031



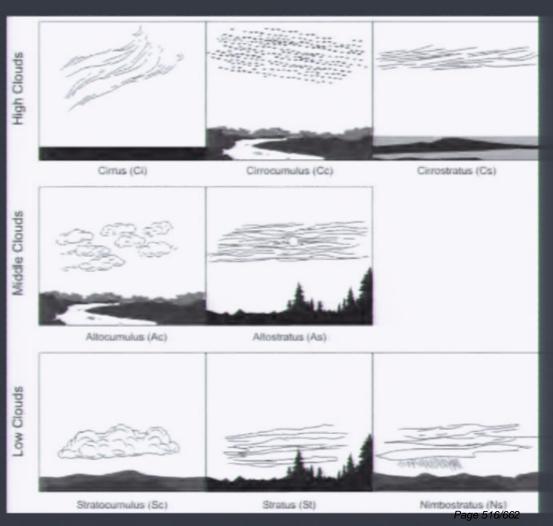
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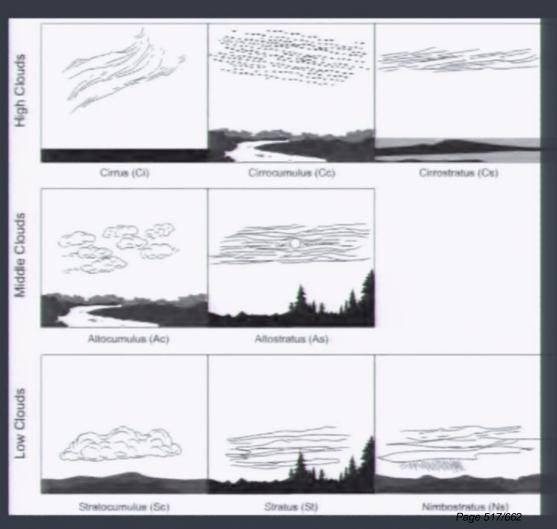
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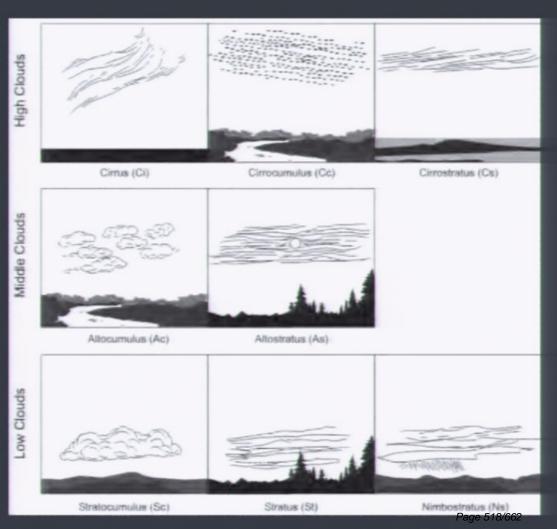
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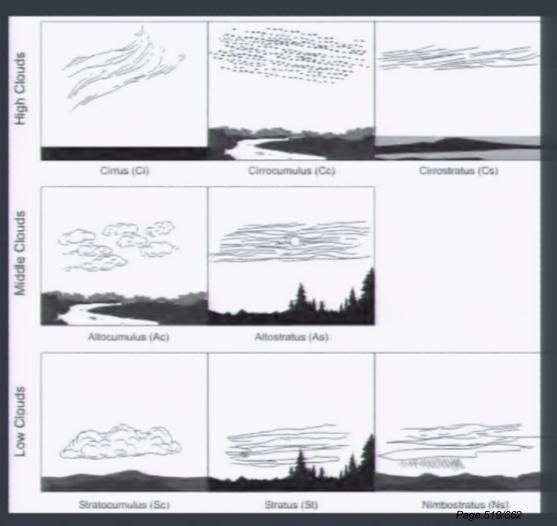
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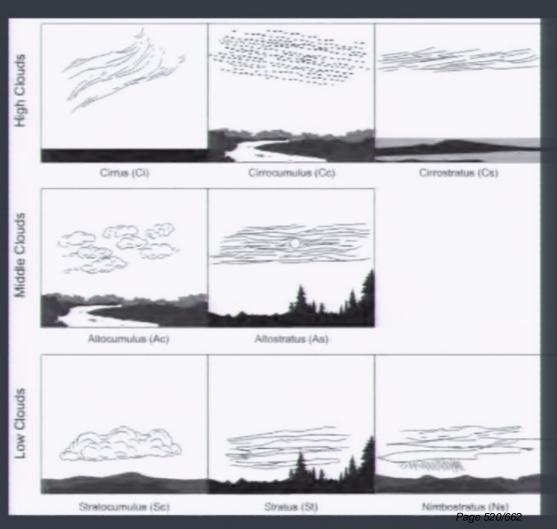
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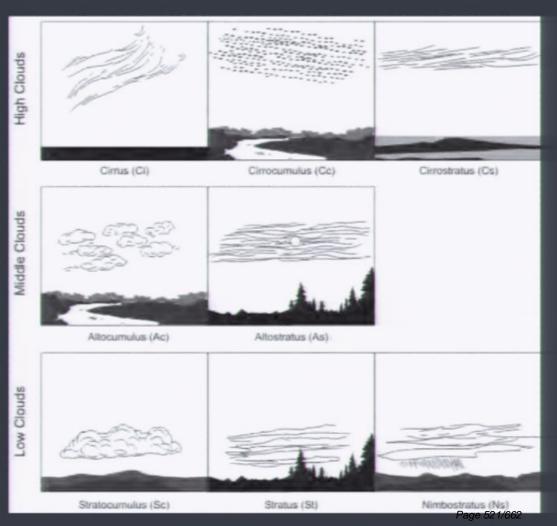
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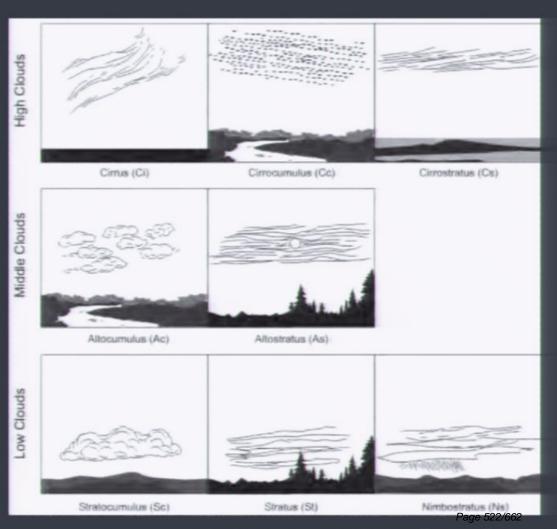


- Different kind of particles and temperature
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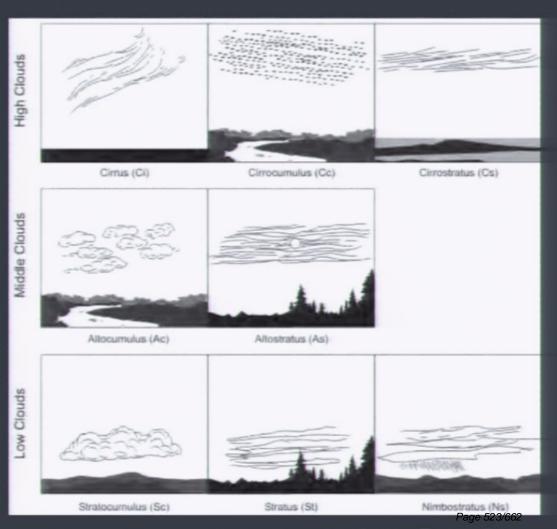
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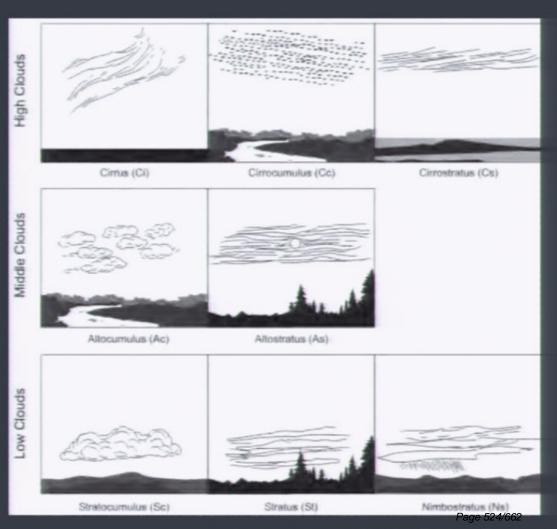


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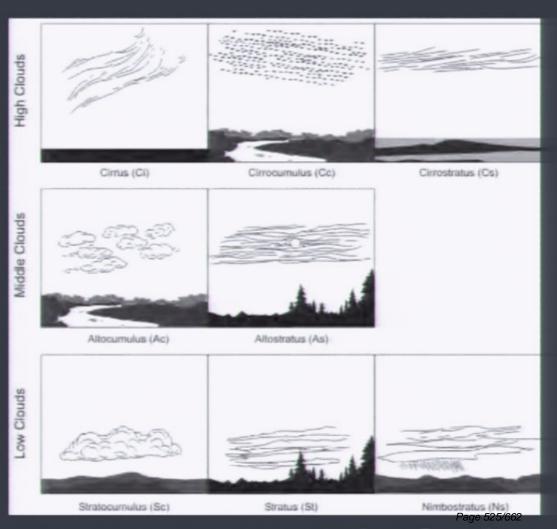
- Different kind of particles and temperature
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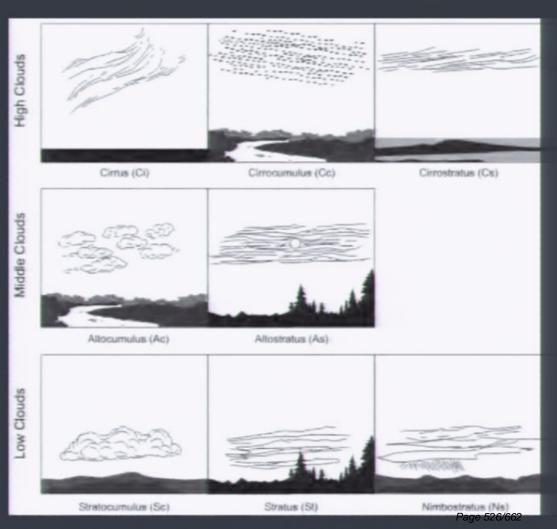
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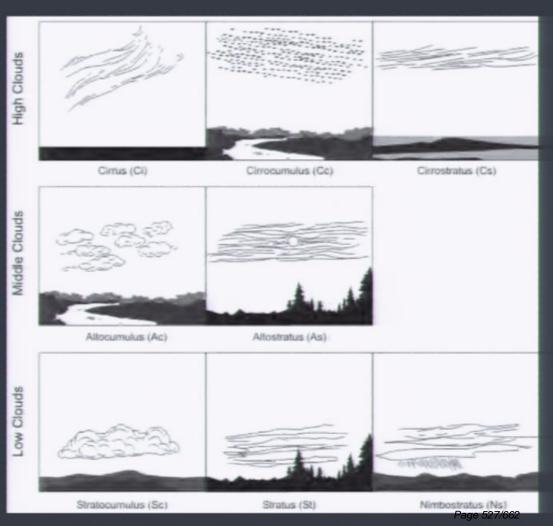
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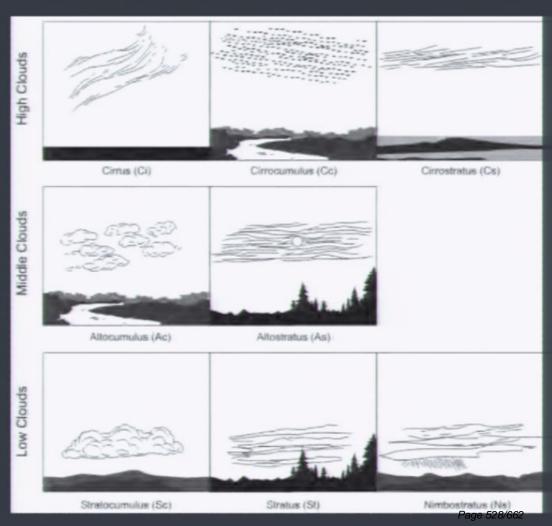
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Pires: 10080031



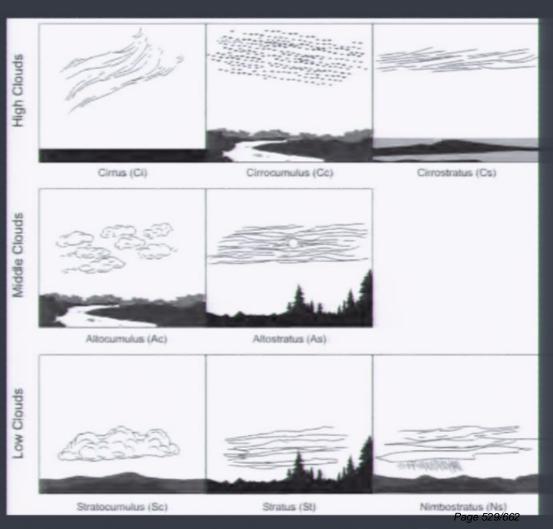
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Pires: 10080031



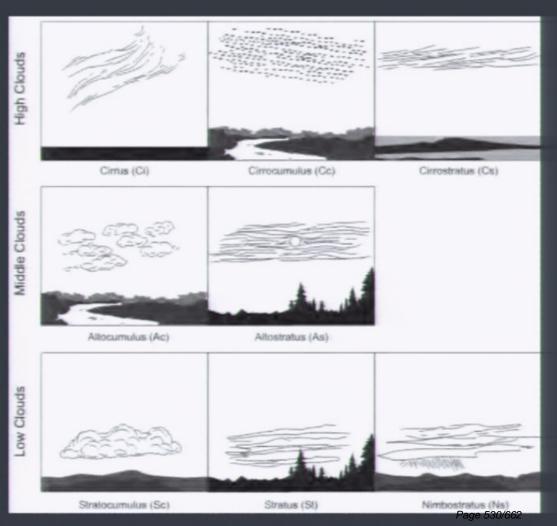
- Different kind of particles and temperature
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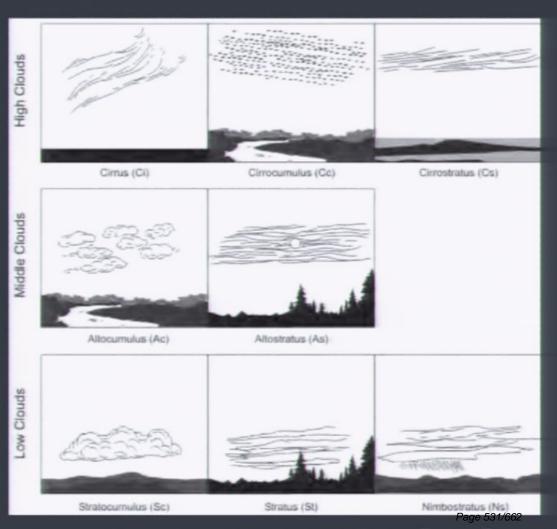
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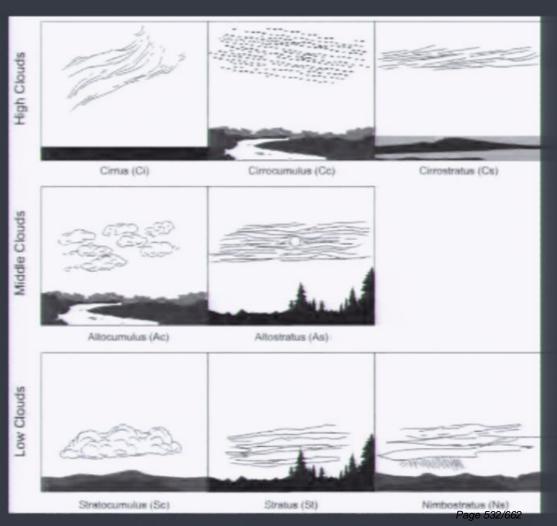
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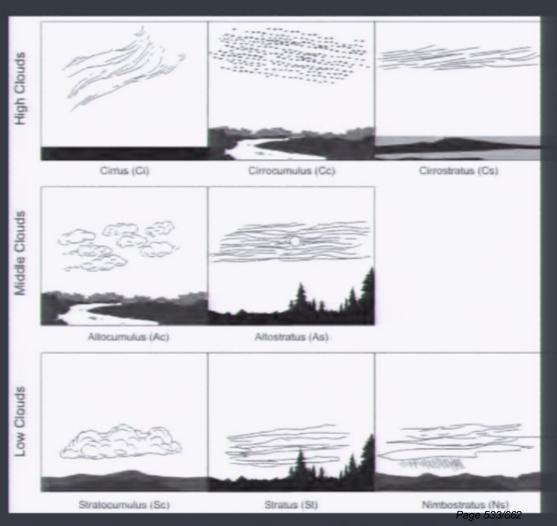
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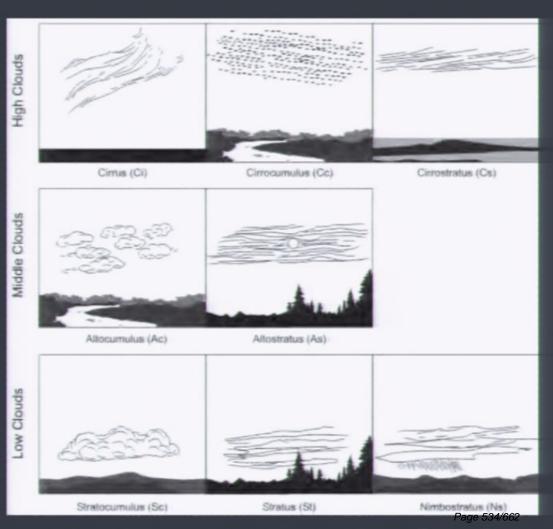


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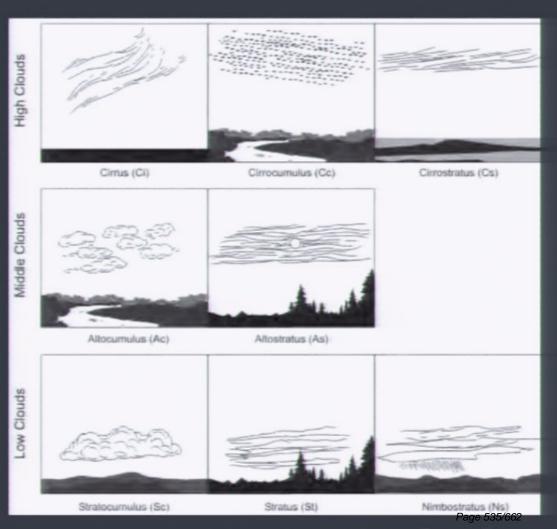
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Pirsa: 10080031

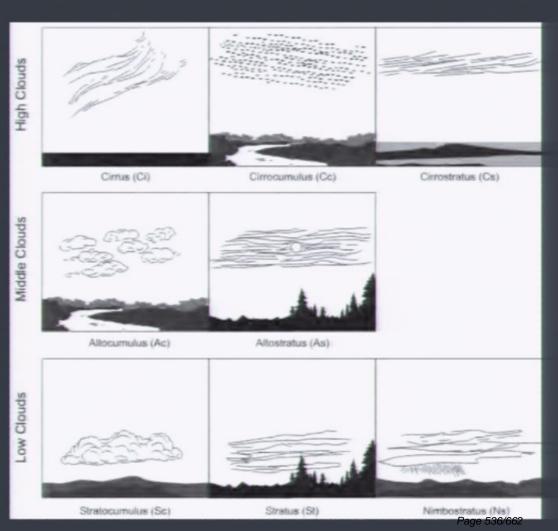


- Different kind of particles and temperature
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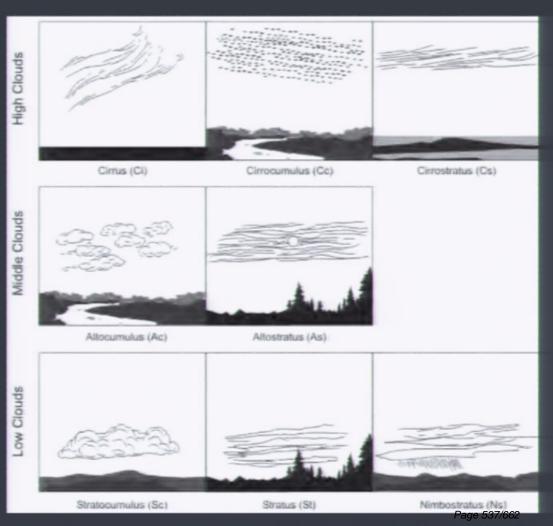
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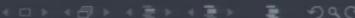




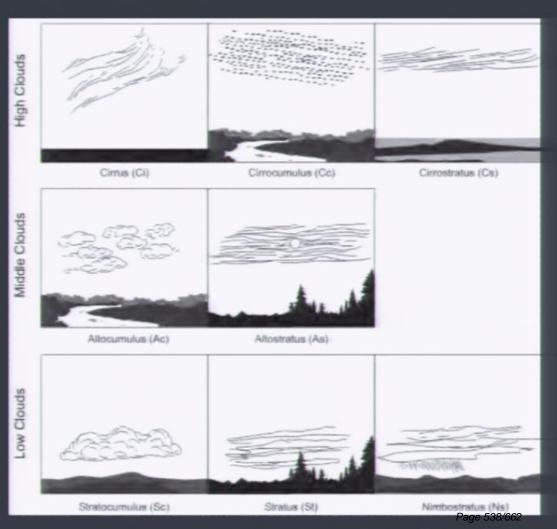
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Pires: 10080031



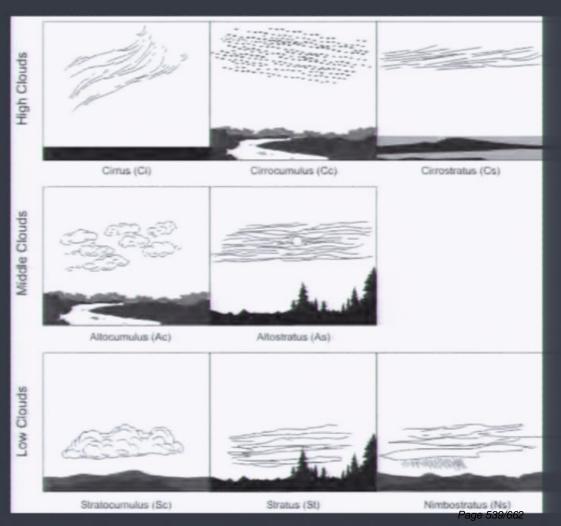
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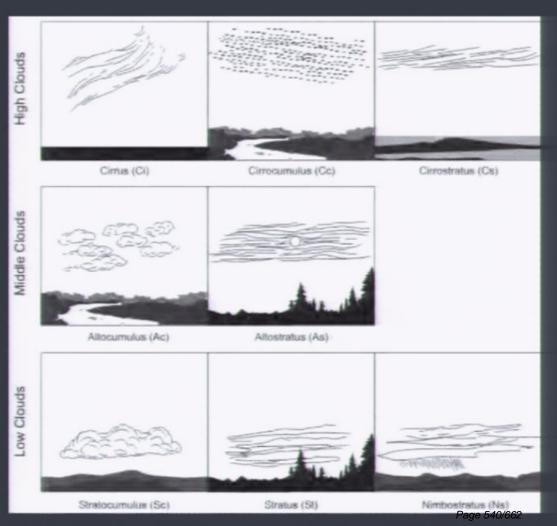
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Pirea: 10080031



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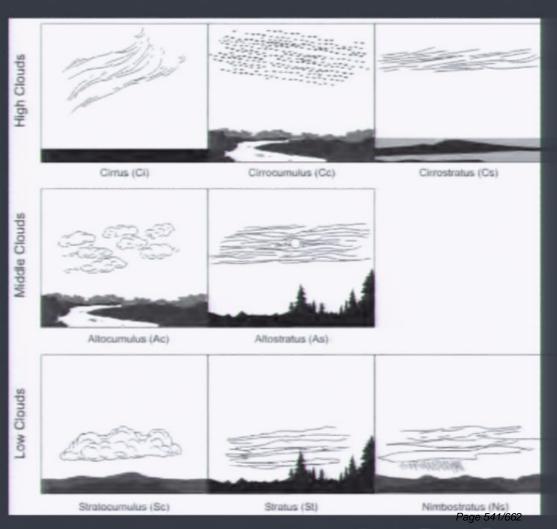


Pires: 10080031



Why do clouds appear in different shapes?

