

Title: Standard Model - Review (PHYS 622) - Lecture 3

Date: Dec 02, 2009 09:00 AM

URL: <http://pirsa.org/09120033>

Abstract:



perimeter scholars
INTERNATIONAL

$$e^+e^- \rightarrow \mu^+\mu^-$$

$$e^+e^- \rightarrow \mu^+\mu^-$$

helicity

$$e^+ e^- \rightarrow \mu^+ \mu^-$$

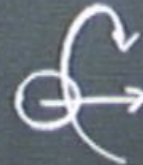
helicity

$$i \bar{\sigma} \cdot \partial \psi_L = 0$$

$$e^+ e^- \rightarrow \mu^+ \mu^-$$

helicity

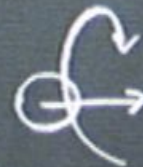
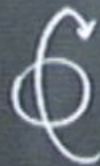
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$$e^+ e^- \rightarrow \mu^+ \mu^-$$

helicity

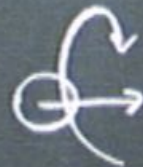
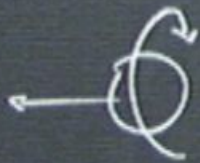
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$$e^+ e^- \rightarrow \mu^+ \mu^-$$

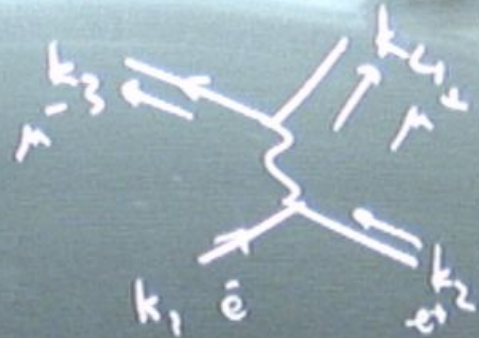
helicity

$$i \vec{\sigma} \cdot \vec{\partial} \psi_L = 0$$

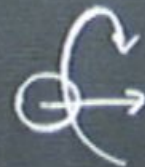
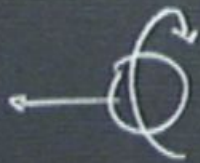


$$e^+ e^- \rightarrow \mu^+ \mu^-$$

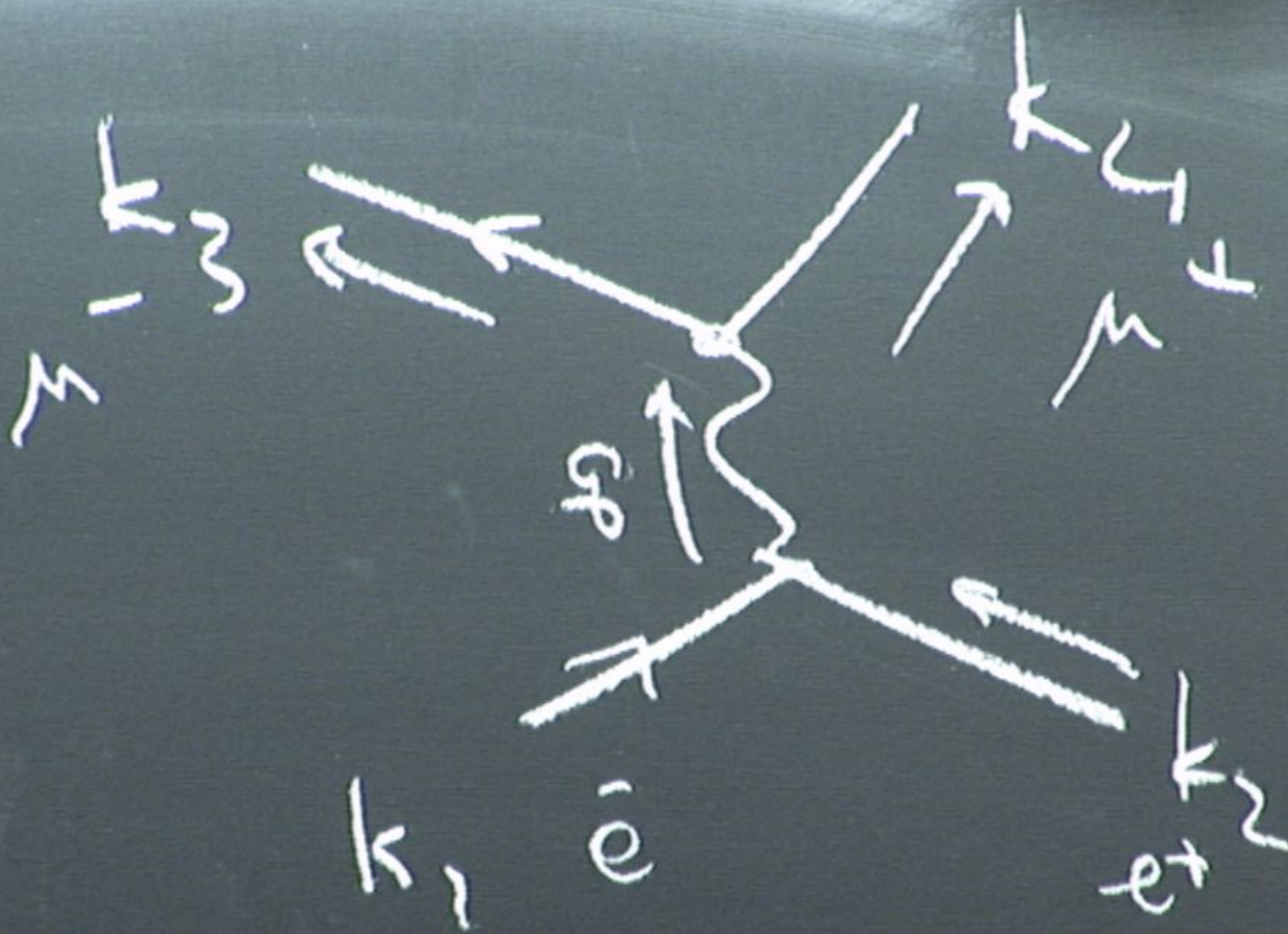
helicity



$$i\vec{\sigma} \cdot \partial \psi_L = 0$$



$$i\eta = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu v(k_1)$$



$$i\eta = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu v(k_1)$$

$$\gamma^\mu = \begin{pmatrix} 0 & \sigma^\mu \\ \bar{\sigma}^\mu & 0 \end{pmatrix}$$

$$\sigma^\mu = (1, \vec{\sigma})$$

$$\bar{\sigma}^\mu = (1, -\vec{\sigma})$$

$$i\cancel{m} = (-ie)^2 \bar{u}(k_2) \gamma^\mu u(k_1) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu v(k_1)$$

$$\gamma^\mu = \begin{pmatrix} 0 & \sigma^\mu \\ \sigma^\mu & 0 \end{pmatrix} \quad \sigma^\mu = (1, \vec{\sigma}) \quad \bar{\sigma}^\mu = (1, -\vec{\sigma})$$

$$k = (E, 0, 0, k)$$

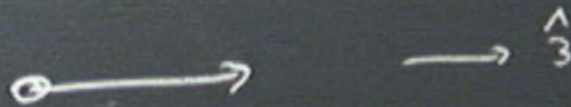
$$(\cancel{k} - m) u = 0$$

$$\begin{pmatrix} -m & E - k\sigma^3 \\ E + k\sigma^3 & -m \end{pmatrix} \begin{pmatrix} u \\ u \end{pmatrix} = 0$$

$$i\mathcal{M} = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\nu u(k_1)$$

$$\gamma^\mu = \begin{pmatrix} 0 & \sigma^\mu \\ \sigma^\mu & 0 \end{pmatrix} \quad \sigma^\mu = (1, \vec{\sigma}) \quad \bar{\sigma}^\mu = (1, -\vec{\sigma})$$

