Title: Phenomenological Cosmology and the Accelerating Universe

Date: Jun 29, 2009 02:00 PM

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Abstract:

This talk is divided into three parts:

1.) Phenomenological cosmology using a model-independent approach

- illustrated using supernovae and radio galaxies

2). The physics of powerful radio galaxies and the supermassive black holes that power these sources

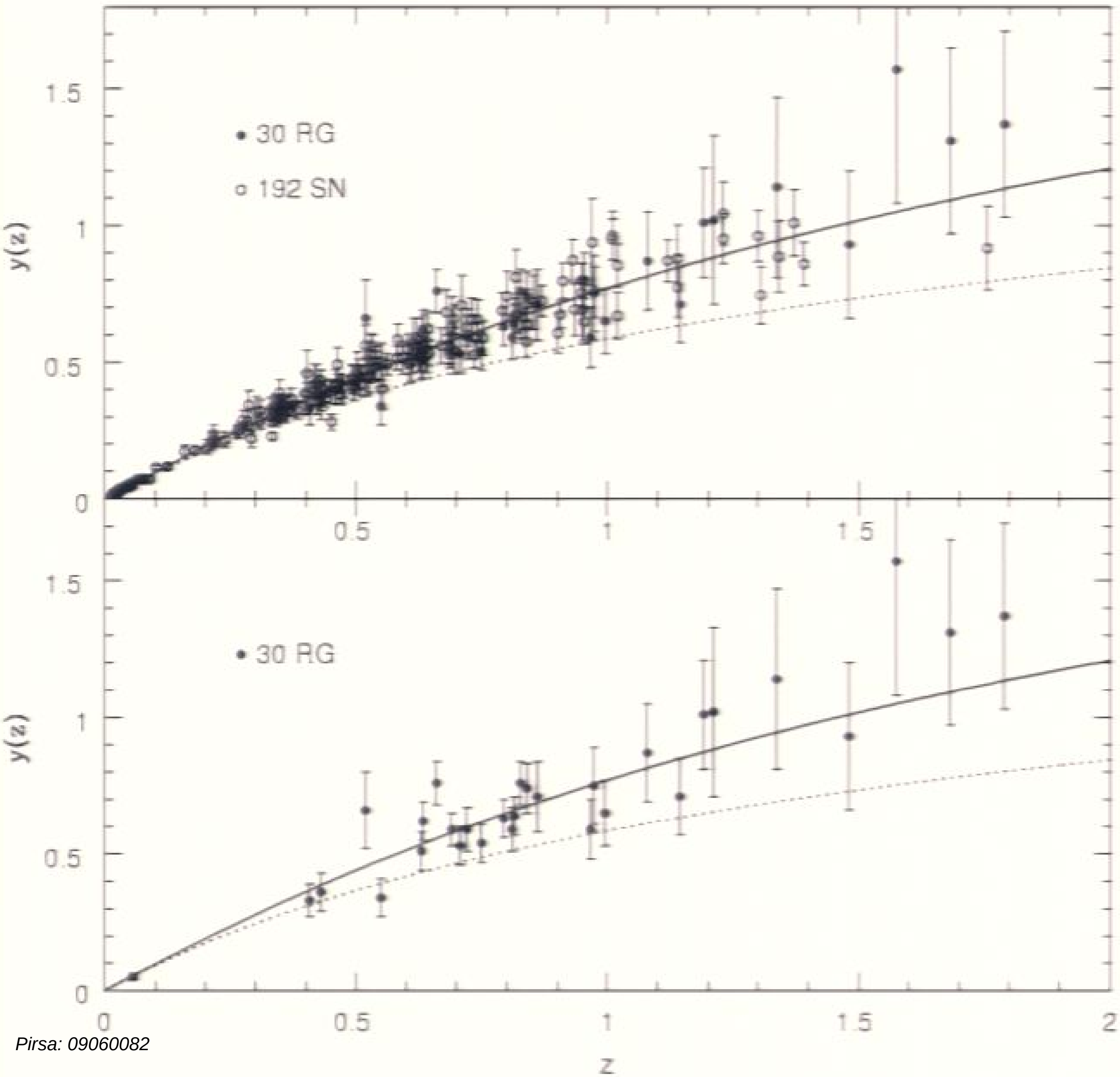
3). The spins of supermassive black holes

The acceleration history of the universe can be studied through measurements of coordinate distances (luminosity distances, or angular size distances) such as those that can be obtained using Type Ia Supernovae & FRIIb Radio Galaxies

RG and SN methods are completely independent & complementary methods.

How are these data used to study cosmology?

Coordinate Distances to RG & SN



Daly et al. (2008) studied 192 SN of Davis et al. (2007), 182 SN of Riess et al. (2006), 115 SN of Astier et al. (2006), and 30 RG of Daly et al. (2009). The solid curve is the LCDM prediction, and the dotted curve is the flat matter-dominated prediction. High z RG have been on plot since 1998.

For k=0: $y = H_0(a_o r) = H_0 \int dt/a(t) = H_0 \int(\acute{a}/a)^{-1}\, dz$

Common Approach: Assume FRW, theory of gravity (GR), select a specific DE model, assume 2 components (DE & NRM), and solve for best fit model parameters.

Einstein Equation (<u>for k=0</u>):

$(\acute{a}/a)^2=(8\pi G/3)\sum\rho_i = H_o{}^2[\Omega_{om}(1+z)^3 + f_E(z,w)]$

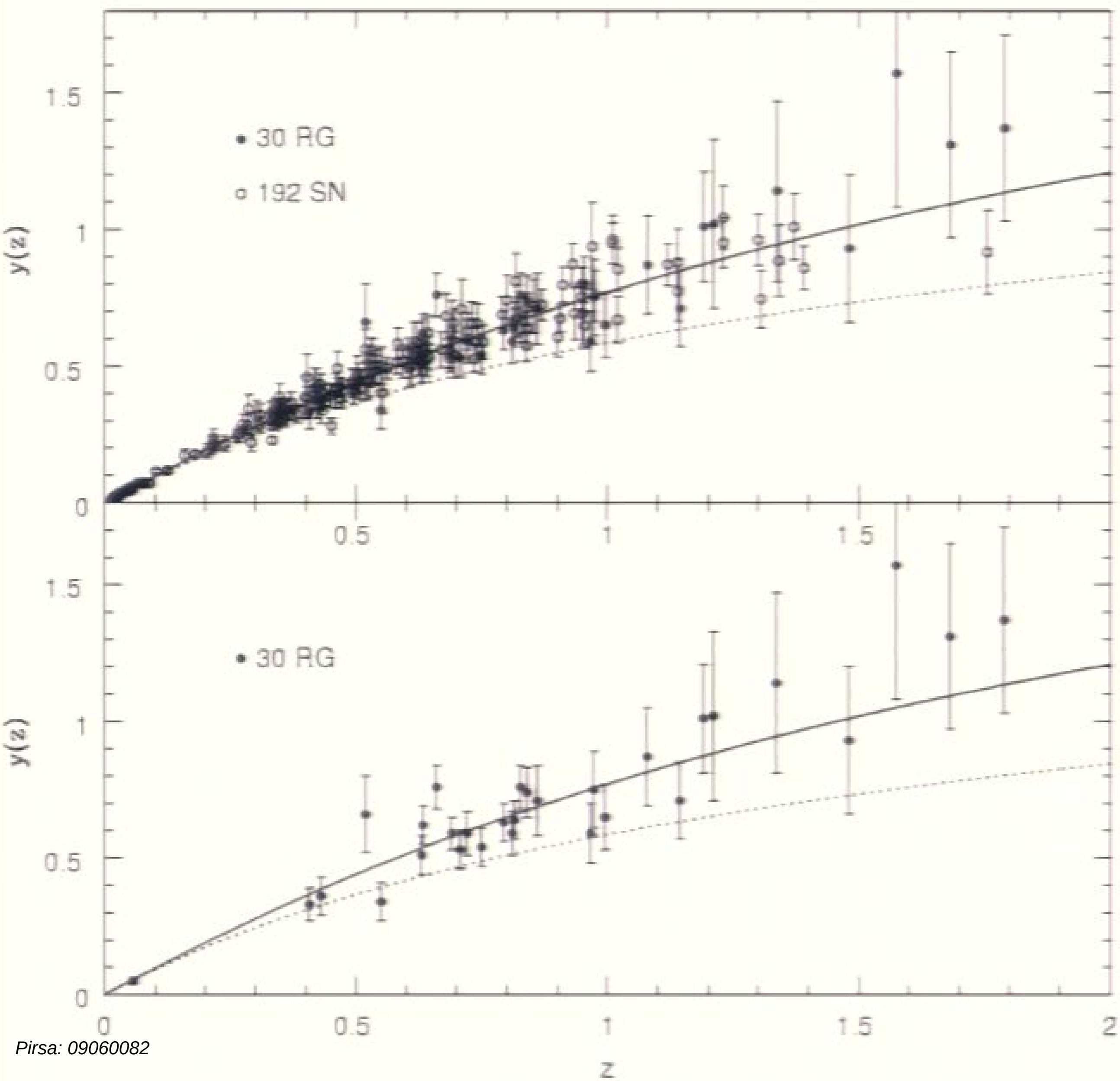
$\rho_E(z)=\rho_{oc} f_E(z,w)$; $w=P_E/\rho_E$; $f_E(0,w) = (1-\Omega_{om})$

For a quintessence model, <u>w=constant</u>, and

$f_E\,(z,w) = (1- \Omega_{om})(1+z)^{3(1+w)}$ or

$(\acute{a}/a)^2 = H_o{}^2[\Omega_{om}(1+z)^3 + (1- \Omega_{om})(1+z)^{3(1+w)}]$

Coordinate Distances to RG & SN



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The coordinate distance, $(a_o r)$; luminosity distance $d_L = (a_o r)(1+z)$; angular size distance $d_A = (a_o r)\ (1+z)^{-1}$ all carry the same cosmological information.

It is convenient to work with $y(z)=H_0\,(a_o r)$, the dimensionless coordinate distance

SN: $5 \log [y(z)(1+z)] - m_{Beff}[\alpha] = -\mathcal{M}'_B = \text{const.}$

RG: $R^* = k_o y^{(6\beta-1)/7} (k_1 y^{-4/7} + k_2)^{\beta/3-1} = \kappa = \text{const.}$ (Daly 94)
where k_o, k_1, and k_2 are observed quantities.
Based on one empirically determined relationship (now understand the physical basis for relationship)

Study 30 RG from LMS89, LPR92, GDW00, & Kharb et al. '08 → Obtain y(z) to each source (Daly et al. 2008)
[have VLA data for another 13 sources]

For $k=0$: $y = H_0(a_o r) = H_0 \int dt/a(t) = H_0 \int (\acute{a}/a)^{-1}\, dz$

Common Approach: Assume FRW, theory of gravity (GR), select a specific DE model, assume 2 components (DE & NRM), and solve for best fit model parameters.

Einstein Equation (for $k=0$):

$(\acute{a}/a)^2 = (8\pi G/3)\sum \rho_i = H_o^2[\Omega_{om}(1+z)^3 + f_E(z,w)]$

$\rho_E(z) = \rho_{oc} f_E(z,w)$; $w = P_E/\rho_E$; $f_E(0,w) = (1-\Omega_{om})$

For a quintessence model, $w=\text{constant}$, and

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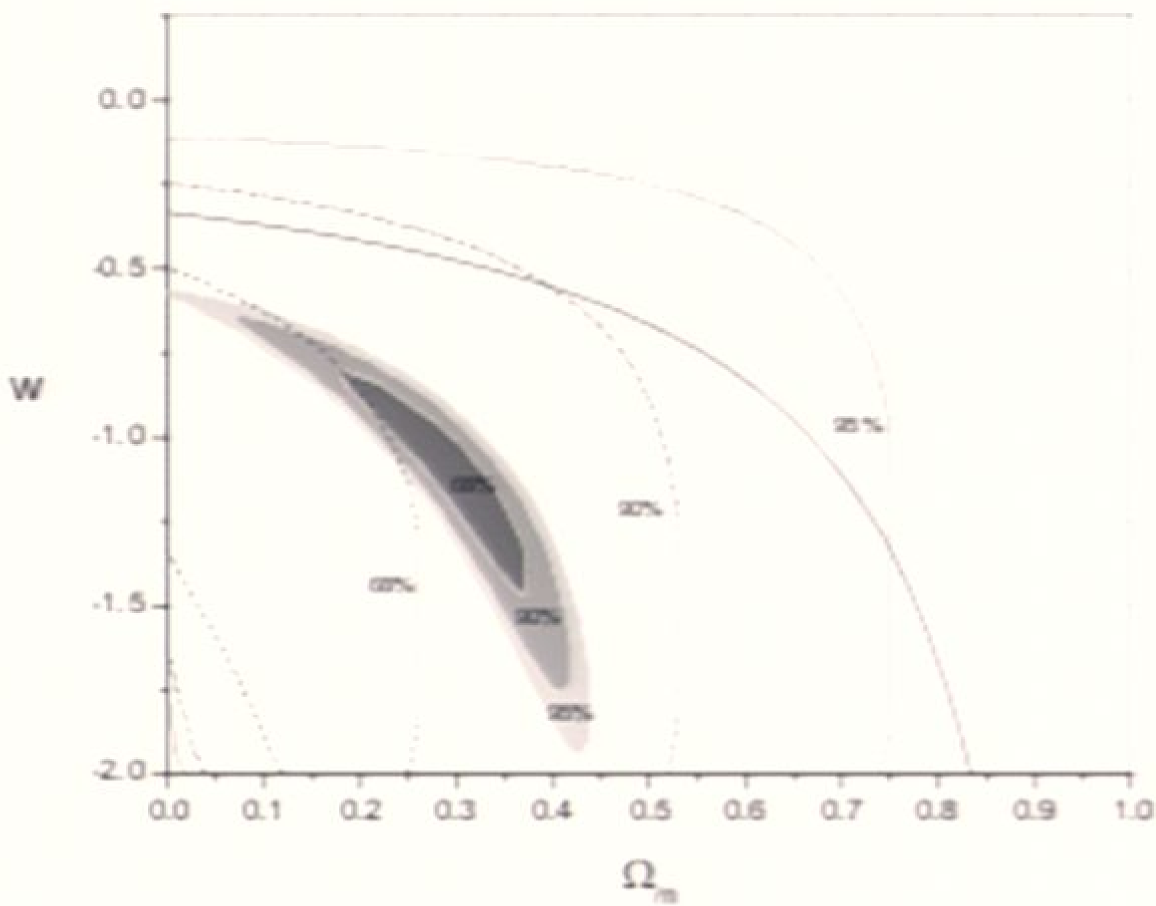
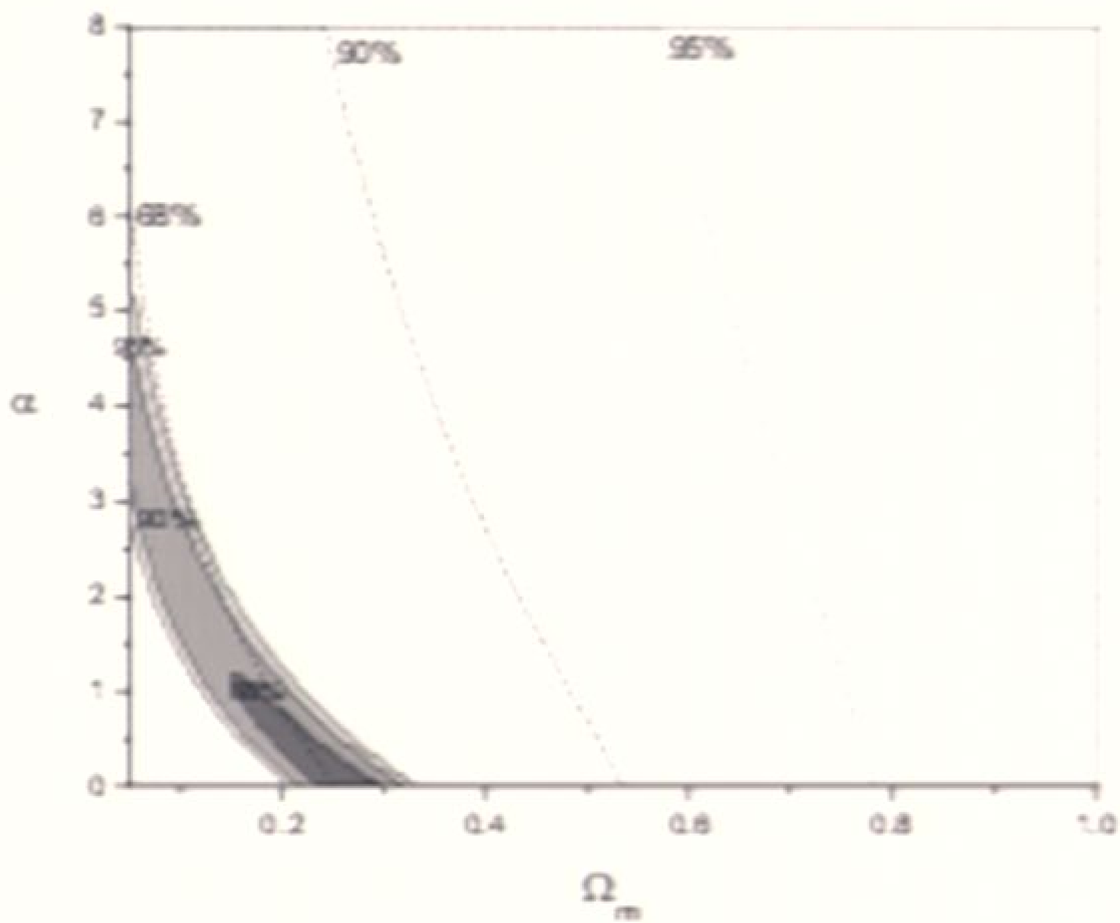
Constraints obtained in a Quintessence Model



From Daly et al. (2009) for a combined sample of 192 SN + 30 RG

Constraints obtained in a Rolling Scalar Field Model, with $V \sim \varphi^{-\alpha}$



Best fit value of α is zero.

(from Daly et al. 2009)

$$\int a_o\, dr/\sqrt{(1-kr^2)} = \int dt/a(t) = \int (\dot{a}/a)^{-1}\, dz$$

Common Approach: Assume FRW, theory of gravity (GR), select a model for the DE, consider a universe with space curvature, & obtain the best fit model parameter values.

e.g. Einstein Equations for a Λ model:

$$(\dot{a}/a)^2=(8\pi G/3)\sum\rho_i - k/a^2$$

$$(\dot{a}/a)^2=H_o^2[\Omega_{om}(1+z)^3 + \Omega_\Lambda + \Omega_k\,(1+z)^2]$$

where $\Omega_{om}+\Omega_\Lambda+\Omega_k=1$ and $\Omega_k=-k/(H_o a_o)^2$

Type Ia Supernovae (in particular models)

→ An Accelerating Universe

Radio Galaxies (in particular models)

→ An Accelerating Universe

The models assume a theory of gravity (GR), specify the properties and redshift evolution of the Dark Energy, assume something about space curvature, and consider a universe with two components, non-relativistic matter and dark energy.

Is there a model-independent way to determine if the universe is accelerating?

Model-Independent Approach: Use y(z) obtained directly from the data; differentiate y(z) to obtain $E(z) = (\dot{a}/a)/H_o$ and $q(z) = - \ddot{a}a/(\dot{a})^2$

q(z) & H(z) [or E(z)] only depend upon the FRW metric!

(Daly 2002; Daly & Djorgovski 2003)

$$d\tau^2 = dt^2 - a^2(t)[dr^2/(1-kr^2) + r^2 d\theta^2 + r^2 \sin^2\theta \, d\varphi^2]$$

for a light ray from source, $dt = -a(t)(-dr)$ when $k=0$ so $dz/dt = -a_o^{-1}(1+z)(dr/dz)^{-1}$. Differentiating $(1+z) = a_o/a(t)$, $\acute{a} = -a_o(1+z)^{-2}(dz/dt) = (1+z)^{-1}(dr/dz)^{-1} \rightarrow$

$H(z) \equiv (\acute{a}/a) = (d(a_o r)/dz)^{-1} = H_o\,(dy/dz)^{-1}$.

$$E(z) \equiv H(z)/H_o = (dy/dz)^{-1}$$

More generally, $E(z) = (y')^{-1}(1+\Omega_k y^2)^{0.5}$ [Weinberg 1972]

Differentiating $\acute{a}$, $\rightarrow$

$\ddot{a} = -(1+z)^{-2}(dz/dt)\,(dr/dz)^{-1}\,[1+(1+z)(dr/dz)^{-1}(d^2r/dz^2)]$

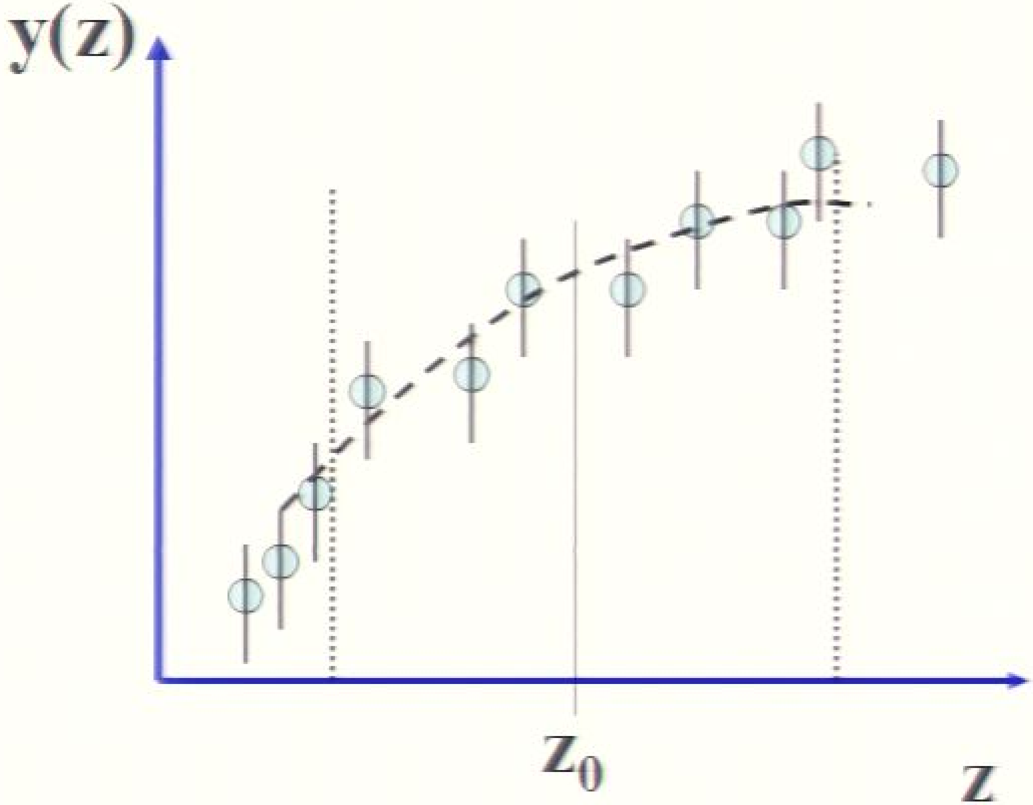
$$q(z) \equiv -(\ddot{a}a)/\acute{a}^2 = -[1+(1+z)(dy/dz)^{-1}\,d^2y/dz^2]$$ [D. 02]

More generally, [D. 02; D. & Djorgovski 2003] showed that:

$$q(z) = -1 - (1+z)y''/y' + \Omega_k y y'(1+z)/(1+y^2\Omega_k)$$

So, $H(z)$ and $q(z)$ can be obtained independent of GR & specific models for the "dark energy;" only assumes FRW metric.

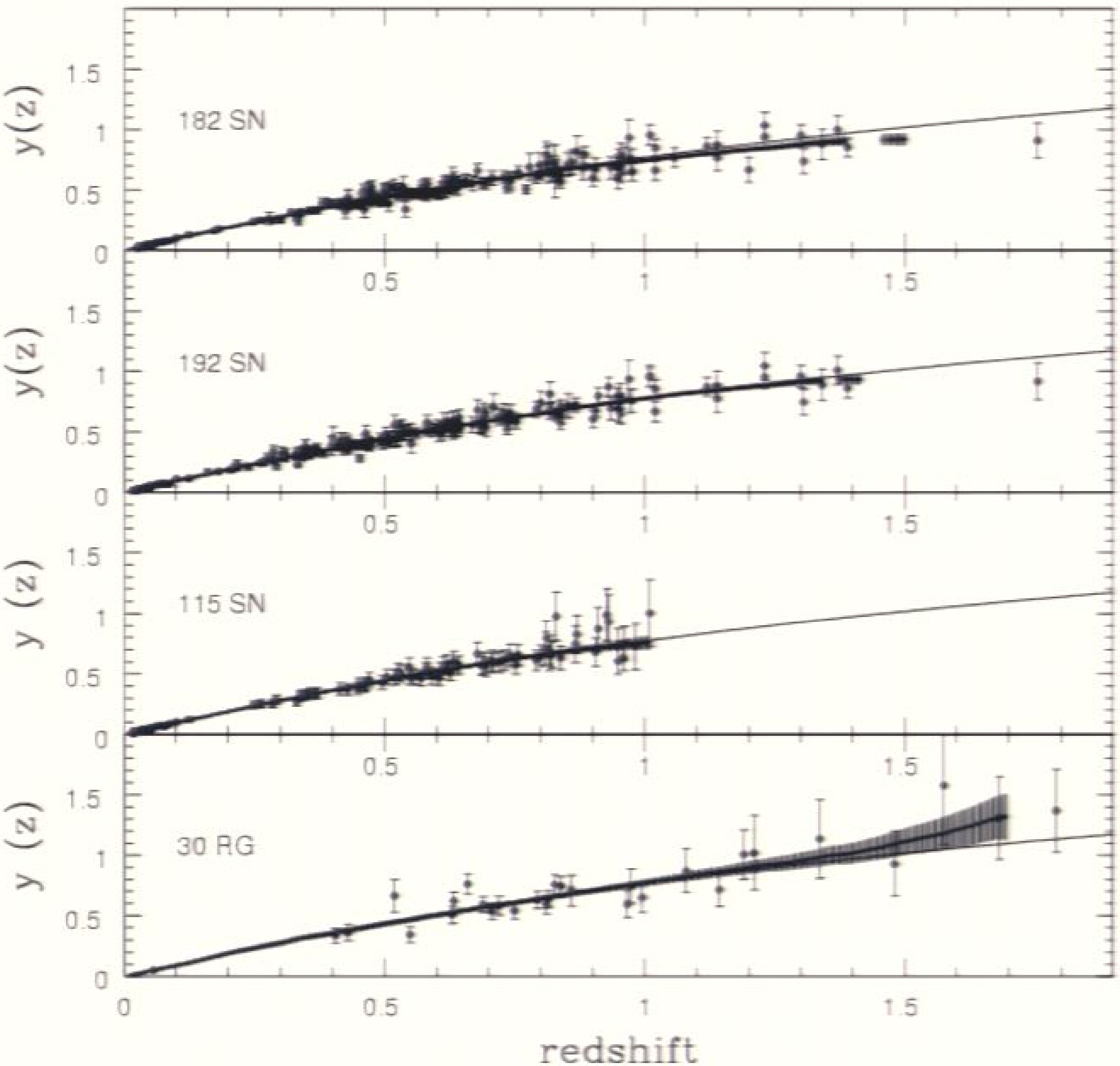
The Methodology



Fit a parabola in a sliding window of Δz around some z_0

From the local fit coefficients, get $y(z_0)$, dy/dz and d^2y/dz^2 *and their errors*

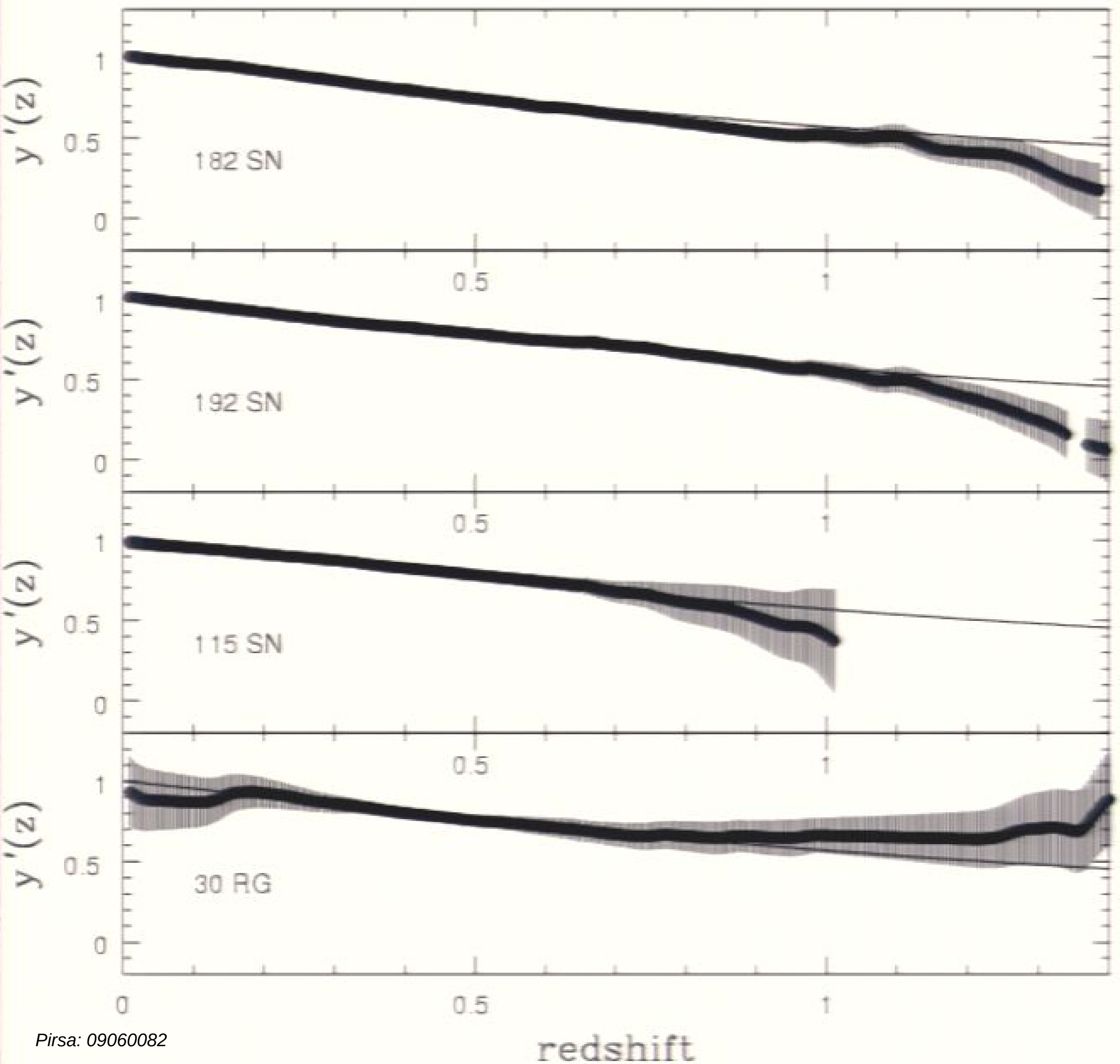
This is equivalent to a local Taylor expansion for y(z); a parabola is a minimum assumption local model for y(z). For noisy/sparse data, need a large Δz: poor redshift resolution, but can determine trends ...



From Daly et al. (2008)

The solid curve is for a standard LCDM model with $\Omega_\Lambda = 0.7$ and $\Omega_m = 0.3$.

High z RG have been on plot since '98

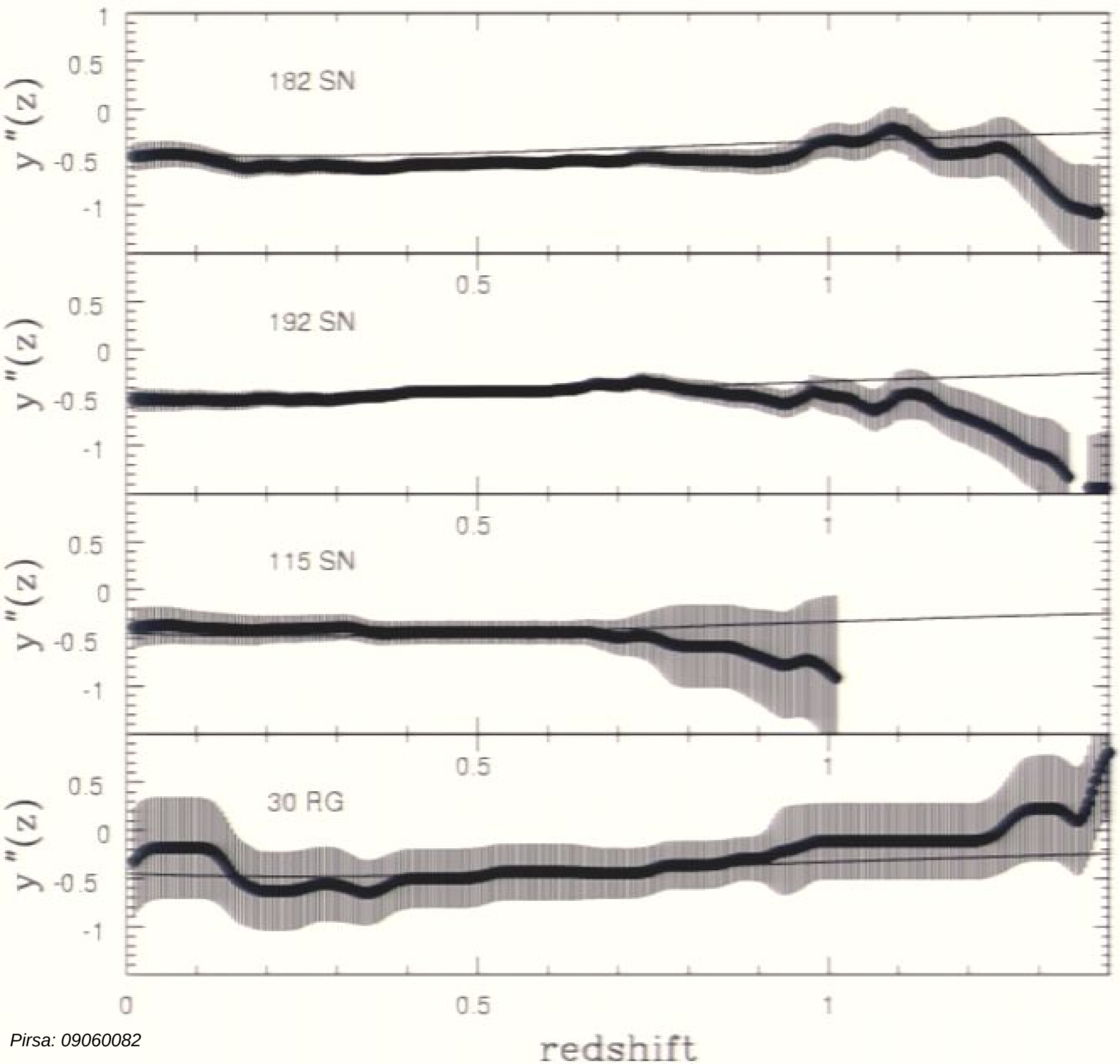


Y' = dy/dz

Model-independent: Provides a large scale test of GR.

