

Title: Mini-Course on Mach's Principle - Lecture 3

Date: Feb 25, 2009 10:30 AM

URL: <http://pirsa.org/09020032>

Abstract:

Recall,

$$S_{\text{OPM}} = \int_{\text{OPM}} [T - v]$$

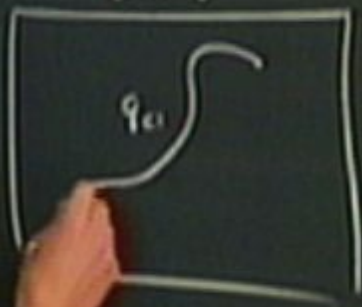
Recall,

$$S_{\text{OPM}} = \int_{\mathcal{O}} d\lambda \left[ \frac{I}{2^0} - \dot{z}^0 v \right] \quad (dt \rightarrow d\lambda \dot{q}^0)$$

Recall,

$$S_{\text{OPM}} = \int_{\text{CS}} d\lambda \left[ \frac{I}{\dot{z}^0} - \dot{z}^0 V \right] \quad (dt \rightarrow d\lambda \dot{z}^0)$$

CS  $\vec{z}, \dot{z}$



$$\dot{z}^0 = \sqrt{\frac{I}{E - V}} \Rightarrow$$

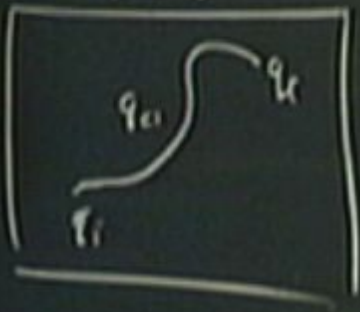


Recall,

$$S_{\text{opt}} = \int d\lambda \left[ \frac{I}{2^0} - \dot{z}^0 V \right]$$

( $dt \rightarrow d\lambda \dot{z}^0$ )

CS  $\vec{z}, z^0$



$$\dot{z}^0 = \sqrt{\frac{I}{E - V}} \Rightarrow$$

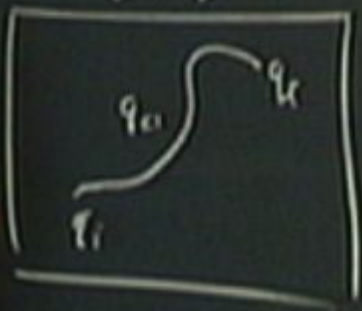
$$z_{i+1} - z_i = \int d\lambda \sqrt{\frac{I}{E - V}}$$

Recall,

$$S_{\text{opt}} = \int d\lambda \left[ \frac{I}{c^2} - \dot{z}^2 v \right]$$

( $dt \rightarrow d\lambda \dot{z}^2$ )

CS  $\vec{z}, \dot{z}$



$$\dot{z}^2 = \sqrt{\frac{I}{E - v}}$$

$\Rightarrow$

$$z_f - z_i = \int d\lambda \sqrt{\frac{I}{E - v}}$$

"length"

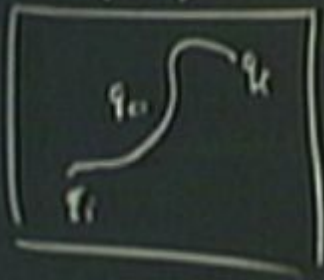


Recall,

$$S_{\text{opt}} = \int d\lambda \left[ \frac{I}{v} - \dot{z} V \right]$$

$$(dt \rightarrow d\lambda \dot{z})$$

CS  $\vec{z}, \dot{z}$



$$\dot{z} = \sqrt{I}$$

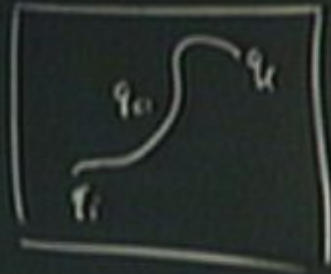


$$z_f - z_i = \int d\lambda \sqrt{\frac{I}{E - V}} \tau$$

$\propto$  "length"

$$S_{\text{opt}} = \int d\lambda \left[ \frac{1}{2} \right]$$

CS  $\vec{q}, q'$



$$q' = \sqrt{\frac{T}{E - v}}$$

$$q' \left( q' = \int d\lambda \sqrt{\frac{T}{E - v}} \right) \approx \ell$$

$E \Rightarrow$  fixed by BC's

$\approx$  "length"