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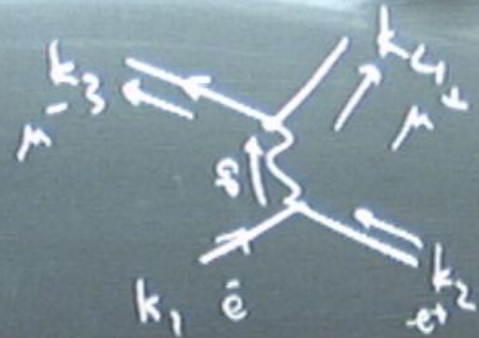
$$h = +\frac{1}{2} \quad u = \begin{pmatrix} \sqrt{E-k} \\ \sqrt{E+k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\begin{pmatrix} -m & E - k\sigma^3 \\ E + k\sigma^3 & -m \end{pmatrix} \begin{pmatrix} u \\ \end{pmatrix} = 0 \quad h = -\frac{1}{2} \quad u = \begin{pmatrix} \sqrt{E+k} \\ \sqrt{E-k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$(K+m)\psi = 0$$

$$k = (E, 0, 0, -k)$$

$$\begin{pmatrix} m & E+k\sigma^3 \\ E-k\sigma^3 & m \end{pmatrix} \psi = 0$$



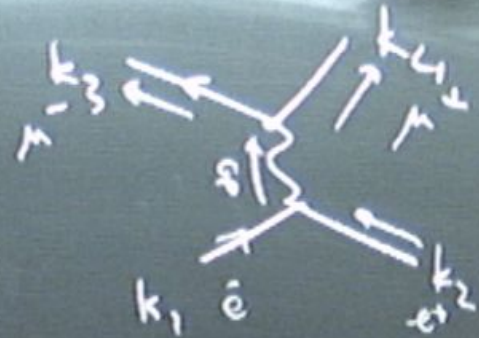
$$(k+m)\psi = 0$$

$$k = (E, 0, 0, -k)$$

$$\begin{pmatrix} m & E+k\sigma^3 \\ E-k\sigma^3 & m \end{pmatrix} \psi = 0$$

$$\psi(k) = \begin{pmatrix} \sqrt{E-k} \\ -\sqrt{E+k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} \sqrt{E+k} \\ -\sqrt{E-k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$



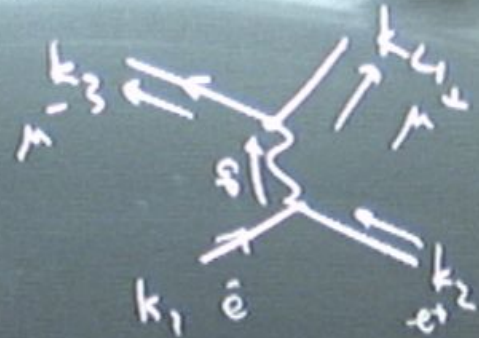
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$$(k+m)\psi = 0$$

$$k = (E, 0, 0, -k)$$

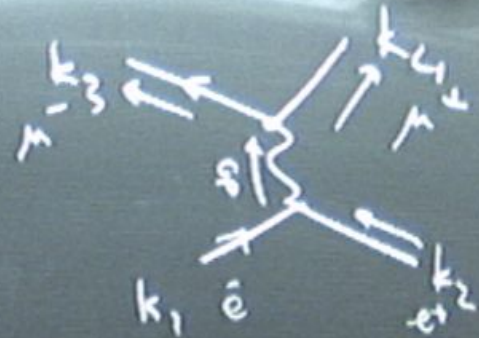
$$\begin{pmatrix} m & E+k\sigma^3 \\ E-k\sigma^3 & m \end{pmatrix} \psi = 0$$

$$\psi(k) = \begin{pmatrix} \sqrt{E-k} \\ -\sqrt{E+k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$h = -\frac{1}{2}$$

$$\begin{pmatrix} \sqrt{E+k} \\ -\sqrt{E-k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$h = +\frac{1}{2}$$



electron $\hat{+z}$

$$h = -\frac{1}{2} \begin{pmatrix} \sqrt{E+k} \\ \sqrt{E-k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$h = +\frac{1}{2} \begin{pmatrix} \sqrt{E-k} \\ \sqrt{E+k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

positron $\hat{-z}$

$$h = -\frac{1}{2} \begin{pmatrix} \sqrt{E-k} \\ \sqrt{E+k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

electron $\hat{3}^+$

$$h = -\frac{1}{2} \begin{pmatrix} \sqrt{E+k} \\ \sqrt{E-k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$h = +\frac{1}{2} \begin{pmatrix} \sqrt{E-k} \\ \sqrt{E+k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

positron $\hat{3}^-$

$$h = -\frac{1}{2} \begin{pmatrix} \sqrt{E-k} \\ -\sqrt{E+k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$h = +\frac{1}{2} \begin{pmatrix} \sqrt{E+k} \\ -\sqrt{E-k} \end{pmatrix} \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$i\mathcal{M} = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu u(k_1)$$

$$\underline{m = 0} \quad \bar{v} \gamma^\mu u = v^\dagger \gamma^0 \gamma^\mu u = v^\dagger \begin{pmatrix} \gamma^0 & 0 \\ 0 & \sigma^i \end{pmatrix} u$$

$$i\mathcal{M} = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu v(k_1)$$

$$m = 0 \quad \bar{v} \gamma^\mu u = v^\dagger \gamma^0 \gamma^\mu u = v^\dagger \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \sigma^4 \end{pmatrix} u$$

$$\bar{e}_L^- e_R^+ \quad (\sqrt{2E})^2 (-1 \ 0) (1 - \vec{\sigma}) \begin{pmatrix} 0 \\ 1 \end{pmatrix} = +2E (0 \ 1, -i, 0)$$

$$e_R^- e_L^+ \quad (\sqrt{2E})^2 (0 \ 1) (1 - \vec{\sigma}) \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -2E (0, 1, i, 0)$$

$$iM = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\nu u(k_1)$$

$$m = 0 \quad \bar{v} \gamma^\mu u = v^\dagger \gamma^0 \gamma^\mu u = v^\dagger \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \sigma^0 \end{pmatrix} u$$

$$\bar{e}_L^- e_R^+ \quad (\sqrt{2E})^2 (-1 \ 0) (1 - \vec{\sigma}) \begin{pmatrix} 0 \\ 1 \end{pmatrix} = +2E (0 \ 1 \ -i \ 0)$$

