Title: Inflation from axion monodromy

Date: May 22, 2009 02:00 PM

URL: http://pirsa.org/09050063

Abstract: TBA

Pirsa: 09050063

based on

McAllister, Silverstein & Westphal and some or all of

Flauger, McAllister, EP, Silverstein, Westphal & Xu

Enrico Pajer

Cornell University, Ithaca

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### Outline

- Motivations
- 2 Phenomenology of the effective model
- 3 A string theory model of axion monodromy
- Constraints and phenomenology
- 6 Conclusions

Page 6/141

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Page 9/141

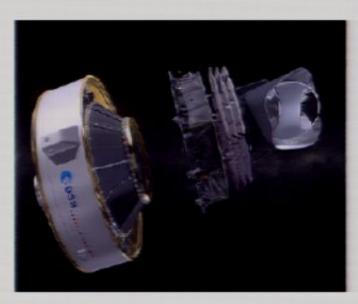
### Cosmological data

We are leaving in the golden age of observational cosmology: COBE goes to Stockholm, WMAP and ...



now Planck: "The satellite was successfully launched at 13:12:02 on 14 May 2009..."





### **UV-sensitivity**

EFT approach: learn about higher scales studying UV-sensitive observables.

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Page 11/141

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Page 12/141

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- In particle physics, e.g. proton lifetime constrains baryon-number-violating higher-dimension operators.
- Analogously, inflation is a UV-sensitive mechanism. E.g. Planck-suppressed dimension 6 operators (with natural coefficients) can and generically do spoil slow roll.
- If we invoke a symmetry, e.g. shift symmetry, we are sensitive to how and where it is broken.

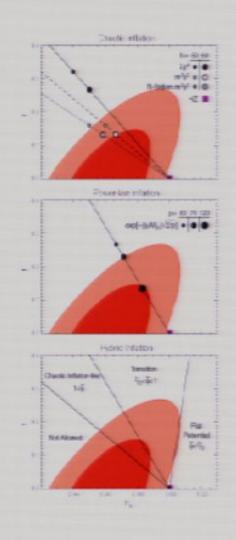
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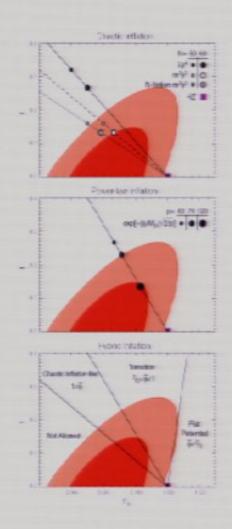


Page 14/141



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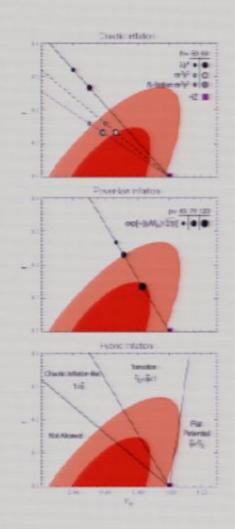
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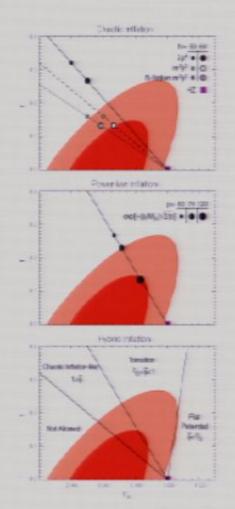


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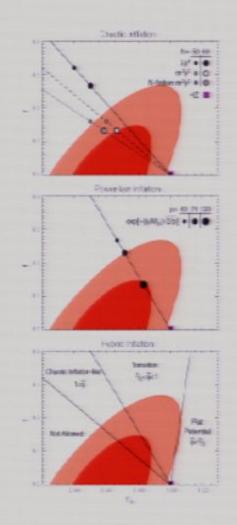


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- features in the scalar spectrum

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Inflation is driven by a real scalar field with potential

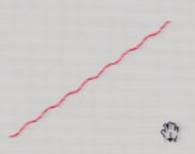
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Page 23/141

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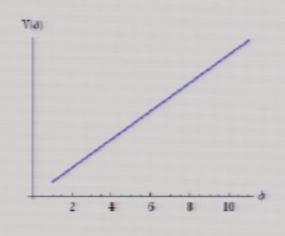
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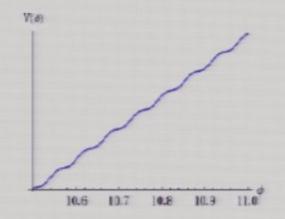
### Background evolution