Compare with prediction in LCDM model based on GR and Λ=0.7, Ω=0.3

Good agreement between RG & SN



$Y'' = d^2y/dz^2$

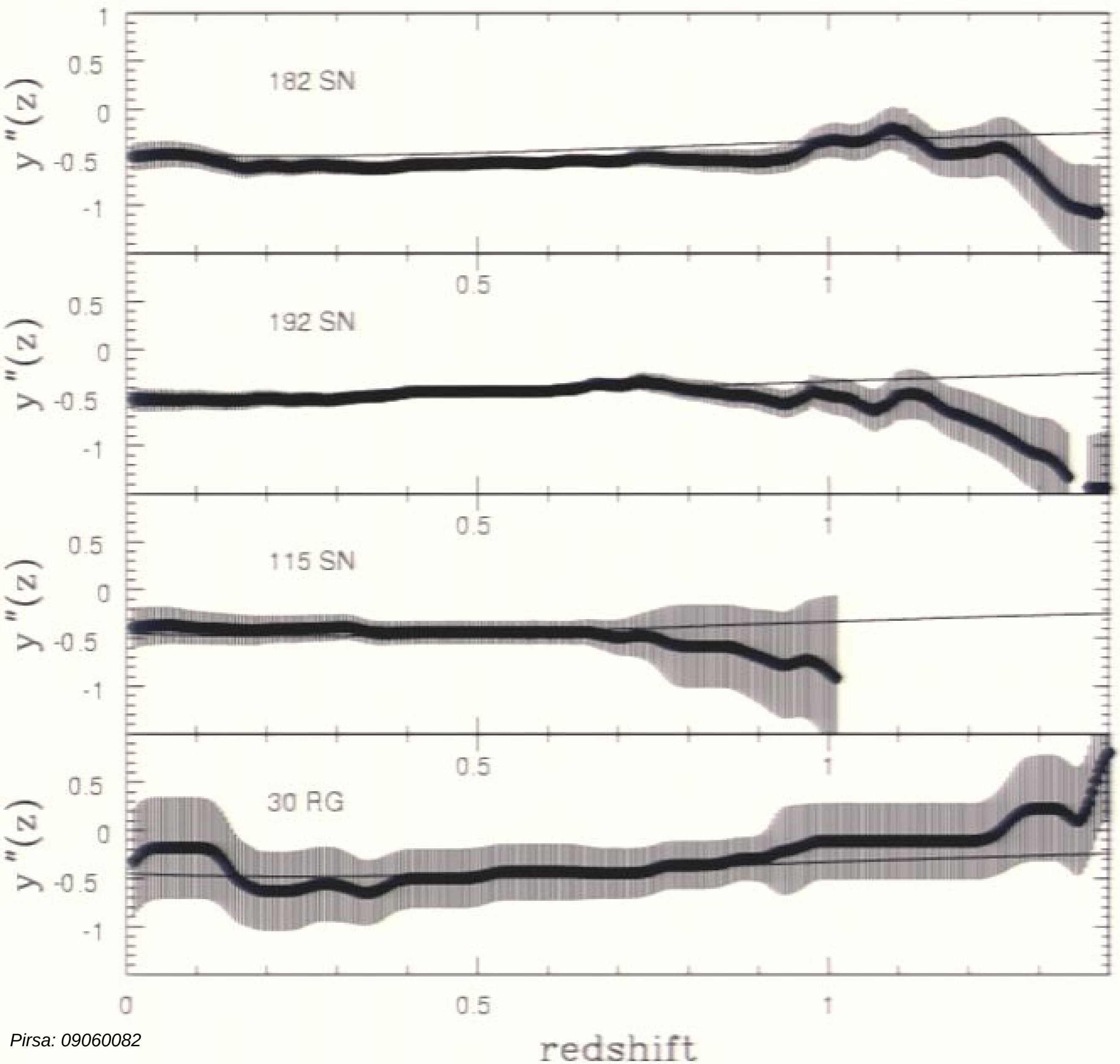
Model-independent

Compare with prediction in LCDM model based on GR

Good agreement between RG & SN

The values of y, y', and y'' obtained directly from the data can be compared with theoretical predictions; there is good agreement with predictions made by GR with $\Lambda \sim 0.7$. This provides a large scale test of GR over look back times of about ten billion years.

Good agreement between y, y', and y'' obtained with SN and RG.



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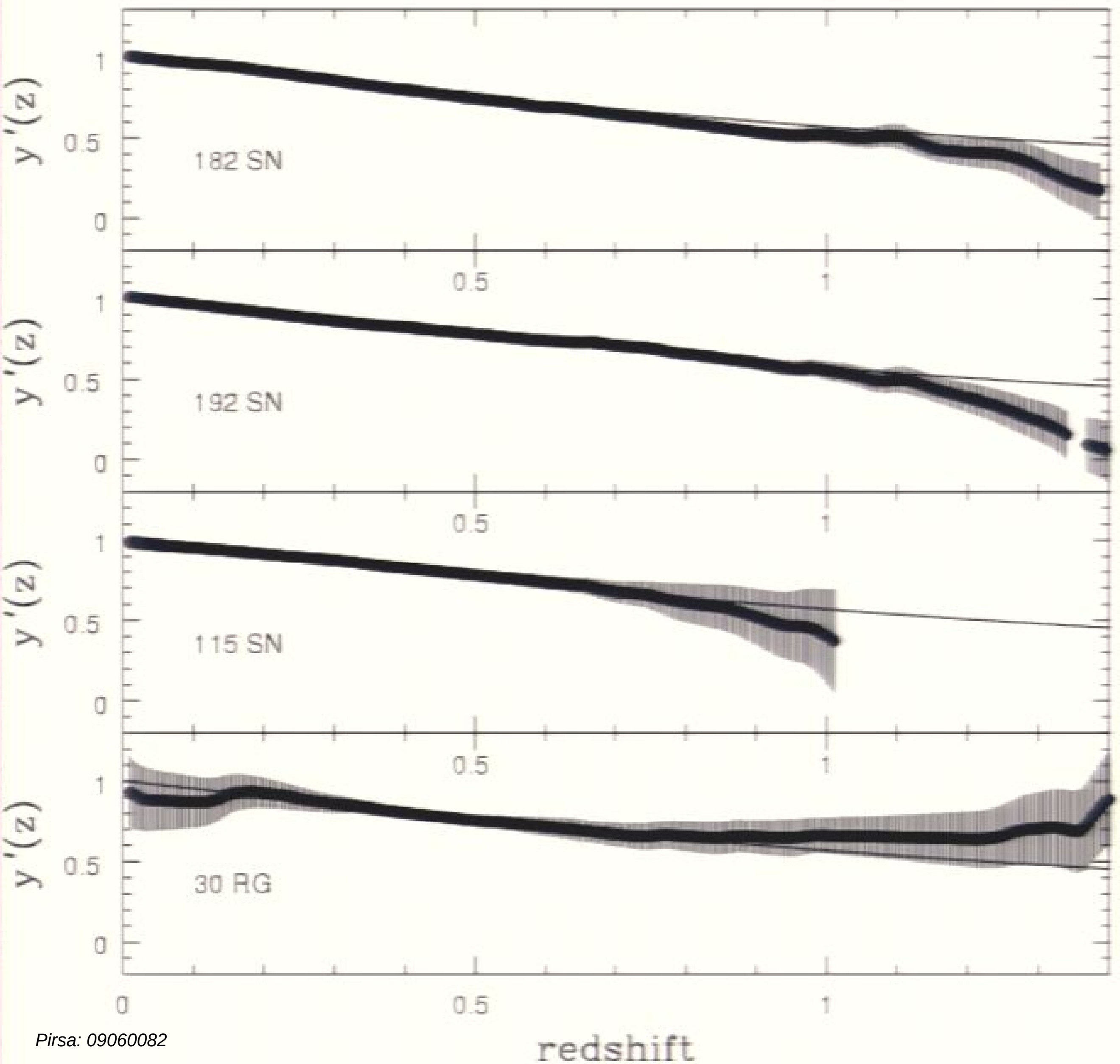

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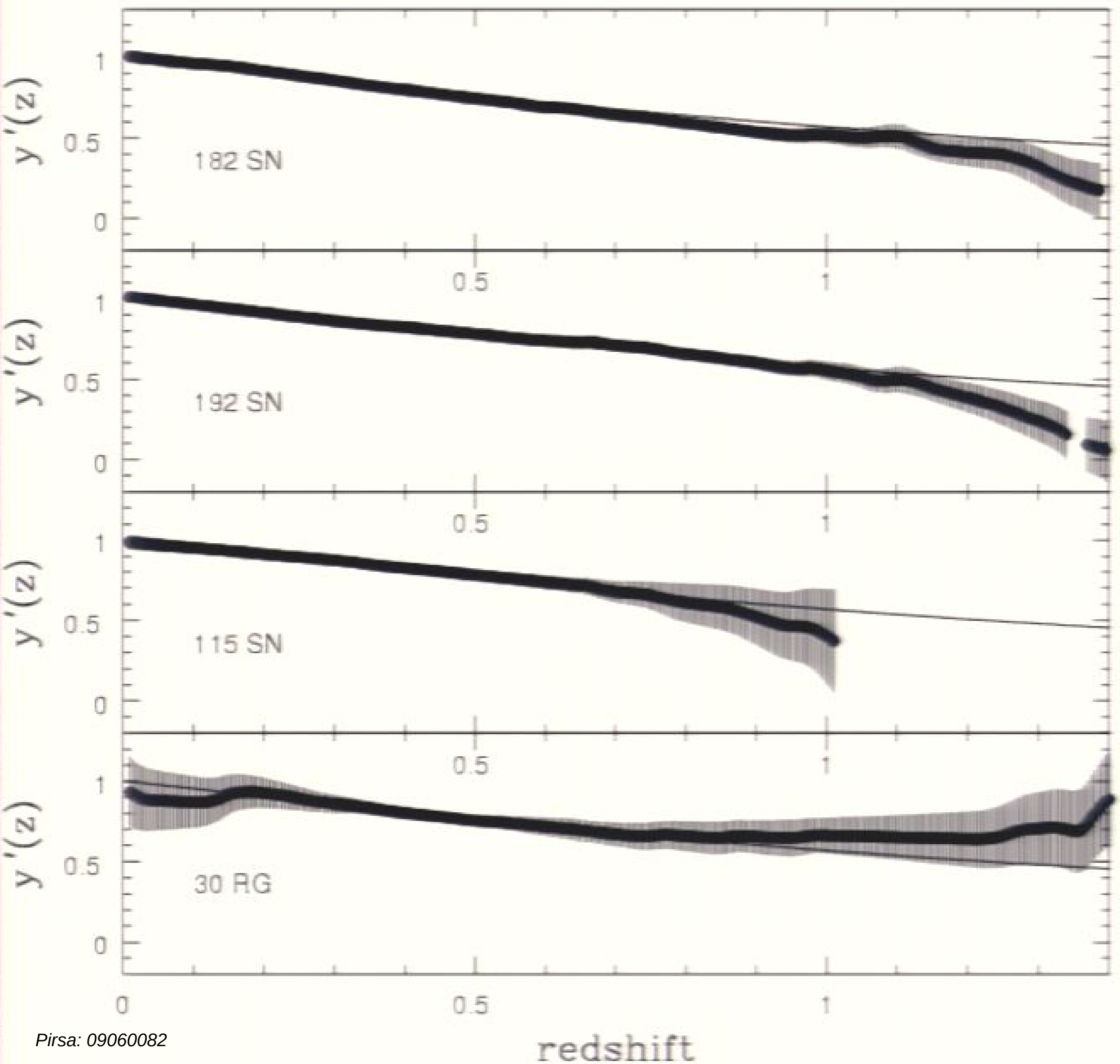

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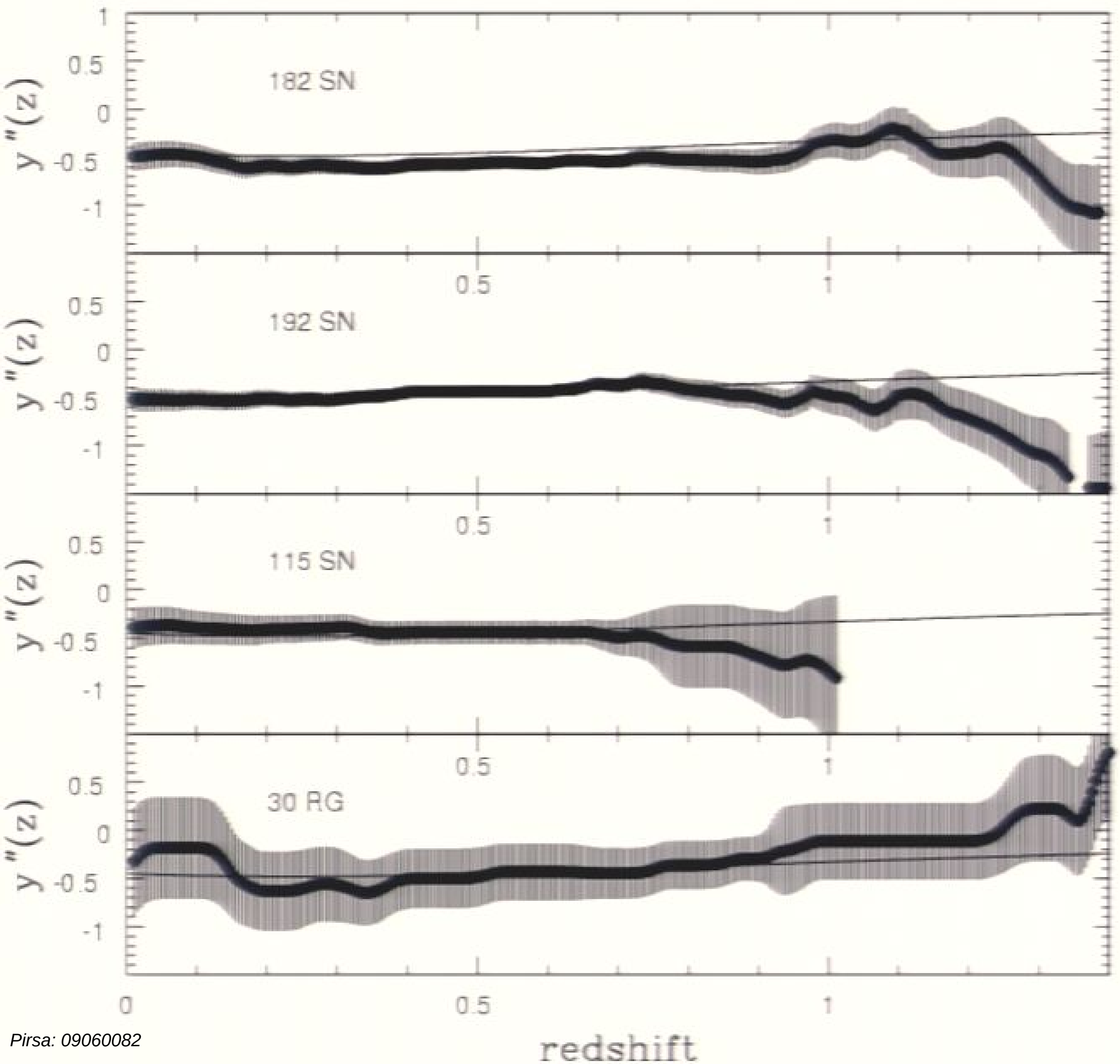

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Good agreement between RG & SN

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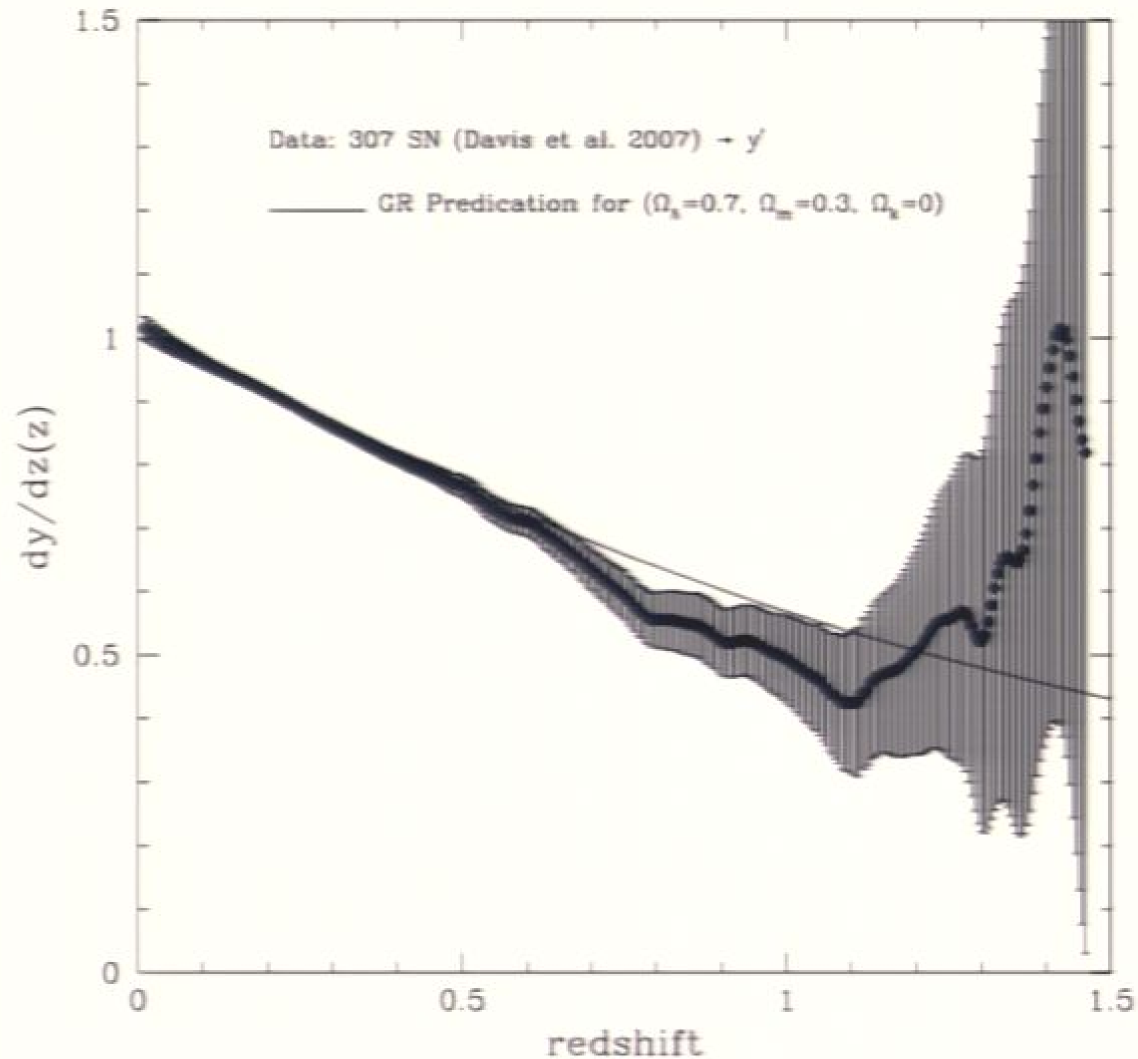
Good agreement between y, y′, and y″ obtained with SN and RG.

307 “Union” SN from Kowalski et al. 08



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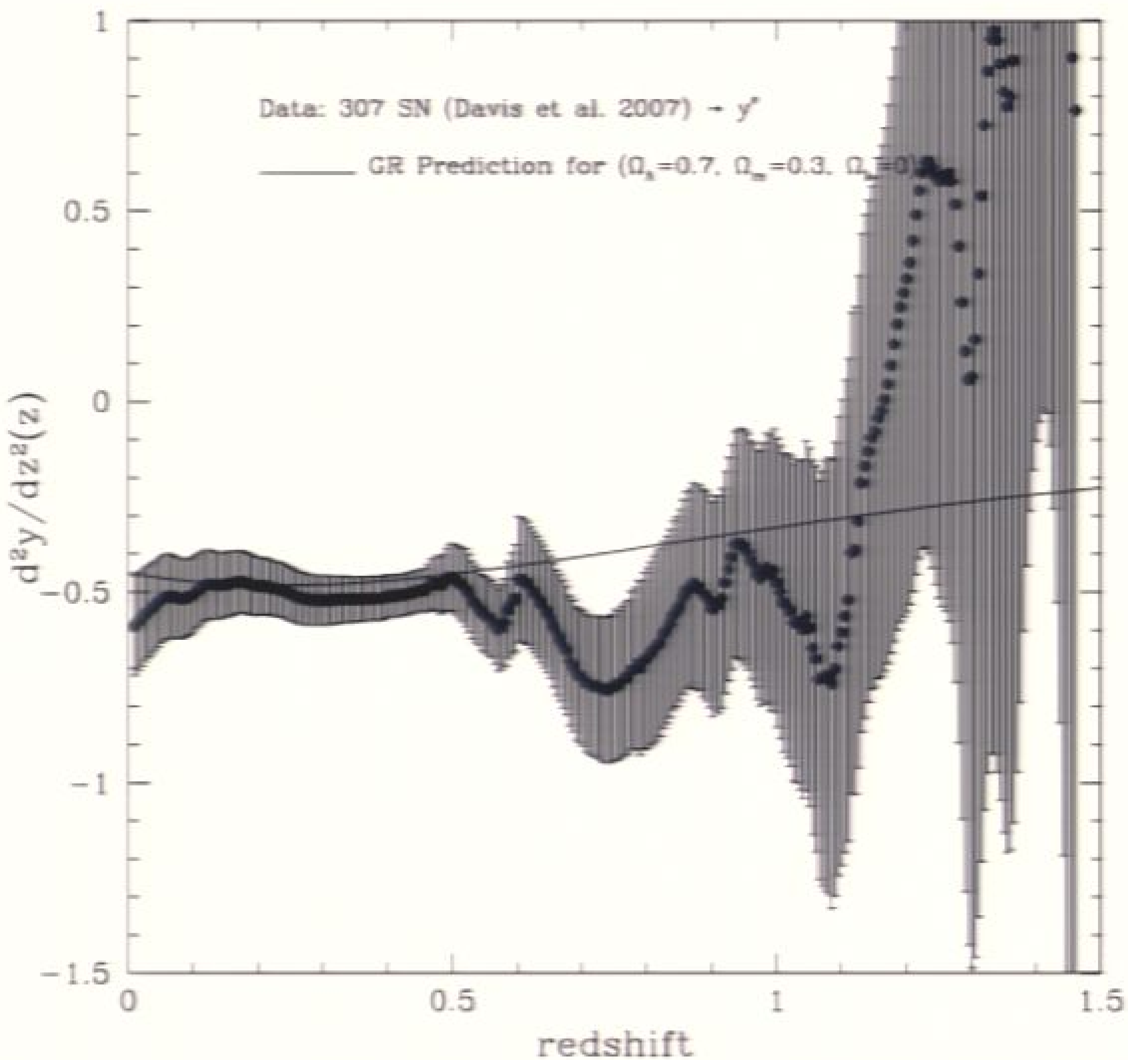
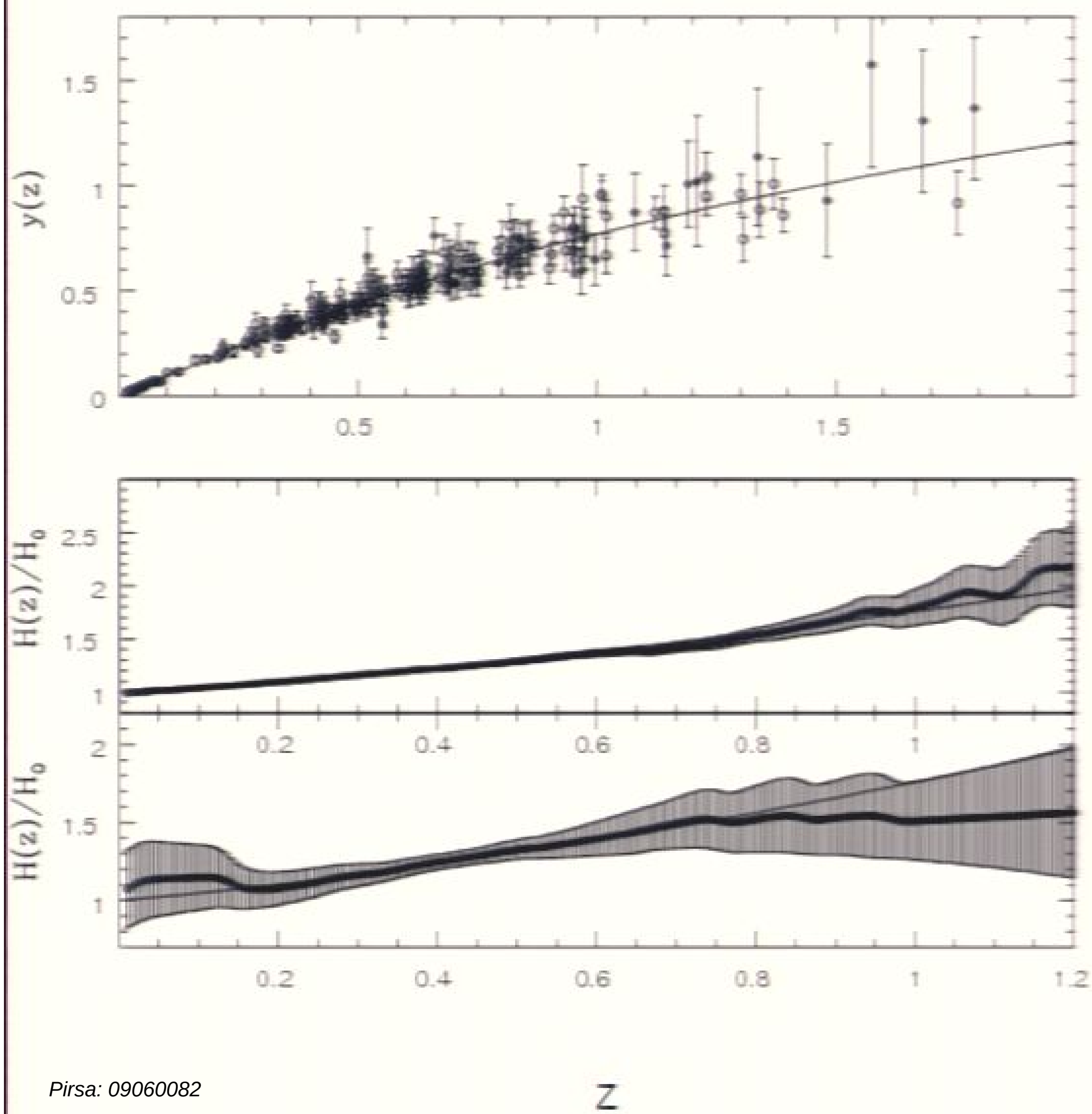


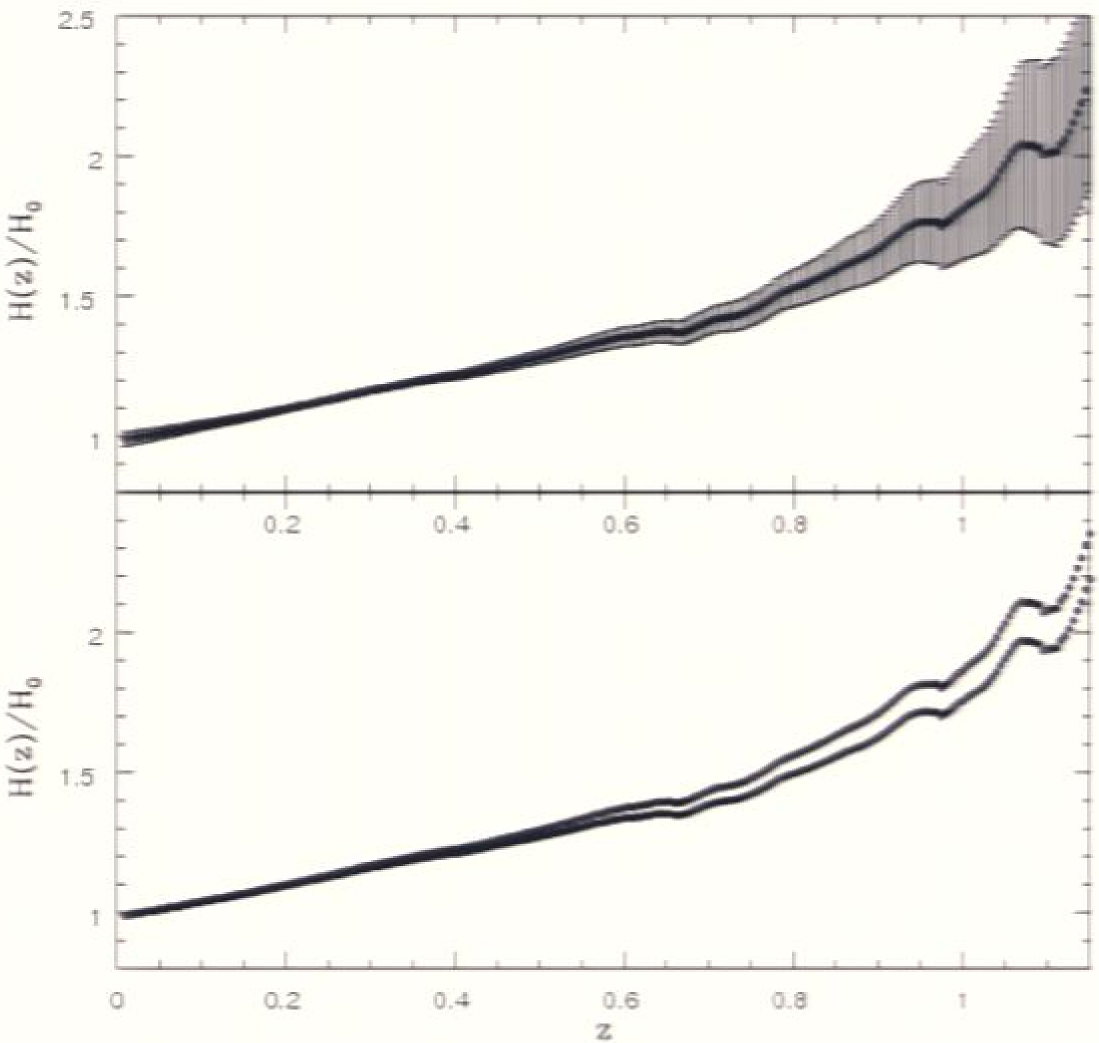
Model-Independent Determinations of $H = (y')^{-1}$ for k=0



H(z) shown here for 192SN of Davis et al. (2007) + 30 RG of Daly et al. (2008)

LCDM shown as solid line

$$H(z)/H_0 = (y')^{-1} (1+\Omega_k y^2)^{1/2}$$



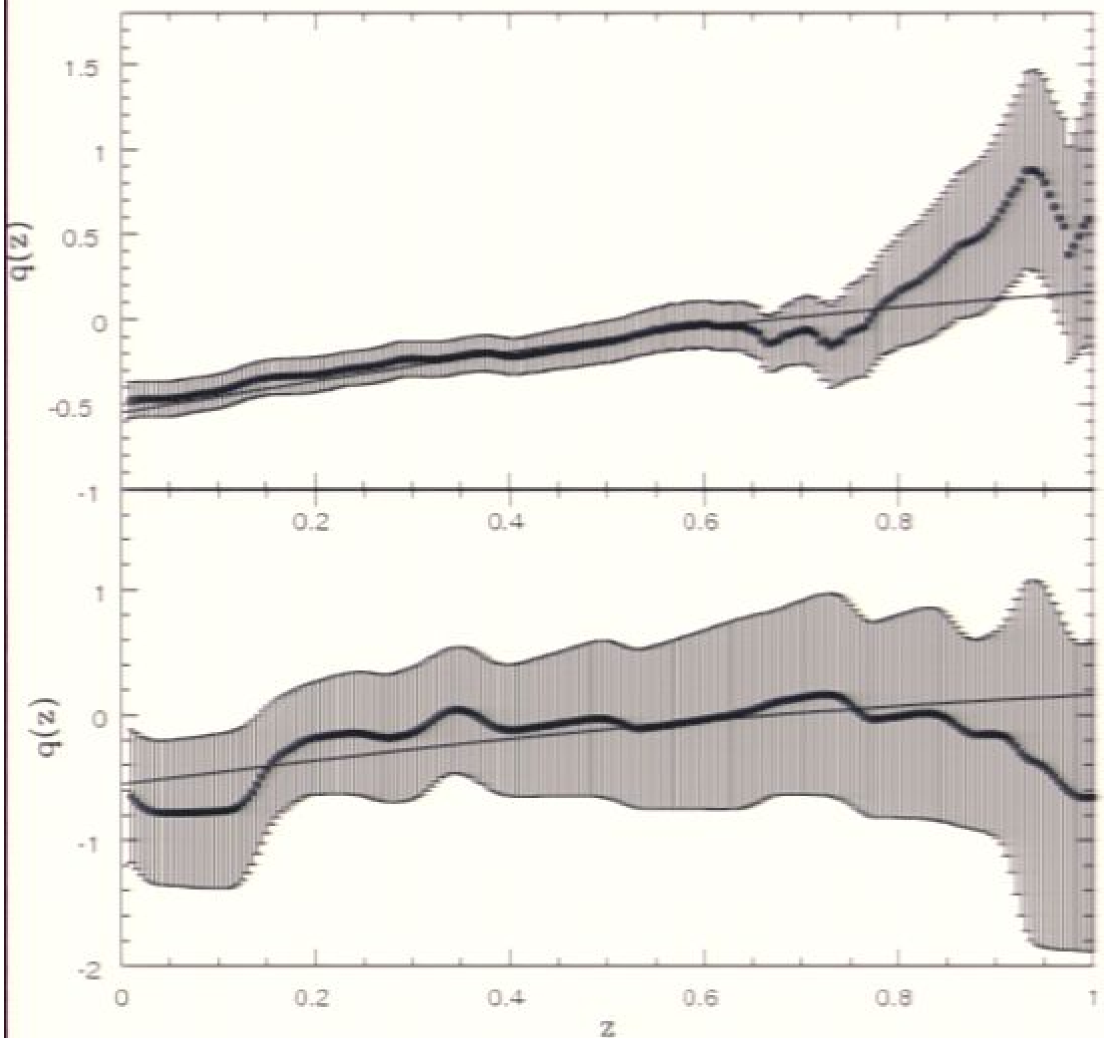
For 192 SN + 30 RG

Effect of k: small for reasonable values of k; Ω_k = 0.1(top) and -0.1(bot)

From Daly et al. (2008)

Model-Independent Determination of q(z); q_o depends only upon FRW metric, independent of k.