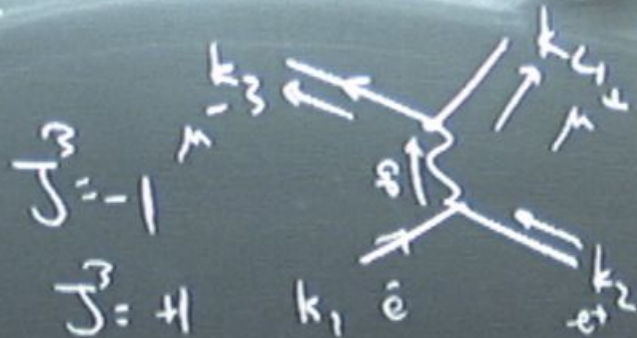
$$\bar{e}_R^- e_L^+ \quad (\sqrt{2E})^2 (0 \ 1) (1 - \vec{\sigma}) \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -2E (0 \ 1 \ i \ 0)$$

helicity
conservation

$$\Sigma_L = \frac{1}{\sqrt{2}} (0 \ 1 \ -i \ 0)$$

$$\Sigma_R = \frac{1}{\sqrt{2}} (0 \ 1 \ i \ 0)$$

$$\Sigma_0 = (0 \ 0 \ 0 \ 1)$$



$$J^3 = 0$$

3

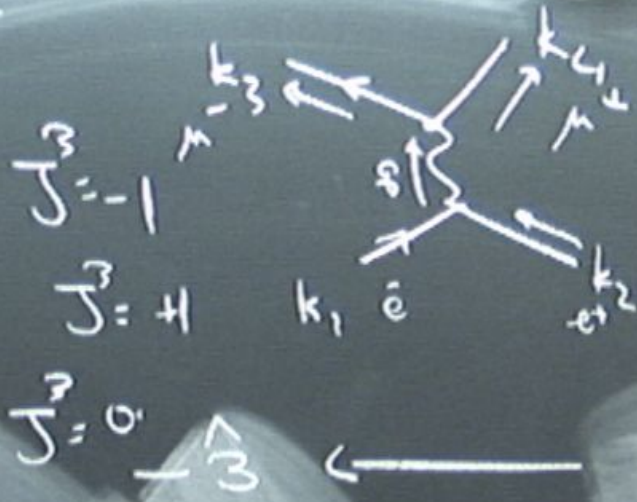
"helicity
conservation"

$$\Sigma_L = \frac{1}{\sqrt{2}} (0 \ 1 \ -i \ 0)$$

$$\Sigma_R = \frac{1}{\sqrt{2}} (0 \ 1 \ i \ 0)$$

$$\Sigma_0 = (0 \ 0 \ 0 \ 1)$$

$$\Sigma_i^* \cdot \Sigma_j = \delta_{ij} (-1)$$



"helicity conservation"

$$iM = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu u(k_1)$$

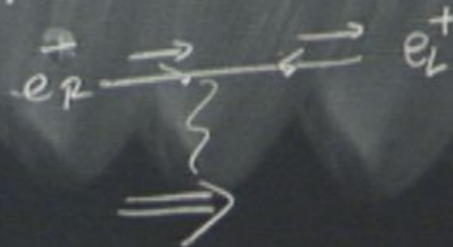
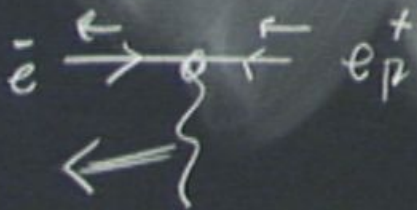
$$m = 0 \quad \bar{v} \gamma^\mu u = v^\dagger \gamma^0 \gamma^\mu u = v^\dagger \begin{pmatrix} \sigma^\mu & 0 \\ 0 & \sigma^\mu \end{pmatrix} u$$

$$\bar{e}_L^- e_R^+ \quad (\sqrt{2E})^2 (-1 \ 0) (1 \ -\vec{\sigma}) \begin{pmatrix} 0 \\ 1 \end{pmatrix} = +2E (0 \ 1 \ -i \ 0)$$

$$e_R^- e_L^+ \quad (\sqrt{2E})^2 (0 \ 1) (1 \ -\vec{\sigma}) \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -2E (0 \ 1 \ i \ 0)$$

$$e_L^- e_R^+ \quad 2E\sqrt{2} \epsilon_L^\mu$$

$$e_R^- e_L^+ \quad -2E\sqrt{2} \epsilon_R^\mu$$



electron \uparrow

$$h = -\frac{1}{2} \begin{pmatrix} \sqrt{E+k} \\ \sqrt{E-k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$h = +\frac{1}{2} \begin{pmatrix} \sqrt{E-k} \\ \sqrt{E+k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

positron \downarrow

$$h = -\frac{1}{2} \begin{pmatrix} \sqrt{E-k} \\ -\sqrt{E+k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$h = +\frac{1}{2} \begin{pmatrix} \sqrt{E+k} \\ -\sqrt{E-k} \end{pmatrix} \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$\sqrt{E+k} \sqrt{E-k} = \sqrt{E^2 - k^2} = mc$$

$$iM = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu u(k_1)$$

$$m = 0 \quad \bar{v} \gamma^\mu u = v^\dagger \gamma^0 \gamma^\mu u = v^\dagger \begin{pmatrix} \sigma^\mu & 0 \\ 0 & \sigma^\mu \end{pmatrix} u$$

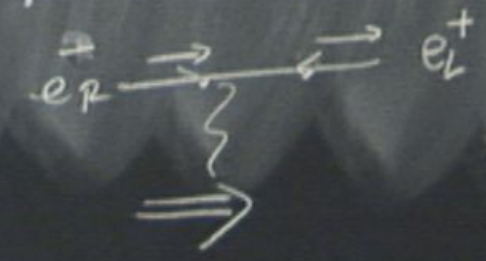
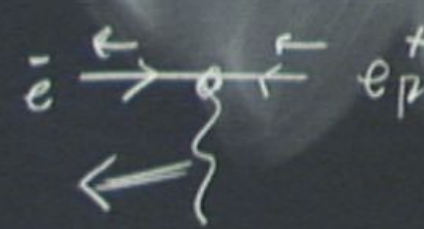
$$\bar{e}_L^- e_R^+ \quad (\sqrt{2E})^2 (-1 \ 0) (1 \ -\vec{\sigma}) \begin{pmatrix} 0 \\ 1 \end{pmatrix} = +2E (0 \ 1 \ -i \ 0)$$

$$\bar{e}_R^- e_L^+ \quad (\sqrt{2E})^2 (0 \ 1) (1 \ -\vec{\sigma}) \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -2E (0 \ 1 \ i \ 0)$$

$$e_L^- e_R^+ \quad 2E \sqrt{2} \epsilon_L^\mu$$

$$e_R^- e_L^+ \quad -2E \sqrt{2} \epsilon_R^\mu$$

$$e_L^- e_L^+ = e_R^- e_R^+ \quad \text{messing}$$



$$= 2m \epsilon_0^\mu$$

$$i\mathcal{M} = (-ie)^2 \bar{u}(k_3) \gamma^\mu u(k_4) \frac{-i}{q^2} \bar{v}(k_2) \gamma^\mu u(k_1)$$

