

Title: Composite pairing in the new "high Tc" Heavy Fermion Superconductors

Date: Apr 23, 2009 09:00 AM

URL: <http://pirsa.org/09040021>

Abstract: The discovery in 1996 of superconductivity at 0.2K near a magnetic quantum phase transition in CeIn<sub>3</sub> opened a new dynasty of superconducting heavy electron materials, with many peculiar parallels to cuprate superconductors. In 2000, the introduction of additional layers of XIn<sub>2</sub>, led to the discovery of the so-called "115" superconductors, with a tenfold increase in T<sub>c</sub>[1]. By 2002, the replacement of Ce by Pu, drove the T<sub>c</sub> up by an additional order of magnitude to 18.5K[2]. The recent discovery of a second material in this family has further deepened the mystery. In this talk I'll discuss the two newest "high temperature" heavy fermion superconductors in this series: PuCoGa<sub>5</sub> and NpPd<sub>2</sub>Al<sub>5</sub>. These materials radically challenge the way we think about strongly correlated superconductivity. The way these materials directly transition from Curie paramagnets into anisotropic superconductors suggests a central role of spin as a driver for heavy electron superconductors - not just as the pairing glue - but as the basic fabric of the condensate. Motivated by these new materials, I'll discuss a model for superconductivity in the highest temperature superconductors in which the superconducting condensate involves formation of composite pairs between spins and conduction electrons[3]. Using this idea, we'll discuss how the physics of superconductivity and the Kondo effect can be combined, giving rise to a composite pairing model for the new superconductors. [1]H. Hegger, C. Petrovic, E. G. Moshopoulou, M. F. Hundley, J. L. Sarrao, Z. Fisk, and J. D. Thompson, "Pressure-Induced Superconductivity in Quasi-2D CeRhIn<sub>5</sub>" Phys. Rev. Lett. 84, 4986-4989 (2000). [2]J. L. Sarrao et al. , "Plutonium-based superconductivity with a transition temperature above 18 K", Nature (London) 420, 297-299 (2002). [3] Rebecca Flint, M. Dzero, P. Coleman, "Heavy electrons and the symplectic symmetry of spin.", Nature Physics 4, 643 - 648 (2008).Nature Physics, '

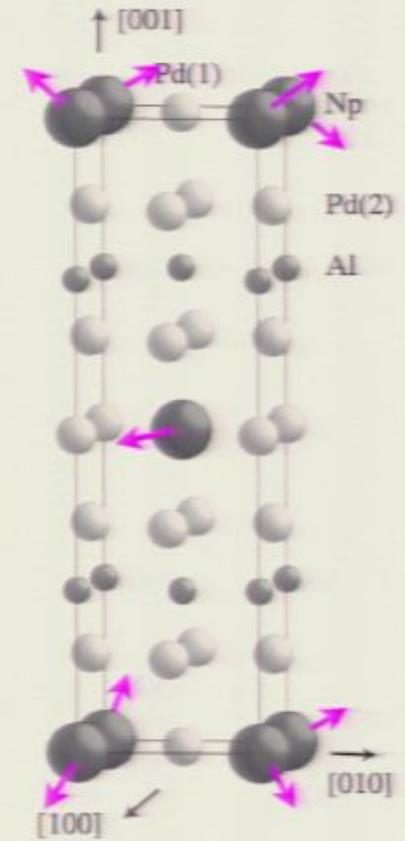
# Superconductivity in the newest generation of Heavy Electron Superconductors: $\text{PuCoGa}_5$ & $\text{NpAl}_2\text{Pd}_5$

4-corners CM Symposium  
PI, Waterloo, April 2009

M. Dzero  
R. Flint  
P. Coleman

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4.5K Heavy Fermion S.C.  
 $\text{NpAl}_2\text{Pd}_5$



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Nature Physics  
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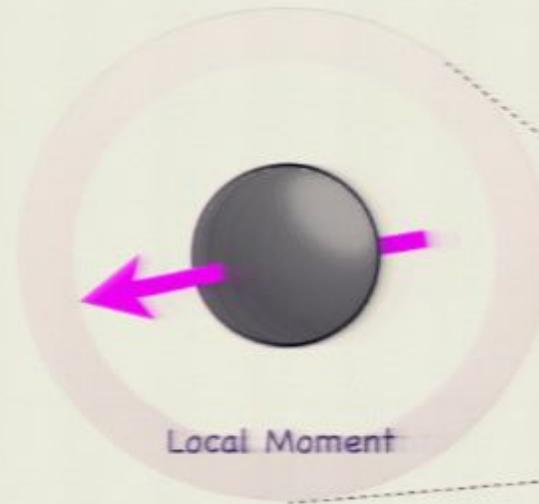
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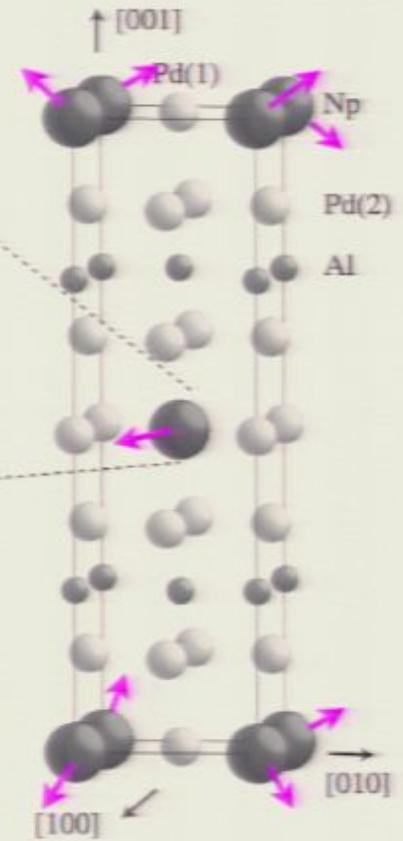
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Local Moment



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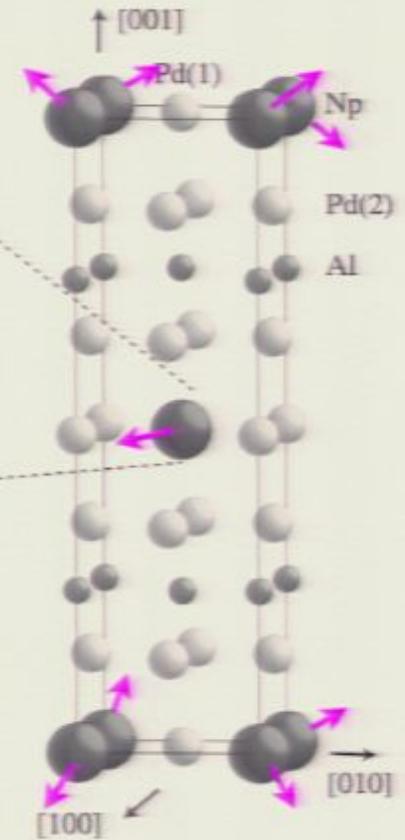
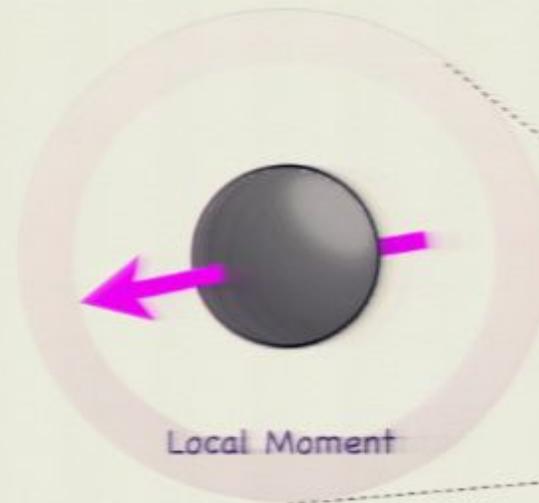
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- New Superconductors
- Composite pairs



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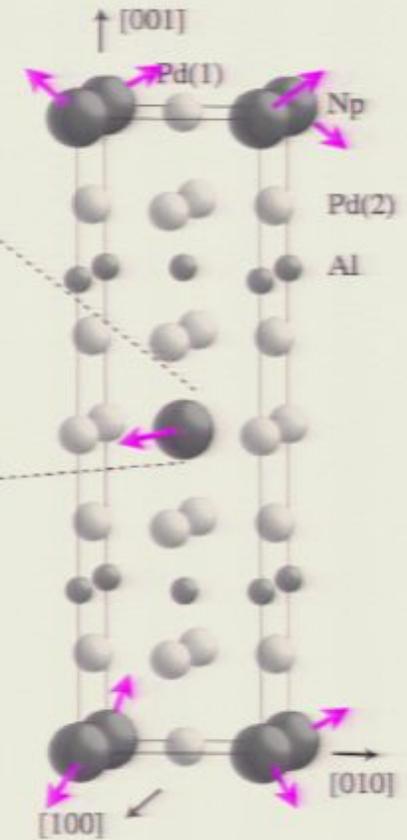
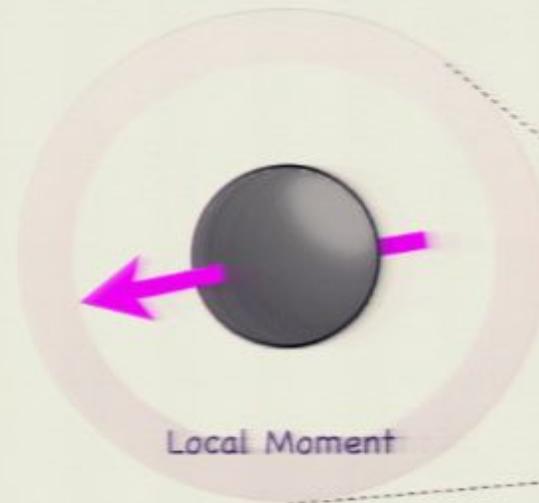
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- Application to the Kondo lattice



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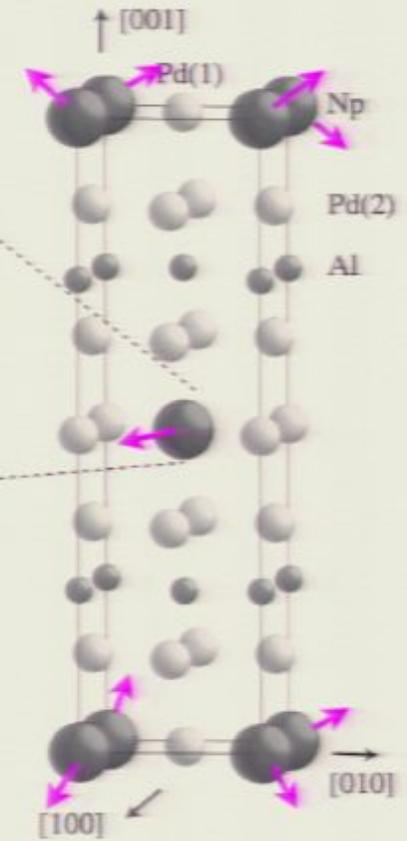
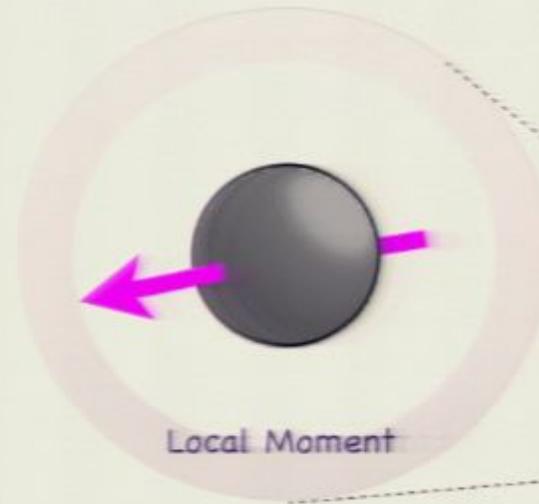
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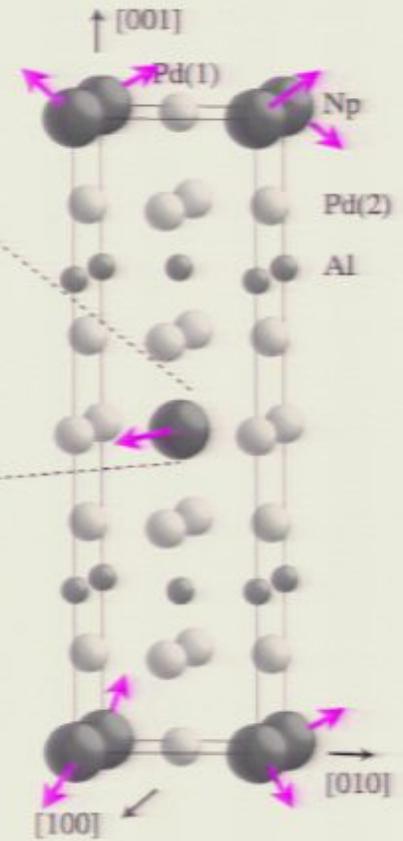
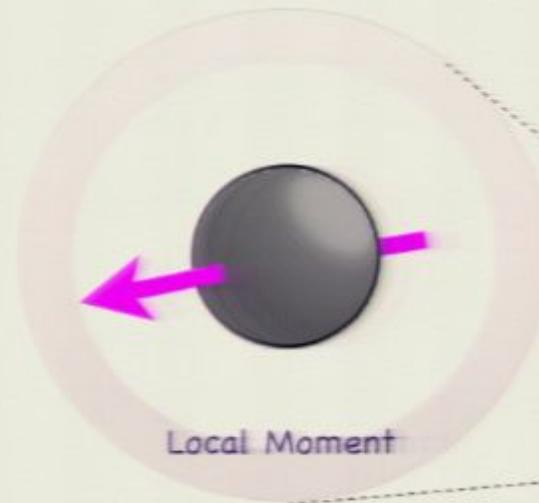
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Center for Materials Theory

- New Superconductors
- Composite pairs
- Symplectic symmetry of spin
- Application to the Kondo lattice
- Predictions



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# Acknowledgments:

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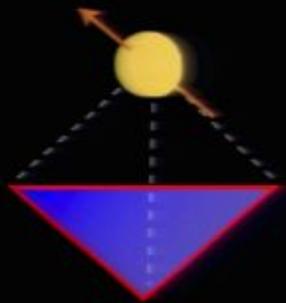
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Natan Andrei (Rutgers)

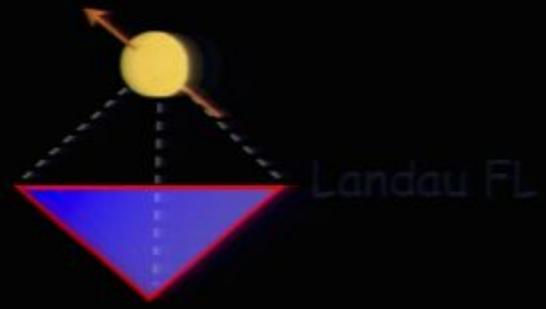
Hae Young Kee (Toronto)

PRB **60**, 3609, (1998).

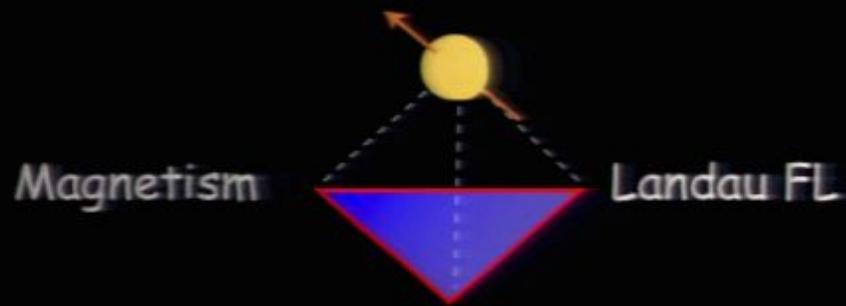
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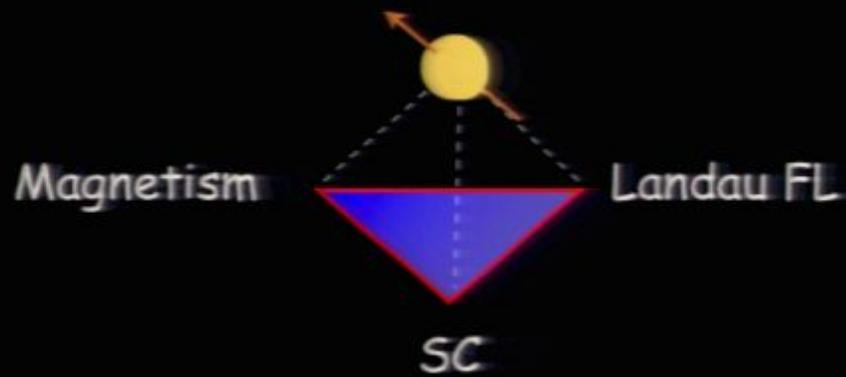
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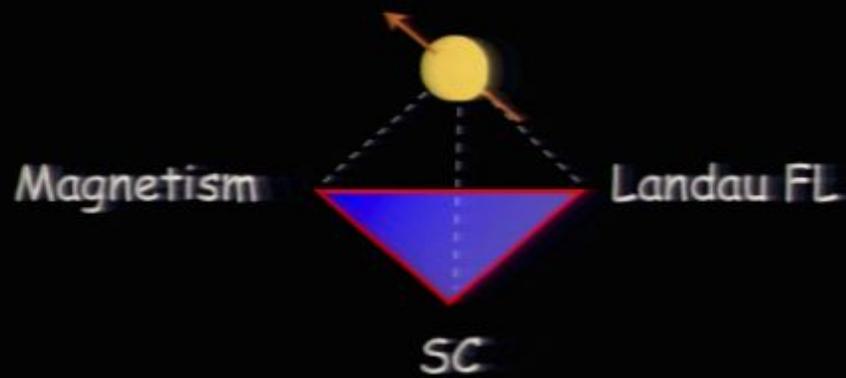
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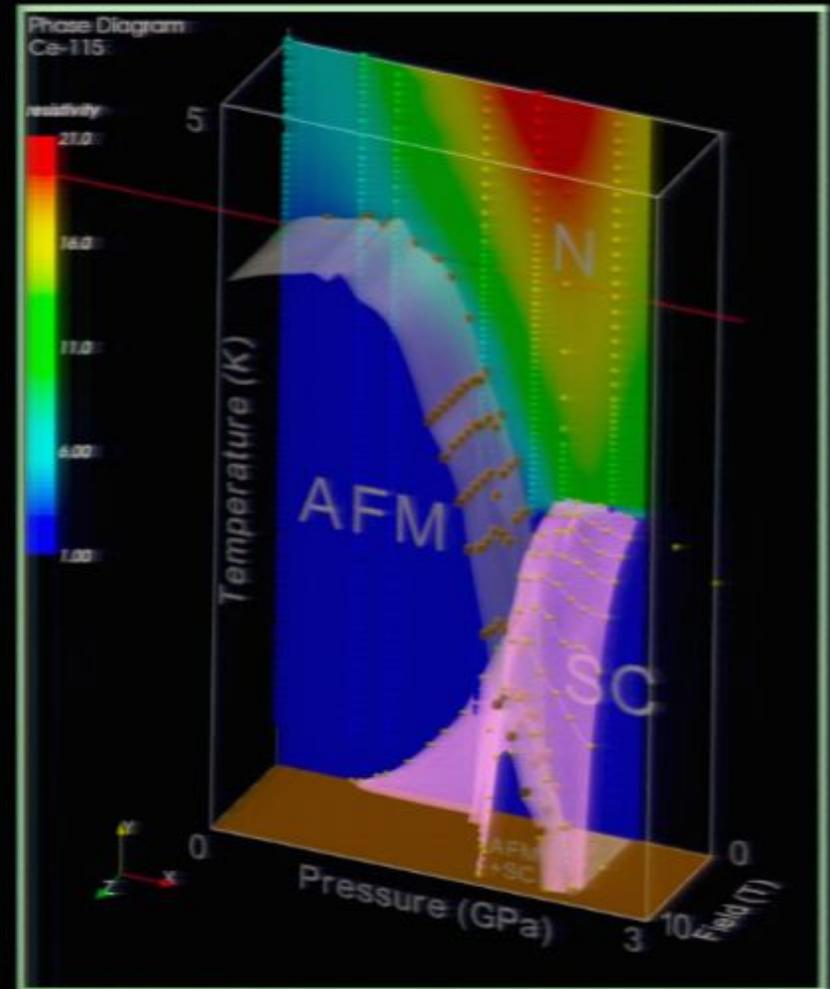


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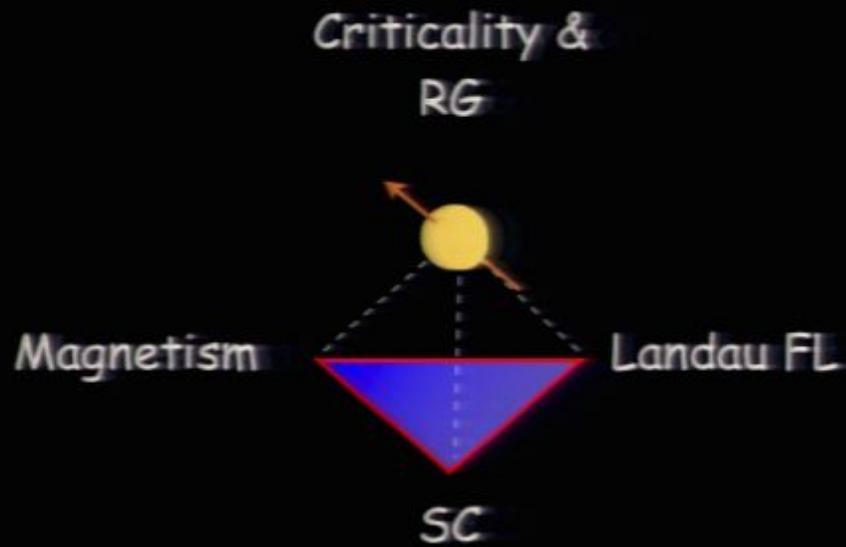


Tuson Park, (2007).

CeRhIn<sub>5</sub>

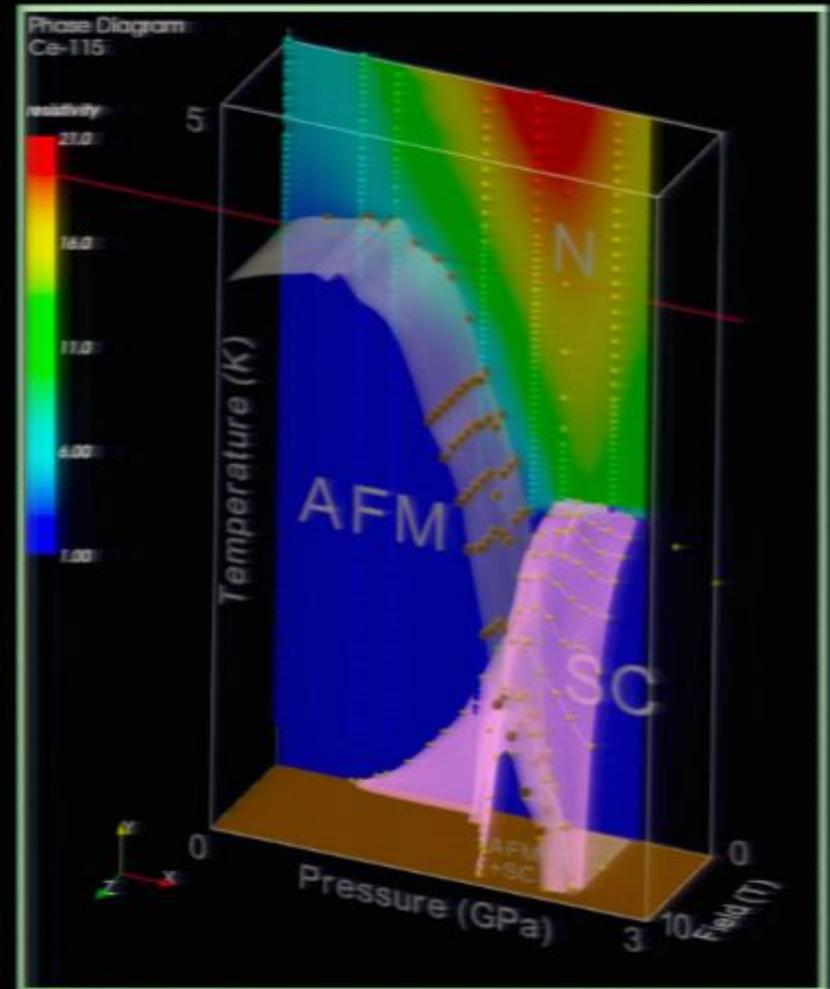


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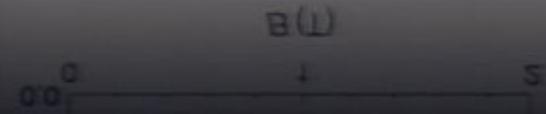
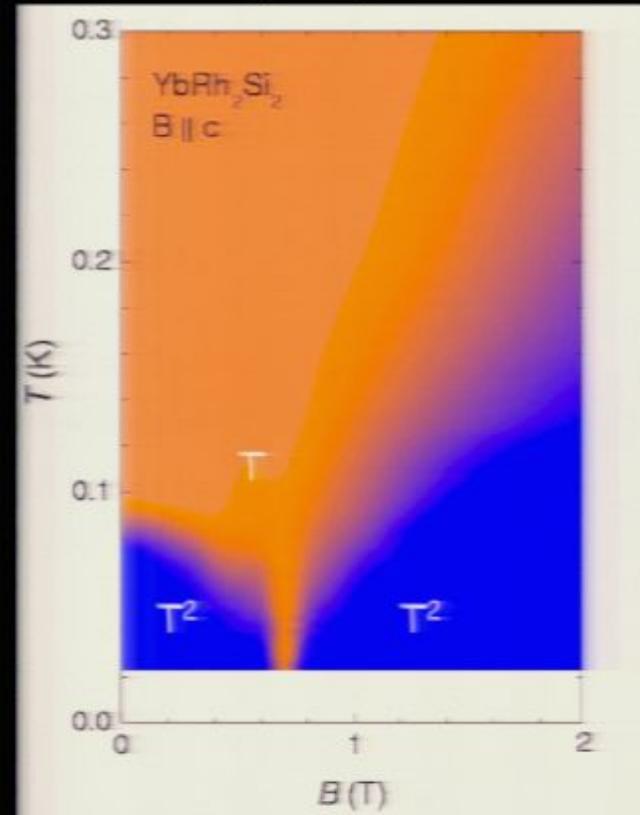


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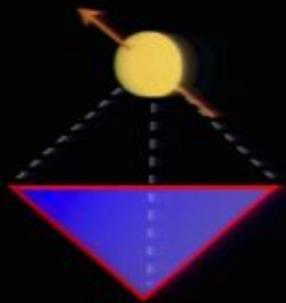
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Custers et al (2003)



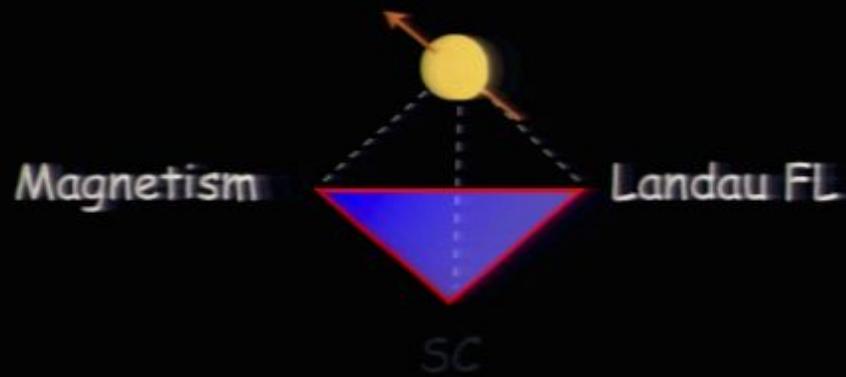
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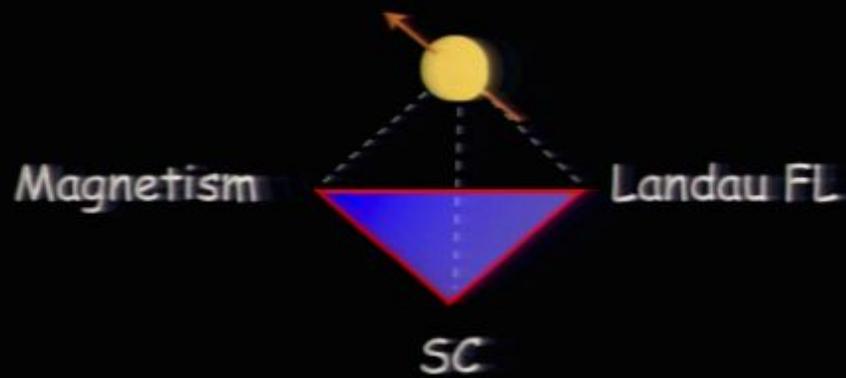
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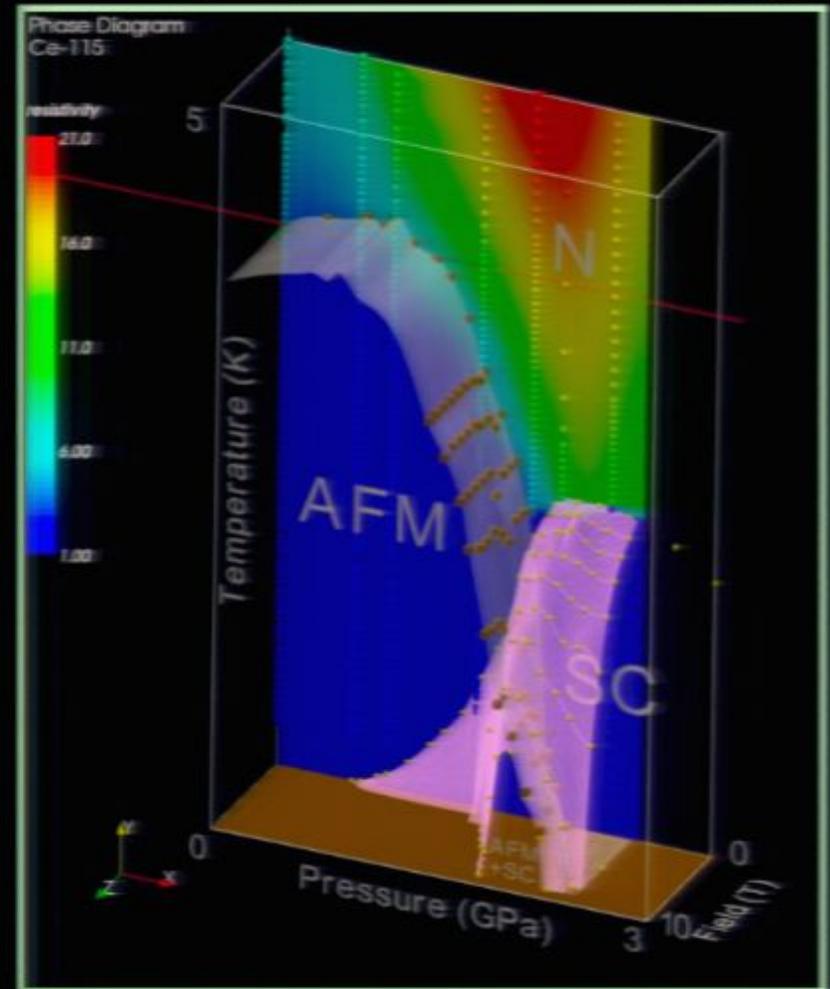


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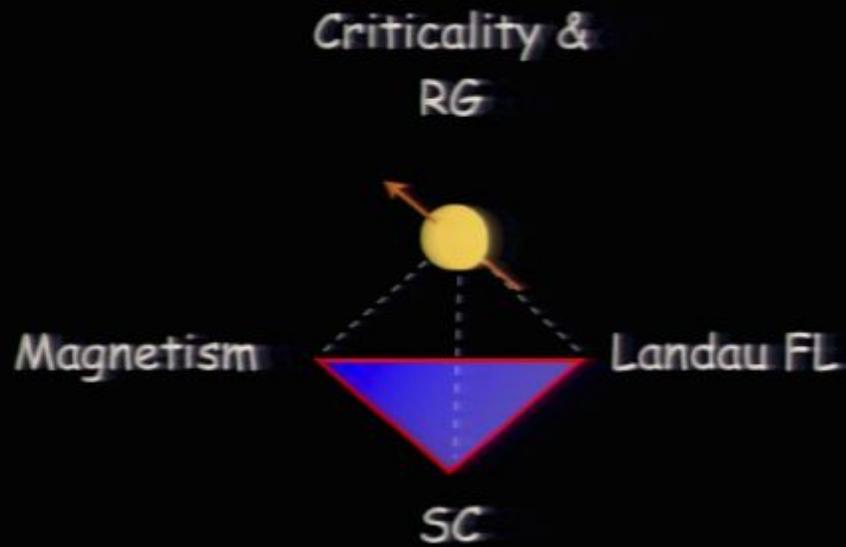


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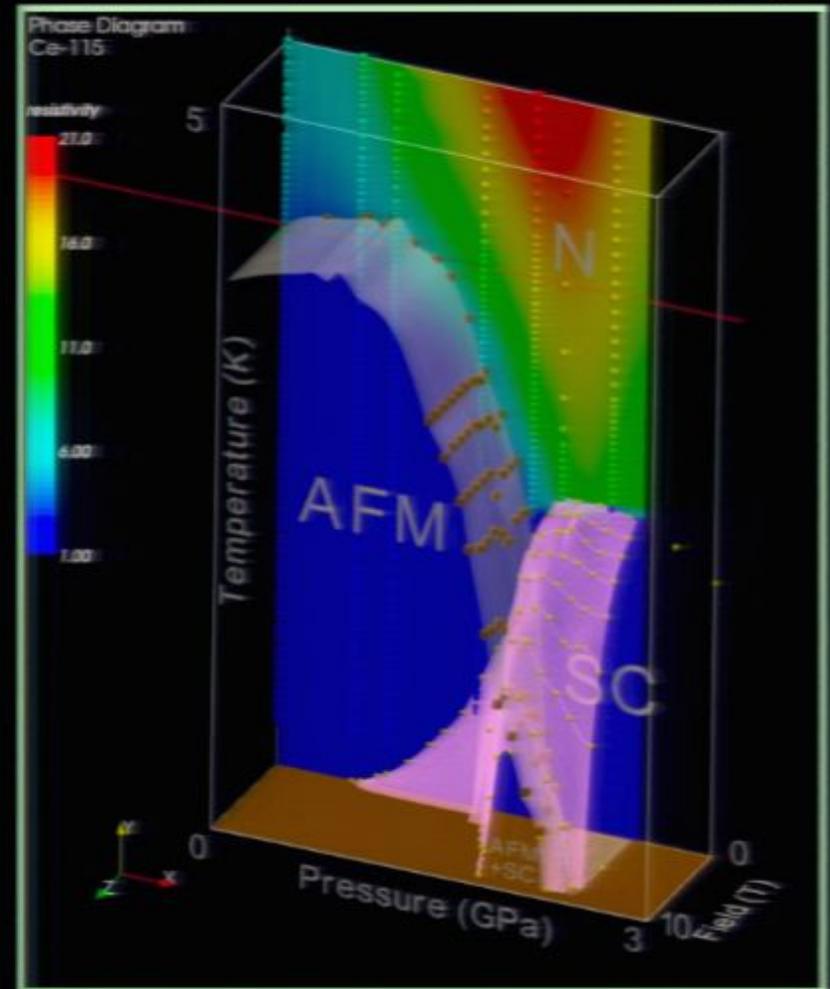


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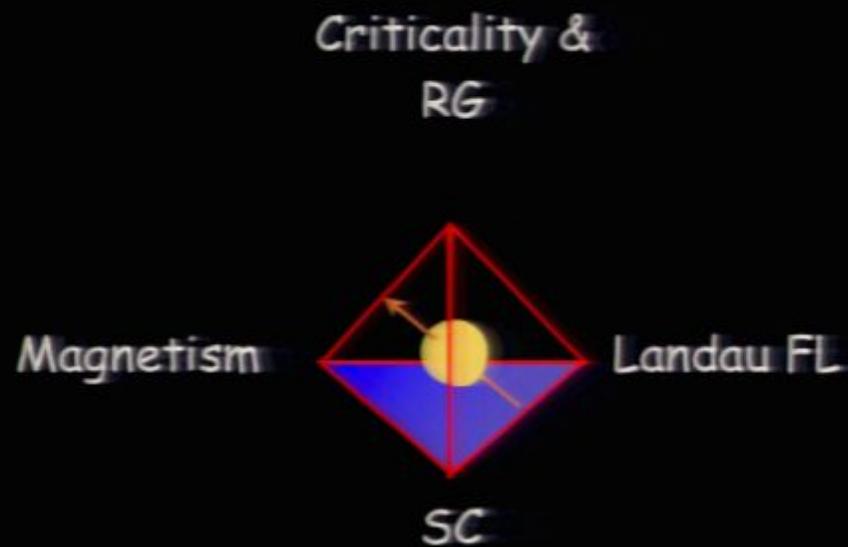


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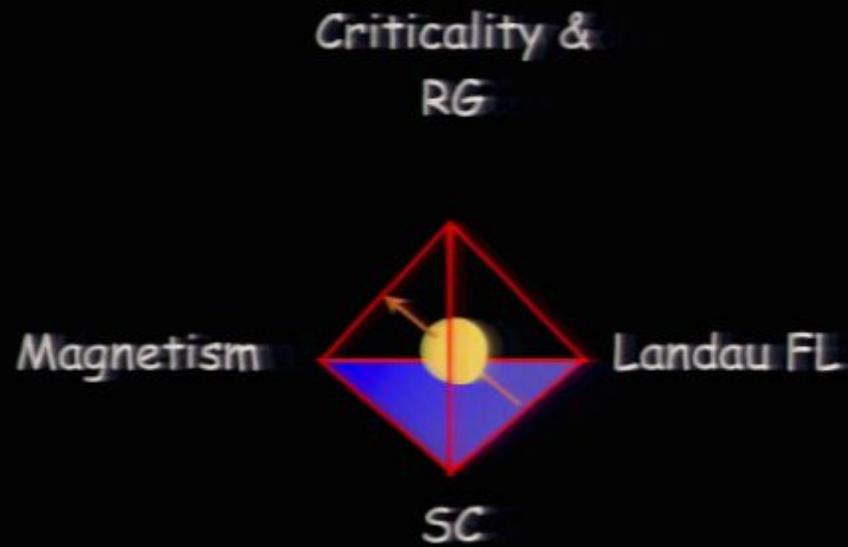
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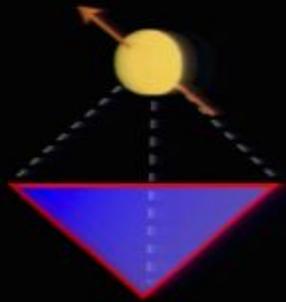
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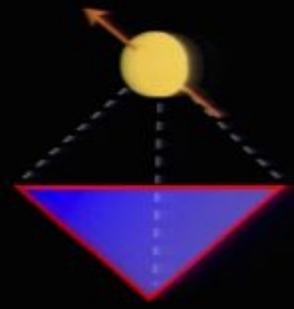
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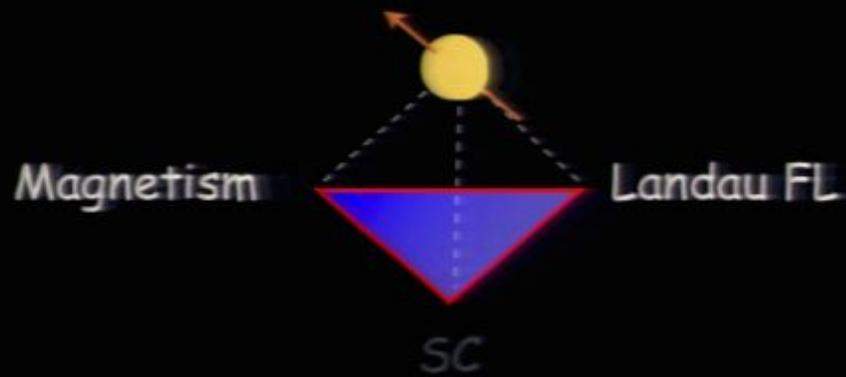
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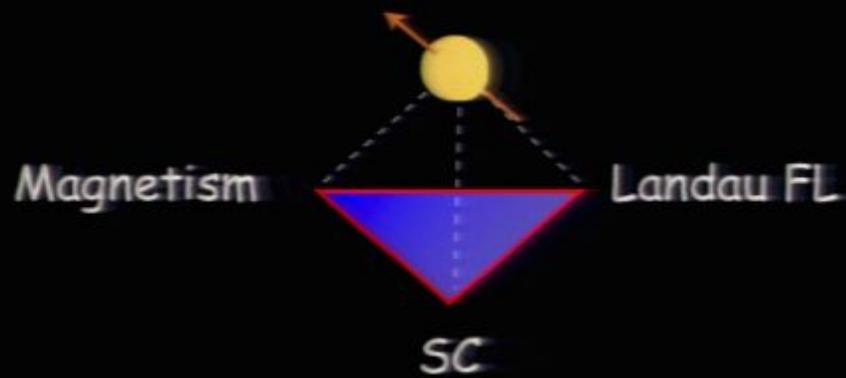
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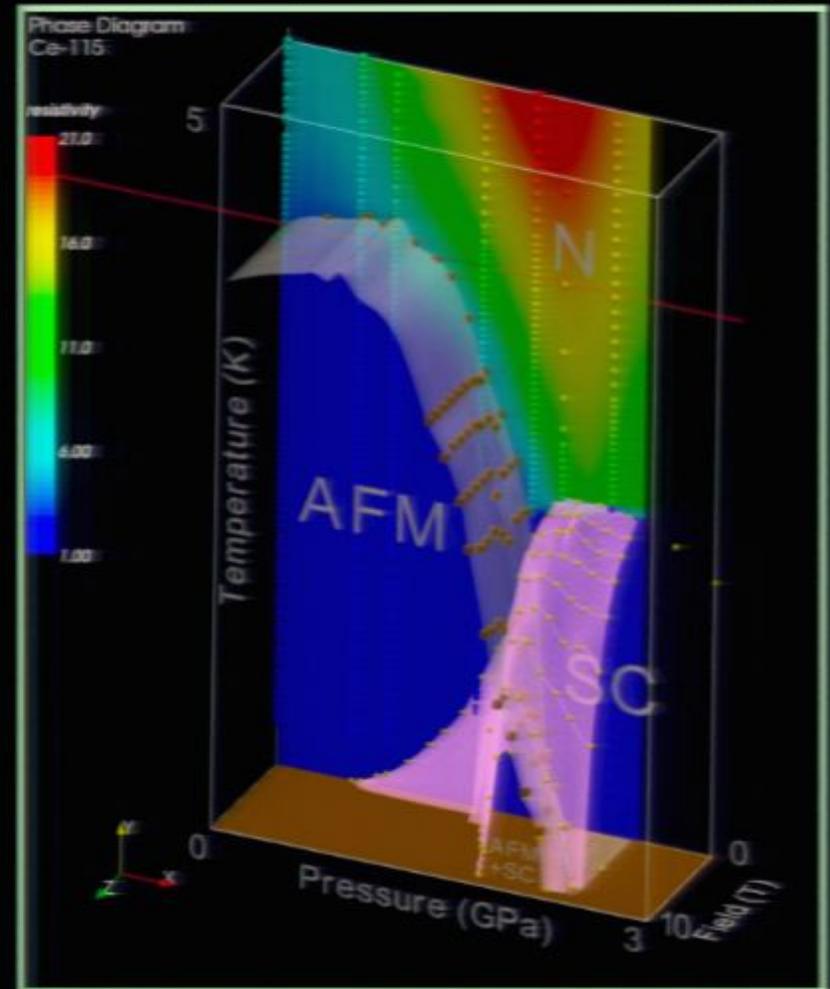


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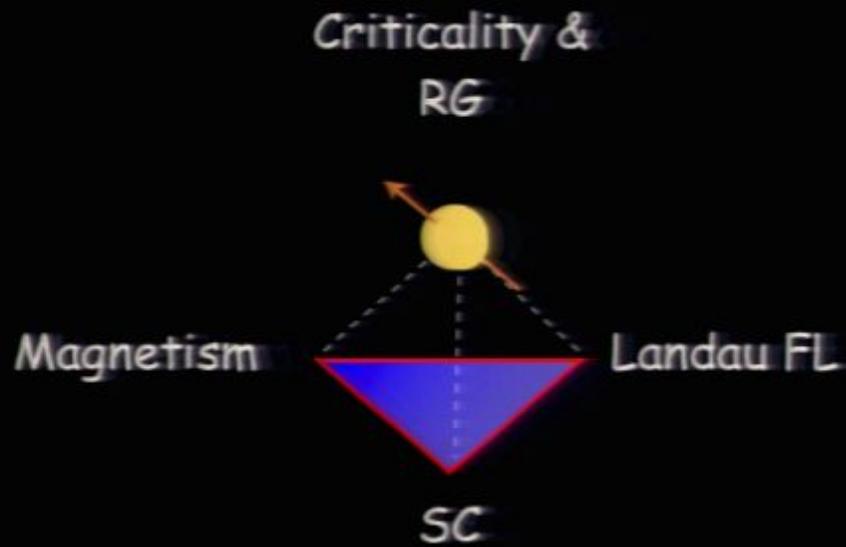


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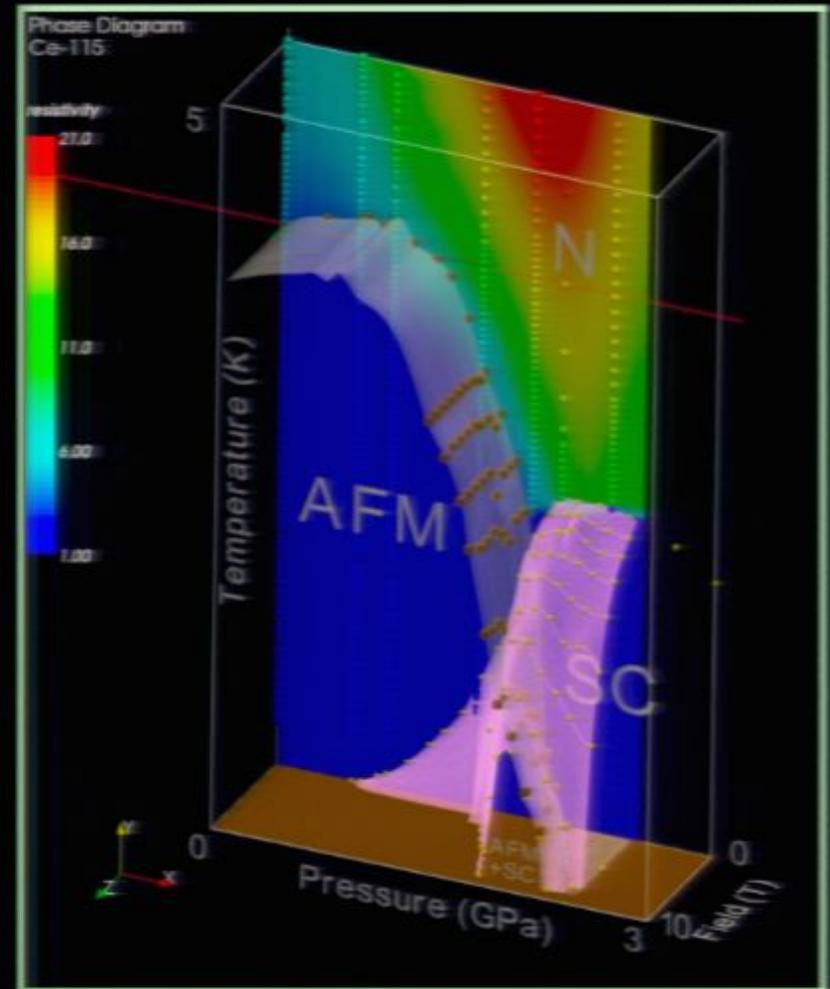


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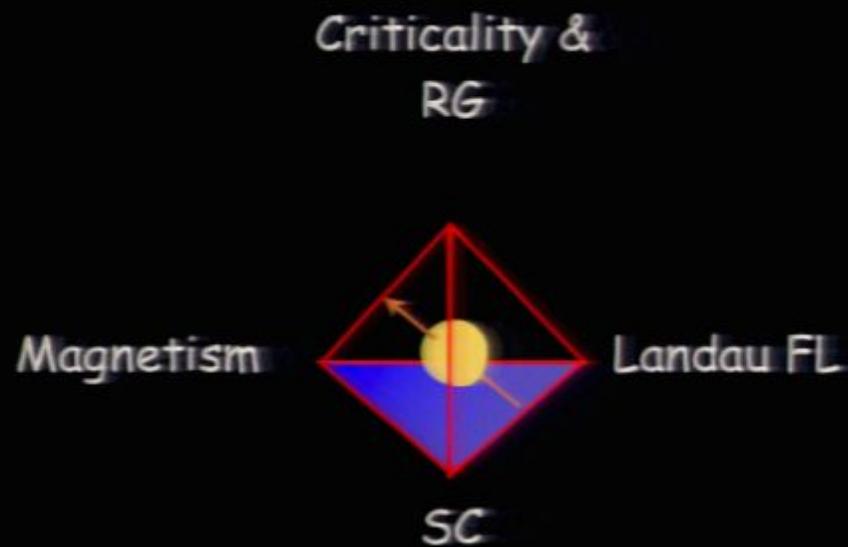


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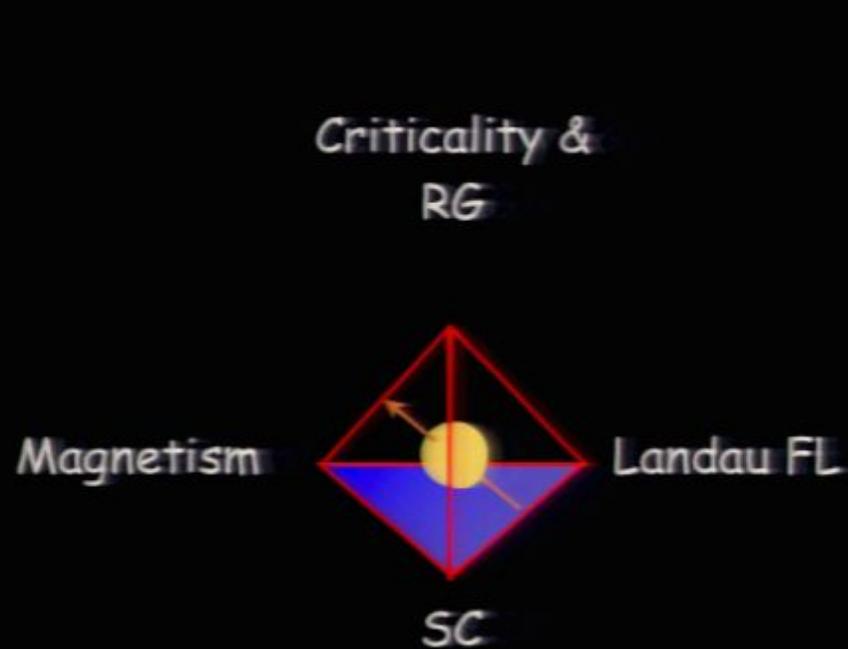
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Oxides

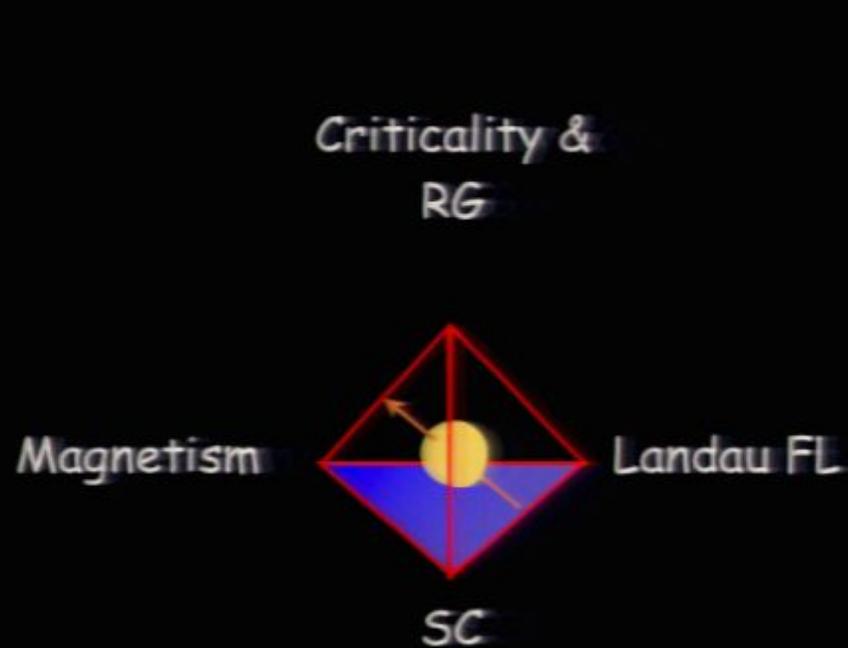
$T_c$

?

YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> 92K

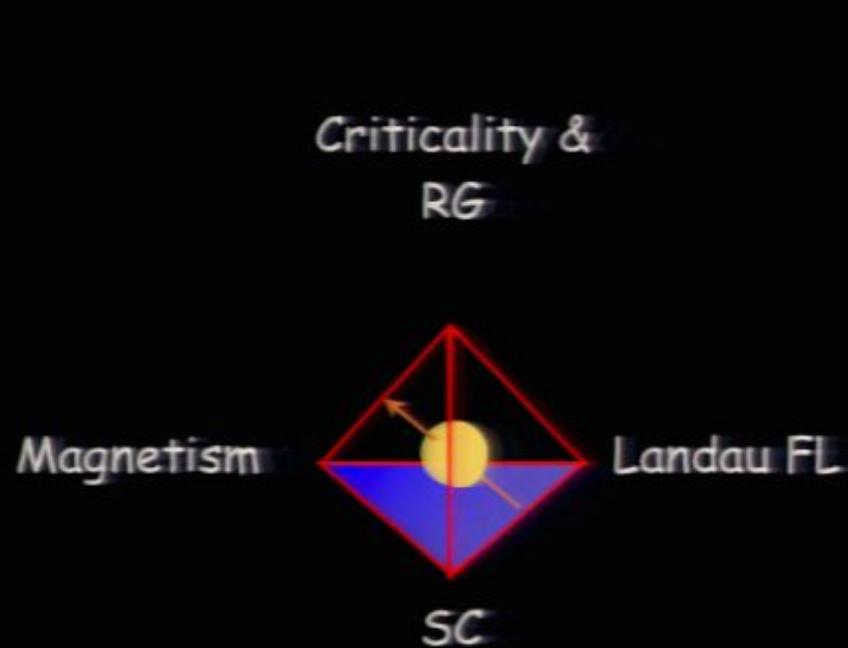
Ba2201 12K

# Heavy Fermions: Collision of ideas



| Oxides  | $T_c$ | Intermetallics | $T_c$                         |
|---|-------|----------------|-------------------------------|
| ?   |       |                |                               |
| <u>YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub></u> | 92K   | 2K             | <u>CeCoIn<sub>5</sub></u> '01 |
| <u>Ba2201</u>                                     | 12K   | 0.2K           | <u>CeIn<sub>3</sub></u> '96   |

# Heavy Fermions: Collision of ideas



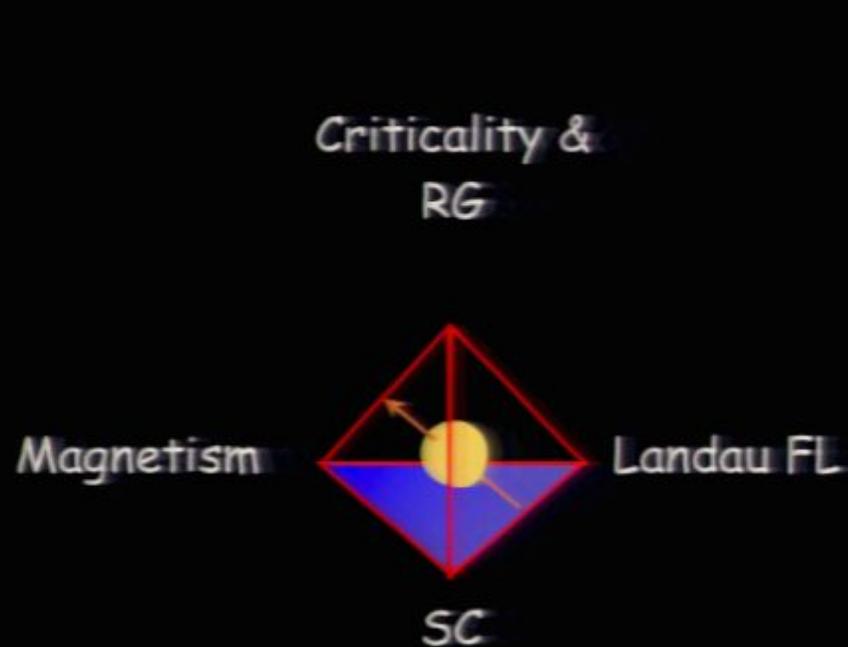
| Oxides  | Intermetallics                      |
|---|-------------------------------------|
| $T_c$   | $T_c$                               |
| ?   | 18.5K <u>PuCoGa<sub>5</sub></u> '02 |
| <u>YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub></u> 92K | 2K <u>CeCoIn<sub>5</sub></u> '01    |
| <u>Ba2201</u> 12K                                     | 0.2K <u>CeIn<sub>3</sub></u> '96    |

# Heavy Fermions: Collision of ideas



"Fruit fly" for correlated materials

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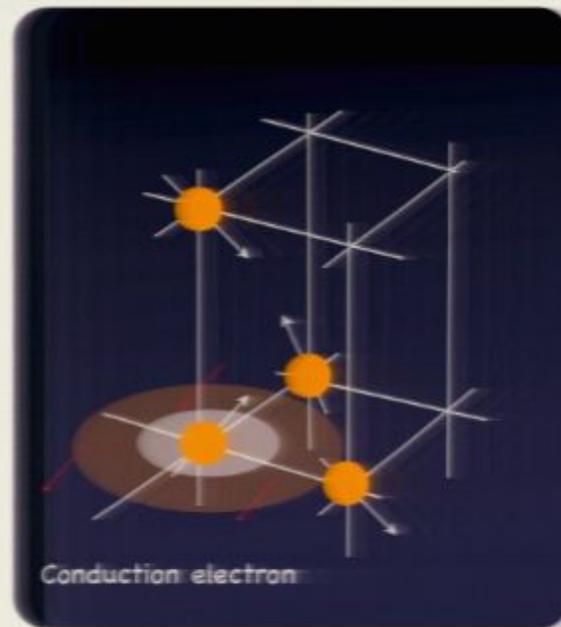
| Oxides  | $T_c$ | Intermetallics                             | $T_c$ |
|---|-------|--|-------|
| ?   |       | 18.5K <u>PuCoGa<sub>5</sub></u>            | '02   |
|   |       | 4.5K <u>NpAl<sub>2</sub>Pd<sub>5</sub></u> | '07   |
| <u>YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub></u> | 92K   | 2K <u>CeCoIn<sub>5</sub></u>               | '01   |
| <u>Ba2201</u>                                     | 12K   | 0.2K <u>CeIn<sub>3</sub></u>               | '96   |

"Fruit fly" for correlated materials

New superconductors

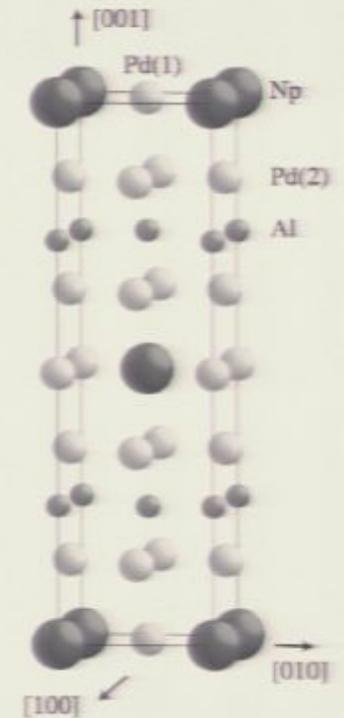
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J. Sarrao et al., Nature 420, (2002)



18K Heavy Fermion S. C.  
 $\text{PuCoGa}_5$

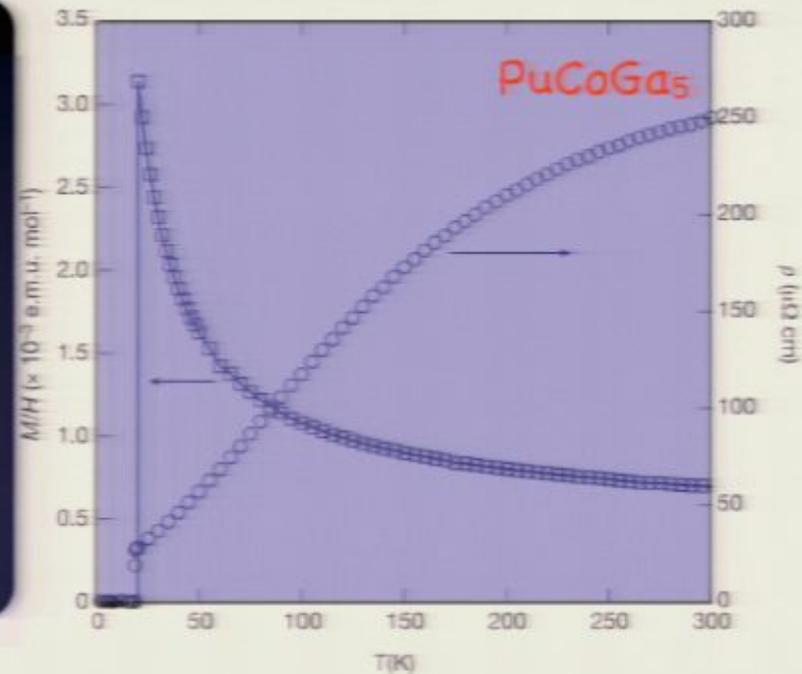
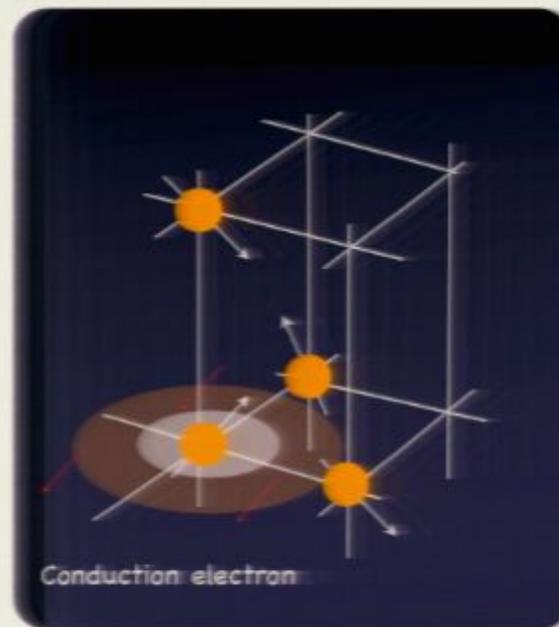
D. Aoki et al., JPSJ 76 (2007)



