

Title: Perspectives for Asymptotic Safety

Date: Nov 08, 2009 11:00 AM

URL: <http://pirsa.org/09110053>

Abstract:

# asymptotic safety

- **RG scaling of gravitational coupling**


dimensionless coupling  $g(\mu) = Z_N(\mu)^{-1} \cdot G_N \cdot \mu^{D-2}$

anomalous dimension  $\eta_N = -\frac{d \ln Z_N}{d \ln \mu}$

RG running  $\frac{dg}{d \ln \mu} = (D - 2 + \eta_N) g$

- **fixed points**

Gaussian:  $g = 0$

 **classical general relativity**

non-Gaussian:  $\eta_N = 2 - D$

**strong quantum effects**

# asymptotic safety

- **RG scaling of gravitational coupling**

dimensionless coupling  $g(\mu) = Z_N(\mu)^{-1} \cdot G_N \cdot \mu^{D-2}$

anomalous dimension  $\eta_N = -\frac{d \ln Z_N}{d \ln \mu}$

RG running  $\frac{dg}{d \ln \mu} = (D - 2 + \eta_N) g$

- **fixed points**

Gaussian:  $g = 0$  classical general relativity

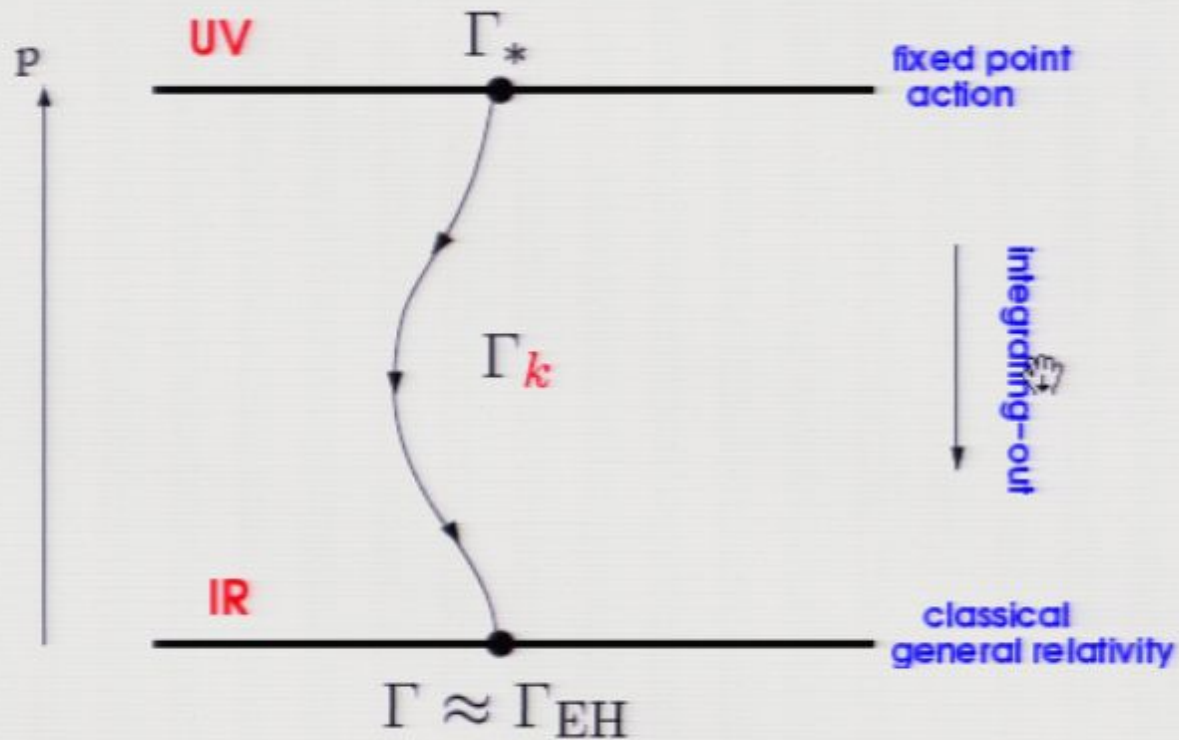
non-Gaussian:  $\eta_N = 2 - D$  strong quantum effects

**UV fixed point** implies weakly coupled gravity at **high energies**

$$\mu \rightarrow \infty : \quad G(\mu) \rightarrow g_* \mu^{2-D} \ll G_N$$

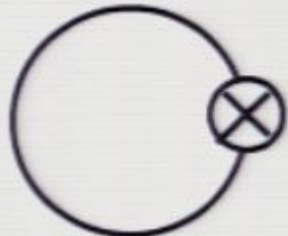
# renormalisation group

- for quantum gravity: “bottom-up”



# renormalisation group

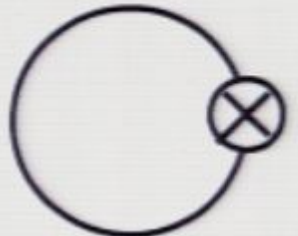
- **Callan-Symanzik equation** (Callan '70, Symanzik '70)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + k^2 \right)^{-1} k \frac{dk^2}{dk} \right]_{\text{ren.}} = \frac{1}{2} \text{Diagram}$$
A Feynman diagram representing a tadpole loop. It consists of a circle with a single external line attached to the right side, ending in a cross symbol (⊗).



# renormalisation group


- **functional RG equation** (Wetterich '93)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Tr} \left[ \text{Tr} \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$
A Feynman diagram representing a tadpole loop. It consists of a circle with a small circle attached to its right side. The small circle contains an 'X' symbol, representing a mass insertion or a tadpole.



# renormalisation group


- **Callan-Symanzik equation** (Callan '70, Symanzik '70)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + k^2 \right)^{-1} k \frac{dk^2}{dk} \right]_{\text{ren.}} = \frac{1}{2} \text{Diagram}$$




# renormalisation group

- **functional RG equation** (Wetterich '93)

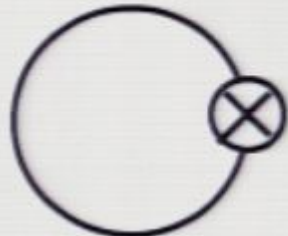
$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Diagram}$$
A Feynman diagram consisting of a circle with a cross inside on the right side, representing a trace over a loop.



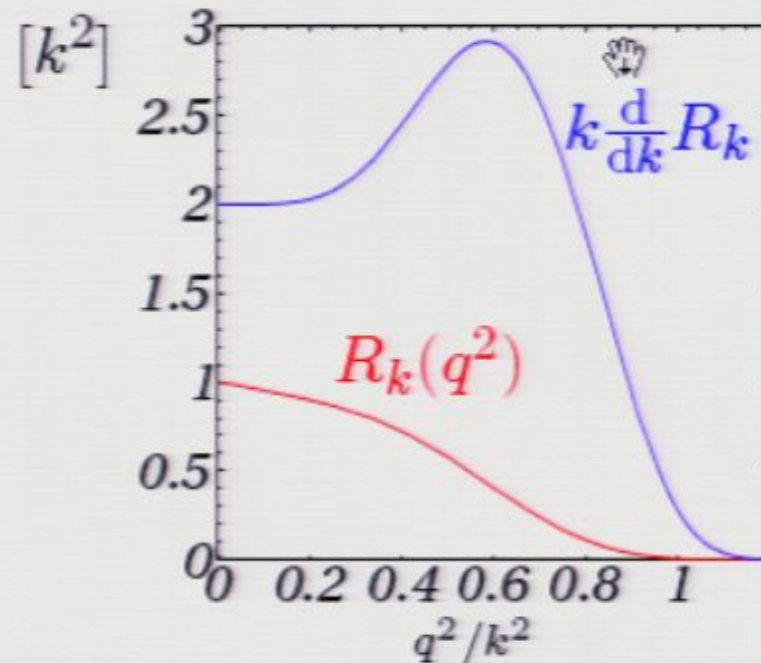


# renormalisation group

- **functional RG equation** (Wetterich '93)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Tr} \left[ \text{Tr} \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$


- **IR momentum cutoff**



# renormalisation group

- **Callan-Symanzik equation** (Callan '70, Symanzik '70)

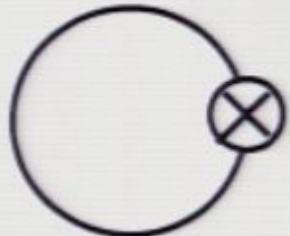
$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + k^2 \right)^{-1} k \frac{dk^2}{dk} \right]_{\text{ren.}} = \frac{1}{2} \text{Diagram}$$

The diagram is a circle with a cross inside, representing a trace operation.



# renormalisation group

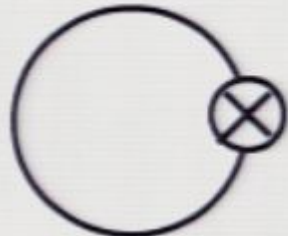
- **functional RG equation** (Wetterich '93)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Tr} \left[ \text{Tr} \left( \frac{dR_k}{dk} \right) \right]$$
A Feynman diagram representing a tadpole loop. It consists of a circle with a small circle attached to its right side. The small circle contains an 'X' symbol, representing a mass insertion or a tadpole.

