

Title: General Relativity 2

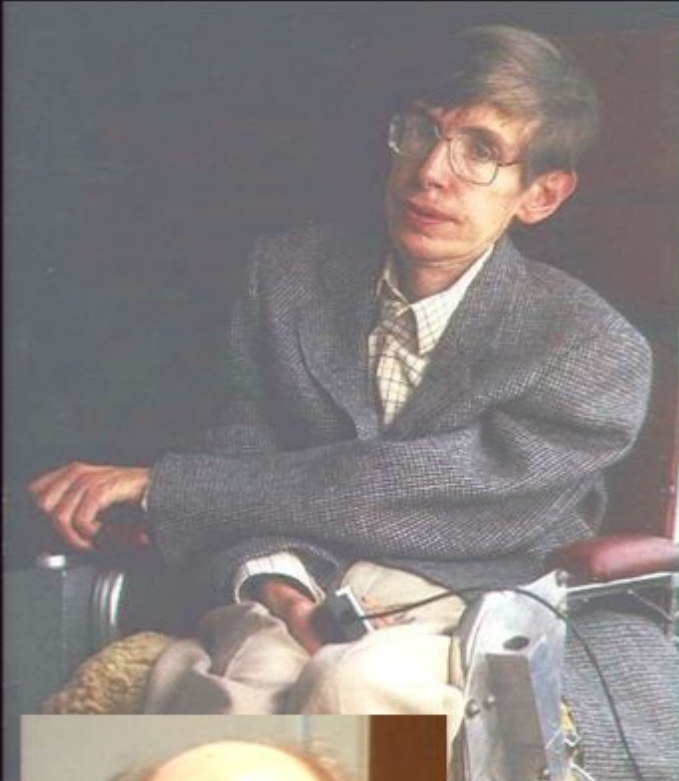
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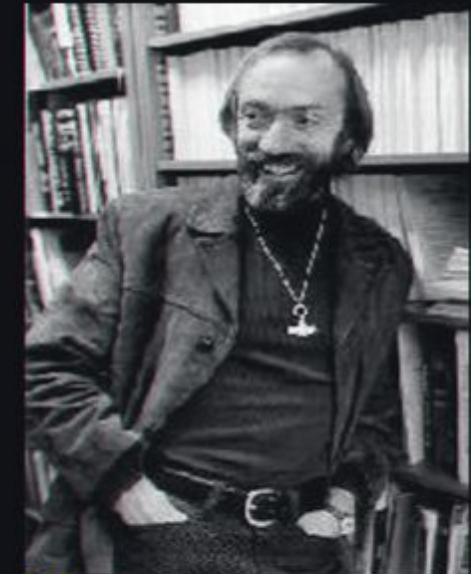
Abstract: The complete story of how the scientistsâ€™ had predicted the final stages of stars of varying masses: from the application of General Relativity, to the latest astronomical observations. Our journey starts with White Dwarfs and ends with a journey to and into a Black Hole and all the implications such a trip would hold for our visitor.

# The Blackhole Stars Today

*Hawking*



*Bekenstein*



*Thorne*

*Susskind*



Pirsa: 09080060

*Werner Israel*

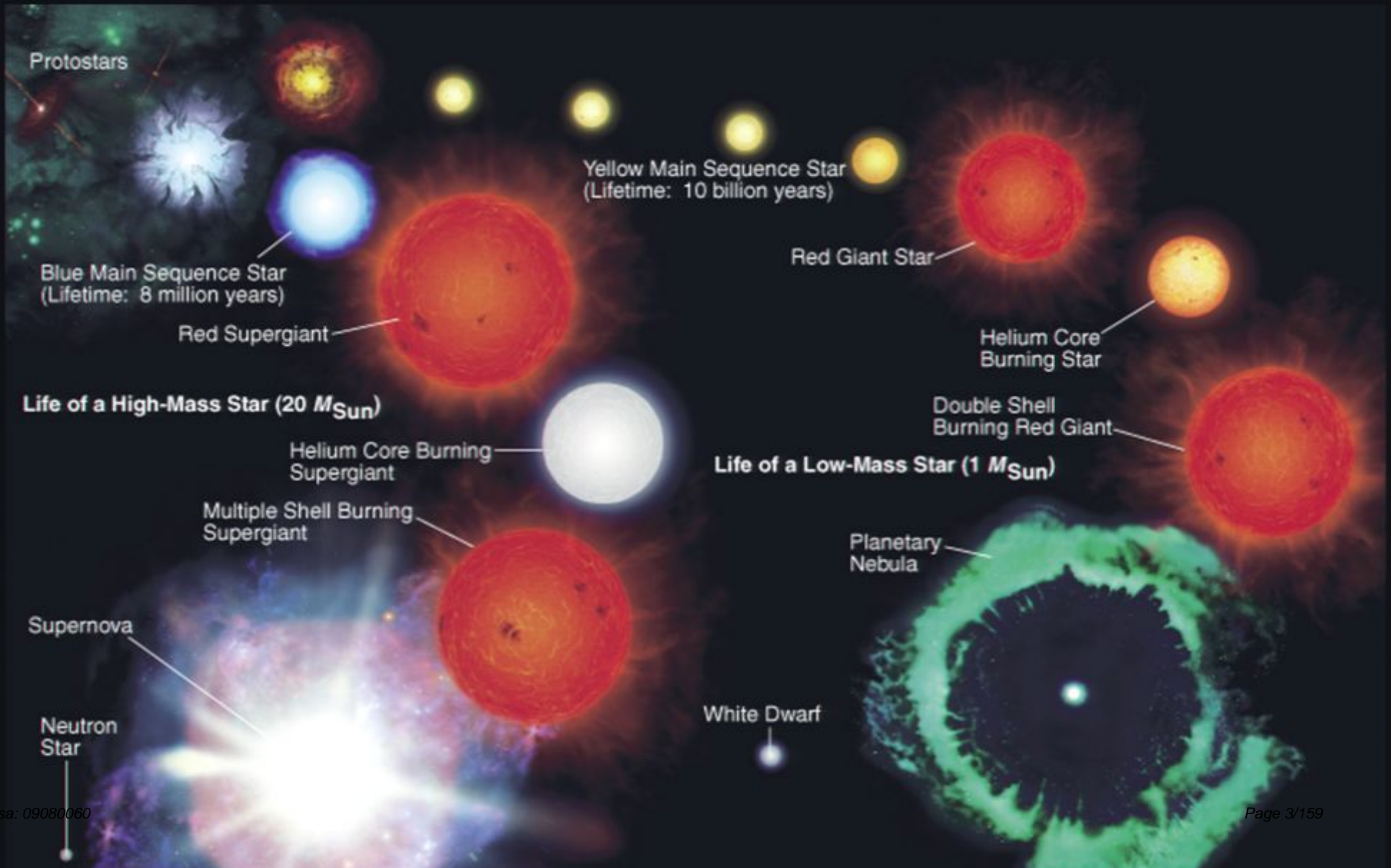


*Robert Wald*

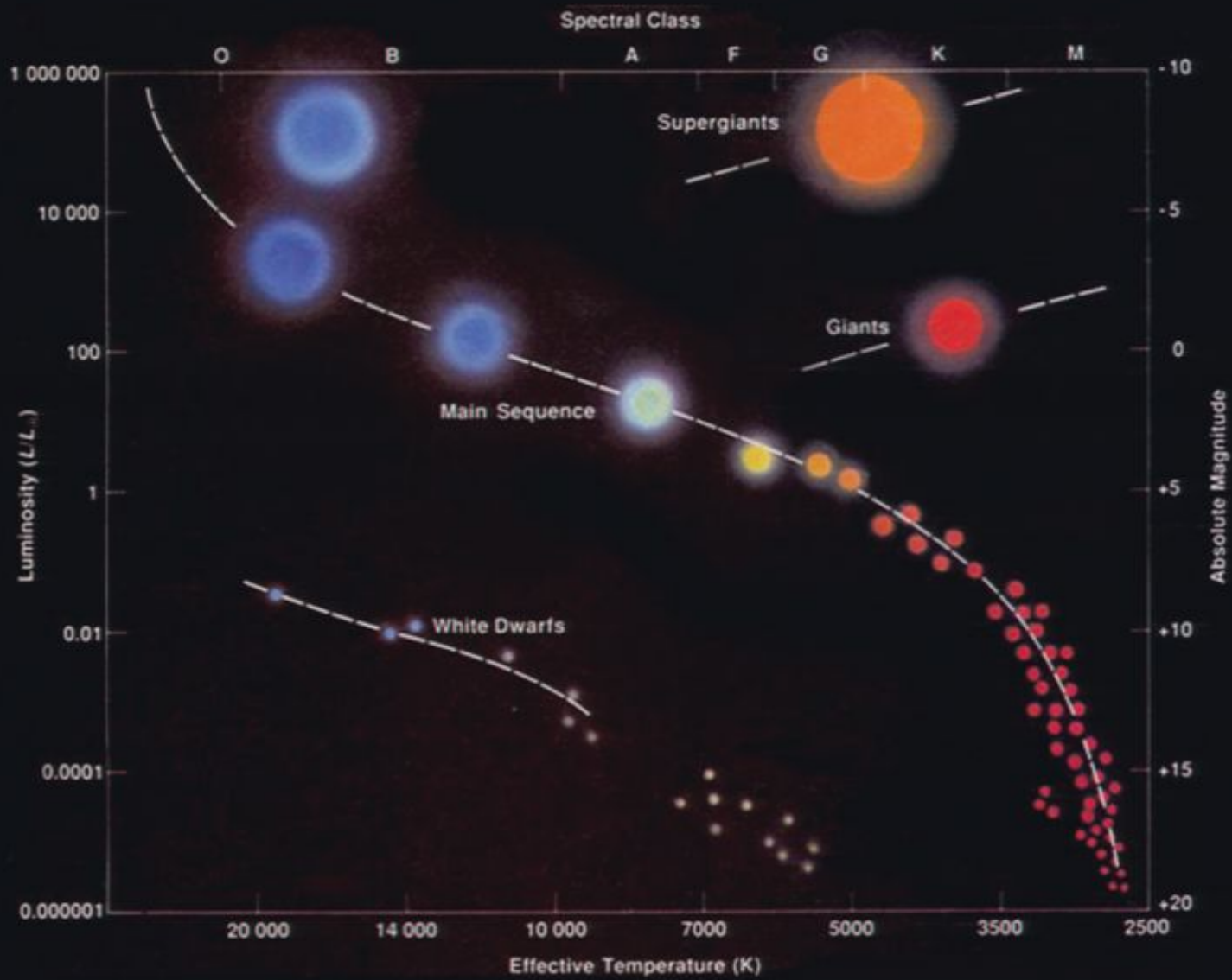


Page 2/159

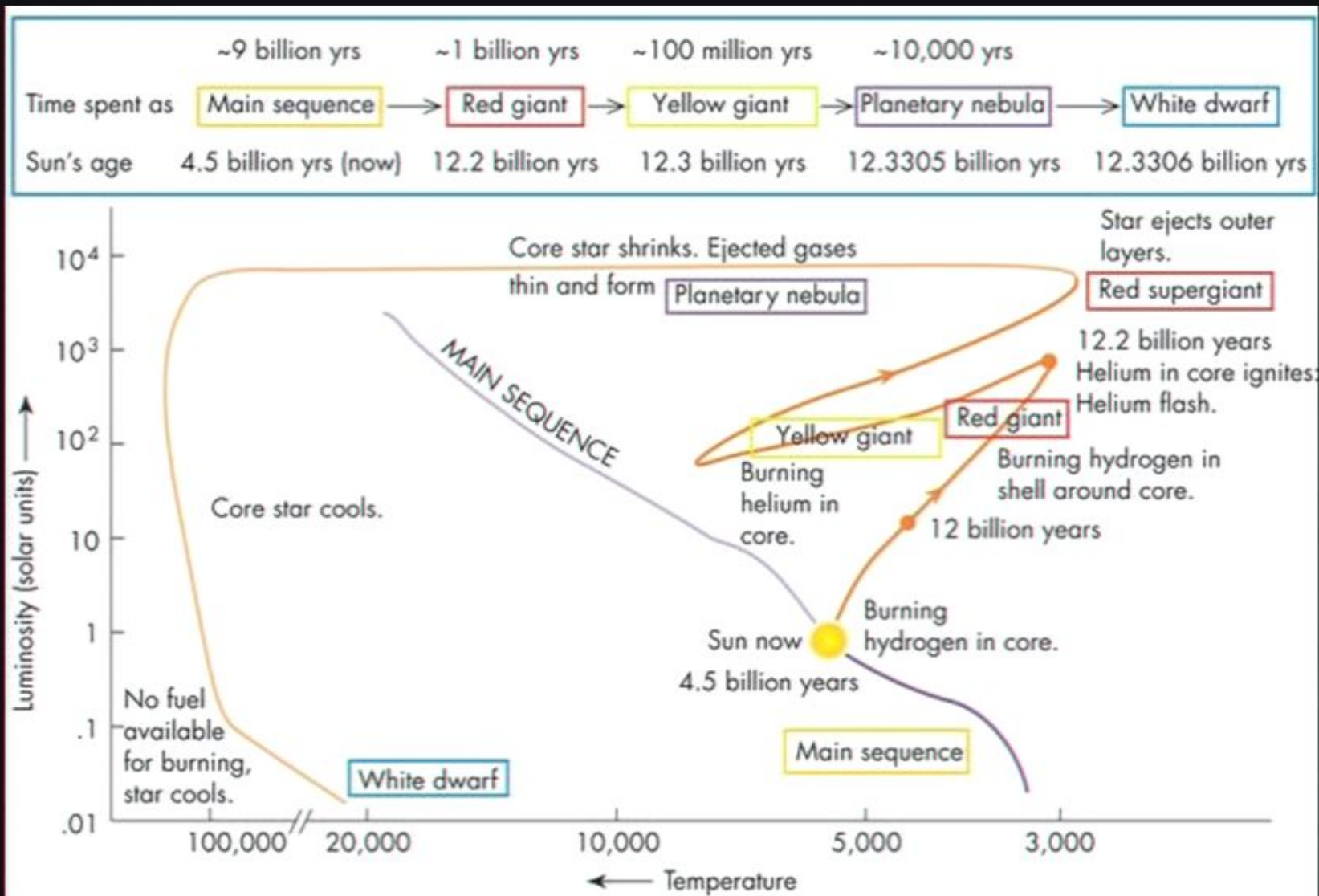
# Life Cycle of Stars

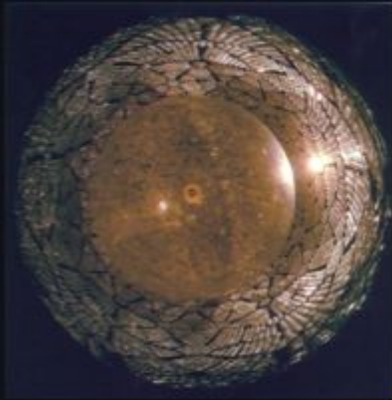


# Hertzsprung-Russell Diagram









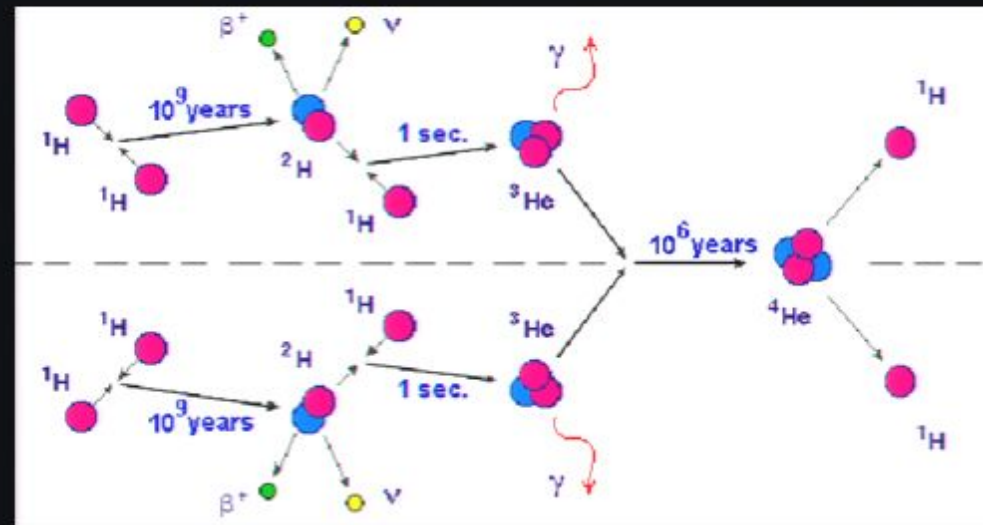
# Stellar Energy

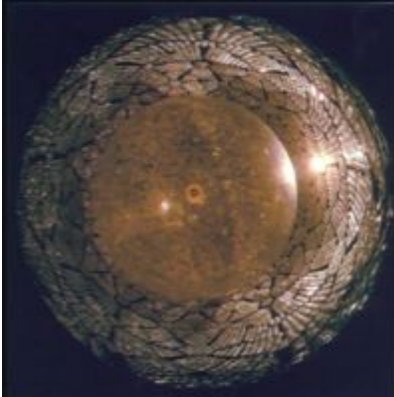
*Proton-Proton Chain* [ $4\text{H} \rightarrow \text{He} + \text{energy}$ ]

*Two hydrogen nuclei merge to produce deuterium nucleus, a positron, and a neutrino. Add another hydrogen and you get helium 3 and a gamma photon (energy). Two Helium 3 merge and produce helium 4 and two Hydrogen nuclei.*

## Proton-Proton Reaction

● — Neutron  
● — Proton





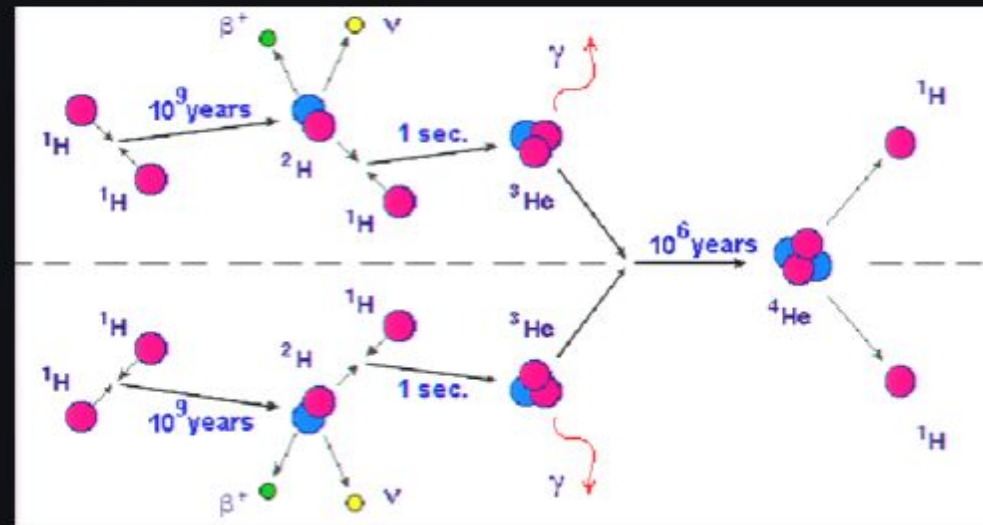
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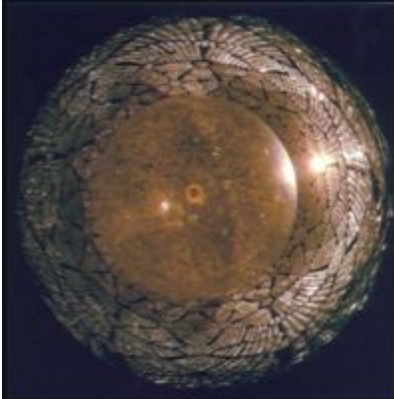
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## Two $1\text{H}$ Atoms Combine

● = Neutron  
● = Proton







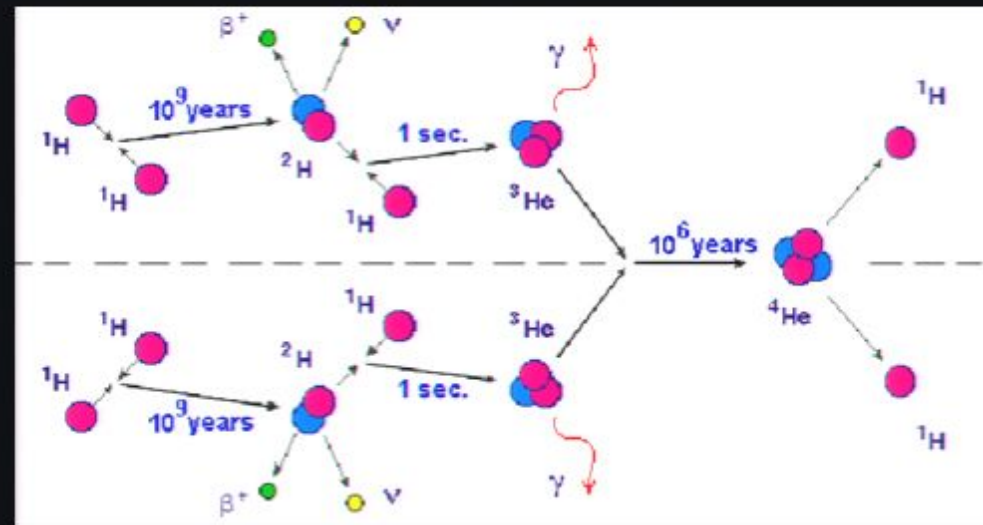
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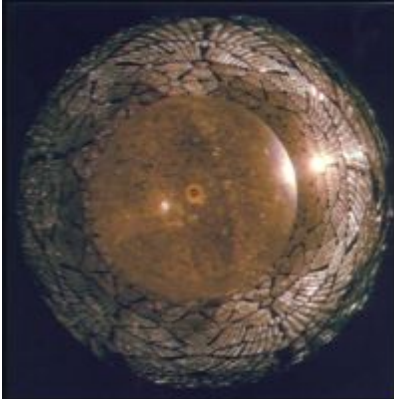
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2He Is Formed

● — Neutron  
● — Proton







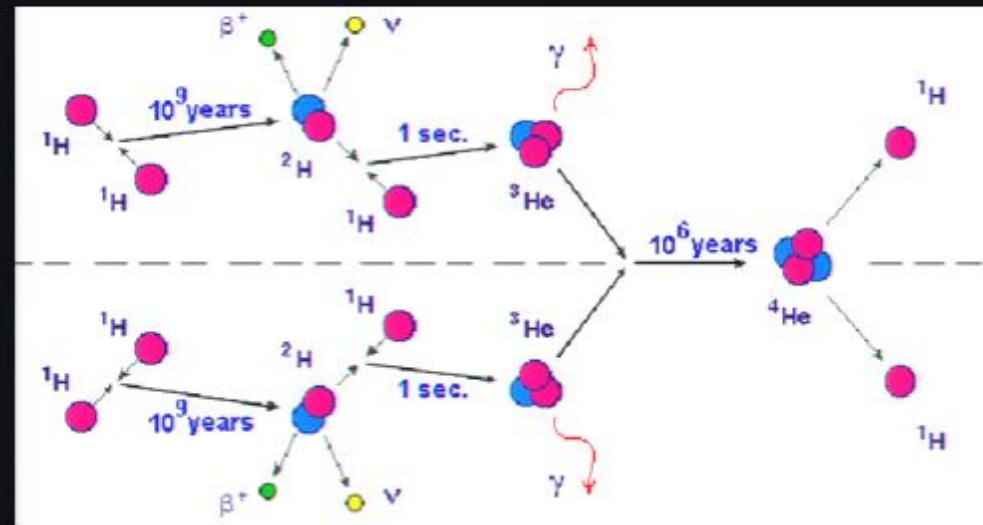
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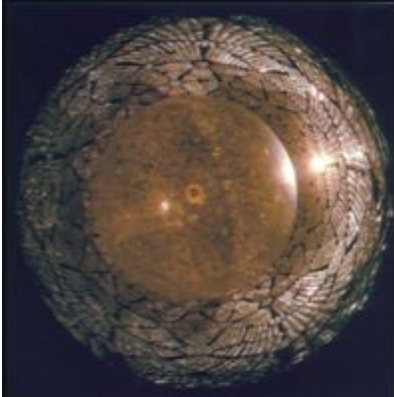
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# Stellar Energy

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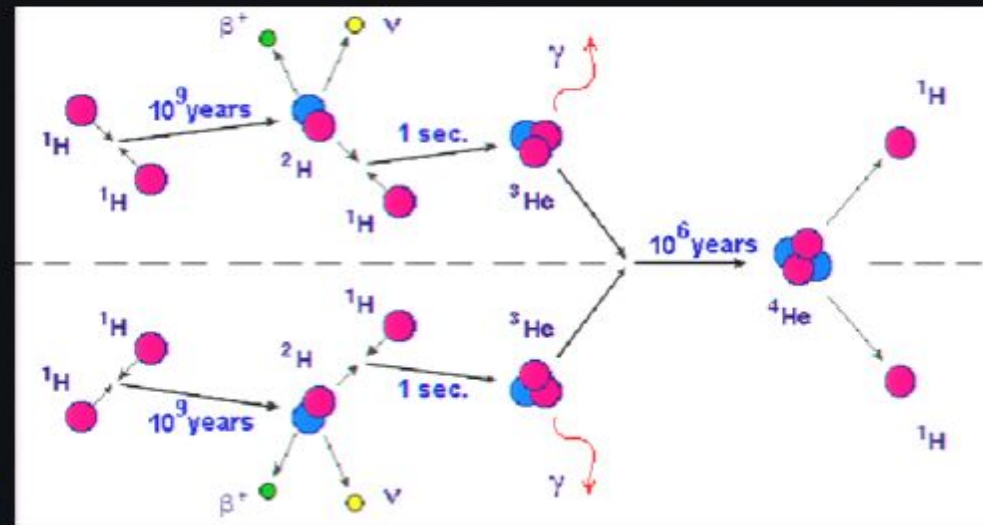
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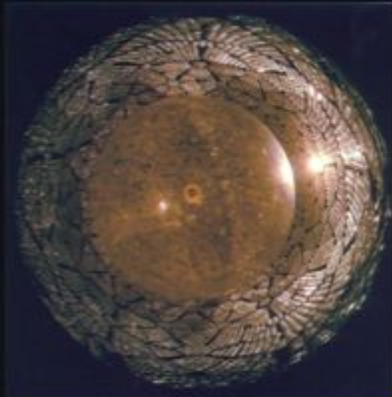
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● — Neutron  
● — Proton

Positron — ● ●

Neutrino — ●





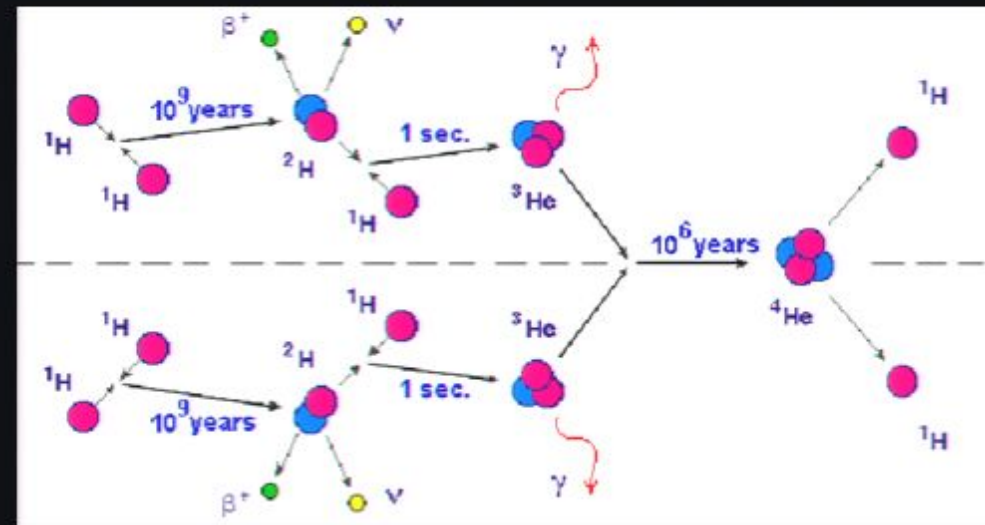
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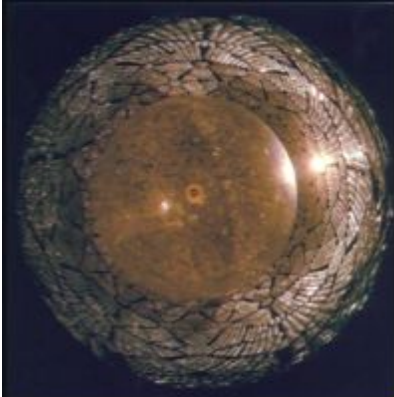
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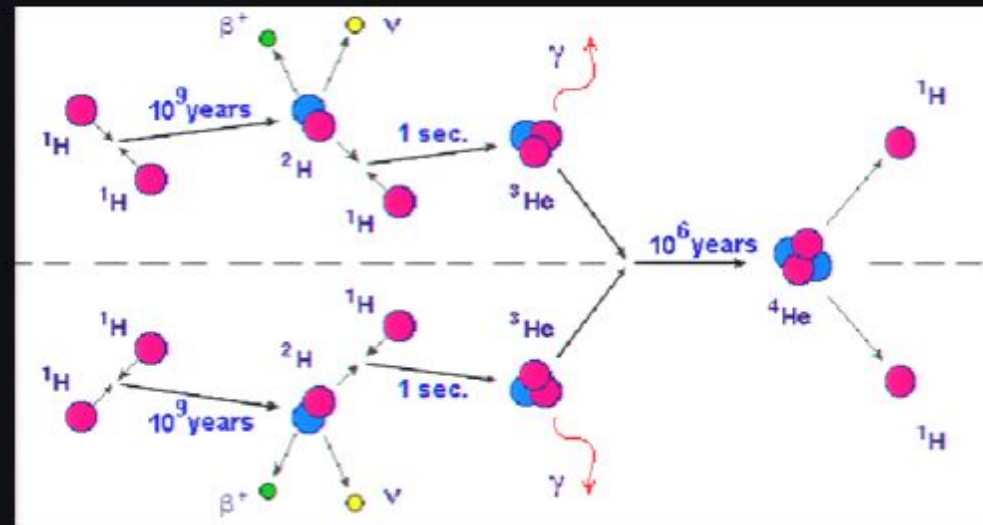
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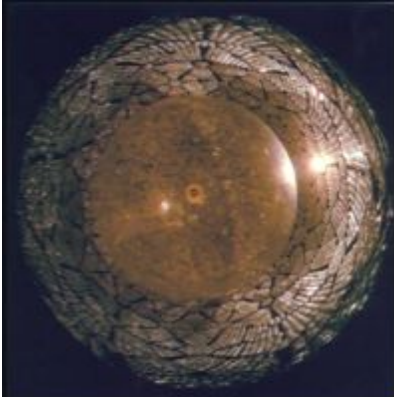
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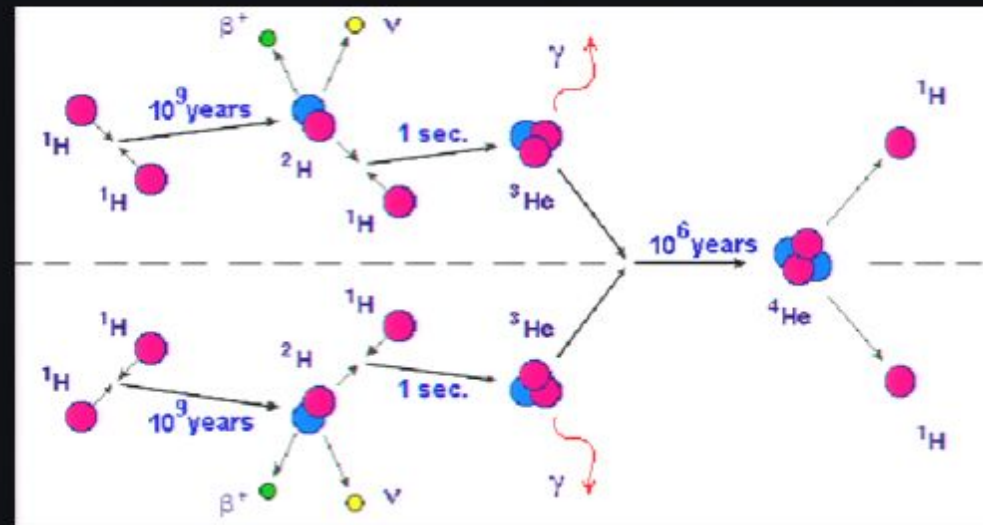
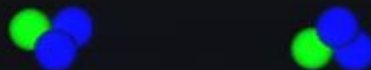
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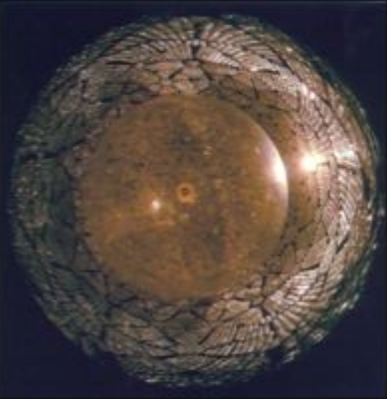
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## Two $3\text{He}$ Fuse Together

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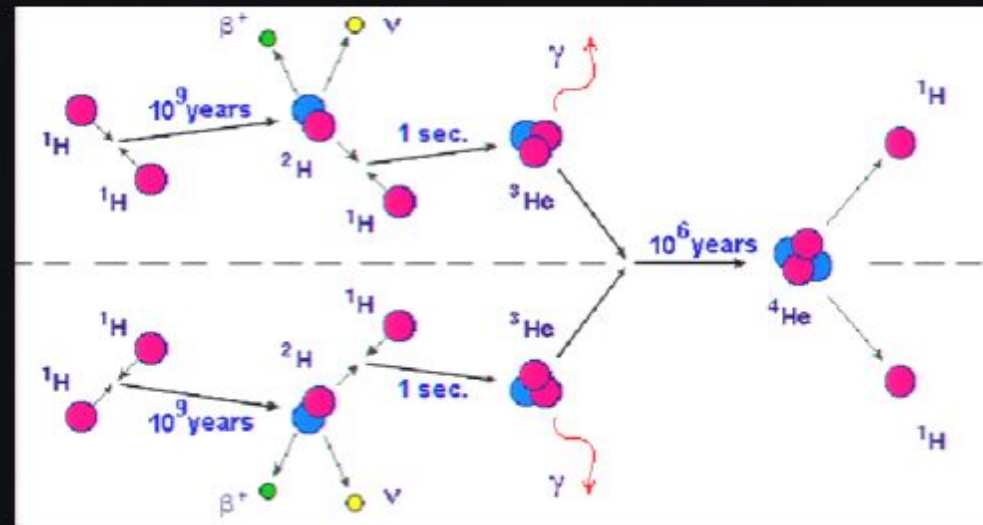
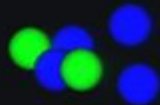
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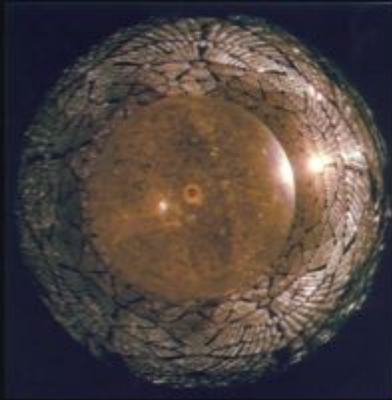
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Two  $1\text{H}$  Atoms Released

