

Title: Gravitational Waves from Core-Collapse Supernovae

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URL: <http://pirsa.org/10060086>

Abstract: We present a short overview on the current state of core-collapse supernova modeling and the set of processes expected to emit gravitational waves in a core collapse event. We go on to show new results from 3D GR simulations focusing on failing black-hole forming supernovae and present the gravitational wave signature of such events.

Gravitational Waves from Core-Collapse Supernovae and Black Hole Formation

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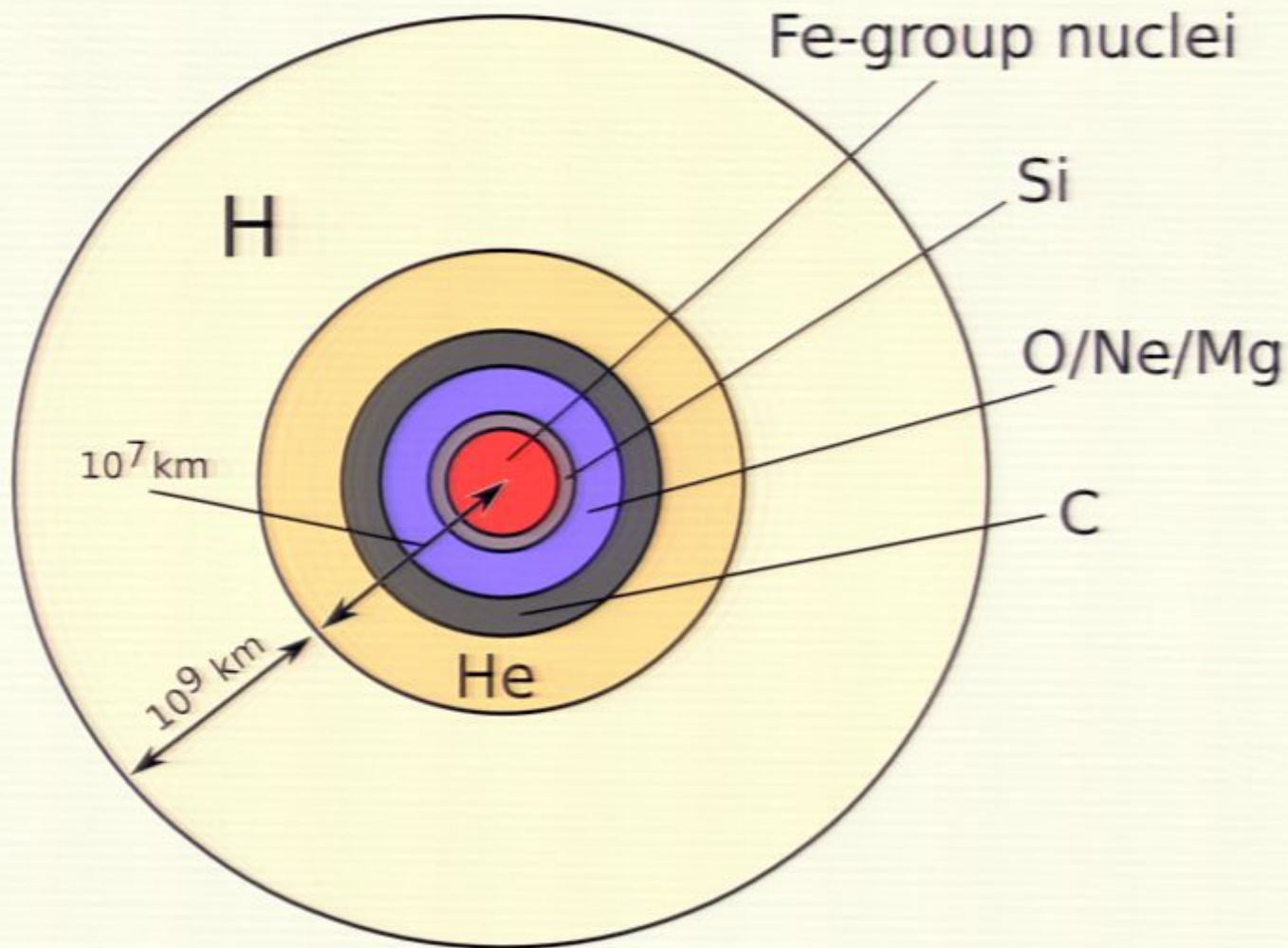
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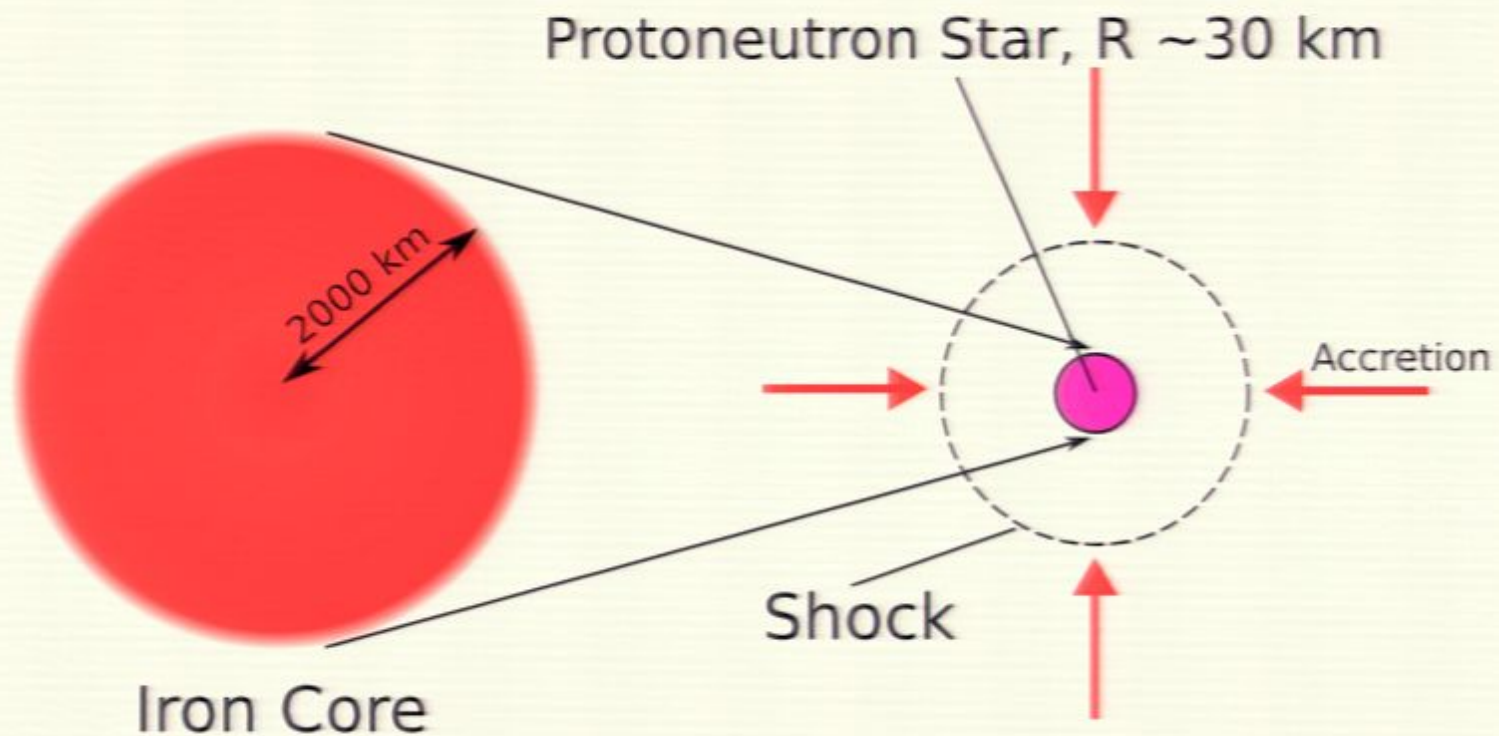
The Core-Collapse Scenario



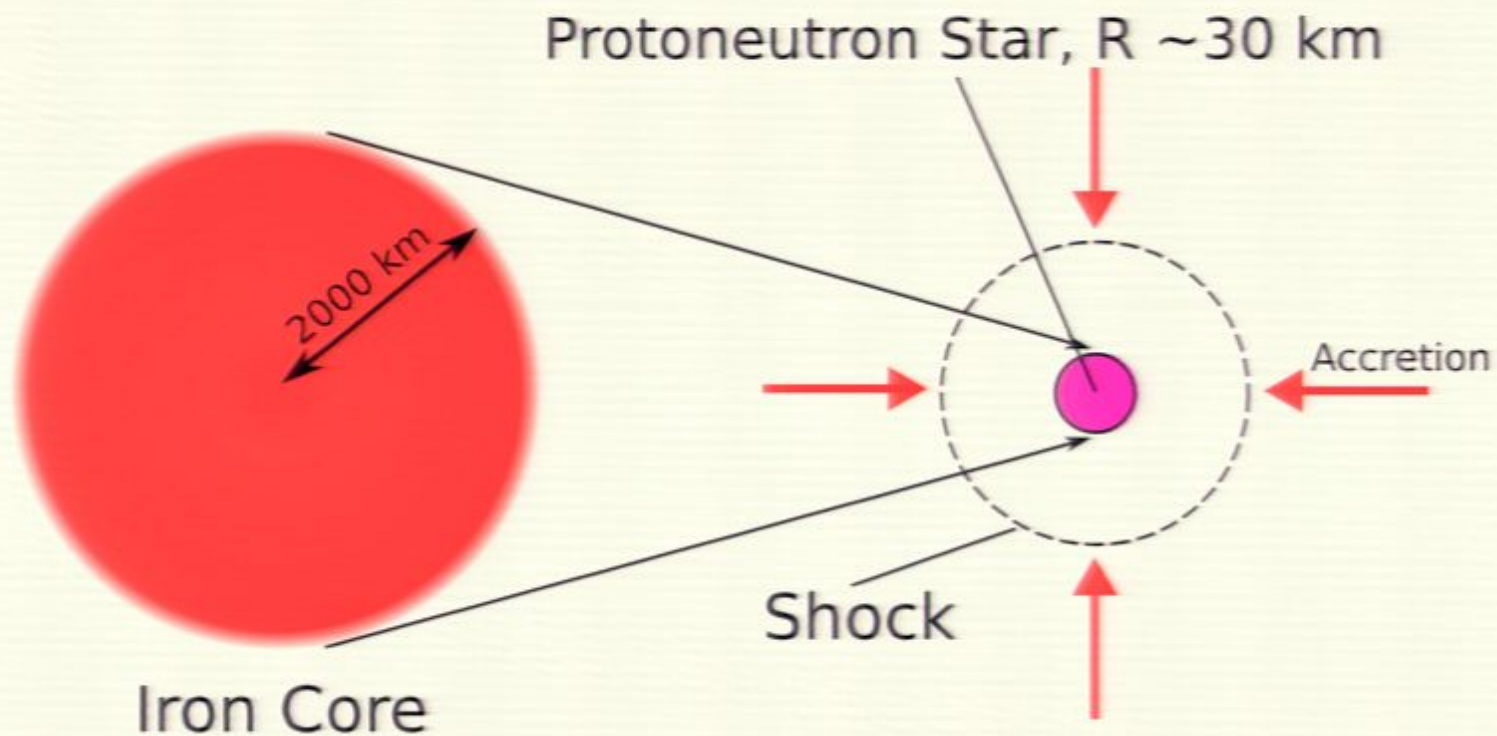
Evolved Massive Star

$M > 8-10 M_{\text{SUN}}$

The Core-Collapse Scenario



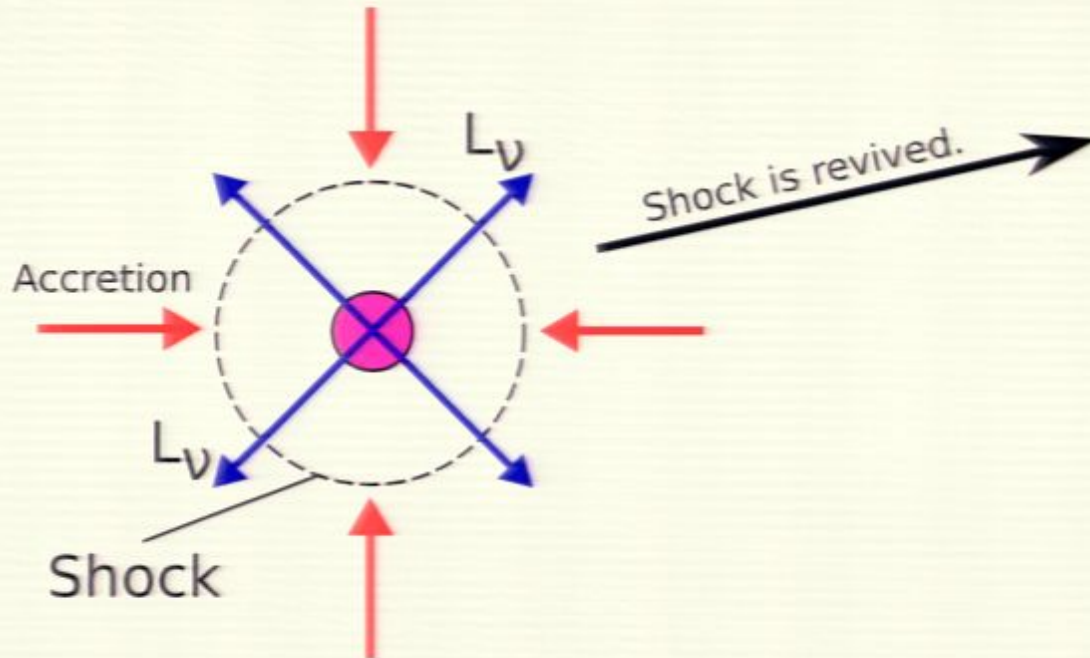
The Core-Collapse Scenario



The Supernova Problem

Protoneutron Star, $R \sim 30$ km

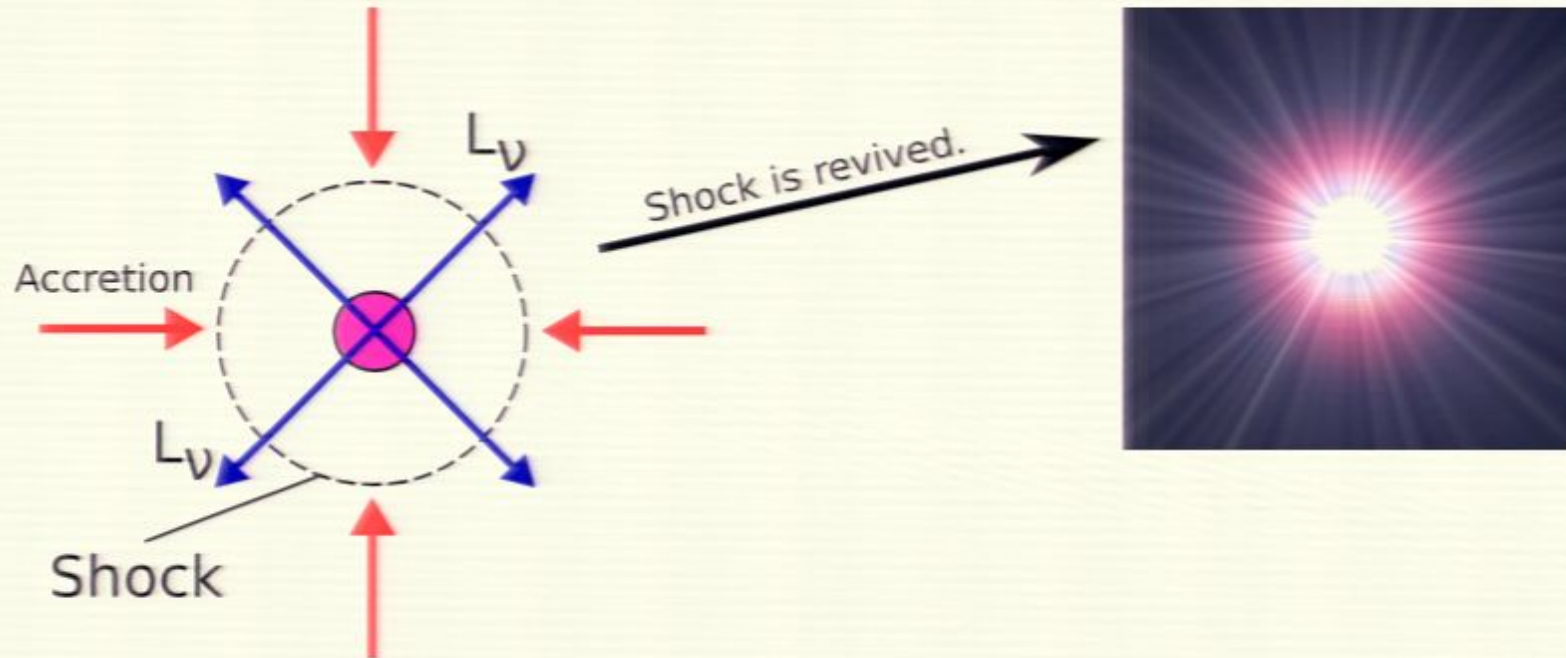
Supernova Explosion



The Supernova Problem

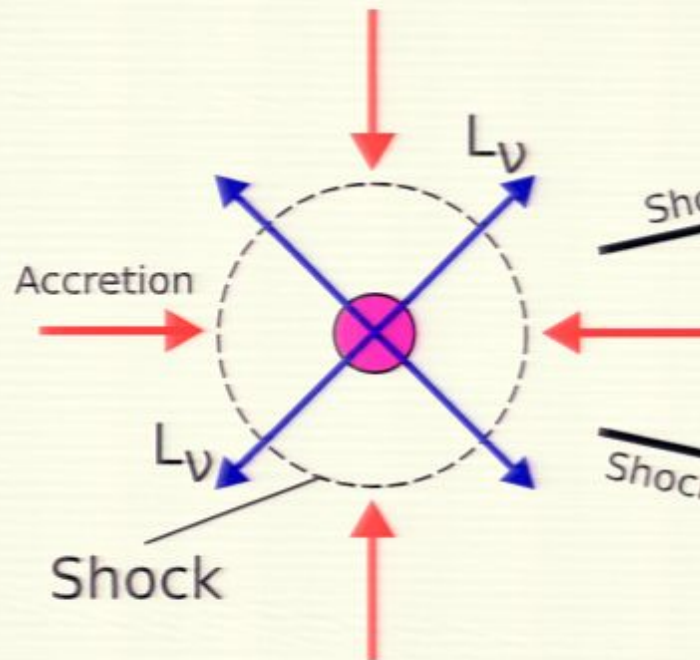
Protoneutron Star, $R \sim 30$ km

Supernova Explosion



The Supernova Problem

Protoneutron Star, $R \sim 30$ km



Supernova Explosion



Shock is revived.

Shock is not revived.

Collapse to Black Hole
(Collapsar)

Needed: **Mechanism for Shock Revival** (The "Supernova Mechanism")

Blowing up Massive Stars: Core-Collapse SN Mechanisms

Neutrino Mechanism

[Colgate & White 1966, Arnett 1966,
Wilson 1985, Bethe & Wilson 1985,
recent: **Marek & Janka 2009**, Ott et al. 2008,
Nordhaus et al. 2010: 3D]

Magnetorotational Mechanism

[LeBlanc & Wilson '70, Bisnovatyi-Kogan et
al. '76, Meier et al. '76, Symbalisty 1984,
recent: Burrows et al. 2007]

Acoustic Mechanism

[proposed by
Burrows et al. 2006, 2007;
not confirmed by other groups/codes]

Blowing up Massive Stars: Core-Collapse SN Mechanisms

Neutrino Mechanism

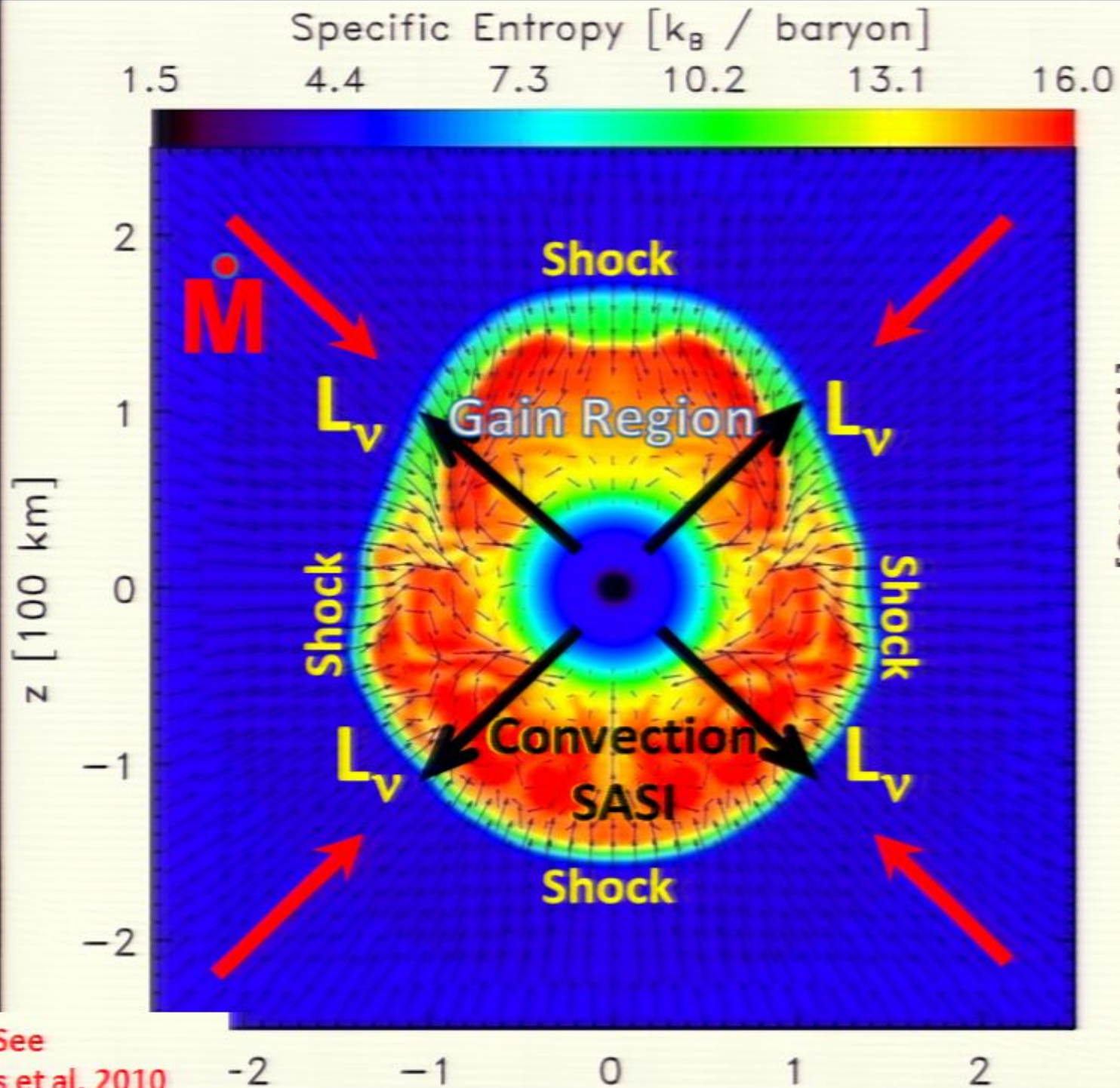
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Magnetorotational Mechanism

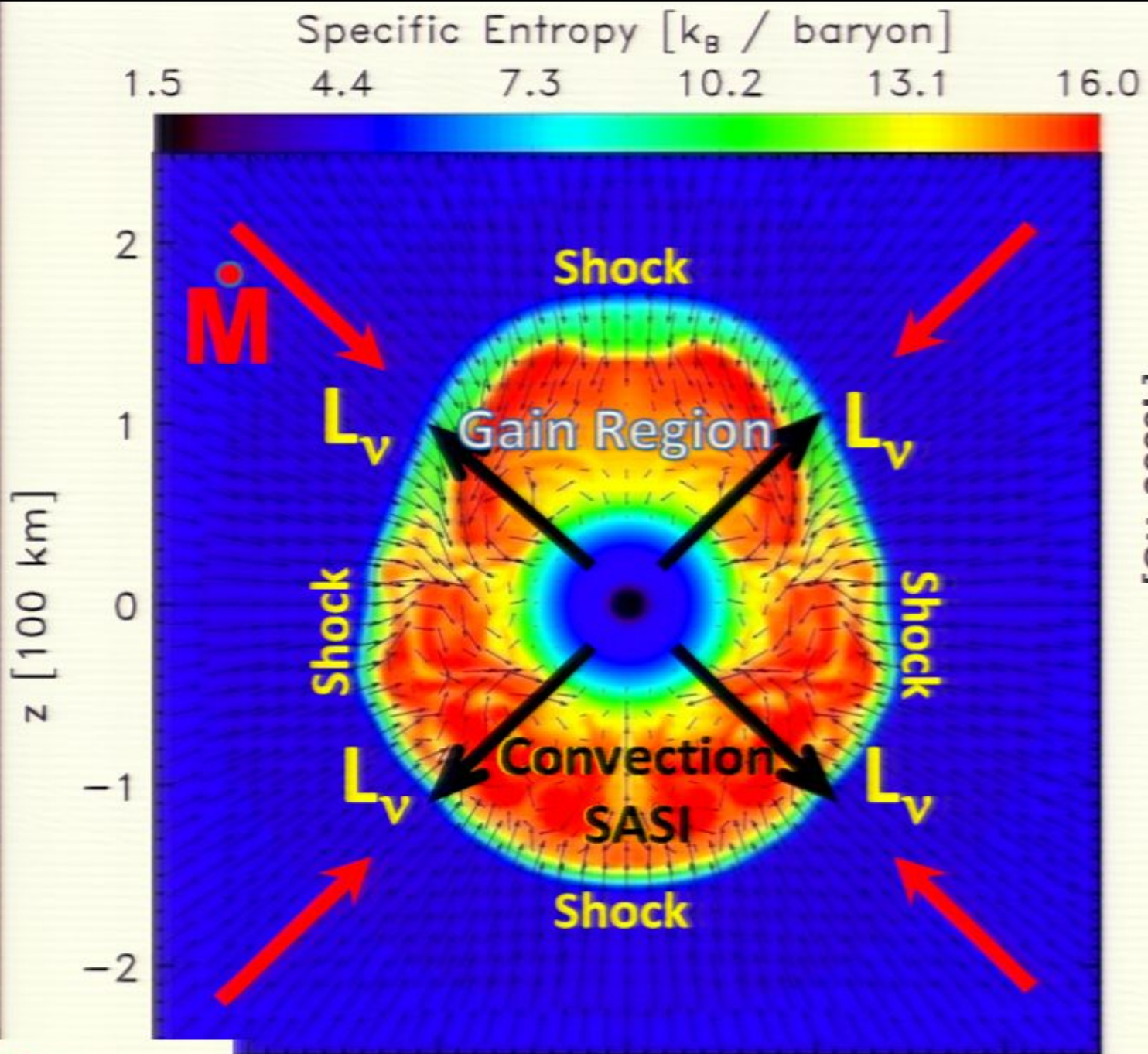
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[Ott 2009b]



GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

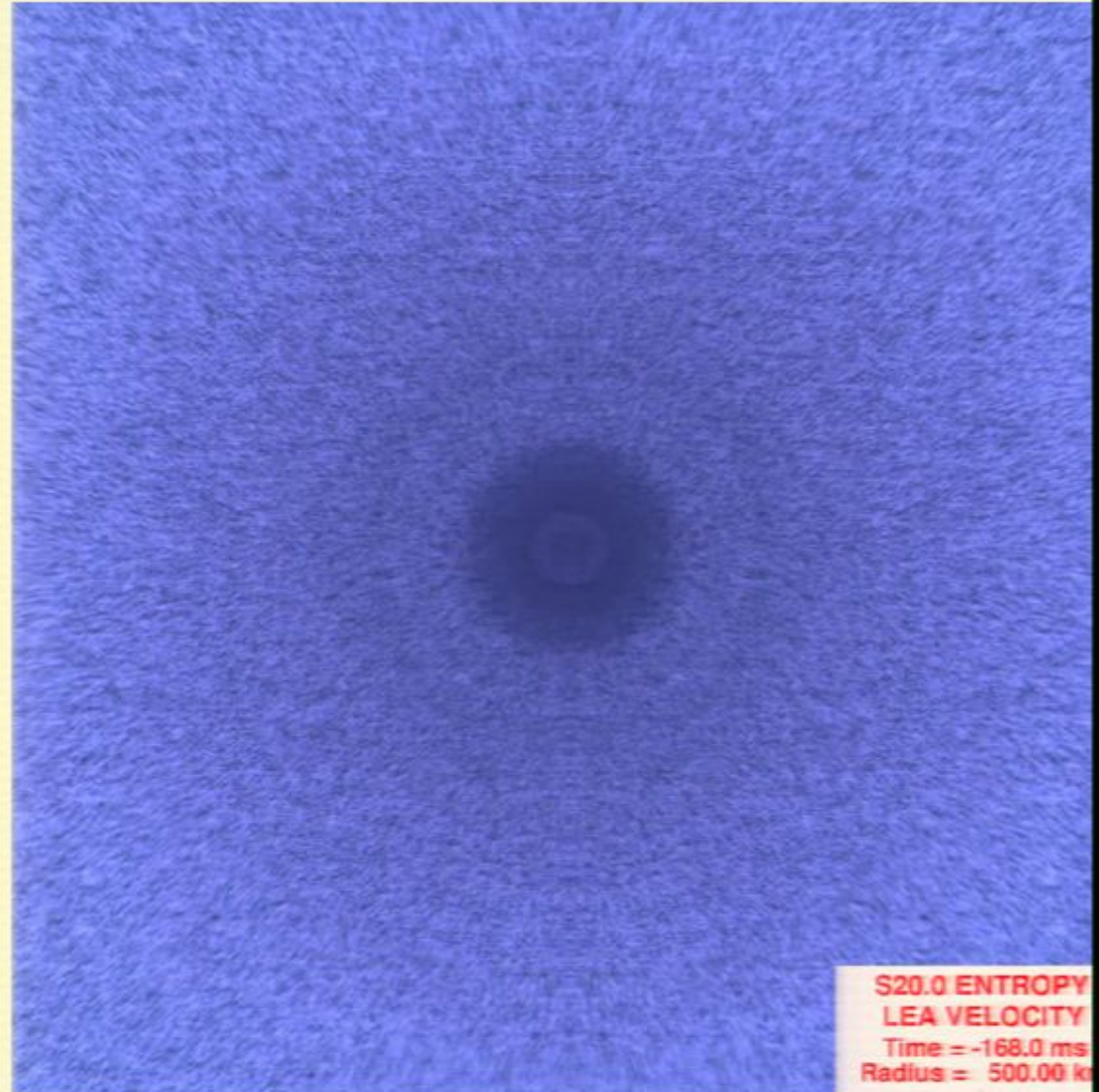
Dominant Multi-D Dynamics:

- Convection/Turbulence in the **protoneutron star** (PNS; $\tau > \sim 10\text{s}$)
- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

$O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = -168.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

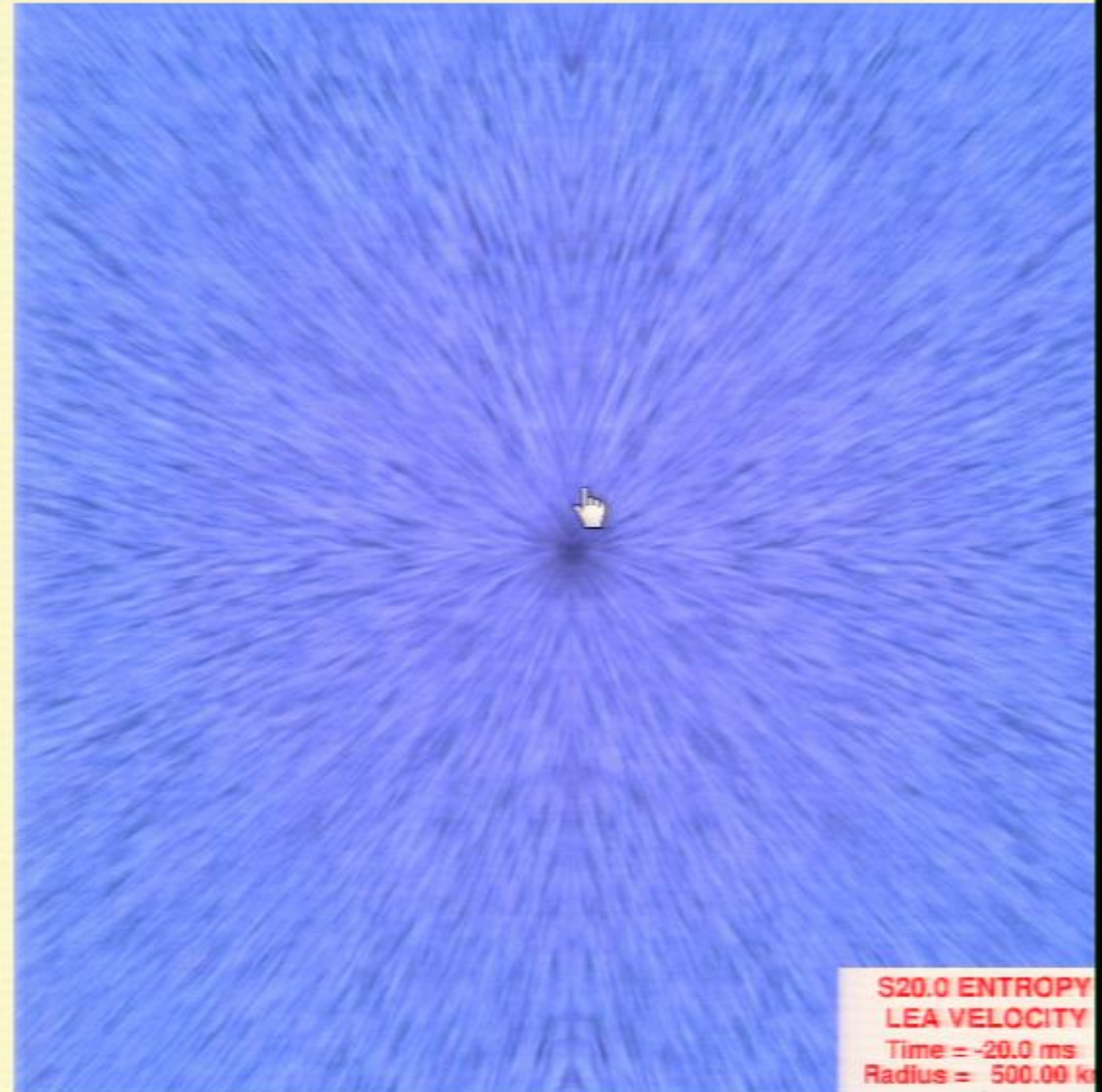
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GW Signature of the Neutrino Mechanism