We solve the e.o.m. perturbatively in b:



zeroth order

$$\phi_0 = \left(\phi_{in}^{3/2} - \frac{\sqrt{3}}{2}\mu^{3/2}t\right)^{2/3}$$



first order

$$\phi_1 \simeq -3bf^2 \phi_0 \sin\left(\frac{\phi_0}{f}\right)$$

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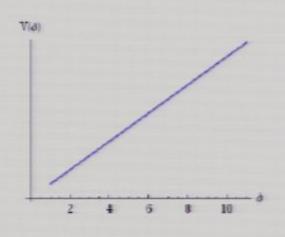
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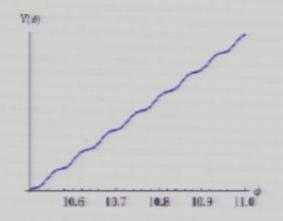
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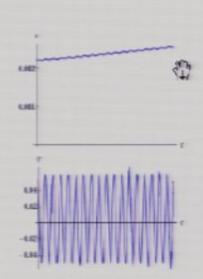
The (Hubble) slow-roll parameters oscillate

$$\epsilon \equiv -\frac{\dot{H}}{H^2} \simeq \epsilon_0 + \epsilon_{osci} \cos\left(\frac{\phi_0}{f}\right)$$

$$\simeq \frac{1}{2\phi_0^2} + \frac{3bf}{\phi_{in}} \cos\left(\frac{\phi_0}{f}\right)$$

$$\eta \equiv \frac{\dot{\epsilon}}{\epsilon H} \simeq \eta_0 + \eta_{osci} \sin\left(\frac{\phi_0}{f}\right)$$

$$\simeq 0 + 6b \sin\left(\frac{\phi_0}{f}\right)$$
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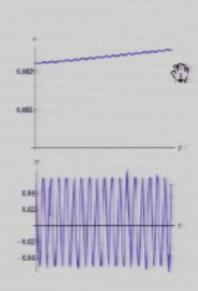
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Notice that  $\dot{\eta} \gg \epsilon$  so one can not use slow-roll formulae to compute the perturbations.

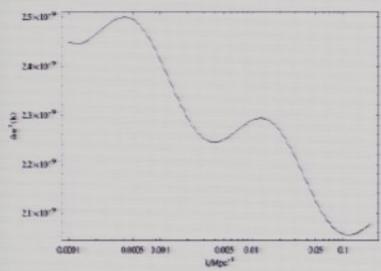
The oscialltions in the potential induce osciallations in the spectrum:

$$P_s(k) = A_s \left(\frac{k}{k_*}\right)^{n_s - 1} \left[1 + \delta n_s \cos\left(\frac{\phi_k}{f}\right)\right]$$
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Page 31/141

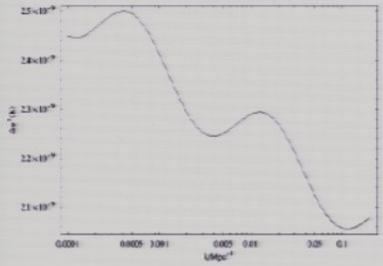
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- We have computed  $\delta n_s$ analytically at leading order in b

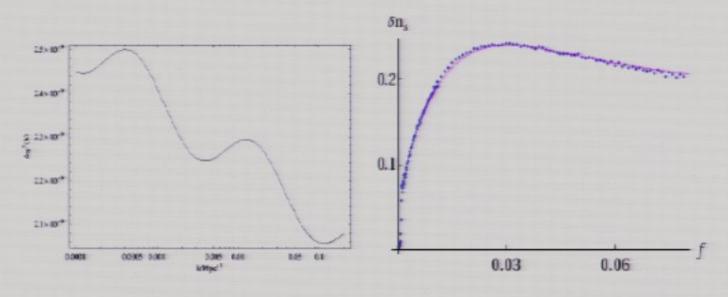
### Solution of the Mukhanov-Sasaki equation

Slow roll is not enough! We solve Mukhanov-Sasaki equation perturbatively in b.

