

Title: The Beauty and Basics of BAO

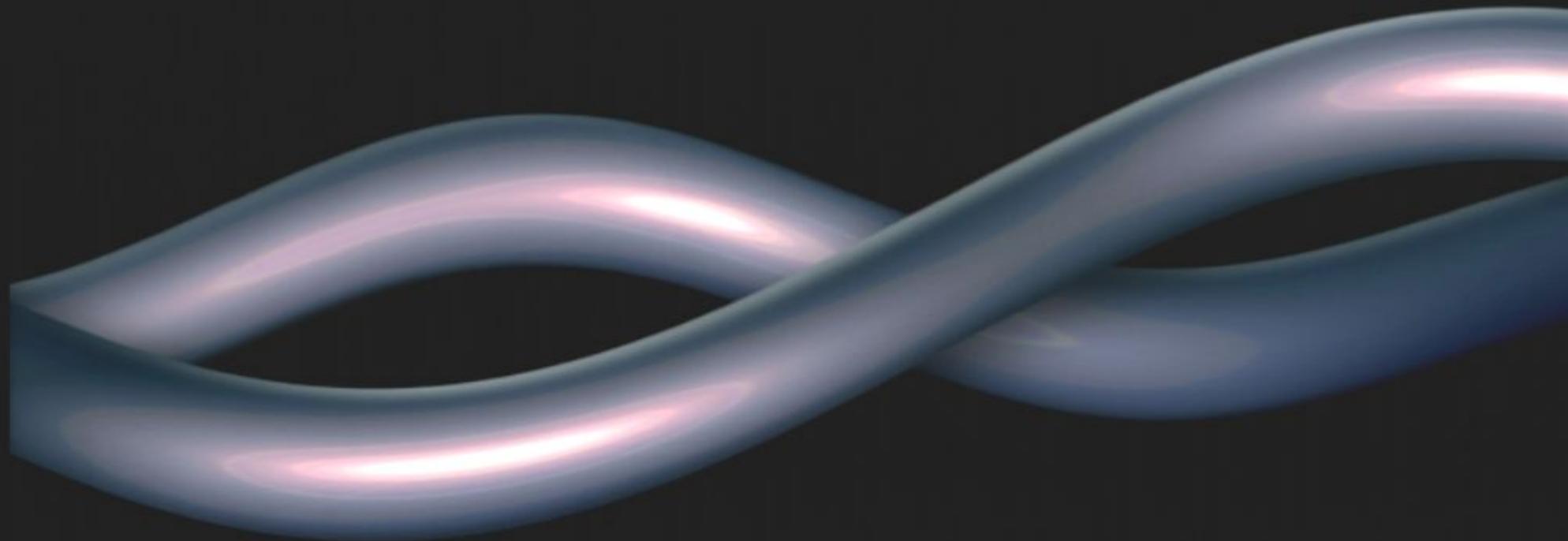
Date: Jul 31, 2009 11:00 AM

URL: <http://pirsa.org/09070039>

Abstract: The Baryon Acoustic Oscillations (BAO) are the latest weapon in the quest for precision cosmology and dark energy. Many presentations on BAO are complicated and unclear and I will therefore present BAO with particular emphasis on trying to give the simplest theoretical description, both at the linear and nonlinear level, and will describe some of the observational challenges to measuring BAO.

Baryon Acoustic Oscillations

Bruce Bassett (SAAO/UCT)



Overview

Overview

- Statistical Standard Rulers

Overview

- Statistical Standard Rulers
- Origins, uses & measurements of BAO

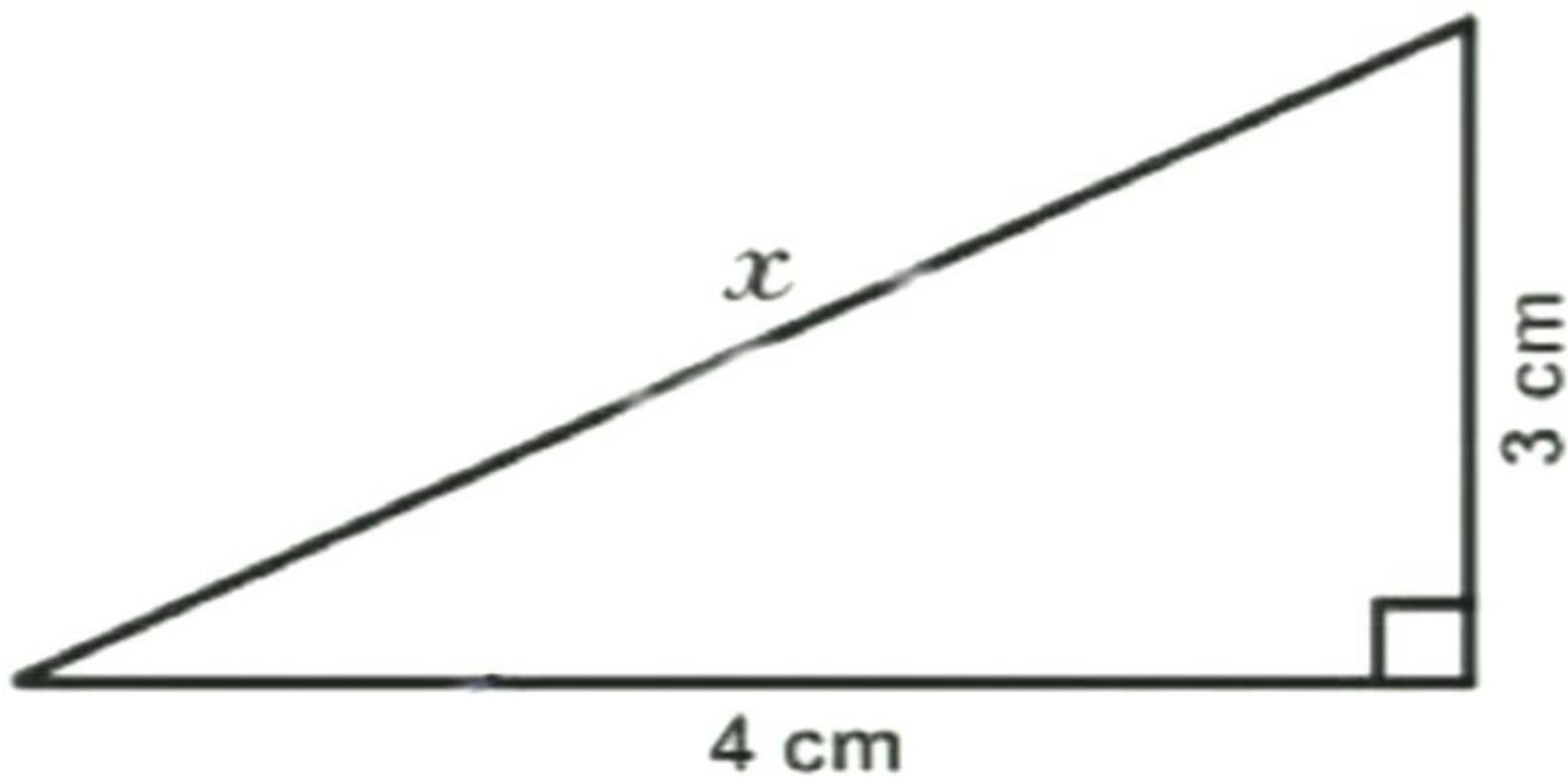
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- Statistical Standard Rulers
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- Targets for BAO surveys

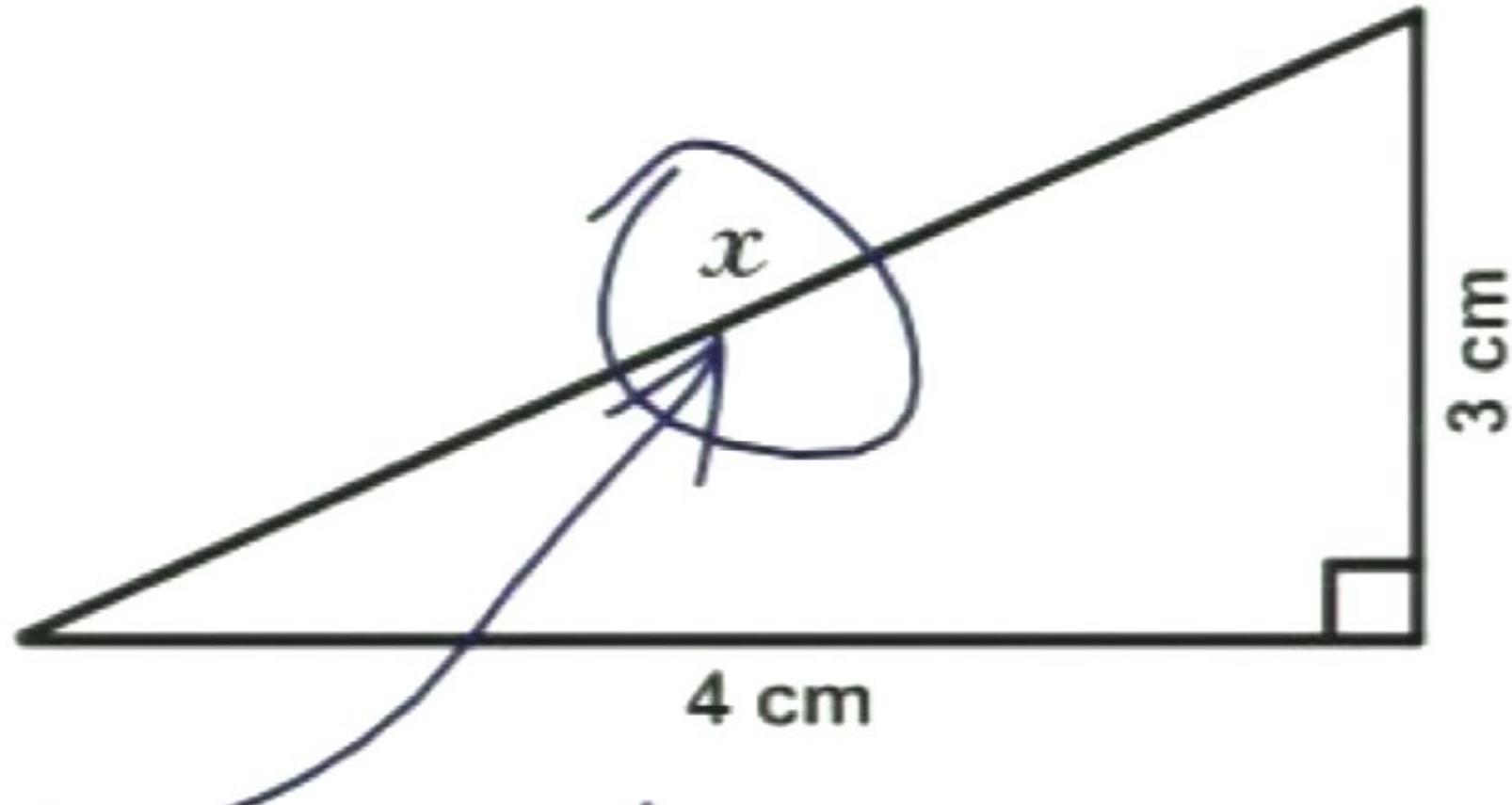
Overview

- Statistical Standard Rulers
- Origins, uses & measurements of BAO
- Targets for BAO surveys
- Complications
 - Nonlinearities
 - Photometric vs spectroscopic surveys

3. Find x.



3. Find x.



Here it is

The Importance of Communication in Science

The Importance of Communication in Science

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ARTICLES

A mathematical model for the determination of total area under glucose tolerance and other metabolic curves

MM Tai

Obesity Research Center, St. Luke's-Roosevelt Hospital Center, New York, New York.

OBJECTIVE--To develop a mathematical model for the determination of total areas under curves from various metabolic studies. RESEARCH DESIGN AND METHODS--In Tai's Model, the total area under a curve is computed by dividing the area under the curve between two designated values on the X-axis (abscissas) into small segments (rectangles and triangles) whose areas can be accurately calculated from their respective geometrical formulas. The total sum of these individual areas thus represents the total area under the curve. Validity of the model is established by comparing total areas obtained from this model to these same areas obtained from graphic method (less than +/- 0.4%). Other formulas widely applied by researchers under- or overestimated total area under a metabolic curve by a great margin. RESULTS--Tai's model proves to be able to 1) determine total area under a curve with precision; 2) calculate area with varied shapes that may or may not intercept on one or both X/Y axes; 3) estimate total area under a curve plotted against varied time intervals (abscissas), whereas other formulas only allow the same time interval; and 4) compare total areas of metabolic curves produced by different studies. CONCLUSIONS--The Tai model allows flexibility in experimental conditions, which means, in the case of the glucose-response curve, samples can be taken with differing time intervals and total area under the curve can still be determined with precision.



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(Statistical) Standard Rulers



(Statistical) Standard Rulers



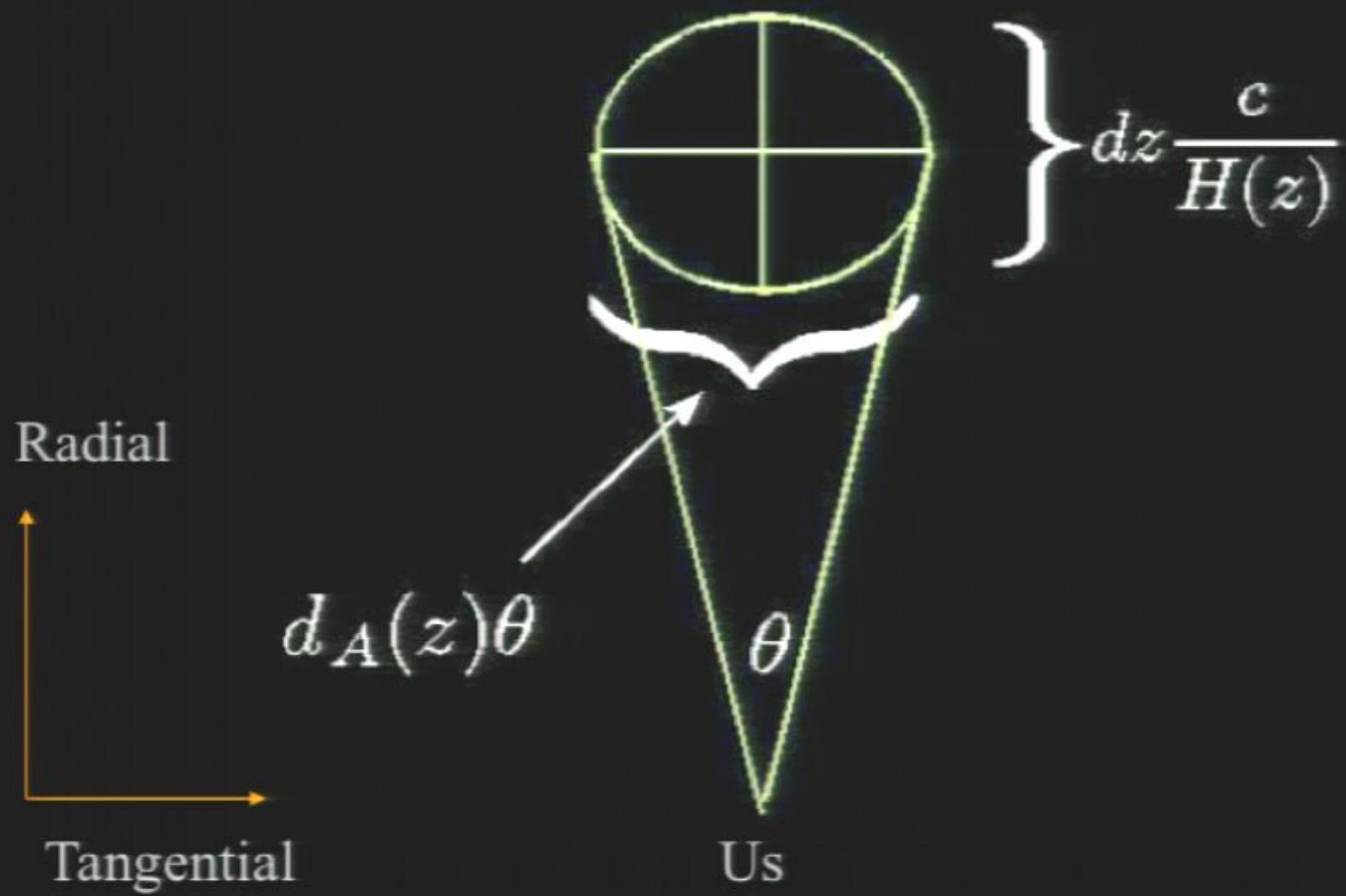
“Standard” is a Crucial Ingredient

(Statistical) Standard Rulers

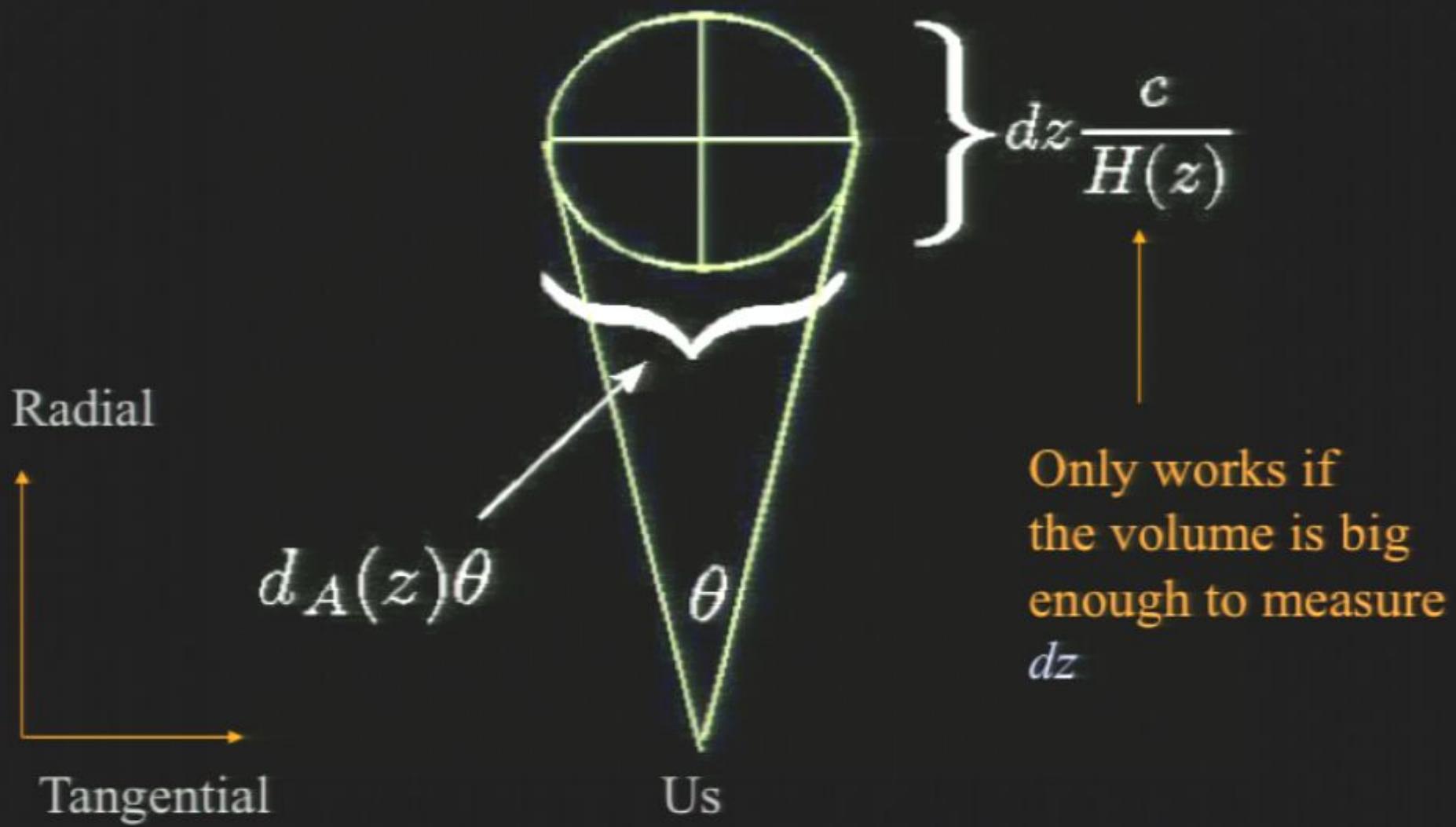


“Standard” is a Crucial Ingredient

The Beauty of Standard Volumes

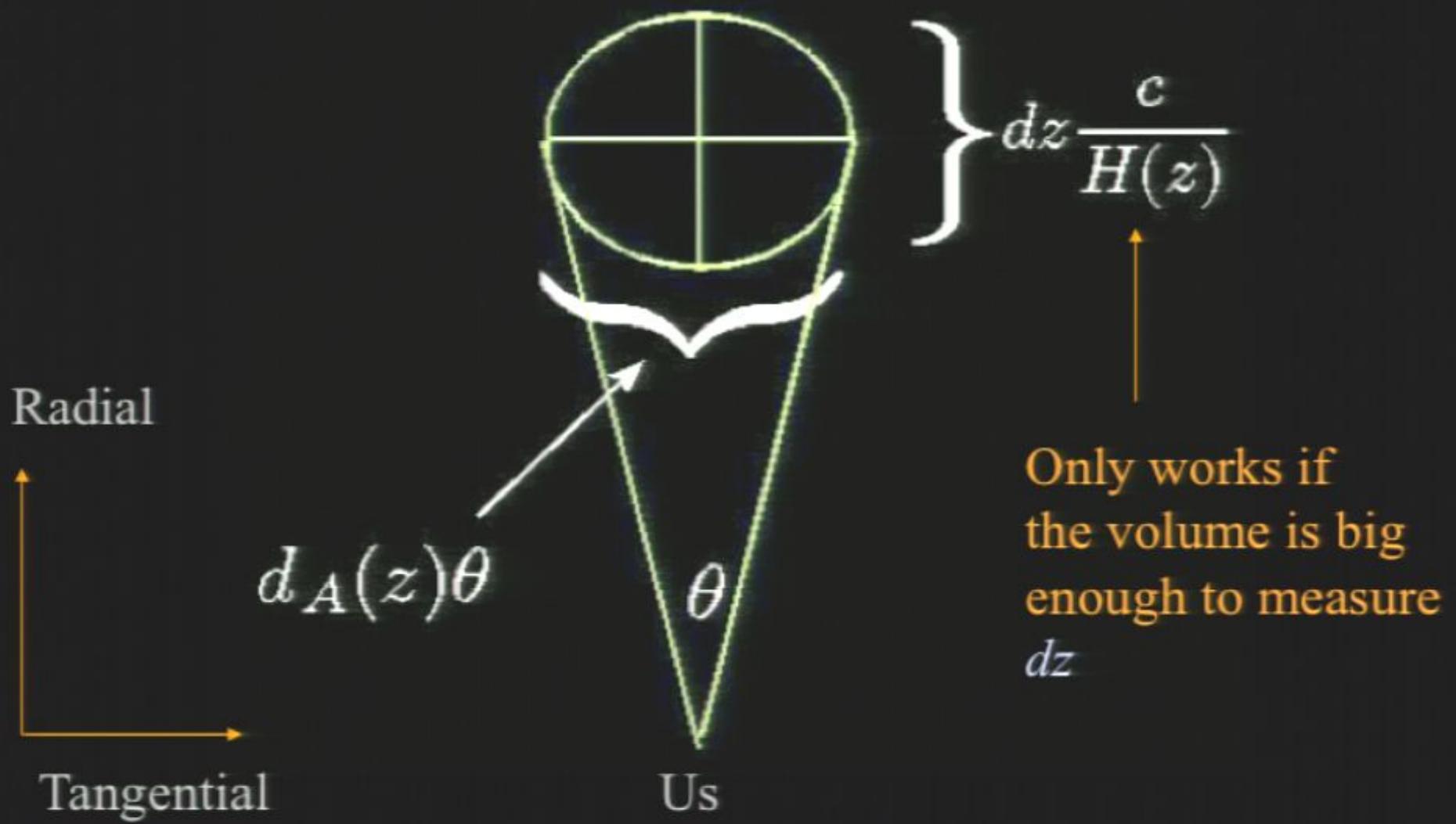


The Beauty of Standard Volumes



BAO and AP

The Beauty of Standard Volumes



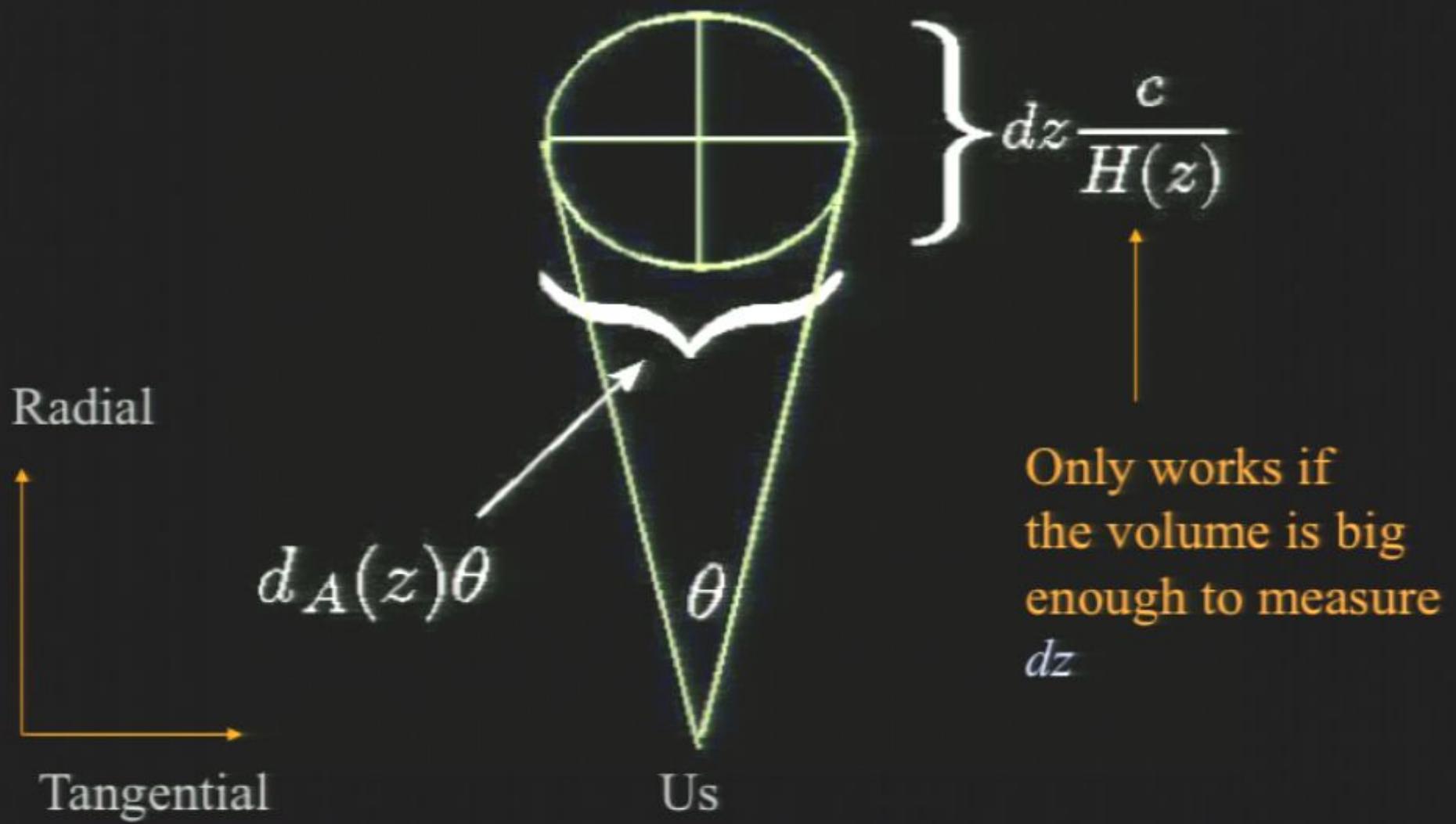
BAO and AP

BAO and AP

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BAO and AP

The Beauty of Standard Volumes



BAO and AP

BAO and AP

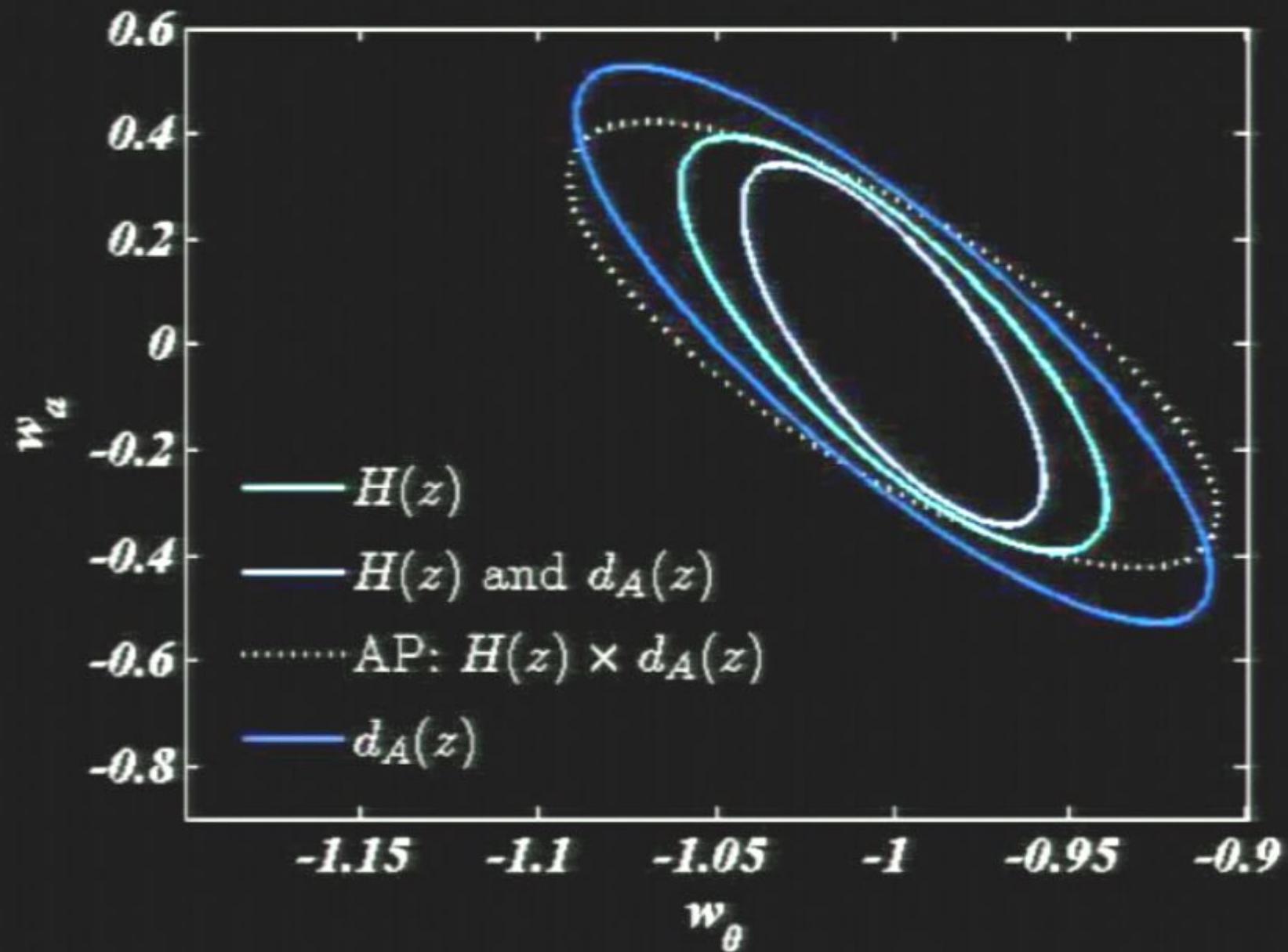
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- If we also know the *absolute* sizes in both radial and tangential directions (like with BAO), we constrain both $d_A(z)$ and $H(z)$ separately.

BAO and AP

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- If we also know the *absolute* sizes in both radial and tangential directions (like with BAO), we constrain both $d_A(z)$ and $H(z)$ separately.
- BAO thus provide an *absolute* AP test.

$$d_A(z) = \frac{c}{H_0 \sqrt{-\Omega_k} (1+z)} \sin\left(\sqrt{-\Omega_k} \int_0^z \frac{H_0}{H(z')} dz' \right)$$

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Testing the Copernican Principle

- Test isotropy of gravitational collapse via comparison of BAO with other probes (e.g. SNIa)
- Compare curvature at different redshifts using

$$\Omega_k = \frac{[H(z)D'(z)]^2 - 1}{[H_0 D(z)]^2}$$

arXiv:0712.3457

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What are BAO and why do we think they are standard rulers?

3D Green's Function for Φ

$$\phi^{(3)}(r, \tau) = \frac{3}{4\pi} (c_s \tau)^{-3} \theta(c_s \tau - r)$$

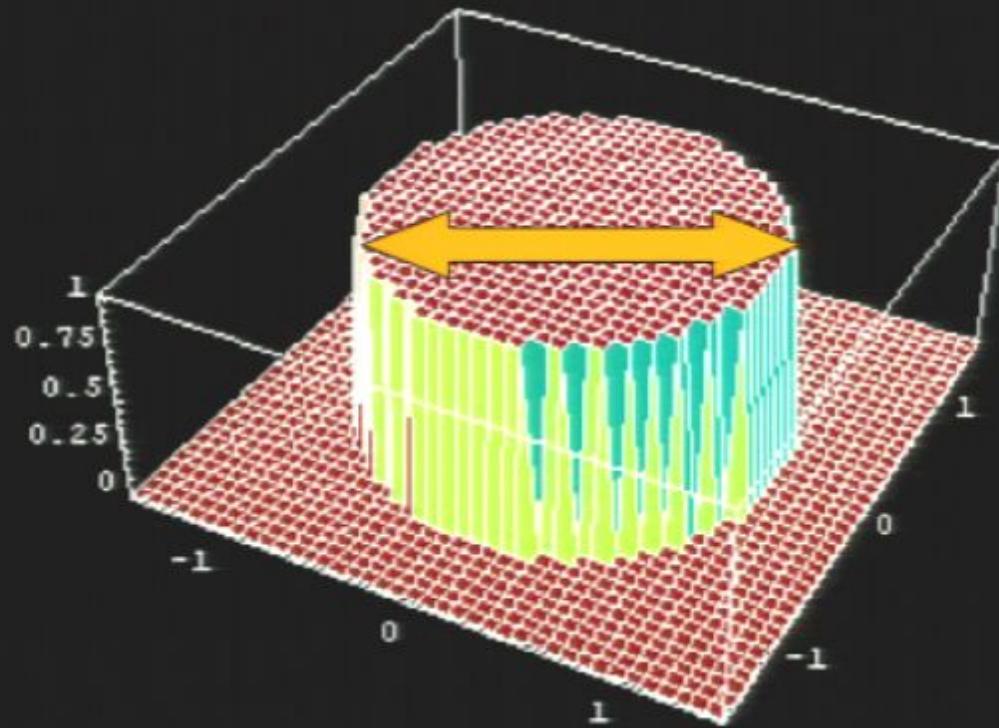
Speed of Sound



Sound Horizon

Bashinsky and Bertschinger, 2000

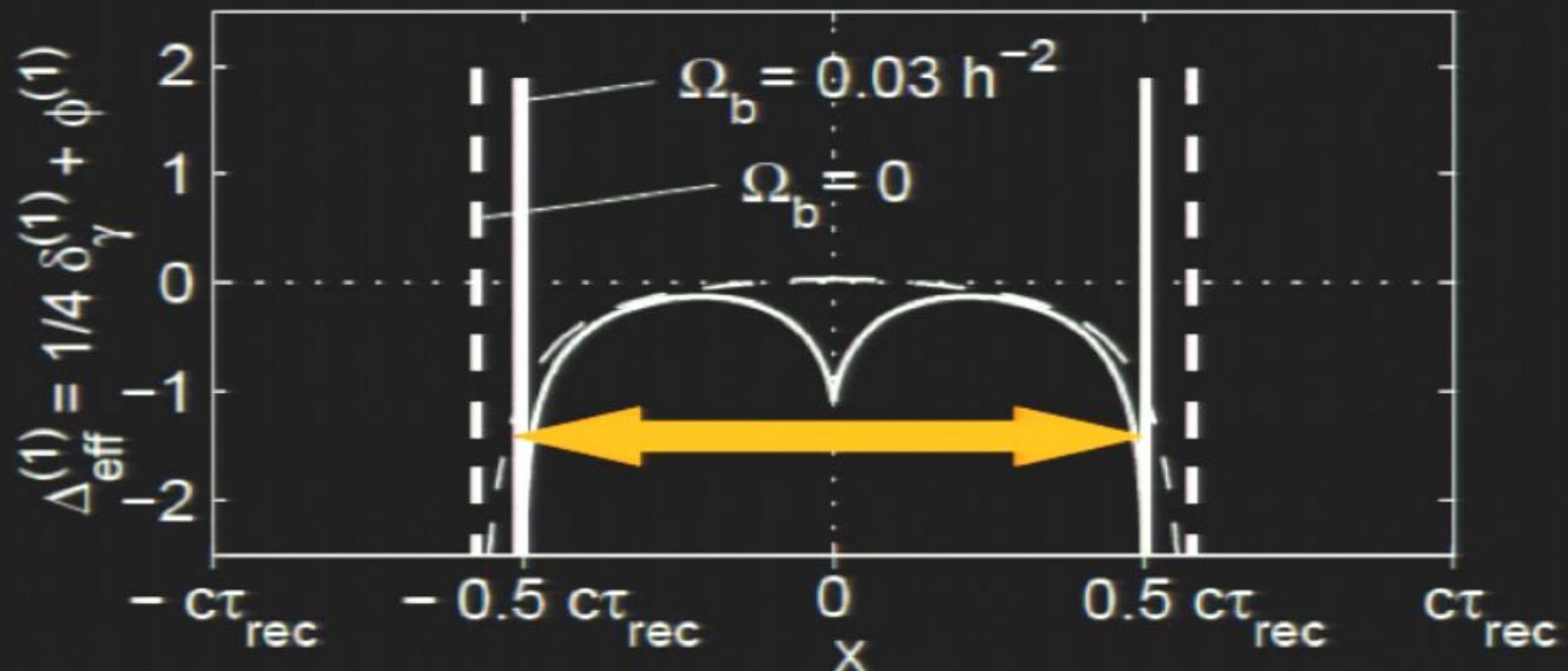
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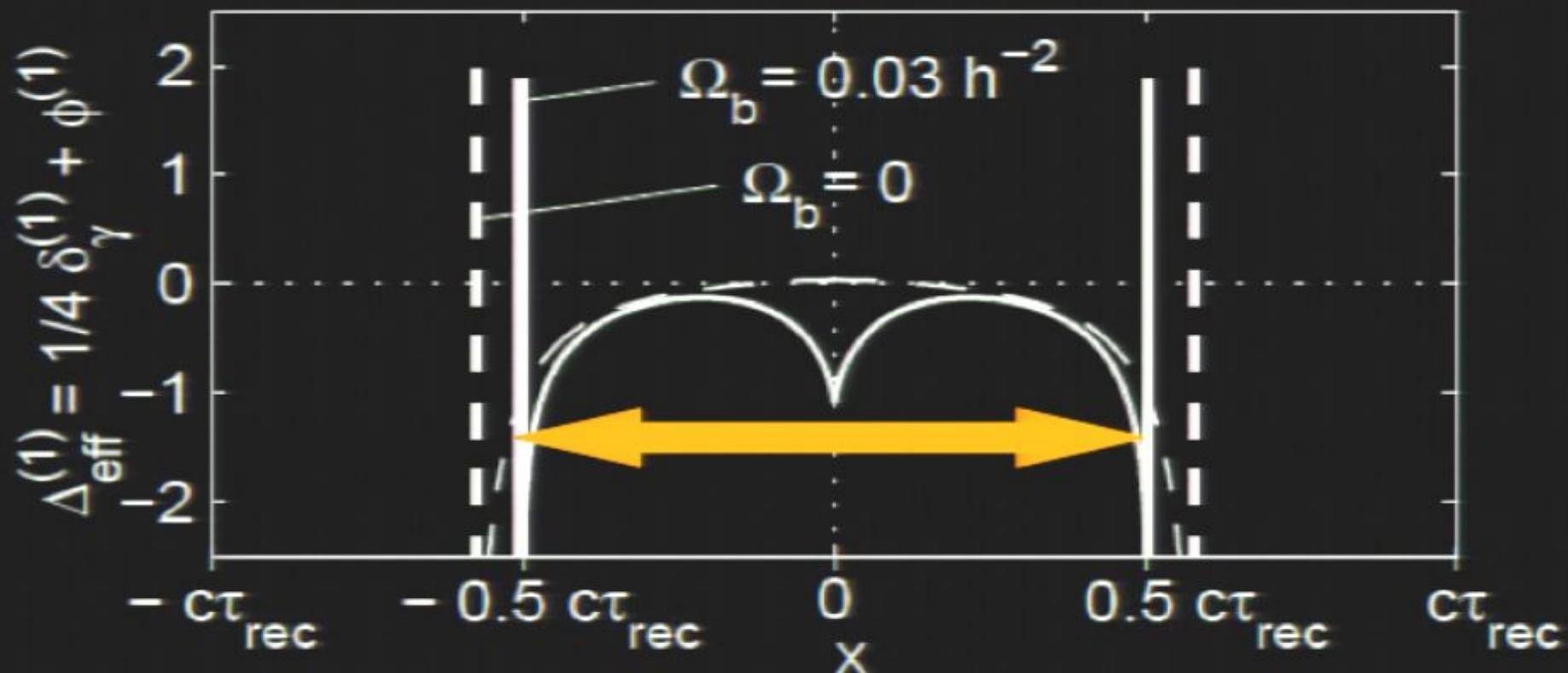
Light travels faster than sound.
This is why some people appear
bright until you hear them speak.

.... only partially true before decoupling

Real Space Transfer Function



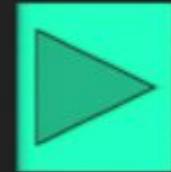
Real Space Transfer Function

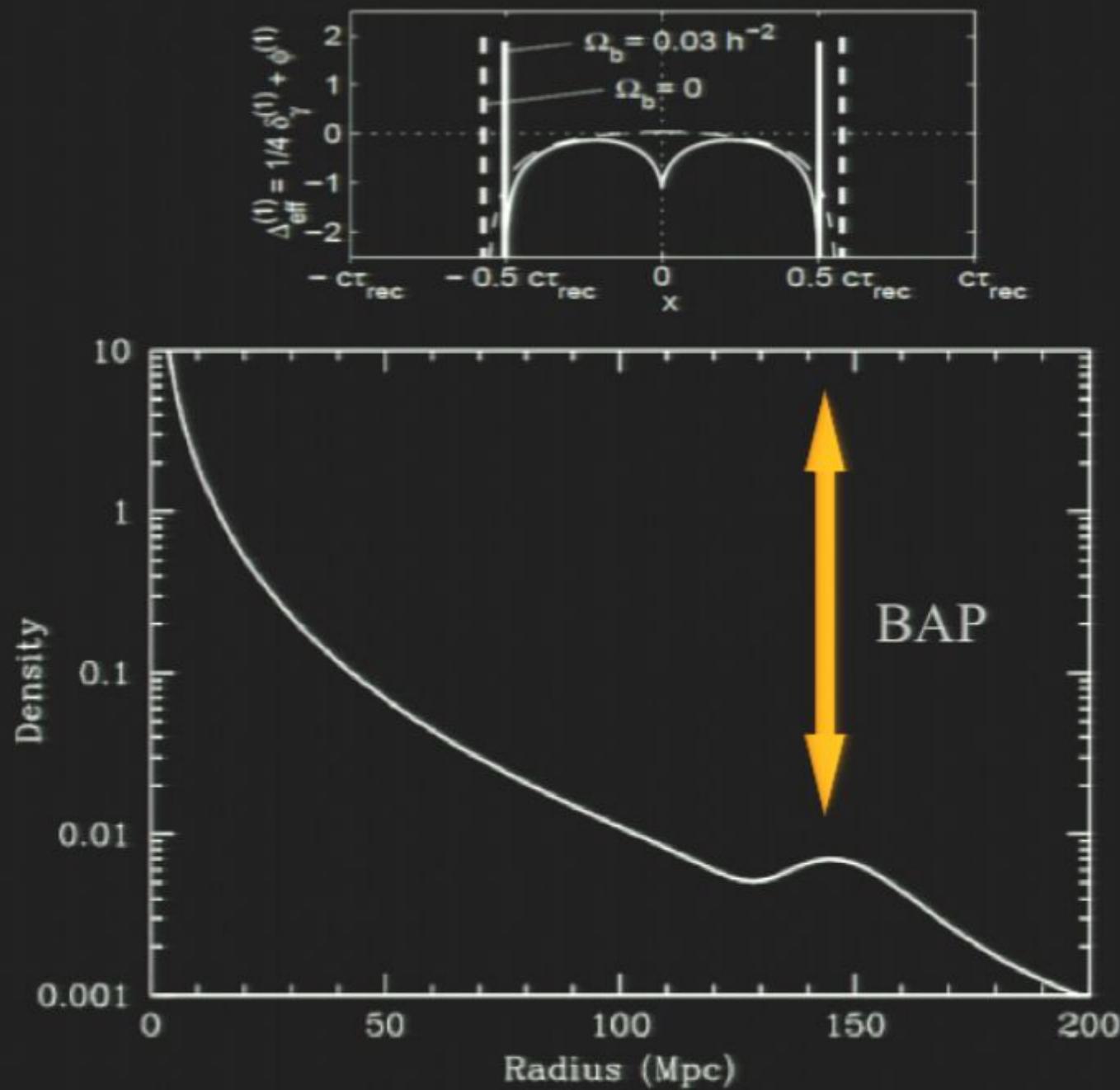


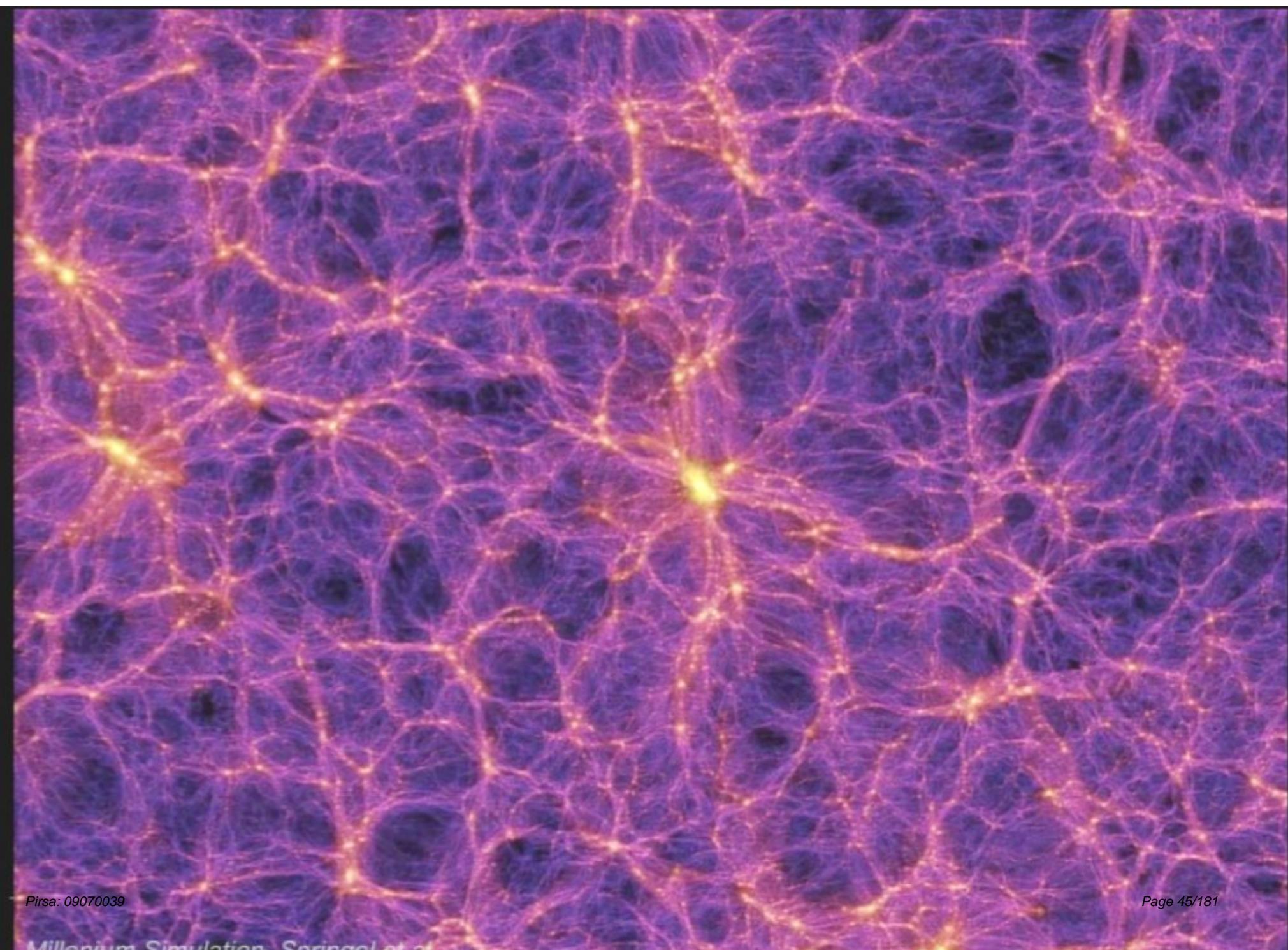
$$c_s^2 = (1/3)/[1 + (3\rho_b)/(4\rho_\gamma)]$$