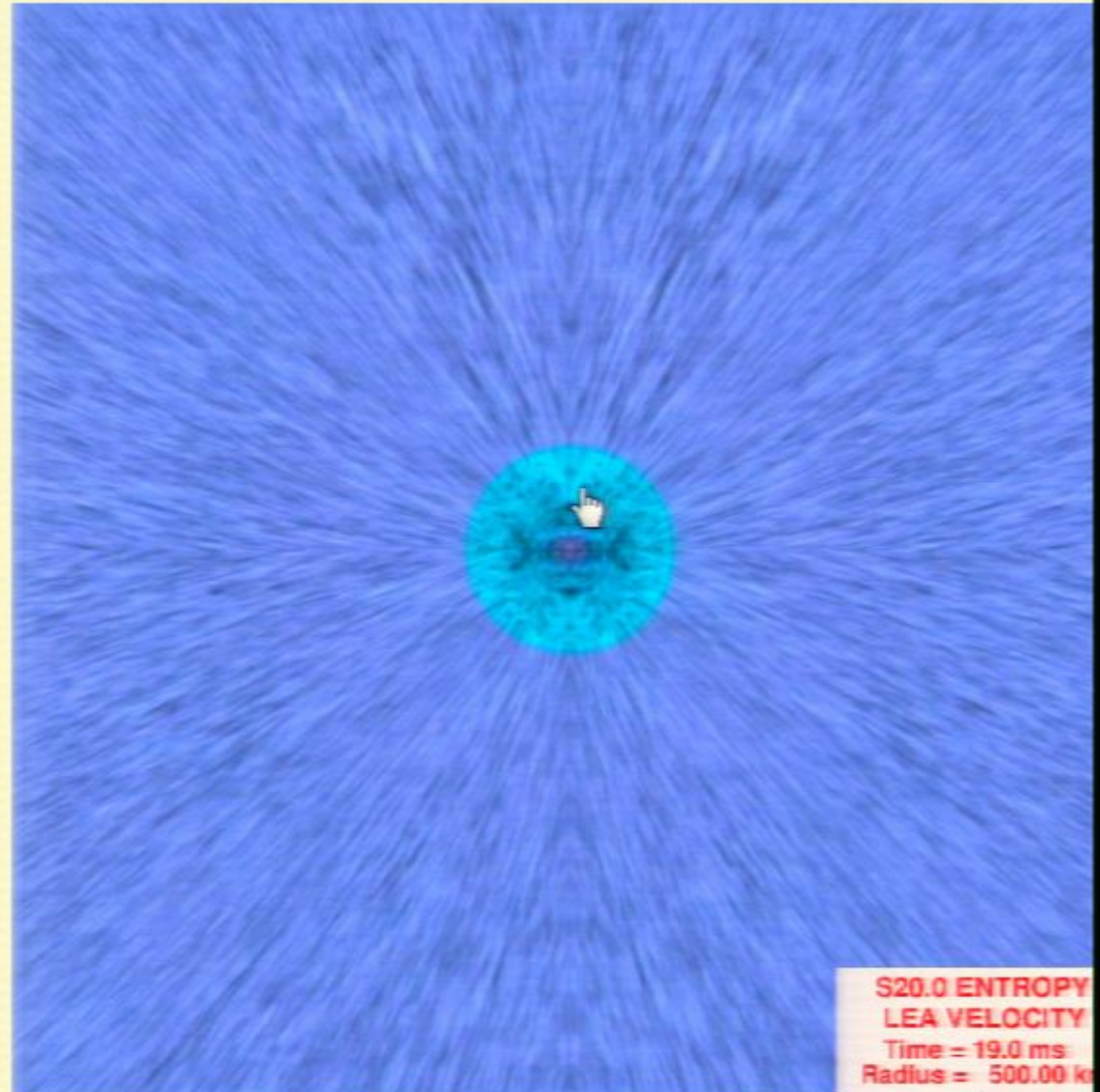
[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

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GW Signature of the Neutrino Mechanism

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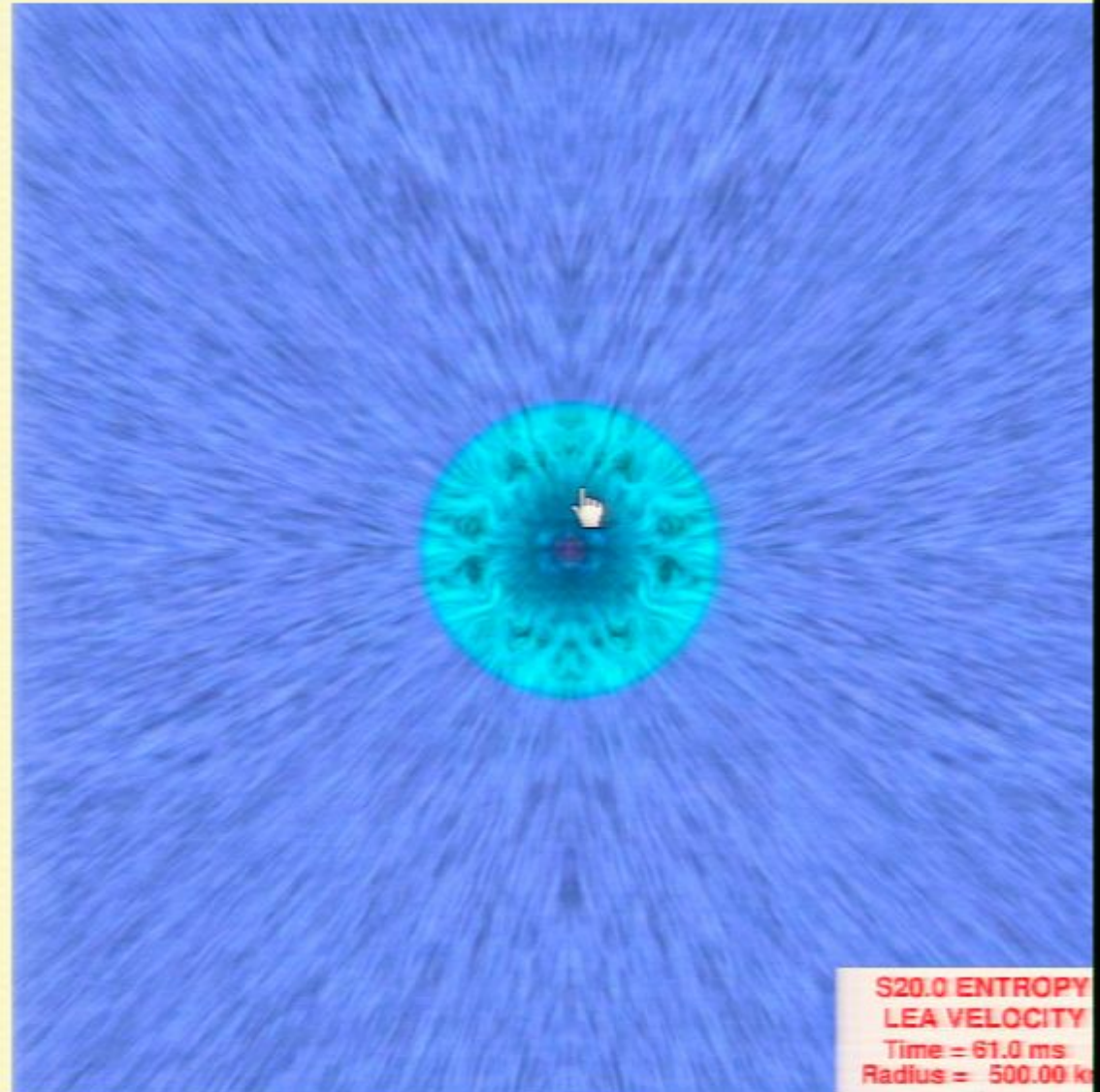
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Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086 $O(10^{-23} - 10^{-22})$ at 10 kpc



GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

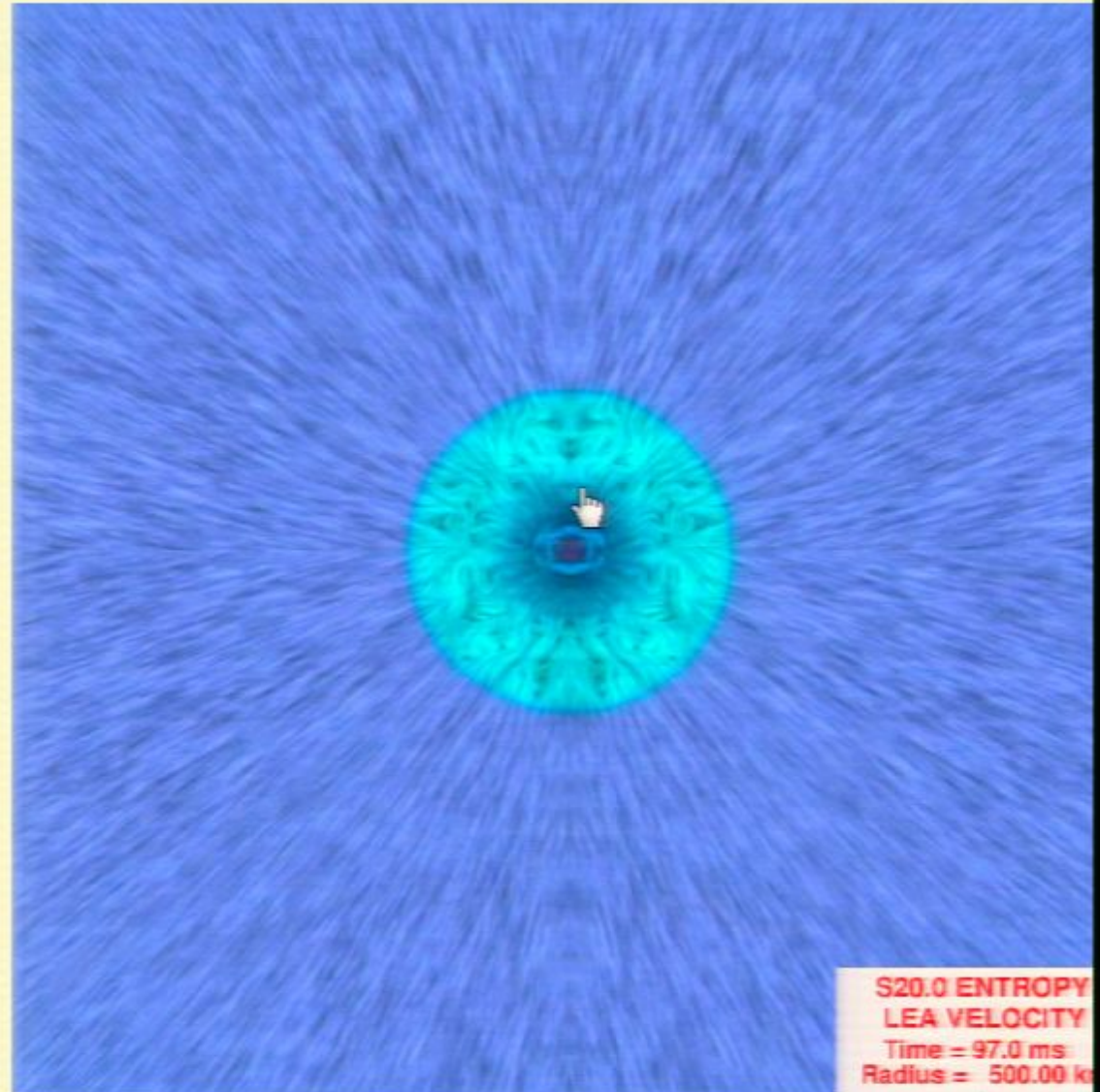
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Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086 $O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 97.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

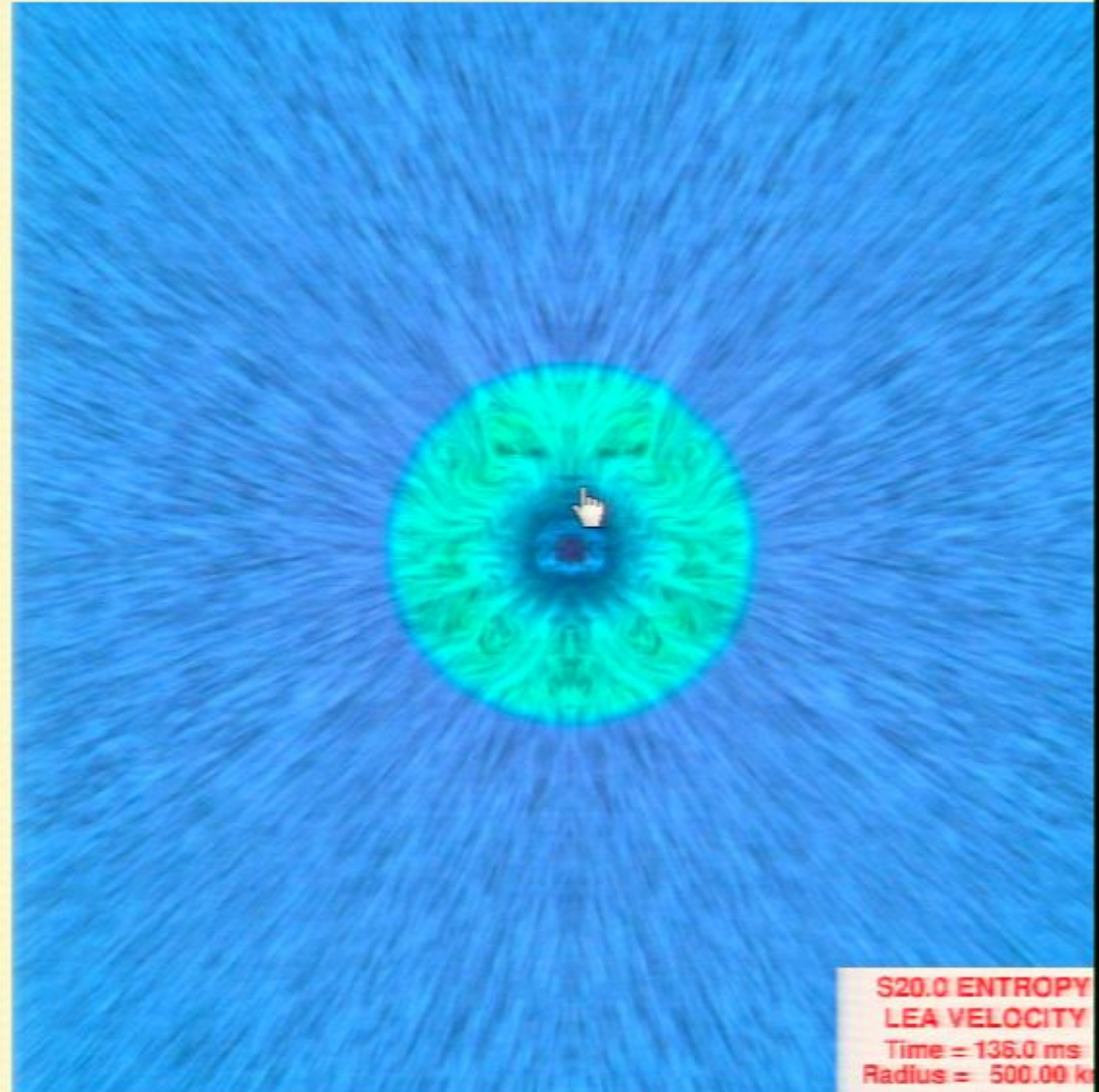
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- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086 $O(10^{-23} - 10^{-22})$ at 10 kpc



GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

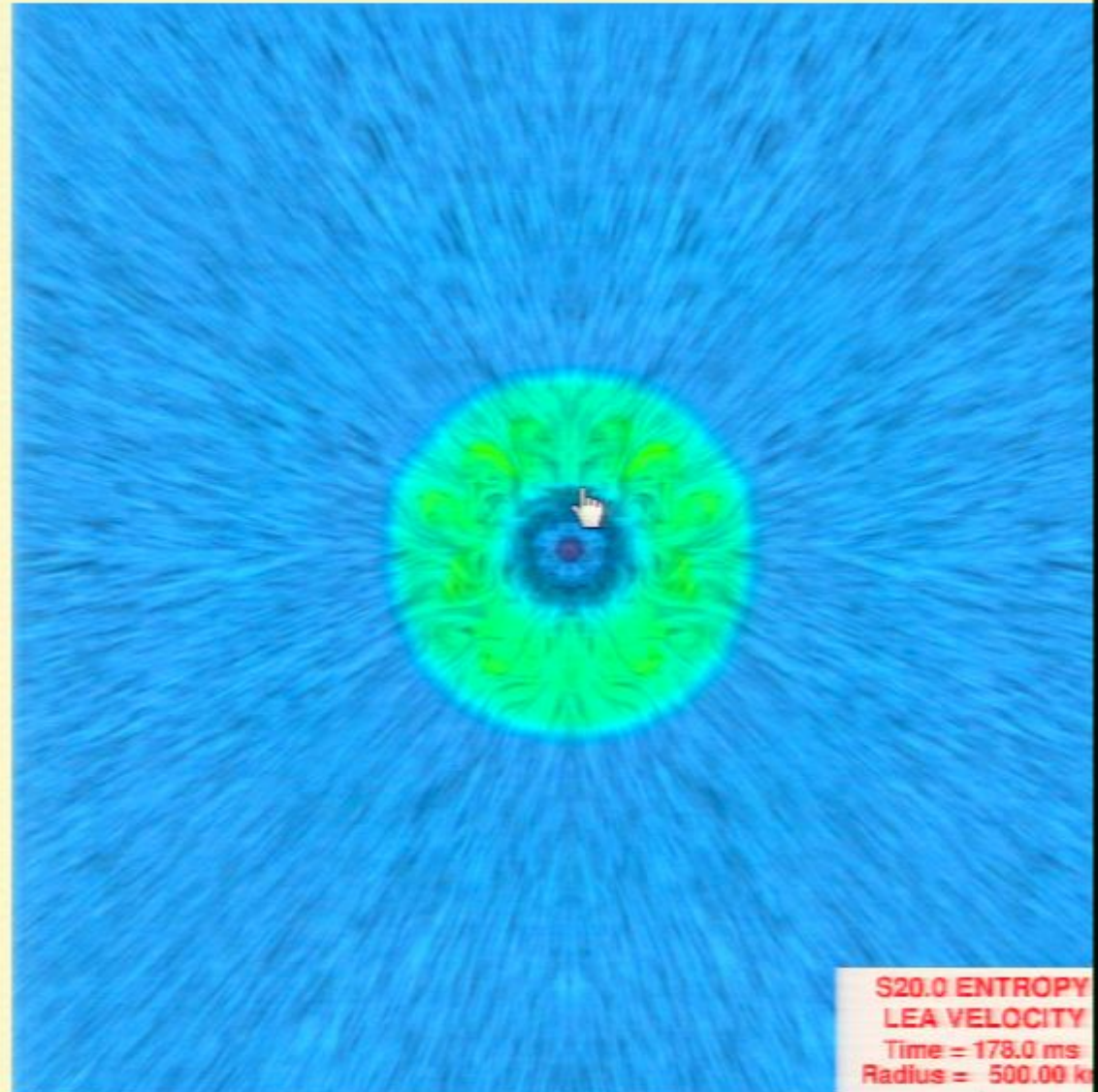
Dominant Multi-D Dynamics:

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- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086 $O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 178.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

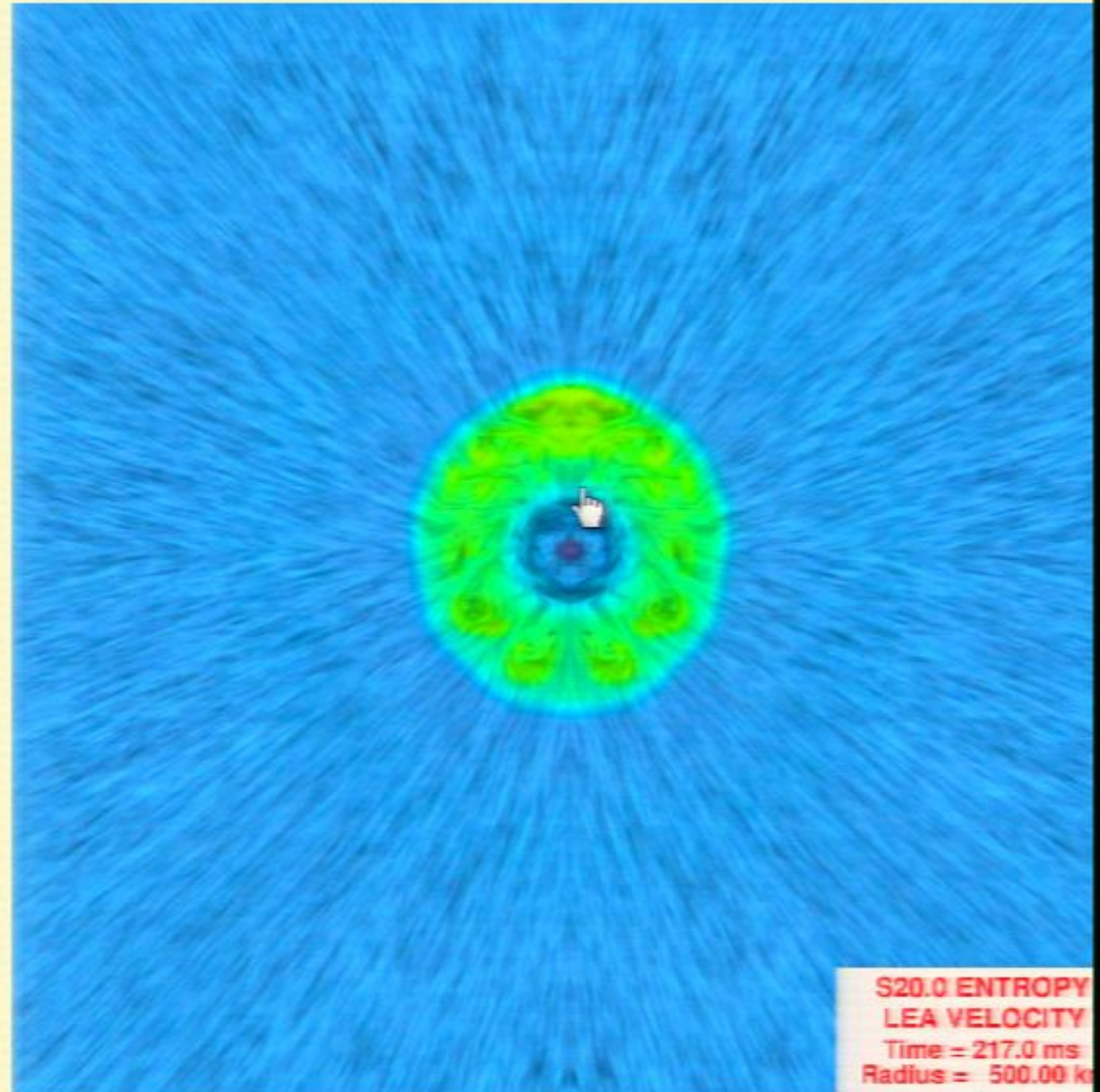
Dominant Multi-D Dynamics:

- Convection/Turbulence in the **protoneutron star** (PNS; $\tau > \sim 10\text{s}$)
- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

$O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 217.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

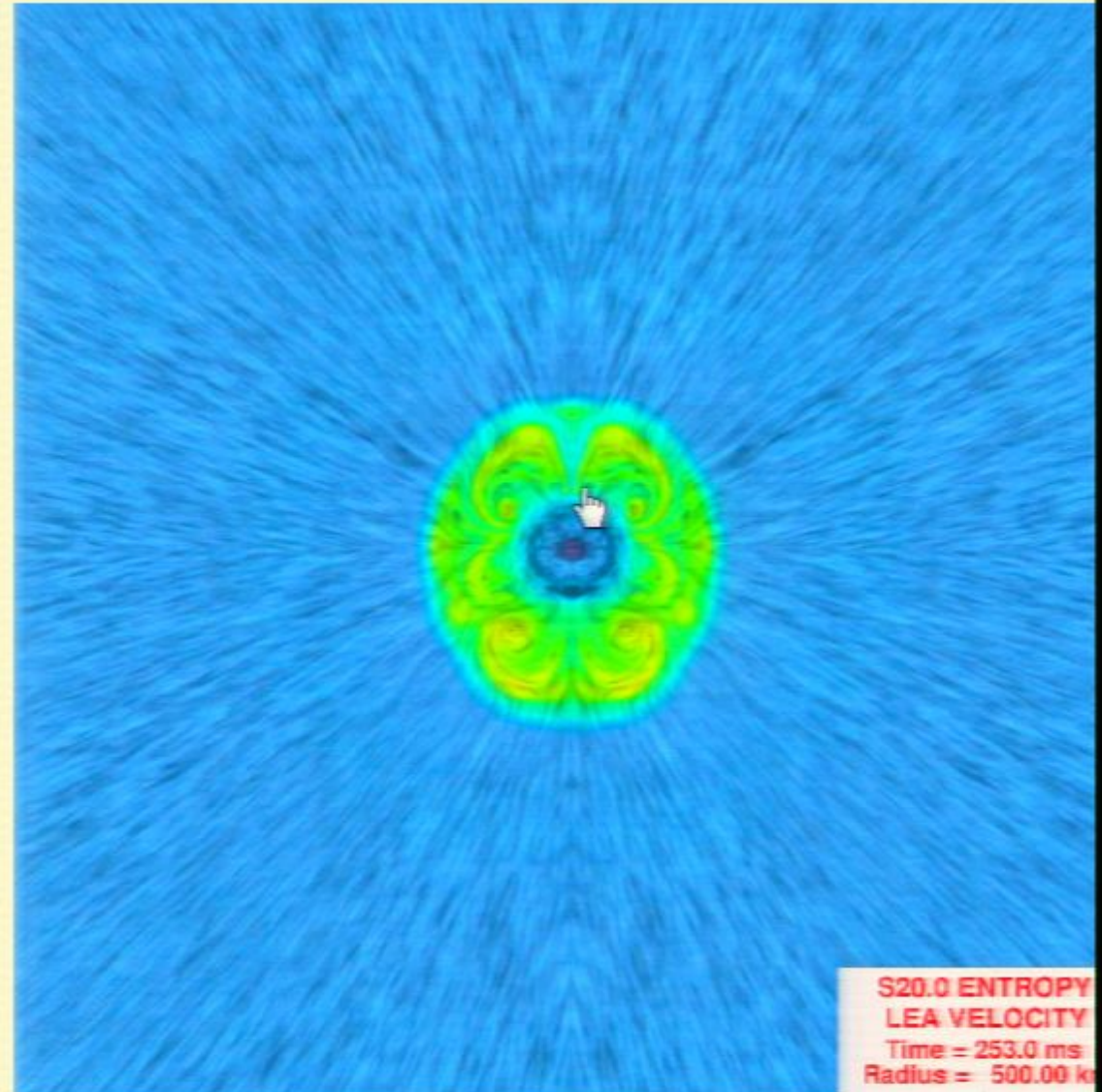
Dominant Multi-D Dynamics:

- Convection/Turbulence in the **protoneutron star** (PNS; $\tau > \sim 10\text{s}$)
- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086
 $O(10^{-23} - 10^{-22})$ at 10 kpc



GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

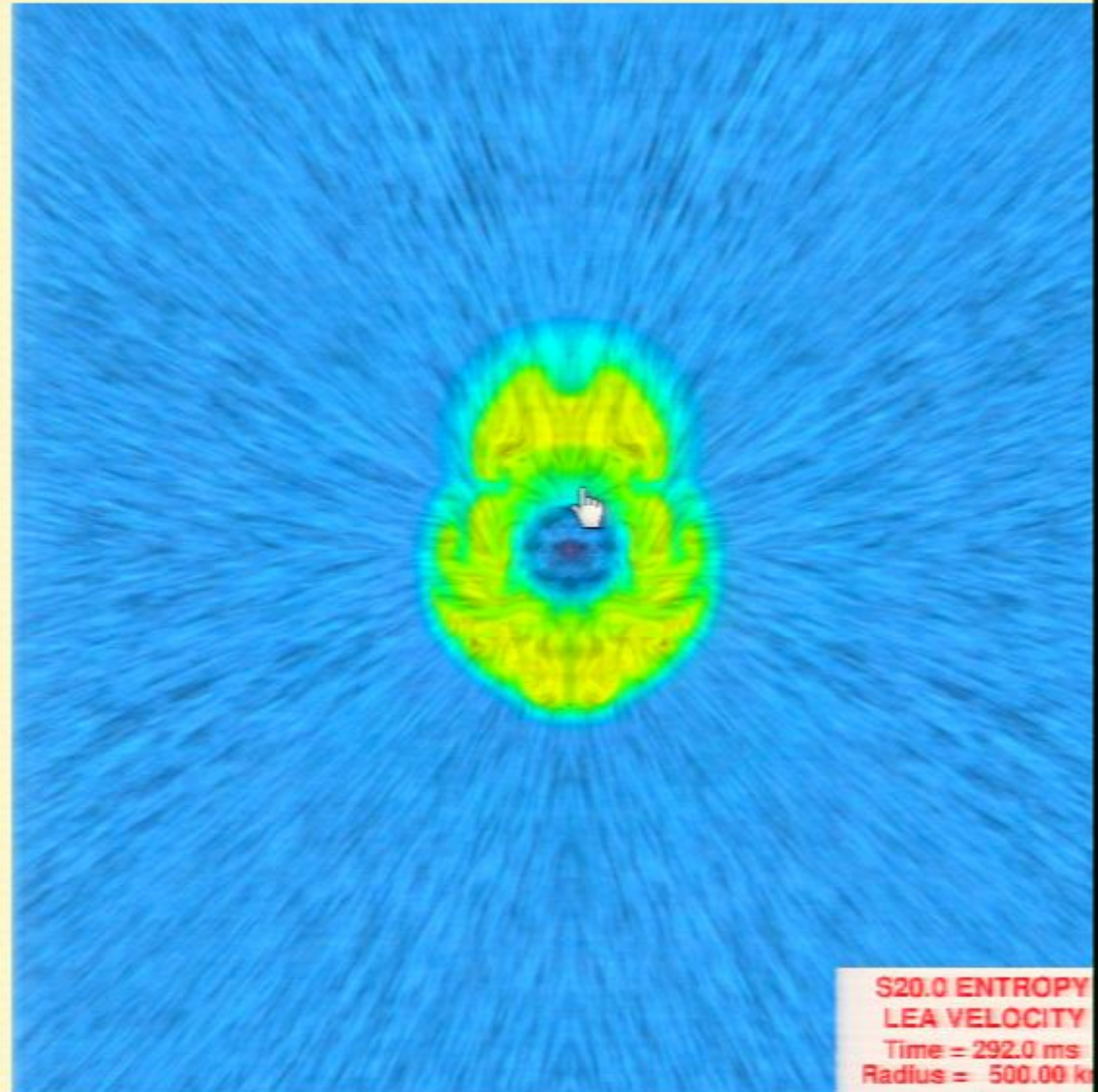
Dominant Multi-D Dynamics:

- Convection/Turbulence in the **protoneutron star** (PNS; $\tau > \sim 10\text{s}$)
- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

$O(10^{-23} - 10^{-22})$ at 10 kpc



GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

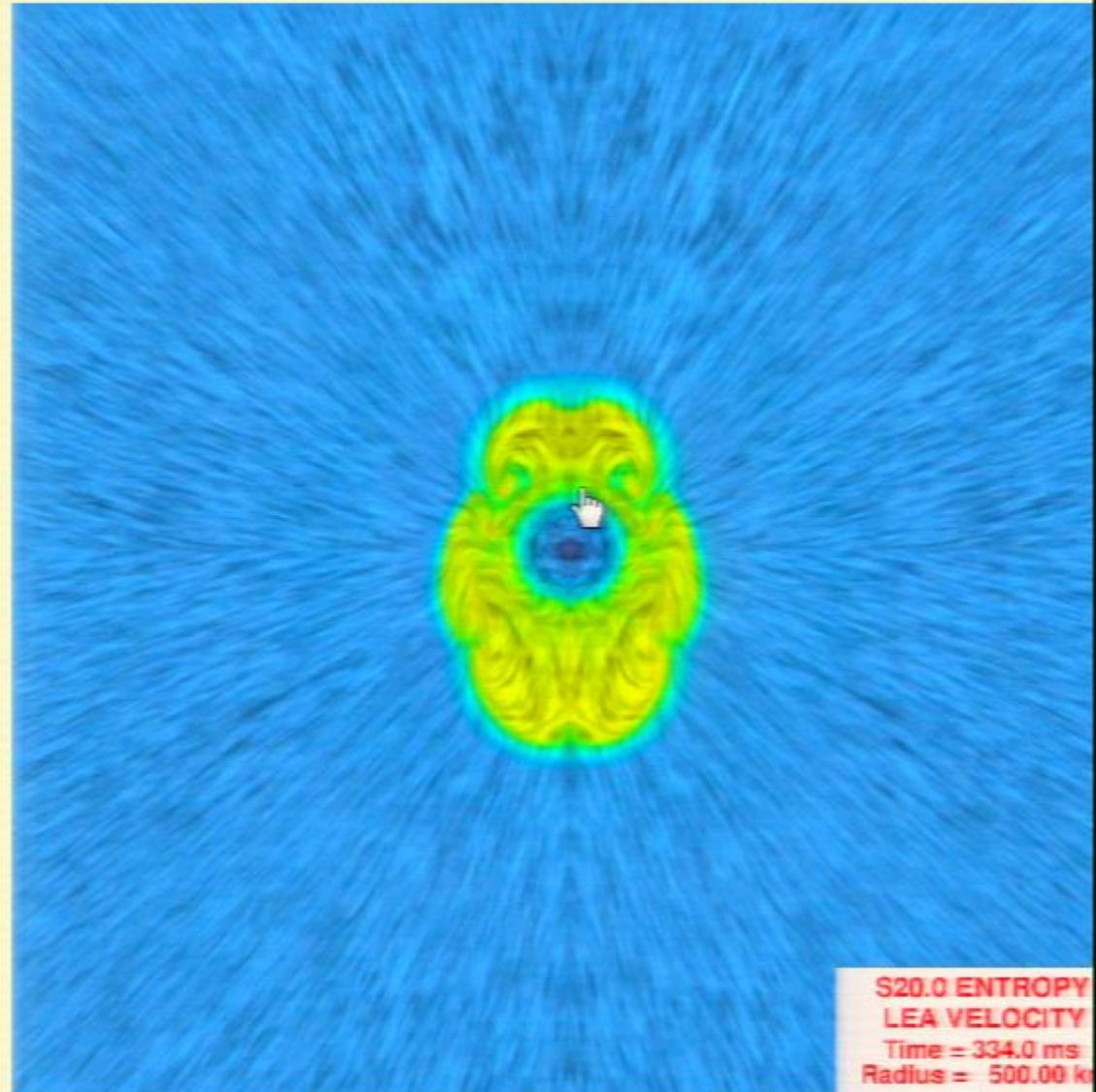
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- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086 $O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 334.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

