Title: Structure Beyond the Horizon: Inflationary Origins of the Cosmic Power Asymmetry

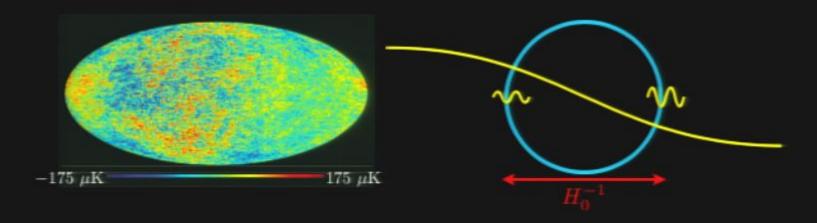
Date: Oct 14, 2008 04:00 PM

URL: http://pirsa.org/08100031

Abstract: WMAP measurements of CMB temperature anisotropies reveal a power asymmetry: the average amplitude of temperature fluctuations in one hemisphere is larger than the average amplitude in the opposite hemisphere at the 99% confidence level. This power asymmetry may be generated during inflation by a large-amplitude superhorizon perturbation that causes the mean energy density to vary across the observable Universe. Such a superhorizon perturbation would also induce large-scale temperature anisotropies in the CMB; measurements of the CMB quadrupole and octupole (but not the dipole!) therefore constrain the perturbation\'s amplitude and wavelength. I will show how a superhorizon perturbation in a multi-field inflationary theory, the curvaton model, can produce the observed power asymmetry without generating unacceptable temperature fluctuations in the CMB. I will also discuss how this mechanism for generating the power asymmetry will be tested by forthcoming CMB experiments.

Pirsa: 08100031 Page 1/97

Structure Beyond the Horizon: Inflationary Origins of the Cosmic Power Asymmetry



Adrienne Erickcek California Institute of Technology

In collaboration with Sean Carroll and Marc Kamionkowski

"A Hemispherical Power Asymmetry from Inflation" arXiv:0806.0377
"Superhorizon Perturbations and the CMB" arXiv:0808.1570

Outline

I. Power Asymmetry from Superhorizon Structure

- What power asymmety?
- How can we make one?

II. Superhorizon Perturbations and the CMB

- If there were superhorizon structures, how would we know?
- Bad news...

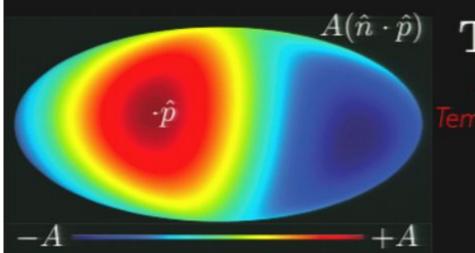
III. The Curvaton Alternative

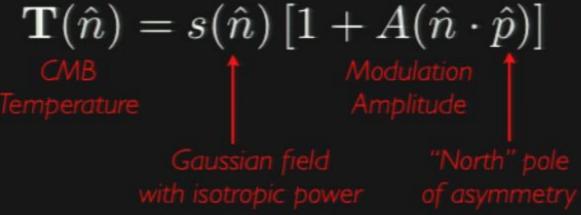
- What went wrong, and how do we fix it?
- What's a curvaton anyway?

IV. A Power Asymmetry from the Curvaton

- How can we make a power asymmetry?
- Does it work?
- Pratical do we test it?

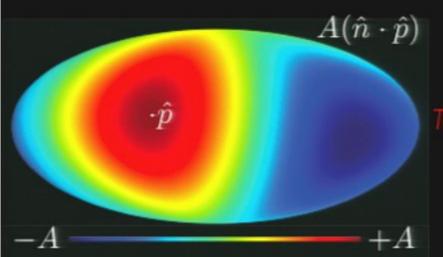
A Hemispherical Power Asymmety





Pirsa: 08100031 Page 4/97

A Hemispherical Power Asymmety

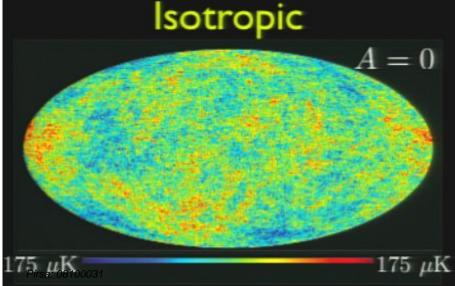


$$\mathbf{T}(\hat{n}) = s(\hat{n}) \left[1 + A(\hat{n} \cdot \hat{p})
ight]$$

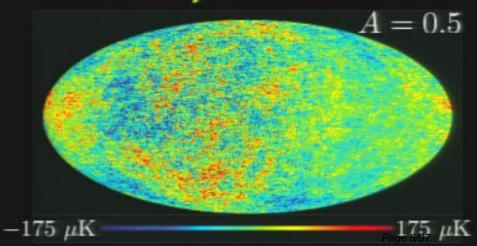
CMB
Temperature

Gaussian field

Worth" pole with isotropic power of asymmetry

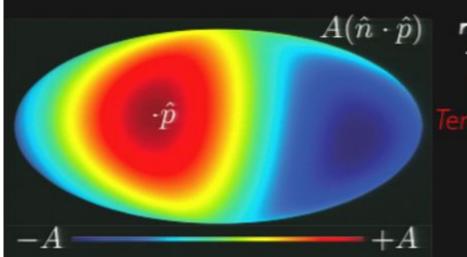






Simulated maps courtesy of H. K. Eriksen

A Hemispherical Power Asymmety

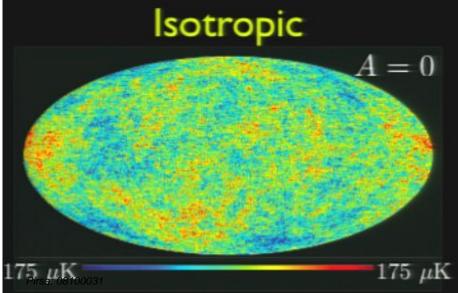


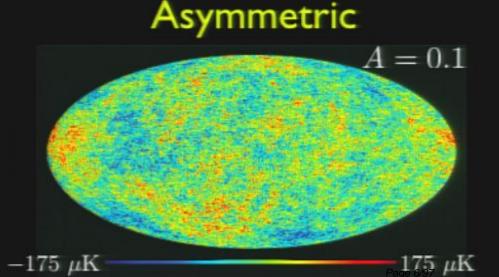
$$\mathbf{T}(\hat{n}) = s(\hat{n}) \left[1 + A(\hat{n} \cdot \hat{p})
ight]$$

CMB
Temperature

Gaussian field

with isotropic power of asymmetry

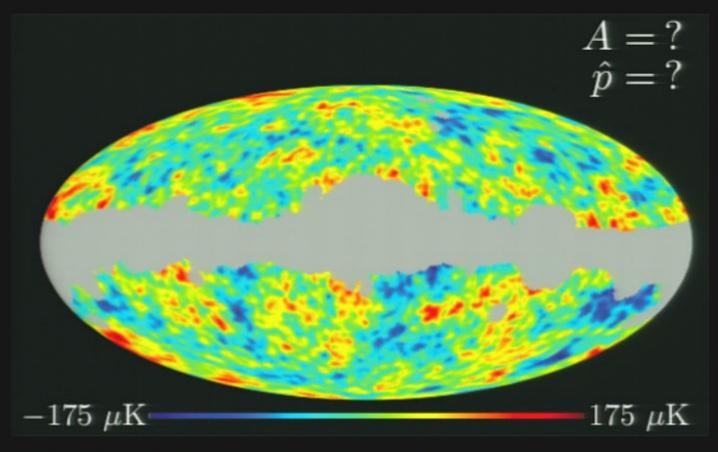




Simulated maps courtesy of H. K. Eriksen

A Power Asymmety?

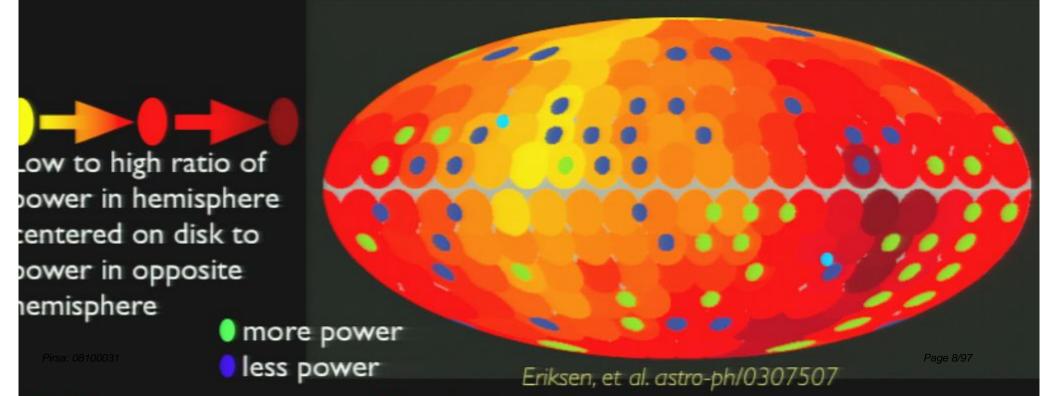
Isotropic or Asymmetric?



WMAP First Year Low-Resolution Map

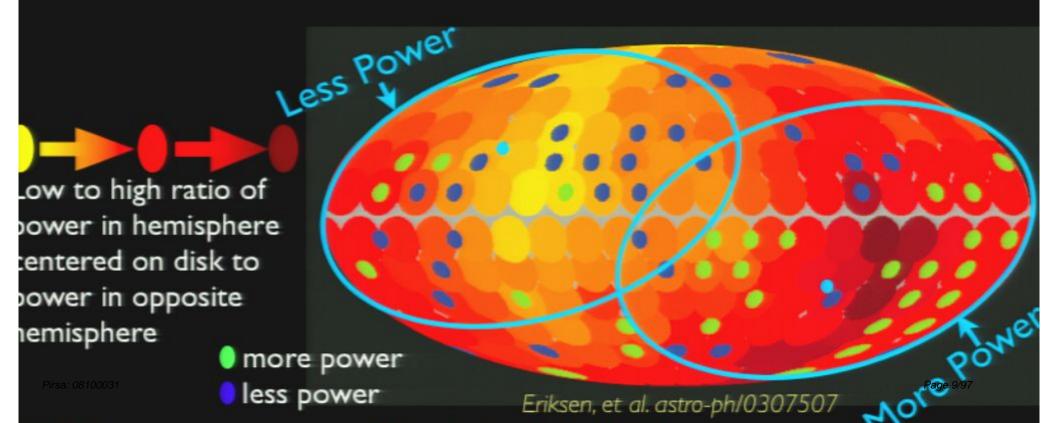
There is a power asymmetry on large angular Eriksen, Hansen, Banday, Gorski, Lilje 2004

Scales in the WMAP 1st year data.



There is a power asymmetry on large angular Eriksen, Hansen, Banday, Gorski, Lilje 2004

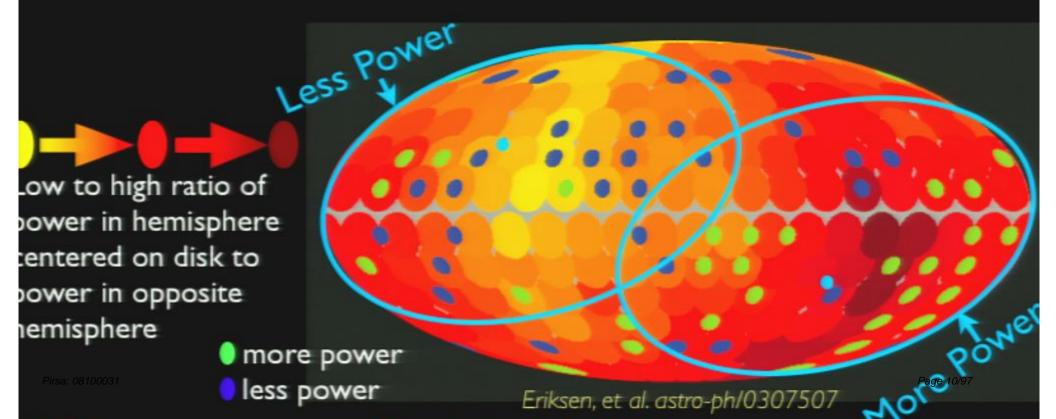
Scales in the WMAP 1st year data.



There is a power asymmetry on large angular Eriksen, Hansen, Banday, Gorski, Lilje 2004

Scales in the WMAP 1st year data.

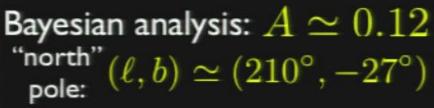
- Power asymmetry is maximized when the "equatorial" plane is tilted with respect to the Galactic plane: "north" pole at $(\ell,b)=(237^\circ,-10^\circ)$.
- Only 0.7% of simulated symmetric maps contain this much asymmetry.



