

Title: Standard Model - Review (PHYS 622) - Lecture 15

Date: Dec 18, 2009 09:00 AM

URL: <http://pirsa.org/09120049>

Abstract:



perimeter scholars  
INTERNATIONAL

Higgs boson

$\phi(x)$

Higgs boson

$\phi(x)$

$V(\phi)$

Higgs boson

$$\phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

$V(\phi)$

## Higgs boson

$$\phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h(x) \end{pmatrix}$$

$$V(\phi)$$

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

$$v = \left| \frac{\mu^2}{\lambda} \right|^{\frac{1}{2}}$$

$$V(h) = -\frac{\mu^2 v^2}{2} + \mu^2 h^2 + \dots$$

## Higgs boson

$$\phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h(x) \end{pmatrix}$$

$$V(\phi)$$

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

$$v = \left| \frac{\mu^2}{\lambda} \right|^{\frac{1}{2}}$$

$$V(h) = -\frac{\mu^2 v^2}{2} + \mu^2 h^2 + \dots$$

$$m_h^2 = 2\mu^2$$

## Higgs boson

$$\phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h(x) \end{pmatrix}$$

$$V(\phi)$$

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

$$v = \left| \frac{\mu^2}{\lambda} \right|^{\frac{1}{2}}$$

$$V(h) = -\frac{\mu^2 v^2}{2} + \mu^2 h^2 + \dots$$

$$m_h^2 = 2\mu^2$$



$$\lambda = \frac{1}{2} \frac{m_H^2}{v^2}$$

$$\frac{\lambda}{4\pi} = \frac{m_H^2}{8\pi v^2}$$

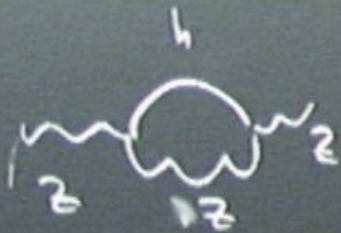
$$\sim 1 \quad \text{when } m_H = 1200 \text{ GeV}$$

$$a = \frac{1}{2} \frac{m_H^2}{v^2}$$

$$\frac{a}{4\pi} = \frac{m_H^2}{8\pi v^2}$$

$$\sim 1 \text{ when } m_H = 1200 \text{ GeV}$$

$$m_H < 180 \text{ GeV}$$



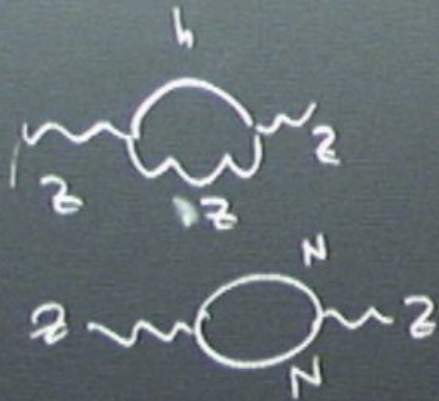
$$\frac{\alpha_W}{4\pi} m_Z^2 \sim \frac{m_H^2}{m_Z^2}$$



$$a = \frac{1}{2} \frac{m_H^2}{v^2}$$

$$\frac{a}{4\pi} = \frac{m_H^2}{8\pi v^2}$$

$$\sim 1 \text{ when } m_H = 1200 \text{ GeV}$$

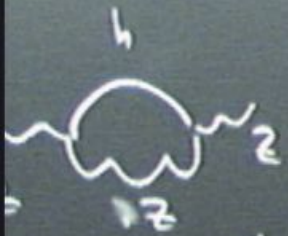


$$\frac{\alpha_s}{4\pi} m_q^2 \sim \frac{m_H^2}{m_q^2}$$

$$m_H < 180 \text{ GeV}$$

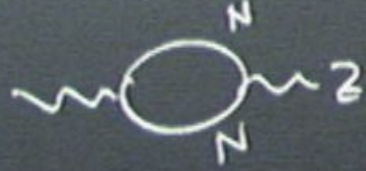
$$= \frac{1}{2} \frac{m_H^2}{v^2}$$

$$\frac{c/v^2}{4\pi} = \frac{m_H^2}{8\pi v^2} \sim 1 \text{ when } m_H = 1,200 \text{ GeV}$$



$$\frac{\alpha}{4\pi} \frac{m_Z^2}{m^2} \sim \frac{m_H^2}{m_Z^2}$$

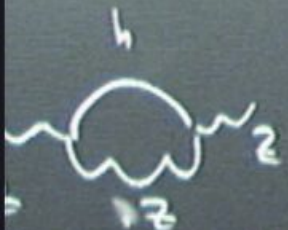
$$m_H < 180 \text{ GeV}$$



$$\mathcal{L} = + g^2 (v+h)^2 W_\mu^+ W^{-\mu} + \frac{1}{2} (g^2 + g'^2) (v+h)^2 Z_\mu Z^\mu - \frac{\partial_\mu h \partial^\mu h}{\sqrt{2}} (v+h) \bar{f} f$$

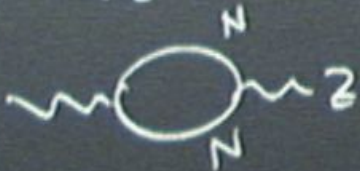
$$= \frac{1}{2} \frac{m_H^2}{v^2}$$

$$\frac{c/v^2}{4\pi} = \frac{m_H^2}{8\pi v^2} \sim 1 \text{ when } m_H = 1200 \text{ GeV}$$

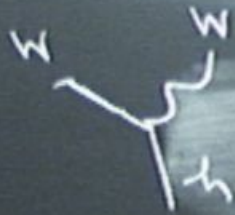


$$\frac{\alpha_W}{4\pi} m_Z^2 \log \frac{m_H^2}{m_Z^2}$$

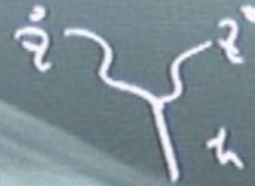
$$m_H < 180 \text{ GeV}$$



$$\mathcal{L} = + g^2 (v+h)^2 W_\mu^+ W^{\mu-} + \frac{1}{2} (g^2 + g'^2) (v+h)^2 Z_\mu Z^\mu - \frac{g_f}{\sqrt{2}} (v+h) \bar{f} f + \text{kinetic} + \text{mixing}$$



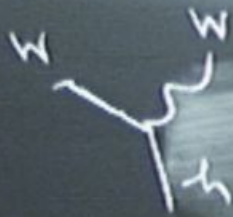
$$= i \frac{m_W^2}{2} g^{WV}$$



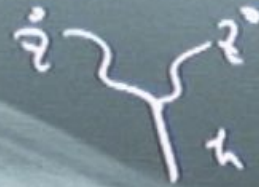
$$= 2i \frac{m_Z^2}{v} g^{WV}$$



$$= -i \frac{m_f}{v}$$



$$= 2i \frac{m_h^2}{2} g_W^2$$



$$= 2i \frac{m_h^2}{4} g_W^2$$



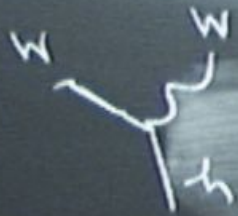
$$= -i \frac{m_f}{v}$$

$$I(h \rightarrow W^+ W^-)$$

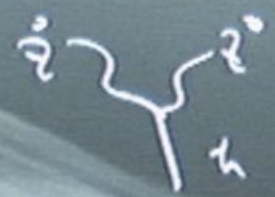
$$I(h \rightarrow z z)$$

$$= \frac{\alpha_W}{16} \frac{m_h^3}{m_W^2} \left( 1 - 4 \frac{m_h^2}{m_W^2} + 12 \frac{m_h^2}{m_W^2} \right) \left( 1 - \frac{4m_W^2}{m_h^2} \right)$$

$$= \frac{\alpha_W}{32} \frac{m_h^3}{m_W^2}$$



$$= 2i \frac{m_h^2}{2} g_W^2$$



$$= 2i \frac{m_h^2}{4} g_W^2$$



$$= -i \frac{m_f}{v}$$

$$I(h^0 \rightarrow W^+W^-)$$

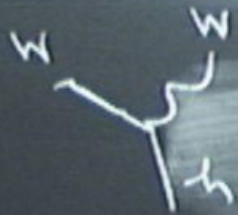
$$I(h^0 \rightarrow z^0z^0)$$

$$= \frac{\alpha_W}{16} \frac{m_h^3}{m_W^2} \left( 1 - 4 \frac{m_h^2}{m_Z^2} + 12 \frac{m_W^2}{m_{H^\pm}^2} \right) \left( 1 - \frac{4m_W^2}{m_h^2} \right)^{1/2}$$

