

Title: IR effects, semiclassical relations, and perturbative limitations in inflationary spacetimes

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Abstract: TBA

the infrared limit...

the infrared limit...

of inflationary spacetimes

# IR effects, semiclassical relations, and perturbative limitations in inflationary spacetimes

Based on:

arXiv: 1005.1056 “Semiclassical relations and IR effects in de Sitter and slow roll spacetimes,”

arXiv: 1005.3287 “Cosmological diagrammatic rules,”

work in progress

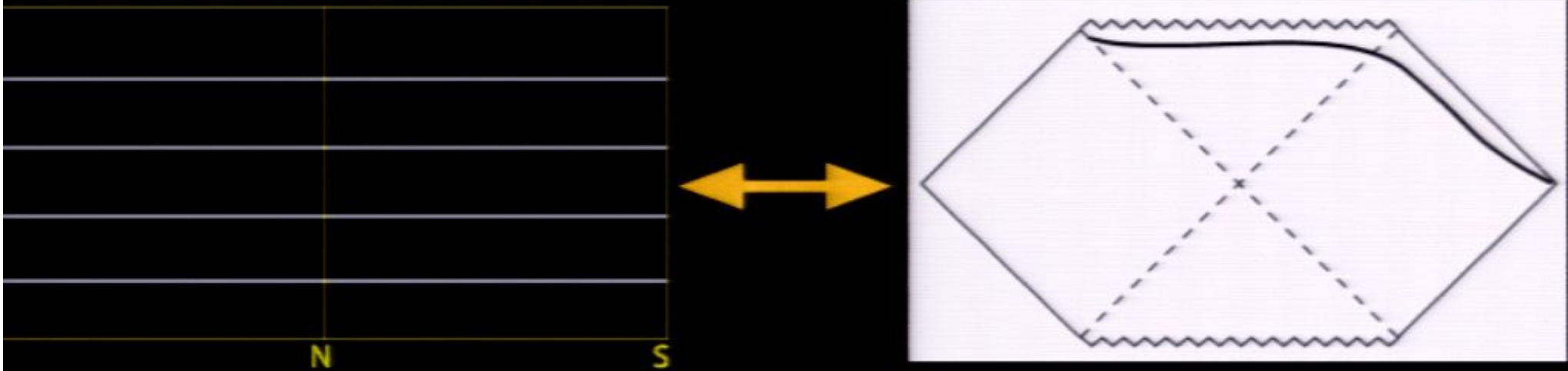
... w/ Martin Sloth

# Motivations

1. Understand how to make precise predictions in inflationary cosmology. Experimental tests (cf. Bond, Verde, ...). Need to control loops. (cf. Senatore, Holman, ...)
2. Test veracity of inflation (cf. Zaldarriaga, ...)
3. Important to understand if inflationary spacetimes have instabilities

# Motivations

## 4. Connections to quantization of black holes

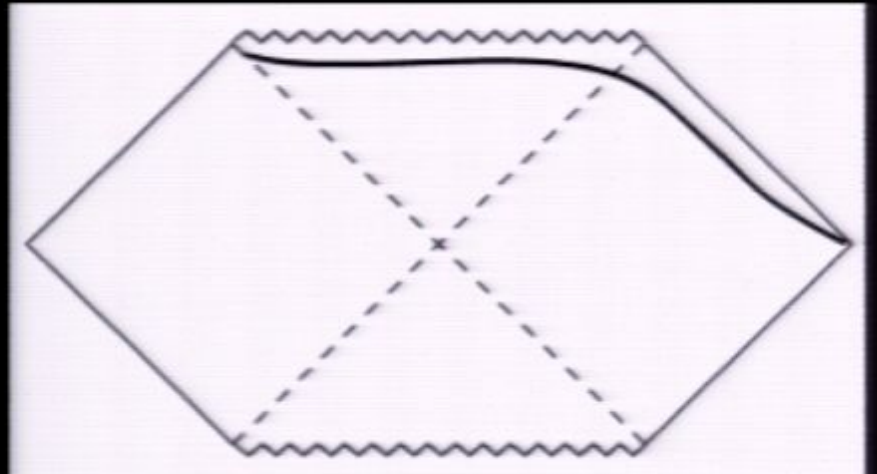


e.g. Arkani-Hamed -String Pheno 2006

SBG hep-th/0703116

Arkani-Hamed et al 0704.1814

The black hole case leads to  
the “information paradox”



hep-th/0703116 proposal to avoid the  
contradiction leading to paradox:

nice slice state not well defined (for long times)  
(e.g. large fluctuations/perturbative breakdown)

(an information **problem** would remain: what  
nonperturbative mechanisms unitarize theory?)

# A basic theme

Rapid expansion produces accumulation of long-distance fluctuations of light fields. These can produce large IR contributions -- how do these affect physical quantities?



## An essential mechanism

$$dS: \quad ds^2 = -dt^2 + e^{2Ht} dx_3^2$$

(flat slicing  
throughout)

Consider a massless scalar field:

$$\langle \sigma(x, t) \sigma(x, t) \rangle = \int \frac{d^3k}{(2\pi)^3 2k} \left( \frac{H^2}{k^2} + e^{-2Ht} \right)$$

$k$  - comoving momentum

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IR div

usual  
UV div

Fluctuations leave horizon, accumulate. ( $\sim$ classical)

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How is this regulated?

I) Add a mass:  $m \ll H$

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2) Finite duration inflation

$$\langle \sigma^2(x, t) \rangle = \int_{a_i H}^{a H} \frac{d^3 k}{(2\pi)^3} \frac{H^2}{2k} \frac{1}{k^2} = \left( \frac{H}{2\pi} \right)^2 2H(t - t_i)$$

largest wavelength

$$H t_i = -\log(\Delta_{IR})$$

True for other light fields:

True for other light fields: e.g. **gravity**

$$ds^2 = -dt^2 + a^2(t)(dx_3^2 + \gamma_{ij}dx^i dx^j) \quad a(t) = e^{Ht}$$

TT gauge:  $\gamma_{ii} = 0 \quad \partial_i \gamma_{ij} = 0$

$$\begin{aligned} \langle \gamma^2(x) \rangle &= \frac{1}{4} \langle \gamma_{ij}(x) \gamma_{ij}(x) \rangle = \int \frac{d^3k}{(2\pi)^3 k} \left( \frac{H^2}{k^2} + a^{-2}(t) \right) \\ &= 2 \langle \sigma^2(x) \rangle \end{aligned}$$