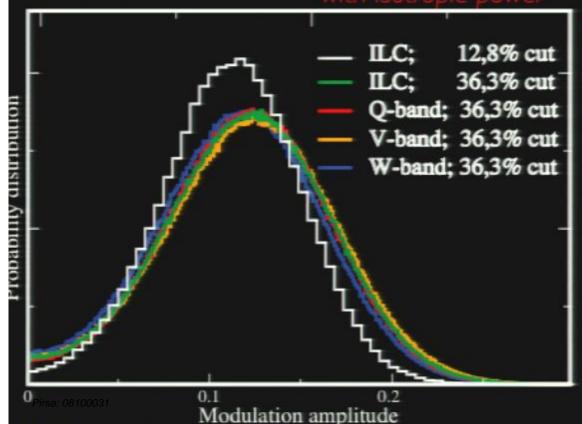
The asymmetry persists in the WMAP3 data.

Eriksen, Banday, Gorski, Hansen, Lilje 2007

 $\mathbf{T}(\hat{n}) = s(\hat{n}) \left[1 + A(\hat{n} \cdot \hat{p}) \right] + \mathbf{N}(\hat{n})$



The probability of measuring this amplitude or larger given an isotropic field is 0.01.

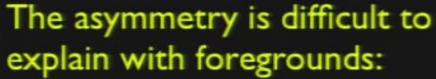


Friksen et al astro-ph/070108

The asymmetry persists in the WMAP3 data.

Eriksen, Banday, Gorski, Hansen, Lilje 2007

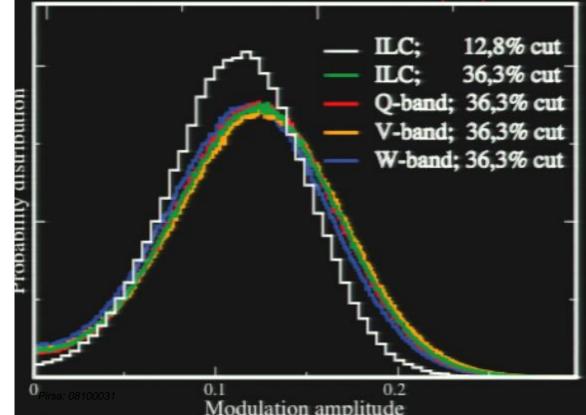
$$\mathbf{T}(\hat{n}) = s(\hat{n}) \left[1 + A(\hat{n} \cdot \hat{p}) \right] + \mathbf{N}(\hat{n})$$



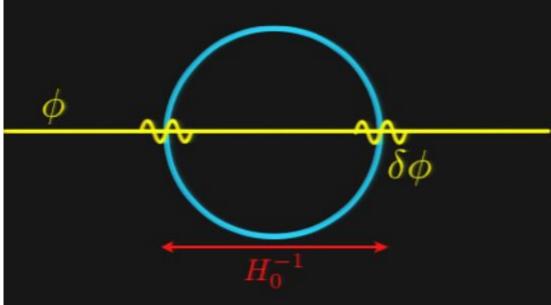
- present in all colors
- not aligned with the Galaxy

The asymmetry is difficult to explain with systematics:

also detected by COBE Hansen, et al. 2004, Eriksen, et al. 2004



Modulation amplitude Friksen et al. astro-ph/070108



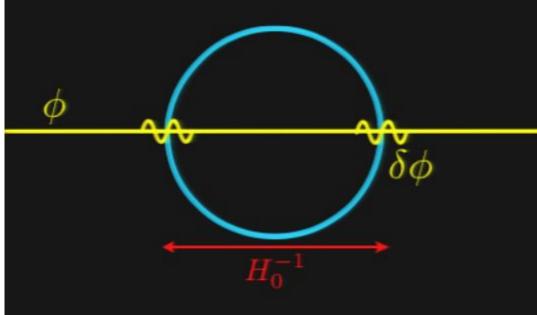
The amplitude of quantum fluctuations depends on the background value of the inflaton field.

$$P_{\Psi} = \frac{2}{9k^3} \left[\frac{H(\phi)^2}{\dot{\phi}} \right]^2 \bigg|_{k=aH}$$

Power Spectrum of Potential Fluctuations

$$ds^{2} = -(1 + 2\Psi)dt^{2} + a^{2}(t)\delta_{ij}(1 - 2\Psi)dx^{i}dx^{j}$$

Pirsa: 08100031 Page 13/97



The amplitude of quantum fluctuations depends on the background value of the inflaton field.

$$P_{\Psi} = \frac{2}{9k^3} \left[\frac{H(\phi)^2}{\dot{\phi}} \right]^2 \bigg|_{k=aH}$$

Power Spectrum of Potential Fluctuations
$$ds^2 = -(1+2\Psi)dt^2 + a^2(t)\delta_{ij}(1-2\Psi)dx^idx^j$$
 $\delta\phi$ Create asymmetry by adding a large-amplitude

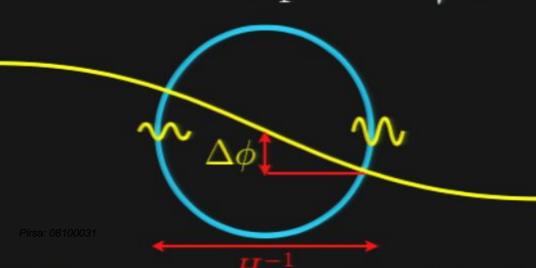
adding a large-amplitude superhorizon fluctuation: a "supermode."

A modulation amplitude
$$A \simeq 0.12 \Longrightarrow \frac{\Delta P_{\Psi}(k)}{P_{\Psi}(k)_{360^{\circ}}} \simeq \pm 0.20$$

Generating this much asymmetry requires a BIG supermode.

- Perturbations with different wavelengths are very weakly coupled.
- The fluctuation power is not very sensitive to $\phi \iff n_s \simeq 1$.

$$\frac{\Delta P_{\Psi}}{P_{\Psi}} = -2\sqrt{\frac{\pi}{\epsilon}}(1 - n_s)\frac{\Delta \phi}{m_{\rm Pl}}$$

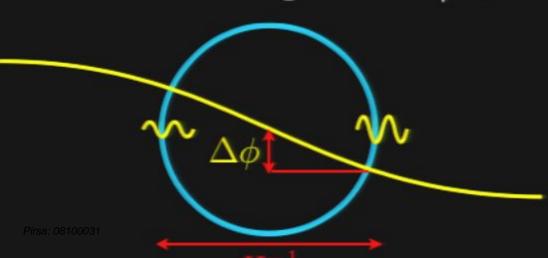


A modulation amplitude
$$A \simeq 0.12 \Longrightarrow \frac{\Delta P_{\Psi}(k)}{P_{\Psi}(k)_{360^{\circ}}} \simeq \pm 0.20$$

Generating this much asymmetry requires a BIG supermode.

- Perturbations with different wavelengths are very weakly coupled.
- The fluctuation power is not very sensitive to $\phi \iff n_s \simeq 1$.

$$\frac{\Delta P_{\Psi}}{P_{\Psi}} = -2\sqrt{\frac{\pi}{\epsilon}}(1 - n_s)\frac{\Delta \phi}{m_{\rm Pl}}$$



$$\Delta \phi \Longrightarrow \Delta \Psi \Longrightarrow \Delta T$$

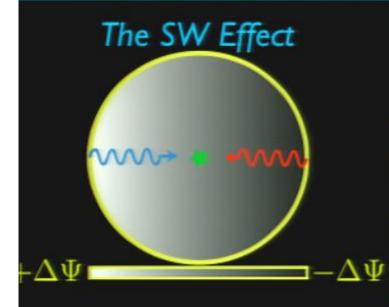
Surely the resulting temperature dipole would be far too large?

Page 16/97

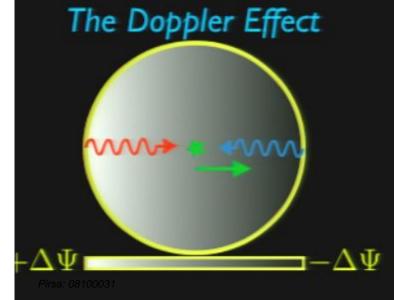
Part II

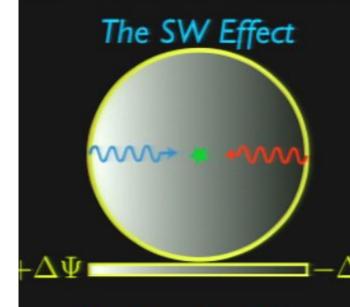
Superhorizon Perturbations and the Cosmic Microwave Background

Pirsa: 08100031 Page 17/97



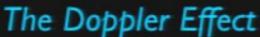
- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- The Doppler dipole:

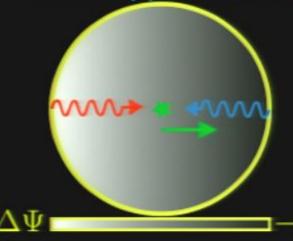


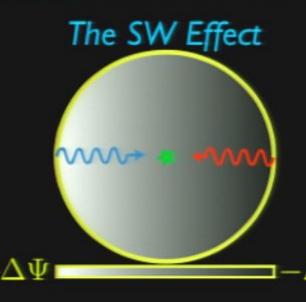


- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- The Doppler dipole:

$$\frac{\Delta T}{T} = \hat{n} \cdot \left[\vec{v}(t_0, \vec{0}) - \vec{v}(t_{\text{dec}}, \vec{x}_{\text{dec}}) \right]$$



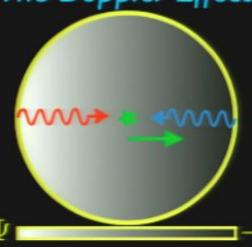


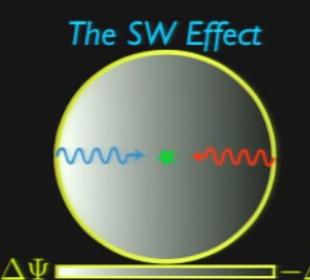


- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- The Doppler dipole:

$$\begin{split} \frac{\Delta T}{T} &= \hat{n} \cdot \left[\vec{v}(t_0, \vec{0}) - \vec{v}(t_{\rm dec}, \vec{x}_{\rm dec}) \right] \\ \hat{n} \cdot \vec{v}(t) &= -\frac{2}{3} \frac{\sqrt{a(t)}}{H_0 x_{\rm dec}} \left[\vec{x}_{\rm dec} \cdot \vec{\nabla} \Psi \right] \end{split}$$







In an Einstein - deSitter Universe, a superhorizon perturbation induces no CMB dipole. Grishchuk, Zel'dovich 1978

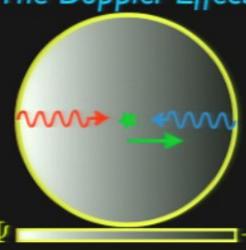
- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- The Doppler dipole:

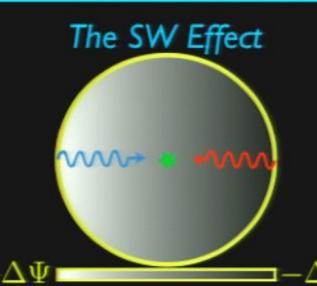
$$\frac{\Delta T}{T} = \hat{n} \cdot \left[\vec{v}(t_0, \vec{0}) - \vec{v}(t_{\text{dec}}, \vec{x}_{\text{dec}}) \right]$$

$$\hat{n} \cdot \vec{v}(t) = -\frac{2}{3} \frac{\sqrt{a(t)}}{H_0 x_{\text{dec}}} \left[\vec{x}_{\text{dec}} \cdot \vec{\nabla} \Psi \right]$$

$$H_0 x_{\text{dec}} = 2 \left[1 - \sqrt{a(t_{\text{dec}})} \right]$$

The Doppler Effect





In an Einstein - deSitter Universe, a superhorizon perturbation induces no CMB dipole. Grishchuk, Zel'dovich 1978

- lacktriangle A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- The Doppler dipole:

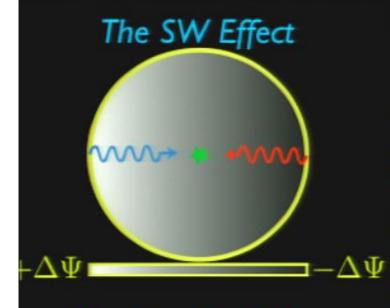
$$\frac{\Delta T}{T} = \hat{n} \cdot \left[\vec{v}(t_0, \vec{0}) - \vec{v}(t_{\text{dec}}, \vec{x}_{\text{dec}}) \right]$$

$$\hat{n} \cdot \vec{v}(t) = -\frac{2}{3} \frac{\sqrt{a(t)}}{H_0 x_{\text{dec}}} \left[\vec{x}_{\text{dec}} \cdot \vec{\nabla} \Psi \right]$$