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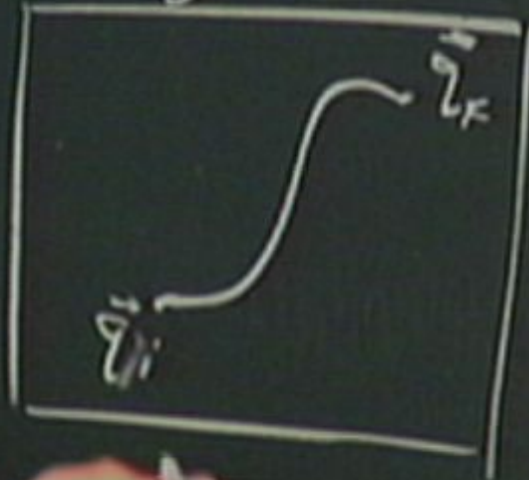
$$S_{\text{DB}} = \int d\lambda \sqrt{T} \sqrt{E - v}$$

CS  $\vec{q}_I$



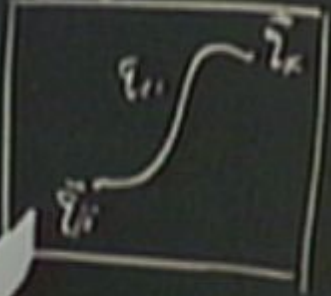
$$S_{\text{JDB}} = \int d\lambda \, 2\sqrt{\epsilon} \sqrt{E - V}$$

CS  $\vec{q}_I$



$$S_{\text{DOB}} = \int d\lambda \sqrt{E - v}$$

CS  $\vec{q}_i$

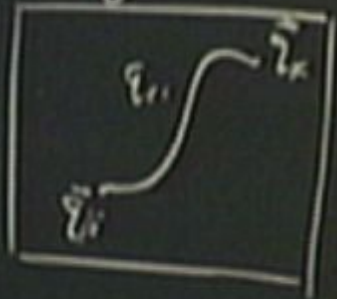


we skilwed  $q_{(1,5m)} \equiv q_{(1,4m)}$



$$S_{\text{DOB}} = \int d\lambda \sqrt{T} \sqrt{E - V}$$

CS  $\vec{q}_i$



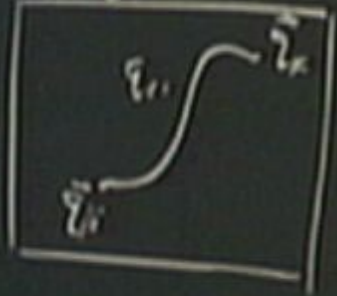
We skilled  $q_{\text{cl, sym}} \equiv q_{\text{cl, para}}$

$$\tau_{\text{opt}} = \int d\lambda \sqrt{\frac{I}{E - V}}$$

$E = \text{param}$

$$S_{\text{DOB}} = \int d\lambda \sqrt{\frac{I}{E-v}}$$

CS  $\vec{q}_i$



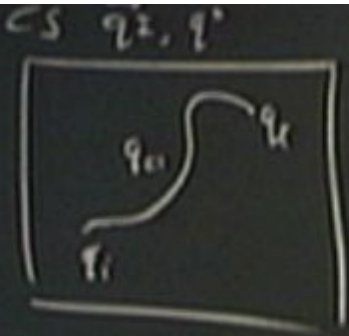
We showed  $q_{(1, \text{long})} \equiv q_{(1, \text{short})}$

$$\tau_{\text{opt}} = \int d\lambda \sqrt{\frac{I}{E-v}}$$

& "length"

$E = \text{param}$





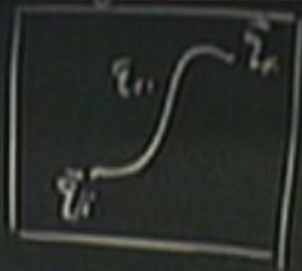
$$\psi^2 = \sqrt{\frac{I}{E-V}} \Rightarrow$$

$$\psi_i - \psi_f = \int d\lambda \sqrt{\frac{I}{E-V}} \tau$$

E  $\Rightarrow$  fixed by BC's

"length"