Bashinsky and Bertschinger, 2

It is the same standard ruler
that suggests the cosmos is flat

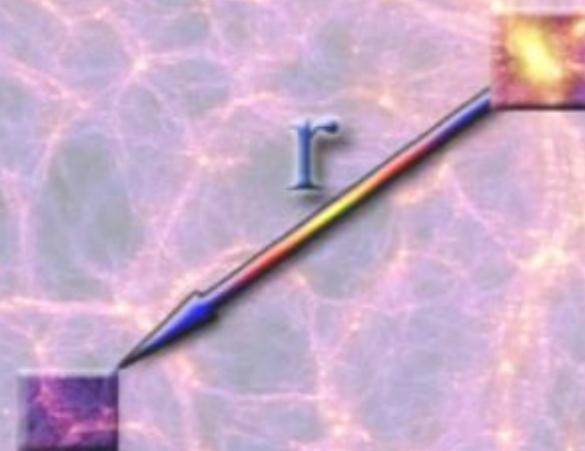






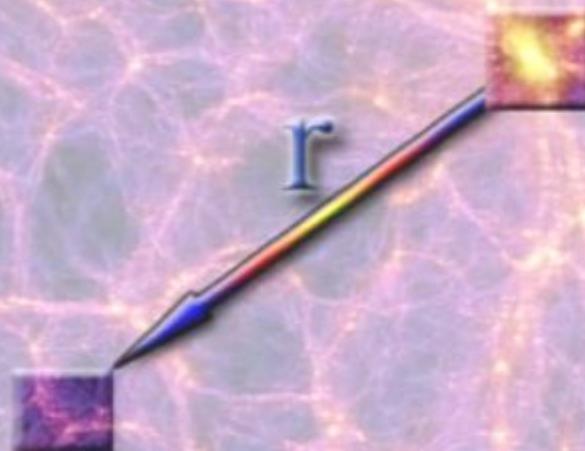
2-point Correlation function

$$\xi(r)$$

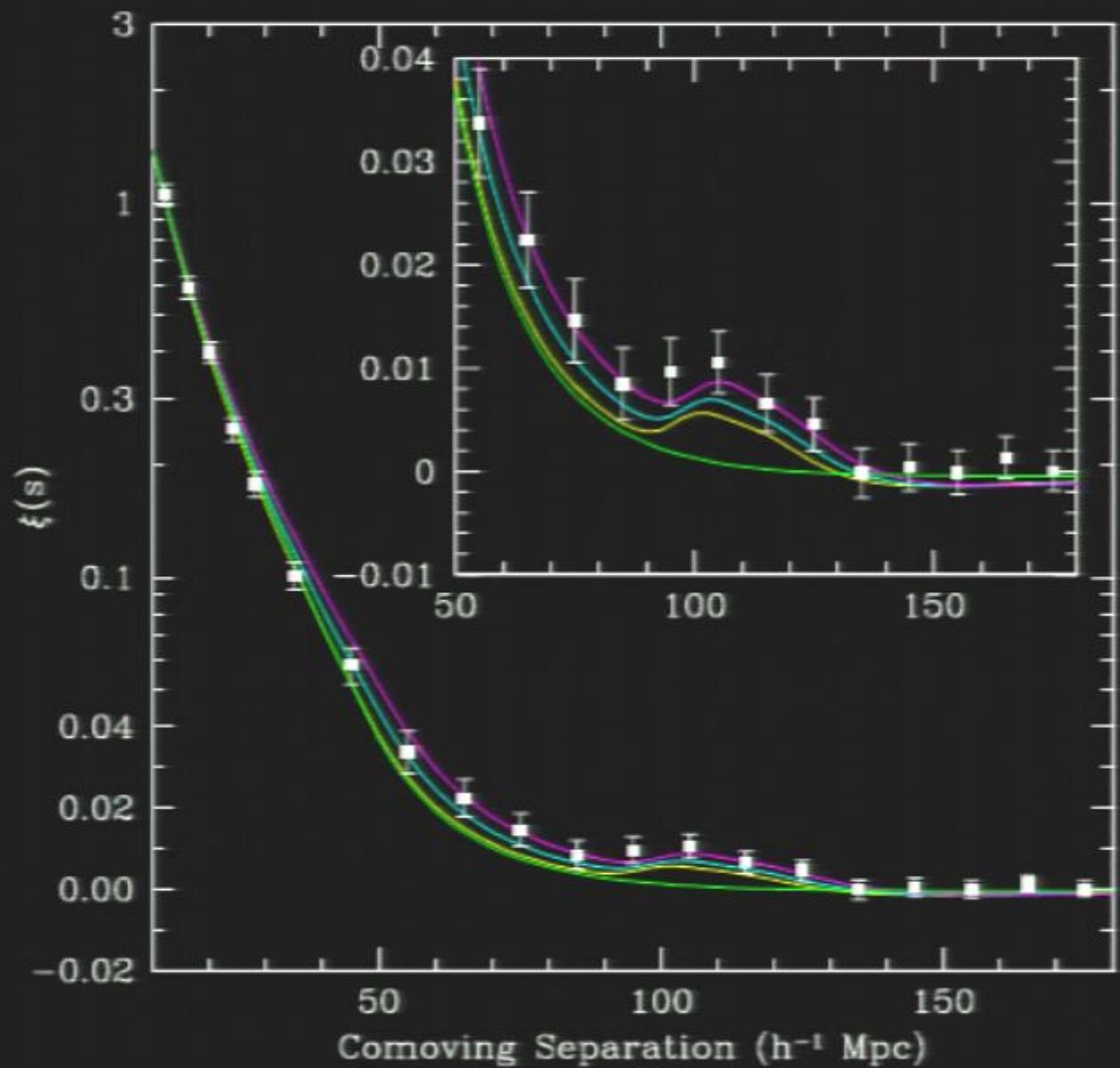


2-point Correlation function

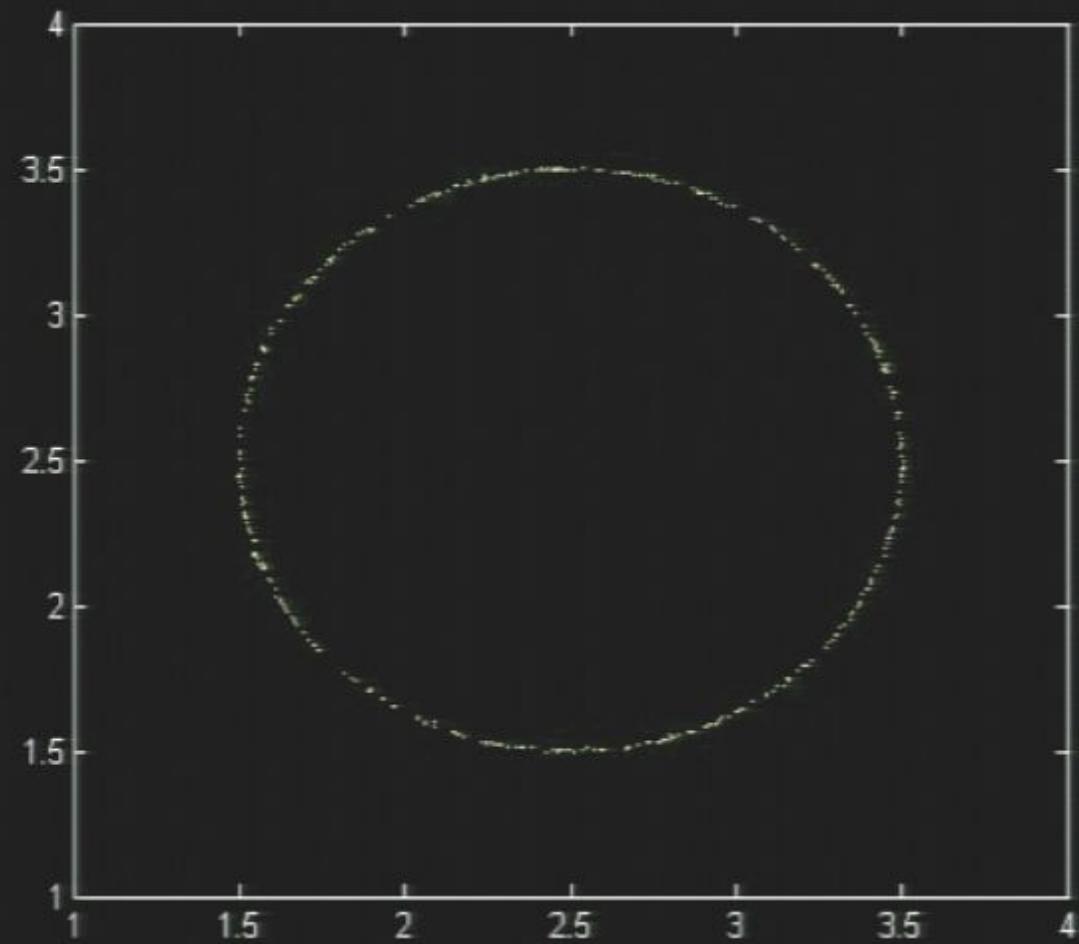
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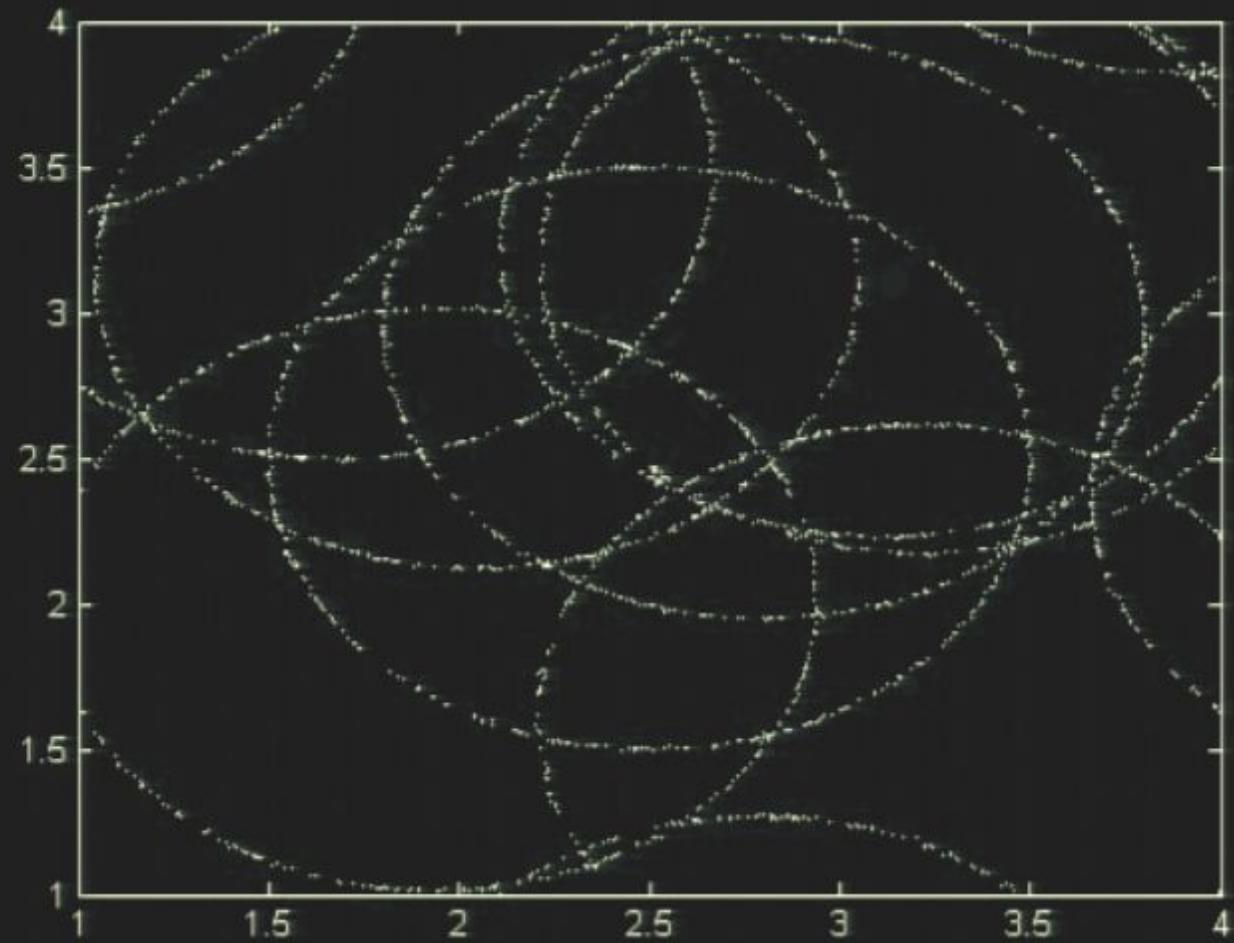


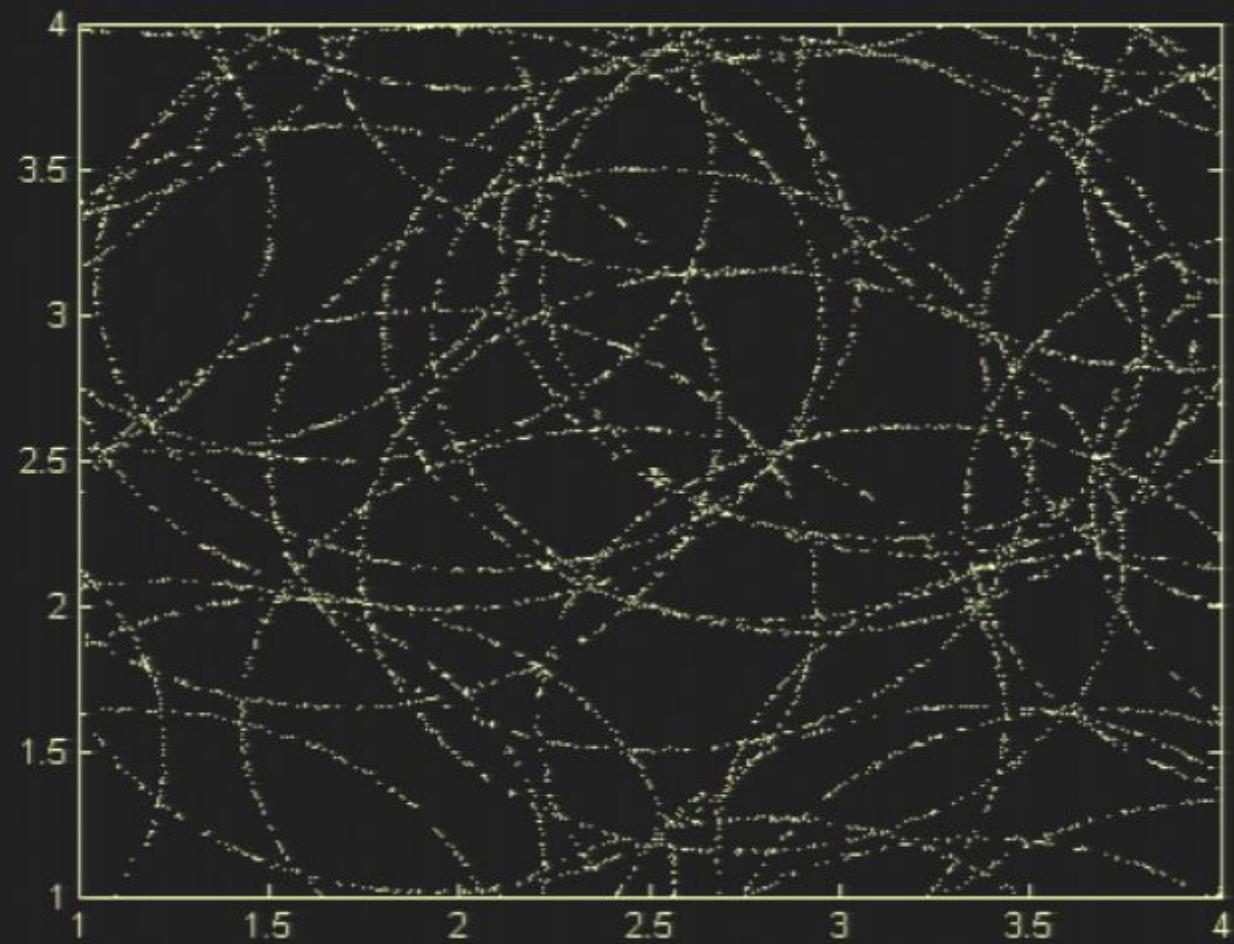
We expect to see an increase
in $\xi(r)$ at $r \sim 100 \text{ Mpc}$

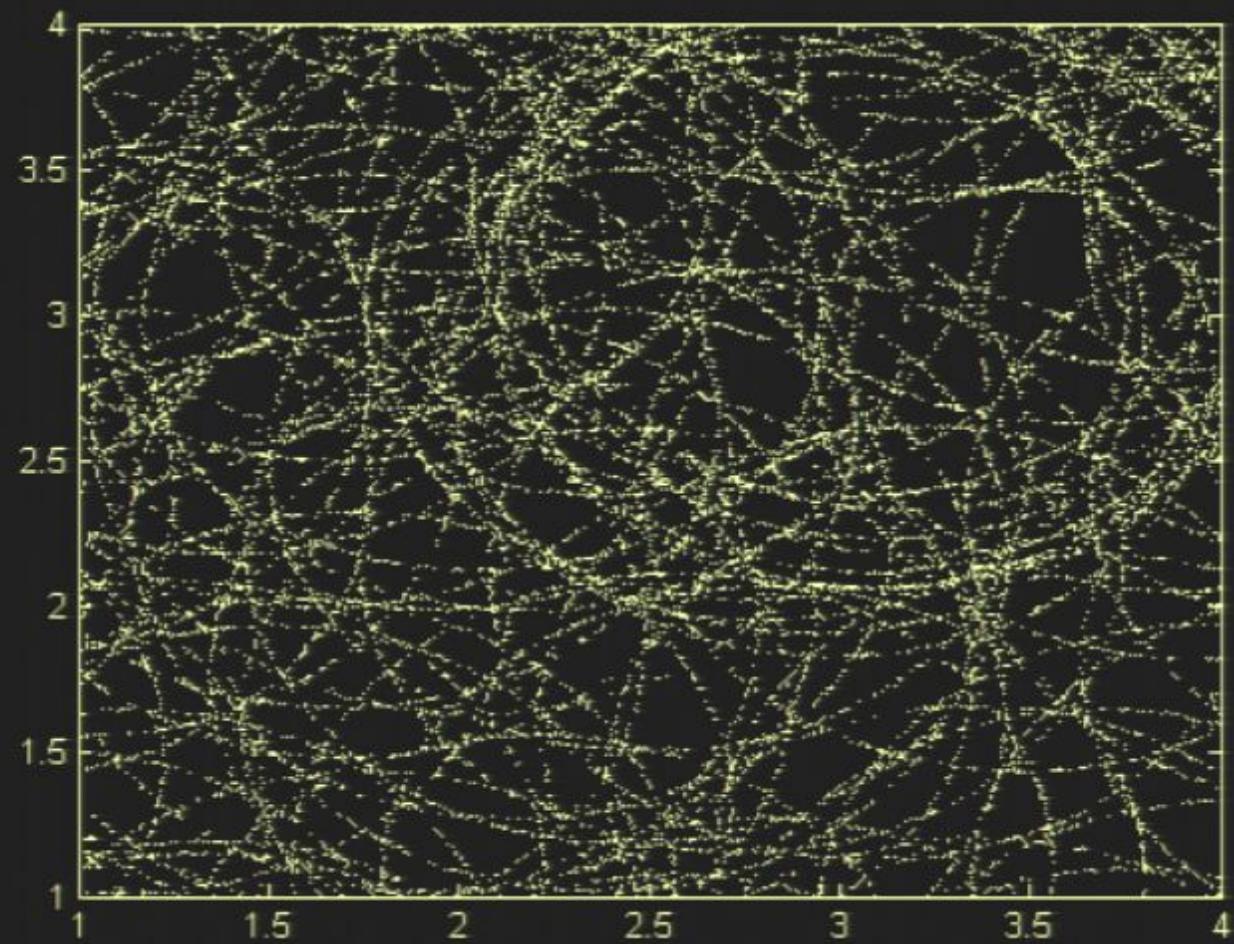


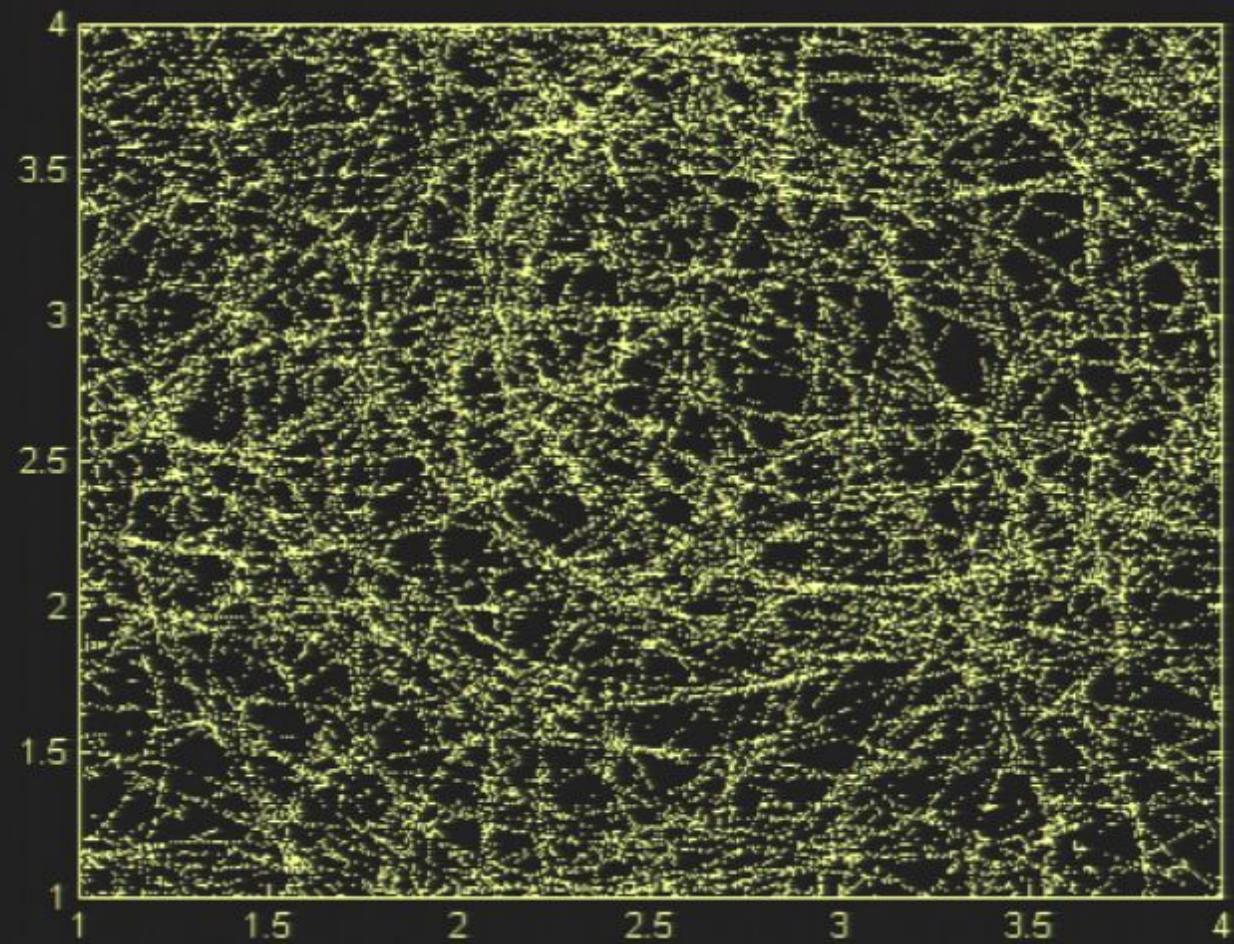
Eisenstein et al. SDSS LR
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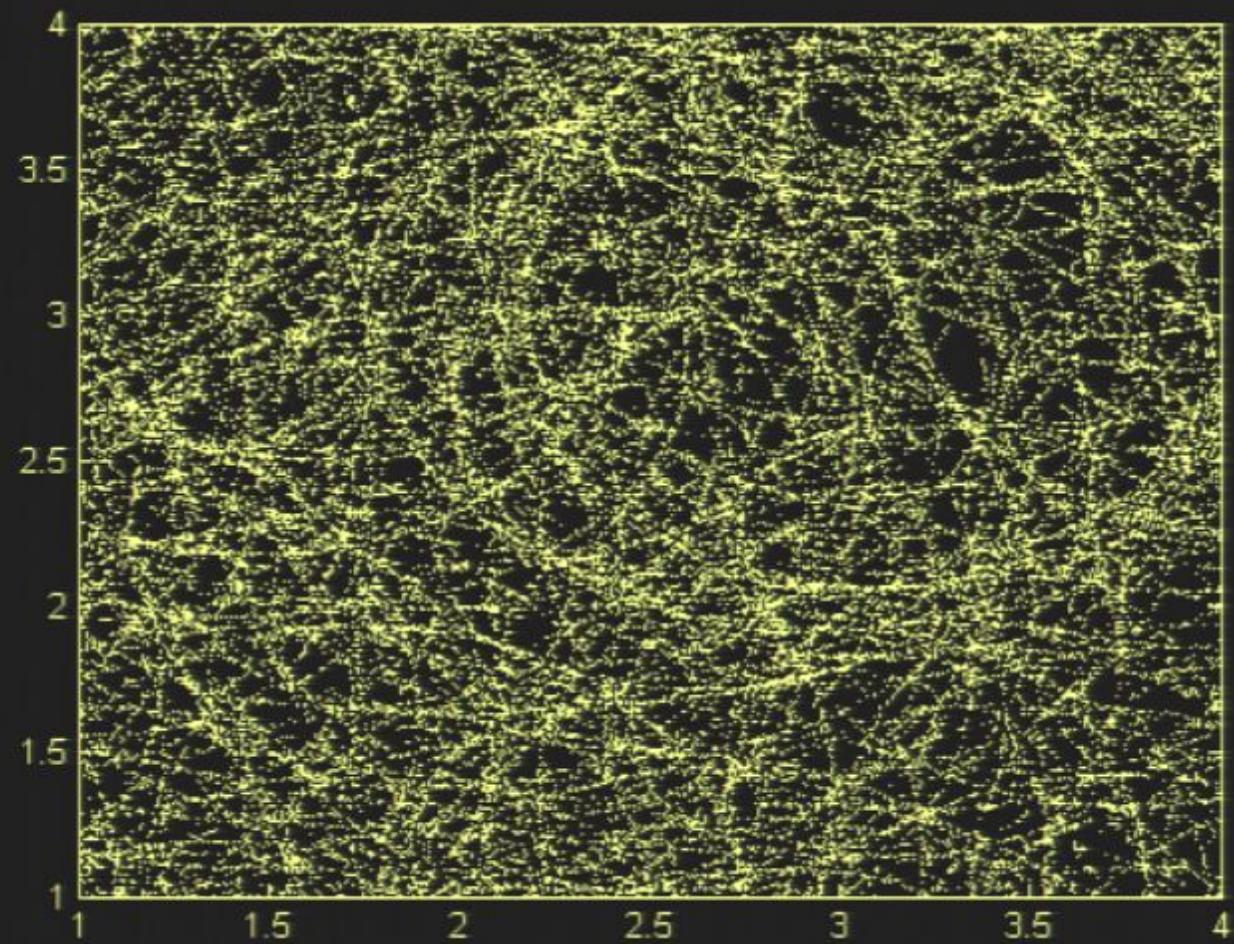


