

Title: Cyclic Universe

Date: May 25, 2009 04:45 PM

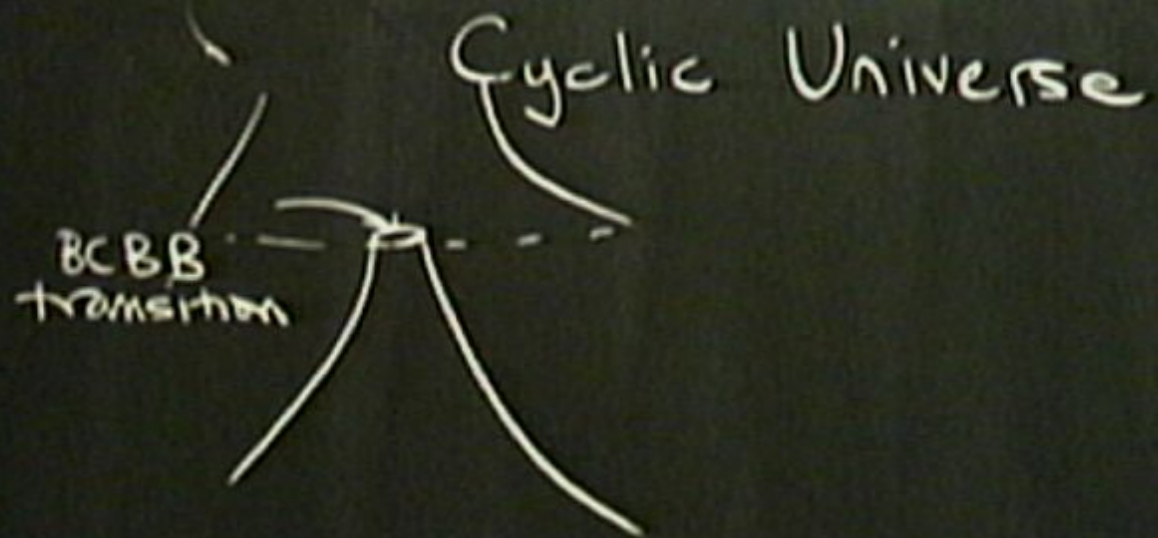
URL: <http://pirsa.org/09050073>

Abstract: TBA

Cyclic Universe

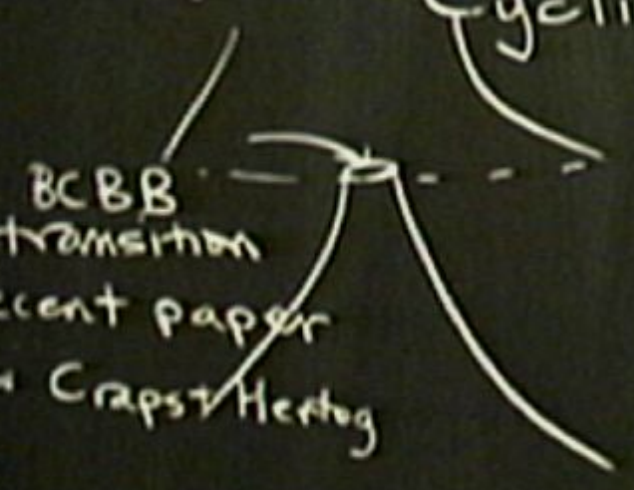
Cyclic Universe





Cyclic Universe

BCBB
transition
recent paper
w Crapst Hertog



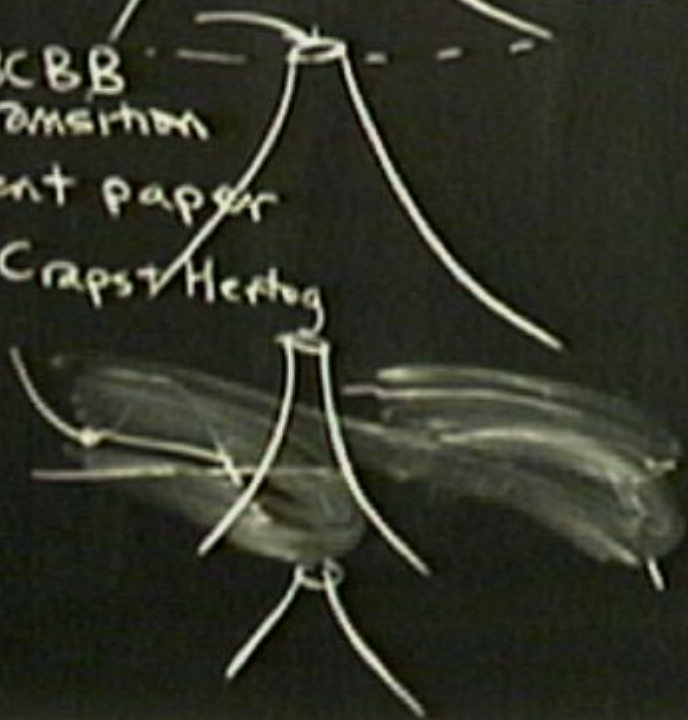
Cyclic Universe

BCBB
transition
recent paper
w Crapst Hertog



Cyclic Universe

BCBB
transition
recent paper
w Crapst Hertog



Cyclic Universe

requires $\Lambda > 0$

BCBB
transition
recent paper
w/ Crapst/Hertog



Cyclic Universe

requires $\Lambda > 0$

BCBB
transition
recent paper
w Crapst Hertog

10^{30}



Cyclic Universe

requires $\Lambda > 0$

BCBB
transition
recent paper
w/ Crapst Herlog

10^{30}



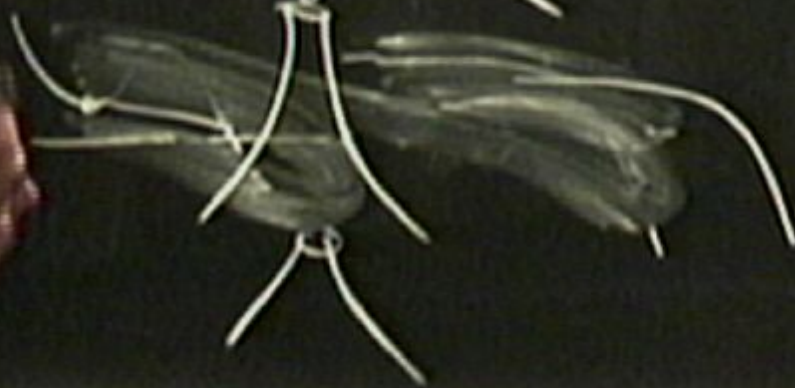
Cyclic Universe

requires $\Lambda > 0$

most of $v.$ is like what we see.

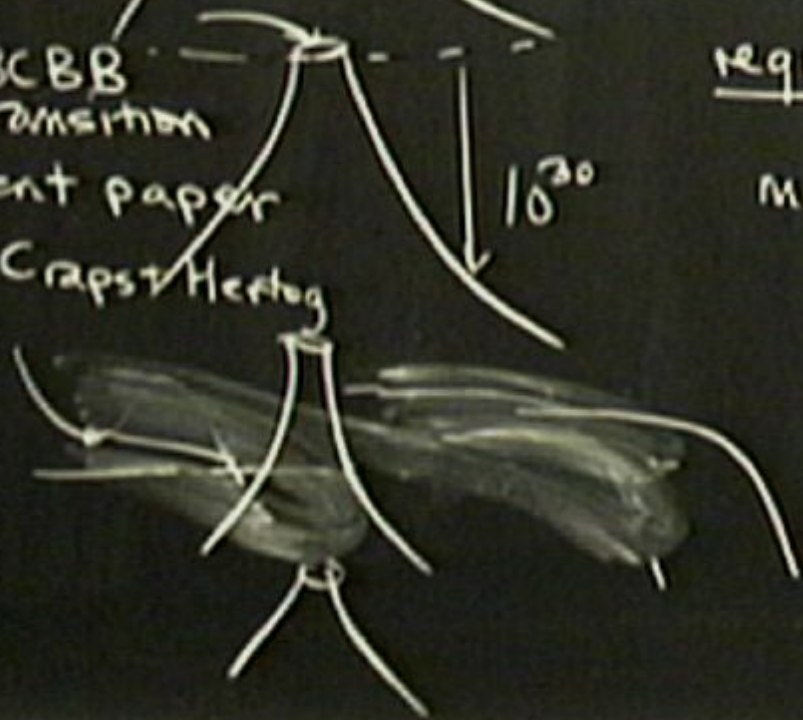
BCBB
transition
recent paper
w/ Crapst Hertog

10^{30}



Cyclic Universe

BCBB
transition
recent paper
w/ Crapst Hertog



requires $\Lambda > 0$

most of v. is like what we see.