$q(z) = -1 - (1+z)y''/y'$ for $k = 0$



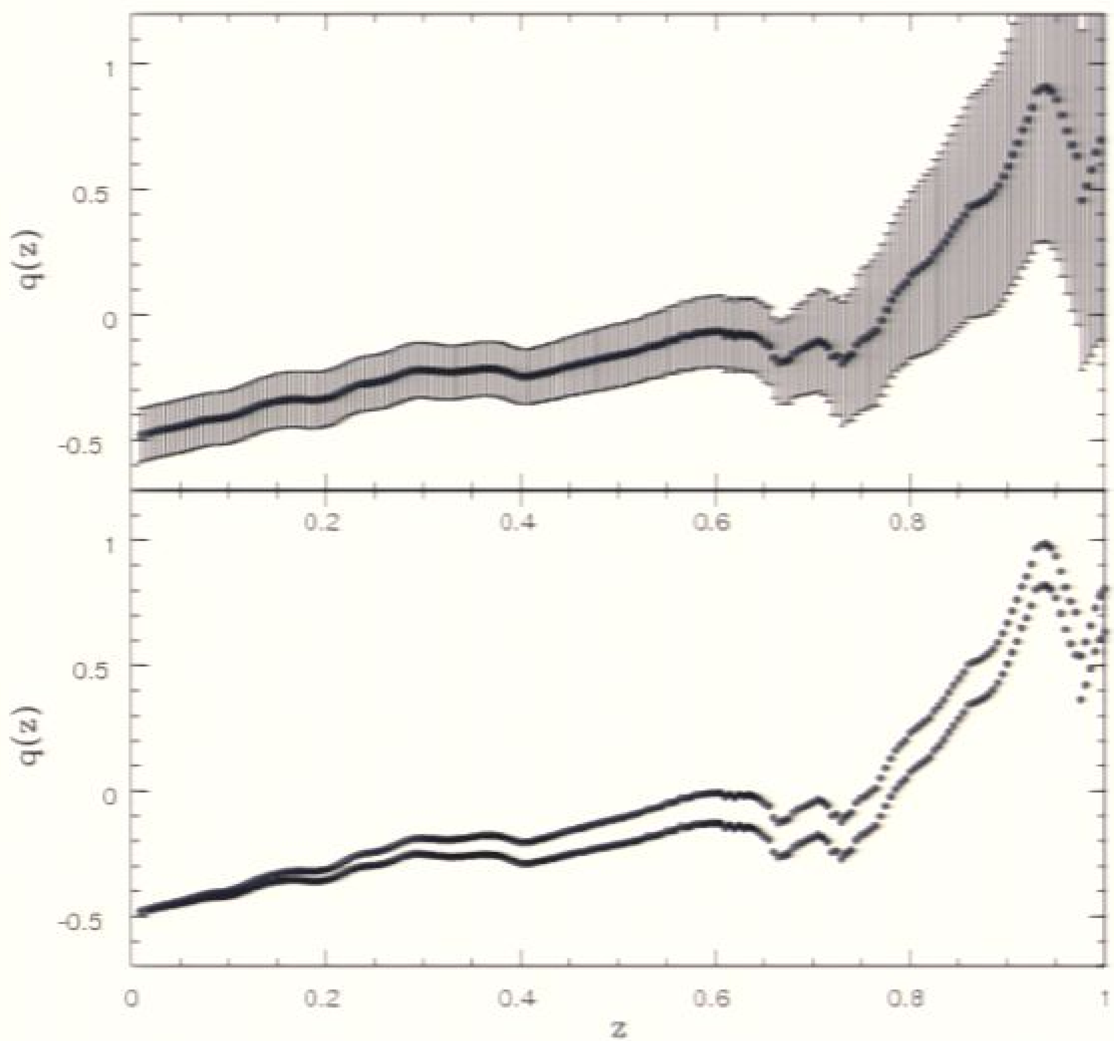
$q_o = -0.48 \pm 0.11$ & $z_T = 0.8 \pm 0.2$ for 192 SN + 30 RG (Daly et al. 2008)

for 30 RG alone $q_o = -0.65 \pm 0.5$.

Solid line is LCDM with $\Omega_m = 0.3$

Model-independent determination of q(z):

$q(z) = -1 -(1+z)y''/y' + \Omega_k yy'(1+z)/(1+y^2\Omega_k)$



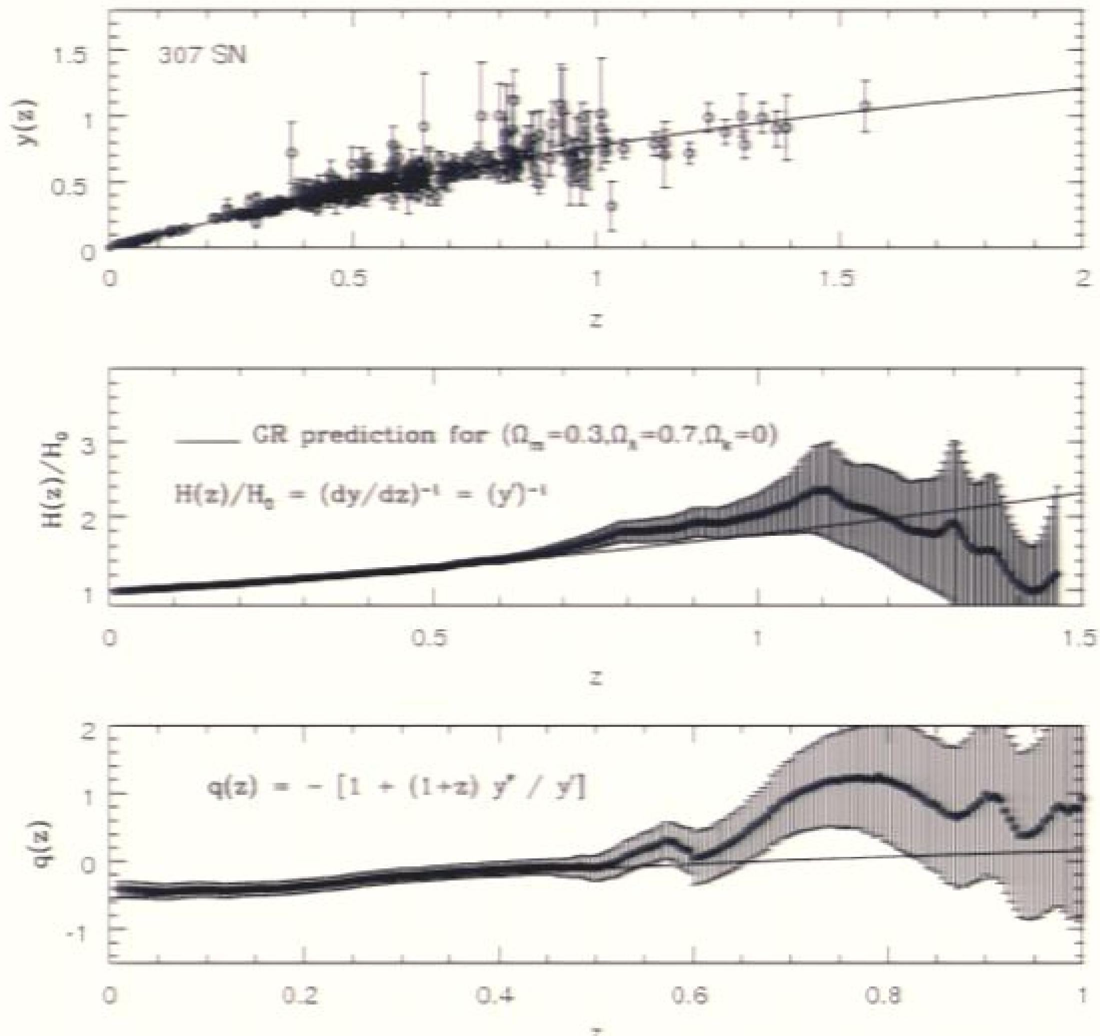
For 192 SN + 30 RG

Effect of k: none on q_0

small effect on z_T for reasonable values of k; Ω_k = 0.1(top) & -0.1(bot)

D. et al. (2008)

307 "Union" SN from Kowalski et al. 08



So, we have shown that assuming only a FRW metric, q_o can be determined; q_0 does not depend on k, GR, or the contents of the universe. SN and RG show that the universe is accelerating today. SN at about 4 sigma, obtained using a sliding window function analysis.

We study the effect of k on q(z) and z_T, and find that it is small for reasonable values of k.

The data suggest that the universe was decelerating in the recent past (1 sigma), with values of q(z) and z_T consistent with predictions in a model based on GR with a cosmological constant and non-relativistic matter (a standard LCDM model).

Another model-independent quantity that can be studied is the Dark Energy Indicator:

A New Model-Independent Function (Daly et al. 2008) the Dark Energy Indicator, s,

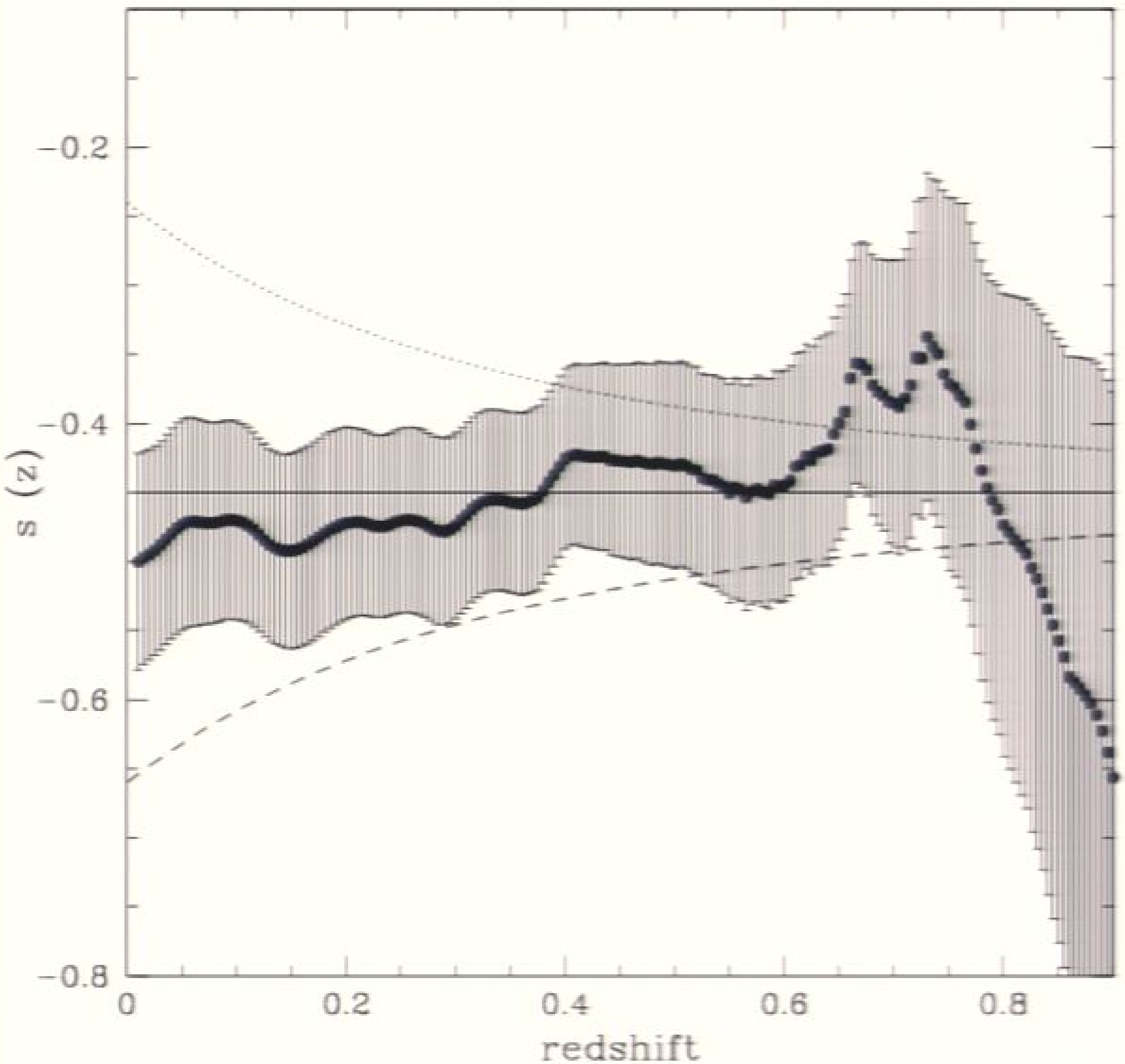
$$s = y'' \, (y')^{-3} \, (1+z)^{-2}$$

In a standard XCDM model based on GR, allowing for variable w, ρ_{DE}, & ρ_m, the predicted value of s is

$$s_p = -1.5\Omega_m \, [1+(w+1)(\rho_{DE}/\rho_m)]$$

If s is constant, it implies that w = -1 & s = -1.5 Ω_m, and s becomes a new and independent measure of Ω_m

In an XCDM model, $w = -1 - (\rho_{DE}/\rho_m)[2s/(3\Omega_m)+1]$



Dark Energy Indicator

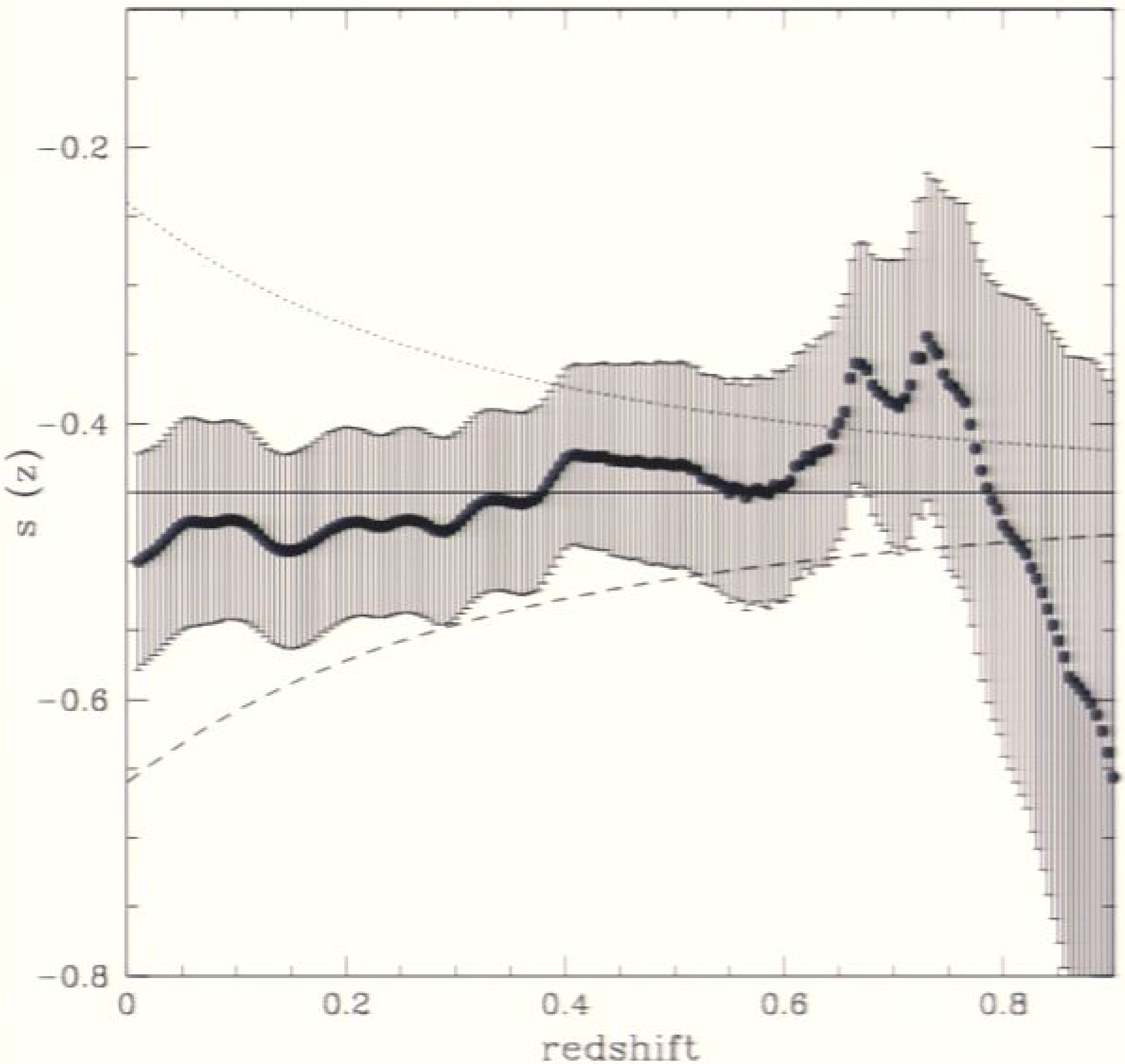
$s = y''(y')^{-3}(1+z)^{-2}$

In a standard XCDM model based on GR, the predicted value of s is

$-1.5\Omega_m[1+(w+1)(\rho_{DE}/\rho_m)]$

Shown: w = -1.2,-1,-0.8

with Ω_m=0.3 &
$(\rho_{DE}/\rho_m)[z=0]$ = .7/.3



S_0 = -0.50 ± 0.08

This implies

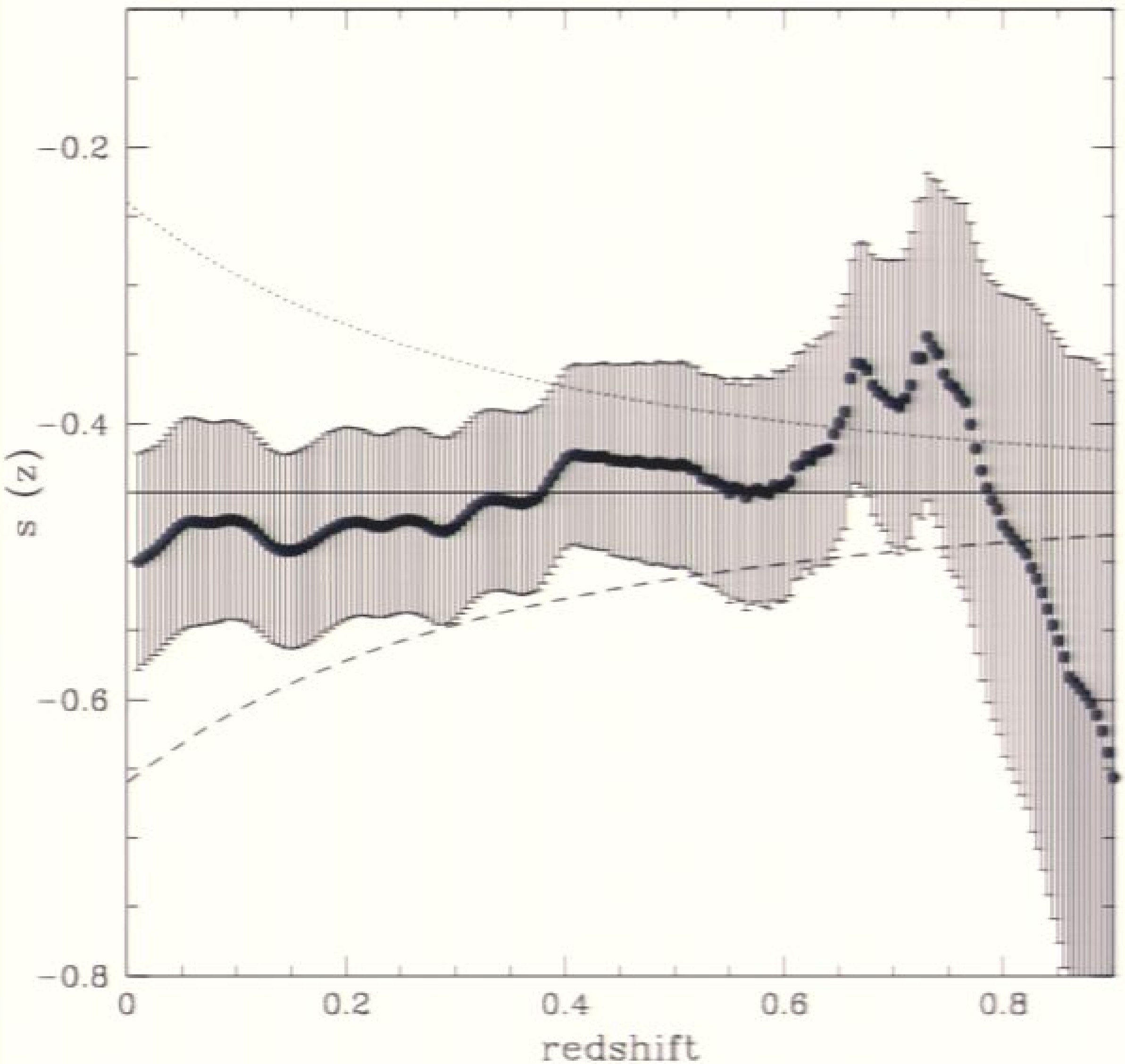
w_0 = -0.95 ± 0.08

for Ω_m = 0.3, and

$[\rho_m/\rho_{DE}](z=0)=0.3/0.7$

For w_0=-1, this implies

Ω_m = 0.33 ± 0.05



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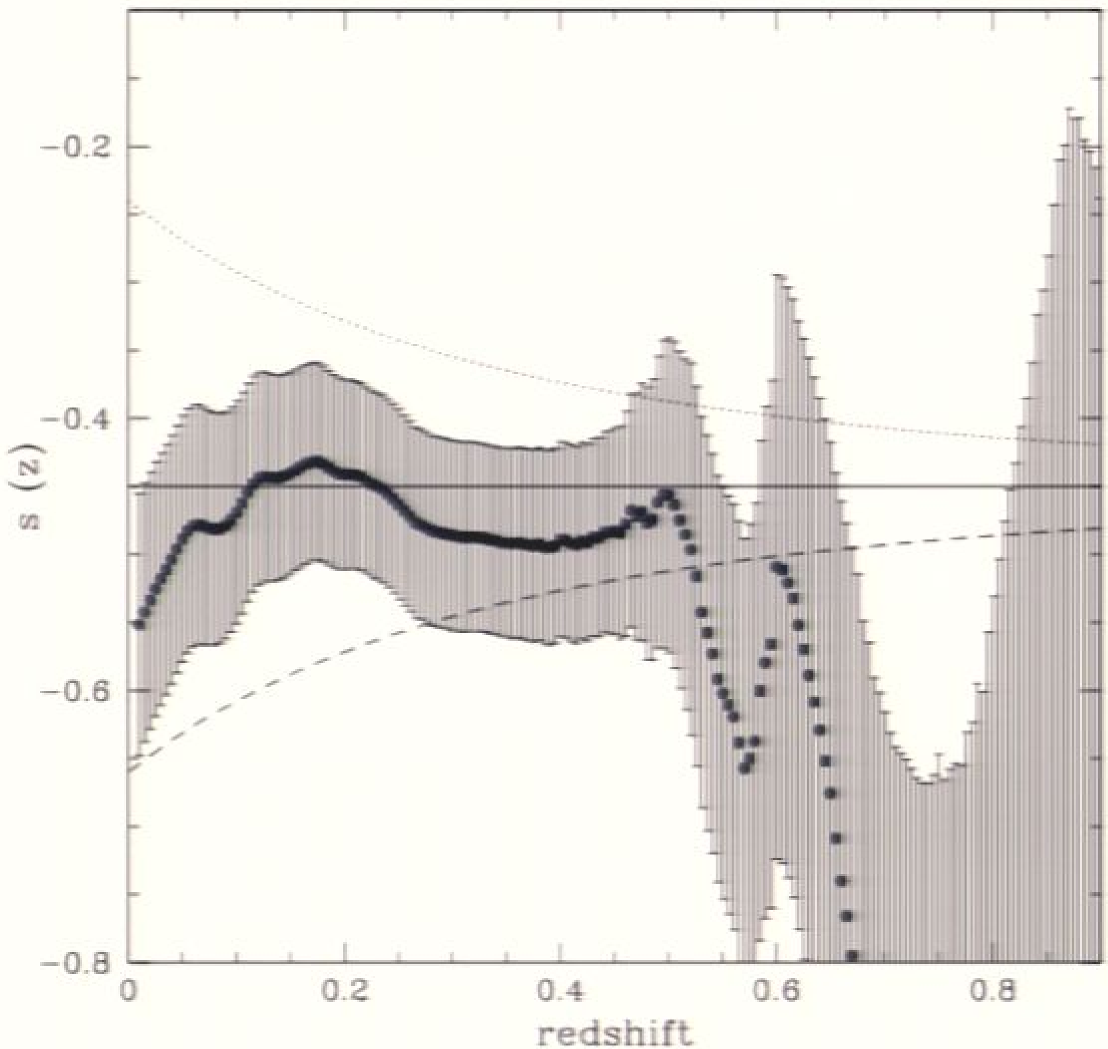
307 SN from Kowalski et al. 08



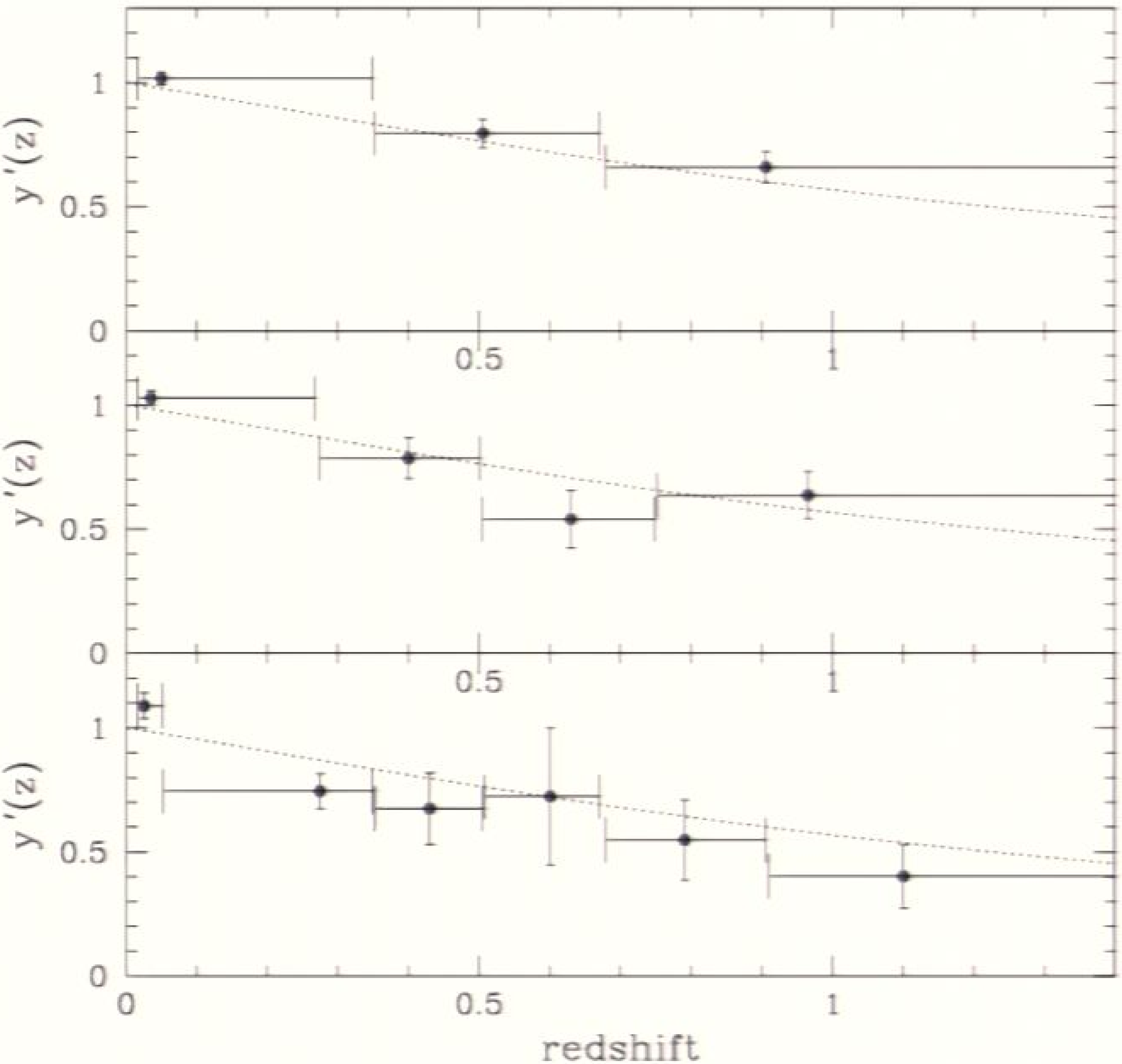
Also interesting to consider results obtained in independent redshift bins (Daly et al. 08); done here for sample of 222 sources (192SN + 30RG) split into

2 bins with 111 sources per bin;

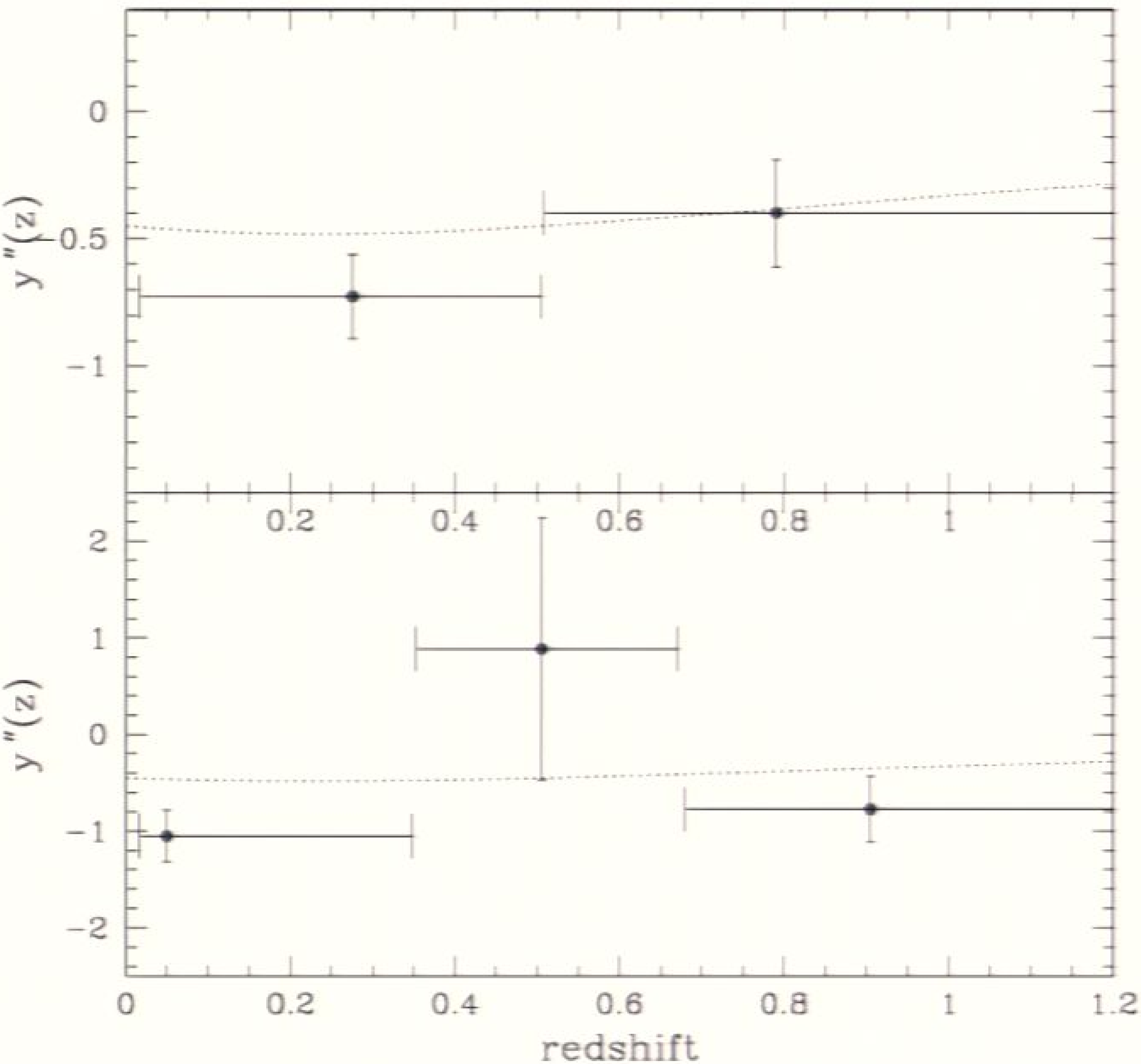
3 bins with 74 sources per bin;

4 bins with 55 sources per bin;

6 bins with 37 sources per bin.