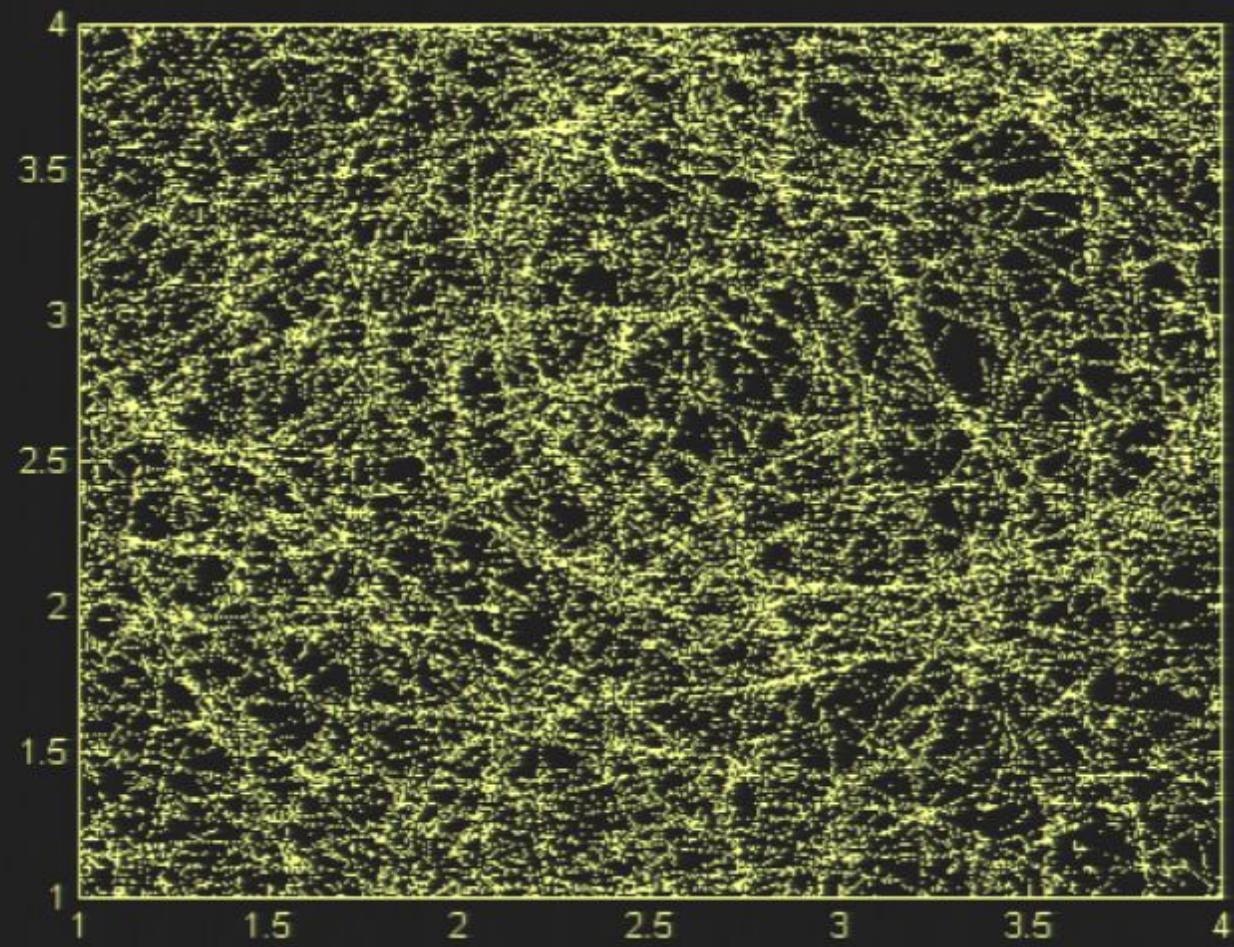




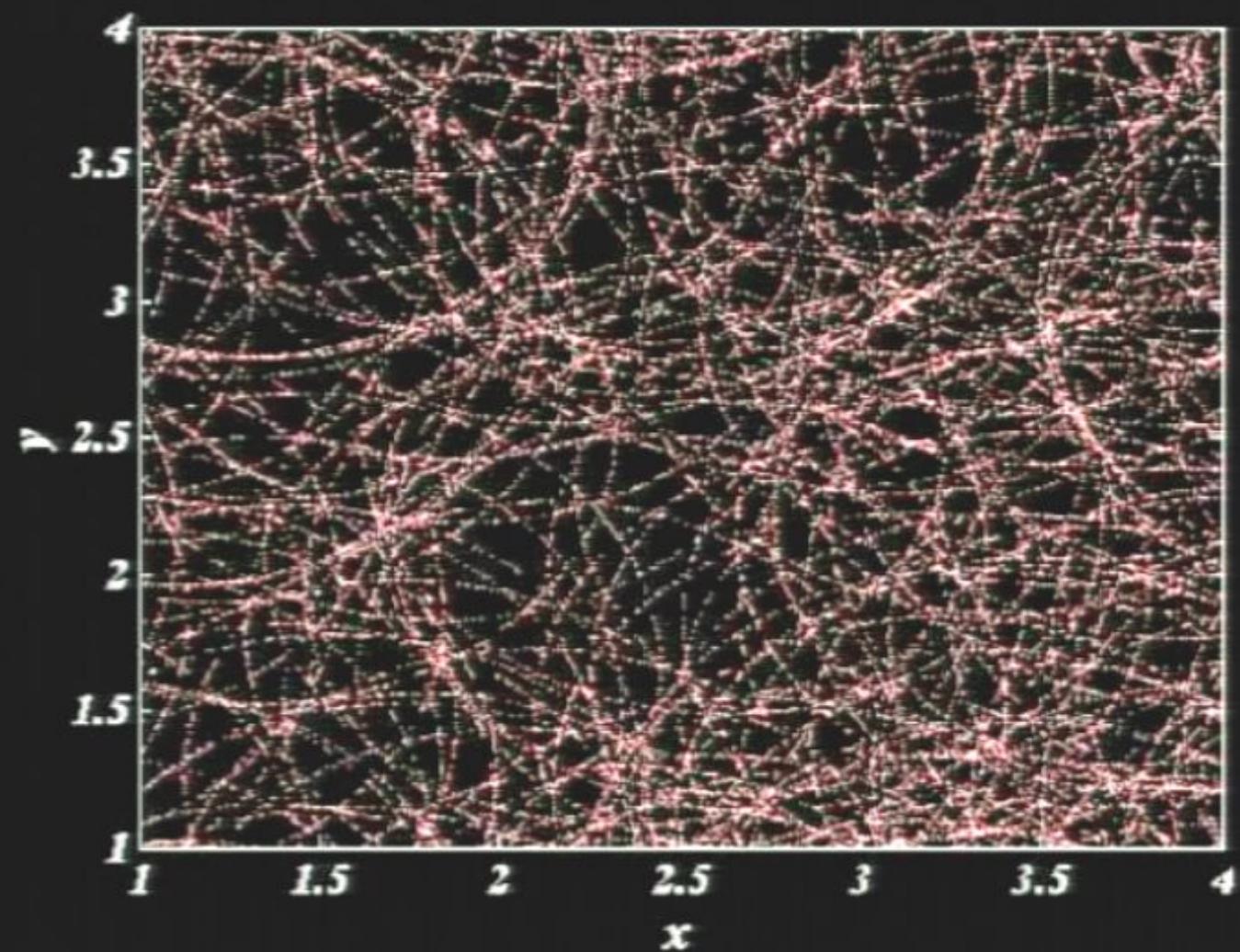




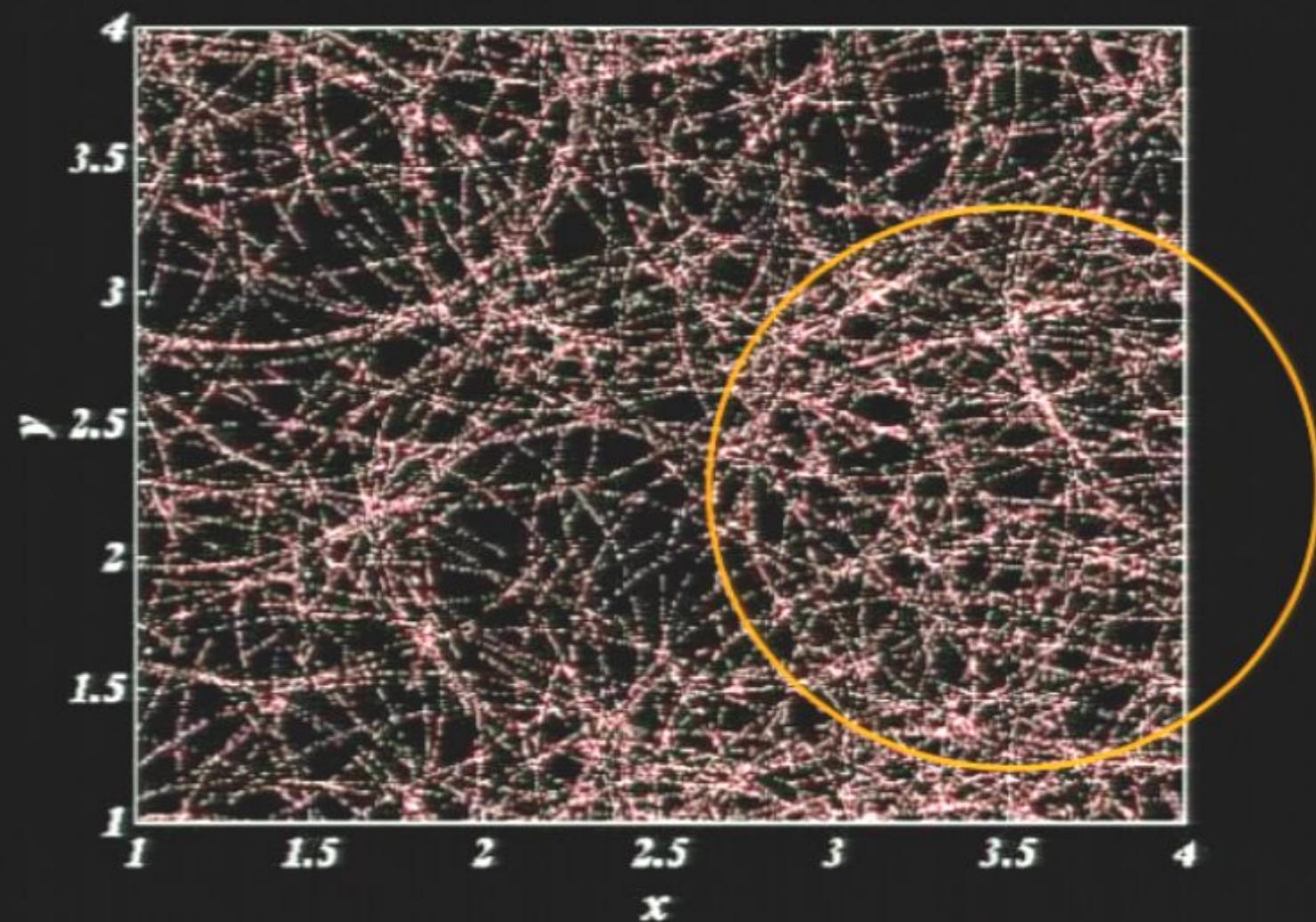




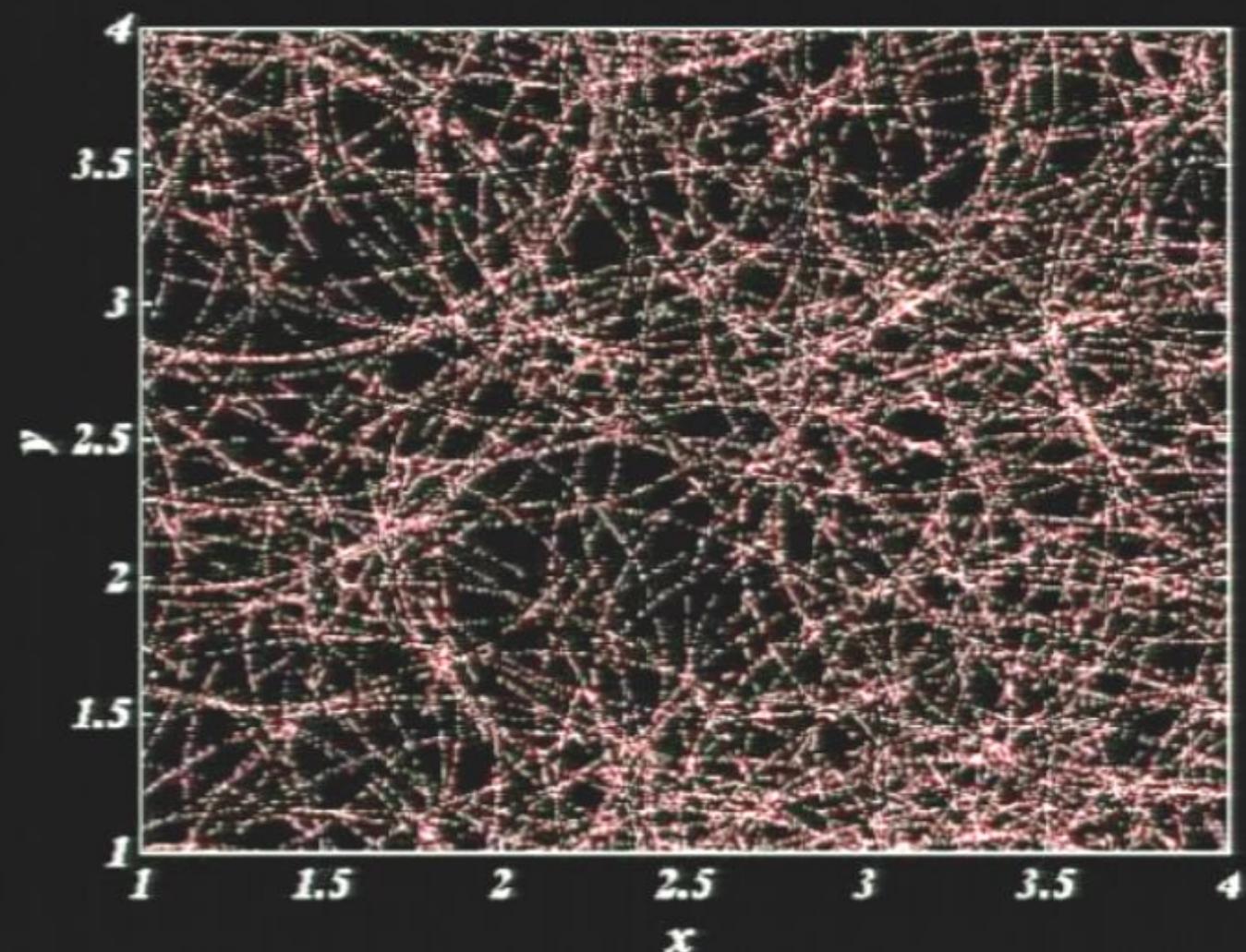
Statistical Standard Rulers



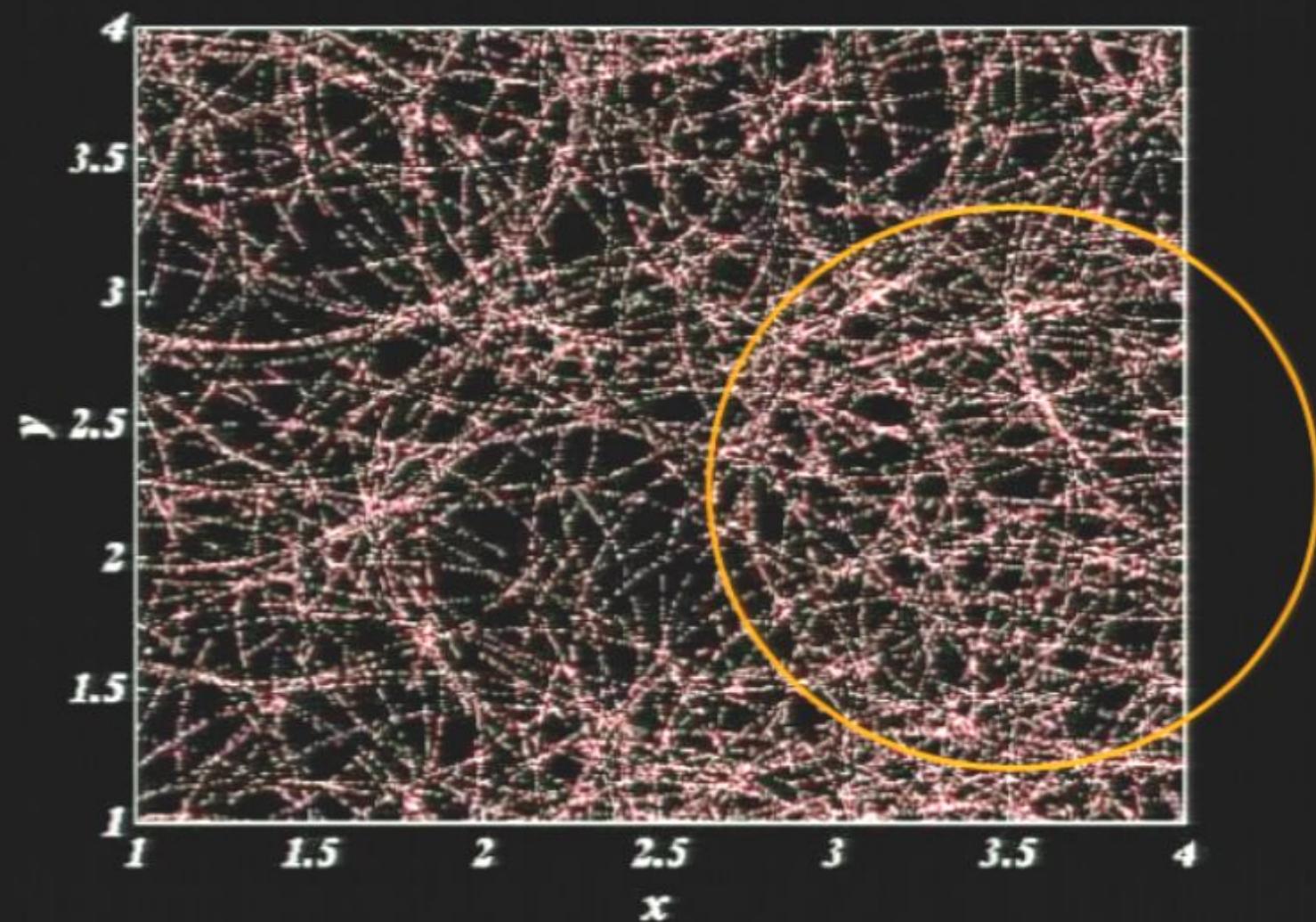
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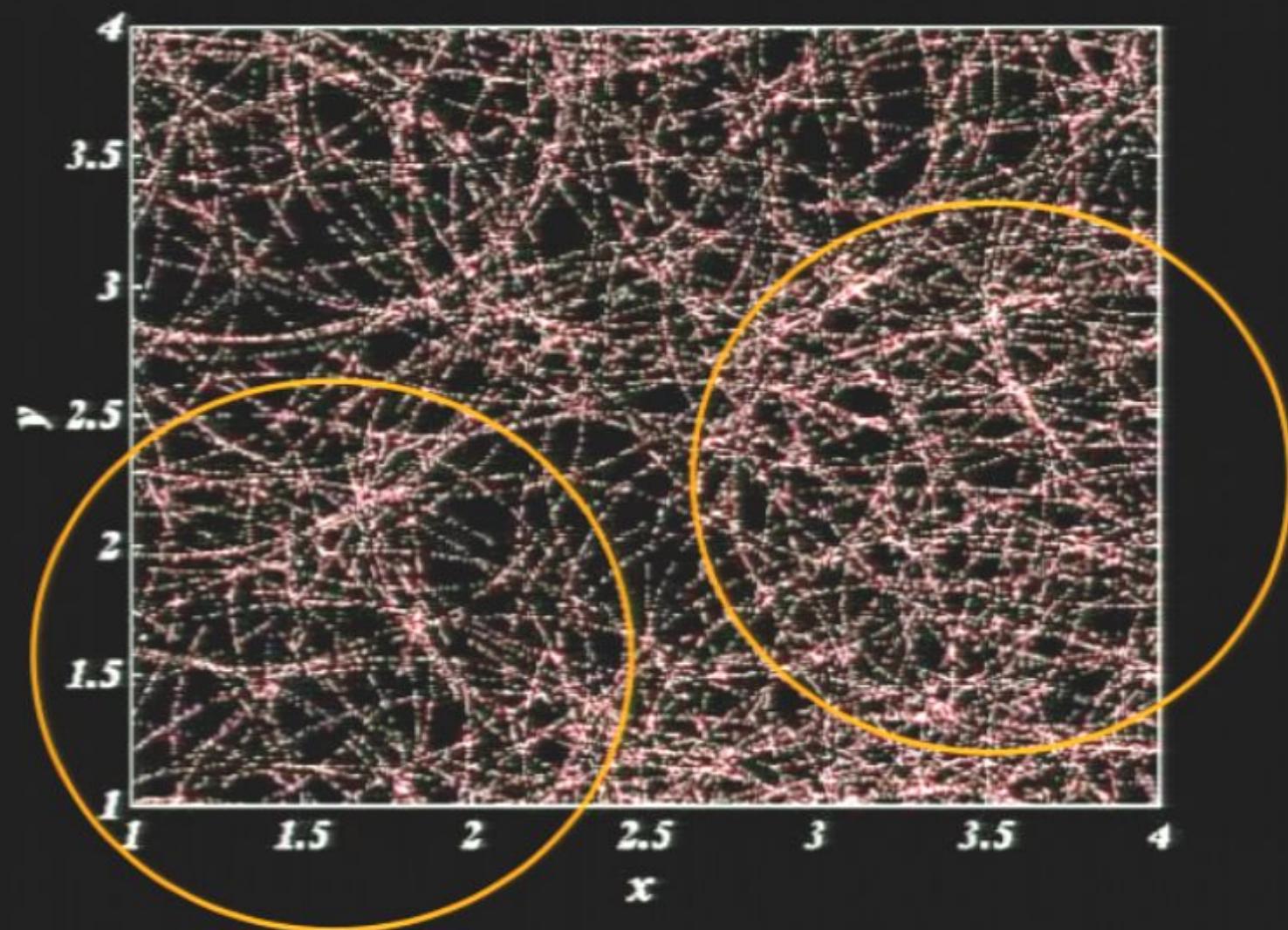
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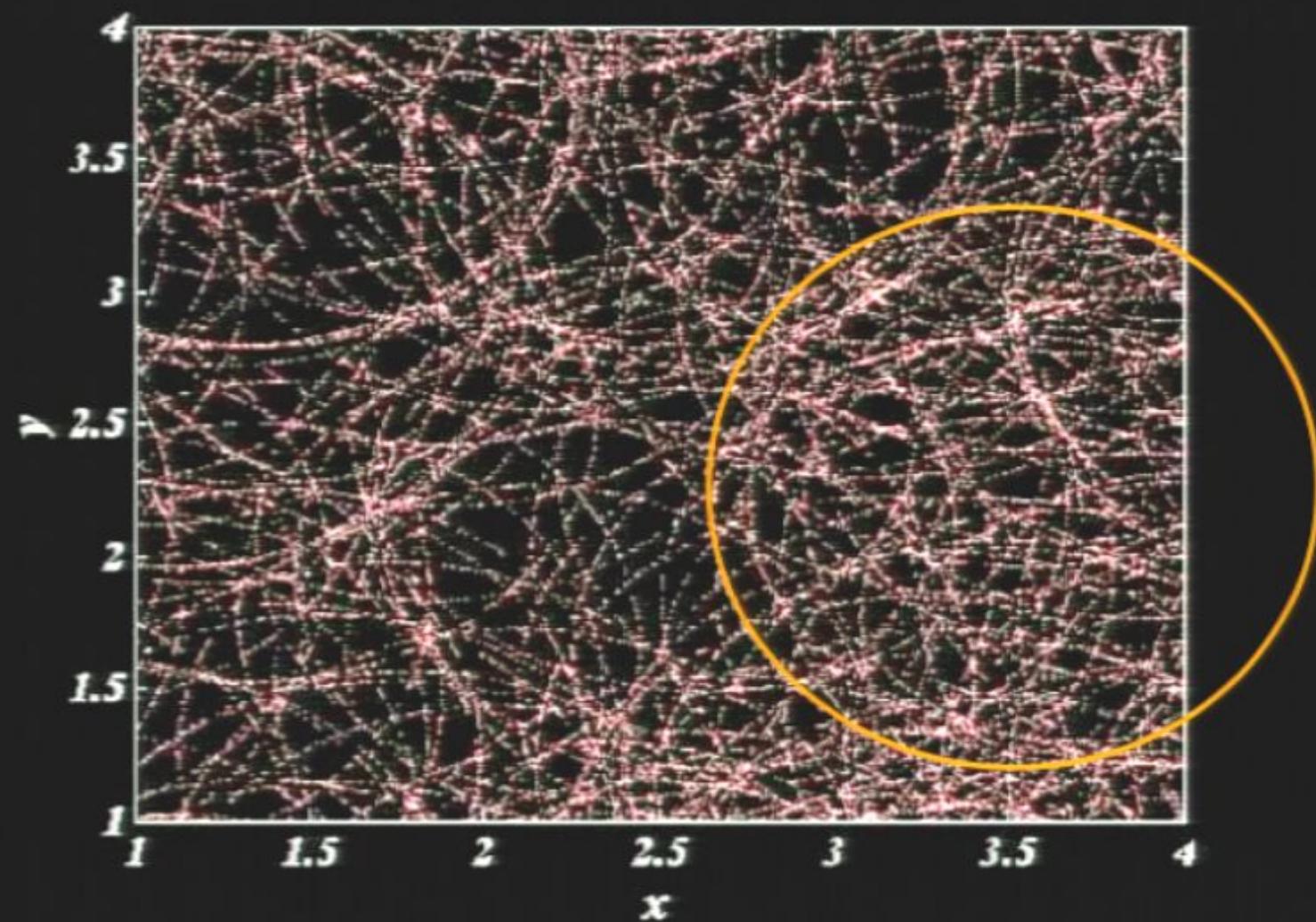
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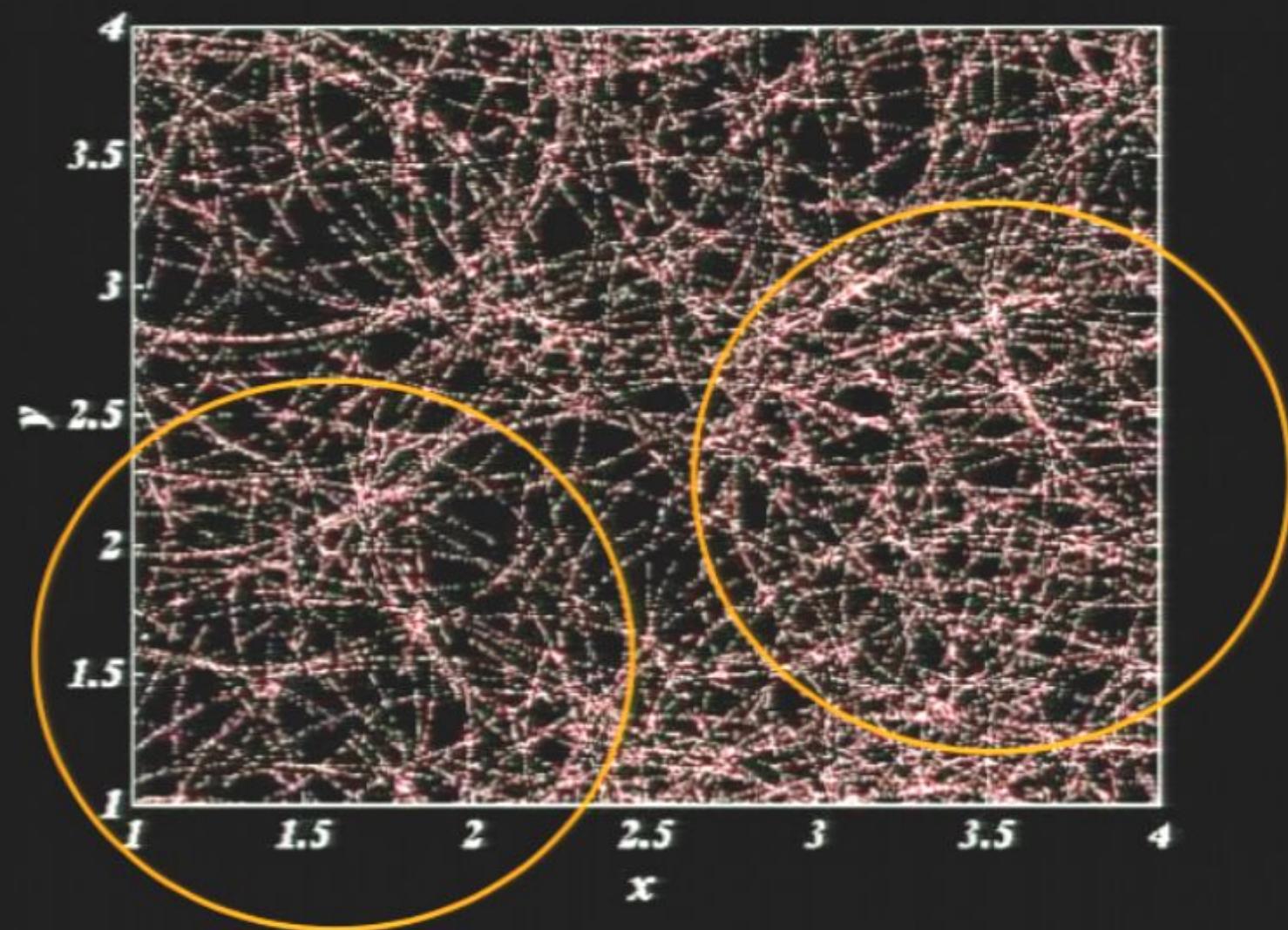
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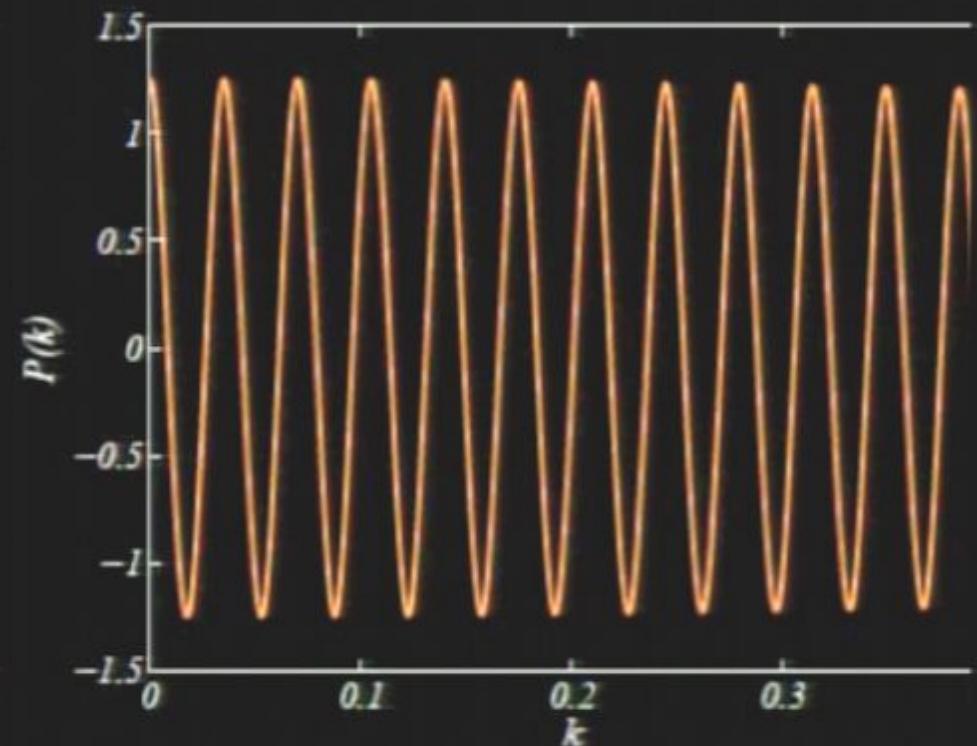
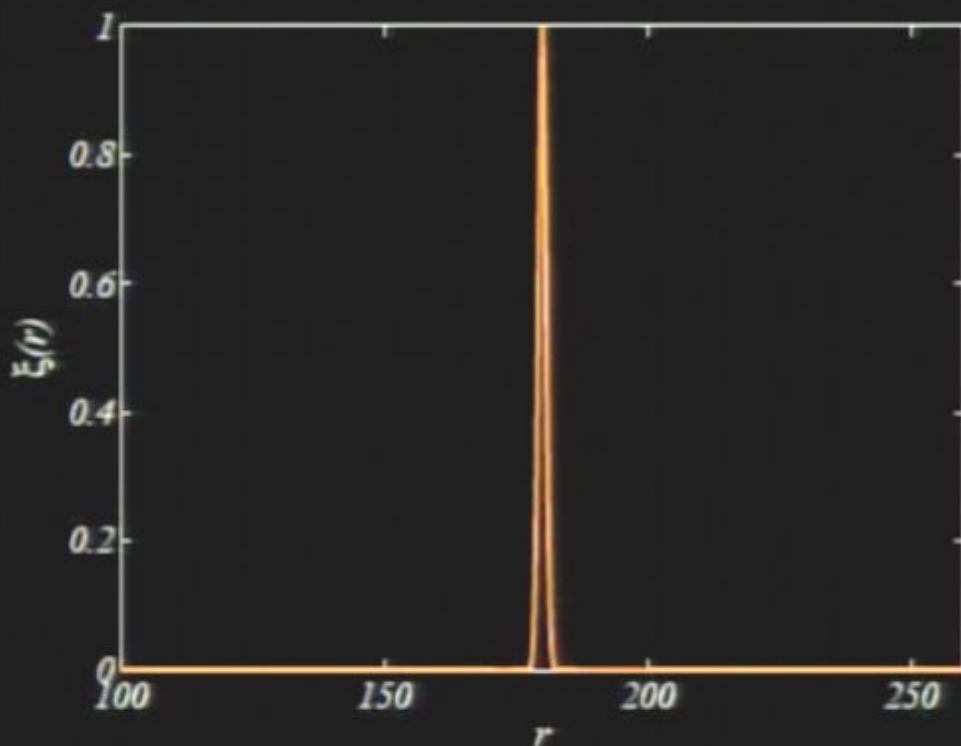
Statistical Standard Rulers



Statistical Standard Rulers



Where are the oscillations in BAO?

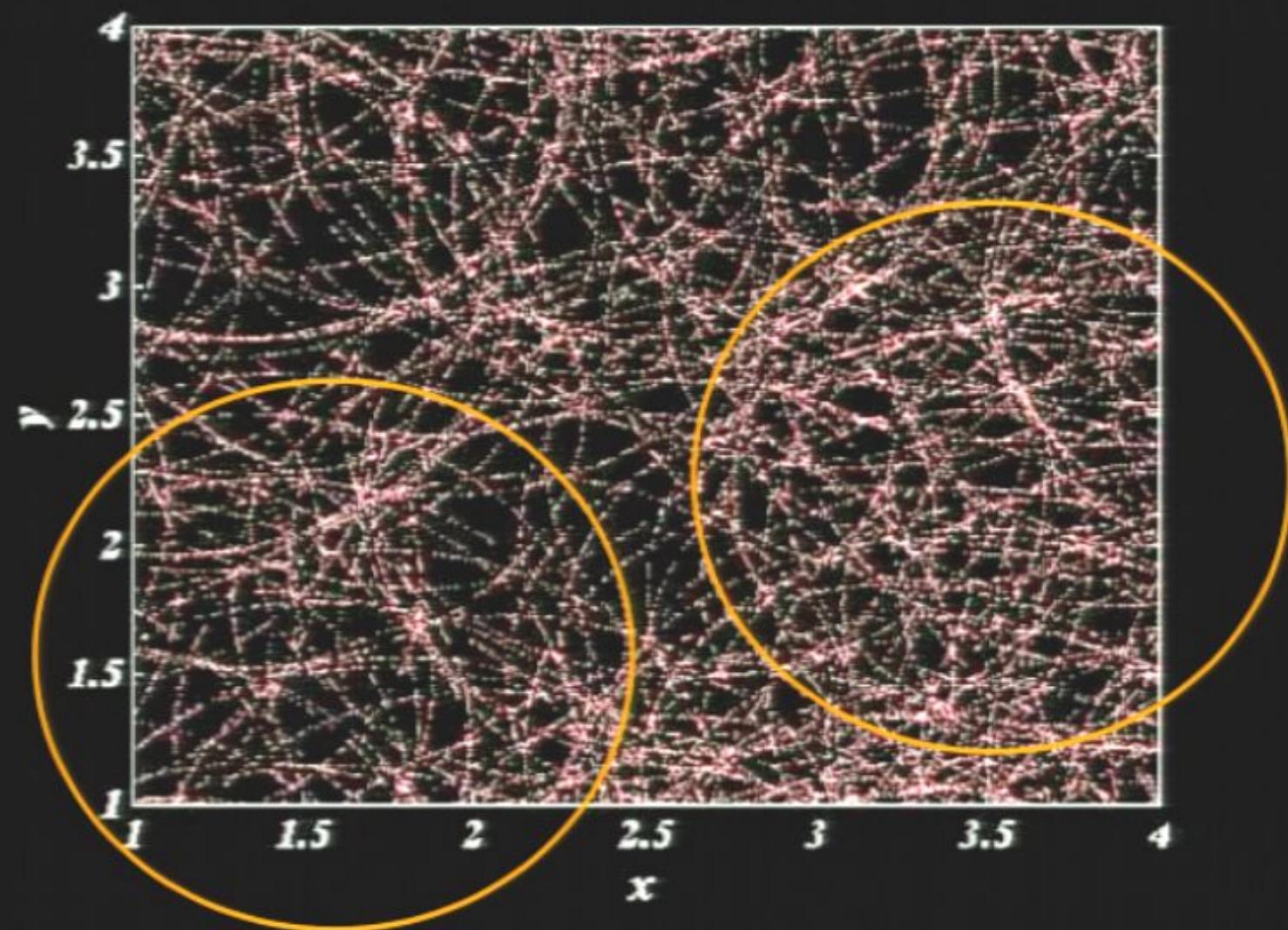


$\xi(r)$

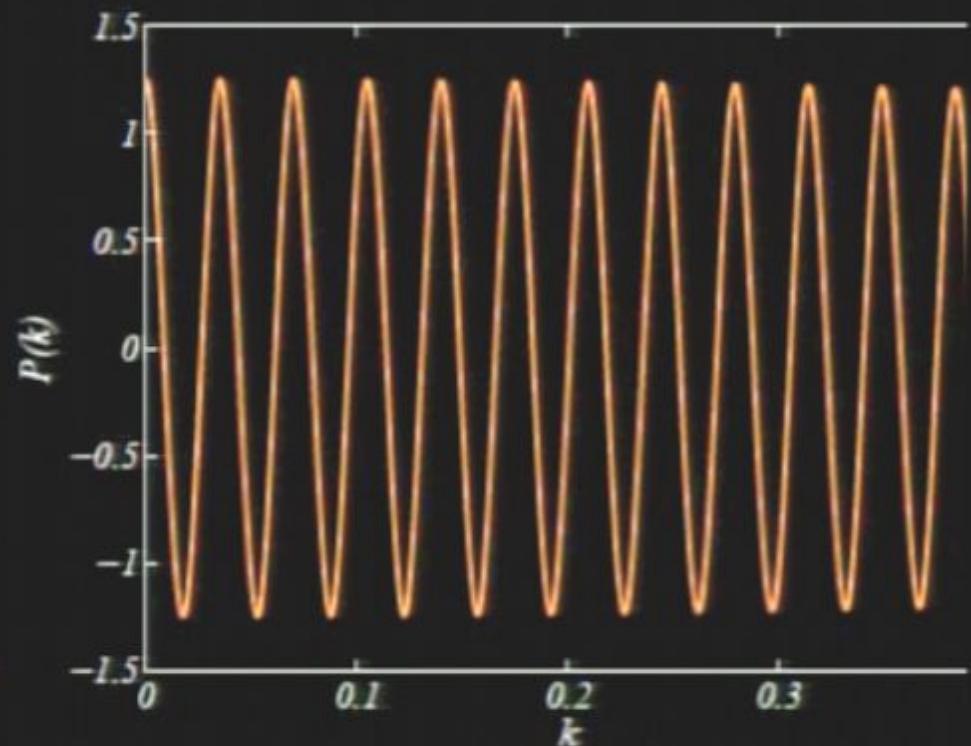
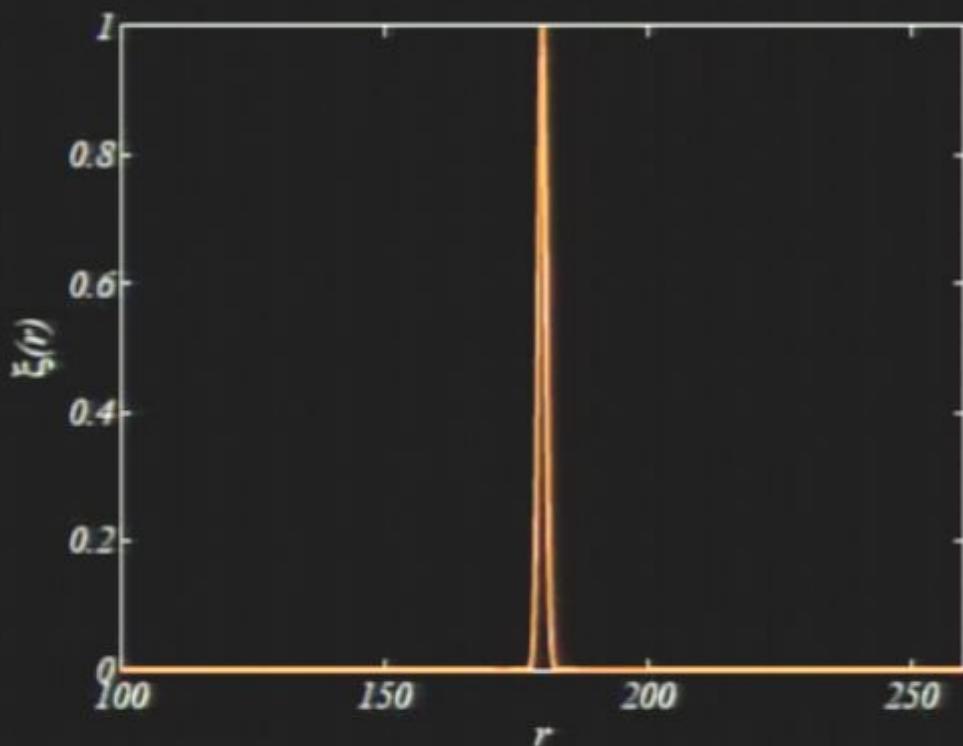


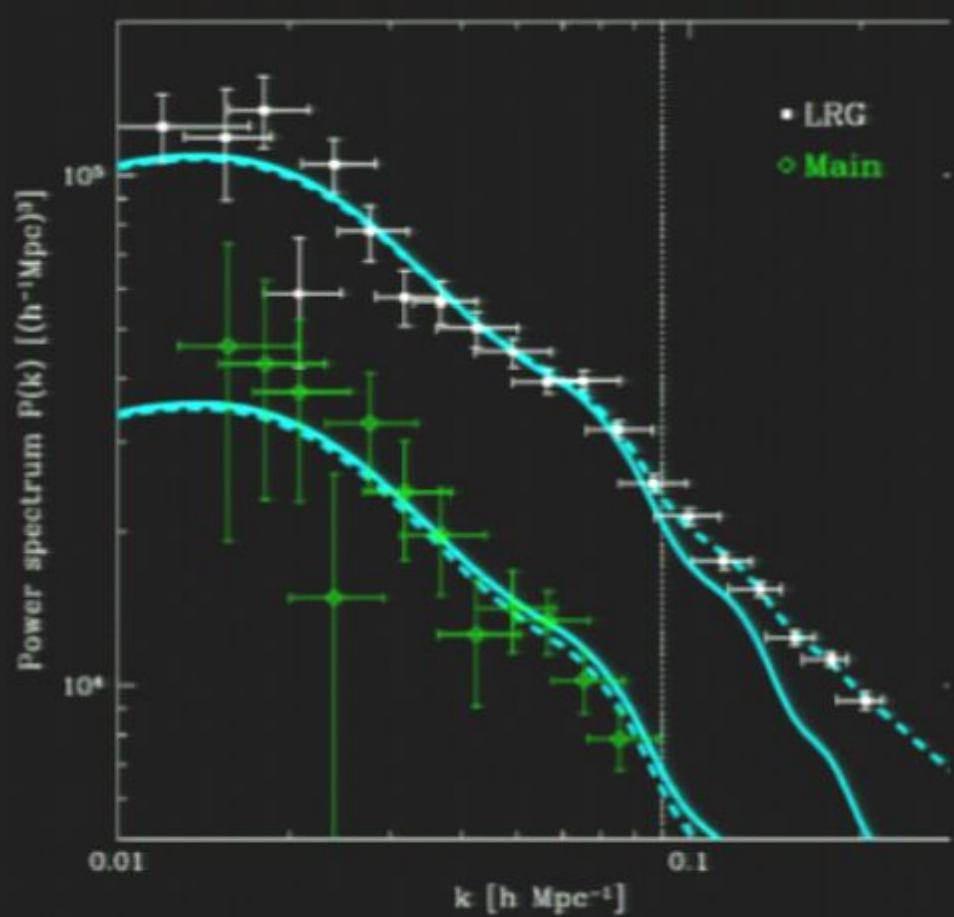
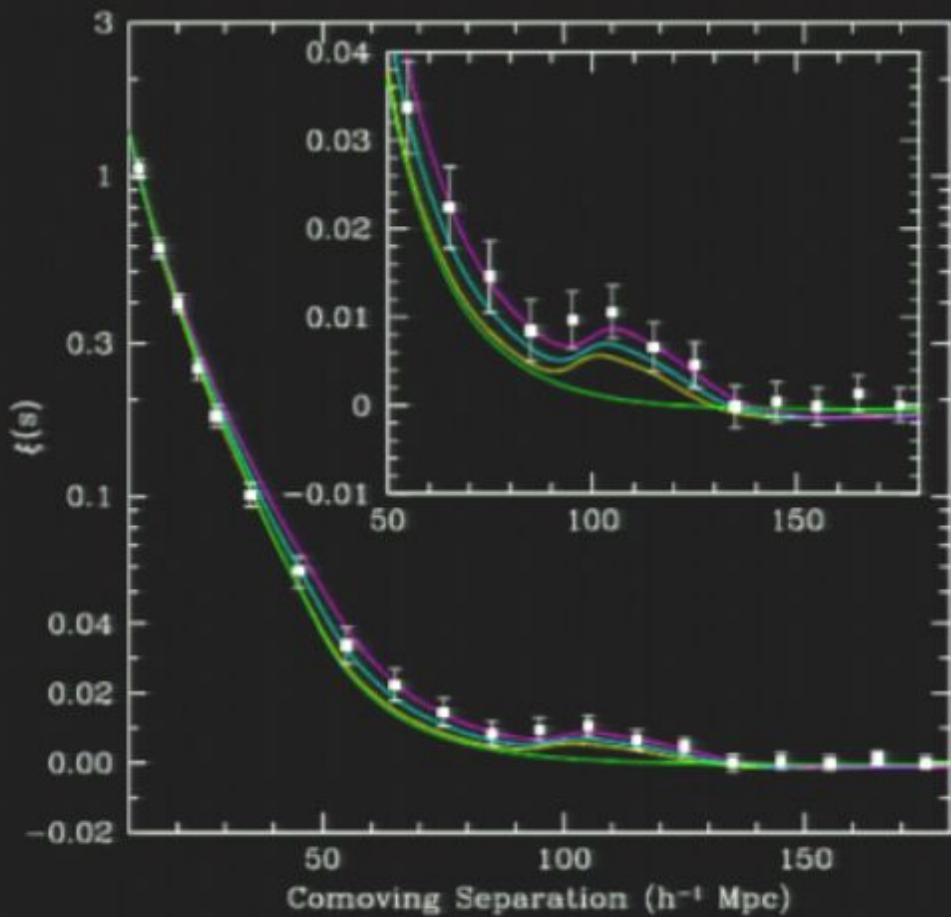
$P(k)$

Statistical Standard Rulers



Where are the oscillations in BAO?

 $\xi(r)$  $P(k)$


 $\xi(r)$

 $P(k)$

BAP Detection Is Hard!

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- Consider a typical LRG. How many LRGs do we expect in a BAP shell around it?

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- Volume = $20 Mpc \times 100^2 Mpc^2 \times 5 \sim 10^6 h^{-3} Mpc^3$

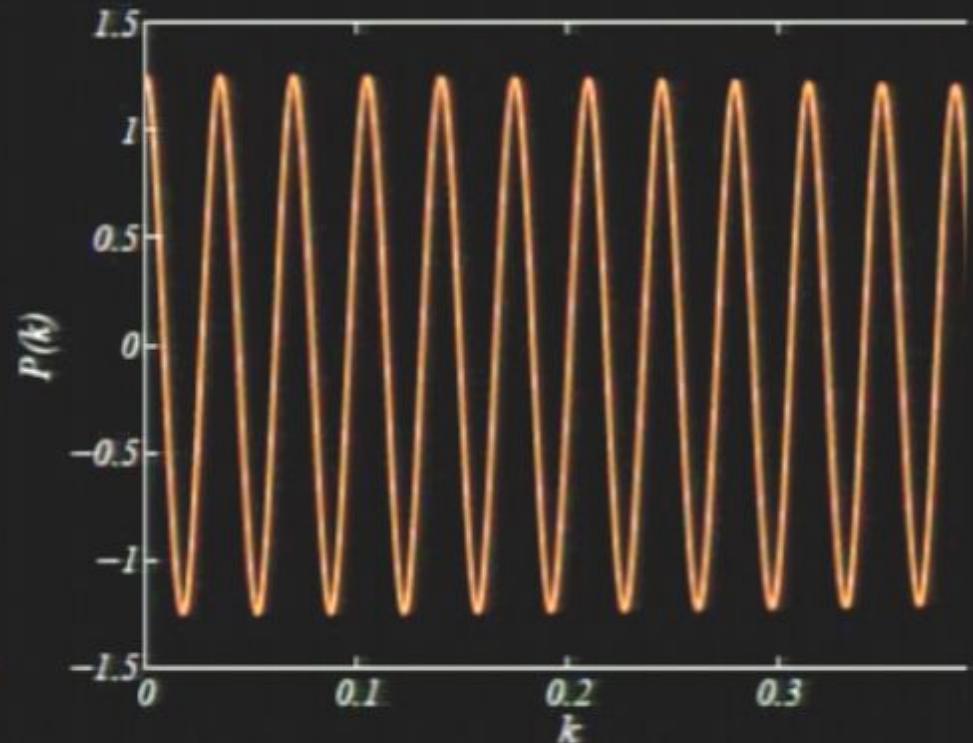
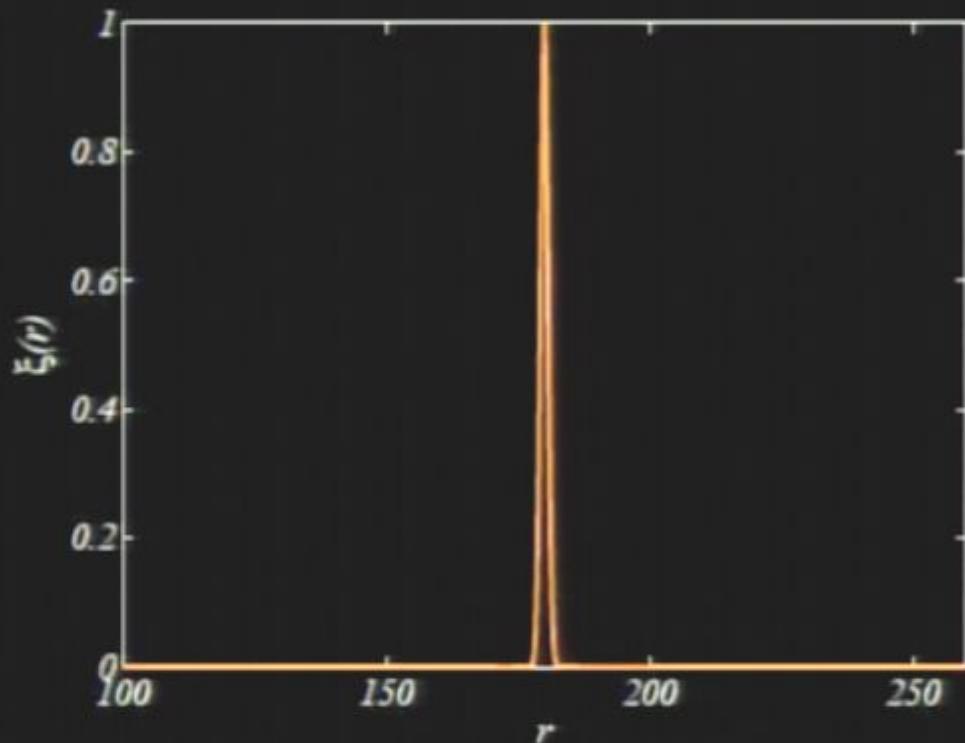
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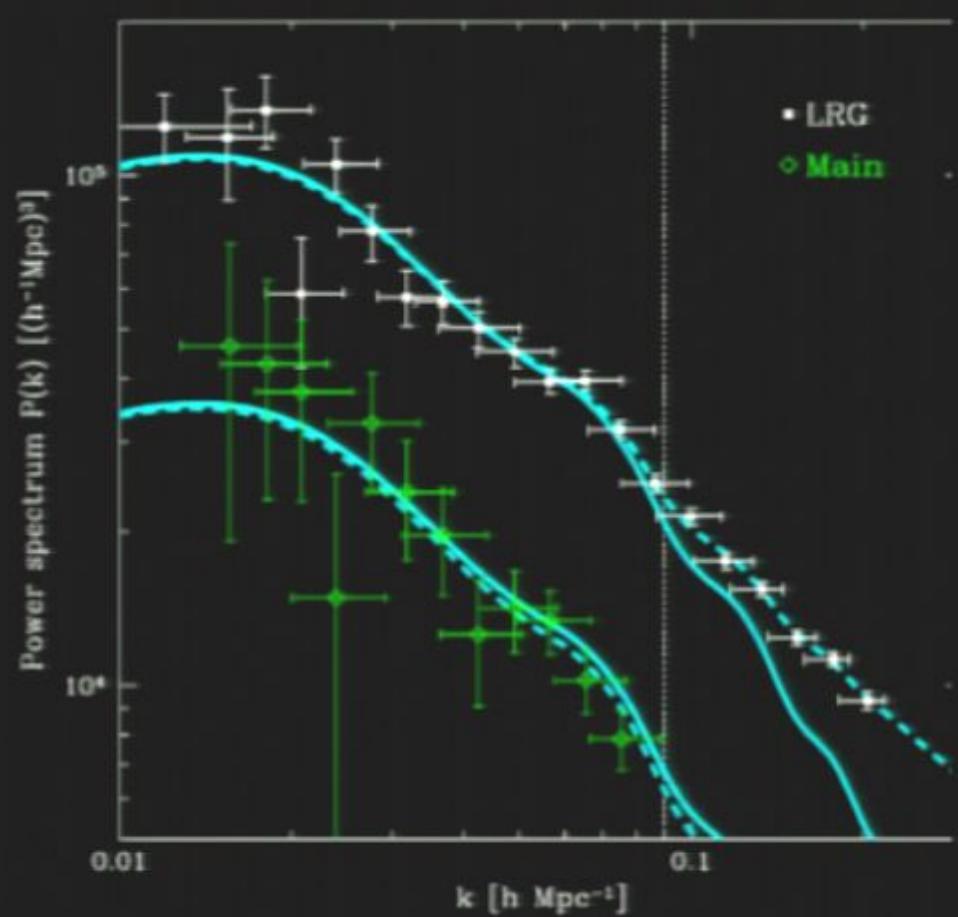
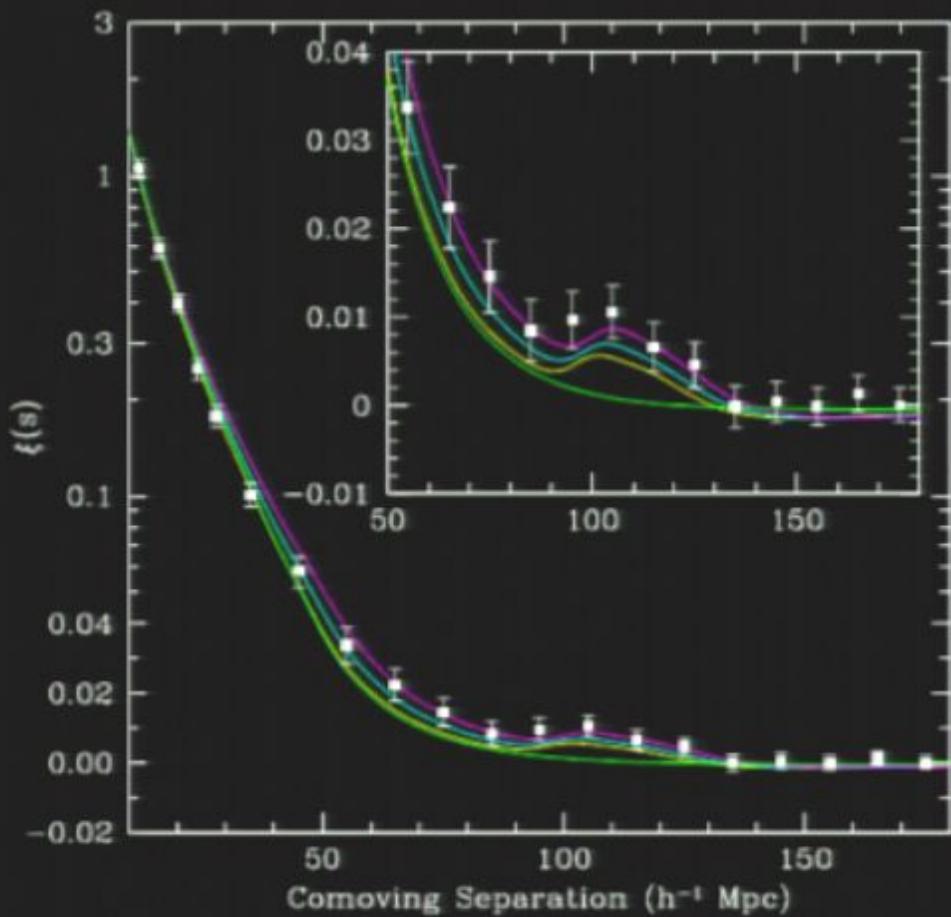
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$\xi(r)$



$P(k)$


 $\xi(r)$

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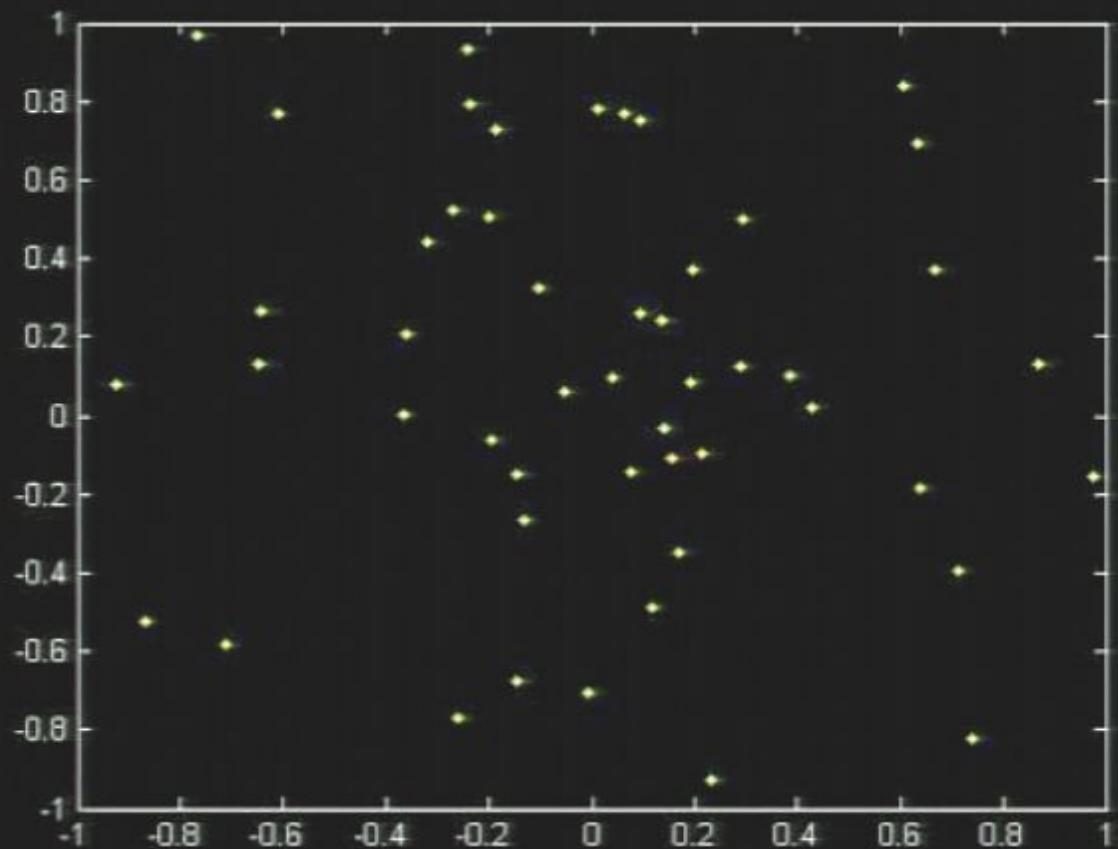
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Power Spectrum Errors

$$\frac{\delta P}{P} = \frac{1}{\sqrt{m}} \left(1 + \frac{1}{nP} \right)$$



Shot Noise



Fixed Volume

50 points

Power Spectrum Errors

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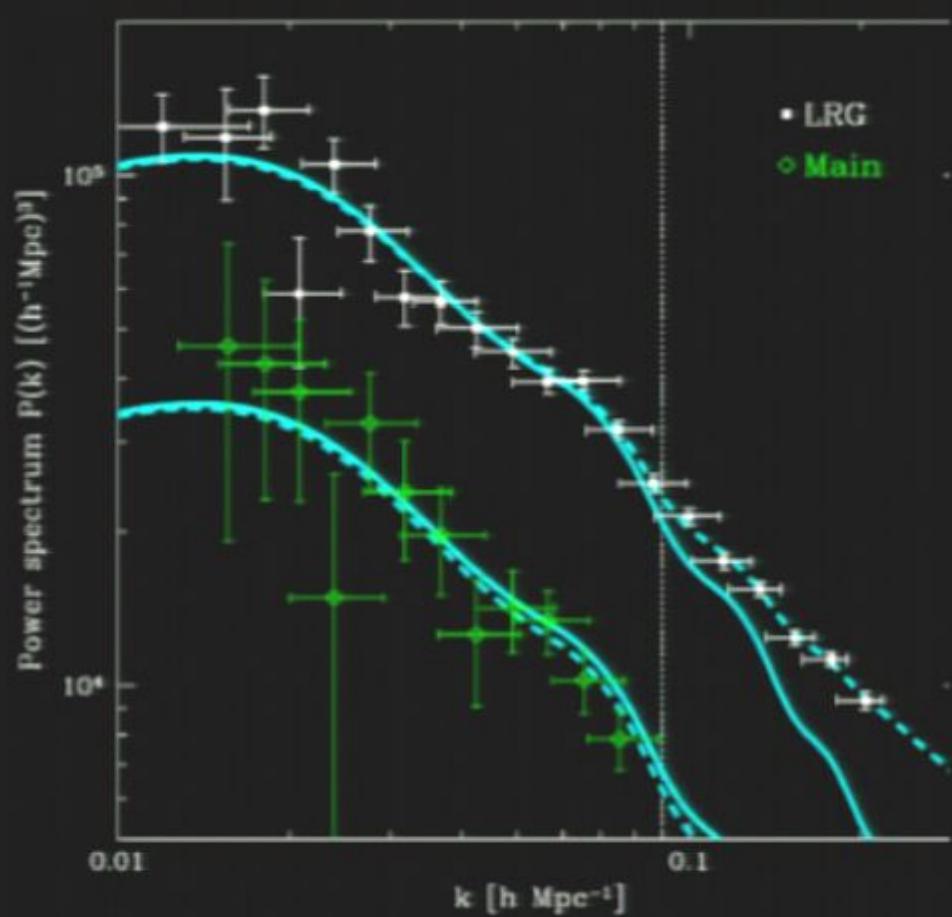
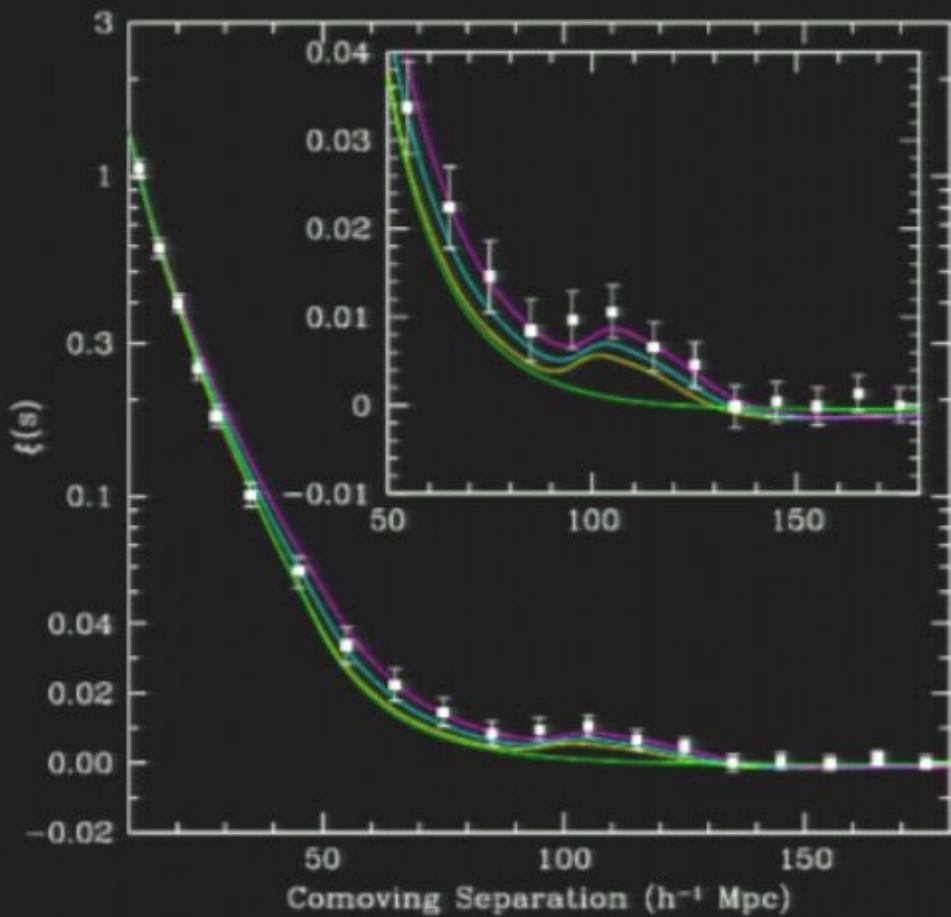

Cosmic Variance Shot Noise

m = number of Fourier modes measured in the survey

n = mean galaxy number density in the survey

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- Need lots of volume and large numbers of galaxies...so we can see the extra galaxy on average!



$$\xi(r)$$



$$P(k)$$

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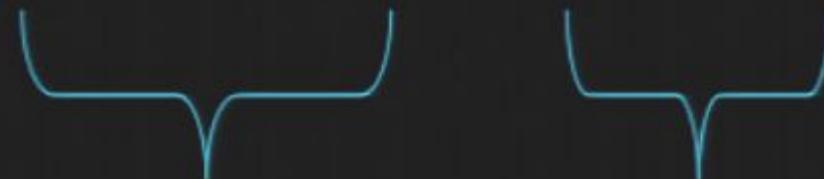
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Cosmic Variance Shot Noise

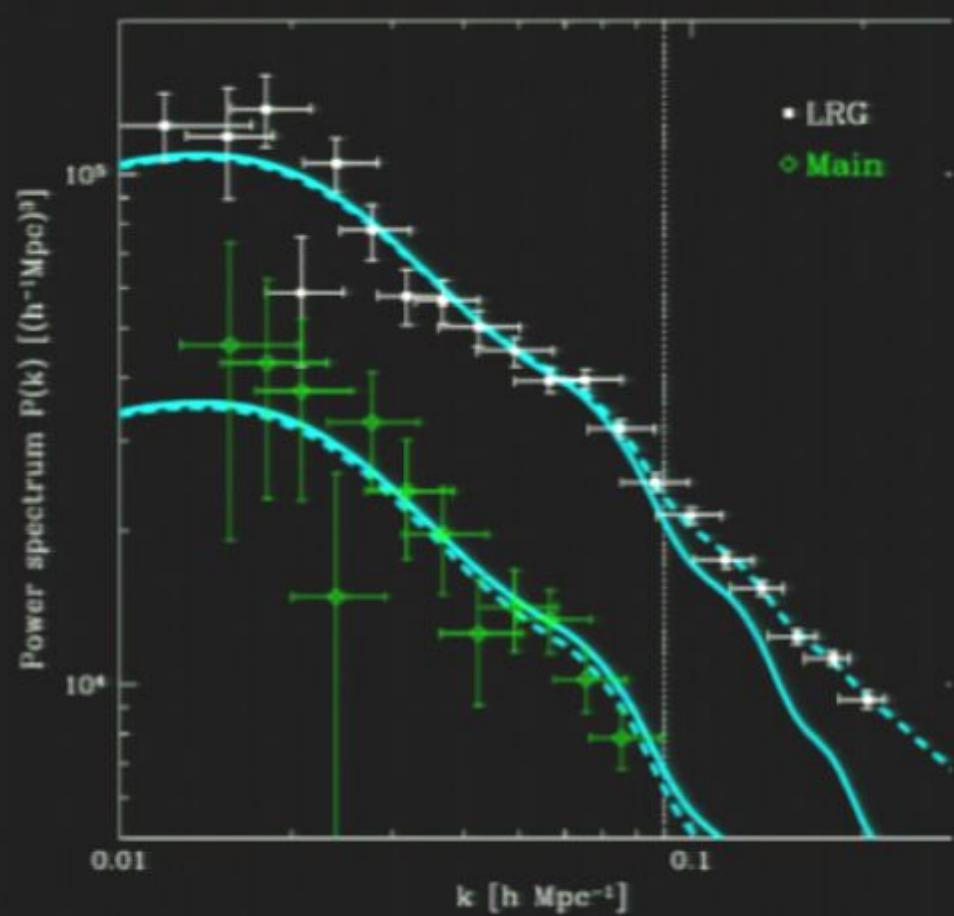
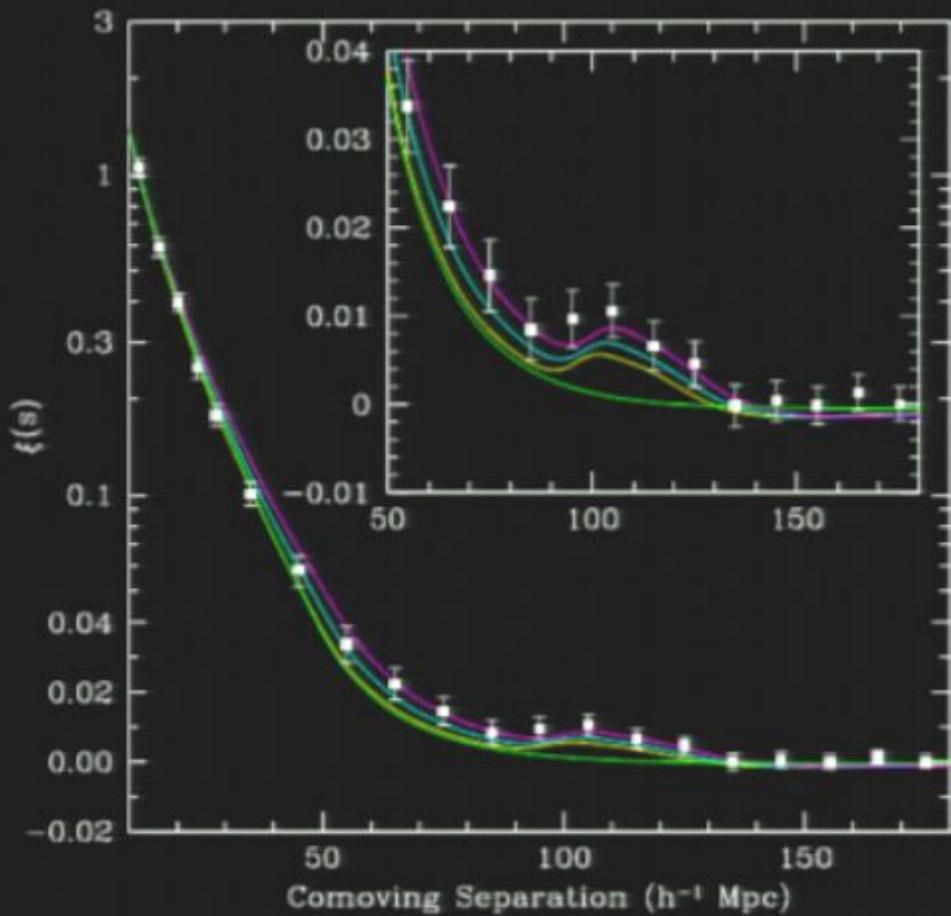
BAP Detection Is Hard!

