

Title: Recent works on holographic cosmology

Date: Jul 07, 2009 11:00 AM

URL: <http://pirsa.org/09070006>

Abstract: My recent works were on new forms of non-gaussianity in CMB from inflationary physics.

Non-Gaussian Spikes from Chaotic Billiards in Inflation Preheating

Lev Kofman

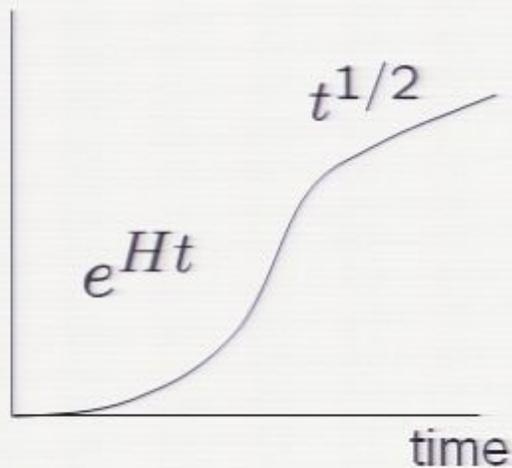
J.R.Bond, A.Frolov, Zh.Huang, LK, arXiv:0903.3407; Phys.Rev.Lett. 2009



Holographic Cosmology Workshop, PI July 7, 2009

Early Universe Inflation

Scale factor $a(t)$



Equation of State $t \leq 10^{-35}$ sec

$$p \approx -\epsilon$$

Inflation $a(t) \approx e^{Ht}$

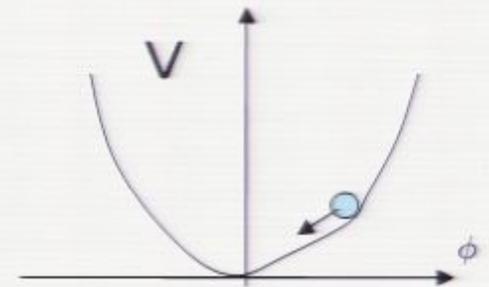
Realization of Inflation

Scalar field

$$\ddot{\phi} + 3H\dot{\phi} + V_{,\phi} = 0$$

$$p = \frac{1}{2}\dot{\phi}^2 - V$$

$$\epsilon = \frac{1}{2}\dot{\phi}^2 + V$$



slow roll $\dot{\phi}^2 \ll V$

choise of $V(\phi)$

Generation of cosmological fluctuations

Scalar metric Fluctuations from Inflation
 $ds^2 = -(1 - 2\Phi)dt^2 + (1 + 2\Phi)a^2d\vec{x}^2$

Initial conditions from Inflation →



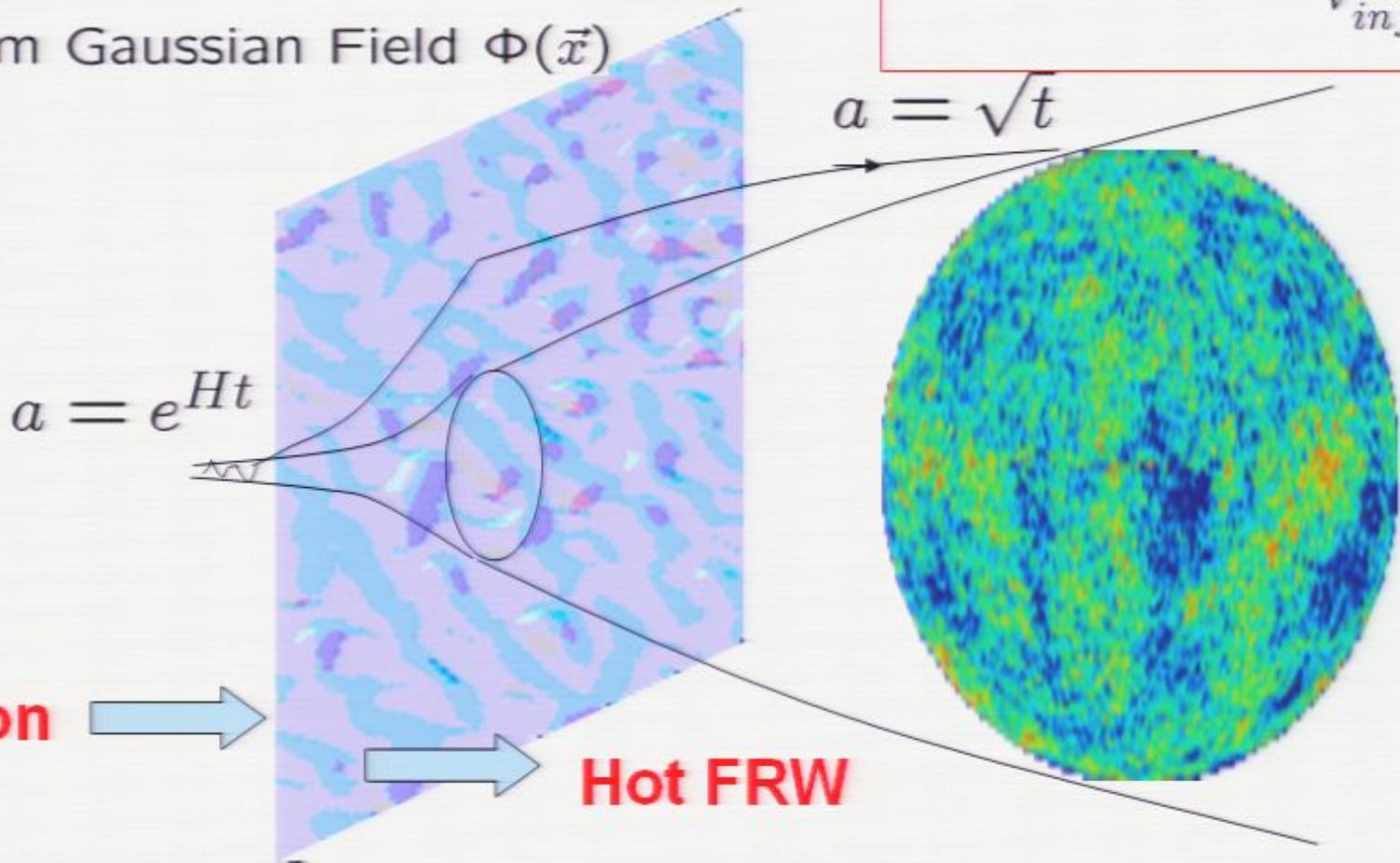
Random Gaussian Field $\Phi(\vec{x})$

$$\Omega_{tot} = 1$$

$$k^3 \Phi_k^2 \rightarrow P_s = A_s k^{n_s - 1}$$

$$P_T = \frac{H^2}{M_p^2} k^{n_T}$$

$$N = 62 - \ln \frac{10^{16} \text{Gev}}{V_{inf}^{1/4}}$$



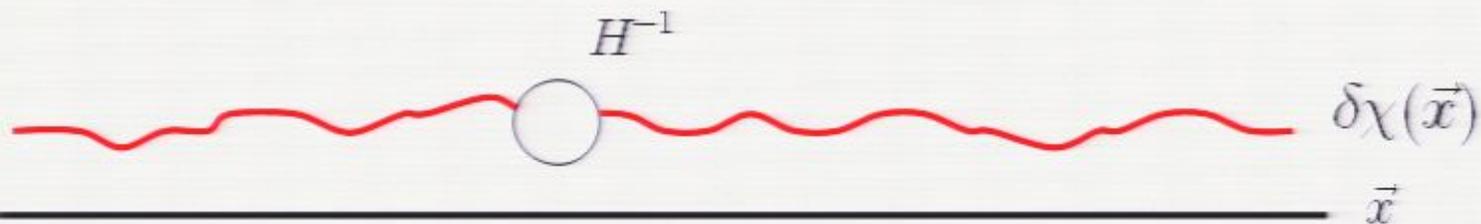
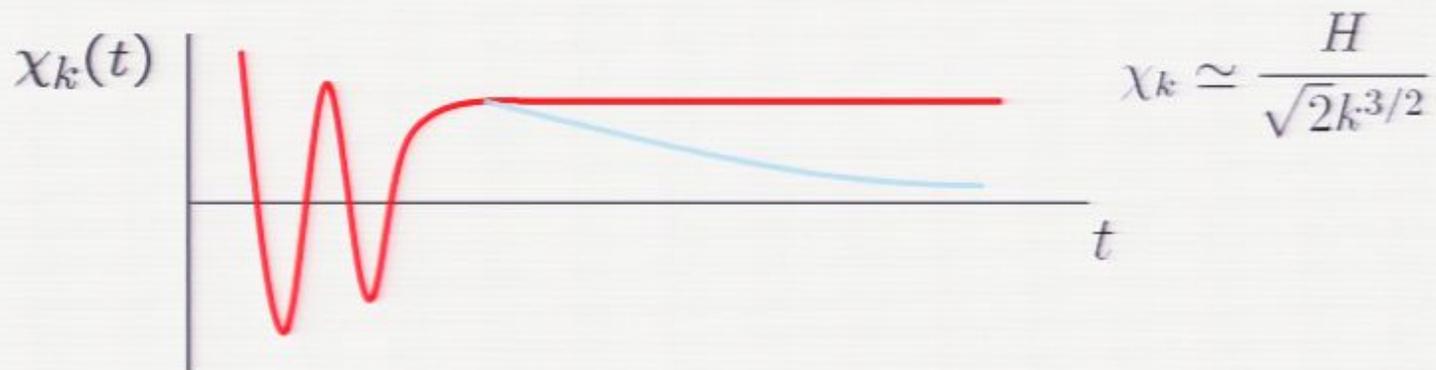
inflation →

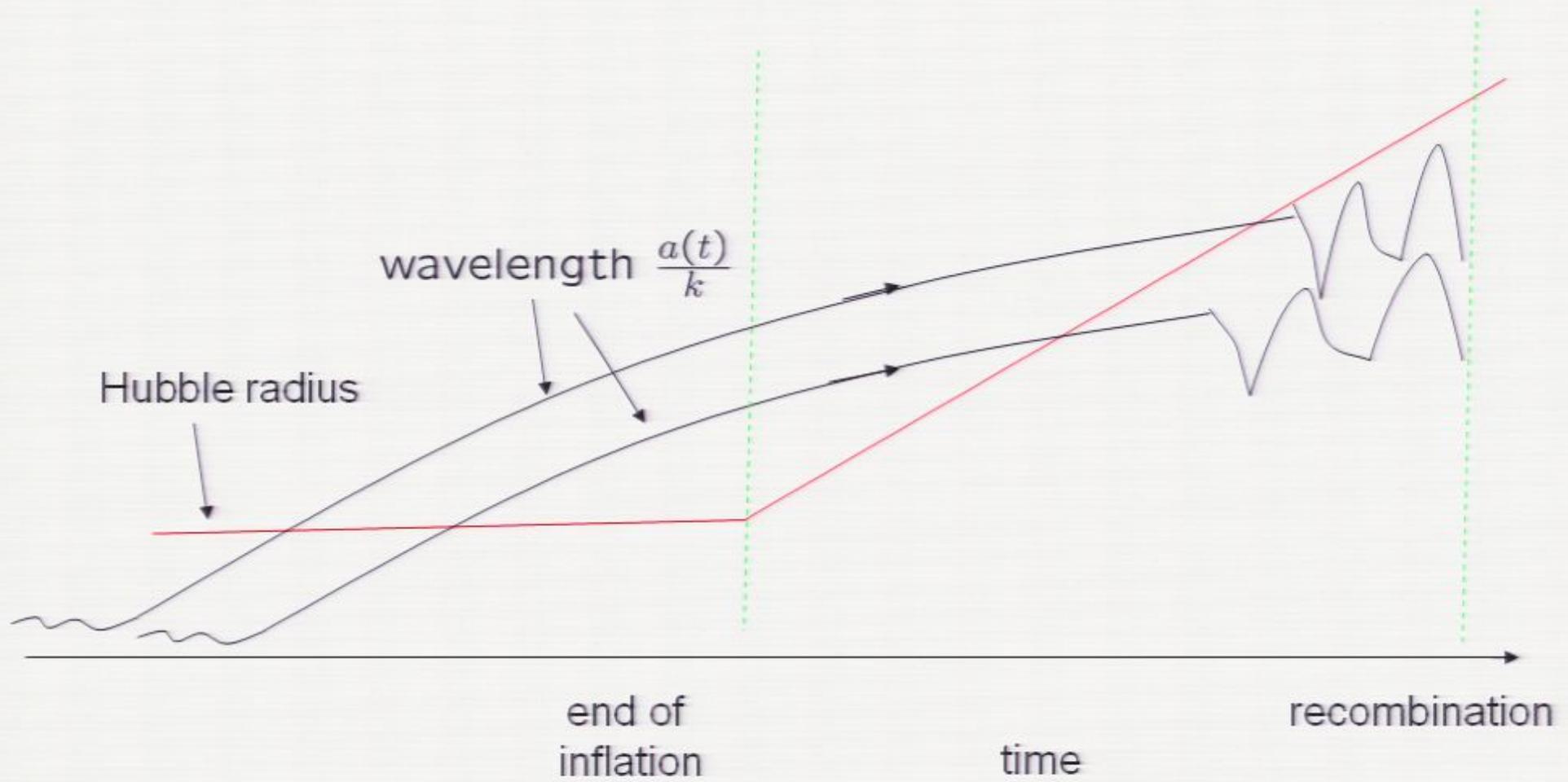
→ **Hot FRW**

Light field at inflation

$$\delta\chi = \int d^3k (a_k \chi_k(t) e^{i\vec{k}\vec{x}} + h.c.)$$

$$\ddot{\chi}_k + 3H\dot{\chi}_k + \frac{k^2}{a^2}\chi_k = 0$$

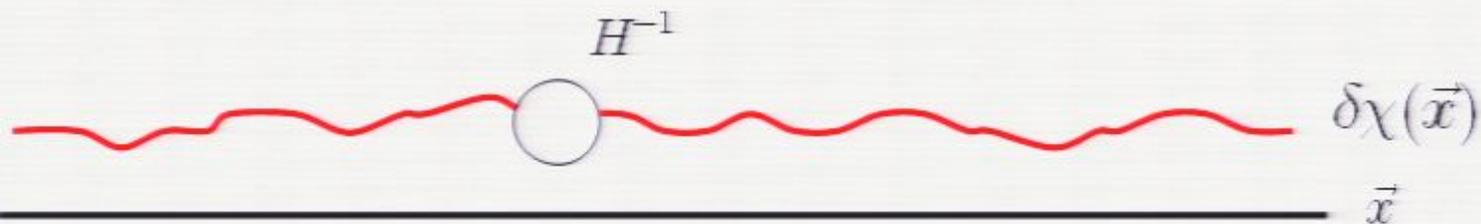
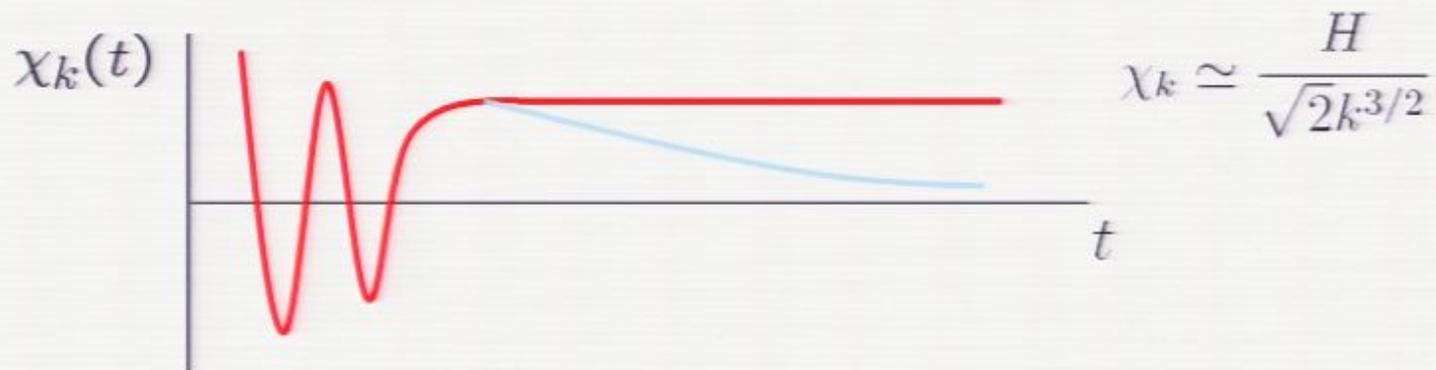


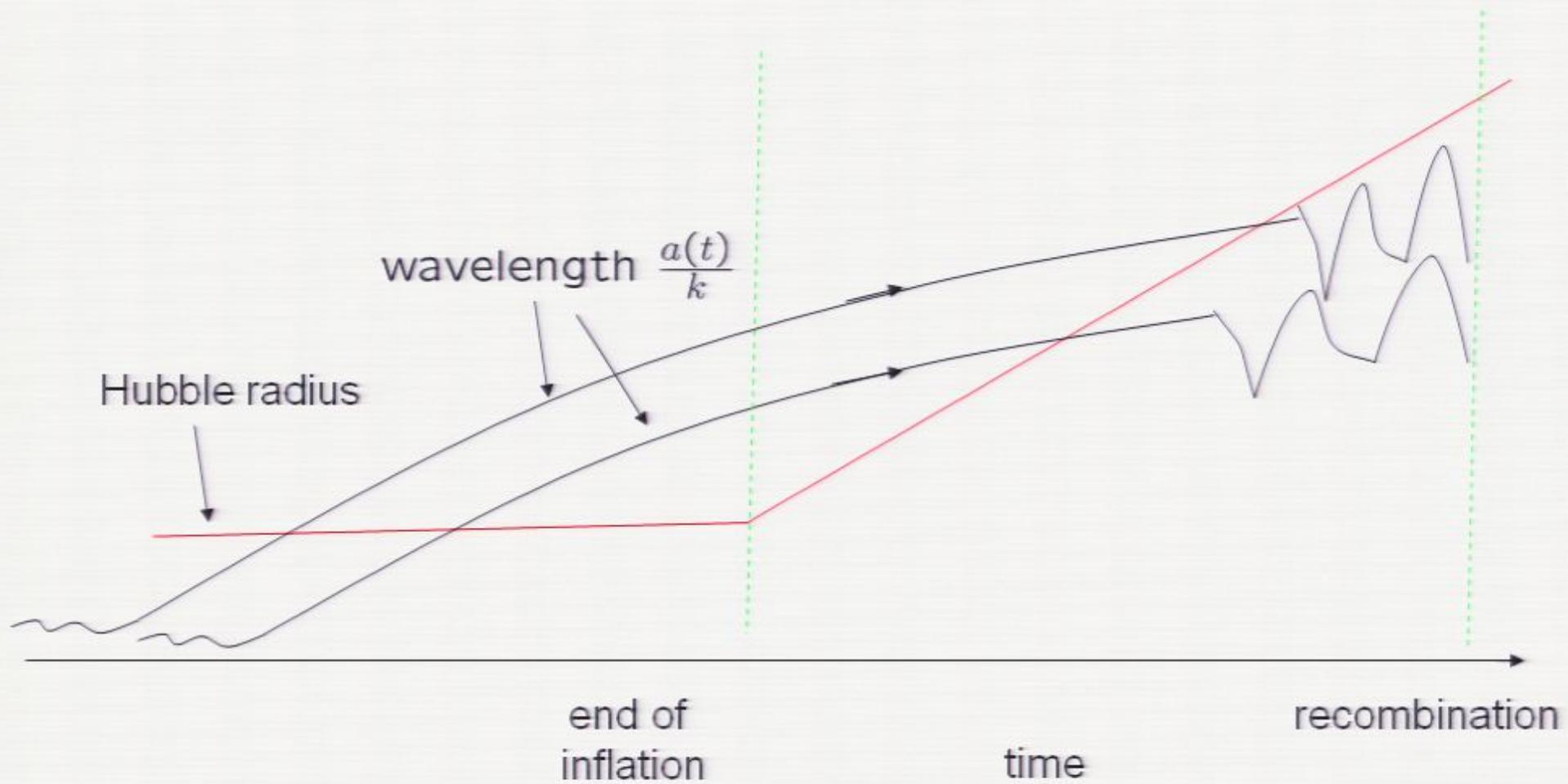


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Scalar metric Fluctuations

$$ds^2 = -(1 - 2\Phi)dt^2 + (1 + 2\Phi)a^2 d\vec{x}^2$$

$$\delta R_{\nu}^{\mu} = \frac{8\pi}{M_p^2} \delta T_{\nu}^{\mu}$$

$$u = a\delta\phi, \quad z = \frac{a\dot{\phi}}{H}, \quad \eta = \int dt/a$$

Scalar field fluctuations

$$\phi(t, \vec{x}) = \phi(t) + \delta\phi(t, \vec{x})$$

$$u_k'' + \left(k^2 - \frac{z''}{z}\right) u_k = 0$$

$$\text{spectrum } P_s(k) = \frac{k^3}{2\pi^2} \left|\frac{u_k}{z}\right|^2 \sim \frac{V^3}{M_p^6 V_{,\phi}^2}$$

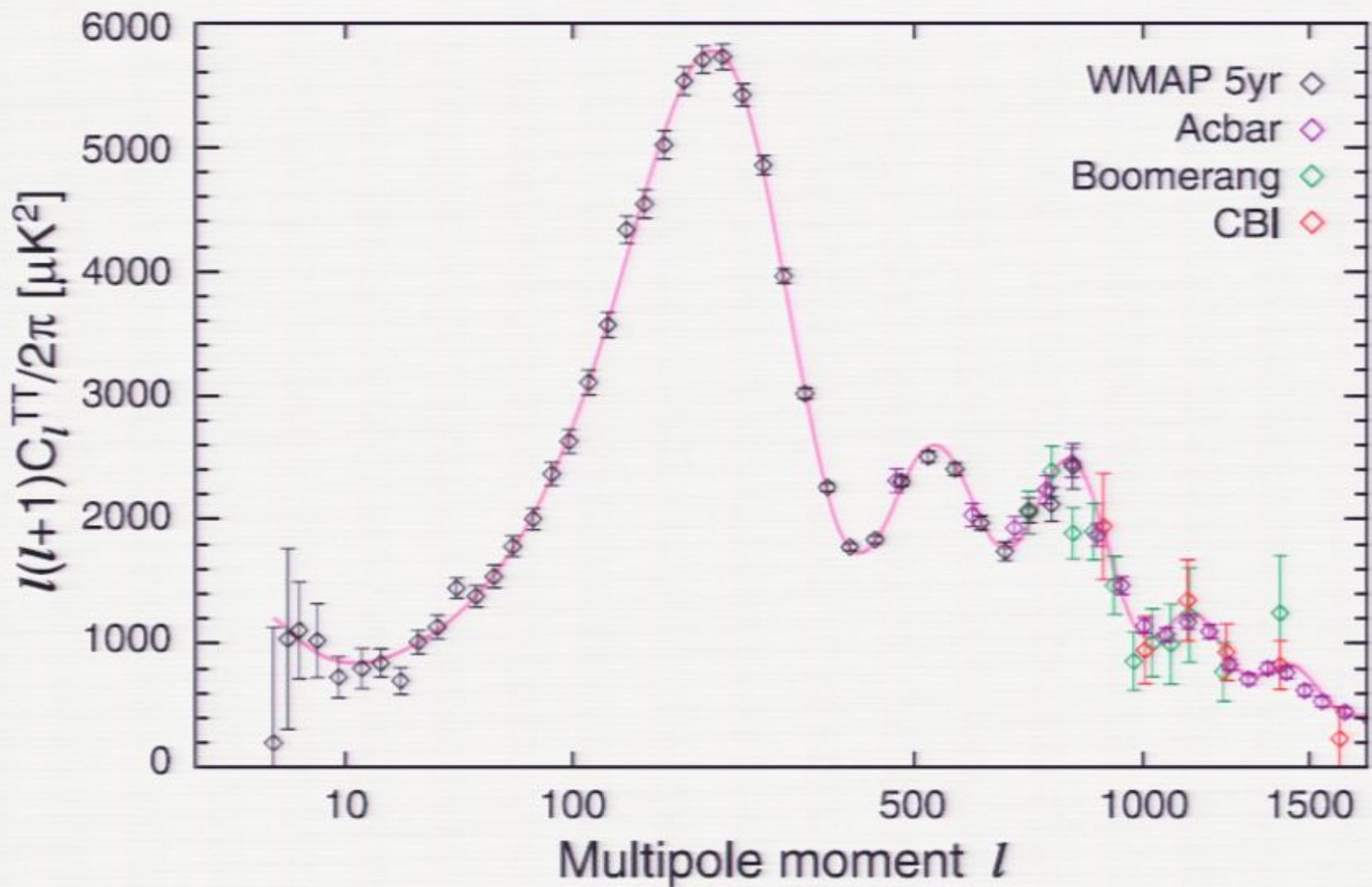
$$k = aH$$

$$\text{often } P_s(k) = A_s \left(\frac{k}{k_*}\right)^{n_s - 1}$$

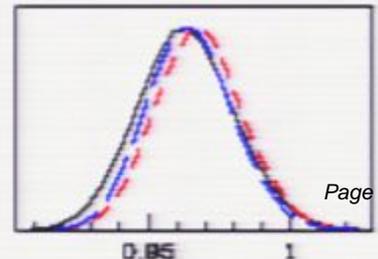
$$V(\phi) \sim \phi^n$$

$$n_s - 1 \approx -\frac{n + 2}{2N}$$

$$V = \frac{1}{2}m^2\phi^2$$
$$V = \frac{1}{4}\lambda\phi^4$$



$$P_s(k) = A_s \left(\frac{k}{k_*} \right)^{n_s - 1}$$

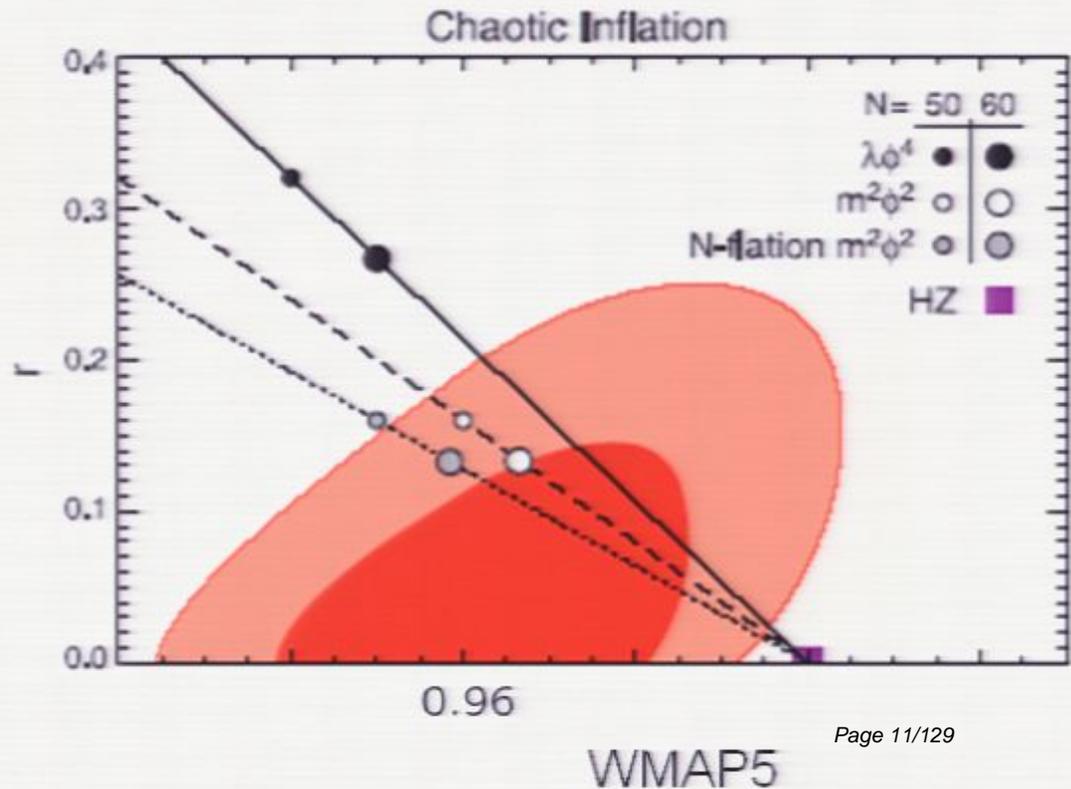
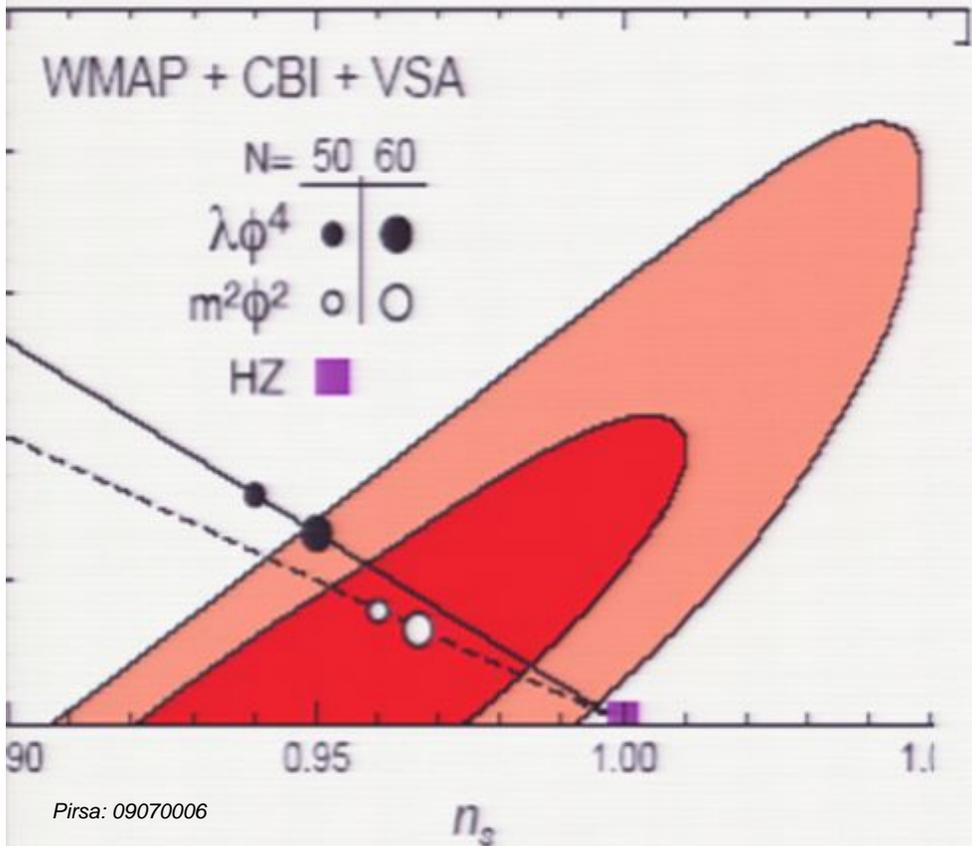


Large field models

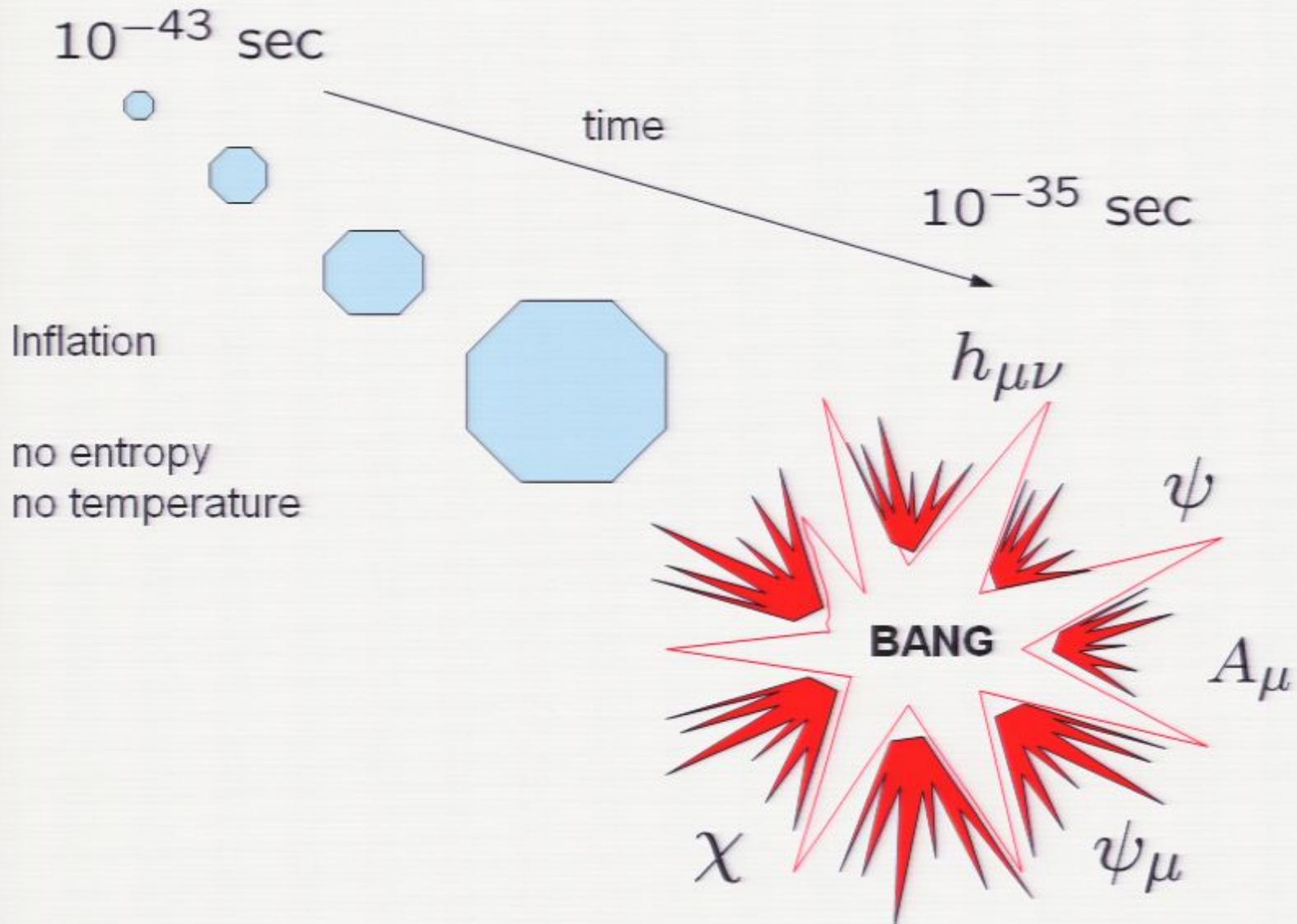
$$V = \phi^n$$

$$n_s - 1 = -\frac{2+n}{2N}$$

$$r = \frac{4n}{N}$$

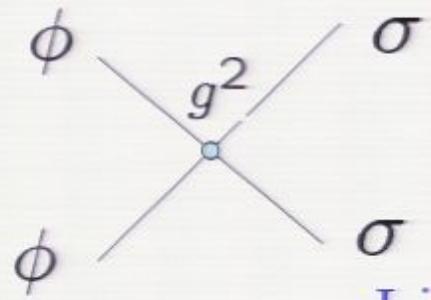


Particlegenesis

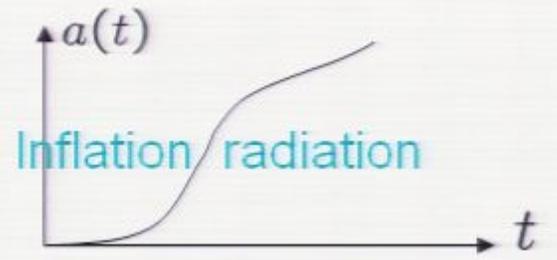


$$g^2 \phi^2 \sigma^2$$

Modulated Fluctuations

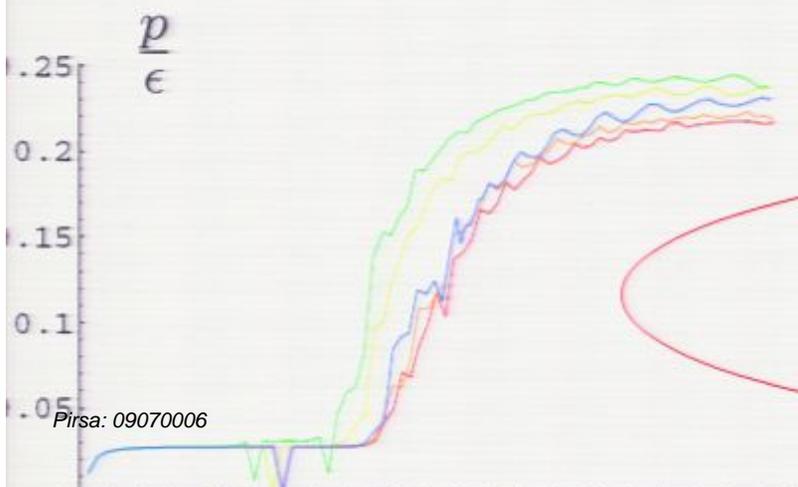
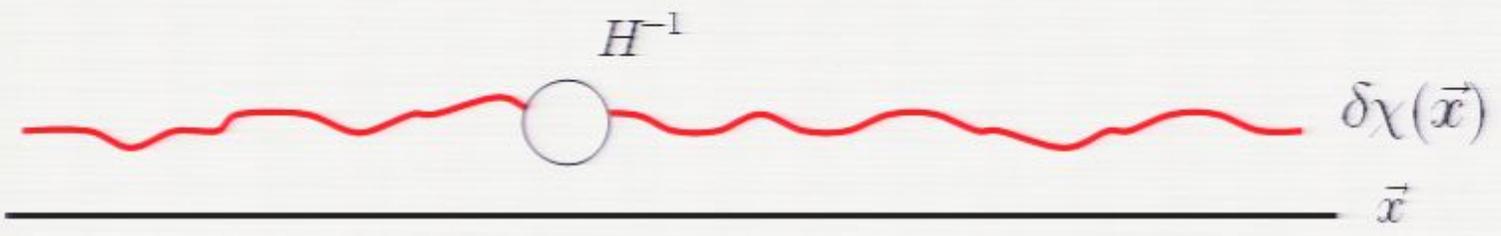


coupling depends on moduli $g^2 = g^2(\chi)$



Light field at inflation develops fluctuations $\chi_k \simeq \frac{H}{\sqrt{2}k^{3/2}}$

spacial variations $\delta g^2 = \frac{\partial g^2}{\partial \chi} \delta \chi$



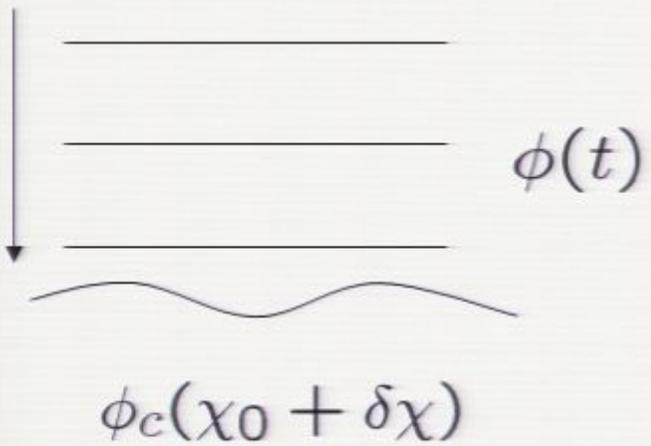
varying $g^2 = 10^{-7}$ by 5%

Generation of metric fluctuations
 $\delta \chi_k \rightarrow \delta g^2 \rightarrow \Phi_k$

