

Title: Clustering in interacting dark energy cosmologies

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Abstract: I will illustrate the case of interacting dark Energy, that is to say cosmologies in which the dark energy scalar field interacts with other things in the universe (gravity, cold dark matter or neutrinos). After briefly presenting the status of our work for the first two classes of models, regarding both linear perturbations and Nbody simulations, I will in particular focus on the case of 'growing neutrinos': in these models, neutrinos with a mass increasing with time might be driven to cluster at very large scales, due to a new interaction stronger than gravity and mediated by the dark energy scalar field.

A cosmic background radiation map showing temperature fluctuations in the universe, with a color scale from dark blue (cooler) to light blue (warmer).

# Clustering in interacting Dark Energy cosmologies

Valeria Pettorino

Institute for Theoretical Physics, Heidelberg

# Overview

- Introduction
- Interacting dark energy
  - Gravity
  - Cold dark matter
  - Neutrinos
- Conclusions and future prospects



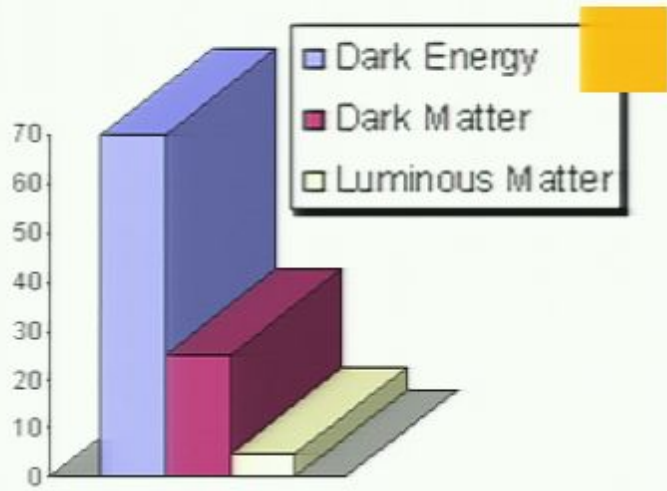
Dark



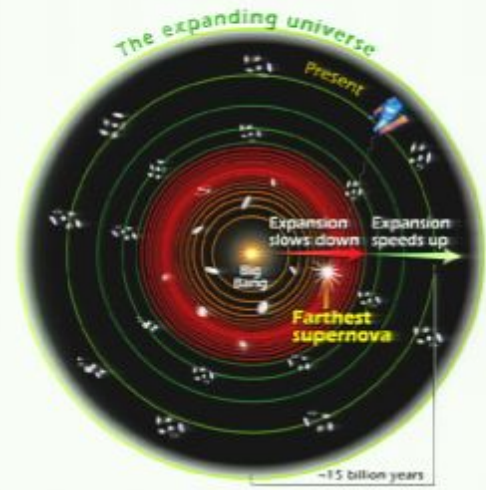
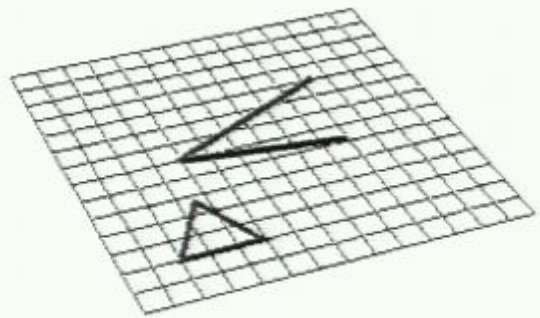
Flat



Accelerating



$$\Omega_{tot} \approx 1$$



# Hopes and troubles

Cosmological constant



Quintessence

Wetterich 1988,  
Ratra & Peebles 1988



Attractor solutions

Steinhardt, Wang and Zlatev 1999,  
Liddle & Scherrer 1999

$$\rho_{\text{DE}}/M^4 \sim 6.5 \times 10^{-121}$$

$$\rho_{\text{m}}/M^4 \sim 3.5 \times 10^{-121}$$

$$M = 2.44 \times 10^{18} \text{ GeV}$$

Why so small?

Why important just today?

Solutions are independent  
on the initial conditions for  
 $\phi$  and  $\phi'$

Details depend on  $V(\phi)$  or on the kinetic term

# Interacting dark energy

The stringent difficulties of quintessence models and the lack of a clear explanation of the dark issue, encourage to pursue new ways of approaching the Dark Energy problem

The interaction keeps the dark energy density closer to matter fields

D  
a  
r  
k  
e  
n  
e  
r  
g  
y



# Interacting Dark Energy

- **Coupling to gravity**

- Cosmological bounds
- role in clustering?

[Boisseau et al 2000]  
[Faraoni 2000]  
[Perrotta, Baccigalupi 2002]  
[Riazuelo Uzan 2002]  
[Pettorino, Baccigalupi 2008]  
and references therein

- **Coupling to dark matter**

- cosmological bounds
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[Wetterich 1995]  
[Amendola 2000, 2004]  
[Mangano Miele Pettorino 2005]  
[Quartin et al 2008]  
[Bean et al 2008]

- **Coupling to neutrinos**

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[Mota, Pettorino, Robbers, Wetterich 2008]

# Interacting Dark Energy

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[Mota, Pettorino, Robbers, Wetterich 2008]



# Generalized theories of...

The temptation to explain the Dark Energy contribution and the cosmological acceleration via a modification of gravity through extensions of General Relativity like scalar tensor theories

A black stick figure is shown from the side, holding a large, red, stylized 'gR' symbol. The 'g' is lowercase and the 'R' is uppercase. The background is a dark blue, textured surface.

**gR**avity

# Extended quintessence

Scalar field

Ricci scalar  $\rightarrow$  metric tensor  $g_{\mu\nu}$

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2\kappa} f(\phi, R) - \frac{1}{2} Z(\phi) g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V(\phi) + \mathcal{L}_{\text{fluid}}[\psi_m; g_{\mu\nu}] \right]$$

$$\kappa = 8\pi G$$

$$F(\phi) \equiv \frac{1}{\kappa} \frac{\partial f}{\partial R}$$

$$Z = 1$$

$$\mathcal{L}_{\text{fluid}} = -i\bar{\psi} g^{\mu\nu} \gamma_\nu \nabla_\mu \psi + m\bar{\psi}\psi$$

The relevant equations change both for the background and for perturbations

Baccigalupi Matarrese Perrotta 2000, Riazuelo Uzan 2002, Bartolo Pietroni 2000...

$$\varphi \rightarrow \varphi + \theta$$

Wetterich 2008



# Weyl scaling

Coupling a scalar field to gravity



GR + coupling to **all matter fields**

$$m(\phi) = m_0 e^{-\frac{\beta}{M}(\phi - \phi_0)}$$



# Weyl scaling

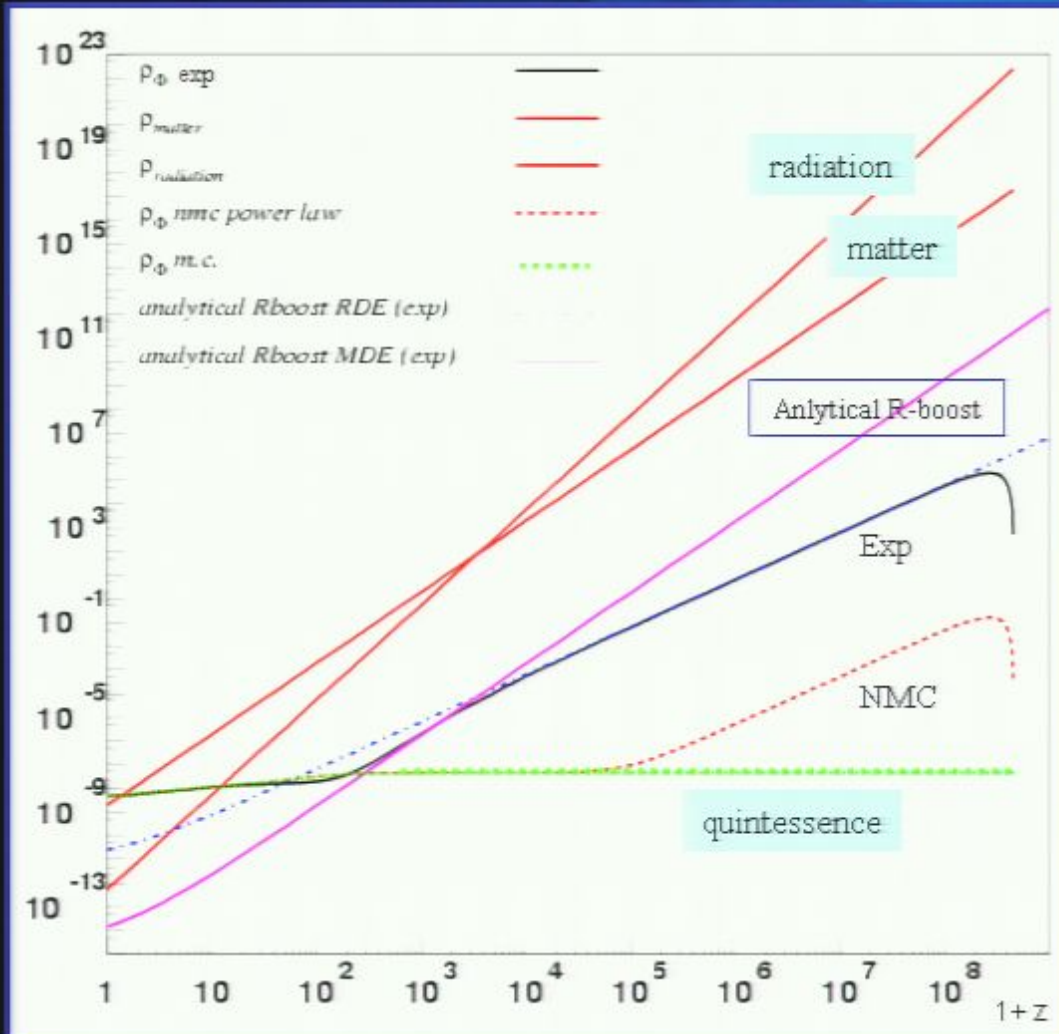
Coupling a scalar field to gravity



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# Background



$$\omega_{JBD} \equiv F \left( \frac{dF}{d\phi} \right)^{-2} = -\frac{1}{\gamma-1} \geq 4 \times 10^4$$

$$\phi'' + 2\mathcal{H}\phi' = \frac{a^2 F_\phi R}{2} - a^2 V_\phi$$

$$R \underset{\text{RDE}}{\cong} \frac{1}{F} \frac{\rho_{matter 0}}{a^3} \neq 0$$

**EXP**

$$\frac{F(\phi)R}{2} = \frac{R}{16\pi G} \exp\left(\frac{\xi(\phi - \phi_0)}{M_p}\right)$$

**NMC**

$$F(\phi)R = \frac{R}{16\pi G} + \xi\phi^2 R$$

Attractor solutions

[Pettorino, Baccigalupi, Mangano 2004]

[Pettorino, Baccigalupi, Perrotta 2005]

# Linear perturbations

Formally the same equations as in GR but...

$$\nabla^2 \Phi_E = -\frac{4\pi G}{F} a^2 \rho_f \delta_f$$

[Pettorino, Baccigalupi 2008]

...with an effective gravitational 'constant'

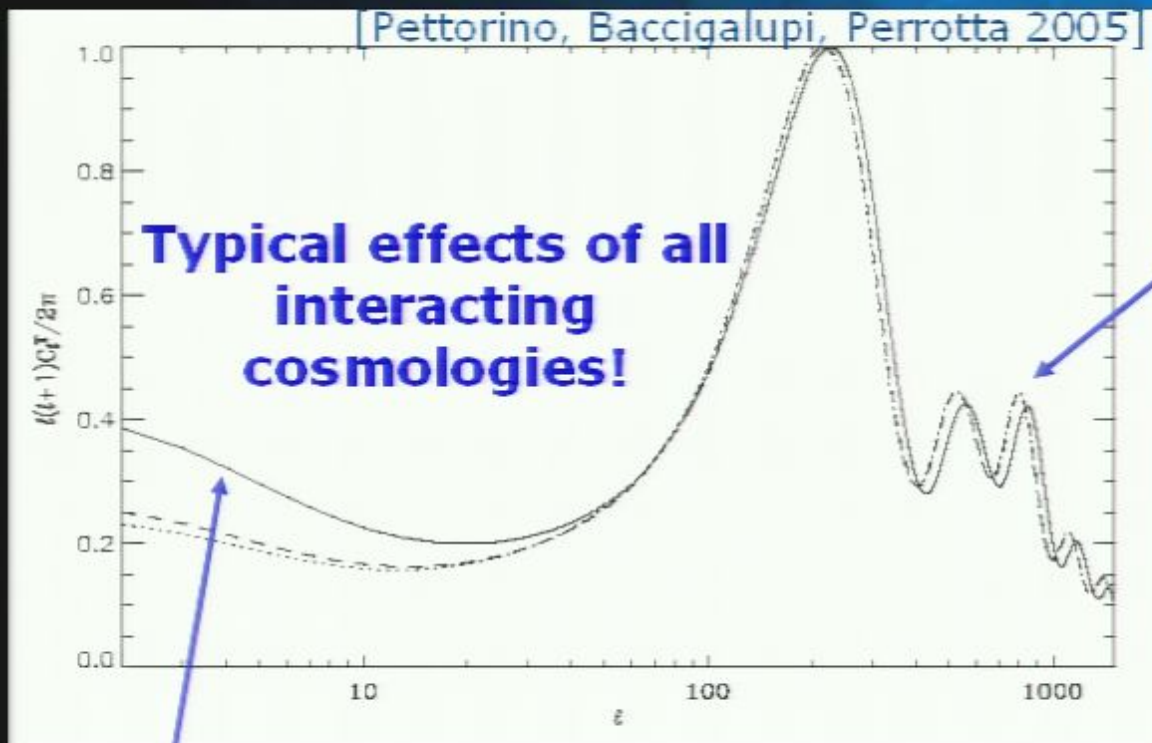
$$\tilde{G} = \frac{2(F + 2F_{,\phi}^2)}{(2F + 3F_{,\phi}^2)} \frac{1}{8\pi F}$$

$$\mathcal{H}^2 = \left(\frac{\dot{a}}{a}\right)^2 = \left(\frac{1}{3F}\right) \left(a^2 \rho_{fluid} + \dots\right)$$

...already visible from the background equations

# Effects on the CMB

The angular scale is proportional to the horizon:  $\theta \propto H^{-1}$



Projection effect

DEfast

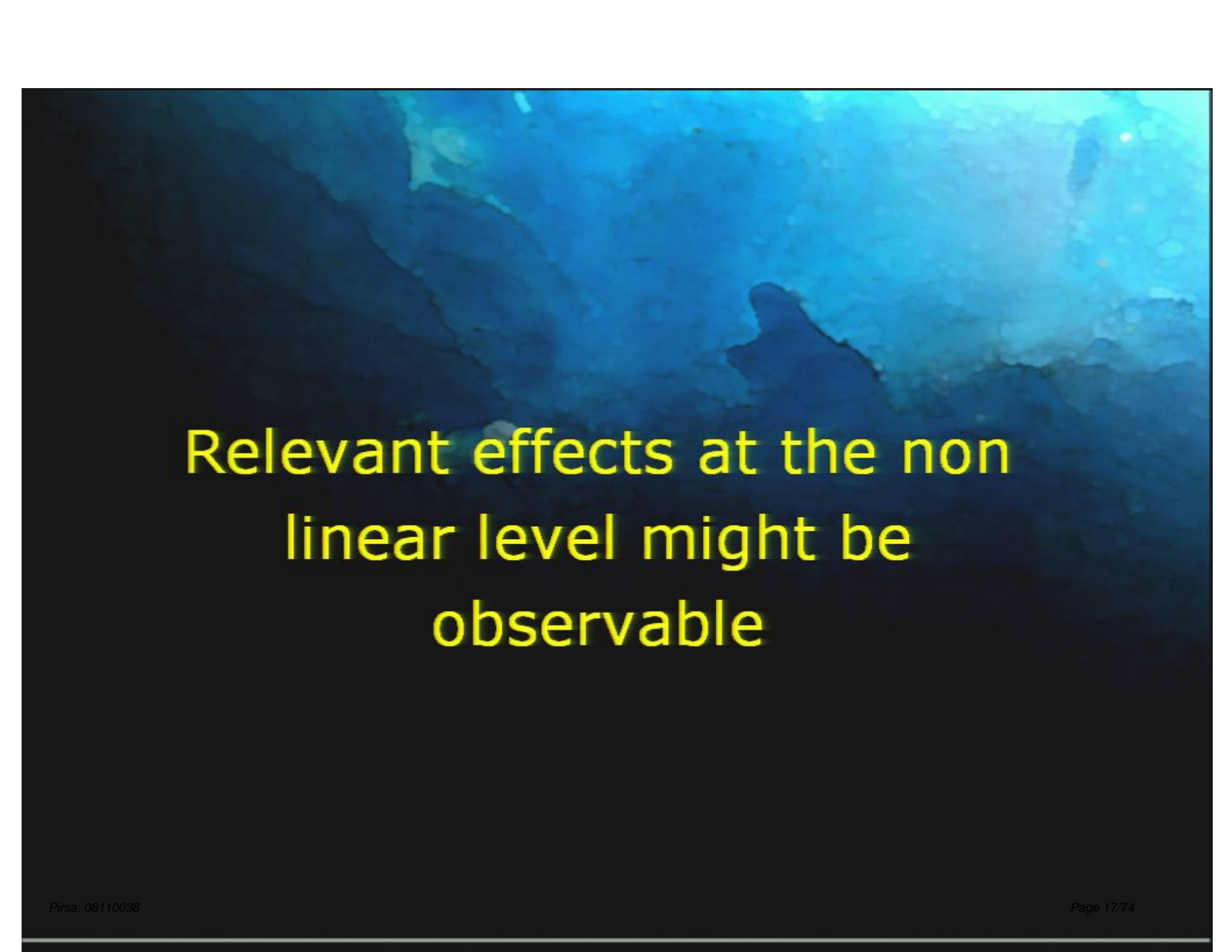
an implementation of CMBfast which allows to study minimal and non-minimal coupled quintessence scenarios.