The amplitude of oscillations in the spectrum is

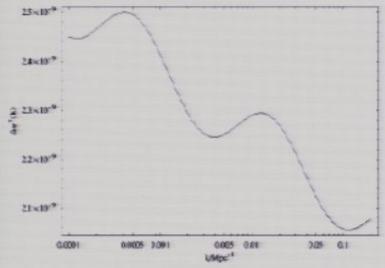
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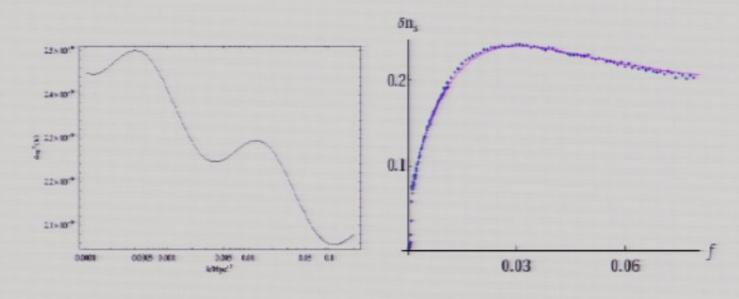
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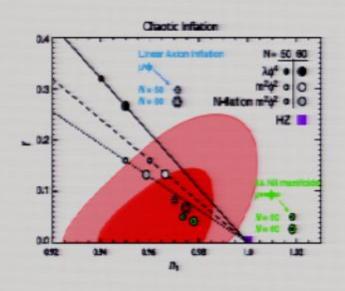
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### Large field model $\Rightarrow$ detectable tensor modes



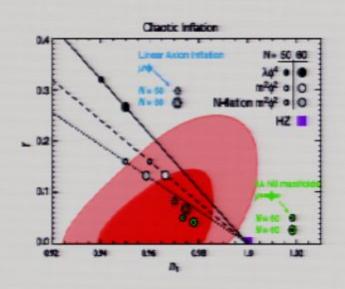
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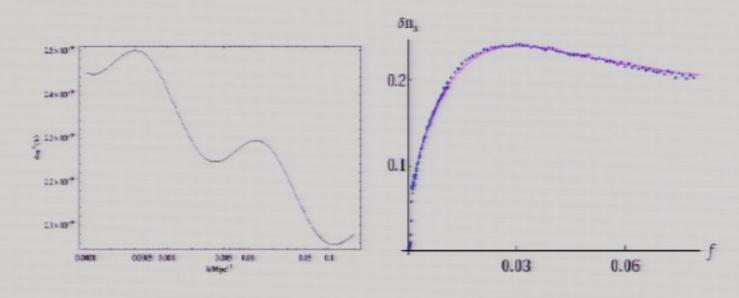
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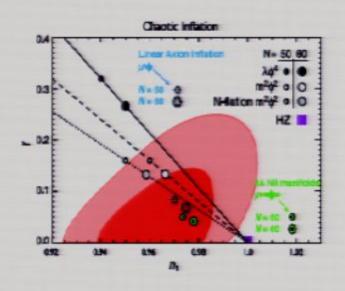
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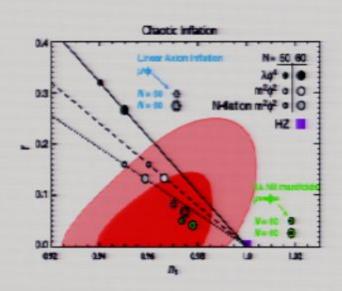
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Page 41/141

### Bispectrum of scalar perturbations

Canonical single-field slow-roll inflation gives  $f_{NL} \ll 1$  [Maldacena 03] , undetectable. In fact

$$<\zeta_{k_1}(t)\zeta_{k_2}(t)\zeta_{k_3}(t)> = -i\int_{t_0}^t dt' < \left[\zeta_{k_1}(t)\zeta_{k_2}(t)\zeta_{k_3}(t), H_I(t'_3)\right] >$$

where the intaracting Hamiltonian at order  $\zeta^3$  is

$$H_{I} = \int a\epsilon^{2}\zeta\zeta'^{2} + a\epsilon^{2}\zeta(\partial\zeta)^{2} - 2\epsilon\zeta'(\partial\zeta)(\partial\chi)$$

$$+ \frac{a}{2}\epsilon\dot{\eta}\zeta^{2}\zeta' + \frac{\epsilon}{2a}(\partial\zeta)(\partial\chi)(\partial^{2}\chi) + \frac{\epsilon}{4a}(\partial^{2}\zeta)(\partial\chi)^{2},$$

$$\chi \equiv a^{2}\epsilon\partial^{-2}\dot{\zeta}$$

Page 42/141

## Resonant enhancement of non-Gaussianity

Condition for the resonance

Schematically [Chen, Easther & Lim 08]

$$\zeta_k = u_k a_k^{\dagger} + u_k^* a_{-k}$$

$$< \zeta^3 > \sim u^3 \int \epsilon^2 u^3 + \epsilon \dot{\eta} u^3 + \dots$$
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### Necessary condition

$$H < \omega < M_{pl}$$
,

where  $\omega$  is the (instant) frequency of oscillation of  $\epsilon$ ,  $\eta$ .

