

Title: 2+1dimensional gauge gravity duality

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Abstract: I discuss our recent investigations into 2+1 dim Chern-Simons theories with gravity duals that have reduced supersymmetry. Many new phenomena such as fractional statistics arise in 2+1 dim field theory that make this duality interesting and subtle. I focus on our work involving an example of such a duality with minimal supersymmetry and propose a field theoretic dual for a long known vacuum of gauged supergravity on AdS<sub>4</sub>. I also argue that 2+1 dim duality might present a favorable landscape for constructing non-supersymmetric conformal fixed points at large but finite N.

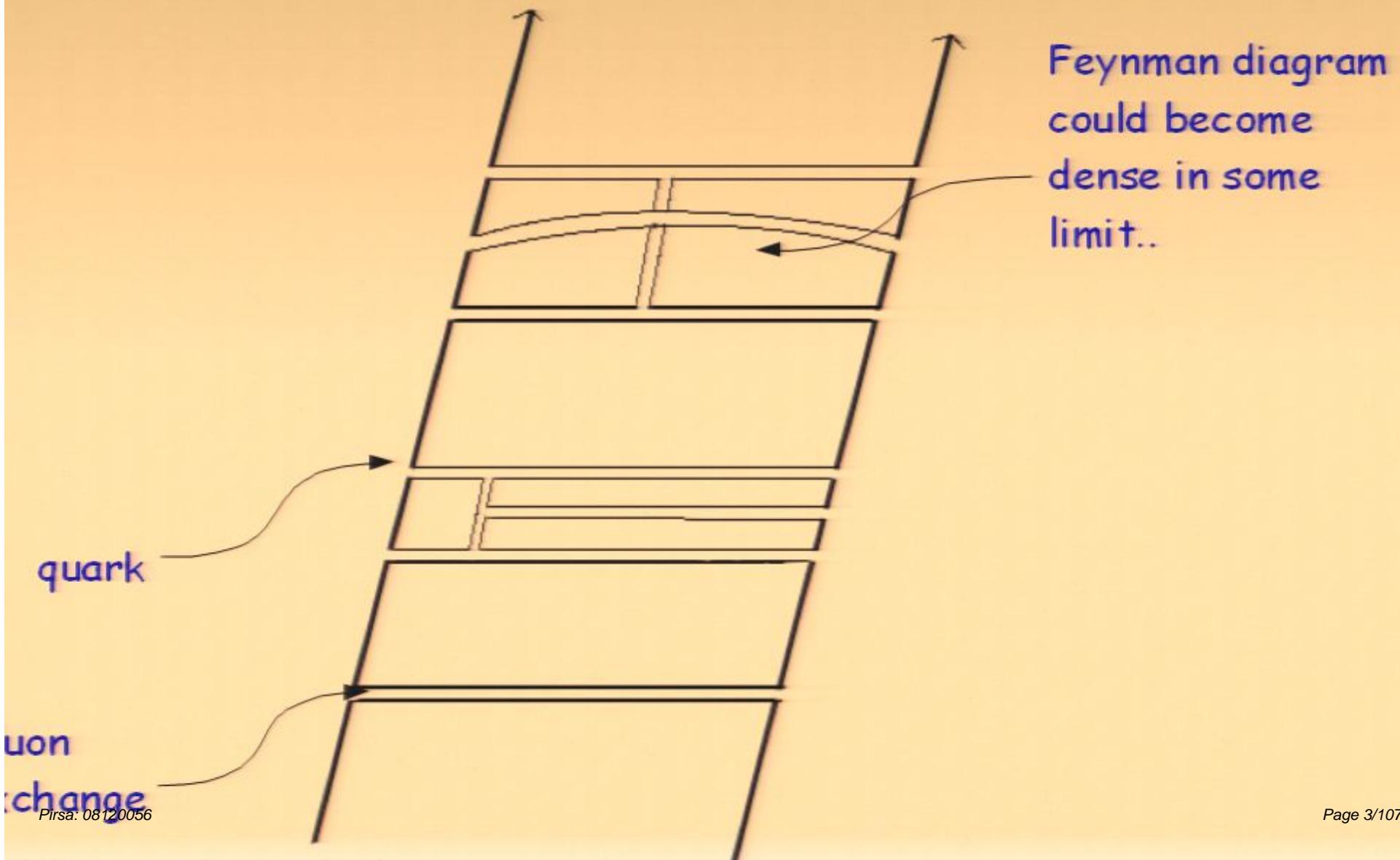
# **Gauge-Gravity duality in 2+1 dimensions**

**Arvind Murugan  
Princeton University**

Work done with I.Klebanov, T.Klose arXiv:0809.3773  
I.Klebanov (in progress)

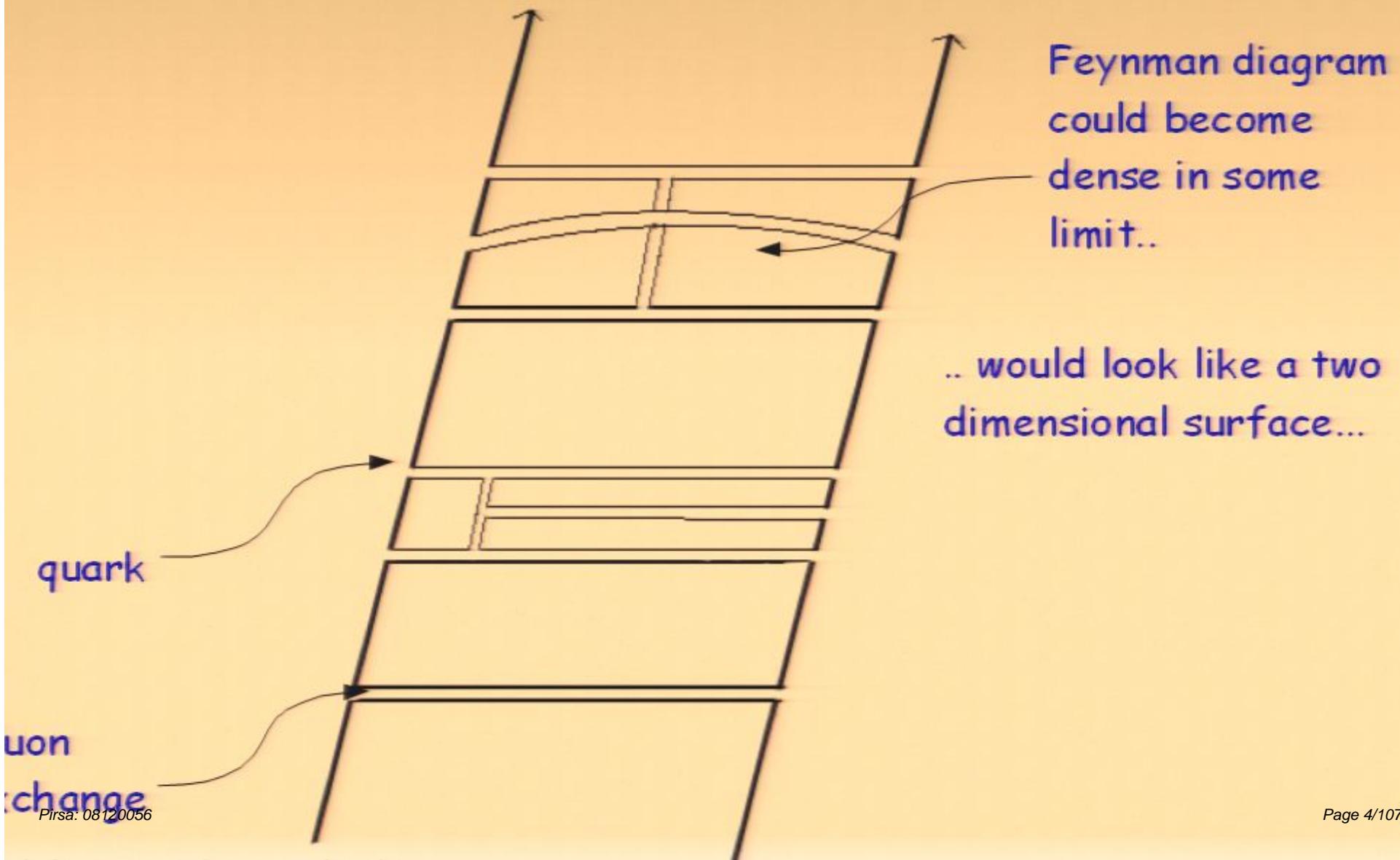
[t Hooft 1974]

# Gauge Gravity duality - origins



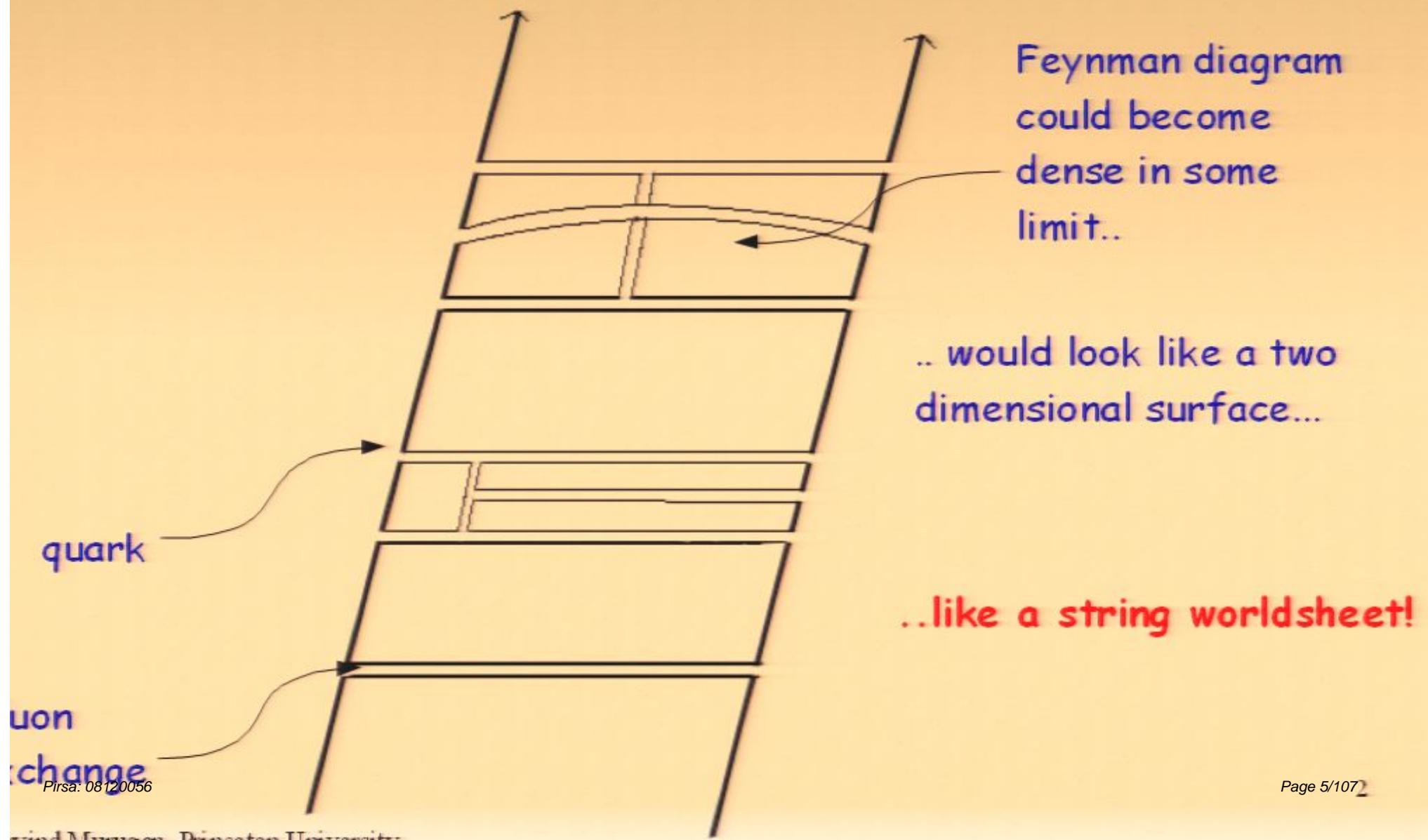
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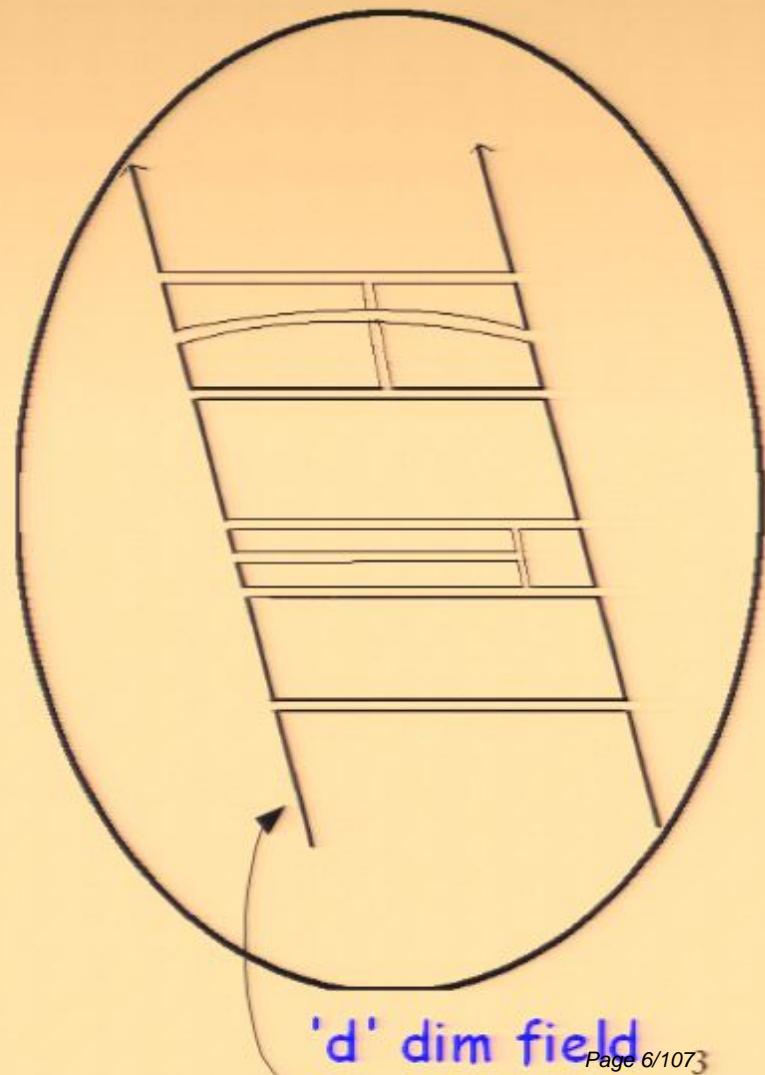
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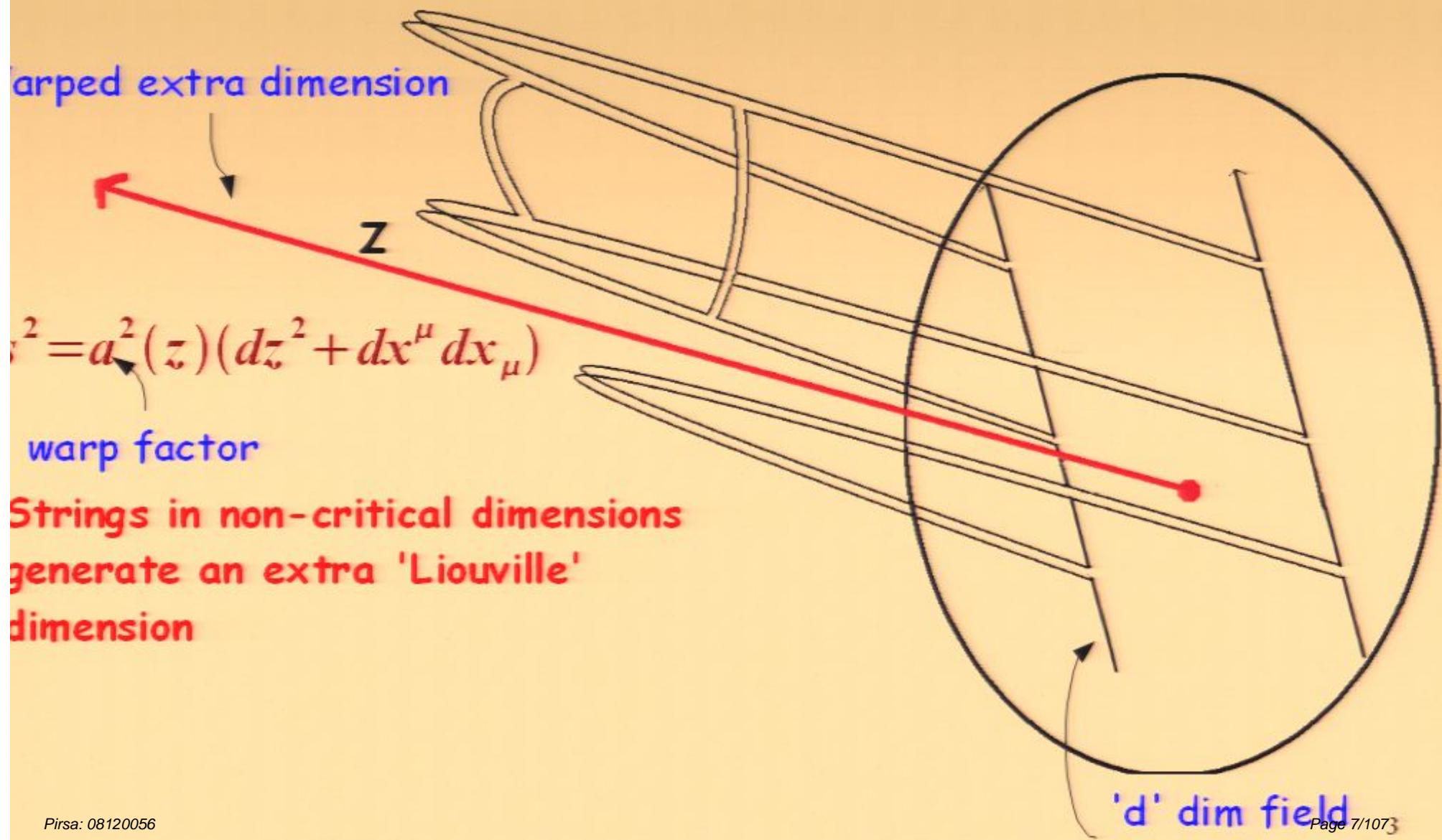
[Polyakov 1981]