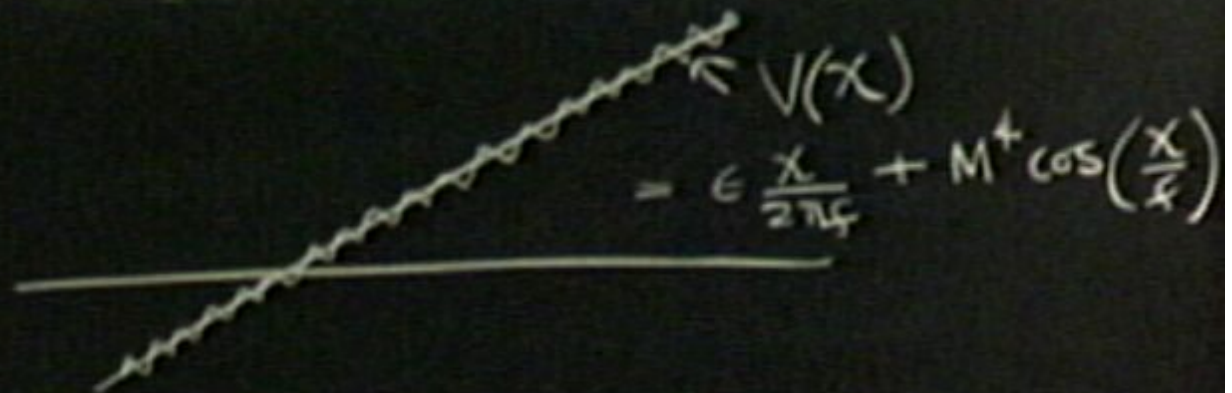
lots of time

Steinhardt

(Abbott 1985)

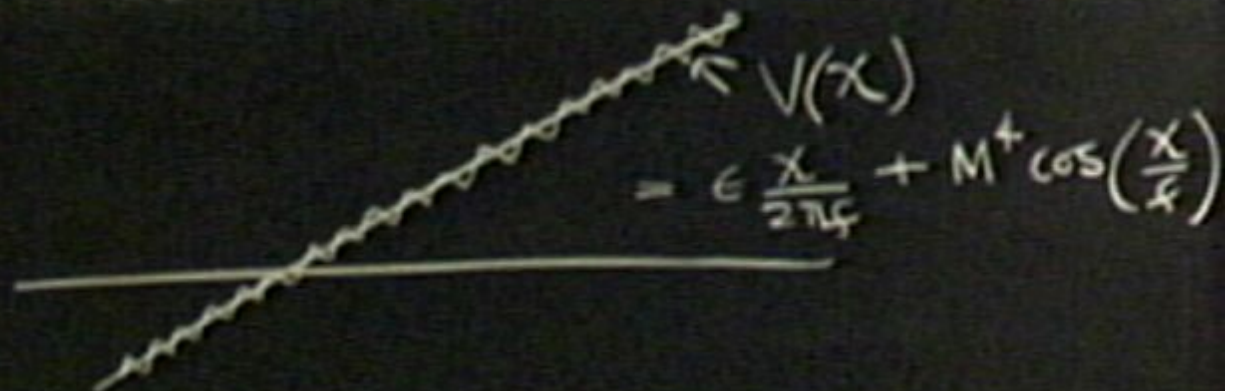
Steinhardt

(Abbott 1985)



Steinhardt

(Abbott 1985)

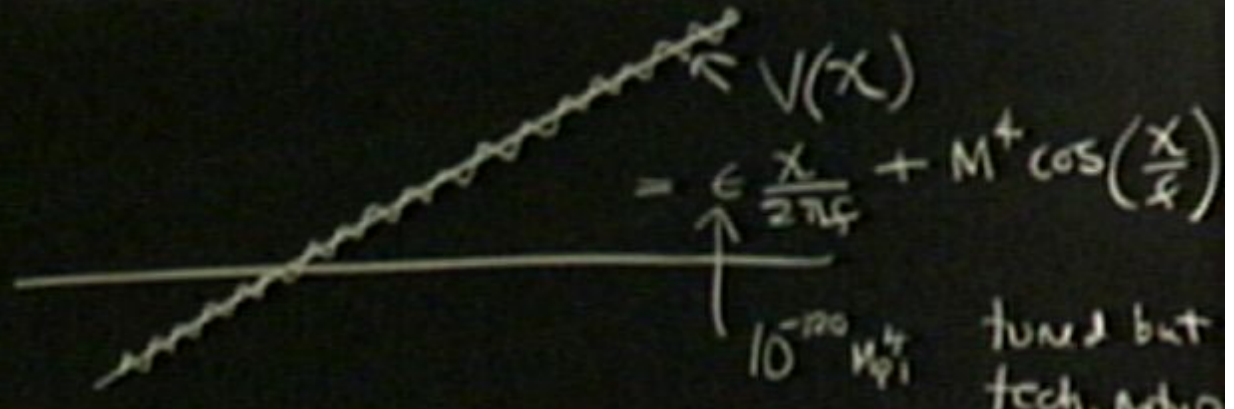


$$x \rightarrow x + \text{const}$$

break by ① soft linear term

Steinhardt

(Abbott 1985)

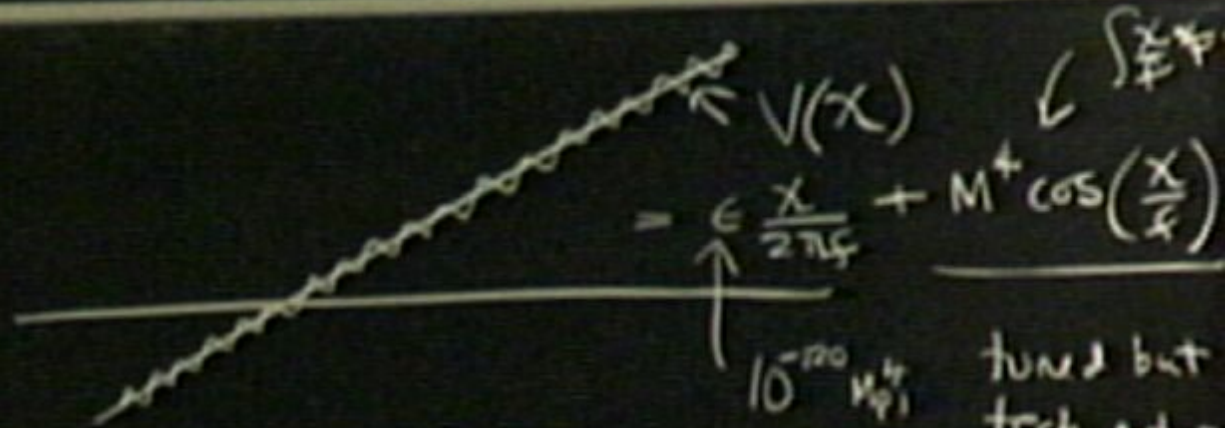


$$x \rightarrow x + \text{const}$$

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Steinhardt

(Abbott 1985)

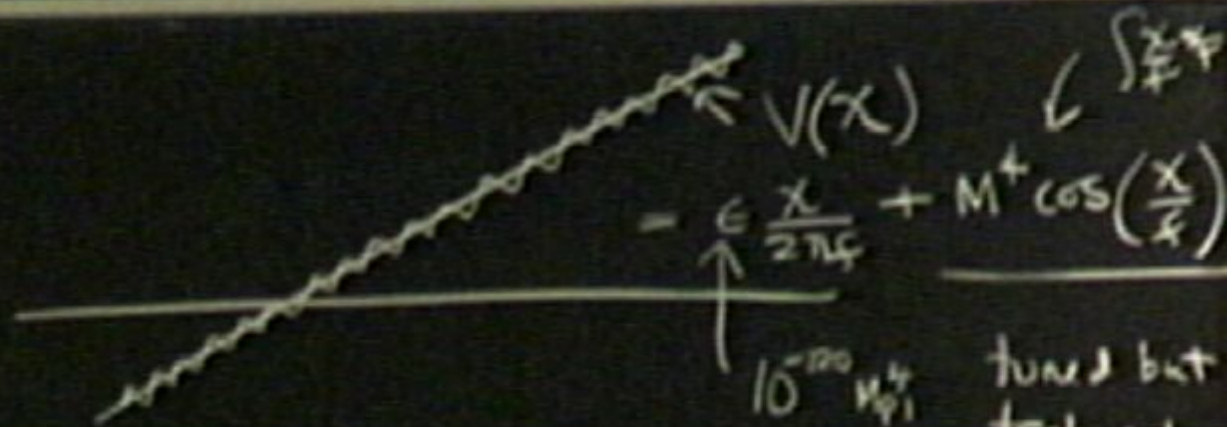


$$X \rightarrow X + \text{const}$$

break by ① soft linear term

Steinhardt

(Abbott 1985)