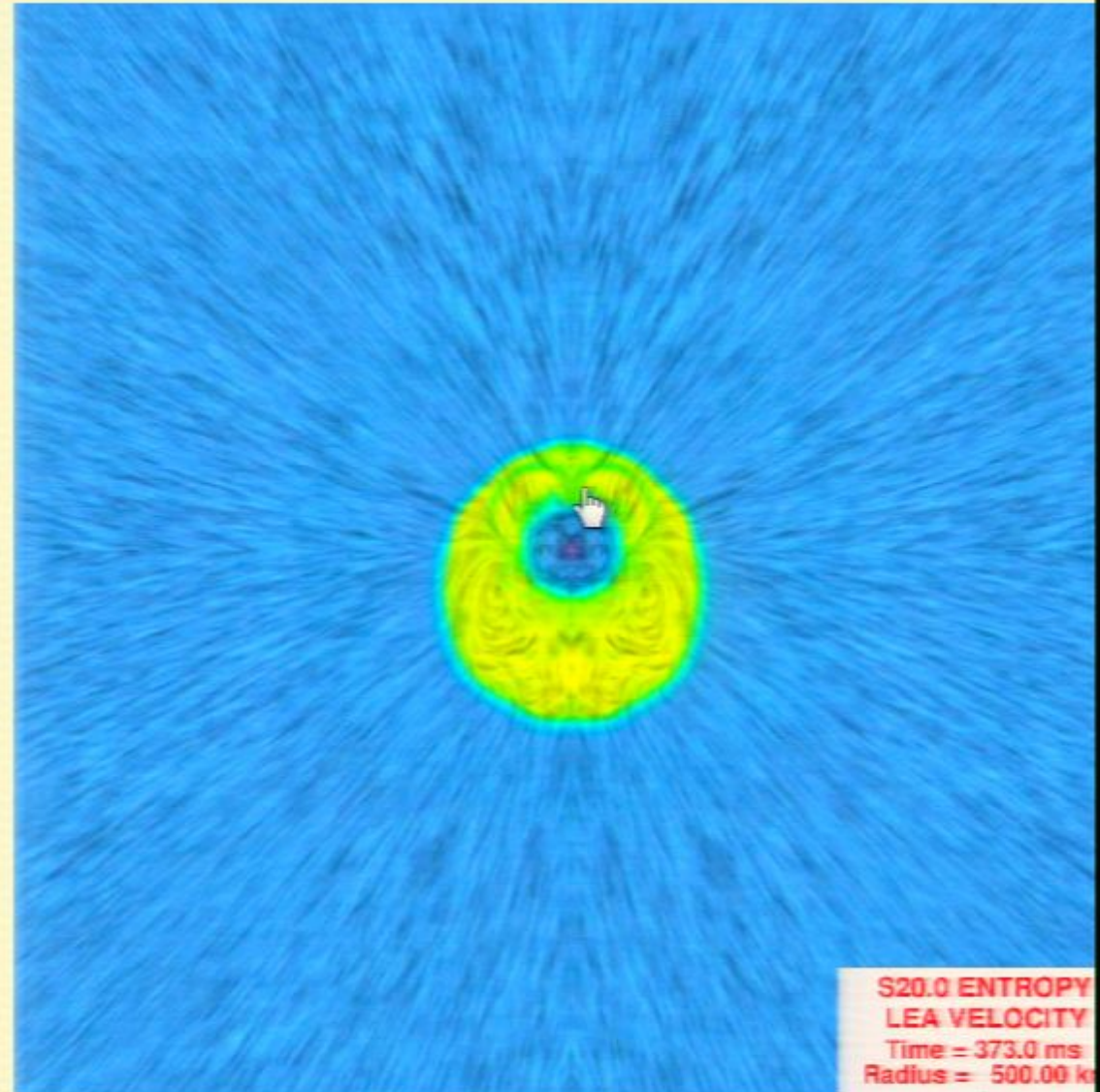
Dominant Multi-D Dynamics:

- Convection/Turbulence in the **protoneutron star** (PNS; $\tau > \sim 10\text{s}$)
- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

$h \sim 10^{-23} - 10^{-22}$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 373.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

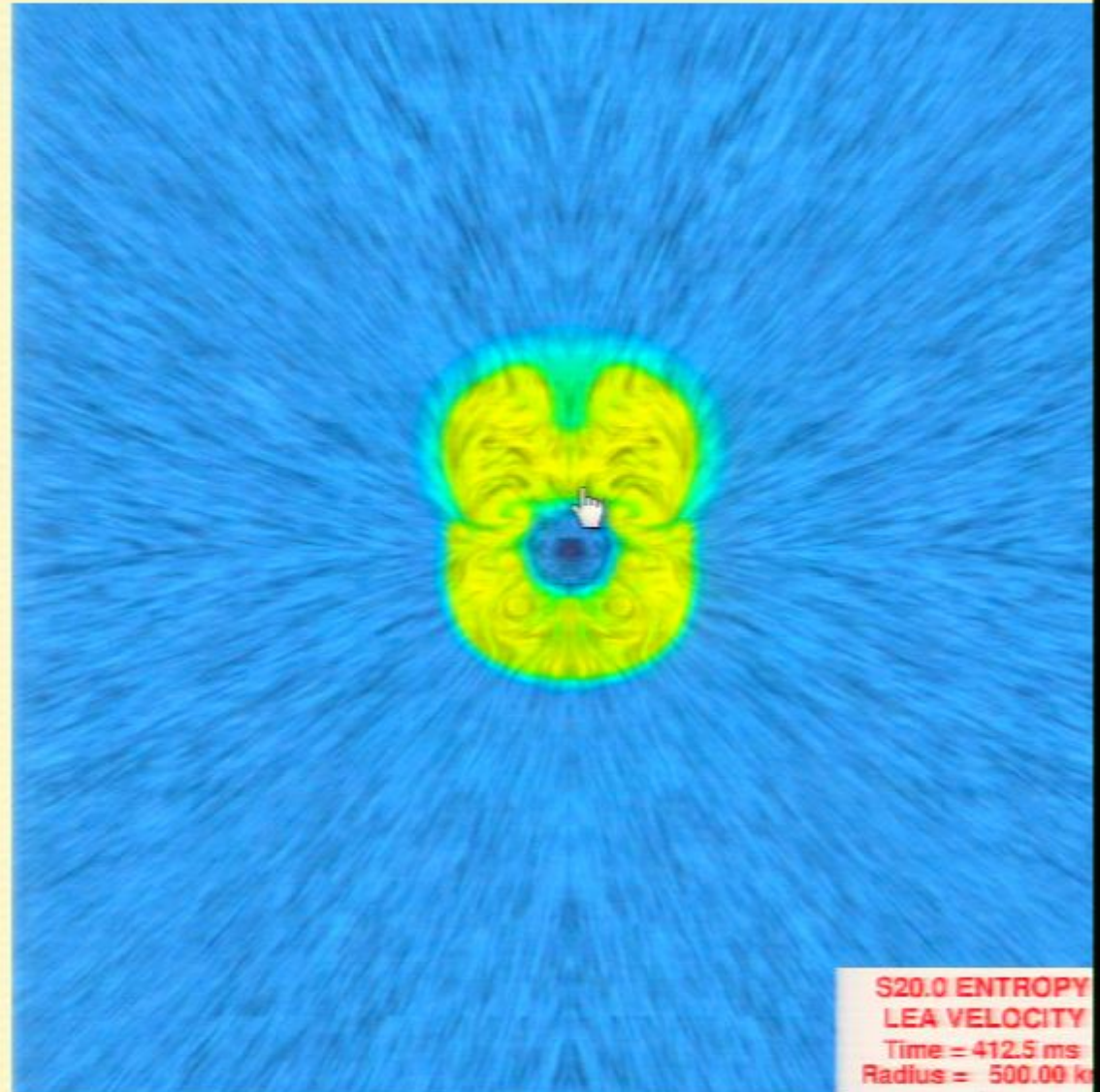
Dominant Multi-D Dynamics:

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- Convection/Turbulence in the **postshock region** ($\tau < 1\text{s}$)
- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

Pirsa: 10060086 $O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 412.5 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

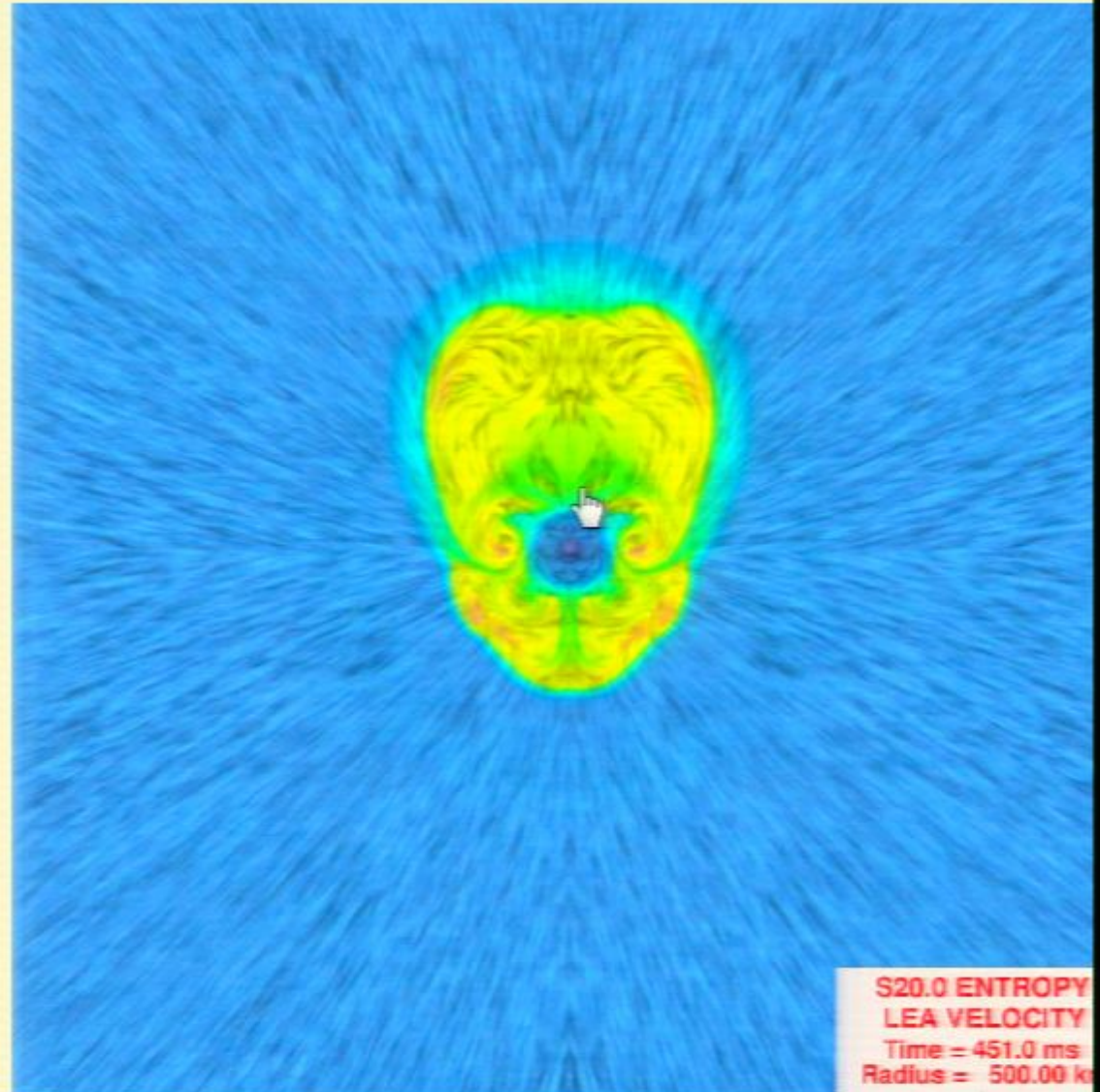
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- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

$O(10^{-23} - 10^{-22})$ at 10 kpc



S20.0 ENTROPY
LEA VELOCITY
Time = 451.0 ms
Radius = 500.00 km

GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

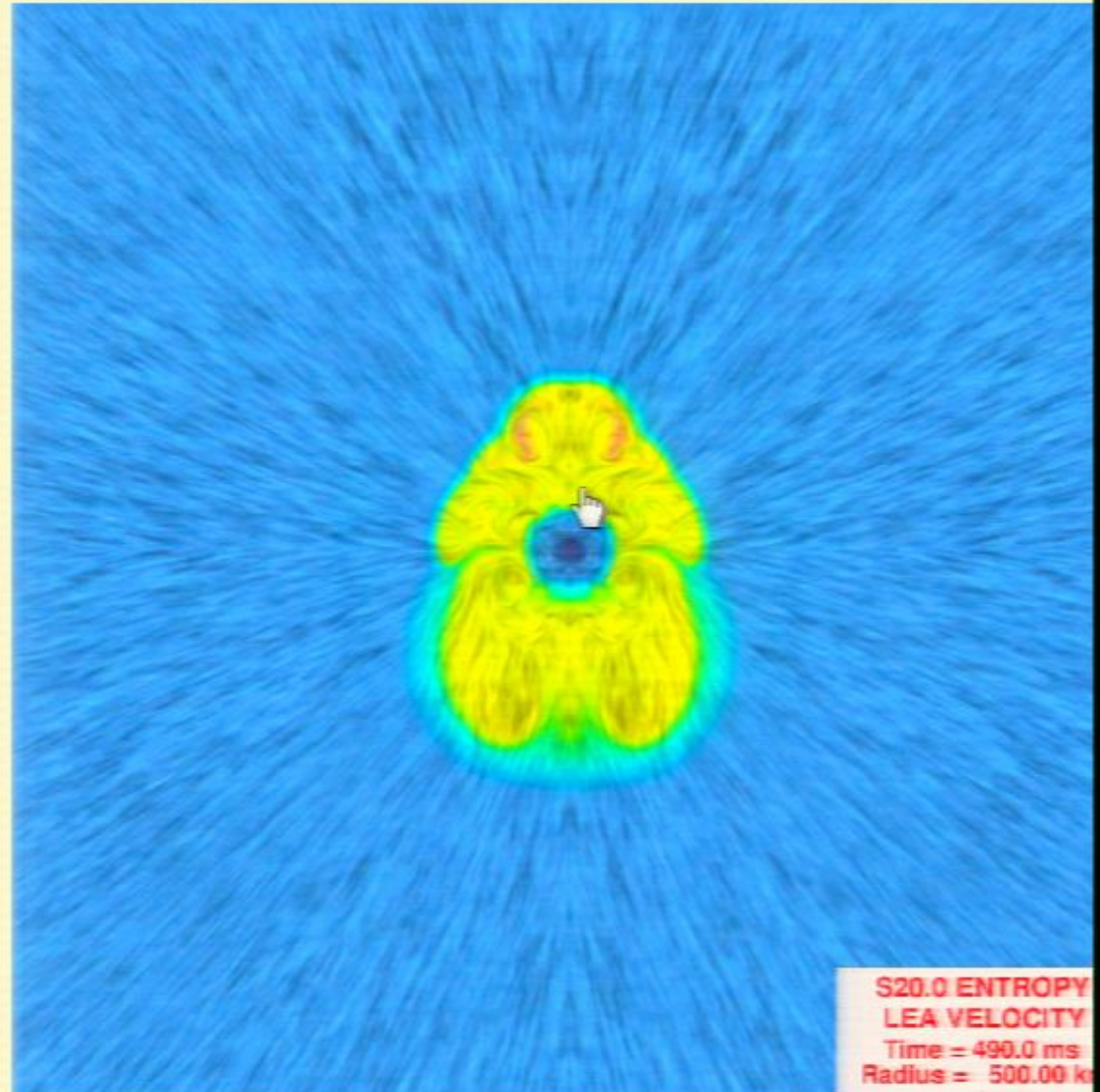
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- Standing accretion shock instability (**SASI**; $\tau < 1\text{s}$)

Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

$O(10^{-23} - 10^{-22})$ at 10 kpc



GW Signature of the Neutrino Mechanism

[Marek et al. '09, Murphy, Ott, & Burrows '09, Yakunin et al. '10]

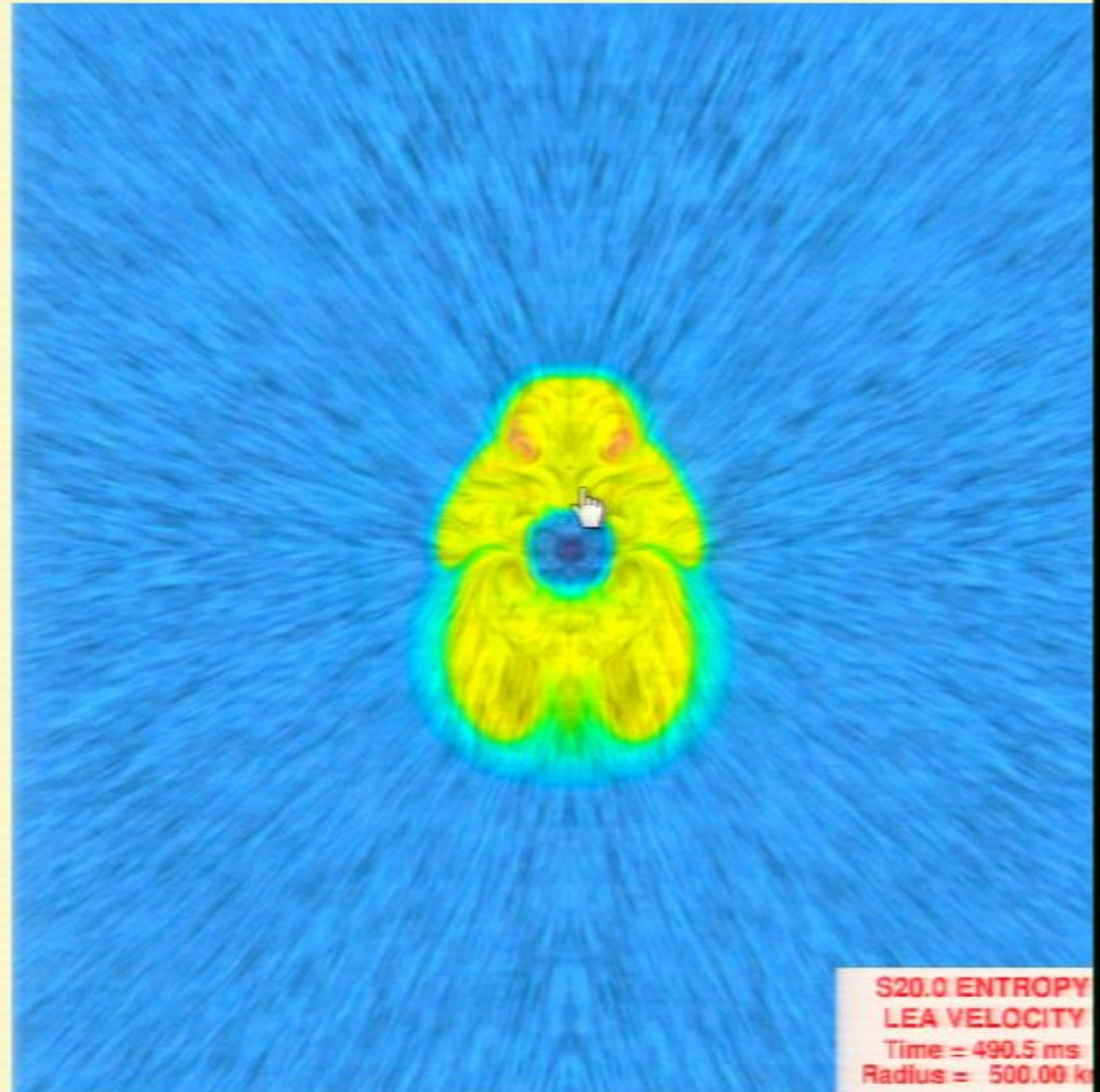
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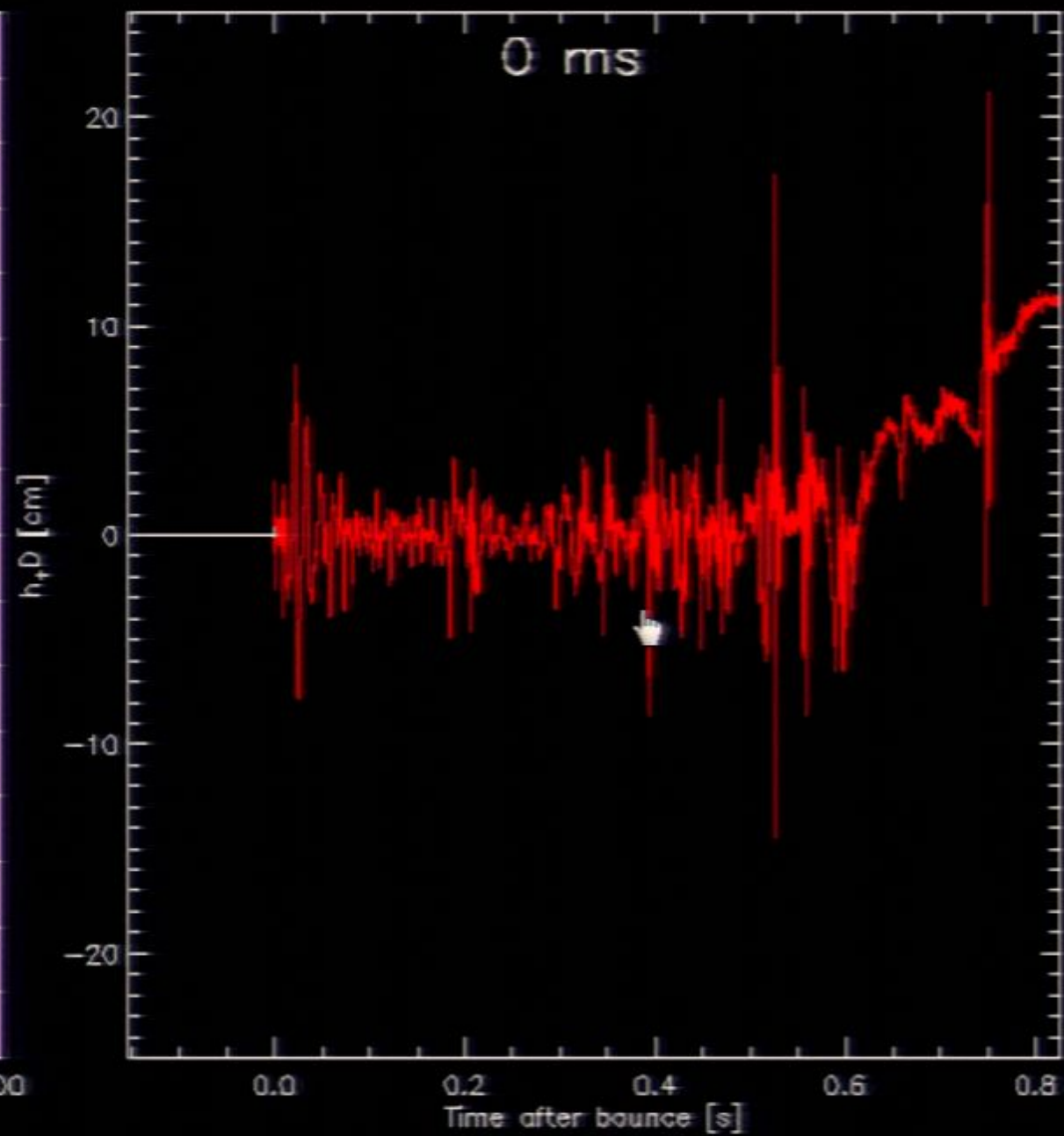
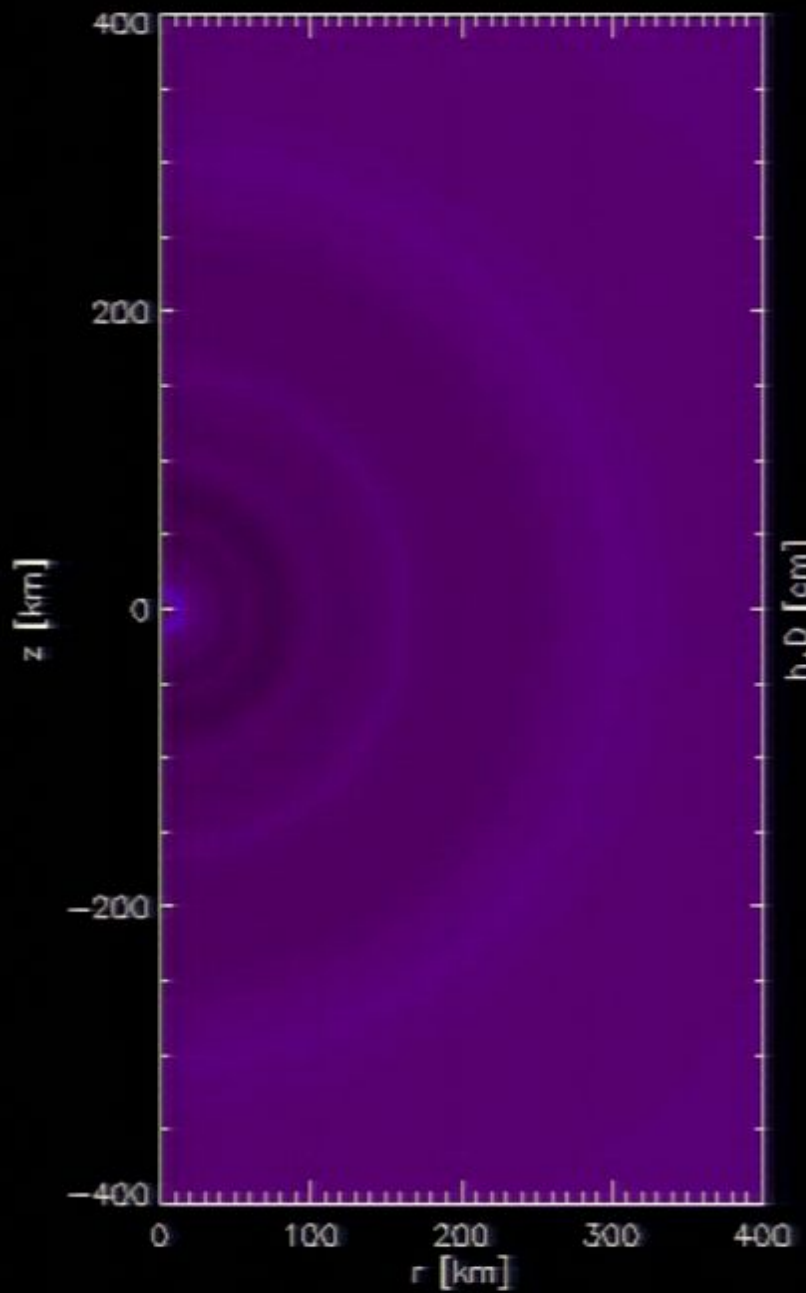
Expected GW Signal:

- Broadband
- Random polarization
- Low amplitude:

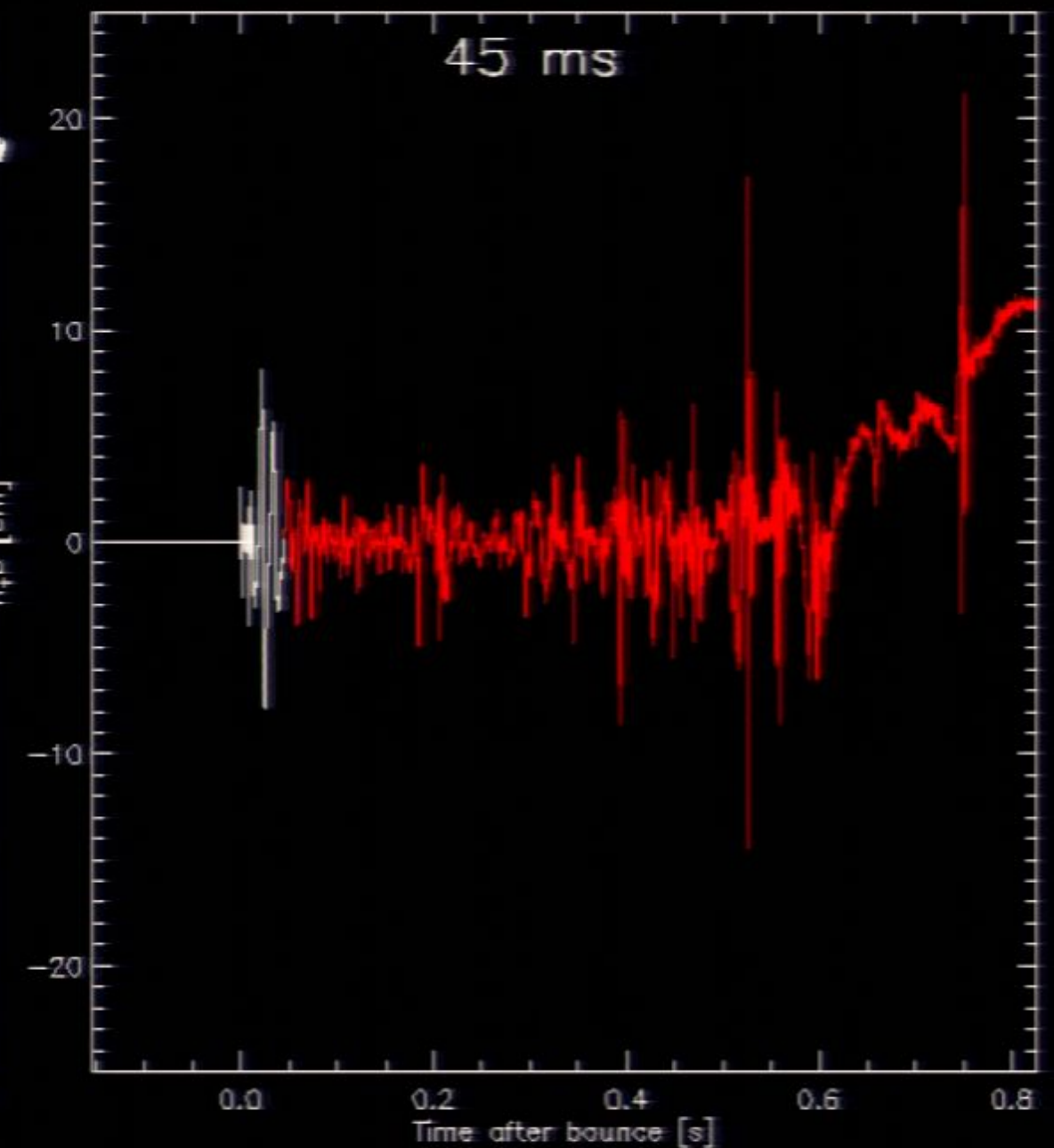
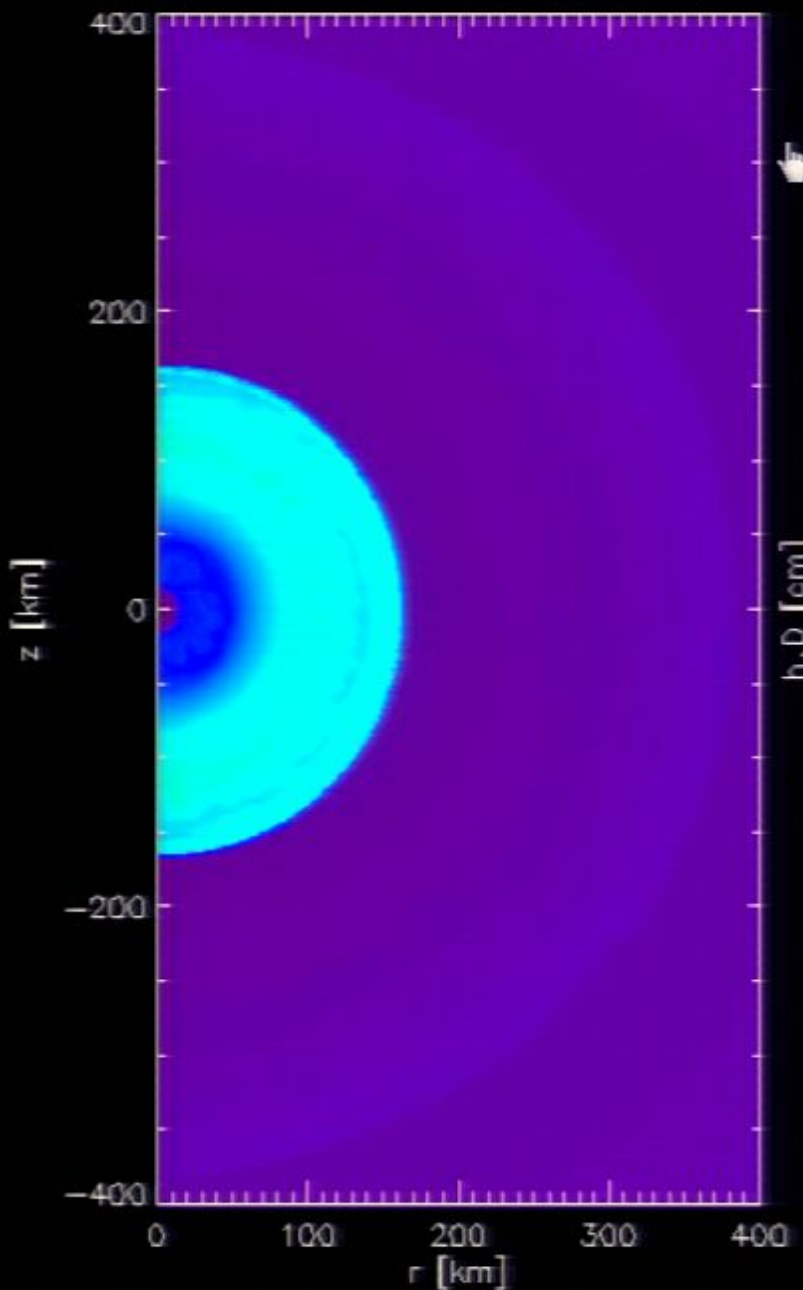
$\sim 10^{-23} - 10^{-22}$ at 10 kpc