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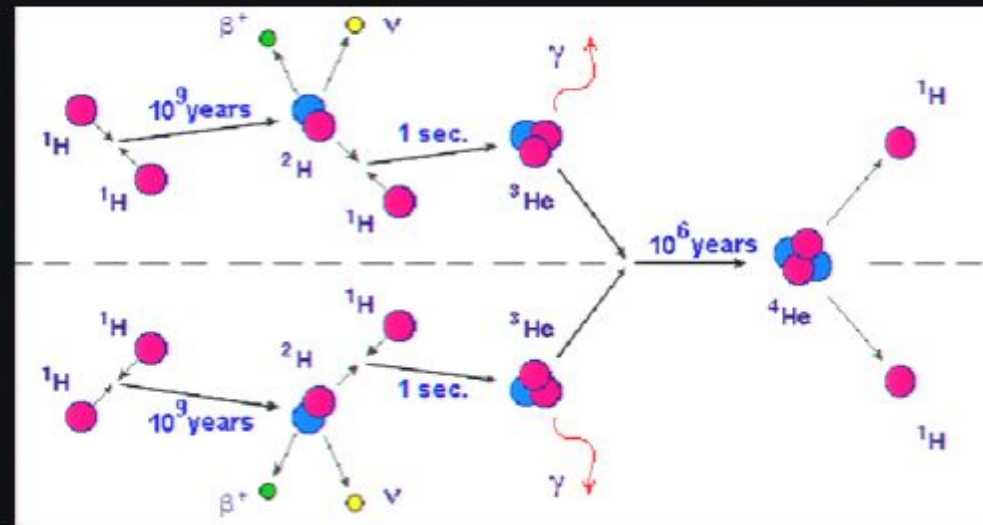
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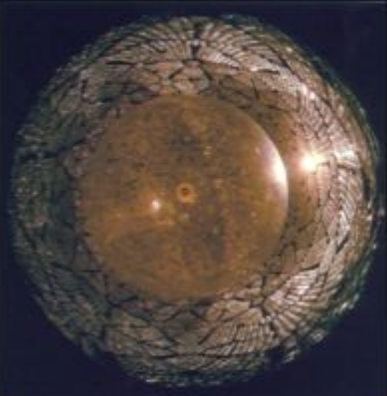
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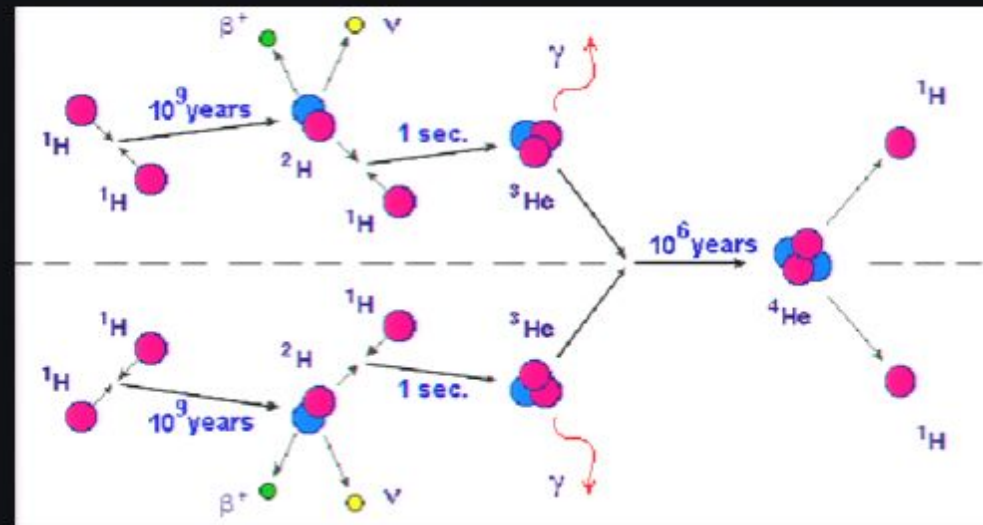
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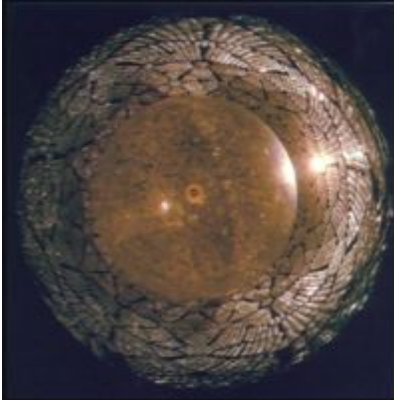
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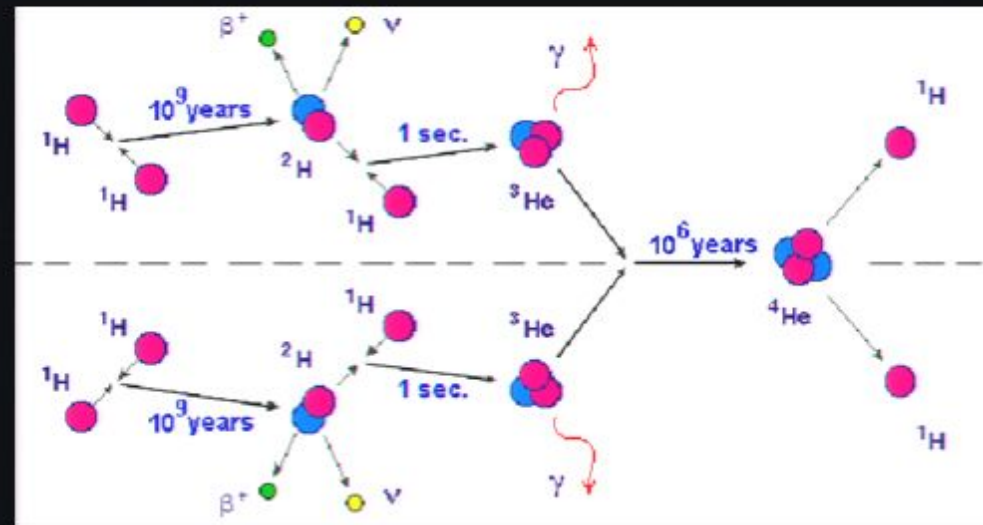
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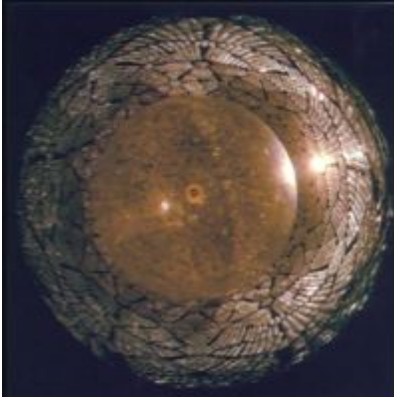
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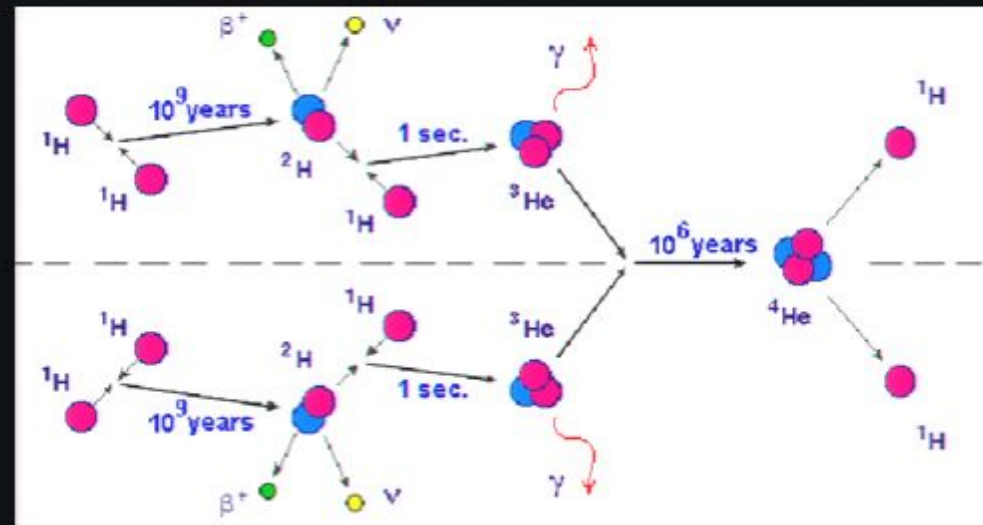
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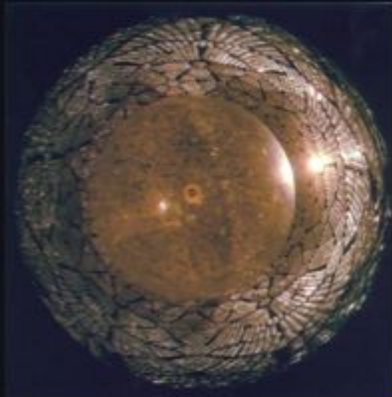
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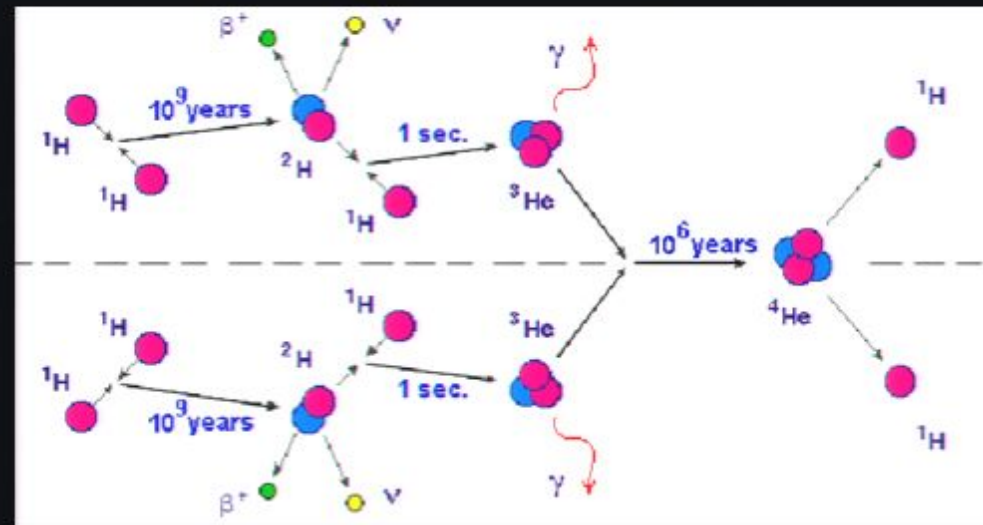
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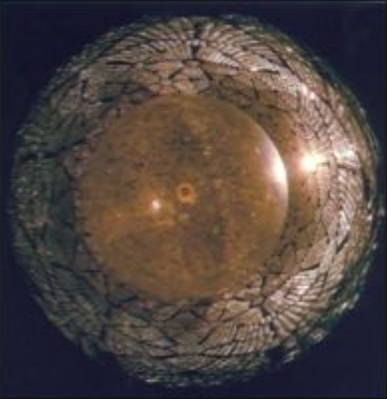
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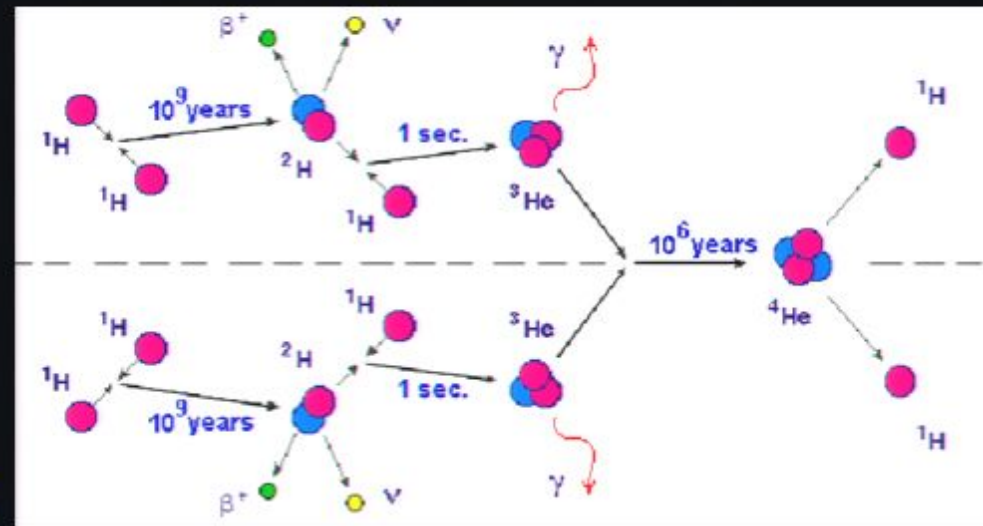
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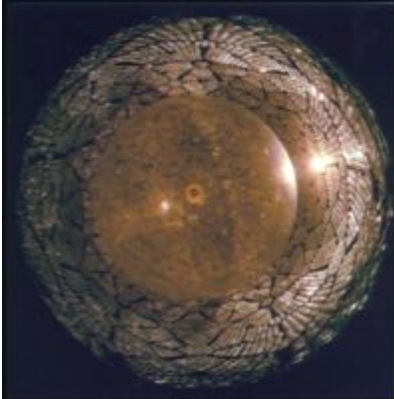
● — Neutron  
● — Proton

Positron — ● ●

Neutrino — ●







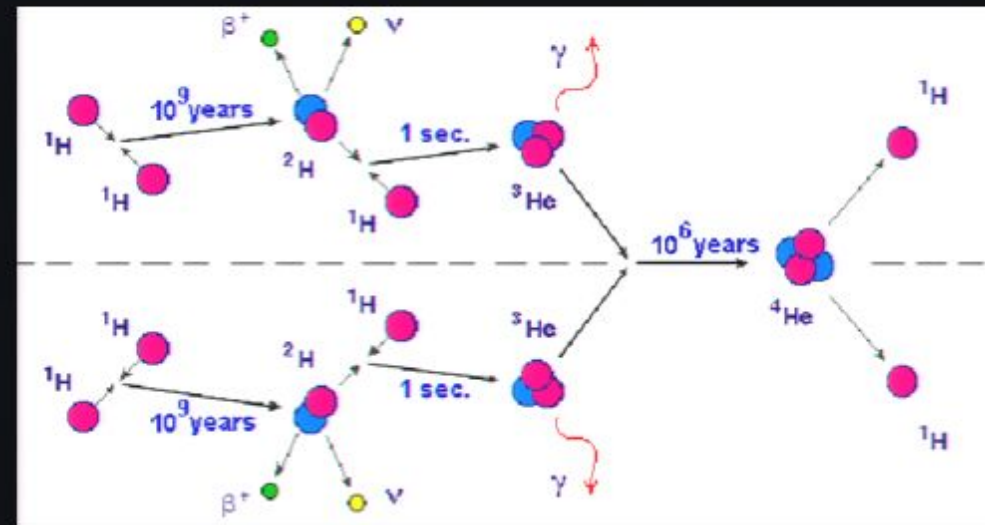
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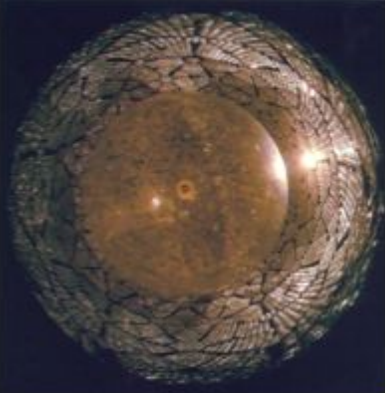
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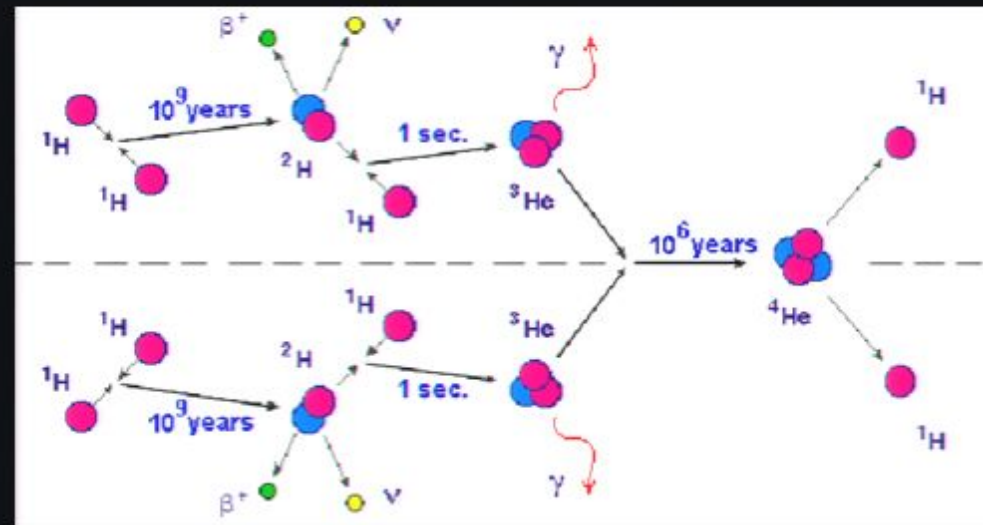
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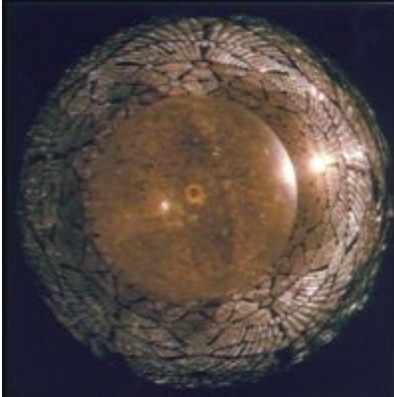
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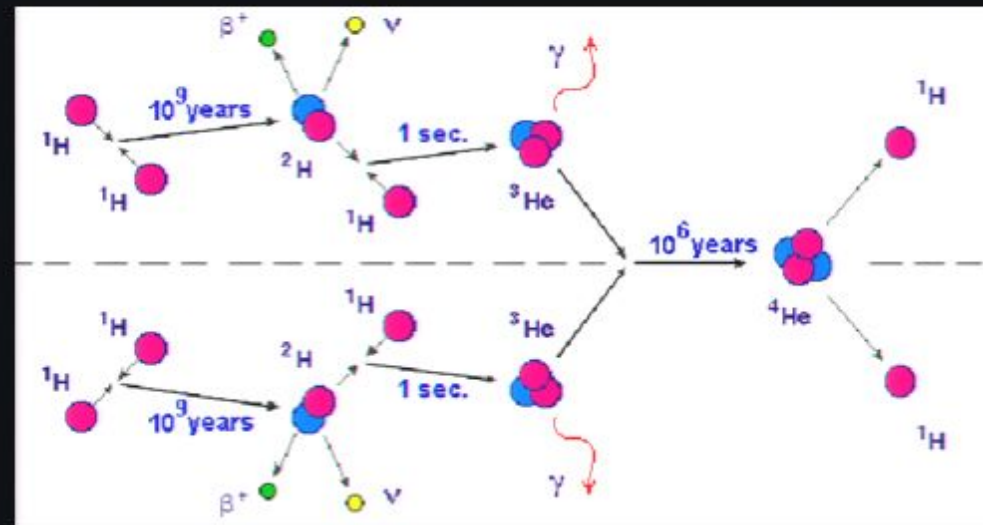
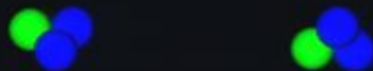
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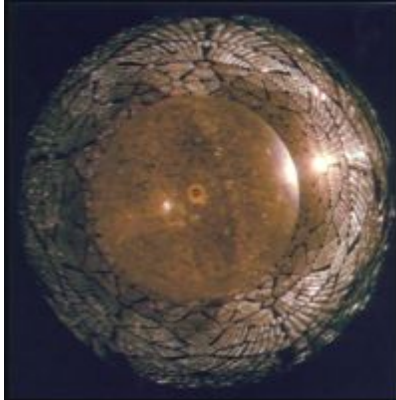
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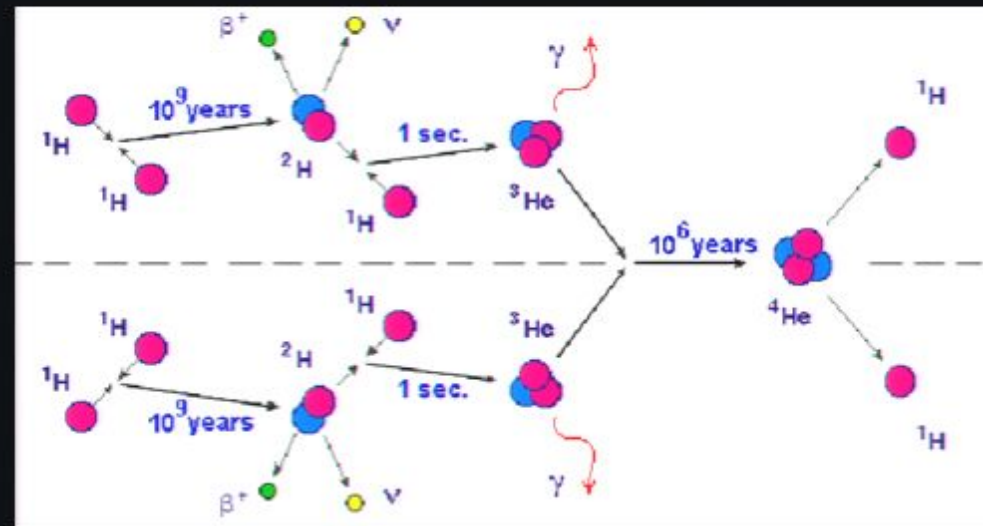
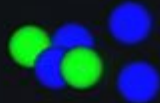
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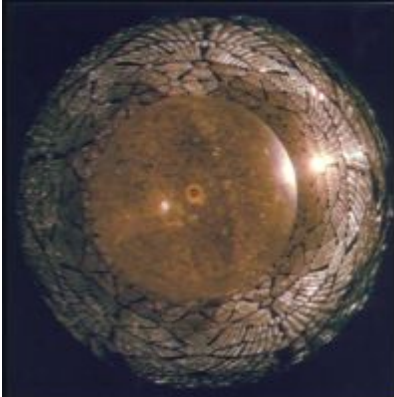
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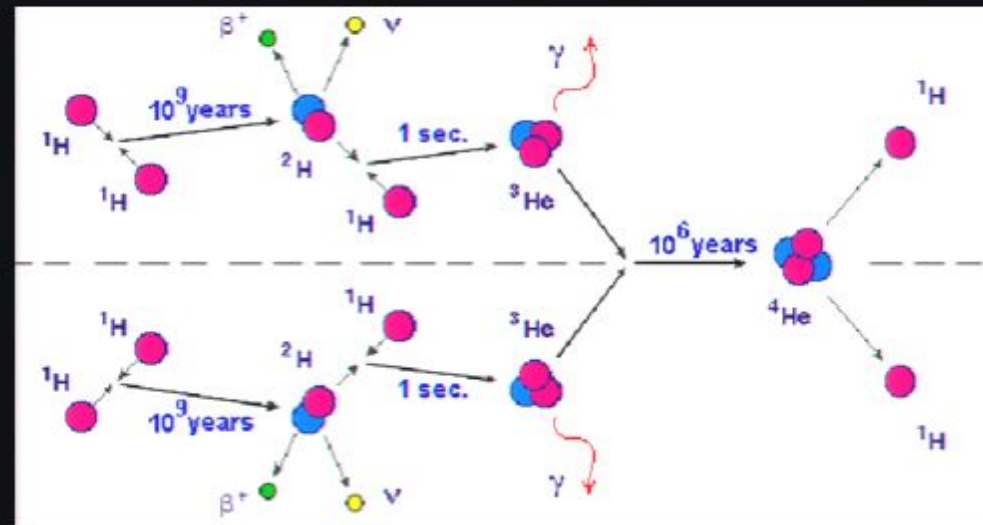
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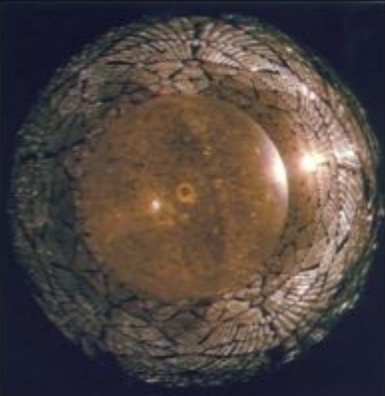
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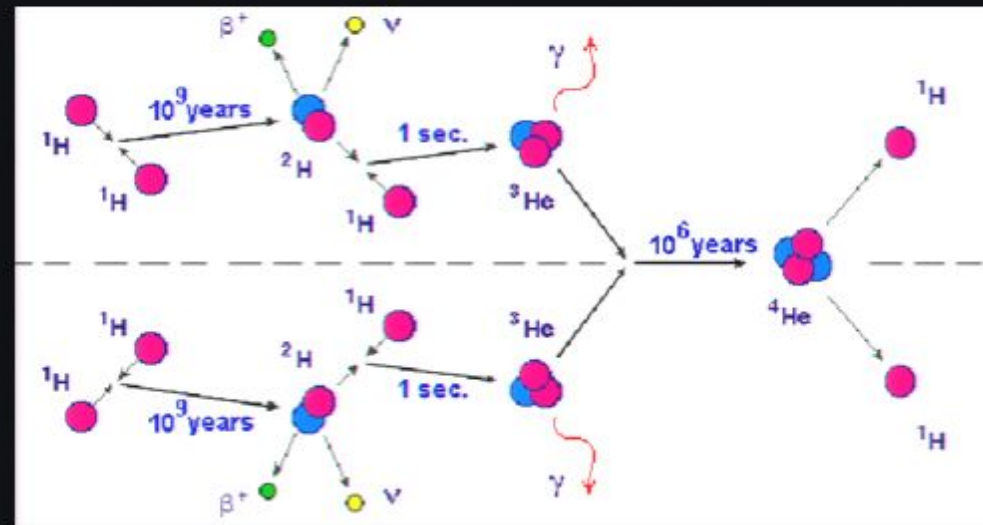
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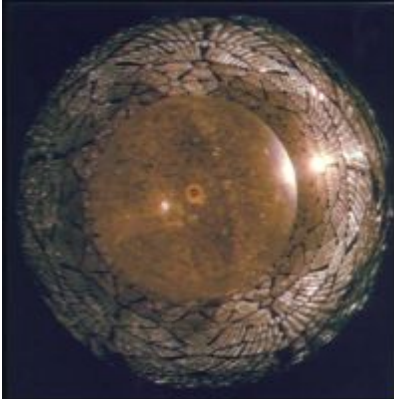
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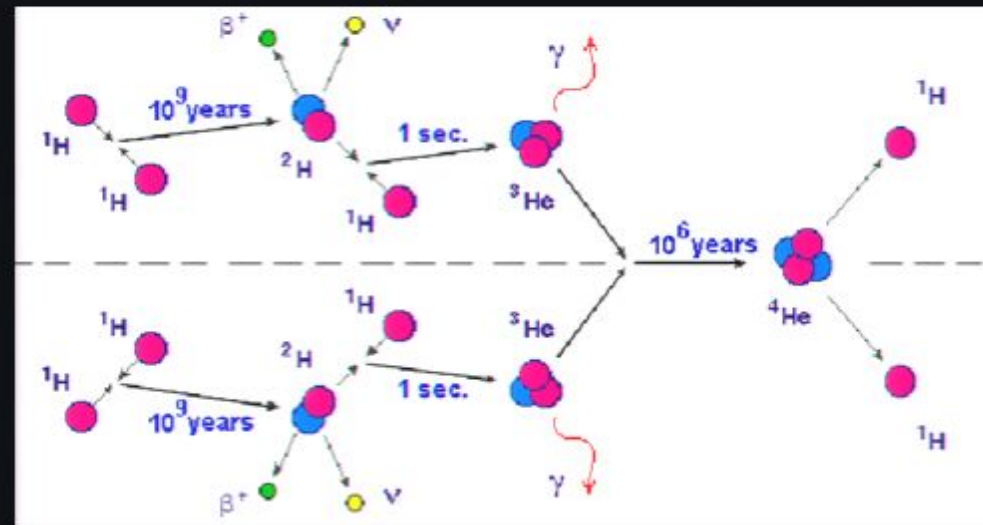
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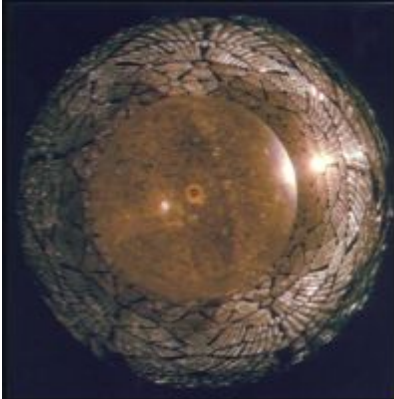
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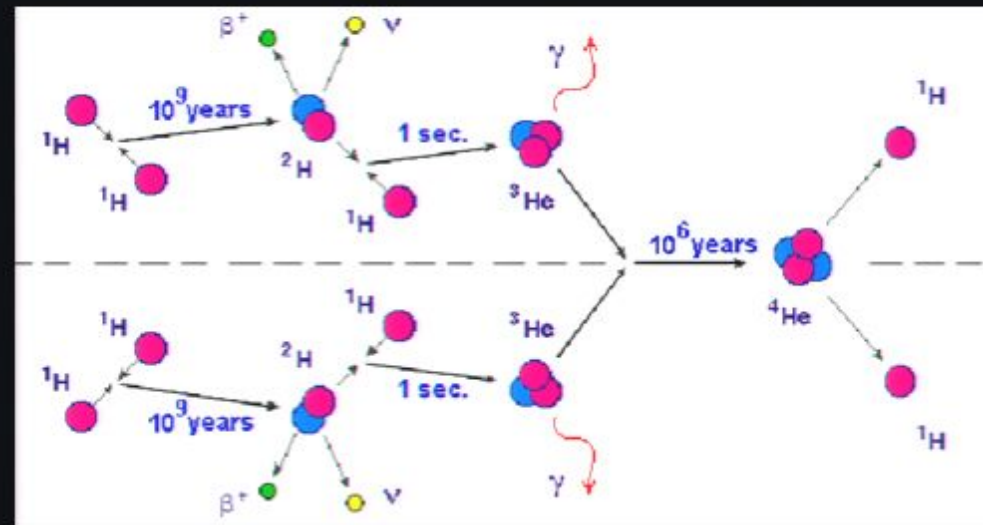
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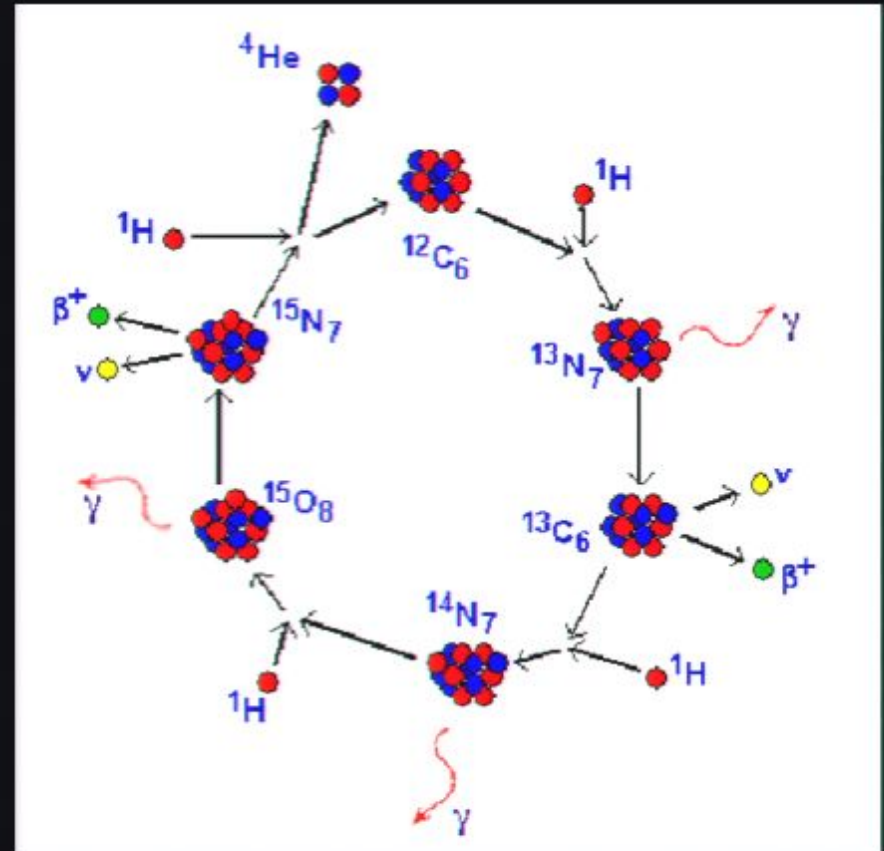
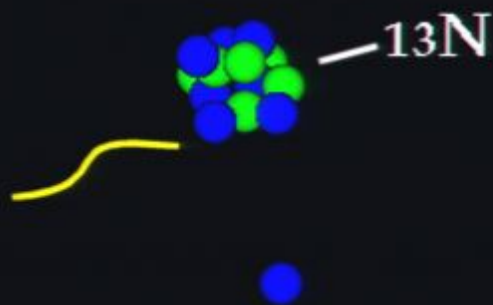


# CNO Cycle

- The higher the temperature, the more important the production of energy from the CNO.
- For stars less than 1 solar mass proton-proton cycle dominates.

Gamma Ray Released

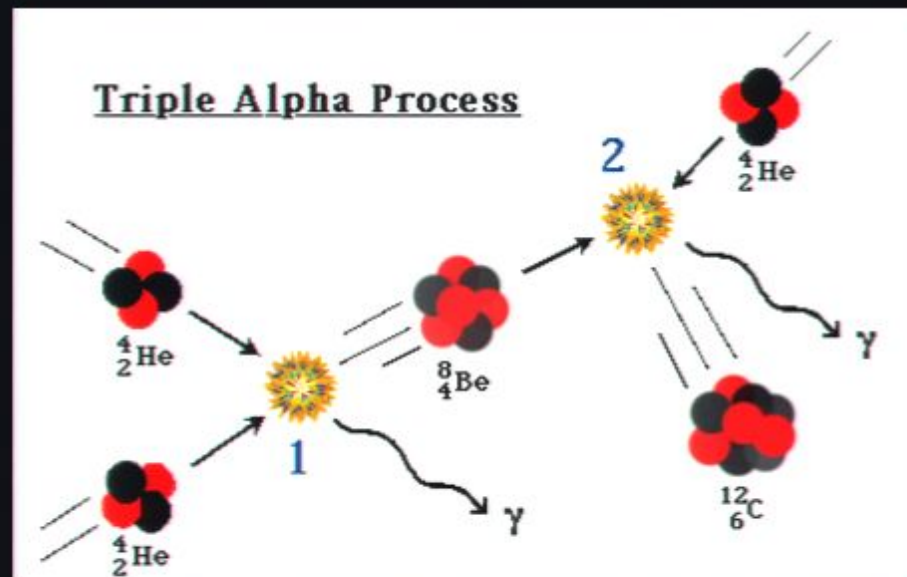
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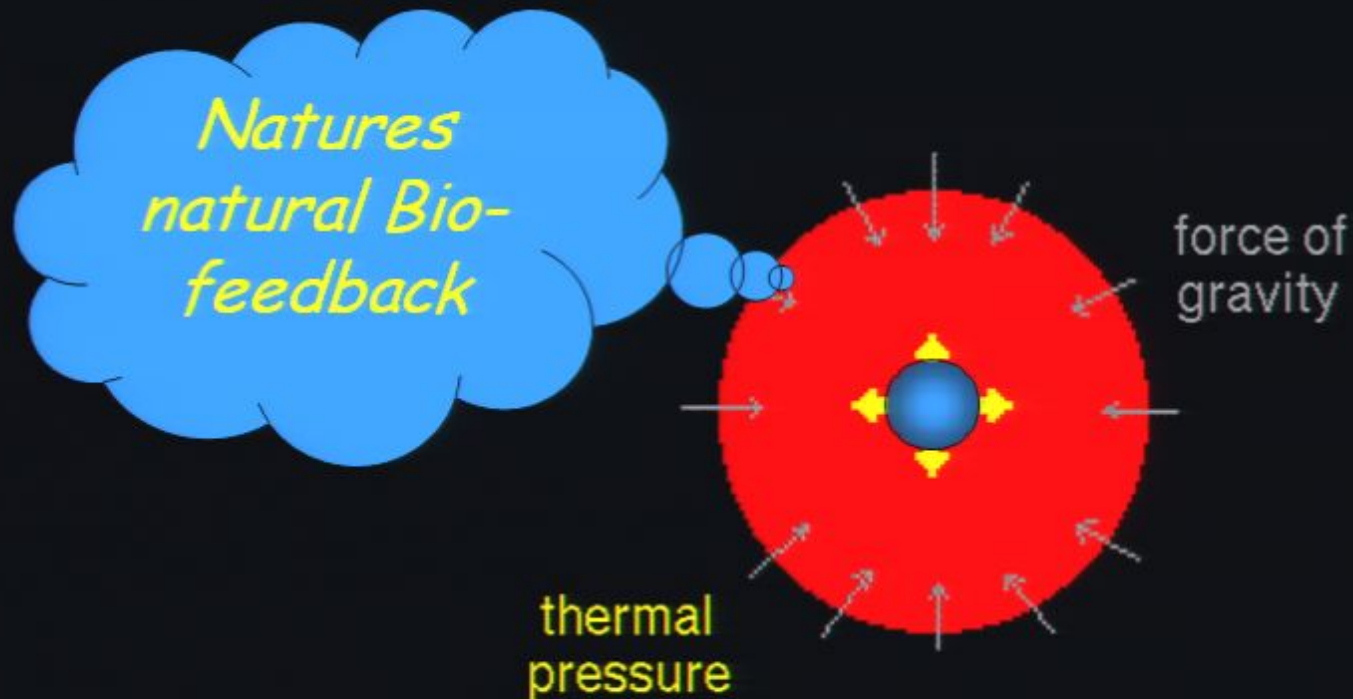
# Beyond Helium

*As Hydrogen is exhausted in the core of the star, Helium nuclei merge to create Beryllium with again fuses with another Helium nucleus to give Carbon and then to Oxygen then to Silicon until we finally end up with Iron.*



# The Death of Stars

# Pressure Balance in a Star



*Thermal Pressure = Force of Gravity*



# Model of an Atom

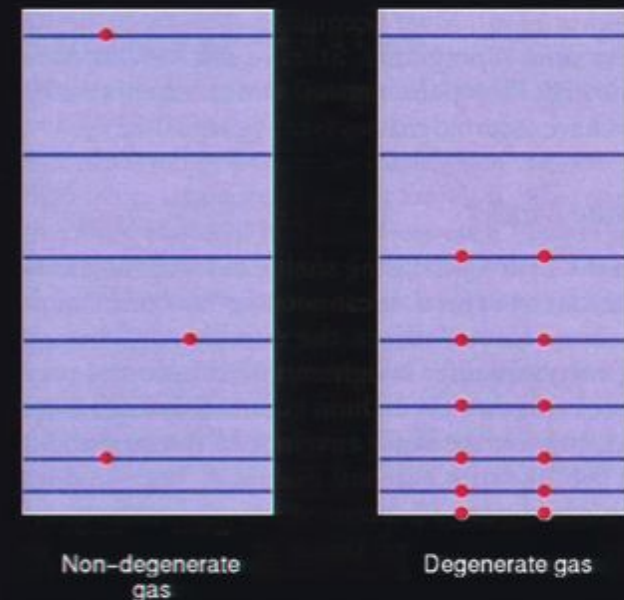


... an atom consists of mostly empty space ...