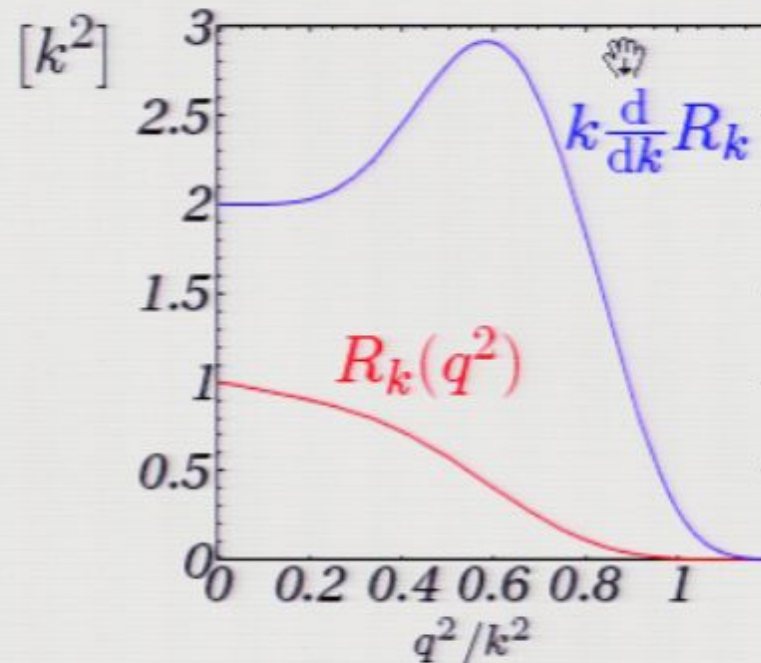


# renormalisation group

- **functional RG equation** (Wetterich '93)

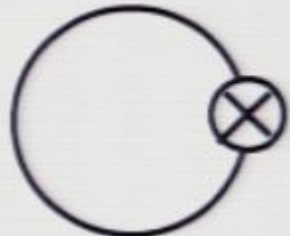
$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Tr} \left[ \text{Tr} \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$


- **IR momentum cutoff**



# renormalisation group

- **functional RG equation** (Wetterich '93)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Diagram}$$


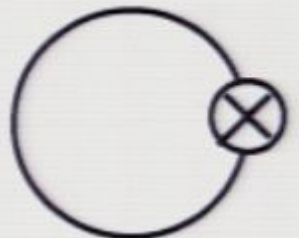
- **definition of the theory**

finite initial (boundary) condition at  $k = \Lambda$ :  $\Gamma_\Lambda$ ,  
 and finite flow equation  $k \partial_k \Gamma_k$ , regulator function  $R_k$ ,  
 altogether:

$$\Gamma = \Gamma_\Lambda + \frac{1}{2} \int_\Lambda^0 dk \partial_k \Gamma_k[\Gamma_k^{(2)}; R_k]$$

# renormalisation group

- **functional RG equation** (Wetterich '93)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Diagram}$$


- **symmetries**

global vs local

if regulator respects symmetry: ok

if not: **(modified) Ward identities** ensure that

the physical theory  $\Gamma_{k=0}$  respects the symmetry

# renormalisation group

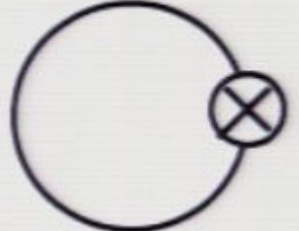
- for quantum gravity (Reuter '96)

$$k \frac{d}{dk} \Gamma_k [g_{\mu\nu}; \bar{g}_{\mu\nu}] = \frac{1}{2} \text{Tr} \left[ \left( \Gamma_k^{(2)} [g_{\mu\nu}; \bar{g}_{\mu\nu}] + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$



# renormalisation group

- **functional RG equation** (Wetterich '93)

$$k \frac{d\Gamma_k}{dk} = \frac{1}{2} \text{Tr} \left[ \left( \frac{\delta^2 \Gamma_k[\phi]}{\delta\phi \delta\phi} + R_k \right)^{-1} k \frac{dR_k}{dk} \right] = \frac{1}{2} \text{Diagram}$$


- **symmetries**

global vs local

if regulator respects symmetry: ok

if not: **(modified) Ward identities** ensure that

the physical theory  $\Gamma_{k=0}$  respects the symmetry



# renormalisation group

- for quantum gravity (Reuter '96)

$$k \frac{d}{dk} \Gamma_k [g_{\mu\nu}; \bar{g}_{\mu\nu}] = \frac{1}{2} \text{Tr} \left[ \left( \Gamma_k^{(2)} [g_{\mu\nu}; \bar{g}_{\mu\nu}] + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$



# renormalisation group

- for quantum gravity (Reuter '96)

$$k \frac{d}{dk} \Gamma_k [g_{\mu\nu}; \bar{g}_{\mu\nu}] = \frac{1}{2} \text{Tr} \left[ \left( \Gamma_k^{(2)} [g_{\mu\nu}; \bar{g}_{\mu\nu}] + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$

- effective action

$$\Gamma_k = \frac{1}{16\pi G_k} \int \sqrt{g} (-R + 2\Lambda_k + \dots) + S_{\text{matter},k} + S_{\text{gf},k} + S_{\text{ghosts},k}$$

# renormalisation group

- **for quantum gravity** (Reuter '96)

$$k \frac{d}{dk} \Gamma_k [g_{\mu\nu}; \bar{g}_{\mu\nu}] = \frac{1}{2} \text{Tr} \left[ \left( \Gamma_k^{(2)} [g_{\mu\nu}; \bar{g}_{\mu\nu}] + R_k \right)^{-1} k \frac{dR_k}{dk} \right]$$

- **effective action**

$$\Gamma_k = \frac{1}{16\pi G_k} \int \sqrt{g} (-R + 2\Lambda_k + \dots) + S_{\text{matter},k} + S_{\text{gf},k} + S_{\text{ghosts},k}$$

- **running couplings**

projection of  $k \partial_k \Gamma_k$  onto  $\sqrt{g}$ ,  $\sqrt{g}R$ ,  $\sqrt{g}R^2$ ,  $\dots$

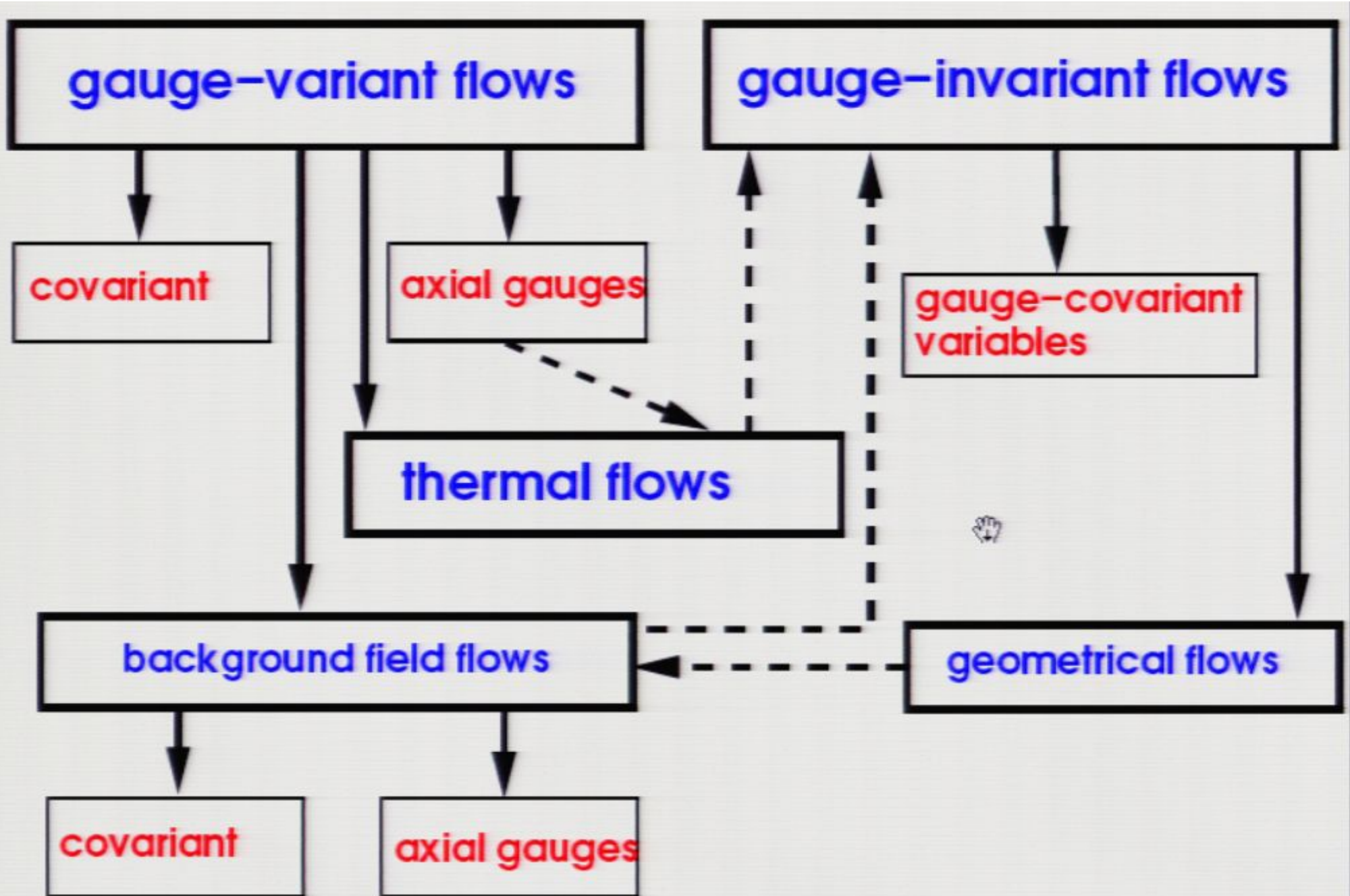
- **optimisation** (DL '00, '01, '02, Pawłowski '05)

choice of regulator function  $R_k$

stability  $\leftrightarrow$  convergence  $\leftrightarrow$  control of approximations

# local symmetry





# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)



# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- background field flow

ansatz

$$\Gamma_k = \int \sqrt{g} \left[ \frac{Z_{N,k}}{16\pi G_N} (-R(g_{\mu\nu}) + 2\bar{\Lambda}_k) + \frac{Z_{A,k}}{4g^2} F_{\mu\nu}^a F_a^{\mu\nu} \right]$$

$$R_k[\bar{\phi}] = \Gamma_k^{(2)}[\bar{\phi}] r[\bar{\phi}] \quad \text{✎}$$

$$r^{gg} = r^{gg}(-\Delta_{\bar{g}}) \quad r^{\bar{\eta}\eta} = -r^{\eta\bar{\eta}} = r^{\bar{\eta}\eta}(-\Delta_{\bar{g}})$$

$$r^{AA} = r^{AA}(-\Delta_{\bar{g}}(A)) \quad r^{\bar{C}C} = -r^{C\bar{C}} = r^{\bar{C}C}(-\Delta_{\bar{g}}(A))$$


# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- background field flow

flow

$$\partial_t \Gamma_k[\phi] = \frac{1}{2} \text{Tr} \frac{1}{1+r[\phi]} \partial_t r[\phi] + \text{Tr} \frac{\partial_t \Gamma_k^{(2)}[\phi, \phi]}{\Gamma_k^{(2)}[\phi, \phi]} \frac{r[\phi]}{1+r[\phi]}$$

result: no graviton contribution at one-loop 

$$\beta_g|_{1\text{-loop}} = \beta_{g,\text{YM}}|_{1\text{-loop}}$$



# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- background field flow

background field dependence

$$\int \frac{\delta R_k}{\delta \bar{\phi}} \frac{\delta \Gamma_k[\phi, \bar{\phi}]}{\delta R_k} = \frac{1}{2} \text{Tr} \frac{1}{\Gamma_k^{(2)}[\phi, \bar{\phi}] + R_k[\bar{\phi}]} \frac{\delta R_k[\bar{\phi}]}{\delta \bar{\phi}}$$