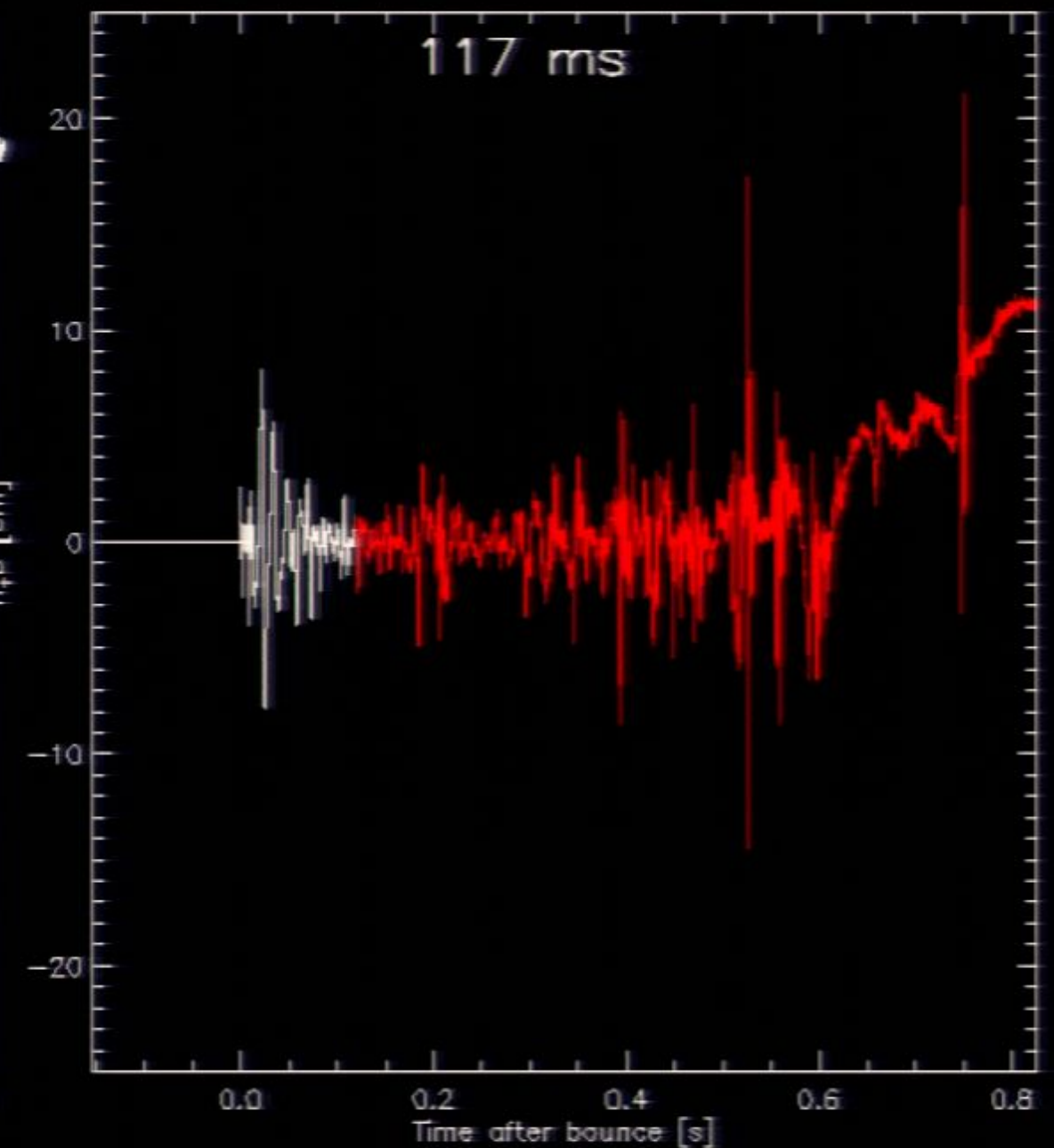
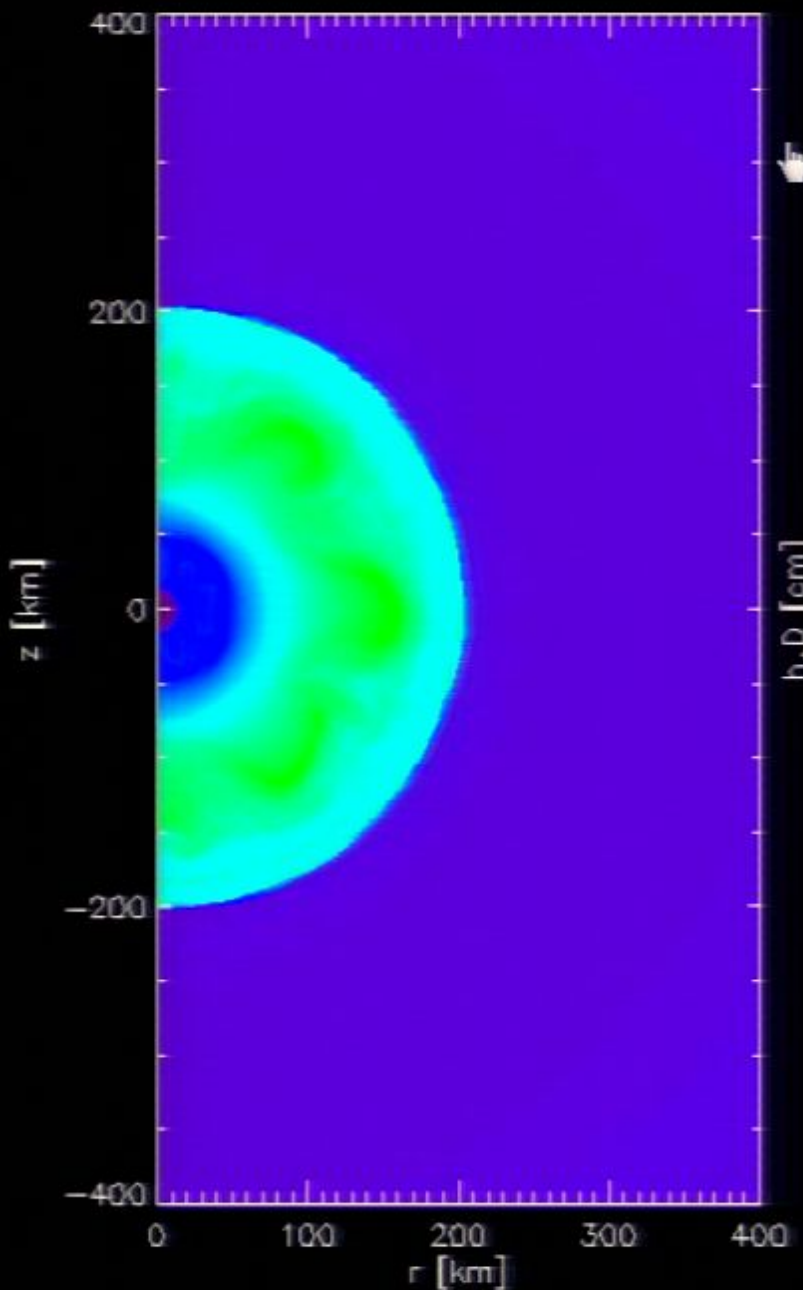
S20.0 ENTROPY
LEA VELOCITY
Time = 490.5 ms
Radius = 500.00 km



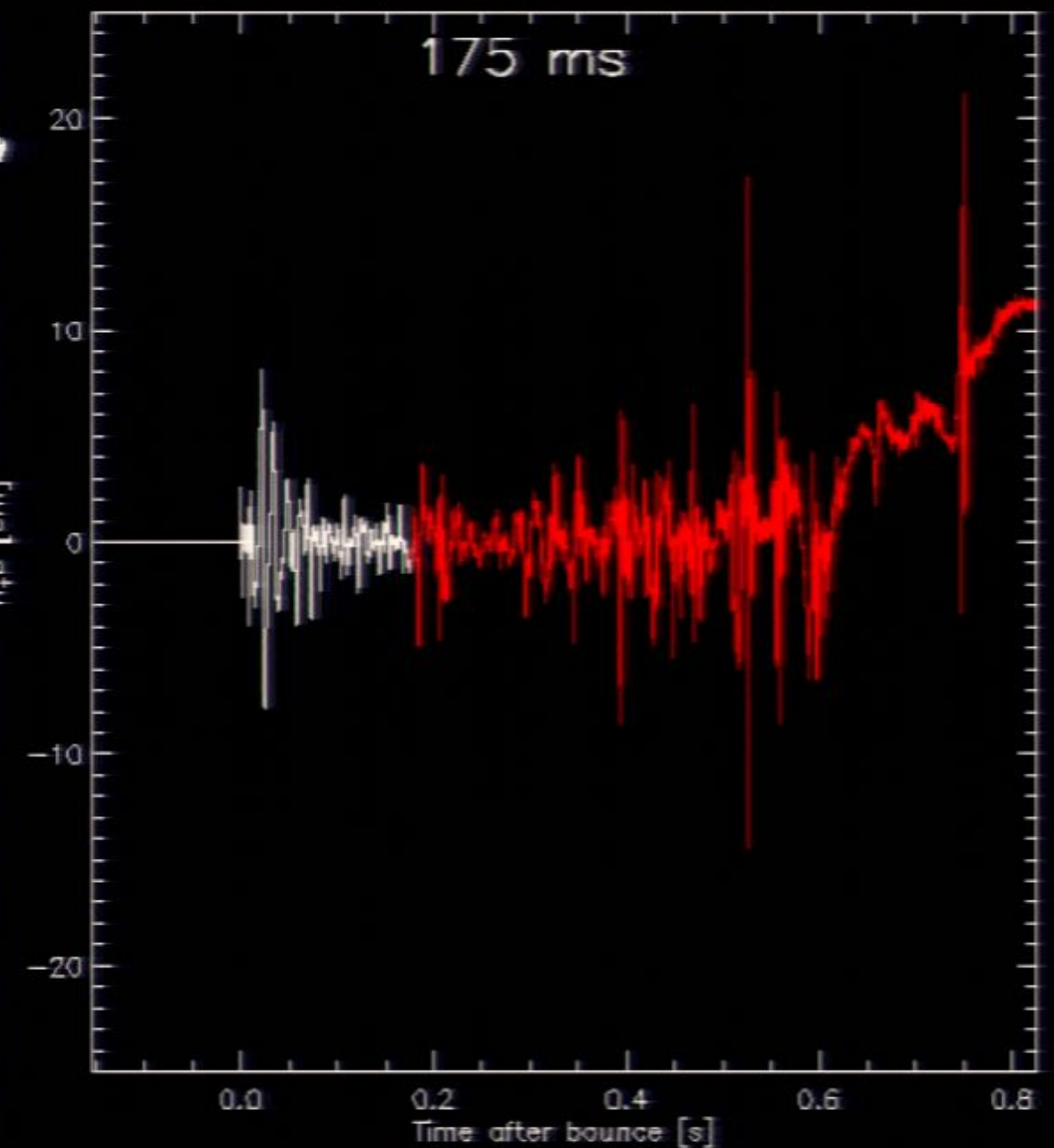
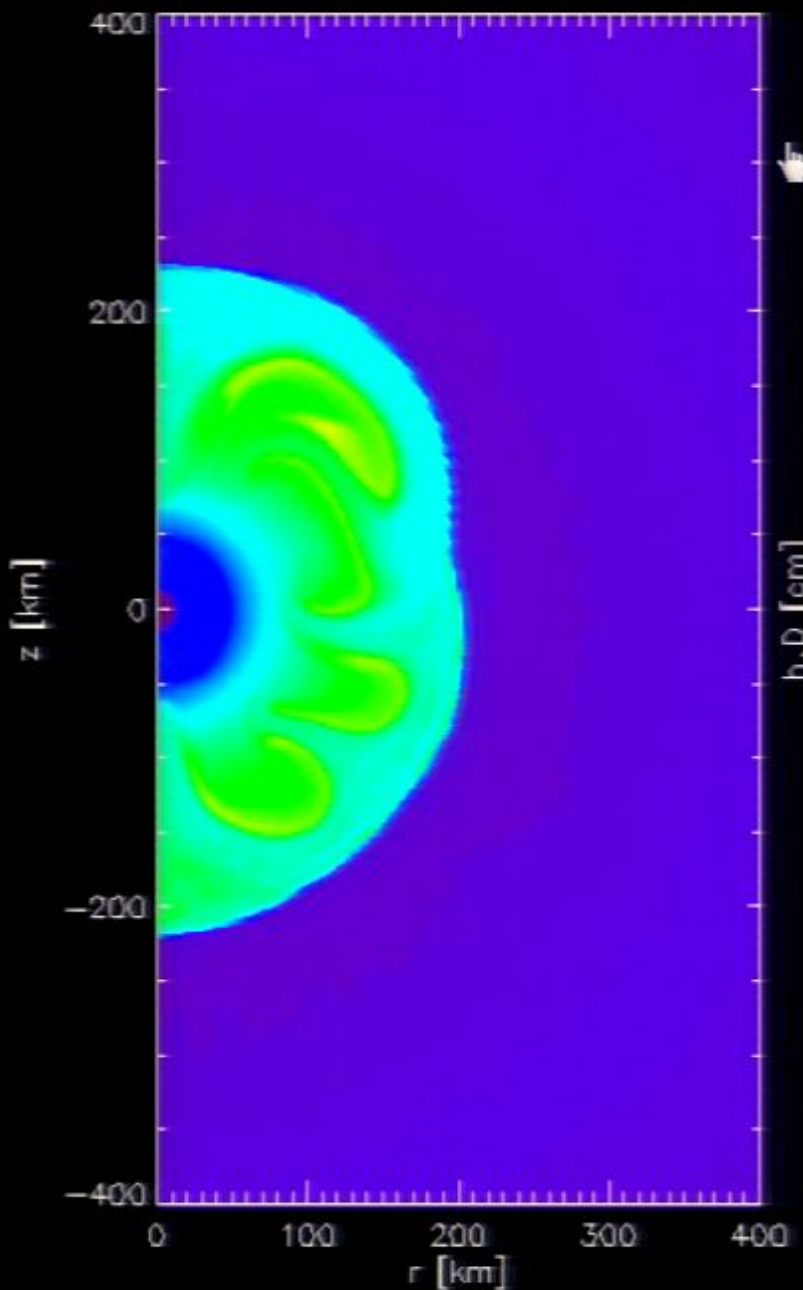
[Murphy, Ott and Burrows 2009]



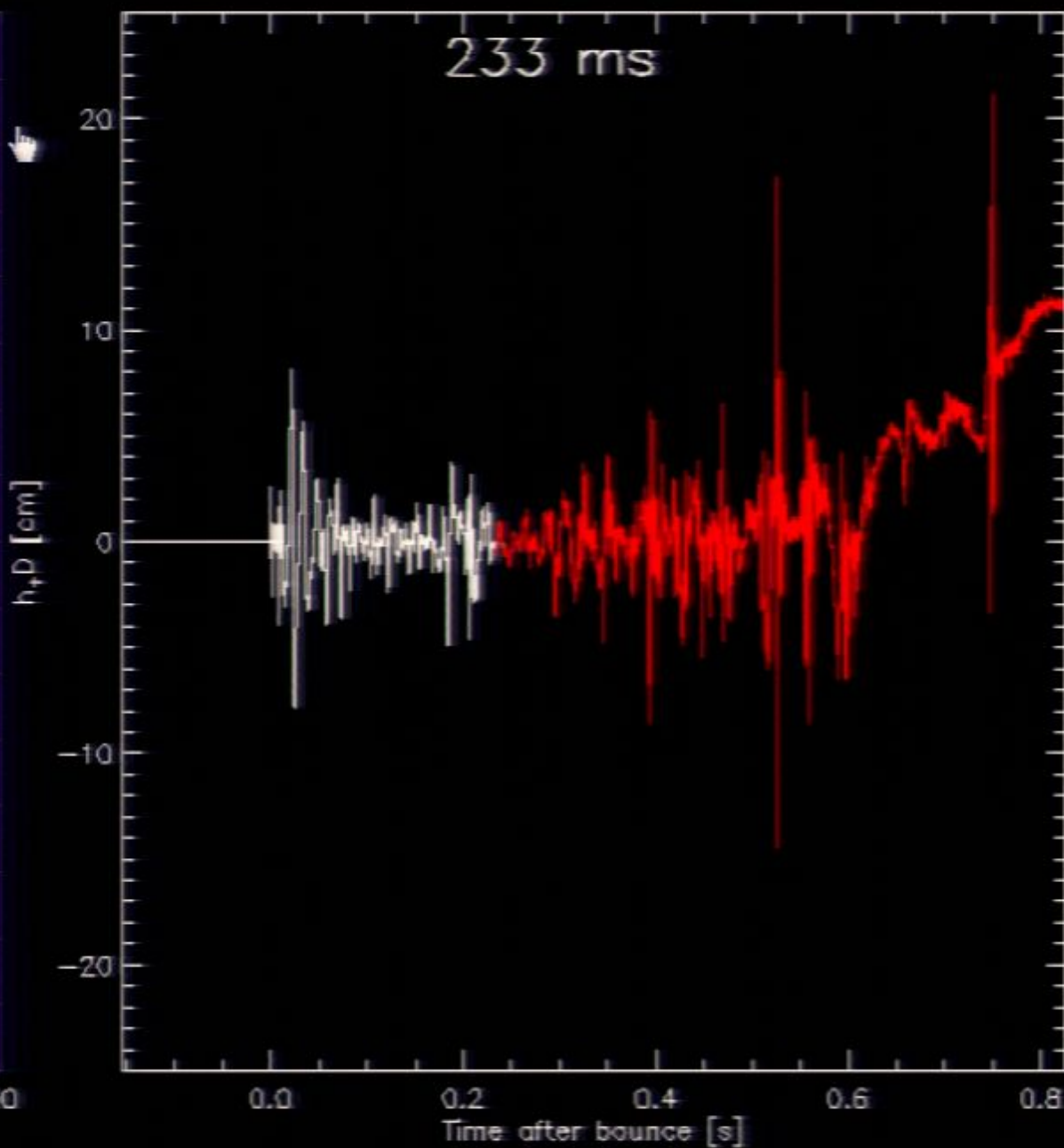
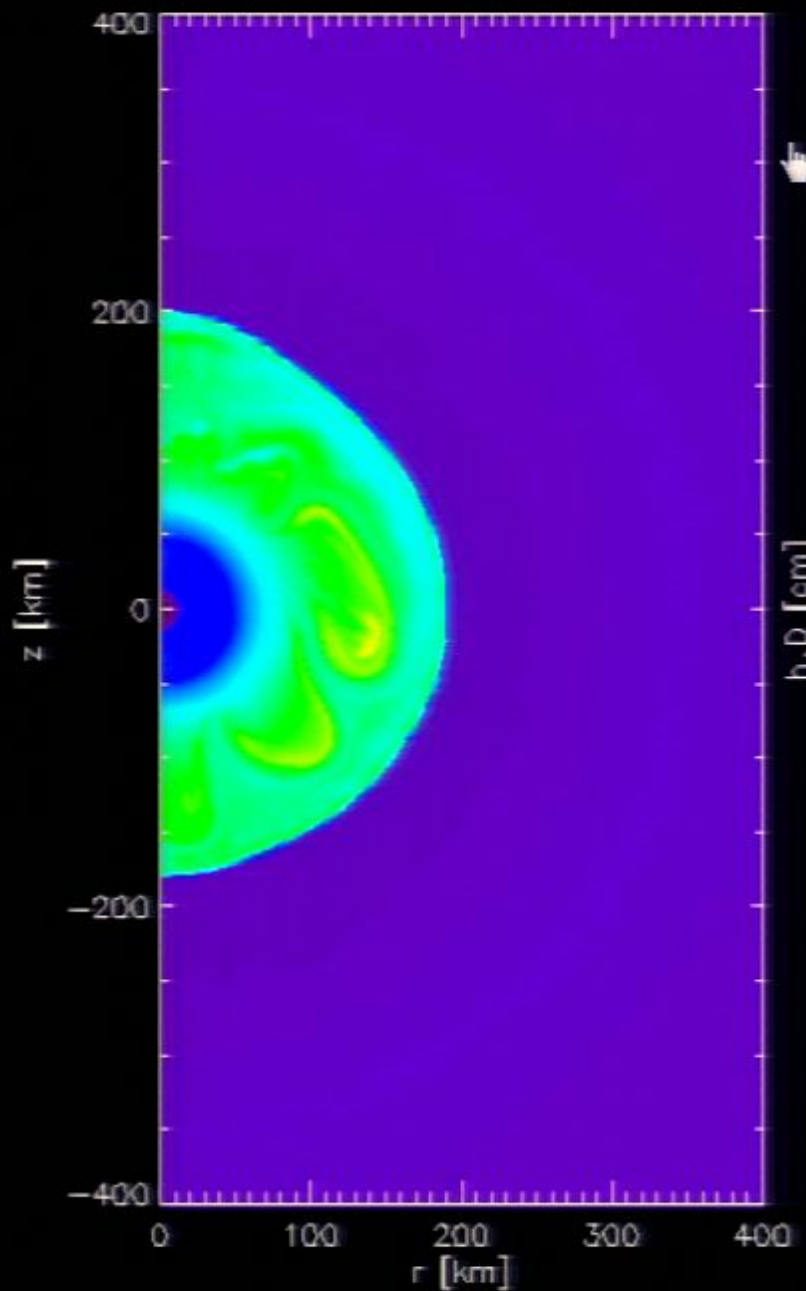
[Murphy, Ott and Burrows 2009]



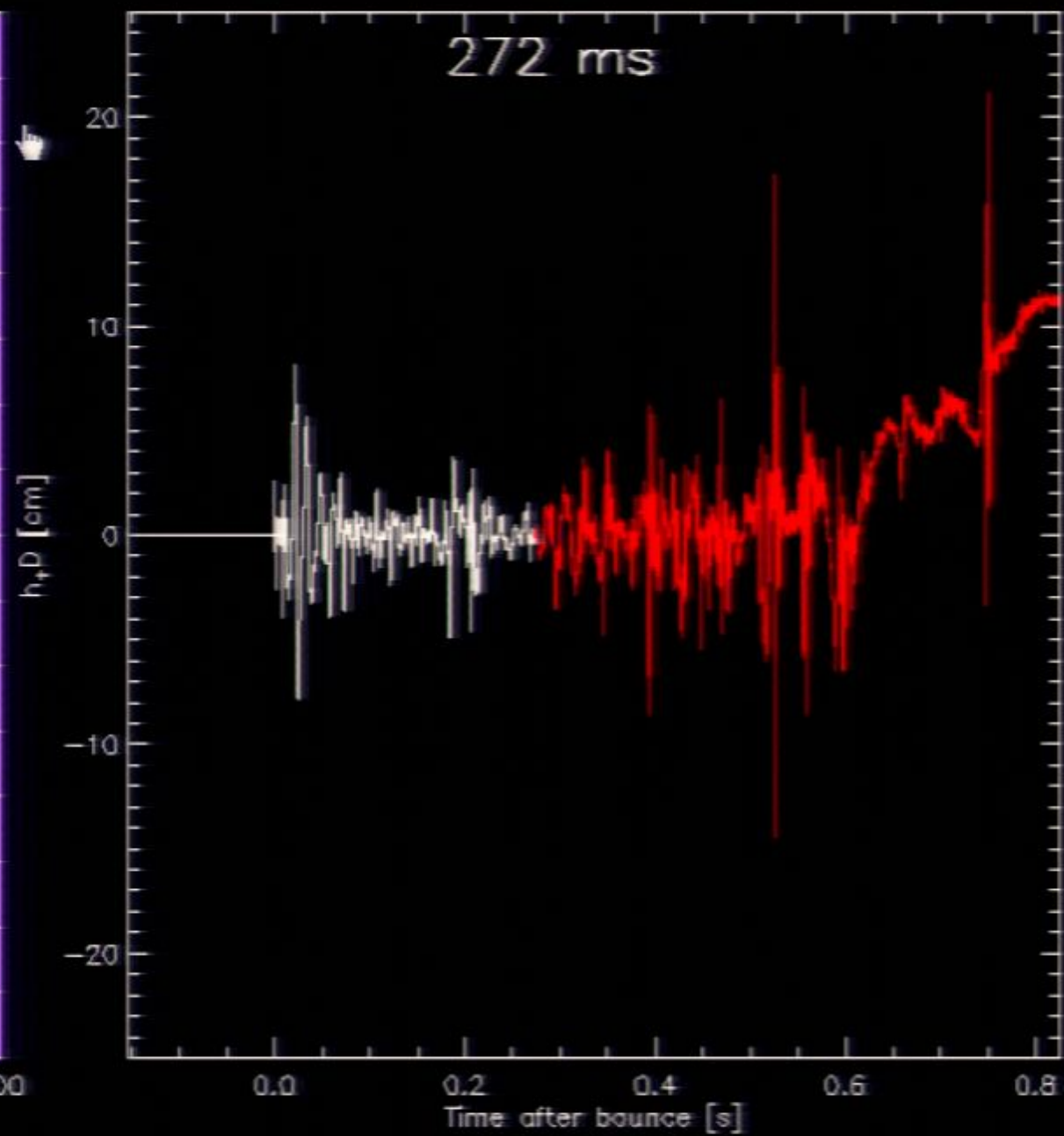
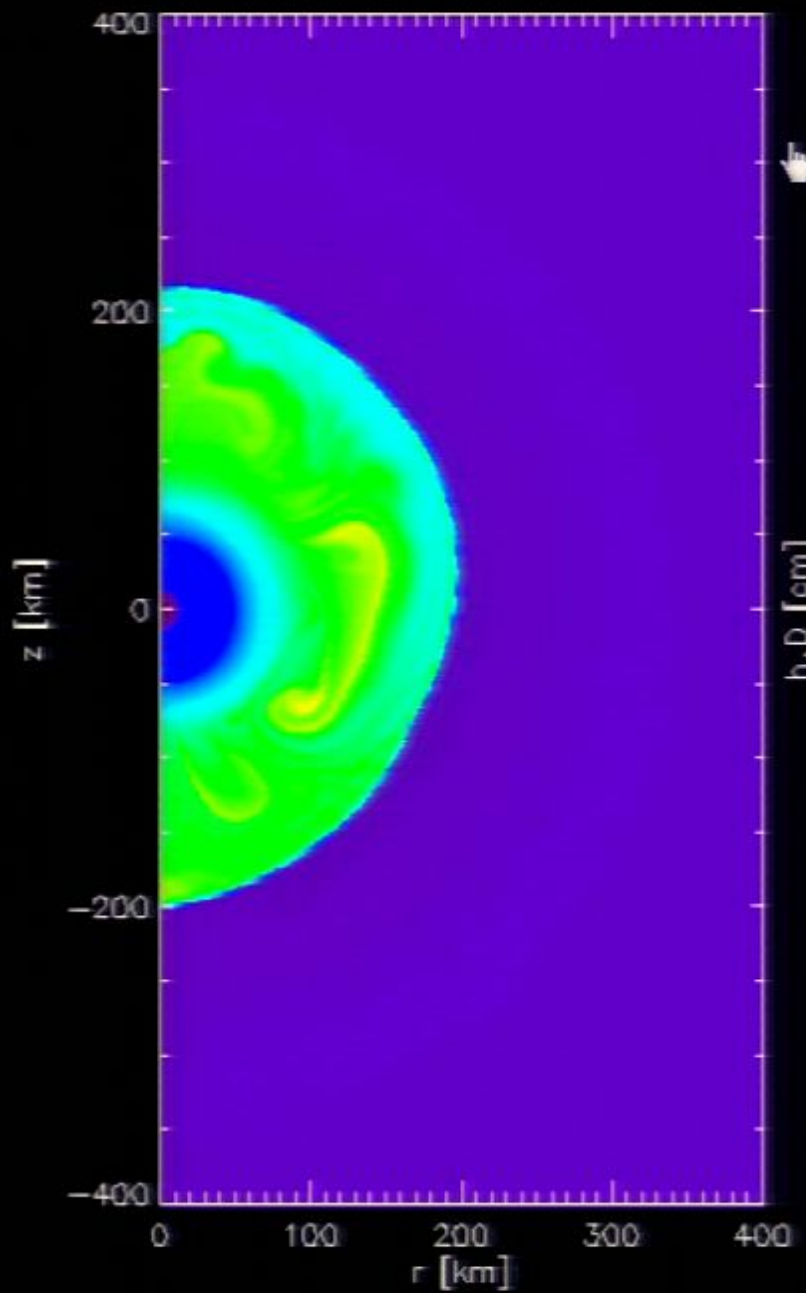
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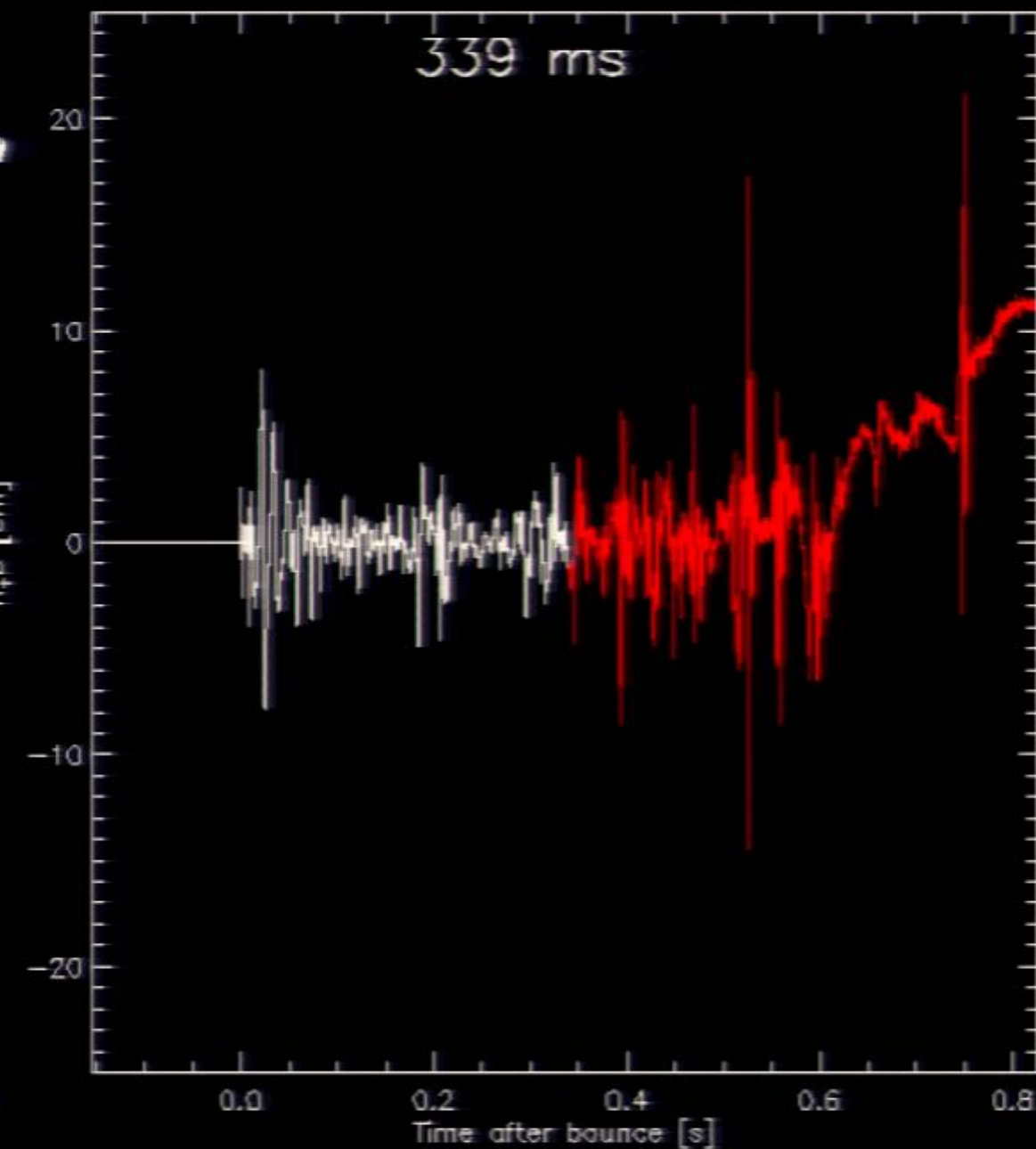
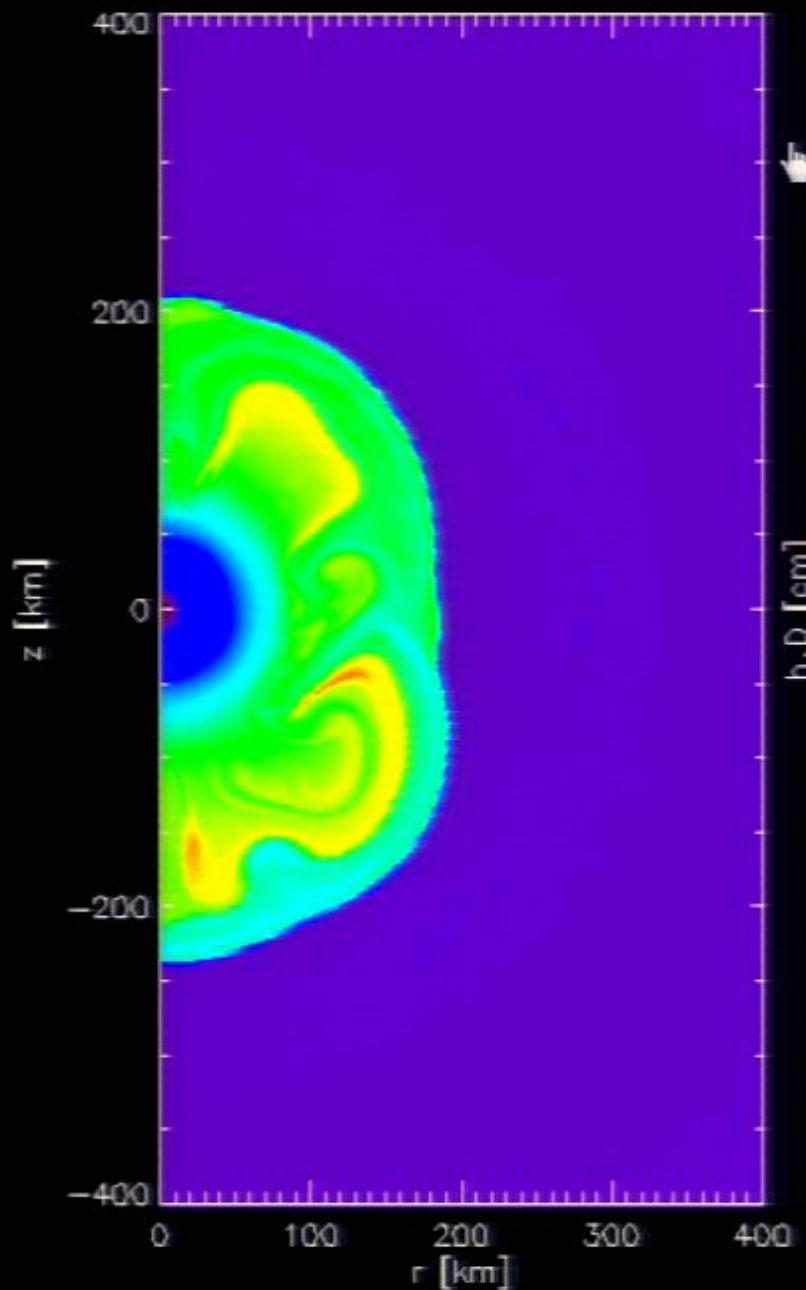
[Murphy, Ott and Burrows 2009]



