Title: Physics Wiki (IT tools for Science)

Date: Sep 09, 2008 06:20 PM

URL: http://pirsa.org/08090057

Abstract: A wiki is an excellent tool for organizing and representing human knowledge. By building a personal wiki notebook, a scientific researcher may optimally organize past and current research notes. In this brief practical introduction I will provide a guided tour of an open scientific notebook -- physicswiki.org -- and discuss the design considerations, features, and content of this open source wiki.

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- natural concept organization
 - many interlinked concepts
 - ideal for research notes (rapid edittttting)
- educational tool
 - deep definitions
- open source science
 - or private notebook
 - collaboration

Advantages of a Wiki

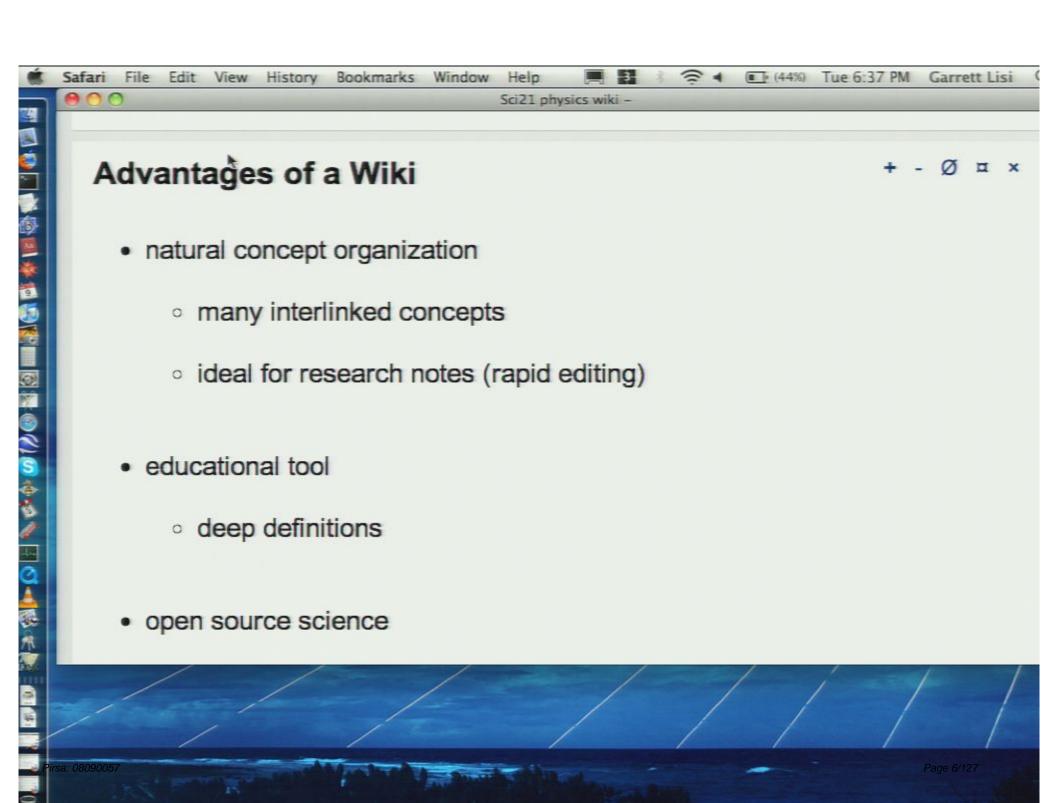
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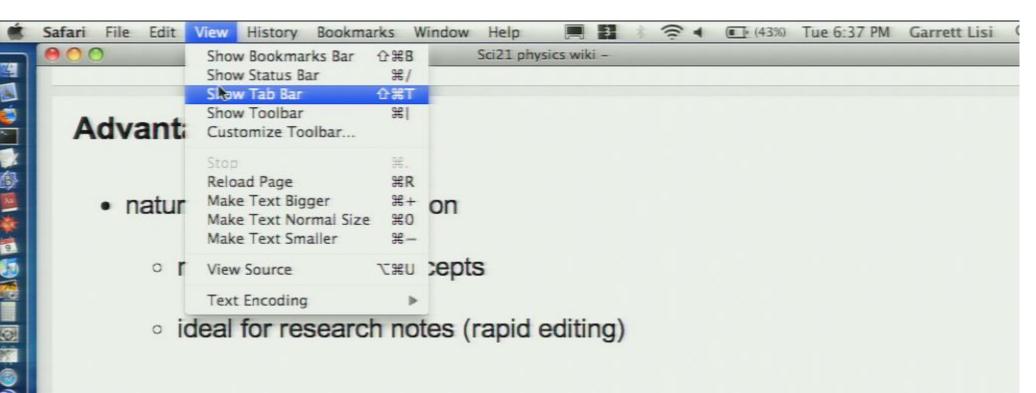
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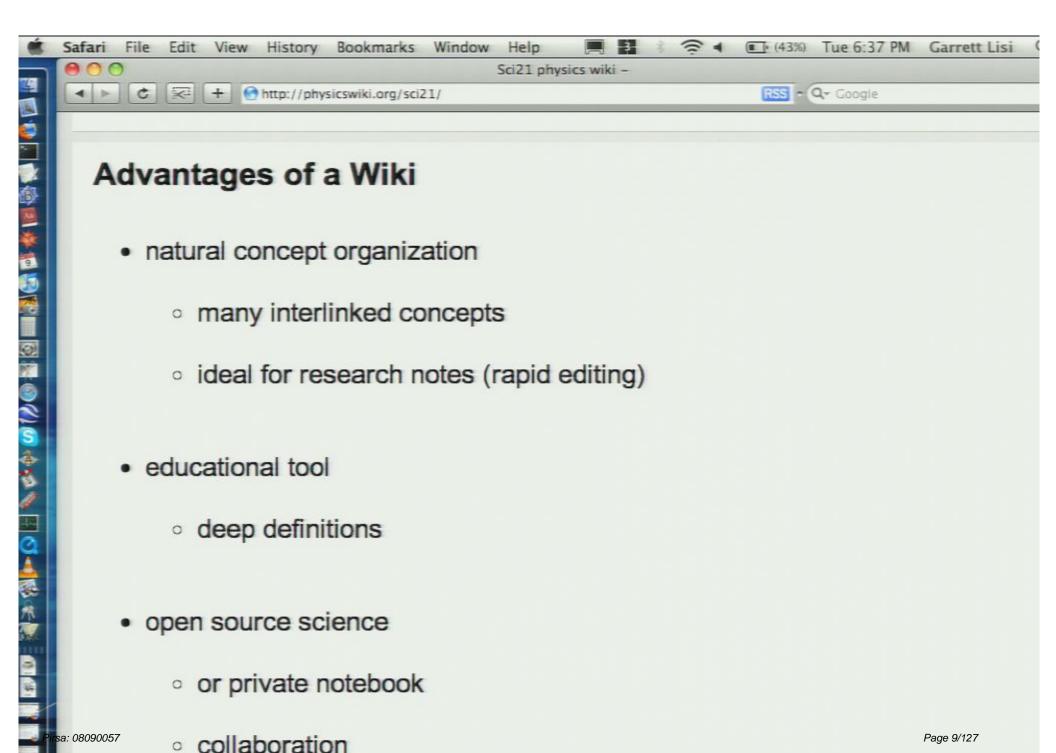
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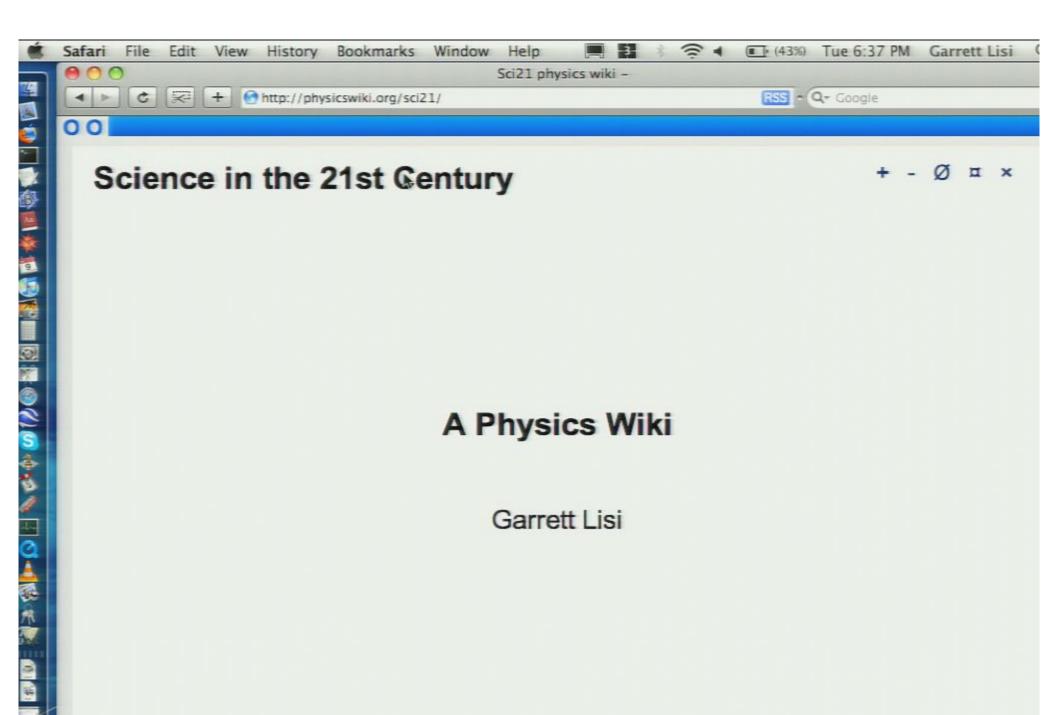
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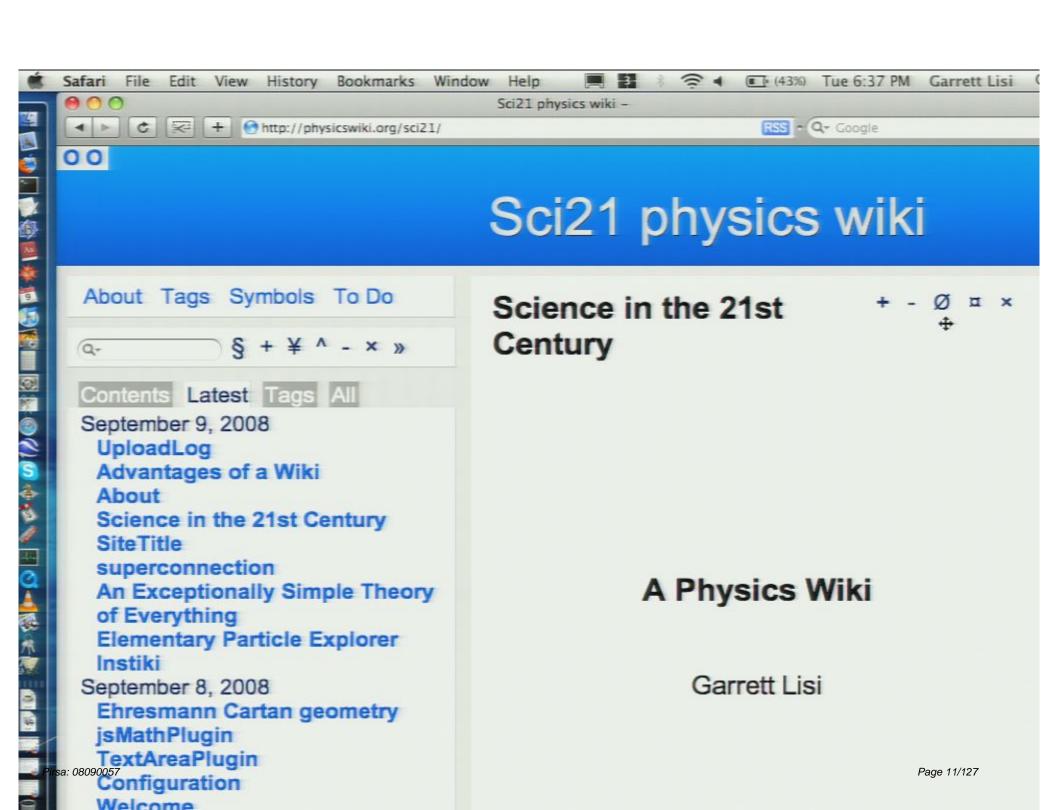
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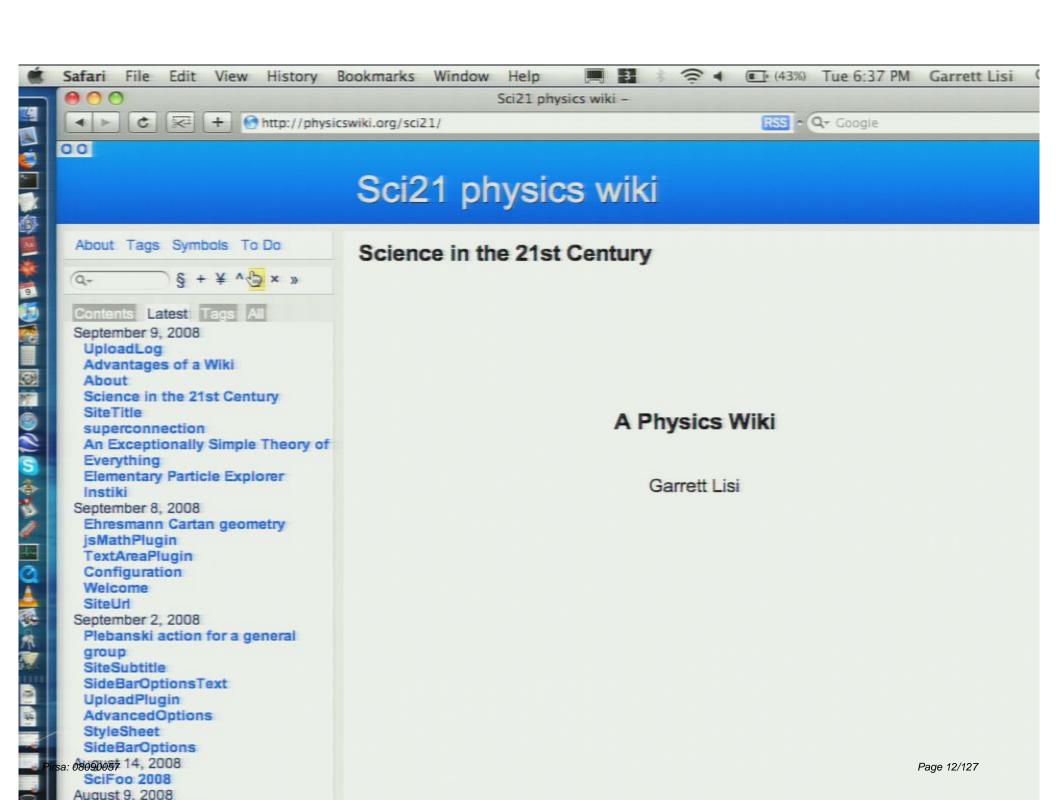


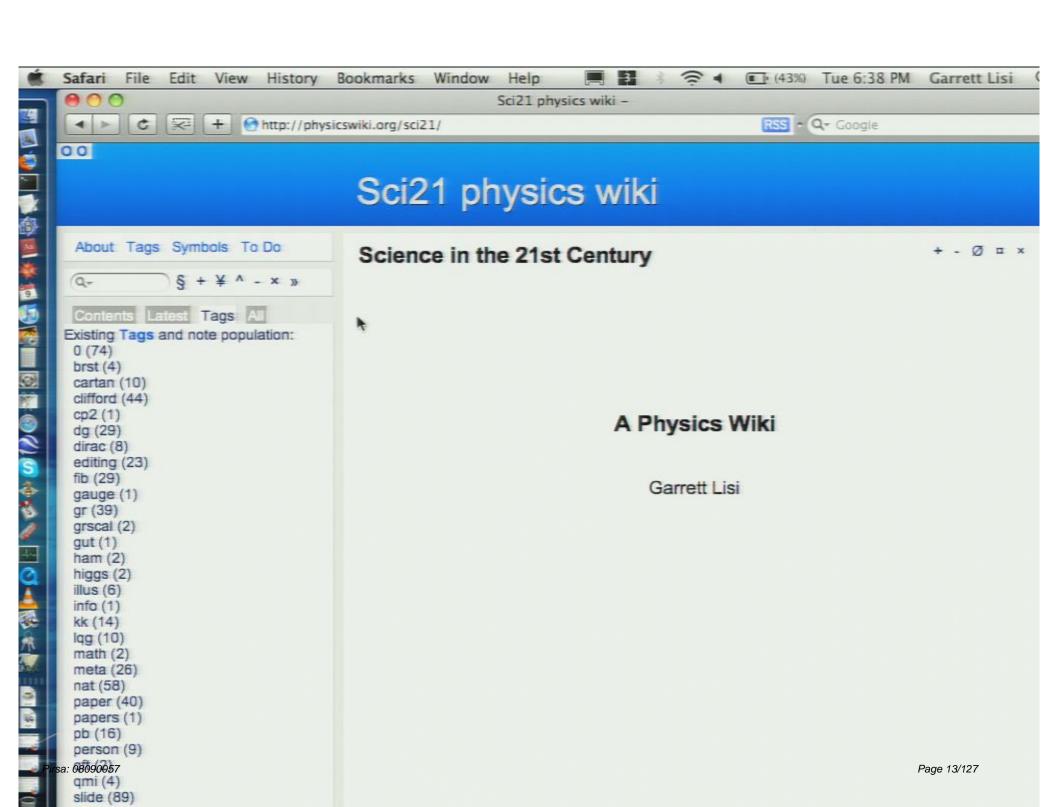


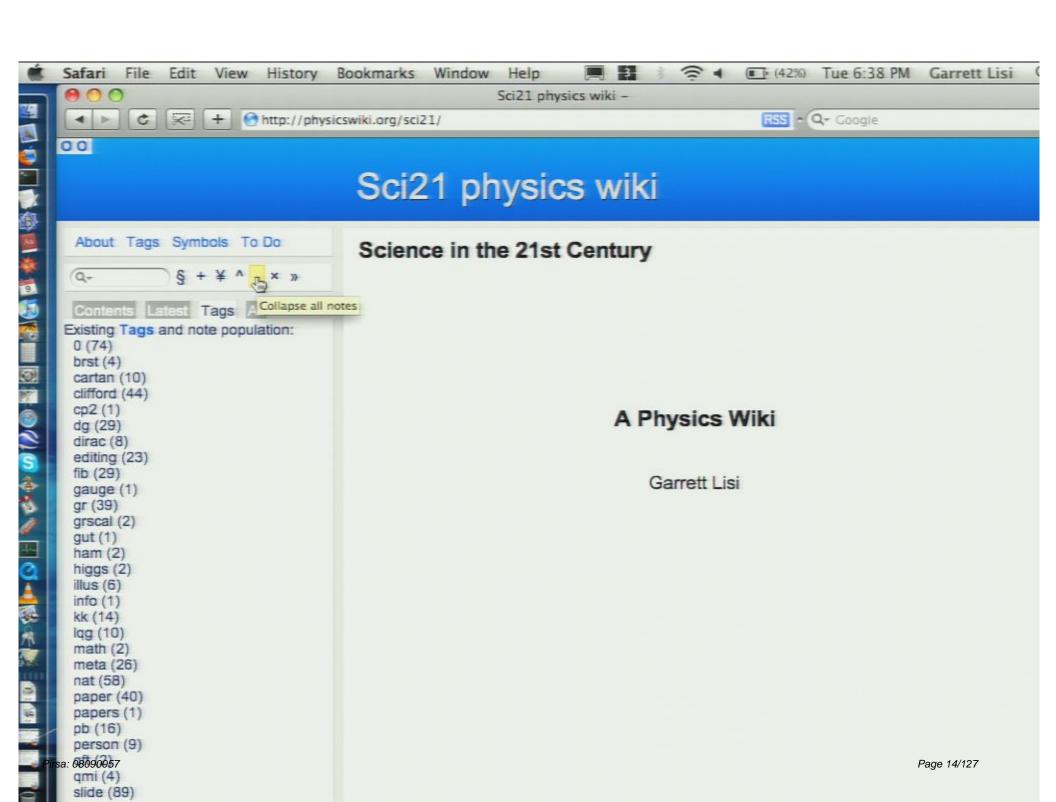
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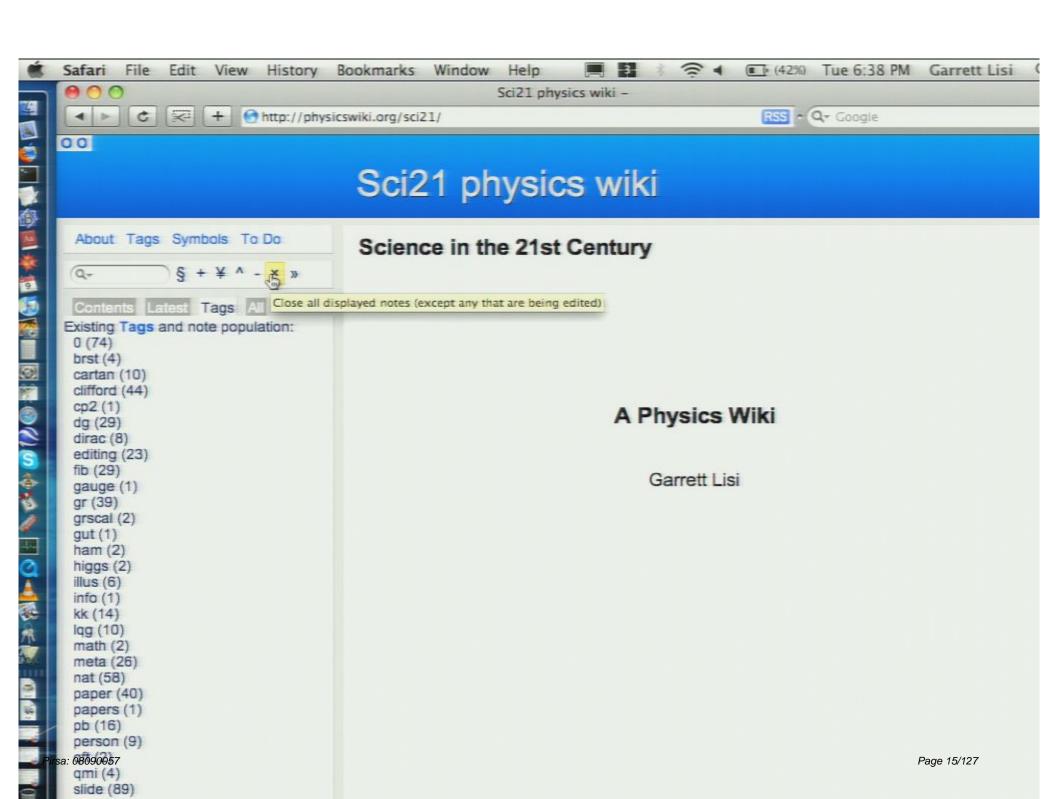
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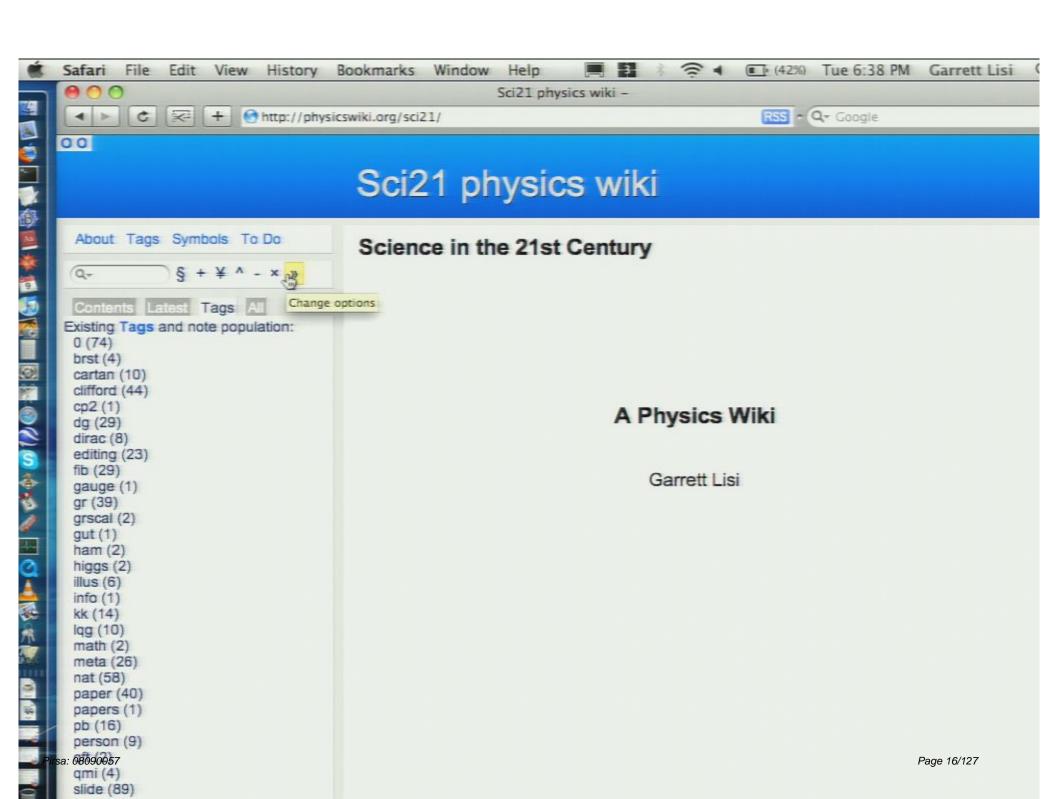