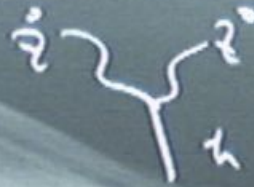
$$- \frac{\alpha_W}{32} \frac{m_h^3}{m_W^2} \left( 1 - 4 \frac{m_h^2}{m_Z^2} + 12 \frac{m_W^2}{m_{H^\pm}^2} \right) \left( 1 - \frac{4m_Z^2}{m_h^2} \right)^{1/2}$$

$$\alpha_W \frac{m_h^2}{m_W^2}$$





$$= 2i \frac{m_W^2}{s} g_W^2$$



$$= 2i \frac{m_Z^2}{s} g_W^2$$



$$= -i \frac{m_f}{s}$$

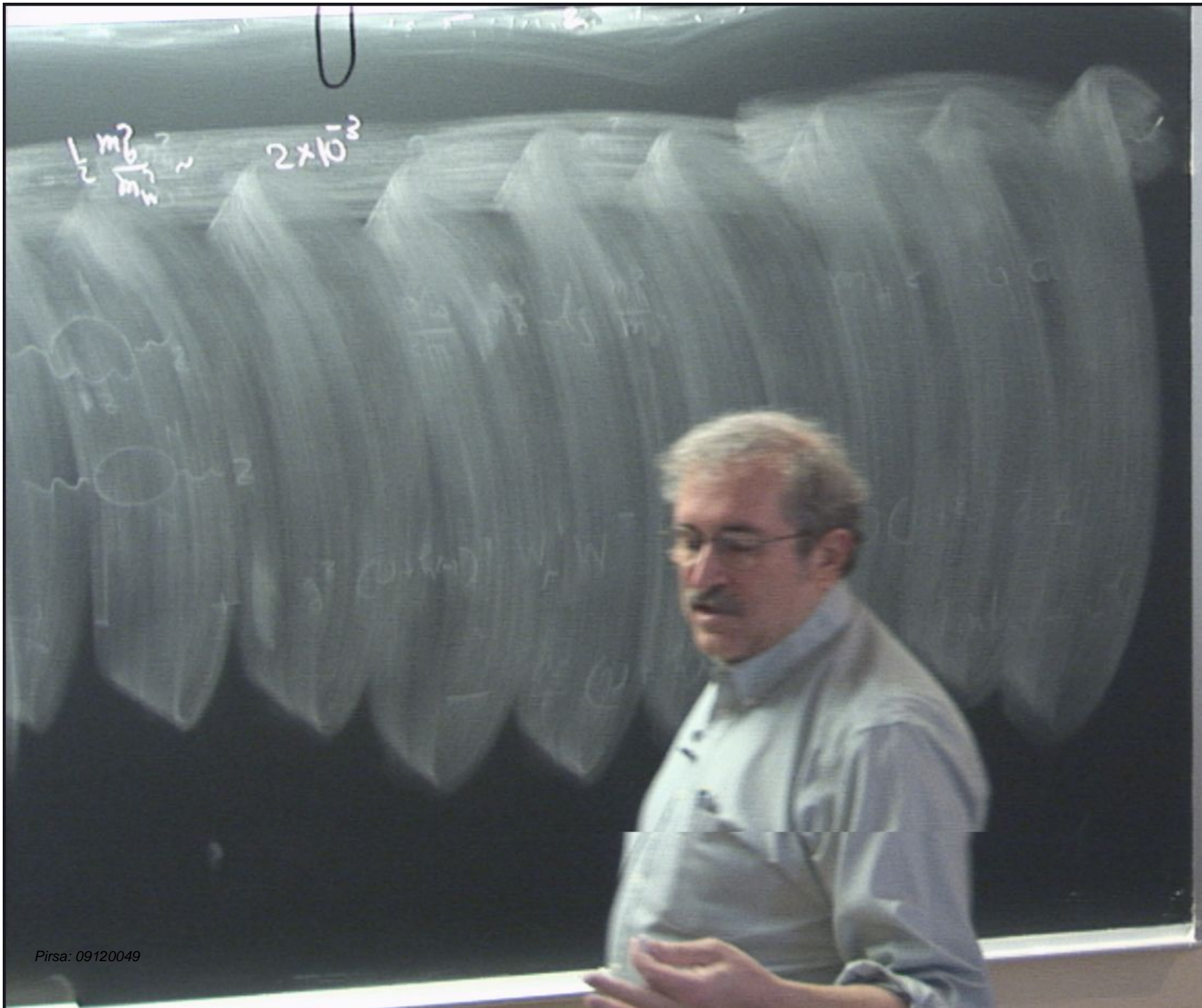
$$I(h \rightarrow W^+ W^-)$$

$$= \frac{\alpha_W}{16} \frac{m_h^3}{m_W^2} \left( 1 - 4 \frac{m_W^2}{m_h^2} + 12 \frac{m_W^2}{m_h^2} \right) \left( 1 - \frac{4m_W^2}{m_h^2} \right)^{1/2}$$

$$I(h \rightarrow Z Z)$$

$$= \frac{\alpha_W}{32} \frac{m_h^3}{m_W^2} \left( 1 - 4 \frac{m_Z^2}{m_h^2} + 12 \frac{m_Z^2}{m_h^2} \right) \left( 1 - \frac{4m_Z^2}{m_h^2} \right)^{1/2}$$