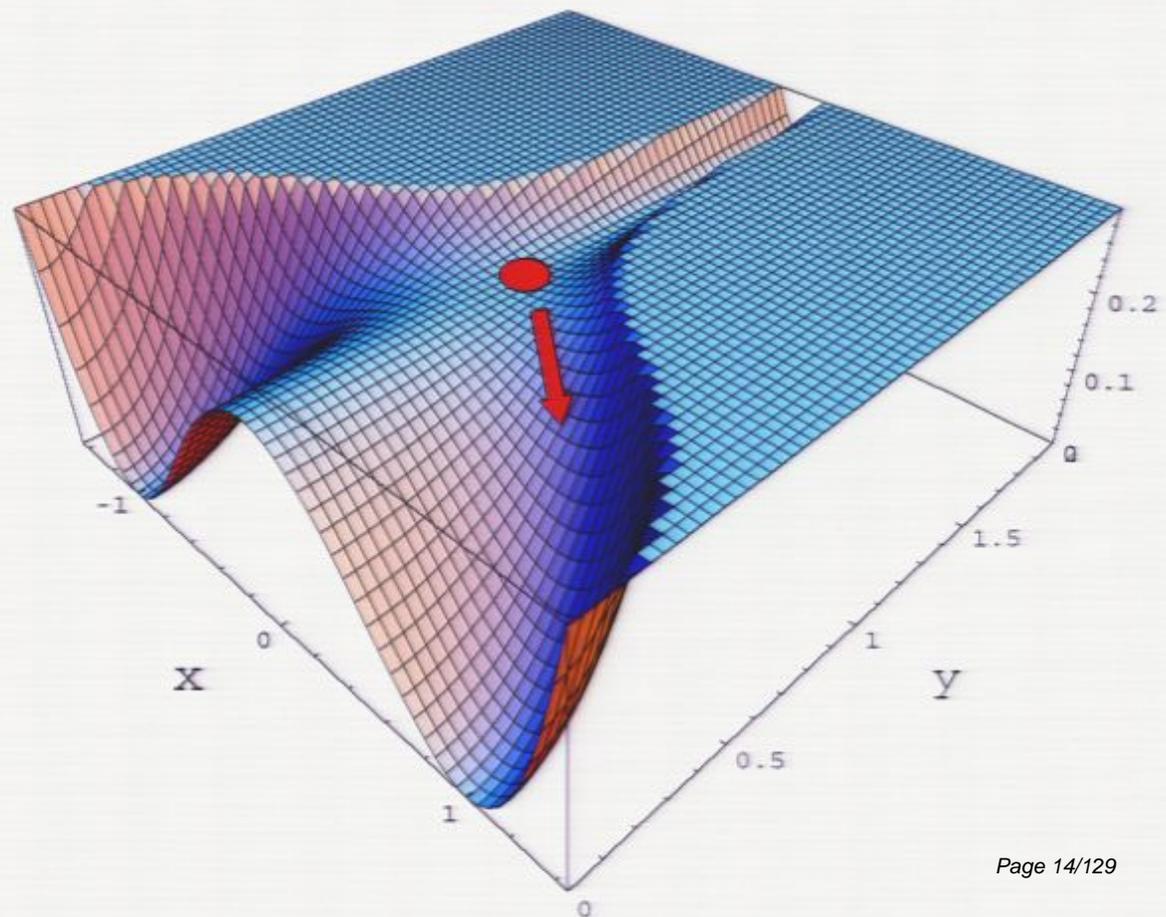
Modulated fluctuations in Hybrid Inflation

$$V(\phi, \sigma) = \frac{\lambda}{4}(\sigma^2 - v^2)^2 + \frac{g^2}{2}\phi^2\sigma^2$$

bifurcation point $\phi_c = \frac{\sqrt{\lambda}v}{g}$



inhomogeneous waterfall



Non-Gaussianity theory

$$\Phi = \Phi_G + f_{NG}^{local} (\Phi_G^2 - \langle \Phi^2 \rangle)$$

single field $f_{NL} = \frac{1}{4}(n_s - 1) \sim 0.01$

modulated/curvaton $f_{NL} \simeq 1$

multiple fields/non-canonical kinetic f_{NL} any

Modulated fluctuations in Hybrid Inflation

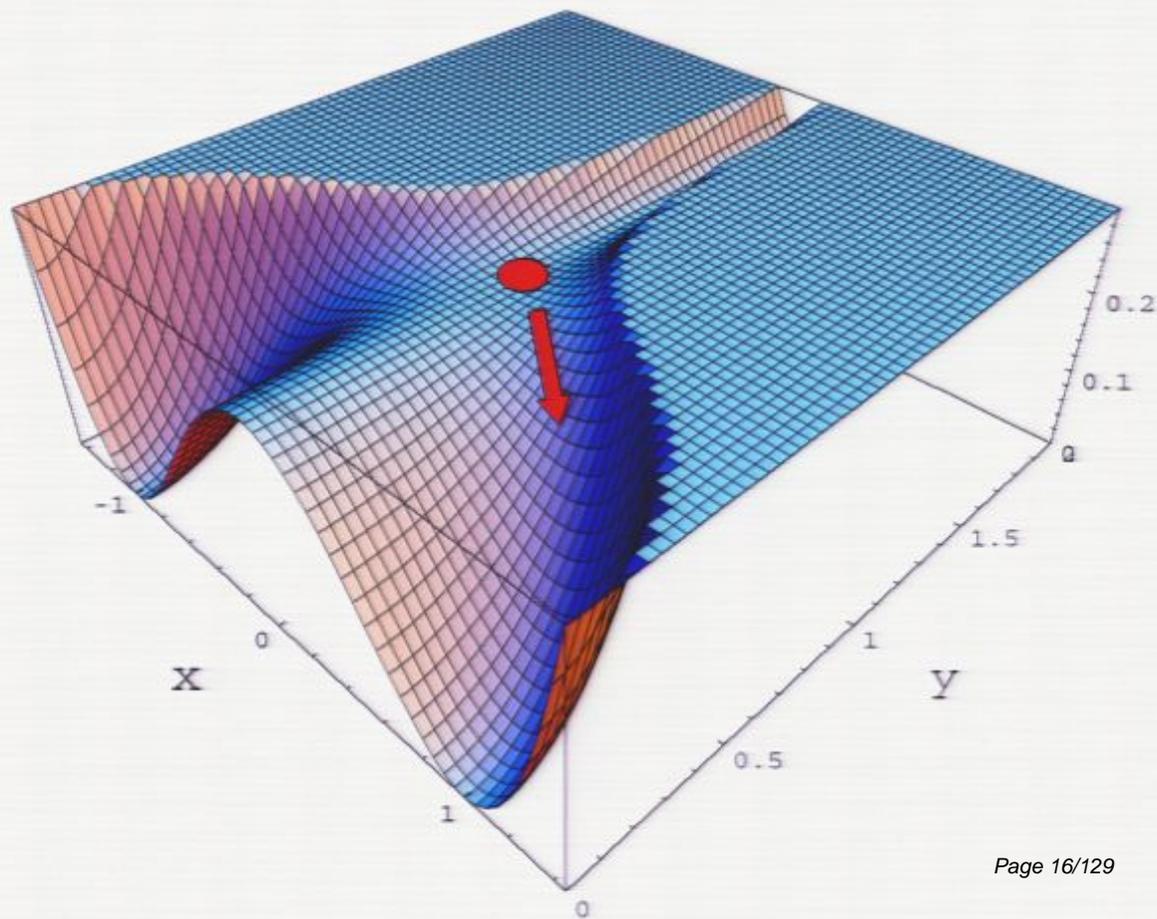
$$V(\phi, \sigma) = \frac{\lambda}{4}(\sigma^2 - v^2)^2 + \frac{g^2}{2}\phi^2\sigma^2$$

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$$\phi_c(\chi_0 + \delta\chi)$$

inhomogeneous waterfall



Non-Gaussianity theory

$$\Phi = \Phi_G + f_{NG}^{local} (\Phi_G^2 - \langle \Phi^2 \rangle)$$

single field $f_{NL} = \frac{1}{4}(n_s - 1) \sim 0.01$

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Non-Gaussianity data

$$\Phi = \Phi_G + f_{NL}^{local} (\Phi_G^2 - \langle \Phi^2 \rangle)$$

WMAP5 $-9 < f_{NL}^{local} < 111$ at 95% C.L.

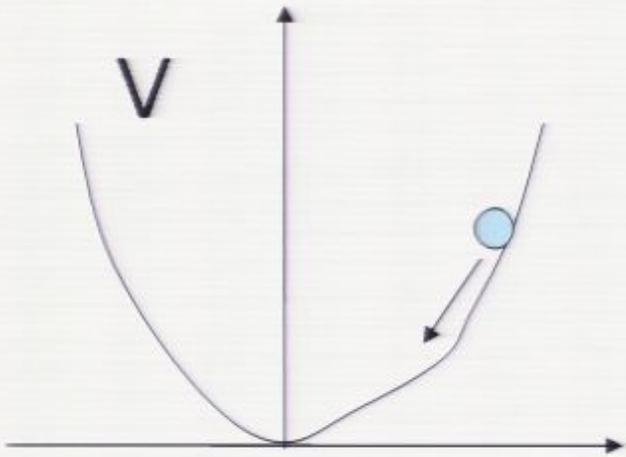
WMAP5+SDSS $-1 < f_{NL}^{local} < 70$ at 95% C.L.

Planck $\Delta f_{NL}^{local} \simeq 4$

CMBPol $\Delta f_{NL}^{local} \sim 2 - 3$

LSS $\Delta f_{NL}^{local} \sim 1$

EUCLID(SPACE+DUNE) $\Delta f_{NL}^{local} \sim 0.2$



$$V(\phi) = \frac{1}{4}\lambda\phi^4$$

New Type of Modulated Fluctuations from Preheating

$$\frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

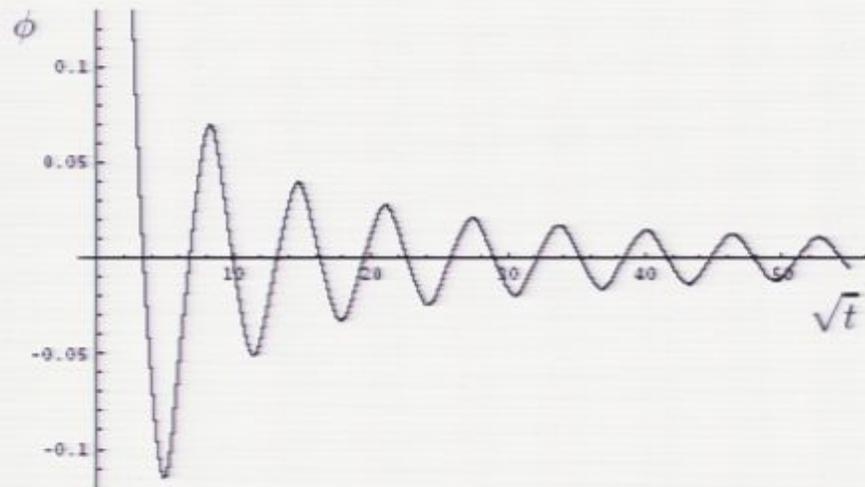
iso-inflaton field is light if

$$g^2/\lambda \sim \mathcal{O}(1)$$

A. Chambers, A. Rajantie [arXiv:0805.4795](https://arxiv.org/abs/0805.4795)

$$\frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

$$H^2 = \frac{8\pi}{3M_p^2} \left(\frac{1}{2}\dot{\phi}^2 + \frac{\lambda\phi^4}{4} \right)$$



$$\ddot{\phi} + 3H\dot{\phi} + \lambda\phi^3 = 0.$$

$$\eta = \int \frac{dt}{a(t)} \quad \varphi = a\phi$$

$$\varphi'' + \lambda\varphi^3 - \frac{a''}{a}\varphi = 0$$

$$\varphi'' + \lambda\varphi^3 = 0$$

$$\varphi \equiv a\phi = \tilde{\varphi}f(x)$$

$$f(x) = \text{cn}\left(x - x_0, \frac{1}{\sqrt{2}}\right)$$

$$x \equiv \sqrt{\lambda}\tilde{\varphi}\eta = \left(\frac{6\lambda M_p^2}{\pi}\right)^{1/4} \sqrt{t}$$

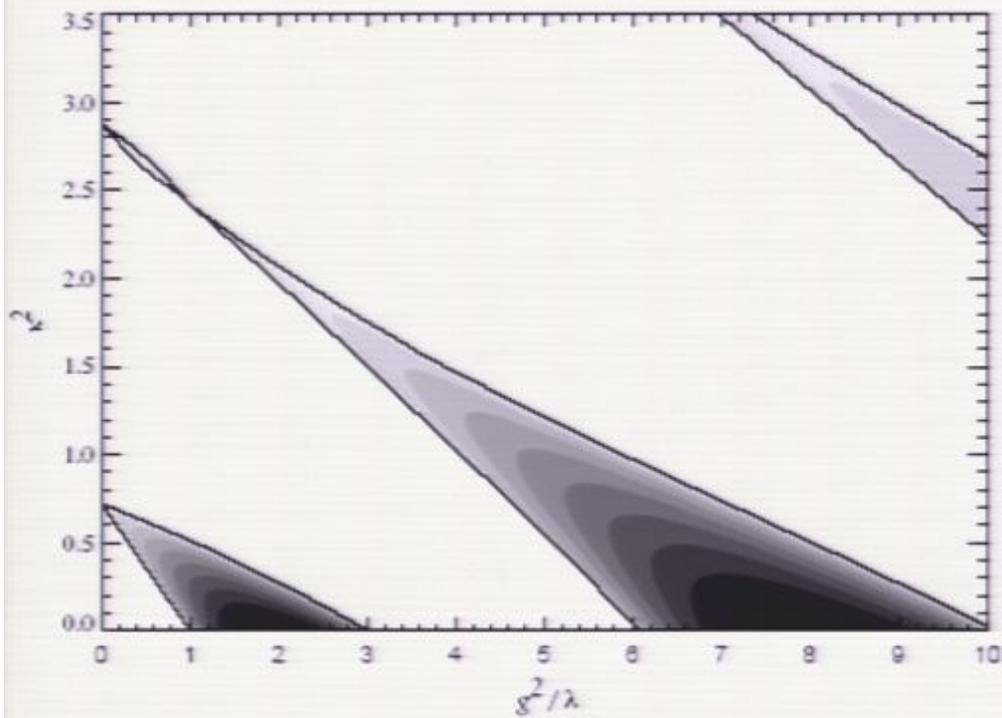
$$\hat{\chi}(t, \mathbf{x}) = \frac{1}{(2\pi)^{3/2}} \int d^3k \left(\hat{a}_k \chi_k(t) e^{-i\mathbf{k}\mathbf{x}} + \hat{a}_k^\dagger \chi_k^*(t) e^{i\mathbf{k}\mathbf{x}} \right)$$

$$\ddot{\chi}_k + 3\frac{\dot{a}}{a}\dot{\chi}_k + \left(\frac{k^2}{a^2} + g^2\phi^2 \right) \chi_k = 0$$

$$X_k(t) = a(t)\chi_k(t)$$

$$X_k'' + \left(\kappa^2 + \frac{g^2}{\lambda} cn^2 \left(x, \frac{1}{\sqrt{2}} \right) \right) X_k = 0$$

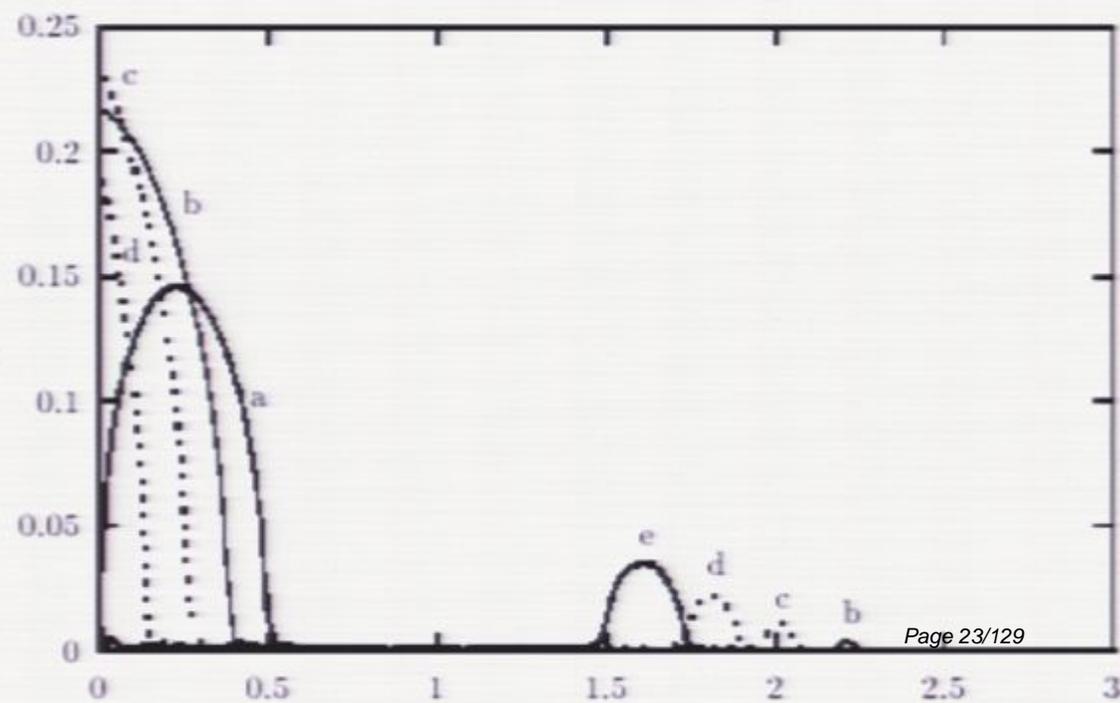
$$\kappa^2 = \frac{k^2}{\lambda\tilde{\varphi}^2} \quad \chi_k(t) = P_k(t)e^{\mu_k t}$$



Stability/instability chart Of the Lamé equation

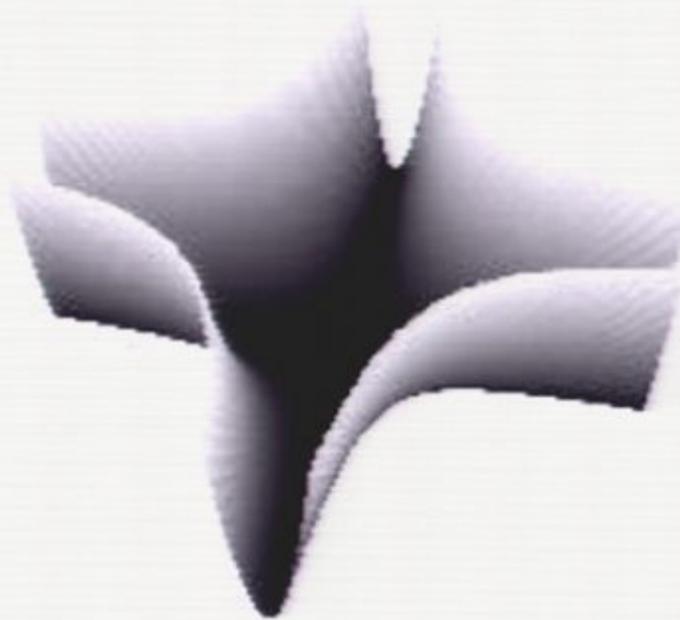
$$X_k'' + \left(\kappa^2 + \frac{g^2}{\lambda} \operatorname{cn}^2 \left(x, \frac{1}{\sqrt{2}} \right) \right) X_k = 0$$

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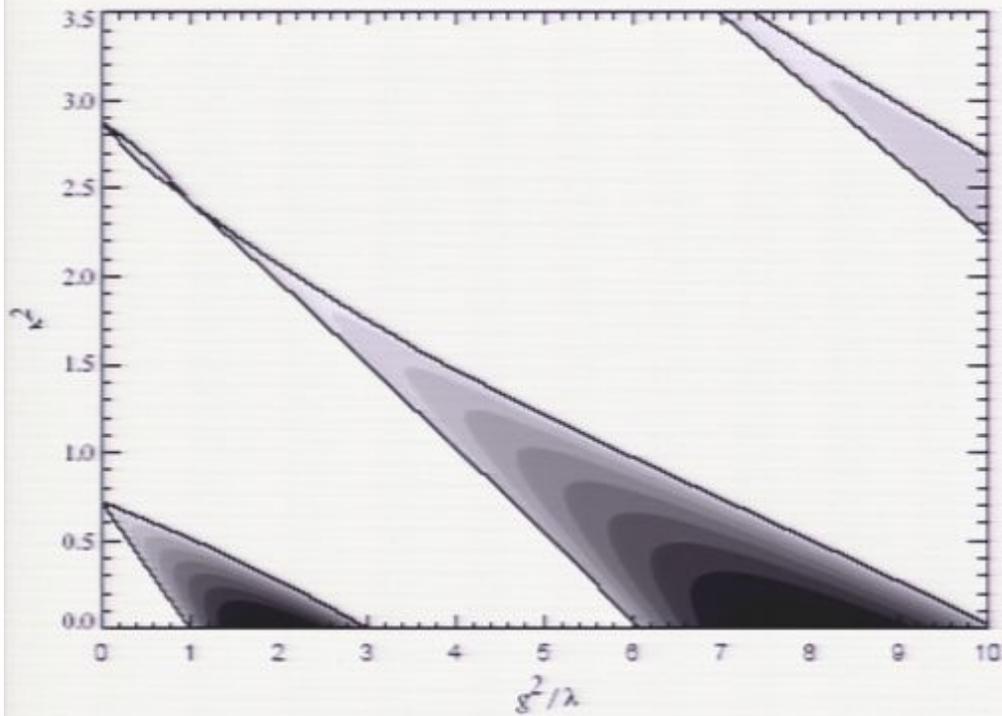
Chaotic Billiards

$$\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2}g^2\phi^2\chi^2$$

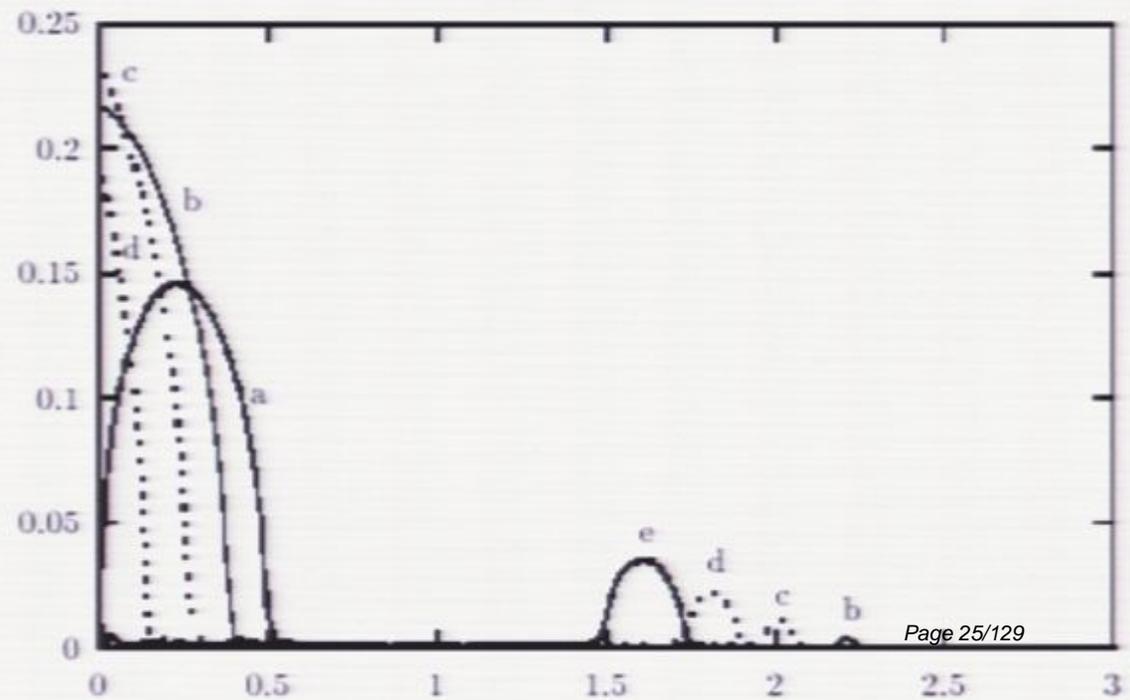


Stability/instability chart Of the Lamé equation

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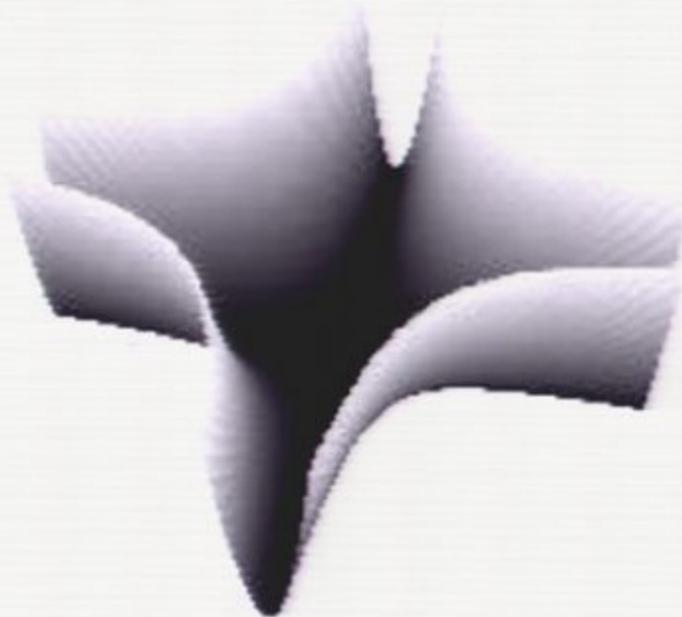


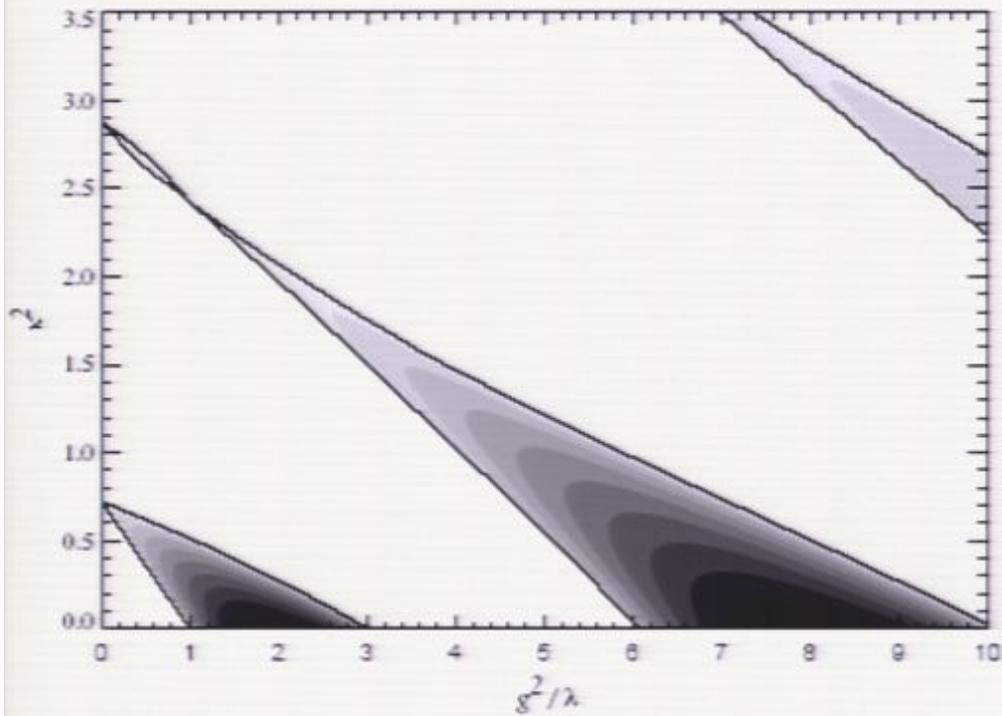
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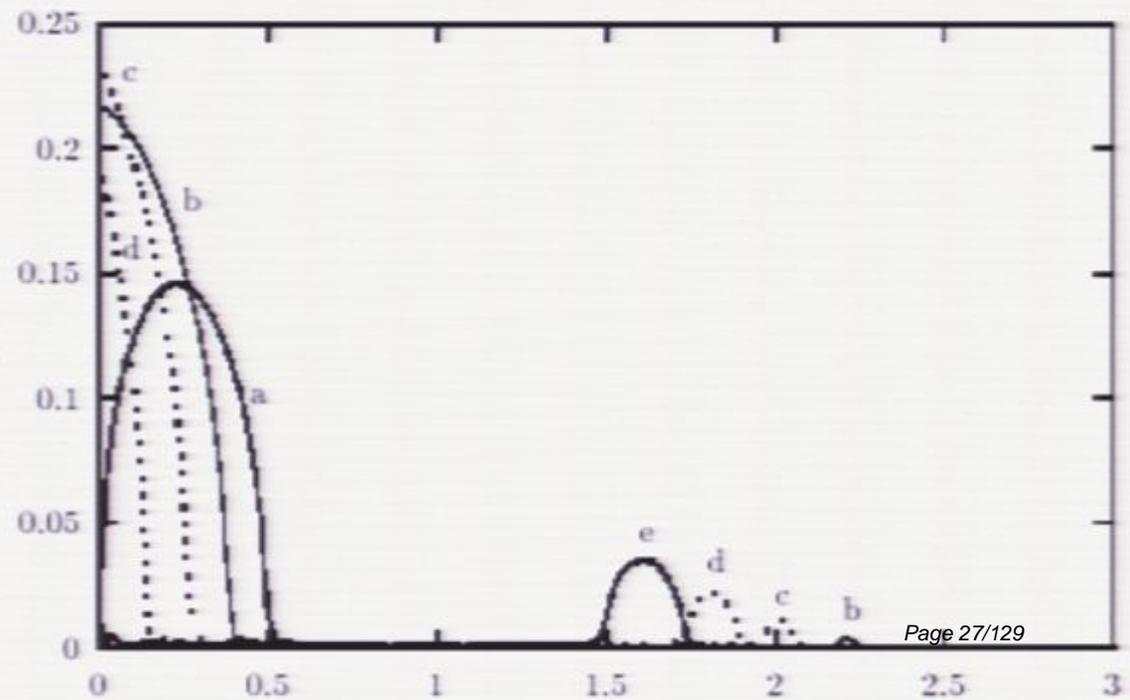




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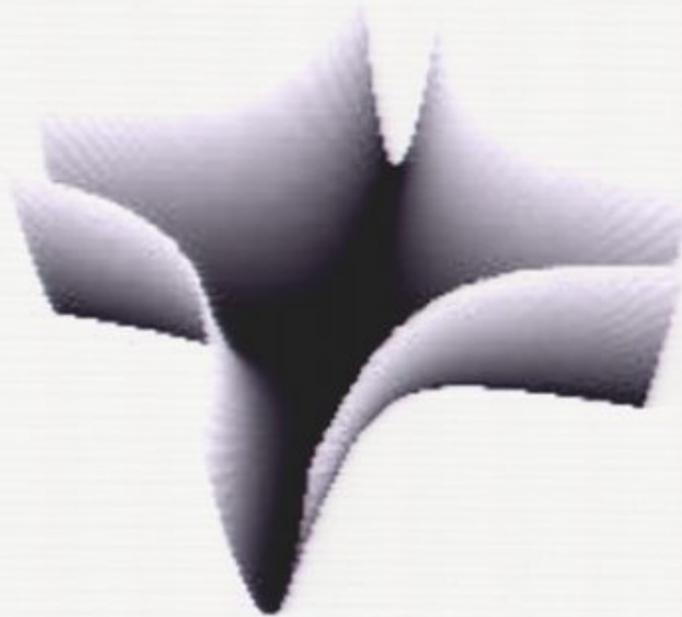
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Chaotic Billiards

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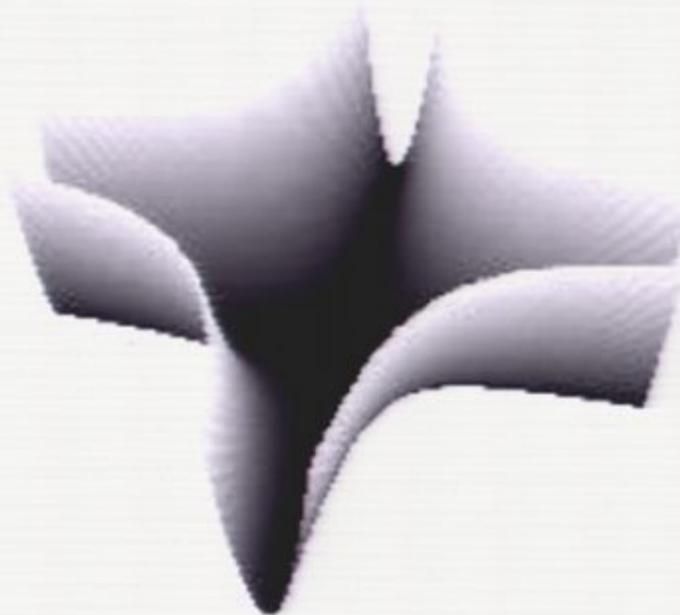
from parametric resonance $\chi_k = P_k(t) e^{\mu_k t}$

from billiard $\chi_0 \sim e^{\Lambda t}$

$$\Lambda = \mu_0$$

Chaotic Billiards

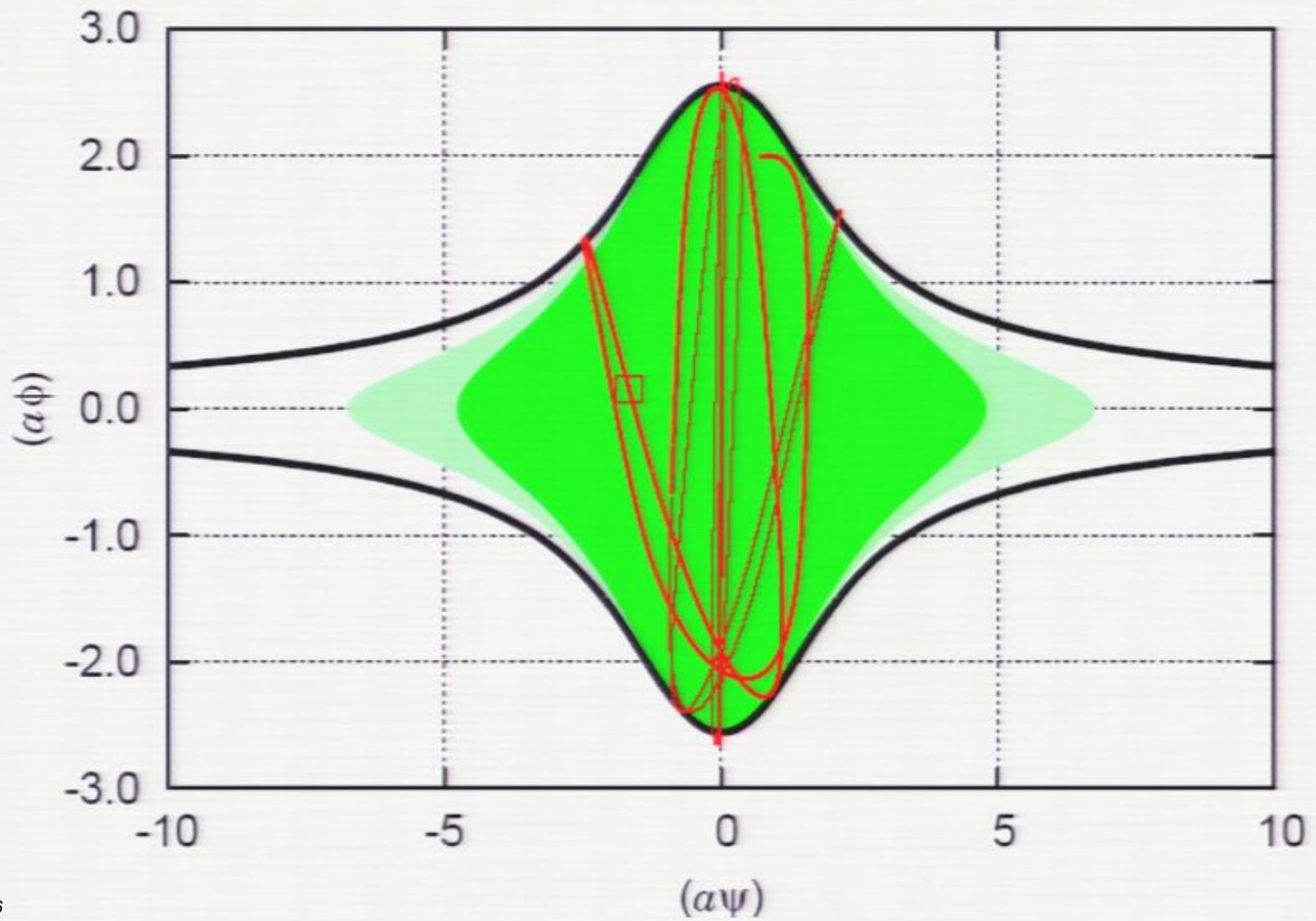
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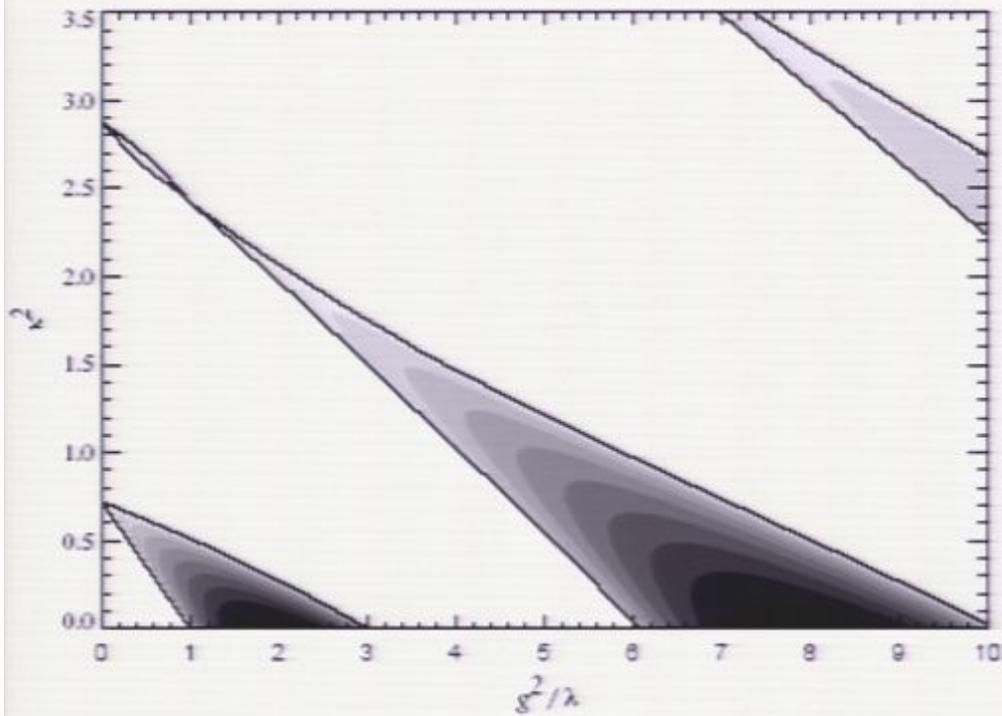


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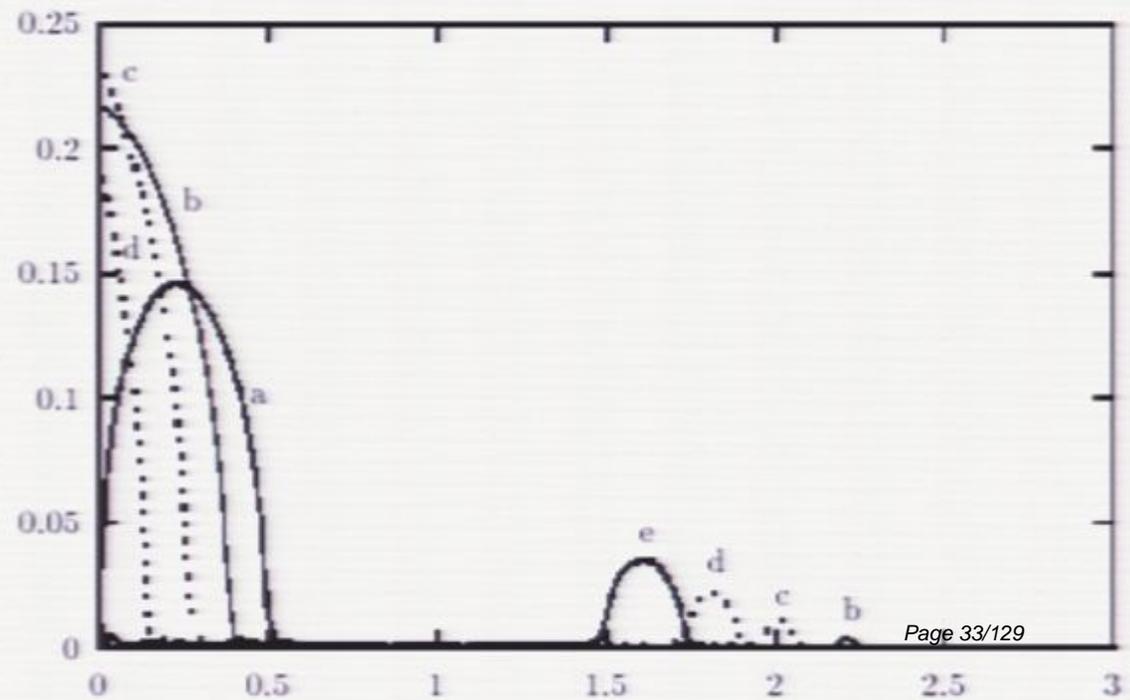