- Consider a typical LRG. How many LRGs do we expect in a BAP shell around it?
- $n \sim 10^{-4} h^3 Mpc^{-3}$
- Volume = $20 Mpc \times 100^2 Mpc^2 \times 5 \sim 10^6 h^{-3} Mpc^3$
→ 100 LRGs from purely uniform distribution
- BAP in $\xi(r)$ gives ~1% excess probability
- So gives a *single extra LRG* on average.
- Need lots of volume and large numbers of galaxies...so we can see the extra galaxy on average!

BAP Detection Is Hard!

- Consider a typical LRG. How many LRGs do we expect in a BAP shell around it?
- $n \sim 10^{-4} h^3 Mpc^{-3}$

BAP Detection Is Hard!



$$\xi(r)$$



$$P(k)$$

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Power Spectrum Errors

$$\frac{\delta P}{P} = \frac{1}{\sqrt{m}} \left(1 + \frac{1}{nP} \right)$$


Cosmic Variance Shot Noise

m = number of Fourier modes measured in the survey

Power Spectrum Errors

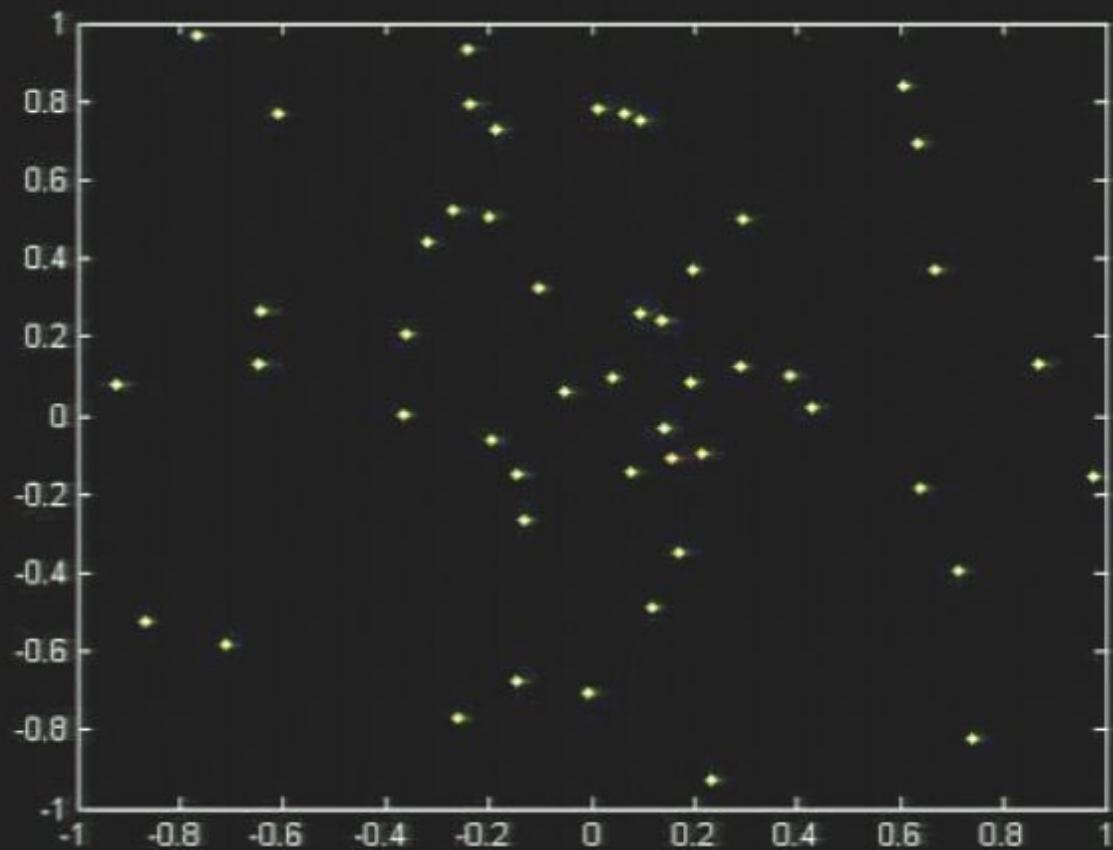
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Cosmic Variance Shot Noise

m = number of Fourier modes measured in the survey

n = mean galaxy number density in the survey

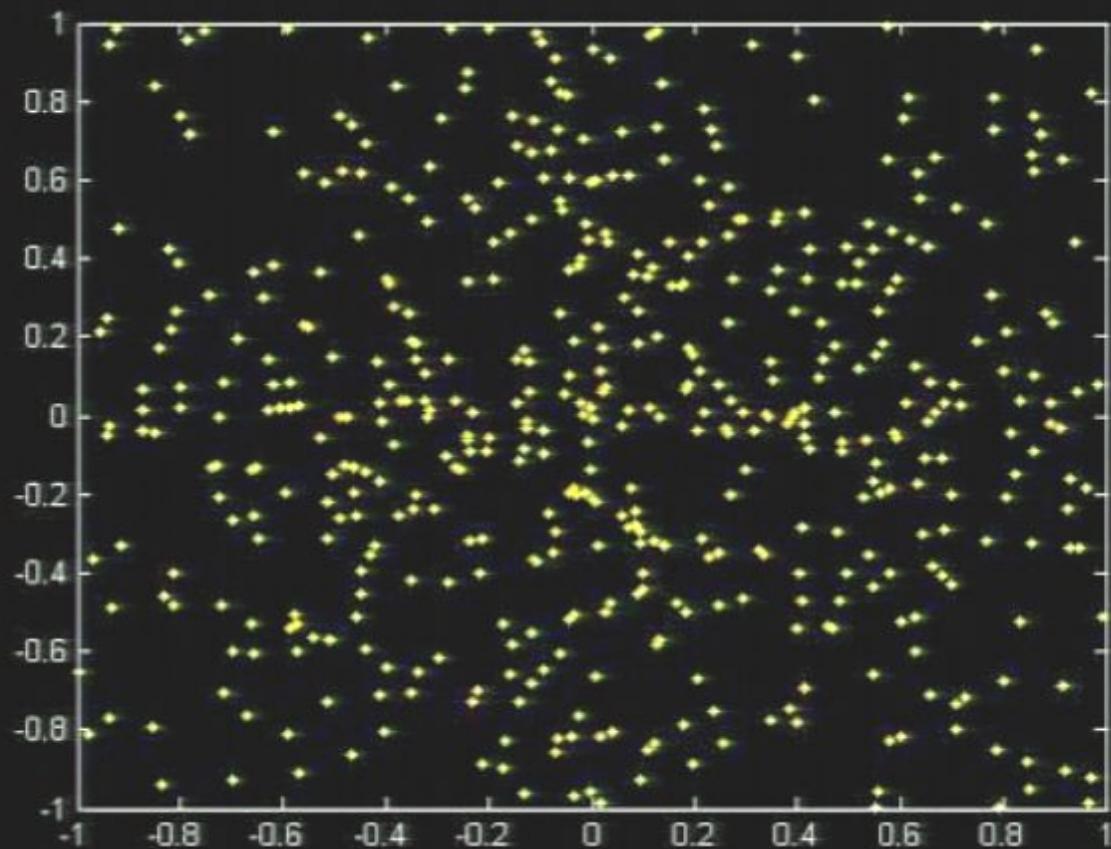
Shot Noise



Fixed Volume

50 points

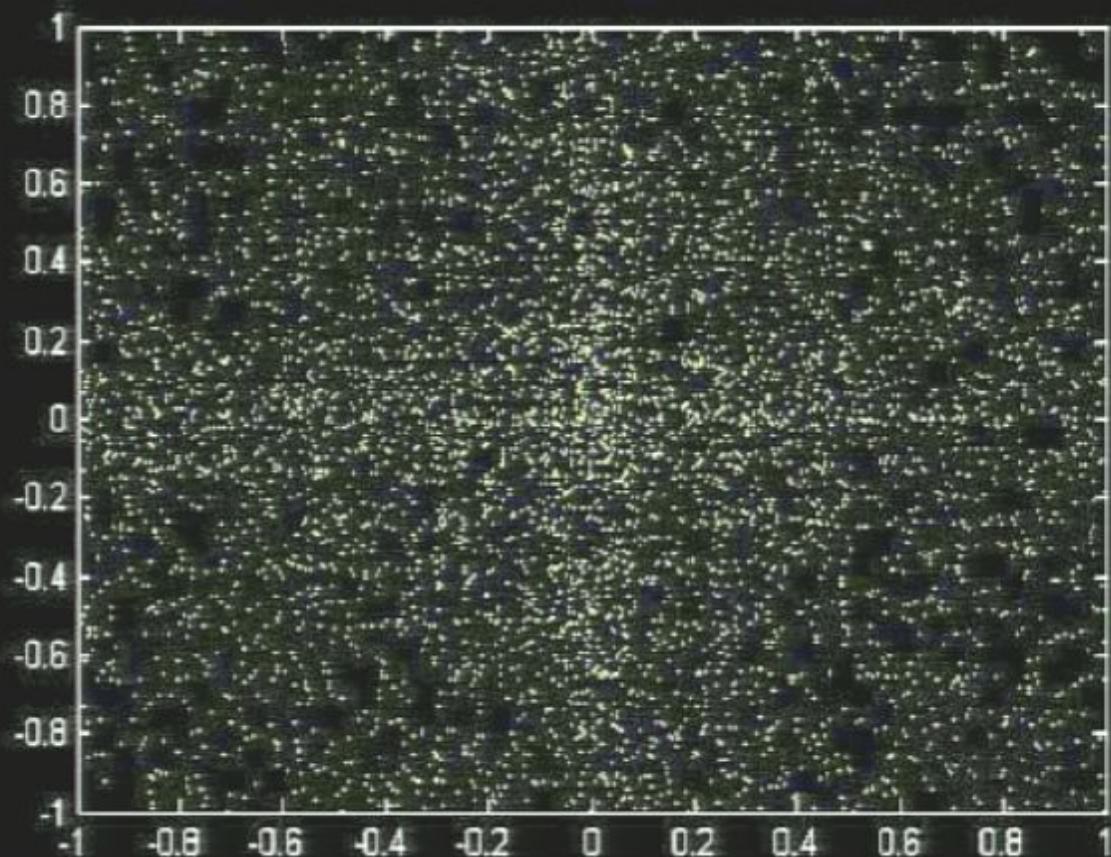
Shot Noise



Fixed Volume

500 points

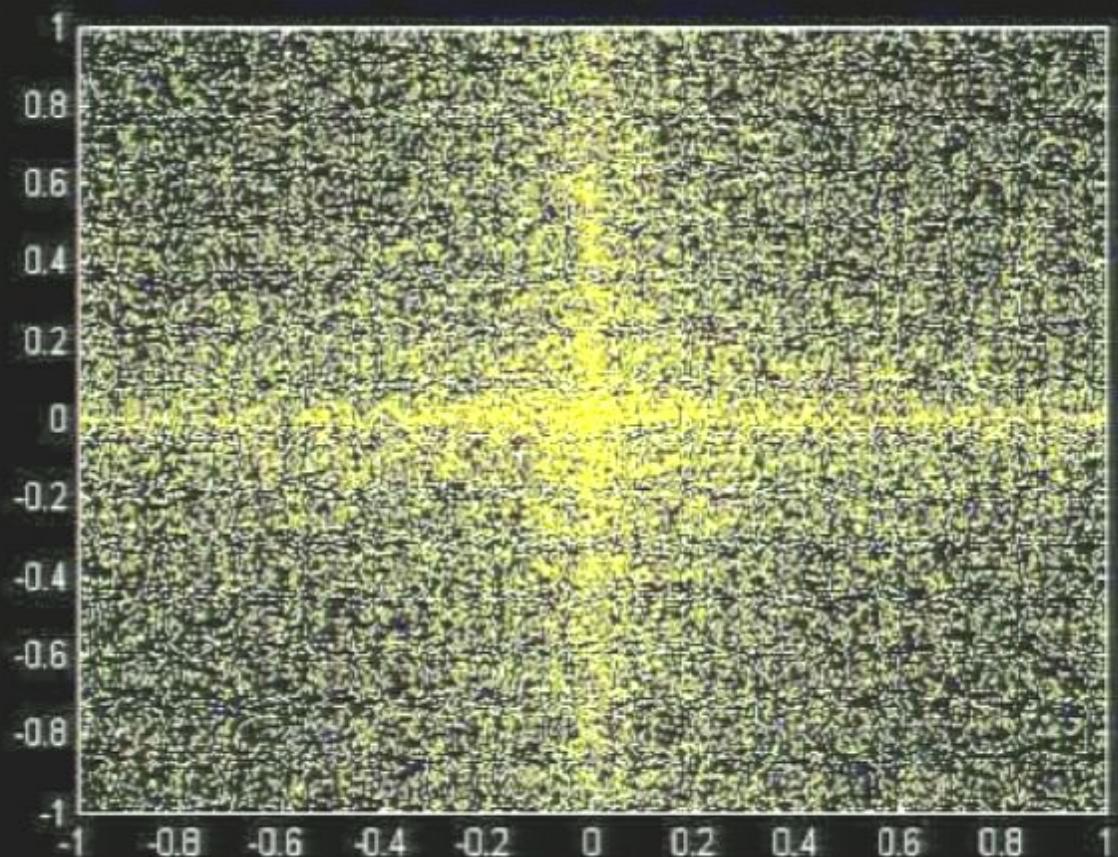
Shot Noise



Fixed Volume

5000 points

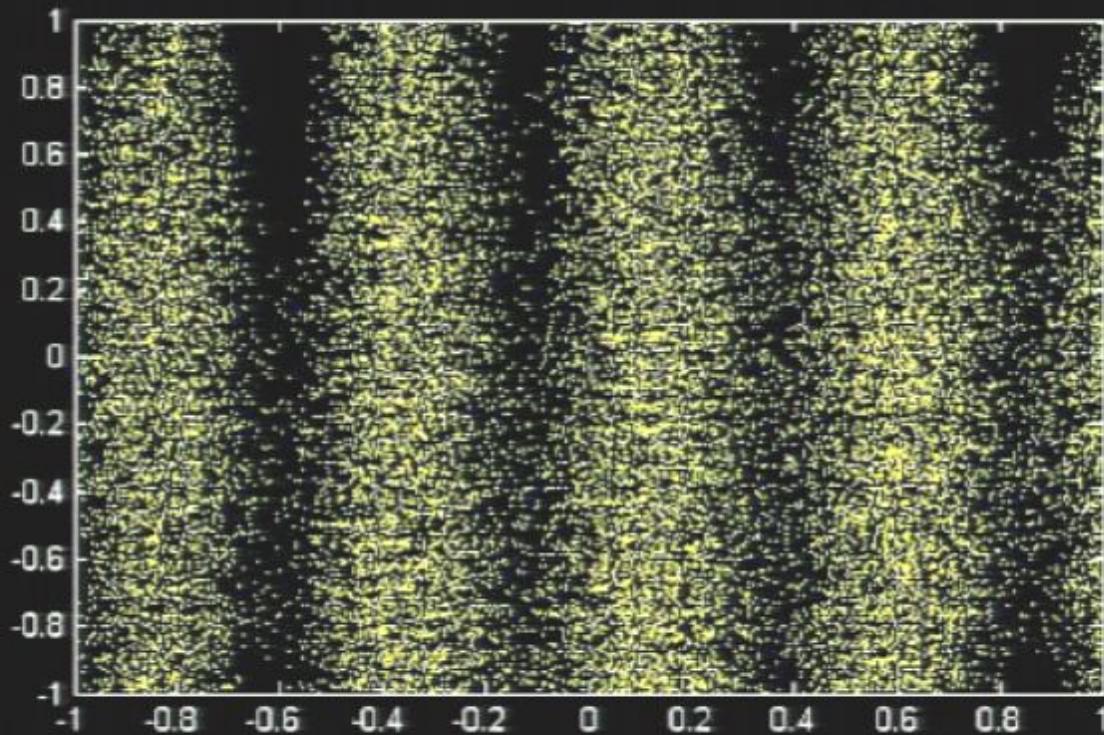
Shot Noise



Fixed Volume

50k points

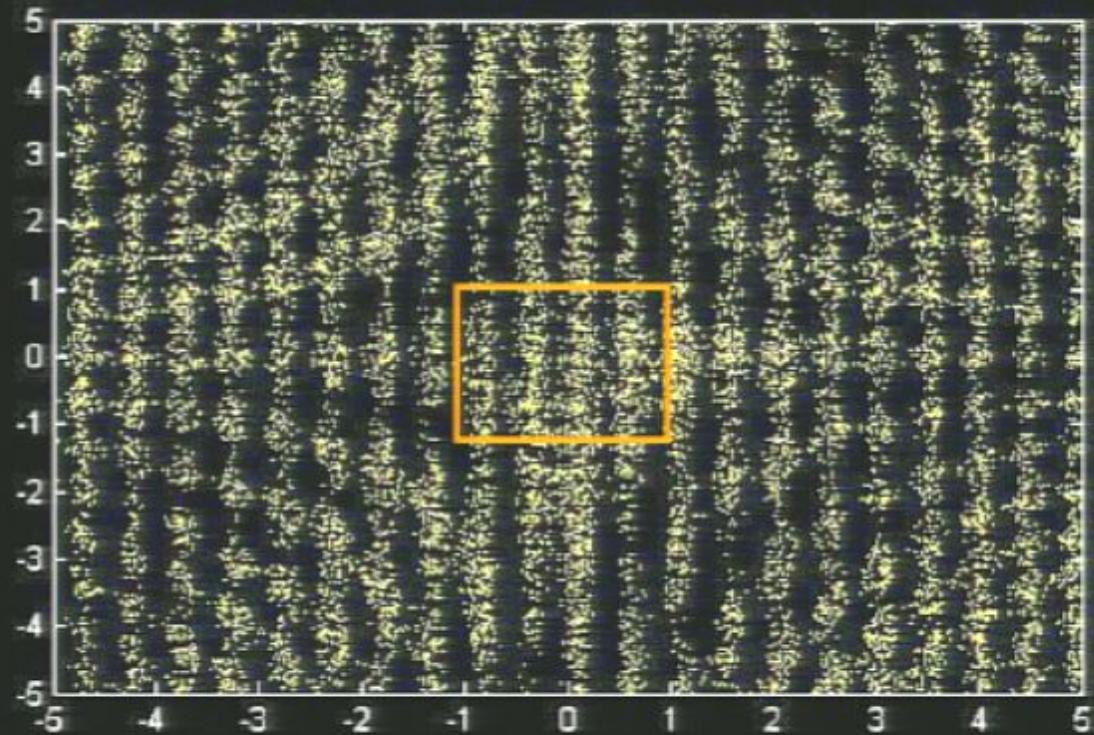
Cosmic Variance



1 x Volume

Fixed 50k points

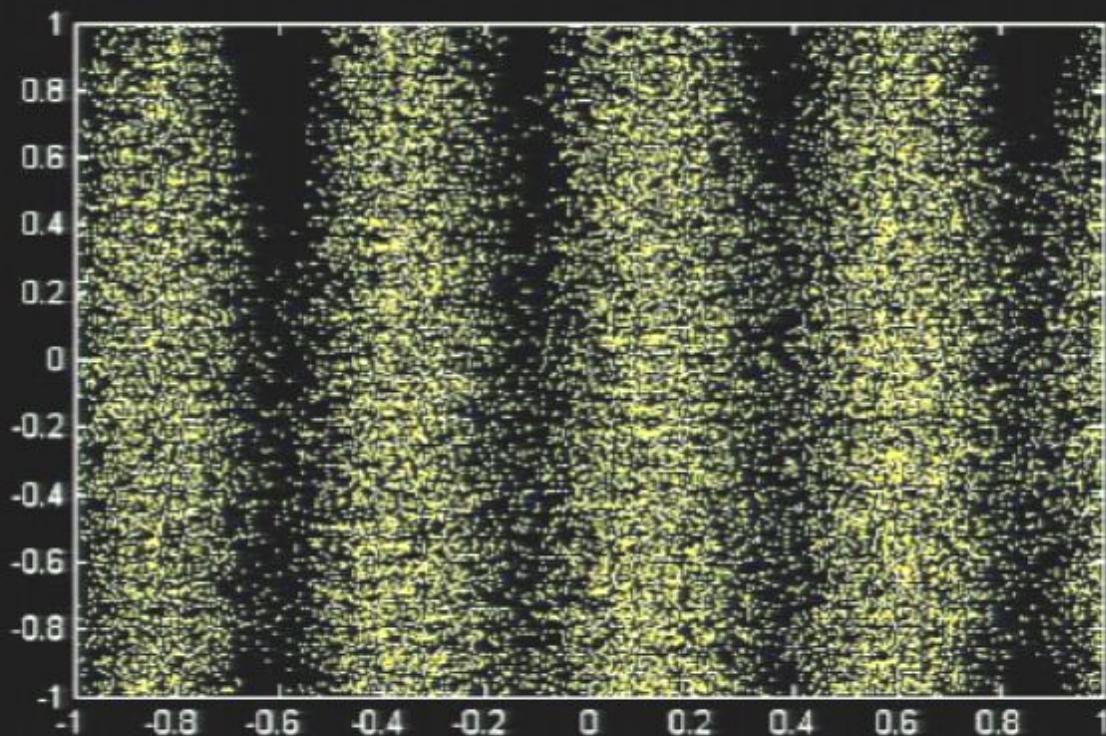
Cosmic Variance



25 x Volume

Fixed 50k points

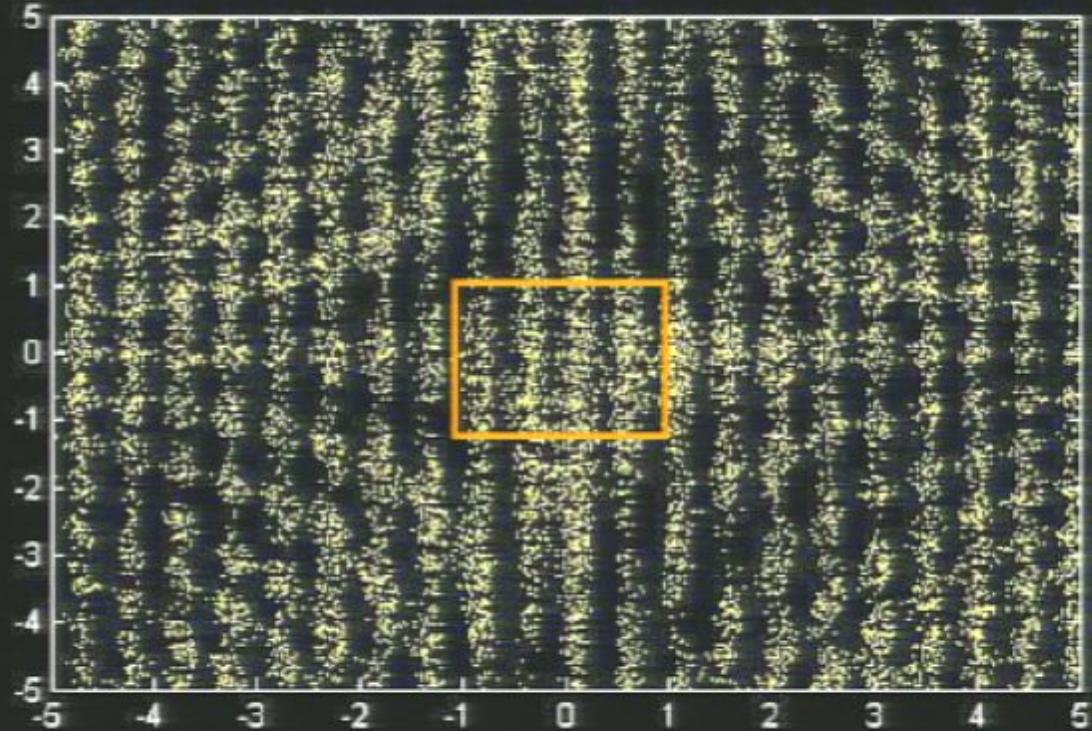
Cosmic Variance



1 x Volume

Fixed 50k points

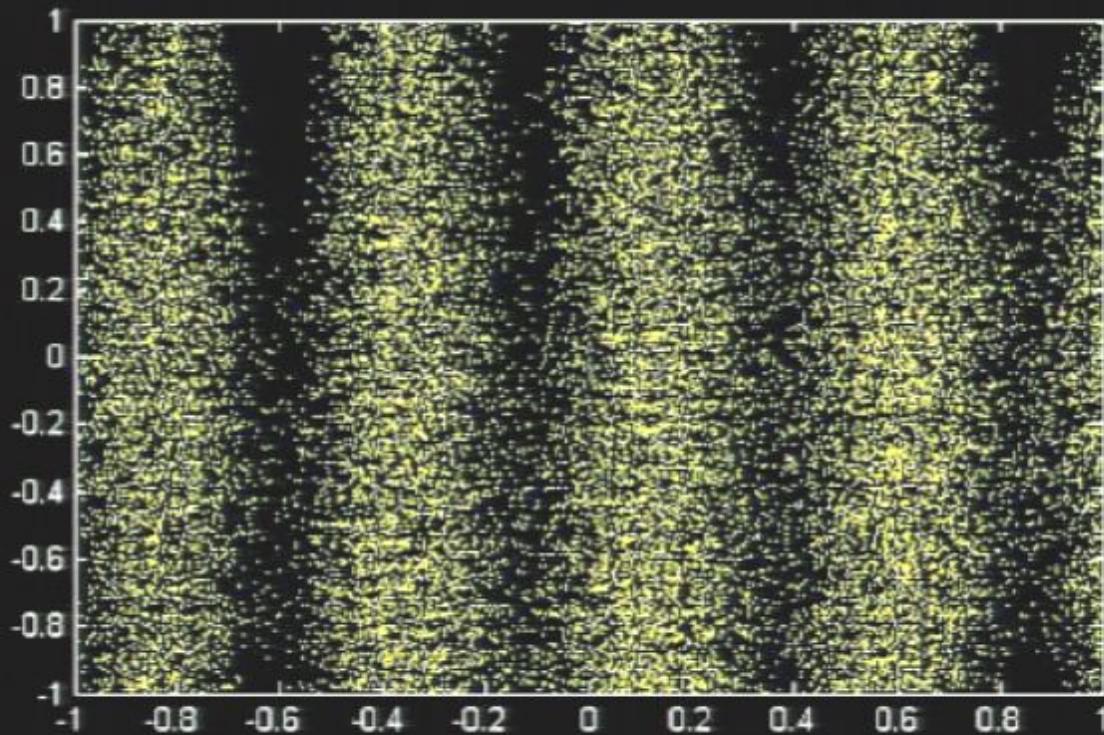
Cosmic Variance



25 x Volume

Fixed 50k points

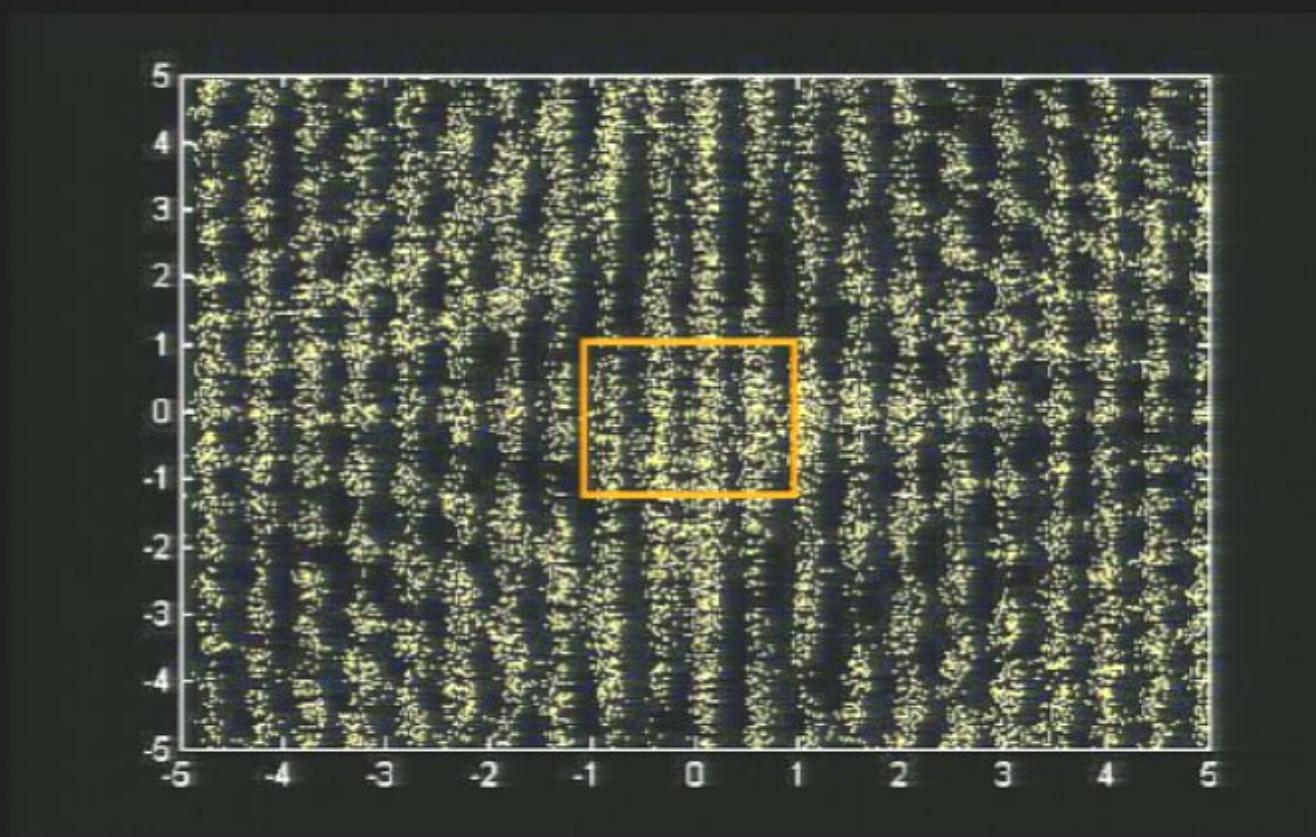
Cosmic Variance



1 x Volume

Fixed 50k points

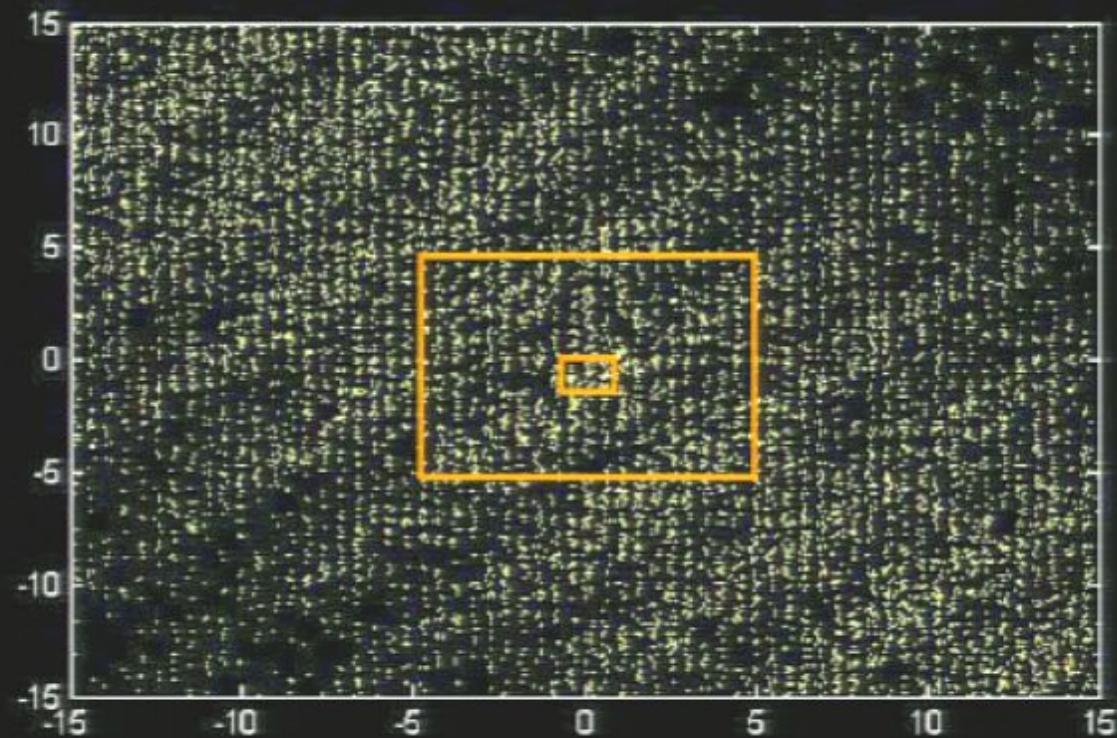
Cosmic Variance



25 x Volume

Fixed 50k points

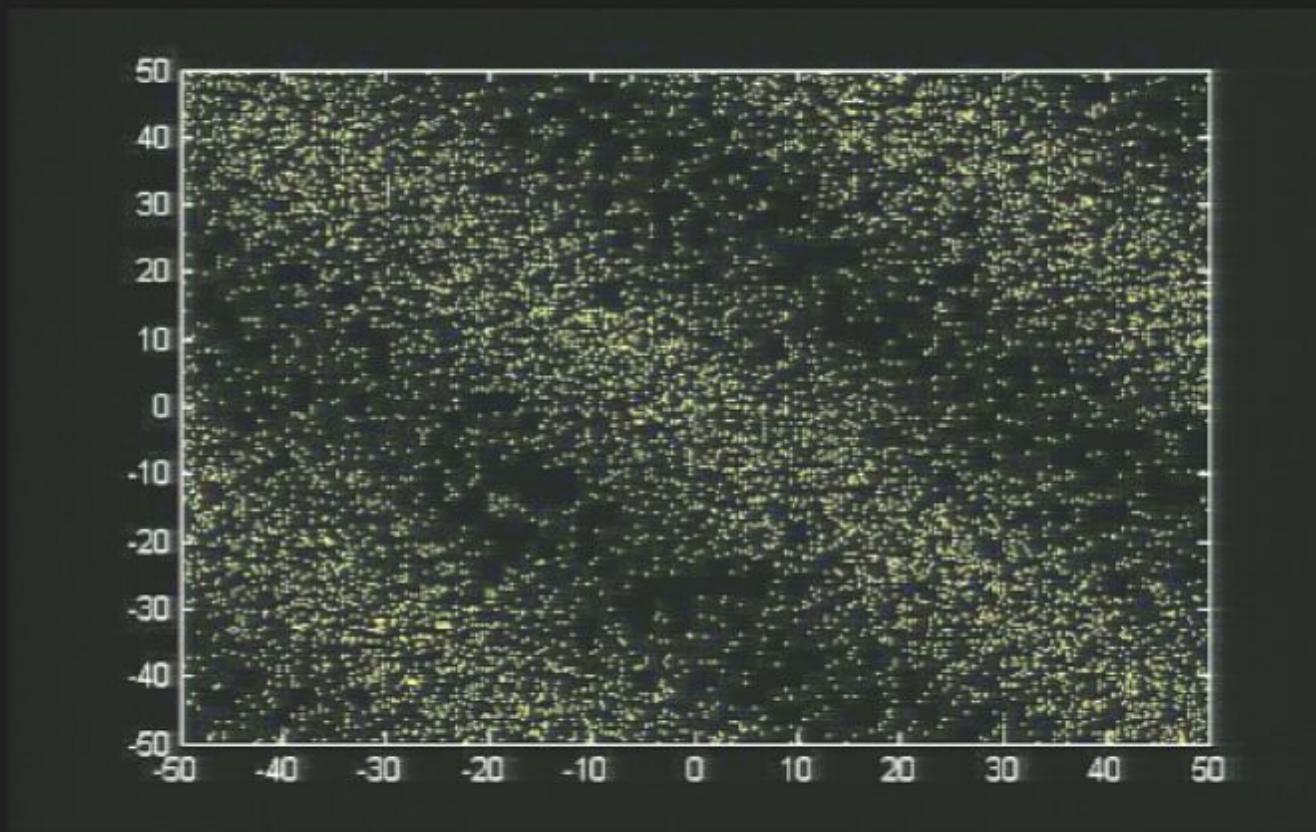
Cosmic Variance



225 x Volume

Fixed 50k points

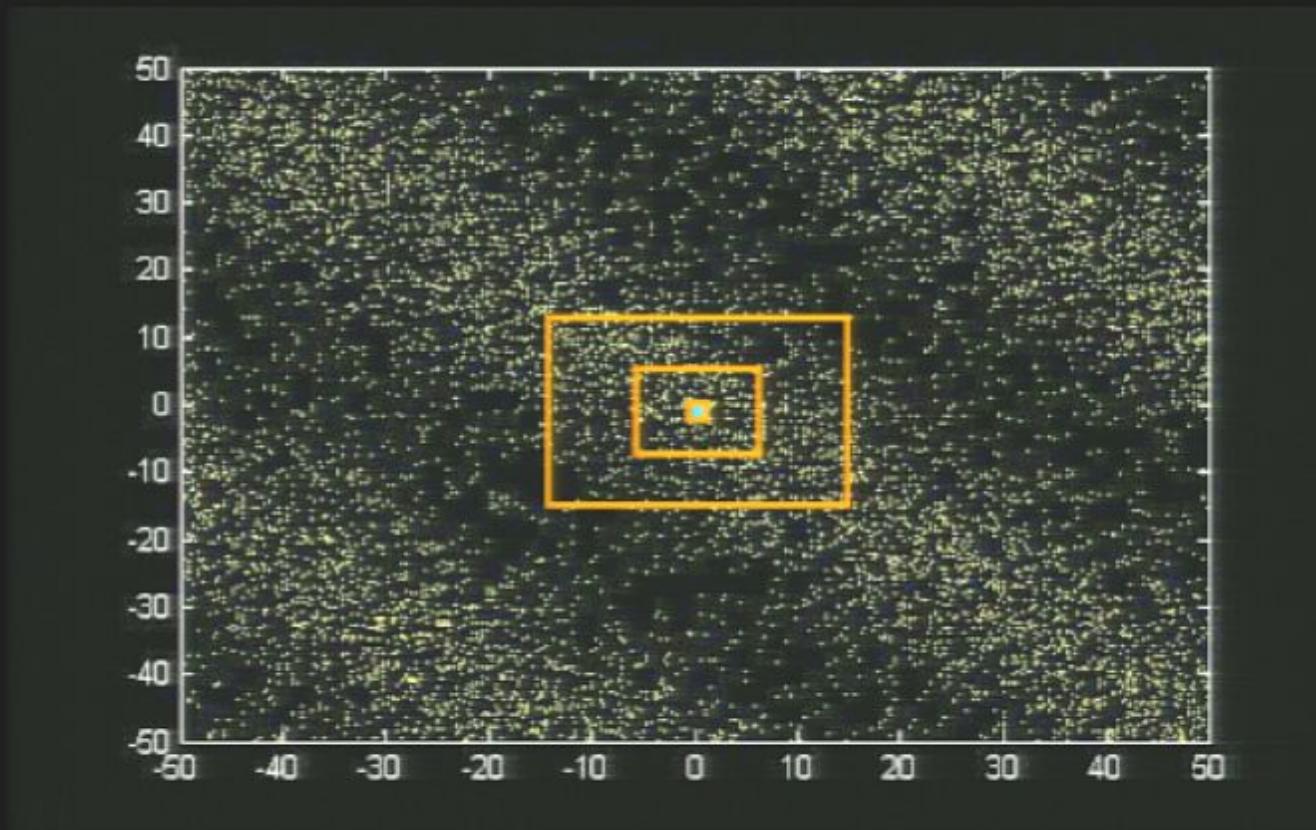
Cosmic Variance



2200 x Volume

Fixed 50k points

Cosmic Variance

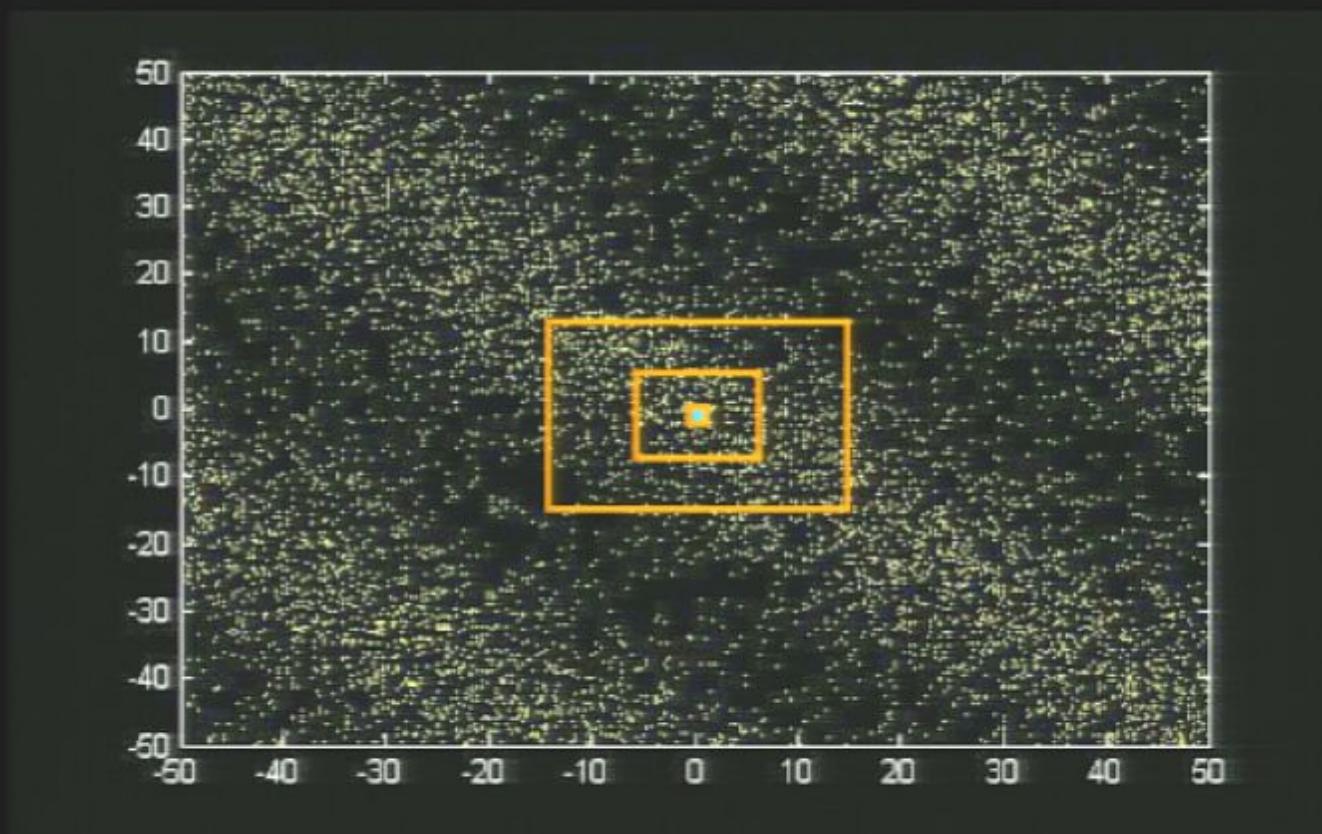


2200 x Volume Fixed 50k points

Optimal Survey Design

- What is the optimal sampling of a page of text?
- Depends what information you want.
- E.g. what language it is written in...
- E.g. what page layout is being used...
- Trade-off between the two...
- $nP \sim 1\text{-}5$ is optimal

Cosmic Variance



2200 x Volume

Fixed 50k points

Optimal Survey Design

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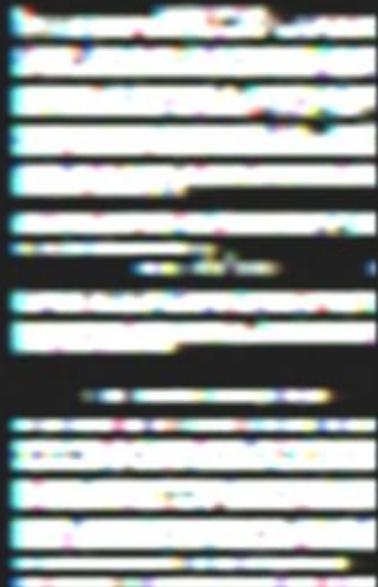
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r of point
r of target
, leading t

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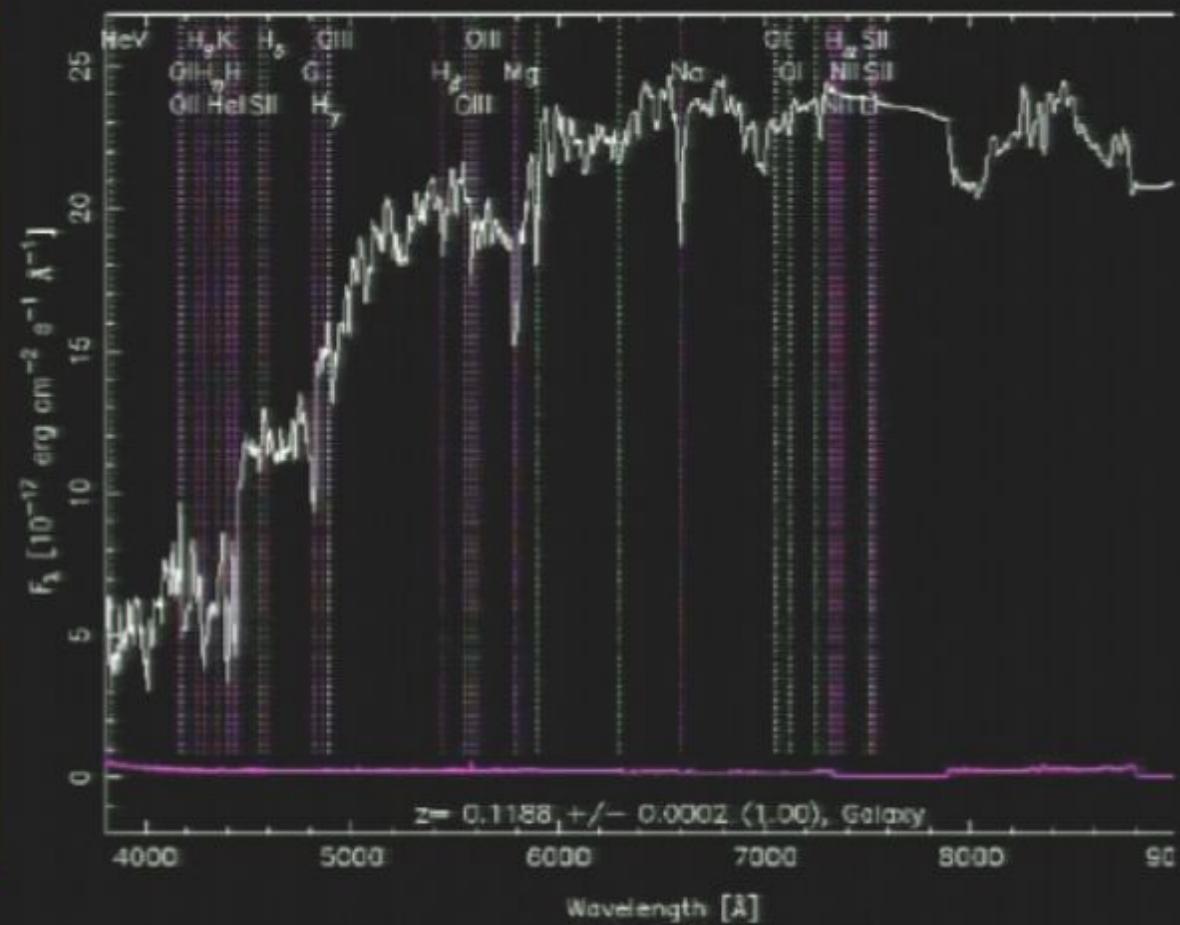
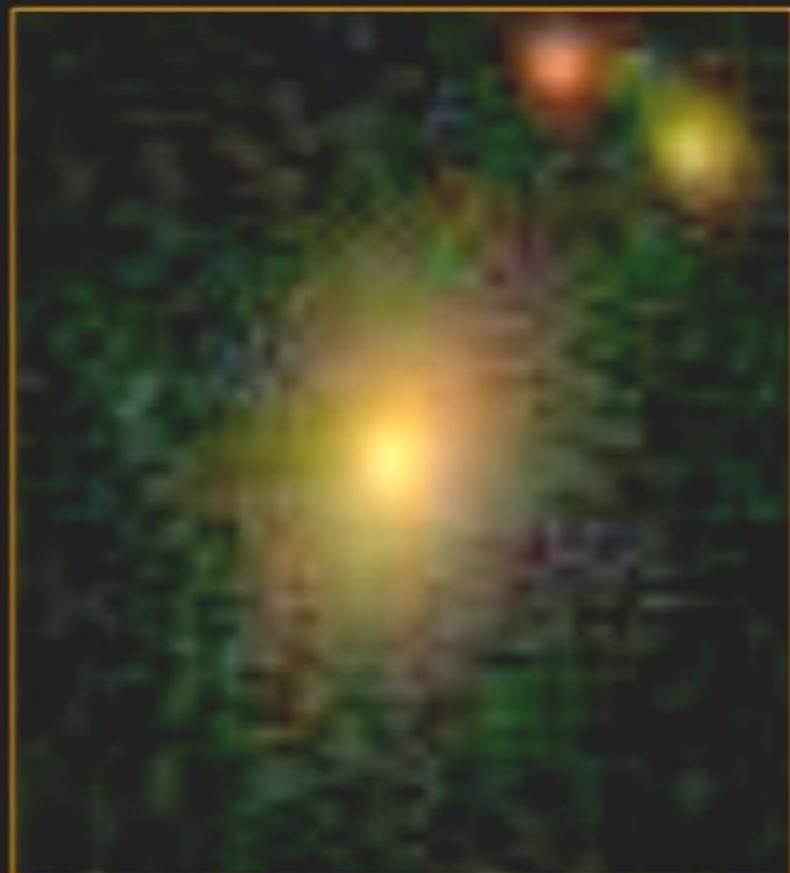