... same IR div

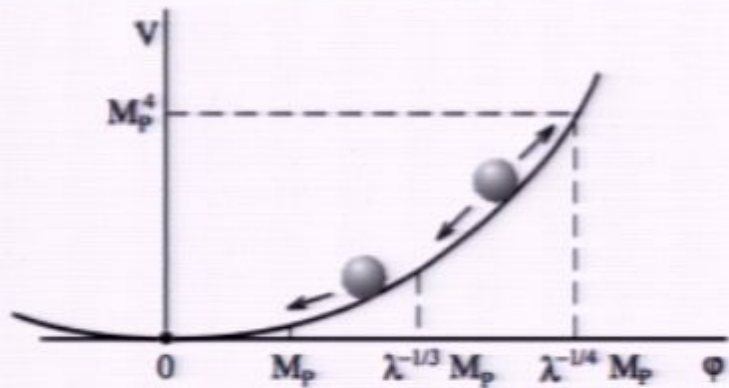
(also true for global slicing - Higuchi)

Are these effects physical?



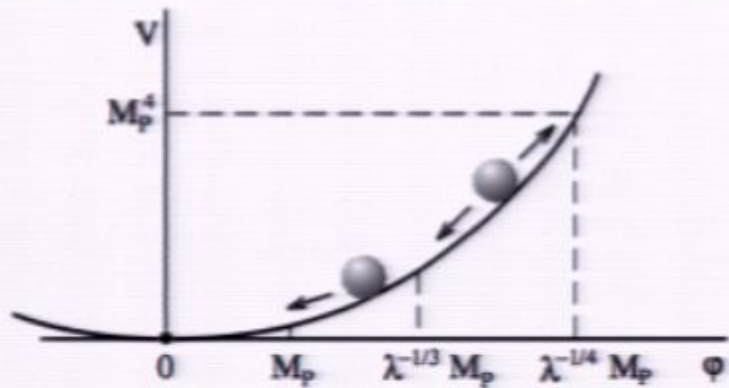
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An example - self reproduction:

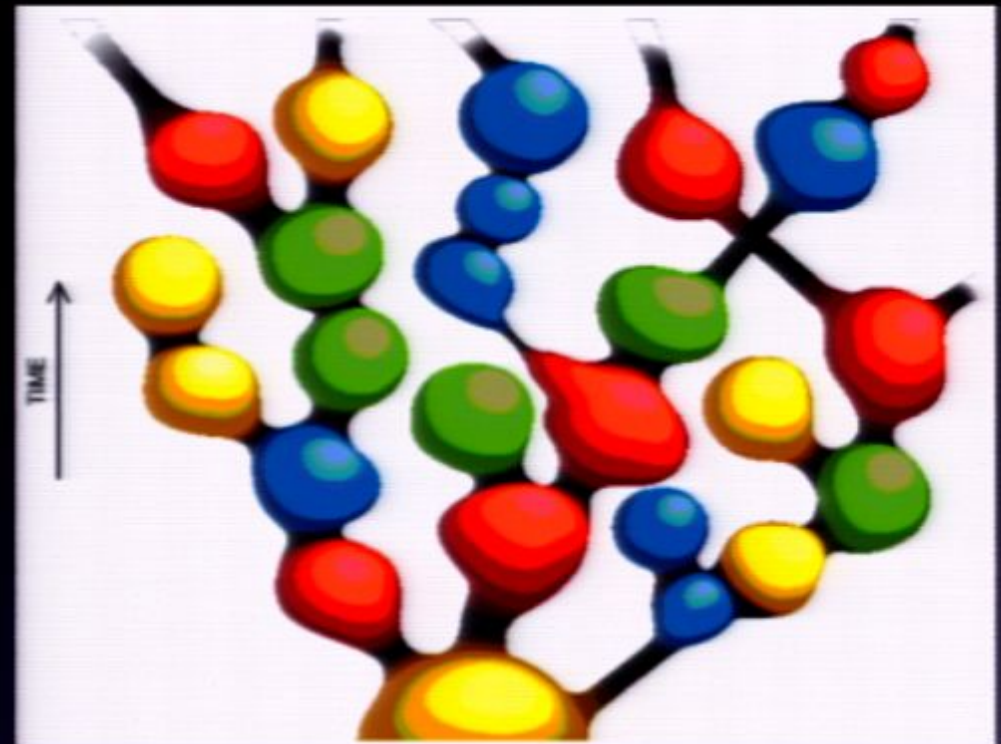


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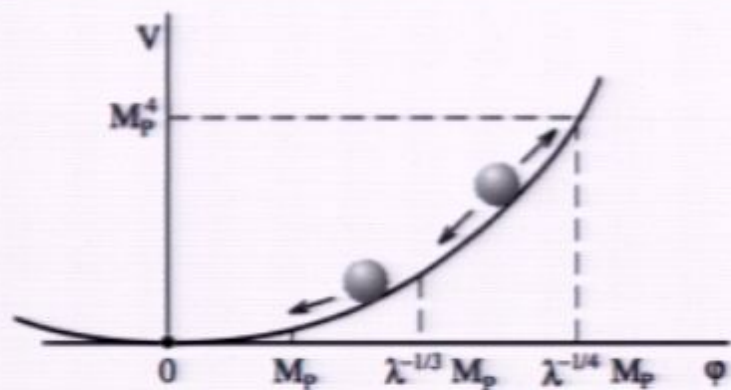


Linde:

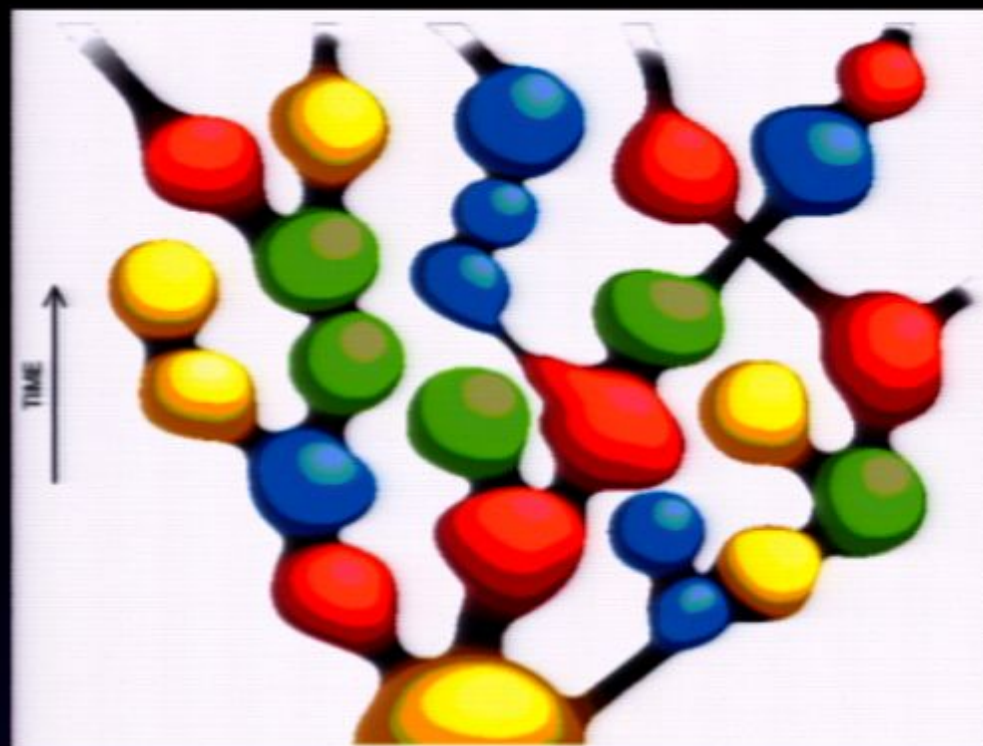


Are these effects physical?

An example - self reproduction:



Linde:



Fluctuations in background get large.

How general is this?

To properly study, need appropriate **observables**

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**No local diff-inv't observables in gravity**

Relational approach: Leibniz, Einstein, DeWitt, ...

Important puzzle: proper quantum implementation  
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For example, hep-th/0512200 w/ Marolf and Hartle:  
recover local observables, in an approximation, from  
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Some progress in dS: arXiv:0705.1178 w/ Marolf

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serious potential pitfalls: Boltzmann brains, measure  
paradoxes and quandries ... (c.f. Freivogel, Susskind,...)



Might expect large IR contributions to amplitudes

e.g. loop corrections, trispectrum, ...

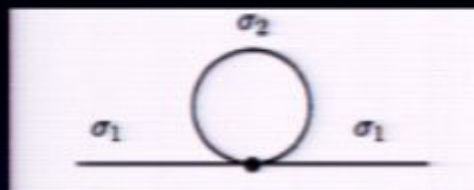
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Loops: toy model -- scalars



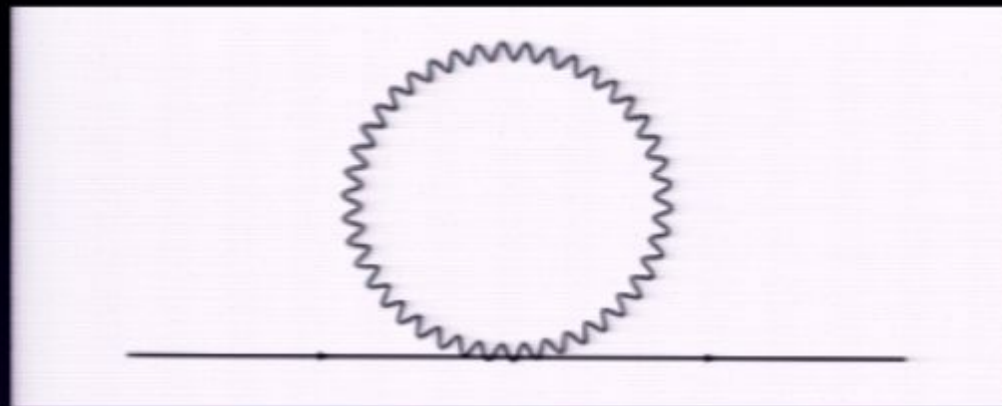
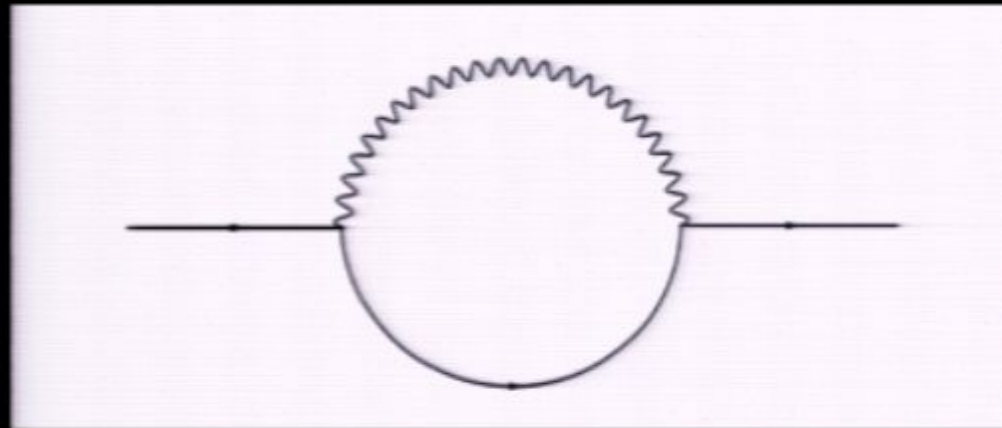
Marolf and Morrison



Burgess et al  
(+many others)

More generic: Gravity

e.g.



Calculation:

(see e.g. Maldacena, ...)