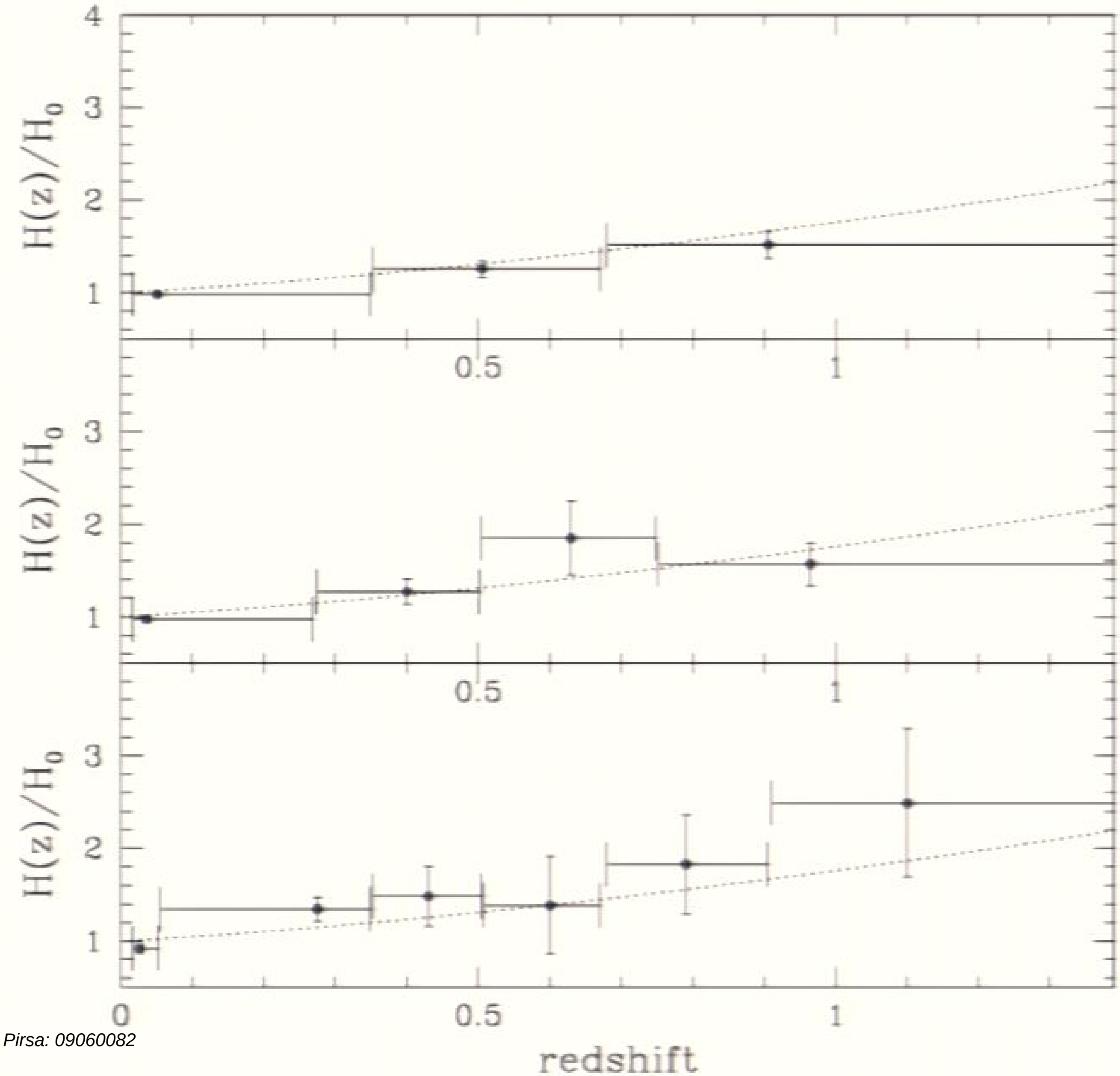


Model-independent results with data analyzed in independent redshift bins with 74 (top), 55 (middle), & 37 (bottom) sources in each bin. Dotted line is LCDM model prediction.

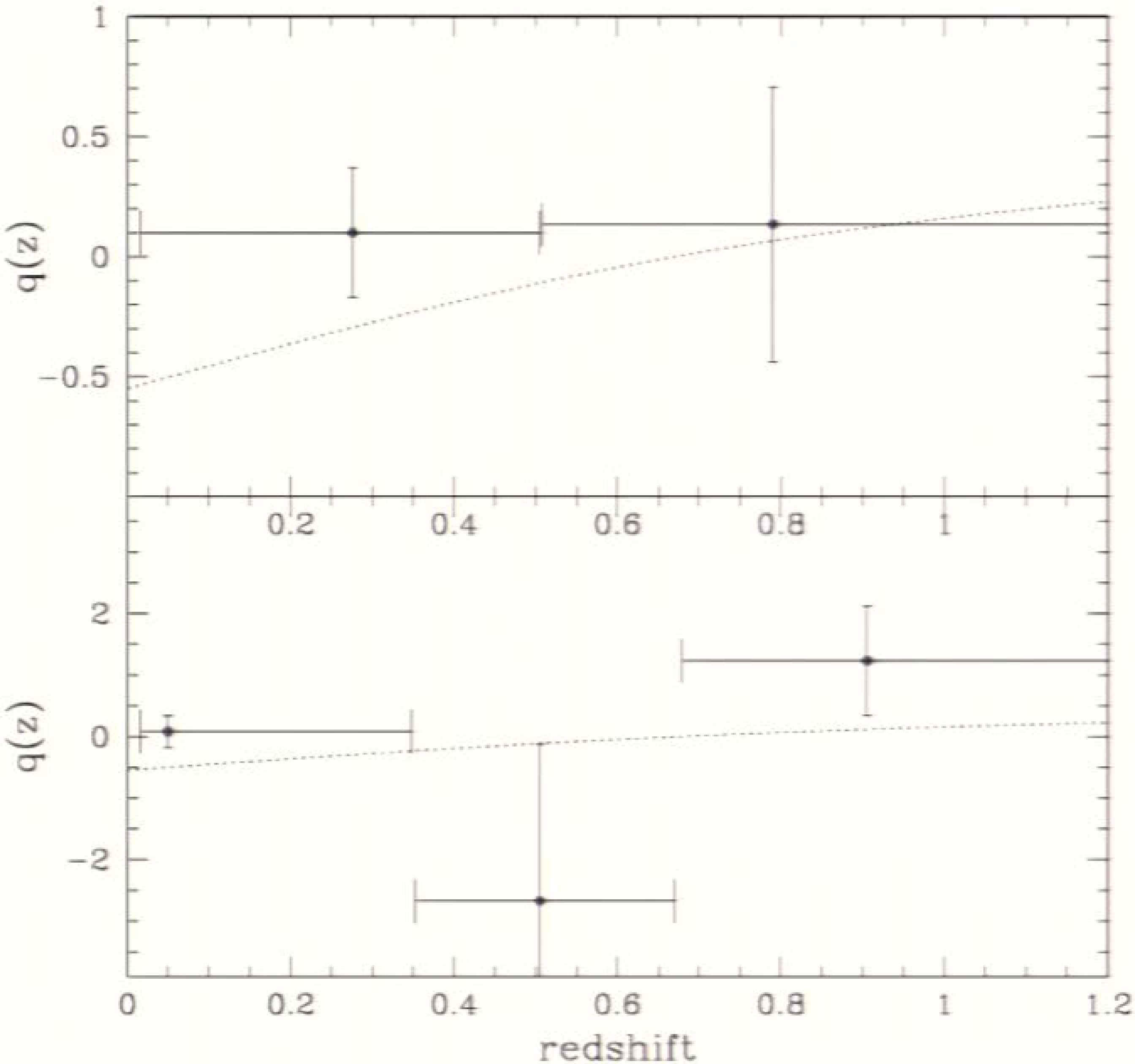


Model-independent results with data analyzed in independent redshift bins with 111 (top) & 74 (bottom) sources per bin.

The LCDM prediction is indicated by the dotted line.



Model-independent determination of H(z) for data analyzed in bins with 74 sources, 55 sources, & 37 sources each; using method of DD03. Dotted line shows the LCDM prediction.



Model-independent determination of q(z) for data analyzed in independent redshift bins of 111 sources (top) & 74 sources (bottom) per bin. Not enough data (yet) to confirm acceleration using binned data.

Now, specify a theory of gravity, GR, &

solve for the pressure $P_E(z)$ of the D.E.

Einstein Equations (for k=0):

$$\ddot{a}/a = -(4\pi G/3)\,[\rho_m + \rho_E + 3\,P_E]$$

$$(\acute{a}/a)^2 = (8\pi G/3)\,[\rho_m + \rho_E]$$

$\rightarrow p_E = [E^2(z)/3]\,[2\,q(z)\,-1]$ or

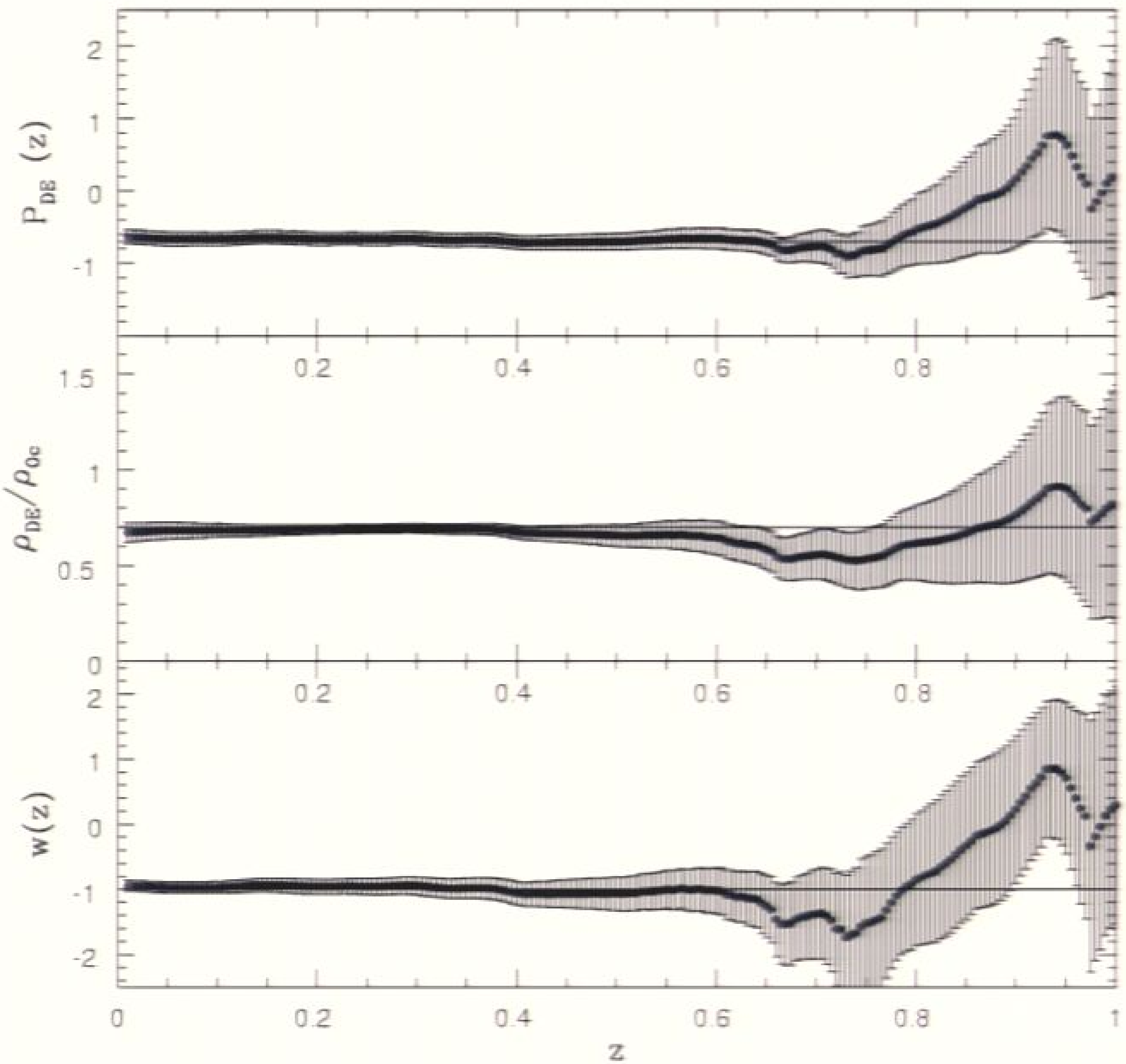
$p_E(z)=-(y')^{-2}[1+(2/3)(1+z)(y')^{-1}\,y'']$, where $p_E(z)\equiv P_E/\rho_{oc}$

With k=0, FRW, + GR, but no specific model for the DE, we have $P_E(z)$. *Can* also solve for the DE energy density and w:

$f_E(z) \equiv \rho_E(z)/\rho_{oc} = (y')^{-2} - \Omega_m(1+z)^3$

$w(z) = p_E(z)/\rho_E(z)$ so

$w = -[1+(2/3)(1+z)(y')^{-1}\,y'']/[1-(y')^2\,\Omega_m(1+z)^3]$



For Λ models, p=-$\Lambda \rightarrow$ direct measure of Λ

We measure P_0=-0.64 ± 0.1

Since $\rho_{0E}=p_0/w_0$, Ω_{0E}=0.64 ± 0.1 for w_0 = -1

We measure w_0 = -0.95±0.08

Consistent with Λ models, but possible evolution

Now, specify a theory of gravity, GR, &

solve for the pressure $P_E(z)$ of the D.E.

Einstein Equations (for k=0):

$$\ddot{a}/a = -(4\pi G/3)\,[\rho_m + \rho_E + 3\,P_E]$$

$$(\dot{a}/a)^2 = (8\pi G/3)\,[\rho_m + \rho_E]$$

$\rightarrow p_E = [E^2(z)/3]\,[2\,q(z) - 1]$ or

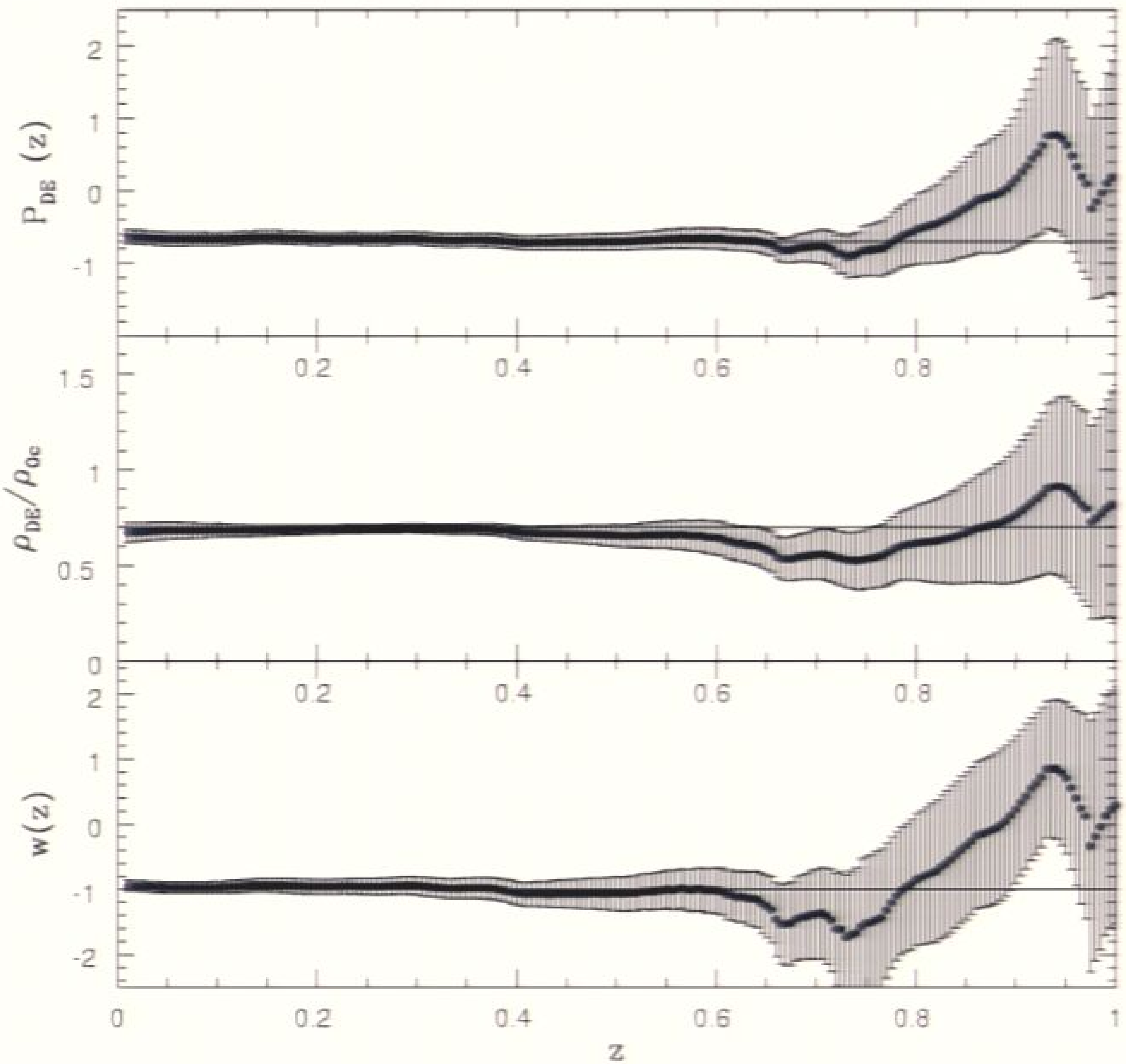
$p_E(z) = -(y')^{-2}[1+(2/3)(1+z)(y')^{-1}\,y'']$, where $p_E(z) \equiv P_E/\rho_{oc}$

With k=0, FRW, + GR, but no specific model for the DE, we have $P_E(z)$. Can also solve for the DE energy density and w:

$f_E(z) \equiv \rho_E(z)/\rho_{oc} = (y')^{-2} - \Omega_m(1+z)^3$

$w(z) = p_E(z)/\rho_E(z)$ so

$w = -[1+(2/3)(1+z)(y')^{-1}\,y'']/[1-(y')^2\,\Omega_m(1+z)^3]$



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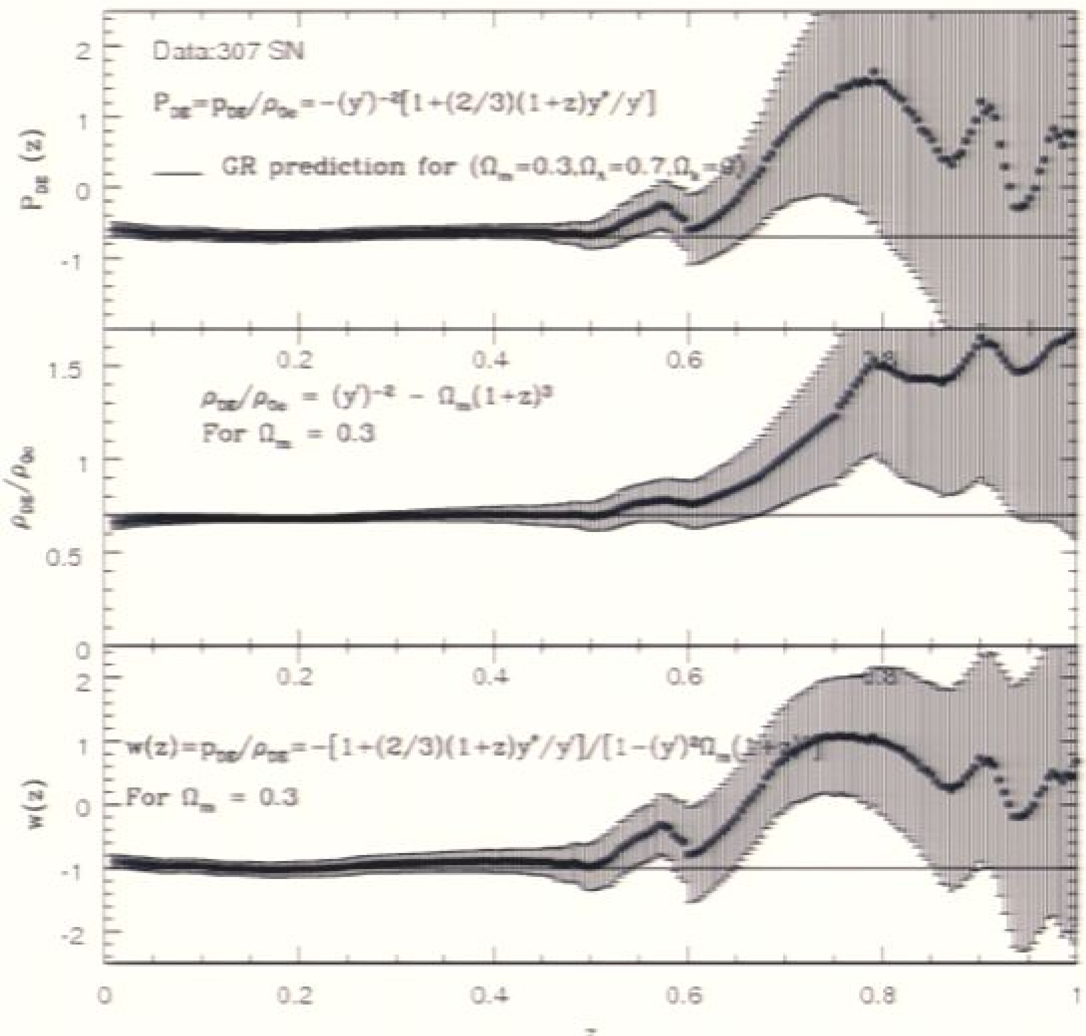
Consistent with Λ models, but possible evolution

307 “Union” SN from Kowalski et al. 08



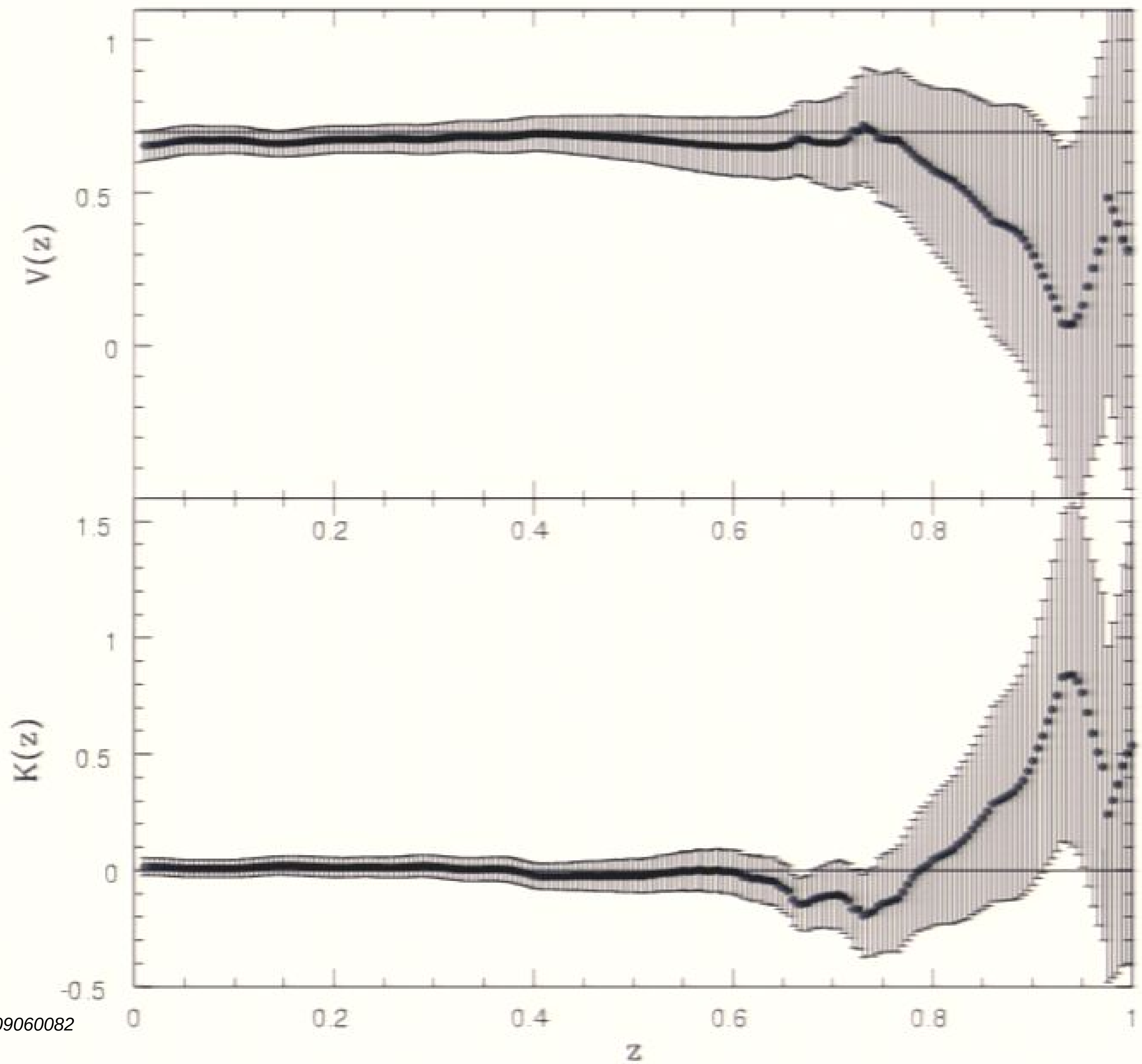
The potential energy density V of a dark energy scalar field and the kinetic energy density K are related to the energy density ρ and pressure P of the dark energy:

$$\rho = K + V; \quad P = K - V \text{ where } K = 0.5\,\dot{o}^2$$

$V = 0.5\,(\rho - P)$ and $K = 0.5\,(\rho + P)$

$$V(z)/\rho_{0c} = (y')^{-2}\,[1+(1+z)(y')^{-1}\,y''/3] - 0.5\Omega_{om}(1+z)^3$$

$$K/\rho_{oc} = -\,(1+z)\,[y']^{-3}y''/3 \;-\; 0.5(1+z)^3\Omega_{om}$$



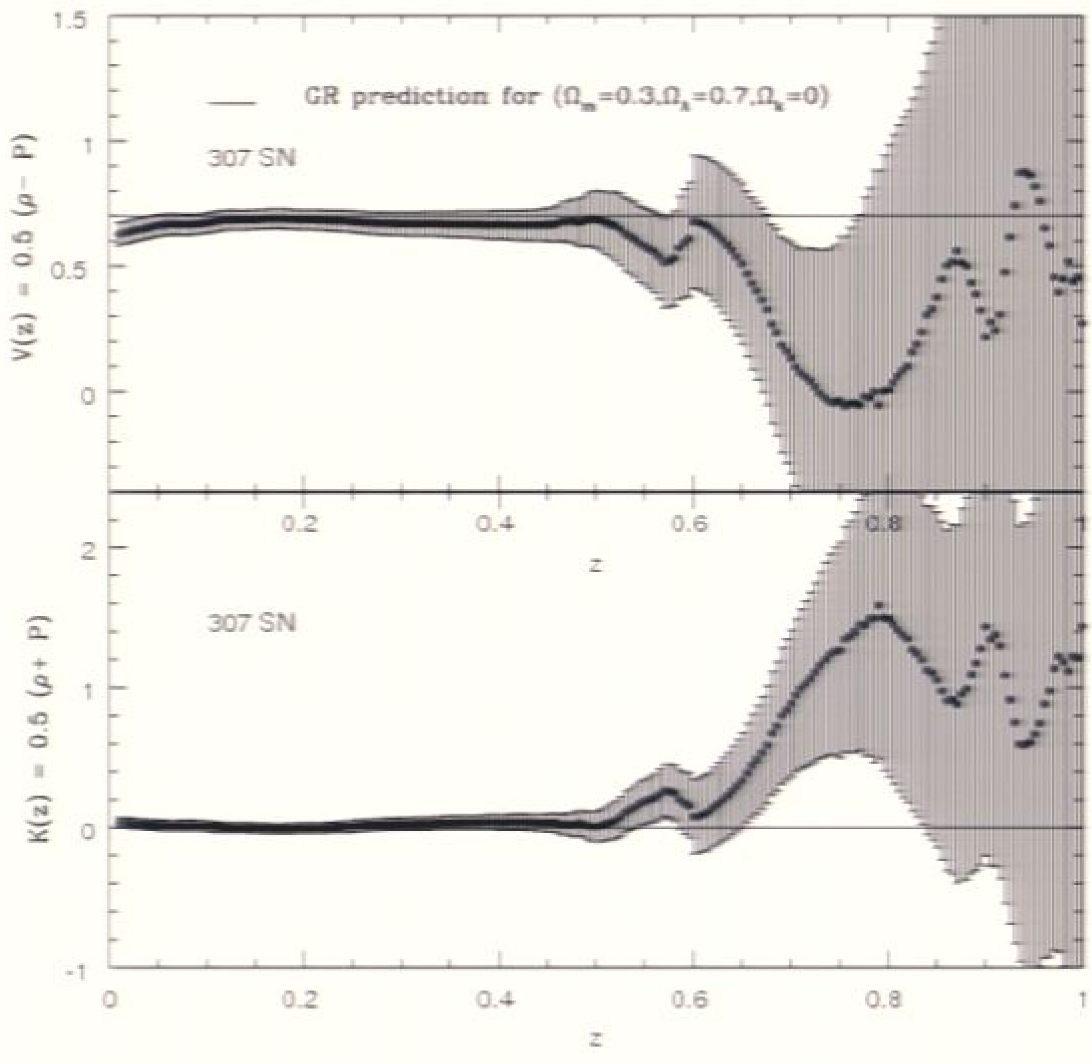
We measure

V_0=0.65±0.05

and

K_0=0.01±0.03

307 SN from Kowalski et al. 08



Summary of Part I

Determinations of y, y', & y", which are completely model-independent, are in very good agreement with predictions in a standard LCDM model based on GR, k = 0, and a cosmological constant; this provides a large-scale test of GR over cosmological distances.

Good agreement between y, y', and y" obtained with RG & SN; provides support for both methods.

Model-independent determinations of H(z) and q(z) have a very weak dependence on k for reasonable values of this parameter, and q_0 is independent of k.

We find $q_0 = -0.48 \pm 0.11$, and a transition redshift of about 0.8 ± 0.15.

A new model-independent function, the dark energy indicator, s, is introduced. A constant value of s indicates that w = -1.

We find that s is constant and that $w_0 = -0.95 \pm 0.08$.

The data may be used to solve for the properties of the DE as functions of redshift (e.g. P, ρ, w, V, & K) assuming GR is the correct theory of gravity and k = 0.

The empirical relationship that forms the basis of the RG method can be understood in context of a standard magnetic braking model for AGN.

SN data is reaching the point where the details of the light curve analysis method is becoming important. In addition, enough high z sources are being observed that k corrections may become significant.

A Bit of History

It has now been about ten years since the acceleration of the universe was first announced. Results obtained with radio galaxies provided one of the first indications that the universe is accelerating.

1997 and 1998 were very exciting years for cosmology!!!

In late 1997, Steve Maran from the AAS press office contacted me and asked me if I would do a press release on cosmological studies with powerful radio galaxies for the January 1998 AAS meeting.

The release explains how the angular diameter test works, and the relationship between the expansion rate of the universe and the intrinsic sizes of radio galaxies; for a given observed angular size, a large intrinsic size means that the universe was accelerating in its expansion.

News from
PRINCETON UNIVERSITY
Office of Communications, Stanhope Hall
Princeton, New Jersey 08544
Tel 609/258-3601; Fax 609/258-1301

Contact: Dr. Ruth Daly 609/258-4413 daly@pupgg.princeton.edu
Date: January 8, 1998

The Ultimate Fate of the Universe

Washington, DC -- Astrophysicists announced today new predictions of the ultimate fate of the universe obtained by calculating the characteristic or maximum size of very distant radio galaxies. Reports being presented by Dr. Ruth A. Daly, and Dr. Erick Guerra, both of Princeton University, in Princeton, New Jersey, to the American Astronomical Society meeting in Washington, DC, suggest that the expanding universe will continue to expand forever, and will expand more and more rapidly as time goes by.