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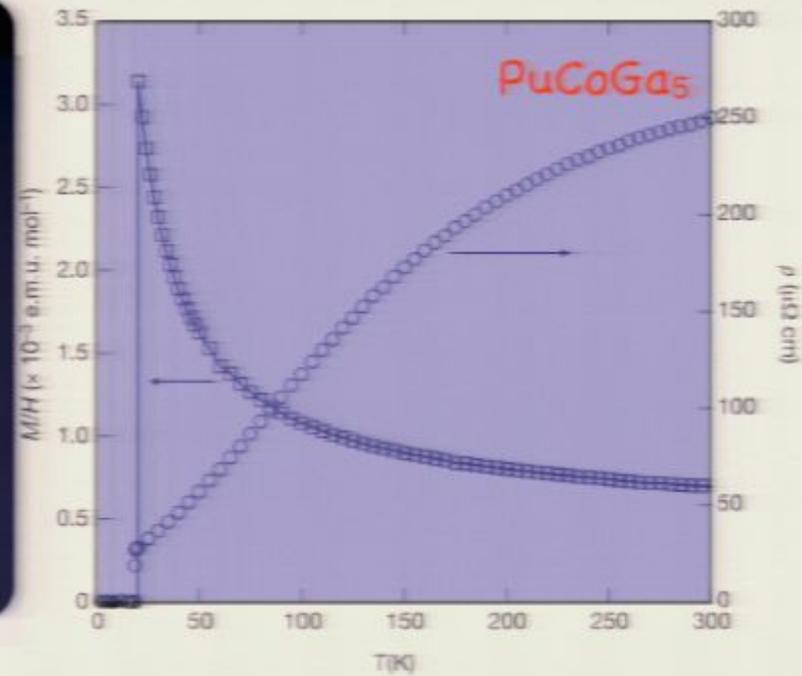
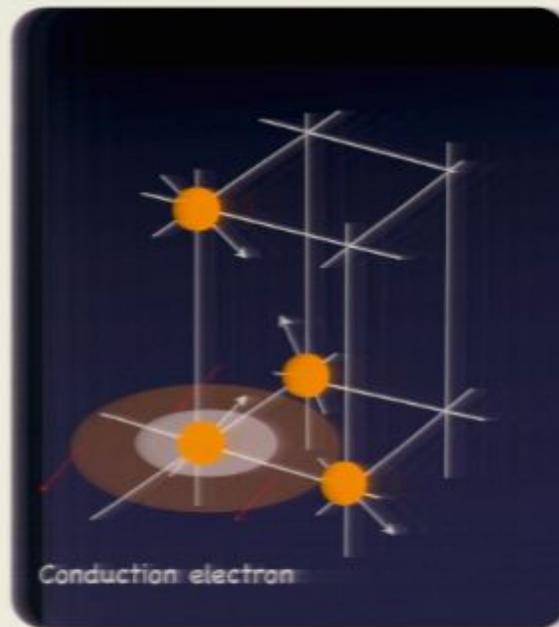
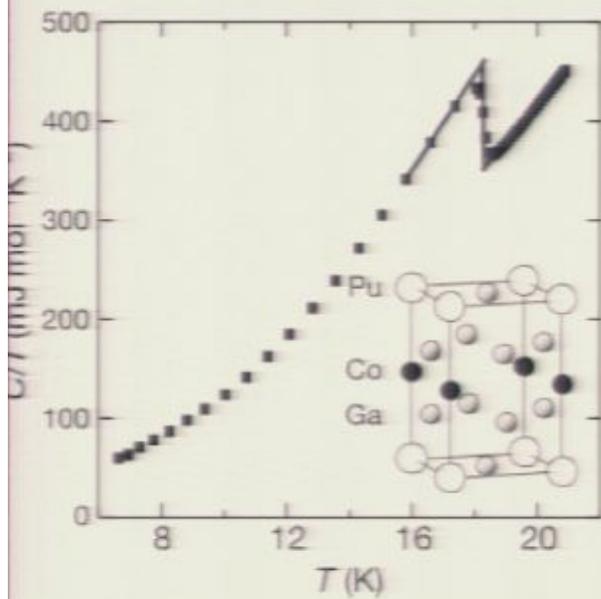
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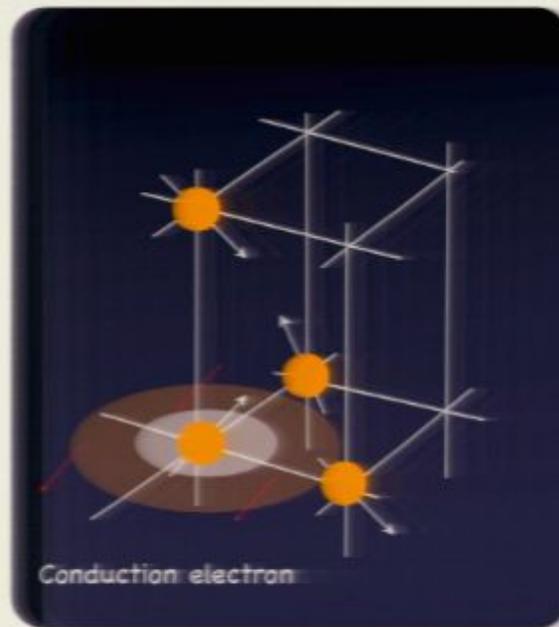
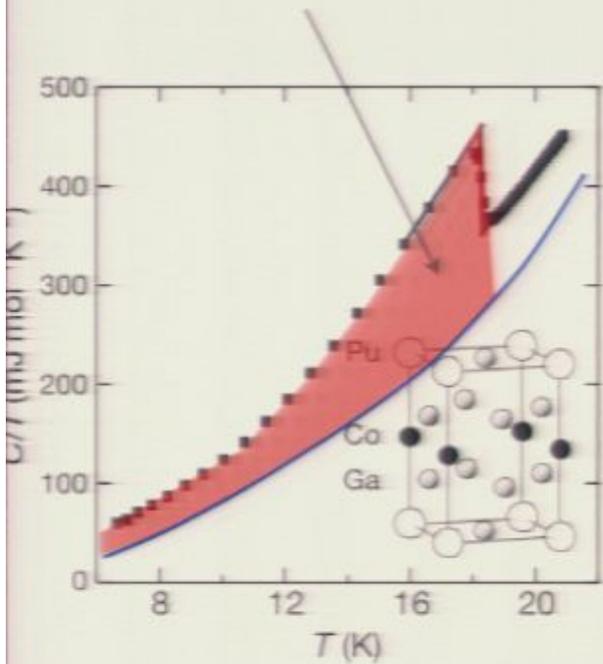


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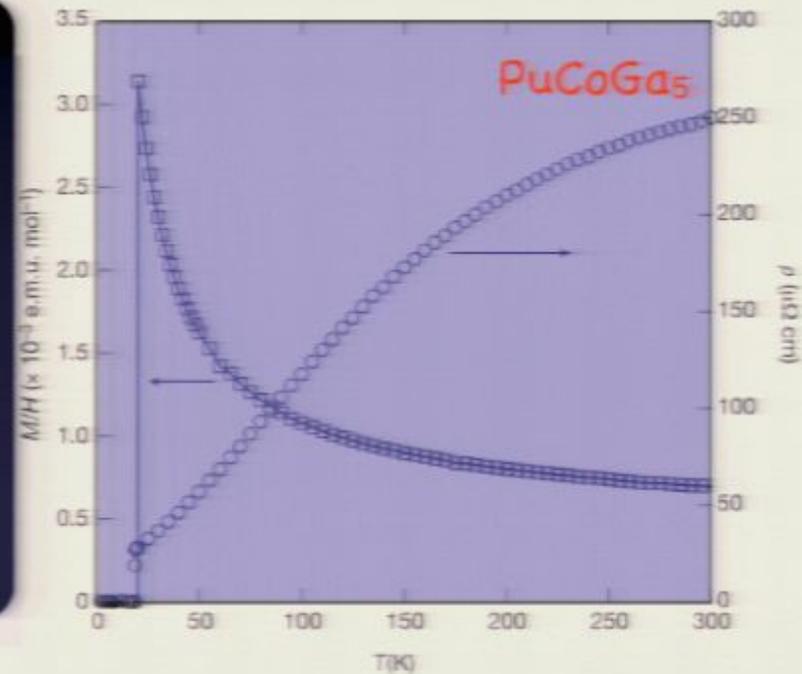
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$$S = 0.3R \ln 2$$

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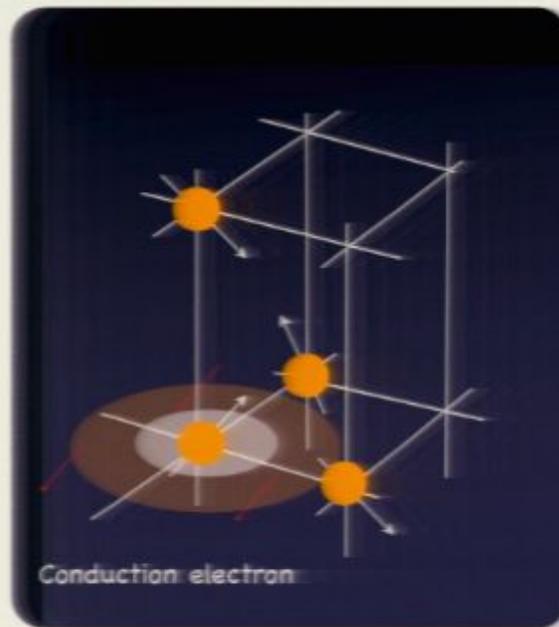
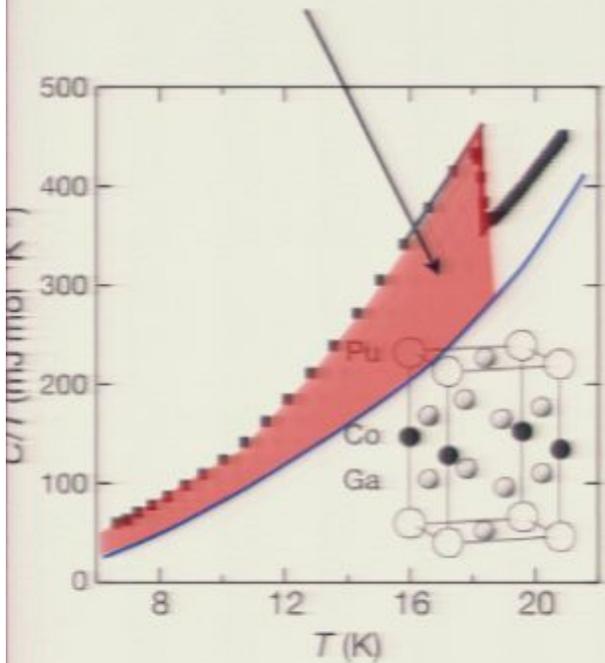
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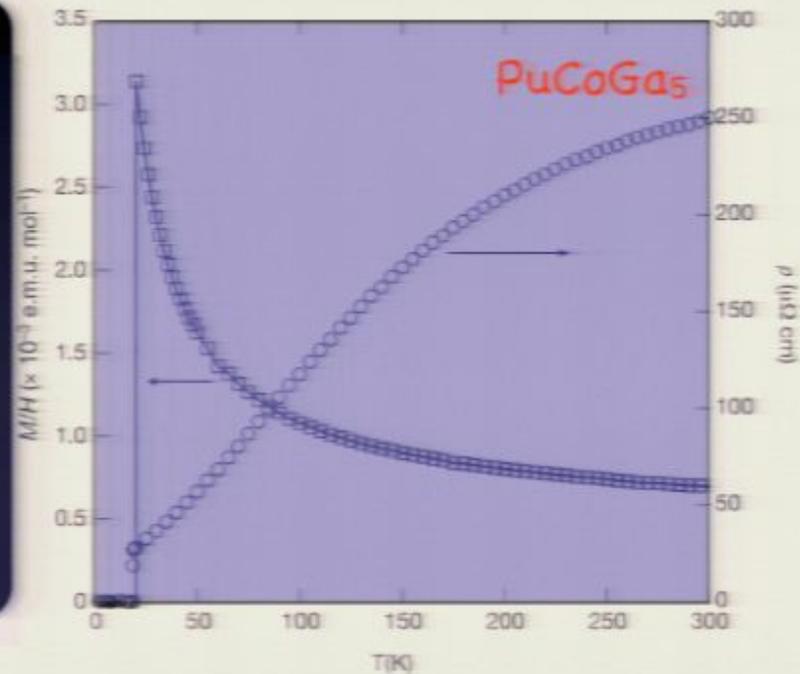
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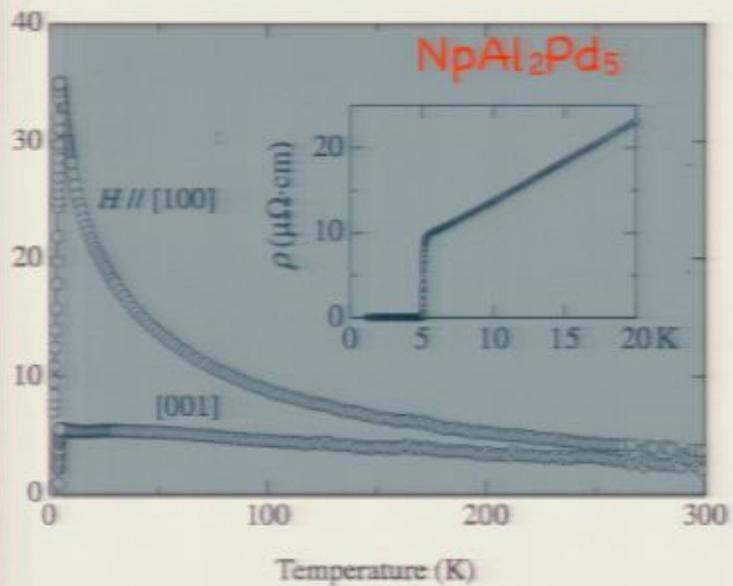


18K Heavy Fermion S. C.  
 $\text{PuCoGa}_5$

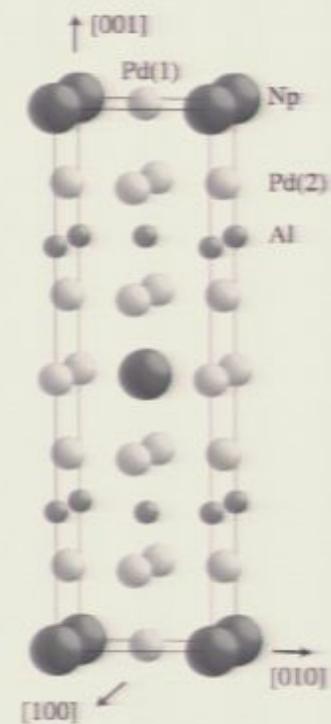


Directly Curie PM to SC

# New HF Superconductors: $\text{PuCoGa}_5$ & $\text{NpAl}_2\text{Pd}_5$

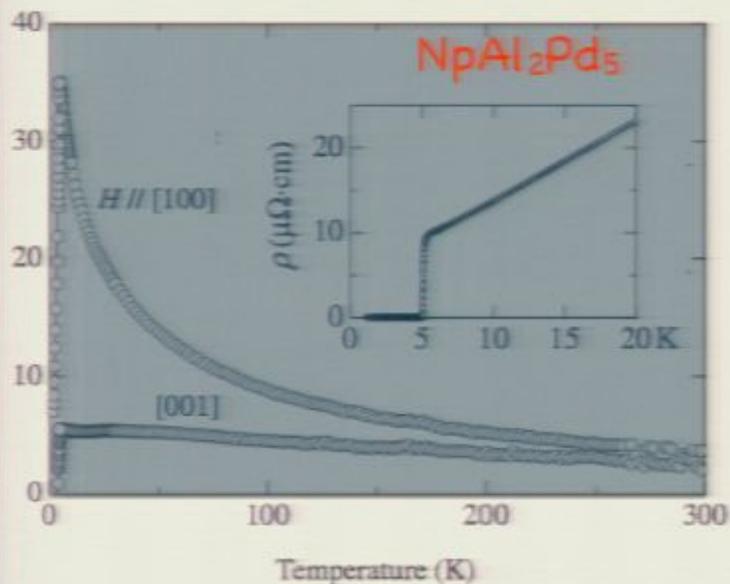


D. Aoki et al., JPSJ 76 (2007)



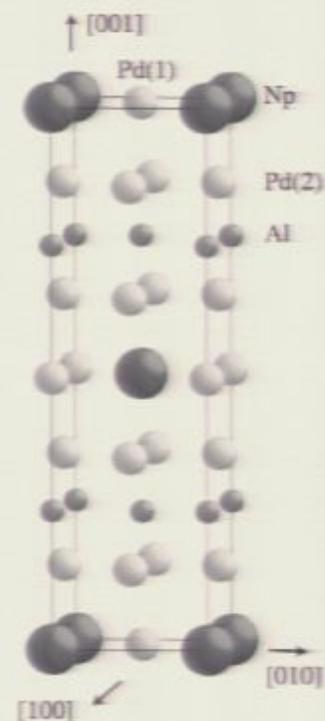
4.5K Heavy Fermion S.C.  
 $\text{NpAl}_2\text{Pd}_5$

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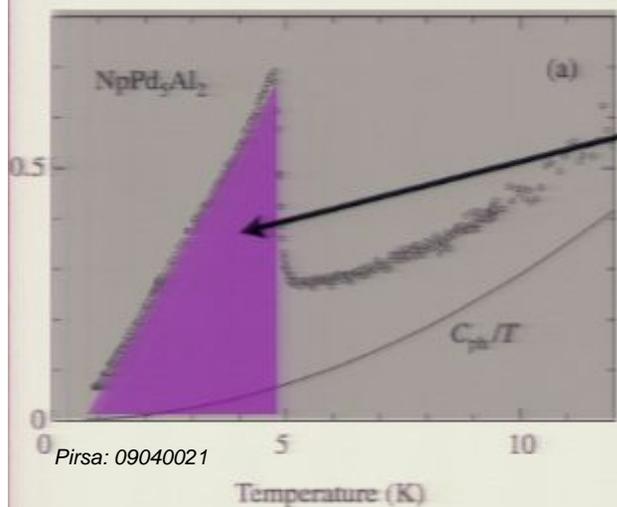


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D. Aoki et al., JPSJ 76 (2007)

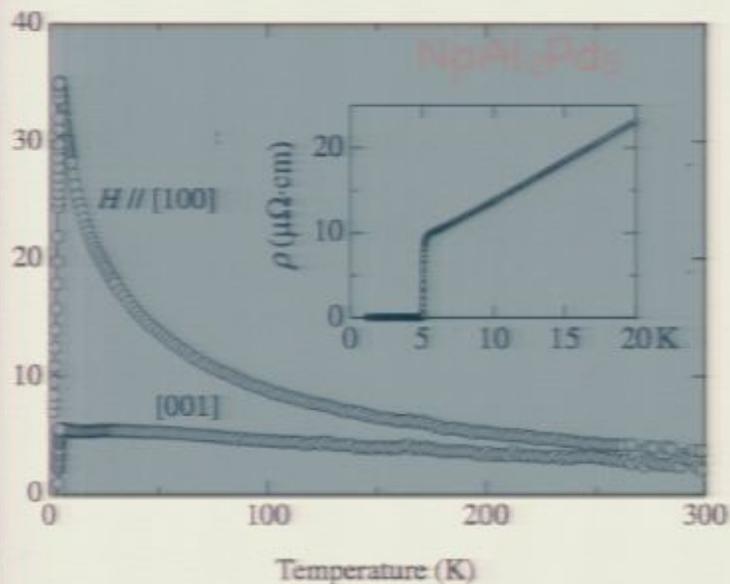


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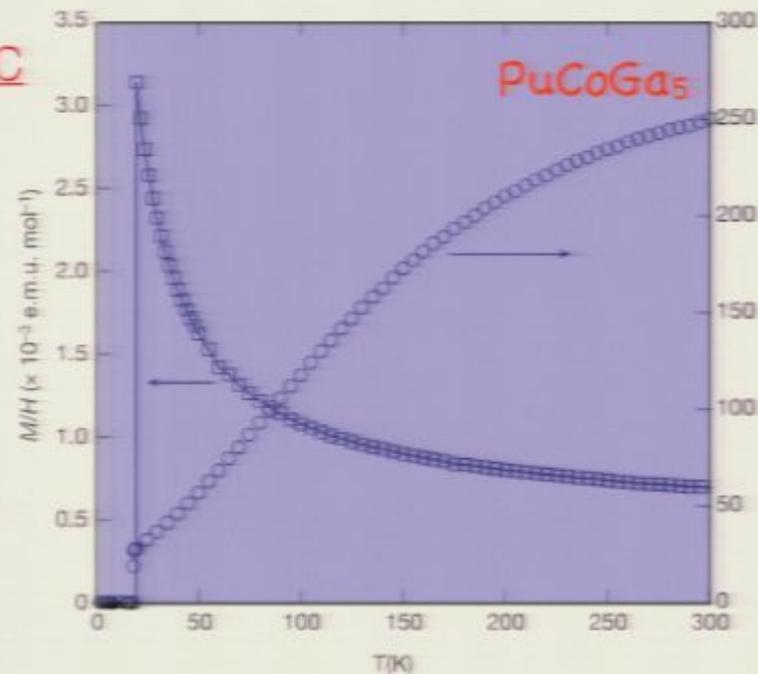


Substantial fraction of  
spin entropy.  
 $1/3 R \ln 2$

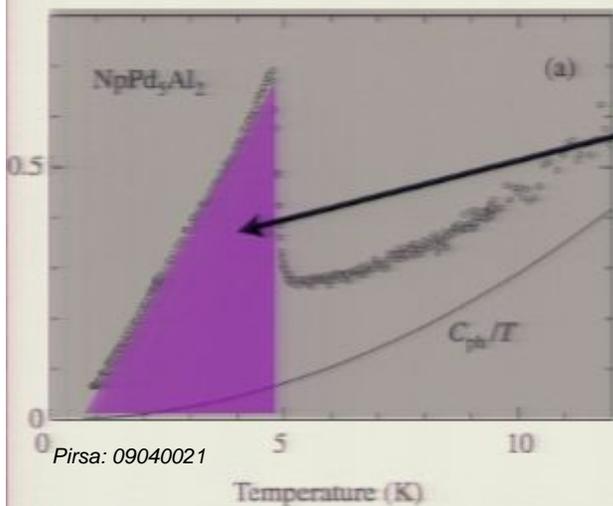
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Directly Curie PM to SC



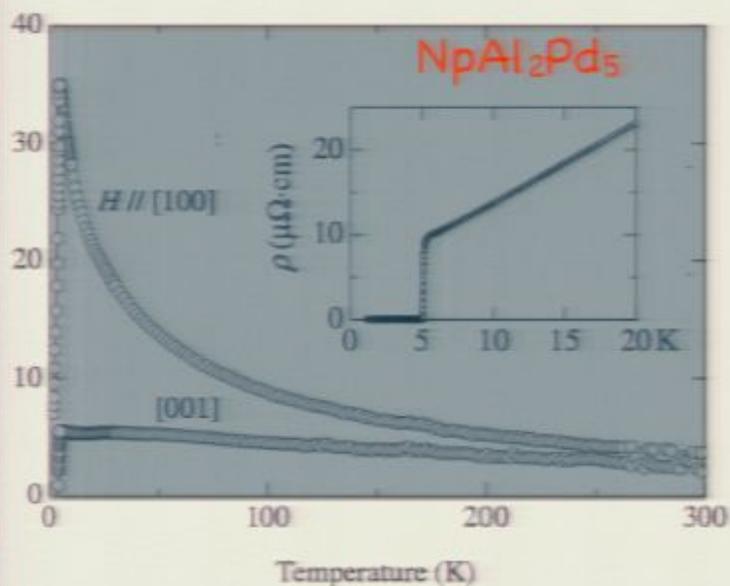
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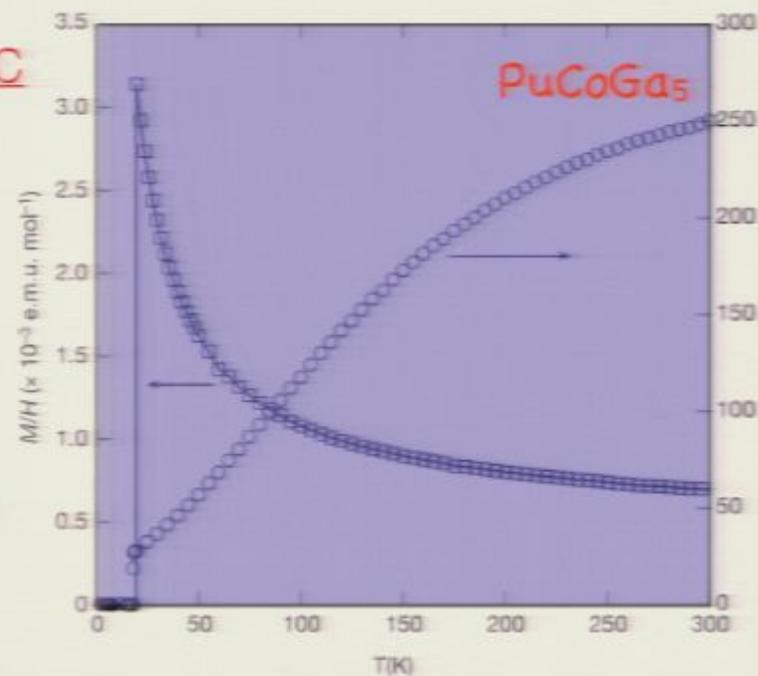
• Suggests Kondo spin quenching and superconductivity develop simultaneously.

• Spin is not the glue, but the *fabric*

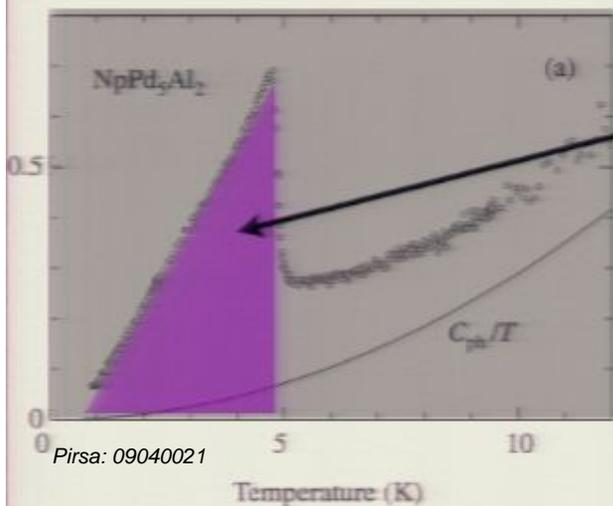
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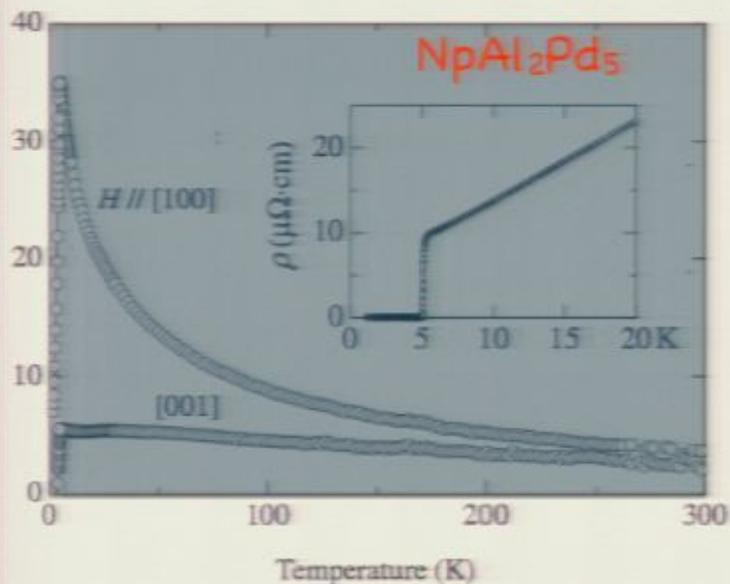


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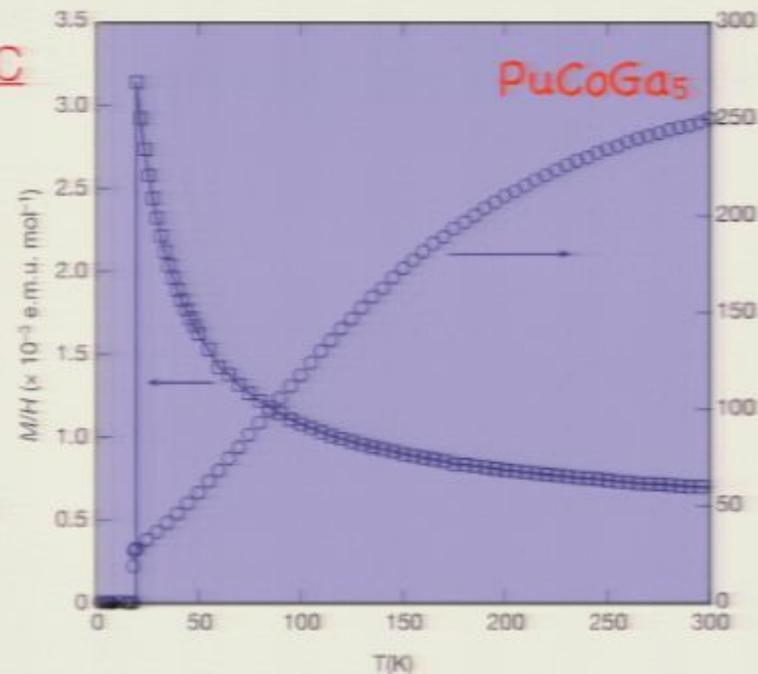


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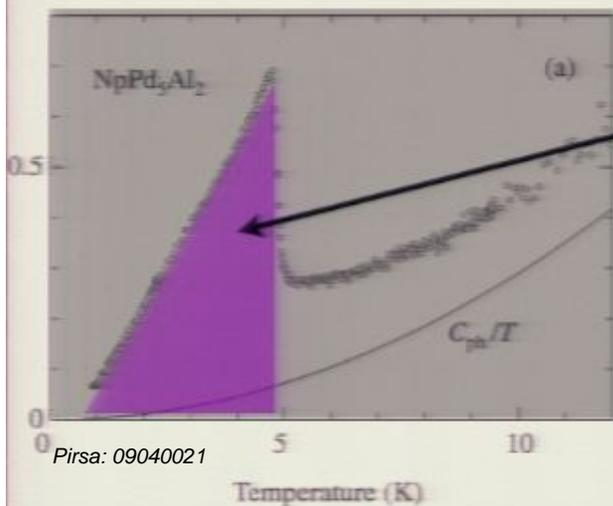
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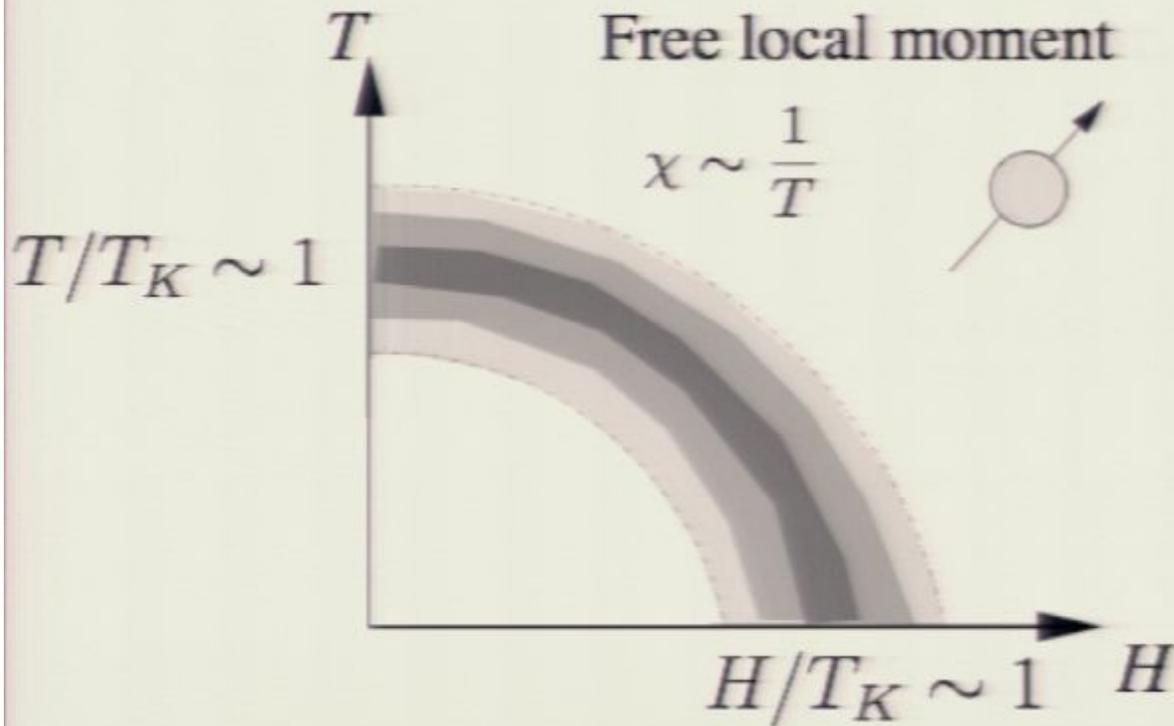
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# Background: Kondo effect and Heavy Fermions

[Review: cond-mat/0612006](#)

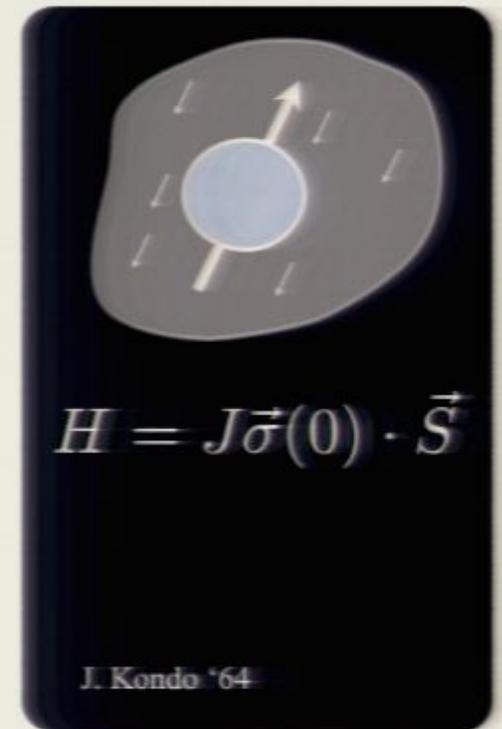
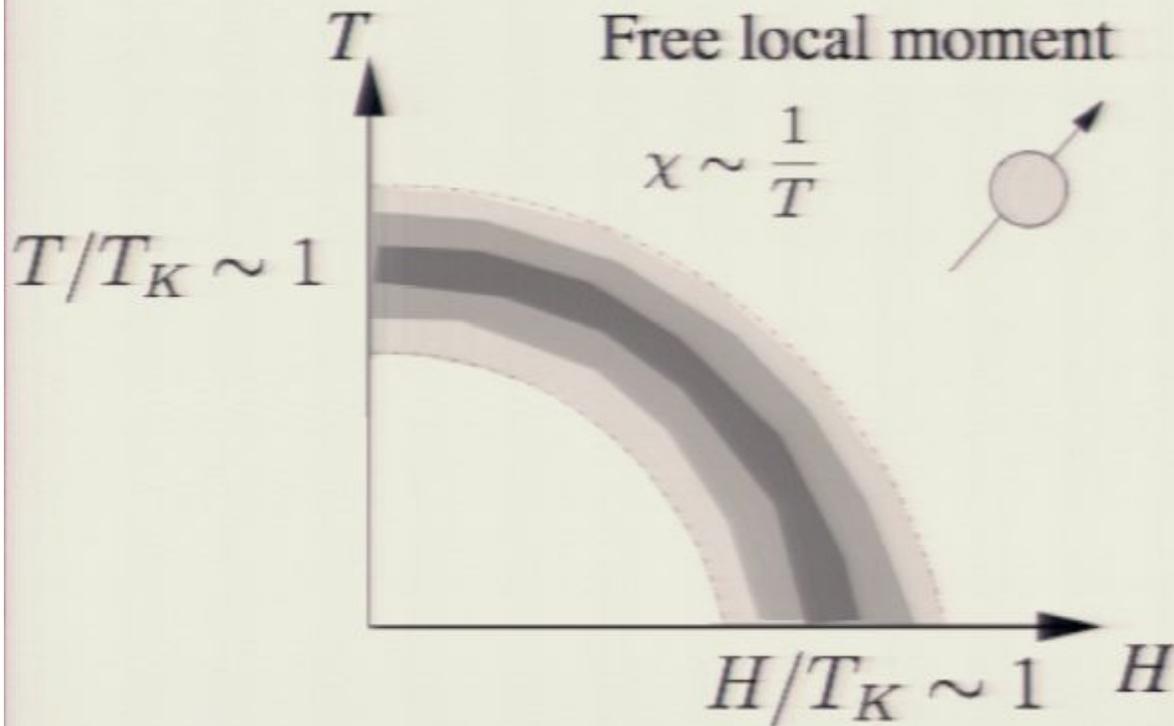


$$H = J\vec{\sigma}(0) \cdot \vec{S}$$

J. Kondo '64

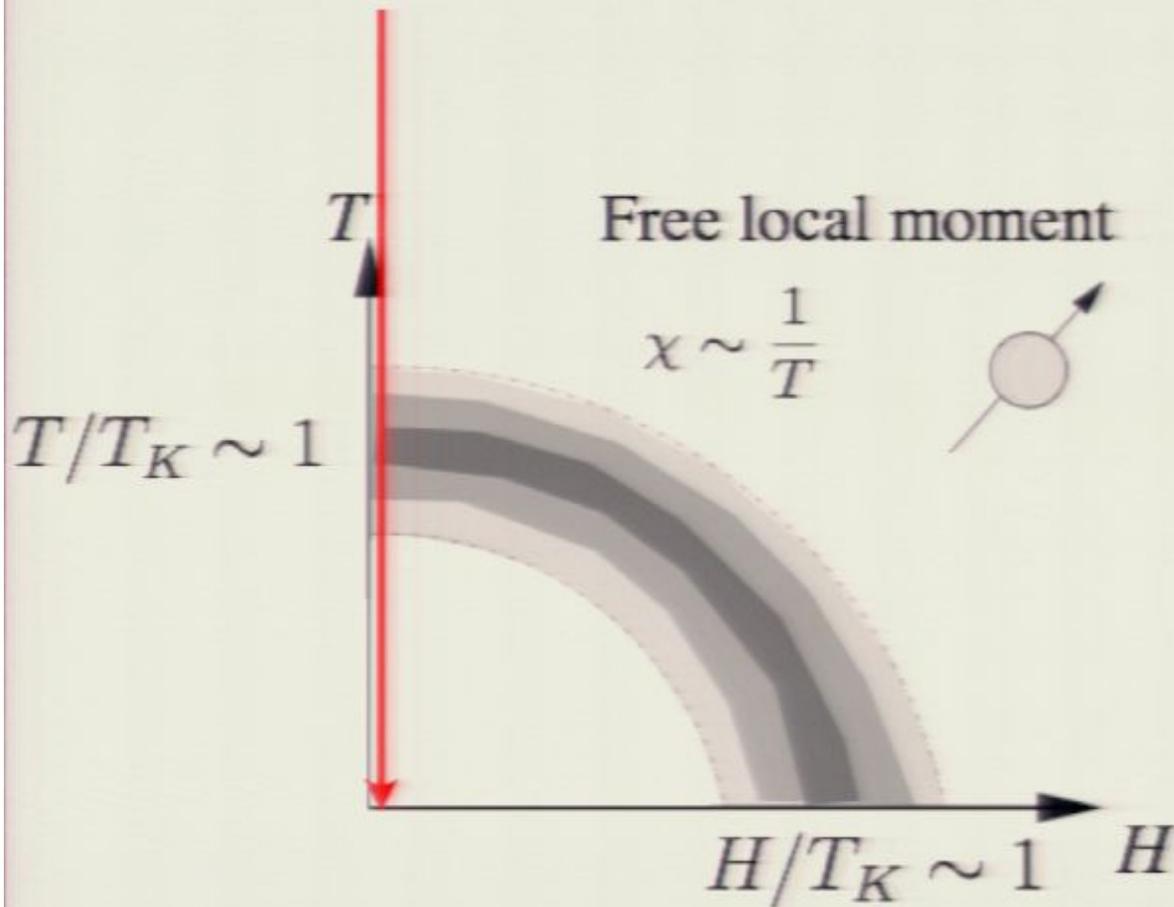
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# Background: Kondo effect and Heavy Fermions

Review: [cond-mat/0612006](https://arxiv.org/abs/cond-mat/0612006)



A diagram showing a central blue circle representing a local moment, surrounded by a larger grey circle representing the lattice. Arrows point from the central circle to the surrounding lattice sites, indicating the interaction. Below the diagram, the following equations are given:

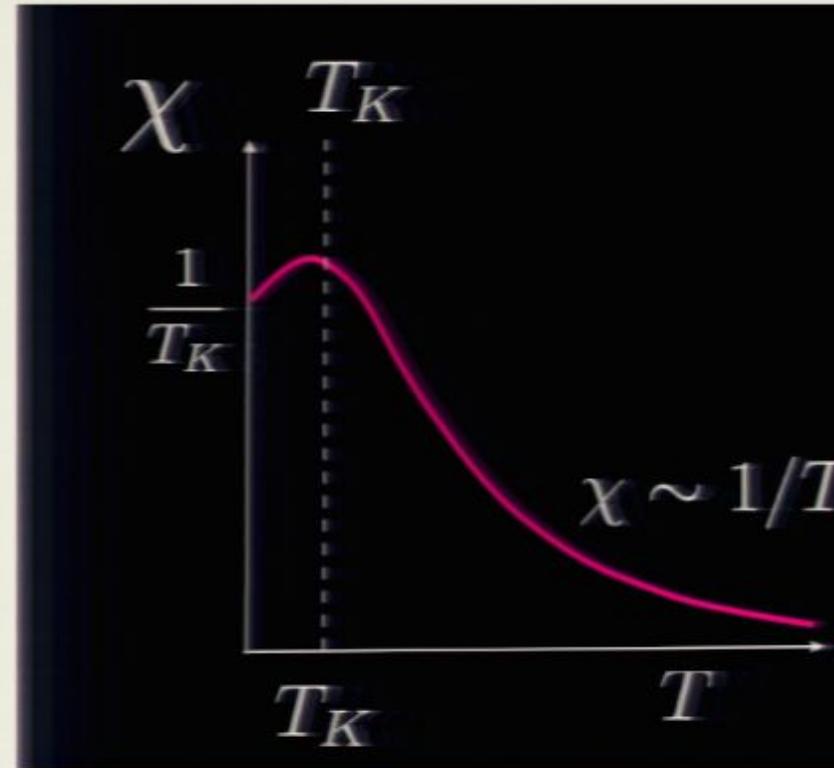
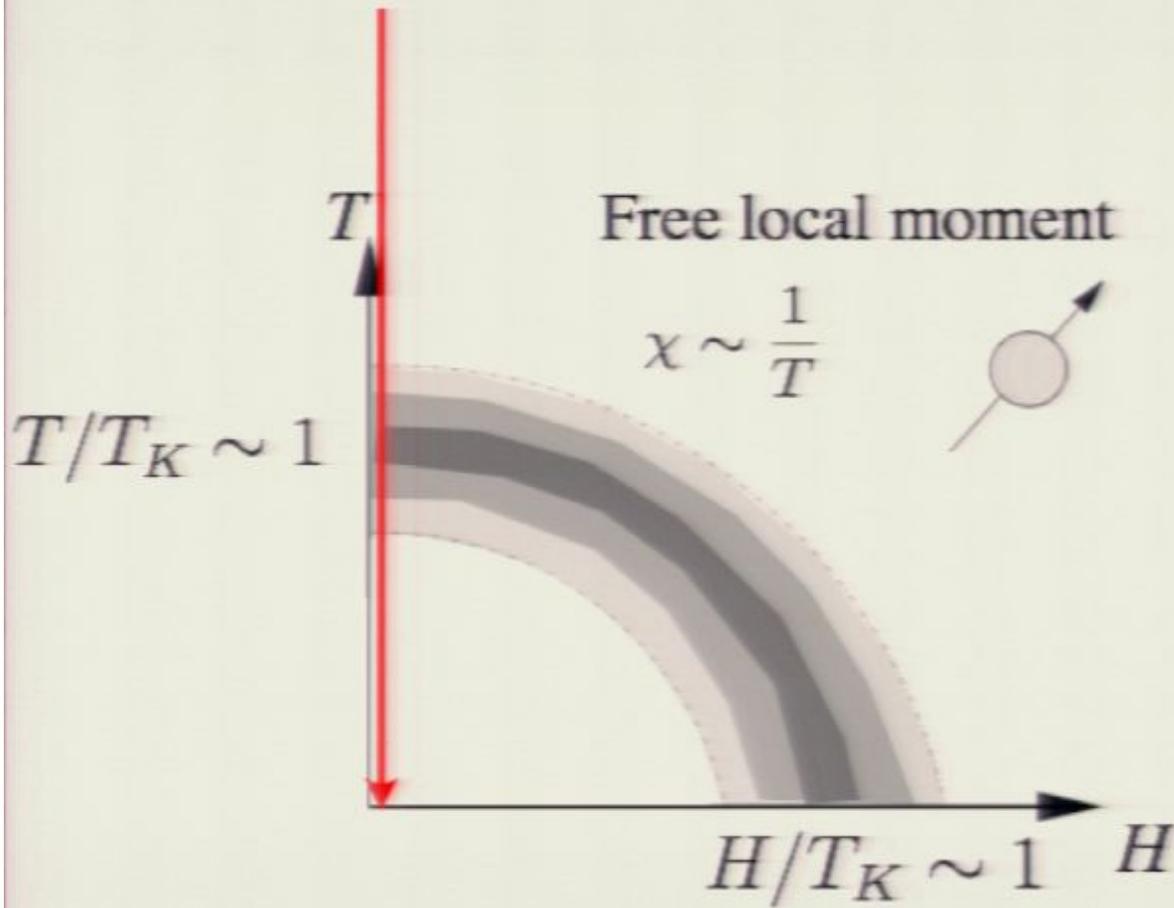
$$H = J\vec{\sigma}(0) \cdot \vec{S}$$

$$T_K \sim \epsilon_F e^{-\frac{\epsilon_F}{J}}$$

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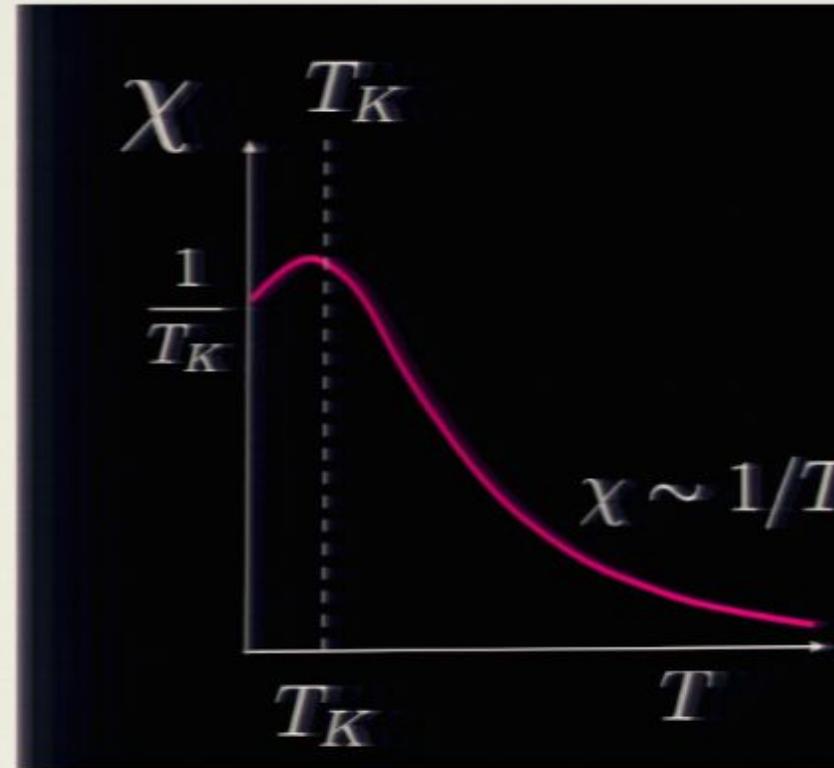
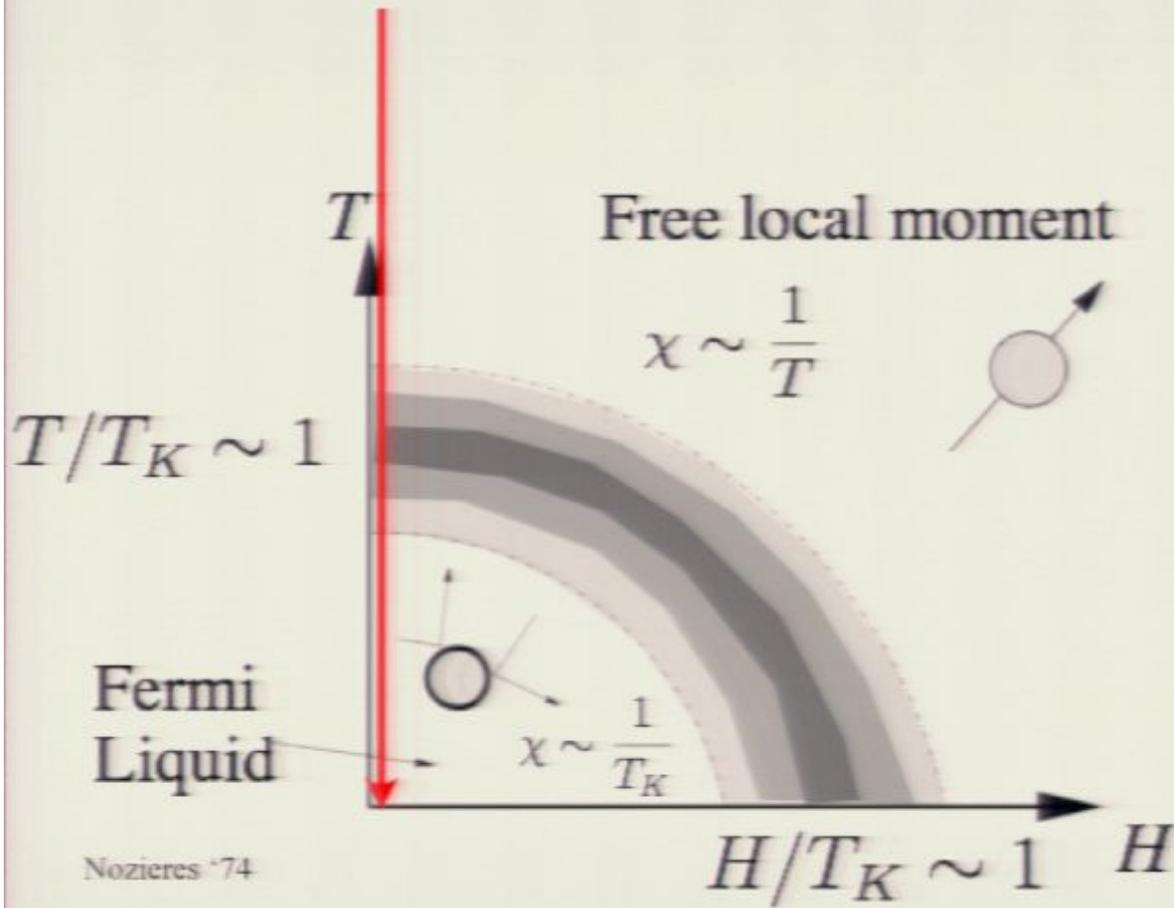
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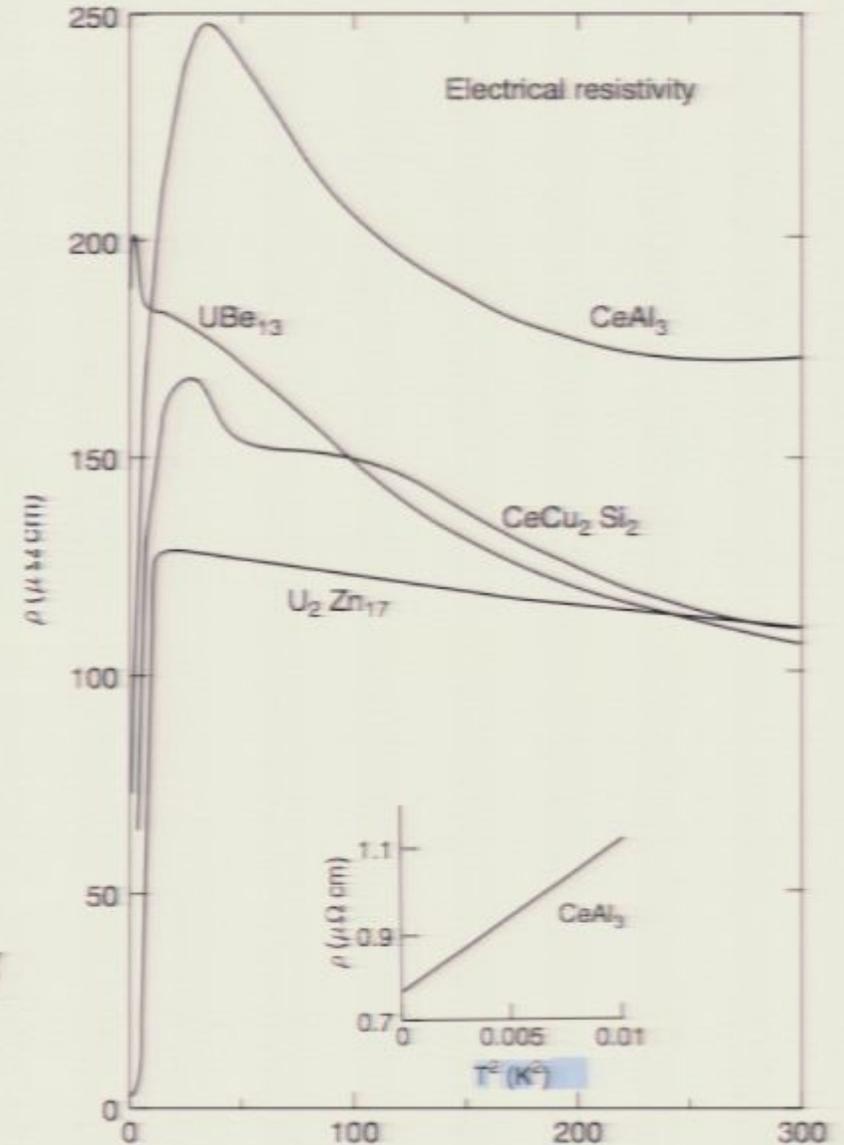
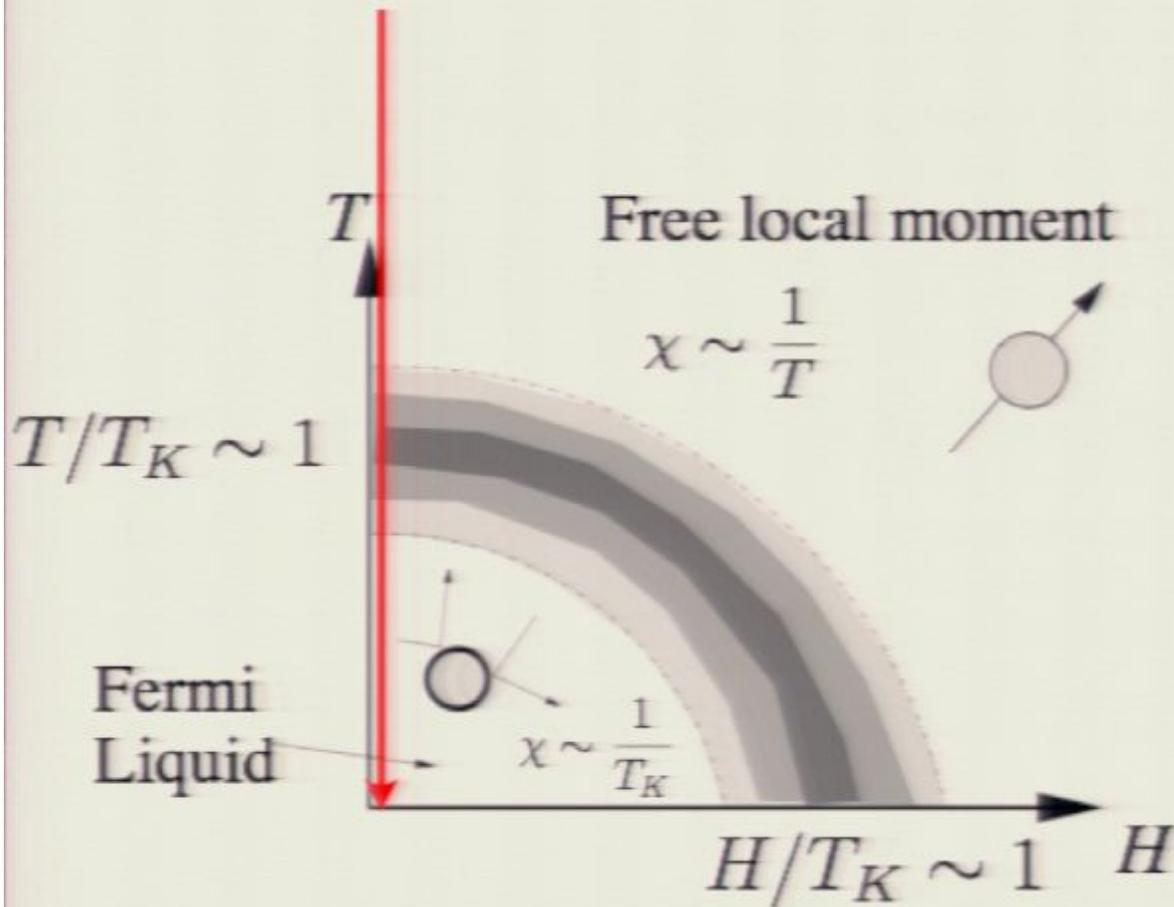
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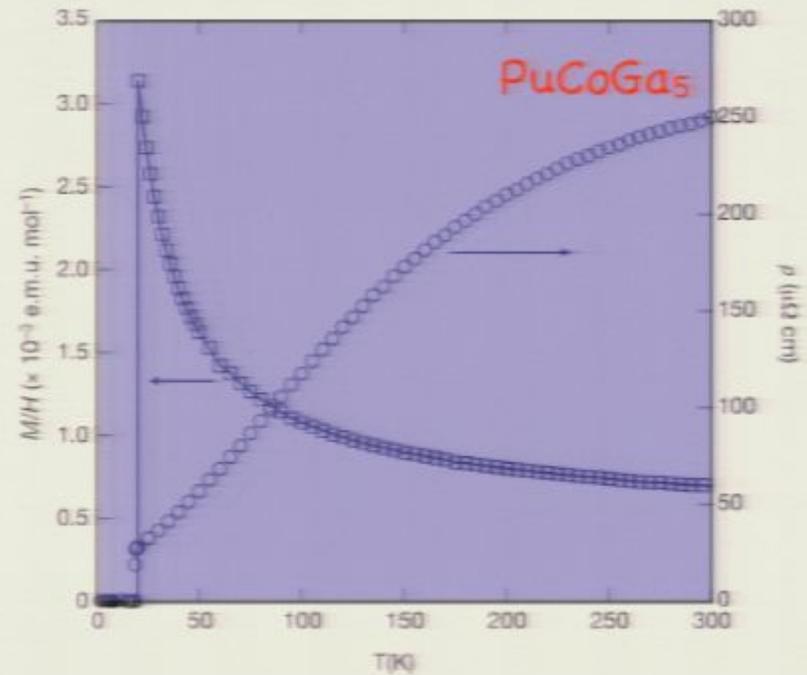
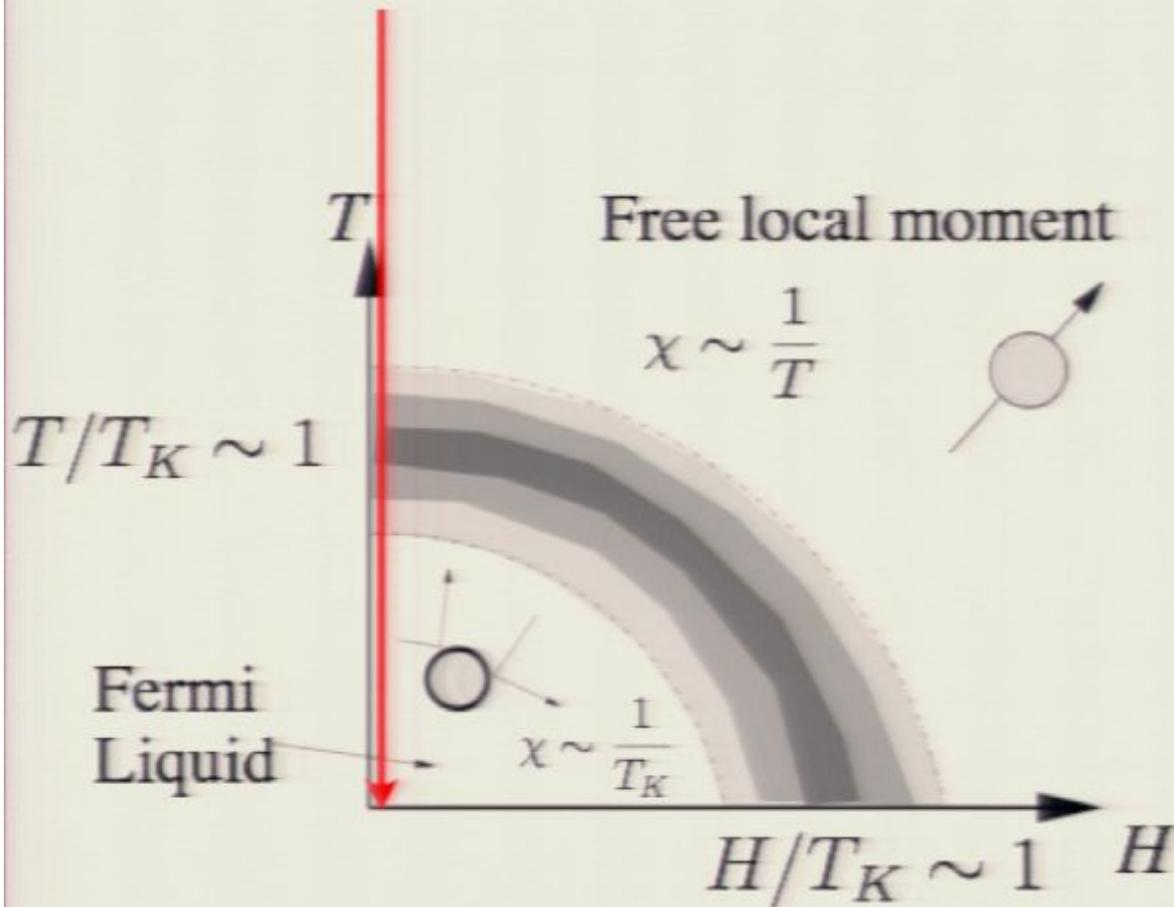
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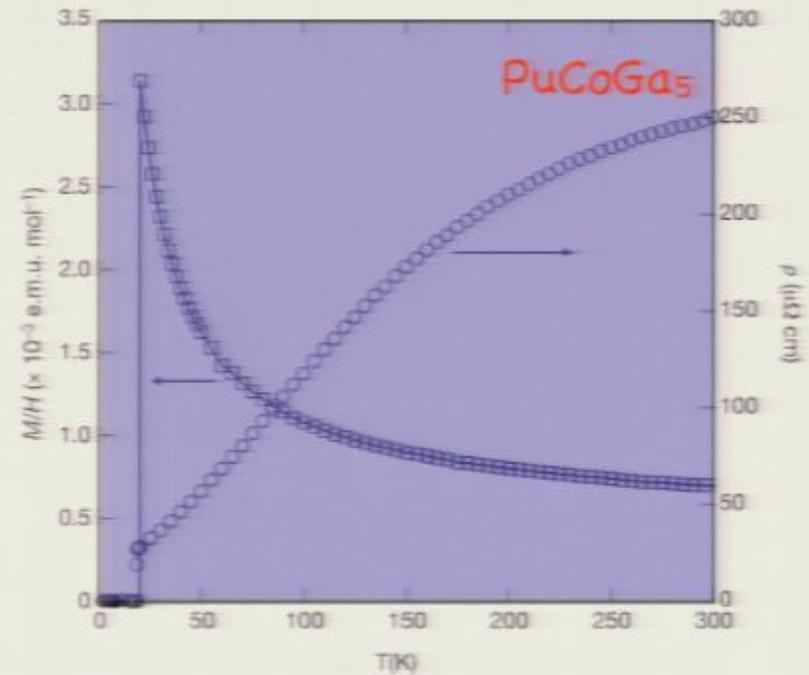
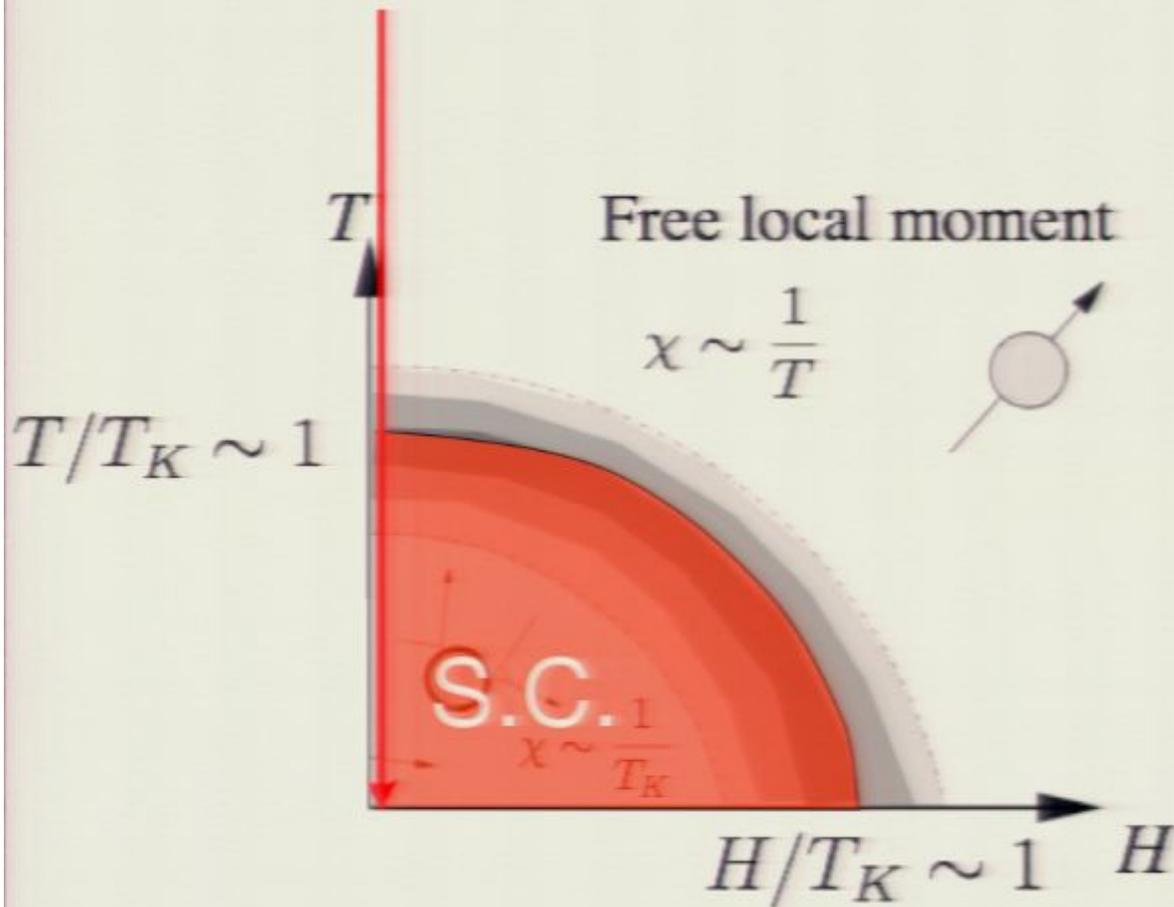
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Directly Curie PM to SC