- YM theory

non-trivial contribution at 1-loop

DL, JM. Pawłowski ('02)

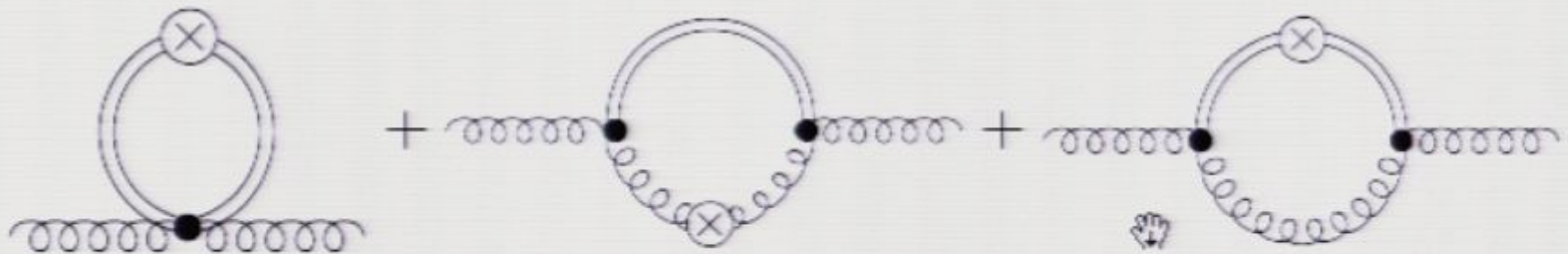
- here:

$$\frac{1}{2} \text{Tr} \frac{1}{1 + r[\phi]} \frac{\delta r}{\delta \phi} + \text{Tr} \frac{\delta \Gamma_k^{(2)}}{\delta \phi}[\phi, \phi] \frac{1}{\Gamma_k^{(2)}[\phi, \phi]} \frac{r[\phi]}{1 + r[\phi]}$$

# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- flat background



# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- flat background



- 1-loop result

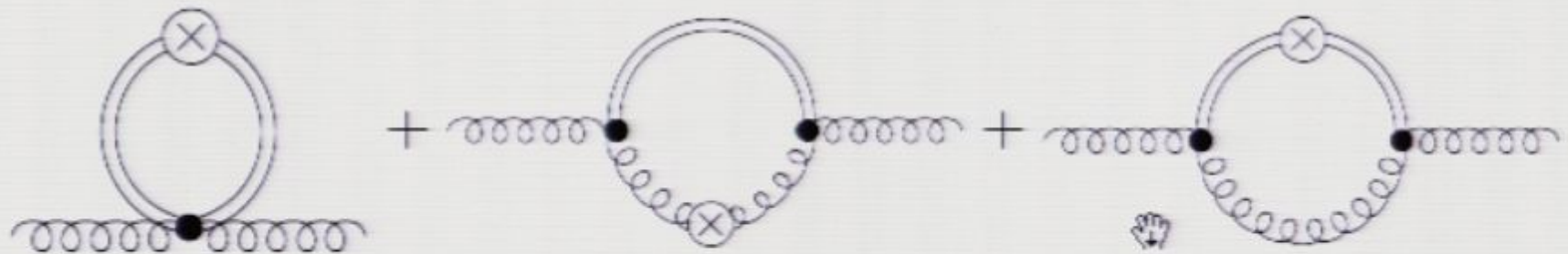
$$\beta_{\text{YM}}|_{\text{grav}} = -\frac{6I}{\pi} G_N g_{\text{YM}} E^2$$

$$I = \int_0^\infty dx \frac{1 + \alpha}{1 + r_g(x)} \left( 1 - \frac{1}{1 + r_A(x)} \right) \geq 0$$

# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- flat background



- beyond 1-loop

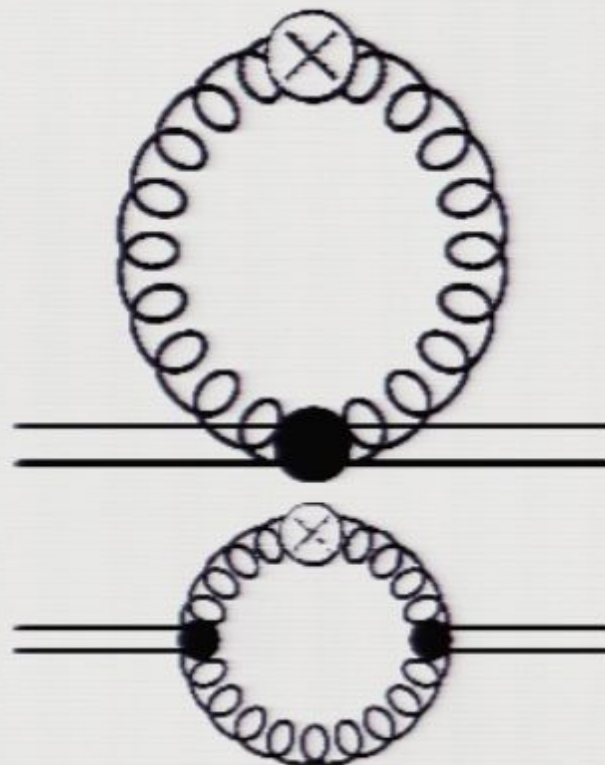
$$\beta_{\text{YM}}|_{\text{grav}} < 0$$

asymptotic freedom persists in presence of gravity FP

# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- Yang-Mills contribution to gravity  
diagrams

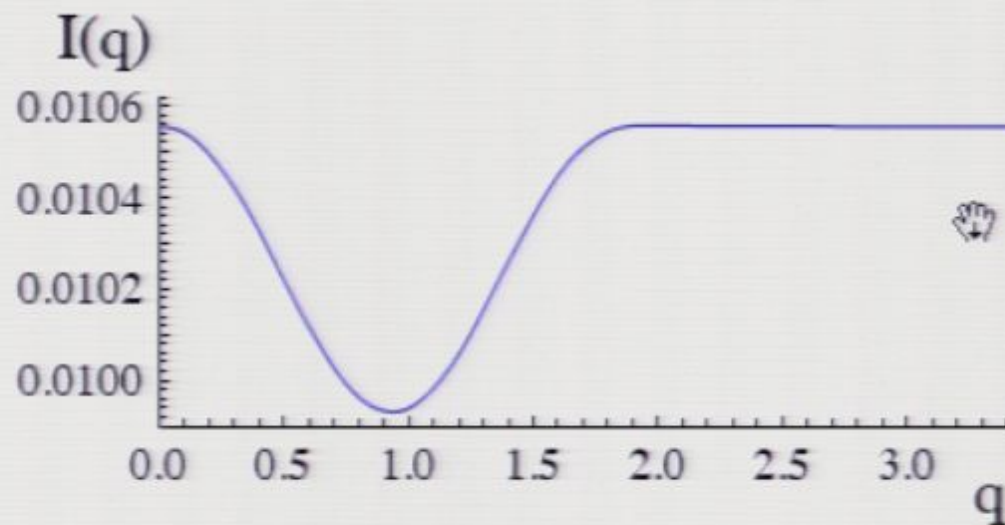


# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- **Yang-Mills contribution to gravity**

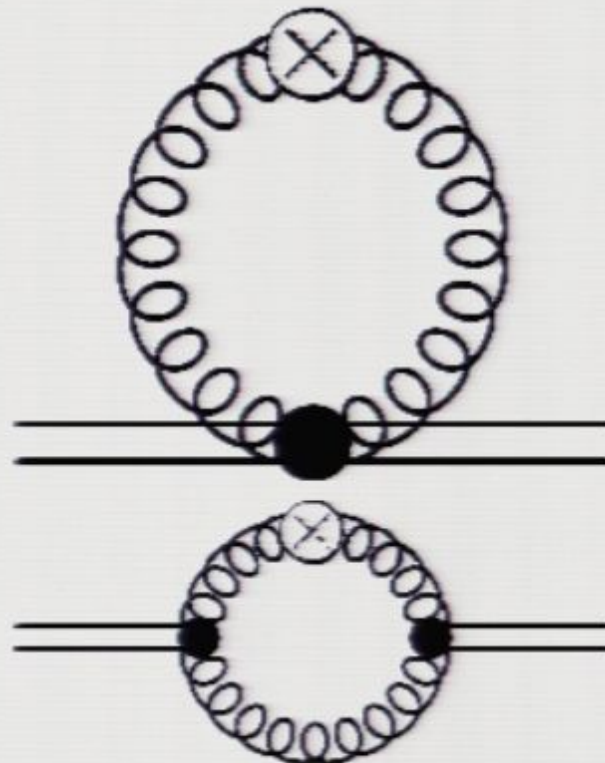
rhs of flow equation (optimised cutoff)



# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- Yang-Mills contribution to gravity diagrams

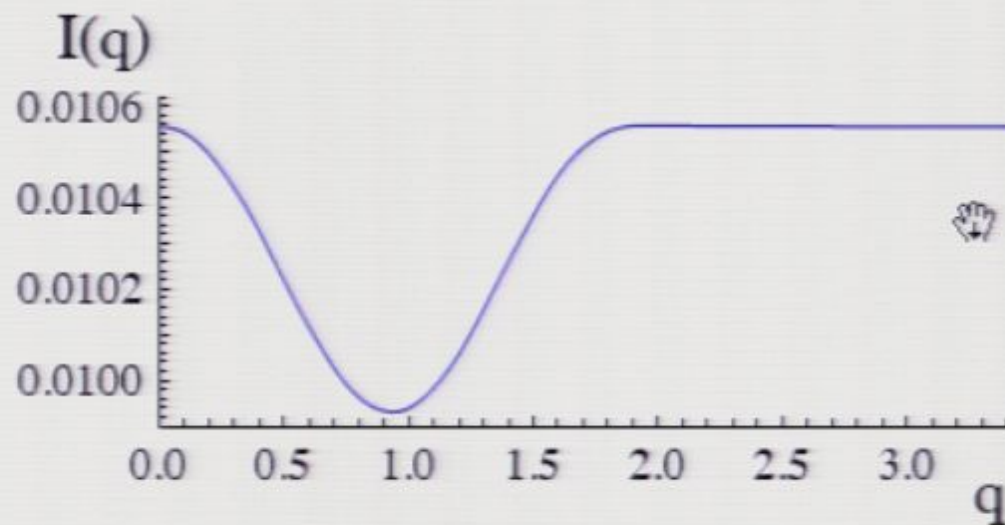


# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- **Yang-Mills contribution to gravity**

rhs of flow equation (optimised cutoff)