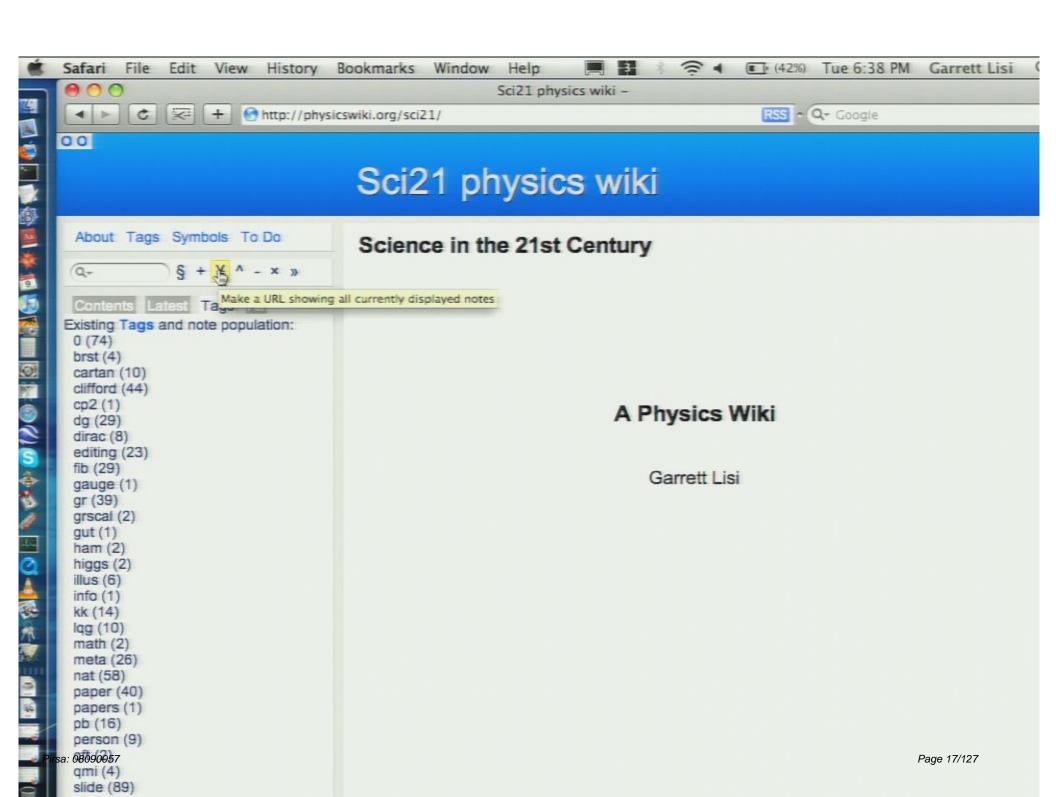


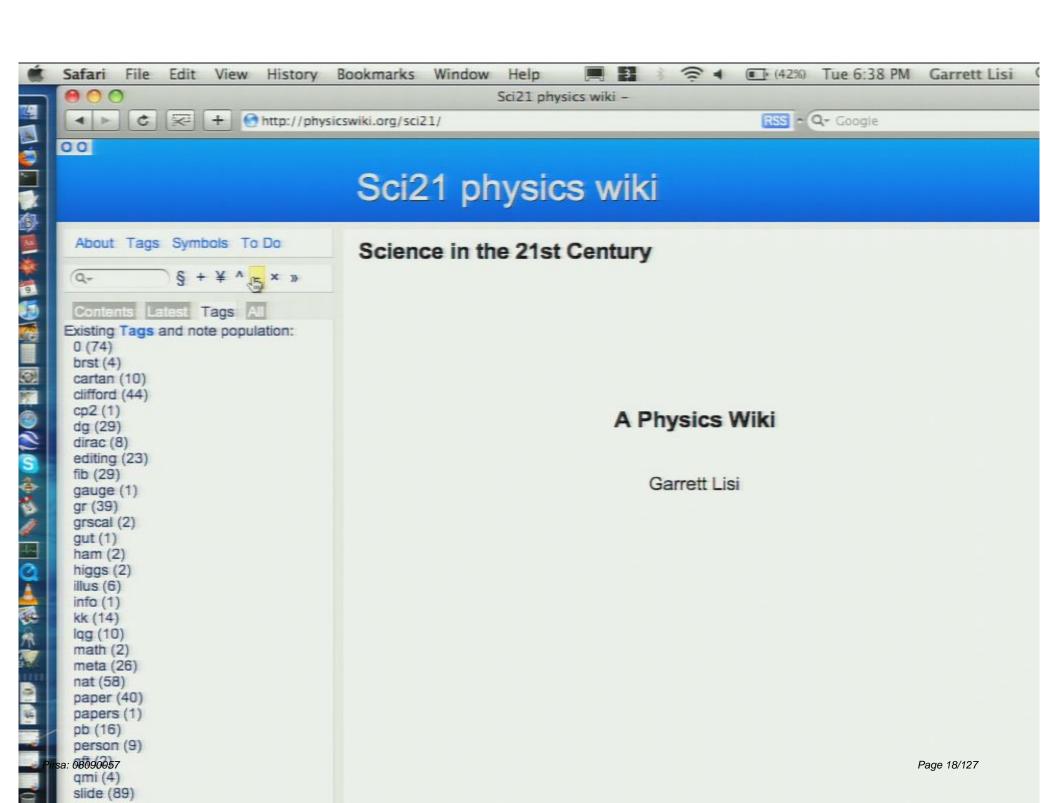


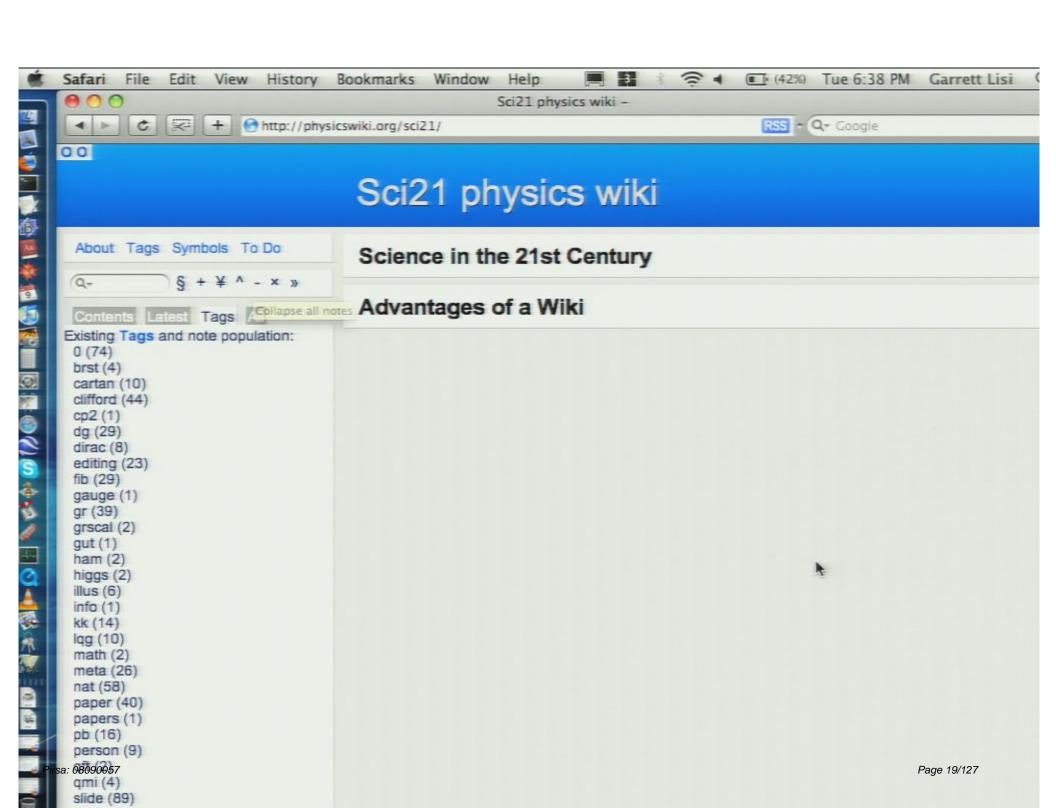


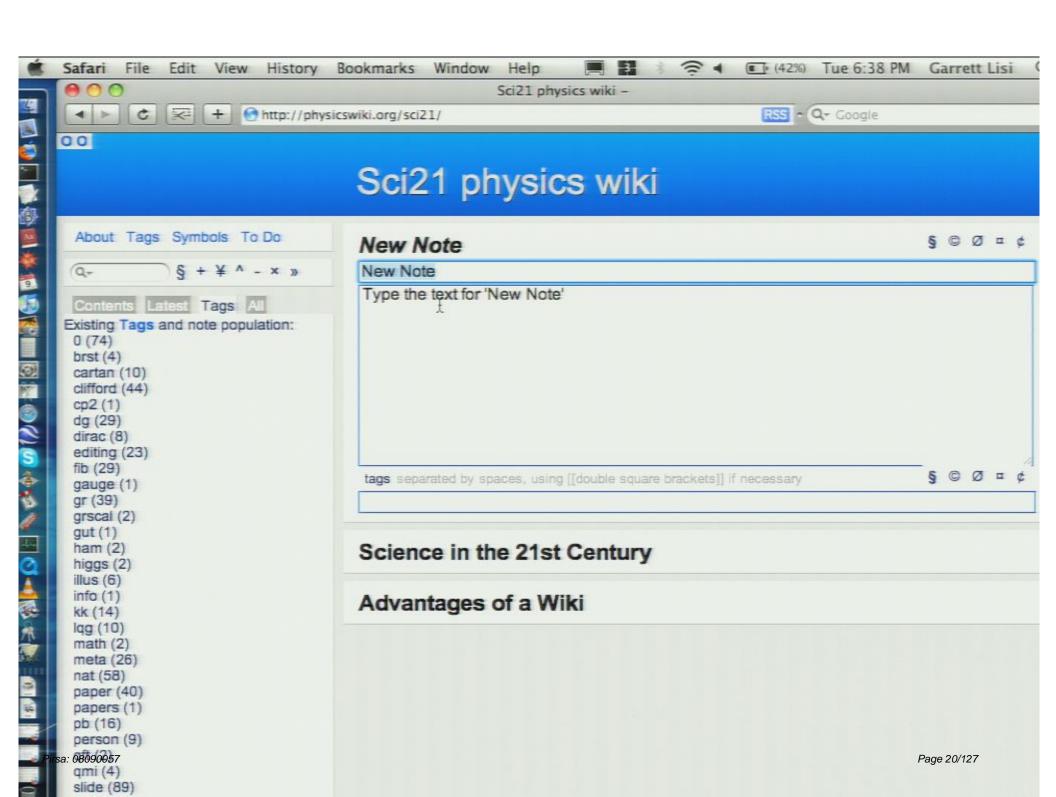


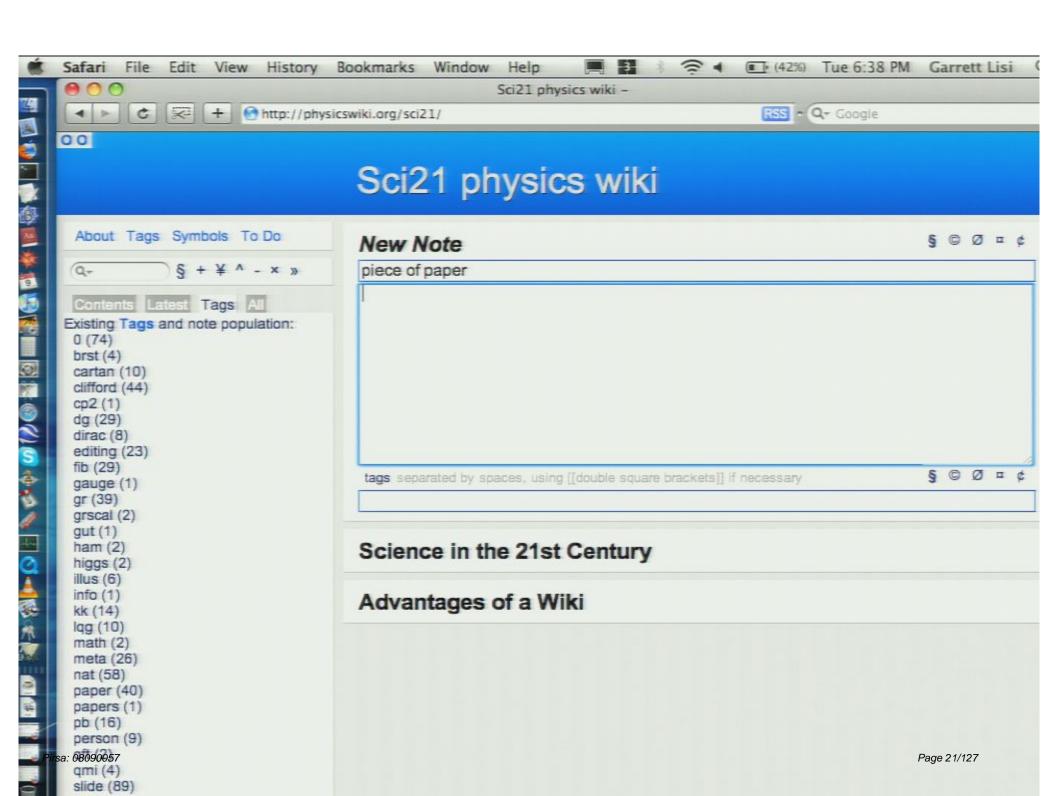


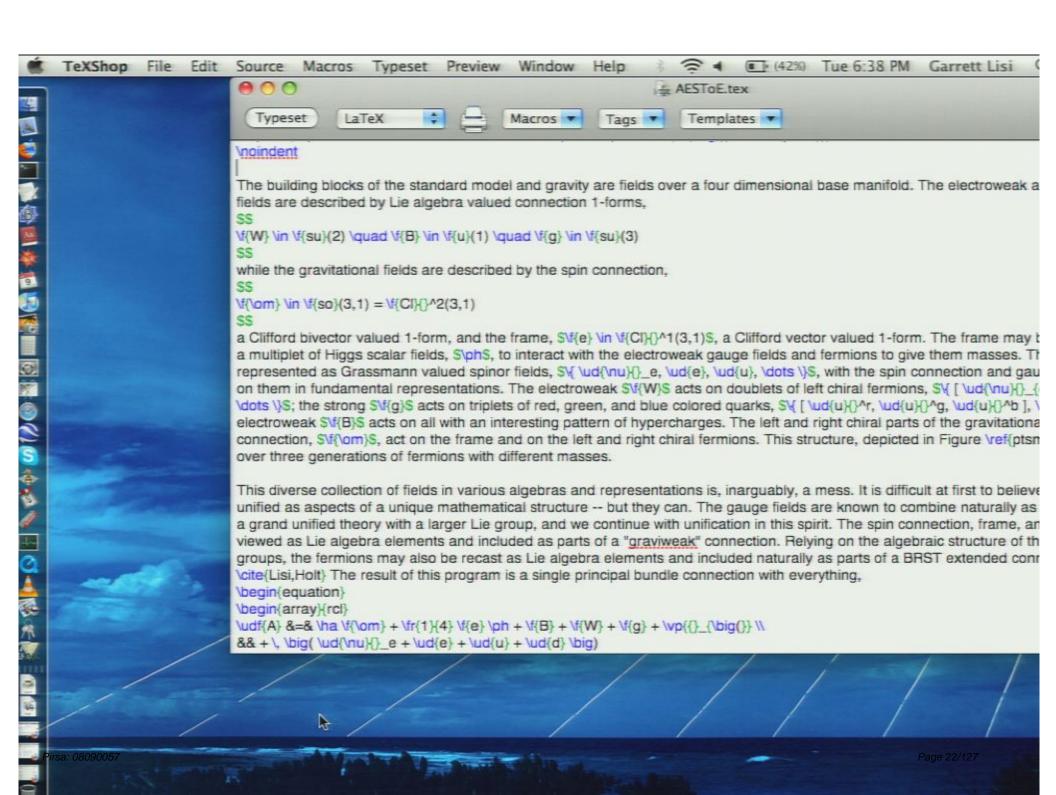


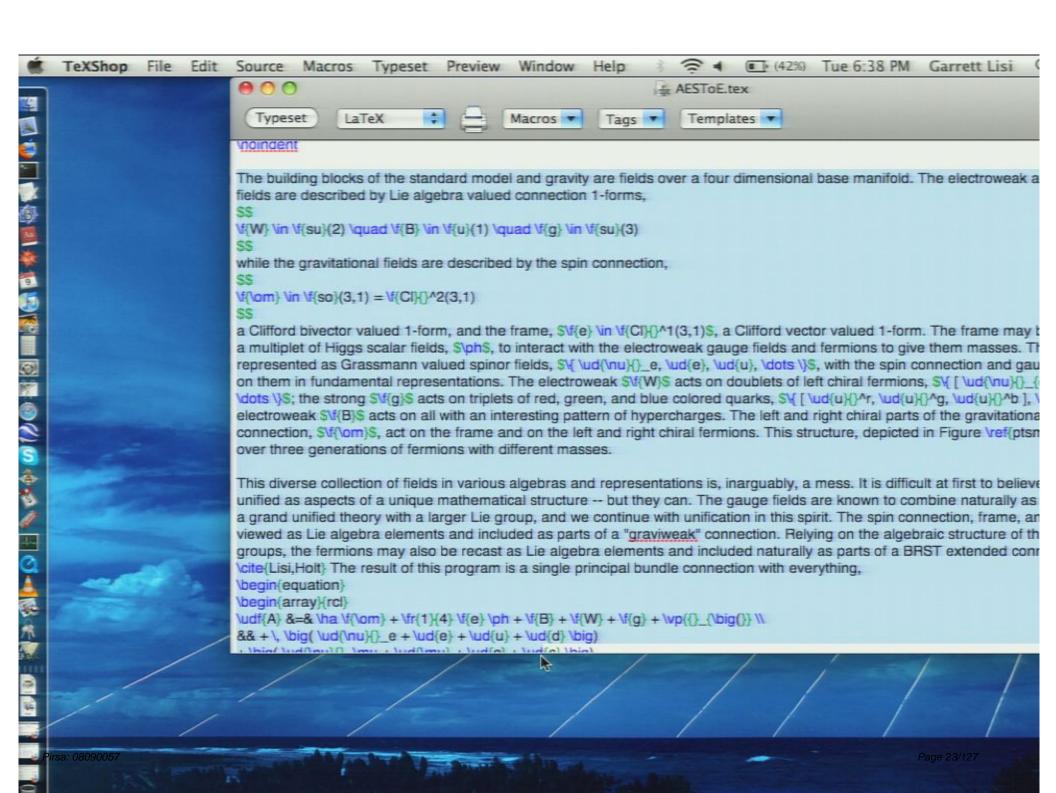


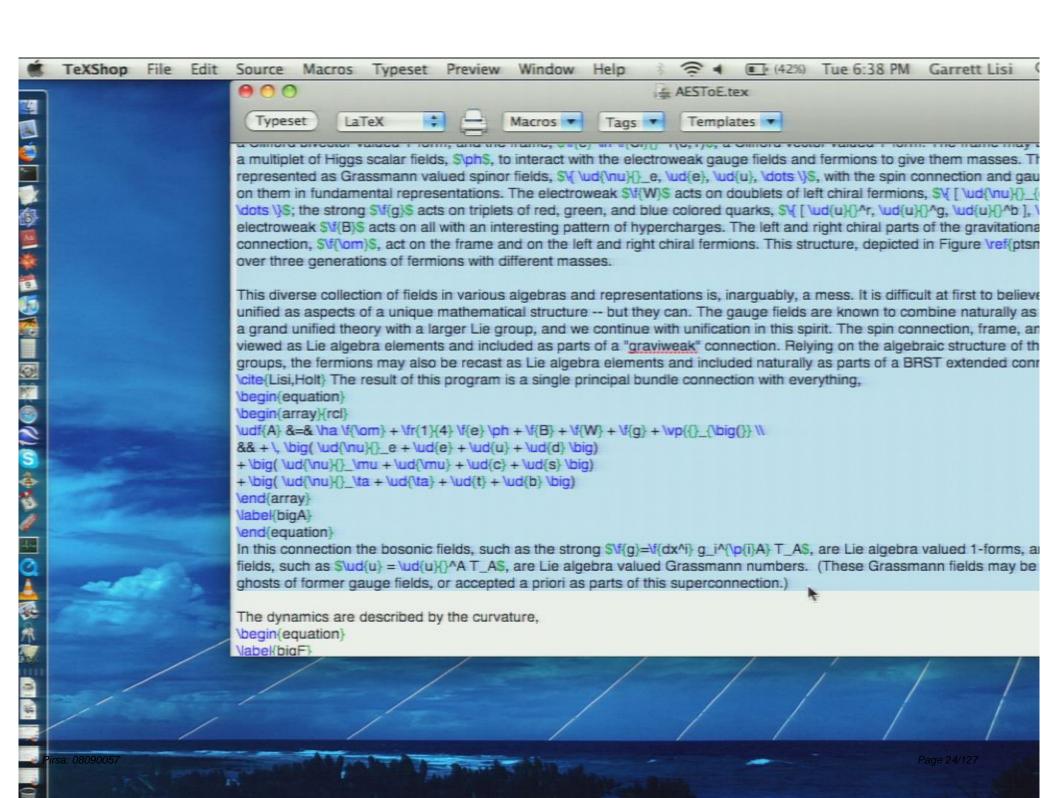


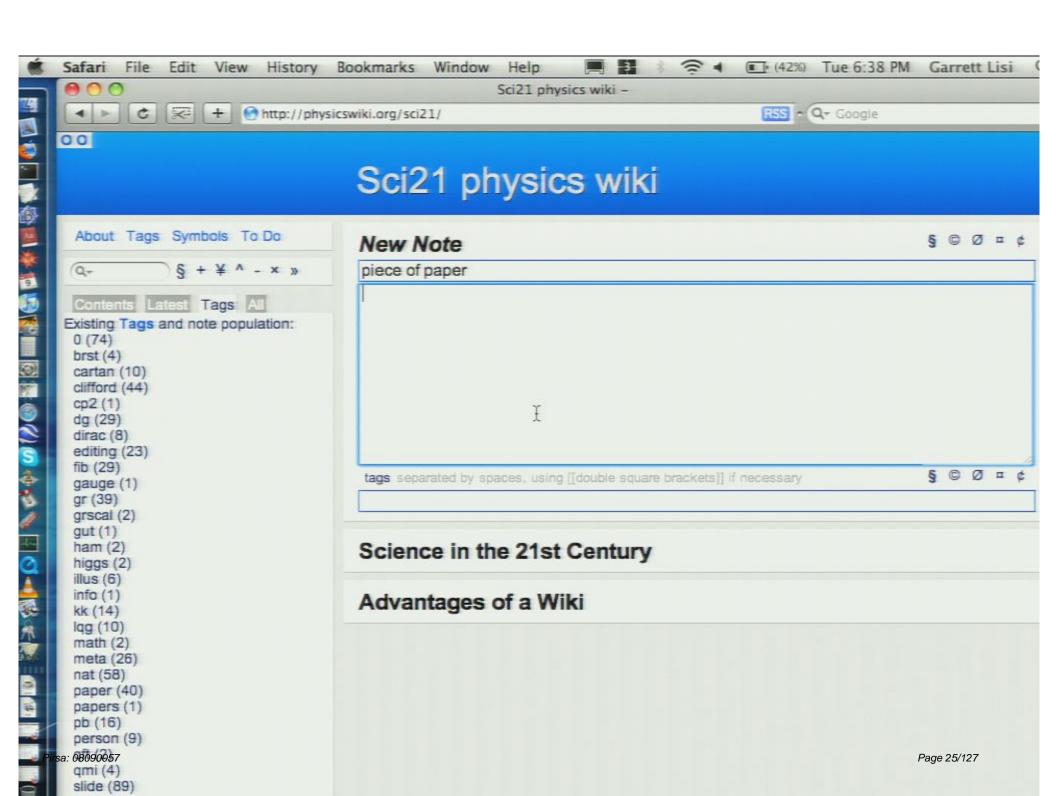


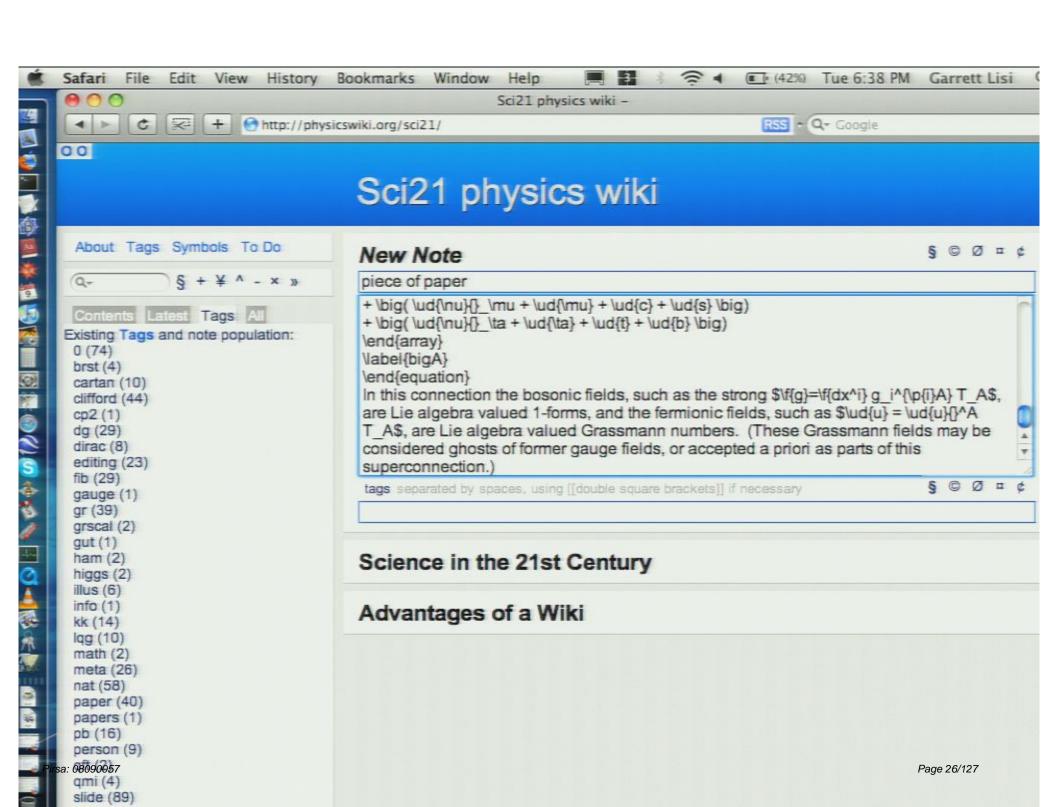


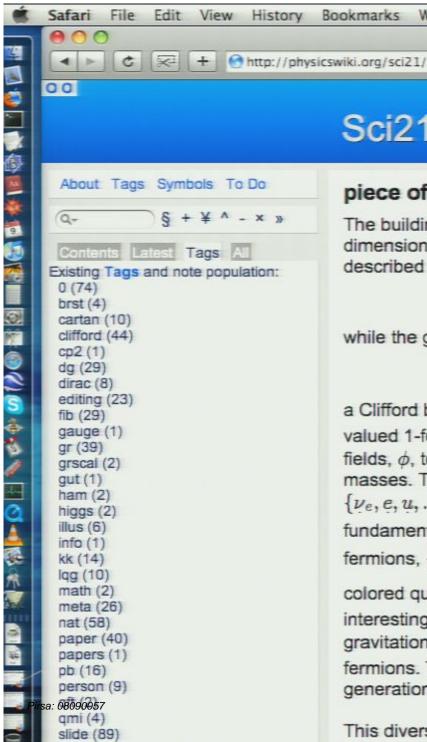












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Window

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$$\underline{W} \in s\underline{u}(2) \quad \underline{B} \in \underline{u}(1) \quad \underline{g} \in s\underline{u}(3)$$

while the gravitational fields are described by the spin connection,

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a Clifford bivector valued 1-form, and the frame, $e \in Cl^1(3,1)$, a Clifford vector valued 1-form. The frame may be combined with a multiplet of Higgs scalar fields, ϕ , to interact with the electroweak gauge fields and fermions to give them masses. The fermions are represented as Grassmann valued spinor fields, $\{\nu_e, e, u, \ldots\}$, with the spin connection and gauge fields acting on them in fundamental representations. The electroweak W acts on doublets of left chiral fermions, $\{[\nu_{eL}, e_L], \ldots\}$; the strong g acts on triplets of red, green, and blue colored quarks, $\{[u^r, u^g, u^b], \ldots\}$; and the electroweak \underline{B} acts on all with an interesting pattern of hypercharges. The left and right chiral parts of the gravitational spin connection, ω , act on the frame and on the left and right chiral fermions. This structure, depicted in Figure ref{ptsm}, is repeated over three generations of fermions with different masses.

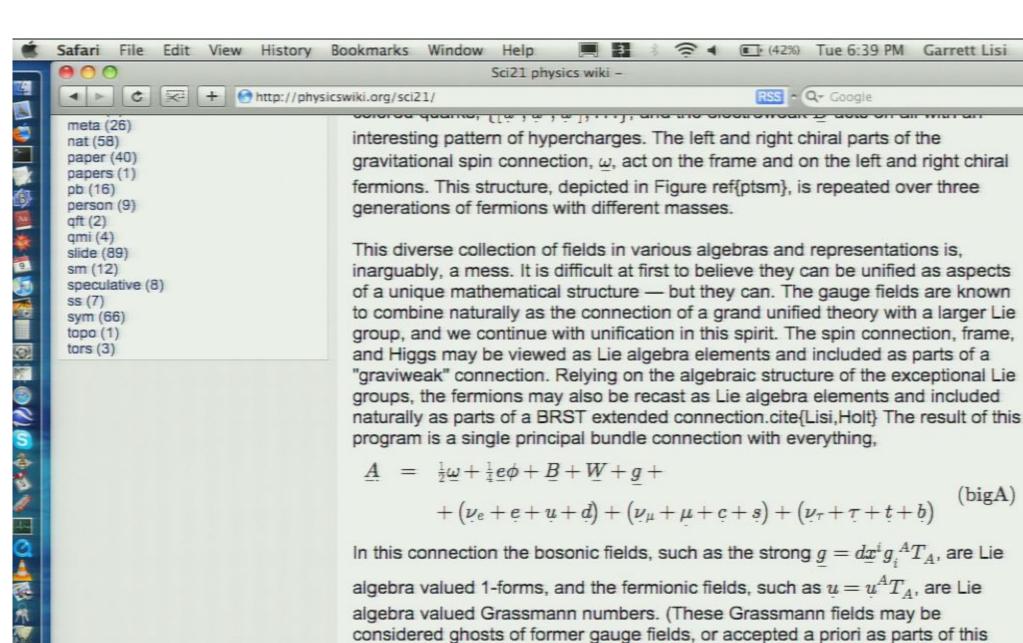
Page 27/127 This diverse collection of fields in various algebras and representations is,

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Garrett Lisi

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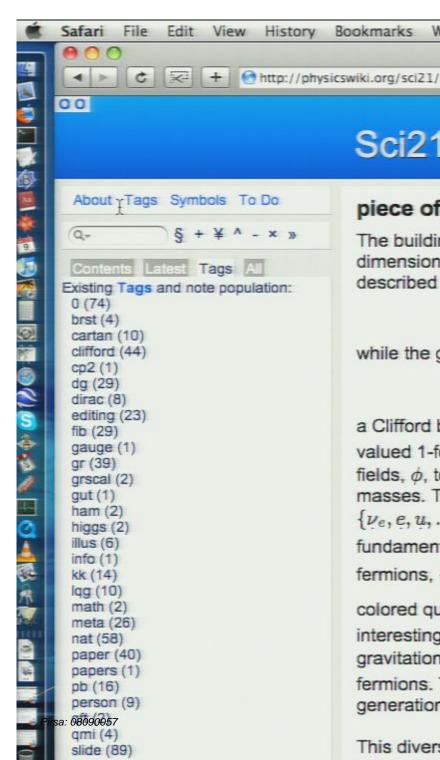


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Garrett Lisi



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Garrett Lisi

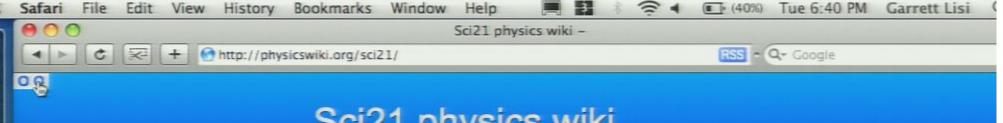
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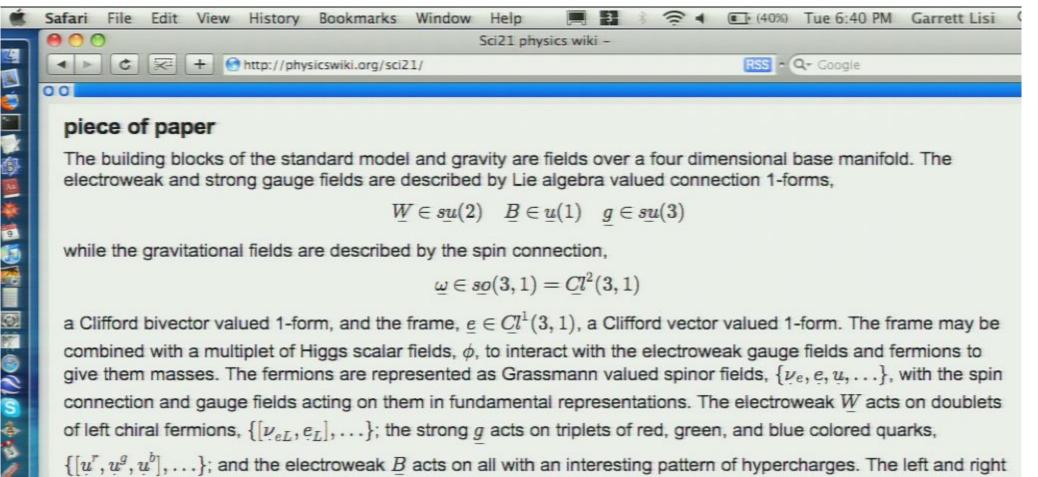
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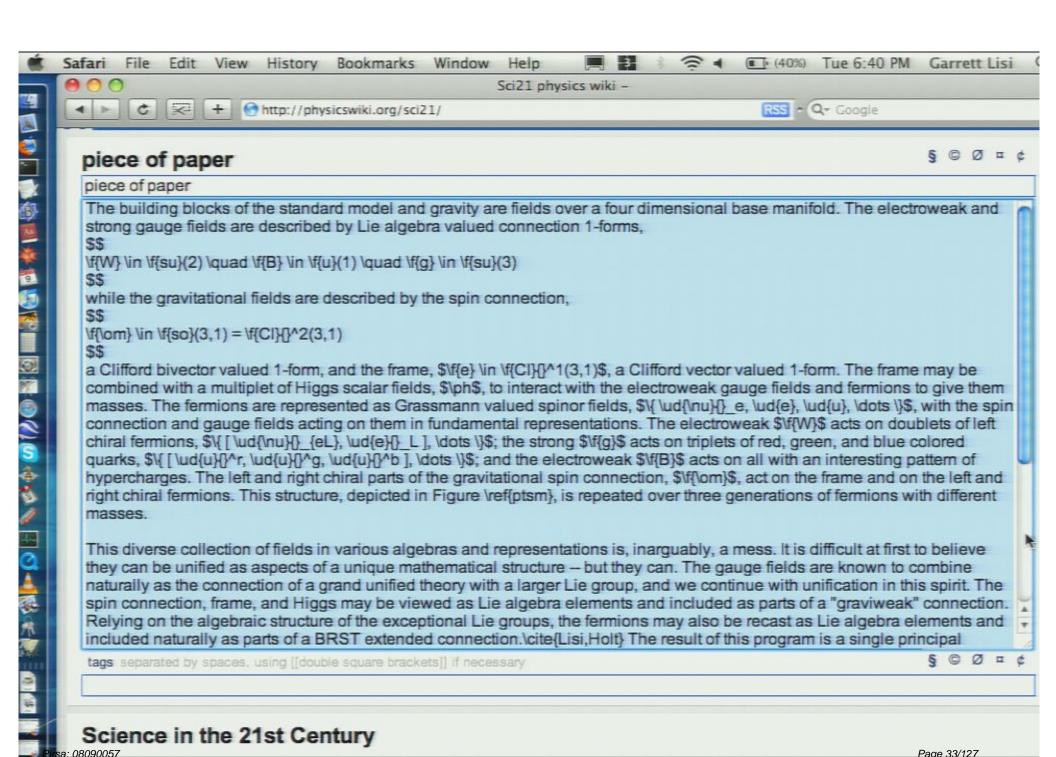
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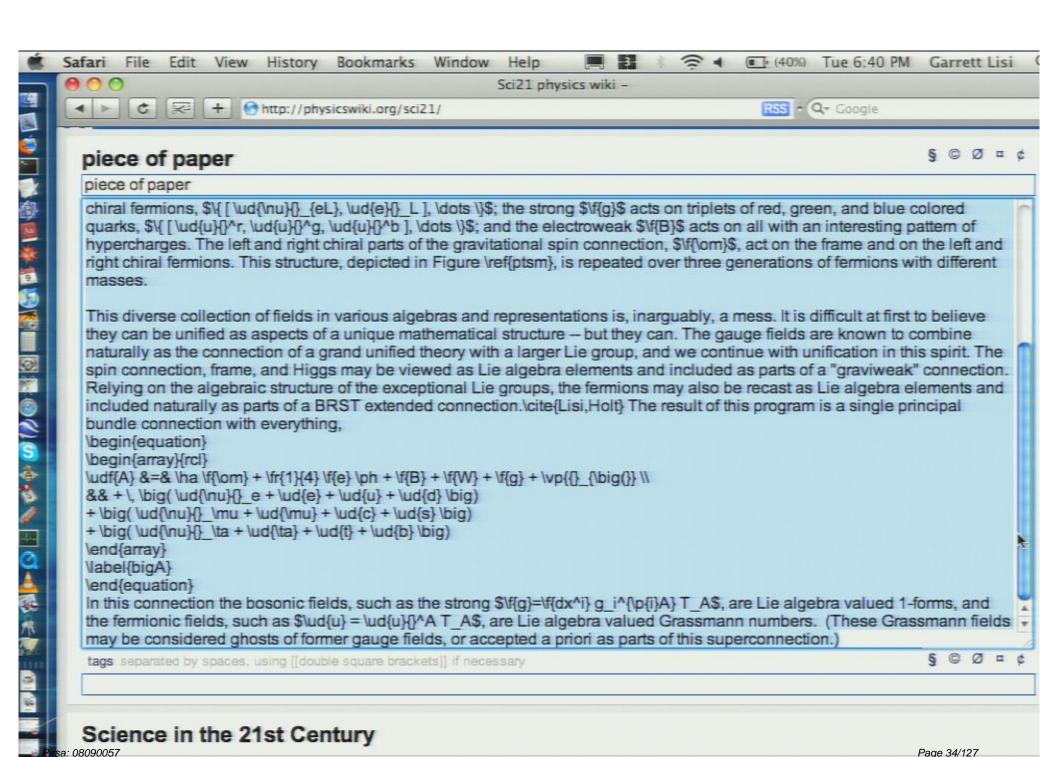
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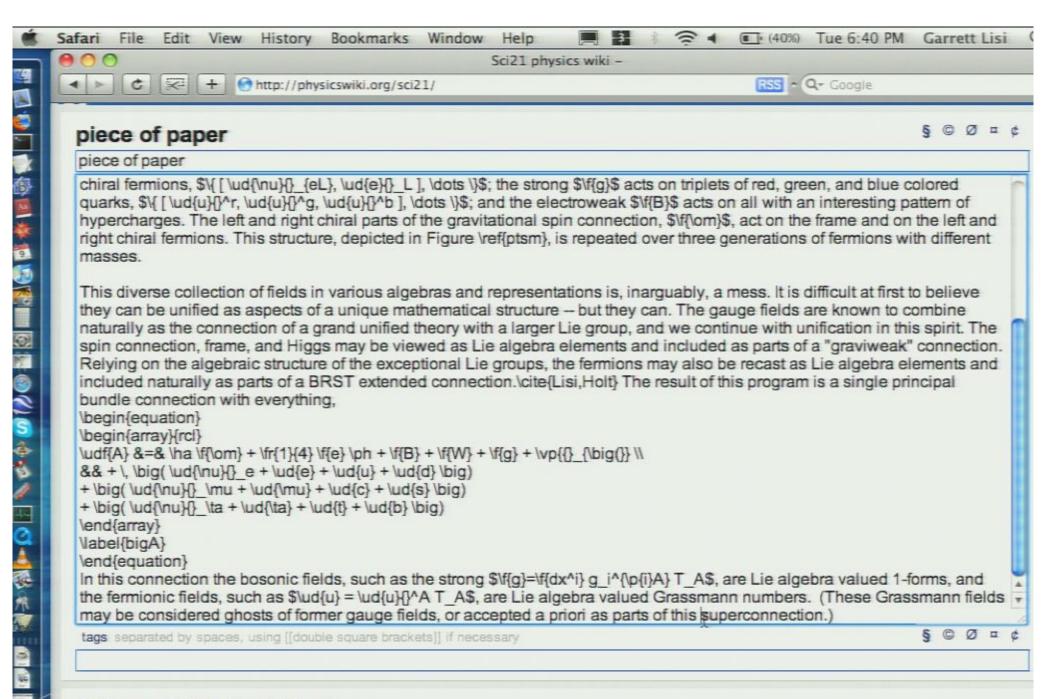
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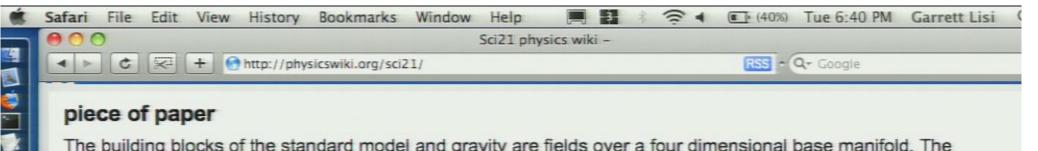
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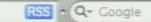
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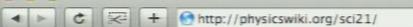
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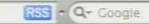
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$$\underline{A} = \frac{1}{2}\underline{\omega} + \frac{1}{4}\underline{e}\phi + \underline{B} + \underline{W} + \underline{g} + \\ + (\nu_e + e + u + d) + (\nu_\mu + \mu + c + s) + (\nu_\tau + \tau + t + b)$$
 (bigA)

In this connection the bosonic fields, such as the strong $g=d\underline{x}^ig_{_i}{}^AT_A$, are Lie algebra valued 1-forms, and the fermionic fields, such as $u = u^A T_A$, are Lie algebra valued Grassmann numbers. (These Grassmann fields may be considered ghosts of former gauge fields, or accepted a priori as parts of this superconnection.)

superconnection

A superconnection,

$$A = A + A$$

is the sum of a Lie algebra valued connection 1-form field, $A=dx^iA_i^BT_B$, and a Lie algebra valued Grassmann number field, $A = A^BT_B$. This construct arises naturally in the BRST technique, in which it is called a BRST extended connection.