[Baccigalupi etal 2000]

Larger LISW

It takes into account the gravitational redshift (blueshift) of photons climbing out time varying gravitational potential wells along the line of sight when DE occurs to dominate



The background of the slide is a blue-toned photograph of a mountain range. The mountains are layered, with some in the foreground appearing darker and more silhouetted, while others in the distance are lighter and more detailed. The sky is a bright, clear blue. In the lower foreground, there is a dark silhouette of what appears to be a person or a large rock formation, adding a sense of scale and depth to the scene.

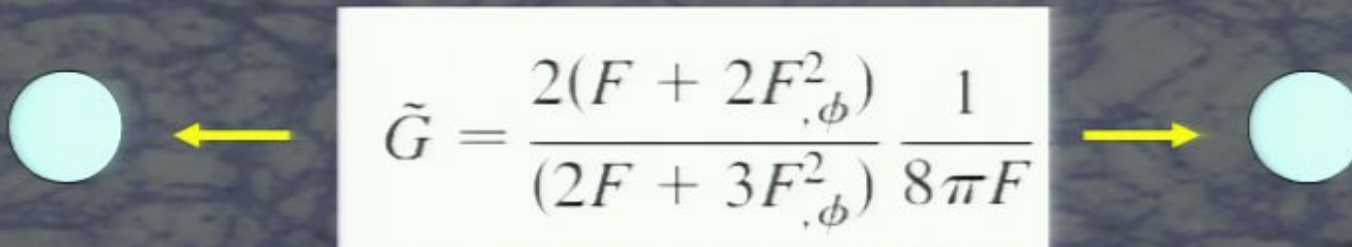
Relevant effects at the non  
linear level might be  
observable

# Nbody simulations for EQ

GADGET [V.Springel 2005] has been implemented:

1. Different background expansion, computed with DEfast
2. Different linear growth factors used to rescale initial conditions
3. Effective gravitational interaction **between all particles**

[Dolag, Pettorino, Moscardini, Baccigalupi, Bartelmann, Meneghetti] in progress


$$\tilde{G} = \frac{2(F + 2F_{,\phi}^2)}{(2F + 3F_{,\phi}^2)} \frac{1}{8\pi F}$$

Hidrodynamical simulations have been carried out

- $L_{box} = 300 \text{ Mpc}/h$ ,  $n_p = 2 \times 768^3$ ,  $\epsilon_G = 7.5 \text{ kpc}/h$   
 $\Rightarrow m_{DM} = 3.7 \times 10^9 M_{\odot}/h$  and  $m_{gas} = 7.3 \times 10^8 M_{\odot}/h$

Data analysis in progress!

# Conclusions for Extended Quintessence

- Attractor properties due to a gravitational effect
- Two main effects on CMB (difficult to see within bounds!)
- Nbody simulations with:
  - dynamical gravitational 'constant' felt by all particles

D  
a  
r  
k  
e  
n  
e  
r  
g  
y



# Coupled quintessence

D  
a  
r  
k  
m  
a  
t  
t  
e  
r



Coupled  
quintessence

=

quintessence

+

cdm (only)

D  
a  
r  
k  
e  
n  
e  
r  
g  
y



D  
a  
r  
k  
m  
a  
t  
t  
e  
r



# Background

Consider dark energy as a quintessence scalar field

$$\rho_\phi = \frac{\dot{\phi}^2}{2a^2} + V(\phi)$$

[Ratra and Peebles 1988]  
[Wetterich 1988]

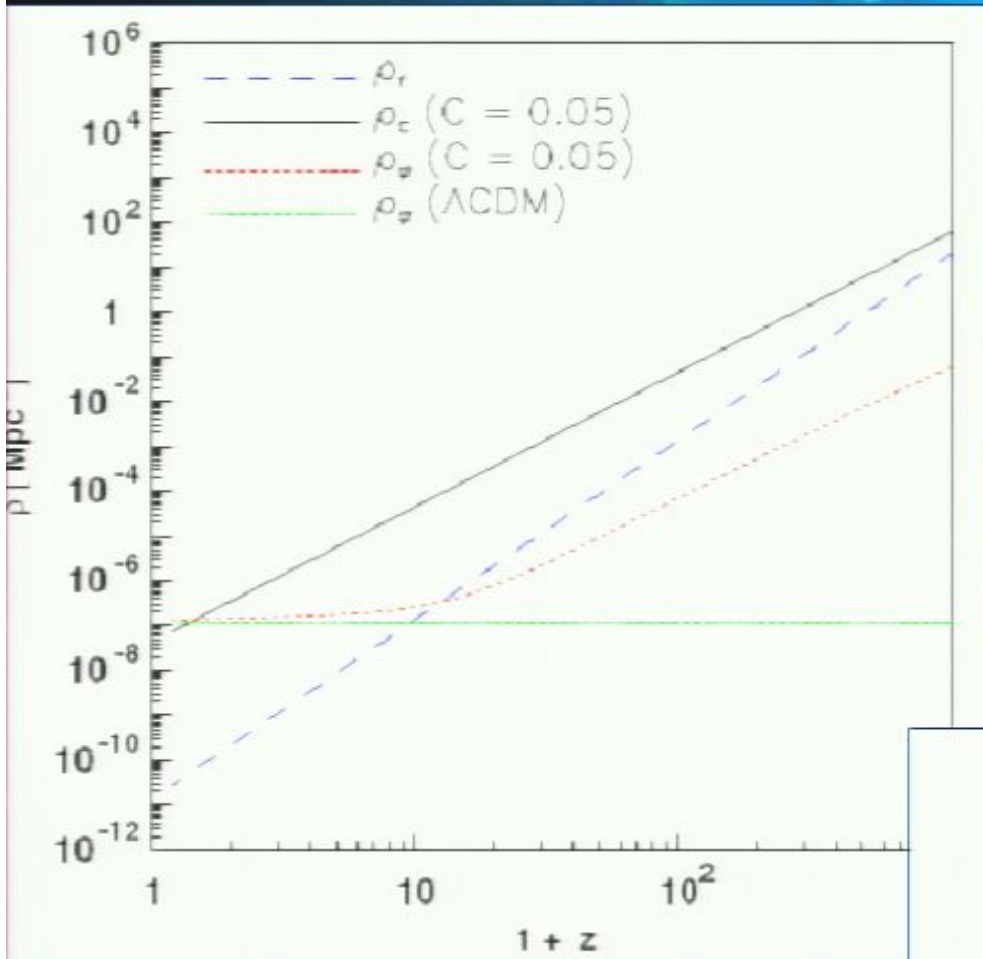
coupled to a species whose mass is now function of  $\phi$

$$m_c = \bar{m} e^{-\tilde{\beta}\phi}$$

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2\kappa} R - \frac{1}{2} \phi^{;\mu} \phi_{;\mu} - U(\phi) - m(\phi) \bar{\psi} \psi + \mathcal{L}_{\text{kin}, \psi} \right]$$

$$\beta(\phi) \equiv - \frac{d \ln m_c}{d\phi}$$

[Wetterich 1995]  
[Amendola 2000, 2004]  
[Mangano, Miele, Pettorino 2005]

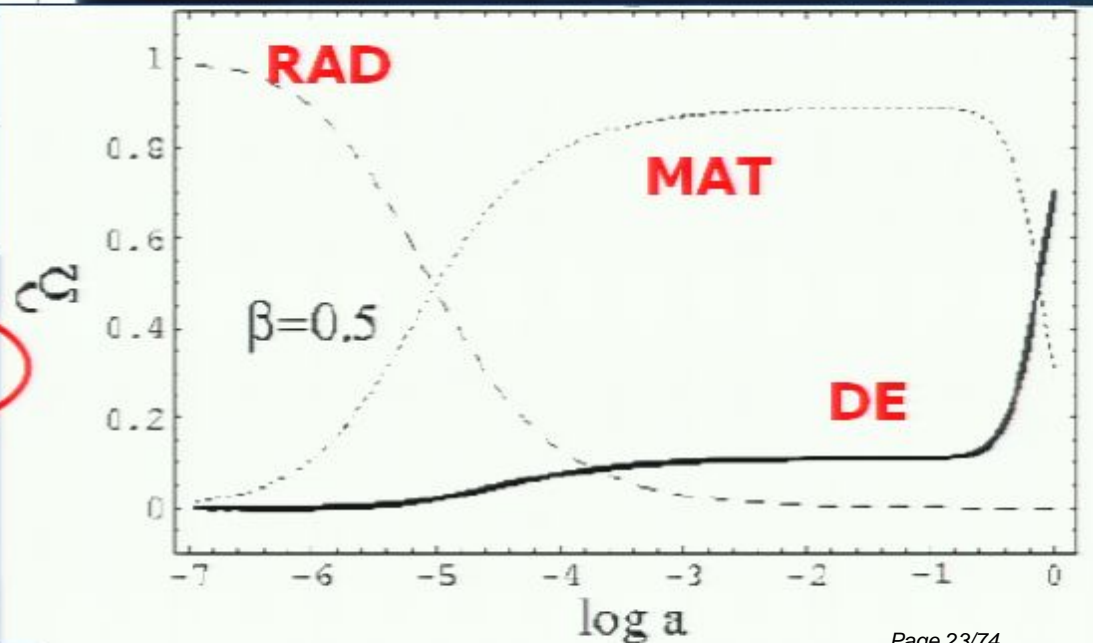


Pattern for the background similar to extended quintessence

Non negligible amount of dark energy in the past

$$\rho'_\phi = -3\mathcal{H}(1 + w_\phi)\rho_\phi + \beta(\phi)\phi' \rho_c$$

$$\rho'_c = -3\mathcal{H}\rho_c - \beta(\phi)\phi' \rho_c$$



# Linear perturbations

$$\begin{aligned}\delta\rho'_\phi + 3\mathcal{H}(\delta\rho_\phi + \delta p_\phi) + kh_\phi v_\phi + 3h_\phi\Phi' &= \frac{\beta(\phi)}{M}\rho_c\delta\phi' + \frac{\beta(\phi)}{M}\phi'\delta\rho_c + \frac{\beta_{,\phi}}{M}\phi'\delta\phi\rho_c \\ \delta\rho'_c + 3\mathcal{H}\delta\rho_c + k\rho_c v_c + 3\rho_c\Phi' &= -\frac{\beta(\phi)}{M}\rho_c\delta\phi' - \frac{\beta(\phi)}{M}\phi'\delta\rho_c - \frac{\beta_{,\phi}}{M}\phi'\delta\phi\rho_c \\ h_\phi v'_\phi + (h'_\phi + 4\mathcal{H}h_\phi)v_\phi - k\delta p_\phi - kh_\phi\Psi &= k\frac{\beta(\phi)}{M}\rho_c\delta\phi \\ v'_c + \left(\mathcal{H} - \frac{\beta(\phi)}{M}\phi'\right)v_c - k\Psi &= -k\frac{\beta(\phi)}{M}\delta\phi\end{aligned}$$



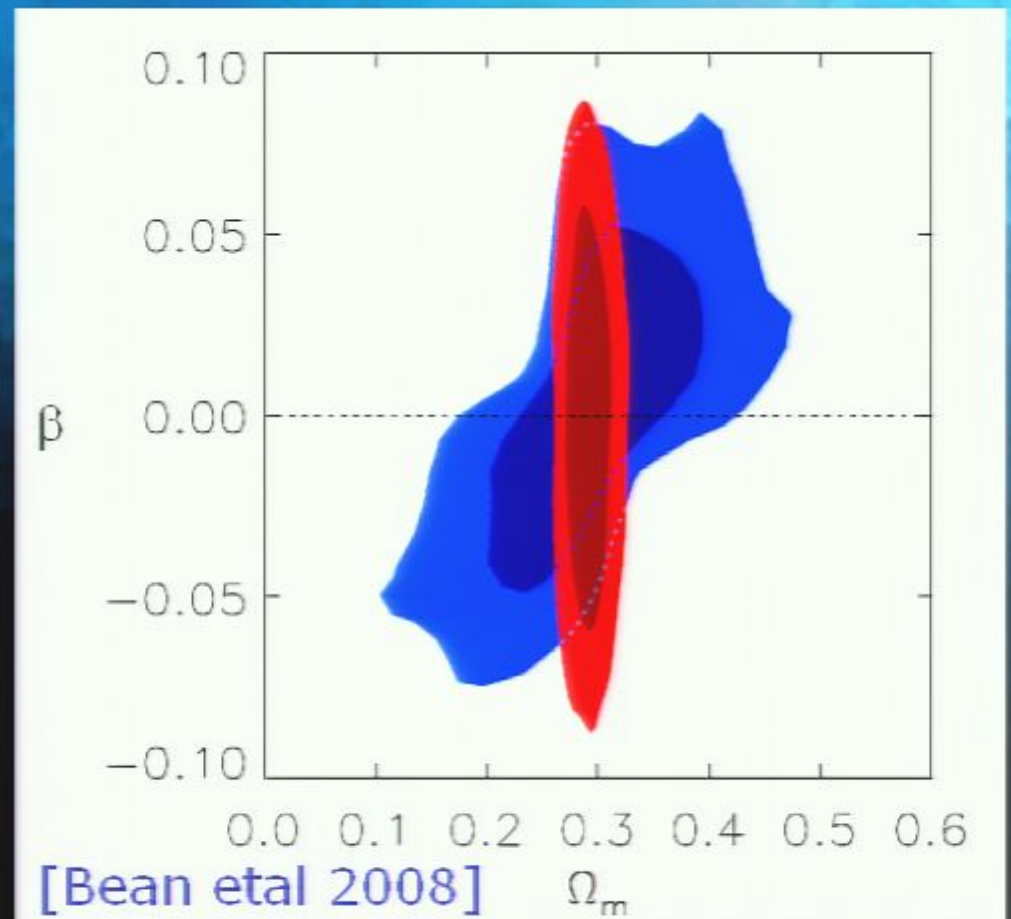
# CMB constraints

Constraints to the coupling from CMB data  $\beta \leq 0.1$  (for a constant coupling)