BAO Targets

What targets should one use for measuring the BAO? Options are:

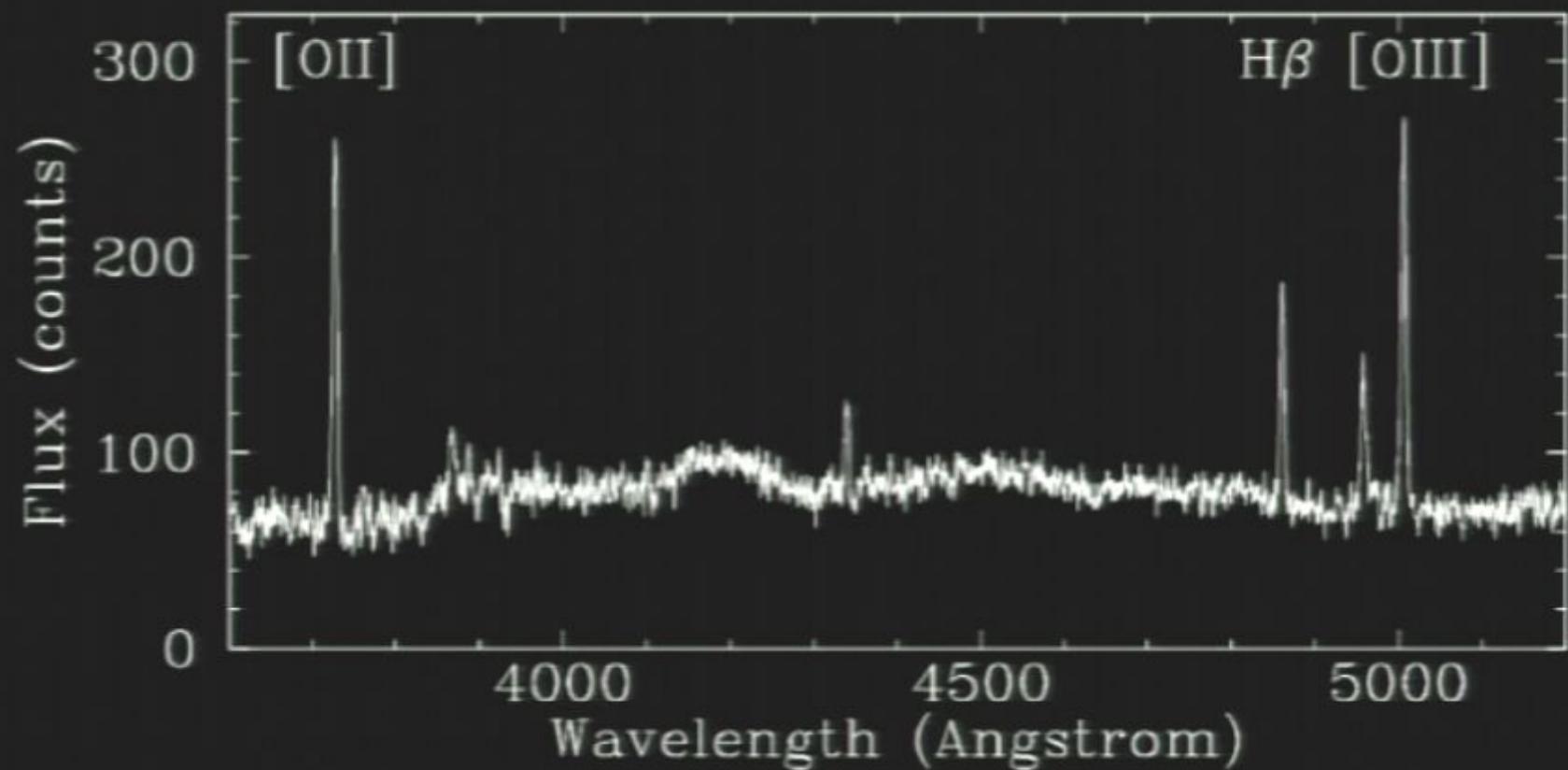
- Luminous Red Galaxies (LRGs)
- Star-forming galaxies (blue)
- Neutral Hydrogen (HI)
- Lyman alpha forest

LRGs



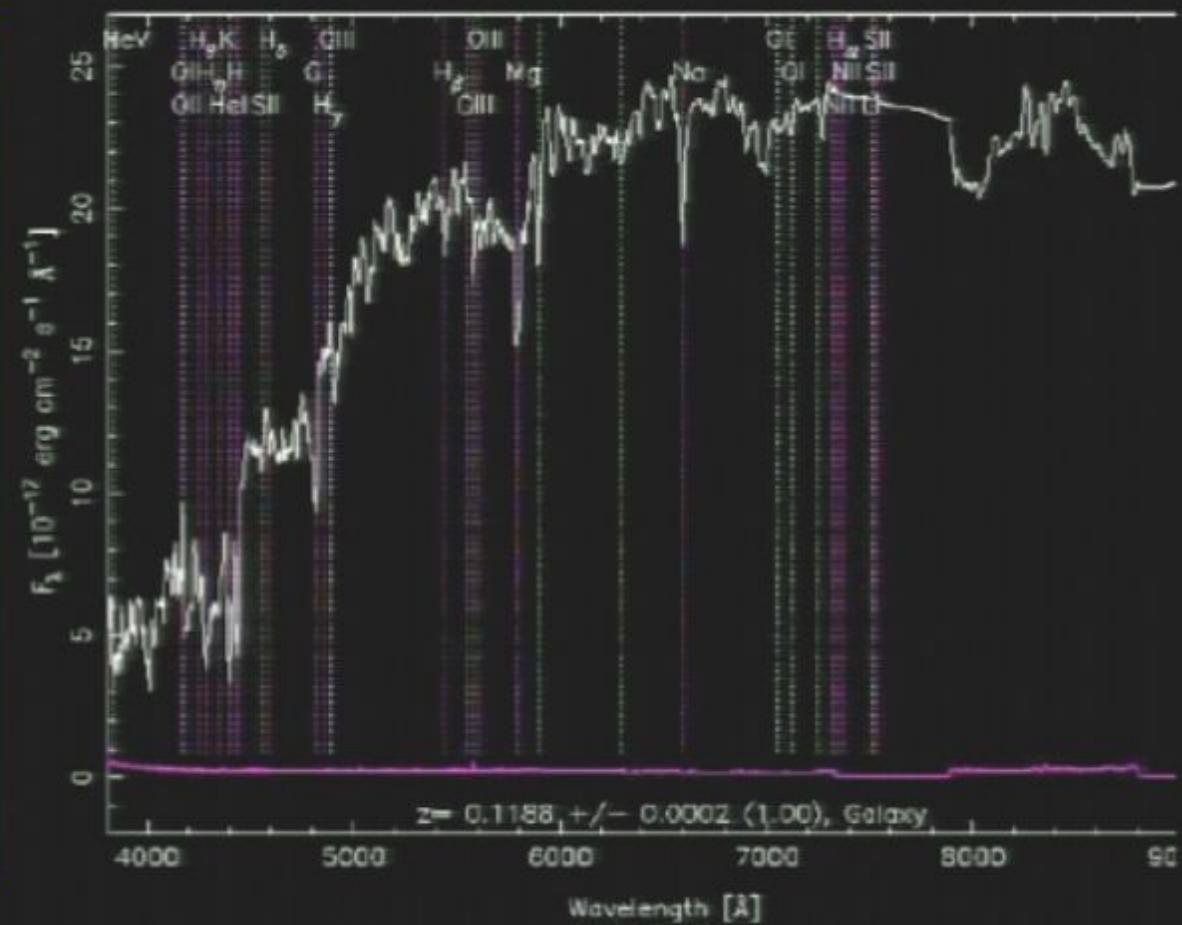
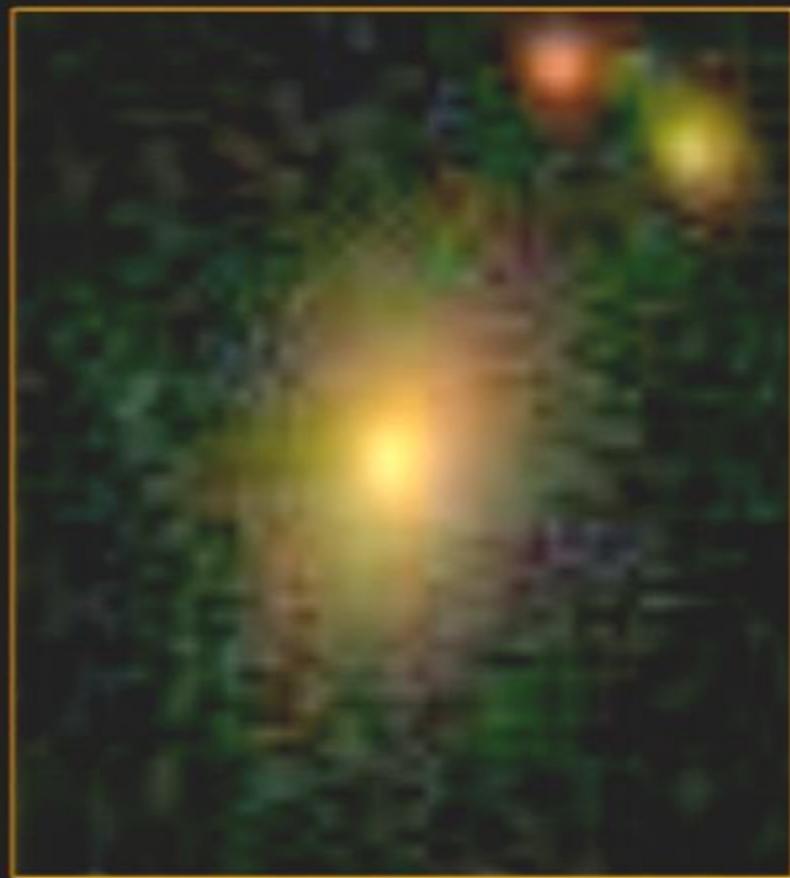
- Used by SDSS, BOSS and LAMOST

Blue, star-forming galaxies



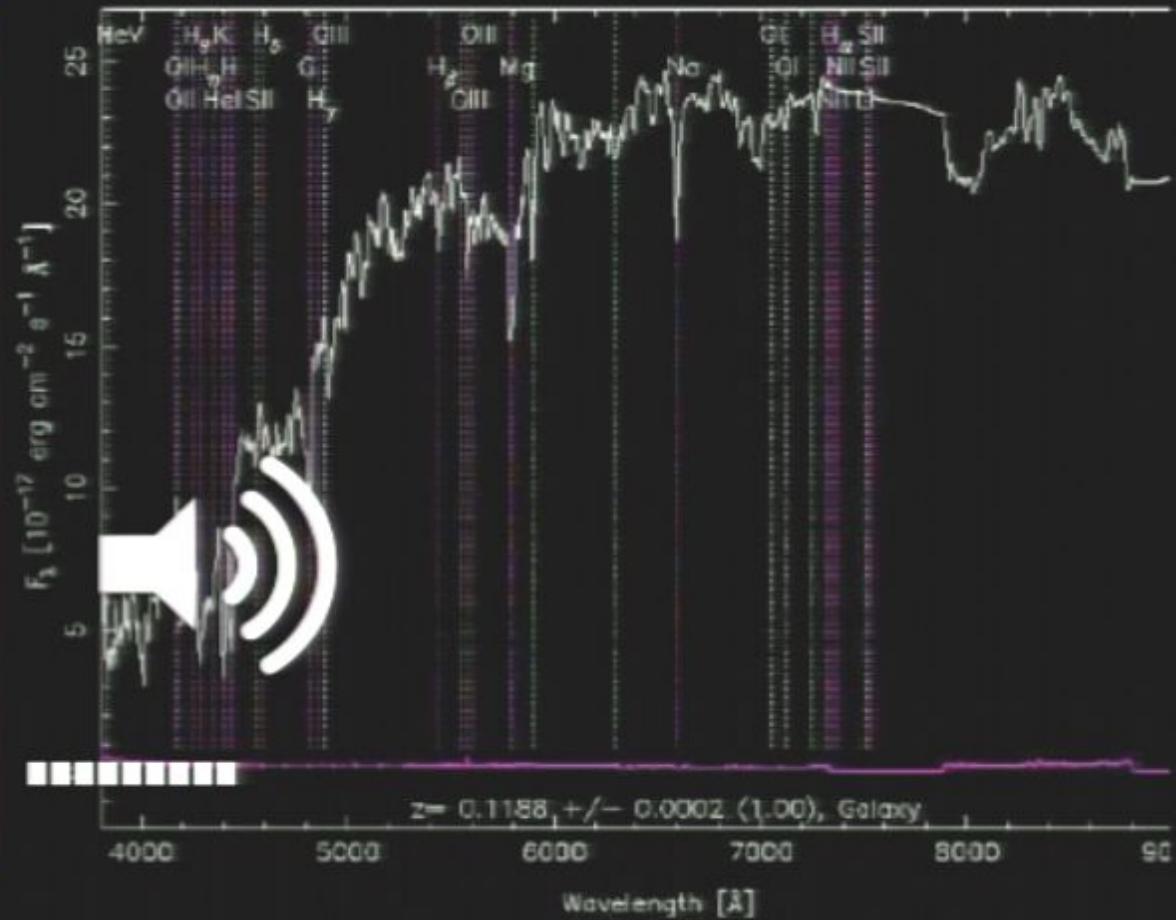
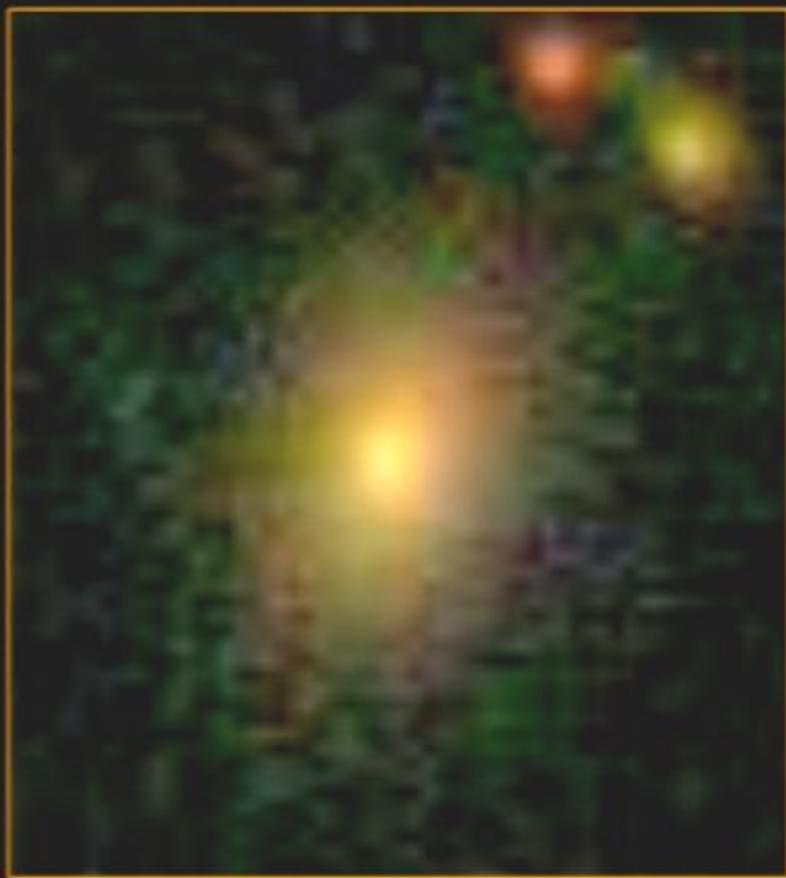
- Used by WiggleZ, preferred for 8m class

LRGs



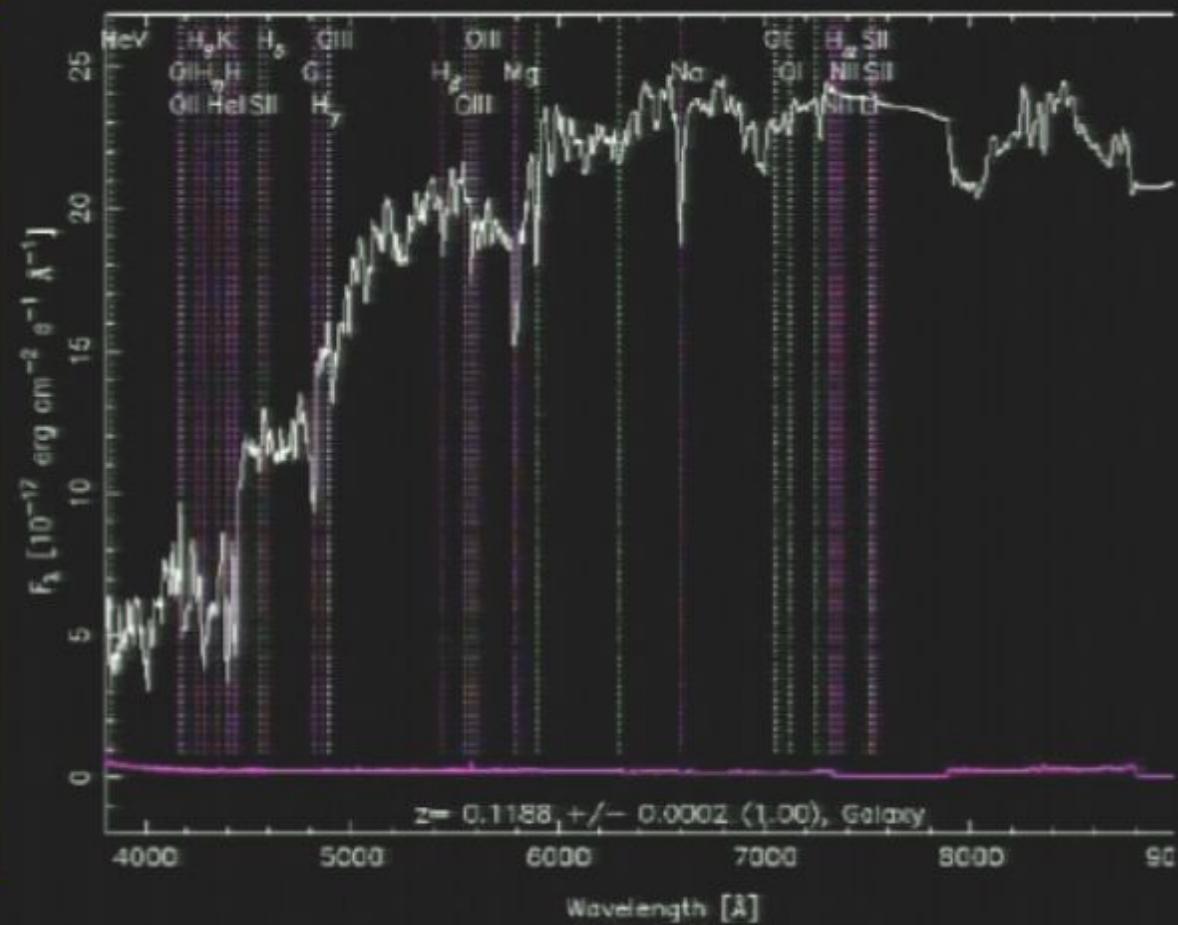
- Used by SDSS, BOSS and LAMOST

LRGs



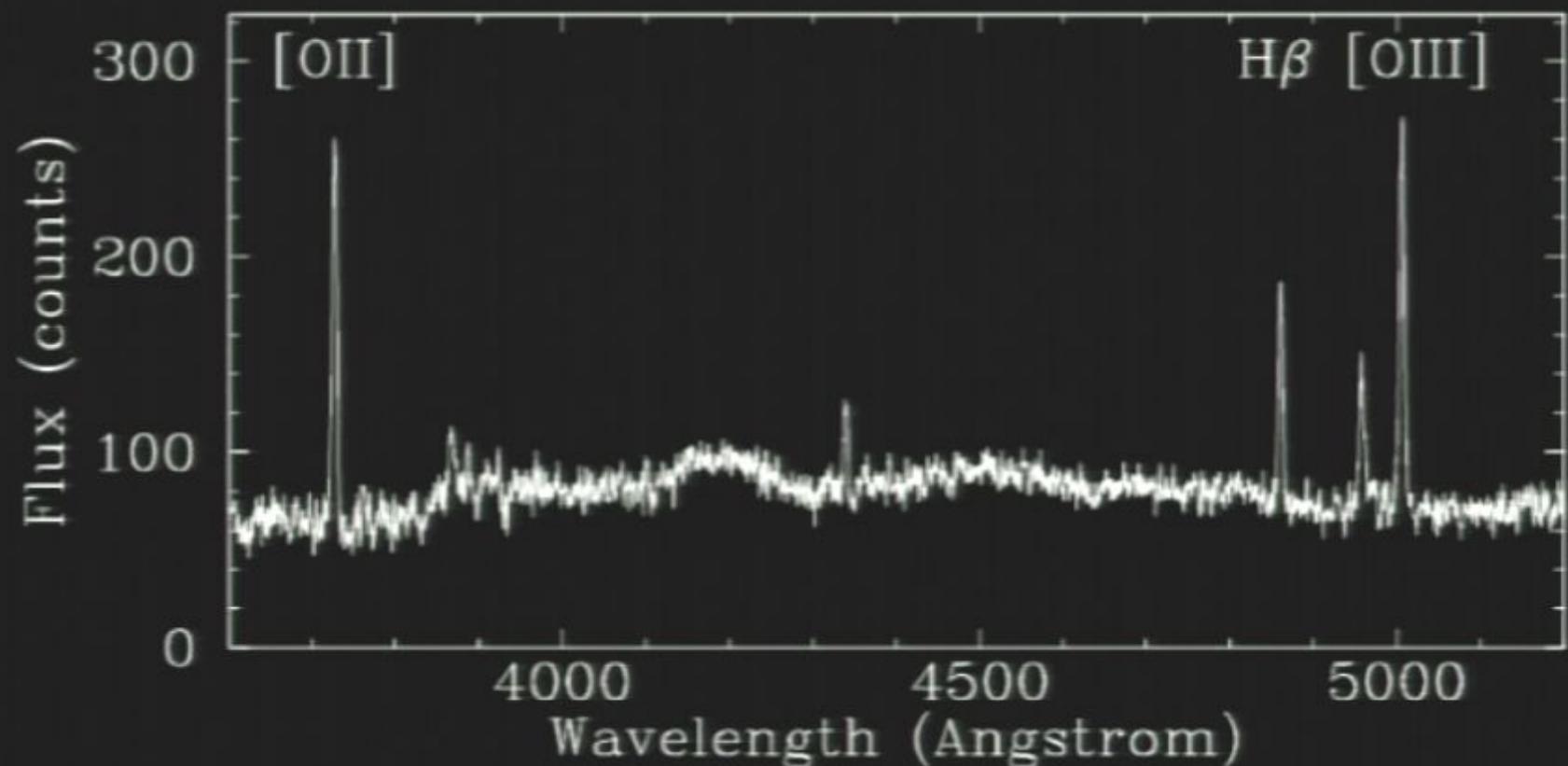
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LRGs



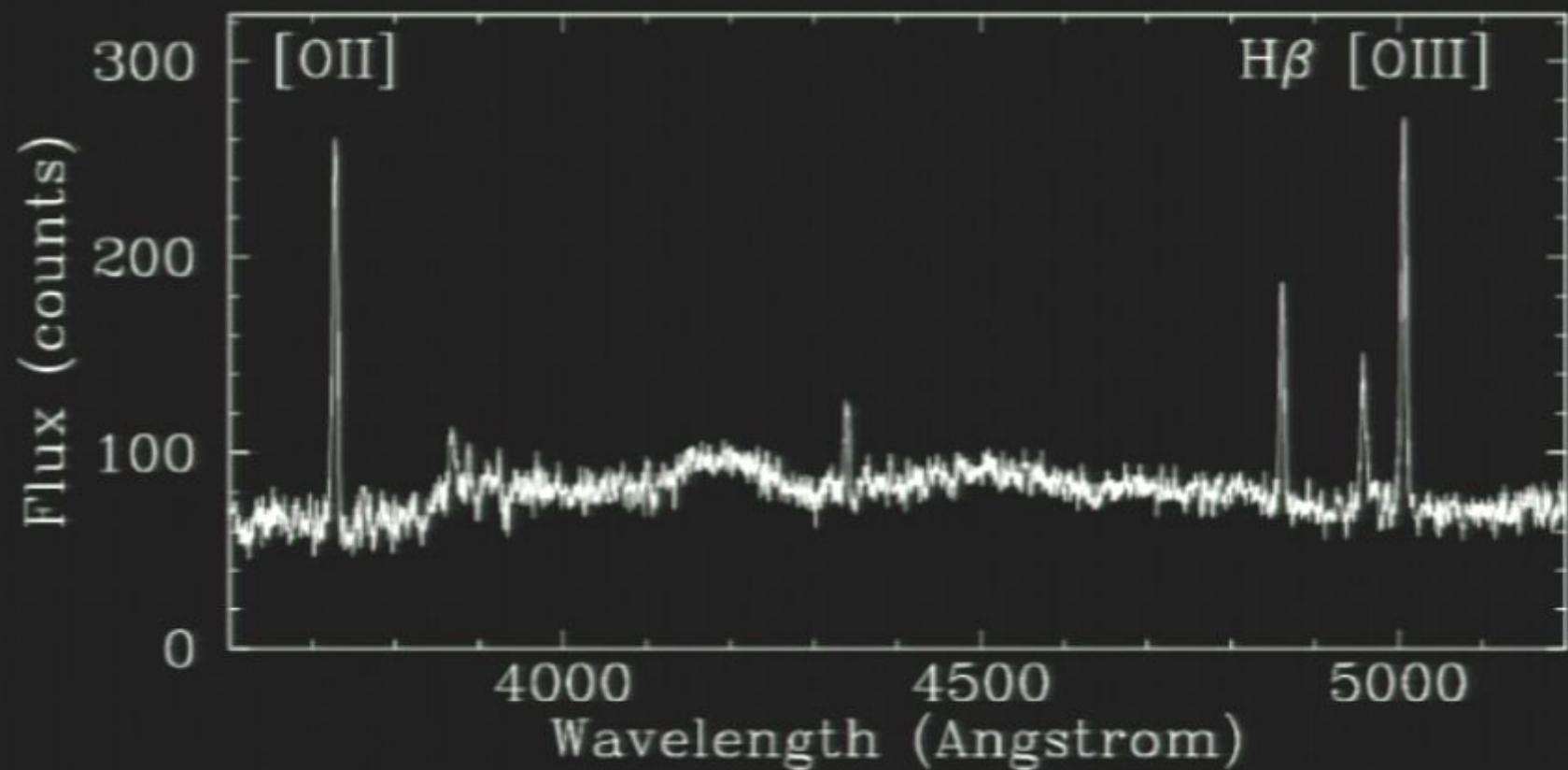
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Blue, star-forming galaxies



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Blue, star-forming galaxies



- Used by WiggleZ, preferred for 8m class

Neutral Hydrogen (HI) and Lyman Alpha Forest

Neutral Hydrogen (HI) and Lyman Alpha Forest

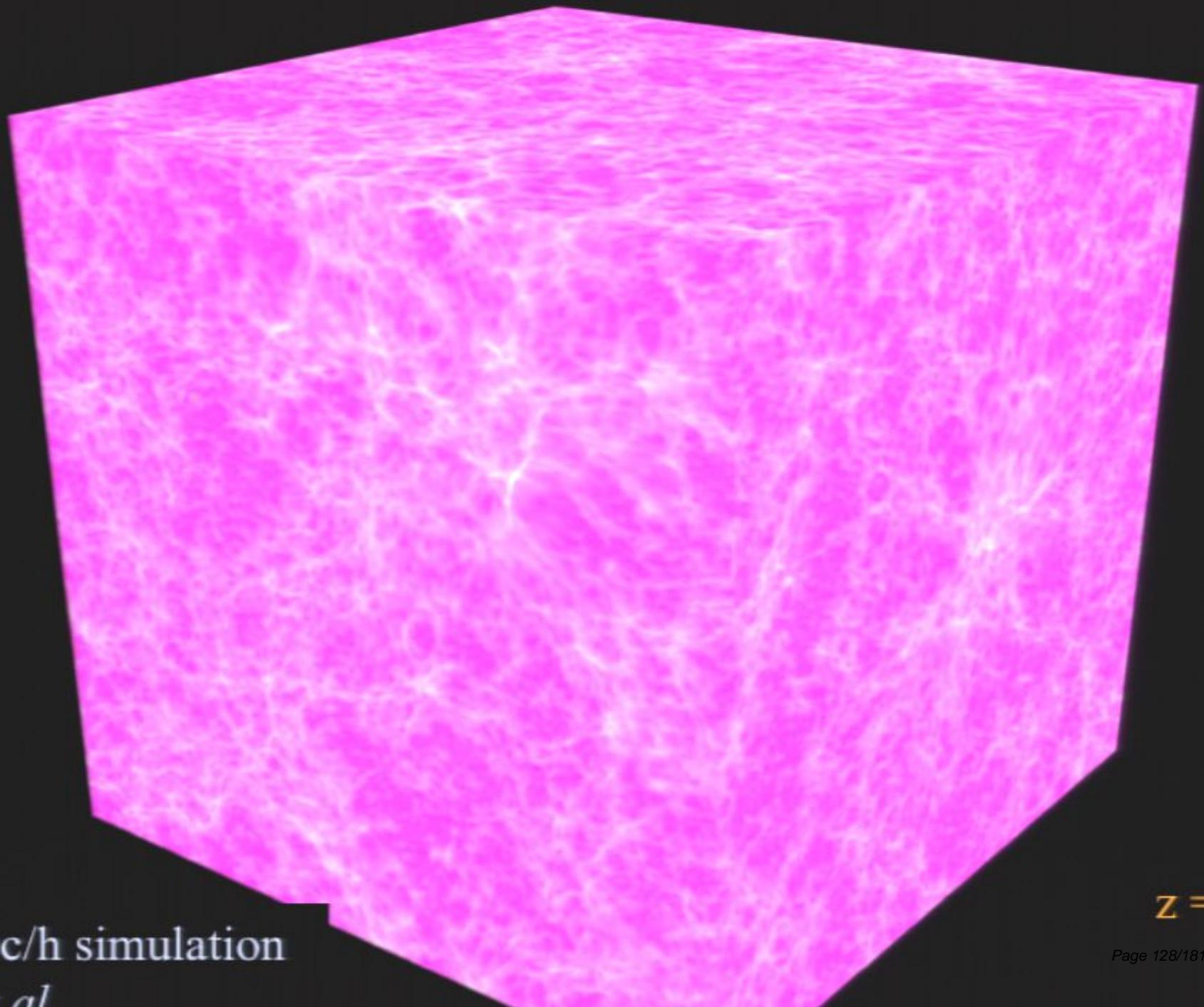
- Neutral hydrogen emits at 21cm (1.6 GHz) through the spin-flip transition. Potentially works for z up to \sim 100.

Neutral Hydrogen (HI) and Lyman Alpha Forest

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- Neutral hydrogen absorbs at the Lyman Alpha frequency ($\sim 126\text{nm}$). Works in the optical for $2 < z < 6$.

Neutral Hydrogen (HI) and Lyman Alpha Forest

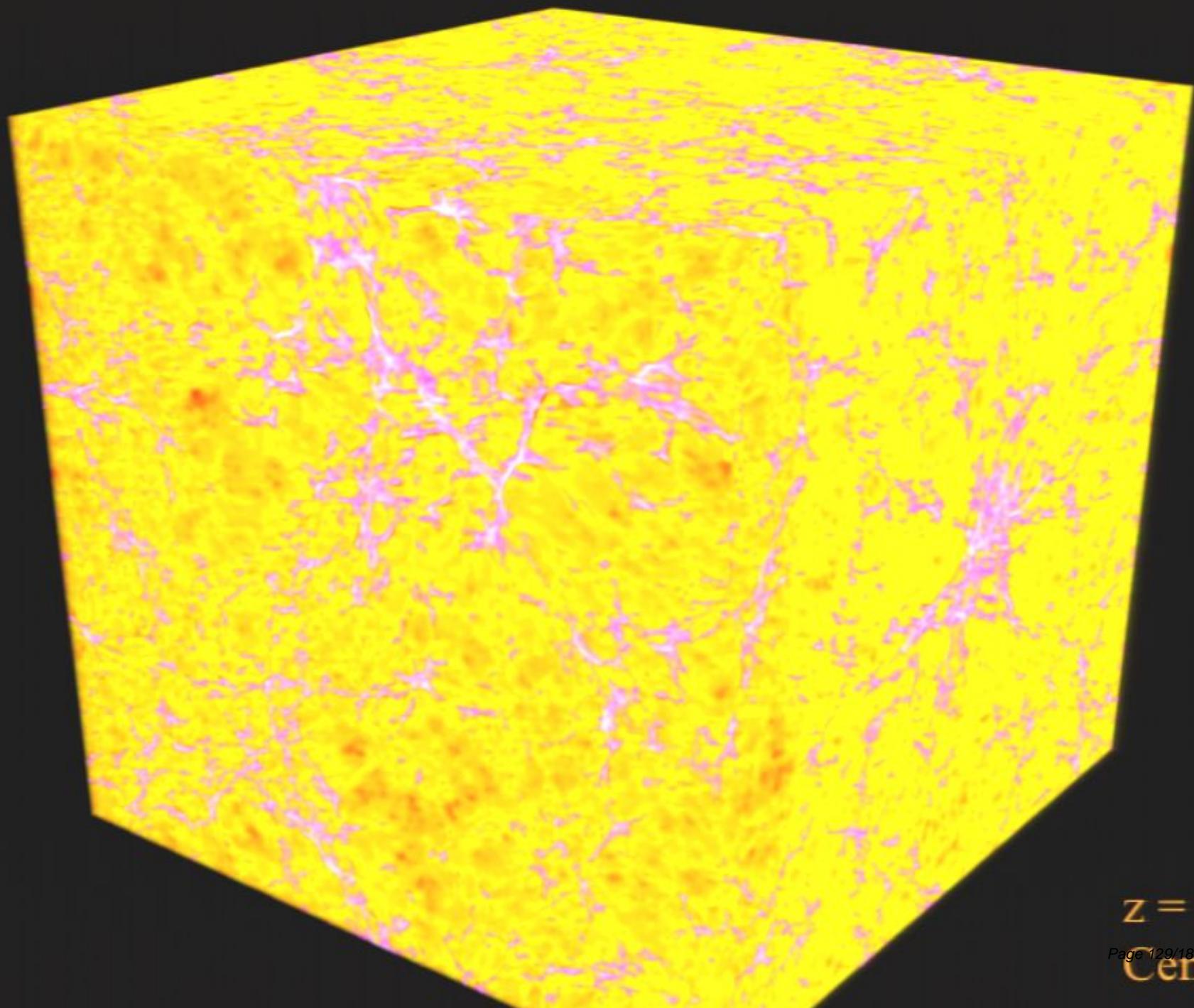
- Neutral hydrogen emits at 21cm (1.6 GHz) through the spin-flip transition. Potentially works for z up to ~ 100 .
- Neutral hydrogen absorbs at the Lyman Alpha frequency ($\sim 126\text{nm}$). Works in the optical for $2 < z < 6$.
- Both of these can be used to map neutral hydrogen when the nonlinear scale was very small.



$z = 11$

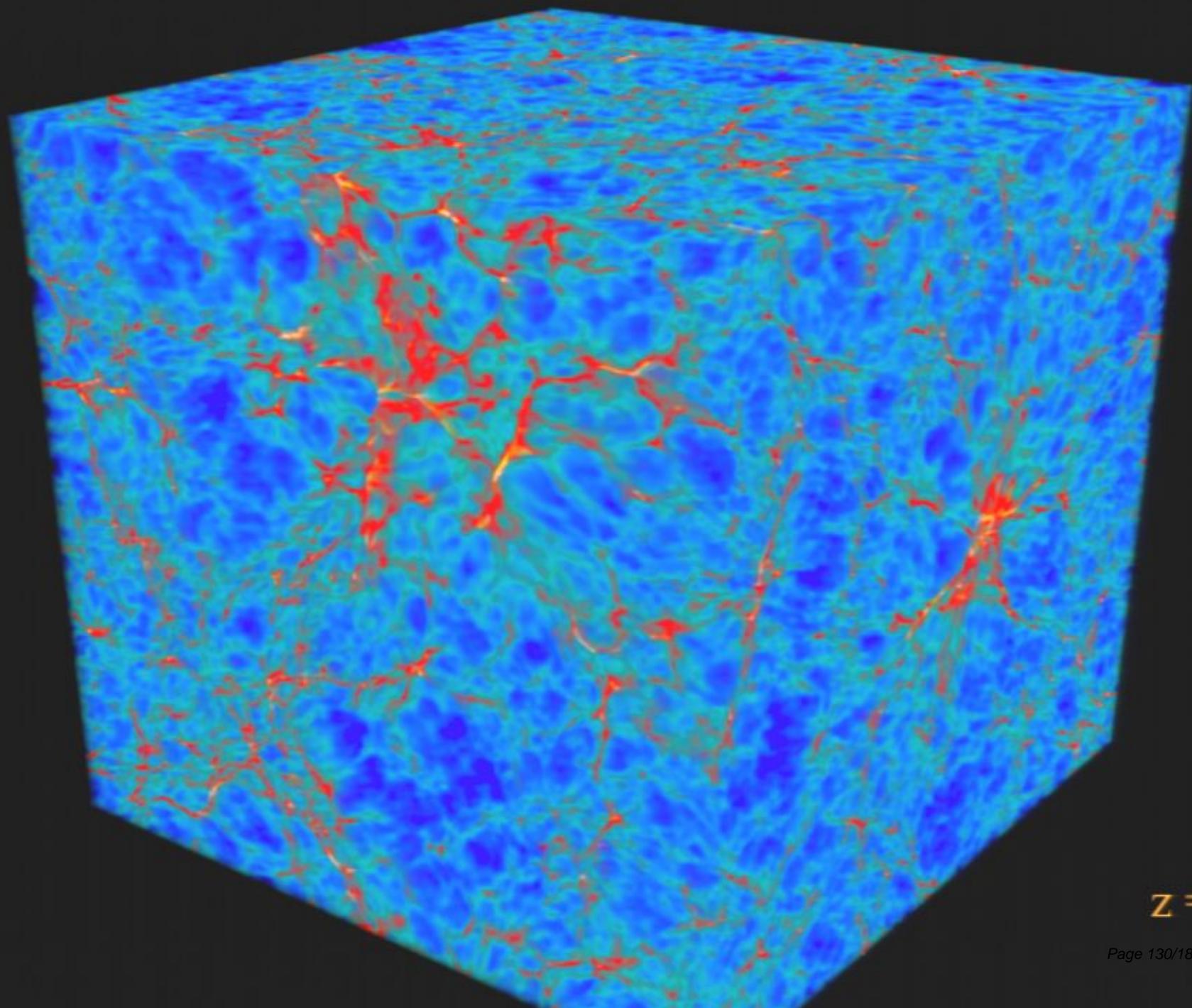
25 Mpc/h simulation
Pisca 09070039

Cen et al.