# Electron Degeneracy Pressure

$$Radius = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_e m_p M}$$

- Pauli Exclusion Principle:  
No two electrons (fermions) can occupy the same position in space at the same time doing the same thing.
- Electrons are packed side by side in a white dwarf
- This prevents it from collapsing any further



*Calculate Magnitude of  
Radius*

# Electron Degeneracy Pressure

$$Radius = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_e m_p M}$$

$$h = 6.6261 \times 10^{-34}$$

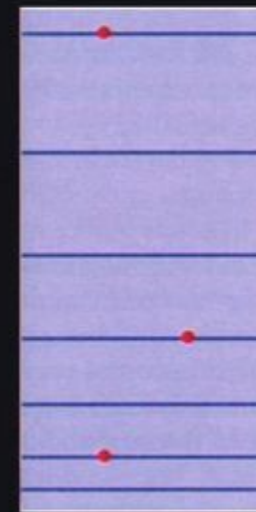
$$G = 6.6726 \times 10^{-11}$$

$$m_e = 9.1094 \times 10^{-31}$$

$$m_p = 1.6726 \times 10^{-27}$$

$$M = 1.989 \times 10^{30}$$

*Calculate Magnitude of  
Radius*



Non-degenerate  
gas



Degenerate gas



# Electron Degeneracy Pressure

$$Radius = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_em_pM}$$



$$2.7 \times 10^{-31} m$$

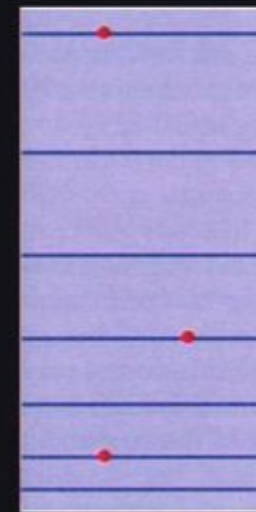
$$h = 6.6261 \times 10^{-34}$$

$$G = 6.6726 \times 10^{-11}$$

$$m_e = 9.1094 \times 10^{-31}$$

$$m_p = 1.6726 \times 10^{-27}$$

$$M = 1.989 \times 10^{30}$$



Non-degenerate  
gas



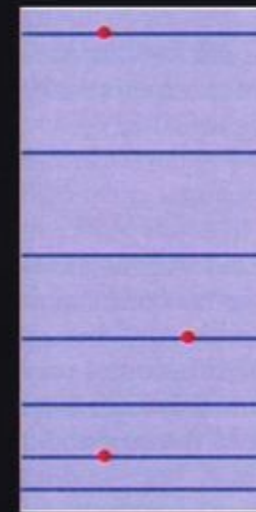
Degenerate gas

# Electron Degeneracy Pressure

$$Radius = N_e^{\frac{2}{3}} \frac{h^2}{8Gm_e m_p M}$$

$(5.95 \times 10^{56})^{\frac{2}{3}}$ 
 $2.7 \times 10^{-31} m$

$$\approx 10^7 m$$

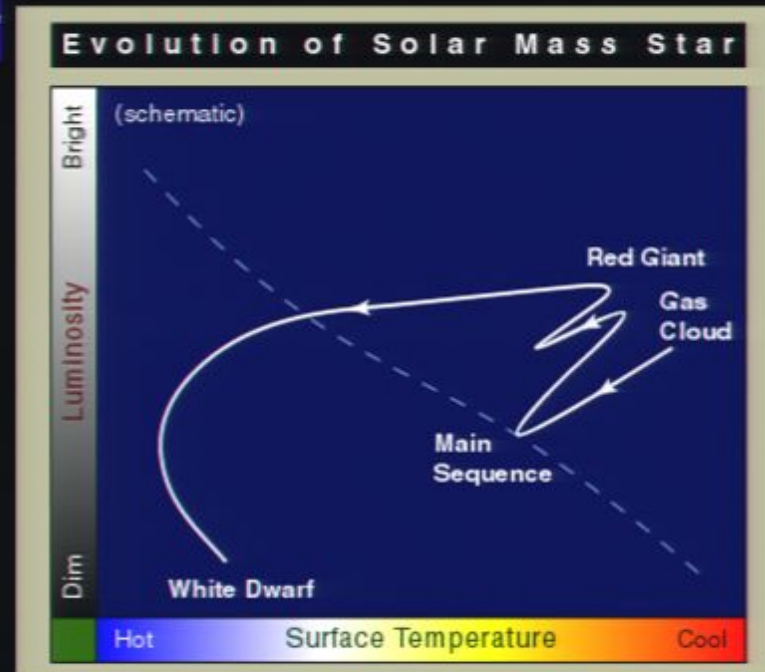
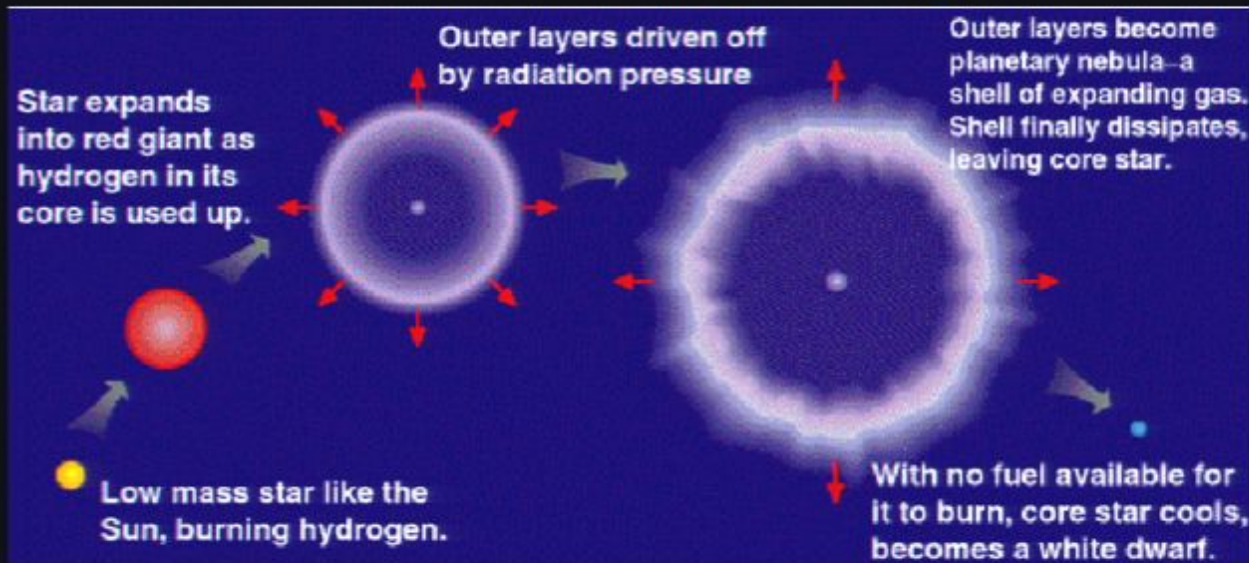


Non-degenerate gas



Degenerate gas

# Path to being a White Dwarf





# Properties of White Dwarfs

- Helium exhausted, core collapses until density forces electrons to leave their orbits around the atomic nuclei.

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- ...are found in the centers of planetary nebula.

# Properties of White Dwarfs

- Helium exhausted, core collapses until density forces electrons to leave their orbits around the atomic nuclei.
- ...are found in the centers of planetary nebula.
- ...have masses less than the Chandrasekhar mass (1.4 Solar Masses).



# White Dwarf Properties

...have diameters about the same as the Earth's.



## Look in the Middle

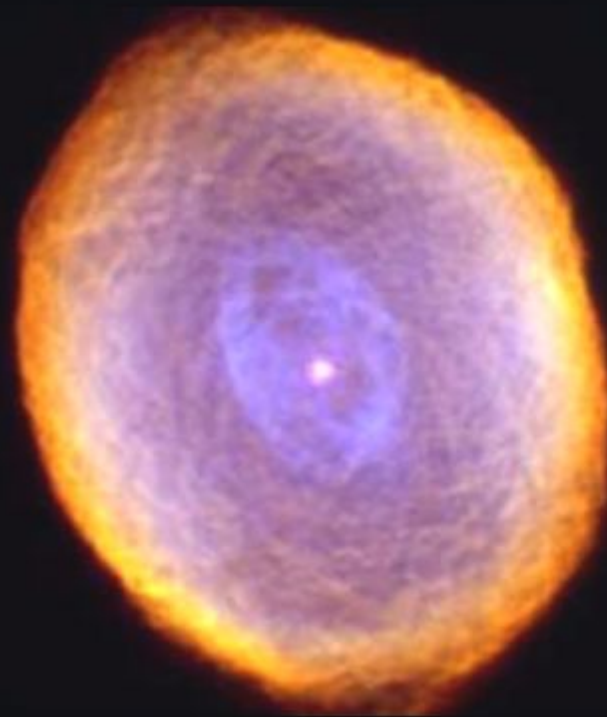


# Cat's eye nebula





# Spirograph Nebula





# Eskimo Nebula





## Above the Chandrasekhar Limit

- The maximum mass of a white dwarf is 1.4 solar masses



## Above the Chandrasekhar Limit

- The maximum mass of a white dwarf is 1.4 solar masses
- Above this, even electron degeneracy pressure cannot counterbalance gravity
- What is the fate of a star more massive than this?



## Above the Chandrasekhar Limit

- The maximum mass of a white dwarf is 1.4 solar masses
- Above this, even electron degeneracy pressure cannot counterbalance gravity
- What is the fate of a star more massive than this?



*Can you feel  
the  
suspense?*

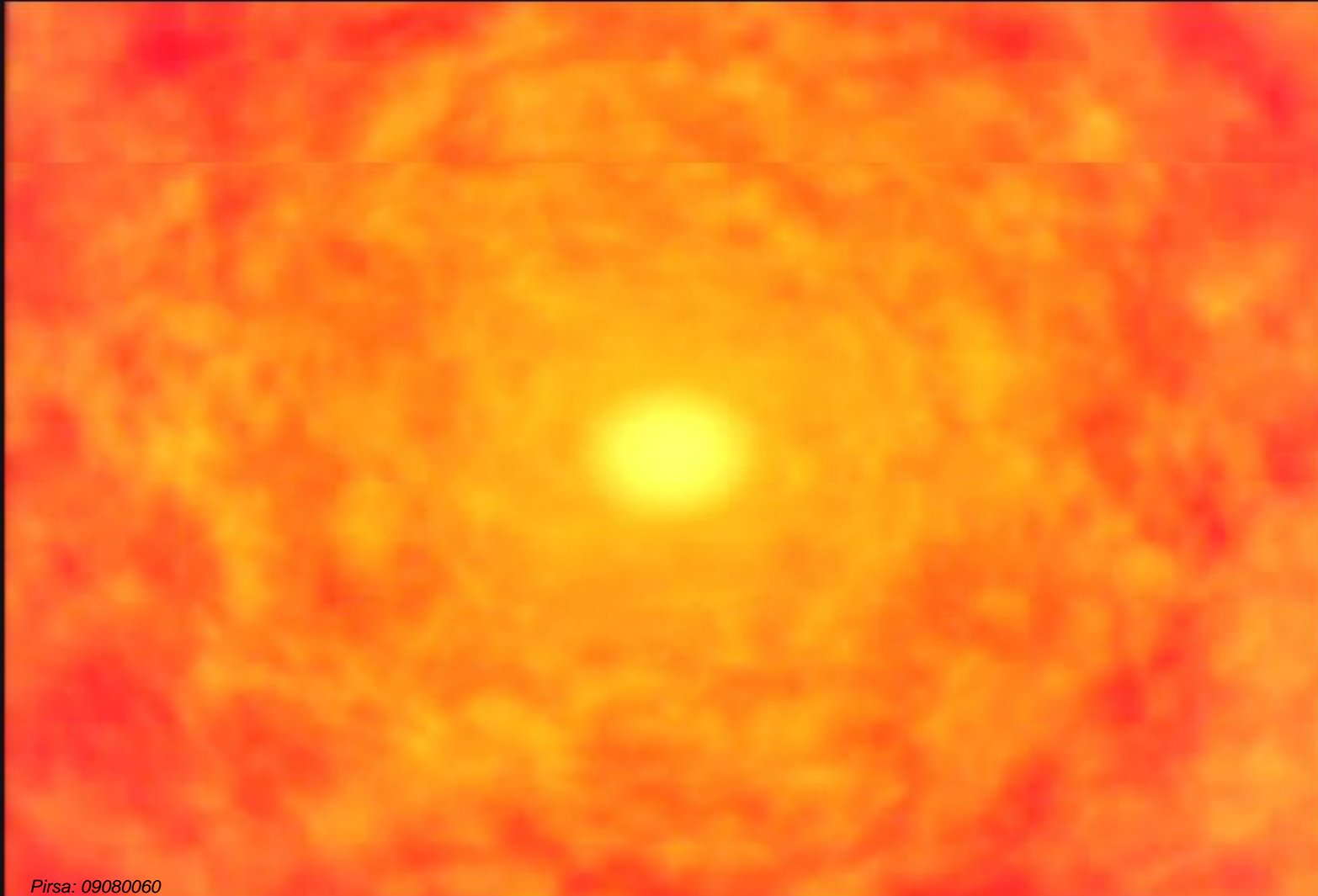




# A Super Nova



# A Super Nova



# A Super Nova



Pirsa: 09080060

*Not what  
you  
thought?*



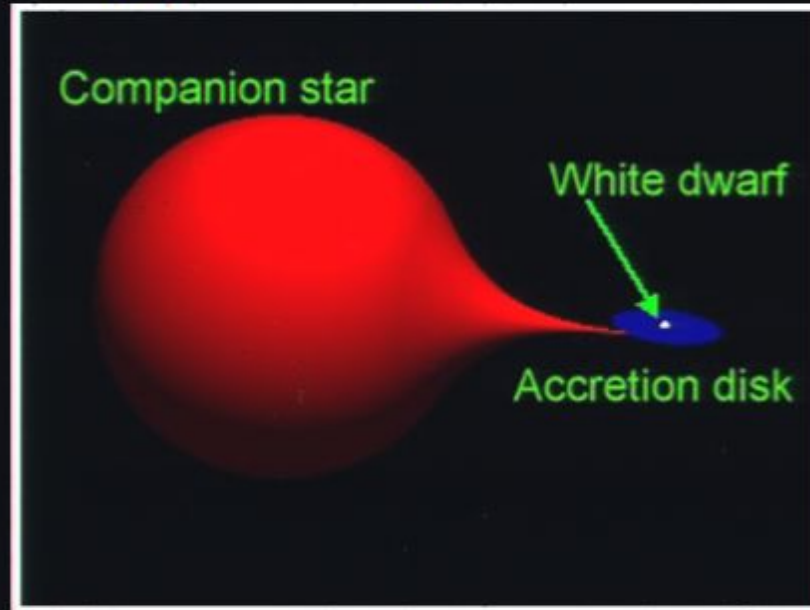
Page 53/159



# Type 1a Super Nova



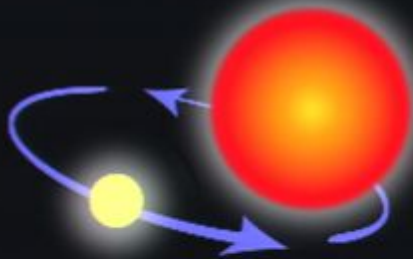
Two normal stars  
are in a binary pair.



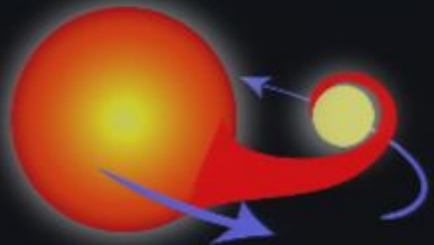
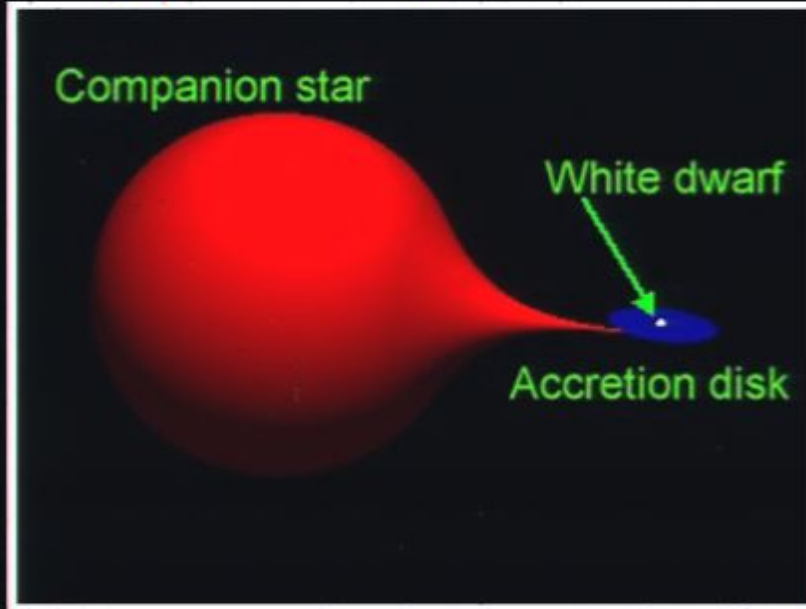
# Type 1a Super Nova



Two normal stars are in a binary pair.



The more massive star becomes a giant...

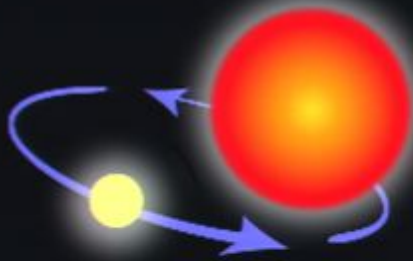


...which spills gas onto the secondary star, causing it to expand and become engulfed

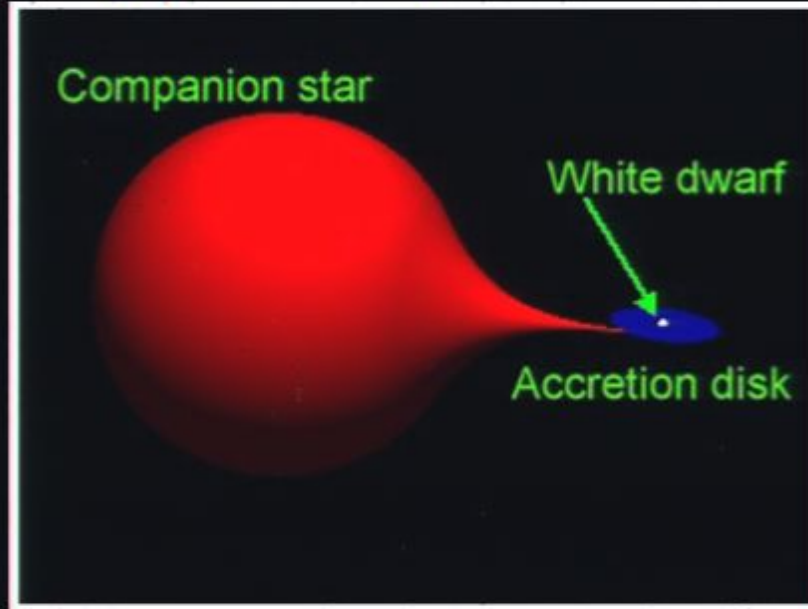
# Type 1a Super Nova



Two normal stars are in a binary pair.



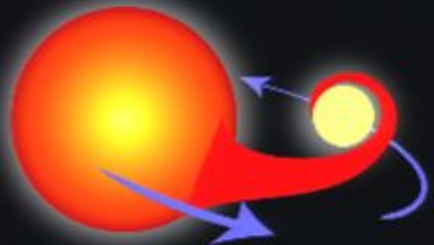
The more massive star becomes a giant...



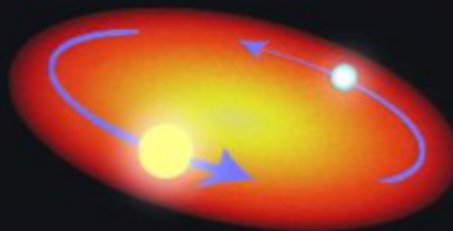
Companion star

White dwarf

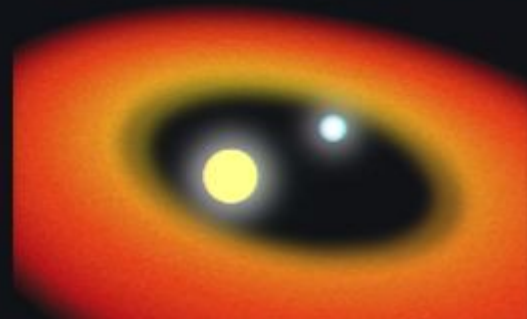
Accretion disk



...which spills gas onto the secondary star, causing it to expand and become engulfed



The secondary, lighter star and the core of the giant star spiral inward within



The common envelope is ejected, while the separation between the core and the



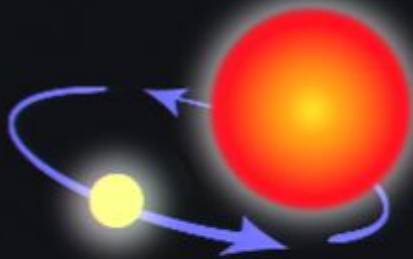
The remaining core of the giant collapses and



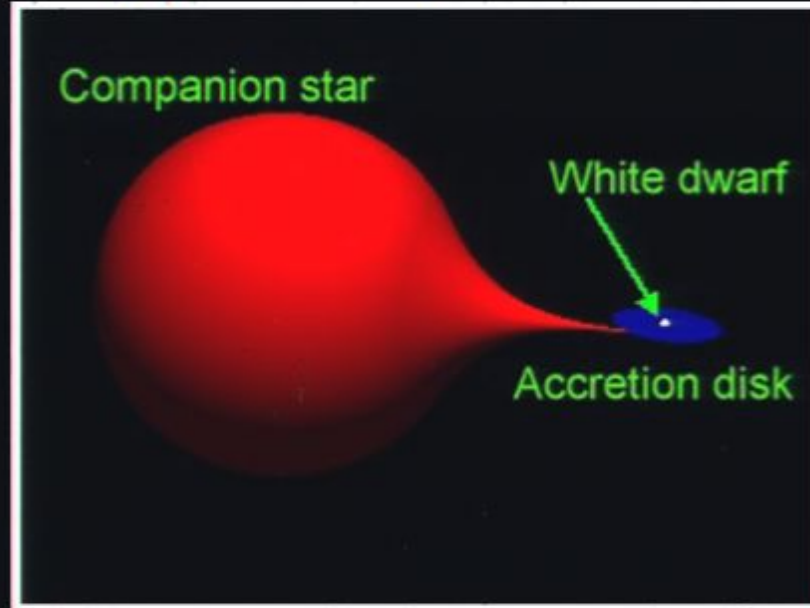
# Type 1a Super Nova



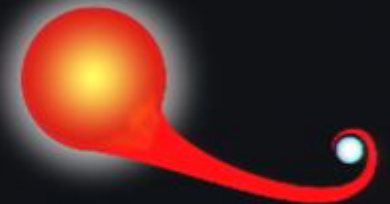
Two normal stars are in a binary pair.



The more massive star becomes a giant...

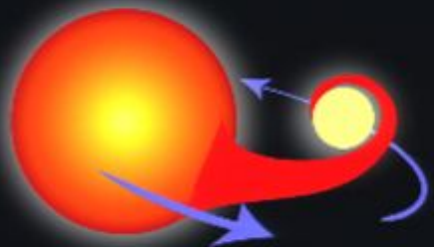


The white dwarf's mass increases until it reaches a critical mass and explodes...

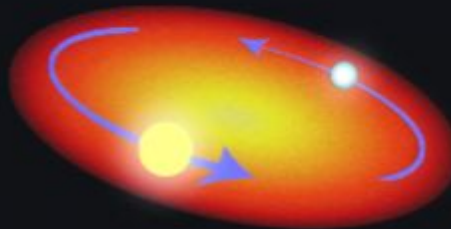


The aging companion star starts swelling, spilling gas onto the white dwarf.

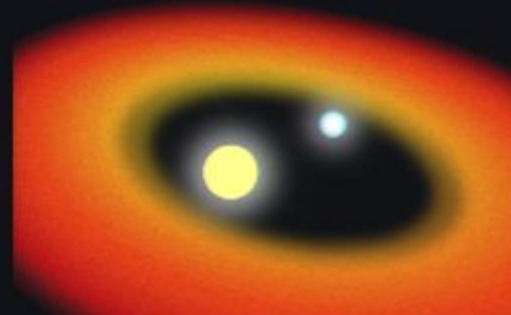
*Not of interest to black hole cosmologists, but type 1a's are great yard sticks in determining distances*



...which spills gas onto the secondary star, causing it to expand and become engulfed



The secondary, lighter star and the core of the giant star spiral inward within



The common envelope is ejected, while the separation between the core and the



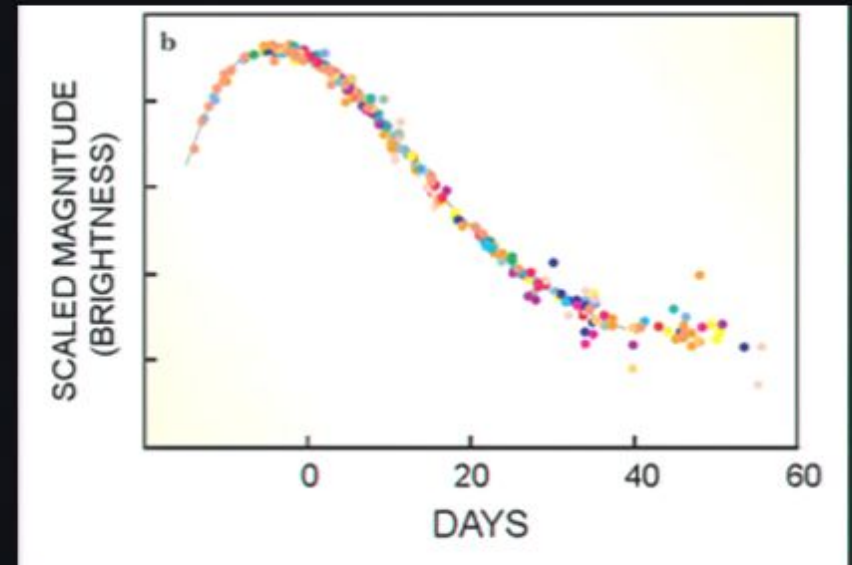
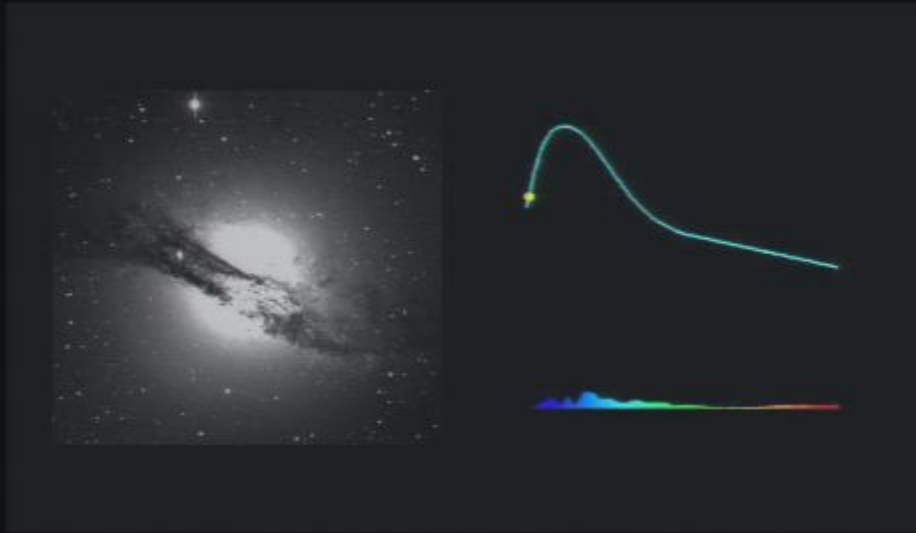
The remaining core of the giant collapses and

# Standard Candle

*Mark Phillips discovered that type 1a Supernova had a period/luminosity relationship. The time it takes for the SN to decline in brightness determined what the maximum brightness was. The decline took weeks so it became easy for astronomers to use these SN as a standard candle.*



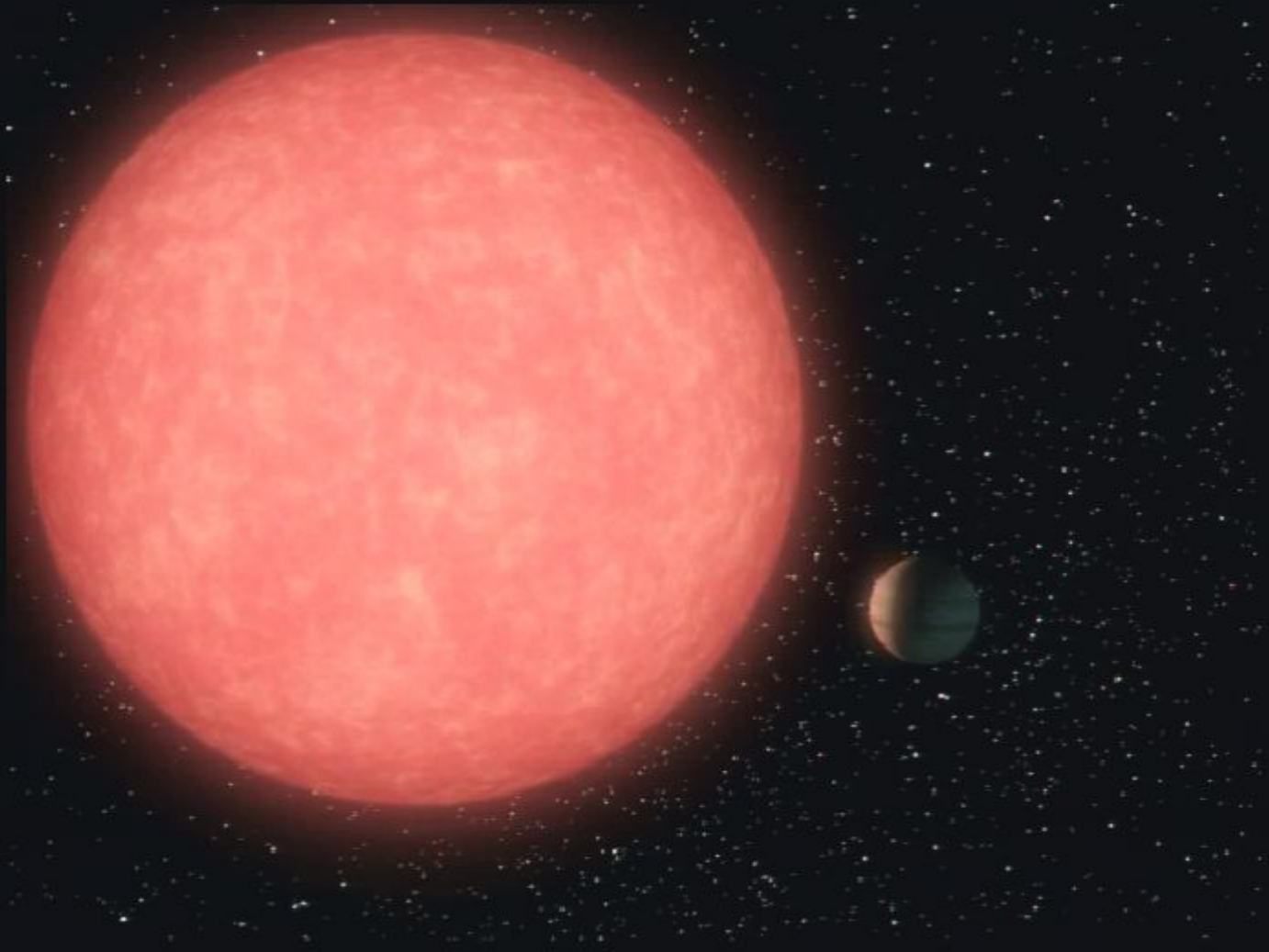
# Standard Candle



*Mark Phillips discovered that type 1a Supernova had a period/luminosity relationship. The time it takes for the SN to decline in brightness determined what the maximum brightness was. The decline took weeks so it became easy for astronomers to use these SN as a standard candle.*



# Type II Supernovae: Birth of a Neutron Star



- *The core survives and is prevented from collapsing any further by neutron degeneracy pressure*

- *These are the type of supernovae we are interested in.*

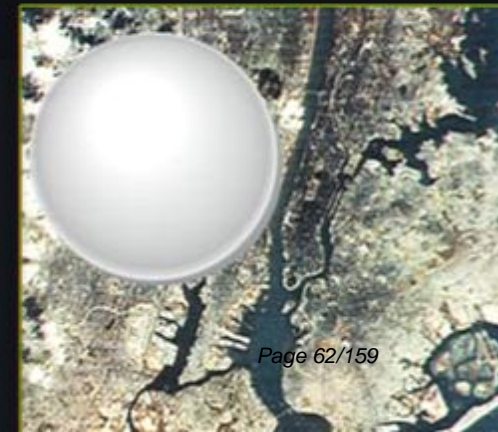
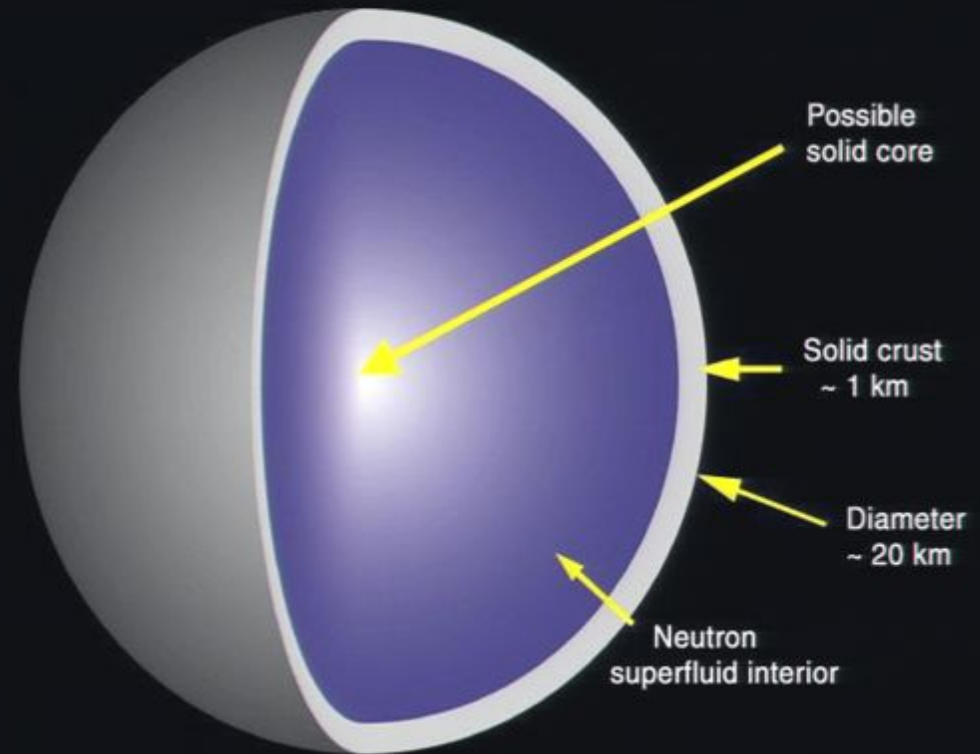
# Supernova Remnant

- In the death of a high-mass star (<40 solar mass), the core is converted to neutrons and collapses catastrophically.
- The collapse and rebound creates a supernova.
- The electrons are 'merged' with the protons which produce neutrons.
- The central core is left behind as a small, dense, sphere of neutrons → a neutron star.
- Collapsing stops now because of Neutron Degeneracy Pressure.