$$\alpha_W \frac{m_h^2}{m_W^2} \sim g^2 \frac{2v^2}{g^2 v^2} \sim 2$$



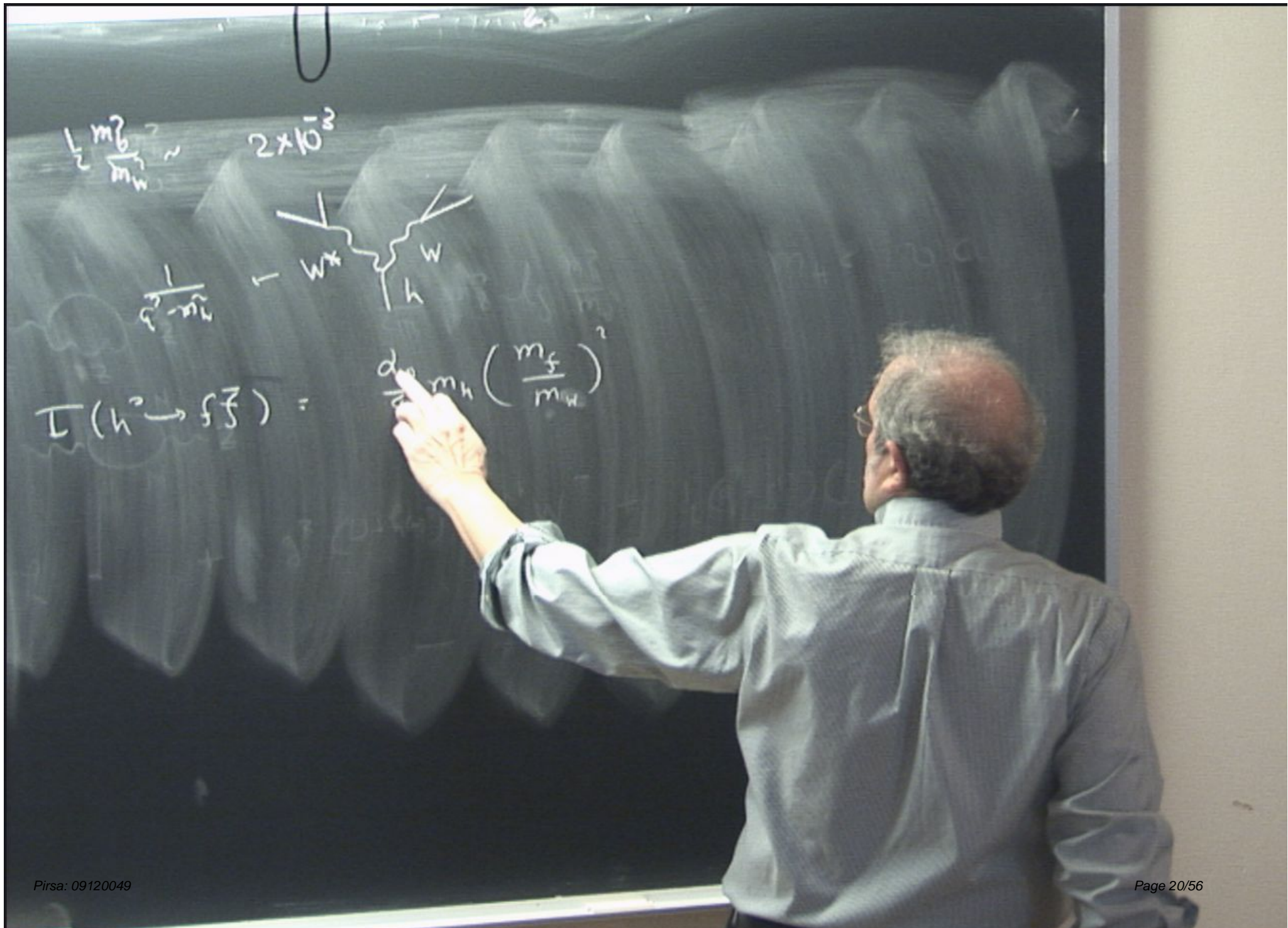
$\frac{1}{2} \frac{m_b}{m_w} \sim 2 \times 10^{-3}$

$\frac{1}{2} \frac{m_b}{m_w}$

$\frac{1}{2} \frac{m_b}{m_w}$

$Wx$   $W$   $h$

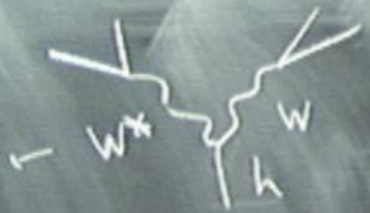




$$\frac{1}{2} \frac{m_b^2}{m_W^2} \sim$$

$$2 \times 10^{-3}$$

$$\frac{1}{s-m_h}$$



$$\Gamma(h^0 \rightarrow f\bar{f}) =$$

$$\frac{d}{dm_h} m_h \left(\frac{m_f}{m_W}\right)^2$$

$$\frac{1}{2} \frac{m_b^2}{m_W^2} \sim$$

$$2 \times 10^{-3}$$

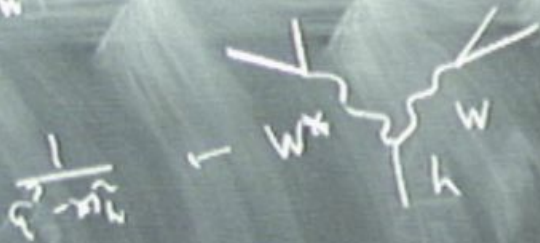


3 quark  
1 lepton

$$\Gamma(h \rightarrow f \bar{f}) = \frac{d\omega}{8} m_h \left( \frac{m_f}{m_W} \right)^2 \left( 1 - 4 \frac{m_f^2}{m_h^2} \right)^{3/2} \cdot N_f$$

$$\frac{1}{2} \frac{m_b^2}{m_W^2}$$

$$2 \times 10^{-3}$$

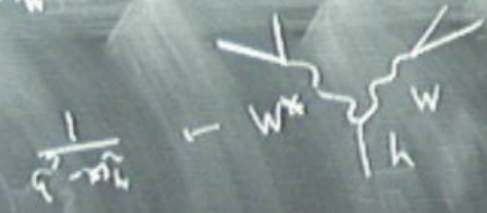


3 quarks  
1 lepton

$$\Gamma(h \rightarrow f \bar{f}) = \frac{d\omega}{8} m_h \left( \frac{m_f}{m_W} \right)^2 \left( 1 - \frac{4m_f^2}{m_h^2} \right)^{3/2} \cdot N_f$$



$$\frac{1}{2} \frac{m_b^2}{m_W^2} \sim 2 \times 10^{-2}$$



$$\Gamma(h \rightarrow f\bar{f}) = \frac{d\omega}{8} m_h \left( \frac{m_f}{m_W} \right)^2 \left( 1 - \frac{4m_f^2}{m_h^2} \right)^{3/2} \cdot N_f$$

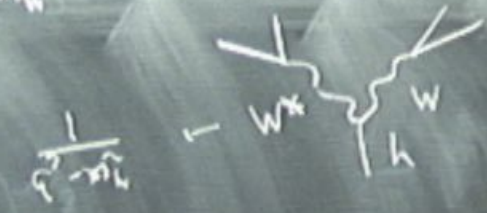
3 quarks  
1 lepton  
↓  
 $N_f$

gluons  
 $m_b > m_h$



$$\Gamma(h \rightarrow gg) = \frac{d\omega d\Omega}{288\pi^2} \frac{m_h^3}{m_W^2}$$

$$\frac{1}{2} \frac{m_b^2}{m_h} \sim 2 \times 10^{-3}$$



$$\Gamma(h \rightarrow f\bar{f}) = \frac{d\omega}{8} m_h \left(\frac{m_f}{m_W}\right)^2 \left(1 - \frac{4m_f^2}{m_h^2}\right)^{3/2} \cdot N_f$$

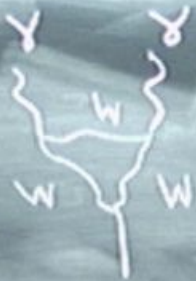
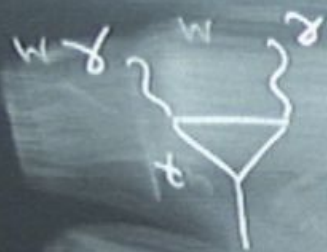
3 quarks  
1 lepton  
↓  
N<sub>f</sub>

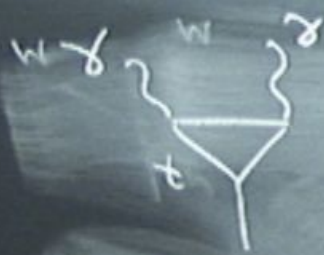
important  
w.  
 $2m_b > m_h \rightarrow$



$$\Gamma(h \rightarrow gg) = \frac{d\omega d\Omega}{288\pi^2} \frac{m_h^3}{m_W^2}$$