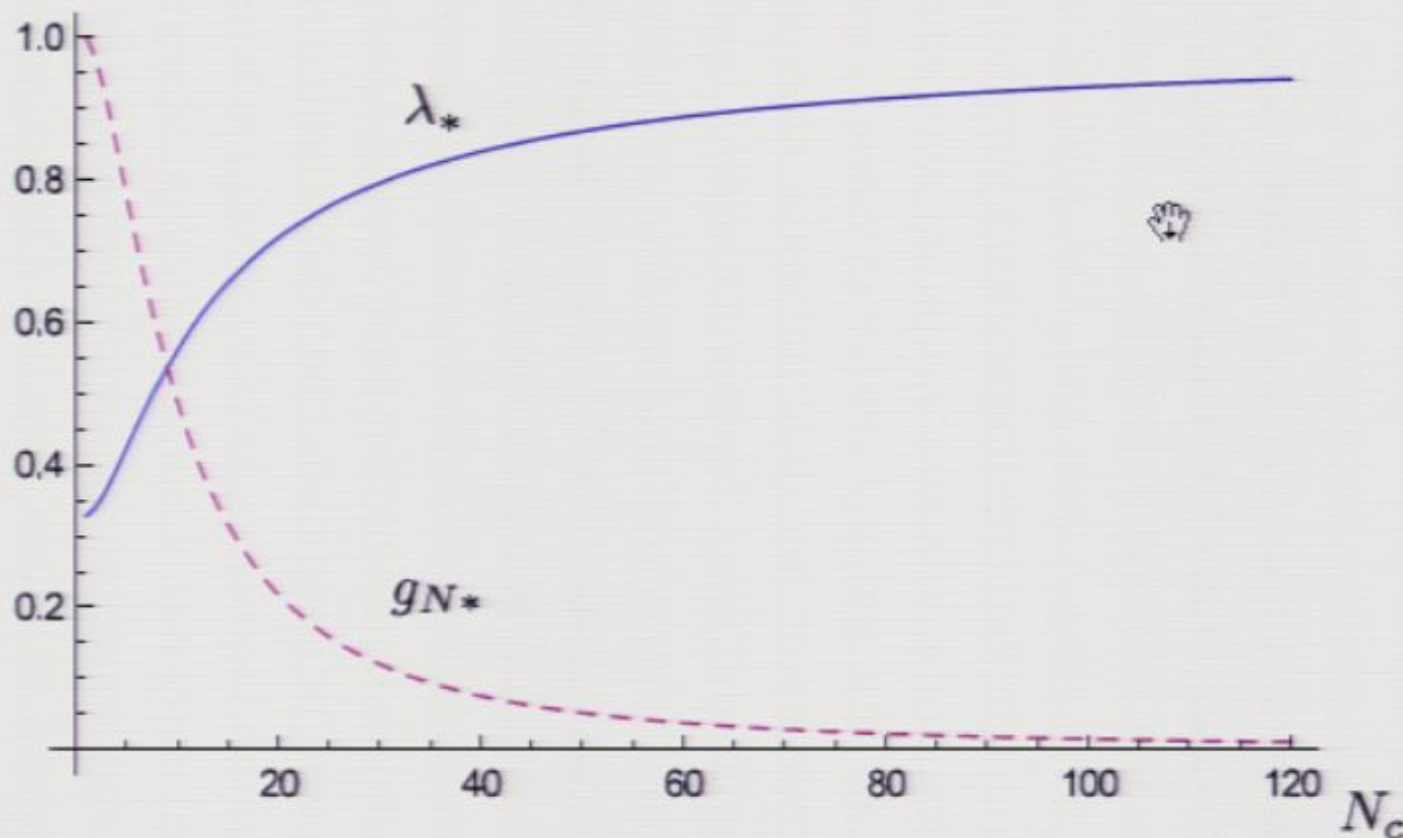


# Yang-Mills + gravity

S. Folkerts, DL, JM. Pawłowski ('09)

- **Yang-Mills contribution to gravity**

UV fixed point of coupled system



# phenomenology for asymptotic safety



# phenomenology for asymptotic safety

- low-scale quantum gravity

what if the **fundamental** Planck scale  $M_D$  obeys

$$M_D \approx \mathcal{O}(M_{EW}) \approx \mathcal{O}(1\text{TeV}) \ll M_{Pl}$$

quantum gravity accessible at colliders



# phenomenology for asymptotic safety

- low-scale quantum gravity

what if the **fundamental** Planck scale  $M_D$  obeys

$$M_D \approx \mathcal{O}(M_{EW}) \approx \mathcal{O}(1\text{TeV}) \ll M_{Pl}$$

quantum gravity accessible at colliders

- large extra dimensions

(Arkani-Hamed, Dimopoulos, Dvali '98)

D=4+n compact spatial dimensions

compact extra dimensions  $M_{\text{Planck}}^2 \sim M_D^2 (M_D L)^n$

roughly  $L \sim 10^{\frac{30}{n}-17} \text{cm} \left(\frac{1\text{TeV}}{m_{EW}}\right)^{1+\frac{2}{n}}$

scale separation  $1/L \ll M_D \ll M_{\text{Planck}}$

# gravitational fixed point

DL ('03), P. Fischer, DL ('06)

- **higher dimensions**

critical dimension for gravity  $D = 2$

expect similarities under RG flow for  $D > 2$



# gravitational fixed point

DL ('03), P. Fischer, DL ('06)

- **higher dimensions**

critical dimension for gravity  $D = 2$

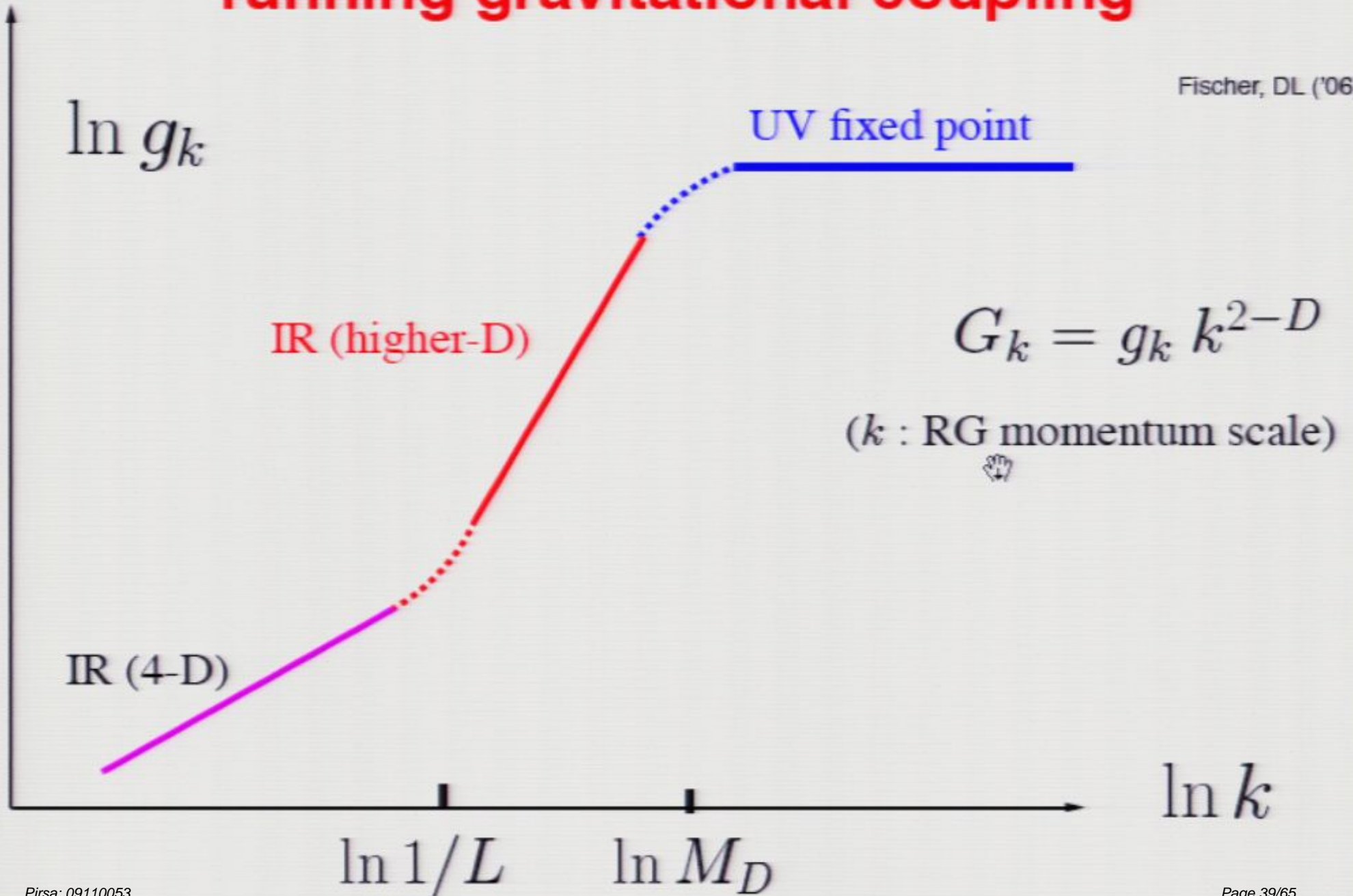
expect similarities under RG flow for  $D > 2$

- **Einstein-Hilbert scaling exponents**

$\theta'$	pow	mexp	exp	mod	opt
$D = 4$	1.63	1.51	1.53	1.51	1.48
5	3.19	2.80	2.83	2.77	2.69
6	5.31	4.58	4.60	4.50	4.33
7	7.83	6.71	6.68	6.54	6.27
8	10.7	9.14	9.03	8.86	8.46
9	13.9	11.9	11.6	11.4	10.9
10	17.4	14.9	14.5	14.2	13.5
11	21.3	18.2	17.6	17.3	16.4

# running gravitational coupling

Fischer, DL ('06)



# gravitational fixed point

DL ('03), P. Fischer, DL ('06)