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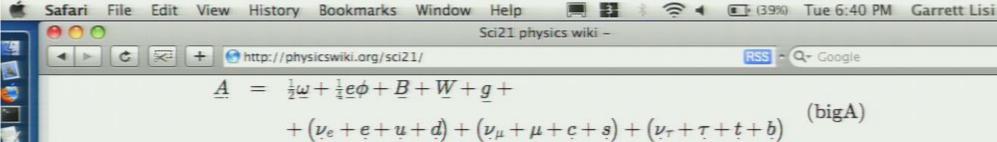
- Shlomo Sternberg
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sa: 08090057G. Catren and J. Devoto

Extended Connection in Yang-Mills Theory

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brst



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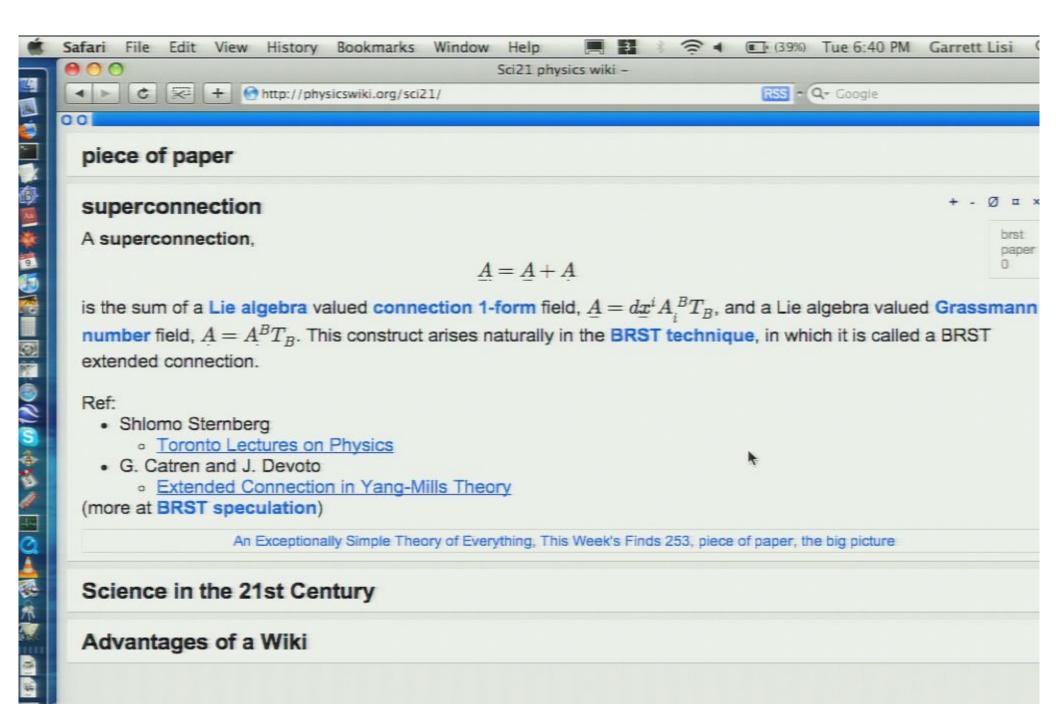
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(more at BRST speculation)

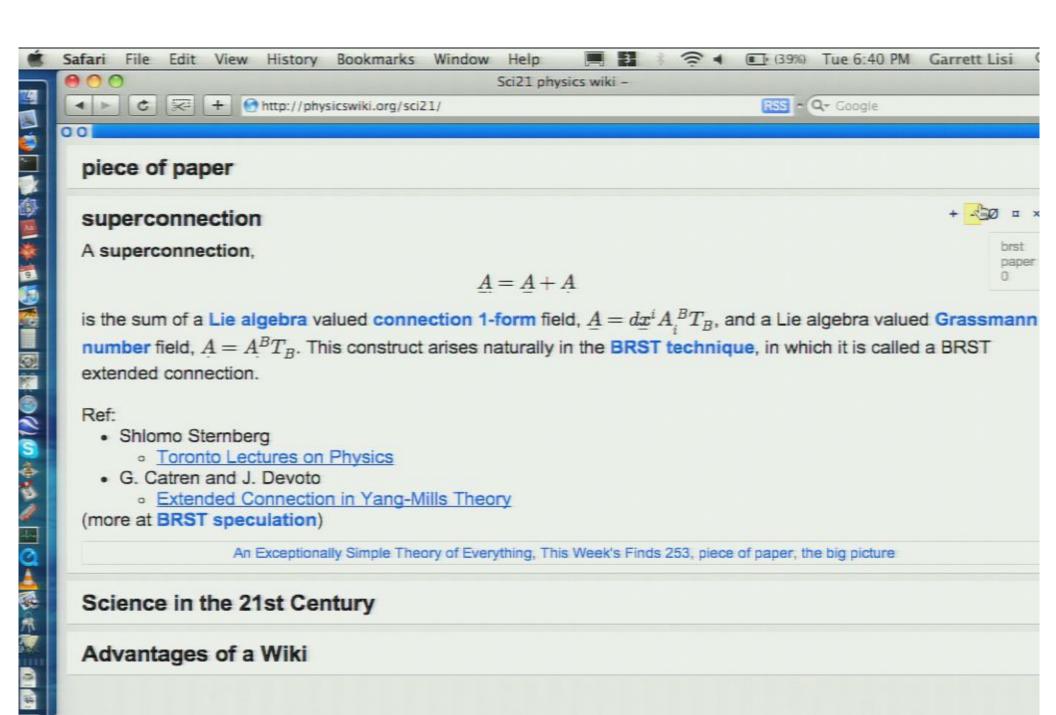
An Exceptionally Simple Theory of Everything, This Week's Finds 253, piece of paper, the big picture

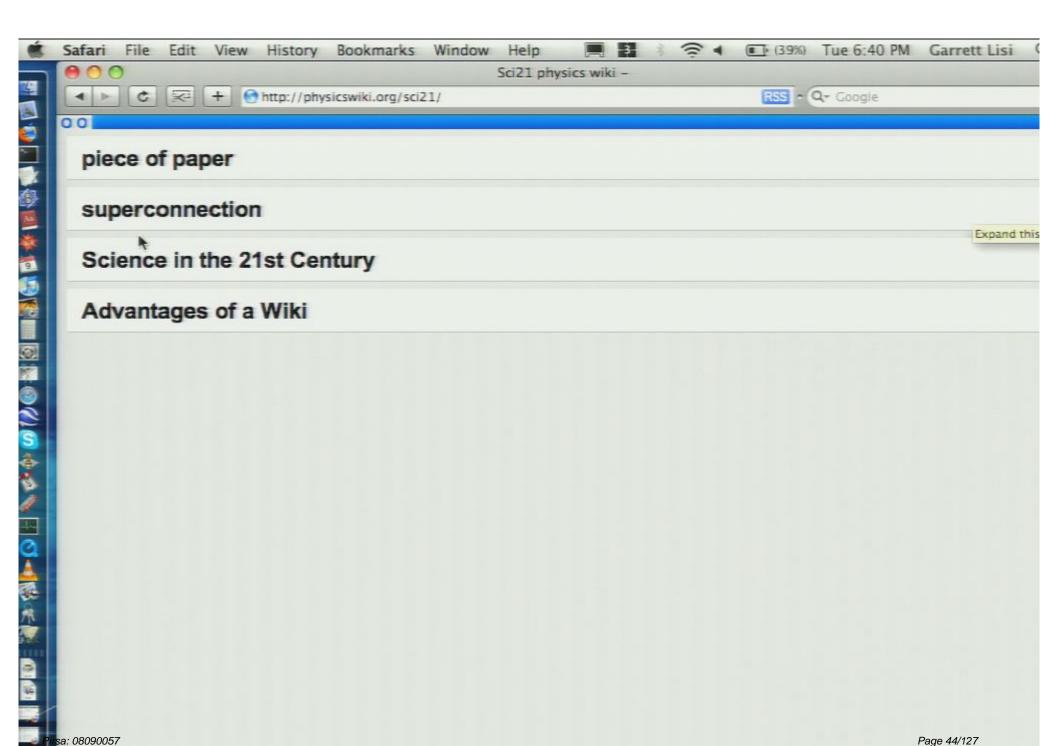
Science in the 21st Century

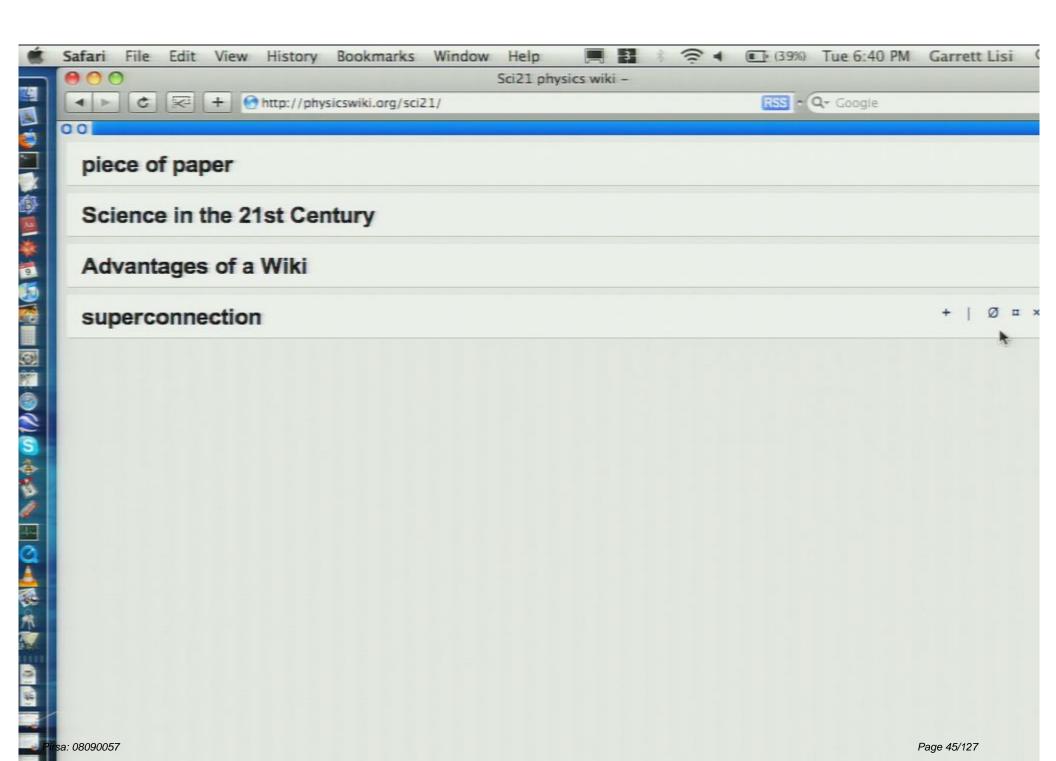
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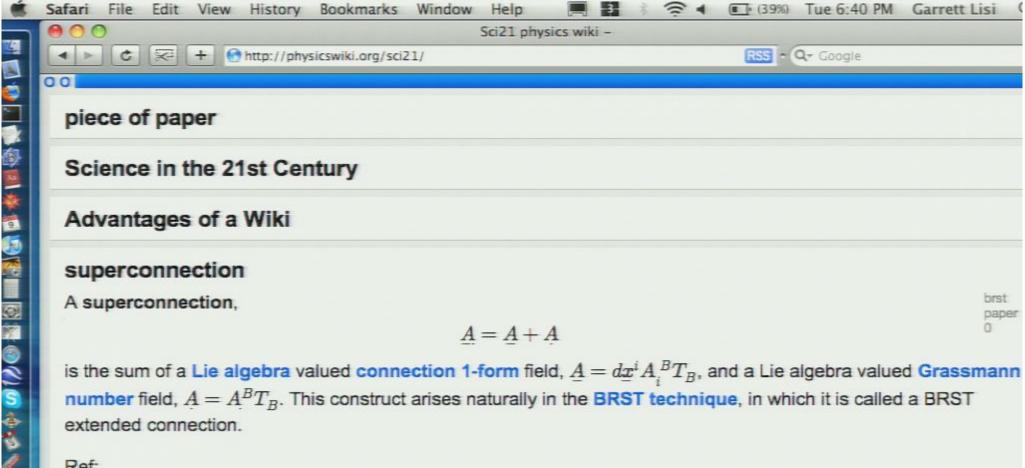


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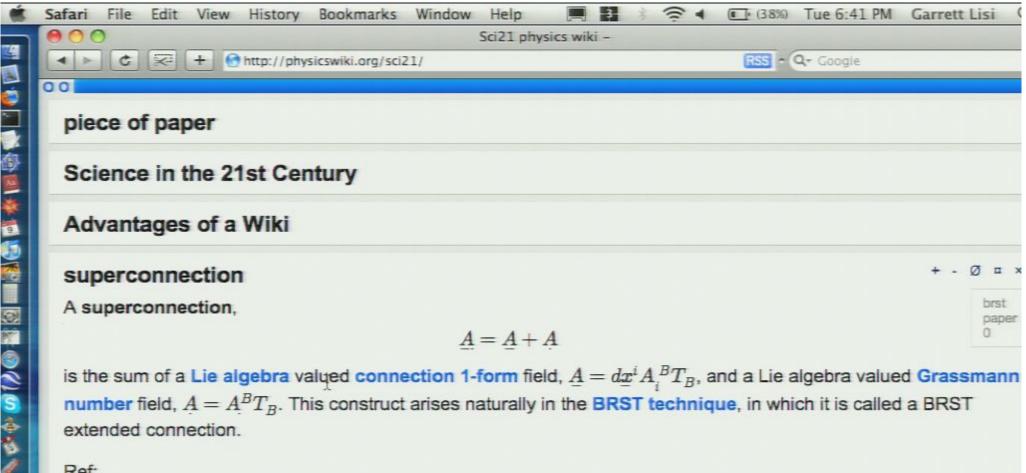
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(more at BRST speculation)

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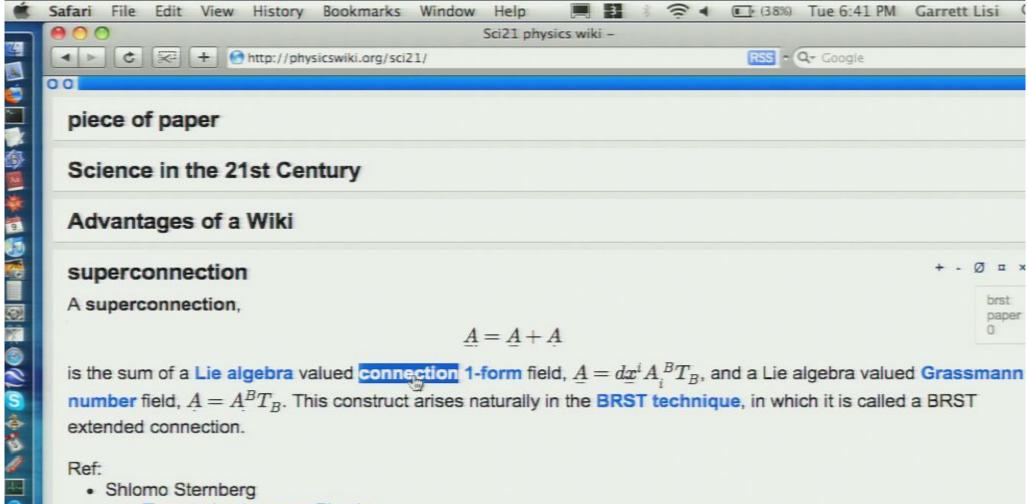
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connection

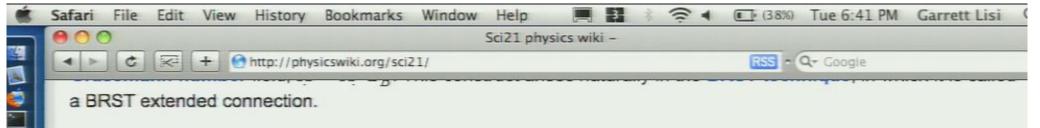
A **connection** completely encodes the local geometry of a **fiber bundle**. Specifically, it describes how the local trivializations change as one moves around on the base manifold. The group of these changes is the same as the structure group, G, of the fiber bundle. From any point, the infinitesimal change of a local trivialization when moving in any direction is described by the operation of a **Lie algebra** element. These changes may be described via a **Lie algebra** valued **1-form** over the base, the connection,

$$\underline{A} = d\underline{x}^i A_i^{\ B}(x) T_B$$

with the appropriate action on the fiber elements. Using this connection, the **covariant derivative** of a section, $\sigma(x)$, (valued in the fiber) is

$$ar{
abla}\sigma=ar{d}\sigma+ar{A}\sigma=dar{x}^i\left(\partial_i\sigma+A_i^{\ B}T_B\sigma
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sa: 08090067hich the Lie algebra basis elements, T_B , act on the fiber. The connection changes under a gauge age 49/127 transformation so as to keep this derivative covariant.



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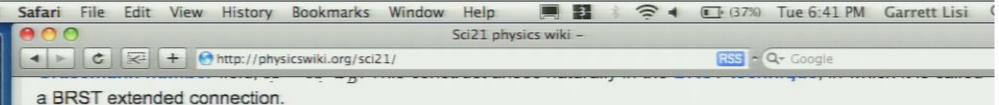
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An Exceptionally Simple Theory of Everything, BRST speculation, Chern-Simons form, Discussion, Ehresmann connection, Ehresmann principal bundle connection, Geometry of Yang-Mills theory, Plan of attack (old), Symbols, This Week's Finds 253, Unification (old), as: 08090057 utomorphism bundle, covariant derivative, curvature, fiber bundle, gauge transformation, holonomy, parallel transport, pare 50/127 my, principal bundle, superconnection, talk for FQXi 07, talk for Loops 07, talk for UCD 08, tangent bundle parallel transport, vector bundle connection, vector bundle parallel transport



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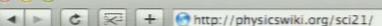
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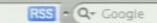
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An Exceptionally Simple Theory of Everything, BRST speculation, Chern-Simons form, Discussion, Ehresmann connection, Ehresmann principal bundle connection, Geometry of Yang-Mills theory, Plan of attack (old), Symbols, This Week's Finds 253, Unification (old), a: 0809005Zutomorphism bundle, covariant derivative, curvature, fiber bundle, gauge transformation, holonomy, parallel transport, patentially and parallel transport and parallel trans principal bundle, superconnection, talk for FQXi 07, talk for Loops 07, talk for UCD 08, tangent bundle parallel transport, vector bundle connection, vector bundle parallel transport

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An Exceptionally Simple Theory of Everything, BRST speculation, Chern-Simons form, Discussion, Ehresmann connection, Ehresmann principal bundle connection, Geometry of Yang-Mills theory, Plan of attack (old), Symbols, This Week's Finds 253, Unification (old), automorphism bundle, covariant derivative, curvature, fiber bundle, gauge transformation, holonomy, parallel transport, path holonomy, principal bundle, superconnection, talk for FQXi 07, talk for Loops 07, talk for UCD 08, tangent bundle parallel transport, vector bundle connection, vector bundle parallel transport

1-form

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A 1-form, or **cotangent vector**, \underline{f} , is a geometric object that acts on a **tangent vector** at a point, p, to give a real number. It may be written in terms of the **coordinate basis 1-forms** as

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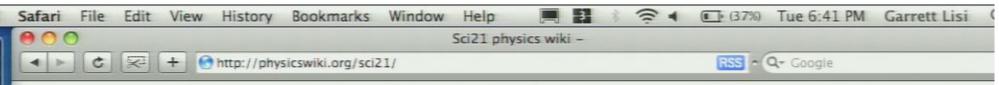
Page 52/127

$$f = f_i d\underline{x}^i \in T_p^*M$$

It is a linear operator, and so may be written as a function of a vector or more simply as a vector-form contraction (product),

$$\underline{f}(\overrightarrow{v}) = \mathbf{i}_{\overrightarrow{v}}\underline{f} = \overrightarrow{v}\underline{f} = v^jf_i\overrightarrow{\partial_j}d\underline{x}^i = v^jf_i\delta^i_j = v^if_i \in \Re$$

The vector space of 1-forms at each point, p, of a manifold, M, is the cotangent space, T^*M , and is spanned



$$\underline{A} = d\underline{x}^i A_i^{\ B}(x) T_B$$

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1-form



A 1-form, or cotangent vector, f, is a geometric object that acts on a tangent vector at a point, p, to give a real number. It may be written in terms of the coordinate basis 1-forms as

$$f = f_i d\underline{x}^i \in T_p^*M$$

It is a linear operator, and so may be written as a function of a vector or more simply as a vector-form contraction (product).

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sa: 08090057 Exceptionally Simple Theory of Everything, Grassmann number, Lie group geometry, Lorentz rotation, Symbols, This Wedige 54/123 253, connection, coordinate basis 1-forms, coordinate change, cotangent bundle, covariant derivative, differential form, frame, left-right rotator, natural, superconnection, vector projection onto a section, vector-form algebra, wedge product





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tangent vector



The **velocity**, or **tangent vector**, \vec{v} , with respect to some parameter, t, of a **path**, c(t), at a point is defined via the **directional derivative** of a **function**, f(x), along the path,

$$\left. rac{df(c(t))}{dt}
ight|_{t=0} = \left. rac{dc^i(t)}{dt}
ight|_{t=0} \left. rac{\partial f}{\partial x^i}
ight|_{c(0)} = \left. v^i rac{\overrightarrow{\partial}}{\partial x^i} [f]
ight|_{c(0)} = \overrightarrow{v}[f]$$

A tangent vector, or simply "vector", can also be visualized in the pseudo-Euclidean embedding space containing the manifold. For a manifold parameterized by coordinates, the coordinate basis vectors are

$$\overrightarrow{\partial_i} = rac{\overrightarrow{\partial}}{\partial x^i} = rac{\partial \overrightarrow{p}}{\partial x^i} = \partial_i \overrightarrow{p}$$

with the parameterized manifold points, $\vec{p}(x)$, vectors from some arbitrary origin in the flat embedding space.

A vector at a point, p, may be written in terms of coordinate basis vectors,

$$\overrightarrow{v}=rac{dc^{i}(t)}{dt}\overrightarrow{\partial_{i}}=v^{i}\overrightarrow{\partial_{i}}$$

sa: 080999857real valued quantities, v^i , are the velocity components. (Summation over repeated indices is impliced 5/127

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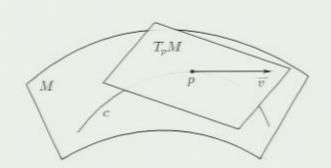
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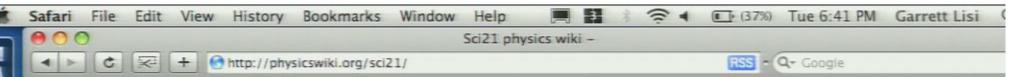
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The space of all tangent vectors to a manifold, M, at a point, p, is a vector space, T_pM , the tangent space to M at p.

The directional derivative of a function may also be be written using the exterior derivative and vector-form algebra as

$$\overrightarrow{v}[f] = \overrightarrow{v}\underline{d}f = v^i\partial_i f$$

1-form, Hodge identities, Killing spinor, Lie derivative, Lorentz rotation, Symbols, commutator, coordinate basis vectors, coordinate change, differential f.Page,56/182 rior



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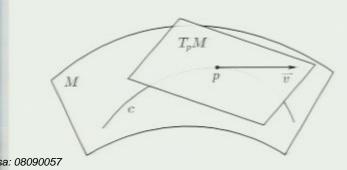
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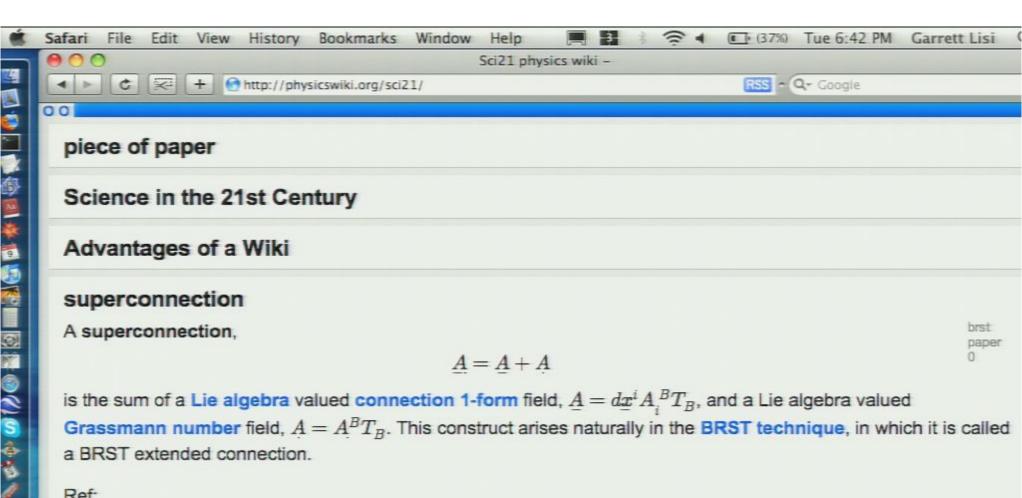
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1-form, Hodge identities, Killing spinor, Lie derivative, Lorentz rotation age 57/127s, commutator, coordinate basis vectors, coordinate change, differential form, exterior

derivative flow frame geodesic natural path proper time pullback rest frame submanifold geometry tangent bundle tangent bundle



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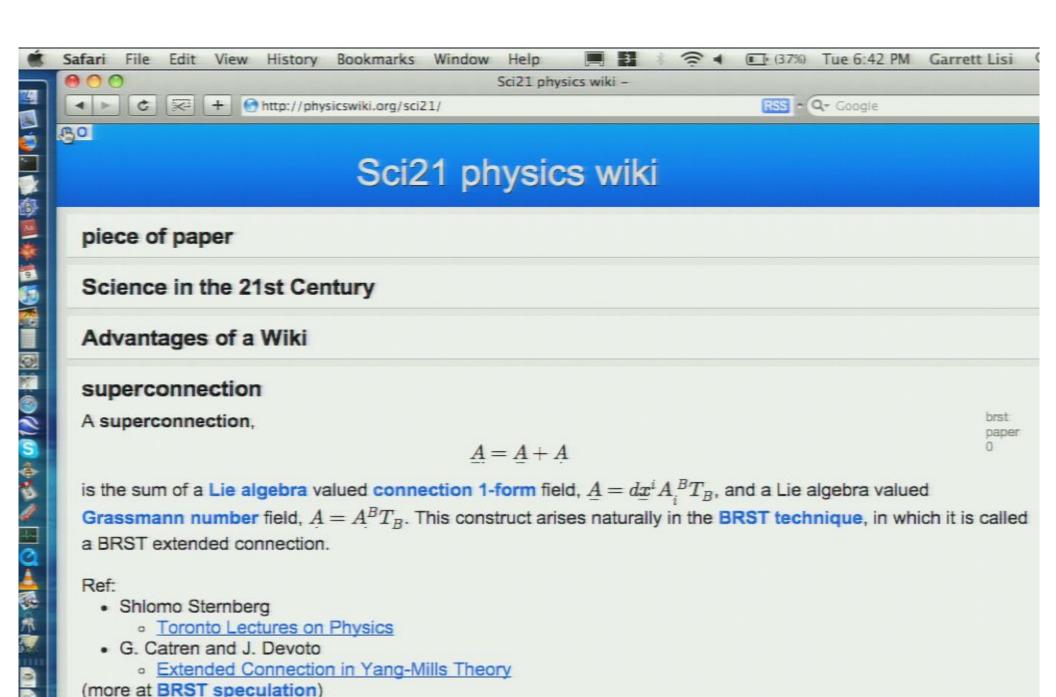
- Shlomo Sternberg
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(more at BRST speculation)

An Exceptionally Simple Theory of Everything, This Week's Finds 253, piece of paper, the big picture