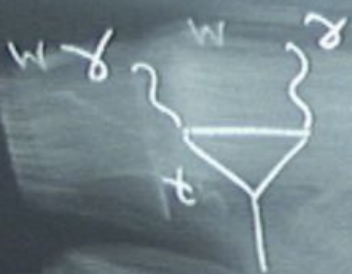


$$m_H = 120 \text{ GeV}$$

$$I(h \rightarrow \gamma\gamma) = 0.027$$

$$\frac{g_W^2}{\pi} \frac{m_H^2}{m_W^2}$$

$$BR \sim 2 \times 10^{-3}$$

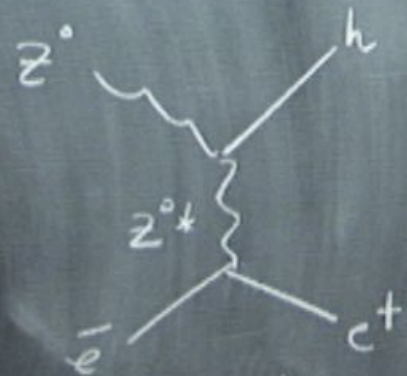


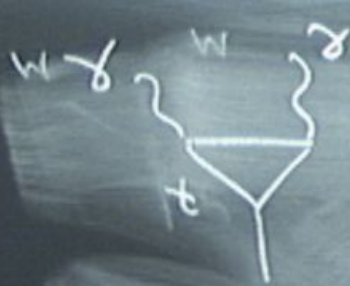
$m_H = 120 \text{ GeV}$

$$I(h \rightarrow \gamma\gamma) = 0.027$$

$$\frac{g_W^2}{\pi} \frac{m_h^2}{m_W^2}$$

$$BR \sim 2 \times 10^{-3}$$





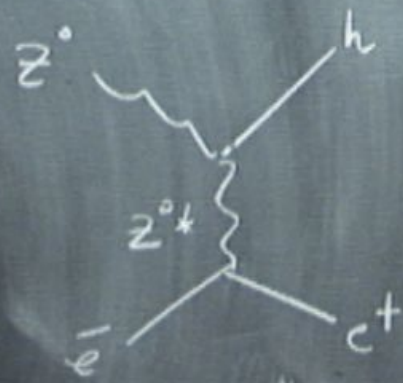
$m_H = 120 \text{ GeV}$

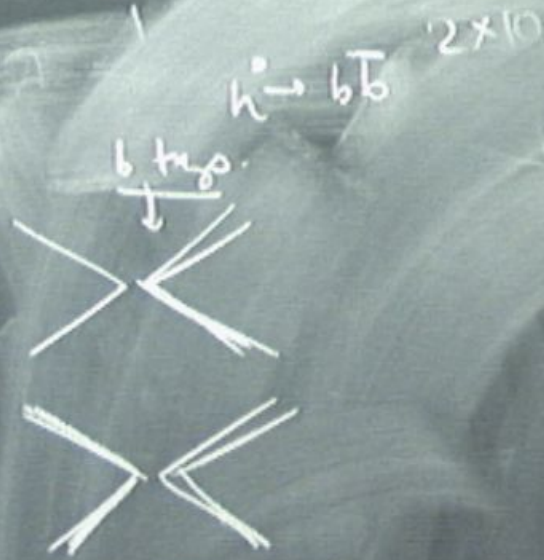
$$I(h \rightarrow \gamma\gamma) = \dots \sim 0.27 \frac{g_w^2}{\pi} \frac{m_h^2}{m_W^2}$$

$$\text{BR} \sim 2 \times 10^{-3}$$

LEP

210 GeV



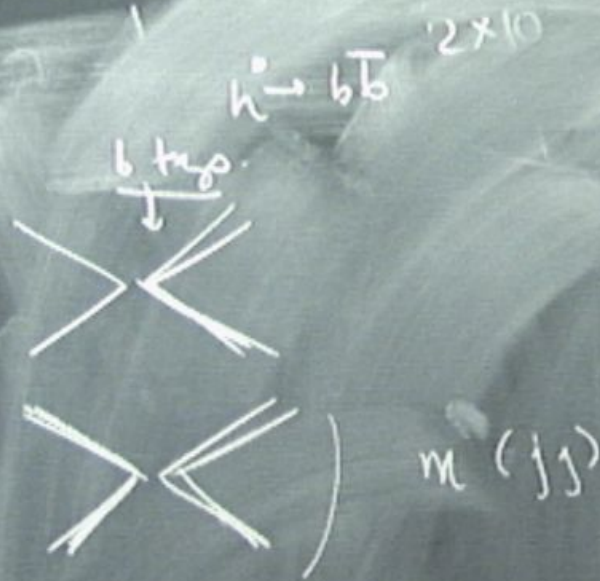


$$\left(\frac{m_t}{m_W}\right)^2 \left(1 - 4\frac{m_t^2}{m_W^2}\right)^{3/2} \cdot N_f$$

$$\rightarrow g_s) = \frac{\alpha_W \alpha_s^2}{288 \pi^2} \frac{m_h^3}{m_W^2}$$

$$BR = 5\%$$

3  
1  
↓



$$\left(\frac{m_j}{m_W}\right)^2 \left(1 - 4\frac{m_j^2}{m_h^2}\right)^{3/2} \cdot N_f$$

