Title: New Superconductors

Date: Nov 26, 2008 02:00 PM

URL: http://pirsa.org/08110002

Abstract: The discovery and understanding of superconductivity has provided important paradigms for physics, including spontaneous gauge symmetry breaking and the Anderson-Higgs mechanism. More recent discoveries in superconductivity have given us examples of doped Mott insulators, still an unsolved theoretical problem, as well as superconductors which spontaneously break time reversal symmetry and which support Majorana fermions and non-Abelian statistics. The latter are of potential interest to quantum computing. This talk will review our current understanding of, and the open issues related to, these new supercondutors, including the high T_c cuprates, iron pnictides, and strontium ruthenate.

Pirsa: 08110002



Outline

Brief introduction to Superconductivity High T_c cuprates Iron superconductors



Superconductors with spontaneous TRSB

Pirsa: 08110002

Superconductor: perfect conductivity and diamagnetism Discovered in 1911 in Hg by Kamerlingh Onnes Explained in 1957



Superconductor: perfect conductivity and diamagnetism Discovered in 1911 in Hg by Kamerlingh Onnes Explained in 1957

Key ideas:







Bardeen

Cooper

Schrieffer

Superconductor: perfect conductivity and diamagnetism Discovered in 1911 in Hg by Kamerlingh Onnes

Explained in 1957

Key ideas:

Electrons pair







Bardeen

Cooper

Schrieffer

Superconductor: perfect conductivity and diamagnetism Discovered in 1911 in Hg by Kamerlingh Onnes Explained in 1957

Key ideas:

Electrons pair
Pairs are coherent







Bardeen

Cooper

Schrieffer

Superconductor: perfect conductivity and diamagnetism Discovered in 1911 in Hg by Kamerlingh Onnes Explained in 1957

Key ideas:

Electrons pair
Pairs are coherent









Bardeen

Cooper

Schrieffer



Superconductivity is described by an order parameter which measures the fraction of coherent pairs. Same

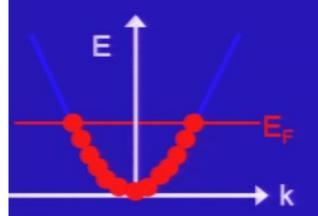
Pirsa: 08110002 ase for all Cooper pairs: <ψ_♠(r)ψ_↓(r)>

Page 8/69

Superconductivity & SSB

Two major paradigms of condensed matter physics:

Fermi liquid theory



Fermi surface obeying Luttinger's theorem # states enclosed unchanged by interactions.

Quasiparticles with same charge/spin.

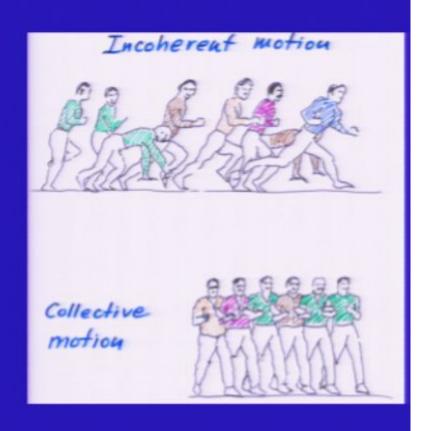
- Spontaneous Symmetry Breaking
- local order parameter (e.g. <m_i> for a ferromagnet)
- Goldstone mode (if continuous symmetry broken, e.g. spinwaves)
- examples: solids, charge and spin order



Superconductivity fit into SSB with "broken gauge symmetry" \rightarrow phase coherence, order parameter $<\psi_{\uparrow}(r)\psi_{\downarrow}(r)>$.

No Goldstone mode due to Higgs mechanism.

[Analogous to E-W symmetry breaking]

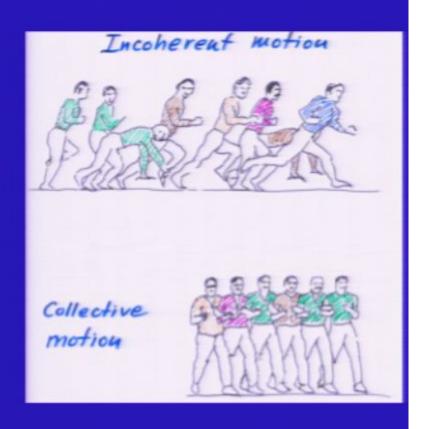


Pirsa: 08110002 Page 10/69

Superconductivity fit into SSB with "broken gauge symmetry" \rightarrow phase coherence, order parameter $<\psi_{\uparrow}(r)\psi_{\downarrow}(r)>$.

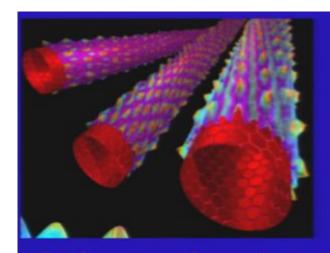
No Goldstone mode due to Higgs mechanism.

[Analogous to E-W symmetry breaking]



Much of CM in last two decades focused on materials and models exhibiting states which do not fit into the paradigms of spontaneous symmetry breaking or Fermi liquids – particularly those with topological order

Pirea: 08110002



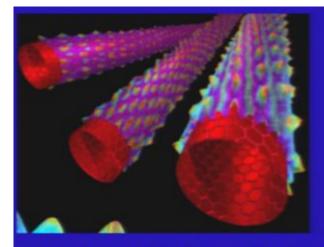
Topological Order

In 1d, FLT breaks down and SSB order destroyed by quantum fluctuations.

d>1: require strong interactions, frustration, degeneracy or nontrivial band structure to stabilize states with topological order. E.g. quantum Hall states.

- no local order parameter, but a quantum order (Wen)
- gs degeneracy which depends on topology
- edge states in finite geometry
- exhibit fractionalization (e.g. spin-charge separation)

Pirsa: 08110002 Page 12/69



Topological Order

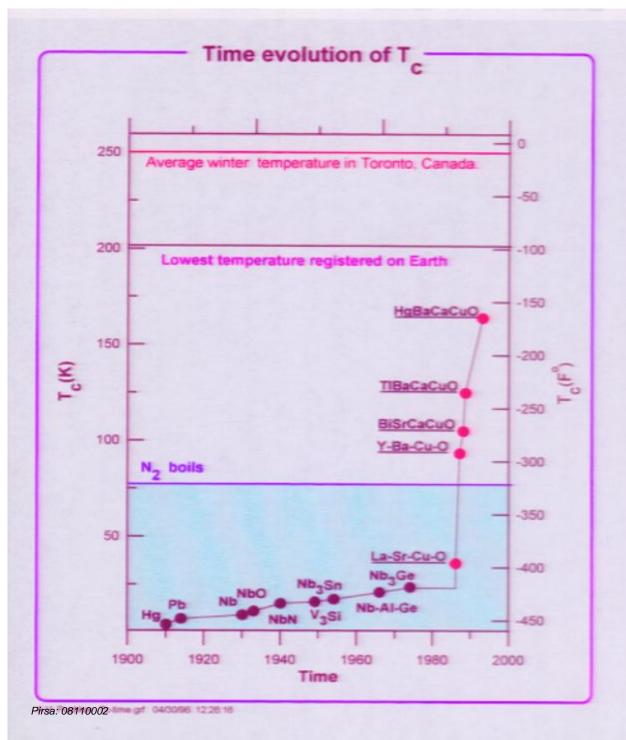
In 1d, FLT breaks down and SSB order destroyed by quantum fluctuations.

d>1: require strong interactions, frustration, degeneracy or nontrivial band structure to stabilize states with topological order. E.g. quantum Hall states.

- no local order parameter, but a quantum order (Wen)
- gs degeneracy which depends on topology
- edge states in finite geometry
- exhibit fractionalization (e.g. spin-charge separation)

Superconductivity now understood as example of topological order, with (gapped) edge states, spin-charge separation.

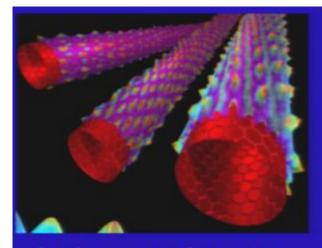
[T. H. Hansson, V. Oganesyan, S. L. Sondhi, 2004.]



High Temperature Superconductivity in the Cuprates

High transition temperatures

Strong electron correlations



Topological Order

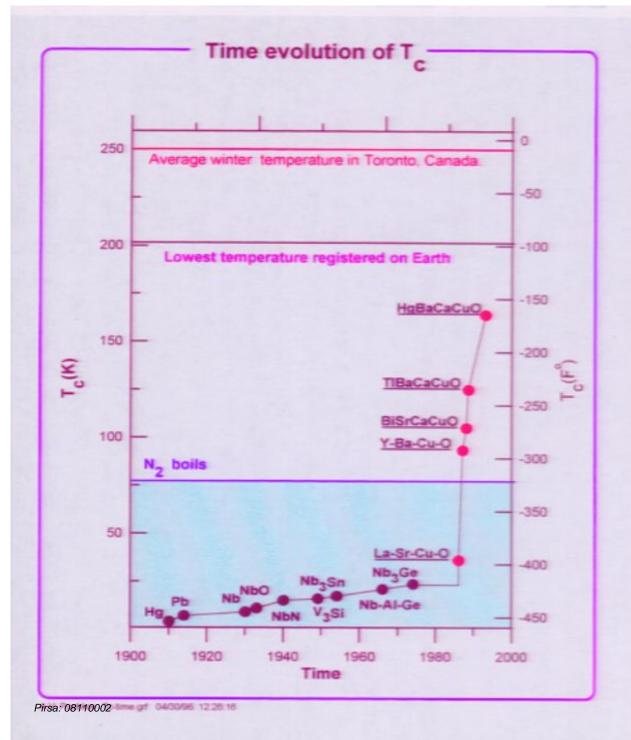
In 1d, FLT breaks down and SSB order destroyed by quantum fluctuations.

d>1: require strong interactions, frustration, degeneracy or nontrivial band structure to stabilize states with topological order. E.g. quantum Hall states.