# Neutron Star Facts

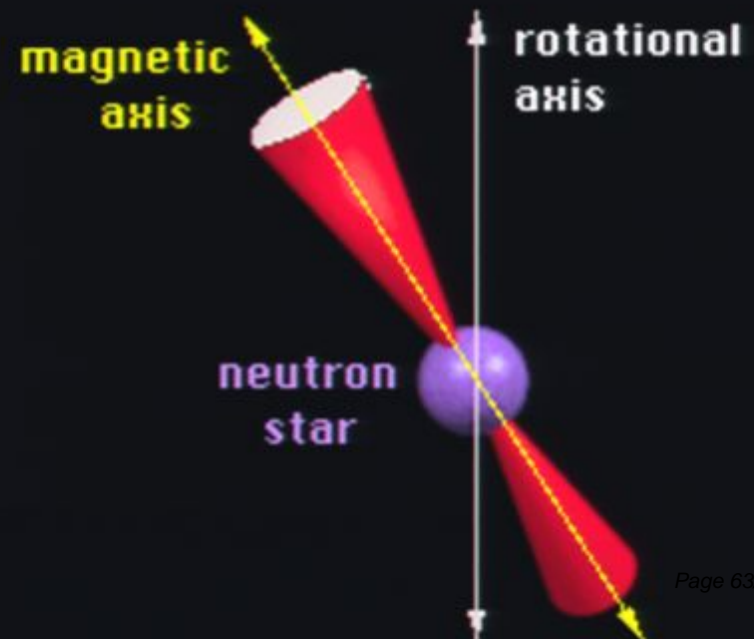
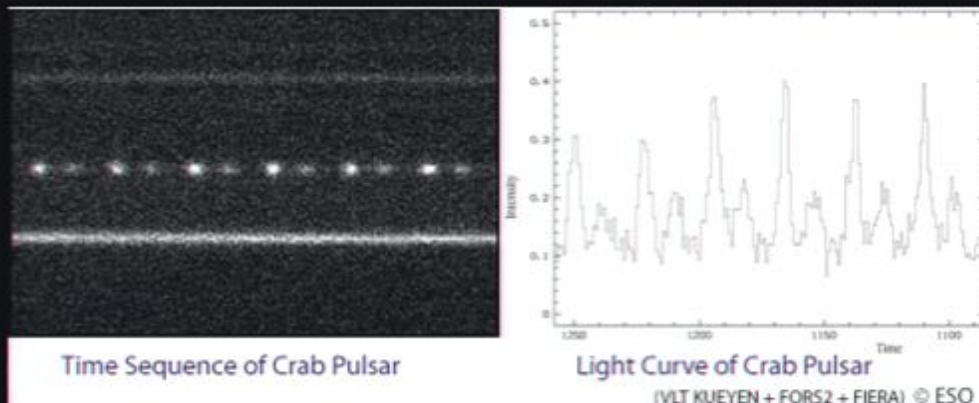
- A giant ball of neutrons.
- Mass : at least 1.4 x mass of the Sun to maximum of about 3 solar masses.
- Temperature 1 million degrees and cooling.
- Diameter: 20 km!
- Density:  $10^{18} \text{ kg/m}^3$ 
  - A sugar cube of this matter weighs 400 billion tons
- Day: 1 - 0.001 seconds!
- Magnetic fields as strong as the Sun, but in the space of a city.
- But just a theory until 1968





# Pulsars

- Discovered by Bell and Hewish in 1968
- Stands for pulsating stars, since they emit regular pulses
- Now known to be spinning neutron stars

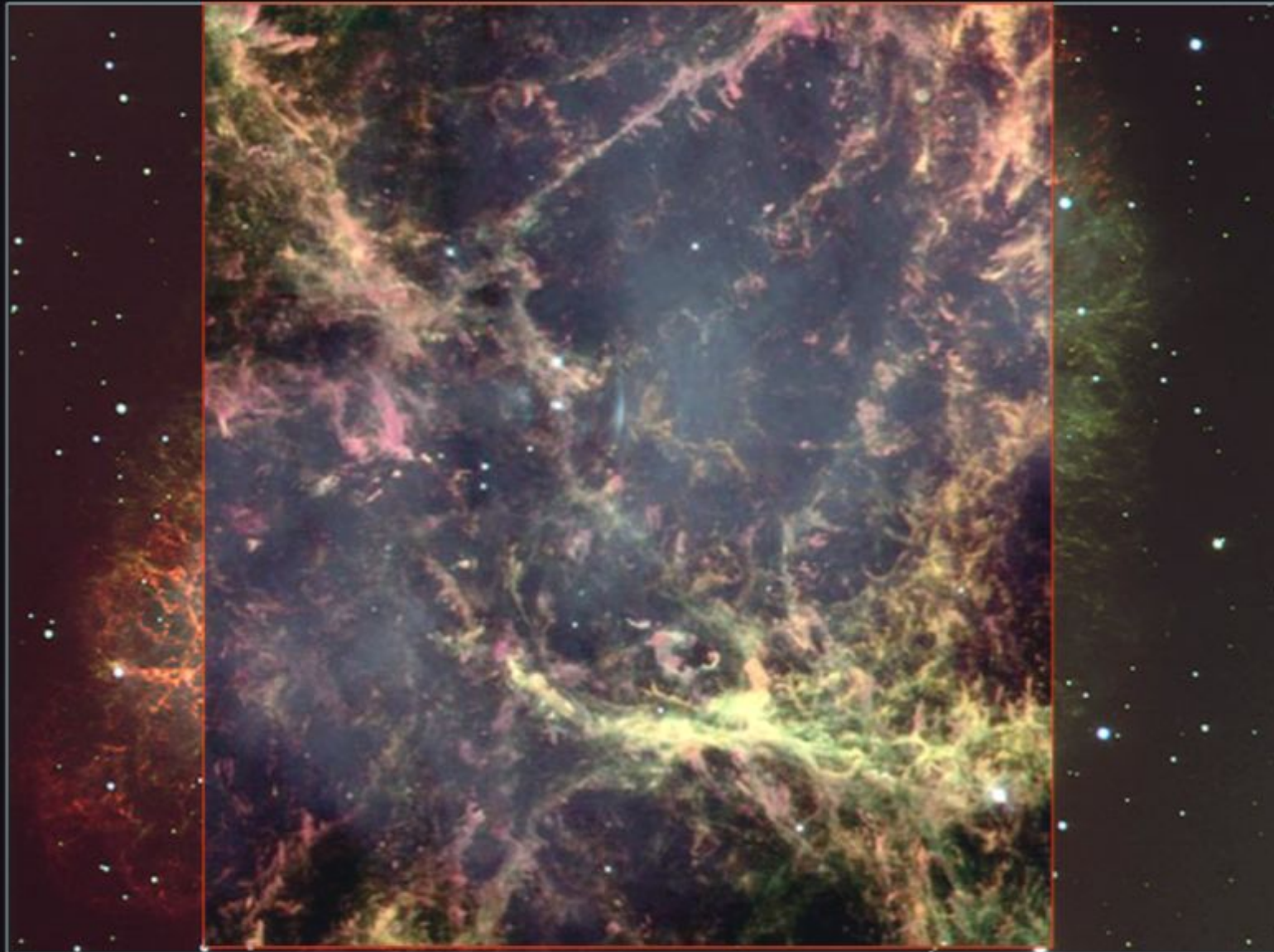


# Crab Nebula Pulsar



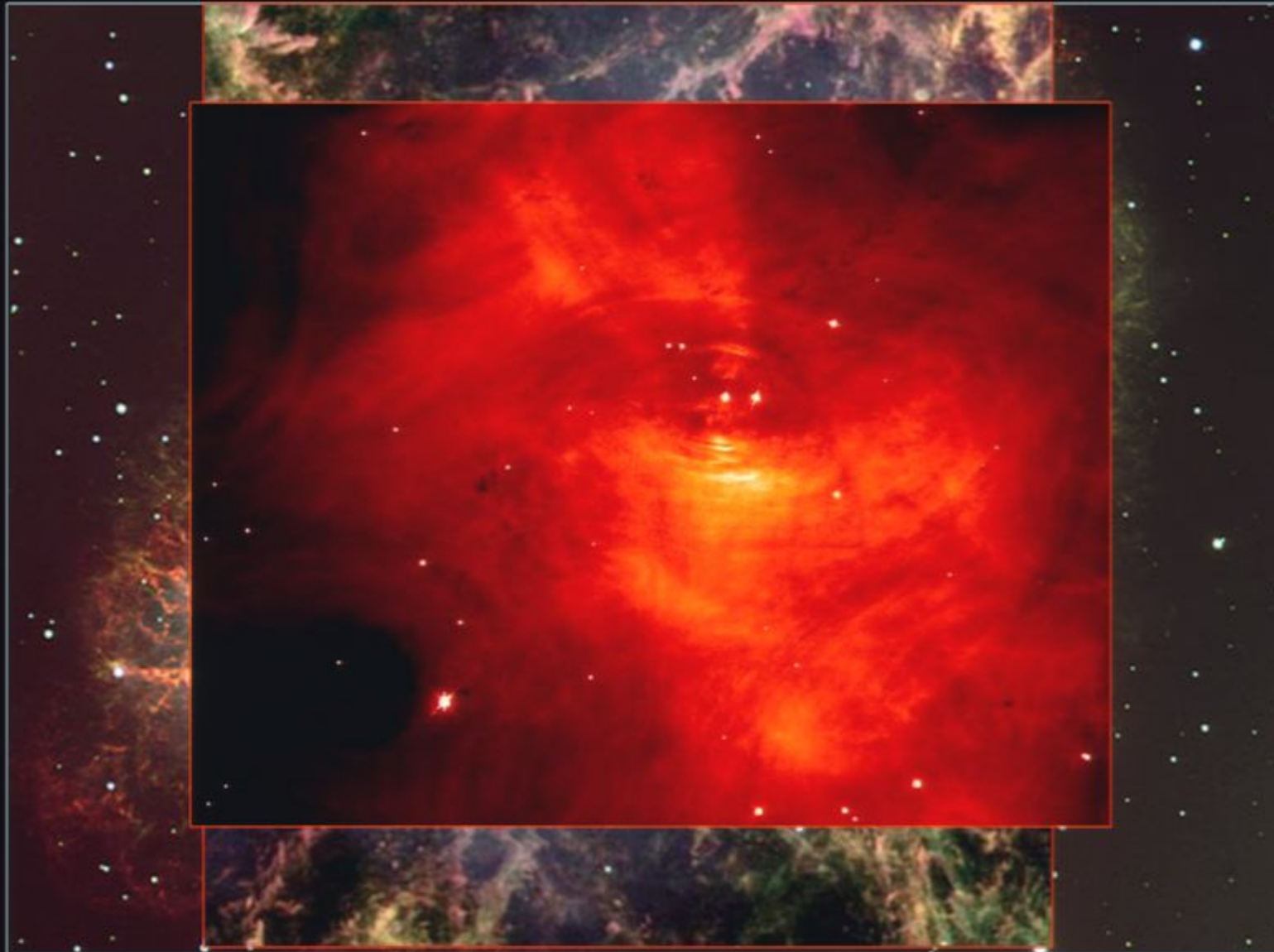


# Crab Nebula Pulsar

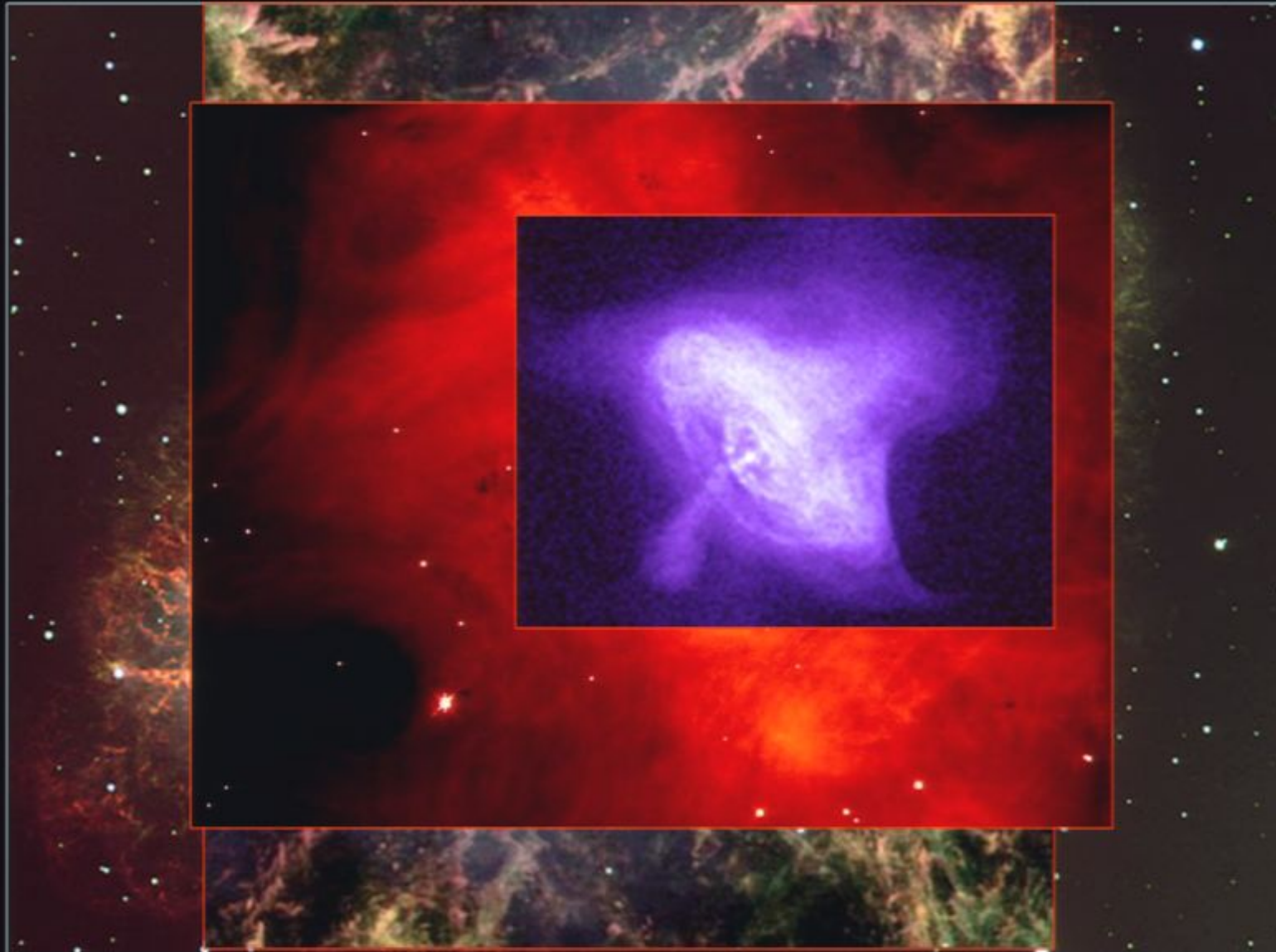




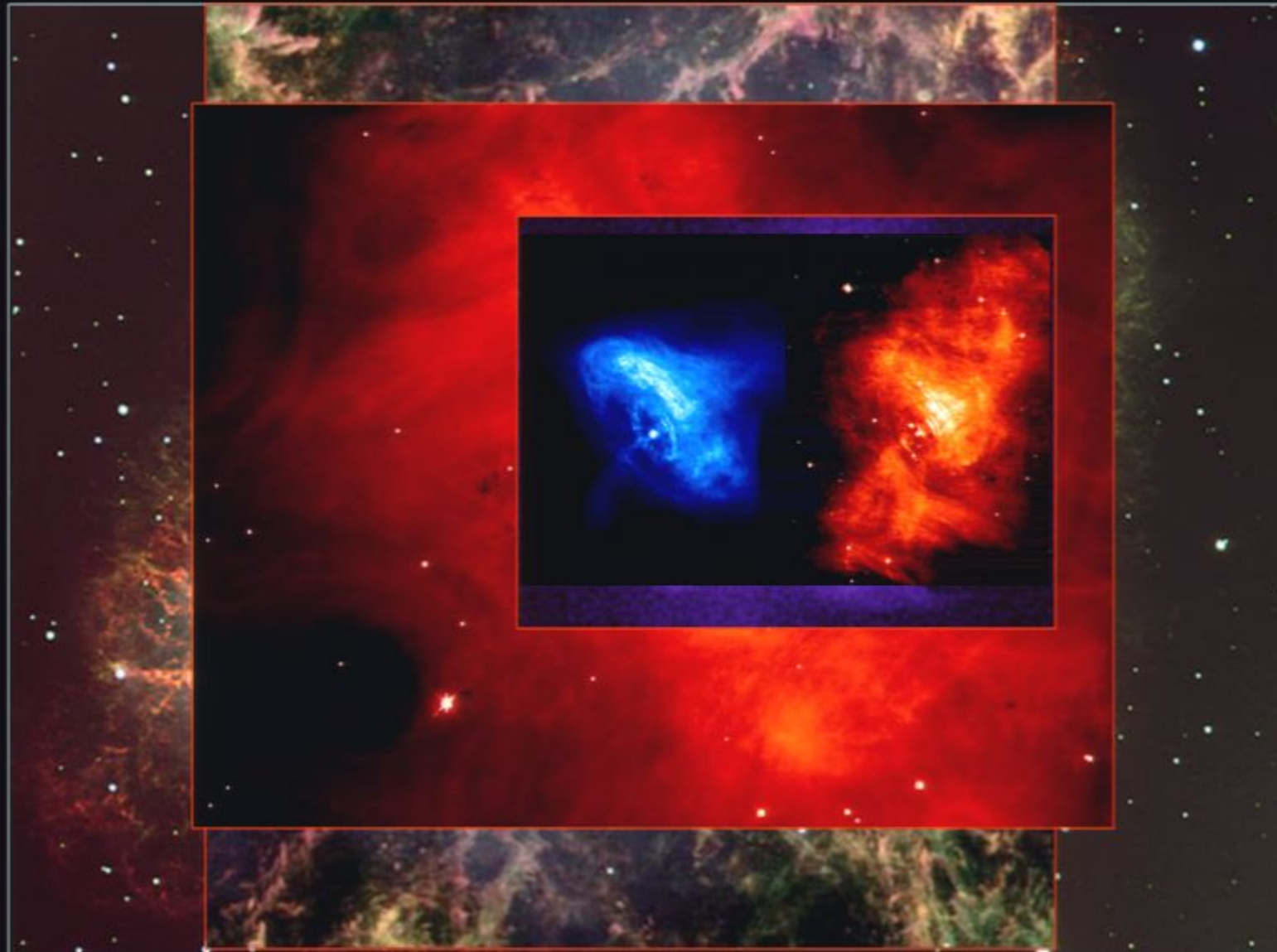
# Crab Nebula Pulsar



# Crab Nebula Pulsar



# Crab Nebula Pulsar





# What Next

# What Next

- Neutron stars are held up by neutron degeneracy pressure.
  - Recall electron degeneracy pressure for white dwarfs.
  - For white dwarfs, maximum mass of  $1.4 M_{\text{sun}}$
- For neutron stars, maximum mass  $\sim 3M_{\text{sun}}$
- What happens if a high-mass star is SO big that its central core is bigger than this?
- What happens when gravity is stronger than even neutron degeneracy pressure?
- How dense can something get?
- How strong can the force of gravity be?
- What if the escape velocity is faster than light?

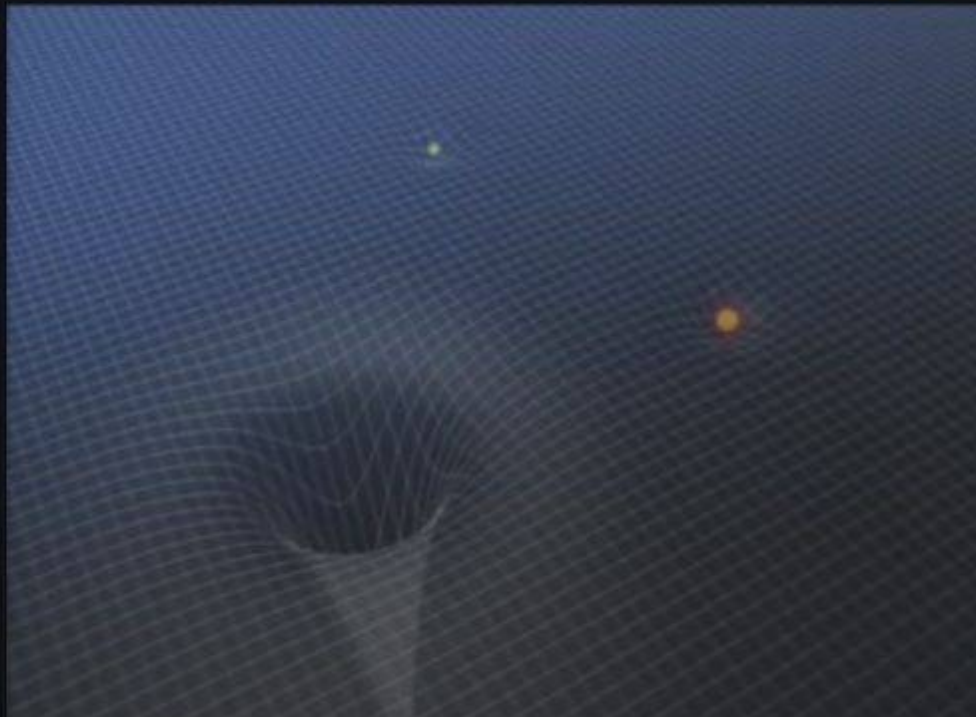
*If we could eliminate the radiation and light, what would it be like to watch the collapsing of a star into a Black Hole? What would it be like to fall into a Black Hole?*



# Watching a Star Collapse from a Safe Distance

*If you watched a star collapsing into a Black Hole, the light emitted from the star would be red-shifted and as a result would get dimmer by a factor of 2 every 20 microseconds per solar mass. At the same time the surface would appear to slow down and become frozen*

*This is not too Exciting... what about visiting the Black Hole?*



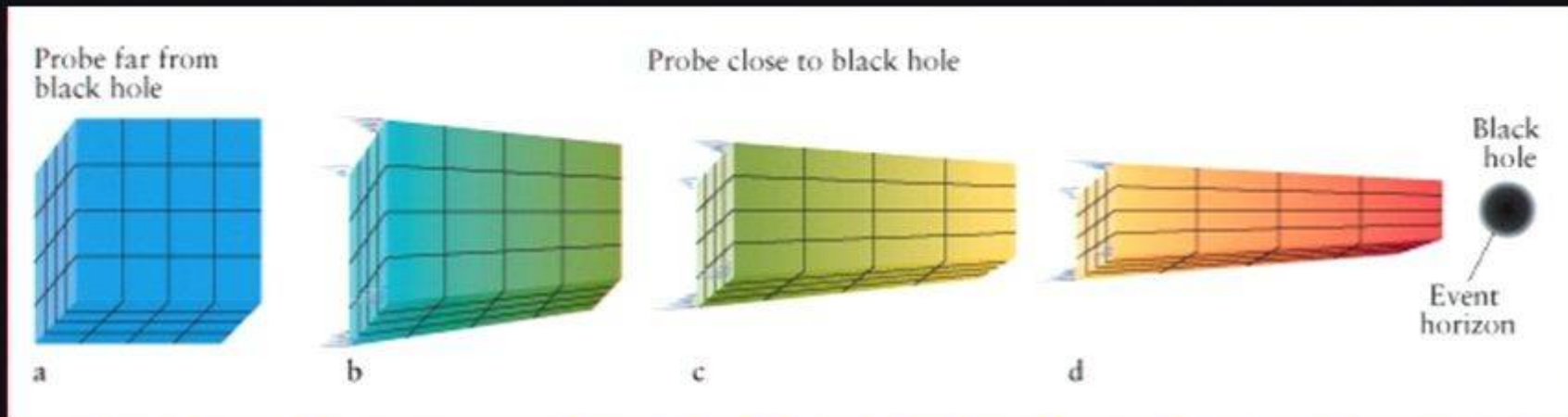
Pirsa: 0908000

$$L \propto e^{-\frac{t}{3\sqrt{3}M}}$$

$$t = 10^{-3} \left( \frac{M_{star}}{M_{\odot}} \right)$$

Page 72/150

# Traveling into a Black Hole



- As the ship approaches the black hole, the ship is elongated by the variation in gravity
- The ship is also gravitationally red shifted at the end closer to the black hole
- From the outside, the ship will appear to hover forever at the edge of the hole to us - an effect of the time dilation, yet in the ship, the occupants do enter into the black hole. Never to be heard from again.



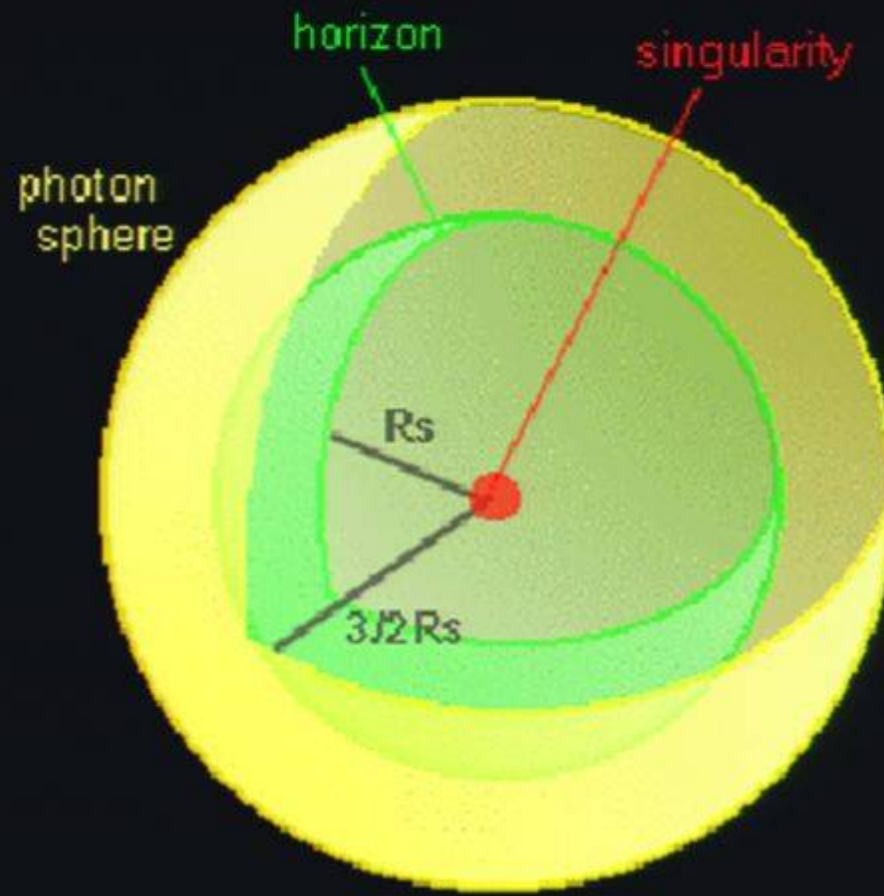
## *Watching a clock fall into a black hole*





*To get a better understanding of what is happening,  
and more specifically where it is happening. Let's look  
at the anatomy of a Black Hole*

# Structure of a Schwarzschild Black Hole

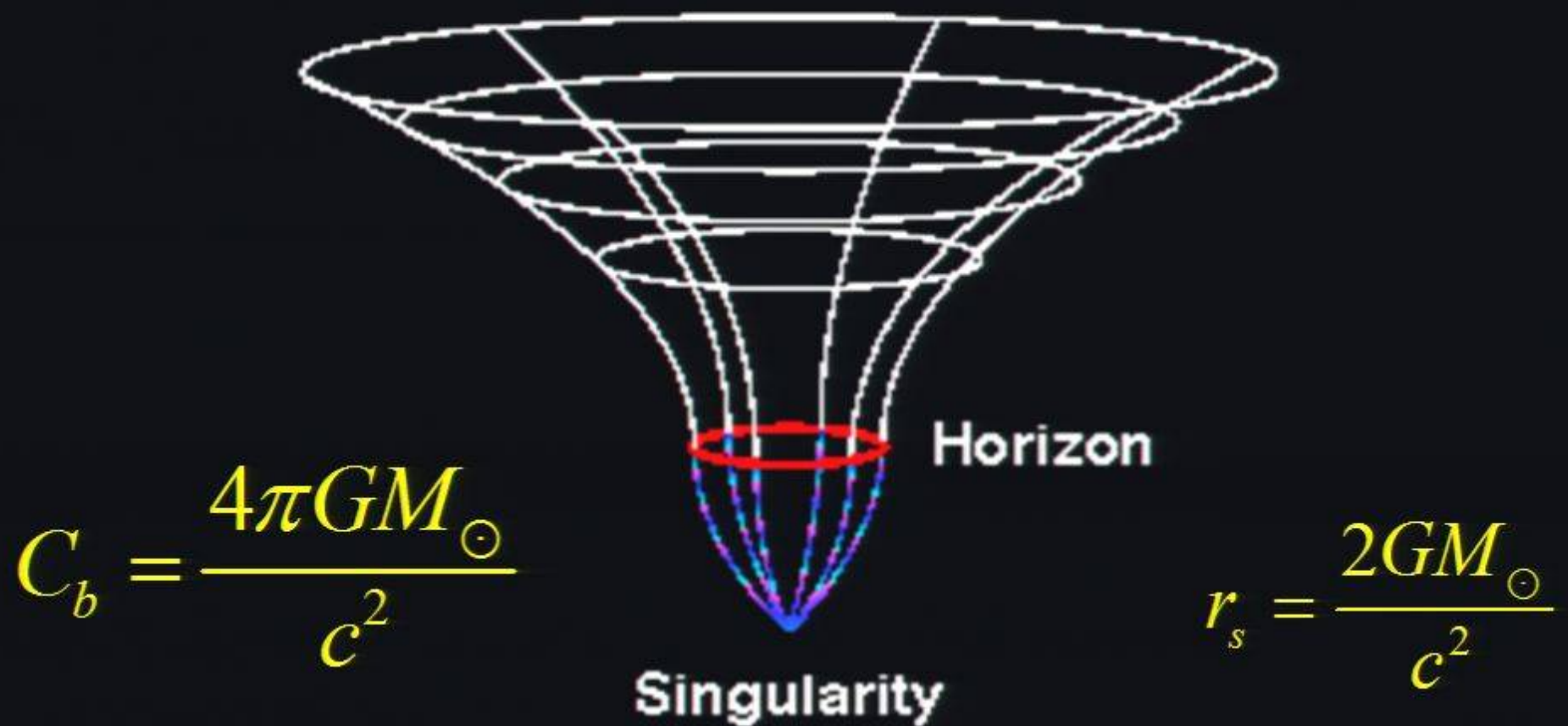


# Singularity

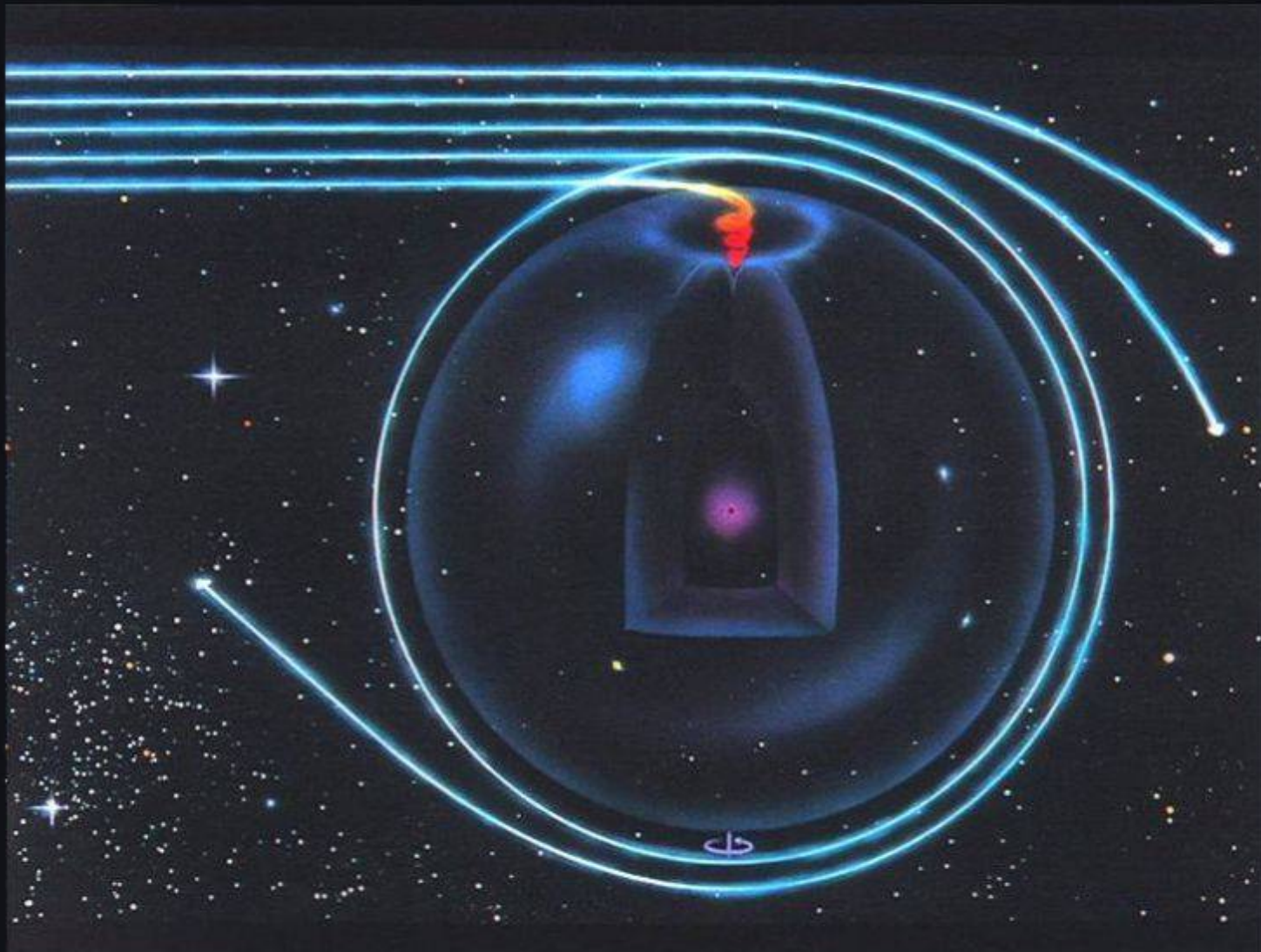
- *Within the singularity, matter is infinitely compressed into a region of infinite density. At the singularity, gravity is infinite. Space-time has become infinitely curved. At the present time, science has no tools to describe conditions within the singularity. All laws of physics lose meaning in such a region.*
- *At a singularity, space and time cease to exist as we know them. The laws of physics as we know them break down at a singularity, so it's not really possible to envision something with infinite density and zero volume.*



# Embedding Structure



# Photon orbits around a black hole



# Time Dilation and Blueshift

$$t_2 = \frac{t_1}{\sqrt{1 - \frac{C_b}{C}}}$$

*If you hovered at 1.00 000 1  
times the event horizon  
circumference, then one day  
for you would mean ...*



# Time Dilation and Blueshift

$$t_2 = \frac{t_1}{\sqrt{1 - \frac{C_b}{C}}}$$

*If you hovered at 1.00 000 1  
times the event horizon  
circumference, then one day  
for you would mean ...  
1024 days for the rest of  
the universe.*

$$\lambda_r = \lambda_e \sqrt{1 - \frac{C_b}{C}}$$

*If you hovered at 1.00 000 8  
times the event horizon  
circumference, visible light ( $5.8 \times 10^{-7} \text{ m}$ ) from the stars would  
appear at wavelength ...*

# The Effects

*No matter how powerful your starship, once you enter the Event Horizon, you might as well enjoy the trip, because you are going in.*



# Visiting a Black Hole





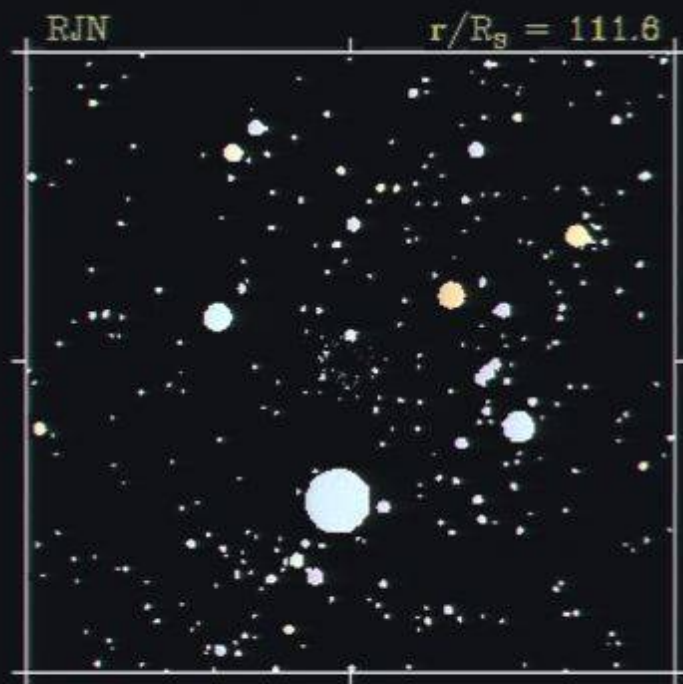
# Spaghettification!