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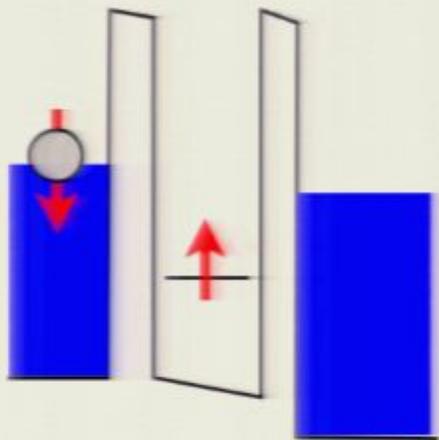


Directly Curie PM to SC

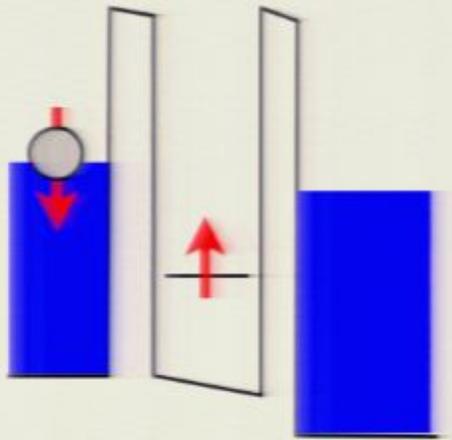
Composite pairs

# Cotunneling and composite fermions

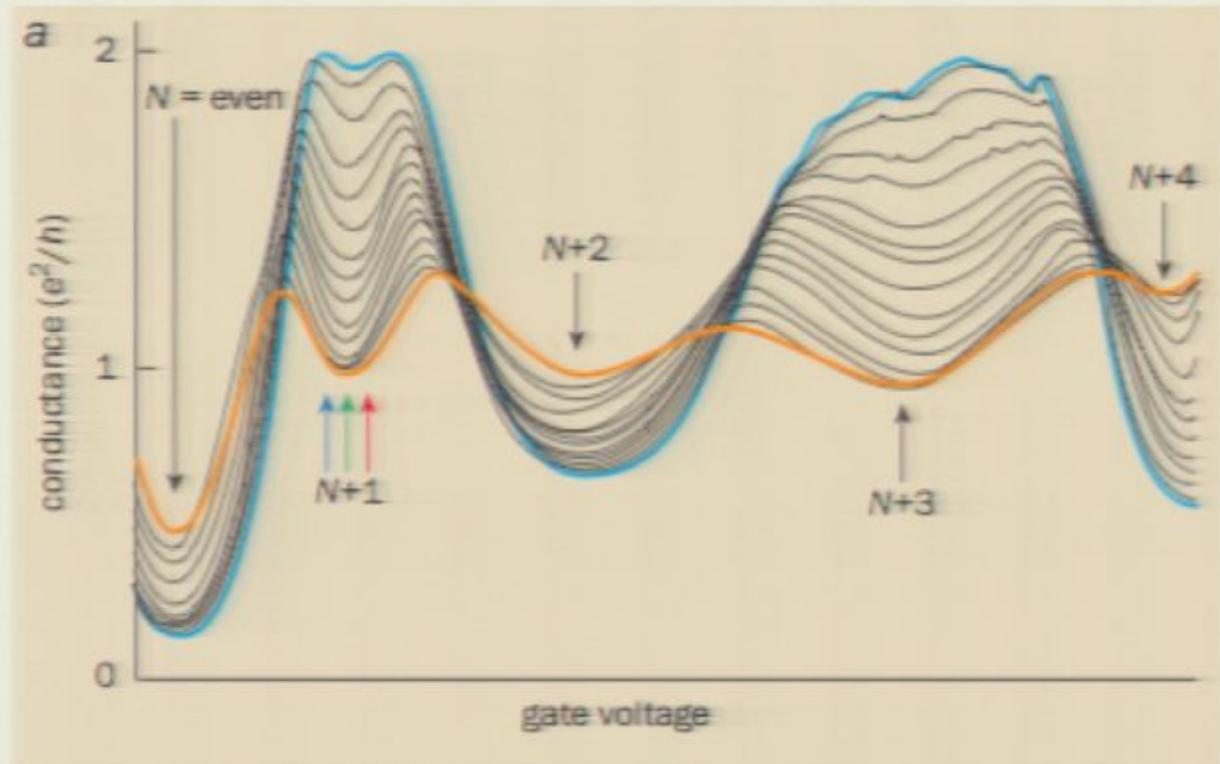
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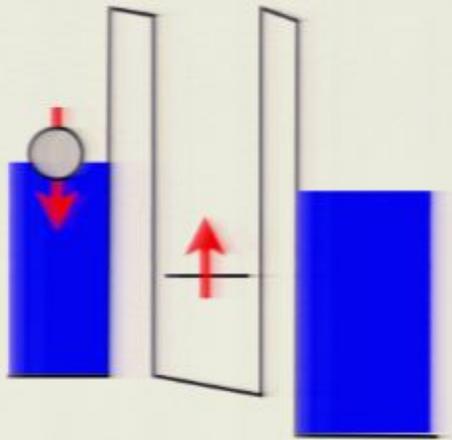
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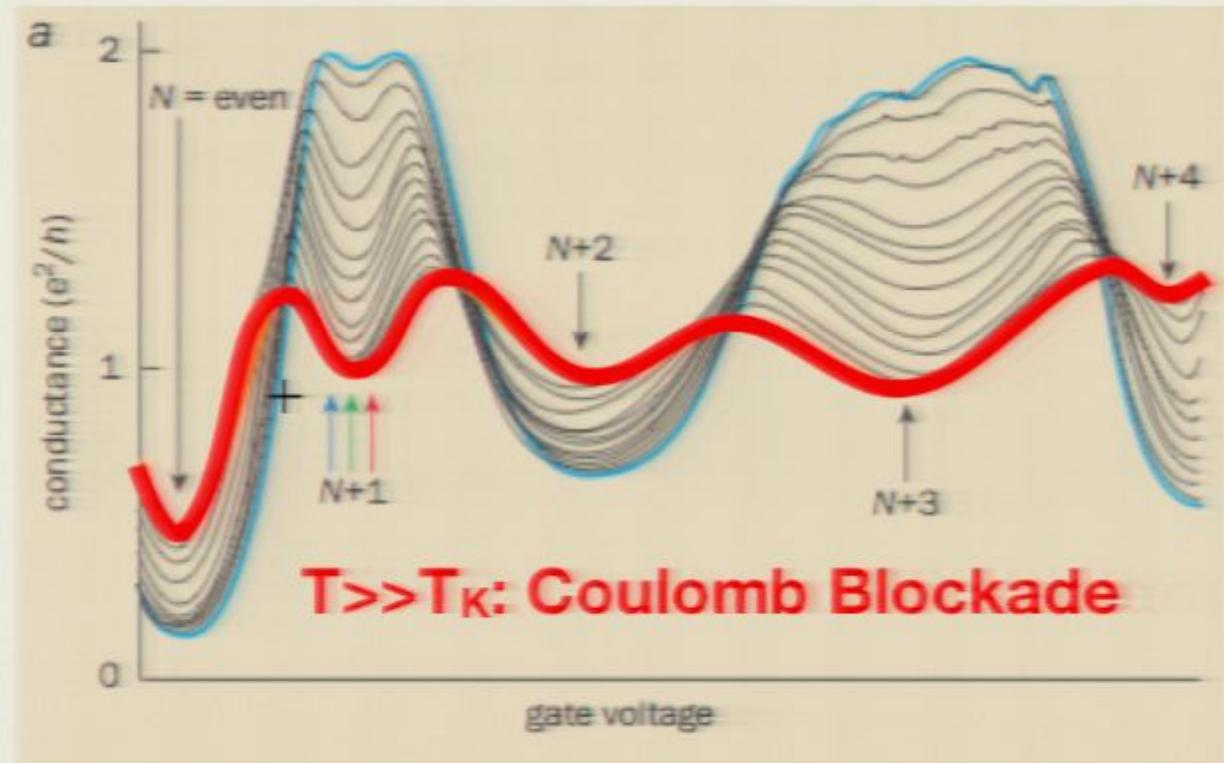
van der Wiel et al, Science (2000)



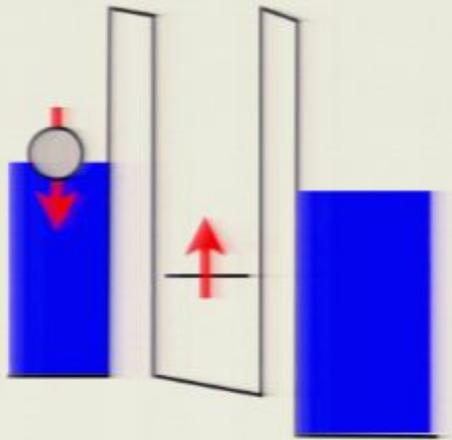
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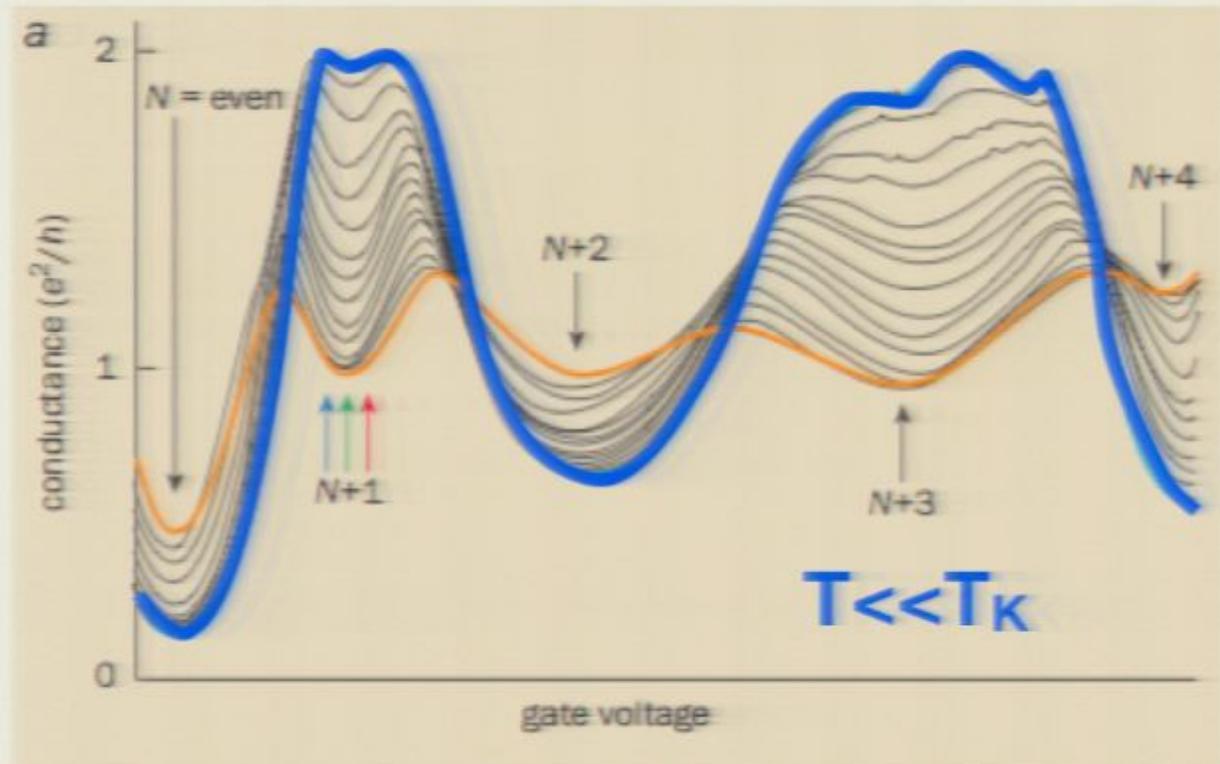
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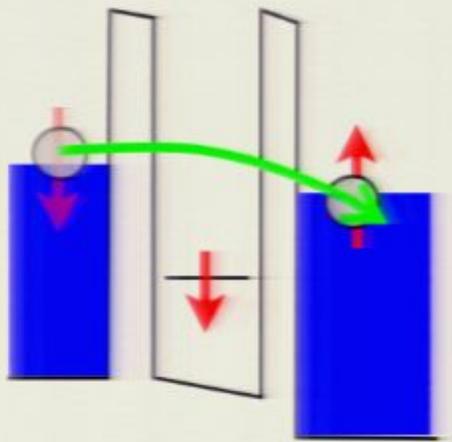
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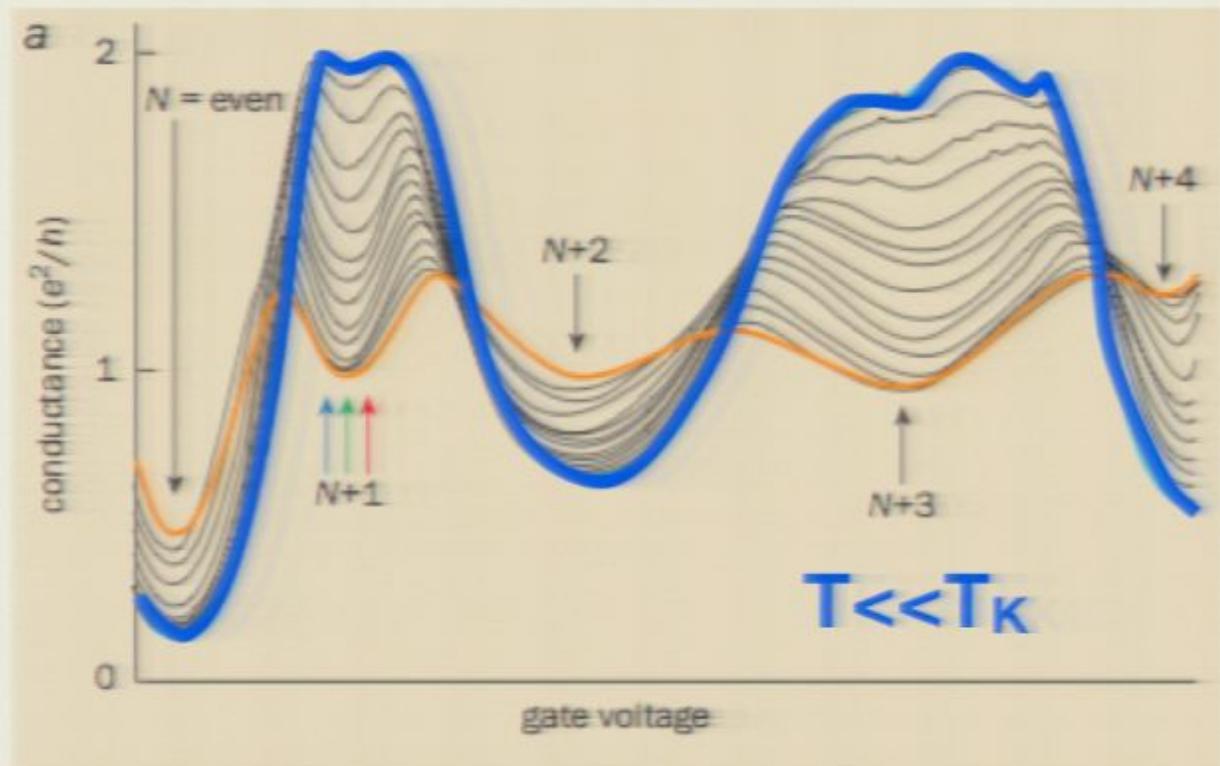
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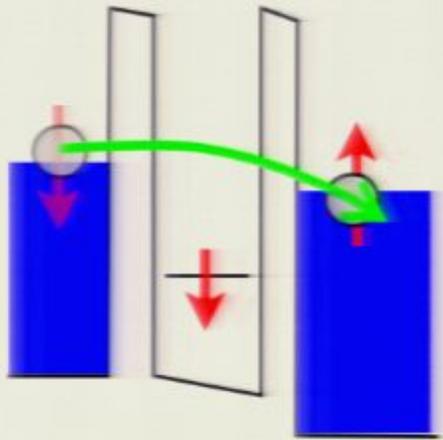
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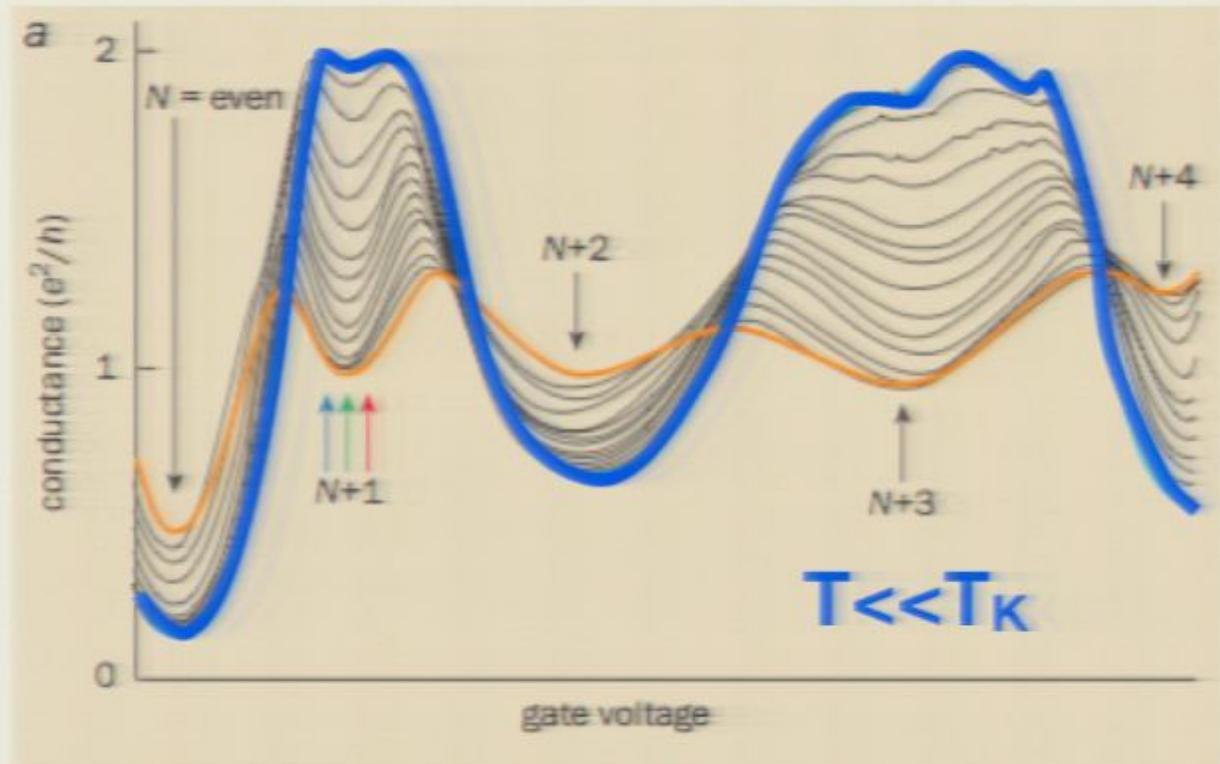
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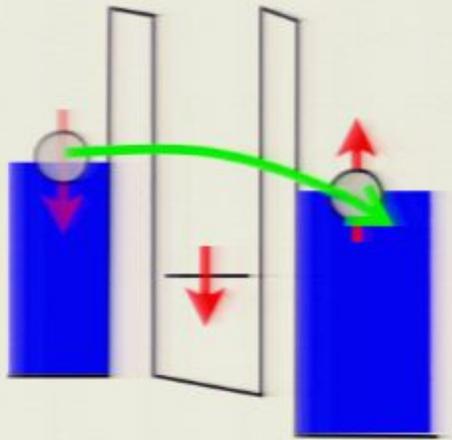
Cotunneling  
 (Glazman + Pustilnik)  
 (quantum dots)

$$f_{\downarrow}^{\dagger} = c_{\uparrow}^{\dagger} S_{-}$$

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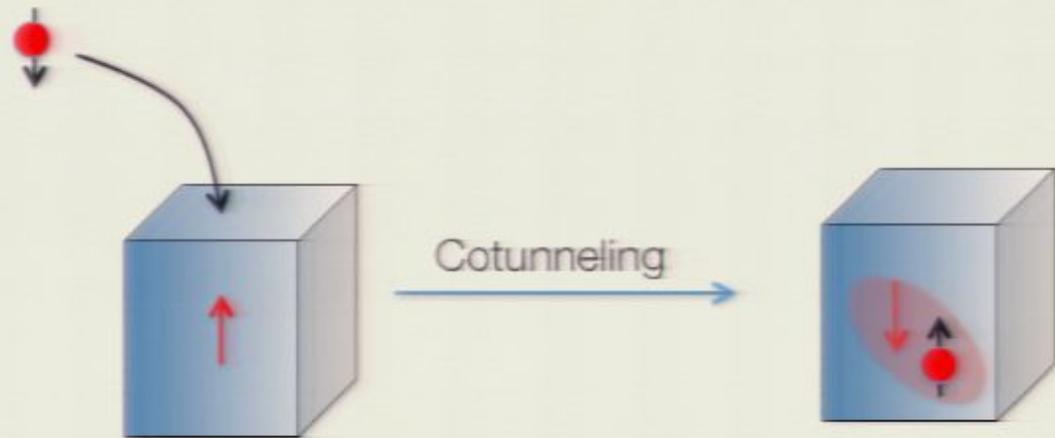


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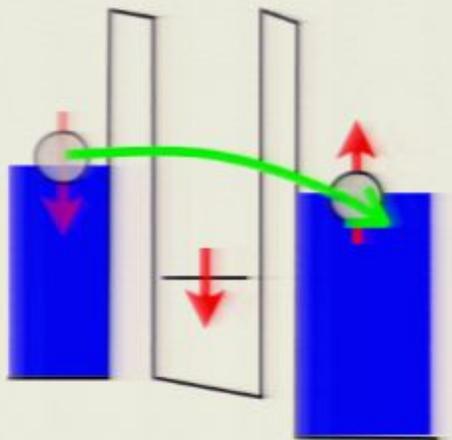
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Heavy electron = (electron x spinflip)

# Cotunneling and copairing:

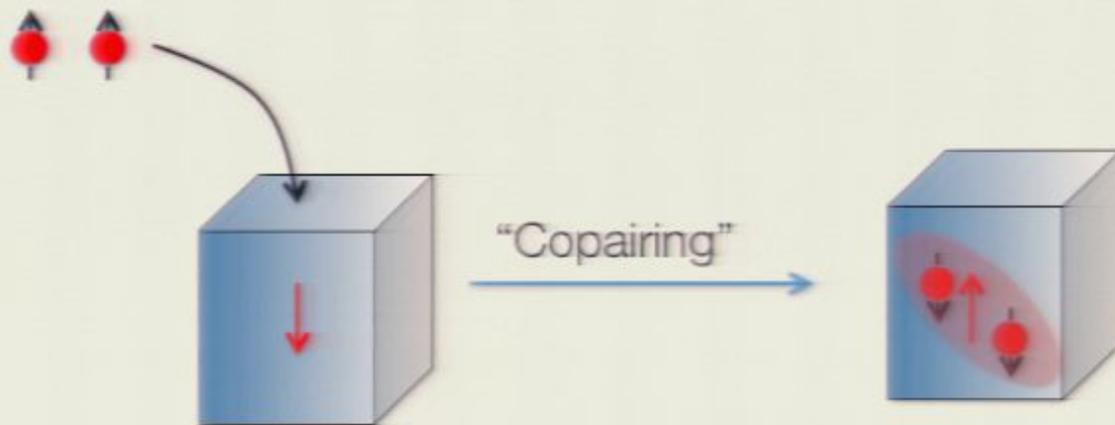


Cotunneling

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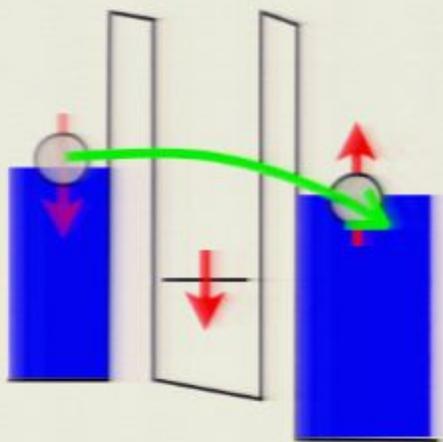
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Heavy Cooper pair = (pair x spinflip)

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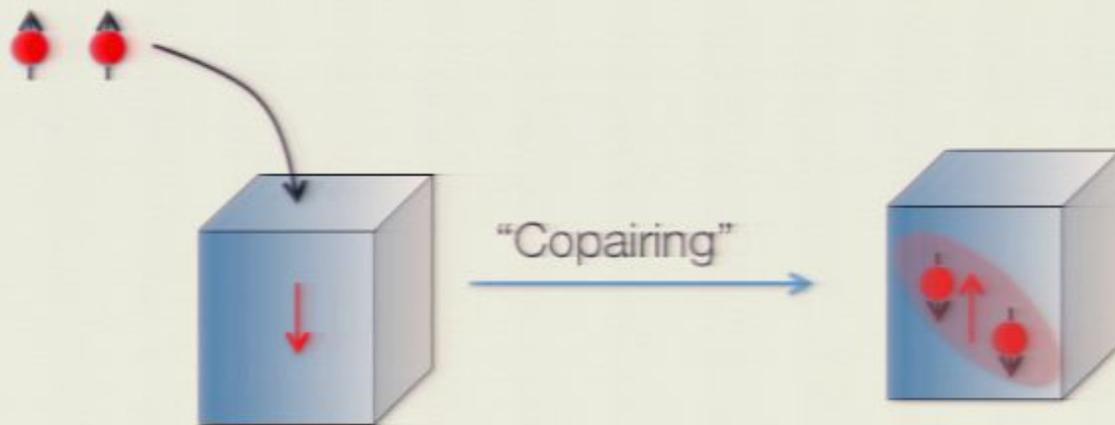


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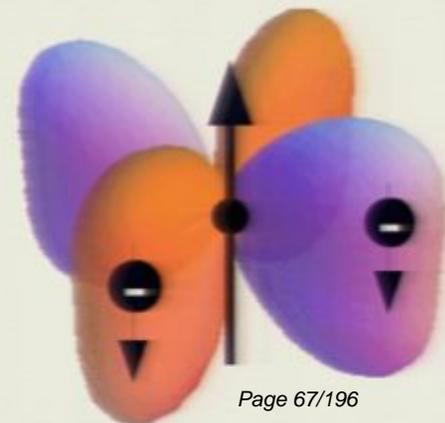
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$$f_{\downarrow}^{\dagger} = c_{\uparrow}^{\dagger} S_{-}$$



Heavy Cooper pair = (pair x spinflip)

$$\Psi^{\dagger} = c_{1\downarrow}^{\dagger} c_{2\downarrow}^{\dagger} S_{+}$$



Theoretical digression.

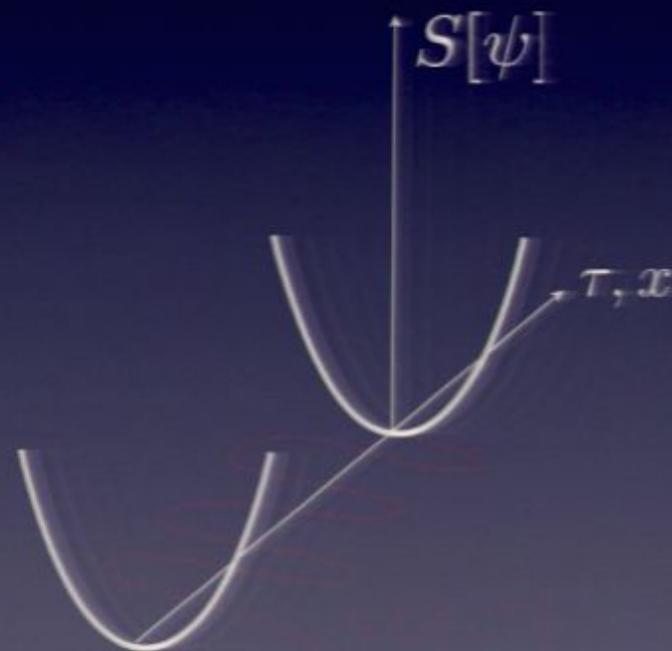
Strongly correlated electron physics: no small parameter

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$$Z = \sum_{\text{configs}} e^{-S[\psi]}$$

Strongly correlated electron physics: no small parameter

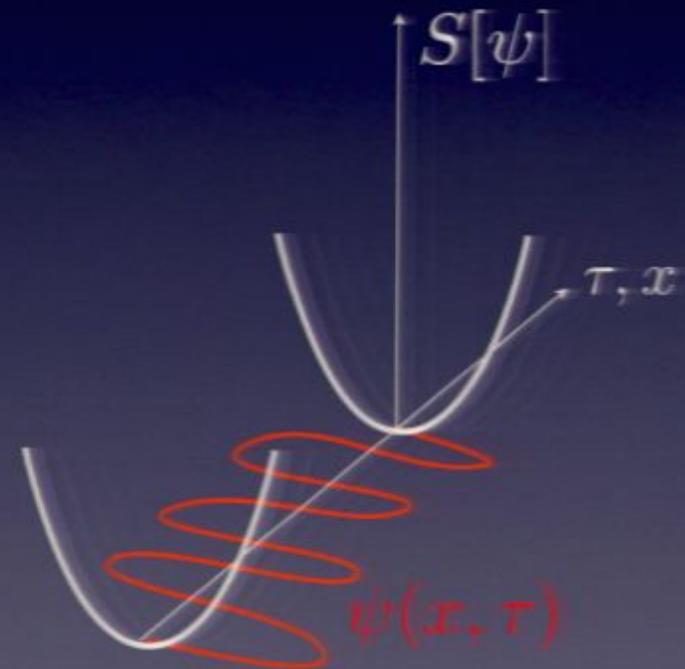
$$Z = \sum_{\text{configs}} e^{-S[\psi]}$$



Strongly correlated electron physics: no small parameter

Large  $N$ : family of models with “ $N$ ” spin components, which retain the key physics and can be solved in the large  $N$  limit.

$$Z = \sum_{\text{configs}} e^{-S[\psi]} \times N$$

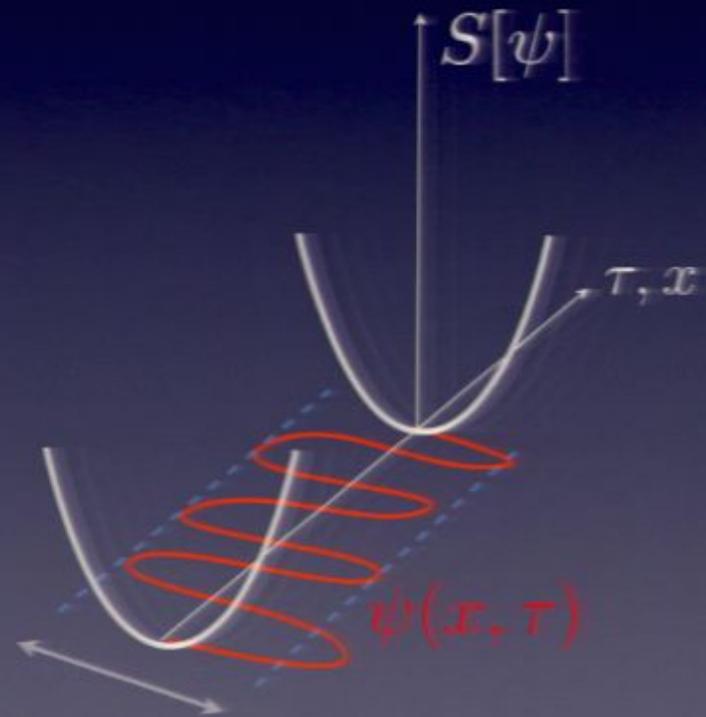


Wild quantum fluctuations!

Strongly correlated electron physics: no small parameter

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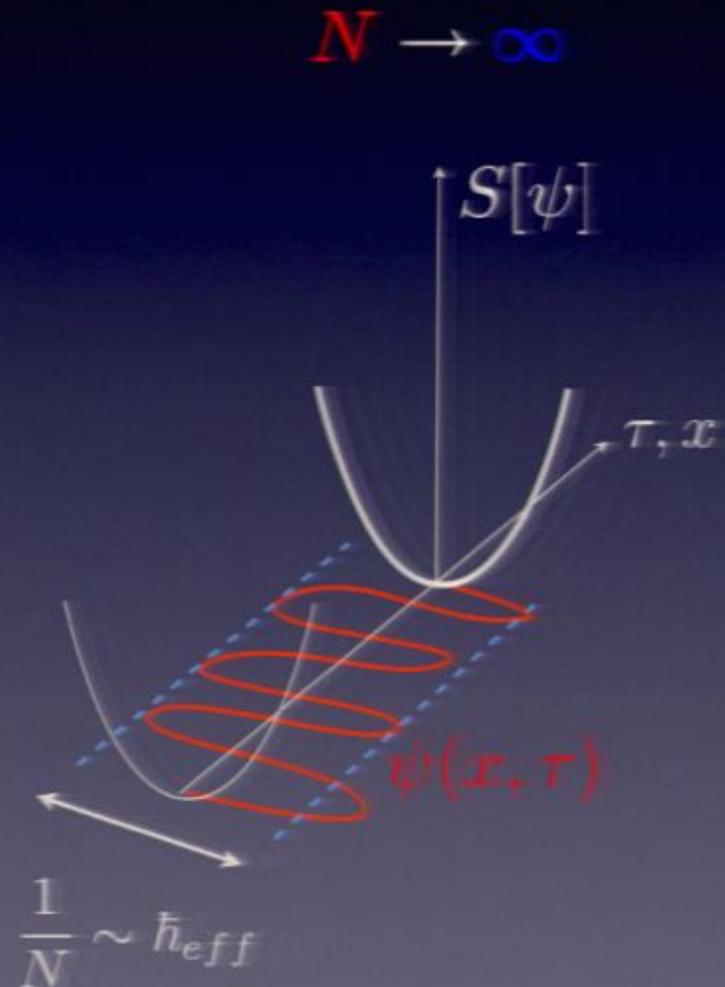


Wild  $\frac{1}{N} \propto \hbar_{\text{eff}}$  quantum fluctuations!

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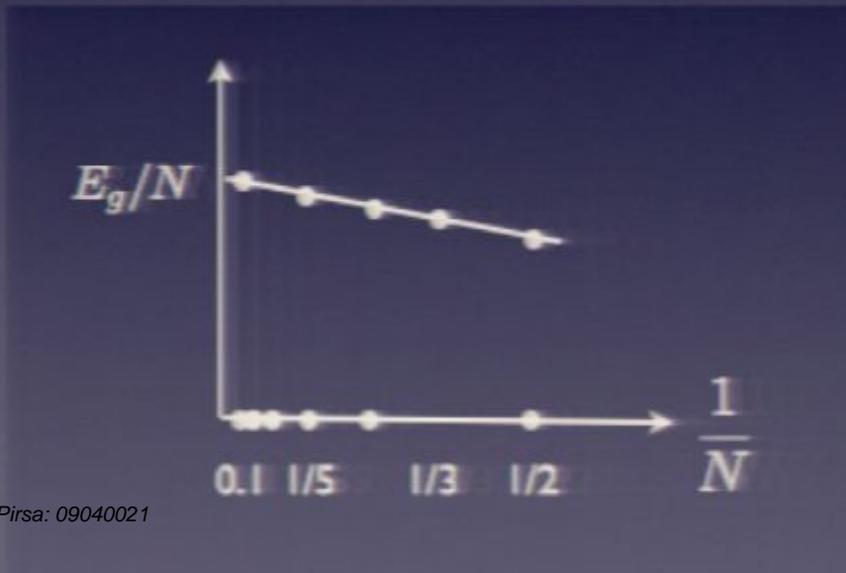
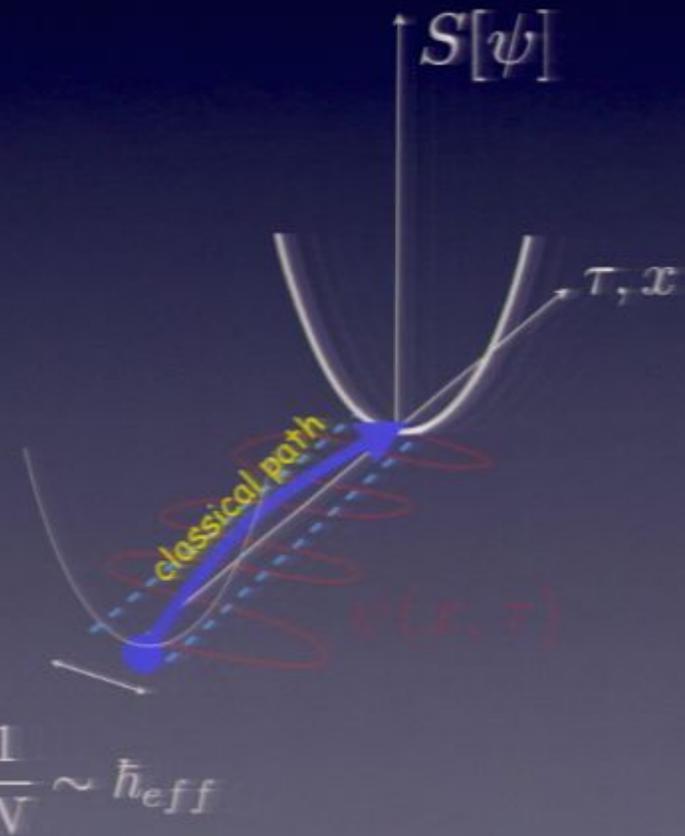
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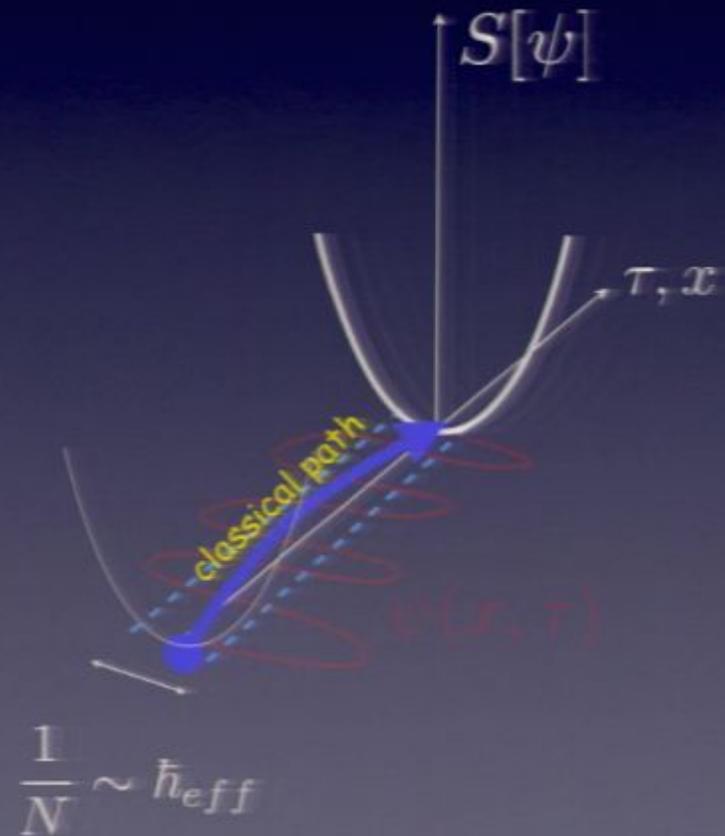
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The magnetism and neutrality of the electron spin are manifested as two discrete parities:

*odd* under time reversal,

*even* under charge conjugation

$$S \xrightarrow{\theta} -S \quad \text{Magnetism}$$

$$S \xrightarrow{C} +S \quad \text{Neutrality}$$

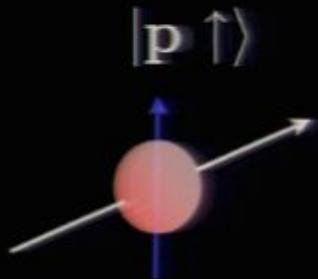
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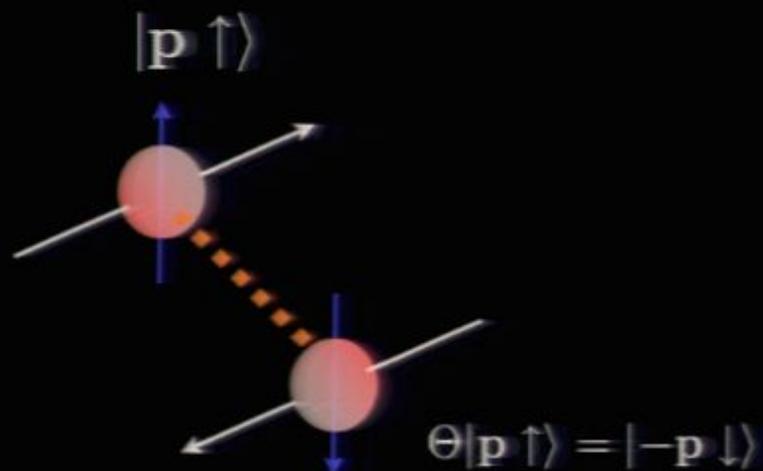
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$$S + S_{\Theta} = S - S = 0$$

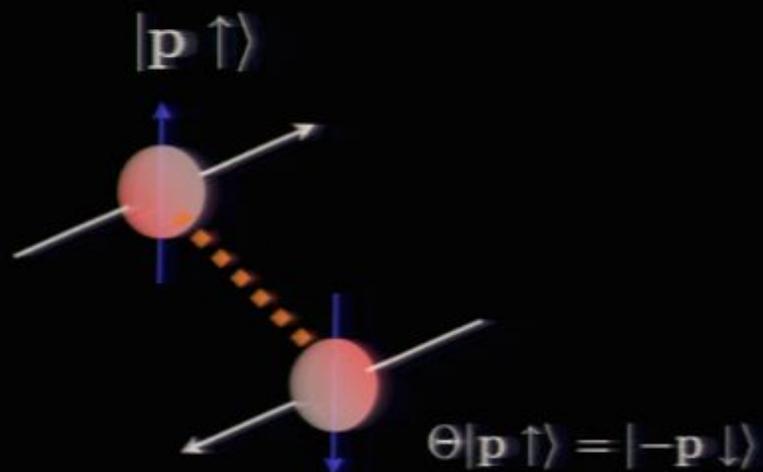
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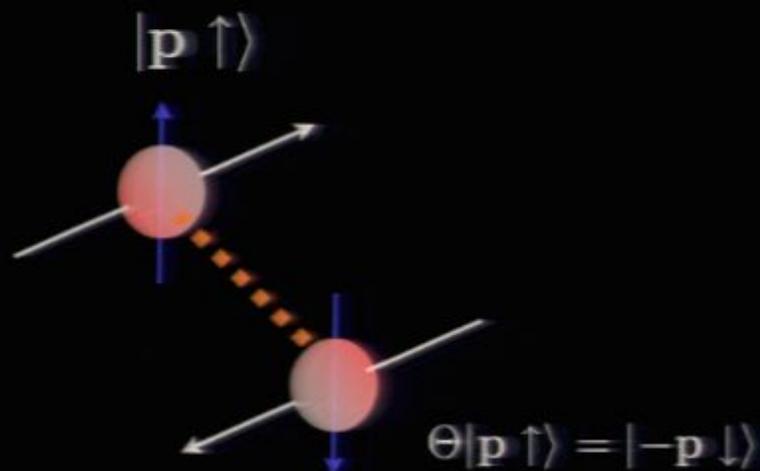


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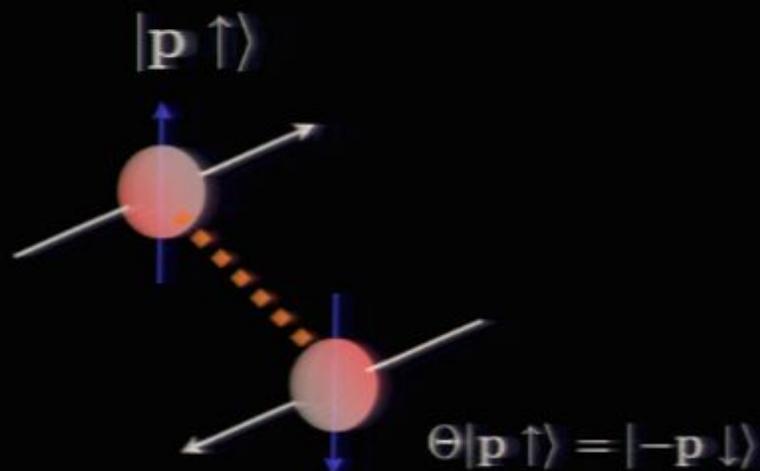
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Singlet pairing is intimately related to the inversion of spins under time-reversal.

The magnetism and neutrality of the electron spin are manifested as two discrete parities:

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$$\begin{array}{ll} S \xrightarrow{\theta} -S & \text{Magnetism} \\ S \xrightarrow{C} +S & \text{Neutrality} \end{array}$$



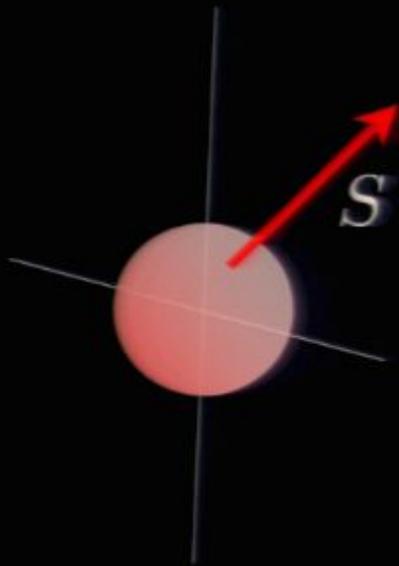
$$S + S_{\theta} = S - S = 0$$

Singlet pairing is intimately related to the inversion of spins under time-reversal

Unfortunately, these discrete parities are lost in conventional large  $N$  expansions:  
**no Cooper pairs.**

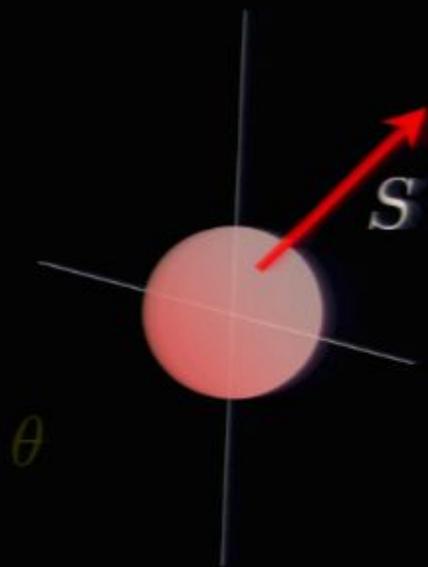
Restoring superconductivity to large N expansions requires that we understand the symmetry of time-reversal.

# The Symplectic symmetry of spin



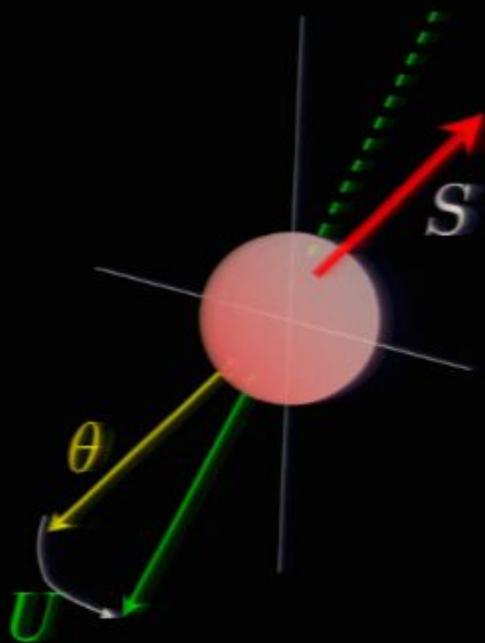
# The Symplectic symmetry of spin

Rotation x time reversal



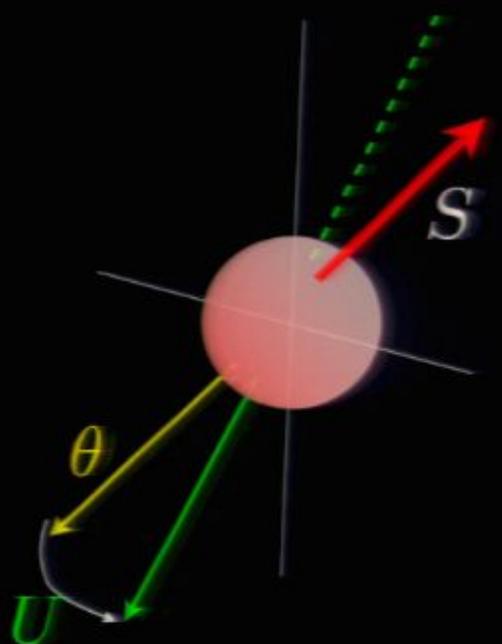
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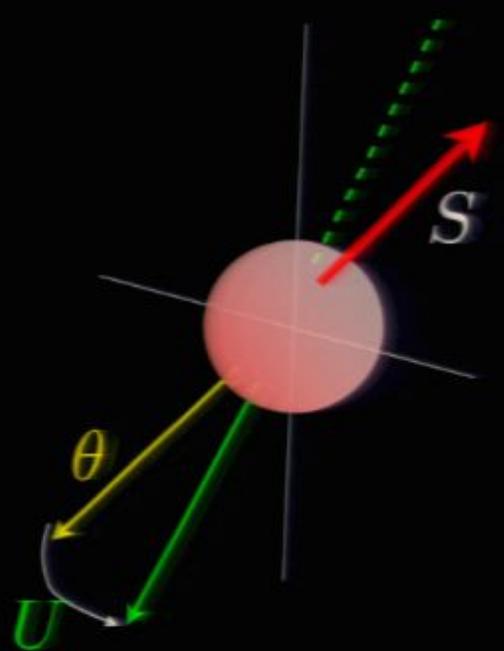


$$S \xrightarrow{U\theta} \underline{R}(-S)$$

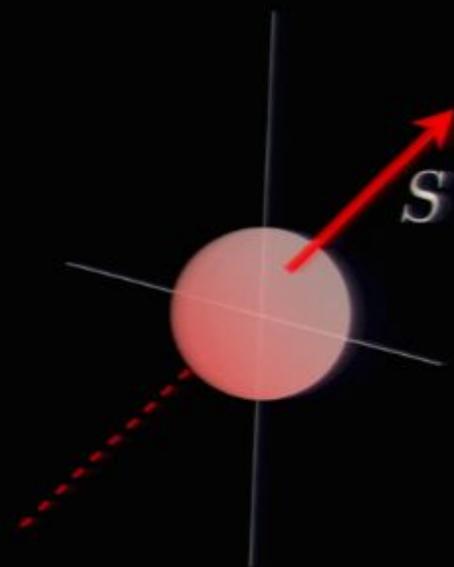
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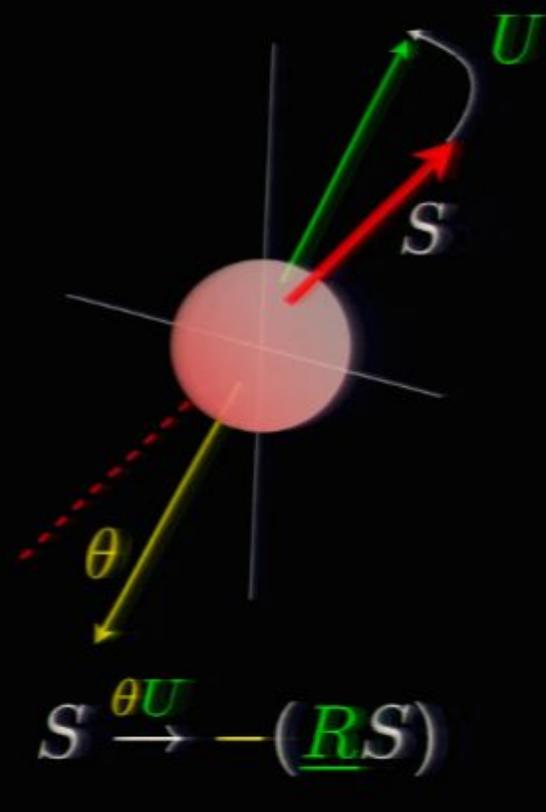
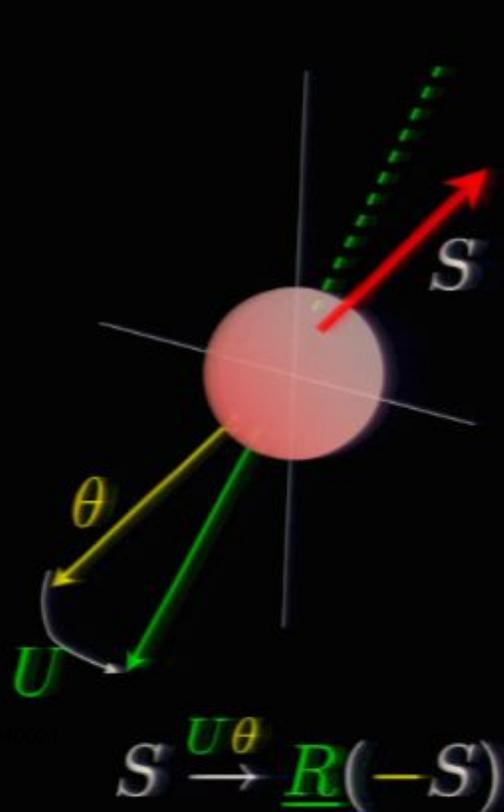
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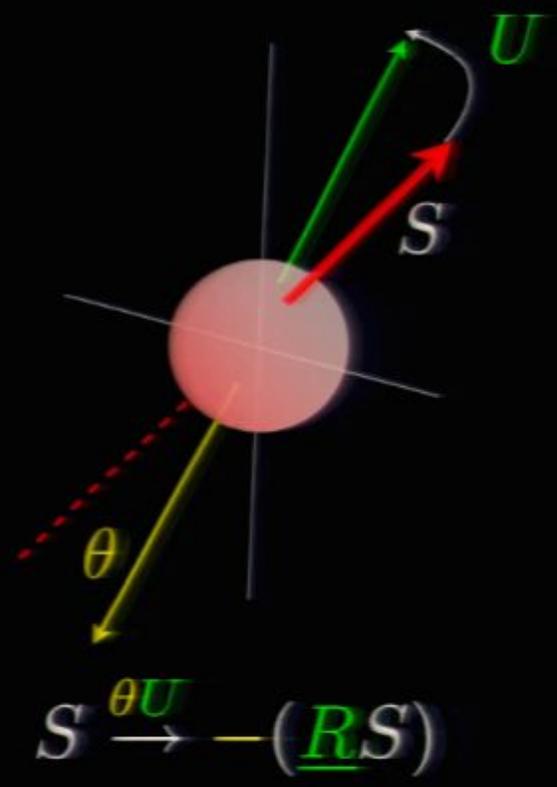
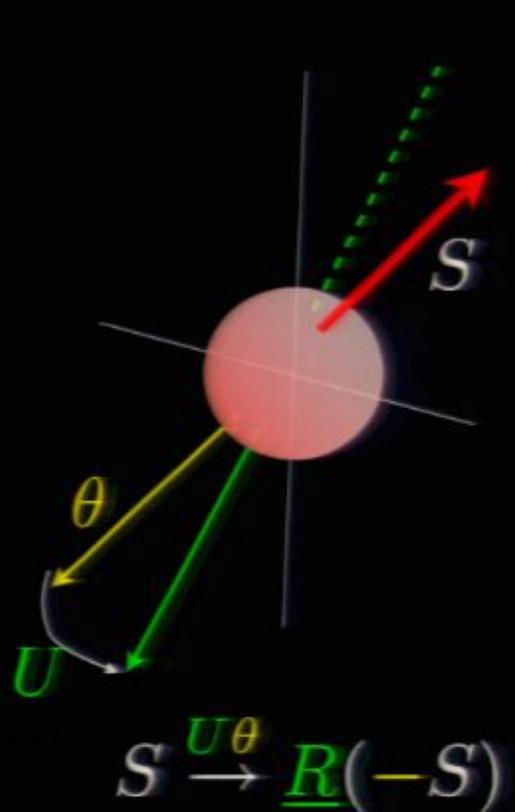
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Rotation x time reversal = Time reversal x rotation

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$$U i\sigma_2 U^T = i\sigma_2$$

**SYMPLECTIC CONDITION**

N-component Symplectic spin operator:  
generator of SP(N)

$$S_{\alpha\beta} = f_{\alpha}^{\dagger} f_{\beta} - \tilde{\alpha}\tilde{\beta} f_{-\beta}^{\dagger} f_{-\alpha}$$

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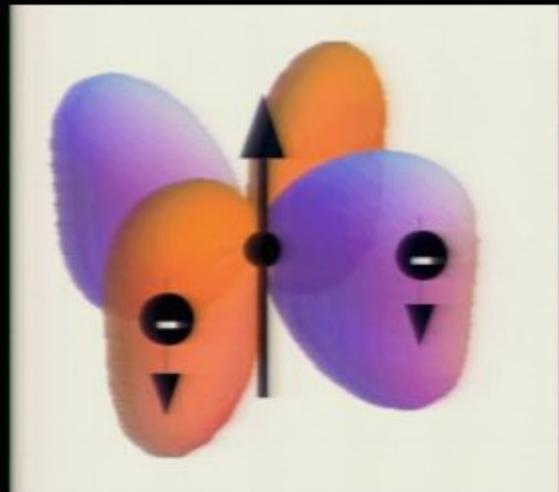
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Singlet pair commutes with symplectic spin

→ Local SU(2) gauge symmetry.