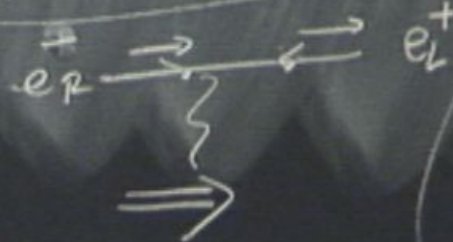
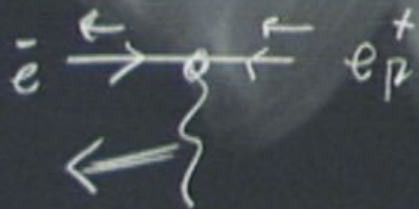
$$m = 0 \quad \bar{v} \gamma^\mu u = v^\dagger \gamma^0 \gamma^\mu u = v^\dagger \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \sigma^0 \end{pmatrix} u$$

$$\bar{e}_L^- e_R^+ \quad (\sqrt{2E})^2 (-1 \ 0) (1 \ -\vec{\sigma}) \begin{pmatrix} 0 \\ 1 \end{pmatrix} = +2E (0 \ 1 \ -i \ 0)$$

$$\bar{e}_R^- e_L^+ \quad (\sqrt{2E})^2 (0 \ 1) (1 \ -\vec{\sigma}) \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -2E (0 \ 1 \ i \ 0)$$

$$\bar{e}_L^- e_R^+ \quad 2E\sqrt{2} \epsilon_L^\mu$$

$$\bar{e}_R^- e_L^+ \quad -2E\sqrt{2} \epsilon_R^\mu$$

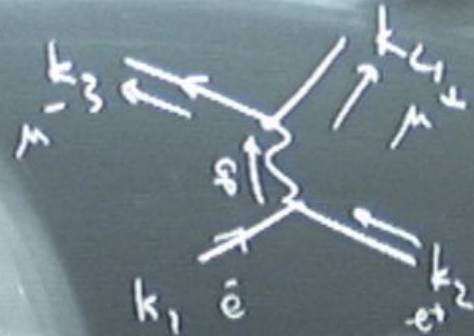


$$\begin{aligned} \bar{e}_L^- e_L^+ &= \bar{e}_R^- e_R^+ \\ &= 2m \epsilon_0^\mu \end{aligned}$$

massive

$$m_e = 0 \quad m_\mu = 0$$

$$M = \frac{ie^2}{s}$$



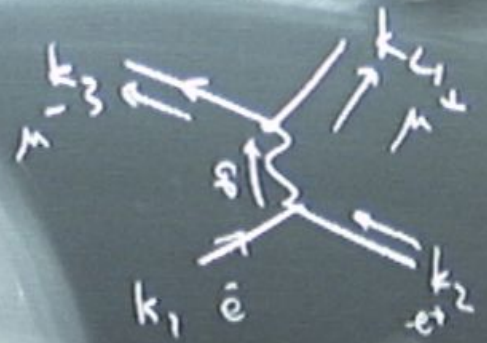
$$E_{cm} = \sqrt{s}$$

" helicity
conservation

$$m_e = 0 \quad m_\mu = 0$$

$$M = \frac{ie^2}{s} 2s \sum_{\mu} \epsilon_{\mu}^* \epsilon_{\mu}$$

$$e_{\mu}^+ \rightarrow \mu_{\mu}^- \mu_{\mu}^+$$



$$E_{cm} = \sqrt{s}$$



" helicity conservation

electron $\hat{\Sigma}^+$ $h = -\frac{1}{2}$ $\begin{pmatrix} \sqrt{E+k} \\ \sqrt{E-k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$

$h = +\frac{1}{2}$ $\begin{pmatrix} \sqrt{E-k} \\ \sqrt{E+k} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$

positron $\hat{\Sigma}^-$ $h = -\frac{1}{2}$ $\begin{pmatrix} \sqrt{E-k} \\ -\sqrt{E+k} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$

$h = +\frac{1}{2}$ $\begin{pmatrix} \sqrt{E+k} \\ -\sqrt{E-k} \end{pmatrix} \begin{pmatrix} -1 \\ 0 \end{pmatrix}$

$\Sigma^+ = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 1 & -i & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{pmatrix}$
 $\Sigma^- = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 1 & i & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{pmatrix}$

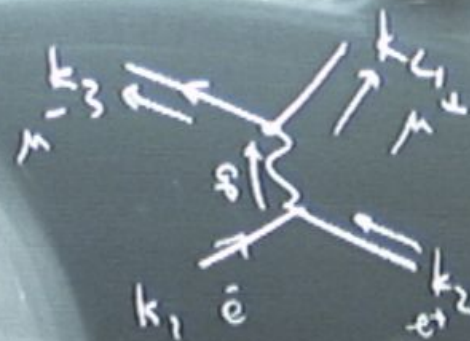
θ

$\frac{1}{\sqrt{2}} \begin{pmatrix} 0 & \cos\theta & -i & -\sin\theta \\ 0 & \sin\theta & 0 & \cos\theta \\ 0 & 0 & 0 & 0 \\ 0 & \cos\theta & i & -\sin\theta \end{pmatrix}$

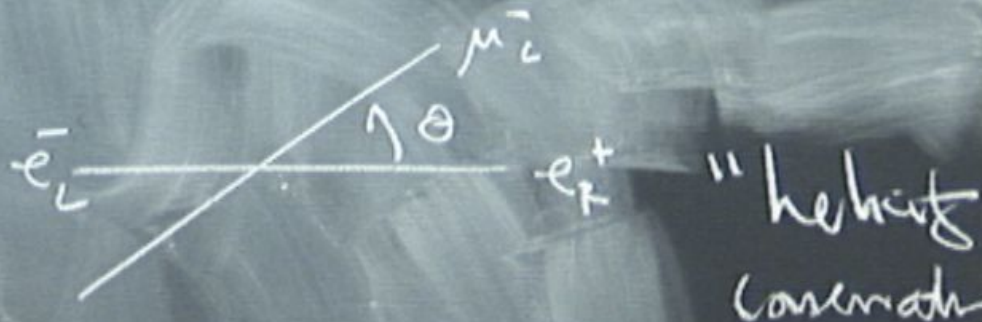
$$m_e = 0 \quad m_\mu = 0$$

$$M = \frac{ie^2}{s} 2s \underbrace{\sum_M^* \epsilon_L^\mu \epsilon_L^\nu}_{-\frac{1}{2}(1 + \cos\theta)}$$