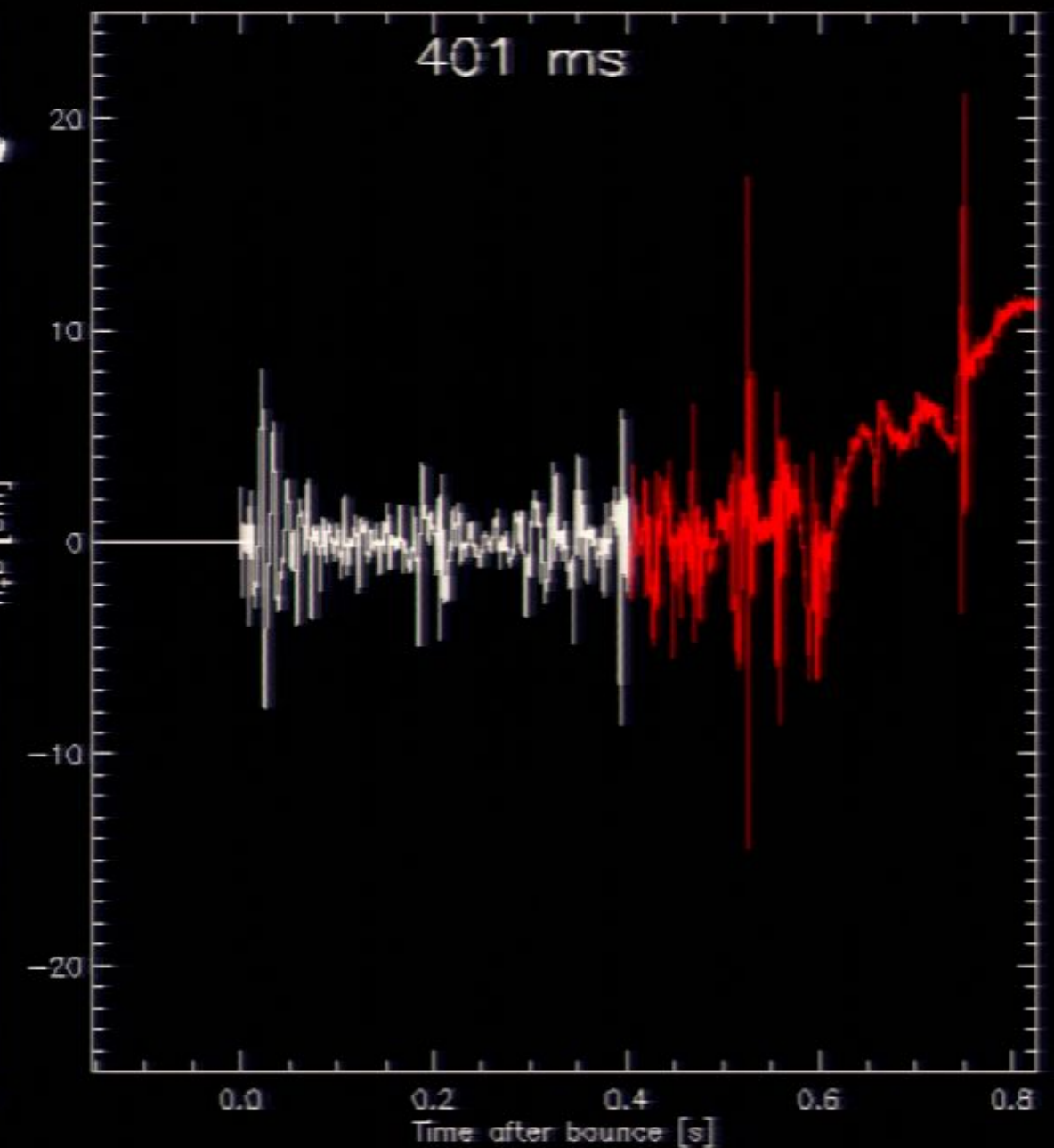
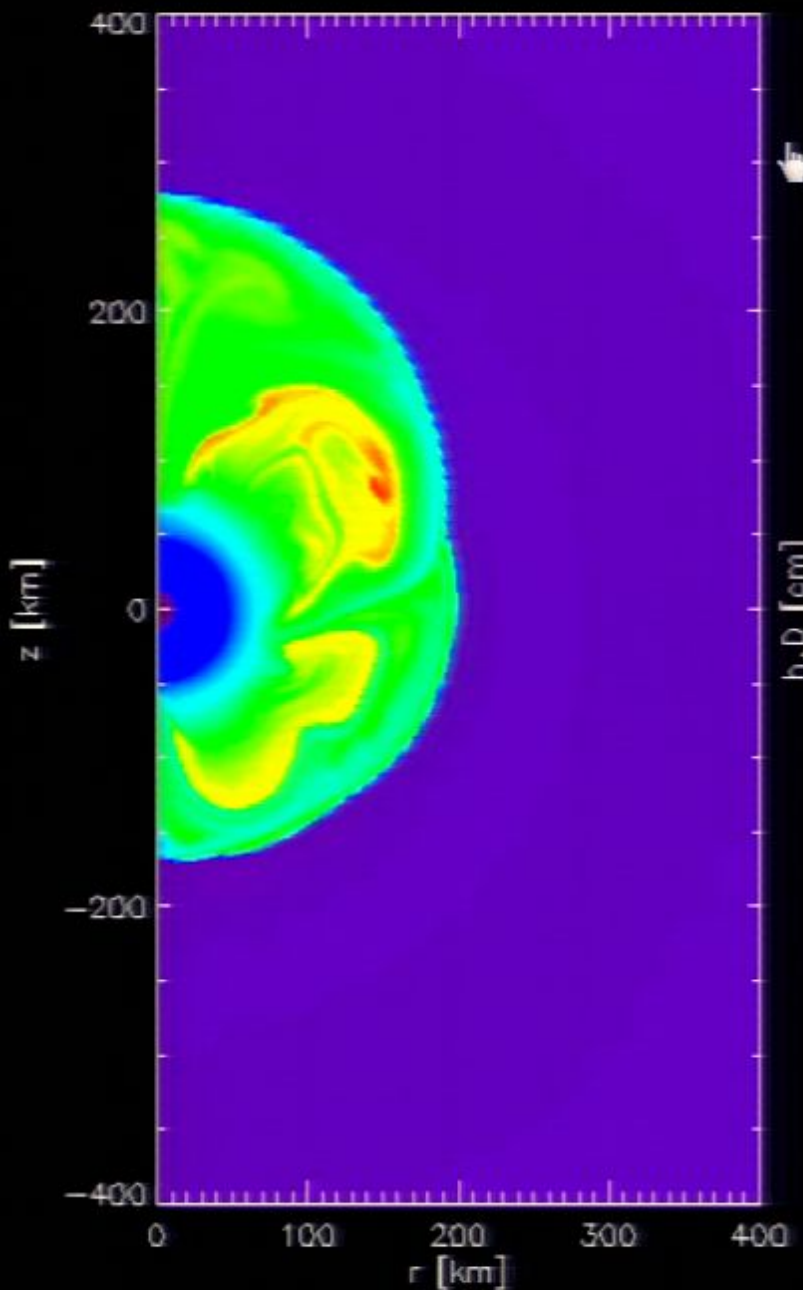
[Murphy, Ott and Burrows 2009]



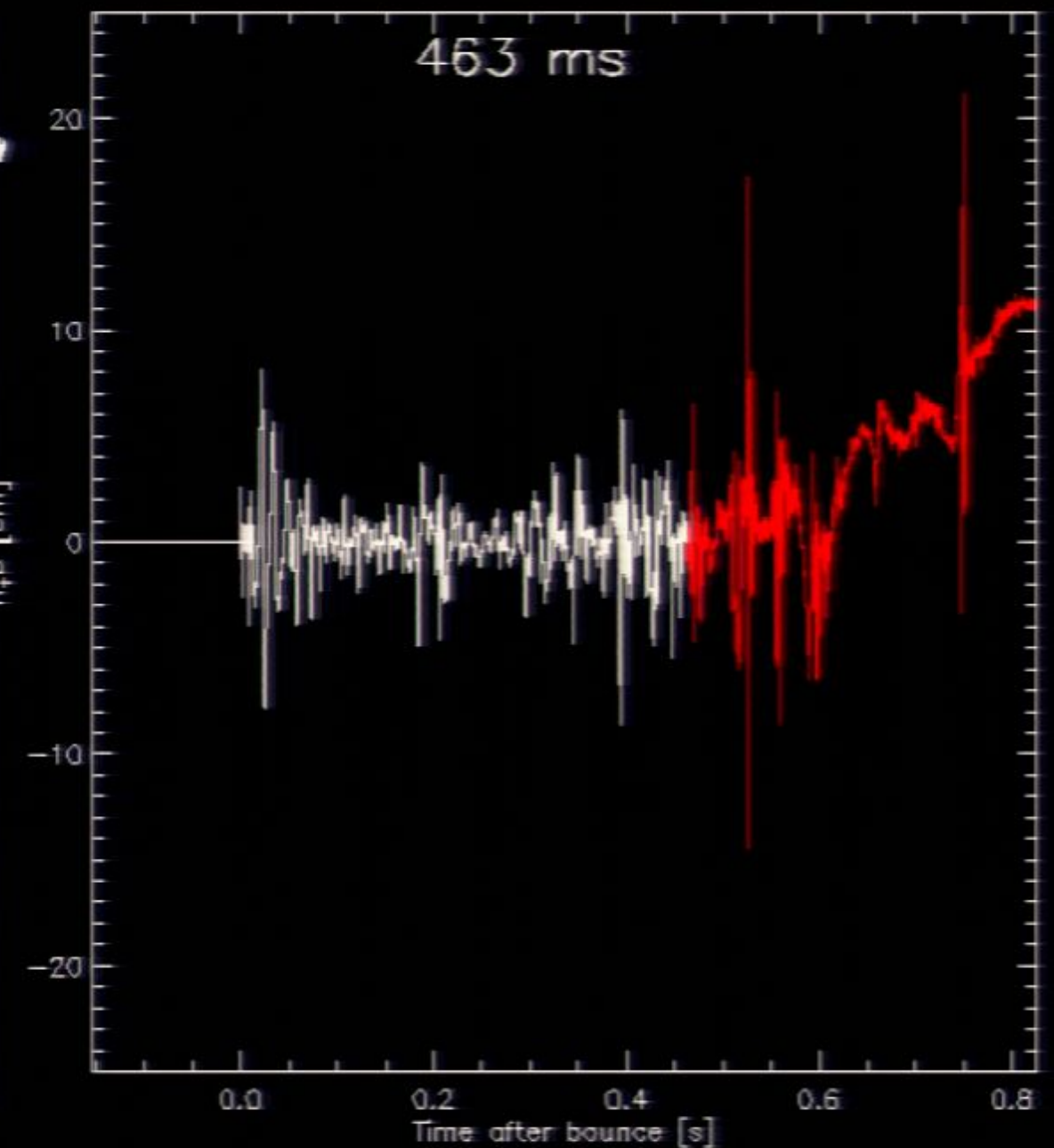
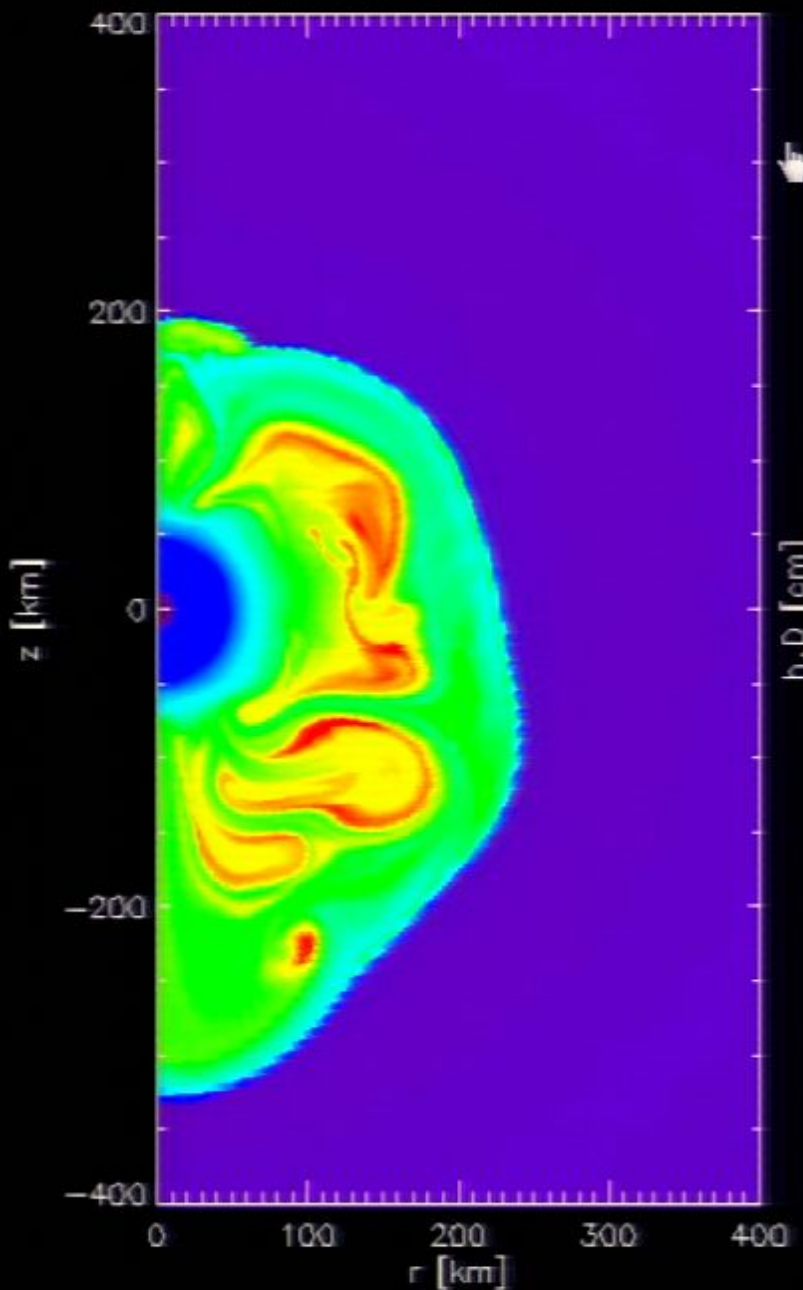
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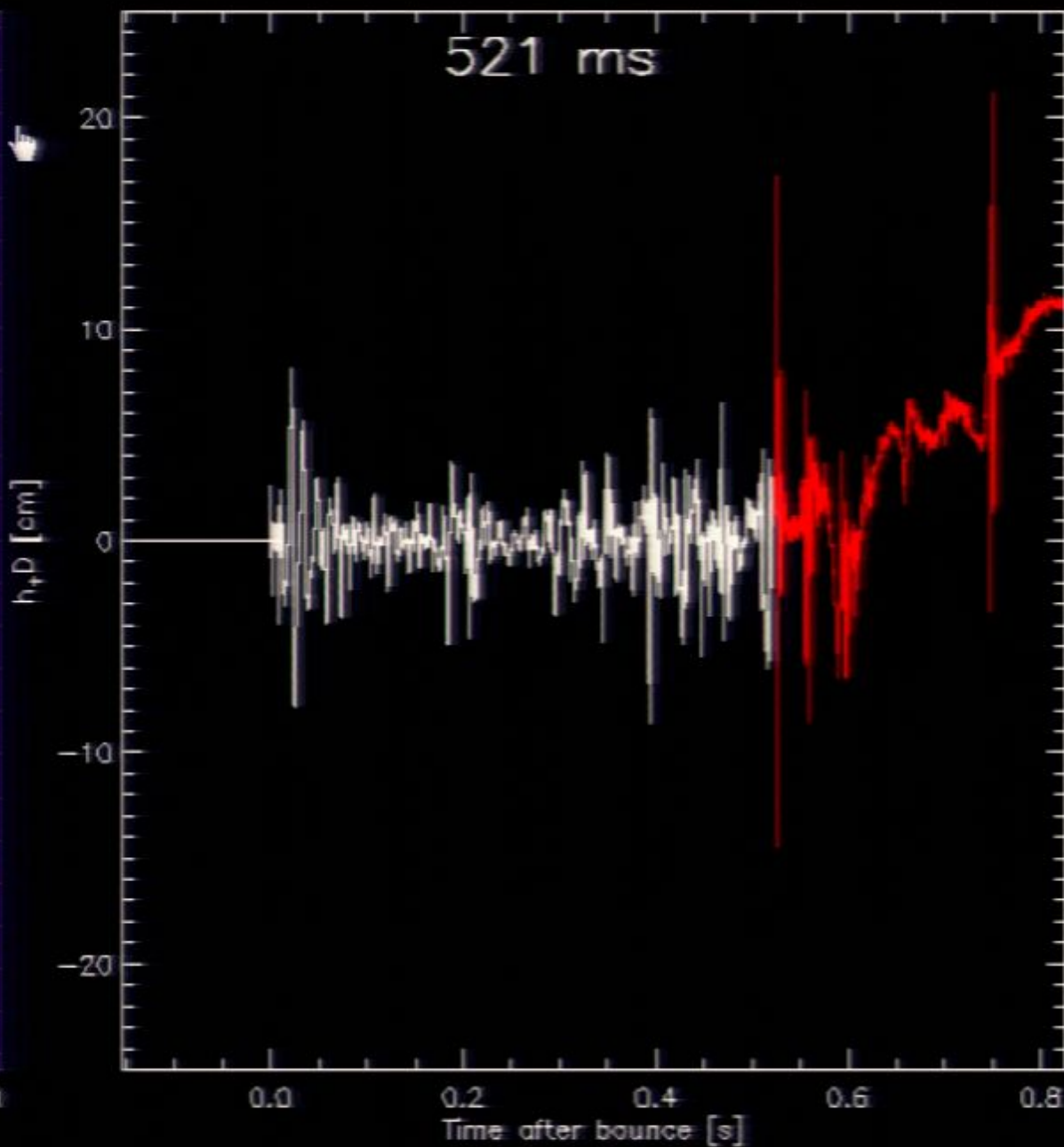
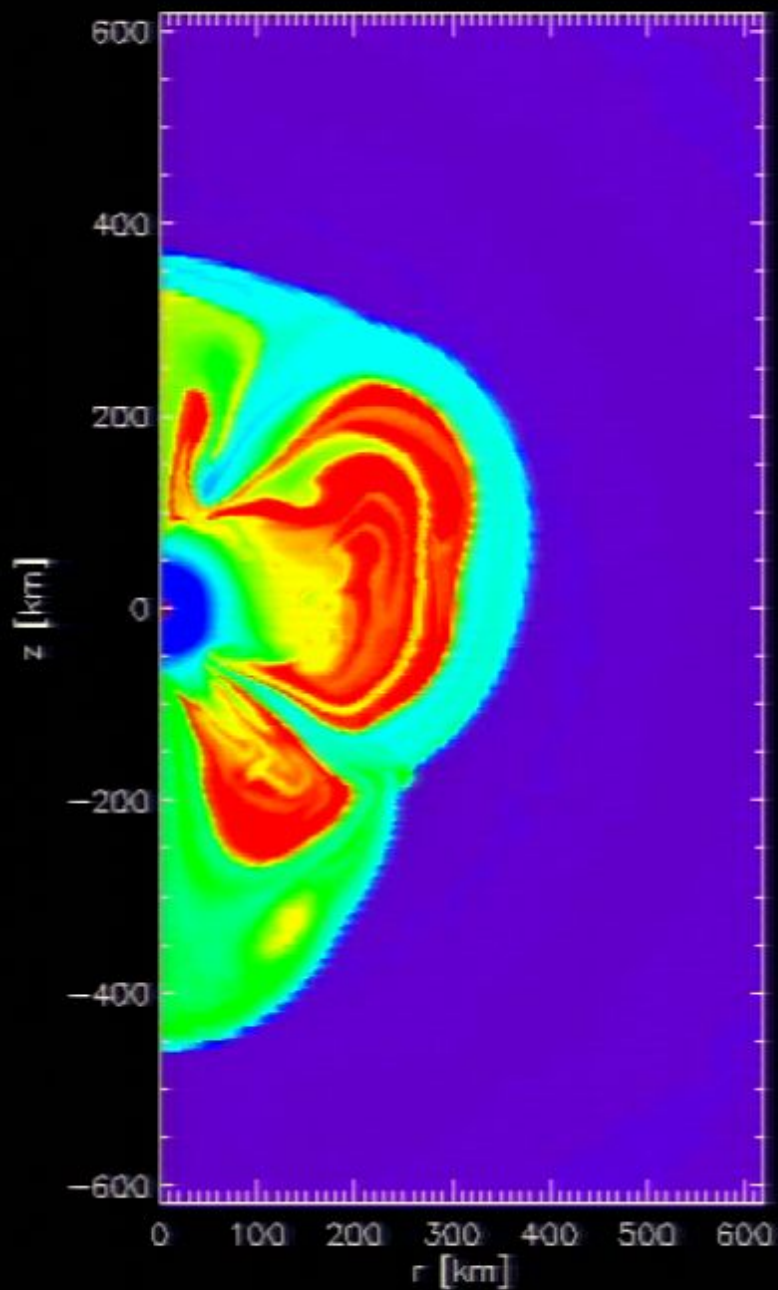
[Murphy, Ott and Burrows 2009]



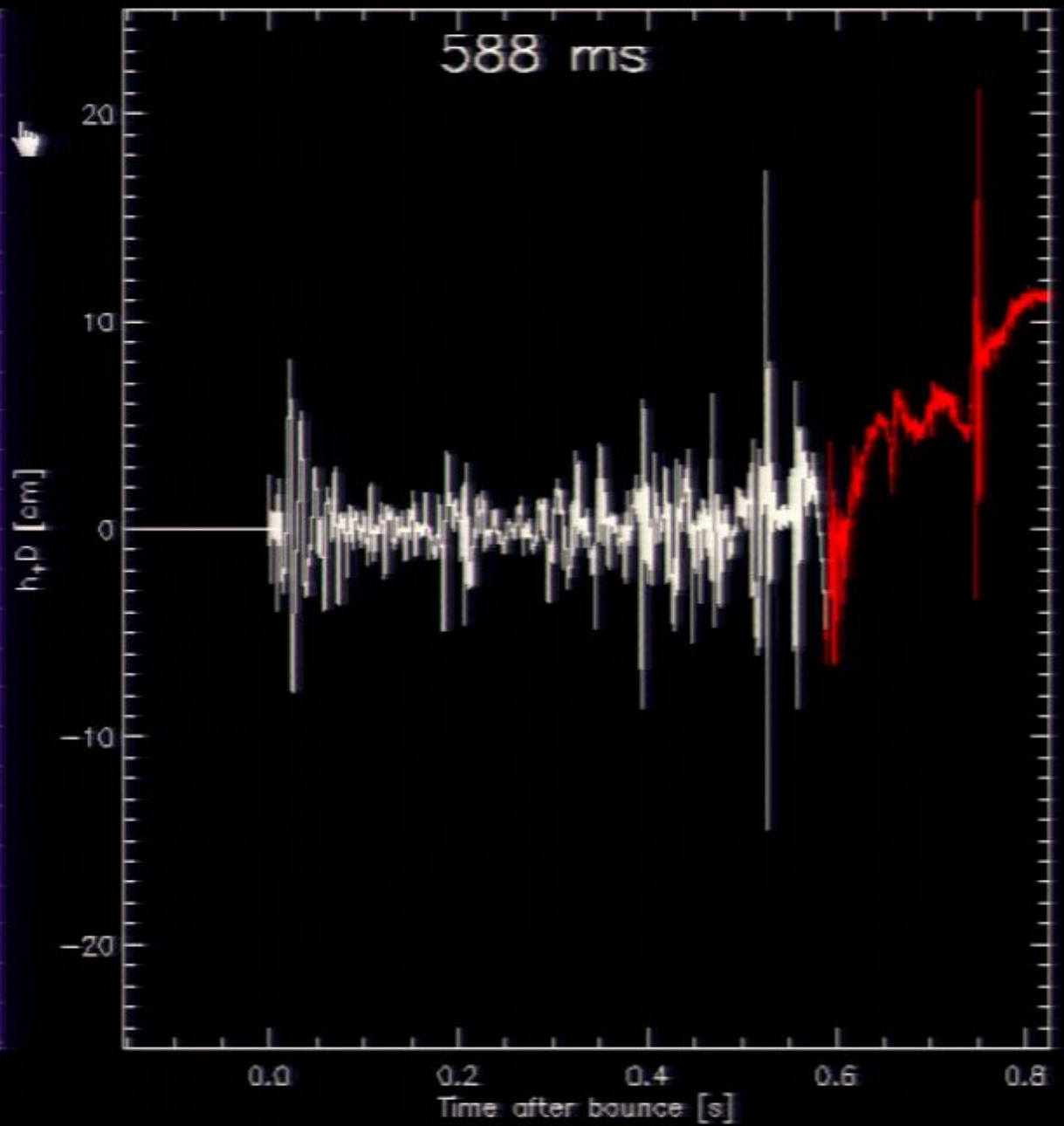
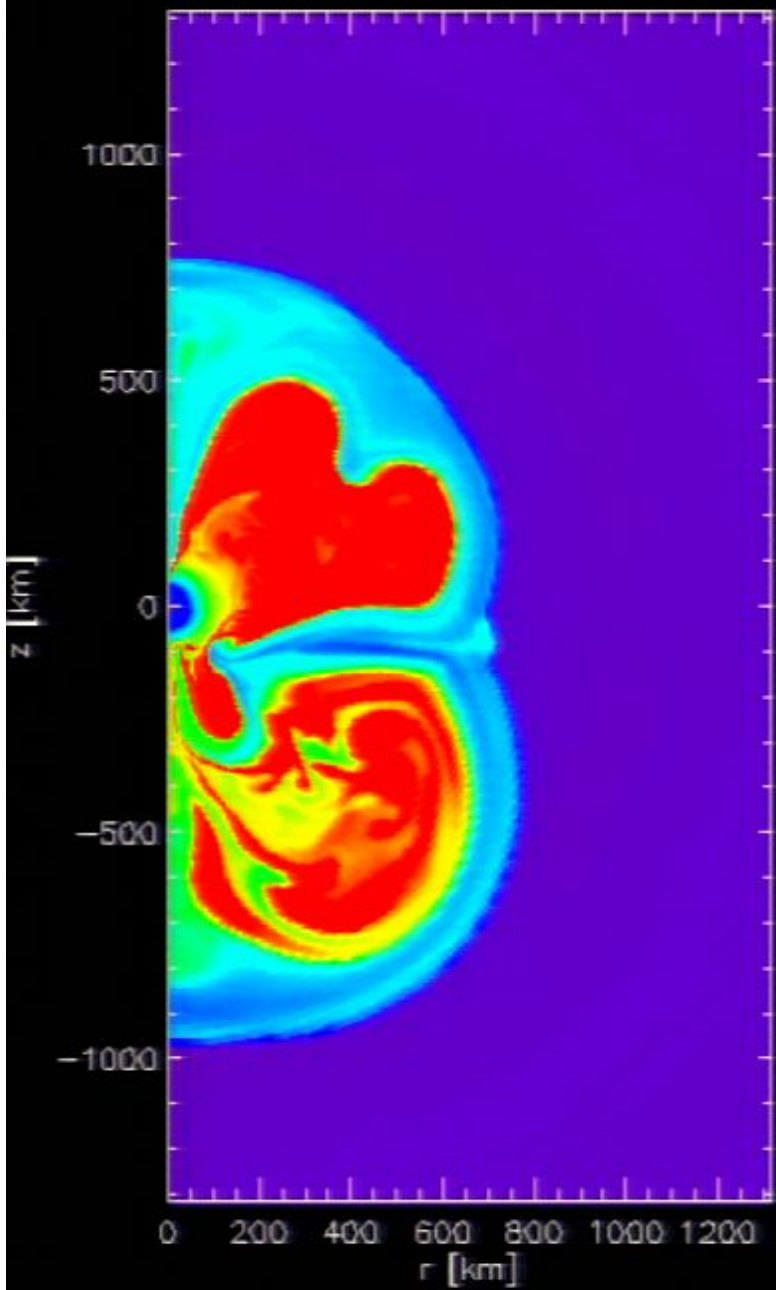
[Murphy, Ott and Burrows 2009]



