

Title: The Search for the Perfect Language

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Abstract: I will tell how the story given in Umberto Eco's book The Search for the Perfect Language continues with modern work on logical and programming languages.(For more information, see <http://www.umcs.maine.edu/~chaitin/hu.html>.)

The Search for the Perfect Language
Gödel, Turing, ...
<http://www.cs.umaine.edu/~vcharitin/ha.html>

Raymond $L_{u,v} \approx 1200$



Raymond Lull ≈ 1200



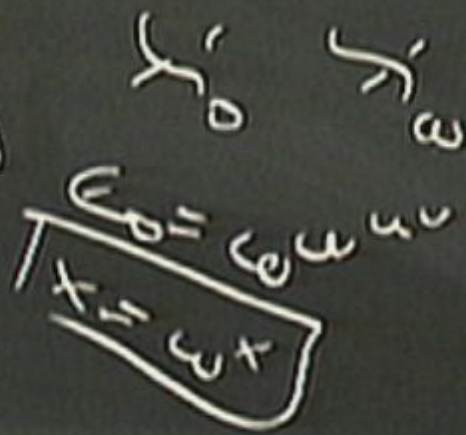
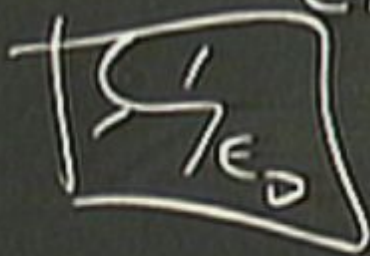
Leibniz

characterica Universalis

Infinite Sets
Cantor

Infinite Sets

Cantor



The Search for the Perfect Language
Umberto Eco + A. I. Bar-Tal, Eschler, Turing, ...
<http://www.cs.umaine.edu/~vchaitin/ha.html>



Infinite Sets

Cantor

$\mathbb{Z} \neq \mathbb{C}$

$\mathbb{R} \neq \mathbb{C}$

x_0

x_1

$x_0, x_1, x_2, x_3, \dots$



Infinite Sets

Cantor

ZFC

\aleph_0

\aleph_1

\aleph_2

Boström

Russell

$\aleph_0, \aleph_1, \aleph_2, \dots$

The Search for the Perfect Language
Gödel, Church, Turing, ...

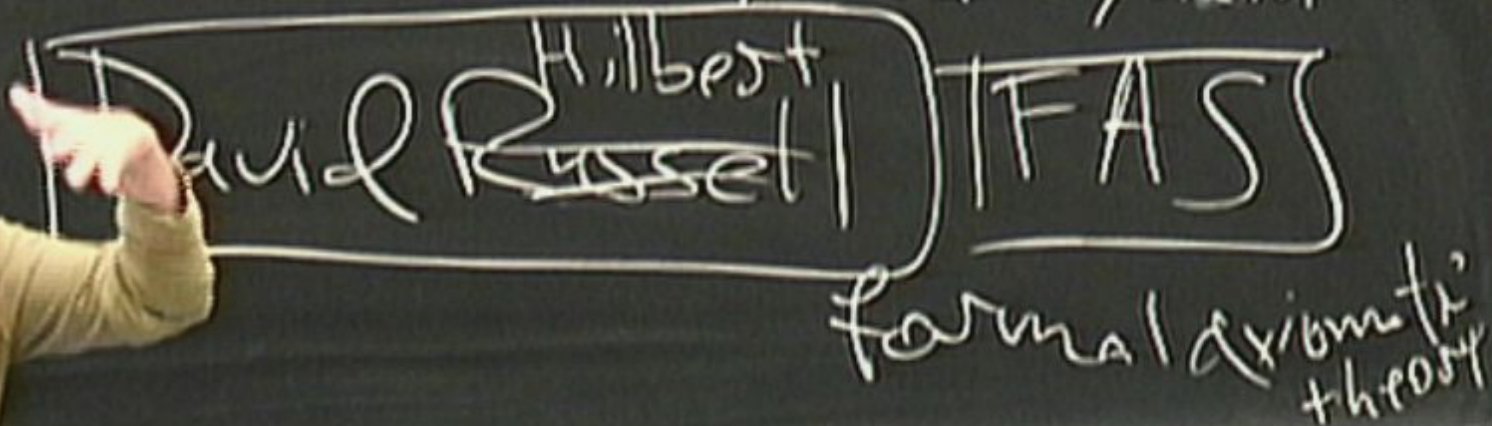
<http://www.cs.umaine.edu/~nchaitin/ha.html>