$$e_R^+ \rightarrow \mu_L^- \mu_R^+$$



$$E_{cm} = \sqrt{s}$$



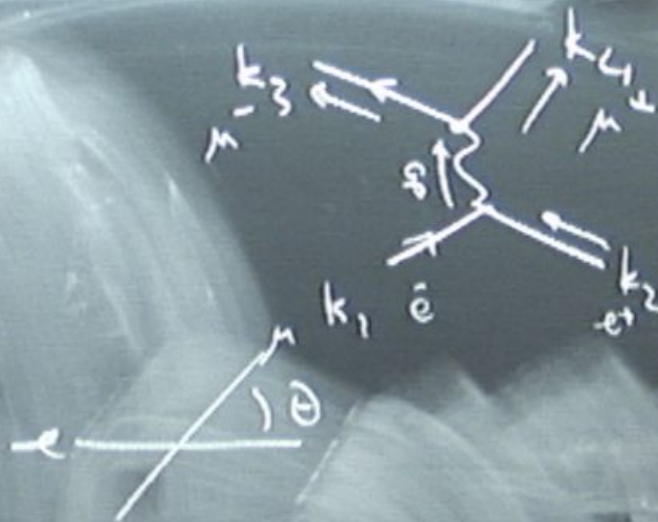
$$m_e = 0 \quad m_\mu = 0$$

$$M = \frac{ie^2}{s} 2 \cancel{s} \underbrace{\sum_L^* \epsilon_L^\mu \epsilon_L^\nu}_{-\frac{1}{2}(1+\cos\theta)}$$

$$e_R^+ \rightarrow \mu_L^- \mu_R^+$$

$$e_L^- e_R^+ \rightarrow \mu_L^- \mu_R^+$$

$$-ie^2 (1+\cos\theta)$$



$$E_{cm} = \sqrt{s}$$

" helicity
conserved

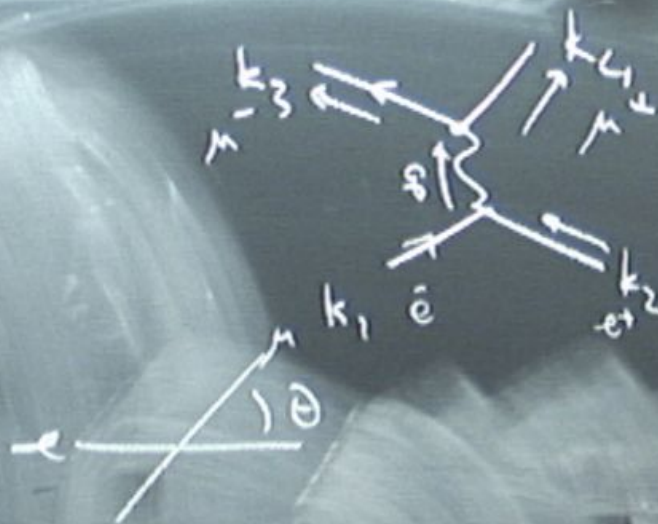
$$m_e = 0 \quad m_\mu = 0$$

$$M = \frac{ie^2}{s} 2 \cancel{s} \underbrace{\sum_M^* \epsilon_L^\mu(\theta) \epsilon_L^\mu}_{-\frac{1}{2}(1 + \cos\theta)}$$

$$e_R^+ \rightarrow \mu_L^- \mu_R^+$$

$$e_L^- e_R^+ \rightarrow \mu_L^- \mu_R^+ \quad -ie^2 (1 + \cos\theta)$$

$$e_L^- e_R^+ \rightarrow \mu_R^- \mu_L^+ \quad ie^2 (1 - \cos\theta)$$



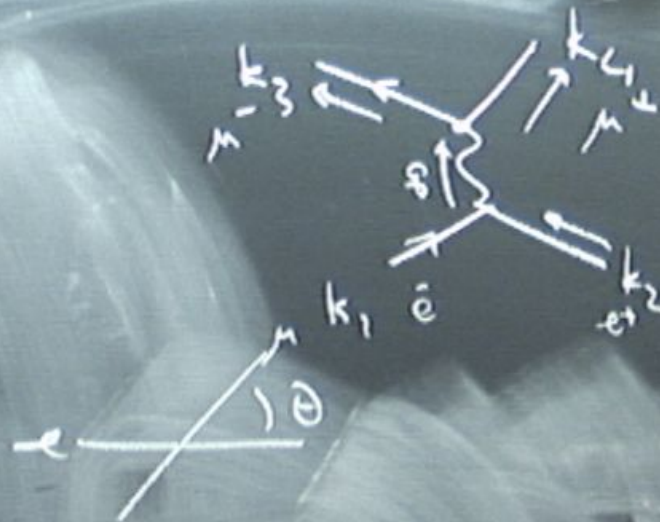
$$E_{cm}^2 = s$$

" helicity
conservation

$$m_e = 0 \quad \cancel{m_e = 0}$$

$$M = \frac{ie^2}{s} 2 \cancel{s} \underbrace{\sum_M^* \epsilon_L^\mu(\theta) \epsilon_L^\nu(\theta)}_{-\frac{1}{2}(1 + \cos\theta)}$$

$$e_R^+ \rightarrow \mu_L^+ \mu_R^+$$



$$E_{cm} = \sqrt{s}$$

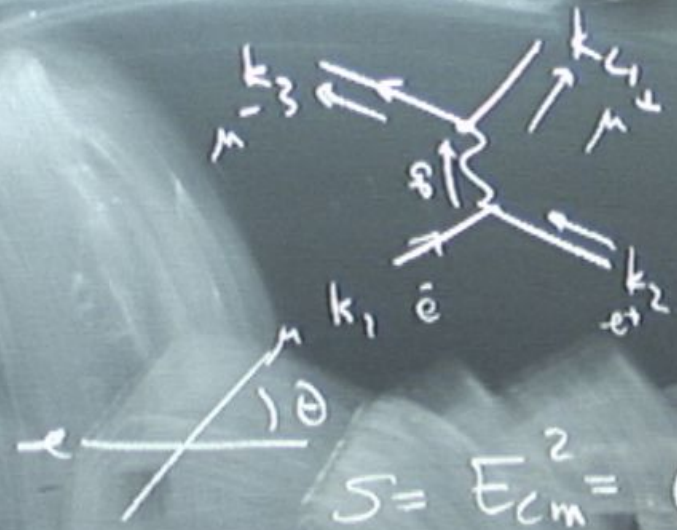
- $e_L^- e_R^+ \rightarrow \mu_L^- \mu_R^+ \quad -ie^2 (1 + \cos\theta)$
- $e_L^- e_R^+ \rightarrow \mu_R^- \mu_L^+ \quad ie^2 (1 - \cos\theta)$
- $e_L^- e_R^+ \rightarrow \mu_L^- \mu_L^+ \quad -ie^2 \frac{m}{E} \sin\theta$
- $\mu_R^- \mu_R^+$

