

Title: The 7-year WMAP Observations: Cosmological Interpretation

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Abstract: We have announced the results from 7 years of observations of the Wilkinson Microwave Anisotropy Probe (WMAP) on January 26. In this talk we will present the cosmological interpretation of the WMAP 7-year data, including the detection of primordial helium, images of polarization of microwave background around temperature peaks, and new limits on inflation and properties of neutrinos. We also report a significant detection of the Sunyaev-Zel'dovich effect and discuss implications for the gas pressure in clusters of galaxies.



# The **7**-Year WMAP Observations: Cosmological Interpretation

**Eiichiro Komatsu** (Texas Cosmology Center, UT Austin)  
Cosmology Seminar, Perimeter Institute, April 27, 2010



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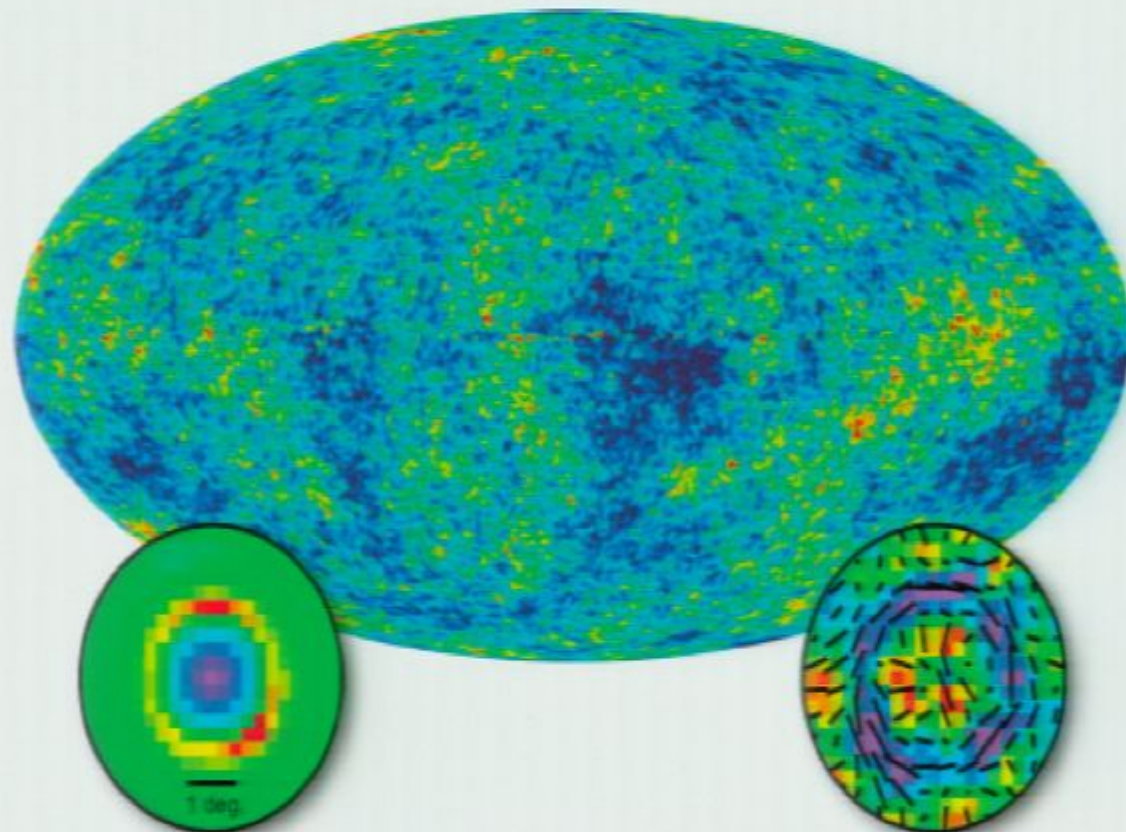
# WMAP will have collected 9 years of data by August

June 2001:  
WMAP launched!

February 2003:  
The first-year data  
release

March 2006:  
The three-year data  
release

March 2008:  
The five-year data  
release



Stacked Temperature

Stacked Polarization

● **January 2010: The seven-year  
data release**



# WMAP 7-Year Papers

- **Jarosik et al.**, “*Sky Maps, Systematic Errors, and Basic Results*”  
[arXiv:1001.4744](https://arxiv.org/abs/1001.4744)
- **Gold et al.**, “*Galactic Foreground Emission*” [arXiv:1001.4555](https://arxiv.org/abs/1001.4555)
- **Weiland et al.**, “*Planets and Celestial Calibration Sources*”  
[arXiv:1001.4731](https://arxiv.org/abs/1001.4731)
- **Bennett et al.**, “*Are There CMB Anomalies?*” [arXiv:1001.4758](https://arxiv.org/abs/1001.4758)
- **Larson et al.**, “*Power Spectra and WMAP-Derived Parameters*”  
[arXiv:1001.4635](https://arxiv.org/abs/1001.4635)
- **Komatsu et al.**, “*Cosmological Interpretation*” [arXiv:1001.4538](https://arxiv.org/abs/1001.4538)

# WMAP 7-Year Science Team

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- G. Hinshaw
- N. Jarosik
- S.S. Meyer
- L. Page
- D.N. Spergel
- E.L. Wright
- M.R. Greason
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- H.V. Peiris
- L. Verde



# 7-year Science Highlights

- First detection ( $>3\sigma$ ) of the effect of primordial **helium** on the temperature power spectrum.
- The primordial **tilt** is less than one at  $>3\sigma$ :
  - $n_s = 0.96 \pm 0.01$  (68%CL)
- Improved limits on **neutrino** parameters:
  - $\sum m_\nu < 0.58 \text{ eV}$  (95%CL);  $N_{\text{eff}} = 4.3 \pm 0.9$  (68%CL)
- First direct confirmation of the predicted **polarization** pattern around temperature spots.
- Measurement of the SZ effect: *missing **pressure**?*

# WMAP 7-Year Science Team

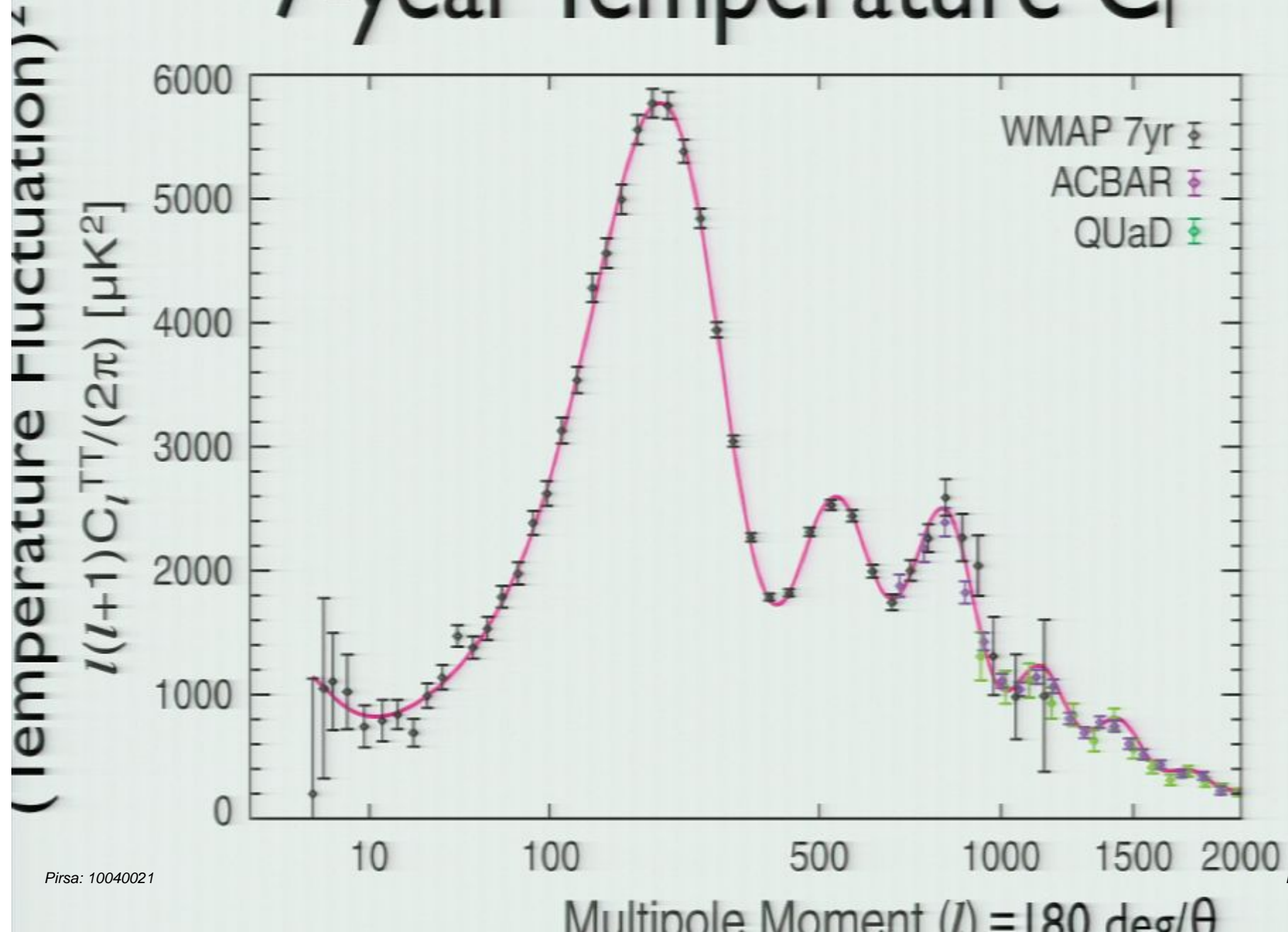
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# 7-year Temperature $C_l$

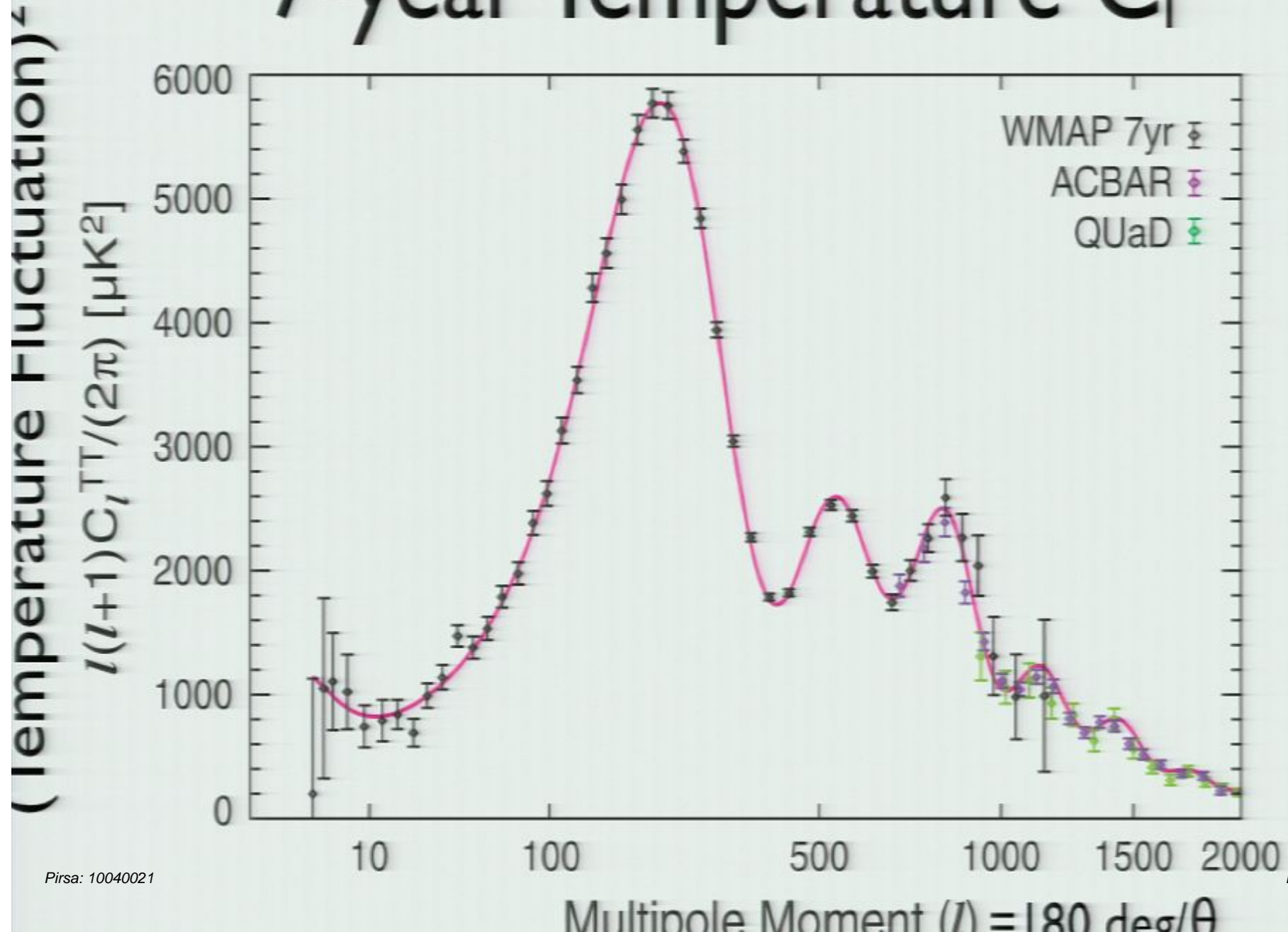




# 7-year Science Highlights

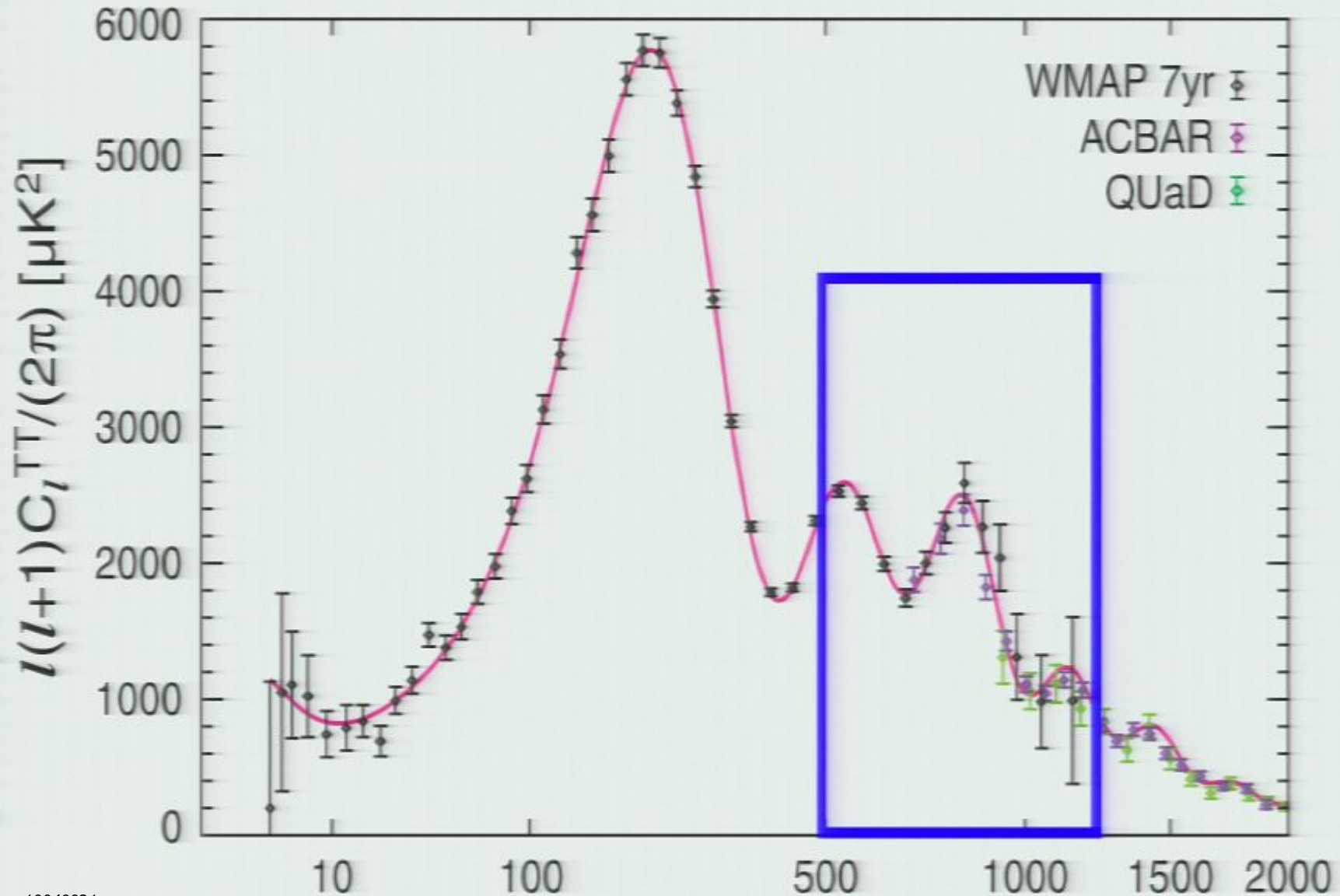
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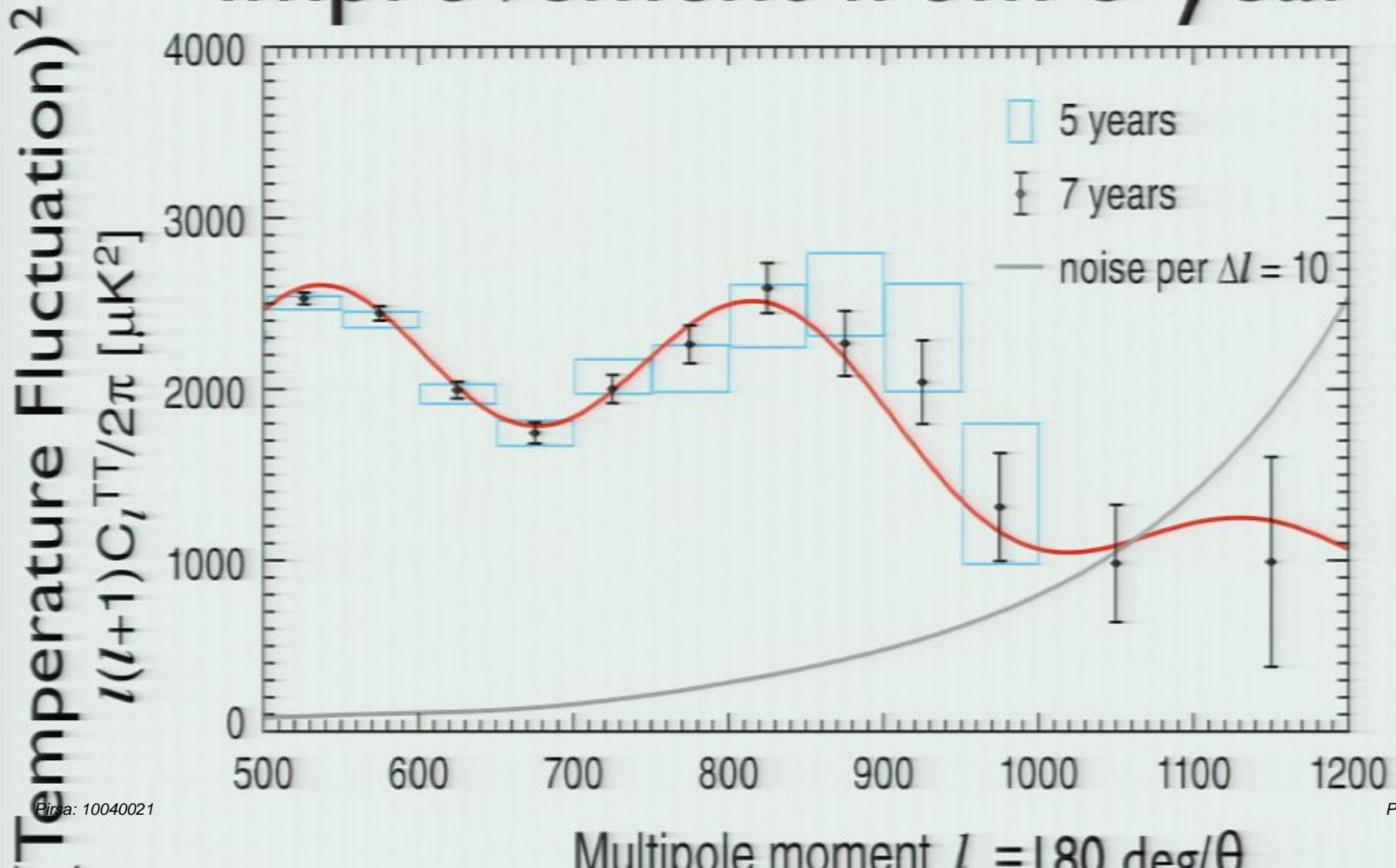
# Zooming into the 3rd peak...