# Gauge Gravity duality - origins

Strings in non-critical dimensions  
generate an extra 'Liouville'  
dimension

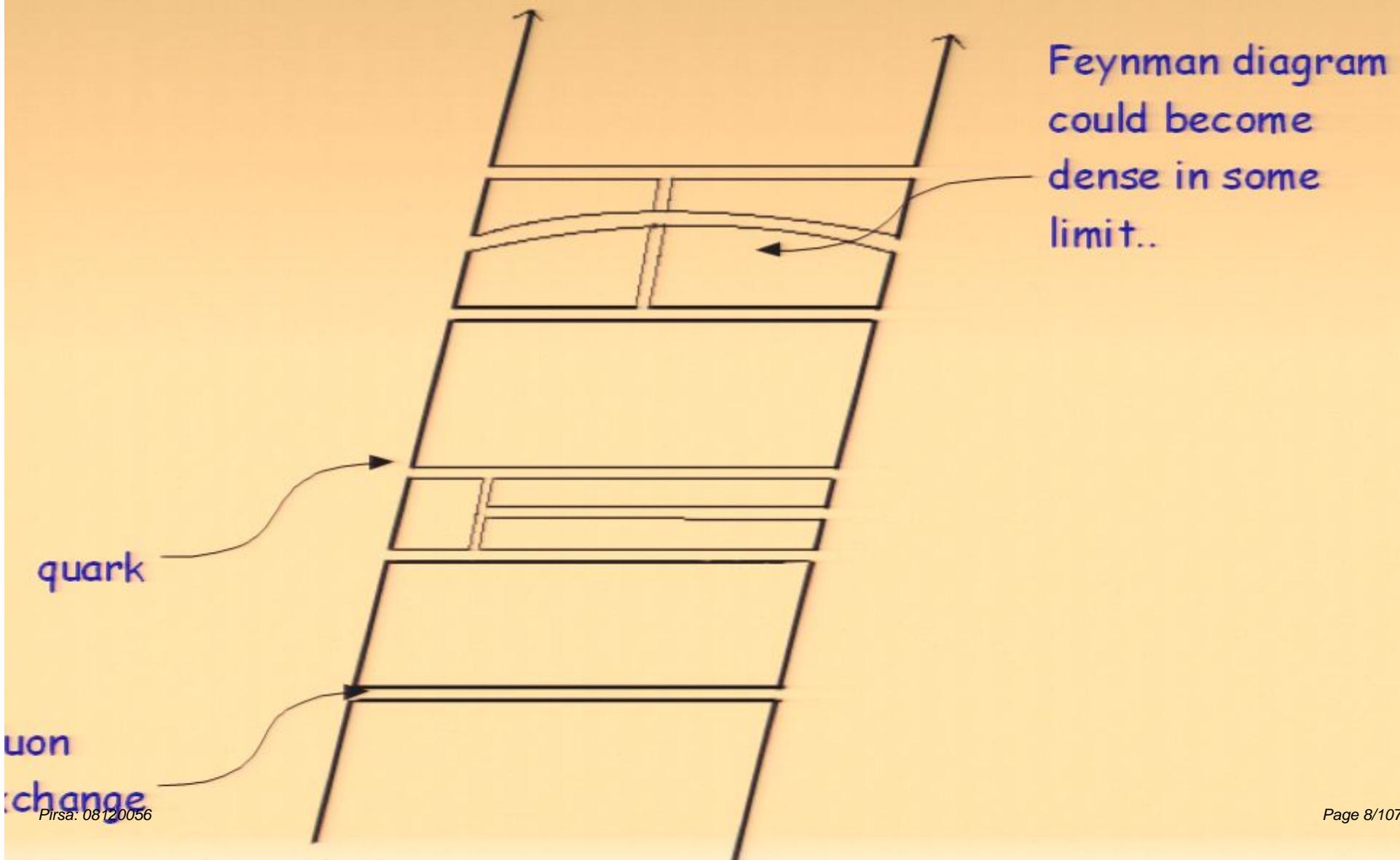


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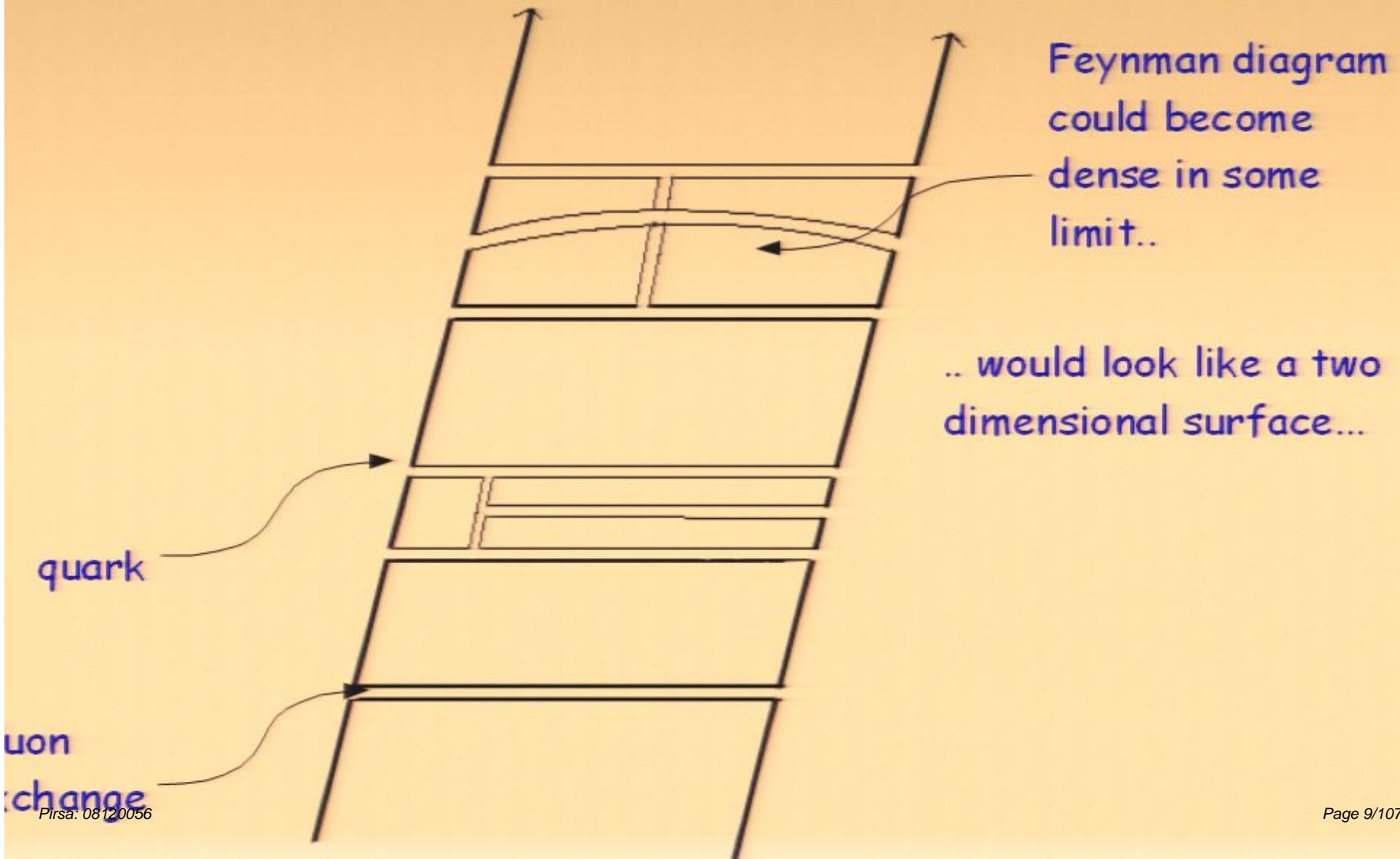
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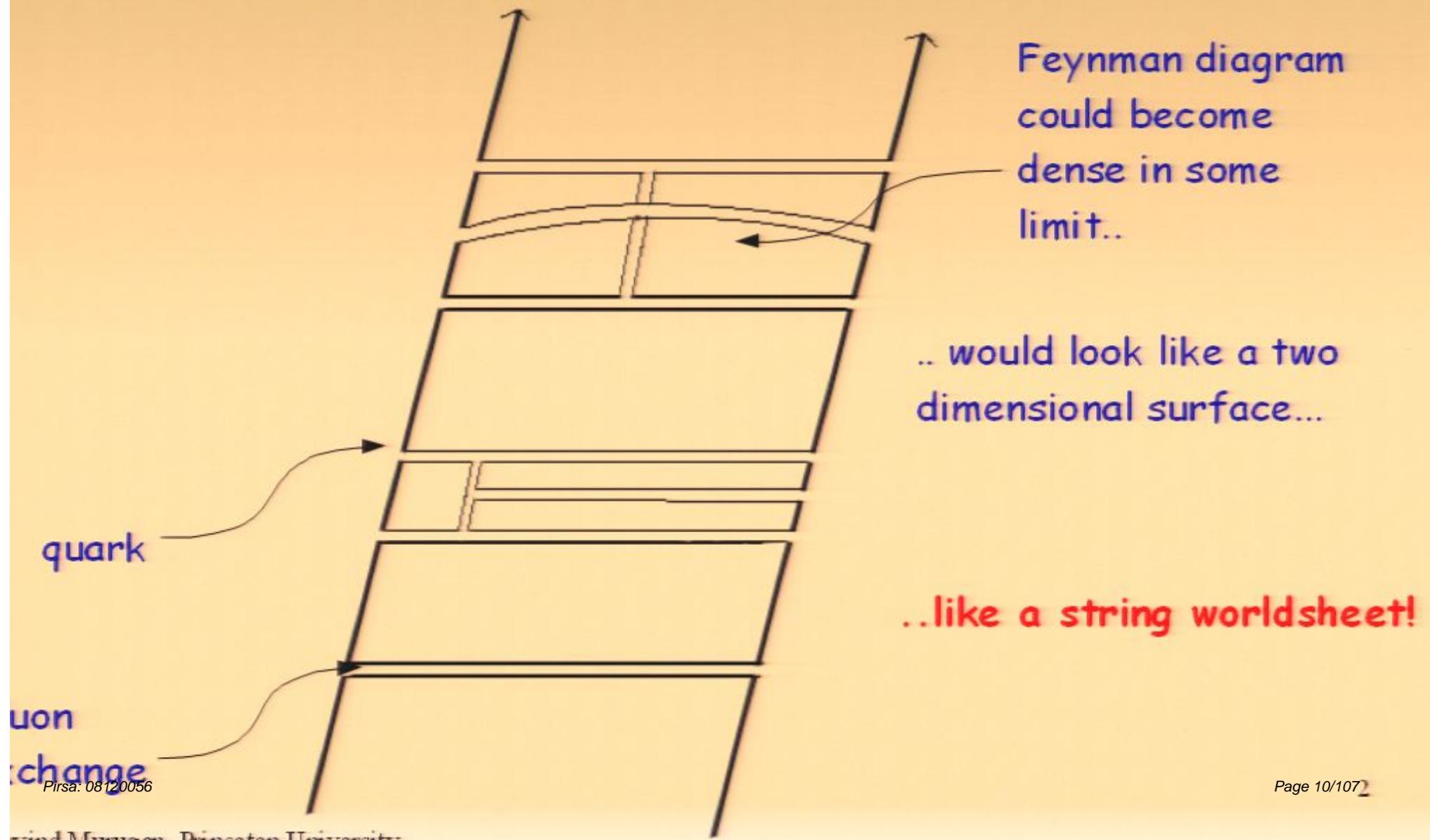
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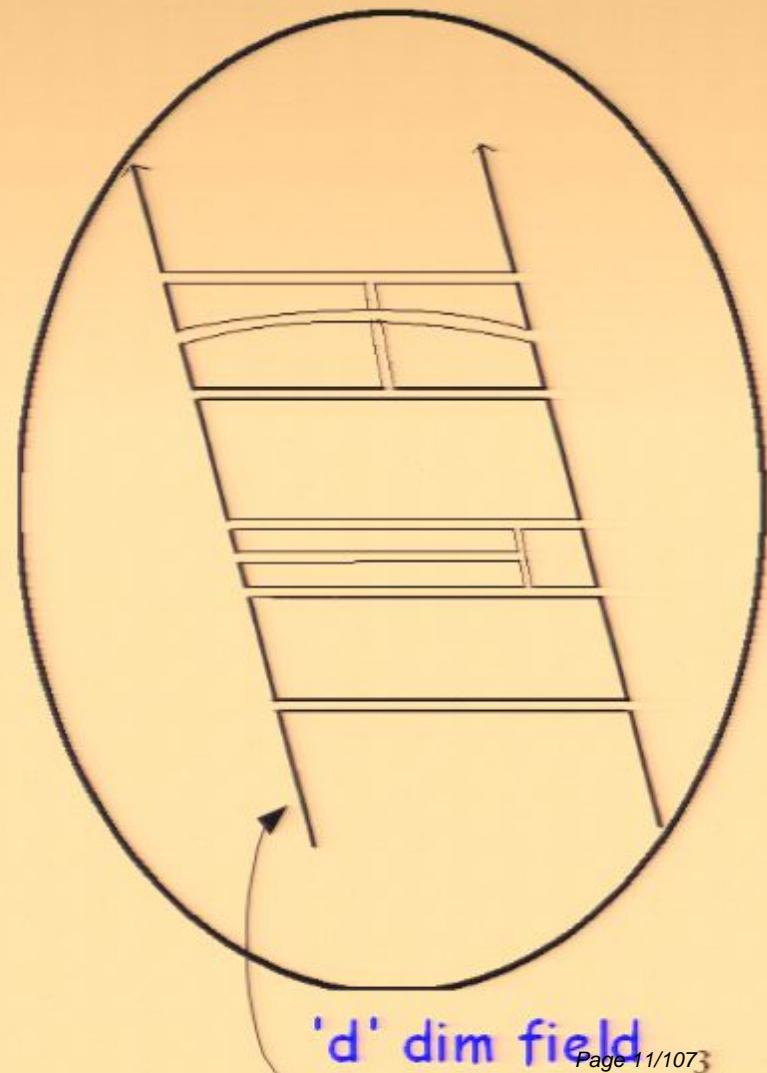
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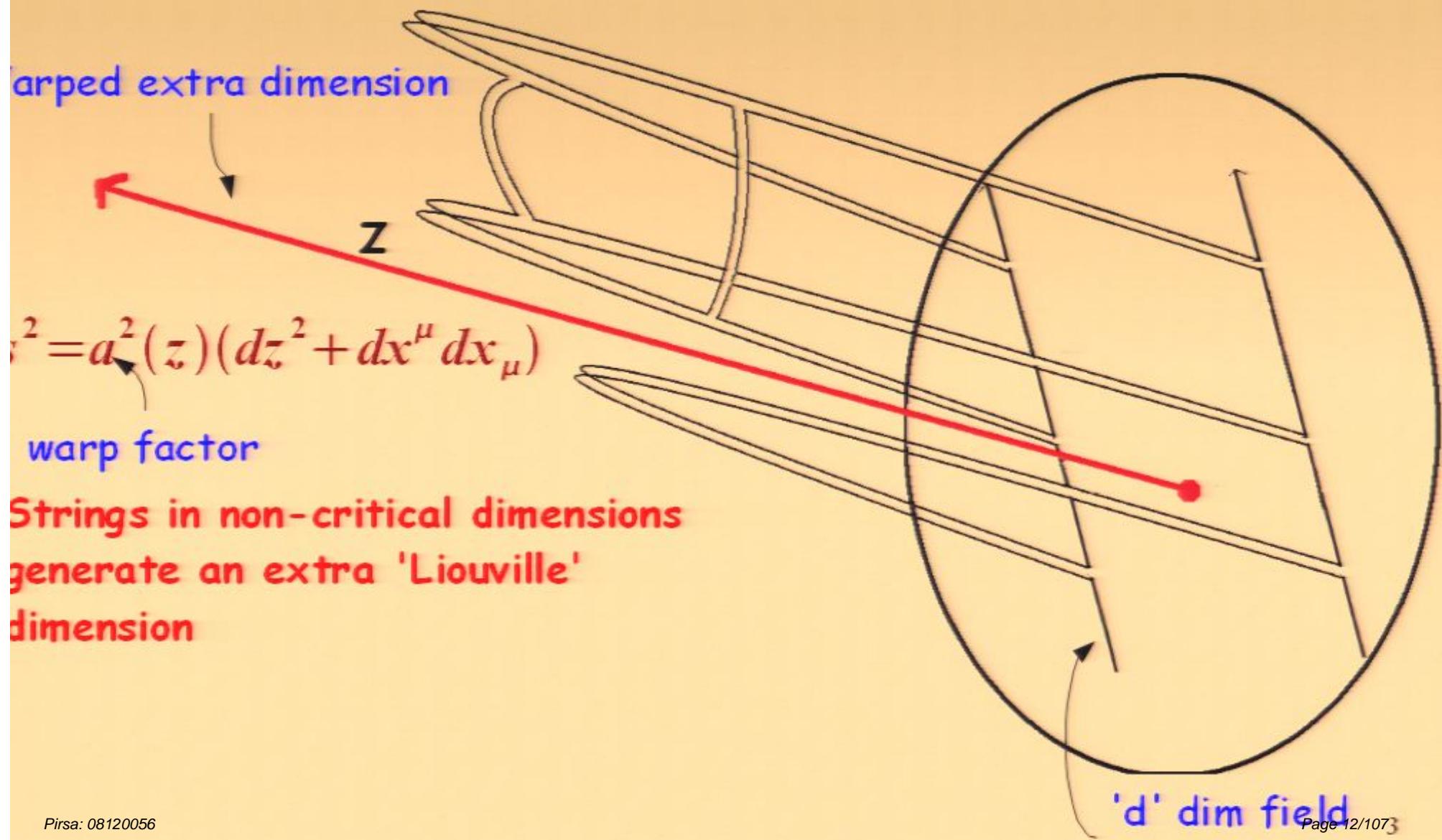
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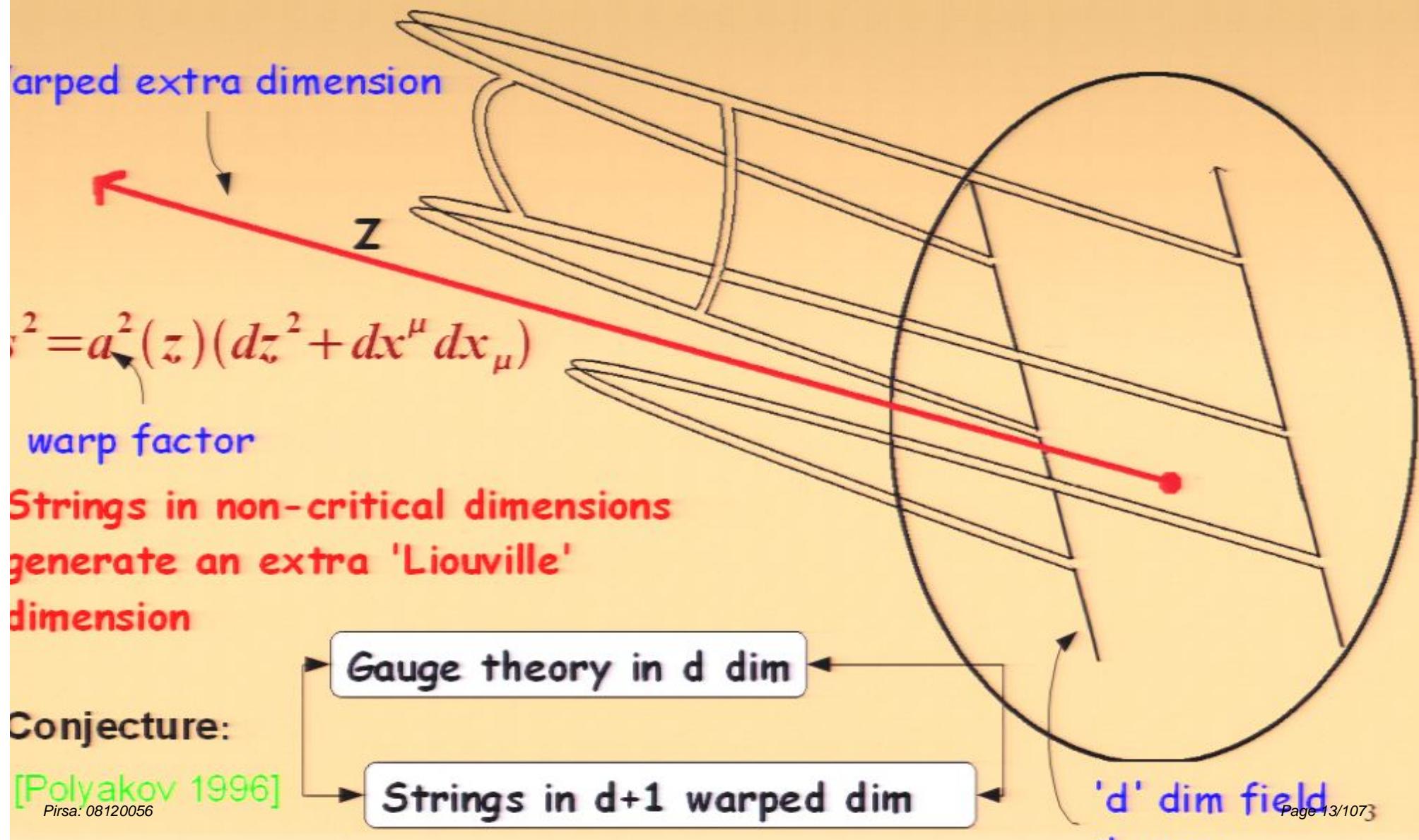
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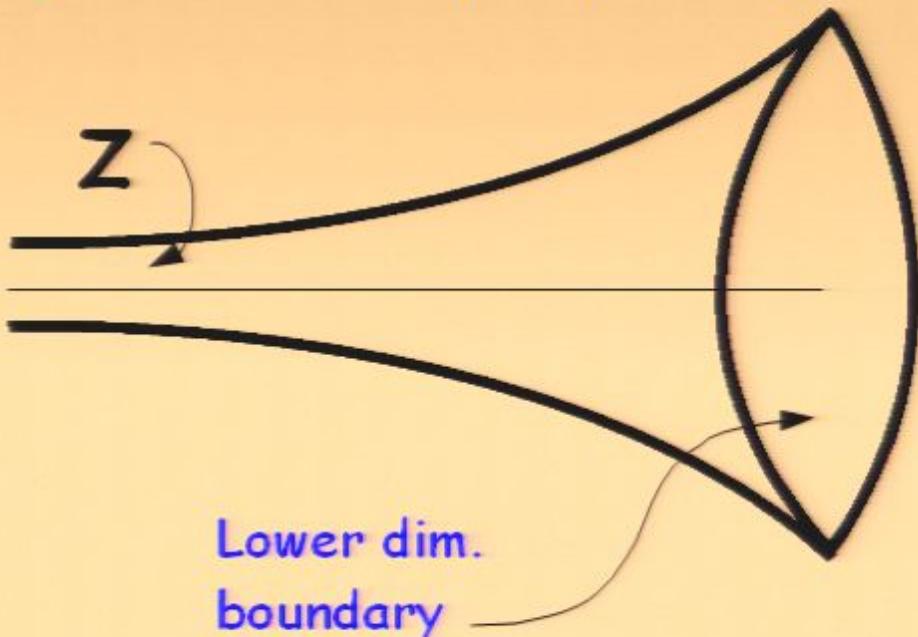
# Gauge Gravity duality - origins



# AdS / CFT duality

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Earlier ideas realized concretely  
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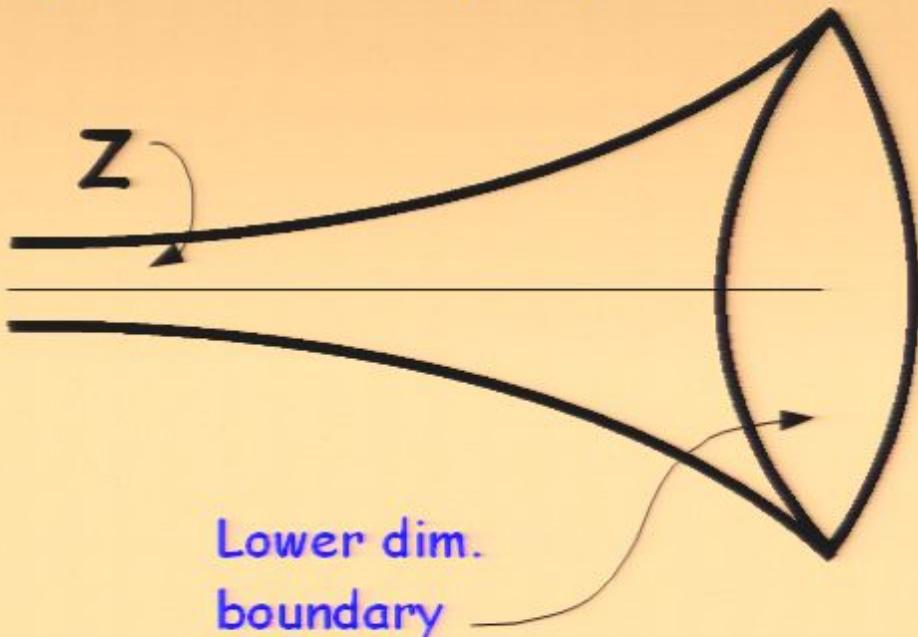
Anti de Sitter space

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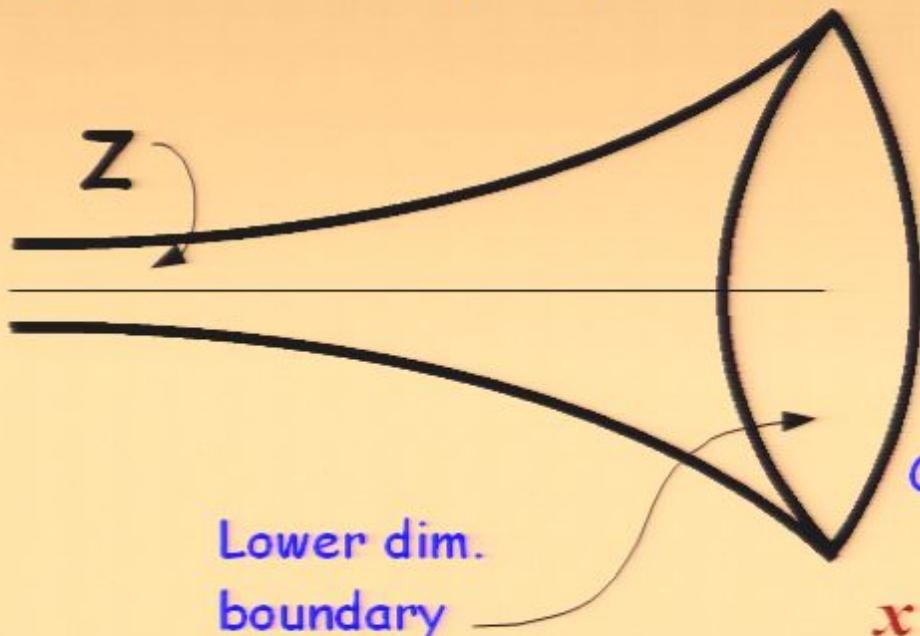
$$a^2(z) = \frac{1}{z}$$