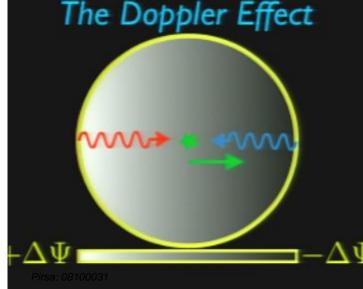
$$H_0 x_{\text{dec}} = 2 \left[1 - \sqrt{a(t_{\text{dec}})} \right]$$

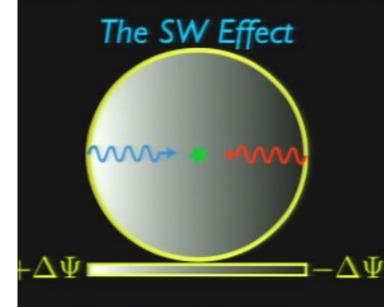
$$\frac{-\Delta\Psi}{T} = \frac{-(2/3)\left[1 - \sqrt{a(t_{\rm dec})}\right]}{2\left[1 - \sqrt{a(t_{\rm dec})}\right]} \Psi_{\rm SM} \left[\vec{k}_{\rm sg}, \vec{x}_{\rm dec}\right]$$

Pirsa: 08100031

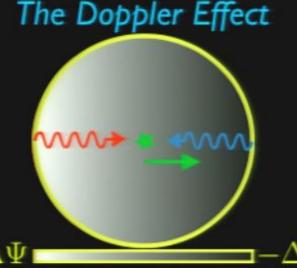


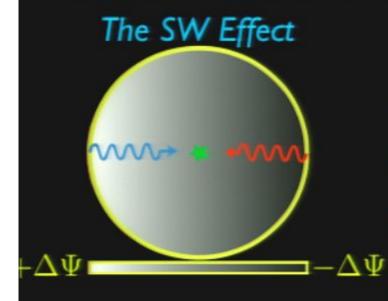
- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- The SW dipole: $\frac{\Delta T}{T} = \frac{1}{3} \Psi_{\rm SM} \left[\vec{k} \cdot \vec{x}_{\rm dec} \right]$
- $lackbox{\bullet}$ The Doppler dipole: $rac{\Delta T}{T} = -rac{1}{3}\Psi_{
 m SM}\left[ec{k}\cdotec{x}_{
 m dec}
 ight]$





- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- ullet The Doppler dipole: $rac{\Delta T}{T} = -rac{1}{3}\Psi_{
 m SM}\left[ec{k}\cdotec{x}_{
 m dec}
 ight]$
- Since Ψ is constant, there is no ISW effect.



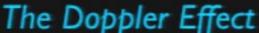


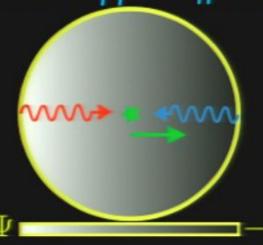
In an Einstein - deSitter Universe, a superhorizon perturbation induces no CMB dipole. Grishchuk, Zel'dovich 1978

- lacksquare A superhorizon mode: $\Psi(ec{x}) \simeq \Psi_{
 m SM} \left[ec{k} \cdot ec{x}
 ight]$
- ullet The SW dipole: $rac{\Delta T}{T} = rac{1}{3} \Psi_{
 m SM} \left[ec{k} \cdot ec{x}_{
 m dec}
 ight]$
- ullet The Doppler dipole: $rac{\Delta T}{T} = -rac{1}{3}\Psi_{
 m SM}\left[ec{k}\cdotec{x}_{
 m dec}
 ight]$
- Since Ψ is constant, there is no ISW effect.

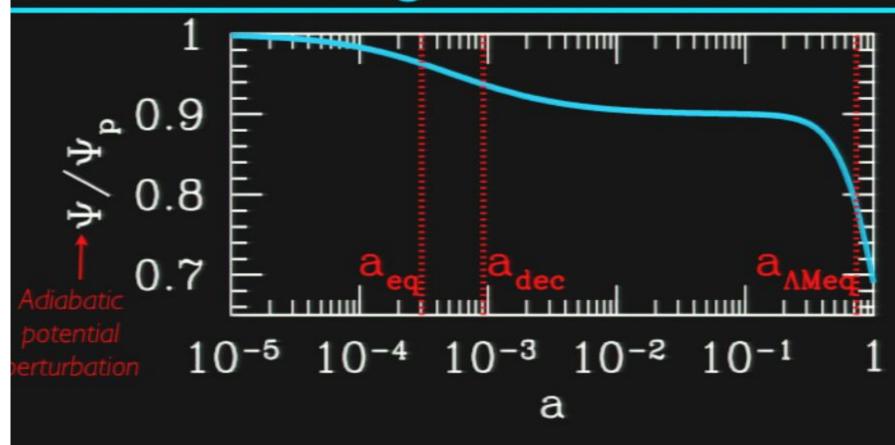
Well that's cute.

But the situation is much more complicated in a Universe like ours!



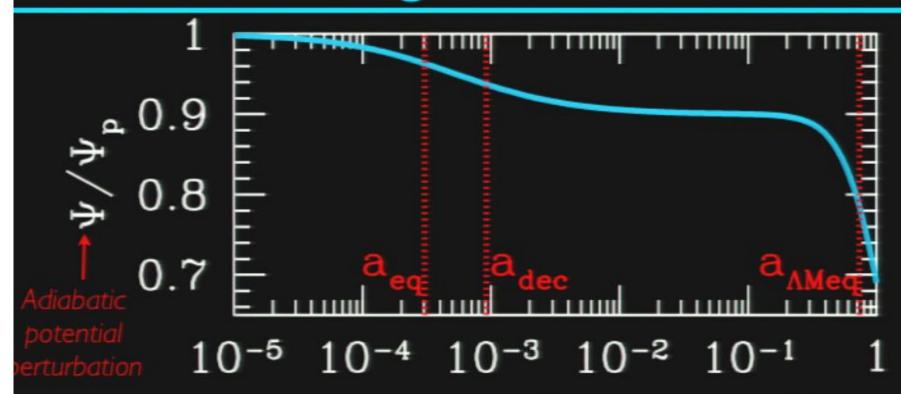


The Evolving Potential in Λ CDM



Pirsa: 08100031 Page 26/97

The Evolving Potential in Λ CDM



- lacksquare Radiation at decoupling increases SW effect: $\dfrac{\Delta T}{T}=0.4\Psi$
- lacktriangle Λ increases $x_{
 m dec}$ and reduces the Doppler dipole.
- Evolution of Ψ leads to ISW effect that will partially cancel the SW anisotropy: $\frac{\Delta T}{T} = 2 \int^{t_0} \frac{d\Psi}{dt} [t, \vec{x}(t)] dt$

The Dipole Cancels!

Adiabatic superhorizon perturbation:

$$\Psi(\vec{x}) = \Psi_{\rm SM} \begin{bmatrix} \vec{k} \cdot \vec{x} \end{bmatrix} \\ kH_0^{-1} \ll 1$$

emperature inisotropy:

$$\frac{\Delta T}{T}(\hat{n}) = \delta_1 \Psi_{\rm SM} \left[\vec{k} \cdot \vec{x}_{\rm dec} \right]$$

ncludes SW, Doppler and ISW misotropies

Pirsa: 08100031 Page 28/9

The Dipole Cancels!

Adiabatic superhorizon

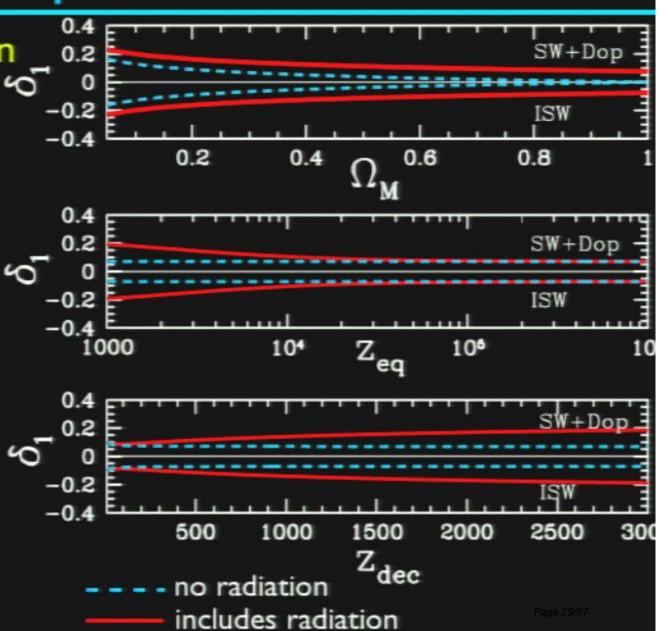
erturbation:

$$\Psi(\vec{x}) = \Psi_{\rm SM} \begin{bmatrix} \vec{k} \cdot \vec{x} \end{bmatrix} \\ kH_0^{-1} \ll 1$$

Temperature Inisotropy:

$$\frac{\Delta T}{T}(\hat{n}) = \delta_1 \Psi_{SM} \left[\vec{k} \cdot \vec{x}_{dec} \right]$$

ncludes SW, Doppler and ISW nisotropies



The Dipole Cancels!

Adiabatic superhorizon

perturbation:

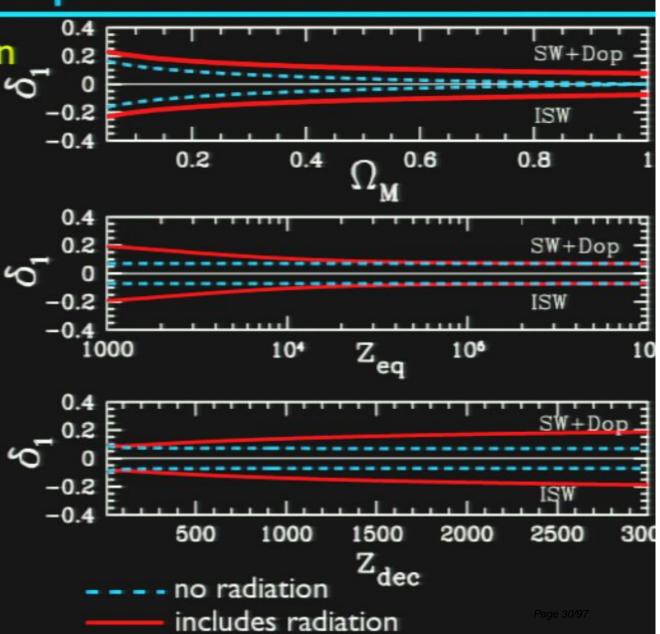
$$\Psi(\vec{x}) = \Psi_{\rm SM} \begin{bmatrix} \vec{k} \cdot \vec{x} \end{bmatrix} \\ kH_0^{-1} \ll 1$$

emperature inisotropy:

$$\frac{\Delta T}{T}(\hat{n}) = \delta_1 \Psi_{SM} \left[\vec{k} \cdot \vec{x}_{dec} \right]$$

ncludes SW, Doppler and ISW Inisotropies

The dipole cancels for all flat $\Lambda {
m CDM}$ universes, even if adiation is included.



Matter and radiation aren't special...

The $\mathcal{O}(kx_{\text{dec}})$ terms in ΔT for adiabatic perturbations cancel in flat universes that contain

- matter
- radiation
- cosmological constant

What if there's something else?

Pirsa: 08100031 Page 31/97

Matter and radiation aren't special...

The $\mathcal{O}(kx_{\rm dec})$ terms in ΔT for adiabatic perturbations cancel in flat universes that contain

- matter
- radiation
- cosmological constant

What if there's something else?
$$H^2(a)=H_0^2\left[rac{\Omega_X}{a^{3(1+w)}}+\Omega_\Lambda
ight]$$

Matter and radiation aren't special...

The $\mathcal{O}(kx_{\mathrm{dec}})$ terms in ΔT for adiabatic perturbations cancel in flat universes that contain

- matter
- radiation
- cosmological constant

What if there's something else?
$$H^2(a)=H_0^2\left[rac{\Omega_X}{a^{3(1+w)}}+\Omega_\Lambda
ight]$$

The dipole terms still cancel for adiabatic perturbations!

cosmologica constant

s there a physical reason for dipole cancellation in flat universes with uperhorizon adiabatic perturbations?