(Temperature Fluctuation)<sup>2</sup>



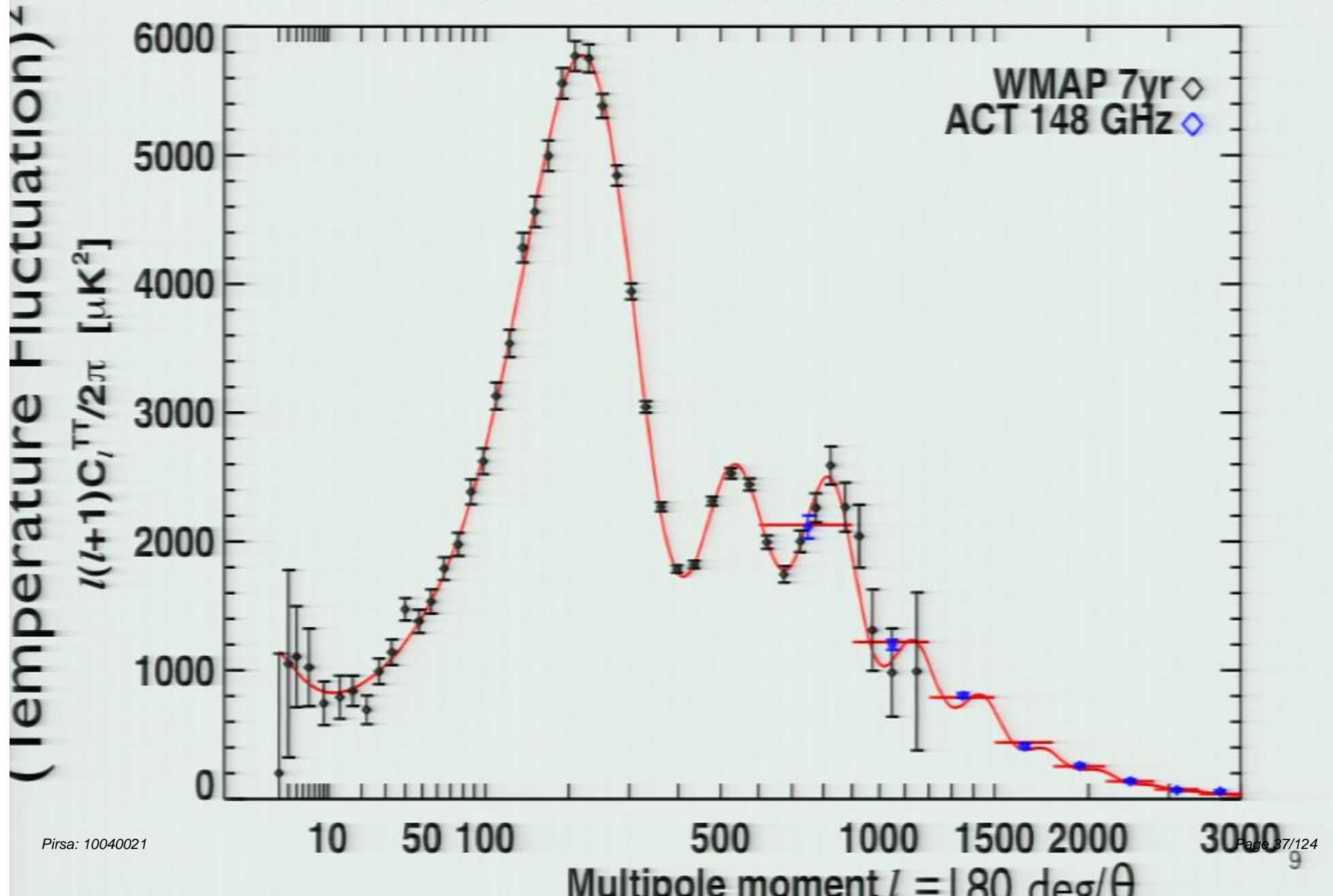


# High- $l$ Temperature $C_l$ : Improvement from 5-year

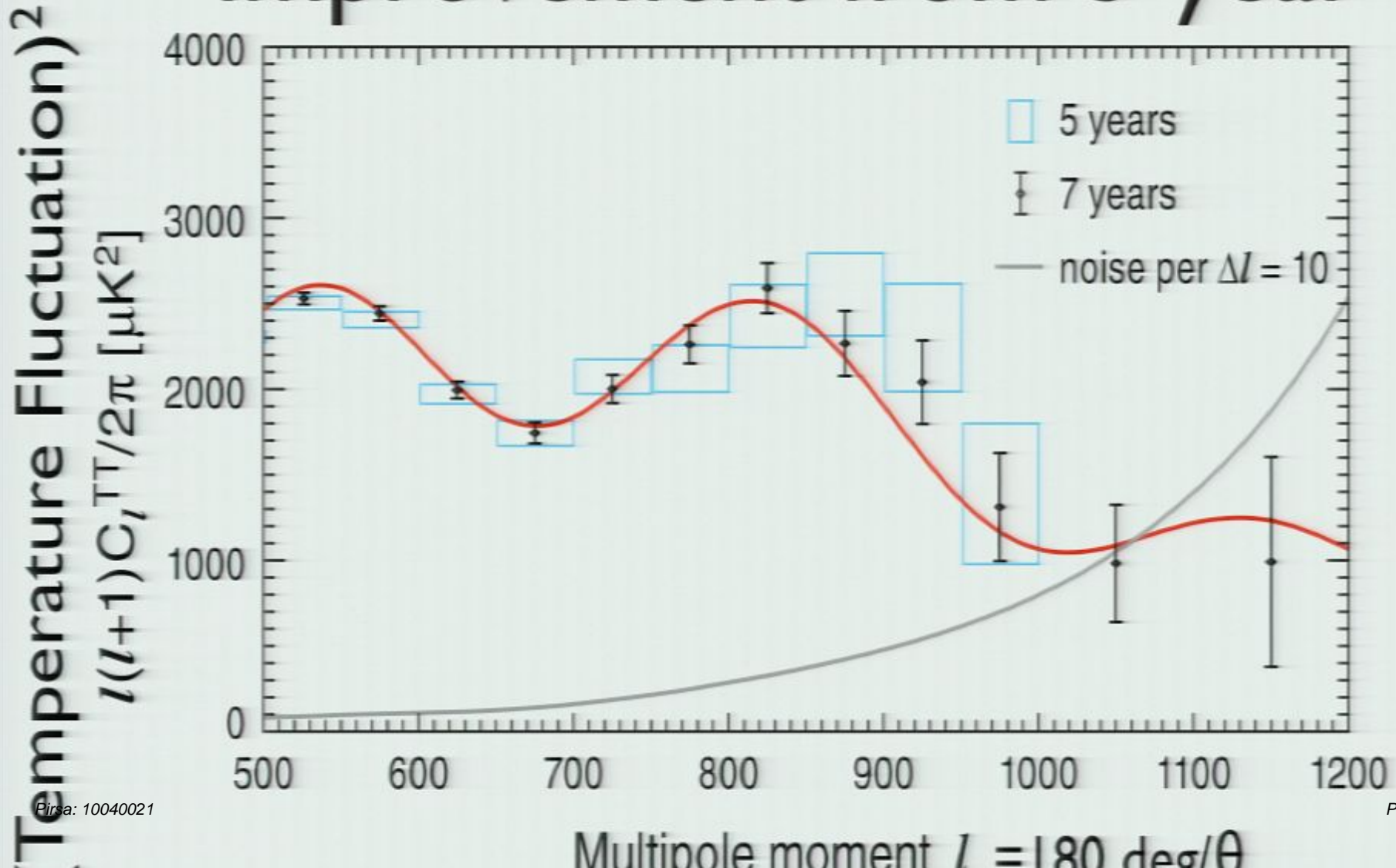




# WMAP and ACT

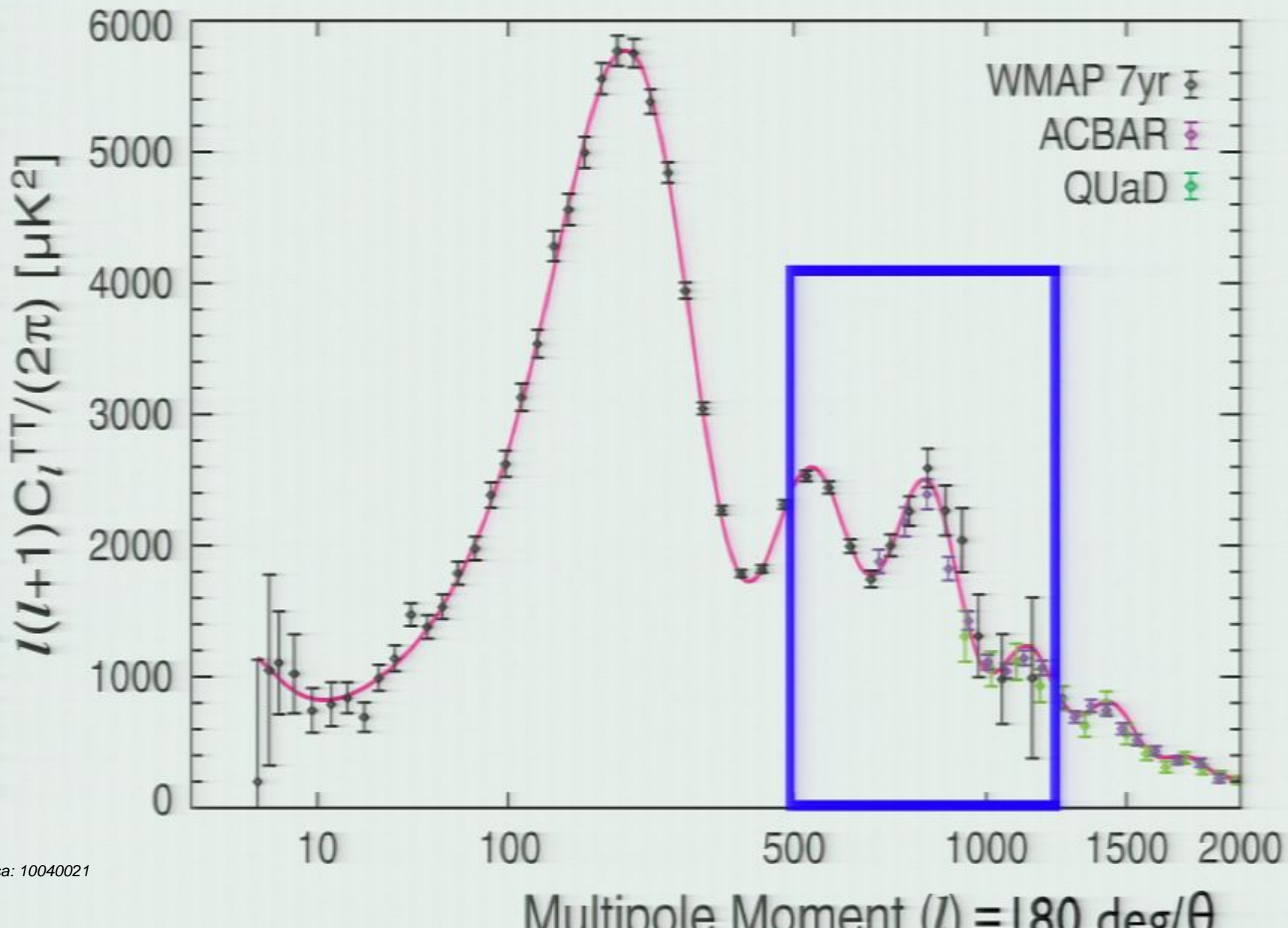


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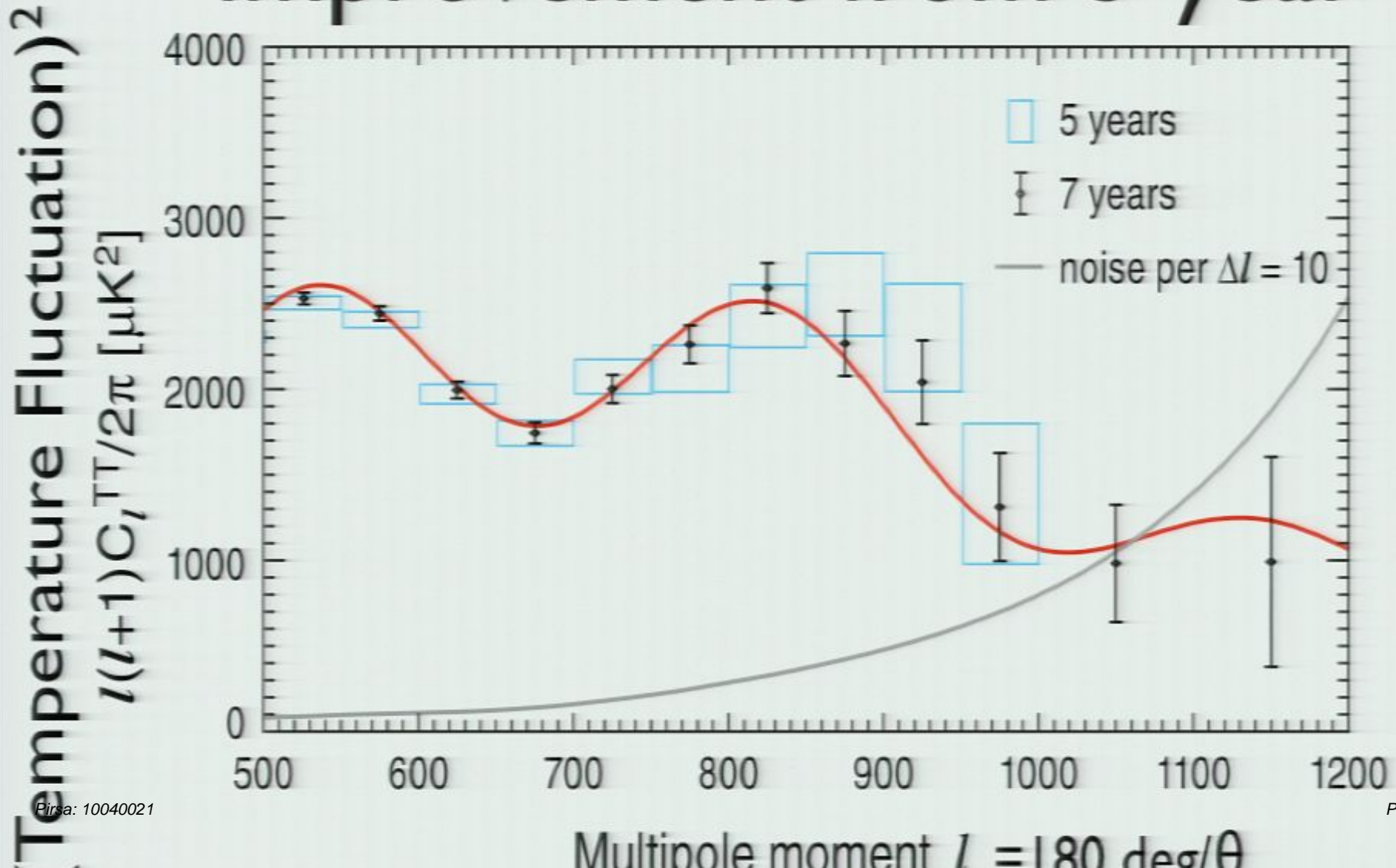
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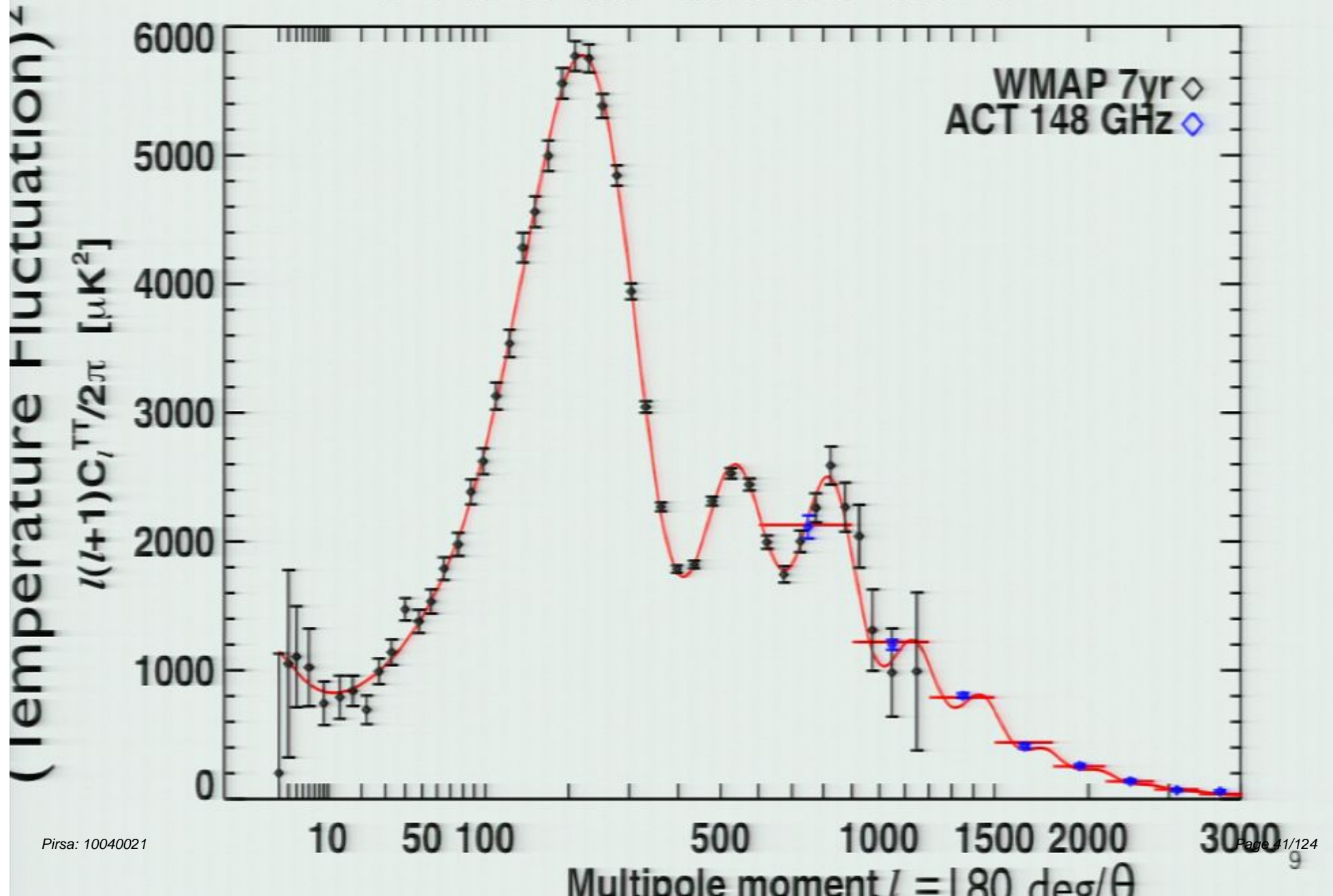


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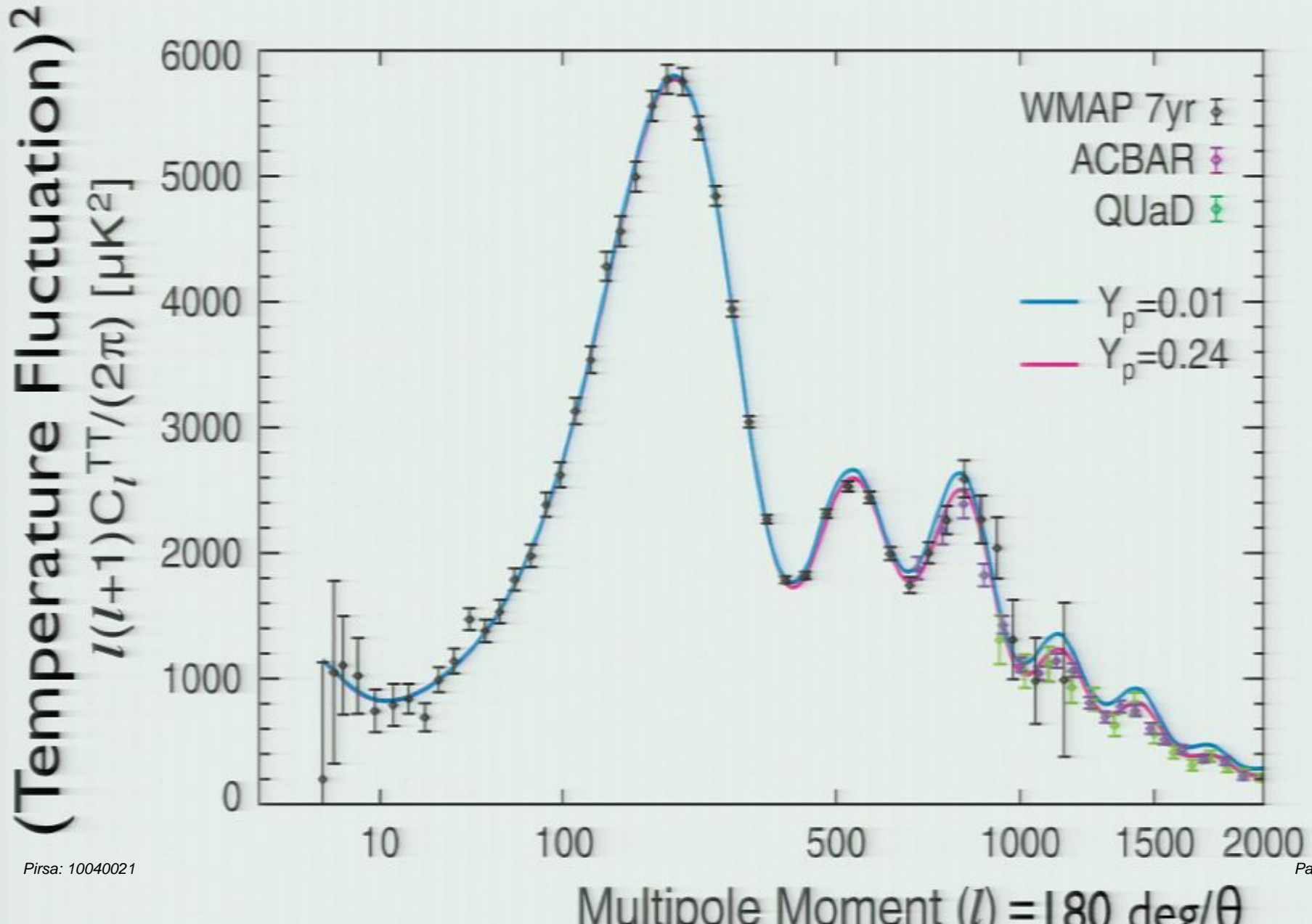




# WMAP and ACT



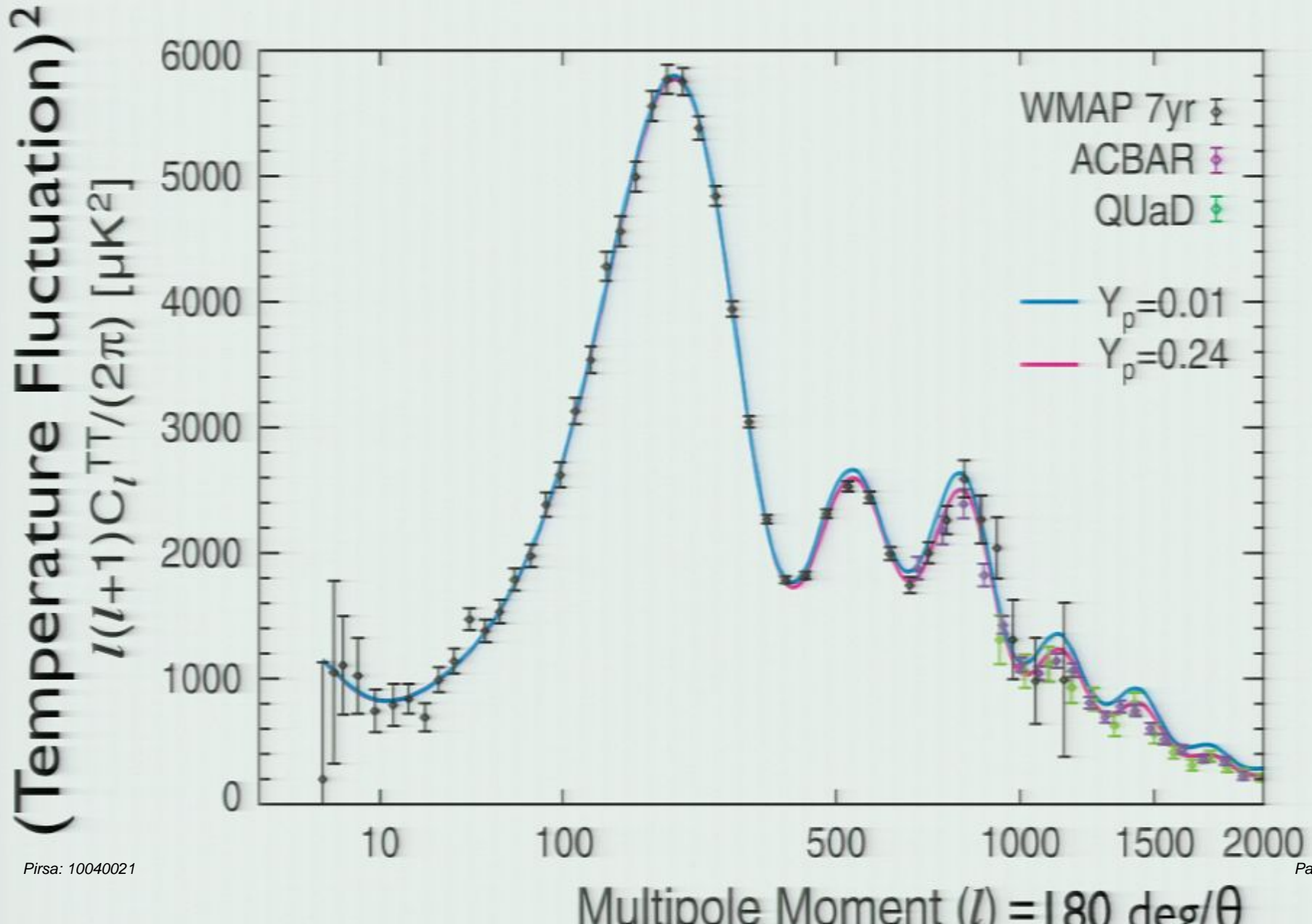
# Detection of Primordial Helium



# Effect of helium on $C_l^{\text{TT}}$

- We measure the baryon number density,  $n_b$ , from the 1st-to-2nd peak ratio.
- As helium recombined at  $z \sim 1800$ , there were fewer electrons at the decoupling epoch ( $z = 1090$ ):  $n_e = (1 - Y_p)n_b$ .
- **More helium** = Fewer electrons = Longer photon mean free path  $1/(\sigma_T n_e) =$  **Enhanced Silk damping**
- This effect might be degenerate with  $\Omega_b h^2$  or  $n_s \dots$

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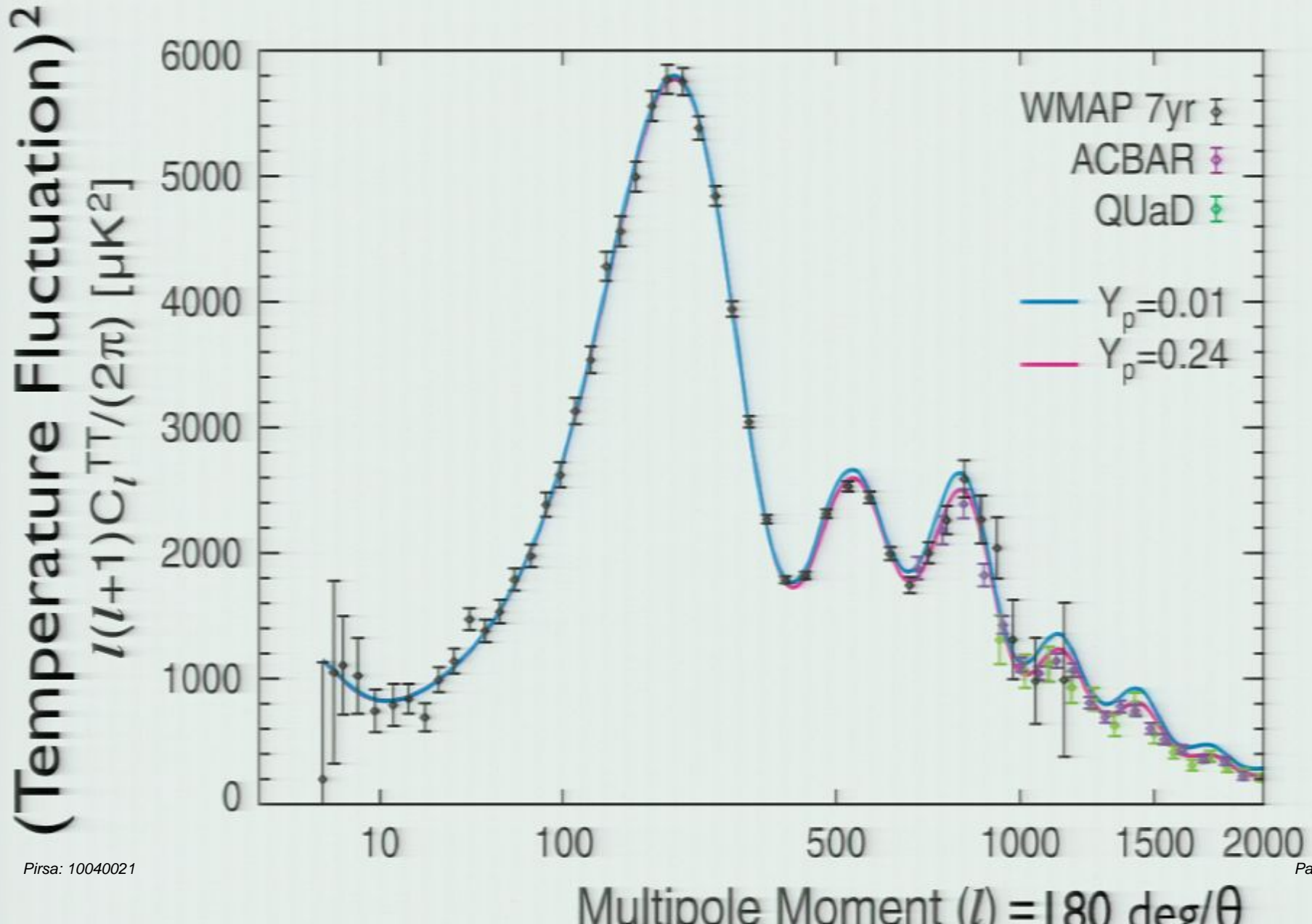




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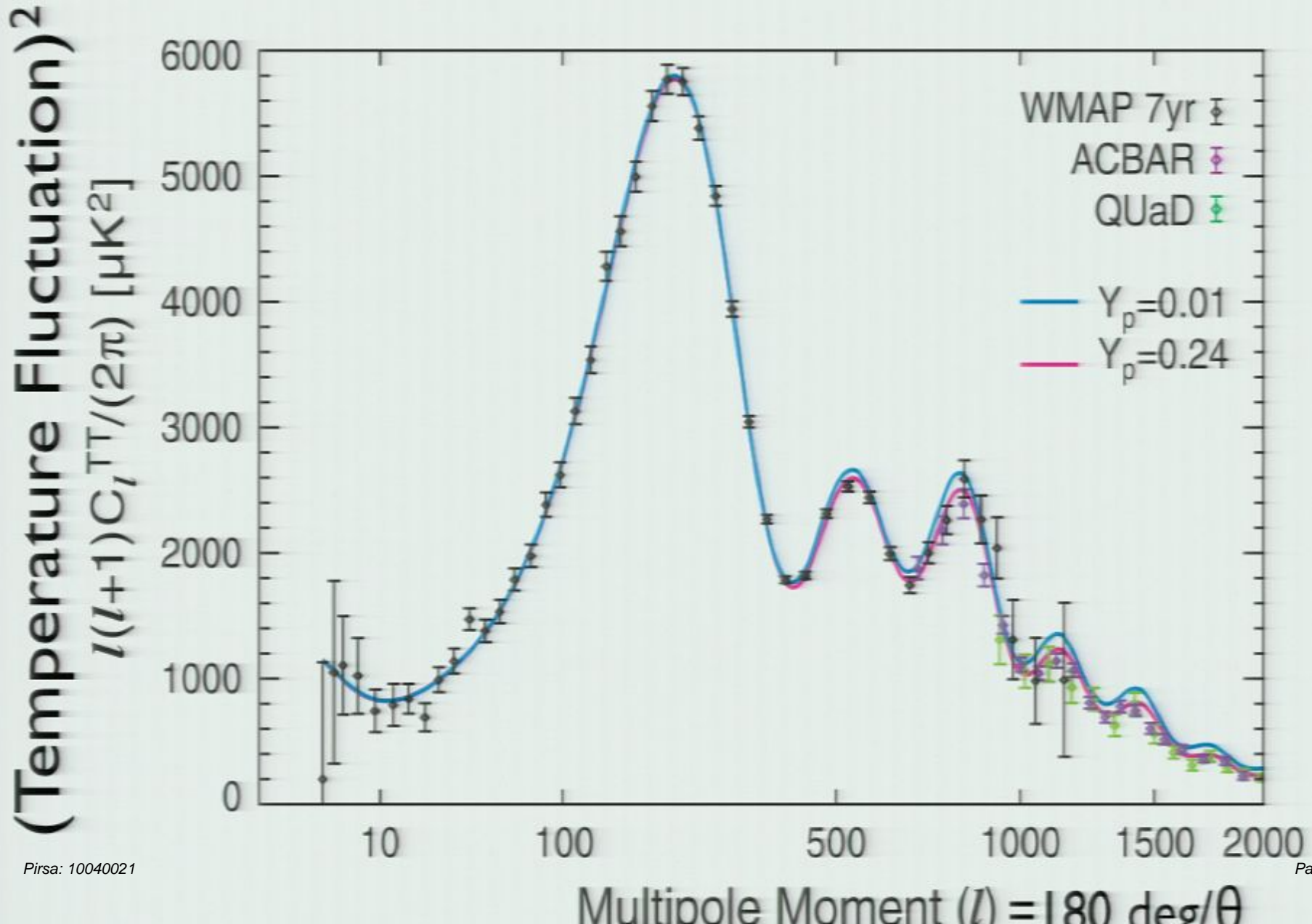
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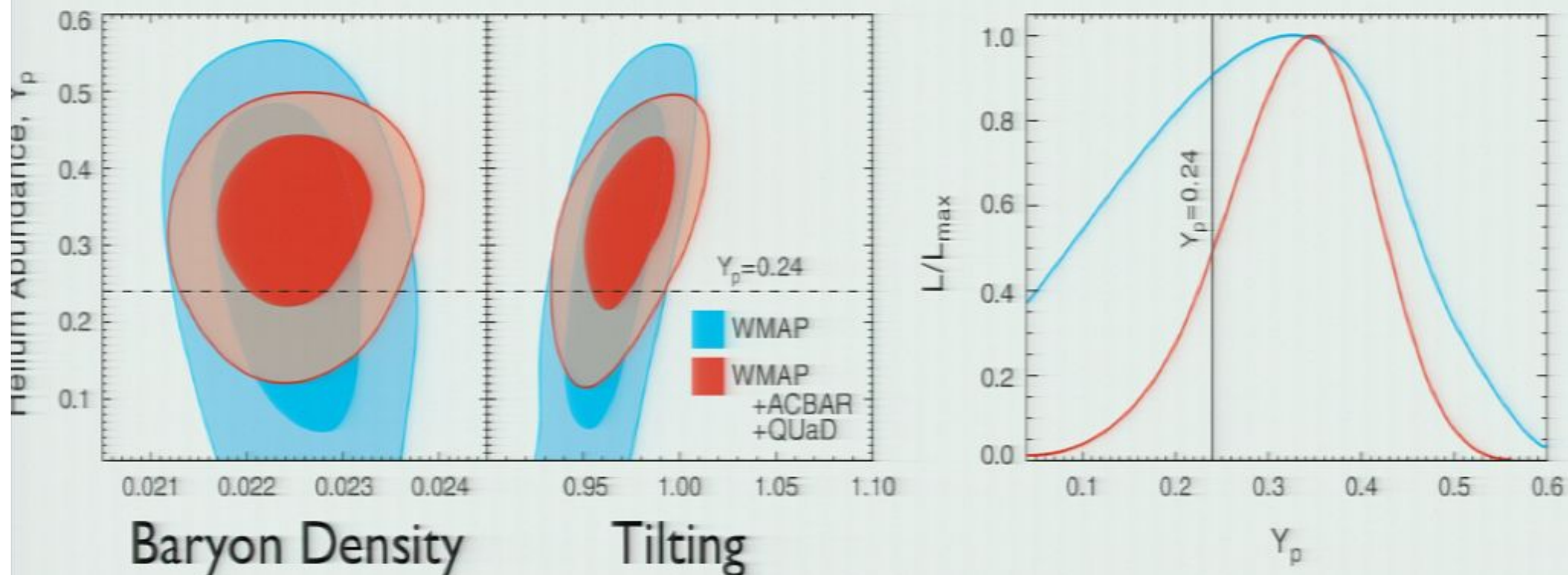
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# Detection of Primordial Helium