- no local order parameter, but a quantum order (Wen)
- gs degeneracy which depends on topology
- edge states in finite geometry
- exhibit fractionalization (e.g. spin-charge separation)

Superconductivity now understood as example of topological order, with (gapped) edge states, spin-charge separation.

[T. H. Hansson, V. Oganesyan, S. L. Sondhi, 2004.]

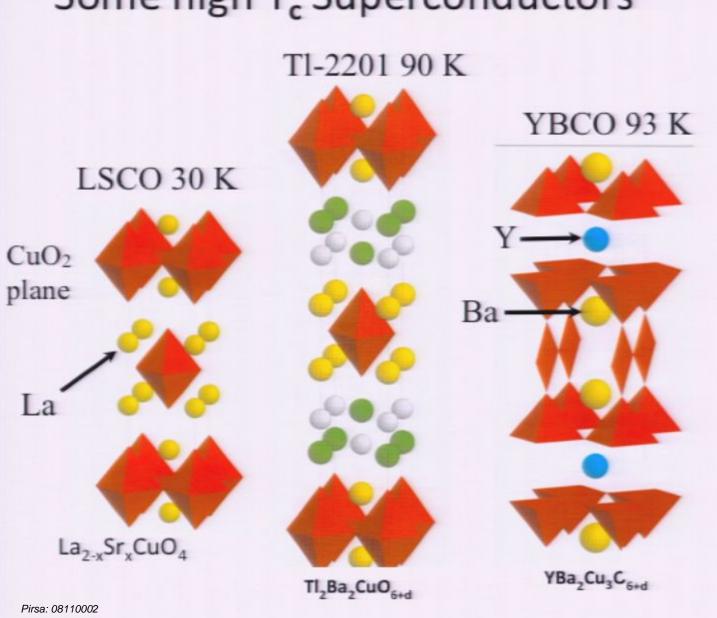


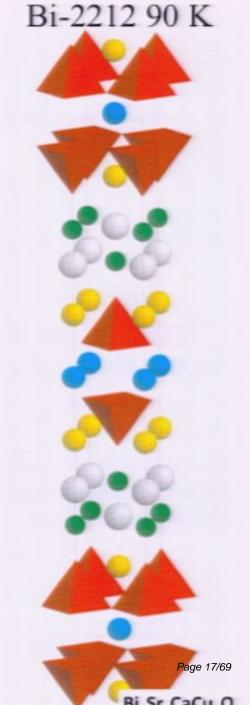
High Temperature Superconductivity in the Cuprates