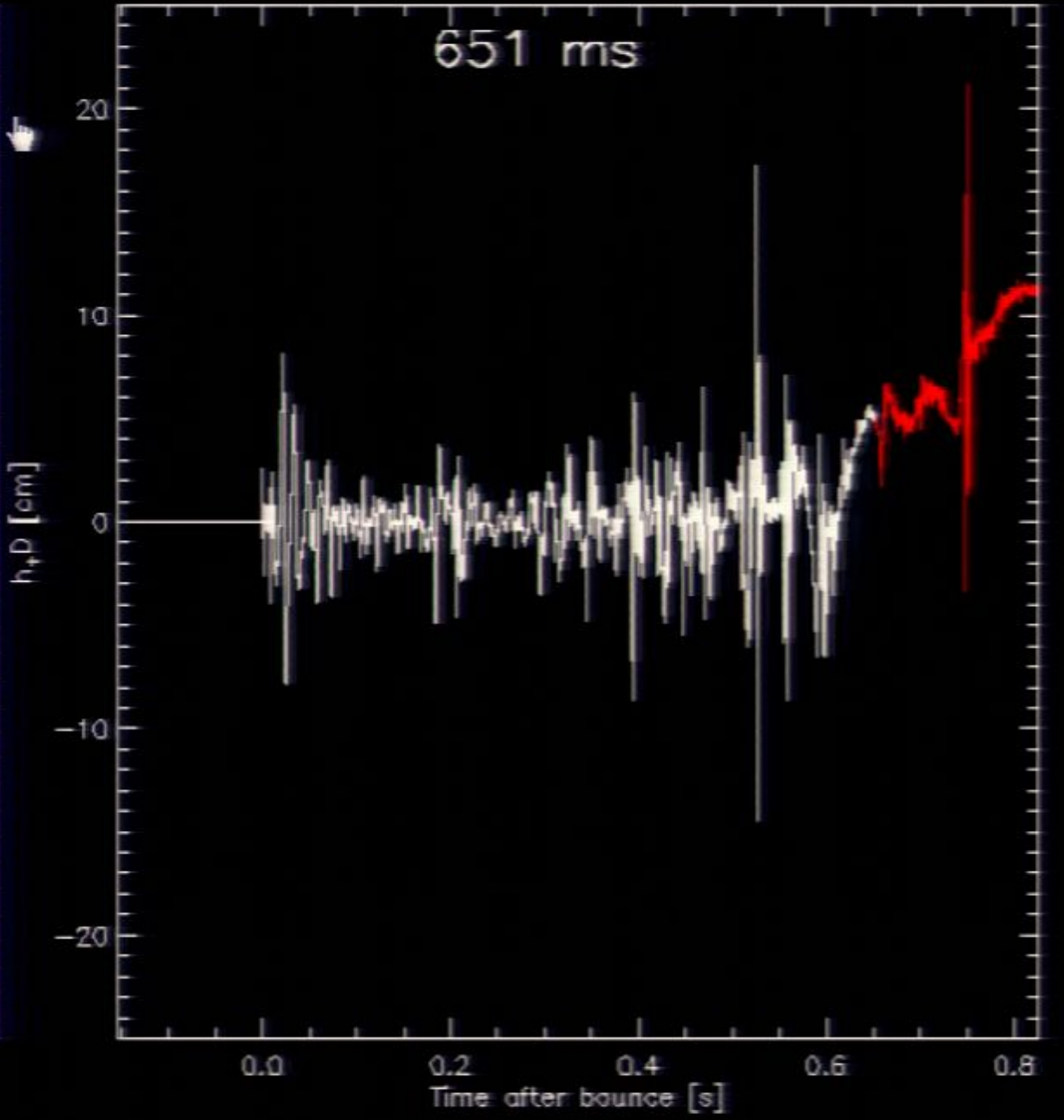
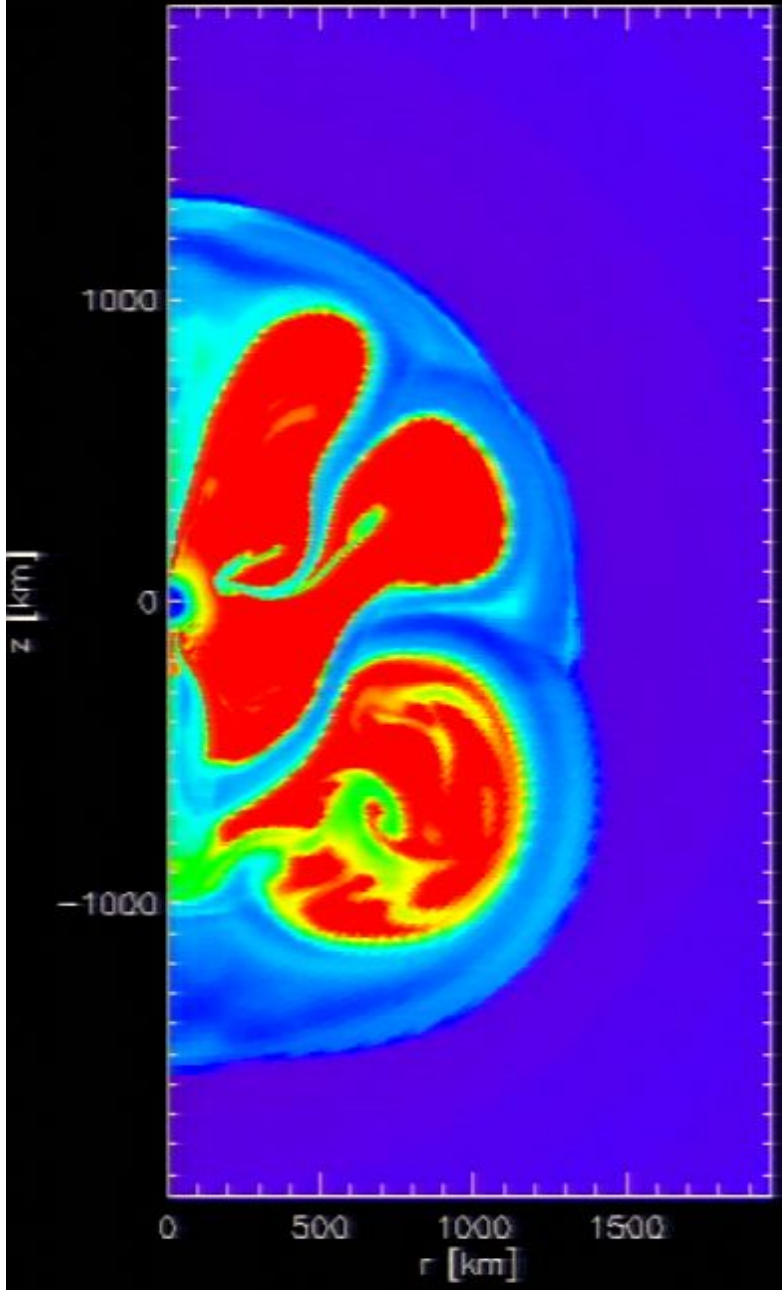
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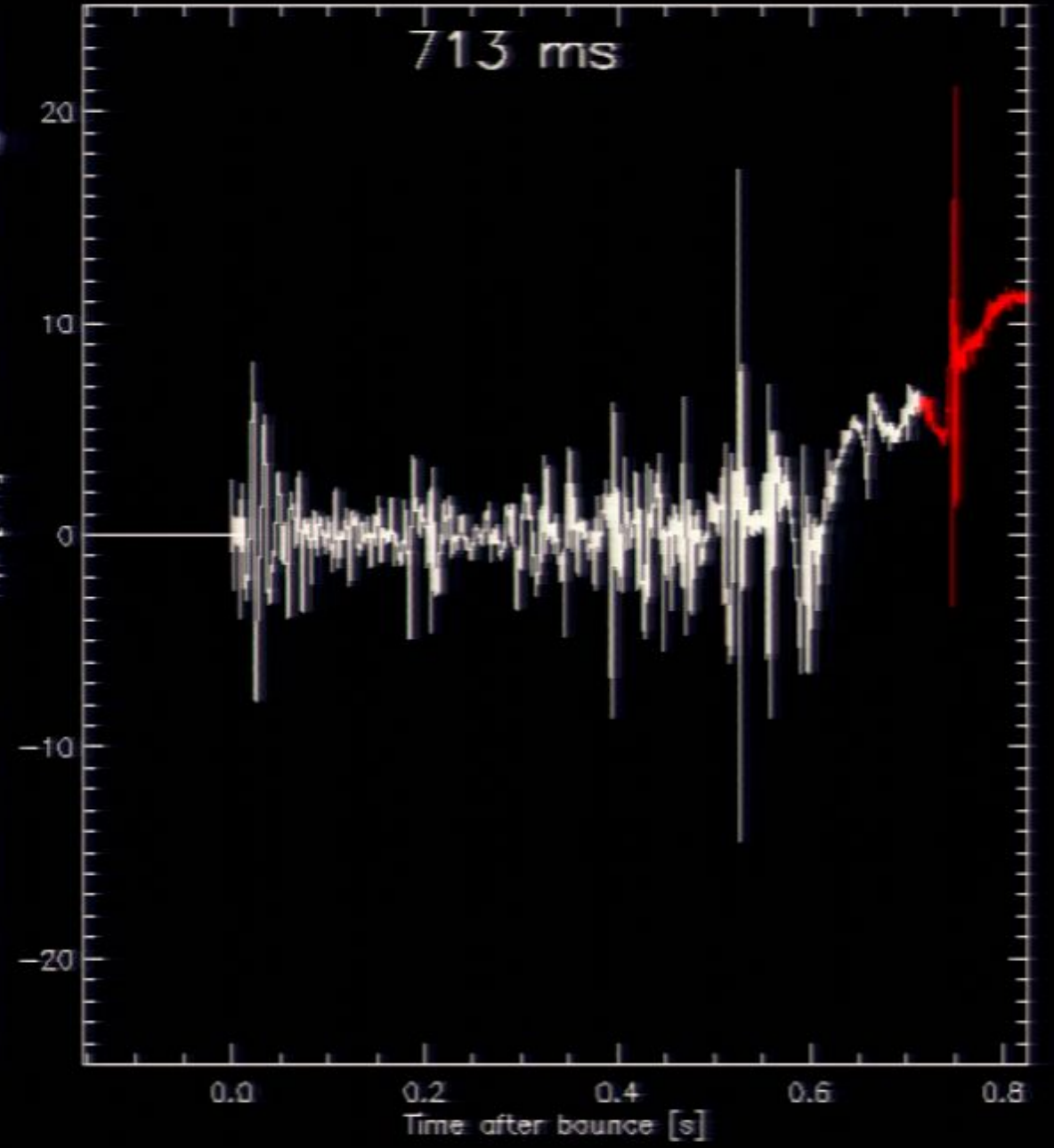
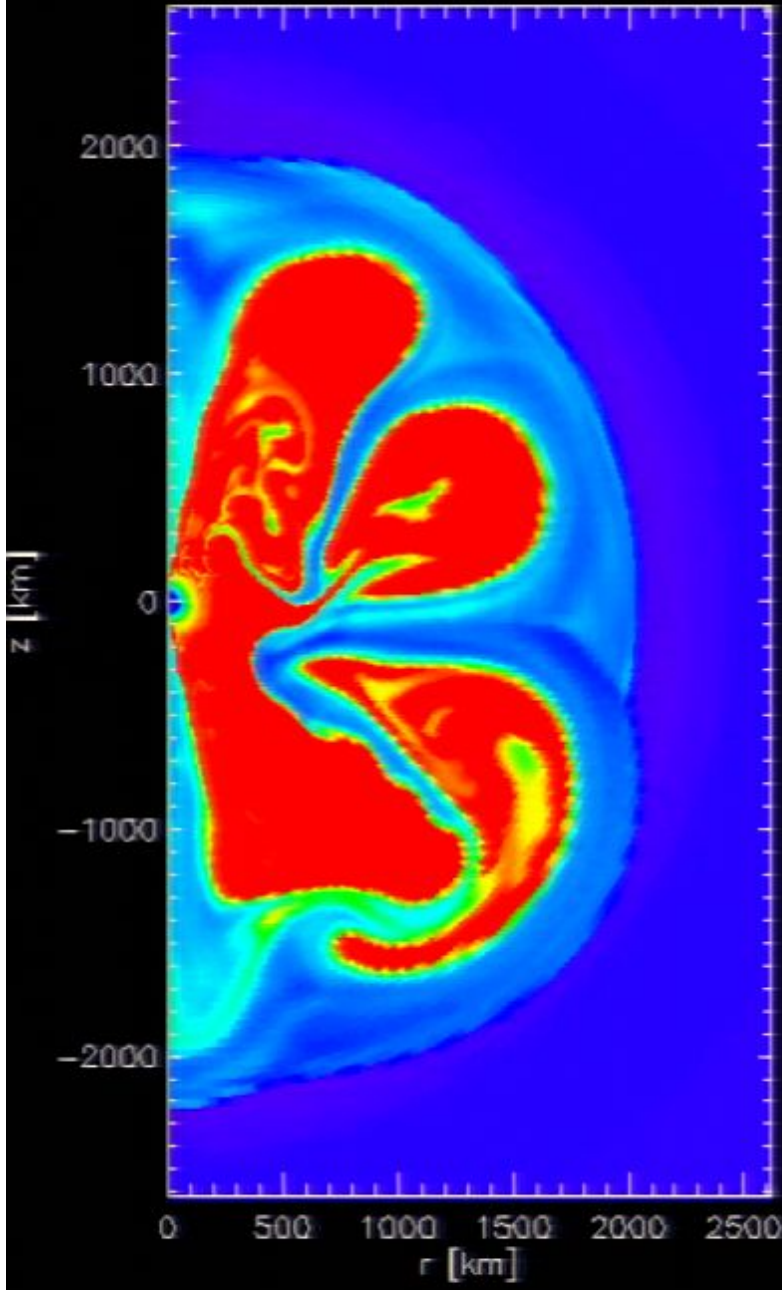
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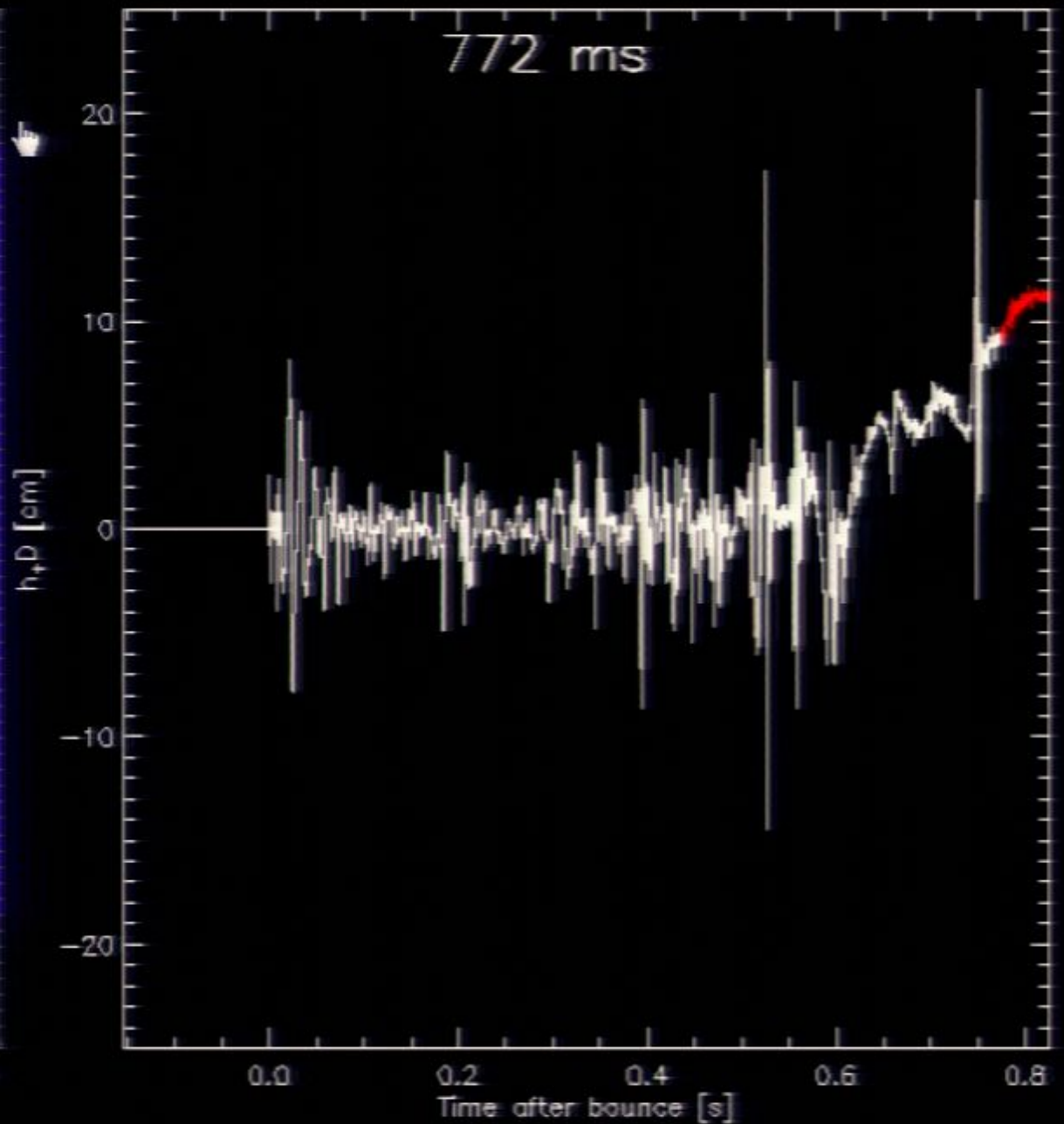
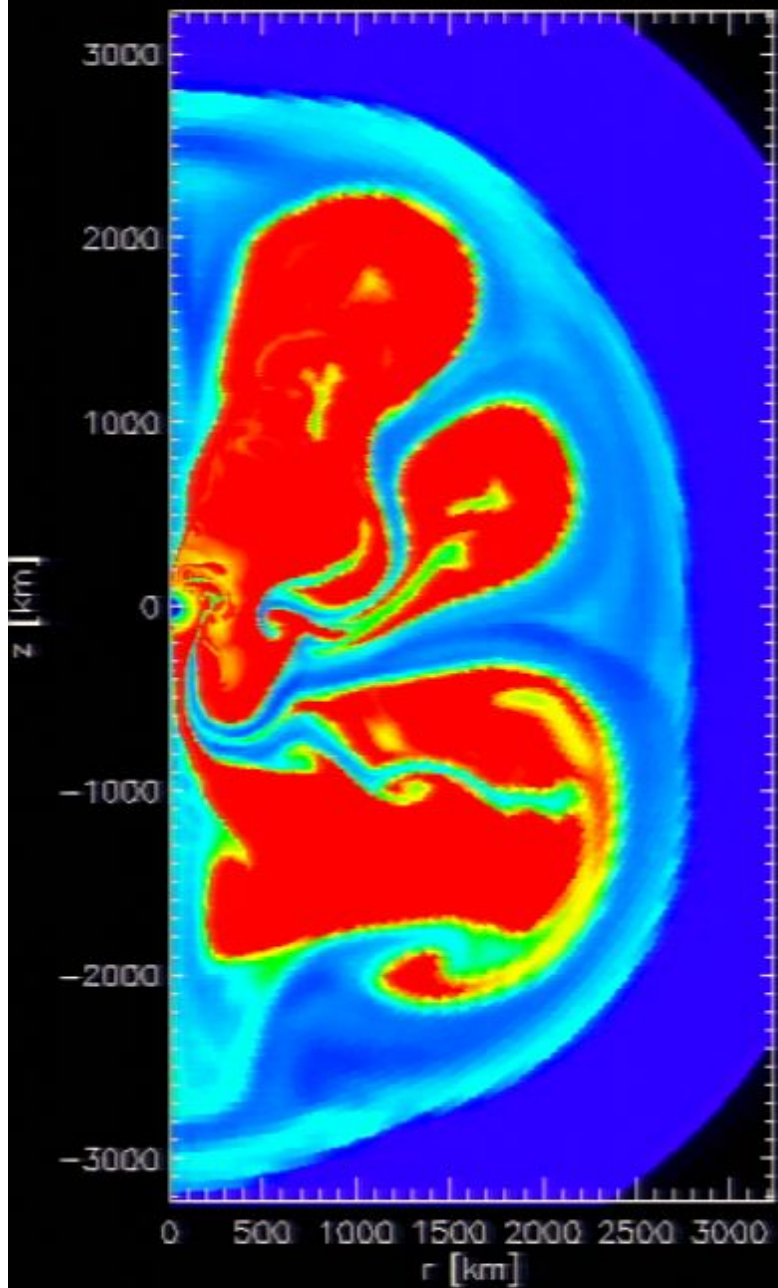
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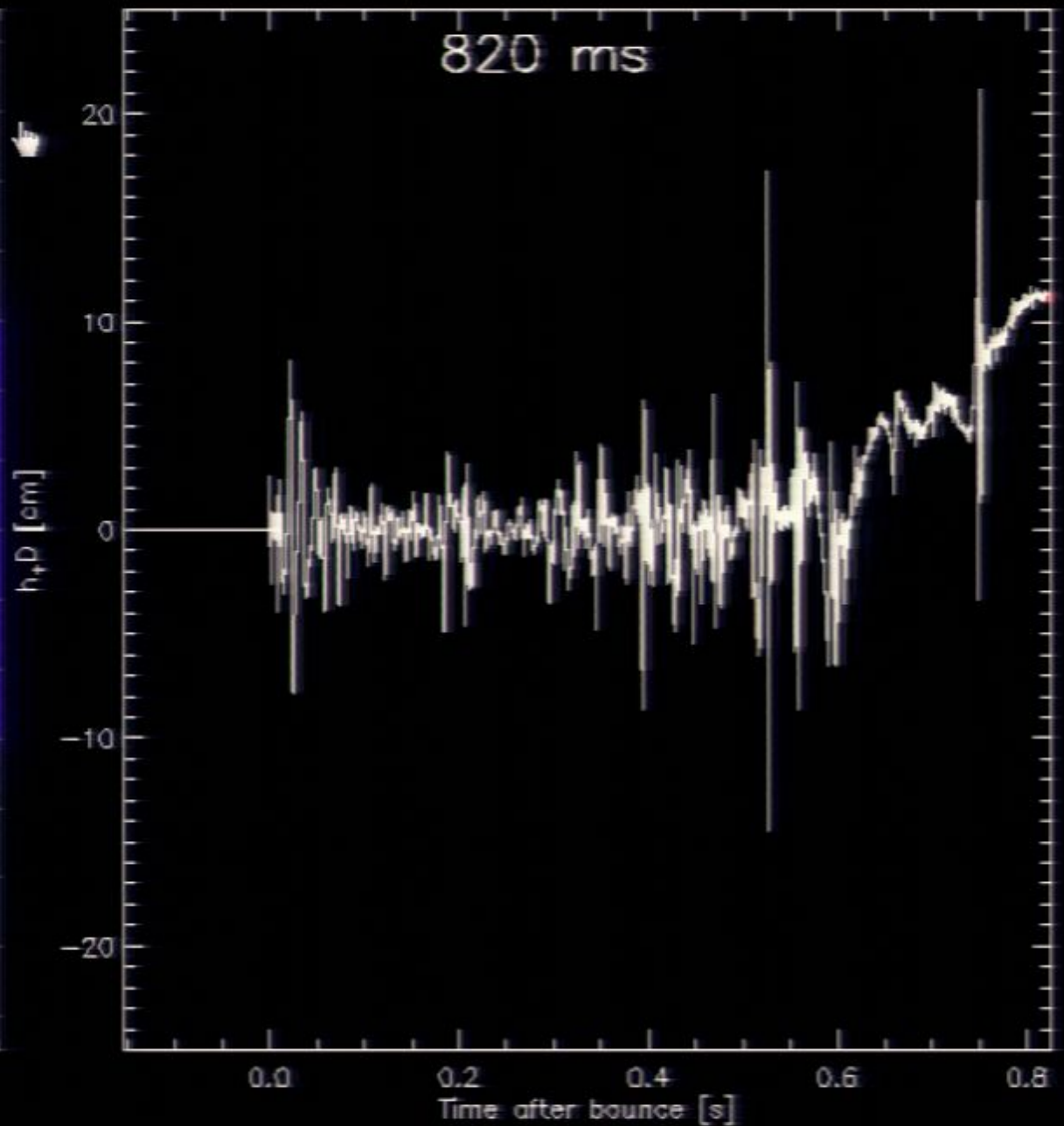
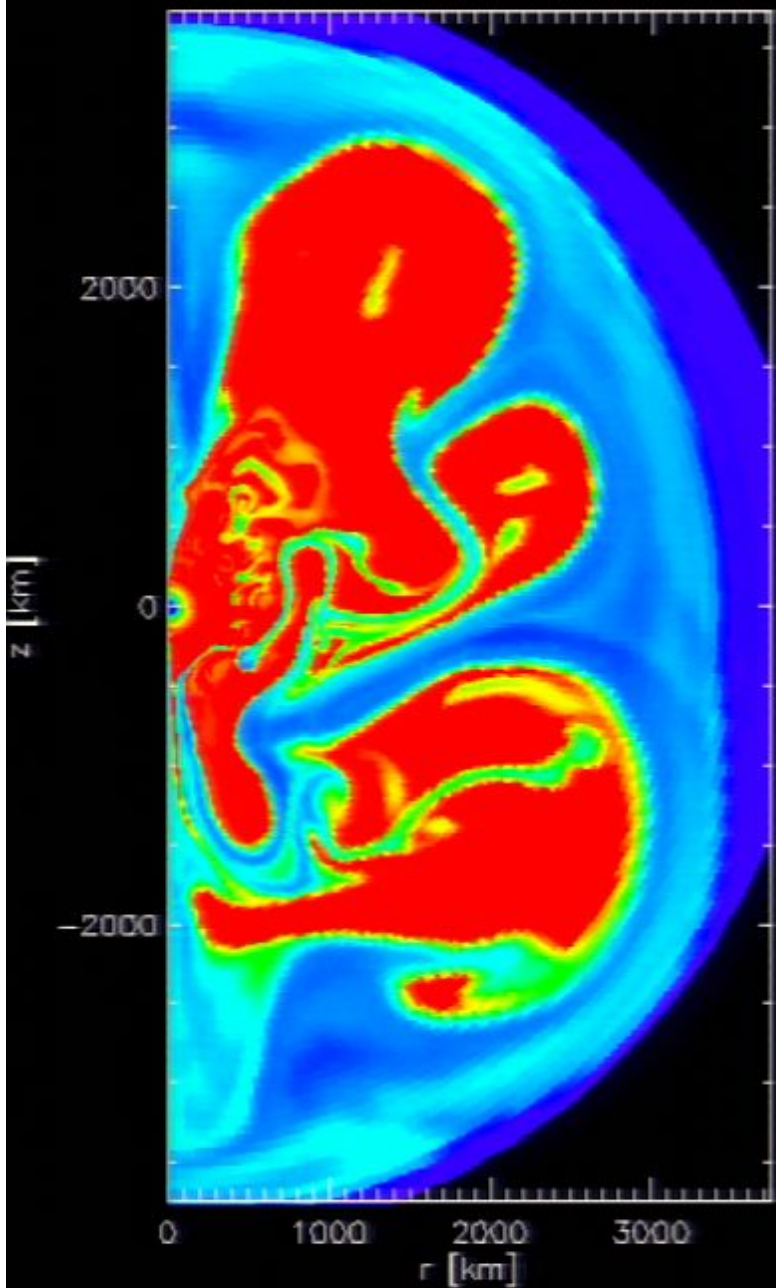
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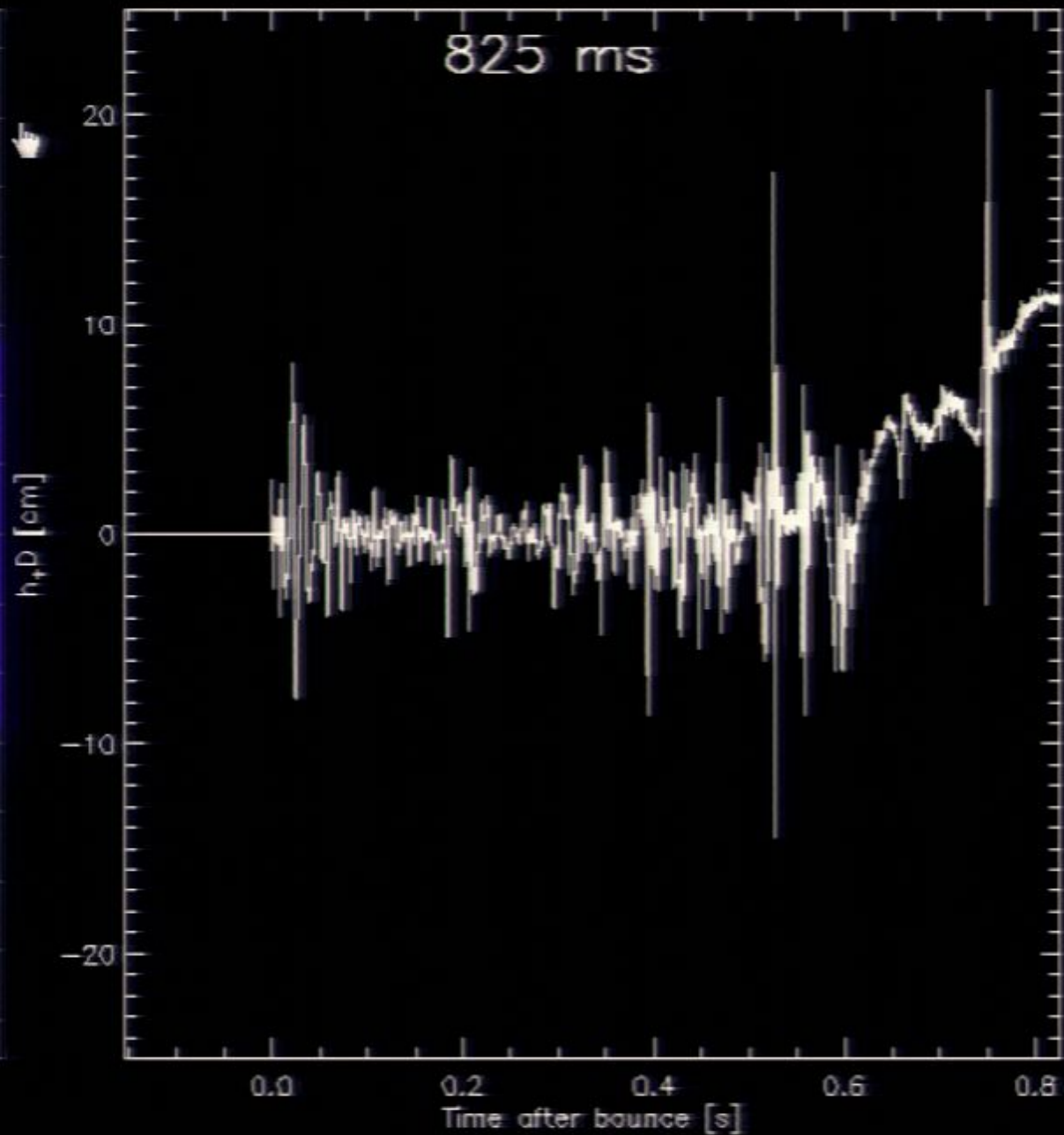
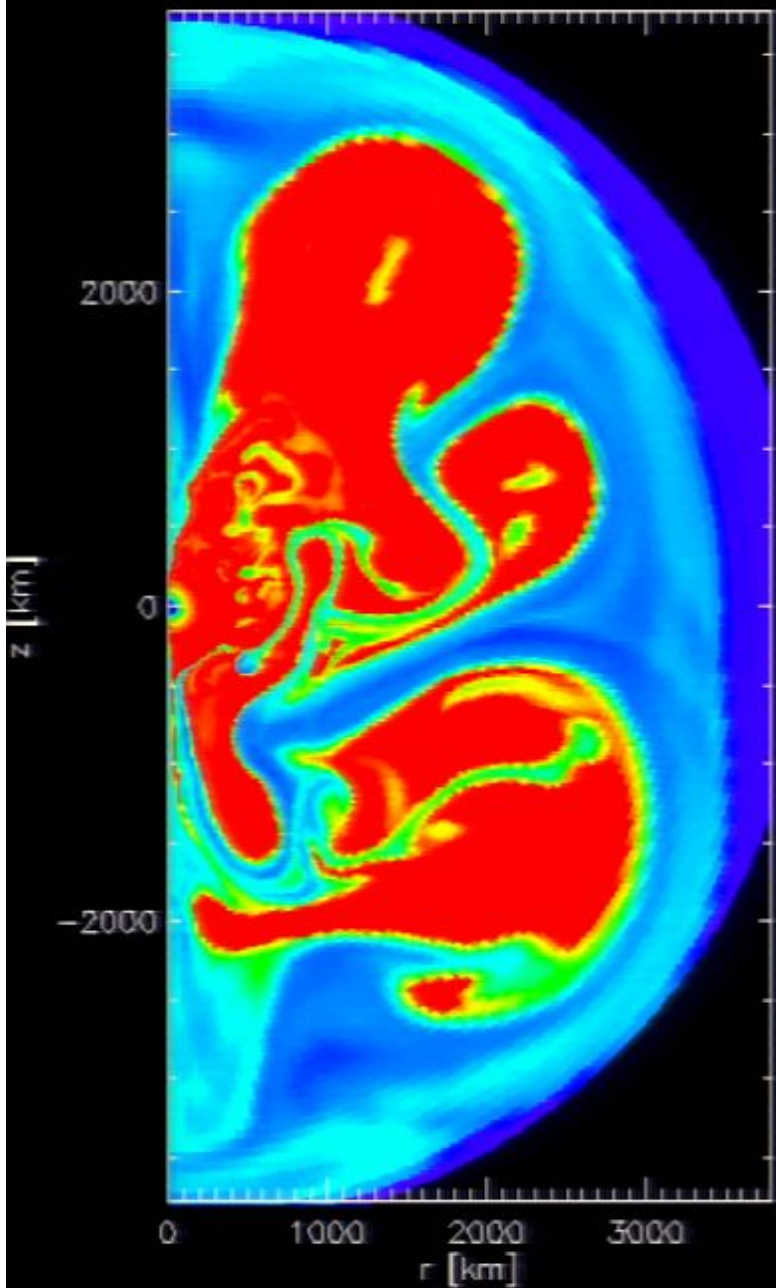
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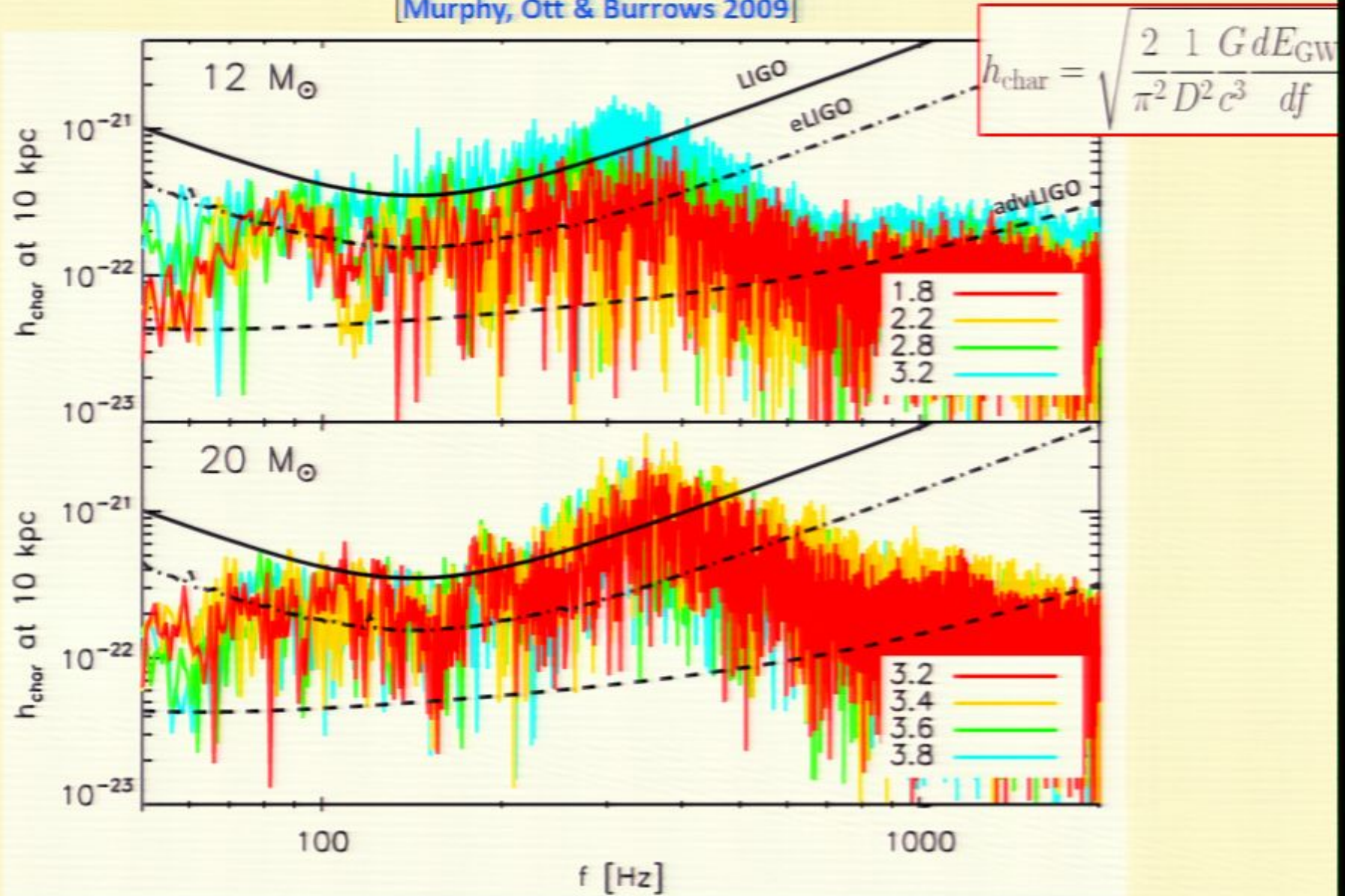
[Murphy, Ott and Burrows 2009]



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Detectability; Dependence on Progenitor & v-Luminosity

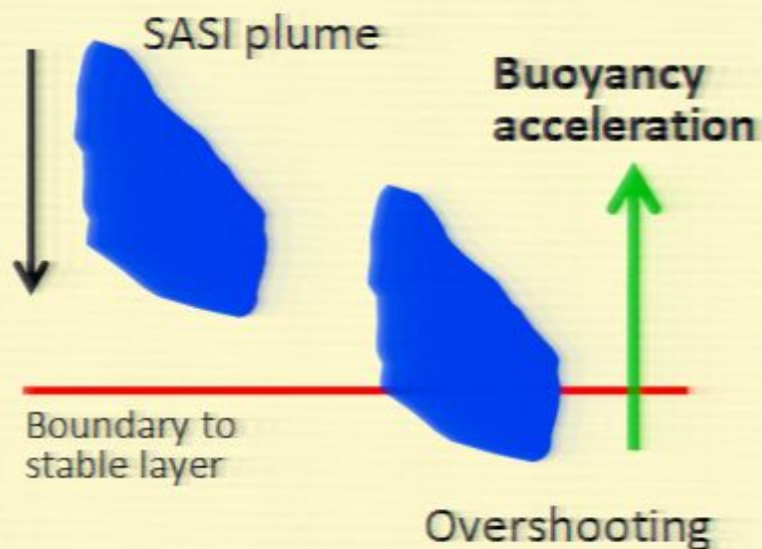
[Murphy, Ott & Burrows 2009]



Understanding the Characteristic GW Frequencies

[Murphy, Ott & Burrows 2009]

- **Assumption:** Strongest GW emission comes from SASI a downflow plume that is decelerated at the PNS surface.
- Use convection theory to study behavior in linear limit.