$$\Delta a = \frac{16\pi^3 GLM_b}{C^3}$$

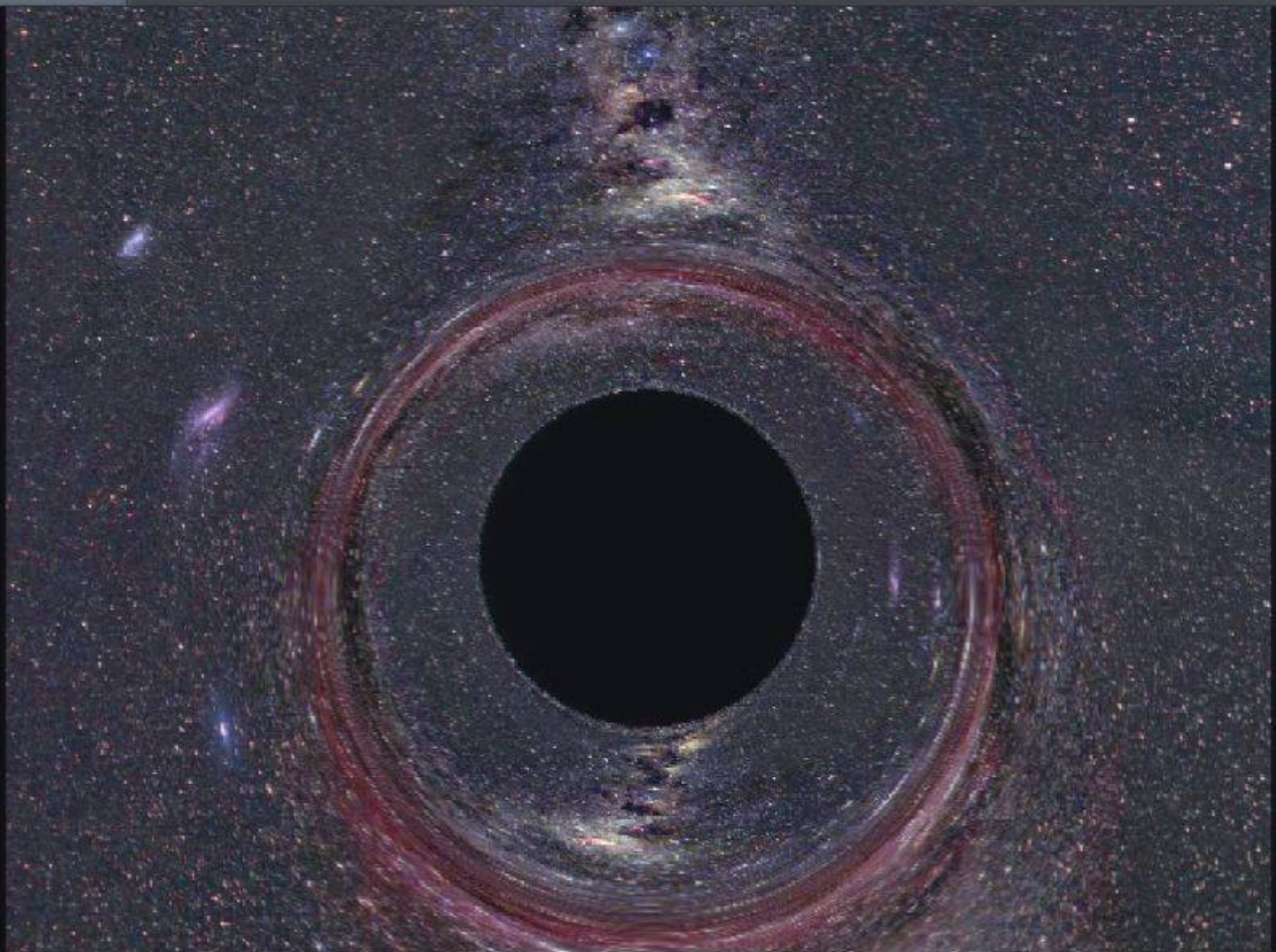


$$\Delta a \propto \frac{1}{M_b^2}$$

# Approaching

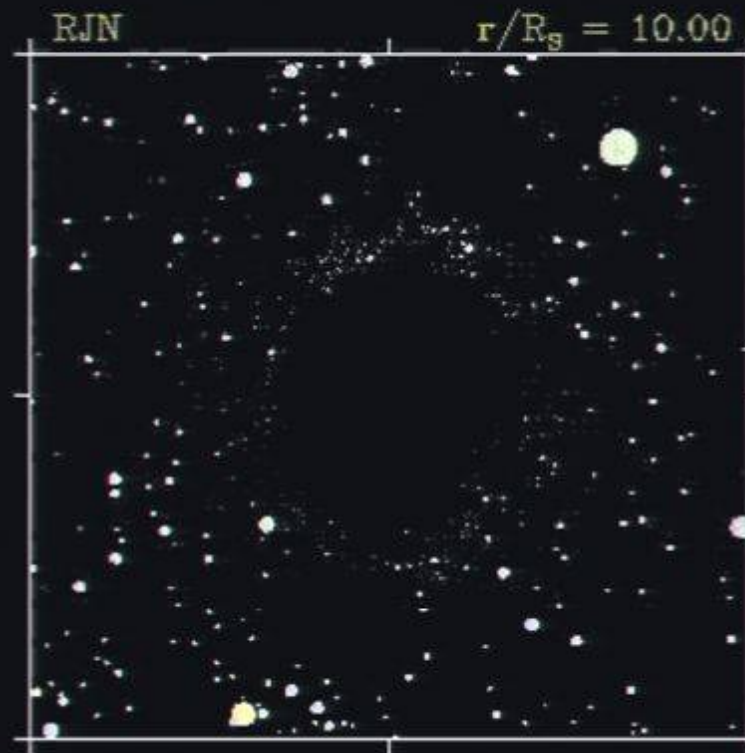


*Modern*

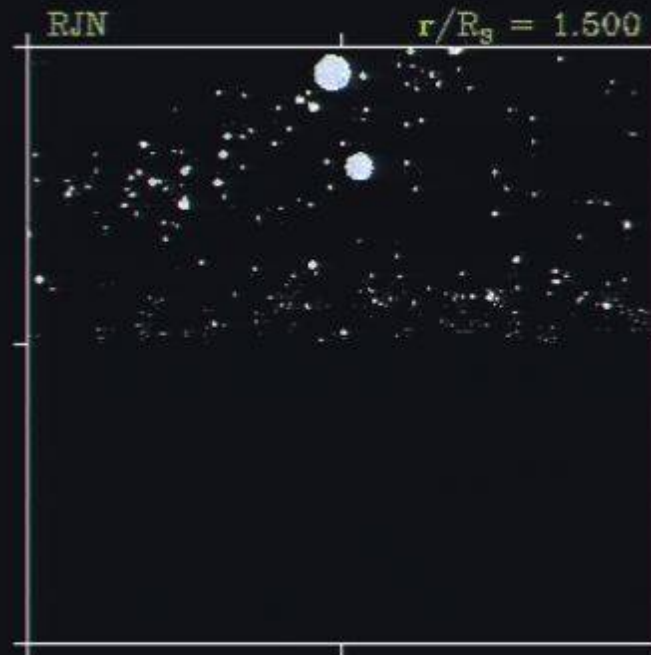




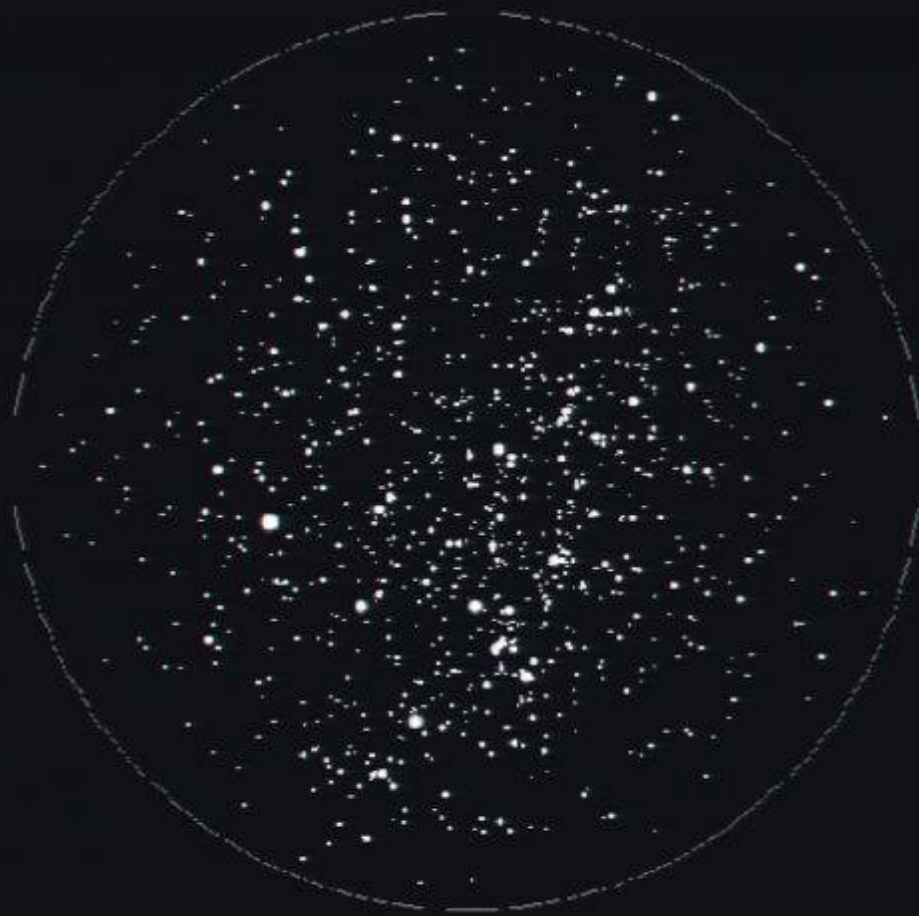
# Orbiting Black Hole Looking Down



# Orbiting Looking Horizontally at Photon Sphere



## Looking Up



$$r = 12 \tan \left( \frac{5\pi}{6} \sqrt{1 - \frac{C_b}{C}} \right)$$



*Forward*

*Sideways*

*Backwards*

*Forward*



*Sideways*



*Backwards*



$$r = 100 r_s$$

*Forward*



*Sideways*



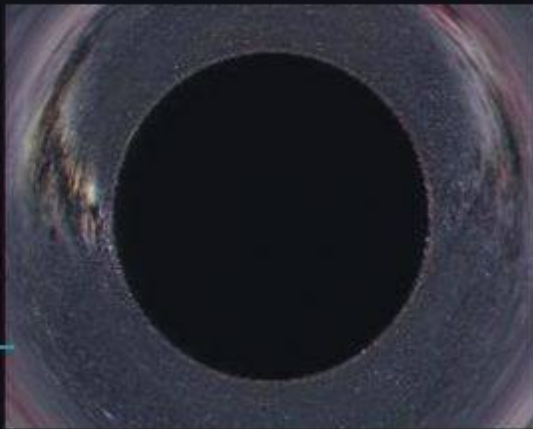
*Backwards*



$$r = 20 r_s$$



*Forward*



*Sideways*



*Backwards*

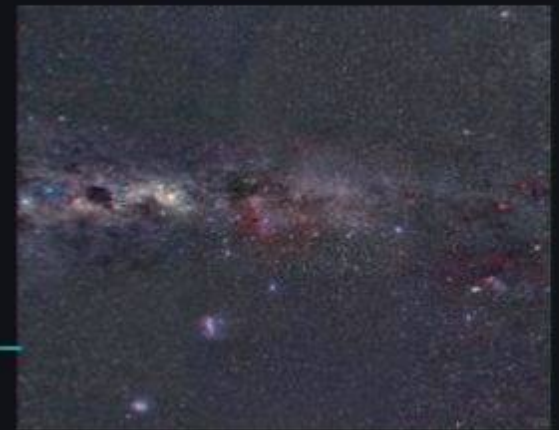


$$r = 4.5 r_s$$

*Forward*

*Sideways*

*Backwards*

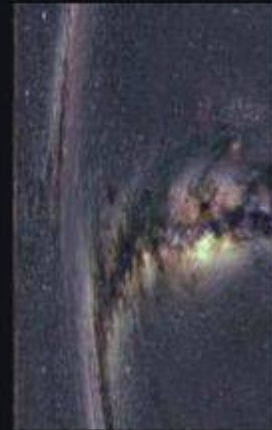


$$r = 2.5 r_s$$

*Forward*

*Sideways*

*Backwards*



$$r = 1.5 r_s$$



*Forward*

*Sideways*

*Backwards*



$$r = 1.2 r_s$$

*Forward*

*Sideways*

*Backwards*

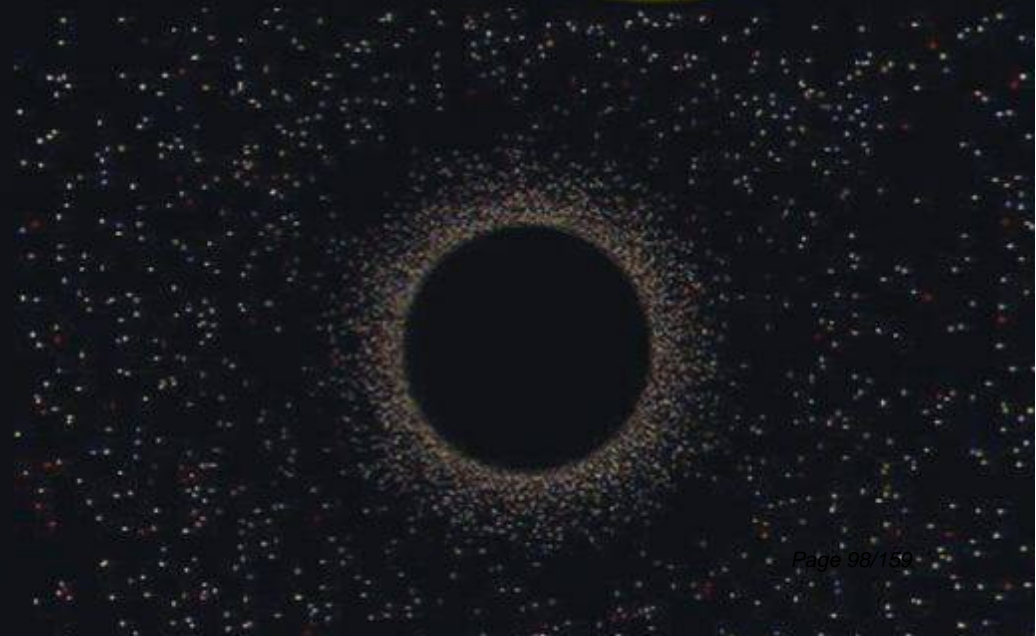
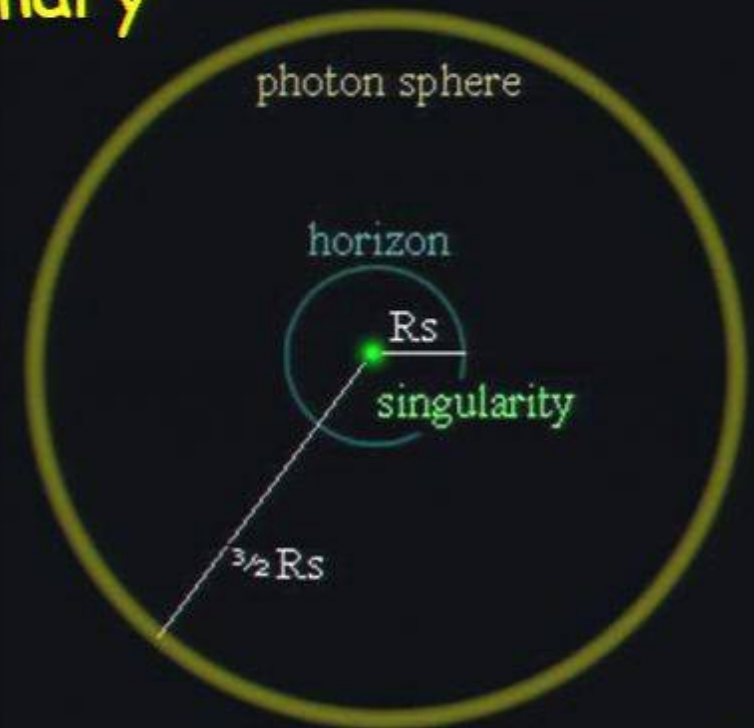


$$r = 1.005 r_s$$

# The Anatomy Summary

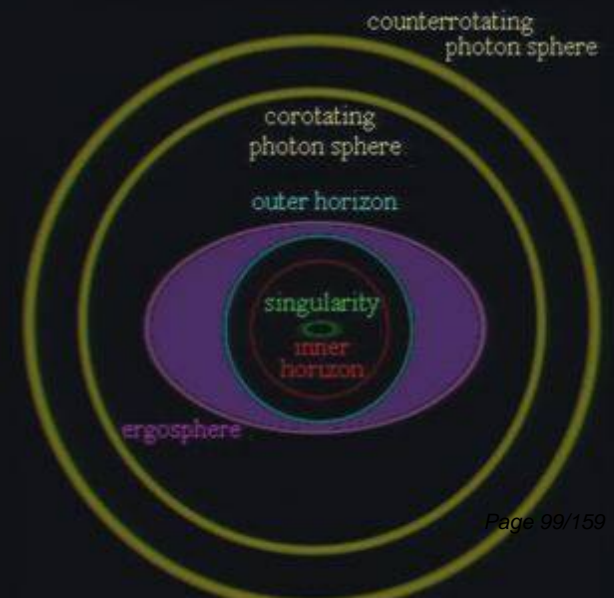
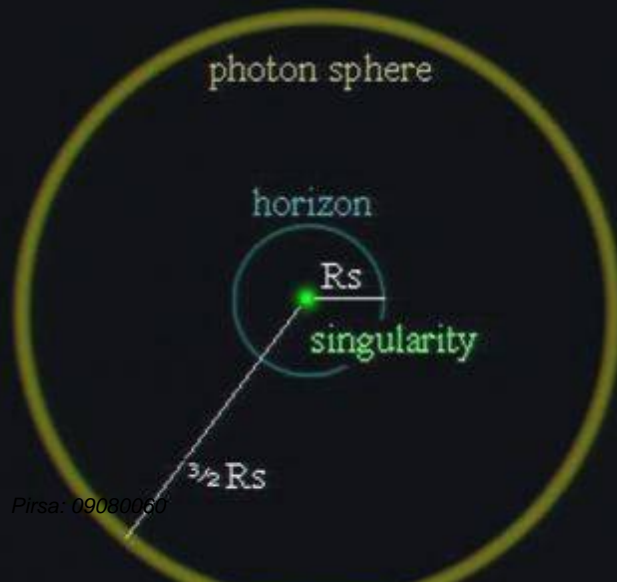
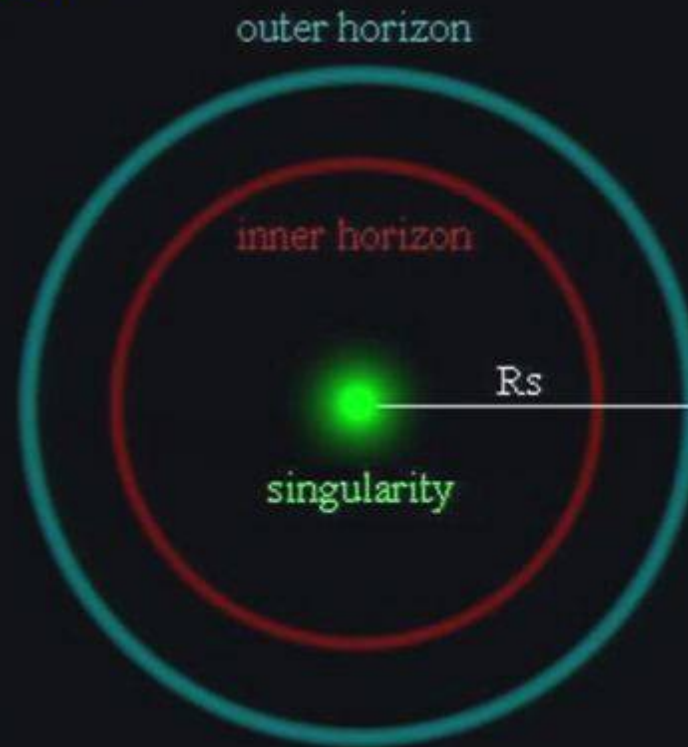
If you calculate the size of an object whose escape velocity is the speed of light, you get the "Schwarzschild radius", which defines the "event horizon". This is the formal size of a black hole (even though there is nothing at that location). It is given by  $R_s = 3\text{km}(M_*/M_{\text{sun}})$ . It is the horizon over which you can see no more events. Outside that at  $1.5 R_s$  photons would orbit the hole (the photon sphere).

Far from the hole, the gravity is the same as it would be if the star were still there (so no "vacuum cleaner" effect). If the Sun collapsed to a BH, the Earth's orbit would be unaffected.



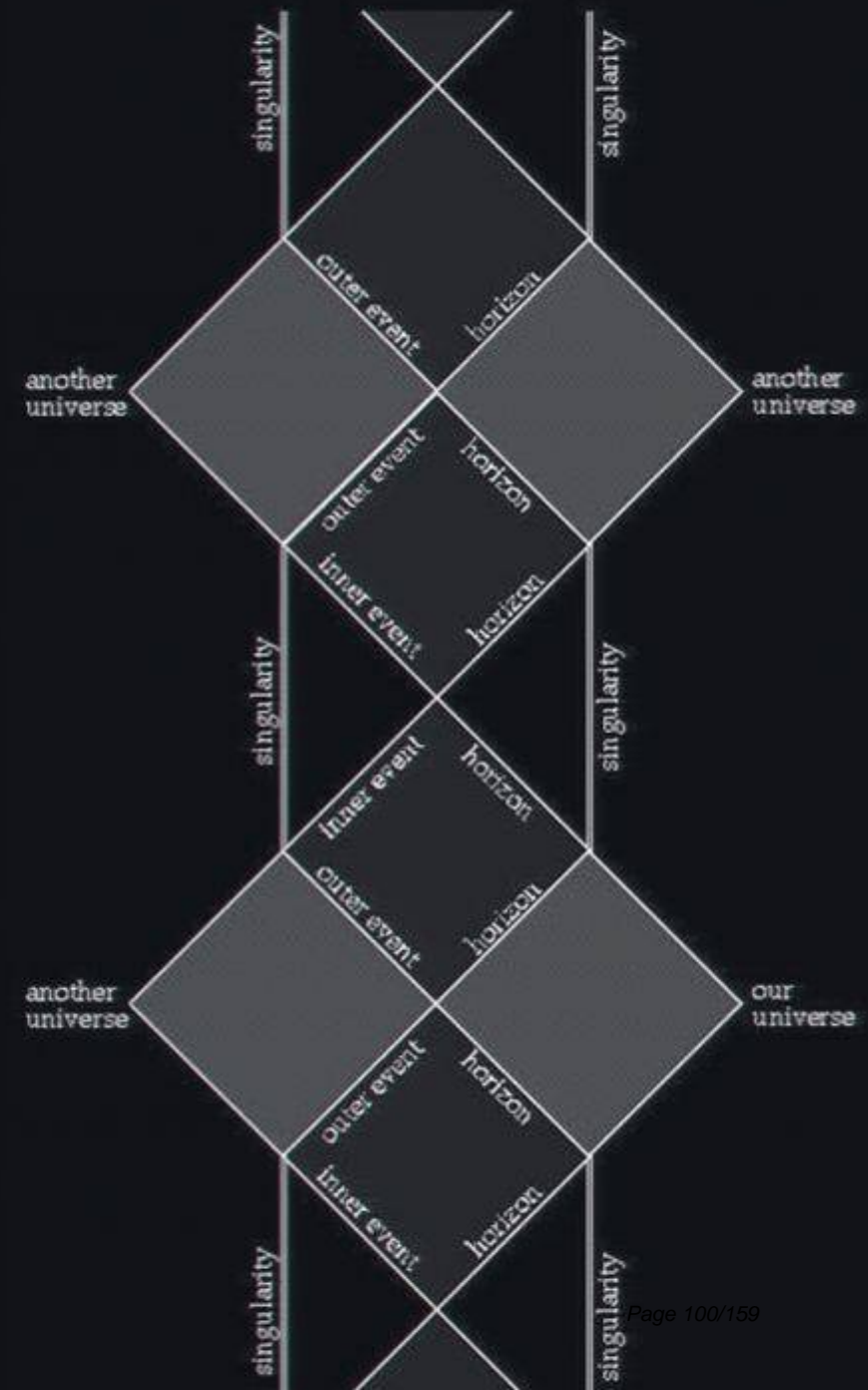
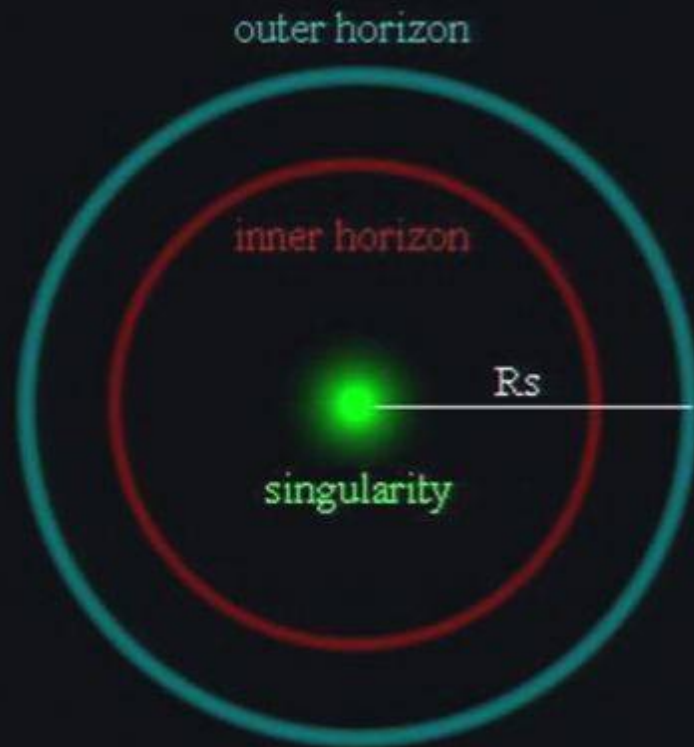


# Types of Black Holes

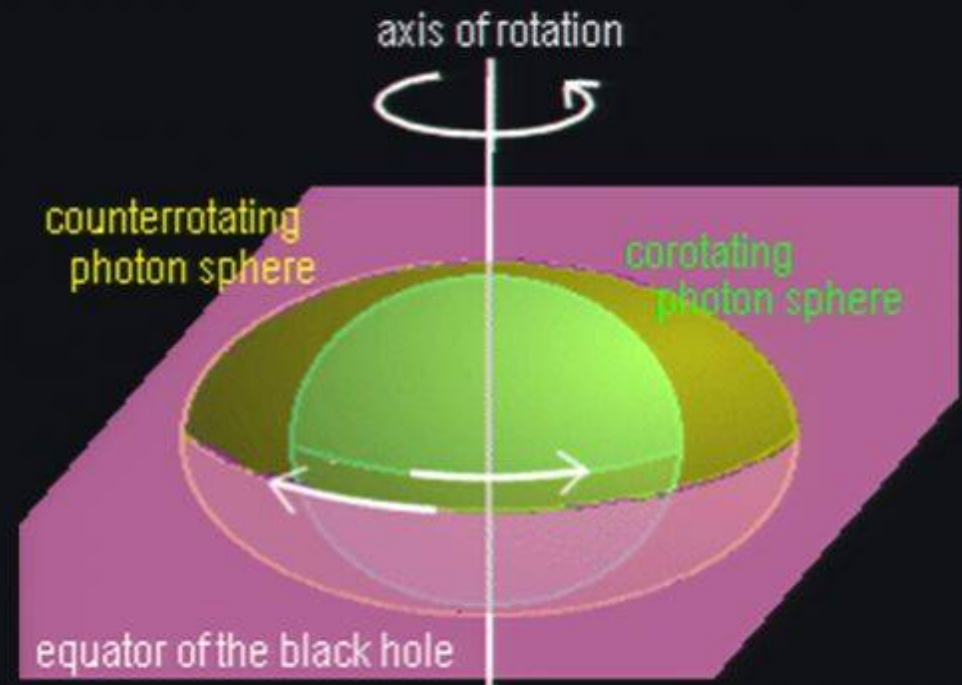
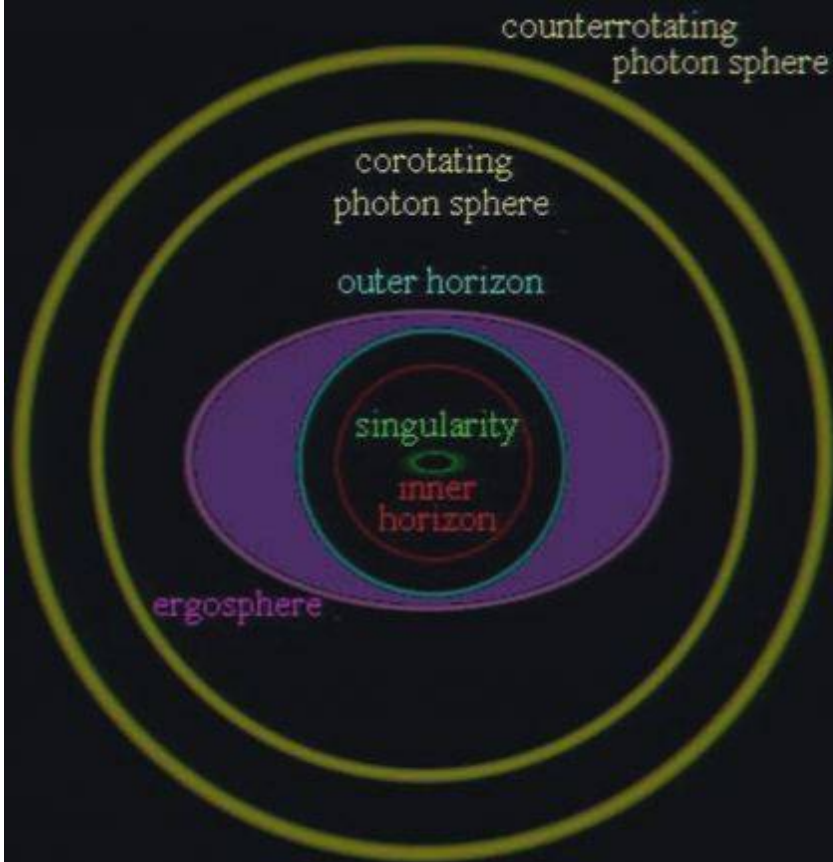


# Reissner-Nordström Black Hole

*An electrically Charged Black Hole*



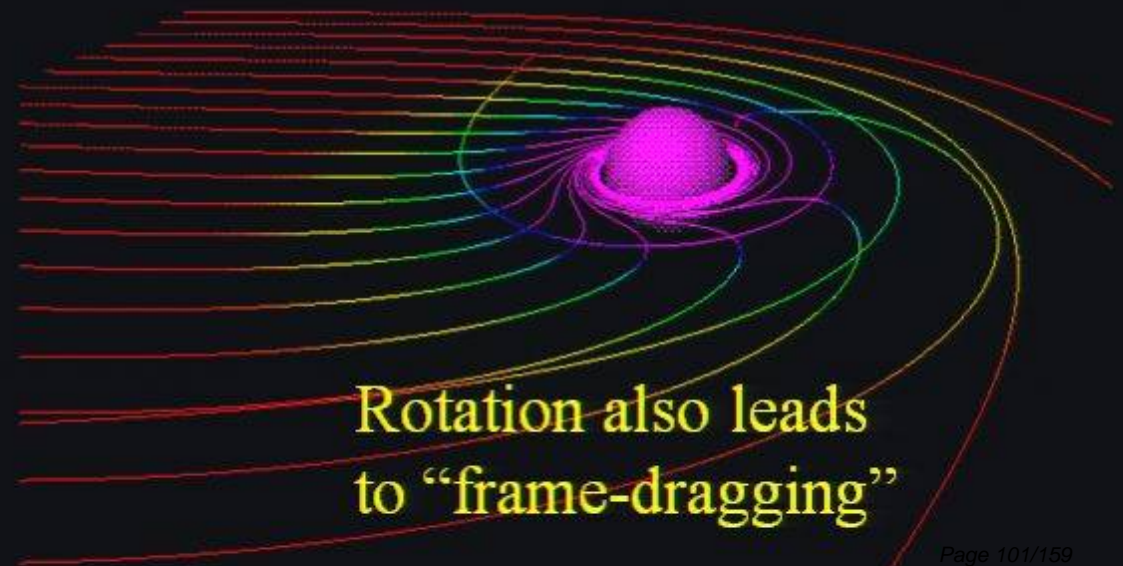
# Rotating Black Holes



$$r_{inner} = \frac{r_s + \sqrt{r_s^2 + 4 \frac{J}{Mc}}}{2}$$

$$r_{outer} = \frac{r_s + \sqrt{r_s^2 + 4 \left( \frac{J}{Mc} \cos(\theta) \right)^2}}{2}$$

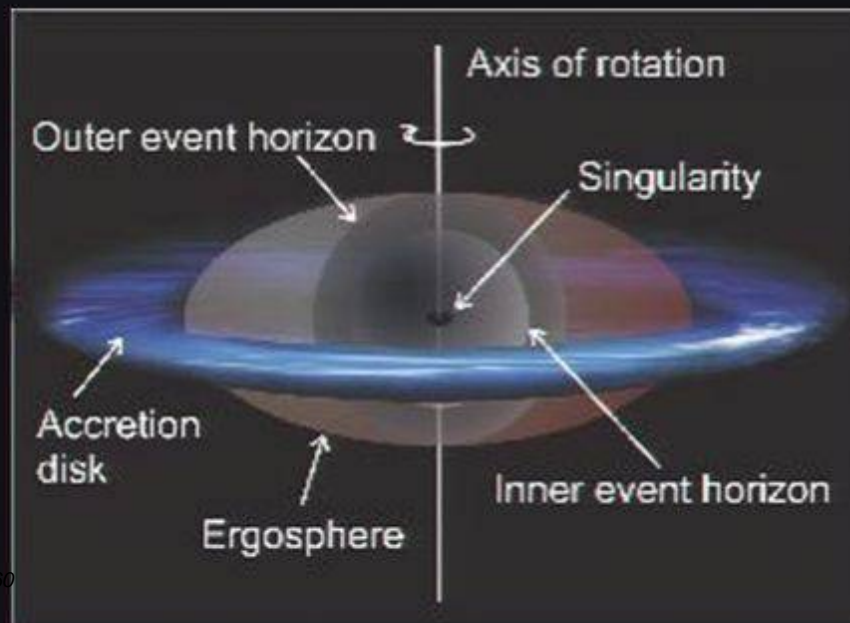
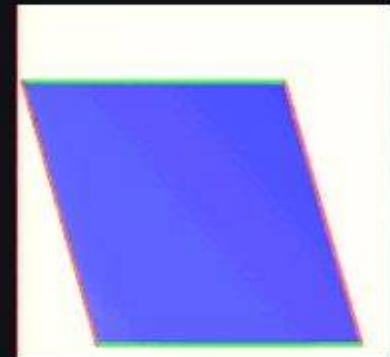
Prisa: 09089960





# A Rotating Black Hole (The Kerr Black Holes)

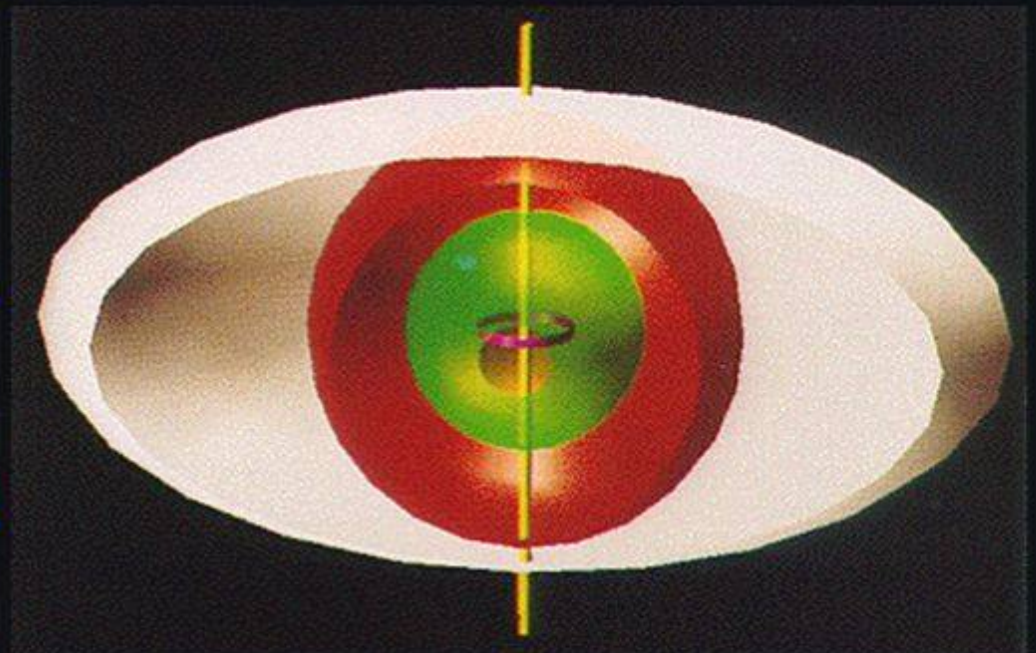
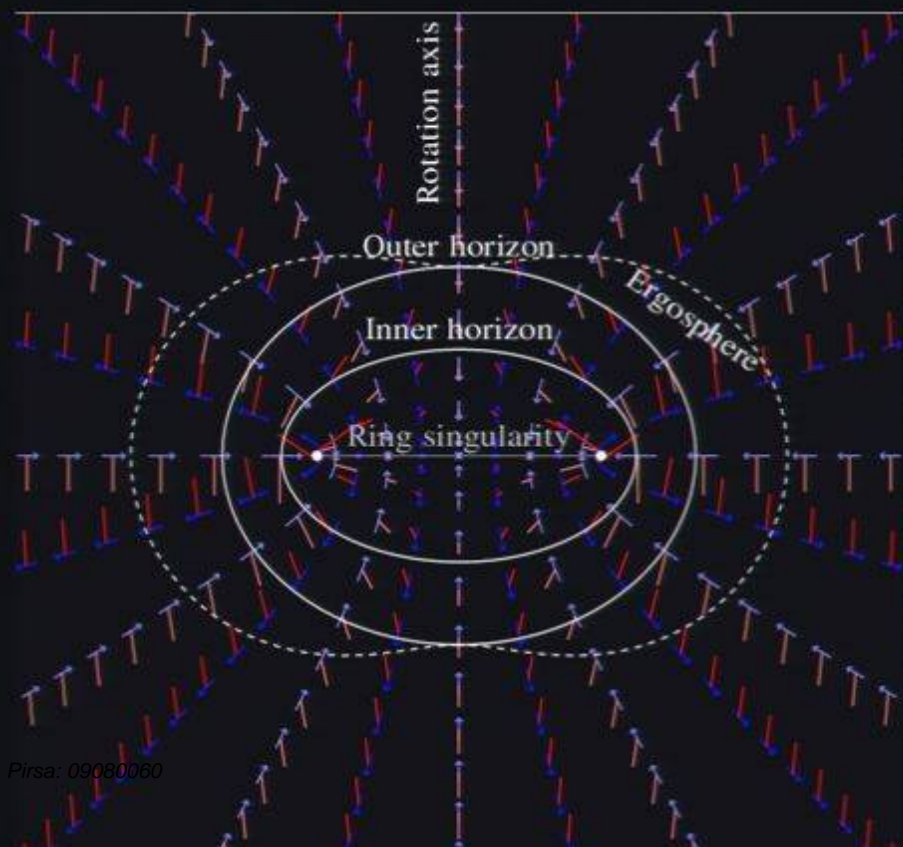
*Why is it called a rotating black hole?  
The event horizon doesn't rotate---it's  
just a boundary-line, Though anything  
inside the **ergosphere** must co-rotate,  
that nothing can remain stationary*



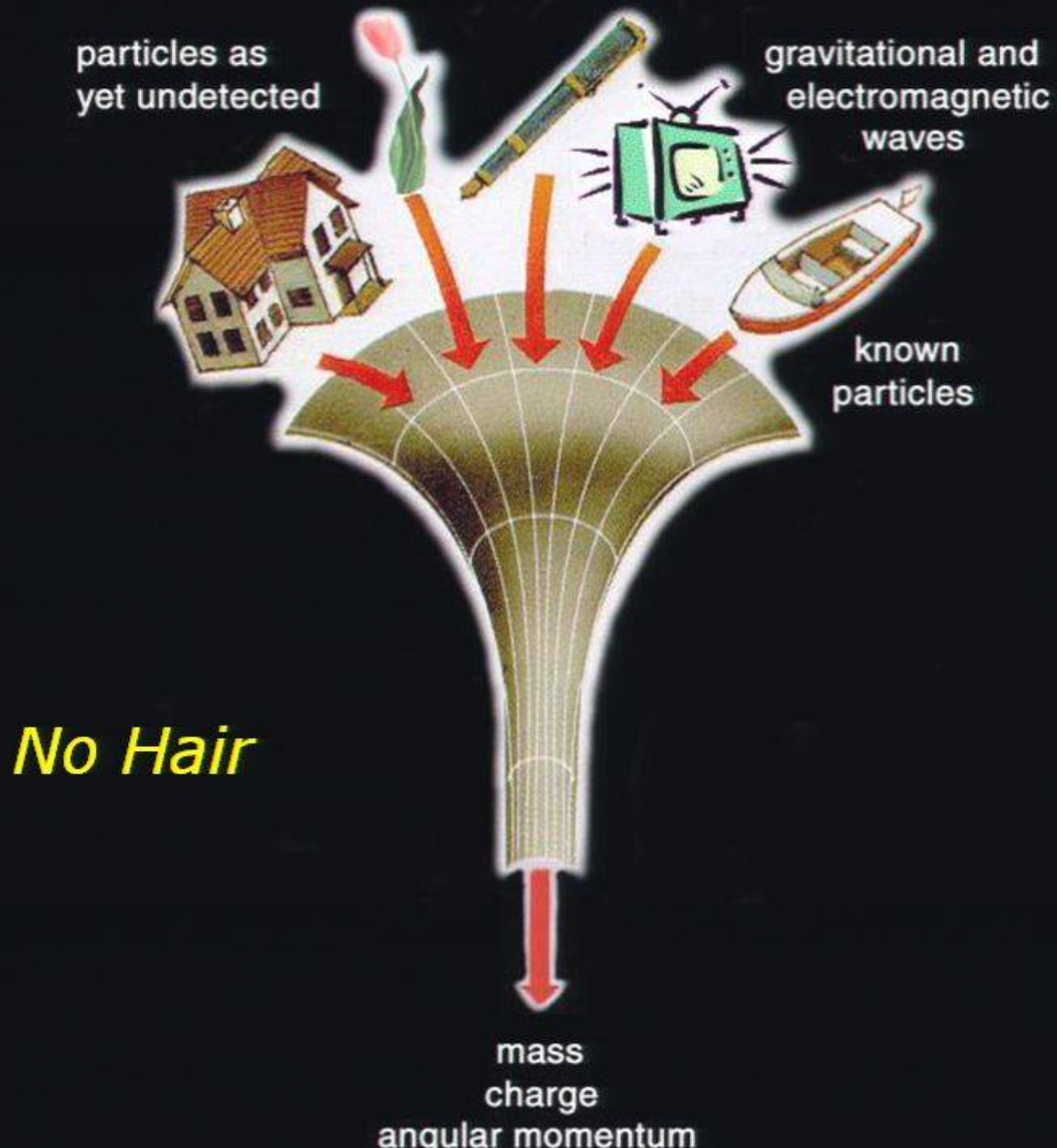
*The Penrose effect  
allows for the black  
hole to lose energy  
from **ergosphere** and  
thus will slow down  
and eventually stop*