- ullet special synchronous gauge: metric is FRW + $\mathcal{O}(k^2H_0^{-2})$ Hirata and Seljak 2005
- galaxies have no peculiar velocity in synchronous gauge
- พาด $\mathcal{O}(kx_{
 m dec})$ temperature anisotropies

Beyond the Dipole

A single superhorizon mode:
$$\Psi(\vec{x},t)=\Psi_{\rm SM}(t)\sin[\vec{k}\cdot\vec{x}+\varpi]$$
 phase of our location

Pirsa: 08100031 Page 34/97

Beyond the Dipole

A single superhorizon mode: $\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$

$$kH_0^{-1} \ll 1$$

Temperature anisotropy: Expansion in powers of $\vec{k} \cdot \vec{x}_d$

$$\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \left[(\vec{k} \cdot \vec{x}_{\rm d}) \delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \right]$$

Beyond the Dipole

A single superhorizon mode: $\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$

Temperature anisotropy: Expansion in powers of $\vec{k} \cdot \vec{x}_{\rm d}$

$$\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \left[(\vec{k} \cdot \vec{x}_{\rm d}) \delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \right]$$

served CMB Dipole Quadrupole Octupole

Temperature Multipole moments:
$$\frac{\Delta T}{T}(\hat{n}) = \sum_{\ell,m} a_{\ell m} Y_{\ell m}(\hat{n}) \ \longleftarrow \hat{k} = \hat{z}$$

Beyond the Dipole

A single superhorizon mode: $\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$

$$kH_0^{-1} \ll 1$$

Temperature anisotropy: Expansion in powers of $\vec{k} \cdot \vec{x}_d$

$$\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \left[(\vec{k} \cdot \vec{x}_{\rm d}) \delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \right]$$

Temperature Multipole moments:
$$\frac{\Delta T}{T}(\hat{n}) = \sum_{\ell,m} a_{\ell m} Y_{\ell m}(\hat{n}) \ \, \longleftarrow \hat{k} = \hat{z}$$

$$a_{10} = -\sqrt{\frac{4\pi}{3}} (kx_{\rm d})^3 \delta_3 \frac{\cos \varpi}{10} \Psi_{\rm SM}(t_{\rm d})$$

- residual dipole moment
- comparable to octupole moment
- less restrictive constraint due to our proper motion

Beyond the Dipole

A single superhorizon mode: $\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$

$$kH_0^{-1} \ll 1$$

Temperature anisotropy: Expansion in powers of $\vec{k} \cdot \vec{x}_{\rm d}$

$$\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \left[(\vec{k} \cdot \vec{x}_{\rm d}) \delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \right]$$

Multipole moments: $\frac{\Delta T}{T}(\hat{n}) = \sum a_{\ell m} Y_{\ell m}(\hat{n}) \leftarrow \hat{k} = \hat{z}$

$$a_{10} = -\sqrt{\frac{4\pi}{3}} (kx_d)^3 \delta_3 \frac{\cos \varpi}{10} \Psi_{SM}(t_d)$$

- residual dipole moment
- comparable to octupole moment
- less restrictive constraint due to our proper motion

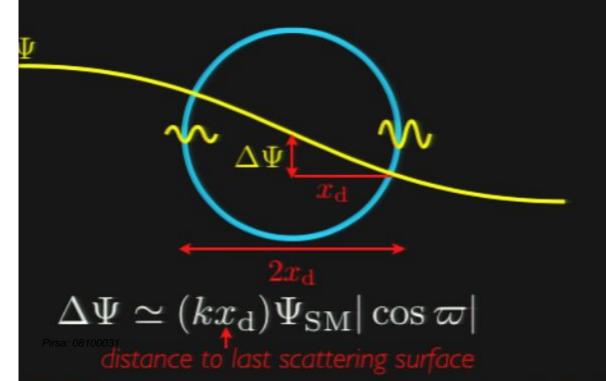
$$a_{20} = -\sqrt{\frac{4\pi}{5}}(kx_d)^2 \delta_2 \frac{\sin \varpi}{3} \Psi_{SM}(t_d)$$

$$a_{30} = -\sqrt{\frac{4\pi}{7}} (kx_{
m d})^3 \delta_3 \frac{\cos \varpi}{15} \Psi_{
m SM}(t_{
m d})$$

Supermode: $\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$ phase of our location

Recall the motivation: $\Delta\phi \Longrightarrow$ power asymmetry

$$\Delta \phi \Longrightarrow \Delta \Psi \Longrightarrow \Delta T$$



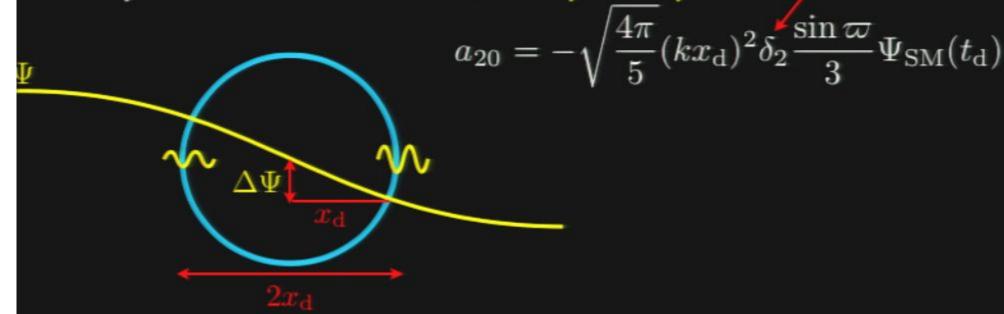
Page 39/9:

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 location

Recall the motivation: $\Delta\phi \Longrightarrow$ power asymmetry

$$\Delta \phi \Longrightarrow \Delta \Psi \Longrightarrow \Delta T$$

The supermode induces a CMB quadrupole: $\int_{0.5}^{\infty} e^{-0.33}$



 $\Delta\Psi \simeq (kx_{\rm d})\Psi_{\rm SM}|\cos\varpi|$

Page 40/97

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 location

Recall the motivation: $\Delta\phi \Longrightarrow$ power asymmetry

$$\Delta \phi \Longrightarrow \Delta \Psi \Longrightarrow \Delta T$$

The supermode induces a CMB quadrupole: 🤌

$$a_{20} = -\sqrt{\frac{4\pi}{5}} (kx_{\rm d})^2 \delta_2 \frac{\sin \varpi}{3} \Psi_{\rm SM}(t_{\rm d})$$

Quadrupole Constraint:

$$\Delta \Psi(kx_{\rm d}) |\tan \varpi| \lesssim 5.8Q$$

maximum allowed $|a_{20}|$

$$Q \lesssim 3\sqrt{C_2} \simeq 1.8 \times 10^{-5}$$

$$\Delta\Psi$$
 x_{d}
 $2x_{\mathrm{d}}$

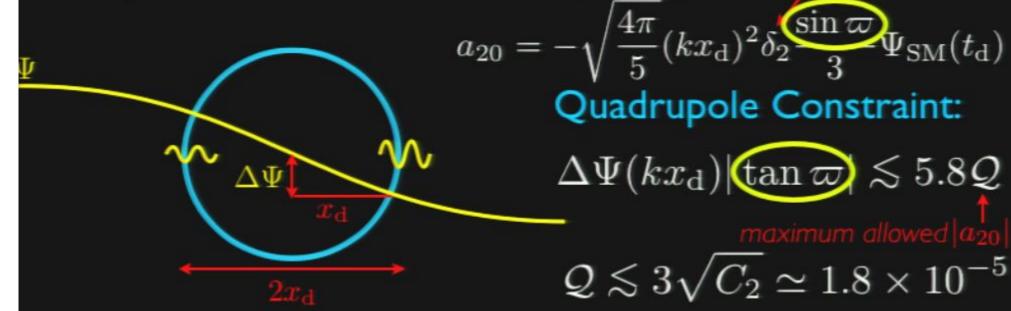
 $\Delta\Psi\simeq(kx_{
m d})\Psi_{
m SM}|\cosarpi$

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 location

Recall the motivation: $\Delta\phi \Longrightarrow$ power asymmetry

$$\Delta \phi \Longrightarrow \Delta \Psi \Longrightarrow \Delta T$$

The supermode induces a CMB quadrupole: $\int_{0.5}^{\infty} = 0.33$



 $\Delta\Psi\simeq (kx_{\rm d})\Psi_{\rm SM}|\cos\varpi|$ Quadrupole vanishes if $\varpi=0$.

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 phase of our location

The supermode induces a CMB octupole: $\delta_3 = 0.3$

$$a_{30} = -\sqrt{\frac{4\pi}{7}} (kx_{\rm d})^3 \delta_3 \frac{\cos \varpi}{15} \Psi_{\rm SM}(t_{\rm d})$$

$$2x_{\rm d}$$

$$\Delta\Psi \simeq (kx_{\rm d})\Psi_{\rm SM}|\cos\varpi|$$

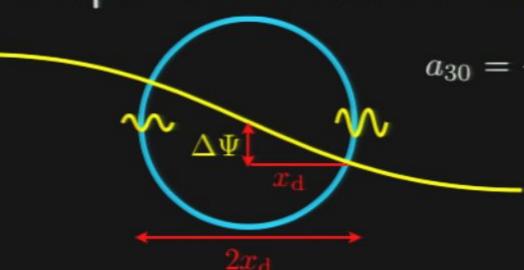
distance to last scattering surface

Pirsa: 08100031 Page 43/97

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 phase of our location

The supermode induces a CMB octupole:

$$\delta_3 = 0.35$$



$$\Delta\Psi \simeq (kx_{\rm d})\Psi_{\rm SM}|\cos\varpi|$$

distance to last scattering surface

$$a_{30} = -\sqrt{\frac{4\pi}{7}} (kx_{\rm d})^3 \delta_3 \frac{\cos \varpi}{15} \Psi_{\rm SM}(t_{\rm d})$$

Octupole Constraint:

$$\Delta \Psi(kx_{\rm d})^2 \lesssim 32\mathcal{O} \leftarrow |a_{30}|$$

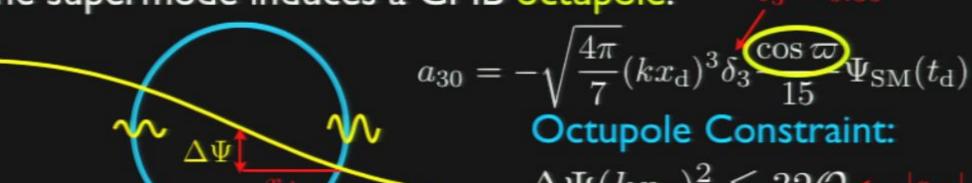
$$\mathcal{O} \lesssim 3\sqrt{C_3} \simeq 2.7 \times 10^{-5}$$

Pires: 08100031

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 phase of our location

The supermode induces a CMB octupole:

$$\delta_3 = 0.35$$



$$\Delta\Psi(kx_{\rm d})^2 \lesssim 32\mathcal{O} \leftarrow |a_{30}|$$

$$\mathcal{O} \lesssim 3\sqrt{C_3} \simeq 2.7 \times 10^{-5}$$

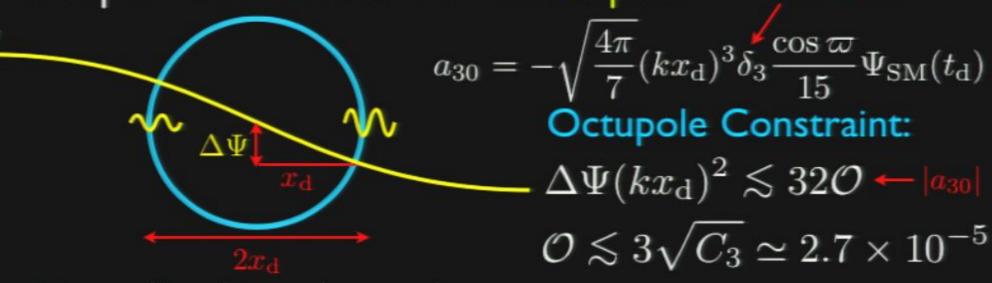
 $\Delta\Psi\simeq(kx_{\rm d})\Psi_{\rm SM}\cos\varpi$ Constraint is phase-independent.

Pirsa: 08100031 Page 45/97

Supermode:
$$\Psi(\vec{x},t)=\Psi_{\mathrm{SM}}(t)\sin[\vec{k}\cdot\vec{x}+arpi]$$
 phase of our location

The supermode induces a CMB octupole:

$$\delta_3 = 0.35$$



 $\Delta\Psi \simeq (kx_{
m d})\Psi_{
m SM}|\cos\varpi|$ distance to last scattering surface

Constraint is phase-independent.