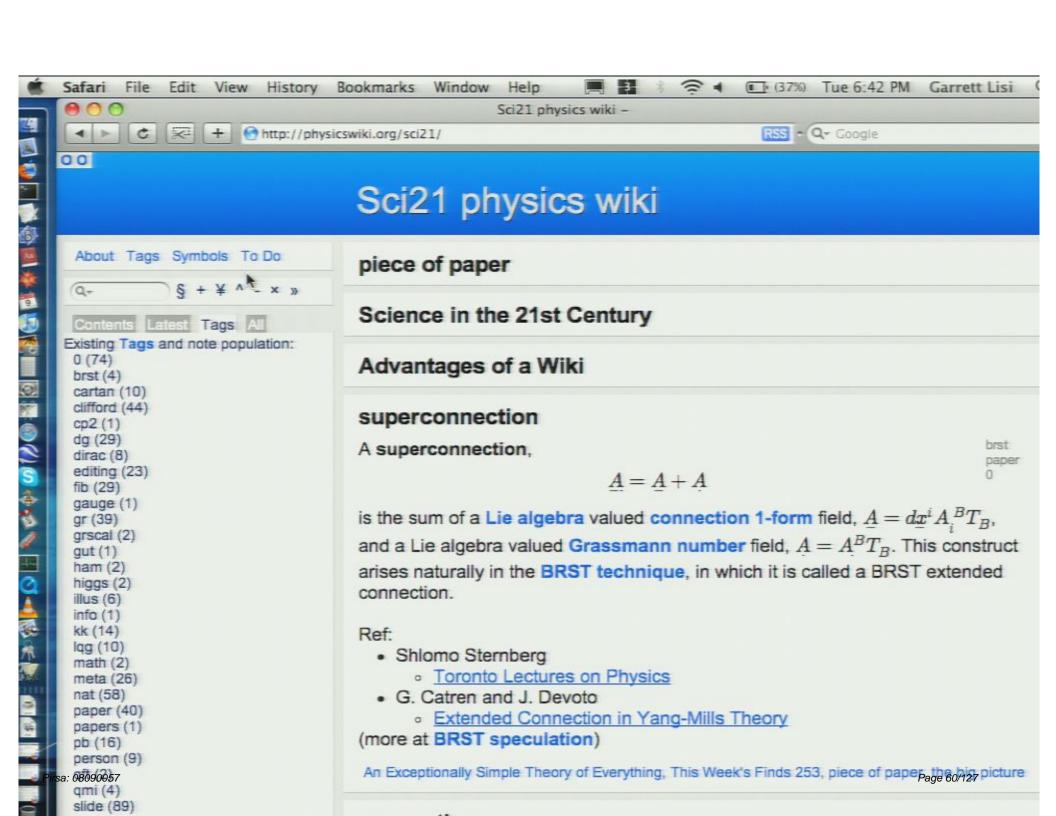
connection

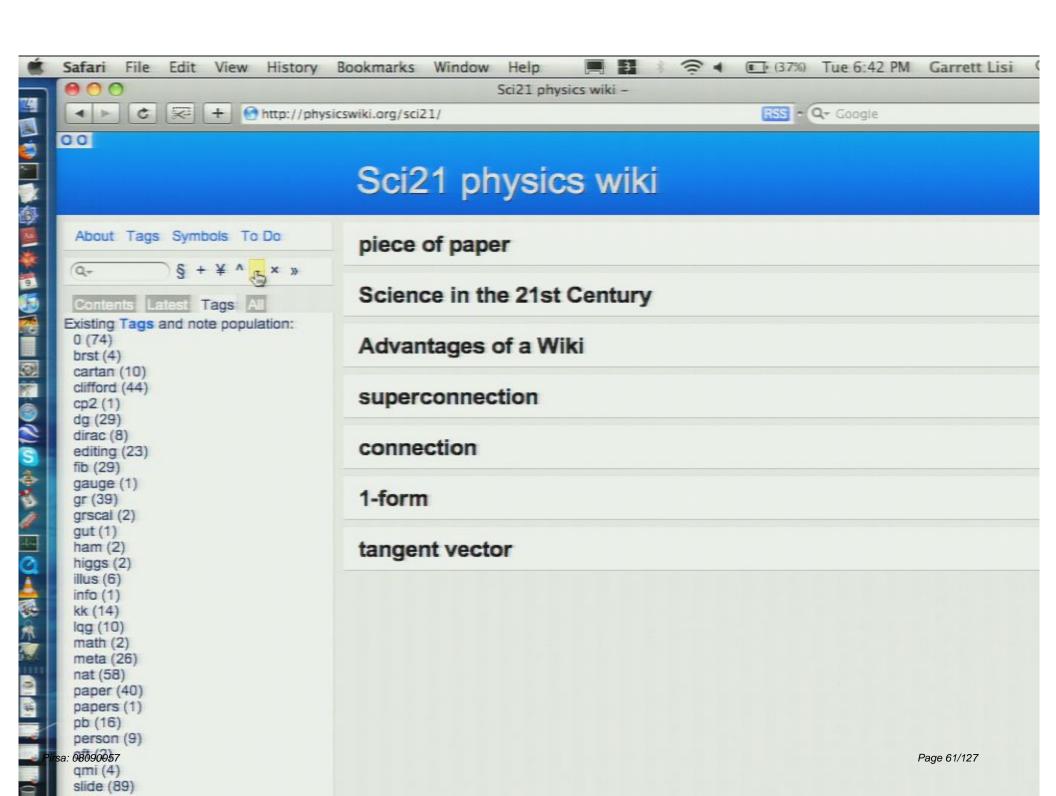
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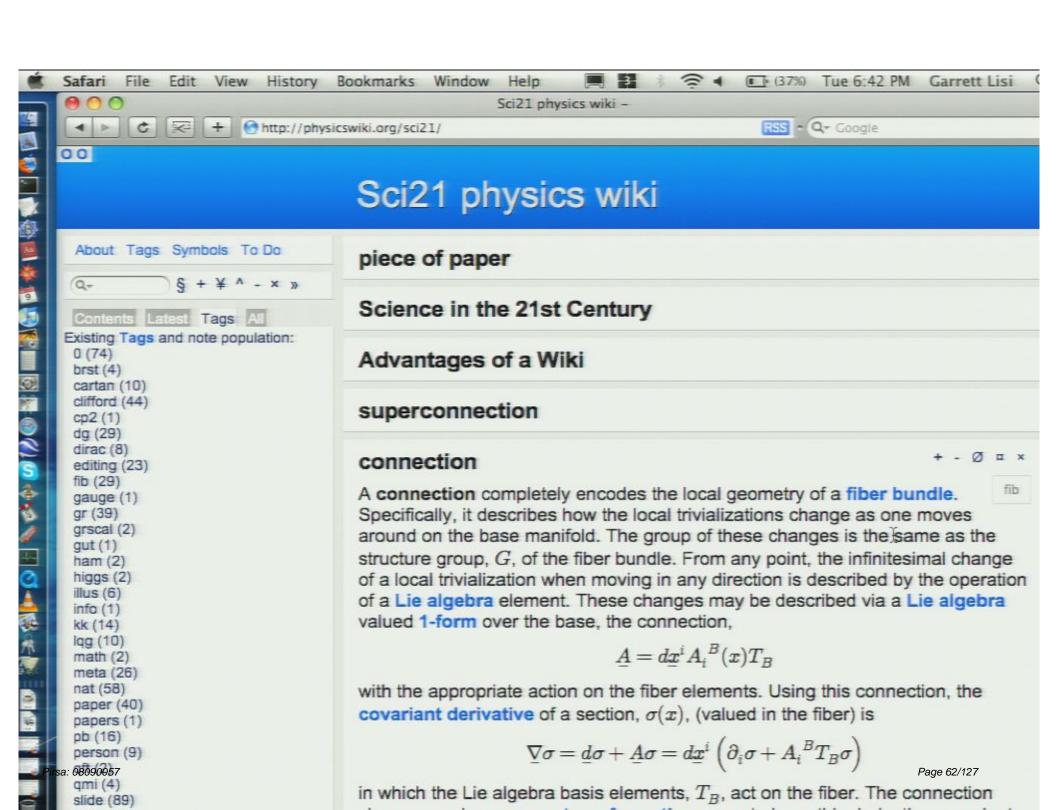


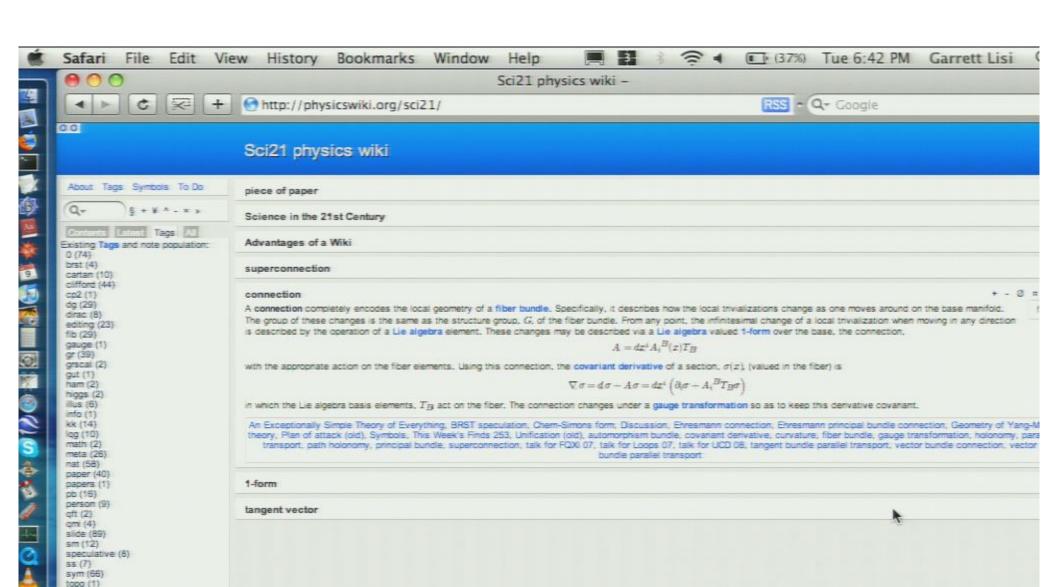
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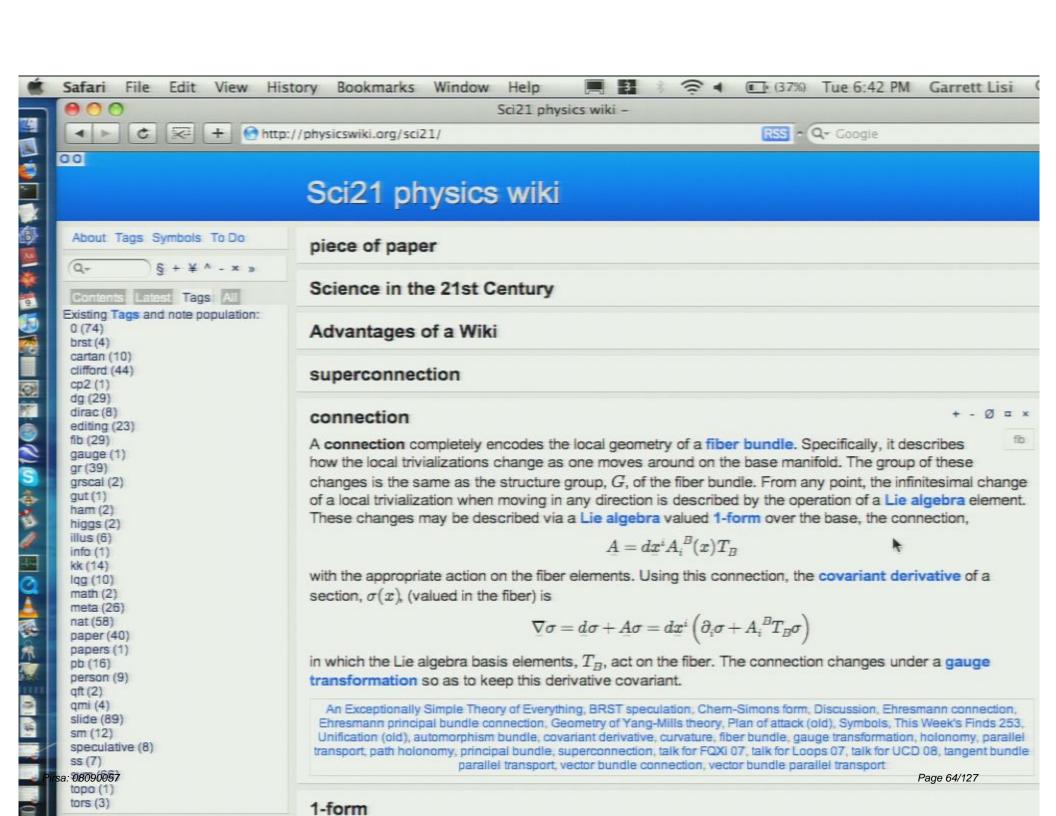


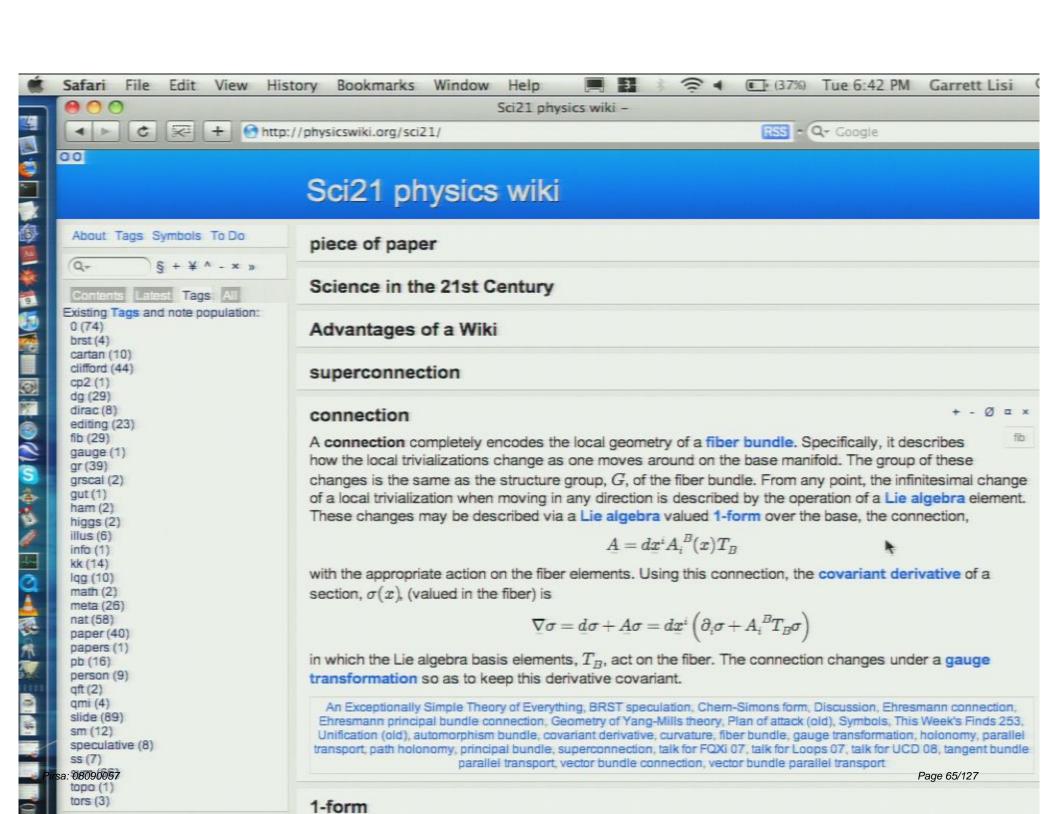


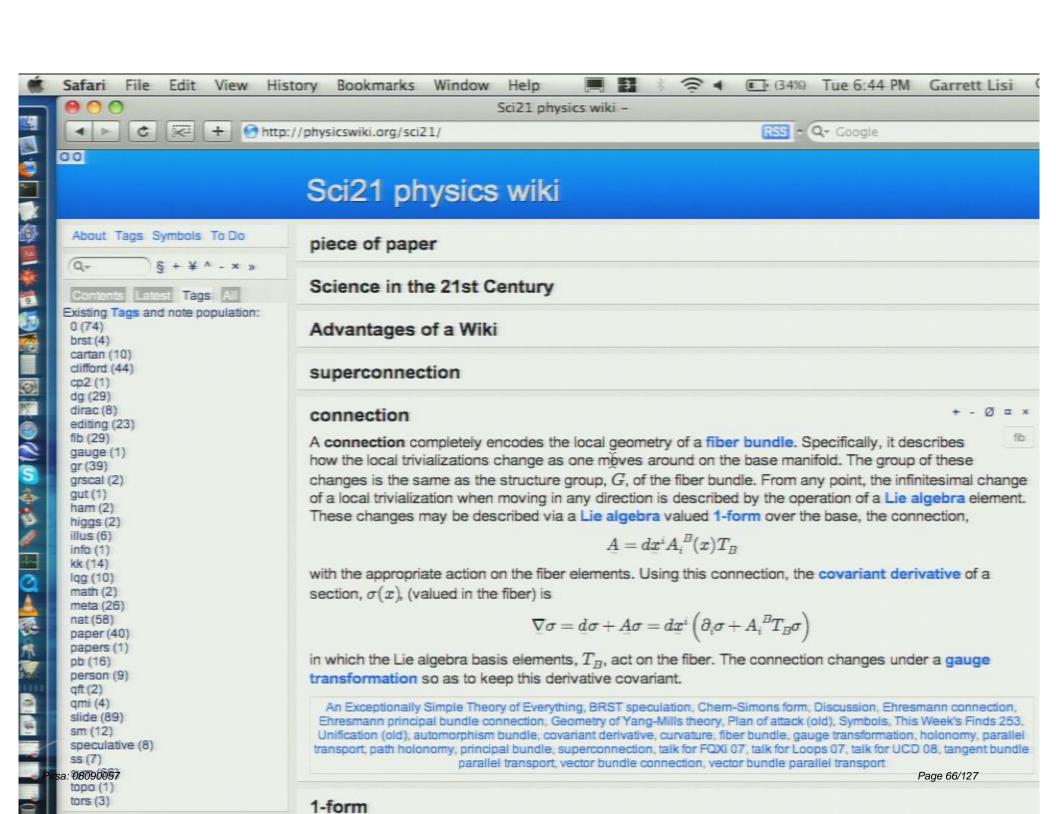


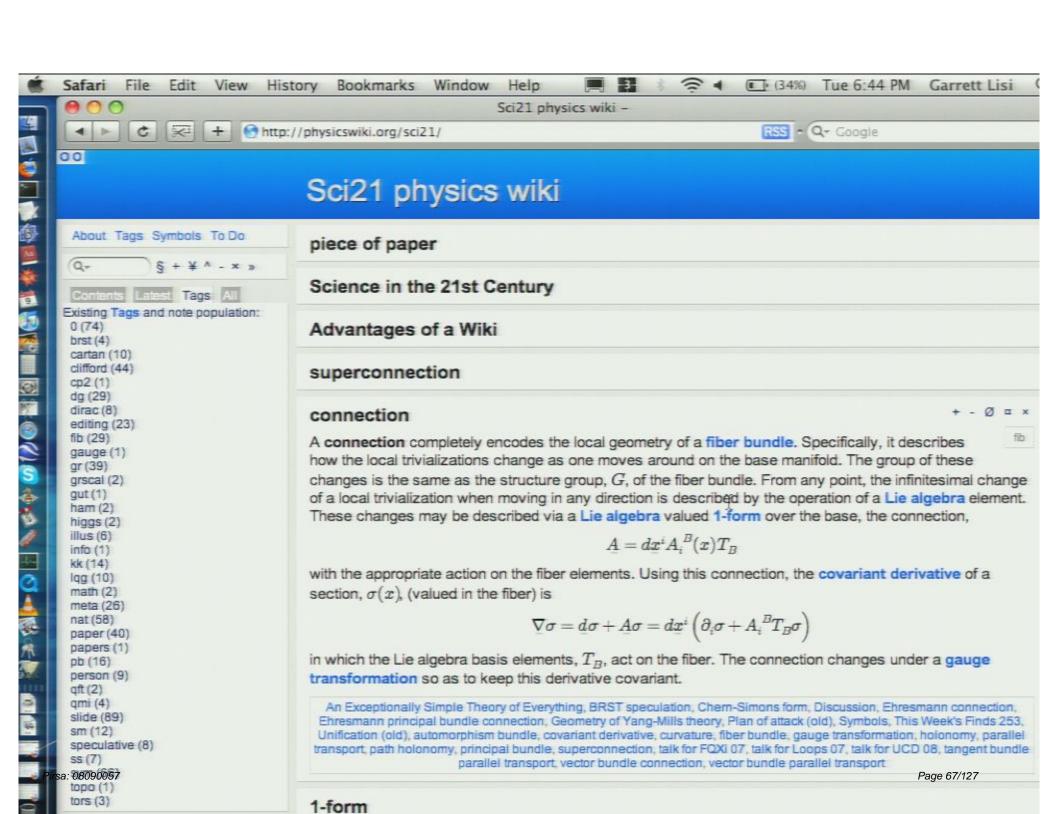
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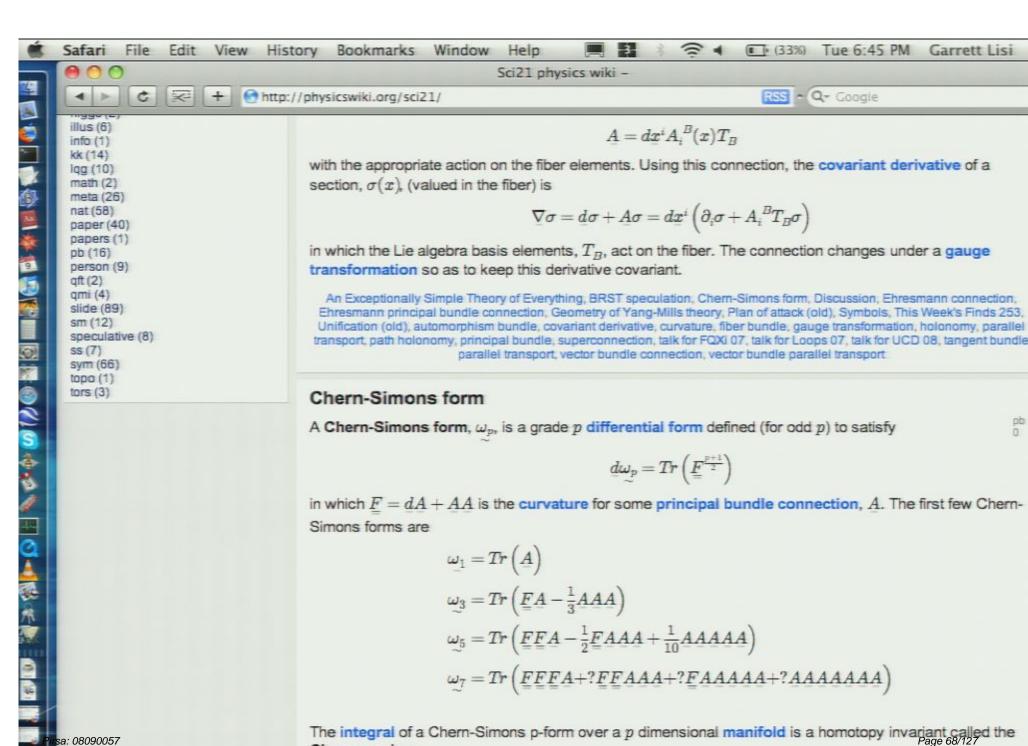
tors (3)





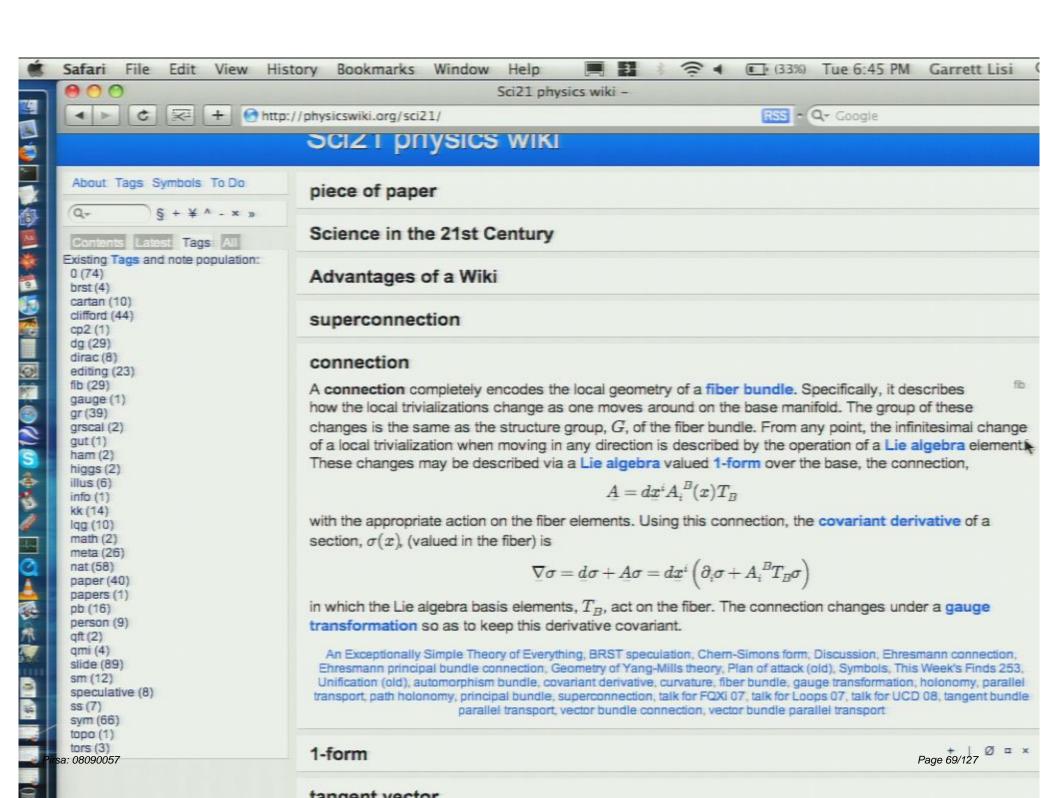


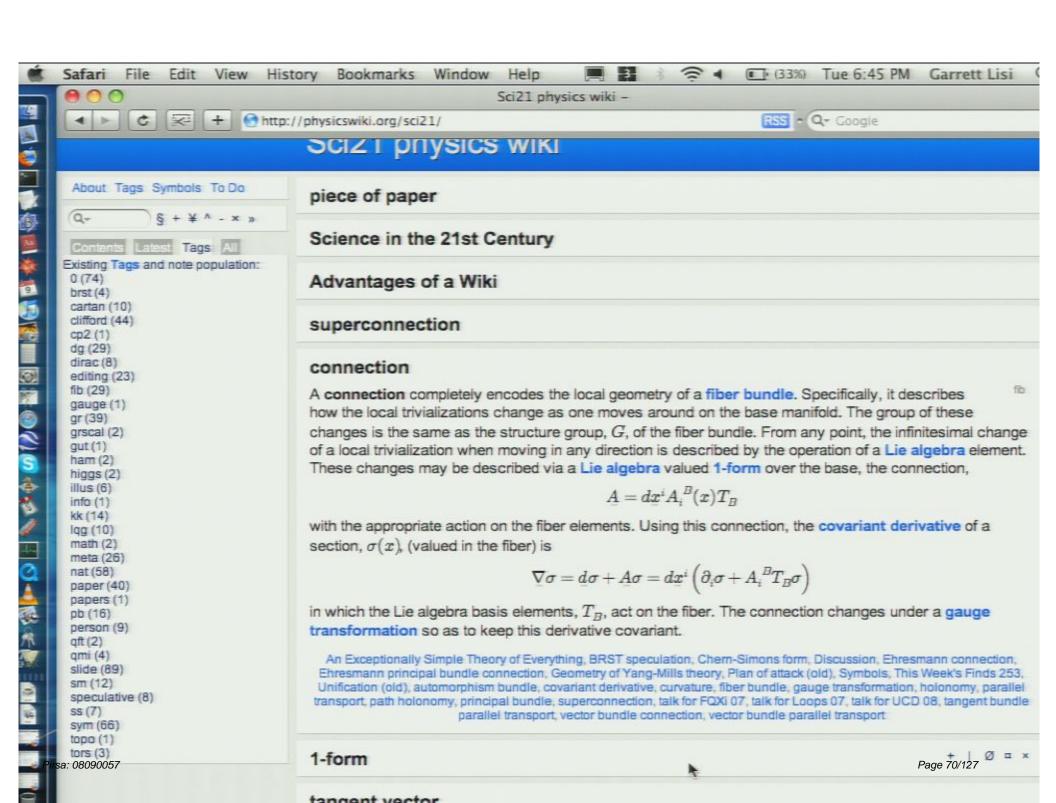


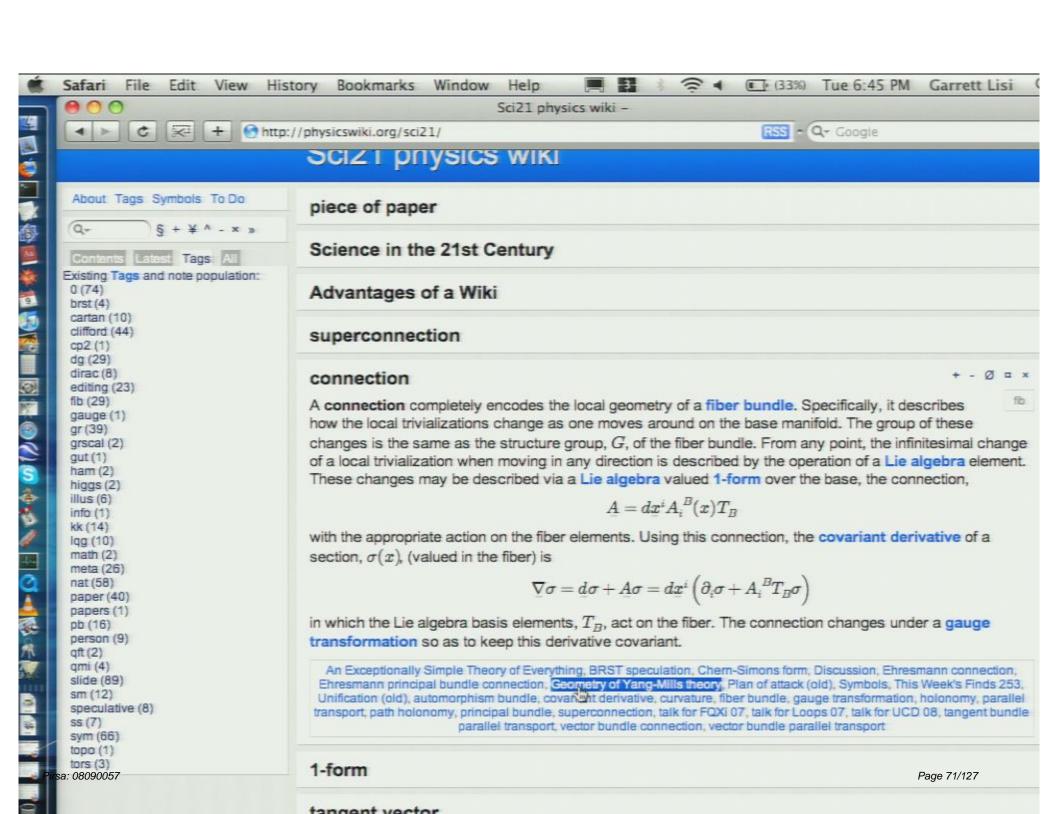


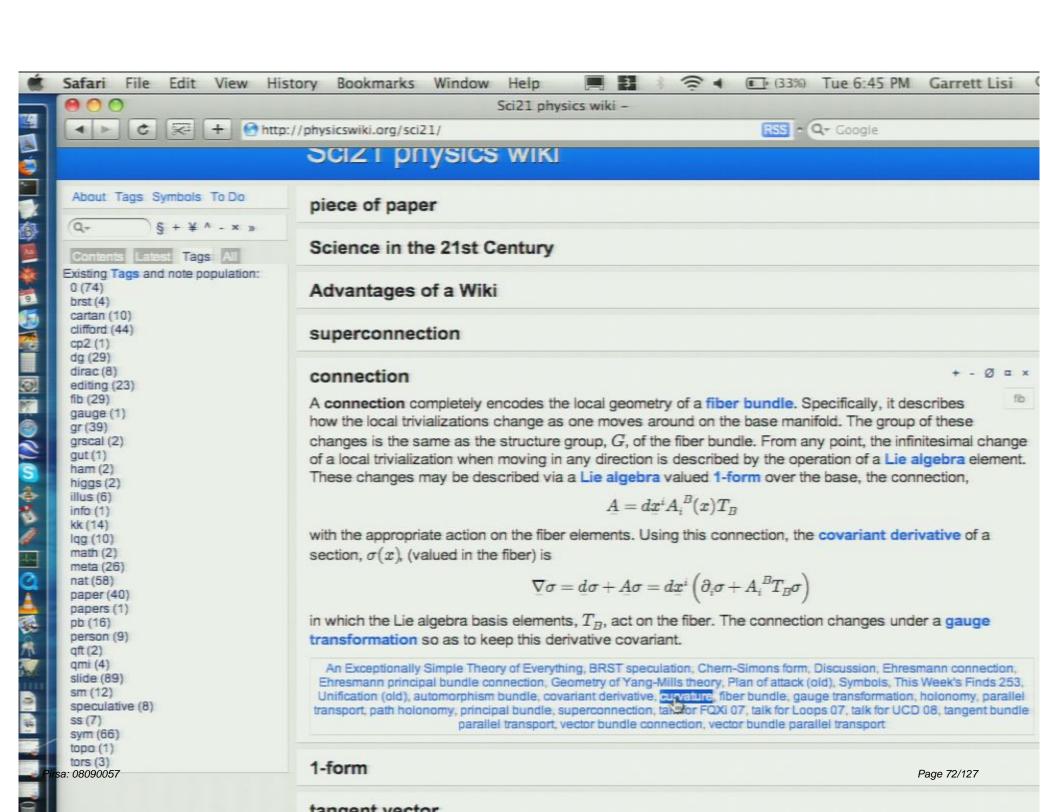
Chern number.