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1) Action 
$$S = \frac{1}{2} \int \sqrt{-g} [R - \partial_\mu \sigma \partial^\mu \sigma - 2\Lambda]$$

2) ADM

$$ds^2 = -N^2 dt^2 + h_{ij} (dx^i + N^i dt)(dx^j + N^j dt)$$

3) Gauge 
$$h_{ij} = a^2(t) (e^\gamma)_{ij} \quad \det(e^\gamma) = 1$$
$$\partial_i \gamma_{ij} = 0$$

Action:

$$S_2 = \frac{1}{2} \int d^3x dt a^3 \left[ \frac{1}{4} (\dot{\gamma}_{ij} \dot{\gamma}_{ij} - a^{-2} \partial_k \gamma_{ij} \partial_k \gamma_{ij}) + \dot{\sigma}^2 - a^{-2} \partial_i \sigma \partial_i \sigma \right]$$

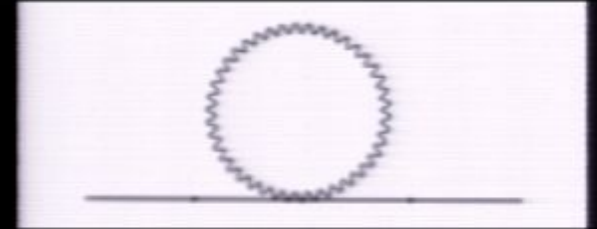
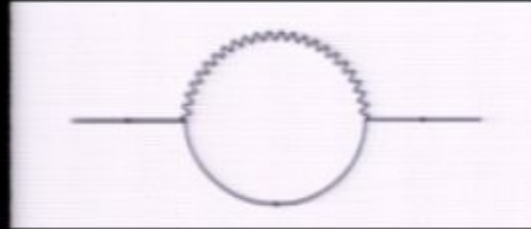
$$S_3 = \int d^3x dt \frac{a}{2} \gamma_{ij} \partial_i \sigma \partial_j \sigma$$

$$S_4 = - \int d^3x dt \frac{a}{4} \gamma_{ik} \gamma_{kj} \partial_i \sigma \partial_j \sigma$$

+ ... ( $\sigma^4$ , etc.)

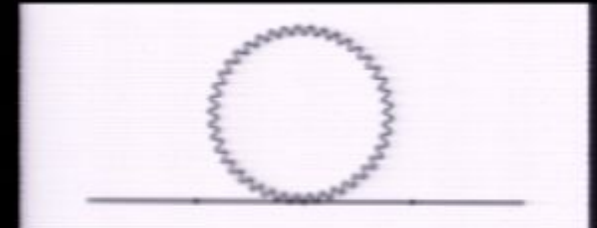
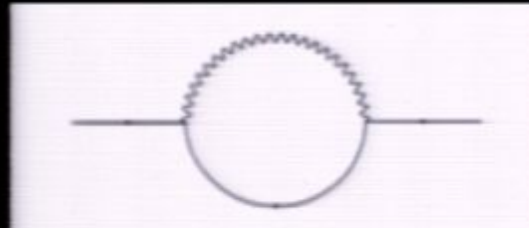
Want corrections to **in-in** correlator, e.g.

$$\langle \sigma_{k_1}(t_0) \sigma_{k_2}(t_0) \rangle \sim$$



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“Cosmological diagrammatic rules:”

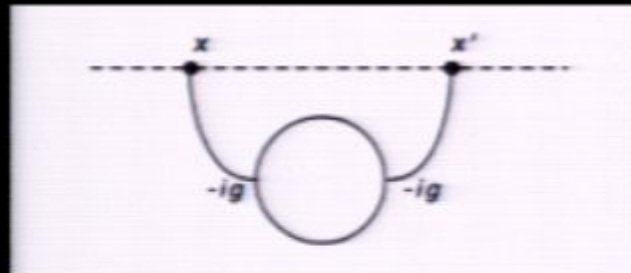
arXiv: 1005.3287

1. Draw a horizontal dotted line, corresponding to  $t_0$ , and place the external points of the correlator on this line.
2. At a given order, enumerate all placements of vertices either above or below the  $t_0$  line, modulo reflections about this line. Then, draw all diagrams connecting these vertices with propagator lines, again modulo reflection.
3. Each propagator line crossing or ending on the dotted line gives a Wightman propagator, whose leftmost/rightmost time argument corresponds to the uppermost/lowermost vertex. Each propagator line below the dotted line gives a Feynman propagator, and each line above the dotted line gives the complex conjugate or time-reversed Feynman propagator.
4. Vertices below/above the line are accompanied by  $V$  or  $V^\dagger$ , respectively; conserve momentum at each vertex and include an overall momentum-conserving delta function, integrate over all internal momenta, and integrate over the time coordinate of each vertex.
5. Divide by the usual Feynman symmetry factors, where present.
6. Once the resulting diagrams are calculated, take twice their real part.

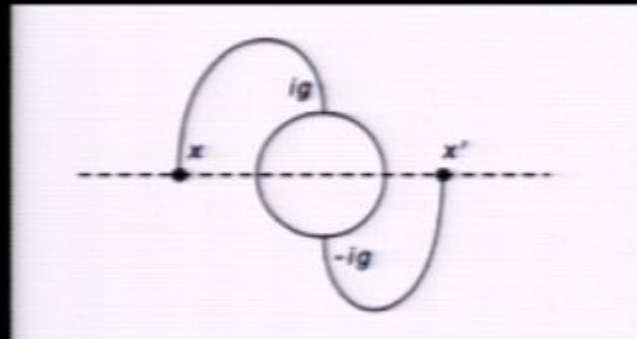


Our example: Three diagrams (scalar analogs shown)

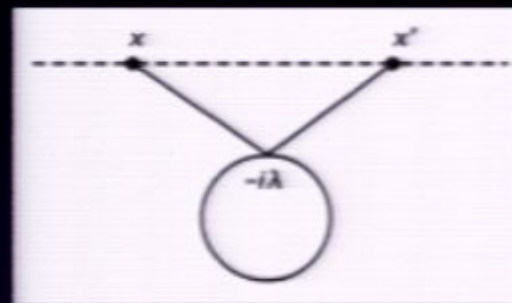
A



B



C



(+ ... -- not IR divergent)

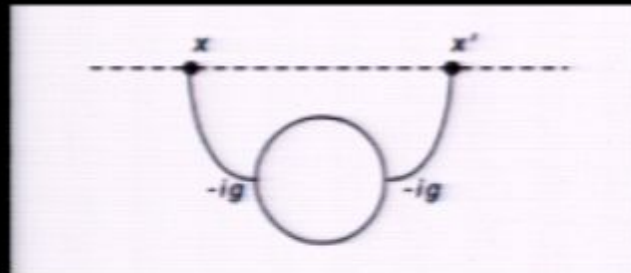
E.g. results:

$$A_k(\eta) + B_k(\eta) = \frac{H^2}{2k^3} \frac{H^2}{(2\pi)^2} \left[ 2 \log(k/\Lambda_{IR}) + \frac{2}{3} \log(\Lambda_{UV}/k) + \frac{101}{90} + \mathcal{O}(k^2 \eta^2, \Lambda_{IR}^2, 1/\Lambda_{UV}^2) \right]$$