# WMAP + higher- $l$ CMB = Detection of Helium

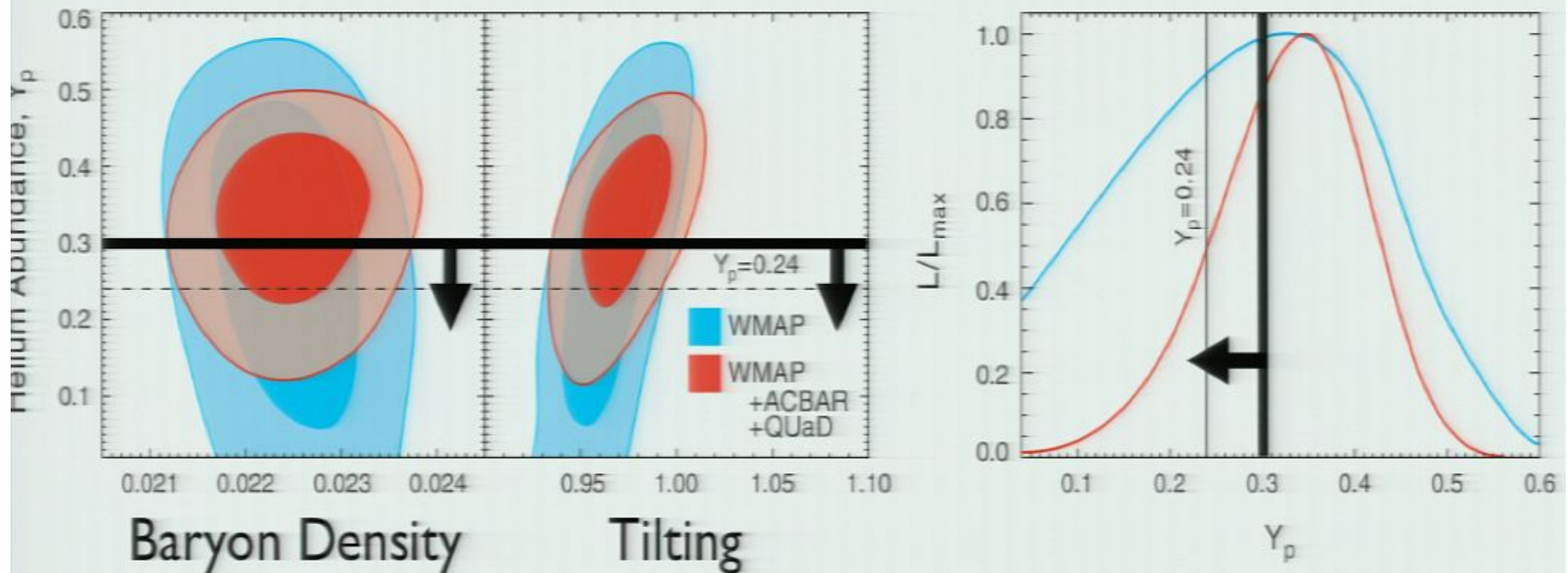


- The combination of WMAP and high- $l$  CMB data (ACBAR and QUaD) is powerful enough to isolate the effect of helium:  **$Y_p = 0.33 \pm 0.08$**  (68%CL)

# Why this can be useful

- The helium abundance has been measured from Sun and ionized regions (HII regions); however, as helium can be produced in the stellar core, one has to extrapolate the measured  $Y_p$  to the zero-metallicity values.
- In other words, the traditional methods give a robust **upper limit** on  $Y_p$ :  $Y_p < 0.3$ .
- The CMB data give us a robust **lower limit** on  $Y_p$ .

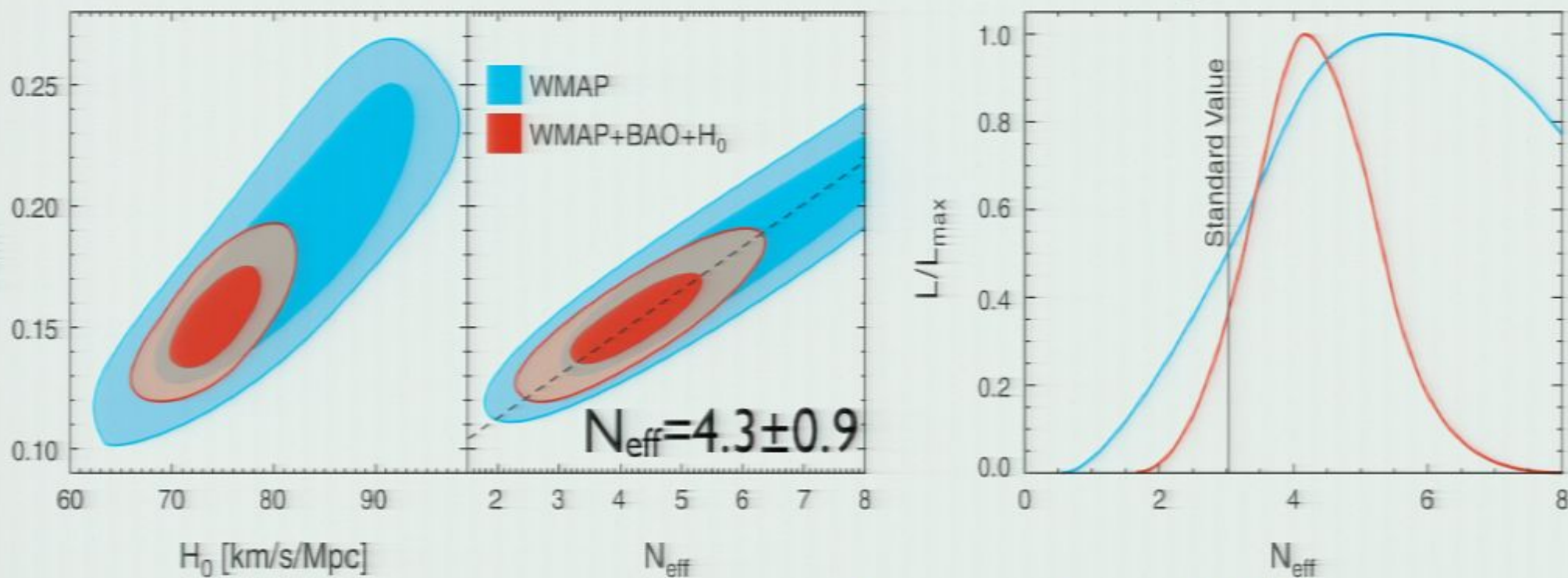
$$0.23 < Y_p < 0.3 \quad (68\% \text{CL})$$



- Planck is expected to yield  $\Delta Y_p \sim 0.01$  (68%CL; Ichikawa et al. 2008).



# Another “3rd peak science”: Number of Relativistic Species



$$N_{\text{eff}} = 3.04 + 7.44 \left( \frac{\Omega_m h^2 \quad \overset{\text{from external data}}{3139}}{0.1308 \quad 1 + z_{\text{eq}} \quad \underset{\text{from 3rd peak}}{1}} - 1 \right)$$



$$P = N_{\text{eff}} T^4$$

$$T_1 = \left(\frac{4}{11}\right)^{1/3} T_2$$

$$P = N_{eff} T_{\nu}^4$$

$$T_{\nu} = \left(\frac{4}{11}\right)^{1/3} T_{\gamma}$$

CAUTION

BE CAREFUL OF THE HOT SURFACE  
DO NOT TOUCH THE HOT SURFACE

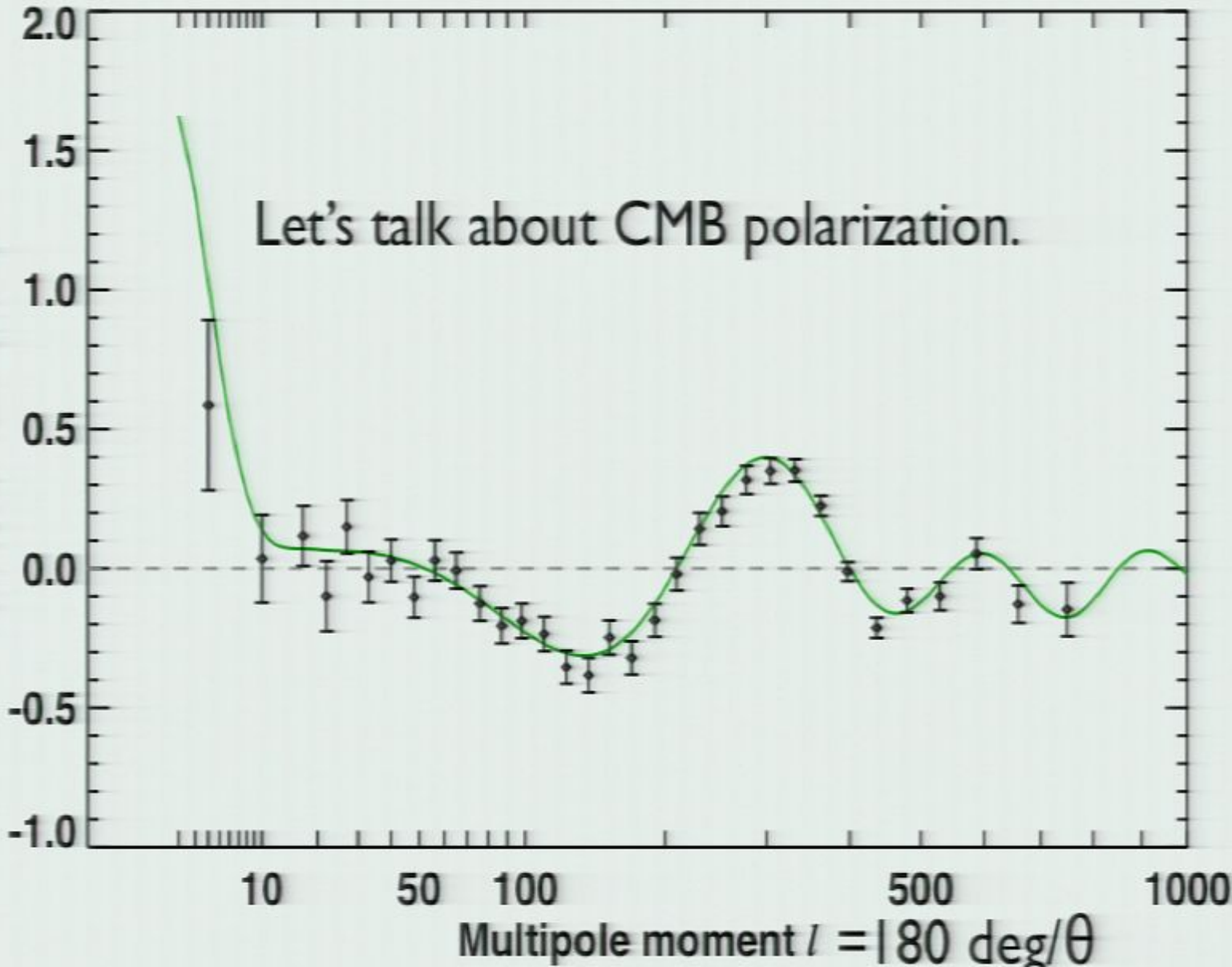
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# 7-year TE Correlation

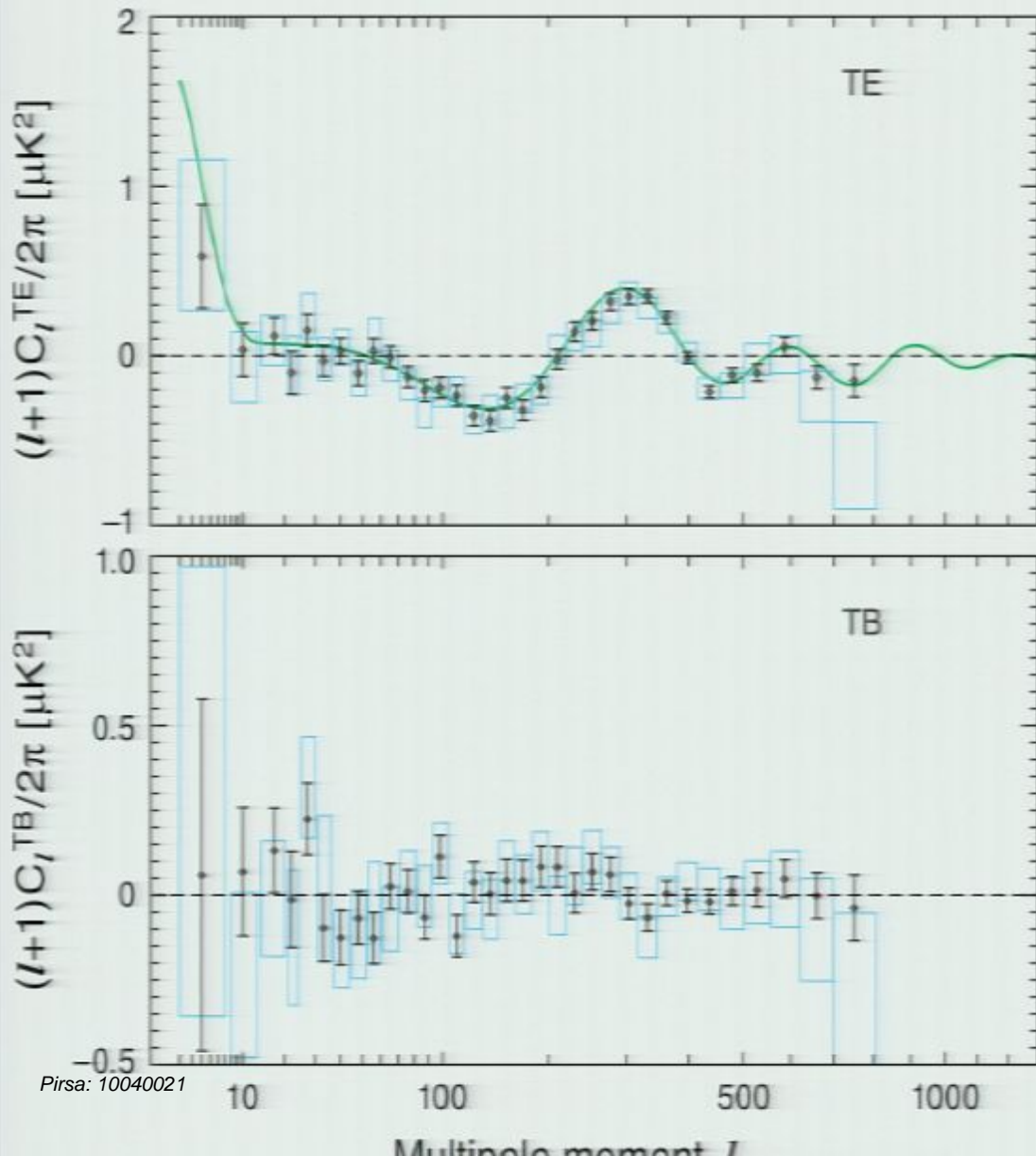
(TxPolarization Fluctuation)

$$(l+1)C_l^{TE}/2\pi \text{ [}\mu\text{K}^2\text{]}$$





# Improvements from 5-year



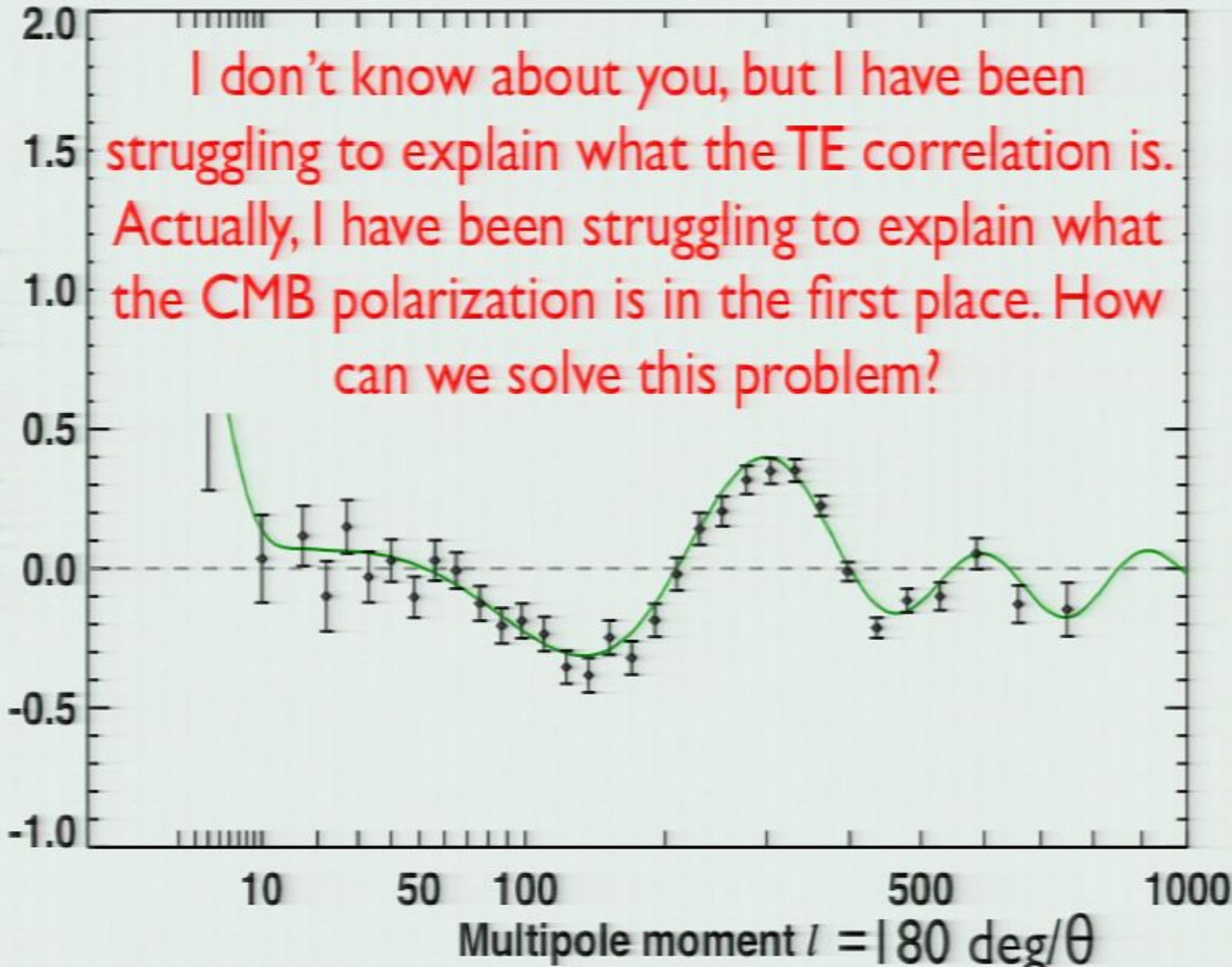
- For 5-year, we used Q and V bands to measure the high- $l$  TE and TB. For 7-year, we also include the W-band data.
- **TE:  $21\sigma$  detection!** (It was  $13\sigma$  in 5 year.)
- TB is expected to vanish in a parity-conserving universe, and it is consistent with zero.



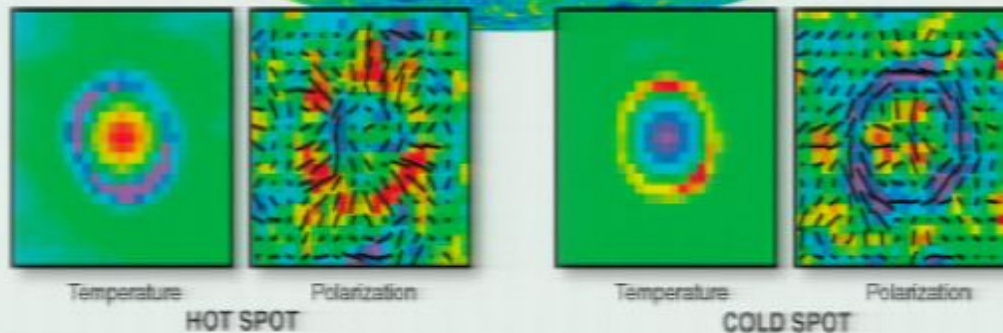
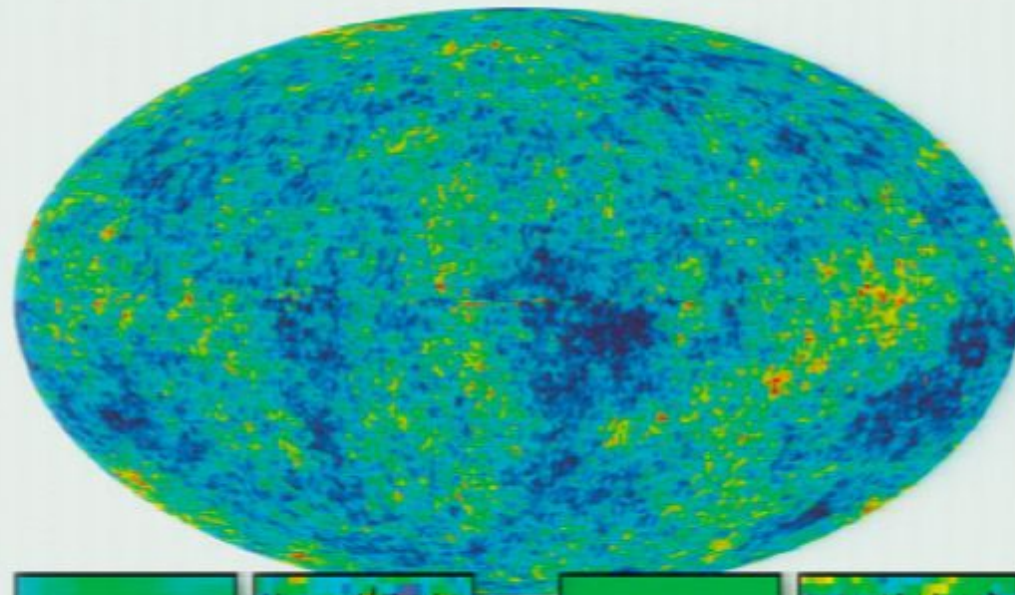
# What Are We Seeing Here?

(TxPolarization Fluctuation)

$(l+1)C_l^{TE}/2\pi$  [ $\mu\text{K}^2$ ]

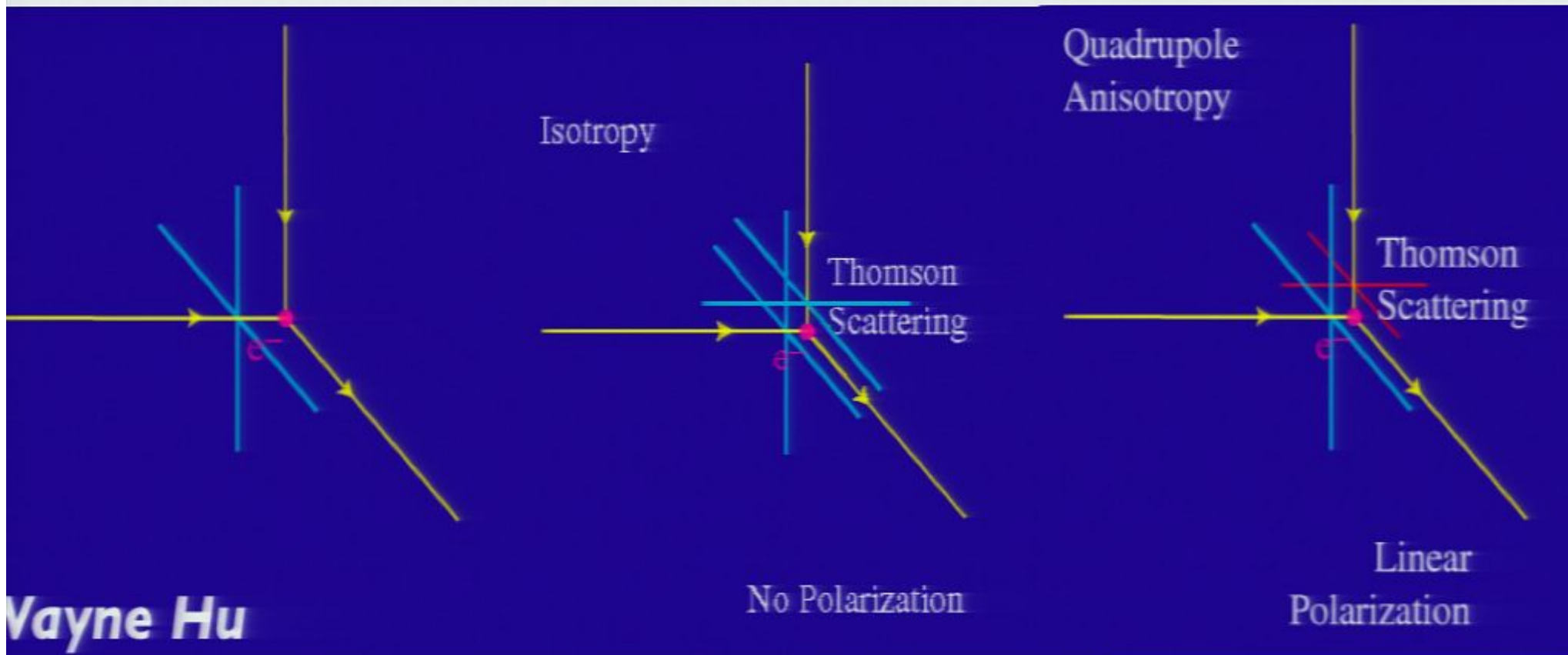


# CMB Polarization On the Sky



- *Solution:* Leave Fourier space.  
Go back to real space.