$$\rightarrow g_s) = \frac{\alpha_W \alpha_s^2}{288 \pi^2} \frac{m_h^3}{m_W^2}$$

$$BR = 5\%$$

3  
1  
↓

$h^0 \rightarrow b\bar{b}$   $2 \times 10$



$m(jj)$

$\left(\frac{g}{m_W}\right)^2$

$(1 - 4\frac{m_c^2}{m_h^2})^{3/2} \cdot N_f$

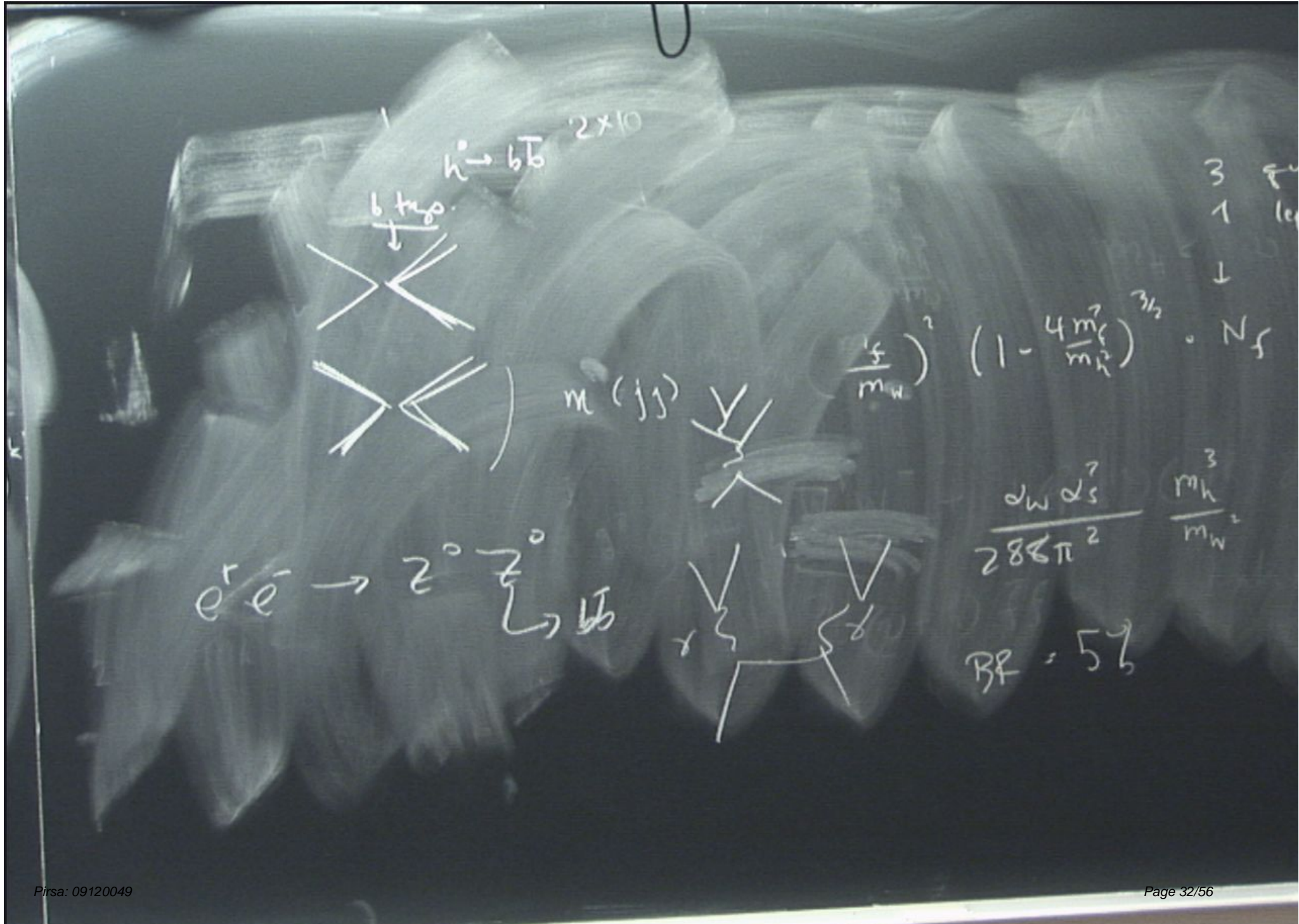
3  
1  
↓

$e^+e^- \rightarrow Z^0 Z^0 \rightarrow b\bar{b}$

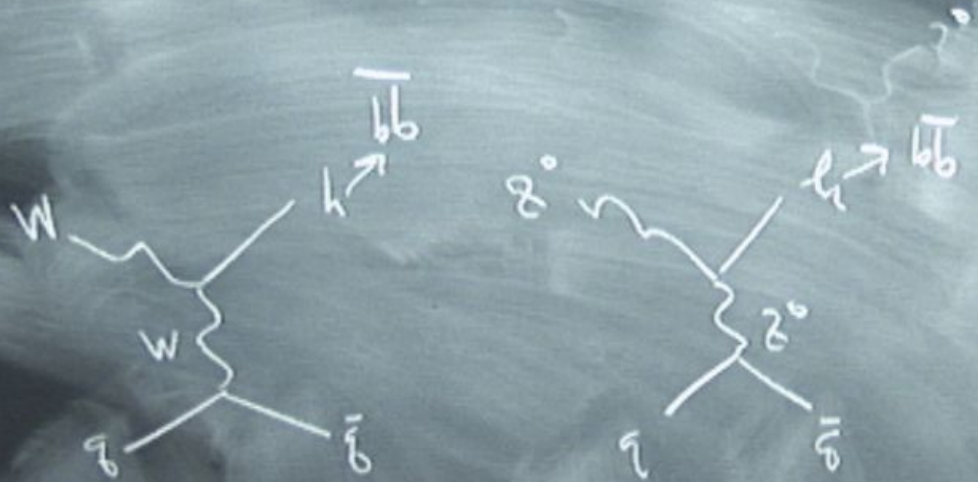
$\rightarrow g_s) =$

$\frac{\alpha_W \alpha_s^2}{288\pi^2} \frac{m_h^3}{m_W^2}$

BR = 5%