Brunt-Väisälä:

$$N^2 = \left(\frac{GM_r}{r^3} \right) \left(\frac{1}{\Gamma_1} \frac{d \ln P}{d \ln r} - \frac{d \ln \rho}{d \ln r} \right)$$

$N^2 > 0$: stable, $N^2 < 0$: unstable

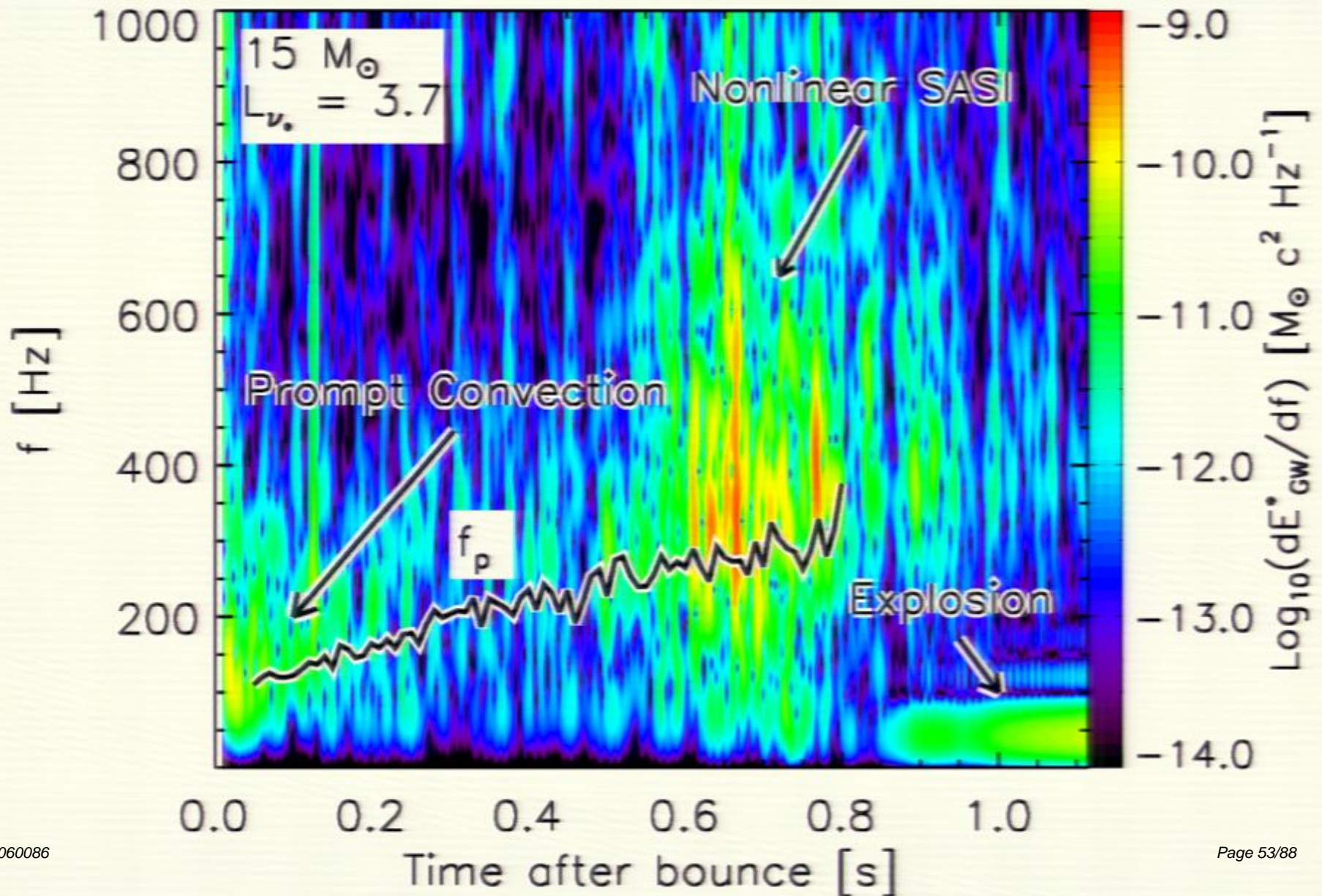
- Characteristic frequencies: Obtained through integration of buoyancy acceleration and analytic model for turning point:

$$f_p = 1/(2\pi t_p)$$

$$f_p \sim \frac{N}{2\pi}$$

GW Time-Frequency Evolution

[Murphy, Ott & Burrows 2009]



GW Extraction from CCSN Spacetimes

[[Reisswig](#), Ott, Sperhake, Schnetter, Pollney, Bishop]

GW Extraction in CCSN Spacetimes

[Reisswig, Ott et al. 2010]

- Most simulations of stellar collapse and core-collapse supernovae use some variant of the quadrupole formula (QF) to extract GWs:

$$h_{jk}^{TT}(t, \vec{x}) = \left[\frac{2}{c^4} \frac{G}{|\vec{x}|} \ddot{I}_{jk} \left(t - \frac{|\vec{x}|}{c} \right) \right]^{TT}$$

- Problems: not gauge invariant, definition of I_{jk} ambiguous in GR.
-> don't know how much we can trust QF GW predictions.

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- Collapse simulations with the open-source **Zelmani** core collapse simulation package.
 - > Based on **Cactus**, **Carpet AMR** driver, and **EinsteinToolkit GRHydro** code.
- Focusing on the axisymmetric GW signal of rotating core collapse:
 - > Physics is well understood and robust predictions can be made.
- Use Ψ_4 , ZM, (& Cauchy-Characteristic Extraction [to come soon])

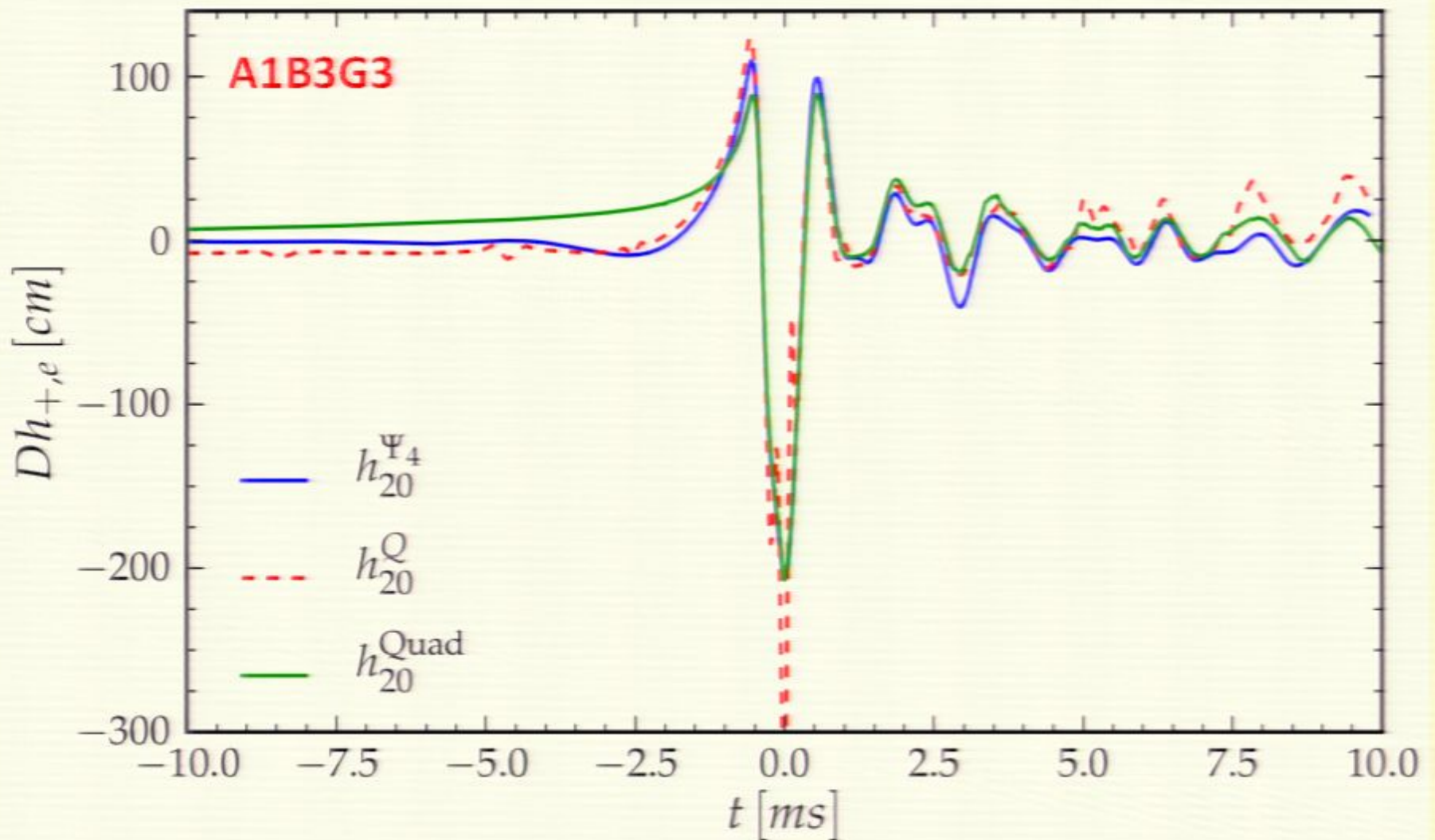
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- Use Ψ_4 , ZM, (& Cauchy-Characteristic Extraction [to come soon])
- Pick 3 models of Dimmellemeier et al. 2002 with simplified microphysics (hybrid cold + thermal EOS):
 - A1B3G3** – standard model, typical h_+
 - A1B3G5** – rapid collapse model (soft subnuclear EOS; small h_+)
 - A3B3G3** – rapid rotation, high h_+
- Extraction at large radii (> 1500 km).

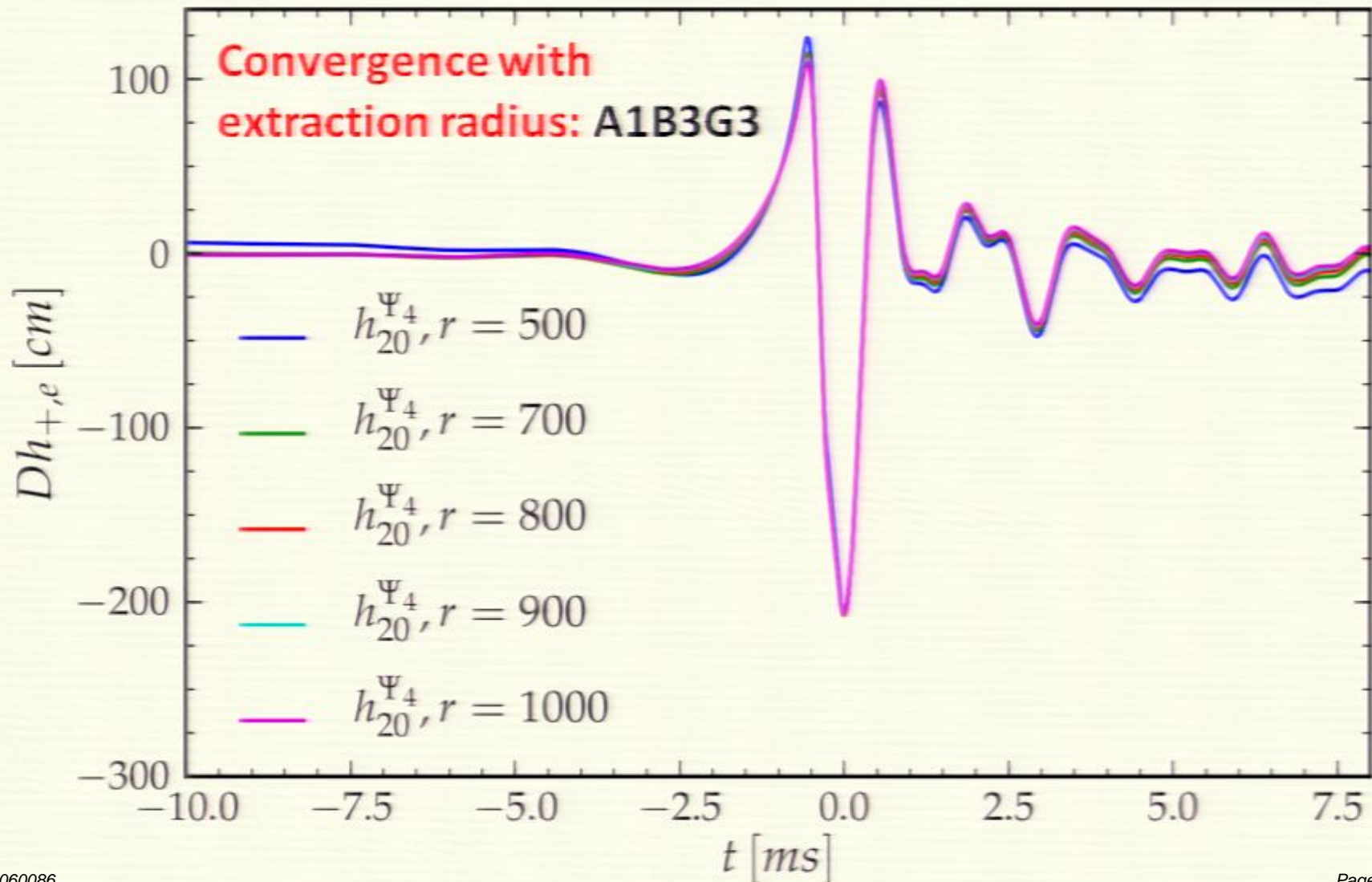
GW Extraction: Preliminary Results

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GW Extraction: Preliminary Results

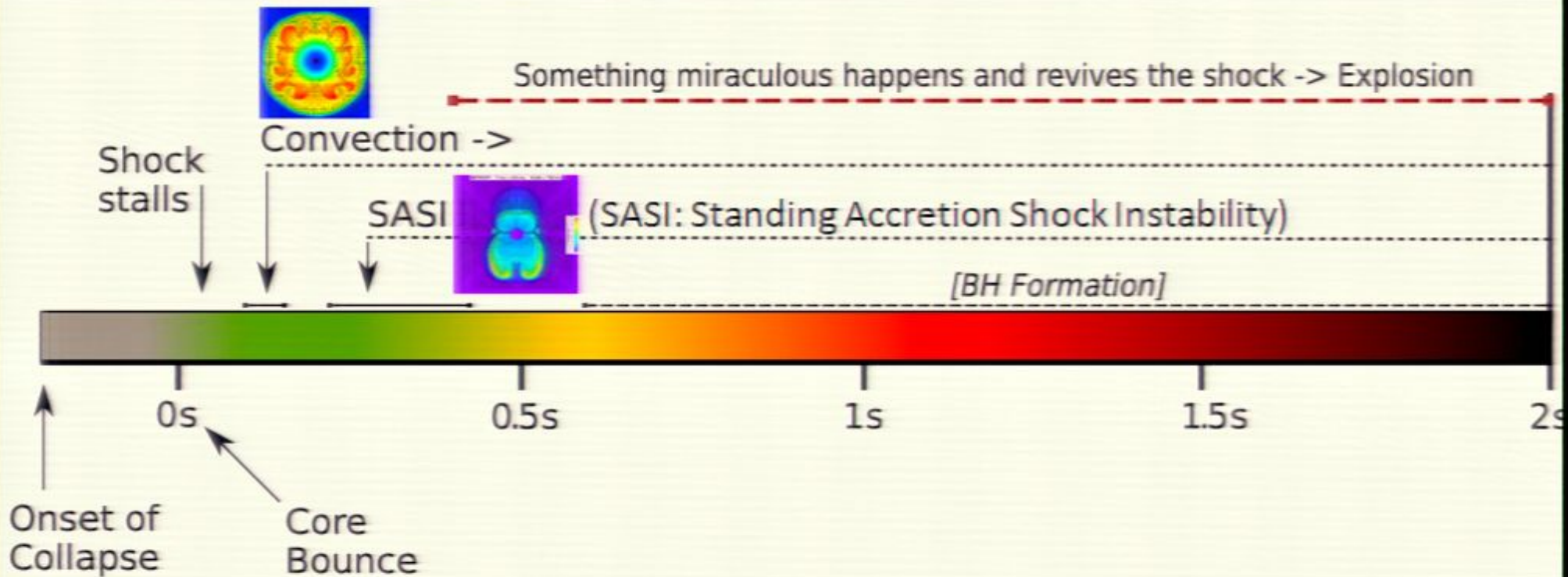
[Reisswig, Ott et al. 2010]



When Supernovae Fail:

Black Hole Formation

Core Collapse Timeline



- Energy reservoir: few $\times 10^{53}$ erg (100 B)
- Explosion energy: ~ 1 B
- Time frame for explosion: $\sim 0.3 - 2.0$ s after bounce.
- BH formation at baryonic PNS mass $\geq 1.8 - 2.5 M_{\text{Sun}}$ (?).

GR1D

[O'Connor & Ott 2010 CQG]

- **GR1D**: *Open-Source 1.5D GR hydrodynamics code.*
- Available from <http://www.stellarcollapse.org>.
- **Eulerian Radial-gauge, polar-slicing** (-> Schwarzschild-like coordinates).

$$ds^2 = -\alpha(r,t)^2 dt^2 + X(r,t)^2 dr^2 + r^2 d\Omega^2$$

$$\alpha(r,t) = \exp[\phi(r,t)], \quad X(r,t) = \left(1 - \frac{2m(r,t)}{r}\right)^{-1/2}$$

- **Choice of coordinates greatly simplifies GR hydro equations (zero shift).**
- **Disadvantage: Cannot evolve past horizon formation**
(like May & White, Misner & Sharp, van Riper formulations).
- **GR Hydro equations in GR1D**
Implemented as finite-volume scheme with PPM & HLLE.

$$\partial_t \vec{U} + \frac{1}{r^2} \partial_r \left[\frac{\alpha r^2}{X} \vec{F} \right] = \vec{S}$$

GR1D: Approximate Rotation

- **Rotation in 1D: “Shellular”** – constant Ω on spherical shells.

Effective centrifugal force: $f_{\text{cent}} = 2/3 \omega^2 r$

$$\partial_t(S_\phi) + \frac{1}{r^2} \partial_r \left(\frac{\alpha r^2}{X} F_\phi \right) = S_\phi$$

$$S_\phi = \rho h W^2 v_\phi r ,$$

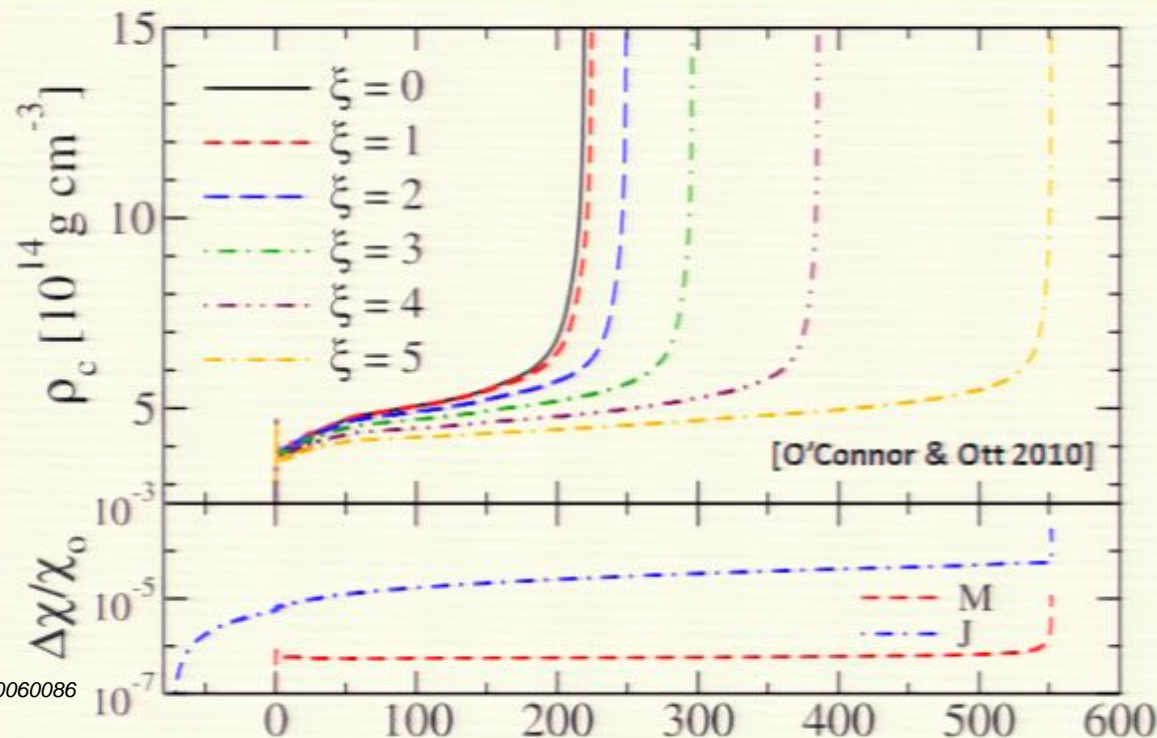
$$F_\phi = \rho h W^2 v_\phi r v = S_\phi v ,$$

$$S_\phi = \rho h W^2 \alpha v v_\phi X \left[4\pi r^2 P + \frac{m}{r} \right]$$

Extra term in equation for r momentum:

$$+ \alpha \frac{2}{3} \left(\frac{\rho h W^2 v_\phi^2}{X r} \right)$$

+ additional terms in metric quantities due to ϕ momentum.



Central density, 40- M_{Sun} model put into rotation with increasing initial central angular velocities.

Conservation of baryonic mass and angular momentum.

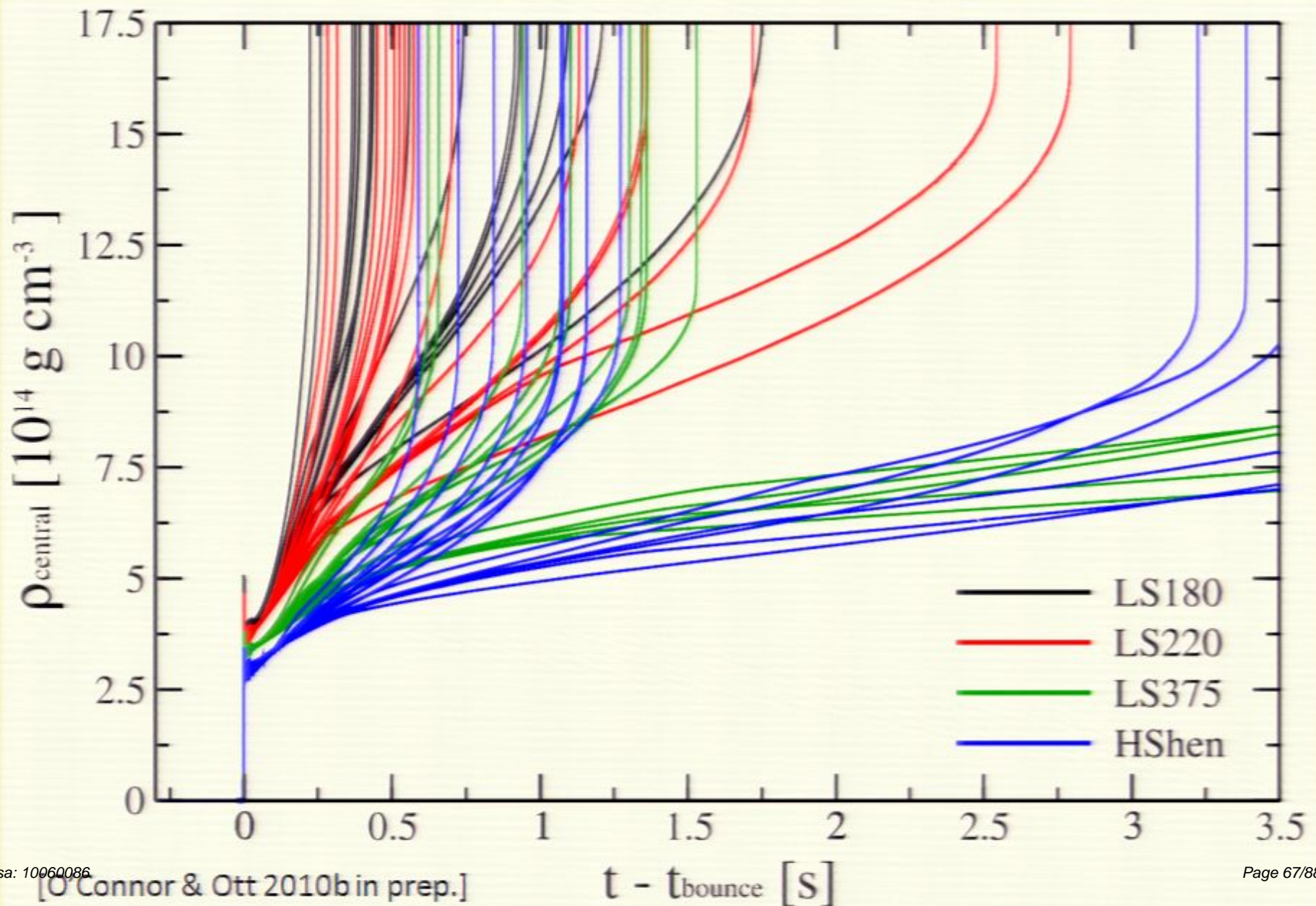
GR1D: EOS & Microphysics

- Multiple finite-temperature microphysical nuclear EOS:
H. **Shen** et al. 1998, **Lattimer & Swesty** 1991 with $K=\{180,220,375\}$ MeV.
EOS tables available in HDF5 format on <http://www.stellarcollapse.org>.
- Low-density EOS: Timmes EOS (tabulated & matched).
- Neutrinos during collapse: effective $Y_e(\rho)$ approx. [Liebendörfer '05].
- Postbounce: **3-flavor, energy-averaged (gray) neutrino leakage scheme**
- Approximate neutrino heating:

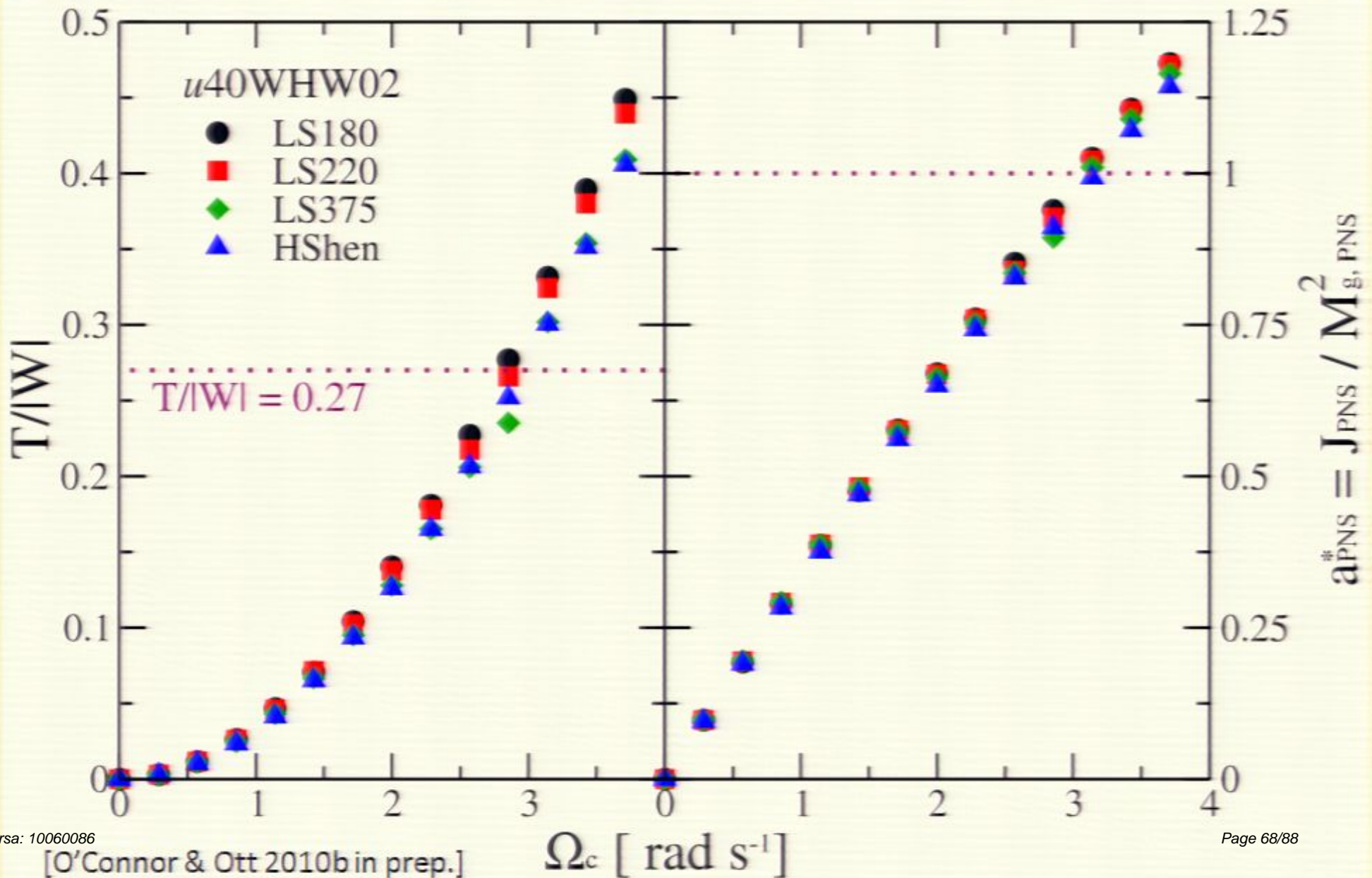
$$Q_{\nu_i}^{\text{heat}}(r) = f_{\text{heat}} \frac{L_{\nu_i}^{\text{FRF}}(r)}{4\pi r^2} \sigma_{\text{heat},\nu_i} \frac{\rho}{m_u} X_i \left\langle \frac{1}{F_{\nu_i}} \right\rangle e^{-2\tau_{\nu_i}}$$

- Nuclear Reaction Network & consistent multi-species advection.
(work in progress)

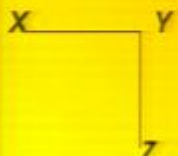
Parameter Study...