High transition temperatures

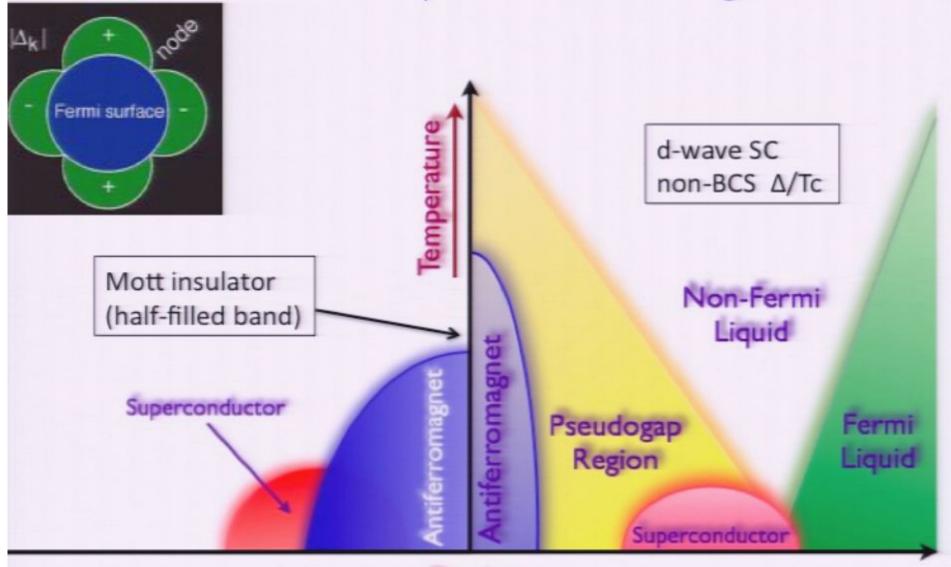
Strong electron correlations

Some high T_c Superconductors

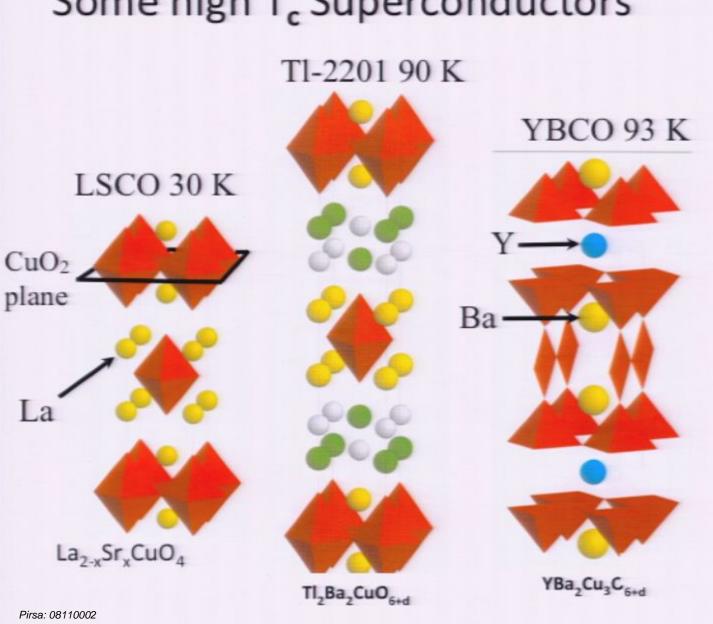


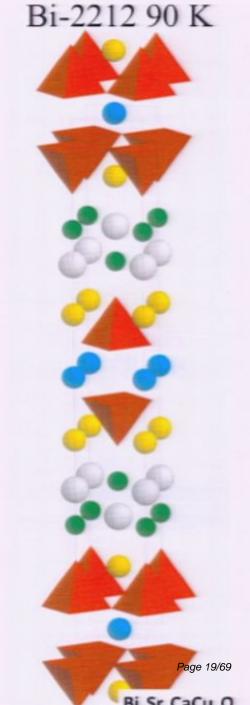


Generic Cuprate Phase Diagram

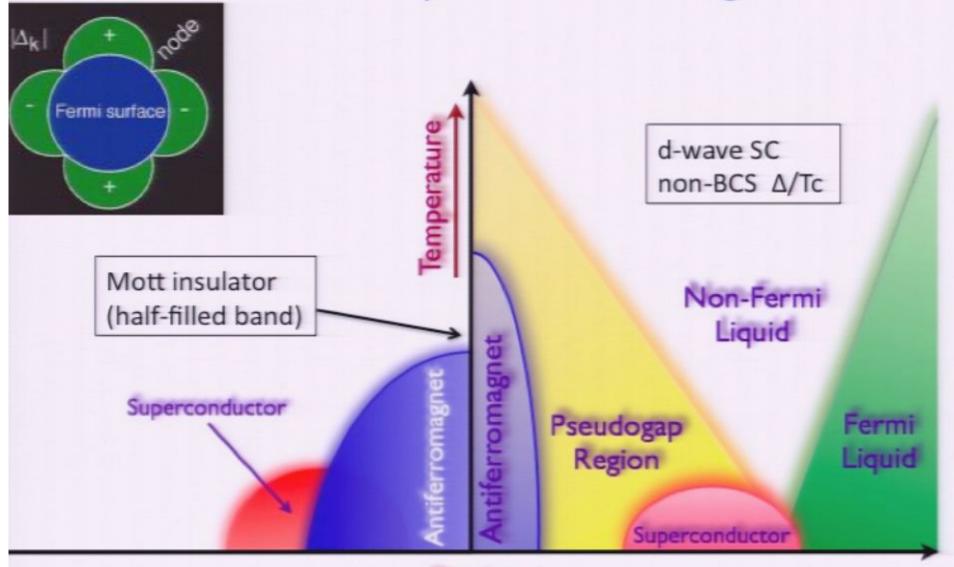


Some high T_c Superconductors

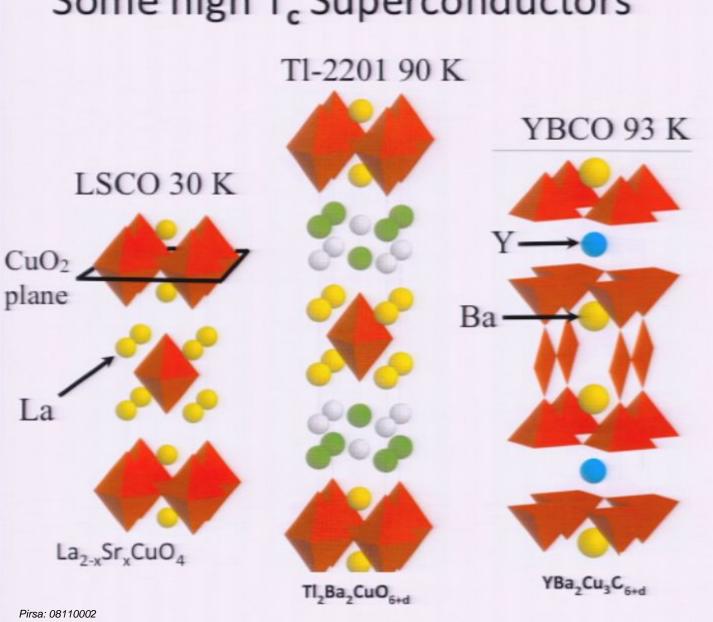


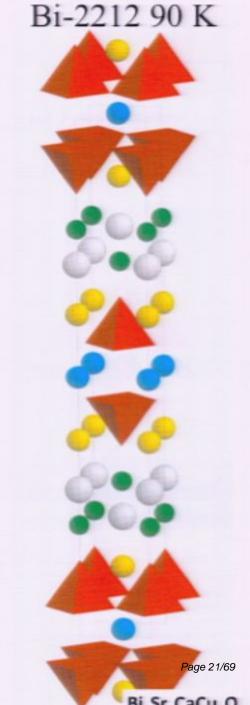


Generic Cuprate Phase Diagram

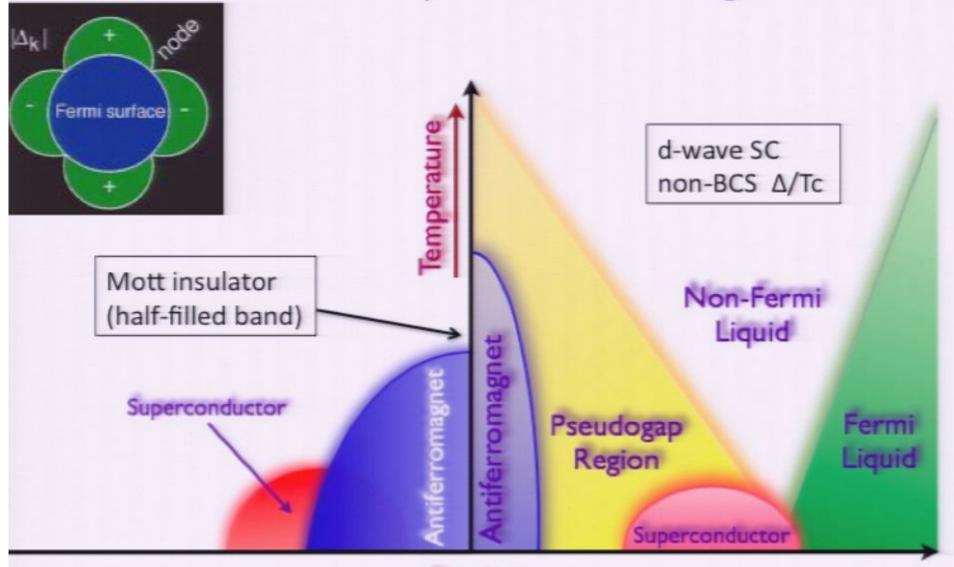


Some high T_c Superconductors

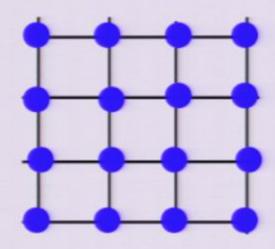




Generic Cuprate Phase Diagram



Mott insulator



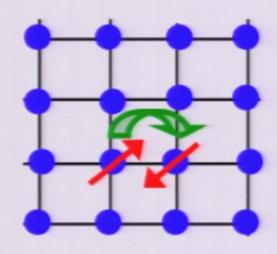
1 electron per site → band theory would predict a metal (half filled band)

large onsite Coulomb energy U →
electrons can't move → Mott insulator
with charge gap U

$$H = t \sum_{i\delta\sigma} c^{+}_{i\sigma} c^{}_{i+\delta,\sigma} + U \sum_{i} n^{}_{i\uparrow} n^{}_{i\downarrow}$$

Doped Mott Insulator

Mott insulator



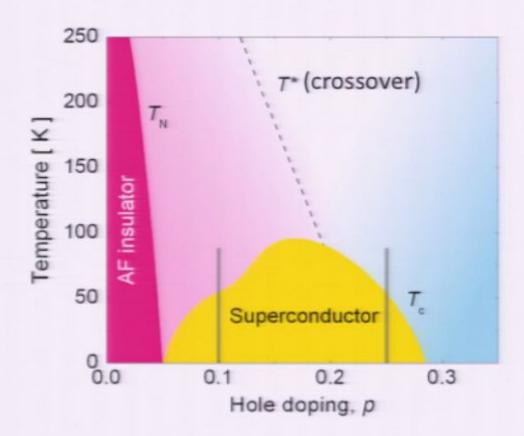
1 electron per site → band theory would predict a metal (half filled band)

large onsite Coulomb energy U →
electrons can't move → Mott insulator
with charge gap U

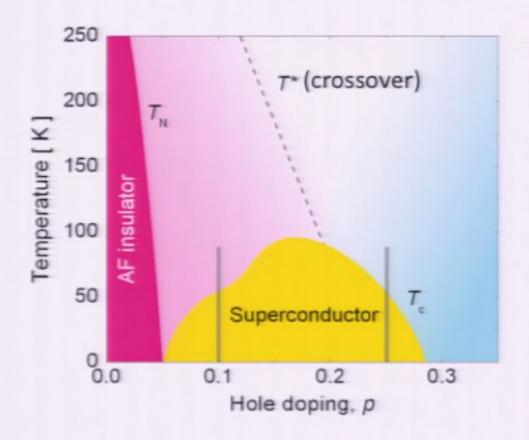
Virtual hops (2nd order perturbation theory) lower energy for antiparallel nn spins by −t²/U → antiferromagnetic insulator

$$H = t \sum_{i\delta\sigma} c^{+}_{i\sigma} c^{}_{i+\delta,\sigma} + U \sum_{i} n^{}_{i\uparrow} n^{}_{i\downarrow}$$

Doped Mott Insulator



Pirsa: 08110002 Page 25/69

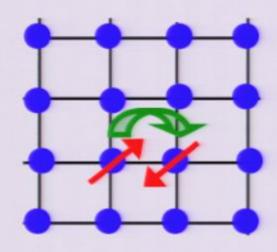


Pseudogap: Key as it connects
AF and d-SC phases and exists
over wide temperature and
doping region. Problem of
doped Mott insulator.

- Preformed pairs
- AF and/or SC fluctuations
- Stripes and fluctuations
- •DDW, ∏-flux
- orbital currents

Pirsa: 08110002 Page 26/69

Mott insulator



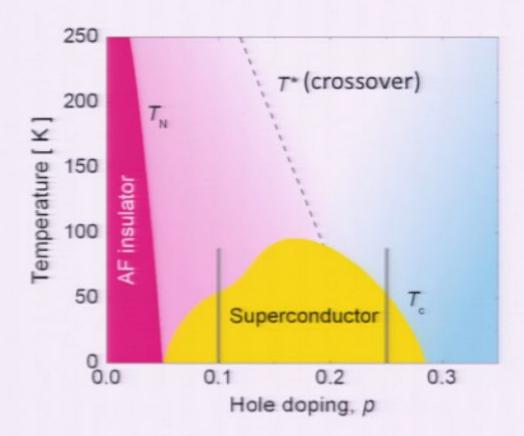
1 electron per site → band theory would predict a metal (half filled band)

large onsite Coulomb energy U →
electrons can't move → Mott insulator
with charge gap U

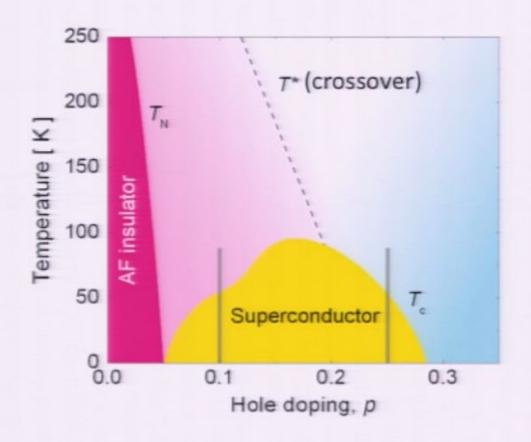
Virtual hops (2nd order perturbation theory) lower energy for antiparallel nn spins by −t²/U → antiferromagnetic insulator

$$H = t \sum_{i\delta\sigma} c^{+}_{i\sigma} c^{}_{i+\delta,\sigma} + U \sum_{i} n^{}_{i\uparrow} n^{}_{i\downarrow}$$

Doped Mott Insulator



Pirsa: 08110002 Page 28/69

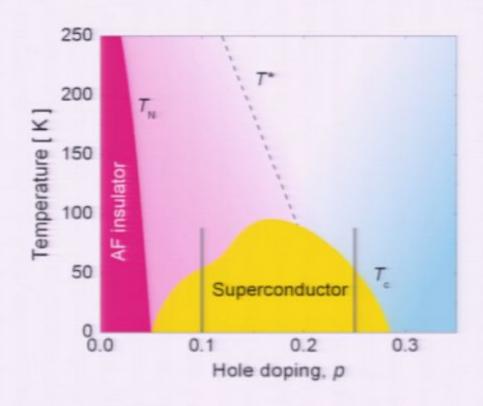


Pseudogap: Key as it connects
AF and d-SC phases and exists
over wide temperature and
doping region. Problem of
doped Mott insulator.