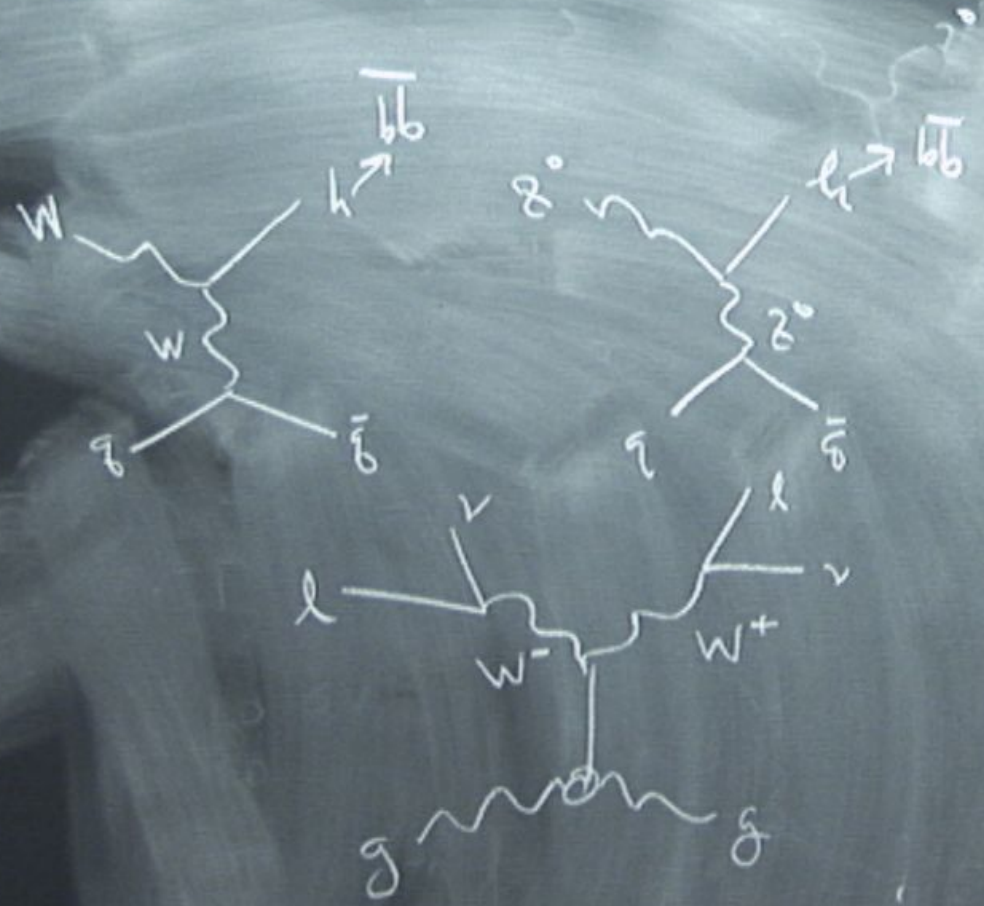


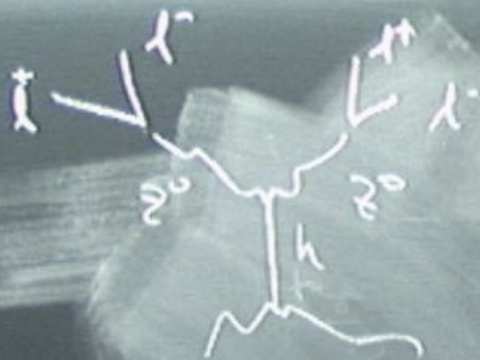


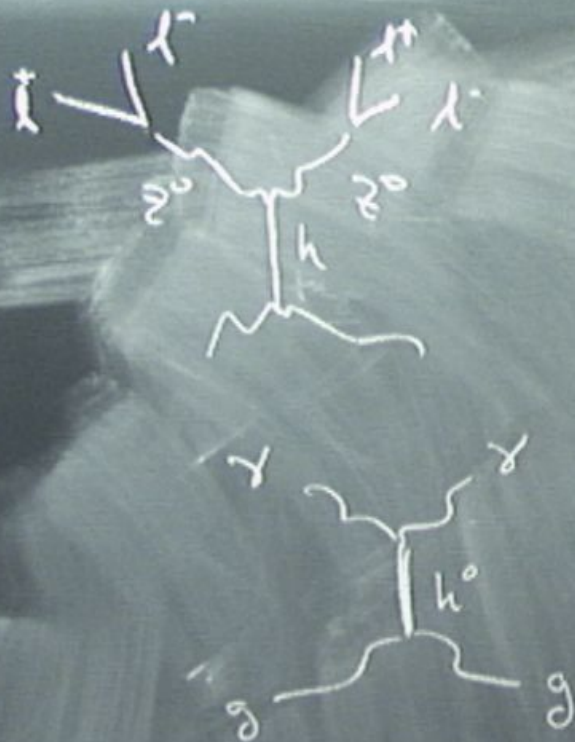


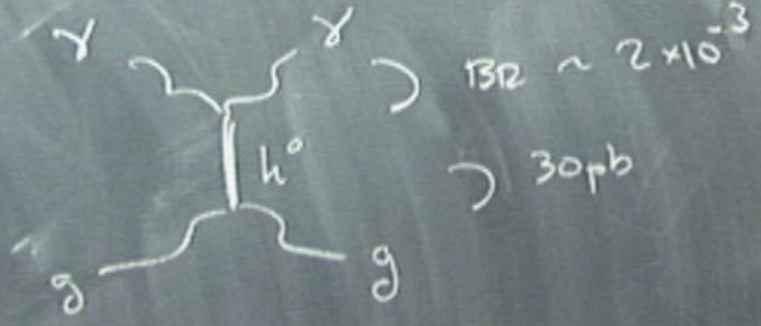
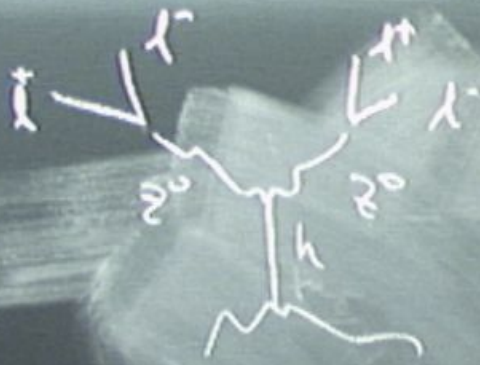
120

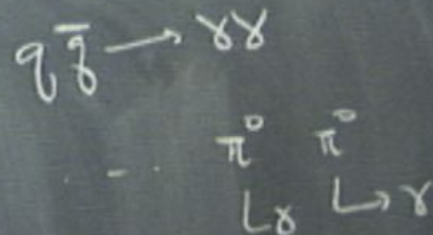
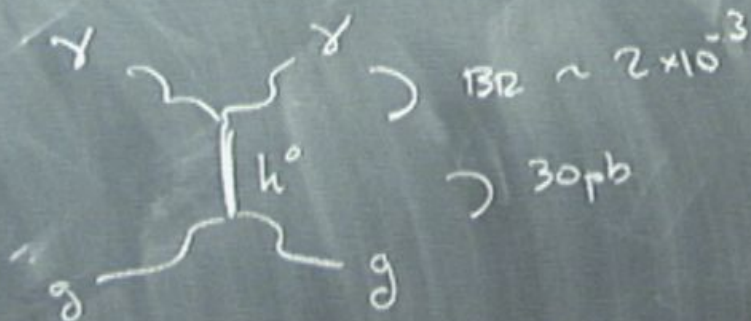
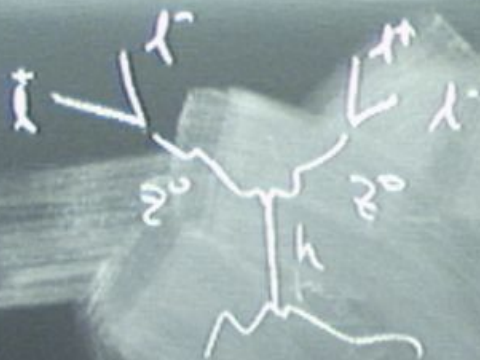
120



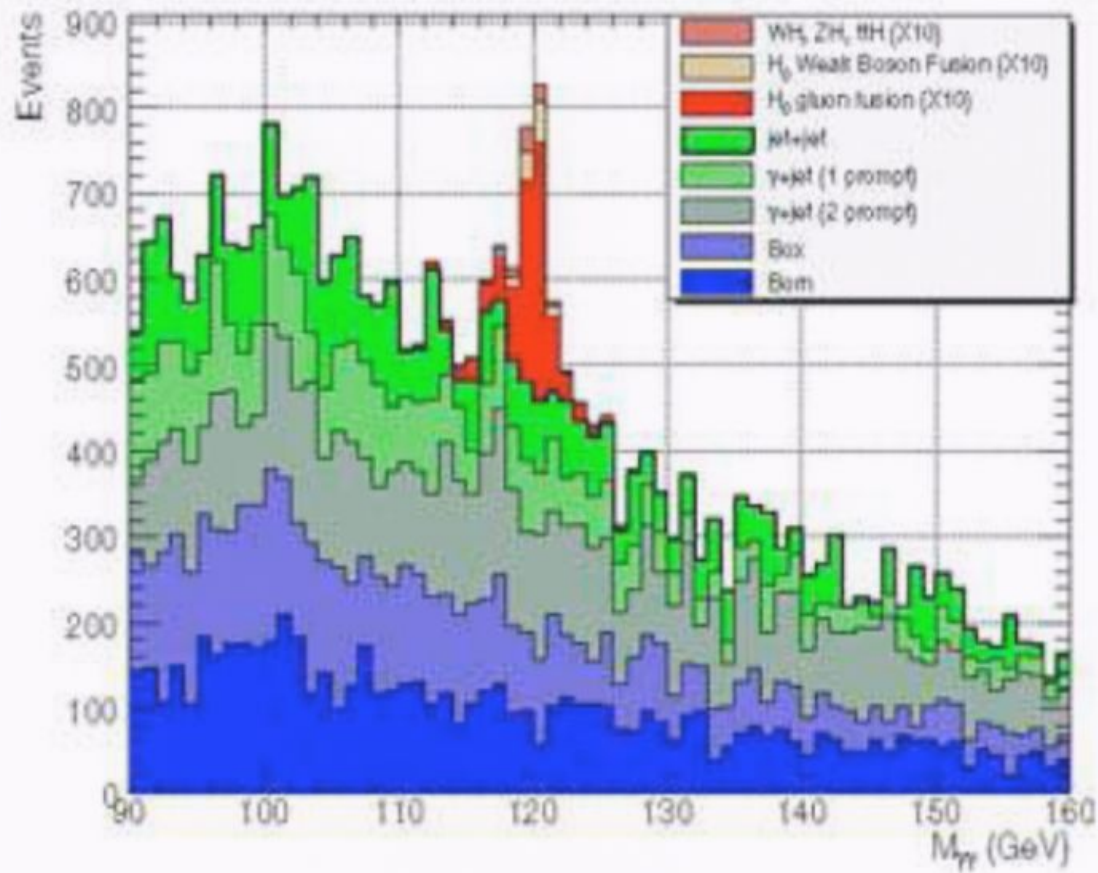




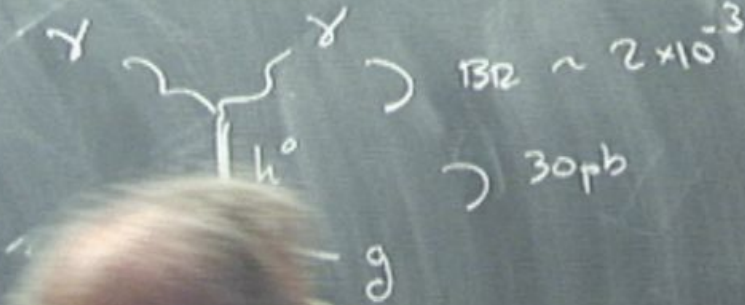
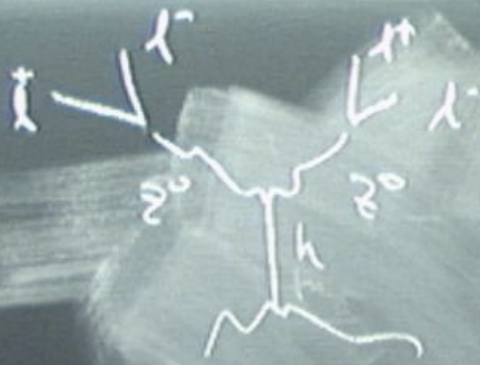