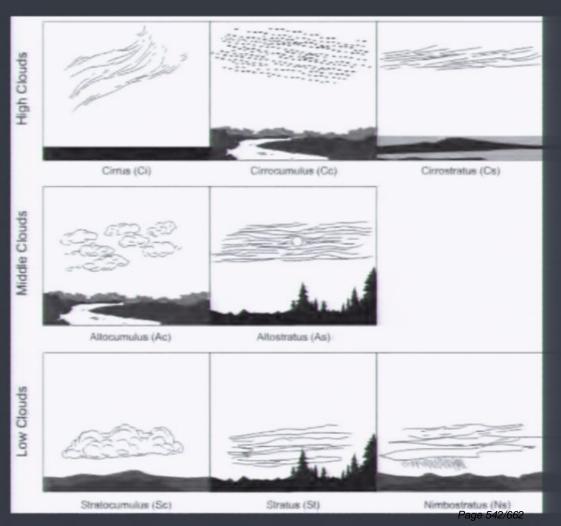
- Different kind of particles and temperature
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Why do clouds appear in different shapes?

- Different kind of particles and temperature
 - icy clouds appear tenuous
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- Altitude









Tenuous, icy clouds





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- Tenuous, icy clouds
- Highest clouds in Earth's atmosphere



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- Tenuous, icy clouds
- Highest clouds in Earth's atmosphere
- 76 to 85 kilometers high (47 to 53 mi)









- Tenuous, icy clouds
- Highest clouds in Earth's atmosphere
- 76 to 85 kilometers high (47 to 53 mi)
- Visible only when illuminated by sunlight from below the horizon while the lower layers of the atmosphere are in Earth's shadow







- Venus
 - Sulfur Dioxide and drops of sulfuric acid
 - Completely opaque

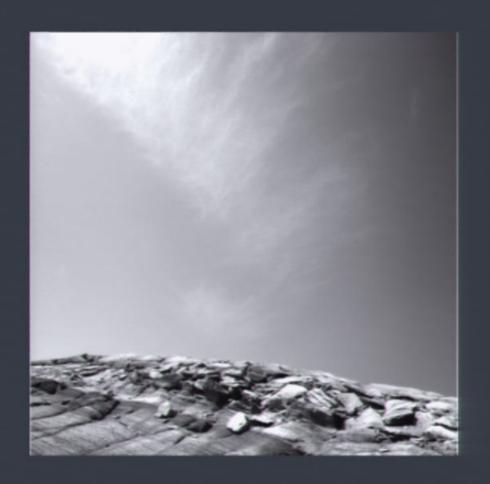


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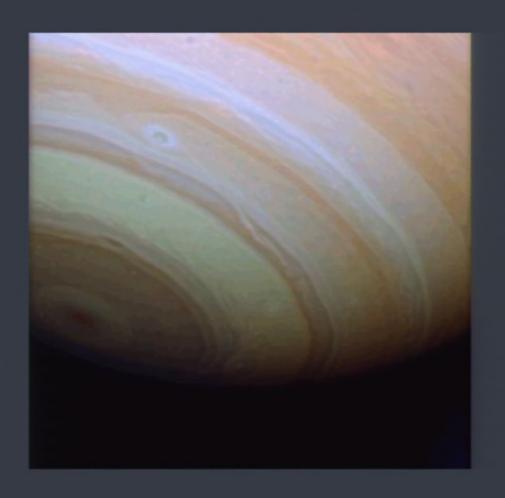




- Venus
 - Sulfur Dioxide and drops of sulfuric acid
 - Completely opaque
- Mars
 - Atmosphere has only a trace of water vapor

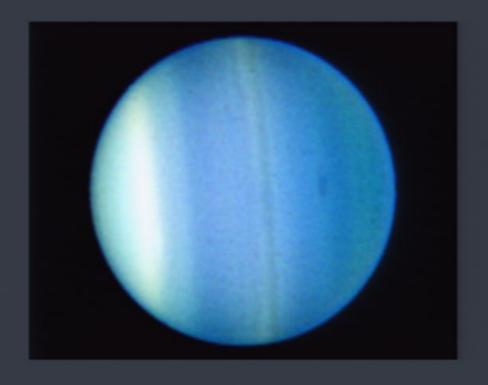


- Venus
 - Sulfur Dioxide and drops of sulfuric acid
 - Completely opaque
- Mars
 - Atmosphere has only a trace of water vapor
- Saturn
 - Ammonia, Ammonia hydrosulfide, water clouds





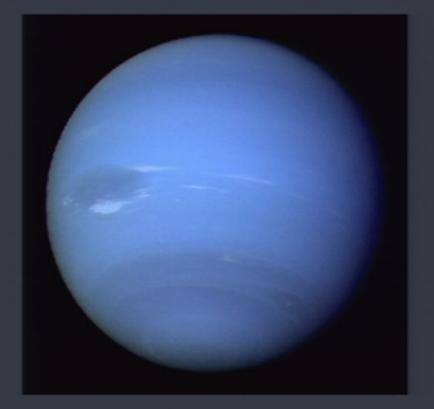
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 - Atmosphere has only a trace of water vapor
- Saturn
 - Ammonia, Ammonia hydrosulfide, water clouds
- Uranus
 - Methane crystals

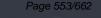


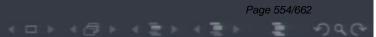


- Venus
 - Sulfur Dioxide and drops of sulfuric acid
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 hydrosulfide, water clouds
- Uranus
 - Methane crystals
- Neptune

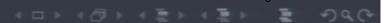
irsa: 10080031







Clouds are not vaporized water



- Clouds are not vaporized water
- There are clouds in different altitudes







- Clouds are not vaporized water
- There are clouds in different altitudes
- Clouds can consist of different kind of particles



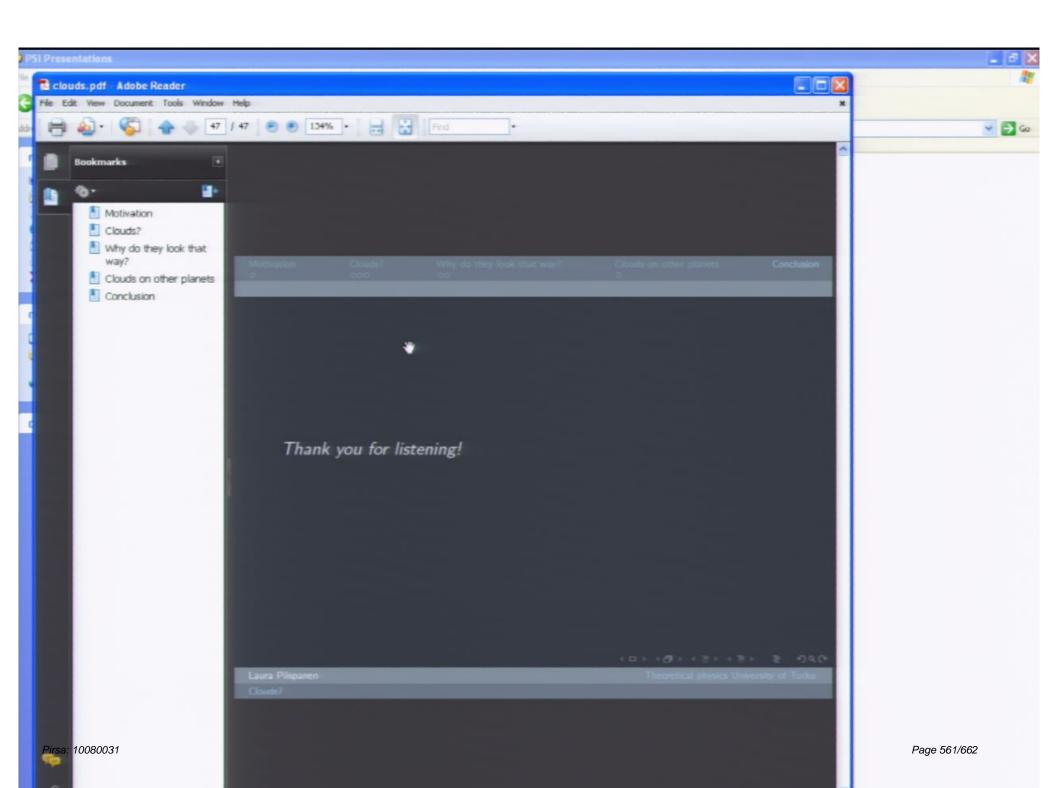
- Clouds are not vaporized water
- There are clouds in different altitudes
- Clouds can consist of different kind of particles
- There are "clouds" on other planets

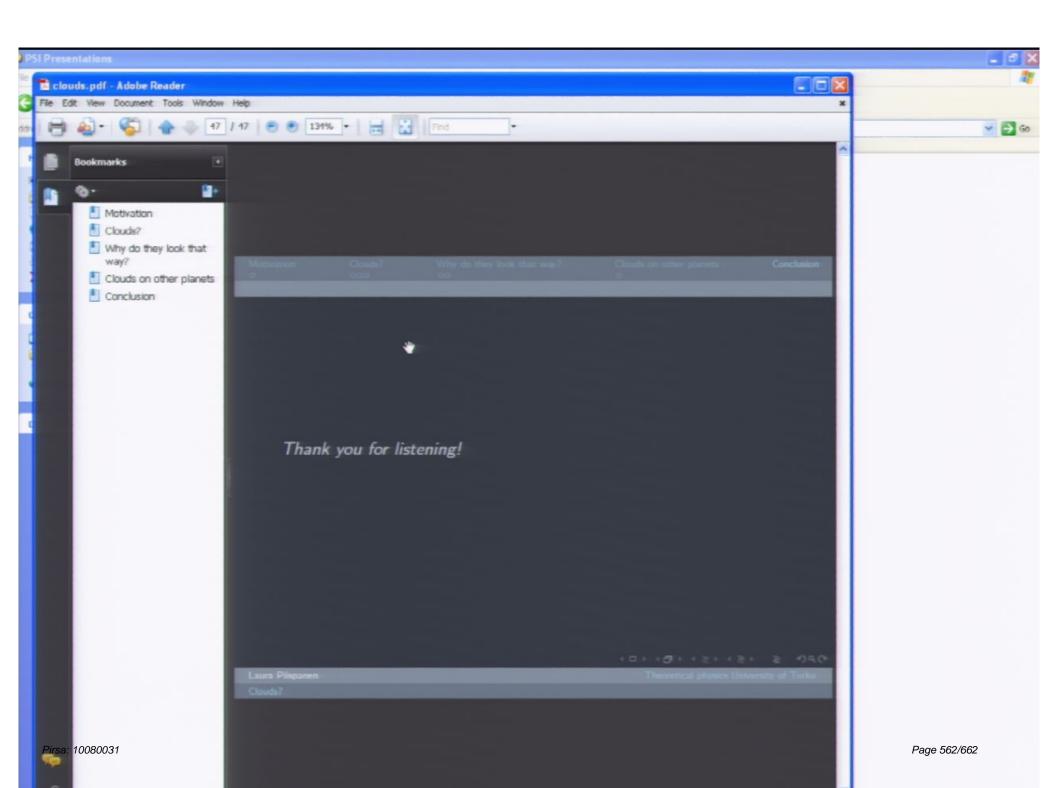


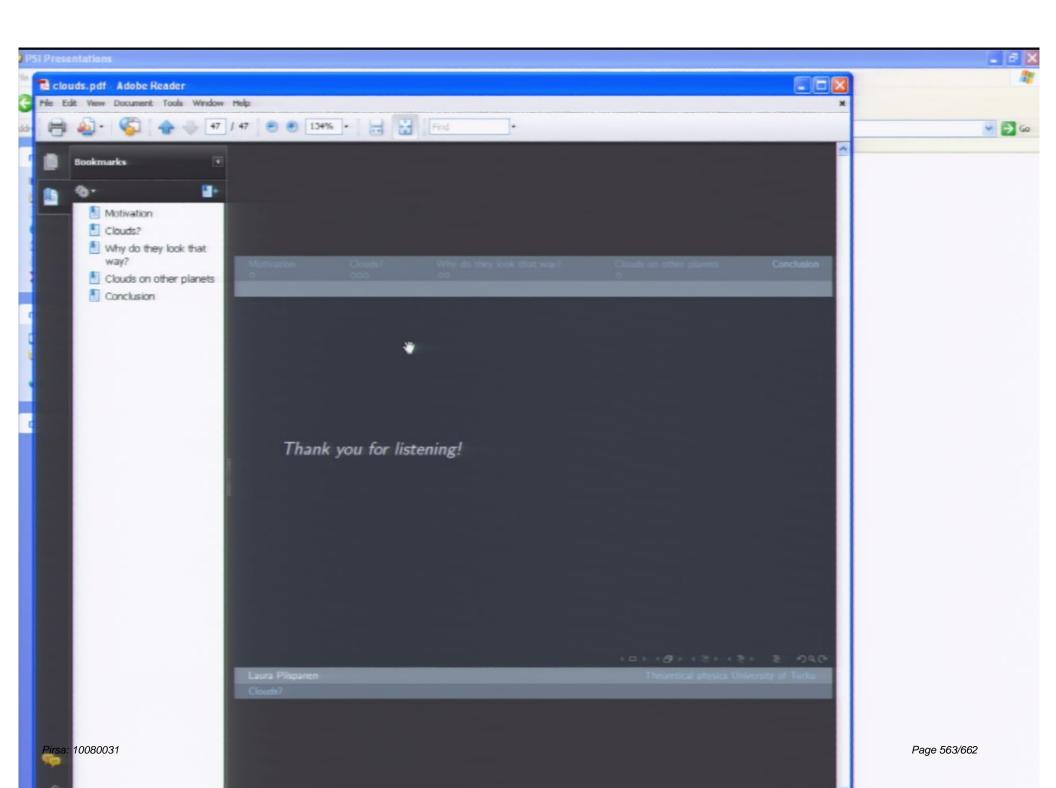
- Clouds are not vaporized water
- There are clouds in different altitudes
- Clouds can consist of different kind of particles
- There are "clouds" on other planets
- You can't jump on a cloud and stay on it!

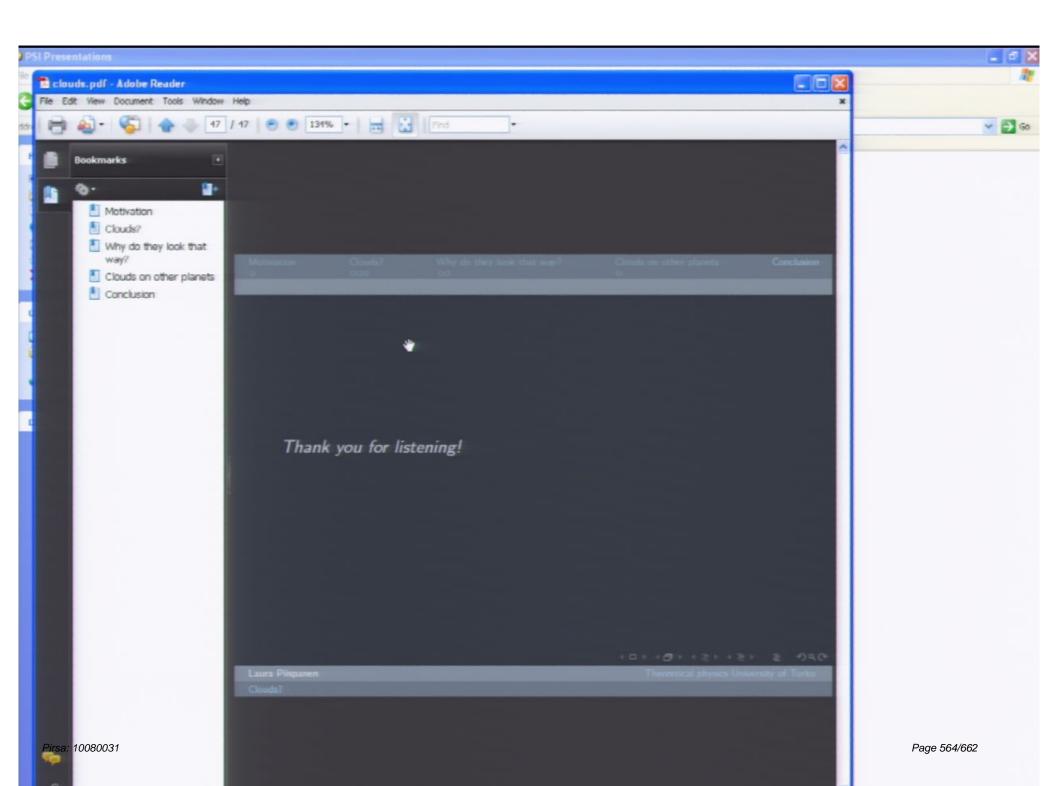
Thank you for listening!