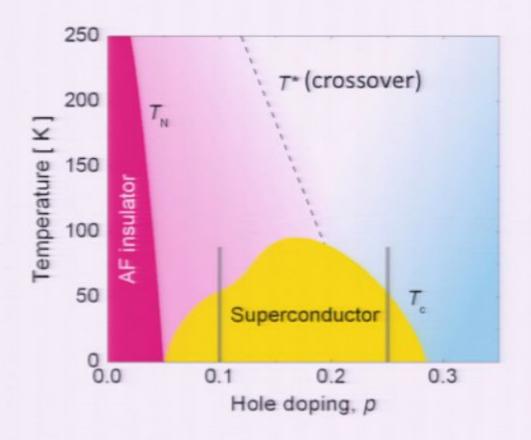
- Preformed pairs
- AF and/or SC fluctuations
- Stripes and fluctuations
- •DDW, ∏-flux
- orbital currents

Pirsa: 08110002 Page 29/69

Fermi surface of hole-doped cuprates



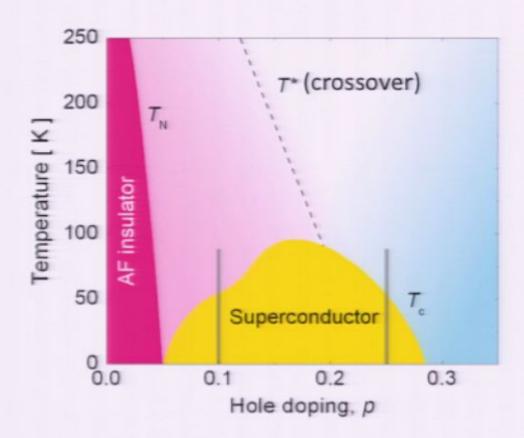
Pirsa: 08110002 Page 30/69



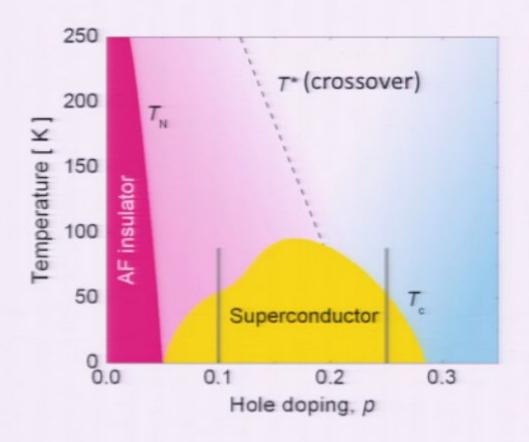
Pseudogap: Key as it connects
AF and d-SC phases and exists
over wide temperature and
doping region. Problem of
doped Mott insulator.

- Preformed pairs
- AF and/or SC fluctuations
- Stripes and fluctuations
- •DDW, ∏-flux
- orbital currents

Pirsa: 08110002 Page 31/69



Pirsa: 08110002 Page 32/69

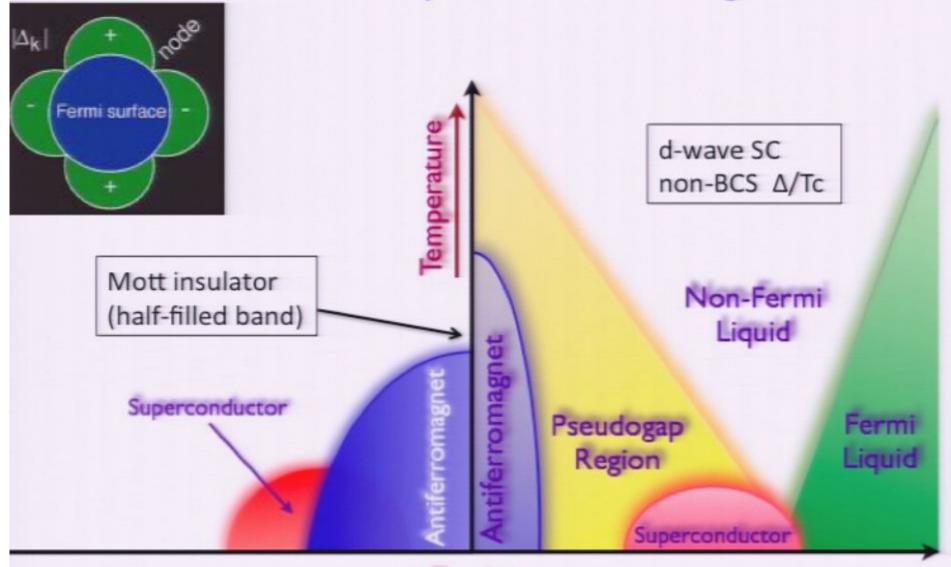


Pseudogap: Key as it connects
AF and d-SC phases and exists
over wide temperature and
doping region. Problem of
doped Mott insulator.

- Preformed pairs
- AF and/or SC fluctuations
- Stripes and fluctuations
- •DDW, ∏-flux
- orbital currents

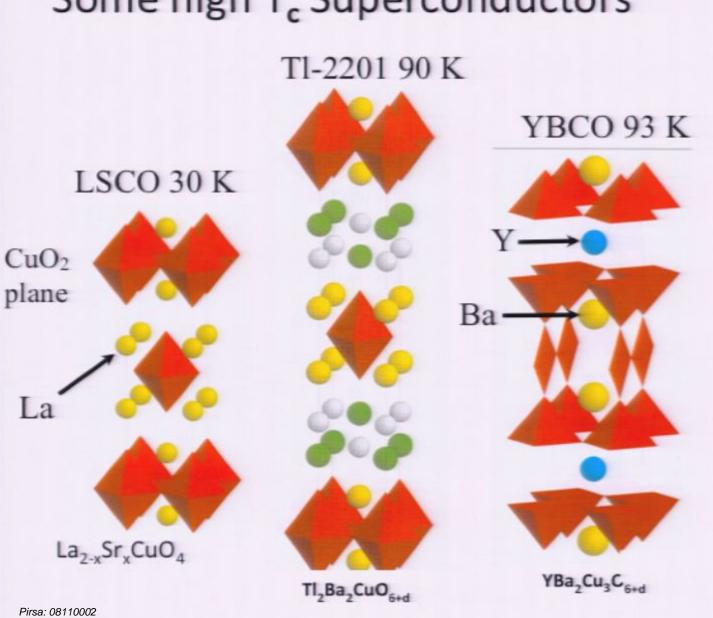
Pirsa: 08110002 Page 33/69

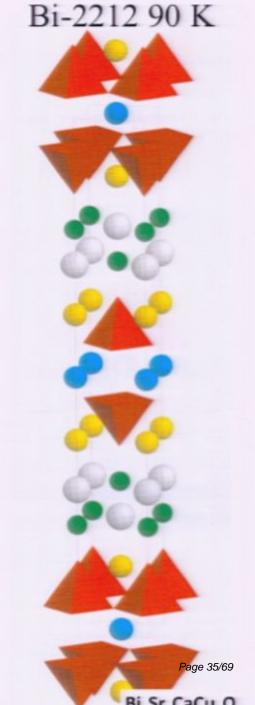
Generic Cuprate Phase Diagram



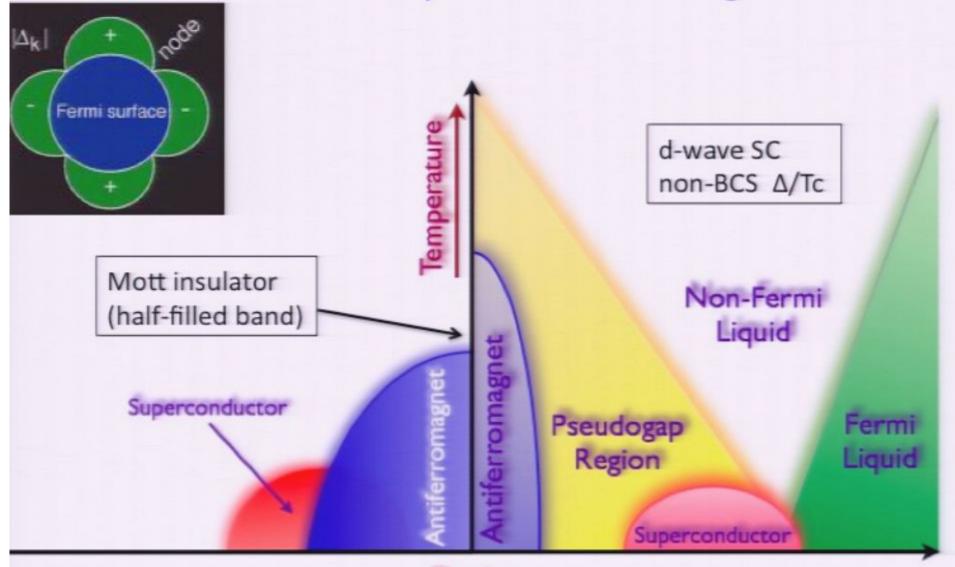
Doping

Some high T_c Superconductors



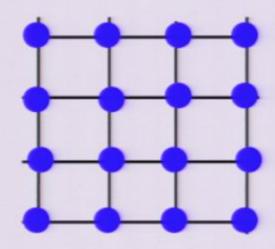


Generic Cuprate Phase Diagram



Pirsa: 08110002

Mott insulator

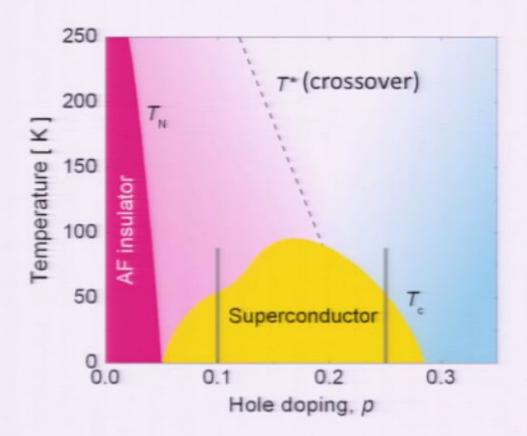


1 electron per site → band theory would predict a metal (half filled band)