- **higher dimensions**

critical dimension for gravity  $D = 2$

expect similarities under RG flow for  $D > 2$

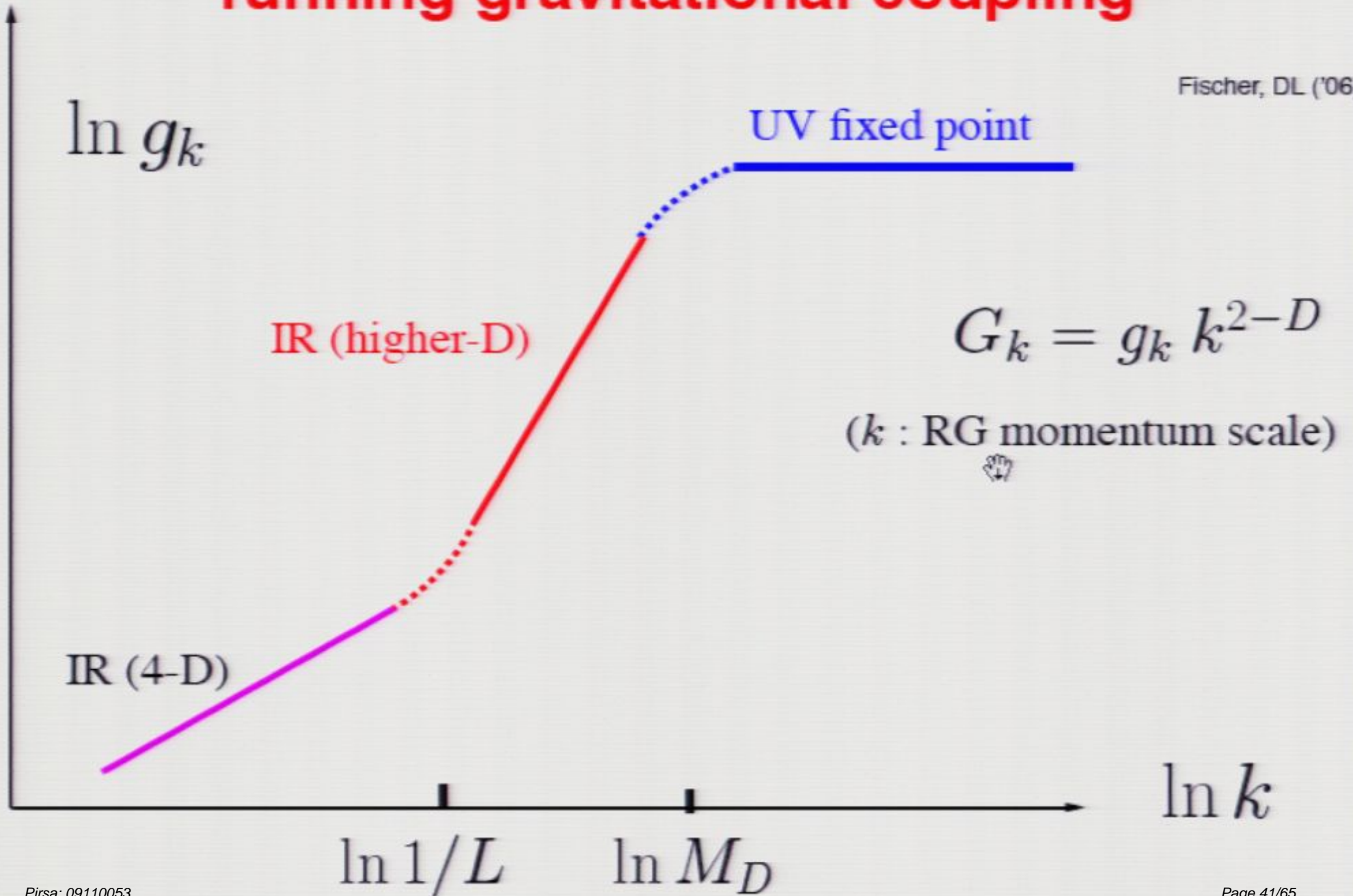
- **weak cutoff sensitivity**

$\tau$	pow	mexp	exp	mod	opt
$D = 4$	0.132	0.132	0.134	0.135	0.137
5	0.463	0.461	0.468	0.469	0.478
6	0.943	0.933	0.946	0.946	0.963
7	1.528	1.502	1.521	1.521	1.544
8	2.186	2.142	2.165	2.162	2.192
9	2.900	2.834	2.858	2.853	2.888
10	3.655	3.568	3.591	3.585	3.623
11	4.445	4.336	4.356	4.348	4.389



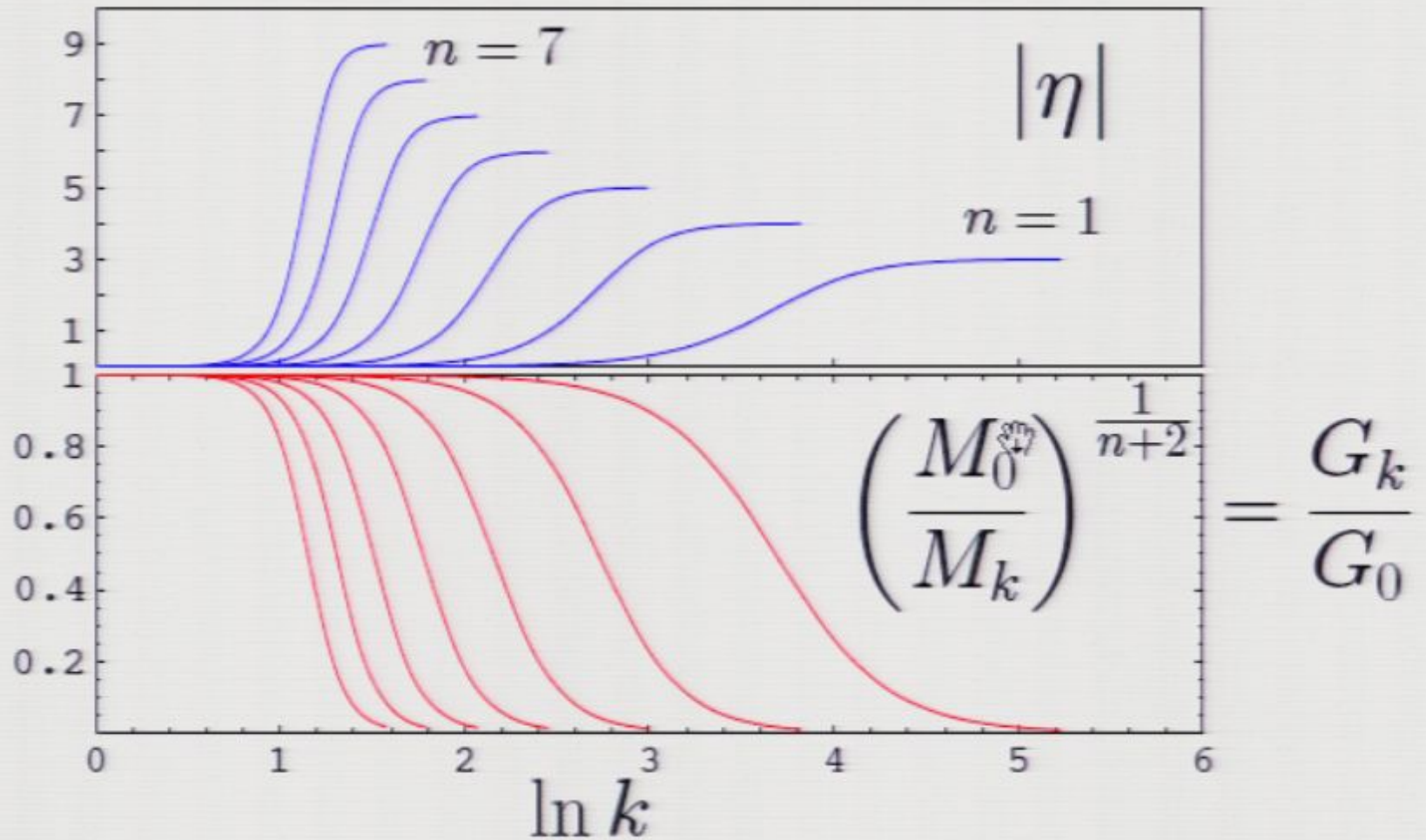
# running gravitational coupling

Fischer, DL ('06)



# RG running and anomalous dimension

DL ('03), Fischer, DL ('05,'06)



# collider signatures of quantum gravity

- **real gravitons**

graviton production via  $p p \rightarrow \text{jet} + G$

**signature:** missing energy



# collider signatures of quantum gravity


- **real gravitons**

graviton production via  $p p \rightarrow \text{jet} + G$

**signature:** missing energy

- **virtual gravitons**

lepton production  $q\bar{q} \rightarrow \ell^+ \ell^-$  via graviton exchange

**signature:** deviations in SM reference processes 

- **mini-black holes**

black hole production and decay

**signature:** spectacular (many body final states)

# gravitational Drell-Yan

- **effective theory** Giudice, Rattazzi, Wells ('98)

scattering amplitude for Drell-Yan lepton production

$$A = \mathcal{S}(s) \times T, \quad T = T^{\mu\nu} T_{\mu\nu} - \frac{1}{n+2} T_{\mu}^{\mu} T_{\nu}^{\nu}$$

$$\mathcal{S}(s) = \frac{1}{M_D^{n+2}} \int_0^{\infty} dm_{kk} m_{kk}^{n-1} \frac{1}{s + m_{kk}^2} \quad \text{✎}$$

UV divergent for  $n \geq 2$ .

# collider signatures of quantum gravity


- **real gravitons**

graviton production via  $p p \rightarrow \text{jet} + G$

**signature:** missing energy

- **virtual gravitons**

lepton production  $q\bar{q} \rightarrow \ell^+ \ell^-$  via graviton exchange

**signature:** deviations in SM reference processes 

- **mini-black holes**

black hole production and decay

**signature:** spectacular (many body final states)

# gravitational Drell-Yan

- **effective theory** Giudice, Rattazzi, Wells ('98)

scattering amplitude for Drell-Yan lepton production

$$A = \mathcal{S}(s) \times T, \quad T = T^{\mu\nu} T_{\mu\nu} - \frac{1}{n+2} T^\mu{}_\mu T^\nu{}_\nu$$

$$\mathcal{S}(s) = \frac{1}{M_D^{n+2}} \int_0^\infty dm_{kk} m_{kk}^{n-1} \frac{1}{s + m_{kk}^2}$$

UV divergent for  $n \geq 2$ .