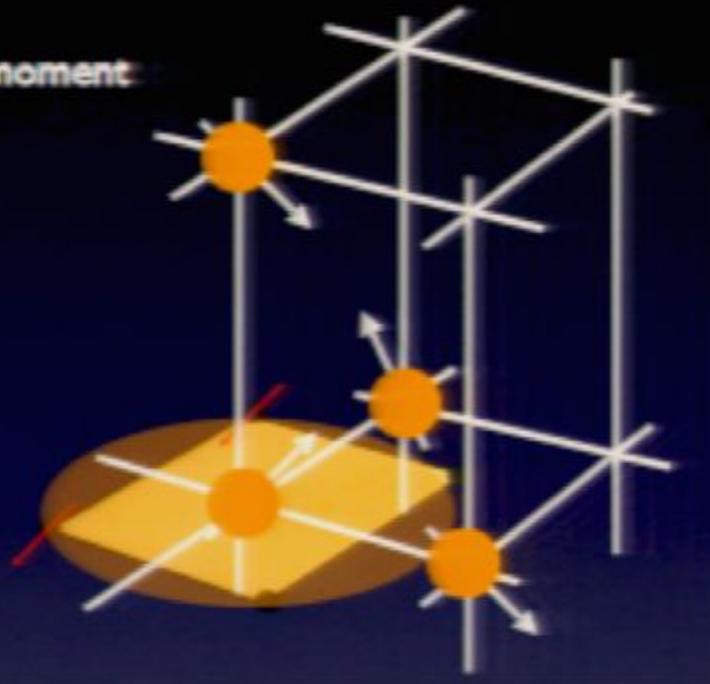
Composite pairing in the Kondo Lattice

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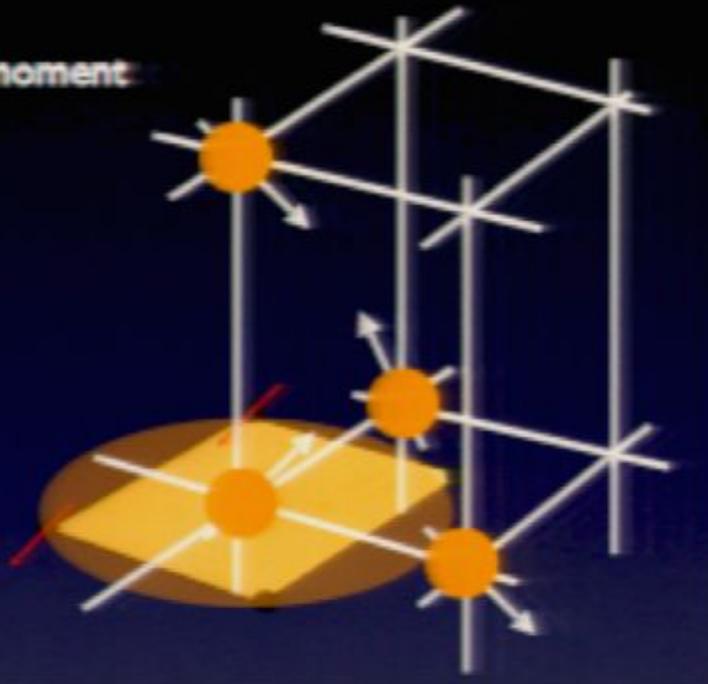
# Model for $\text{PuCoGa}_5$ & $\text{NpPd}_2\text{Al}_5$

Pu moment:



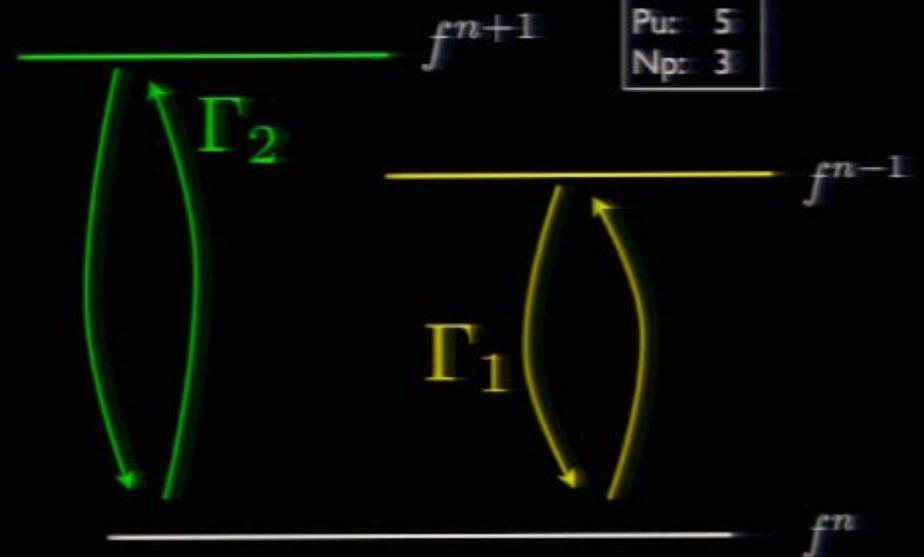
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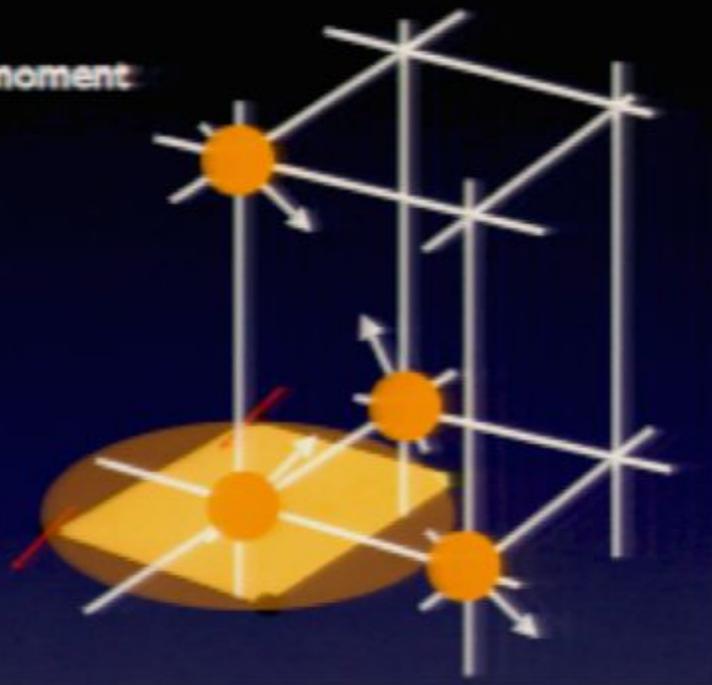
Tetragonal CF

|     |     |
|-----|-----|
|     | $n$ |
| Pu: | 5   |
| Np: | 3   |



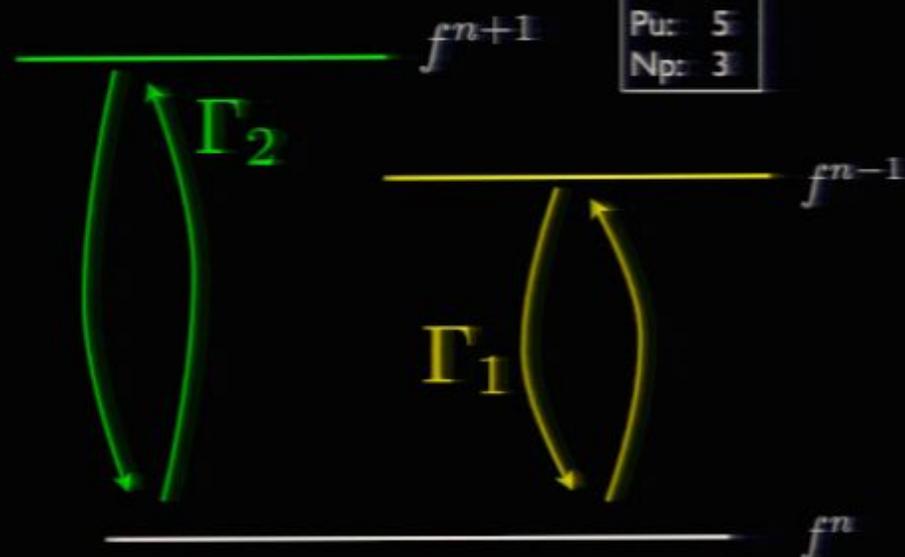
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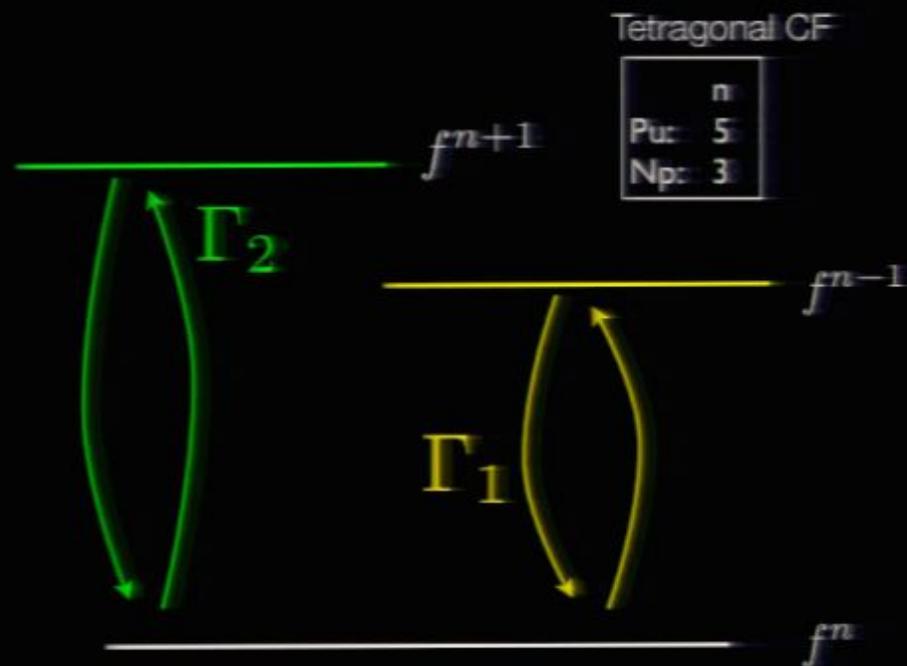
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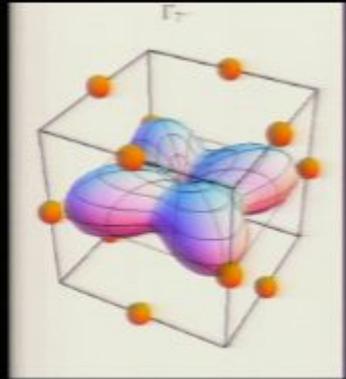
Virtual valence fluctuations mediate  
Kondo-spin exchange in two channels with  
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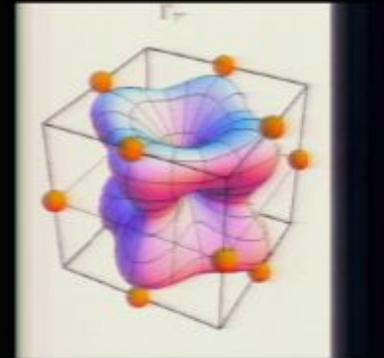
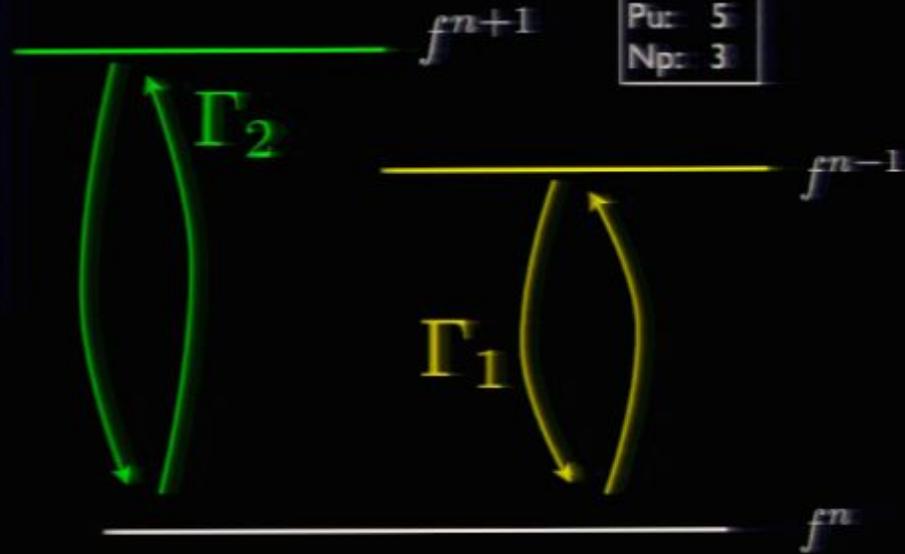


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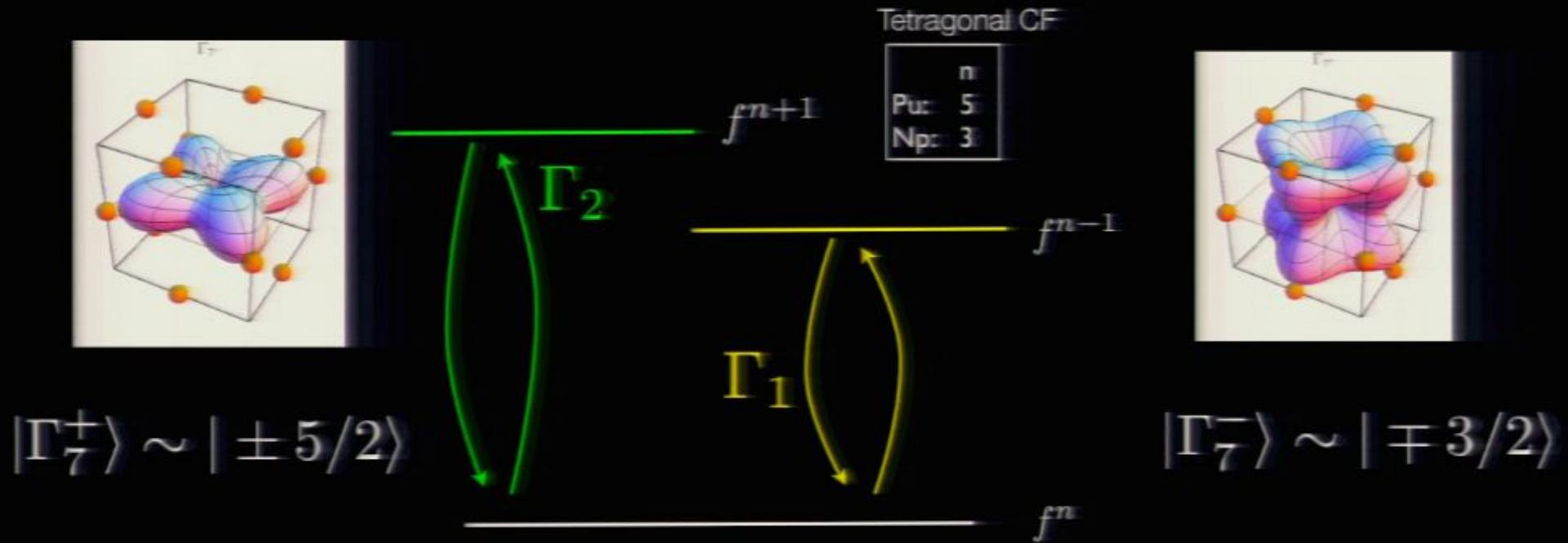
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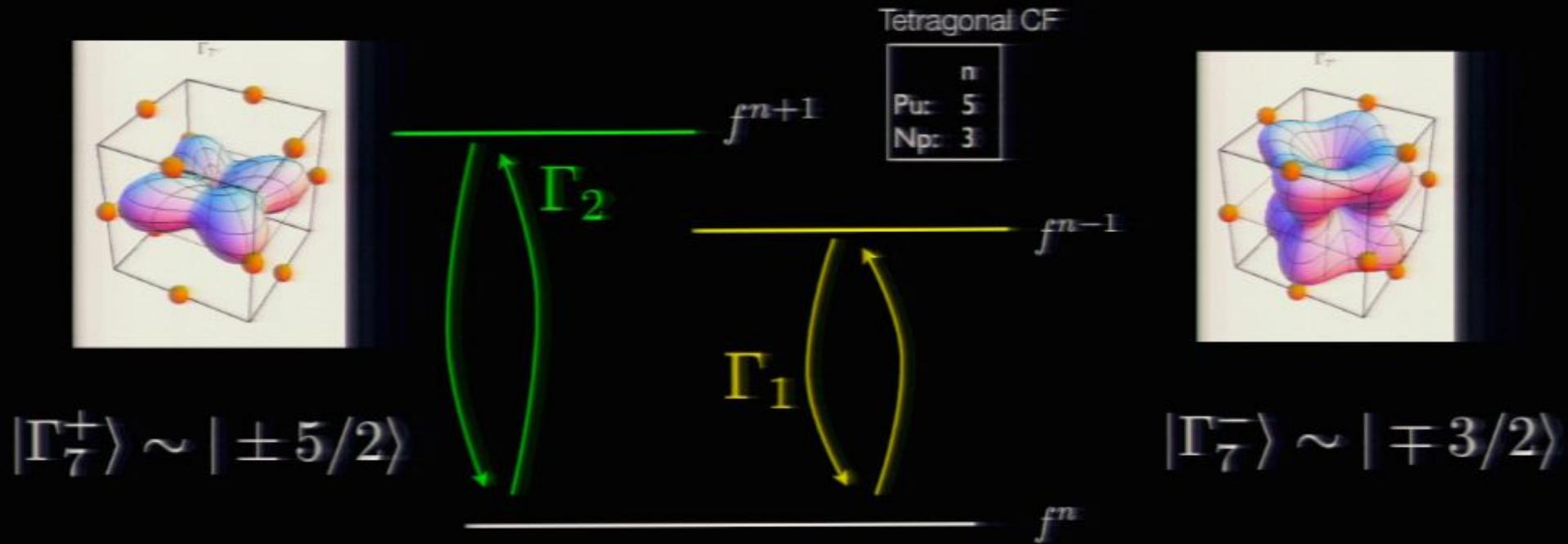
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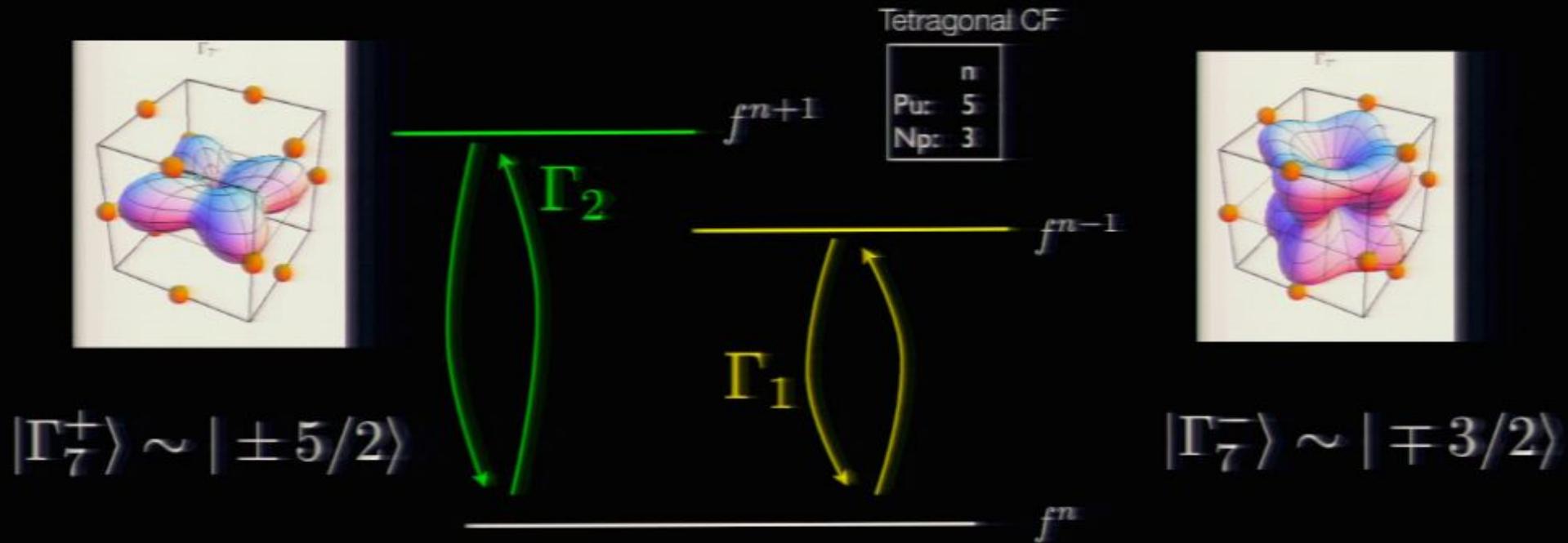
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$$H = \sum_k \epsilon_k c_{k\sigma}^{\dagger} c_{k\sigma} + \frac{1}{N} \sum_{k,k'} \left( J_1 \psi_{1a}^{\dagger}(j) \psi_{1b}(j) + J_2 \psi_{2a}^{\dagger}(j) \psi_{2b}(j) \right) S^{ba}(j)$$

Single FS, two channels.

$$\psi_{\Gamma}(j) = \frac{1}{\sqrt{V}} \sum_k \gamma_{\Gamma k} c_k e^{ik \cdot x_j}$$

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# Decoupling the interactions:

$$\begin{aligned} H_I &= \frac{J_K}{N} \sum \psi_a^\dagger \psi_b \overbrace{\left( f_b^\dagger f_a - \tilde{a}\tilde{b} f_{-a}^\dagger f_{-b} \right)}^{S_{ba}} \\ &= -\frac{J_K}{N} \sum \left[ (\psi^\dagger f)(f^\dagger \psi) + (\psi^\dagger \sigma_2 f^\dagger)(f \sigma_2 \psi) \right]. \end{aligned}$$

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The gauge-invariant cross term  $V_1 \Delta_2 - V_2 \Delta_1$  describe the overscreened formation of composite pairs

$$\langle \vec{S} \cdot \psi_1 \sigma_2 \vec{\sigma} \psi_2 \rangle \sim V_1 \Delta_2 - V_2 \Delta_1$$

PC, Kee, Andrei & Tsvetlik. (97)

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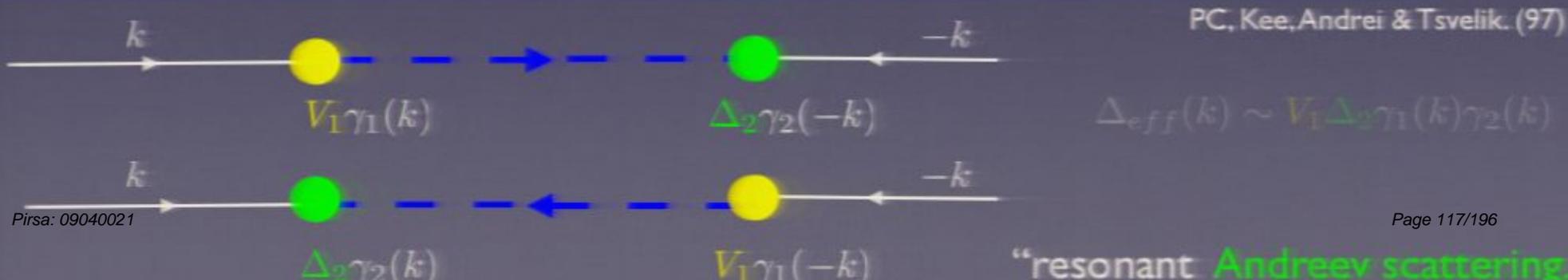
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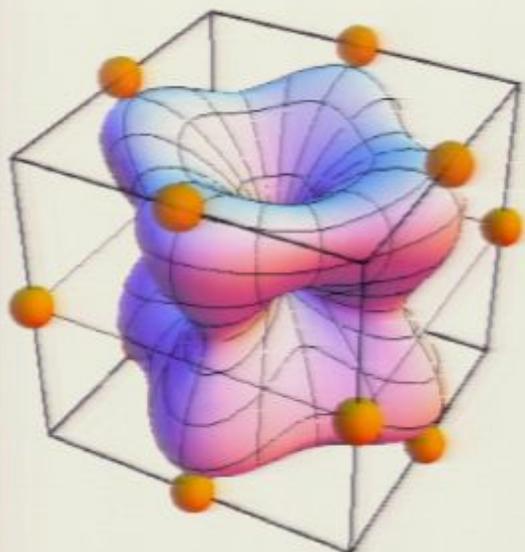
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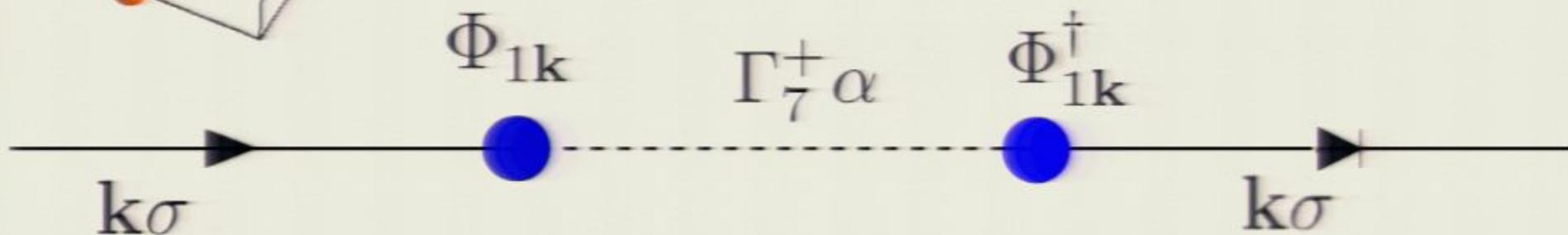
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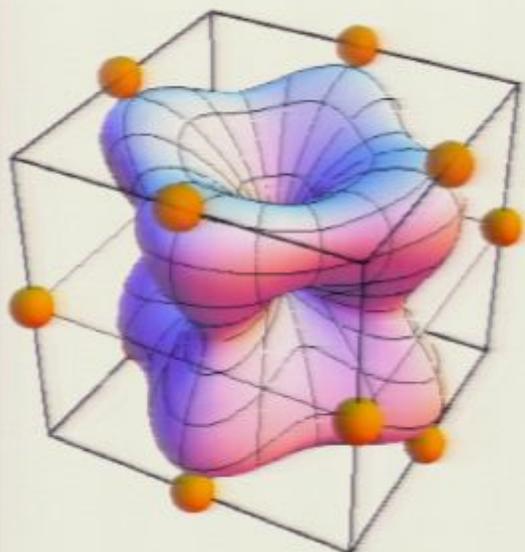
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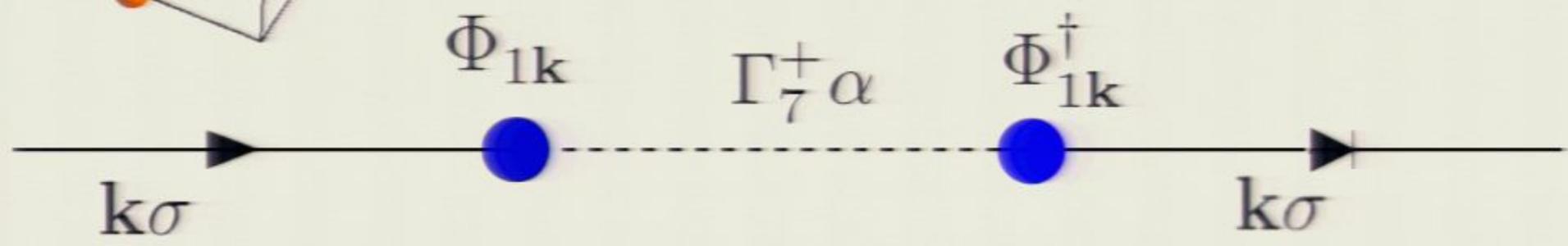


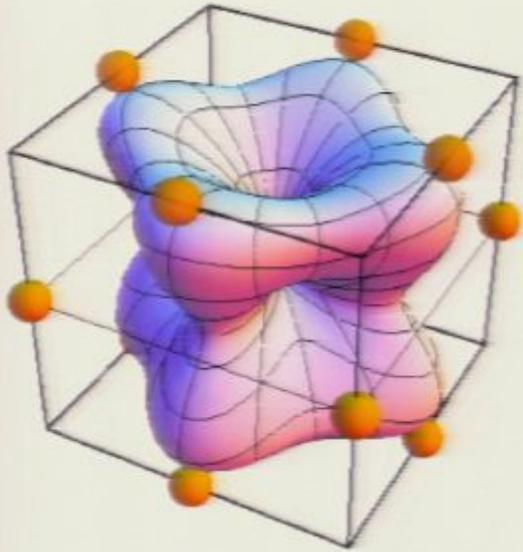
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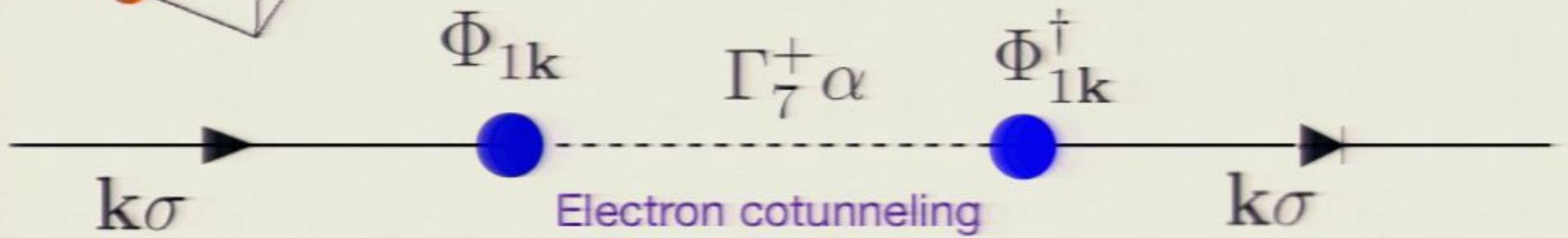


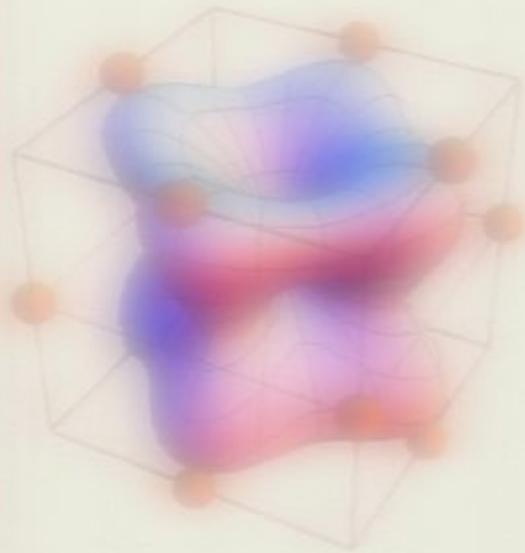
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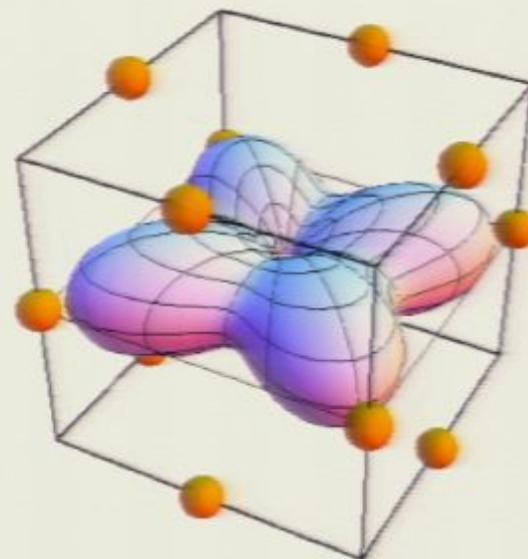
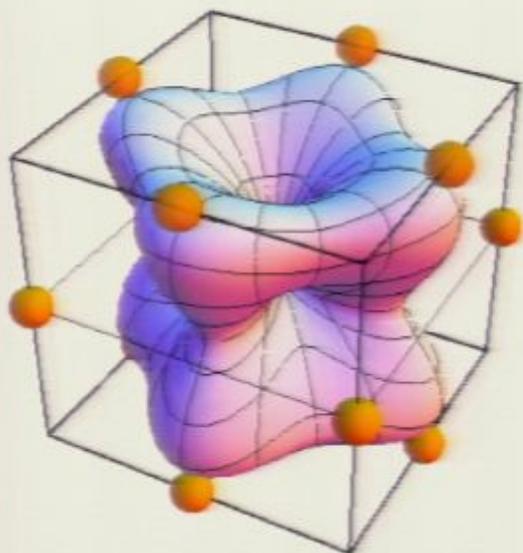


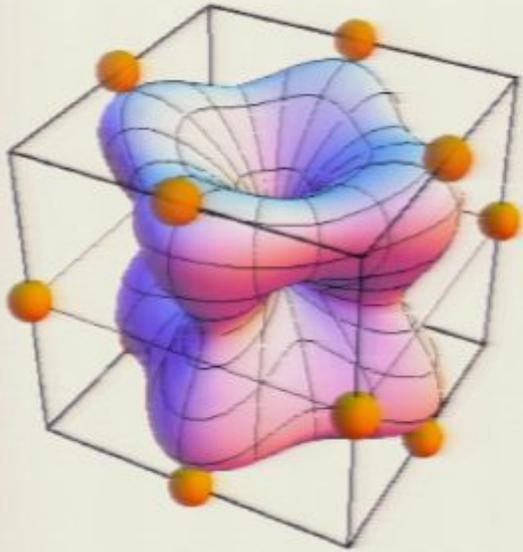


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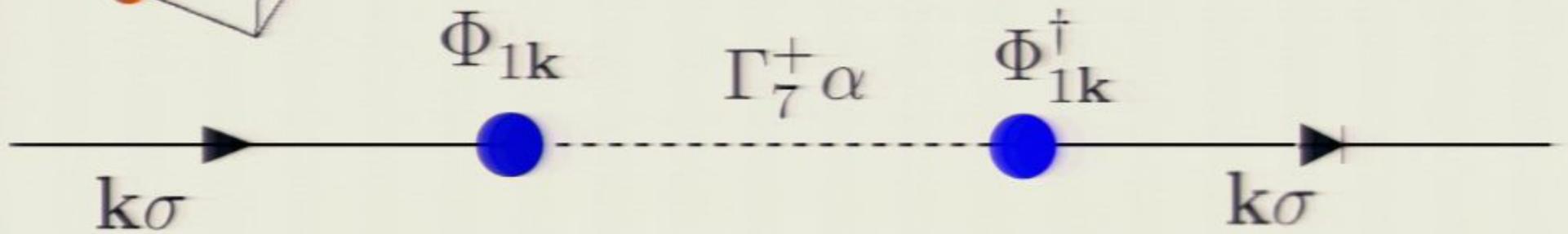


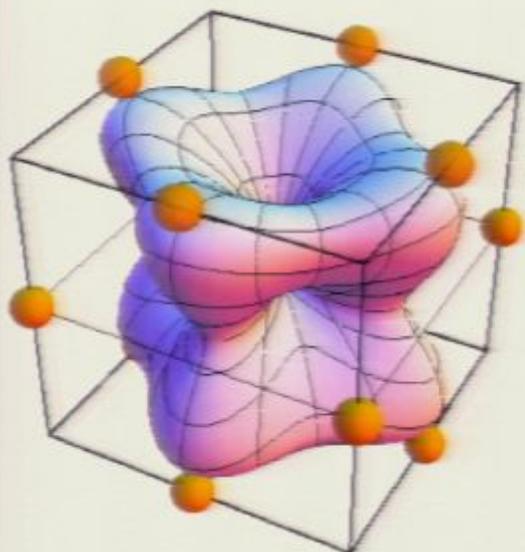




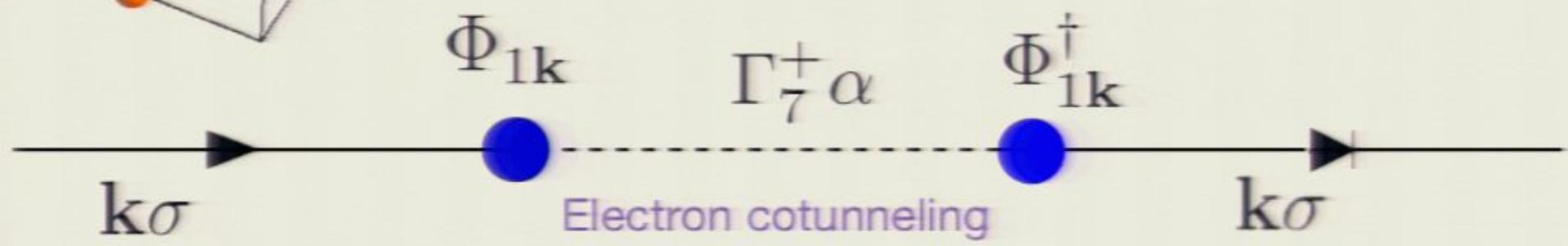


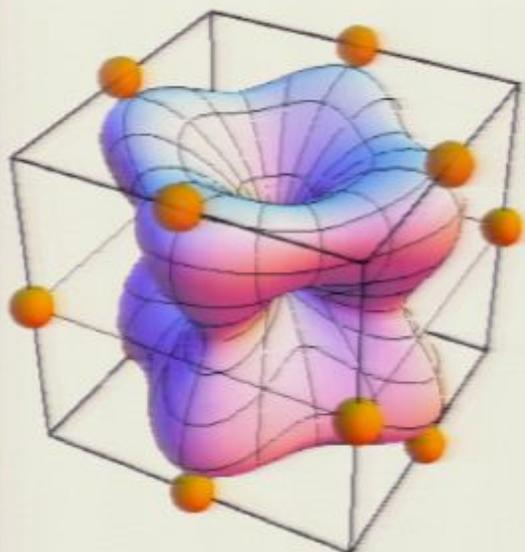
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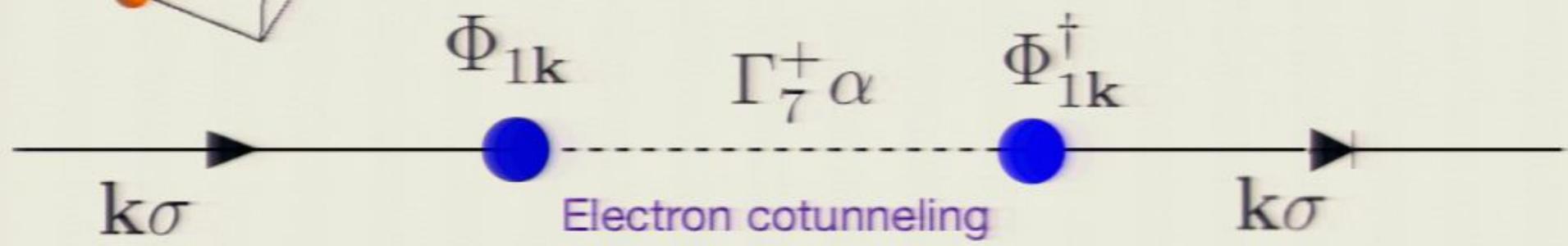


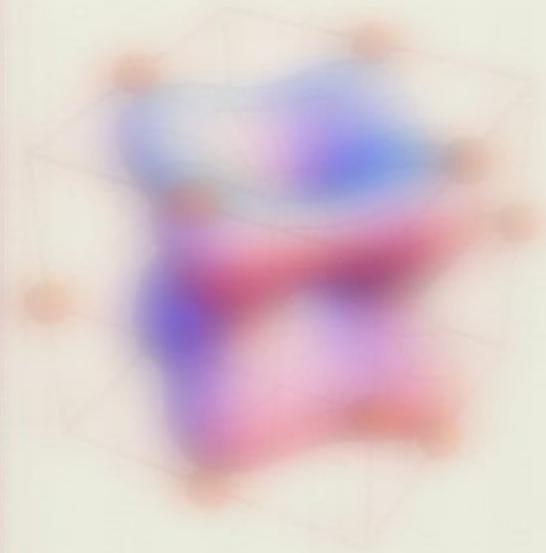
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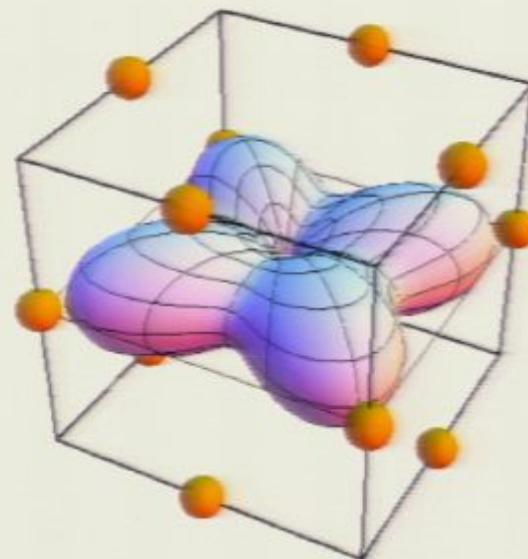
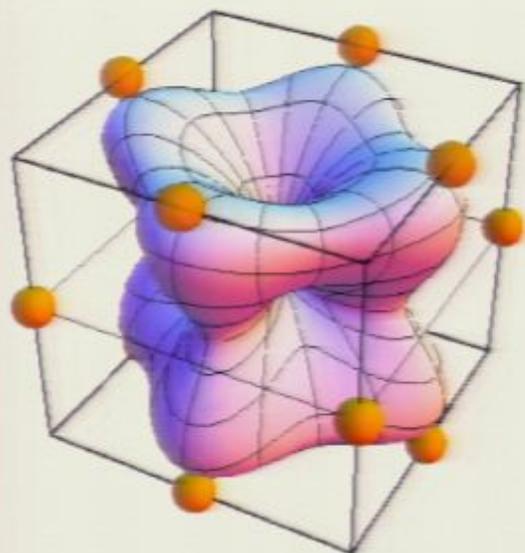


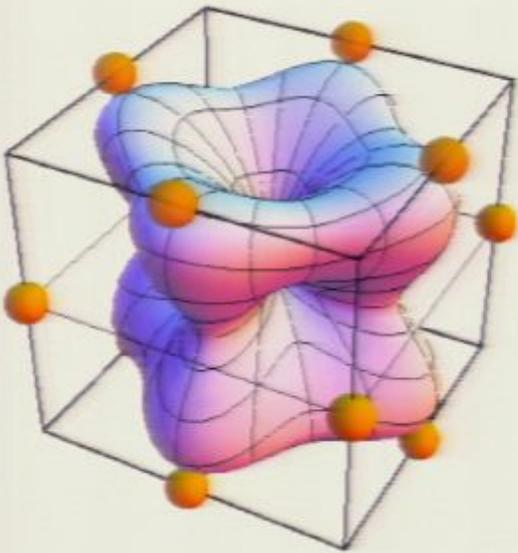


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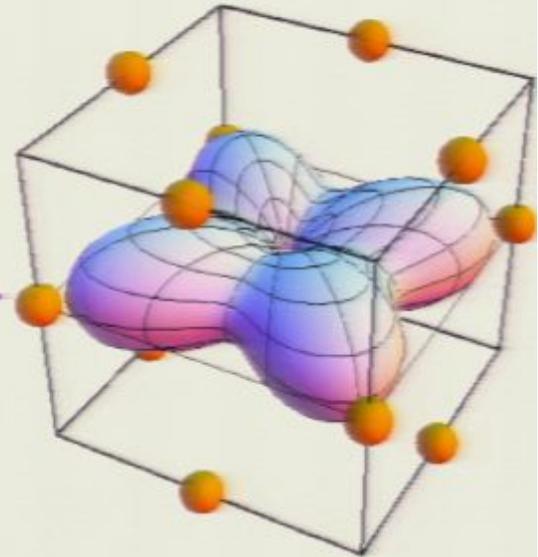
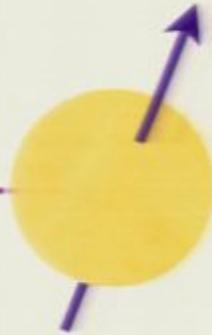


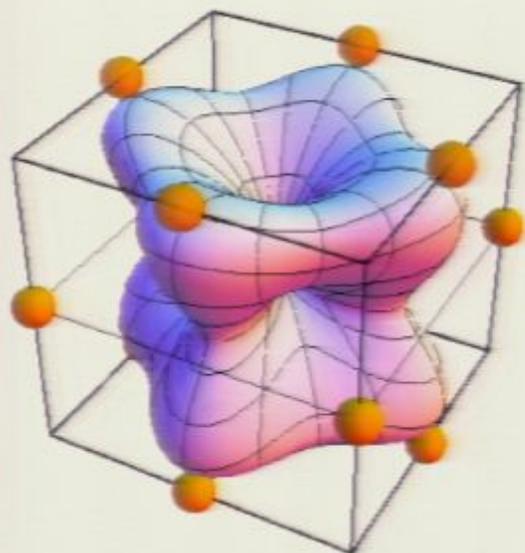




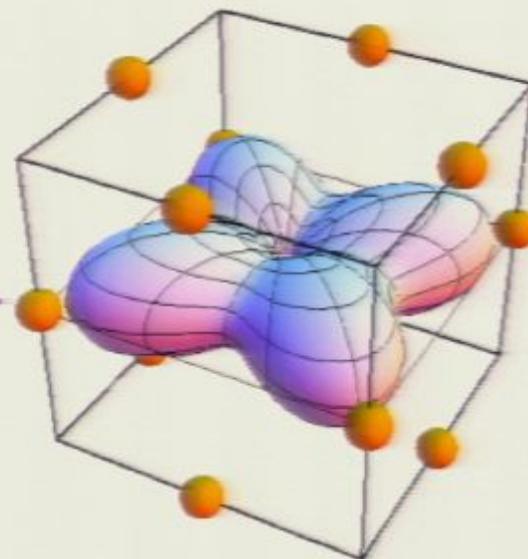
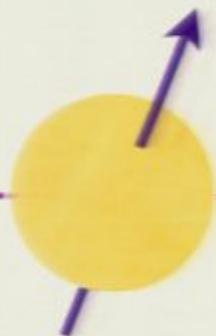


$$\langle \psi_2^\dagger \vec{\sigma} \epsilon \psi_1^\dagger \cdot \vec{S} \rangle$$



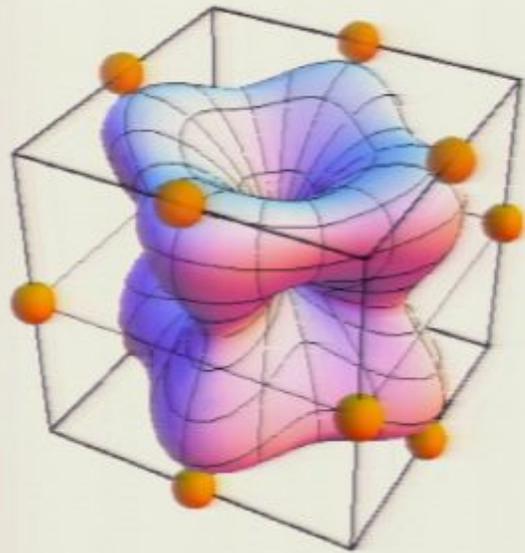


$$\langle \psi_2^\dagger \vec{\sigma} \epsilon \psi_1^\dagger \cdot \vec{S} \rangle$$

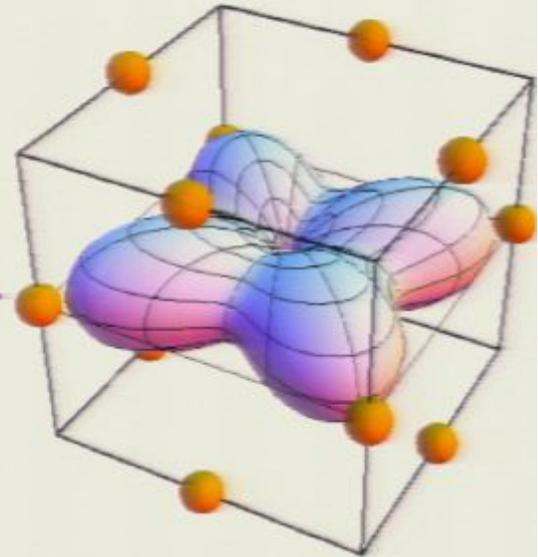
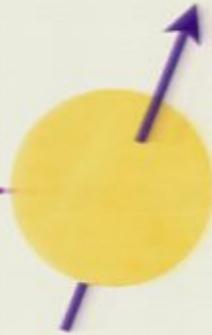


$$\Phi_{1k}$$



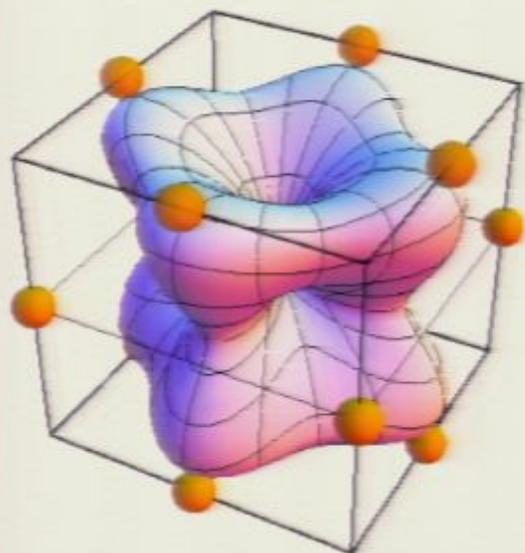


$$\langle \psi_2^\dagger \vec{\sigma} \epsilon \psi_1^\dagger \cdot \vec{S} \rangle$$

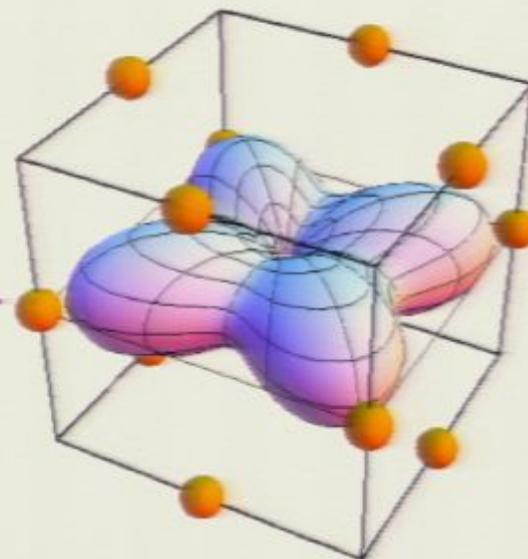
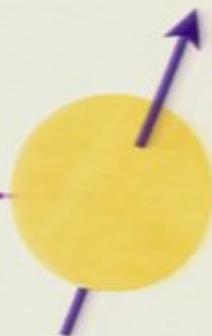


$$\Phi_{1k}$$



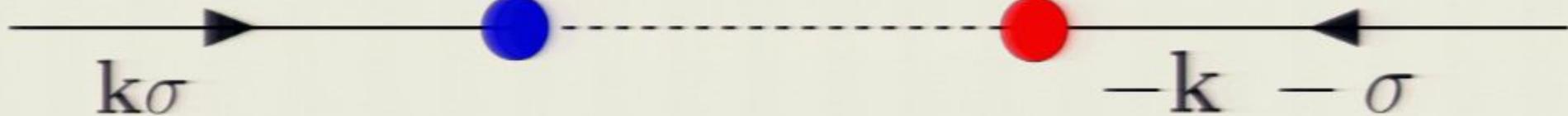


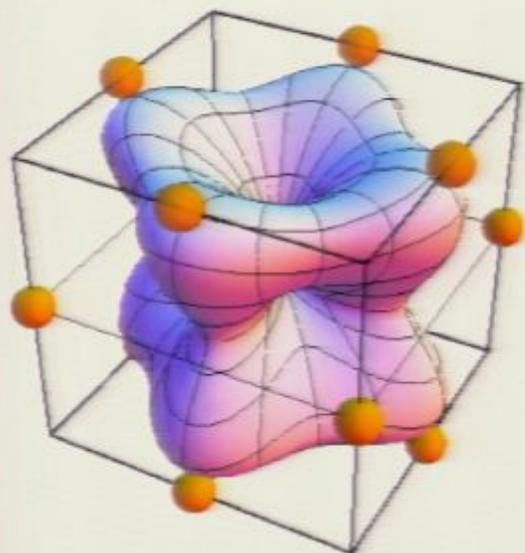
$$\langle \psi_2^\dagger \vec{\sigma} \epsilon \psi_1^\dagger \cdot \vec{S} \rangle$$



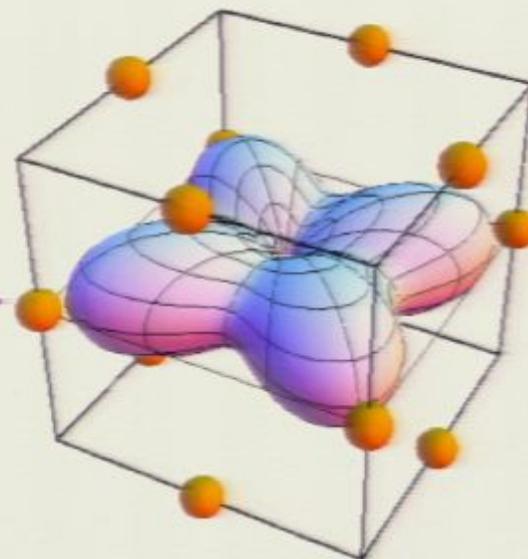
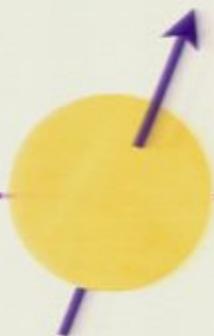
$$\Phi_{1\mathbf{k}}$$

$$\Phi_{2\mathbf{k}}^\dagger$$



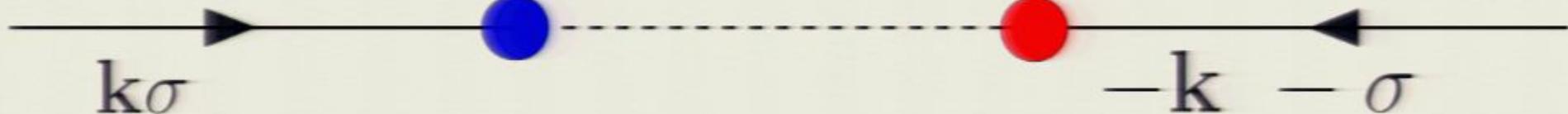


$$\langle \psi_2^\dagger \vec{\sigma} \epsilon \psi_1^\dagger \cdot \vec{S} \rangle$$

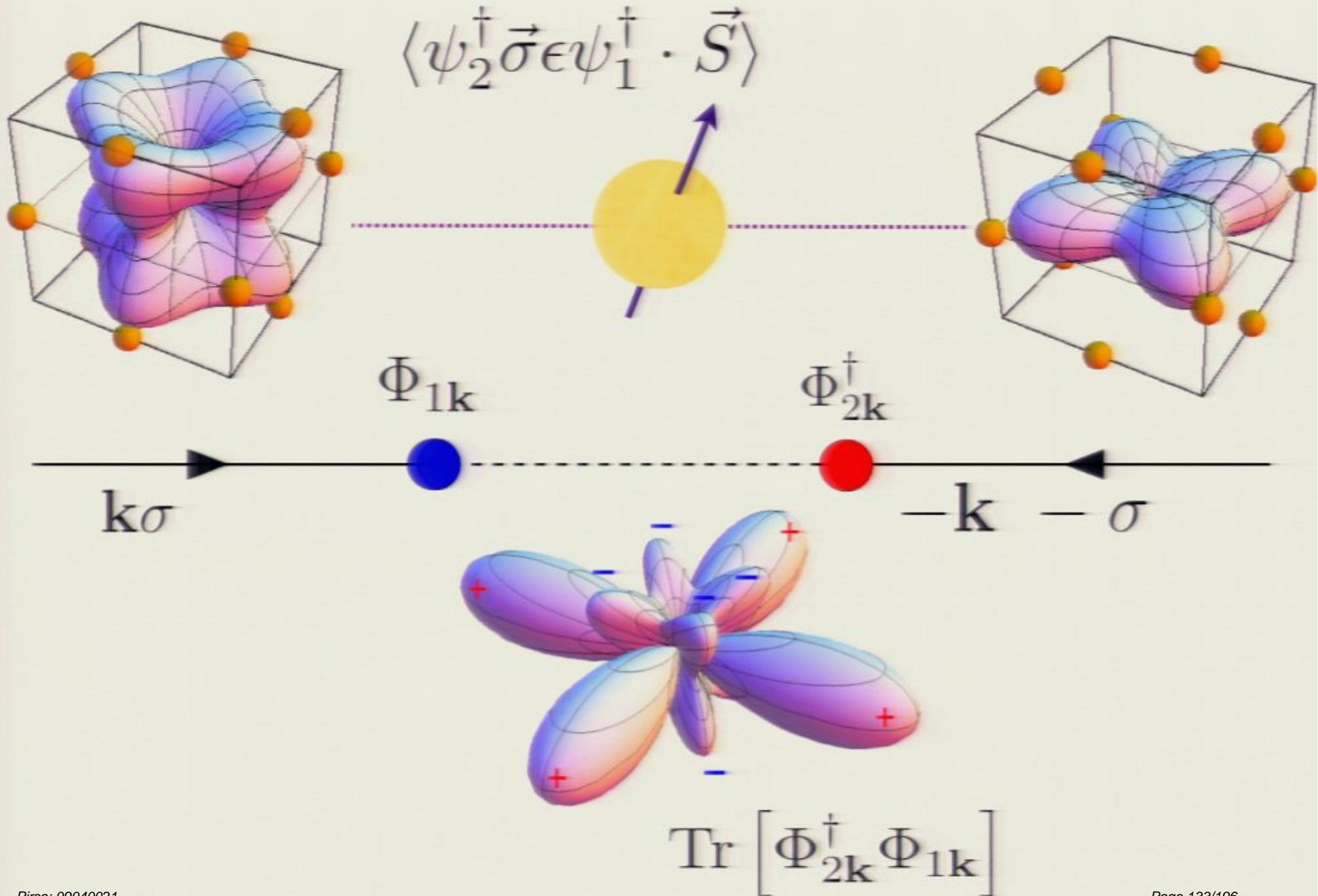


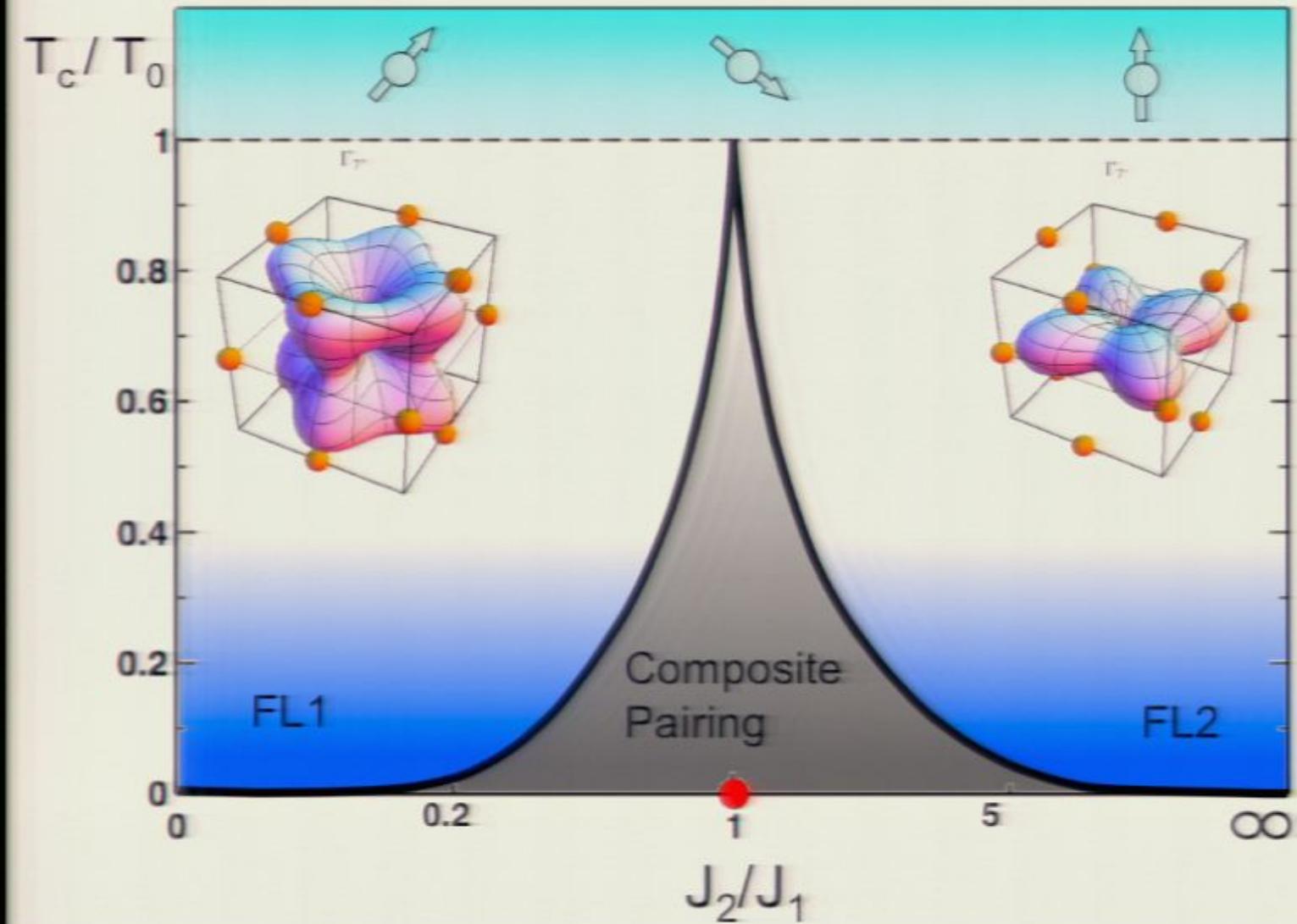
$$\Phi_{1\mathbf{k}}$$

$$\Phi_{2\mathbf{k}}^\dagger$$

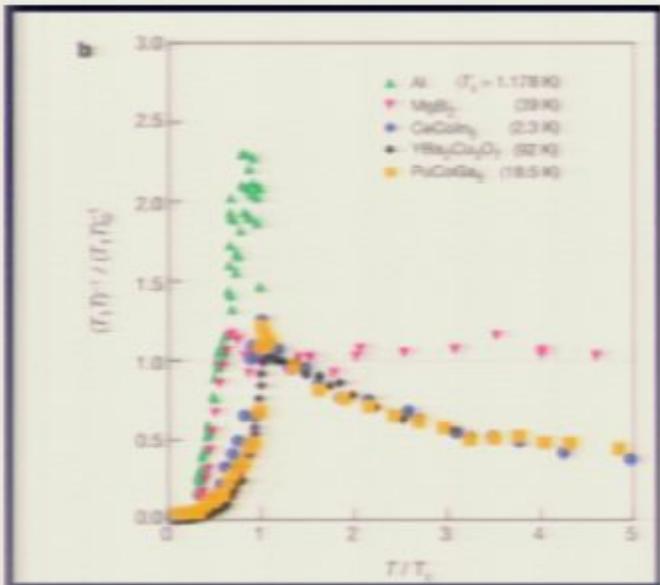


$$\text{Tr} \left[ \Phi_{2\mathbf{k}}^\dagger \Phi_{1\mathbf{k}} \right]$$

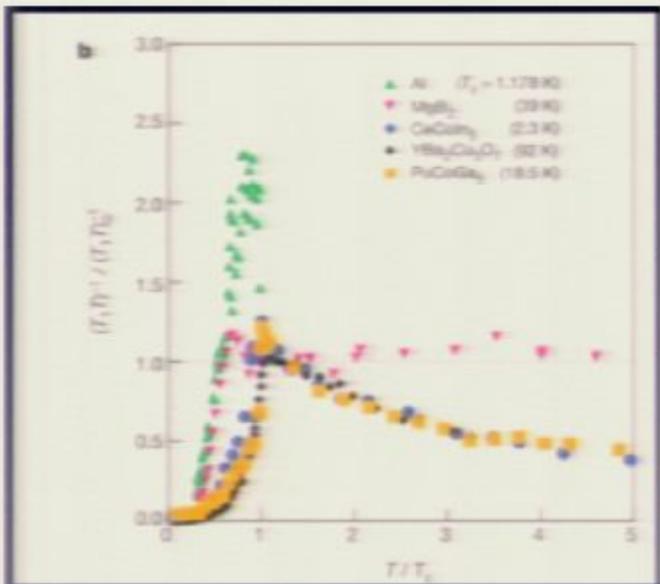




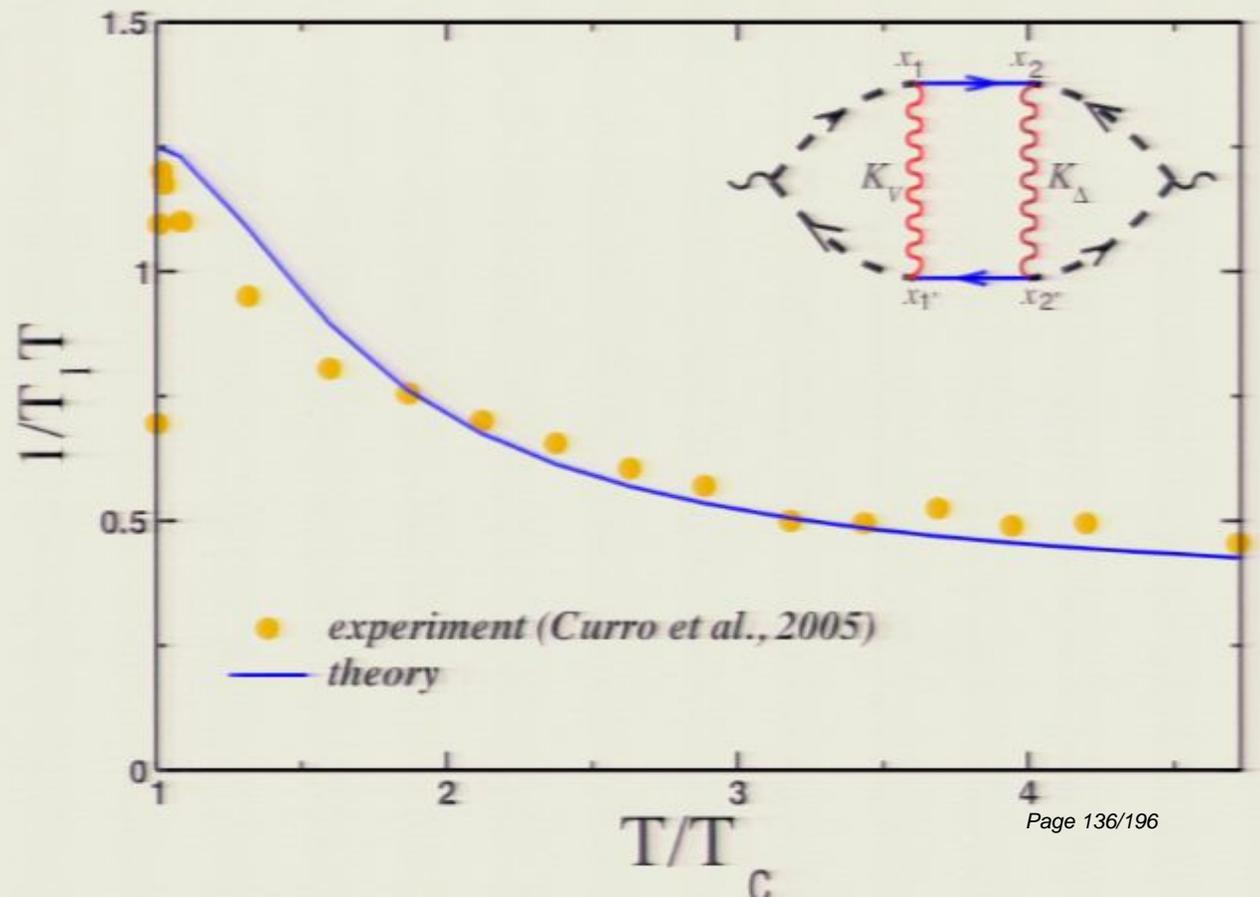
Avoided two-channel critical point gives rise to composite pairing



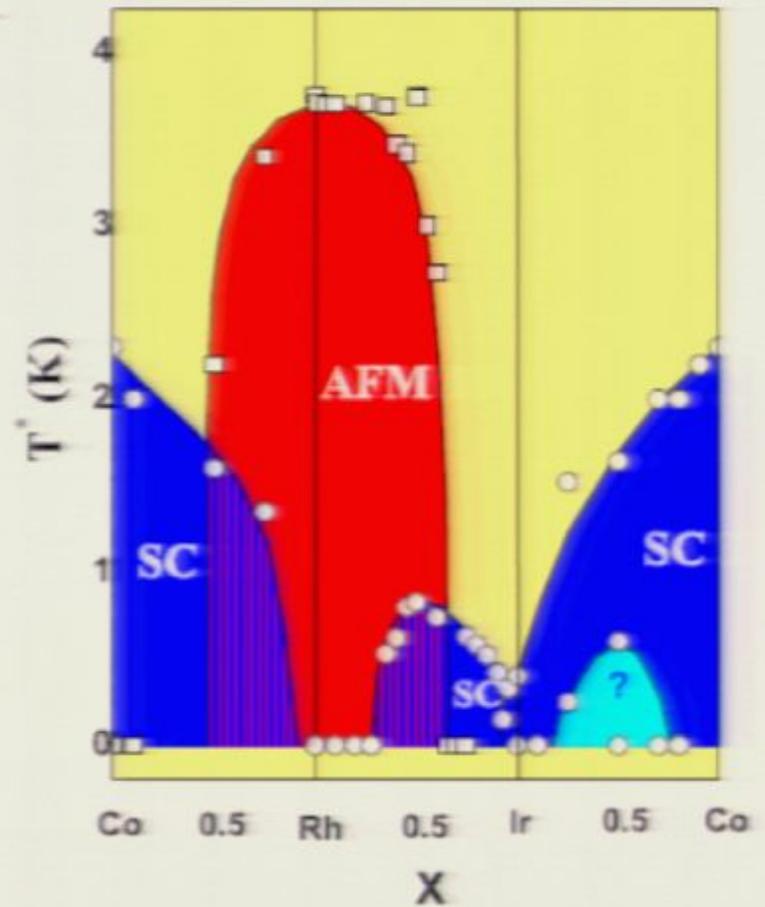
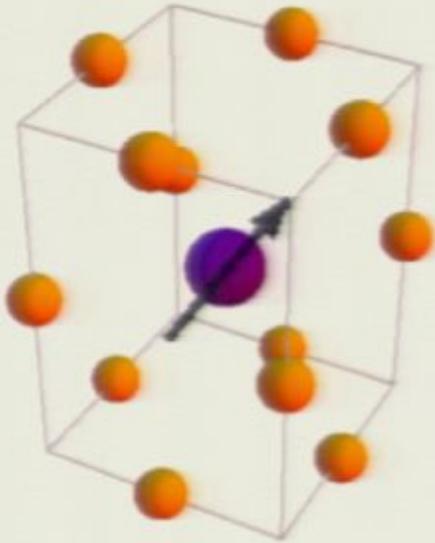
Curro et al, Nature, 434,622 (2005).