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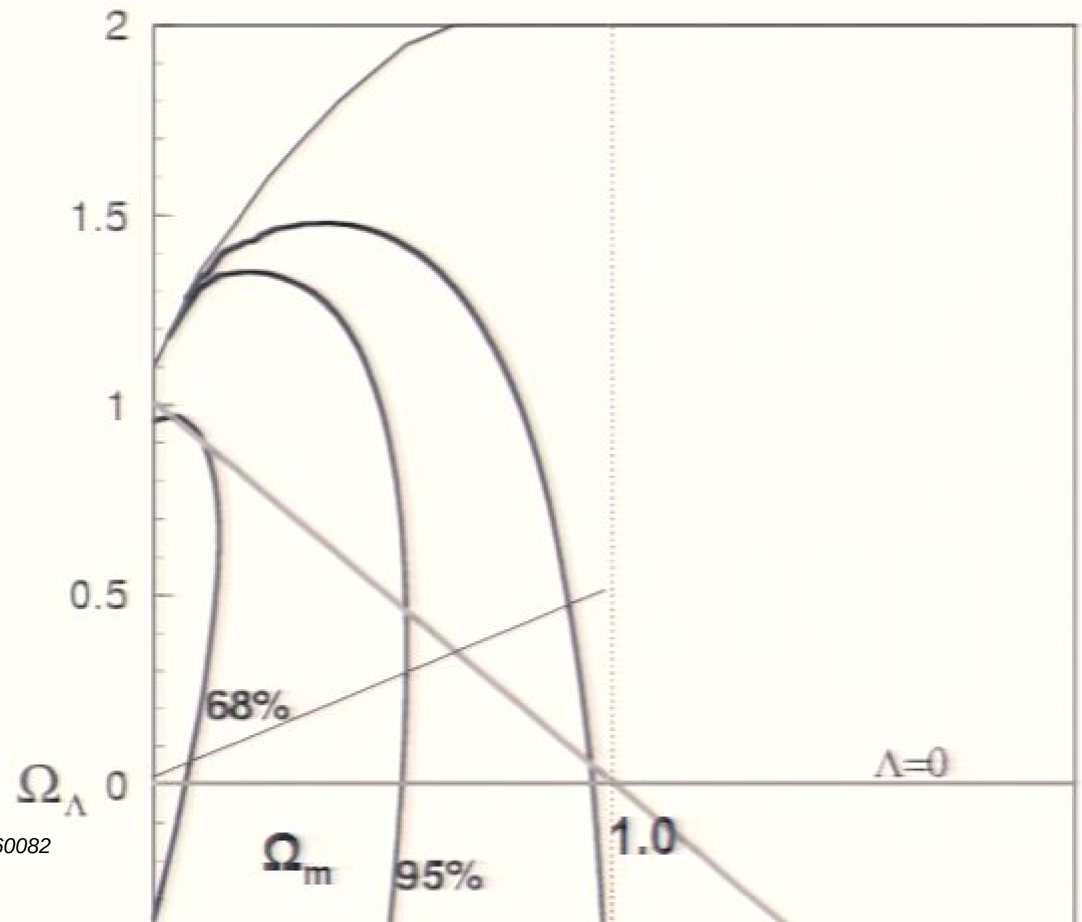
Fourteen radio galaxies with redshifts between zero and two were used for this study. All of the radio galaxies included in the study are classical double radio sources similar to the nearby radio galaxy Cygnus A. Such classical double radio sources are cigar -shaped, with a black hole at the center and a radio "hot spot" at either end of the gaseous cigar. Astrophysicists consider the size of a classical double radio galaxy to be the distance between the two radio hot spots.

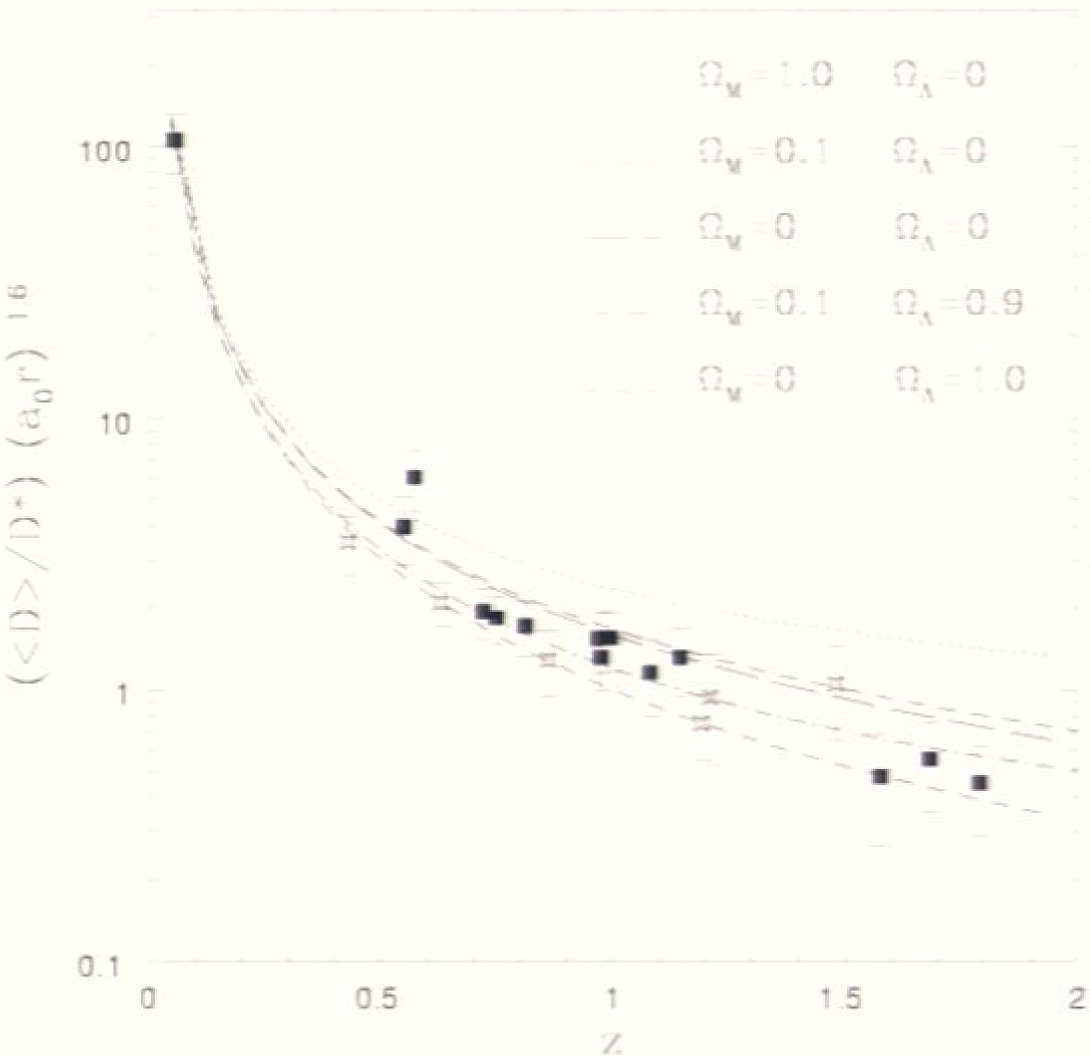
Previous work by the Princeton group had established that all classical double radio galaxies at a given redshift, or distance from earth, are of similar maximum or characteristic size; this size depends on the inverse of the distance from earth. The apparent characteristic or maximum size of the full population of radio galaxies at the same redshift depends on the distance to the sources. Thus, equating the two measures of the characteristic or maximum size of the sources allows an estimate of the distance to the sources. Knowing this distance is equivalent to knowing the global geometry of the universe, or the ultimate fate of the universe. This new work measures more radio galaxies, and radio galaxies at higher redshift, or greater distance from earth; it also involves more sophisticated statistical manipulations of the measurements.

The apparent size, or distance from hotspot to hotspot, of a high redshift radio galaxy is a clue to which of the competing models of the nature of the universe is most likely. A relatively small size at great distance from earth would suggest a universe that will halt its current expansion and recollapse; a larger size suggests a universe that will continue to expand forever, but at an ever decreasing rate; an even larger size suggests the universe will continue to expand, and will expand at a faster and faster rate. The current work finds that at high redshift the galaxies are very large, with widely separated radio hotspots. Thus, the universe will continue to expand forever and will expand at a faster and faster rate as time goes by.

From Guerra, Daly, & Wan (1998)
(astro-ph/9807249)

And presented at Jan. 1998 AAS meeting.





From Guerra, Daly, & Wan (1998) (astro-ph/9807249)

And presented at Jan. 1998 AAS meeting.

Note high z RG

This work was presented during the Jan. '98 press release session and during a regular AAS session. The press release session was very exciting. Adam Riess and Saul Perlmutter were there, and I had a chance to discuss my results and conclusions with each of them.

At the time, I had the highest z source being used for cosmological studies, 3C 239 at a z of 1.79; a decade later, this is still the highest z RG or SN being used for cosmological studies.

A month later the SN groups announced the acceleration of the universe at the 1998 UCLA Dark Matter in the Universe conference.

The results indicated that in a standard model in which General Relativity is adopted as the correct theory of gravity, and the universe had two components, non-relativistic matter & a cosmological constant, and space curvature is included, the universe is accelerating today.

Later it became clear that these two completely independent methods, powerful radio galaxies and type Ia supernovae, based on totally different types of sources and source physics, give very similar results.

This suggested that neither method was plagued by unknown systematic errors.

Model-independent analyses now confirm that the expansion of the universe is accelerating at the current epoch, independent of the contents of the universe, and of space curvature.

The Radio Galaxy Method

The Sample:

We consider a subset of FRII radio sources

Leahy & Williams (1984) FRII-Type I (called FRIIb sources)

Leahy, Muxlow, & Stephens (1989): most powerful FRII RG, $P_r(178MHz) \geq 3 \times 10^{26}\, h^{-2}$ W/Hz/sr (about 10 x classical FRI/FRII).

→ sources have very regular bridge structure

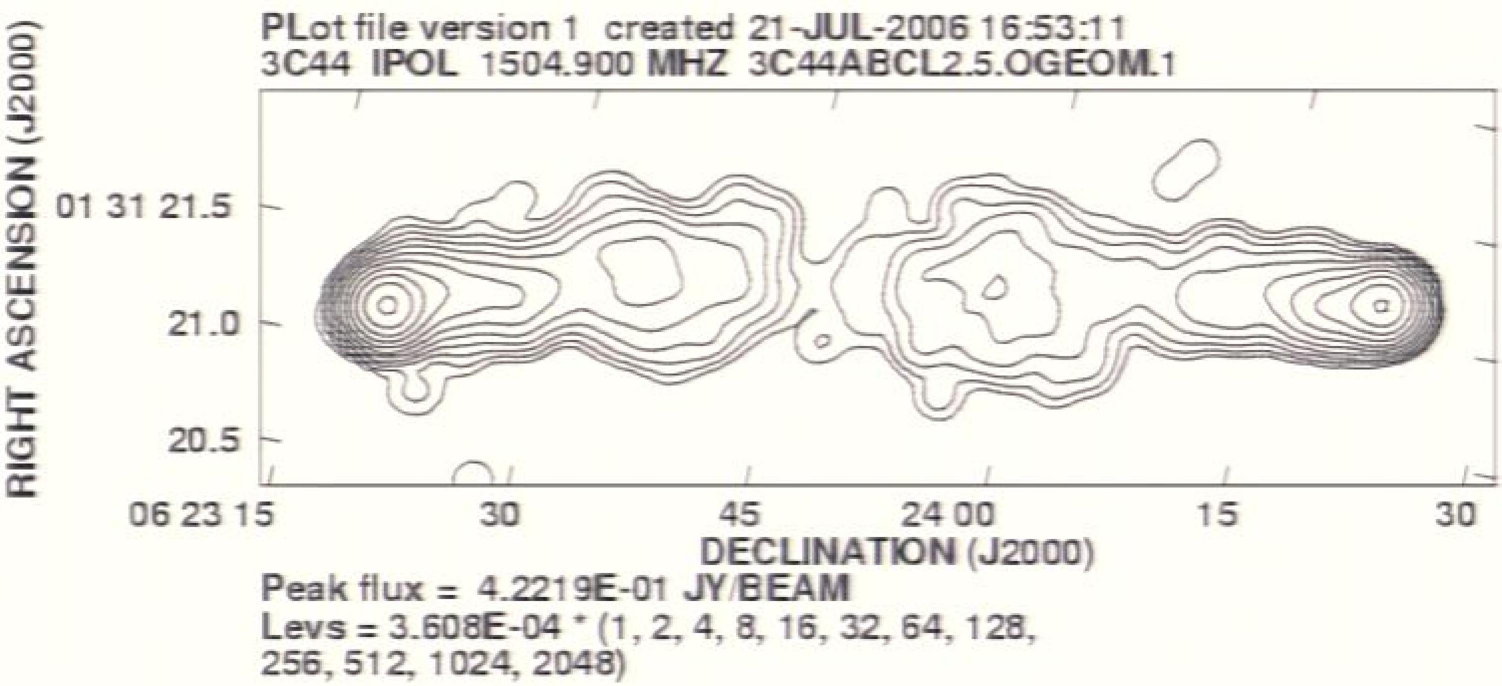
→ rate of growth well into supersonic regime

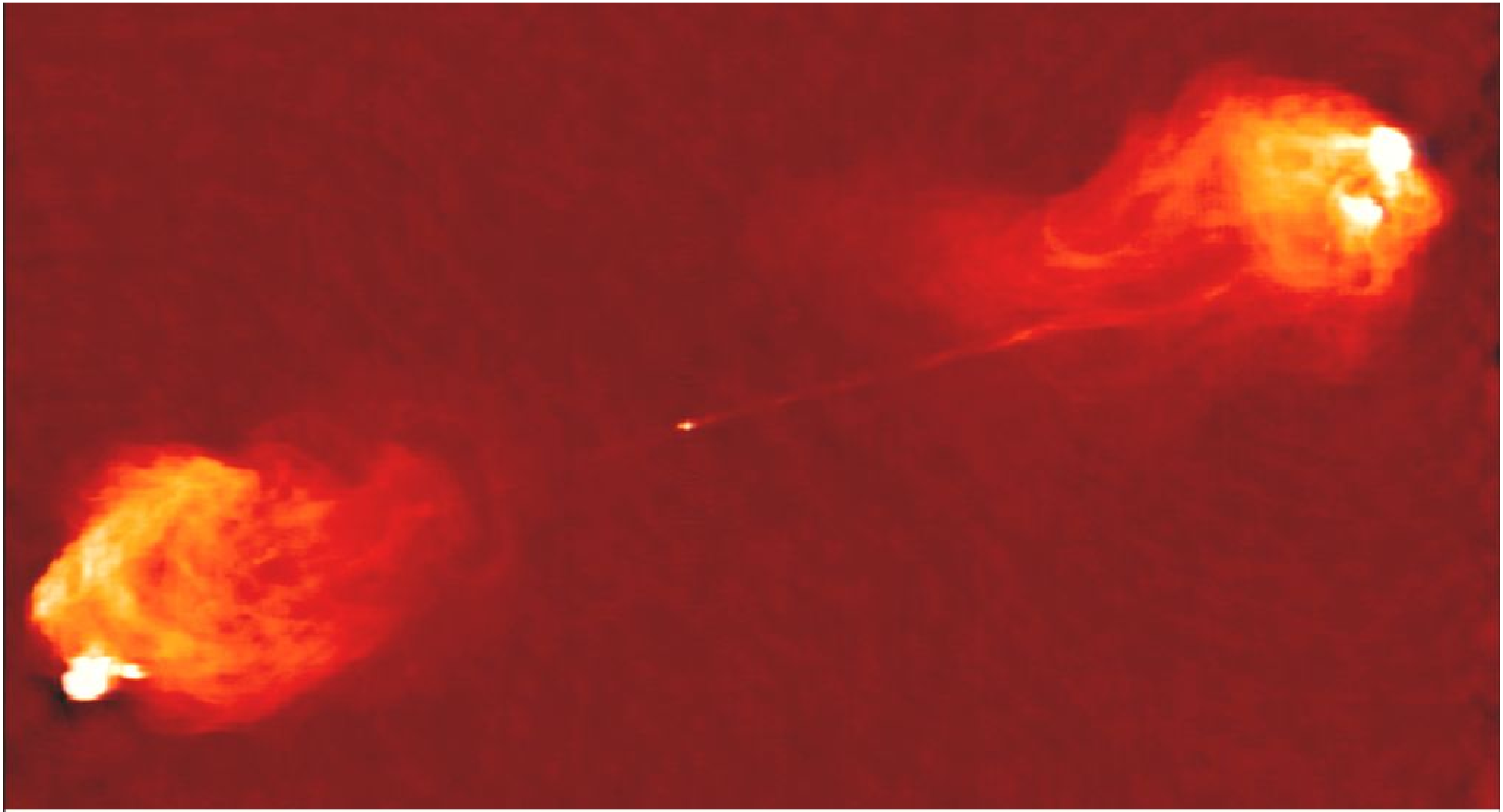
→ equations of strong shock physics apply & negligible backflow in bridge (LMS89).

→ Form a very homogenous population

& RG (not RLQ) to minimize projection effects.

For example, here is the 1.5 GHz image of 3C 44

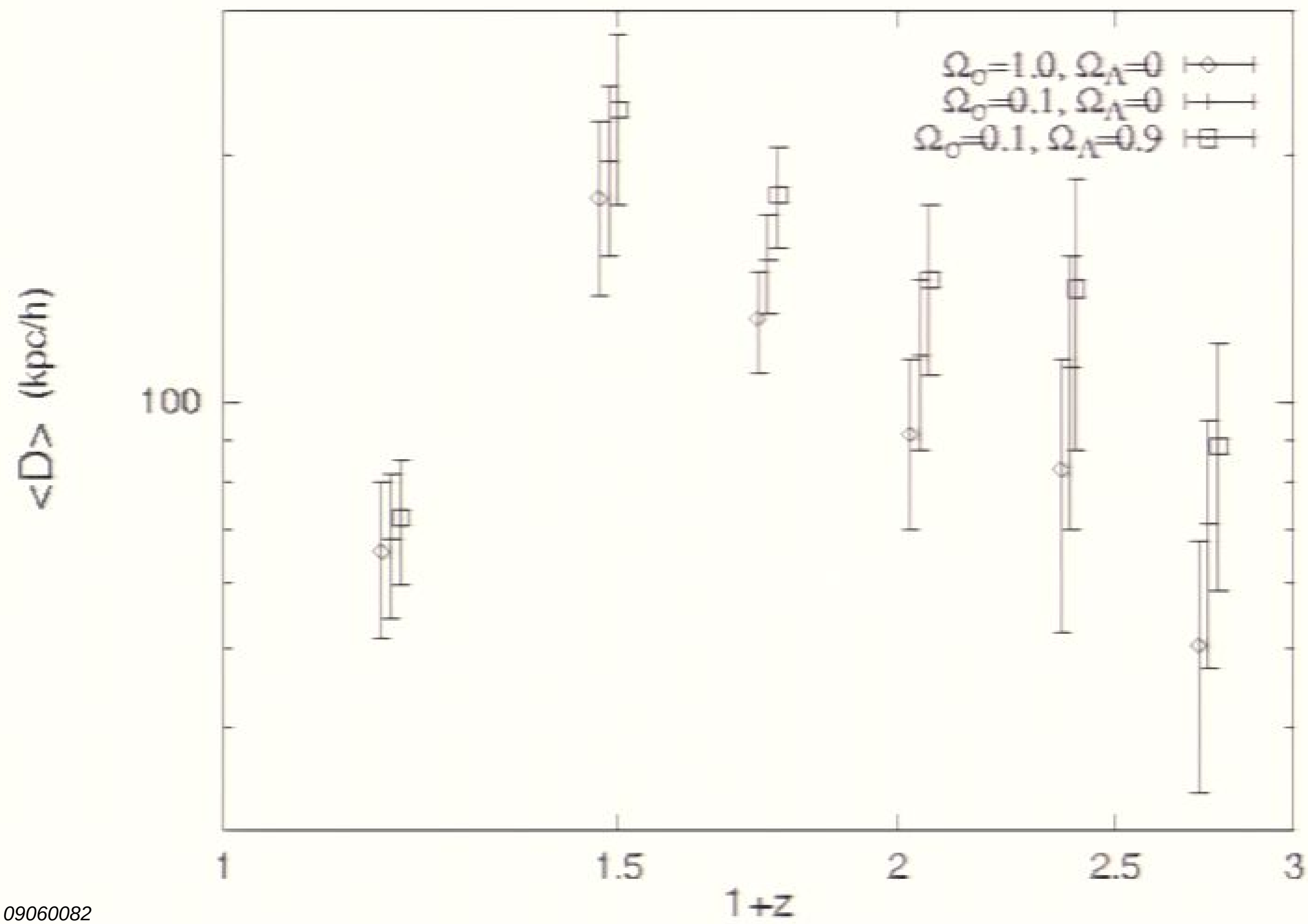


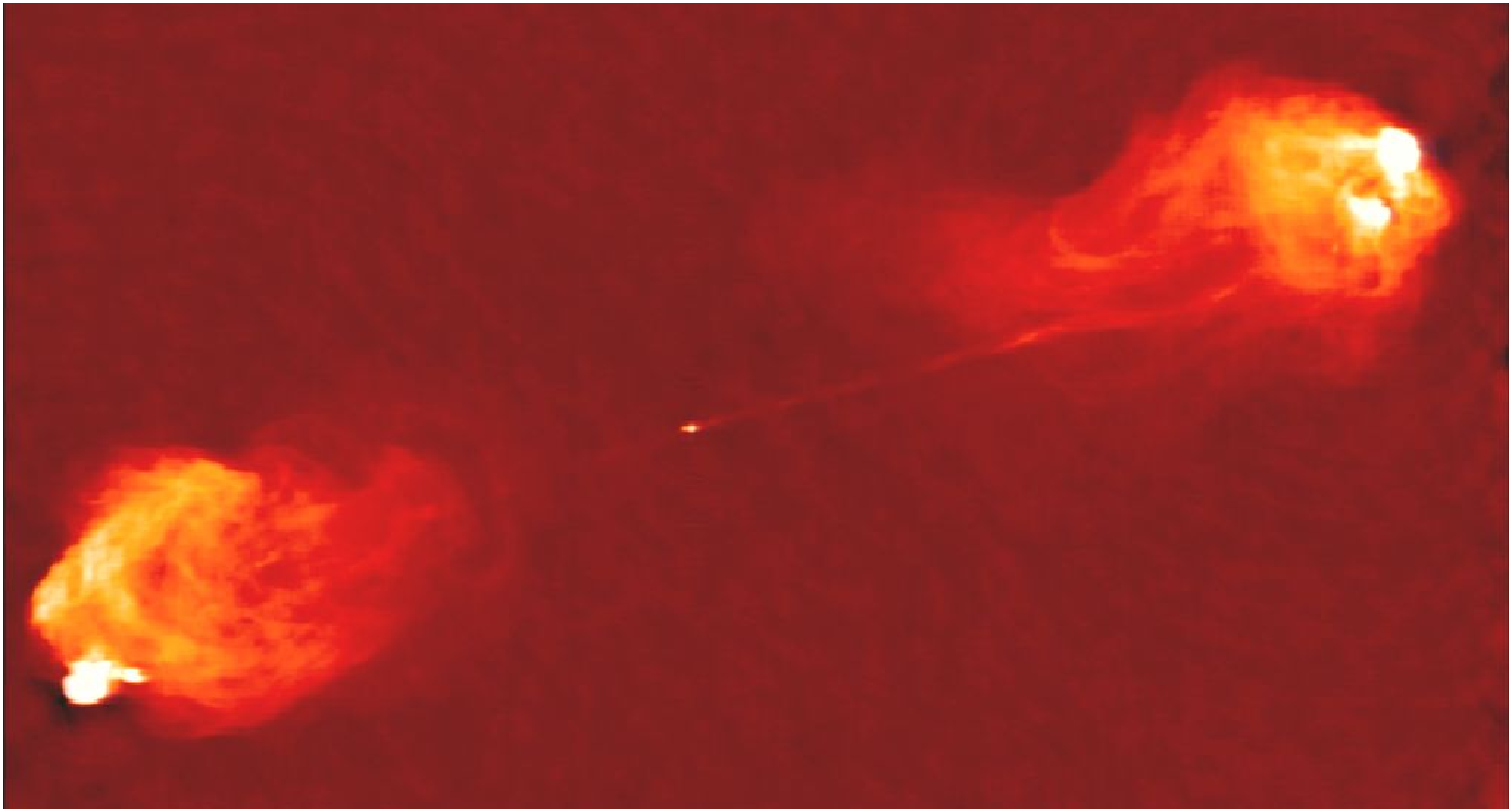


FRIIb Radio Galaxy

<D> for the parent population of 70 3C Radio Galaxies with 178 MHz powers > 3 h^{-2} x 10^{26} W/Hz/sr

<D> is defined using the largest linear size





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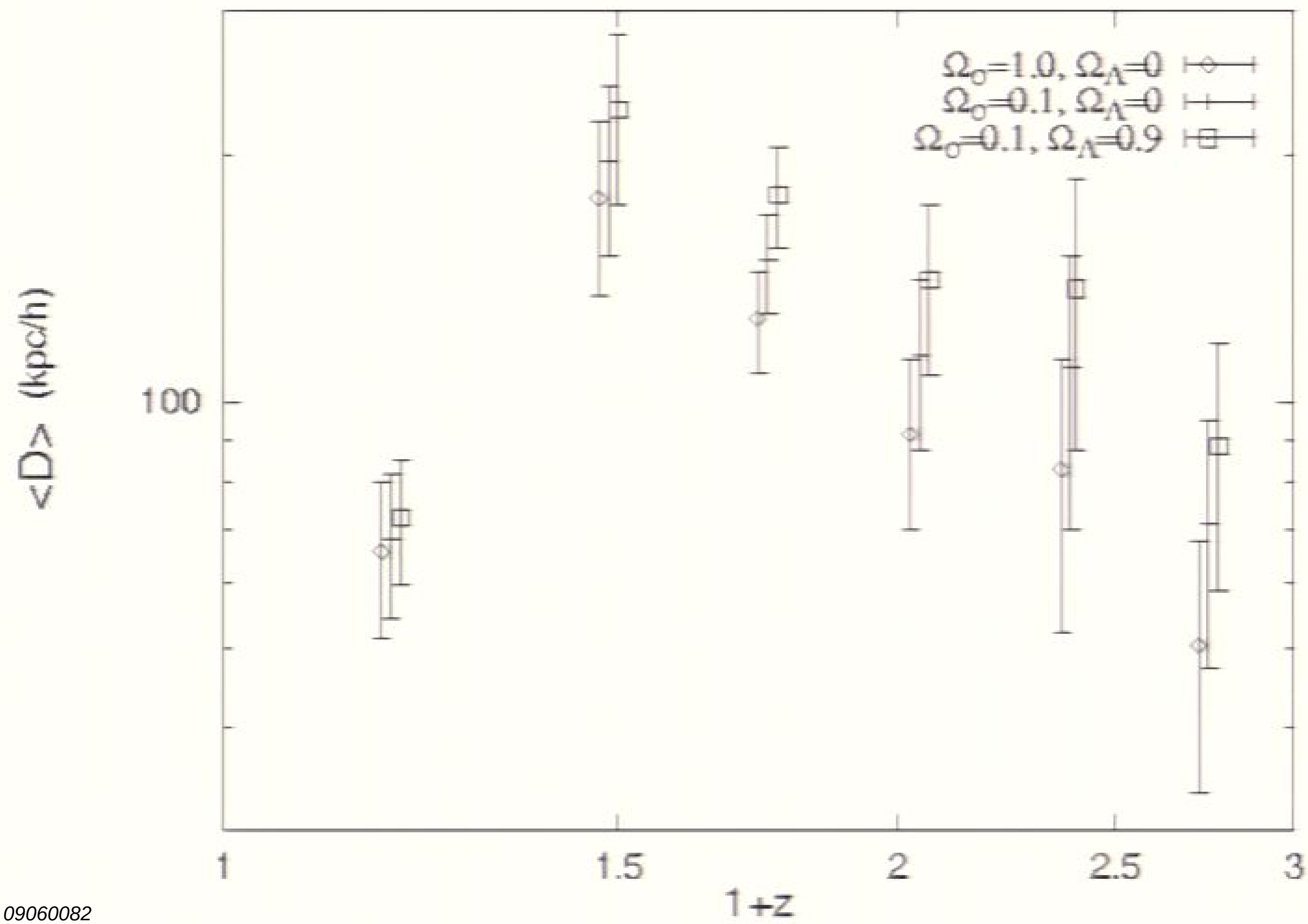
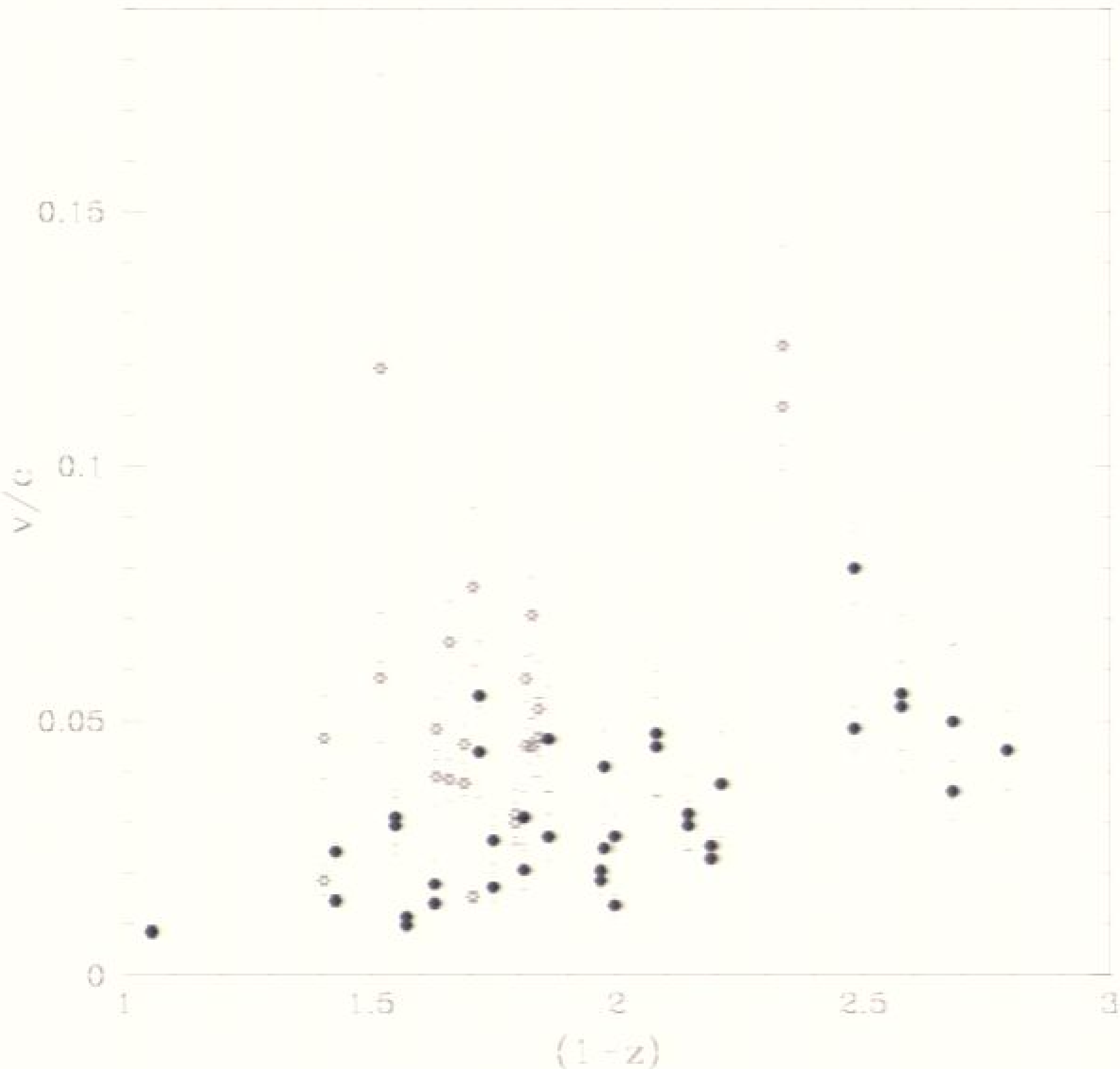


The overall rate of growth of each side of each source



The source sizes decrease systematically with z, but rate of growth of sources do not decrease with z.

We find no statistically significant correlation of v with z.

The original 20 sources are shown as solid circles, and the 11 new sources are shown as open stars.

From O'Dea et al. ('09)

Interesting and unexpected that <D> has a small dispersion at a given z and is decreasing with z for $z \geq 0.5$; source v do not decrease with z.

The average size of a given source, D_*, should mirror that of the parent population at that z, so expect that $D_* \sim \langle D \rangle$.

Comparing the properties of individual sources, D_*, with those of parent population, <D>, minimizes the role of selection effects.

The average size of a given source is $D_* \sim v\, t_*$

t_* = total outflow lifetime (often taken to be constant as expected for an Eddington limited system)

Generalize the relationship between t_* & L_j to be $t_* \sim L_j^{-\beta/3}$ (Daly '94)

For an Eddington limited system, $\beta = 0$, which is a special case of this more general relationship. Other paths lead to this relation.