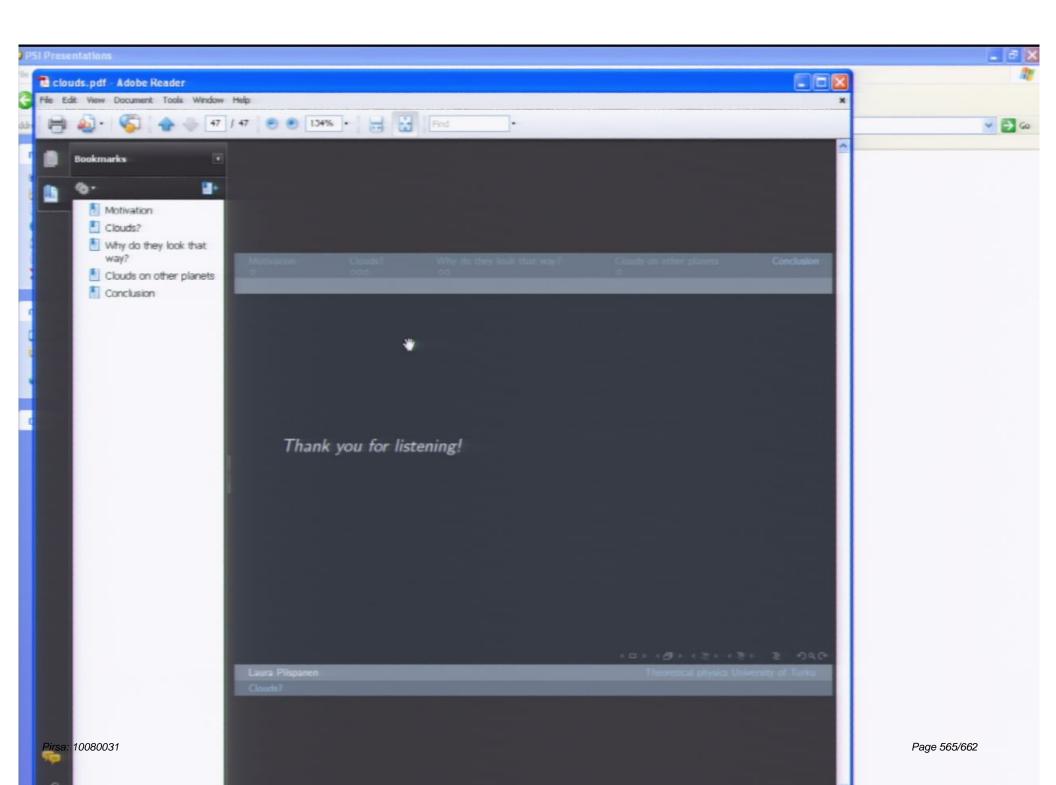


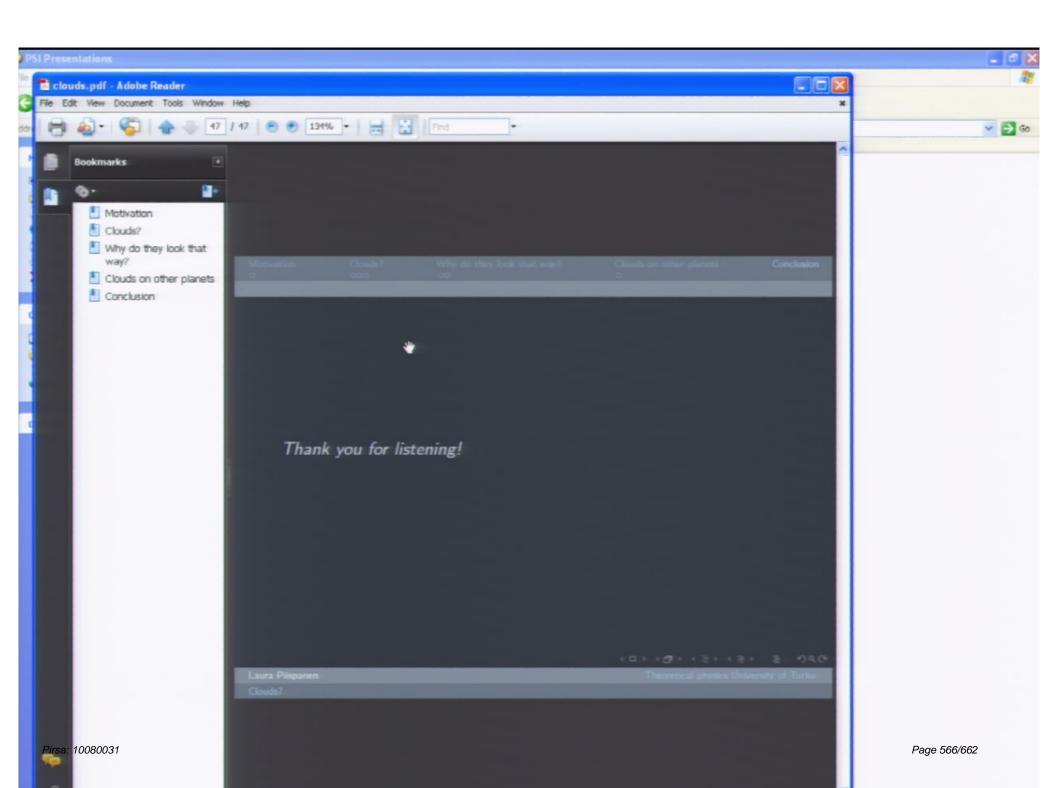


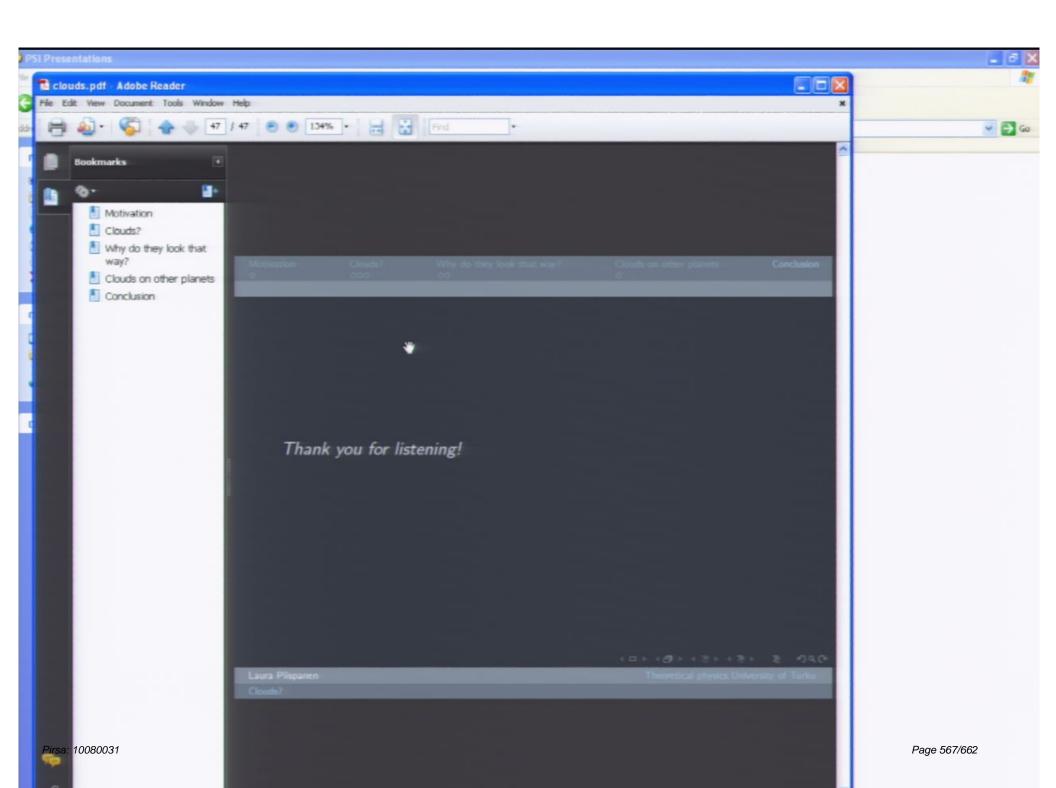


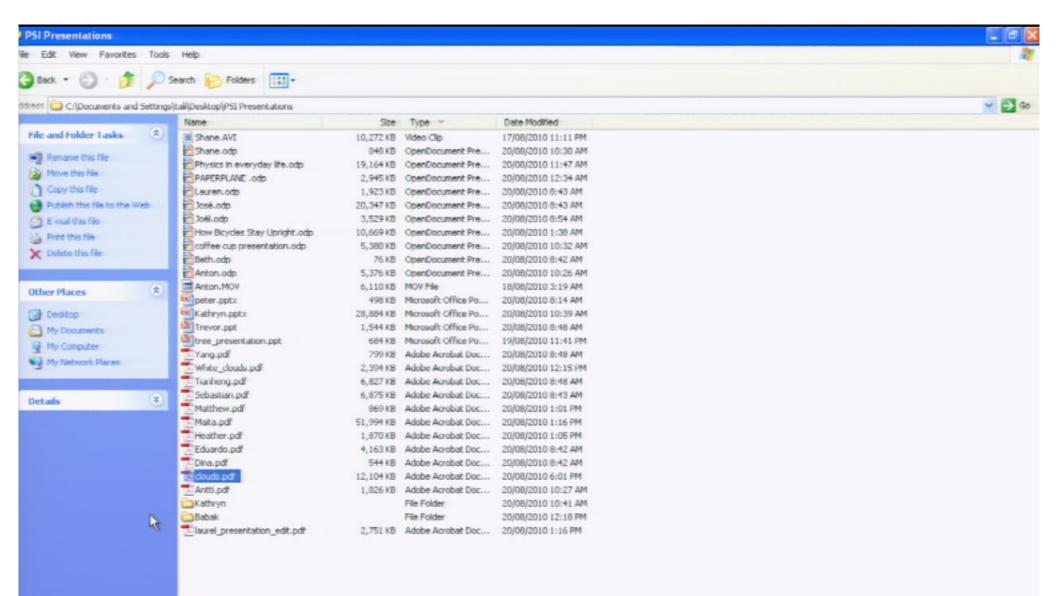




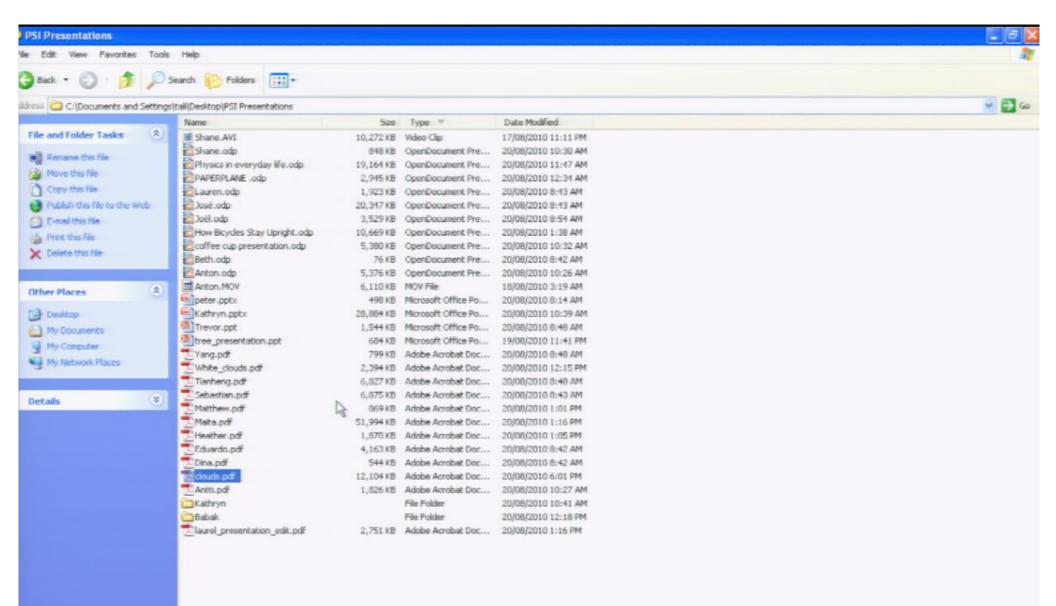




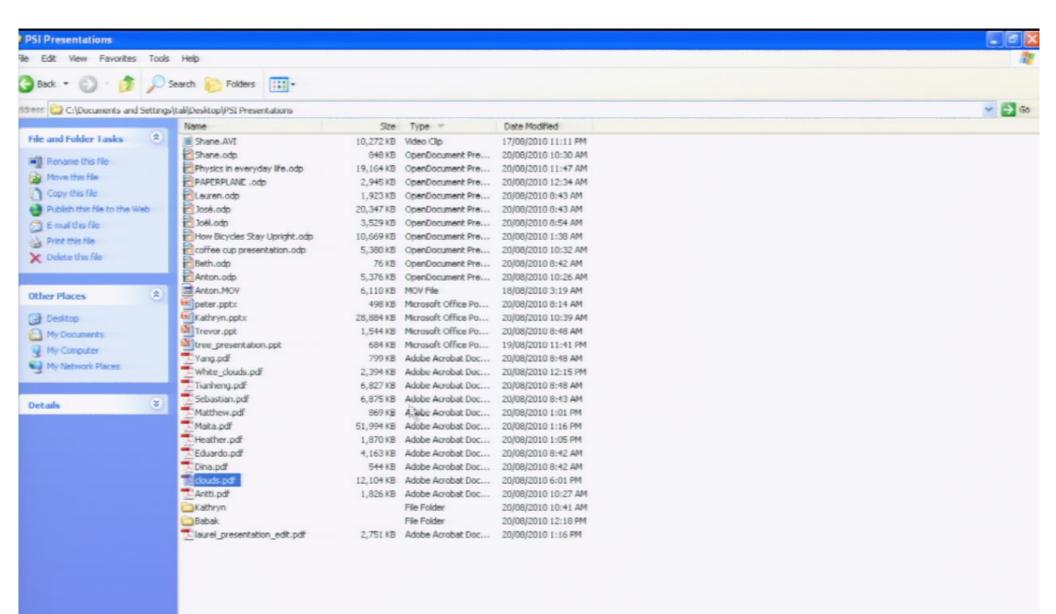




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Pirsa: 10080031 Page 571/662

Photograph from Ohio University's Fluid Mechanics Laboratory. Athens, Ohio USA



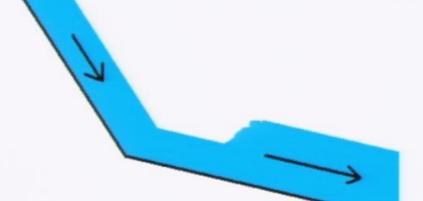
Photograph from Ohio University's Fluid Mechanics Laboratory. Athens, Ohio USA



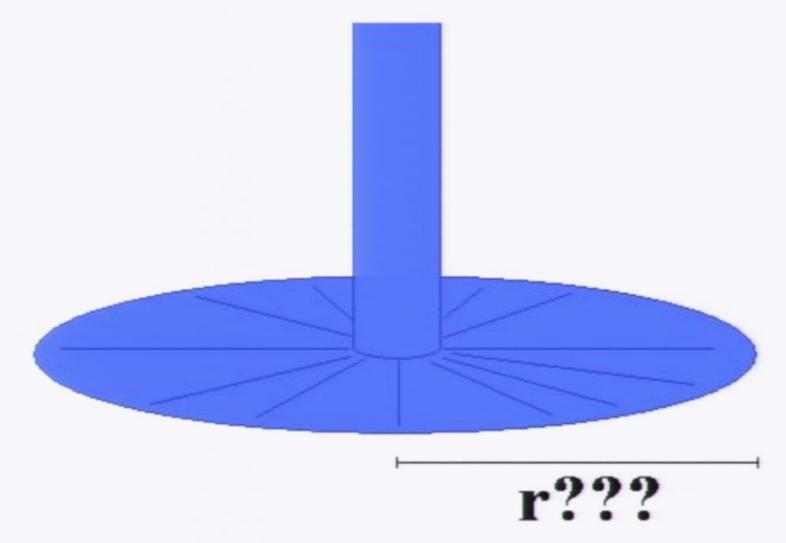
where do we see Hydraulic Jumps in nature?



Photograph from Wiki



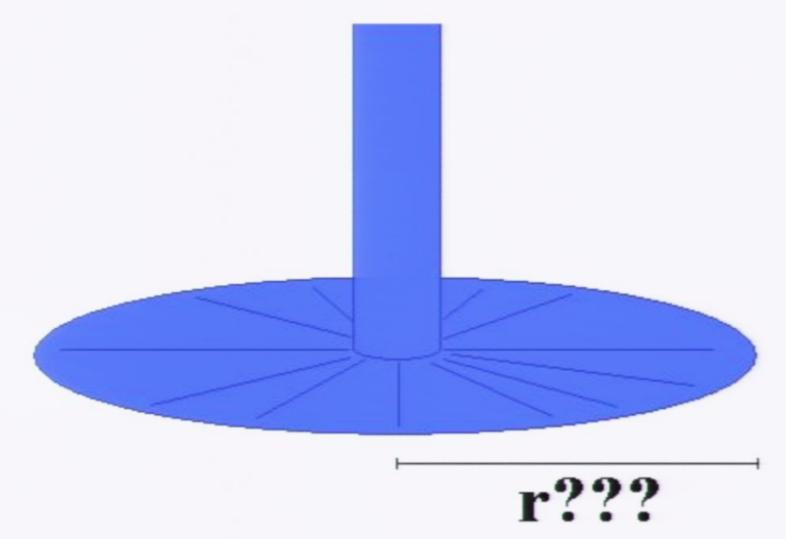
Lets do something different



Pirsa: 10080031

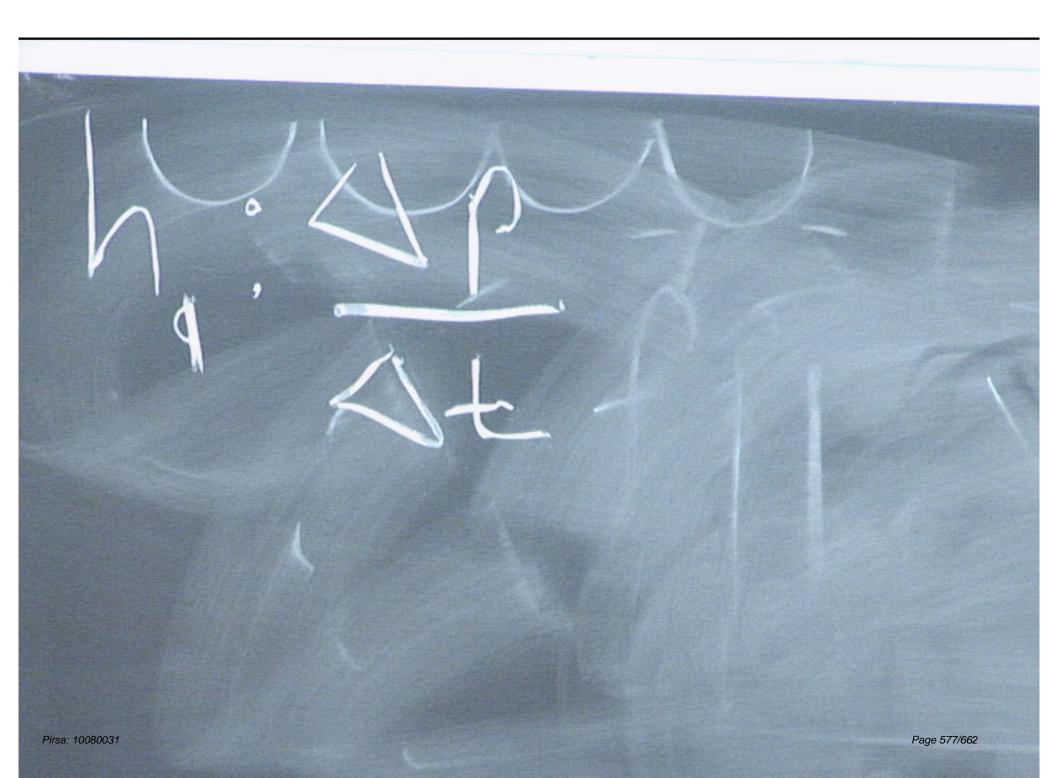
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Lets do something different



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hill = X (Aratirh, p)

Pires: 10080031

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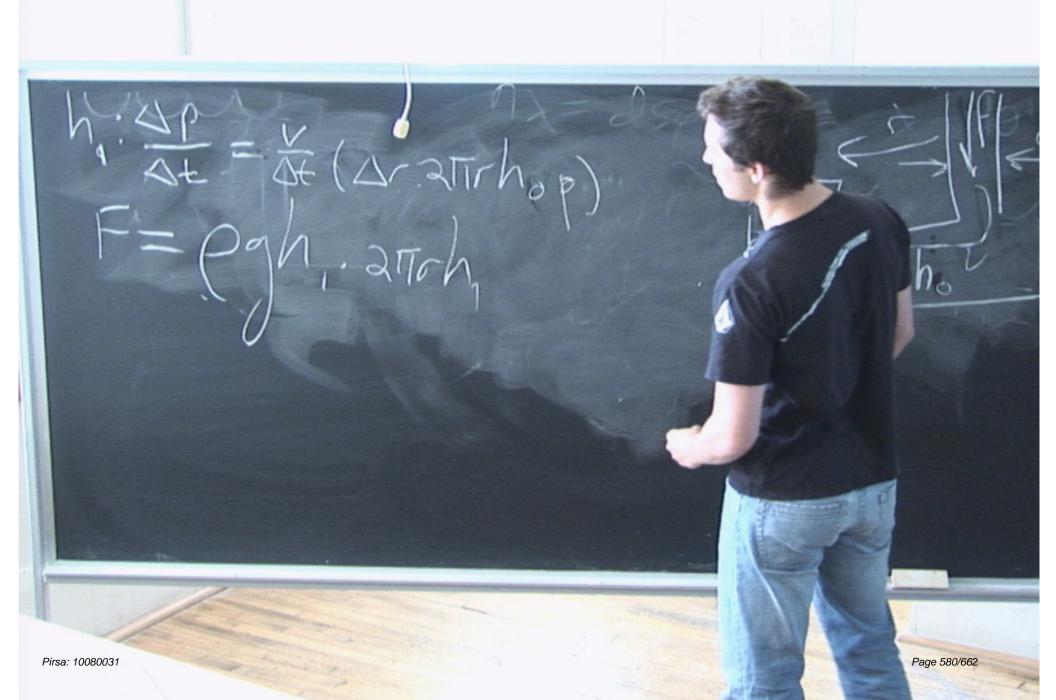
in la A

hist = XX (Aratirhop)

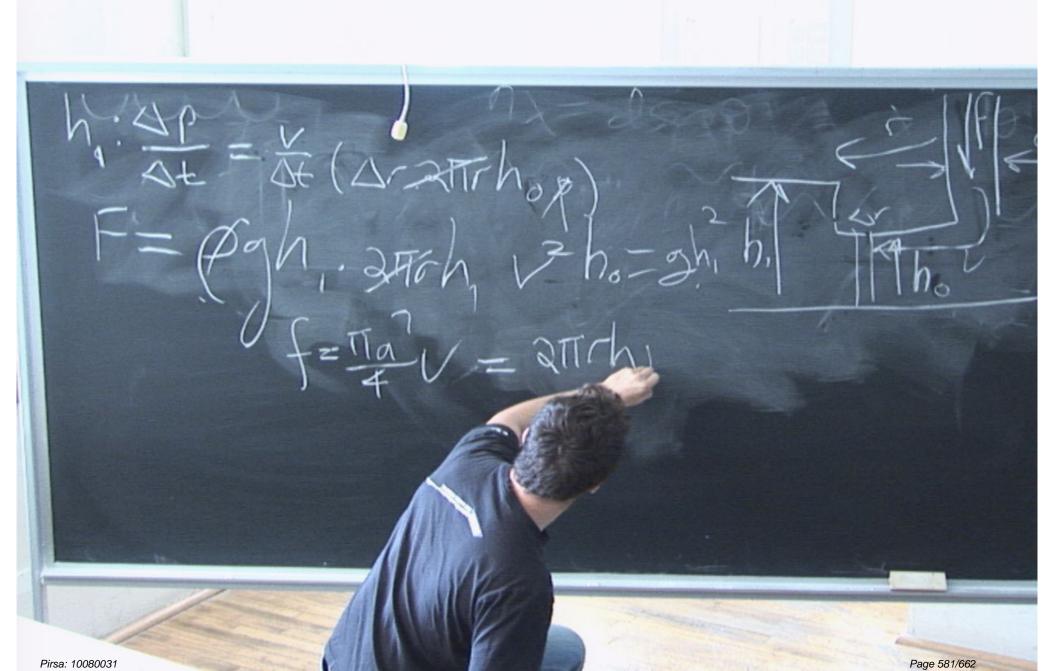
F= Poph, attorn

h, Th.