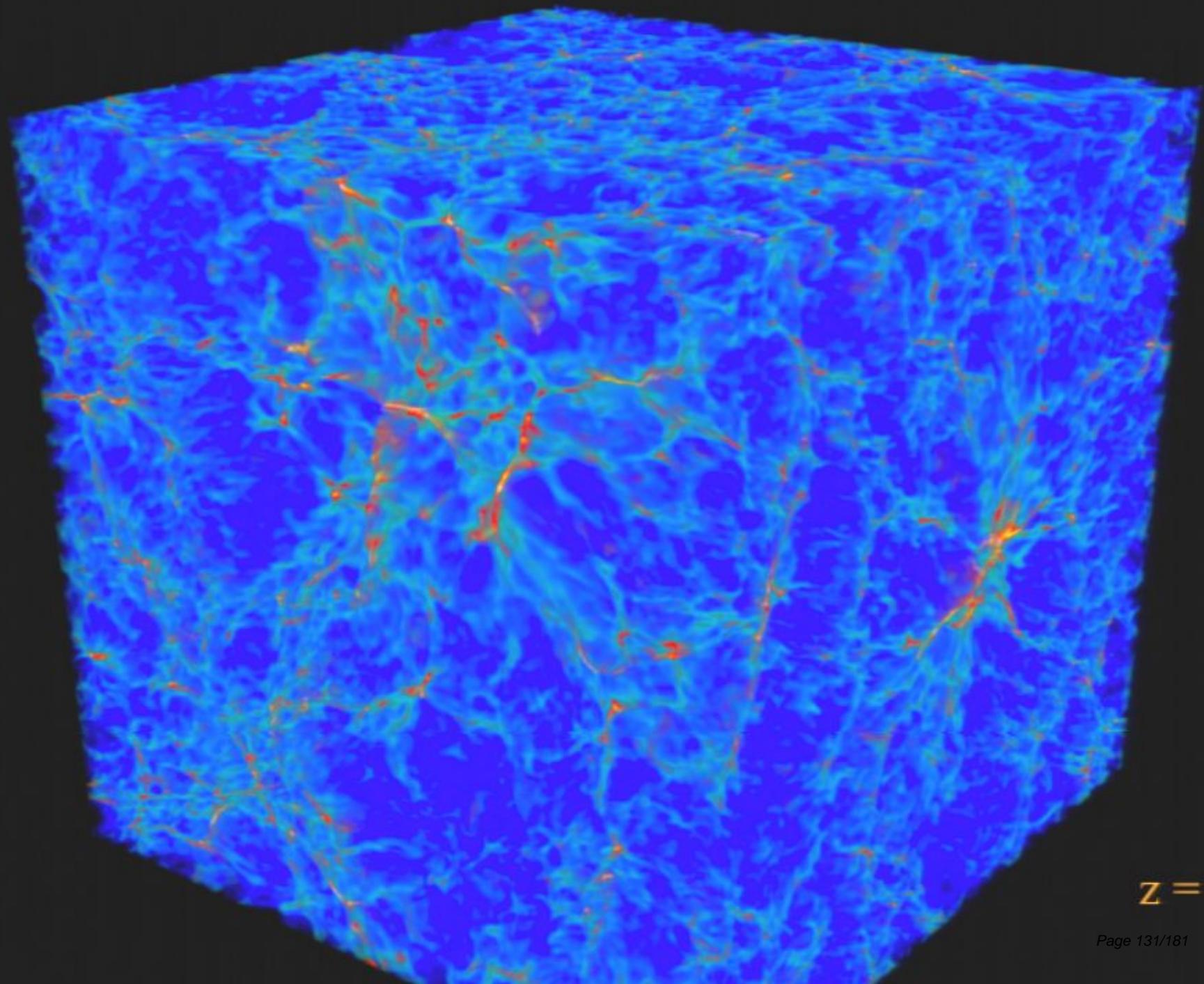


$z = 8.55$

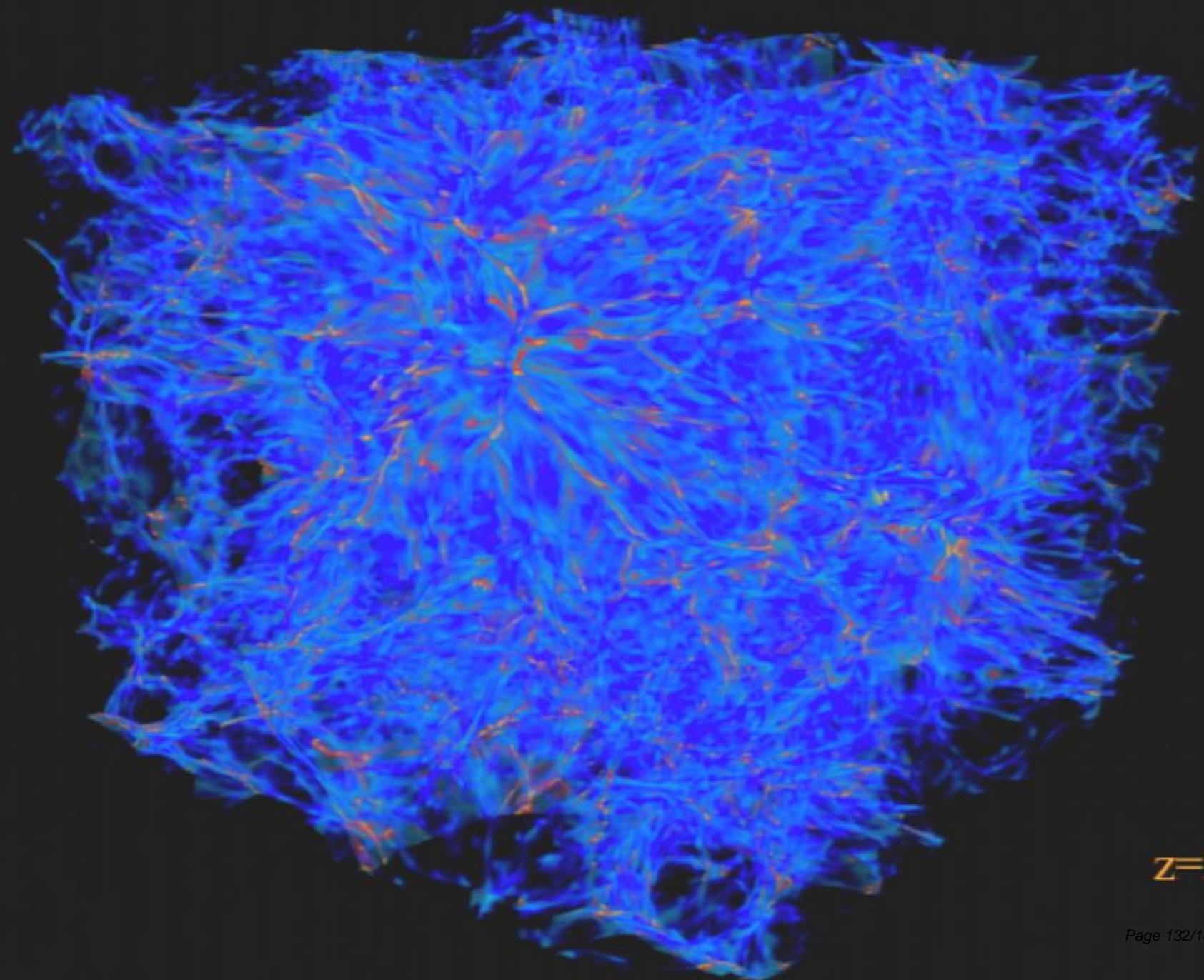
Page 129/181
Cen

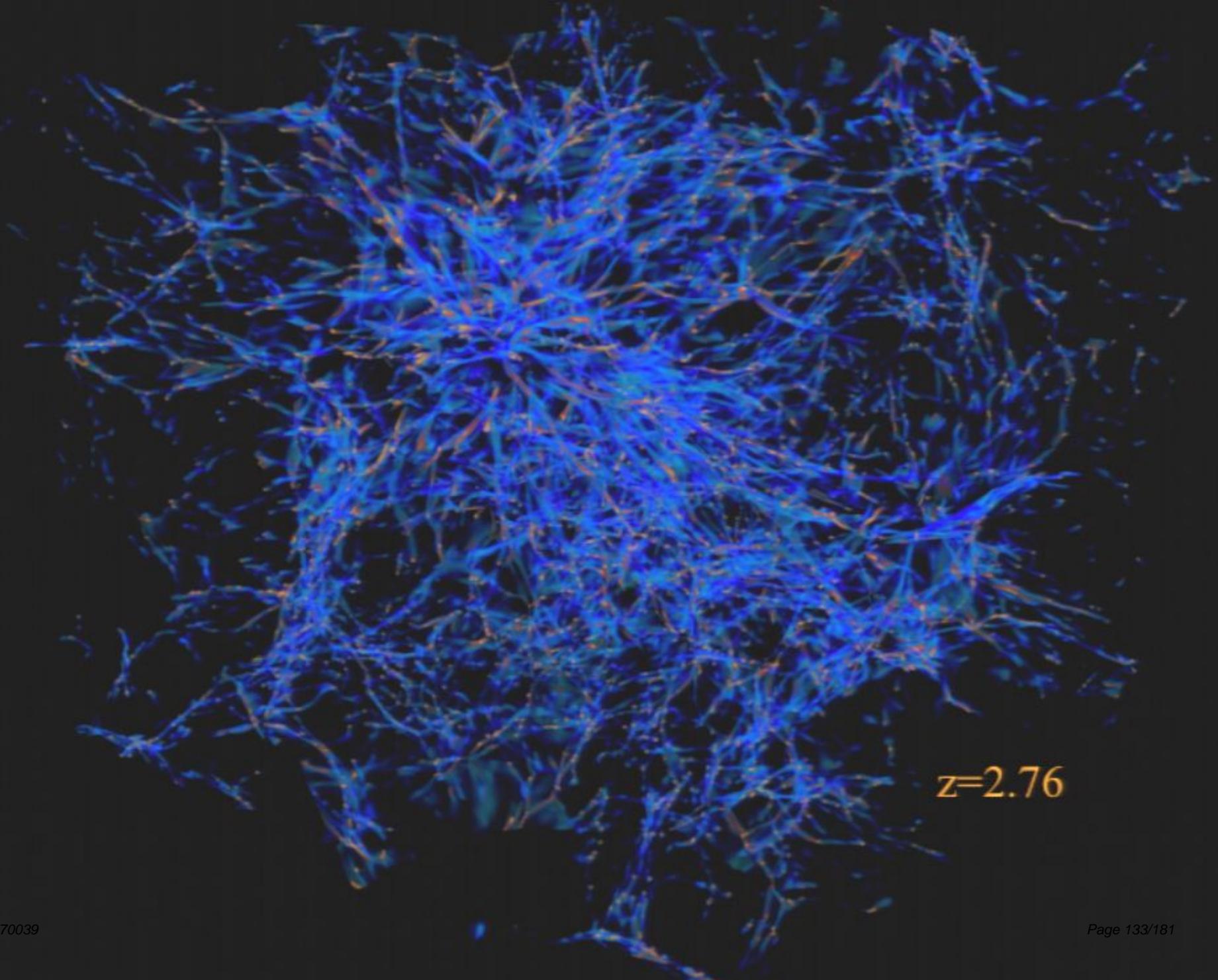


$z = 8.8$

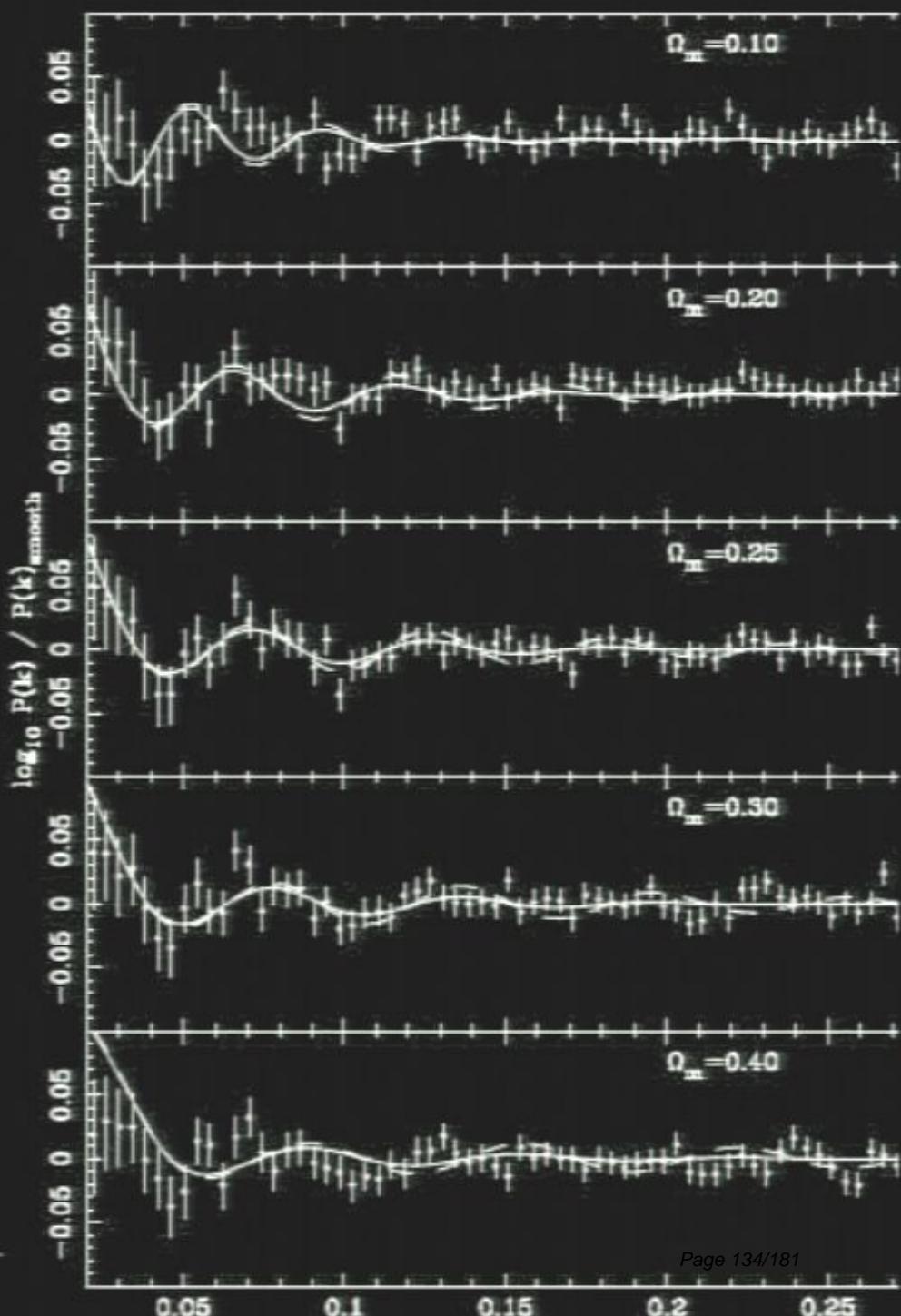


$z = 6.5$



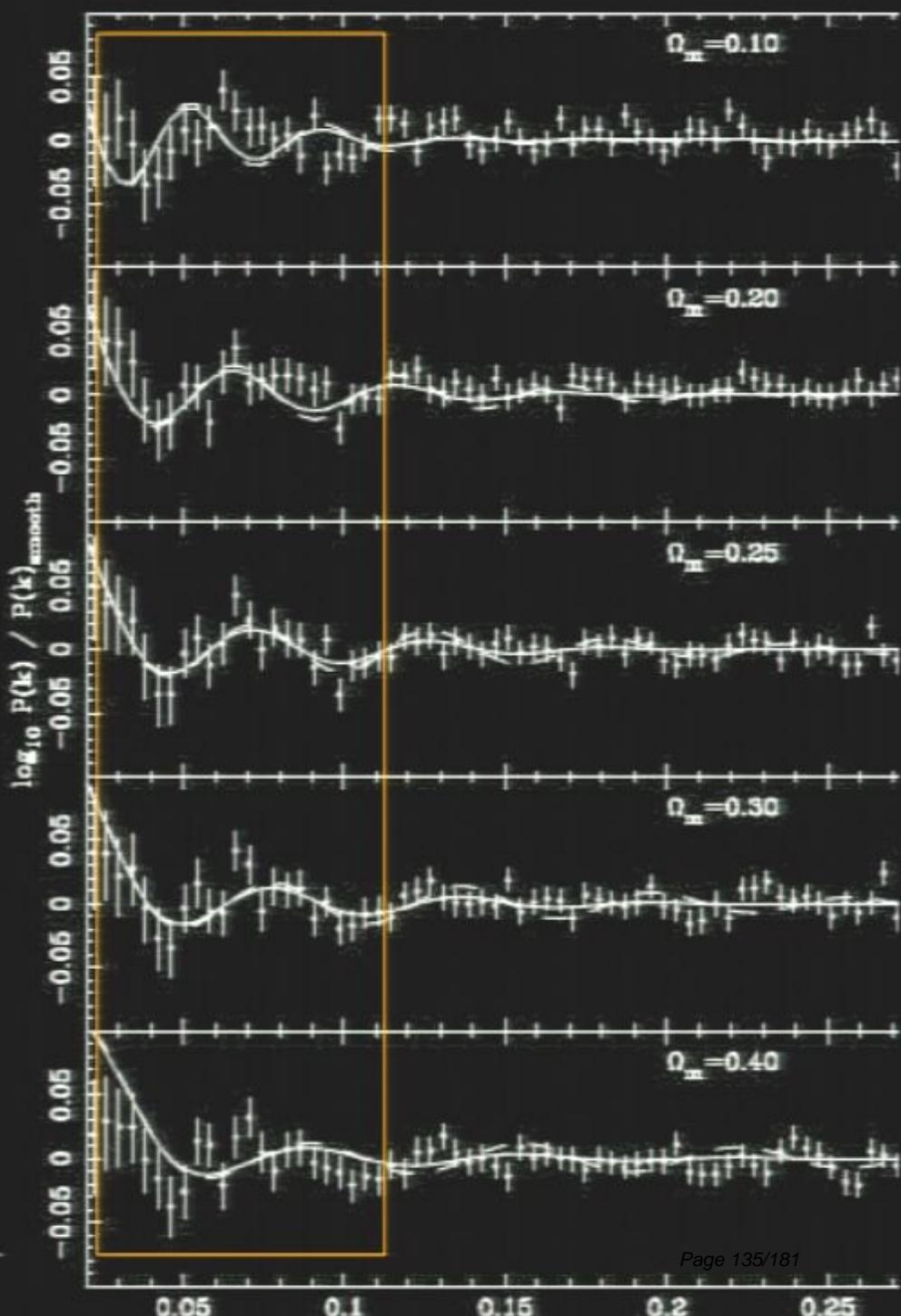


Current Data



Current Data

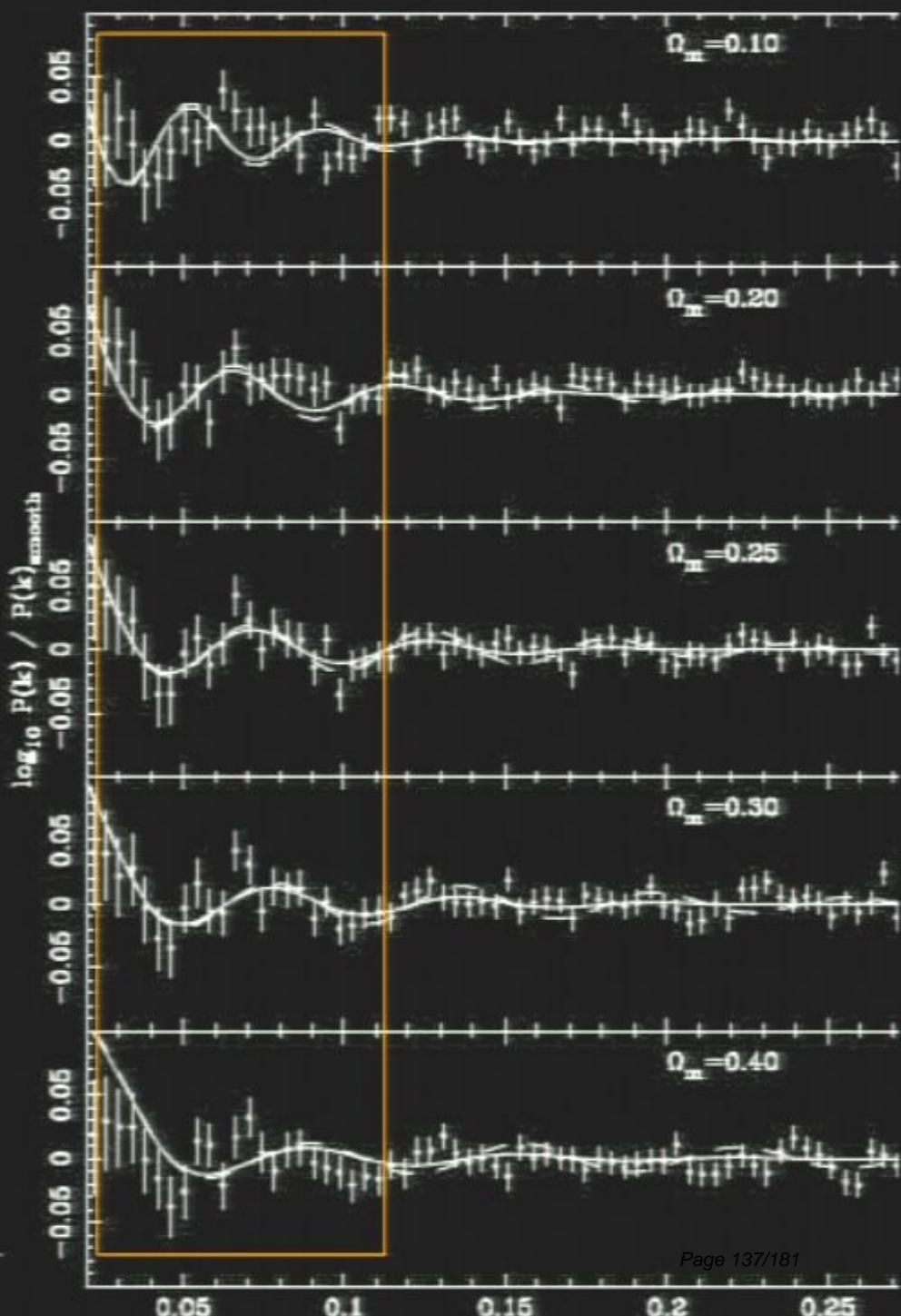
- Just the BAO wiggles
- Produced for SDSS + 2df galaxies combined



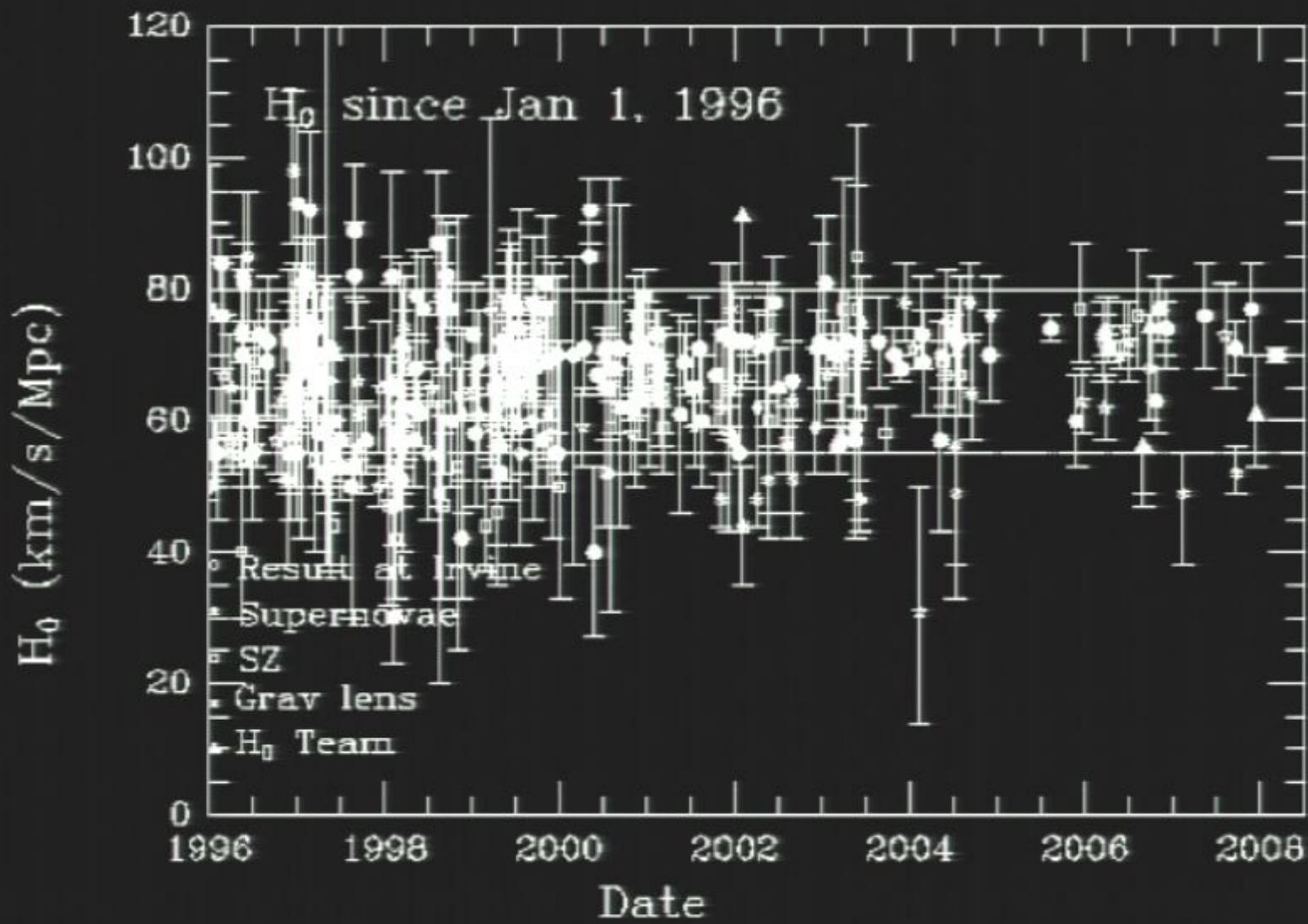
BAO
have provided the *first* ever
cosmic distance measure based
on *linear* physics

Current Data

- Just the BAO wiggles
- Produced for SDSS + 2df galaxies combined



BAO
have provided the *first* ever
cosmic distance measure based
on *linear* physics



J. Huchra

Complications

A man falls from a window and on the way down
someone asks... ``*how's it going?*''

The man replies: ``*So far so good!*''

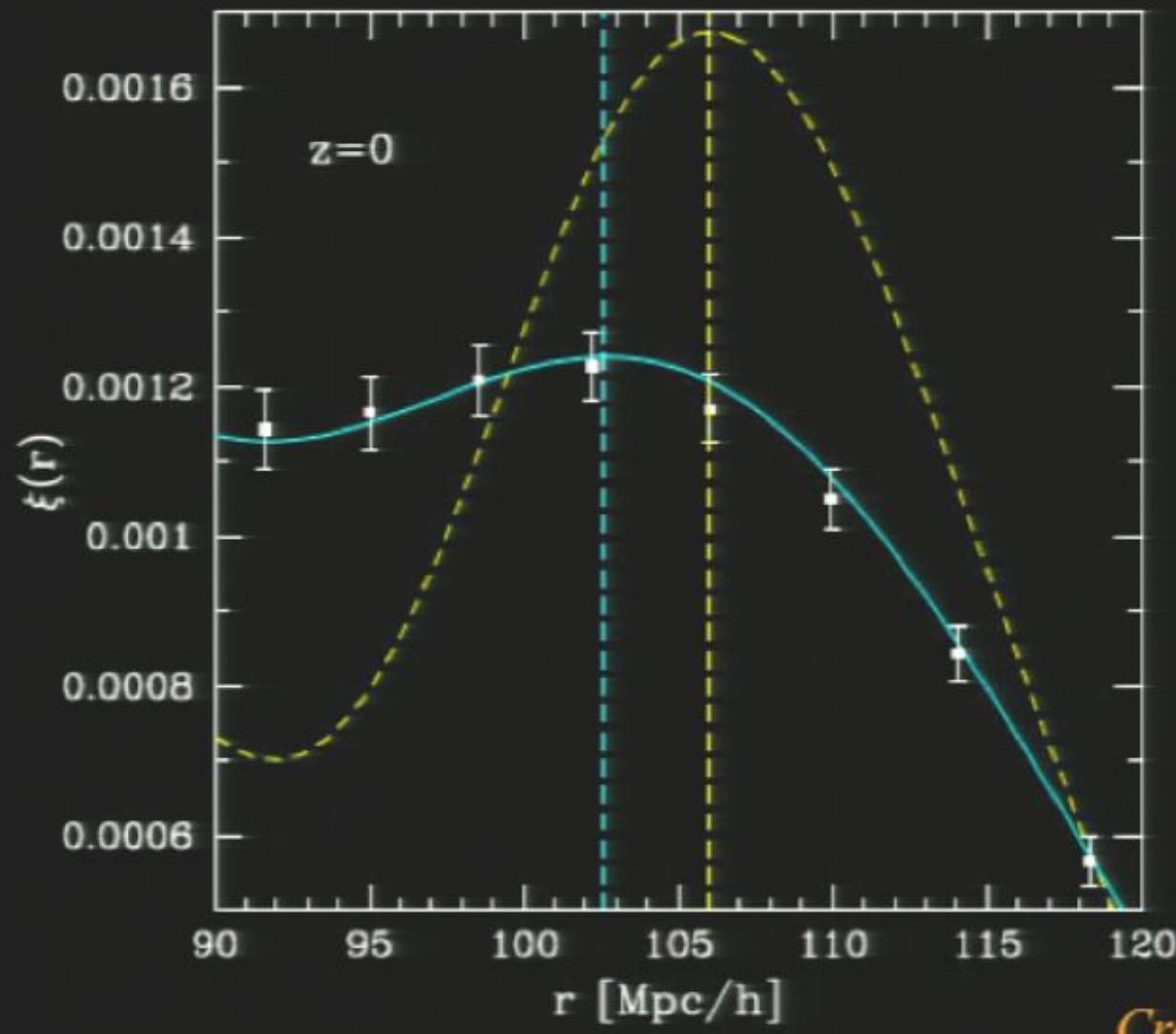
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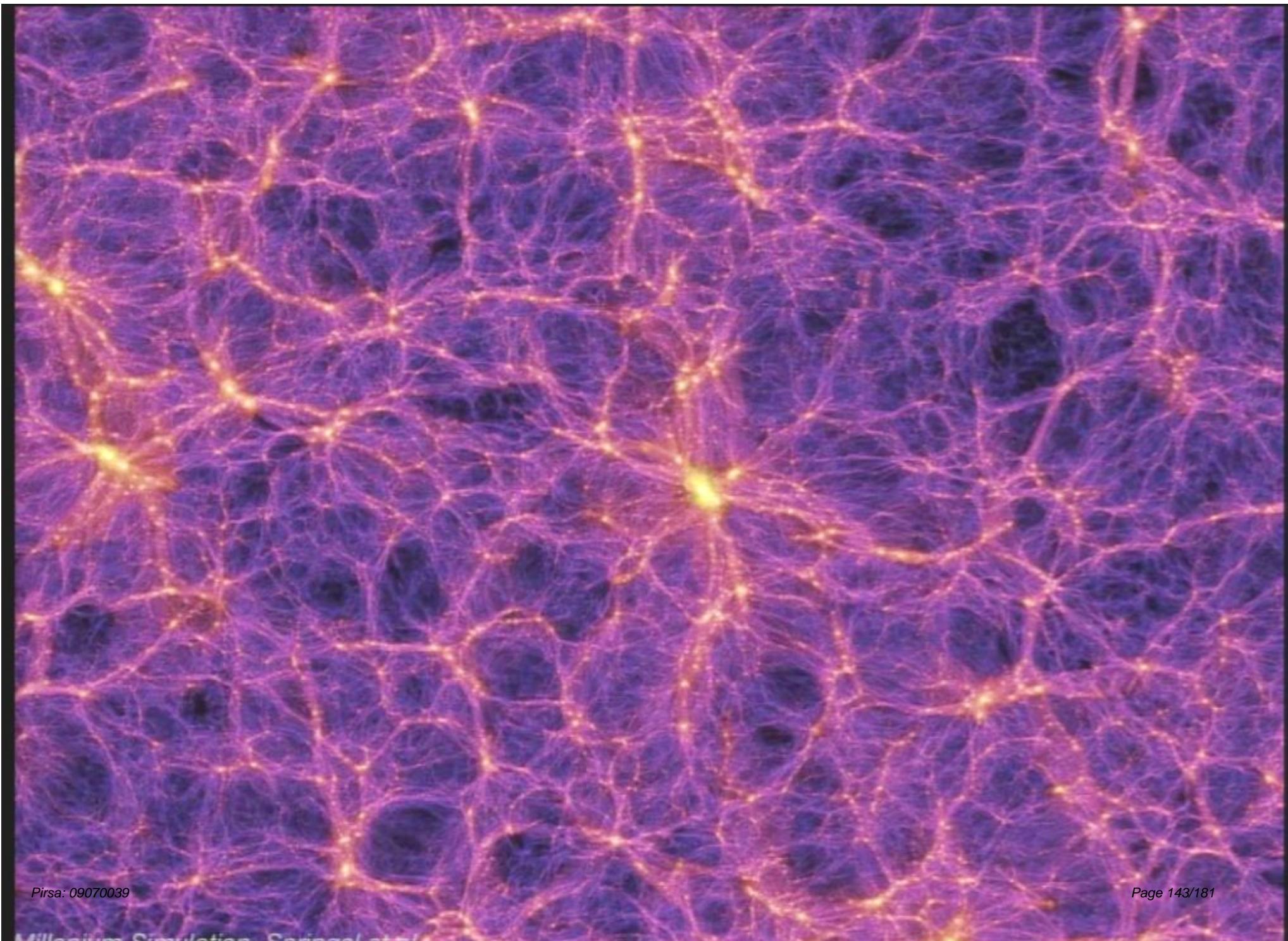
The man replies: ``*So far so good!*''

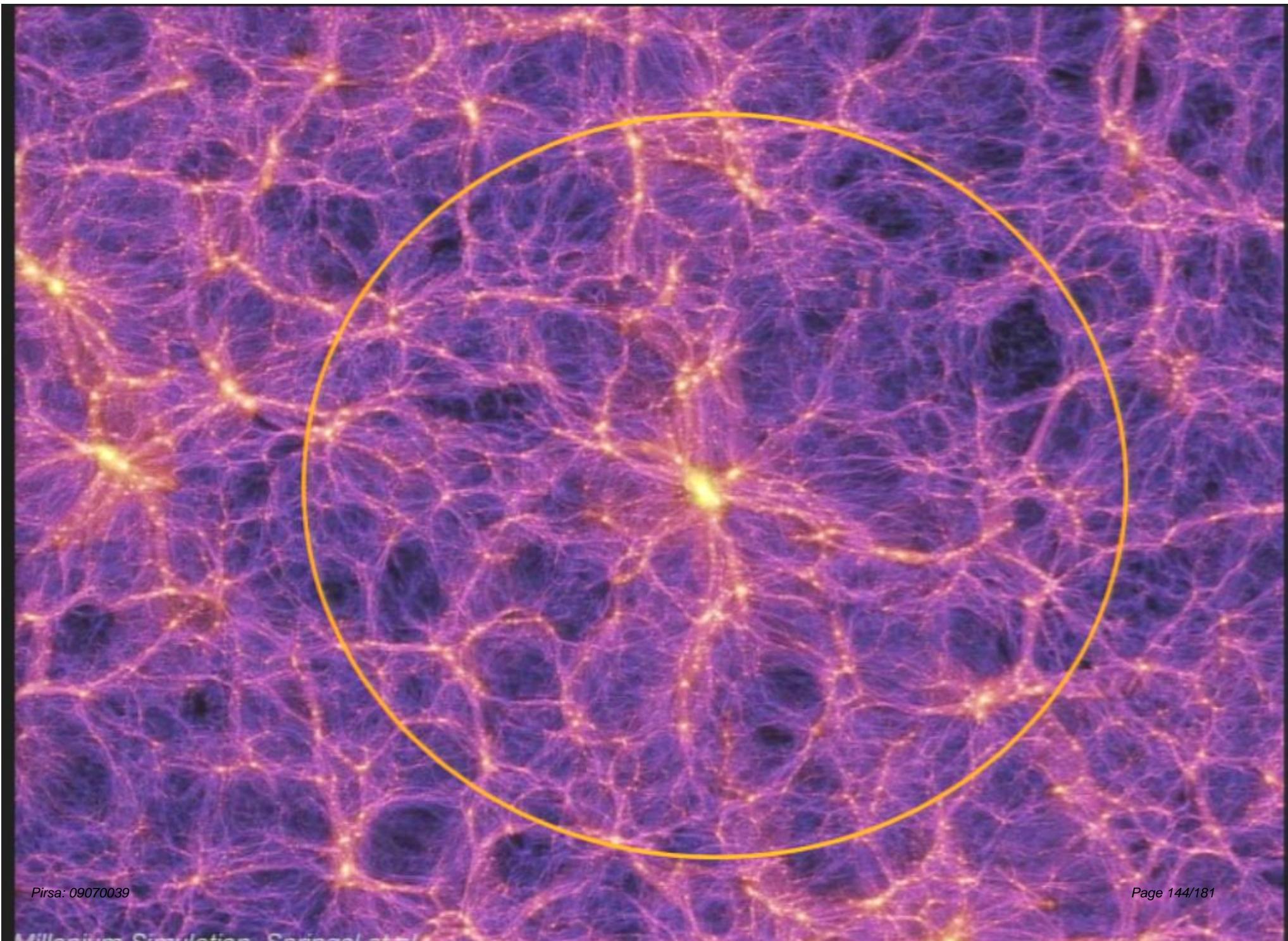
Cosmological Methods are similar – they have a
free-fall zone and a hard, systematic “floor” where things
get tough

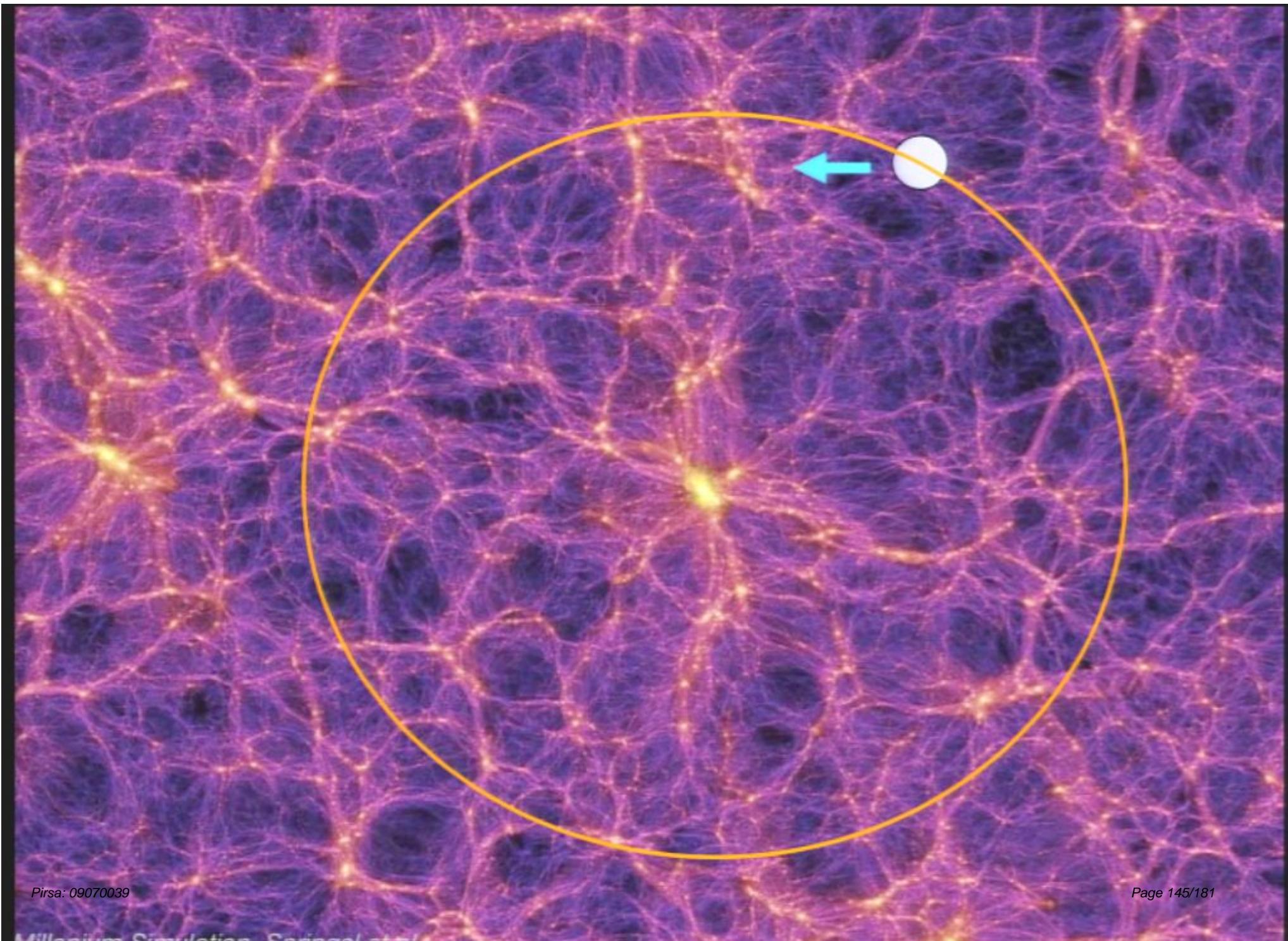
BAO and Nonlinearity

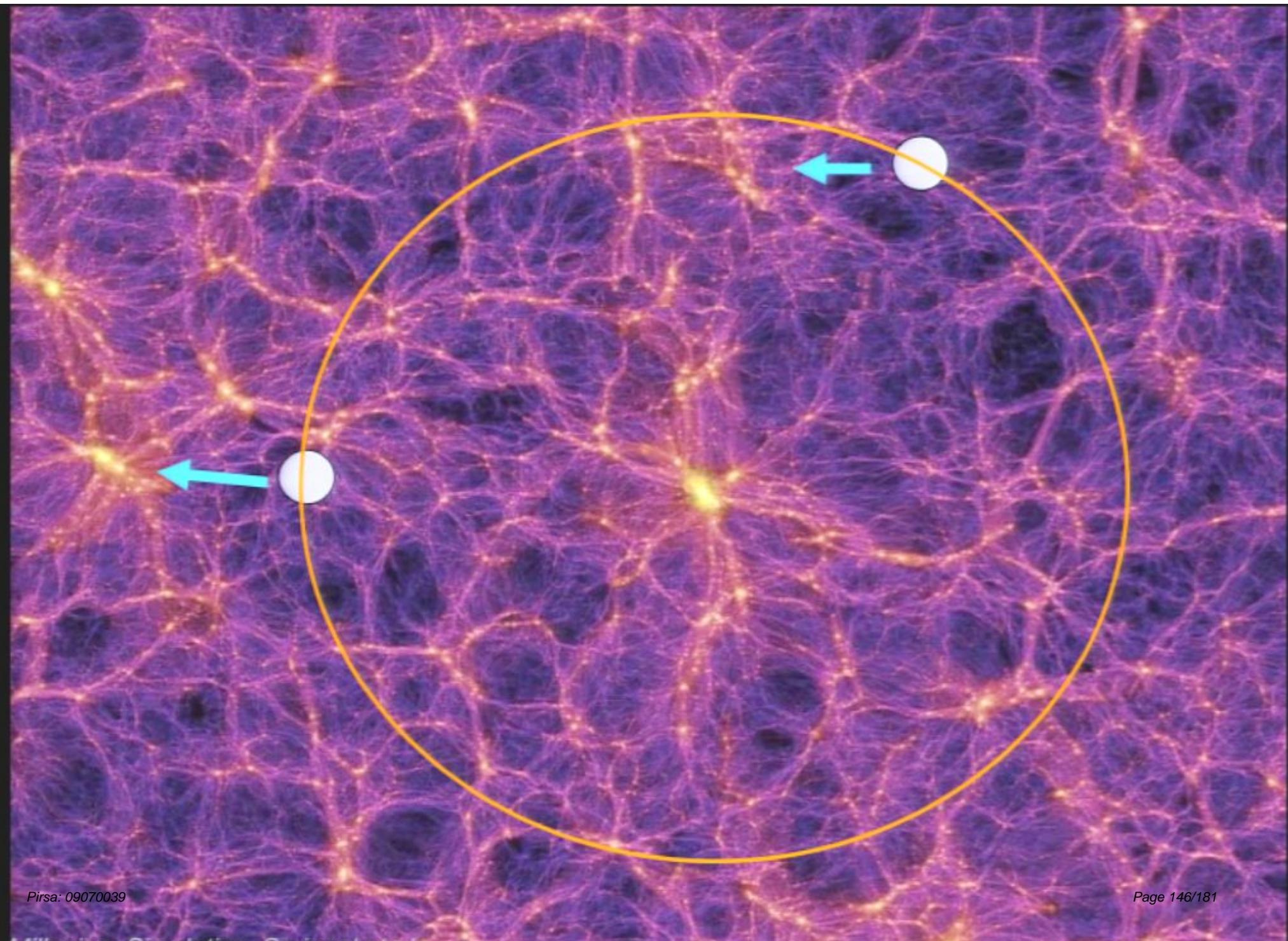


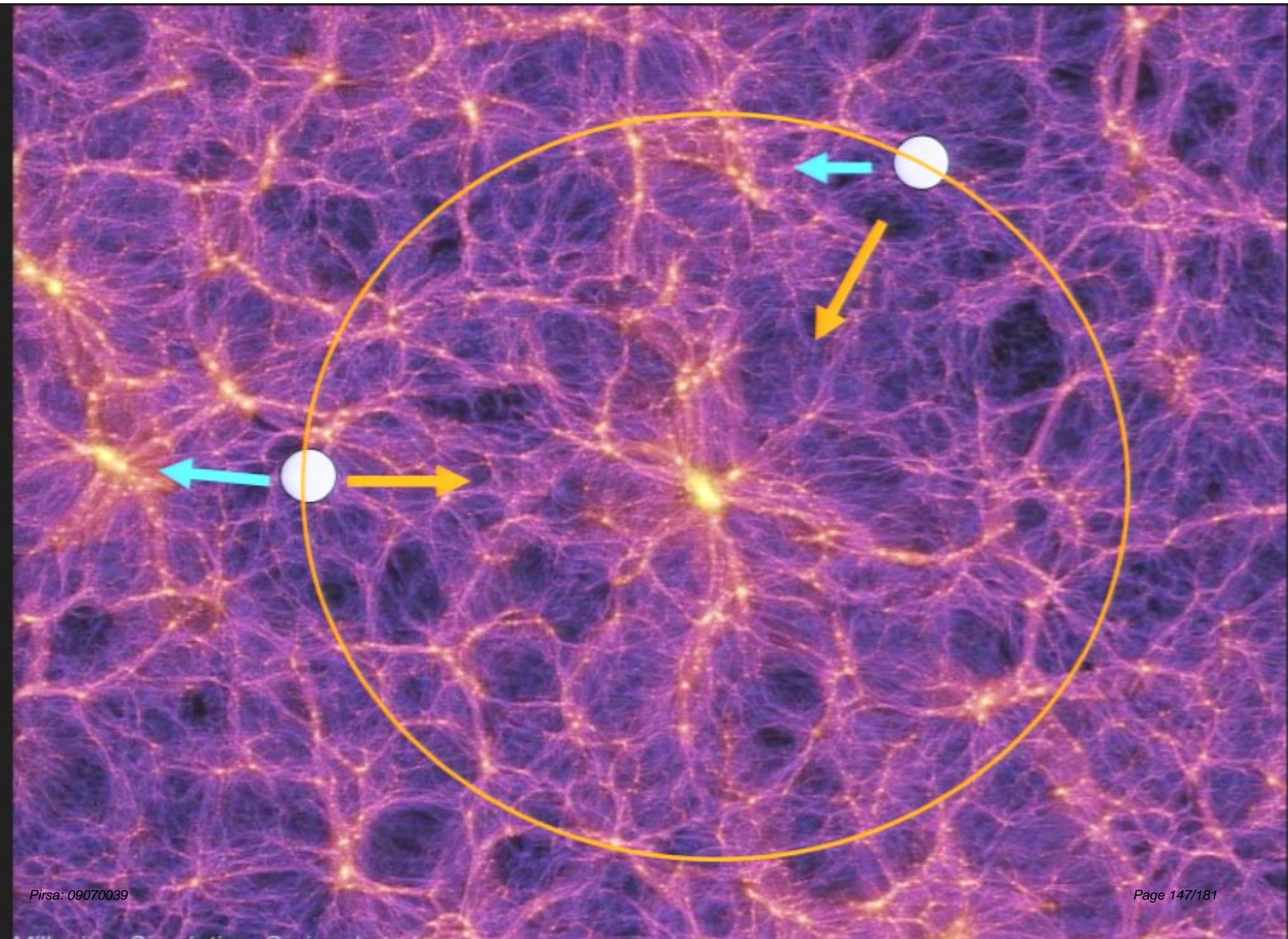
Crocce et al

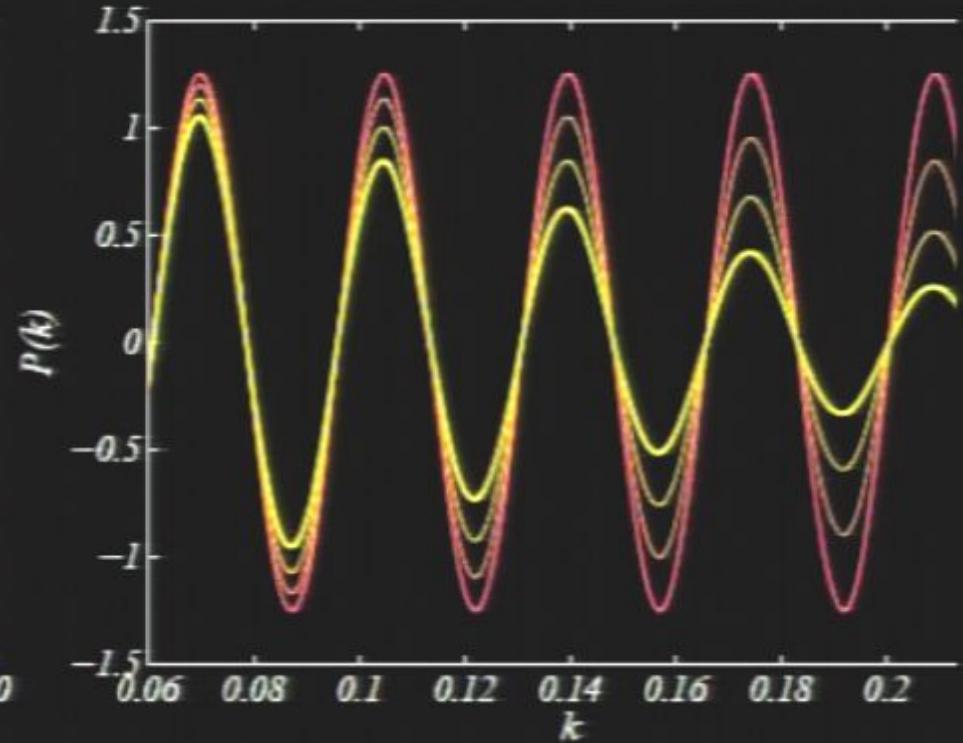
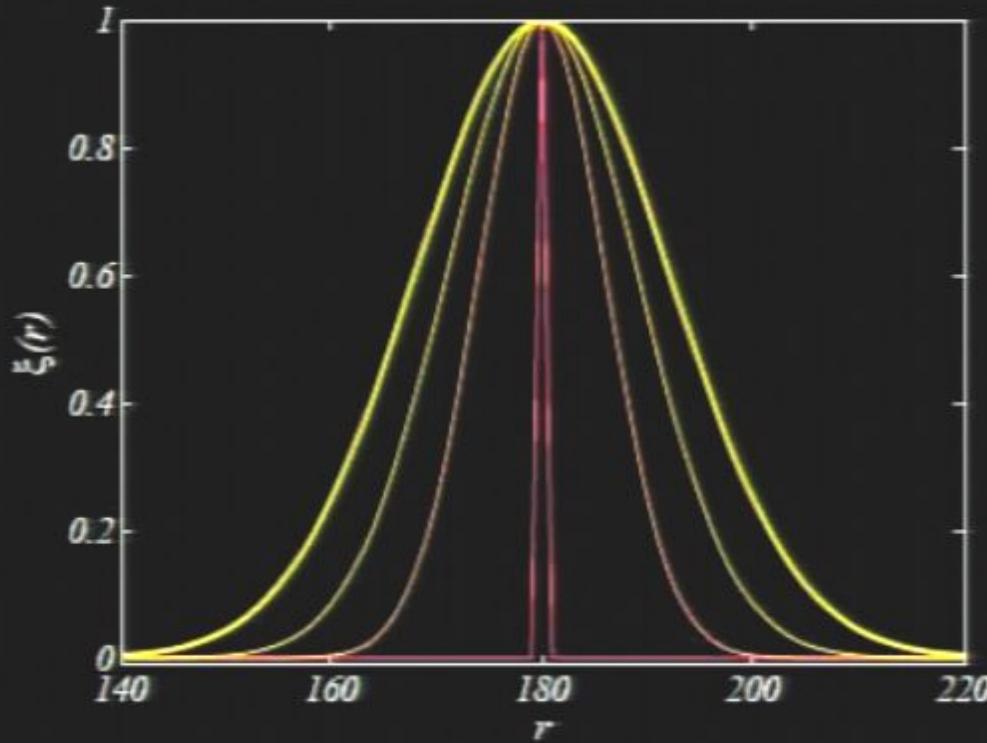




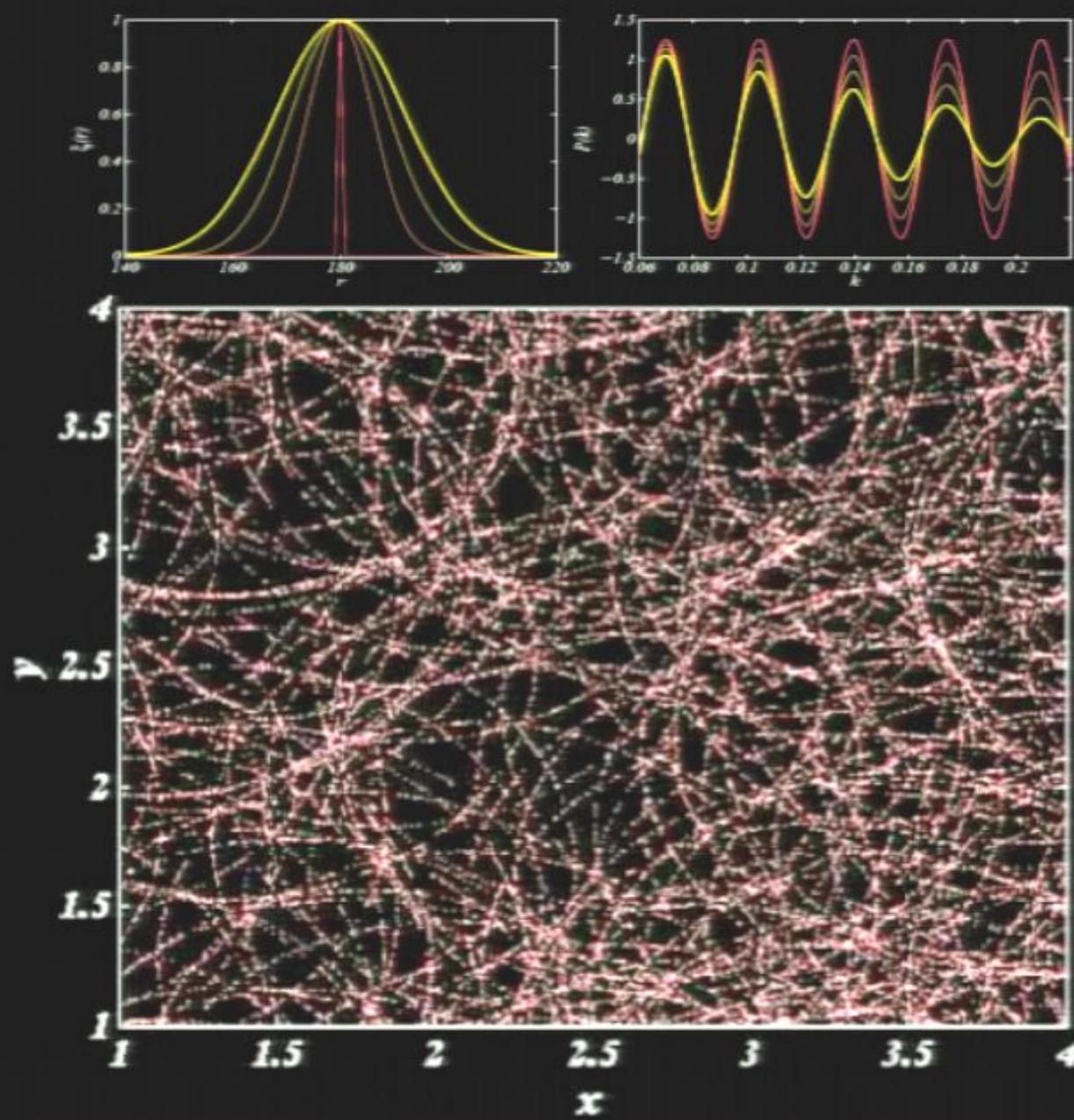


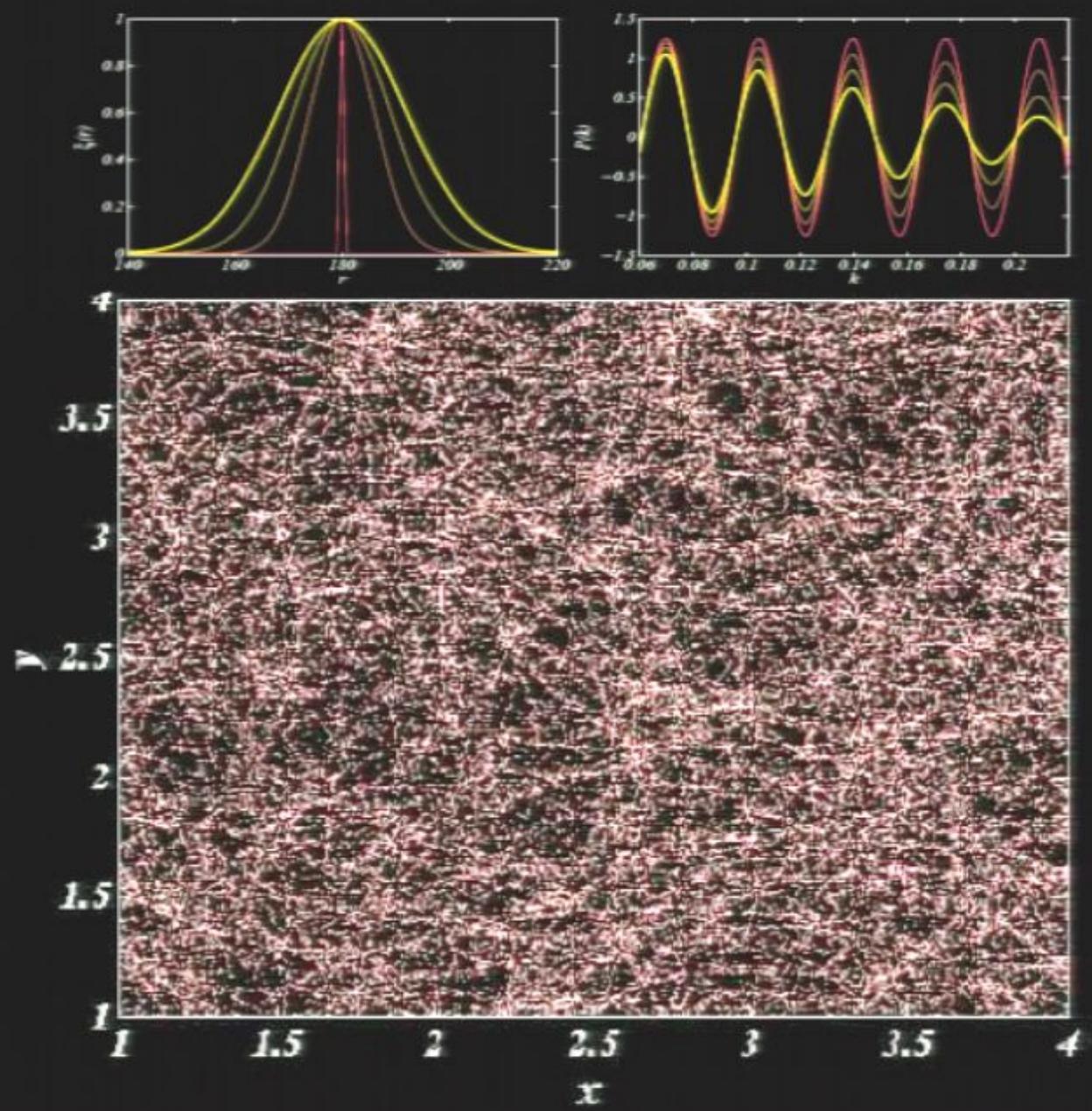


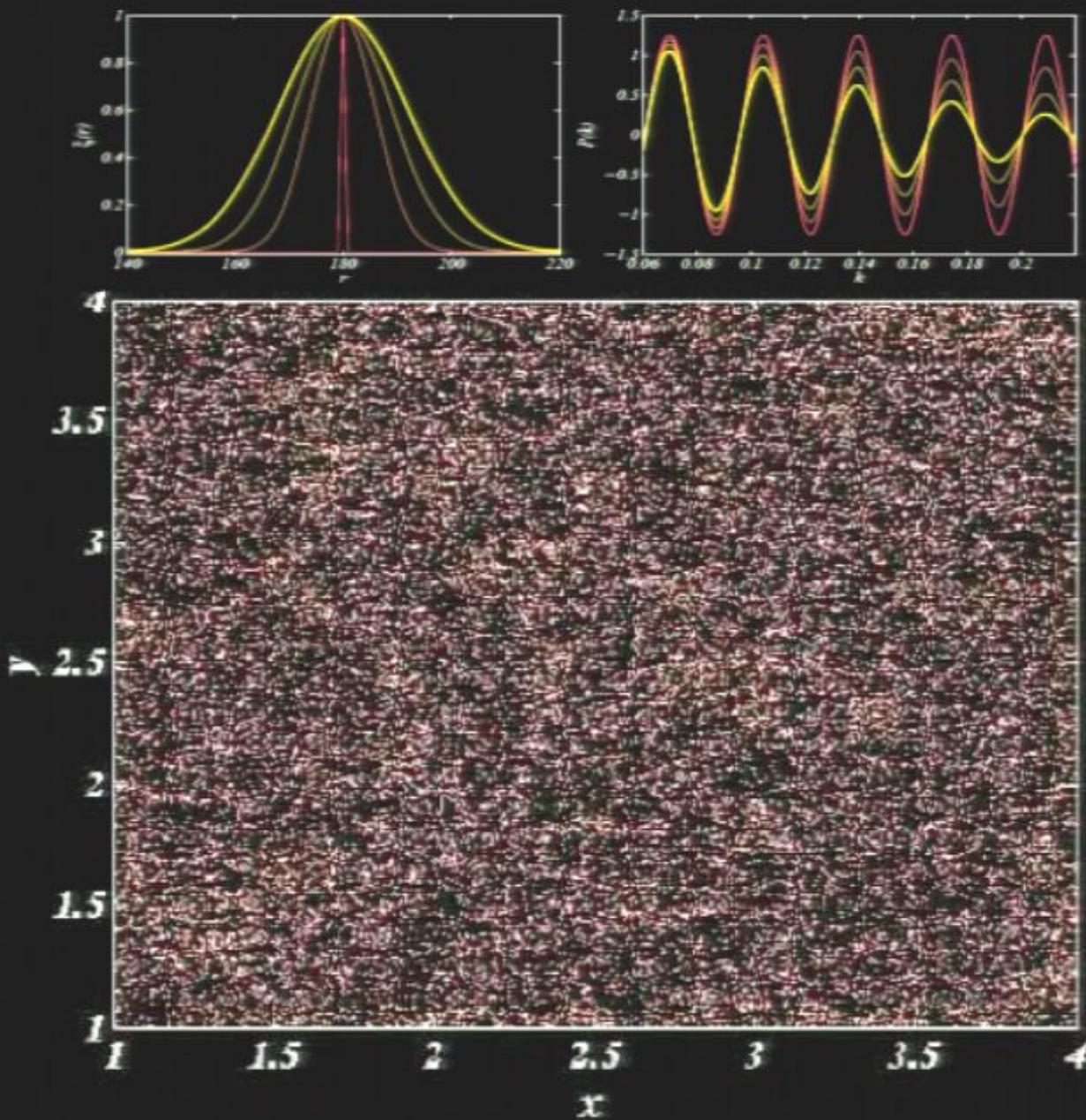




$$\xi(r) \longleftrightarrow P(k)$$







Calibrating Nonlinearity

- Although it is (weakly) nonlinear, gravity is still quite clean (compare turbulent MHD in strong gravitational field)
- Good reasons to believe the nonlinear effects can be calibrated at the 1% level for BAO/BAP
- Still needs more theoretical and numerical study
- Only true if background is FLRW ... what do we do in LTB?