Hilbert
David Russell | I F A S
formal axiomatic

The Search for the Perfect Language

Umberto Eco + Hilbert, Gödel, Turing, ...

<http://www.cs.umaine.edu/~velho/in/ha.html>



The Search for the Perfect Language
Gödel, Church, Turing, ...

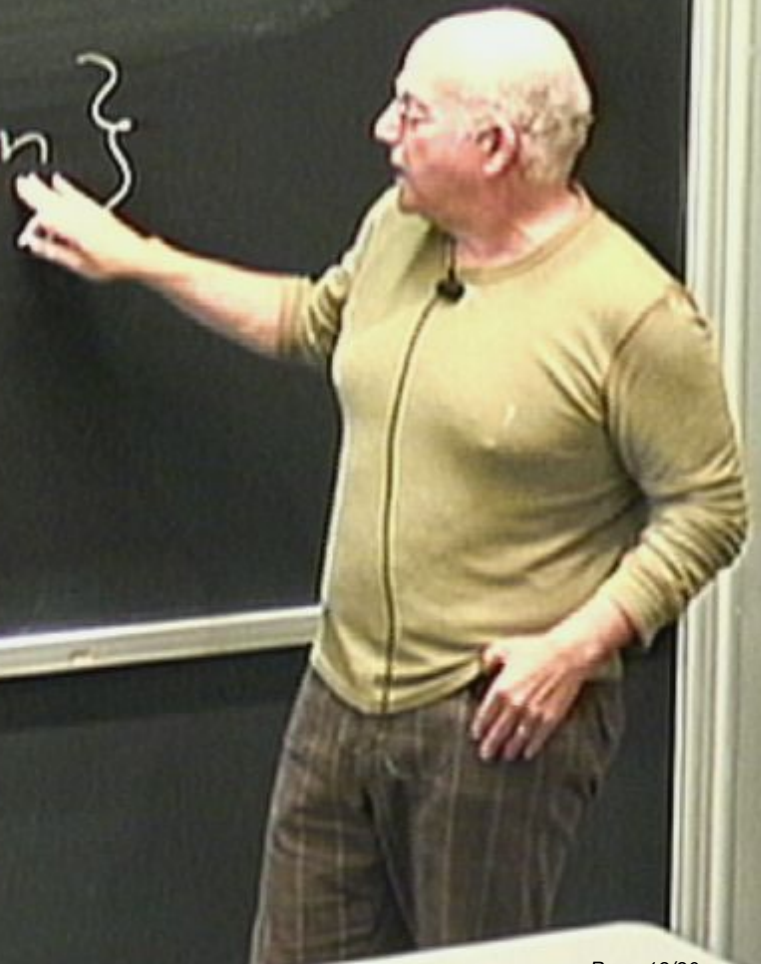
<http://www.cs.umaine.edu/~velho/in/ha.html>

Hilbert
David ~~Russell~~ | I F A S

formal axiomatic
theory

$$0 = \{\}$$

$$n+1 = \{0, 1, 2, \dots, n\}$$



CAUTION
DO NOT TOUCH
EQUIPMENT

Goal 1931
Tunji 1935

Gold 1931
Turing 1935

"This stmt is ~~the~~!"
"unprovable!"