# Kerr-Newman Black Hole

*Same Structure as Kerr Black Hole. But now it has a charge as well as a rotation. This type of Black hole is not a stable configuration.*









# No-hair theorem (well maybe 3 hairs)

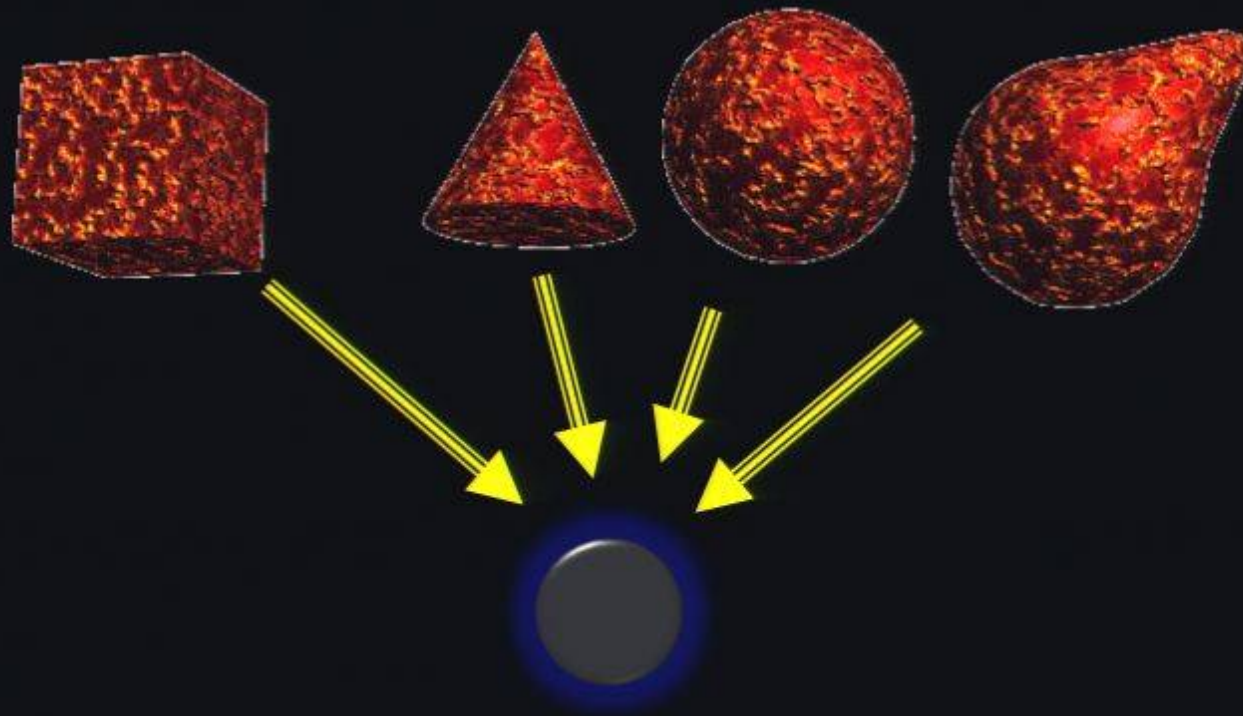
- A black hole has no hair;  
its only 'hair' are its

1. Mass
2. Angular momentum
3. Electric charge



John A. Wheeler (b1911)

# Stars of all Shapes and Sizes



*All end up looking the same*

# Types of black holes

- Schwarzschild (1916)
  - mass
- Reissner-Nordström (1916, 1918)
  - mass, electric charge
- Kerr (1963)
  - mass, angular momentum
- Kerr-Newman (1965)
  - mass, angular momentum, electric charge





# Latest Mathematical Model of falling into a Black Hole



# Entropy of Black Hole

- **Black hole presents us with a problem: What happens to the information when a particle falls inside a Black Hole?**
- **Remember only 3 parameters are required to describe a Black Hole (charge, mass, and angular momentum).**
- **In order to describe a physical system, we need entropy (a measure of disorder).**
- **Hawking had no problem with this “entropy eater”**
- **Hawking (after changing mind) and Bekenstein produced laws of Black Hole mechanics that bore an amazing resemblance to laws of thermodynamics.**
- **The 2<sup>nd</sup> law of thermodynamics “Entropy (randomness) increases**
- **You replace “Horizon Area” with “Entropy”**

$$S(\text{entropy}) = \frac{kAc^3}{4hG}$$

# Entropy of Black Hole

*New problem: if the Black Hole has an entropy, it must have a temperature too.*

*Worse Problem: If it has a temperature it must radiate, but in classical definition, nothing can escape a Black Hole.*

*Crisis:*

- *Several ways to picture how a black Hole evaporates*
  - *Some ways correspond to different ways of formulating laws of quantum fields.*
  - *Some ways correspond to String Theory*
  - *Some ways correspond to Quantum Gravity*
  - *Some ways make no sense at all.*
  - *Next Talk will discuss this.*





Stephen W. Hawking (b1942)

# Hawking radiation

*Virtual photon is  
its own  
antiparticle*

virtual  
particles

*Black Holes Ain't So Black*

# Hawking Radiation

- The Hawking Radiation theory states that virtual particle-antiparticle pairs are sometimes created outside the event horizon of a black hole. Three things can happen to a pair of particles just outside the event horizon:
  - Both particles are pulled into the black hole.
  - Both particles escape from the black hole.
  - One particle escapes while the other is pulled into the black hole.
- For the third possibility, the particle that has escaped becomes real and can therefore be observed from Earth. The energy to separate the two virtual particles (thus making them real particles) is taken from the horizon, thus reducing the energy of the Black Hole.
- The wavelength of the particle/wave that enters the a hole will be of 25% of the hole's circumference.
- **For Example:** A black hole of 2 Solar Masses with a circumference of about 35Km will emit a wavelength of:

$$\frac{35}{4} \approx 9 \text{ km}$$



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# Hawking Radiation

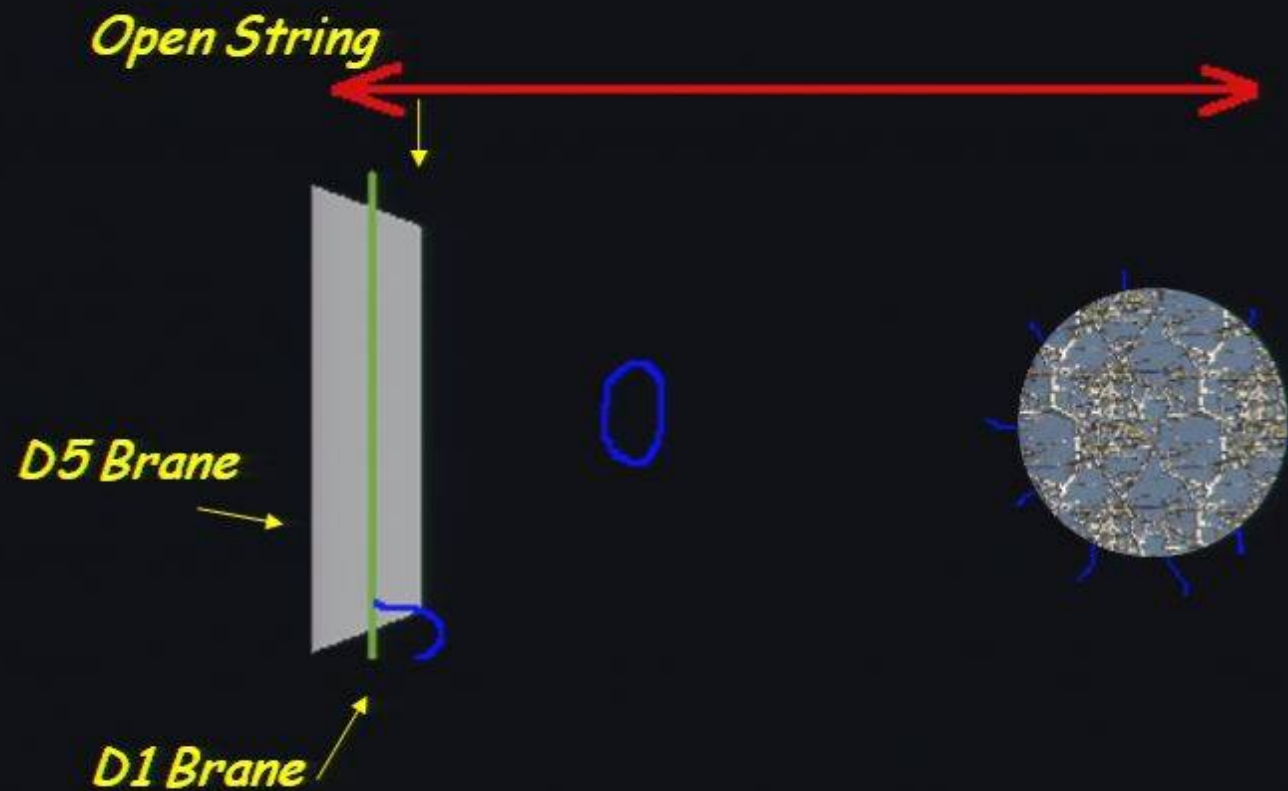
- The larger (more massive) the Black Hole the lower the temperature and the longer it takes to evaporate.

$$Temp_K \approx \frac{6 \times 10^{-8}}{M_{\oplus}}$$

$$time \approx 10^{66} \cdot [M_{\oplus}]^3$$

- Remember the age of the Universe is  $10^{10}$  years give or take 3 days.

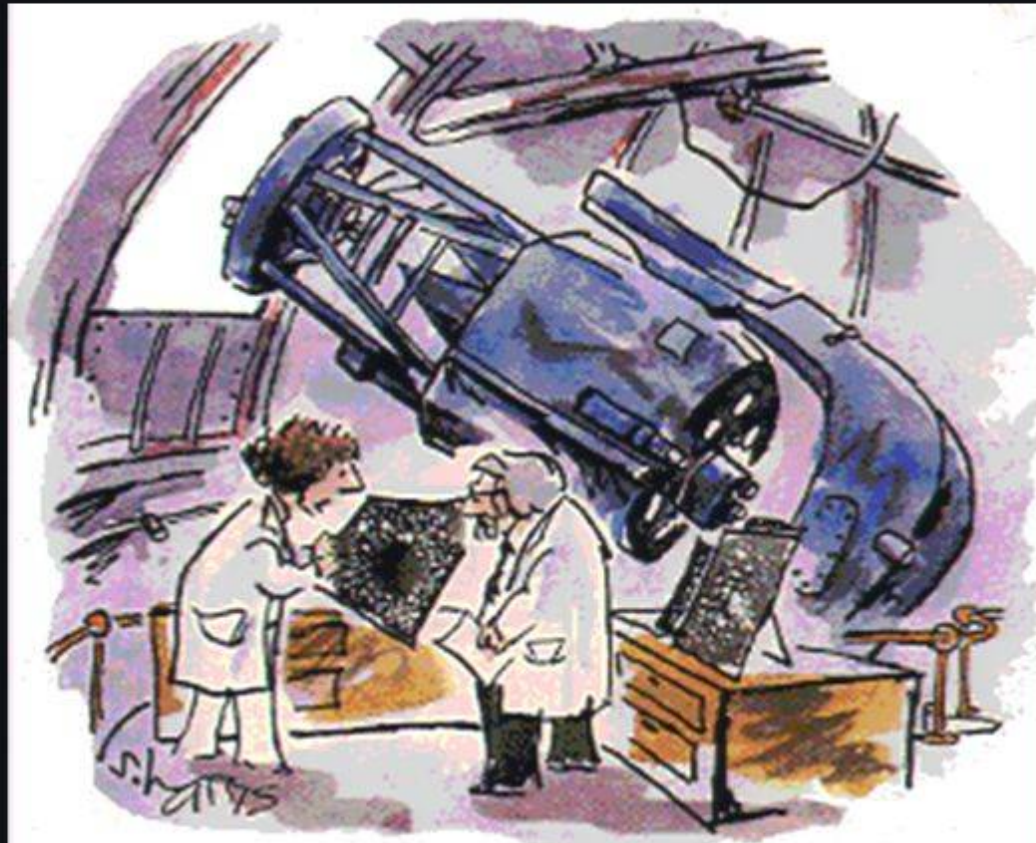
# Superstring Method



*One of the most dramatic recent results in string theory is the derivation of the Bekenstein-Hawking entropy*

# Are Black Holes Real

*What are we going to look for if Black Holes are Real*



*Sidney Harris*

"It's black, and it looks like a hole.  
I'd say it's a black hole."



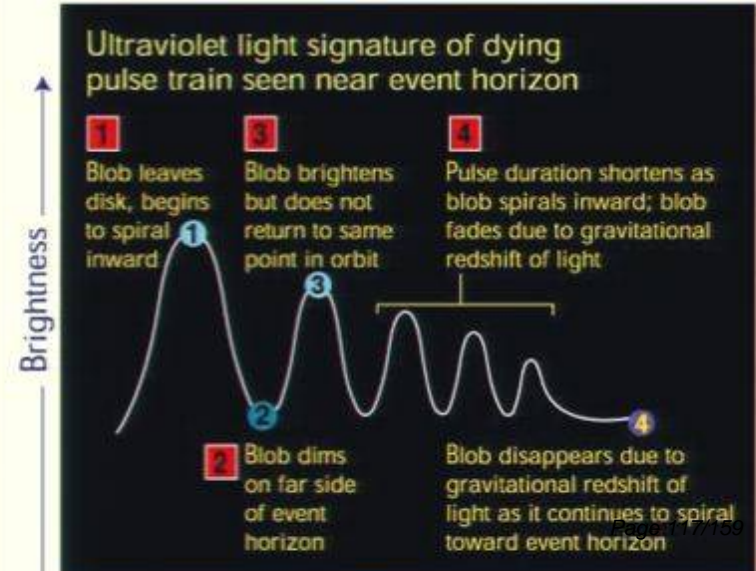
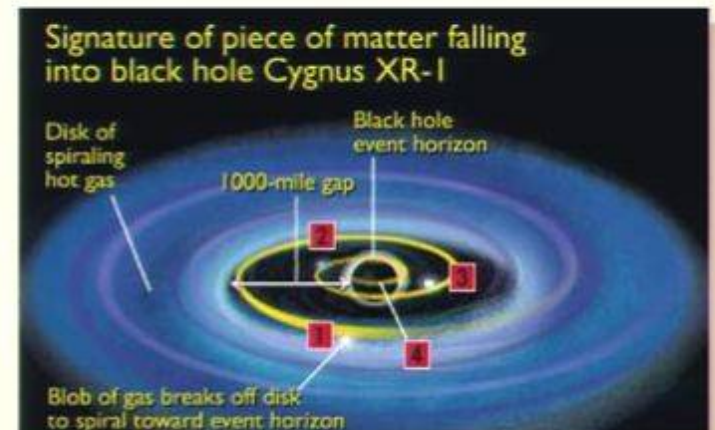
# Finding Black Holes

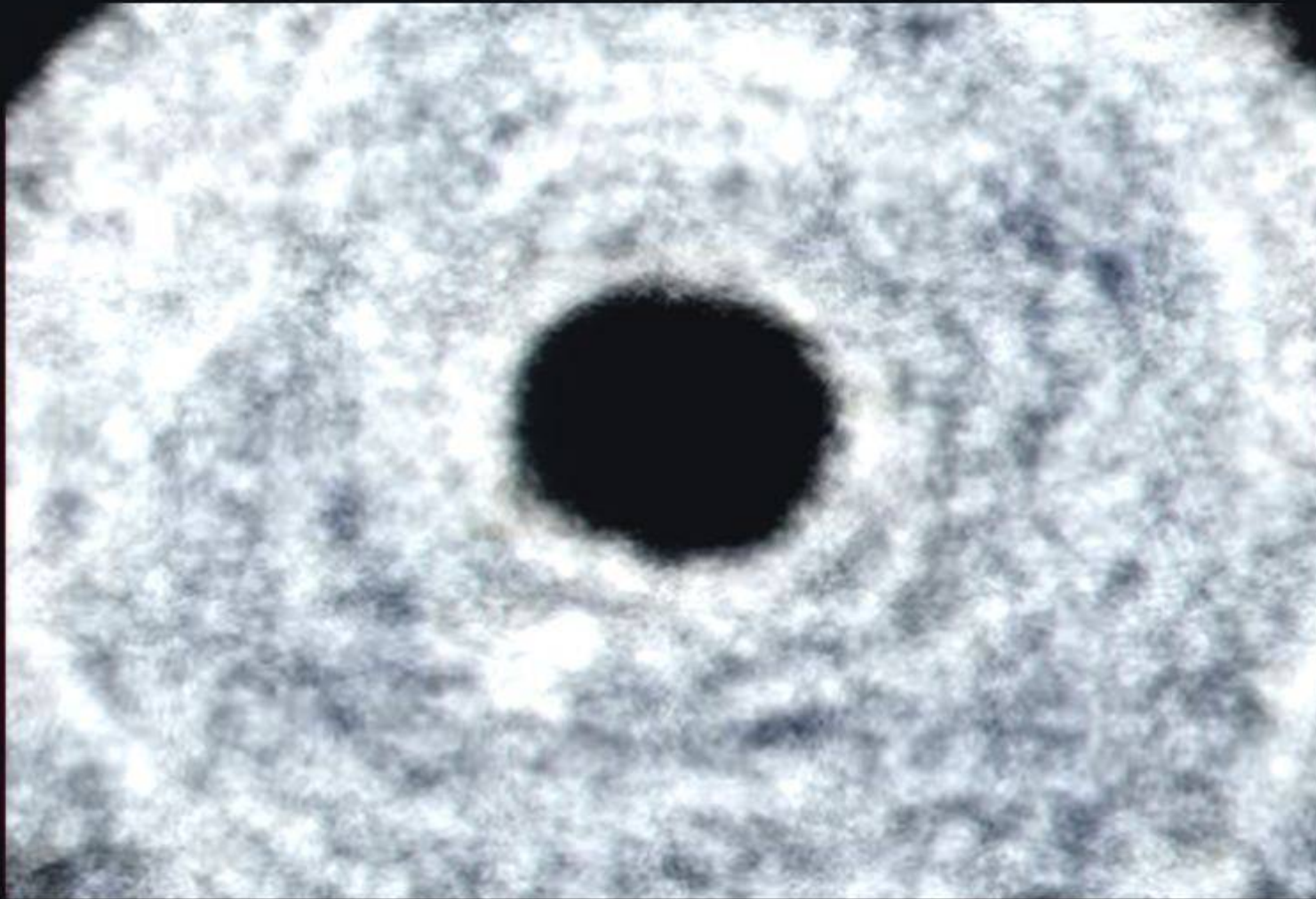
## Ultraviolet and X-rays

### Seeing Matter Disappear

Hubble observed pulses of UV light emitted by material as it fell into a black hole.

- Pulses arise from material orbiting around intense gravity of the black hole.
- Light pulses, lasting 0.2 s, are red-shifted from X-ray to UV, as they fall into gravity of the black hole.



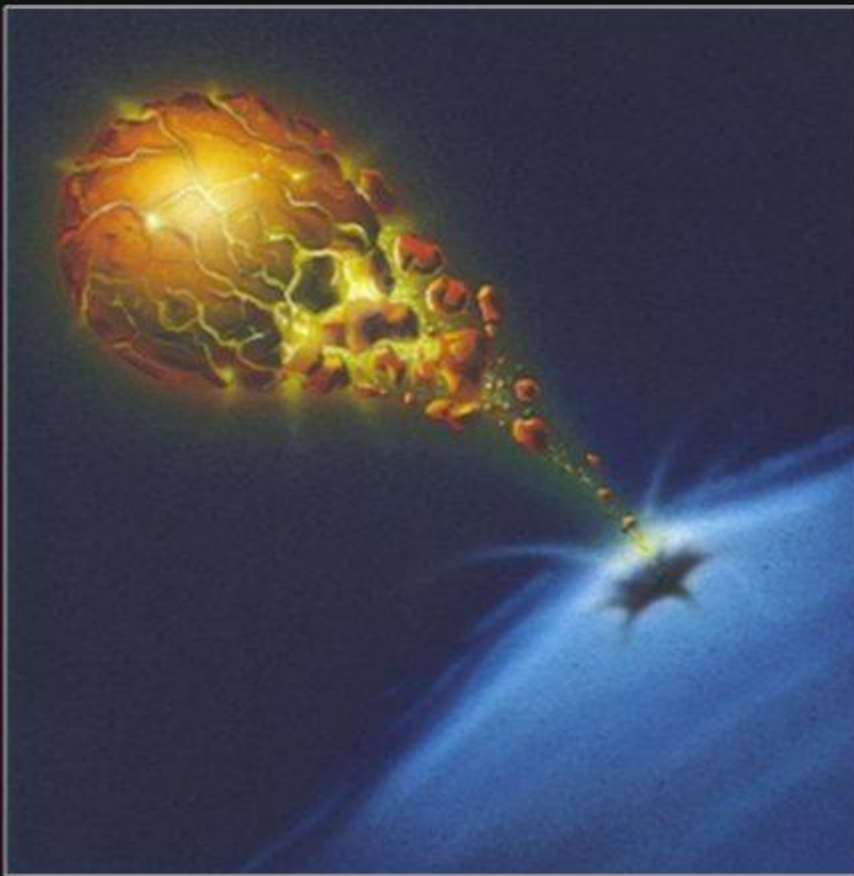


• Zel'dovich speculated that if a black hole was surrounded by gas and this gas was orbiting the black hole in an accretion disk, it would give off x-rays

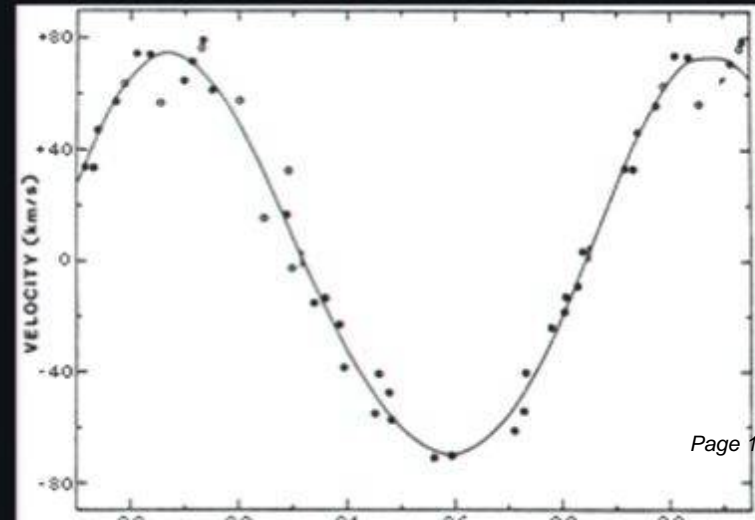
• The U.S. then used WW2 V-2 rockets with a simple x-ray machine in the 1940s to see if it could detect black holes



# Seeing Holes



- Can't see black hole itself, but can see matter falling into a hole.
- Gravitational forces stretch and rip matter: heats up.
- Very hot objects emit in X-rays (interior of Sun)



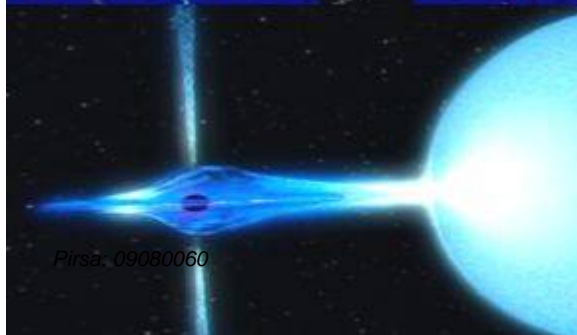
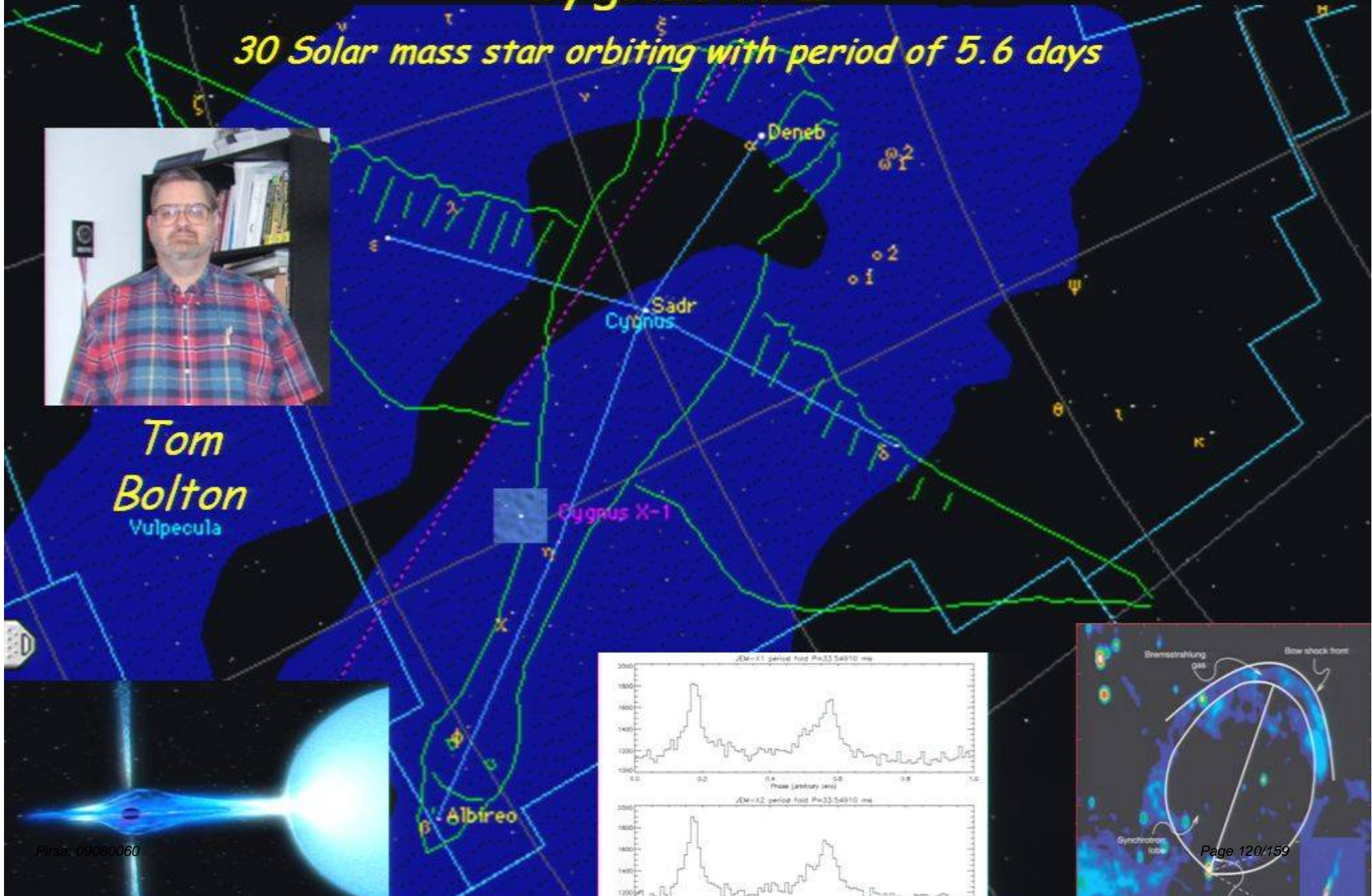


# Cygnus X-1

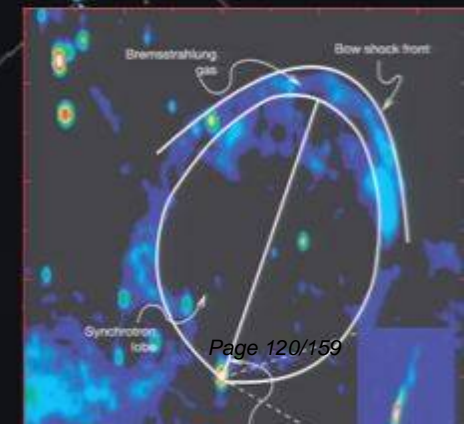
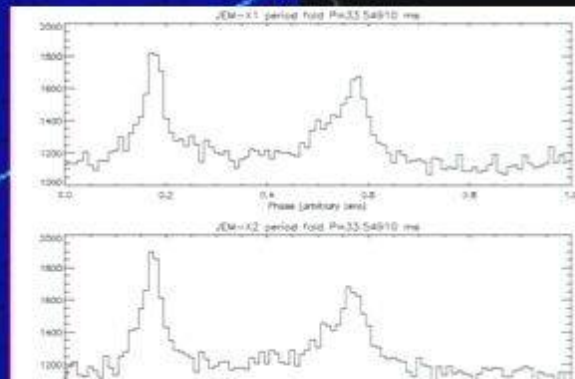
*30 Solar mass star orbiting with period of 5.6 days*



**Tom  
Bolton**  
Vulpecula



Pirsa: 09080060



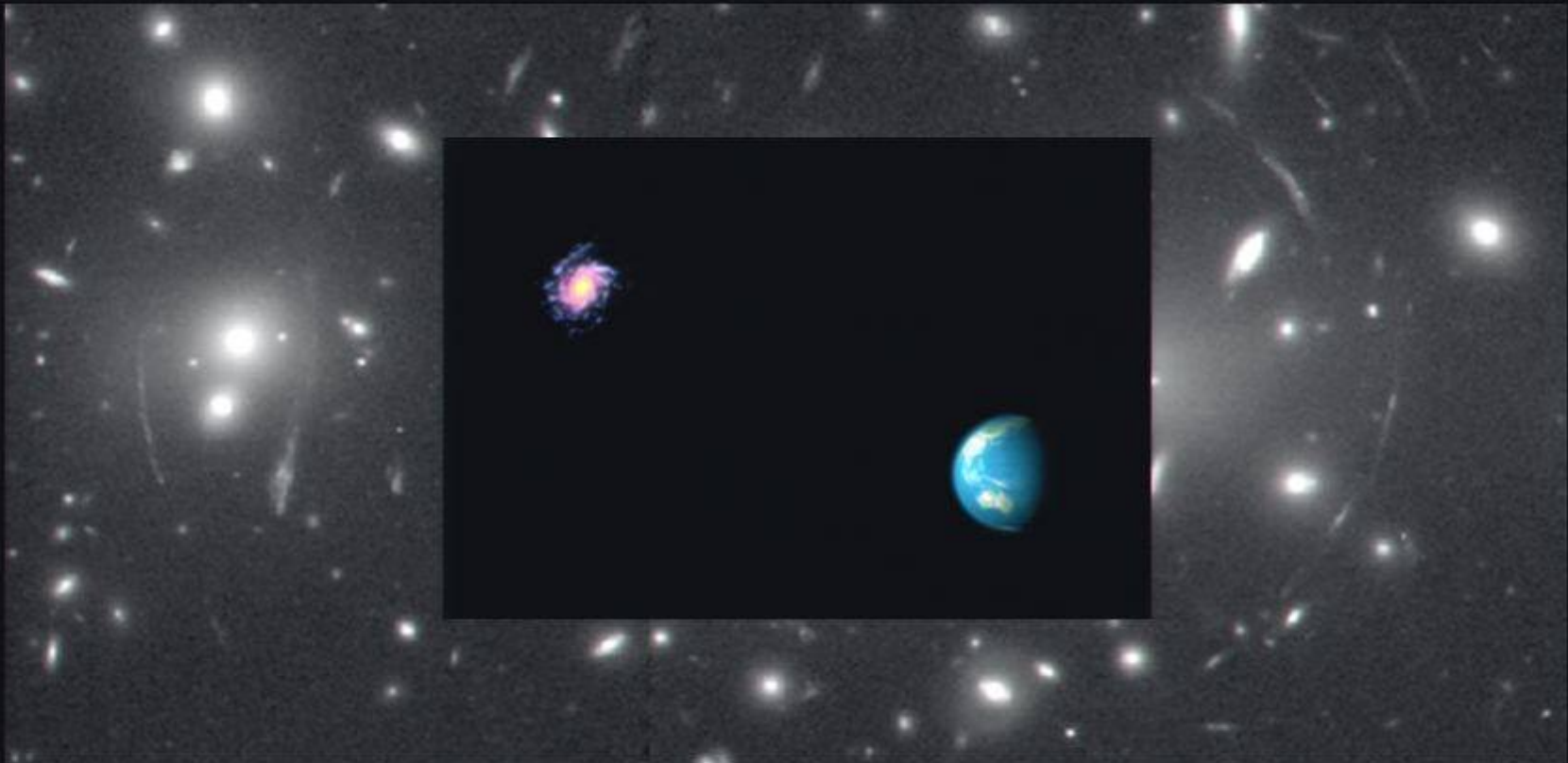
Page 120/159

## *Even More Binary Black Holes*

<b>Name of Binary System</b>	<b>Companion Star Spectral Type</b>	<b>Orbital Period (days)</b>	<b>Black Hole Mass (Solar Units)</b>
Cygnus X-1	B supergiant	5.6	6-15
LMC X-3	B main sequence	1.7	4-11
A0620-00 (V616 Mon)	K main sequence	7.8	4-9
GS2023+338 (V404 Cyg)	K main sequence	6.5	> 6
GS2000+25 (QZ Vul)	K main sequence	0.35	5-14
GS1124-683 (Nova Mus 1991)	K main sequence	0.43	4-6
GRO J1655-40 (Nova Sco 1994)	F main sequence	2.4	4-5
H1705-250 (Nova Oph 1977)	K main sequence	0.52	> 4



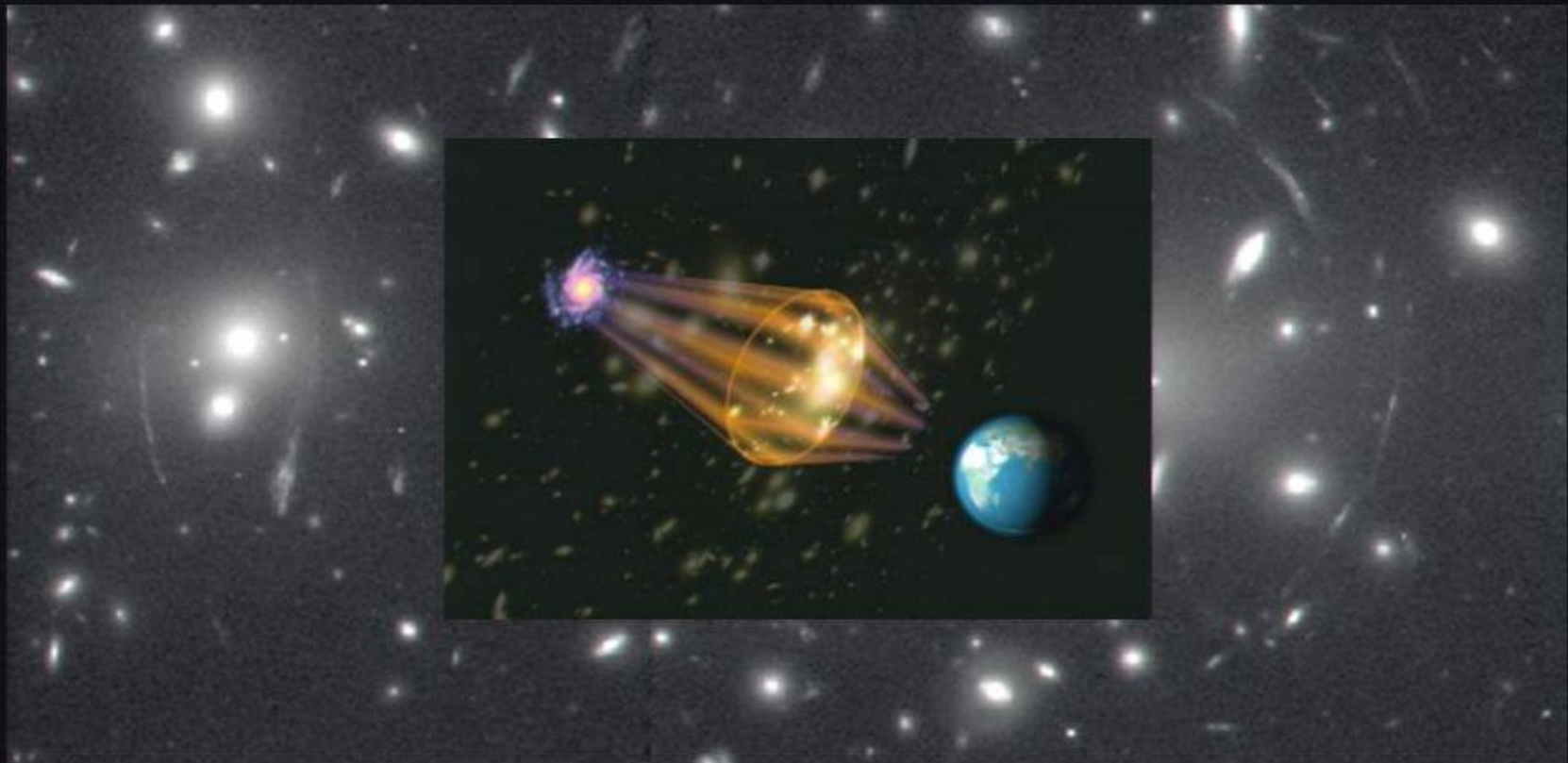
# Lens



*Black Holes can act like a lens. Almost all of the bright objects in this image are galaxies in the cluster known as Abell 2218..*



# Lens



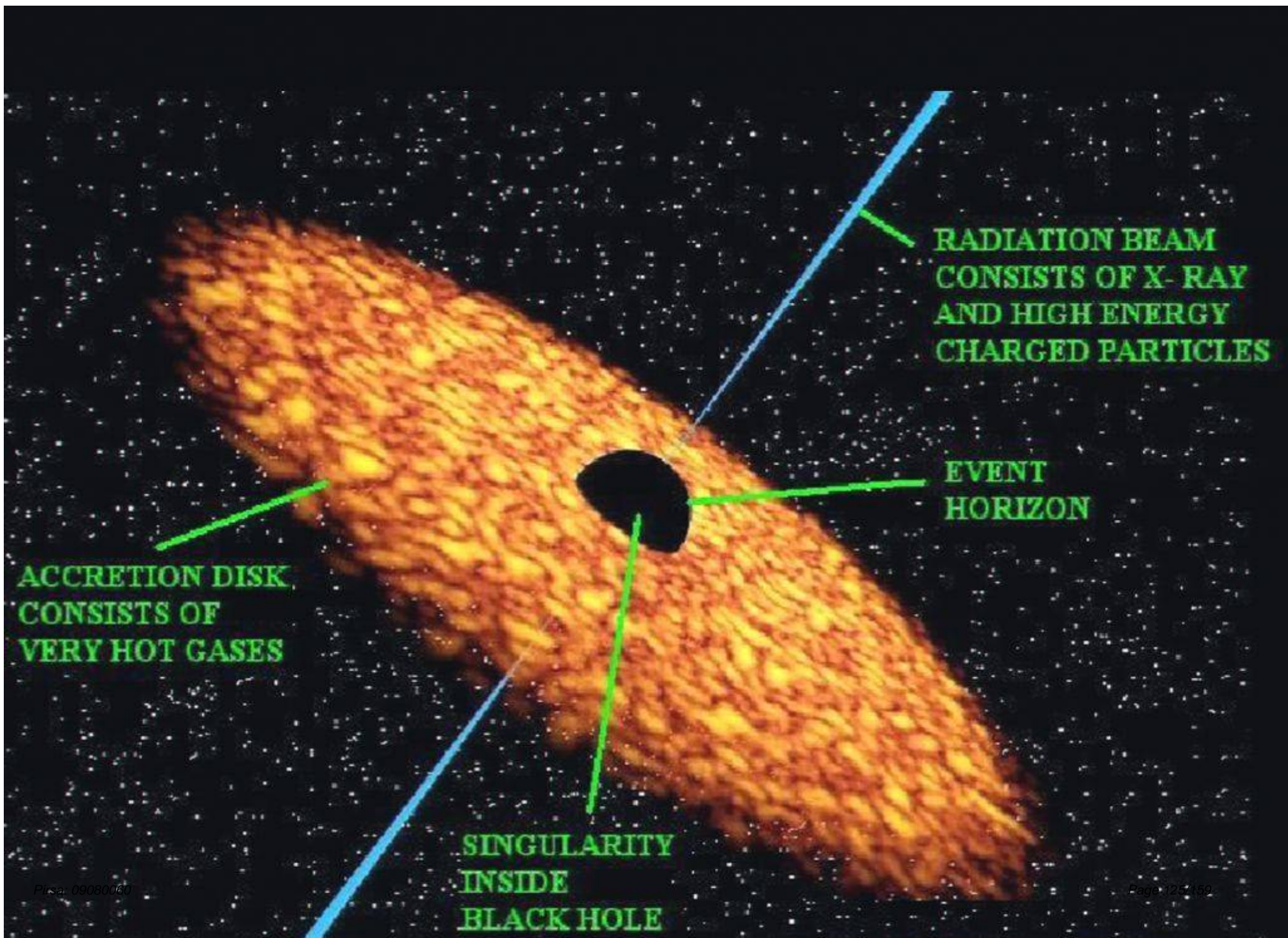
*Black Holes can act like a lens. Almost all of the bright objects in this image are galaxies in the cluster known as Abell 2218..*

What else should we look for?