Photometric BAO Surveys

It is tempting to want to just do an imaging survey instead of taking spectra

Photometric BAO surveys primarily sacrifice $H(z)$ information and need much larger volume to compete.



Skincolor: Earthy Copper
Background: none
Default Input: See & Eisenstein 2003

Parameters

H_0 O_m O_k w_0 w_a

Base parameters

70 0.3 0 -1 0

Prior matrix

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

UsePrior

Observable

H d_A G

Derivative Type

Analytical Analytical Numerical

Data Redshifts

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

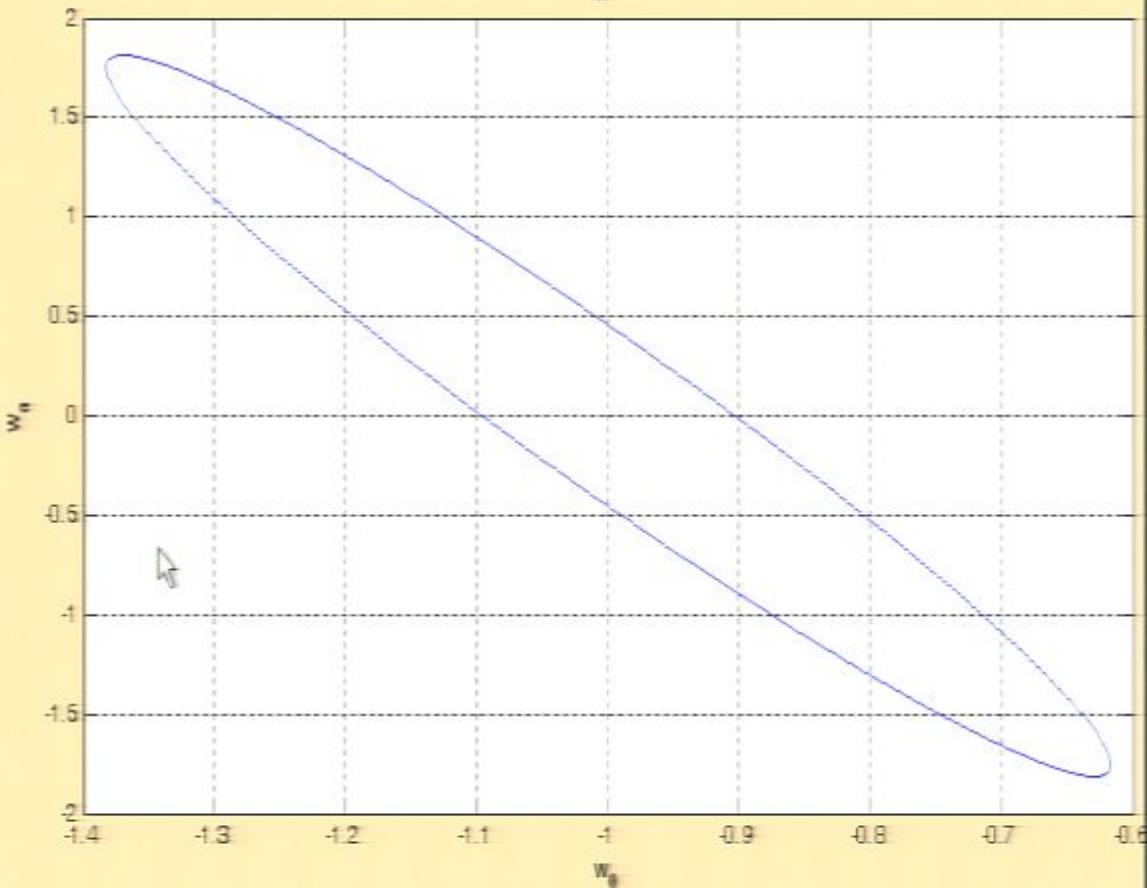
Fractional Errors on Observables:

0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0253	0.0203
0.0148	0.0119
	0.0022

Pirsa: 09070039

Fisher Error Ellipse for Observables:

$d_A(z)$



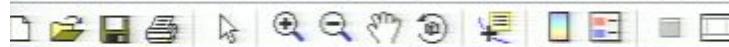
Hold on Line Style: - xlim: [-1.6-0.5] Clear
 Area Fill Sigma Level: 1 sigma ylim: [-1 1] Edit axis labels
 Line Color Grid: over plot Saving Features
 Grid

Run

Figure of Merit =

DETF (1/Area 2-sigma)

Local Area Connection 2
Page 155/181
A network cable is unplugged.
Reset from



Skin colour: Earthy Copper
 Background: none
 Default input: Seo & Eisenstein 2003

Parameters:

Base parameters

H_0 O_m O_k w_0 w_a

70	0.3	0	-1	0
10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix

Use Prior

Observable

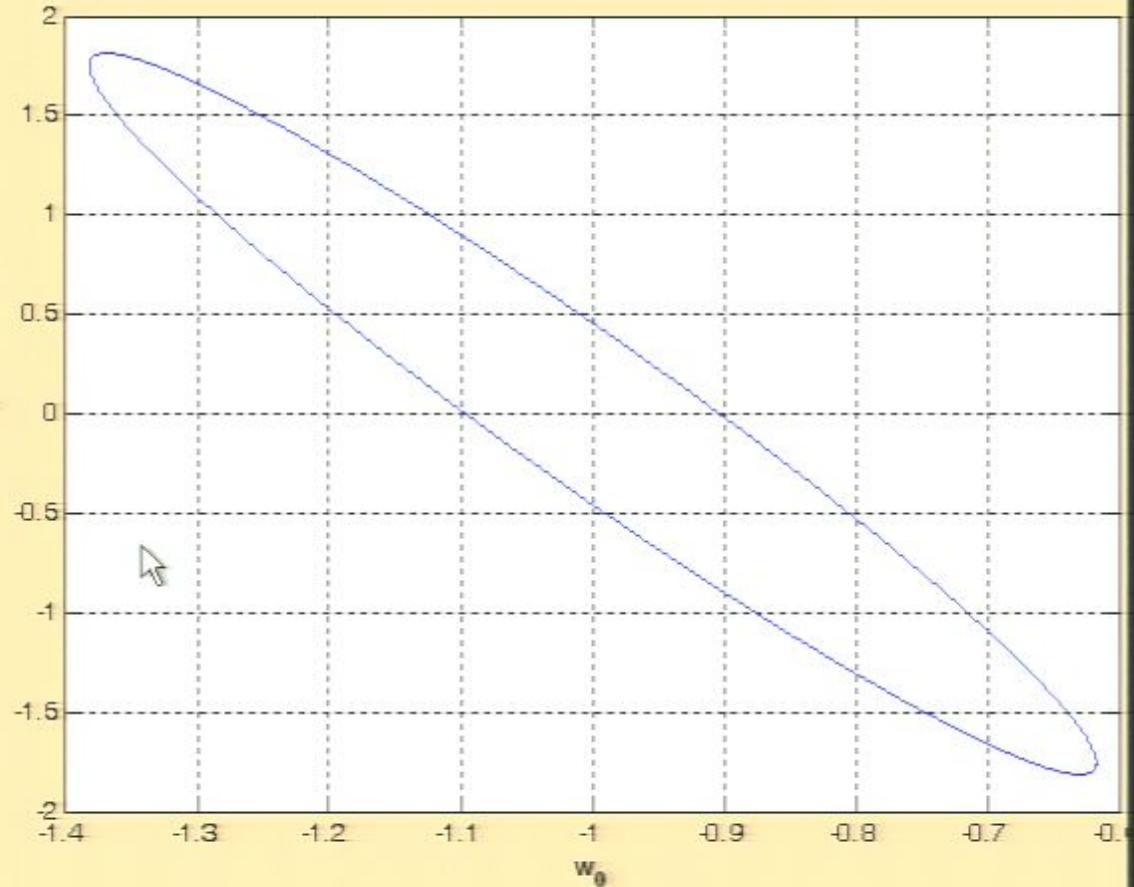
Derivative Type

Data Redshifts

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:
 $d_A(z)$



Hold on Line Style:
 Area Fill Sigma Level:
 Line Color Grid: over plot
 xlim: [-1.5 -0.5] ylim: [-1 1]

Run

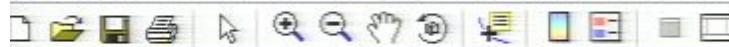
Figure of

Local Area Connection 2

A network cable is unplugged.

DETF (1/Area 2-...

Page 157/181
 Reset FoM



Skin colour Earthy Copper
 Background none
 Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O_m O_k w_0 w_a

70	0.3	0	-1	0
10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix

Use Prior

Observable

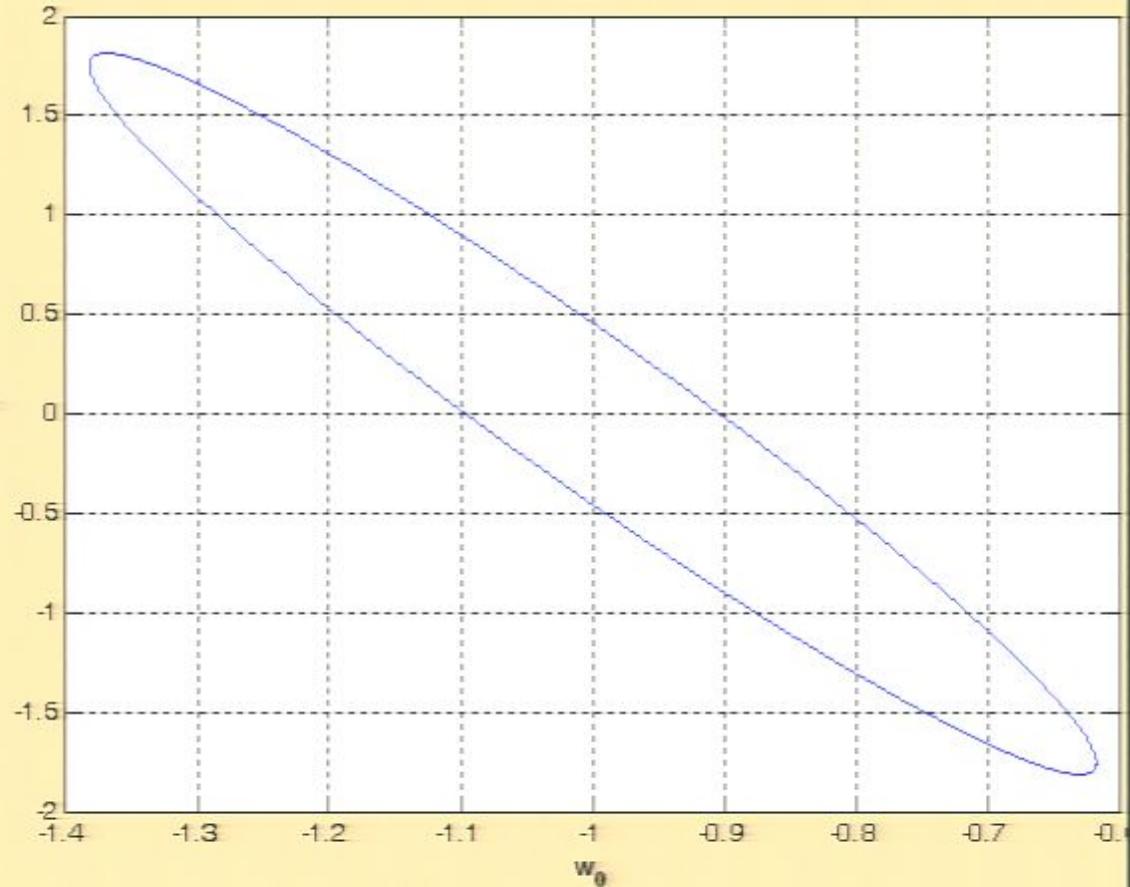
Derivative Type

Data Redshifts

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:
 $d_A(z)$



Hold on Line Style:
 Area Fill Sigma Level:
 Line Color Grid: over plot
 xlim: [-1.5 -0.5] ylim: [-1 1]

Run

Figure of Merit = 1.70

DETF (1/Area 2-...)

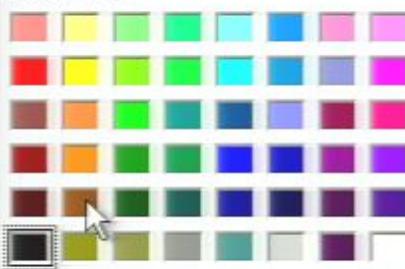
Page 158/181
 Reset FOM

Choose Fill Color



View Insert Tools Desktop Window Help

Basic colors:



Custom colors:



Define Custom Colors >>

OK

Cancel

Observable

 H d_A G

Derivative Type

Analyti...

Analyti...

Numerical

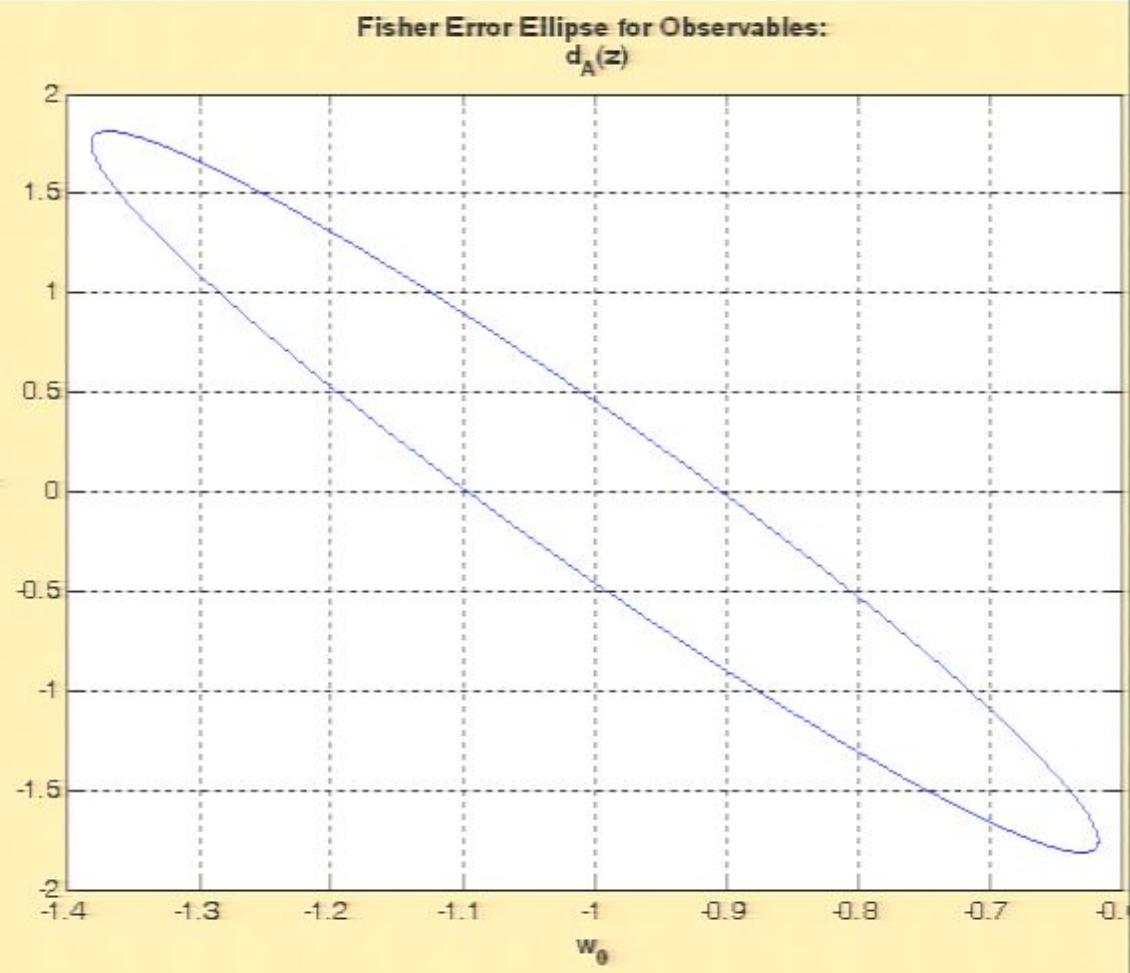
Data Redshifts

0.3
0.6
0.8
1
1.2
3
10000.3
0.6
0.8
1
1.2
3
10000.3
0.6
0.8
1
1.2
3
1000

Fractional Errors on Observables

0.058
0.0519
0.0369
0.0284
0.0253
0.01480.0519
0.043
0.0322
0.023
0.0203
0.0119
0.00220.0519
0.043
0.0322
0.023
0.0203
0.0119
0.0022

Pirsa: 09070039



Hold on Line Style: xlim [-1.5 -0.5]

Area Fill Sigma Level: ylim [-1 1]

Line Color Grid over plot Saving Feature...
Figure of Merit = 1.70

Run

Figure of Merit = 1.70

DET(1/Area 2-...

Page 159/181
Reset FOM

Tacklebox GUI D:\Bruce\tex\Fisher Tackle\Stable Releases\version 2.0

Fisher4Cast F4C Extensions File Edit View Insert Tools Desktop Window Help



Skin colour Earthy Copper
Background none
Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O_m O_k w_0 w_a

70 0.3 0 -1 0

Prior matrix

Use Prior

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Observable

Derivative Type

Data Redshifts

H d_A G

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

Normalise Growth at $z =$

0

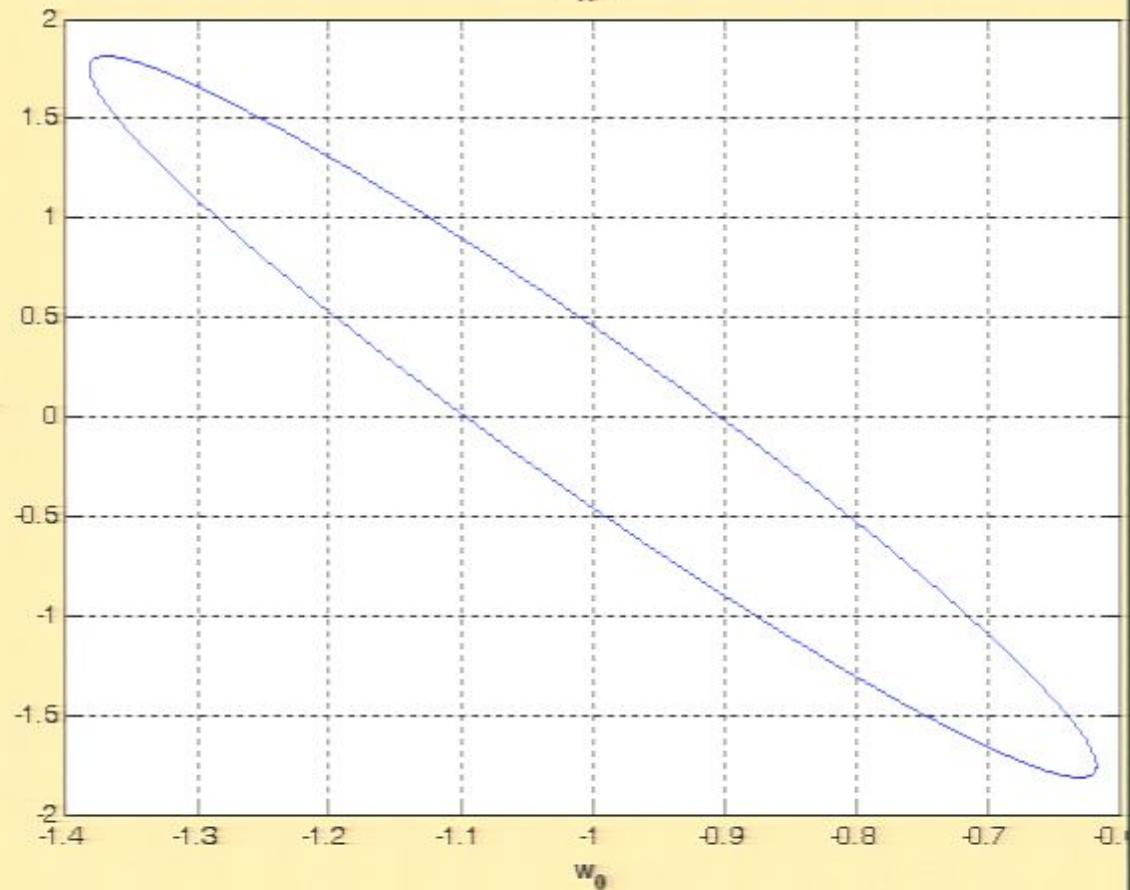
0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0263	0.0203
0.0148	0.0119
	0.0022

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:

$d_A(z)$



Hold on

Line Style

-

xlim

[-1.5 -0.5]

Clear

Area_Fill

Sigma Level

1 sigma

ylim

[-1 1]

Edit axis labels

Line Color

Grid

over plot

xlim

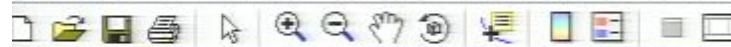
Saving Features...

Run

Figure of Merit = 1.70

DETF (1/Area 2-...

Page 160/181
Reset FOM



Skin colour Earthy Copper
Background none
Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O_m O_k w_0 w_a

70	0.3	0	-1	0
10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix

Use Prior

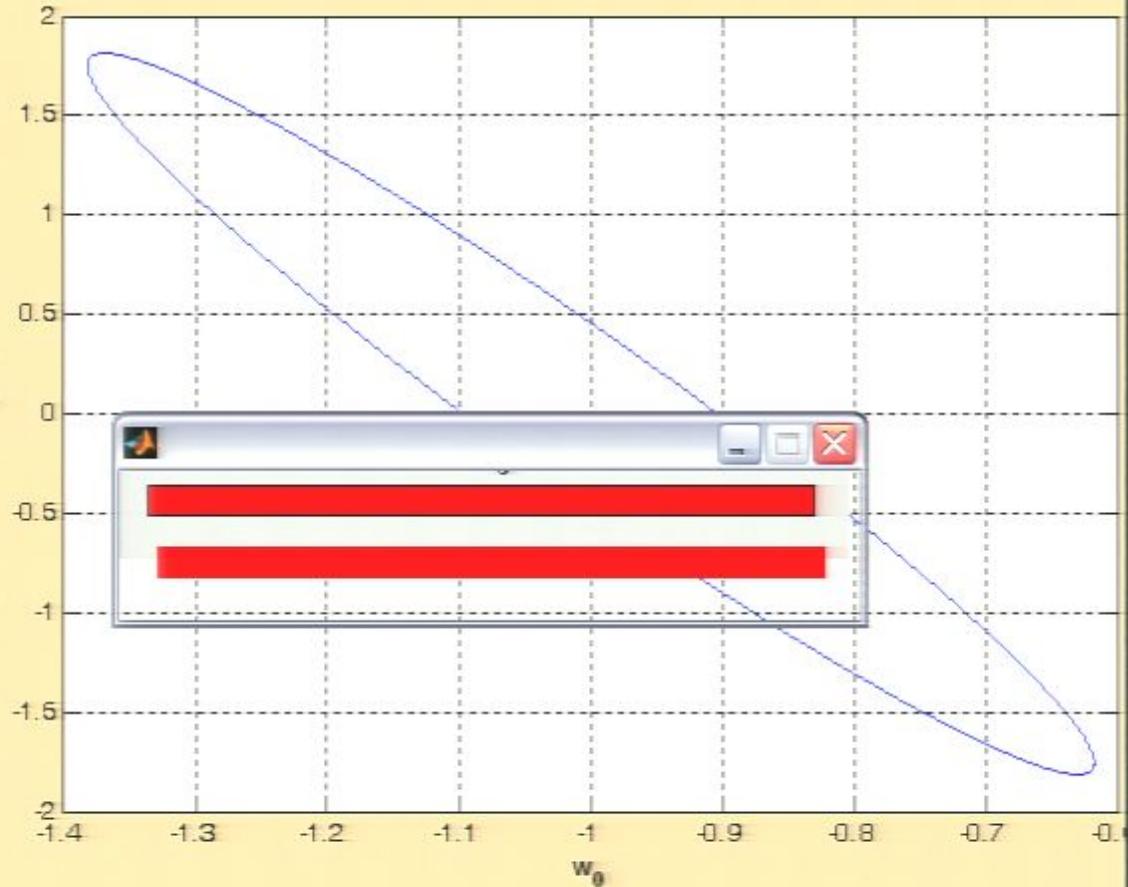
Observable

Derivative Type

Data Redshifts

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:
 $d_A(z)$ 

Hold on Line Style:
 Area Fill Sigma Level:
 Line Color Grid:

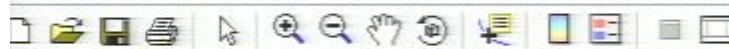
Figure of Merit = 1.70

DET F (1/Area 2-...)

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Reset FoM

Tacklebox GUI D:\Bruce\tex\Fisher Tackle\Stable Releases\version 2.0

Fisher4Cast F4C Extensions File Edit View Insert Tools Desktop Window Help



Skin colour Earthy Copper
Background none
Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O_m O_k w_0 w_a

70 0.3 0 -1 0

Prior matrix

Use Prior

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Observable

Derivative Type

Data Redshifts

H d_A G

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

Normalise Growth at $z =$

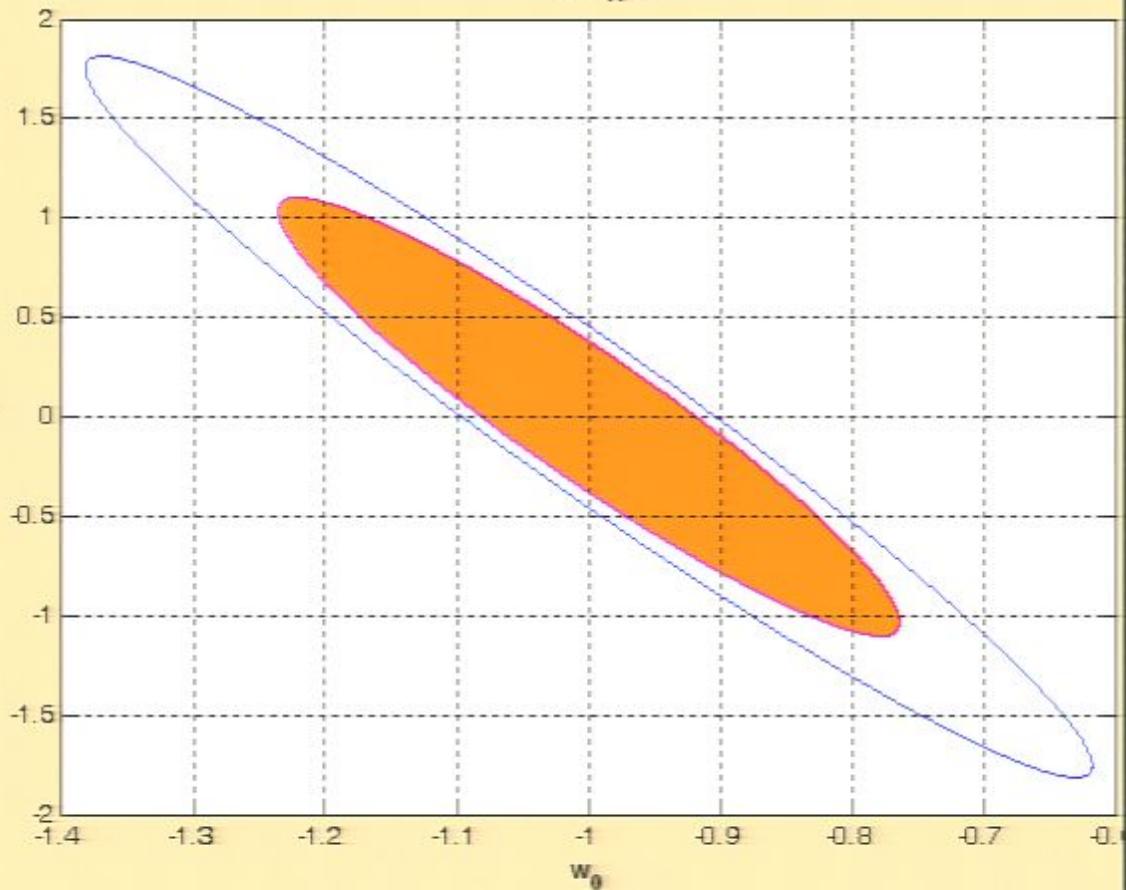
0

0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0263	0.0203
0.0148	0.0119
	0.0022

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:
 $H(z), d_A(z)$



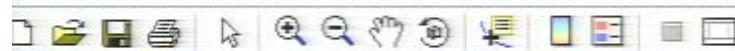
Hold on Line Style - xlim [-1.5 -0.5] Clear
 Area Fill Sigma Level 1 sigma ylim [-1 1] Edit axis labels
 Line Color Grid over plot Saving Feature...
 Grid over plot

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

Page 162/181
Reset FOM



Skin colour Earthy Copper
Background none
Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O... O_k w_0 w_a

70	0.3	0	-1	0
10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix

Use Prior

Observable

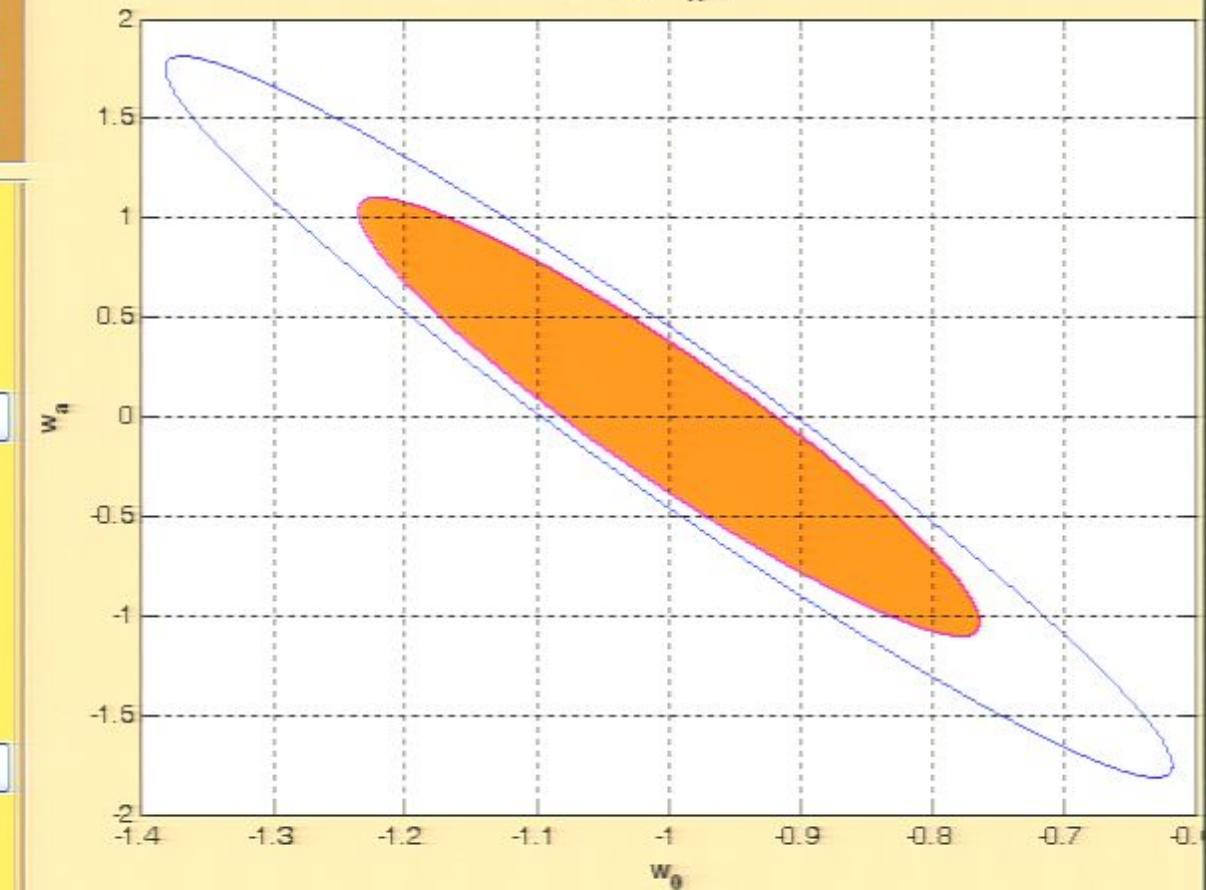
Derivative Type

Data Redshifts

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:
 $H(z)$, $d_A(z)$



Normalise Growth at $z =$ 0

<input checked="" type="checkbox"/> Hold on	Line Style: <input type="button" value="-"/>	<input type="checkbox"/> xlim [-1.5 -0.5]	<input type="button" value="Clear"/>
<input checked="" type="checkbox"/> Area Fill	Sigma Level: <input type="button" value="1 sigma"/>	<input type="checkbox"/> Edit axis labels	
<input type="checkbox"/> Line Color	<input checked="" type="checkbox"/> Grid over plot	<input type="button" value="Saving Features..."/>	
0.058	3.30	1.70	
0.0519	0	0	
0.043			
0.0369			
0.0284			
0.0263			
0.0148			

Figure of Merit = 3.30

DET F (1/Area 2-...)
Reset FOM



Skin colour Earthy Copper
Background none
Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O_m O_k w_0 w_a

70 0.3 0 -1 0

Prior matrix

Use Prior

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Observable

Derivative Type

H d_A G

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

Normalise Growth at $z =$

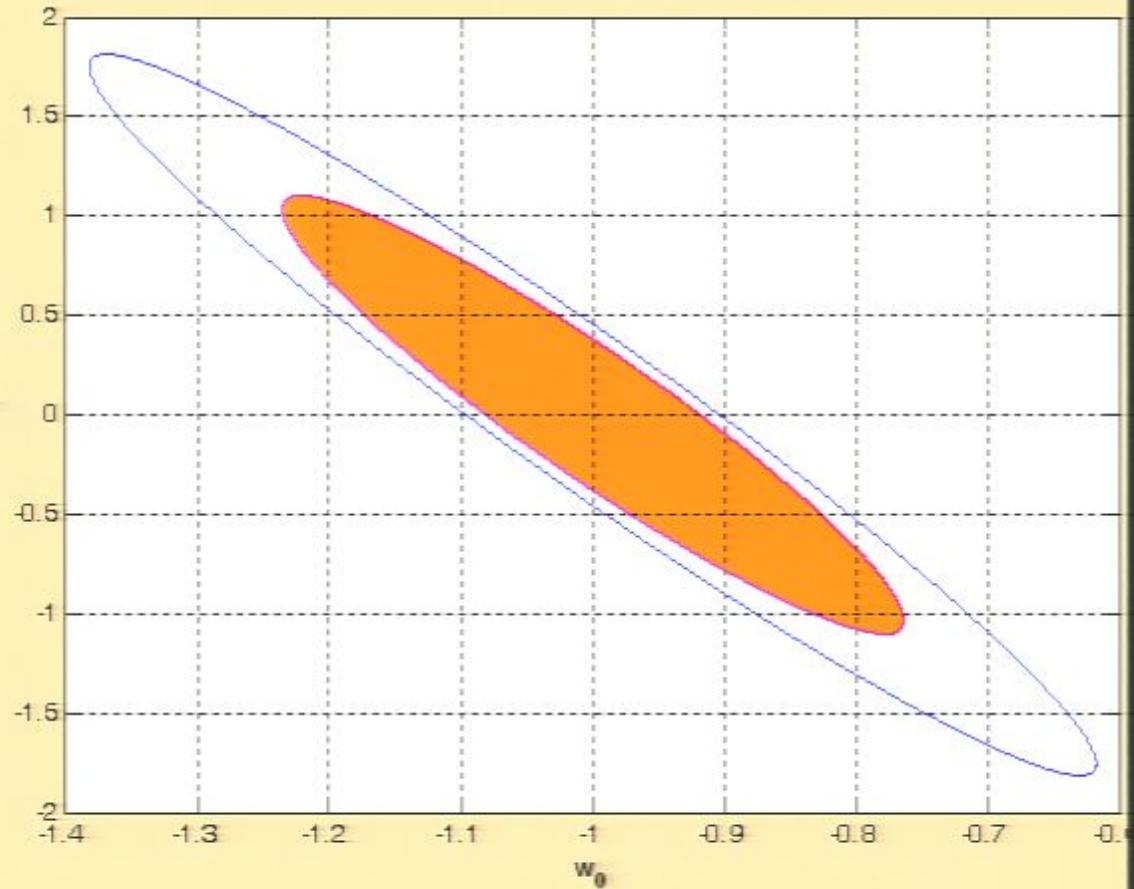
0

0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0253	0.0203
0.0148	0.0119
	0.0022

Fractional Errors on Observables

Pirsa: 09070039

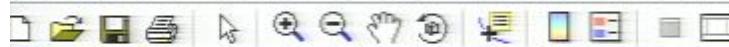
Fisher Error Ellipse for Observables:
 $H(z)$, $d_A(z)$



Hold on Line Style: xlim [-1.5 -0.5] Clear
 Area Fill Sigma Level: ylim [-1 1] DETF (1/Area 2-sigma)
 Line Color Grid: over plot Figure of Merit = 3.30
 Trace(cov)
 sum(cov^2)
 DETF (1/Area 2-sigma)
 Page 164/181
 Reset FOM

Run

Figure of Merit = 3.30



Skin colour Earthy Copper
Background none
Default input Seo & Eisenstein 2003

Parameters

Base parameters

H_0 O_m O_k w_0 w_a

70 0.3 0 -1 0

Prior matrix

Use Prior

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Observable

Derivative Type

H d_A G

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

Normalise Growth at $z =$

0

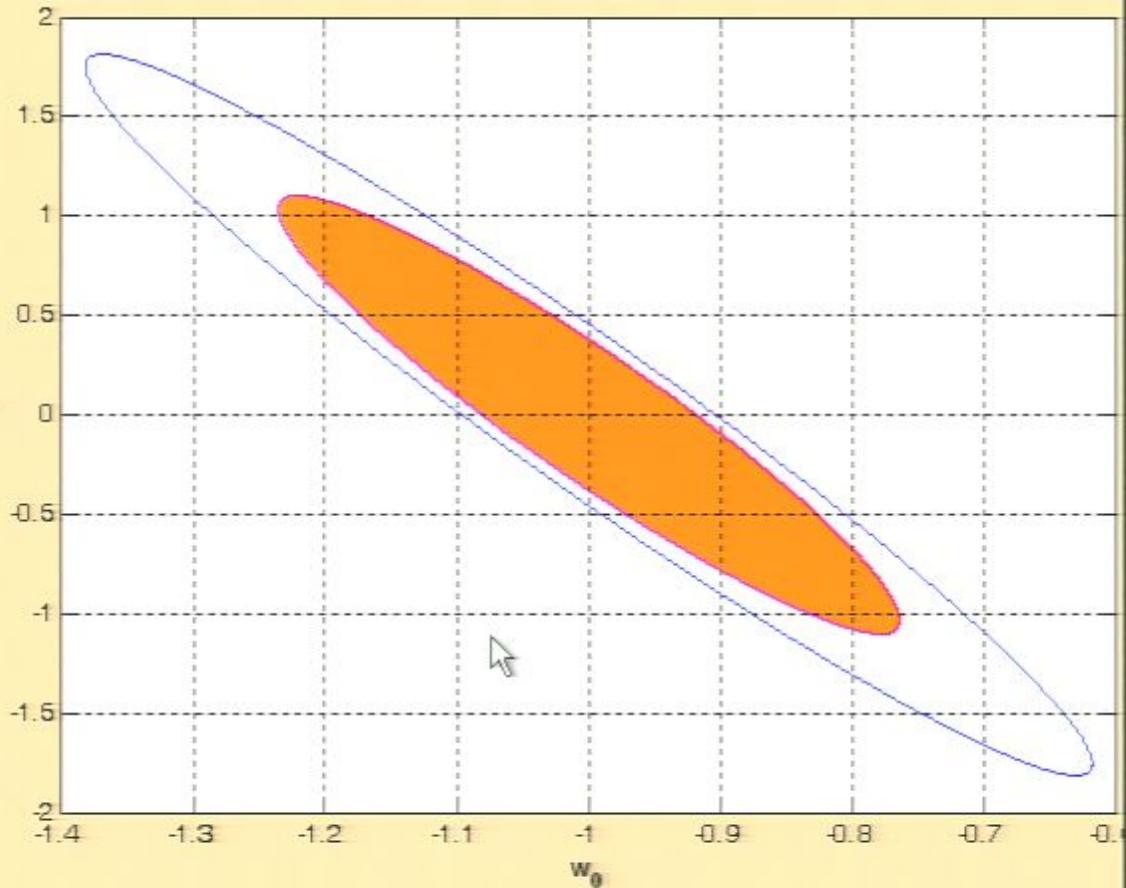
0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0263	0.0203
0.0148	0.0119
	0.0022

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:

$H(z), d_A(z)$



Hold on

Line Style

-

xlim

[-1.6 -0.5]

Clear

Area Fill

Sigma Level

1 sigma

ylim

[-1 1]

Edit axis labels

Line Color

Grid

over plot

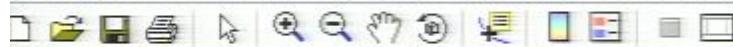
Saving Featur...

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

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Reset FOM



Skin colour

Earthy Copper

Background

none

Default input

none

WMAP

Millenium Simulation

The Matrix

Load from file

Parameters

Base parameters

H_0 O...

70 0.3 0 -1 0

Prior matrix

 Use Prior

Observable

 H d_A G

Derivative Type

Analyti... Analyti... Numerical

0.3

0.6

0.8

1

1.2

3

0.3

0.6

0.8

1

1.2

3

1000

Data Redshifts

Normalise Growth at z = 0

0.058

0.0519

0.0369

0.0284

0.0253

0.0148

0.0519

0.043

0.0322

0.023

0.0203

0.0119

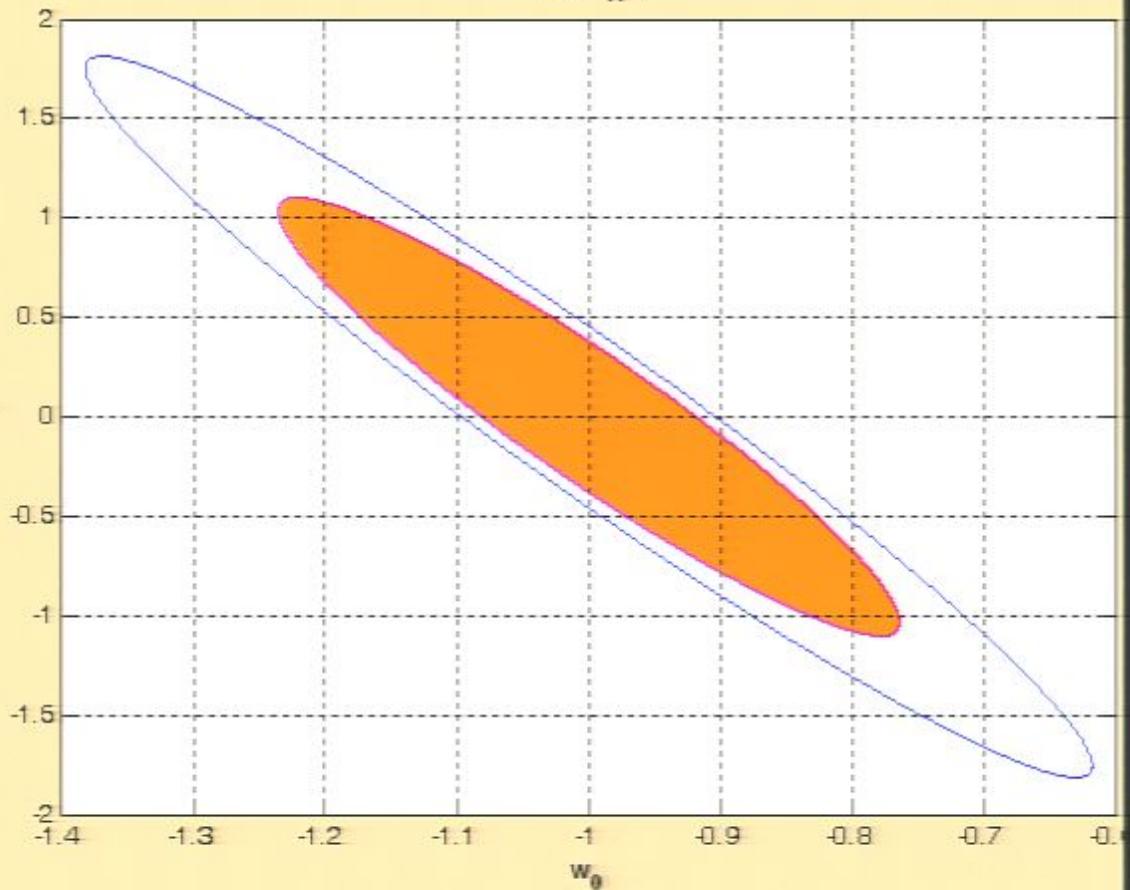
0.0022

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:

H(z), d_A(z)

 Hold on

Line Style

-

xim

[-1.5 -0.5]

Clear

 Area Fill

Sigma Level

1 sigma

yim

[-1 1]

Edit axis labels

 Line Color

Grid

over plot

ylim

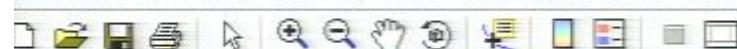
Saving Feature...