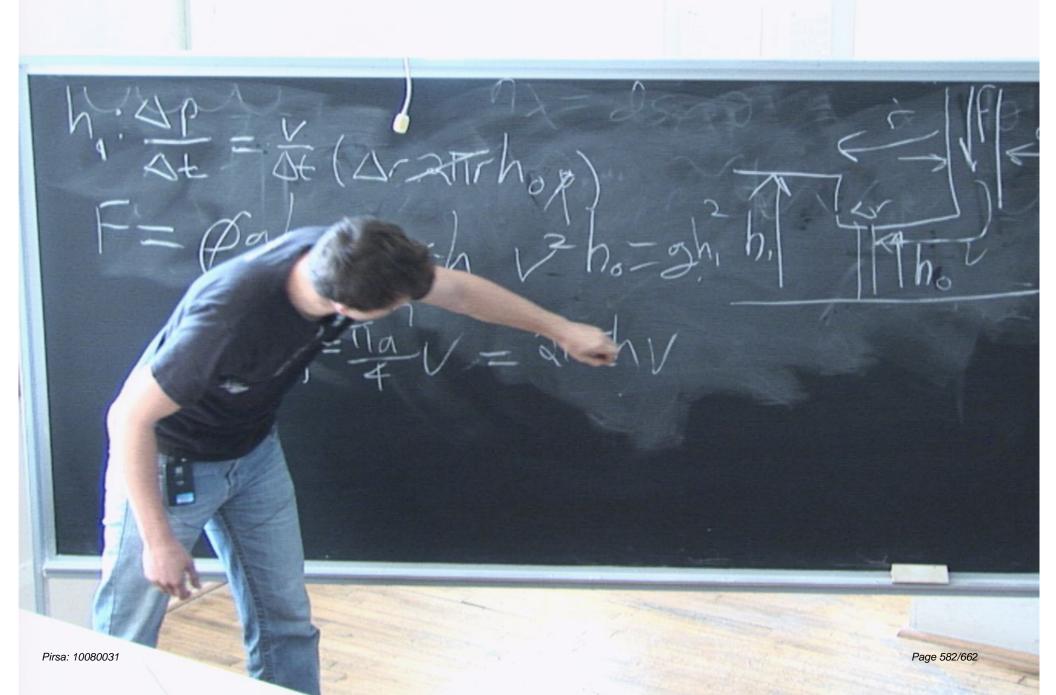
iolecule!



blecolet



in la A

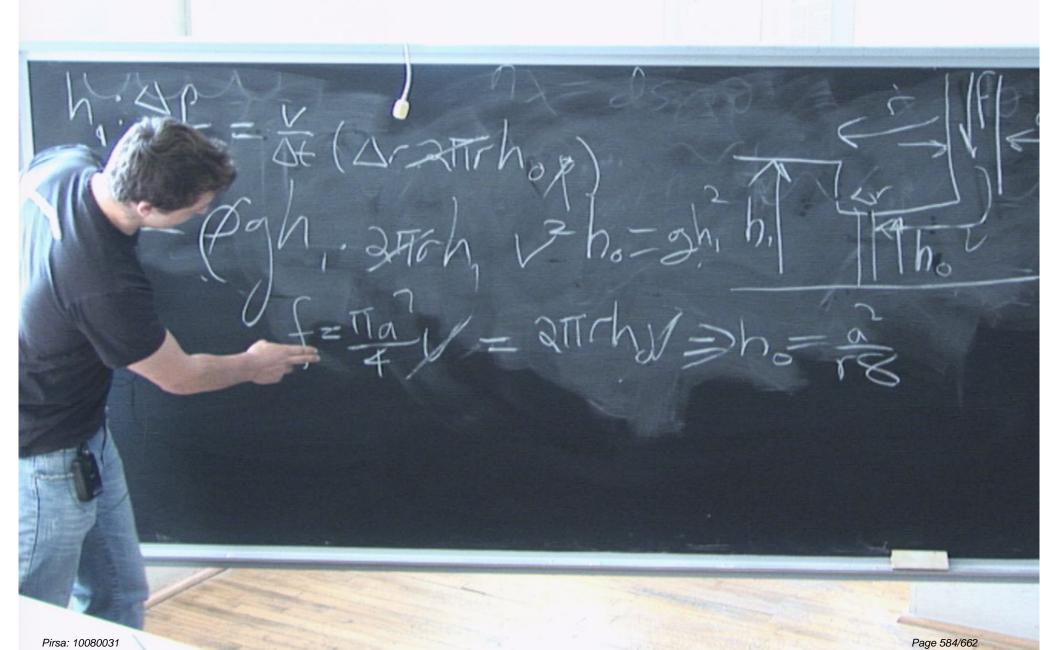


Tolecule!

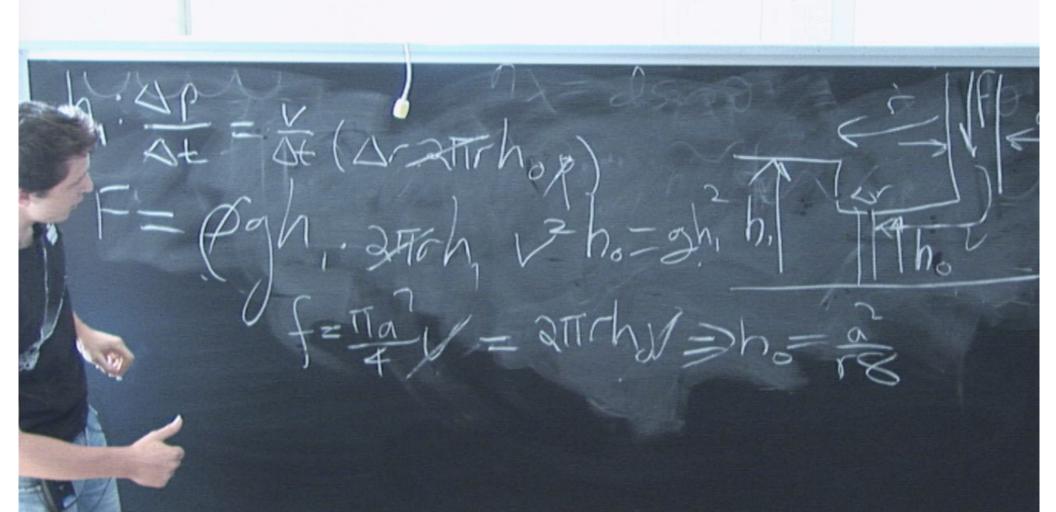
Pirsa: 10080031

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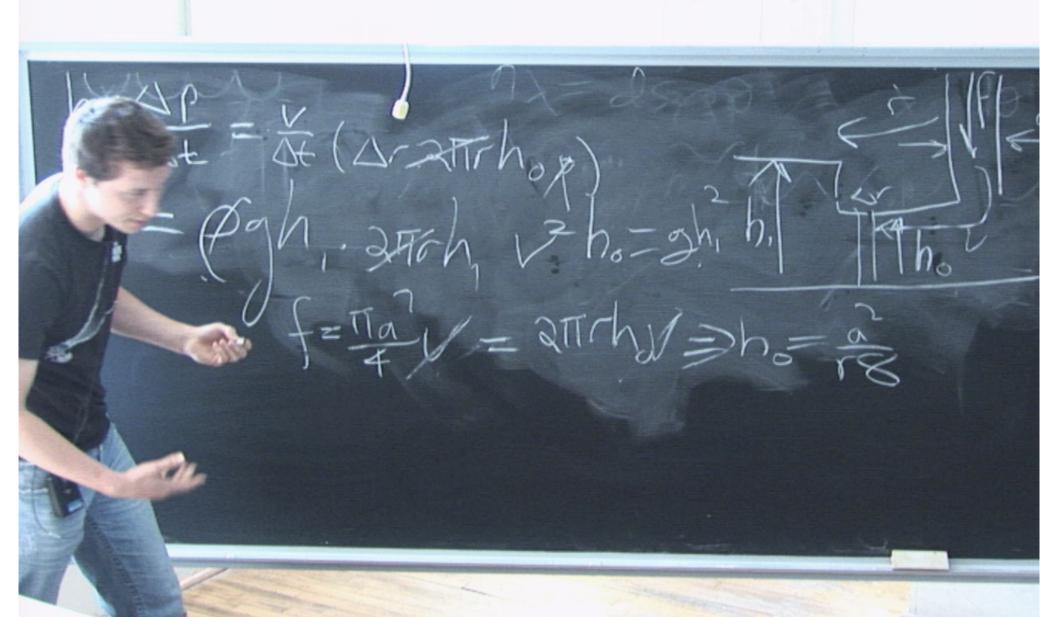
Tolecule!



lolecule!



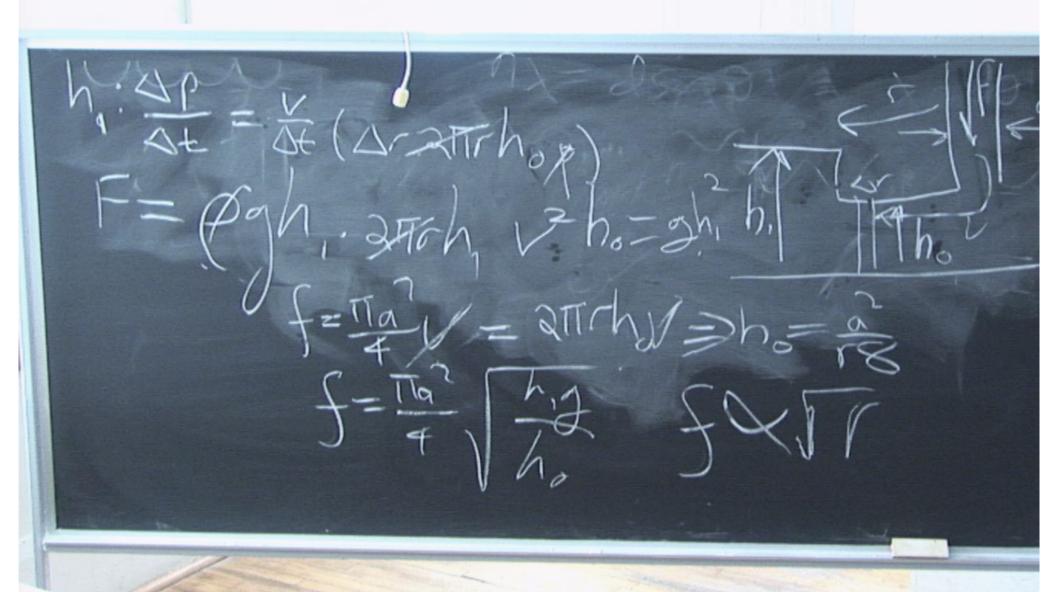
"blecole!



Pirsa: 10080031

Page 586/662

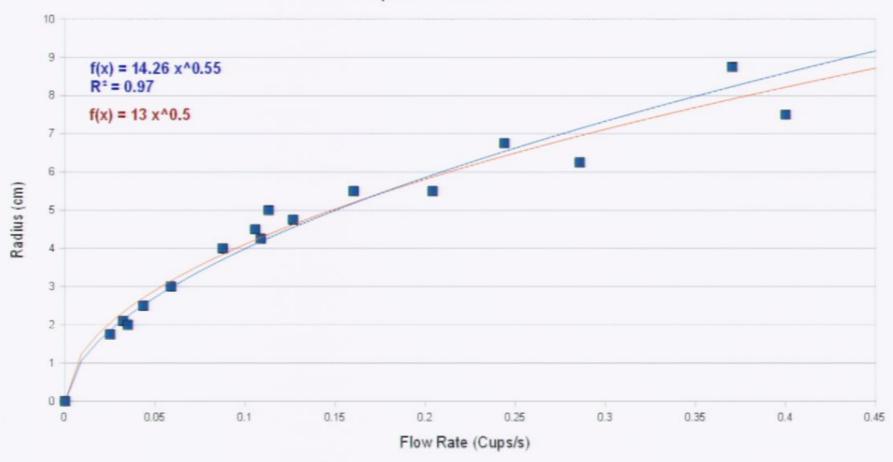
Evidence in la A



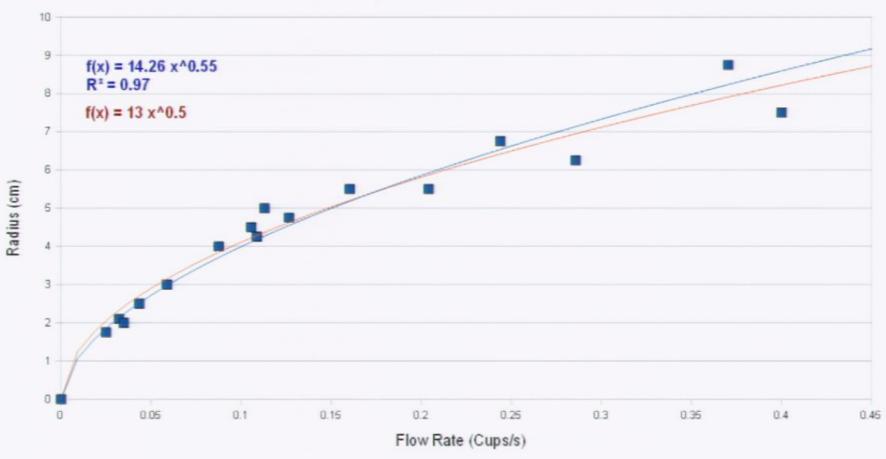
Pirsa: 10080031

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Jump Radius Vs Flow Rate



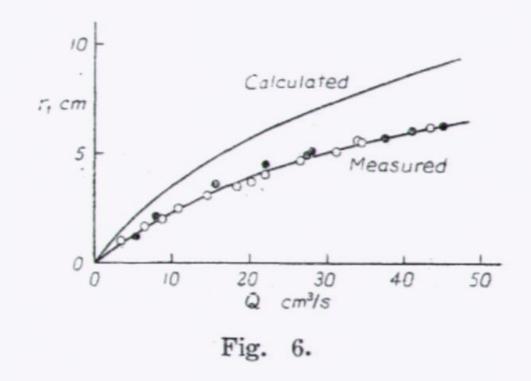
Jump Radius Vs Flow Rate



$$\frac{dh}{dr} = \frac{5\pi\nu}{Q} r.$$

Integration gives

$$h = \frac{5\pi v}{Q} \frac{r^2}{2}.$$



I. Tani "Water jump in the boundary later" J. Phys. Soc.

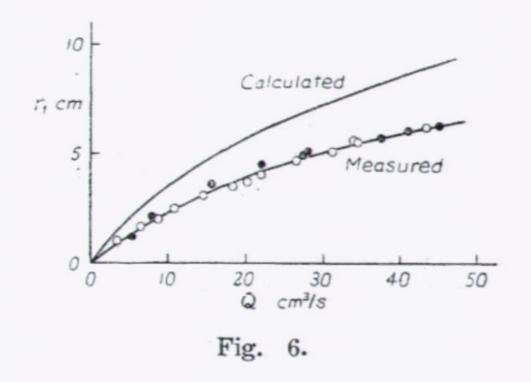
Japan. 4 212-215 (1949)

Page 590/662

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

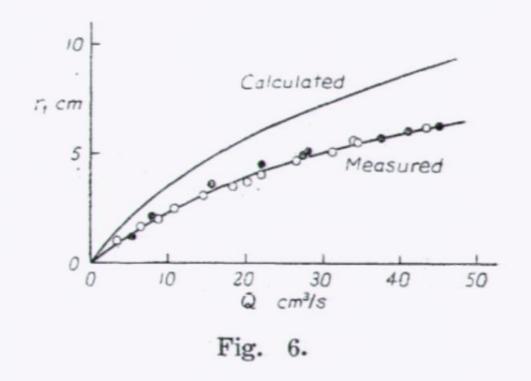
Pirsa: 10080031 Japan. 4 212-215 (1949)

Page 591/662

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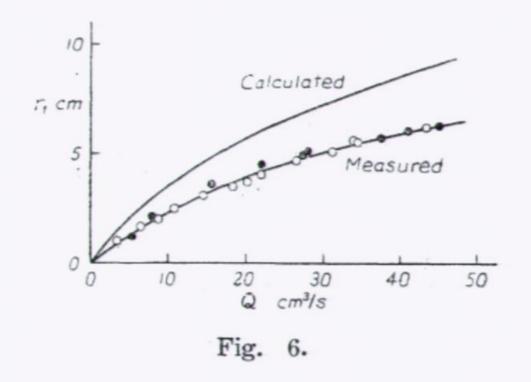
Japan. 4 212-215 (1949)

Page 592/662

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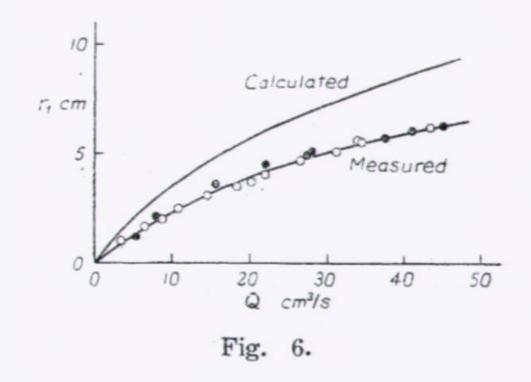
Japan. 4 212-215 (1949)

Page 593/662

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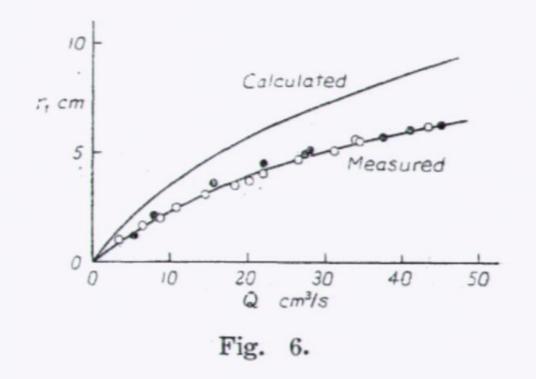
Pirsa: 10080031 Japan. 4 212-215 (1949)

Page 594/662

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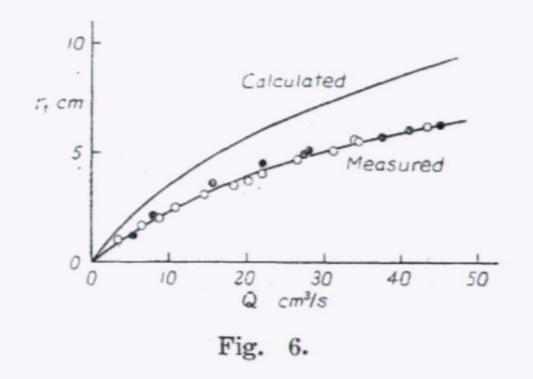
Japan. 4 212-215 (1949)

Page 595/662

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

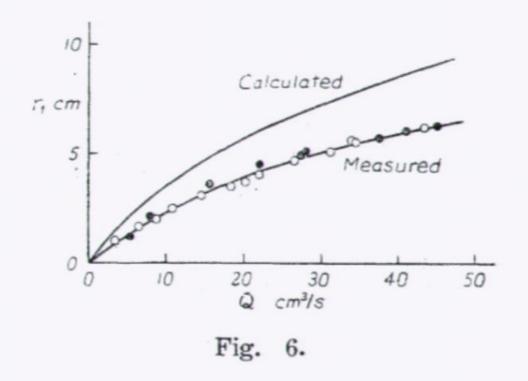
Japan. 4 212-215 (1949)

Page 596/662

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

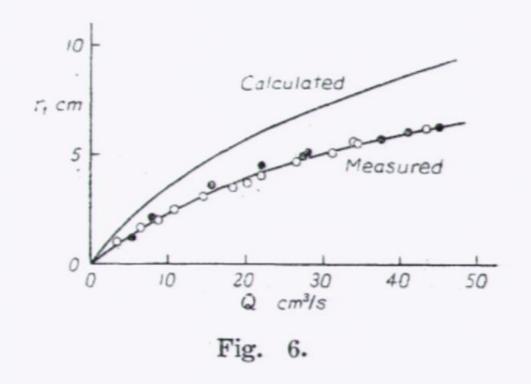
Japan. 4 212-215 (1949)

Page 597/662

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Integration gives

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

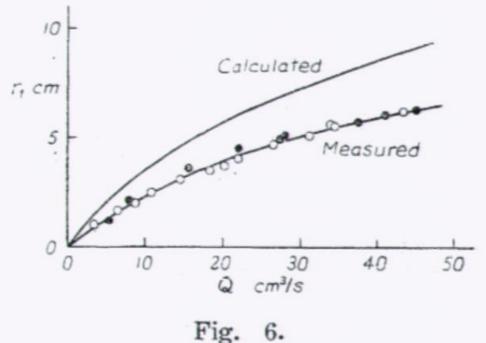
Japan. 4 212-215 (1949)

Page 598/662

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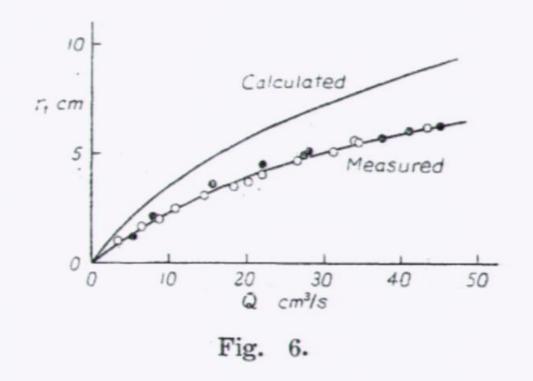


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I. Tani "Water jump in the boundary later" J. Phys. Soc.