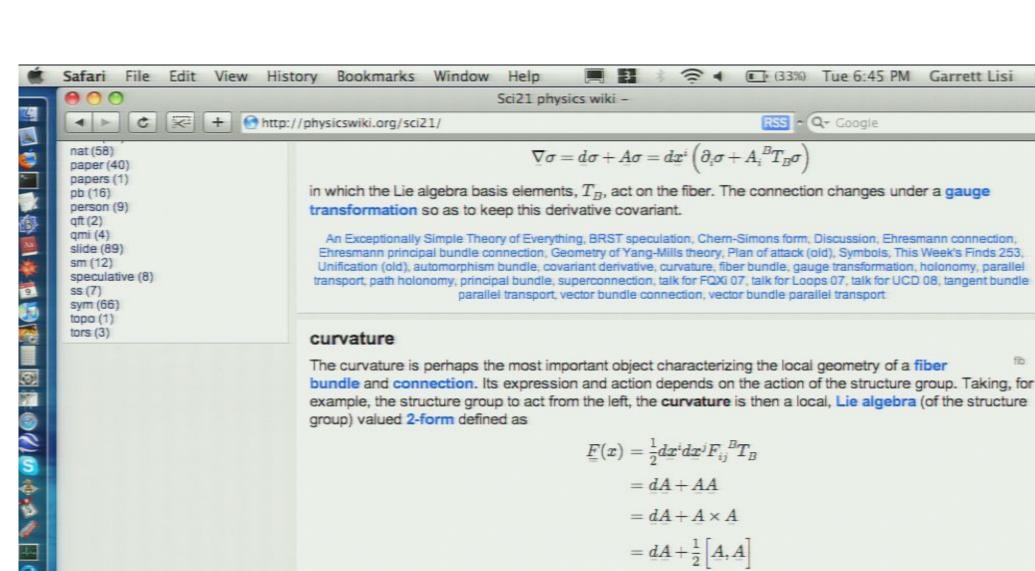
Garrett Lisi











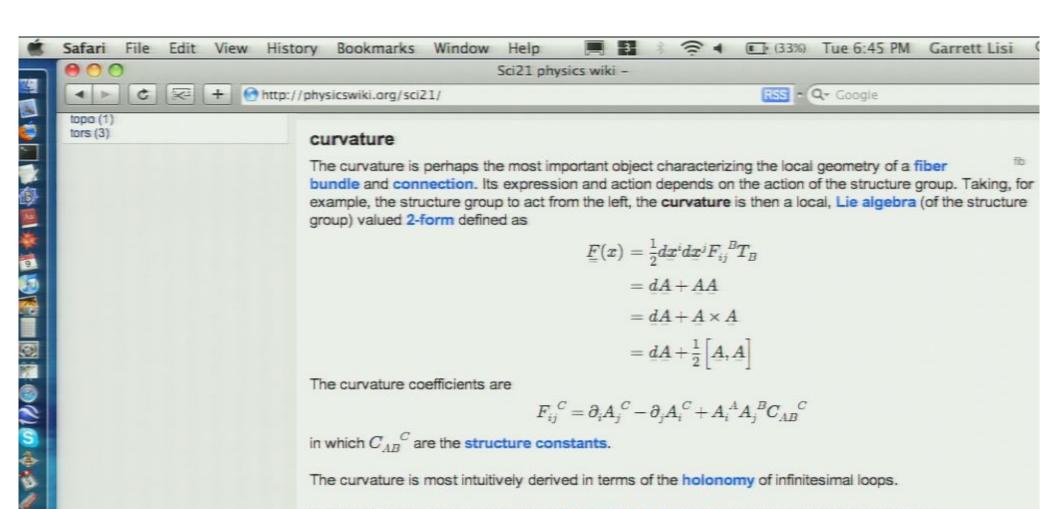
The curvature coefficients are

$$F_{ij}^{\ C} = \partial_i A_j^{\ C} - \partial_j A_i^{\ C} + A_i^{\ A} A_j^{\ B} C_{AB}^{\ C}$$

The curvature is most intuitively derived in terms of the holonomy of infinitesimal loops.

It may also be derived by applying the covariant derivative twice to any fiber bundle section,

$$abla
abla C = \left(d + A\right)\left(d + A\right)C = ddC + dAC + AdC + AdC + AAC = \left(dA + AA\right)C = FC$$
Page 73/127



= dA + AA $= dA + A \times A$ $=dA+\frac{1}{2}\left[A,A\right]$

The curvature coefficients are

$$F_{ij}^{C} = \partial_i A_j^{C} - \partial_j A_i^{C} + A_i^{A} A_j^{B} C_{AB}^{C}$$

in which C_{AB}^{C} are the structure constants.

The curvature is most intuitively derived in terms of the holonomy of infinitesimal loops.

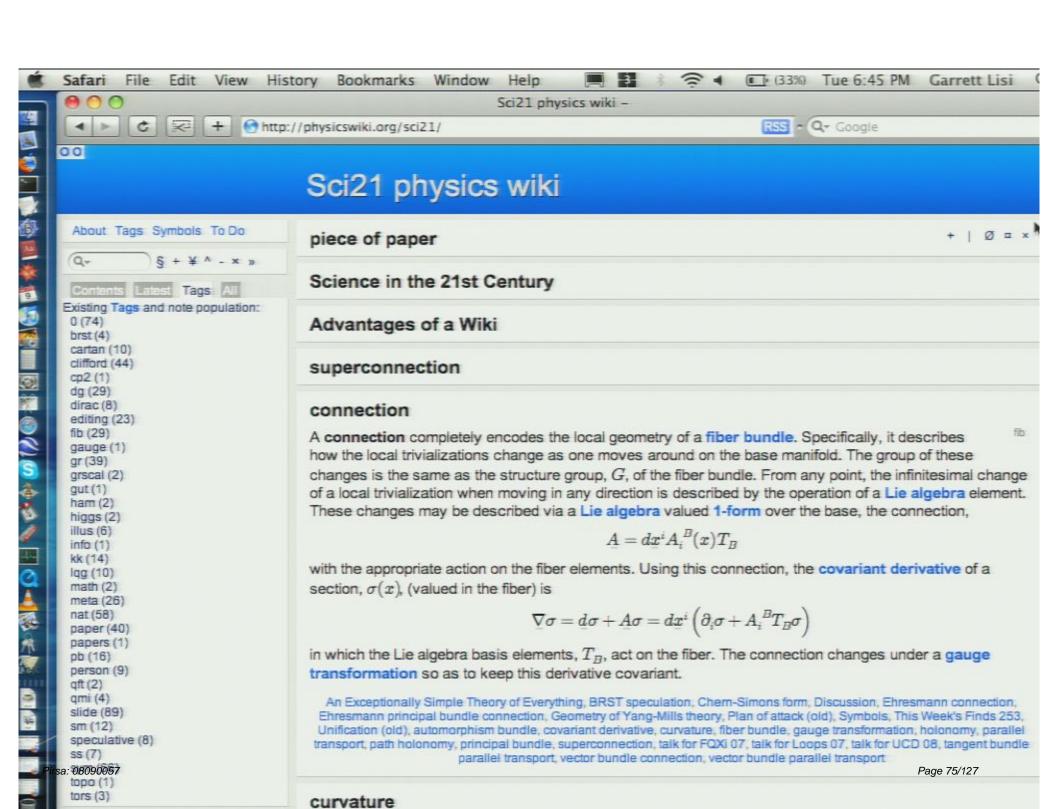
It may also be derived by applying the covariant derivative twice to any fiber bundle section,

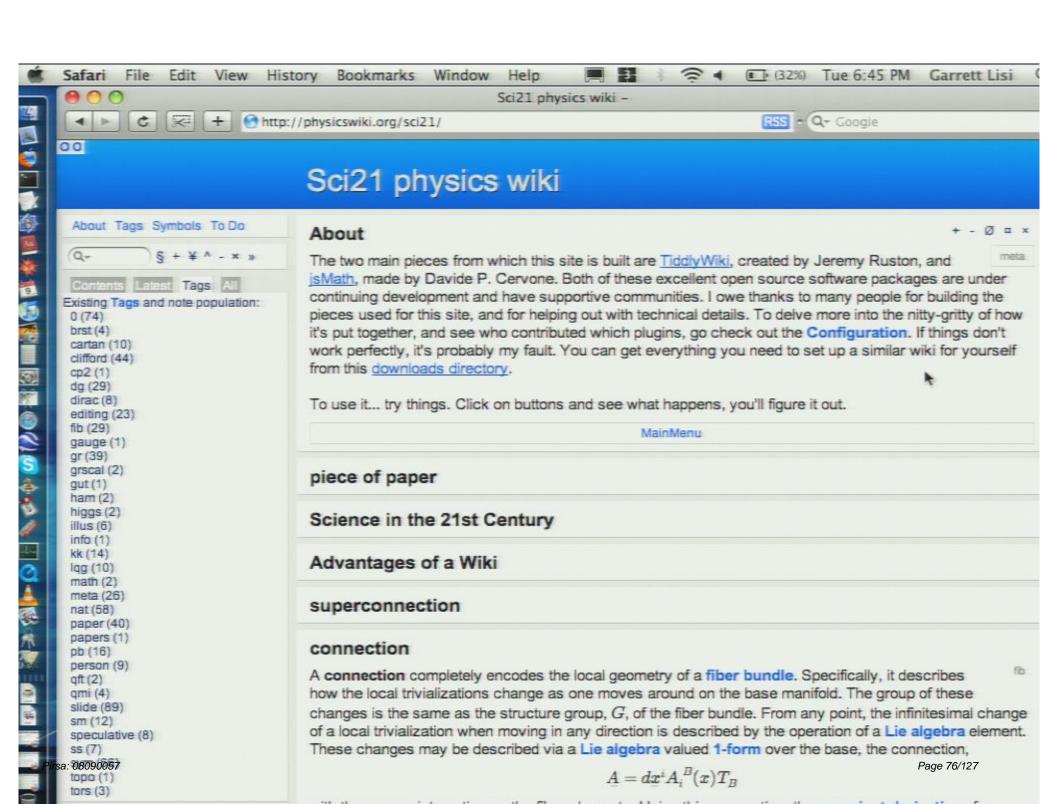
$$\nabla \nabla C = \left(\underline{d} + \underline{A}\right) \left(\underline{d} + \underline{A}\right) C = \underline{d}\underline{d}C + \underline{d}\underline{A}C + \underline{A}\underline{d}C + \underline{A}\underline{A}C = \left(\underline{d}\underline{A} + \underline{A}\underline{A}\right) C = \underline{F}C$$

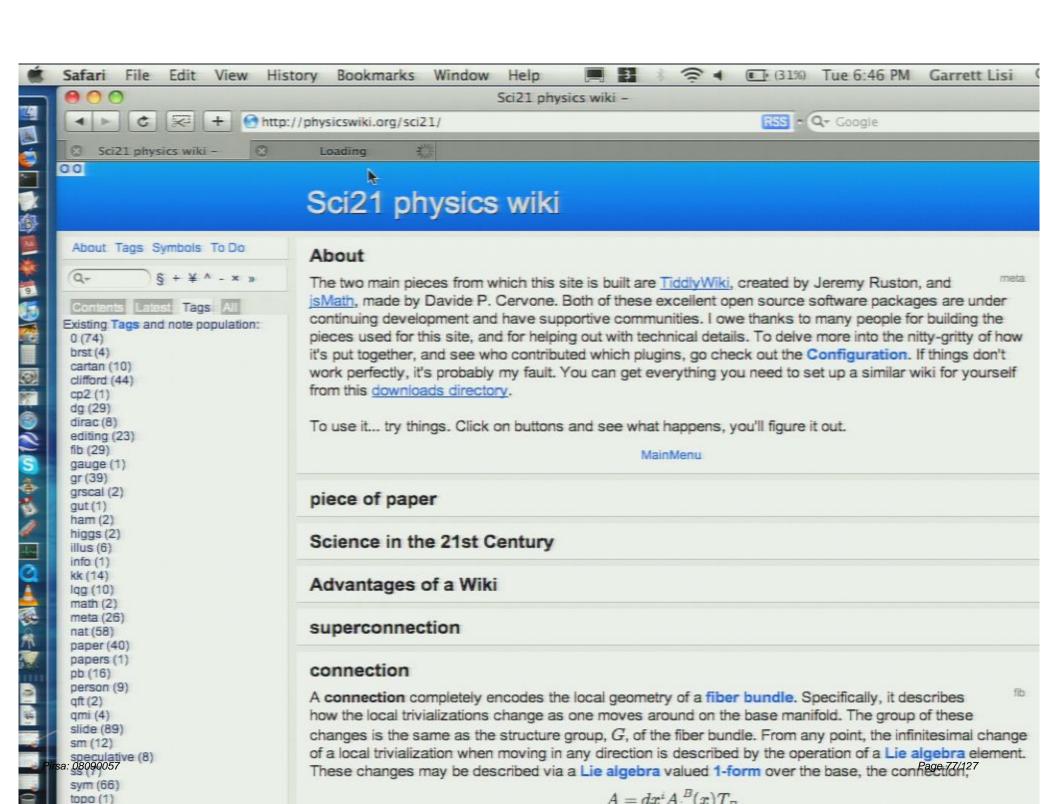
The curvature changes under gauge transformations, $C \mapsto C' = gC$, as $F \mapsto F' = gFg^-$.

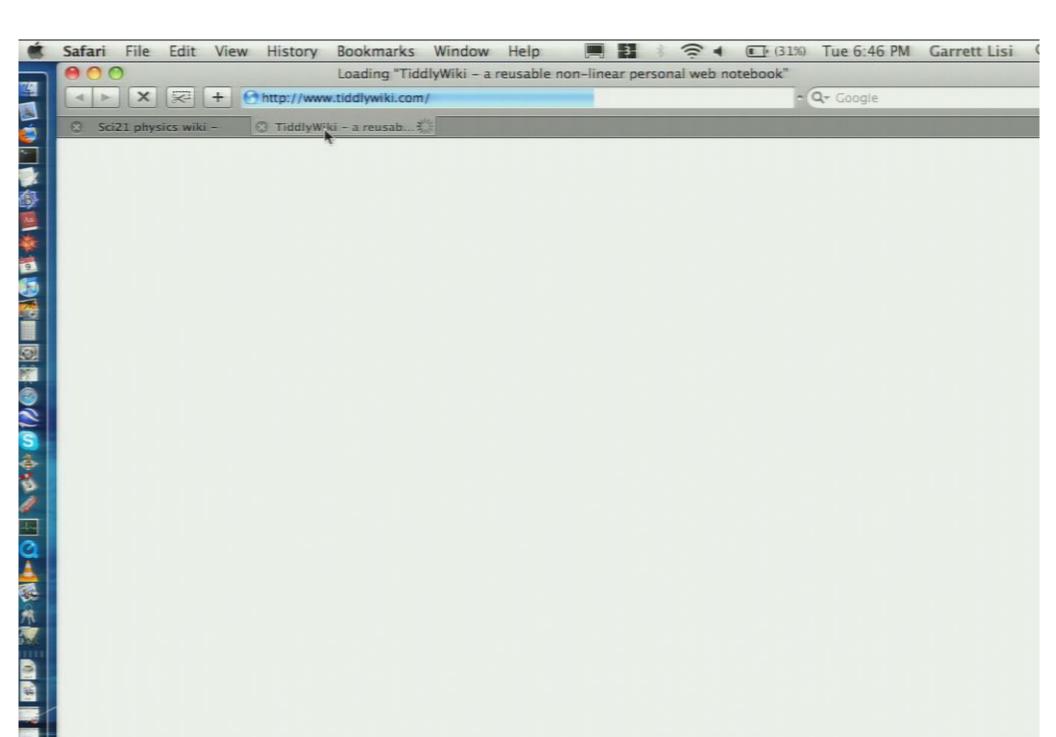
Note again that the expression of the curvature, and its action, depends on the form of the group action.

An Exceptionally Simple Theory of Everything, Cartan geometry, Cartan tangent bundle spin connection, Chern-Simons form, Clifford-Riemann curvature, Maurer-Cartan form, Plan of attack (old), Standard model and gravity in a matrix, Symbols, This Week's Finds 253, Unification (old), automorphism bundle, covariant derivative, fiber bundle, gauge transformation, holonomy, homogeneous space tangent bundle geometry, principal bundle, talk for FQXi 07, talk for Loops 07, talk for UCD 08, the big picture, vector bundle curvature