# CMB Polarization is a Real-space Stuff



- CMB Polarization is created by a local temperature **quadrupole** anisotropy.



# CMB Polarization on Large Angular Scales ( $>2$ deg)

Matter  
Density



Potential



$$\Delta T/T = (\text{Newton's Gravitation Potential})/3$$

$\Delta T$



Polarization



- How does the photon-baryon plasma move?



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Matter  
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Polarization



- How does the photon-baryon plasma move?

# CMB Polarization Tells Us How Plasma Moves at $z=1090$

*Zaldarriaga & Harari (1995)*

Matter Density



Potential



$$\Delta T/T = (\text{Newton's Gravitation Potential})/3$$

$\Delta T$



Polarization



- Plasma **falling into** the gravitational potential well = **Radial** polarization pattern

# Quadrupole From Velocity Gradient (Large Scale)

$\Delta T$



Sachs-Wolfe:  $\Delta T/T = \Phi/3$

Potential  $\Phi$



Stuff flowing *in*

Acceleration

$$a = -\partial\Phi$$



$$a > 0 \quad = 0$$

Velocity



Velocity gradient

Velocity in the rest  
frame of electron



The left electron sees colder  
photons along the plane wave

Polarization

Radial None



# Quadrupole From Velocity Gradient (Small Scale)

$\Delta T$



Compression increases temperature

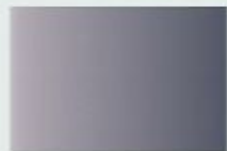
Potential  $\Phi$



Stuff flowing in

Acceleration

$$a = -\partial\Phi - \partial P$$



Pressure gradient slows down the flow

$$a > 0 < 0$$

Velocity



Velocity gradient

Velocity in the rest frame of electron



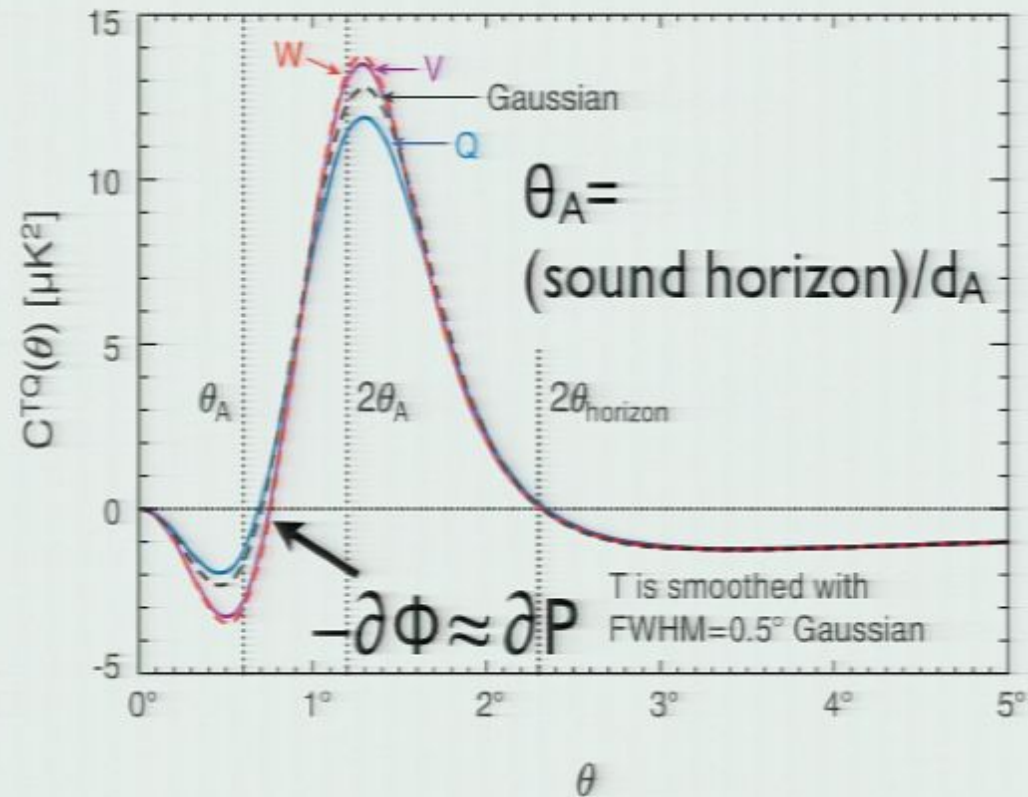
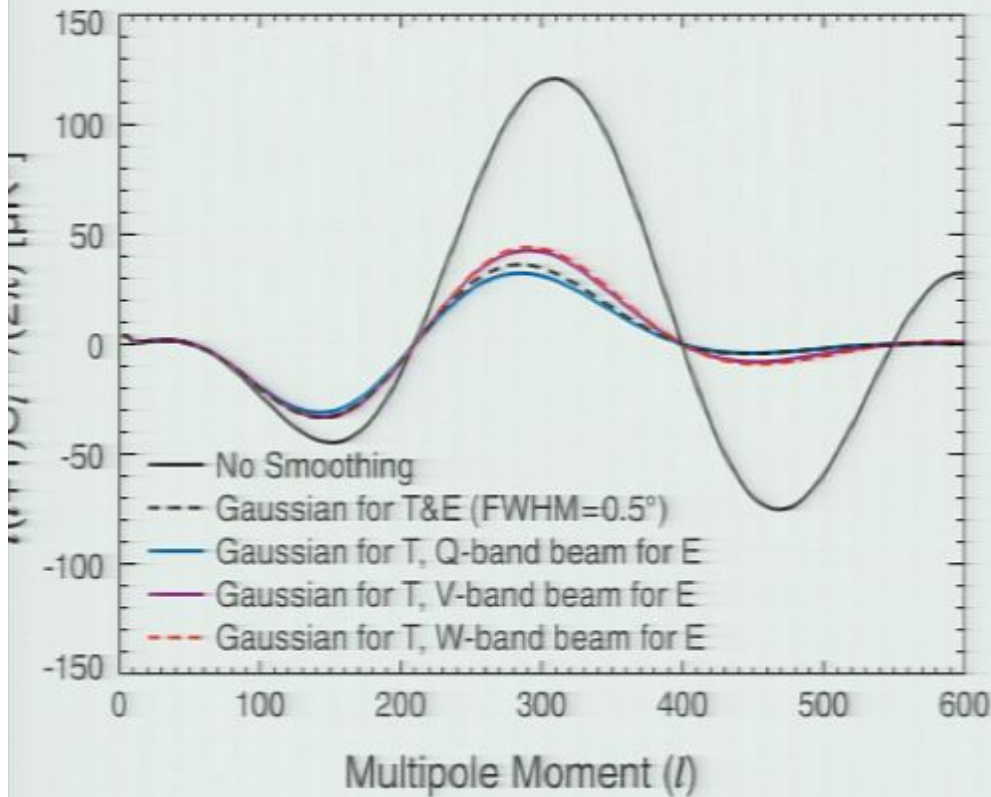
Polarization

Radial

Tangential



# Hence, TE Correlation (Coulson et al. 1994)



Pirsa: 100.002

$$C^{TQr}(\theta) = -\int dl n_l \left[ \frac{l^2 C_l^{TE}}{(2\pi)} \right] J_2(l\theta)$$

Page 65/124 27

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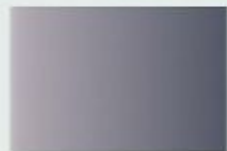
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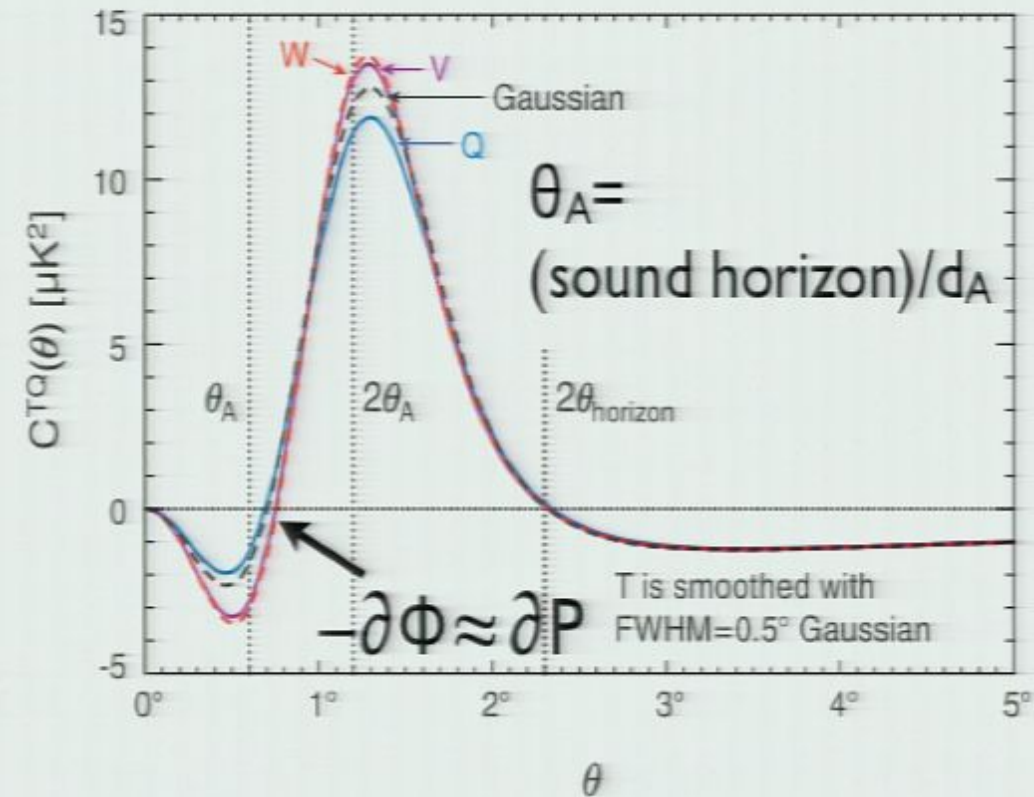
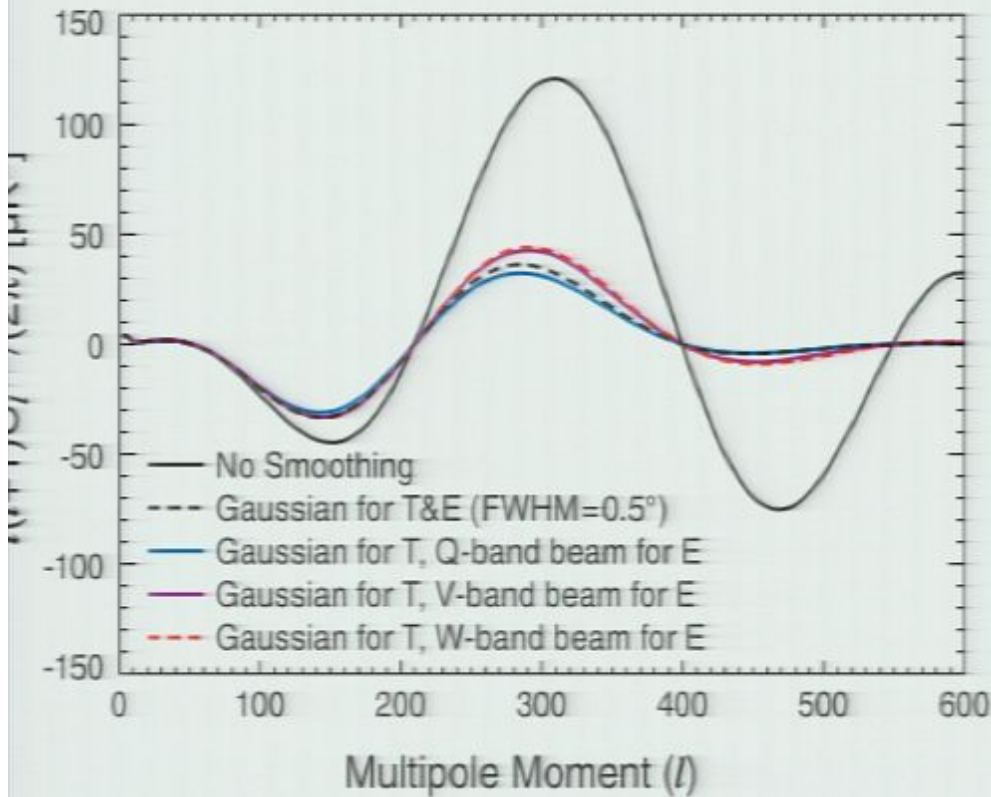


Polarization

Radial

Tangential

# Hence, TE Correlation (Coulson et al. 1994)



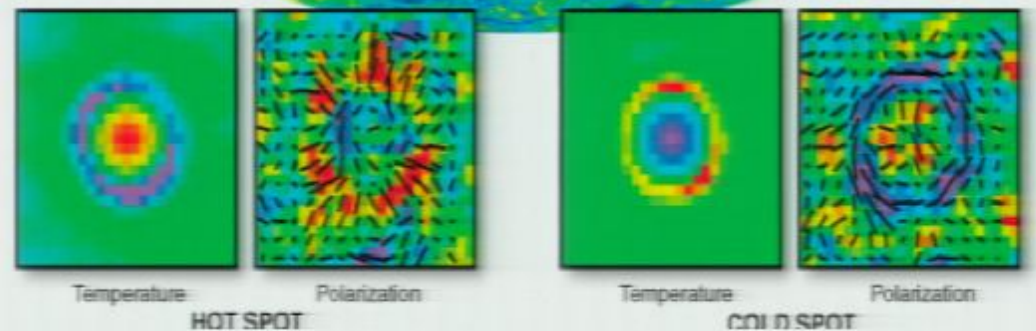
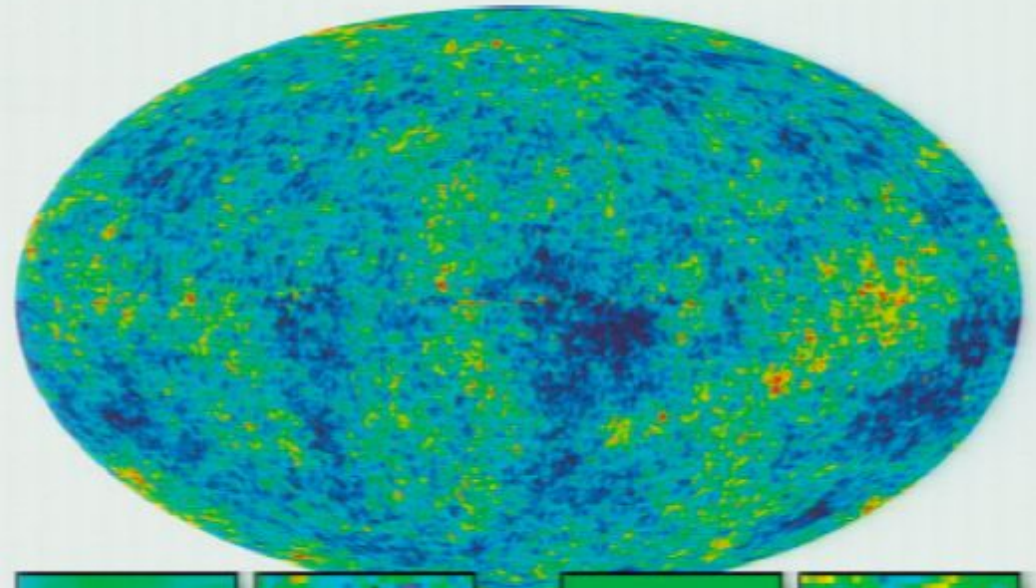
$$\bullet C^{TQr}(\theta) = -\int dl n_l \left[ \frac{l^2 C_l^{TE}}{(2\pi)} \right] J_2(l\theta)$$



# Peak Theory and Stacking Analysis

- Stack polarization images around temperature hot and cold spots.

- Outside of the Galaxy mask (not shown), there are **12387 hot spots** and **12628 cold spots**.



- Peak theory gives:

[Note the  $l^2$  term!

(Desjacques 2008)]

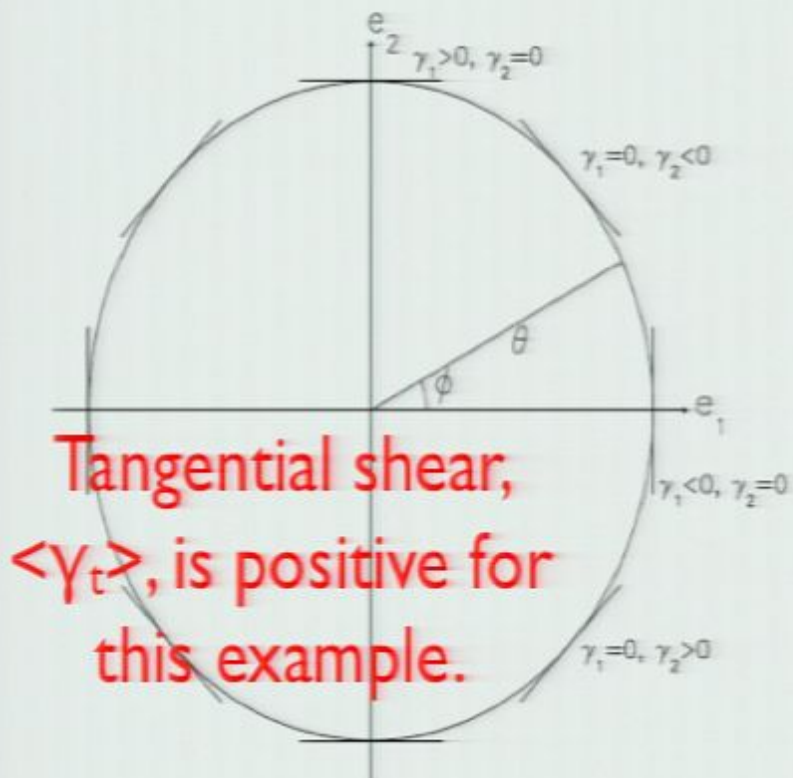
$$\langle Q_r \rangle(\theta) = - \int \frac{ldl}{2\pi} W_l^T W_l^P (\bar{b}_\nu + \bar{b}_\zeta l^2) C_l^{TE} J_2(l\theta),$$

$$\langle U_r \rangle(\theta) = - \int \frac{ldl}{2\pi} W_l^T W_l^P (\bar{b}_\nu + \bar{b}_\zeta l^2) C_l^{TB} J_2(l\theta),$$



# Analogy to Weak Lensing

- If you are familiar with weak lensing, this statistic is equivalent to the *tangential shear*:  $\langle \bar{\gamma}_t^h \rangle(R, z_L) = \frac{\Delta\Sigma(R, z_L)}{\Sigma_c(z_L)}$

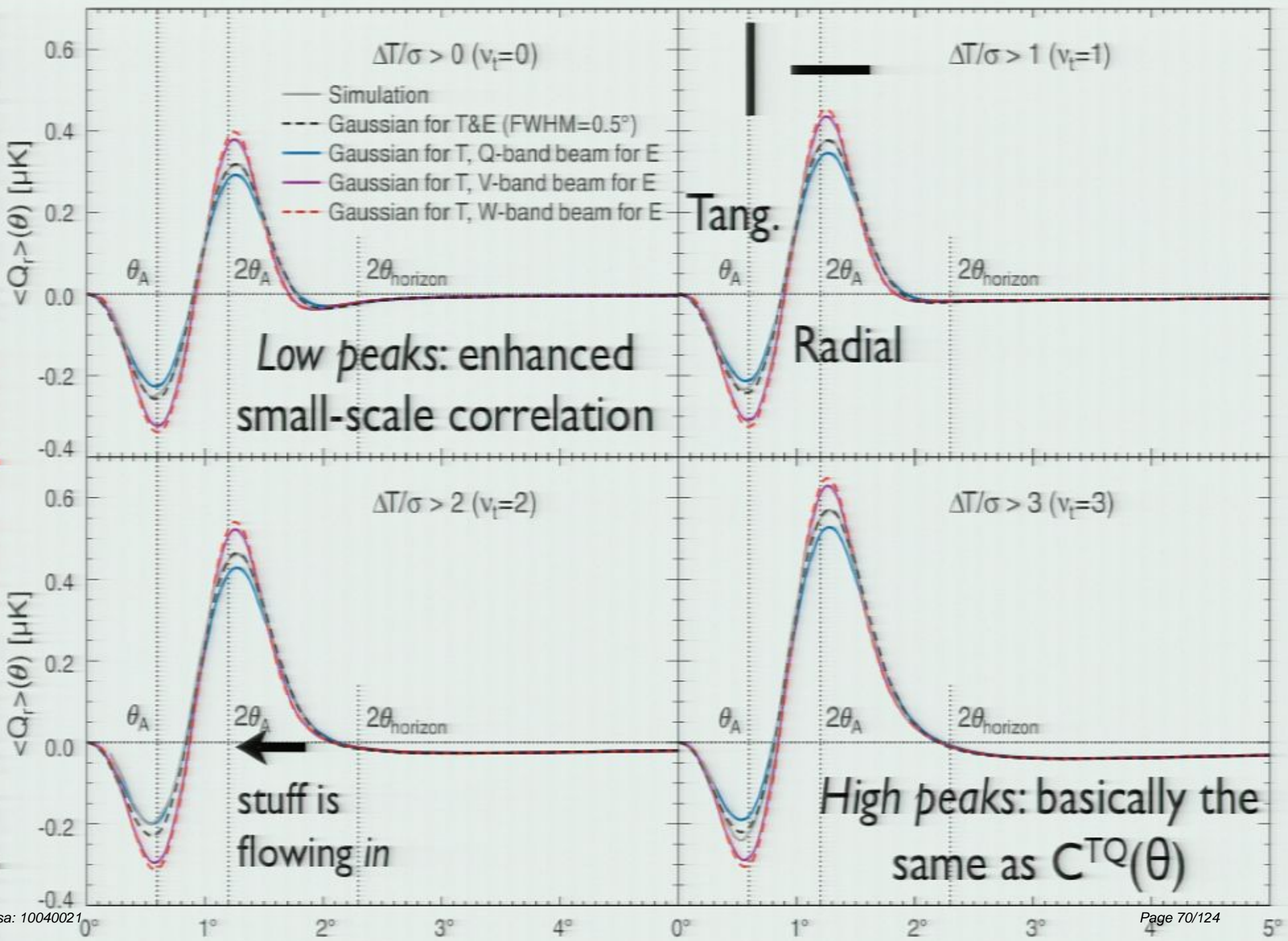


$$\Delta\Sigma(R, z_L) = \rho_0 b_1 \int \frac{k dk}{2\pi} P_m(k, z_L) J_2(kR)$$

However, all the formulae given in the literature use a scale-independent bias,  $b_1$ . This formula must be modified to include the  $k^2$  term.