[Bean etal 2008]



**WARNING:**  
constraints for constant  
coupling models



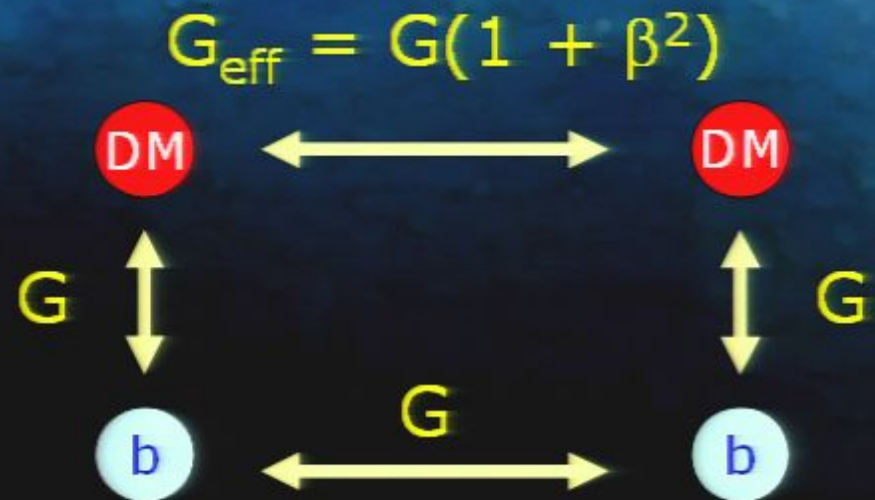
Implementation of CMBEASY  
to include general coupling  
mass function  $m(\phi)$

Monte Carlo analysis in progress!  
[Robbers, Pettorino]

# Recipe for N-body codes

Extra interaction between cdm particles, mediated by the quintessence scalar field

1. Effective **gravitational interaction** between DM particles
2. The **mass** of DM particles varies
3. An extra **friction** term is present



$$\delta_c'' + (\mathcal{H} - \beta\phi')\delta_c' - \frac{3}{2}\mathcal{H}^2 [(1 + 2\beta^2)\Omega_c\delta_c + \Omega_b\delta_b] = 0$$

# Nbody simulations for CQ

M. Baldi, V. Pettorino, G. Robbers  
in preparation, very soon to come!

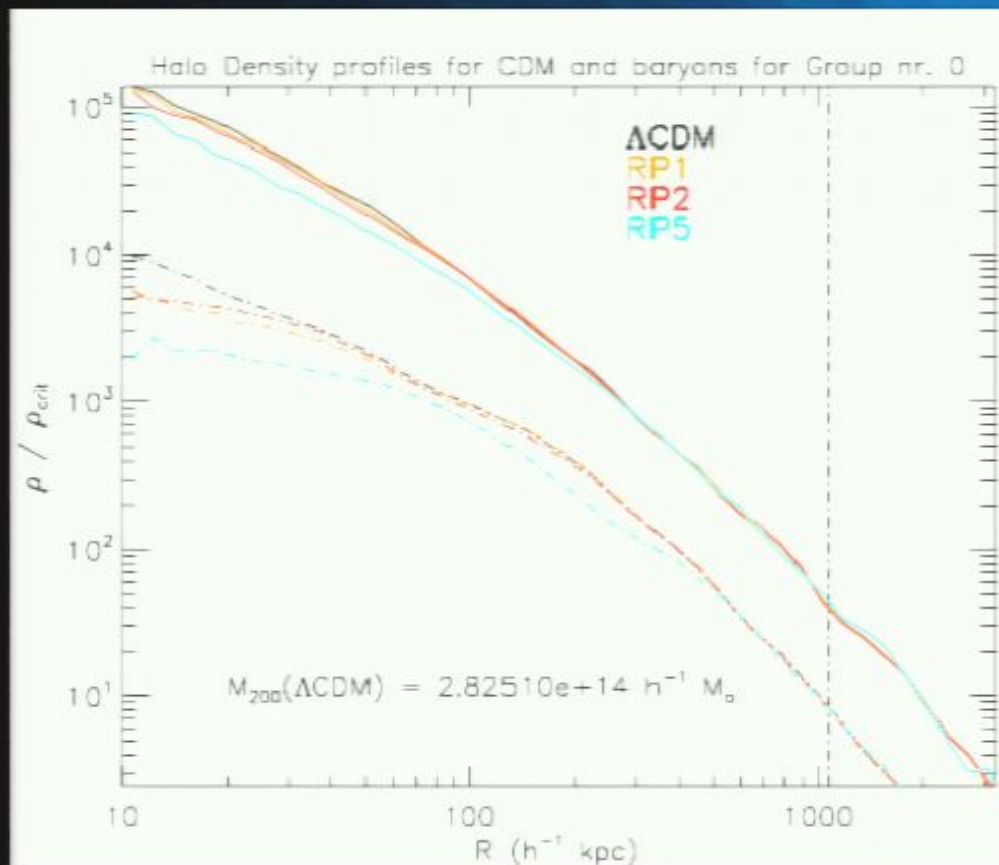
$L_{\text{box}} = 80 \text{ h}^{-1} \text{ Mpc}$	$m_c(z=0) \sim 2 \cdot 10^8 \text{ h}^{-1} M_{\odot}$
$N = 2 \times 512^3$	$m_b \sim 5 \cdot 10^7 \text{ h}^{-1} M_{\odot}$
$\epsilon_g = 3.5 \text{ h}^{-1} \text{ kpc}$	$z_i = 60$

All the corrections have been implemented in GADGET

[V. Springel 2005]

- Less steep density profiles
- Lower halo concentrations
- Scale dependent bias between baryons and cdm

# Results: density profiles



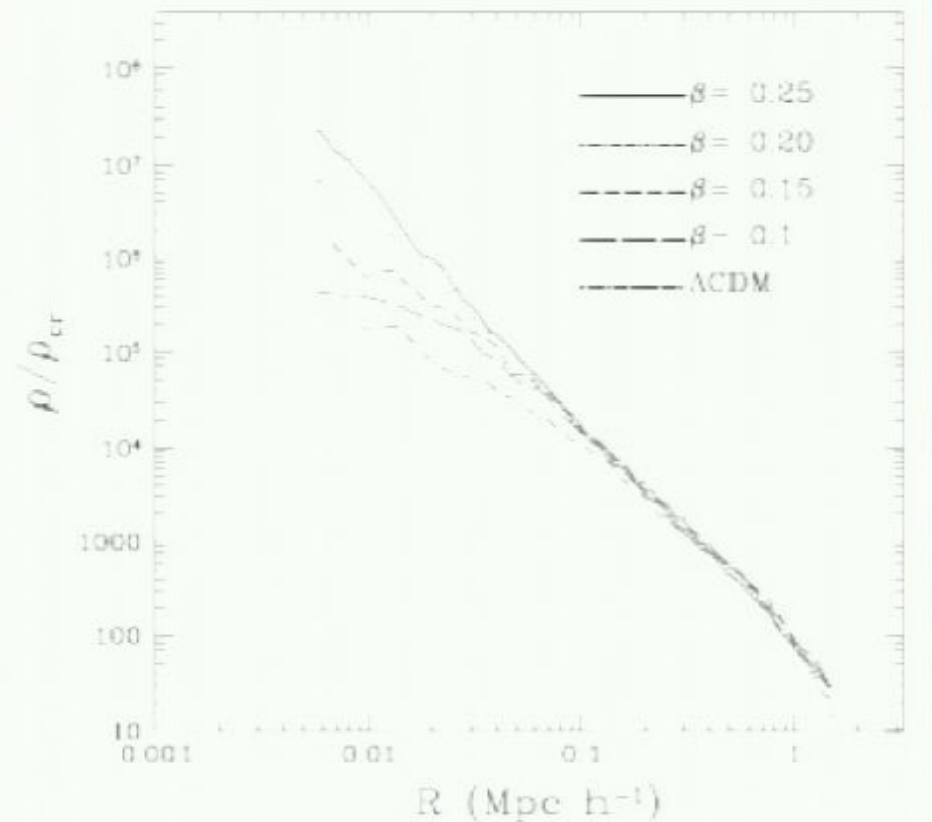
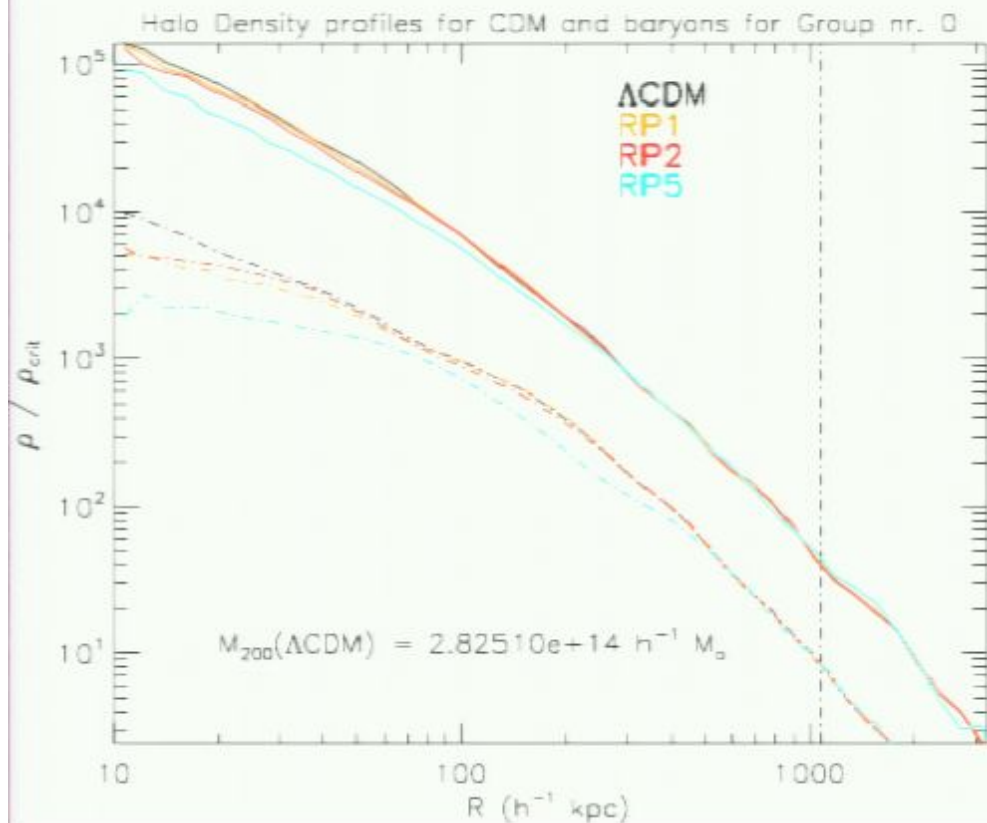
The inner density decreases with increasing coupling both for cdm and for baryons

Results in contrast with Macciò et al 2004

Baldi Pettorino Robbers  
in preparation



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Baldi Pettorino Robbers  
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Macciò etal 2004

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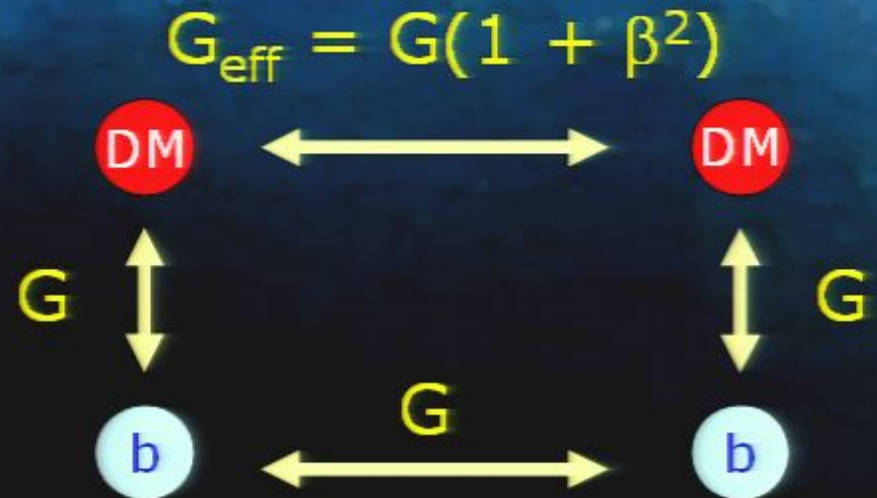
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# Recipe for N-body codes