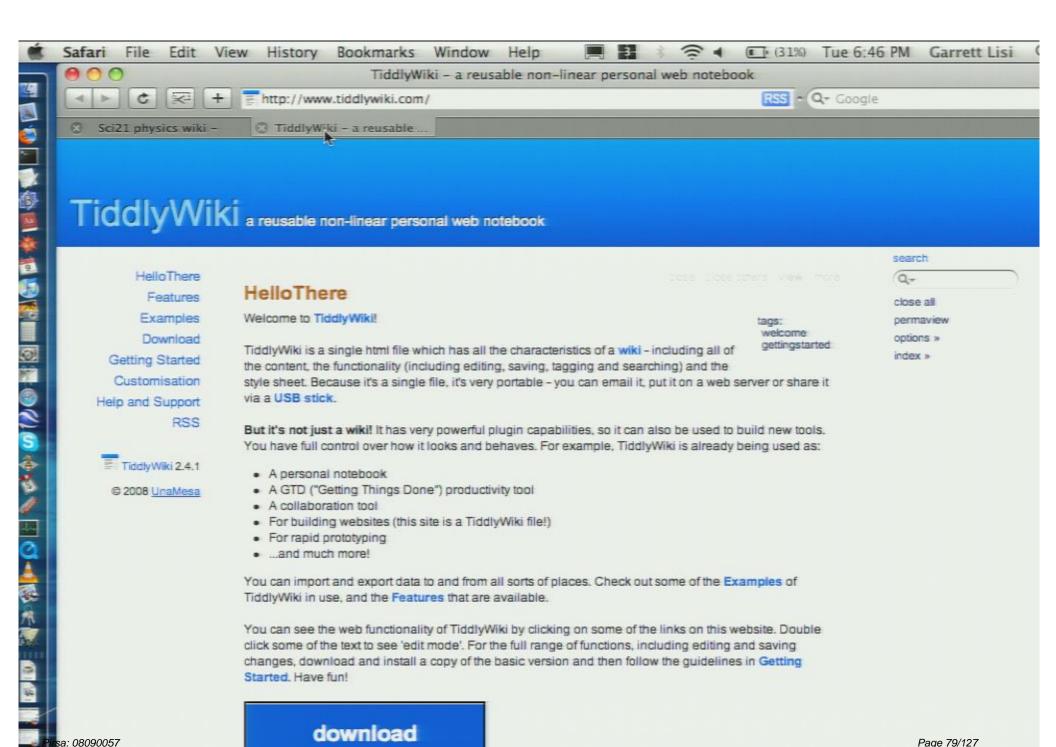


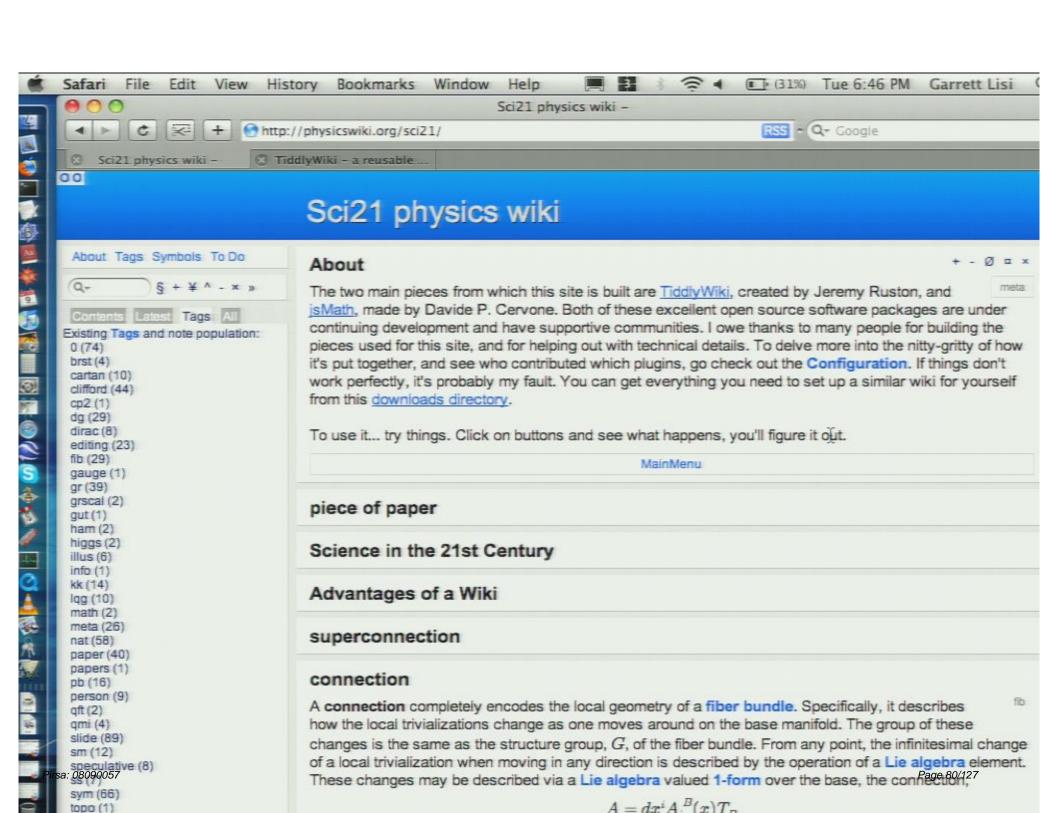


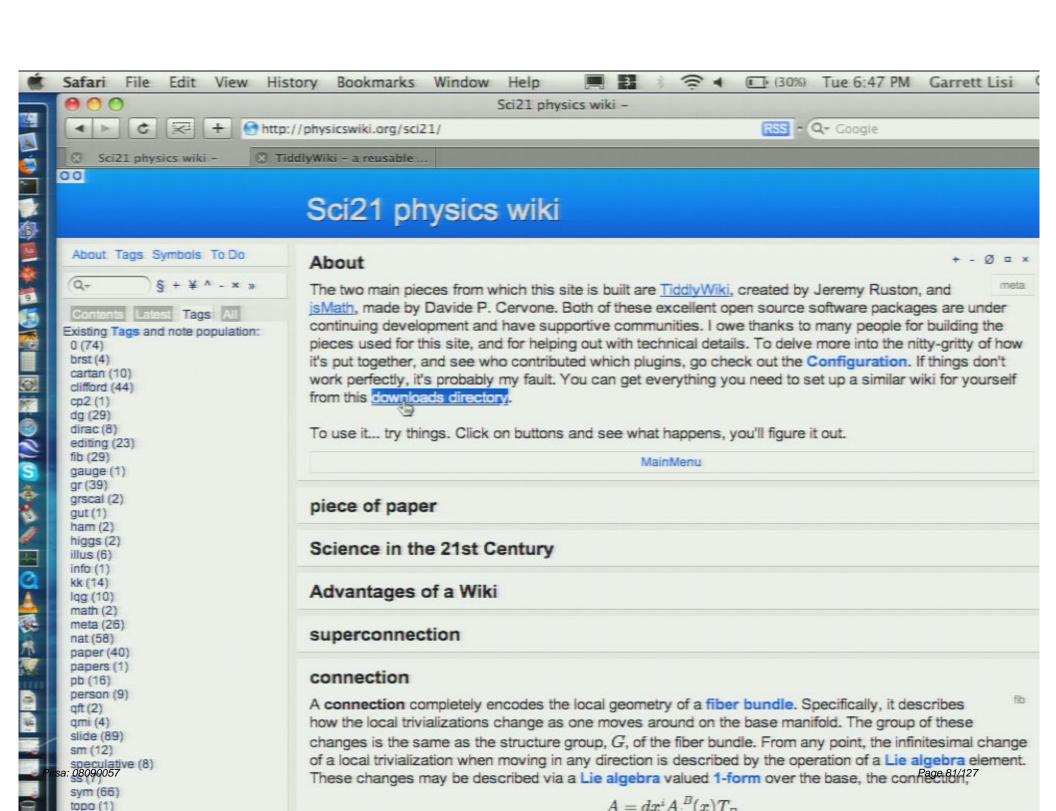


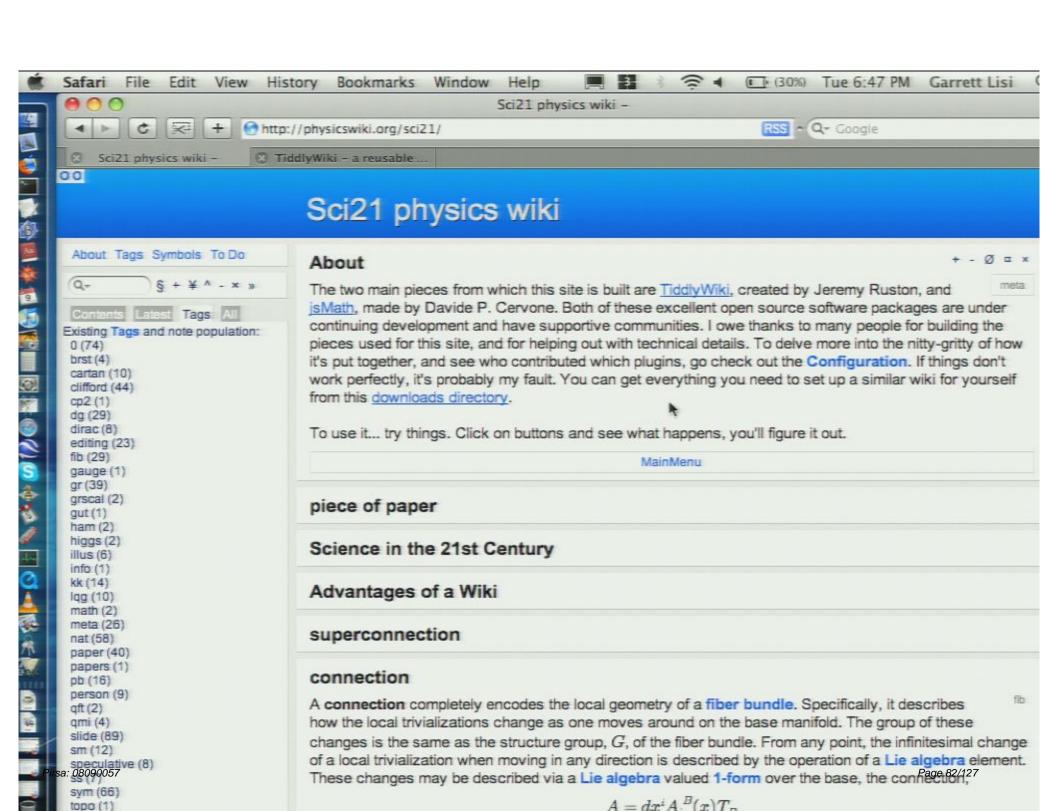


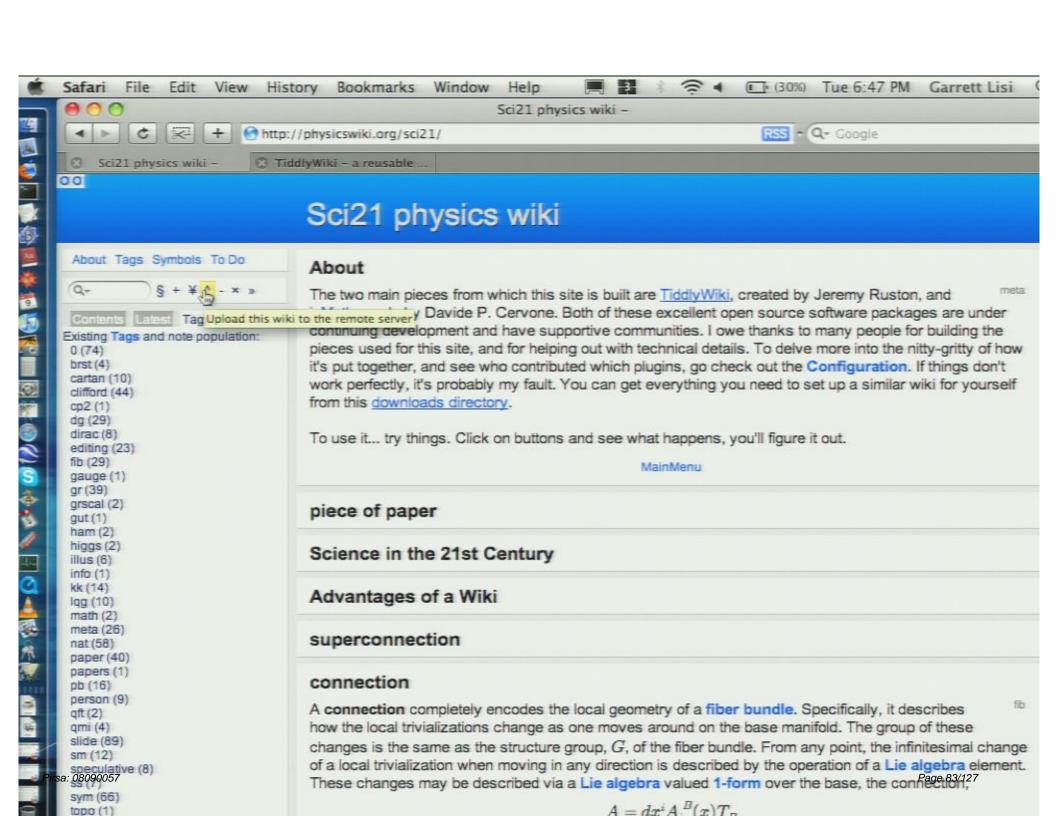
sa: 08090057 Page 78/127

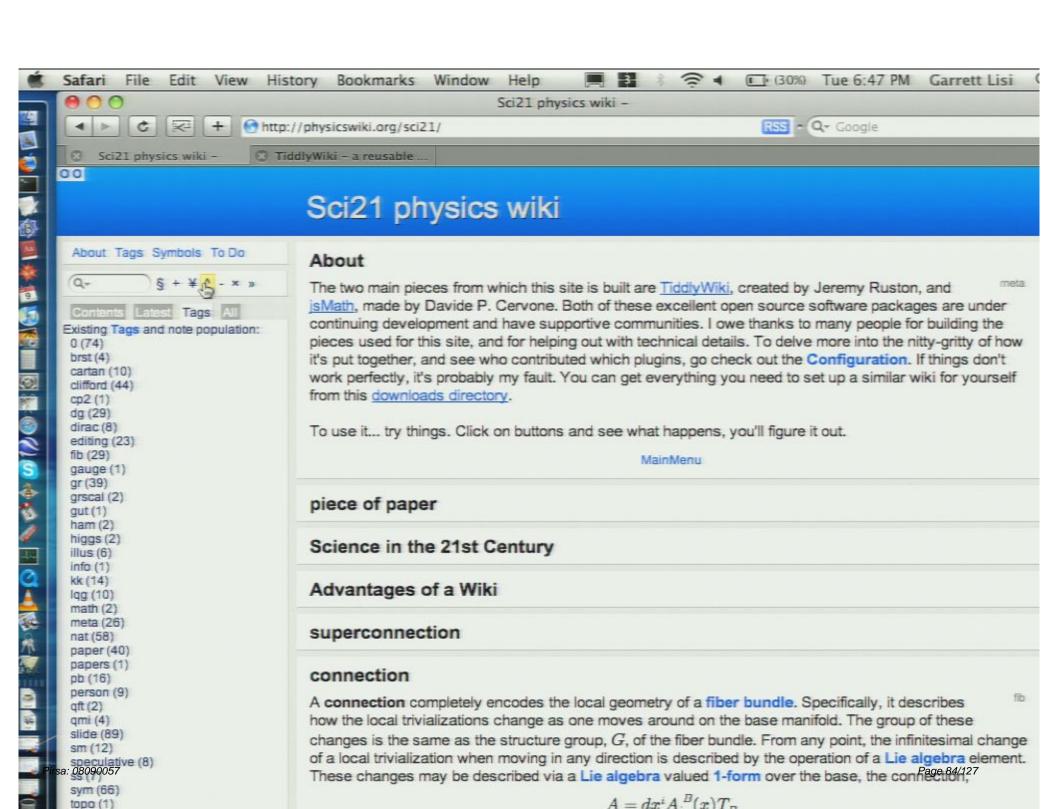


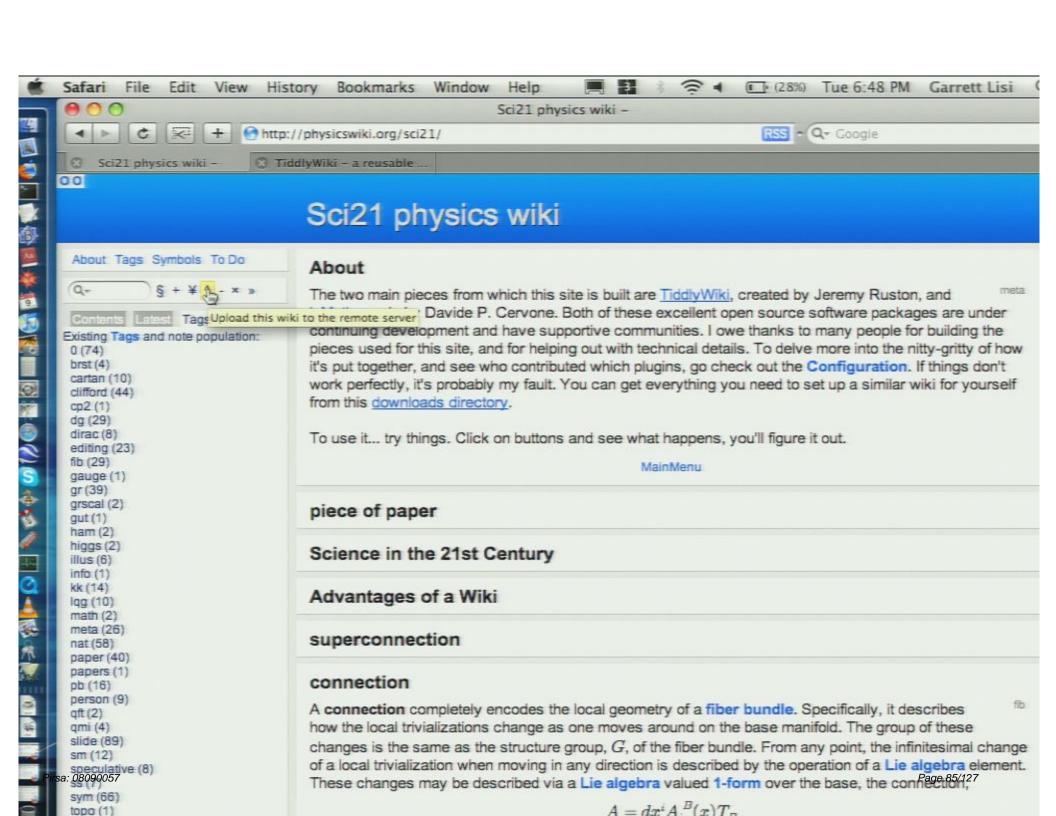


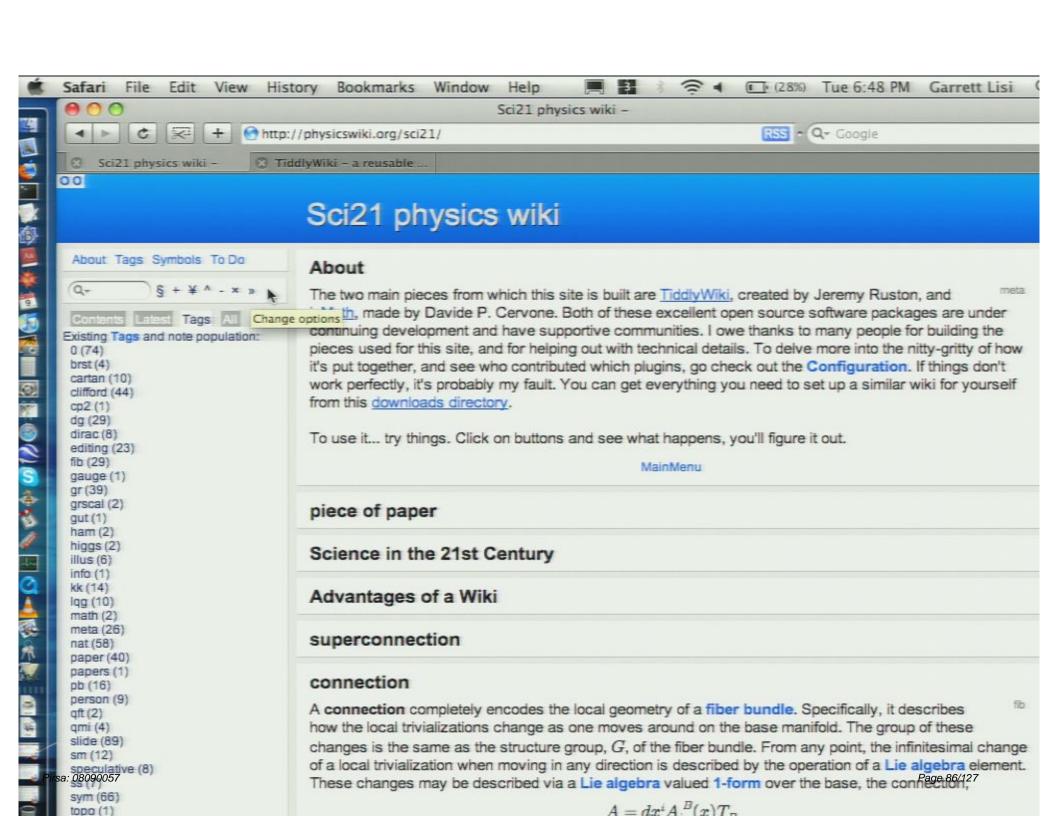


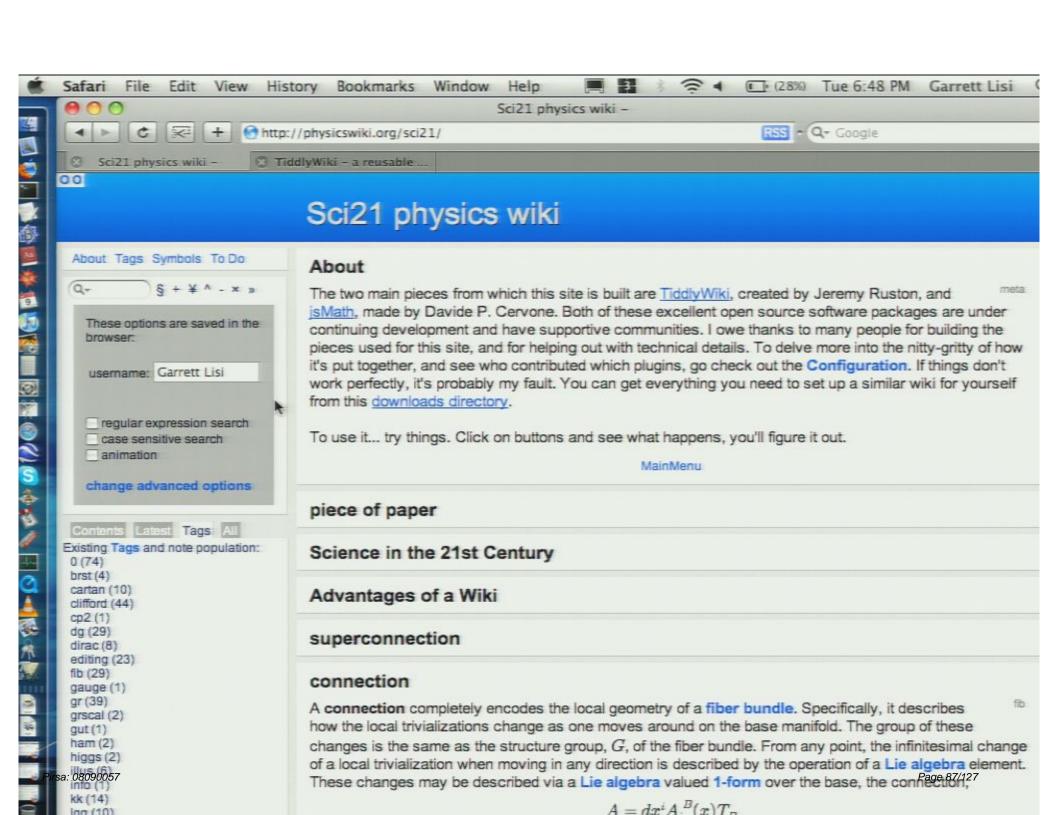


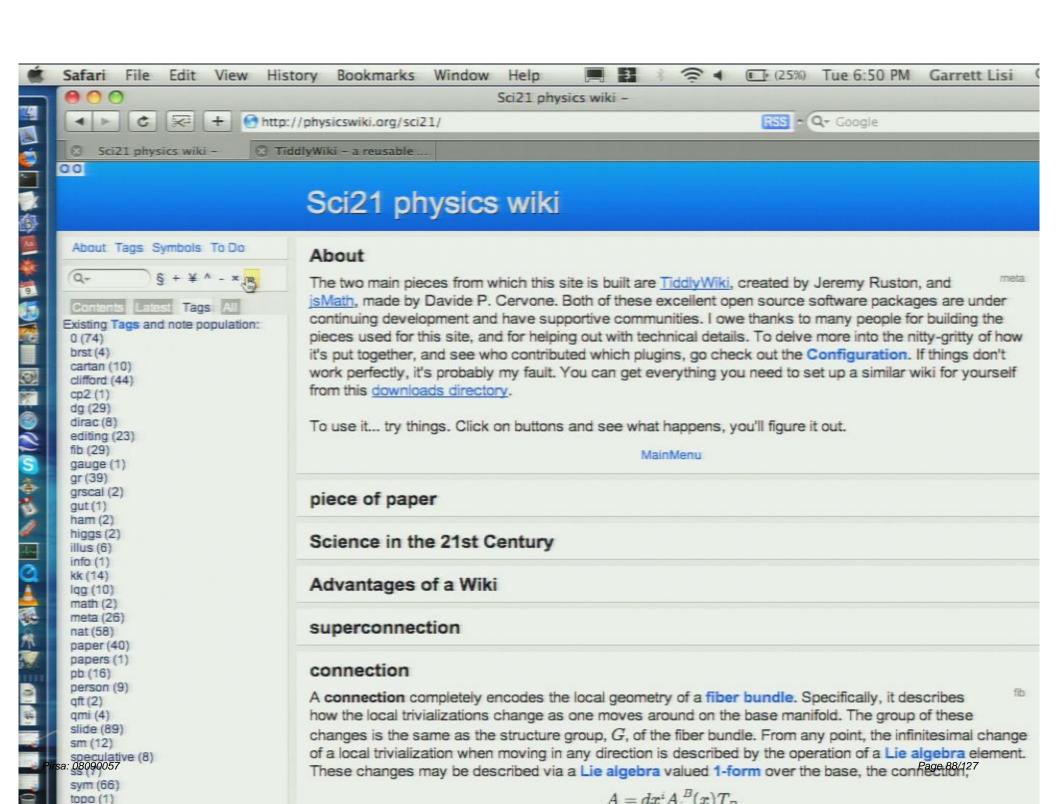


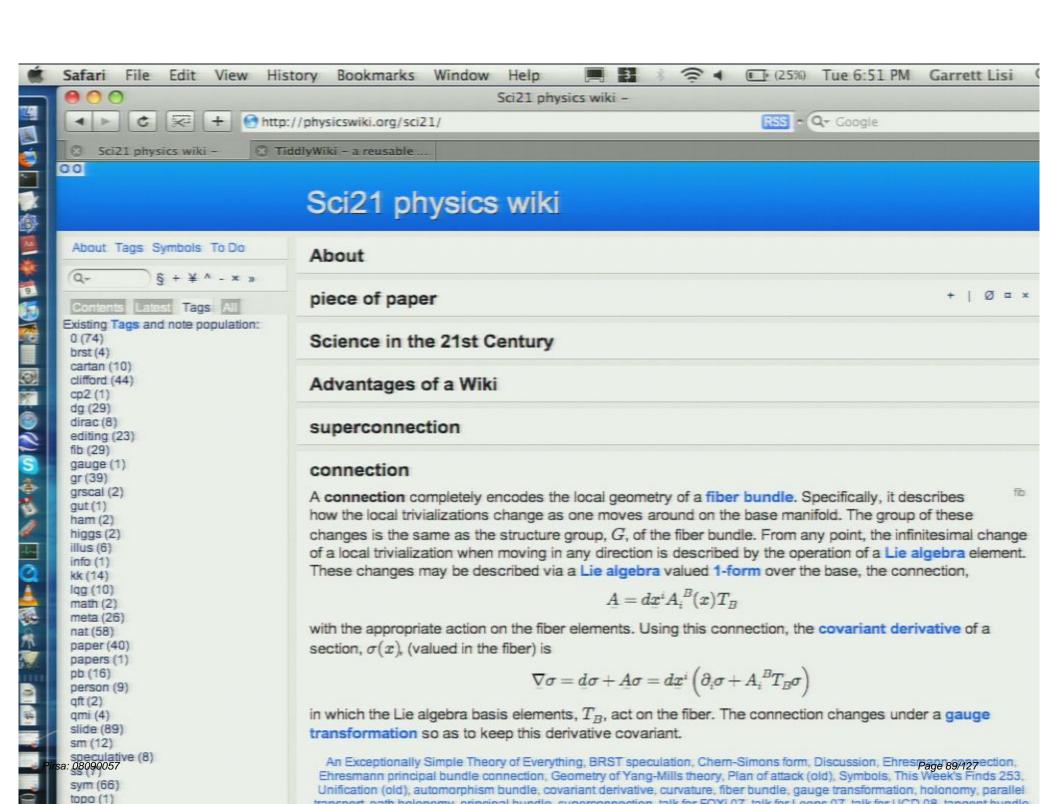


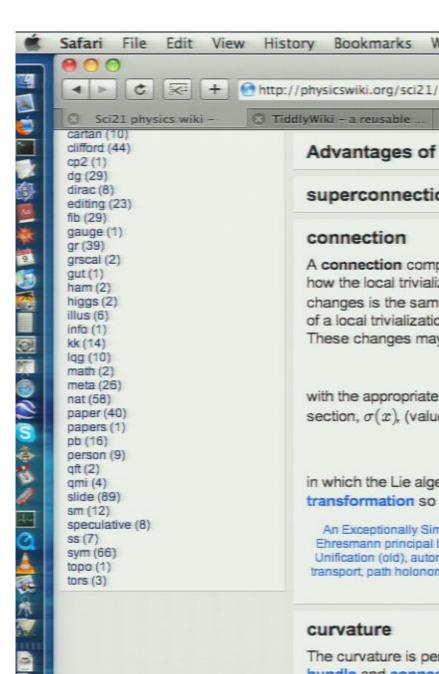












Advantages of a Wiki

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superconnection

Bookmarks

connection

fib A connection completely encodes the local geometry of a fiber bundle. Specifically, it describes how the local trivializations change as one moves around on the base manifold. The group of these changes is the same as the structure group, G, of the fiber bundle. From any point, the infinitesimal change of a local trivialization when moving in any direction is described by the operation of a Lie algebra element. These changes may be described via a Lie algebra valued 1-form over the base, the connection,

(25%) Tue 6:51 PM

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Garrett Lisi

$$A = dx^i A_i^{\ B}(x) T_B$$

with the appropriate action on the fiber elements. Using this connection, the covariant derivative of a section, $\sigma(x)$, (valued in the fiber) is

$$abla \sigma = d\sigma + A\sigma = dx^i \left(\partial_i \sigma + A_i{}^B T_B \sigma
ight)$$

in which the Lie algebra basis elements, T_R , act on the fiber. The connection changes under a gauge transformation so as to keep this derivative covariant.

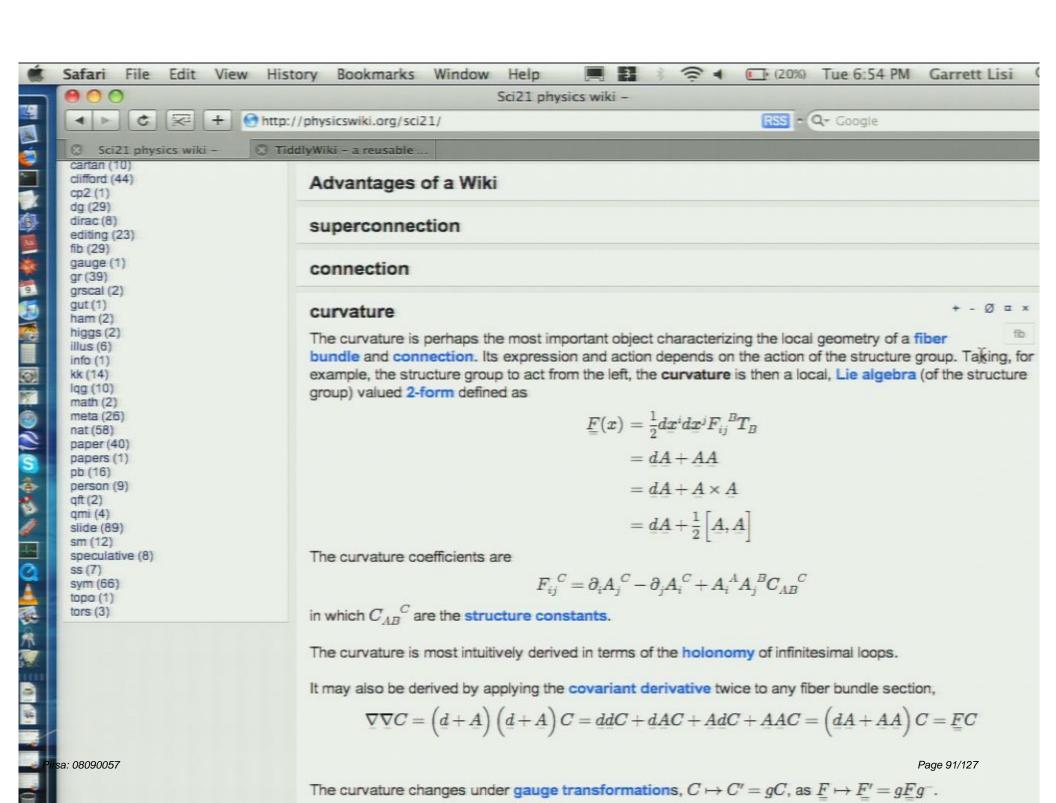
An Exceptionally Simple Theory of Everything, BRST speculation, Chern-Simons form, Discussion, Ehresmann connection, Ehresmann principal bundle connection, Geometry of Yang-Mills theory, Plan of attack (old), Symbols, This Week's Finds 253, Unification (old), automorphism bundle, covariant derivative, curvature, fiber bundle, gauge transformation, holonomy, parallel transport, path holonomy, principal bundle, superconnection, talk for FQXi 07, talk for Loops 07, talk for UCD 08, tangent bundle parallel transport, vector bundle connection, vector bundle parallel transport

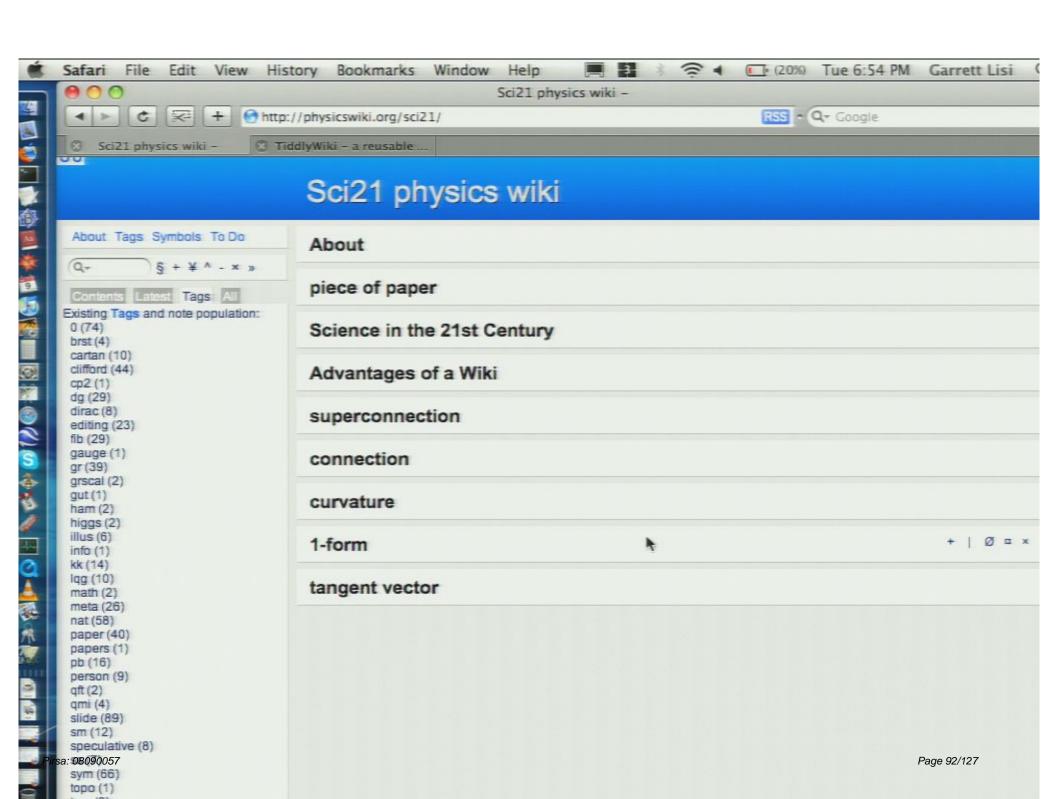
curvature

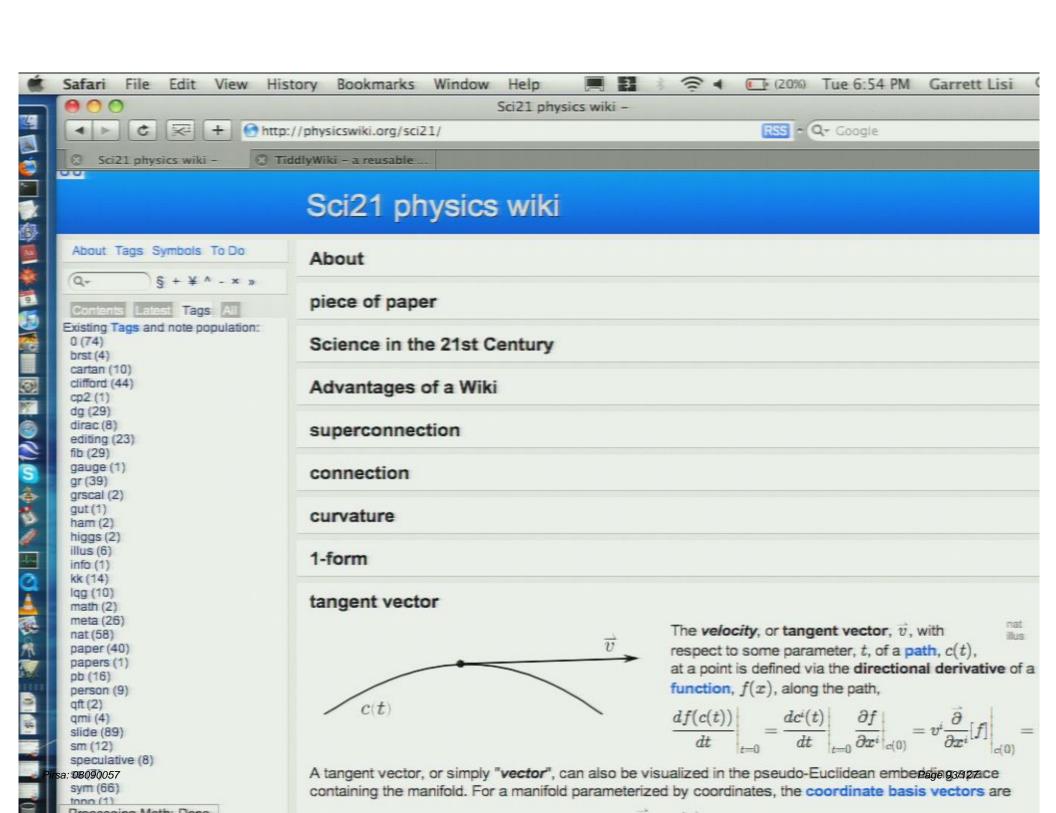
The curvature is perhaps the most important object characterizing the local geometry of a fiber bundle and connection. Its expression and action depends on the action of the structure group. Taking, for example, the structure group to act from the left, the curvature is then a local, Lie algebra (of the structure group) valued 2-form defined as

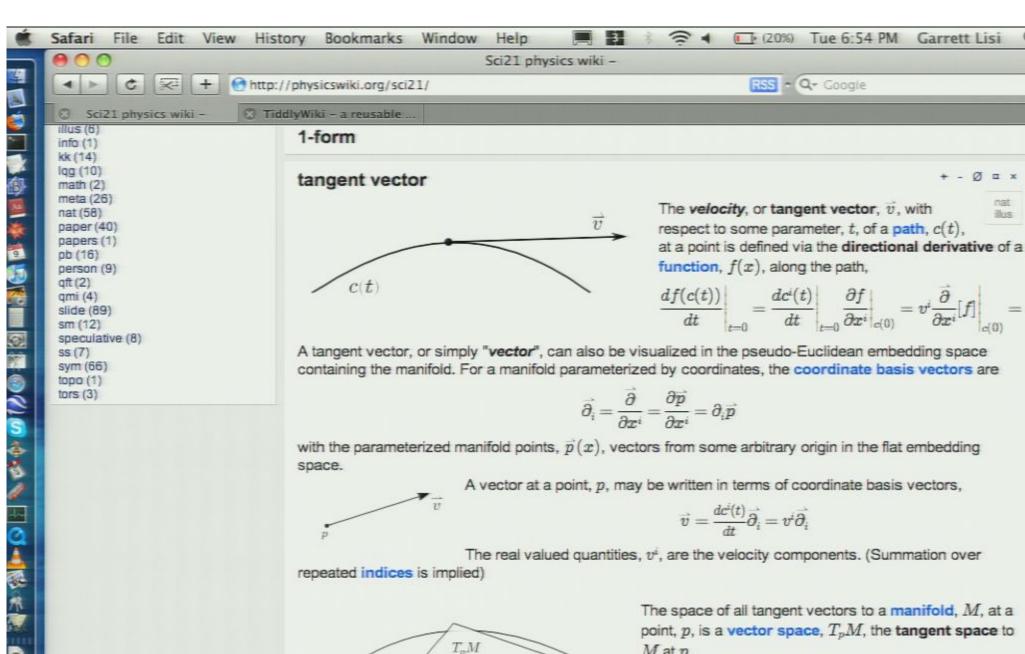
$$\underline{\underline{F}}(x) = rac{1}{2} d \underline{x}^i d \underline{x}^j F_{ij}^{B} T_B$$

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M

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The space of all tangent vectors to a manifold, M, at a point, p, is a vector space, T_pM , the tangent space to M at p.

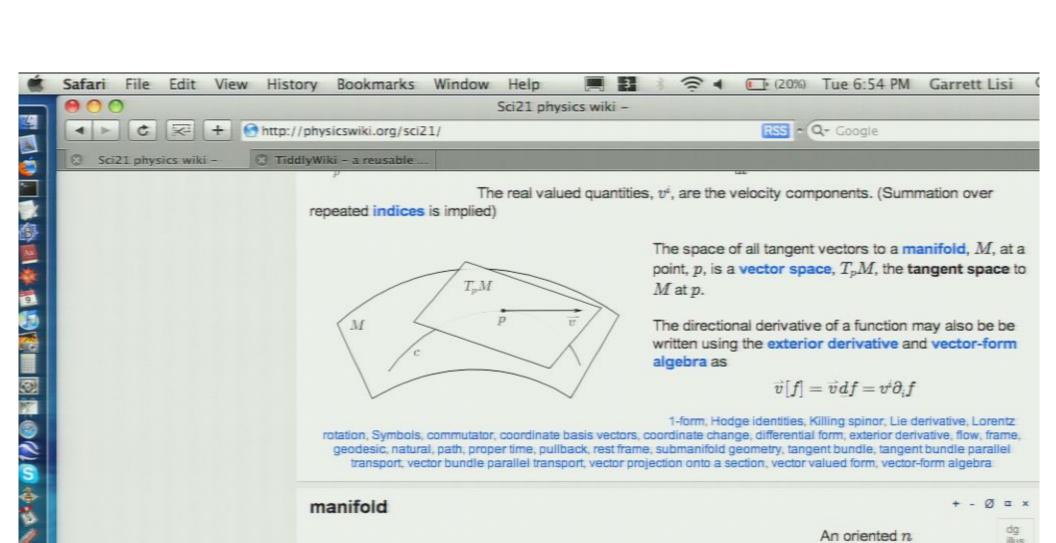
Garrett Lisi

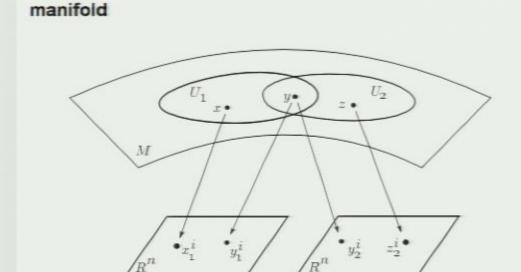
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illus

The directional derivative of a function may also be be written using the exterior derivative and vector-form algebra as Page 94/127

$$\vec{v}[f] = \vec{v}df = v^i \partial_i f$$





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Ø = x

An oriented n. dimensional

differentiable manifold, M. may be visualized as a curved

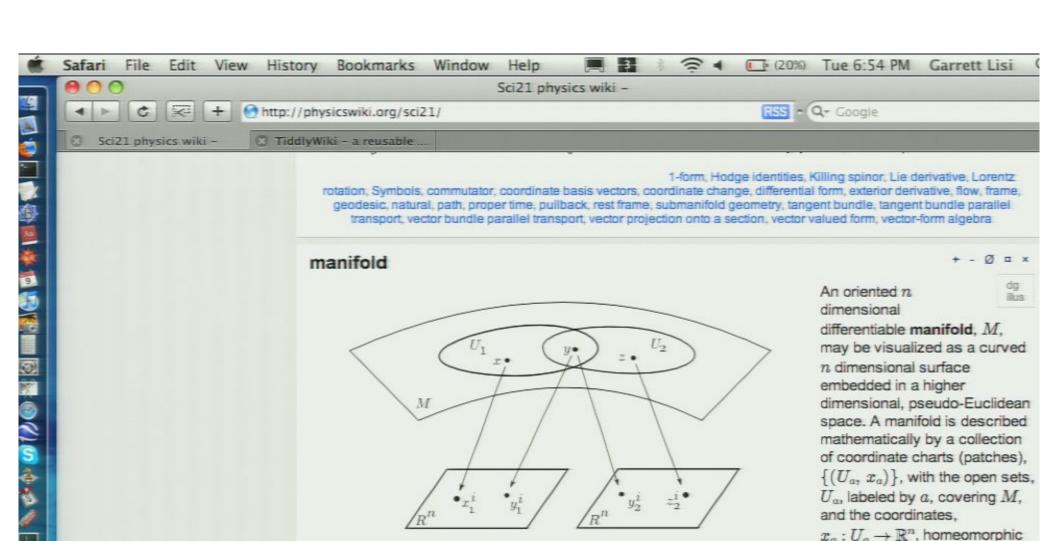
dimensional, pseudo-Euclidean space. A manifold is described mathematically by a collection of coordinate charts (patches), $\{(U_a, x_a)\}$, with the open sets, U_a , labeled by a, covering M.