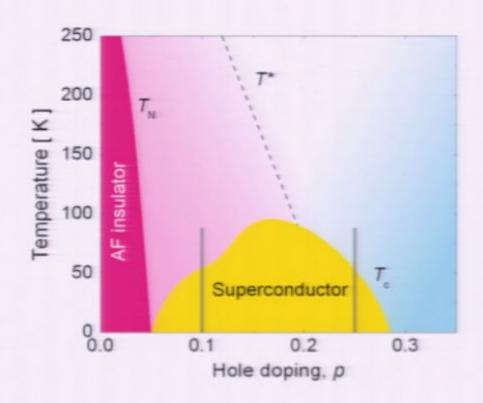
large onsite Coulomb energy U →
electrons can't move → Mott insulator
with charge gap U

$$H = t \sum_{i\delta\sigma} c^{+}_{i\sigma} c^{}_{i+\delta,\sigma} + U \sum_{i} n^{}_{i\uparrow} n^{}_{i\downarrow}$$

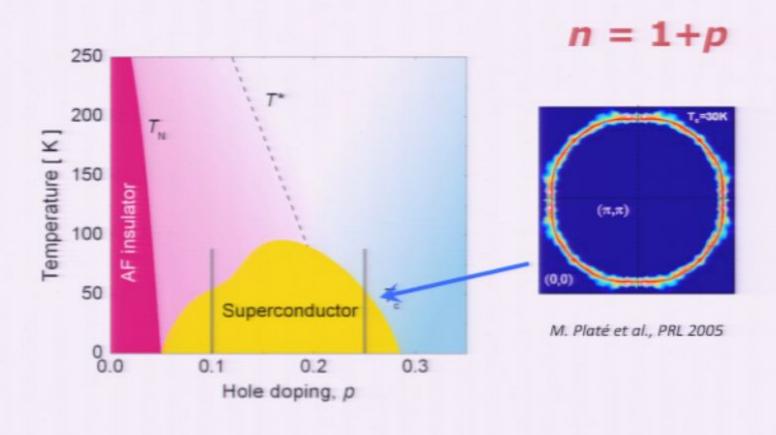
Doped Mott Insulator Goal: Explain all universal properties in the insulating, pseudogap and superconducting phases within a single theory which can make verifiable predictions.



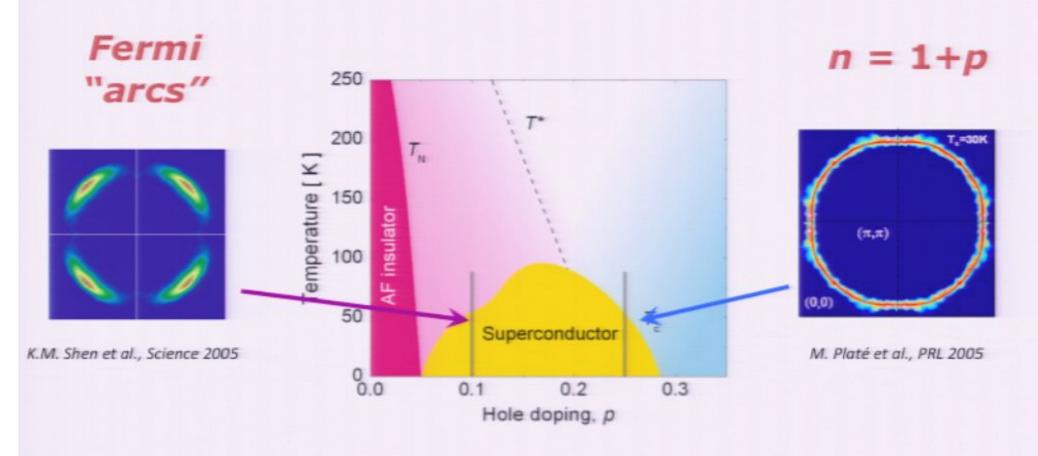
Pirsa: 08110002 Page 38/69



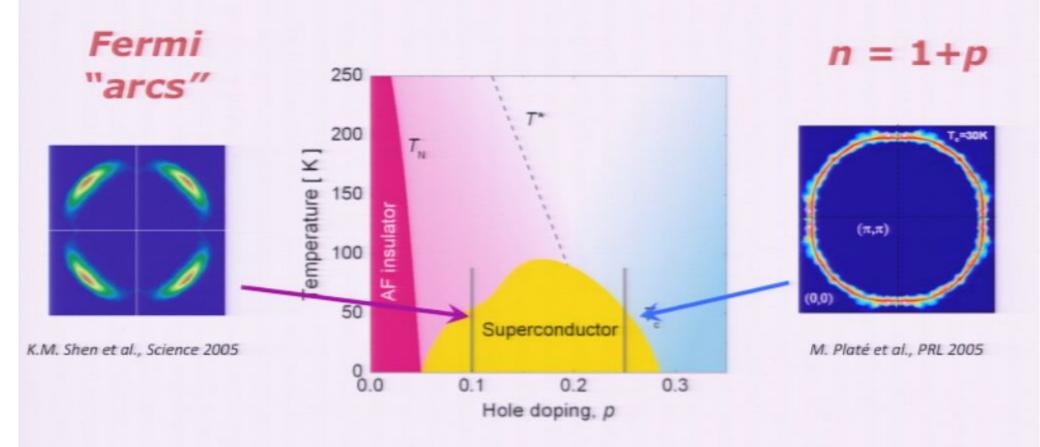
Pirsa: 08110002 Page 39/69



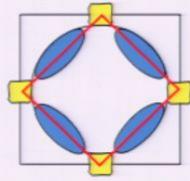
Pirsa: 08110002 Page 40/69



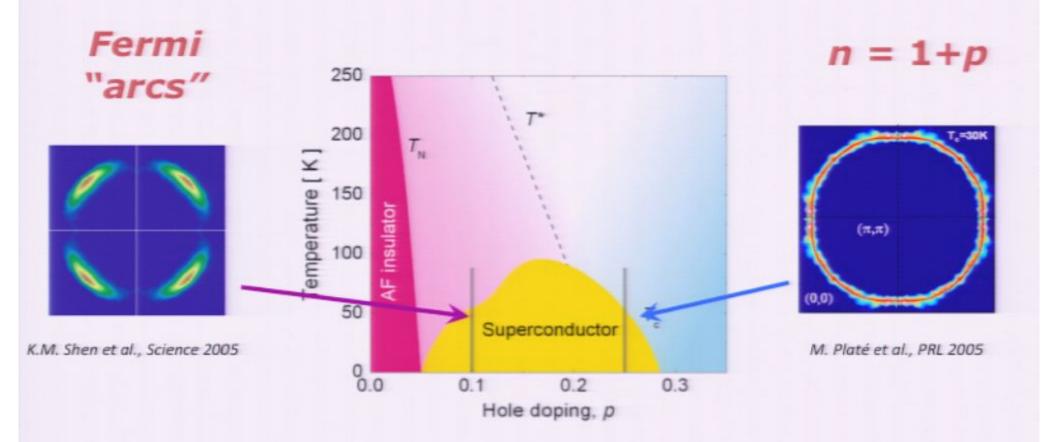
Pirsa: 08110002 Page 41/69



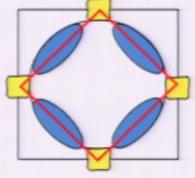
Recent SdH and dHvA measurements give information about the Fermi surface in the pseudogap phase



Page 42/69



Recent SdH and dHvA measurements give information about the Fermi surface in the pseudogap phase



Nature of pseudogap phase still open question

Page 43/60

N Doiron-Levraud et al. Nature 2007

Iron Superconductors

```
26K LaO<sub>1-x</sub>F<sub>x</sub>FeAs (Hosono, February 2008)
```

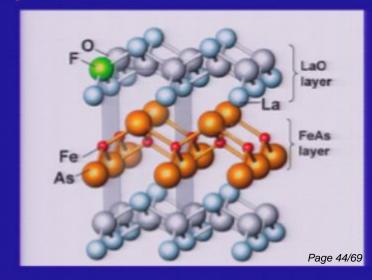
43K SmO_{1-x}F_xFeAs (Chen, March 2008)

52K PrO_{1-x}F_xFeAs (Zhao, March 2008)

55K PrO_{1-x}F_xFeAs grown under pressure (Zhao, April 2008)

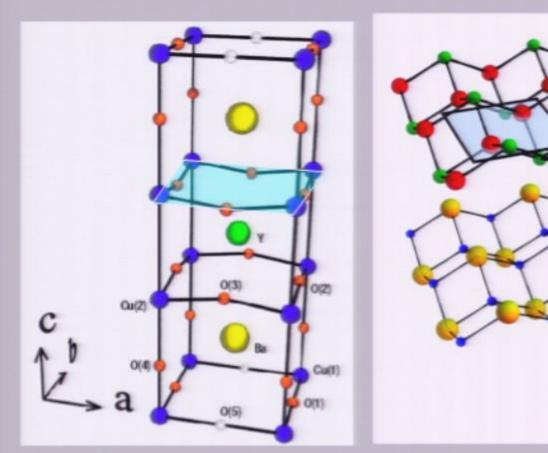
111: ROFeAs, LiFeAs R=Ce,Pr,Nd,Sm,...

