Title: An Introduction to Quantum Information

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Abstract: A game that illustrates that quantum theory requires non-locality; an overview of the concept and basic mathematics of entanglement; and the concept of spin introduced via a Stern Gerlach set-up.

# An Introduction to Quantum Information

**ISSYP 2009** 

#### A Game of Probabilities: Set-up

- Two people, called observers
- Two priors, duck or goose
- Two outcome choices, it or not it

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#### A Game of Probabilities: Part 1

#### How to win:

- If both observers have the same prior information, they both choose the same outcome.
- If the observers have different prior information, they choose the opposite outcomes.

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#### A Game of Probabilities: Part 3

#### How to win:

- If both observers have the prior, Goose, they both choose the opposite outcomes.
- 2. If both observers have the prior, Duck, they choose the same outcome.
- If the observers have different priors, they choose the same outcome.

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#### A Game of Probabilities: Part 3

#### How to win:

- If both observers have the prior, Goose, they both choose the opposite outcomes.
- If both observers have the prior, Duck, they choose the same outcome.
- If the observers have different priors, they choose the same outcome.

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What is the best probability of winning?

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- What is the best probability of winning?
- Classically, 75%

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- What is the best probability of winning?
- Classically, 75%
- With quantum systems, we can do better!

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#### Entanglement

"Spooky action-at-a-distance"

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$$ket \rightarrow |\psi\rangle$$

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$$tensor \rightarrow |\psi\rangle_A \otimes |\varphi\rangle_B$$

#### Composite system

Every composite system can be represented as

$$|\psi\rangle_{AB} = \sum_{i,j} c_{ij} |i\rangle_A \otimes |j\rangle_B$$

#### Separable states

• If 
$$|\psi\rangle_{AB} = |\psi\rangle_{A} \otimes |\varphi\rangle_{B}$$

where 
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## If a state is not separable, it is entangled!

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Separable or entangled?

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## So what does this math tell you?

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Separable or entangled?

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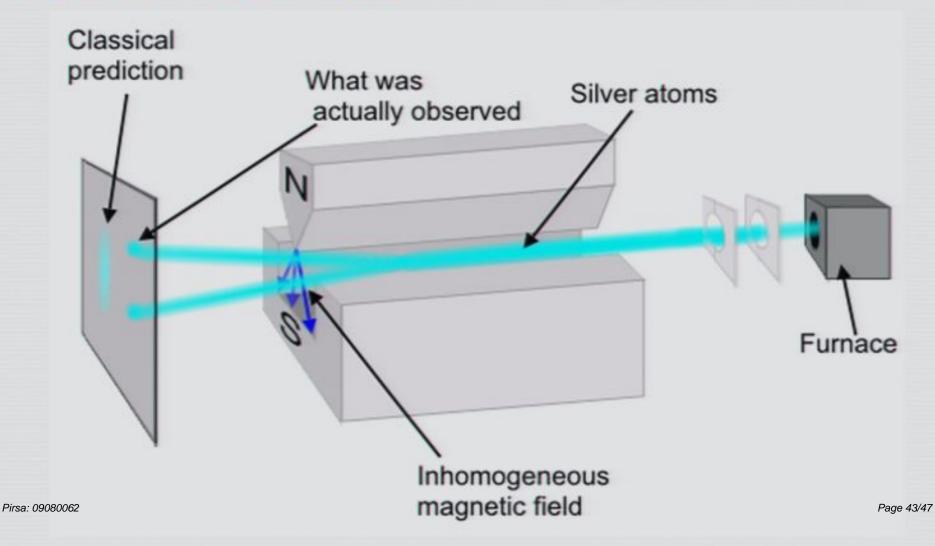
## So what does this math tell you?

### Spin

My favourite quantum feature

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#### Stern-Gerlach



#### Spin is...

- an intrinsic property
- equivalent to polarization for light (photons)
- the basis for the qubit
- weird

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#### Using spin: NMR

- Rough procedure: count number of protons, number of neutrons, and probe with EM radiation
- The spin of a molecule is dependent on the parity of the number of protons and the number of neutrons.
- Spin gives rise to a magnetic moment with a proportionality constant called the gyromagnetic ratio.
- NMR works on the principle that an object with a nonzero spin will absorb (and then emit) radiation at characteristic frequencies.

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