$$\sum \frac{\hat{p}}{2m} (\hat{q}_i + \hat{p}_i) = 0$$



$$\tau_{\text{eff}} = \int d\lambda \sqrt{\frac{I}{E-V}}$$

$\propto$  length

LUU90  
Bierline



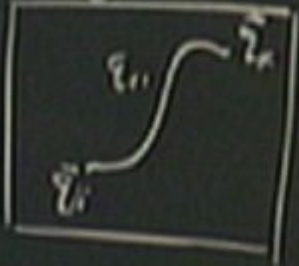
$E \Rightarrow$  fixed by BC's

$\left( \sum \frac{A_i}{2m\hbar} + V(x) + \hat{p}_x \right) \psi = 0$

*length*

$$S_{\text{DB}} = \int d\lambda \sqrt{2T} \sqrt{E - V}$$

CS  $\vec{q}_2$



We skipped  $q_{cl, \text{in}} \approx q_{cl, \text{out}}$

$$\tau_{\text{tth}} = \int d\lambda \sqrt{\frac{\hbar}{E - V}}$$

*length*

$E = \text{param}$

Quantization:

$$\mathcal{H} = \sum_i \frac{\vec{p}_i^2}{2m_i} + V(q_2) - E = 0$$

$$\begin{aligned} \vec{p}_i &\rightarrow \hat{p}_i \\ q_i &\rightarrow \hat{q}_i \end{aligned}$$

Quantization:

$$\hat{H} = \left[ \sum_i \frac{\hat{p}_i^2}{2m_i} + V(\hat{q}_i) - E \right] |\psi\rangle = 0 \quad \text{Time Ind. SE.}$$

$$\begin{aligned} \vec{p}_i &\rightarrow \hat{p}_i \\ \vec{q}_i &\rightarrow \hat{q}_i \end{aligned}$$



Quantization:

$$\hat{H} = \left[ \sum_i \frac{\hat{p}_i^2}{2m_i} + V(\hat{q}_i) - E \right] \psi = 0 \quad \text{Time Ind. SE.}$$

$$\begin{aligned} \vec{p}_i &\rightarrow \hat{p}_i \\ \vec{q}_i &\rightarrow \hat{q}_i \end{aligned}$$

Quantization:

$$\hat{H} = \left[ \sum_i \frac{\hat{p}_i^2}{2m_i} + V(\hat{q}_i) - E \right] \psi = 0 \quad \text{Time Ind. SE.}$$

$$\begin{aligned} \vec{p}_i &\rightarrow \hat{p}_i \\ \vec{q}_i &\rightarrow \hat{q}_i \end{aligned}$$

Problem of time!

# Disappearance of Time:

## 1. Path Integral



Disappearance of Time:

1. Path Integral

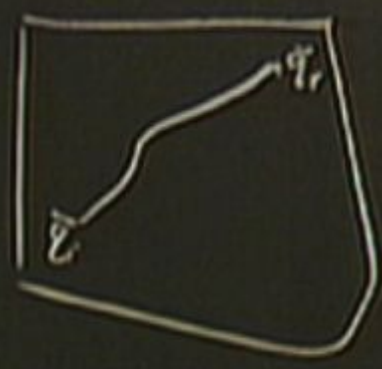
SKB

PPM

Disappearance of Time:

1. Path Integral

SKB



PPM



1. Path Integral

SBS

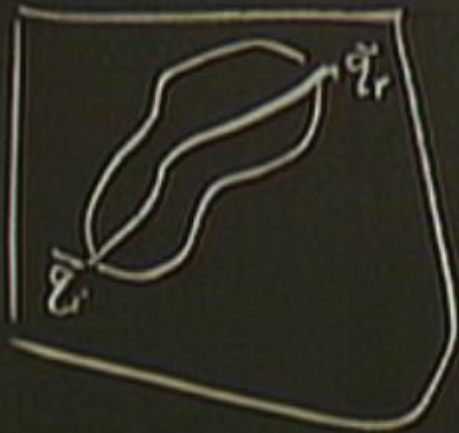
PPM



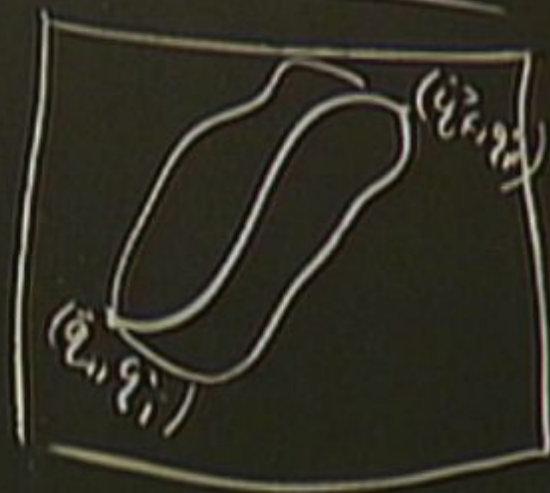


# 1. Path Integral

SBS



PPM



$\mathbb{R}^n$

$\mathbb{R}^n$

$\int$  over all paths  
 $\tau = q_i^* - q_i$

J.R.R.

P.P.M.

$\sum$  over all paths  
 $\tau = q_i - q_k$

Superposition of  $E$ 's



$\rightarrow R, R$

RRM

$\sum$  over all paths

$\sum$  over all paths,  
 $\tau = q_i - q_k$

Superposition of  $\tau$ 's

RRR

$\sum$  over all paths

$\Rightarrow$  average over all times

RRR

$\sum$  over all paths  
 $\tau = q_i - q_f$

Superposition of E's



RRR

$\Sigma$  over all paths

$\Rightarrow$  average over all times

check axiu

RRR

$\Sigma$  over all paths  
 $\tau = q_i - q_j$

Superposition of  $E$ 's

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RRR

$\Sigma$  over all paths

$\Rightarrow$  average over all times

check rxiv

RRR

$\Sigma$  over all paths  
 $\tau = q_i - q_s$

Superposition of E's



JRB

$\Sigma$  over all paths

$\Rightarrow$  Superposition of times

check axiu

PPM

$\Sigma$  over all paths  
 $\tau = q_i - q_s$

Superposition of  $E$ 's

JR B

PBM

$\int$  over all paths

$\int$  over all paths  
 $\tau = q_i - q_f$

Superposition of times

Superposition of  $E$ 's

check axiu

Stationary Phase: approx.  $\int D e^{iS[x]}$   
 $\approx e^{iS[x_{cl}]} / \sqrt{\det \dots}$



→ R.B.

$\Sigma$  over all paths

⇒ Superposition of times

Check axiu

Stationary Phase: approx  $\int p e^{iS}$

$\approx e^{iS_{min}} / \sqrt{\dots}$

⇒ Yep it's good!

P.B.17

$\Sigma$  over all paths  
 $\tau = q_i - q_f$

Superposition of E's

Quantization:

$$\hat{H} = \left[ \sum_i \frac{\hat{p}_i^2}{2m_i} + V(\hat{q}_i) - \textcircled{E} \right] \psi = 0$$

Time Ind. SE //

$$\begin{aligned} \vec{p}_i &\rightarrow \hat{p}_i \\ \vec{q}_i &\rightarrow \hat{q}_i \end{aligned}$$

Problem of time!

Quantization:

$$\hat{H} = \left[ \sum_i \frac{\hat{p}_i^2}{2m_i} + V(\hat{q}_i) - \textcircled{E} \right] \psi = 0 \quad \text{Time Ind. SE.}$$

$$\vec{p}_i \rightarrow \hat{p}_i$$

$$\vec{q}_i \rightarrow \hat{q}_i$$

Problem of time!



## Quantization

$$\hat{H} = \left[ \sum_i \frac{\hat{p}_i^2}{2m_i} + V(\hat{q}_i) - E \right] \psi = 0 \quad \text{Time Ind. SE.}$$

$$\begin{aligned} \vec{p}_i &\rightarrow \hat{p}_i \\ \vec{q}_i &\rightarrow \hat{q}_i \end{aligned}$$

Problem of time

check axiu

Stationary Phase: approx.  $\int p_2 e^{iS_2}$

$\Rightarrow$   $\int e^{iS_2} \frac{1}{q_2}$   
 $\Rightarrow$   $\int e^{iS_2} \frac{1}{q_2}$

K.K. { "heavy" dot  $\Rightarrow$  give a time  
"light" dot  $\Rightarrow$  evolve  $q_m$  according to this time.

$\Rightarrow$   $\int_{\text{path}} \vec{v} \cdot d\vec{r}$  !

K.K. { "heavy" dot  $\Rightarrow$  give a time  
"light" dot  $\Rightarrow$  evolve qm according to this time.