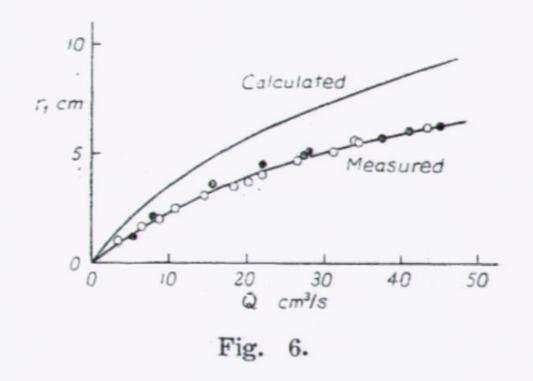
Pirsa: 10080031 Japan. 4 212-215 (1949)

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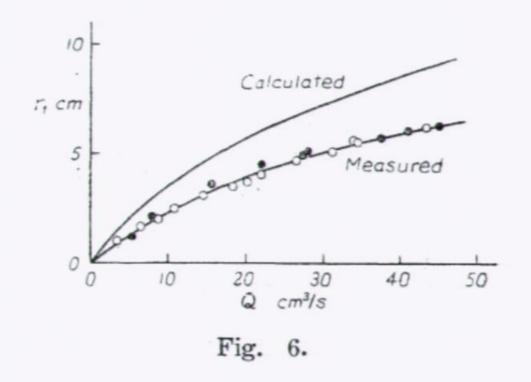
Japan. 4 212-215 (1949)

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

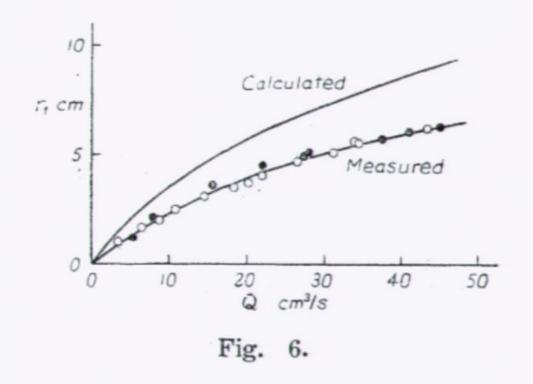
Japan. 4 212-215 (1949)

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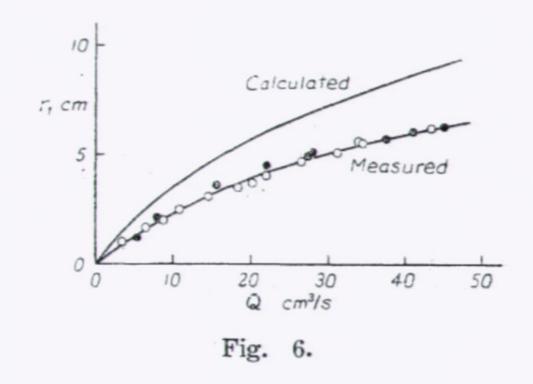
Pirsa: 10080031 Japan. 4 212-215 (1949)

Page 603/662

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Integration gives

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

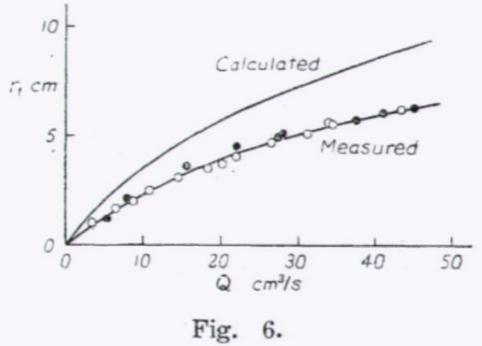
Japan. 4 212-215 (1949)

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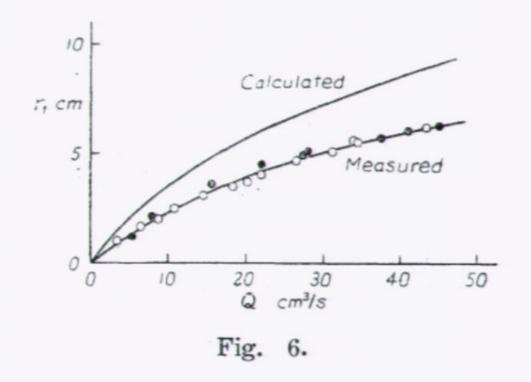


 Tani "Water jump in the boundary later" J. Phys. Soc. Japan. 4 212-215 (1949) Pirsa: 10080031 Page 605/662

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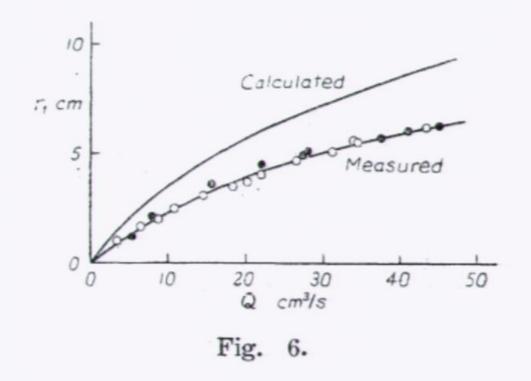
Pirsa: 10080031 Japan. 4 212-215 (1949)

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

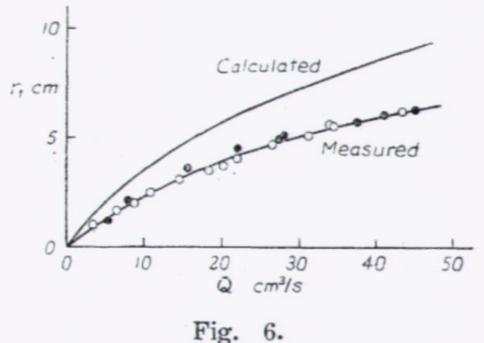
Japan. 4 212-215 (1949)

Page 607/662

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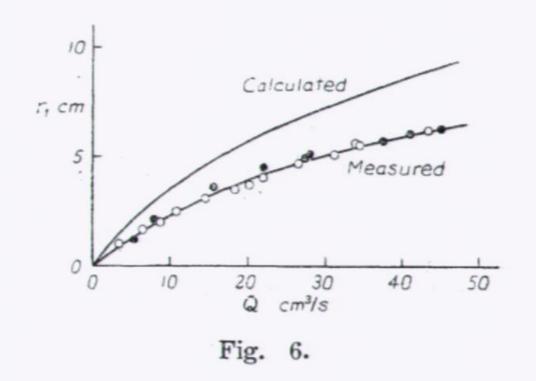


 Tani "Water jump in the boundary later" J. Phys. Soc. Japan. 4 212-215 (1949) Pirsa: 10080031 Page 608/662

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

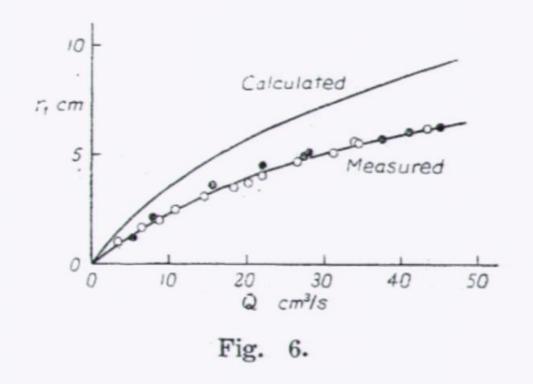
Japan. 4 212-215 (1949)

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I. Tani "Water jump in the boundary later" J. Phys. Soc.

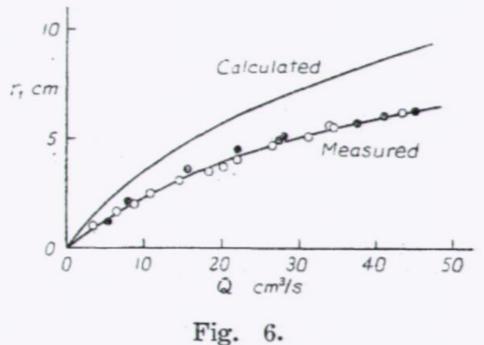
Japan. 4 212-215 (1949)

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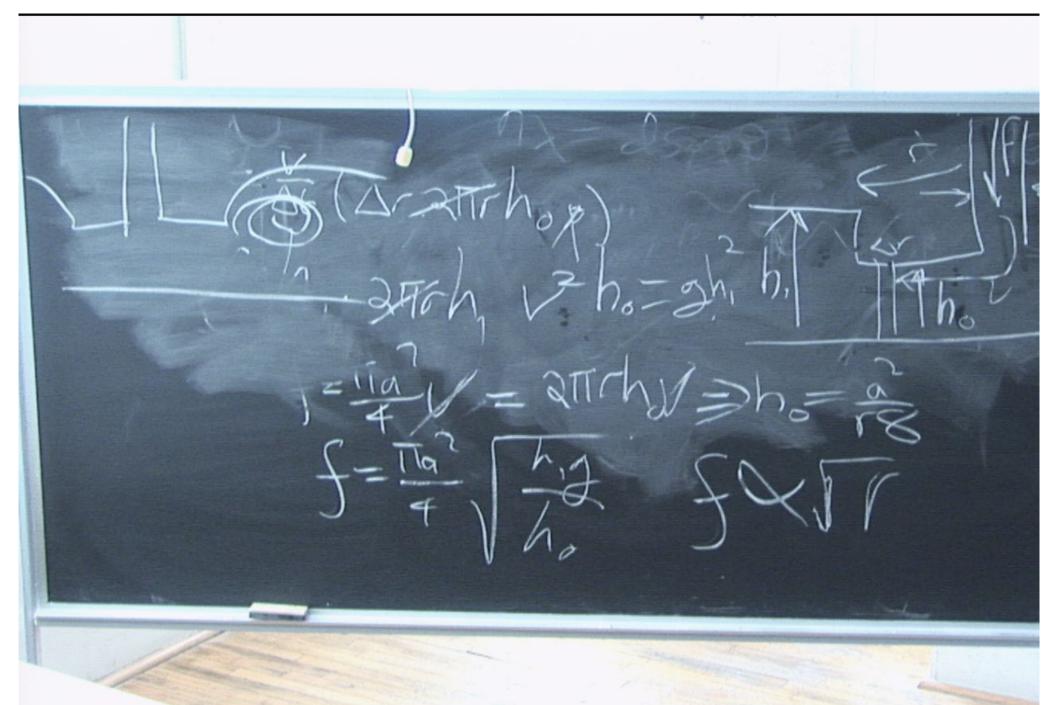
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 Tani "Water jump in the boundary later" J. Phys. Soc. Japan. 4 212-215 (1949) Pirsa: 10080031 Page 611/662



Pirsa: 10080031

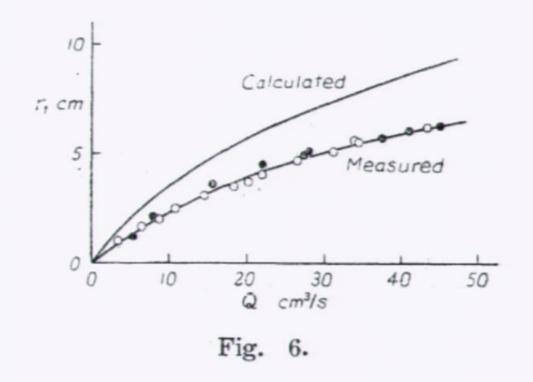
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Using Navier-Stockes and the no slip condition at stagnation

$$\frac{dh}{dr} = \frac{5\pi v}{Q} r.$$

Integration gives

$$h = \frac{5\pi v}{Q} \frac{r^2}{2}$$



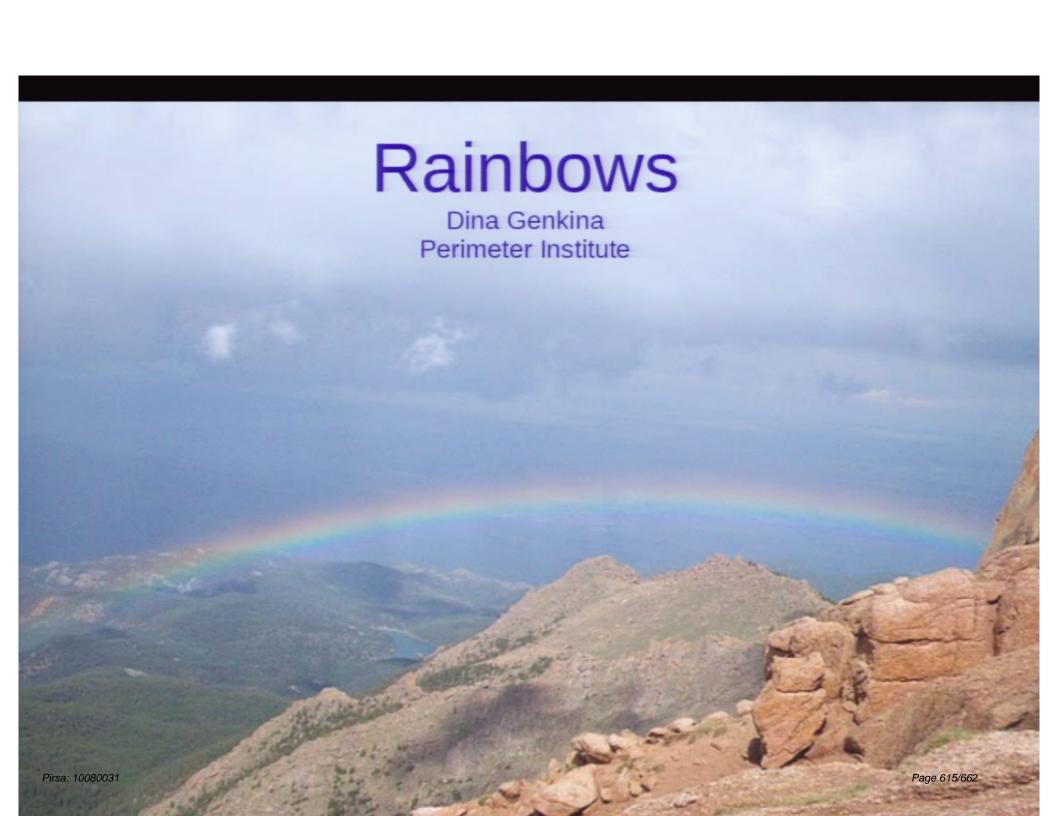
I. Tani "Water jump in the boundary later" J. Phys. Soc.

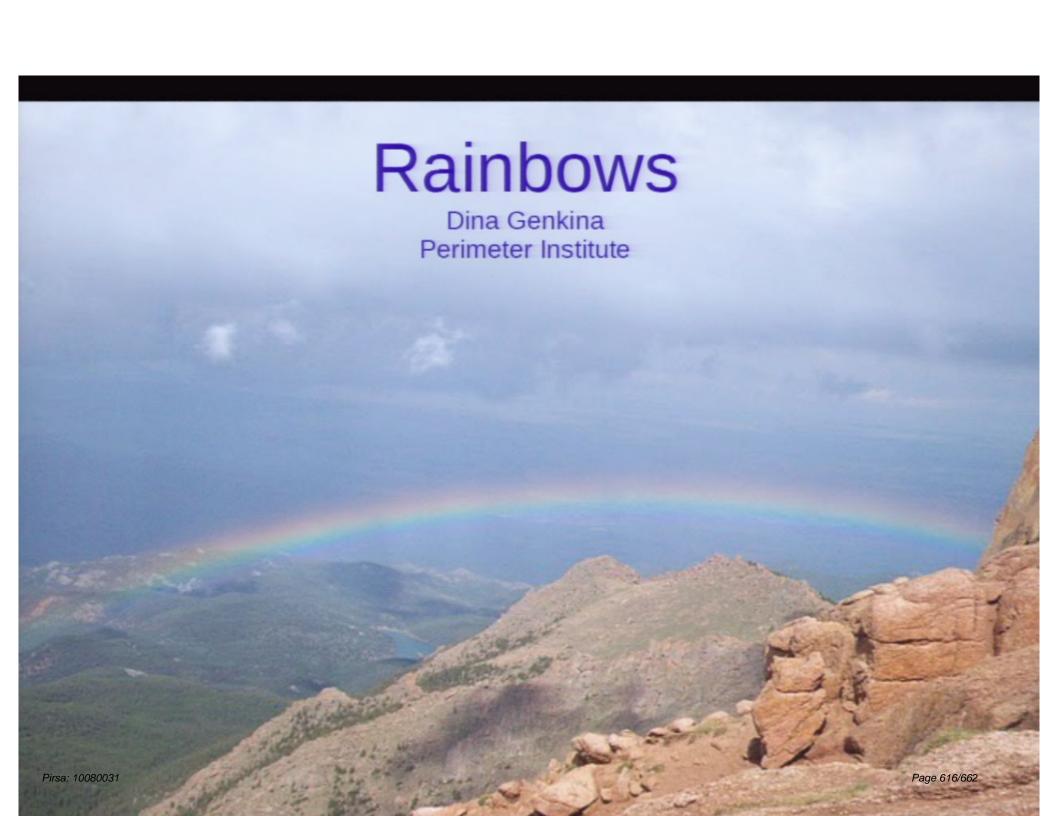
Japan. 4 212-215 (1949)

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Pirsa: 10080031 Page 614/662





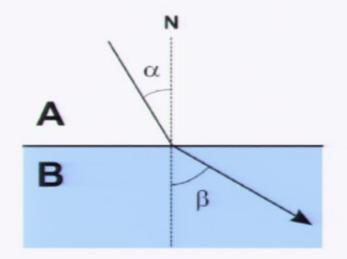
Overview

- Where do rainbows come from?
- Why Roy G. Biv?
- Why is it an arc?
- Where do double rainbows come from?
- Pretty Pictures

Pirsa: 10080031

Snell's Law – A review

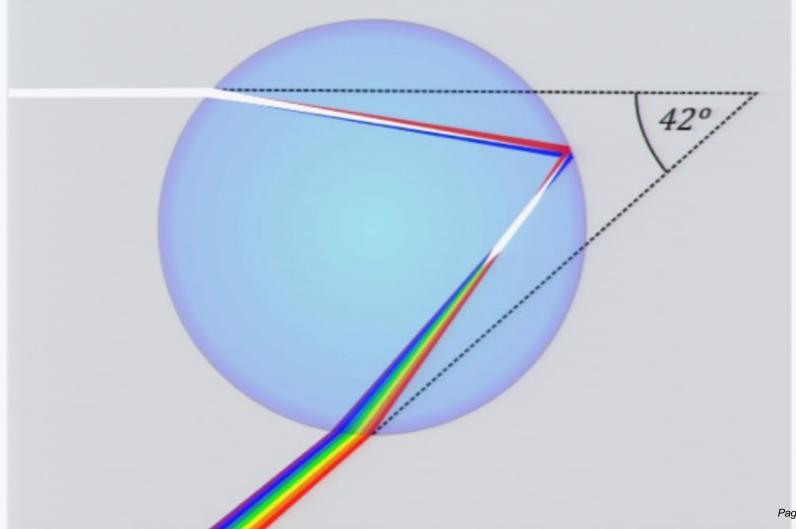
$$n_1 \sin(\alpha) = n_2 \sin(\beta)$$



Index of refraction of water is a function of the light wavelength:

$$n(red) = 1.3312$$

$$n(blue) = 1.3404$$

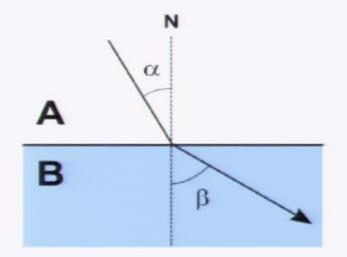


Pirsa: 10080031

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Snell's Law – A review

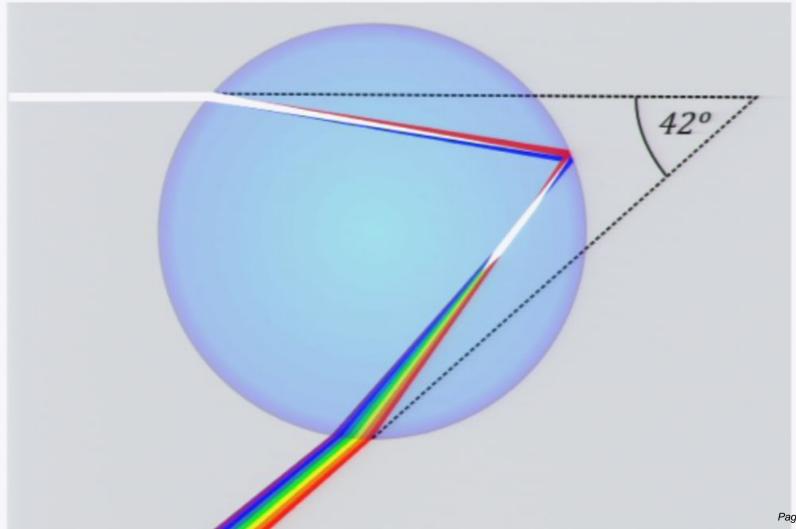
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Index of refraction of water is a function of the light wavelength:

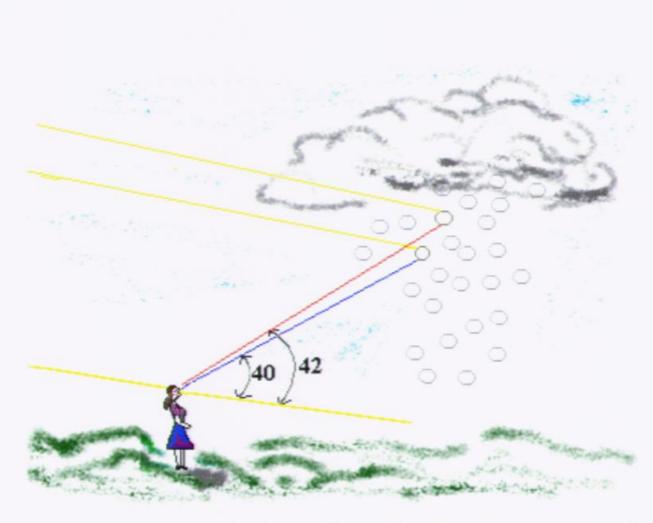
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Pirsa: 10080031