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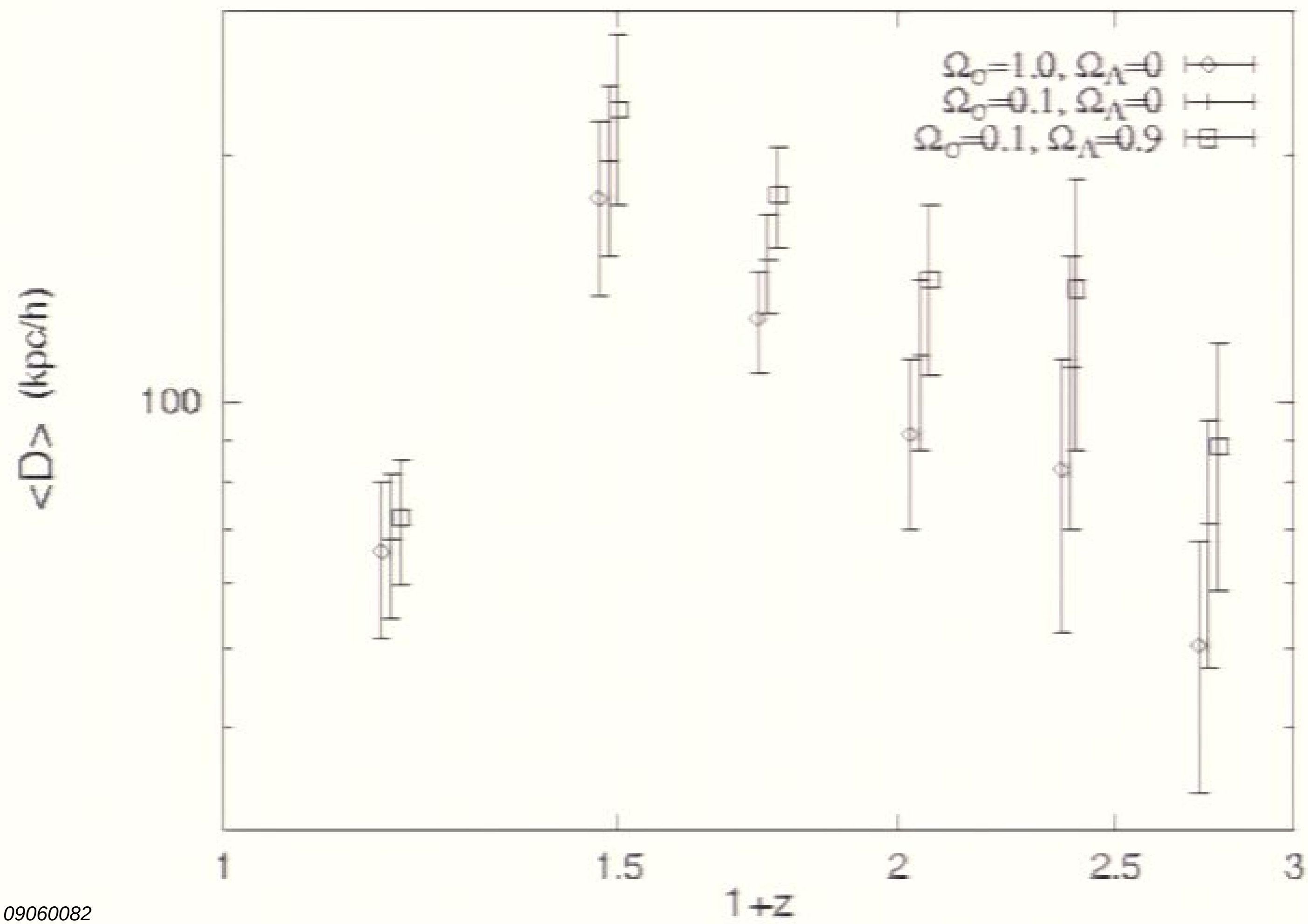

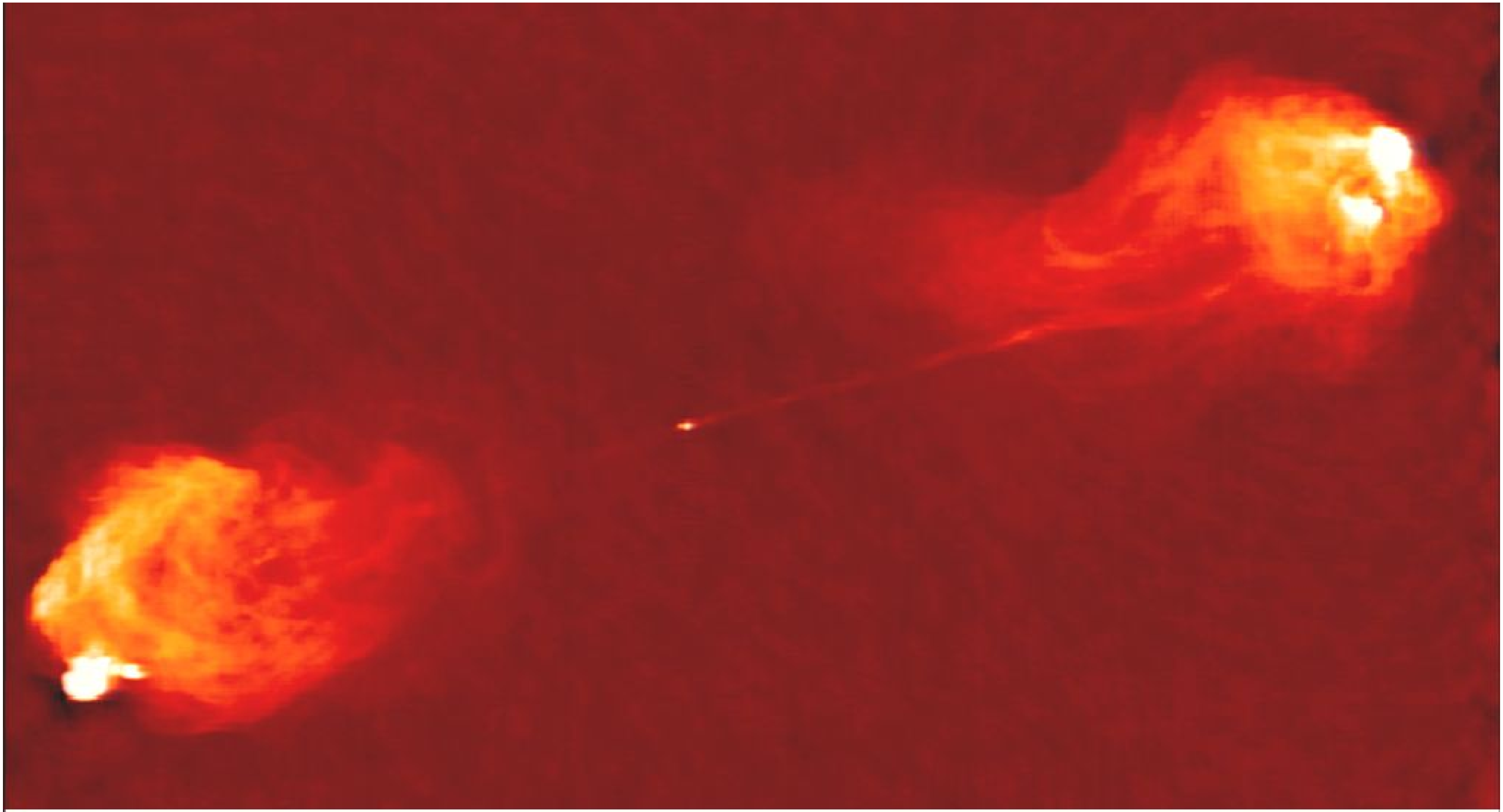

FRIIb Radio Galaxy

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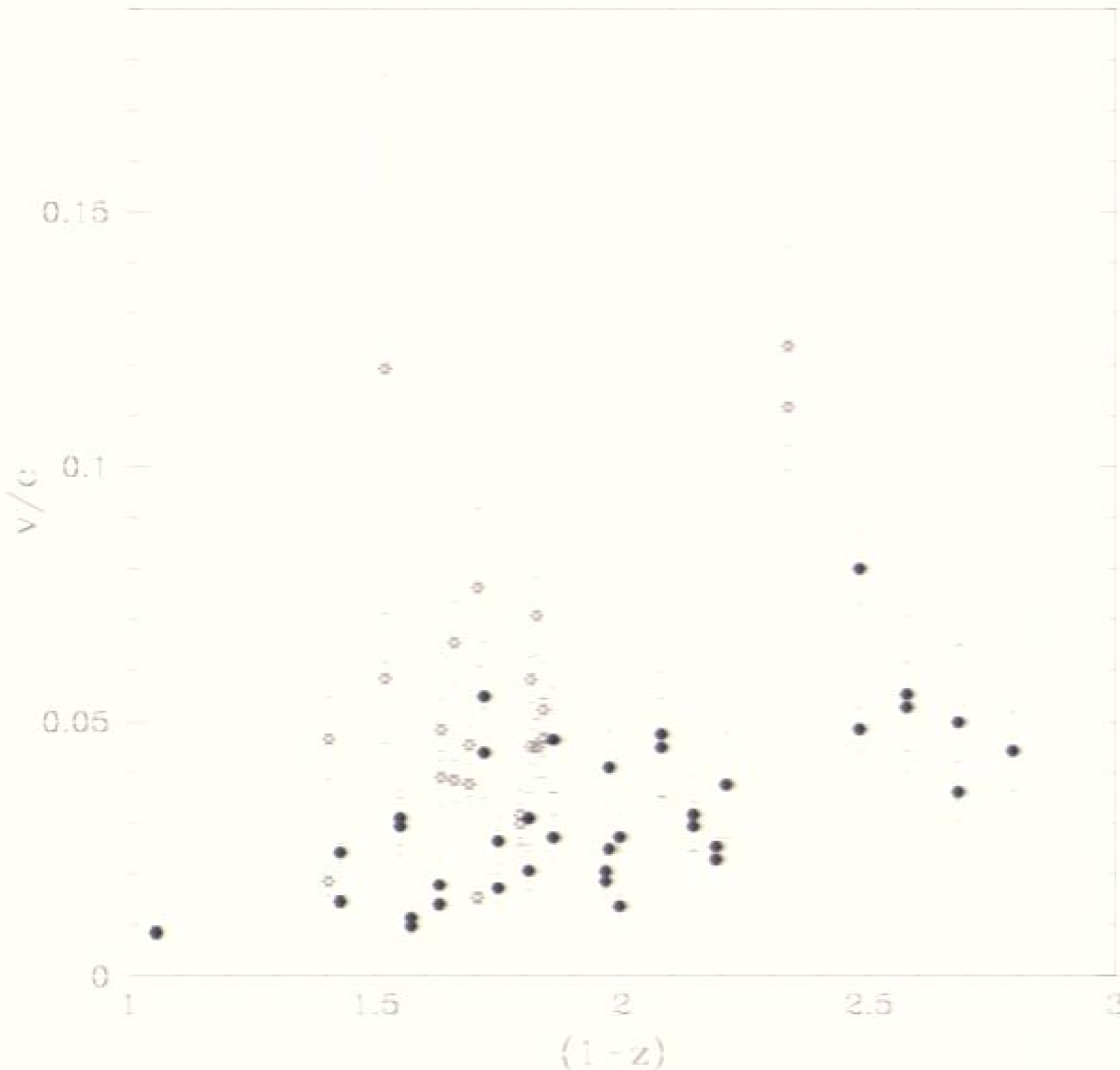

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Generalize the relationship between t_* & L_j to be $t_* \sim L_j^{-\beta/3}$ (Daly '94)

For an Eddington limited system, $\beta = 0$, which is a special case of this more general relationship. Other paths lead to this relation.

Thus, $D_* = v\,t_* \sim v\,L_j^{-\beta/3}$

$L_j \sim v\,a^2\,P$ (from strong shock physics; applied across the leading edge)

So $D_* \sim v^{1-\beta/3}\,(a^2\,P)^{-\beta/3}$ [has one model parameter]

(could also view as purely empirical relation)

This determination of the average size of a given source depends upon the model parameter β and the coordinate distance $(a_o r)$ to the source, going roughly as $(a_o r)^{-0.6}$ for our best fit β of 1.5 (after accounting for v, a, and P)

Comparing <D>, which goes as $(a_o r)$, with D_* allows a determination of β and cosmological parameters

→ require $\langle D\rangle/D_* = \kappa$ and solve for $(a_o r)$ and β; roughly **κ** $\sim \text{obs}\cdot(a_o r)^{1.6}$

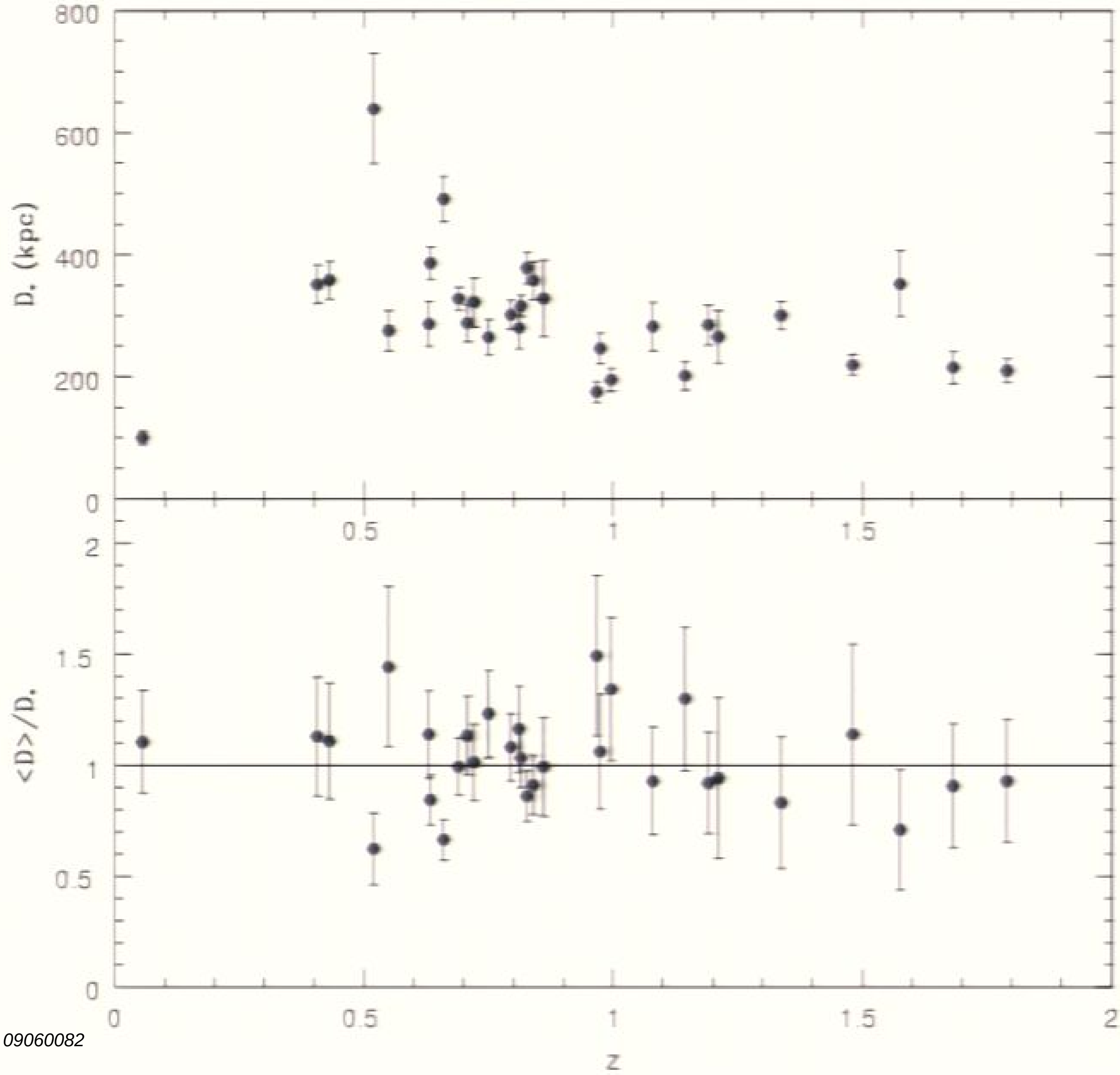
We obtain D_* for each of the 30 sources studied here and compare it with <D> for the parent population of 70 sources to solve for best fit values of β & cosm.

The method accounts for variations in L_j from source to source and variations in source environments (i.e. we do not make any assumptions about n_a)

We do not assume that any properties of the sources are constant, or pre-determined.

Only assumptions: $t_* \sim L_j^{-\beta/3}$, eqn. of strong shock physics apply, + v & L_j const for a given source over the source lifetime, which are consistent with the observations.

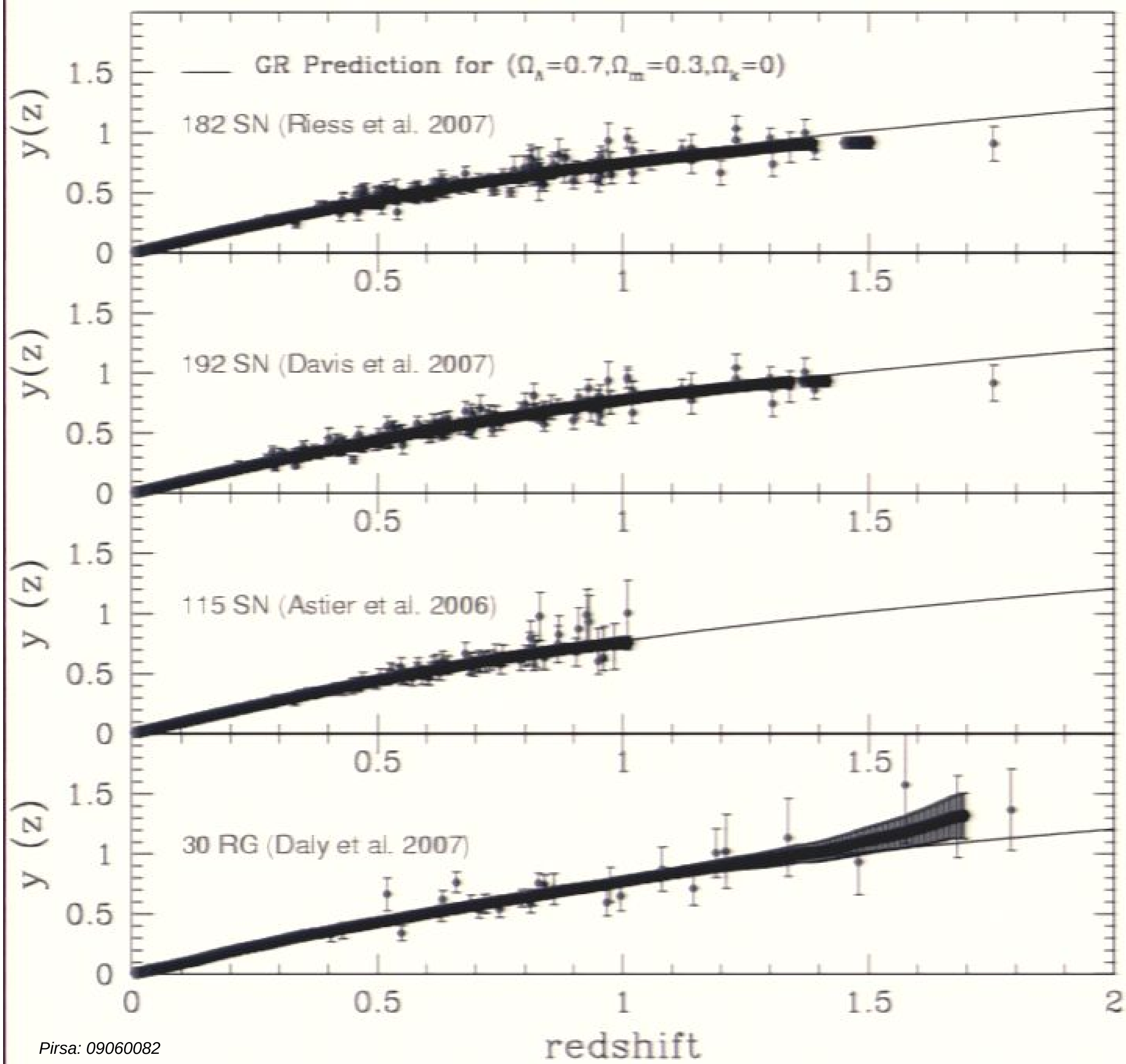
$D_* \sim v^{1-\beta/3} (a^2 P)^{-\beta/3} \sim v^{1/2} (a^2 P)^{-1/2}$ for $\beta = 1.5$



D_* shown for best fit parameters $\beta = 1.5 \pm 0.15$, $\Omega_m = 0.3 \pm 0.1$ and $w = -1.1 \pm 0.3$, obtained in a quintessence model.

The χ^2_r of the fit is about 1 (1.03)

From Daly et al. (2009)

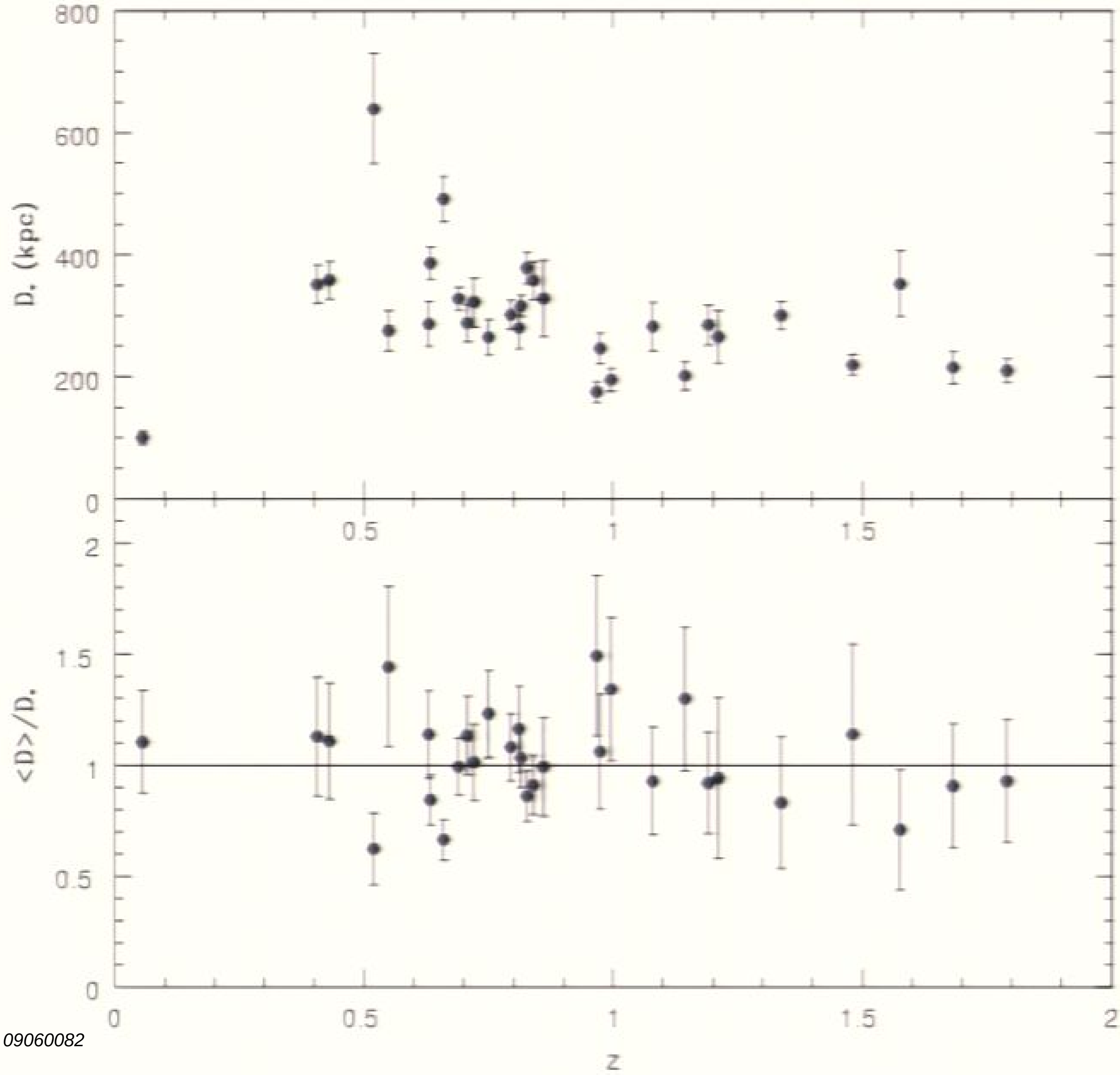


The values of ⟨D⟩/D* are used to solve for the coordinate distance y without specifying a cosmological model (y is equivalent to a luminosity dist.)

There is very good agreement between SN and RG

(from Daly et al. 2008)

$D_* \sim v^{1-\beta/3} (a^2 P)^{-\beta/3} \sim v^{1/2} (a^2 P)^{-1/2}$ for $\beta = 1.5$



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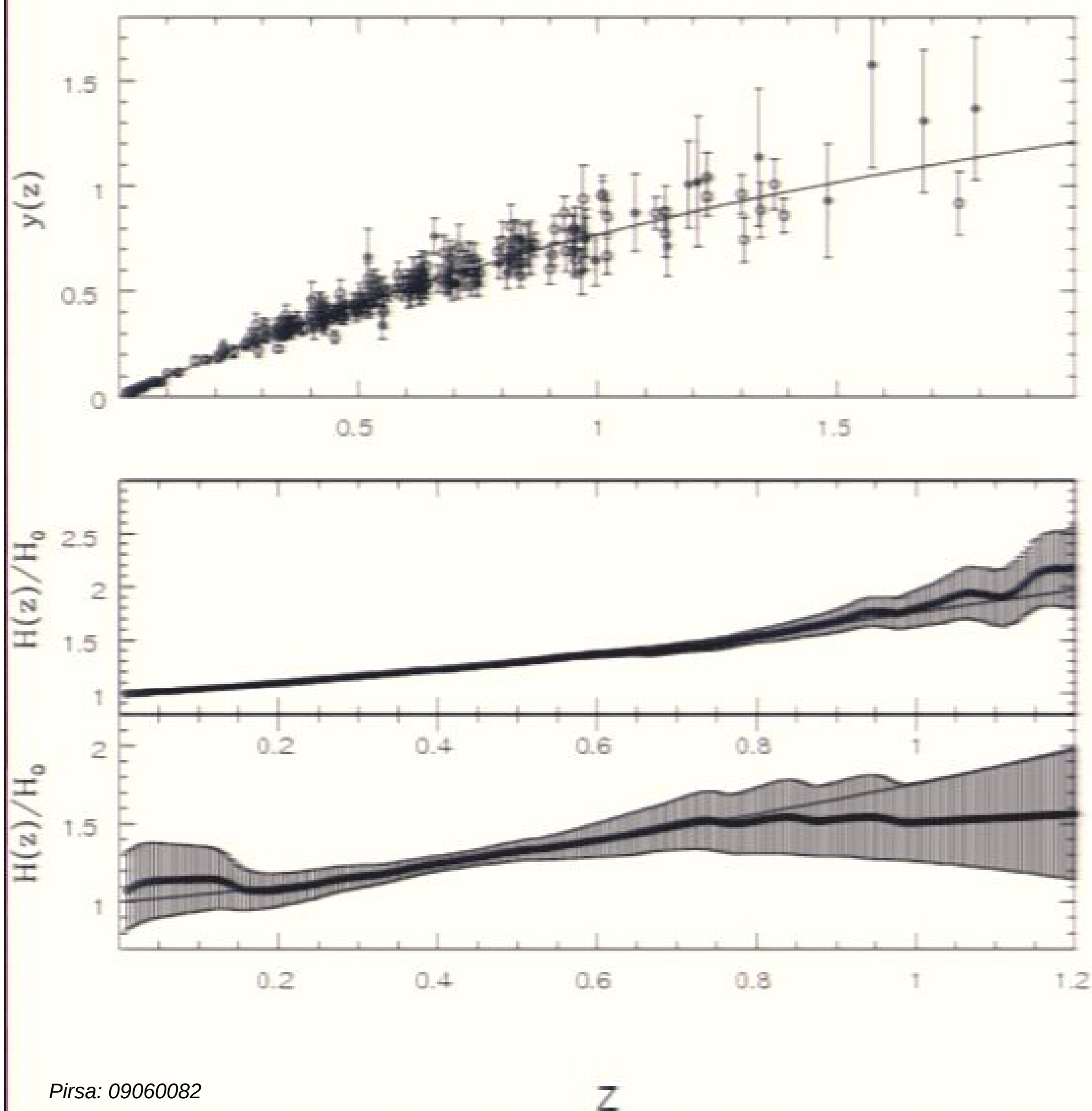
The χ^2_r of the fit is about 1 (1.03)

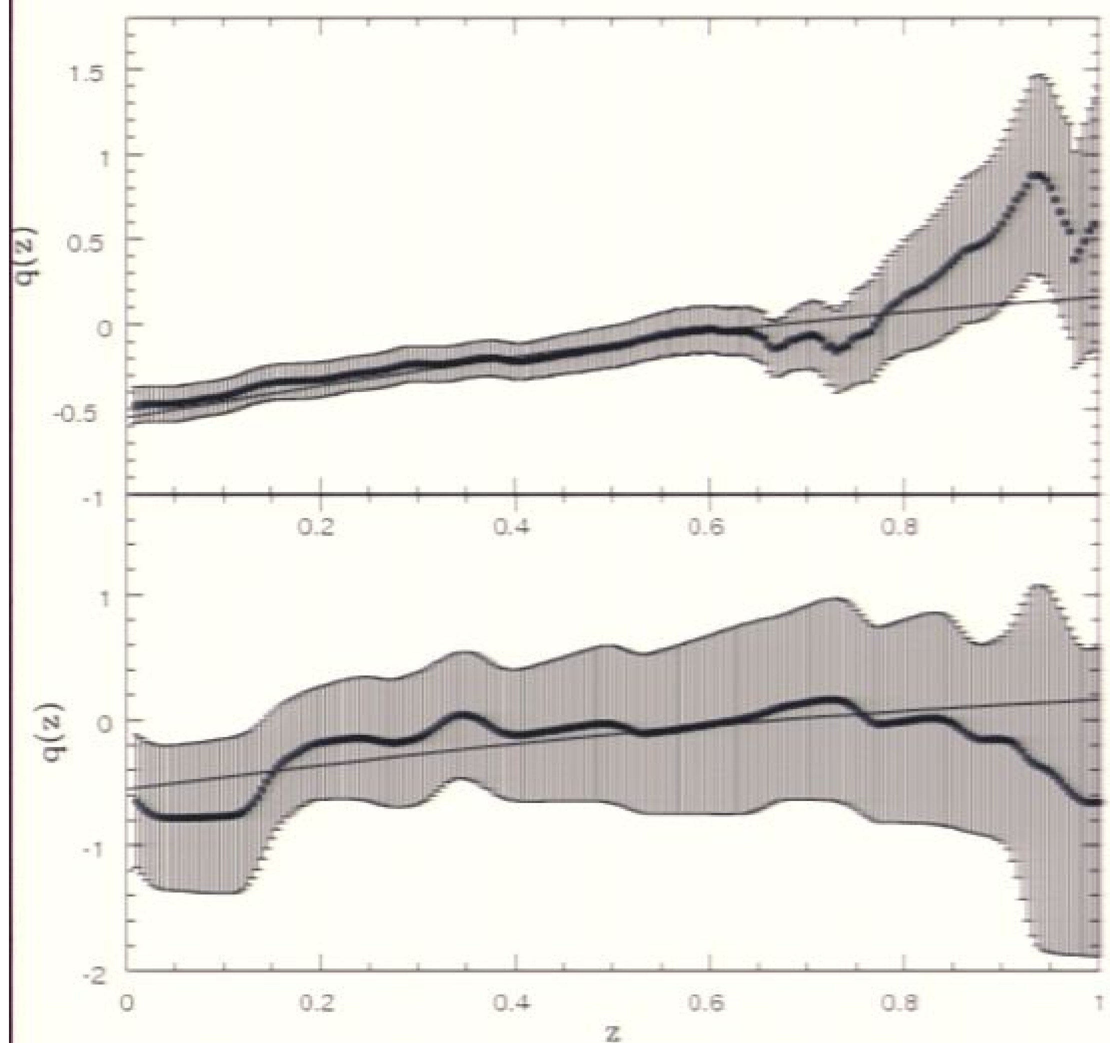
From Daly et al. (2009)

Model-Independent Determinations of y, H, & q
(from Daly et al. 2008)



The coordinate distances, y, for RG and SN can be used to obtain H(z) and q(z) without having to specify a particular model (e.g. quintessence model); using a strictly kinematic approach. Shown here for 192SN of Davis et al. (2007) & 30 RG of Daly et al. (2008). For comparison the LCDM line for Ω_m = 0.3 is shown. Data are well described by LCDM model.