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Chaotic Billiards

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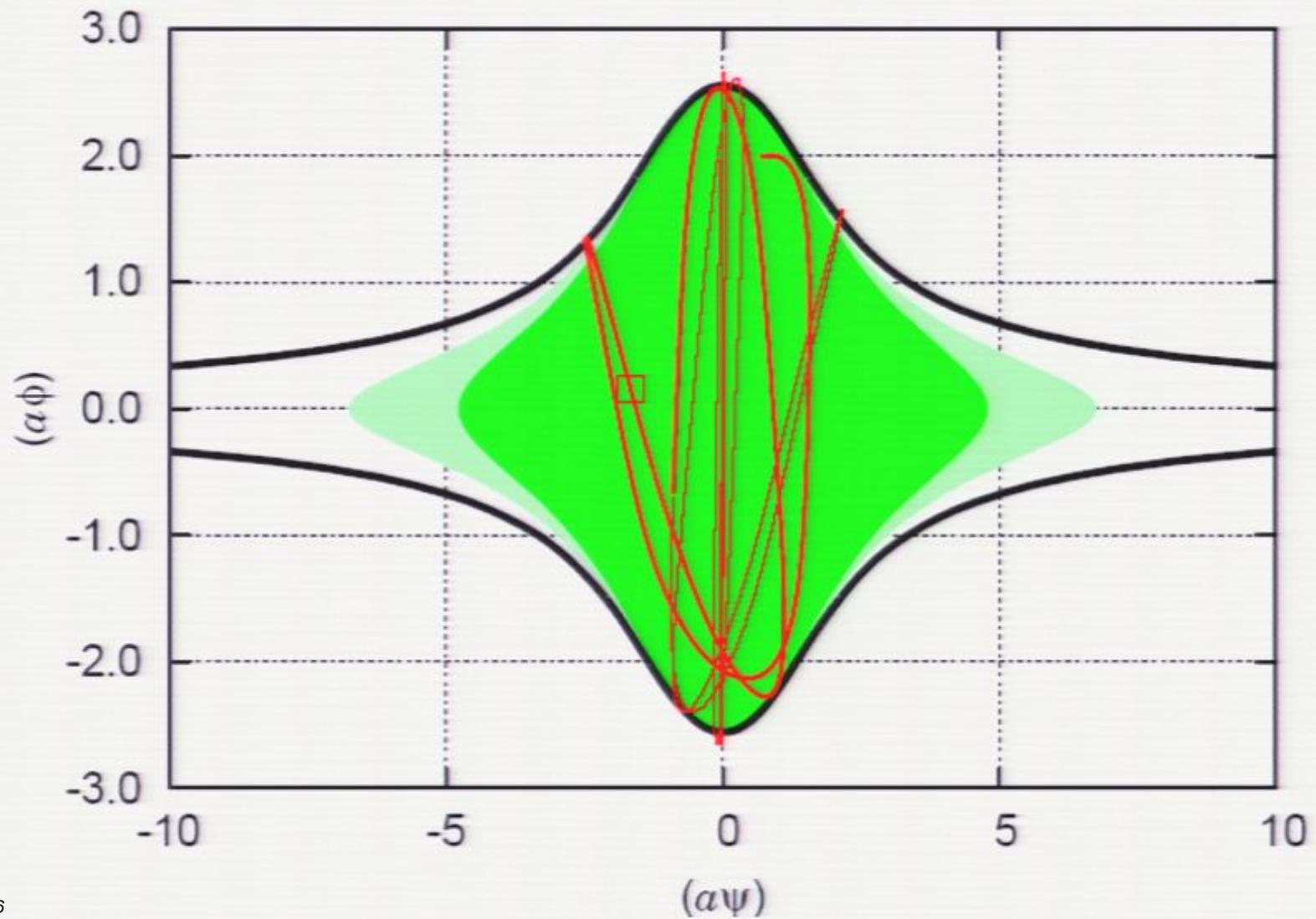
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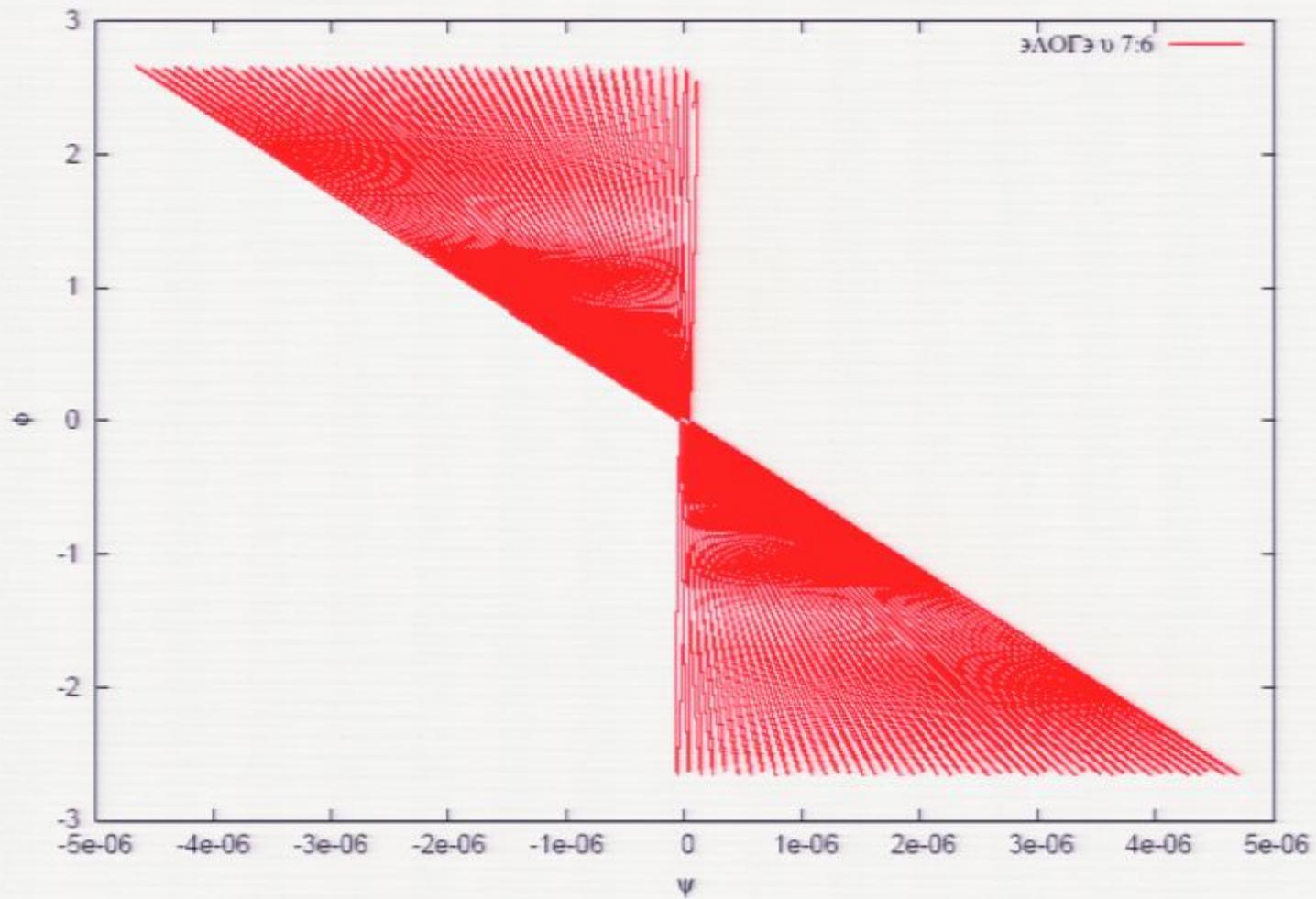
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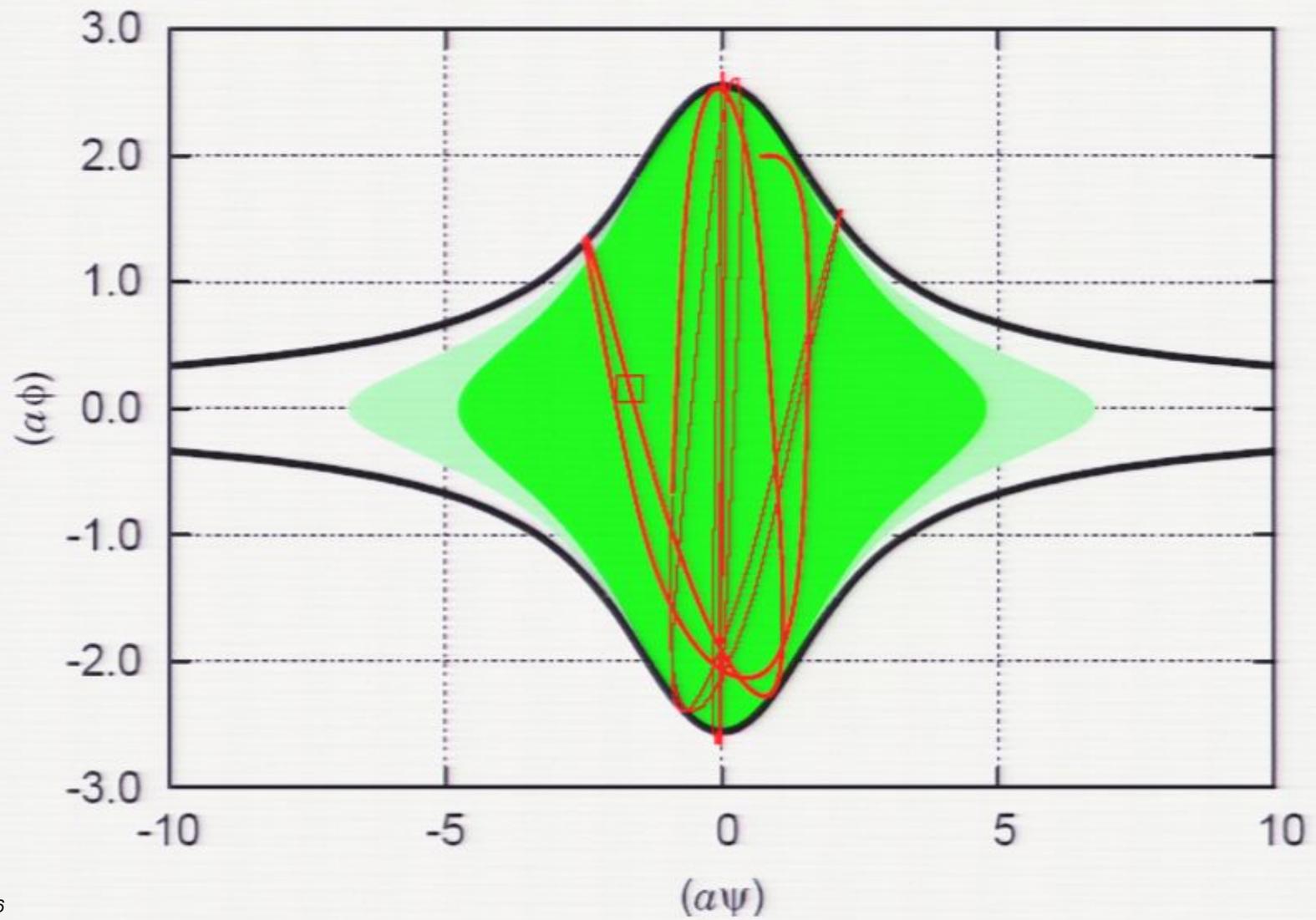
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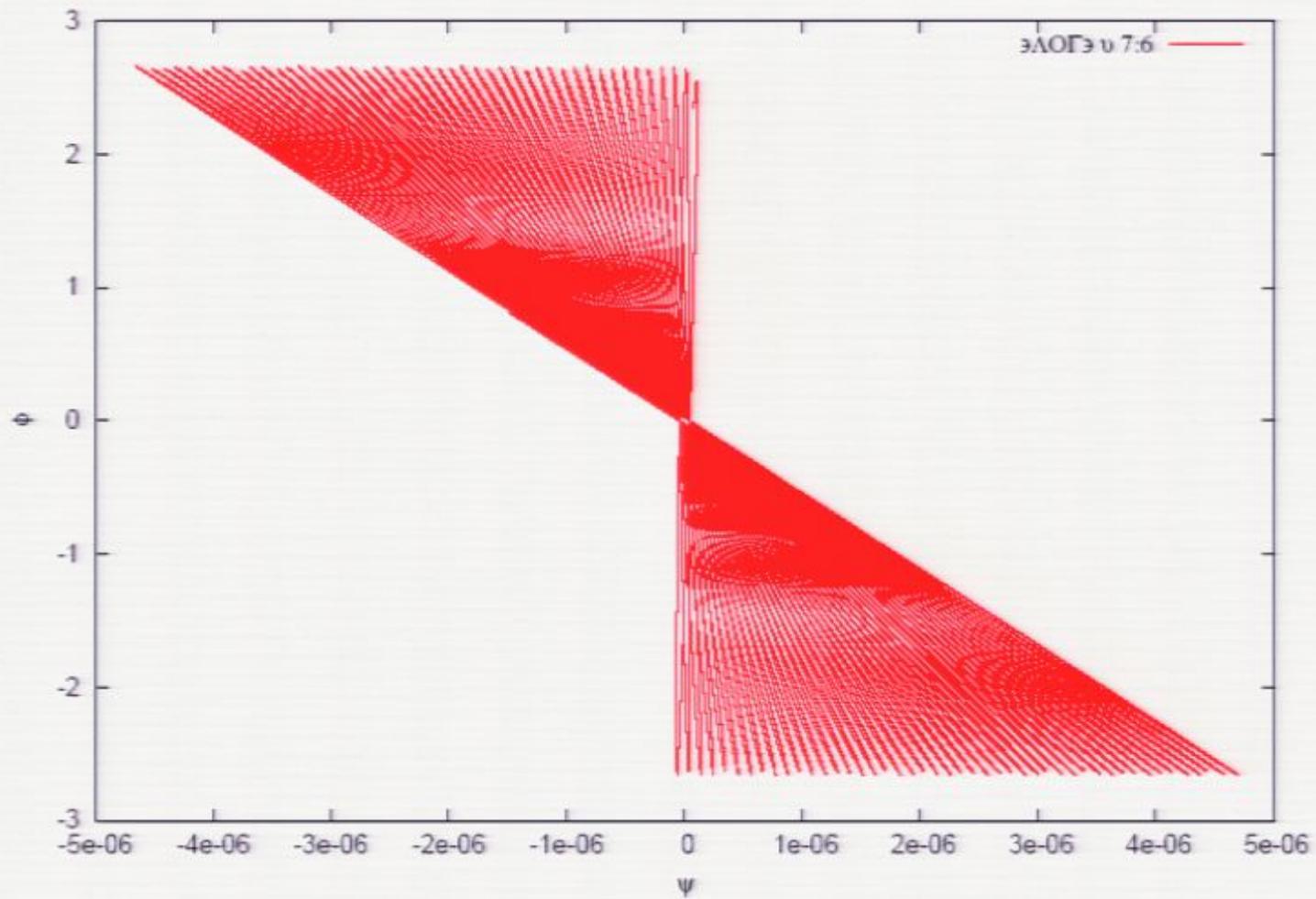
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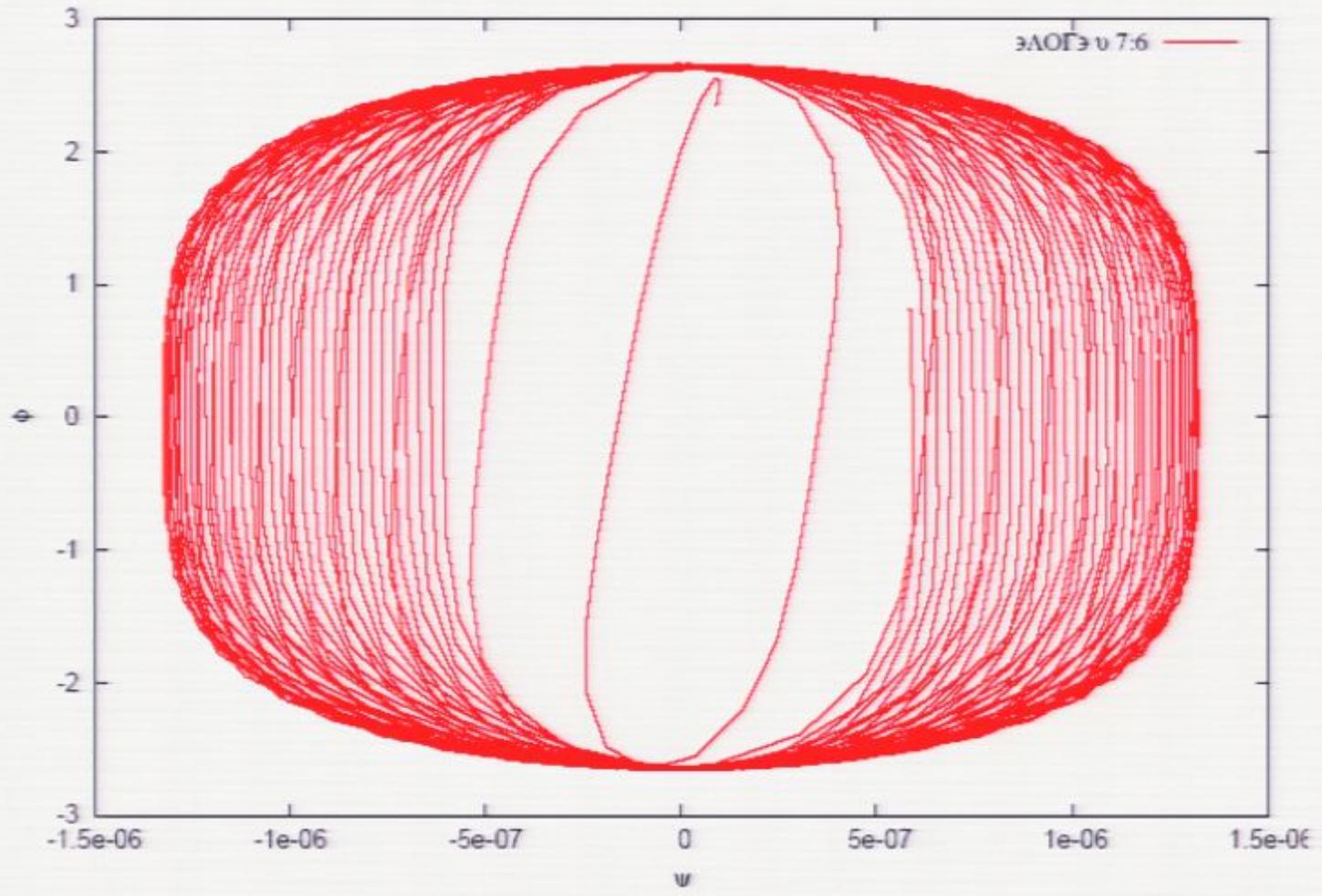
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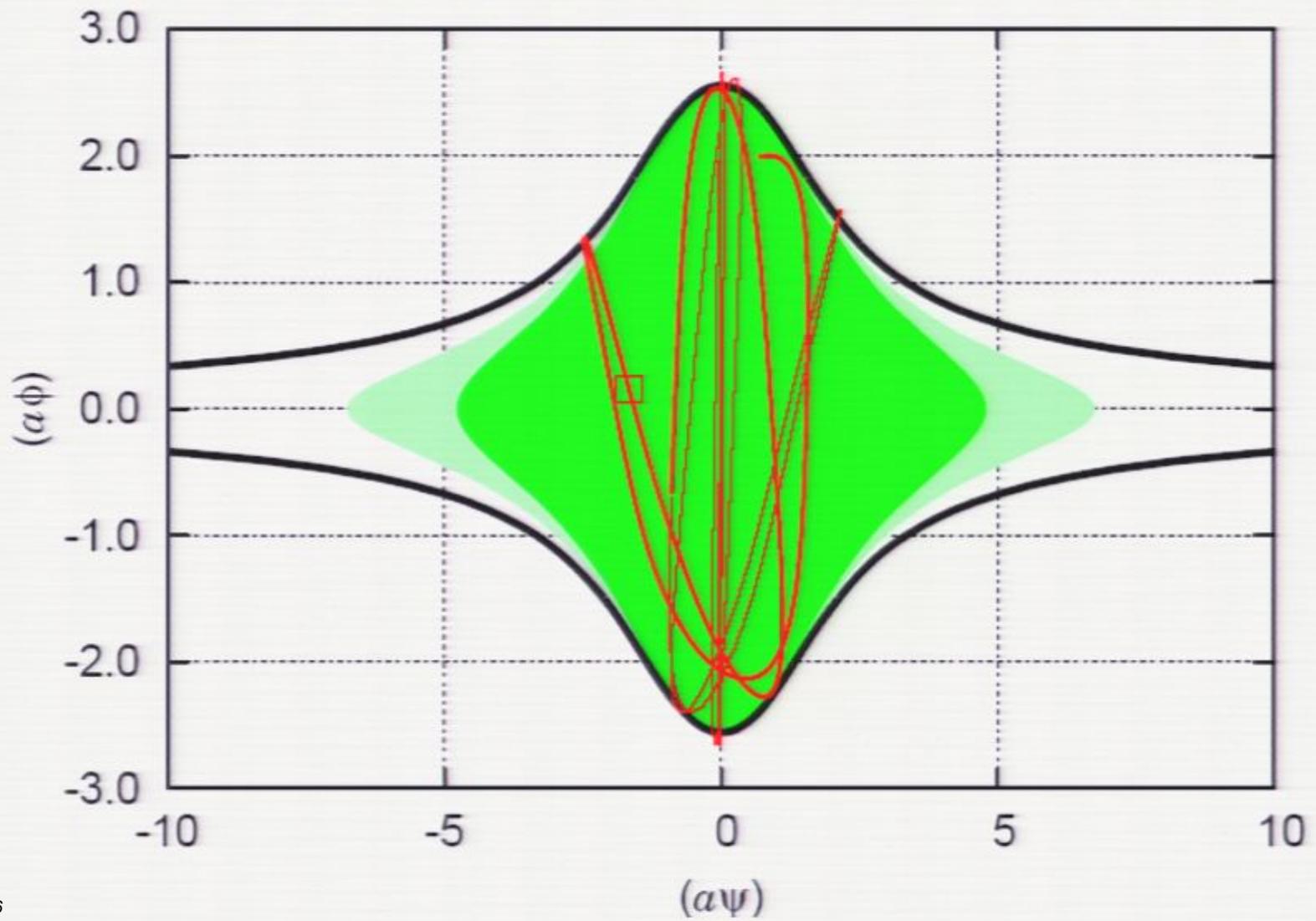




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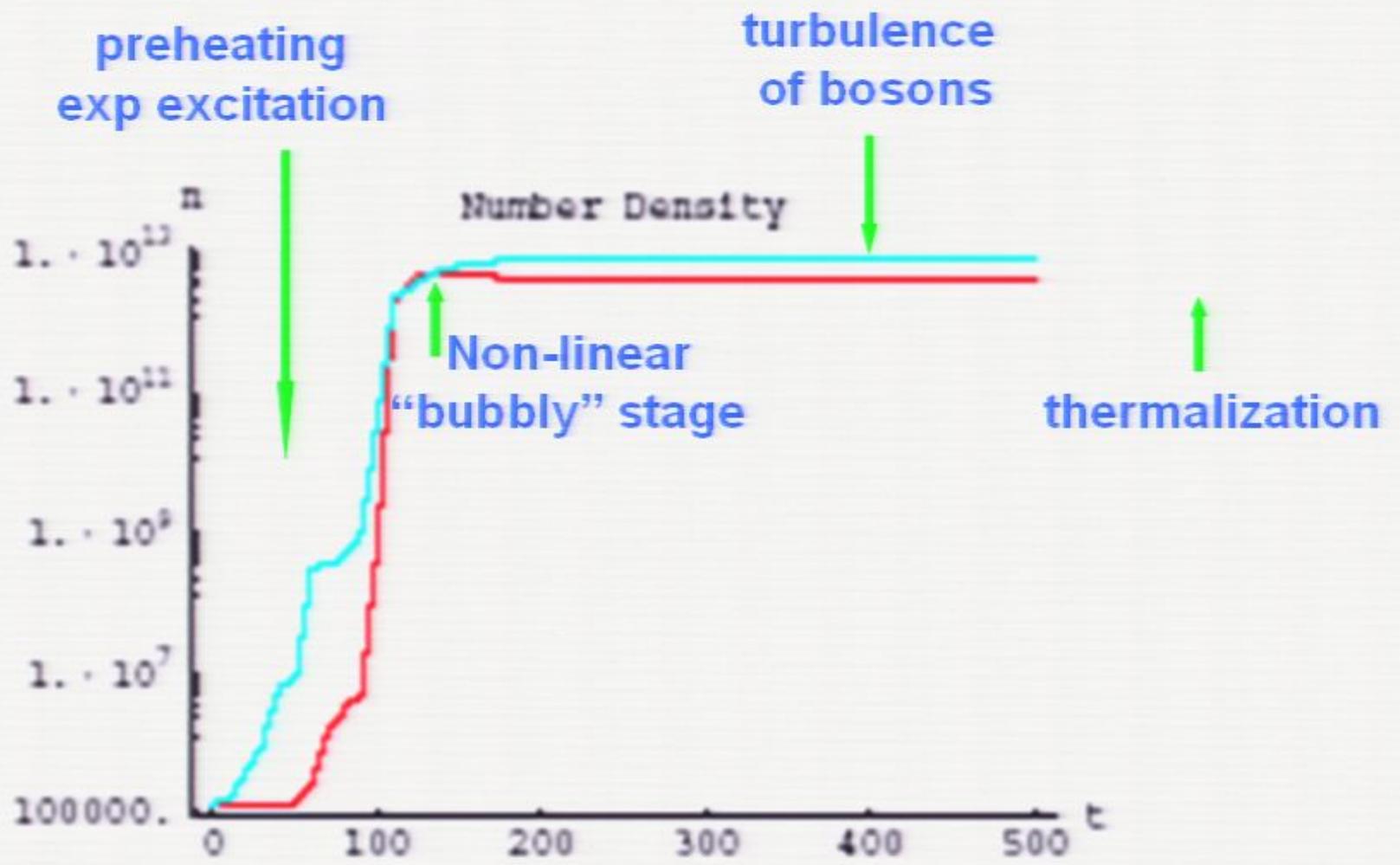
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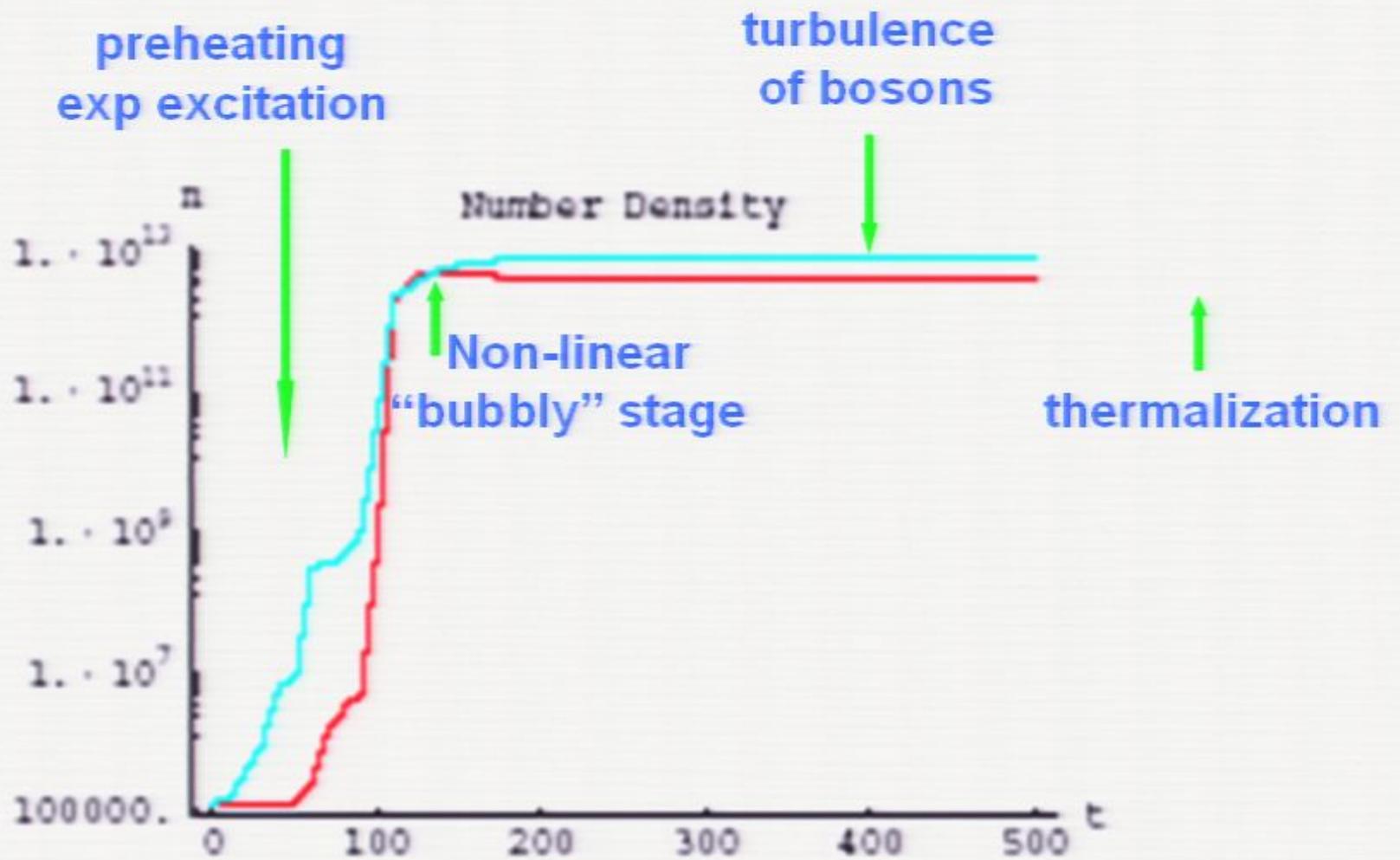
Evolution of total energy density

$$g^2\phi^2\chi^2 \text{ up to } t = 256/m$$



Evolution of total energy density

$$g^2\phi^2\chi^2 \text{ up to } t = 256/m$$

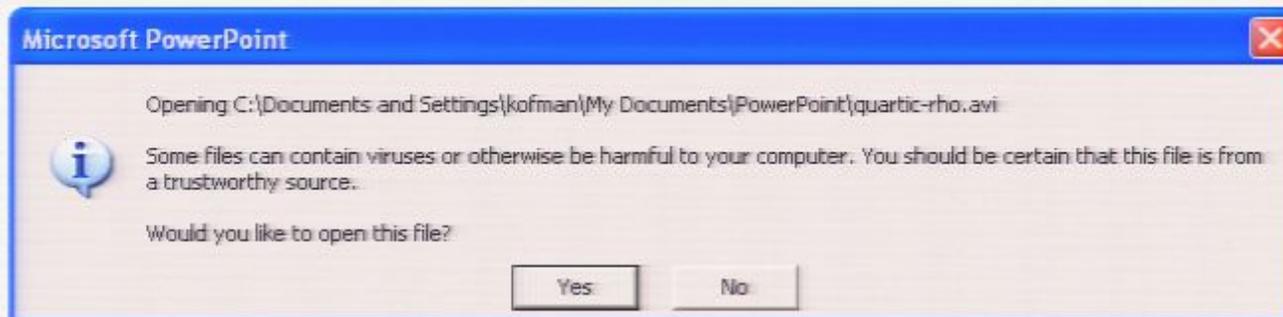


Evolution of total energy density

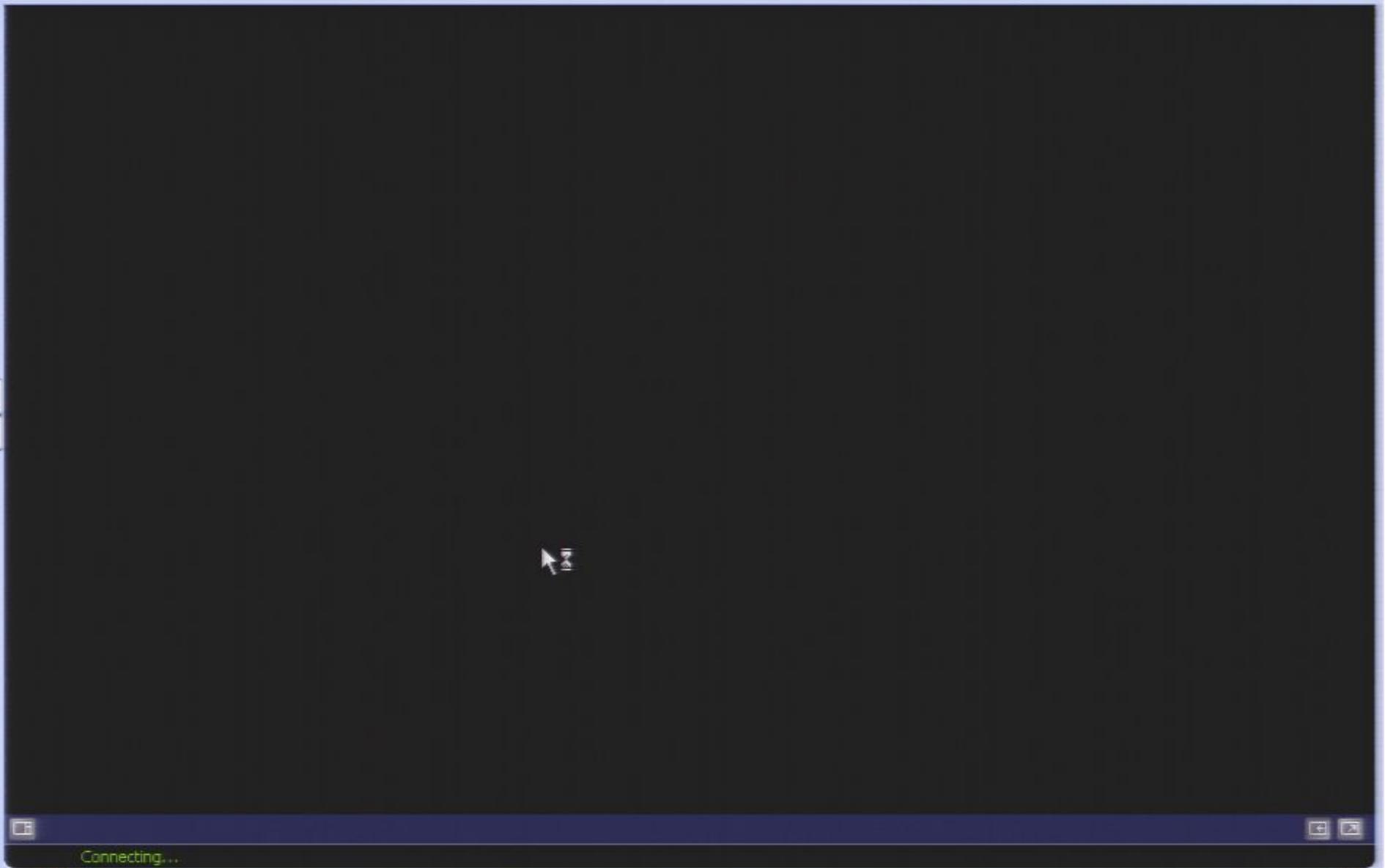
$$g^2\phi^2\chi^2 \text{ up to } t = 256/m$$

Evolution of total energy density

$$g^2 \phi^2 \chi^2 \text{ up to } t = 256/m$$



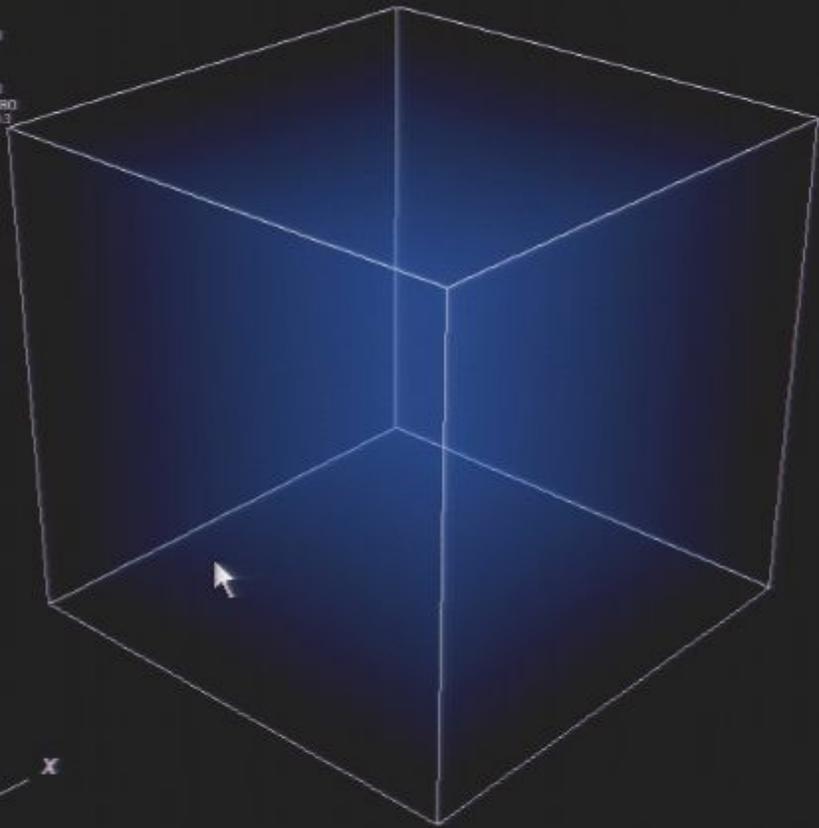
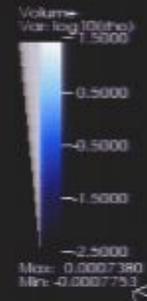
- Now Playing
- Media Guide
- Copy from
- Media Library
- Radio
- Copy to CD Device
- Premium Services
- Audio
- Booster



Connecting...

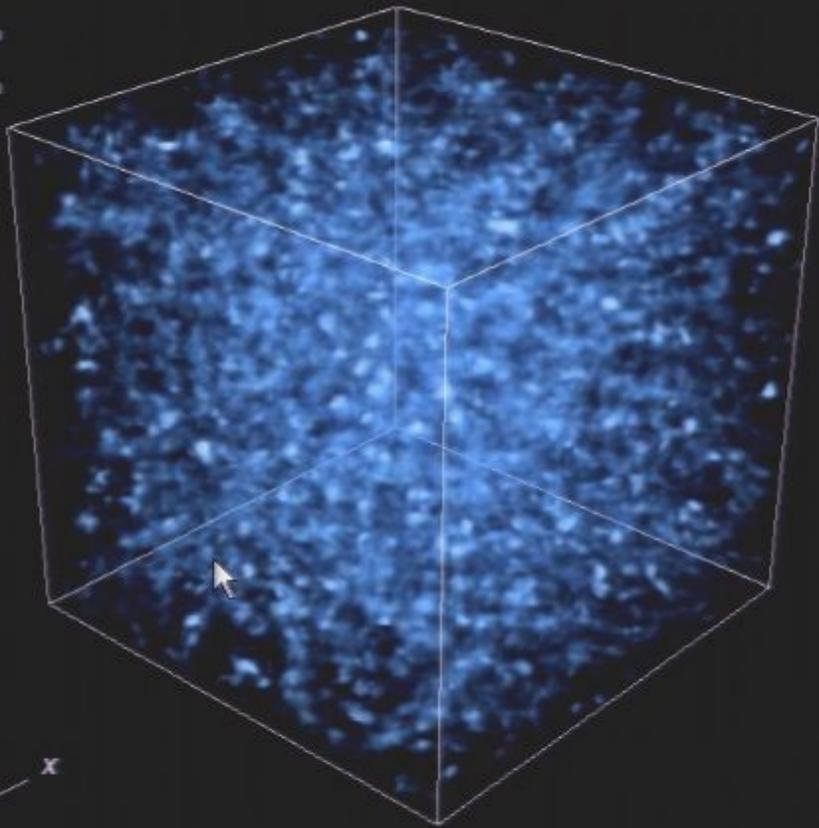
Windows Media Player playback controls including play/pause, stop, previous, next, volume, and full screen buttons.