*Jets*









# Radio Jets from Black Holes

- Many black holes emit jets.
  - Material in jet moving at  $0.9c$ .
  - Jet likely composed of electrons and positrons.
- Magnetic fields surrounding black hole expel material and form the jet.
  - Interaction of jet material with magnetic field gives rise to Radio emission.

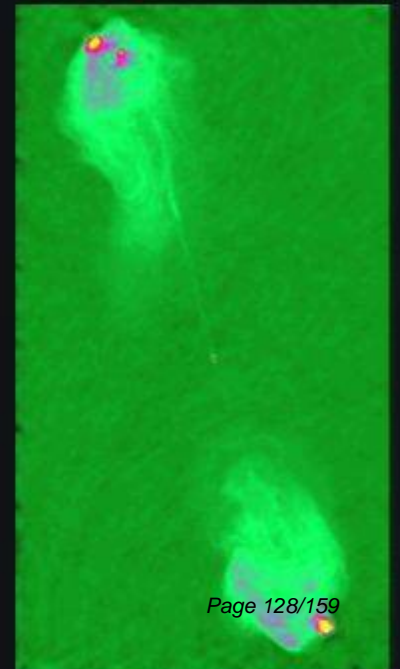
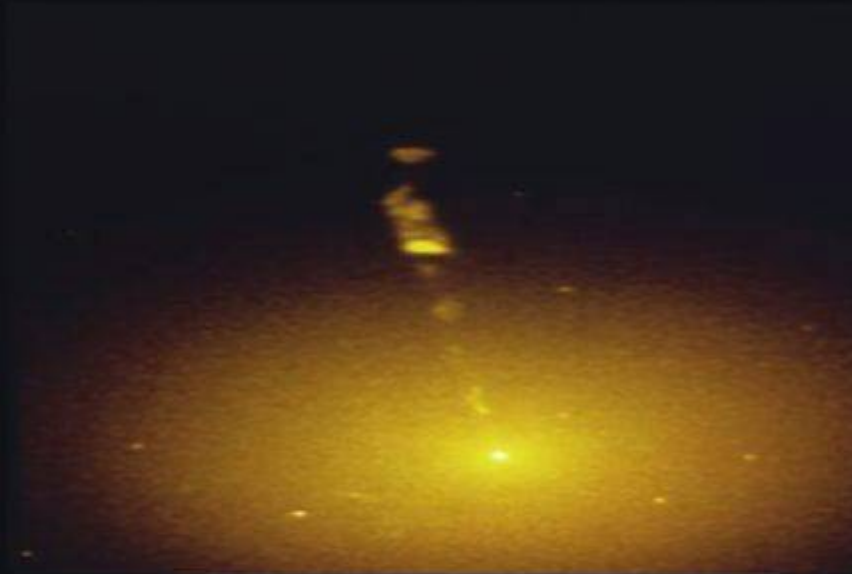
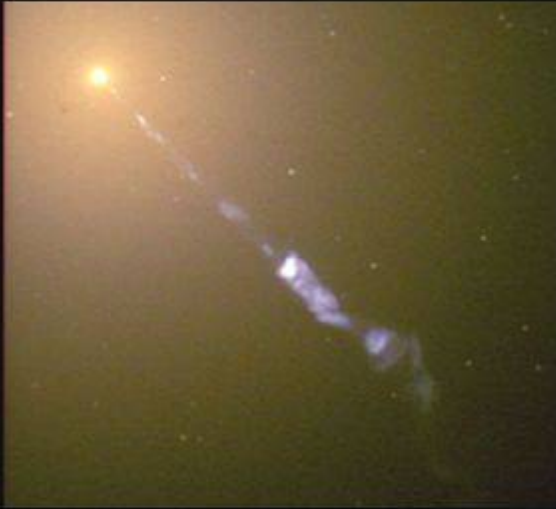


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# Jets



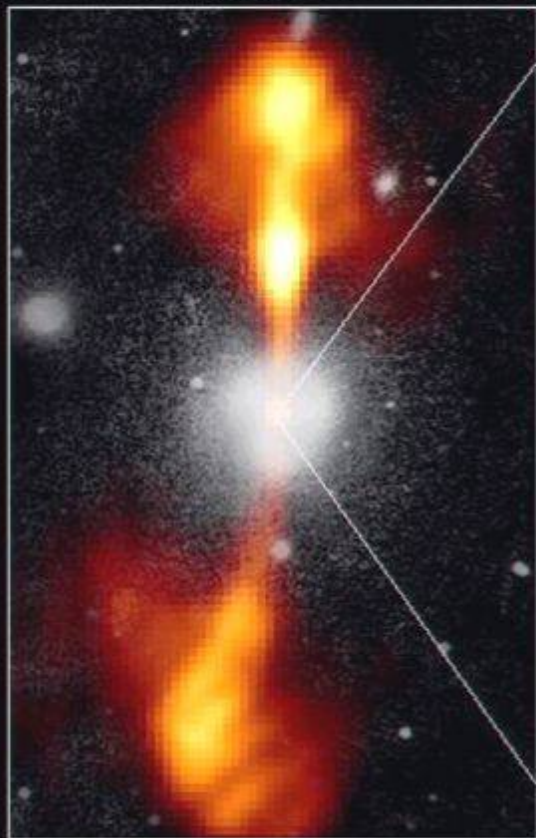


# Core of Galaxy NGC 4261

Hubble Space Telescope

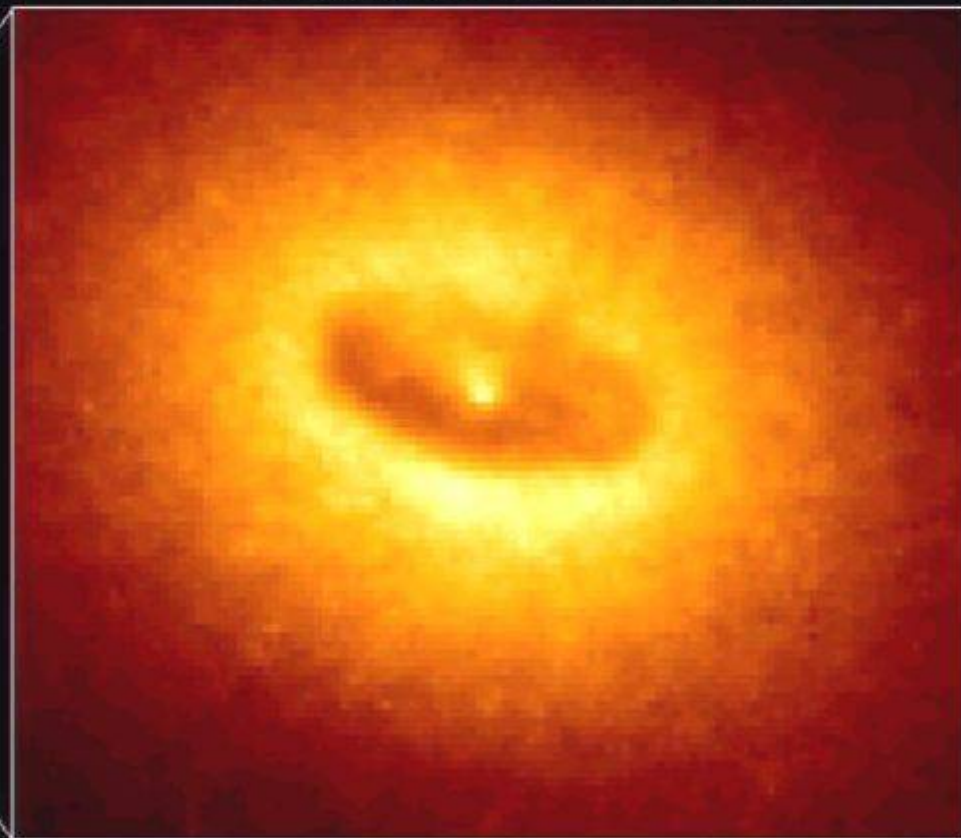
Wide Field / Planetary Camera

Ground-Based Optical/Radio Image



380 Arc Seconds  
88,000 LIGHTYEARS

HST Image of a Gas and Dust Disk

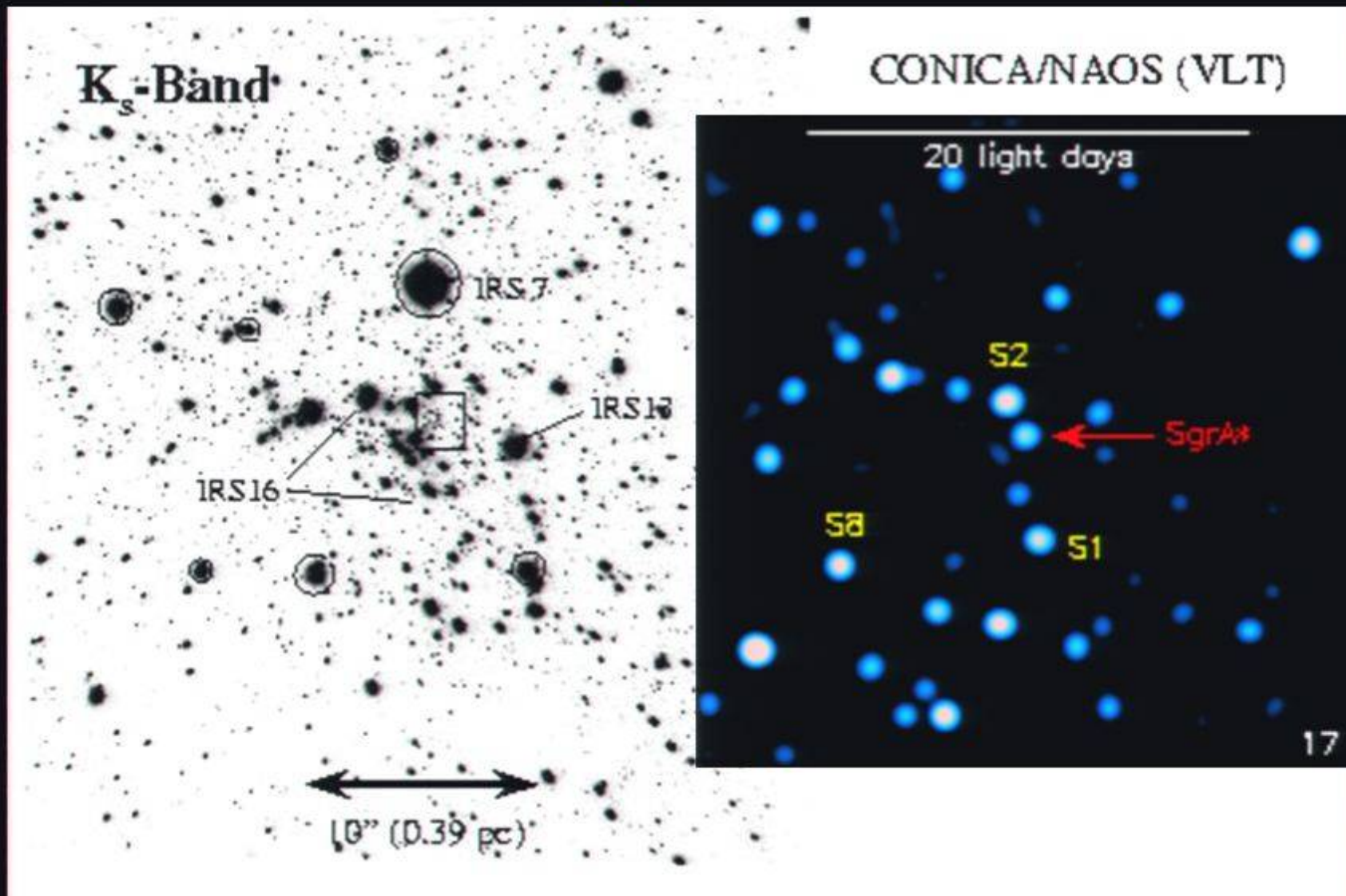


17 Arc Seconds  
400 LIGHTYEARS

## More Evidence



# SgrA\*



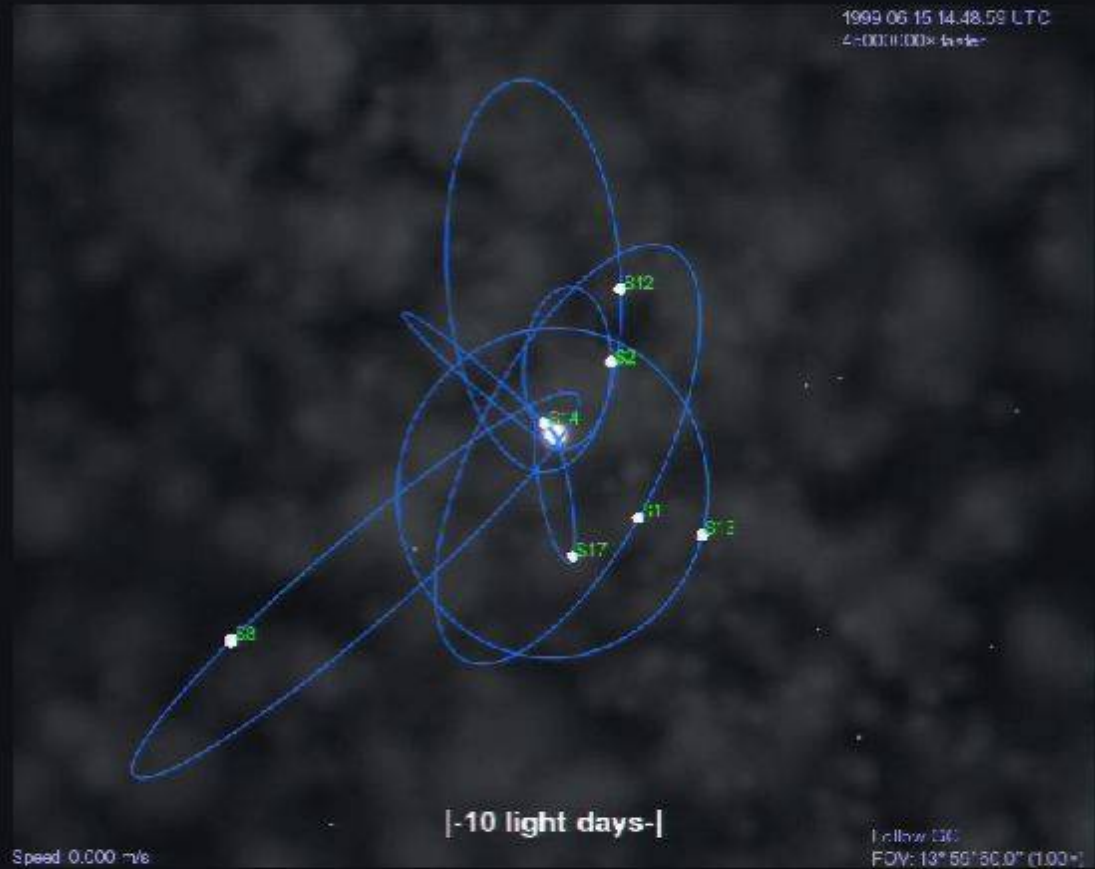
*3,700,000 solar masses*



# SgrA\*

1994.4

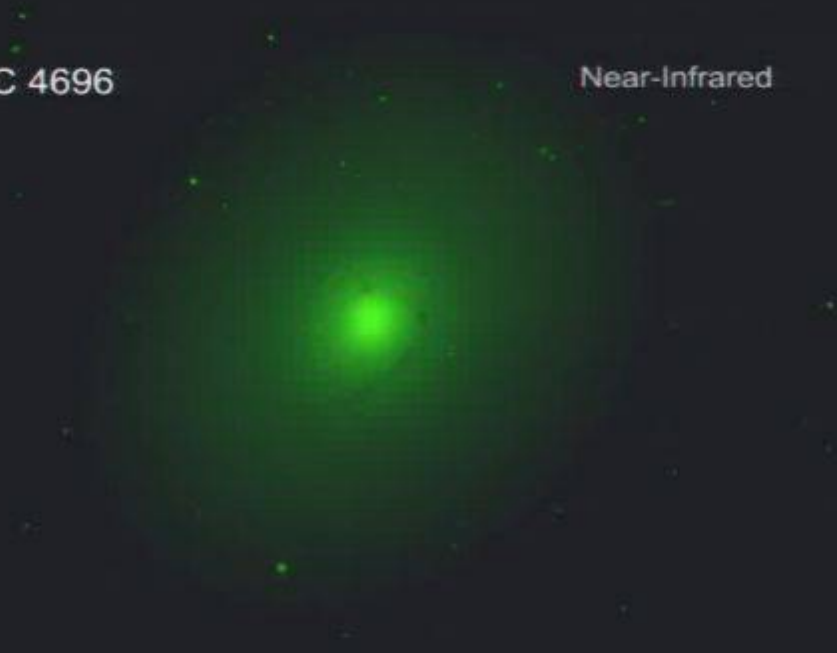
10 light days



# Black Hole Evidence

NGC 4696

Near-Infrared



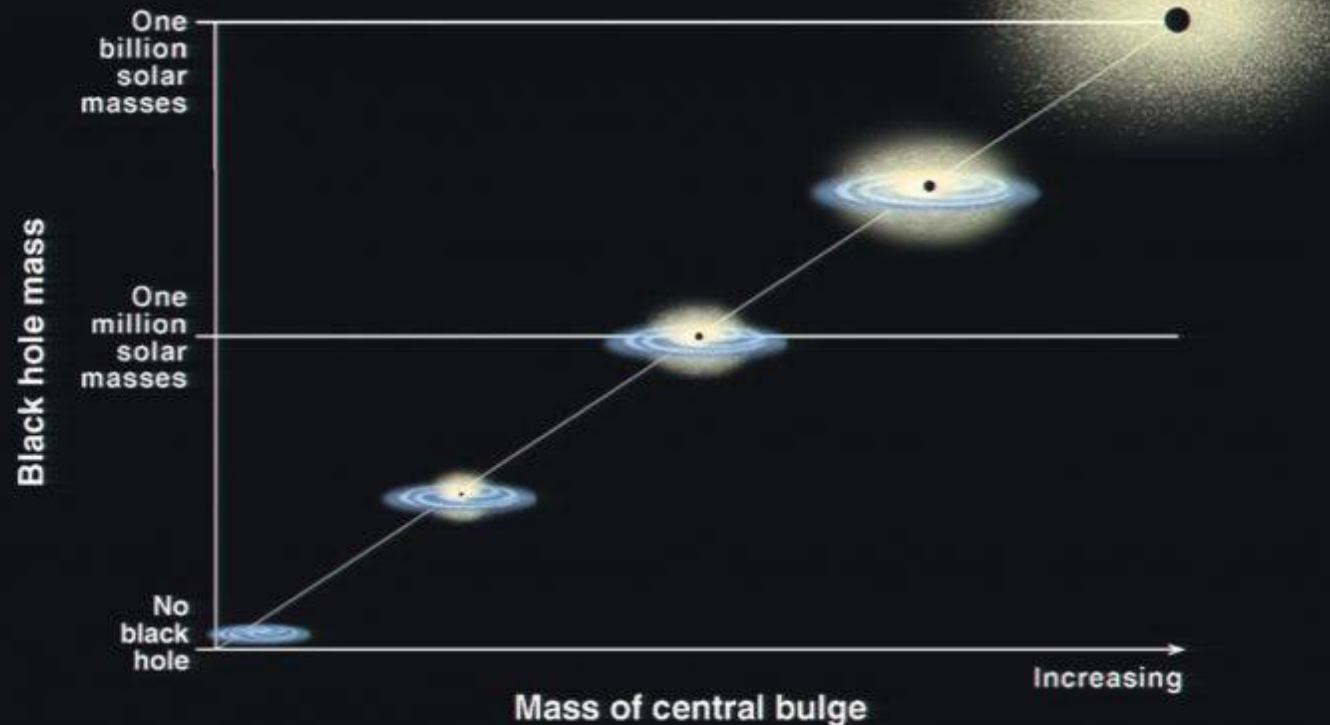
M33

Optical  
(Kitt Peak)



# Speed of Gas and Black Holes

## Correlation Between Black Hole Mass and Bulge Mass



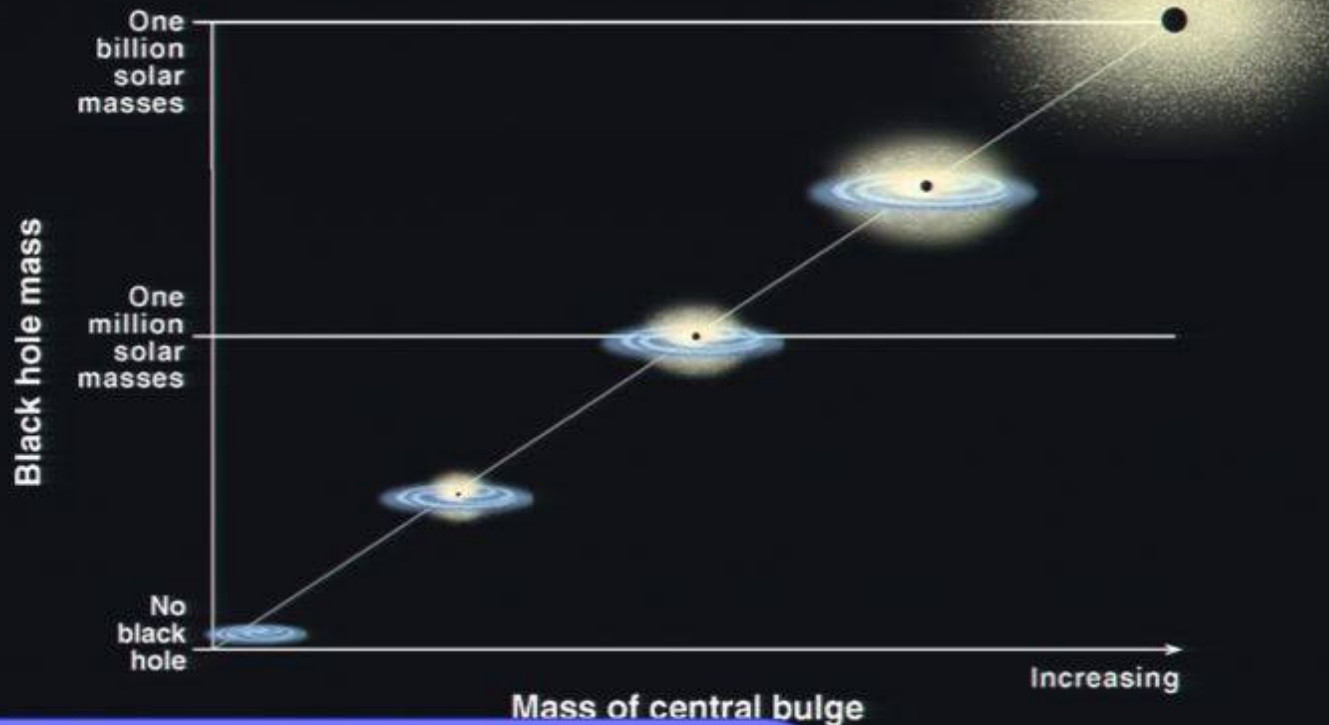
- It discovered a correlation between a Black Hole's mass and the average speed of the stars in the galaxy's central bulge.
- The faster the stars are moving, the larger the black hole.
- The central Black Hole comprises 0.5% of mass of stars in the spheroid of the galaxy. (Magorrian Relation)
- Previously, black holes were seen as the endpoints of evolution, the final resting state of most or all of the matter in the universe. Now we believe black holes also play a critical role in the evolution of galaxies.





# Speed of Gas and Black Holes

## Correlation Between Black Hole Mass and Bulge Mass



*In Jan 2009, at the American Astronomical Society meeting, evidence from the Very Large Array Radio telescope, demonstrated (based on Black hole mass to Galactic Bulge) that Black Holes came First*

ss and the average speed of the

one.

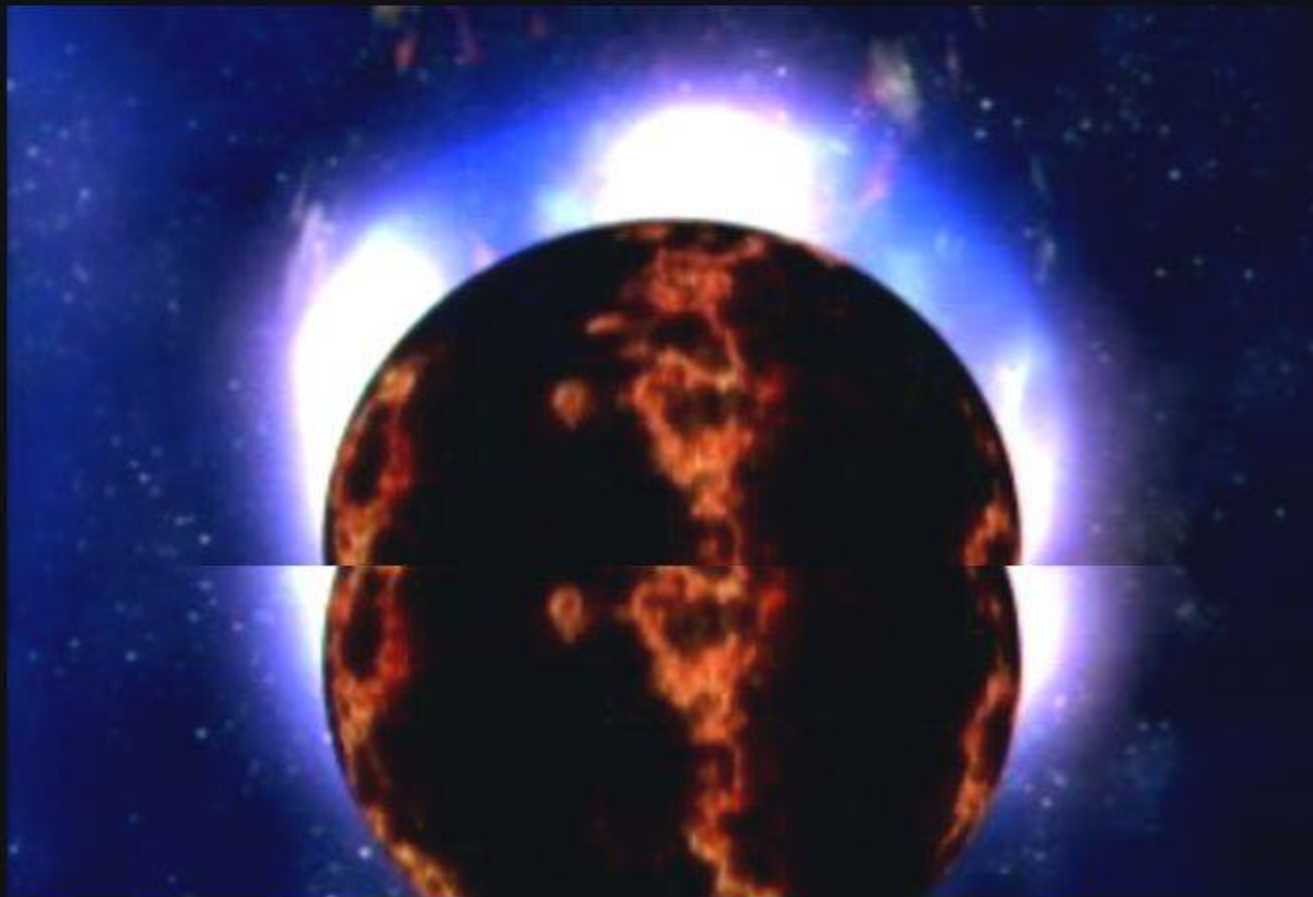
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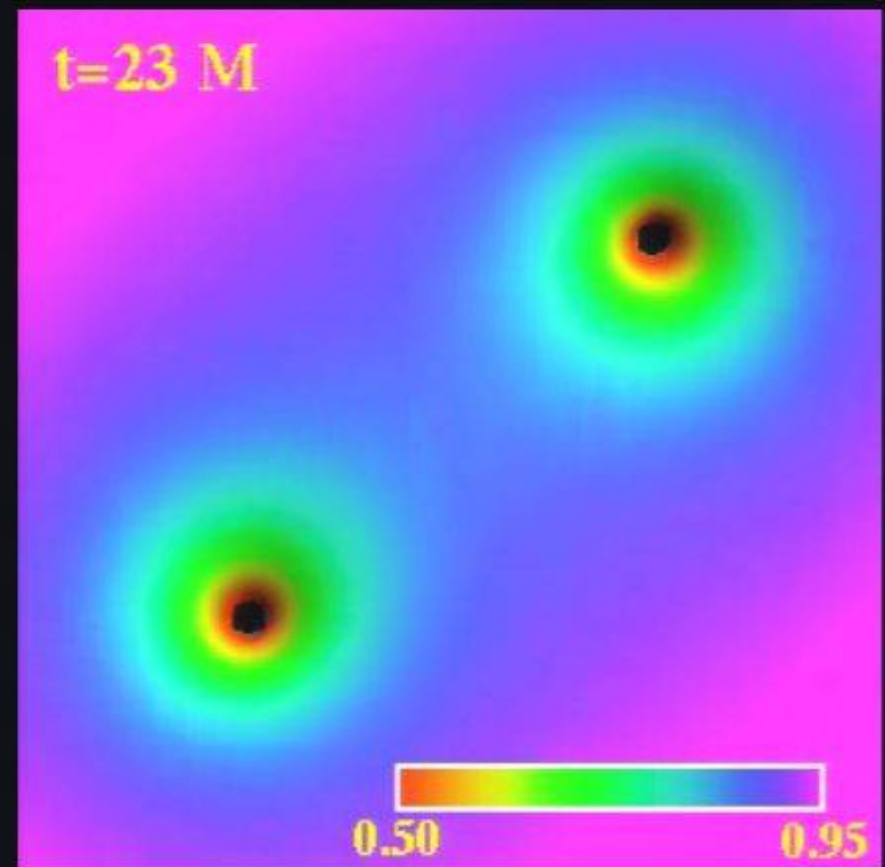
# When Black Holes Collide



# The Best Simulation

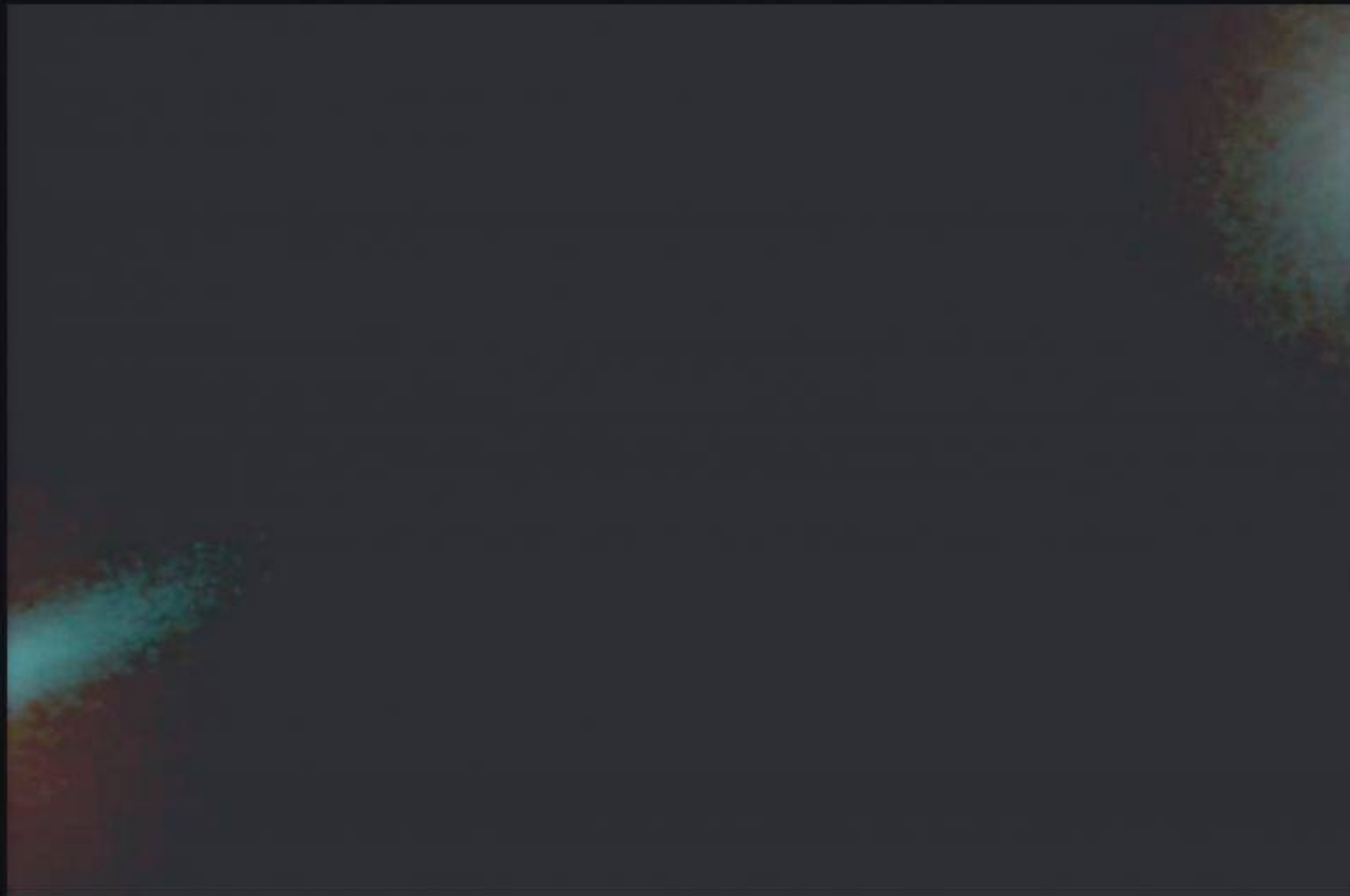
*For over 20 years  
cosmologist have been  
trying to simulate  
colliding black holes.*

*In 2005 at Banff, Frans  
Pretorius was able to  
provide an accurate  
simulation of only 5  
orbits of two colliding  
black holes*