# collider signatures of quantum gravity


- **real gravitons**

graviton production via  $p p \rightarrow \text{jet} + G$

**signature:** missing energy

- **virtual gravitons**

lepton production  $q\bar{q} \rightarrow \ell^+ \ell^-$  via graviton exchange

**signature:** deviations in SM reference processes 

- **mini-black holes**

black hole production and decay

**signature:** spectacular (many body final states)



# gravitational Drell-Yan

- **effective theory** Giudice, Rattazzi, Wells ('98)

scattering amplitude for Drell-Yan lepton production

$$A = \mathcal{S}(s) \times T, \quad T = T^{\mu\nu} T_{\mu\nu} - \frac{1}{n+2} T_{\mu}^{\mu} T_{\nu}^{\nu}$$

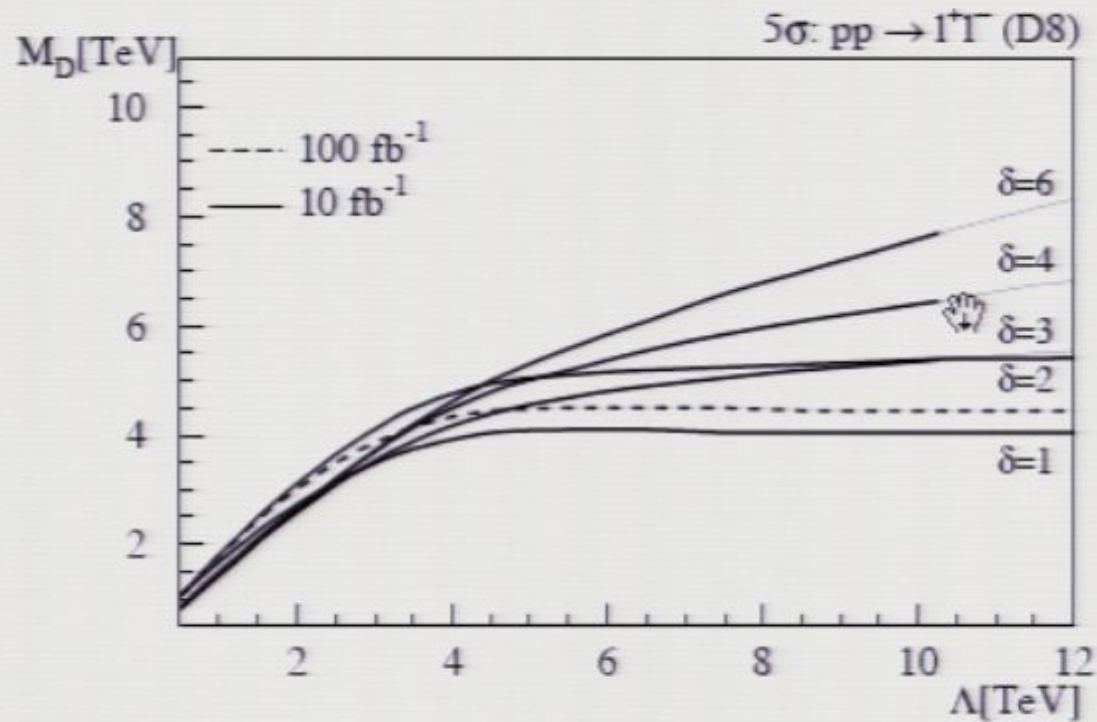
$$\mathcal{S}(s) = \frac{1}{M_D^{n+2}} \int_0^{\infty} dm_{kk} m_{kk}^{n-1} \frac{1}{s + m_{kk}^2} \quad \text{✎}$$

UV divergent for  $n \geq 2$ .

# gravitational Drell-Yan

- effective theory + Monte Carlo simulations

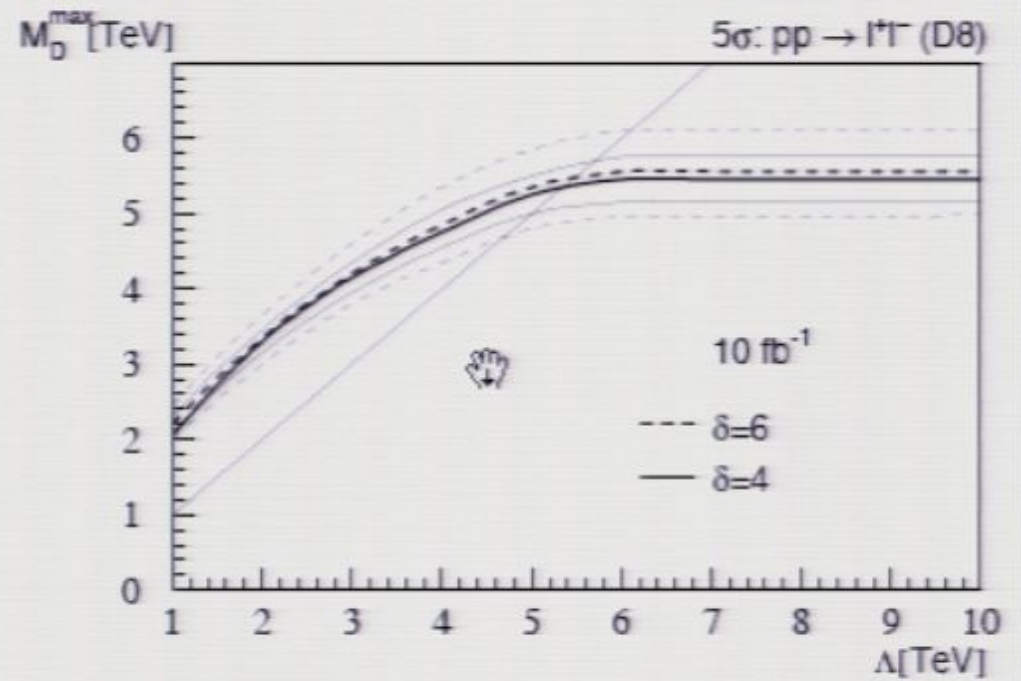
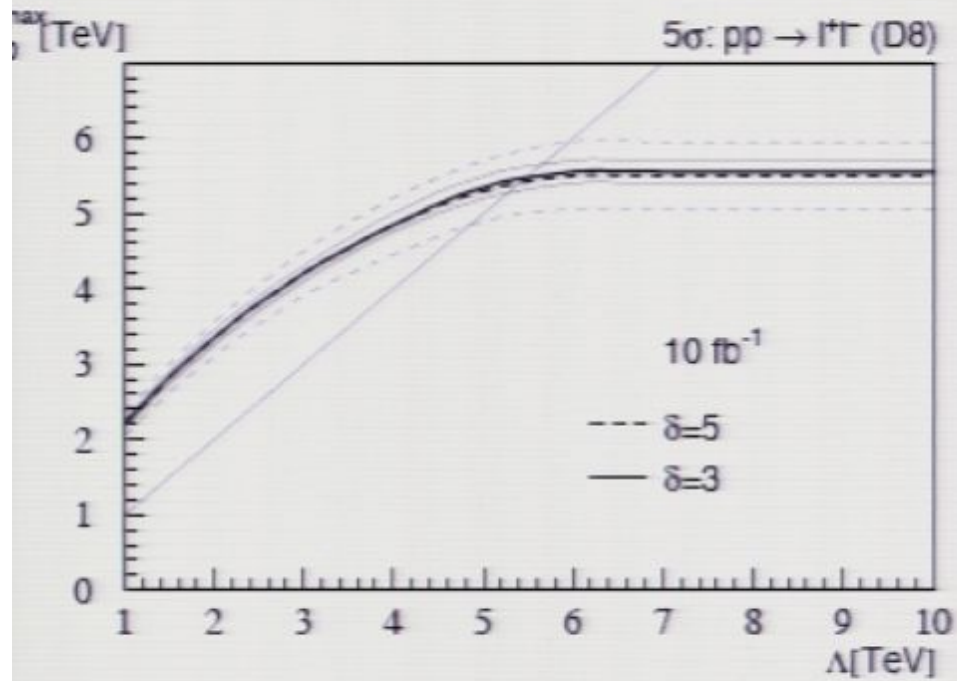
Giudice, Plehn, Strumia ('04)



# gravitational Drell-Yan

- renormalisation group + Monte Carlo simulation

DL, Plehn ('07)



# black holes at the LHC

Dimopoulos, Landsberg ('01)  
Giddings, Thomas ('01)

- **classical Schwarzschild black holes**

metric

$$ds^2 = -f(r) dt^2 + f^{-1}(r) dr^2 + r^2 d\Omega_{d-2}^2, \quad f = 1 - \frac{G_N M}{r^{d-3}}$$

classical Schwarzschild radius

$$r_{\text{cl}} = (G_N M)^{1/(d-3)}$$



- **production cross section**

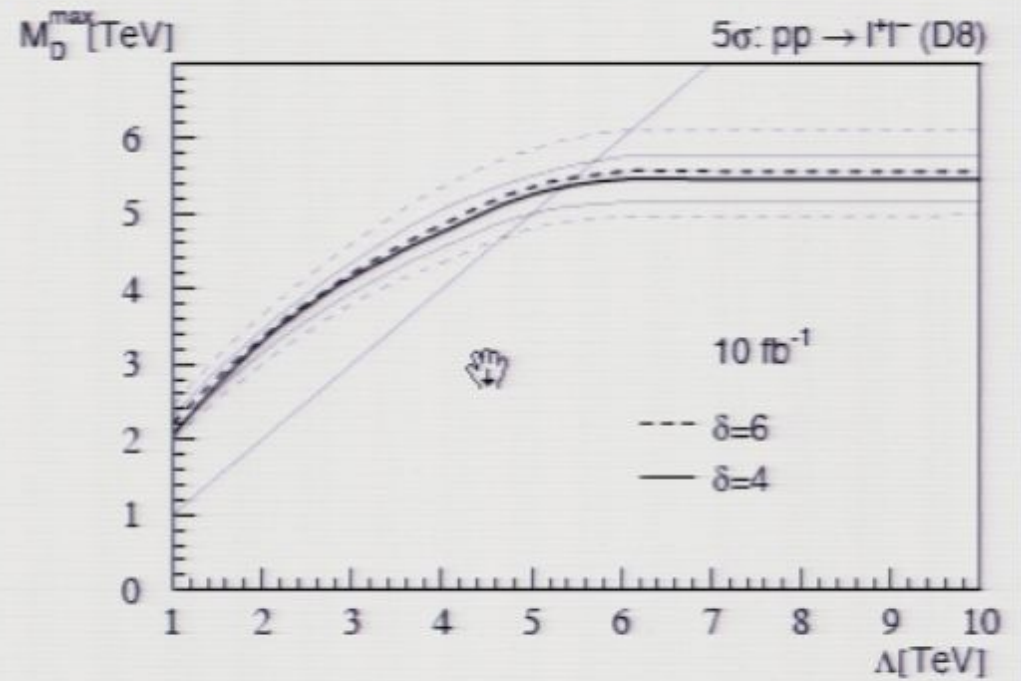
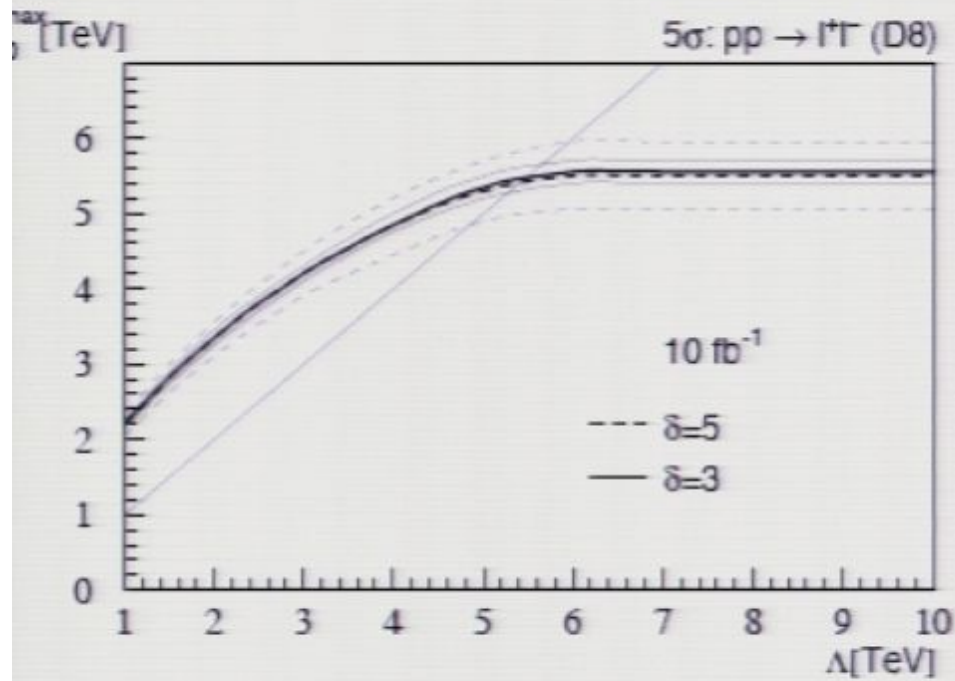
semi-classical  $\hat{\sigma} = F \times \pi r_{\text{cl}}^2 (M = \sqrt{s}) \times \theta(\sqrt{s} - M_{\text{min}})$