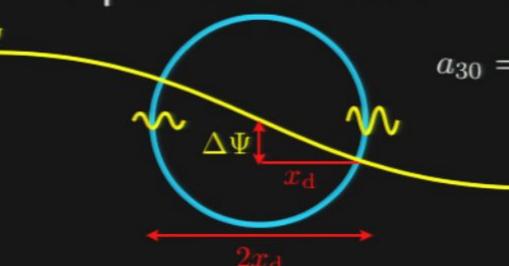
Evade constraint by decreasing kx_d ? Not if we want linearity beyond horizon!

$$|\Psi| \stackrel{\text{\tiny obs}}{<} 1 \Longrightarrow \Delta \Psi \lesssim kx_{\mathrm{d}}$$

Supermode:
$$\Psi(ec{x},t)=\Psi_{ ext{SM}}(t)\sin[ec{k}\cdotec{x}+arpi]$$
 phase of our location

The supermode induces a CMB octupole:

$$\delta_3 = 0.35$$



$$\Delta\Psi \simeq (kx_{\rm d})\Psi_{\rm SM}|\cos\varpi|$$

distance to last scattering surface

$$a_{30} = -\sqrt{\frac{4\pi}{7}} (kx_{\rm d})^3 \delta_3 \frac{\cos \varpi}{15} \Psi_{\rm SM}(t_{\rm d})$$

Octupole Constraint:

$$\Delta \Psi(kx_{\rm d})^2 \lesssim 32\mathcal{O} \leftarrow |a_{30}|$$

$$\mathcal{O} \lesssim 3\sqrt{C_3} \simeq 2.7 \times 10^{-5}$$

$$\Delta\Psi \lesssim [32\mathcal{O}]^{1/3} = 0.095$$

Recall:
$$\frac{\Delta P_{\Psi}}{P_{\Psi}} \propto \Delta \phi \propto \Delta \Psi$$

$$\left|rac{\Delta P_\Psi}{P_\Psi}\lesssim 0.01
ight|_{_{Page}4}$$

Supermode:
$$\Psi(\vec{x},t)=\Psi_{\mathrm{SM}}(t)\sin[\vec{k}\cdot\vec{x}+arpi]$$
 phase of our location

The supermode induces a CMB octupole:

$$\delta_3 = 0.35$$

$$a_{30} = -\sqrt{\frac{4\pi}{7}}(kx_{\rm d})^3 \delta_3 \frac{\cos\varpi}{15} \Psi_{\rm SM}(t_{\rm d})$$
Octupole Constraint:

Observed: $\frac{\Delta P_{\Psi}}{P_{\Psi}} \simeq 0.2$

Way too big!

$$\Psi(kx_{\rm d})^2 \lesssim 32\mathcal{O} \leftarrow |a_{30}|$$

$$3\sqrt{C_3} \simeq 2.7 \times 10^{-5}$$

$$\Psi \lesssim [32\mathcal{O}]^{1/3} = 0.095$$

all:
$$\frac{\Delta P_\Psi}{P_\Psi} \propto \Delta \phi \propto \Delta \Psi$$

$$\frac{\Delta P_{\Psi}}{P_{\Psi}} \lesssim 0.01$$

Part III The Curvaton Alternative

Mollerach 1990; Linde, Mukhanov 1997; Lyth, Wands 2002; Moroi, Takahashi 2001; and others...

Pirsa: 08100031 Page 49/97

The Curvaton to the Rescue!

The problem with the inflaton model is two-fold:

- The fluctuation power is only weakly dependent on the background value.
 - $P \Delta P \propto (1 n_s) \Delta \phi$
 - lacktriangle A small power asymmetry requires a large fluctuation in ϕ .
- The inflaton dominates the energy density of the universe, so a "supermode" in the inflaton field generates a huge potential perturbation.
 - CMB octupole places upper bound on $\Delta\Psi$.
 - lacksquare $\Delta P \propto \Delta \phi \propto \Delta \Psi$ with no wiggle room.

Pirsa: 08100031 Page 50/97

The Curvaton to the Rescue!

The problem with the inflaton model is two-fold:

- The fluctuation power is only weakly dependent on the background value.
 - $P \Delta P \propto (1 n_s) \Delta \phi$
 - lacktriangle A small power asymmetry requires a large fluctuation in ϕ .
- The inflaton dominates the energy density of the universe, so a "supermode" in the inflaton field generates a huge potential perturbation.
 - CMB octupole places upper bound on $\Delta\Psi$.
 - lacksquare $\Delta P \propto \Delta \phi \propto \Delta \Psi$ with no wiggle room.

The solution: the primordial fluctuations could be generated by a subdominant scalar field, the curvaton.

- The fluctuation power depends strongly on the background curvaton value.
- The CMB constraints on $\Delta\Psi$ do not directly constrain ΔP . There is a new free parameter: the fraction of energy in the curvaton.

- The inflaton still dominates the energy density and drives inflation.
- The curvaton (σ) is a subdominant light scalar field during inflation.

$$V(\sigma) = rac{1}{2} m_\sigma^2 \sigma^2$$
 with $m_\sigma \ll H_{
m inf}(\phi)$ and $ho_\sigma \ll
ho_\phi$ subdominant

Pirsa: 08100031 Page 52/97

- The inflaton still dominates the energy density and drives inflation.
- The curvaton (σ) is a subdominant light scalar field during inflation.

$$V(\sigma)=rac{1}{2}m_{\sigma}^2\sigma^2$$
 with $m_{\sigma}\ll H_{
m inf}(\phi)$ and $ho_{\sigma}\ll
ho_{\phi}$ potential light scalar field subdominant

There are quantum fluctuations in both the inflaton and curvaton.

$$(\delta\phi)_{\rm rms}=(\delta\sigma)_{\rm rms}=rac{H_{\rm inf}}{2\pi}\llar\sigma$$
 homogeneous auantum fluctuations

Pirsa: 08100031 Page 53/97

- The inflaton still dominates the energy density and drives inflation.
- The curvaton (σ) is a subdominant light scalar field during inflation.

$$V(\sigma)=rac{1}{2}m_{\sigma}^2\sigma^2$$
 with $m_{\sigma}\ll H_{
m inf}(\phi)$ and $ho_{\sigma}\ll
ho_{\phi}$ potential light scalar field subdominant

There are quantum fluctuations in both the inflaton and curvaton.

$$(\delta\phi)_{\rm rms}=(\delta\sigma)_{\rm rms}=rac{H_{\rm inf}}{2\pi}\llar\sigma$$
 thomogeneous duantum fluctuations

Outside the horizon, $\delta\sigma$ and $\bar{\sigma}$ obey the same equation of motion:

$$\ddot{\bar{\sigma}} + 3H\dot{\bar{\sigma}} + V'(\bar{\sigma}) = 0$$

$$\delta\ddot{\sigma} + 3H\delta\dot{\sigma} + \left[rac{k^2}{a^2} + V''(ar{\sigma})
ight]\delta\sigma = 0$$

- The inflaton still dominates the energy density and drives inflation.
- The curvation (σ) is a subdominant light scalar field during inflation.

$$V(\sigma)=rac{1}{2}m_\sigma^2\sigma^2$$
 with $m_\sigma\ll H_{
m inf}(\phi)$ and $ho_\sigma\ll
ho_\phi$ subdominant

There are quantum fluctuations in both the inflaton and curvation.

$$(\delta\phi)_{\rm rms}=(\delta\sigma)_{\rm rms}=rac{H_{\rm inf}}{2\pi}\llar\sigma$$
 thomogeneous duantum fluctuations

Outside the horizon, $\delta \sigma$ and $\bar{\sigma}$ obey the same equation of motion:

$$\ddot{\sigma}+3H\dot{\bar{\sigma}}+V'(\bar{\sigma})=0$$
 For superhorized is conserved by after inflation. $\delta\ddot{\sigma}+3H\delta\dot{\sigma}+\left[\frac{k_{//}^{2}}{\sqrt{2}}+V''(\bar{\sigma})\right]\delta\sigma=0$

For superhorizon perturbations, $\frac{\delta \sigma}{2}$ is conserved both during and

$$\delta \sigma = 0$$

The Curvaton after Inflation

The curvaton equation of motion: $\ddot{\sigma} + 3H\dot{\sigma} + m_{\sigma}^2\sigma^2 = 0$

- lacktriangle As long as $m_{\sigma} \ll H$, the curvaton is frozen: $\dot{\sigma} = 0$
- When $m_{\sigma} \simeq H$, the curvaton oscillates: $\langle \dot{\sigma}^2 \rangle = \langle m_{\sigma}^2 \sigma^2 \rangle$

$$p = \frac{1}{2}\dot{\sigma}^2 - \frac{1}{2}m_{\sigma}^2\sigma^2 \implies \langle p \rangle = 0$$

Pirsa: 08100031 Page 56/97

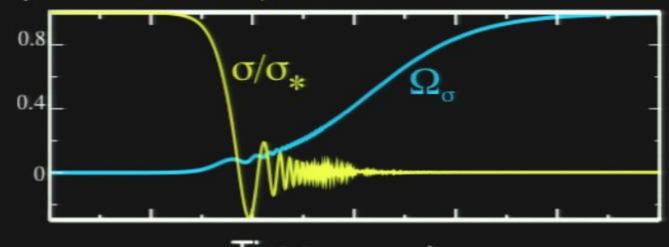
The Curvaton after Inflation

The curvaton equation of motion: $\ddot{\sigma} + 3H\dot{\sigma} + m_{\sigma}^2\sigma^2 = 0$

- lacktriangle As long as $m_{\sigma} \ll H$, the curvaton is frozen: $\dot{\sigma} = 0$
- When $m_{\sigma} \simeq H$, the curvaton oscillates: $\langle \dot{\sigma}^2 \rangle = \langle m_{\sigma}^2 \sigma^2 \rangle$

$$p = \frac{1}{2}\dot{\sigma}^2 - \frac{1}{2}m_{\sigma}^2\sigma^2 \implies \langle p \rangle = 0$$

While the curvaton oscillates, it behaves as matter: $ho_\sigma \propto a^{-3}$ Meanwhile, $ho_r \propto a$, so $ho_\sigma/
ho_r$ increases.



Time ———>
Langlois and Vernizzi, PRD 70 063522 (2004).

Growth of a Curvature Perturbation

Curvature perturbation: $\zeta = -\Psi - H \frac{\delta \rho}{\dot{\rho}}$

Superhorizon ζ is not conserved due to curvaton isocurvature

fluctuation, but $\zeta_i = -\Psi - H \frac{\delta \rho_i}{\dot{c}}$ is constant.

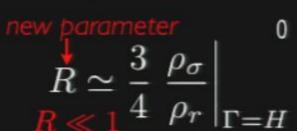
$$\zeta = \frac{4\rho_r \zeta_r + 3\rho_\sigma \zeta_\sigma}{4\rho_r + 3\rho_\sigma}$$

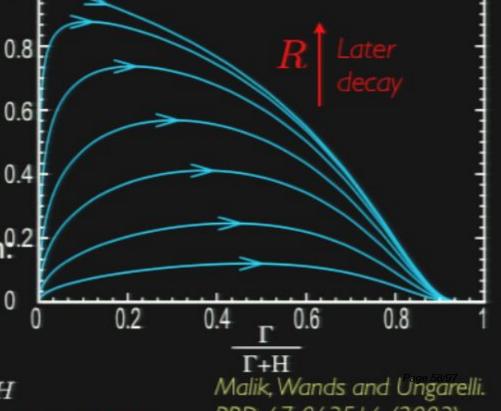
As ρ_{σ}/ρ_{r} increases, ζ evolves.

In the very early universe, the curvaton decays into radiation.

- lacktriangle decay at $\Gamma \simeq H$
- residual curvature perturbation.^{0.2}

$$\zeta=R\zeta_{\sigma}$$
 curvature perturbation





Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_\sigma = \frac{R}{3} \frac{\delta \rho_\sigma}{\rho_\sigma} \quad \text{where} \quad R \simeq \frac{3}{4} \left. \frac{\rho_\sigma}{\rho_r} \right|_{\Gamma = H}$$
 curvature perturbation evaluated just prior to curvaton decay

$$R \simeq \frac{3}{4} \left. \frac{\rho_{\sigma}}{\rho_{r}} \right|_{\Gamma=H}$$
 evaluated just prior to curvaton decay

and
$$R \ll 1$$
 keep the curvator subdominant

Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_\sigma = \frac{R}{3}\frac{\delta\rho_\sigma}{\rho_\sigma} \quad \text{where} \quad R \simeq \frac{3}{4}\frac{\rho_\sigma}{\rho_r}\bigg|_{\Gamma=H} \quad \text{and} \quad R \ll 1$$
 curvature perturbation evaluated just prior to curvaton decay

Curvaton energy:
$$\rho_{\sigma} = \frac{1}{2} m_{\sigma}^2 \sigma^2 \Longrightarrow \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} = 2 \left(\frac{\delta \sigma}{\bar{\sigma}} \right) + \left(\frac{\delta \sigma}{\bar{\sigma}} \right)^2$$

conserved outside horizon

Pirsa: 08100031 Page 60/97

Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_\sigma = \frac{R}{3}\frac{\delta\rho_\sigma}{\rho_\sigma} \quad \text{where} \quad R \simeq \frac{3}{4}\frac{\rho_\sigma}{\rho_r}\bigg|_{\substack{\Gamma = H \\ \text{evaluated just prior} \\ \text{to curvation}}} \quad \text{and} \quad R \ll 1$$

Curvaton energy:
$$\rho_{\sigma} = \frac{1}{2} m_{\sigma}^2 \sigma^2 \Longrightarrow \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} = 2 \left(\frac{\delta \sigma}{\bar{\sigma}} \right) + \left(\frac{\delta \sigma}{\bar{\sigma}} \right)^2$$

Quantum fluctuations:
$$\left(\delta\sigma\right)_{\mathrm{rms}}=\frac{H_{\mathrm{inf}}}{2\pi}\ll\bar{\sigma}$$

conserved outside horizon

Pirsa: 08100031 Page 61/97

Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_\sigma = \frac{R}{3}\frac{\delta\rho_\sigma}{\rho_\sigma} \quad \text{where} \quad R \simeq \frac{3}{4}\frac{\rho_\sigma}{\rho_r}\bigg|_{\substack{\Gamma = H \\ \text{evaluated just prior} \\ \text{to curvation}}} \quad \text{and} \quad R \ll 1$$

Curvaton energy:
$$\rho_{\sigma}=\frac{1}{2}m_{\sigma}^{2}\sigma^{2}\Longrightarrow \frac{\delta\rho_{\sigma}}{\rho_{\sigma}}=2\left(\frac{\delta\sigma}{\bar{\sigma}}\right)+\left(\frac{\delta\sigma}{\bar{\sigma}}\right)^{2}$$

Quantum
$$(\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi} \ll \bar{\sigma}$$

During matter domination,
$$\Psi = -\frac{3}{5}\zeta$$
.