Model-Independent Determination of $q(z)$; q_o depends only upon FRW metric; independent of k (from Daly et al. 2008)



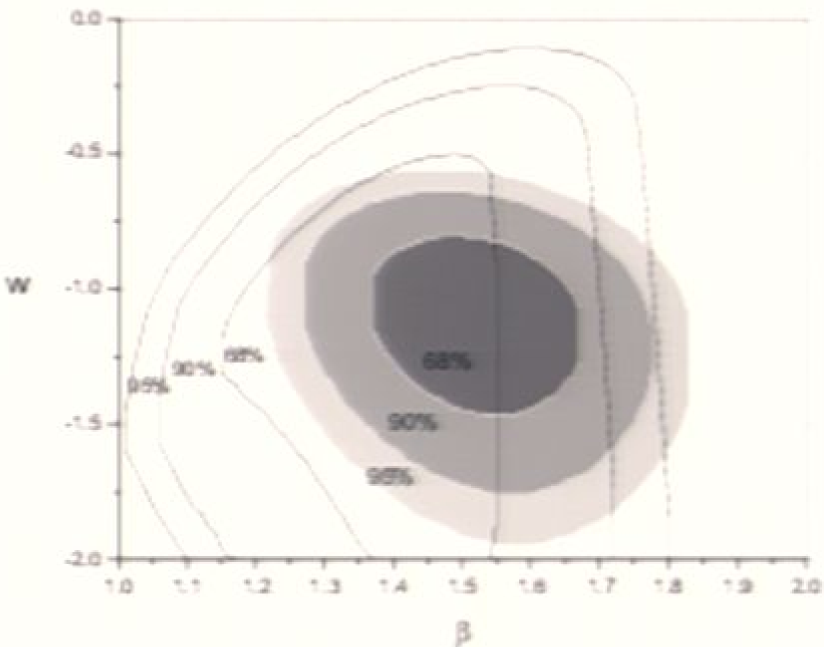
The data can be used to obtain $q(z)$ in a completely model-independent way, using a strictly kinematic approach. Shown here for 192 SN & 30 RG; for SN find $q_o = -0.48 \pm 0.11$ & $z_T = 0.8 \pm 0.2$;

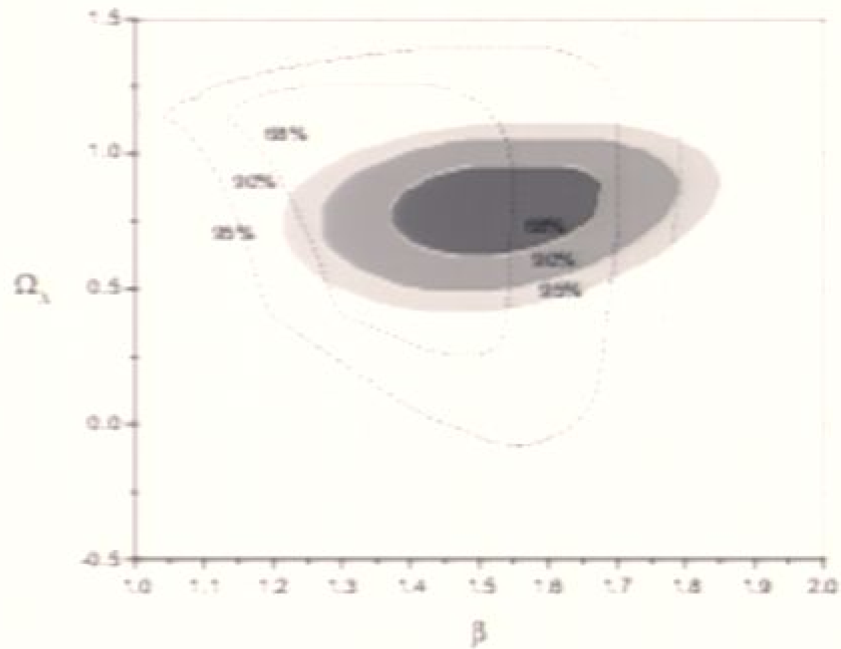
for 30 RG alone $q_o = -0.65 \pm 0.5$;

Solid line is LCDM with $\Omega_m = 0.3$

Good agreement between RG & SN

The RG model parameter β in a quintessence model for RG alone and combined 30 RG + 192 SN sample. The best fit value is $\beta = 1.5 \pm 0.15$ and there is no covariance of β with w or Ω_Λ; very similar values obtained in other models (from Daly et al. 2009).





What does our best fit value of $\beta = 1.5 \pm 0.15$ suggest about the production of relativistic jets from the AGN?

In a standard magnetic braking model in which jets are produced by extracting the spin energy of a rotating massive black hole with spin angular momentum per unit mass a, gravitational radius m, black hole mass M, and magnetic field strength B, we have (Blandford 1990):

$L_j = 10^{45} (a/m)^2 B_4^2 M_8^2$ erg/s $\sim (a/m)^2 B^2 M^2$

$E_* = 5 \times 10^{61} (a/m)^2 M_8$ erg $\sim (a/m)^2 M$

In our parameterization, $E_* = L_j t_* \sim L_j^{1-\beta/3}$, which implies that

$B \sim M^{(2\beta-3)/2(3-\beta)} (a/m)^{\beta/(3-\beta)} \sim (a/m)$ for $\beta = 1.5$

Our empirical determination of β implies that $\beta = 1.5 \pm 0.15$

This very special value of β indicates that B depends only upon (a/m) and does not depend explicitly on the black hole mass M.

It suggests that the relativistic outflow is triggered when the magnetic field strength reaches this limiting or maximum value, and is ultimately the cause of the decrease in <D> for this type of radio source.

The outflows are clearly not Eddington limited, since $\beta = 0$ is ruled out at 10σ.

Mini-Summary II: the Radio Galaxy Method

With the very simple relations, $D_* = v\, t_*$, $t_* \sim L^{-\beta/3}$, and applying the strong shock relation $L \sim v\, a^2\, P$ near the forward region of the shock, we can solve for the model parameter β and cosmological parameters; no assumptions are made about the source environments or beam powers.

The cosmological parameters we determine are in very good agreement with those obtained by independent methods, such as the type Ia SN method.

The model parameter β can be analyzed in a standard magnetic braking model, and the value we obtain is a very special value, $\beta = 1.5 \pm 0.15$, which implies that $B \sim (a/m)$ for each source.

This leads to a picture in which the collimated outflow is generated when $B \sim (a/m)$, producing jets with roughly constant L_j over their lifetime t_*, and $t_* \sim L_j^{-1/2}$, $t_* \sim E_*^{-1}$, and $L_j \sim E^2$.

The outflows are unrelated to the Eddington luminosity, and have beam powers well below L_{EDD} ; there is no need to require that each source produces an outflow for the same total time.

More coming soon….we have VLA data for another 13 sources

The sources may be used to study the spins of supermassive black holes.

The spin energy of a BH, E_*, is related to the BH mass, M, and spin $j = a/m$,
[j is defined in terms of the spin angular momentum S, $a = S/(Mc)$, and the gravitational radius $m = GM/c^2$]:

$$E_* = Mc^2 \left[1 - (0.5 \{1+[1-j^2]^{1/2}\})^{1/2} \right]$$

Solving this for j, and setting $r = E_*/Mc^2$,

$$j = 2 \{2r - 5r^2 + 4r^3 - r^4 \}^{1/2}$$

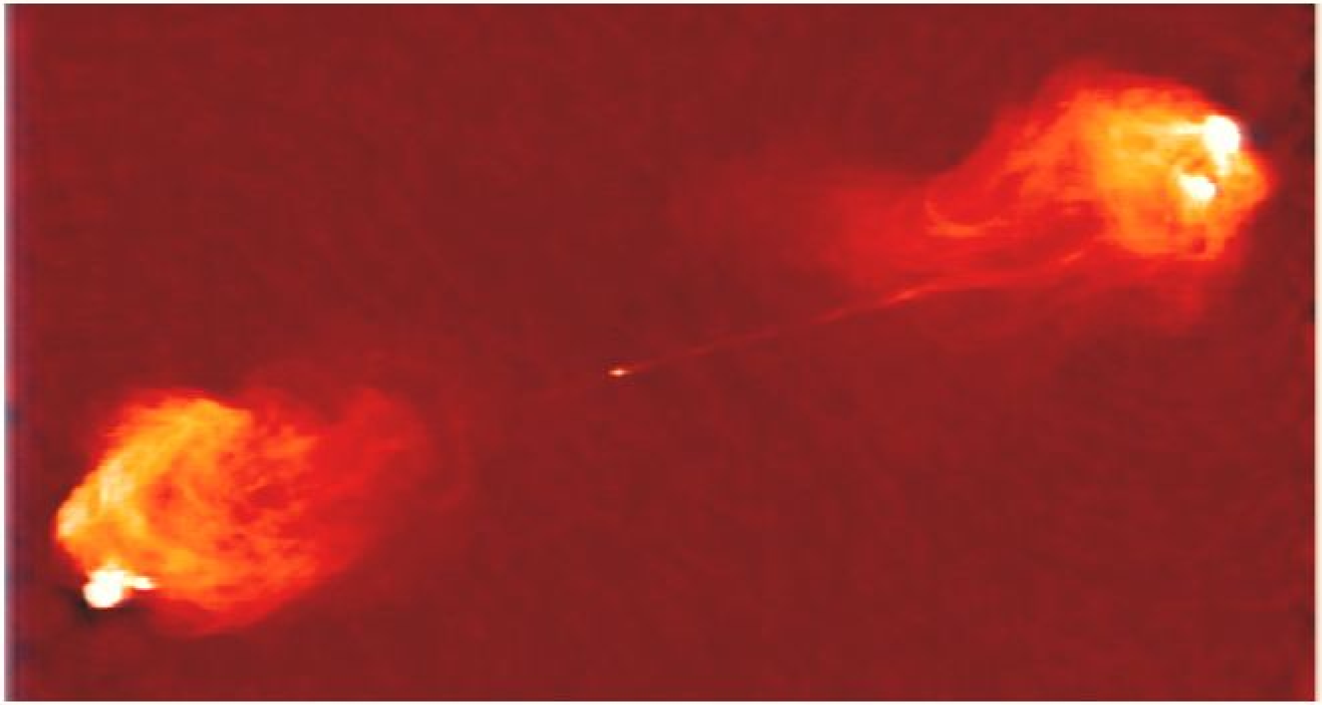
If extraction of spin energy from a SMBH powers an outflow (e.g. the BZ model), the energy of the outflow may be taken as a lower bound on the initial black hole spin energy (D09a).

$$j = 2\{2r - 5r^2 + 4r^3 - r^4\}^{1/2}$$

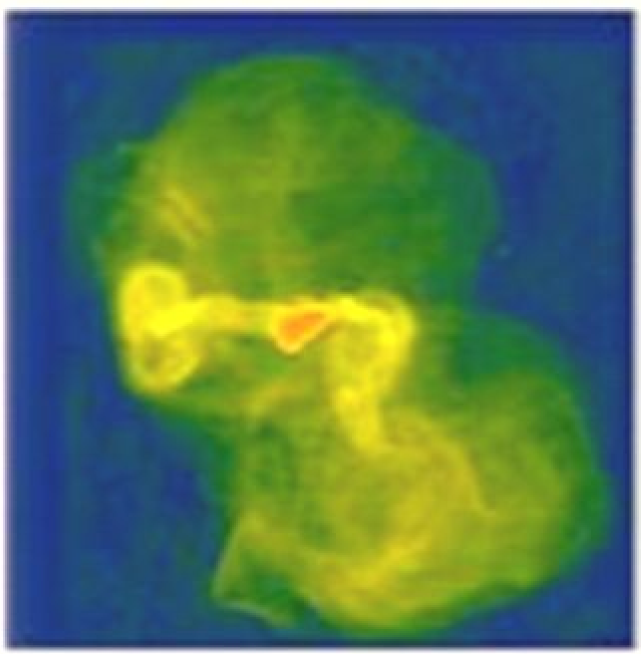
Where $r = E_*/Mc^2$

If sources can be identified for which E_* can be bounded from below, and M is known, then j can be bounded from below for these systems.

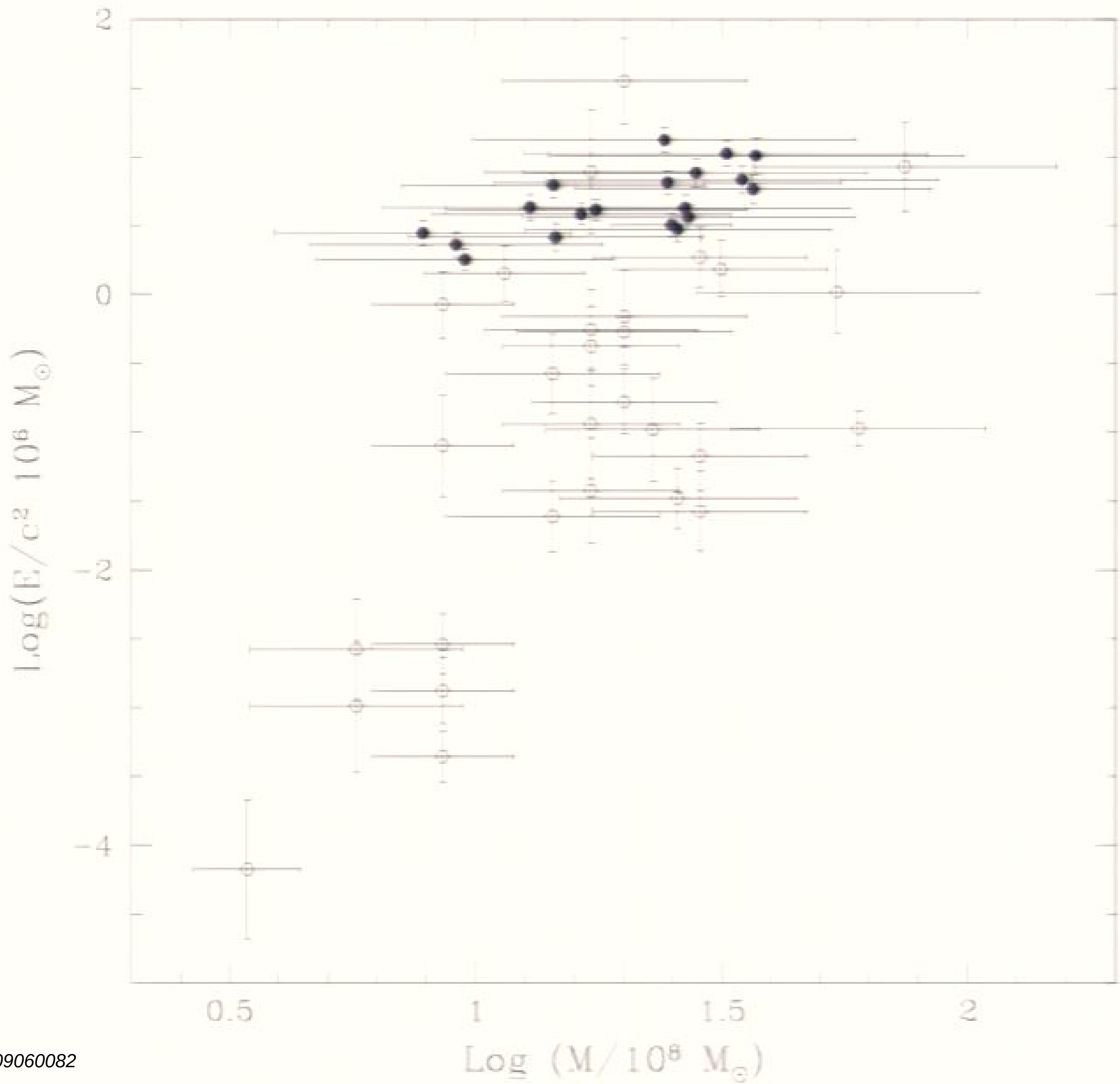
Daly (2009a) identified a sample of 19 very powerful classical double radio galaxies and a sample of 29 central dominant galaxies (most of which have FRI radio structure) for which both E_* and M have been estimated. These sample were used to place a lower bound on j. The 19 FRII sources are from O'Dea et al. (2009), and the radio sources associated with CD galaxies are from Rafferty et al. (2006); masses for the systems were obtained from Tadhunter et al. (2003), McLure et al. (2004, 2006), McLure (2008), and Rafferty et al. (2006).



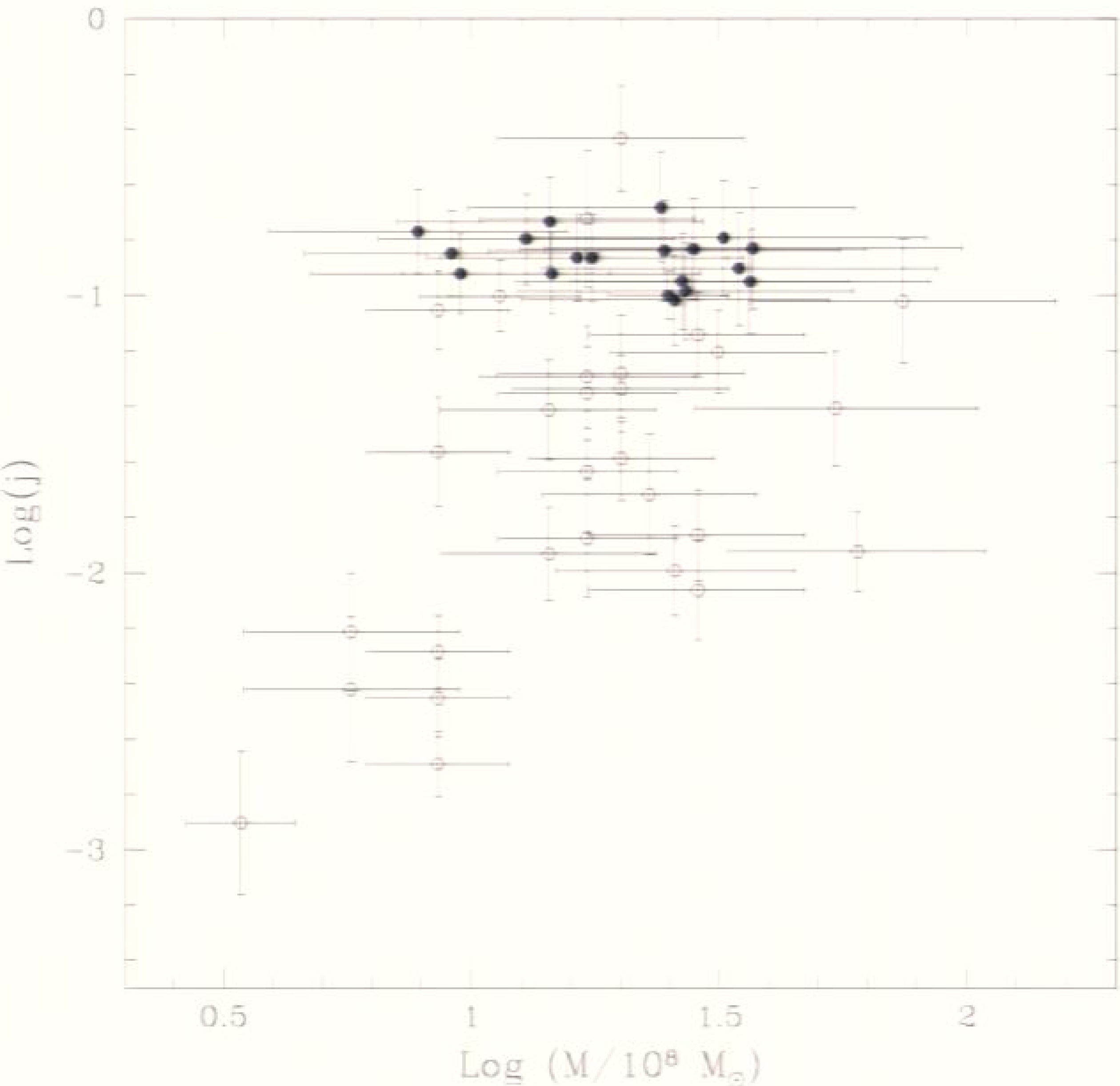
Cygnus A



M87



FRII radio galaxies are indicated by solid circles, and radio sources associated with CD galaxies are indicated by open circles; from Daly (2009a).



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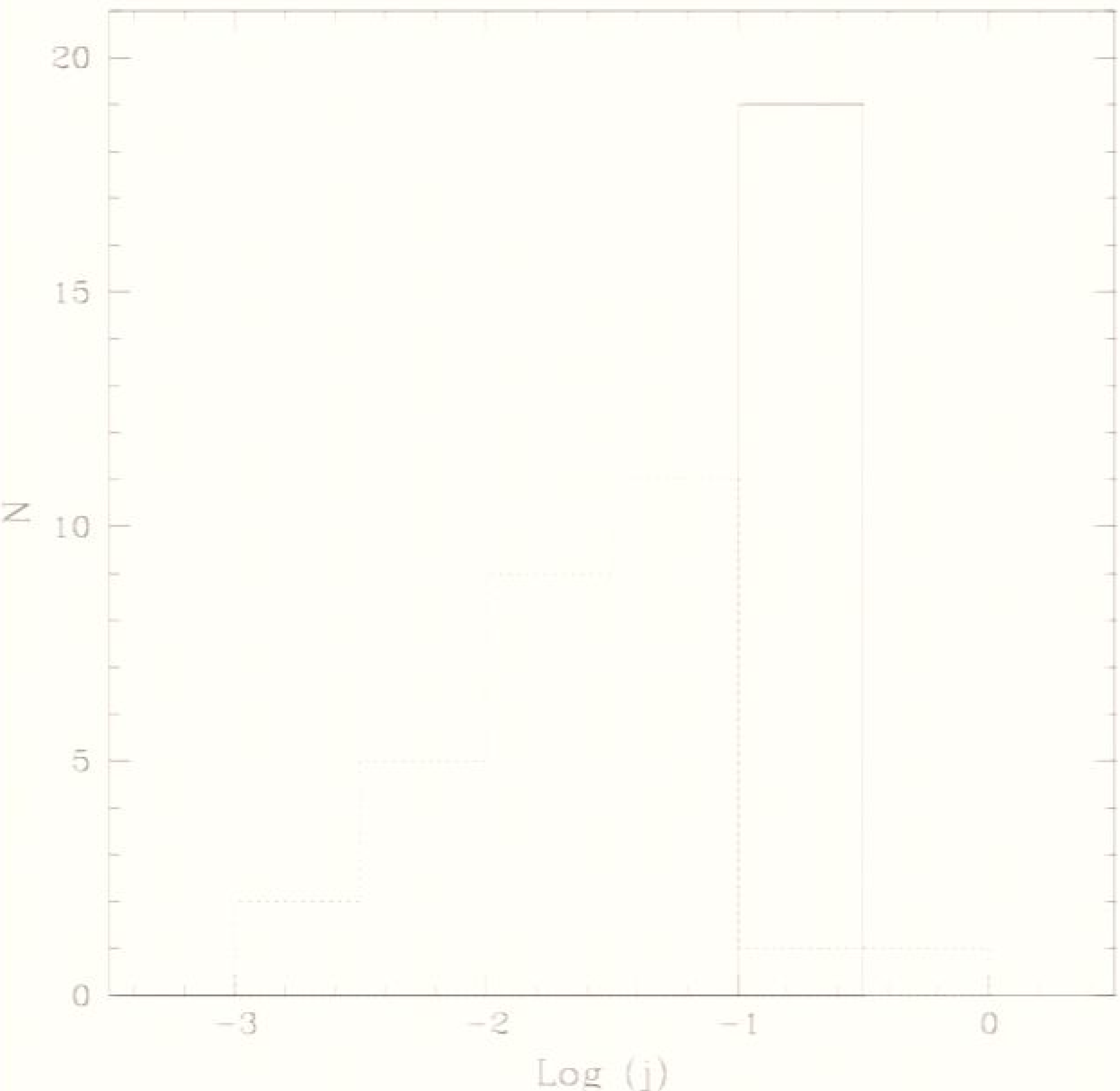


FRII radio galaxies are indicated by solid lines, and radio sources associated with CD galaxies are indicated by dotted lines; from Daly (1990a).

The weighted mean value of the lower bound on j for the powerful (FRII) radio galaxies studied is 0.12 ± 0.01. All of the sources have values of j consistent with this value; thus, the data indicate that r is the same for each of these RG ($r \approx 0.002$). This suggests that the outflow is triggered when a particular threshold is reached, that is, when the black hole system reaches a particular physical state. The values of j obtained are independent of z and P_r; it turns out that both E_* and M vary roughly as $(1+z)^2$, and that their ratio is constant.

Note that E_* obtained for these sources does not depend upon when they are observed; this is an estimate of the total energy that will be expelled by the BH through large-scale jets over the entire lifetime of the source, as discussed in detail by Daly et al. (2009) and O'Dea et al. (2009).

A wide range of values of r and j were obtained for the sample of 29 radio sources associated with CDGs. The values of j range from about 0.001 to 0.4. This may result from the fact that the energy E_* is the total energy associated with the extended radio source at the time it is observed.

It turns out that there is a second way that extended radio sources may be used to study spins of supermassive black holes (Daly 2009b). This can be done by combining the beam powers of sources with BH mass estimates.

The beam power, L_j, of a radio source may also be used to study the spin of the BH, assuming that the outflow is powered by the spin energy of the hole. This requires that a particular model for the energy extraction be specified. Daly (2009b) considered the models of Blandford & Znajek (1977) [the BZ model], and Meier (1999).

For the BZ model

$$L_j = (j^2 B^2 R^2 \omega^2 c)/32 \approx 2 \times 10^{43} j^2 M_8^2 B_4^2 \text{ erg/s}$$

Where B_4 is the poloidal field strength at the horizon in units of 10^4 G; M_8 is the BH mass in units of $10^8 M_s$;
R is the horizon, $R = (1+[1-j^2]^{0.5})GM/c^2 \approx 1.7\, GM/c^2$;
$\omega^2 = \Omega_F(\Omega_h - \Omega_F)/\Omega_h^2 = (0.5)^2$ [e.g. Blandford 1990].
As discussed by Daly (2009b), when values of M and L_j are known, the product jB can be studied.

The maximum value of j is one, and the magnetic field strength is not expected to exceed the "Eddington" field strength of $B_{EDD} \approx 6 \times 10^4 (M_8)^{-0.5}$ G.

Writing $b = B/B_{EDD}$, we expect that $b \leq 1$.

Since both $j \leq 1$, and $b \leq 1$, the product jb must also satisfy $jb \leq 1$.

Solving $L_j \approx 2 \times 10^{43} j^2 M_8^2 B_4^2$ erg/s for the product jB, we find

$$jb \approx 0.37 [L_{44}/M_8]^{1/2}$$

This product provides a lower bound on j and a lower bound on b; here L_{44} is the beam power in units of 10^{44} erg/s.

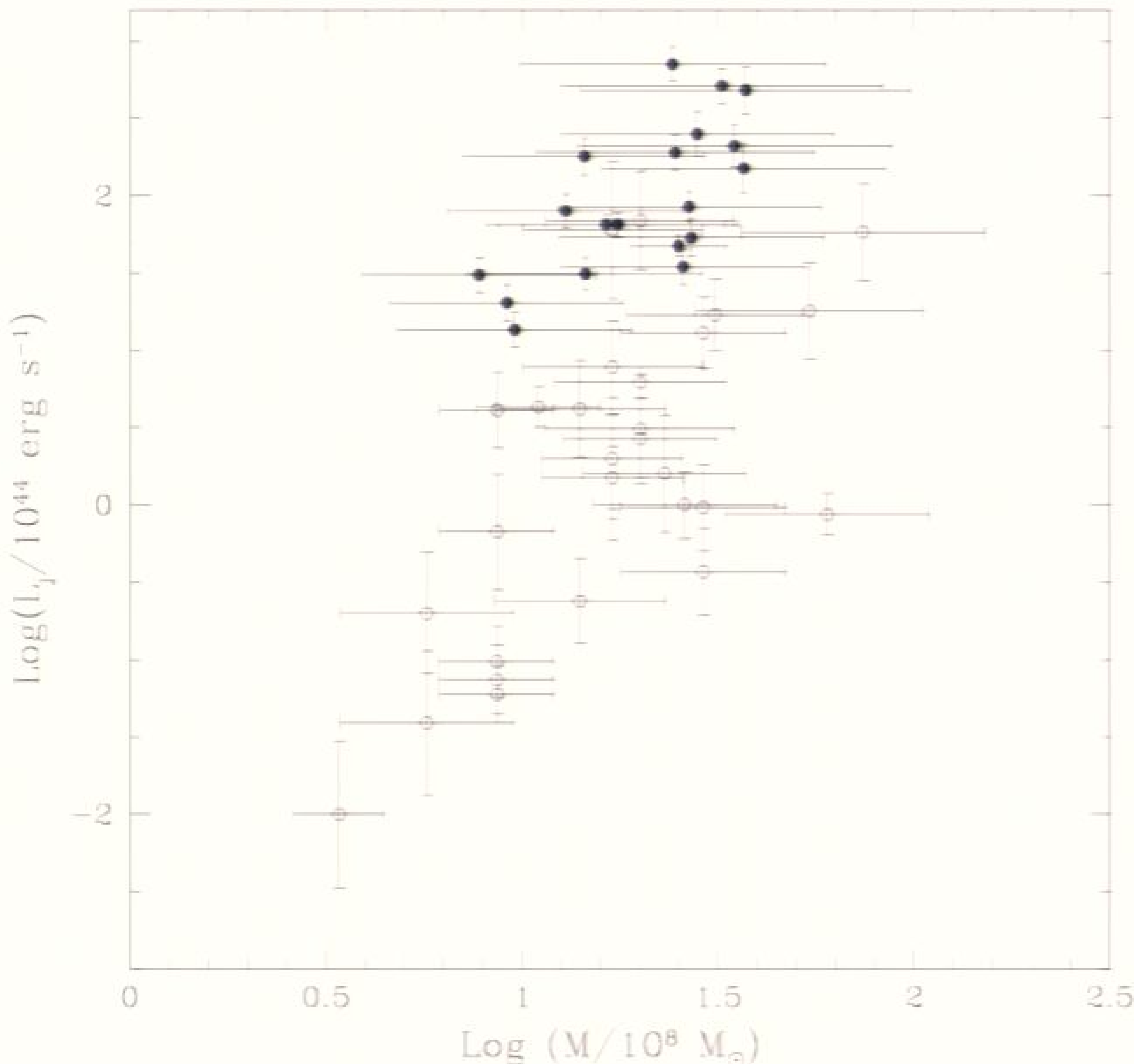
Values of the beam power L were obtained for 19 powerful FRII radio sources (O'Dea et al. 2009) and for 29 central dominant galaxies (Rafferty et al. 2006).

Values of the beam power L were obtained for 19 powerful FRII radio sources (O'Dea et al. 2009; Wan et al. 2000; Daly & Guerra 2002); BH masses for these systems were obtained from McLure et al. (2004, 2006), McLure (2008), and Tadhunter et al. (2003).

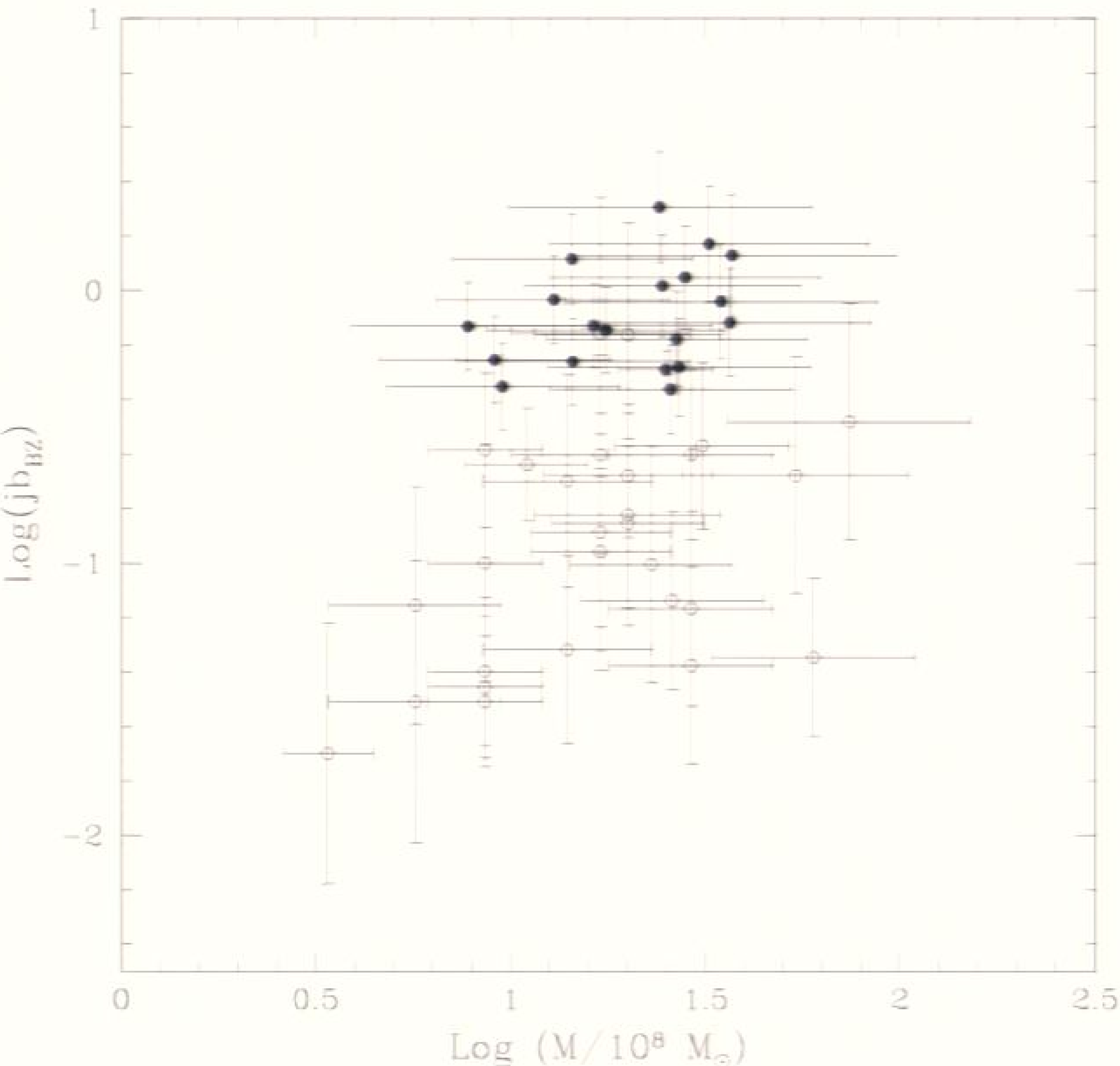
Values of L and M and for 29 central dominant galaxies were obtained from Rafferty et al. (2006).

These values of L and M were used to study the product jb using the relation $jb_{BZ} \approx 0.37\ [L_{44}/M_8]^{1/2}$, which is the relation predicted by the BZ model of energy extraction.

In the hybrid model proposed by Meier (1999), this expression is decreased by the factor $5^{-1/2}$ or $jb_M = jb_{BZ}/\surd 5$.



FRII radio galaxies are indicated by solid circles, and radio sources associated with CD galaxies are indicated by open circles; from Daly (2009b).