- Now playing
- Media guide
- Copy from
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- Radio tuner
- Copy to CD Device
- Premium services
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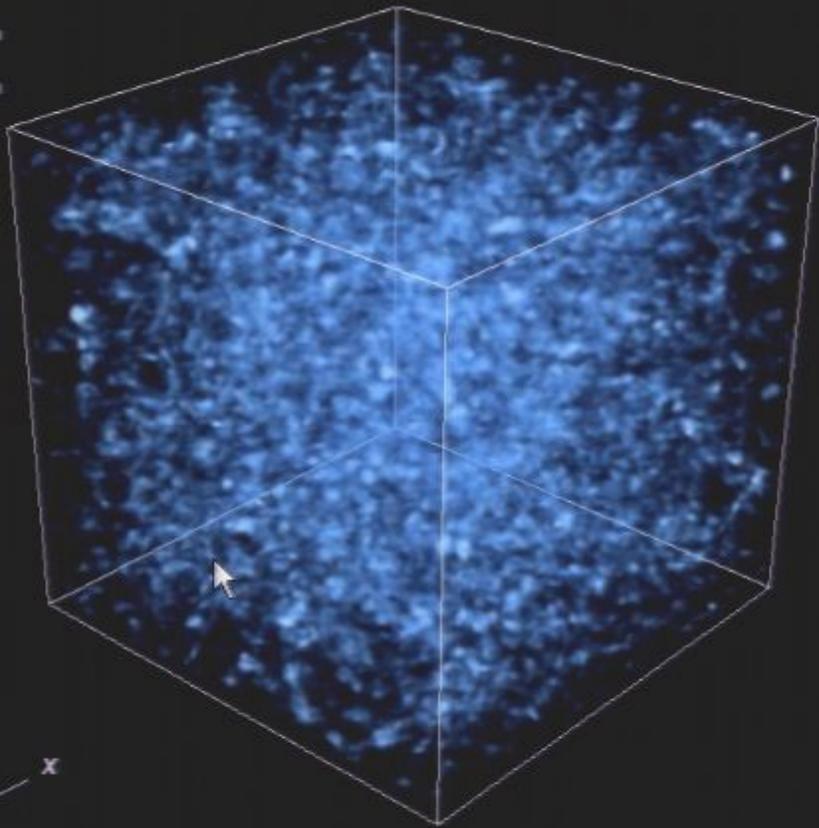
Playing 00:01

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster



Playlist: Playlist1 00:11

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster

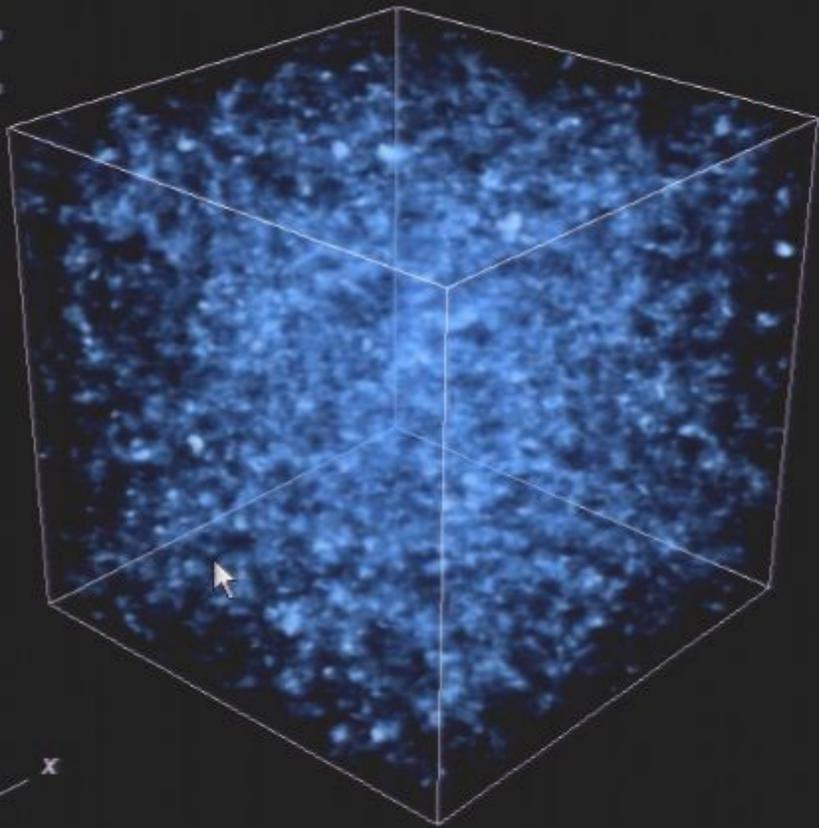


t = 155.50

Clip: quartic-rho

00:12

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Online
- Booster

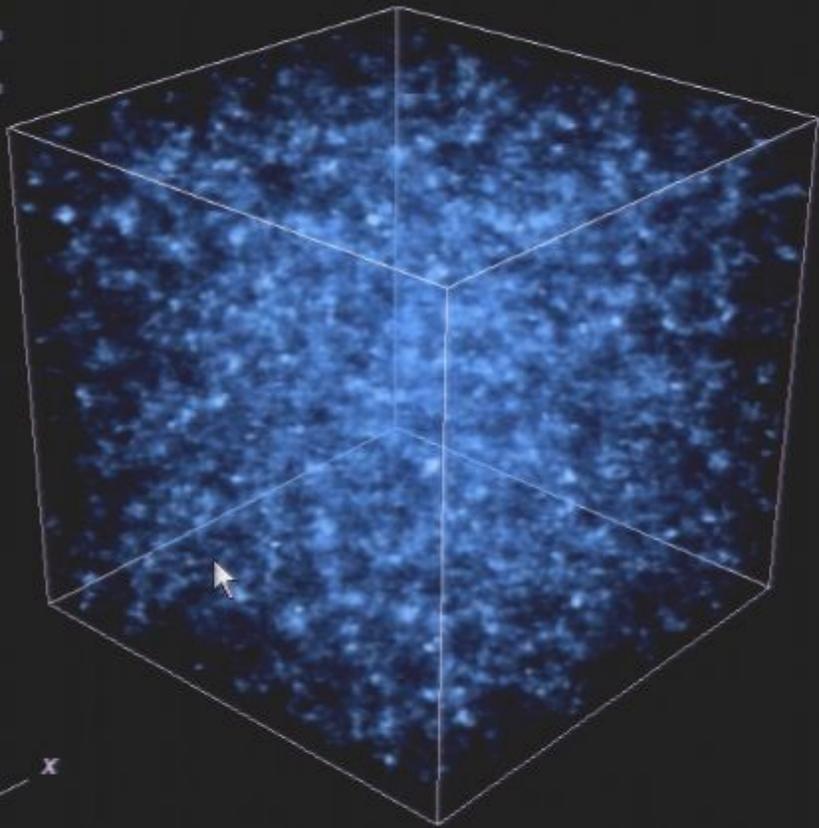


t = 182.50

Clip: quartic-rho

00:14

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster

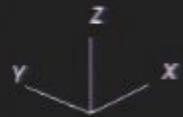
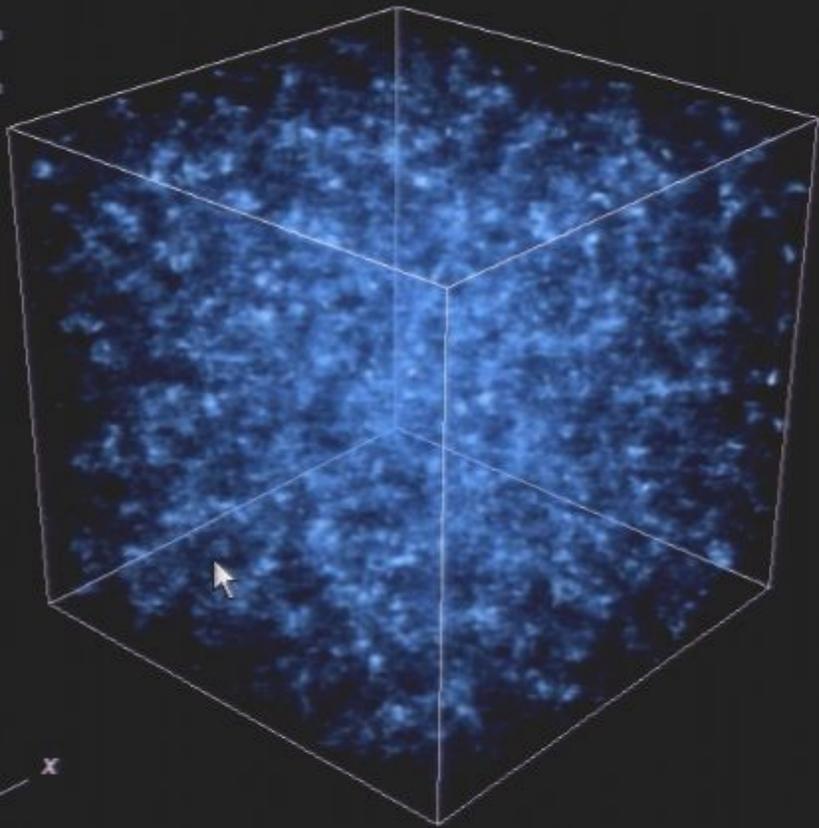


t = 212.00

Clip: quartic-rho

00:17

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster

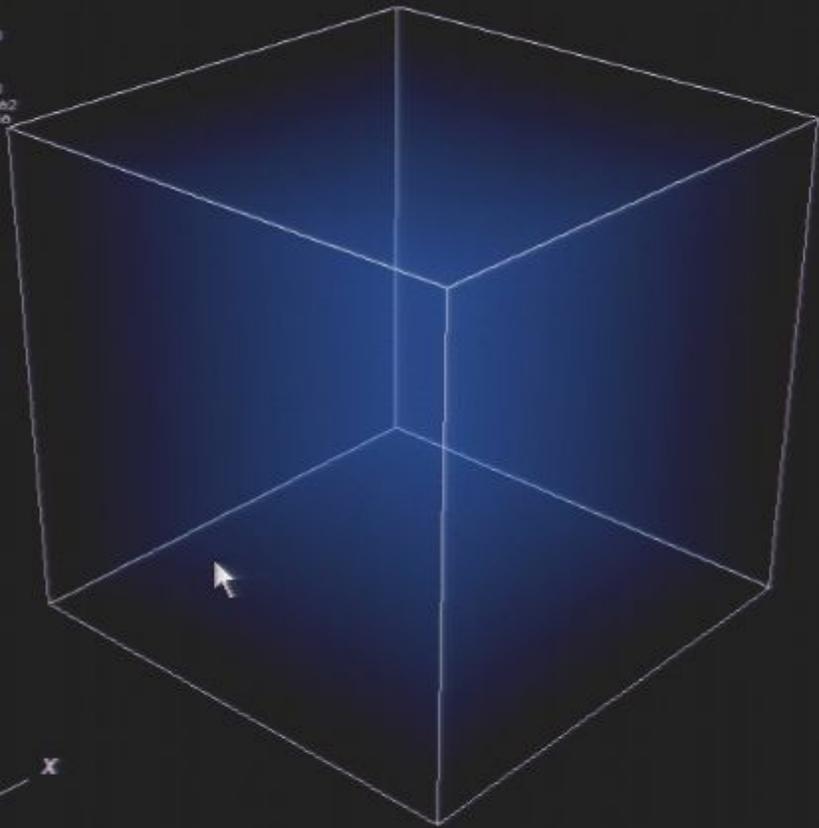
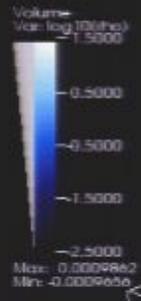


t = 240.50

Clip: quartic-rho

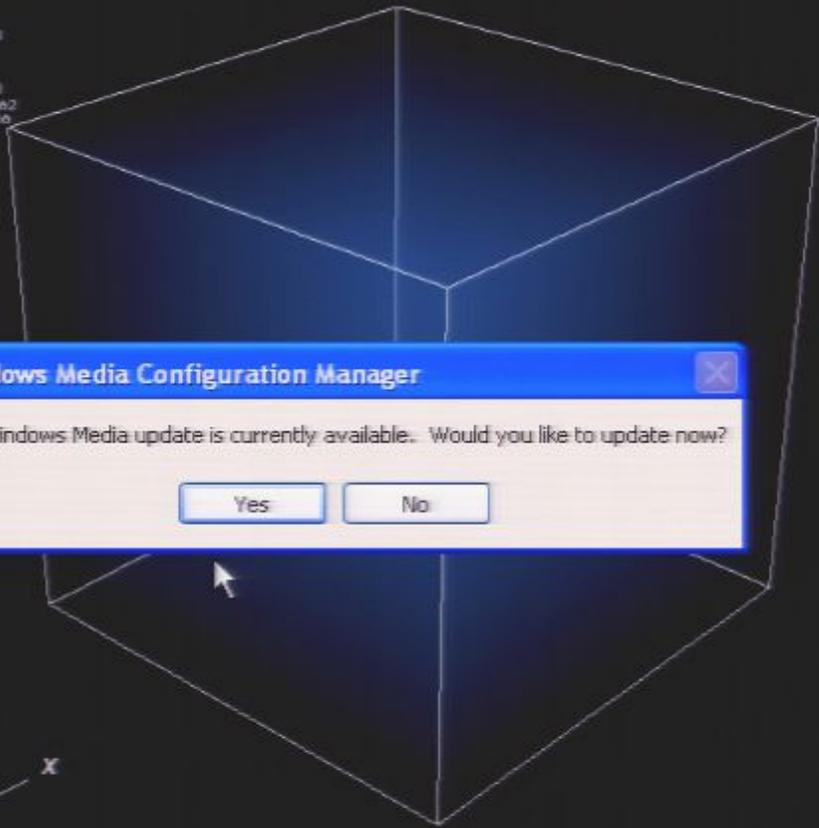
00:19

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster



Stopped

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music Center



Windows Media Configuration Manager

A Windows Media update is currently available. Would you like to update now?



t = 0.00

Stopped

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster



Windows Media Player 9 Series

Windows Media Player Update

A Windows Media Player update is available. Please review the following information.

- The Windows Media Player update is 1 MB. This will take approximately 0 minutes to download on a 28.8kbps connection.
- Click Next to begin the download and update process or Click Cancel to postpone the update.

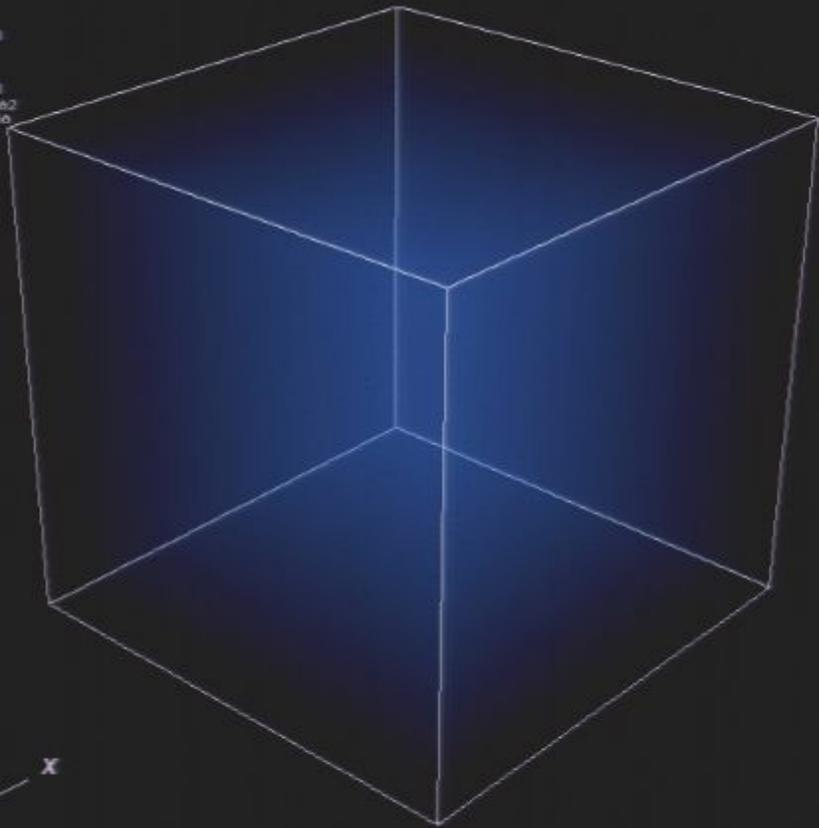
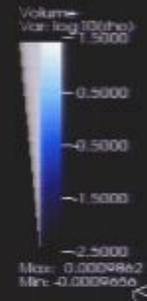
Windows Media Player 9 Series

< Back Next > Cancel

t = 0.00

Stopped

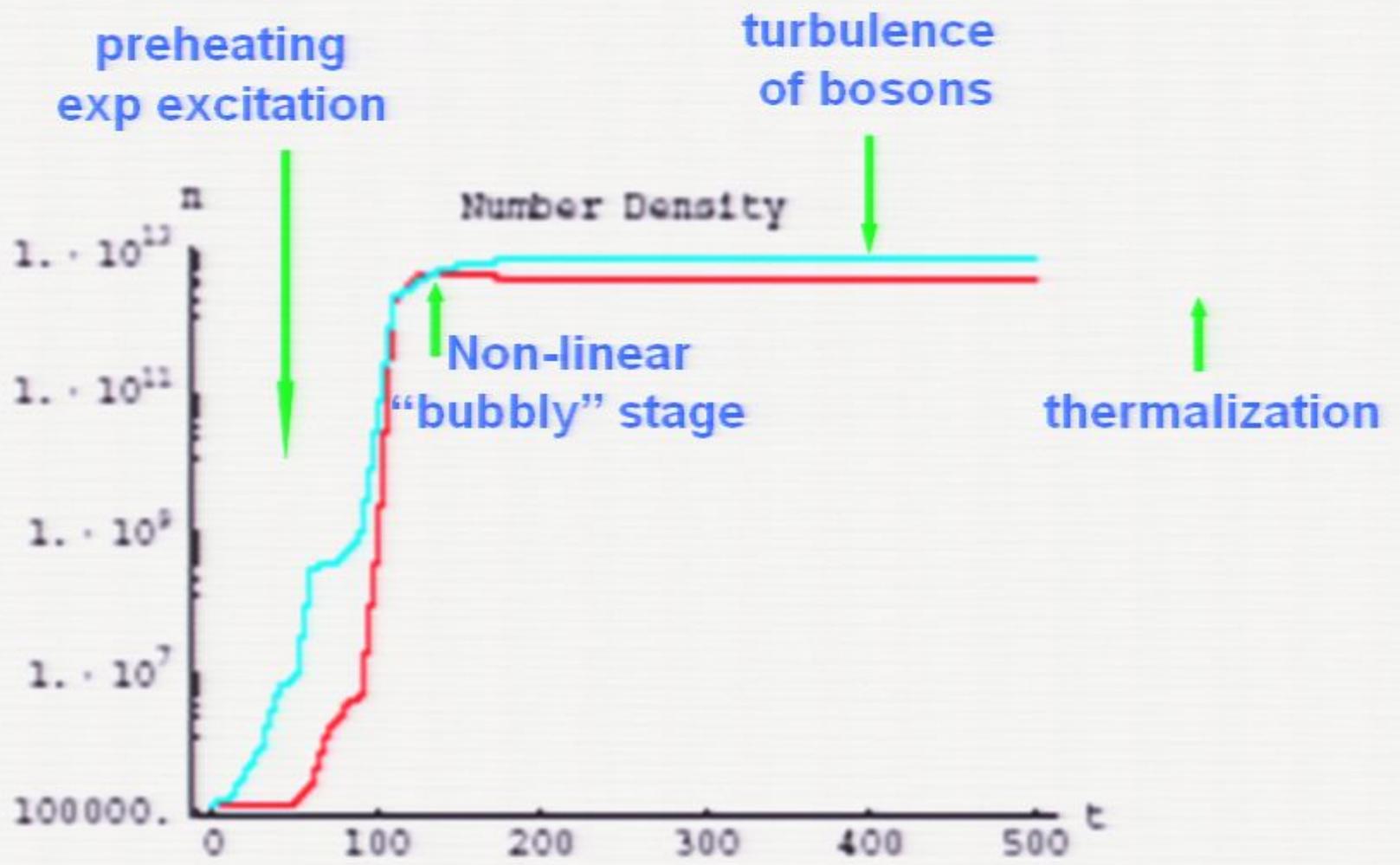
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster



Stopped

Evolution of total energy density

$$g^2 \phi^2 \chi^2 \text{ up to } t = 256/m$$

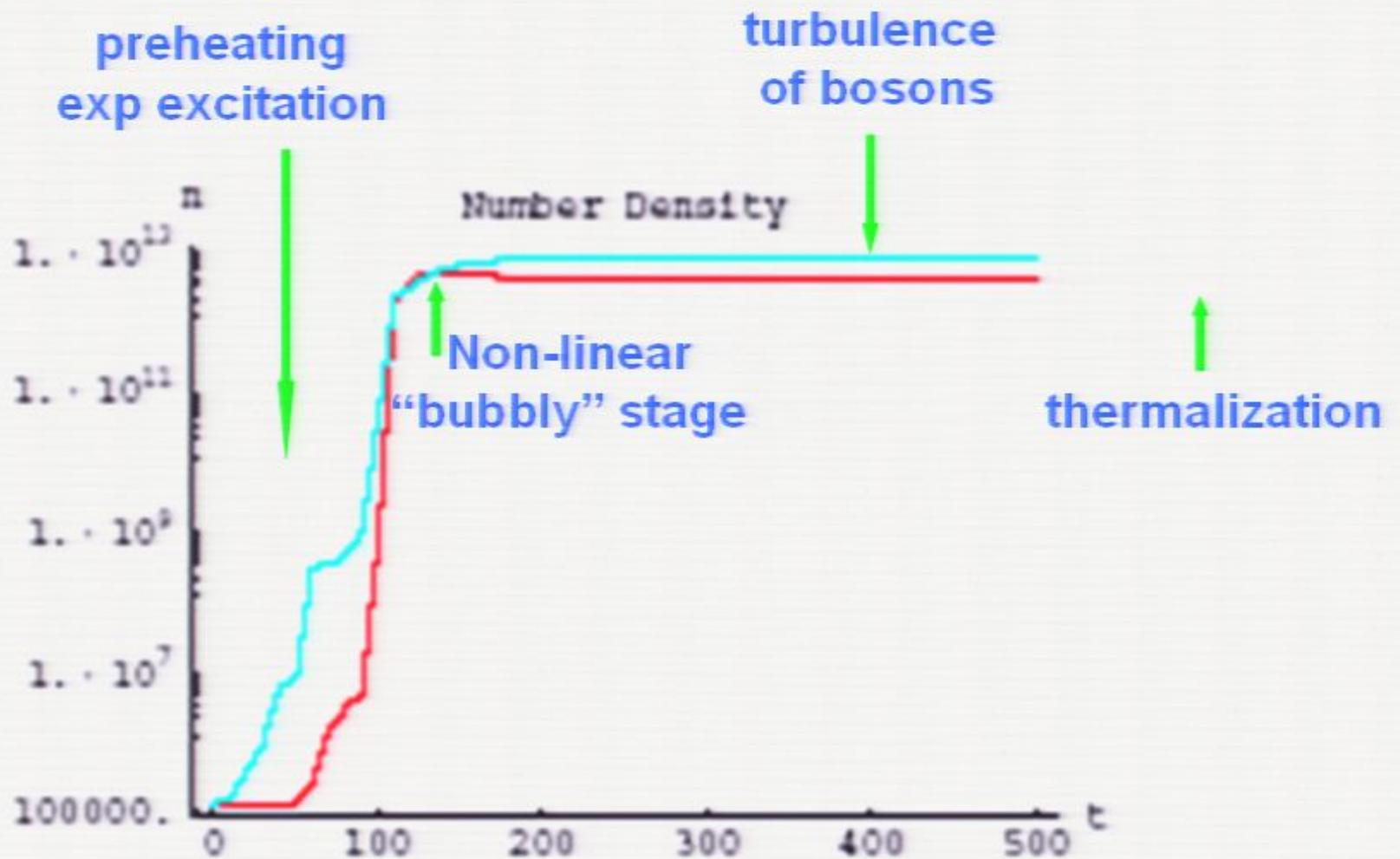


$$V(\phi, \chi) = \frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

$$\ddot{\phi} - \nabla^2\phi + g^2\chi^2\phi = 0$$

$$\ddot{\chi} - \nabla^2\chi + g^2\phi^2\chi = 0$$

$$3H^2 = \frac{8\pi}{M_p^2} \left(\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2a^2}\nabla\phi^2 + \frac{1}{2a^2}\nabla\chi^2 + V(\phi, \chi) \right)$$

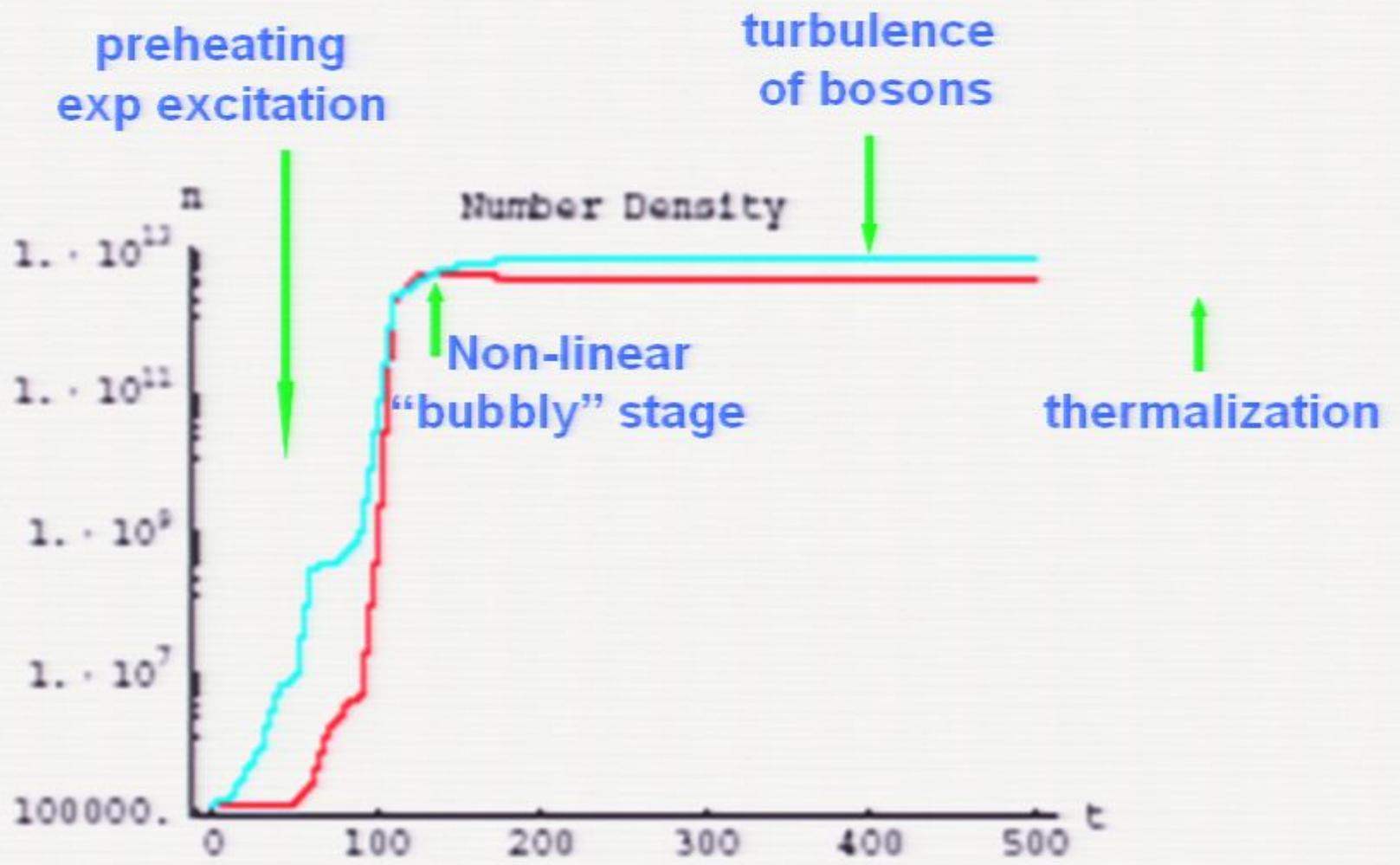


$$V(\phi, \chi) = \frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

$$\ddot{\phi} - \nabla^2\phi + g^2\chi^2\phi = 0$$

$$\ddot{\chi} - \nabla^2\chi + g^2\phi^2\chi = 0$$

$$3H^2 = \frac{8\pi}{M_p^2} \left(\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2a^2}\nabla\phi^2 + \frac{1}{2a^2}\nabla\chi^2 + V(\phi, \chi) \right)$$

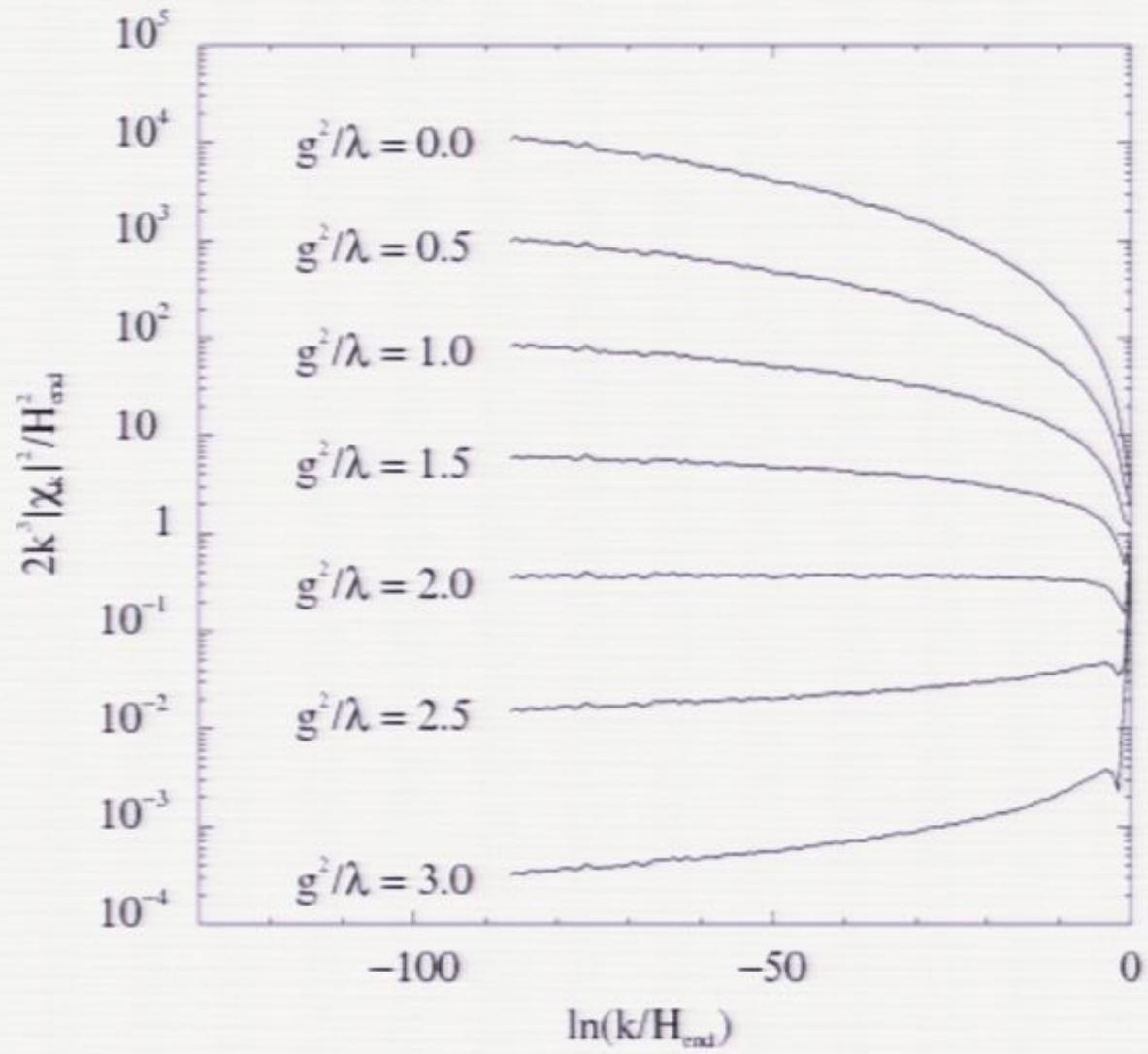


$$V(\phi, \chi) = \frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

$$\ddot{\phi} - \nabla^2\phi + g^2\chi^2\phi = 0$$

$$\ddot{\chi} - \nabla^2\chi + g^2\phi^2\chi = 0$$

$$3H^2 = \frac{8\pi}{M_p^2} \left(\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2a^2}\nabla\phi^2 + \frac{1}{2a^2}\nabla\chi^2 + V(\phi, \chi) \right)$$



$$V(\phi, \chi) = \frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

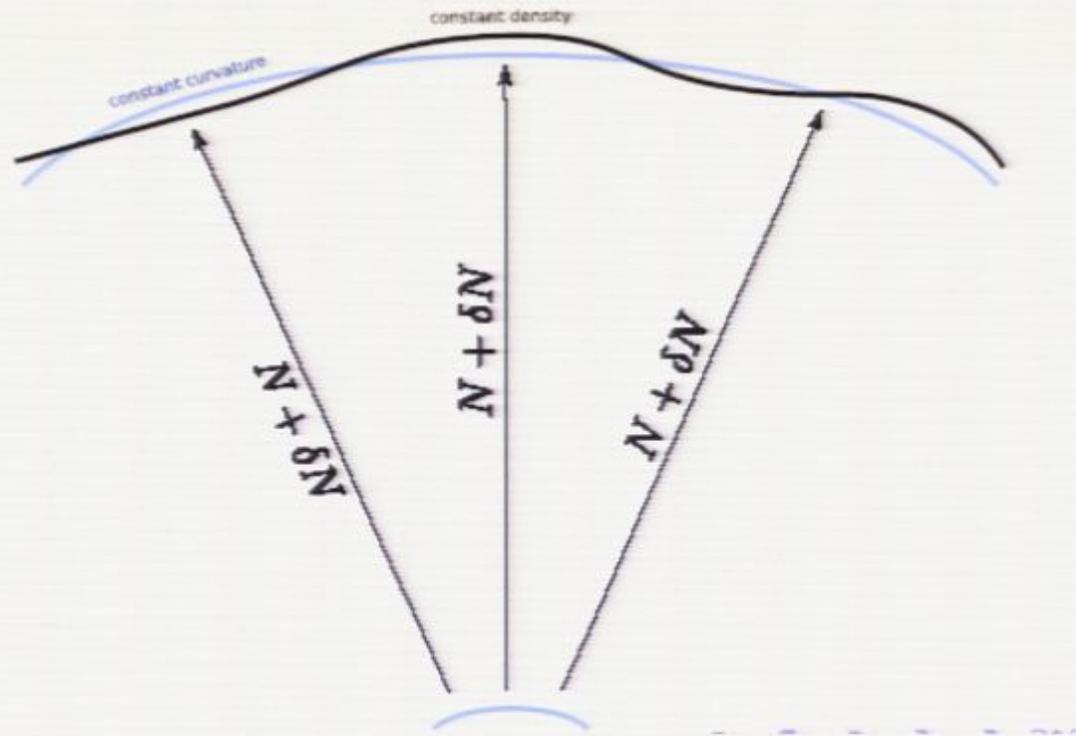
$$\ddot{\phi} - \nabla^2\phi + g^2\chi^2\phi = 0$$

$$\ddot{\chi} - \nabla^2\chi + g^2\phi^2\chi = 0$$

$$3H^2 = \frac{8\pi}{M_p^2} \left(\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2a^2}\nabla\phi^2 + \frac{1}{2a^2}\nabla\chi^2 + V(\phi, \chi) \right)$$

"separated universes" approximation

$$\zeta = \delta \ln a|_H = \delta N(\chi_i)$$



$$V(\phi, \chi) = \frac{1}{4}\lambda\phi^4 + \frac{1}{2}g^2\phi^2\chi^2$$

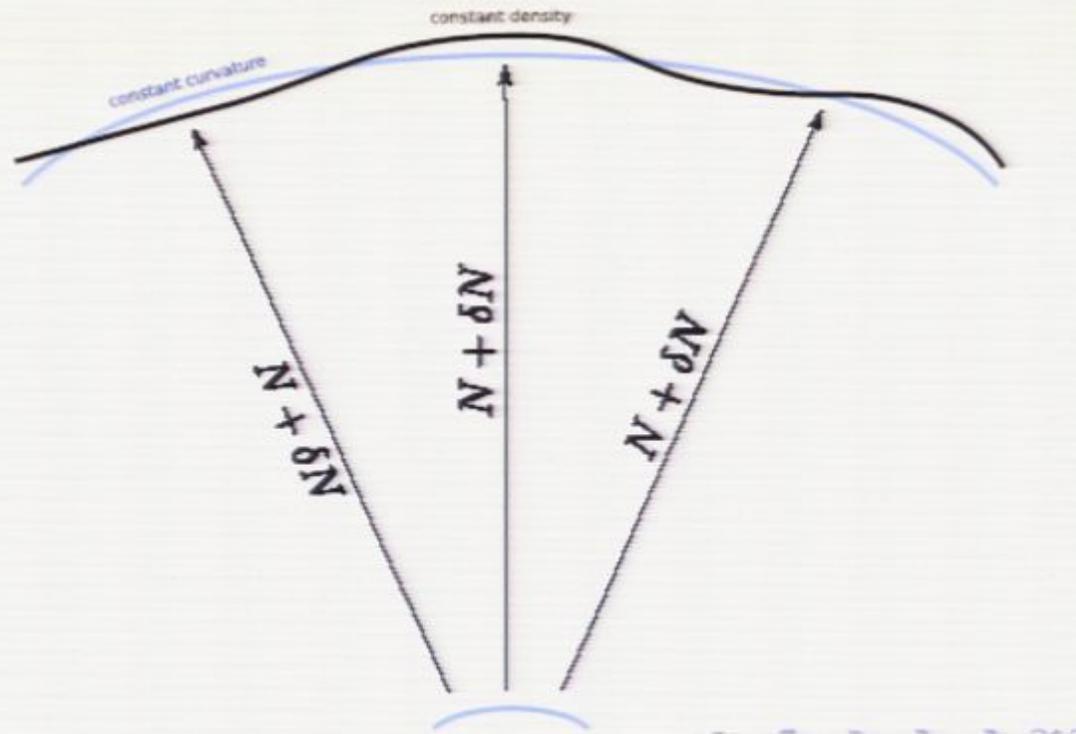
$$\ddot{\phi} - \nabla^2\phi + g^2\chi^2\phi = 0$$

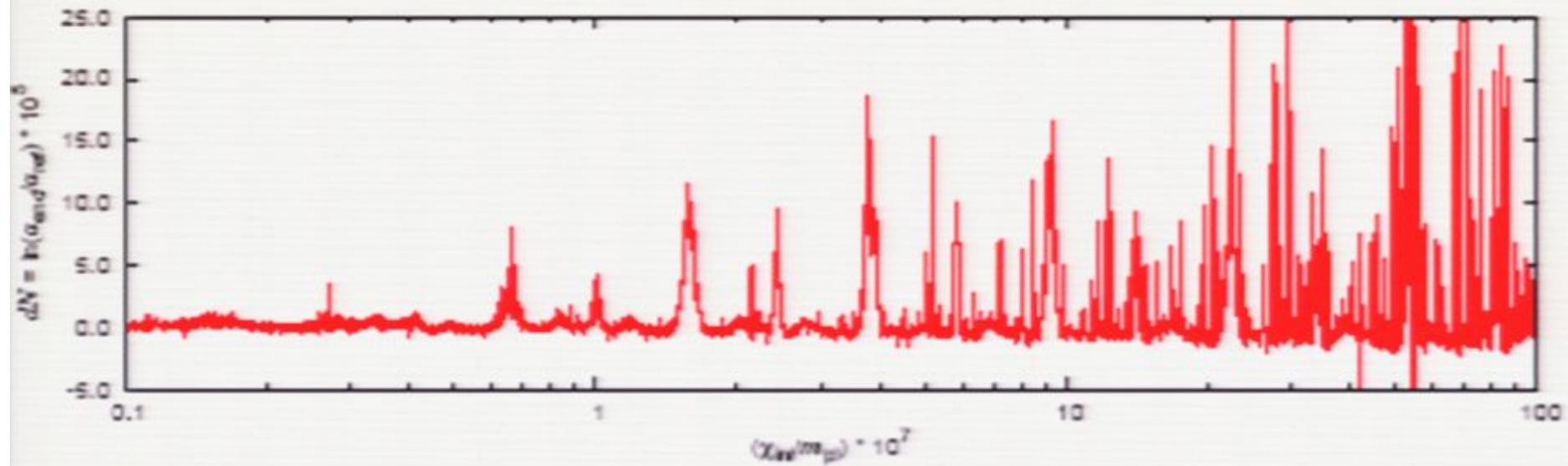
$$\ddot{\chi} - \nabla^2\chi + g^2\phi^2\chi = 0$$