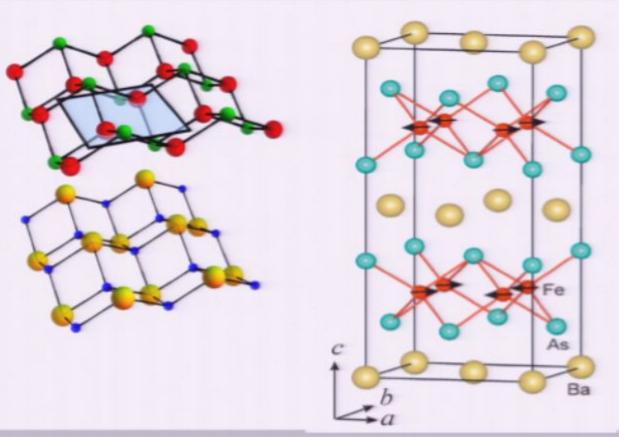
122: (Ba,K)Fe,As, (Sr,A) Fe,As, A=K,Cs



Pirsa: 08110002

Cu-oxides versus Fe-pnictides

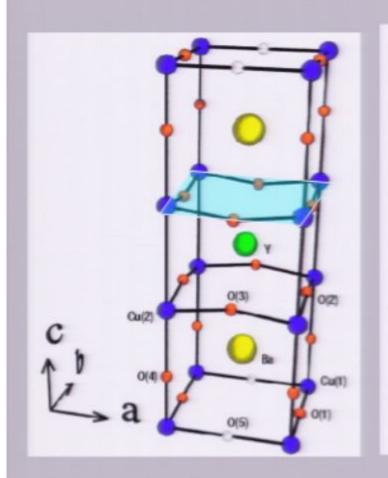


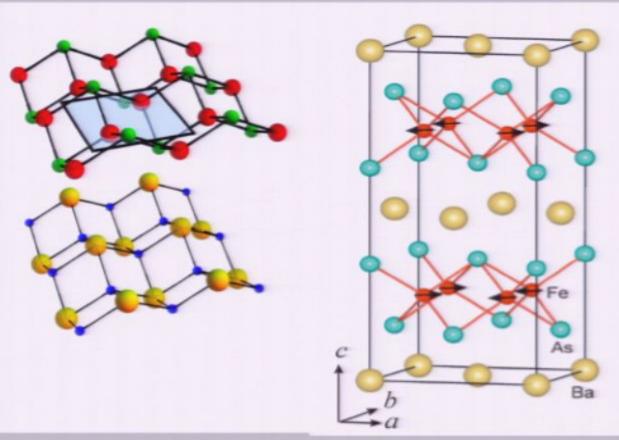


Both have d-electrons in key role (Cu vs Fe)
Both are layered (CuO2 vs FeAs)
Both have AF and SC in close proximity

Pirsa Booth are poor metals

Cu-oxides versus Fe-pnictides





Both have d-electrons in key role (Cu vs Fe)
Both are layered (CuO2 vs FeAs)
Both have AF and SC in close proximity

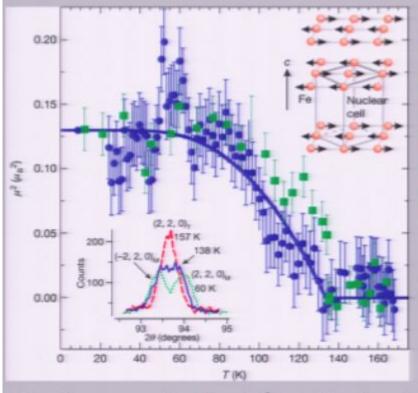
Pirsa Particles are poor metals

However, there are also differences which may be important.

Page 46/69

Phase diagram of Fe-pnictides

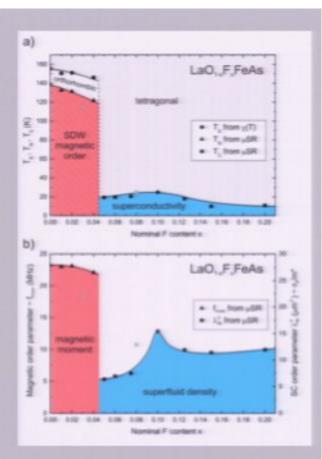
C. de la Cruz, et al., Nature 453, 899 (2008)



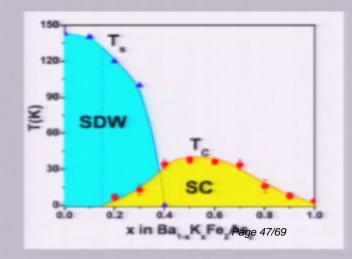
Like CuO₂, phase diagram FeAs has SDW (AF) in proximity to the SC state.

Small moment (in plane) → no Hunds rule

SC coexists with SDW (AF) in 122 compounds →



H. Chen, et al., arXiv/0807.3950



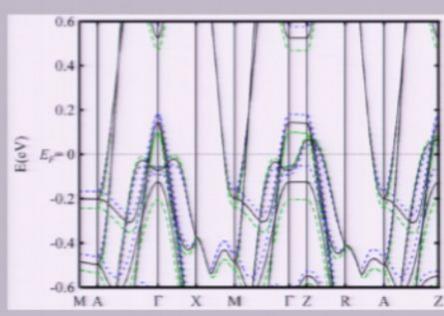
Key Difference: odd versus even number of d-electrons

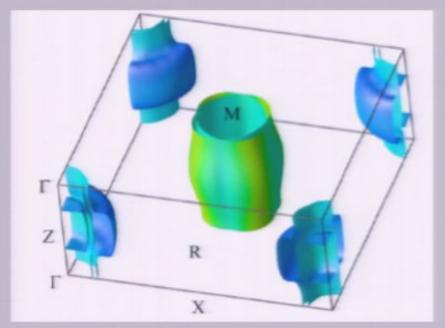
$$Cu^{2+} \rightarrow 3d^9$$

Fe²⁺ $\rightarrow 3d^6$

- → In CuO₂ start with half-filled single band
- → In FeAs nearly full or empty bands

Undoped FeAs bands are nearly full or nearly empty → no insulating phase → less correlated than cuprates





Pirsa: 08110002

Page 48/69

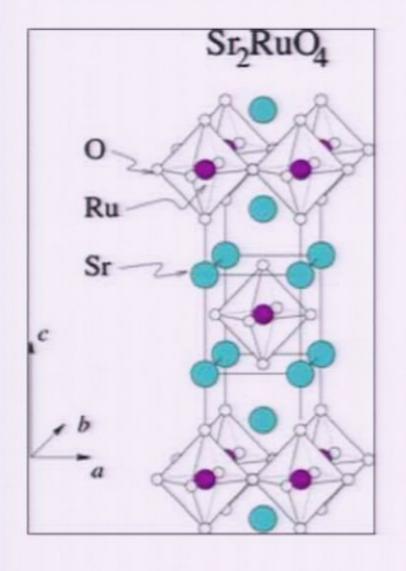
Theory of Fe SC

- Not compatible with only phonons (Haule, Shim, Kotliar)
- Phonons (intraband) and e-e interactions (interband) –
 Tesanovic (s-wave, but gaps on different bands may have opposite sign)
- Many electron correlation theories (AF fluctuations, some with large U -> s-wave or d-wave)
- → Different than cuprates? U not as important?

 Accurate techniques are available (unlike early days of cuprate SC) but still need to still need high quality single crystals (some crystals are available).

Pirsa: 08110002 Page 49/69

Strontium Ruthenate

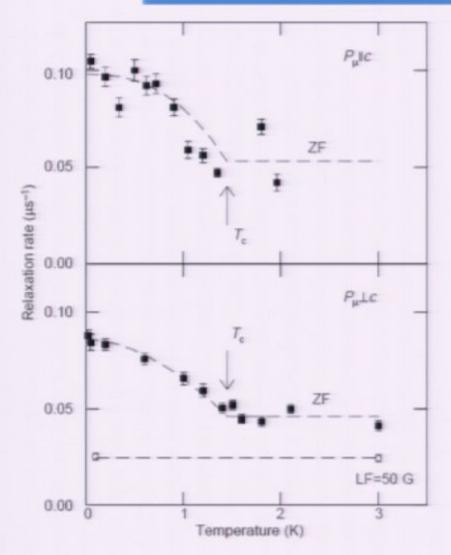




- Discovered in 1994 (Maeno)
- Same structure as cuprates
- Quasi-two-dimensional; multiband
- T_c ≤1.5K, strongly disorder dependent

→ unconventional pairing

ZF-muSR Decay Rate vs Temperature: Evidence for TRSB in SC State



Pirsa: 6800002 t al., Nature 394, 558 (1998).

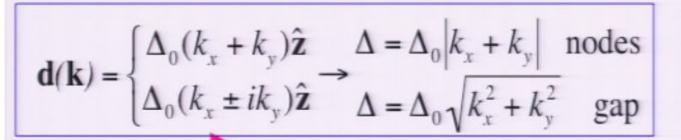
- Spontaneous field seen below T_c, for P_m//c, //a. B_{loc}~1G.
- NMR sees evidence for triplet pairing (spin susceptibility constant thru T_c) → p-wave.
- These and crystal symmetry point to chiral p-wave superconductivity

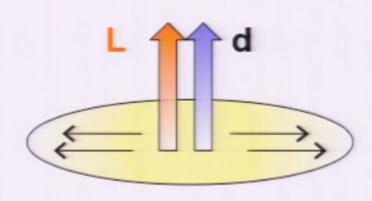
Introduction to px+ipy SC

$$S=1\Rightarrow \left|\uparrow\uparrow\rangle,\frac{1}{\sqrt{2}}\left(\left|\uparrow\downarrow\rangle+\left|\downarrow\uparrow\rangle\right\rangle\right),\left|\downarrow\downarrow\rangle\right\rangle$$

$$\Delta(\mathbf{k}) = i\{\mathbf{d}(\mathbf{k}) \cdot \mathbf{\sigma}\}\sigma_{\mathbf{y}}$$

2x2 matrix in s,s'. $d \| z \leftrightarrow S_z = 0$ or equal spin pairing in xy plane