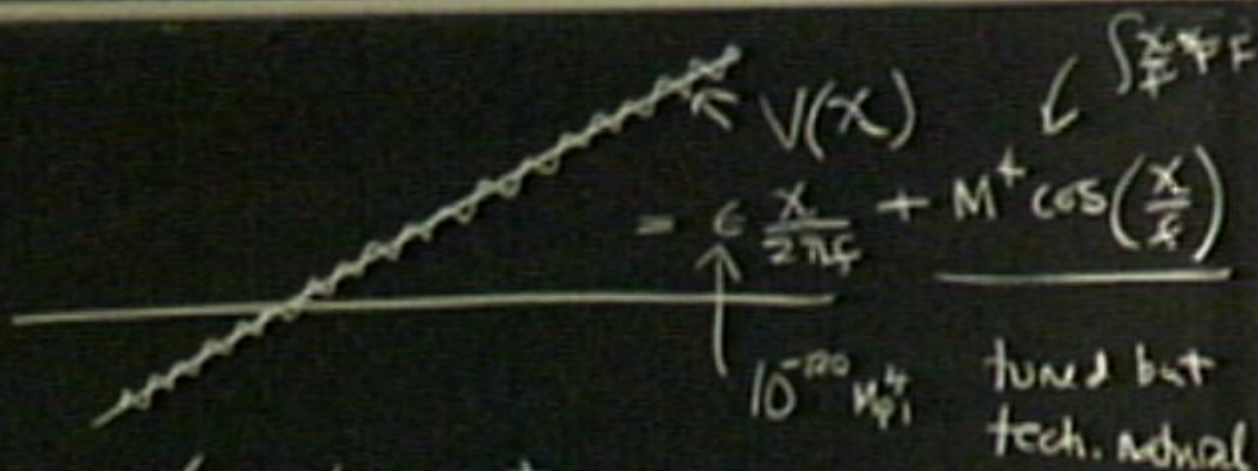


$$x \rightarrow x + \text{const}$$

break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

Steinhardt
(Abbott 1985)



$$x \rightarrow x + \text{const}$$

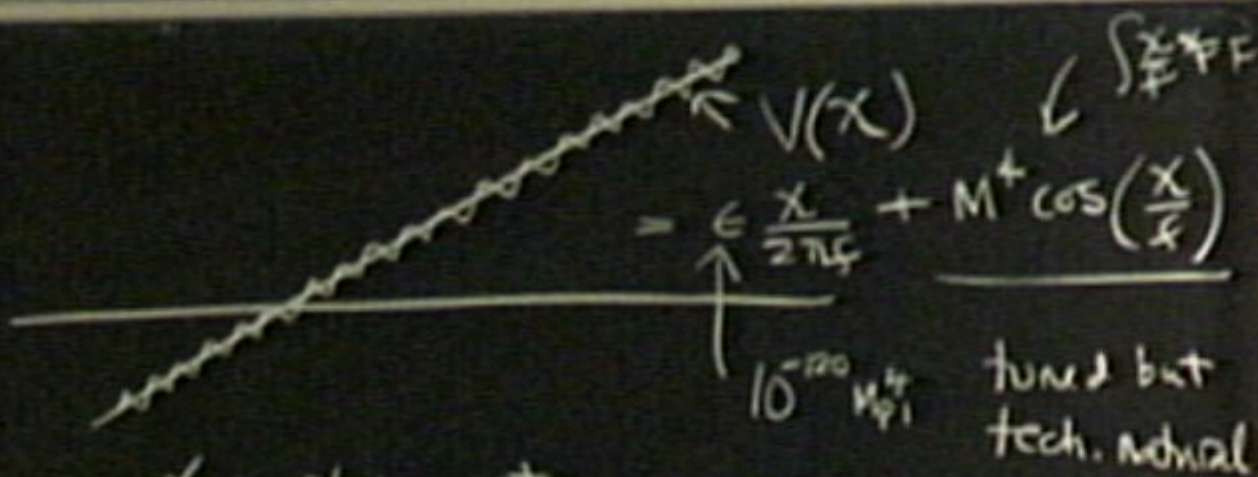
break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

$$M \sim M_{Pl} e^{-\frac{1}{\alpha(M_{Pl})}}$$

Steinhardt

(Abbott 1985)



$$X \rightarrow X + \text{const}$$

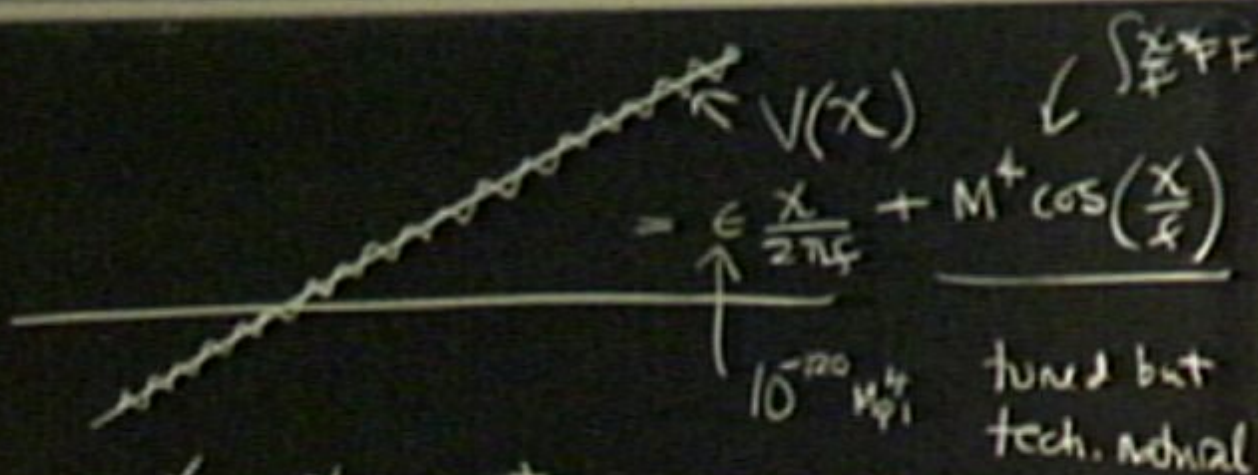
break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

$$M \sim M_{Pl} e^{-\frac{1}{\alpha(M_{Pl})}}$$

$$\alpha(M_{Pl}) \sim \frac{1}{45} \rightarrow \sim 10^{-3} \text{ eV},$$

Steinhardt
(Abbott 1985)



$$X \rightarrow X + \text{const}$$

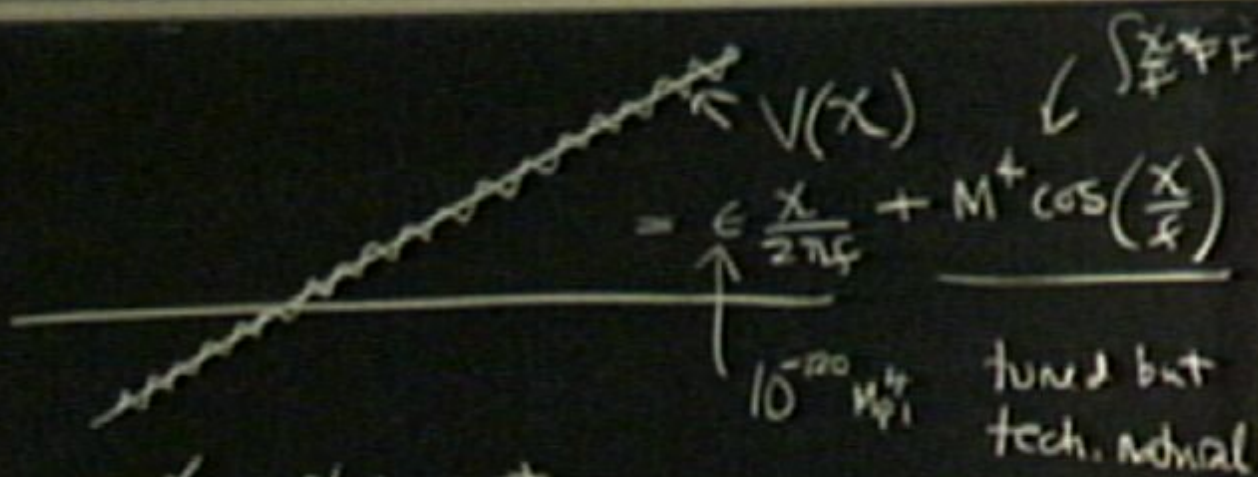
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Steinhardt
(Abbott 1985)