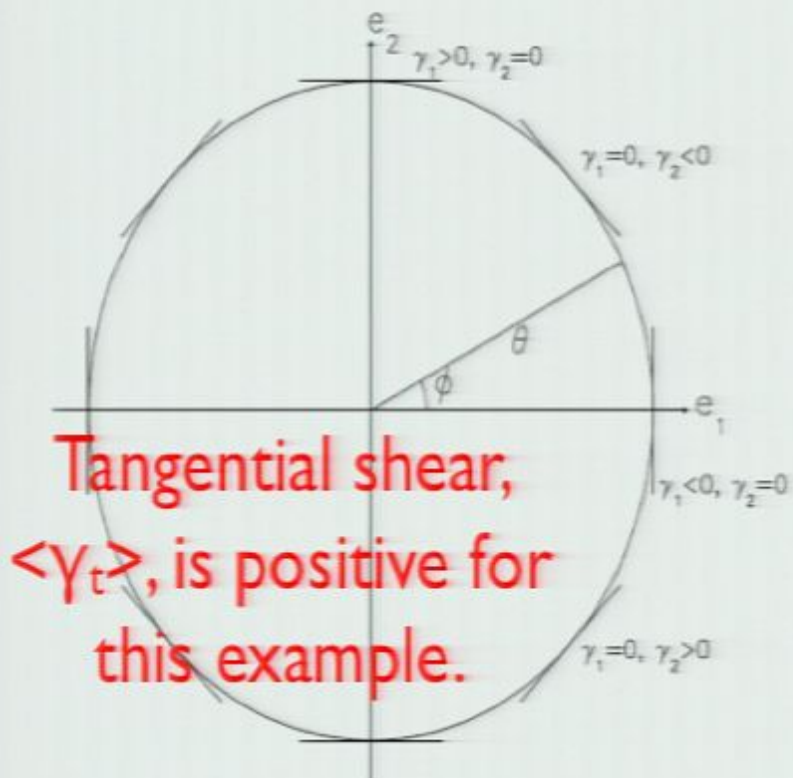
$$\gamma_t(\theta) = -\gamma_1(\theta) \cos(2\phi) - \gamma_2(\theta) \sin(2\phi)$$

temperature hot spots are stacked



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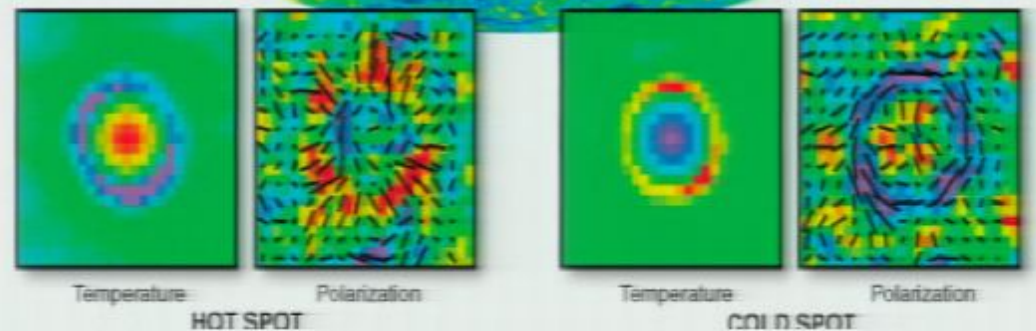
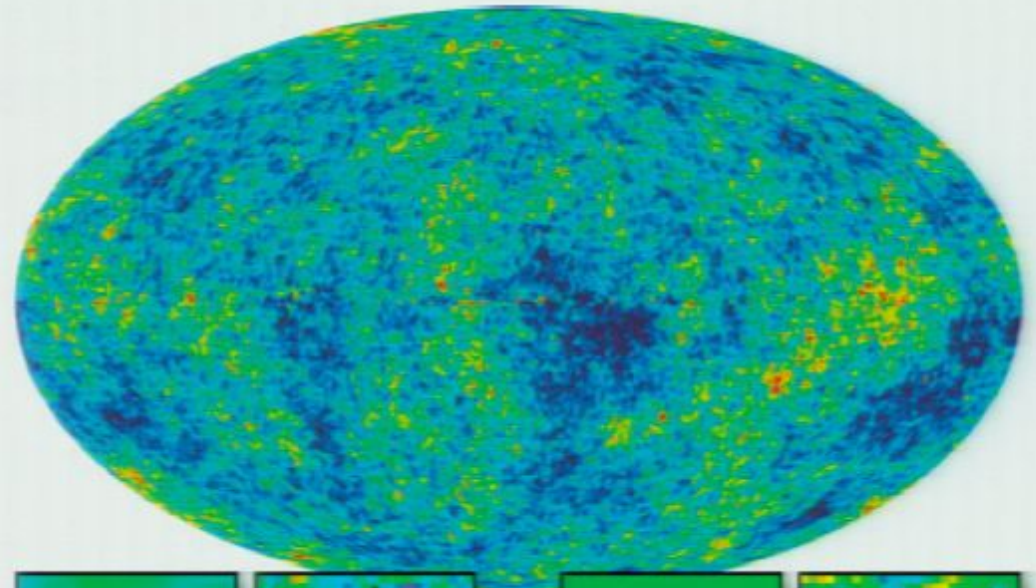
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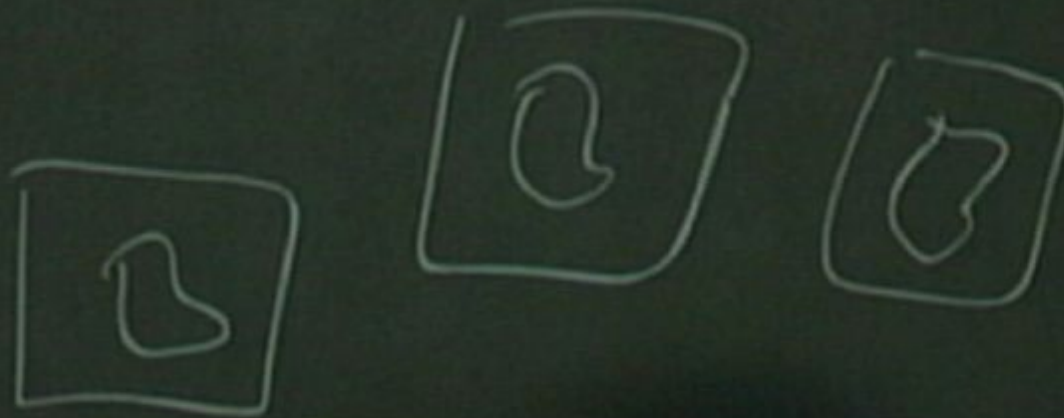
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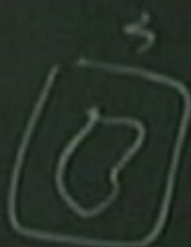
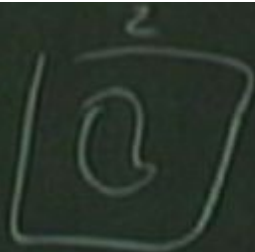
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T. ^





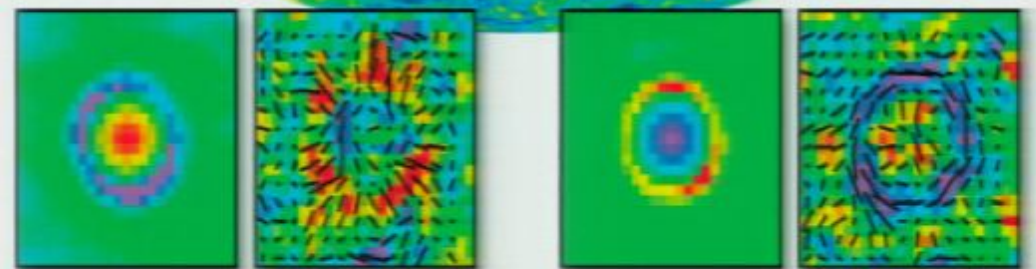
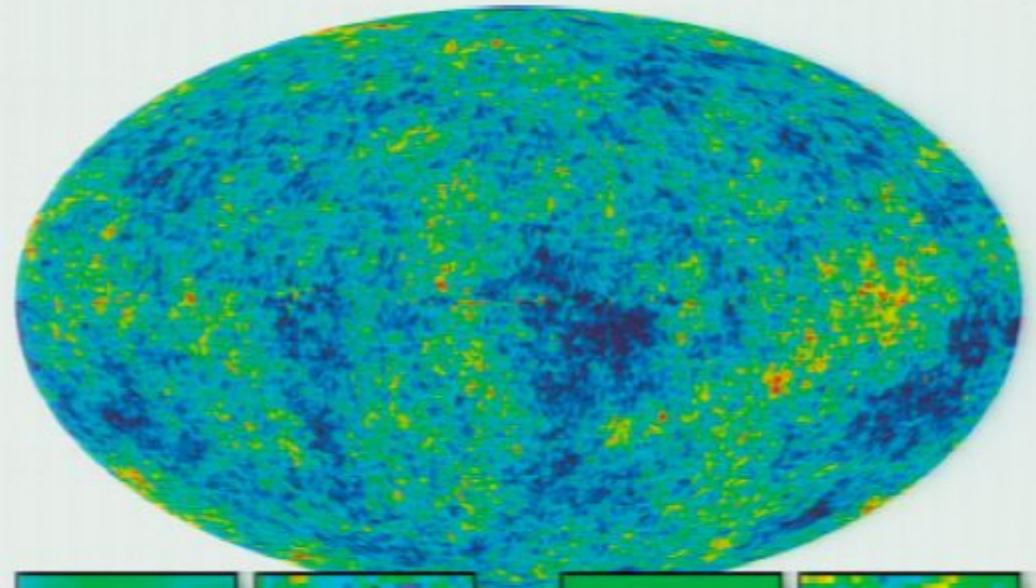
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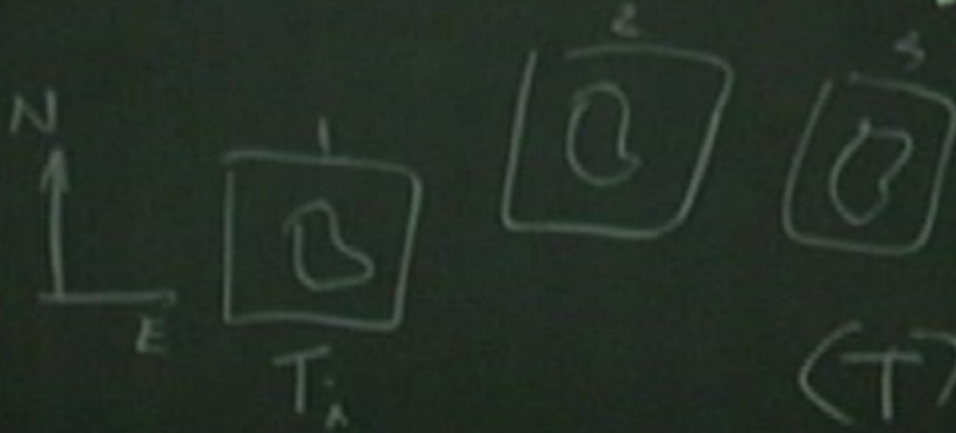
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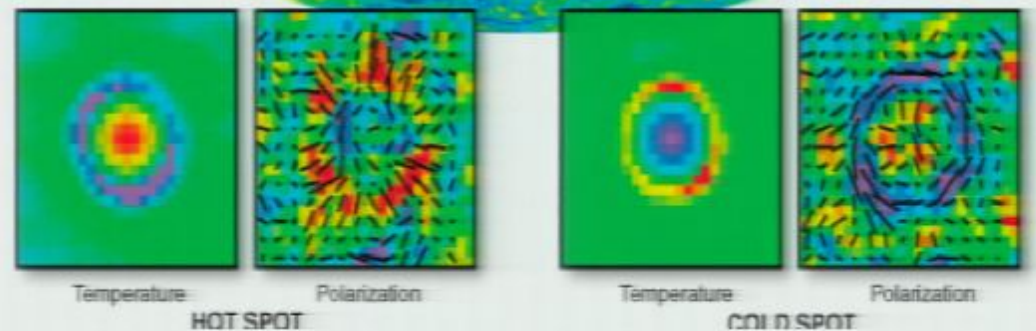
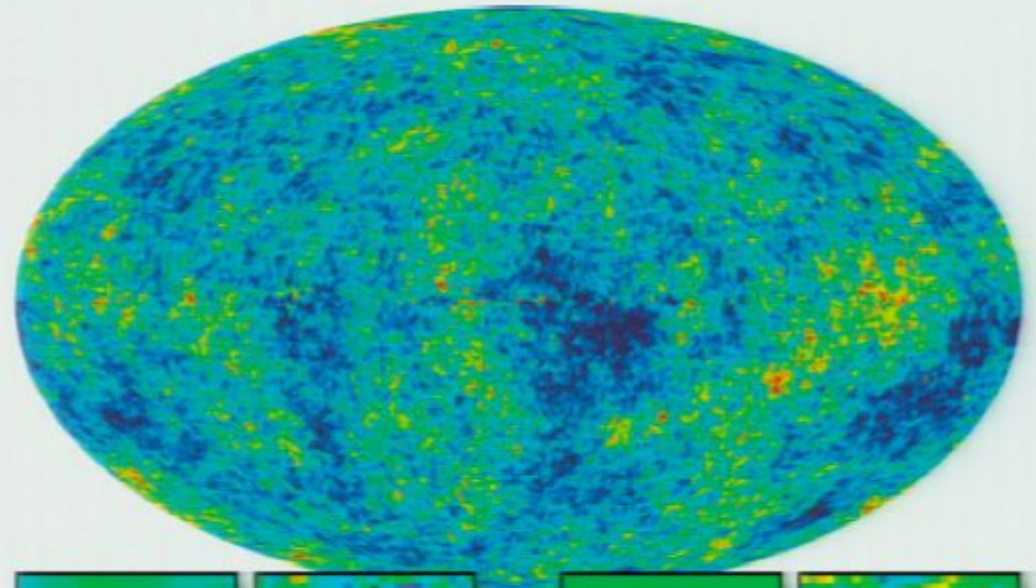


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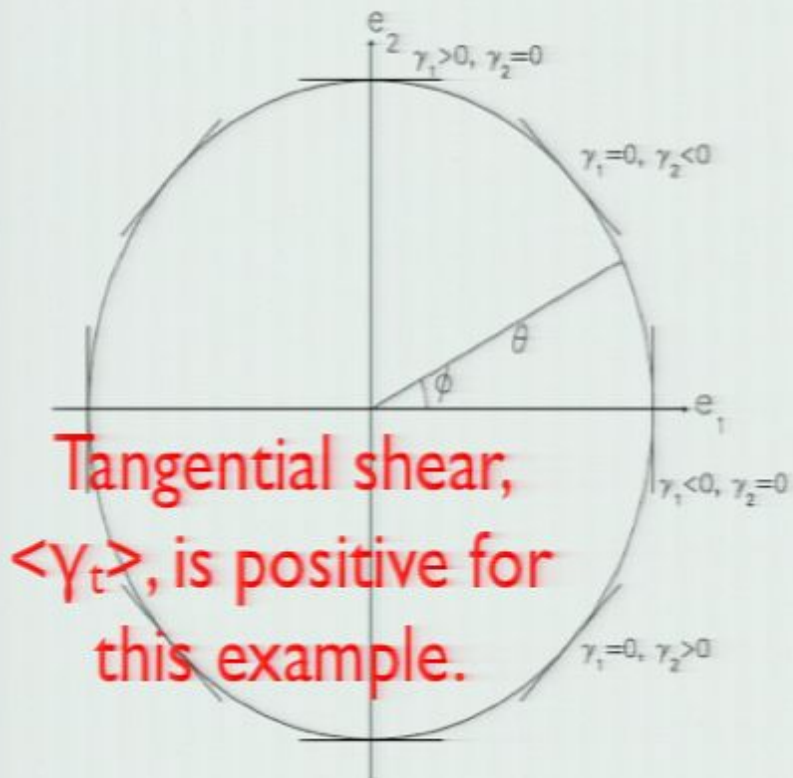
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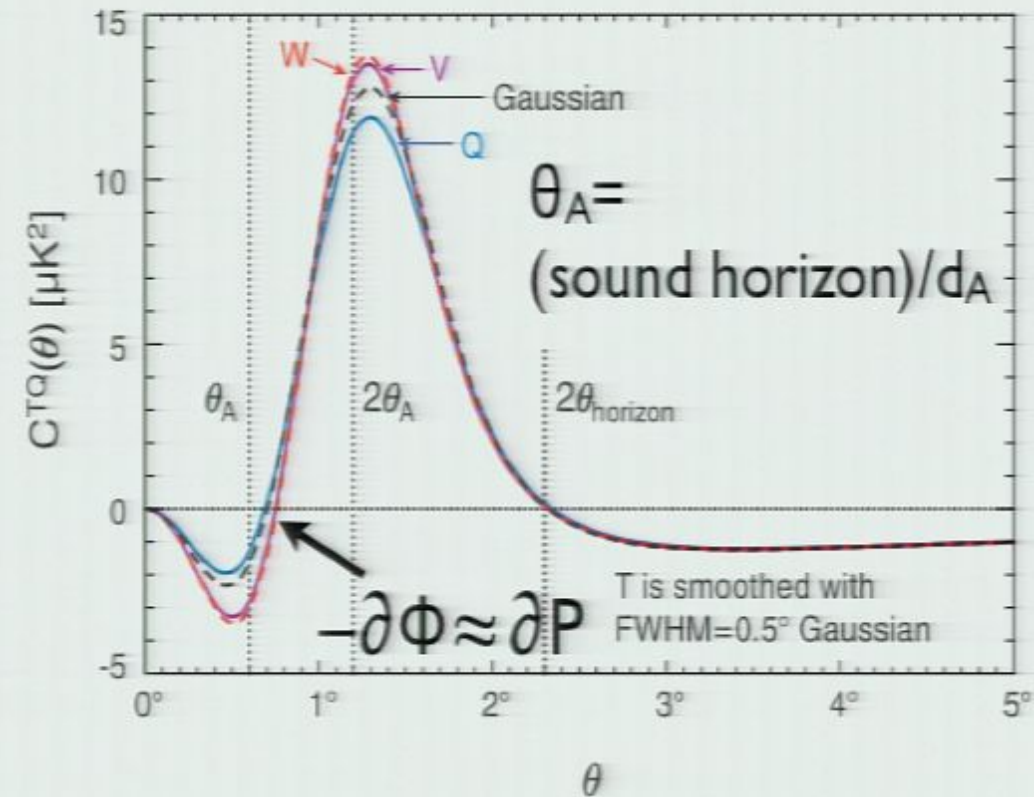
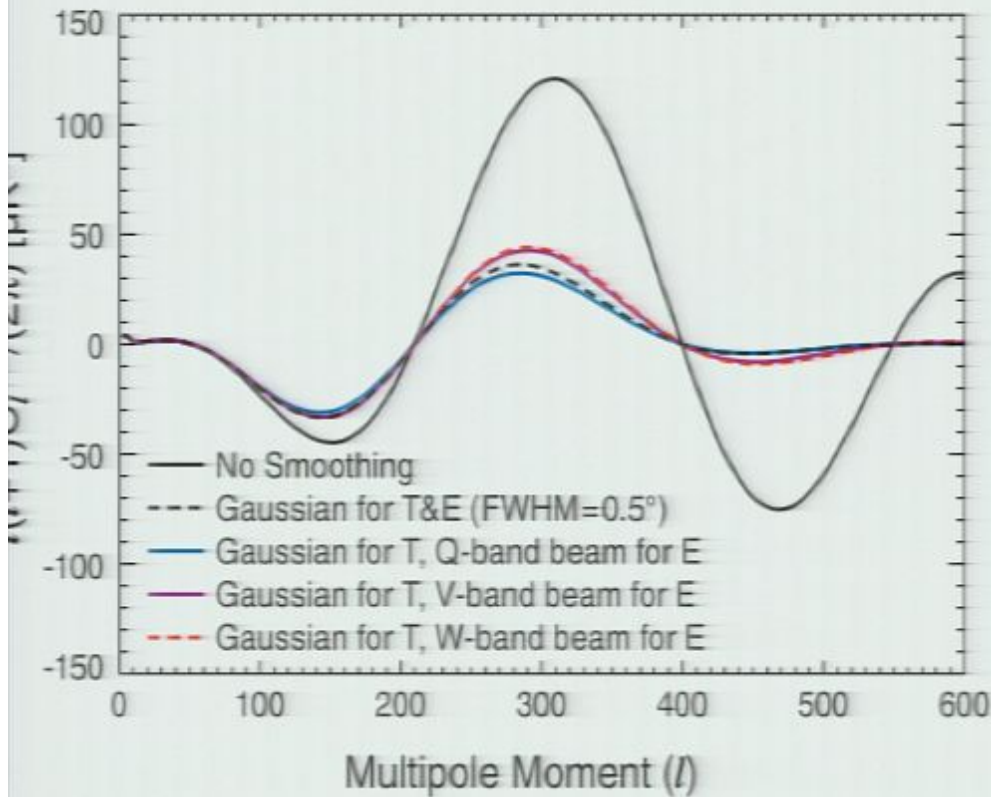
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# Hence, TE Correlation (Coulson et al. 1994)



Pirsa: 100.002

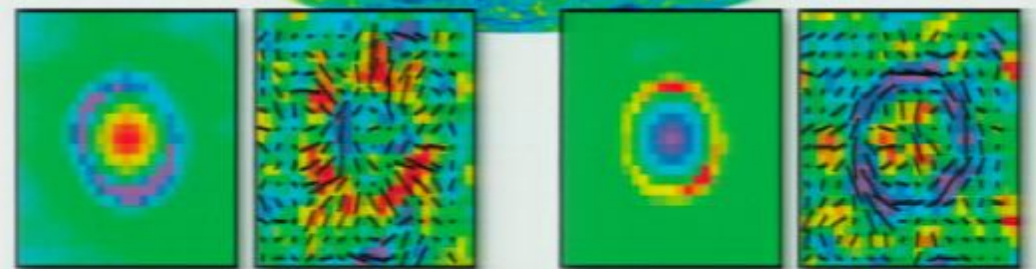
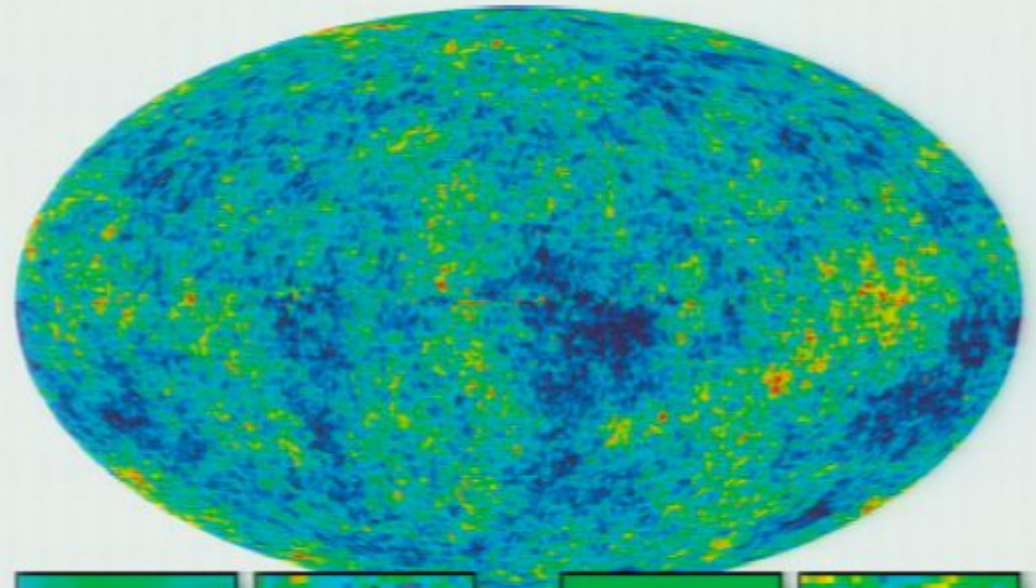
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Page 79/124 27

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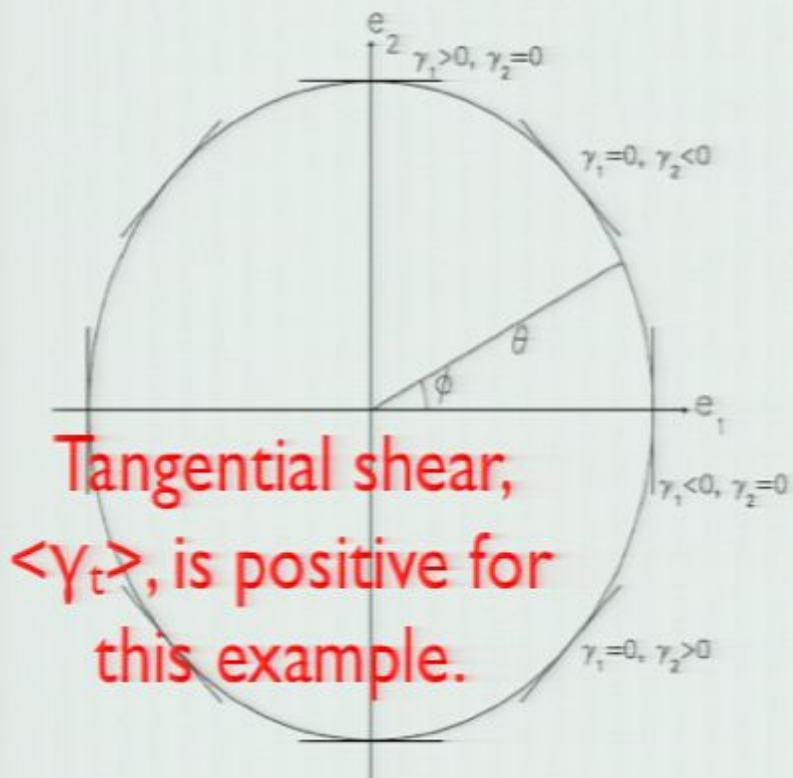
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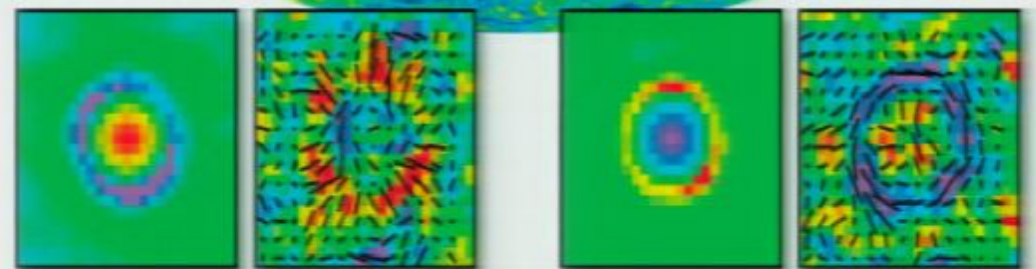
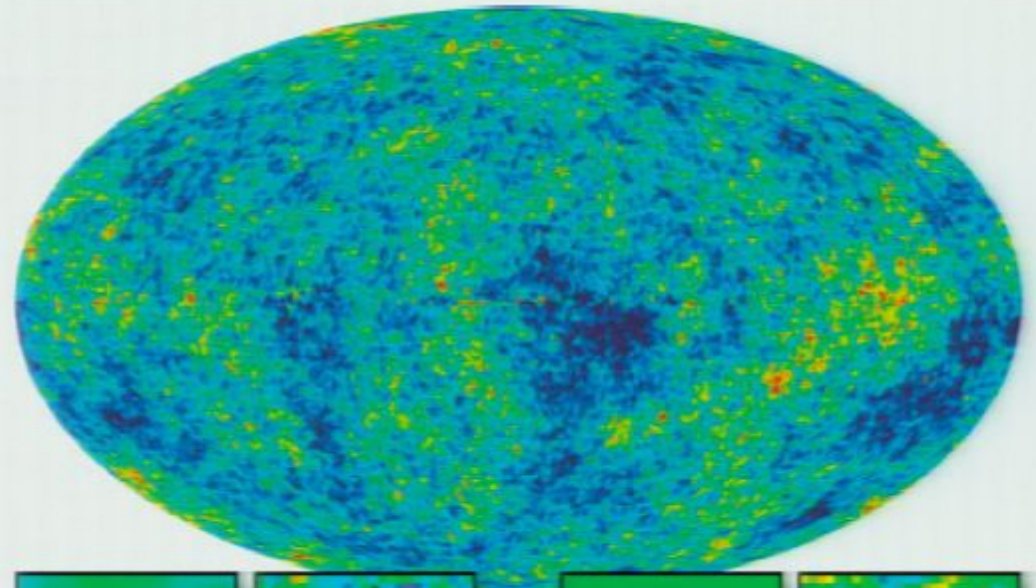
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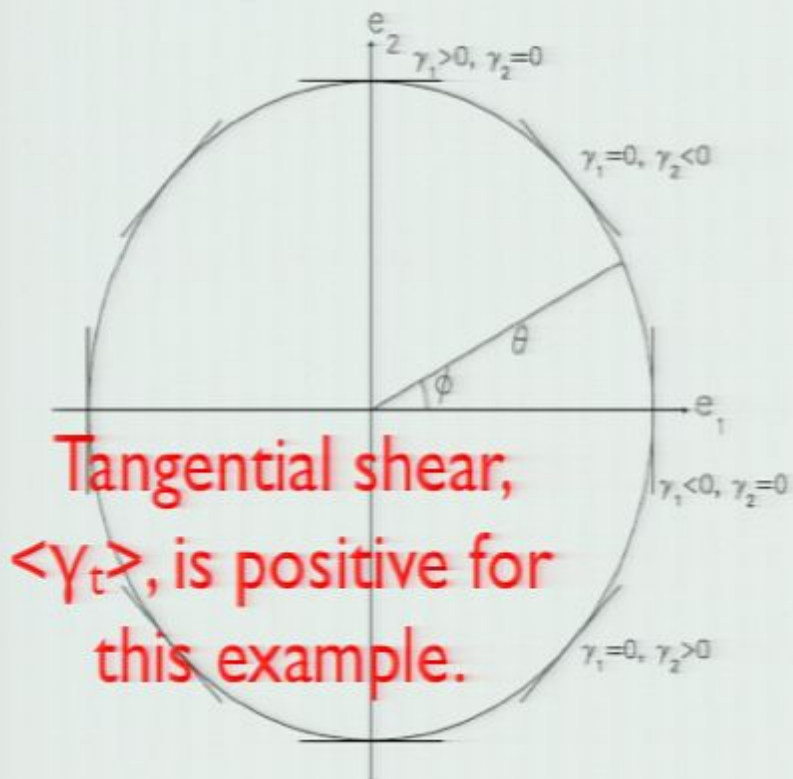
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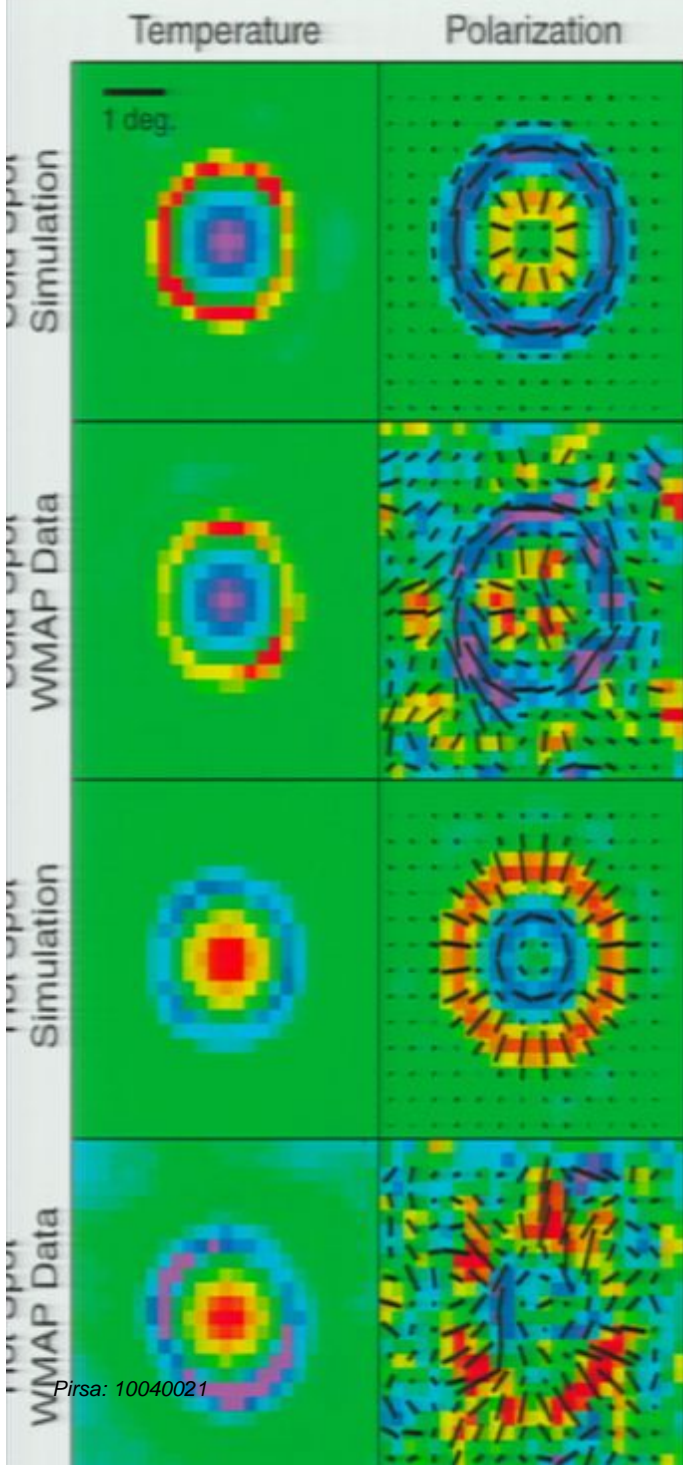