Robert Brout a



Rep. Inu.

CS



1<sup>st</sup> Class constraints

CAUTION  
DO NOT TOUCH THE BOARD  
OR THE CHALK  
OR THE MARKERS  
OR THE ERASER  
OR THE WIPER  
OR THE DUST  
OR THE BOARD  
OR THE BOARD

Rep. Inv.

CS

Gauge Theory



1<sup>st</sup> Class constraints



Rep Inv.

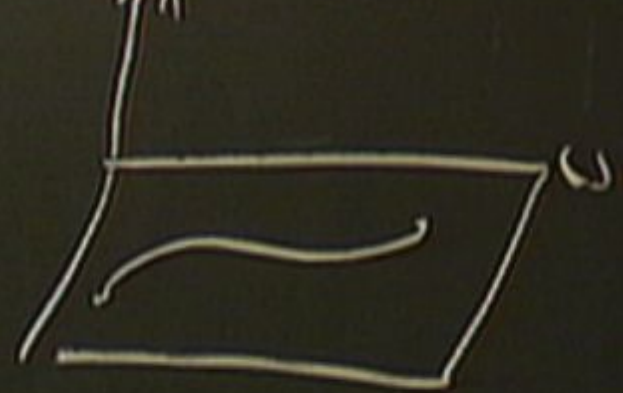
CS

Change Theory



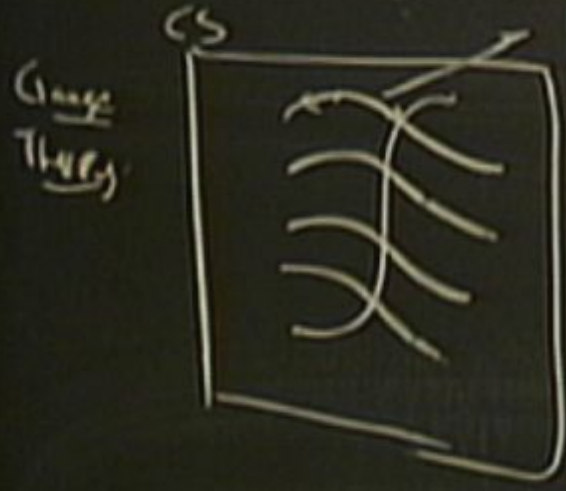
Class constraints

Rep T Inv.





Rep Invar.



1<sup>st</sup> Class constraints

Rep T Inv.



Rep Invar.