$$X \rightarrow X + \text{const}$$

break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

$$\epsilon < M^4$$

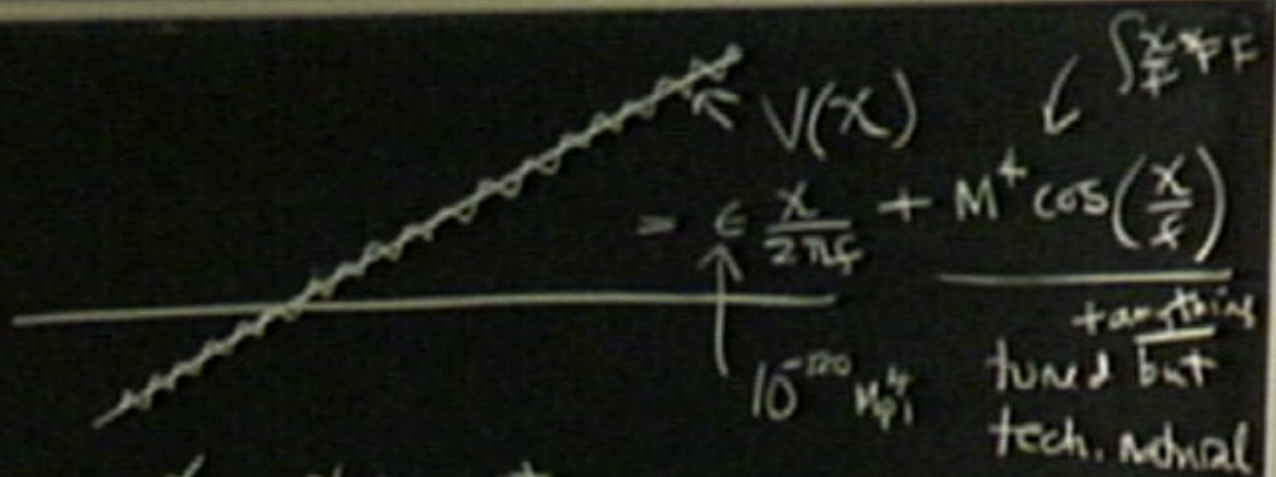
$\exists$ a minimum w/ V_0

$$0 < V_0 < \epsilon$$

$$M \sim M_{Pl} e^{-\frac{1}{\alpha(M_{Pl})}}$$

$$\alpha(M_{Pl}) = \frac{1}{f_5} \rightarrow \sim 10^{-3} \text{ eV}$$

Steinhardt
(Abbott 1985)



$$X \rightarrow X + \text{const}$$

break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

$$\epsilon < M^4$$

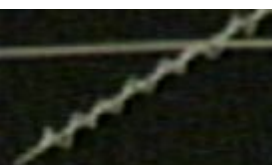
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(Abbott 1985)



$$10^{-20} M_{Pl}^4$$

anything
tuned but
tech. natural

$$\chi \rightarrow \chi + \text{const}$$

break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

$$E < M^4$$

$\exists$ a minimum w/ V_0

$$0 < V_0 < E$$

$$\frac{f^2}{M_{Pl}^2} \ll \frac{E}{M^4} < 1$$

$$M \sim M_{Pl} e^{-\frac{1}{\alpha(M_{Pl})}}$$

$$\alpha(M_{Pl}) = \frac{1}{f^2} \rightarrow \sim 10^{-3} \text{ eV}$$

Scenario: imagine starting with $V \gg E$

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$$V \gg M_{\text{Pl}}^2 M^4 \rightarrow \text{no barriers}$$

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① Hawking Mass

Scenario: imagine starting with $V \gg E$

$$V \gg M_{\text{Pl}}^2 M^4 \rightarrow \text{no barriers}$$

① Hawking Moss

② Coleman De Luccia

⇒ a minimum w/ V_0

$$0 < V_0 < \epsilon$$

$$\frac{f^2}{M_{Pl}^2} \ll \frac{\epsilon}{M_{Pl}^2} < 1$$

⑤ next part: formula for M_{Pl}

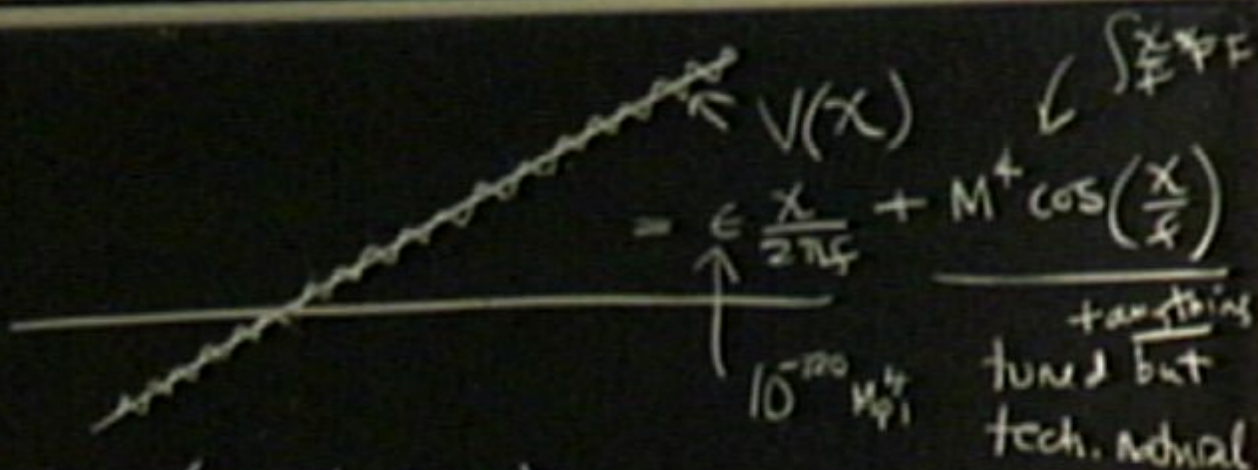
$$M \sim M_{Pl} e^{-\frac{1}{\sqrt{3}} \frac{\phi}{M_{Pl}}}$$

$$M(\phi) = \frac{1}{2} m^2 \phi^2 \rightarrow \sim 10^{13} \text{ eV}$$

$$V \gg M_{Pl}^2 M^4 \rightarrow \text{no barriers}$$

- ① Ling Moss
- ② Alan De Luccia
- ③ Flat ST bubble

Steinhardt
(Abbott 1985)



$$X \rightarrow X + \text{const}$$

break by ① soft linear term

② nonpert., natural for $M \ll M_{Pl}$.

$$\epsilon < M^4$$

$\exists$ a minimum w/ V_0

$$0 < V_0 < \epsilon$$

$$\frac{f^2}{M_{Pl}^2} \ll \frac{\epsilon}{M^4} < 1$$

$$M \sim M_{Pl} e^{-\frac{1}{2}(M_{Pl})^2}$$

$$X(M_0) = \frac{1}{\sqrt{5}} \rightarrow \sim 10^{-3} \text{ eV}$$

$$\frac{f^2}{M_{Pl}^2} \ll \frac{E}{M^2} < 1$$

Scenario: imagine starting with $V \gg E$

$$V \gg M_{Pl}^2 M^4 \rightarrow \text{no barriers}$$

- ① Hawking Moss
- ② Coleman De Luccia
- ③ $\sim$ Flat ST bubble

$$\frac{f^2}{M_{Pl}^2} \ll \frac{E}{M^4} < 1$$

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- ① Hawking Moss
- ② Coleman De Luccia
- ③ $\sim$ Flat ST bubble S_E