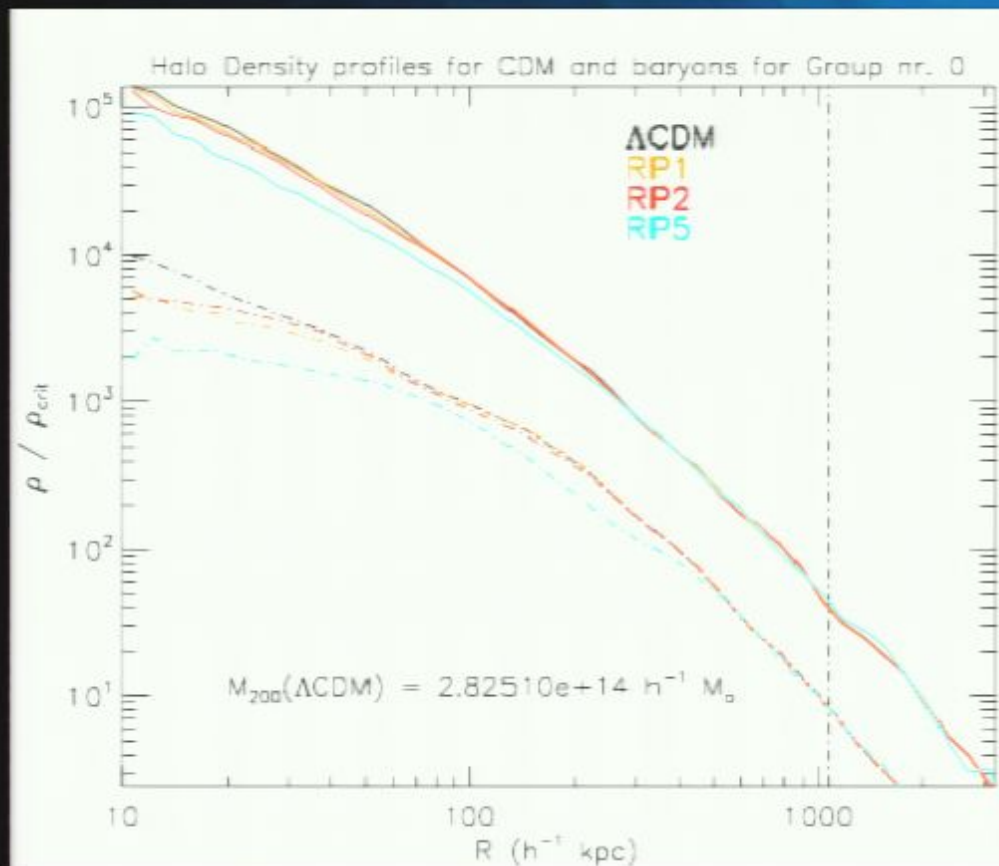
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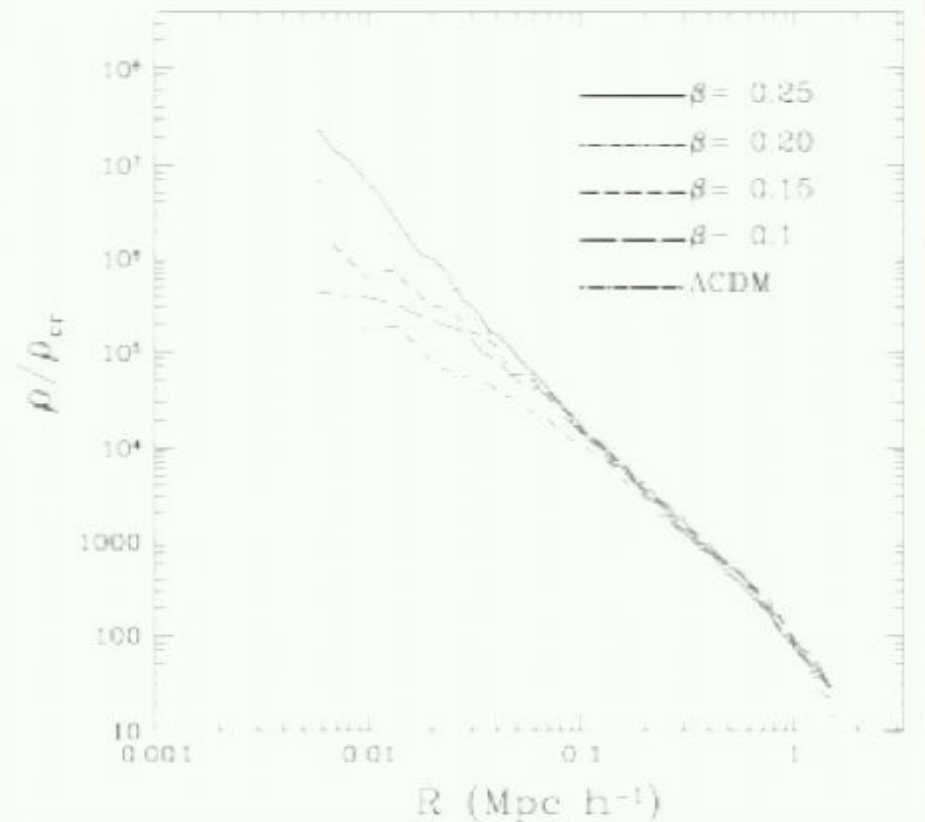
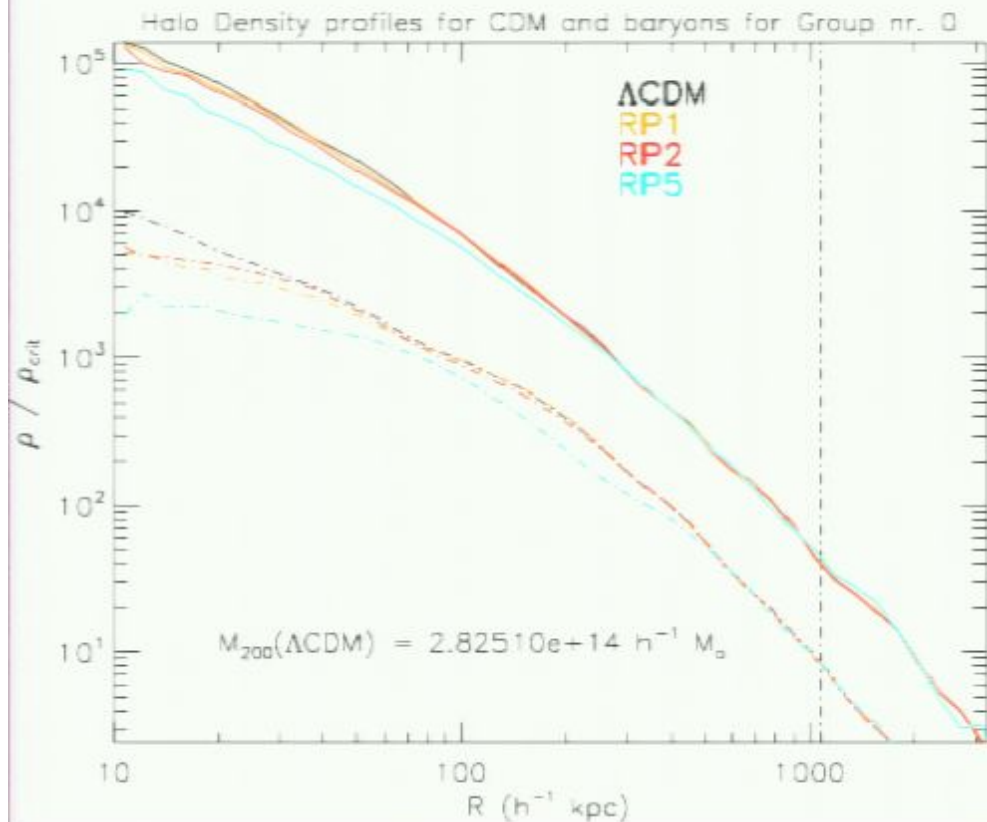
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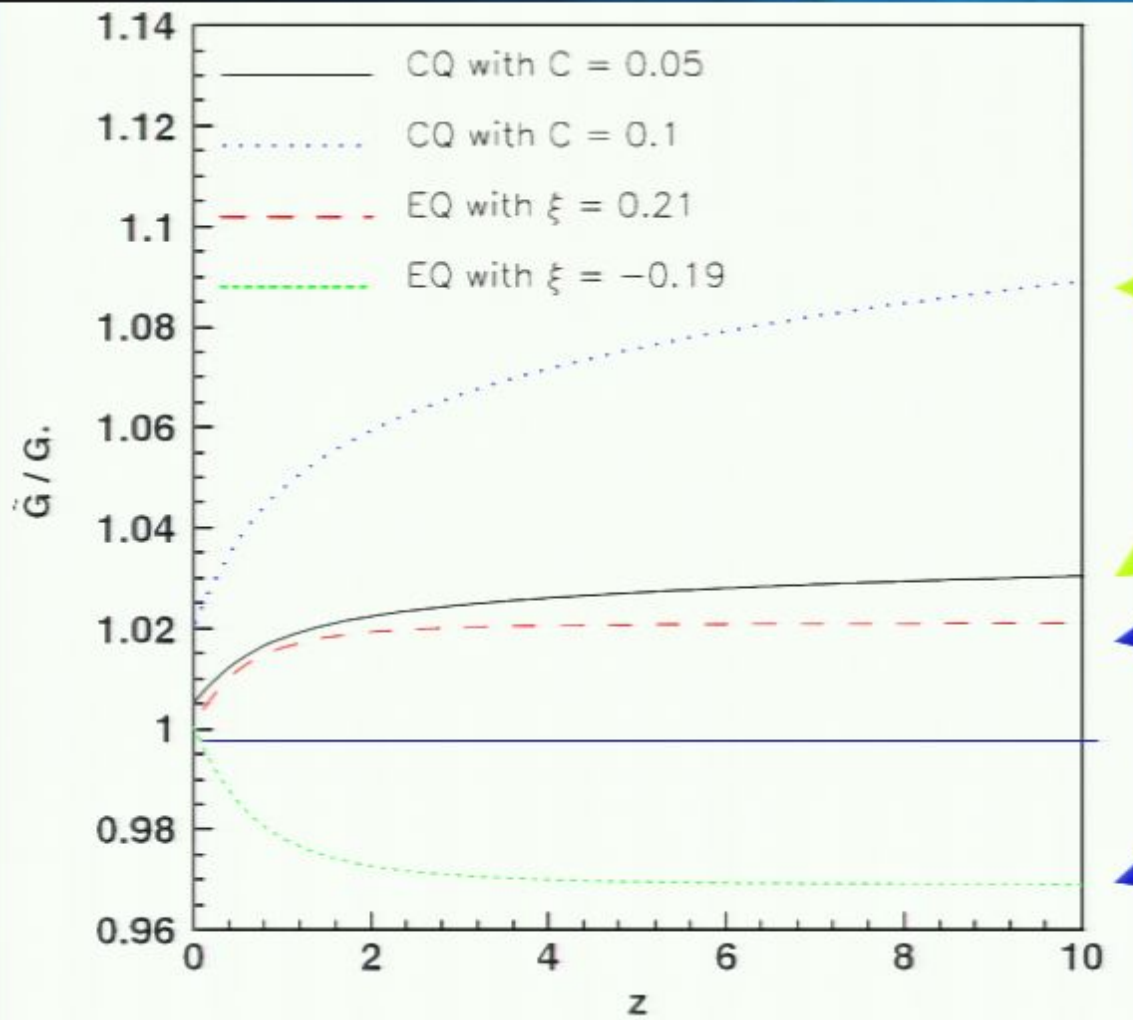
# Results: density profiles



Baldi Pettorino Robbers  
in preparation

Macciò et al 2004

Note that...



$\beta^2$

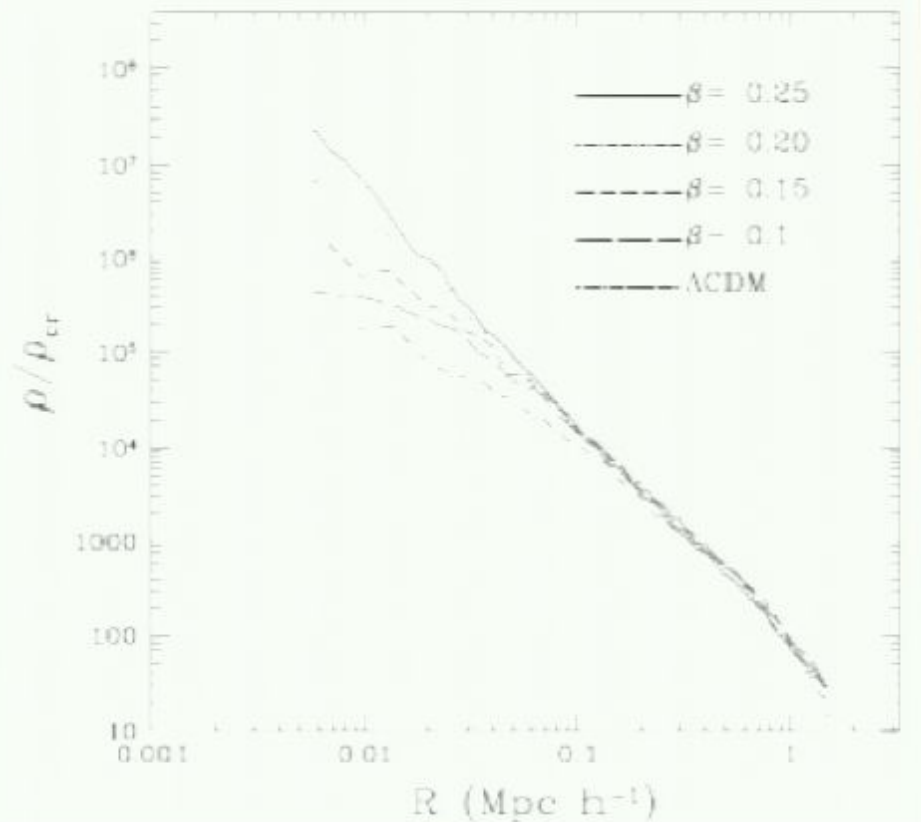
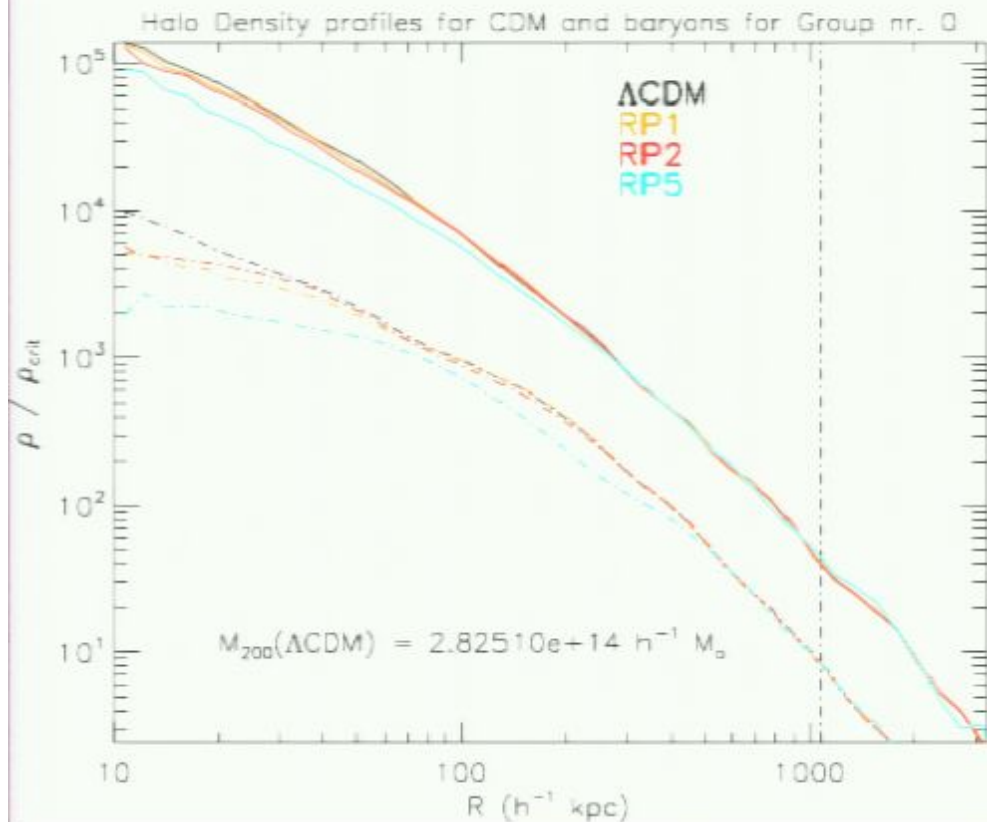
$\xi > 0$

$\xi < 0$

[Pettorino, Baccigalupi 2008]

In constant coupling CQ the effective gravitational constant is always stronger than G

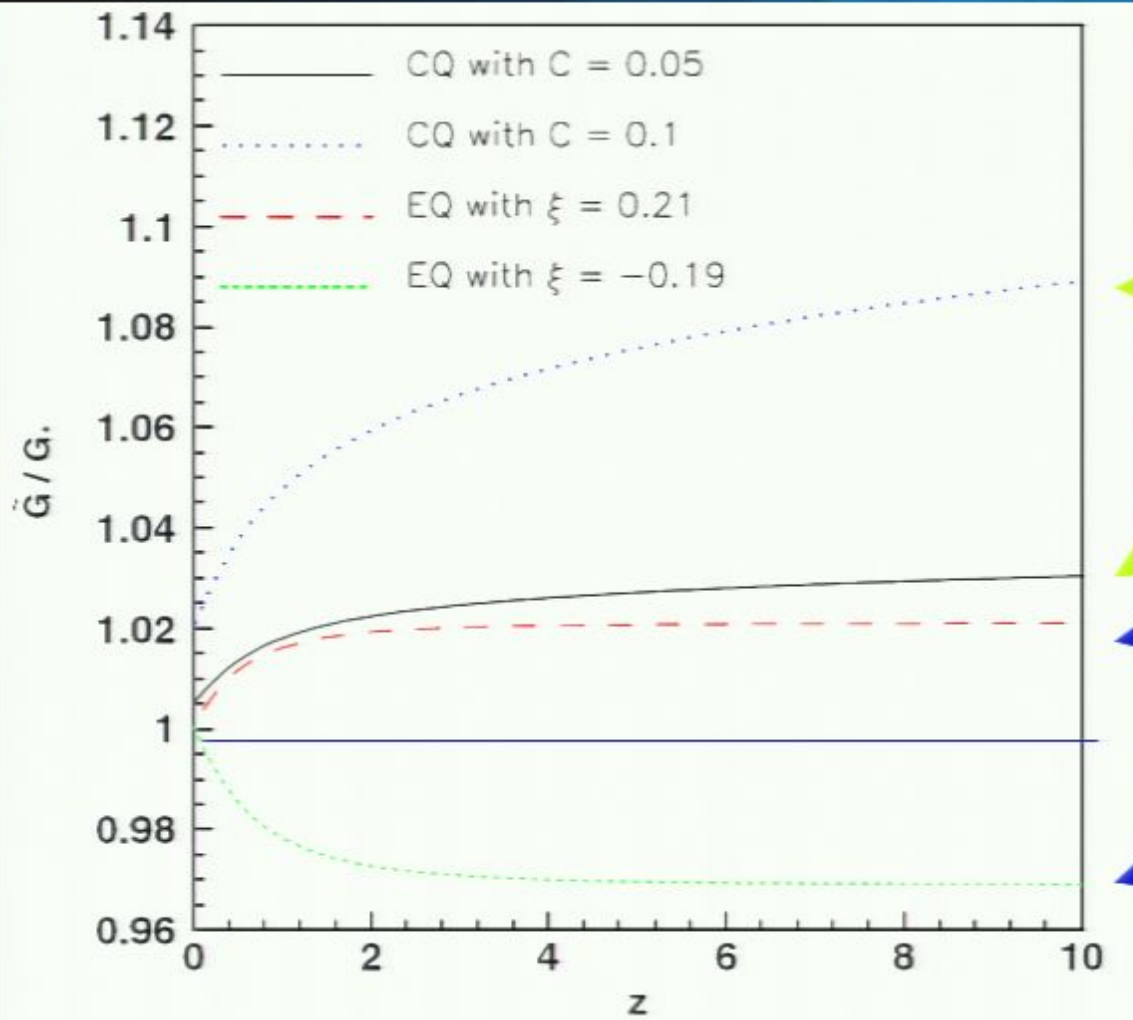
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Note that...