Compare to  
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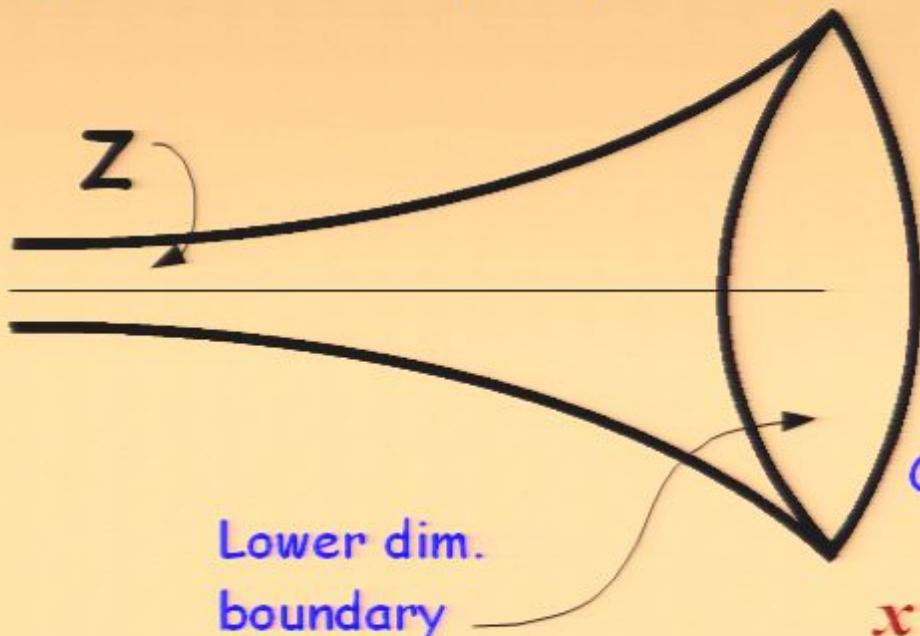
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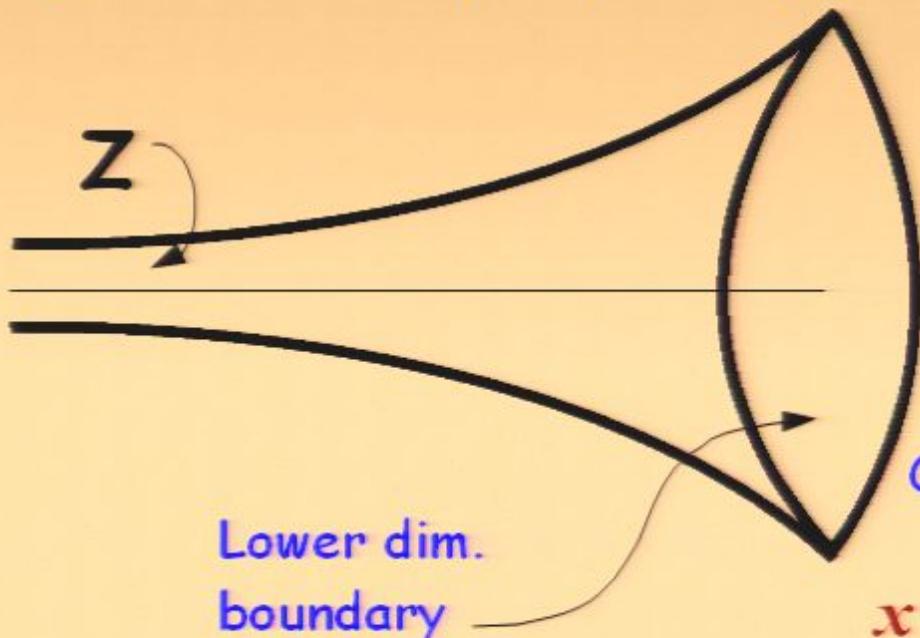
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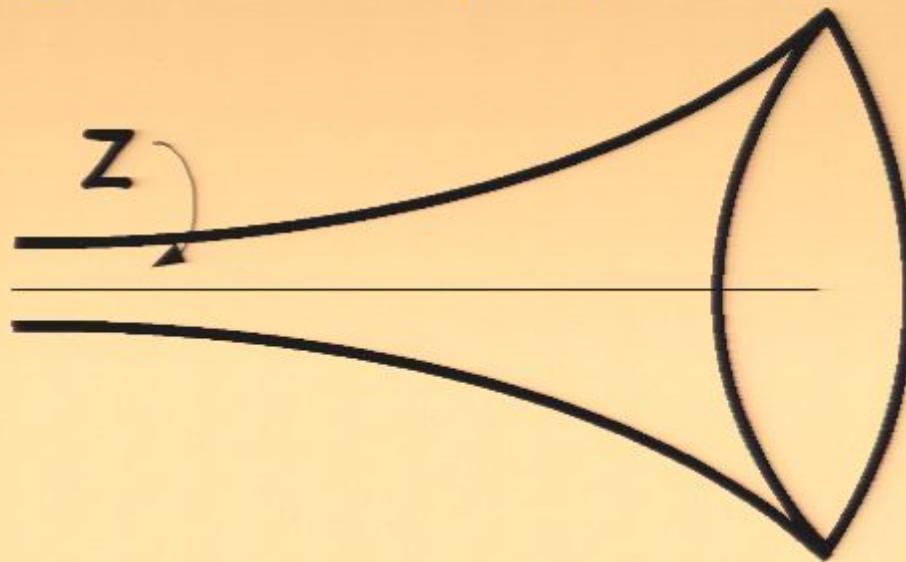
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Introduces length scale  
Non-trivial RG flow

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$$AdS_4 \times X^7$$



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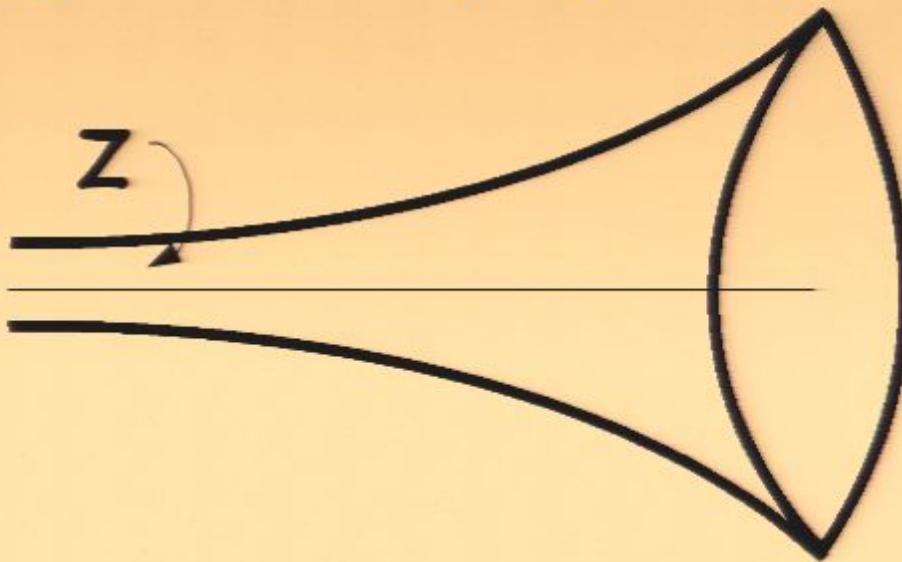
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- Gauge symmetry
- Global symmetry
- Supersymmetry
- Matter content

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# Maximally Supersymmetric Duals

$$AdS_4 \times S^7$$

What is the 2+1 field theory dual?

[Aharony, Bergman,  
Jafferis, Maldacena 2008]

Most (super)  
symmetric  
space

# Maximally Supersymmetric Duals

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Gauge group:  $U(N) \times U(N)$

gauge fields  
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[Warner 1983]

.. but the potential has 5 other extrema (with some min. symmetry).

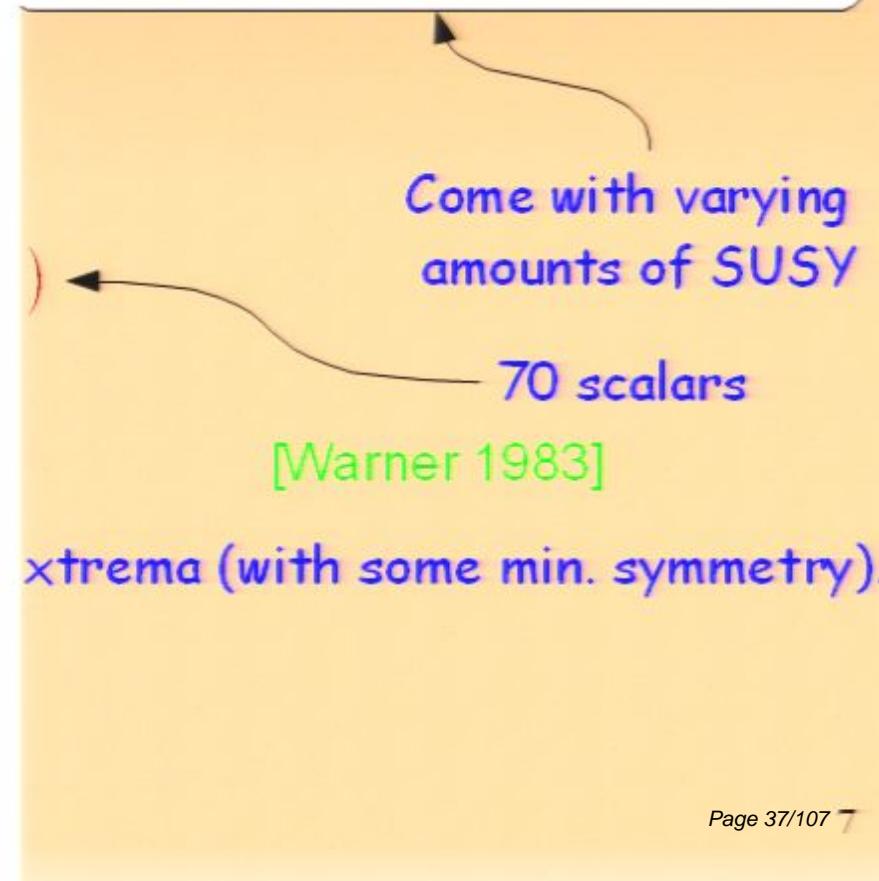
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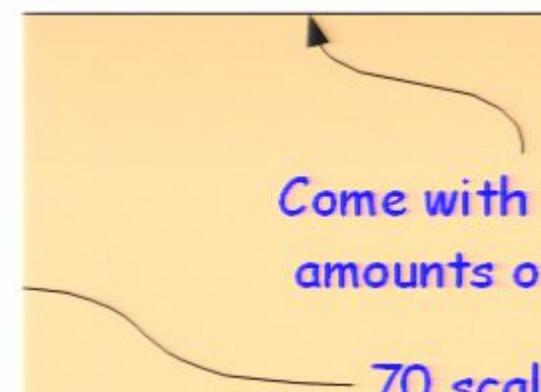
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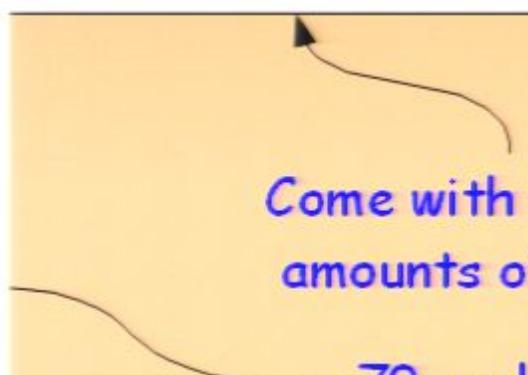
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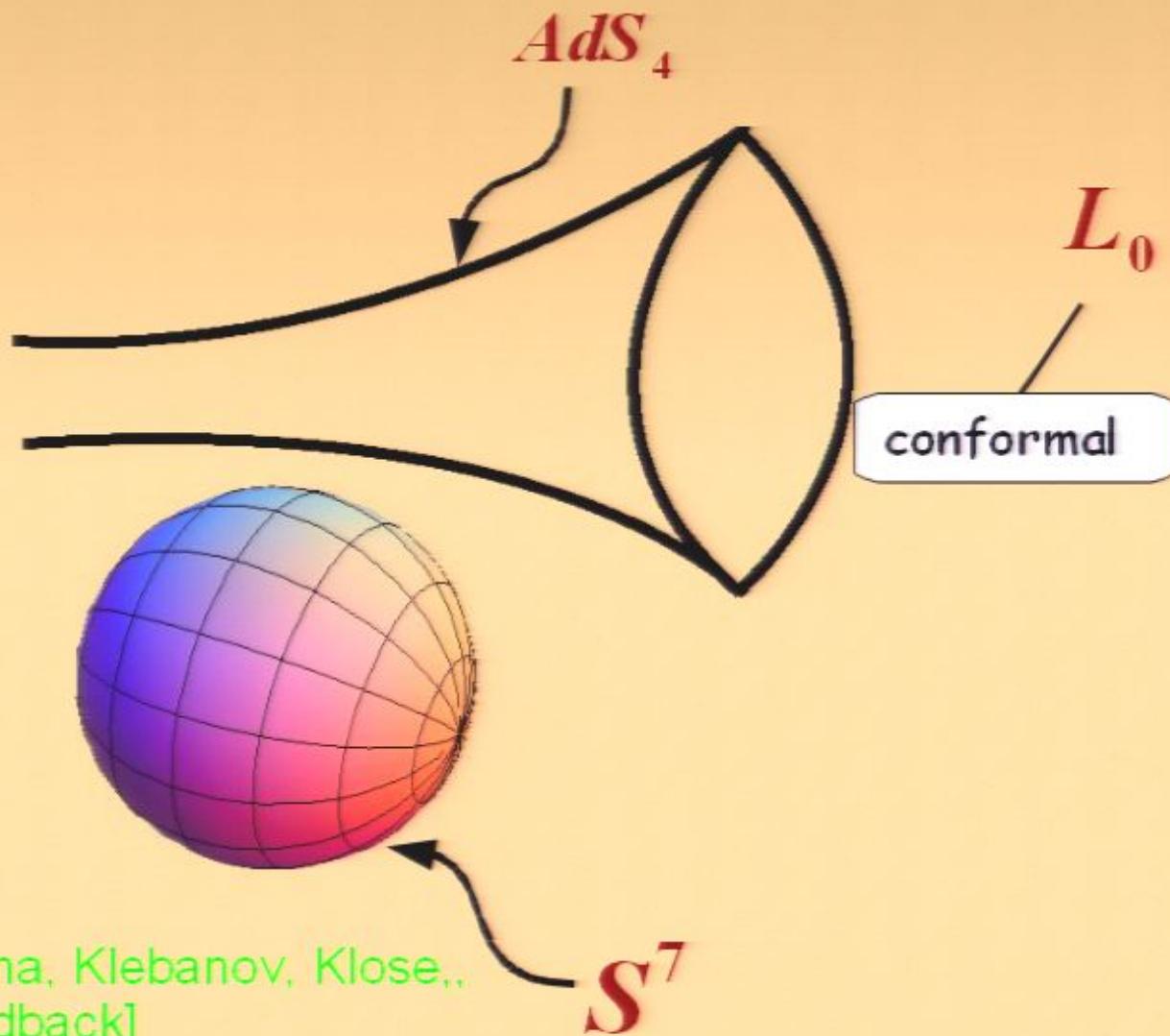
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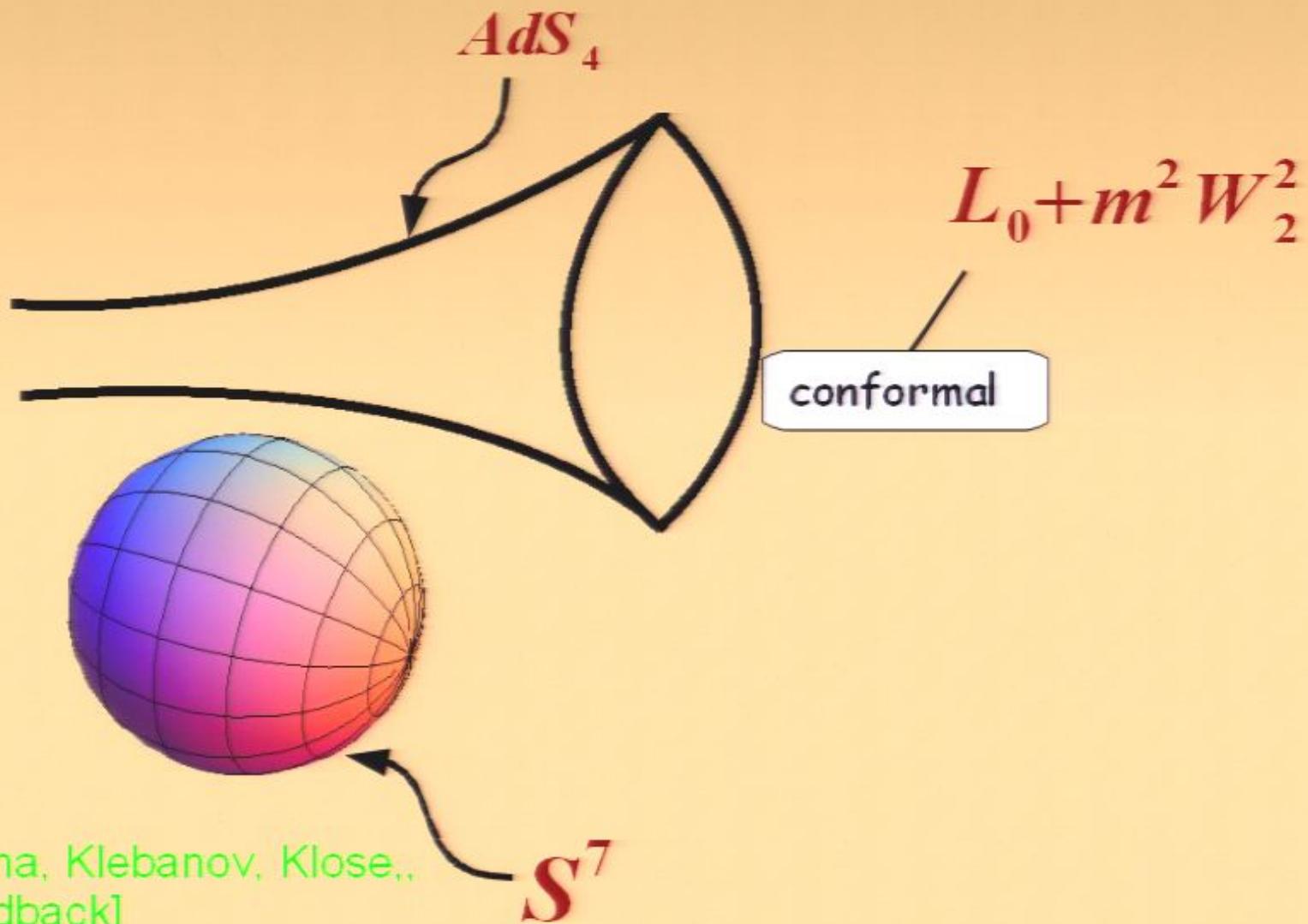
What is the  
gauge dual of  
this low SUSY  
vacuum?

# Adding a mass term



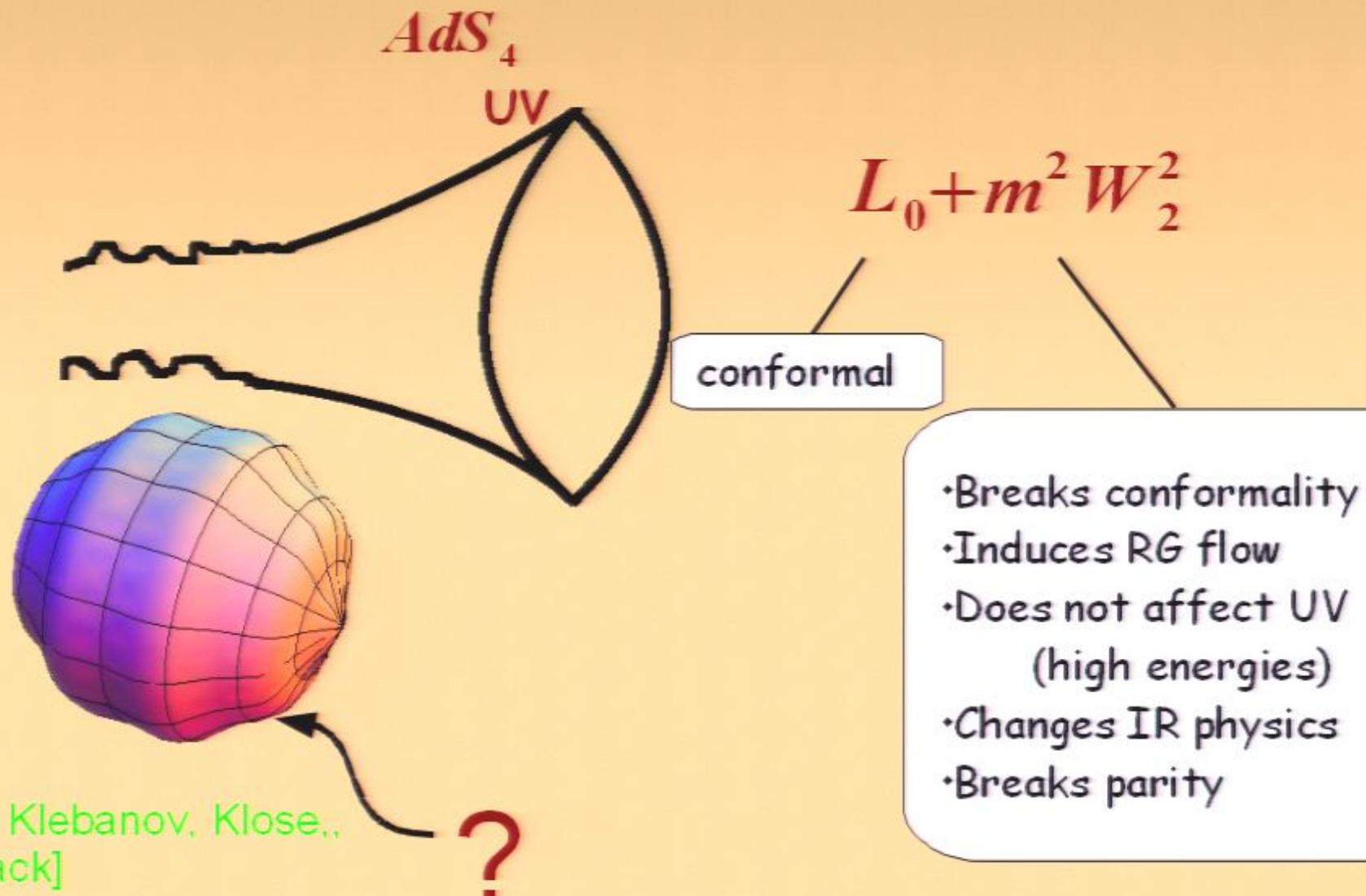
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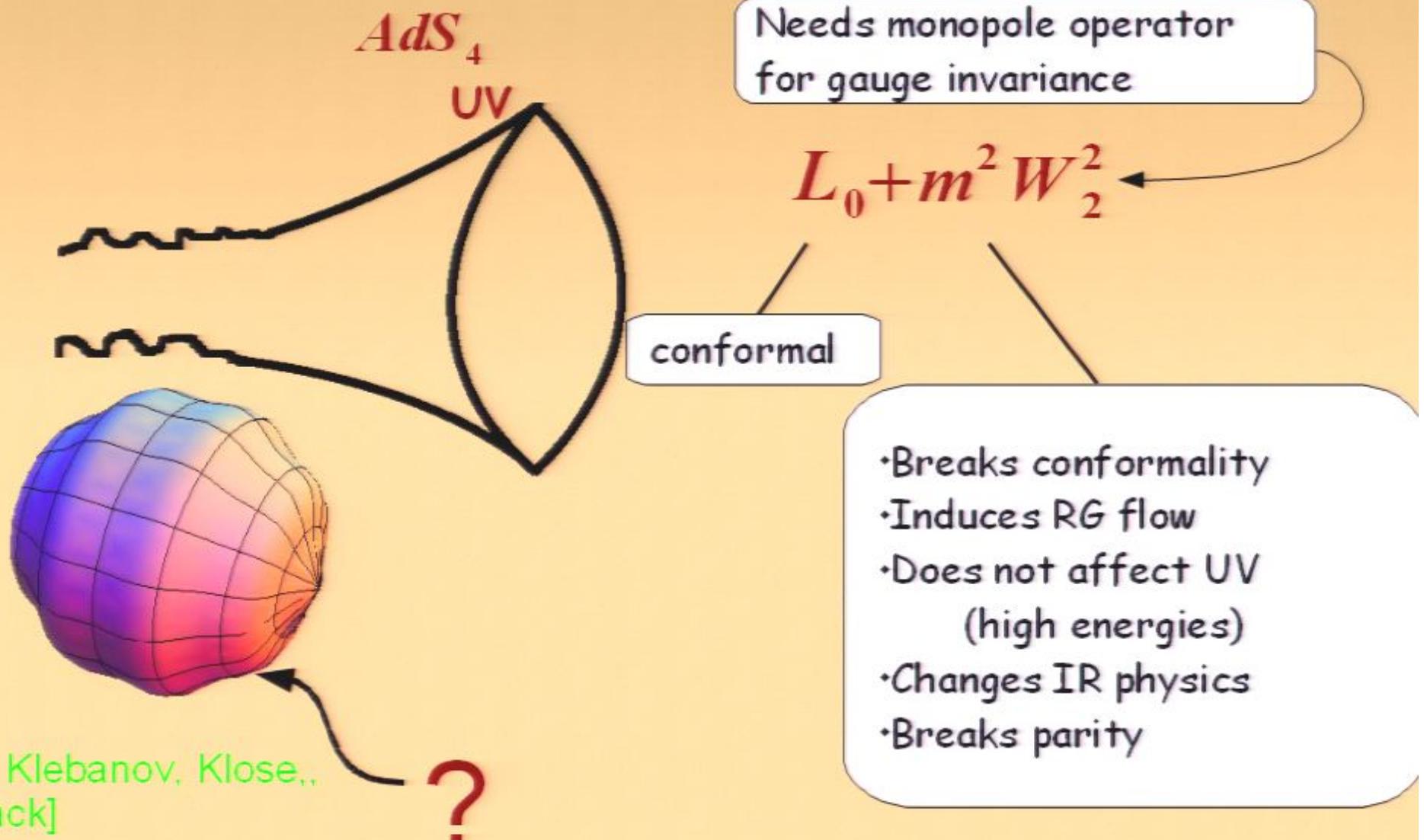


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# Field theory analysis

$$W \sim \text{Tr}(Z_1 W_1 Z_2 W_2 - Z_1 W_2 Z_2 W_1) + m W_2^2$$

Write in terms of  $Z$ s using monopole operators for convenience..