$$\frac{f^2}{M_{Pl}^2} \ll \frac{E}{M^4} < 1$$

Scenario: imagine starting with $V \gg E$

$$V \gg M_{Pl}^2 M^4 \rightarrow \text{no barriers}$$

- ① Hawking Moss
- ② Coleman De Luccia
- ③ $\sim$ Flat ST bubble

$$S_E = S_0 \left(1 - \frac{(V_H + V_{H-1}) T^2}{M_{Pl}^2 E^2} \right)$$

bubble wall tension

$$\frac{\lambda}{M_{Pl}^2} \ll \frac{E}{M^4} < 1$$

Scenario: imagine starting with $V \gg E$

$$V \gg M_{Pl}^2 M^4 \rightarrow \text{no barriers}$$

- ① Hawking Moss
- ② Coleman De Luccia
- ③ $\sim$ Flat ST bubble

e.g. $f \sim 10^4 \text{ GeV}$
 $\frac{f}{M} = 0.1$
 $M \sim 10^3 \text{ eV}$

$$S_E = S_0 \left(1 - \frac{(V_N + V_{N-1}) T^2}{M_{Pl}^2 E^2} \right)$$

$\downarrow$
 10^{110}

bubble wall tension
 $\uparrow$

Scenario: imagine starting with $V \gg E$

$$V \gg M_{Pl}^2 M^4 \rightarrow \text{no barriers}$$

- ① Hawking Moss
- ② Coleman De Luccia
- ③ $\sim$ Flat ST bubble

e.g. $f \sim 10^4 \text{ GeV}$
 $\frac{f}{M_{Pl}} = 0.1$
 $M \sim 10^3 \text{ eV}$

$$S_E = S_0 \left(1 - \frac{\alpha N (V_H + V_{H-1}) T^2}{M_{Pl}^2 E^2} \right)$$

bubble wall tension

10^{110}

Scenario: imagine starting with $V \gg E$

$$V \gg M_{Pl}^2 M^4 \rightarrow \text{no barriers}$$

- ① Hawking Moss
- ② Coleman De Luccia
- ③ $\sim$ Flat ST bubble

rate $\propto e^{10^{10} N}$

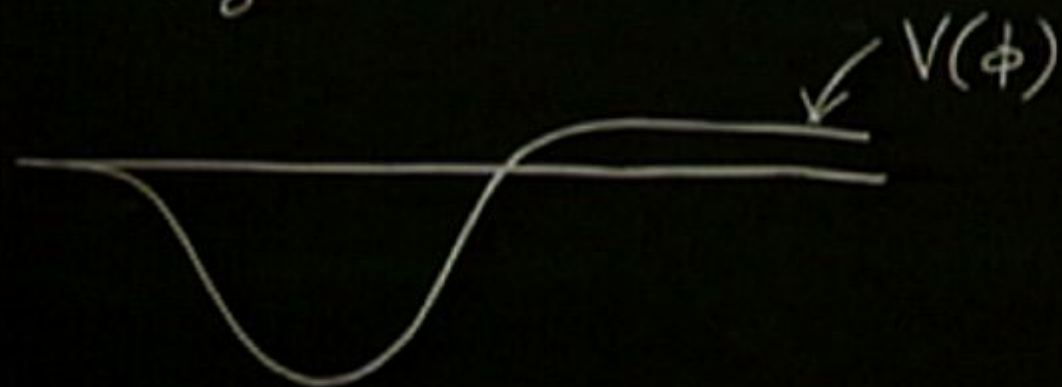
e.g. $f \sim 10^4 \text{ GeV}$
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 $M \sim 10^{-3} \text{ eV}$

$$S_E = S_0 \left(1 - \frac{(V_N + V_{N-1}) T^2}{M_{Pl}^2 E^2} \right)$$

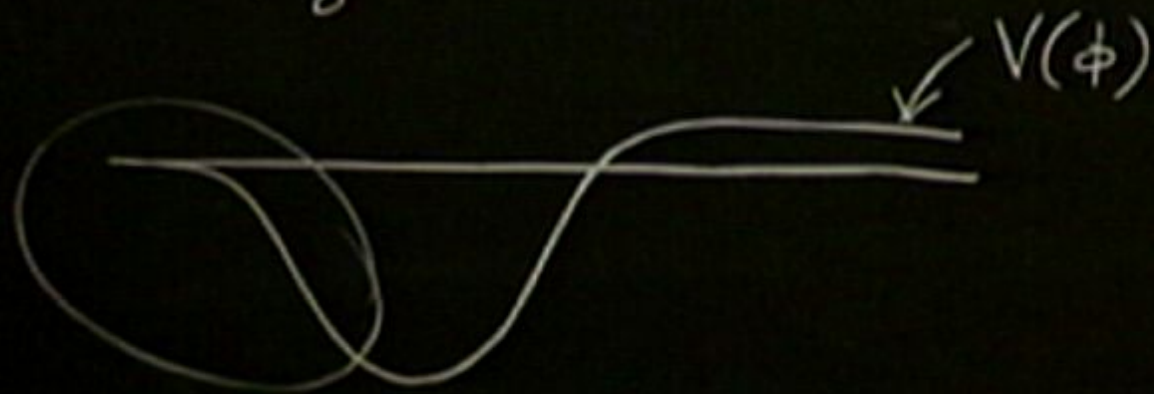
$\propto N$ bubble wall tension

10^{110}

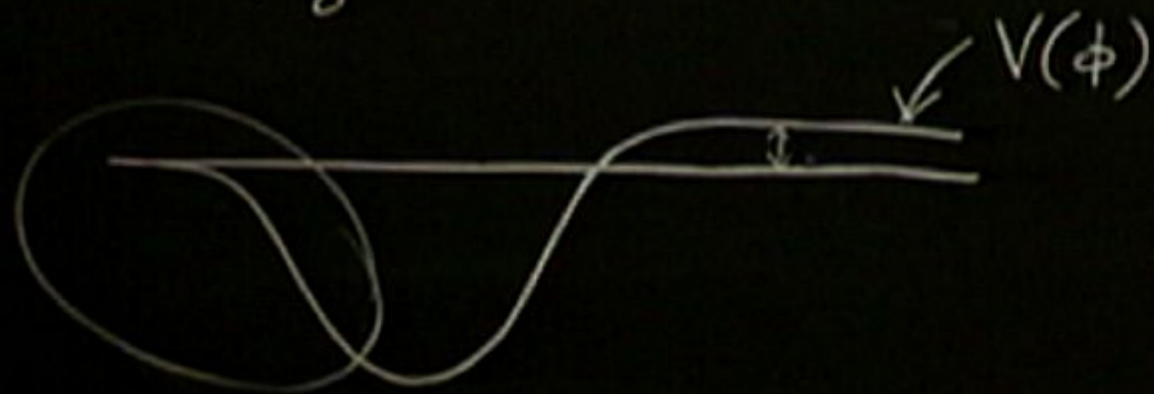
Empty universe problem!



Empty universe problem!



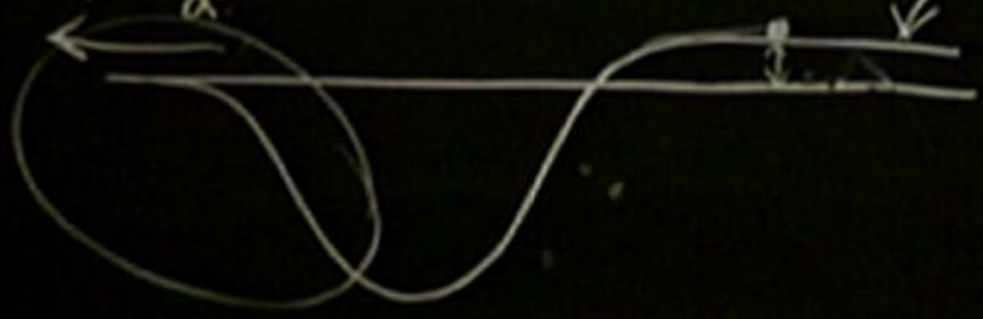
Empty universe problem!



Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^2}$$

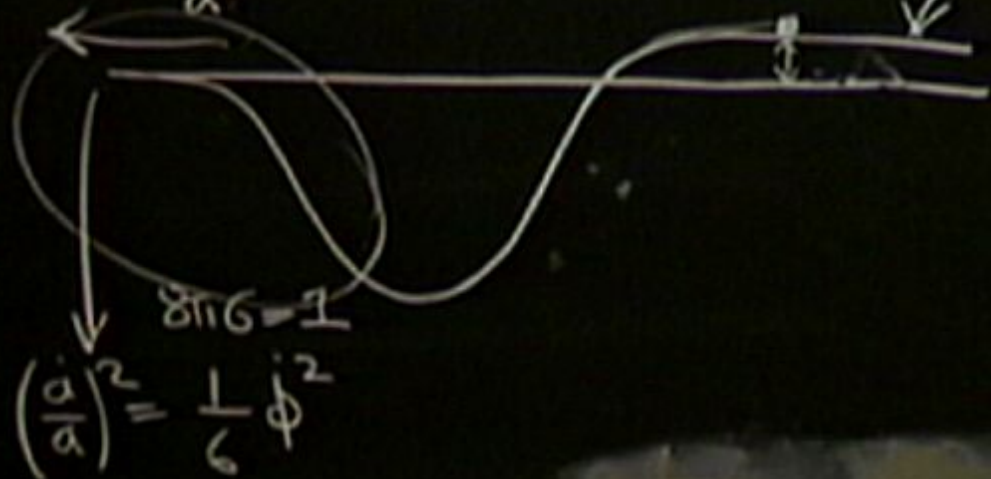
$V(\phi)$

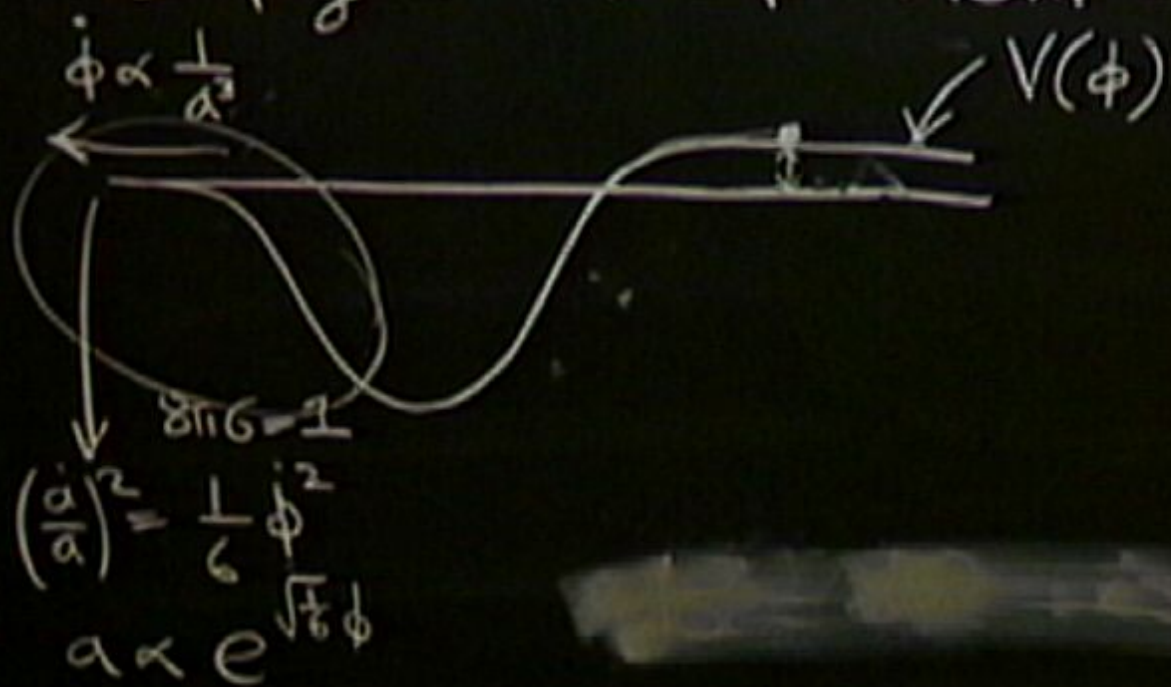


Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

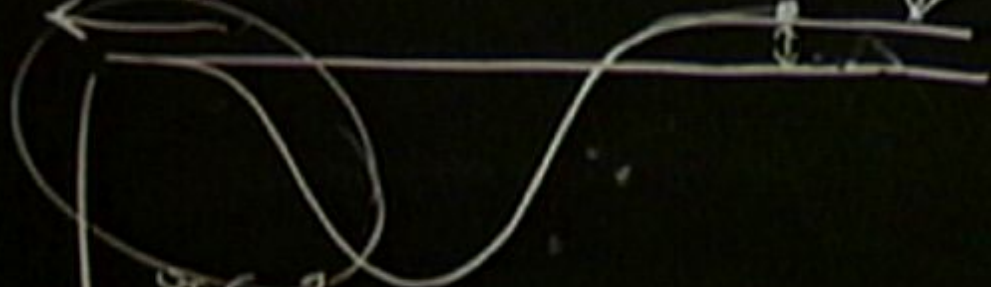
$V(\phi)$





$$\dot{\phi} \propto \frac{1}{a^3}$$

$$V(\phi)$$



$$8\pi G = 1$$

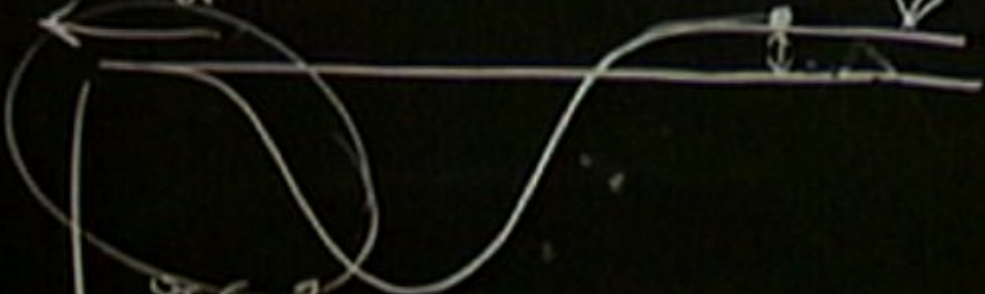
$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$e^{-\sqrt{\frac{3}{2}} \phi} g_{\mu\nu}^E = \text{finite at Sing?}$$

$$\dot{\phi} \propto \frac{1}{a^3}$$

$$V(\phi)$$



$$8\pi G = 1$$

$$\left(\frac{da}{da}\right)^2 = \frac{1}{6} \phi^2$$

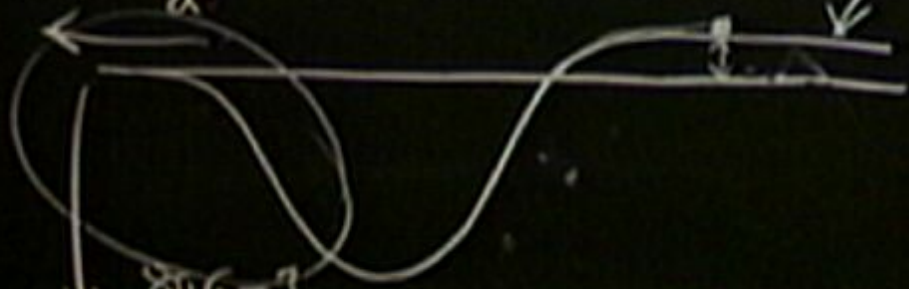
$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^E = e^{-\sqrt{\frac{2}{3}} \phi} \quad g_{\mu\nu}^E = \text{finite at Sing?}$$

Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

$V(\phi)$



$$8\pi G = 1$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

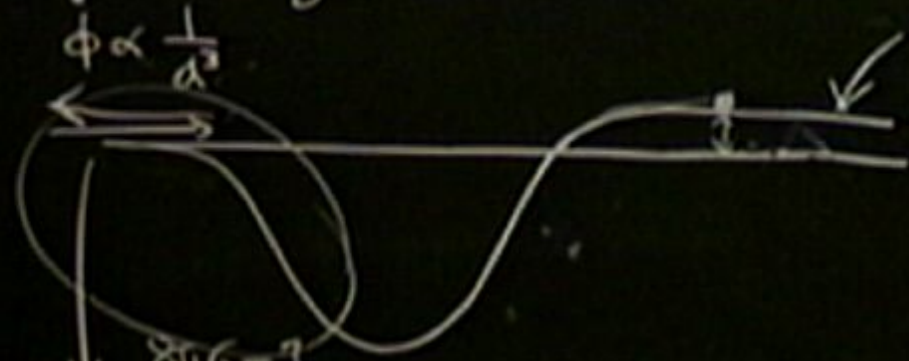
$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{\text{st}} = e^{-\sqrt{\frac{1}{3}} \phi} \quad g_{\mu\nu}^{\text{E}} = \text{finite at Sing!}$$

Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

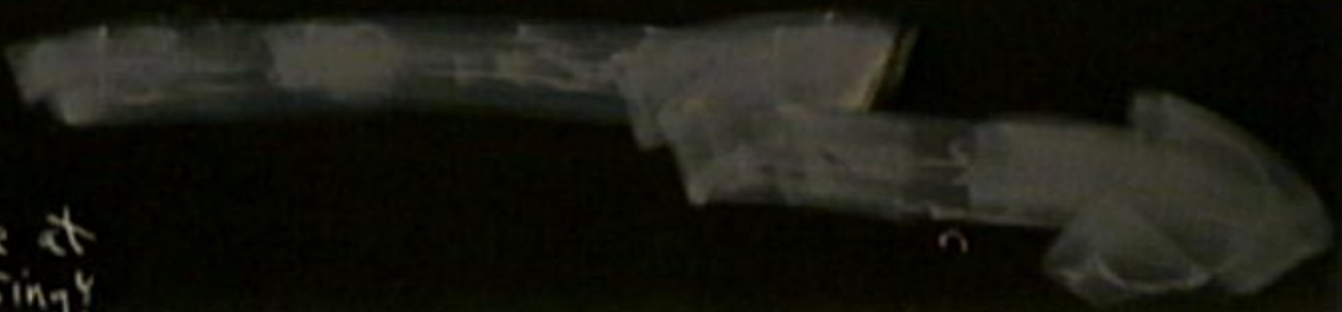
$V(\phi)$



$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{\text{st}} = e^{-\sqrt{\frac{1}{3}} \phi} \quad g_{\mu\nu}^{\text{E}} = \text{finite at Sing!}$$



Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

$V(\phi)$

$k \approx m$

$$8\pi G = 1$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{\text{ad}} = e^{-\sqrt{\frac{1}{6}} \phi} \quad g_{\mu\nu}^{\text{E}} = \text{finite at Sing!}$$

Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

$V(\phi)$

$k \approx 10^{-10} m$

$$8\pi G = 1$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{\text{ad}} = e^{-\sqrt{\frac{1}{6}} \phi} \quad g_{\mu\nu}^{\text{E}} = \text{finite at Sing!}$$

Empty universe problem!

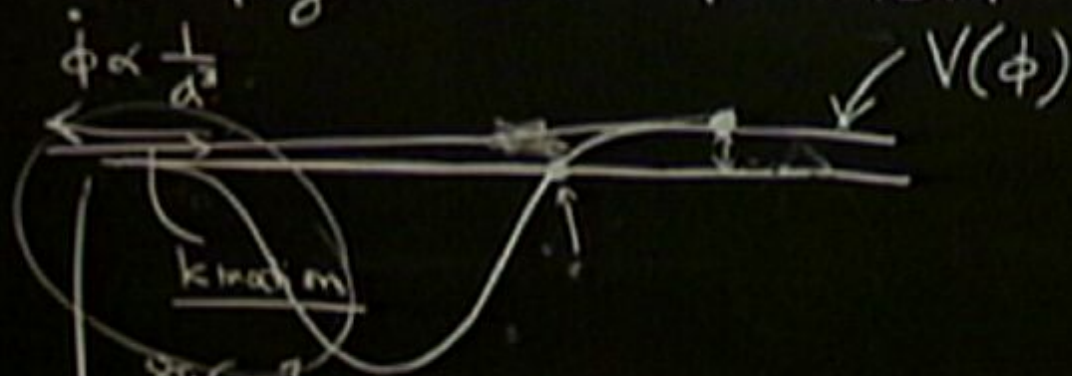


$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{\text{st}} = e^{-\sqrt{\frac{1}{3}} \phi} \quad g_{\mu\nu}^{\text{E}} = \text{finite at Sing!}$$

Empty universe problem!

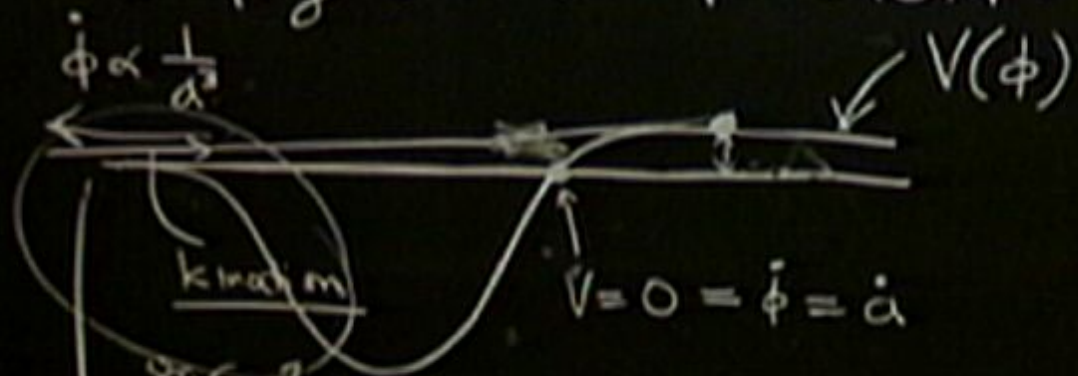


$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{(3d)} = e^{-\sqrt{\frac{1}{3}} \phi} \quad g_{\mu\nu}^{(E)} = \text{finite at Sing!}$$

Empty universe problem!



$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2$$

$$a \propto e^{\sqrt{\frac{1}{6}} \phi}$$

$$g_{\mu\nu}^{SD} = e^{-\sqrt{\frac{2}{3}} \phi} \quad g_{\mu\nu}^E = \text{finite at Sing!}$$

Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

$$V(\phi)$$

$$\underline{V=0 = \dot{\phi} = \dot{a}}$$

$$k \approx 10^{-26} m$$

$$8\pi G = 1$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2 - \sqrt{\frac{2}{3}} \phi$$

$$\dot{\phi}^2 \propto \frac{1}{a^6}$$

$$a \propto e$$

$$g_{\mu\nu}^{\text{SI}} = e^{-\sqrt{\frac{2}{3}}\phi} \quad g_{\mu\nu}^{\text{E}} = \text{finite at Sing!}$$

Empty universe problem!

$$\dot{\phi} \propto \frac{1}{a^3}$$

$$V(\phi)$$

$$\underline{V=0 = \dot{\phi} = \dot{a}}$$

coincidence
problem

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{6} \dot{\phi}^2 - \sqrt{\frac{2}{3}} \phi$$

$$\dot{\phi}^2 \propto \frac{1}{a^6}$$

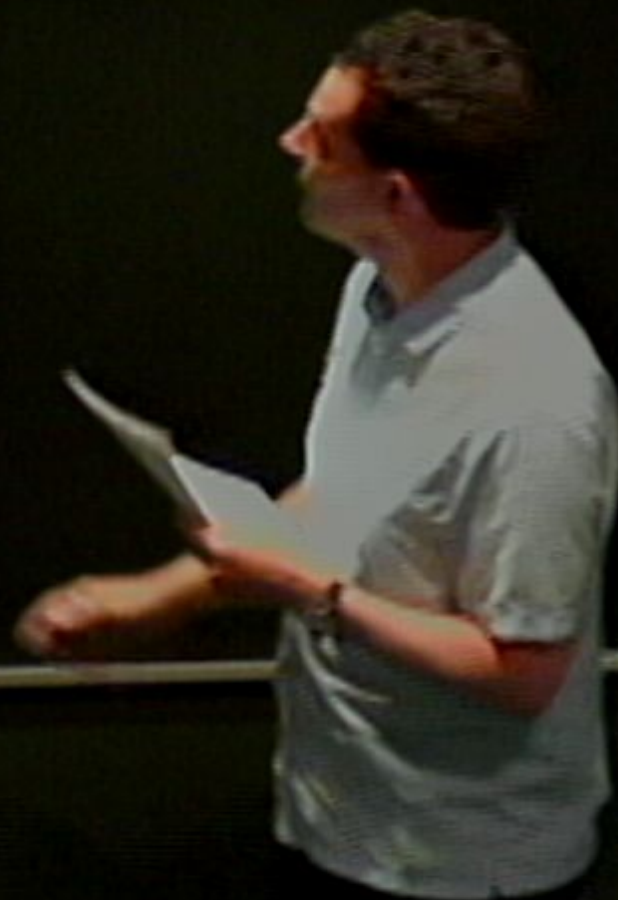
$$a \propto e^{\dots}$$

$$g_{\mu\nu}^E = \text{finite at Sing!}$$

Sing?