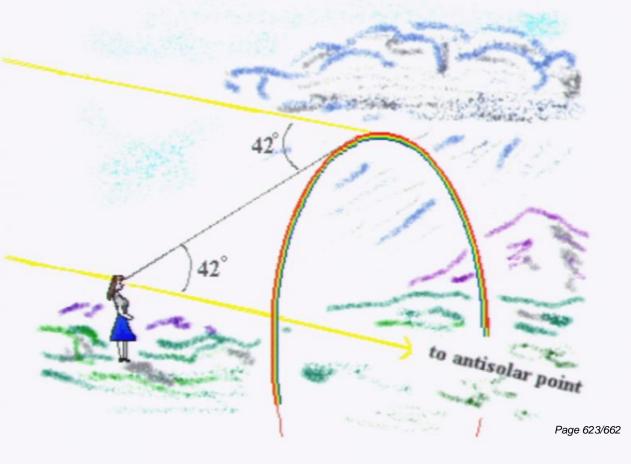
Page 621/662

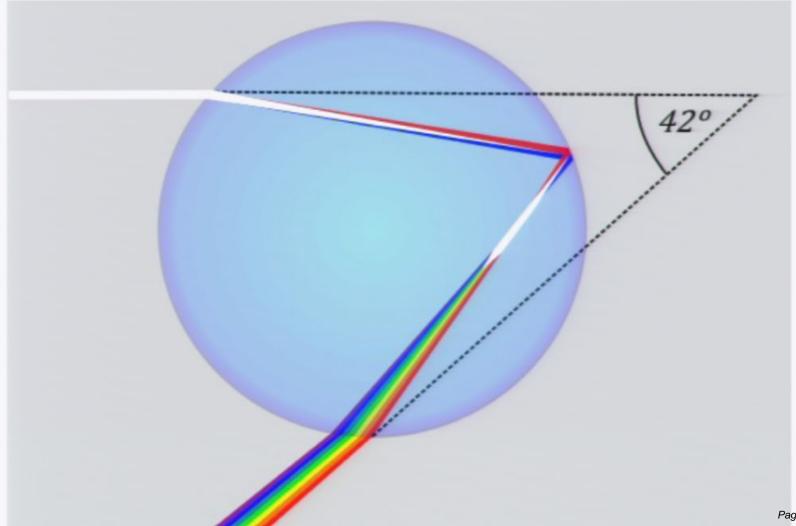


An observer sees different colors reflected from distinct raindrops, so that red appears on top. Page 622/662

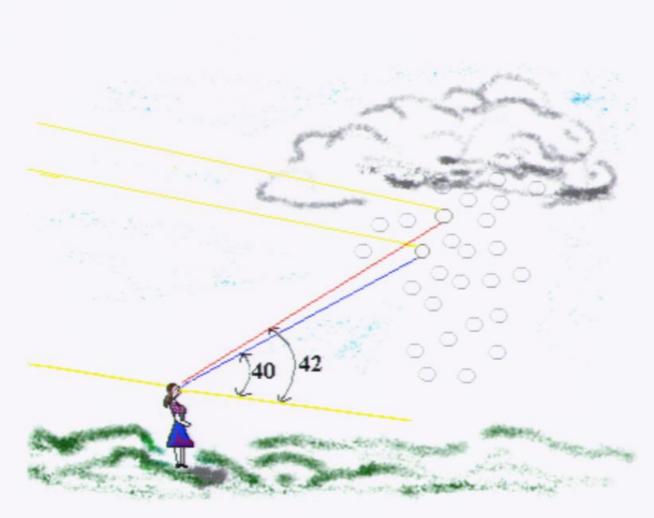
An observer will see red light from all raindrops in a 42 degree cone around them, producing and arc above the horizon.

The sun must be less than 42 degrees above the horizon for a rainbow to be visible at sea level.





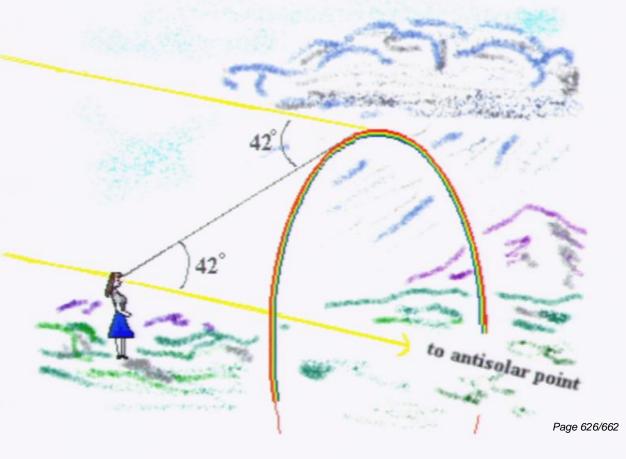
Pirsa: 10080031



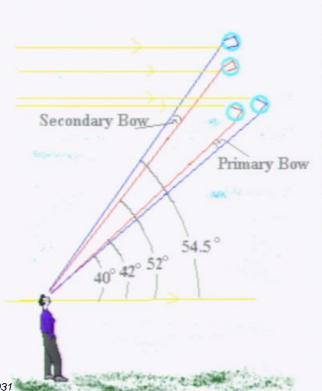
An observer sees different colors reflected from distinct raindrops, so that red appears on top. Page 625/662

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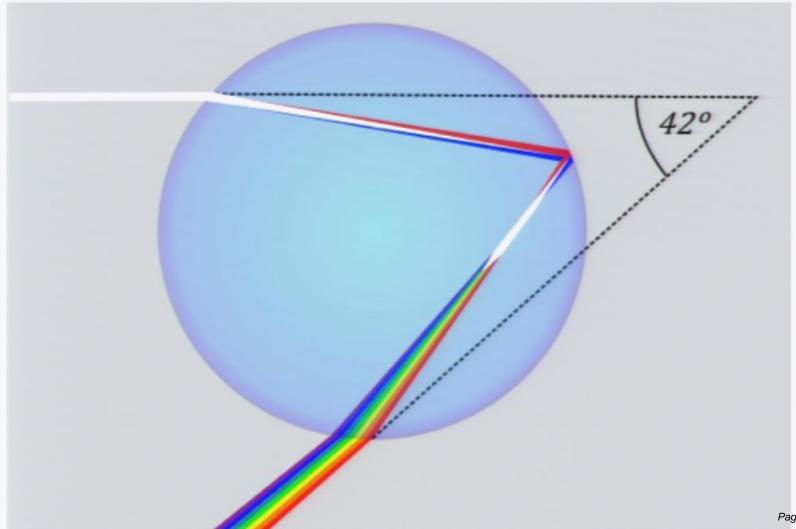


The double rainbow





The dark space between the rainbows is called Alexander's band and is caused by light reflected through larger angles than the Page 627/662 maximum intensity

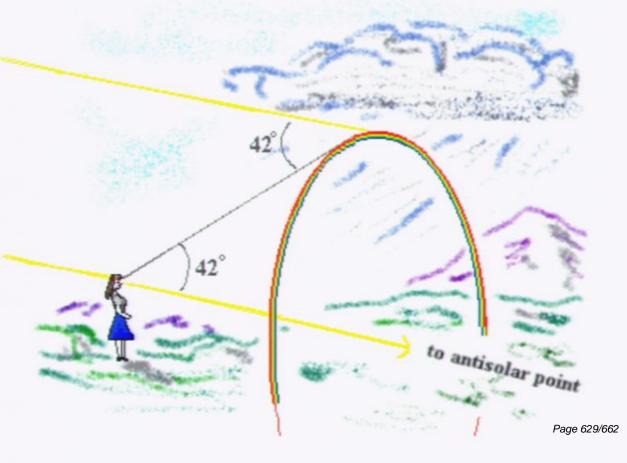


Pirsa: 10080031

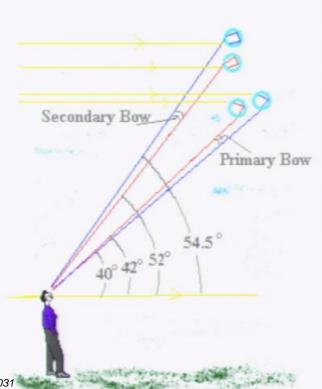
Page 628/662

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The double rainbow





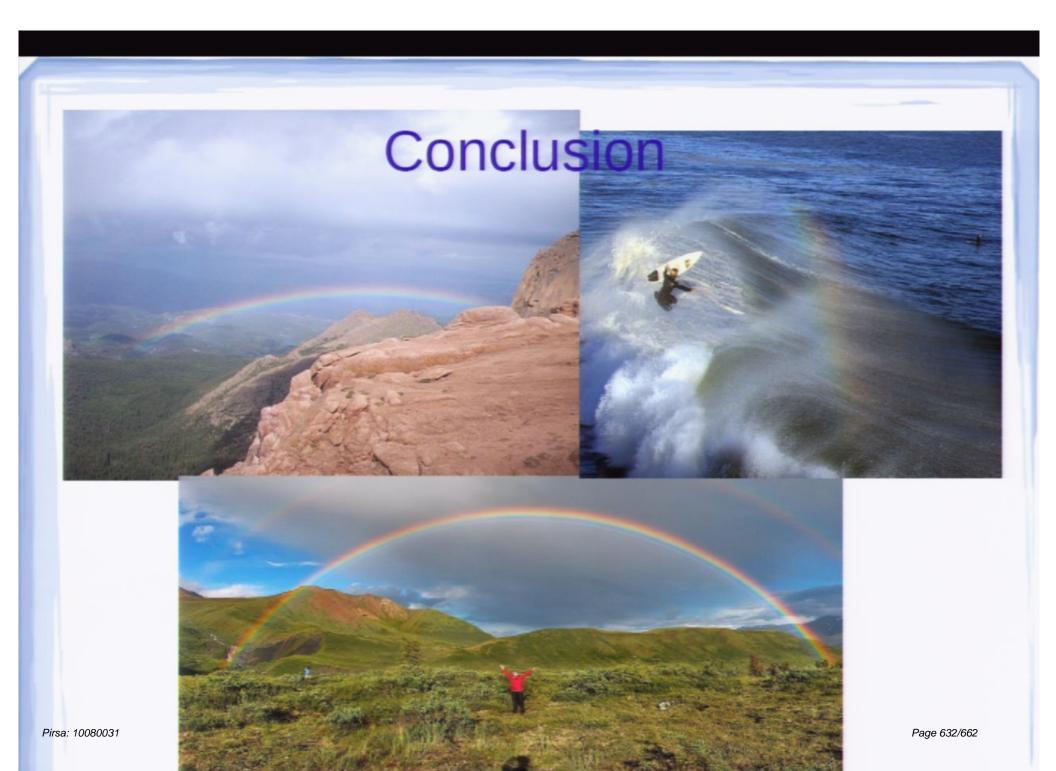
The dark space between the rainbows is called Alexander's band and is caused by light reflected through larger angles than the Page 630/662 maximum intensity

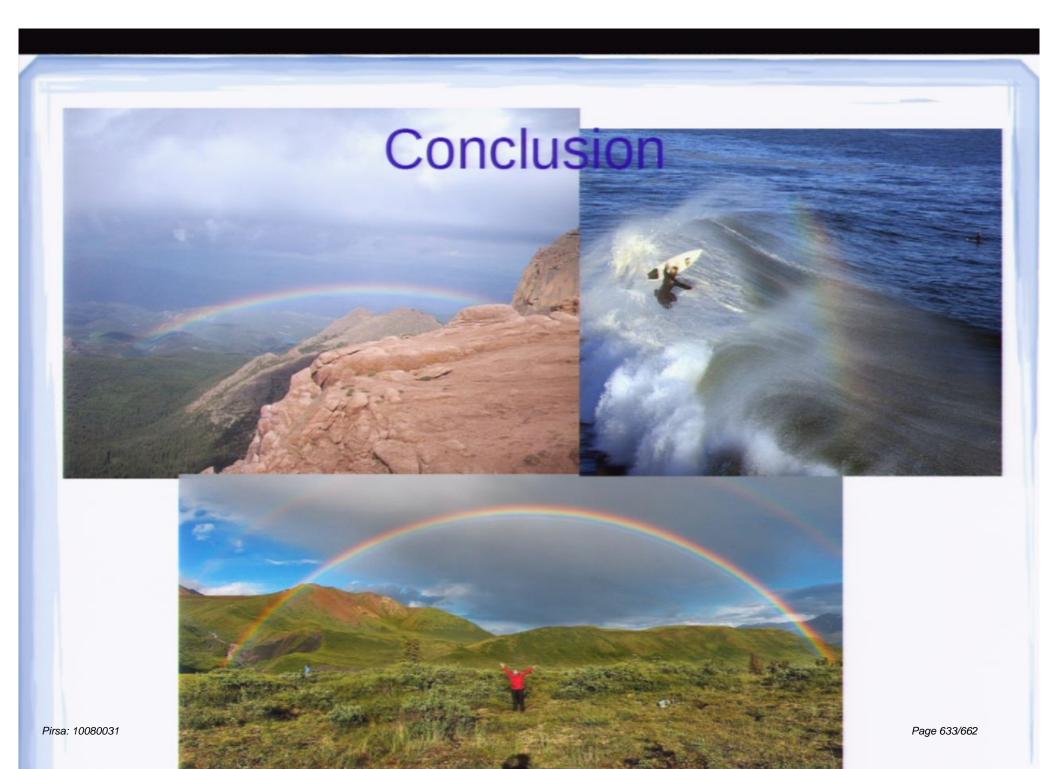
Higher Order Rainbows

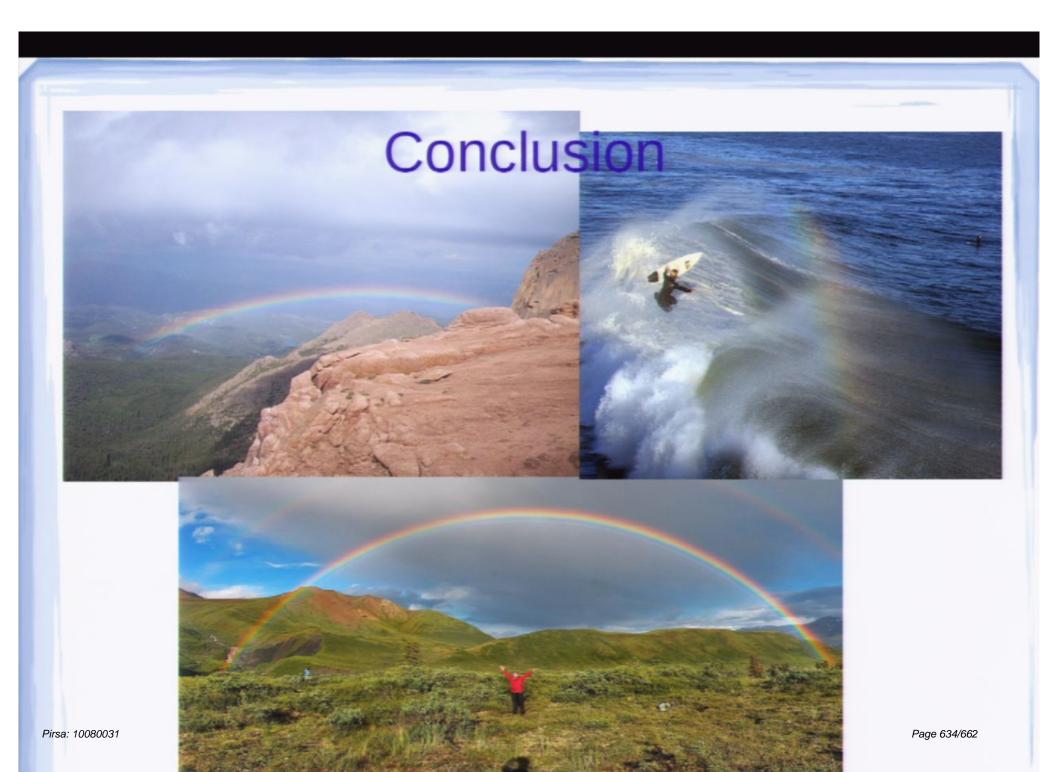
A fifth order rainbow (right) falls within Alexander's band.

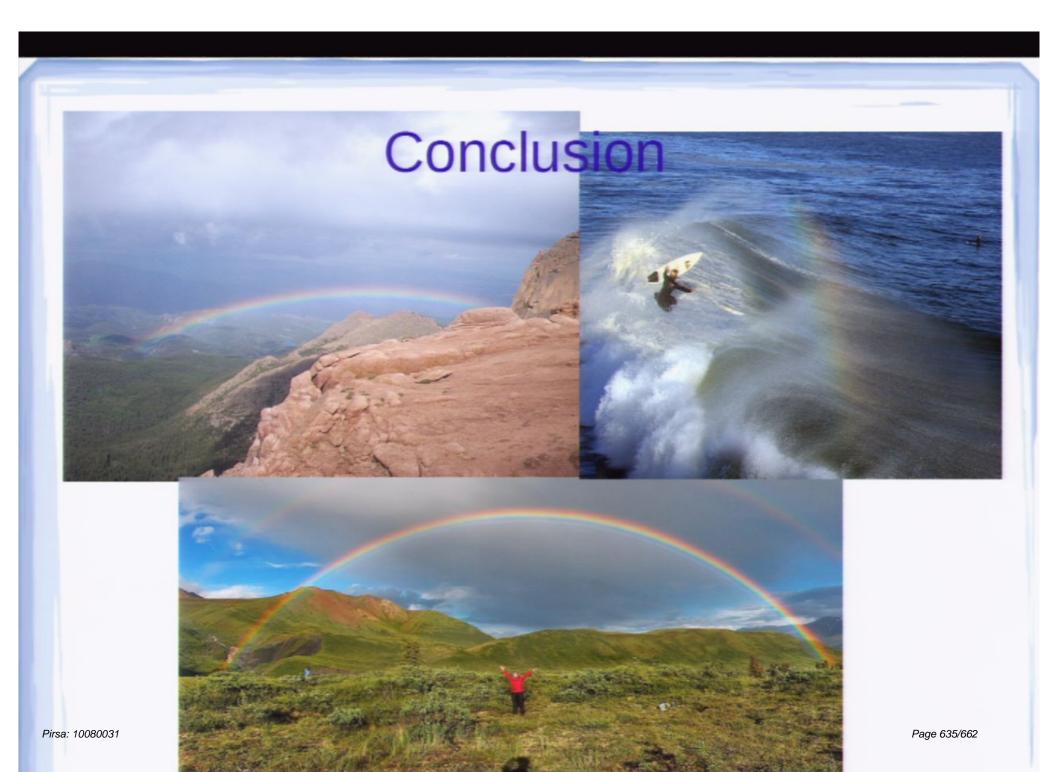


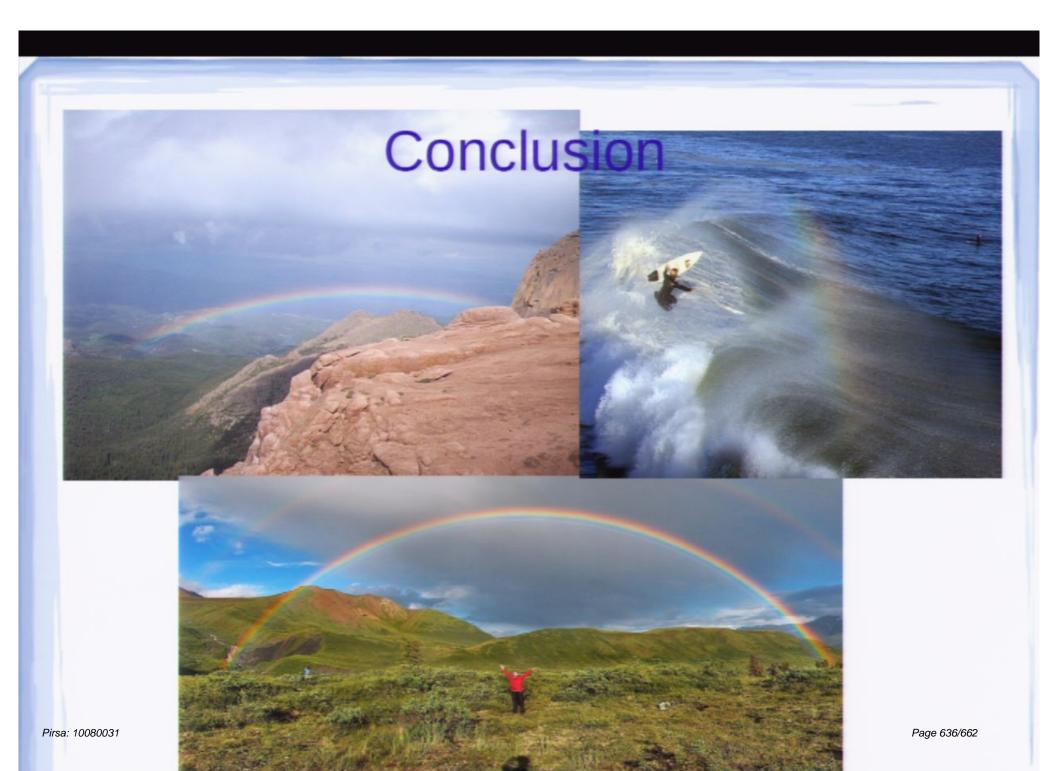
Using extremely strong laser light and suspended droplets, rainbows of order over 200 have been created in labs