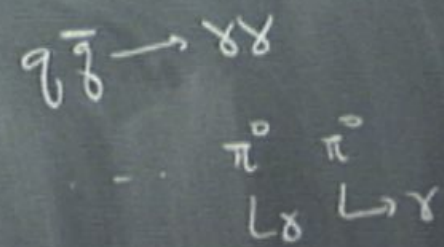
# CMS $h^0 \rightarrow \gamma\gamma$ $7.7 \text{ fb}^{-1}$



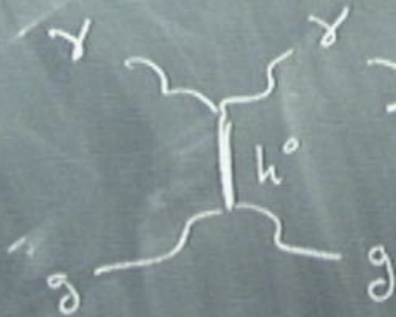
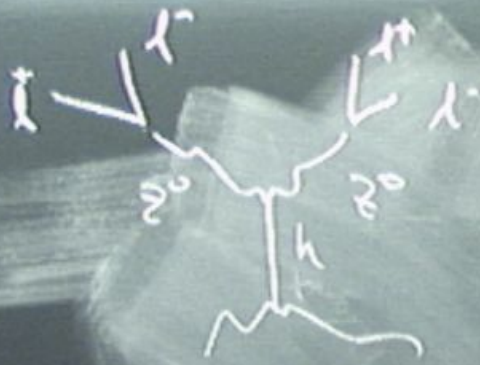
signal x 10 for visibility



$\text{BR} \sim 2 \times 10^{-3}$   
 $\sim 30 \text{ pb}$







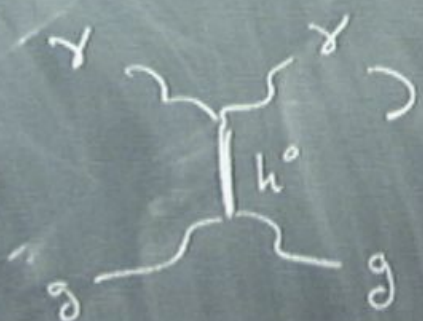
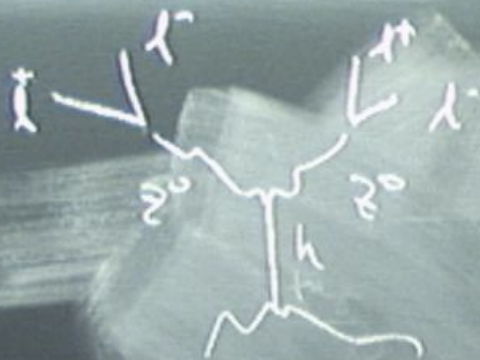
$BR \sim 2 \times 10^{-3}$   
 $\sim 30 \text{ pb}$

1 barn =  $(10 \text{ fm})^2 = 10^{-28} \text{ m}^2$

$\sigma(pp) \sim 100 \text{ mb}$   $\mu n p$   
 $\sigma(pp \rightarrow t\bar{t}) \sim 900 \text{ pb}$

$q\bar{q} \rightarrow \gamma\gamma$

$\pi^0 \pi^0$   
 $L\gamma L\gamma$



$$BR \sim 2 \times 10^{-3}$$

$$30 \text{ pb}$$

$$1 \text{ yr} \approx 100 \text{ event}$$

$$\text{for } \sigma = 1 \text{ fb}$$

$$100,000$$

$$\text{for } \sigma = 1 \text{ pb}$$

$$1 \text{ barn} = (10 \text{ fm})^2 = 10^{-28} \text{ m}^2$$

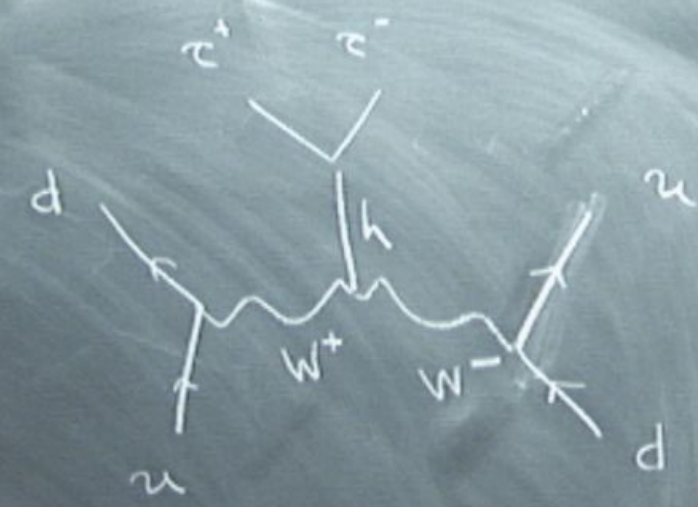
$$\sigma(pp) \sim 100 \text{ mb} \quad \mu n p$$