" helicity conservation

$$m_e = 0 \quad \cancel{m_e = 0}$$

$$M = \frac{ie^2}{s} 2 \cancel{s} \underbrace{\sum_M^* \epsilon_L^\mu(\theta) \epsilon_L^\nu(\theta)}_{-\frac{1}{2}(1 + \cos\theta)}$$

$$e_R^+ \rightarrow \mu_L^+ \mu_R^+$$



$$E_{cm}^2 = s$$


$$s = E_{cm}^2 = (2E)^2$$

$$e_L^- e_R^+ \rightarrow \mu_L^- \mu_R^+ \quad -ie^2 (1 + \cos\theta)$$

$$e_L^- e_R^+ \rightarrow \mu_R^- \mu_L^+ \quad ie^2 (1 - \cos\theta)$$

$$e_L^- e_R^+ \rightarrow \begin{matrix} \mu_L^- \mu_L^+ \\ \mu_R^- \mu_R^+ \end{matrix} \quad -ie^2 \frac{m}{E} \sin\theta \quad \left. \begin{matrix} \text{helicity} \\ \text{flip} \end{matrix} \right\}$$

"helicity conservation"



$$\sigma = \frac{1}{2E_A 2E_B |v_A - v_B|} \int d\Omega |m|^2$$

① mass initial



$$\frac{1}{2s}$$



$$\sigma = \frac{1}{2E_A 2E_B |v_A - v_B|} \int d\Omega |M|^2$$

2-body final

① mass initial

$$\frac{1}{16\pi} \int d\cos\theta \left(\frac{2k}{E_{cm}} \right) |M|^2$$

$$d\sigma = \frac{1}{2S}$$

$$\frac{ds}{d\cos\theta} (e_L^- e_R^+ \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \left| \frac{k}{E} \left((1+\cos\theta)^2 + (1-\cos\theta)^2 + 2 \frac{m^2}{E^2} \sin^2\theta \right) \right.$$

$$-ie^2 (1+\cos\theta)$$

$$ie^2 (1-\cos\theta)$$

$$ie^2 \frac{m}{E} \sin\theta \left. \vphantom{\frac{m}{E} \sin\theta} \right) \text{ helicity flip}$$

$$\frac{ds}{d\cos\theta} (e_L^- e_R^+ \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \frac{k}{E} \left((1+\cos\theta)^2 + (1-\cos\theta)^2 + 2 \frac{m^2}{E^2} \sin^2\theta \right)$$

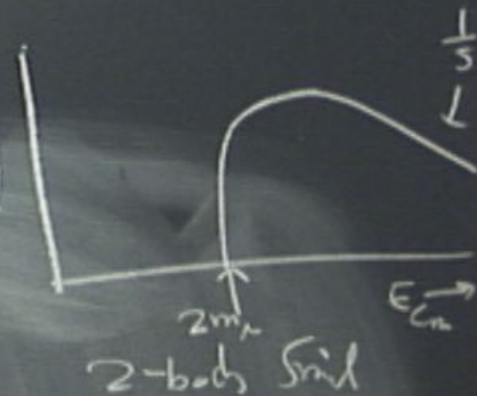
$$\frac{ds}{d\cos\theta} (\bar{e} e^+ \rightarrow \mu^- \mu^+) = \frac{\pi \alpha^2}{2s} \left(1 - \frac{m^2}{E^2}\right)^2 \left(1 + \cos^2\theta + \frac{m^2}{E^2} \sin^2\theta \right)$$

$e_L^- e_R^+ \rightarrow \mu_L^- \mu_R^+$	$-ie^2 (1 + \cos\theta)$) helicity flip
$e_L^- e_R^+ \rightarrow \mu_R^- \mu_L^+$	$ie^2 (1 - \cos\theta)$	
$e_L^- e_R^+ \rightarrow \mu_L^- \mu_L^+$ $\mu_R^- \mu_R^+$	$-ie^2 \frac{m}{E} \sin\theta$	

$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi}{3} \alpha^2 \left(1 - \frac{m^2}{E^2}\right)^2 \left(1 + \frac{m^2}{E^2}\right)$$



① mass initial

$$d\sigma = \frac{1}{2s}$$

$$\frac{1}{16\pi} \int d\cos\theta \left(\frac{2k}{E_{cm}}\right)^2 |M|^2$$

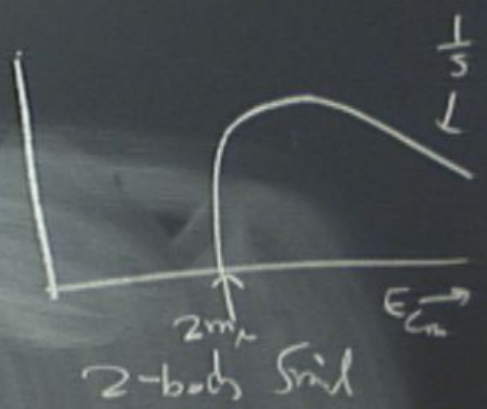
$$\frac{(e^2)^2}{16\pi} = \pi \alpha^2$$

$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

$$+ \frac{m^2}{E^2} 8 \sin^2 \theta$$

$$\sigma = \frac{4\pi}{3} \alpha^2 \left(1 - \frac{m^2}{E^2}\right)^2 \left(1 + \frac{m^2}{E^2}\right)$$

$$\frac{4\pi}{3} \alpha^2 \left(1 - \frac{m^2}{E^2}\right)^2$$



① mass initial

$$\frac{1}{16\pi} \int d\cos\theta \left(\frac{2k}{E_{cm}}\right) |M|^2$$

$$d\sigma = \frac{1}{2s}$$

$$\frac{(e^2)^2}{16\pi} = \pi \alpha^2$$

$$\frac{ds}{ds\Theta} (e^-_L e^+_R \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \frac{k}{E^2} \left((1 + \cos\Theta)^2 + (1 - \cos\Theta)^2 \right)$$

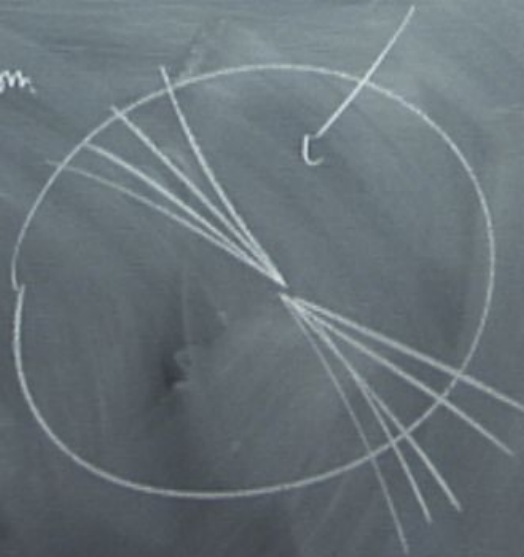
$$\frac{ds}{ds\Theta} (e^- e^+ \rightarrow \mu^- \mu^+) = \frac{\pi \alpha^2}{2s} \left(1 - \frac{m_\mu^2}{E^2} \right)^2 (1 + \cos^2\Theta)$$