$$W \sim T^2 \text{Tr}(Z_1 Z_3 Z_2 Z_4 - Z_1 Z_4 Z_2 Z_3) + m T Z_4^2$$

$$\rightarrow Z_4 \sim T \epsilon^{abc} Z_a Z_b Z_c \quad \text{Integrating out massive field..}$$

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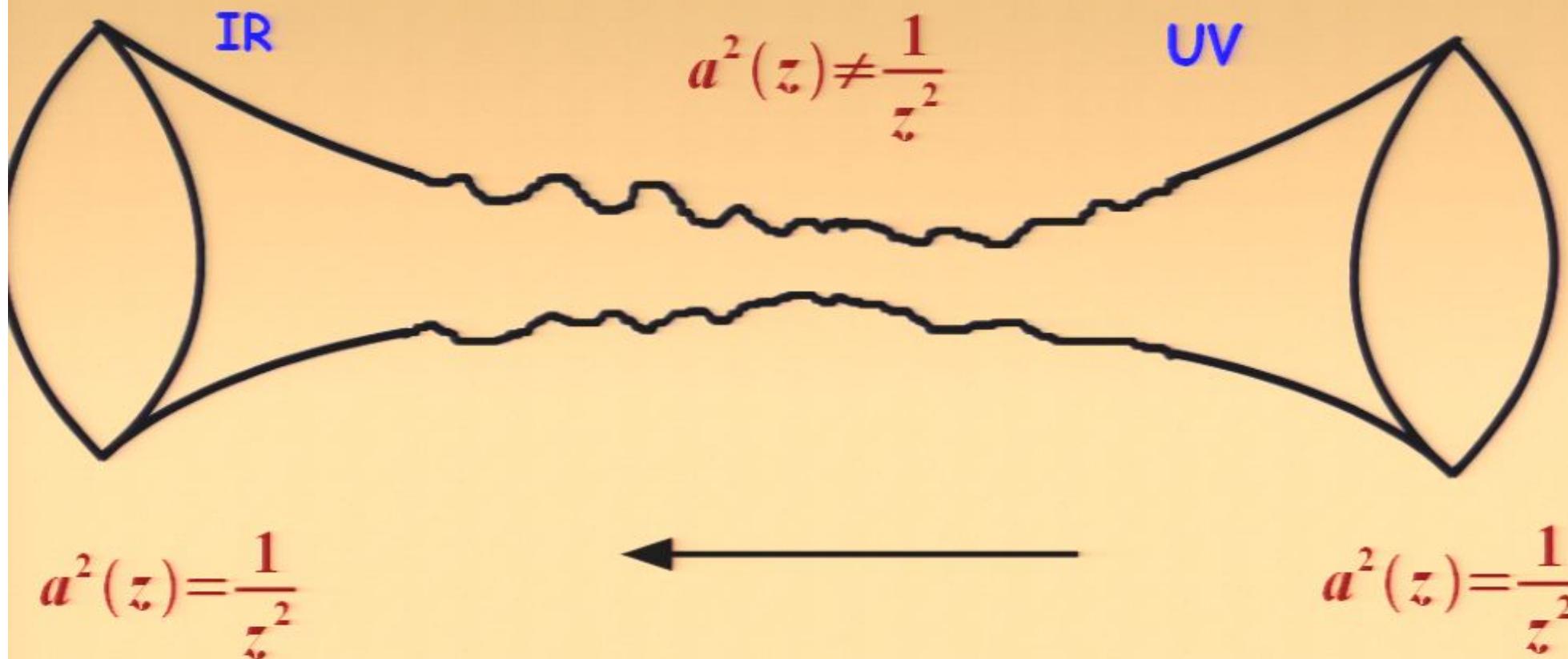
SU(3) symmetric

Sextic superpotential.. each  $Z$  must have dimension 1/3 for  $W$  to be marginal.

$$\Delta(Z_a) = \frac{1}{3}$$

# RG Flow

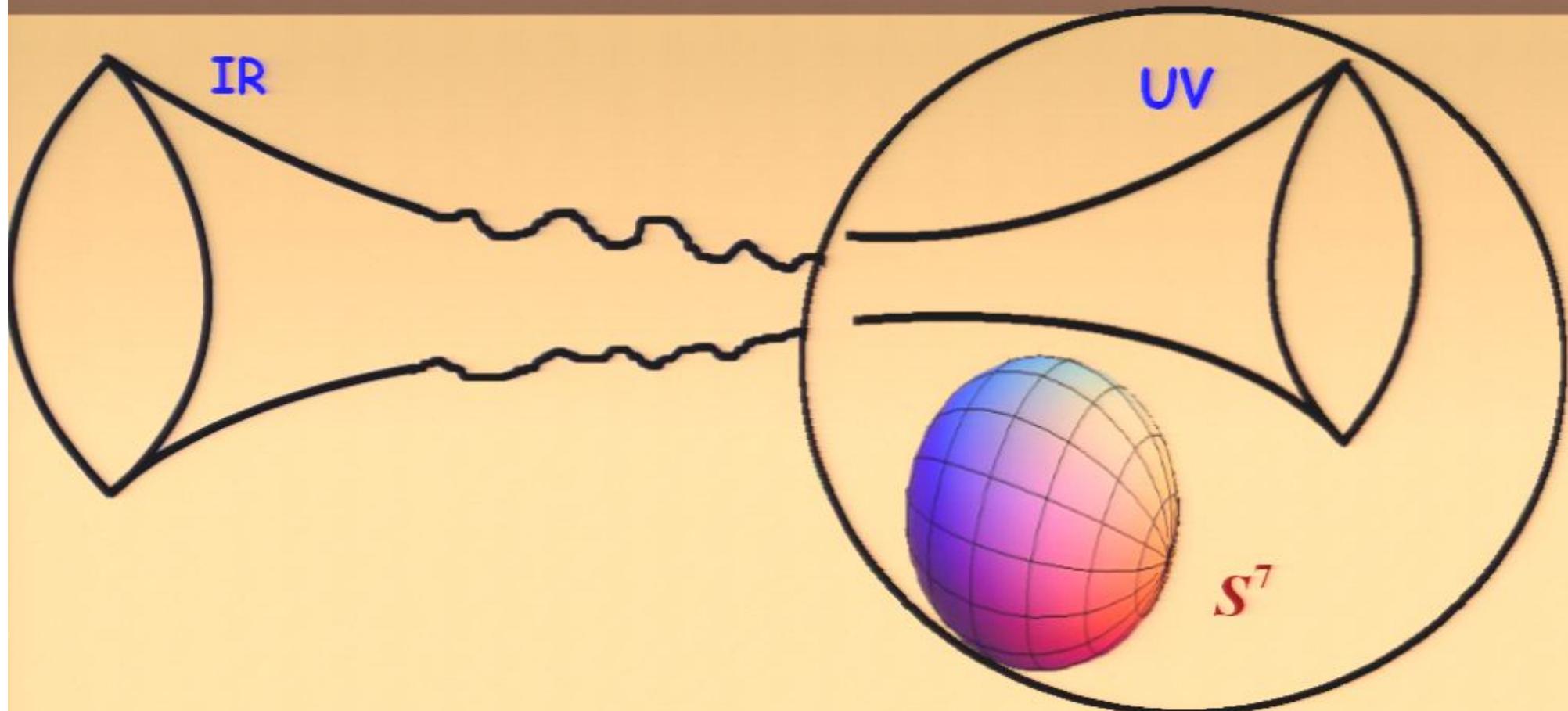
[Nicolai, Warner],  
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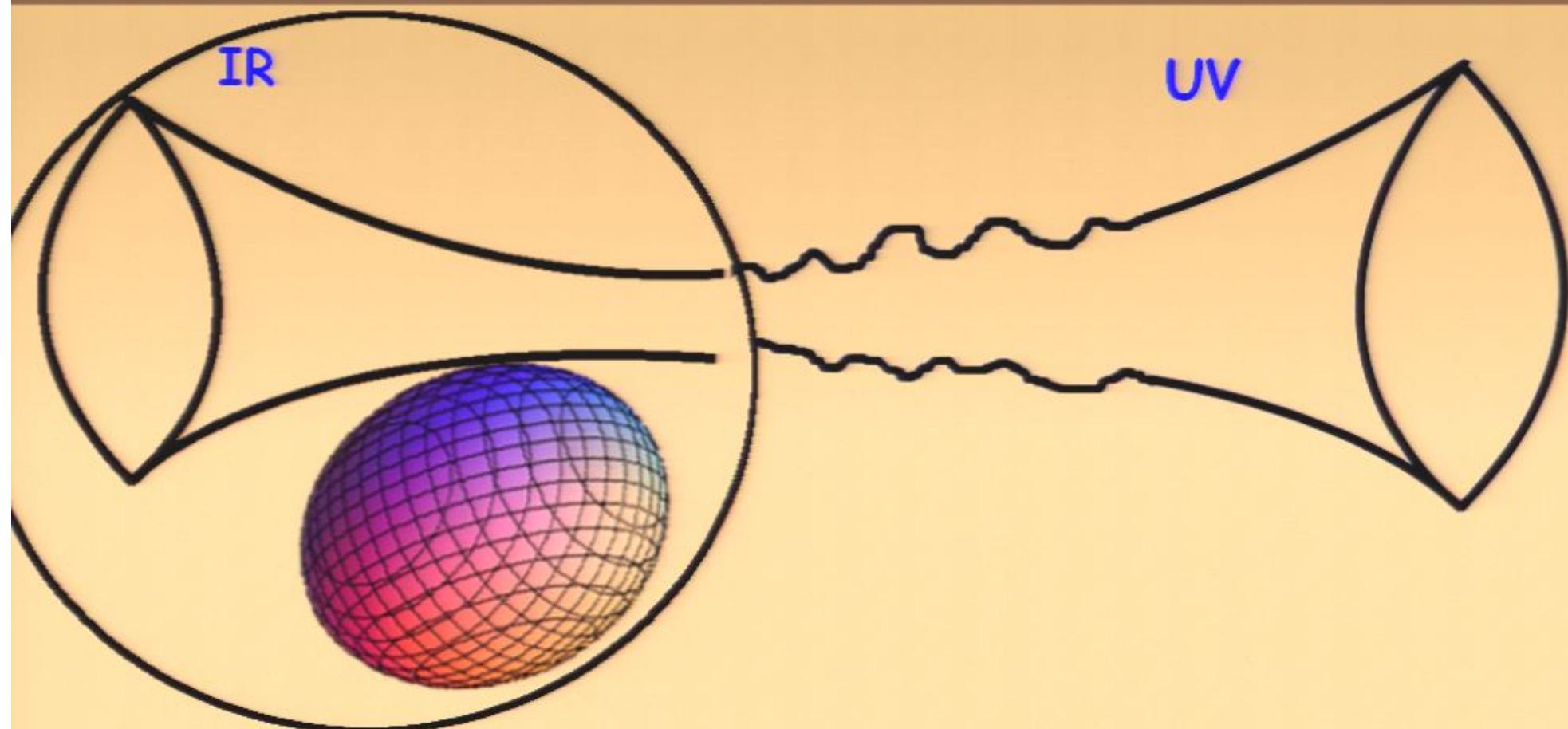
Pirsa: 08120056

N = 8 SUSY  
SO(8) symmetry  
Dual to 'ABJM' field  
theory

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# RG Flow

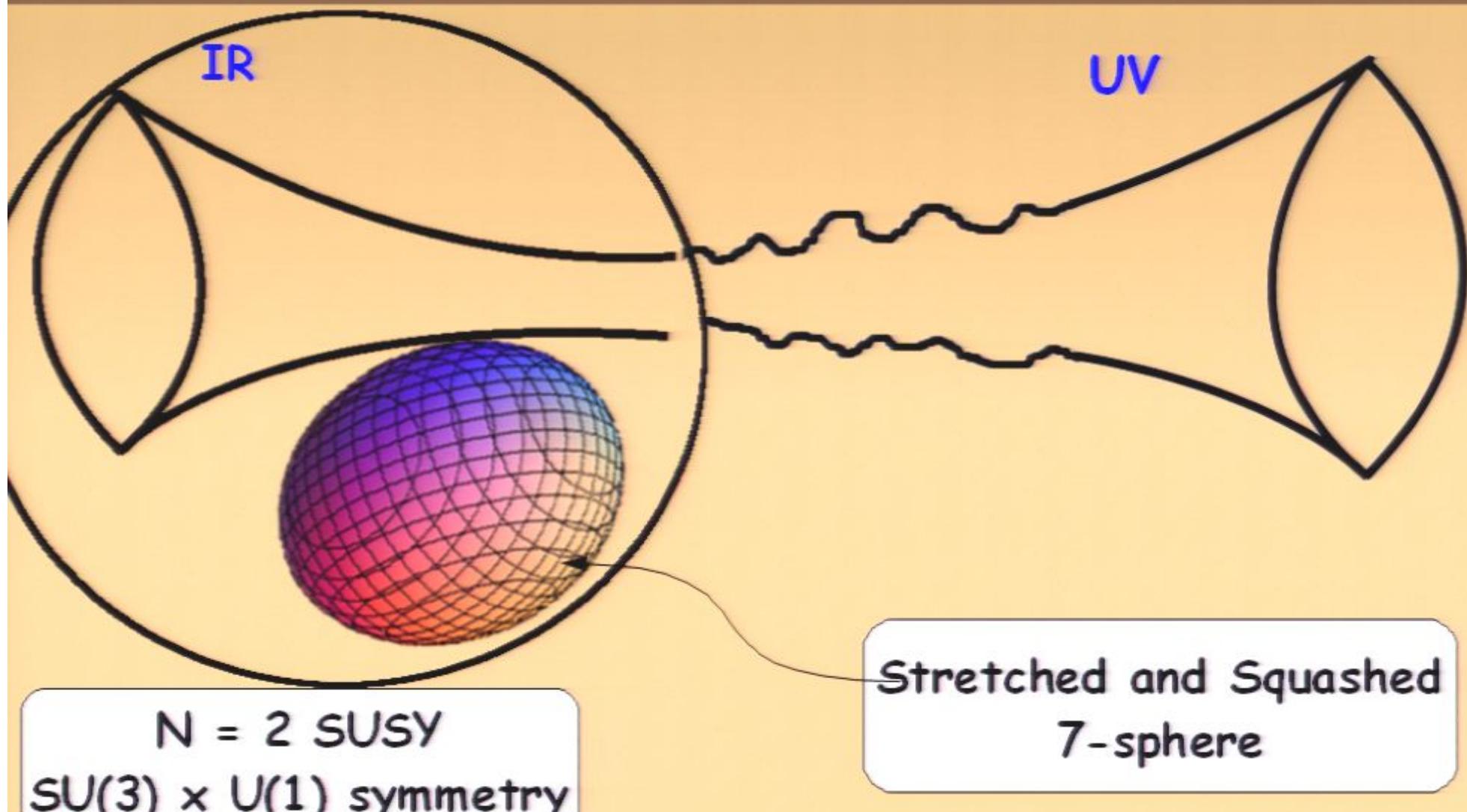
[Nicolai, Warner],  
[Corrado, Pilch, Warner ]  
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$N = 2$  SUSY  
 $SU(3) \times U(1)$  symmetry

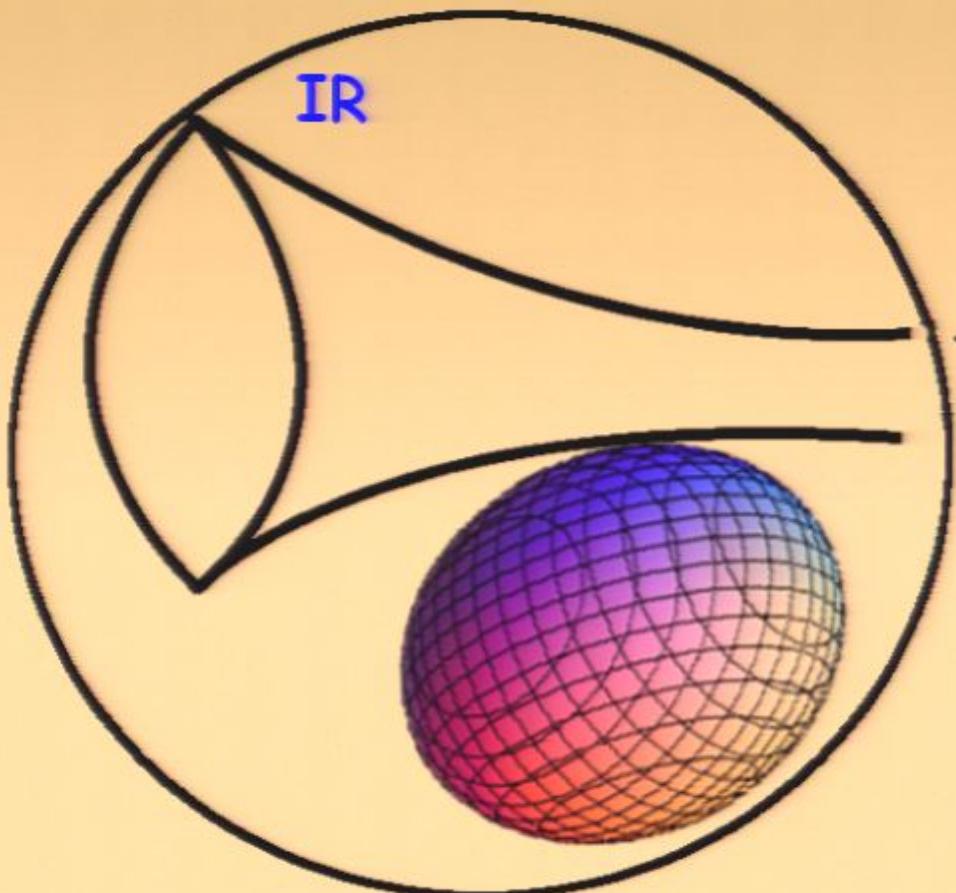
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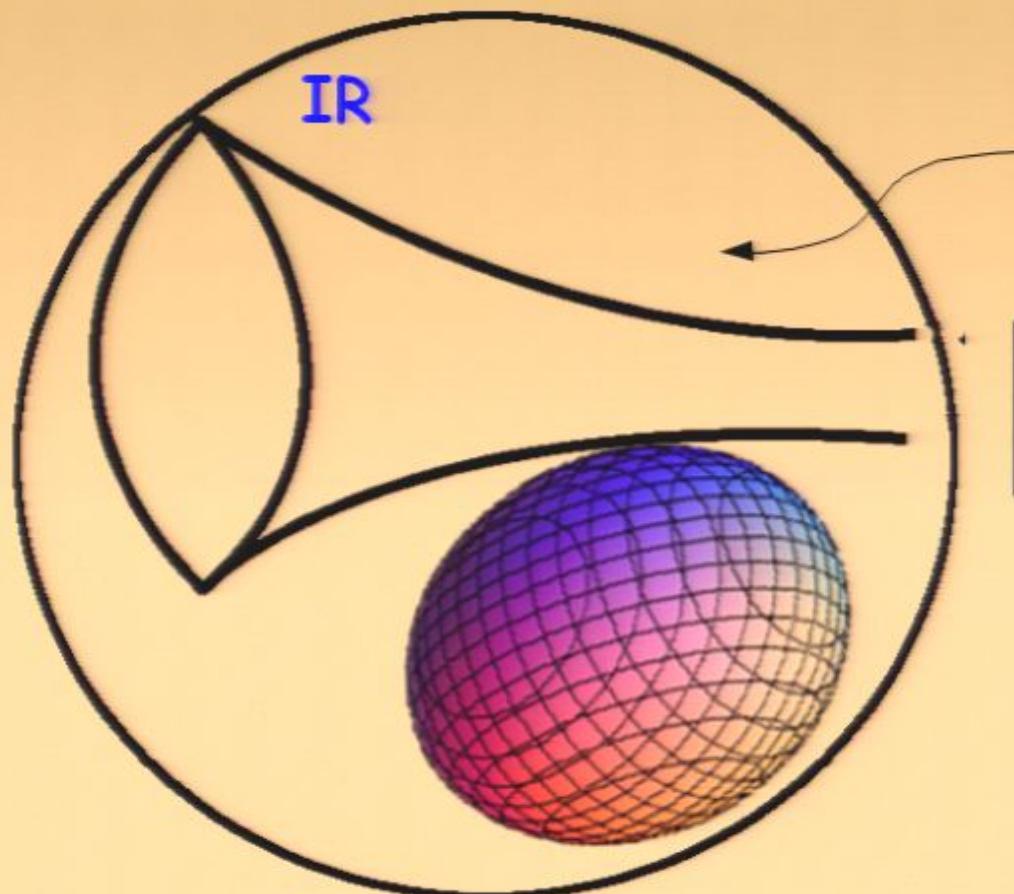
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$$ds^2 = \frac{1}{z^2} (dz^2 + dx^\mu dx_\mu)$$

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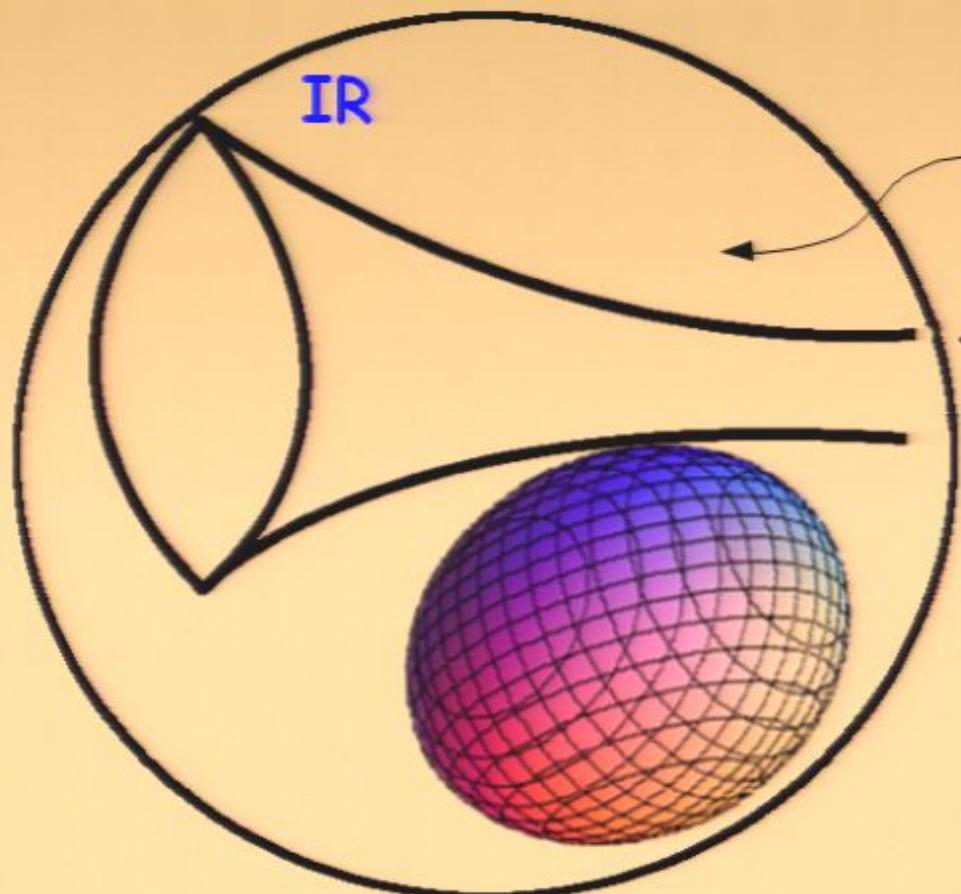
$$ds^2 = \frac{h(\theta)}{z^2} (dz^2 + dx^\mu dx_\mu)$$