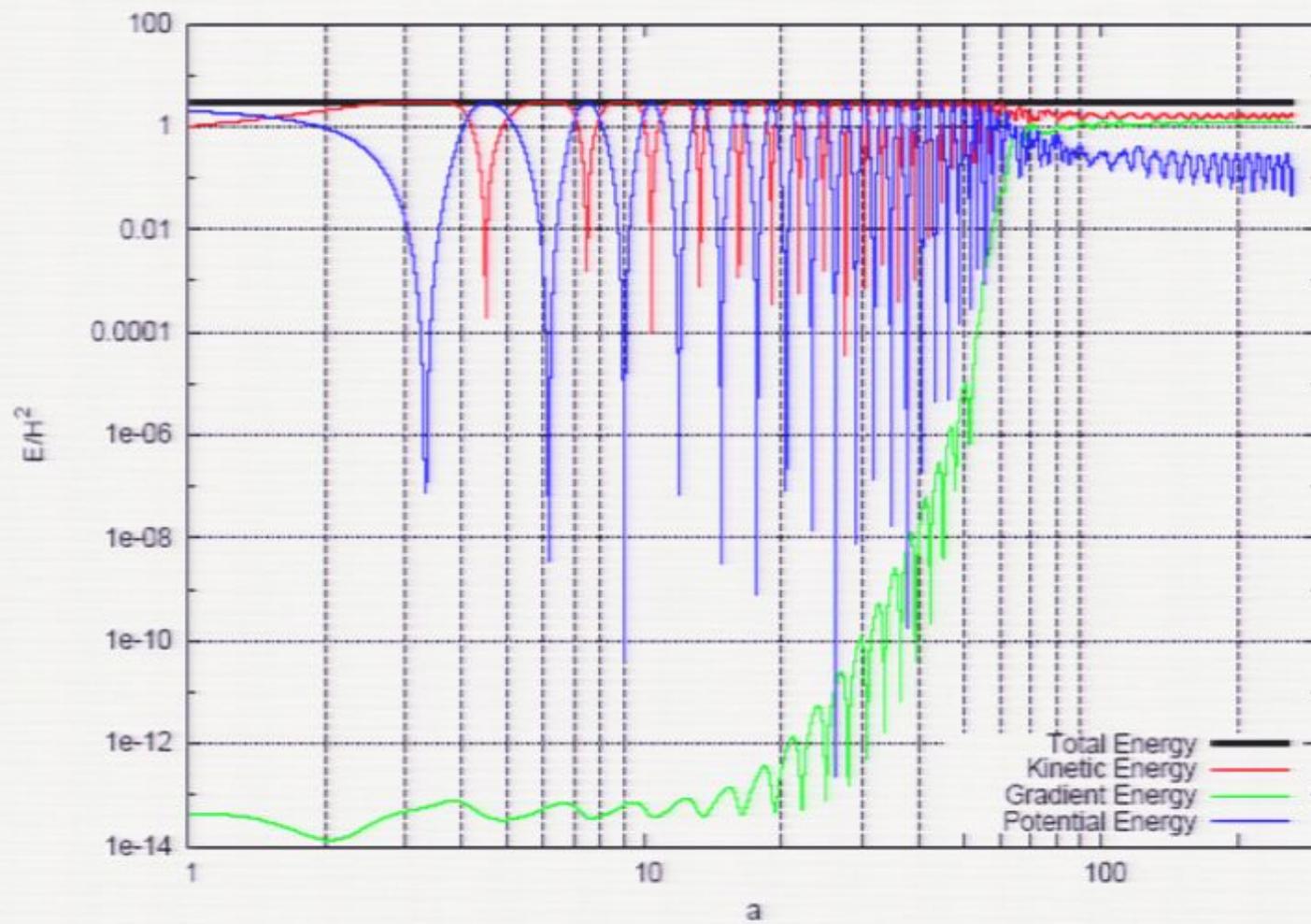
$$3H^2 = \frac{8\pi}{M_p^2} \left(\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2a^2}\nabla\phi^2 + \frac{1}{2a^2}\nabla\chi^2 + V(\phi, \chi) \right)$$

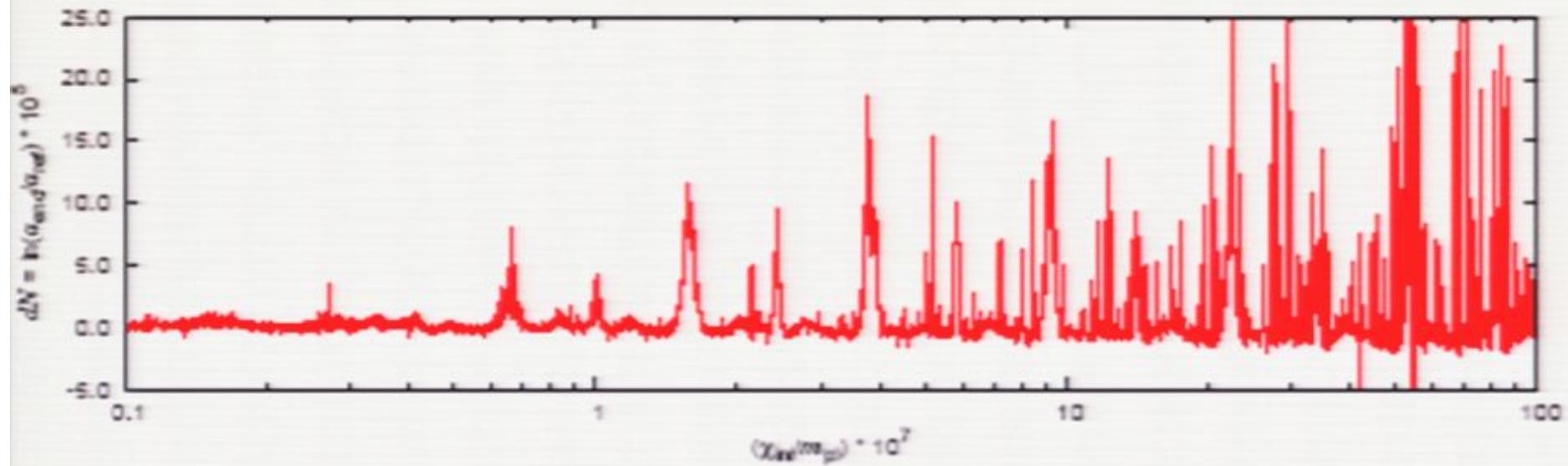
"separated universes" approximation

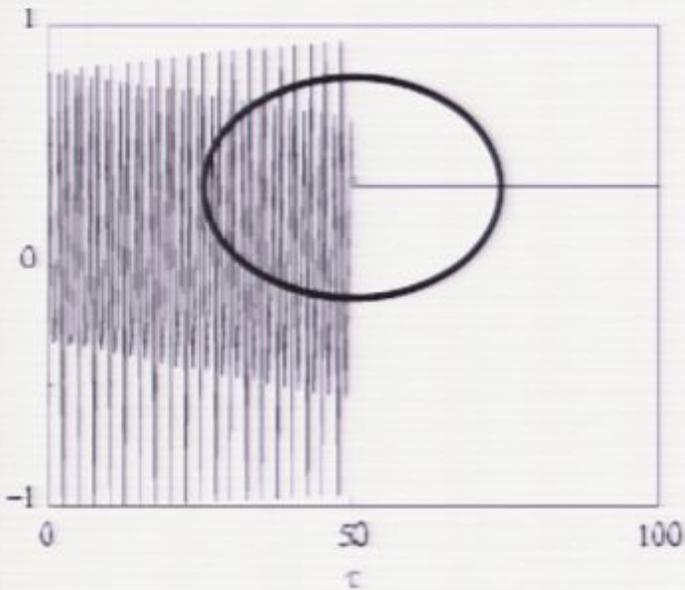
$$\zeta = \delta \ln a|_H = \delta N(\chi_i)$$











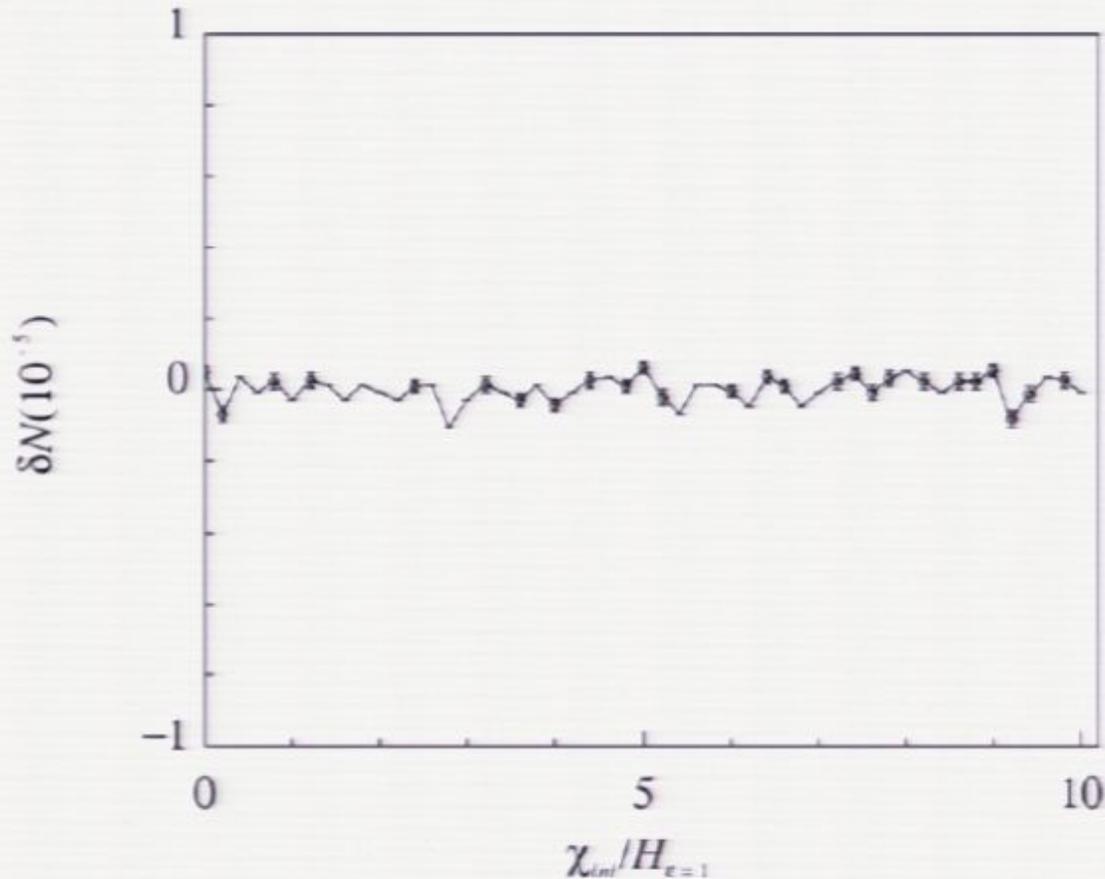
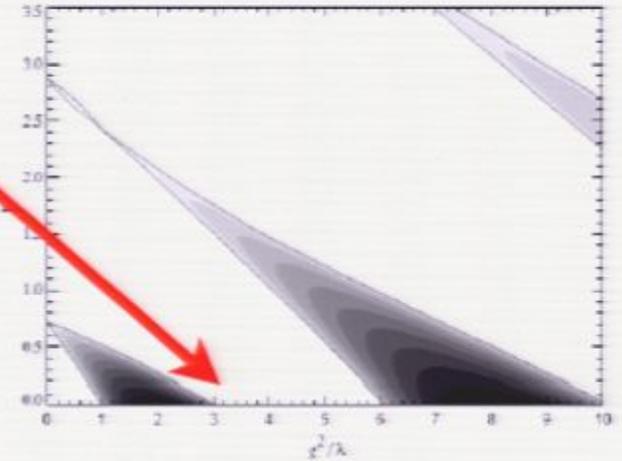
We search for ppm effects^a
 \Rightarrow Symplectic **DEFROST**:

energy conservation $\sim 10^{-13}$ level!!
 cf. **DEFROST** $\sim 10^{-5}$ level & Felder's **LatticeEasy**
 $\sim 10^{-4}$ level.

Lattice simulation codes

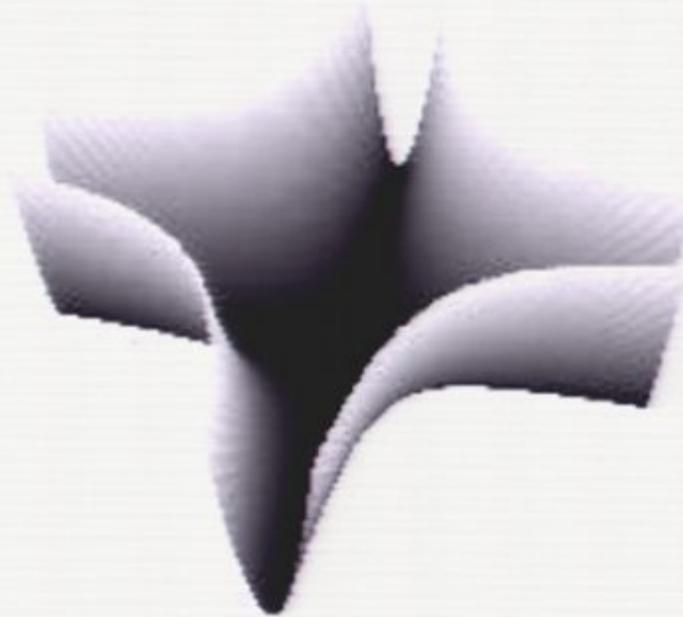
- Good publicly available codes:
LatticeEasy (G. Felder), 2nd order PDE solver;
DEFROST (A. Frolov), 2nd order PDE solver;
- Our new lattice simulation code:
 - Higher (optional 2nd, 4th, 6th, 8th) order Symplectic PDE integrator
 - Energy conservation $\sim 10^{-13}$ level!!
 - MPI parallelized for large size simulation
 - initialization in configuration space (DEFROST algorithm) or momentum space (LatticeEasy algorithm).
 - Numerically calculate initial super-horizon mode functions
 - More recent updates (non-canonical scalar fields simulation; a module for GW spectrum calculation...)

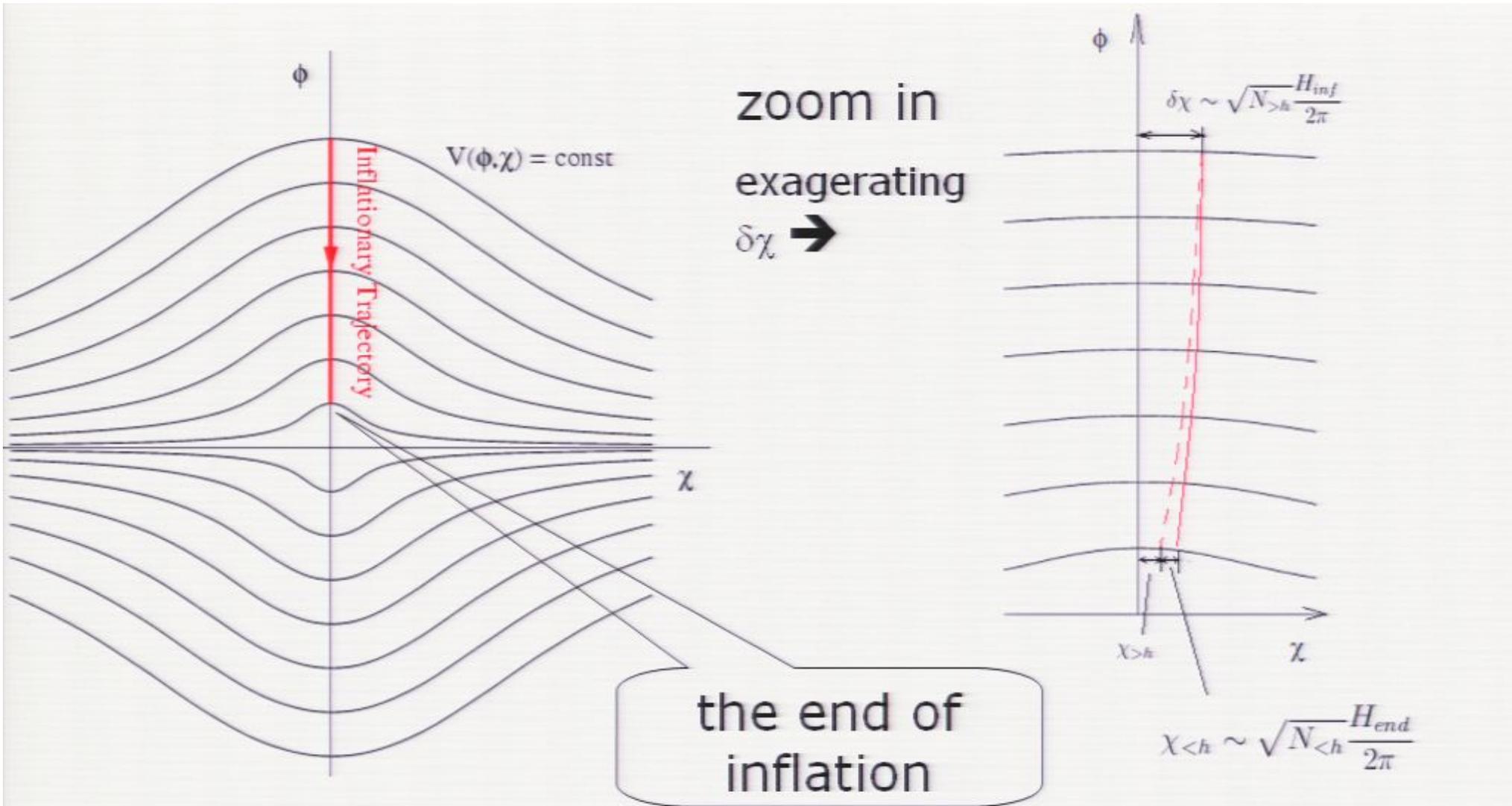
if the $k=0$ mode is not in the parametric resonance bands ($g^2/\lambda=3$ example)
then $\delta \ln a$ is not modulated by χ_b



Chaotic Billiards

$$\frac{1}{2}\dot{\phi}^2 + \frac{1}{2}\dot{\chi}^2 + \frac{1}{2}g^2\phi^2\chi^2$$

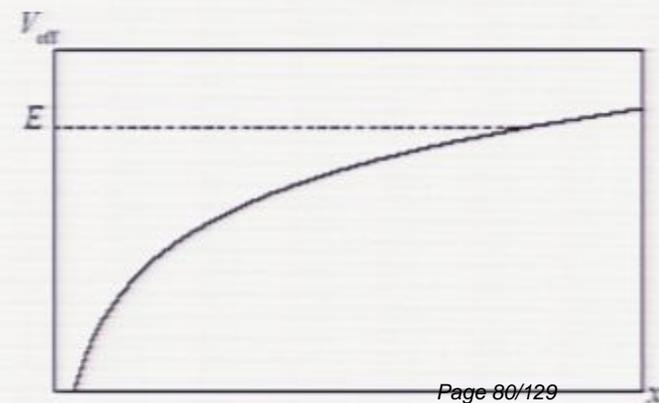
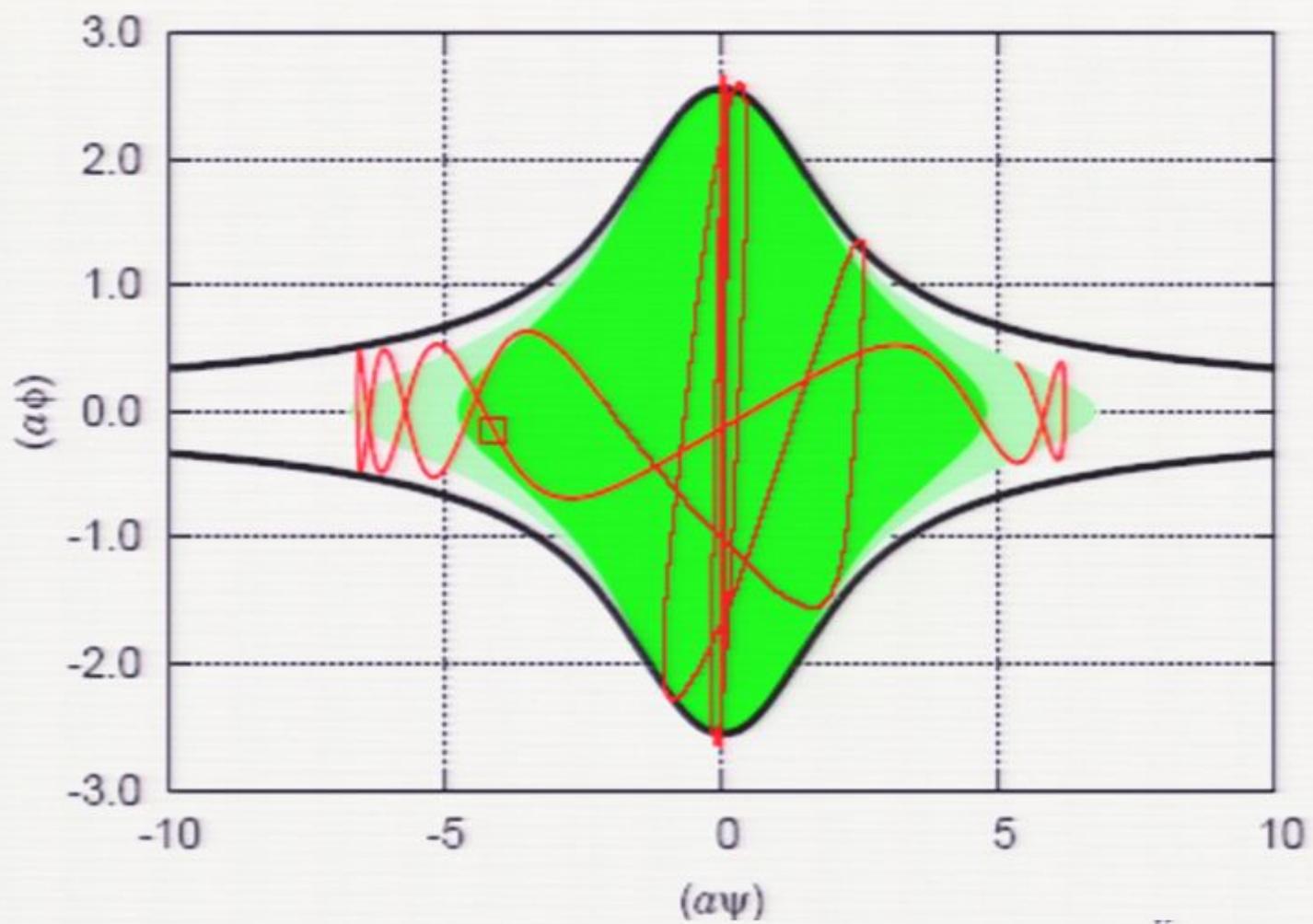


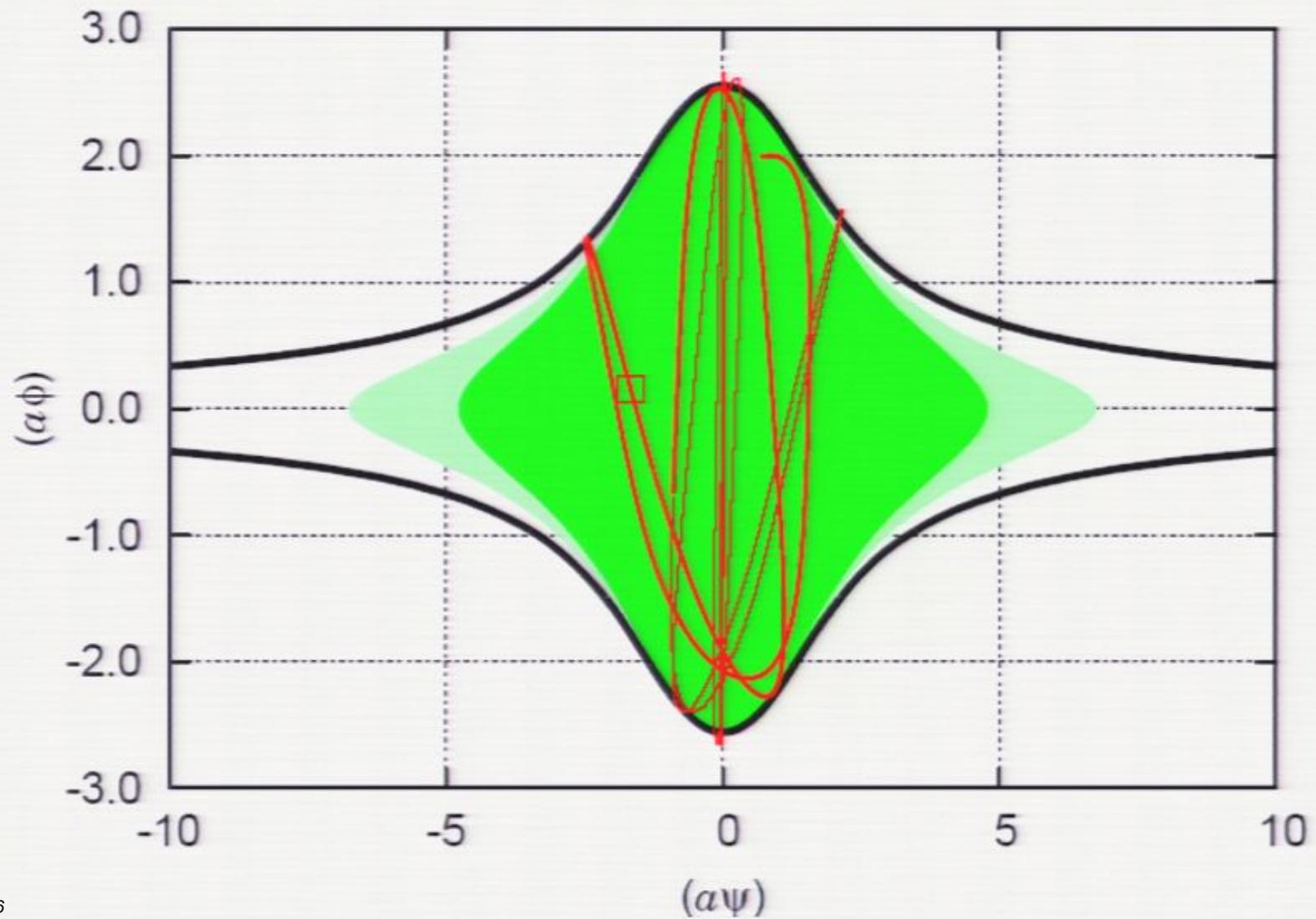


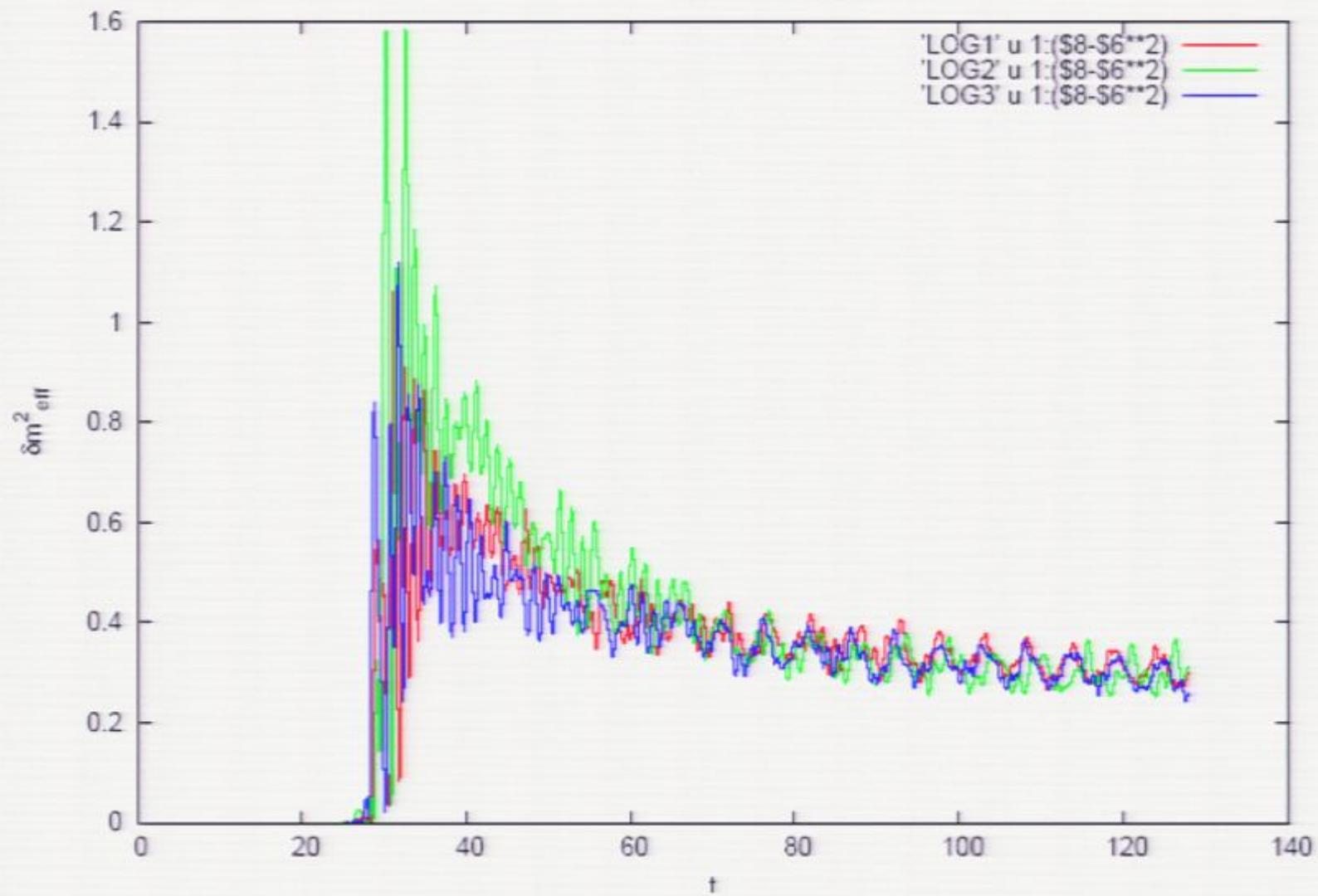
$$\chi_i = \chi_{>h} + \chi_{<h}$$

$N_{>h}$ (? efolds) \rightarrow # of efolds before current horizon scale (10^4 Mpc) exits the horizon

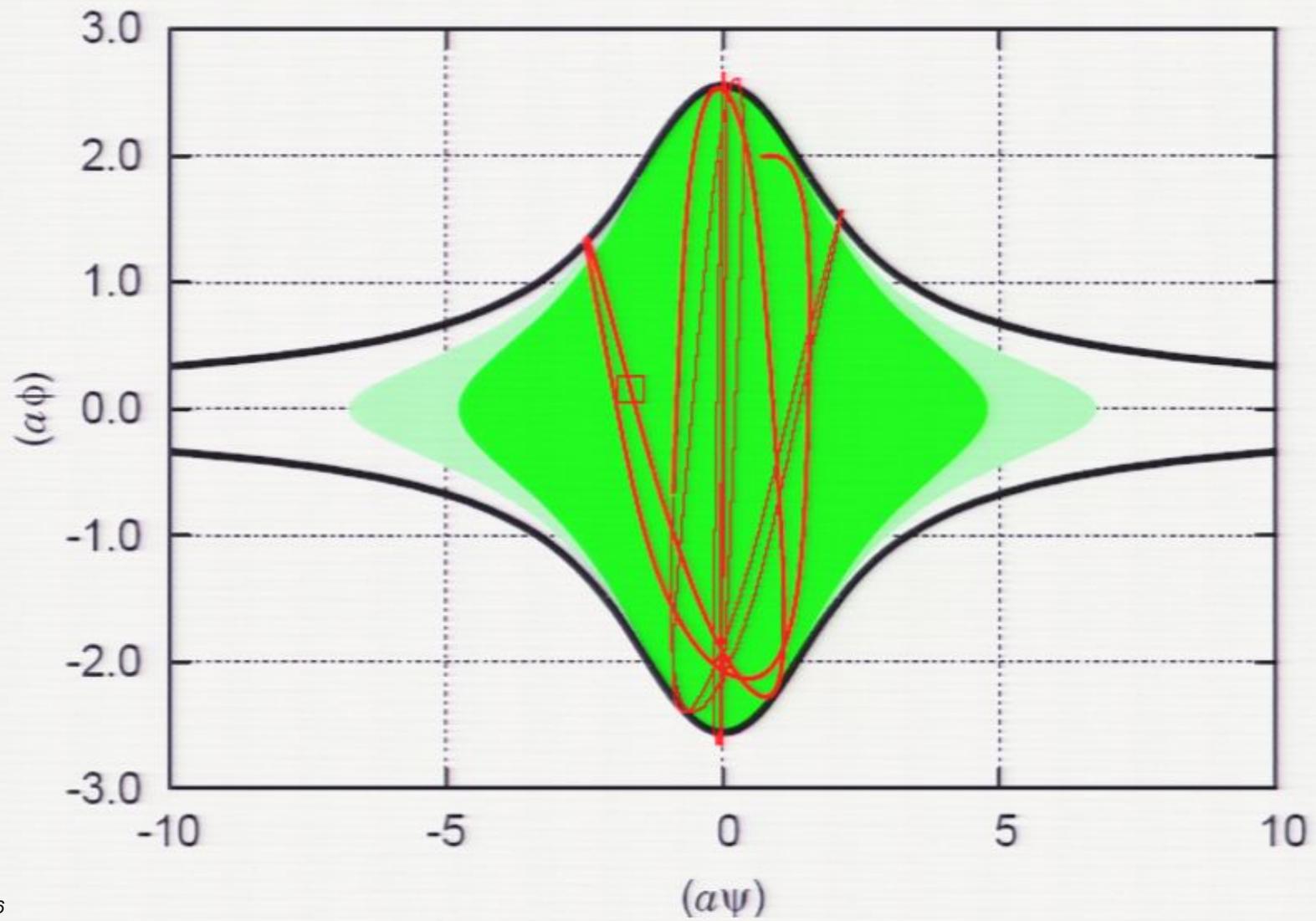
$N_{<h}$ (~65 efolds) \rightarrow # of efolds – from when current horizon scale exits the horizon until the end of inflation