form factor  $F$

# gravitational Drell-Yan

- renormalisation group + Monte Carlo simulation

DL, Plehn ('07)



# black holes at the LHC

Dimopoulos, Landsberg ('01)  
Giddings, Thomas ('01)

- **classical Schwarzschild black holes**

metric

$$ds^2 = -f(r) dt^2 + f^{-1}(r) dr^2 + r^2 d\Omega_{d-2}^2, \quad f = 1 - \frac{G_N M}{r^{d-3}}$$

classical Schwarzschild radius

$$r_{\text{cl}} = (G_N M)^{1/(d-3)}$$



- **production cross section**

semi-classical  $\hat{\sigma} = F \times \pi r_{\text{cl}}^2 (M = \sqrt{s}) \times \theta(\sqrt{s} - M_{\text{min}})$

form factor  $F$

# black holes at the LHC

- **RG improved black holes**

K. Falls, DL, A. Raghuraman (ERG '08, '09)

running gravitational coupling

$$G_N \rightarrow G(r), \quad f(r) \rightarrow f_{\text{imp}}(r) = 1 - \frac{G(r) M}{r^{d-3}}$$

improved Schwarzschild radius  $r_s$  from

$$f'_{\text{imp}}(r_s) = 0$$

**critical** black hole mass  $M_c$  from

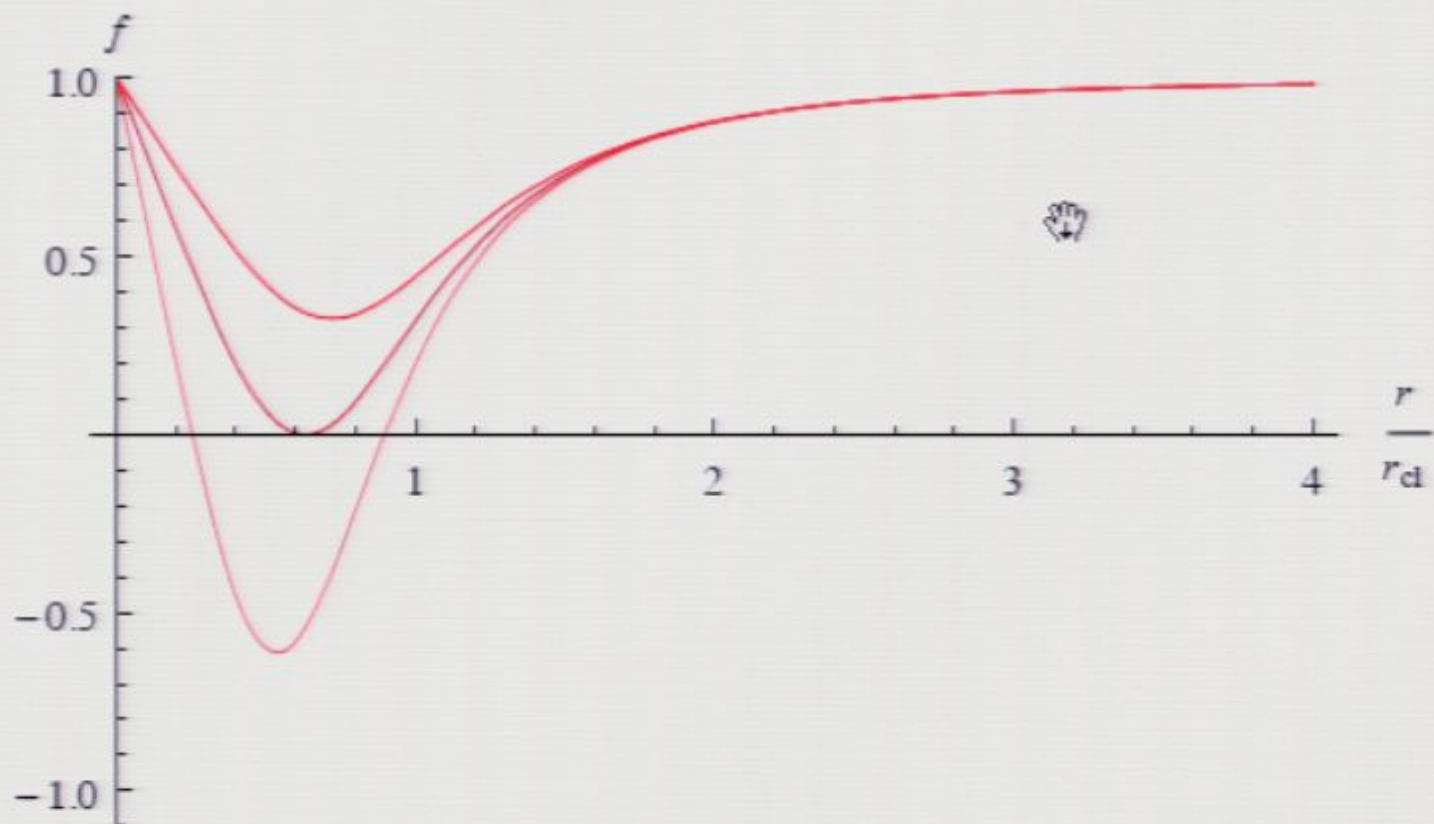
$$(d-3)M_c = r \partial_r G(r)|_{r=r_c(M_c)}$$

# black holes at the LHC

- **RG improved black holes**

K. Falls, DL, A. Raghuraman (ERG '08, '09)

smallest black hole  $M_c$   $D=6$ :



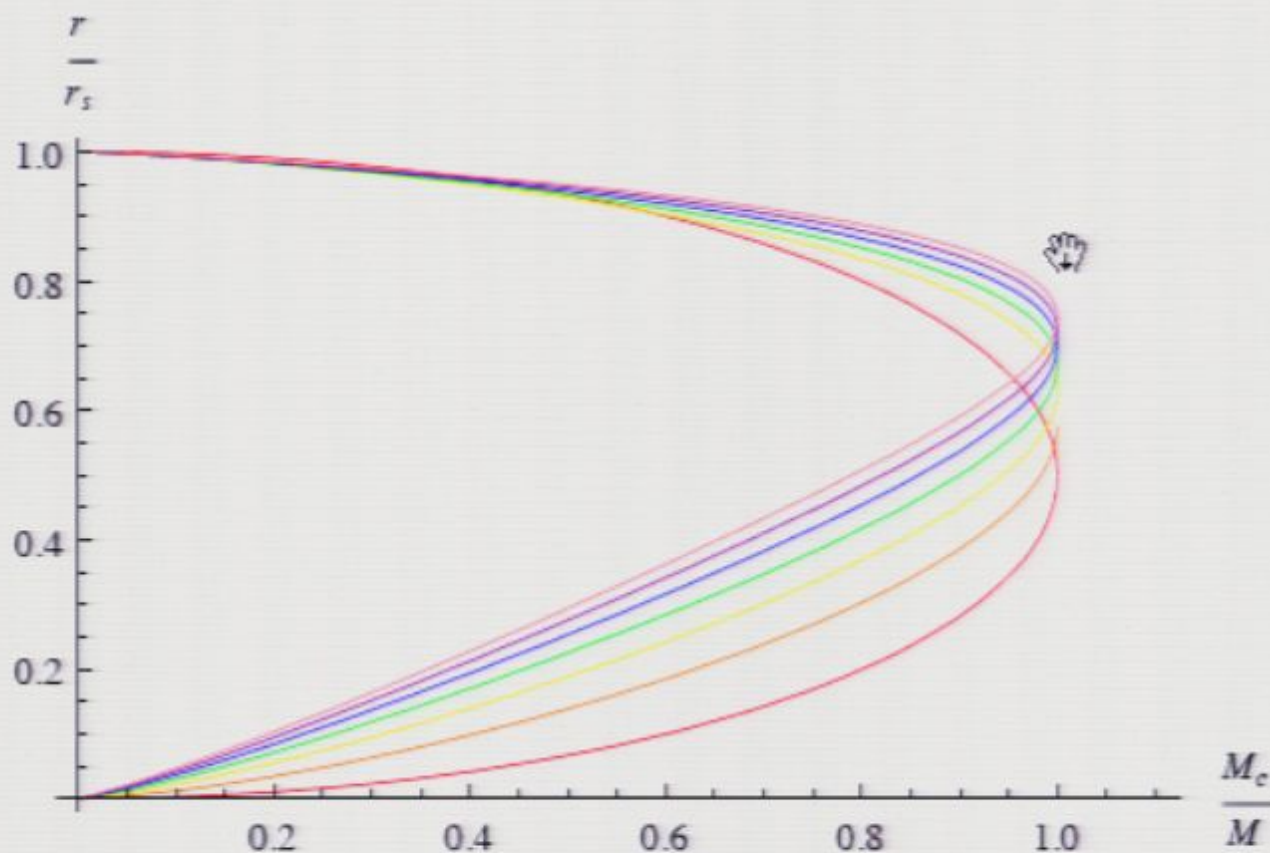


# black holes at the LHC

- **RG improved black holes**

K. Falls, DL, A. Raghuraman (ERG '08, '09)

improved Schwarzschild radii, various dimension



# black holes at the LHC

- semi-classical vs renormalisation group

G. Hiller, DL ('09)

elastic BH production  $pp \rightarrow \mathbf{BH}$

$$\frac{d\sigma}{dM} = \frac{2M}{s} \sum_{i,j} \int_{M^2/s}^1 \frac{dx}{x} f_i \left( \frac{M^2}{xs} \right) f_j(x) \hat{\sigma}(q_i q_j \rightarrow \mathbf{BH})|_{\hat{s}=M^2}.$$