AdS metric is warped by  
function 'h' on internal space

$$AdS_4 \times_h X^7$$

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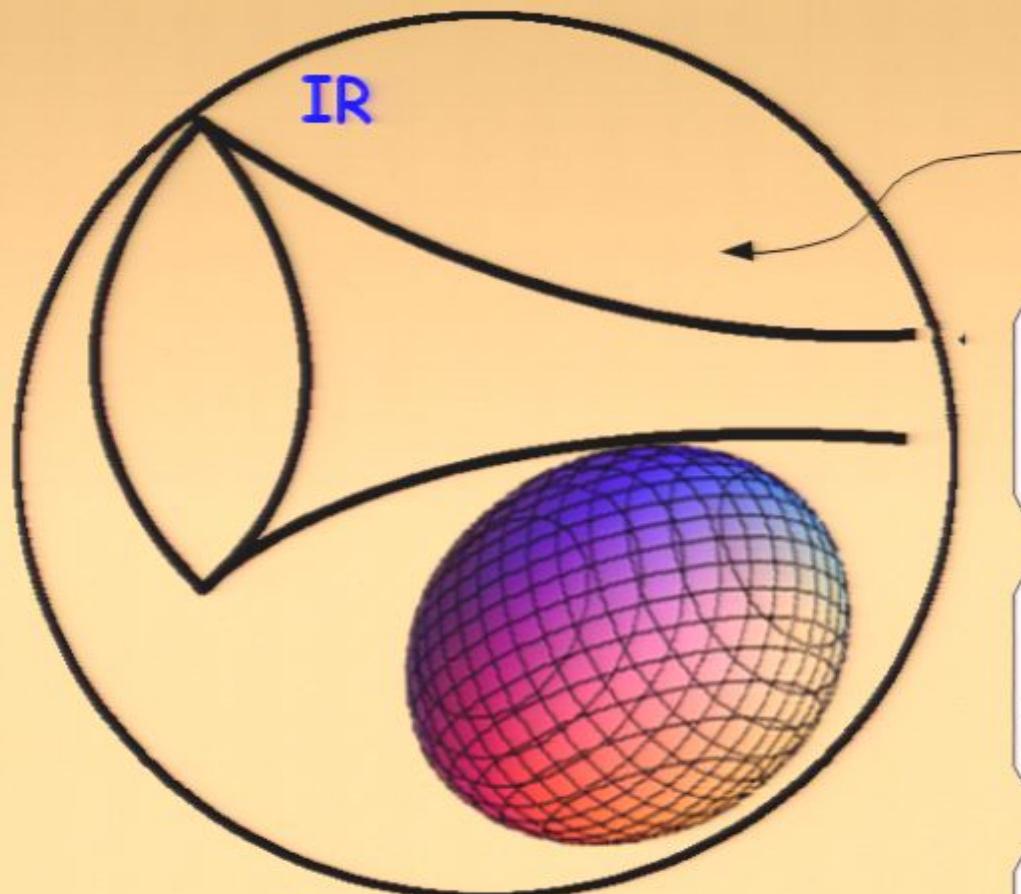
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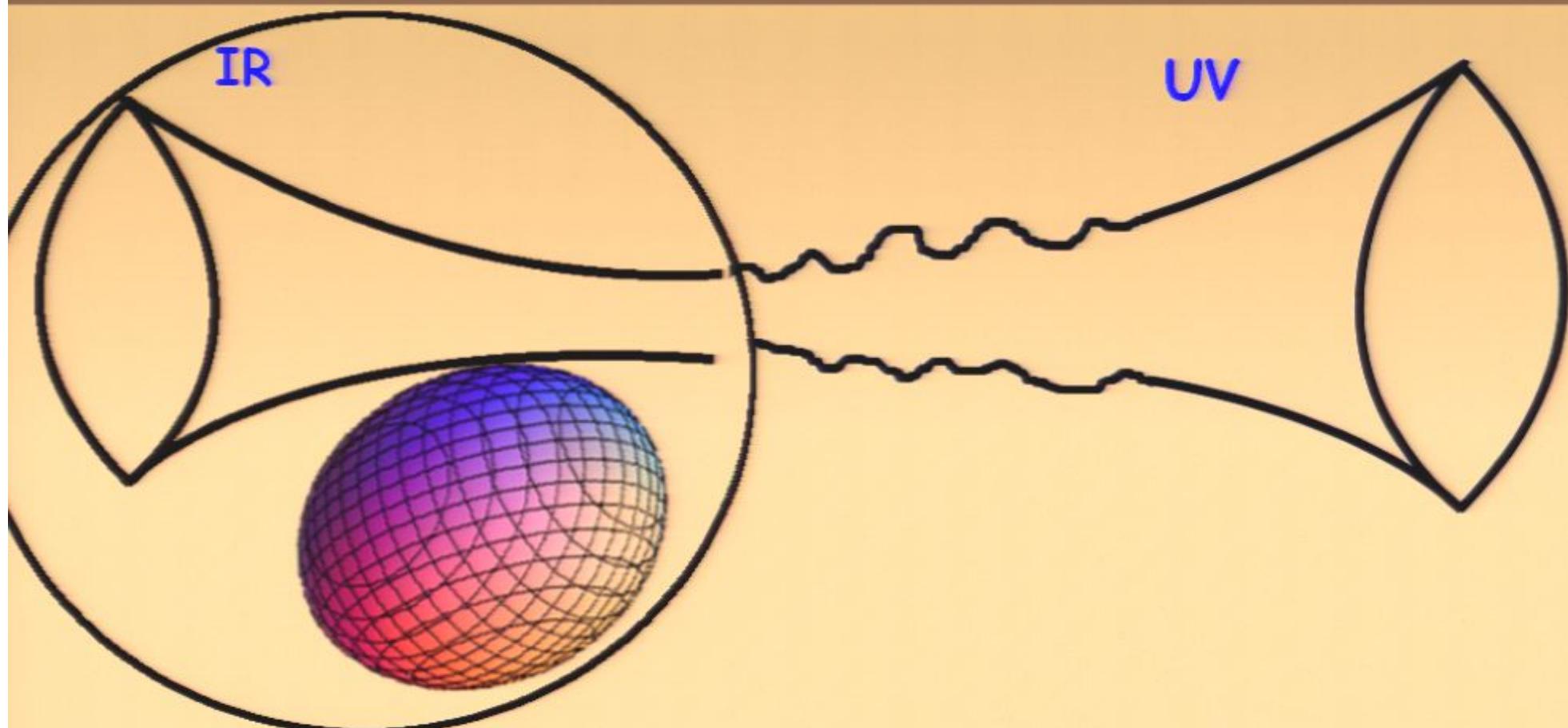
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 $SU(3) \times U(1)$  symmetry

# Field theory analysis

$$W \sim \text{Tr}(Z_1 W_1 Z_2 W_2 - Z_1 W_2 Z_2 W_1) + m W_2^2$$

Write in terms of  $Z$ s using monopole operators for convenience..

$$W \sim T^2 \text{Tr}(Z_1 Z_3 Z_2 Z_4 - Z_1 Z_4 Z_2 Z_3) + m T Z_4^2$$

→  $Z_4 \sim T \epsilon^{abc} Z_a Z_b Z_c$  Integrating out massive field..

$$W \sim T^3 (\epsilon^{abc} Z_a Z_b Z_c)^2$$

SU(3) symmetric

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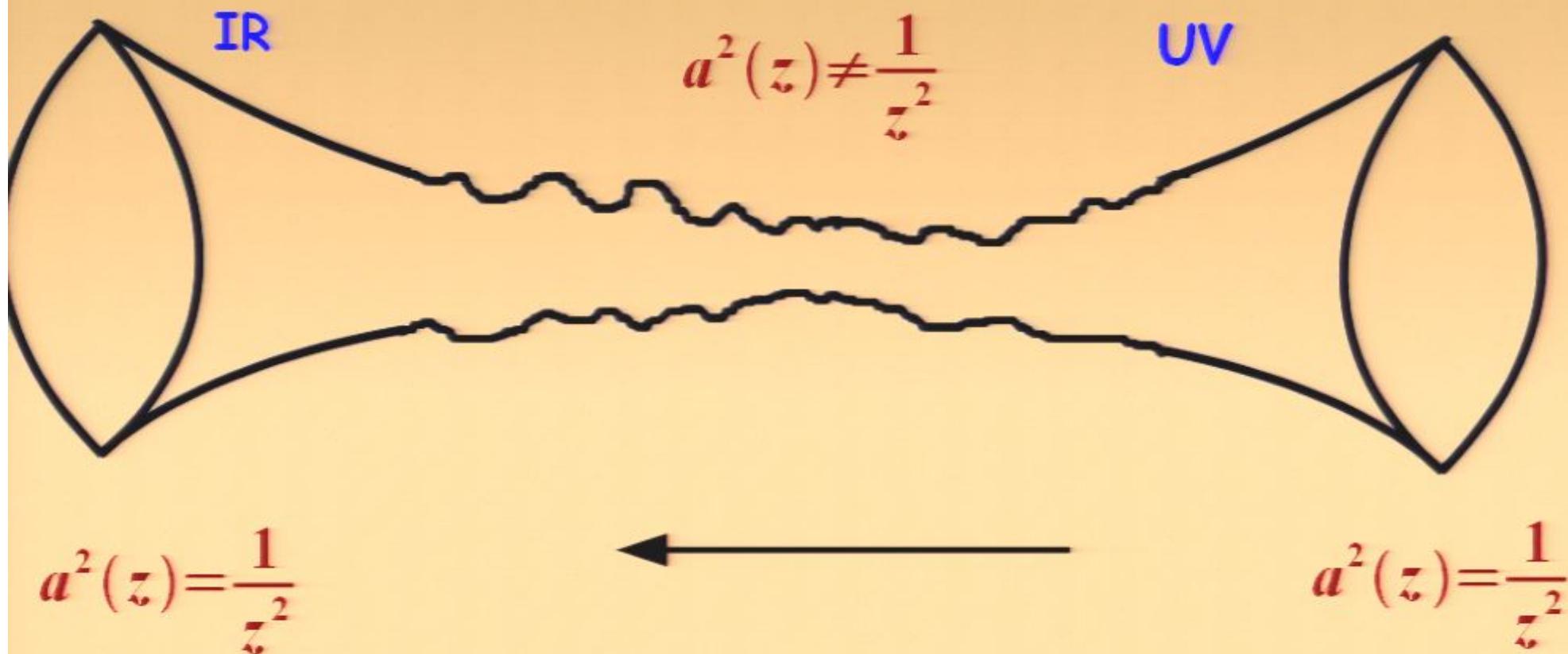
SU(3) symmetric

Sextic superpotential.. each  $Z$  must have dimension 1/3 for  $W$  to be marginal.

$$\Delta(Z_a) = \frac{1}{3}$$

# RG Flow

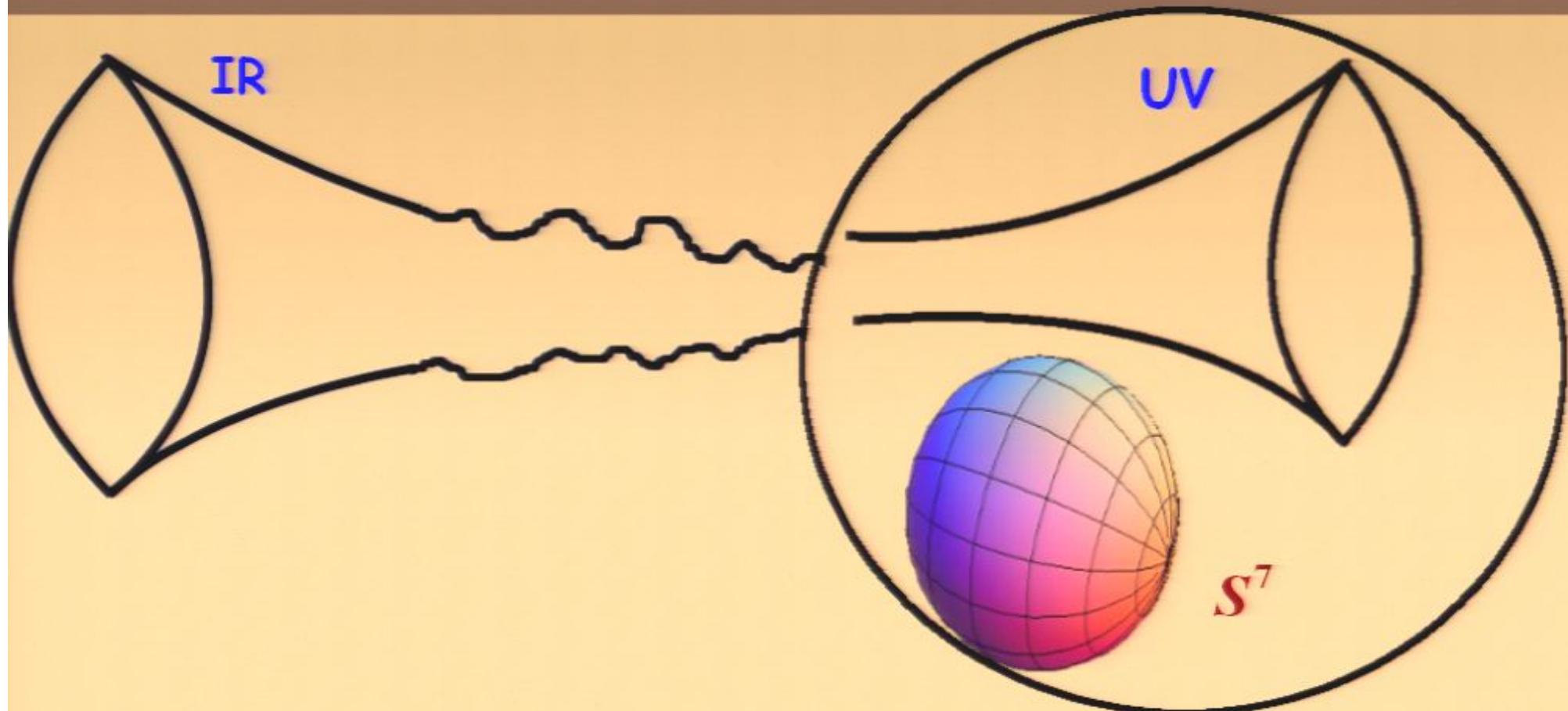
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A background with two AdS  
throats had been already  
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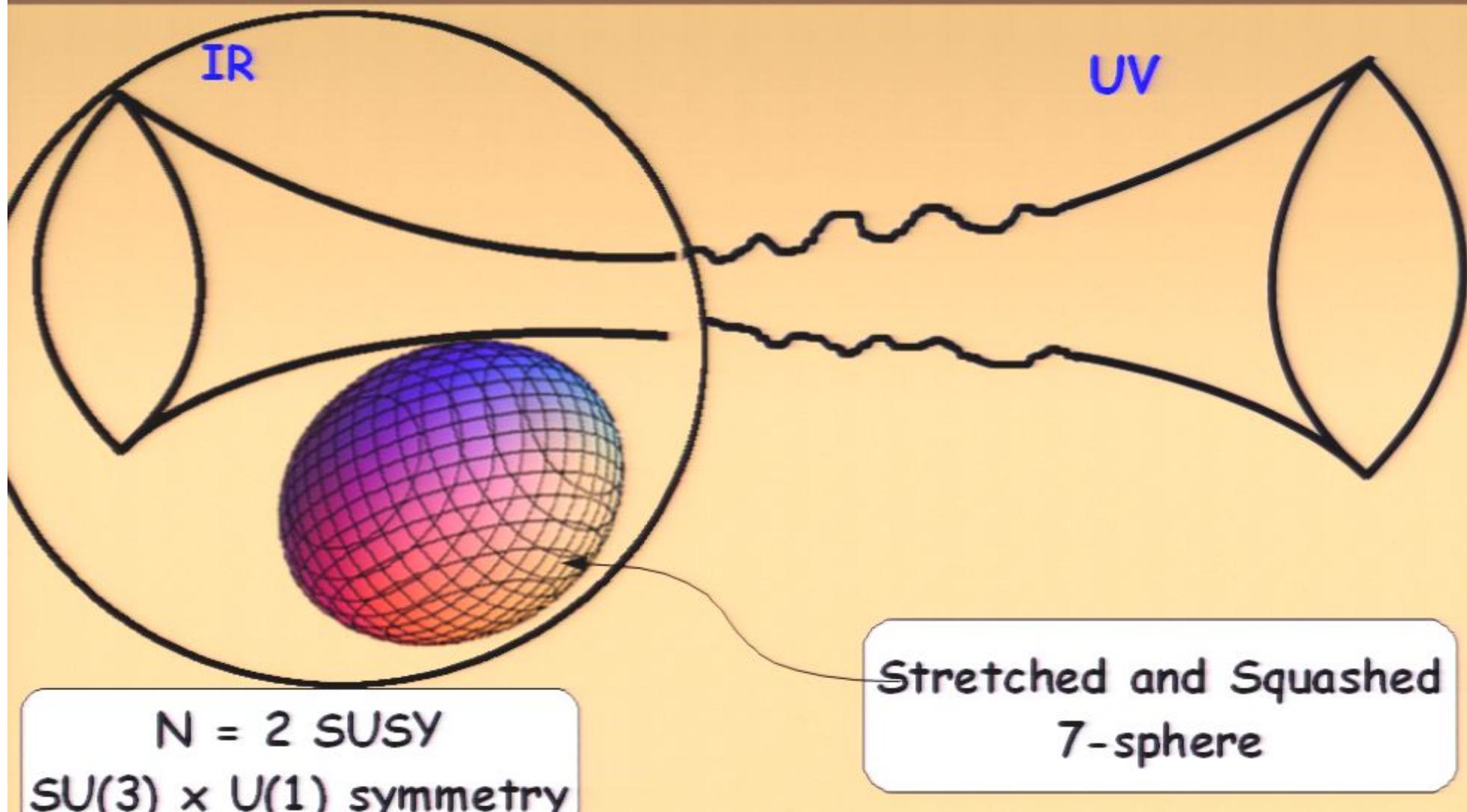
Pirsa: 08120056

N = 8 SUSY  
SO(8) symmetry  
Dual to 'ABJM' field  
theory

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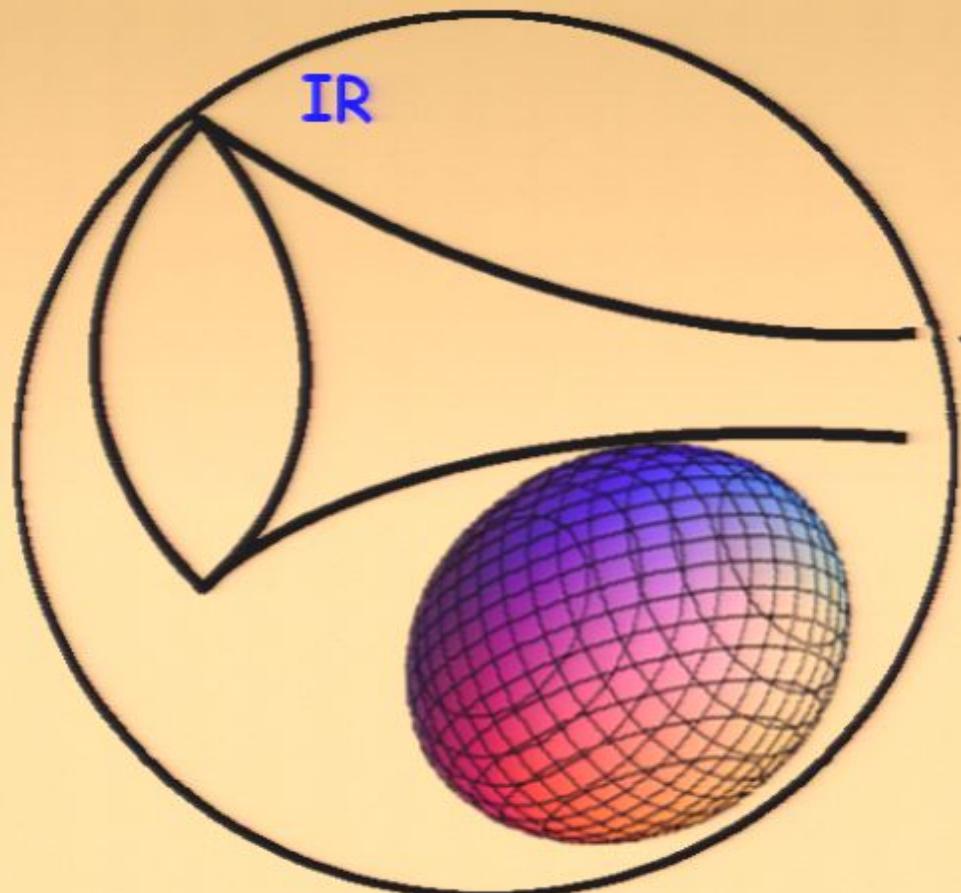
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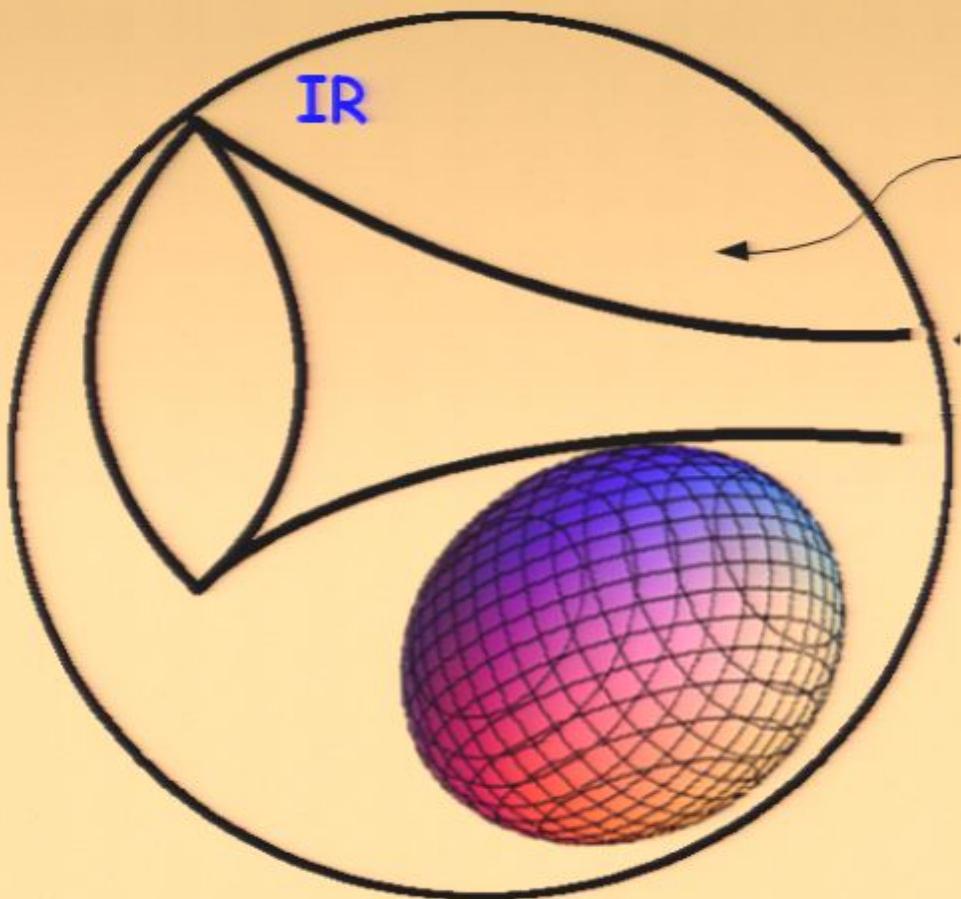
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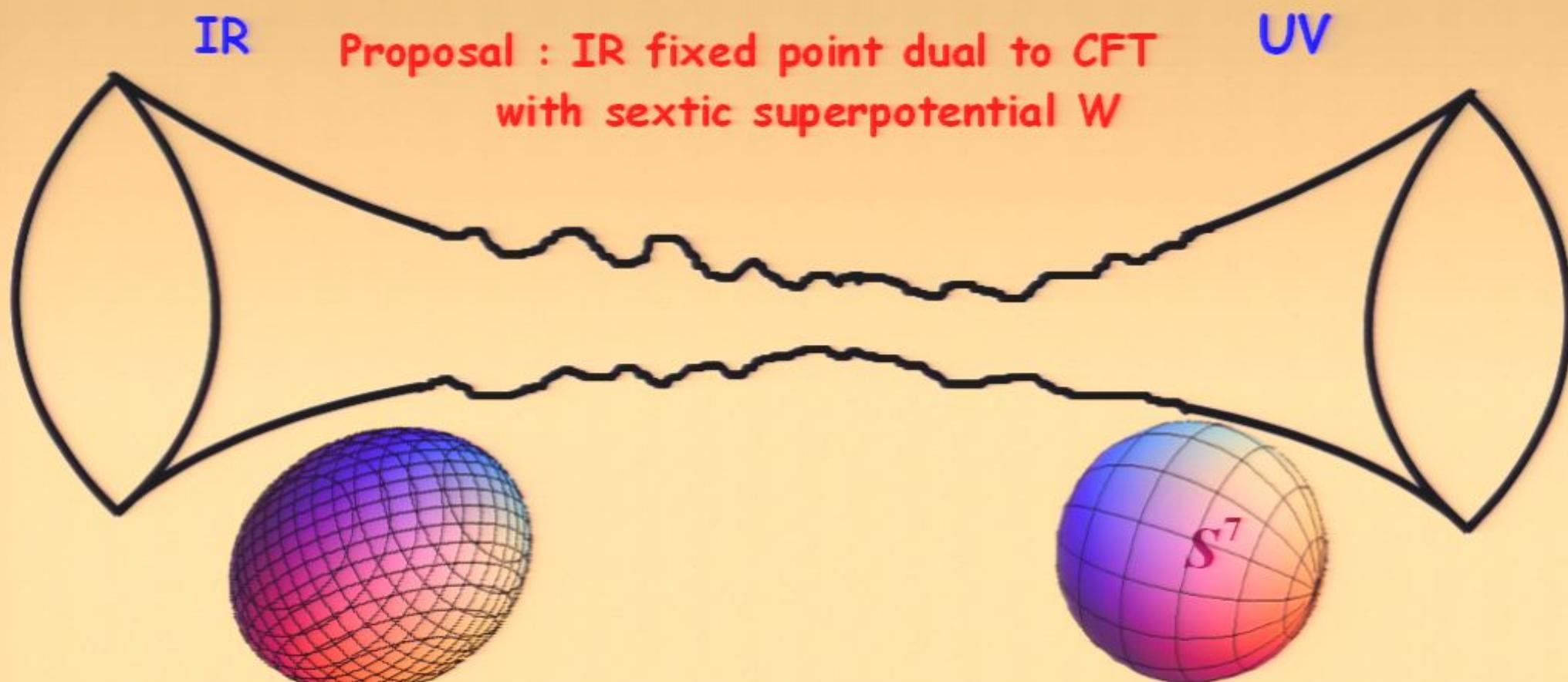
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# Gravity spectrum, the easy way