Pirsa: 08100031 Page 62/97

Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_{\sigma} = \frac{R}{3} \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} \quad \text{where} \quad R \simeq \frac{3}{4} \frac{\rho_{\sigma}}{\rho_{r}} \bigg|_{\Gamma = H} \quad \text{and} \quad R \ll 1$$
 curvature perturbation evaluated just prior to curvaton decay

Curvaton energy:
$$\rho_{\sigma} = \frac{1}{2} m_{\sigma}^2 \sigma^2 \Longrightarrow \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} = 2 \left(\frac{\delta \sigma}{\bar{\sigma}} \right) + \left(\frac{\delta \sigma}{\bar{\sigma}} \right)^2$$

Quantum fluctuations:
$$(\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi} \ll \bar{\sigma}$$

During matter domination, $\Psi = -\frac{3}{5}\zeta$.

$$P_{\Psi,\sigma} \propto R^2 \left(\frac{H_{\rm inf}}{\bar{\sigma}_*}\right)^2$$

Page 63/97

Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_\sigma = \frac{R}{3}\frac{\delta\rho_\sigma}{\rho_\sigma} \quad \text{where} \quad R \simeq \frac{3}{4}\frac{\rho_\sigma}{\rho_r}\bigg|_{\Gamma=H} \quad \text{and} \quad R \ll 1$$
 curvature perturbation evaluated just prior to curvaton decay

Curvaton energy:
$$\rho_{\sigma} = \frac{1}{2} m_{\sigma}^2 \sigma^2 \Longrightarrow \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} = 2 \left(\frac{\delta \sigma}{\bar{\sigma}} \right) + \left(\frac{\delta \sigma}{\bar{\sigma}} \right)^2$$

Quantum $(\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi} \ll \bar{\sigma}$

During matter domination, $\Psi = -\frac{3}{5}\zeta$.

$$P_{\Psi,\sigma} \propto (\bar{\sigma}_*)^4 \left(\frac{H_{\rm inf}}{\bar{\sigma}_*}\right)^2$$

Page 64/97

Power Asymmetry from the Curvaton

Fluctuations in the curvaton field become curvature perturbations.

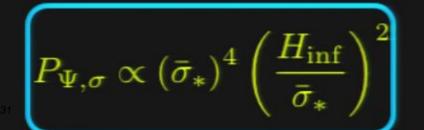
$$\zeta = R\zeta_{\sigma} = \frac{R}{3} \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} \quad \text{where} \quad R \simeq \frac{3}{4} \frac{\rho_{\sigma}}{\rho_{r}} \bigg|_{\Gamma = H} \quad \text{and} \quad R \ll 1$$
 curvature perturbation evaluated just prior to curvaton decay

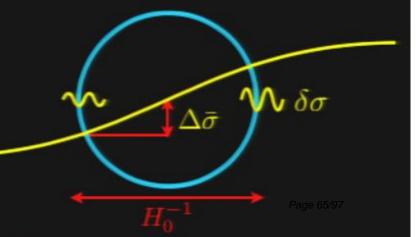
 $\delta \bar{\sigma}$

Curvaton energy:
$$\rho_{\sigma} = \frac{1}{2} m_{\sigma}^2 \sigma^2 \Longrightarrow \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} = 2 \left(\frac{\delta \sigma}{\bar{\sigma}} \right) + \left(\frac{\delta \sigma}{\bar{\sigma}} \right)^2$$

Quantum
$$\left(\delta\sigma\right)_{\mathrm{rms}}=rac{H_{\mathrm{inf}}}{2\pi}\llar{\sigma}$$

During matter domination,
$$\Psi = -\frac{3}{5}\zeta$$
. potential perturbation at decoupling





Power Asymmetry from the Curvaton

Fluctuations in the curvaton field become curvature perturbations.

$$\zeta = R\zeta_{\sigma} = \frac{R}{3} \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} \quad \text{where} \quad R \simeq \frac{3}{4} \frac{\rho_{\sigma}}{\rho_{r}} \bigg|_{\Gamma = H} \quad \text{and} \quad R \ll 1$$
 curvature perturbation evaluated just prior to curvaton decay

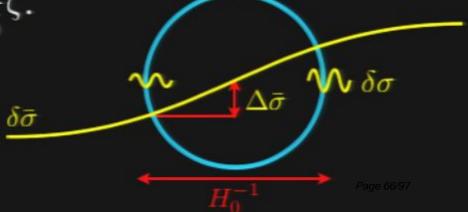
$$R \simeq \frac{3}{4} \frac{\rho_{\sigma}}{\rho_{r}}\Big|_{\Gamma=H}$$
evaluated just prio

Curvaton energy:
$$\rho_{\sigma} = \frac{1}{2} m_{\sigma}^2 \sigma^2 \Longrightarrow \frac{\delta \rho_{\sigma}}{\rho_{\sigma}} = 2 \left(\frac{\delta \sigma}{\bar{\sigma}} \right) + \left(\frac{\delta \sigma}{\bar{\sigma}} \right)^2$$

Quantum
$$\left(\delta\sigma\right)_{\mathrm{rms}}=rac{H_{\mathrm{inf}}}{2\pi}\llar{\sigma}$$

During matter domination,
$$\Psi = -\frac{3}{5}\zeta$$
.

$$\frac{\Delta P_{\Psi,\sigma}}{P_{\Psi,\sigma}} = 2\frac{\Delta \bar{\sigma}}{\bar{\sigma}}$$



Part IV A Power Asymmetry from the Curvaton

Piggs 08100031

Curvaton Supermodes in the CMB

Curvaton supermode:

$$\delta \bar{\sigma}(\vec{x},t) = \bar{\sigma}_{\rm SM}(t) \sin[\vec{k} \cdot \vec{x} + \vec{\omega}] \ kH_0^{-1} \ll 1 \ \delta \bar{\sigma}$$

The curvaton supermode generates a superhorizon potential fluctuation, but it is suppressed.

$$\Psi = -\frac{R}{5} \left[2 \left(\frac{\delta \bar{\sigma}}{\bar{\sigma}} \right) + \left(\frac{\delta \bar{\sigma}}{\bar{\sigma}} \right)^2 \right] - \frac{\delta \rho_{\sigma}}{\rho_{\sigma}}$$

The potential perturbation is not sinusoidal!



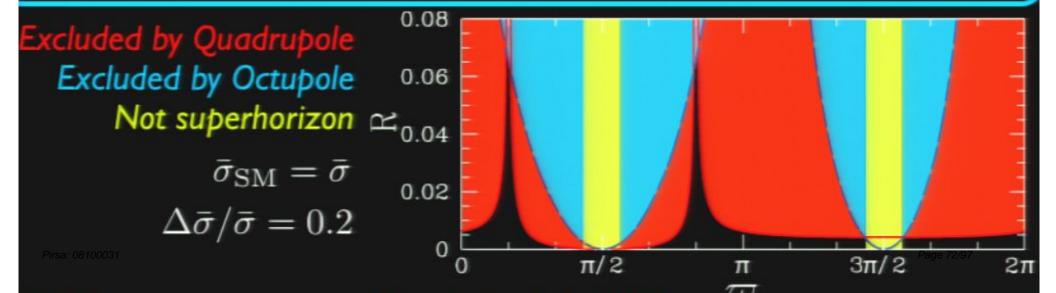
Part IV A Power Asymmetry from the Curvaton

Part IV A Power Asymmetry from the Curvaton

Piggs 08100031

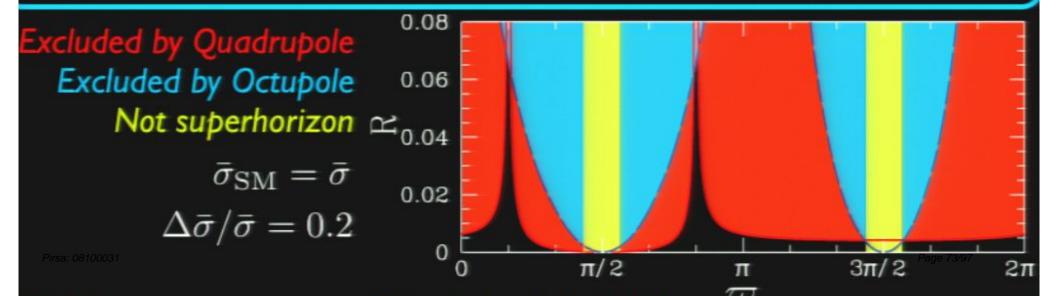
Curvaton Supermodes in the CMB

The CMB quadrupole implies an upper bound:



Curvaton Supermodes in the CMB

The CMB quadrupole implies an upper bound:



Perturbation Mixture

Both the curvaton and the inflaton may contribute to P_{Ψ} .

$$\epsilon \equiv \frac{m_{\rm Pl}^2}{16\pi} \left[\frac{V'(\phi)}{V(\phi)} \right]^2 \qquad (\delta\phi)_{\rm rms} = (\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi}$$

$$= \frac{m_{\rm Pl}^2}{16\pi} \left[\frac{V'(\phi)}{V(\phi)} \right]^2 \qquad (\delta\phi)_{\rm rms} = (\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi}$$

$$= \frac{R}{2\pi} \approx \frac{3}{4} \frac{\rho_{\sigma}}{\rho_{r}} \Big|_{\Gamma = H}$$

$$P_{\Psi, \phi} = \left(\frac{9}{10} \right)^2 \frac{8\pi}{9\epsilon} \left(\frac{H_{\rm inf}^2}{k^3 m_{\rm Pl}^2} \right) \qquad P_{\Psi, \sigma} = \left(\frac{2R}{5} \right)^2 \frac{H_{\rm inf}^2}{2k^3 \bar{\sigma}^2}$$

Pirsa: 08100031 Page 74/97

Perturbation Mixture

Both the curvaton and the inflaton may contribute to P_{Ψ} .

$$\epsilon \equiv \frac{m_{\rm Pl}^2}{16\pi} \left[\frac{V'(\phi)}{V(\phi)} \right]^2 \qquad (\delta\phi)_{\rm rms} = (\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi} \\ P_{\Psi,\phi} = \left(\frac{9}{10} \right)^2 \frac{8\pi}{9\epsilon} \left(\frac{H_{\rm inf}^2}{k^3 m_{\rm Pl}^2} \right) \qquad P_{\Psi,\sigma} = \left(\frac{2R}{5} \right)^2 \frac{H_{\rm inf}^2}{2k^3 \bar{\sigma}^2} \\ \text{Define a new parameter: } \xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$$

$$\xi = \frac{\tilde{\epsilon}}{\tilde{\epsilon} + 1} \quad \tilde{\epsilon} \equiv \frac{1}{9\pi} \left(\frac{m_{\rm Pl}}{\bar{\sigma}}\right)^2 R^2 \epsilon$$

$$\bar{\sigma} \ll m_{\rm Pl} \Longrightarrow \mathcal{E} \simeq 1$$

$$\bar{\sigma} \lesssim m_{\rm Pl} \Longrightarrow \xi \ll 1$$

Perturbation Mixture

Both the curvaton and the inflaton may contribute to $P_\Psi.$

$$\epsilon \equiv \frac{m_{\rm Pl}^2}{16\pi} \left[\frac{V'(\phi)}{V(\phi)} \right]^2 \qquad (\delta\phi)_{\rm rms} = (\delta\sigma)_{\rm rms} = \frac{H_{\rm inf}}{2\pi} \\ P_{\Psi,\phi} = \left(\frac{9}{10} \right)^2 \frac{8\pi}{9\epsilon} \left(\frac{H_{\rm inf}^2}{k^3 m_{\rm Pl}^2} \right) \qquad P_{\Psi,\sigma} = \left(\frac{2R}{5} \right)^2 \frac{H_{\rm inf}^2}{2k^3 \bar{\sigma}^2} \\ \text{Define a new parameter: } \xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$$

$$\xi = \frac{\tilde{\epsilon}}{\tilde{\epsilon} + 1} \quad \tilde{\epsilon} \equiv \frac{1}{9\pi} \left(\frac{m_{\rm Pl}}{\bar{\sigma}}\right)^2 R^2 \epsilon$$

$$\bar{\sigma} \ll m_{\rm Pl} \Longrightarrow \xi \simeq 1$$

$$\bar{\sigma} \lesssim m_{\rm Pl} \Longrightarrow \xi \ll 1$$

Tensor-Scalar Ratio:

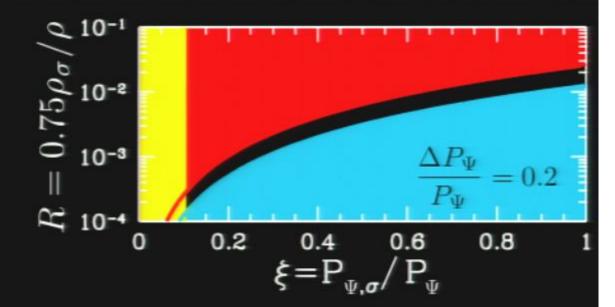
$$r = 16\epsilon(1 - \xi)$$

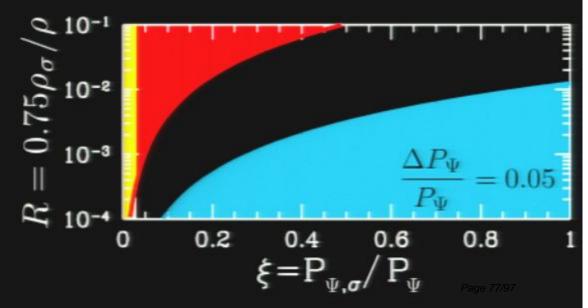
Pires: 0810003

The curvaton and inflaton both contribute to $P_{\Psi}(k)$:

$$\xi \equiv rac{P_{\Psi,\sigma}}{P_{\Psi}}$$
 fractional power from curvation $rac{\Phi}{T} = 2\xirac{\Deltaar{\sigma}}{T}$ power asymmetry

$$rac{\Delta P_{\Psi}}{P_{\Psi}} = 2\xi rac{ar{\Delta}ar{\sigma}}{ar{\sigma}}$$
 power asymmetry $rac{\Deltaar{\sigma}}{ar{\sigma}}\lesssim 1\Longrightarrow \xi\gtrsim rac{1}{2}rac{\Delta P_{\Psi}}{P_{\Psi}}$





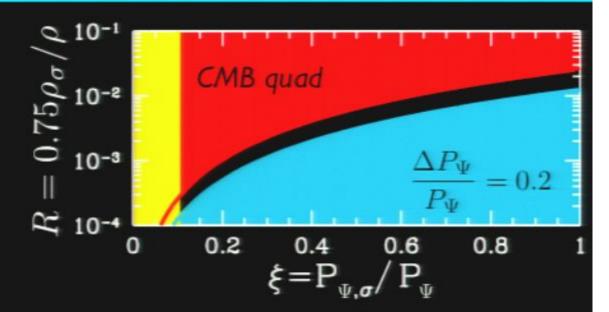
The curvaton and inflaton both contribute to $P_{\Psi}(k)$:

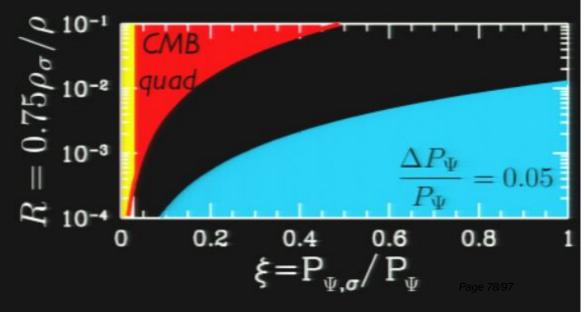
$$\xi\equivrac{P_{\Psi,\sigma}}{P_{\Psi}}$$
 fractional power from curvation $rac{\Delta P_{\Psi}}{P_{\Psi}}=2\xirac{\Deltaar{\sigma}}{ar{\sigma}}$ power asymmetry

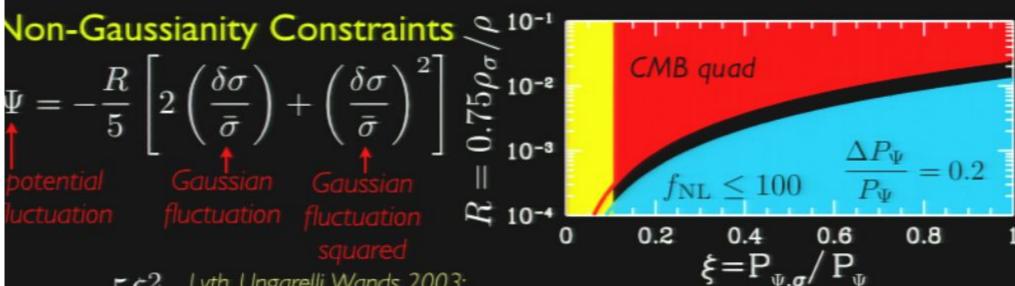
$$\frac{\Delta \bar{\sigma}}{\bar{\sigma}} \lesssim 1 \Longrightarrow \xi \gtrsim \frac{1}{2} \frac{\Delta P_{\Psi}}{P_{\Psi}}$$

CMB Quadrupole:

$$R\left(rac{\Deltaar{\sigma}}{ar{\sigma}}
ight)^2\lesssimrac{5}{2}(5.8\mathcal{Q})$$
 $R\lesssim58\mathcal{Q}\,\xi^2\left(rac{\Delta P_\Psi}{P_\Psi}
ight)^{-2}$





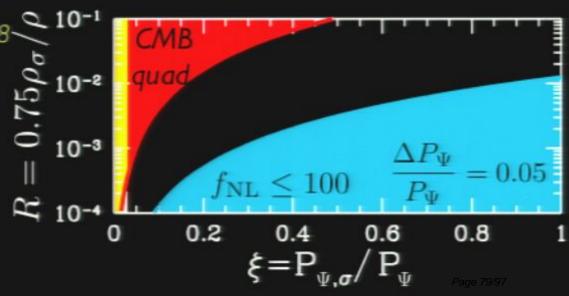


 $f_{
m NL} \simeq rac{5 \xi^2}{4 R}$ Lyth, Ungarelli, Wands 2003; Ichikawa, Suyama, Takahashi, Yamaguchi 2008 \sim 10-1

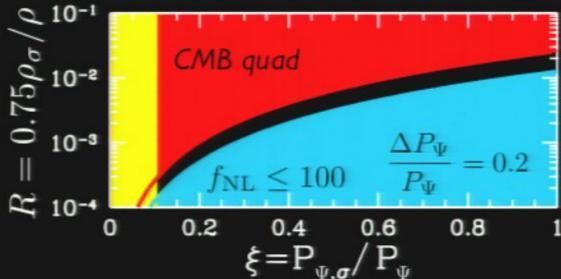
Jpperbound from WMAP:

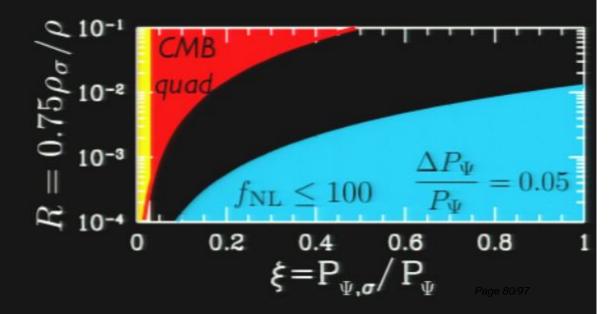
 $f_{\rm NL} \lesssim 100$

Komatsu et al. 2008 Yadav, Wandelt 2008



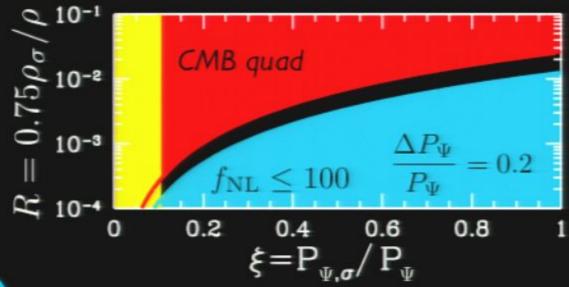
The Allowed Region





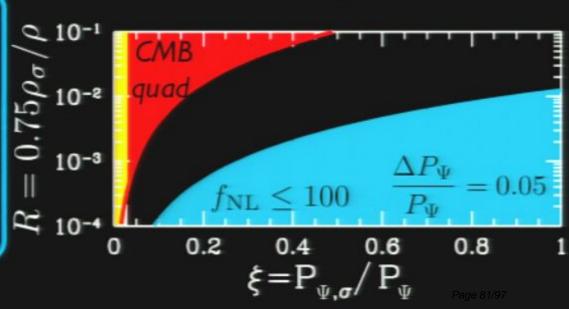
The Allowed Region

The Allowed Region
$$\frac{5}{4\,f_{\rm NL,max}} \lesssim \frac{R}{\xi^2} \lesssim \frac{58\,Q}{(\Delta P_\Psi/P_\Psi)^2} \stackrel{\text{C}}{\sim} 10^{-2} \\ \text{Ion-Gaussianity} \qquad \text{CMB Quadrupole} \qquad 10^{-3} \\ \text{Allowed window} \qquad \approx 10^{-4}$$

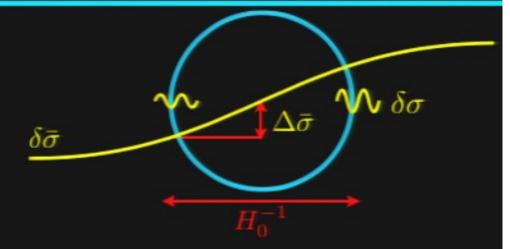


The Dealbreaker

The window for $\frac{\Delta P_{\Psi}}{P_{\Psi}}=0.2$ $\frac{10^{-2}}{10^{-2}}$ disappears if $f_{\rm NL,max}\lesssim 50$



Could the supermode be a quantum fluctuation?



Pirsa: 08100031 Page 82/97

 $\delta \bar{\sigma}$

Could the supermode be a quantum fluctuation?

Power spectrum from curvaton

$$P_{\Psi,\sigma} = \left(\frac{2R}{5}\right)^2 \left\langle \left(\frac{\delta\sigma}{\bar{\sigma}}\right)^2 \right\rangle = \xi P_{\Psi} \simeq 10^{-9} \xi \qquad \frac{H_0^{-1}}{\text{Observed power spectrum}}$$

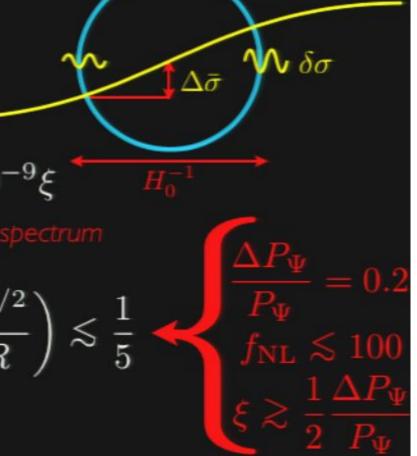
Pirsa: 08100031 Page 83/97

Could the supermode be a quantum fluctuation?

Power spectrum from curvator

$$P_{\Psi,\sigma} = \left(\frac{2R}{5}\right)^2 \left\langle \left(\frac{\delta\sigma}{\bar{\sigma}}\right)^2 \right\rangle = \xi P_{\Psi} \simeq 10^{-9} \xi$$
Observed power spectra

$$\frac{\bar{\sigma}}{\Delta \bar{\sigma}} \left(\frac{\delta \sigma}{\bar{\sigma}} \right)_{\rm rms} = \frac{2\xi}{\Delta P_{\Psi}/P_{\Psi}} \left(8 \times 10^{-5} \frac{\xi^{1/2}}{R} \right) \lesssim \frac{1}{5}$$



Pirsa: 08100031 Page 84/97

Could the supermode be a quantum fluctuation?