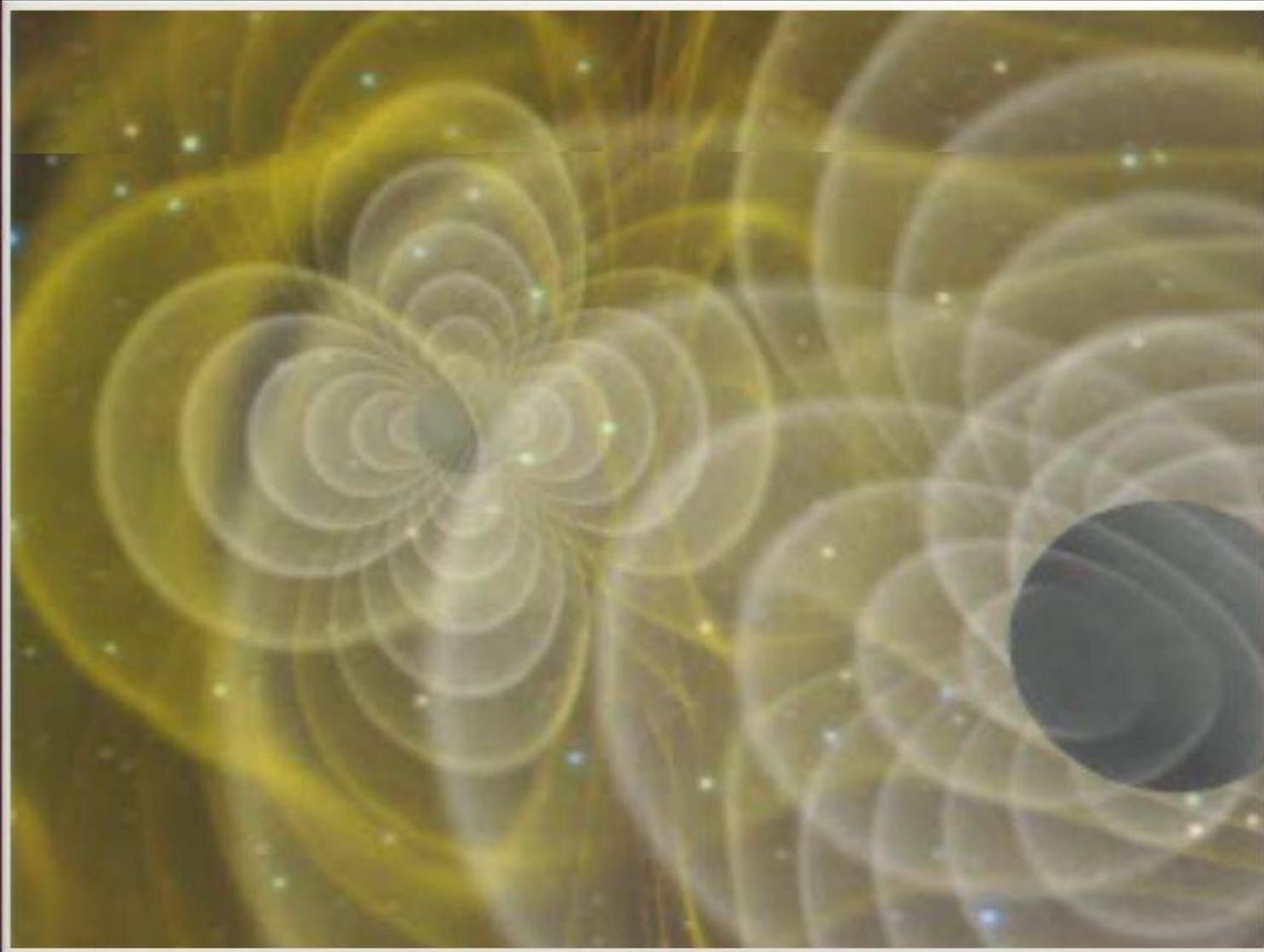
# Frame Dragging and Gravitational Waves



# Frame Dragging and Gravitational Waves

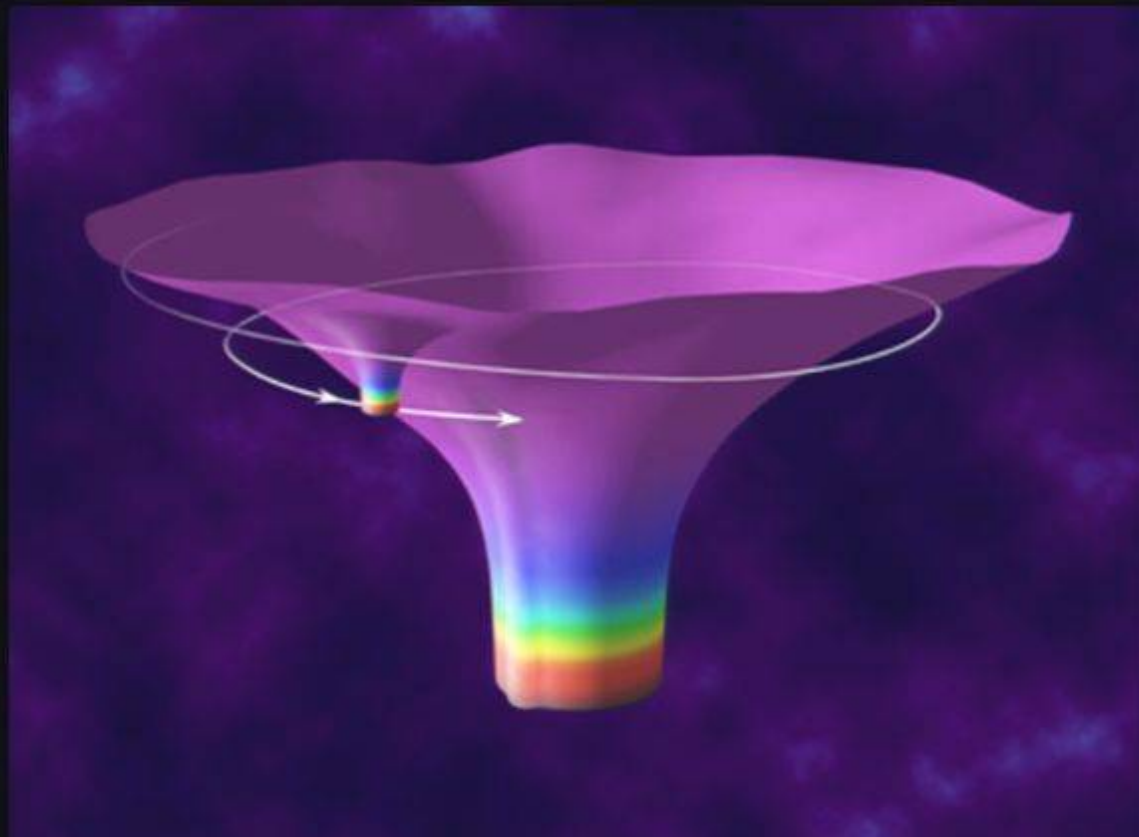


## *Nasa's Latest Animation*





*This is the final  
piece of the  
puzzle that needs  
to be verified*



# Wave Detection

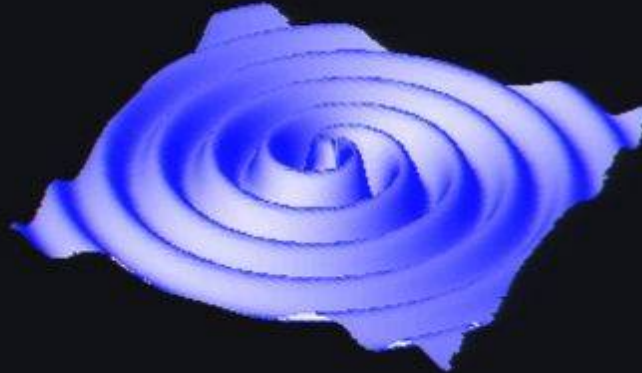
*The race is on and the detectors  
are in place or being readied for  
orbit:*

LIGO  
VIRGO  
GEO600  
TAMA  
AURIGA

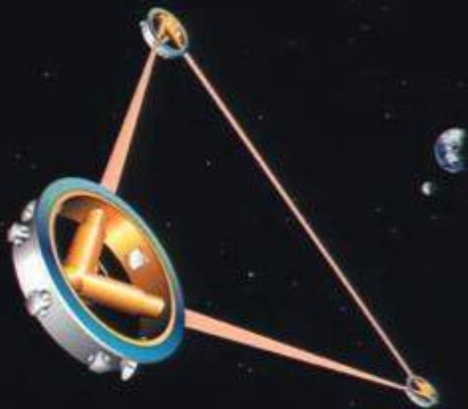
# Wave Detection



*The GEO600 detector, located in a field outside Hannover in Germany*



*Auriga*



*Laser Interferometer Space Antenna*

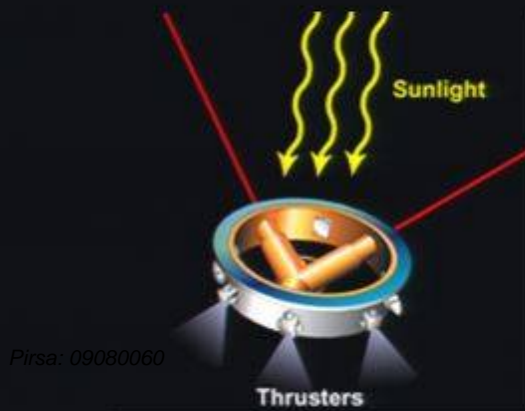
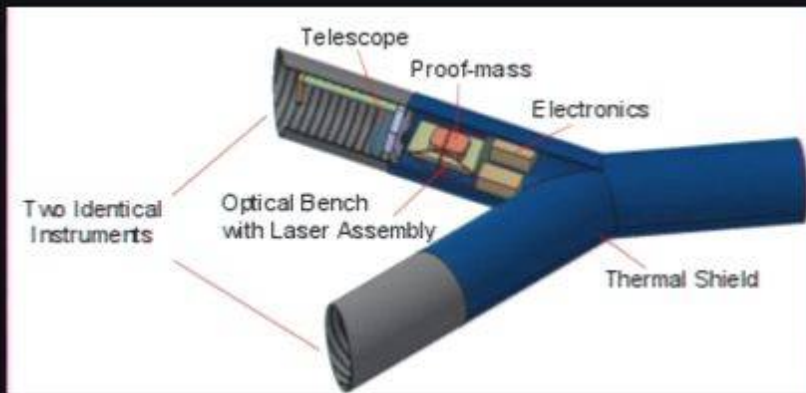


*Laser Interferometer Gravitational Wave Observatory (LIGO) Richland*



# Lisa

- Distance between each craft is 5,000,000 km
- Will follow Earth's orbit by 20 degrees
- Will be able to detect  $\Delta L/L$  less than  $10^{-21}$  (that  $\Delta L$  of  $10^{-10}$  cm)
- Launch date set for 2015 (5 year duration)



## *The Sound of collapse*

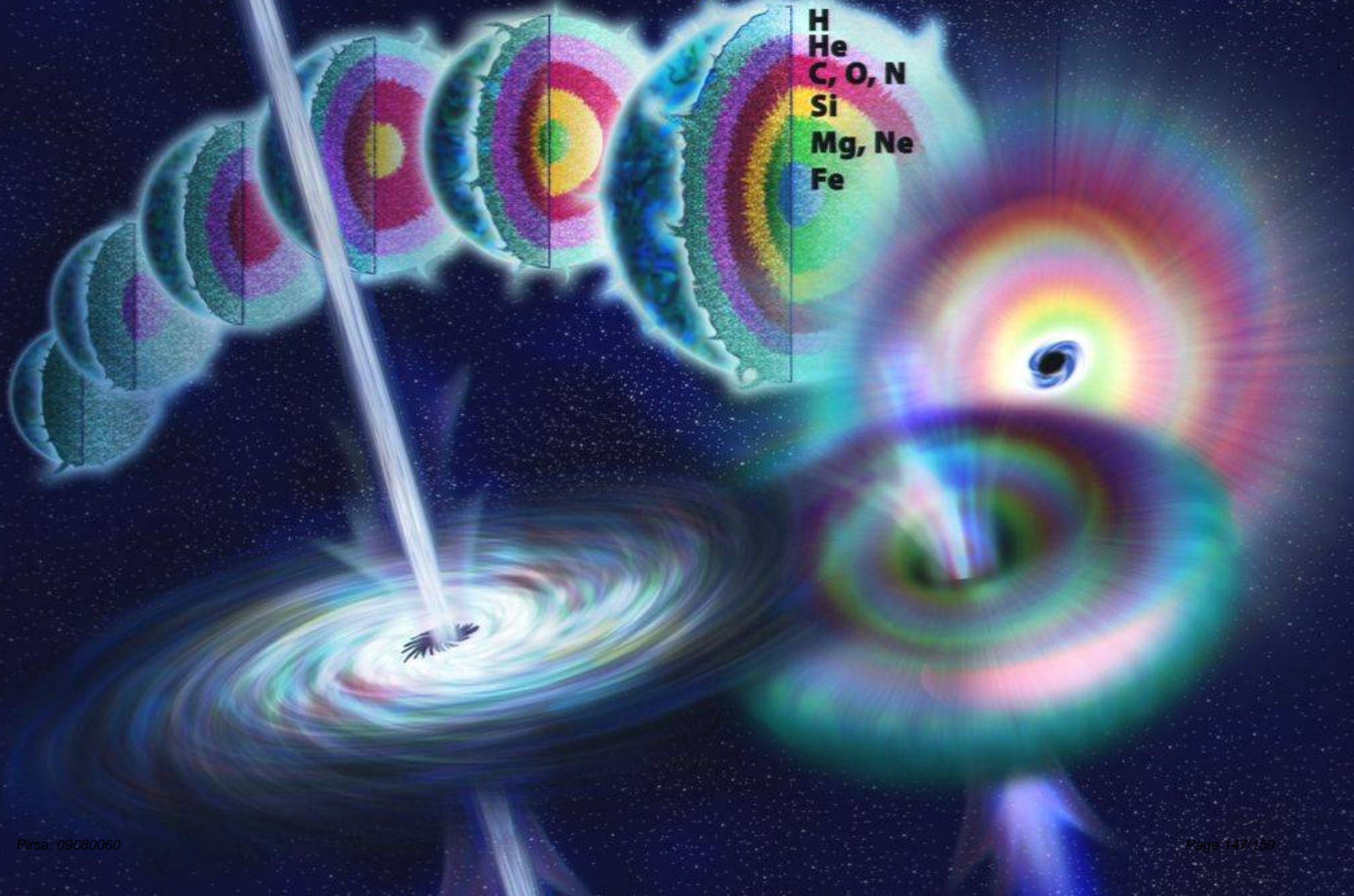


# Strange Predictions





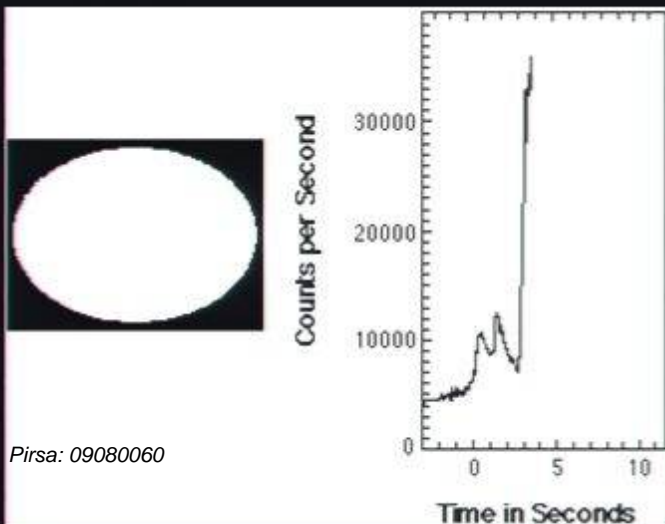
# Gamma Ray Bursts





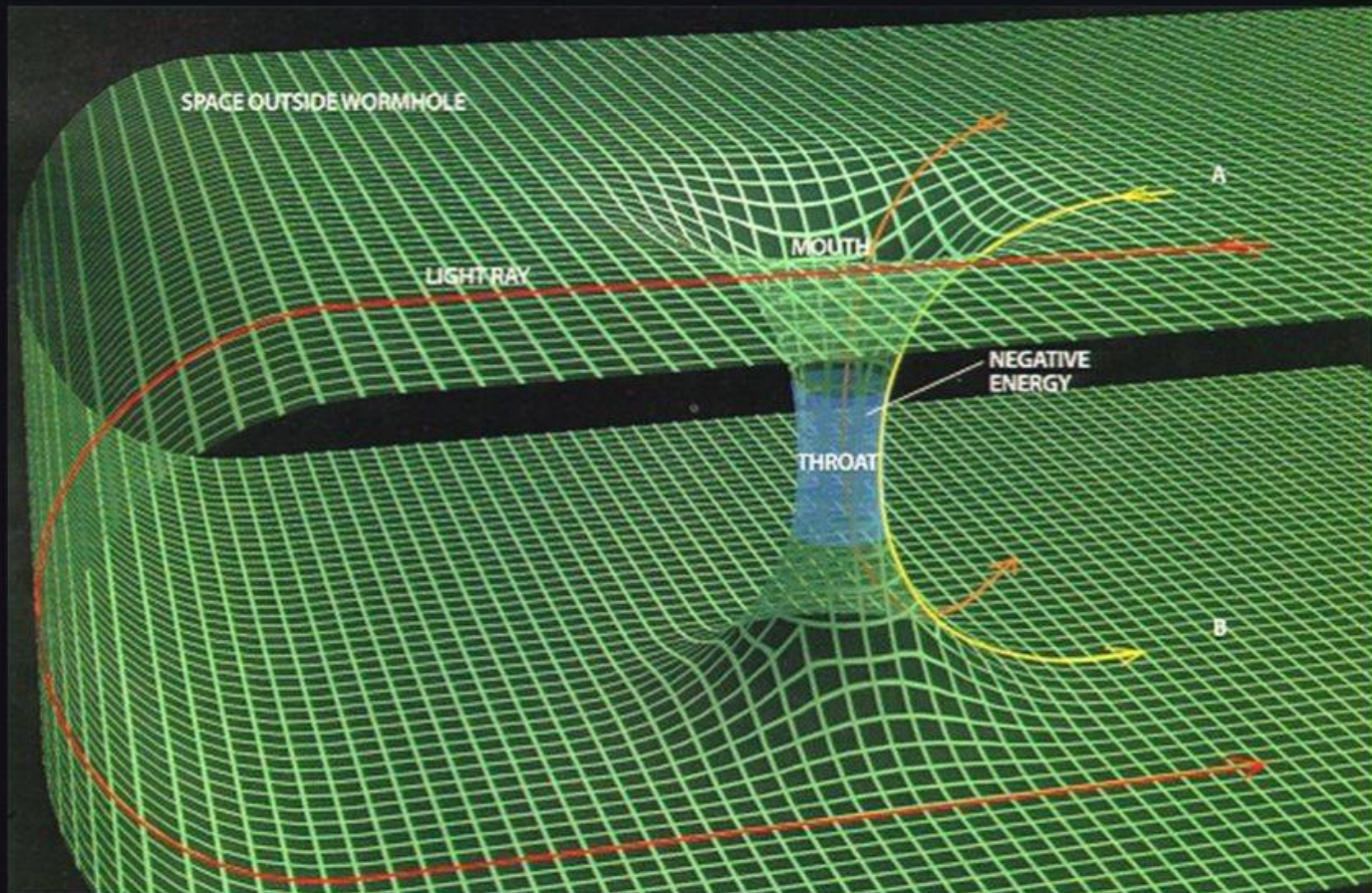
# GRB

*Record-breaking Gamma Ray Burst (GRB) in the act on Wednesday (March 19<sup>th</sup>, 2008), the worlds telescopes swung toward the constellation of Boötes to watch the afterglow of this massive explosion. One instrument in a Chile observatory was observing in Swift's field of view at the time of the blast and has put together a short frame-by-frame video of the event. So if you missed this historic burst from 7.5 billion years ago (which you probably did!) you can watch it now...*





# Wormholes

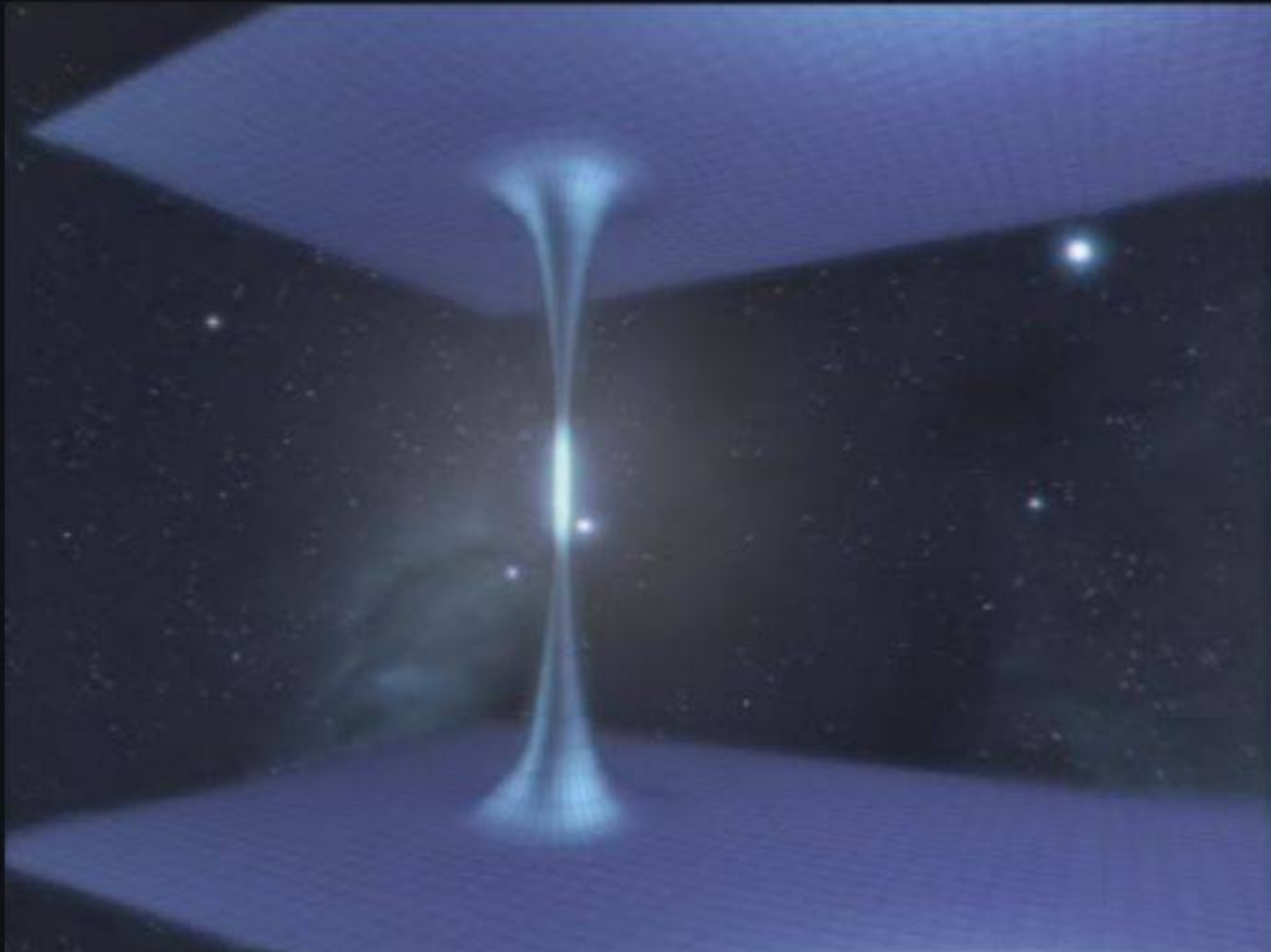




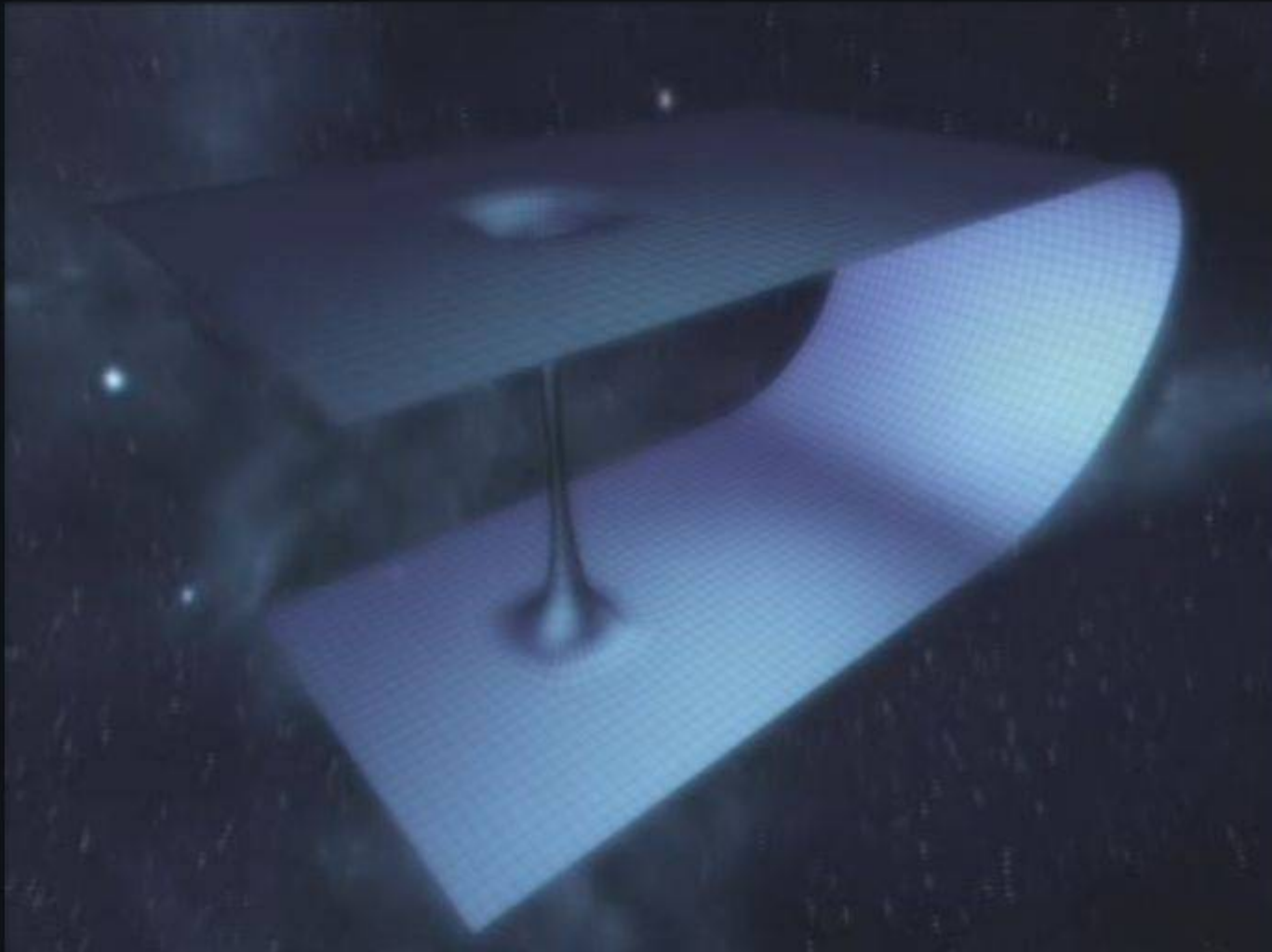
# Wormholes (the traveler's view)



# Wormholes (the traveler's view)



# Wormholes (the traveler's view)





# Naked Singularity

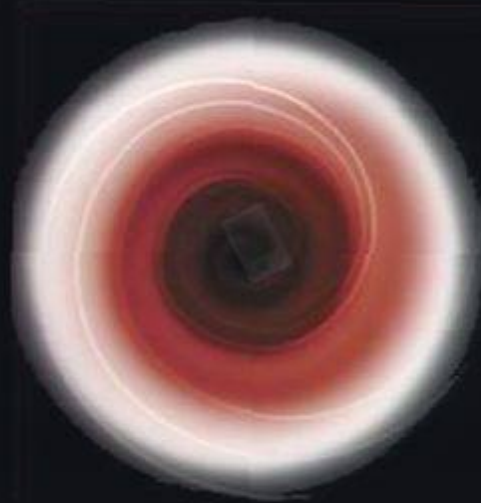
*Such a naked singularity would be a breakdown in the laws of physics. After that, you could no longer guess what would come out of the black hole--it could be anything (to quote William H. Press) "from television sets to busts of Abraham Lincoln."*



A singularity that is not inside a black hole (not surrounded by an event horizon), and therefore can be seen by someone outside it.

# Naked Singularity

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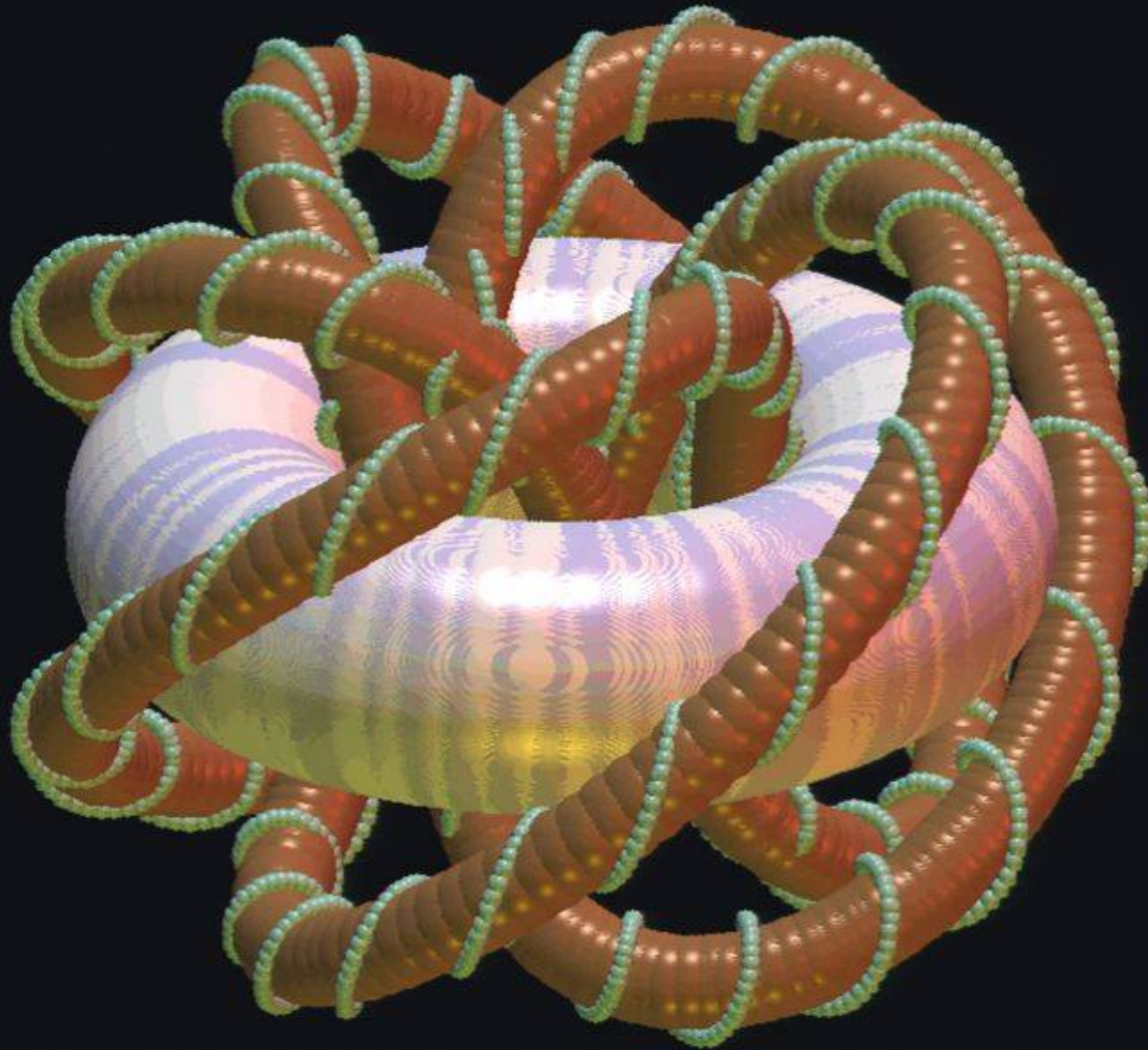
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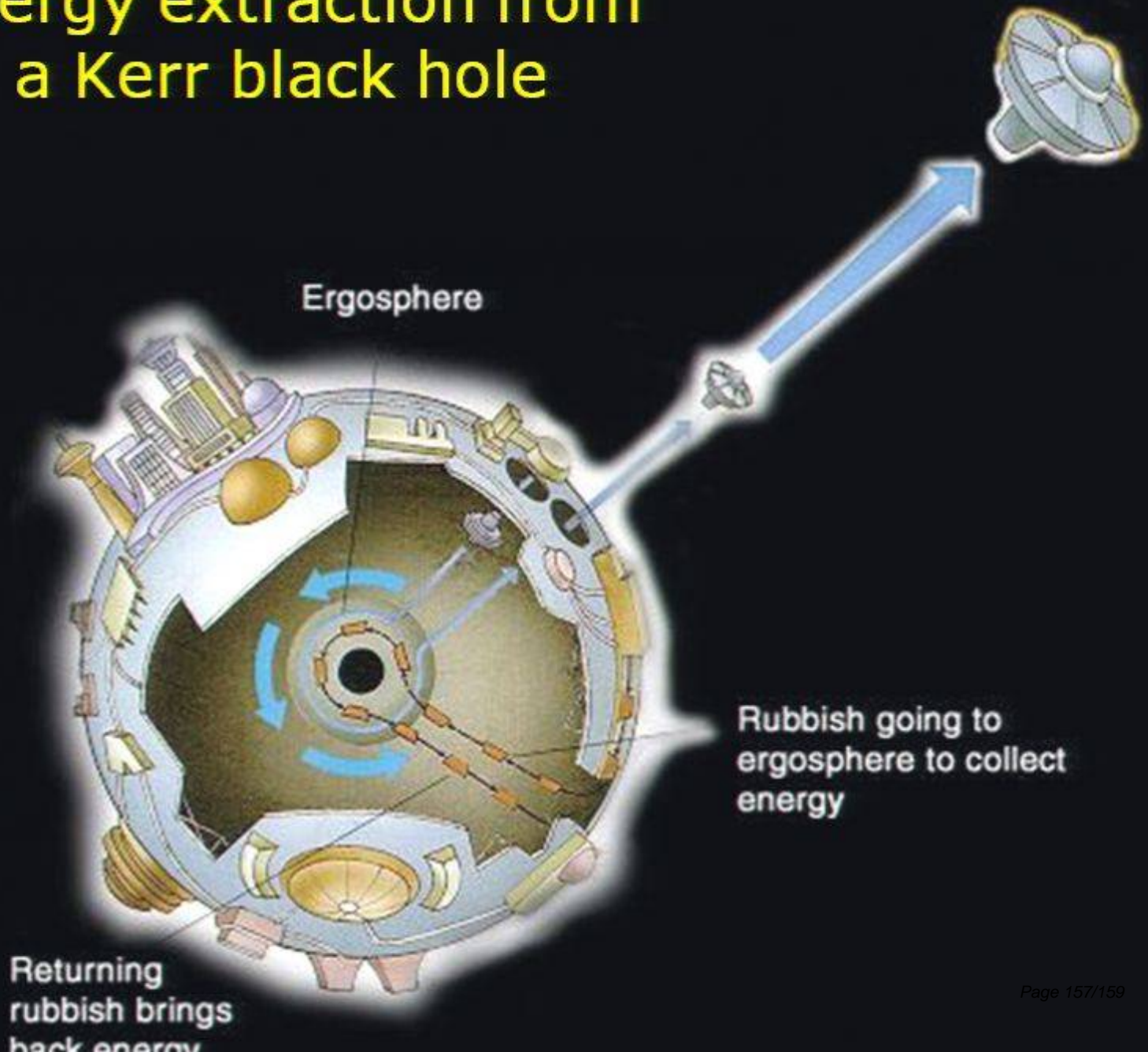
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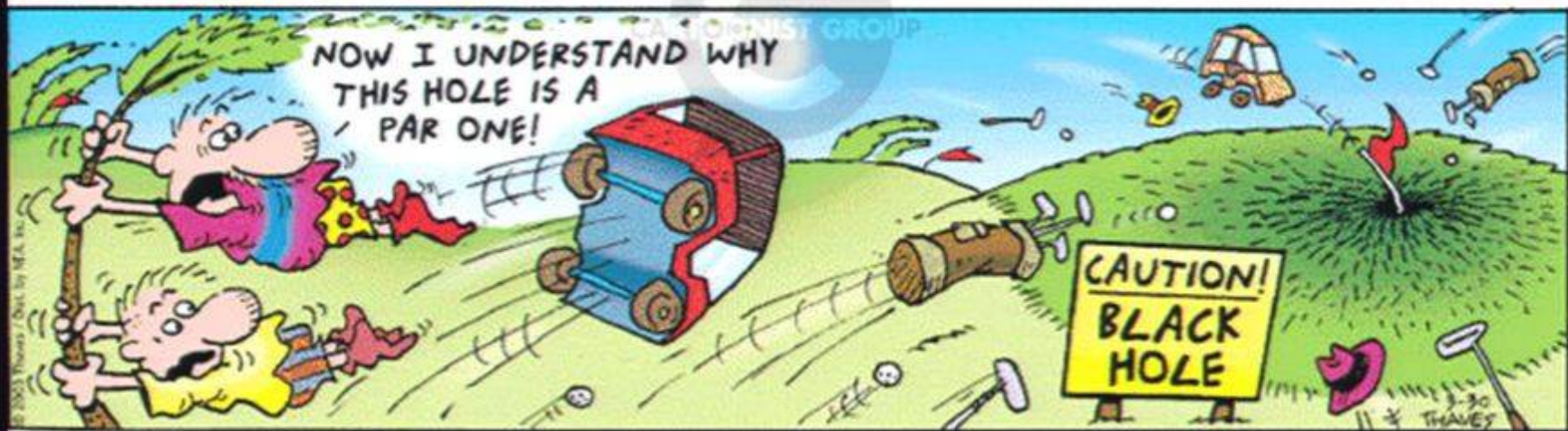
# Time Travel



# Energy extraction from a Kerr black hole









*The End*