$e^+ e^- \rightarrow$ hadron

$$\frac{ds}{d\cos\theta} (\bar{e}_L e_R^+ \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \frac{k}{E} \left((1+\cos\theta)^2 + (1-\cos\theta)^2 \right)$$

$$\frac{ds}{d\cos\theta} (\bar{e} e^+ \rightarrow \mu^- \mu^+) = \frac{\pi \alpha^2}{2s} \left(1 - \frac{m_\mu^2}{E^2} \right)^2 (1 + \cos^2 \theta)$$

$e^+ e^- \rightarrow$ hadron

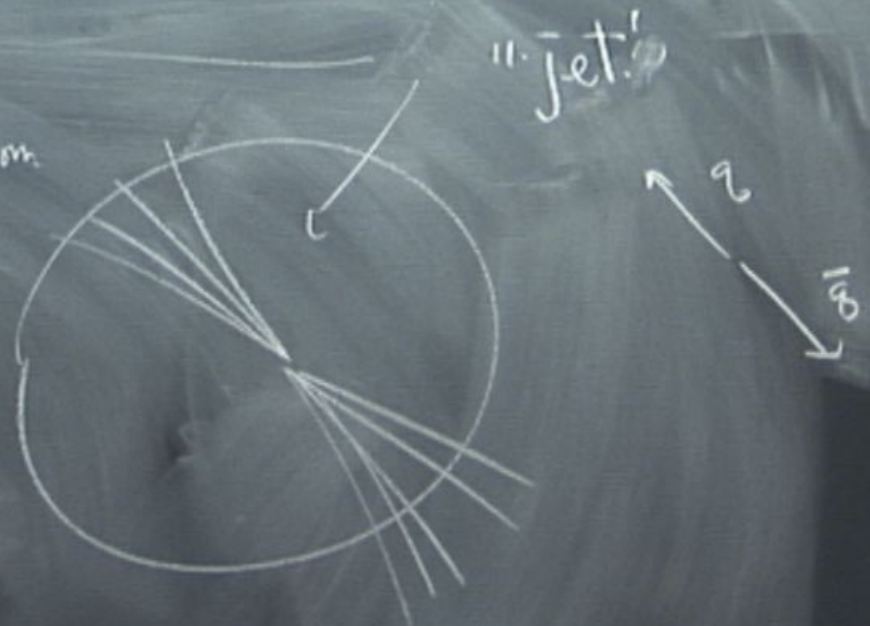


"jet"

$$\frac{ds}{ds\Theta} (\bar{e}_L e_R^+ \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \frac{k}{E^2} \left((1+\cos\Theta)^2 + (1-\cos\Theta)^2 \right)$$

$$\frac{ds}{ds\Theta} (\bar{e} e^+ \rightarrow \mu^- \mu^+) = \frac{\pi \alpha^2}{2s} \left(1 - \frac{m_\mu^2}{E^2} \right)^2 (1 + \cos^2 \Theta)$$

$e^+ e^- \rightarrow$ hadron



$$\frac{ds}{ds\Theta} (\bar{e}_L e_R^+ \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \frac{k}{E^2} \left((1+\cos\Theta)^2 + (1-\cos\Theta)^2 \right)$$

$$\frac{ds}{ds\Theta} (\bar{e} e^+ \rightarrow \mu^- \mu^+) = \frac{\pi \alpha^2}{2s} \left(1 - \frac{m_\mu^2}{E^2} \right)^2 (1 + \cos^2 \Theta)$$

$$\sigma = \frac{4\pi \alpha^2}{s}$$

$$\frac{d\sigma}{d\cos\Theta} (e^-_L e^+_R \rightarrow \mu^- \mu^+) = \frac{1}{2s} \pi \alpha^2 \frac{k}{E^2} \left((1 + \cos\Theta)^2 + (1 - \cos\Theta)^2 \right)$$

$$\frac{d\sigma}{d\cos\Theta} (e^- e^+ \rightarrow \mu^- \mu^+) = \frac{\pi \alpha^2}{2s} \left(1 - \frac{m_\mu^2}{E^2} \right)^2 (1 + \cos^2\Theta)$$

$$\sigma = \frac{4\pi \alpha^2}{s}$$

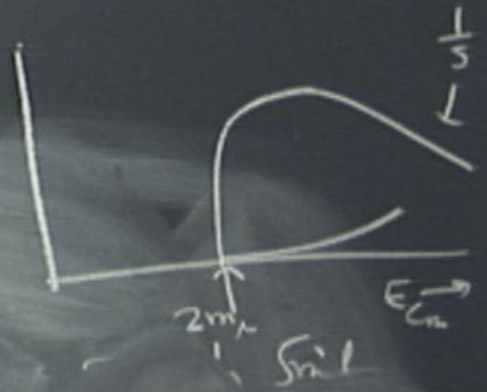
$$e^+ e^- \rightarrow \mu^+ \mu^-$$

$$R = \frac{\sigma(e^+ e^- \rightarrow \text{hadrons})}{\sigma(e^+ e^- \rightarrow \mu^+ \mu^-)}$$

$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi}{s} \frac{d^2\sigma}{d\Omega^2} \left(1 - \frac{m^2}{E^2}\right) \left(1 + \frac{m^2}{E^2}\right)$$

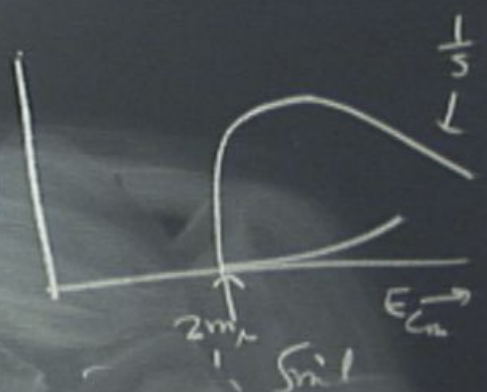


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$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi}{s} \frac{e^2}{s} \left(1 - \frac{m^2}{E^2}\right) \left(1 + \frac{m^2}{E^2}\right)$$

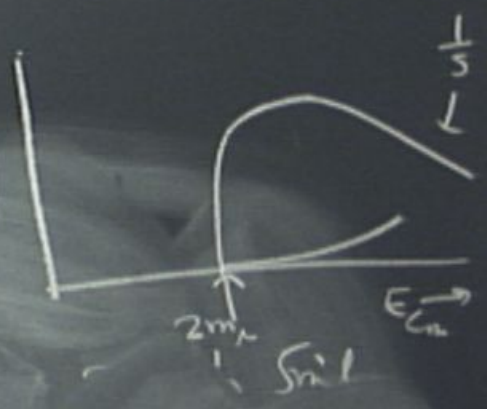
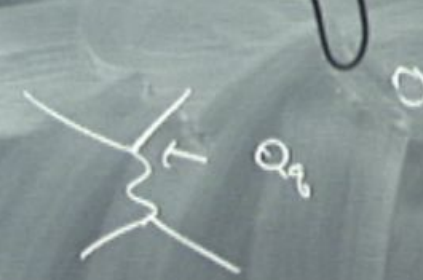


$$= 3 \left[\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right] = 2$$

$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi}{s} \frac{e^2}{s} \left(1 - \frac{m^2}{E^2}\right) \left(1 + \frac{m^2}{E^2}\right)$$



$$= 3 \left[\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right] = 2$$

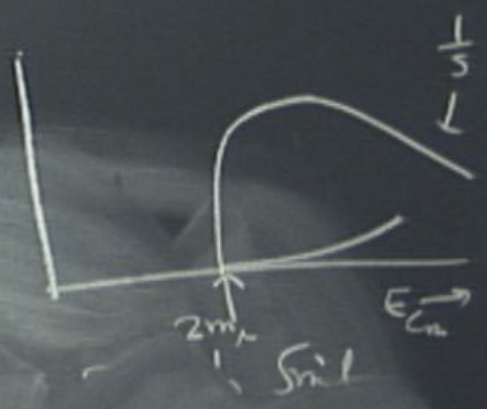
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$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