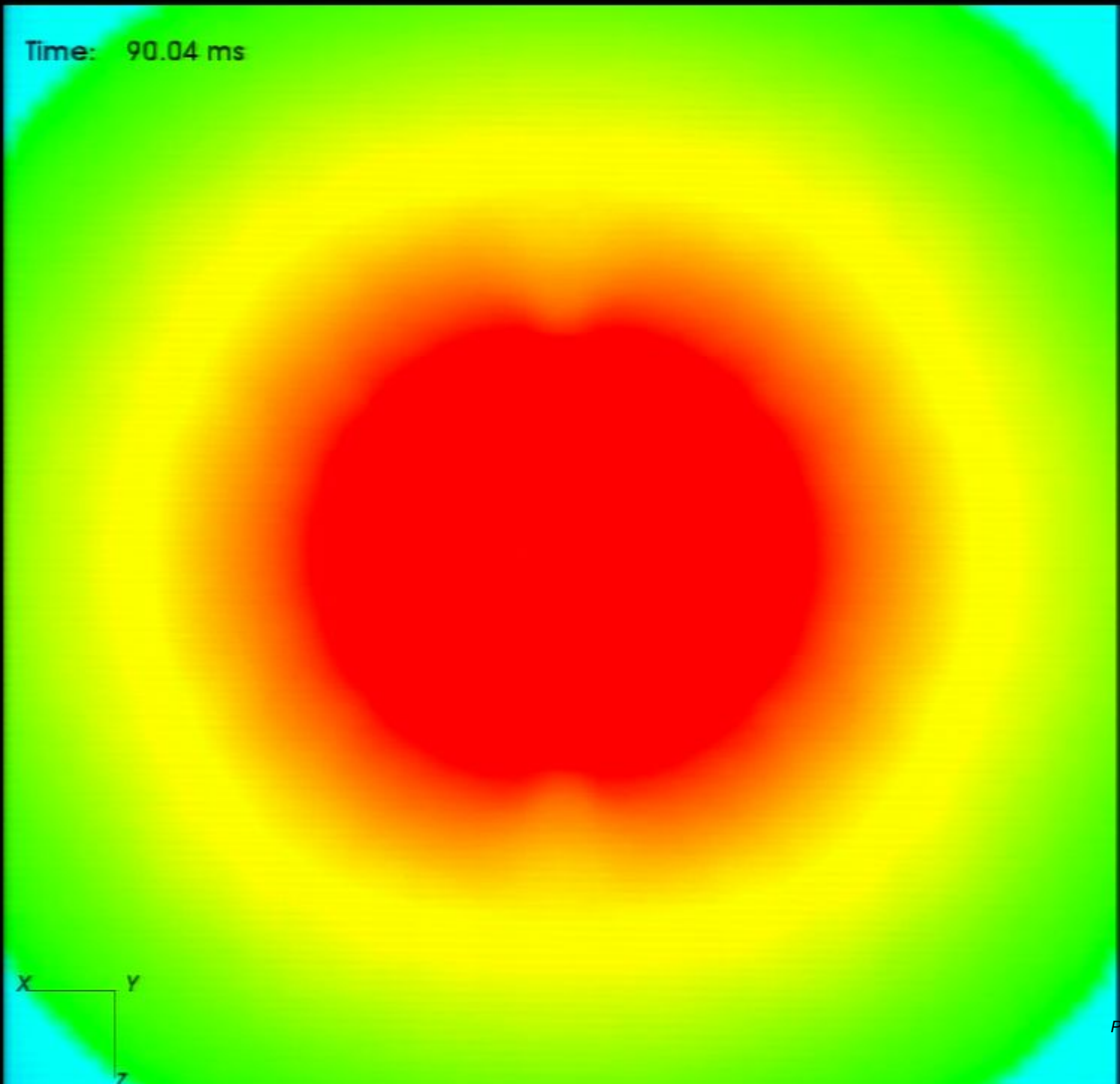
BH Birth Spin



Time: 75.67 ms

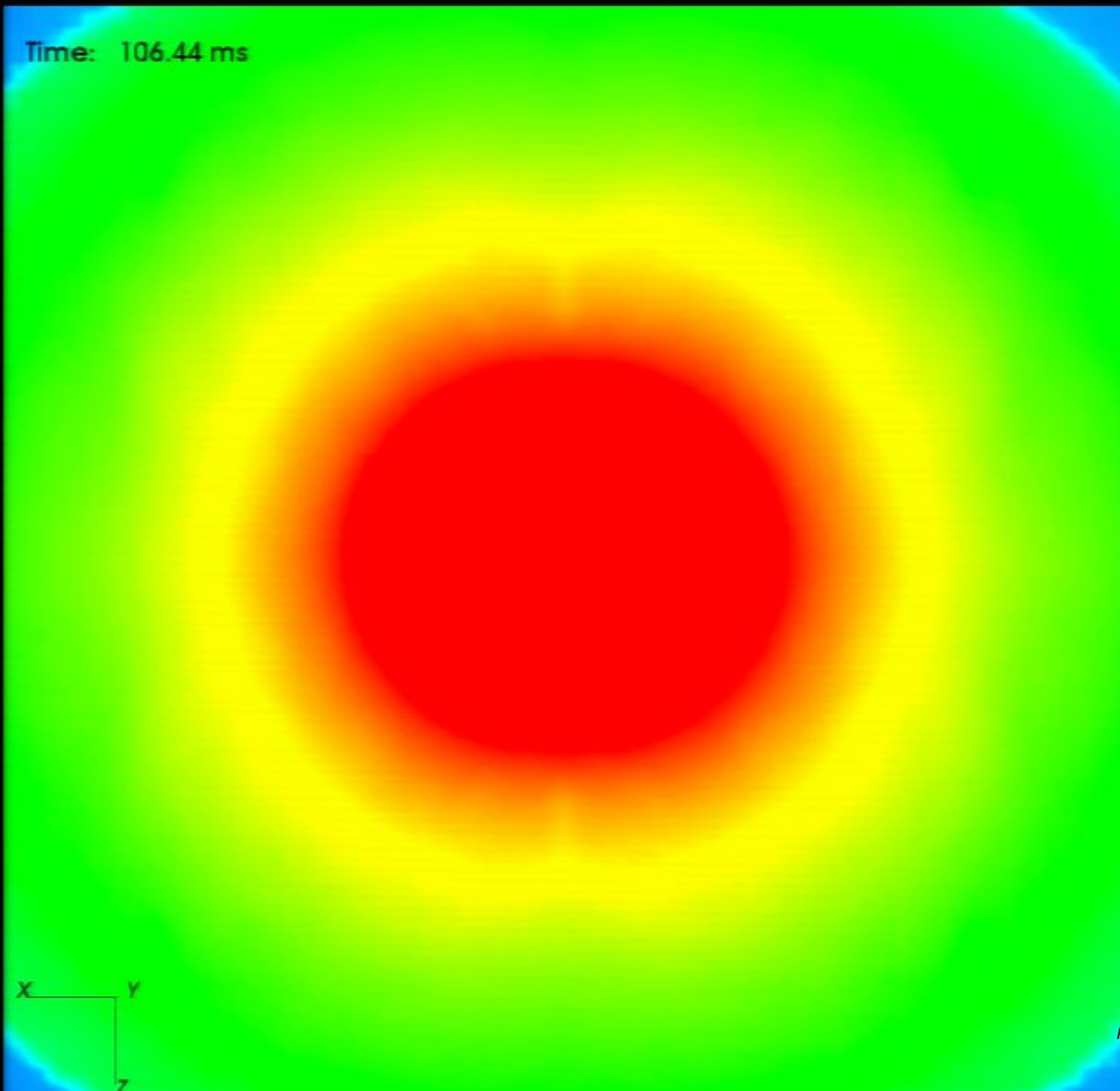


Time: 90.04 ms



Page

Time: 106.44 ms



X Y
Z

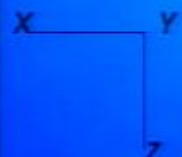
P

Time: 114.25 ms

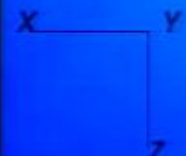


Pa

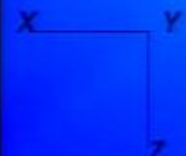
Time: 130.40 ms



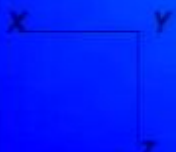
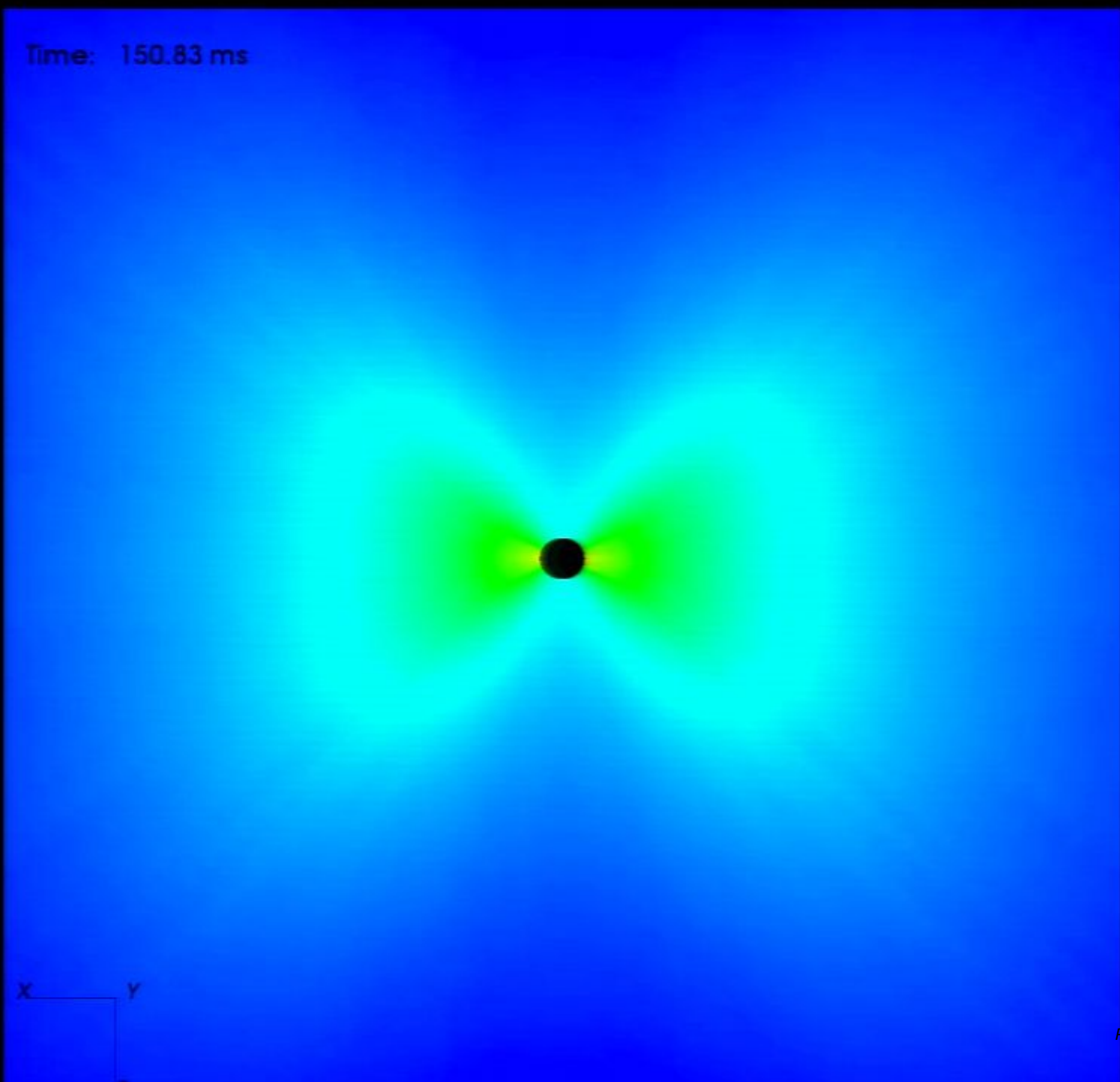
Time: 136.95 ms



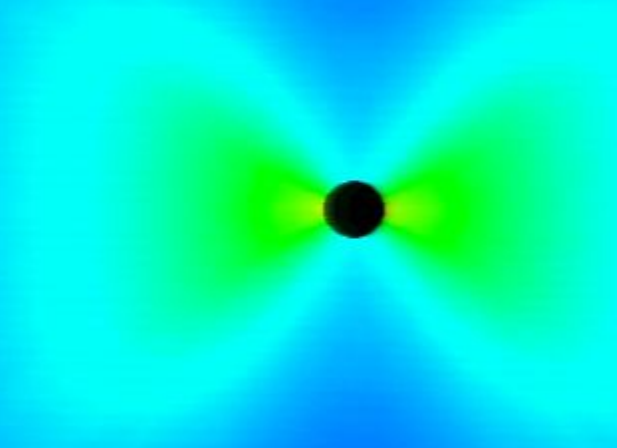
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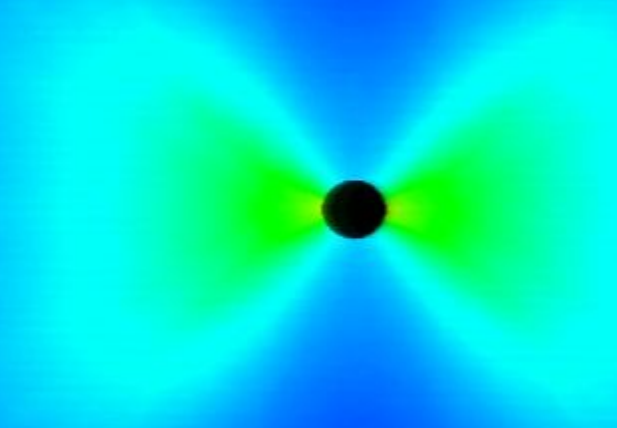
Time: 150.83 ms



Time: 157.13 ms



Time 167.22 ms

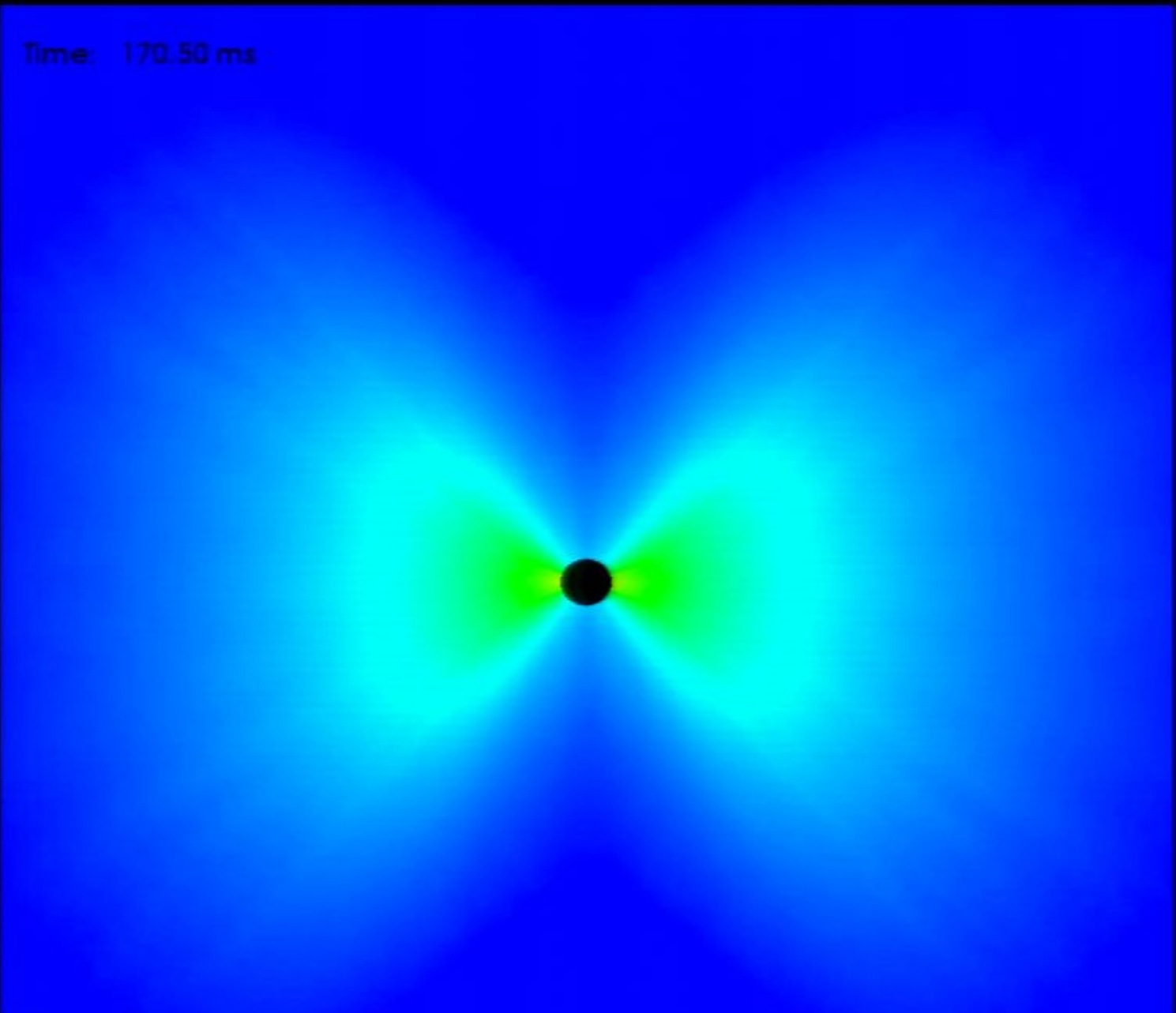


X Y

Z

Page

Time: 170.50 ms

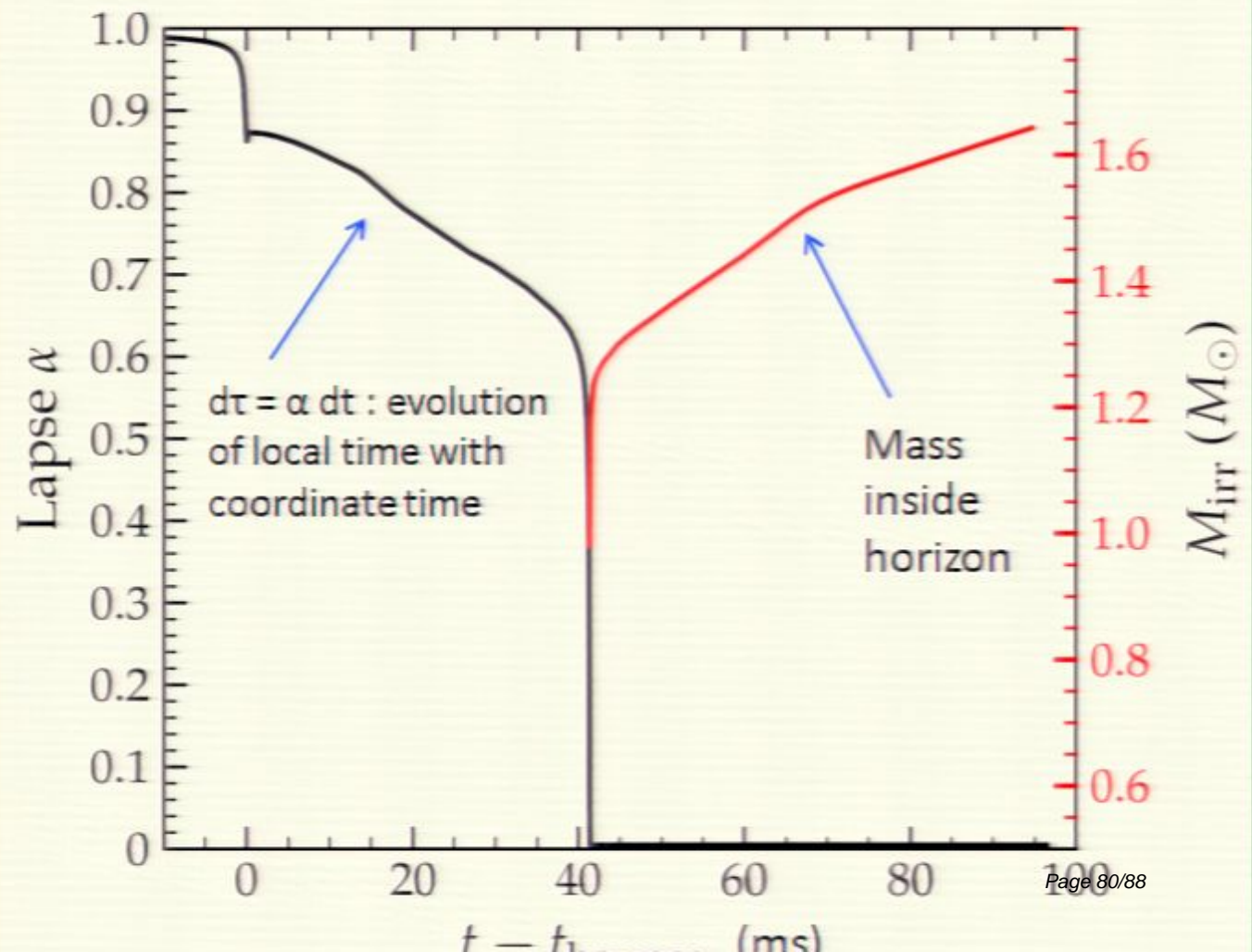


X Y

Z

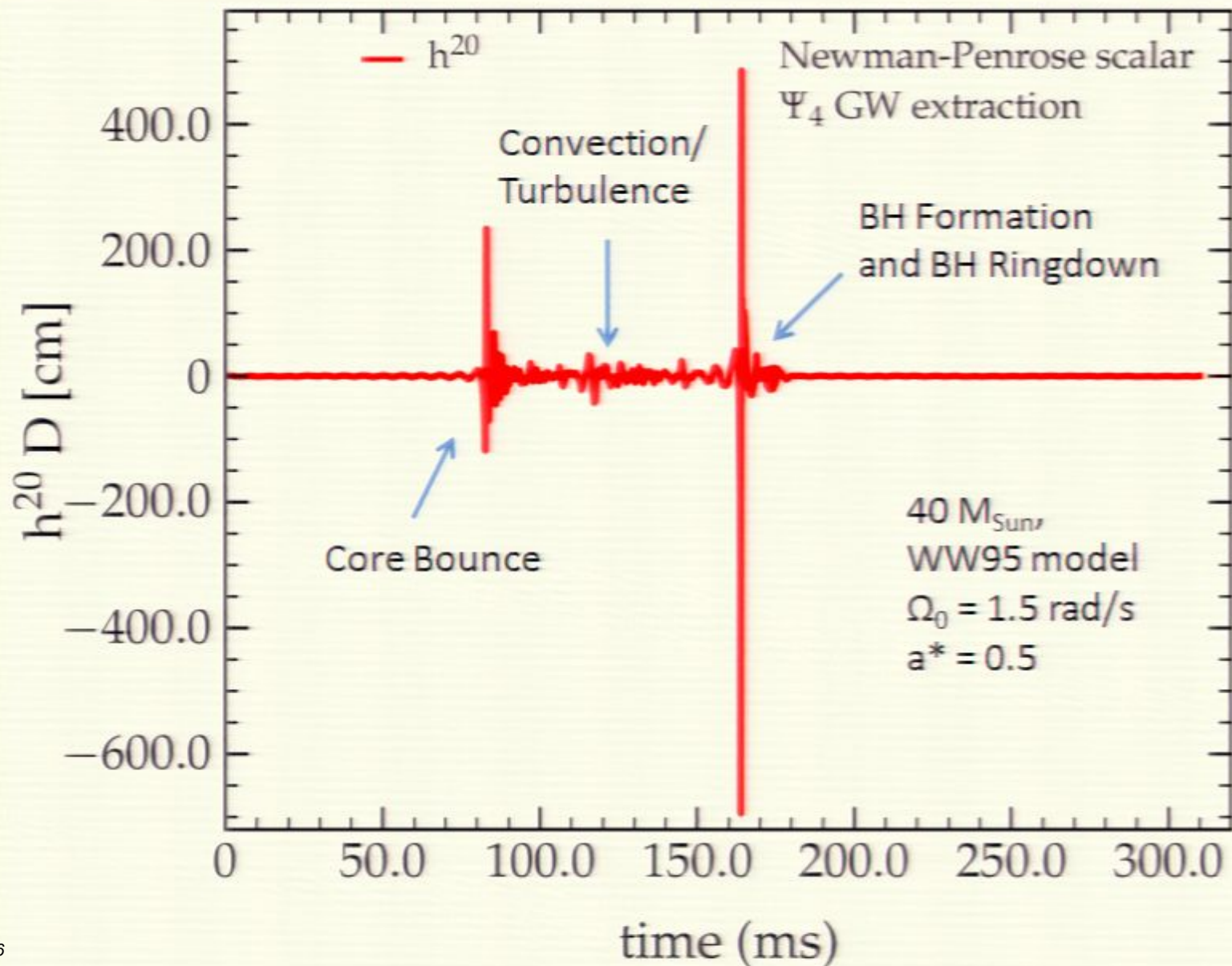
3D BH Formation [Ott et al. 2010 in prep.]

- Exploratory calculation: 3D, but restricted to octant ($m \geq 4$).
 - 40- M_{Sun} Woosley & Weaver 1995 progenitor.
 - Simplified EOS: Piecewise polytrope with thermal component, $\Gamma=2$ supernuclear
 - Moderate rotation, $\Omega_0 = 1.5$ rad/s.
 - 11 levels of AMR.
 - BH forms with Kerr spin parameter $a^* = J/M^2 \sim 0.5$



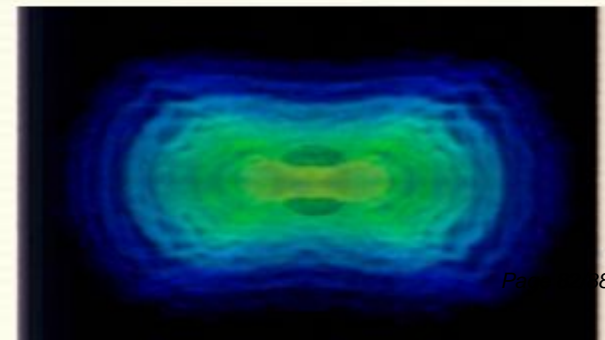
Gravitational Waves from BH Formation

[Ott et al. 2010 in prep.]



Summary

- Physical model for the spectral characteristics of GW emission from neutrino-driven core-collapse supernovae.
- Comparison of quadrupole formula with Zerilli-Moncrief and Newman-Penrose for core collapse spacetimes.
QF good enough, considering SN physics/distance uncertainties.
- **Comprehensive study of black hole formation in 1.5D:**
 - No ‘prompt’ black hole formation in ordinary massive stars.
 - Protoneutron stars that would make super-Kerr BHs go nonaxisymmetrically unstable (-> limit on BH spin!)
- First preliminary results from 3D GR simulations of failing core-collapse supernovae and black hole formation.



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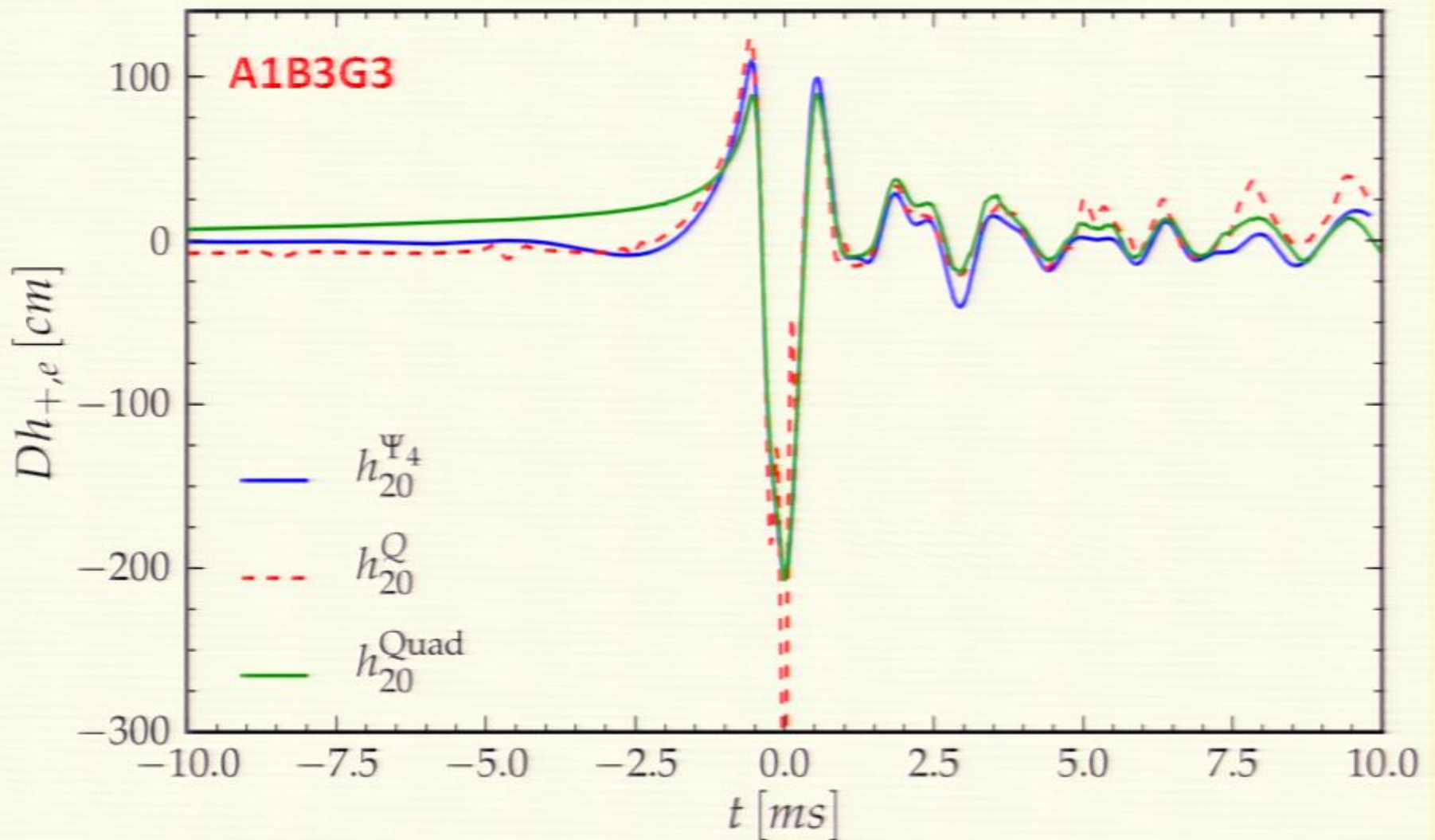
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[Reisswig, Ott et al. 2010]



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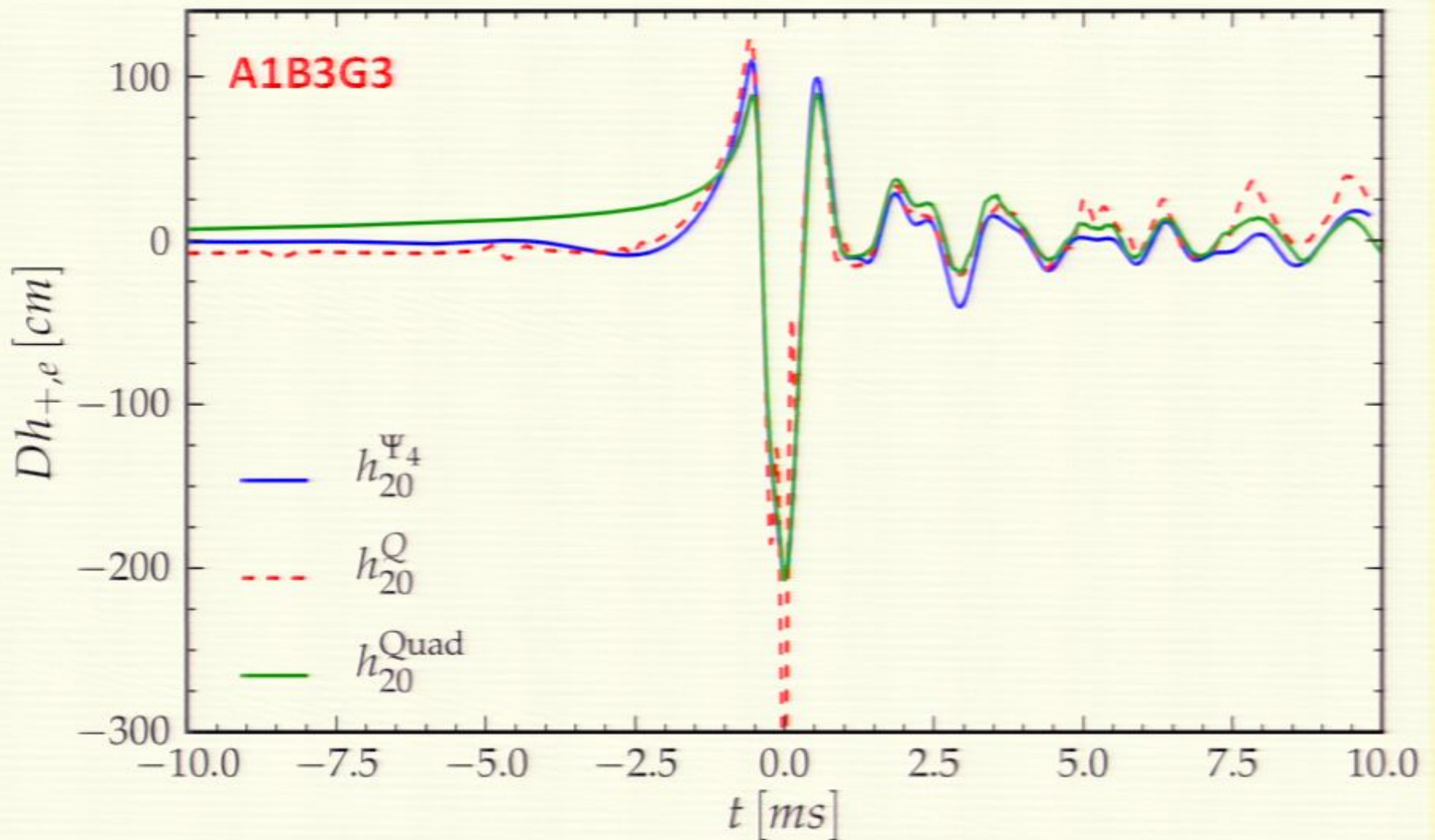
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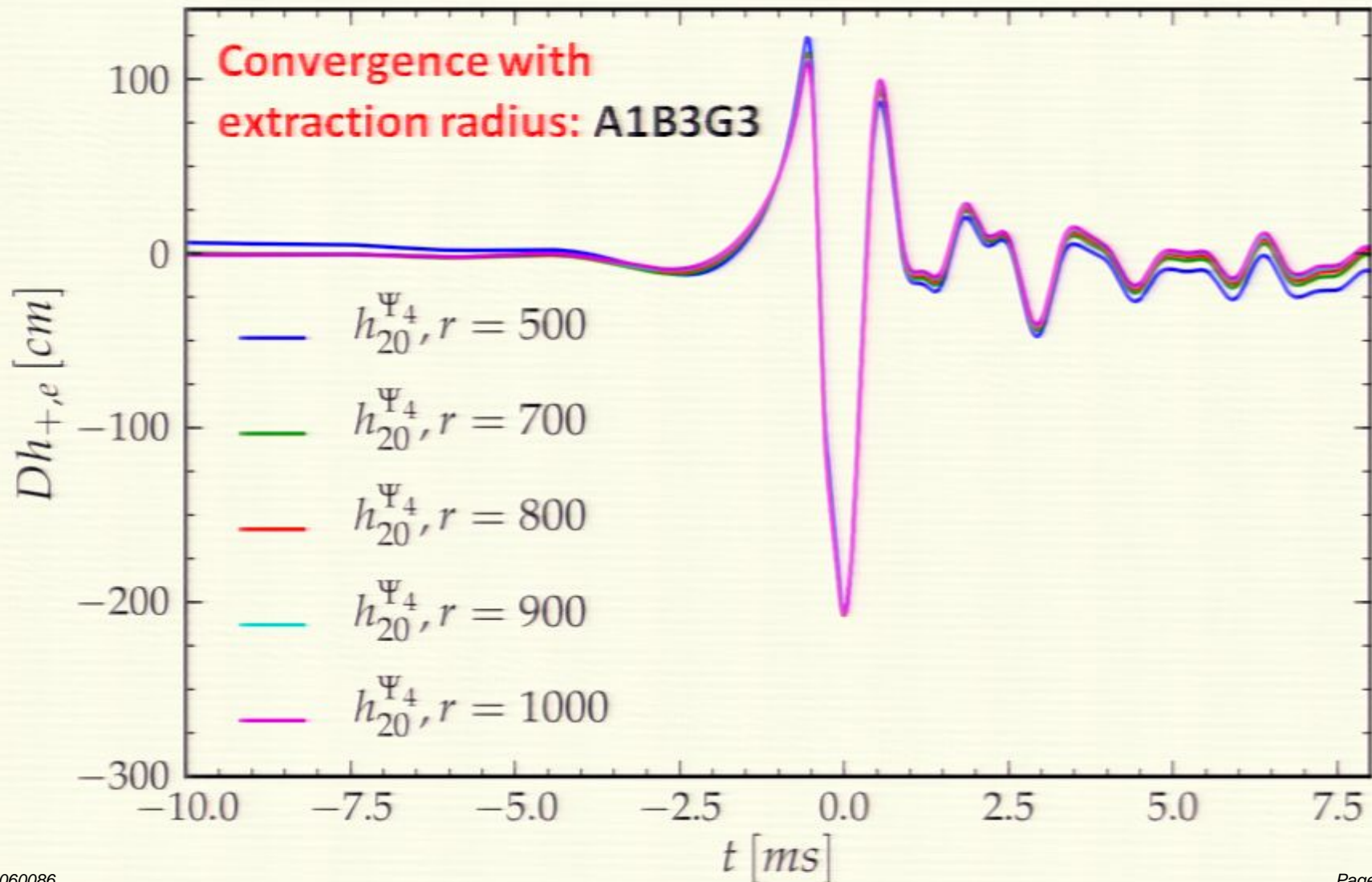
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Slides Outline

- 18 GW Extraction: Preliminary Results
- 19 When Supremacy Falls: Black Hole Formation
- 20 Core Collapse: Trains
- 21 QED: Approximate Relation
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- 23 QED: QED & Microphysics

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