Curro et al, Nature, 434,622 (2005).

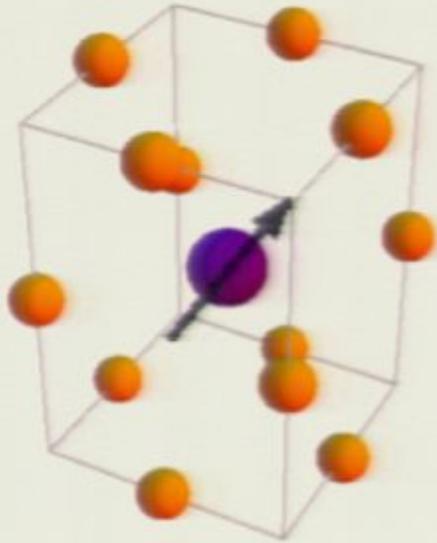


Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$

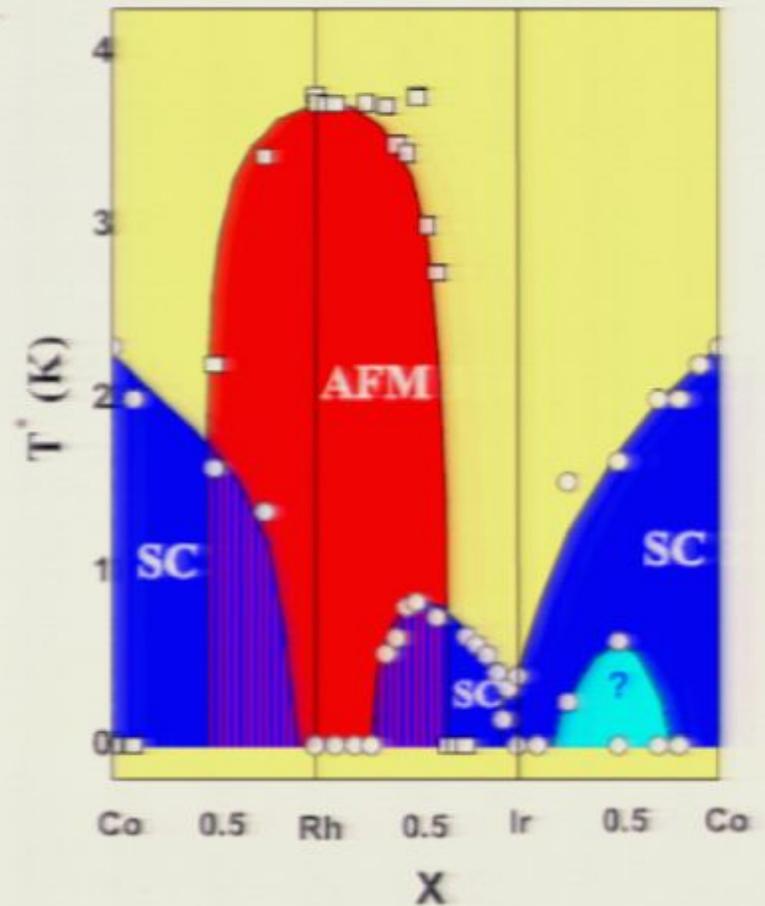


Sarrao and Thomson. JPSJ 76. 051013(2007)

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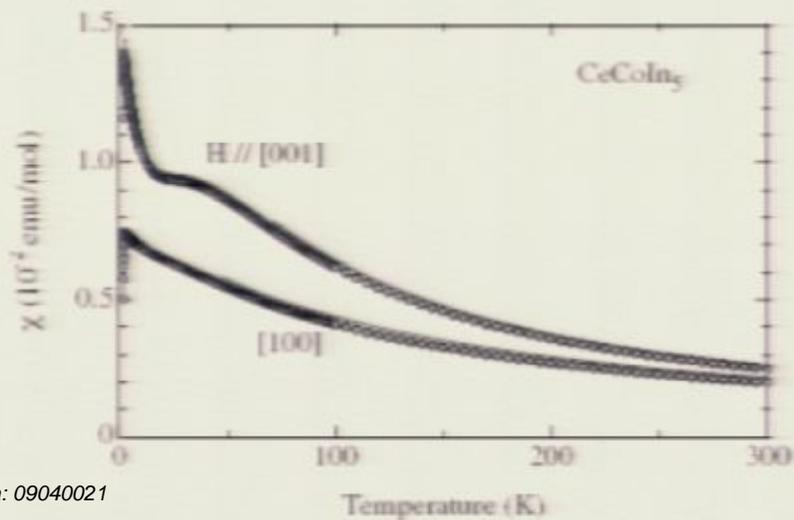
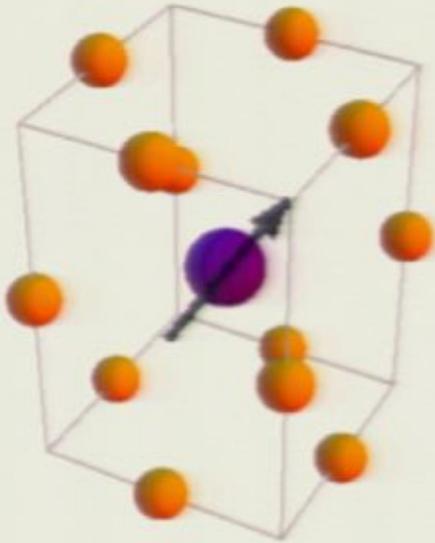


"Magnetically mediated pairing"

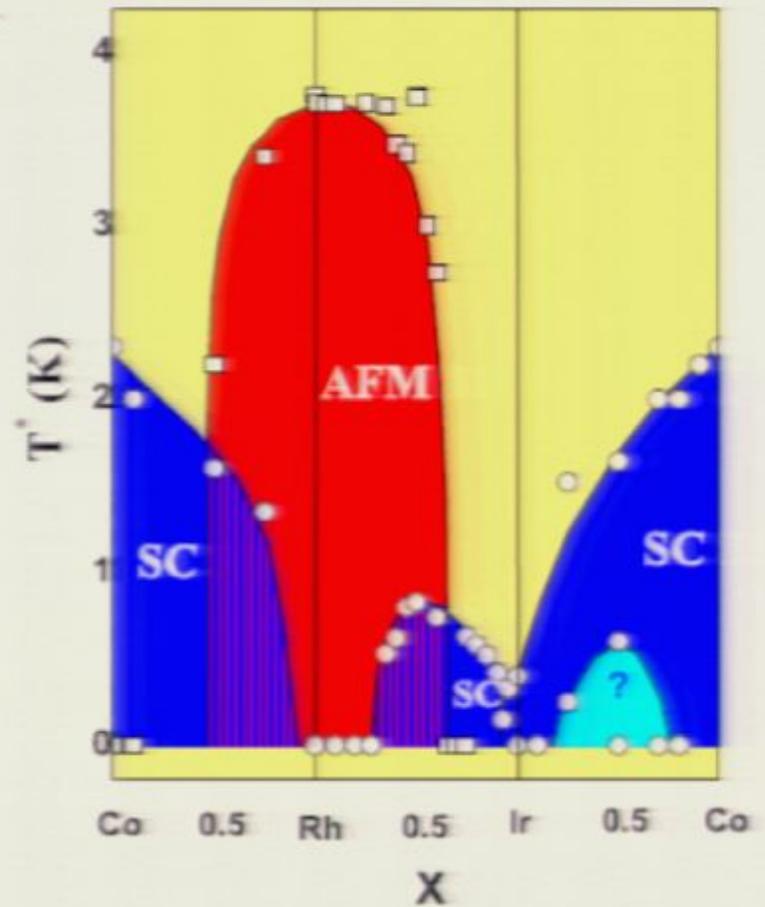


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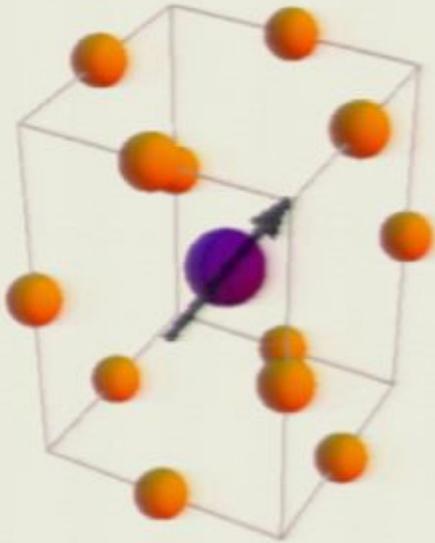


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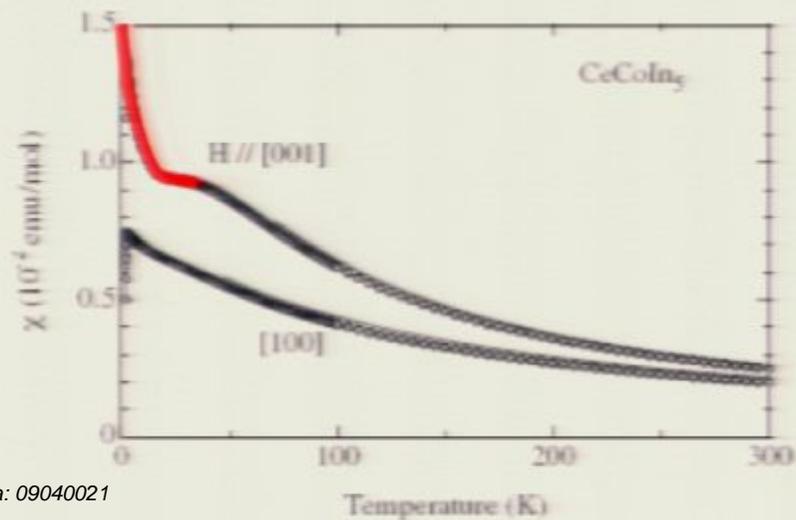


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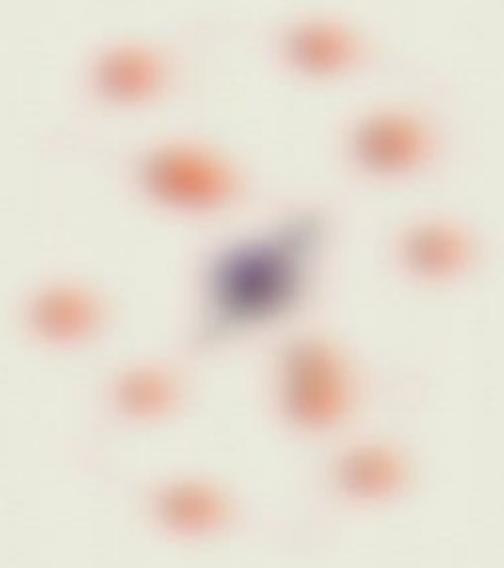


Composite pairing?



Temperature dependence of the heat capacity of a diatomic gas

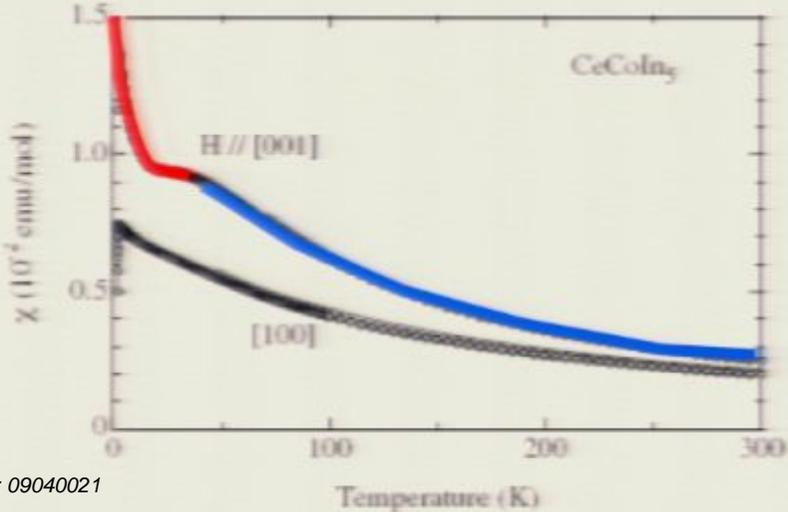
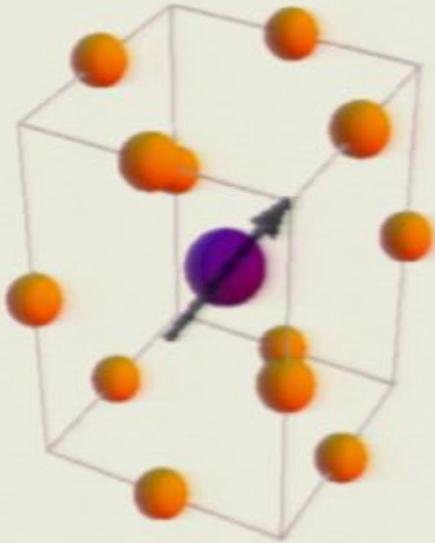
Equipartition theorem



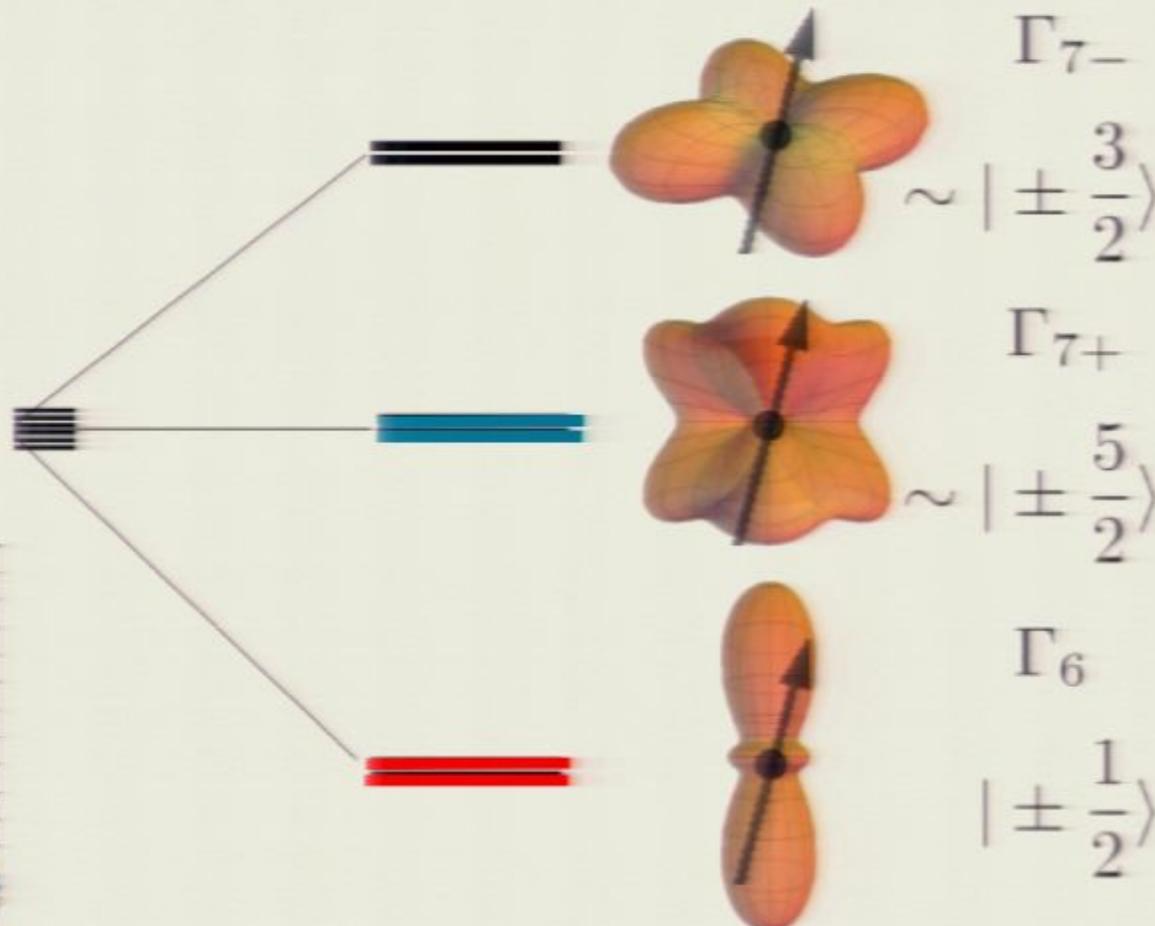
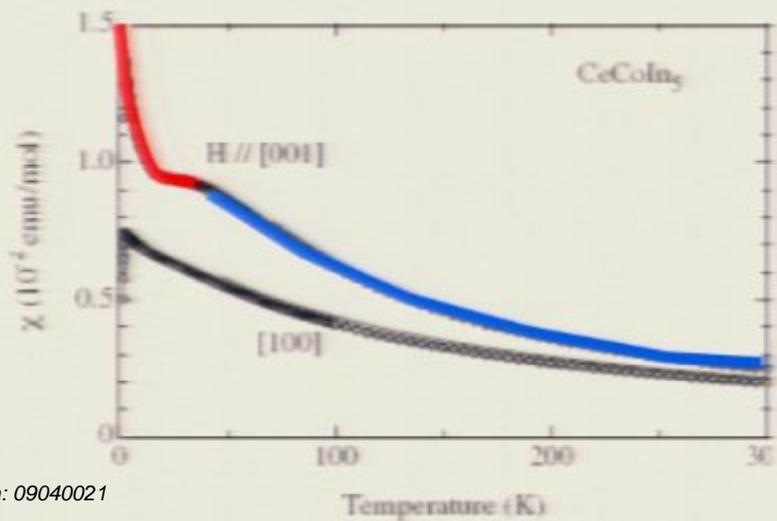
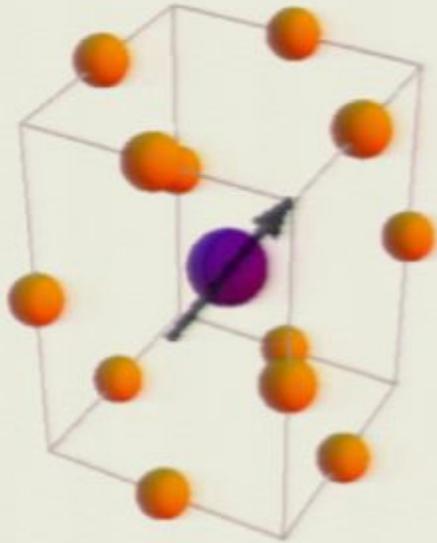
Equipartition theorem



# Ongoing challenge to unify magnetically mediated pairing and composite pairing: $\text{CeCoIn}_5$

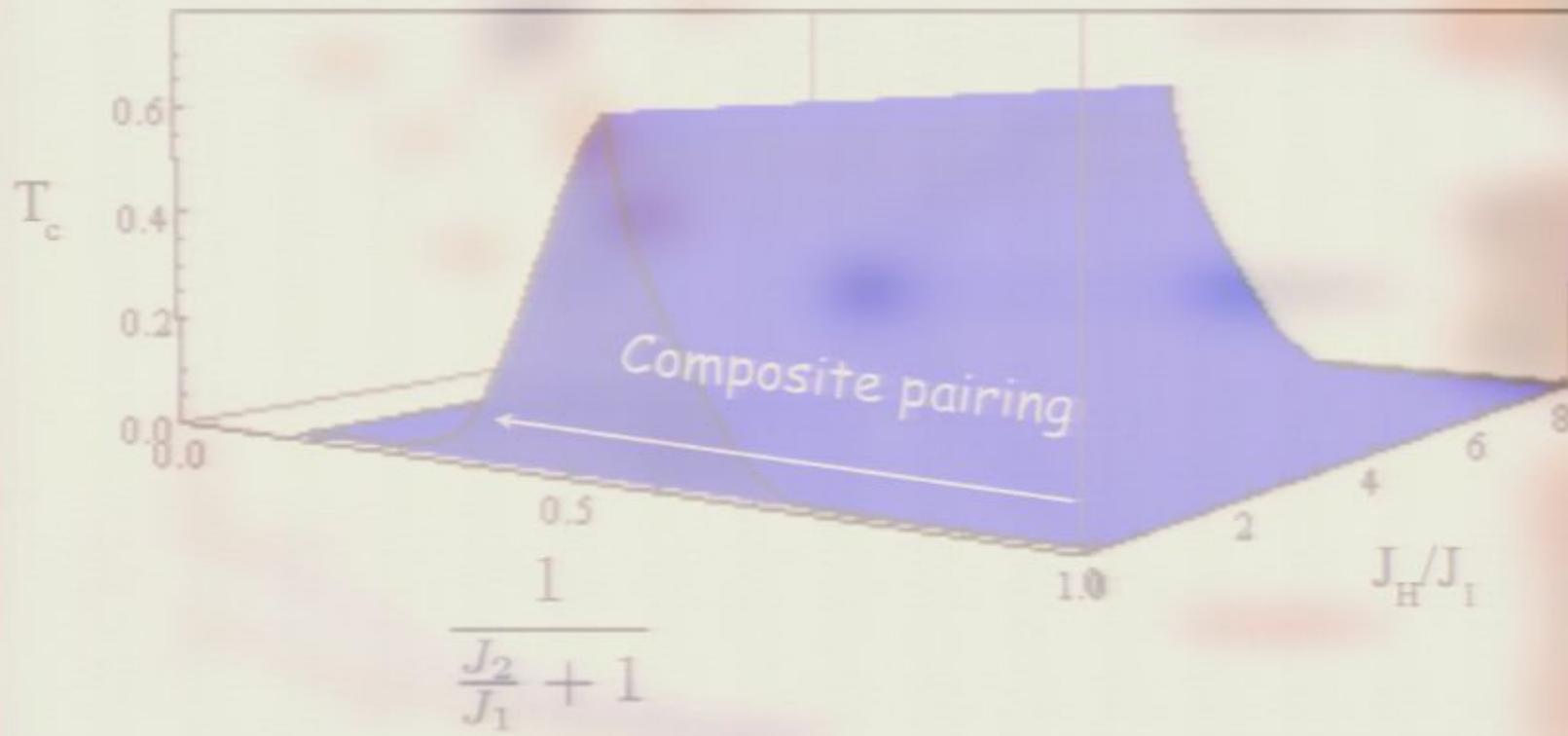


# Ongoing challenge to unify magnetically mediated pairing and composite pairing: $\text{CeCoIn}_5$



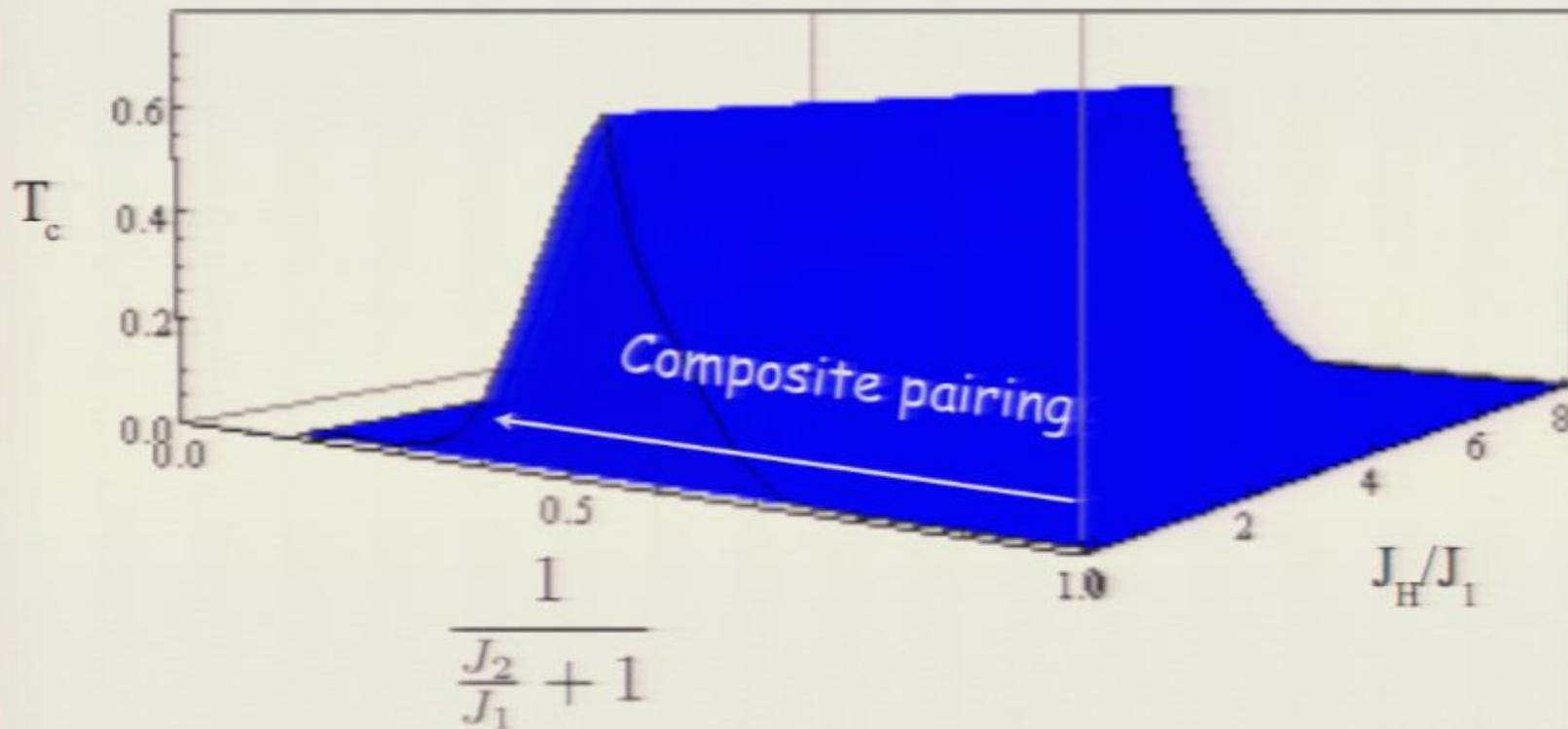
Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$

- Composite Pair Superconductivity



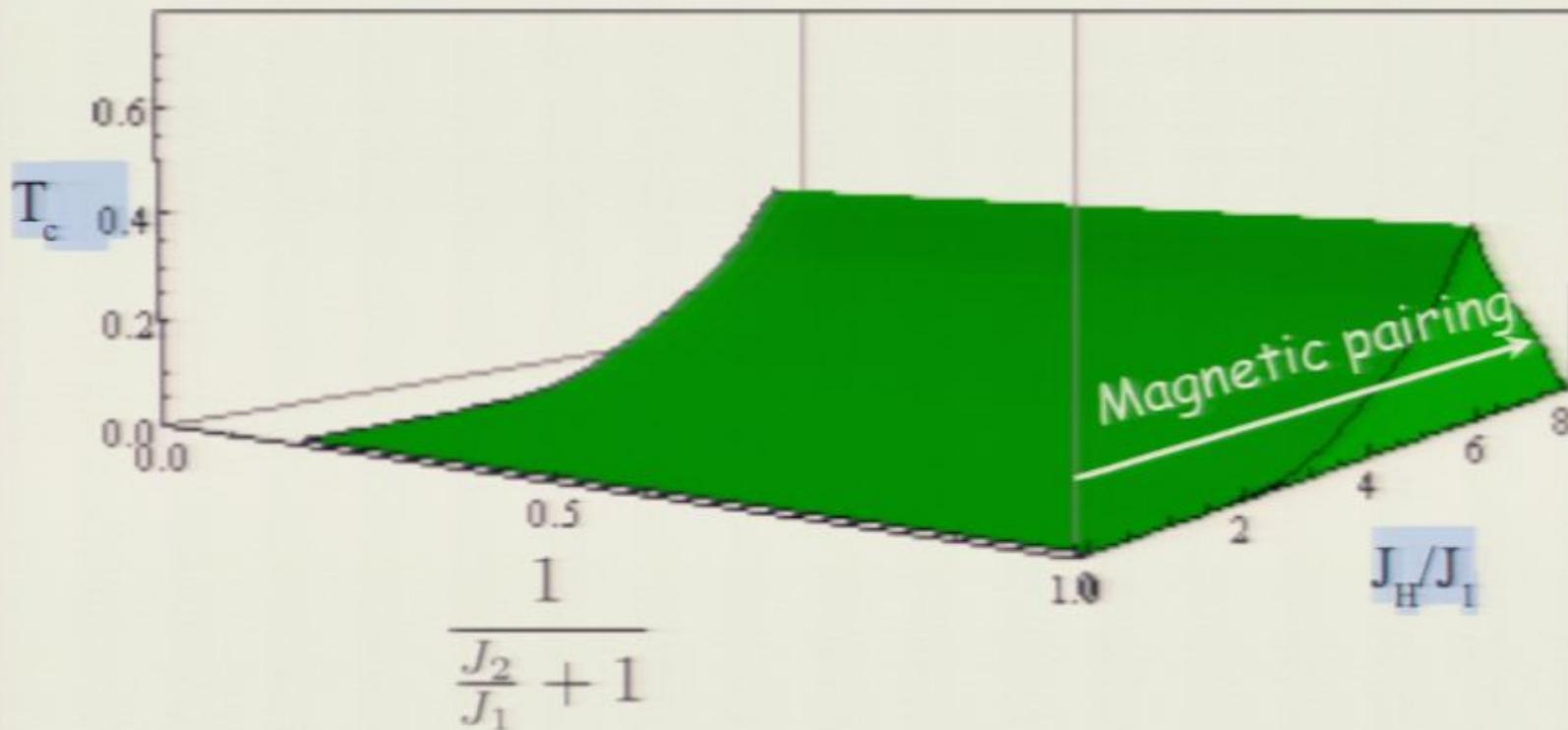
Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$

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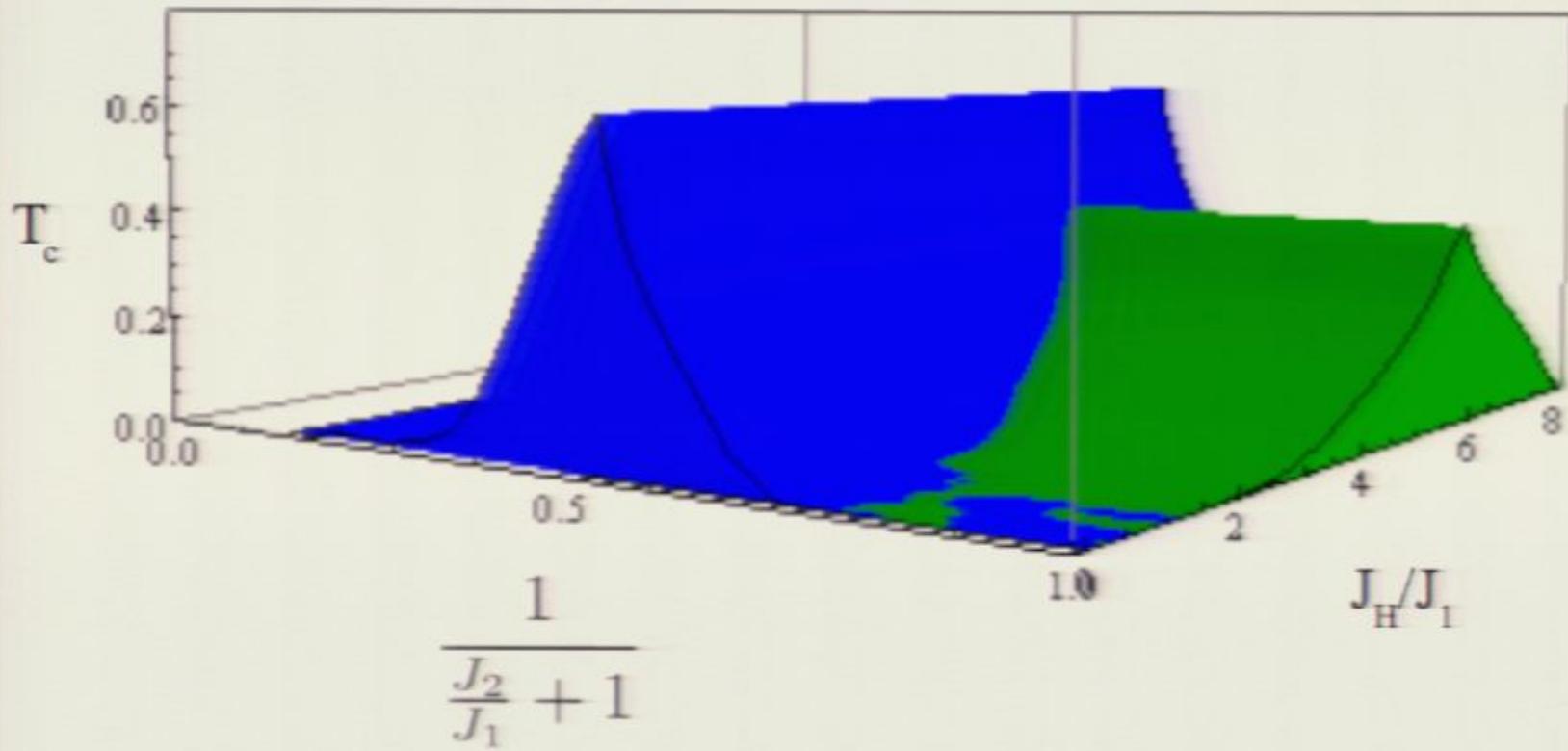


Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$

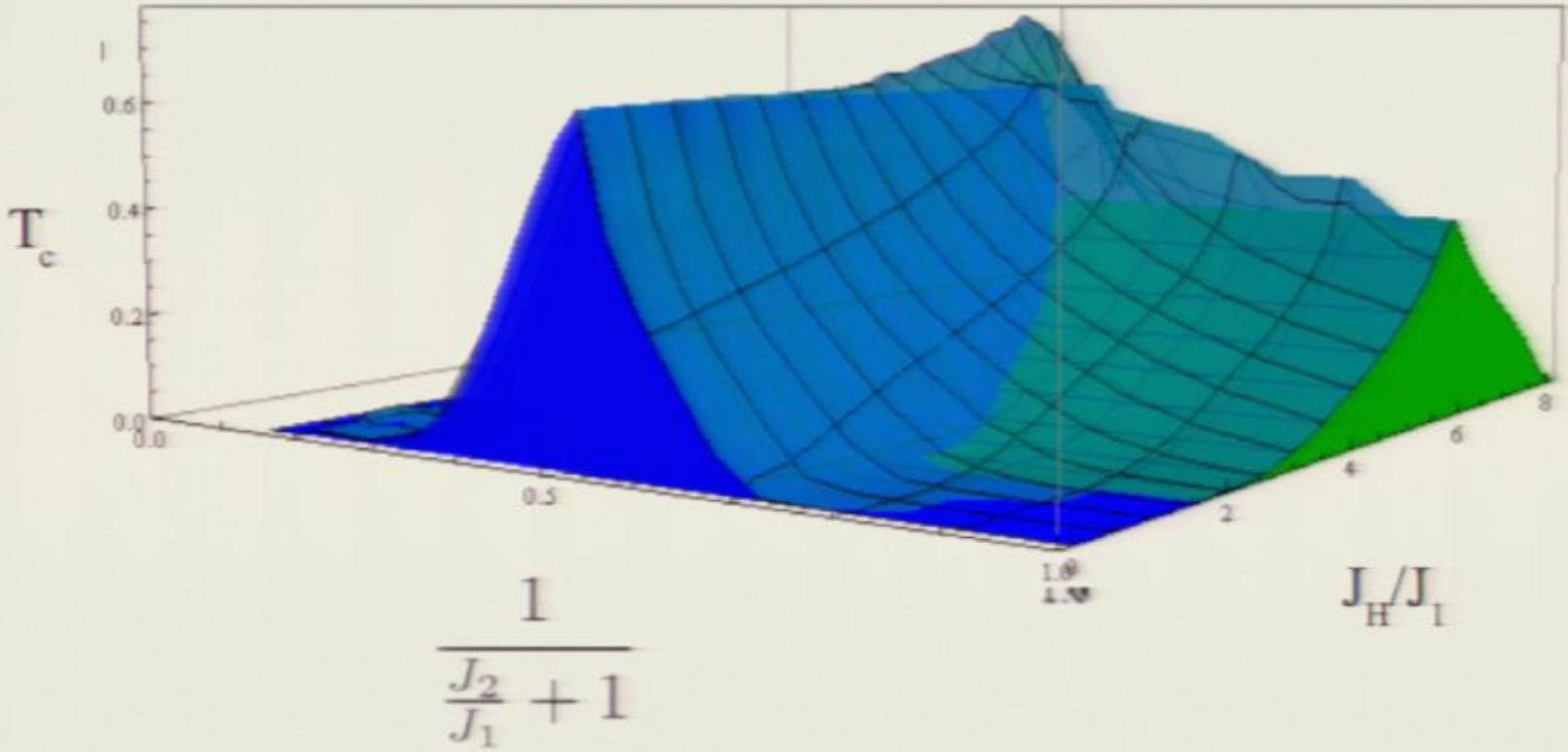
- RVB superconductivity



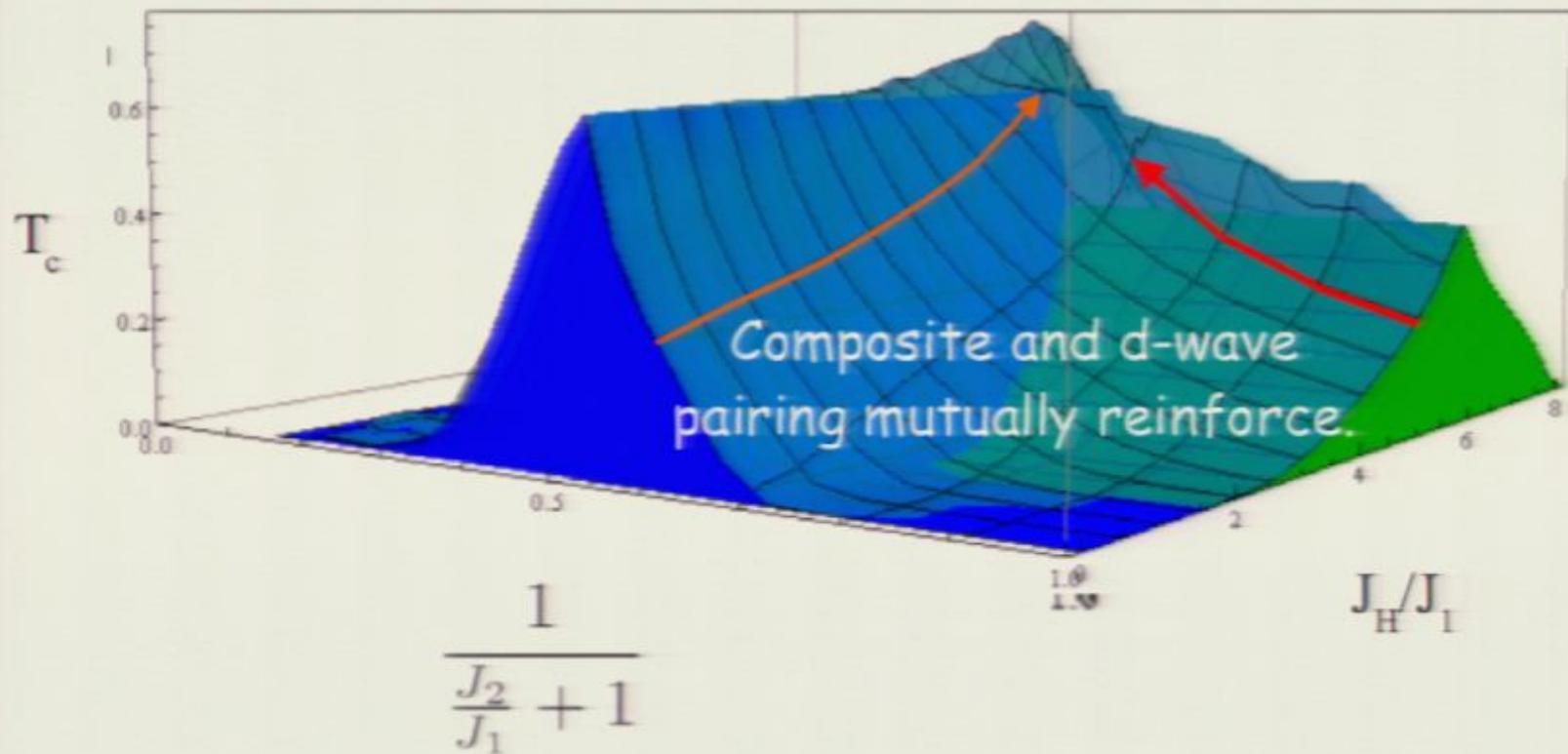
Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$



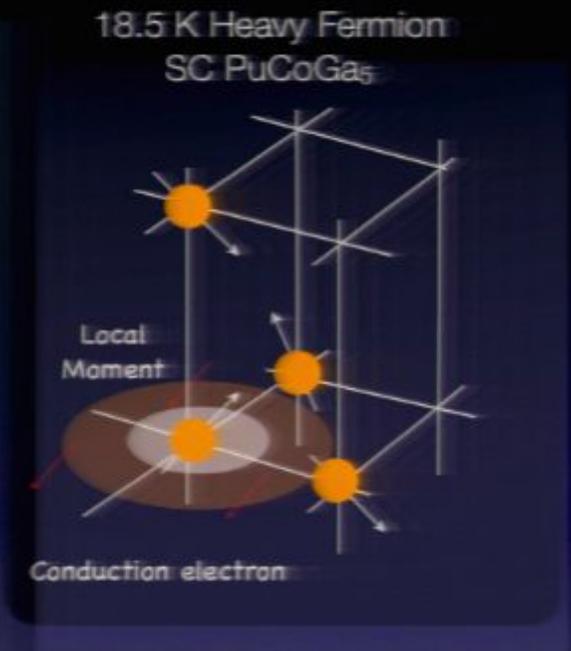
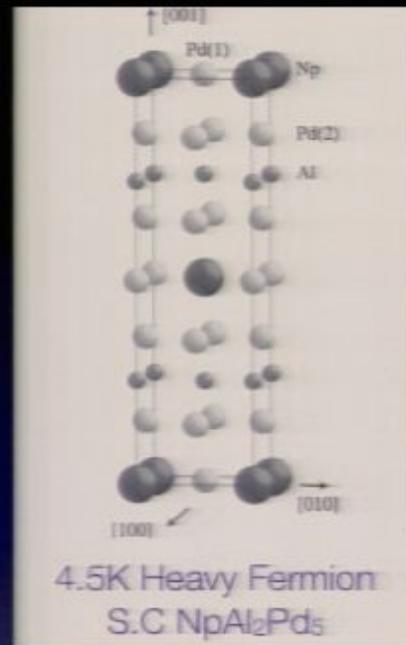
Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$



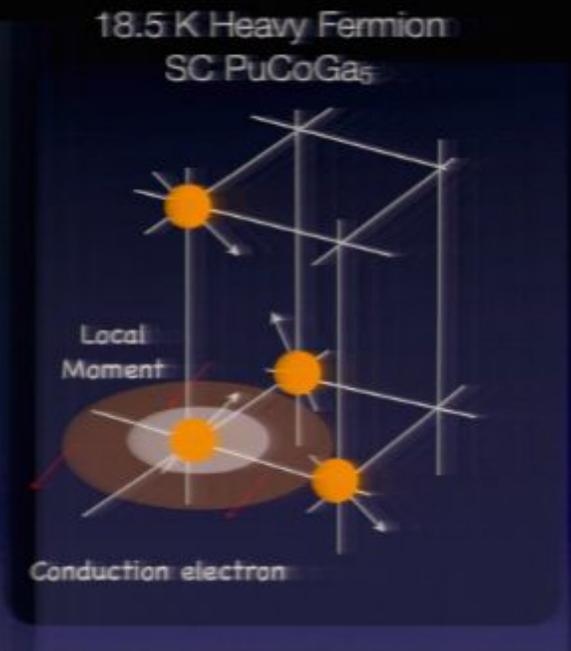
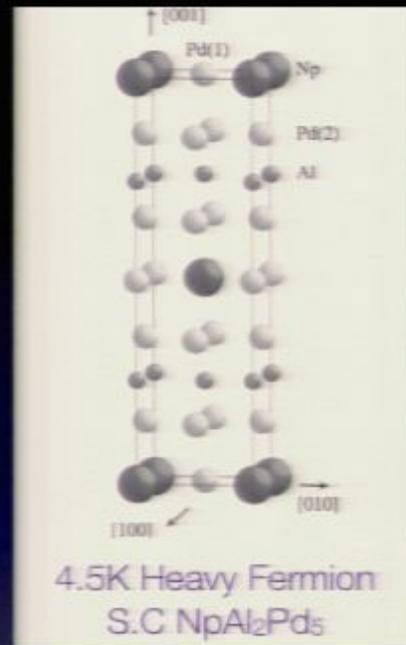
Ongoing challenge to unify magnetically mediated pairing and composite pairing:  $\text{CeCoIn}_5$



# Conclusions

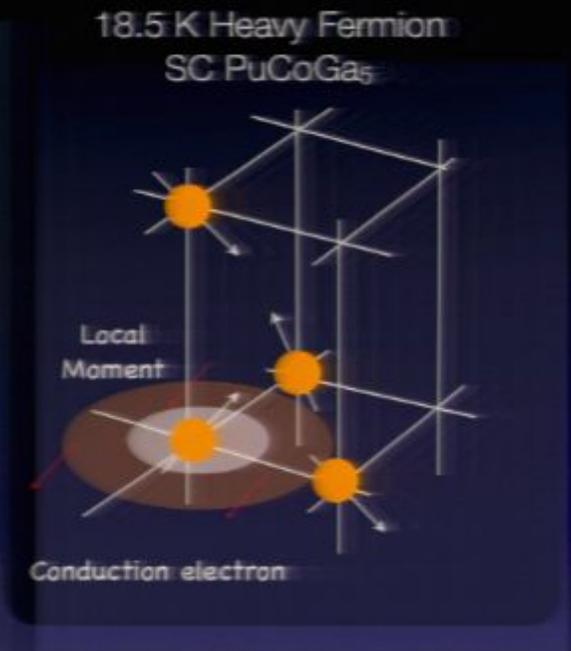
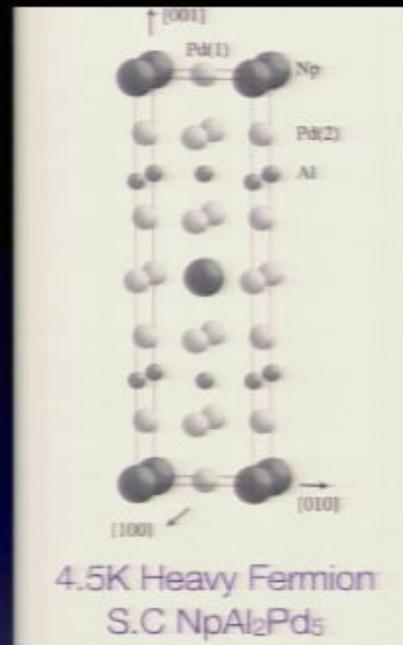


# Conclusions



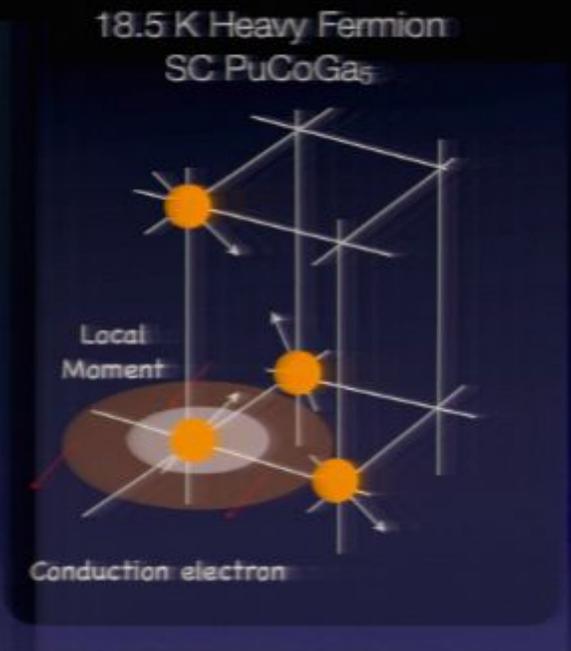
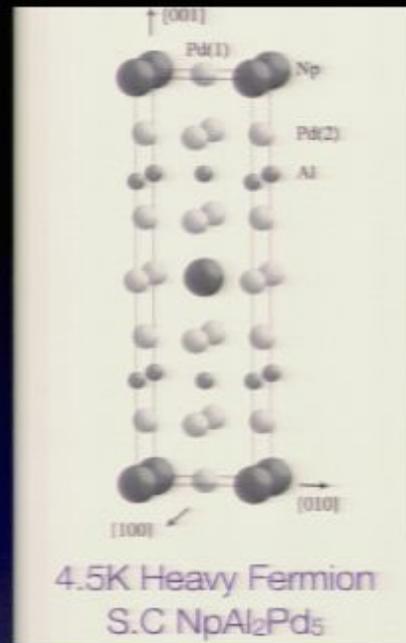
# Conclusions

- Symplectic spins:  $1/N$  expansion for heavy fermion superconductivity



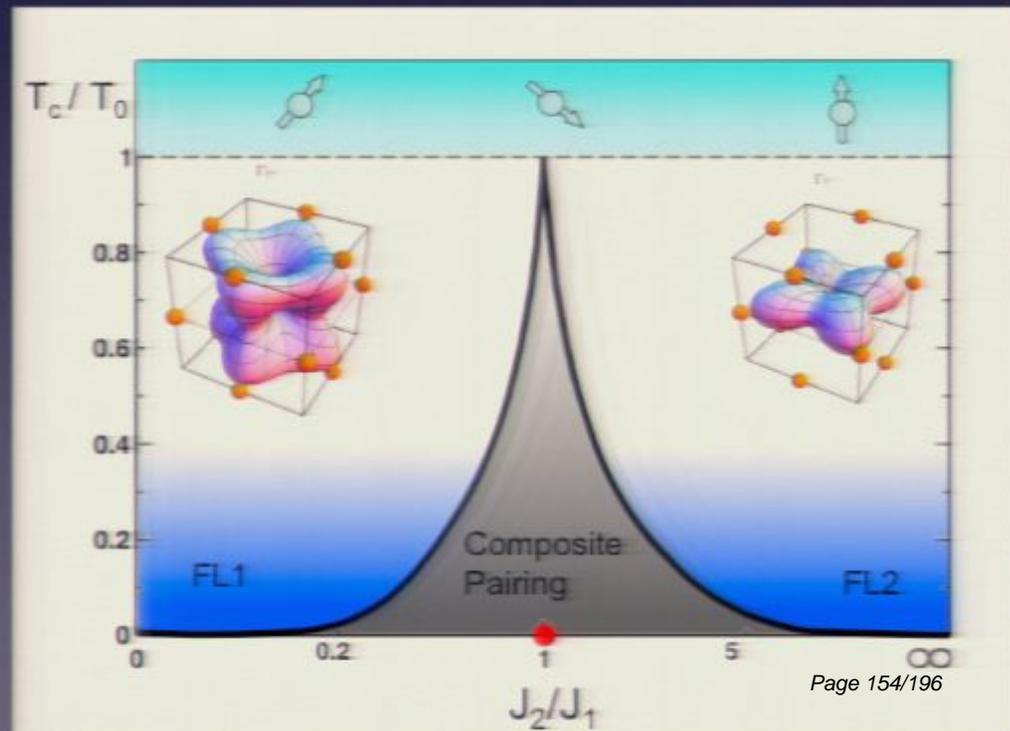
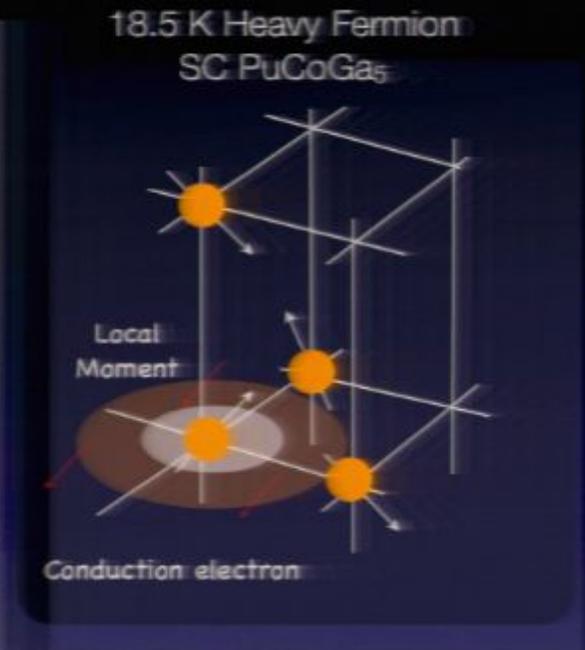
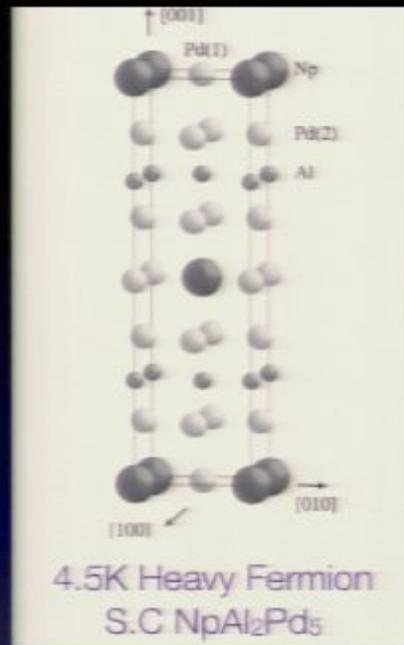
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- Predicts: avoided criticality.