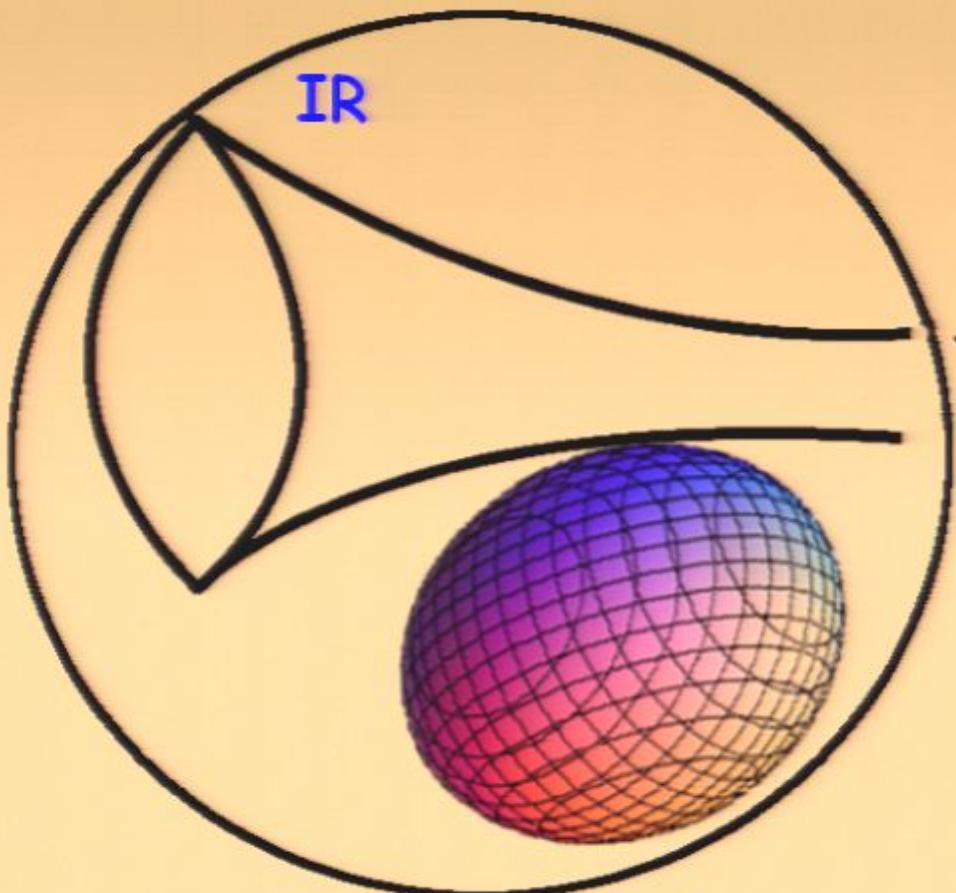
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$$SU(3) \times U(1)_R \subset SO(8)$$

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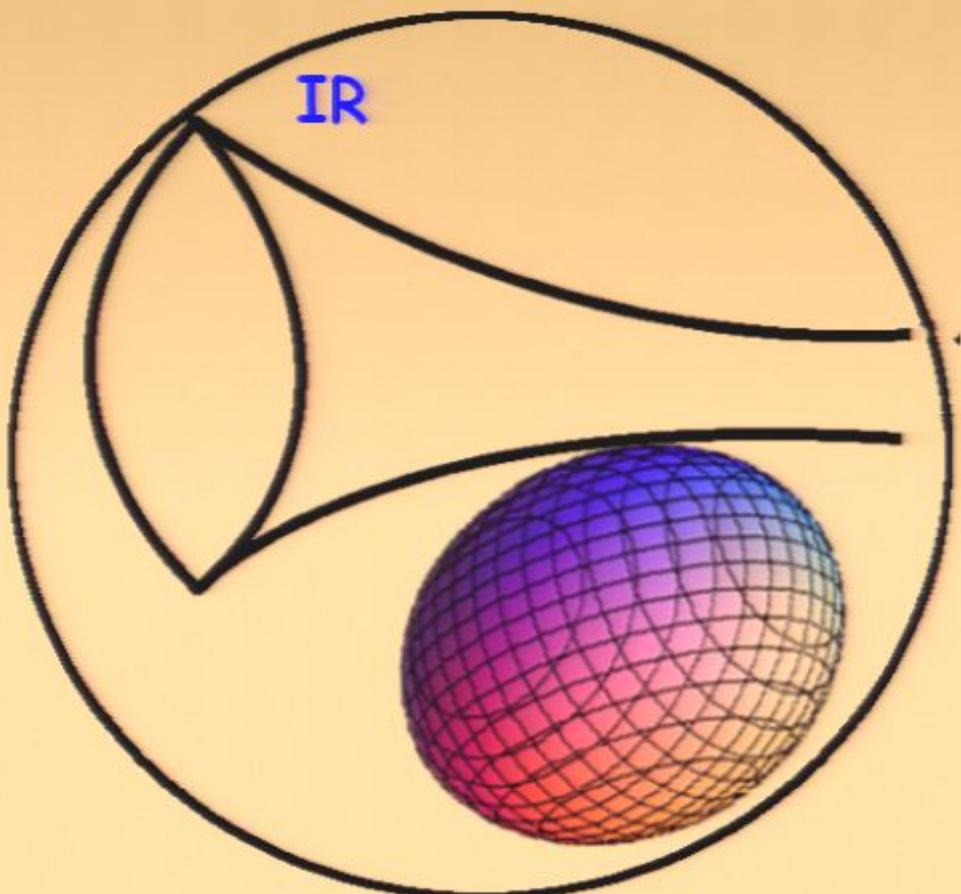
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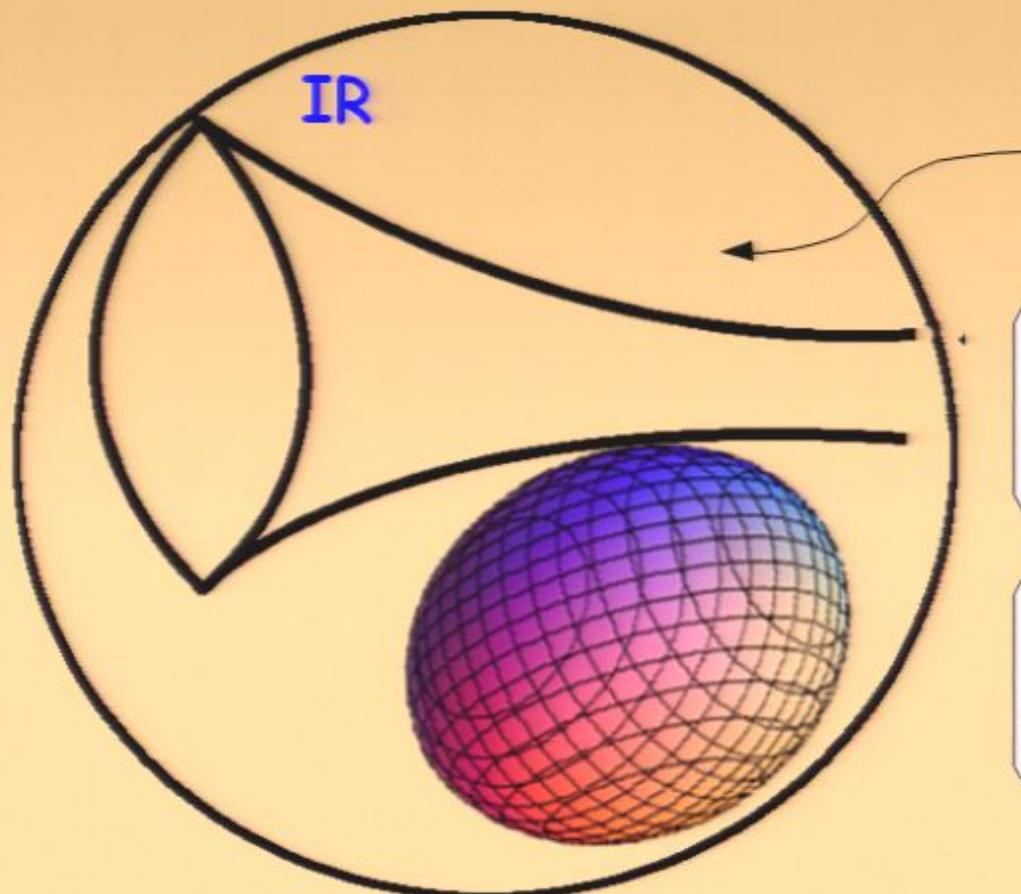
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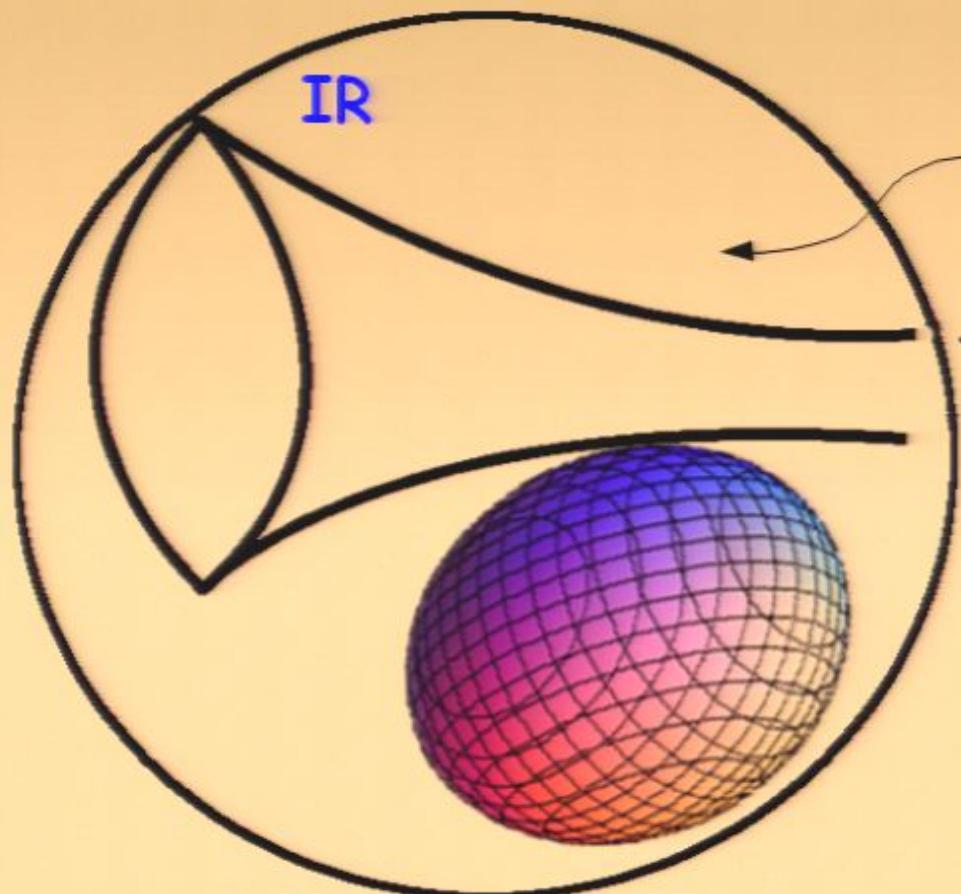
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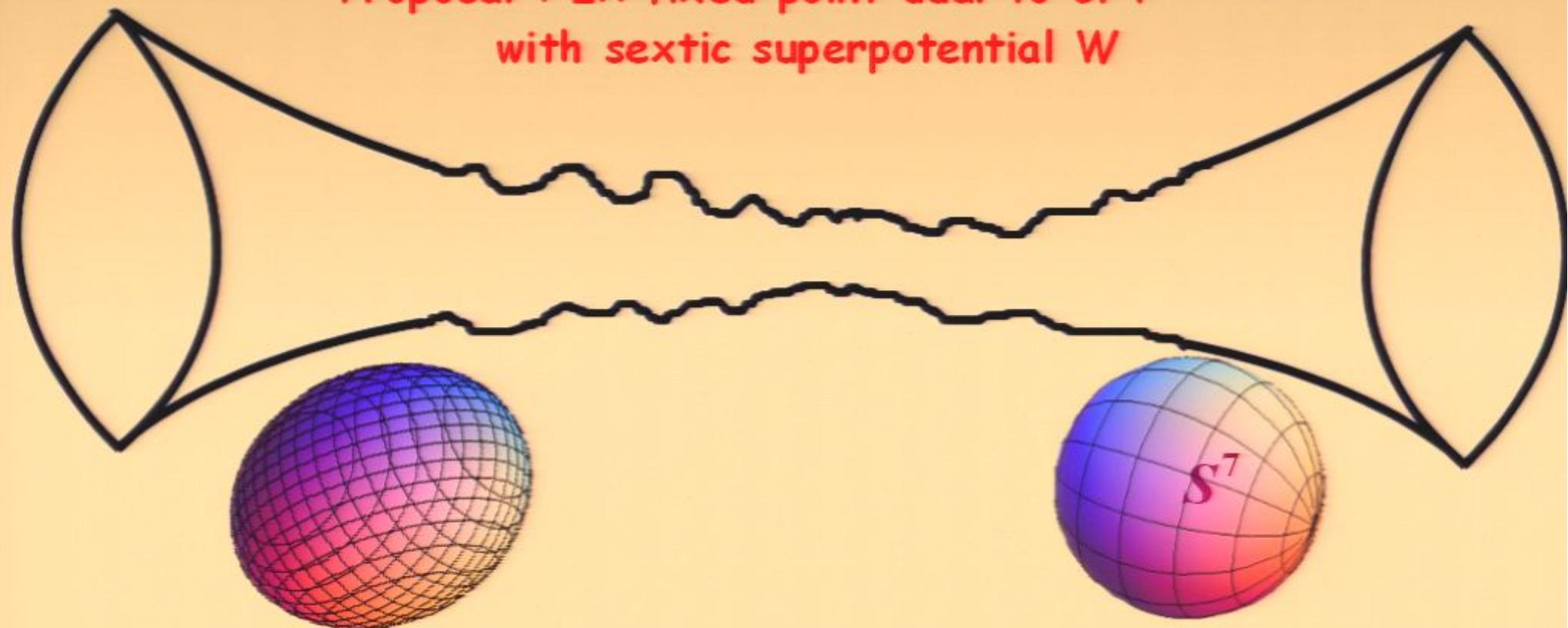
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# RG Flow

IR

Proposal : IR fixed point dual to CFT  
with sextic superpotential  $W$

UV



$N = 2$  SUSY

$SU(3) \times U(1)$  symmetry

$N = 8$  SUSY

$SO(8)$  symmetry

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Gravity spectrum from explicit KK reduction is difficult...

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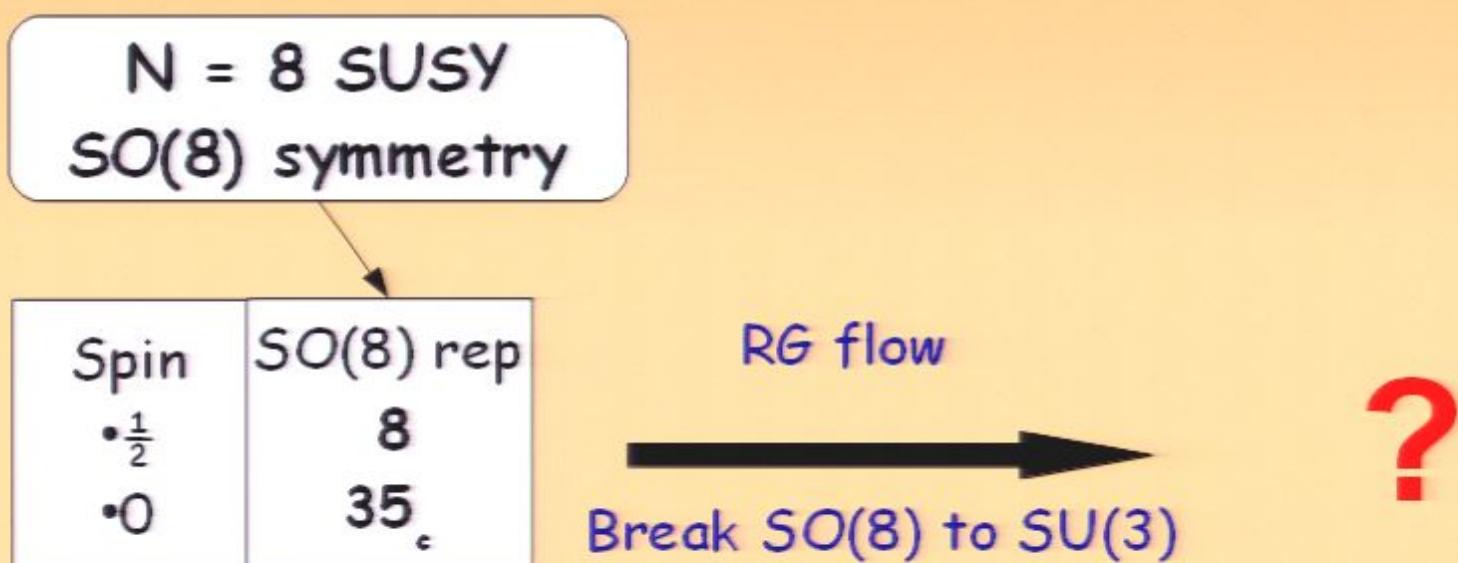


Spin	$SO(8)$ rep
$\cdot \frac{1}{2}$	8
$\cdot 0$	35 <sub>c</sub>

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RG flow

Break  $SO(8)$  to  $SU(3)$

Spin	$SU(3)$ rep
$\cdot \frac{1}{2}$	$3 + \underline{3} + 1 + 1$
$\cdot 0$	$\dots + 3 + \underline{3} + 1 + 1 + \dots$

Choice of  $U(1)_R \subset SO(8)$

Spin	$SU(3) \times U(1)$ rep
$\cdot \frac{1}{2}$	$3(a) + \underline{3(-a)} + 1(c) + 1(e)$
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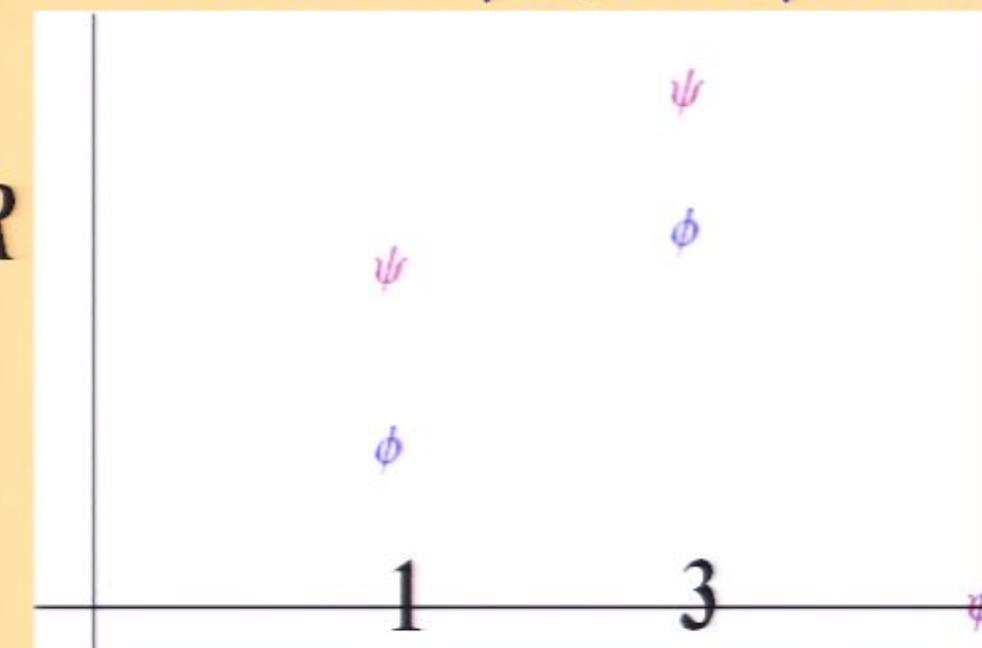
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to vary  $a, b, c, d, e, f$

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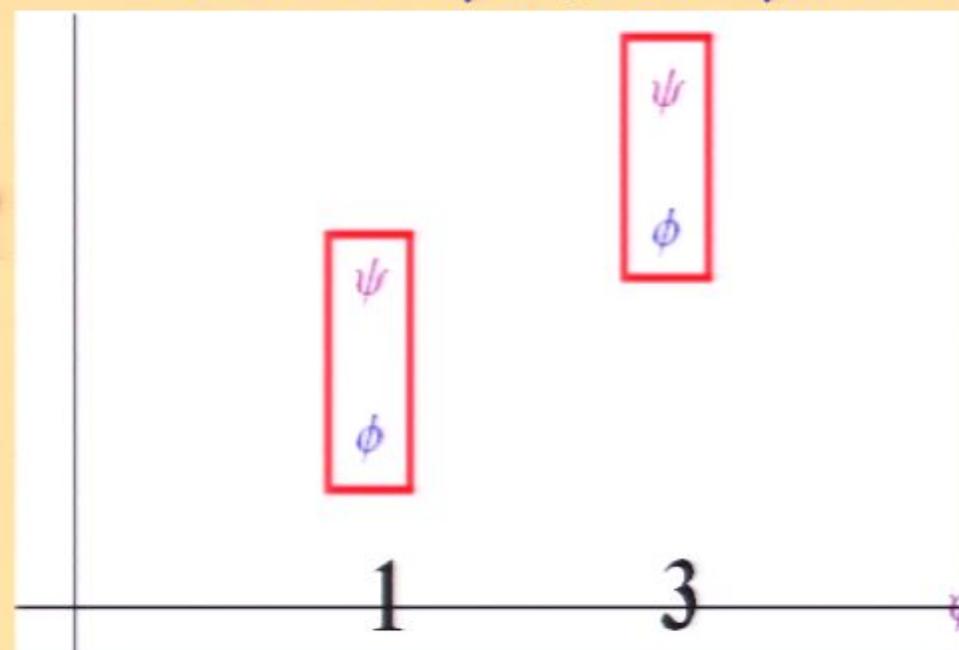