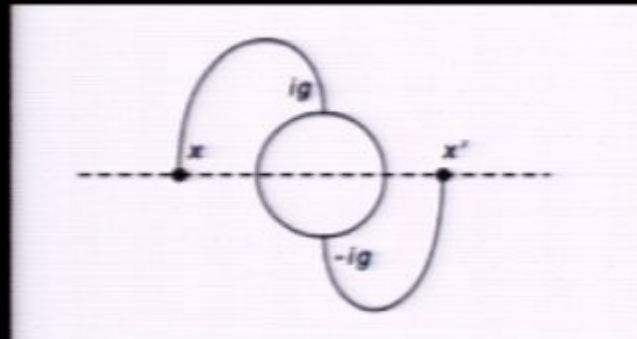
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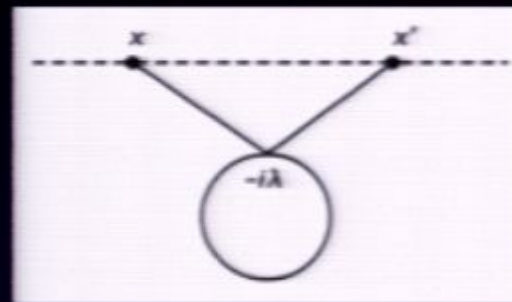
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Calculation hard, even in pure dS, much less slow roll.

Results simple: another method?

And, can we understand the IR behavior?

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(note also: cancellation for this correlator -- scale invariance; not for others)

“Semiclassical relations:”

Observation: the long wavelength fluctuations “freeze”  
and behave  $\sim$  classical background

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E.g. consider  $\langle \sigma_{k_1} \sigma_{k_2} \rangle_\gamma$  ← “background”

$$k^2 = k_i k_i \rightarrow k_i (e^{-\gamma})_{ij} k_j = k_i k_i - \gamma_{ij} k_i k_j + \frac{1}{2} \gamma_{il} \gamma_{lj} k_i k_j + \dots$$

$$\begin{aligned} \langle \sigma_{k_1} \sigma_{k_2} \rangle_\gamma &= \langle \sigma_{k_1} \sigma_{k_2} \rangle_0 \\ &+ \left( -\gamma_{ij} k_i k_j + \frac{1}{2} \gamma_{il} \gamma_{lj} k_i k_j \right) \frac{\partial}{\partial k^2} \langle \sigma_{k_1} \sigma_{k_2} \rangle \Big|_0 + \frac{1}{2} (\gamma_{ij} k_i k_j)^2 \left( \frac{\partial}{\partial k^2} \right)^2 \langle \sigma_{k_1} \sigma_{k_2} \rangle \Big|_0 + \dots \end{aligned}$$

Next, average over fluctuations:

$$\begin{aligned}
 \langle (\sigma_{k_1} \sigma_{k_2})_t \rangle &= \langle \sigma_{k_1} \sigma_{k_2} \rangle \\
 &= \frac{1}{2} k_1 k_2 (\gamma_u \gamma_v) \frac{\partial}{\partial k^2} \langle \sigma_{k_1} \sigma_{k_2} \rangle + \frac{1}{2} k_1 k_2 k_i k_j (\gamma_u \gamma_v) \left( \frac{\partial}{\partial k^2} \right)^2 \langle \sigma_{k_1} \sigma_{k_2} \rangle
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Use:

$$\langle \gamma_{ij}(x) \gamma_{kl}(x) \rangle = \sum_s \int \frac{d^3 k}{(2\pi)^3 k} \left[ \frac{H^2}{k^2} + a^{-2}(t) \right] \epsilon_{ij}^s(k) \epsilon_{kl}^{s*}(k)$$

$$\Rightarrow \langle (\sigma_{k_1} \sigma_{k_2})_\gamma \rangle = \left\{ 1 + \frac{2}{3} \langle \gamma^2(x) \rangle_* \left[ \frac{2}{5} k^4 \left( \frac{\partial}{\partial k^2} \right)^2 + k^2 \frac{\partial}{\partial k^2} \right] \right\} \langle \sigma_{k_1} \sigma_{k_2} \rangle$$

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$$\langle \gamma^2(x) \rangle_* \approx -2 \frac{H^2}{(2\pi)^2} \log(\Lambda_{IR}/a_* H)$$

Exactly reproduces  
IR divergence

Toy example: cf Marolf-Morrison,  $\phi^3$   
(similar exp. for Burgess et al -- cf Holman's talk)

$$\mathcal{L} = -\frac{(\partial\phi)^2 + m^2\phi^2}{2} + \frac{g}{3!}\phi^3 ;$$

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$$\phi = \varphi + \bar{\phi}$$

“background”

$$\mathcal{L} = -\frac{1}{2} [(\partial\varphi)^2 + (m^2 - g\bar{\phi})\varphi^2] + \dots$$

$$\delta\langle\varphi\varphi\rangle_{\bar{\phi}} = \frac{1}{2}g^2\bar{\phi}^2 \left(\frac{\partial}{\partial m^2}\right)^2 \langle\varphi\varphi\rangle$$

$$\langle\delta\langle\varphi\varphi\rangle_{\bar{\phi}}\rangle = \frac{1}{2}g^2\langle\bar{\phi}^2\rangle \left(\frac{\partial}{\partial m^2}\right)^2 \langle\varphi\varphi\rangle \quad \langle\bar{\phi}^2\rangle \sim \frac{3H^4}{8\pi^2 m^2}$$

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$$\sim \frac{3g^2 H^4}{32\pi^2 m^6} \langle\varphi\varphi\rangle$$

(small m:

large correction!)

Apply to slow roll:

$$h_{ij} = a^2(t) e^{2\zeta} (e^\gamma)_{ij}$$

Apply to slow roll:

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$$\langle (\zeta_{k_1} \zeta_{k_2}) \rangle = \langle \zeta_{k_1} \zeta_{k_2} \rangle_0 \left[ 1 + \frac{1}{2}(n_s - 1)^2 \langle \zeta^2(x) \rangle_* + \frac{n_s - 1}{3} \frac{n_s - 1}{5} \langle \gamma^2(x) \rangle_* \right]$$

scalar fluctuations

tensor fluctuations

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Can give large shifts to:  $r \propto \frac{\langle\gamma^2\rangle}{\langle\zeta^2\rangle}$   $f_{NL}$  ...