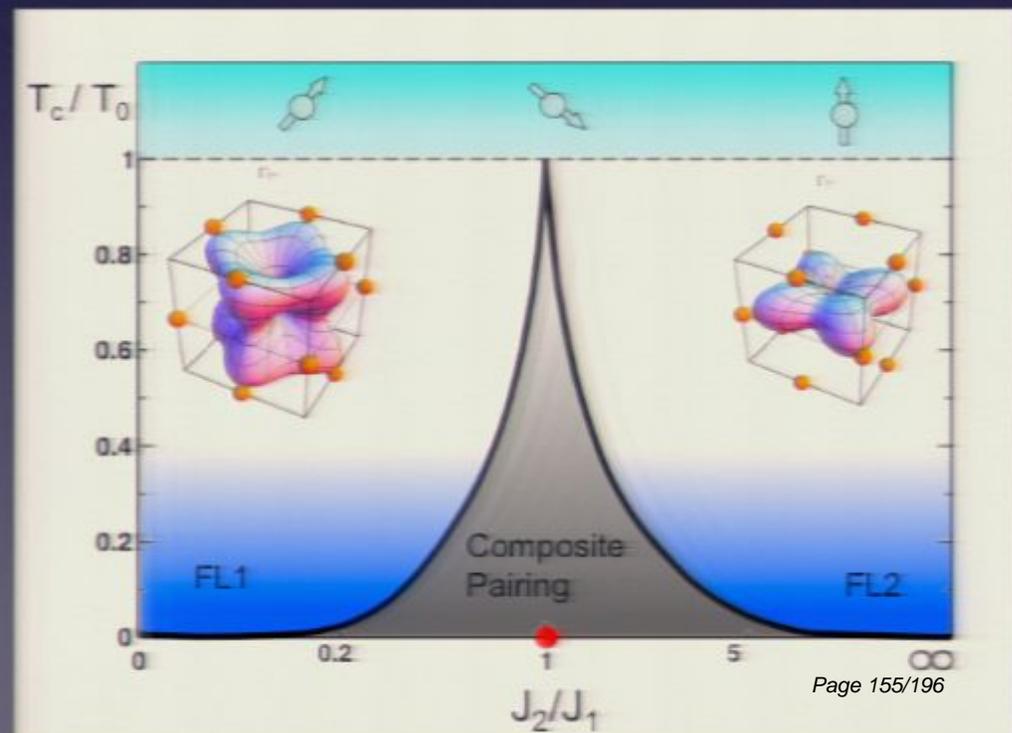
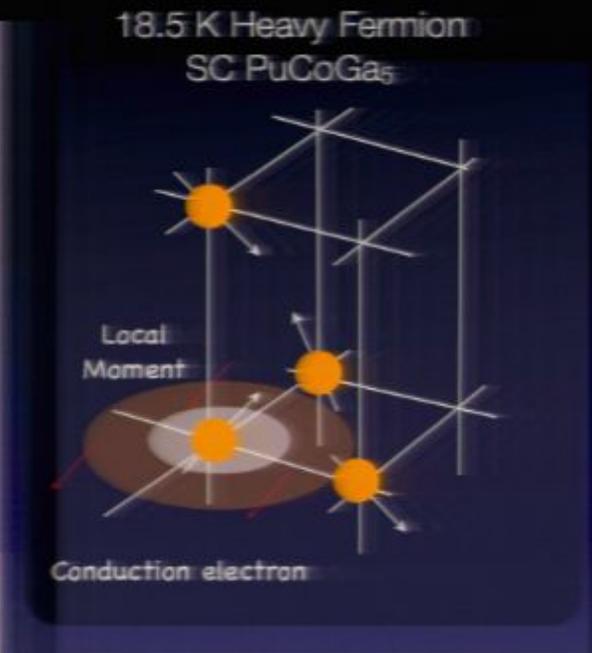
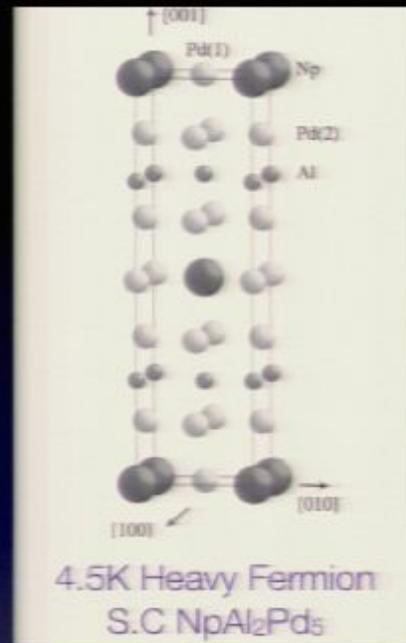
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# Conclusions

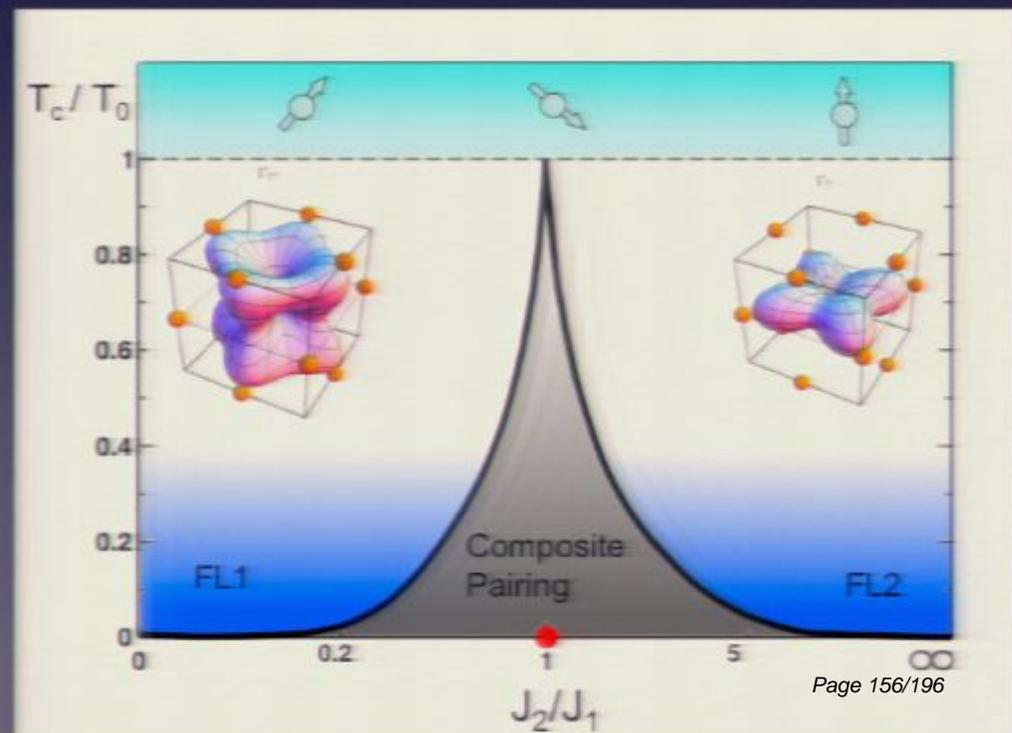
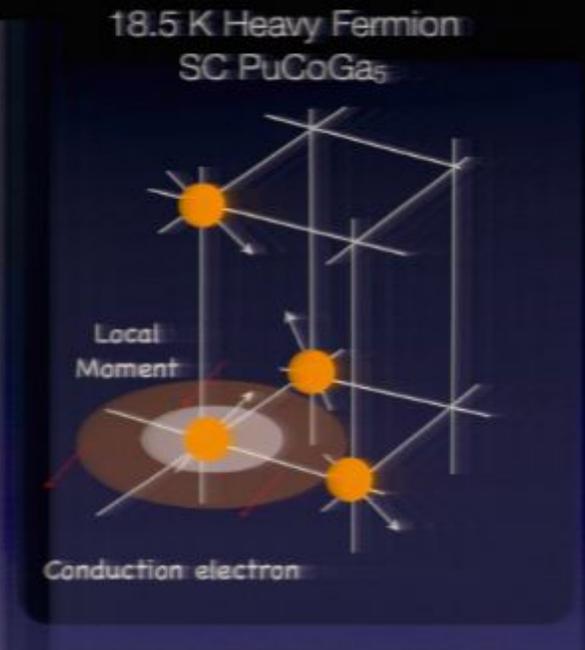
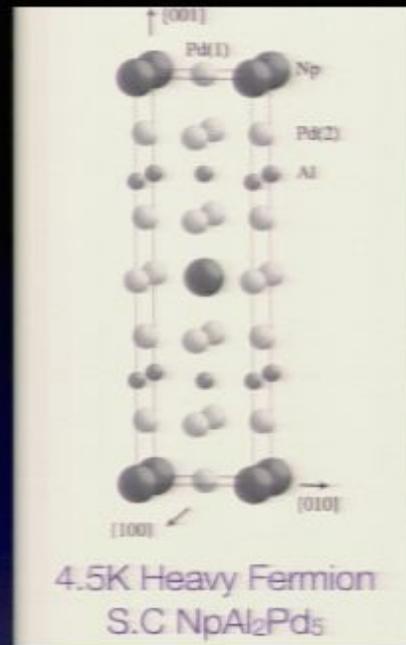
- Symplectic spins: 1/N expansion for heavy fermion superconductivity
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# Conclusions



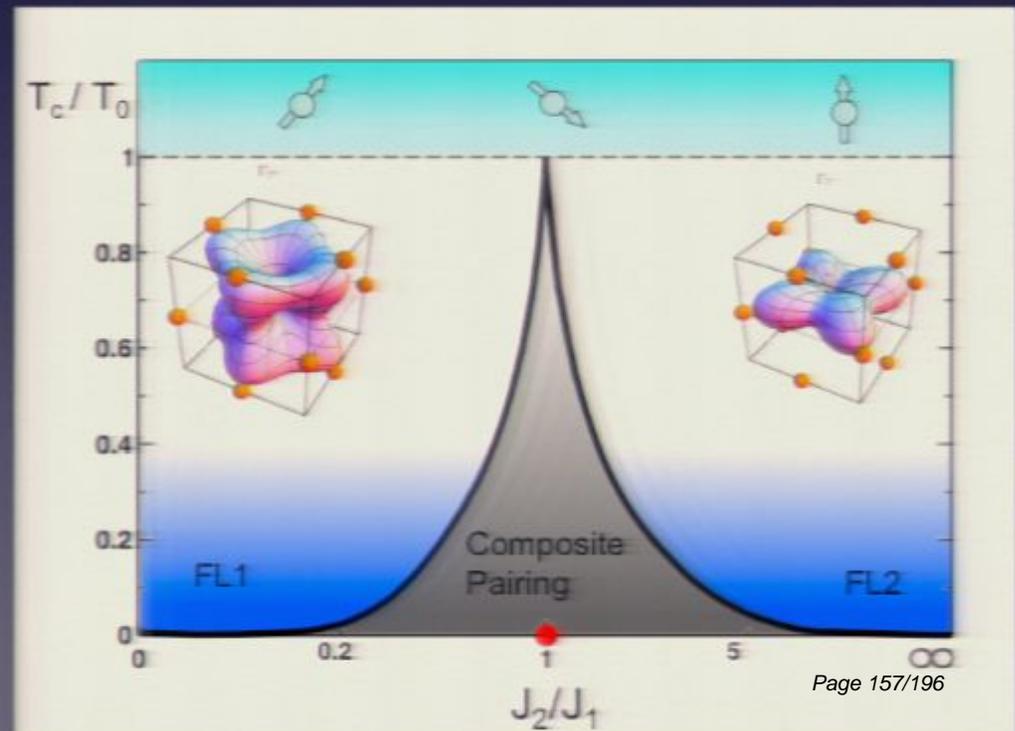
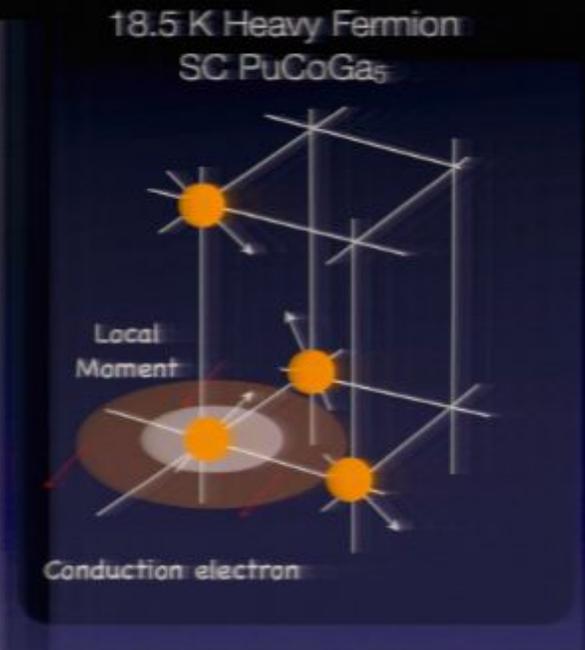
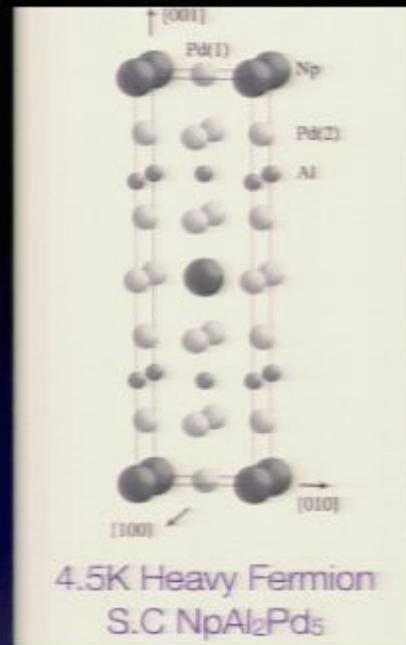
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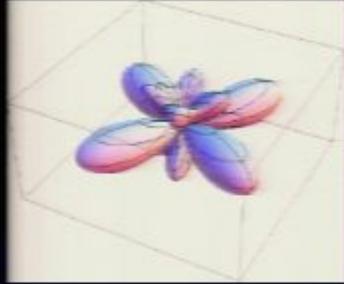
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- enhancement of  $1/T_1$  above  $T_c$ .