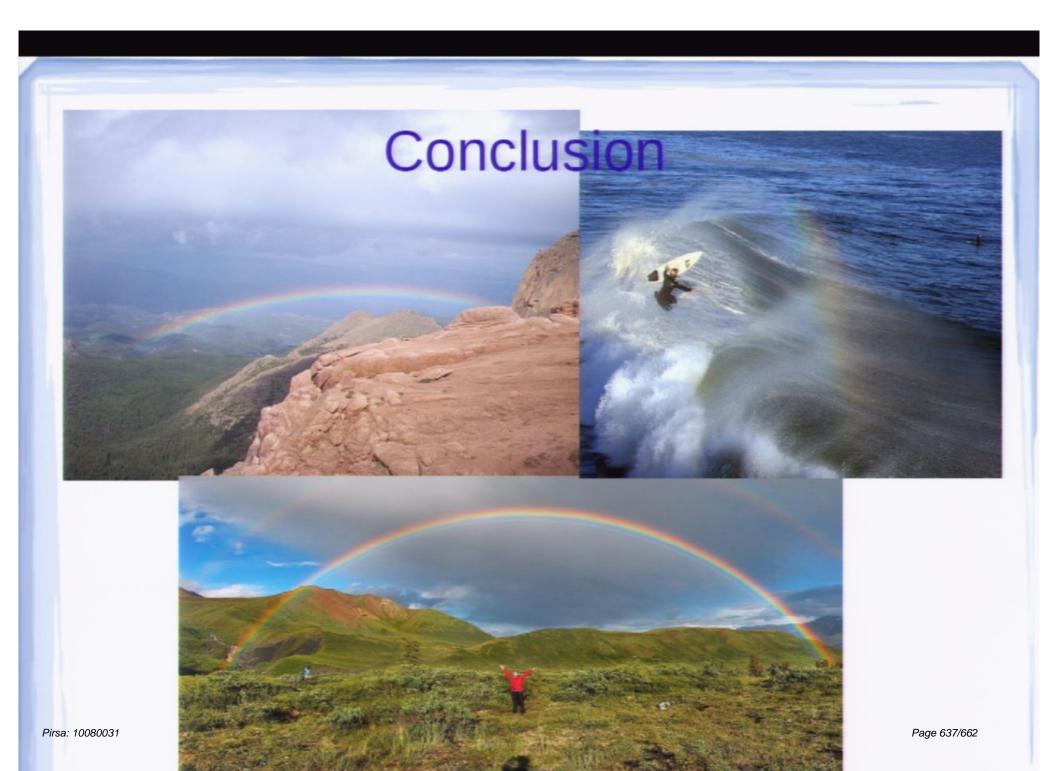


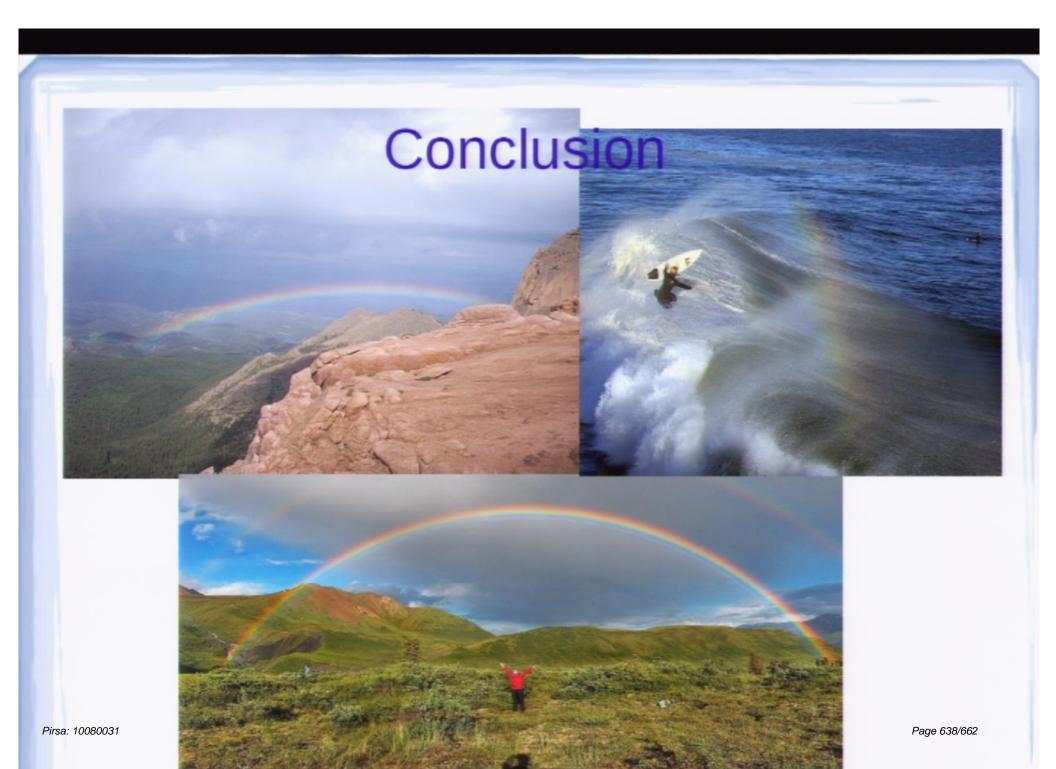


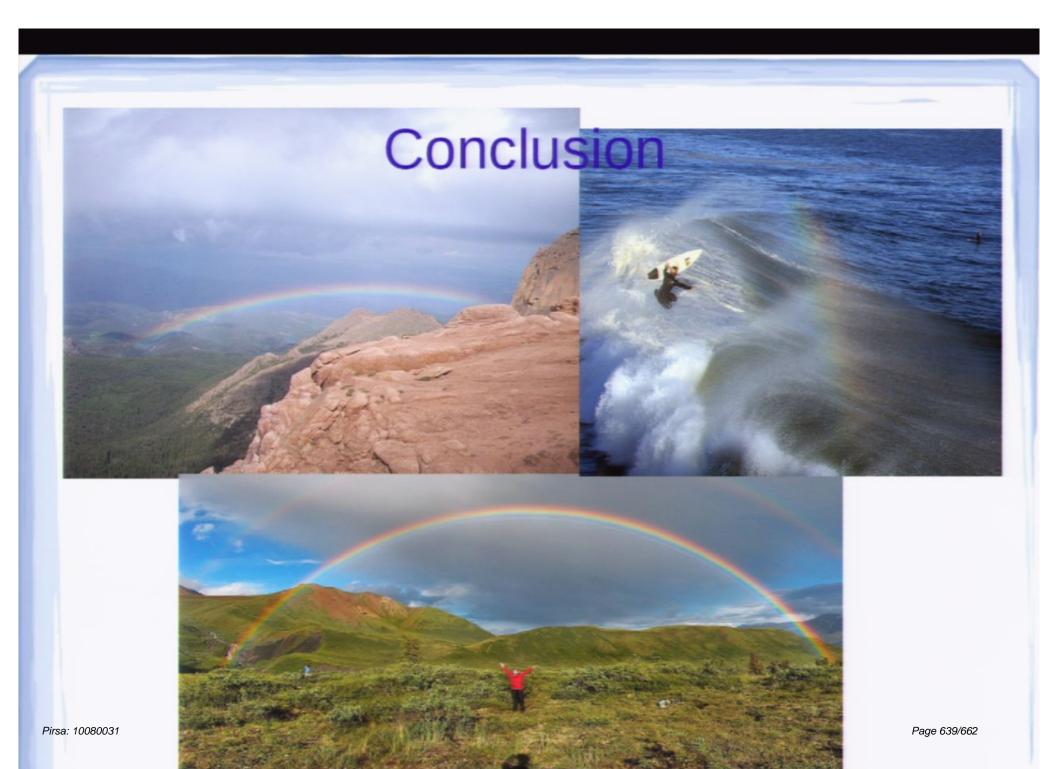


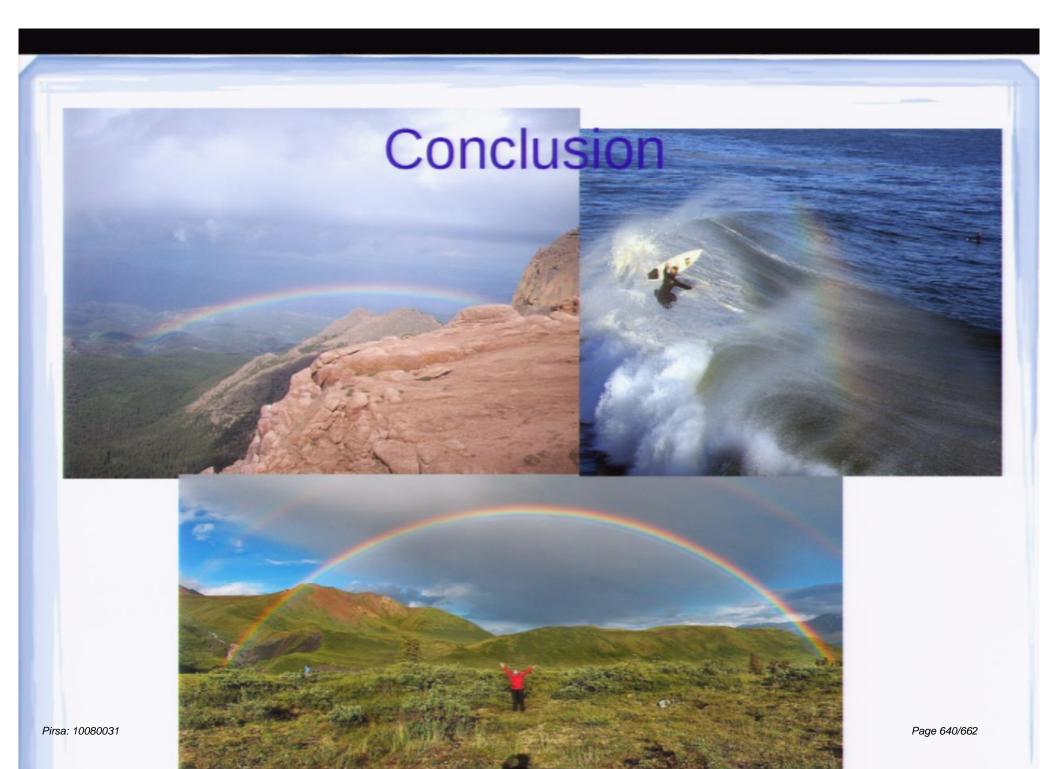


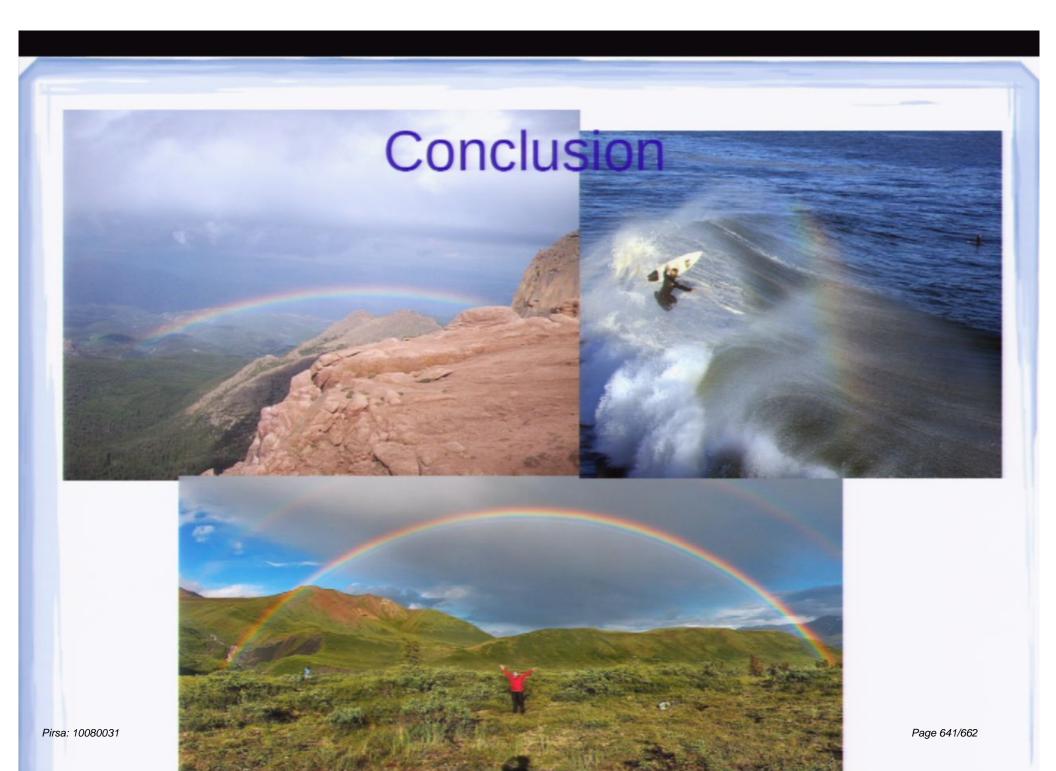


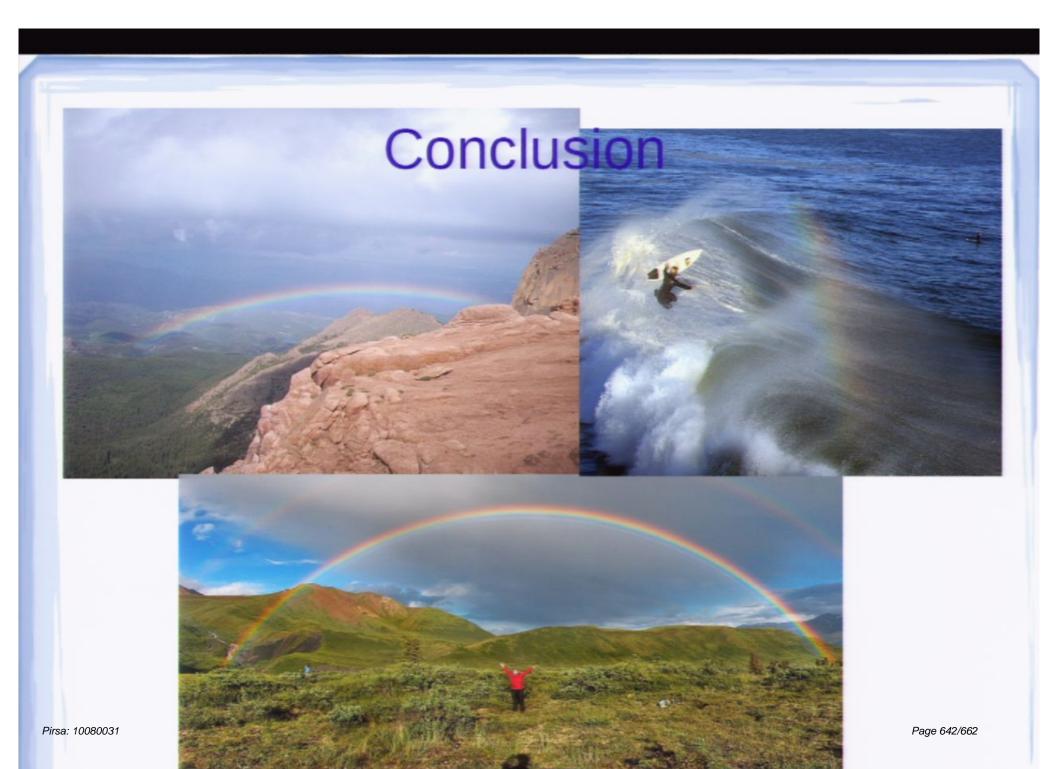


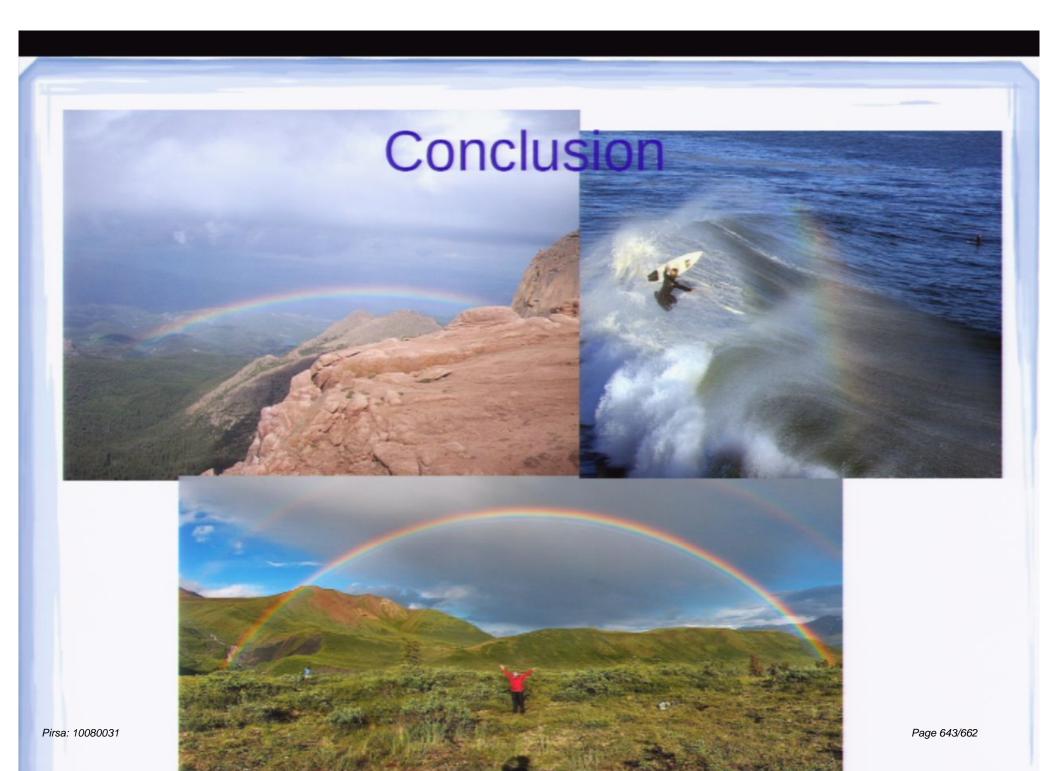


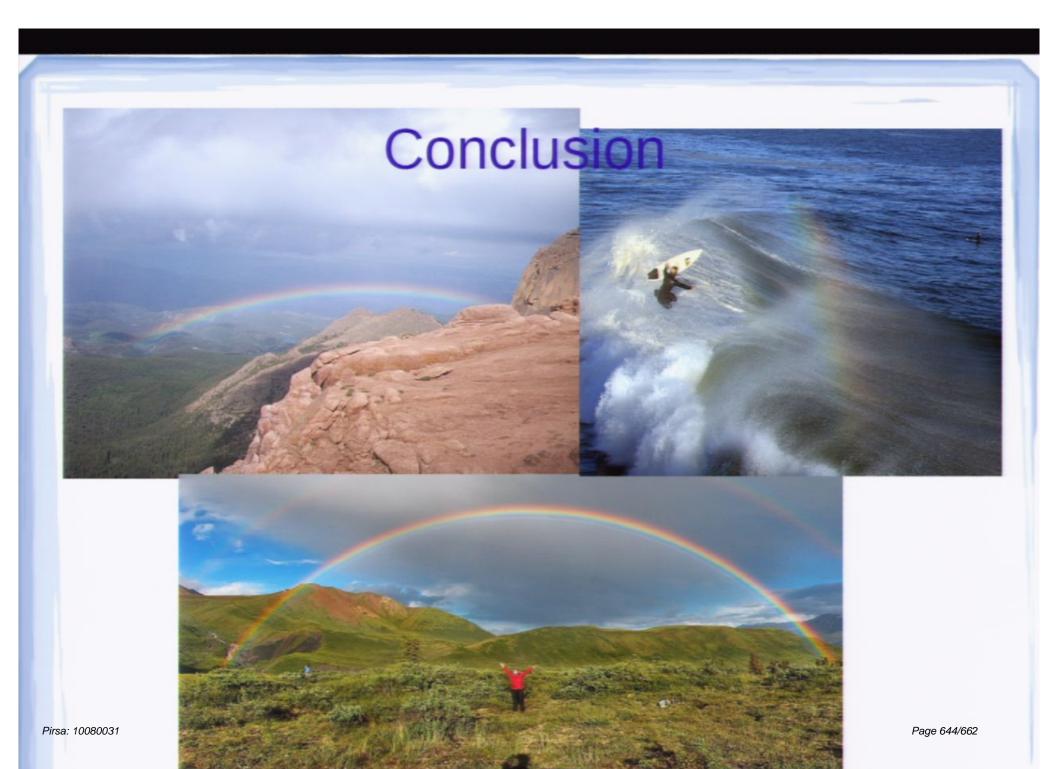






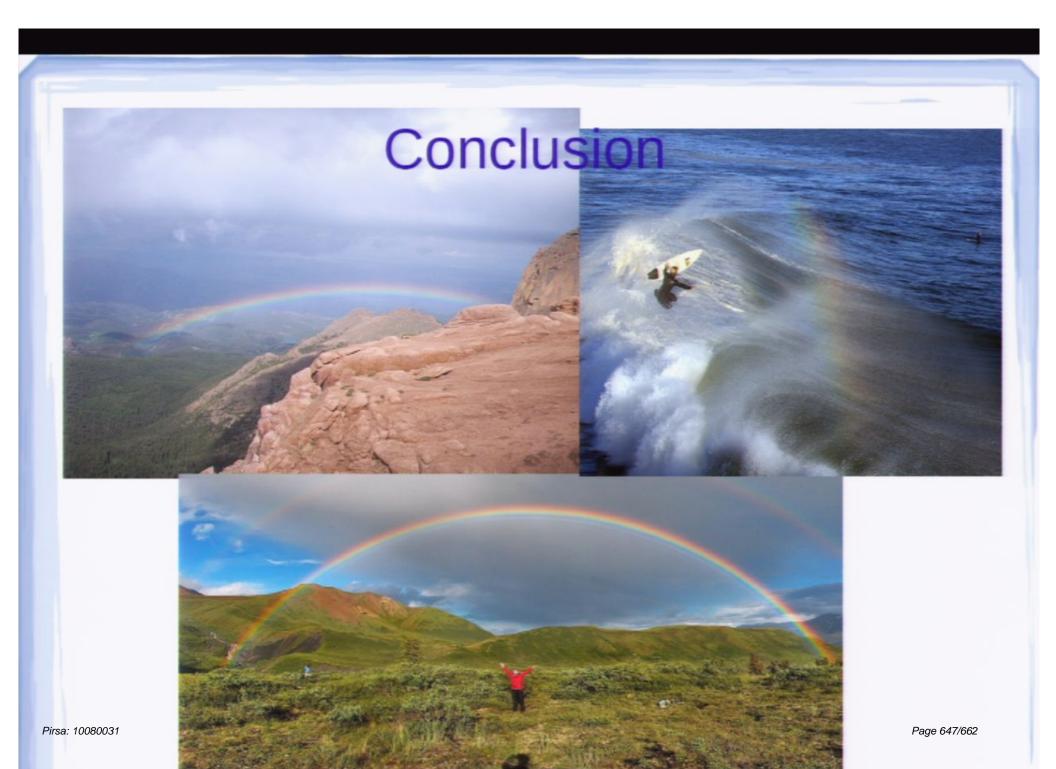


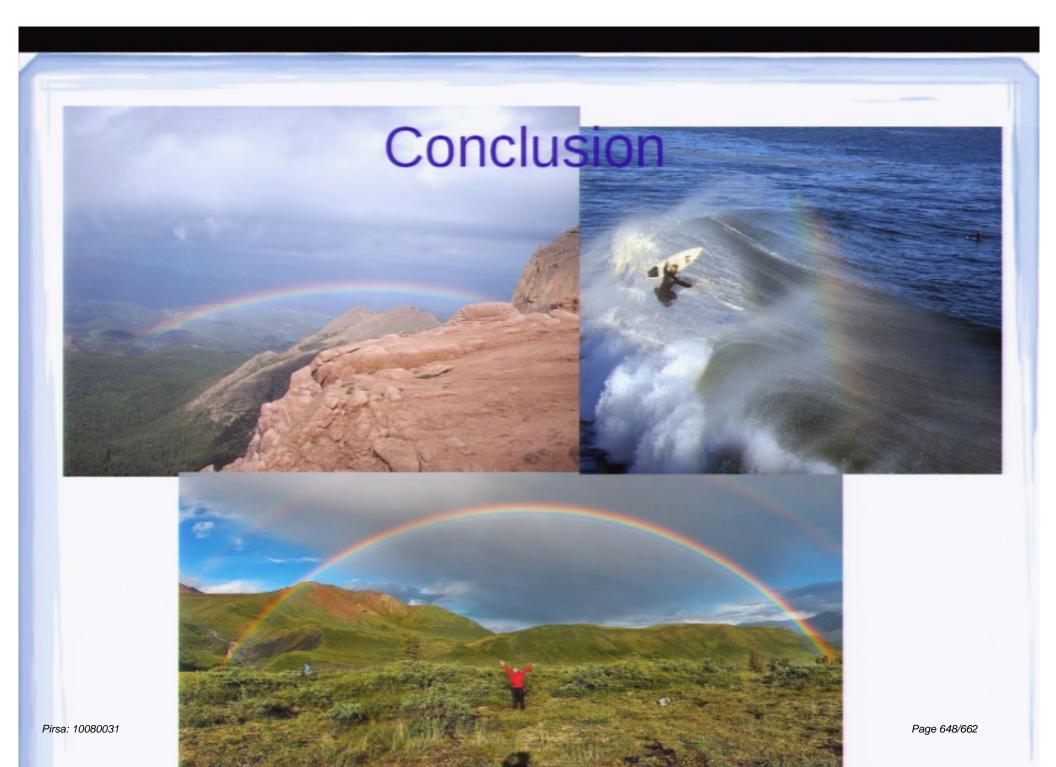


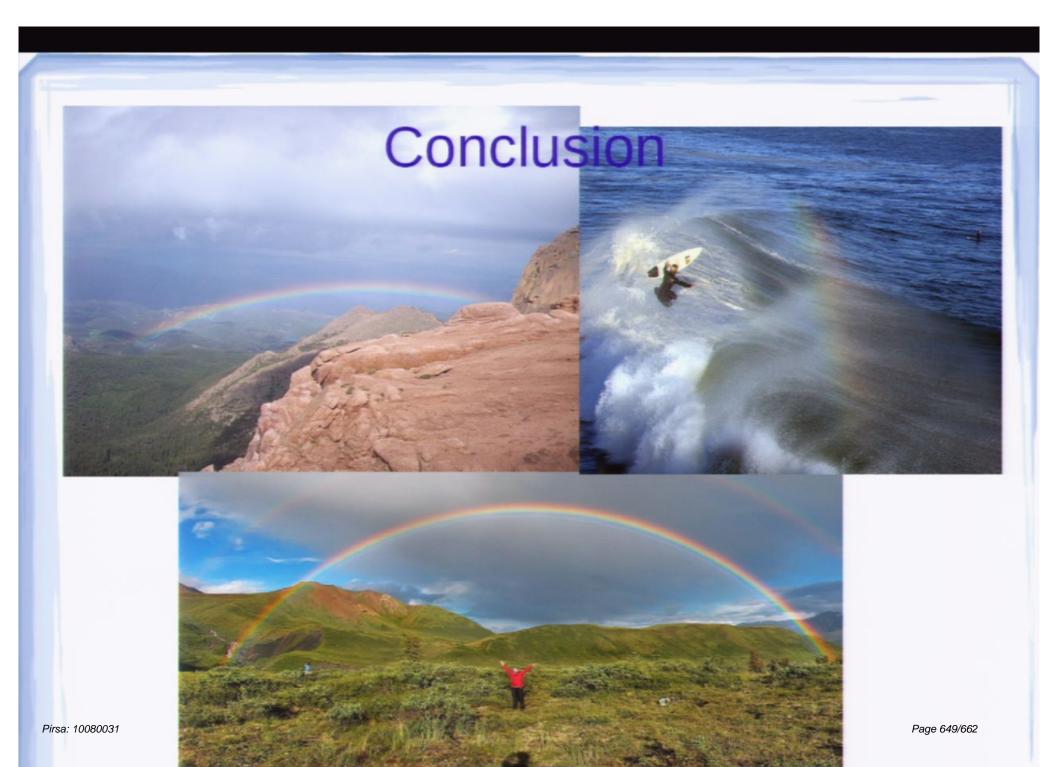


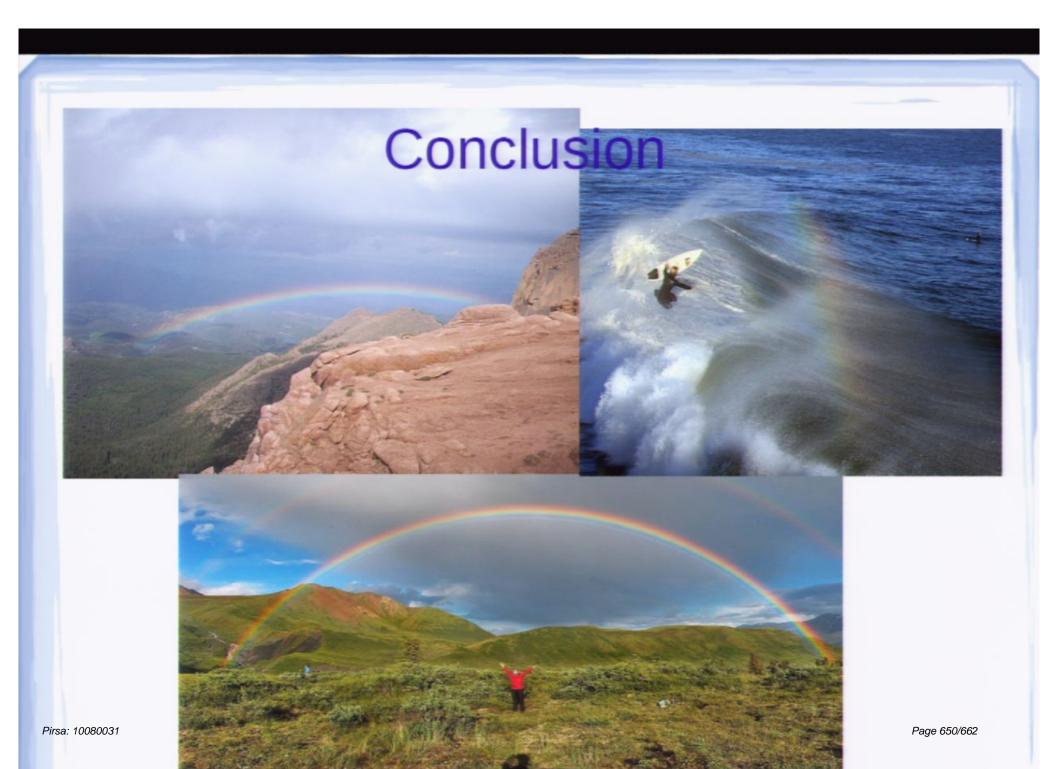


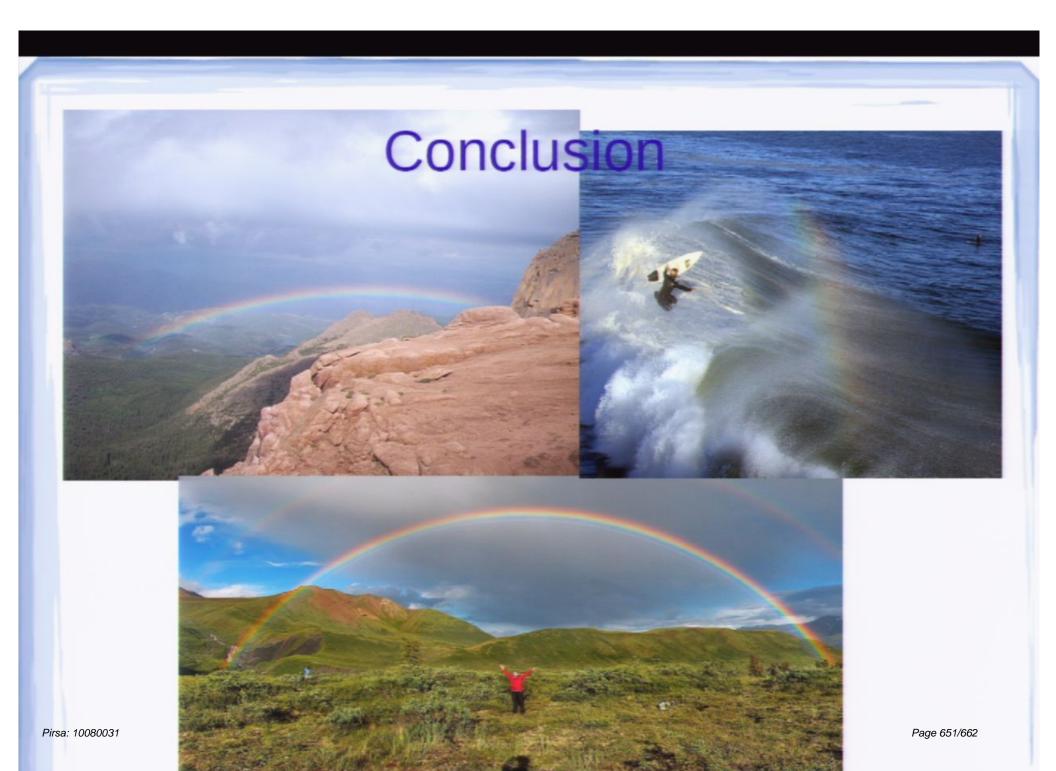


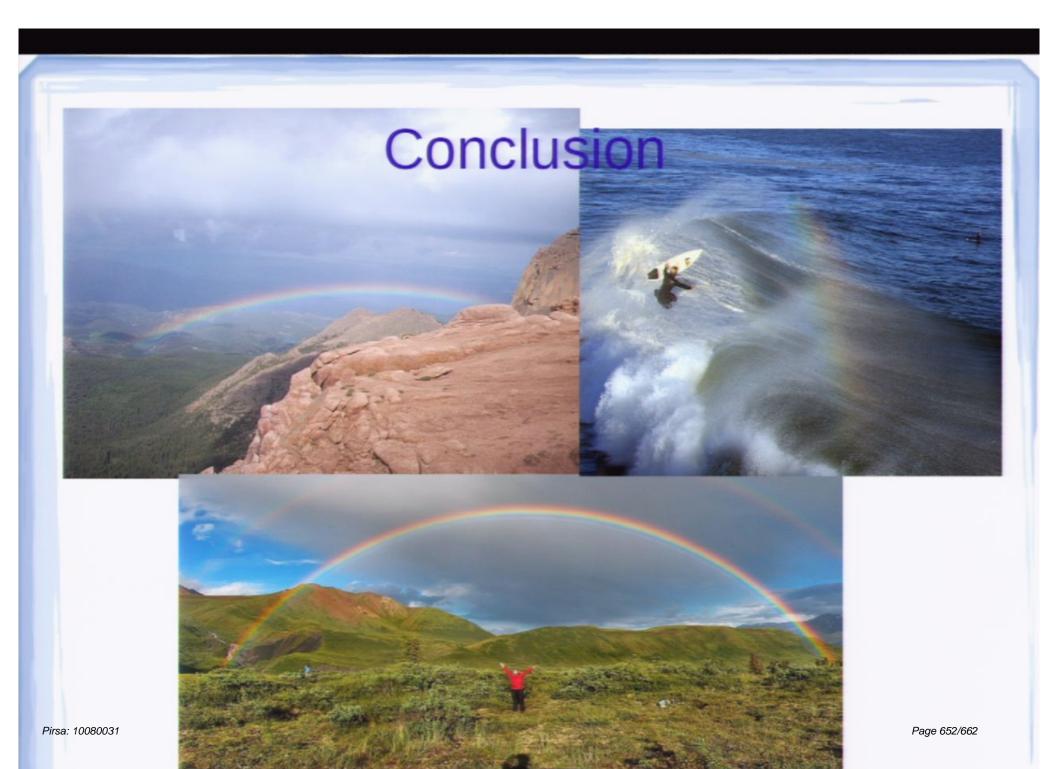


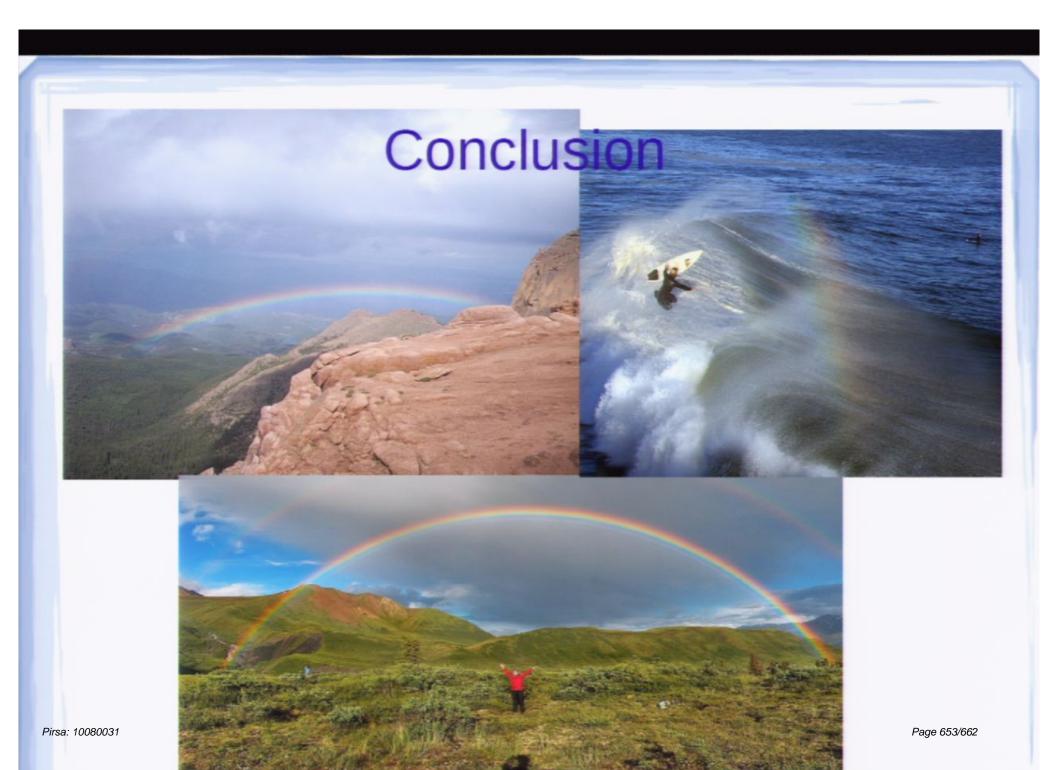


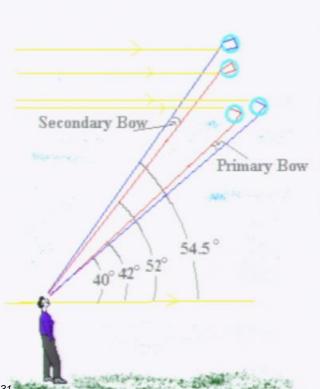






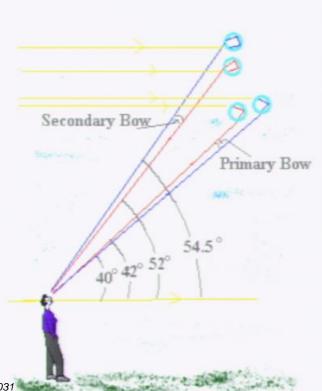








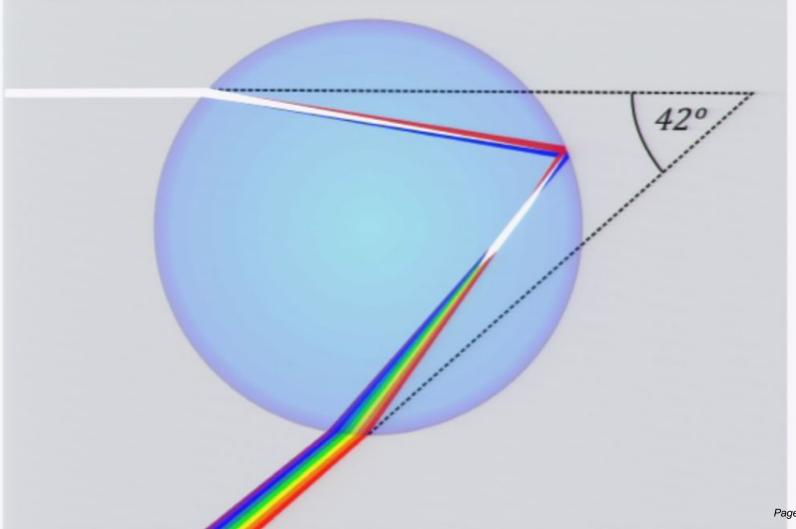