Power spectrum from curvaton

$$P_{\Psi,\sigma} = \left(\frac{2R}{5}\right)^2 \left\langle \left(\frac{\delta\sigma}{\bar{\sigma}}\right)^2 \right\rangle = \xi P_{\Psi} \simeq 10^{-9} \xi$$
Observed power spectrum

$$\frac{\bar{\sigma}}{\Delta \bar{\sigma}} \left(\frac{\delta \sigma}{\bar{\sigma}} \right)_{\rm rms} = \frac{2\xi}{\Delta P_{\Psi}/P_{\Psi}} \left(8 \times 10^{-5} \frac{\xi^{1/2}}{R} \right) \lesssim \frac{1}{5}$$

$$\bar{\sigma}_{\rm SM} > \Delta \bar{\sigma} > 5(\delta \sigma)_{\rm rms}$$

The supermode would be at least a 5-sigma fluctuation: that's highly improbable!

 $\frac{\Delta P_{\Psi}}{P_{\Psi}} = 0.2$ $f_{\rm NL} \lesssim 100$ $\xi \gtrsim \frac{1}{2} \frac{\Delta P_{\Psi}}{P_{\tau}}$

Could the supermode be a quantum fluctuation?

Power spectrum from curvator

$$P_{\Psi,\sigma} = \left(\frac{2R}{5}\right)^2 \left\langle \left(\frac{\delta\sigma}{\bar{\sigma}}\right)^2 \right\rangle = \xi P_{\Psi} \simeq 10^{-9} \xi \qquad \qquad H_0^{-1}$$
 Observed power

$$\frac{\bar{\sigma}}{\Delta \bar{\sigma}} \left(\frac{\delta \sigma}{\bar{\sigma}} \right)_{\rm rms} = \frac{2\xi}{\Delta P_{\Psi}/P_{\Psi}} \left(8 \times 10 \right)$$

$$\bar{\sigma}_{\rm SM} > \Delta \bar{\sigma} > 2$$

Signature of "curvaton web?"

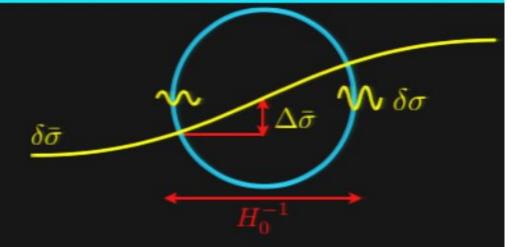
Linde and Mukhanov, 2006

$$\bar{\sigma}_{\rm SM} > \Delta \bar{\sigma} > Z_{(\sigma\sigma)_{\rm Inns}}$$

The supermode would be at least a 5-sigma fluctuation: that's highly improbable!

Page 86/97

Could the supermode be a quantum fluctuation?



Pirsa: 08100031 Page 87/97

Could the supermode be a quantum fluctuation?

Power spectrum from curvaton

$$P_{\Psi,\sigma} = \left(\frac{2R}{5}\right)^2 \left\langle \left(\frac{\delta\sigma}{\bar{\sigma}}\right)^2 \right\rangle = \xi P_{\Psi} \simeq 10^{-9} \xi$$

Observed power spectrum

$$\frac{\bar{\sigma}}{\Delta \bar{\sigma}} \left(\frac{\delta \sigma}{\bar{\sigma}} \right)_{\rm rms} = \frac{2\xi}{\Delta P_{\Psi}/P_{\Psi}} \left(8 \times 10^{-5} \frac{\xi^{1/2}}{R} \right) \lesssim \frac{1}{5}$$

$$\bar{\sigma}_{\rm SM} > \Delta \bar{\sigma} > 5(\delta \sigma)_{\rm rms}$$

The supermode would be at least a 5-sigma fluctuation: that's highly improbable!

 $\frac{\Delta P_{\Psi}}{P_{\Psi}} = 0.2$ $f_{\rm NL} \lesssim 100$ $\xi \gtrsim \frac{1}{2} \frac{\Delta P_{\Psi}}{2}$

Page 88/97

Could the supermode be a quantum fluctuation?

Power spectrum from curvator

$$P_{\Psi,\sigma} = \left(\frac{2R}{5}\right)^2 \left\langle \left(\frac{\delta\sigma}{\bar{\sigma}}\right)^2 \right\rangle = \xi P_{\Psi} \simeq 10^{-9} \xi \qquad \frac{H_0^{-1}}{}$$
 Observed power

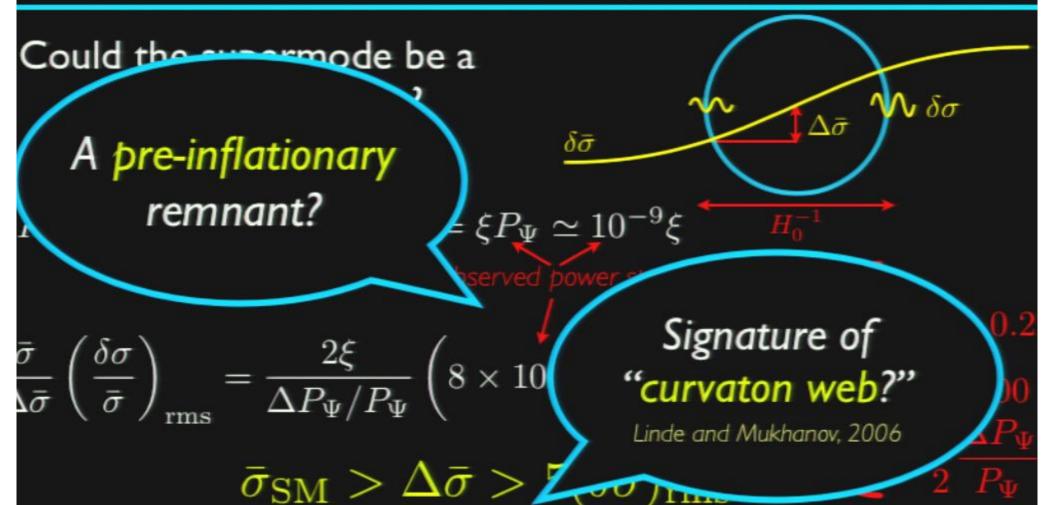
$$rac{ar{\sigma}}{\Delta ar{\sigma}} \left(rac{\delta \sigma}{ar{\sigma}}
ight)_{
m rms} = rac{2 \xi}{\Delta P_\Psi / P_\Psi} \left(8 imes 10
ight)_{
m Linde \ and } ar{\sigma}_{
m SM} > \Delta ar{\sigma} > 0$$

Signature of "curvaton web?"

Linde and Mukhanov, 2006

The supermode would be at least a 5-sigma fluctuation: that's highly improbable!

Pa



The supermode would be at least a 5-sigma fluctuation: that's highly improbable!

There are indications that only large scales are asymmetric.

Donoghue and

Donoghue 2005;

Lew 2008.

- Asymmetry detected for $\ell = 5 40$.
- Some analyses see reduced asymmetry for $\ell \gtrsim 100$. How could the asymmetry disappear at small scales?

Only the perturbations from the curvaton are asymmetric; the inflaton perturbations are still statistically isotropic.

Introduce scale dependence through
$$\xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$$
 .

Pirsa: 08100031

There are indications that only large scales are asymmetric.

- Asymmetry detected for $\ell=5-40$.
- Some analyses see reduced asymmetry for $\ell \gtrsim 100$. How could the asymmetry disappear at small scales?

Donoghue and Donoghue 2005; Lew 2008.

Only the perturbations from the curvaton are asymmetric; the inflaton perturbations are still statistically isotropic.

Introduce scale dependence through $\xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$.

lacktriangle A feature in $V(\phi)$ Gordon 2007

There are indications that only large scales are asymmetric.

- Asymmetry detected for $\ell = 5 40$.
- Some analyses see reduced asymmetry for $\ell \gtrsim 100$. How could the asymmetry disappear at small scales?

Donoghue and Donoghue 2005; Lew 2008.

Only the perturbations from the curvaton are asymmetric; the inflaton perturbations are still statistically isotropic.

Introduce scale dependence through $\xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$.

lacksquare A feature in $V(\phi)$ Gordon 2007

$$\xi = \frac{\tilde{\epsilon}}{\tilde{\epsilon} + 1} - \tilde{\epsilon} \equiv \frac{1}{9\pi} \left(\frac{m_{\rm Pl}}{\bar{\sigma}}\right)^2 R^2 \epsilon$$

Pirea: 08100031

There are indications that only large scales are asymmetric.

- Asymmetry detected for $\ell = 5 40$.
- Some analyses see reduced asymmetry for $\ell \gtrsim 100$. How could the asymmetry disappear at small scales?

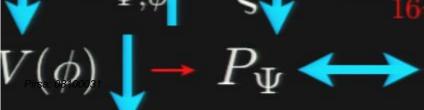
Donoghue and Donoghue 2005; Lew 2008.

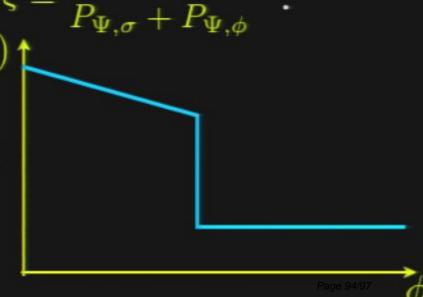
Only the perturbations from the curvaton are asymmetric; the inflaton perturbations are still statistically isotropic.

Introduce scale dependence through $\xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$

A feature in
$$V(\phi)$$
 Gordon 2007 $V(\phi)$ $\xi = \frac{\tilde{\epsilon}}{\tilde{\epsilon} + 1}$ $\tilde{\epsilon} \equiv \frac{1}{9\pi} \left(\frac{m_{\rm Pl}}{\bar{\sigma}}\right)^2 R^2 \epsilon$







There are indications that only large scales are asymmetric.

- Asymmetry detected for $\ell = 5 40$.
- Some analyses see reduced asymmetry for $\ell \gtrsim 100$.

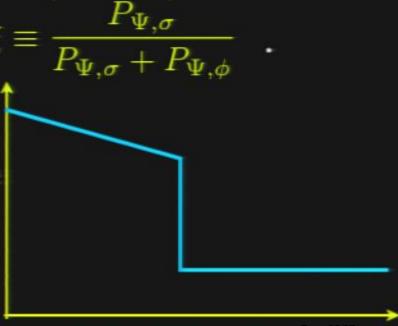
How could the asymmetry disappear at small scales?

Only the perturbations from the curvaton are asymmetric; the inflaton perturbations are still statistically isotropic.

Introduce scale dependence through $\xi \equiv \frac{P_{\Psi,\sigma}}{P_{\Psi,\sigma} + P_{\Psi,\phi}}$

- lacksquare A feature in $V(\phi)$ Gordon 2007 $V(\phi)$
- Isocurvature modes from curvaton?
 - curvaton can produce isocurvature perturbations
 - isocurvature perturbations contribute more on large scales

1810031 rk in progress....



Donoghue and

Donoghue 2005;

Lew 2008.

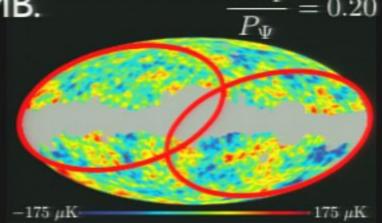
lummary: How to Generate the Power Asymmetry

There is a power asymmetry in the CMB.

present at the 99% confidence level

detected on large scales

Hansen, Banday, Gorski, 2004 Eriksen, Hansen, Banday, Gorski, Lilje 2004 Eriksen, Banday, Gorski, Hansen, Lilje 2007



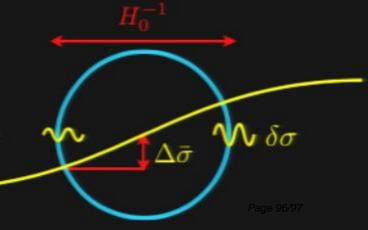
A superhorizon perturbation during inflation generates a power asymmetry.

- also generates large-scale CMB temperature perturbations
- no dipole; quadrupole and octupole set limits.

Erickcek, Carroll, Kamionkowski arXiv:0808.1570

- an inflaton perturbation is ruled out
- lacktriangle a curvaton perturbation is a viable source of the observed asymmetry $\delta \bar{\sigma}$

Erickcek, Kamionkowski, Carroll arXiv:0806.0377



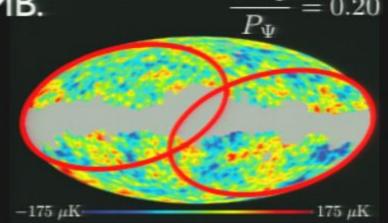
lummary: How to Generate the Power Asymmetry

There is a power asymmetry in the CMB.

present at the 99% confidence level

detected on large scales

Hansen, Banday, Gorski, 2004 Eriksen, Hansen, Banday, Gorski, Lilje 2004 Eriksen, Banday, Gorski, Hansen, Lilje 2007



Features of the Curvaton-Generated Power Asymmetry

- the superhorizon curvaton perturbation is not a quantum fluctuation
- the produced asymmetry is scale-invariant, but it is possible to modify that
- suppressed tensor-scalar ratio: $r \propto (1 \xi)$
- high non-Gaussianity: $f_{\rm NL} \gtrsim 50$