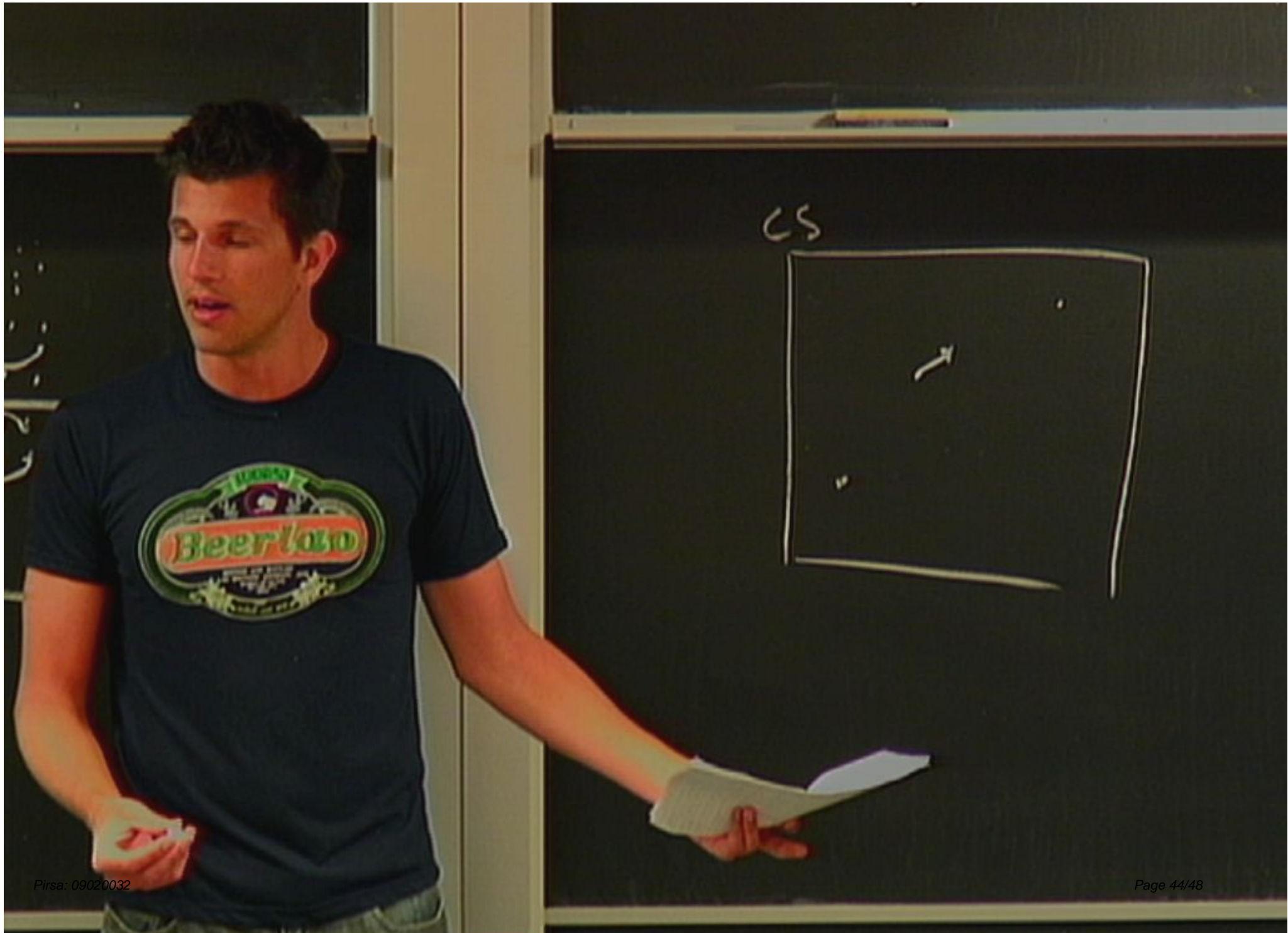
Gauge Theory



1<sup>st</sup> Class constraints

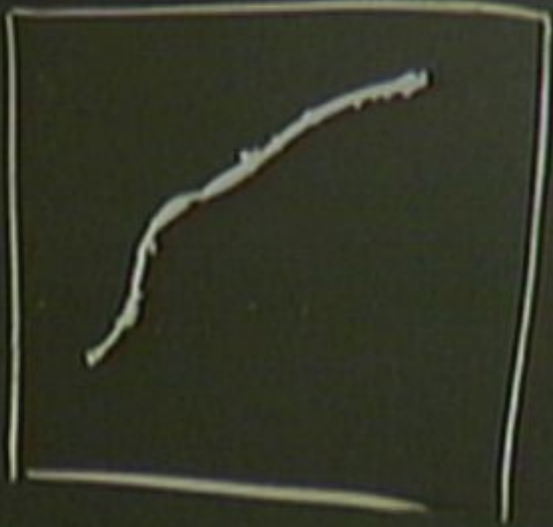
Rep Inv.





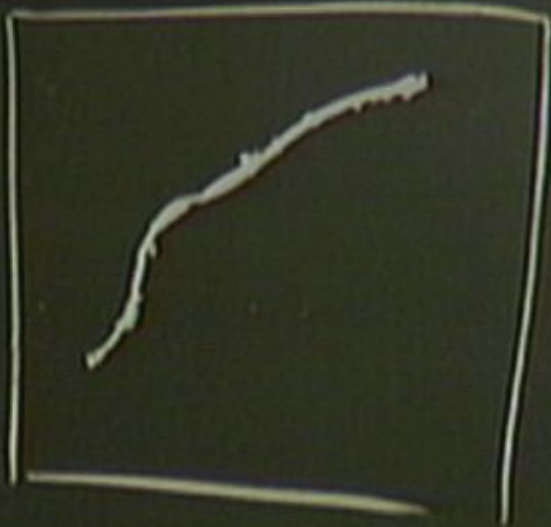


CS



History  $\equiv$  physical state

CS



History  $\equiv$  physical state

CS



History  $\equiv$  physical state

Barhou d Foster



CS



History  $\equiv$  physical state

Barlow & Foster

Kuchan