 $x_a:U_a o \mathbb{R}^n$ Page 95/127 norphic maps into open subsets of \mathbb{R}^n

n dimensional surface embedded in a higher

and the coordinates.

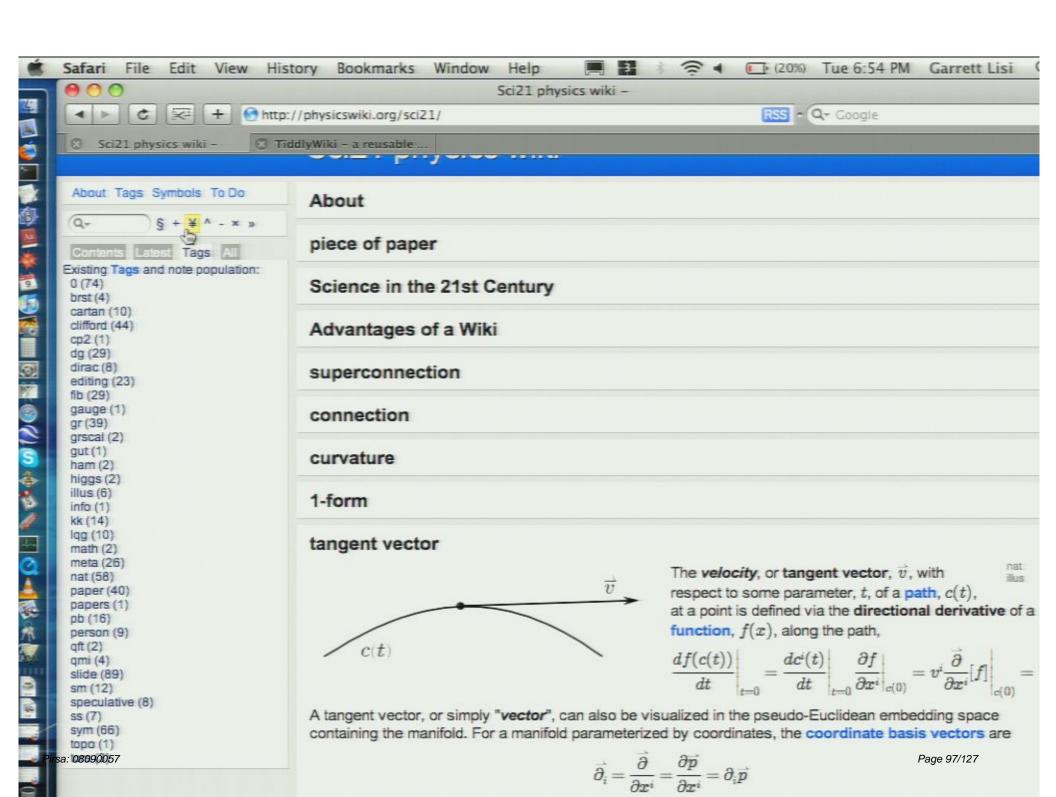
dg

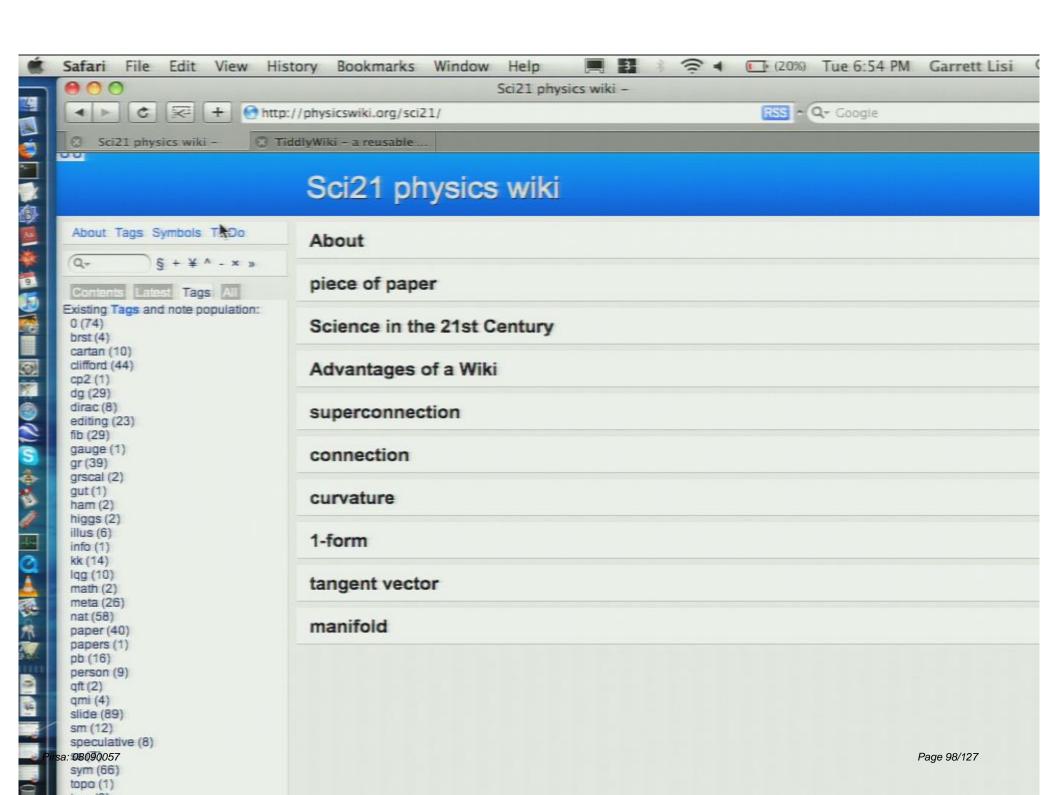


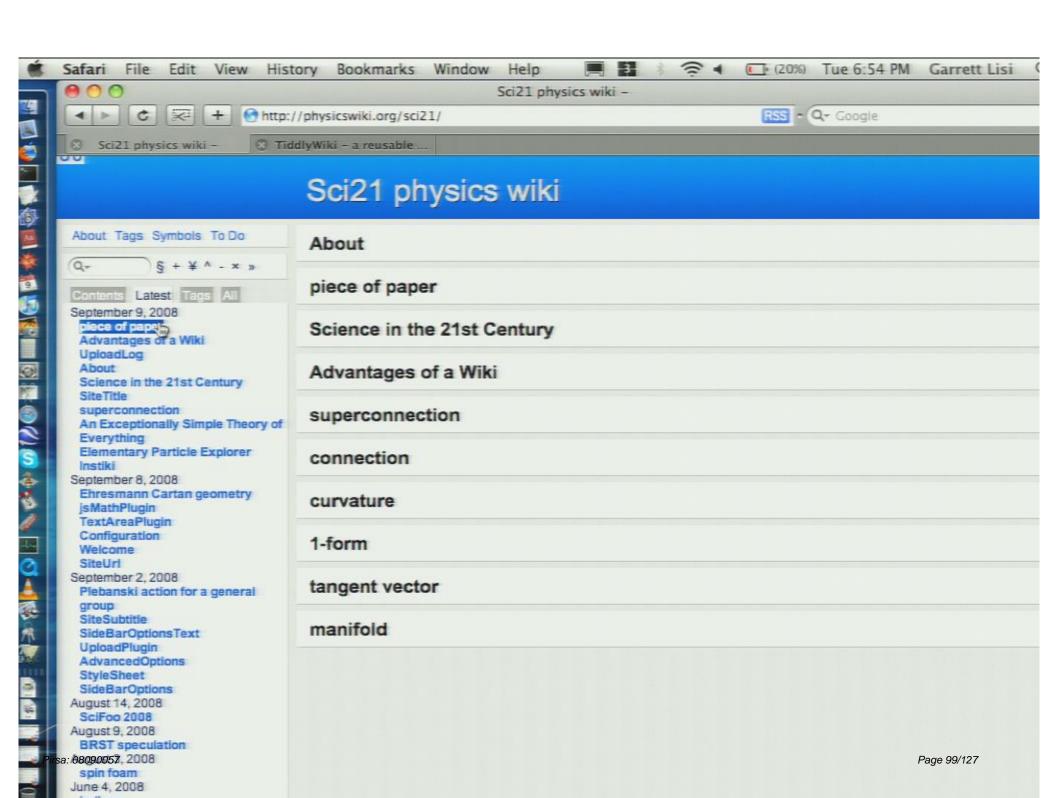
such that overlap maps, $x_a \circ x_b^- : \mathbb{R}^n \to M \to \mathbb{R}^n$, defined on $x_b(U_a \cap U_b)$, are infinitely differentiable. So, every point, x, on the manifold is labeled by a set of n real **coordinates**, $x_a^i(x)$, in some chart, U_a , with coordinate **indices**, i, typically running from 1 to n or from 0 to (n-1). In most practical cases the chart label, a, is not written and the coordinates are simply written as x^i with some chart implied.

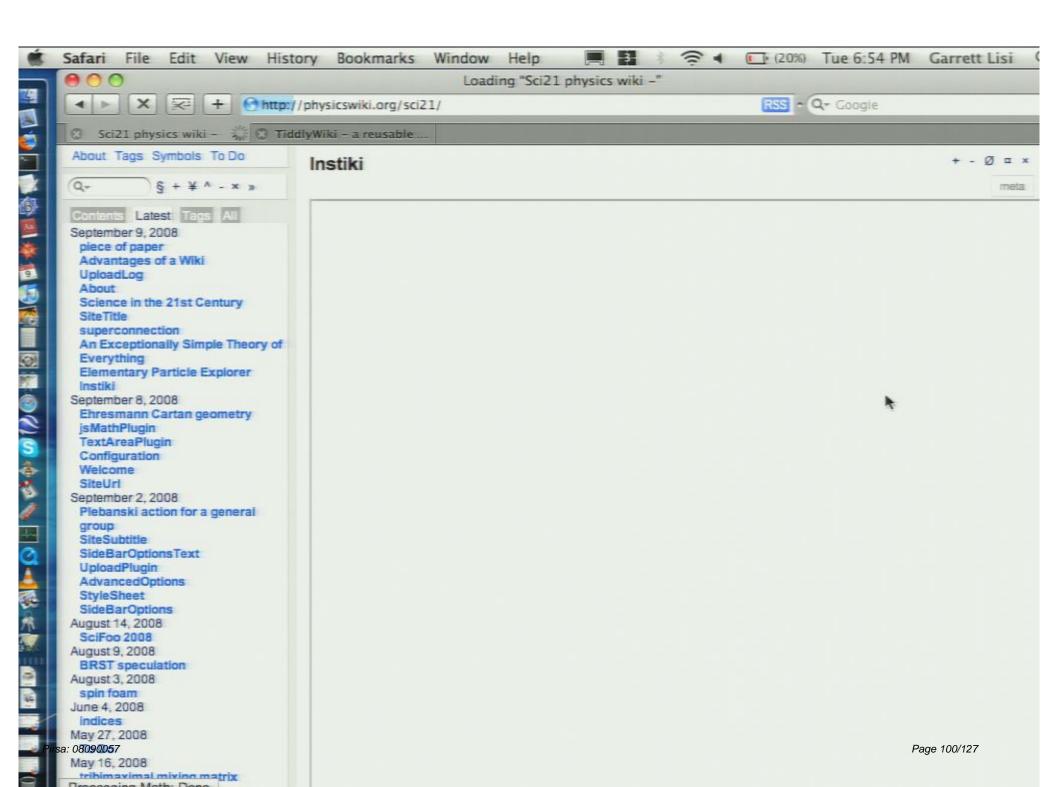
For more on manifolds, see http://en.wikipedia.org/wiki/Manifold

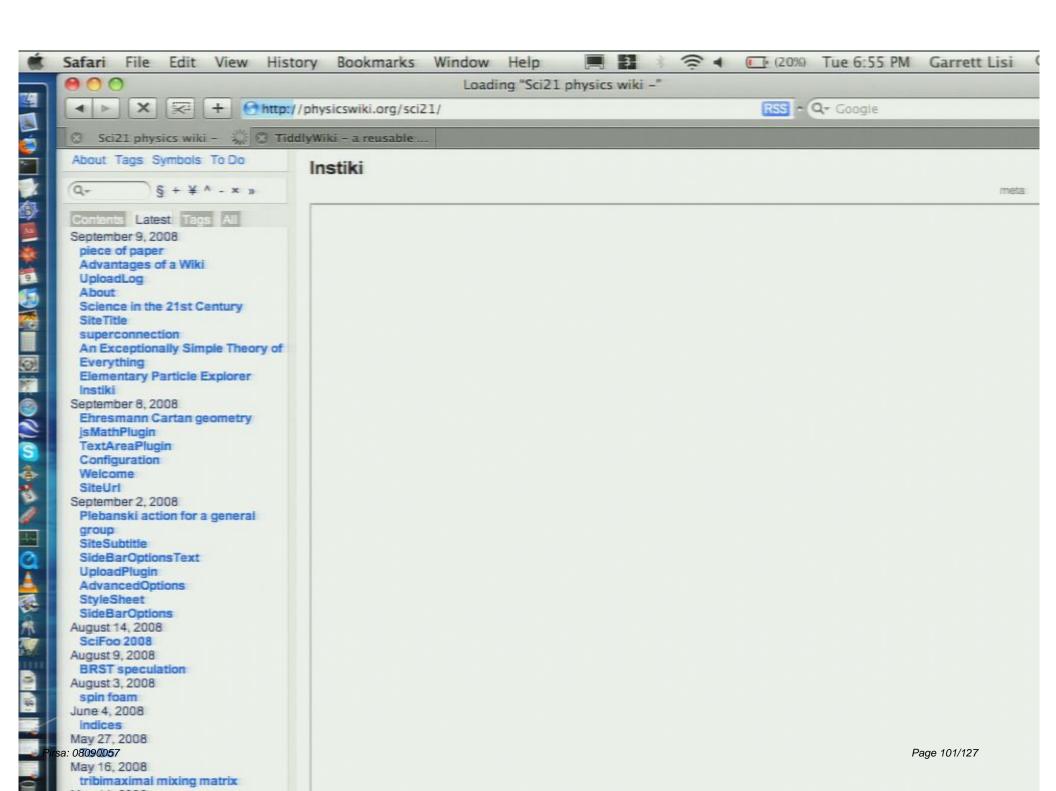
1-form, 2-sphere, 3-sphere, An Exceptionally Simple Theory of Everything, Chern-Simons form, Clifford bundle, Clifford vector bundle, Curvature of bosonic part, Discussion, Killing vector, Lie group, Lie group geometry, Symbols, This Week's Finds 253, almost complex structure, closed, cohomology, coordinate basis vectors, coordinate change, cotangent bundle, diffeomorphism, differential form, distribution, exact, fiber bundle, function, geodesic, homogeneous spacepage 96/127 atural, partial derivative, path, pullback, rest frame, spacetime, submanifold, submanifold geometry, tangent bundle, tangent vector, the big picture, vector space, vector valued form

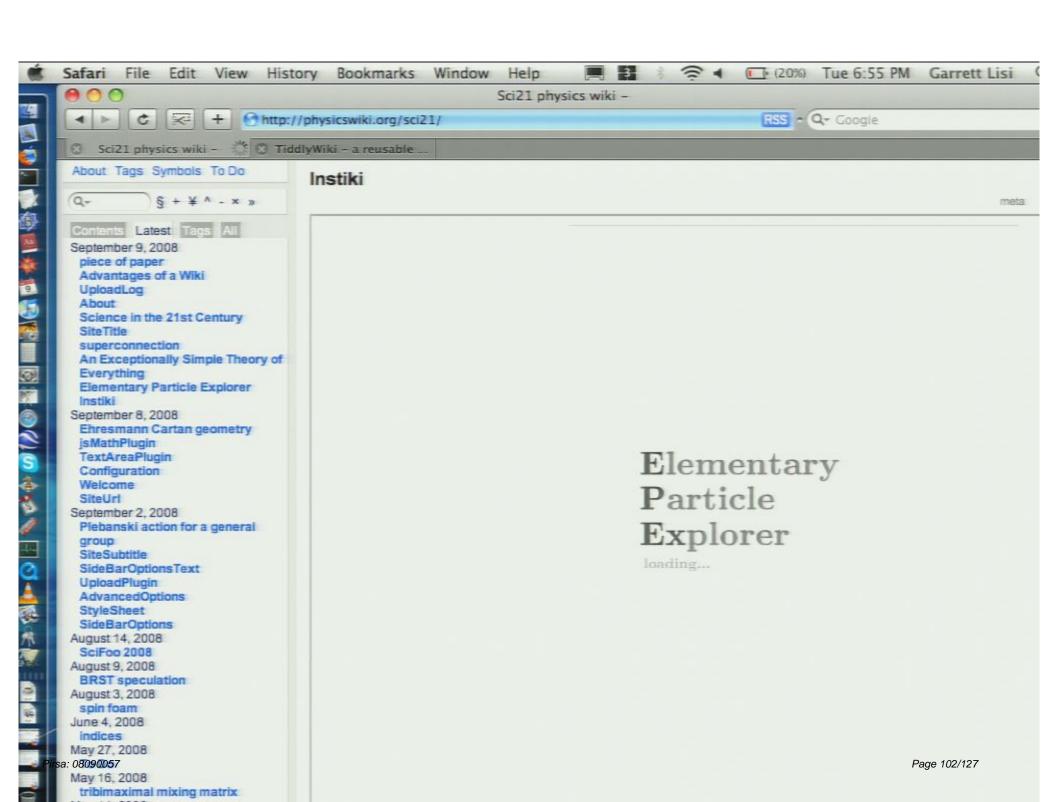


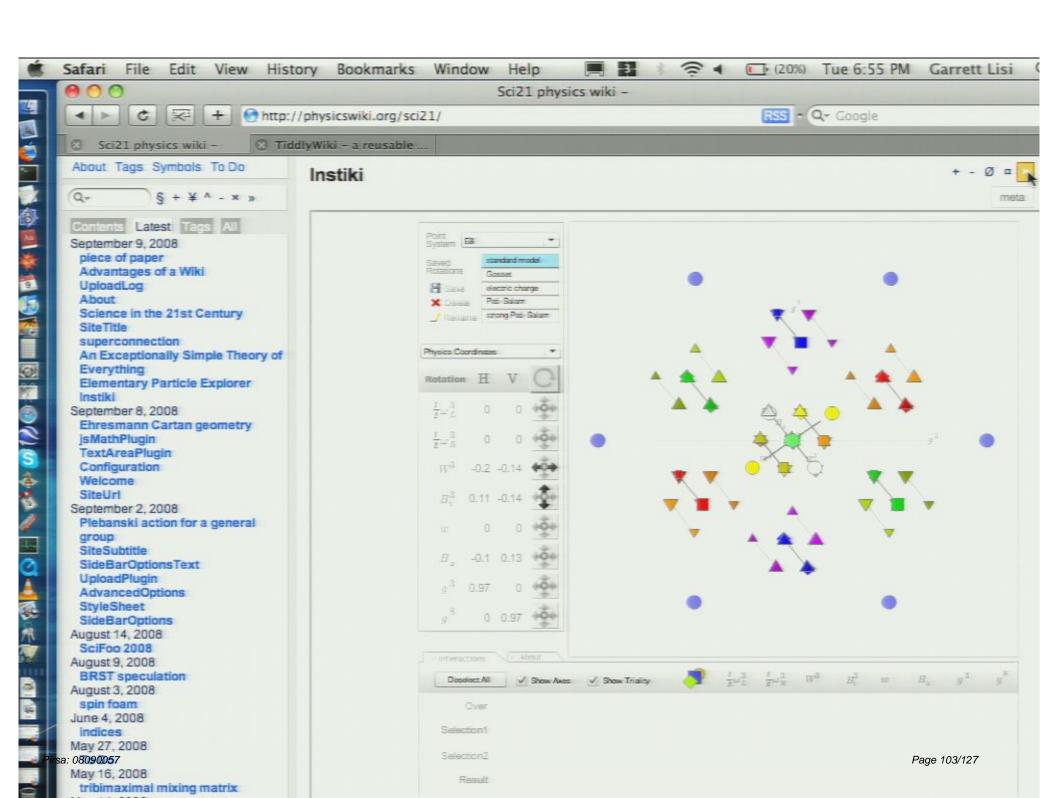


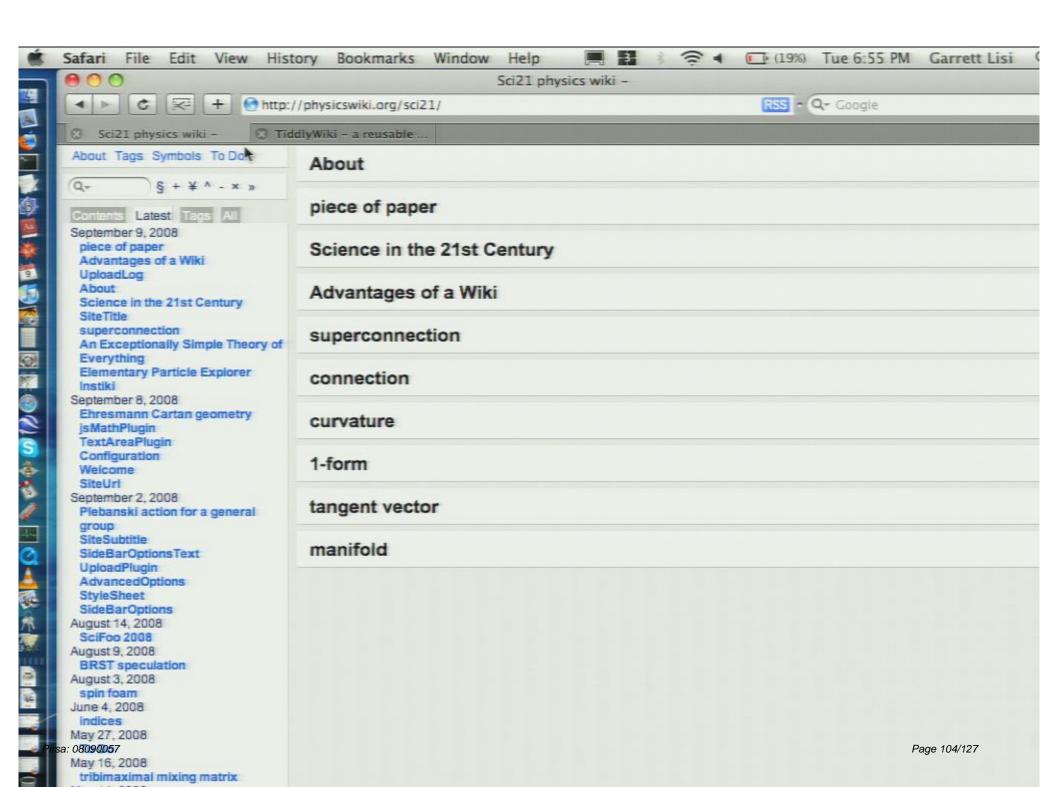


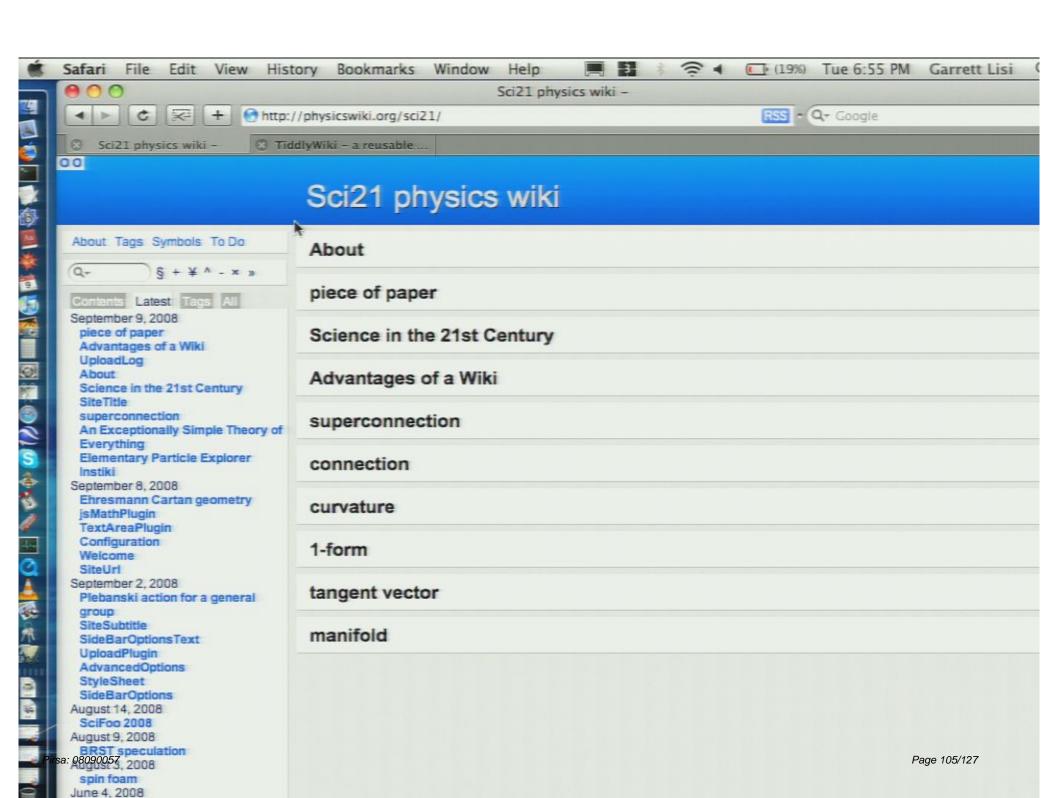


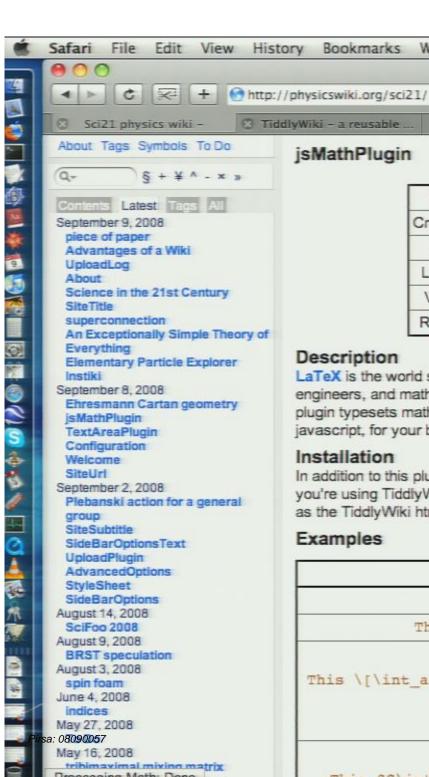












isMathPlugin

Bookmarks

Window Help

Name	Plugin: jsMath	
Created by	BobMcElrath (edited by Garrett)	
Email	my first name at my last name dot org	
Location	http://bob.mcelrath.org/tiddlyjsmath-2.0.3.html	
Version	1.3.g	
Requires	TiddlyWiki ≥ 2.1, jsMath ≥ 3.0	

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systemConfig editing plugin

(16%) Tue 6:57 PM Garrett Lisi

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Description

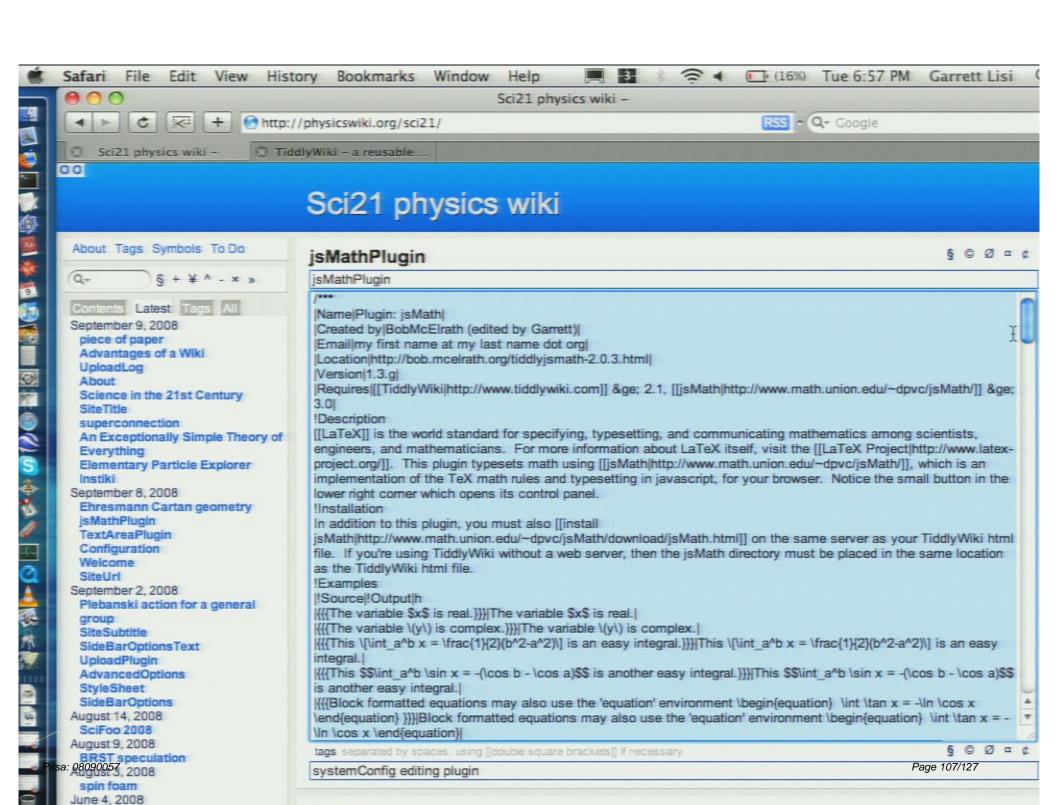
LaTeX is the world standard for specifying, typesetting, and communicating mathematics among scientists, engineers, and mathematicians. For more information about LaTeX itself, visit the LaTeX Project. This plugin typesets math using isMath, which is an implementation of the TeX math rules and typesetting in javascript, for your browser. Notice the small button in the lower right corner which opens its control panel.