A good fit to the numerical computations is [Chen, Easther & Lim 08]

$$<\zeta_{k_1}\zeta_{k_2}\zeta_{k_3}> = (2\pi)^7 \delta^3(K) \frac{P^2}{(k_1k_2k_3)^2} f_{res} \sin\left(\frac{2\log(K)}{\phi f}\right)$$

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$$<\zeta_{k_1}\zeta_{k_2}\zeta_{k_3}> = (2\pi)^7\delta^3(K)\frac{P^2}{(k_1k_2k_3)^2}f_{res}\sin\left(\frac{2\log(K)}{\phi f}\right)$$

A

The size of the resonant non-G is

$$f_{res} \simeq \frac{9}{4} \frac{b}{(f\phi)^{3/2}}$$

$$= \frac{9}{4} b \left(\frac{\omega}{H}\right)^{3/2}$$

- Liner in b as for the spectrum
- Inversely proportional to  $f^{3/2}$
- Oscillations appear at all scales, both in spectrum and in the bispectrum
- Such non-scale-invariant signal has not yet been compared with the data.

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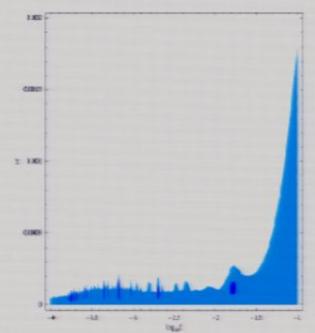
Page 56/141

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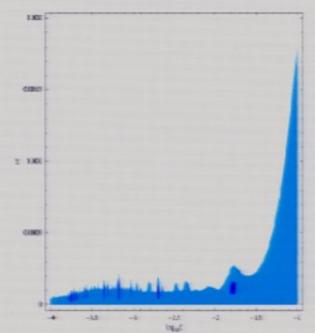
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We are going to present a possible embedding of this effective model in string theory and address the above questions.

• Axions are scalar fields with only derivative couplings and might arise e.g. from the breaking of a U(1) symmetry [Peccei & Quinn 77]



Page 68/141

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- Continuous shift symmetry is broken to a discrete shift symmetry by non-perturbative effects
- The axion decay constant f determines the periodicity of the canonically normalized axion

$$\mathcal{L} \supset \frac{1}{2} (\partial \phi)^2 + \Lambda^4 \cos \left(\frac{\phi}{f}\right) \Rightarrow \phi(x) \to \phi(x) + 2\pi f$$

### Outline

- Motivations
- Phenomenology of the effective model
- 3 A string theory model of axion monodromy
- Constraints and phenomenology
- Conclusions

String theory seen from a low energy 4D observer has in general many axions:

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- The axion decay constant f is determined by geometrical data of the compactification

# Shift symmetry

Consider the 4D axion b(x) from  $B_{ij} = b(x)\omega_{ij}$  for some internal two-form  $\omega$ . In (bosonic) closed string theory, the vertex operator for b particles at zero momentum integrated over the world-sheet is

$$V(k=0) = \int_{ws} d^2 \sigma \epsilon^{\alpha \beta} \partial_{\alpha} X^i \partial_{\beta} X^j \omega_{ij} b = \int_{ts} B \qquad \textcircled{2}$$

In perturbation theory the world-sheet wraps a topologically trivial cycle in the target space, hence V(0) = 0, i.e. no non-derivative coplings.

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- Non-perturbative effects
- World sheet with boundaries, i.e. D-branes

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Page 81/141

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# Linear potential for the inflaton

The shift symmetry can be broken in the presence of boundaries.