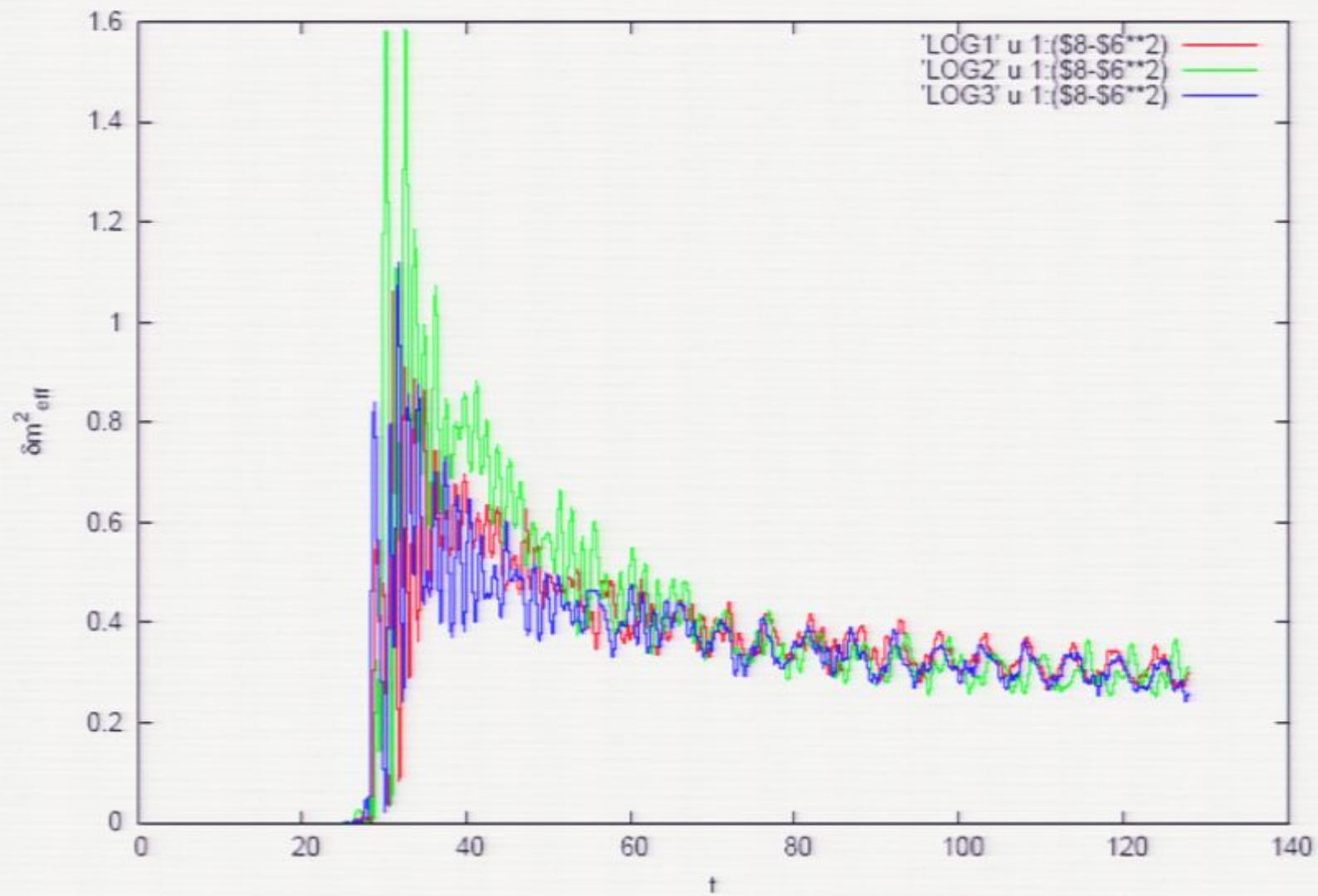


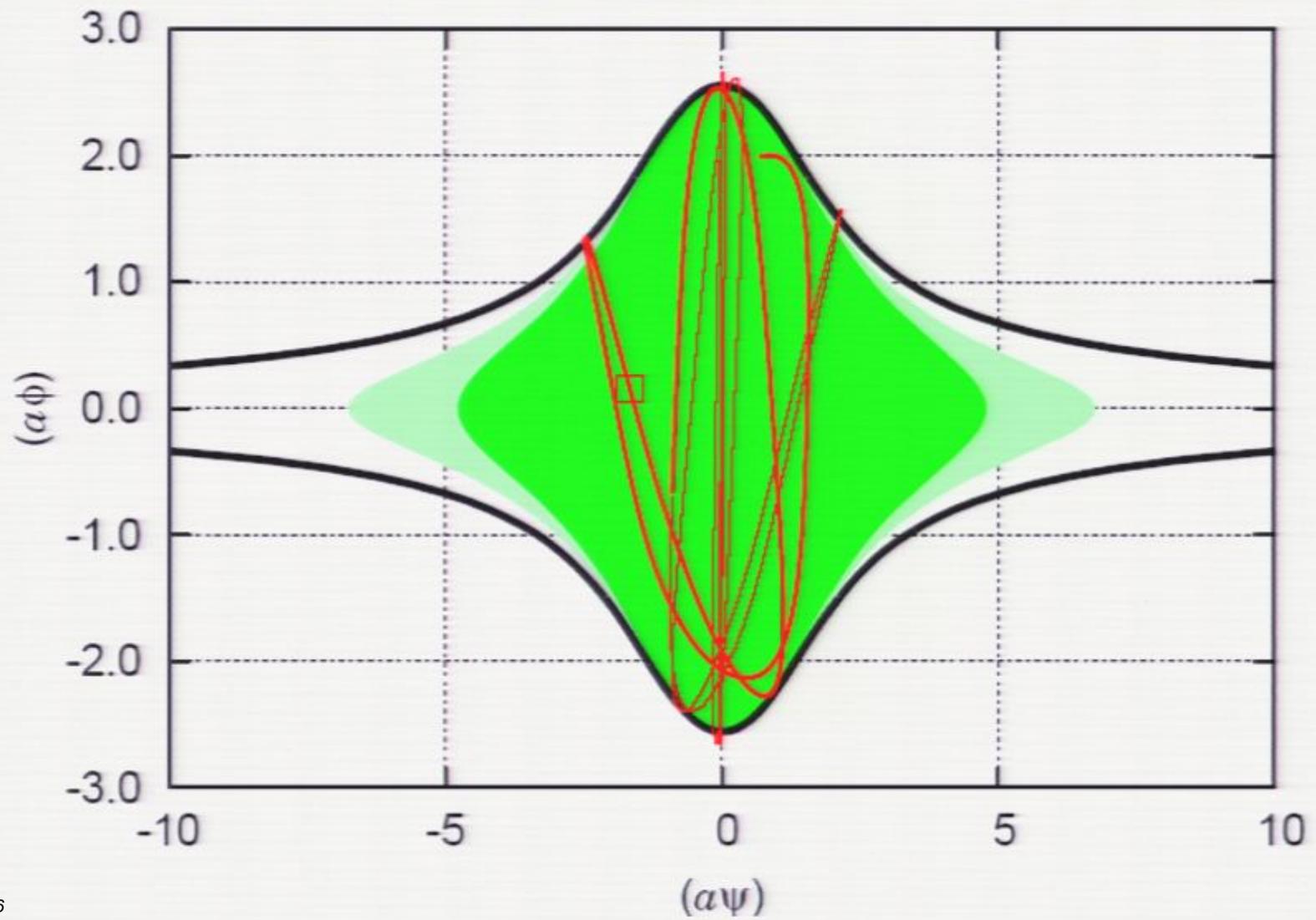




Billiard no spikes

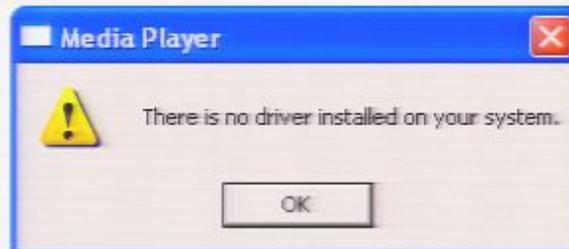




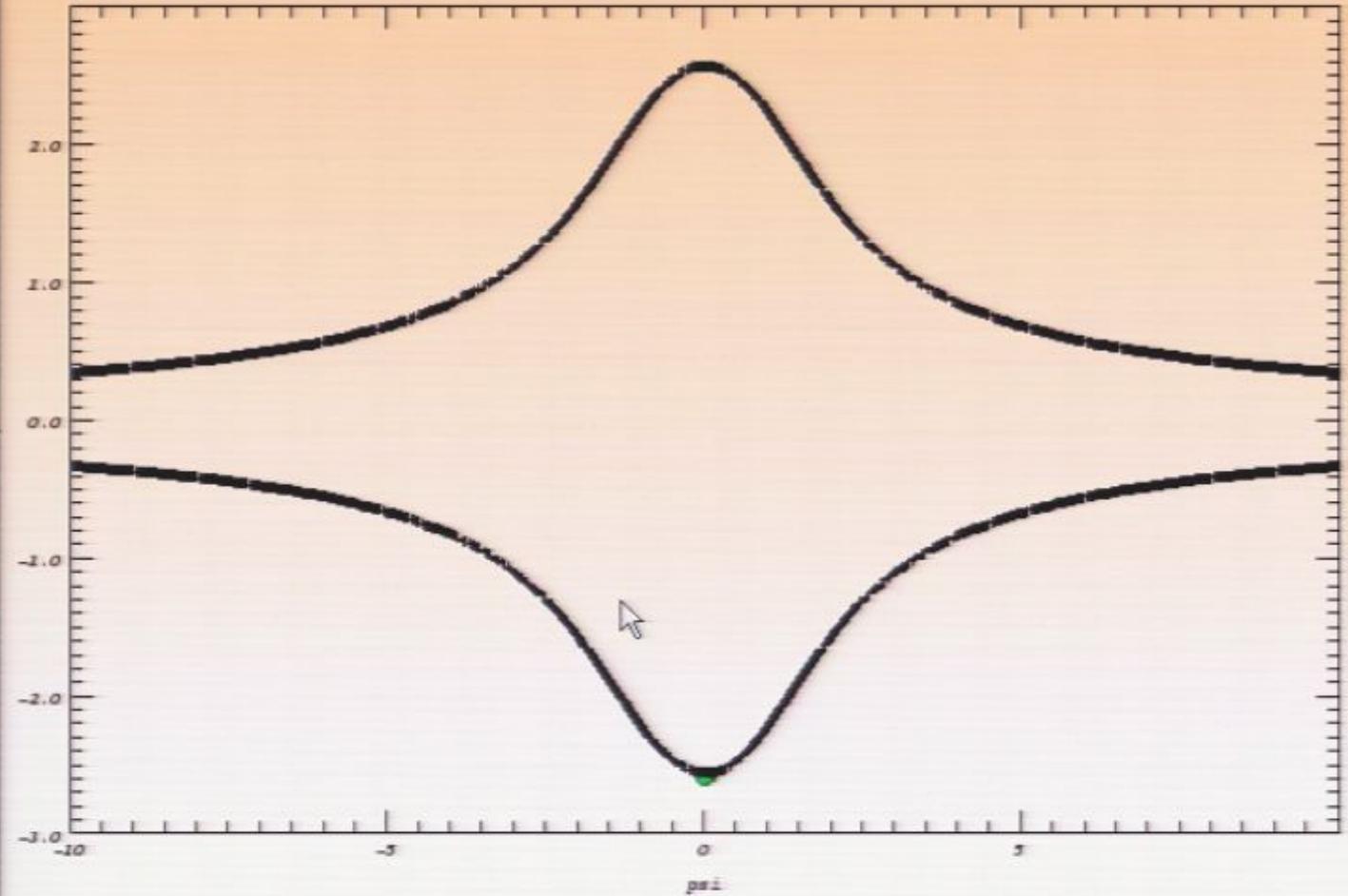


Billiard no spikes

Billiard no spikes



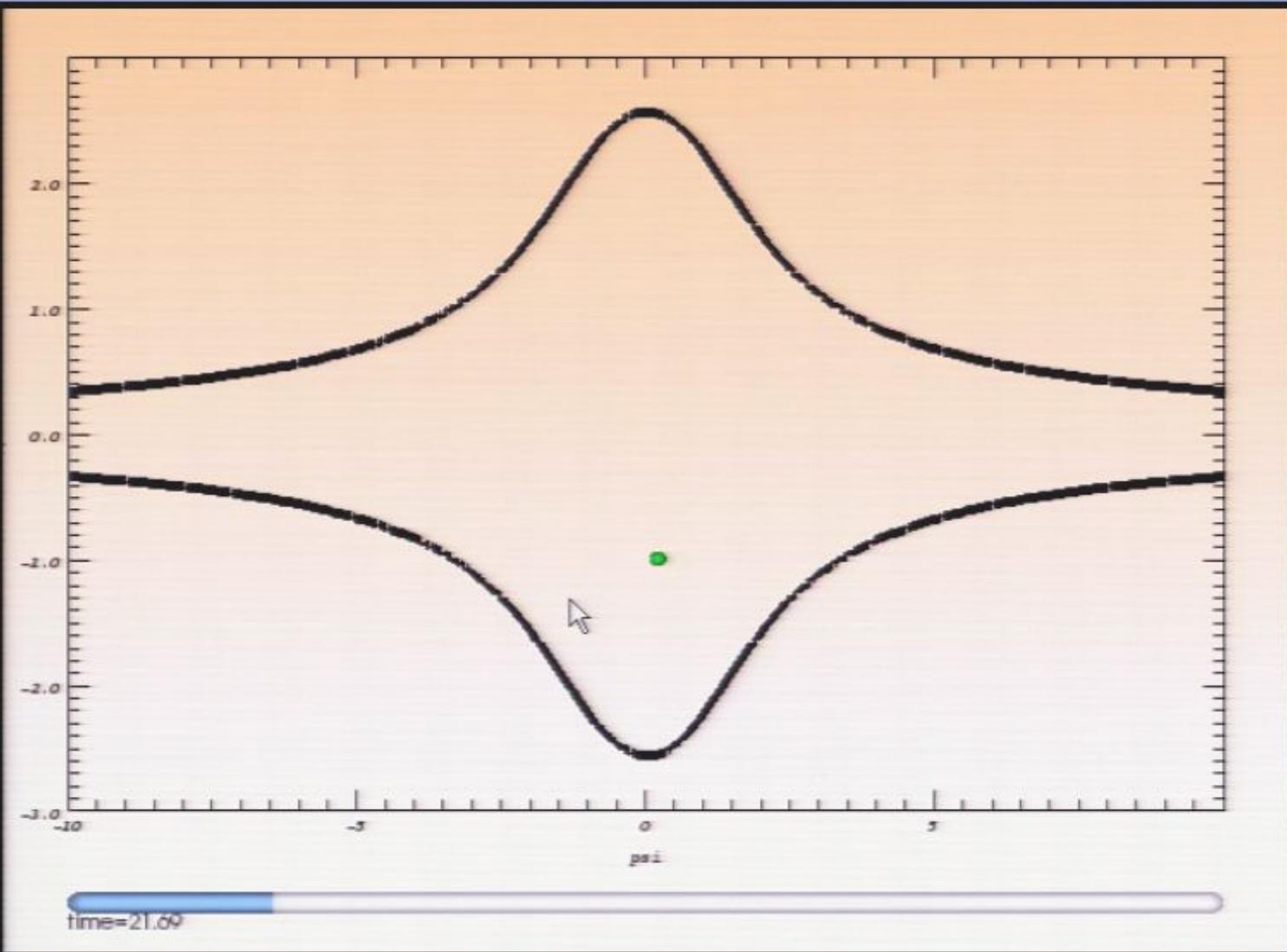
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster



time=1.56

Playing 00:00

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Online
- Hooser

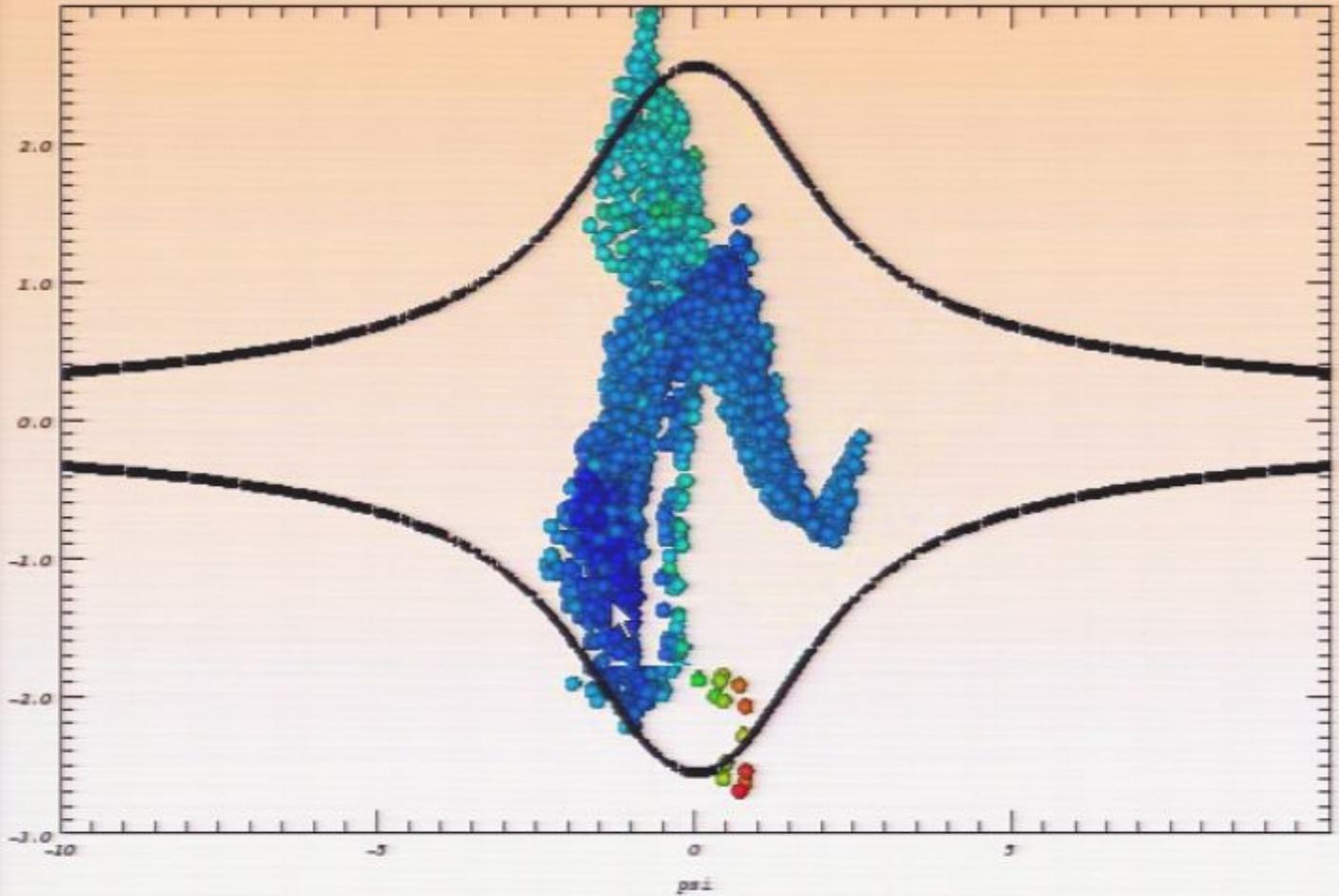


time=21.09

Clip: billiard-none

00:13

- Now Playing
- Media Guide
- Copy from
- Media Library
- Radio
- Copy to CD Device
- Premium Services
- Music Center

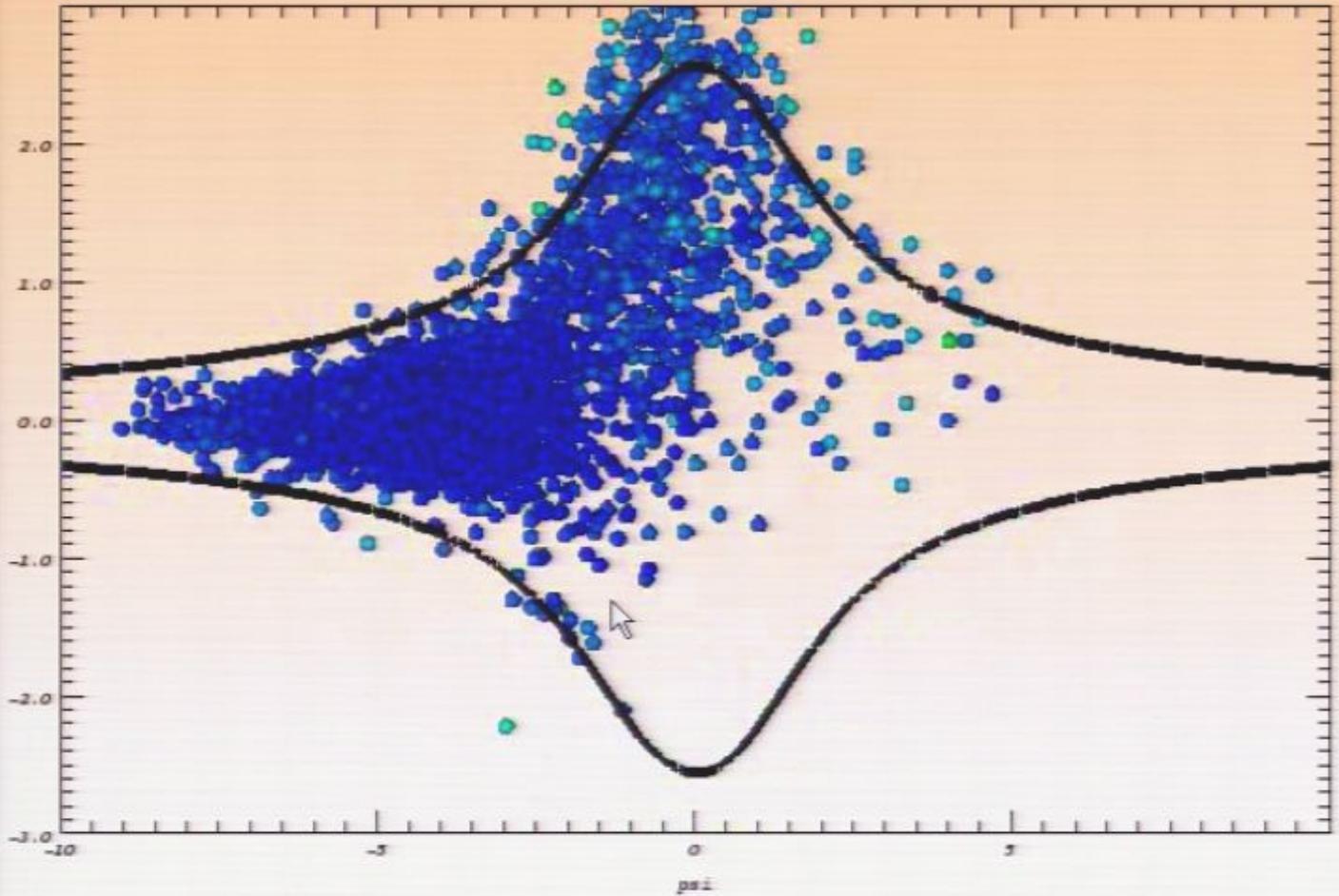


time=32.56

Clip: billiard-none

00:20

- Now Playing
- Media Guide
- Copy from
- Media Library
- Radio
- Copy to CD Device
- Premium Services
- Audio
- Booster

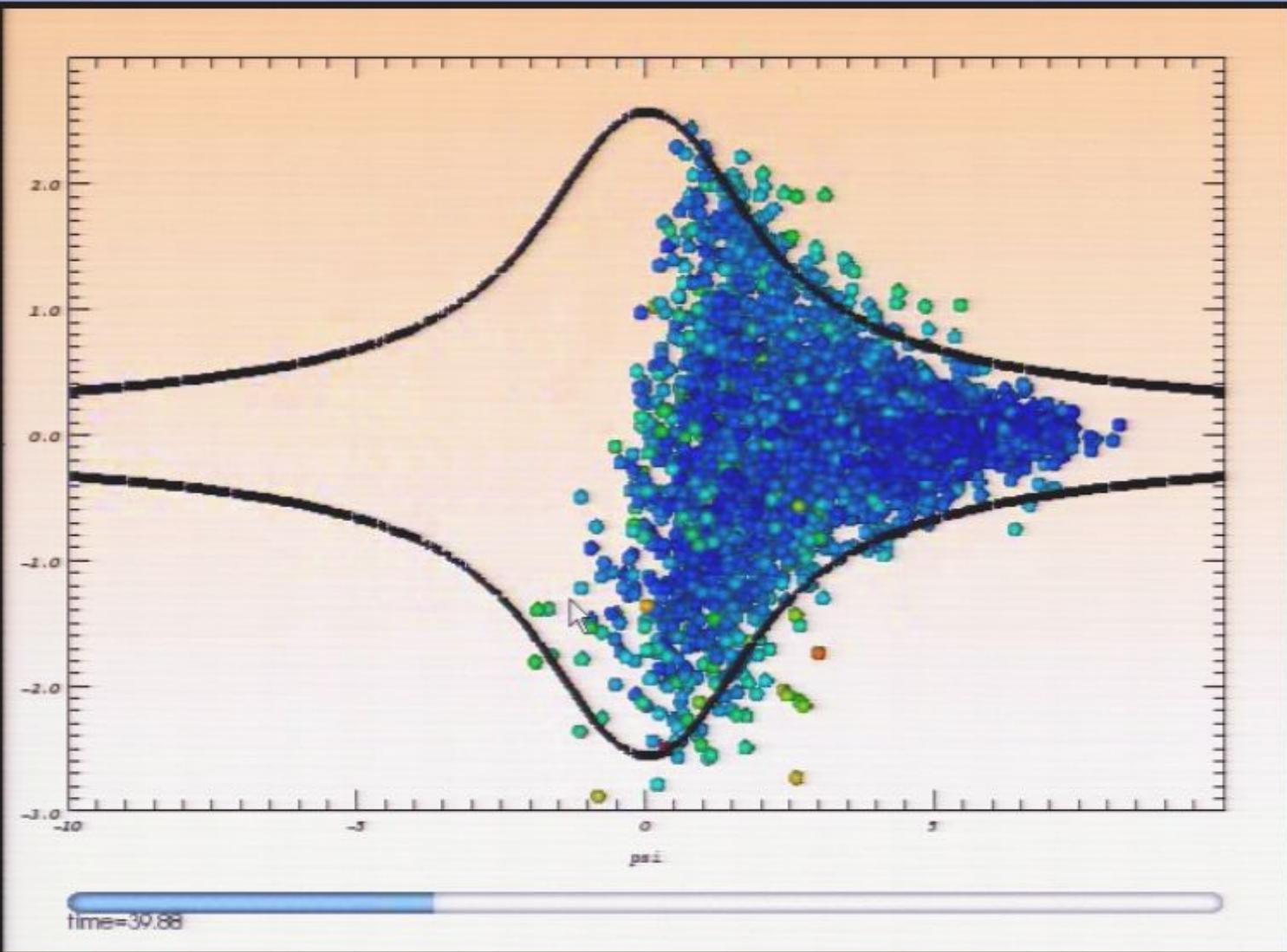


time=36.31

Clip: billiard-none

00:22

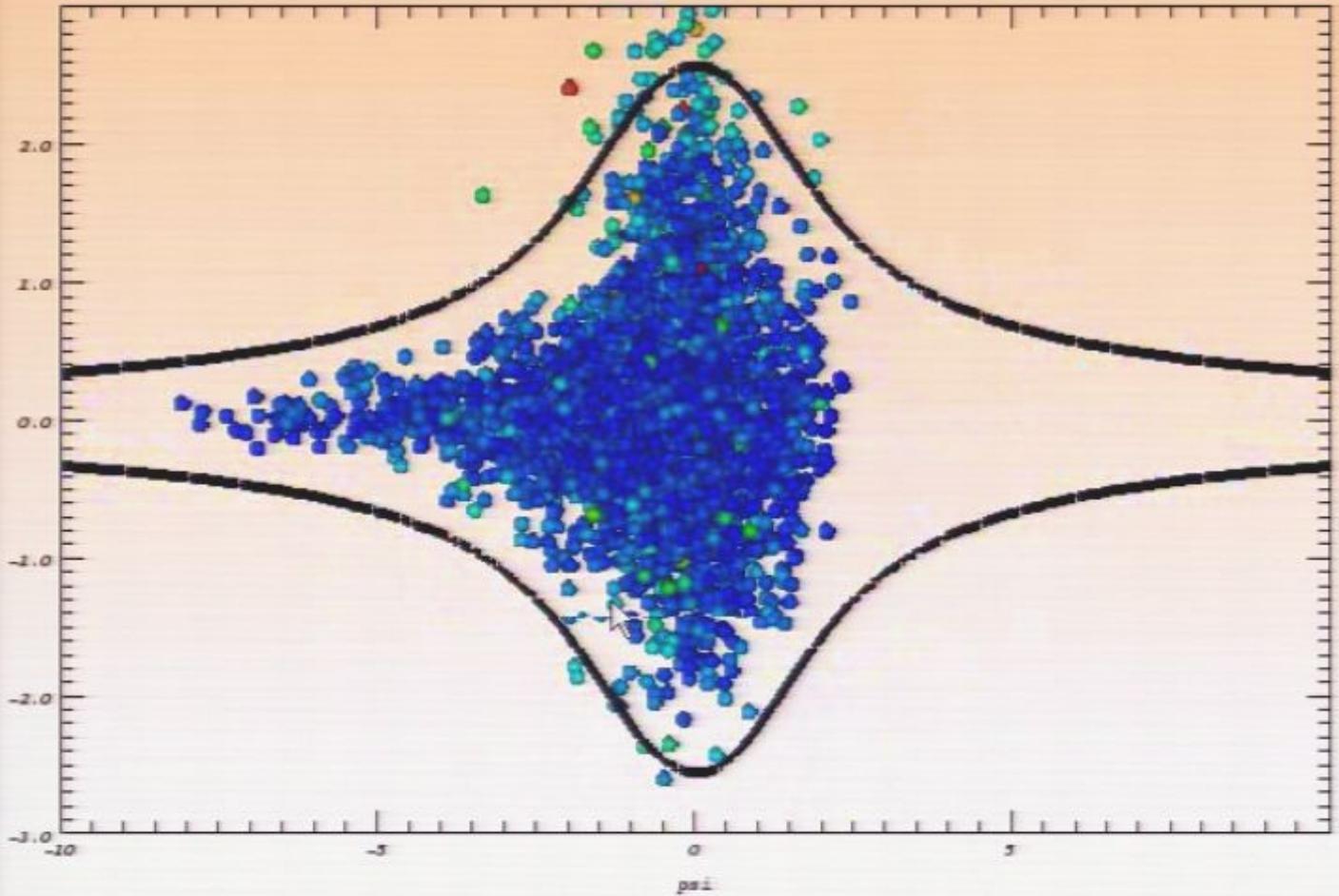
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster



Playing

00:26

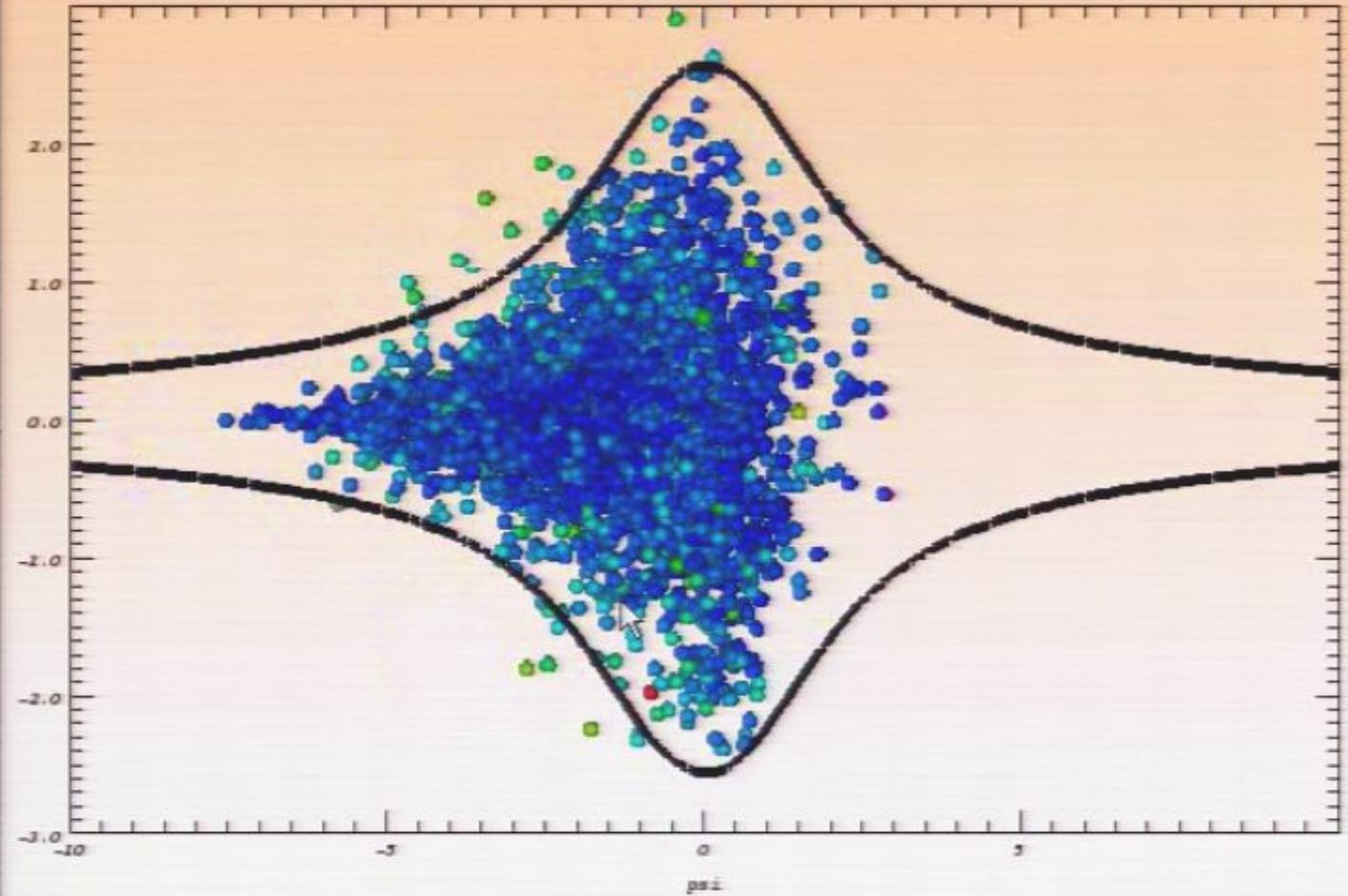
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster



Playing

00:28

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster

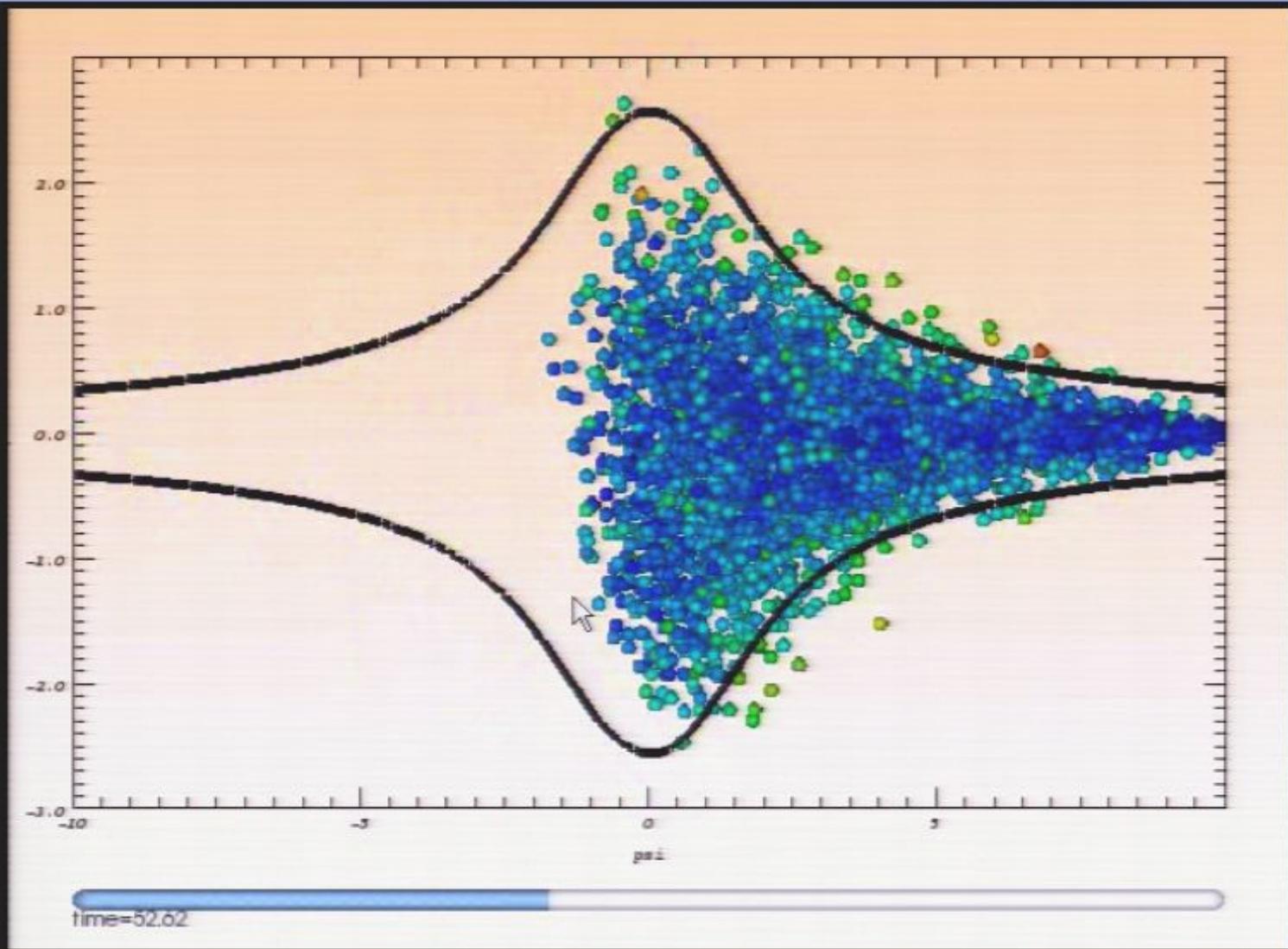


time=48.88

Playing

00:31

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music Center

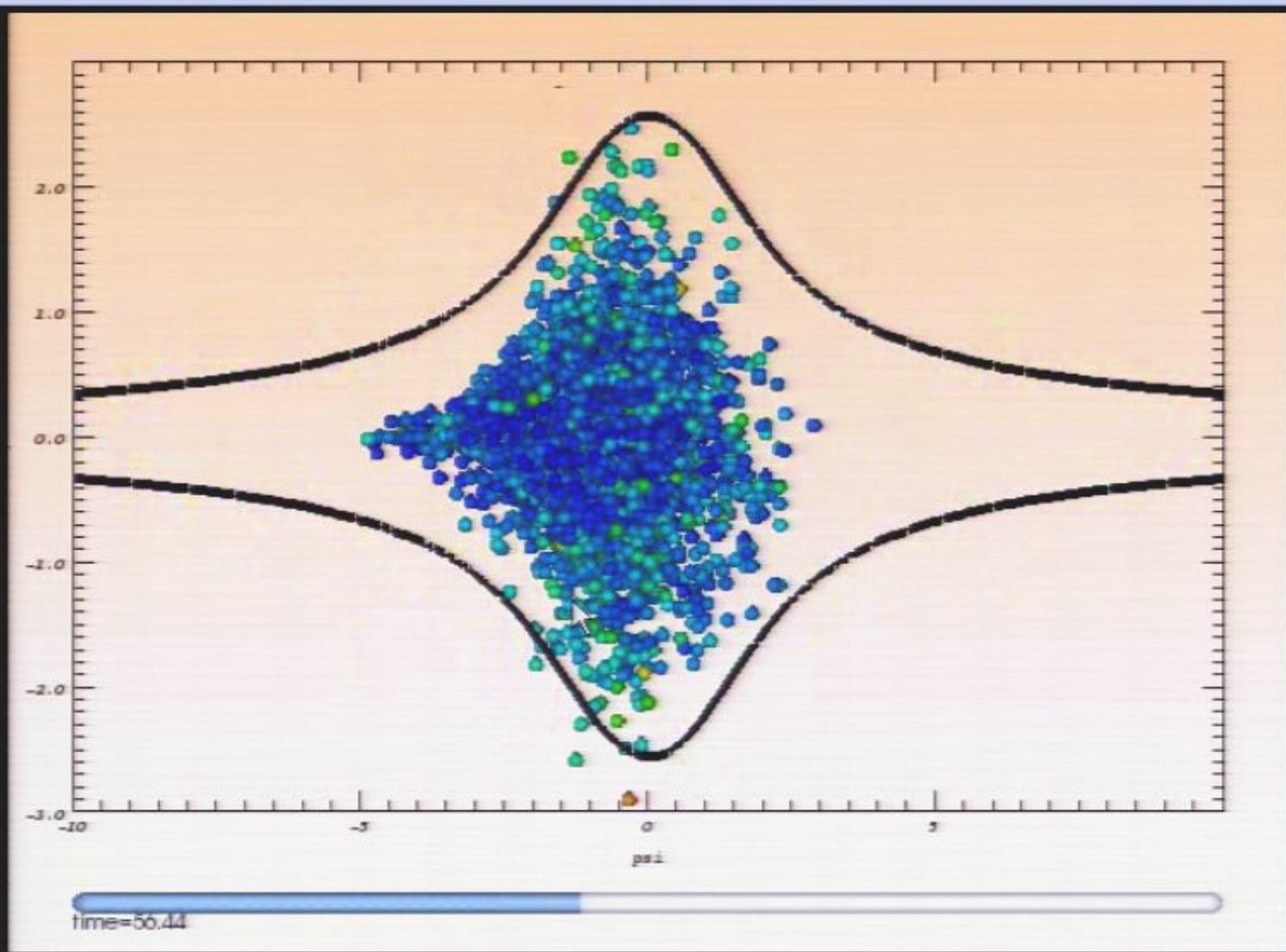


time=52.62

Playlist: Playlist1

00:33

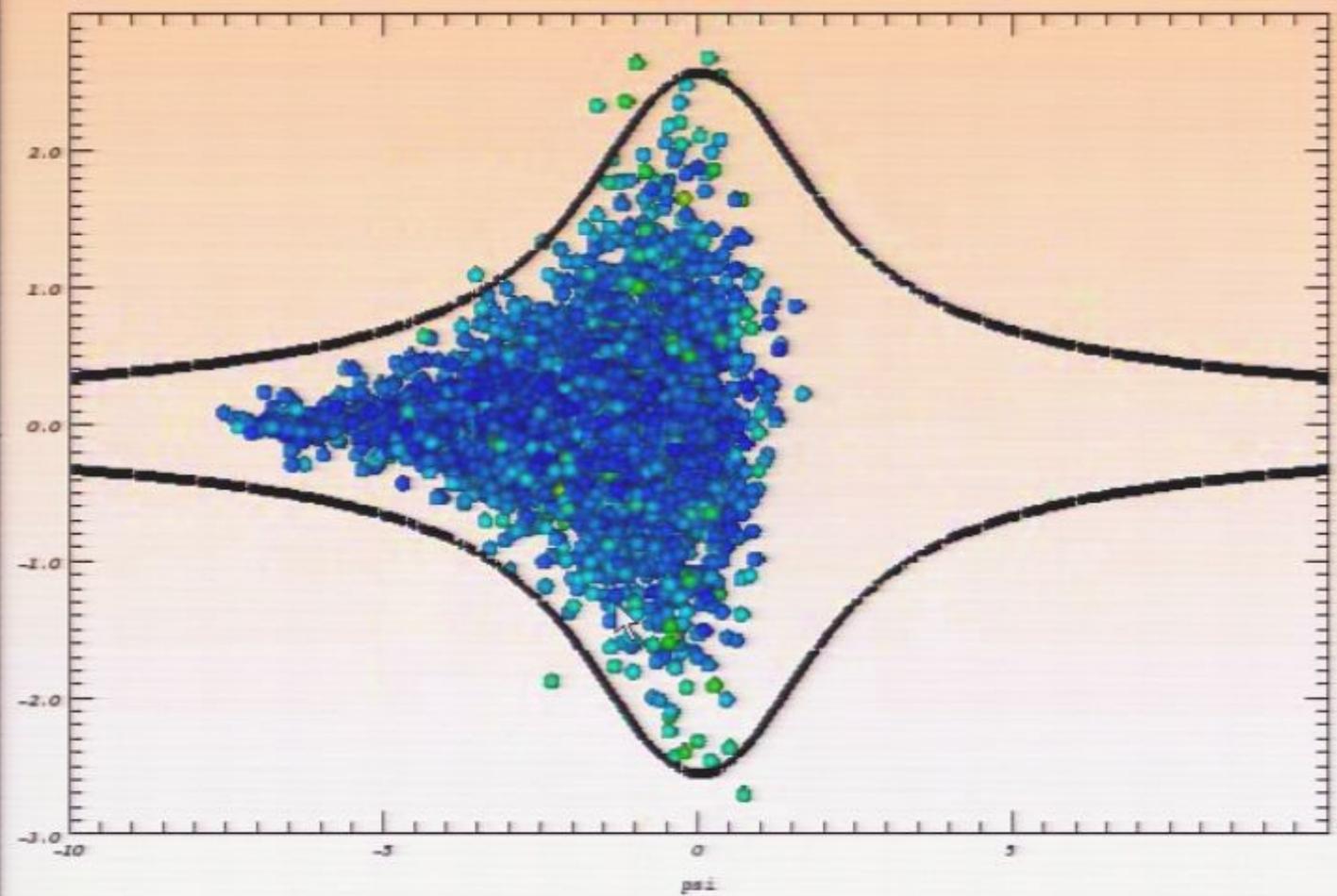
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Online
- Booster