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[Pettorino, Baccigalupi 2008]

In constant coupling CQ the effective gravitational constant is always stronger than G

# Conclusions for Quintessence - CDM

- Interaction keeps DE and DM closer in the background evolution
- Attractor solutions
- Constrains by CMB
- Three features implemented in the Nbody code:
  - bigger gravitational 'constant' felt by DM particles
  - varying mass of DM
  - extra friction term in the direction of the velocity
- Three main results:
  - less clumpy inner profiles, smaller halo concentrations, scale dependent bias

The background of the slide is a Cosmic Microwave Background (CMB) fluctuation map, showing a complex pattern of blue and white tones representing temperature variations across the sky. The map is centered on the slide, with the text overlaid in the lower-middle portion.

# Growing neutrino quintessence

# Interaction with neutrinos

## Coupling to neutrinos

can have a significant influence in cosmology  
(Wetterich 2007)

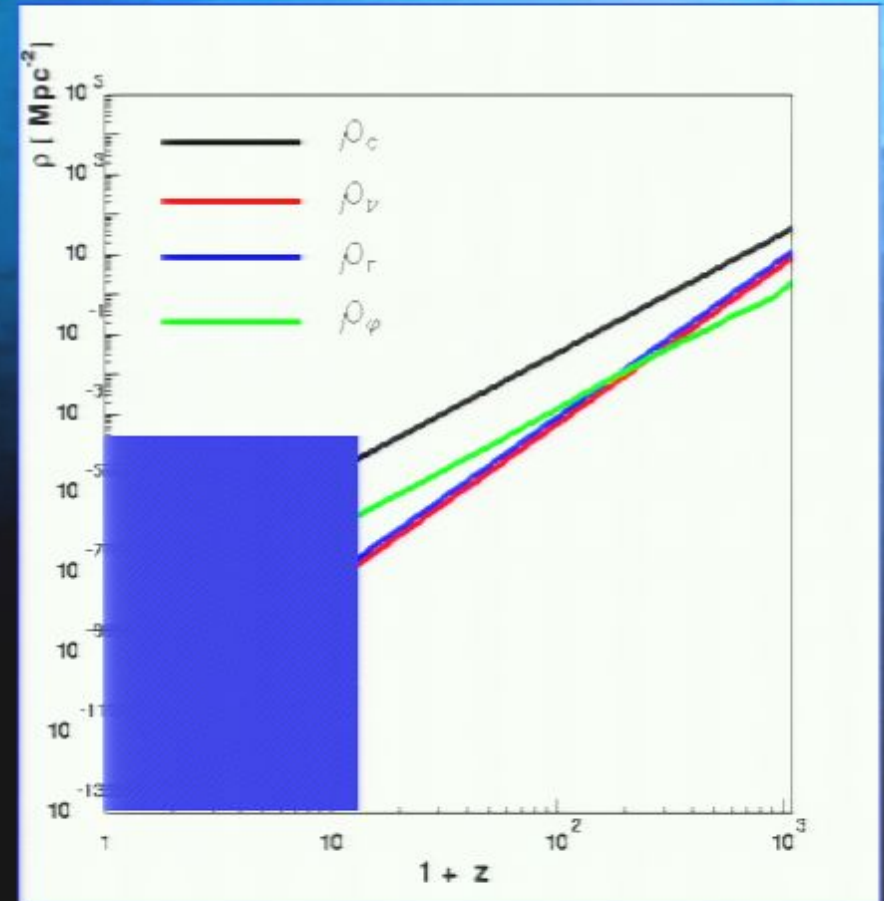


**MAVANS:** Fardon etal 2004, Afshordi etal 2005, Bjaelde etal 2008, Brookfield etal 2007, ...

**Growing neutrinos:** Amendola etal 2007, Wetterich 2007, Mota etal 2008, Brouzakis etal 2007

# Exponential potential

- $V(\phi) = M^4 \exp(-\alpha\phi)$
- Solutions independent of the initial conditions
- DE scales as a constant fraction tracking the background:  
 $\Omega_\phi = n/\alpha^2$   
with  $n = 3(4)$  in MDE (RDE)

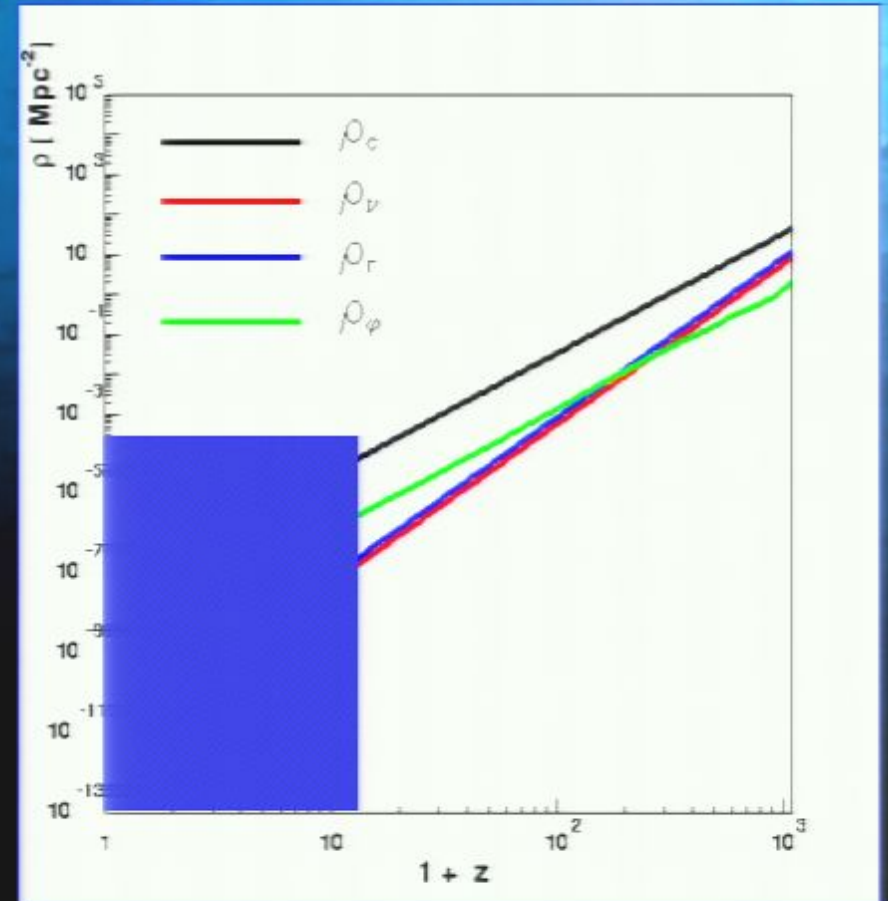


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Need a cosmological event that triggers the end of the attractor era

# Neutrinos become non relativistic

Attractor with constant fraction of DE + coupling

$$\rho'_\phi = -3\mathcal{H}(1 + w_\phi)\rho_\phi + \beta(\phi)\phi'(1 - 3w_\nu)\rho_\nu$$

$$\rho'_\nu = -3\mathcal{H}(1 + w_\nu)\rho_\nu - \beta(\phi)\phi'(1 - 3w_\nu)\rho_\nu$$

$$\phi'' + 2\mathcal{H}\phi' + a^2 \frac{dU}{d\phi} = a^2 \beta(\phi)(\rho_\nu - 3p_\nu)$$

$$\beta(\phi) \equiv -\frac{d \ln m_\nu}{d\phi}$$

$$m_\nu = \bar{m}_\nu e^{-\tilde{\beta}(\phi)\phi}$$

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Neutrino mass grows ( $\beta < 0$ )

$$m_\nu = \bar{m}_\nu e^{-\tilde{\beta}(\phi)\phi}$$

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Neutrino mass grows ( $\beta < 0$ )

$$m_\nu = \bar{m}_\nu e^{-\tilde{\beta}(\phi)\phi}$$

Neutrinos become non relativistic

The coupling to DE turns on and almost stops  $\phi$

# Neutrinos become non relativistic

Attractor with constant fraction of DE + coupling

$$\begin{aligned}\rho'_\phi &= -3\mathcal{H}(1+w_\phi)\rho_\phi + \beta(\phi)\phi'(1-3w_\nu)\rho_\nu \\ \rho'_\nu &= -3\mathcal{H}(1+w_\nu)\rho_\nu - \beta(\phi)\phi'(1-3w_\nu)\rho_\nu\end{aligned}$$

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Neutrino mass grows ( $\beta < 0$ )

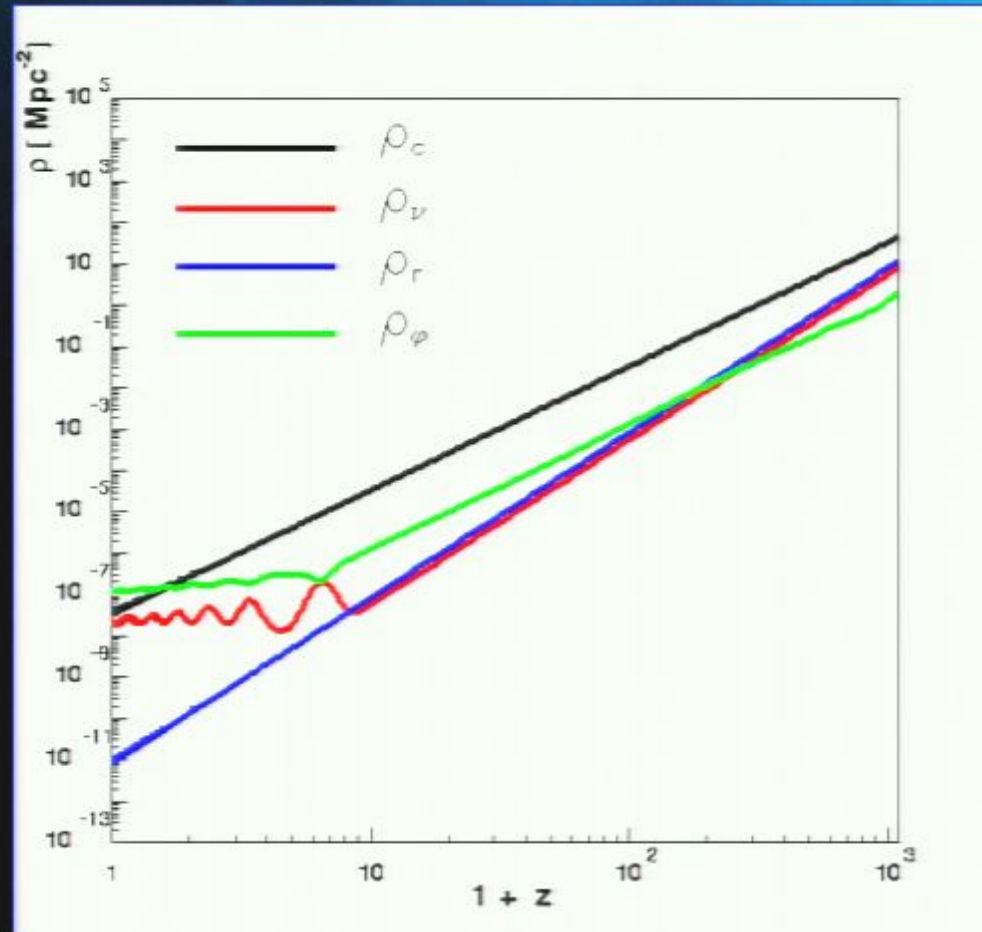
$$m_\nu = \bar{m}_\nu e^{-\tilde{\beta}(\phi)\phi}$$

Neutrinos become non relativistic

The coupling to DE turns on and almost stops  $\phi$

Acceleration

# Coupling Dark Energy to neutrinos



# Dark energy - neutrino connection

- Dark energy and neutrino properties are related

$$\Omega_h(t_0) \approx \frac{\gamma m_\nu(t_0)}{16eV}$$

The present amount of DE is set by a cosmological event and not by ground state properties

$$\gamma = -\frac{\beta}{\alpha}$$

DE- $\nu$  fluid equation of state

$$w_0 \approx -1 + \frac{m_\nu(t_0)}{12eV}$$



# Neutrinos become non relativistic

Attractor with constant fraction of DE + coupling

$$\begin{aligned}\rho'_\phi &= -3\mathcal{H}(1+w_\phi)\rho_\phi + \beta(\phi)\phi'(1-3w_\nu)\rho_\nu \\ \rho'_\nu &= -3\mathcal{H}(1+w_\nu)\rho_\nu - \beta(\phi)\phi'(1-3w_\nu)\rho_\nu\end{aligned}$$

$$\phi'' + 2\mathcal{H}\phi' + a^2 \frac{dU}{d\phi} = a^2 \beta(\phi)(\rho_\nu - 3p_\nu)$$

$$\beta(\phi) \equiv -\frac{d \ln m_\nu}{d\phi}$$

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$$\varphi \rightarrow \varphi + \theta$$

Wetterich 2008

$\phi_c$

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Wetterich 2008

$$\alpha \frac{1}{\phi - \phi_c}$$

$$\varphi \rightarrow \varphi + \theta$$

Wetterich 2008

$$\propto \frac{1}{\phi - \phi_c}$$

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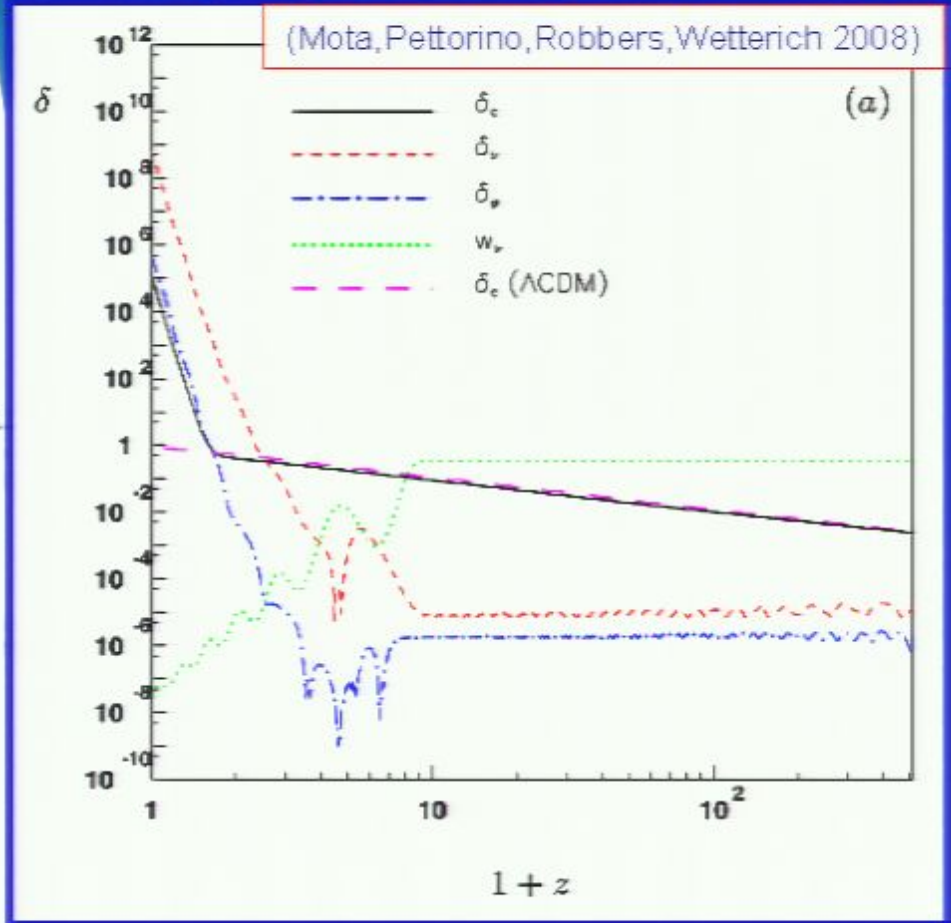
# Linear perturbations