Consider a D5-brane wrapped on a two-cycle  $\Sigma$ . The DBI action

$$-T_5 \int d^5x e^{-\Phi} \sqrt{\det\left(G^{ind} + B^{ind}\right)}$$



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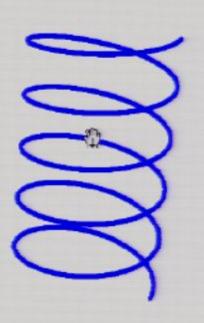
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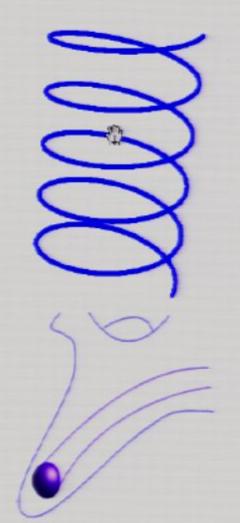
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The shift  $b(x) \to b(x) + \text{const of } b(x) = \int_{\Sigma} B_2$  stores some potential energy.

$$V(b) = T_5 \sqrt{L^4 + b^2} \sim T_5 b$$
 for large  $b$ 

This generates the linear inflaton potential (and break SUSY). COBE normalization and control require to red-shift  $T_5$ 



gravity multiplet	1	g <sub>pe</sub>
vector multiplets	$h_{+}^{(2,1)}$	$V^{\kappa}$
chiral multiplets	$h_{-}^{(2,1)}$	-k
	1	(0.!)
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Page 92/141

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#### Supermultiplets

$$G^{a} \equiv 2\pi \left(c^{a} - i\frac{b^{a}}{g_{s}}\right),$$

$$T_{\alpha} \equiv i\rho_{\alpha} + \frac{1}{2}c_{\alpha\beta\gamma}v^{\beta}v^{\gamma} + \frac{g_{s}}{4}c_{\alpha b c}G^{b}(G - \bar{G})^{c},$$

The tree-level Kähler potential and superpotential

$$K = -2\log \mathcal{V}_E = -2\log \left[ \frac{1}{6} c_{\alpha\beta\gamma} v^{\alpha}(T, G) v^{\beta}(T, G) v^{\gamma}(T, G) \right]$$

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 $c^a$  and  $b^a$  enjoy a shift symmetry (world-sheet argument). Næscale structure of  $K \Rightarrow T_\alpha$  are not stabilized.

Page 95/141

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Page 97/141

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which stabilize  $T_{\alpha}$  [Kachru et al. 03] .

63 Page 98/141

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### Non-perturbative breaking of shift symmetry

Non-perturbative effects could spoil the shift symmetry. In fact they induce an  $\eta$ -problem for  $b^a$ , analogous to D3-brane inflation.

### Moduli stabilization

The supersymmetric conditions ensuring a minimum are

$$0 = D_{\alpha}W = -A_{\alpha}a_{\alpha}e^{-a_{\alpha}T_{\alpha}} - W\frac{v^{\alpha}}{2V_{E}},$$

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Page 100/141

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- c<sup>a</sup> still enjoy a shift symmetry

### Non-perturbative breaking of shift symmetry

It is crucial to know what, how and when breaks the shift symmetry. Moduli stabilization á la KKLT is incompatible with  $b^a$  shift symmetry.

# The axion decay constant

Which values can f take? Direct KK reduction from  $C_2 = c(x)\omega/2\pi$  gives

$$\frac{f^2}{M_{pl}^2} = \frac{g_s \pi^2}{3 \mathcal{V}_E} \left( \frac{\int \omega \wedge *\omega}{(2\pi)^{10} (\alpha')^3} \right) \propto \frac{L_c^2}{\mathcal{V}_E}.$$



Page 103/141

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#### Axion decay constant in string theory

The axion decay constant is given in terms the intersection numbers, geometrical data of the compact manifold.

Page 105/141

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### Constraints from the moduli stabilization

A series of constraints follow from consistency and computability



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$$\Rightarrow g_s \ll 1$$

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$$\Rightarrow v^{\alpha} > \frac{1}{\pi \sqrt{g_s}}$$



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small coupling 
$$\Rightarrow g_s \ll 1$$

small world-sheet instantons 
$$\Rightarrow v^{\alpha} > \frac{1}{\pi \sqrt{g_s}}$$

no higher instantons 
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, with  $N_{\alpha} \lesssim 50$  D7-branes

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Page 117/141

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Page 120/141

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 D-term corrections (W) should be holomorphic. They can arise from instantons with two fermionic zero modes It is still controversial if such instantons exist.

The result of the moduli stabilization is

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Page 126/141

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#### Outline

- Motivations
- Phenomenology of the effective model
- A string theory model of axion monodromy
- Constraints and phenomenology
- 6 Conclusions

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Page 133/141

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Page 134/141

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Page 135/141

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Page 137/141

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