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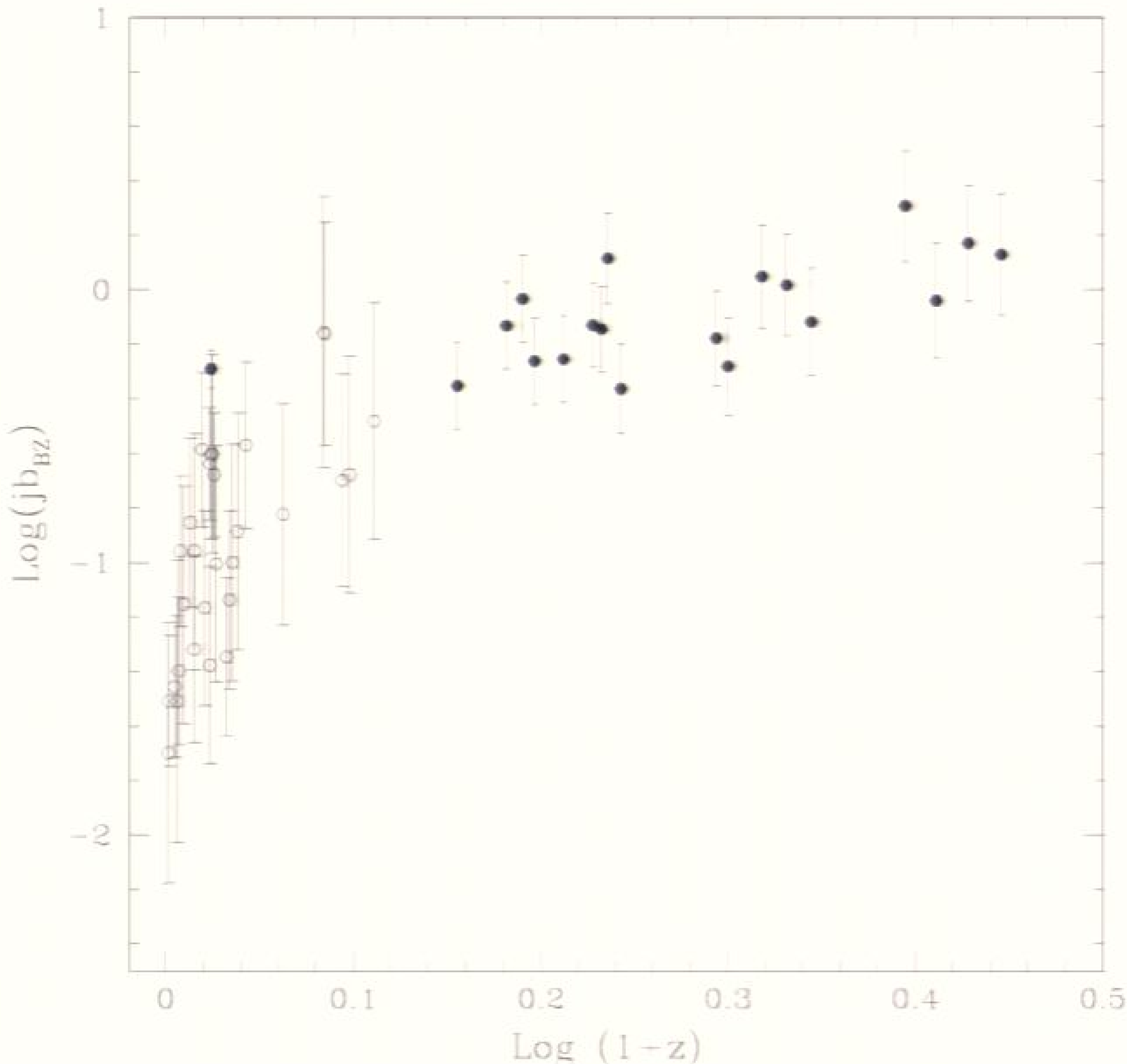

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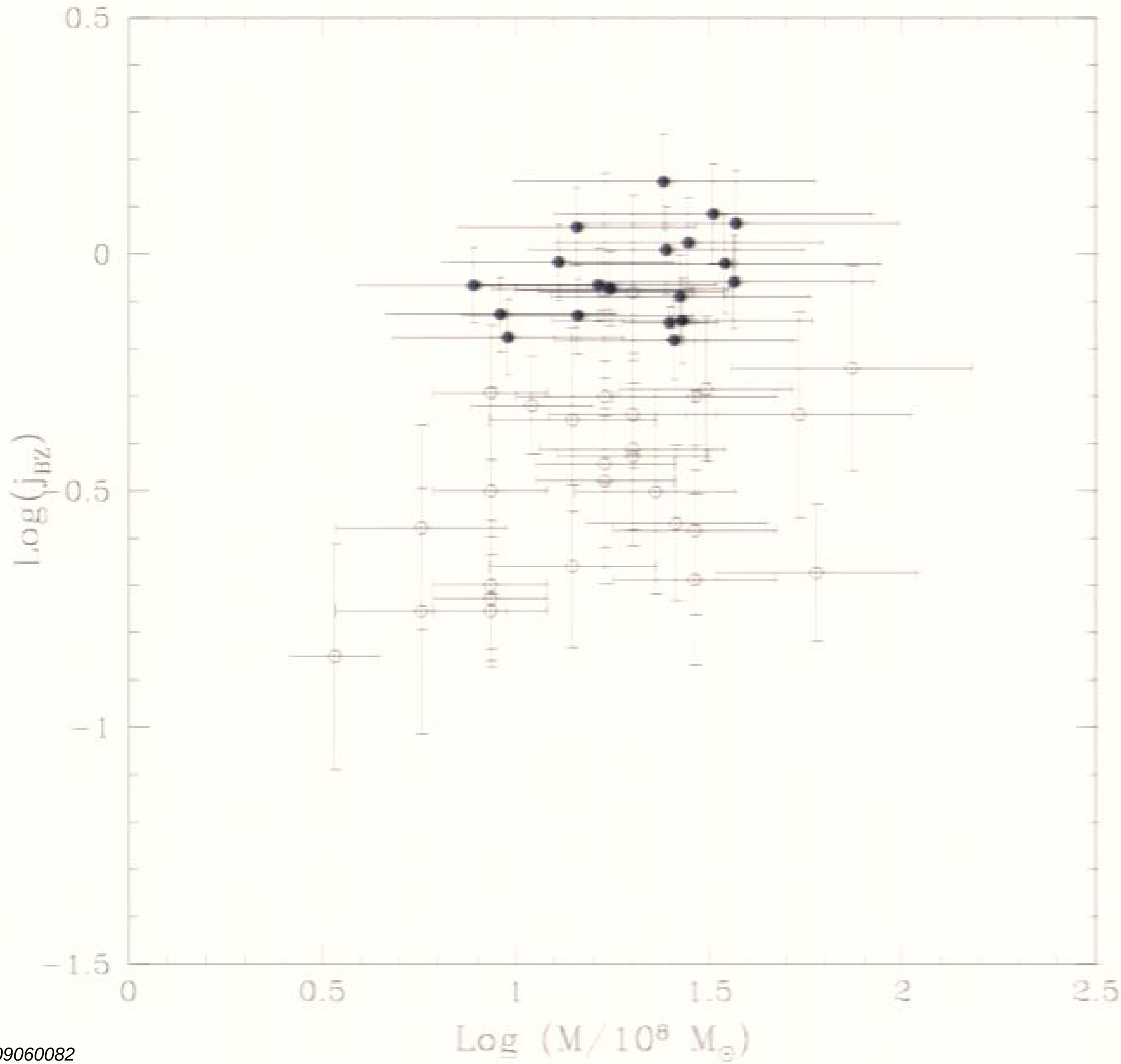
There are some indications that B is proportional to j. In this case, $b = b_o j$, and the results obtained showing that $bj \approx 1$ suggest that $b_o \approx 1$ since both b and j must be ≤ 1. In this case, we can solve for j.



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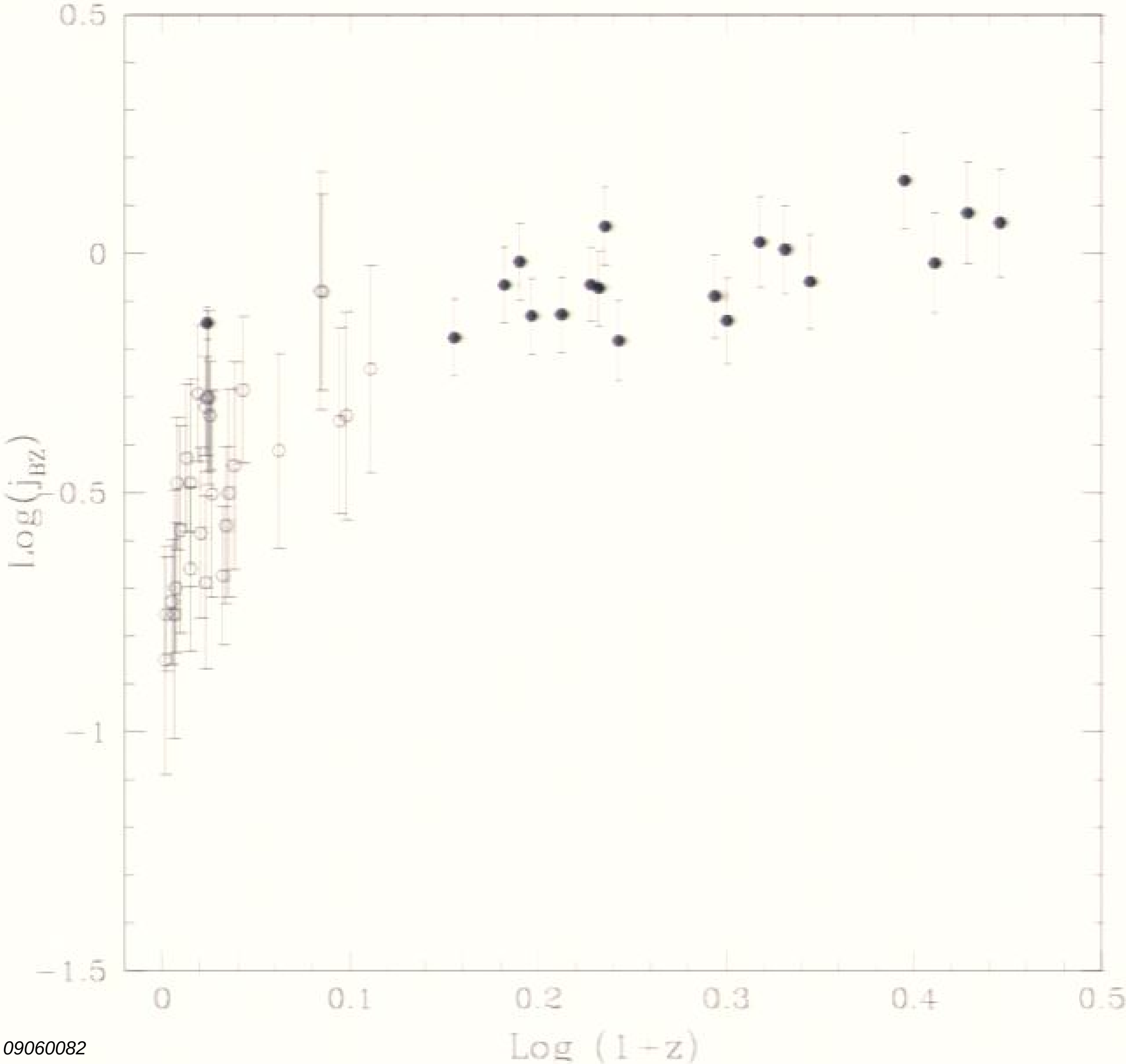

FRII radio galaxies are indicated by solid circles, and radio sources associated with CD galaxies are indicated by open circles; from Daly (2009b).

Thus, extended radio sources can be used to study the **spins** of supermassive black holes IF the outflows are powered by the spin of the black hole.

This may be done in 2 ways:

(1) The outflow energy may be taken as a lower bound on the initial spin energy of the black hole. The outflow energy may be combined with the black hole mass to obtain a lower bound on the initial black hole spin, as proposed by Daly (2009a).

(2) The beam power of the outflow may be considered in the context of a particular model for the production of large-scale jets [e.g. the models of Blandford & Znajek (1977) and Meier (1999)]. The beam power may be combined with the BH mass to study the BH spin, as proposed by Daly (2009b).

Mini-Summar III - Results obtained with the first application of these methods are:

(1.) The study of E_* and M for FRII RG indicates that the lower bound on j is the same for each of the 19 RG studied: $j = 0.12 \pm 0.01$, with no dependence on z or P_r. That is, the ratio $r = E_*/Mc^2$ seems to be constant! This suggests that each BH system is in a similar physical state at the time the outflow is generated. This may indicate that the outflow is triggered when a particular threshold, related to $r \approx 0.002$, is reached.

(2.) From the study of L_j and M for FRII RG, we find that each source has a lower bound on j that is significantly larger than the lower bound on j obtained from considerations of E_* and M. This suggests that each source may undergo multiple outflow events, and that only a small part of the spin energy is extracted during each outflow event.

These first studies of FRII RG and BH spin suggest that the spins of the supermassive that power large-scale outflows have values of j close to unity at redshifts of above one; the sources have values of j that decrease with decreasing redshift and have values close to 0.7 at low redshift.

This behavior is predicted in models in which the BH accretes gas in a series of accretion events, such as the models discussed by King & Pringle (2006, 2007) and King et al. (2008). This is also predicted in the merger models for evolution of BH growth of Hughes & Blandford (2003).

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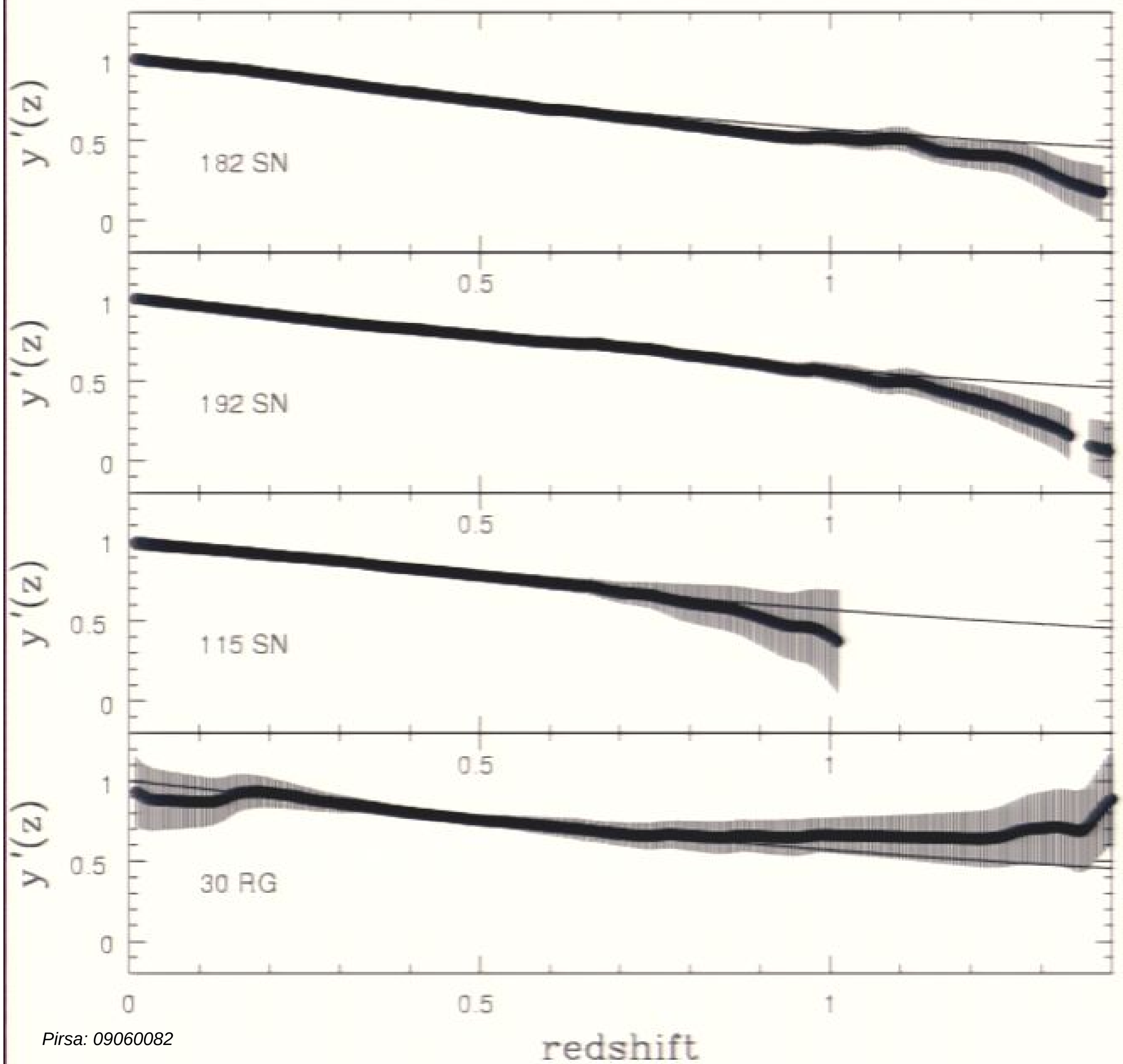
The coordinate distance, $(a_o r)$; luminosity distance $d_L = (a_o r)(1+z)$; angular size distance $d_A = (a_o r)\ (1+z)^{-1}$ all carry the same cosmological information.

It is convenient to work with $y(z)=H_0\,(a_o r)$, the dimensionless coordinate distance

SN: $5 \log [y(z)(1+z)] - m_{Beff}\,[\alpha] = -\mathcal{M}'_B = \text{const.}$

RG: $R^* = k_o y^{(6\beta-1)/7}\,(k_1 y^{-4/7} + k_2)^{\beta/3-1} = \kappa = \text{const.}$ (Daly 94)
where k_o, k_1, and k_2 are observed quantities.
Based on one empirically determined relationship (now understand the physical basis for relationship)

Study 30 RG from LMS89, LPR92, GDW00, & Kharb et al. '08 → Obtain y(z) to each source (Daly et al. 2008) [have VLA data for another 13 sources]

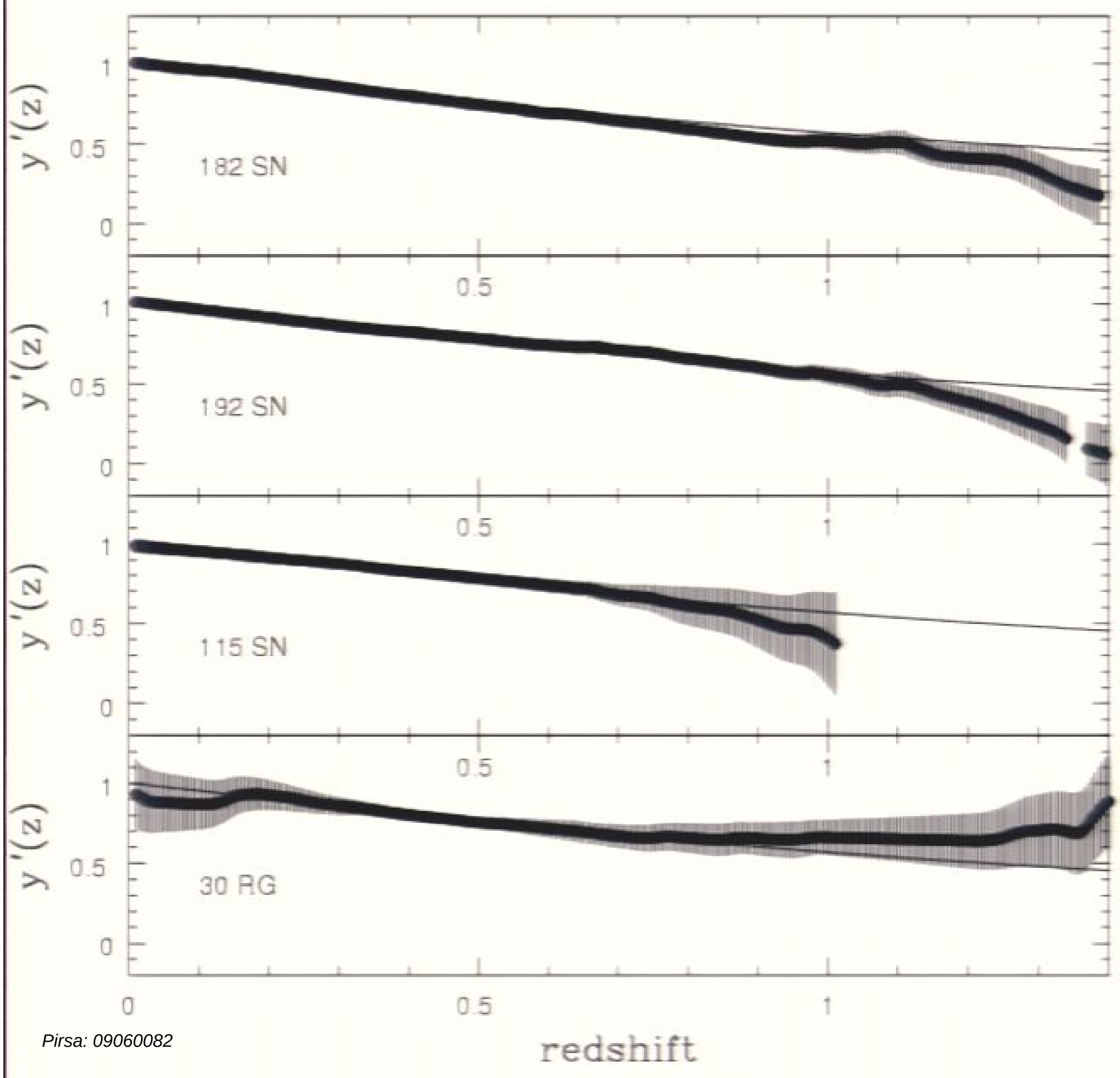


$Y' = dy/dz$

Model-independent: Provides a large scale test of GR.

Compare with prediction in LCDM model based on GR and Λ=0.7, Ω=0.3

Good agreement between RG & SN



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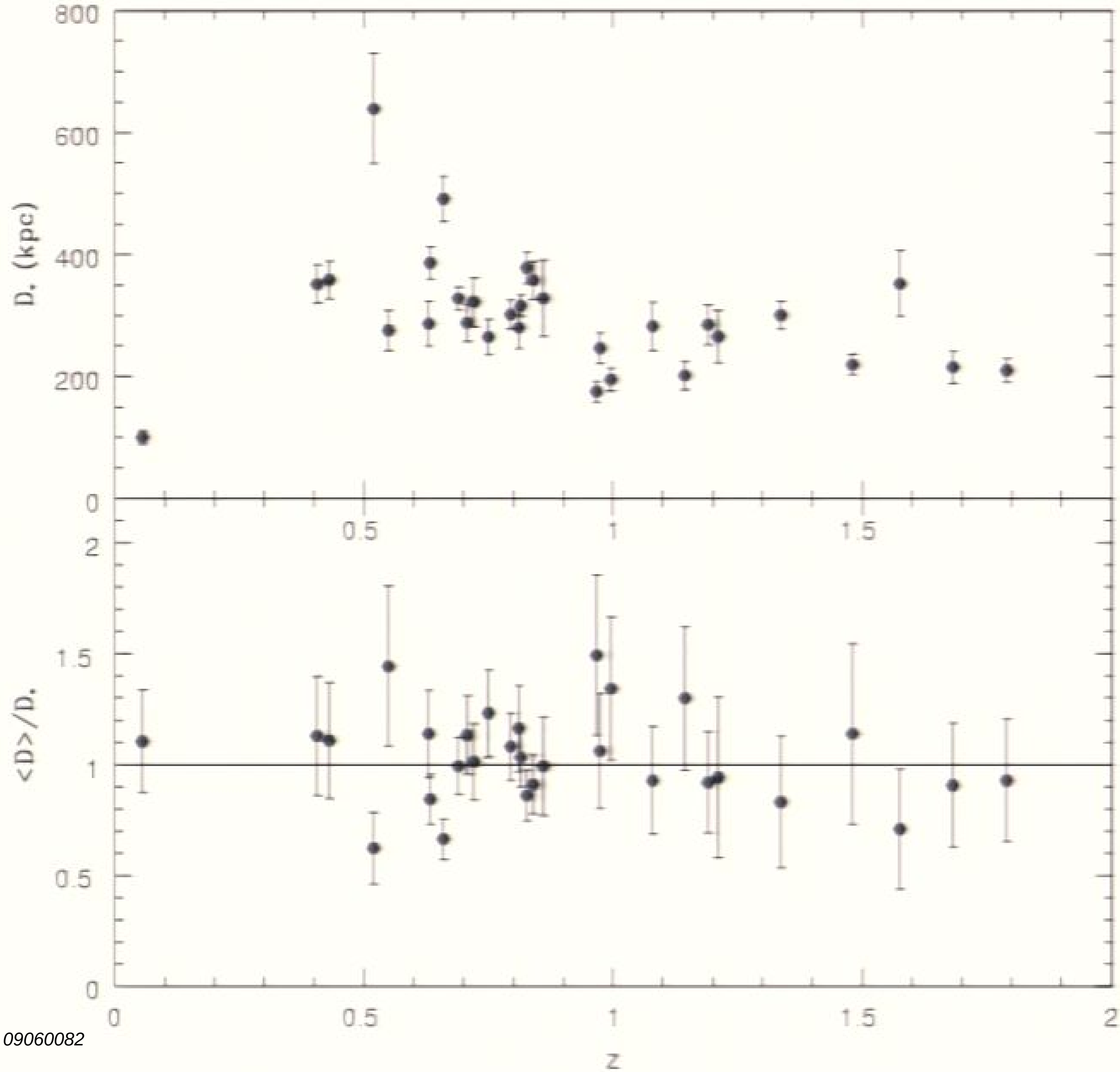
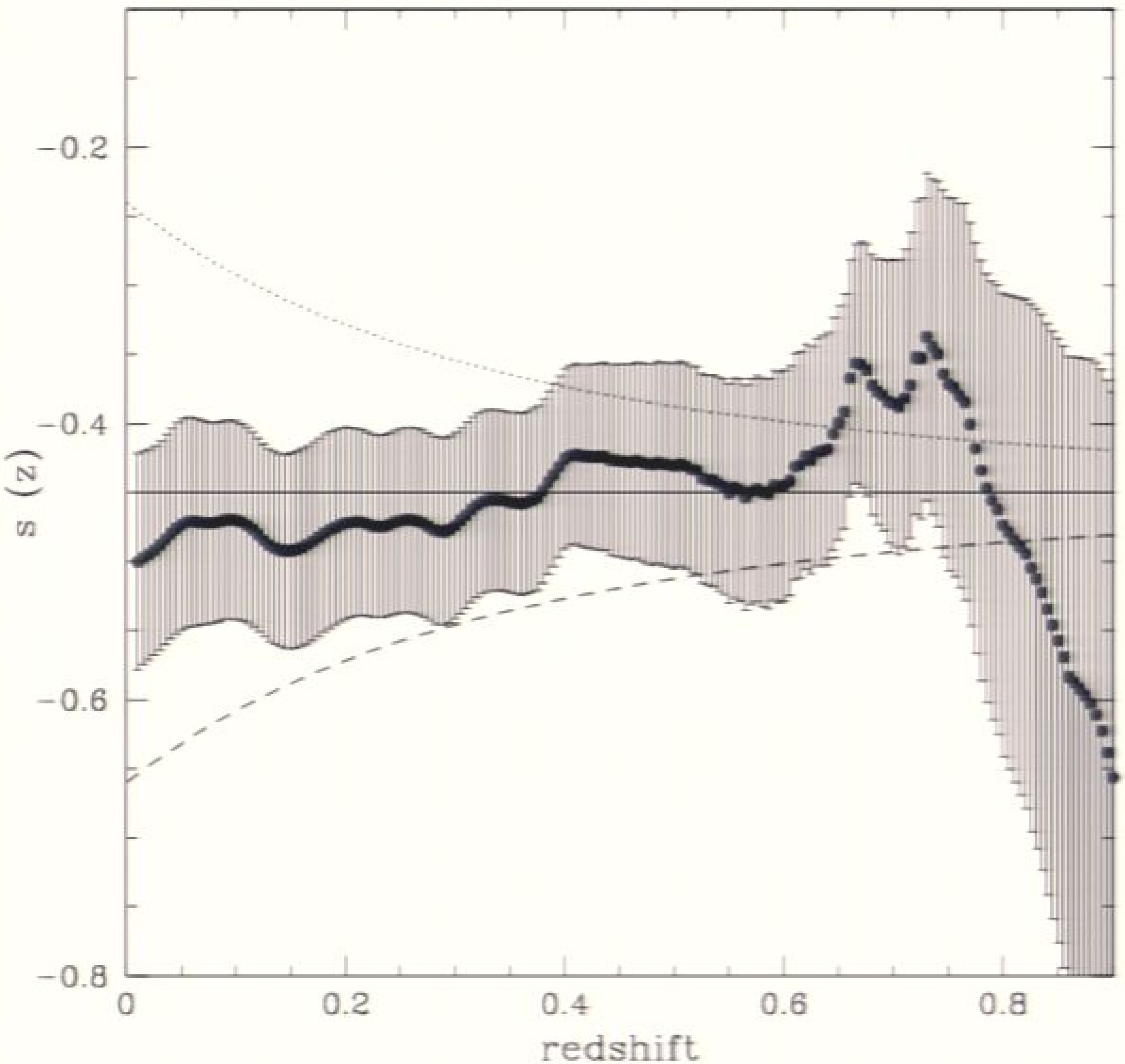
$D_* \sim v^{1-\beta/3} (a^2 P)^{-\beta/3} \sim v^{1/2} (a^2 P)^{-1/2}$ for $\beta = 1.5$



D_* shown for best fit parameters $\beta = 1.5 \pm 0.15$, $\Omega_m = 0.3 \pm 0.1$ and $w = -1.1 \pm 0.3$, obtained in a quintessence model.

The χ^2_r of the fit is about 1 (1.03)

From Daly et al. (2009)



Dark Energy Indicator

$s = y''(y')^{-3}(1+z)^{-2}$

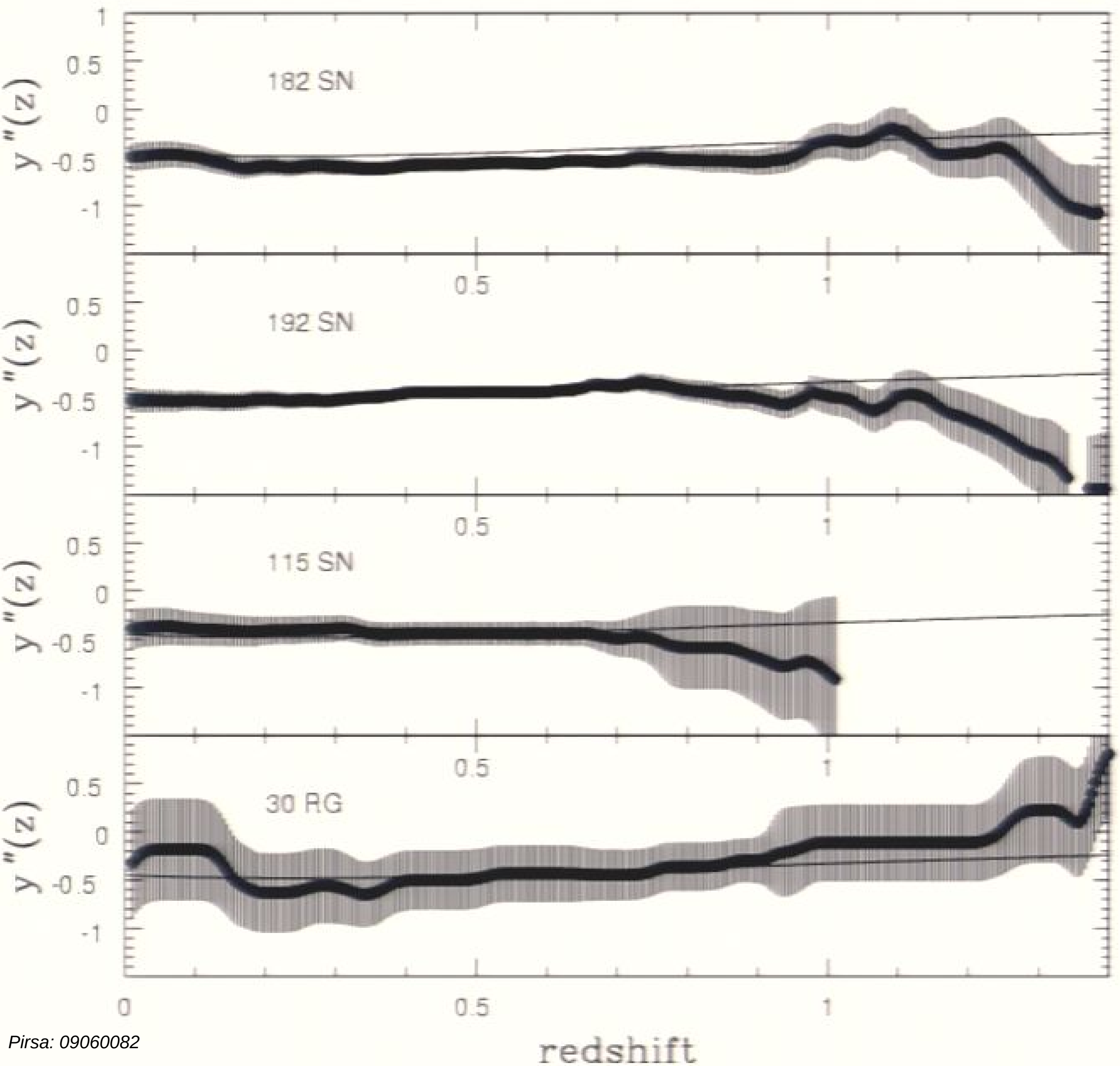
In a standard XCDM model based on GR, the predicted value of s is

$-1.5\Omega_m[1+(w+1)(\rho_{DE}/\rho_m)]$

Shown: w = -1.2,-1,-0.8

with Ω_m=0.3 &

$(\rho_{DE}/\rho_m)[z=0] = .7/.3$



$Y'' = d^2y/dz^2$

Model-independent

Compare with prediction in LCDM model based on GR

Good agreement between RG & SN