$$S' \sim - \int g(\phi) \rho$$

$$\ddot{\phi} + 3H\dot{\phi}$$



$$S' \sim -\int g(\phi) \rho \quad \rightarrow \quad \Box \phi = g'(\phi) \rho \quad \frac{\beta}{M_{Pl}} = \frac{g'(\phi)}{g(\phi)}$$

$$\ddot{\phi} + 3H$$

$$S' \sim -\int g(\phi) \rho \quad \rightarrow \quad \square\phi = g'(\phi) \rho \quad \cdot \quad \frac{\beta}{M_{Pl}} = \frac{g'(\phi)}{g(\phi)}$$

$$\ddot{\phi} + 3H\dot{\phi}$$

$$\frac{\beta_{\text{ord}} < 10^{-3}}{\underline{\hspace{1cm}}}$$

$$\text{STEP} \rightarrow \underline{\underline{< 10^{-6}}}$$

$$S' \sim - \int g(\phi) \rho \quad \rightarrow \quad \square \phi = g'(\phi) \rho \quad \cdot \quad \frac{\beta}{M_{Pl}} = \frac{g'(\phi)}{g(\phi)}$$

$$\ddot{\phi} + 3H\dot{\phi} = - \frac{\beta_v}{M_{Pl}} (\rho_v - 3p_v)$$

$$\frac{\beta_{v,d} < 10^{-3}}{\underline{\hspace{1cm}}}$$

$$\text{STEP} \rightarrow \underline{< 10^{-6}}$$

$$S' \sim - \int g(\phi) \rho \quad \rightarrow \quad \square \phi = g'(\phi) T^\lambda{}_\lambda \quad \frac{\beta}{M_{Pl}} = \frac{g'(\phi)}{g(\phi)}$$

$$\ddot{\phi} + 3H\dot{\phi} = - \frac{\beta_v}{M_{Pl}} (\rho_v - 3p_v)$$

$$\frac{\beta_{v,d} < 10^{-3}}{\text{STEP} \rightarrow \underline{< 10^{-6}}}$$

$$a \propto e^{\dots}$$

$$g_{\mu\nu}^{\text{st}} = e^{-\sqrt{\frac{2}{3}}\phi} \quad \textcircled{g_{\mu\nu}^{\text{E}}} = \text{finite at Sing!}$$

$$\phi + 3H\dot{\phi} = -\frac{\beta_v}{M_{\text{pl}}} (\rho_v - 3p_v)$$

$$+ \frac{\beta_c}{M_{\text{pl}}} p_c$$

$$\frac{\beta_{\text{ord}} < 10^{-3}}{\text{STEP} \rightarrow \underline{< 10^{-6}}}$$

$$a \propto e^{\dots}$$

$$g_{\mu\nu}^{\text{st}} = e^{-\sqrt{\frac{2}{3}}\phi} \quad \textcircled{g_{\mu\nu}^{\text{E}}} = \text{finite at Sing!}$$

$$\phi + 3\dot{\phi} = -\frac{\beta_v}{M_{\text{pl}}} (\rho_v - 3p_v)$$

$$+ \frac{\beta_c}{M_{\text{pl}}} p_c$$

$$\Rightarrow \rho_{c, \text{eq}} > \rho_\Lambda$$

$$\frac{\beta_{\text{ord}} < 10^{-3}}{\text{STEP} \rightarrow \underline{< 10^{-6}}}$$

$$h \propto e^{\sqrt{3}\phi/2}$$

$$g_{\mu\nu}^E = e^{-\sqrt{3}\phi/2} \quad \text{finite at Sing!}$$

$$\phi + 3\dot{\phi} = -\frac{\beta_v}{M_{pl}} (p_v - \cancel{3}p_v) + \frac{\beta_c}{M_{pl}} p_c$$

$$\Rightarrow p_{c,e2} > p_\Lambda > \beta_v \underline{p_{v,nn}}$$

$$\frac{\beta_{ord} < 10^{-3}}{\text{STEP} \rightarrow \underline{< 10^{-6}}}$$

$$h \propto e^{-\sqrt{3}\phi}$$

$$g_{\mu\nu}^E = e^{-\sqrt{3}\phi} \quad \text{finite at Sing!}$$

$$\phi + 3\dot{\phi} = -\frac{\beta_v}{M_{pl}} (\rho_v - 3p_v)$$

$$+ \frac{\beta_c}{M_{pl}} p_c$$

$$\Rightarrow \rho_{c,e2} > \rho_\Lambda > \beta_v \underline{\rho_{v,nn}}$$

$$\frac{\beta_{ord} < 10^{-3}}{\text{STEP} \rightarrow < 10^{-6}}$$

$$a \propto e^{\dots}$$

$$g_{\mu\nu}^E = e^{-\sqrt{3}\phi} \quad \text{finite at Sing!}$$

$$\phi + 3(1)\dot{\phi} = -\frac{\beta_v}{M_{pl}} (p_v - 3p_v)$$

$$+ \frac{\beta_c}{M_{pl}} p_c$$

$$\Rightarrow \underline{p_{c,e2} > p_\Lambda > \beta_v p_{v,nn}}$$

$$\frac{\beta_{v,d} < 10^{-3}}{\text{STEP} \rightarrow < 10^{-6}}$$

$$h \propto e^{-\sqrt{\frac{2}{3}} \phi}$$

$$g_{\mu\nu}^E = e^{-\sqrt{\frac{2}{3}} \phi} \quad \text{finite at Sing!}$$

$$\phi + 3(1)\dot{\phi} = -\frac{\beta_v}{M_{pl}} (p_v - 3p_v)$$

$$+ \frac{\beta_c}{M_{pl}} p_c$$

$$\Rightarrow \left(p_{c,e2} \geq p_\Lambda > \beta_v p_{v,nn} \right)$$

$$M_\nu > 0.05 \text{ eV}$$

$$\frac{\beta_{ord} < 10^{-3}}{\text{STEP} \rightarrow < 10^{-6}}$$

$$h \propto e^{\sqrt{3}\phi}$$

$$g_{\mu\nu}^E = e^{-\sqrt{3}\phi} \quad \text{finite at Sing!}$$

$$\phi + 3(1)\dot{\phi} = -\frac{\beta_v}{M_{Pl}} (p_v - 3p_v)$$

$$+ \frac{\beta_c}{M_{Pl}} p_c$$

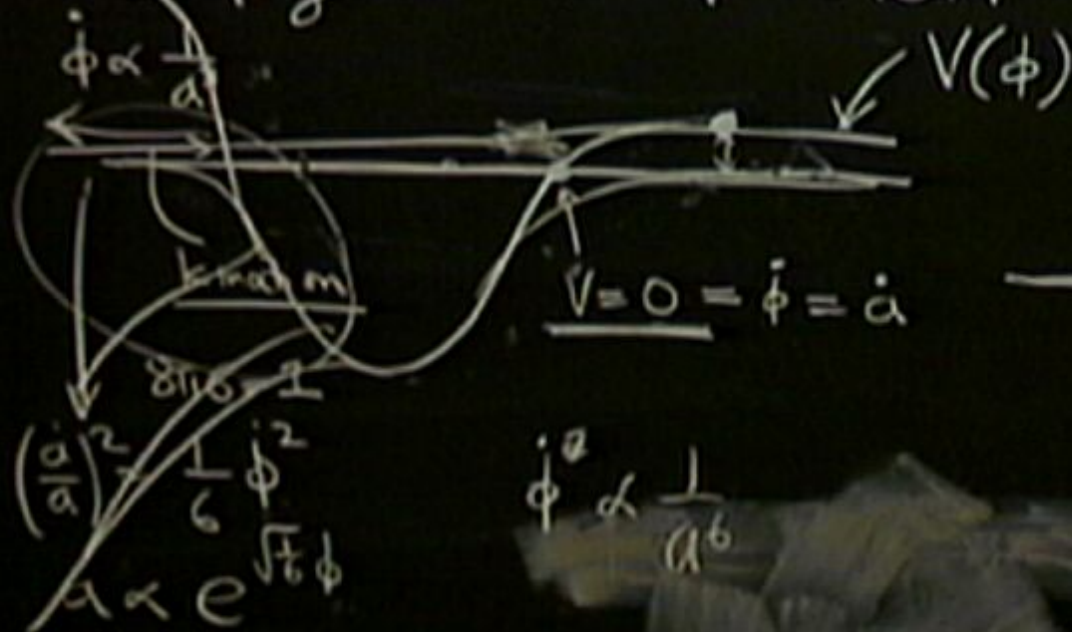
$$\Rightarrow \underbrace{p_{c,e2} \geq p_\Lambda > \beta_v p_{v,nn}}$$

$$M_\nu > 0.05 \text{ eV}$$

$$\frac{\beta_{ord} < 10^{-3}}{\text{STEP} \rightarrow < 10^{-6}}$$

Rube Goldberg?

Empty universe problem!



coincidence
problem

$$g_{\mu\nu}^{(4)} = e^{-\sqrt{\frac{1}{6}} \phi} \quad \text{finite at Sing!}$$

$$m_\nu \sim 0.05 \text{ eV}$$