Implement CMBEASY, CAMB...

$$\delta'_\phi = 3\mathcal{H}(w_\phi - c_\phi^2)\delta_\phi - \beta(\phi)\phi' \frac{\rho_\nu}{\rho_\phi} [(1 - 3w_\nu)\delta_\phi - (1 - 3c_\nu^2)\delta_\nu] - (1 + w_\phi)(k v_\phi + \frac{\rho_\nu}{\rho_\phi}(1 - 3w_\nu)) v'_\phi + \frac{\rho_\nu}{\rho_\phi}(1 - 3w_\nu) v'_\phi$$

$$v'_\phi = -\mathcal{H}(1 - 3w_\phi)v_\phi - \beta(\phi)\phi'(1 - 3w_\nu) \frac{w'_\phi}{1 + w_\phi} v_\phi + k c_\phi^2 \frac{\delta_\phi}{1 + w_\phi} + k\Psi - \frac{2}{3} k \frac{w_\nu}{1 + w_\nu} \pi_{T\nu}$$

$$v'_\nu = (1 - 3w_\nu)(\beta(\phi)\phi' - \mathcal{H})v_\nu - \frac{w'_\nu}{1 + w_\nu} v_\nu + k c_\nu^2 \frac{\delta_\nu}{1 + w_\nu} + k\Psi - \frac{2}{3} k \frac{w_\nu}{1 + w_\nu} \pi_{T\nu} - k\beta(\phi)\delta\phi \frac{1 - 3w_\nu}{1 + w_\nu}$$



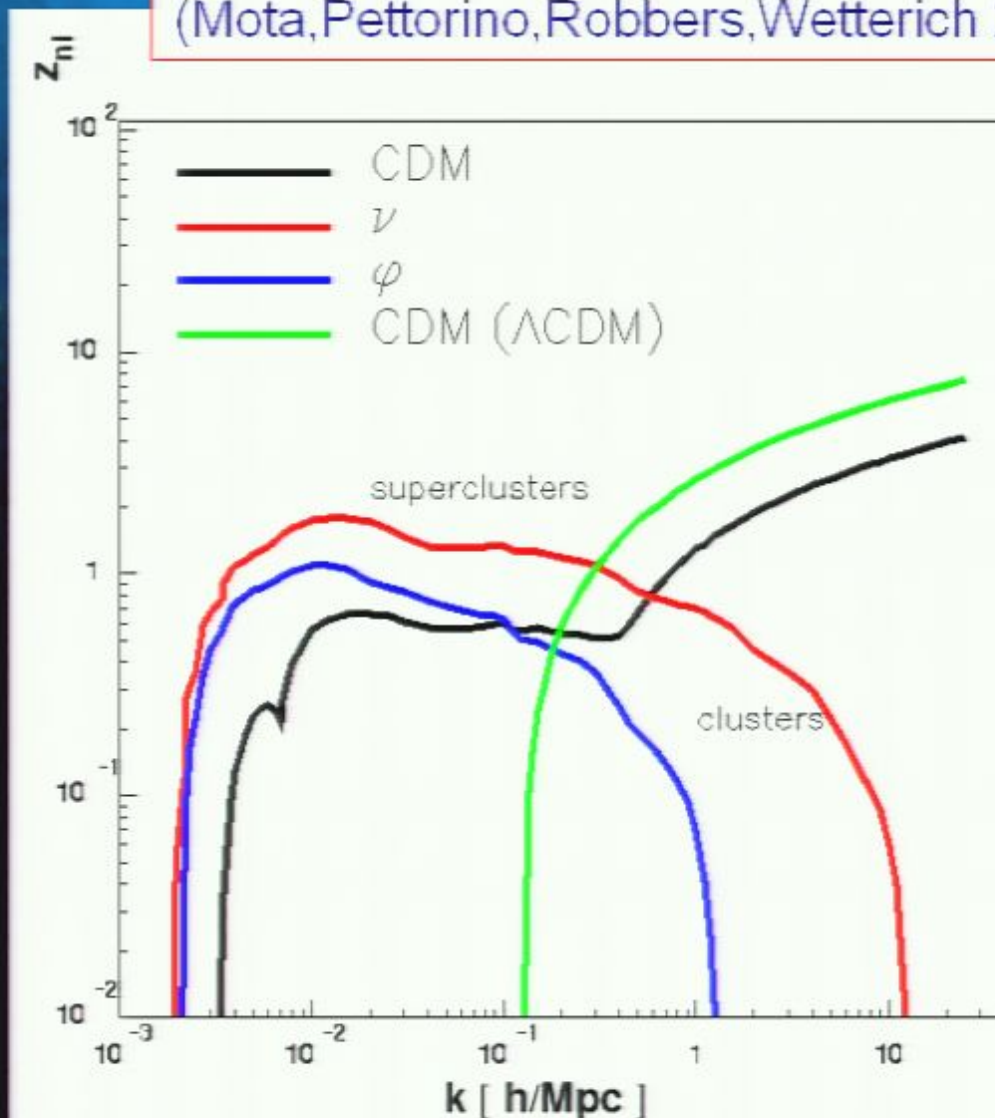
$k = 0.1 \text{ h/Mpc}$   
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# Neutrino clustering

- Neutrino structures become non linear at  $z \sim 1$  for supercluster scales
- At small scales neutrinos reduce CDM structures
- Stable neutrino lumps/nuggets

Afshordi etal 2005  
Brouzakis etal 2007

(Mota, Pettorino, Robbers, Wetterich 2008)



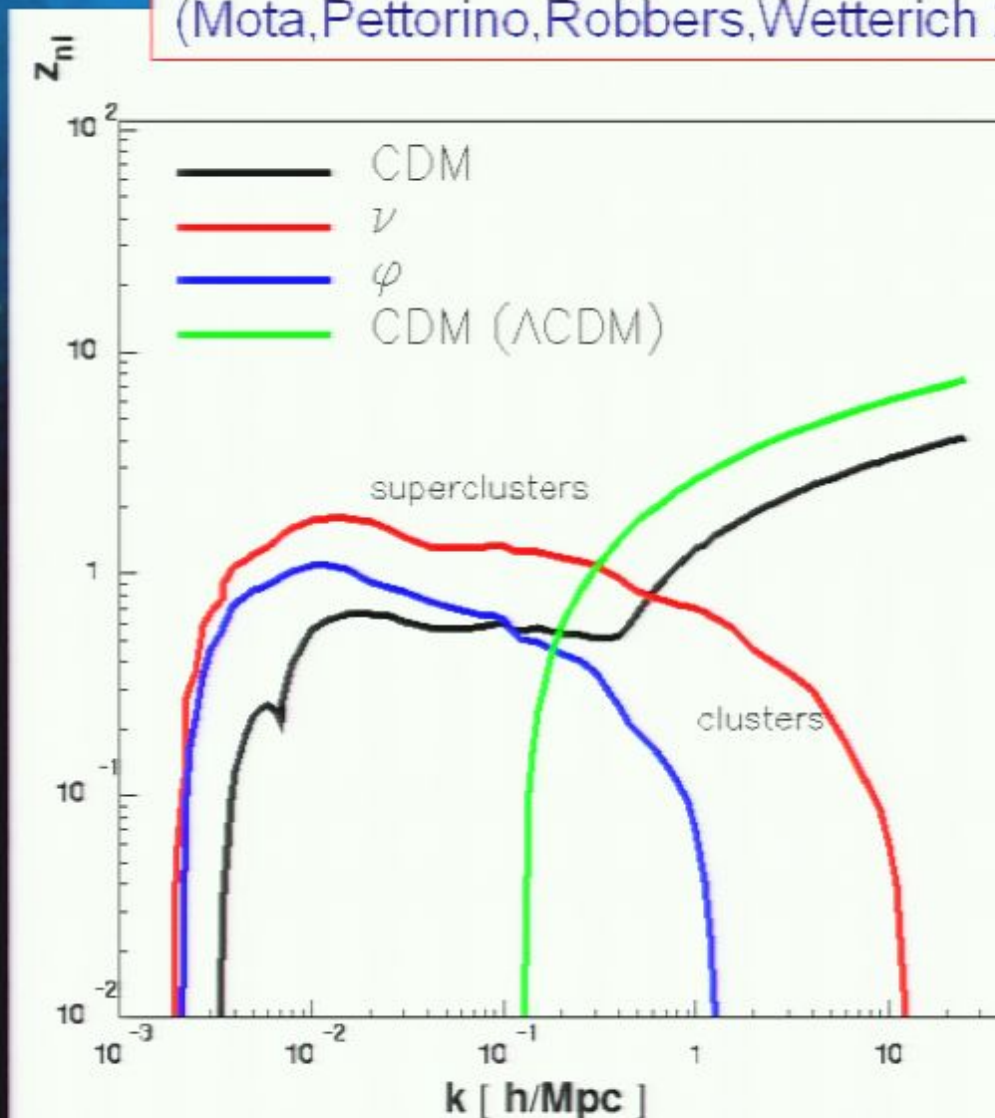


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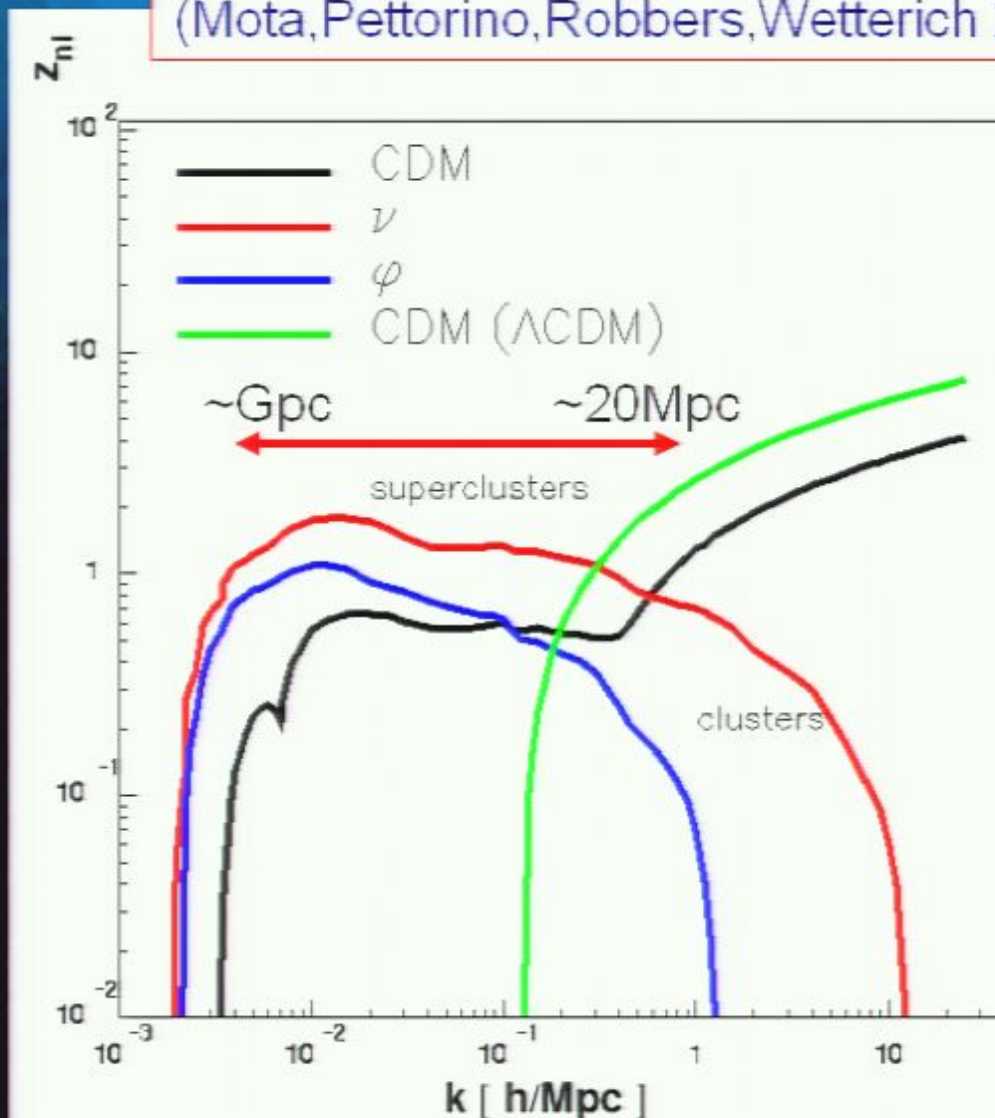


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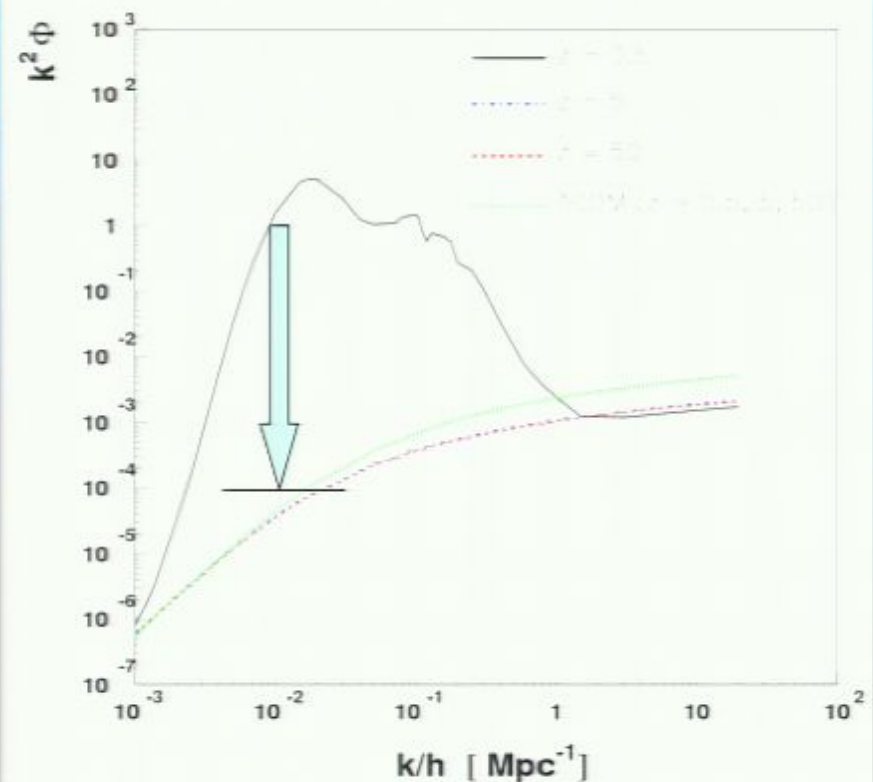


# Gravitational potential

- Linear analysis is not sufficient. The gravitational potential is not realistic and can lead to a huge ISW in CMB. However...