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Large when?  $\langle\gamma^2\rangle \sim H^3 t \sim 1 \Leftrightarrow t \sim 1/H^3$

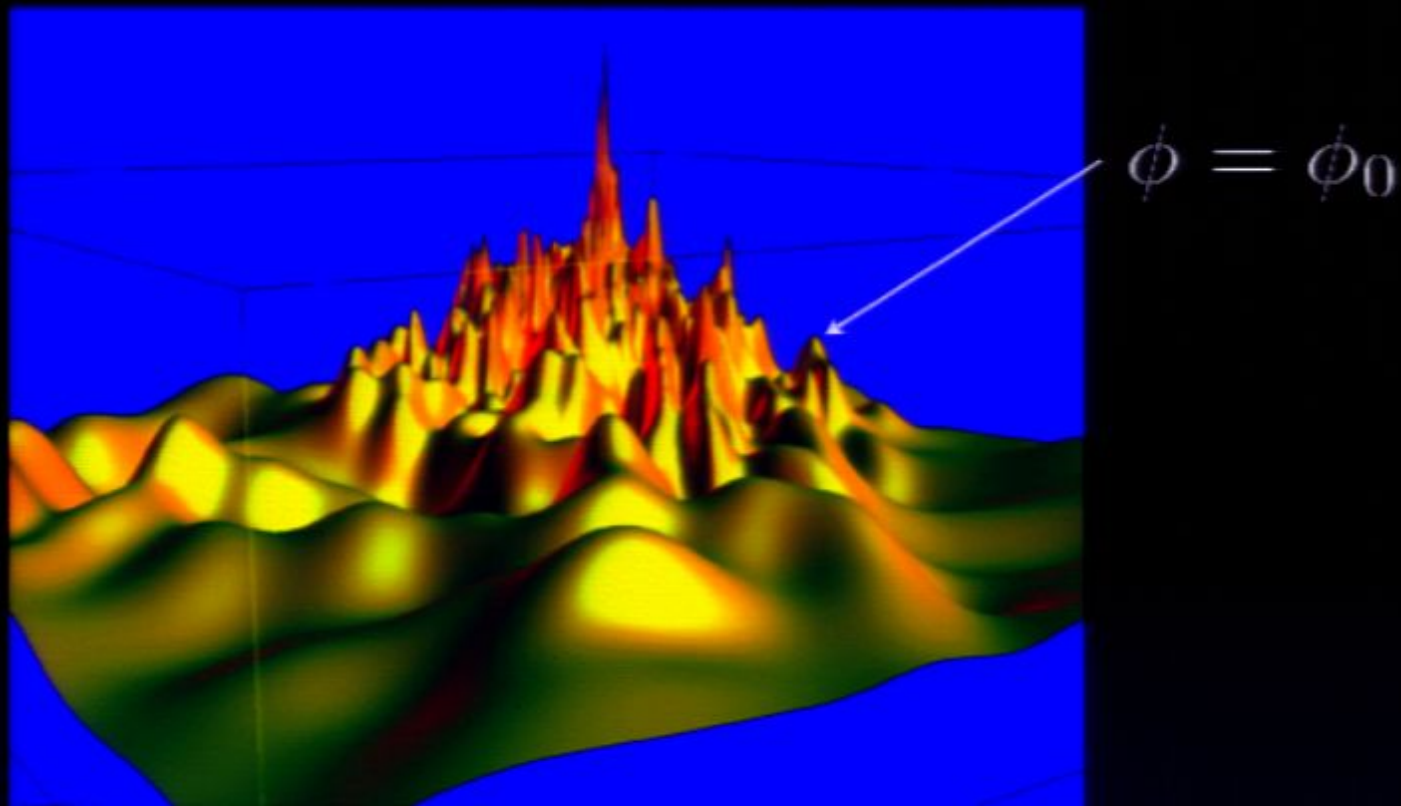
general dimension:  $t \sim \text{RS}$

(Studying other observables ...)

Can resum/absorb into background?

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E.g. self-reproducing universe

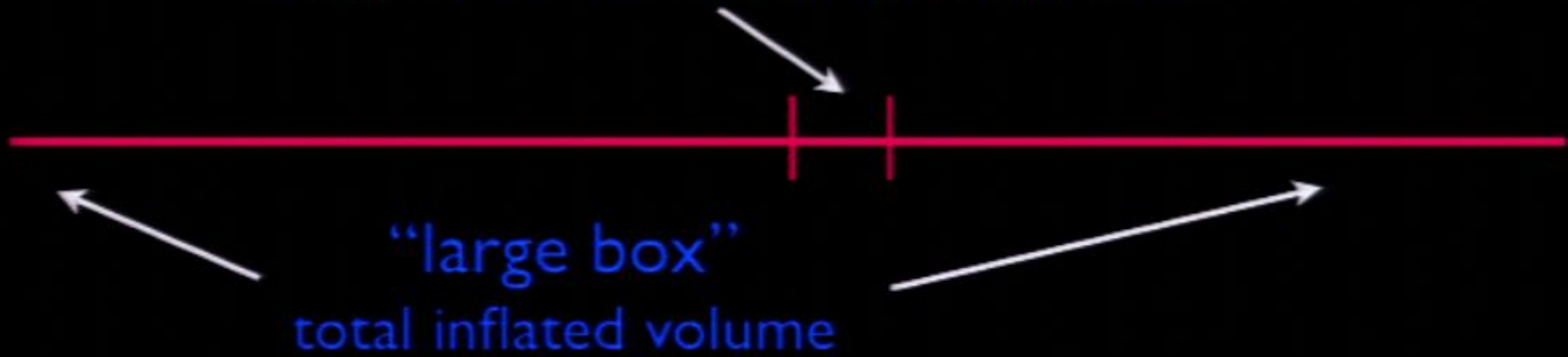


Expect can make predictions about local observables,  
with appropriate conditionals ...