# Thank You!



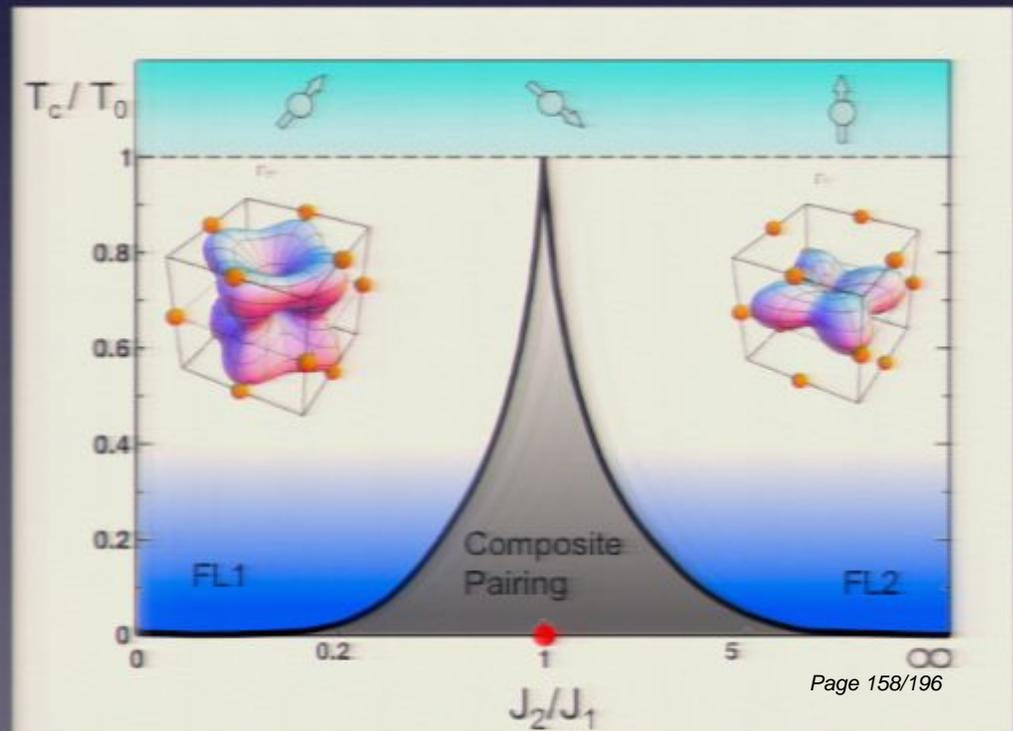
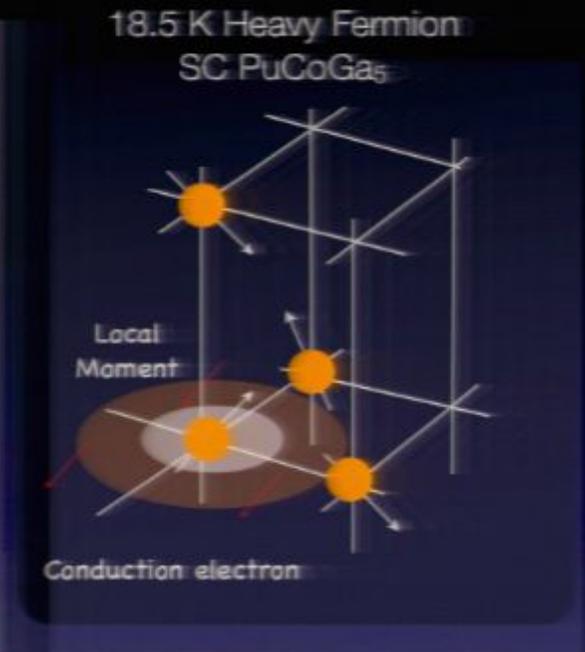
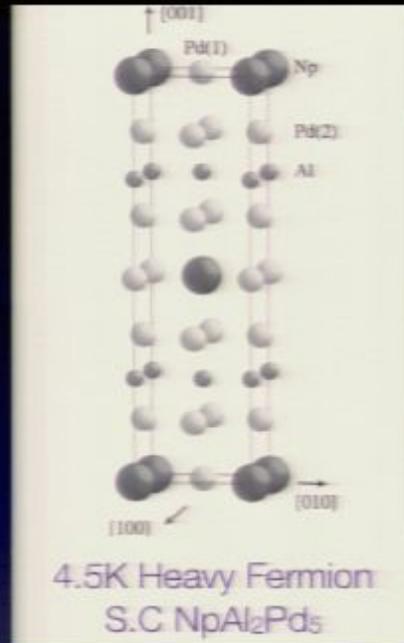
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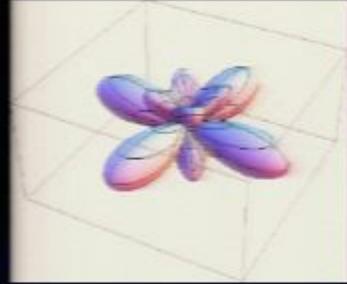
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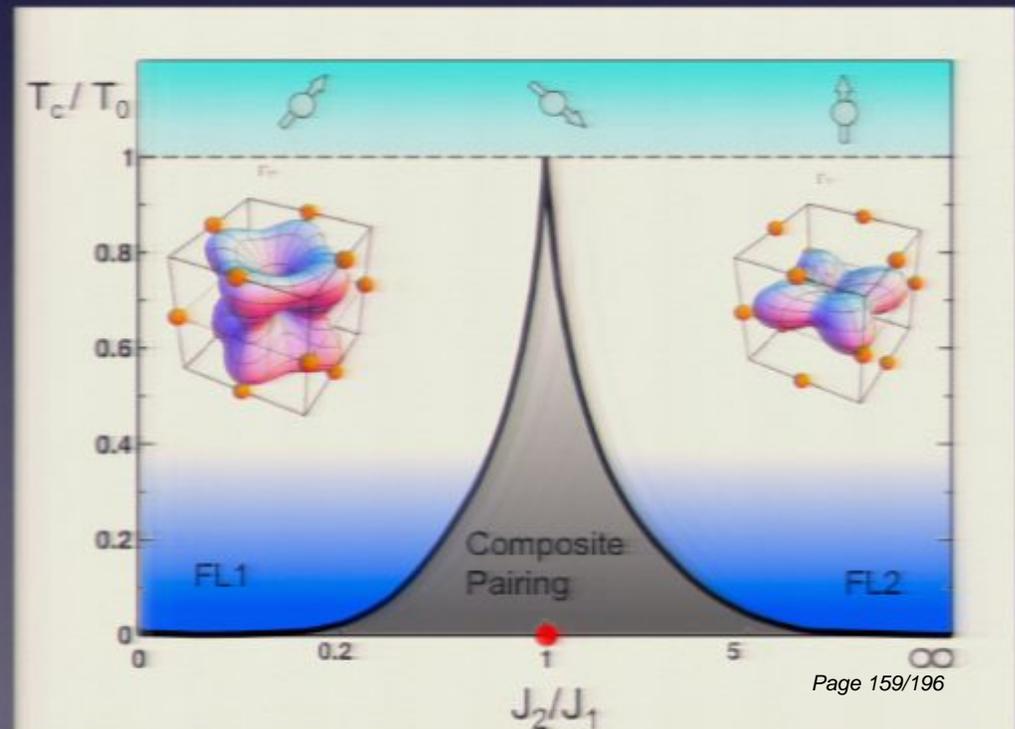
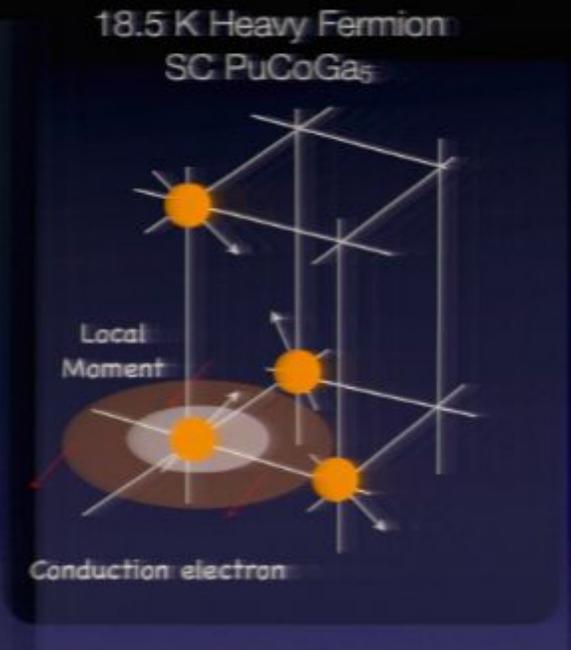
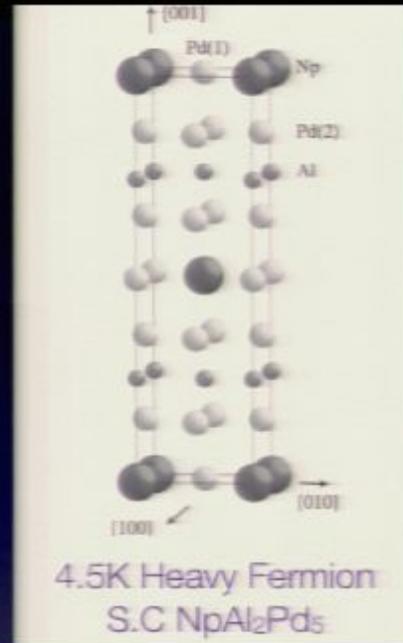
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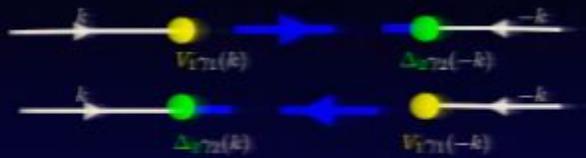
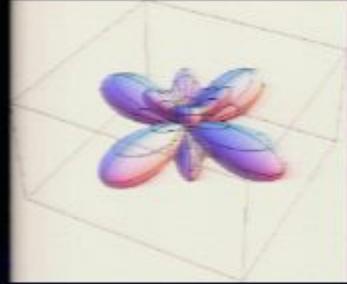
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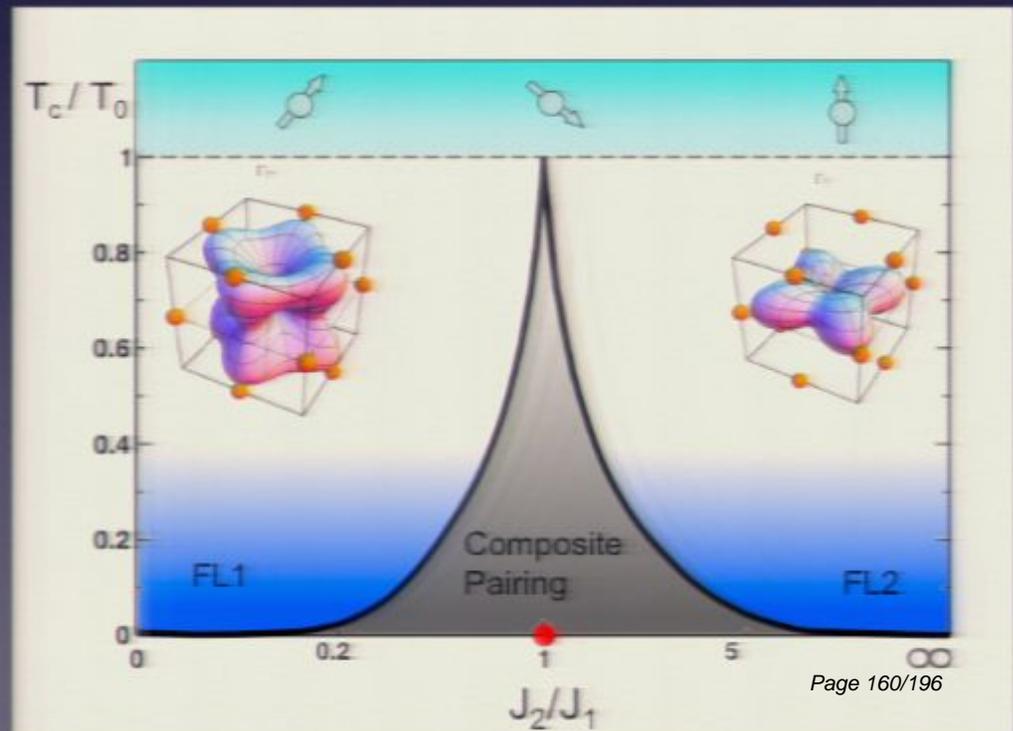
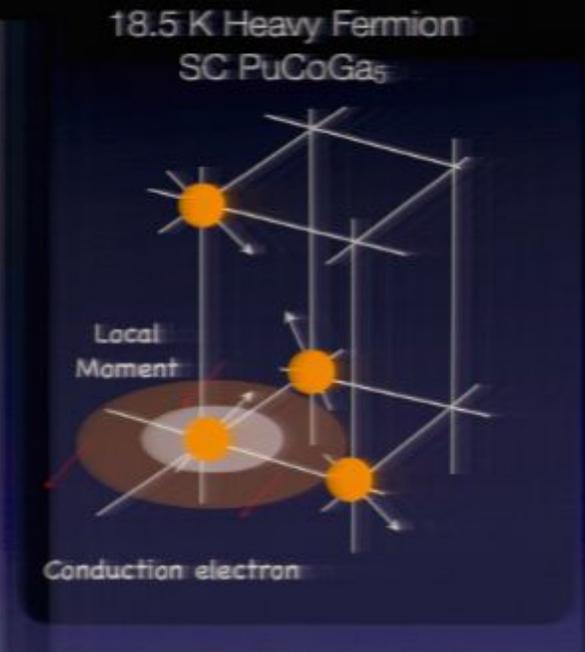
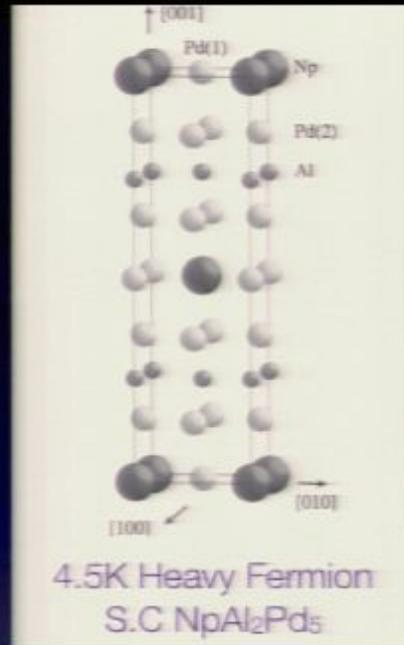
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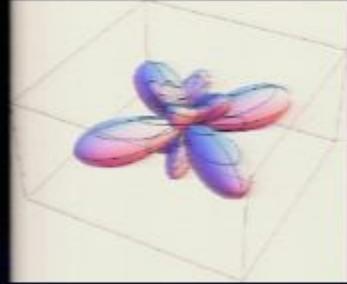
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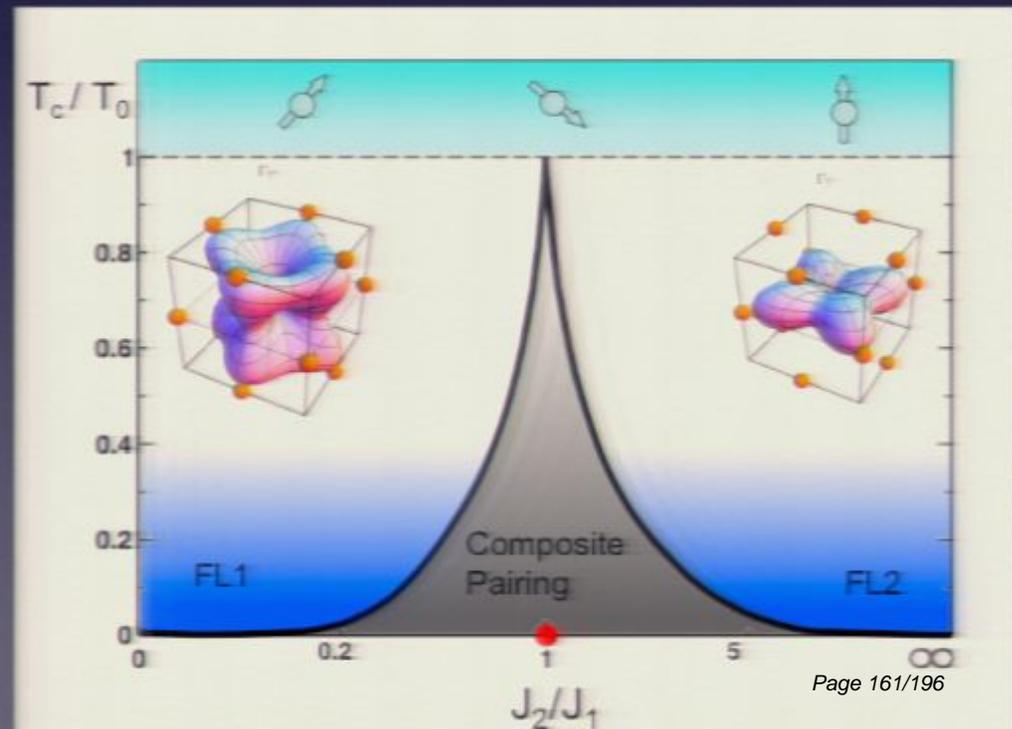
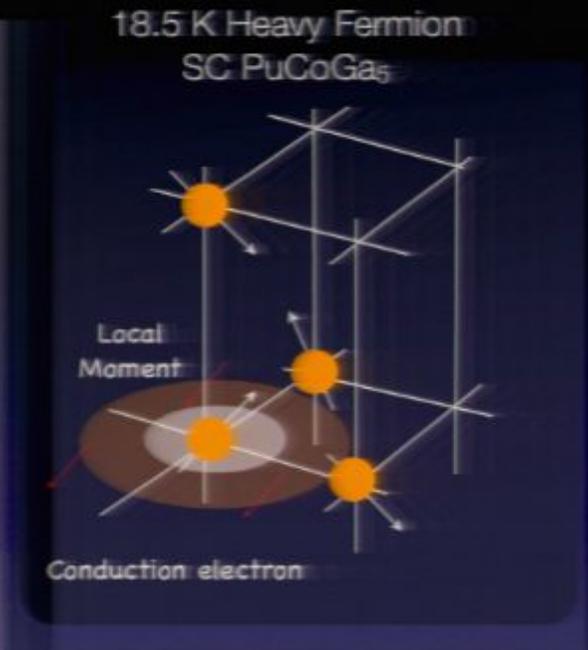
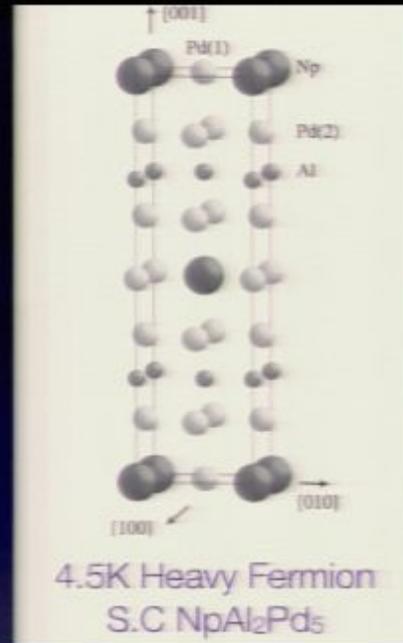
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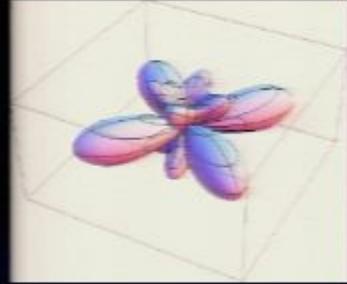
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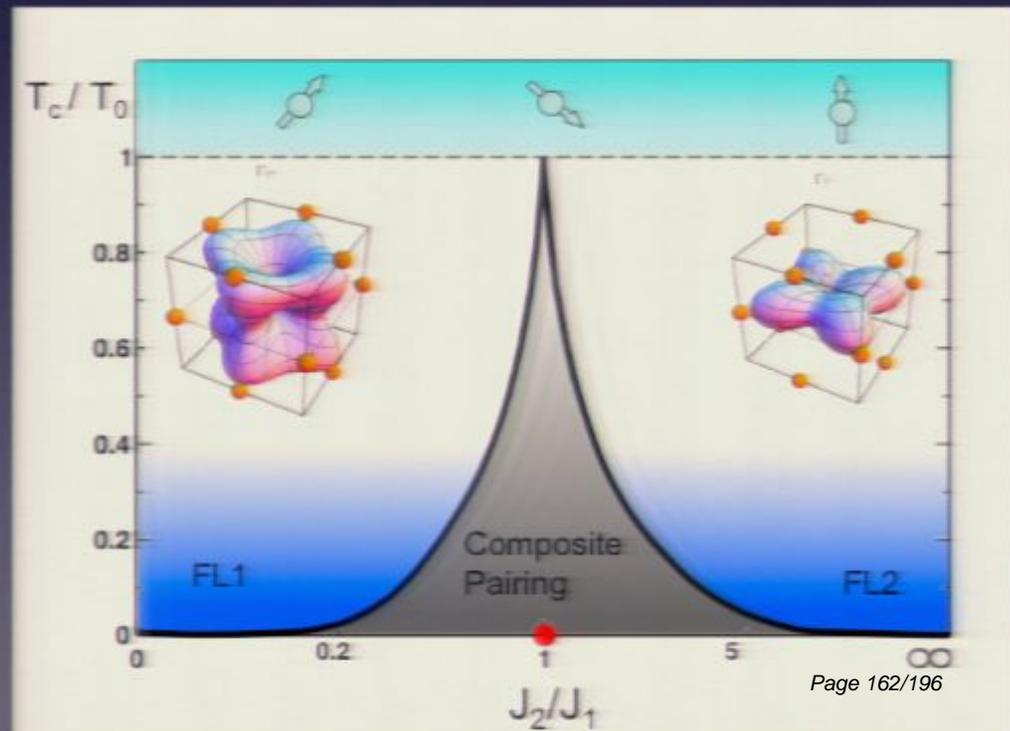
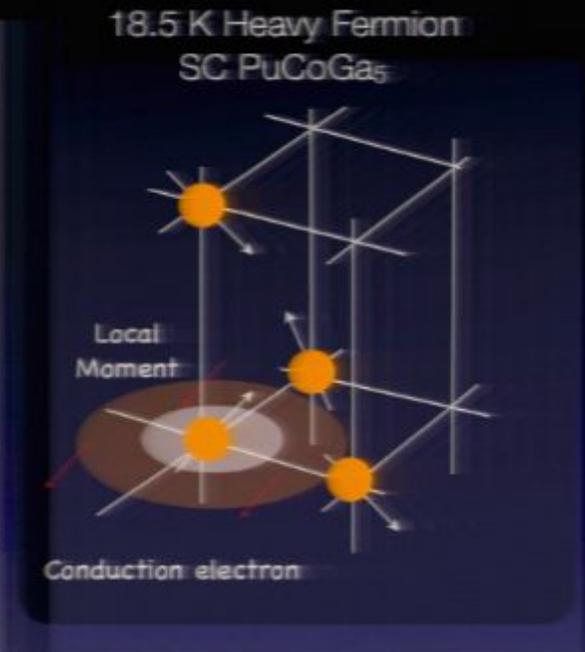
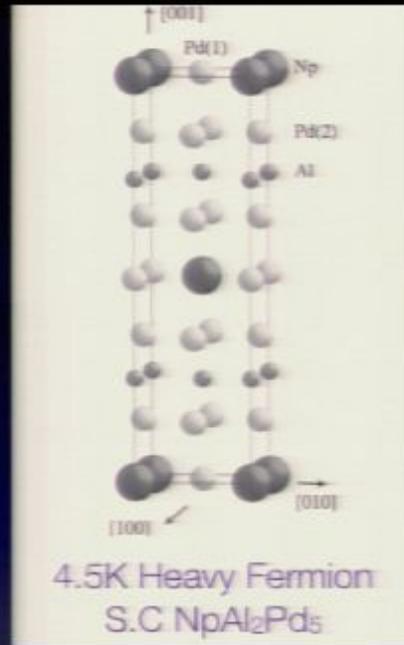
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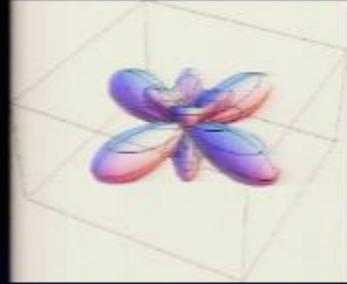
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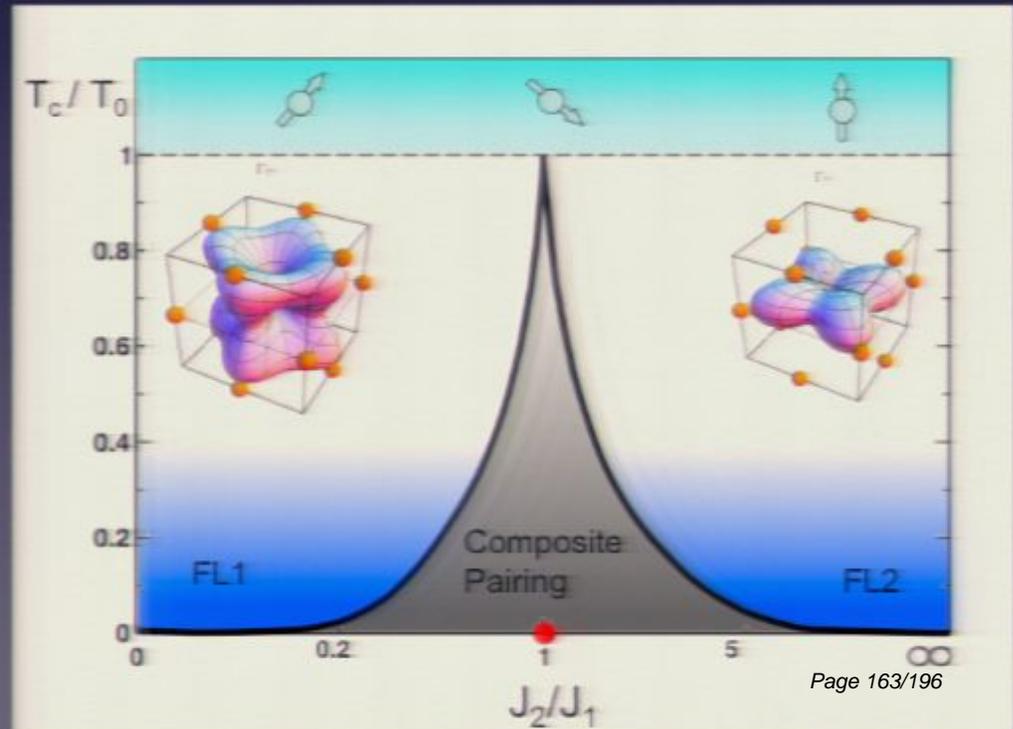
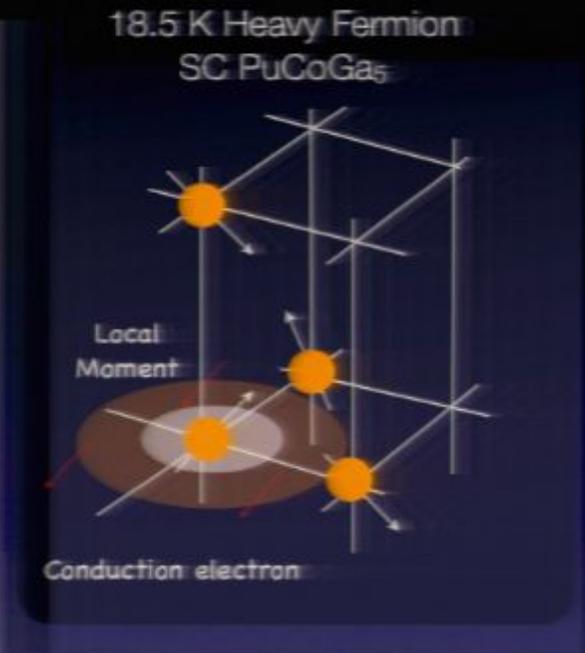
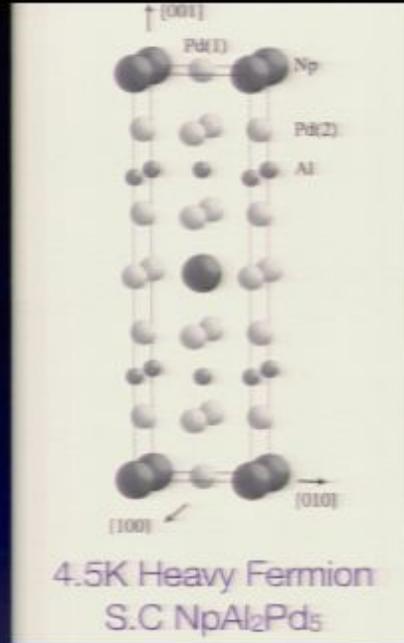
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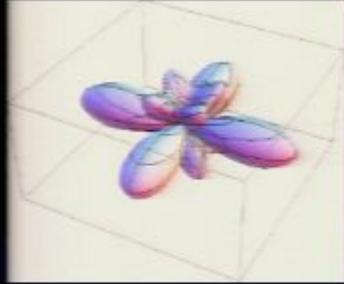
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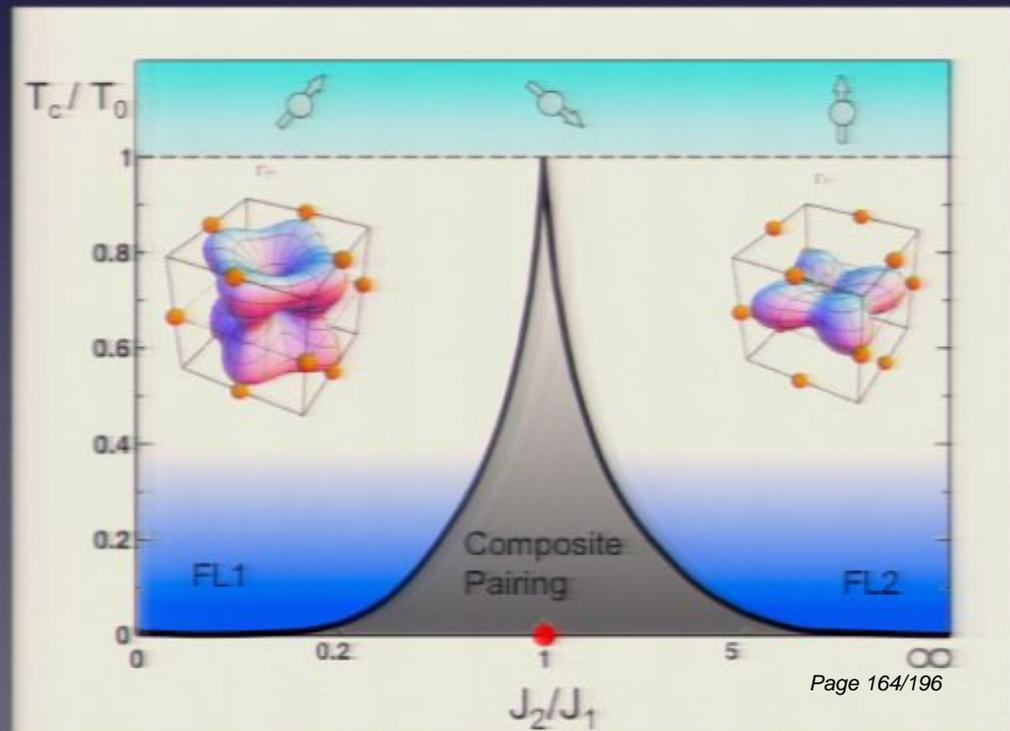
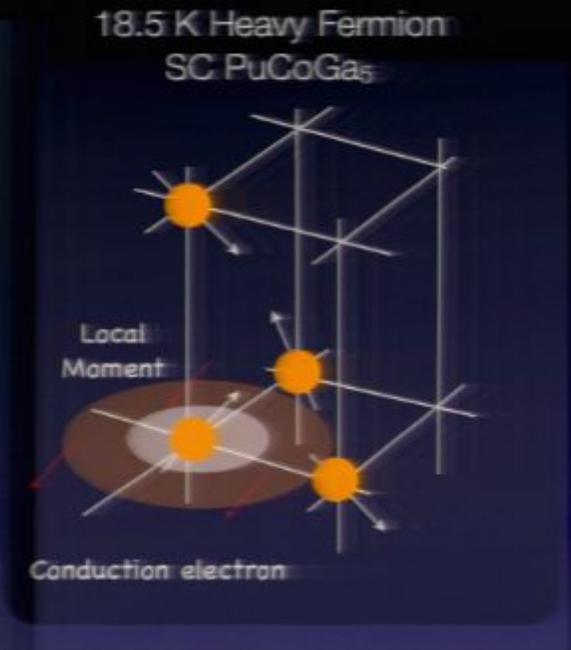
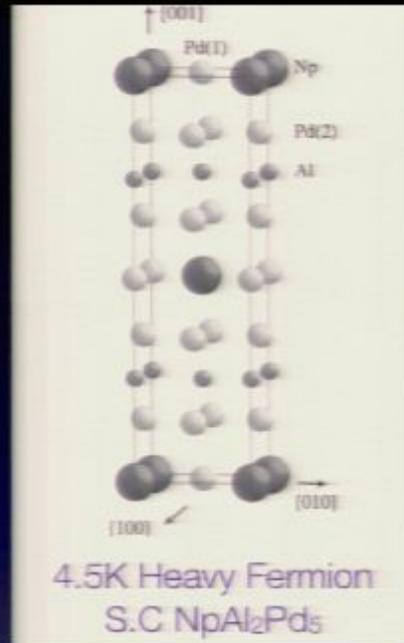
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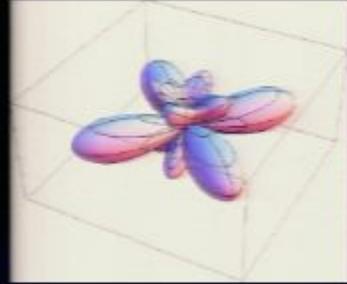
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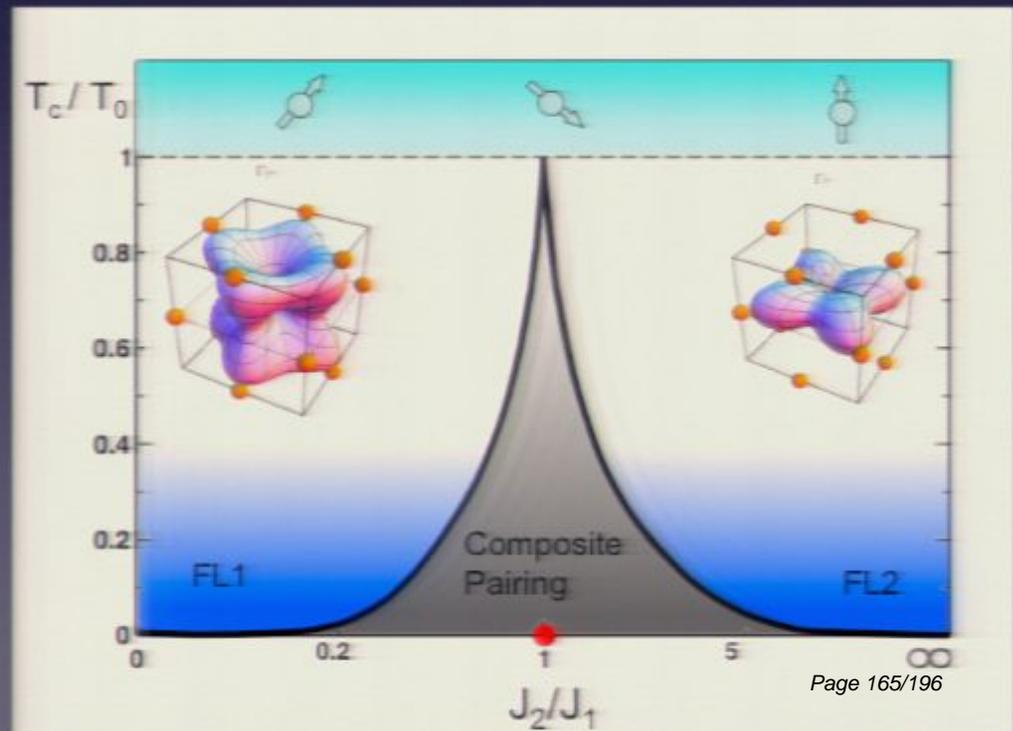
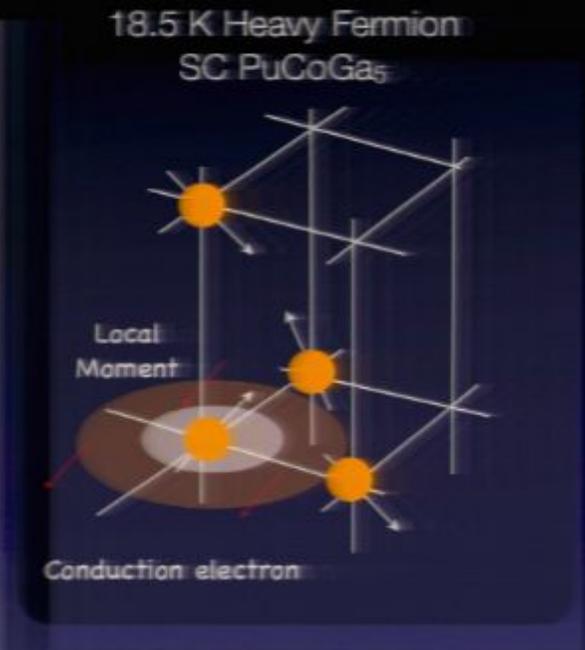
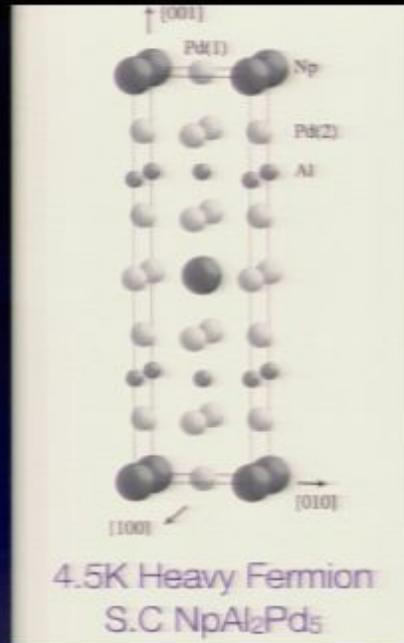
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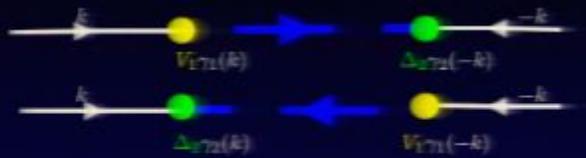
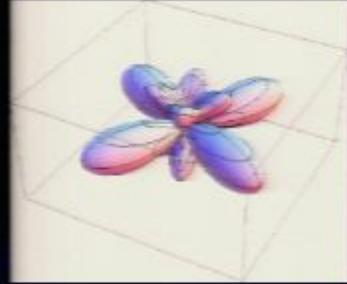
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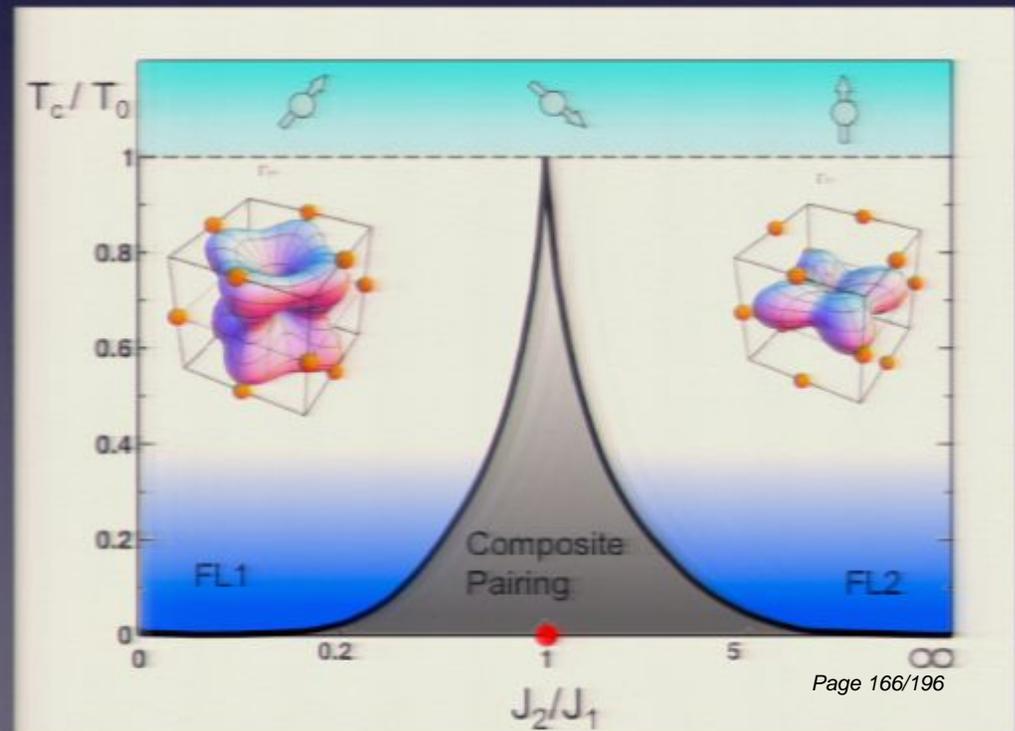
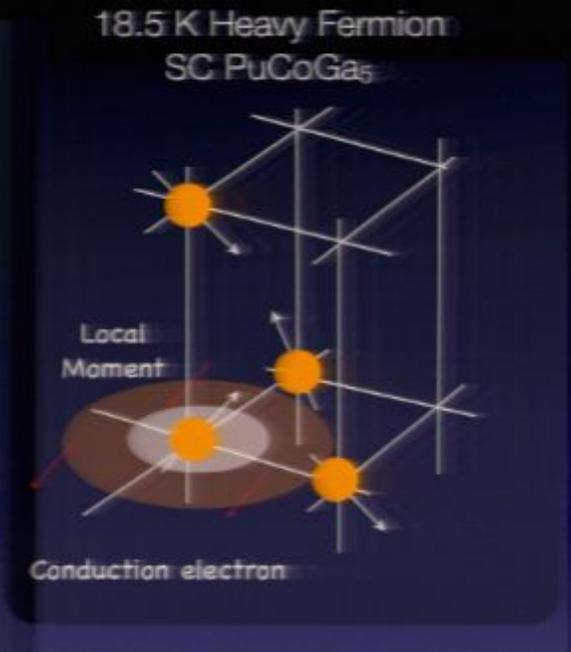
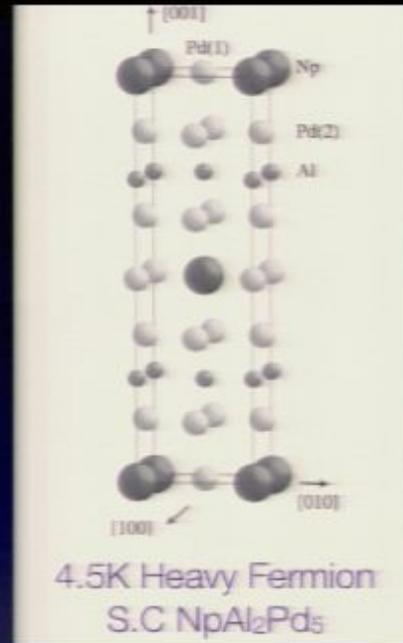
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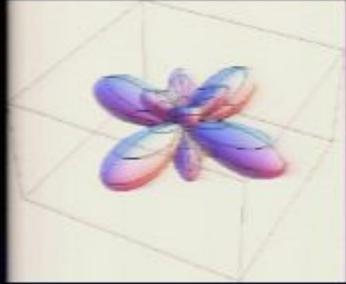
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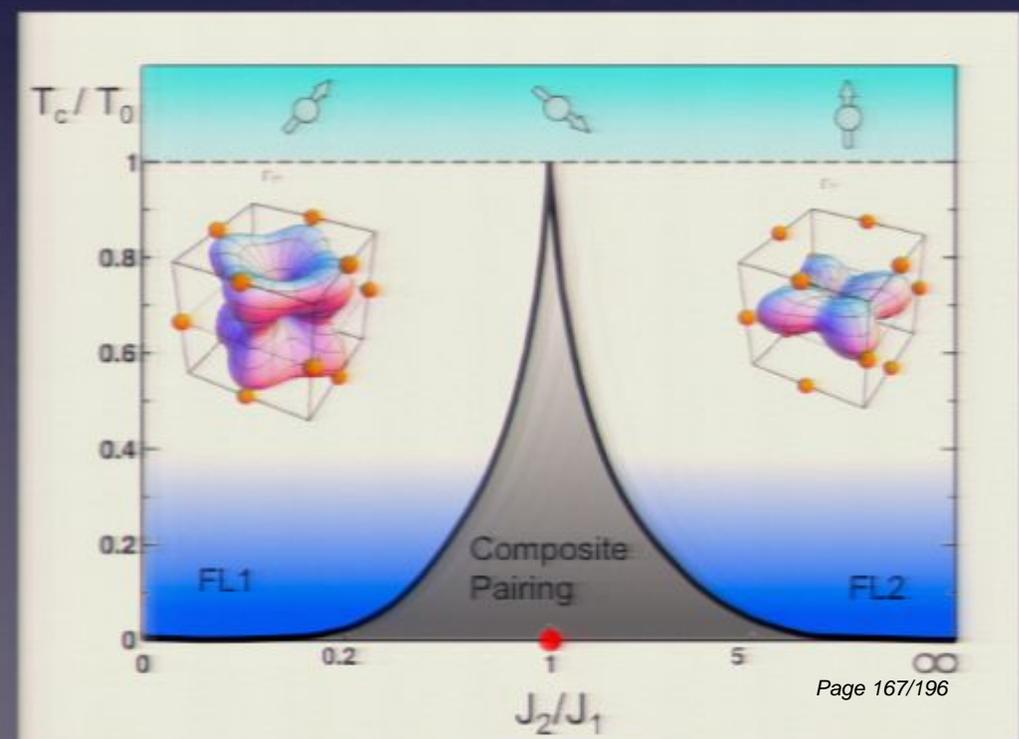
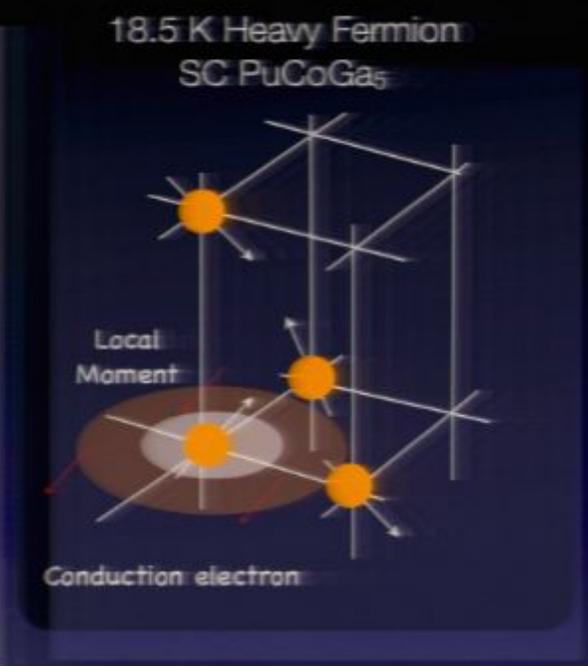
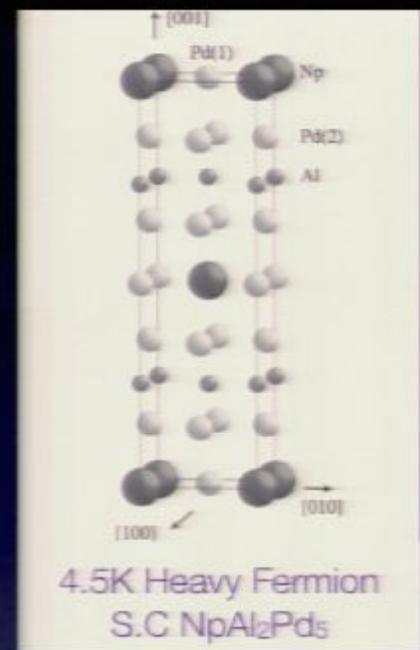
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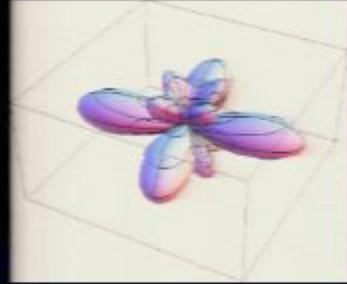
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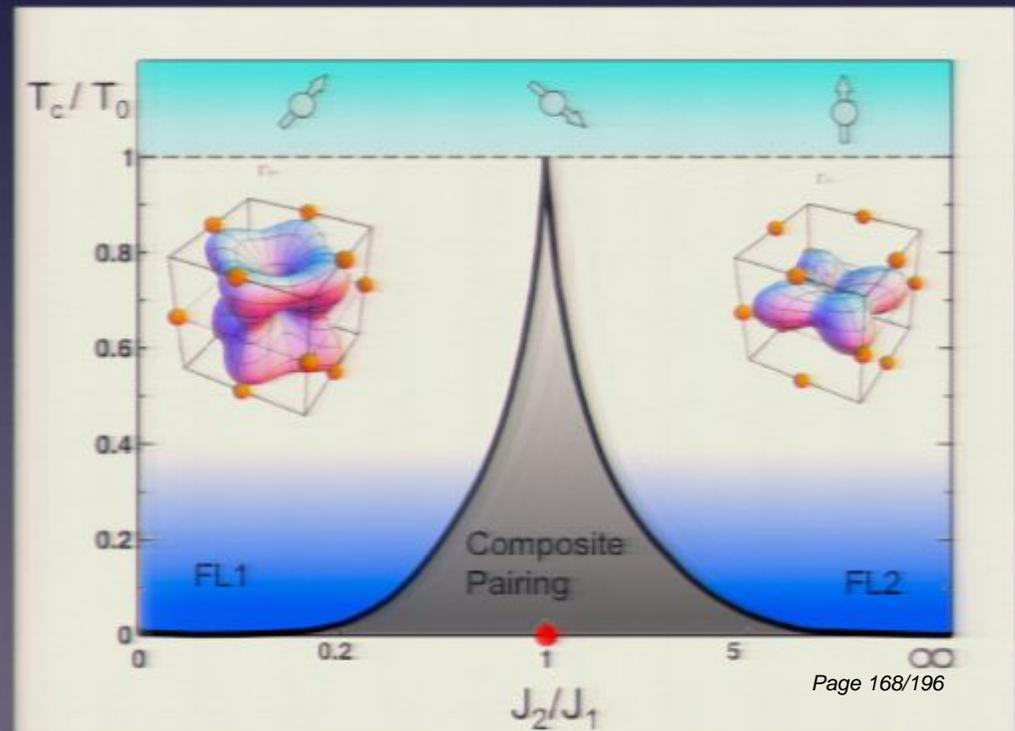
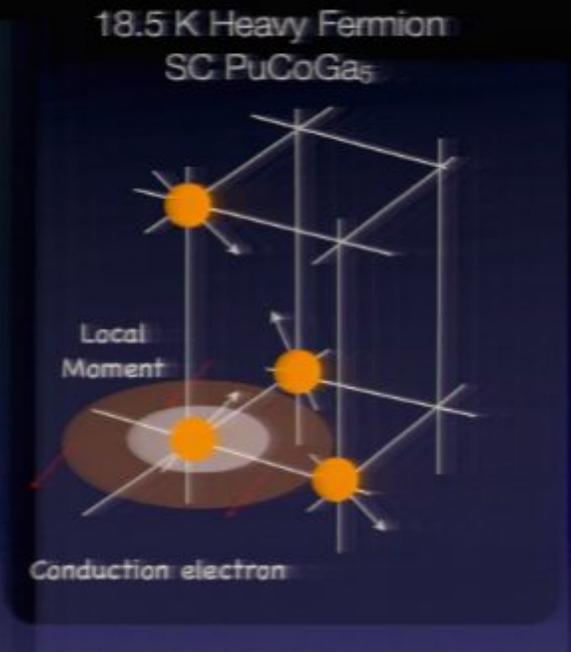
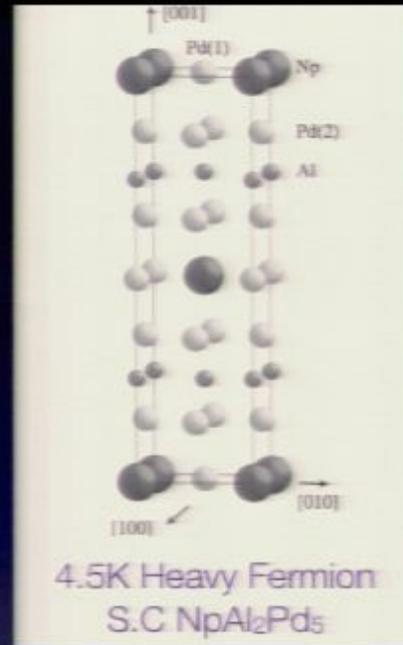
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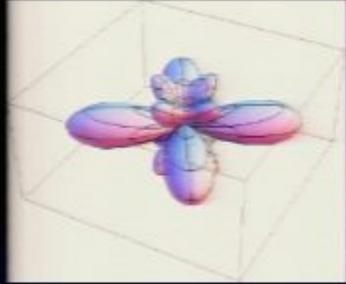
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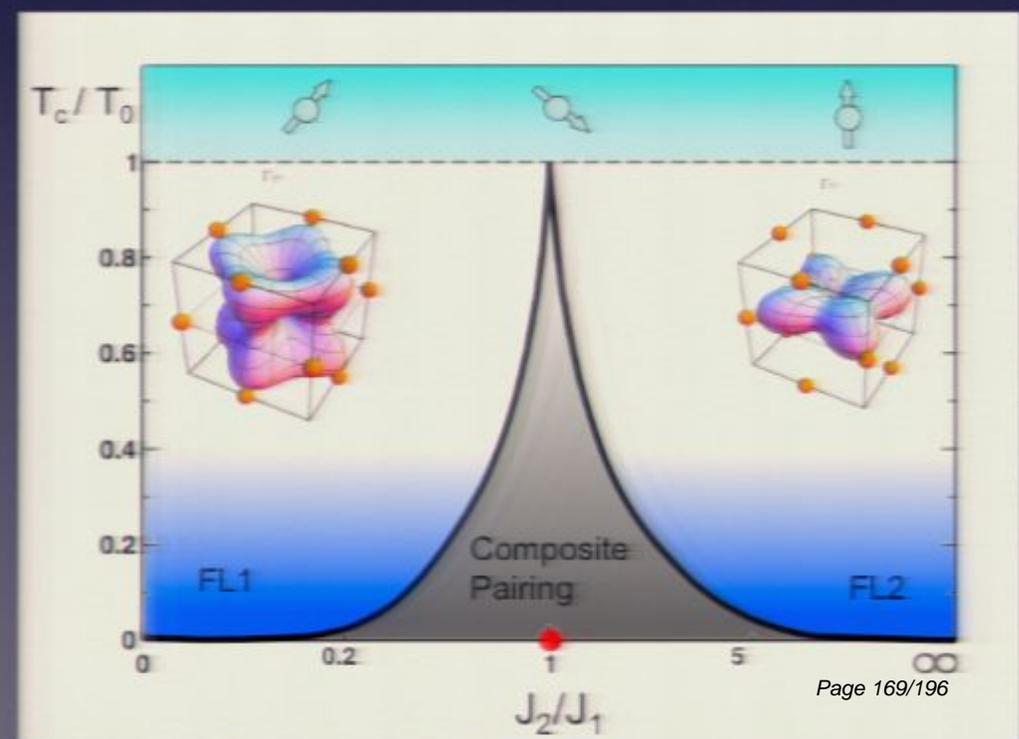
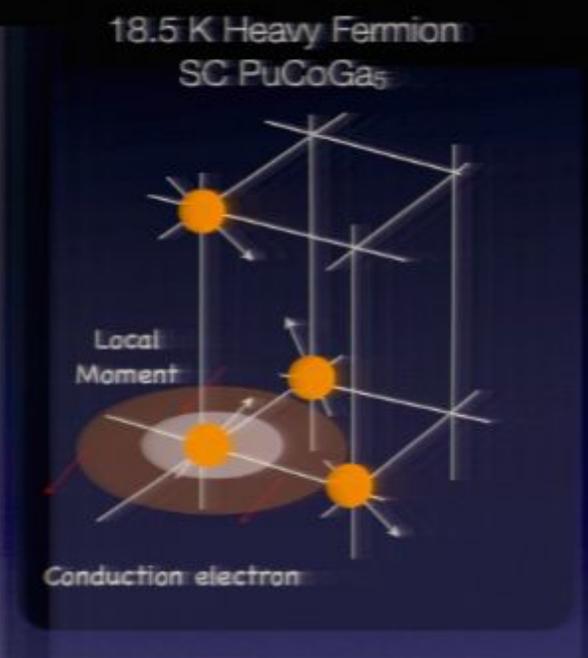
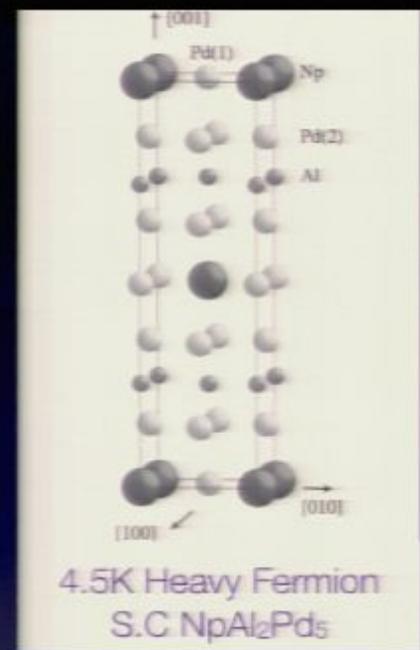
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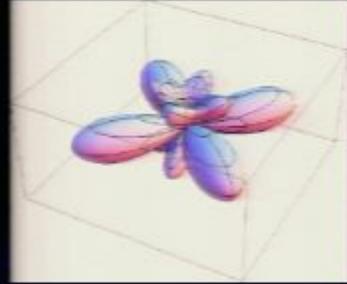
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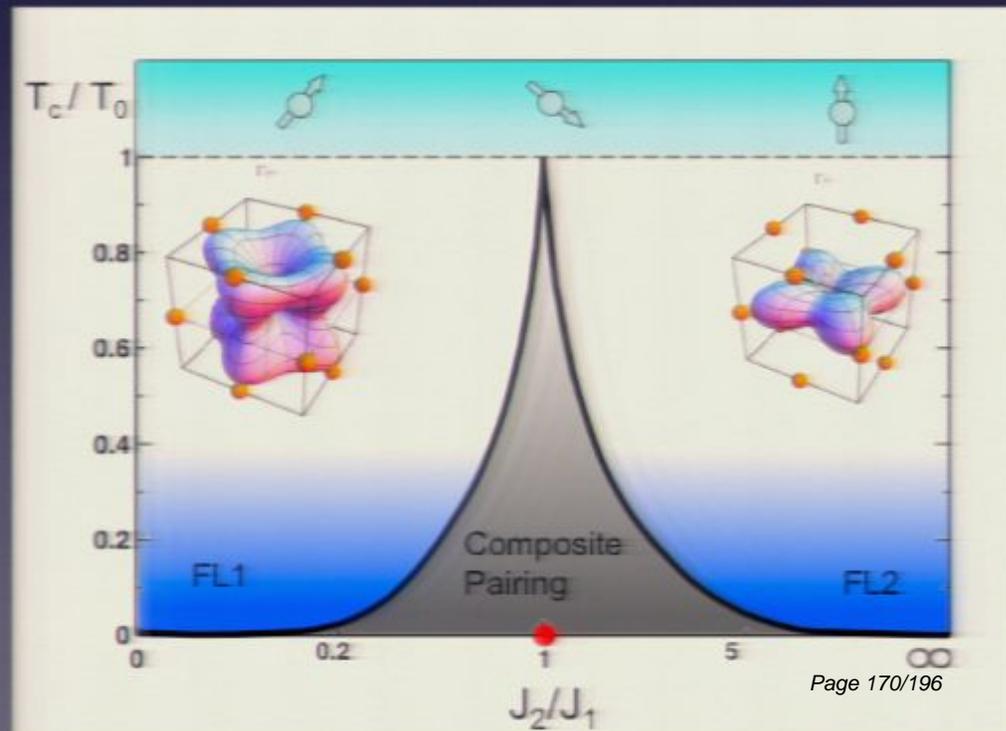
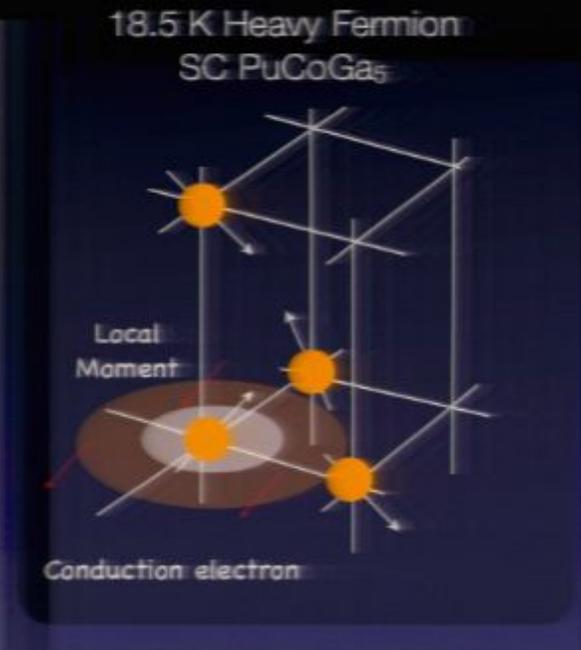
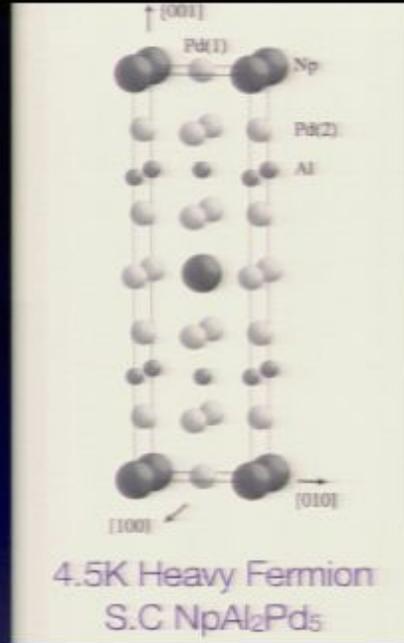
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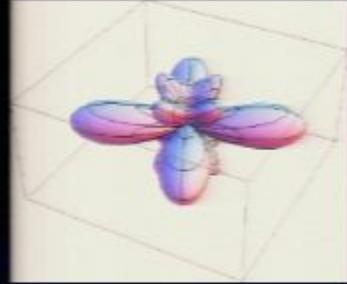
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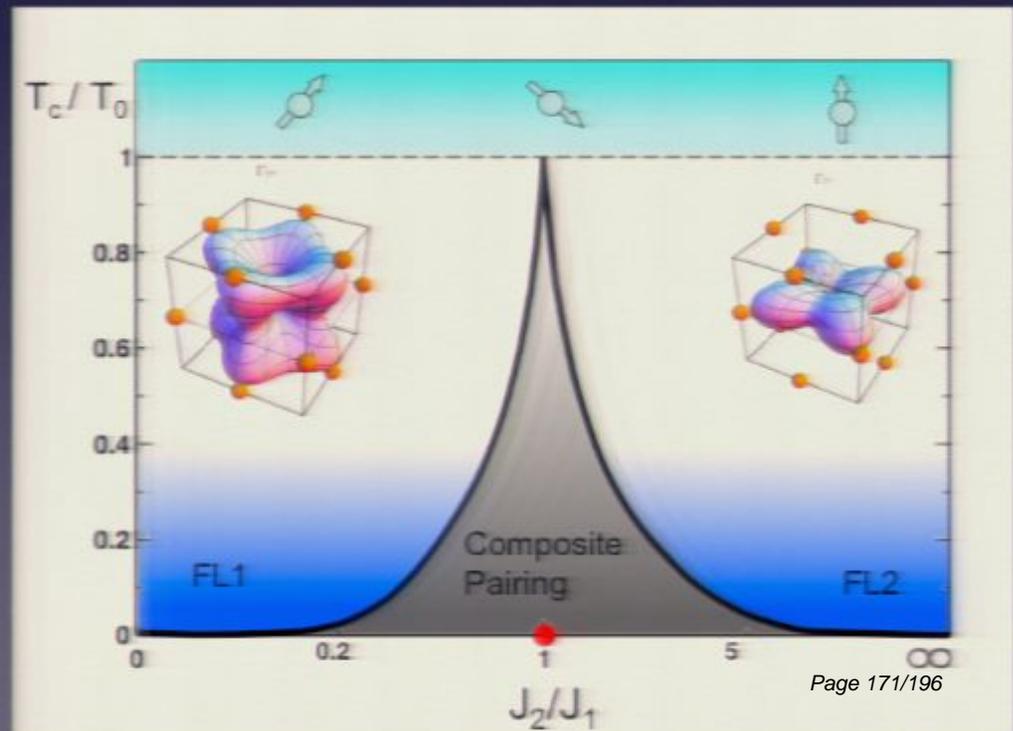
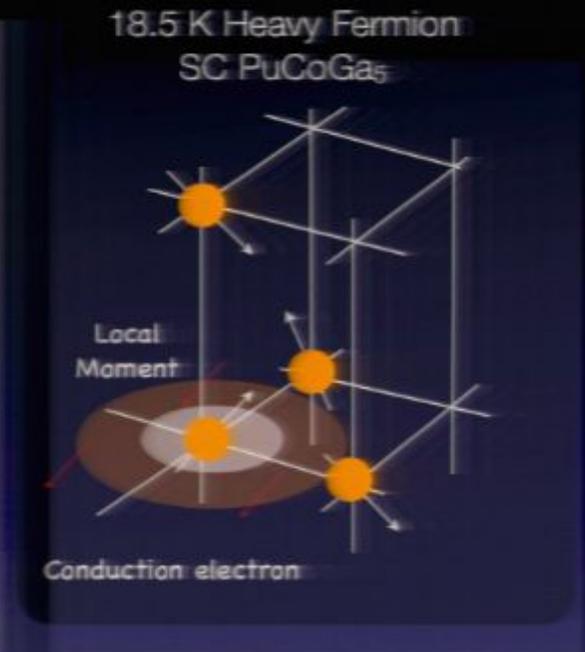
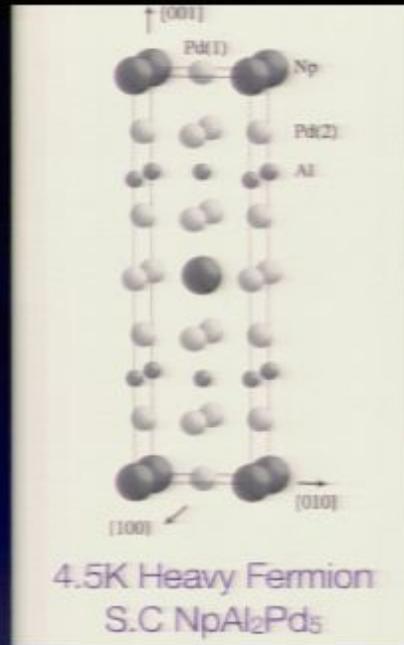
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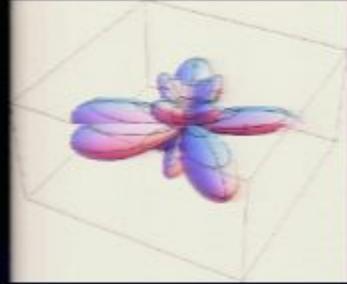
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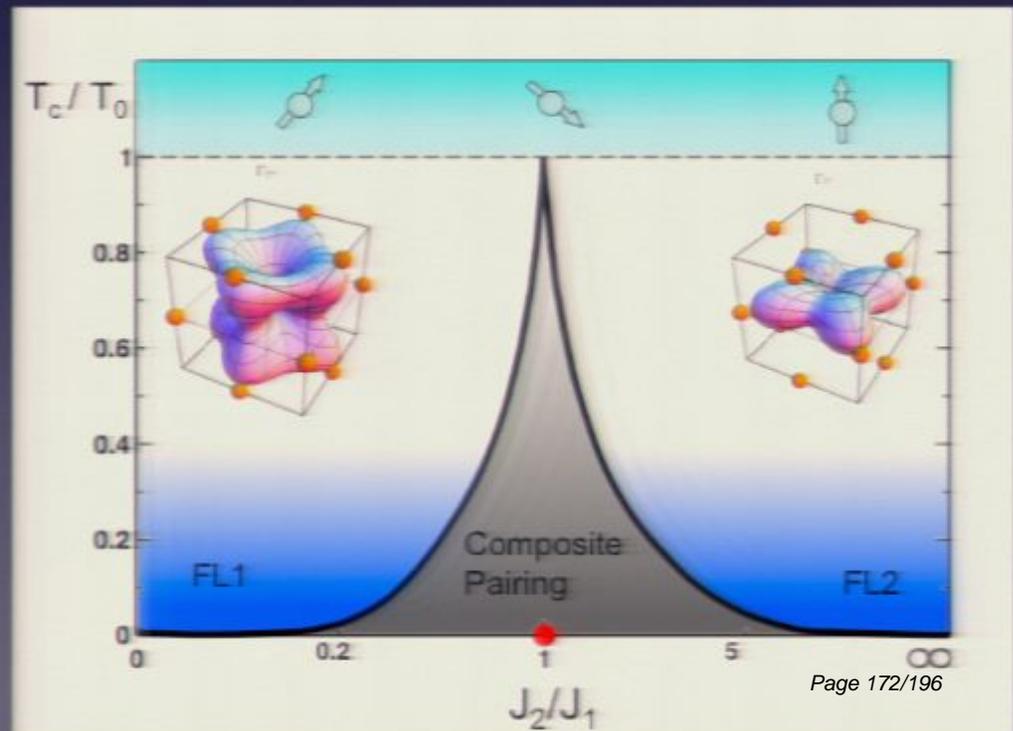
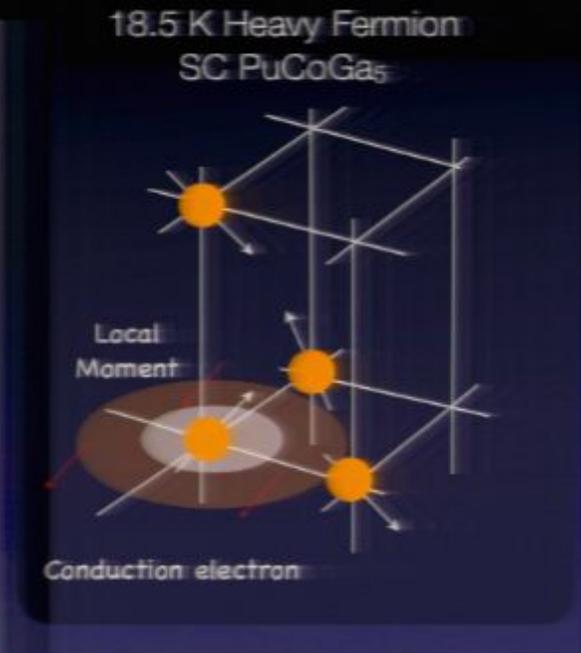
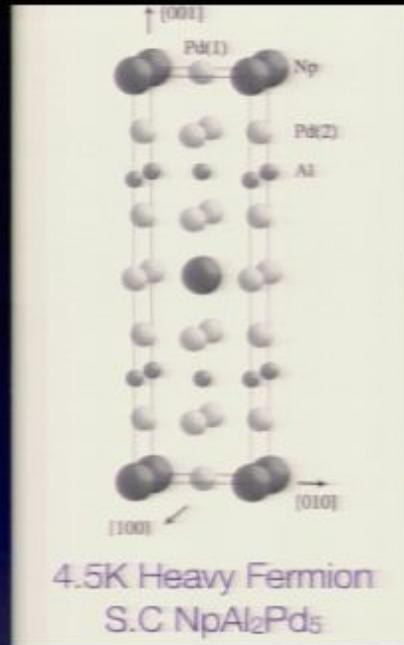
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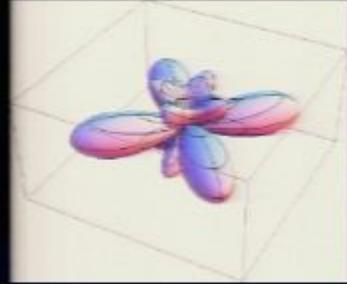
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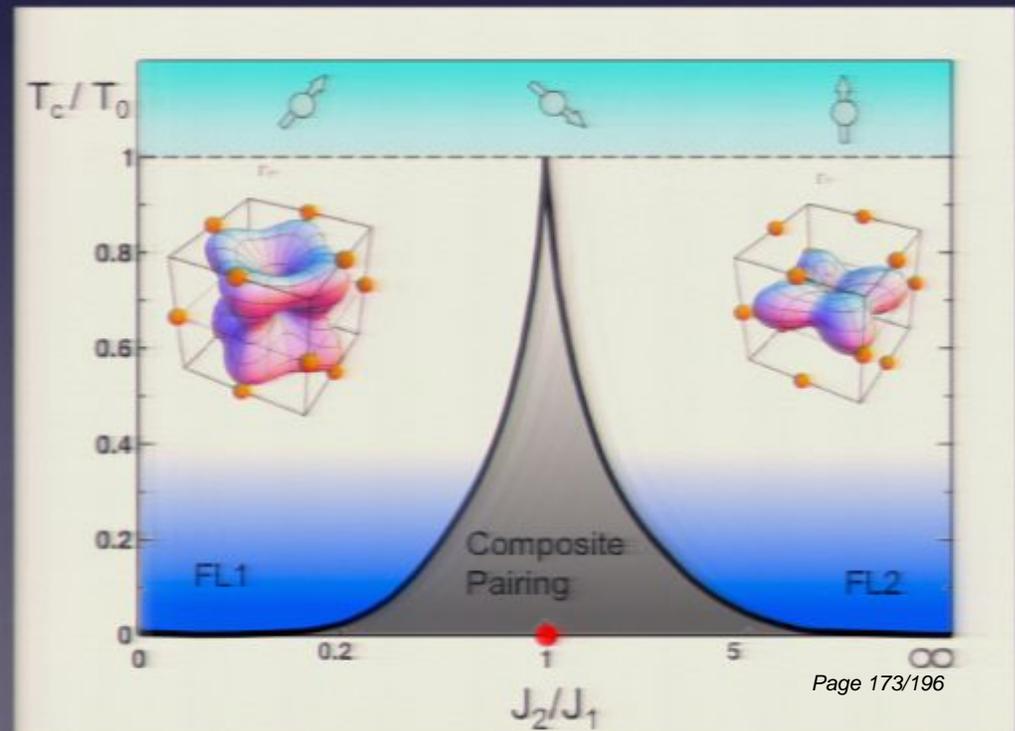
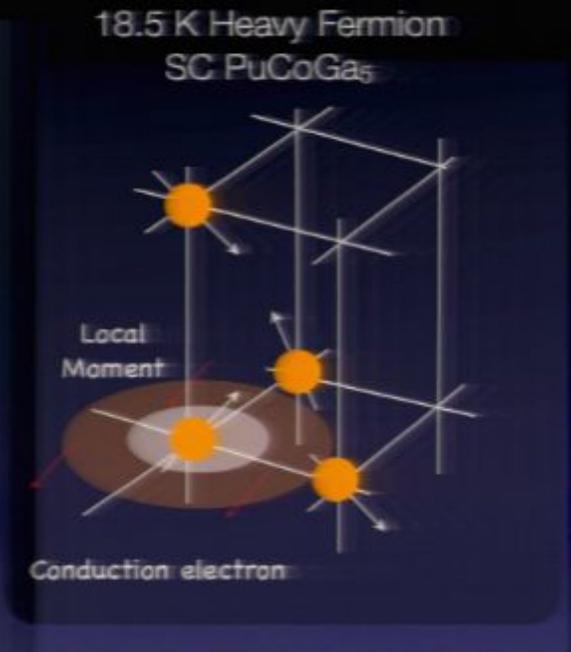
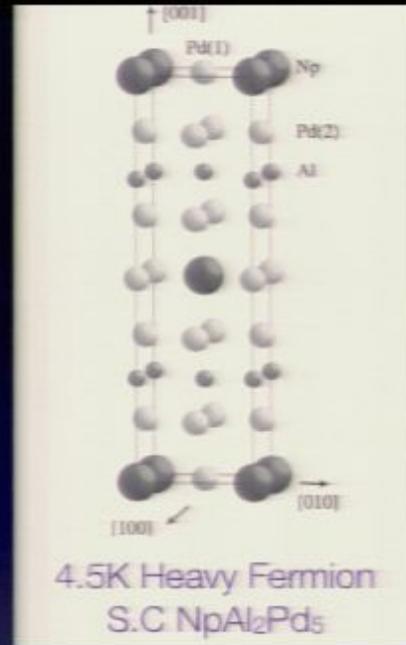
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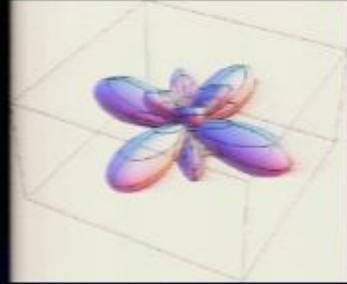
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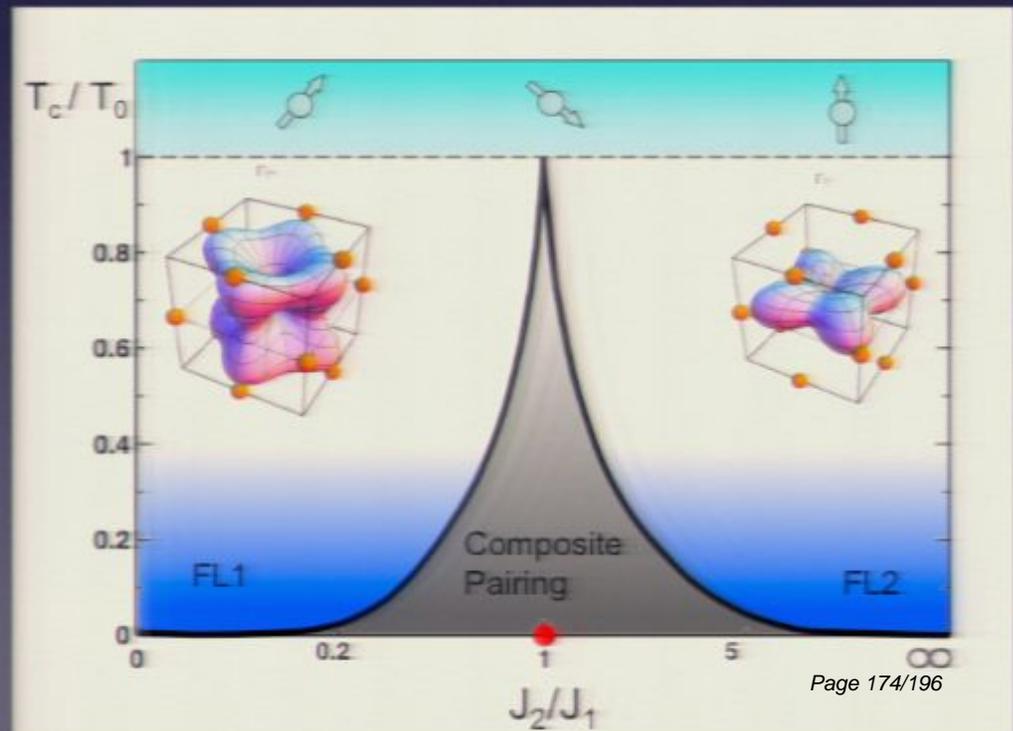
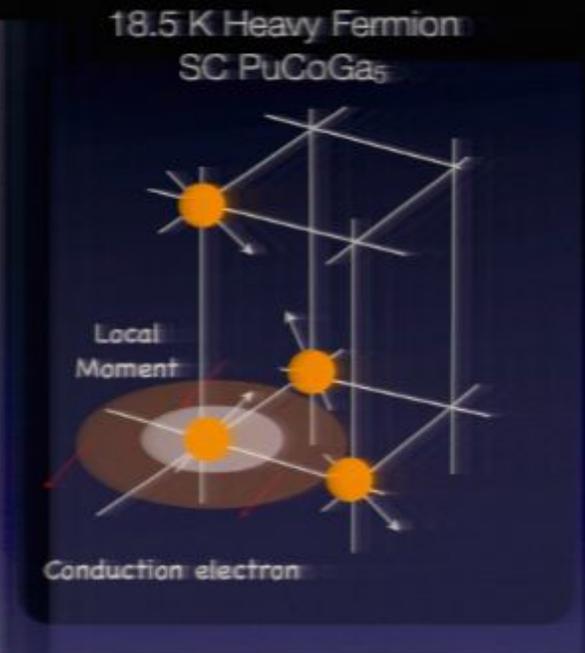
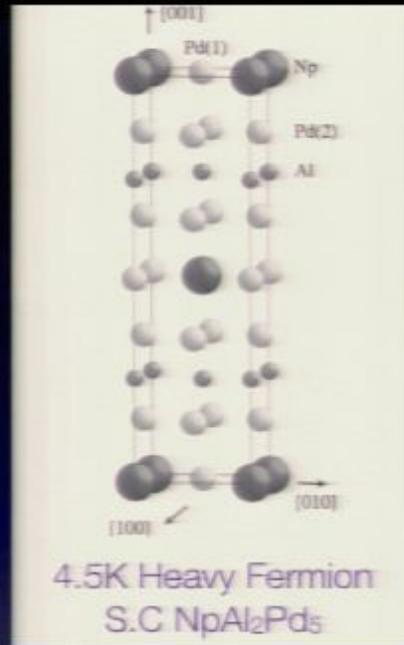
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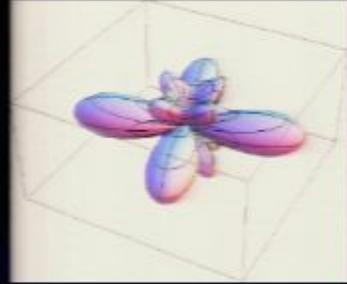
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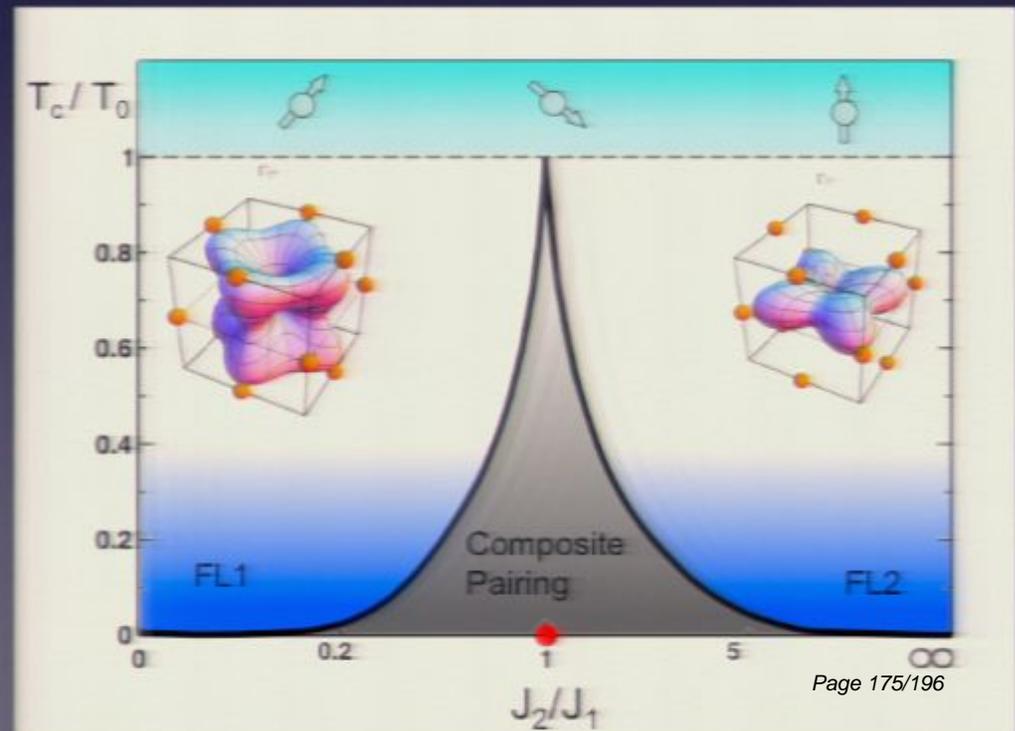
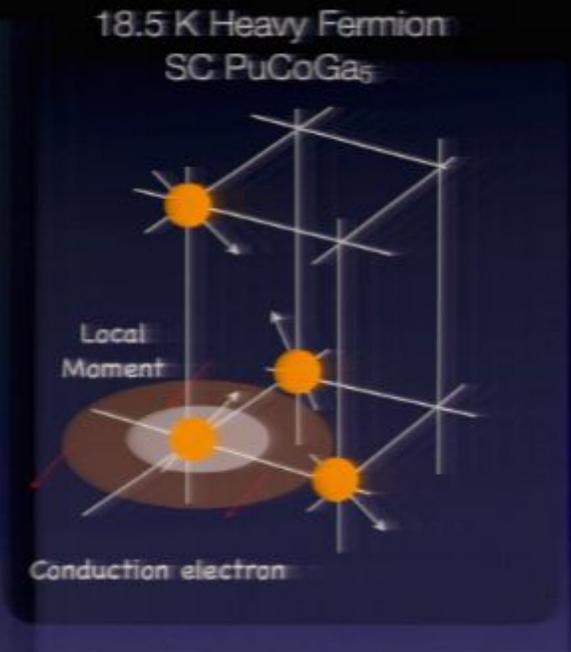
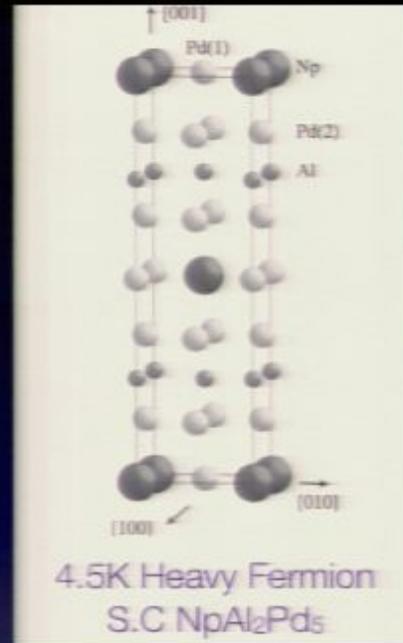
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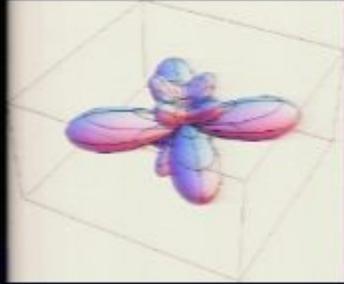
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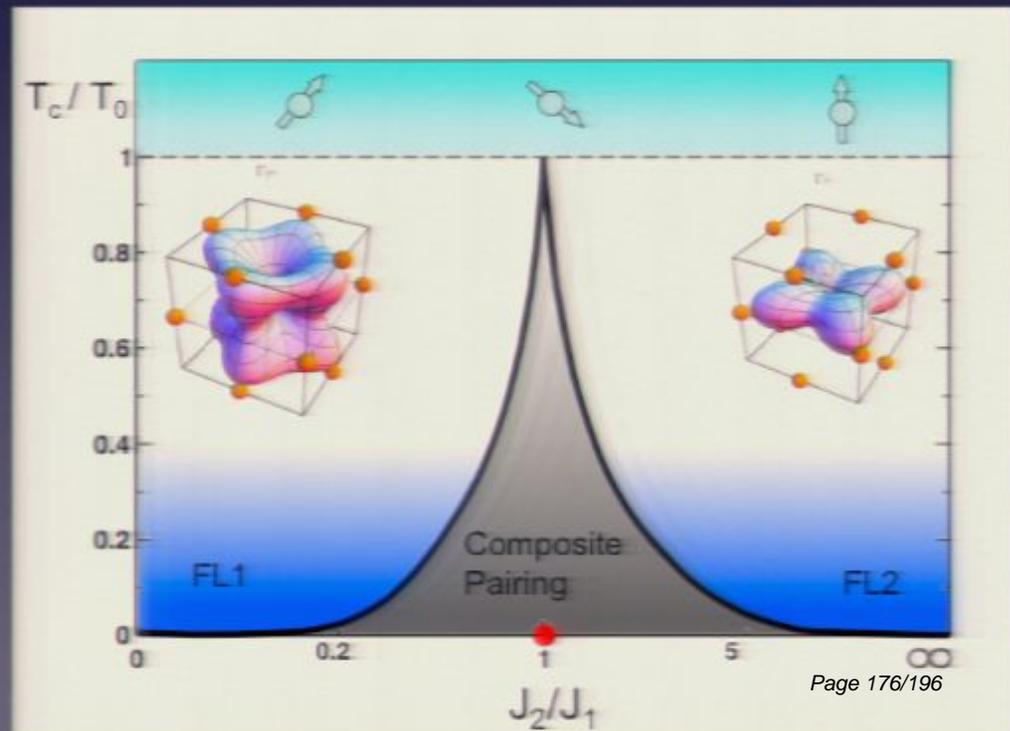
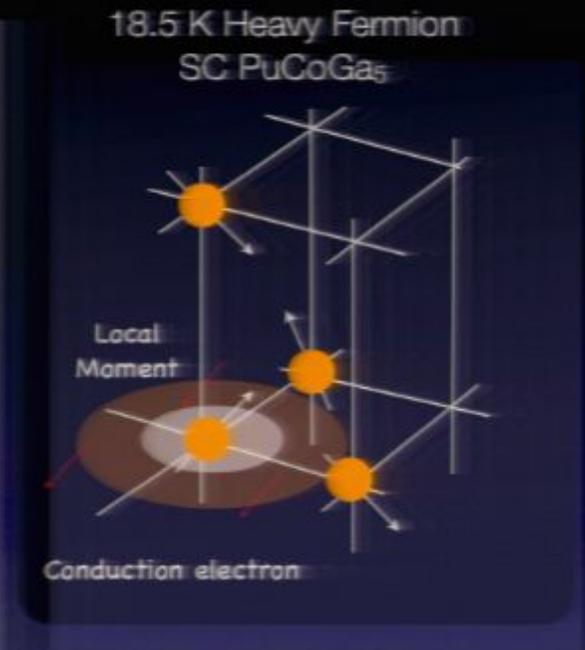
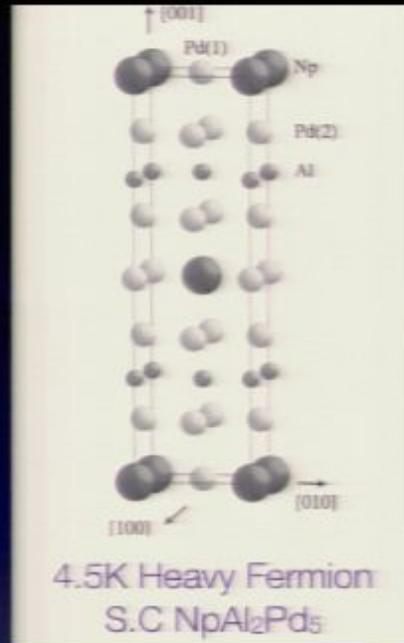
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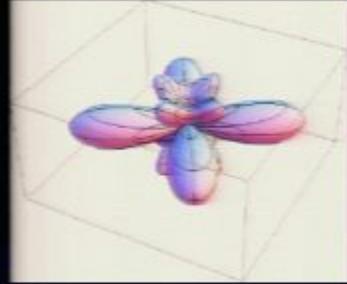
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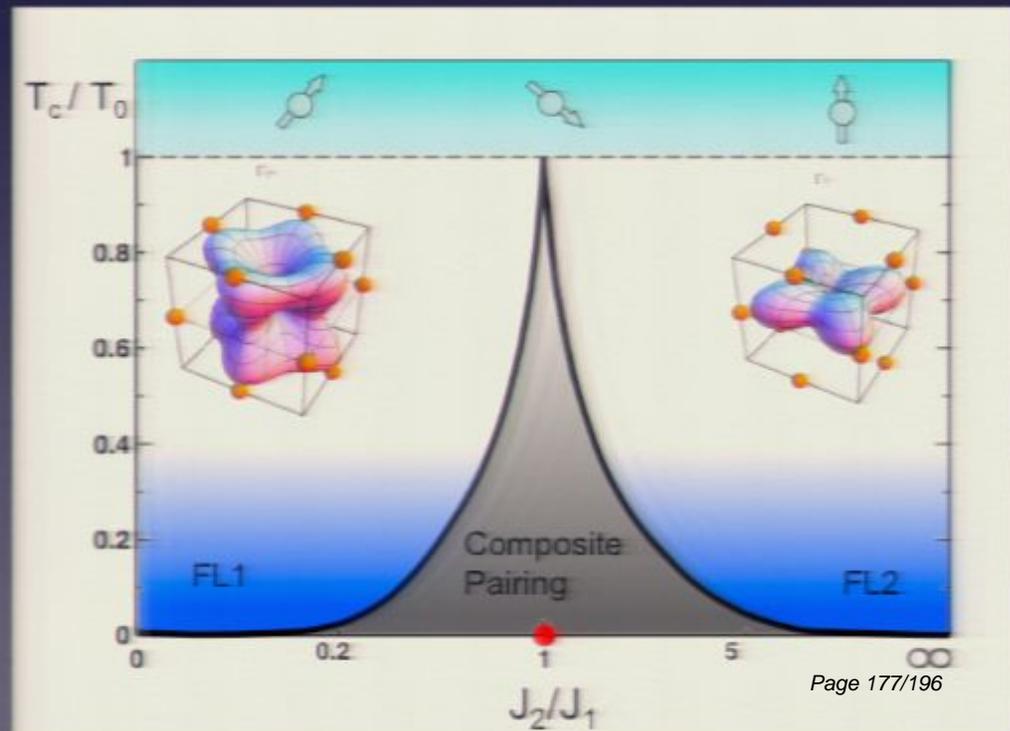
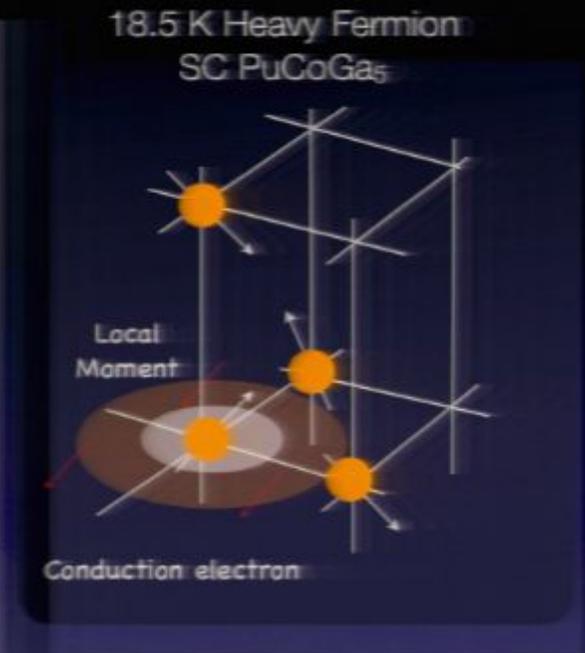
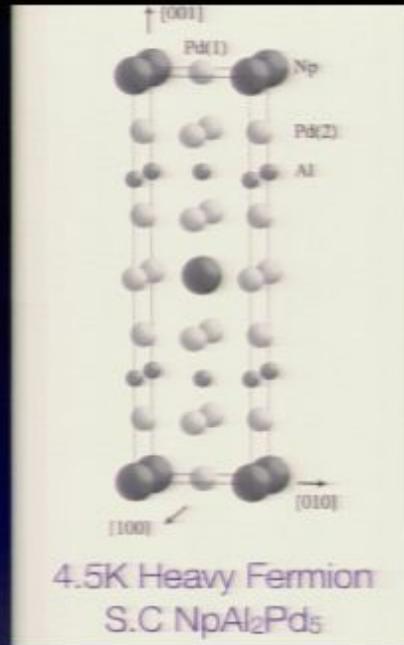
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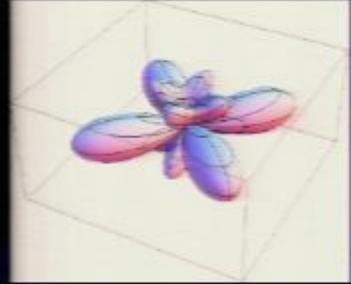
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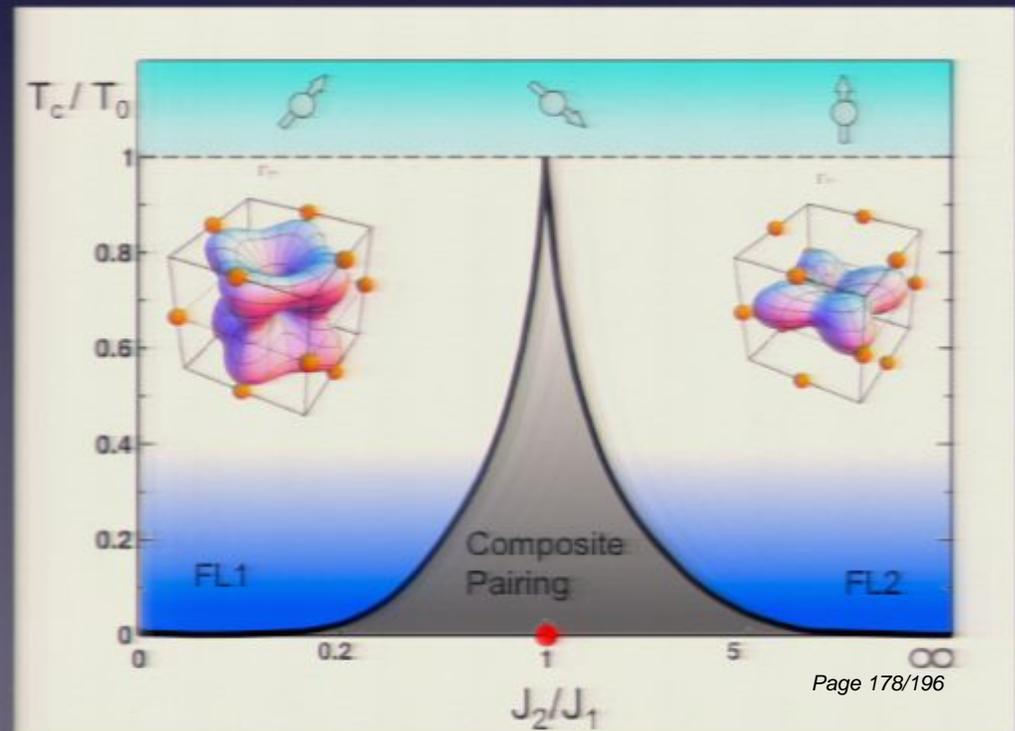
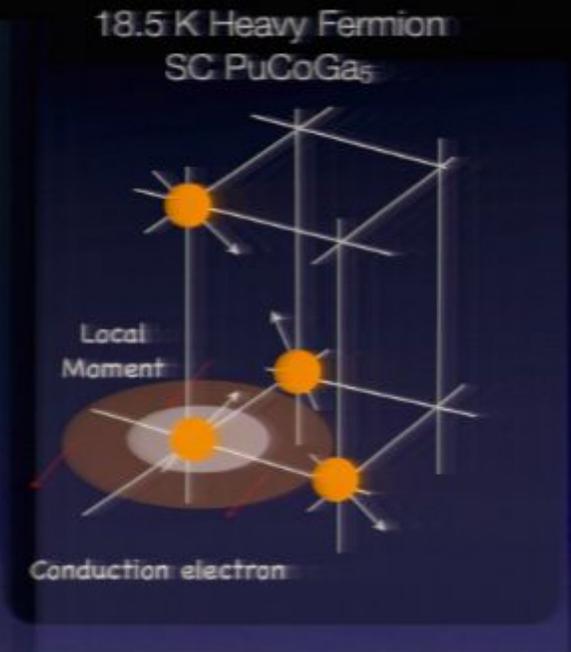
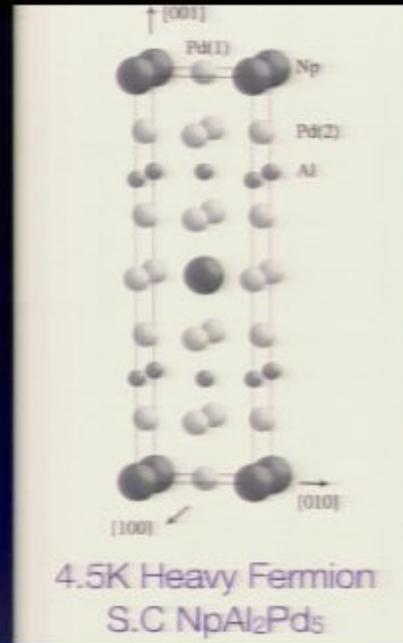
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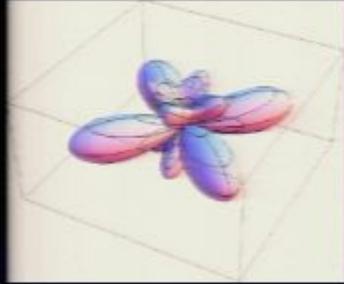
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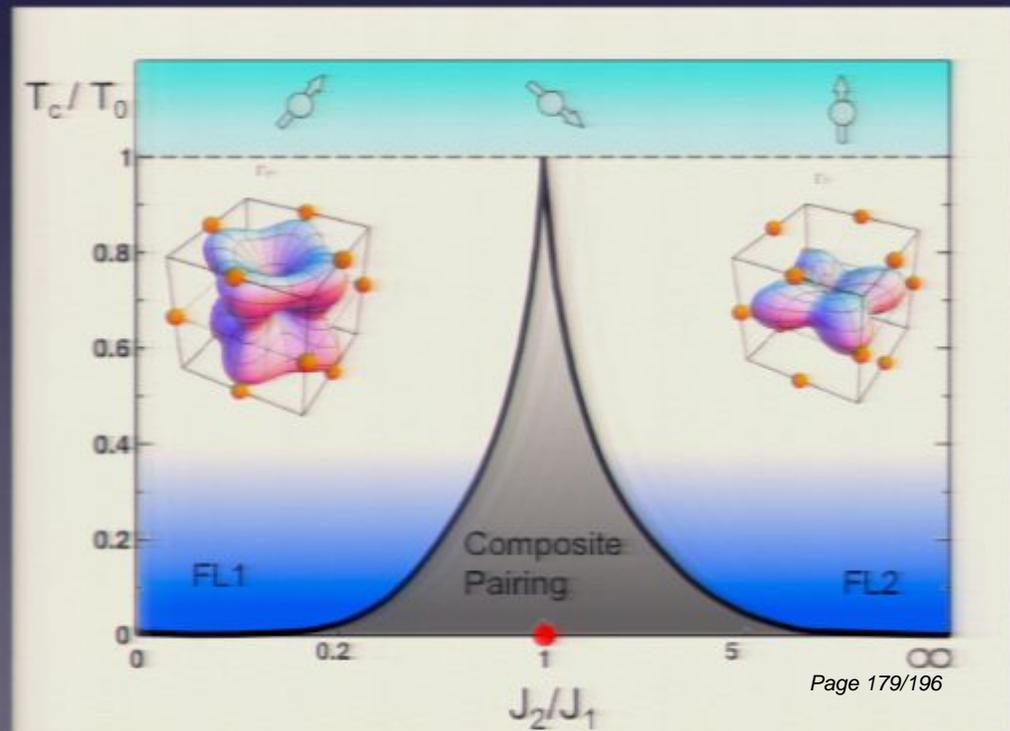
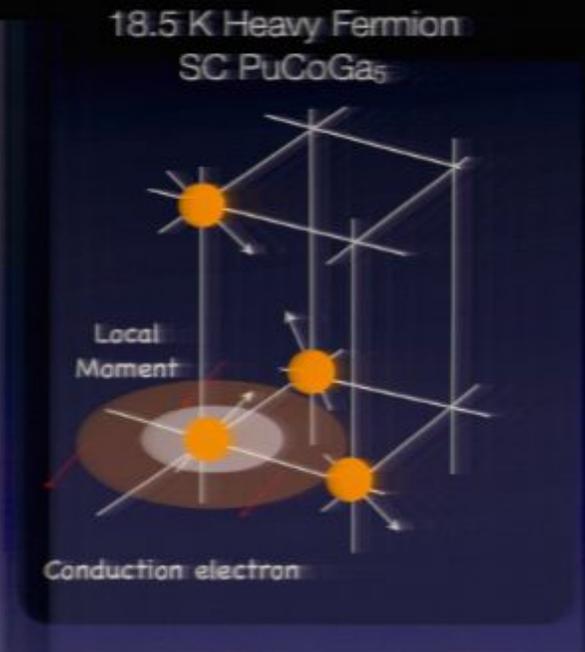
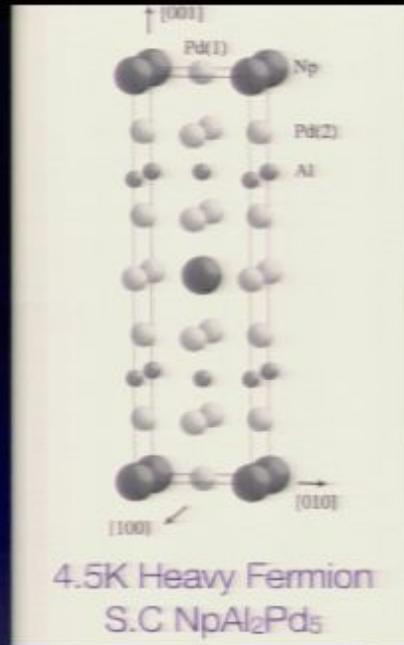
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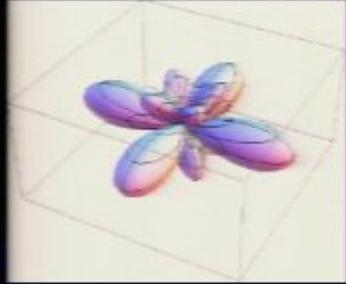
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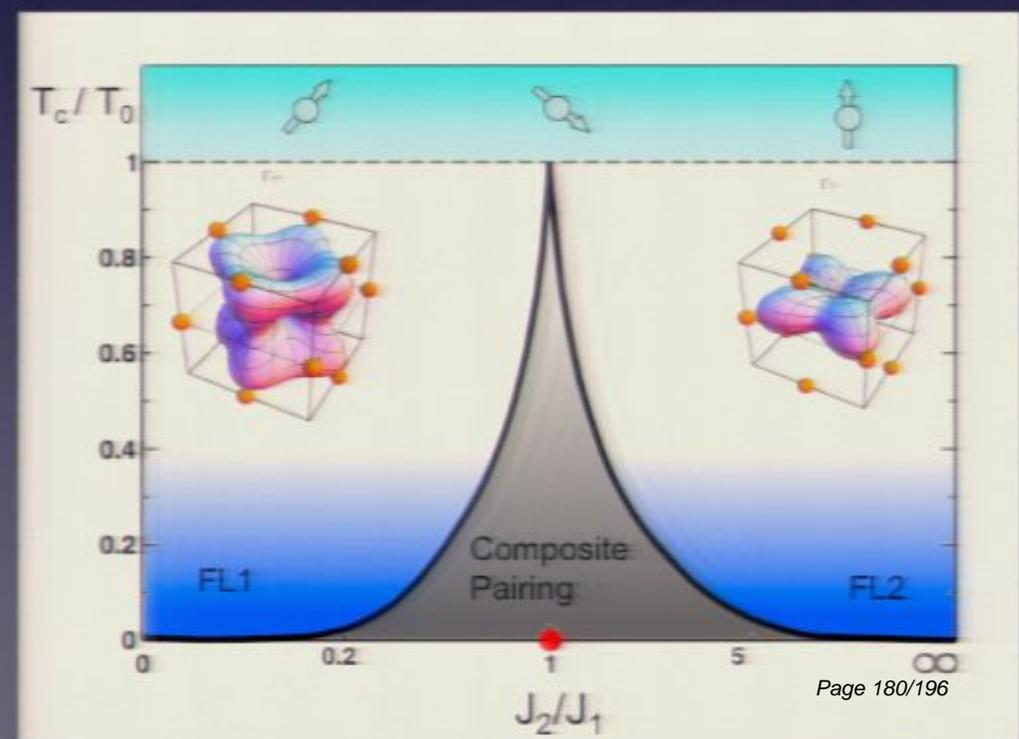
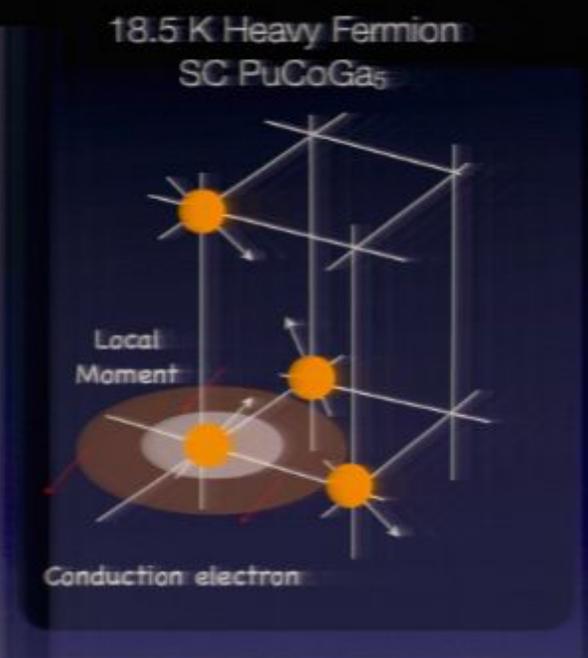
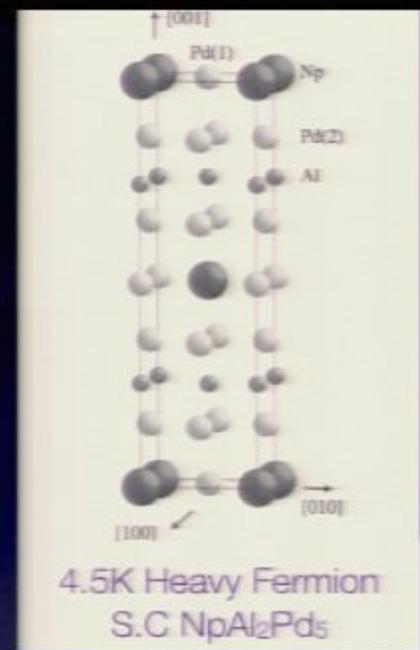
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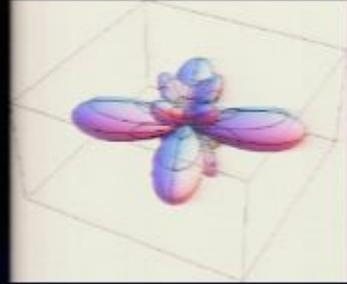
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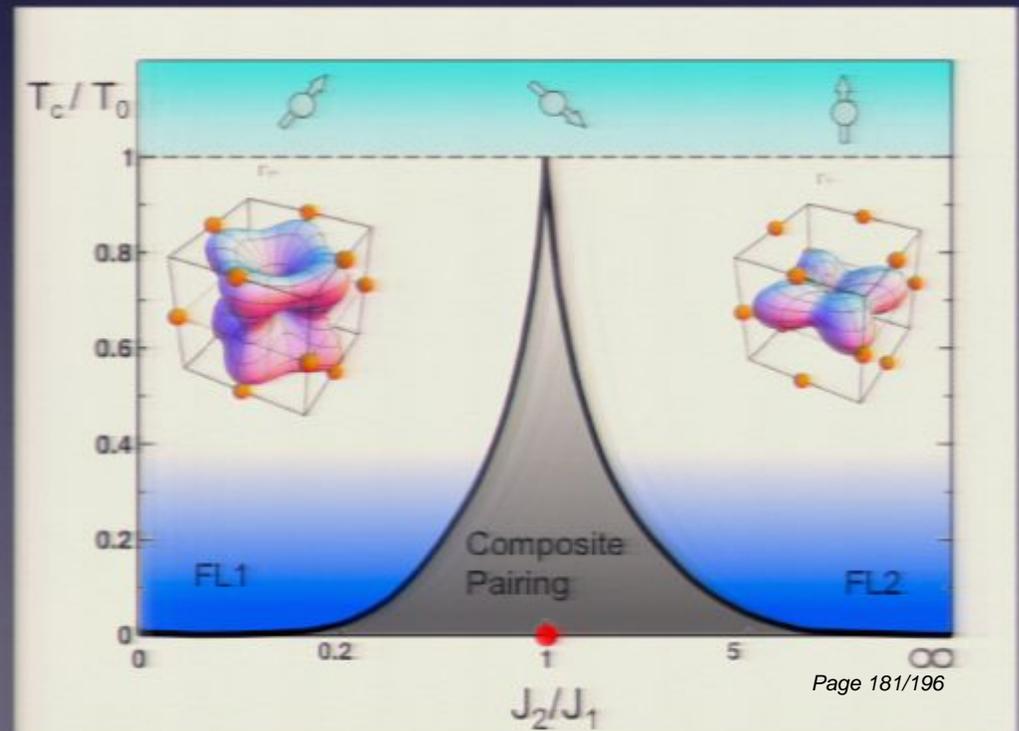
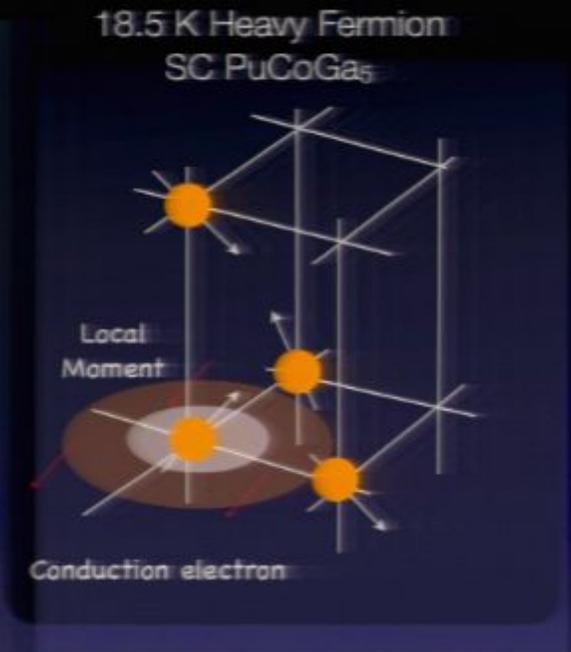
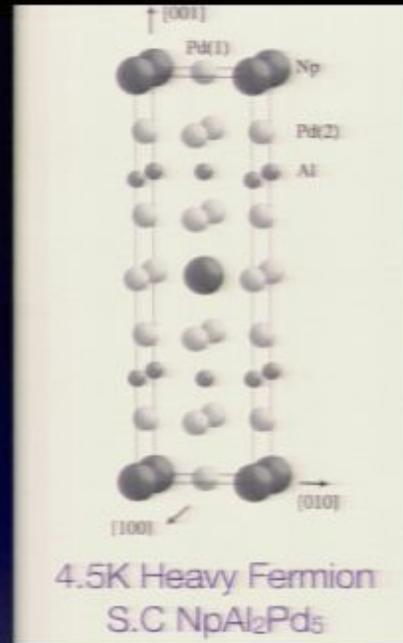
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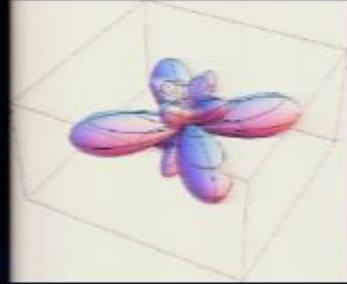
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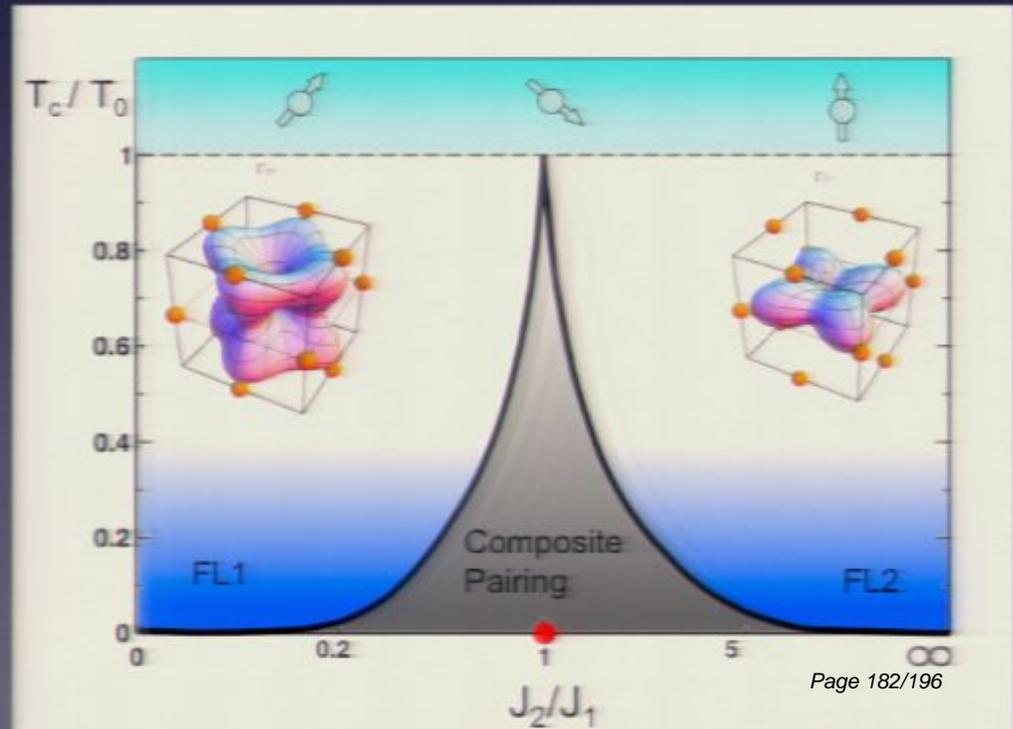
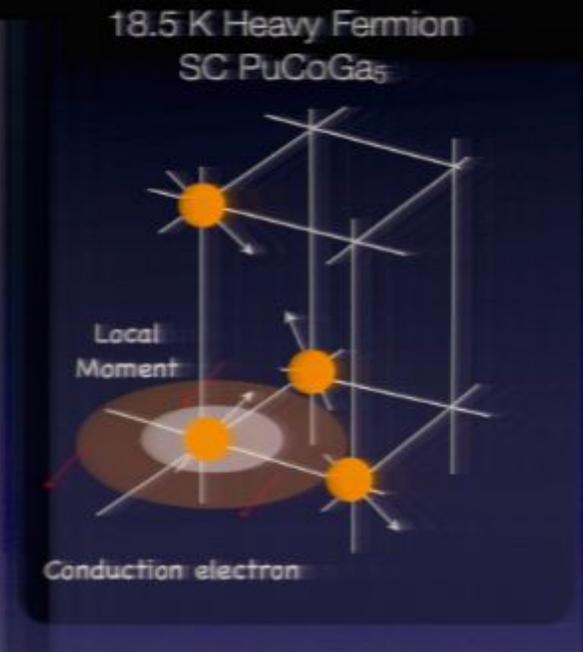
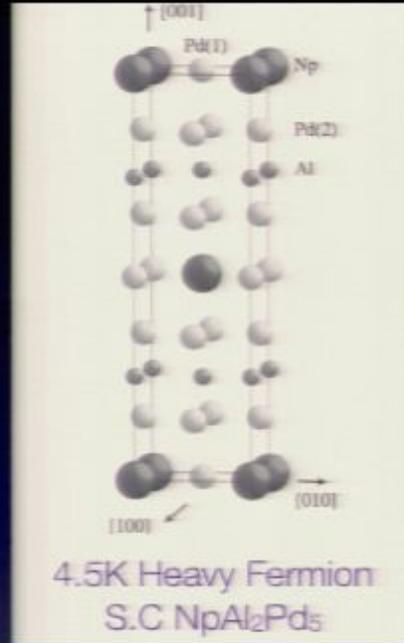
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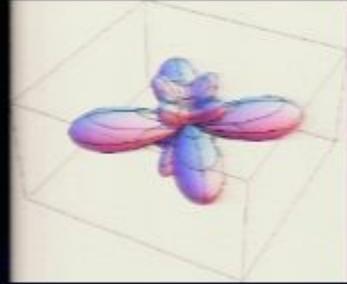
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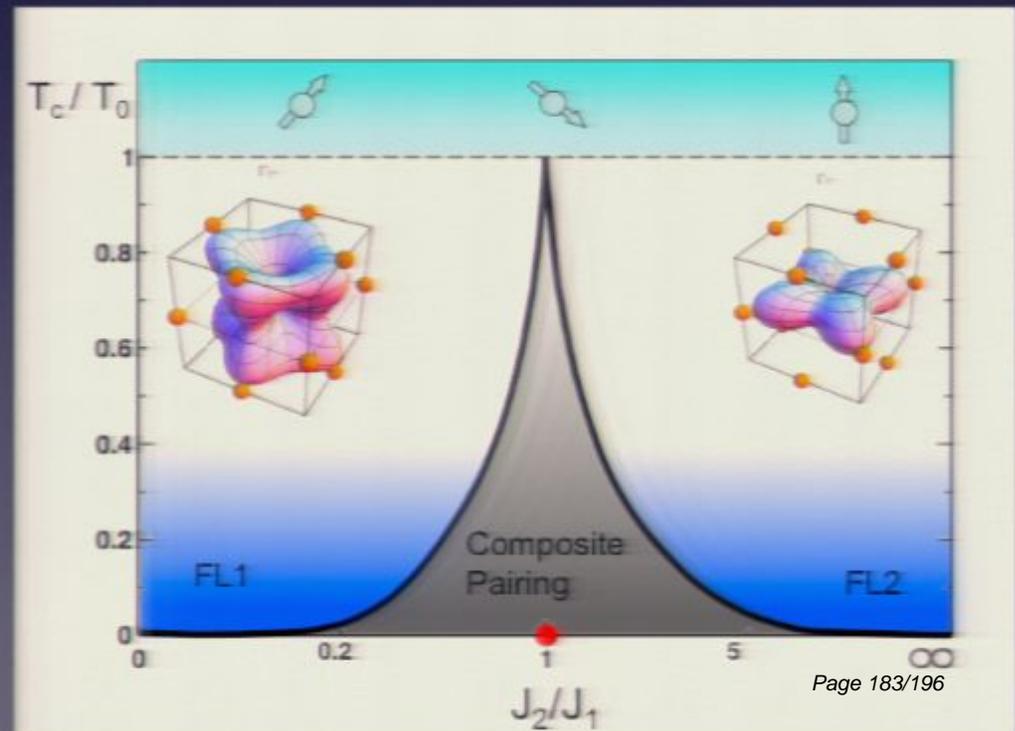
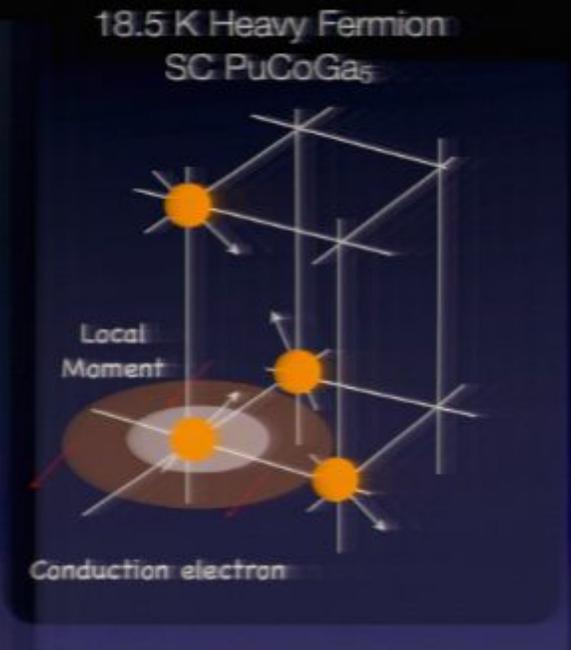
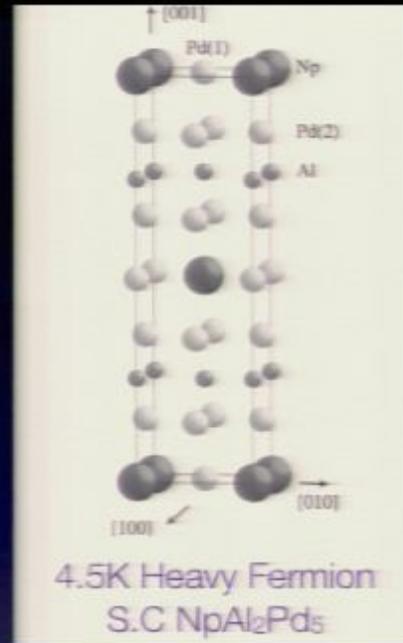
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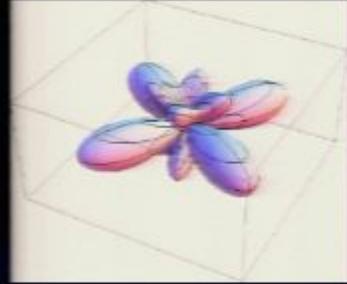
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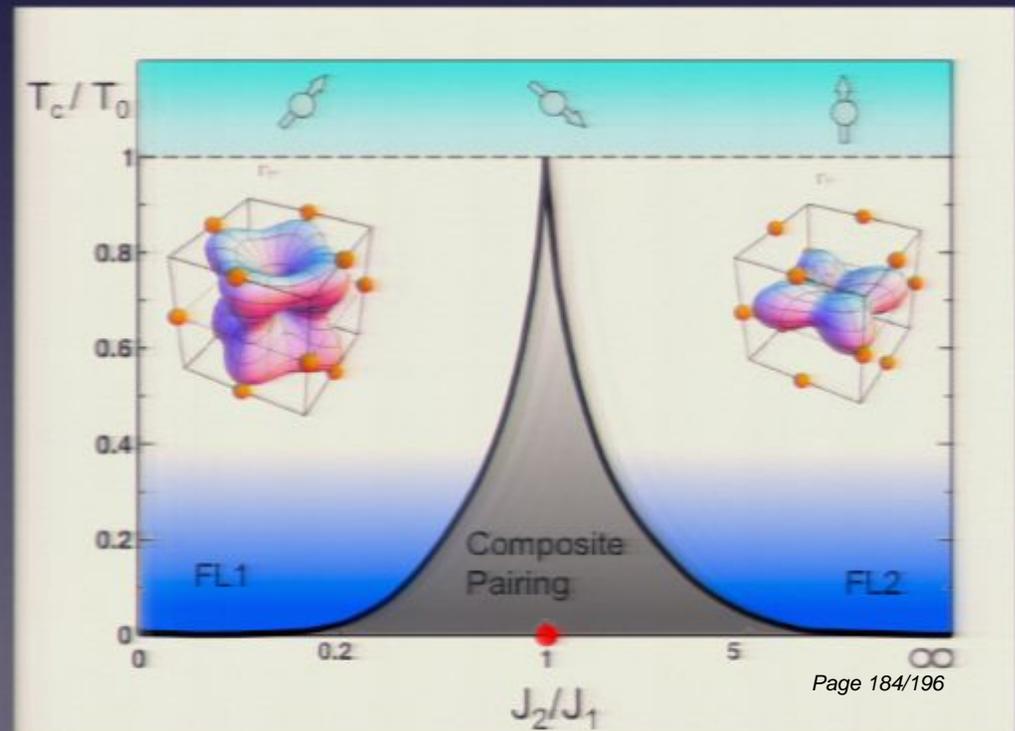
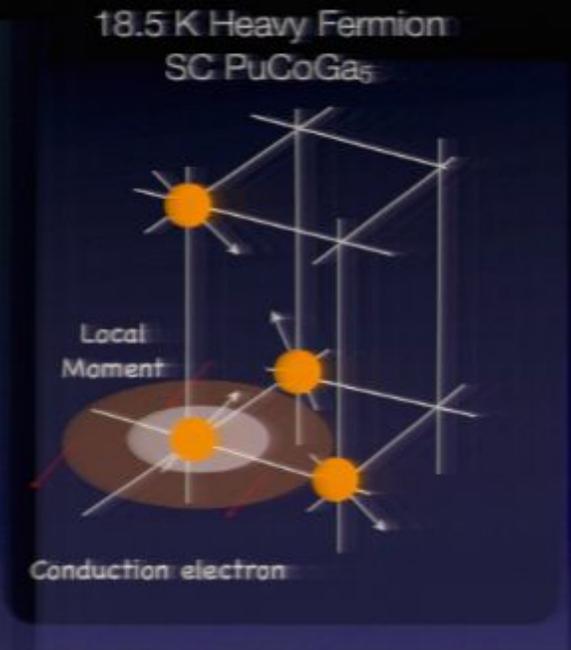
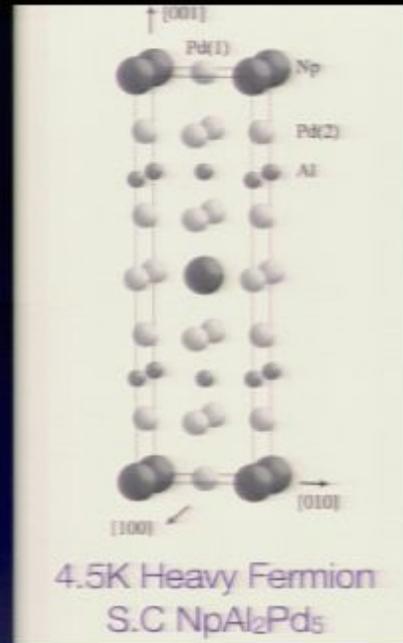
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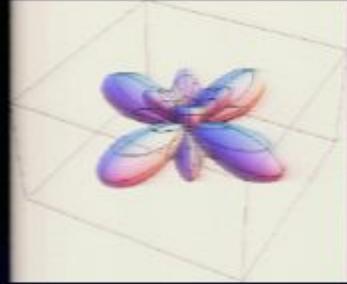
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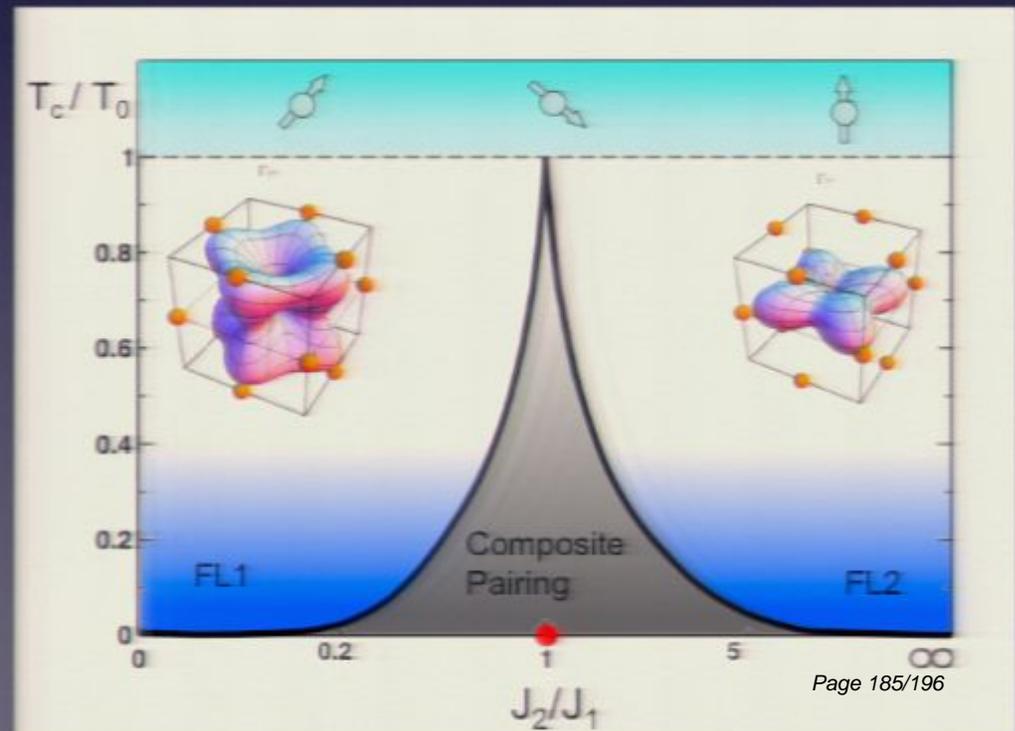
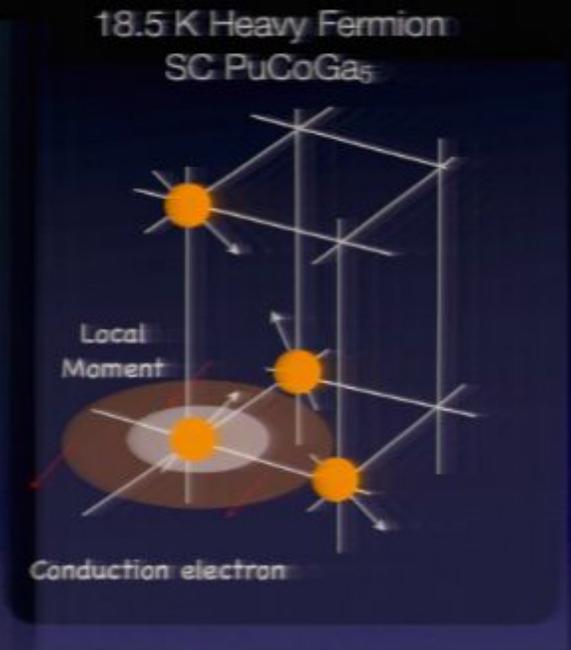
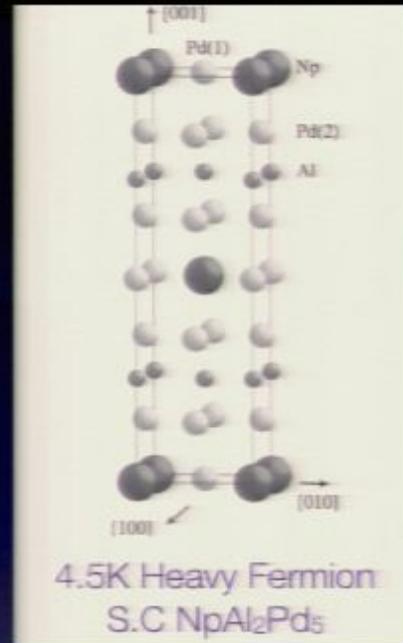
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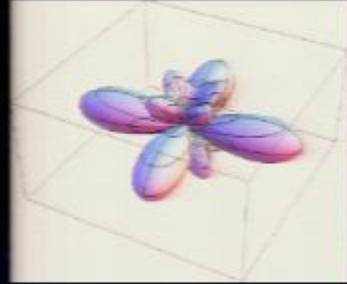
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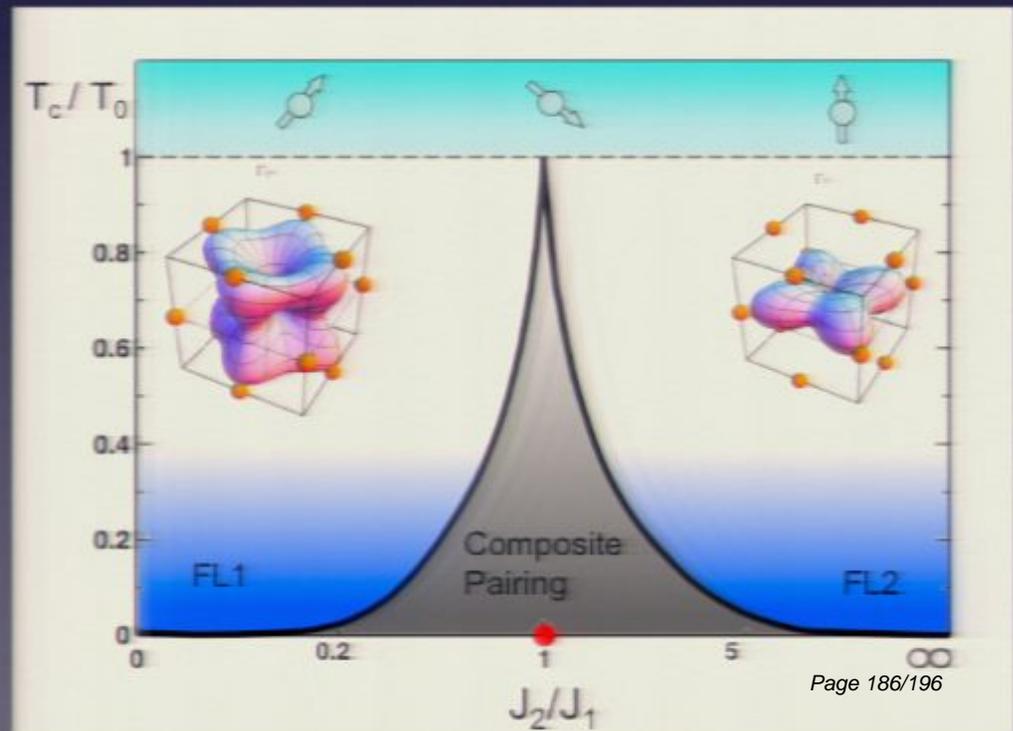
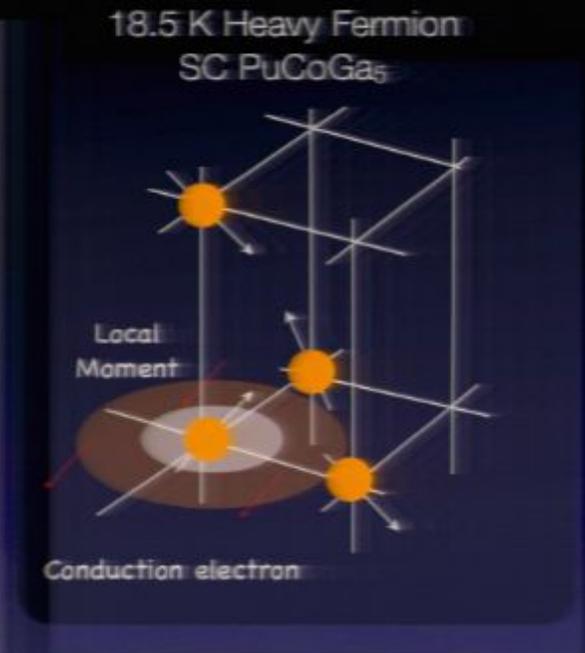
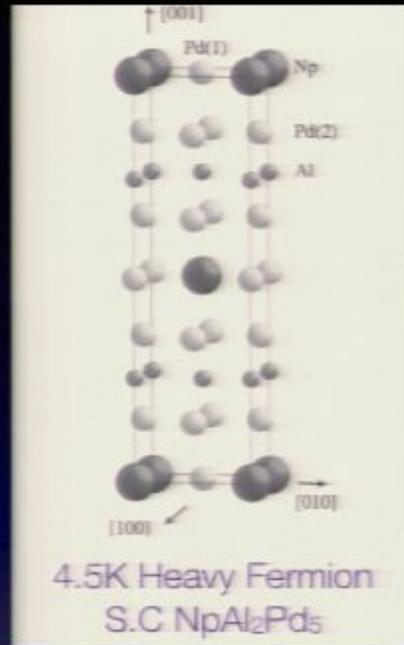
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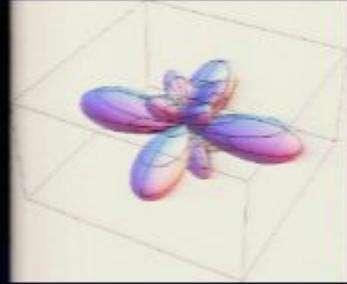
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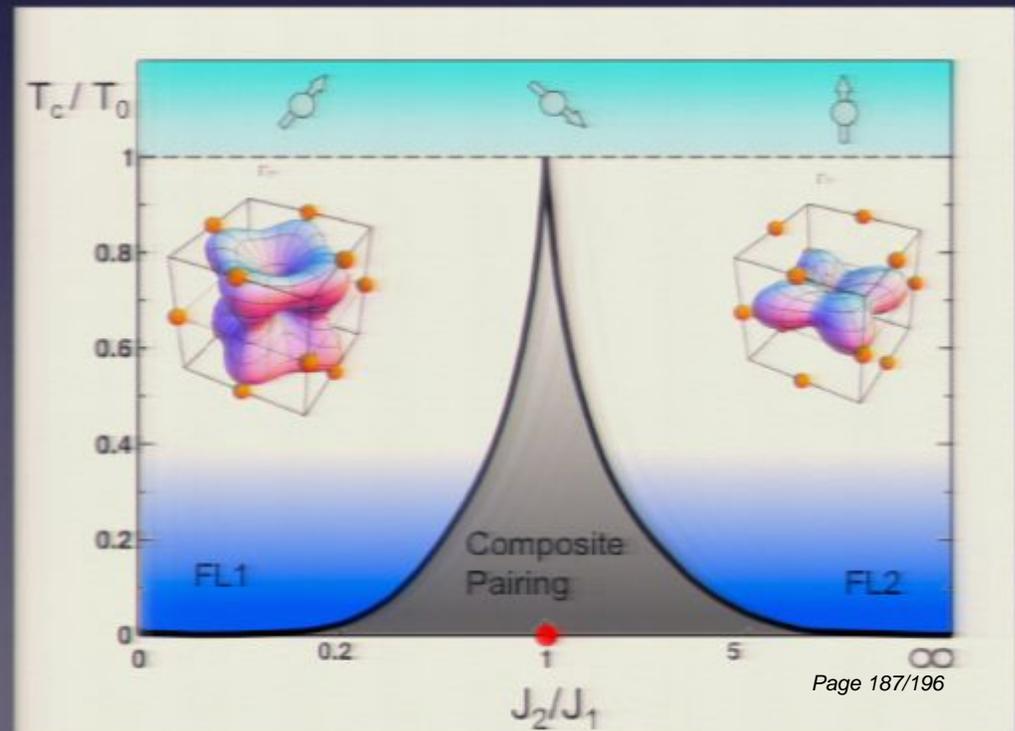
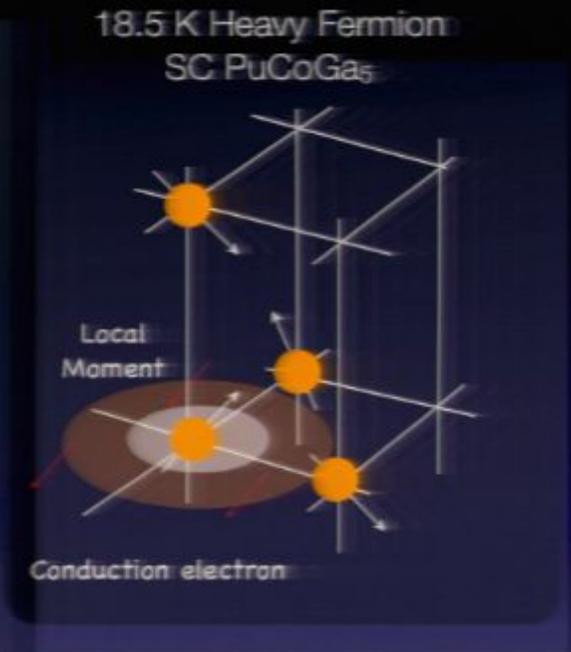
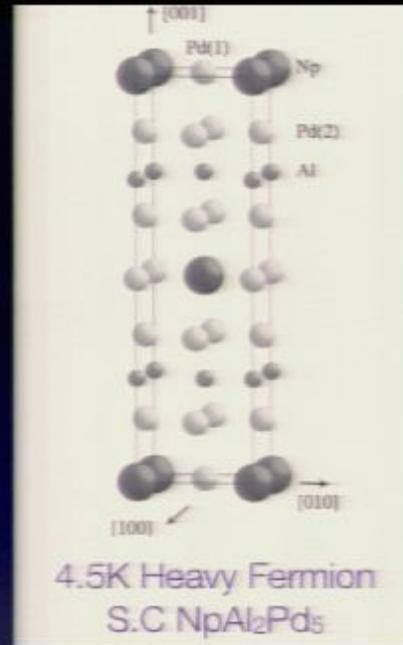
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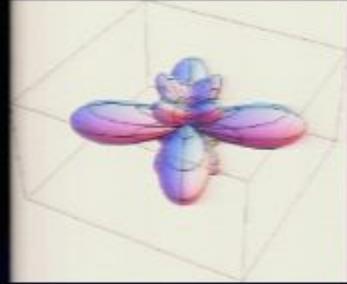
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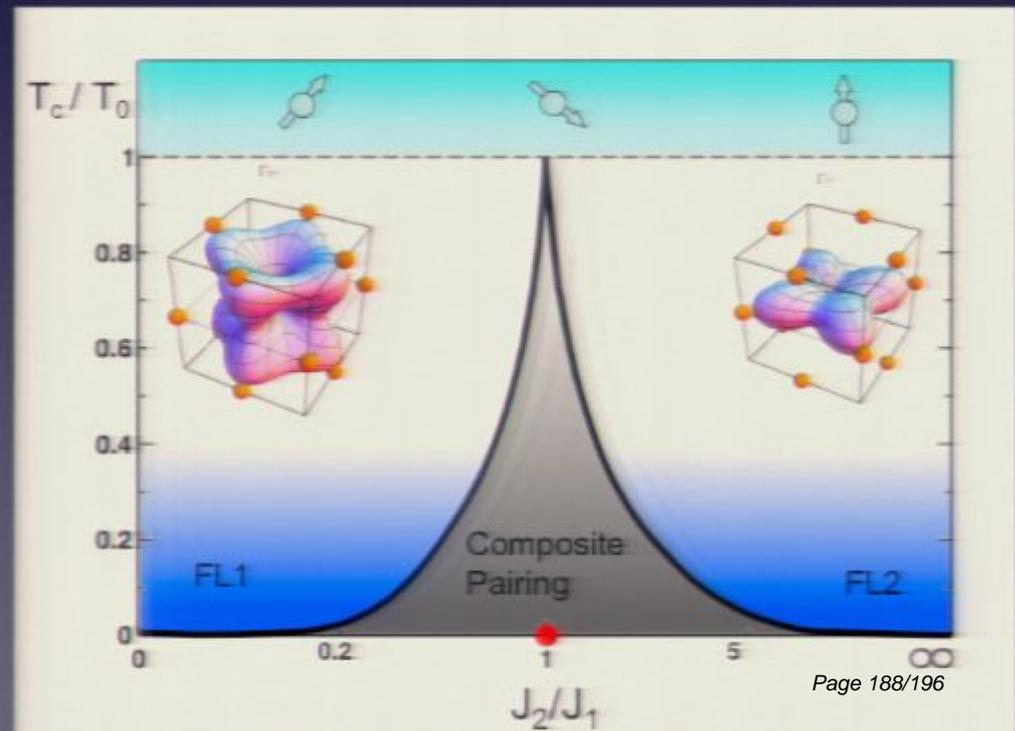
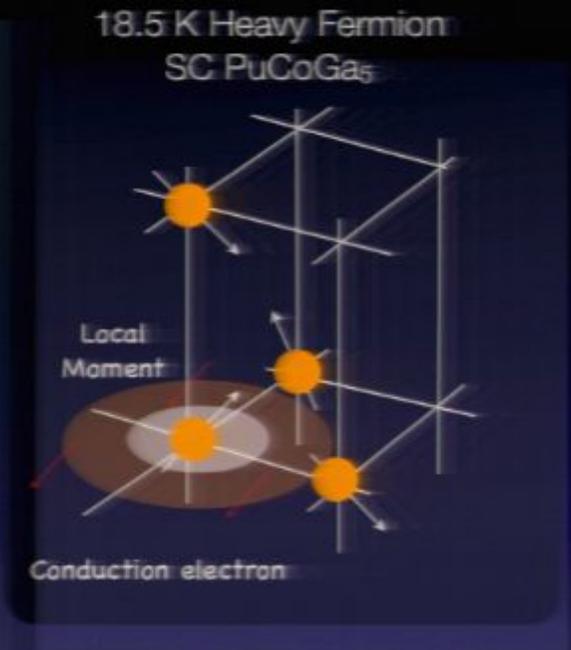
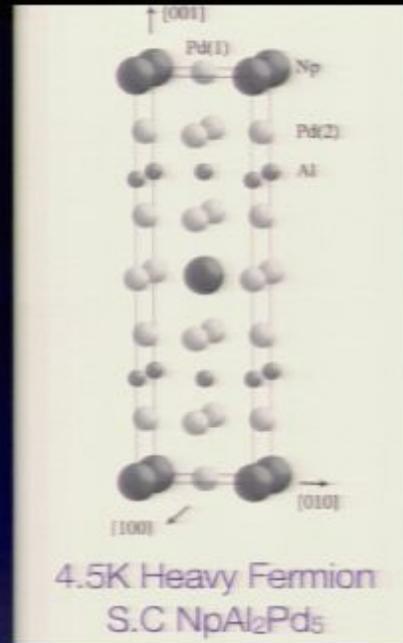
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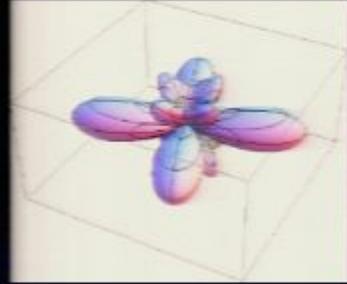
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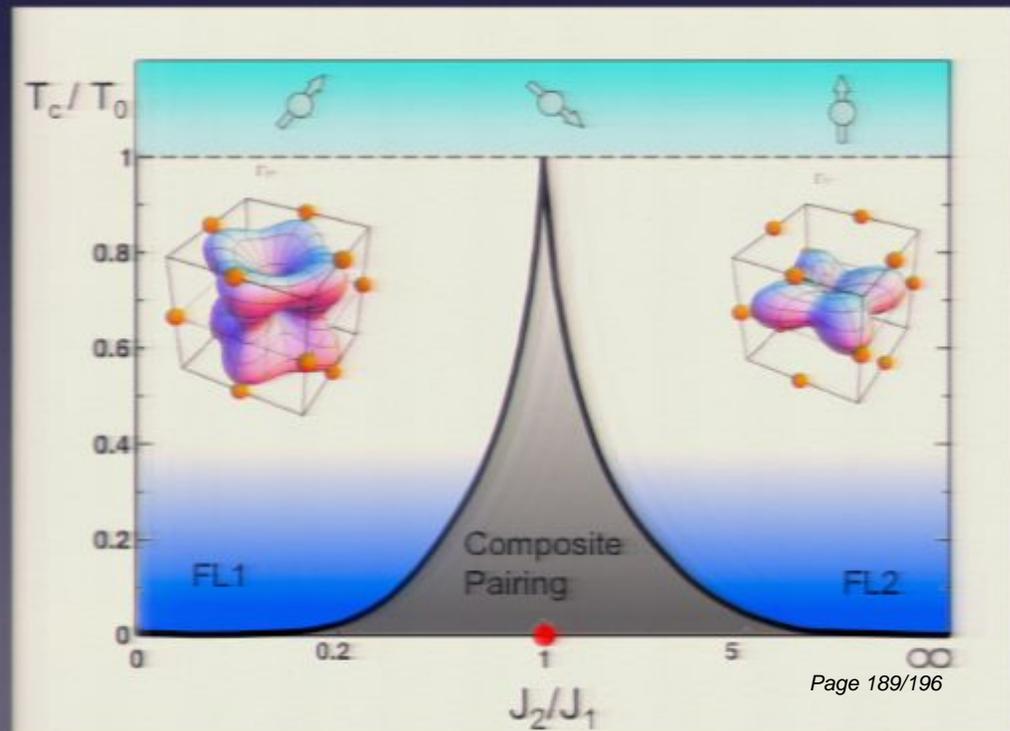
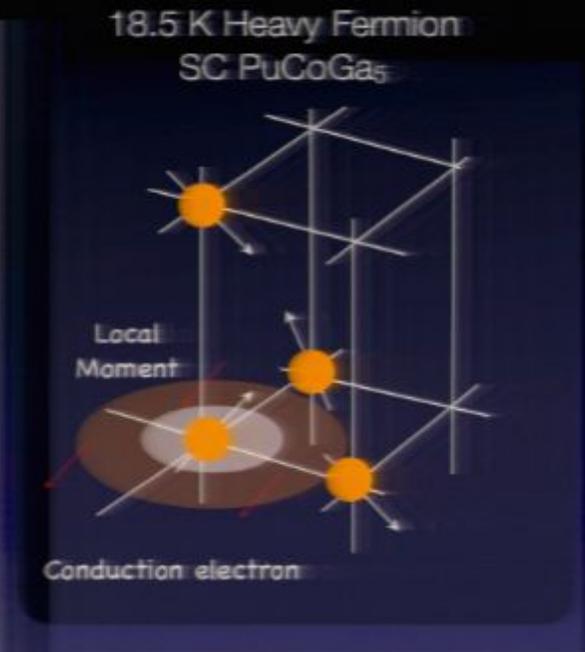
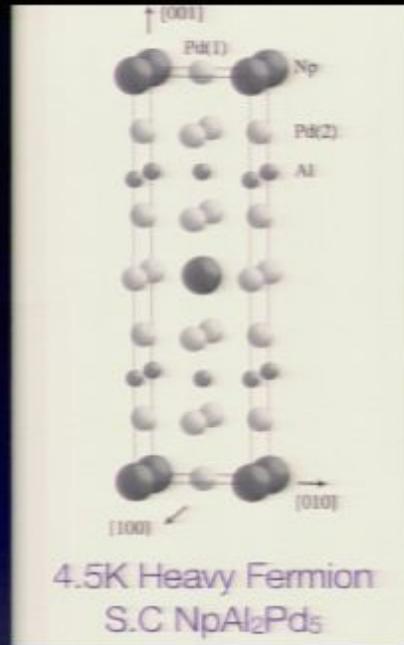
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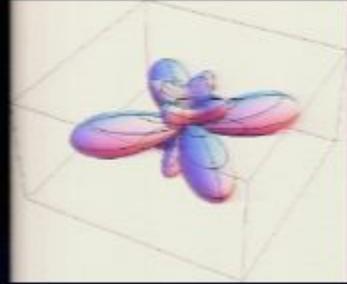
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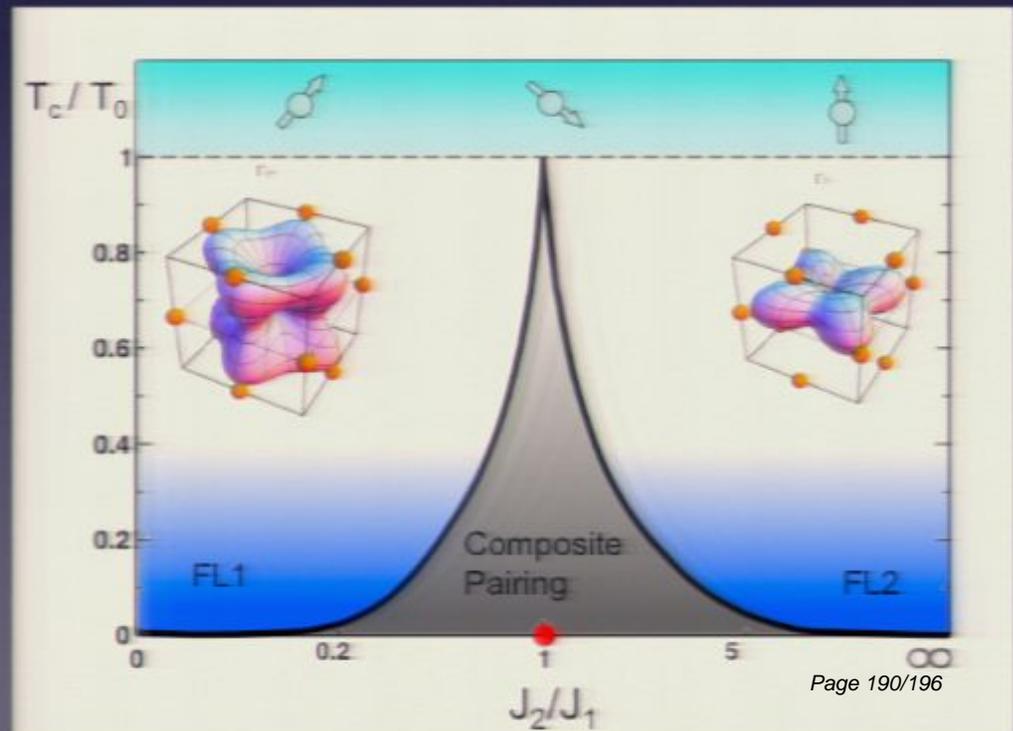
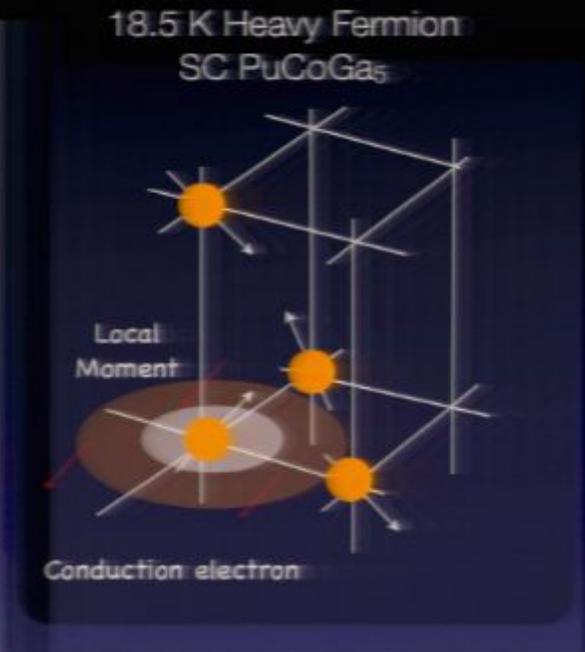
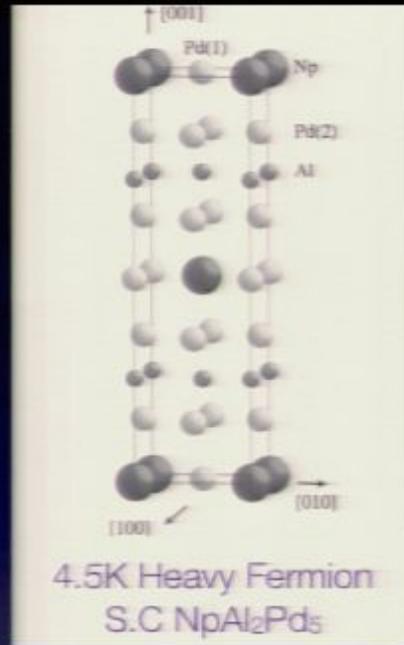
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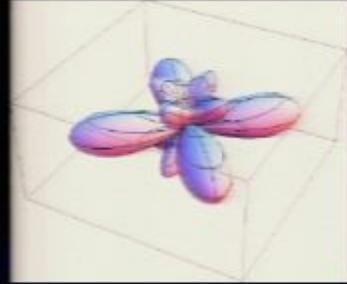
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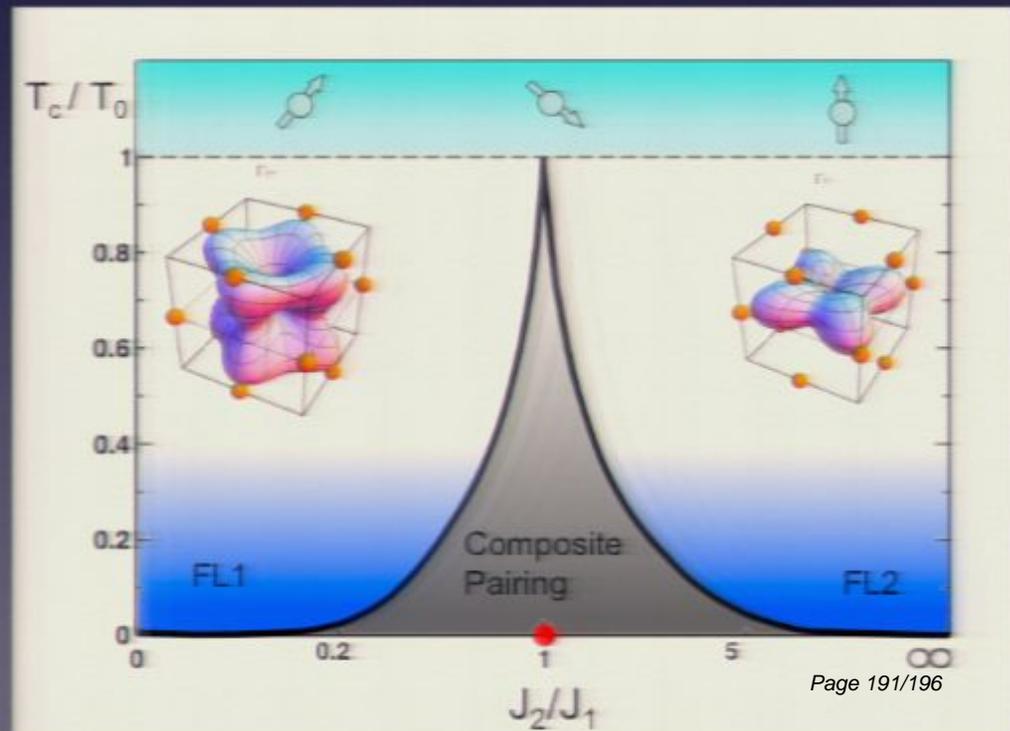
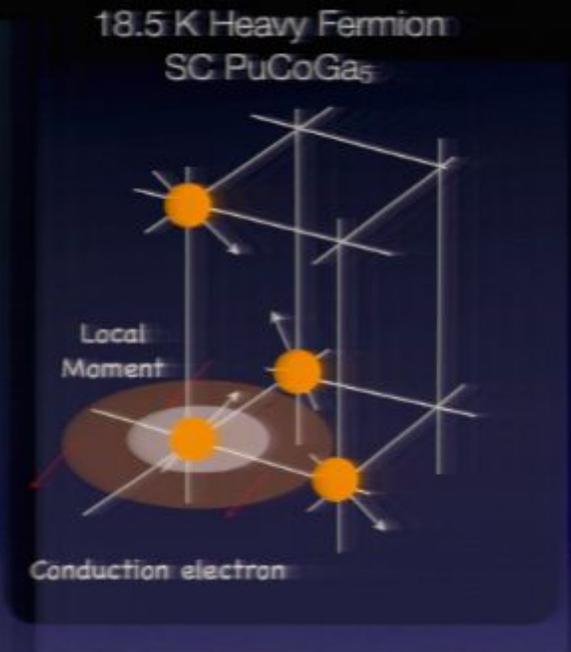
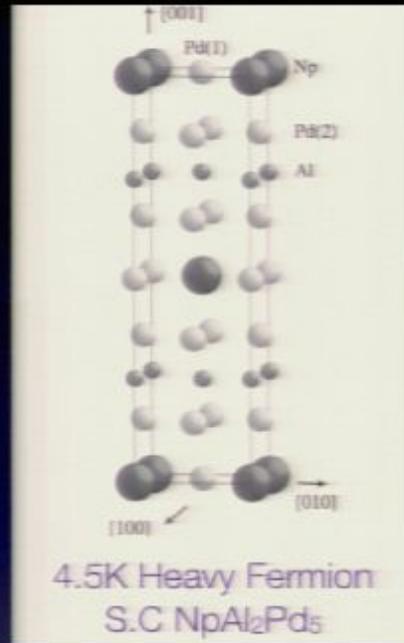
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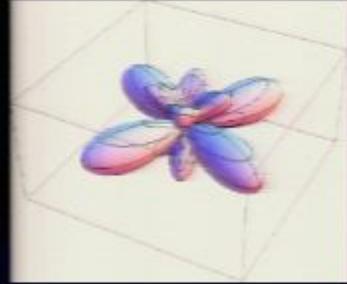
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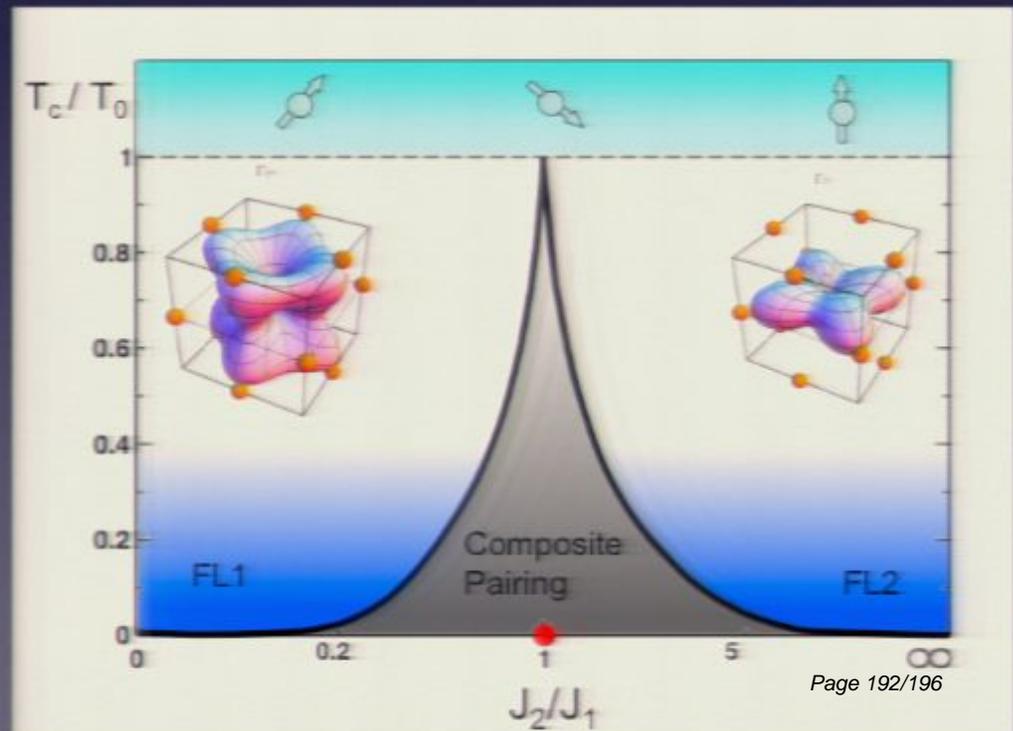
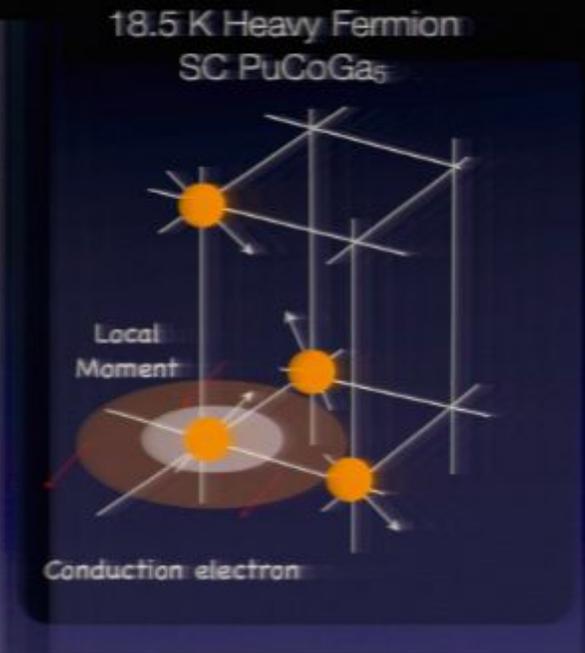
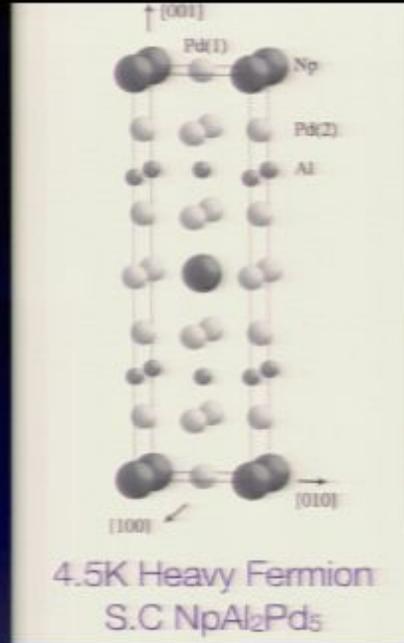
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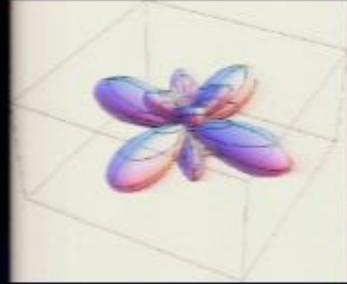
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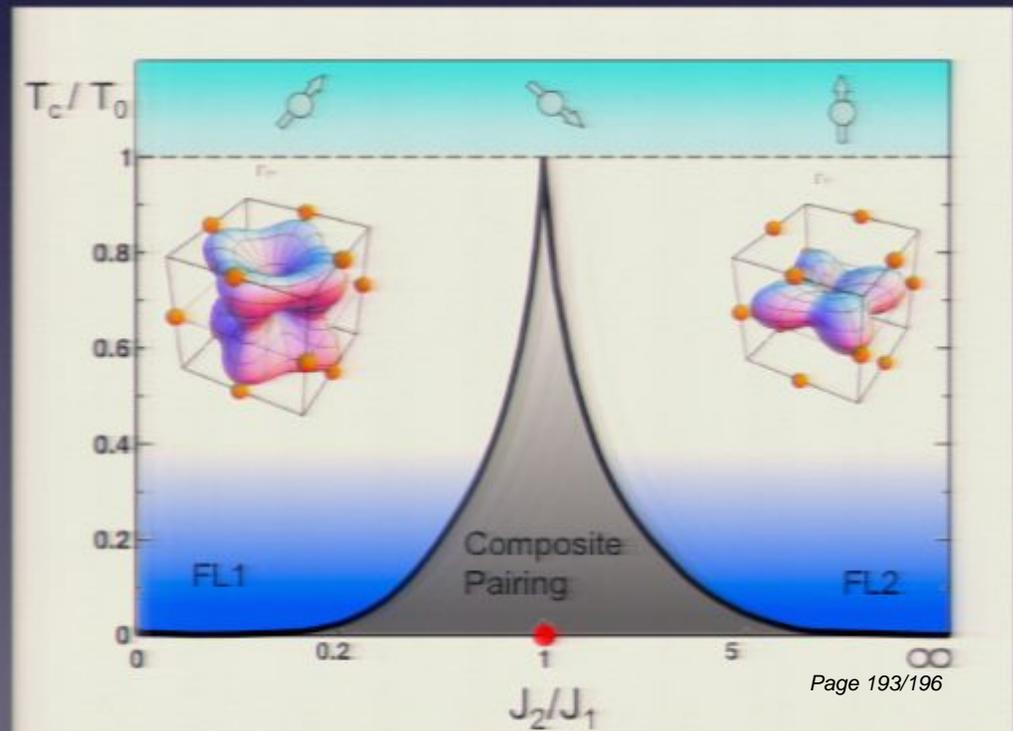
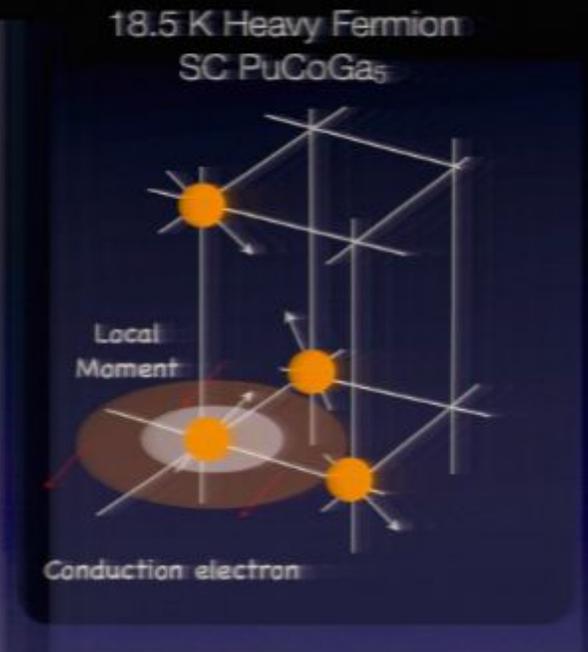
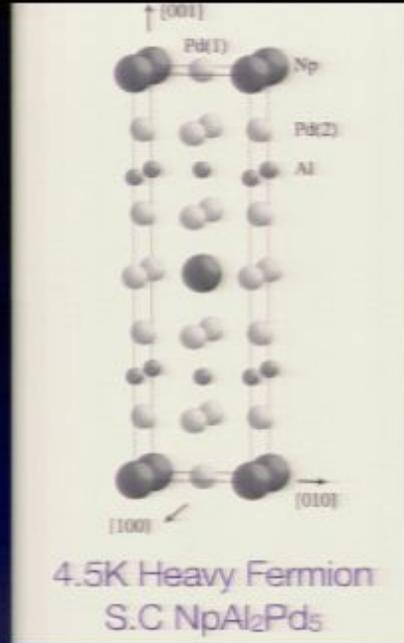
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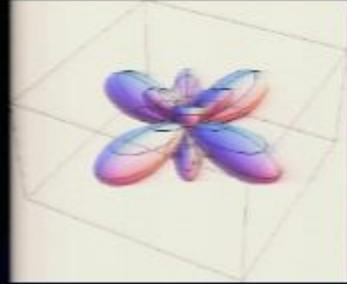
# Thank You!