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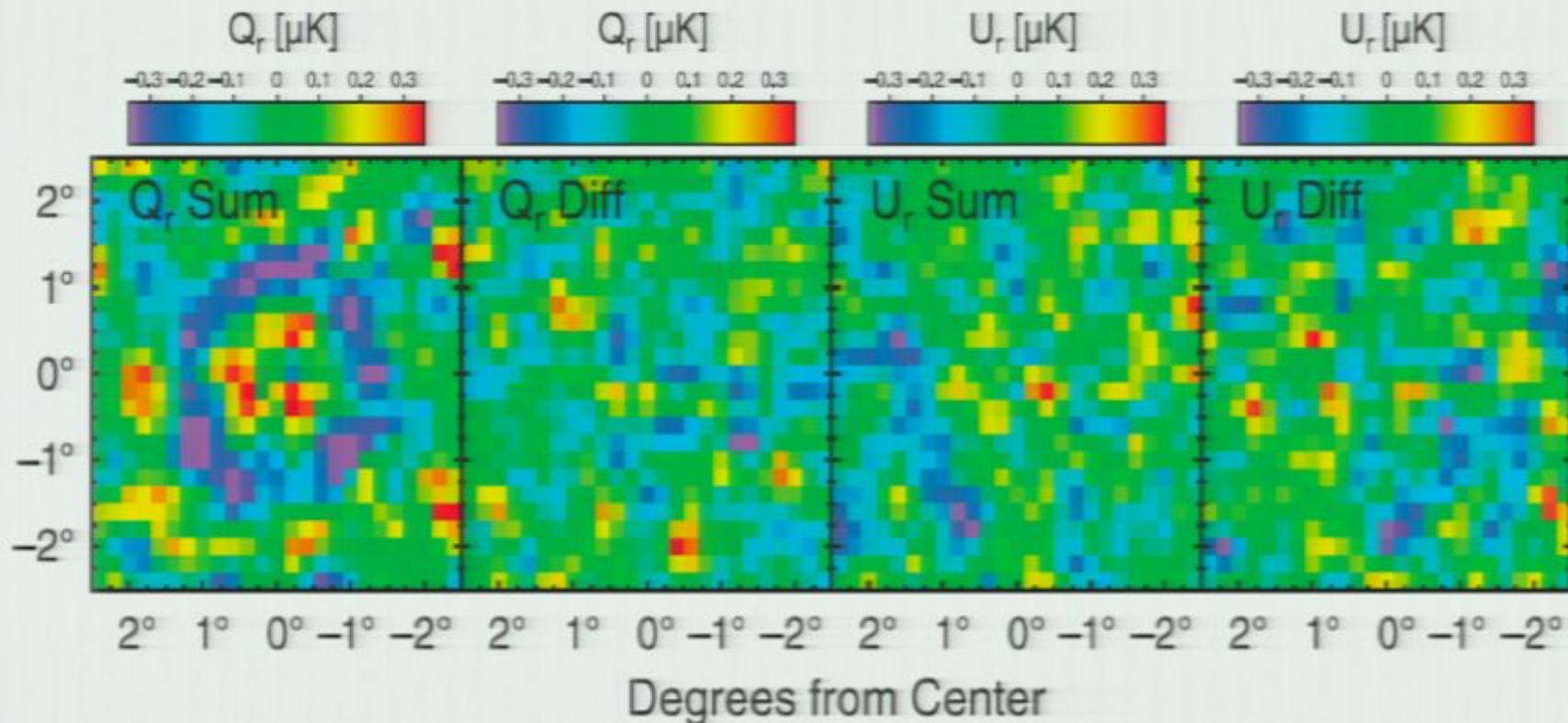
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- All hot and cold spots are stacked (the threshold peak height,  $\Delta T/\sigma$ , is zero)
- “Compression phase” at  $\theta=1.2$  deg and “slow-down phase” at  $\theta=0.6$  deg are predicted to be there and we observe them!
  - The overall significance level:  $8\sigma$
- Striking confirmation of the physics of CMB and the dominance of **adiabatic** & **scalar** perturbation.

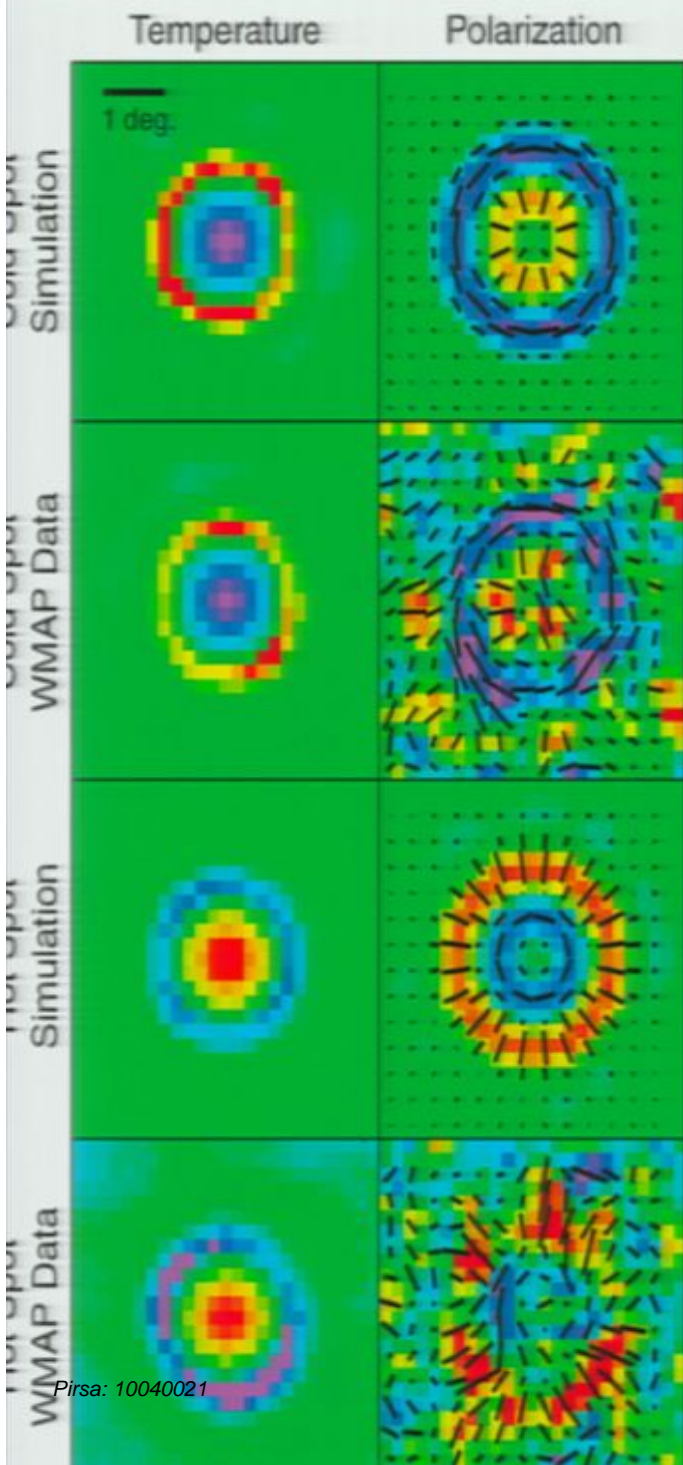


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- $U_r$  is produced by the TB correlation, which is expected to vanish in a parity-conserving universe.



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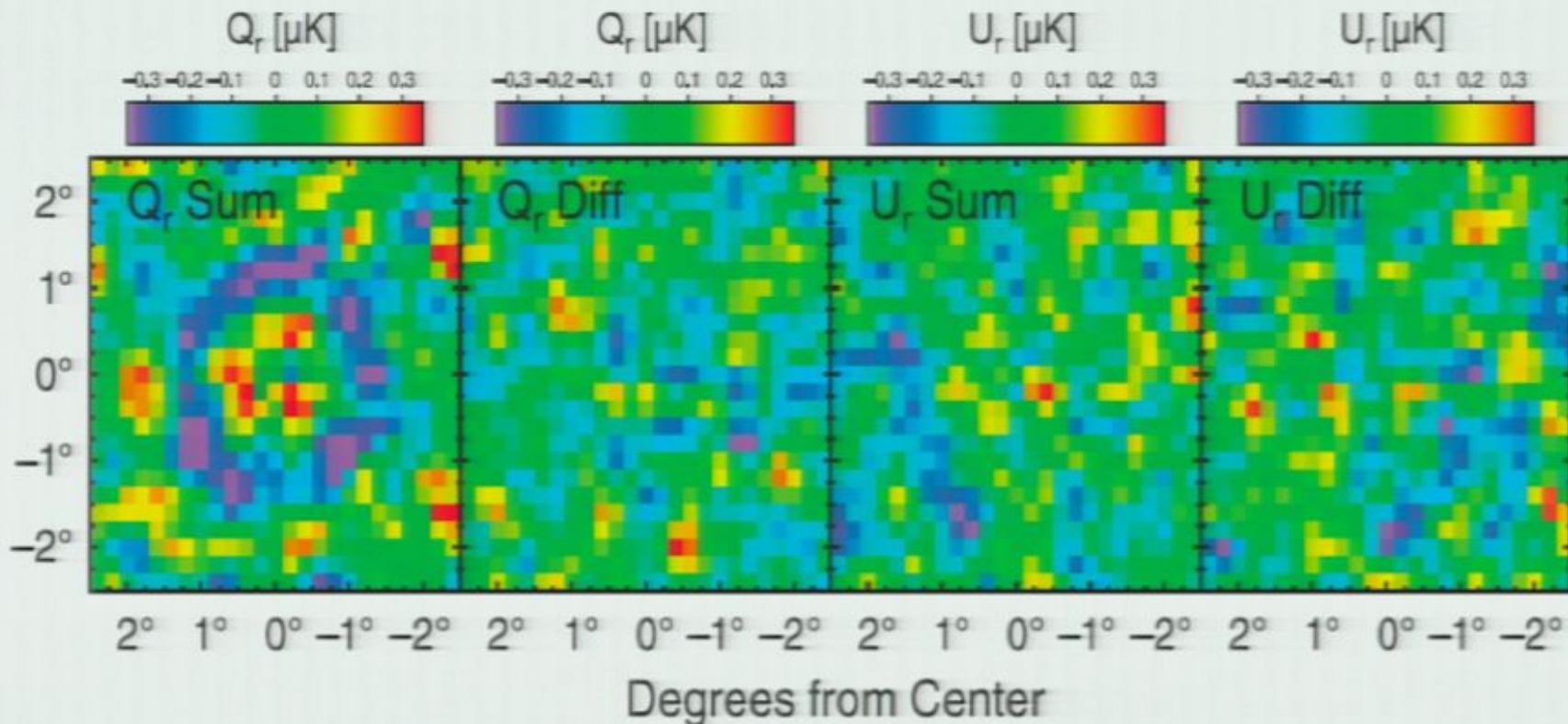
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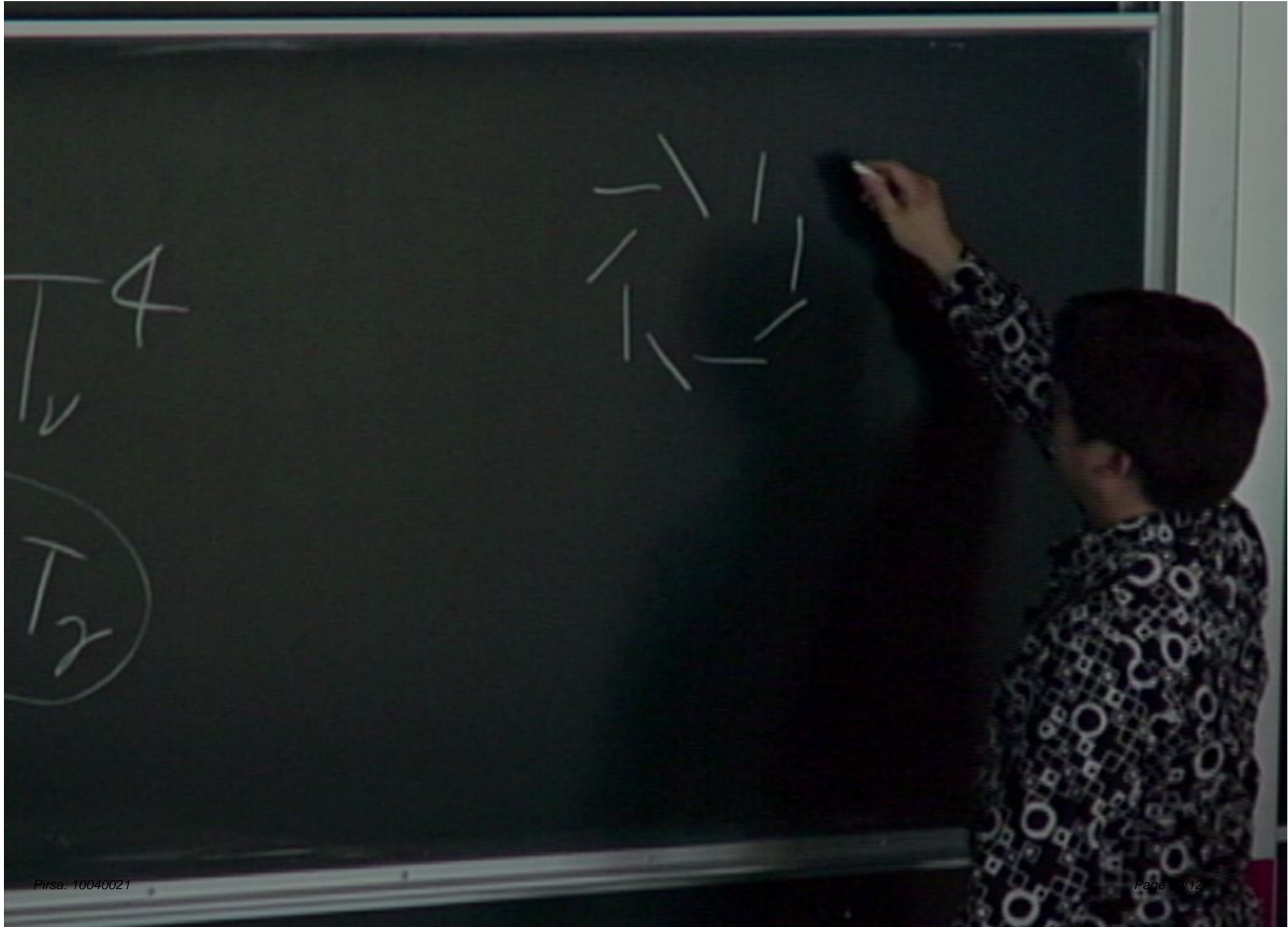


# Probing Parity Violation

- Cosmological parity violation (“birefringence,” Carroll 1998; Lue et al. 1999) may rotate the polarization plane by an angle  $\Delta\alpha$ , and convert E modes to B modes:

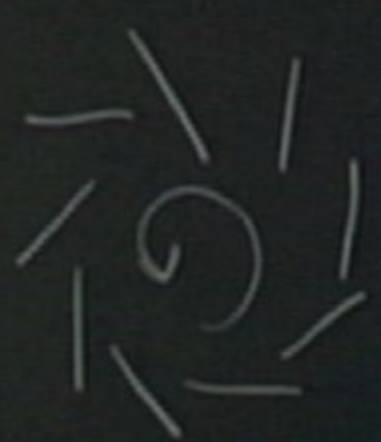
$$C_l^{\text{TB,obs}} = C_l^{\text{TE}} \sin(2\Delta\alpha)$$

- Non-detection of  $U_r$  gives  $\Delta\alpha = 1 \pm 3$  deg (68%CL)
- The full analysis using  $C_l^{\text{TB}}$  (as well as  $C_l^{\text{EB}}$ ) gives
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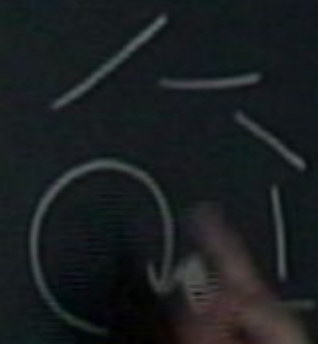


$T_4$

$T_2$



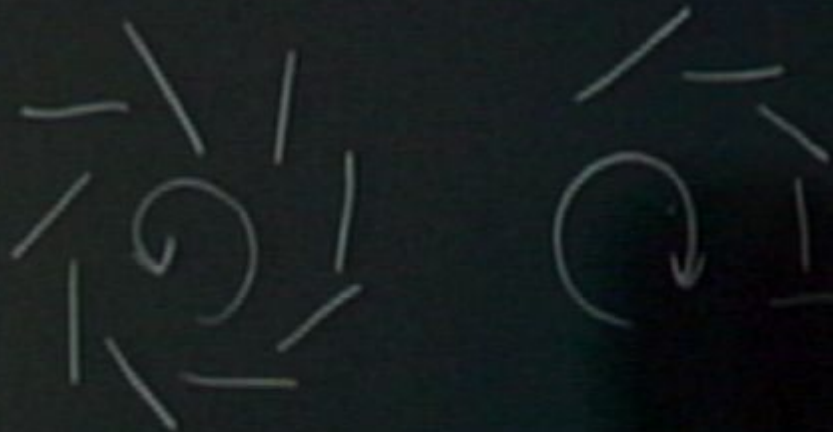
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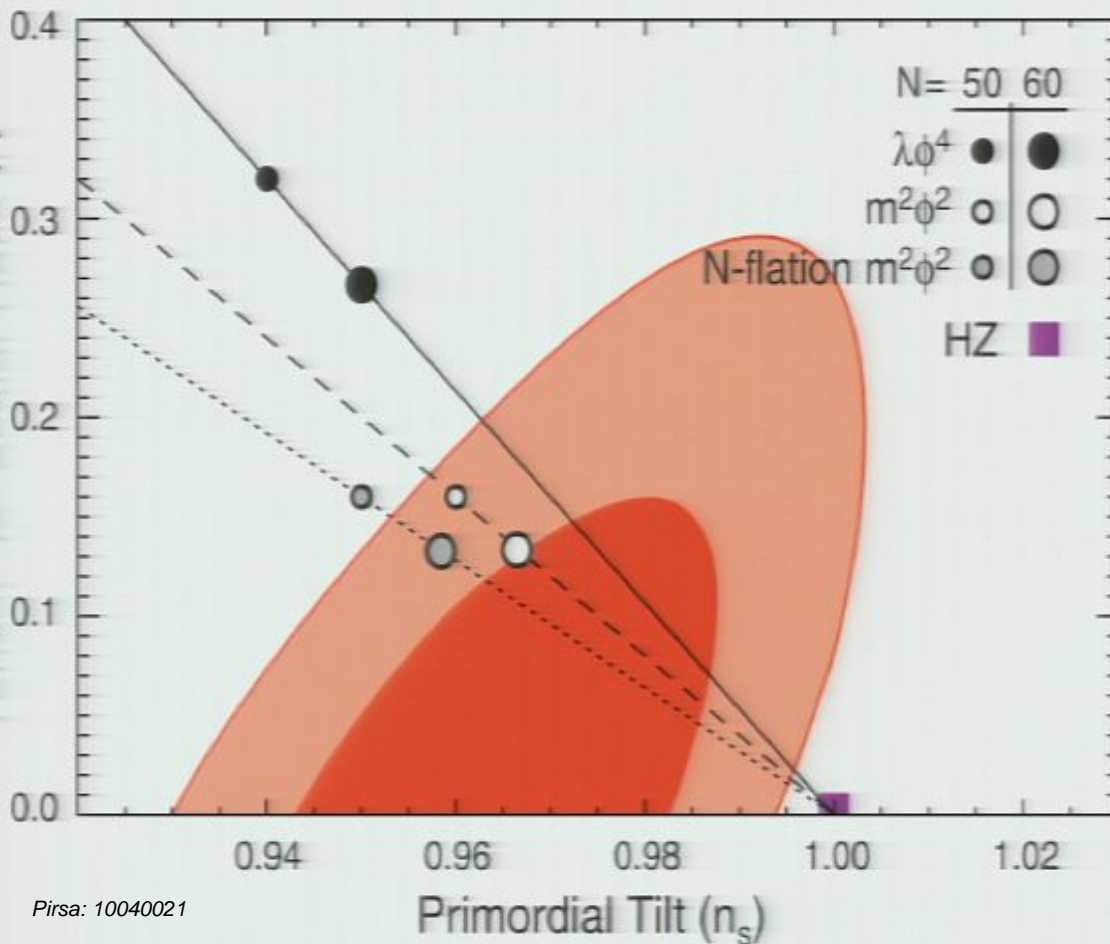
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# Probing Inflation (Power Spectrum)



- Joint constraint on the primordial tilt,  $n_s$ , and the tensor-to-scalar ratio,  $r$ .
- Not so different from the 5-year limit.
- $r < 0.24$  (95%CL; w/o SN)
- $r < 0.20$  (95%CL; w/ SN)



# Probing Inflation (Bispectrum)

- No detection of 3-point functions of primordial curvature perturbations. The 95% CL limits are:
  - $-10 < f_{\text{NL}}^{\text{local}} < 74$
  - $-214 < f_{\text{NL}}^{\text{equilateral}} < 266$
  - $-410 < f_{\text{NL}}^{\text{orthogonal}} < 6$
- The WMAP data are consistent with the prediction of **simple single-inflation inflation** models:
  - $1 - n_s \approx r \approx f_{\text{NL}}^{\text{local}}, f_{\text{NL}}^{\text{equilateral}} = 0 = f_{\text{NL}}^{\text{orthogonal}}$ .