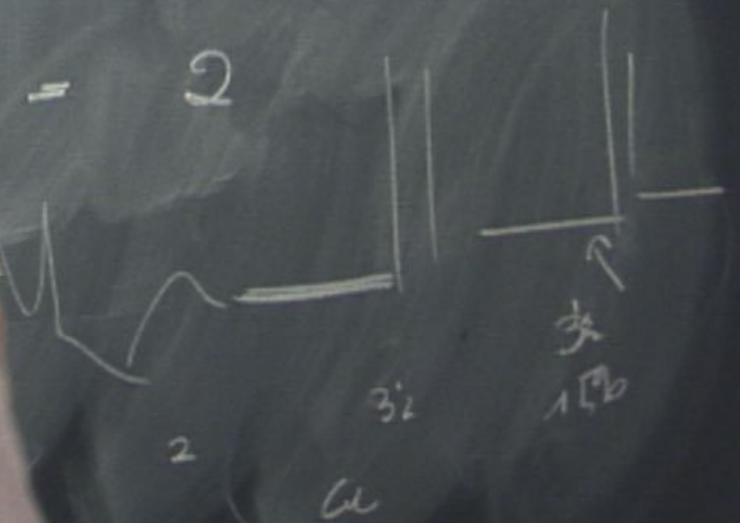
$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi R^2}{s^2} \left(1 - \frac{m^2}{E^2}\right) \left(1 + \frac{m^2}{E^2}\right)$$



$$= 3 \left[\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right] = 2$$

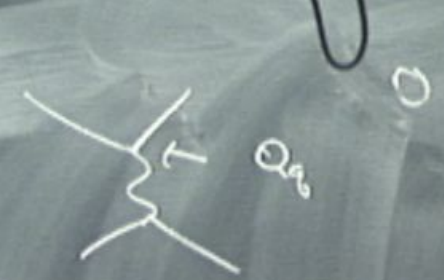
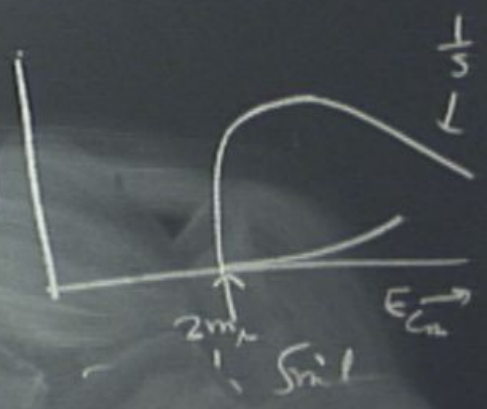
$$+ \left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2$$



$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

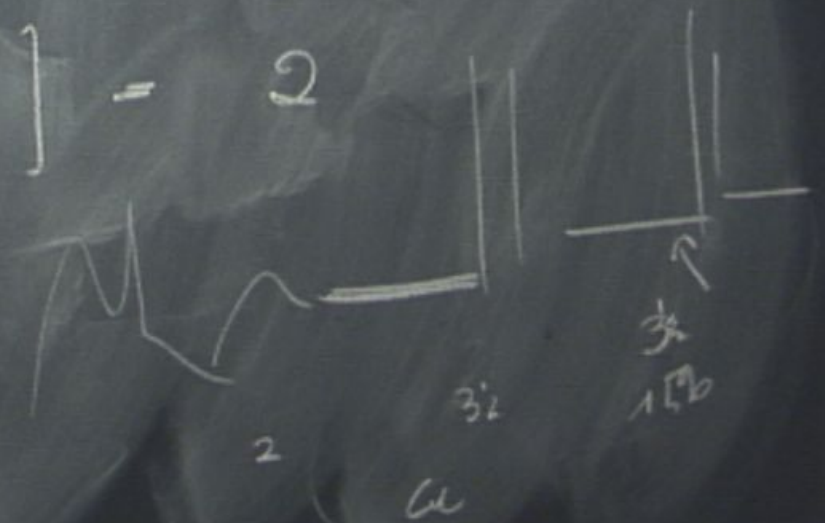
$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi}{s} \frac{e^2}{s} \left(1 - \frac{m^2}{E^2}\right)^2 \left(1 + \frac{m^2}{E^2}\right)$$



$$= 3 \left[\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right] = 2$$

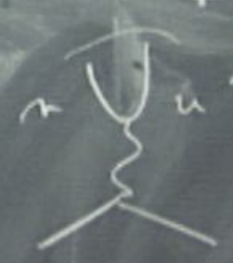
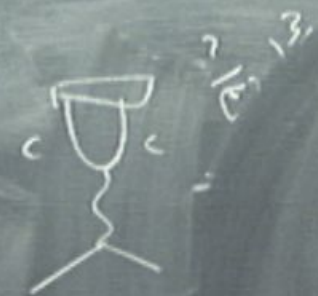
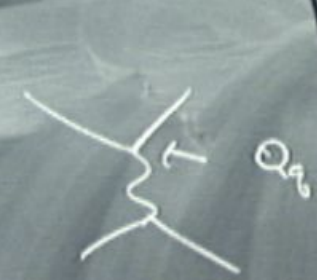
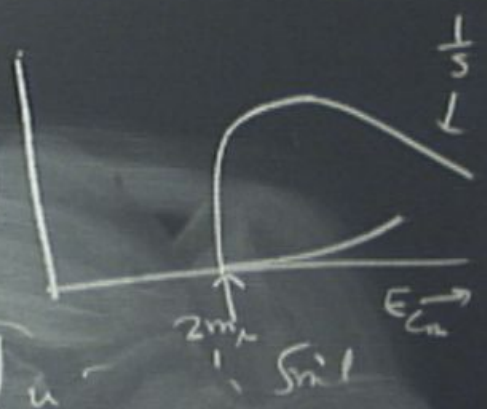
$$+ \left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2$$



$$+ 2 \frac{m^2}{E^2} \sin^2 \theta$$

$$+ \frac{m^2}{E^2} \sin^2 \theta$$

$$\sigma = \frac{4\pi}{s} \frac{e^2}{s} \left(1 - \frac{m^2}{E^2}\right) \left(1 + \frac{m^2}{E^2}\right)$$



$$= 3 \left[\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right] = 2$$

$$+ \left(\frac{2}{3}\right)^2$$

$$\left(-\frac{1}{3}\right)^2$$