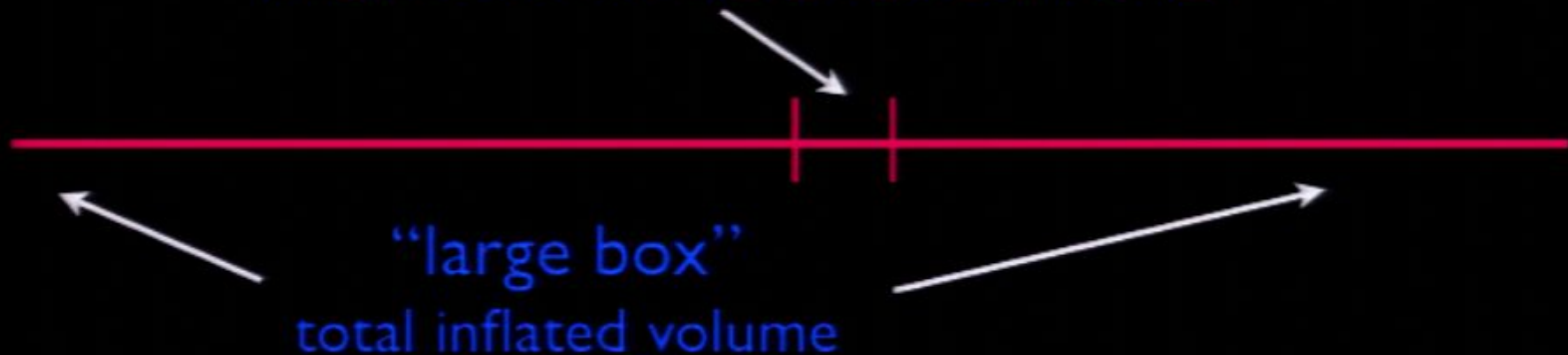
But can one calculate a “wavefunction of the universe”?



“small box” our observable universe

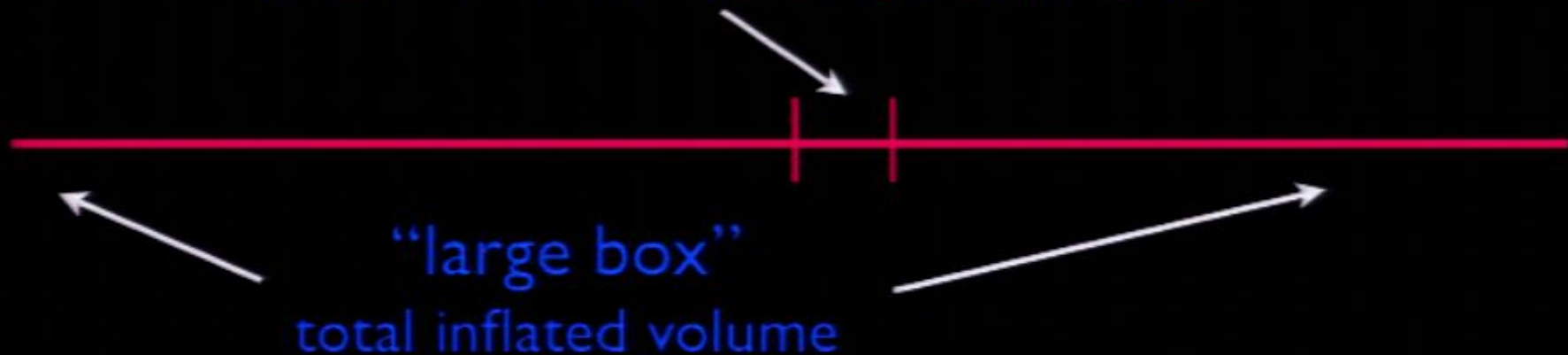


“small box” our observable universe



- plausibly can resum to eliminate large  $\langle \zeta^2 \rangle$  corrections for observables in small box (e.g.  $\sim$ DRG ... Burgess, et al;  $\delta N$  - Byrnes et al 1005.3307)  
small region -- short time

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$$\langle \zeta^2 \rangle \leftrightarrow \delta N, \dots?$$

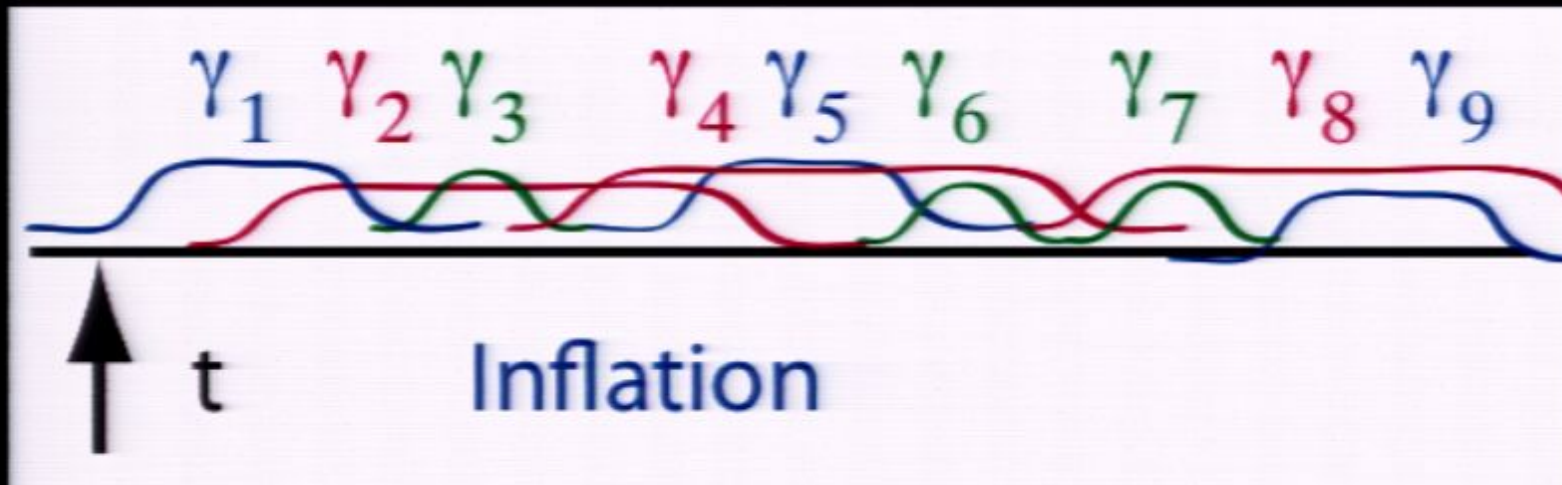
e.g. self-repro regime

stochastic, “Mandelbrot” (c.f. Susskind),  $\rho(V)$  (c.f. Senatore)