$$\sigma(pp \rightarrow t\bar{t}) \sim 900 \text{ pb}$$

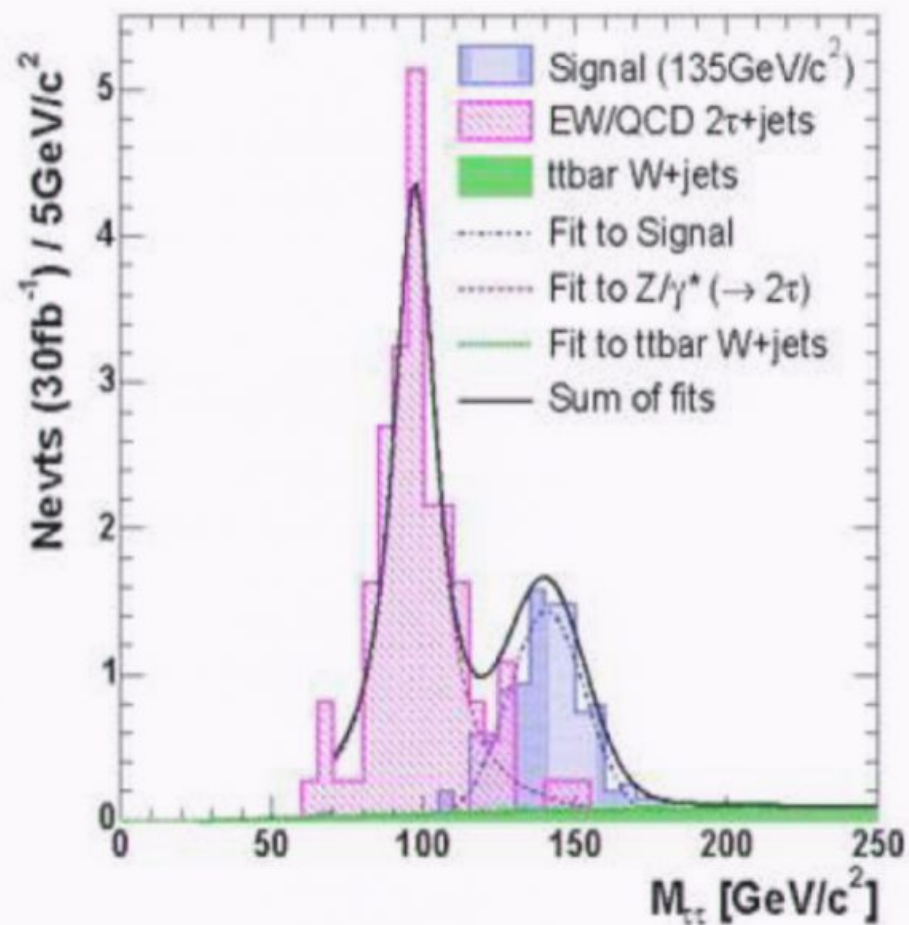
$$q\bar{q} \rightarrow \gamma\gamma$$

$$\pi^0 \pi^0 \rightarrow \gamma\gamma$$

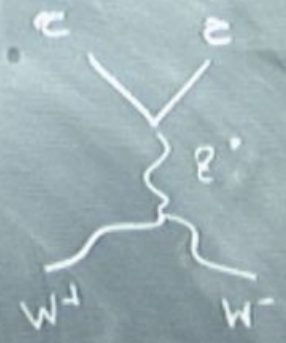
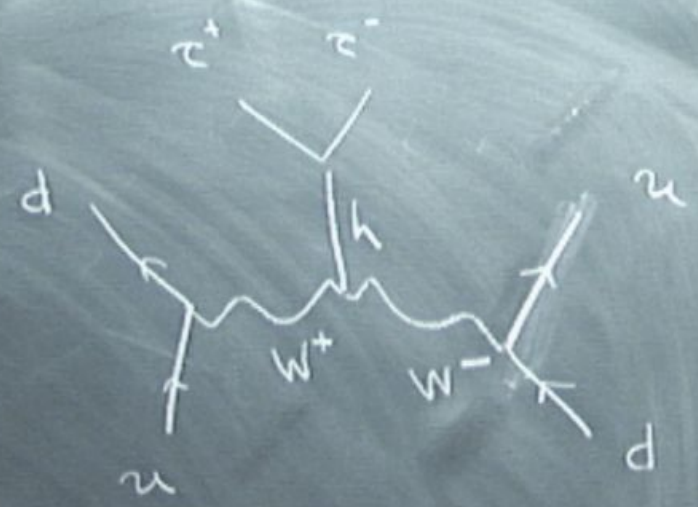
120

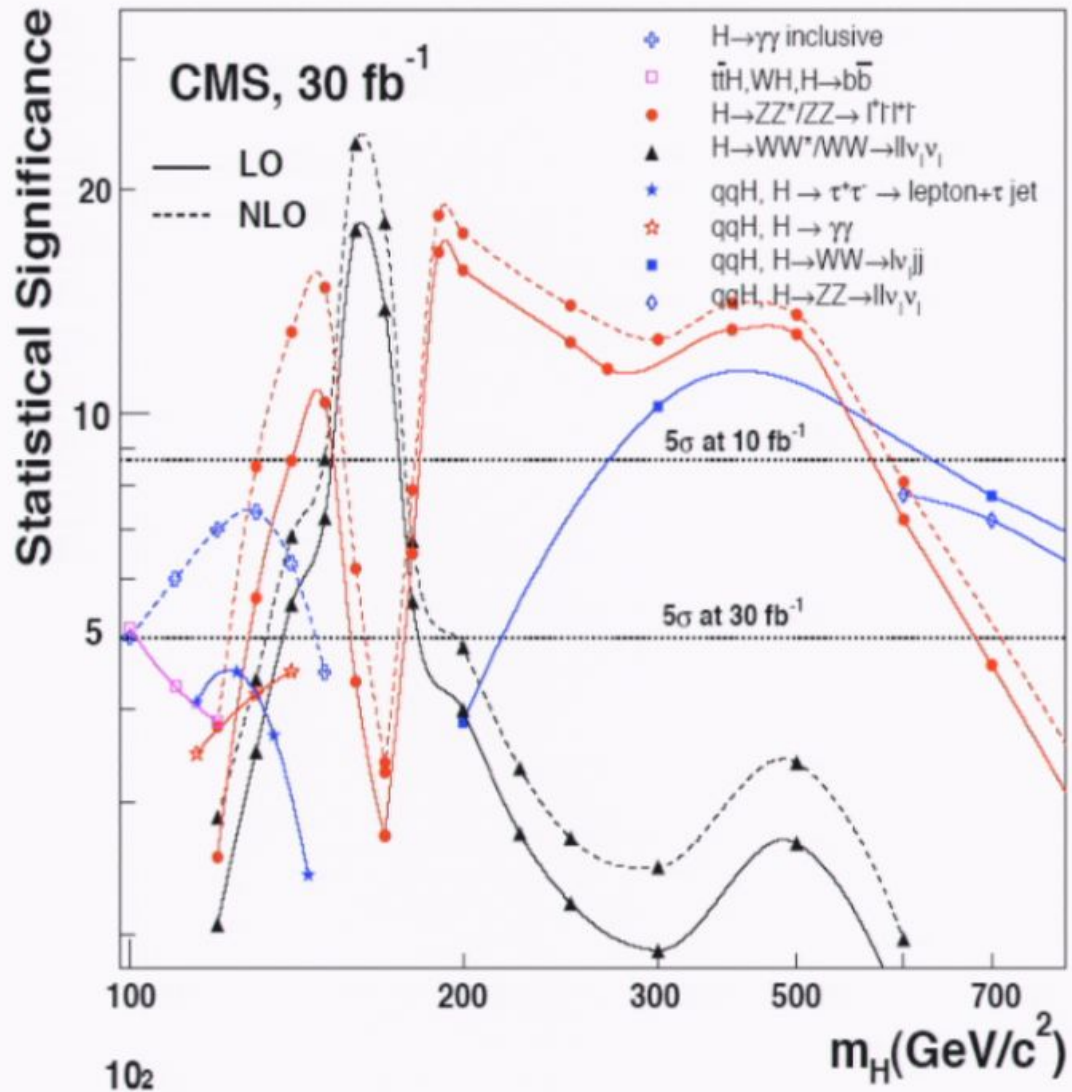


CMS  $h^0 \rightarrow \tau^+ \tau^-$   $30 \text{ fb}^{-1}$   $m(h) = 135 \text{ GeV}$



-120





$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

120

$\phi$

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$+ 2\lambda^2$$

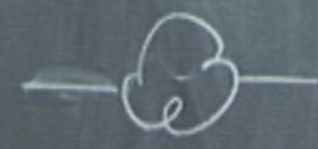


$\phi$

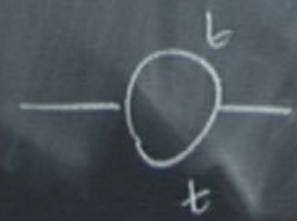
$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$



$$+ 2\Lambda^2$$



$$+ 2\Lambda^2$$



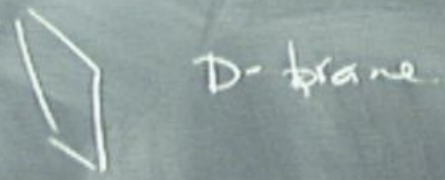
$$- 2\Lambda^2$$

Why  $SU(3) \times SU(2) \times U(1)$   $8 \otimes 8 \otimes 8$

Why reps? Why 3 gens?

Why  $SU(3) \times SU(2) \times U(1)$   $\mathfrak{g}_2 \mathfrak{g}_m$

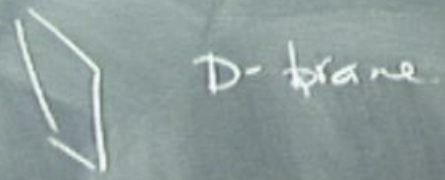
Why reps? Why 3 gen's?



- Kohnen  $\rightarrow$  gen's

Why  $SU(3) \times SU(2) \times U(1)$   $\mathfrak{g}_8 \times \mathfrak{g}_m$

Why reps? Why 3 gen's?



- Knecht  $\rightarrow$  gauge ?

- CP violation

Why  $SU(3) \times SU(2) \times U(1)$  sym sym

Why reps? Why 3



D-brane

- mechanism of gravity ?
- CP violation
- dark matter and dark energy

Why  $SU(3) \times SU(2) \times U(1)$  ggs gm

Why reps? Why 3



D-brane

— Inclusion of gravity ?

— CP violation

— dark matter and dark energy

$$m(\text{DM}) \sim \frac{100 \text{ GeV}}{c^2}$$

Why  $SU(3) \times SU(2) \times U(1)$  sym sym

Why reps? Why 3



D-brane

- Inclusion of gravity?
- CP violation
- dark matter and dark energy  
 $m(\text{DM}) \sim \frac{100 \text{ GeV}}{c^2}$
- origin of electroweak sym breaking



perimeter scholars  
INTERNATIONAL