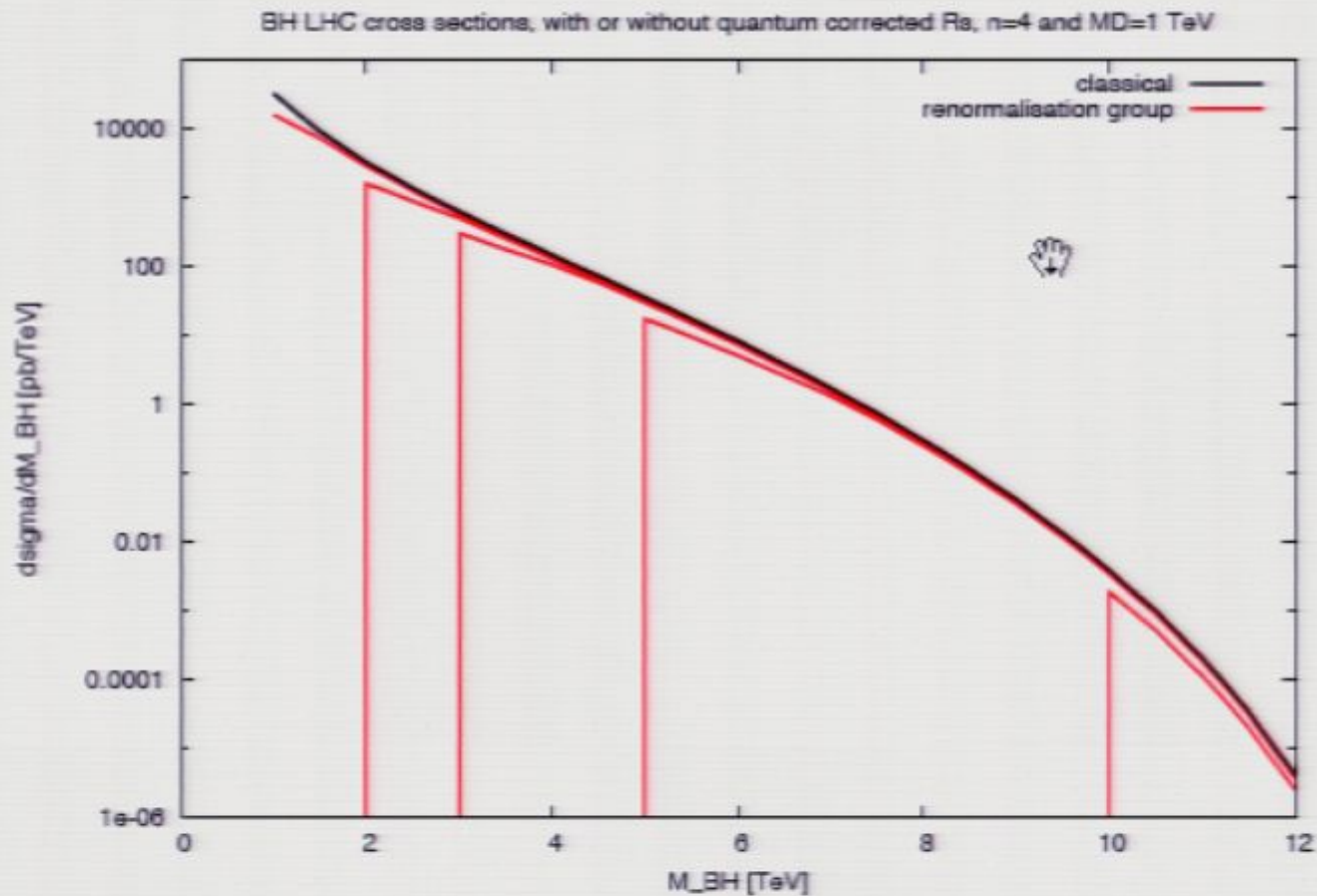
parton distribution functions from **CTEQ61**  
evaluated at  $Q^2 = M_{\mathbf{BH}}^2$ .

# black holes at the LHC

- semi-classical vs renormalisation group

G. Hiller, DL ('09)

$n = 4$  extra dimensions



# unitarity bounds

J. Brinkmann, G. Hiller, DL ('09)

- **Higgs-Higgs elastic scattering**

extra dimensions, gravity-mediated, KK modes

effective theory study X.G. He ('00)

partial wave decomposition:

$$M(s, t) = 16\pi \sum_J (2J + 1) a_J(s) P_J(\cos \theta), \quad t = t(\cos \theta)$$

$$\sigma \approx 16\pi \frac{|a_0(s)|^2}{s}, \quad a_0(s) = \frac{1}{16\pi} \frac{1}{s - 4m_h^2} \int_{4m_h^2 - s}^0 dt M(s, t)$$

optical theorem, unitarity bound

$$|a_0(s)| \leq 1$$

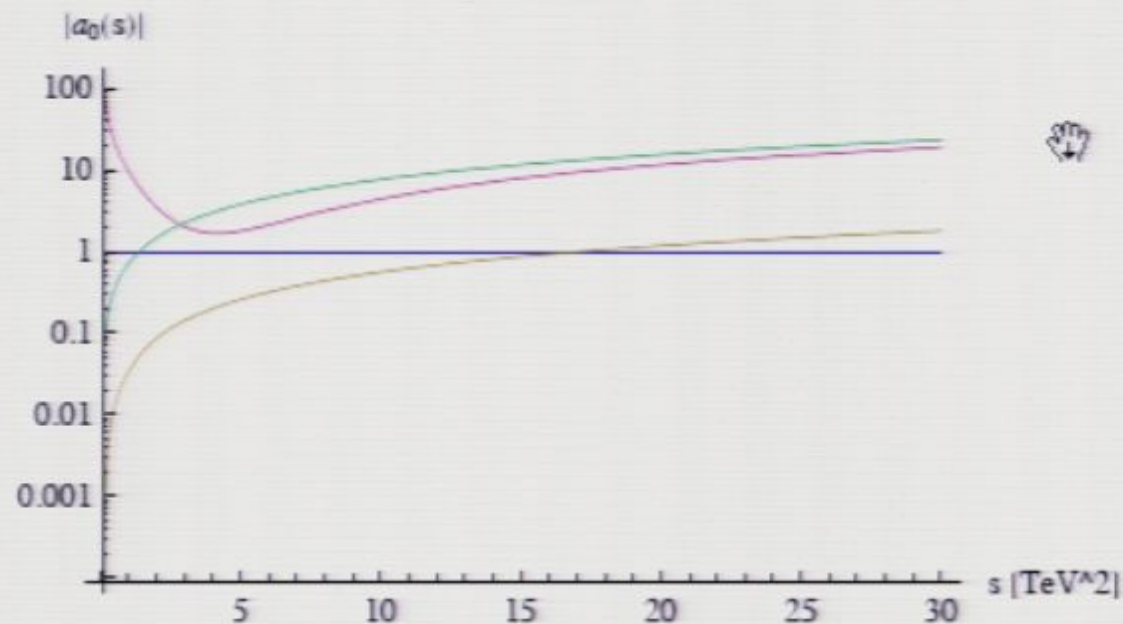
# unitarity bounds

- results

$$|a_0(s)| \rightarrow c_n \frac{s}{M_D^2}$$

effective theory: valid for  $s < M_D^2$

RG study:  $c_n \ll 1$  J. Brinkmann, G. Hiller, DL ('09)



# conclusions

- **30 years of asymptotic safety**  
fascinating idea, many scenarios



# conclusions

- **30 years of asymptotic safety**

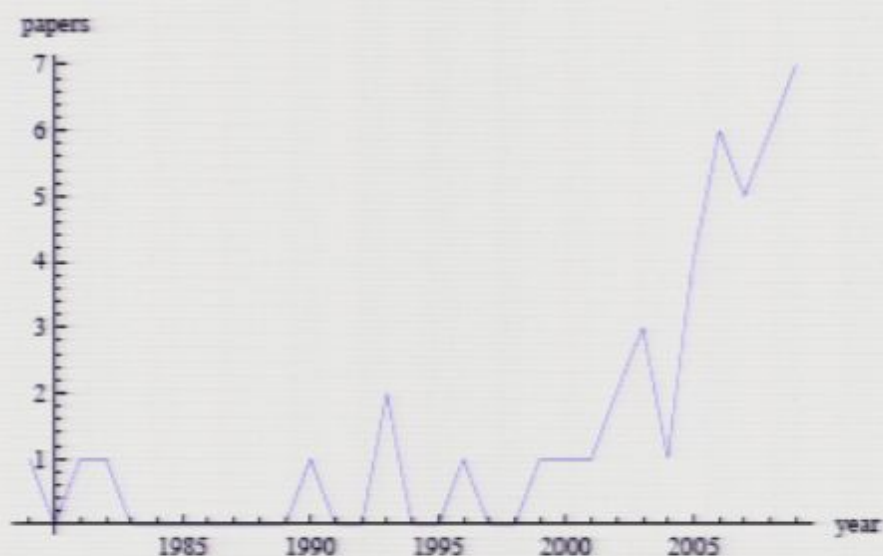
fascinating idea, many scenarios

- **asymptotic safety for quantum gravity and beyond**

tools are available

eg. PT / renormalisation group / lattice

results promising, increased activity level



# conclusions

- **30 years of asymptotic safety**

fascinating idea, many scenarios

- **asymptotic safety for quantum gravity and beyond**

tools are available

eg. PT / renormalisation group / lattice

results promising, increased activity level



- **phenomenology of asymptotic safety**

cosmology, physics of black holes

particle physics models, signatures at colliders



# conclusions

- **30 years of asymptotic safety**

fascinating idea, many scenarios

- **asymptotic safety for quantum gravity and beyond**

tools are available

eg. PT / renormalisation group / lattice

results promising, increased activity level



- **phenomenology of asymptotic safety**

cosmology, physics of black holes

particle physics models, signatures at colliders

- **challenges for theory and experiment**

physics at the Planck scale

lattice  $\leftrightarrow$  continuum RG  $\leftrightarrow$  spin foams  $\leftrightarrow$  LQG