Both d-vector and L aligned along c-axis equal spin pairing in ab-plane

Breaks time-reversal symmetry

$$\vec{L} = \hbar \hat{\mathbf{z}}$$

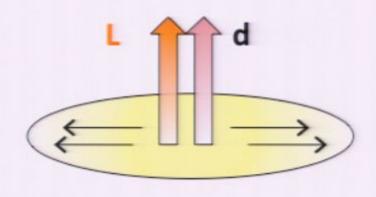
kx+iky degenerate with kx-iky

-> can have domains

Chiral p-wave Superconductivity

$$\mathbf{d}(\mathbf{k}) = \Delta_{_{0}}\hat{\mathbf{z}}(k_{x} \pm ik_{y})$$

Each Cooper pair carries angular momentum \hbar and the BCS SC state carries ang mom $\langle L_z \rangle = \hbar N/2$



- analogous to A phase of He-3
- topological state → Moore-Read QH state (Read & Green, 1999)
- Majorana zero modes at edges and vortex cores
- rotated d-vector → isolated Majorana zero modes

Pirsa: 08110002

Zero modes = Majorana Fermions

$$H\psi_{n} = \begin{pmatrix} h & \Delta \\ \Delta^{+} & -h^{T} \end{pmatrix} \begin{pmatrix} u_{n} \\ v_{n} \end{pmatrix} = E_{n}\psi_{n} \implies H = \sum_{n} E_{n}\gamma_{n}^{+}\gamma_{n}$$

$$\text{where } \gamma_{n}^{+} = \sum_{i} (u_{n}a_{i}^{+} + v_{n}a_{i})$$

$$H\psi_{n} = E_{n}\psi_{n} \implies H(\sigma_{1}\psi_{n}^{*}) = -E_{n}(\sigma_{1}\psi_{n}^{*})$$

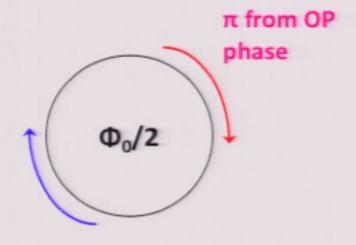
$$\sigma_{1} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

If $H\psi = 0$ then $H\sigma_1\psi^* = 0$. Let $\psi_0 = \psi + \sigma_1\psi^*$. Then $\sigma_1\psi_0^* = \psi_0$.

$$\psi_0 = \begin{pmatrix} u_0 \\ u_0^* \end{pmatrix} \Rightarrow \gamma_0^+ = \sum_i (u_0 a_i^+ + u_0^* a_i^-) = \gamma_0$$
 Majorana Fermion

Can have one Majorana zero mode at vortex

chiral p-wave and quantum computing



π from rotation of d-vector d-vector perpendicular to z

- may have half-quantum vortices with a single Majorana zero mode bound at the core
- → non-Abelian statistics (Ivanov, PRL 2001)
- fractionalization is protected by superconducting energy gap
- → useful for quantum computing because of the topological stability and non-trivial winding connects distinct, degenerate ground states with topological stability

NMR for H | | z may be explained by rotating d-vector

Zero modes = Majorana Fermions

$$H\psi_{n} = \begin{pmatrix} h & \Delta \\ \Delta^{+} & -h^{T} \end{pmatrix} \begin{pmatrix} u_{n} \\ v_{n} \end{pmatrix} = E_{n}\psi_{n} \implies H = \sum_{n} E_{n}\gamma_{n}^{+}\gamma_{n}$$

$$\text{where } \gamma_{n}^{+} = \sum_{i} (u_{n}a_{i}^{+} + v_{n}a_{i})$$

$$H\psi_{n} = E_{n}\psi_{n} \implies H(\sigma_{1}\psi_{n}^{*}) = -E_{n}(\sigma_{1}\psi_{n}^{*})$$

$$\sigma_{1} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

If $H\psi = 0$ then $H\sigma_1\psi^* = 0$. Let $\psi_0 = \psi + \sigma_1\psi^*$. Then $\sigma_1\psi_0^* = \psi_0$.

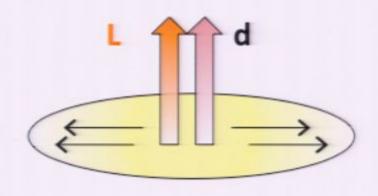
$$\psi_0 = \begin{pmatrix} u_0 \\ u_0^* \end{pmatrix} \Rightarrow \gamma_0^+ = \sum_i (u_0 a_i^+ + u_0^* a_i) = \gamma_0$$
 Majorana Fermion

Can have one Majorana zero mode at vortex

Chiral p-wave Superconductivity

$$\mathbf{d}(\mathbf{k}) = \Delta_{_{0}}\hat{\mathbf{z}}(k_{x} \pm ik_{y})$$

Each Cooper pair carries angular momentum \hbar and the BCS SC state carries ang mom $\langle L_z \rangle = \hbar N/2$



- analogous to A phase of He-3
- topological state → Moore-Read QH state (Read & Green, 1999)
- Majorana zero modes at edges and vortex cores
- rotated d-vector → isolated Majorana zero modes

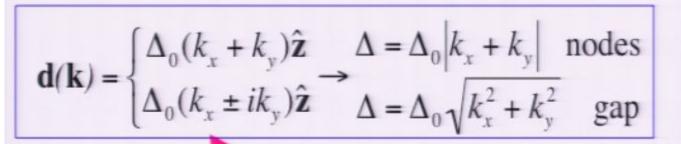
Pirsa: 08110002

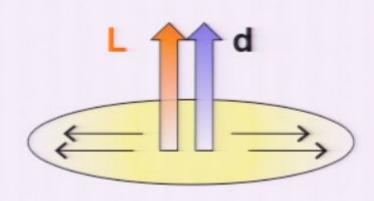
Introduction to px+ipy SC

$$S=1\Rightarrow \left|\uparrow\uparrow\rangle\right\rangle, \frac{1}{\sqrt{2}}\left(\left|\uparrow\downarrow\rangle\right\rangle + \left|\downarrow\uparrow\rangle\right\rangle\right), \; \left|\downarrow\downarrow\rangle\right\rangle$$

$$\Delta(\mathbf{k}) = i\{\mathbf{d}(\mathbf{k}) \cdot \mathbf{\sigma}\}\sigma_{\mathbf{y}}$$

2x2 matrix in s,s'. $d \| z \leftrightarrow S_z = 0$ or equal spin pairing in xy plane





Both d-vector and L aligned along c-axis equal spin pairing in ab-plane

Breaks time-reversal symmetry

$$\vec{L} = \hbar \hat{\mathbf{z}}$$

k_x+ik_y degenerate with k_x-ik_y

> can have domains

Zero modes = Majorana Fermions

$$H\psi_{n} = \begin{pmatrix} h & \Delta \\ \Delta^{+} & -h^{T} \end{pmatrix} \begin{pmatrix} u_{n} \\ v_{n} \end{pmatrix} = E_{n}\psi_{n} \implies H = \sum_{n} E_{n}\gamma_{n}^{+}\gamma_{n}$$

$$\text{where } \gamma_{n}^{+} = \sum_{i} (u_{n}a_{i}^{+} + v_{n}a_{i})$$

$$H\psi_{n} = E_{n}\psi_{n} \implies H(\sigma_{1}\psi_{n}^{*}) = -E_{n}(\sigma_{1}\psi_{n}^{*})$$

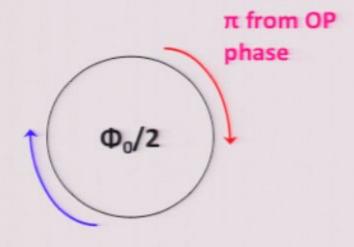
$$\sigma_{1} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

If $H\psi = 0$ then $H\sigma_1\psi^* = 0$. Let $\psi_0 = \psi + \sigma_1\psi^*$. Then $\sigma_1\psi_0^* = \psi_0$.

$$\psi_0 = \begin{pmatrix} u_0 \\ u_0^* \end{pmatrix} \Rightarrow \gamma_0^+ = \sum_i (u_0 a_i^+ + u_0^* a_i) = \gamma_0$$
 Majorana Fermion

Can have one Majorana zero mode at vortex

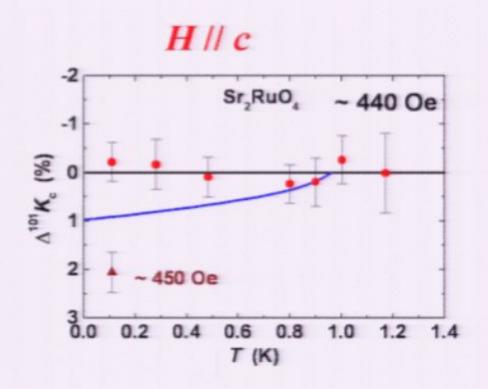
chiral p-wave and quantum computing



π from rotation of d-vector d-vector perpendicular to z

- may have half-quantum vortices with a single Majorana zero mode bound at the core
- non-Abelian statistics (Ivanov, PRL 2001)
- fractionalization is protected by superconducting energy gap
- → useful for quantum computing because of the topological stability and non-trivial winding connects distinct, degenerate ground states with topological stability

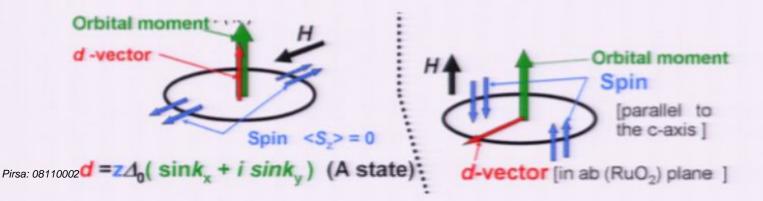
NMR for H | | z may be explained by rotating d-vector