Zel'dovich & Sunyaev (1969); Sunyaev & Zel'dovich (1972)

# Sunyaev–Zel'dovich Effect

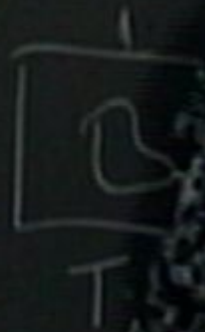
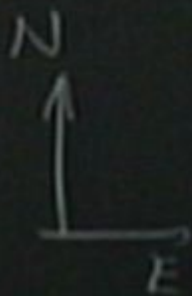


Hot gas with the  
electron temperature of  $T_e \gg T_{\text{cmb}}$

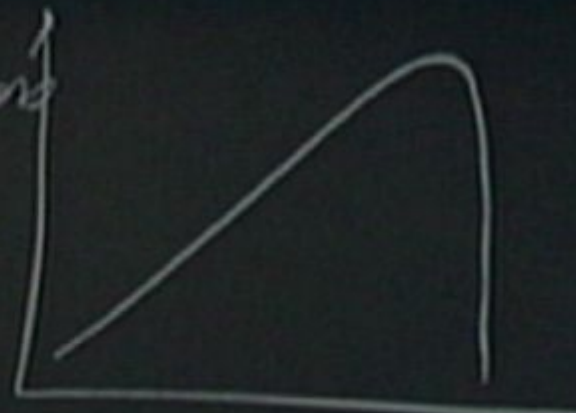
- $\Delta T/T_{\text{cmb}} = g_V \mathbf{y}$

$$\begin{aligned} y &= (\text{optical depth of gas}) k_B T_e / (m_e c^2) \\ &= [\sigma_T / (m_e c^2)] \int n_e k_B T_e d(\text{los}) \\ &= [\sigma_T / (m_e c^2)] \int (\text{electron pressure}) d(\text{los}) \end{aligned}$$

$$g_V = -2 \quad (v=0); \quad -1.91, -1.81 \text{ and } -1.56 \text{ at } v=41, 61 \text{ and } 94 \text{ GHz}$$

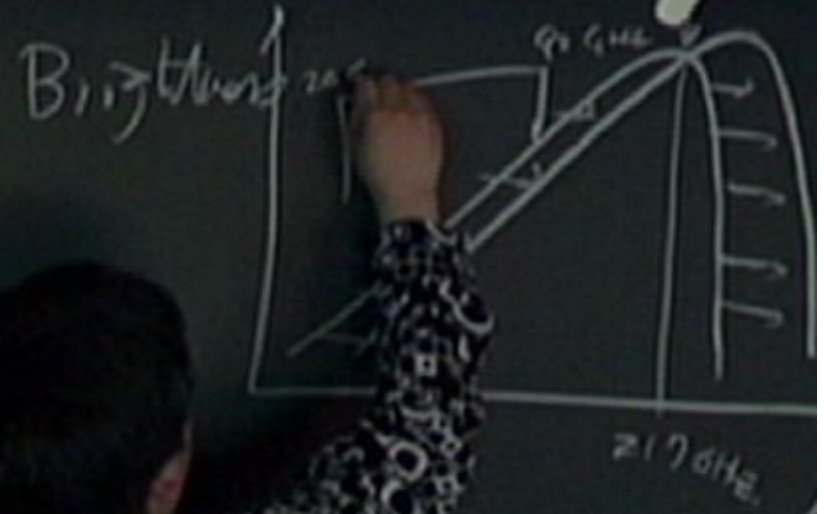
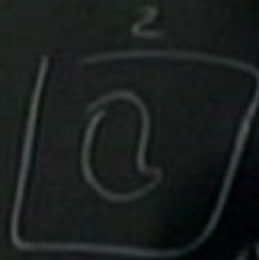
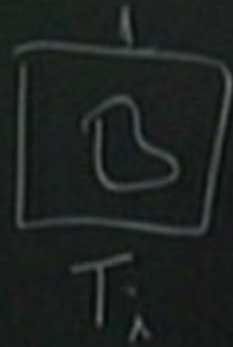
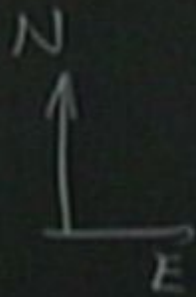


Brightness

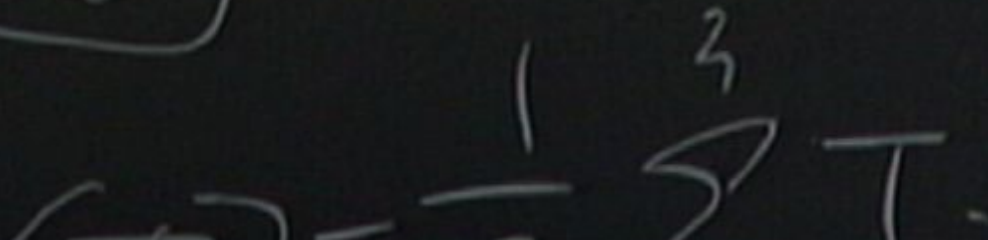
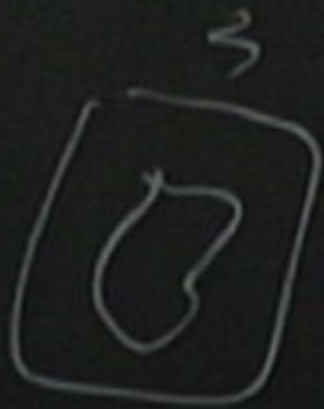
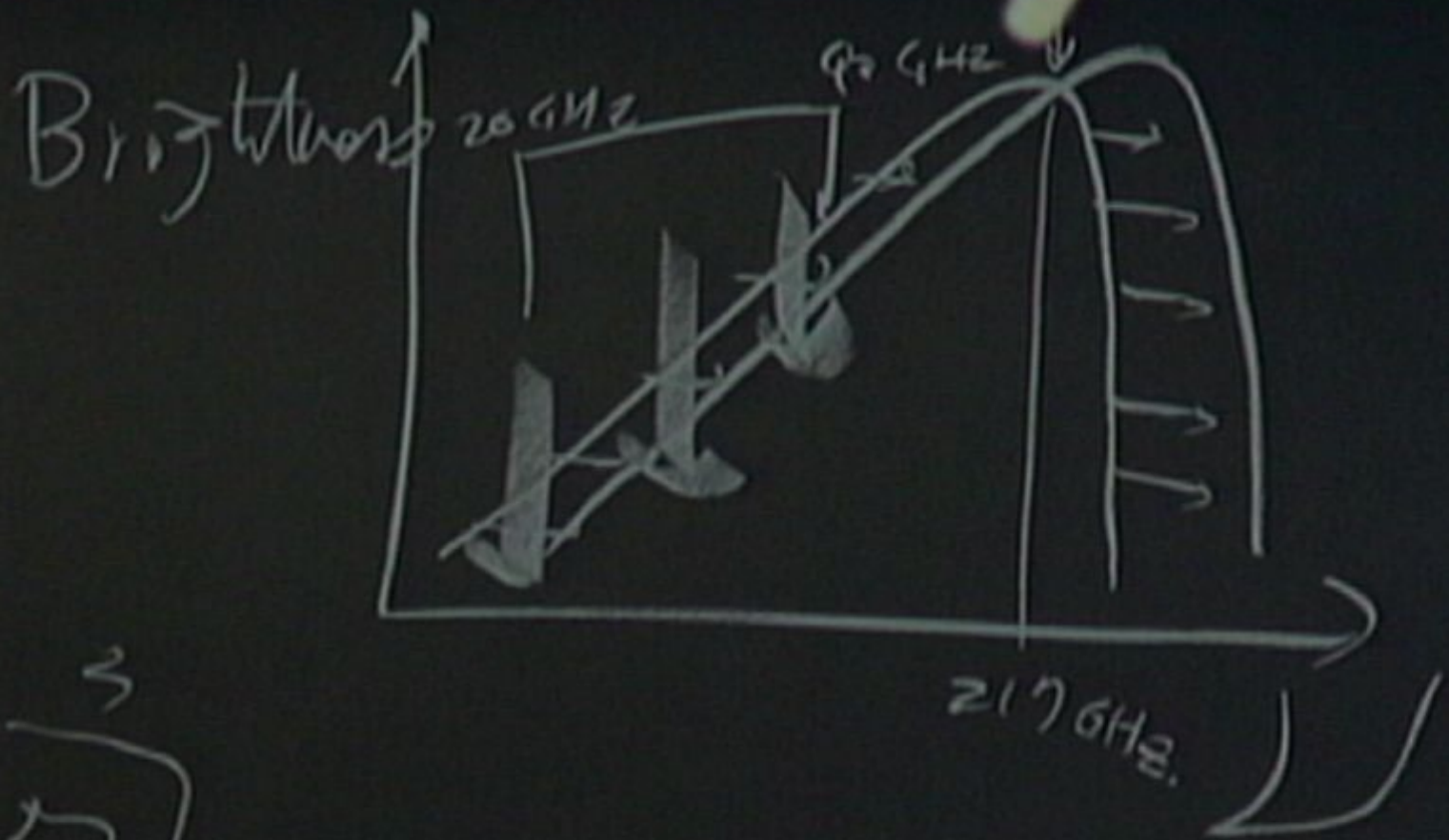


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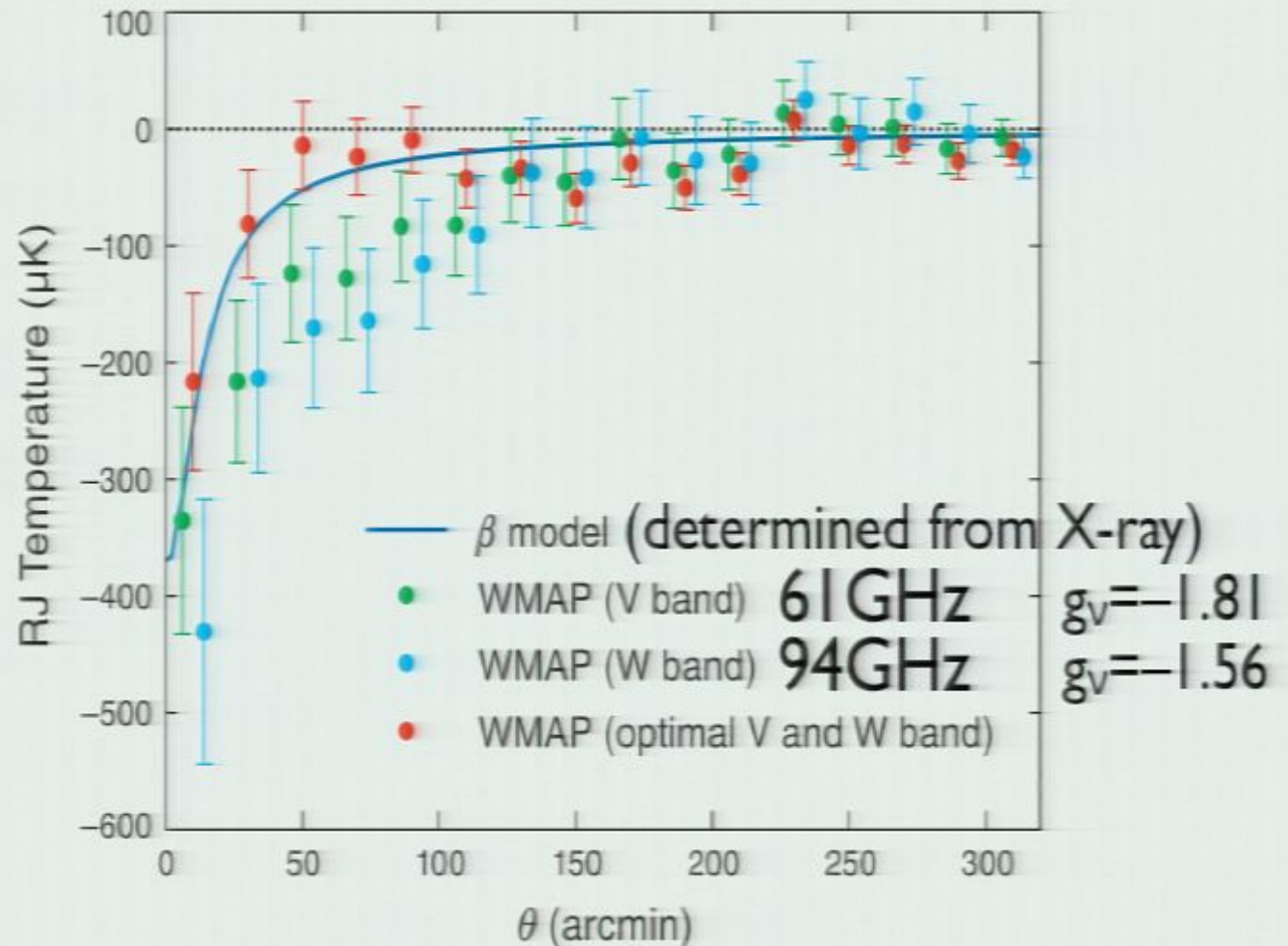
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# Coma Cluster ( $z=0.023$ )

We find that the CMB fluctuation in the direction of Coma is  $\approx -100\mu\text{K}$ . (This is a new result!)

$$y_{\text{coma}}(0) = (7 \pm 2) \times 10^{-5} \quad (68\% \text{CL})$$



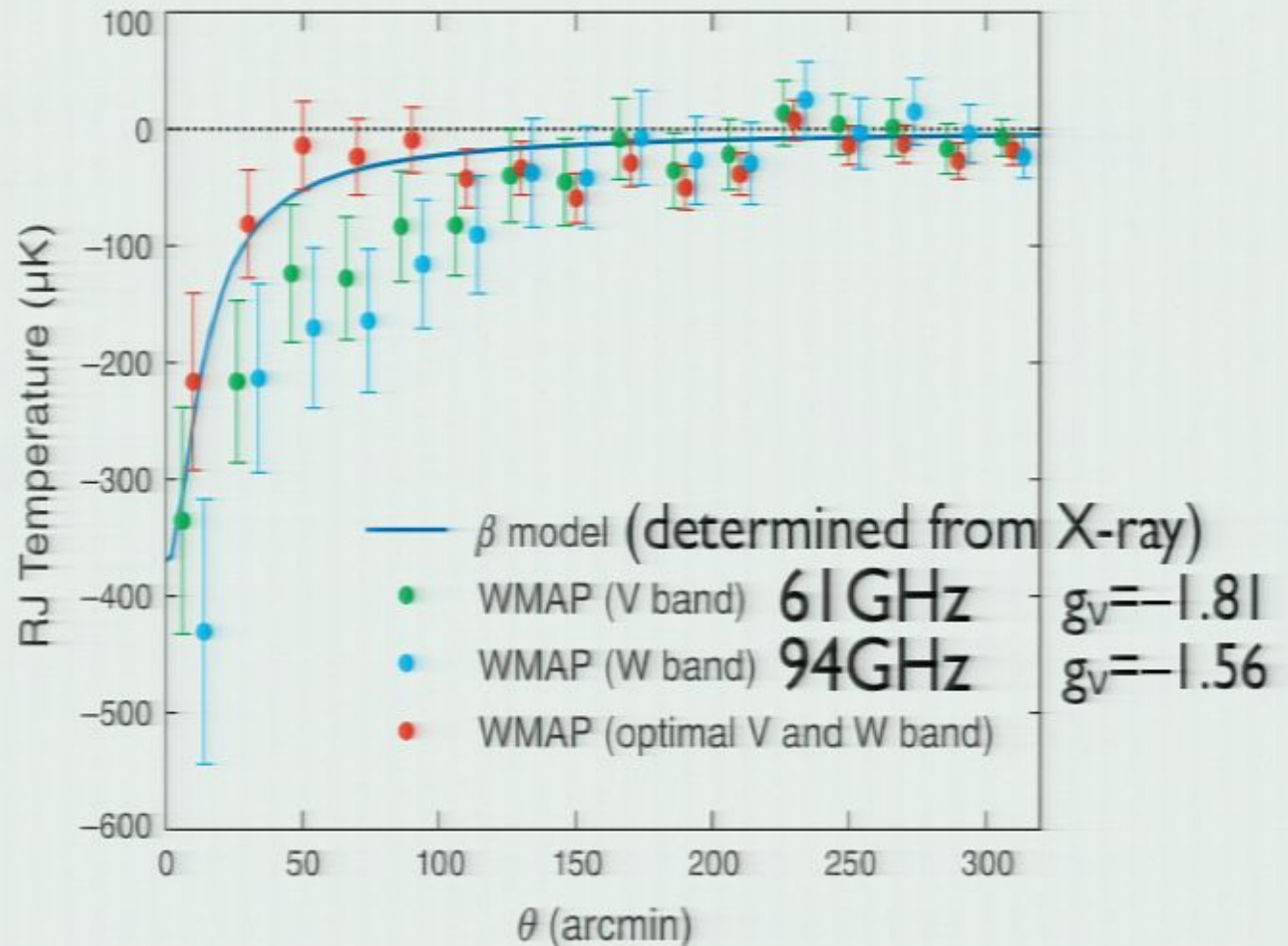
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# A Question

- Are we detecting the **expected** amount of electron pressure,  $P_e$ , in the SZ effect?
- Expected from X-ray observations.
- Expected from theory.

# Three approaches

- 1. Compare the WMAP data and X-ray data on individual clusters individually.
- But, not all clusters are detected individually by the WMAP data...
- 2. Compare the stacked WMAP data and the expected average X-ray profiles.
- Systematic effects in the stacking analysis must be carefully studied.
- 3. Compare the stacked WMAP data and the expected profiles from theory (hydro simulation etc).



# Arnaud et al. Profile

- A fitting formula for the average electron pressure profile as a function of the cluster mass ( $M_{500}$ ), derived from 33 nearby ( $z < 0.2$ ) clusters.

# Three approaches

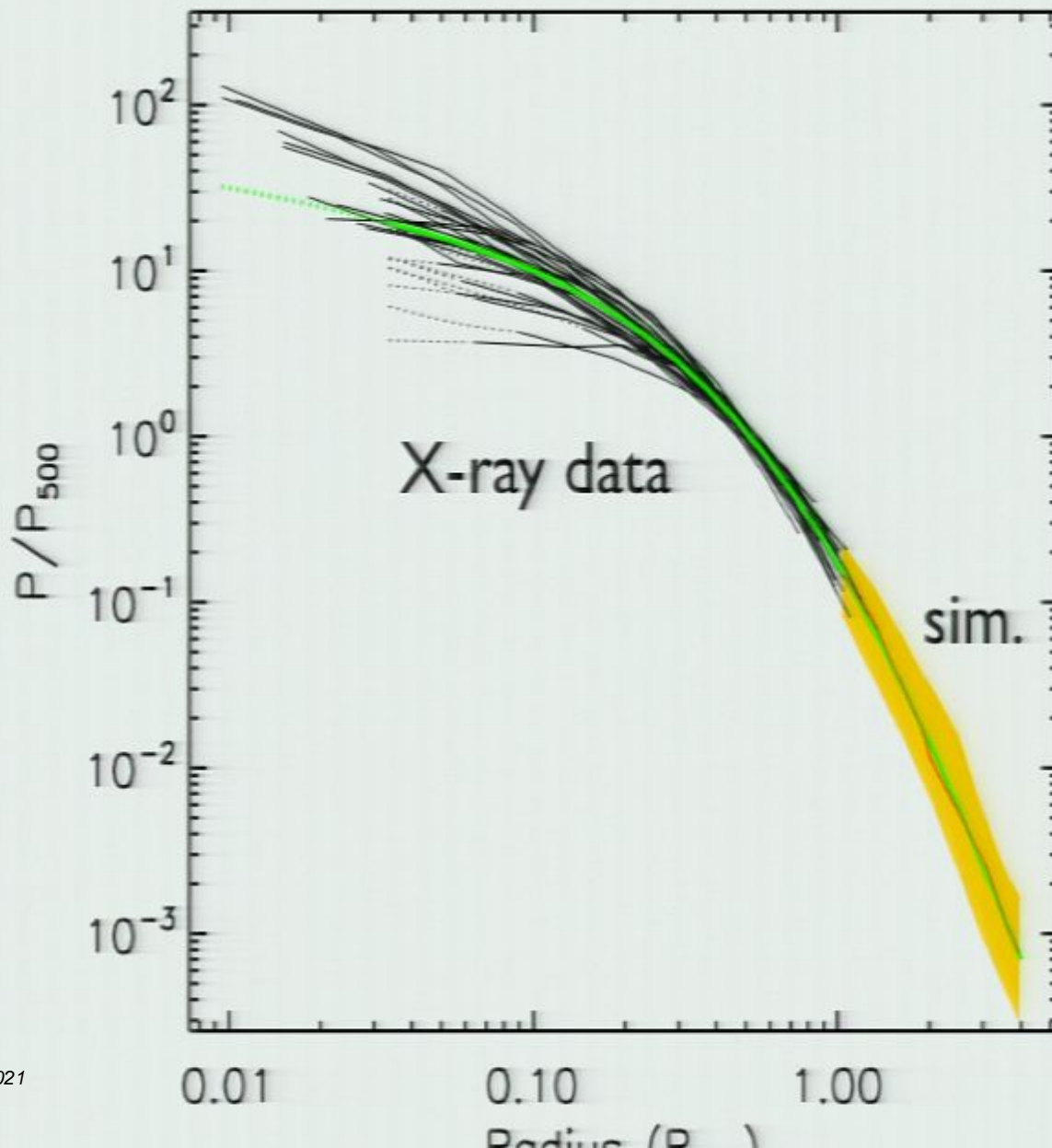
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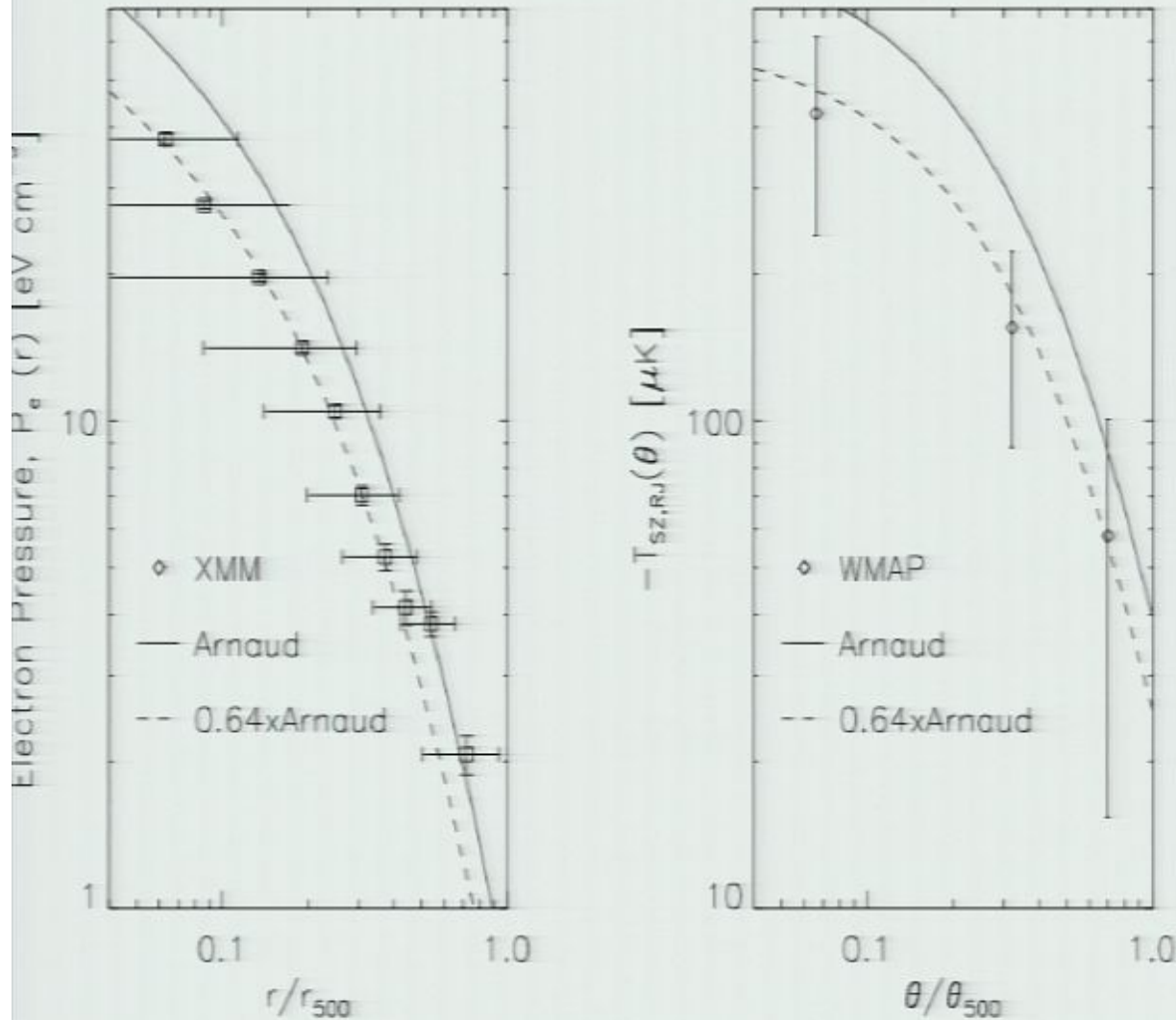


# Arnaud et al. Profile



- A significant scatter exists at  $R < 0.2R_{500}$ , but a good convergence in the outer part.

# Coma Data vs Arnaud



- $M_{500} = 6.6 \times 10^{14} h^{-1} M_{\text{sun}}$  is estimated from the mass-temperature relation (Vikhlinin et al.)

- $T_X^{\text{coma}} = 8.4 \text{ keV}$ .

- Arnaud et al.'s profile overestimates both the direct X-ray data and WMAP data by the same factor (0.64)!

- To reconcile them,  $T_X^{\text{coma}} = 6.5 \text{ keV}$  is required, but that is way too low.

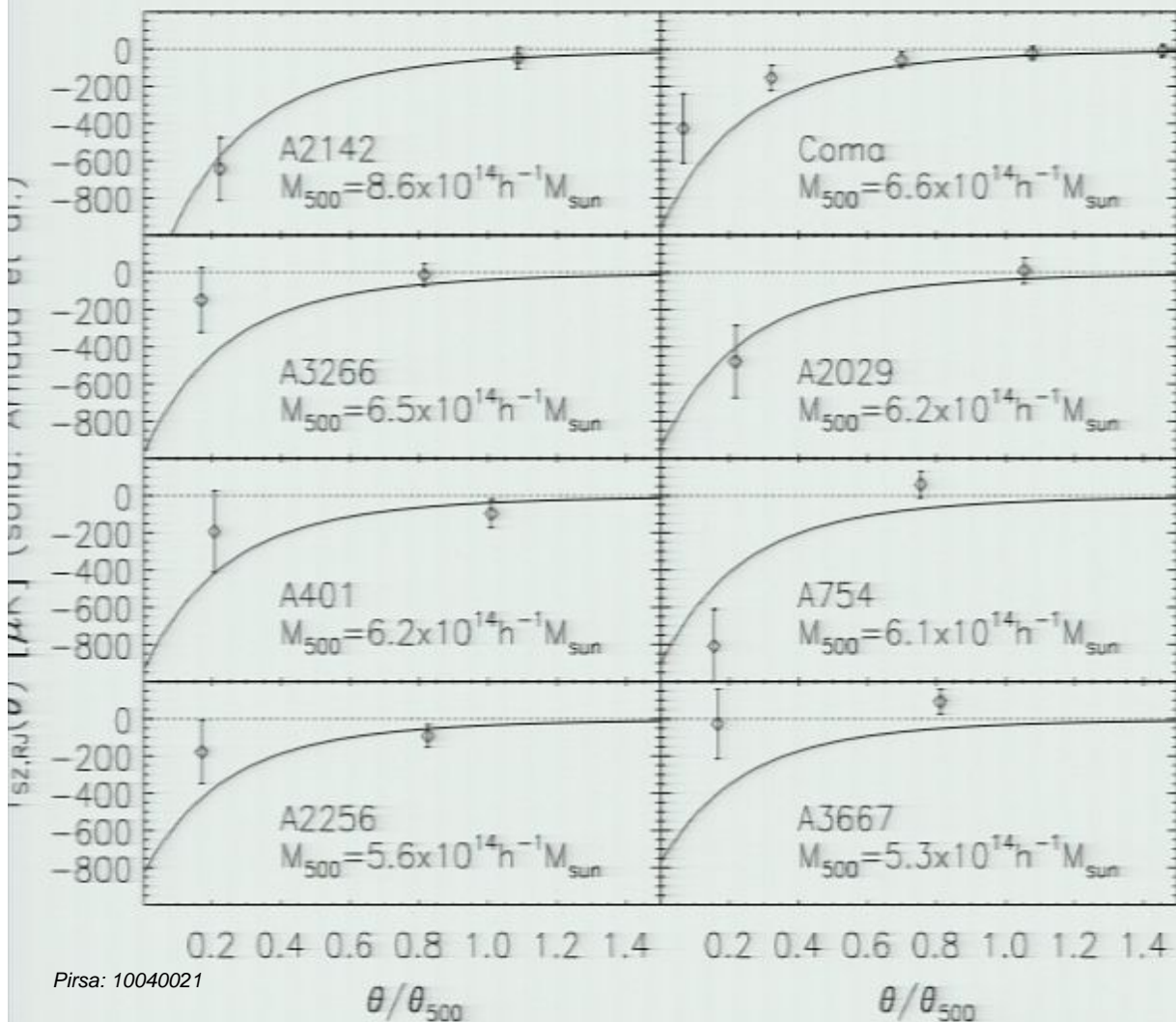
The X-ray data (XMM) are provided by A. Finoguenov.

# Well...

- That's just one cluster. What about the other clusters?
- We measure the SZ effect of a very nice sample of well-studied nearby clusters compiled by Vikhlinin et al.