... capture certain gross features

but: quantum wavefunction of the universe??

have lost perturbative control



$$\langle \gamma^2 \rangle \propto H^3 t$$

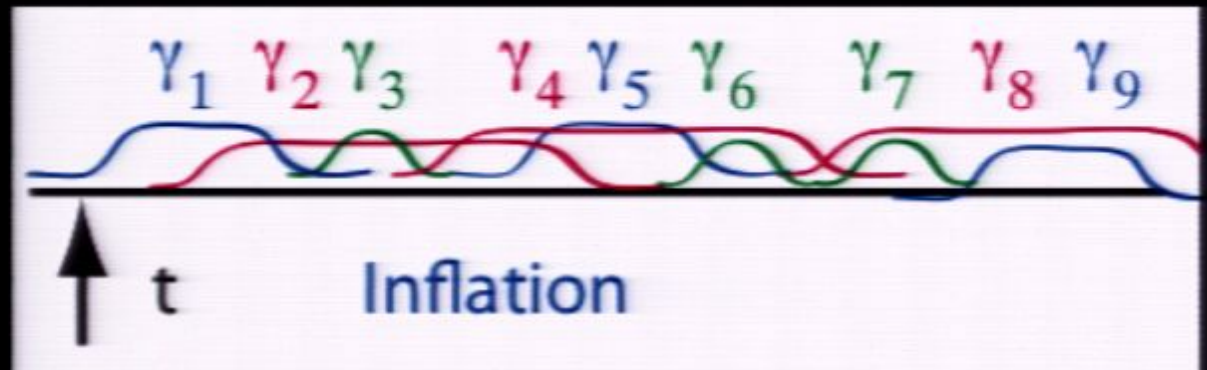
“spacetime foam, writ large”

(cf Masui)

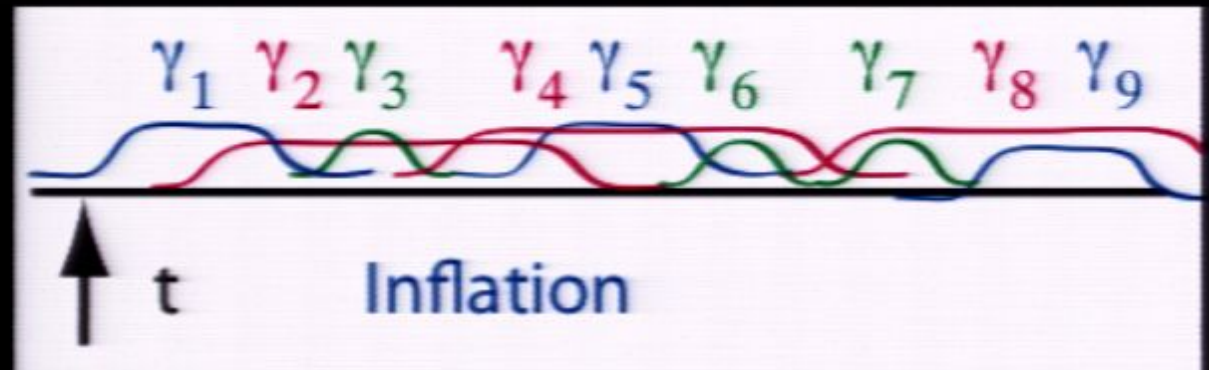
Plausible story (under investigation):

- ~local observables: resum - eliminate large effects
- but globally??      plausibly can't eliminate  
(instability of dS?)

What observables?



What observables?



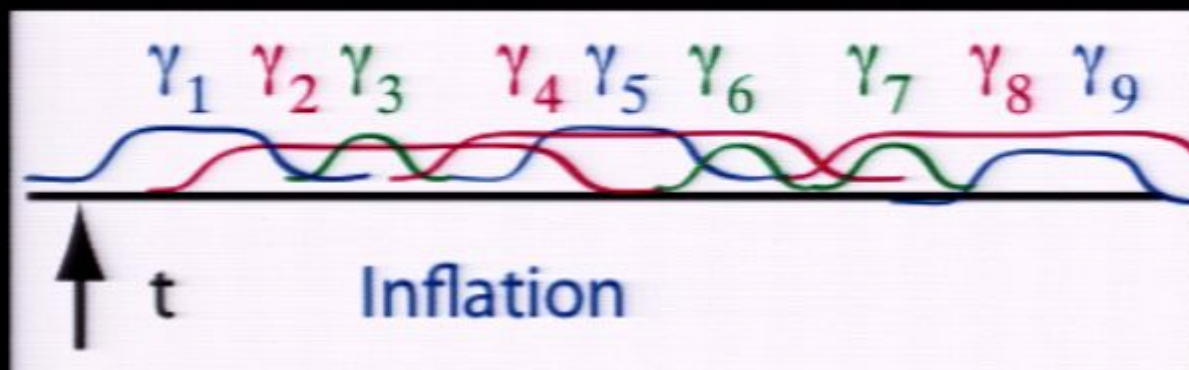
Compare self reproduction: (Creminelli et al -- c.f. Senatore)

$$\rho(V) \quad V = \int d^3x \sqrt{h} \quad (\text{or: fluctuations in } V)$$

sensitive to  $\zeta$  fluctuations



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sensitive to  $\zeta$  fluctuations

$\gamma$  fluctuations: volume preserving

So try:

$$\int_{\Gamma} ds$$

$\Gamma$  :

- Curve between comoving point masses
- Nontrivial holonomy -- e.g. on  $T^3$

So, such perturbative gravity calculations can fail, due to development of large fluctuations, on large enough scales at large enough times.

$\tau \sim RS$  (possibly times couplings)

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Important question:

Is there a controlled framework for calculating a “wavefunction of the Universe?”

resummation?

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Important question:

Is there a controlled framework for calculating a “wavefunction of the Universe?”

resummation?

(And compare the analogous statements made for “nice slice” state of black hole ... there we need the state on the full slice!)



on behalf of all participants  
including those past the horizon

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**THANKS!**

to the organizers for a very  
stimulating and enjoyable  
conference