- There aren't many neutrinos!
- If they distribute more or less homogeneously in more lumps, the gravitational potential can be significantly reduced

(Mota, Pettorino, Robbers, Wetterich 2008)

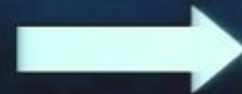


Essential to have a knowledge of the realistic gravitational potential due to the presence of a distribution of virialized neutrino lumps

# Non linear analysis...

- Non linear analysis of structure formation, from semi analytical approaches to N-body simulations

Non linear evolution of the primordial overdensities driven by the fifth force



$\Phi$

N.Wintergest, V.Pettorino, D.F.Mota, L.Schrempp, C.Wetterich

- Use data to constrain the coupling (or the neutrino mass)

## ...and CMB

E.Carlesi, D.Mota, V.Pettorino, G.Robbers, C.Wetterich

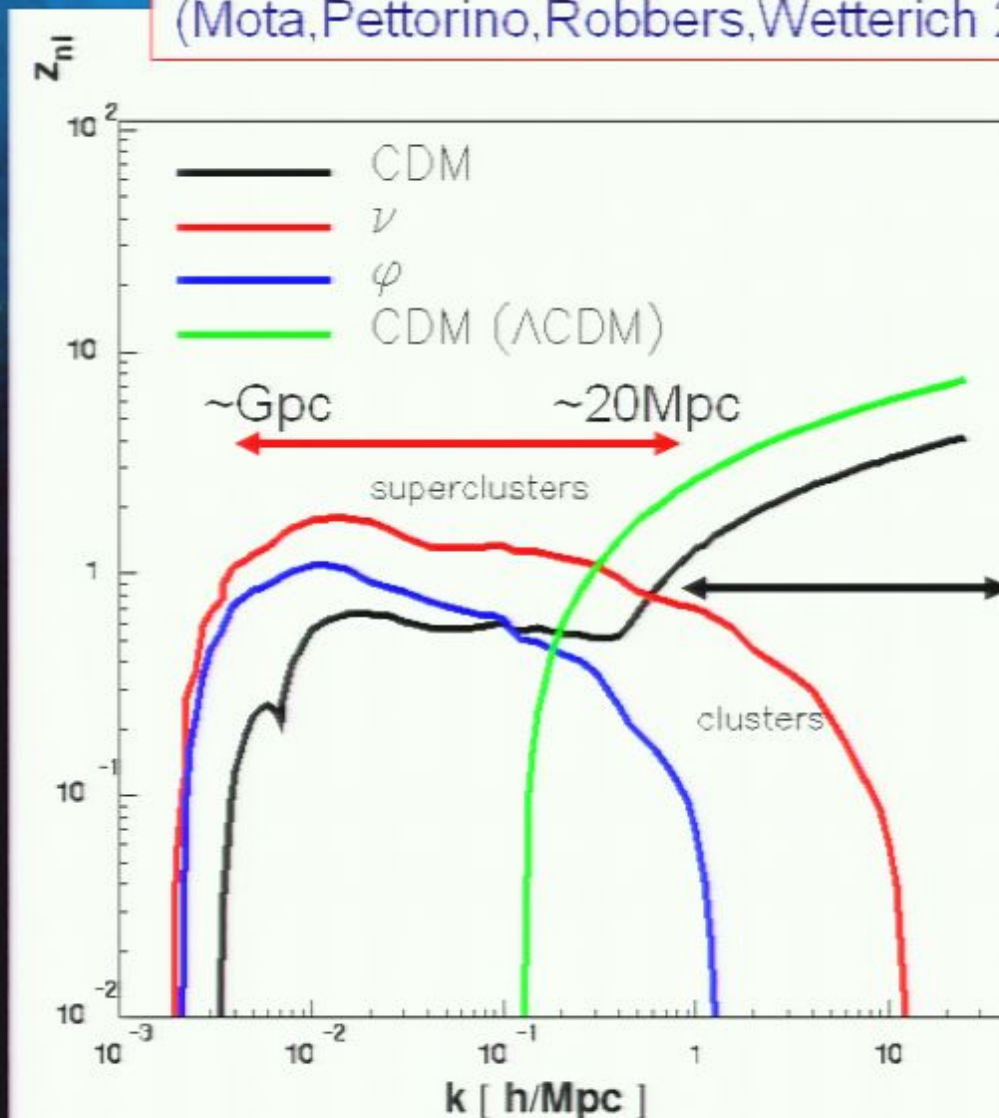
...first results are encouraging

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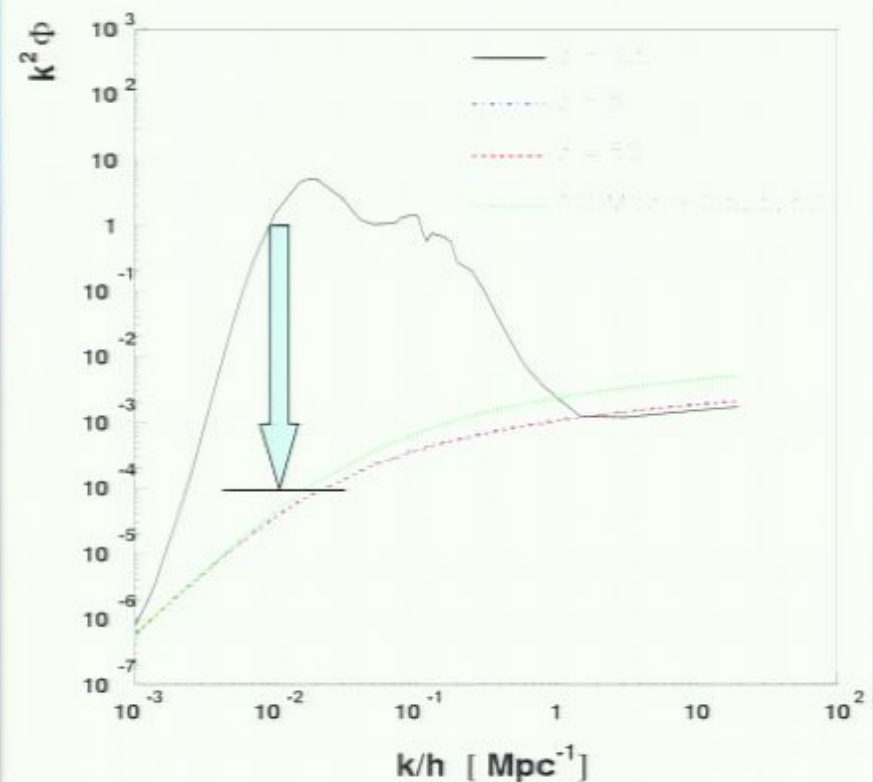


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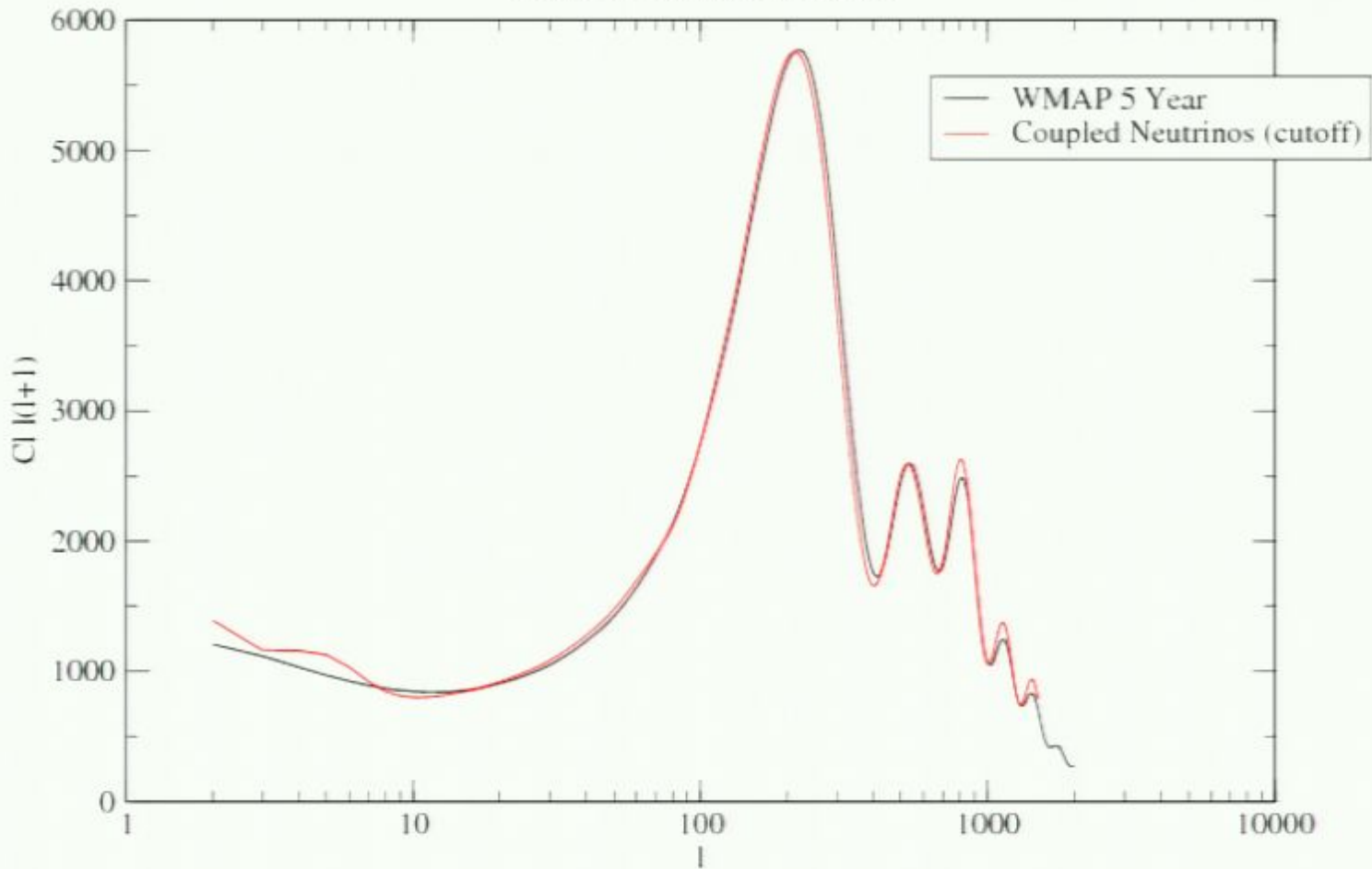
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CMB Spectrum  
WMAP vs. Coupled Neutrinos

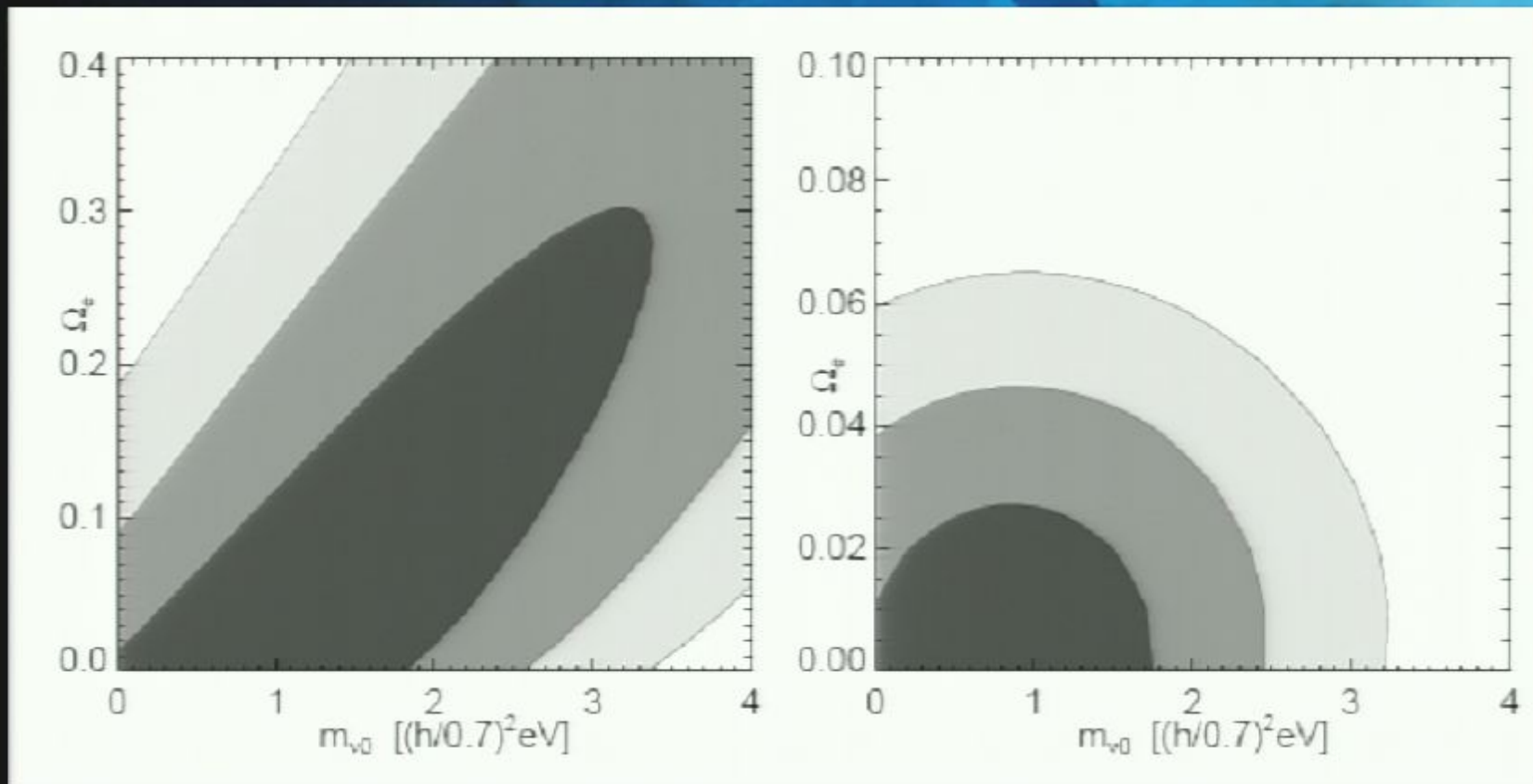


**Monte Carlo analysis necessary!**

*Work in progress!*



# Supernovae constraints



Rubin etal 2008

# Dark energy

Cosmological constant



Dark energy



Non coupled DE



Interacting DE



Attractors



Gravity



Dark Matter



Neutrinos

# Summary

Interacting Dark Energy	Linear	Non Linear
Gravity	✓	~ data analysis of Nbody in progress
CDM	✓	coming soon: Baldi etal
Neutrinos	✓	Under investigation