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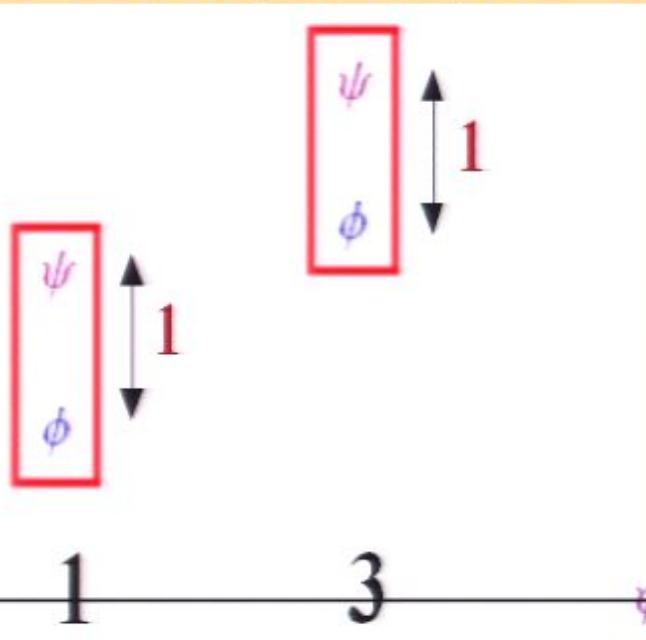


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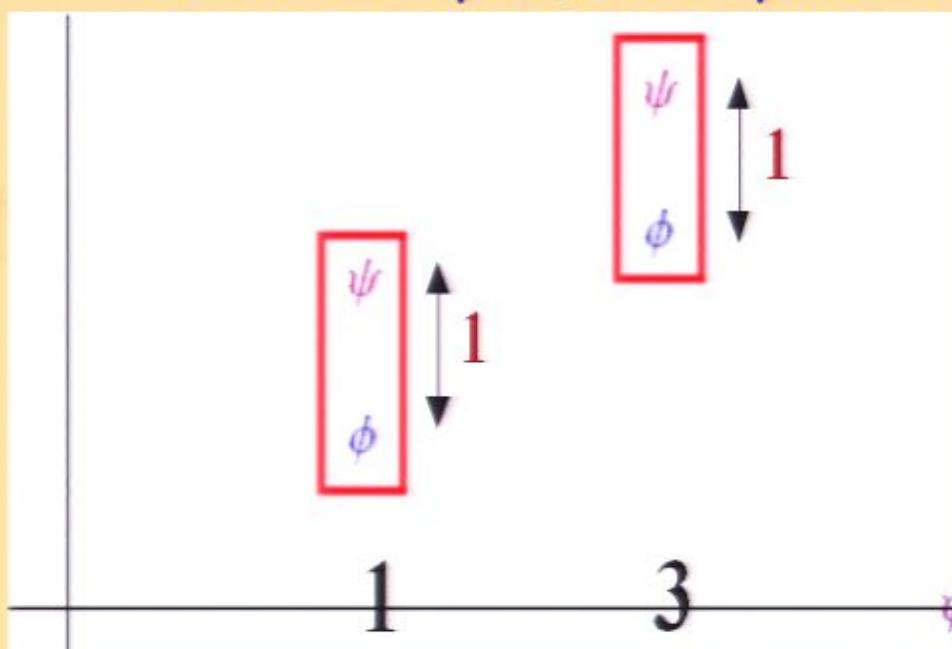


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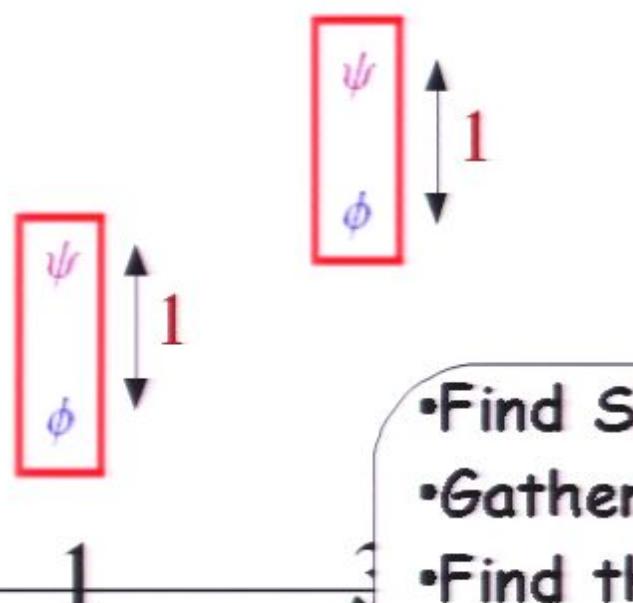
Using SUSY and group theory

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Using SUSY and group theory

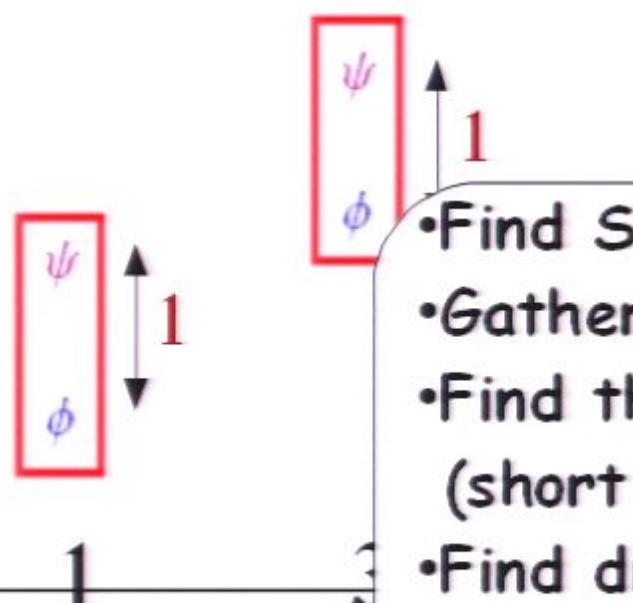
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Using SUSY and group theory

- Find  $SU(3) \times U(1)$  in  $SO(8)$
- Gather all particles into supermultiplets
- Find the structure of all multiplets (short and long)
- Find dimensions and charges of short multiplets
- Find charges of long multiplets

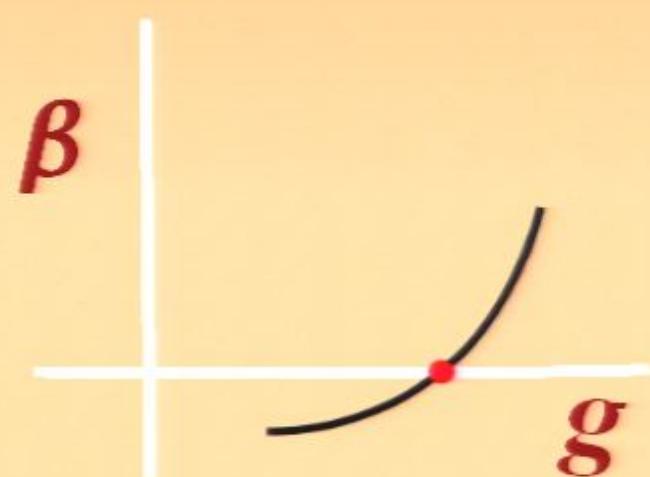
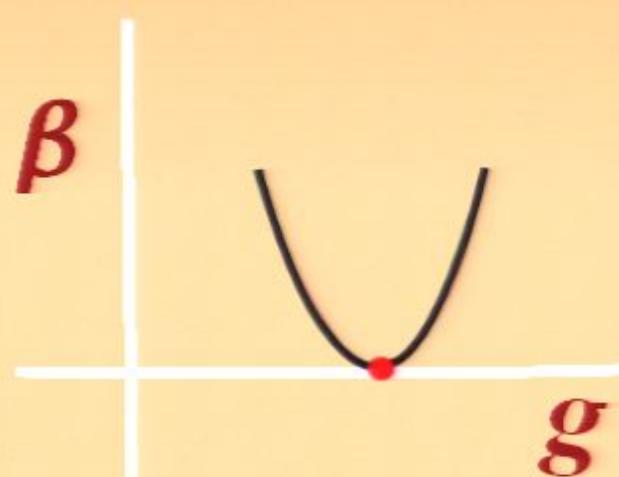
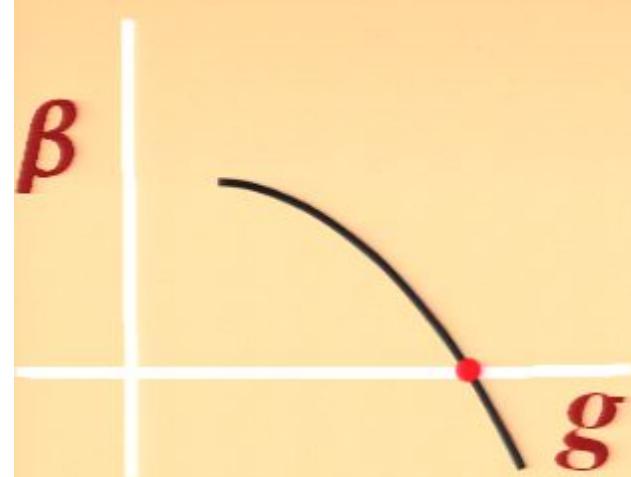
# Non-supersymmetric CFTs?

Three kinds of operators at a conformal fixed point

Relevant

Marginal

Irrelevant



At a fixed point

$$\beta(g_0) = 0$$

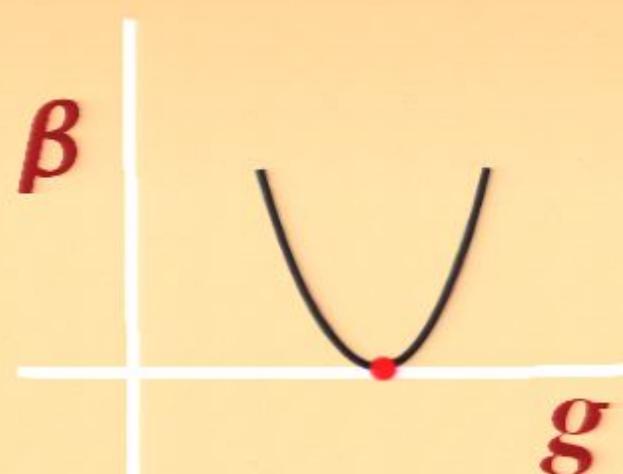
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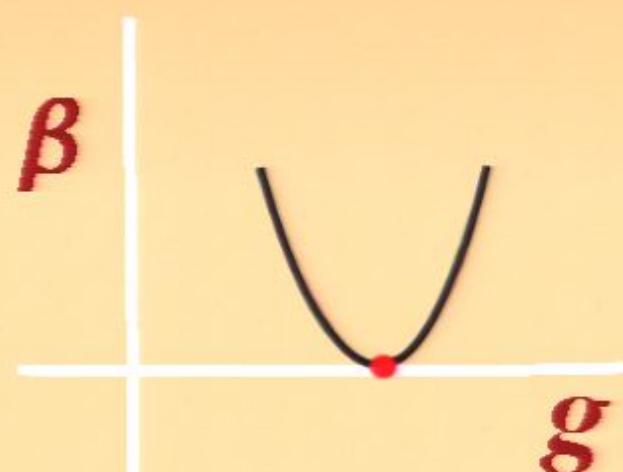
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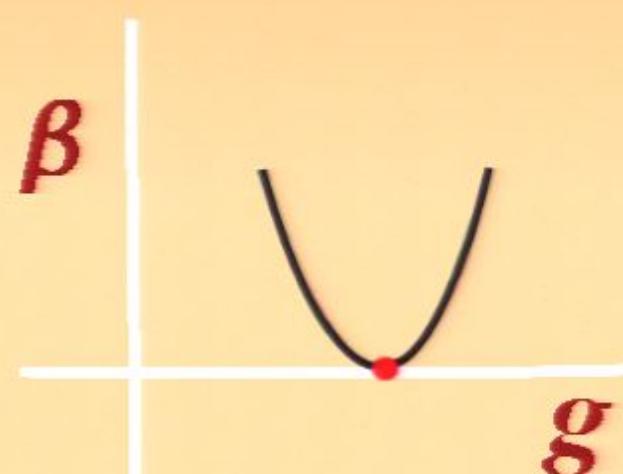
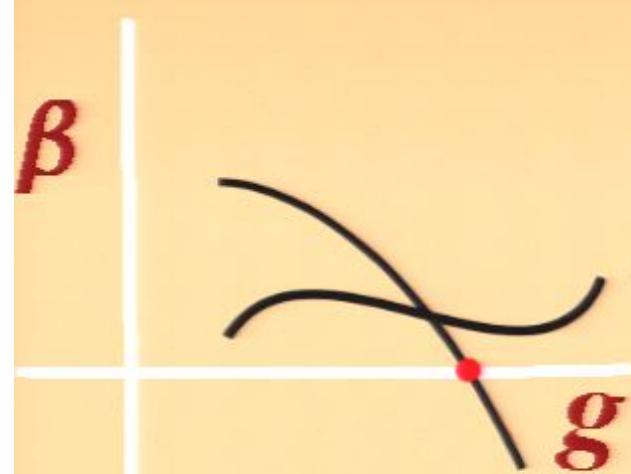
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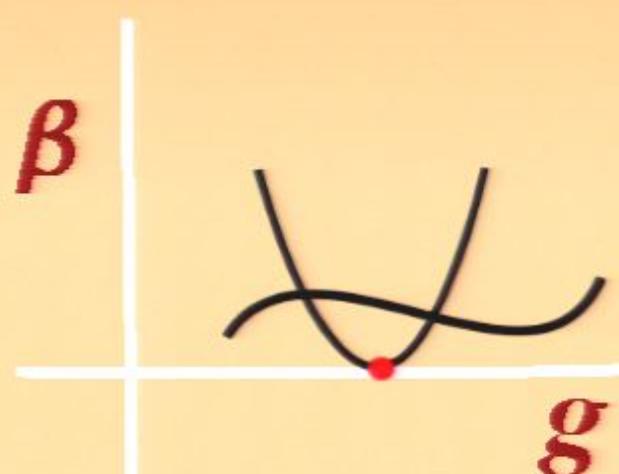
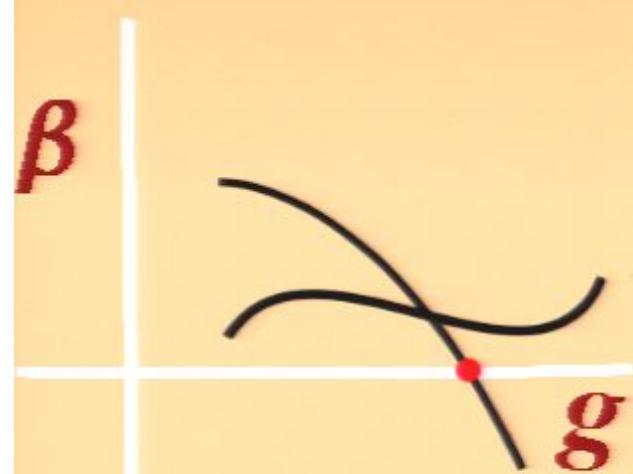
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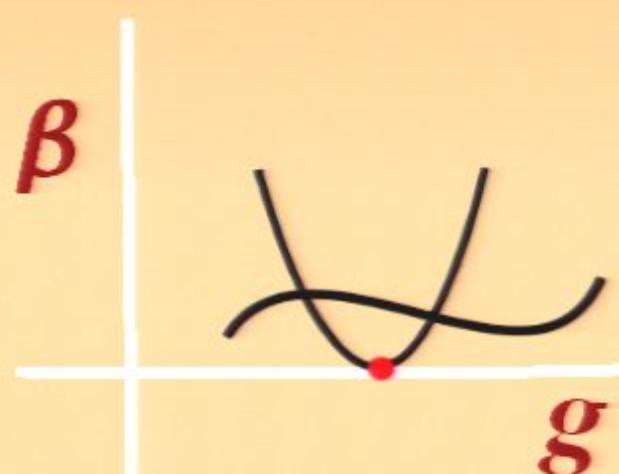
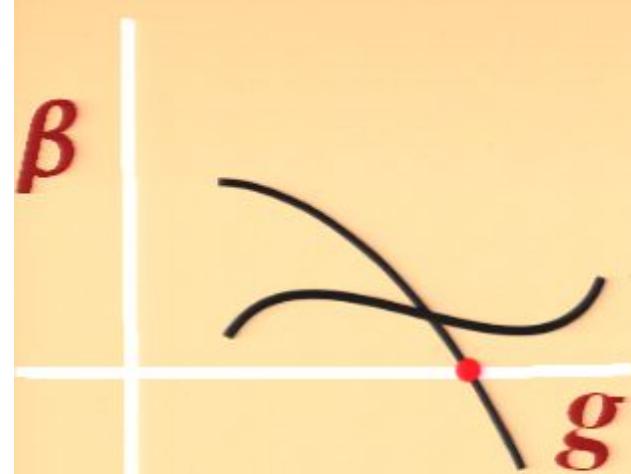
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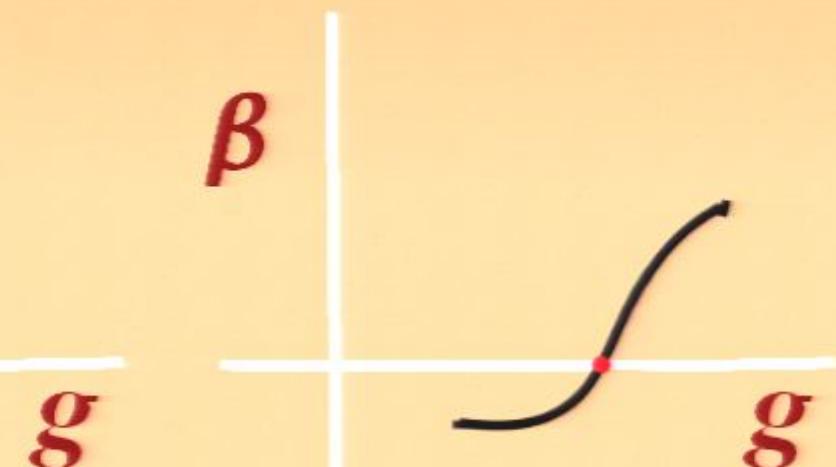
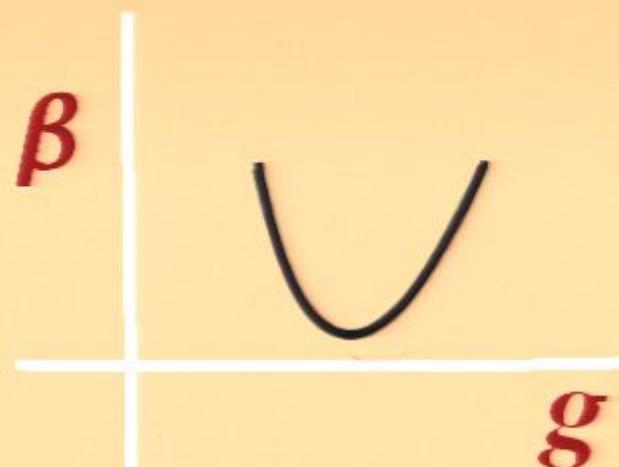
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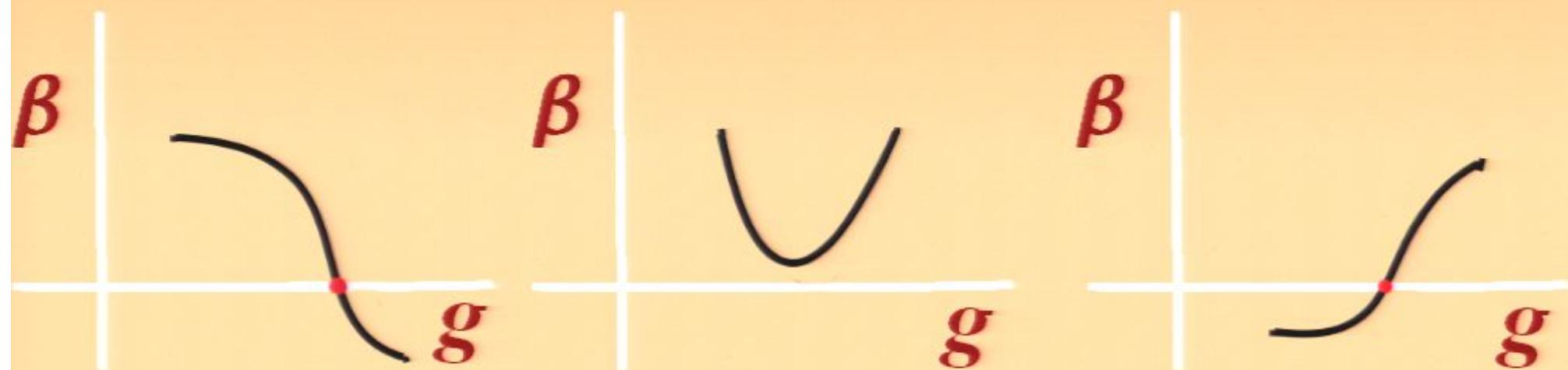
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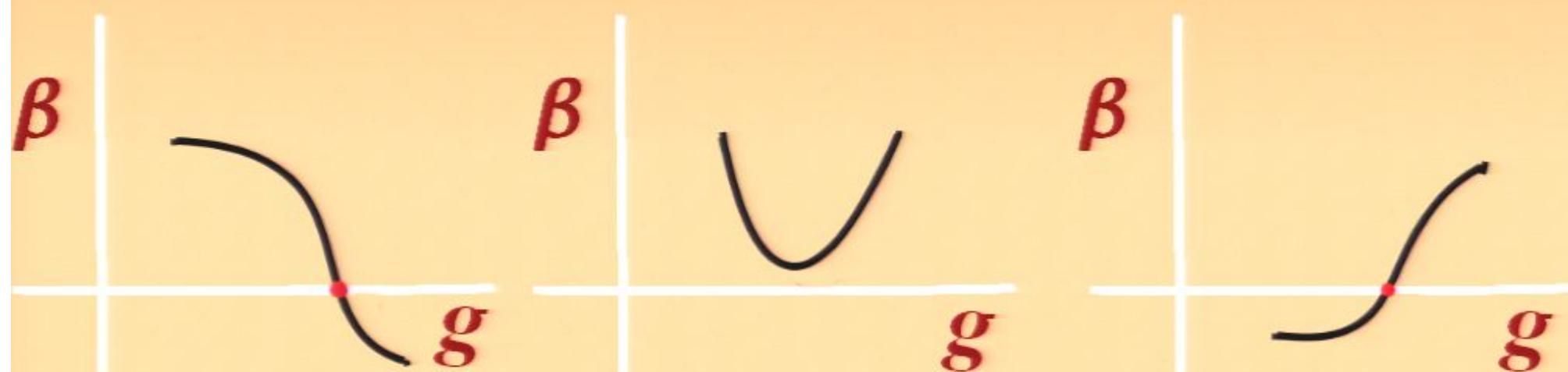
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Three kinds of operators at a conformal fixed point

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Irrelevant



Marginal operators could destroy conformal fixed points.

$$AdS_5 \times X^5_{\text{non-SUSY}}$$

Pirsa: 08120056

$$\frac{1}{g^2} \text{Tr } F \wedge *F$$

Gauge coupling is always marginal

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# Non-supersymmetric CFTs?

$$AdS_4 \times X^7(n)$$

Any non-SUSY family.  
Let  $n=0$  be SUSY.