Gödel (1931) "This stmt is ~~the~~!"
Turing (1936) "unprovable!"
uncomputability

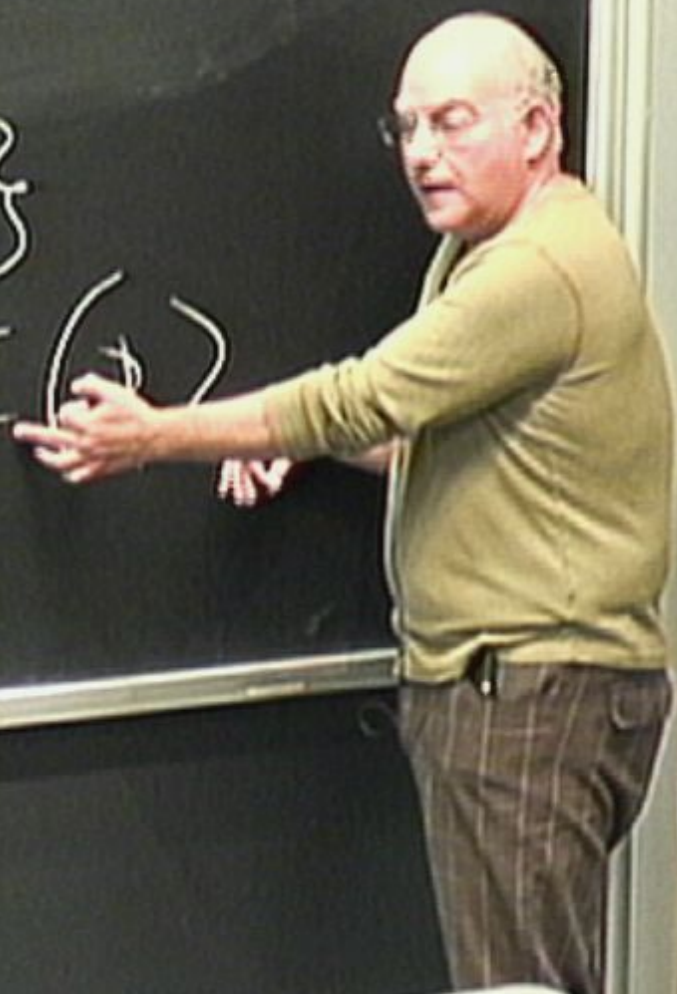
Goedel 1931 "This stmt is ~~the~~!"
Turing 1935 "unprovable!"
universal TM
uncomputability programming

Gold 1931 "this stmt is ~~the~~"
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Turing 1935 universal TM
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Gold 1931 "this stmt is ~~the~~!"
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universal TM
uncomputability
AIT randomness
programming

Goedel 1931 "This stmt is ~~the~~!"
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universal TM
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programming
|||||
,9999

$$0 = \{\}$$
$$n+1 = \{0, 1, 2, \dots, n\}$$
$$U(\mathbb{P} \subset \mathbb{P}) = C(\#)$$



CAUTION
DO NOT TOUCH
EQUIPMENT

$$0 = \{\}$$
$$n+1 = \{0, 1, 2, \dots, n\}$$
$$\mathcal{U}(\mathcal{P} \subset \mathcal{P}) = \mathcal{C}(\mathcal{P})$$