Clip: billiard-none

00:36

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster

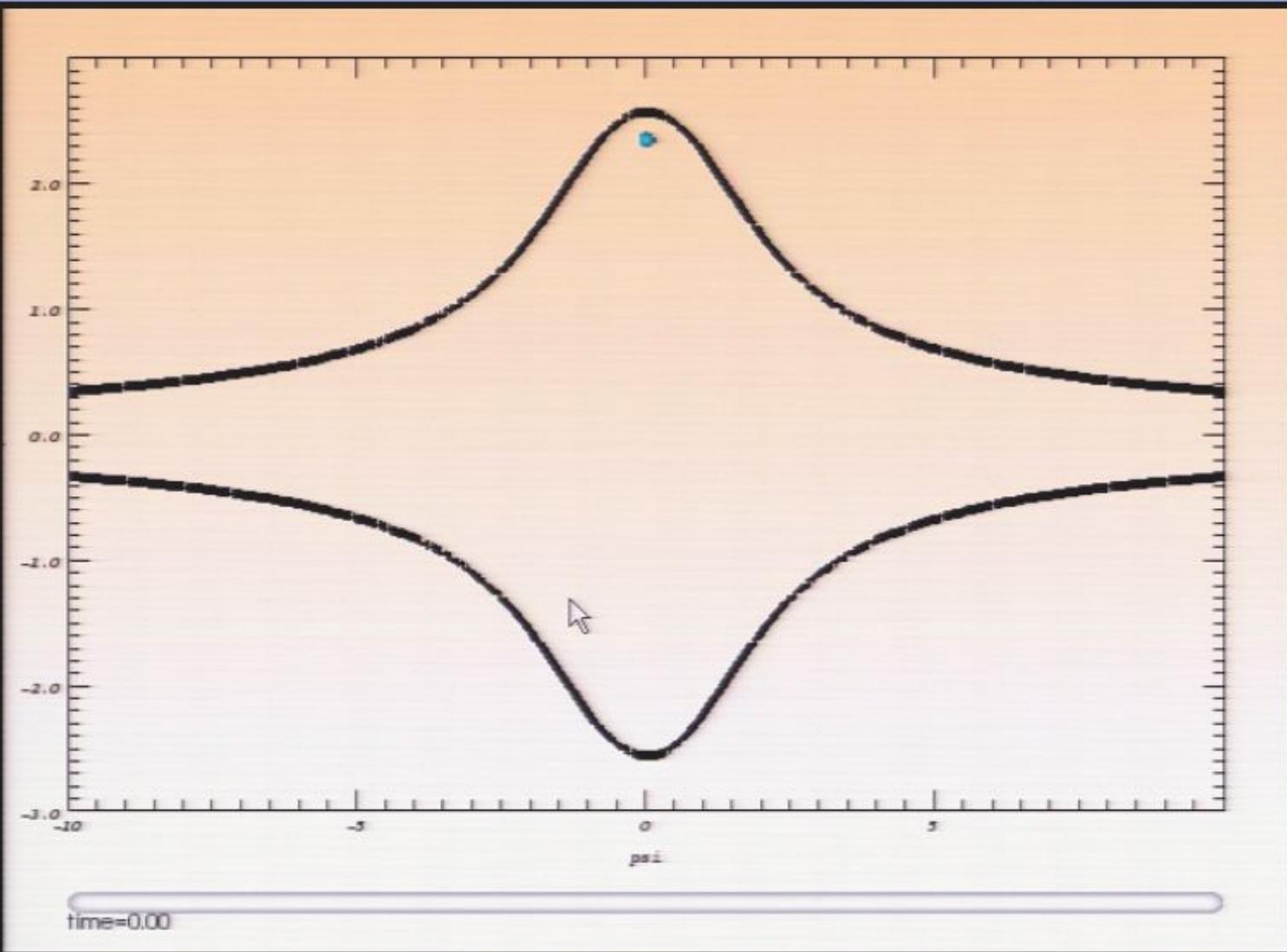


time=00:04

Clip: billiard-none

00:38

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster



time=0.00

Stopped

Billiard no spikes



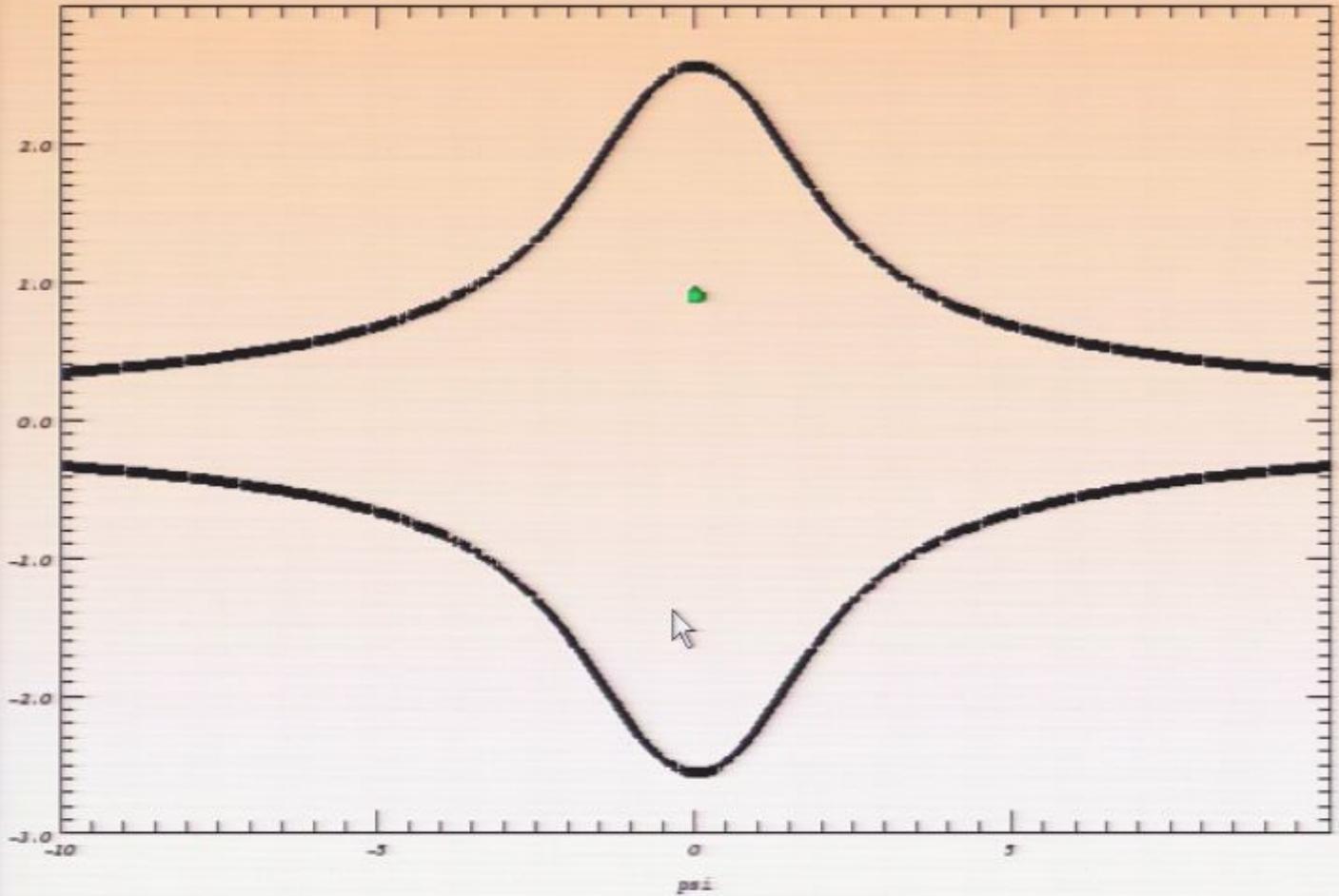
Billiar with [spikes](#)



Billiar with [spikes](#)



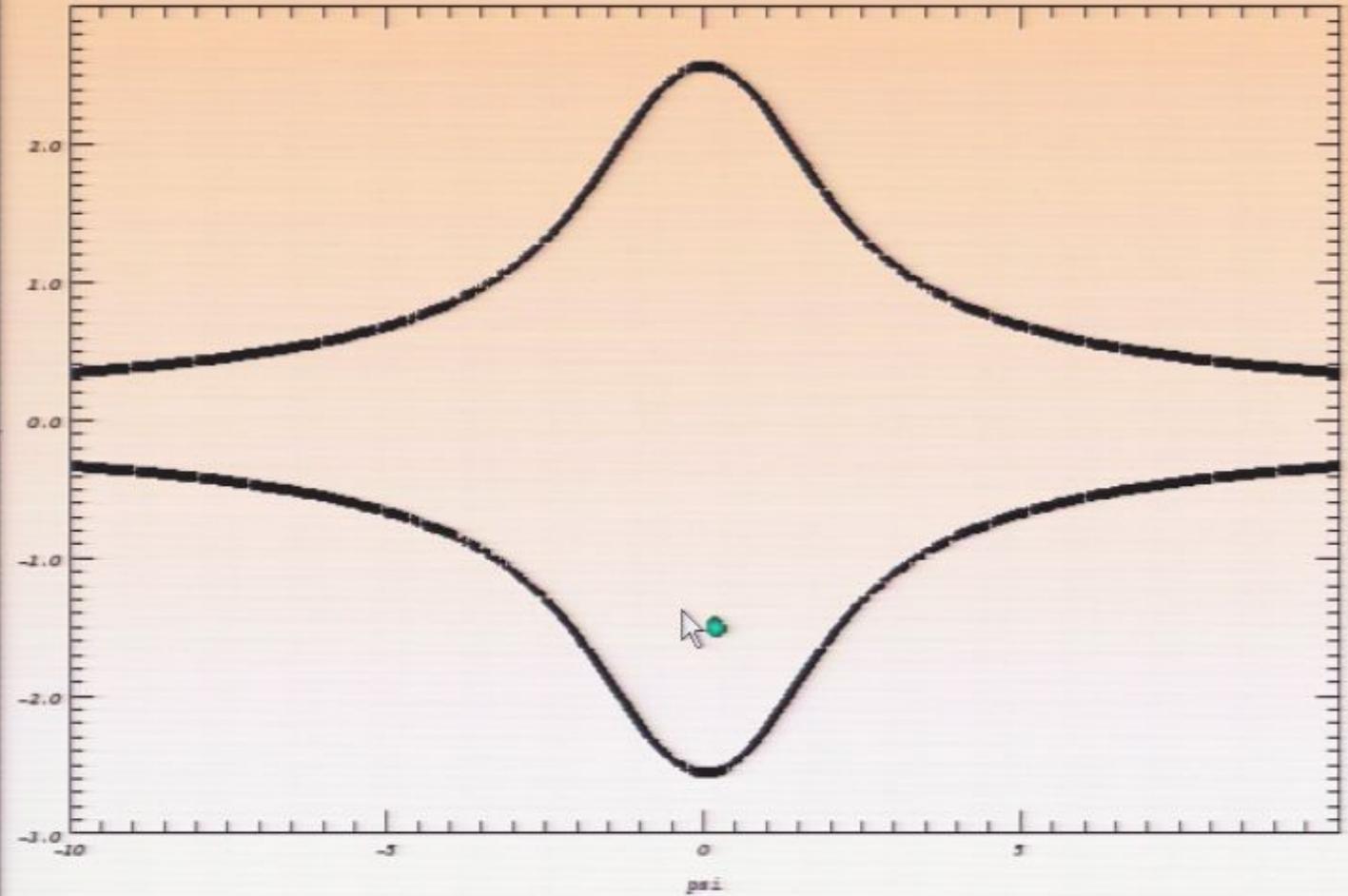
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster



time=0.81

Playing 00:00

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music booster

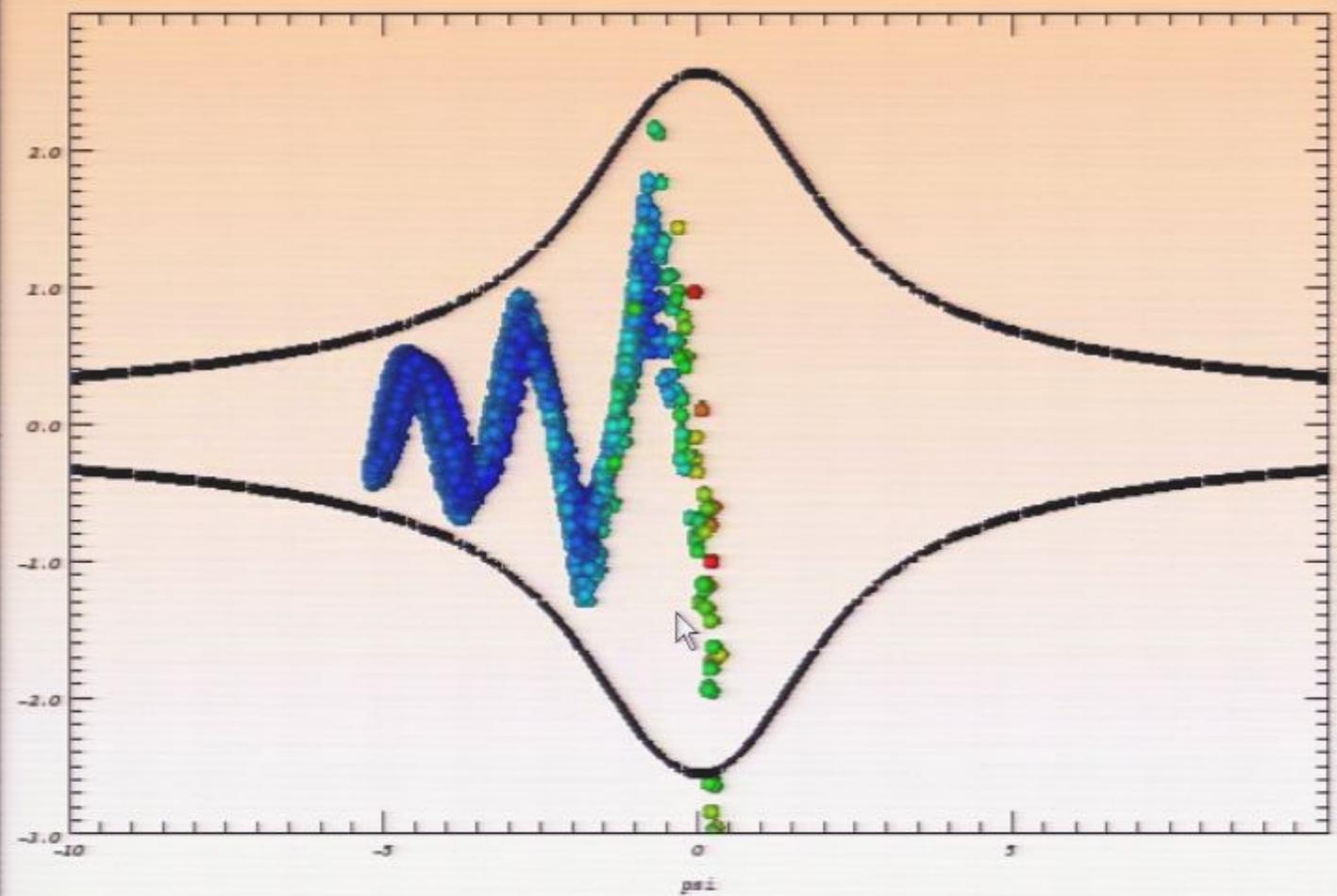


time=24.31

Clip: billiard-peak

00:15

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Online music

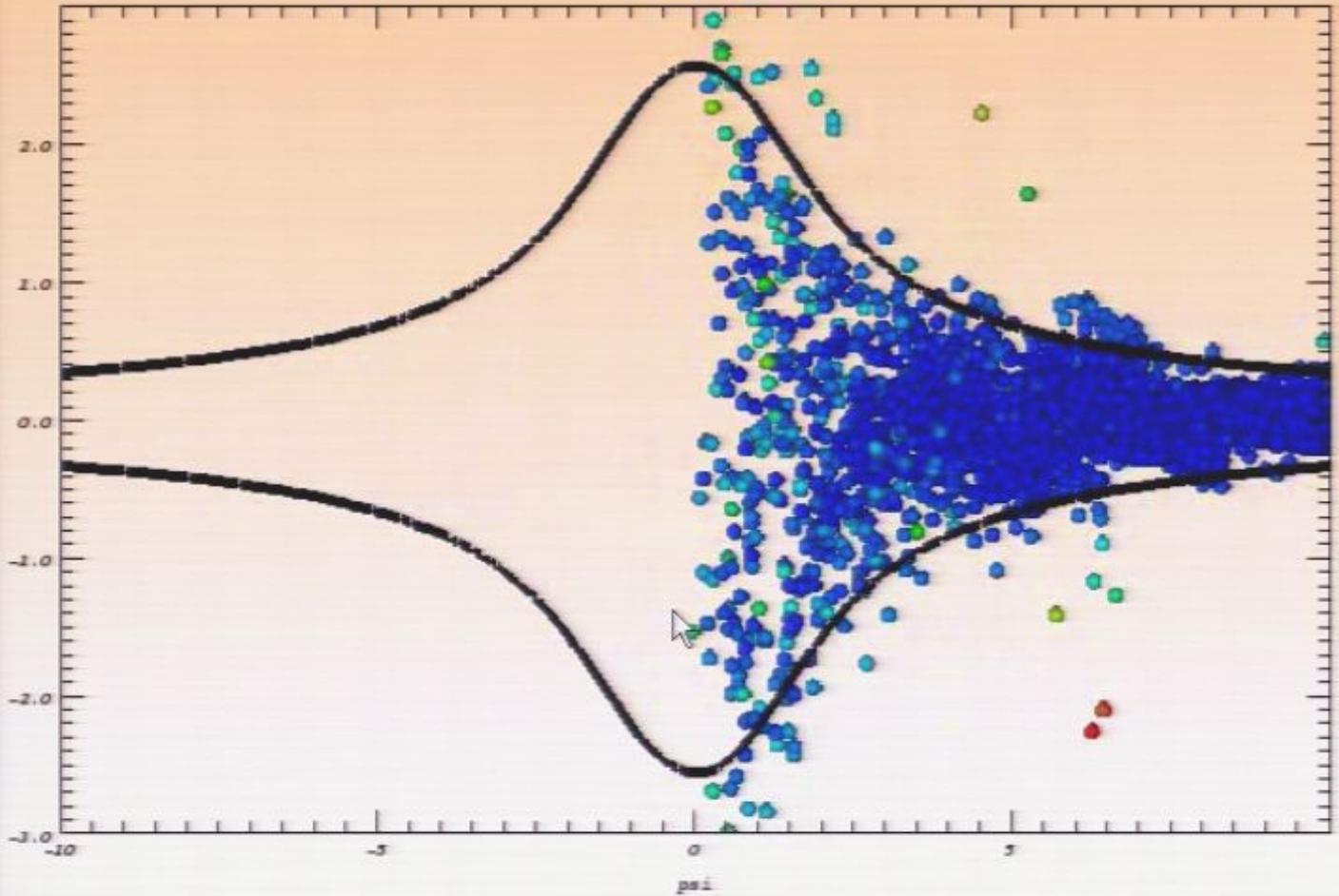


time=32.38

Clip: billiard-peak

00:21

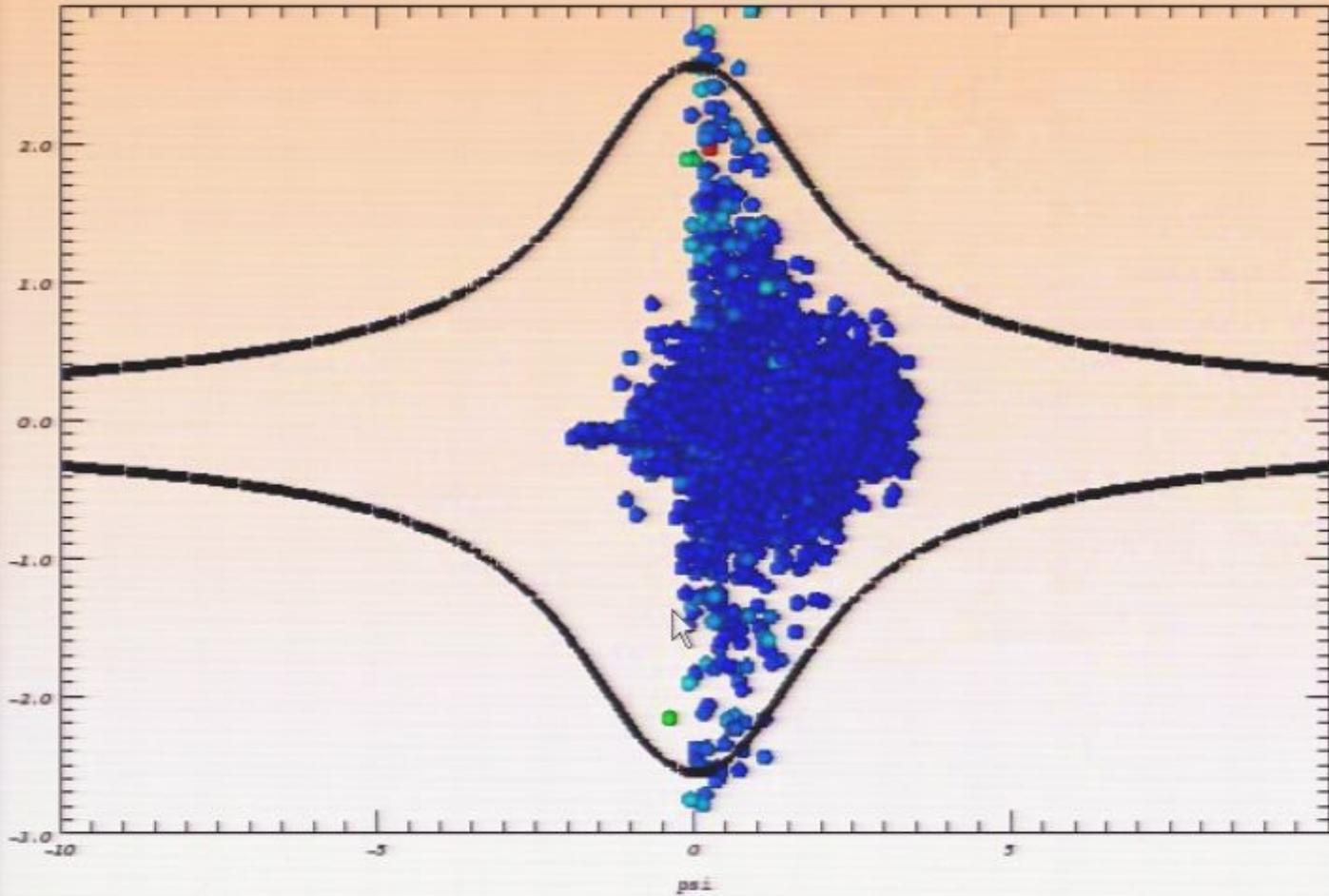
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster



time=36.81

Clip: billiard-peak

00:23

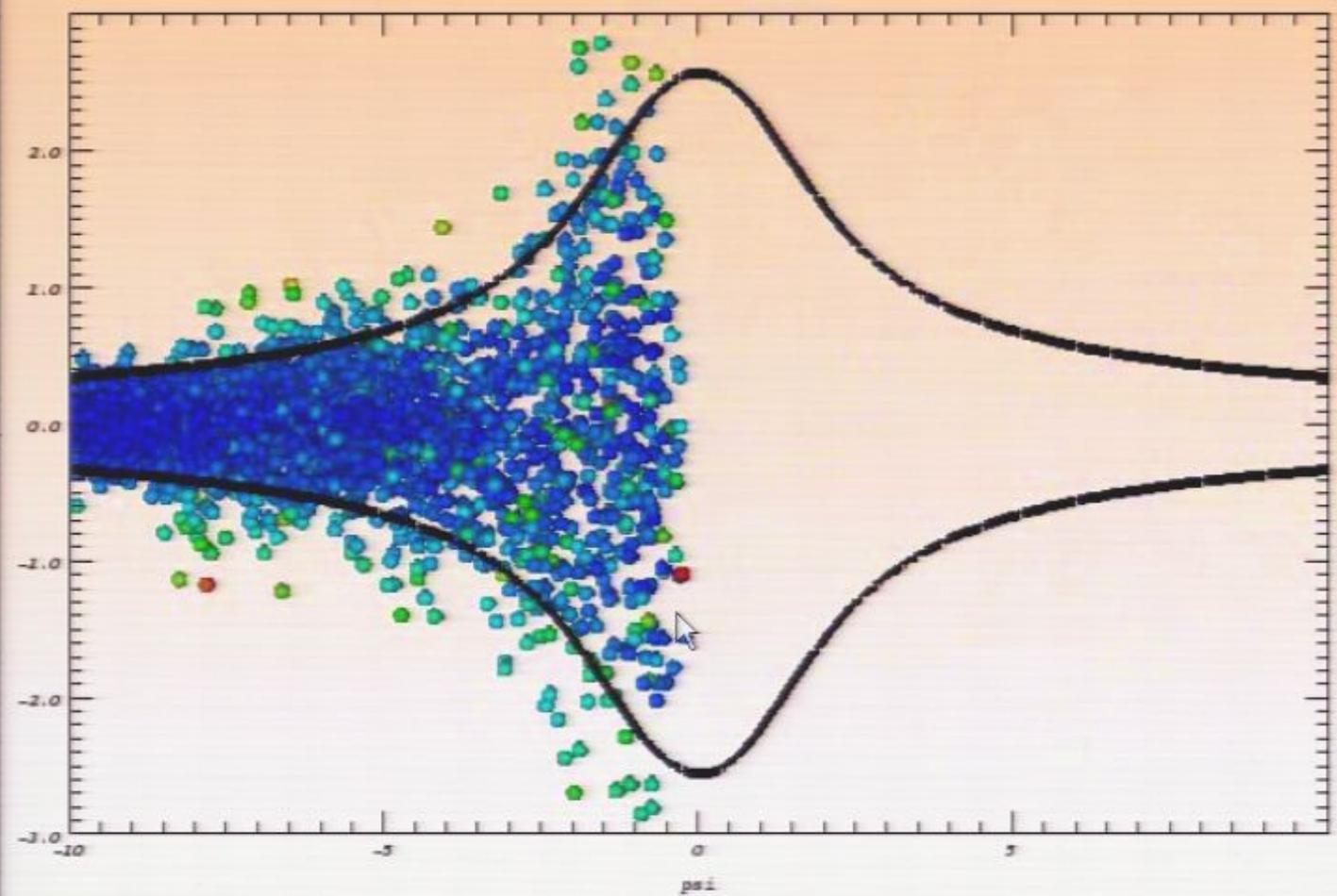


time=41.12

Playing

00:26

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music Center

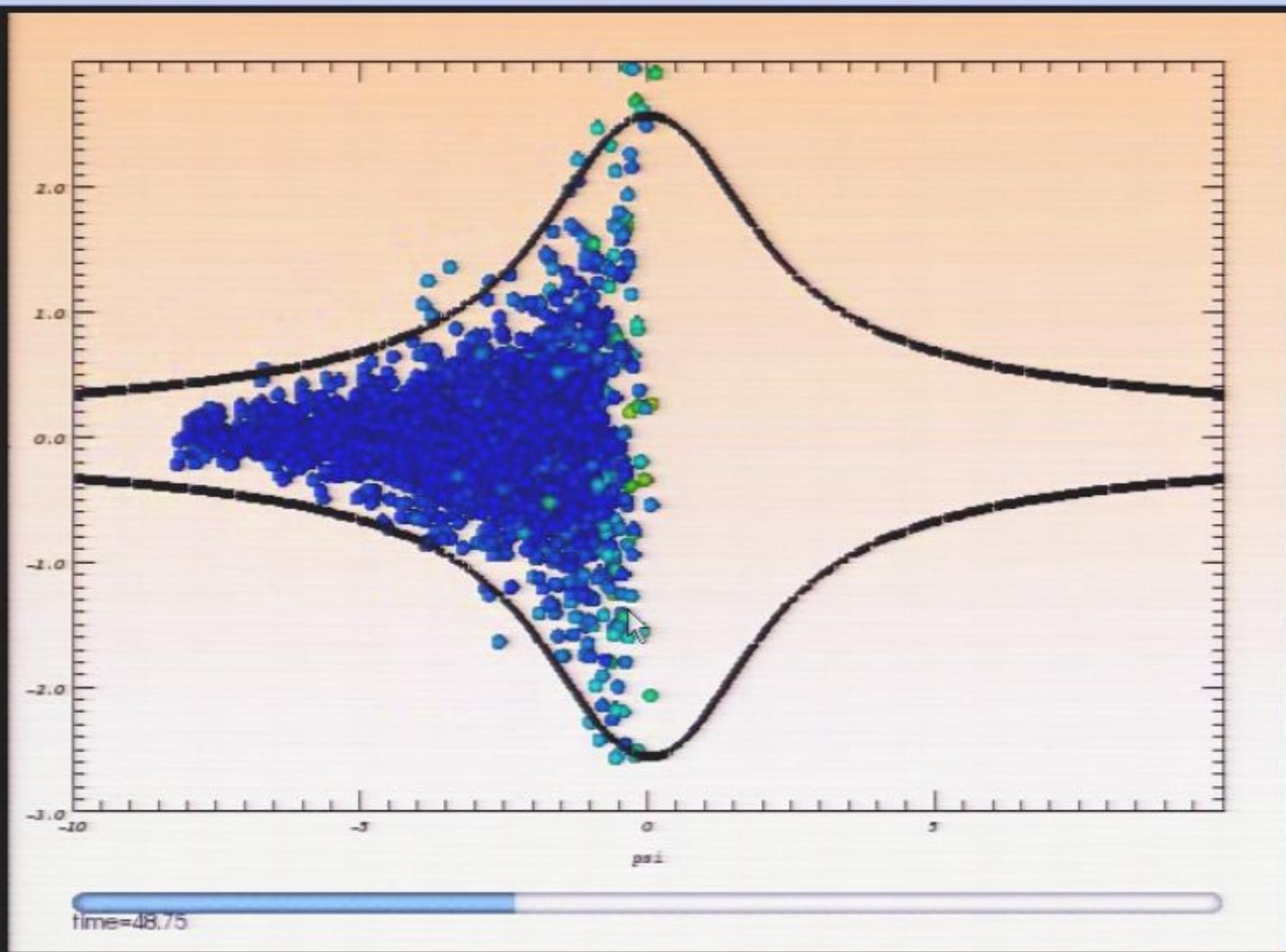


time=44.56

Playing

00:28

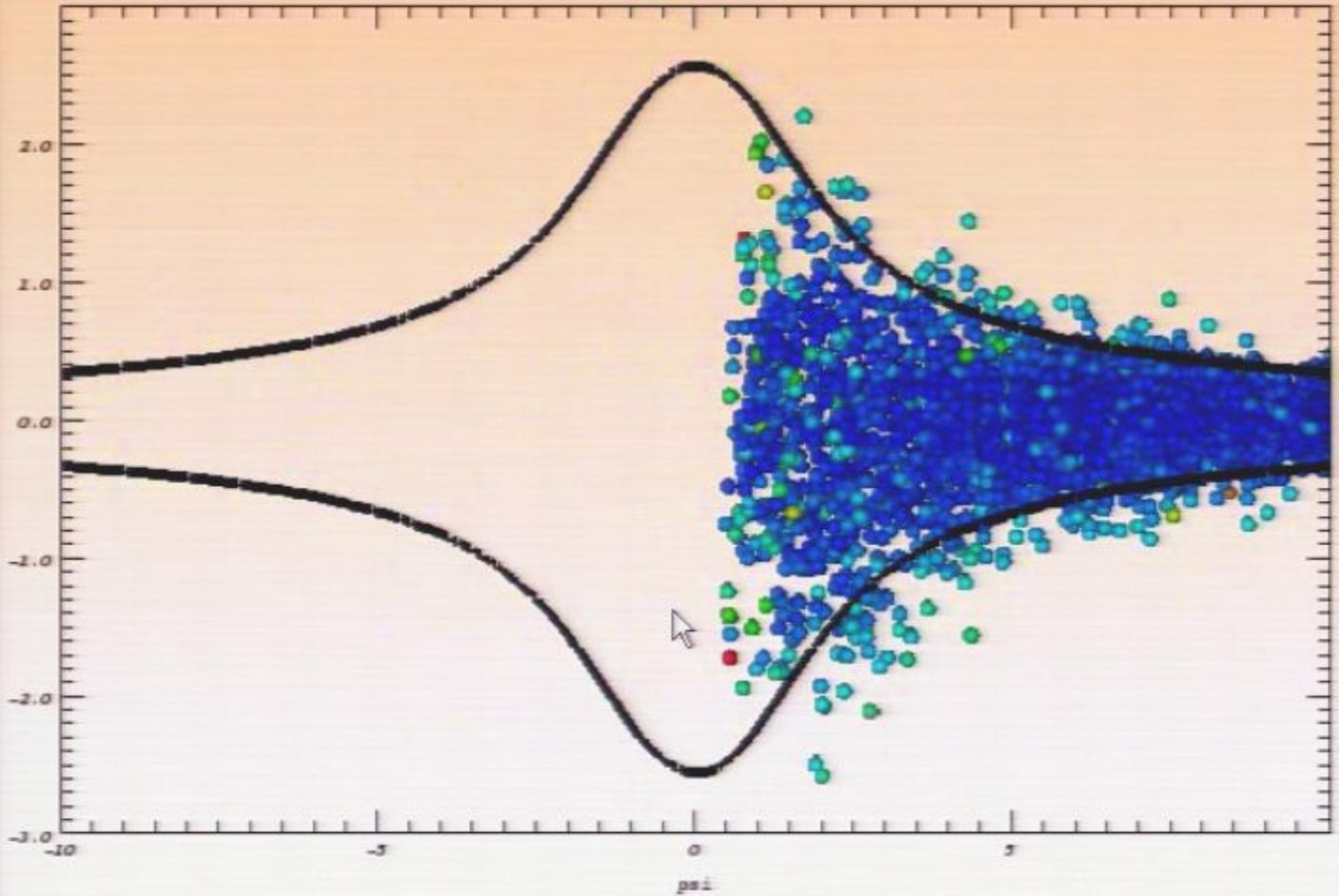
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Online
- Booster



Playing

00:31

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- On
- Hooser

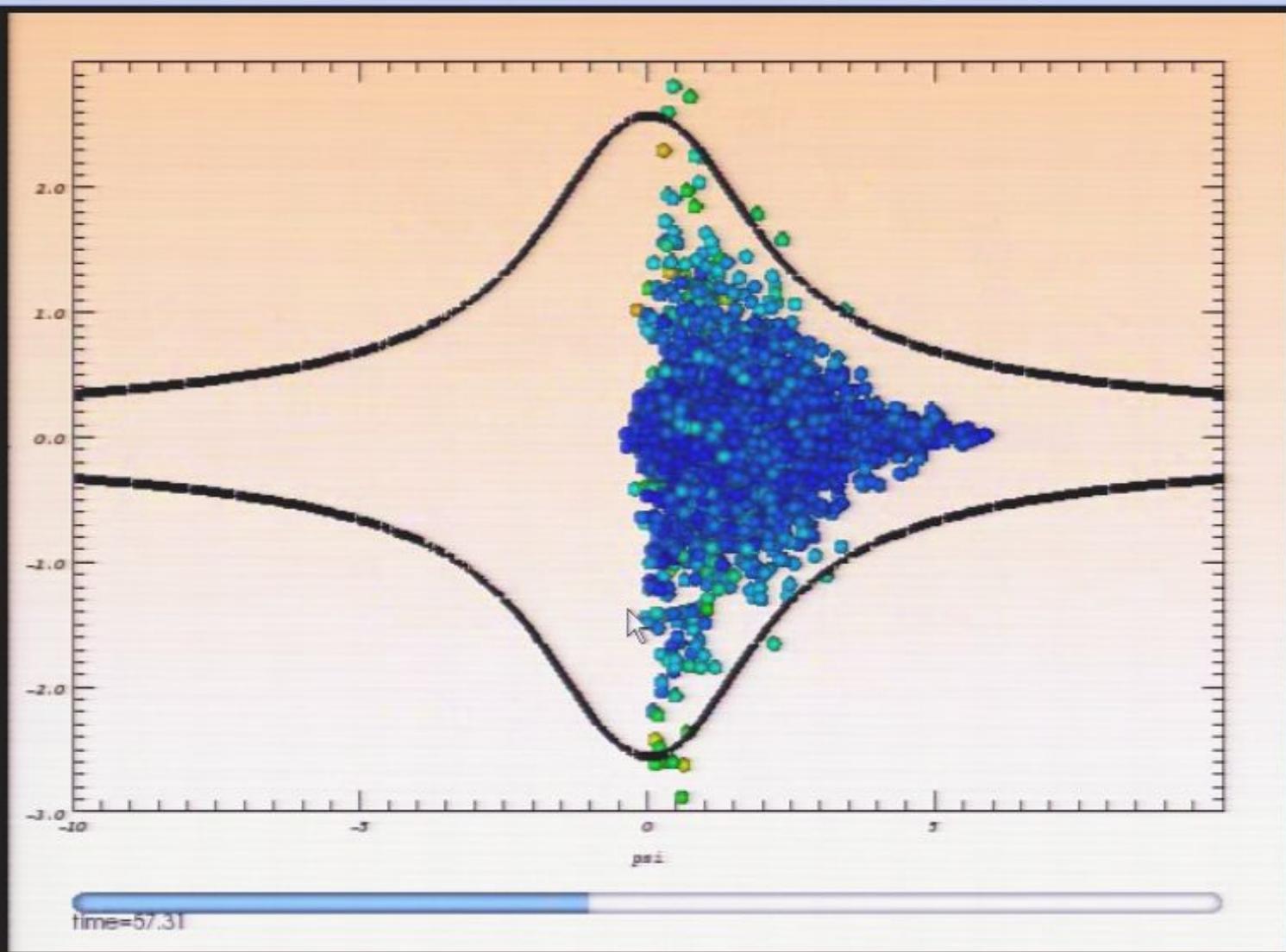


time=53.38

Playlist: Playlist1

00:33

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Music browser

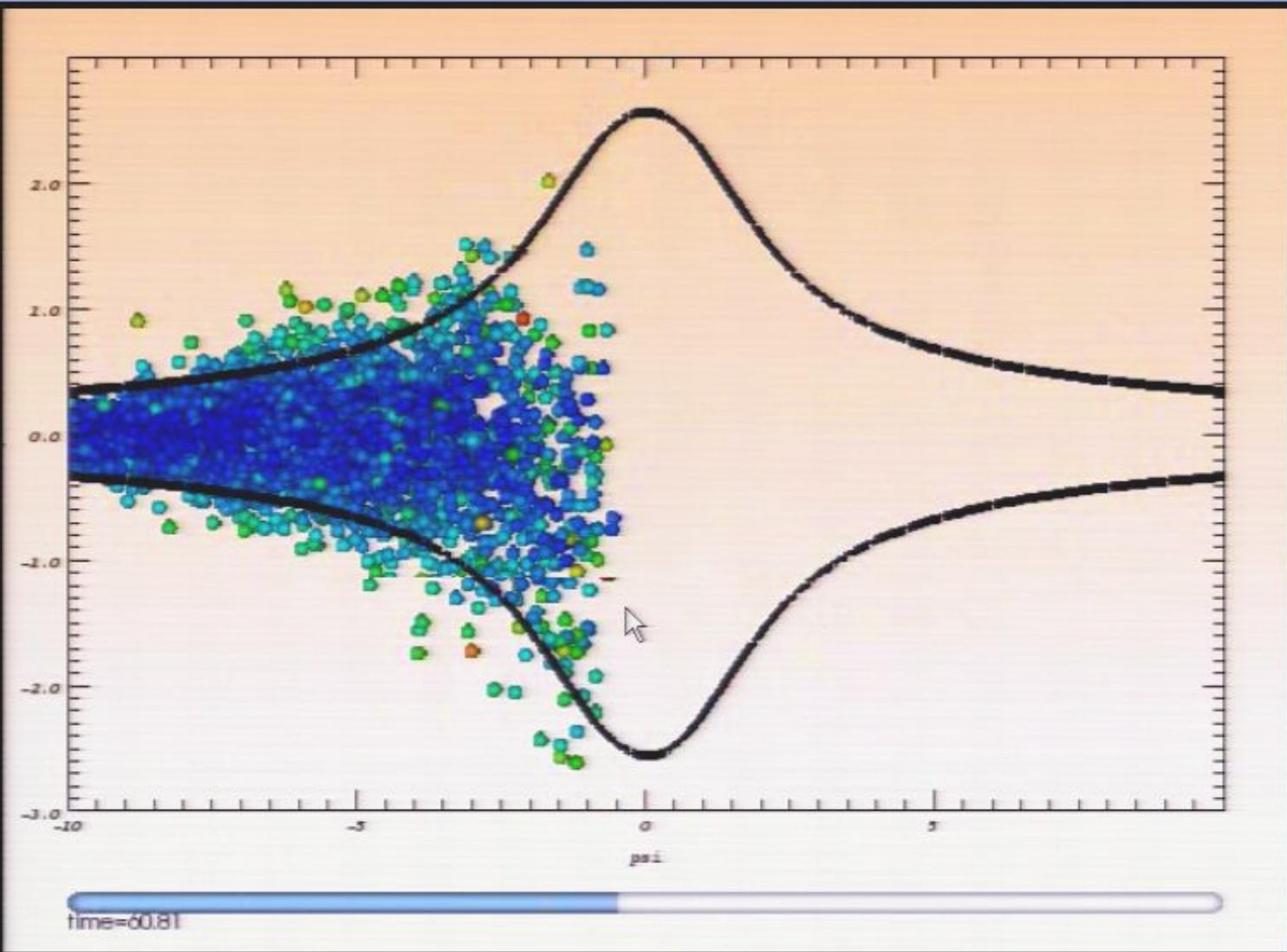


time=57.31

Clip: billiard-peak

00:36

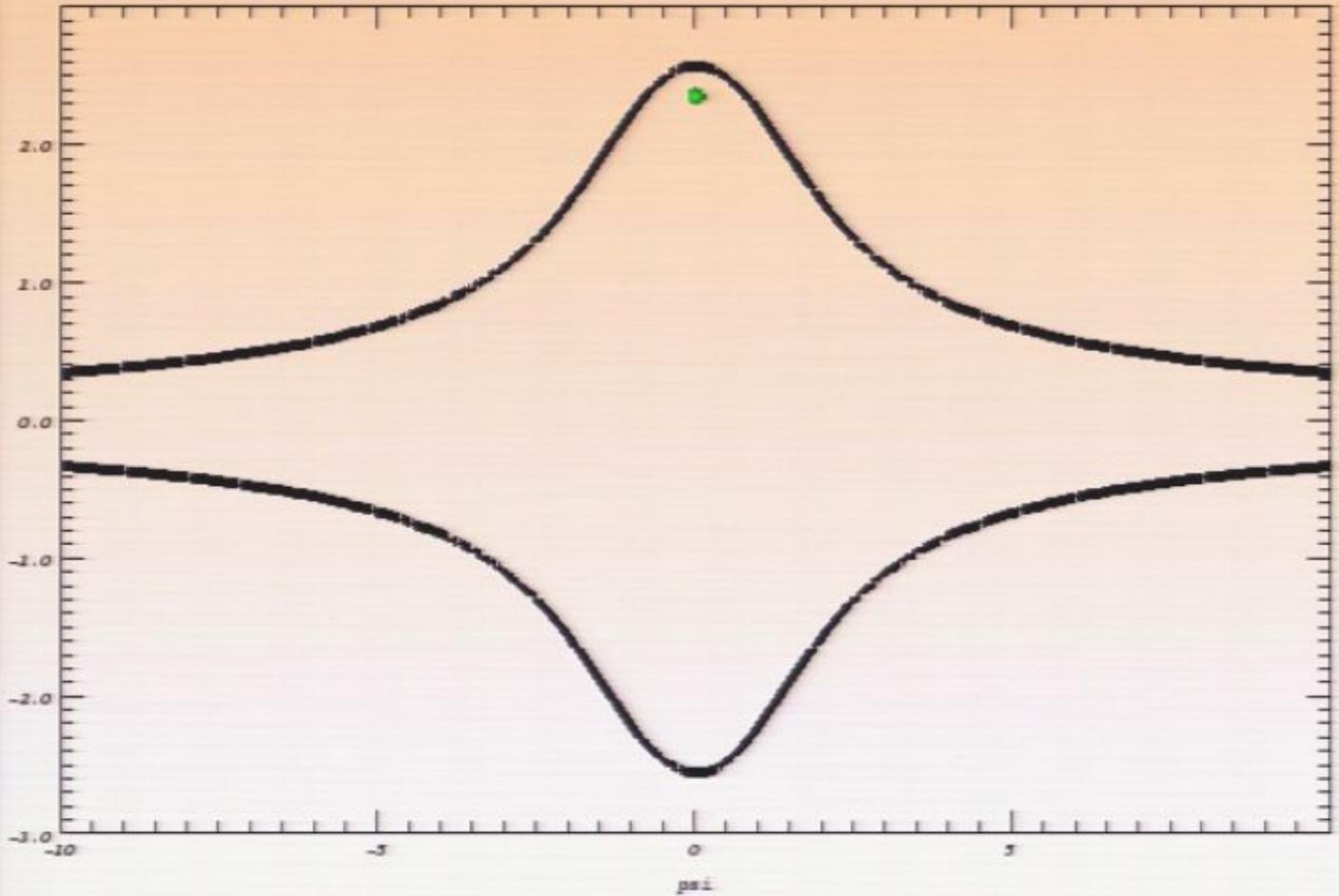
- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- On
- Hooser