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

Page 166/181
Reset FOM



Skin colour: Earthy Copper

Background: WMAP

Default Input: Seo & Eisenstein 2003

Parameters:

 H_0 O_m O_K w_0 w_a

70 0.3 0 -1 0

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix:

 Use Prior

Observable:

 H d_A G

Derivative Type:

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

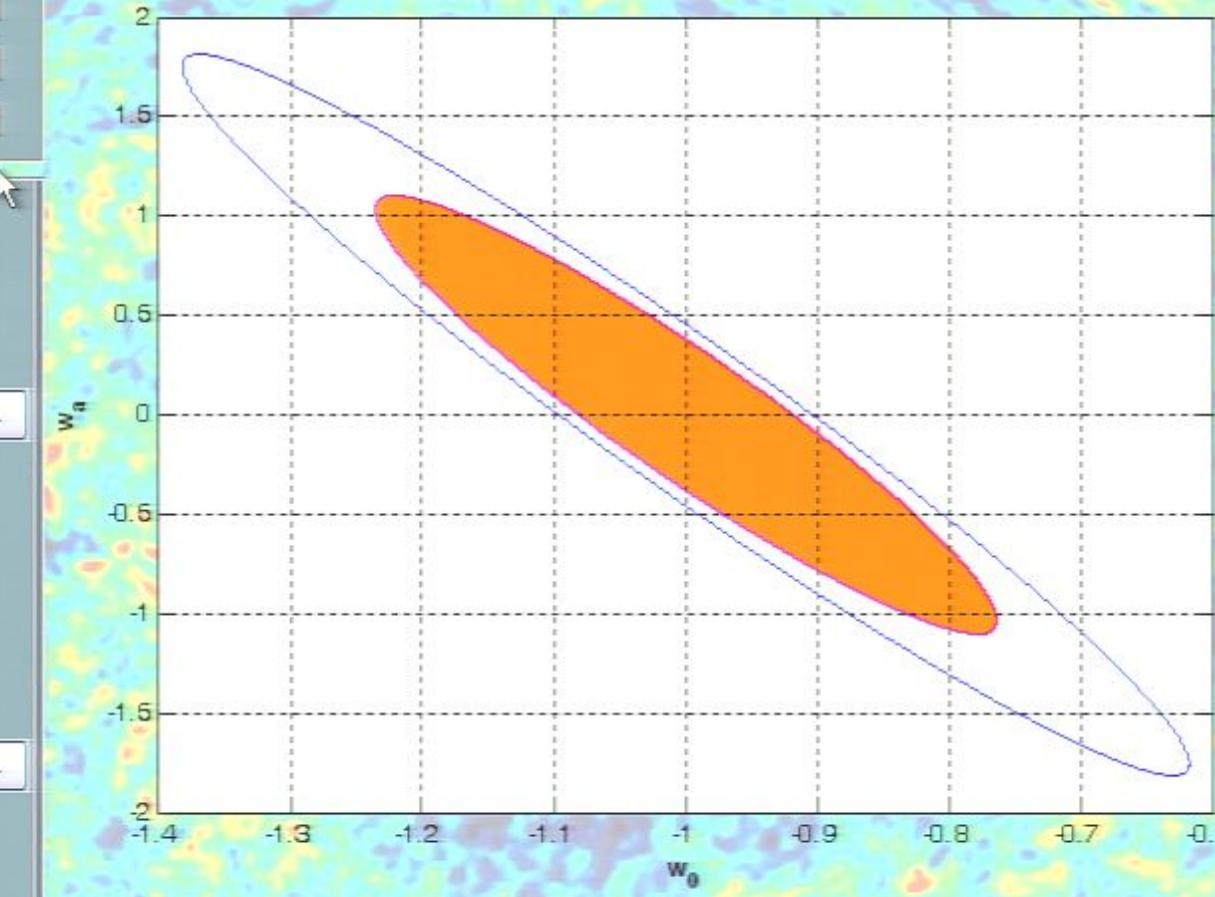
Data Redshifts:

Fractional Errors on Observables:

0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0263	0.0203
0.0148	0.0119
	0.0022

Pirsa: 09070039

Fisher Error Ellipse for Observables:

 $H(z)$, $d_A(z)$ 

Hold on Line Style: - xlim: [-1.5 -0.5] Clear
 Area Fill Sigma Level: 1 sigma ylim: [-1 1] Edit axis labels
 Line Color Grid over plot Saving Feature...
 Grid

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

Page 167/181
Reset FOM



Skin colour: Earthy Copper

Background: WMAP

Default Input: Seo & Eisenstein 2003



Parameters

 H_0 O... O_K w_0 w_a

70 0.3 0 -1 0

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix

 Use Prior

Observable

 H d_A G

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

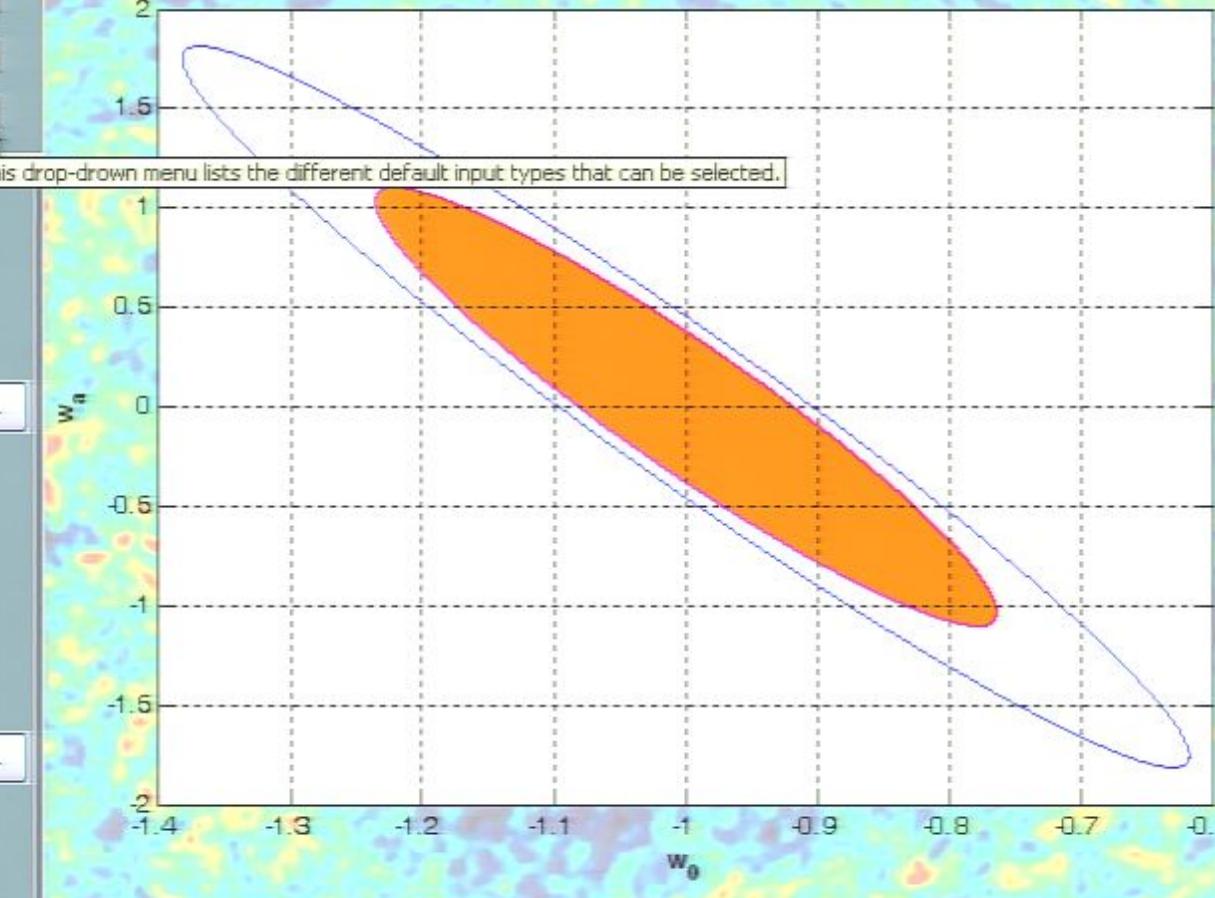
Derivative Type

Data Redshifts

Fractional Errors on Observables

0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0263	0.0203
0.0119	0.0022

This drop-down menu lists the different default input types that can be selected.

Fisher Error Ellipse for Observables:
H(z), d_A(z)

Hold on Line Style: - xlim: [-1.5 -0.5] Clear
 Area Fill Sigma Level: 1 sigma ylim: [-1 1] Edit axis labels
 Line Color Grid over plot Saving Feature...

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

Page 168/181
Reset FoM



Skin colour: Earthy Copper

Background: WMAP

Default Input: Seo & Eisenstein 2003

Parameters

 H_0 O_m O_K w_0 w_a

70 0.3 0 -1 0

10000	0	0	0	0
0	10000	0	0	0
0	0	10000	0	0
0	0	0	0	0
0	0	0	0	0

Prior matrix

 Use Prior

Observable

 H d_A G

Analyti... Analyti... Numerical

0.3	0.3
0.6	0.6
0.8	0.8
1	1
1.2	1.2
3	3
1000	

Derivative Type

Data Redshifts

Normalise Growth at $z =$

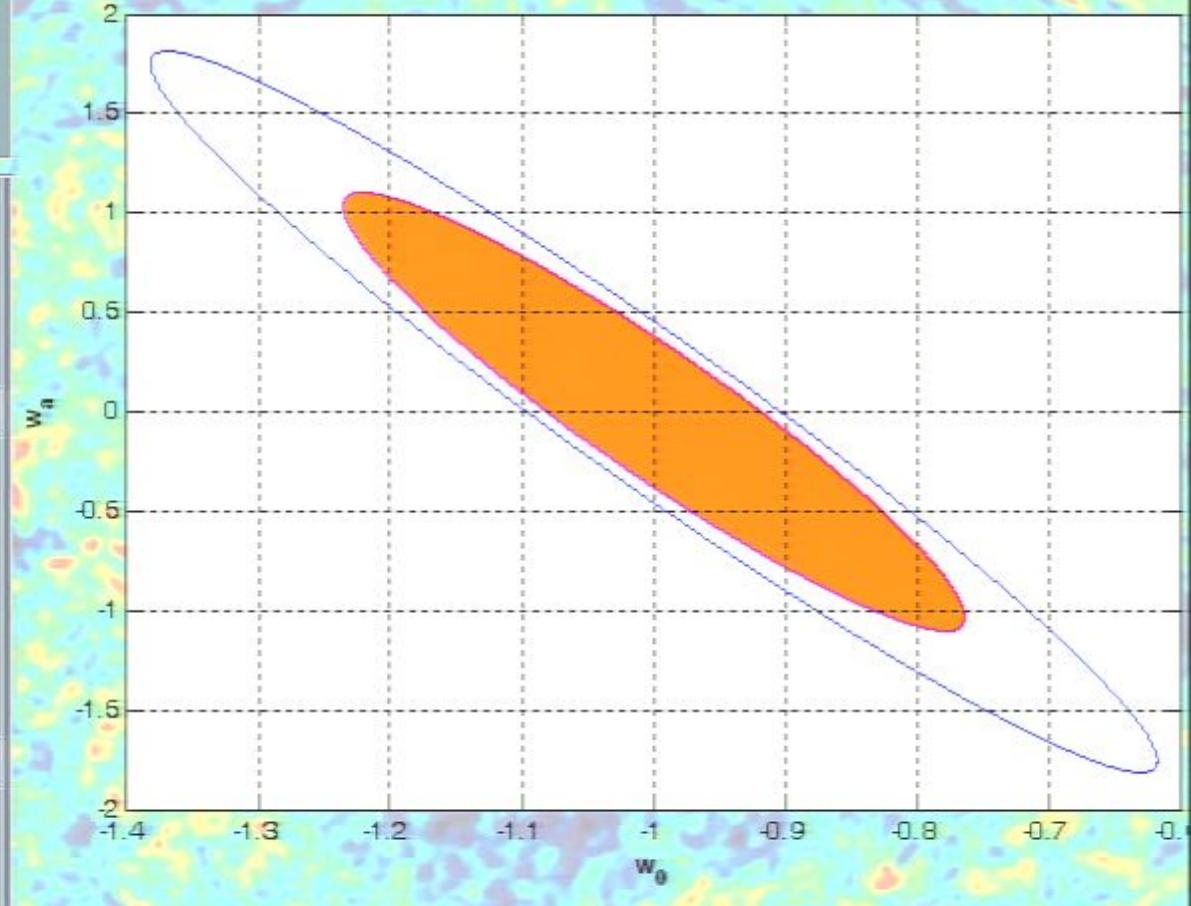
0

0.058	0.0519
0.0519	0.043
0.0369	0.0322
0.0284	0.023
0.0253	0.0203
0.0148	0.0119
	0.0022

Fractional Errors on Observables

Pirsa: 09070039

Fisher Error Ellipse for Observables:

 $H(z), d_A(z)$ 

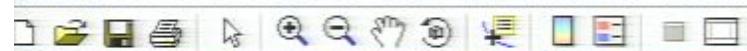
Hold on Line Style: - xlim: [-1.5 -0.5] Clear
 Area Fill Sigma Level: 1 sigma ylim: [-1 1] Edit axis labels
 Line Color Grid: over plot Saving Feature...
 Grid

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

Page 169/181
Reset FoM



Skin colour: Earthy Copper

Background: WMAP

Default Input: Seo & Eisenstein 2003

Parameters

 H_0 O_m O_K w_0 w_a

70 0.3 0 -1 0

```
10000 0 0 0 0
0 10000 0 0 0
0 0 10000 0 0
0 0 0 0 0
0 0 0 0 0
```

Prior matrix

 Use Prior

Observable

 H d_A G

Derivative Type

 Analytic

 Analytic Numerical

Analytical Numerical

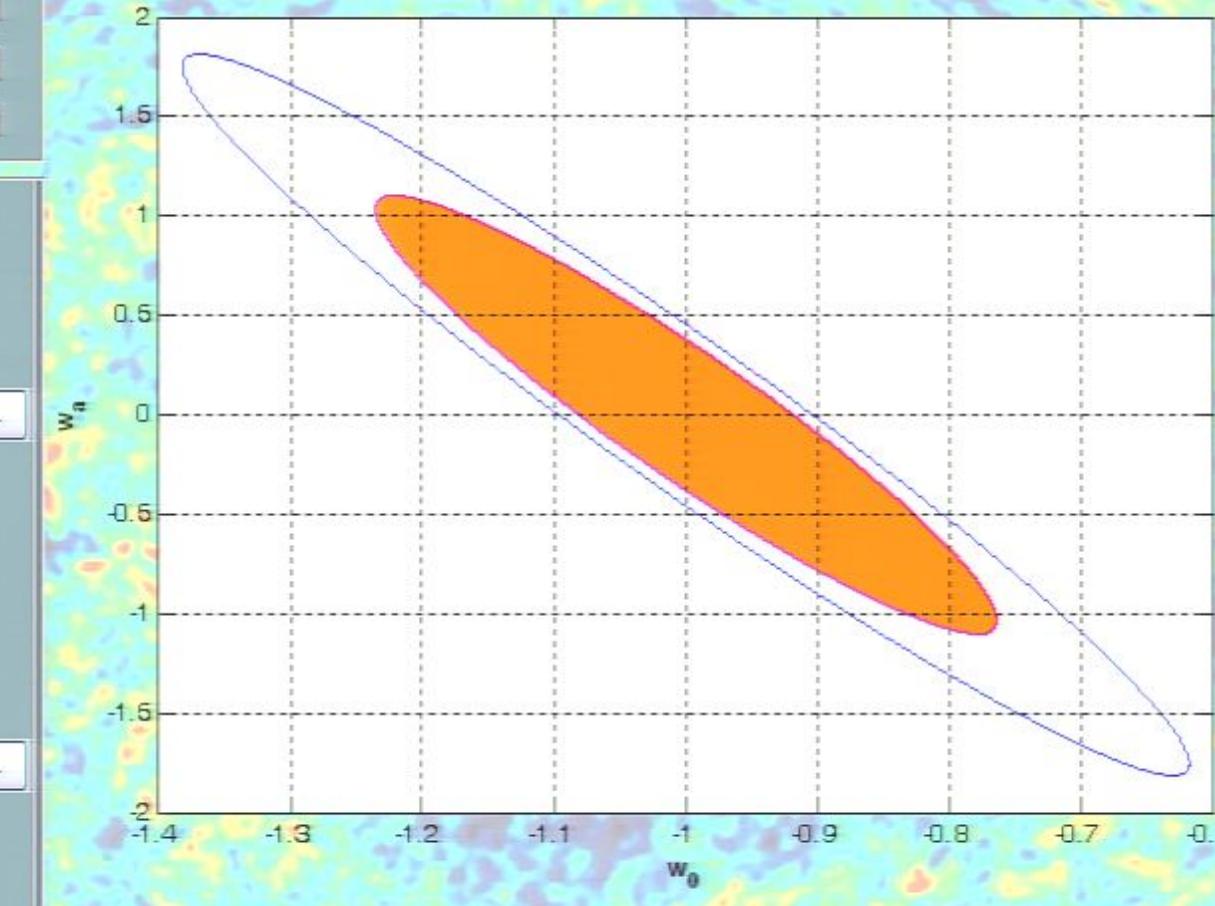
Data Redshifts

0.3 0.6 0.8 1 1.2 3 1000

Fractional Errors on Observables

0.058 0.0519 0.043 0.0369 0.0284 0.0263 0.0148

Fisher Error Ellipse for Observables:

 $H(z), d_A(z)$ 

Hold on Line Style: - xlim: [-1.5 -0.5] Clear

Area Fill Sigma Level: 1 sigma ylim: [-1 1] Edit axis labels

Line Color Grid: over plot Saving Features... Saving Features...

Run

Figure of Merit = 3.30

DETF (1/Area 2-...

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Reset FoM

Editor - D:\Bruce\tex\Fisher Tackle\Stable Releases\version 2.0\FM_GUI.m

File Edit Text Cell Tools Debug Desktop Window Help

Stack: Base

```
1 % -----
2 % Copyright (C) 2008-2009
3 % Bruce Bassett Yabebal Fantaye Renee Hlozek Jacques Kotze
4 %
5 %
6 %
7 % This file is part of Fisher4Cast.
8 %
9 % Fisher4Cast is free software: you can redistribute it and/or modify
10 % it under the terms of the Berkeley Software Distribution (BSD) license.
11 %
12 % Fisher4Cast is distributed in the hope that it will be useful,
13 % but WITHOUT ANY WARRANTY; without even the implied warranty of
14 % MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
15 % BSD license for more details.
16 %
17 %
18 % FM_GUI sets a Gui for the Fisher matrix tacklebox.
19 %
20 % It executes the callbacks which are
21 % USERIN- the input for the GUI. During the first
22 % initialisation of this function, USERIN is zero
23 % which opens the new GUI window. All buttons and controls follow a specific
24 % format as outlined in the Matlab Help files, and indentation is key in
25 % this code. The GUI also contains floating help to aid the user.
26 % For more information on GUI's, please see the Matlab documentation.
27 %
28 %
29 function FM_GUI(USERIN)
30
31 % global axis_spec tacklebox
32
33
34 % if nargin <> 0
```

Editor - D:\Bruce\tex\Fisher Tackle\Papers\isoFoM_movie.m

File Edit Text Cell Tools Debug Desktop Window Help



Stack: Base



```
1 function isoFoM_movie
2 % movie of iso FoM surface - either slice or isosurface
3 % BB 1 June 09
4
5 close all
6 %load v_30_new.mat; old data
7 load new_detf_fom_vol_out.mat % new DETF FoM data
8 %v = v_30_new;
9 v = fom_vol;
10 H=linspace(0.1,5,30); da=linspace(0.1,5,30); G=linspace(0.1,5,30);
11 [x y z] = meshgrid(H,da,G);
12
13 xmin = 0.1;
14 xmax = 5;
15 ymin = 0.1;
16 ymax = 5;
17 zmin = 0.1;
18 zmax = 5;
19 minv = min(min(min(v)));
20 maxv = max(max(max(v)));
21
22 figure(2)
23 whitebg('white') % colour of background
24 %%%%%%%%%%%%%%
25 n = 75; % number of threshold steps
26 step = (maxv-minv). /n; % union step in threshold
27 thresh = minv:step:maxv; % threshold vector
28 %%%%%%%%%%%%%%
29
30 slice_flag = 1; % 1 if slice animation, 0 if union
31
32 nslice = 50;
33
```

Editor - D:\Bruce\tex\Fisher Tackle\Papers\isoFoM_movie.m

File Edit Text Cell Tools Debug Desktop Window Help



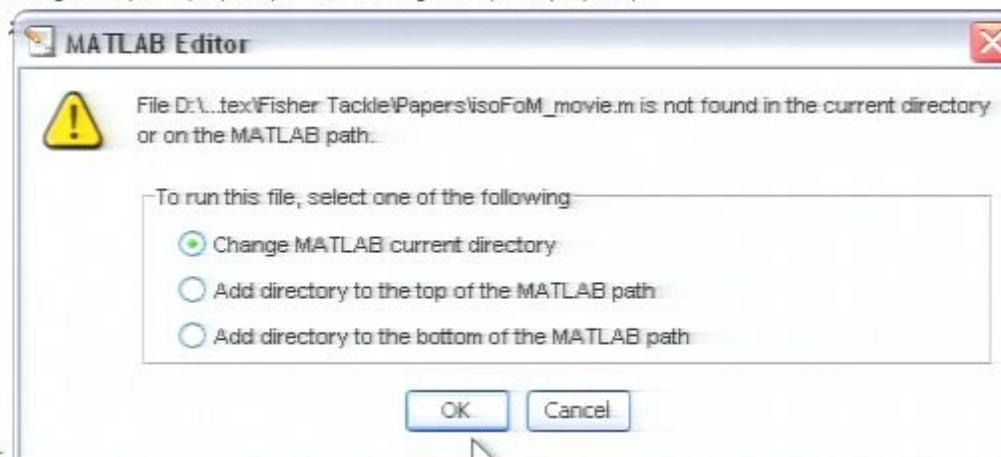
Stack: Base



```

1 function isoFoM_movie
2 % movie of iso FoM surface - either slice or isosurface
3 % BB 1 June 09
4
5 close all
6 %load v_30_new.mat; old data
7 load new_detf_fom_vol_out.mat % new DETF FoM data
8 %v = v_30_new;
9 v = fom_vol;
10 H=linspace(0.1,5,30); da=linspace(0.1,5,30); G=linspace(0.1,5,30);
11 [x y z] = meshgrid(H,da,G);
12
13 xmin = 0.1;
14 xmax = 5;
15 ymin = 0.1;
16 ymax = 5;
17 zmin = 0.1;
18 zmax = 5;
19 minv = min(min(min(v)));
20 maxv = max(max(max(v)));
21
22 figure(2)
23 whitebg('white') % colour
24 %%%%%%%%%%%%%%
25 n = 75; % number of threshold steps
26 step = (maxv-minv). /n; % union step in threshold
27 thresh = minv:step:maxv; % threshold vector
28 %%%%%%%%%%%%%%
29
30 slice_flag = 1; % 1 if slice animation, 0 if union
31
32 nslice = 50;
33

```



Editor - D:\Bruce\tex\Fisher TacklePapers\isoFoM_movie.m

```
File Edit Text Cell Tools Debug Desktop Window Help
1 function isoFoM_movie
2 % movie of iso FoM surface - either slice or
3 % BB 1 June 09
4
5 close all
6 %load v_30_new.mat; old data
7 load new_detf_fom_vol_out.mat % new DETF F
8 %v = v_30_new;
9 v = fom_vol;
10 H=linspace(0.1,5,30); da=linspace(0.1,5,30)
11 [x y z] = meshgrid(H,da,G);
12
13 xmin = 0.1;
14 xmax = 5;
15 ymin = 0.1;
16 ymax = 5;
17 zmin = 0.1;
18 zmax = 5;
19 minv = min(min(min(v)));
20 maxv = max(max(max(v)));
21
22 figure(2)
23 whitebg('white') % colour of background
24 %*****%
25 n = 75; % number of threshold steps
26 step = (maxv-minv). /n; % union step in threshold
27 thresh = minv:step:maxv; % threshold vector
28 %*****%
29
30 slice_flag = 1; % 1 if slice animation, 0 if union
31
32 nslice = 50;
33
```

Figure 2

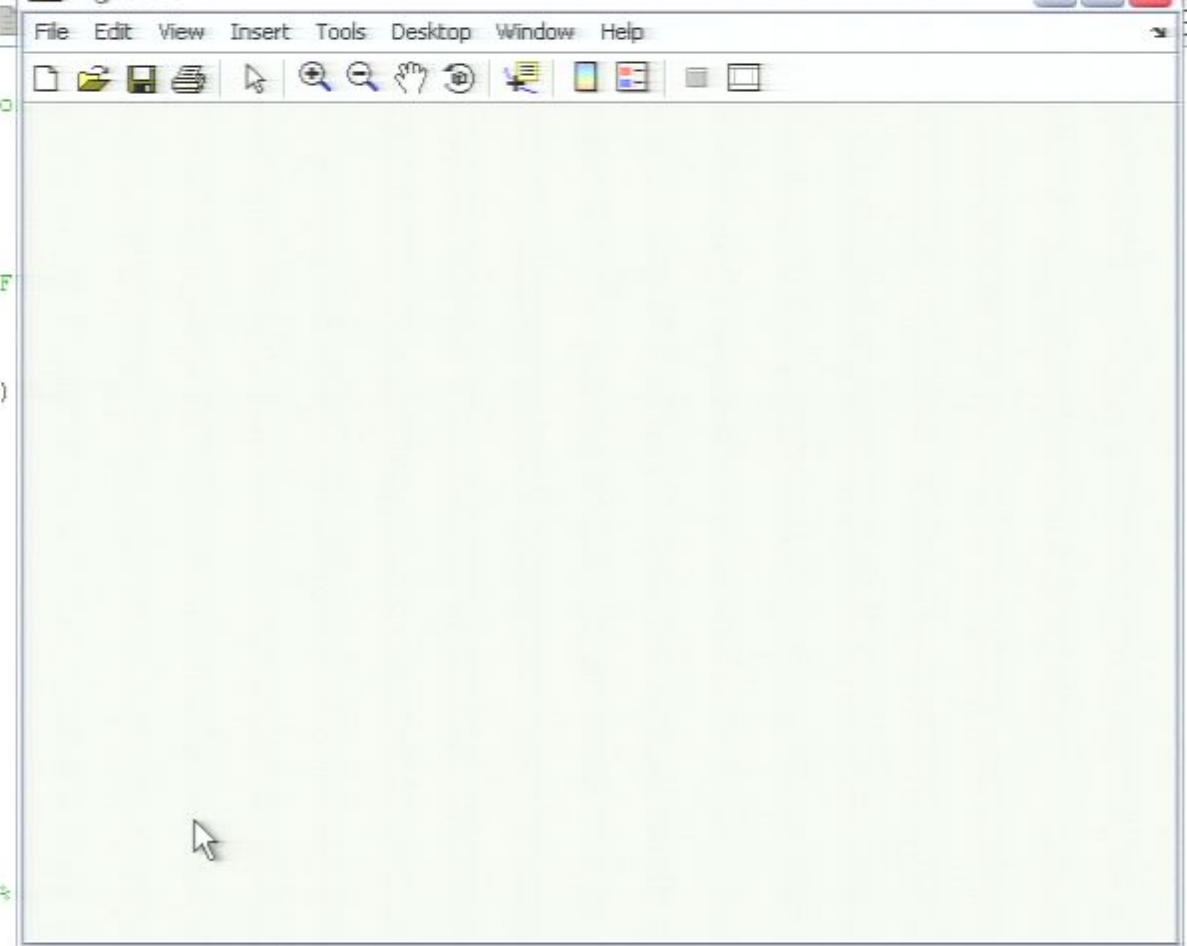


Figure 2

File Edit View Insert Tools Desktop Window Help



Figure 2

File Edit View Insert Tools Desktop Window Help

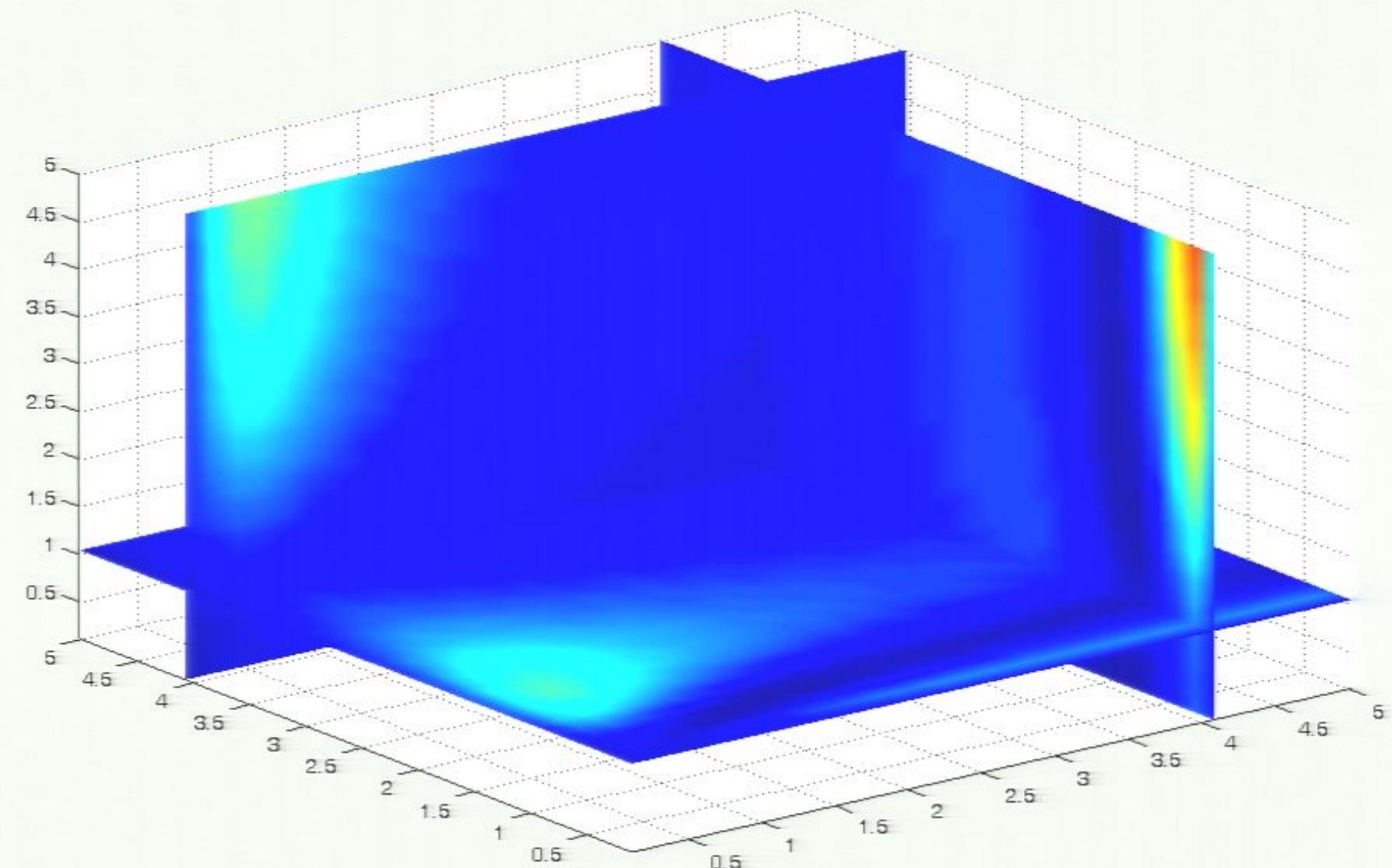
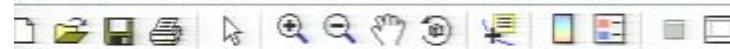


Figure 2

File Edit View Insert Tools Desktop Window Help

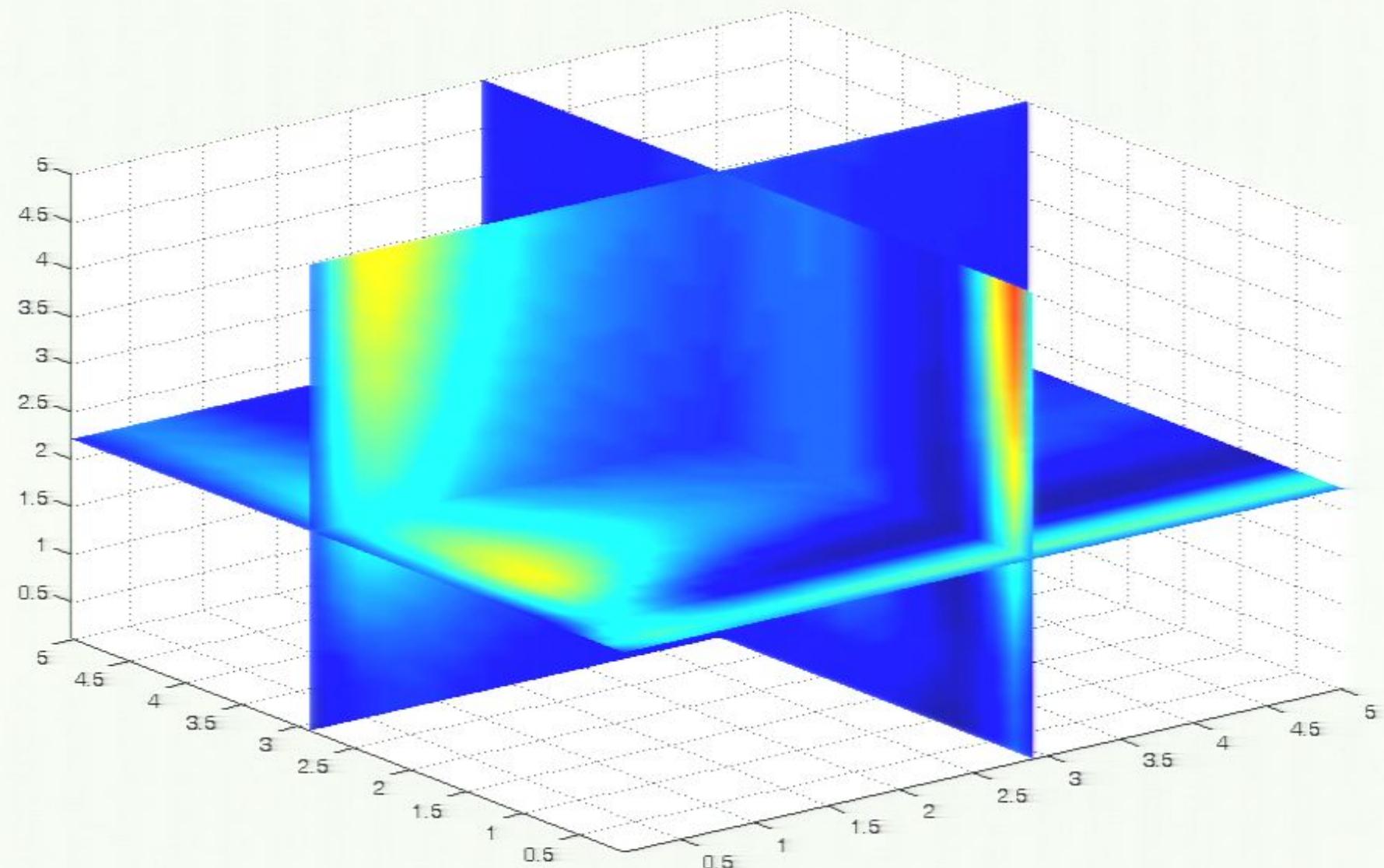
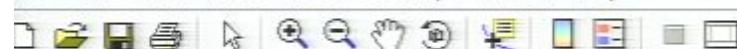


Figure 2

File Edit View Insert Tools Desktop Window Help

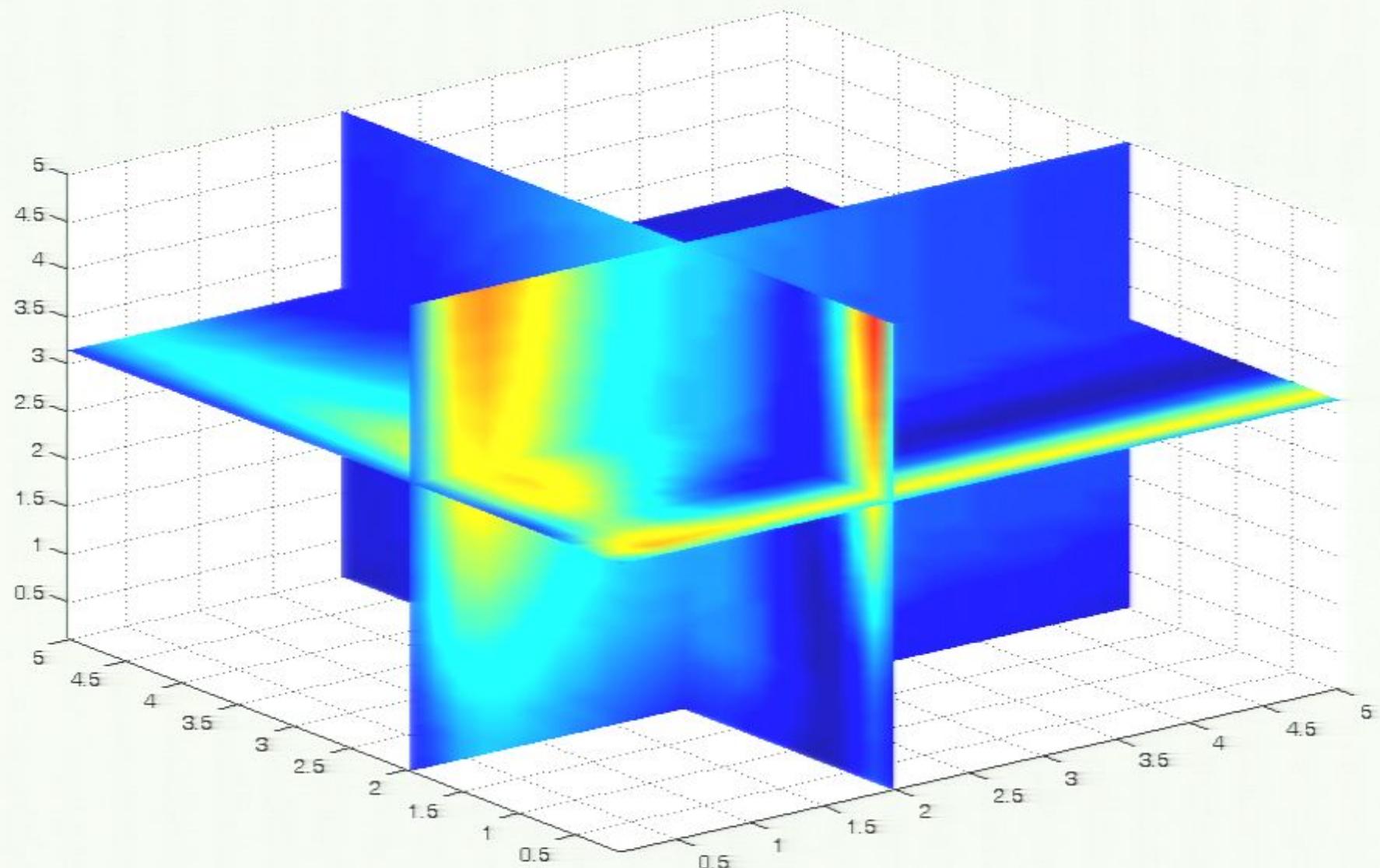
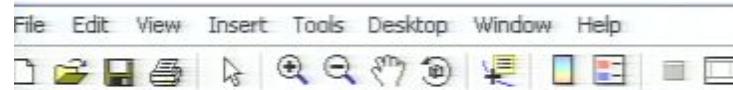


Figure 2

File Edit View Insert Tools Desktop Window Help

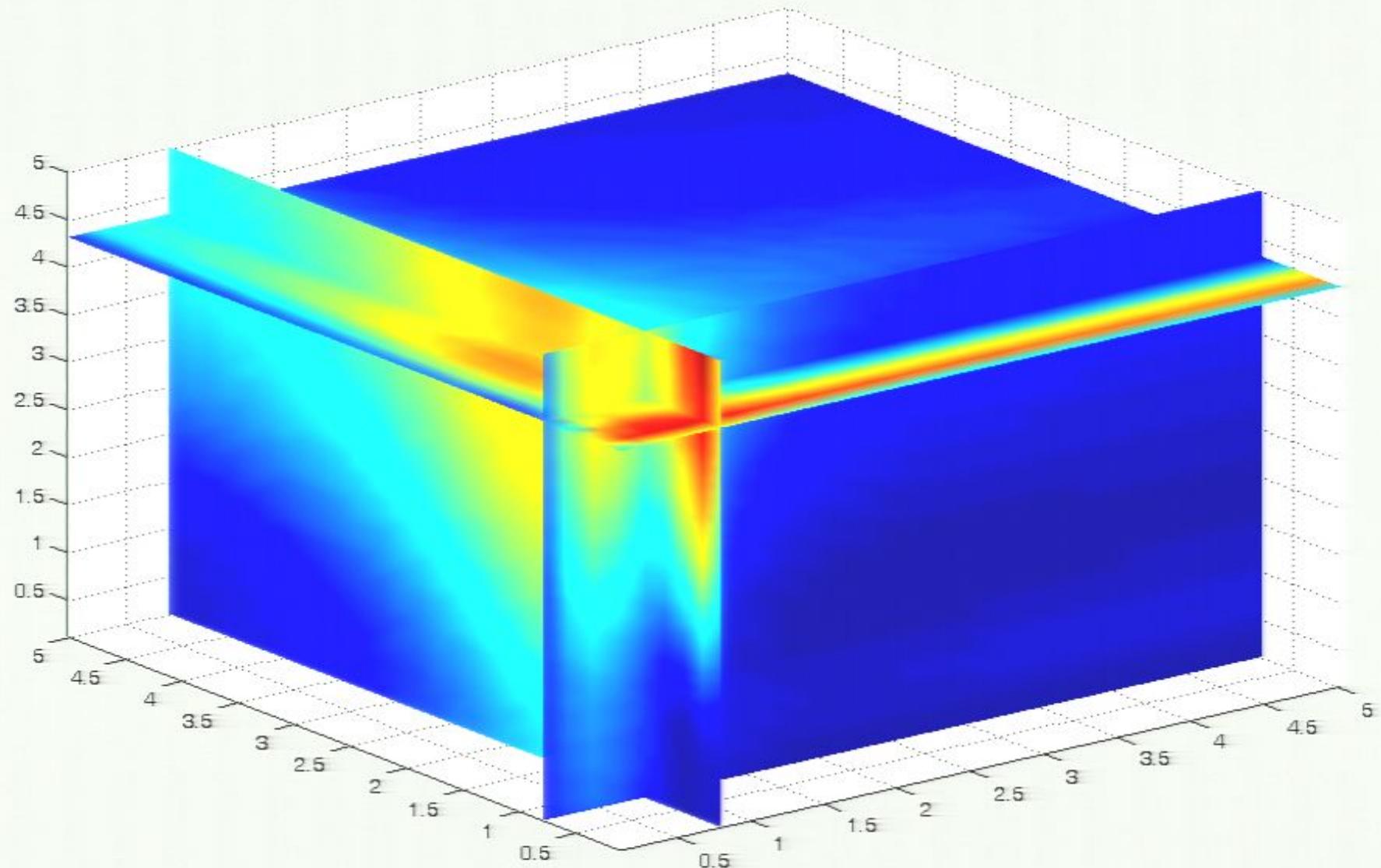
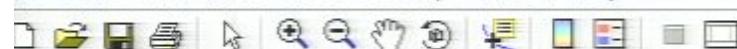
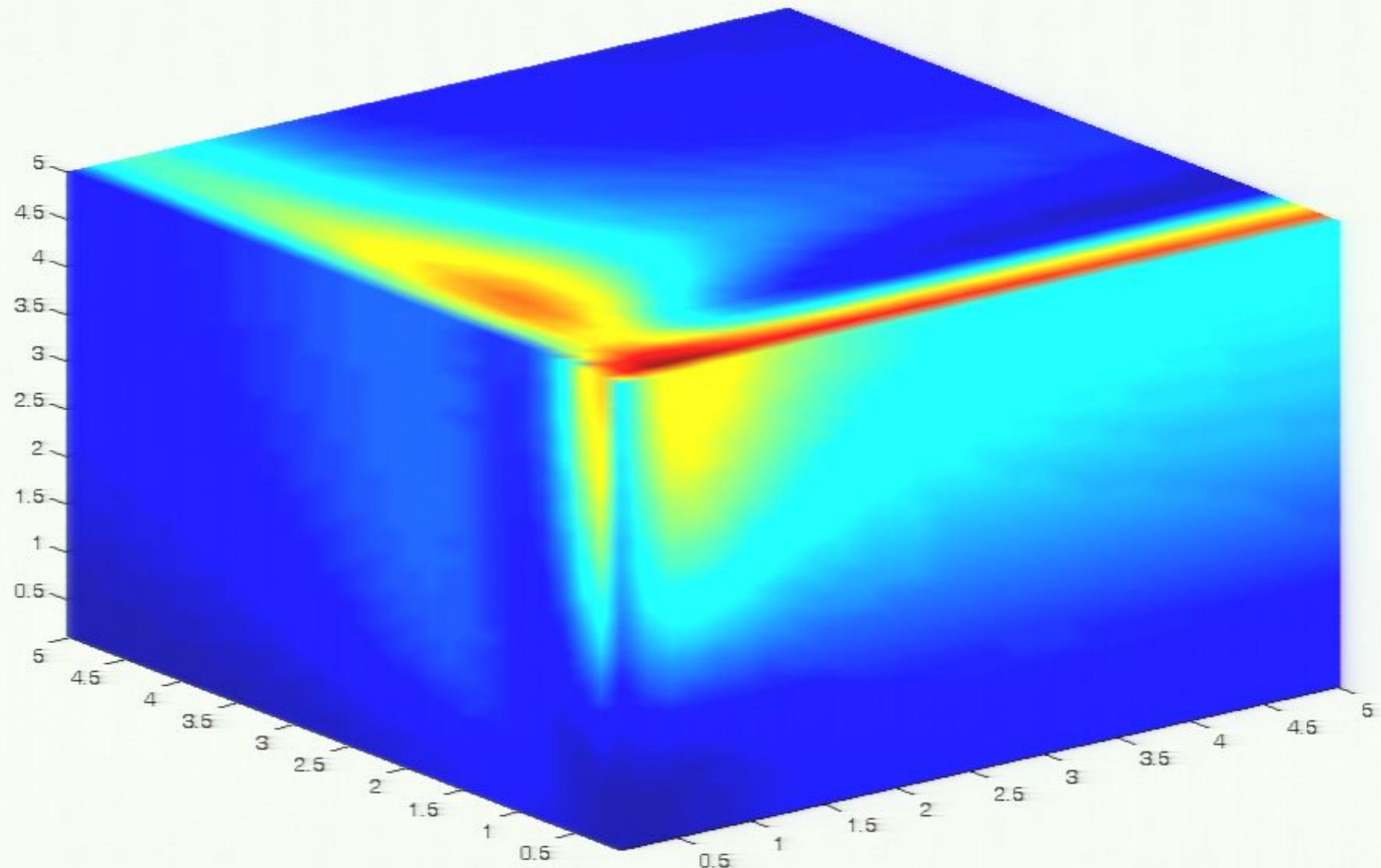
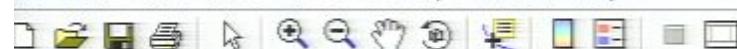


Figure 2

File Edit View Insert Tools Desktop Window Help



Editor - D:\Bruce\tex\Fisher Tackle\Papers\isoFoM_movie.m

File Edit Text Cell Tools Debug Desktop Window Help



```
1 function isoFoM_movie
2 % movie of iso FoM surface - either slice or isosurface
3 % BB 1 June 09
4
5 close all
6 %load v_30_new.mat; old data
7 load new_detf_fom_vol_out.mat % new DETF FoM data
8 %v = v_30_new;
9 v = fom_vol;
10 H=linspace(0.1,5,30); da=linspace(0.1,5,30); G=linspace(0.1,5,30);
11 [x y z] = meshgrid(H,da,G);
12
13 xmin = 0.1;
14 xmax = 5;
15 ymin = 0.1;
16 ymax = 5;
17 zmin = 0.1;
18 zmax = 5;
19 minv = min(min(min(v)));
20 maxv = max(max(max(v)));
21
22 figure(2)
23 whitebg('white') % colour of background
24 %%%%%%%%%%%%%%
25 n = 75; % number of threshold steps
26 step = (maxv-minv)/n; % union step in threshold
27 thresh = minv:step:maxv; % threshold vector
28 %%%%%%%%%%%%%%
29
30 slice_flag = 1; % 1 if slice animation, 0 if union
31
32 nslice = 50;
33
```