$$0 = \{ \}$$

$$n+1 = \{ 0, 1, 2, \dots, n \}$$

$$U(\mathbb{T} \subset \mathbb{P}) = \mathbb{C}(\mathbb{P})$$

$$0000 \mid \quad 0 \rightarrow 00 \mid \rightarrow 11 \quad 01$$

1960s ✓
1970s AIT

$$0 = \{ \}$$

$$n+1 = \{0, 1, 2, \dots, n\}$$

$$H(\mathbb{P}) = C(\mathbb{P})$$

$$0000 \mid \quad 0 \rightarrow 00 \mid \rightarrow 11 \quad 01$$

1960s ✓

1970s $n + \log_2 n$

$n + H(n)$

$$O = \{ \}$$

$$n+1 = \{ 0, 1, 2, \dots, n \}$$

$$U(\Pi_C P) = C(P)$$

0000 | $0 \rightarrow 00 \quad 1 \rightarrow 11 \quad 01$

1960s ✓

1970s

$$n + \log_2 n$$

$$n + H(n)$$

$$\Omega = \sum 2^{-|p|}$$

p helts

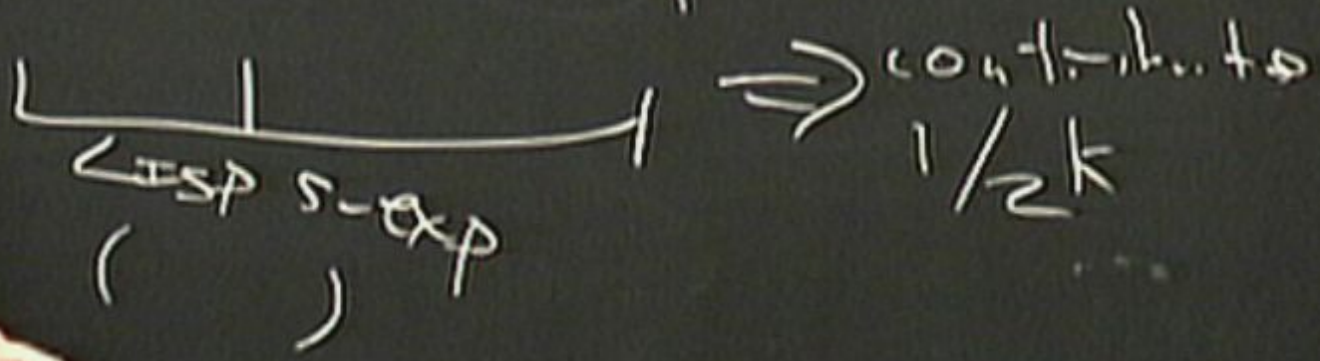
p has k bits

\Rightarrow contributes
 $1/2^k$

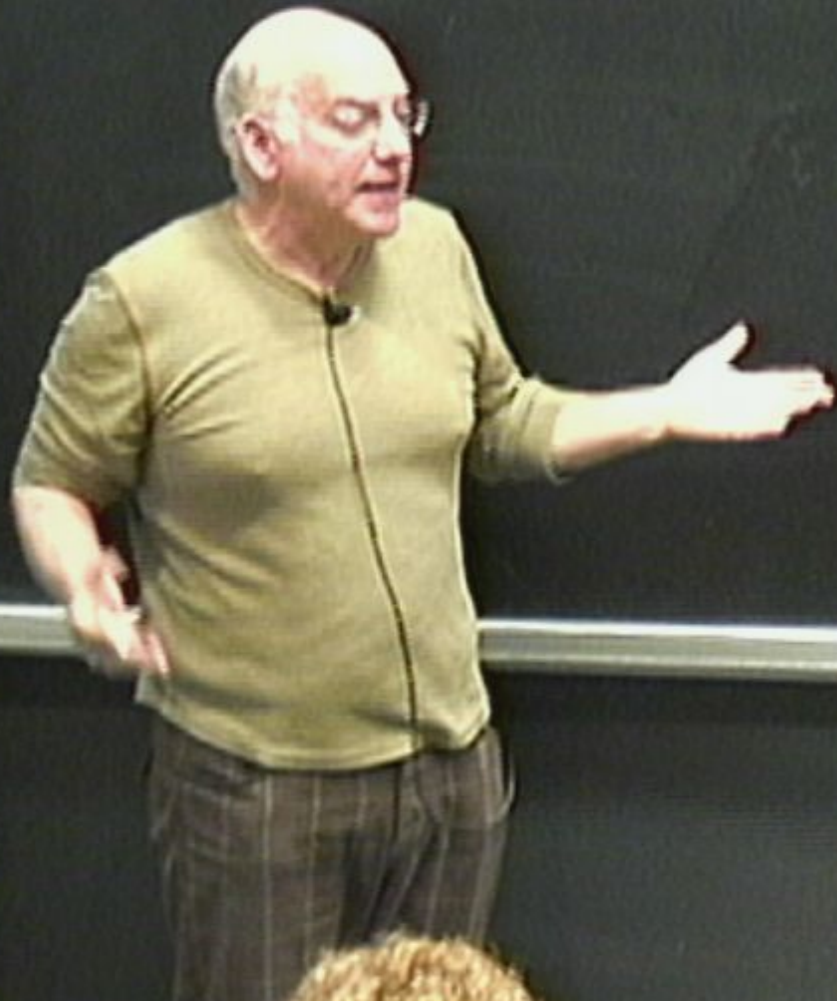
$$\text{OR } \Omega = \sum_{p \text{ bits}} 2^{-|p|} \leq 1$$