Clip: billiard-peak

00:39

- Now playing
- Media guide
- Copy from
- Media library
- Radio tuner
- Copy to CD Device
- Premium services
- Audio booster

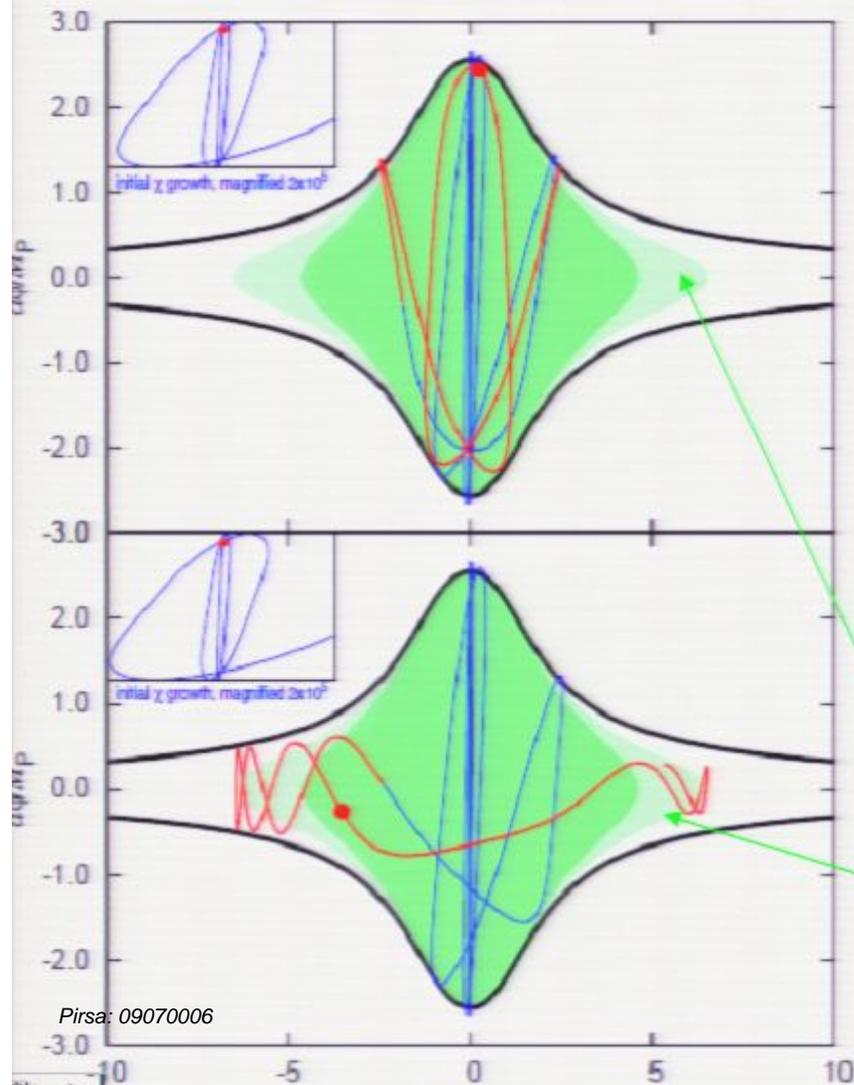


time=0.00

Stopped

Instability of the $k=0$ mode, billiards picture

two classes of trajectories:

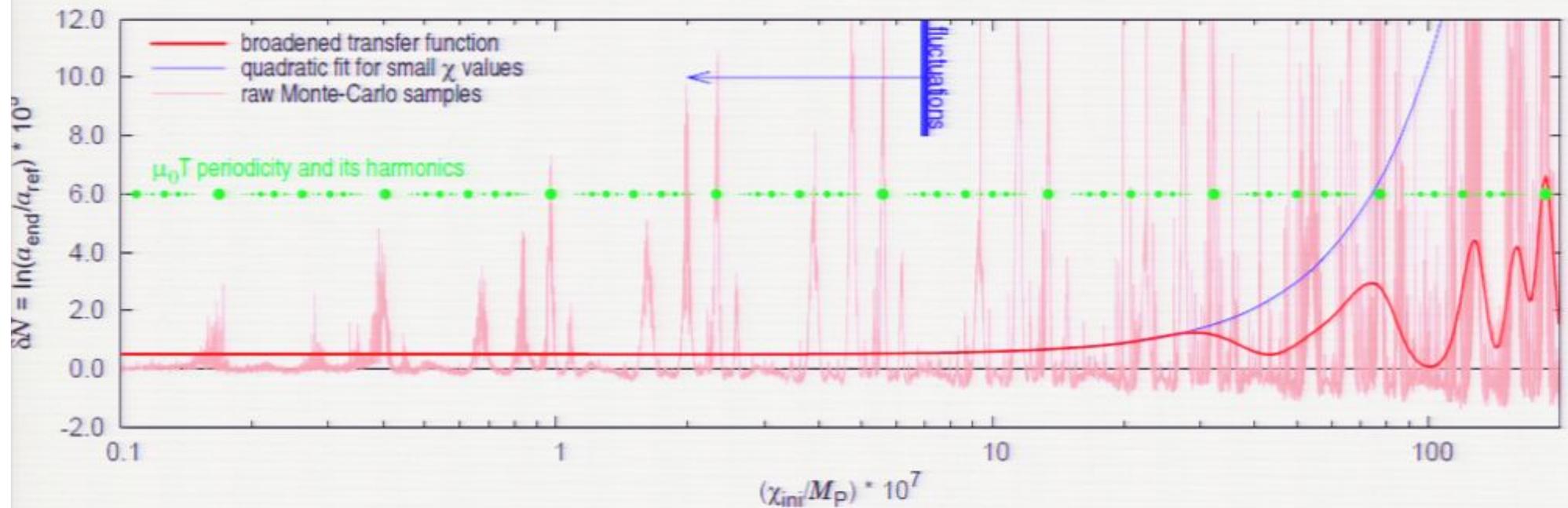


not entering the arms

entering the arms

arms close up during non-linear regime

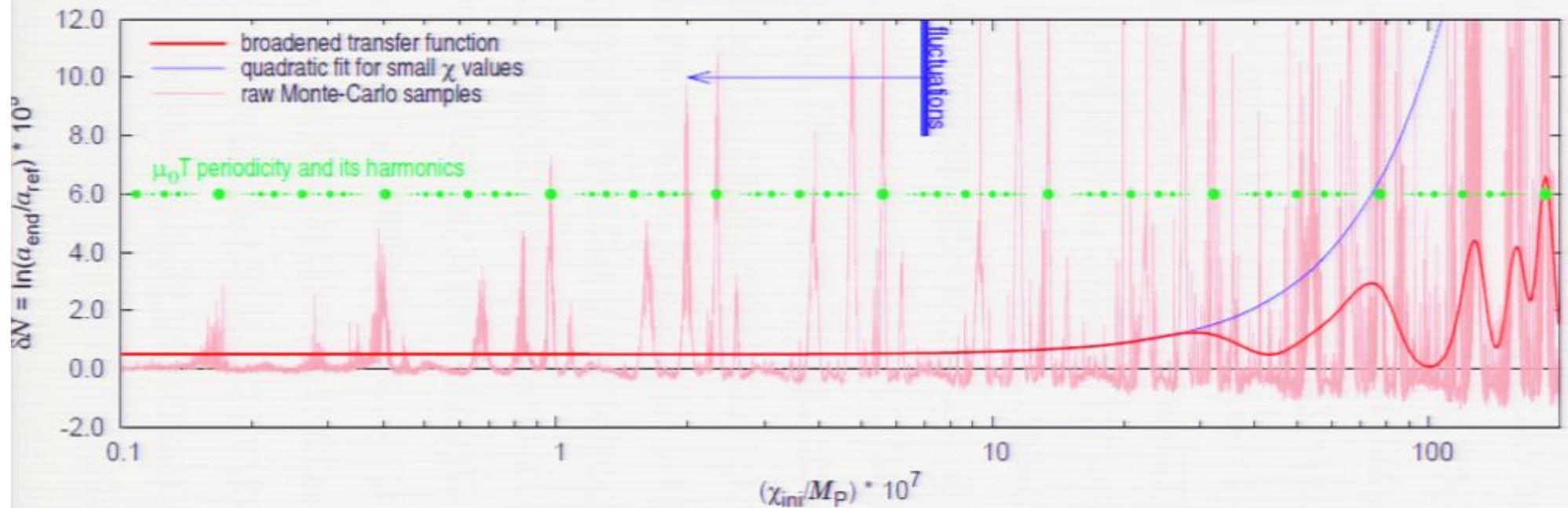
$$V(x, y) = \frac{1}{2}g^2\phi^2\chi^2 + \sigma(\phi^2 + \chi^2)$$



spikes correspond to the trajectories that entering the arms;

equal-distance in $\ln \chi$ is explained by theory: $\Delta \ln \chi_i = \mu_K T$

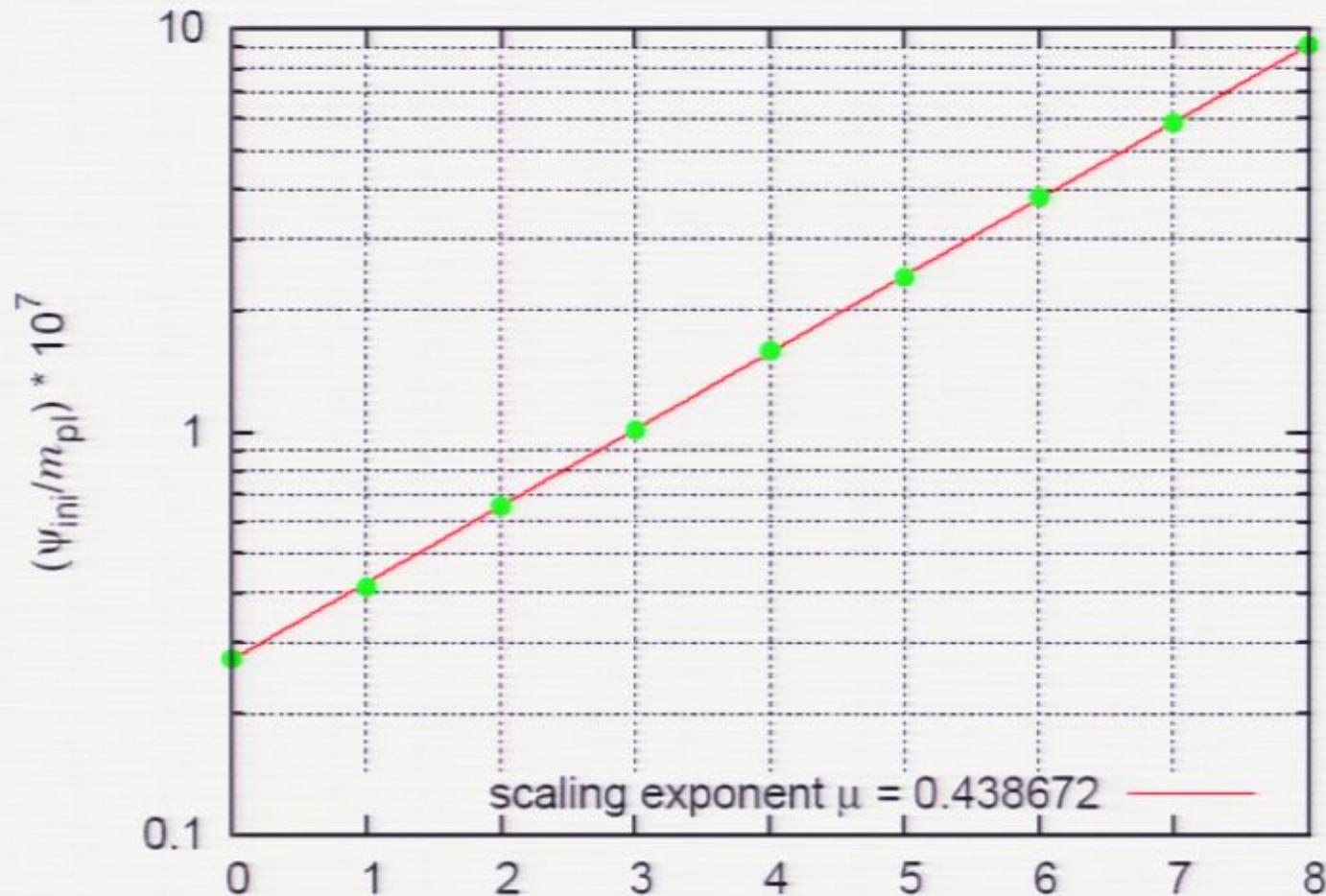
Non-Gaussian Spiked Patterns



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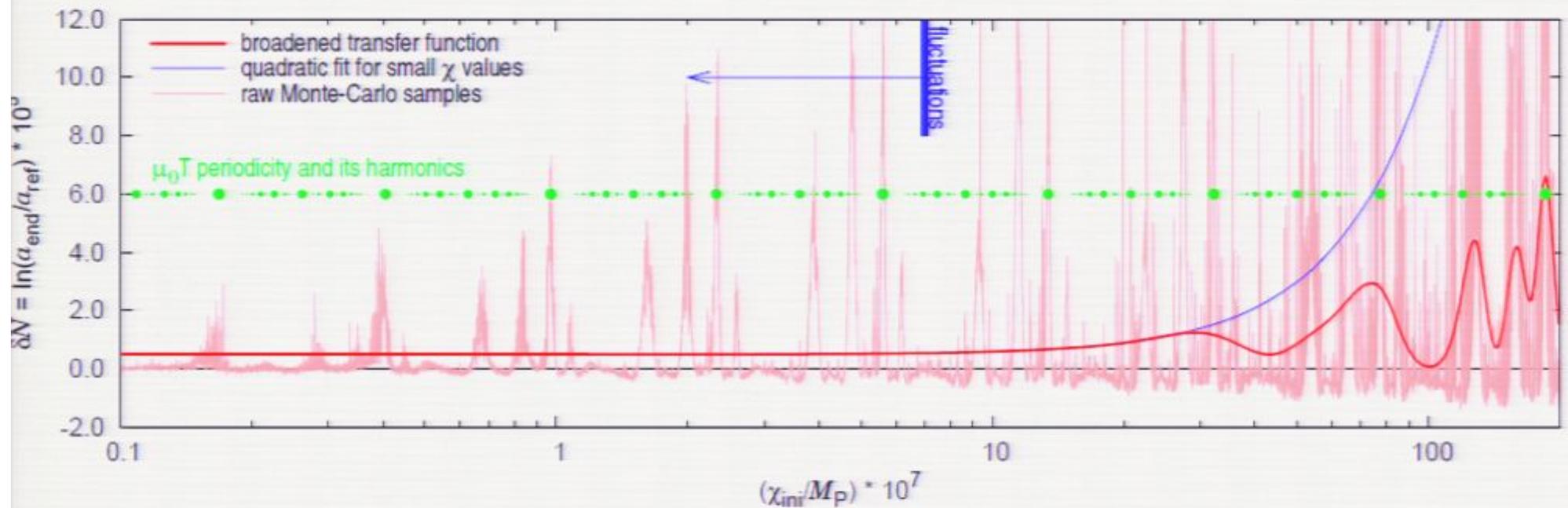
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$$\Phi(\vec{x}) = \Phi_G(\vec{x}) + f_{\text{NL}}\Phi_G^2(\vec{x})$$

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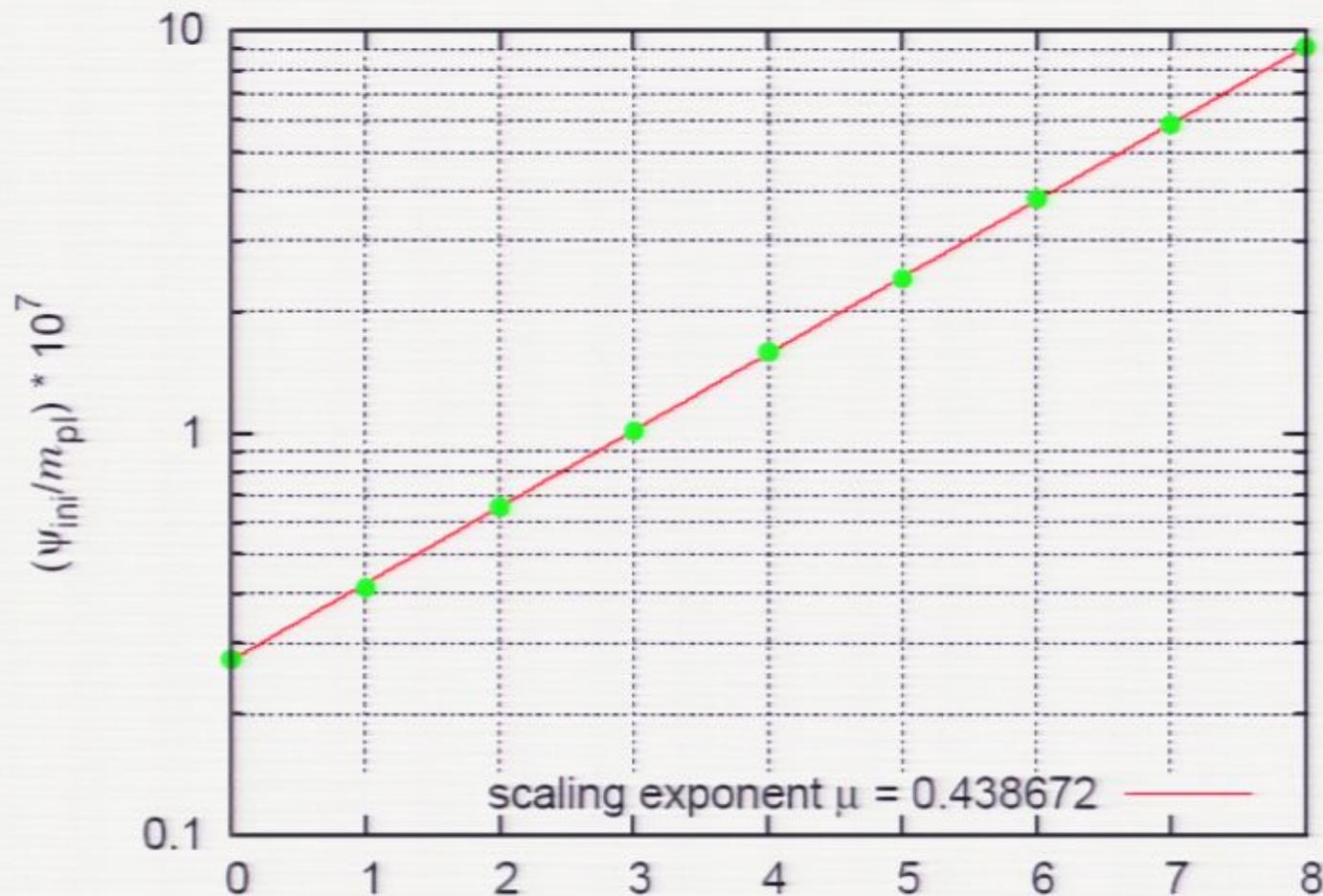
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Non-Gaussian Cold Spots

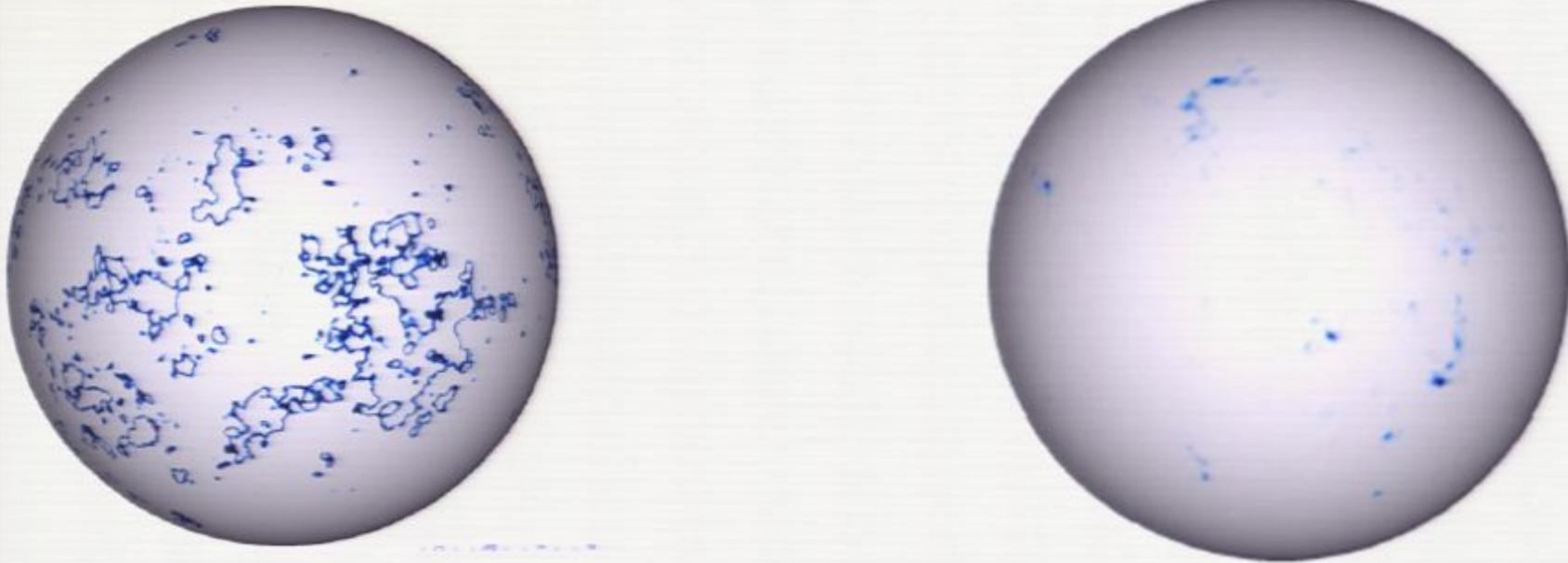
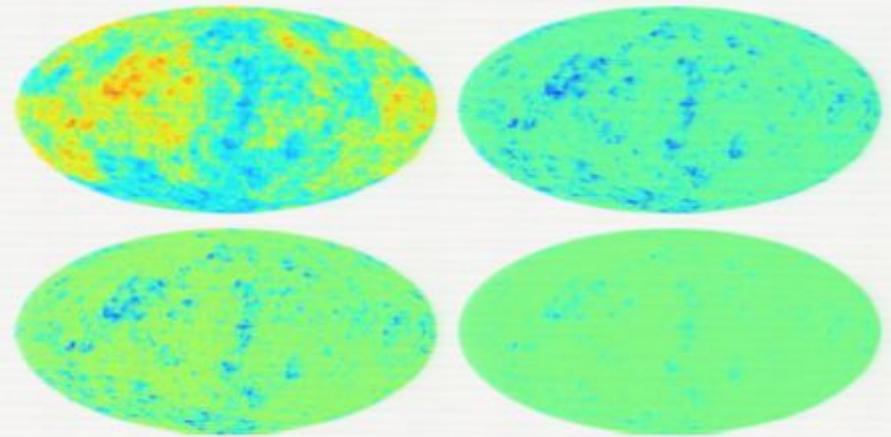


FIG. 3: What is plotted: $F(g)$ applied to scale-invariant GRF realization $\chi(x)$ with $1/f$ spectrum, with $F(g) = \exp(-(g - t)^2/(2w^2))$ threshold set to $t = 5RMS(\chi)$, and peak width $w = 1RMS(\chi)$.

Implication: cold spot

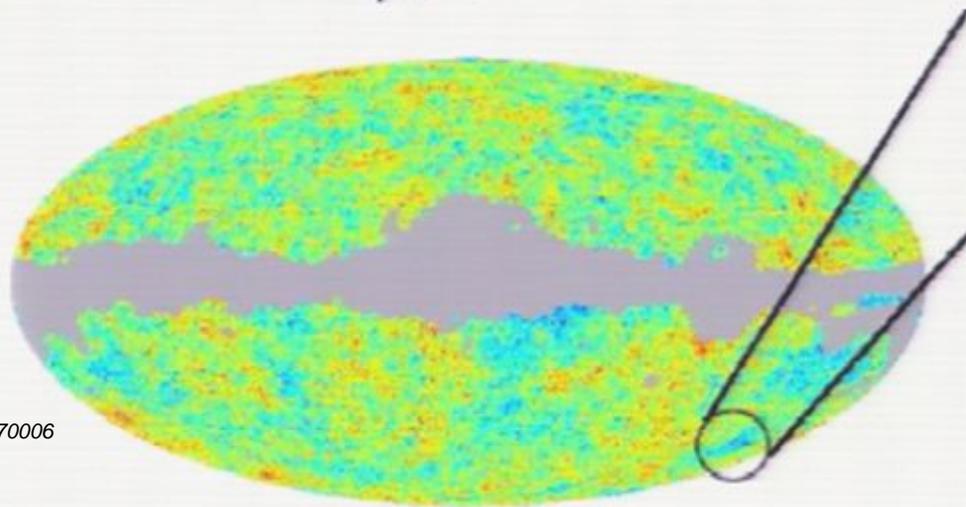
Positive δN

- positive curvature perturbation \mathcal{R}
- negative Newtonian potential
- negative $\delta T/T$ (ignoring ISW)
- cold spot

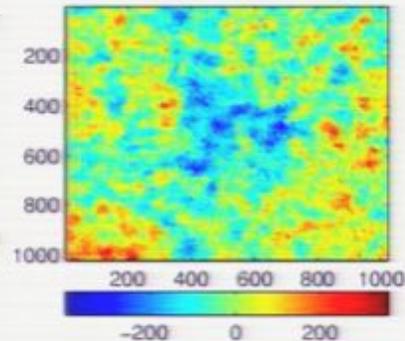


THE NON-GAUSSIAN COLD SPOT IN THE 3-YEAR WMAP DATA

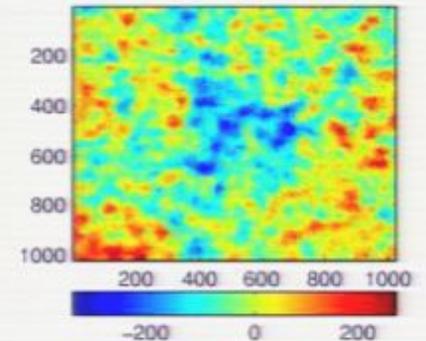
M. CRUZ¹
IFCA, CSIC-Univ. de Cantabria, Avda. los Castros, s/n,
E-39005-Santander,
Spain



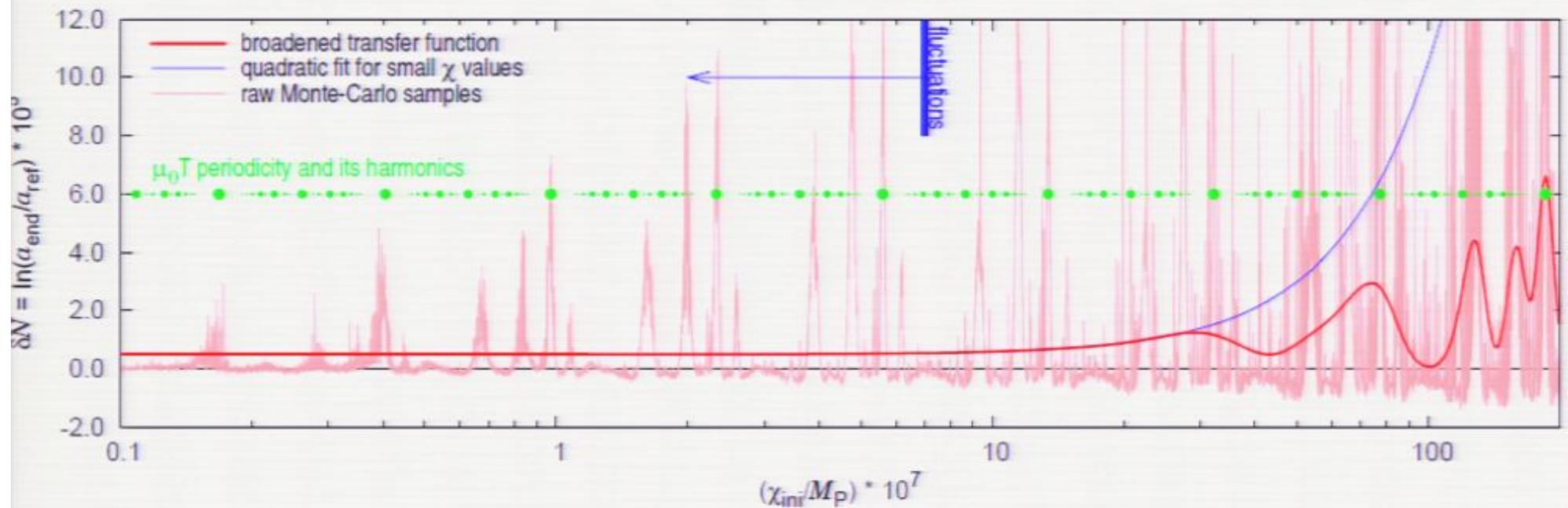
WCM 1- year, real space



WCM 3- year, real space



Non-Gaussian Spiked Patterns



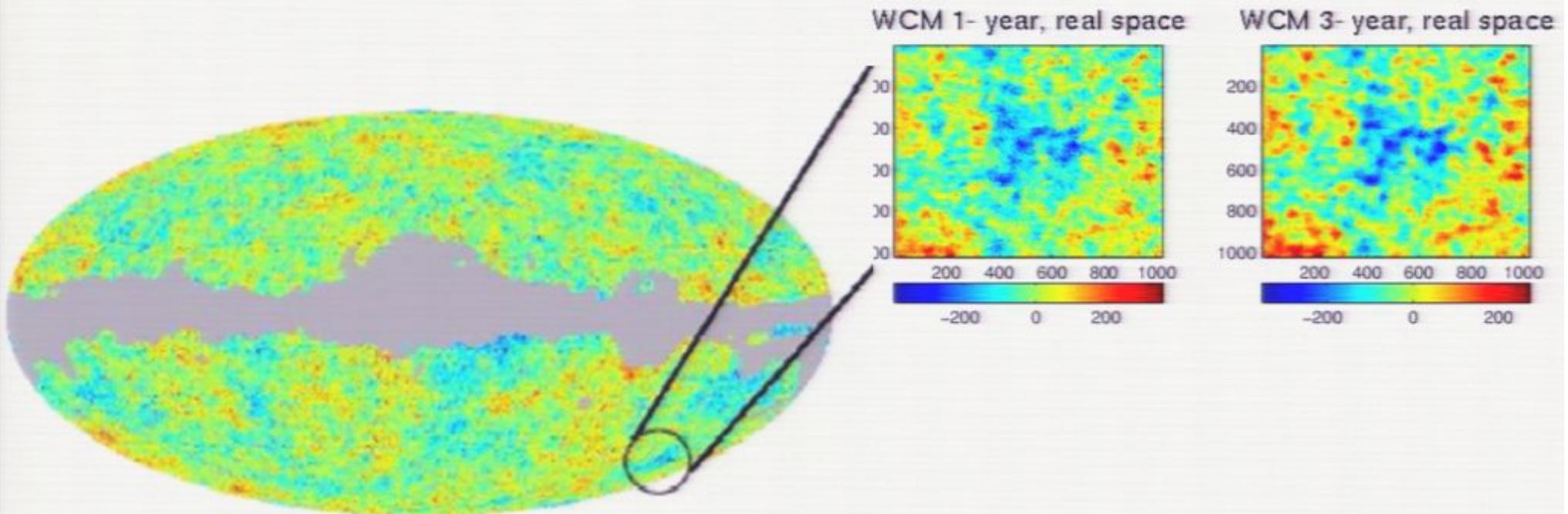
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M. CRUZ¹

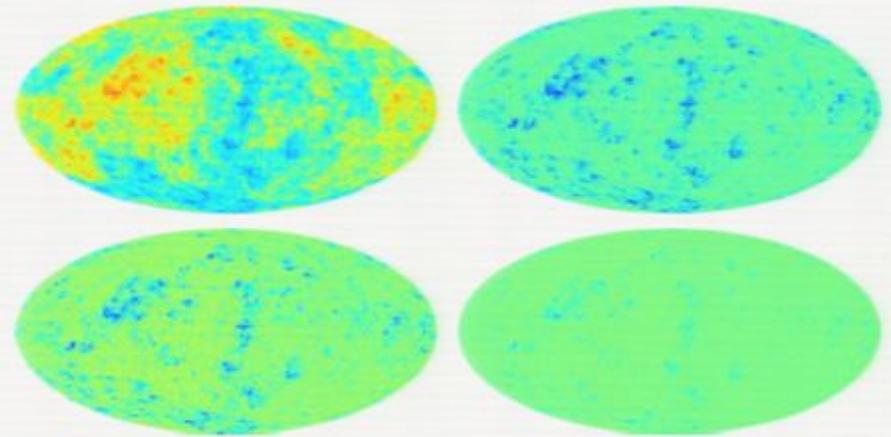
IFCA, CSIC-Univ. de Cantabria, Avda. los Castros, s/n,
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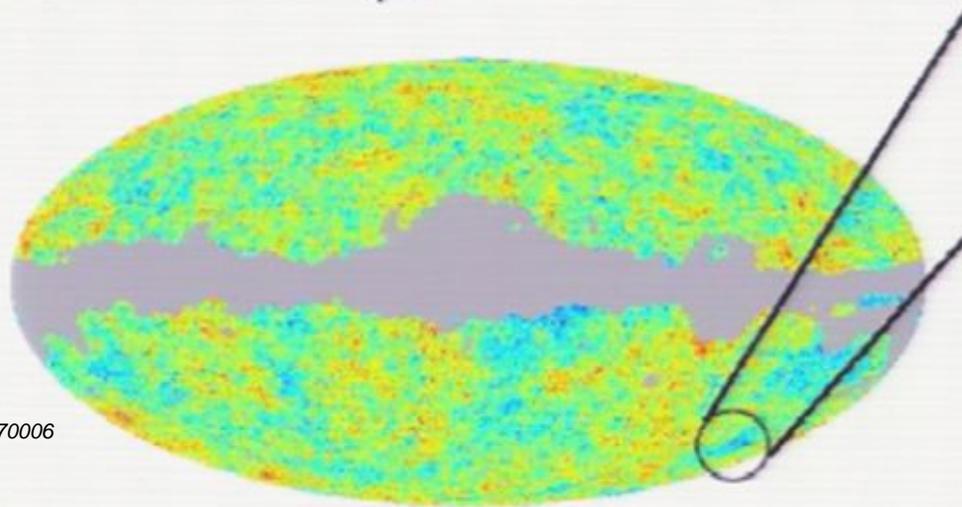
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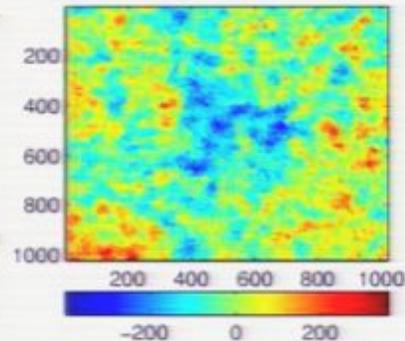


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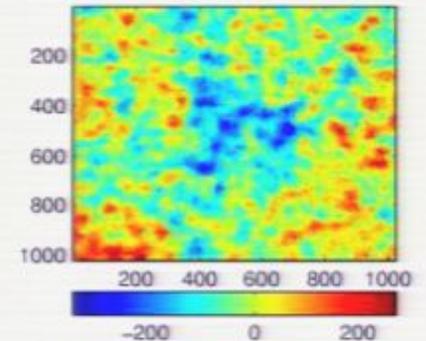
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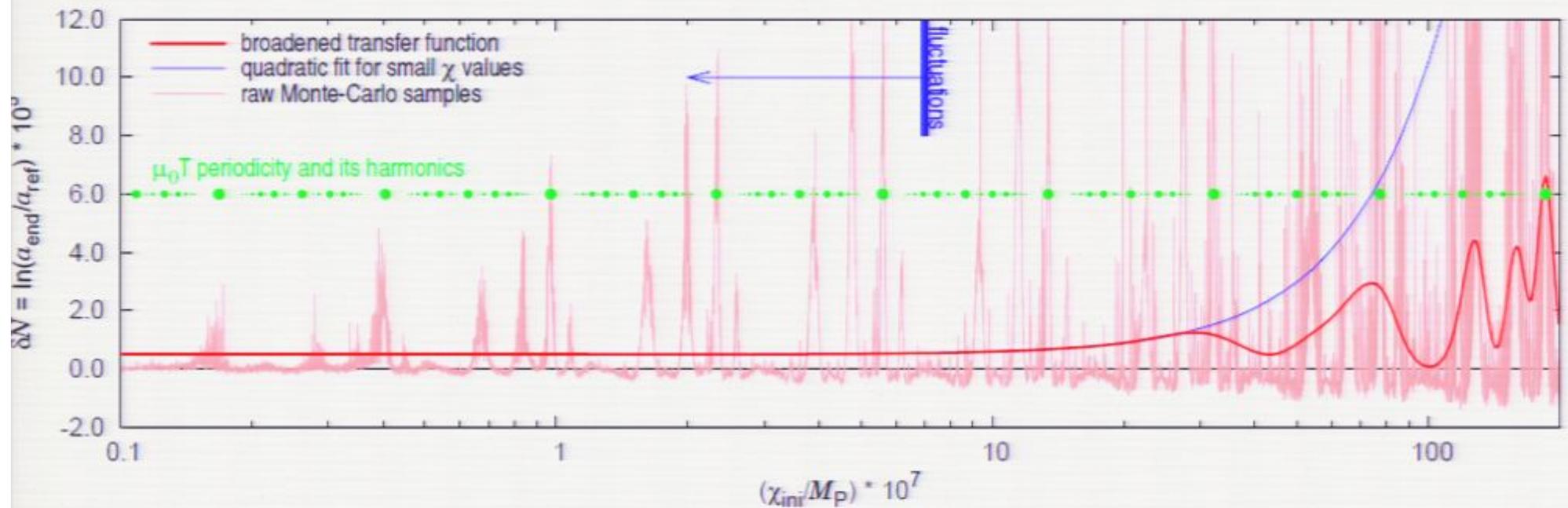
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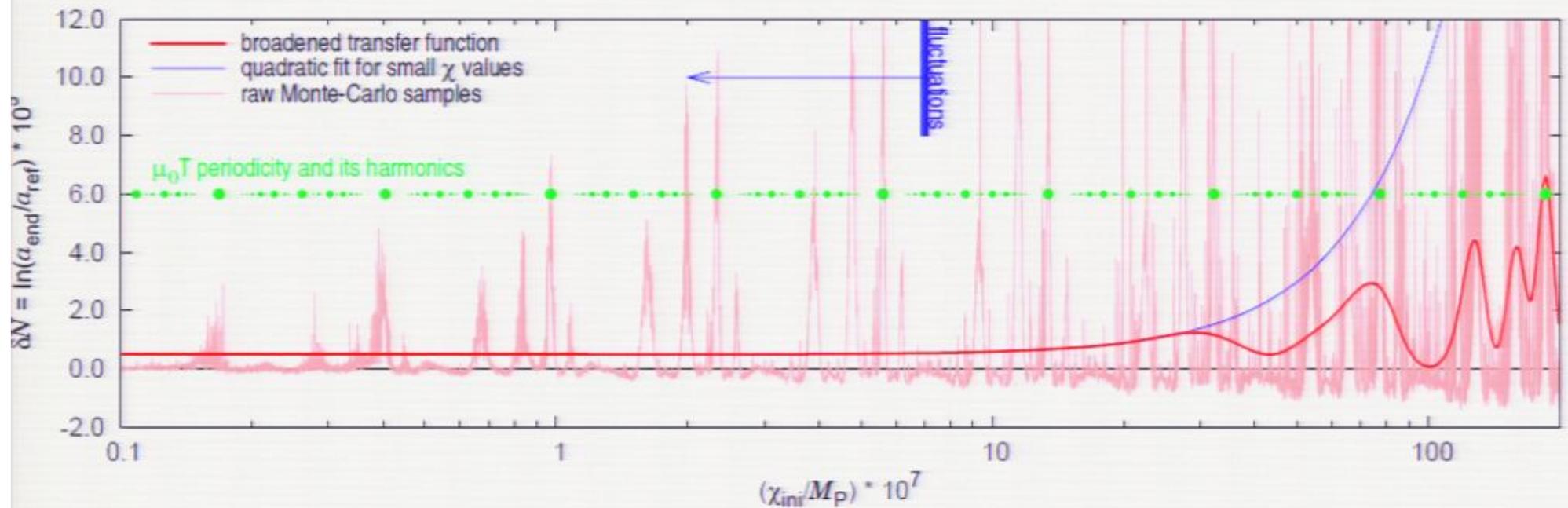
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