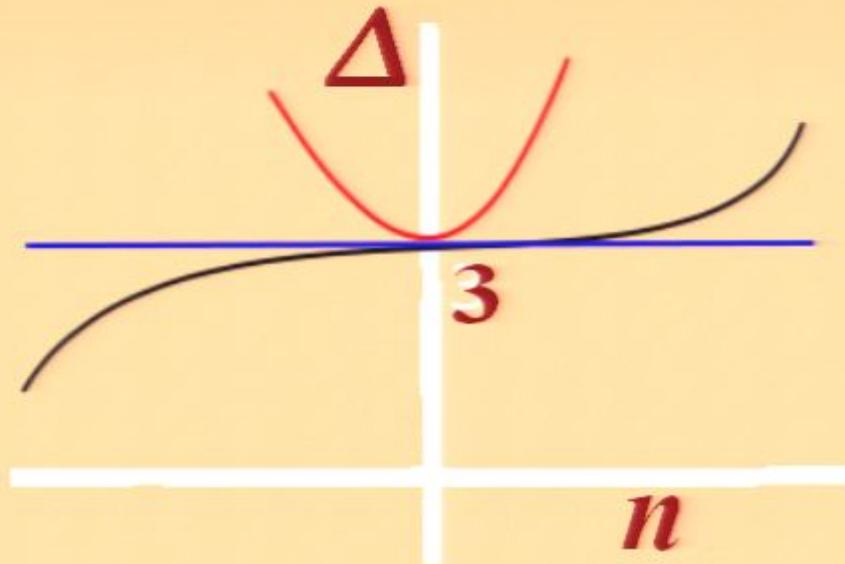
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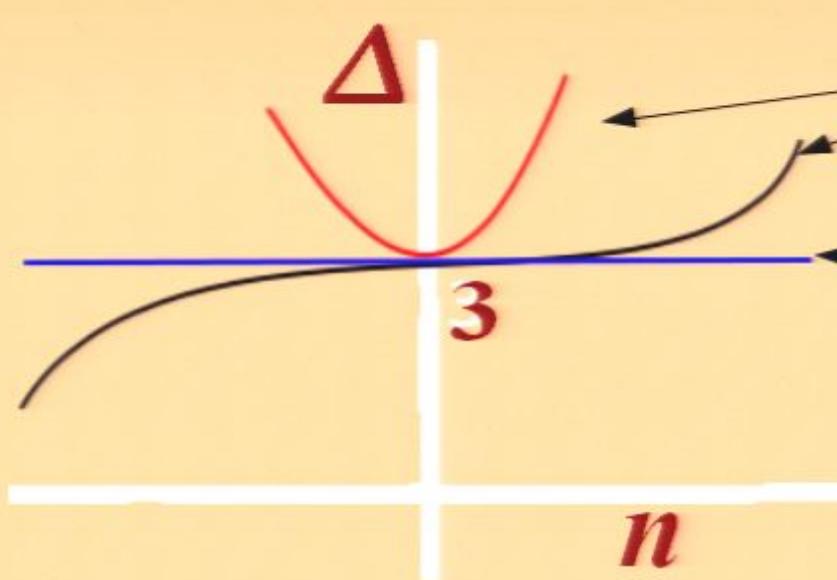


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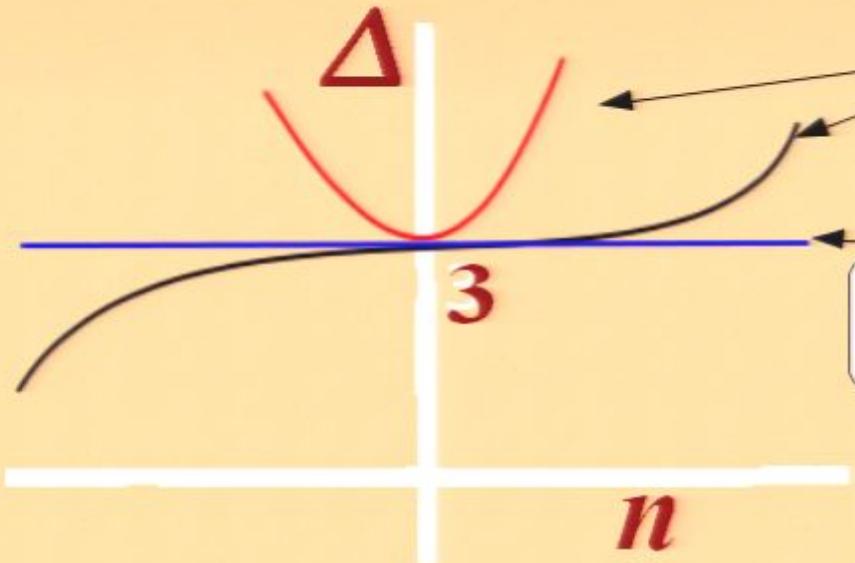
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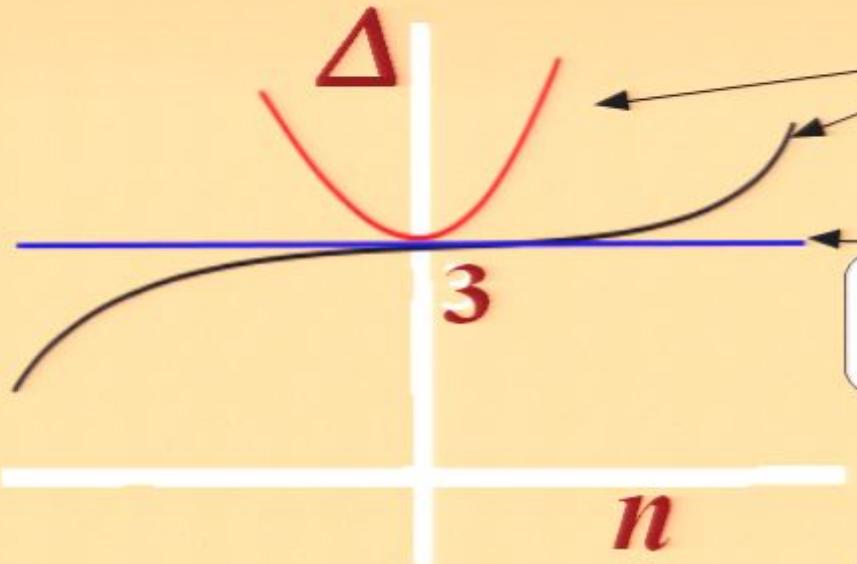
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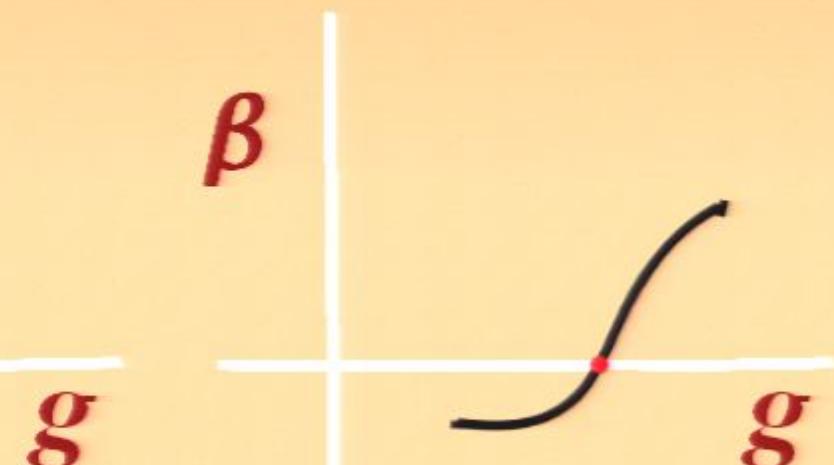
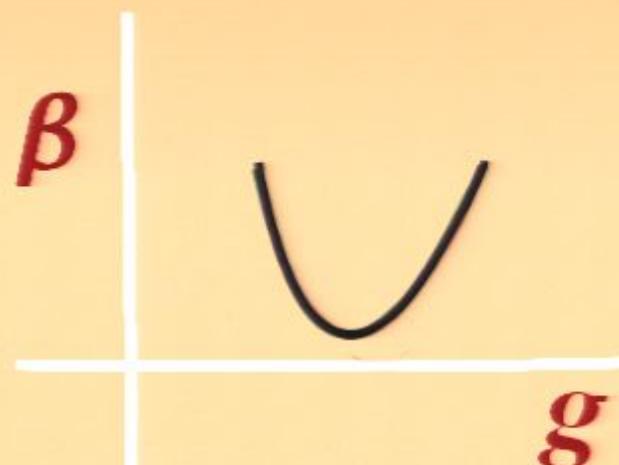
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Three kinds of operators at a conformal fixed point

Relevant

Marginal

Irrelevant



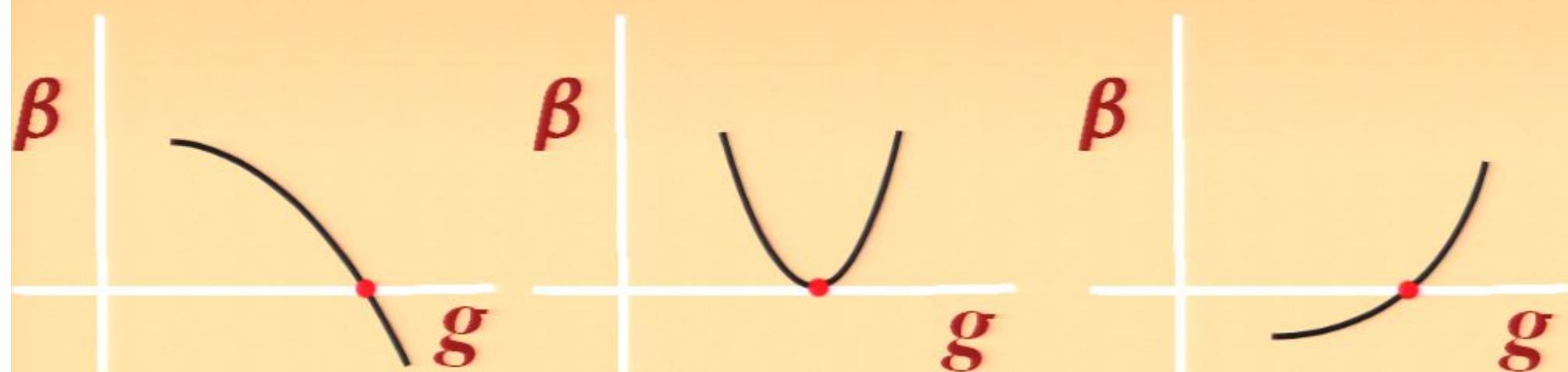
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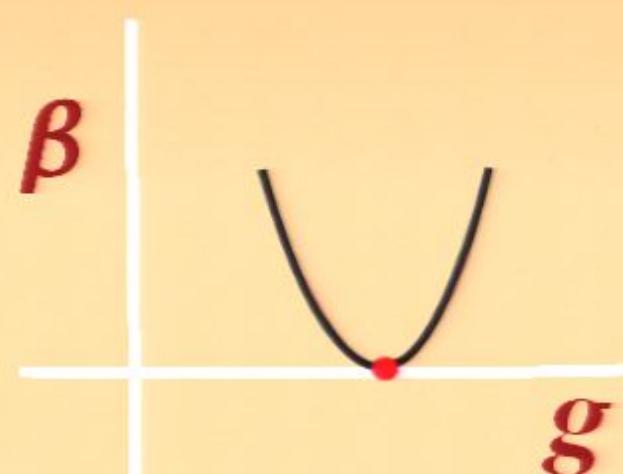
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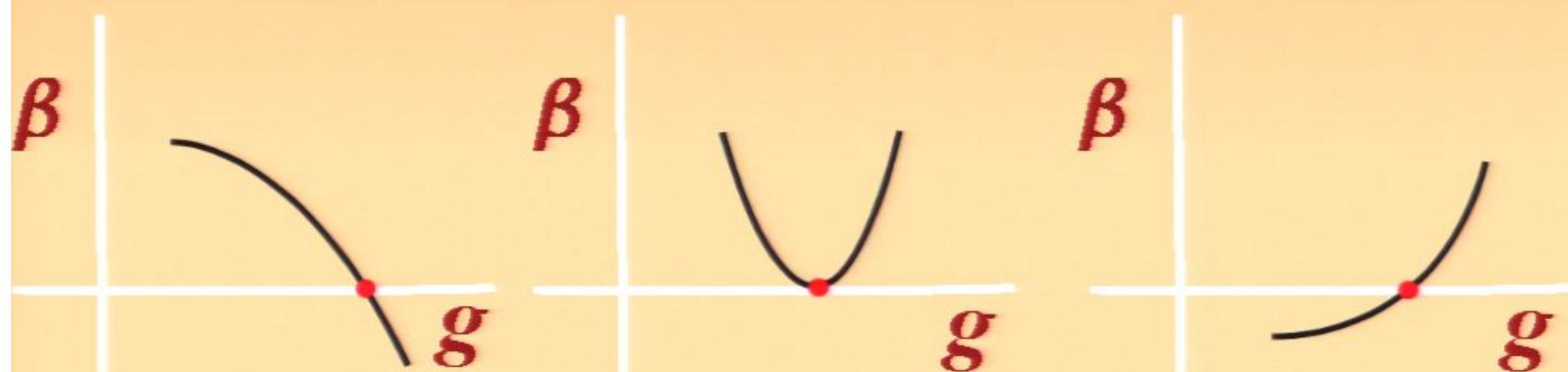
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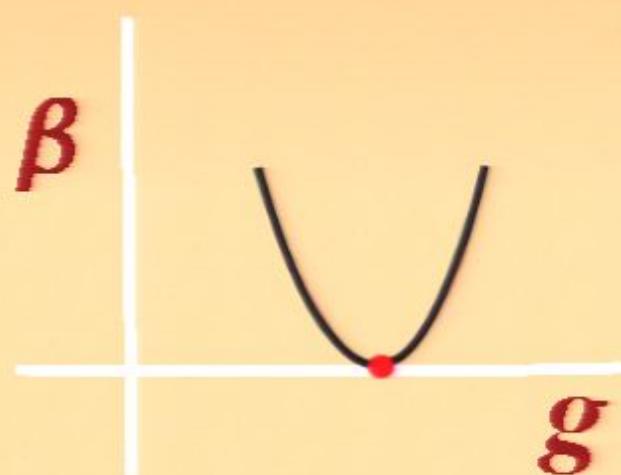
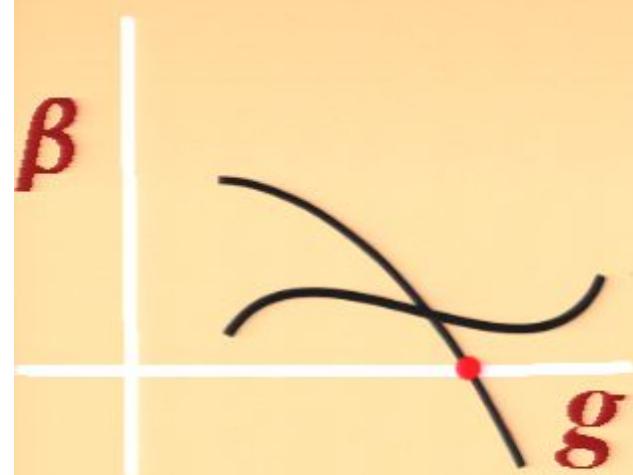
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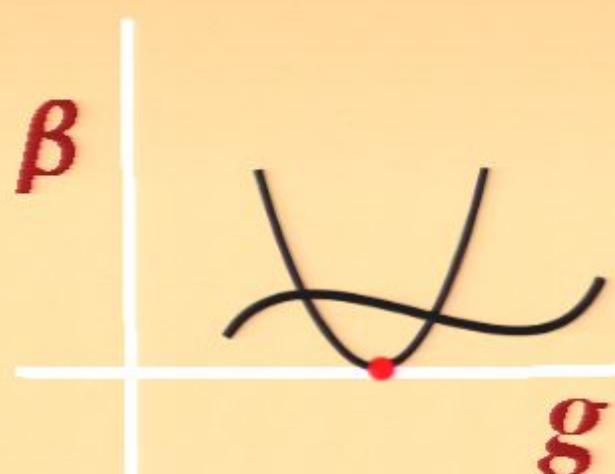
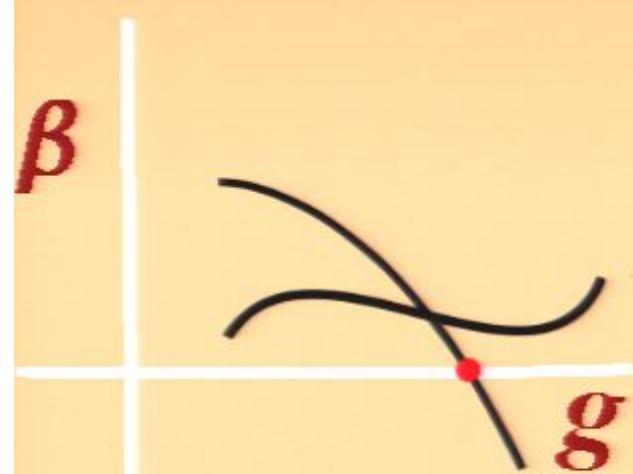
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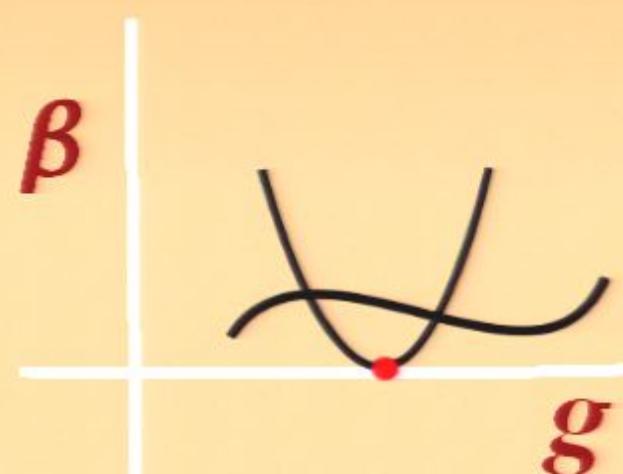
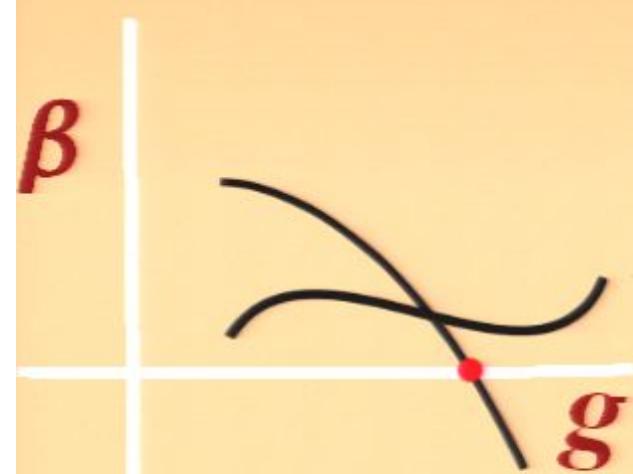
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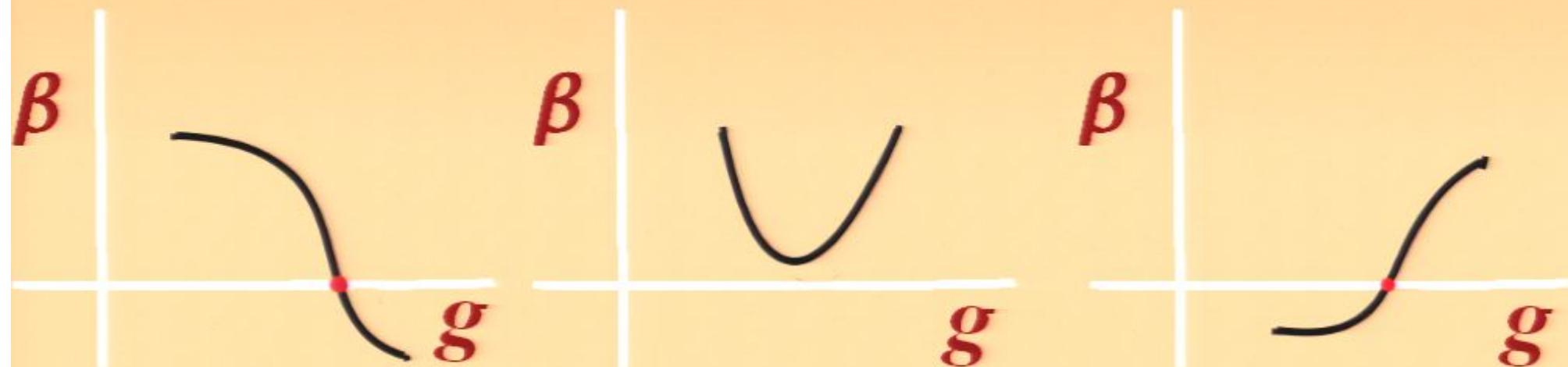
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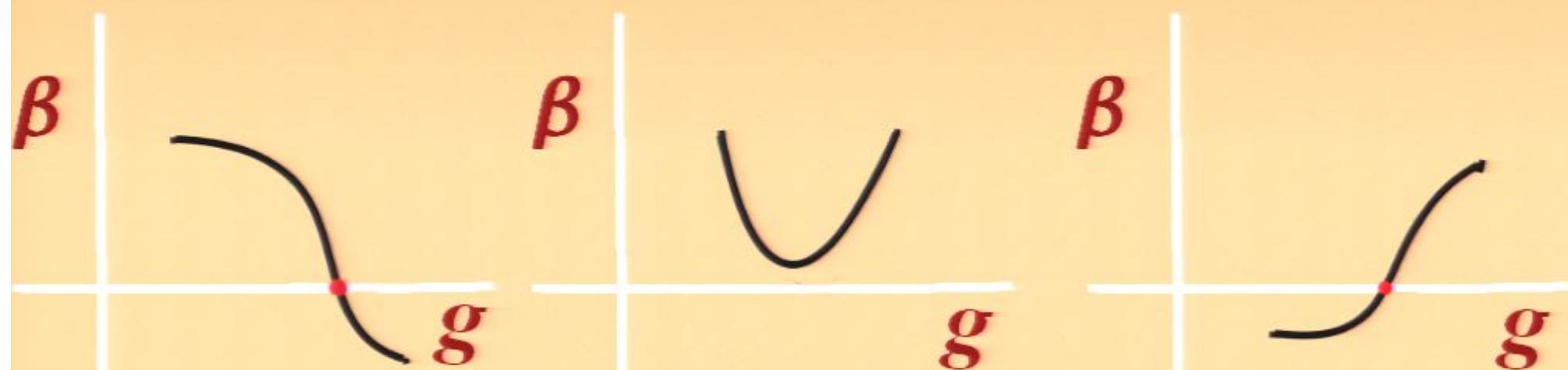
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Marginal operators could destroy conformal fixed points.

$$AdS_5 \times X^5_{\text{non-SUSY}}$$

Pirsa: 08120056

$$\frac{1}{g^2} \text{Tr } F \wedge *F$$

Gauge coupling is always marginal

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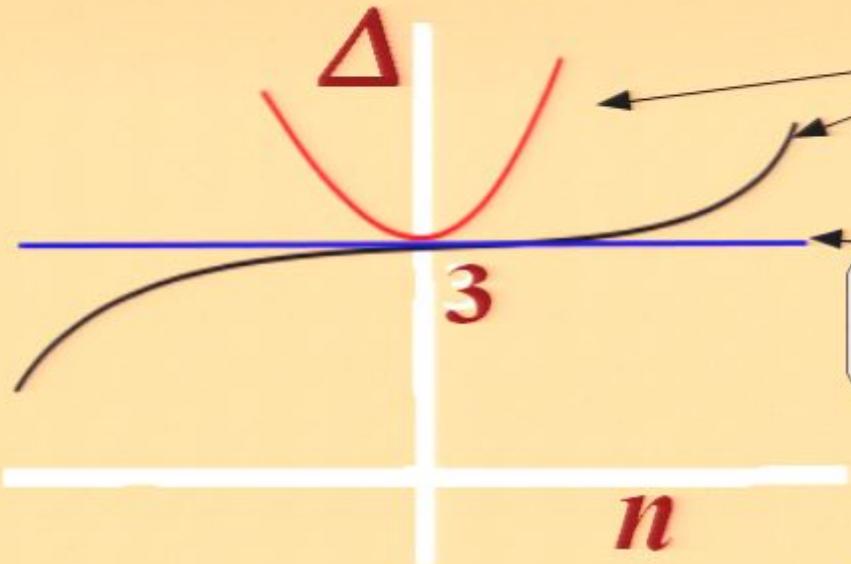
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# Future directions

- Hidden SUSY and monopole operators
- Other interesting vacua of SUGRA
- Rich "landscape" of AdS<sub>4</sub> compactifications.. stable non-SUSY backgrounds?
- Transport coefficients from field theory
- Other condensed matter applications..?