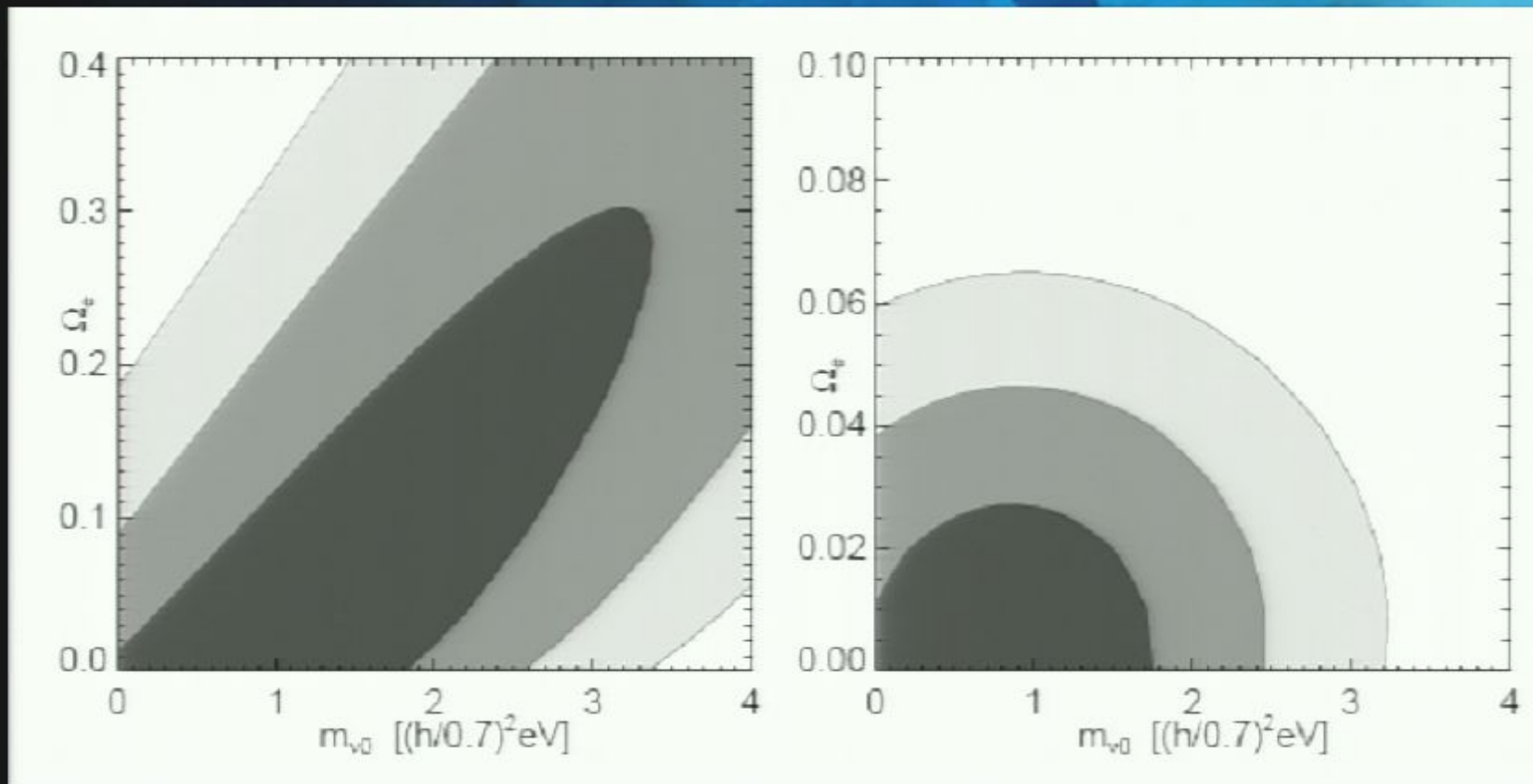
# Conclusions for DE - neutrinos

- When neutrinos become non relativistic, they activate the coupling.
- Transition from attractor to an almost static dark energy, independent of ground state properties.
- Neutrinos first cluster at  $z \sim 1$  at supercluster scales and beyond.
- At small scales, neutrinos don't contribute to the clumping but they reduce cdm structures.
- Detection of such a population of large scale structures via gravitational potential or correlation with CMB can be an indication for a new attractive force stronger than gravity.

# Future prospects

- Non linear features of interacting dark energy models
- Data analysis of N-body simulations
- Cross correlation with CMB
- Applications and forecast for future dark energy missions

# Supernovae constraints



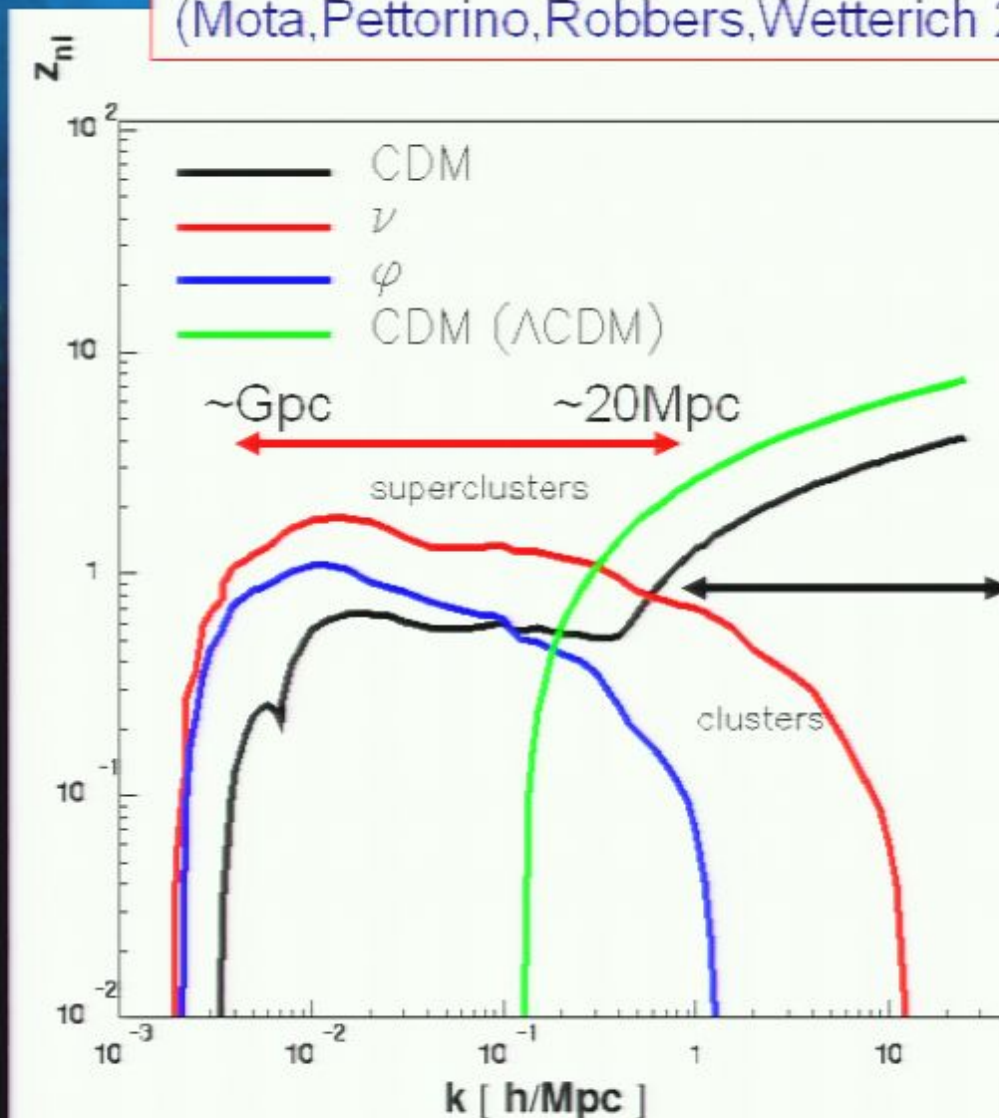
Rubin etal 2008

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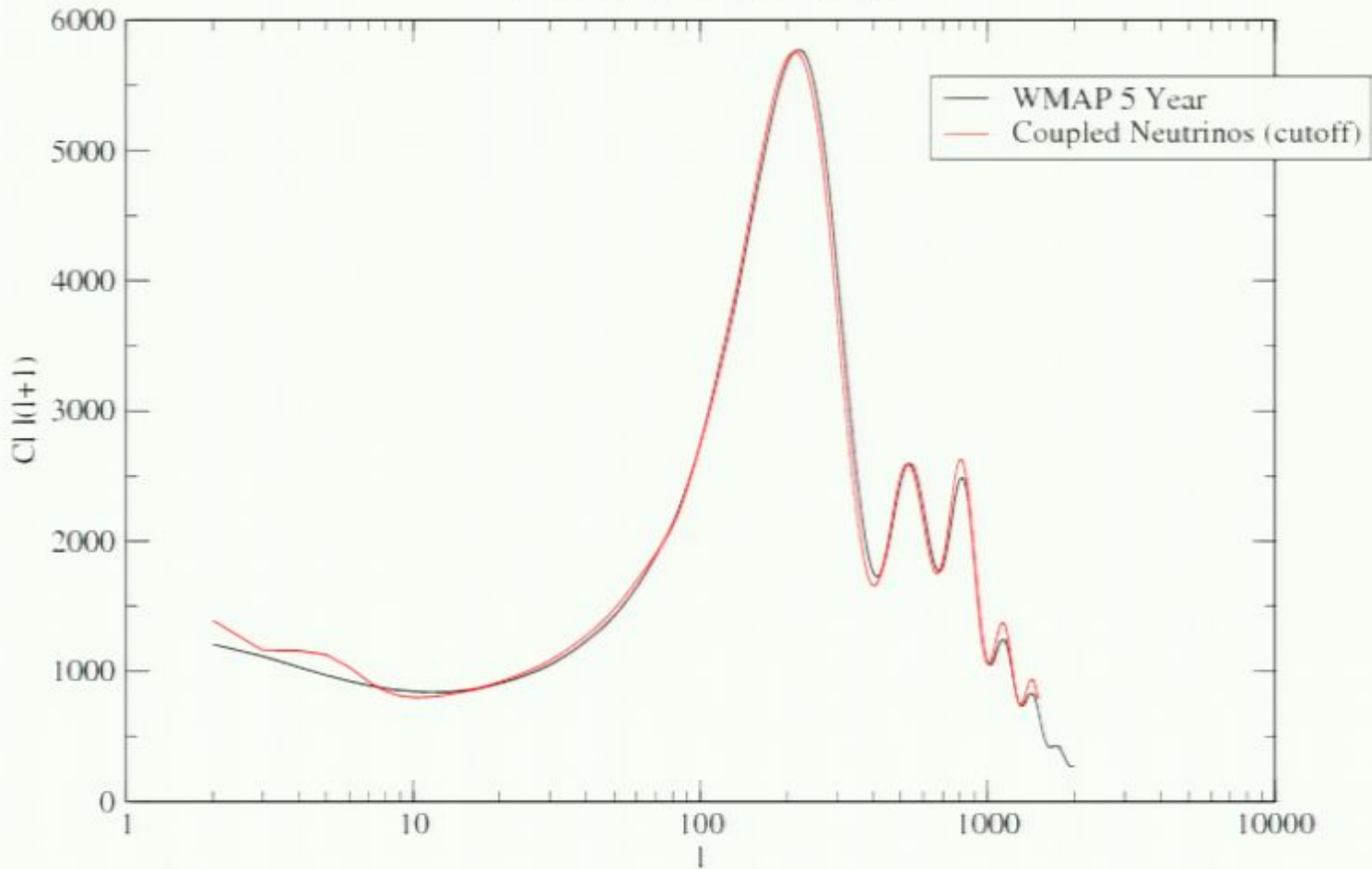
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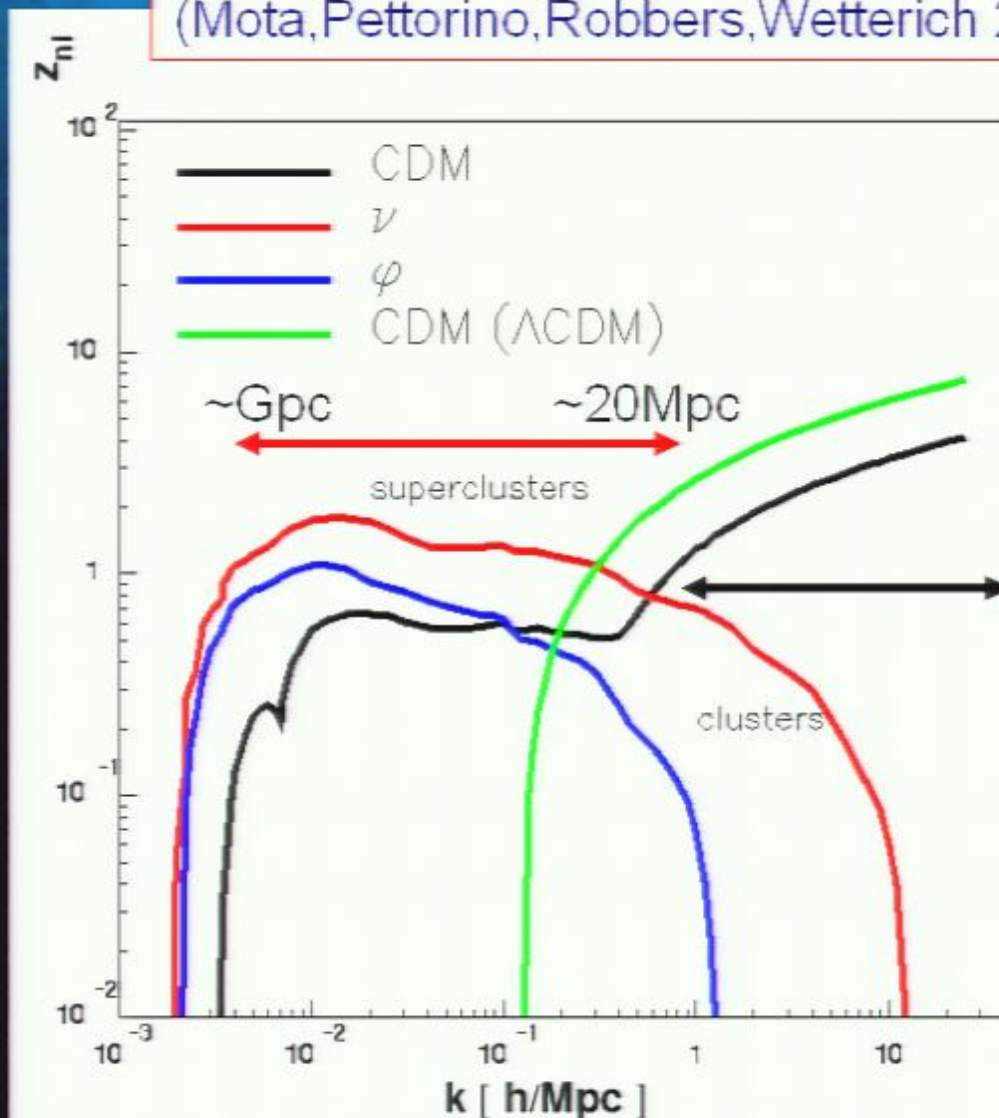


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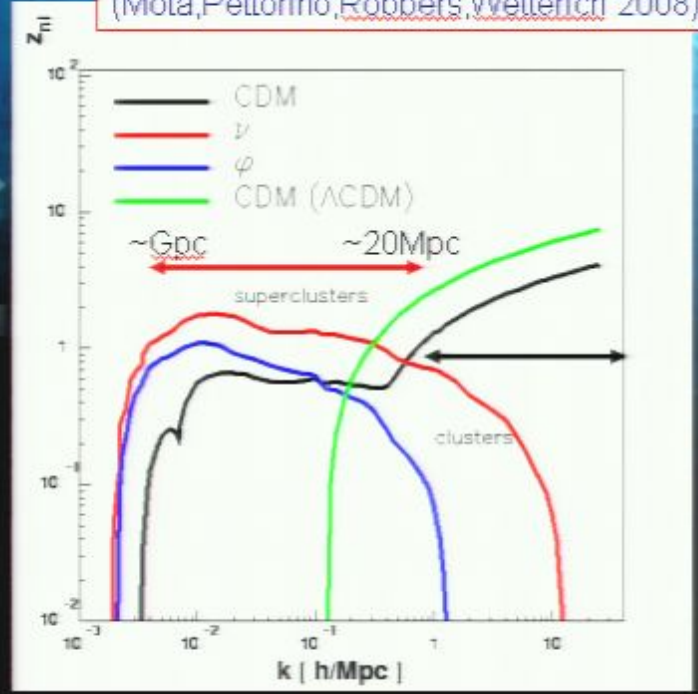


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Valeria Pettorino, ITP Heidelberg

PI, 14th November 2008

We can trust until.. Then we feed grav pot with non linear quantities without taking into account the realistic distrib of nu lumps which will have some maximum density value