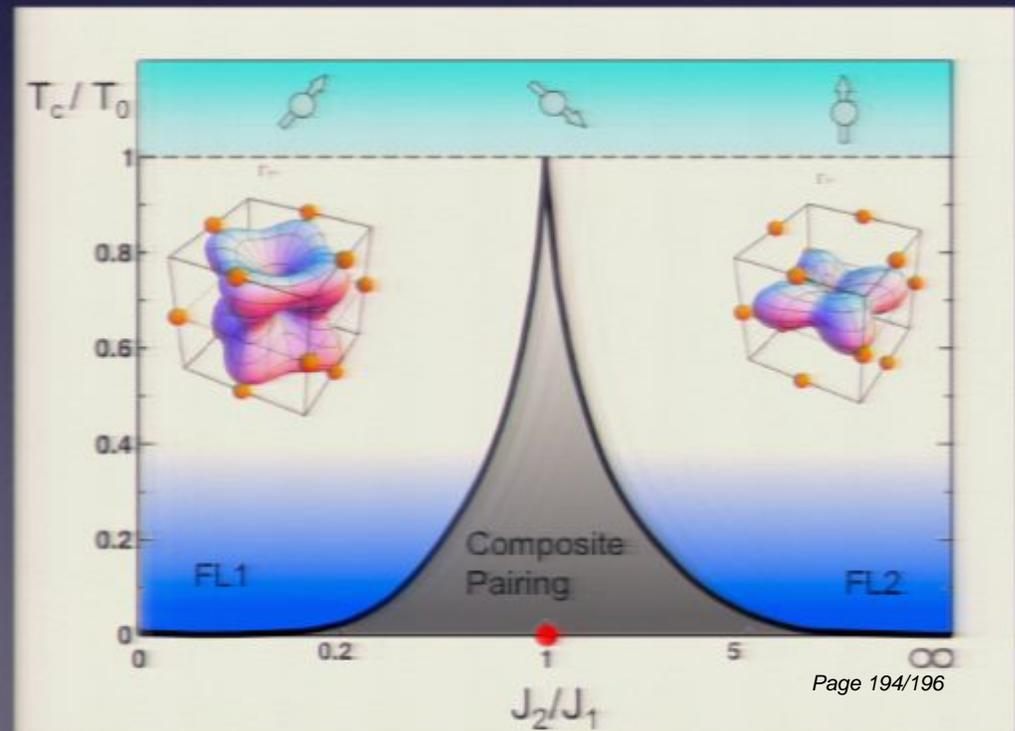
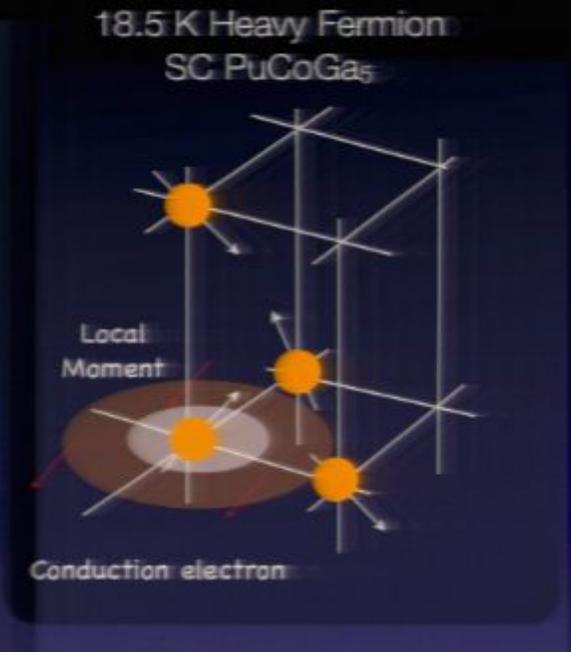
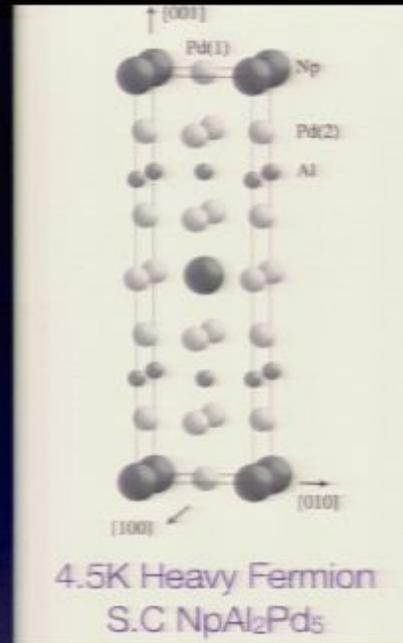
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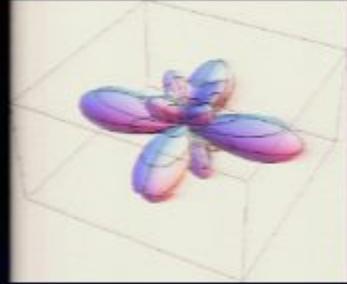
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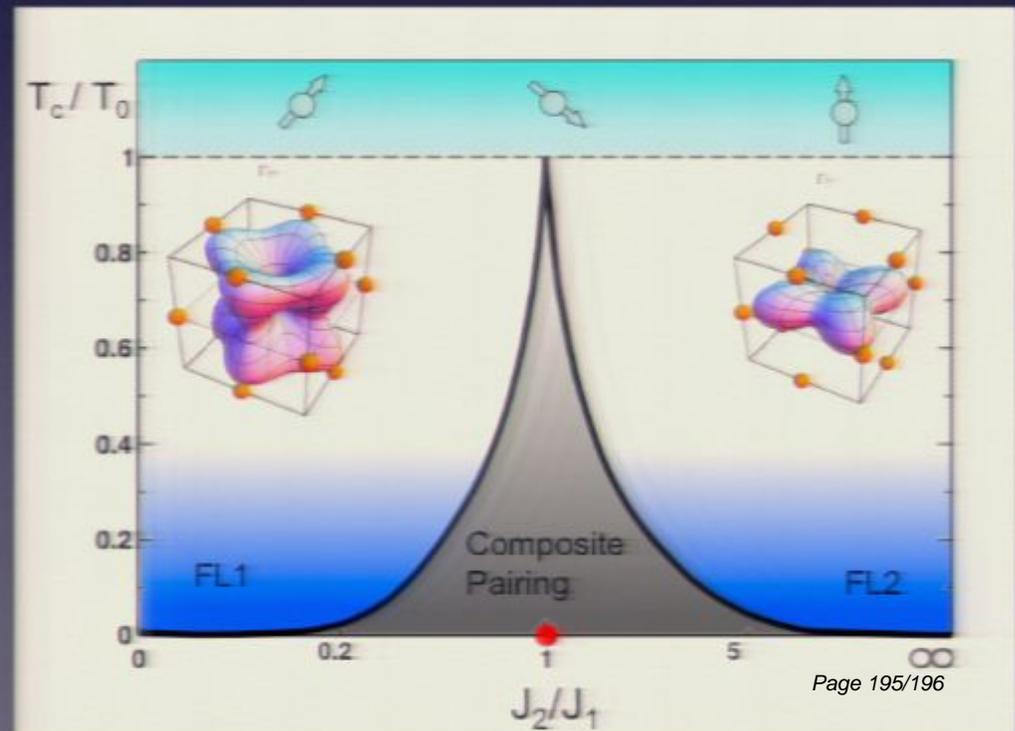
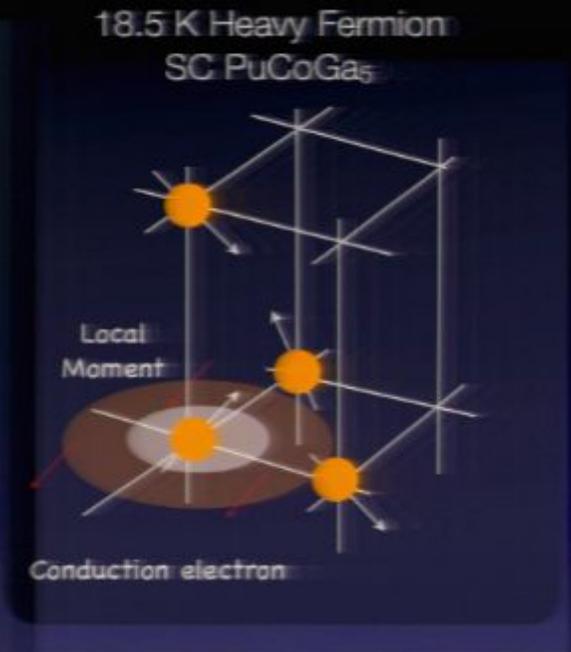
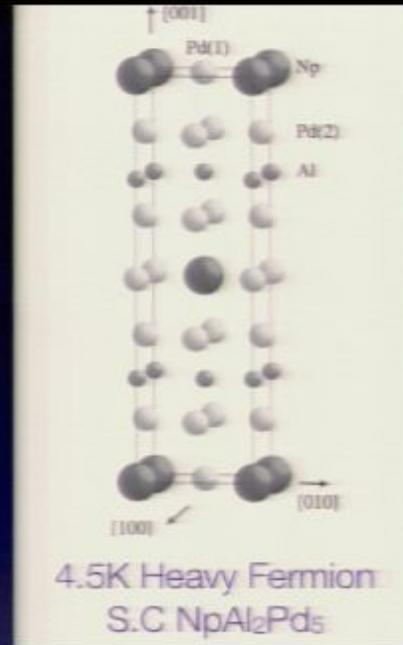
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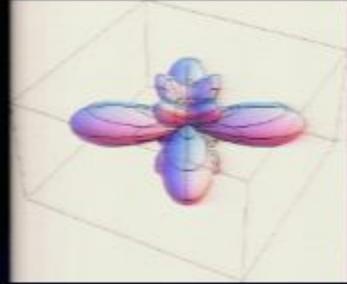
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