The dark space between the rainbows is called Alexander's band and is caused by light reflected through larger angles than the Page 654/662 maximum intensity





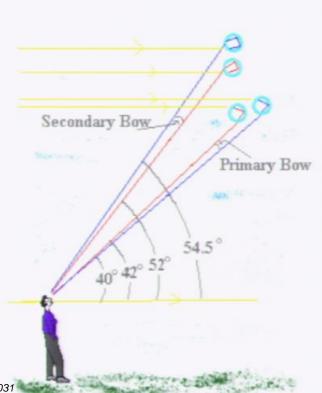
The dark space between the rainbows is called Alexander's band and is caused by light reflected through larger angles than the Page 655/662 maximum intensity

Inside a rain drop



Pirsa: 10080031

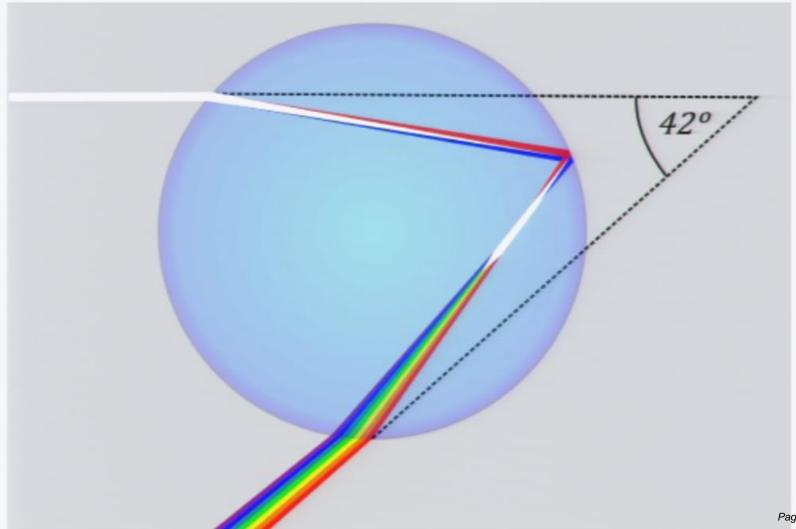
Page 656/662





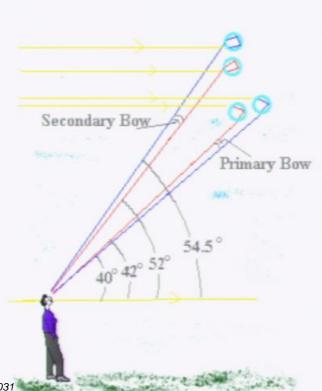
The dark space between the rainbows is called Alexander's band and is caused by light reflected through larger angles than the Page 657/662 maximum intensity

Inside a rain drop



Pirsa: 10080031

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The dark space between the rainbows is called Alexander's band and is caused by light reflected through larger angles than the Page 659/662 maximum intensity