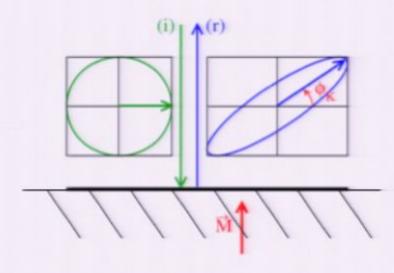
[From Ishida (KITP 2007)]

More recent NMR with H | c also found no supression of Knight shift below Tc

- → triplet with spins along c?
- → not necessarily same orbital state
- → NMR lineshapes broader



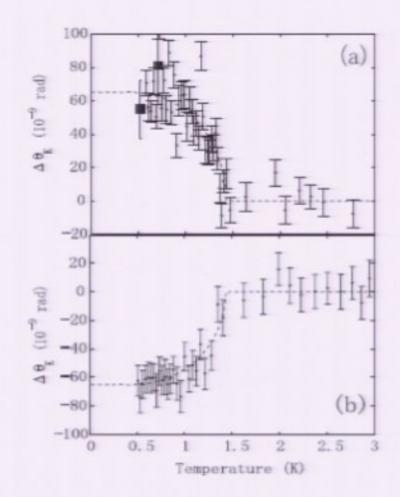
Polar Kerr effect



Linearly polarized light is reflected as elliptically polarized light, with rotation of polarization axis by Kerr angle

Measure magnetization perpendicular to surface in FM

Requires broken time-reversal symmetry



Cooled in (a) 93 G (b) -43 G $[\omega$ =0.8ev; Θ =60 nanorads]

J. Xia, Y. Maeno, P.T. Beyersdorf, M.M. Fejer, A. Kapitulnik, PRL 97, 167002 (2006).

Clean chiral p-wave SC has $\sigma_{xy}(k,\omega) \rightarrow 0$ for $k \rightarrow 0$, although interesting signatures at finite k.

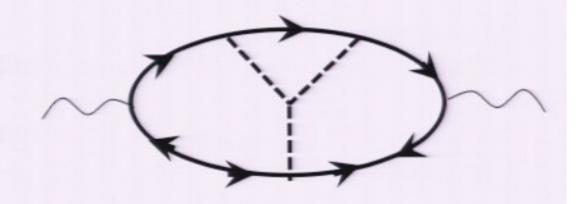
One can show lowest disorder contribution (n_iU²) also vanishes.

Goryo identified diagrams of order n_iU³ (skew scattering) which contribute.

 $Tr[\tau_3G(p)G(k)]=2i\Delta^2sin\theta$ $\Rightarrow sin^2\theta \Rightarrow nonzero, only for l=1!$

~ comparable to experiment; a bit small & likely to be reduced

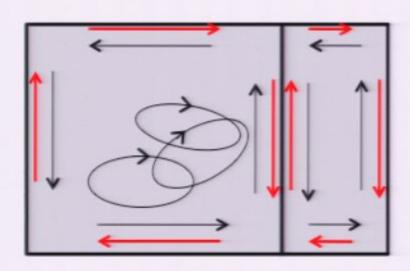
Explanation? Test by studying disorder and frequency dependence of Kerr effect.



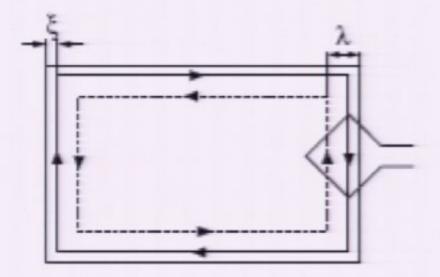
$$\sigma_{xy}^{(v)}(\omega) = \gamma_{BCS}^2 \left(1 - \frac{T}{T_c}\right) \frac{l_i}{\xi_0} \left(\frac{\epsilon_F}{\pi \tau_0}\right)^{3/2} \frac{\sigma_{xy}^{(0)}}{(\omega + i/\tau_0)^3}$$

Jun Goryo, arXiv:0806.0548age 63/69

Spontaneous equilibrium supercurrents flow at the edges and domain walls (related to macroscopic angular momentum of the chiral p-wave state). These are screened by counterflowing supercurrents.



Stone and Roy (2004) Matsumato and Sigrist (1999)



Can detect the field due to these currents with scanning SQUID microscopy

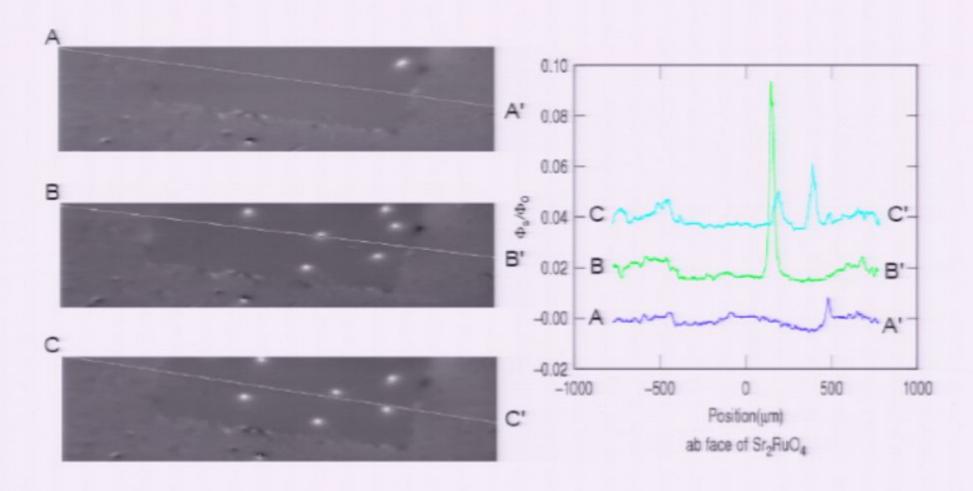
Fig. 5. Electric currents (solid lines) of the chiral edge states along the inner and outer edges of Sr₂RuO₄. The dashed lines show superfluid counterflow. The rectangular coil on the right represents a SQUID pickup loop.

Pirsa: 08110002

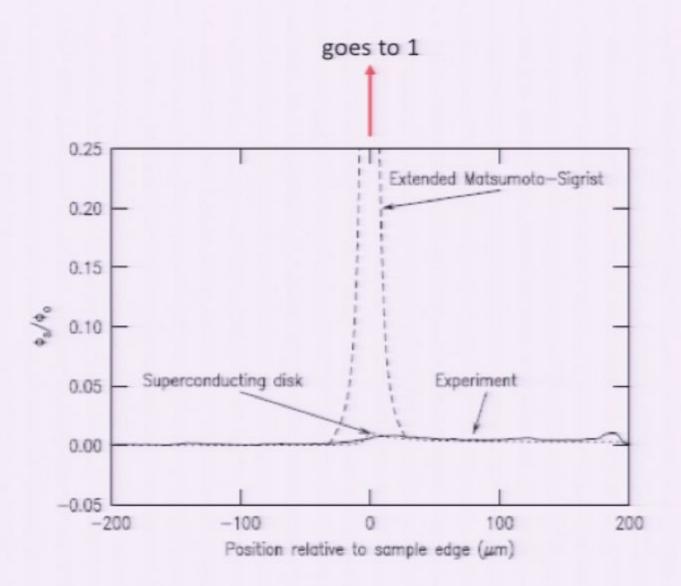
Page 64/69

Scanning SQUID microscopy: search for edge and domain currents

J.R. Kirtley, C. Kallin, C. Hicks, E.A. Kim, Y. Liu, K.A. Moler, Y. Maeno, PRB (2007).



Pirsa: 08110002 Page 65/69



Pirsa: 08110002 Page 66/69

No (weak) spontaneous edge currents ← → chiral p-wave?

- Rough and pairbreaking surfaces cause little suppression
- Alternative to BCS wave function proposed by Leggett

$$|\psi_{\text{BCS}}\rangle = \prod_{k} (u_k + v_k a_{k\uparrow}^+ a_{-k\downarrow}^+)|0\rangle \qquad u_k = |u_k|, \ v_k = |v_k|e^{i\phi_k}$$

$$|\psi_N\rangle = \sum_p f_p(\Omega_+)^p(\Omega_-)^p|FS\rangle$$
 $\Omega_+ = \sum_{k>k_f} \frac{v_k}{u_k} a_k^+ a_{-k}^+ \quad \Omega_- = \sum_{k< k_f} \frac{u_k}{v_k} a_{-k} a_k$

$$L_{\rm BCS} = N\hbar/2 \quad \Leftrightarrow \quad L_{\rm Leggett} = \left(\frac{\Delta}{E_f}\right)^2 N\hbar/2$$

Pirsa: 08110002 Page 67/69

Time Reversal Symmetry Breaking

Experiment	TRSB?	Domain size [limit >0.3µ]
muSR (Luke & Ishida)	Yes	< 2 µ
Kerr rotation (Kapitulnik)	Yes	> 50 µ with field cooling ~> 15-20 µ in ZFC
Scanning Hall Probe (Moler)	No	< 1 µ
SQUID (Kirtley)	No	< 2 µ
Tunneling (van Harlingen)	Yes	< 1 μ ~0.5 μ dynamic
Tunneling (Liu) Corner junctions Pirsa: 08110002	Parity Yes	>10-50 µ Page 68/69

Conclusion

- In SRO questions remain about symmetry and angular momentum of BCS state. Compelling evidence for chiral order, but lack of edge supercurrents puzzling. Note Leggett's wave function would also give very reduced muSR signal.
- In cuprates, Hubbard model yields many competing orders and many signatures seen in the pseudogap phase. Still much to understand about this phase and connection to high Tc.
- Fe superconductors field is moving rapidly but nature of superconductivity and connection to cuprates still under debate.

Pirsa: 08110002