p bits

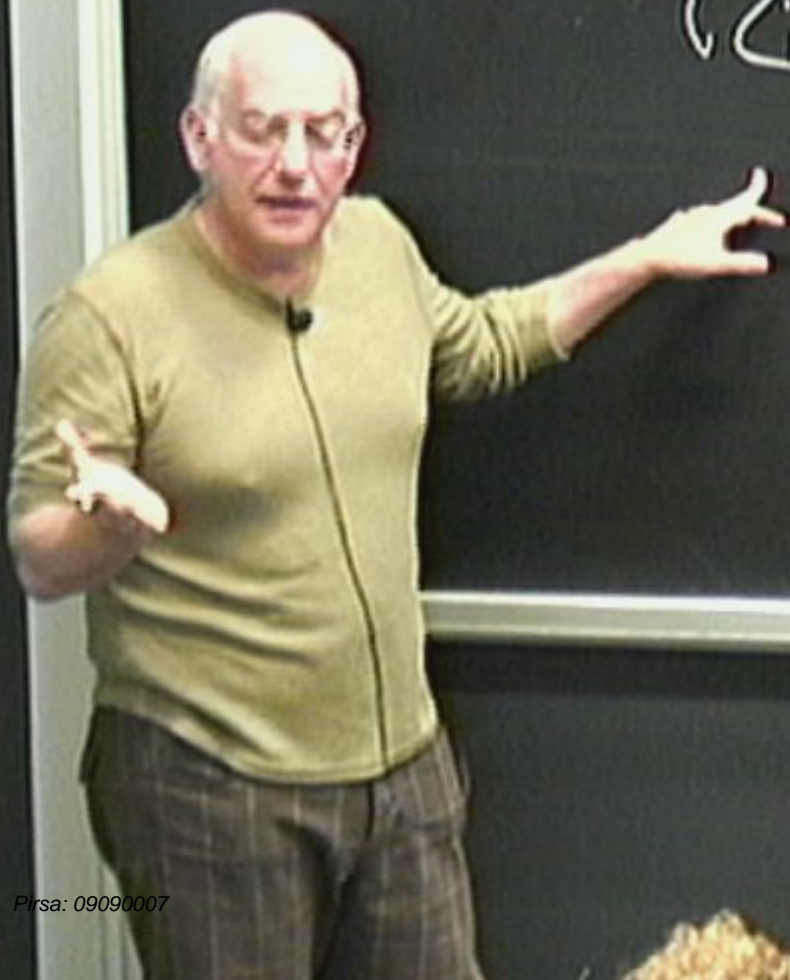
p has k bits



$P \neq NP$



$P \neq NP$
Riemann



$P \neq NP$
Riemann
 $\mathbb{R}F$ + projective
determinacy