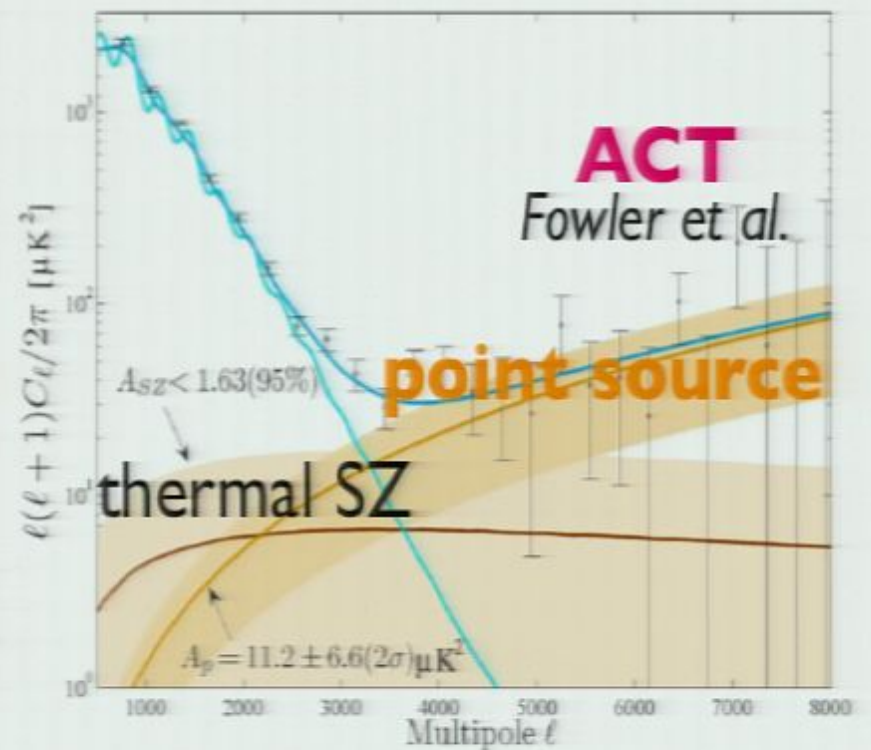
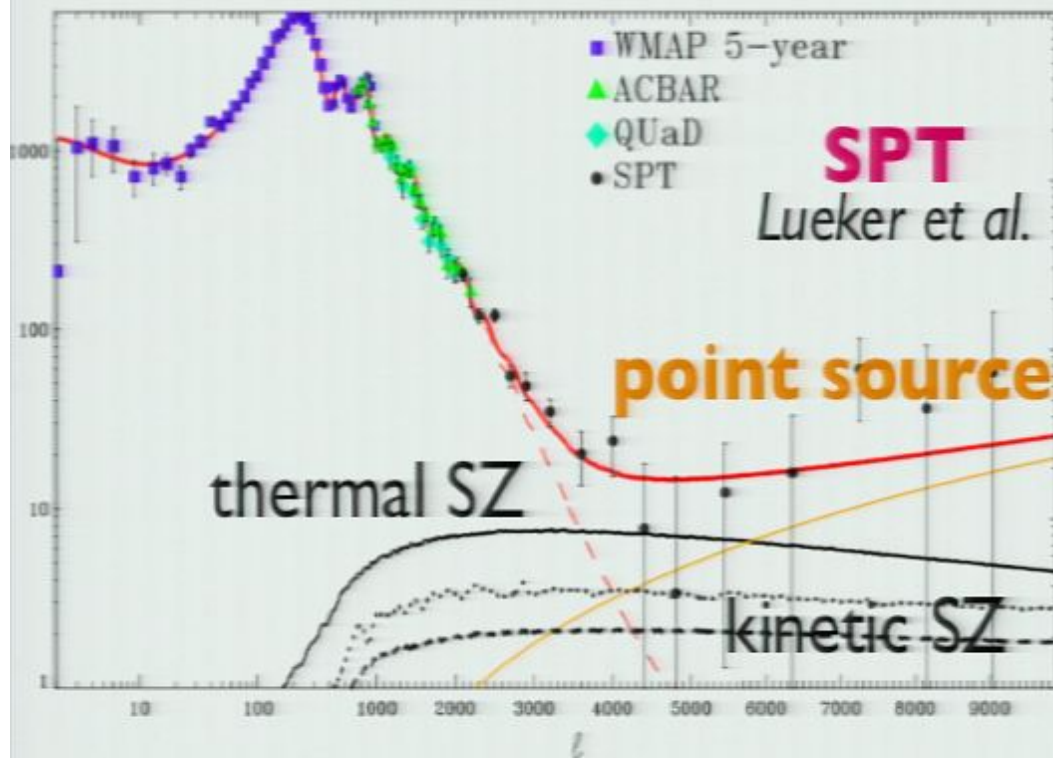


# New results! (Prelim.)



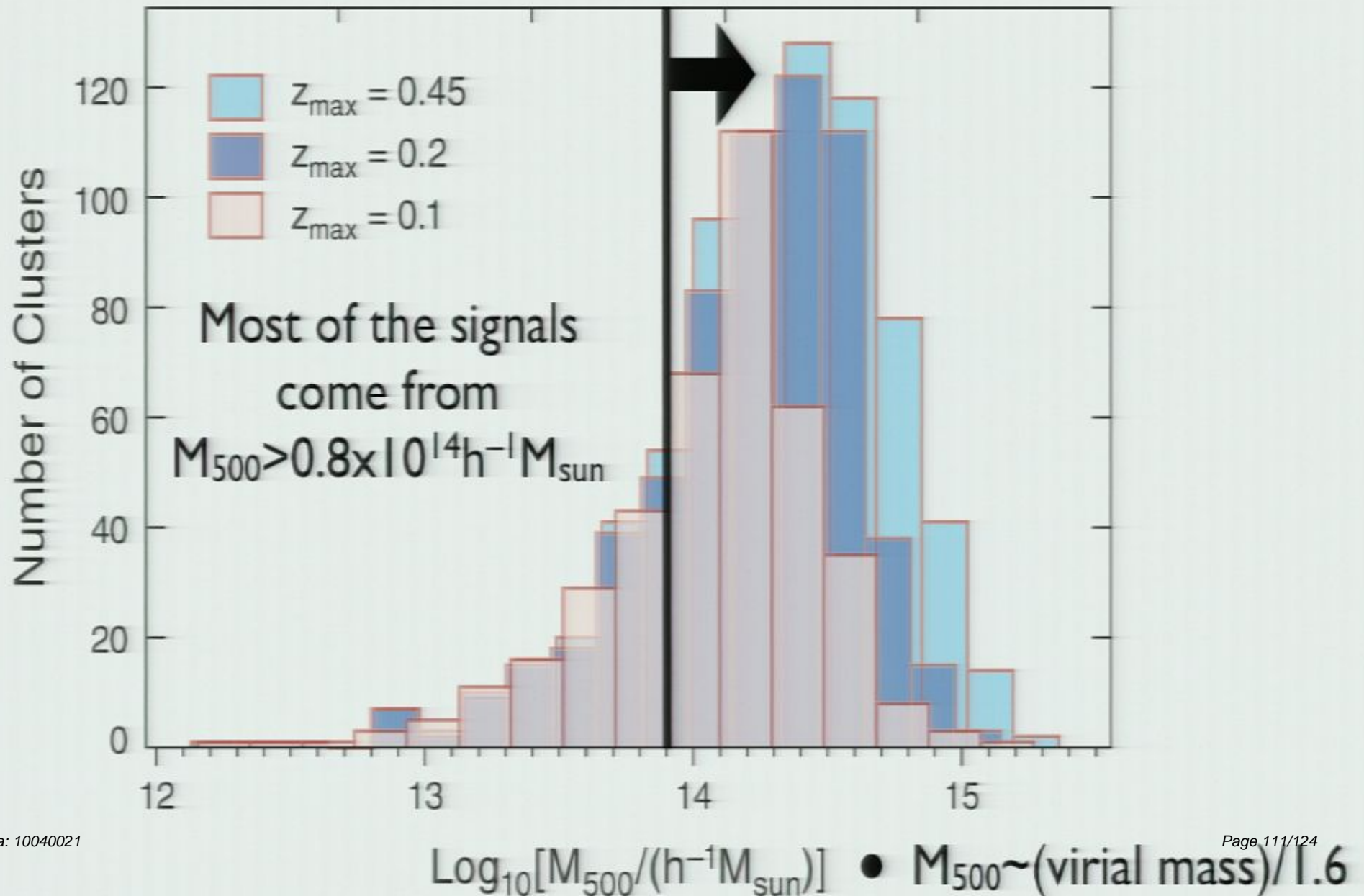
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# Small-scale CMB Data



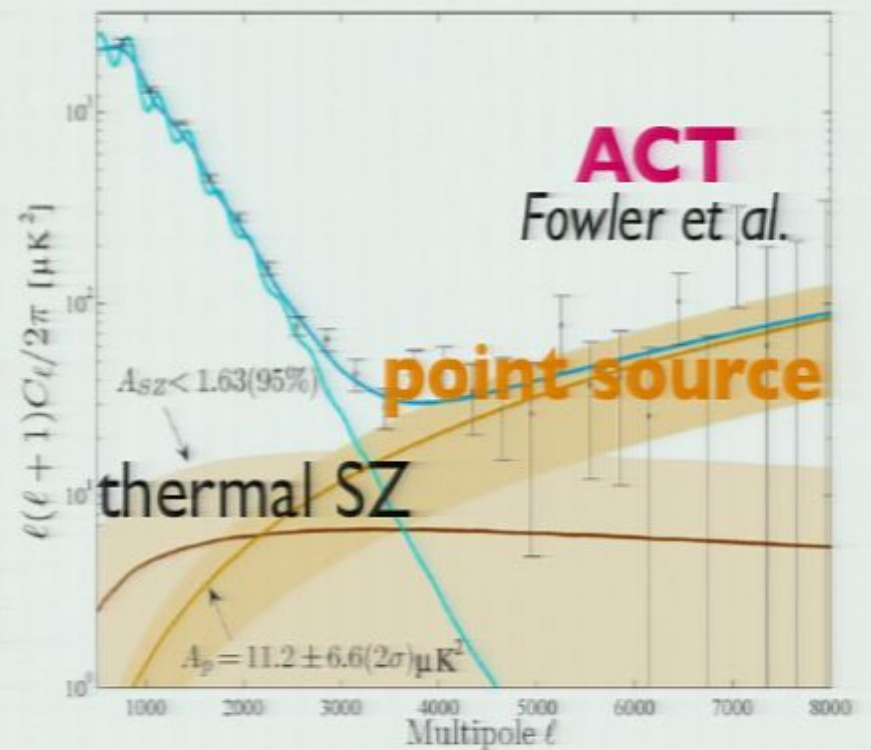
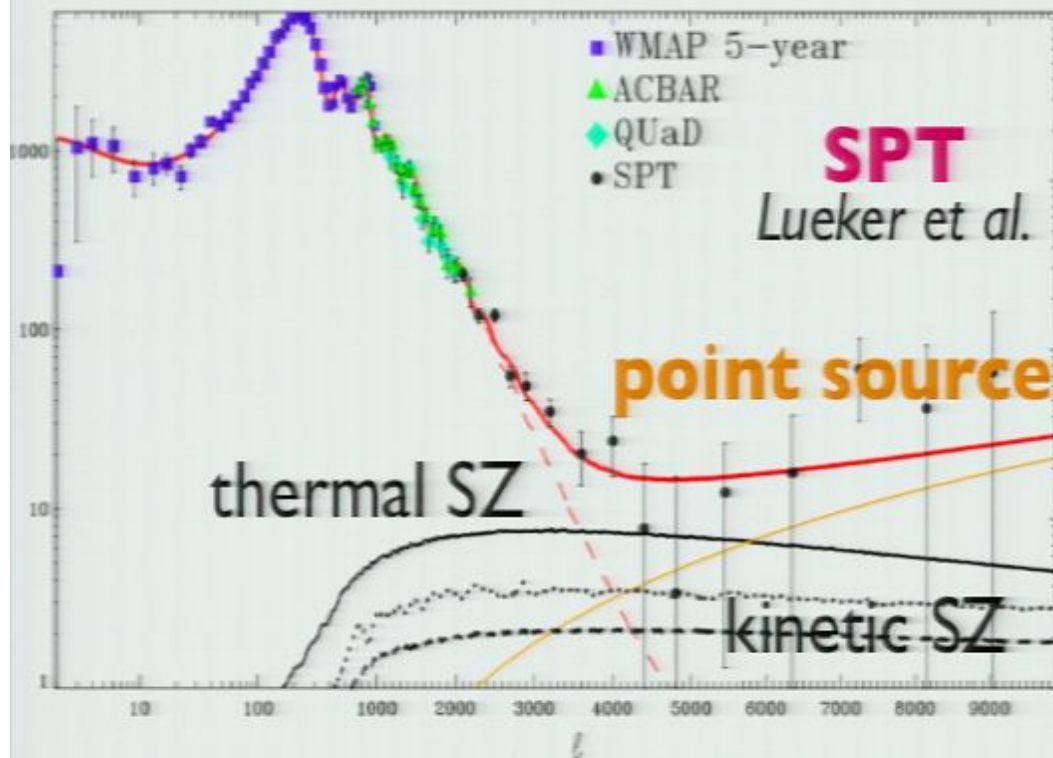
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# Mass Distribution





# Small-scale CMB Data



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# Lower $A_{SZ}$ : Two Possibilities

$$C_l = g_\nu^2 \int_0^{z_{\max}} dz \frac{dV}{dz} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} |\tilde{y}_l(M, z)|^2$$

→  $\frac{l(l+1)C_l}{2\pi} \simeq 330 \mu\text{K}^2 \sigma_8^7 \left(\frac{\Omega_b h}{0.035}\right)^2 \times [\text{gas pressure}]$

- The SZ power spectrum is sensitive to the number of clusters (i.e.,  $\sigma_8$ ) and the pressure of individual clusters.
- Lower SZ power spectrum can imply:
  - $\sigma_8$  is 0.77 (rather than 0.8):  $\sum m_\nu \sim 0.2\text{eV}$ ?
  - Gas pressure per cluster is lower than expected

→ **WMAP measurement favors this possibility.**

# Size-Luminosity Relations

- To calculate the expected pressure profile for each cluster, we need to know the size of the cluster,  $r_{500}$ .
- This needs to be derived from the observed properties of X-ray clusters.
- The best quantity is the gas mass times temperature, but this is available only for a small subset of clusters.
- We use  $r_{500}$ - $L_X$  relation (Boehringer et al.):

$$r_{500} = \frac{(0.753 \pm 0.063) h^{-1} \text{ Mpc}}{E(z)}$$

**Uncertainty in this relation is the major source of sys. error.**

$$\times \left( \frac{L_X}{10^{44} h^{-2} \text{ erg s}^{-1}} \right)^{0.228 \pm 0.015}$$

$$E(z) \equiv H(z)/H_0 = \left[ \Omega_m (1+z)^3 + \Omega_\Lambda \right]^{1/2}$$



# Summary

- Significant improvements in the **high-l temperature** data, and the **polarization data at all multipoles**.
- High-l temperature:  $n_s < 1$ , detection of helium, improved limits on neutrino properties.
- Polarization: polarization on the sky!
  - Polarization-only limit on  $r$ :  $r < 0.93$  (95%CL).
  - All data included:  $r < 0.24$  (95%CL; w/o SN)
  - $\Delta\alpha = -1.1 \pm 1.3$ (statistical)  $\pm 1.5$ (systematic) deg.

# Puzzle?

- SZ effect: Coma's radial profile is measured, several massive clusters are detected, and the statistical detection reaches  $8\sigma$ .
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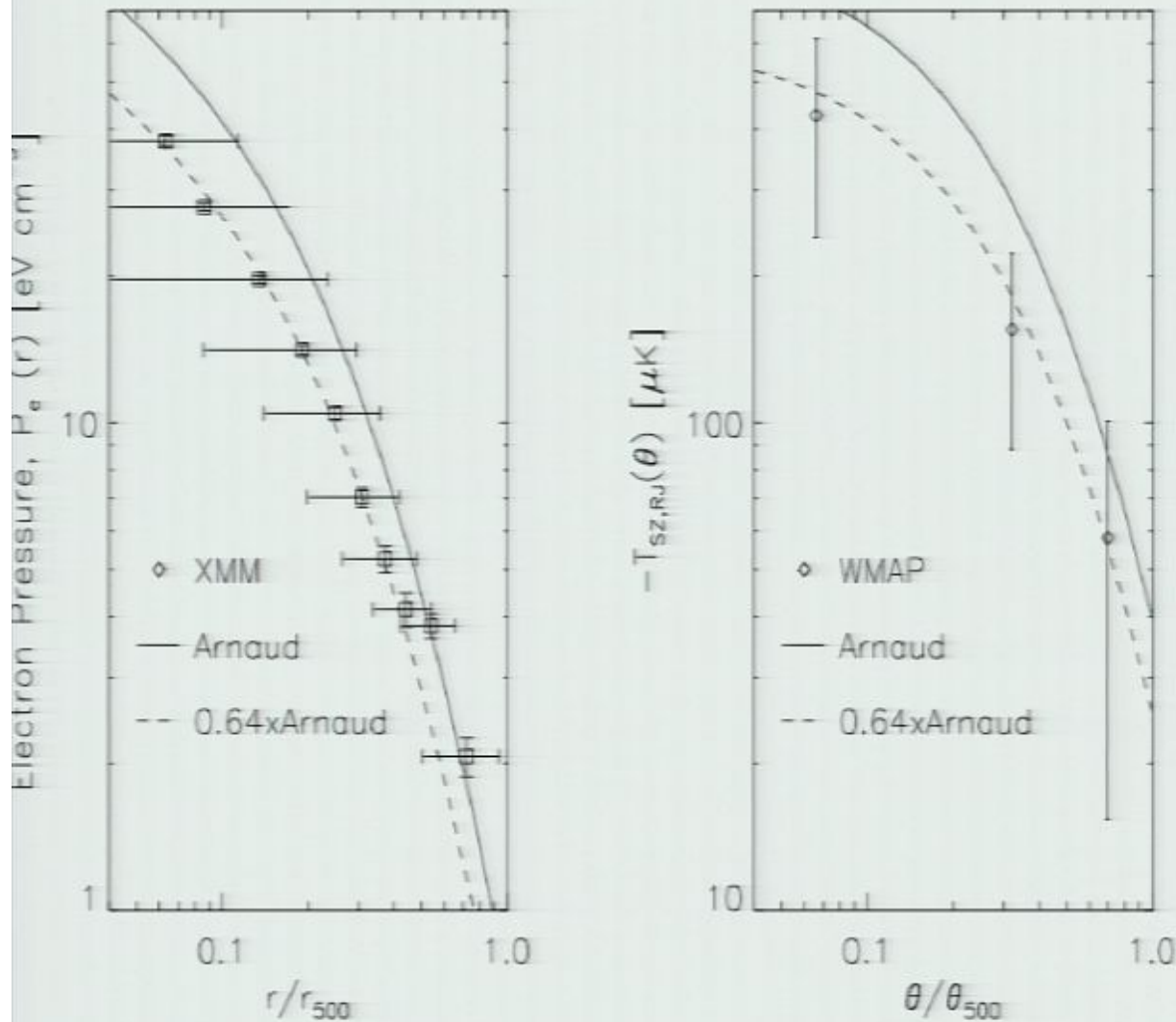
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# Well...

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# Coma Data vs Arnaud



- $M_{500} = 6.6 \times 10^{14} h^{-1} M_{\text{sun}}$  is estimated from the mass-temperature relation (Vikhlinin et al.)

- $T_X^{\text{coma}} = 8.4 \text{ keV}$ .

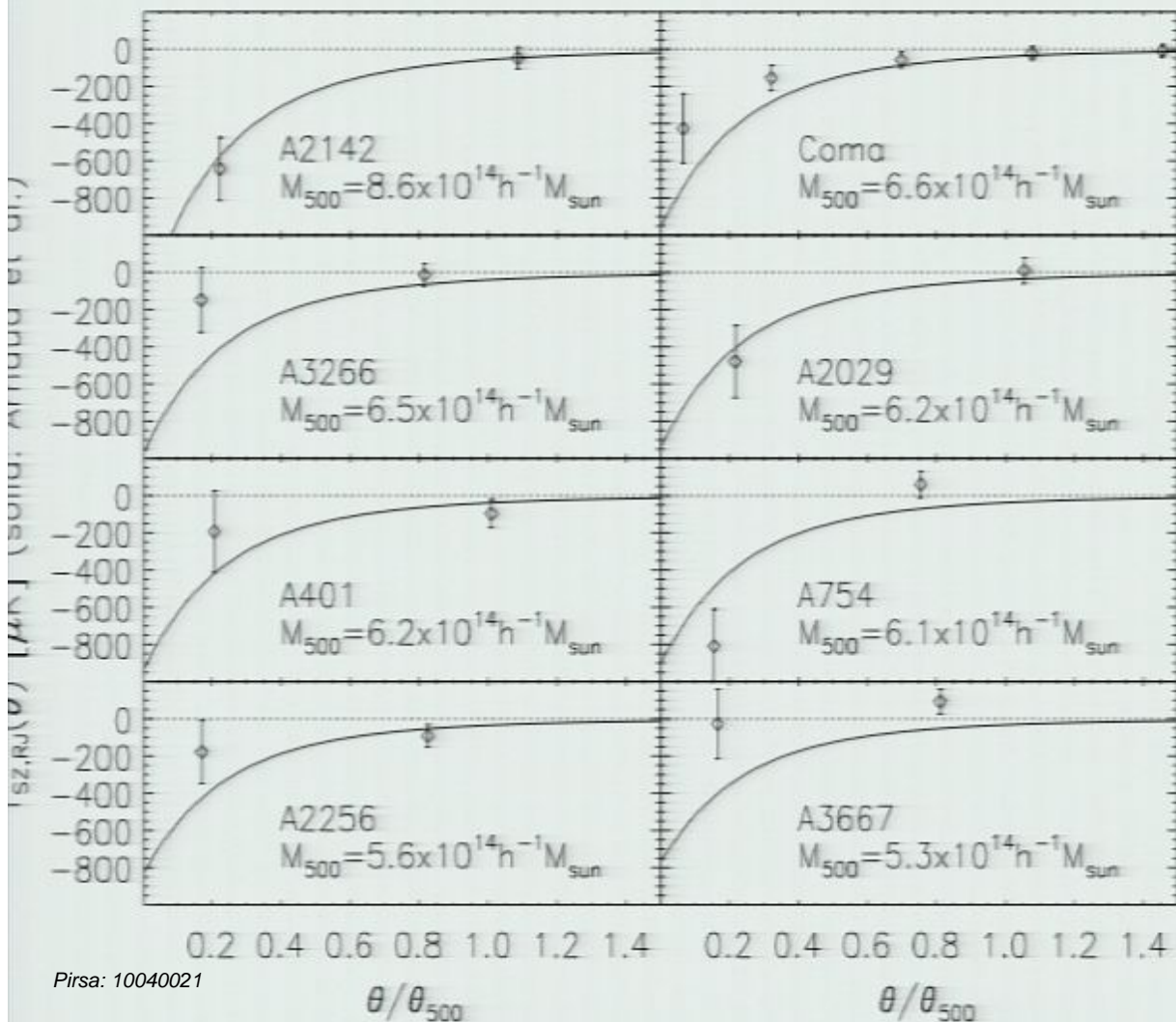
- Arnaud et al.'s profile overestimates both the direct X-ray data and WMAP data by the same factor (0.64)!

- To reconcile them,  $T_X^{\text{coma}} = 6.5 \text{ keV}$  is required, but that is way too low.

The X-ray data (XMM) are provided by A. Finoguenov.



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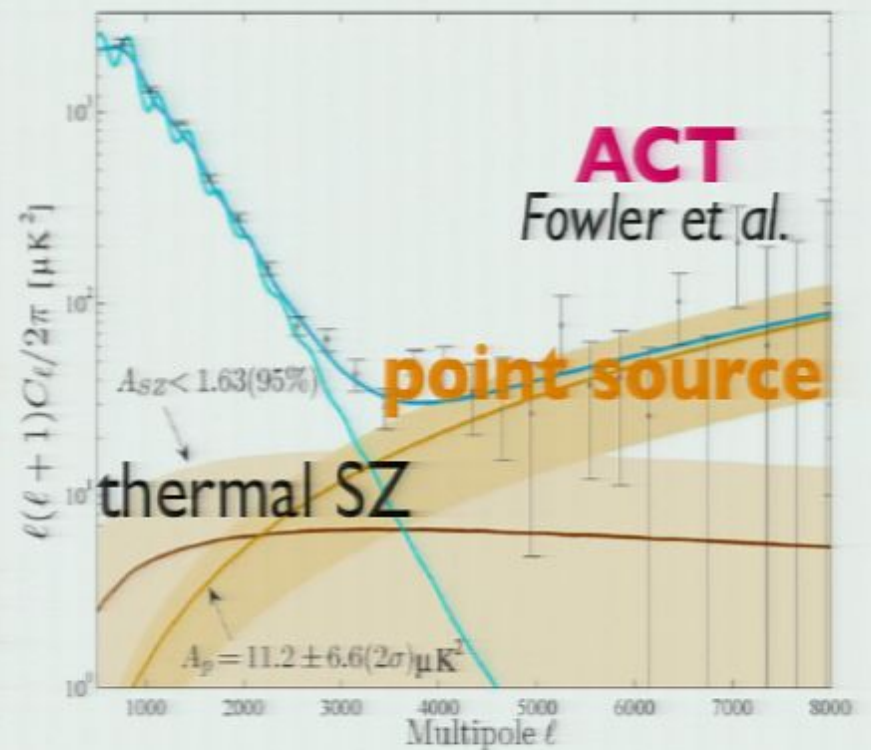
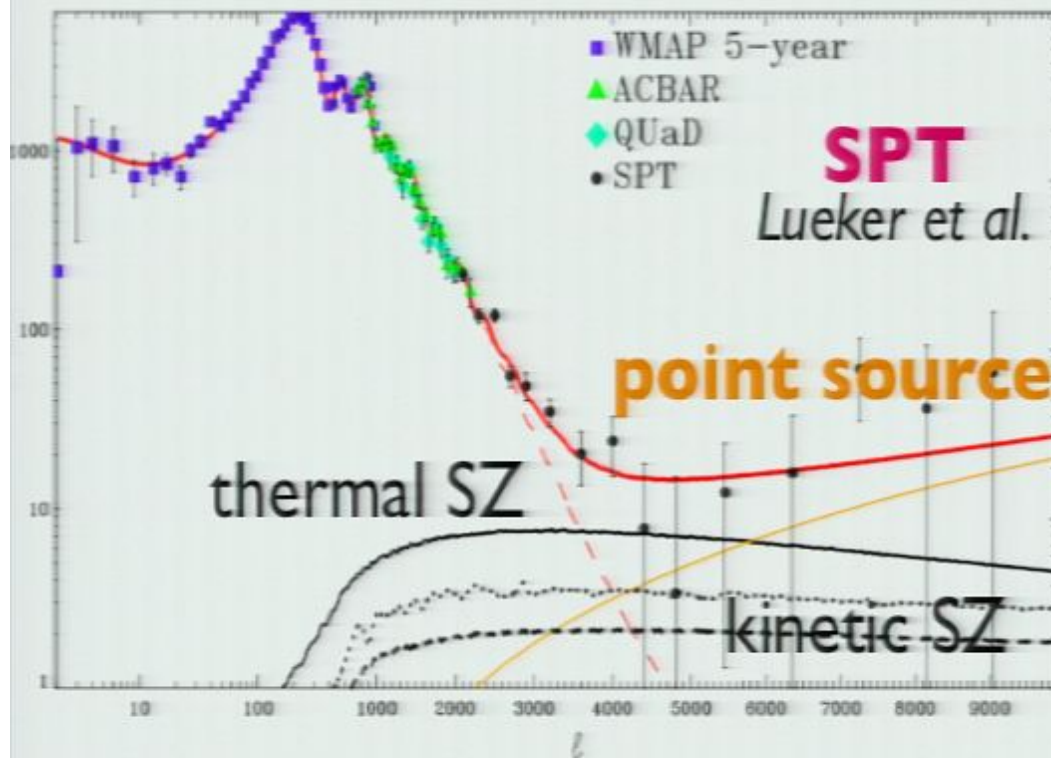
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