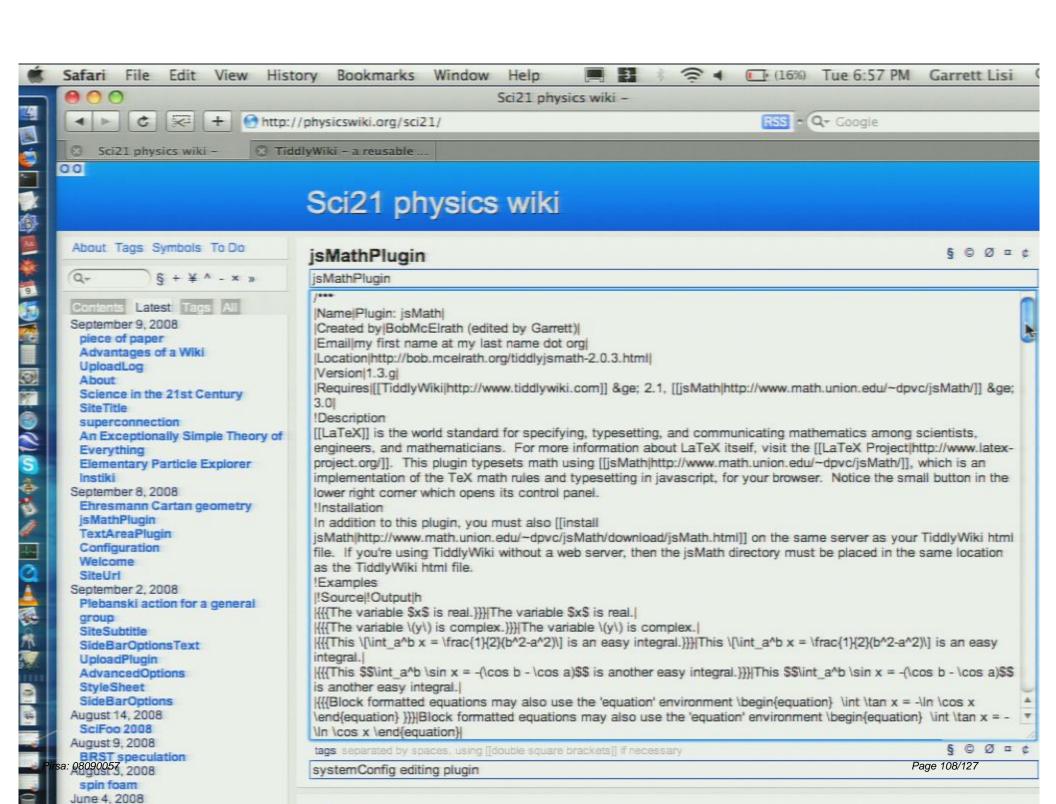
Installation

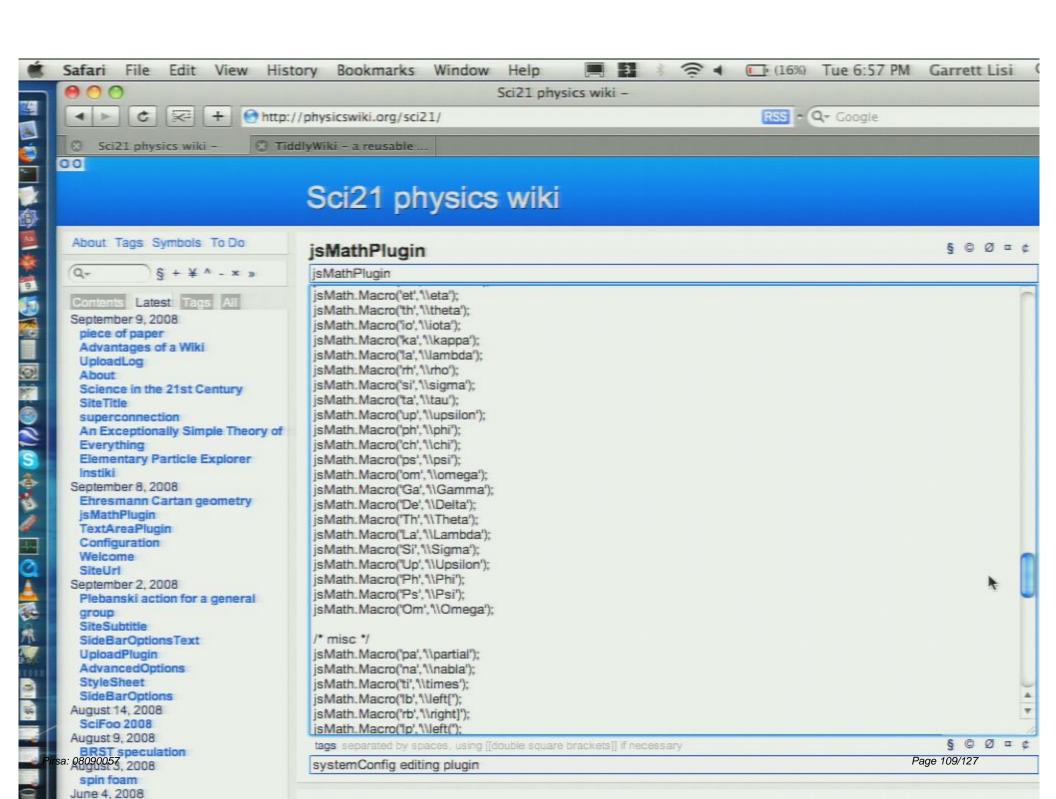
In addition to this plugin, you must also install is Math on the same server as your Tiddly Wiki html file. If you're using TiddlyWiki without a web server, then the jsMath directory must be placed in the same location as the TiddlyWiki html file.

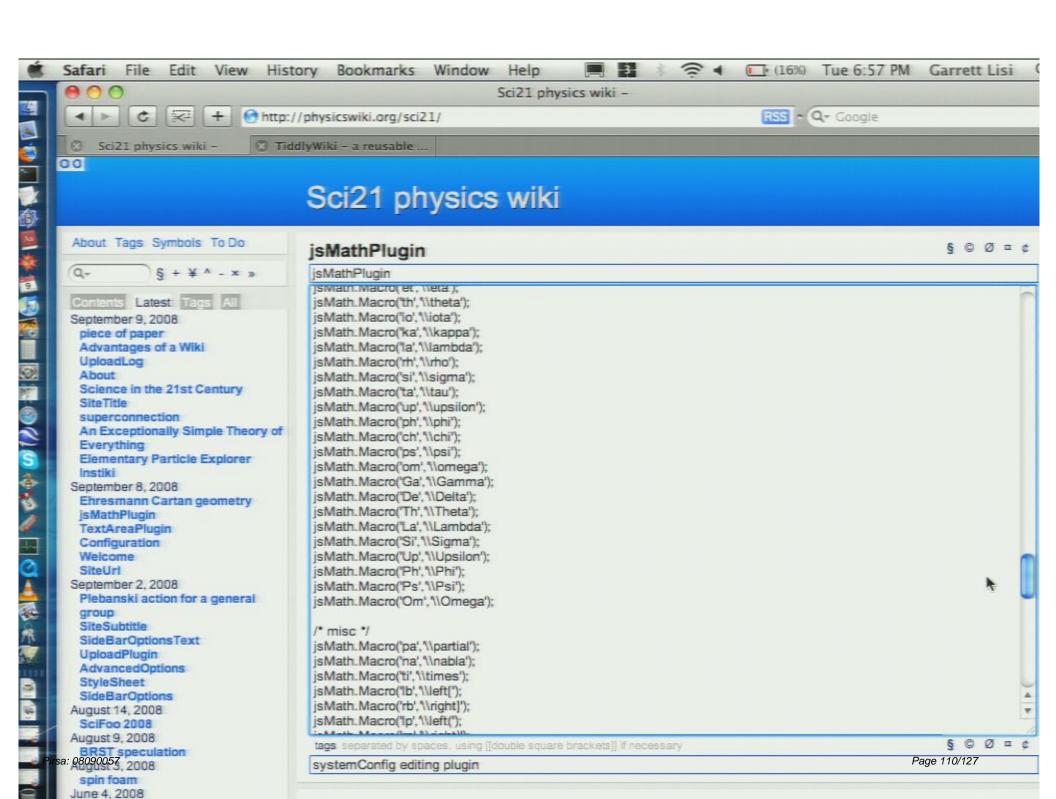
Examples

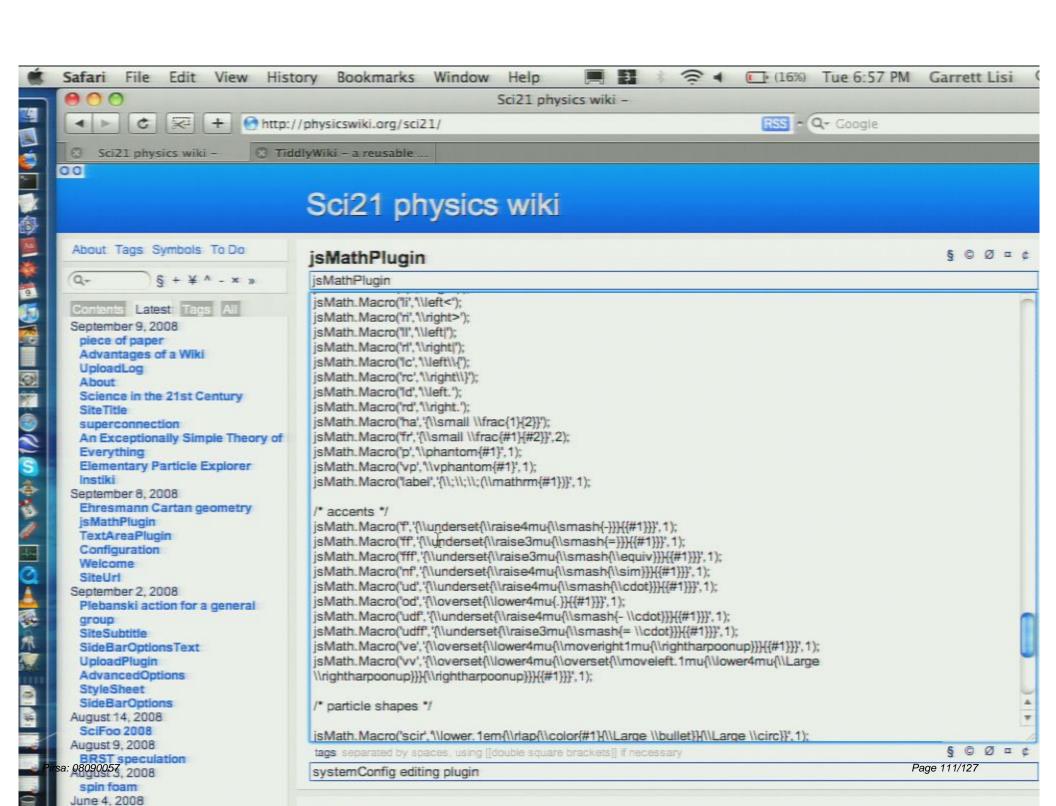
Source	Output
The variable \$x\$ is real.	The variable x is real.
The variable \(y\) is complex.	The variable y is complex.
This \[\int_a^b x = \frac{1}{2}(b^2-a^2)\] is an easy integral.	This $\int_a^b x = rac{1}{2}(b^2-a^2)$
	is an easy integral. Page 106/127 This

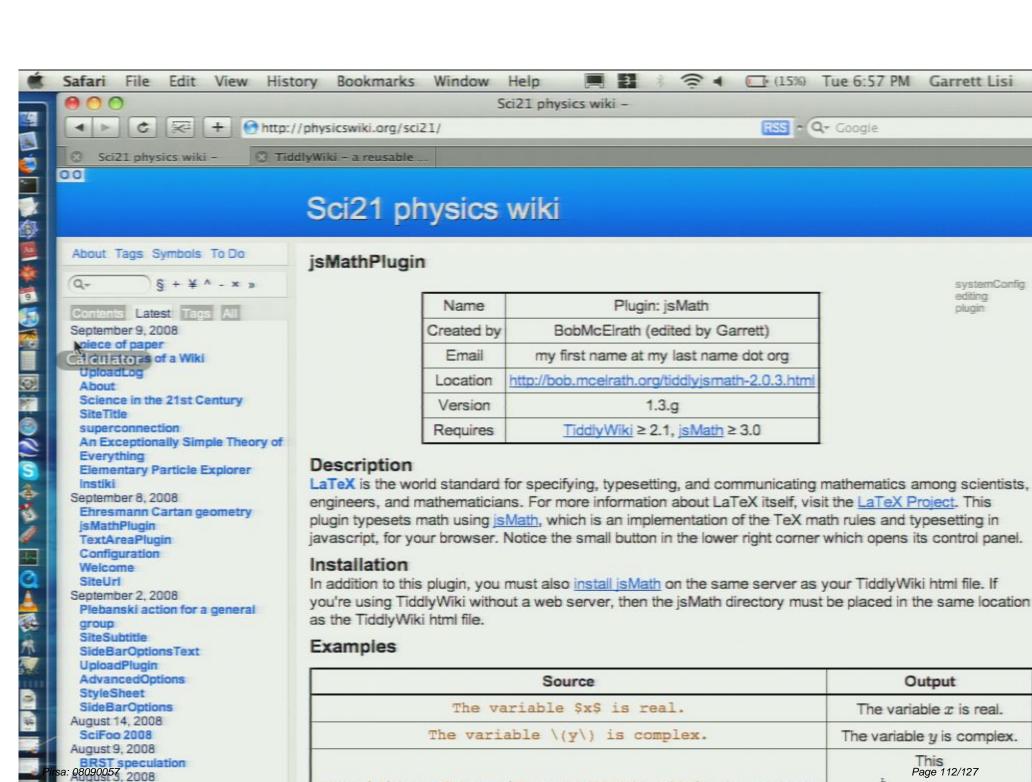












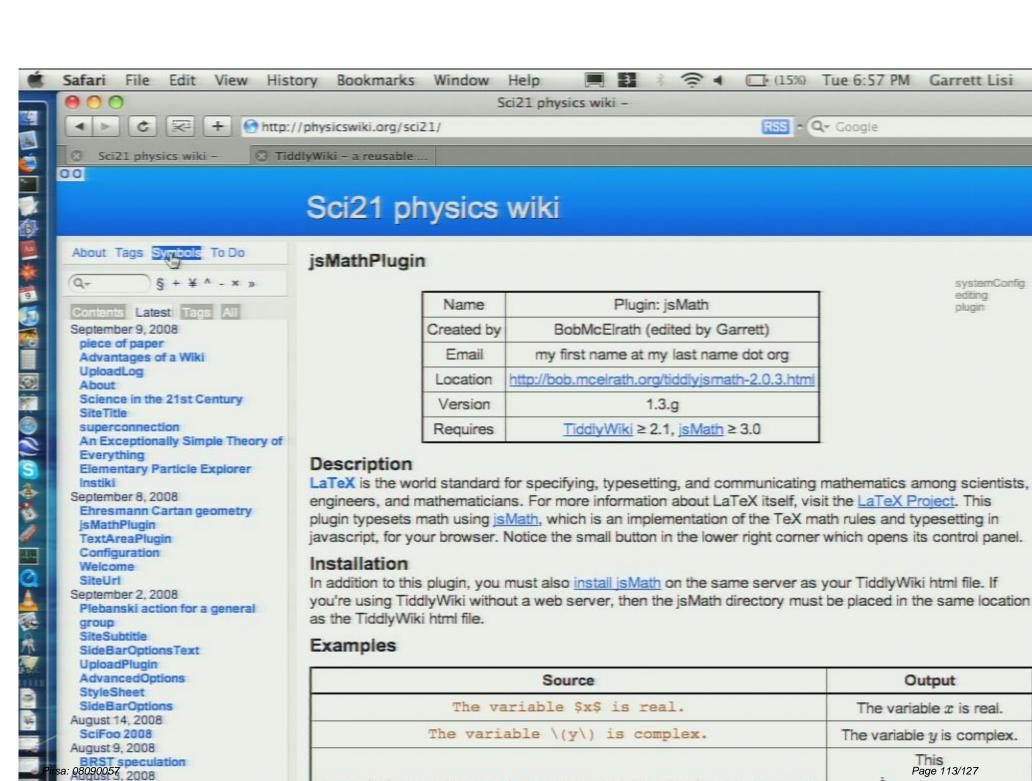
spin foam

This $\left(\int x = \frac{1}{2}(b^2-a^2) \right)$ is an easy

systemConfig

editing

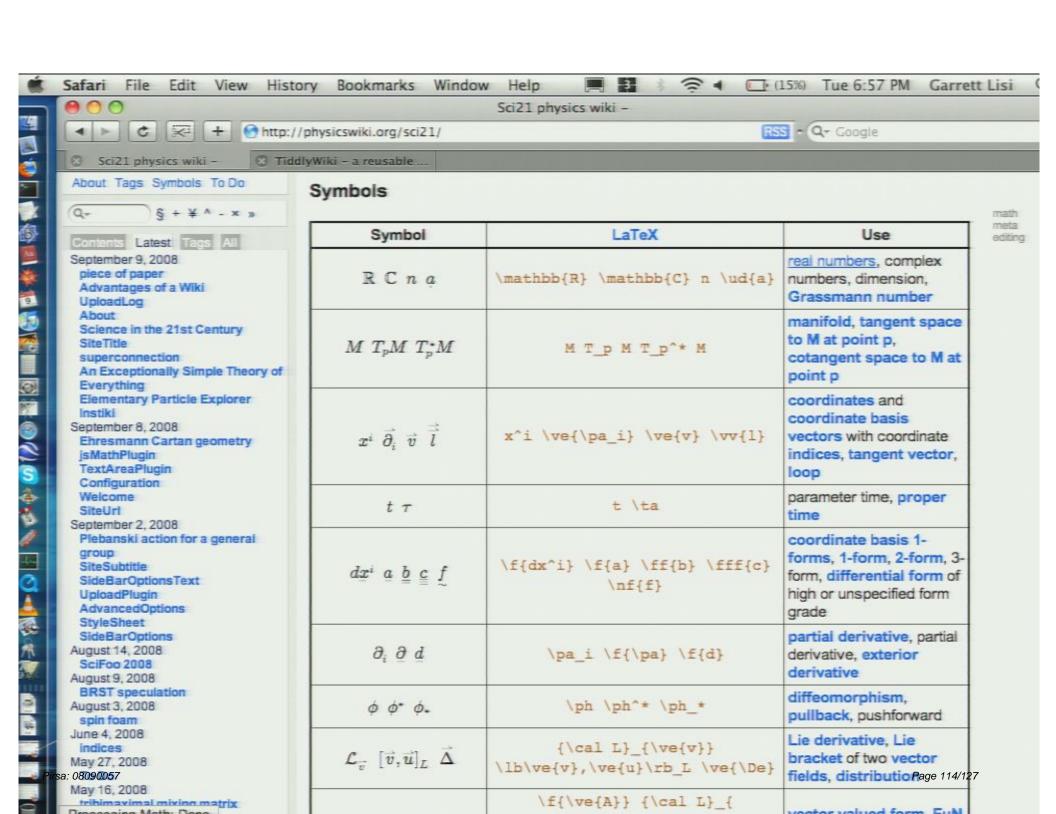
plugin

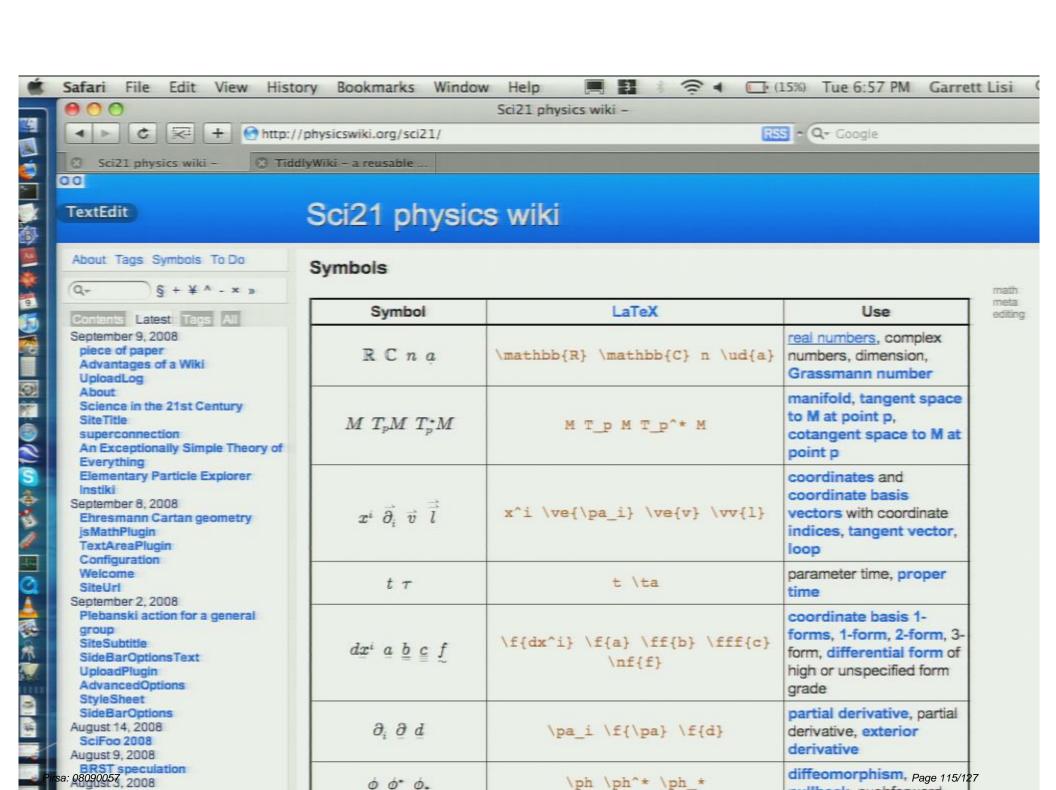


spin foam June 4, 2008 This $\left(\right) = \frac{1}{2}(b^2-a^2)$ is an easy

systemConfig editing

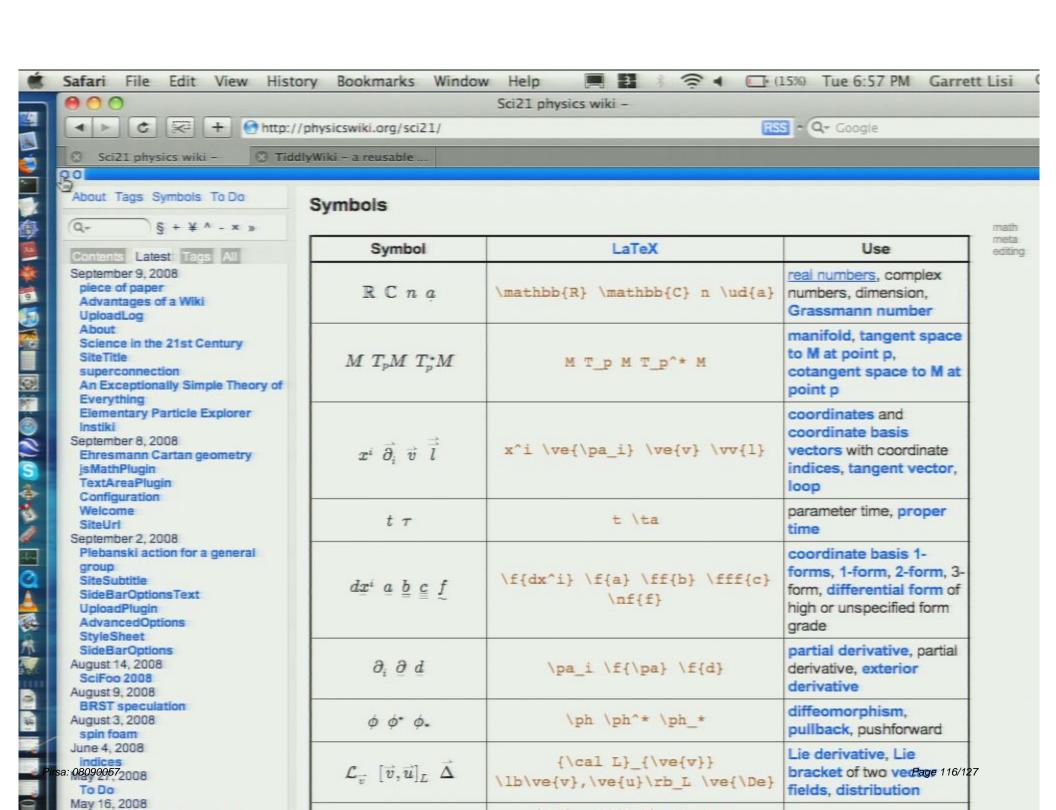
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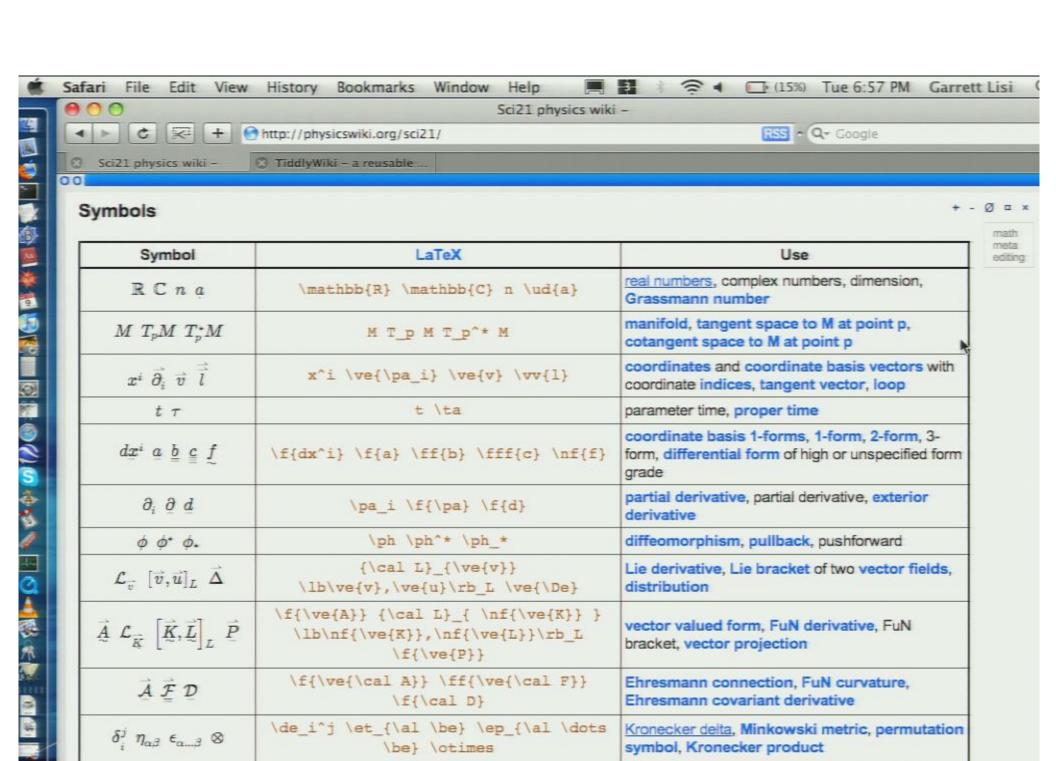




spin foam June 4, 2008 pullback, pushforward

the appropriate the



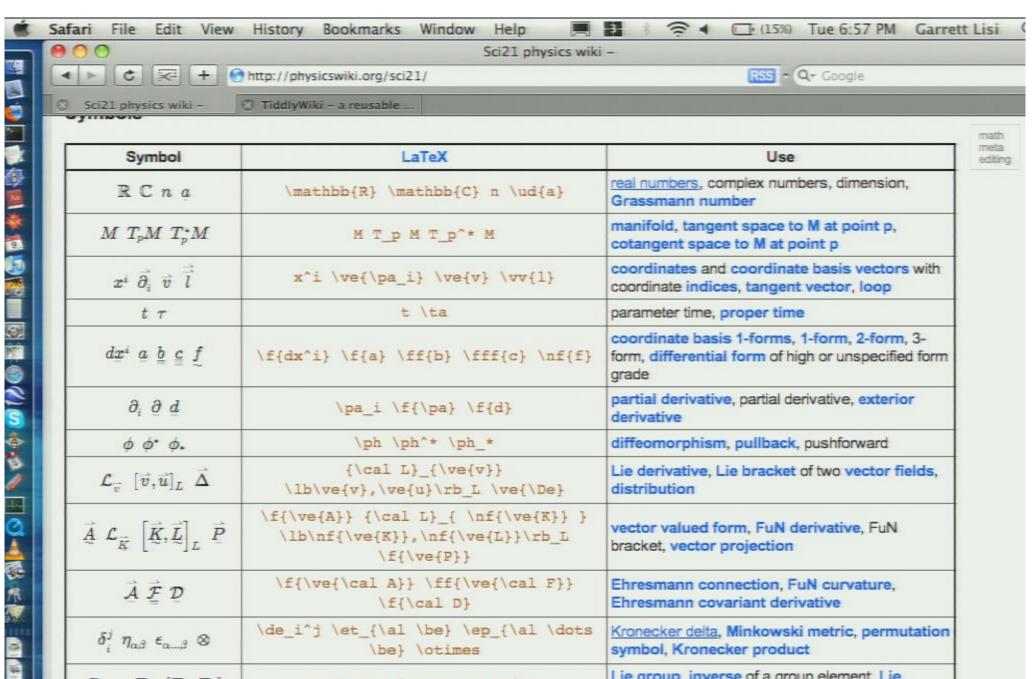


G q^- T A \lb{T A, T B}\rb

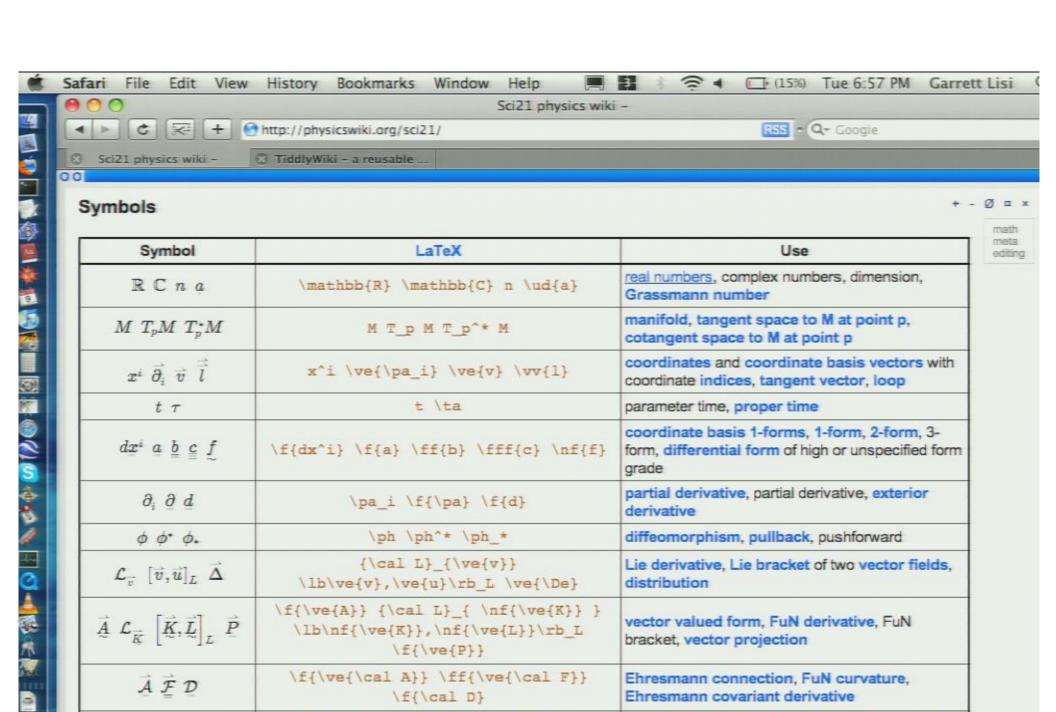
sa: 08090057 g = T_A $\left[T_A,T_B
ight]$

Lie group, inverse of a group element, Liepage 117/127

algebra generators, commutator bracket



Symbol	LaTeX	Use
R C n a	\mathbb{R} \mathbb{C} n \ud{a}	real numbers, complex numbers, dimension, Grassmann number
$M T_p M T_p^* M$	M T_p M T_p^* M	manifold, tangent space to M at point p, cotangent space to M at point p
$oldsymbol{x}^i \; \overrightarrow{oldsymbol{\partial}}_i \; \overrightarrow{v} \; \stackrel{ ightharpoonup}{\overrightarrow{l}}$	x^i \ve{\pa_i} \ve{v} \vv{1}	coordinates and coordinate basis vectors with coordinate indices, tangent vector, loop
tτ	t \ta	parameter time, proper time
$dx^i \ \underline{a} \ \underline{b} \ \underline{c} \ \underline{f}$	\f{dx^i} \f{a} \ff{b} \fff{c} \nf{f}	coordinate basis 1-forms, 1-form, 2-form, 3- form, differential form of high or unspecified form grade
$\partial_i \ \underline{\partial} \ \underline{d}$	\pa_i \f{\pa} \f{d}	partial derivative, partial derivative, exterior derivative
φ φ* φ.	\ph \ph^* \ph_*	diffeomorphism, pullback, pushforward
$\mathcal{L}_{\overrightarrow{v}} \ \ [\overrightarrow{v}, \overrightarrow{u}]_L \ \ \overrightarrow{\Delta}$	{\cal L}_{\ve{v}} \lb\ve{v},\ve{u}\rb_L \ve{\De}	Lie derivative, Lie bracket of two vector fields, distribution
$\vec{A} \ \mathcal{L}_{\vec{K}} \ \left[\vec{K}, \vec{L} \right]_L \ \vec{P}$	\f{\ve{A}} {\cal L}_{ \nf{\ve{K}}} } \lb\nf{\ve{K}},\nf{\ve{L}}\rb_L \f{\ve{P}}	vector valued form, FuN derivative, FuN bracket, vector projection
$\vec{\mathcal{A}} \not = \mathcal{D}$	\f{\ve{\cal A}} \ff{\ve{\cal F}} \f{\cal D}	Ehresmann connection, FuN curvature, Ehresmann covariant derivative
$\delta_i^j \; \eta_{lphaeta} \; \epsilon_{lphaeta} \; \otimes$	<pre>\de_i^j \et_{\al \be} \ep_{\al \dots \be} \otimes</pre>	Kronecker delta, Minkowski metric, permutation symbol, Kronecker product
G $g^ T_A$ $[T_A, T_B]$	G g^- T_A \lb{T_A,T_B}\rb	Lie group, inverse of a group element, Lie algebra generators, commutator bracket
: 08090057 $\ $	\f{\na} \f{A} \ff{F}	covariant derivative, connection, curvat@ge 118/12
	\f{\cal I} \f{\ve{\cal I}}	Maurer-Cartan form, Ehresmann-Maurer-Cartan



Kronecker delta, Minkowski metric, permutation

Lie group, inverse of a group element, Liepage 119/127

algebra generators, commutator bracket

symbol, Kronecker product

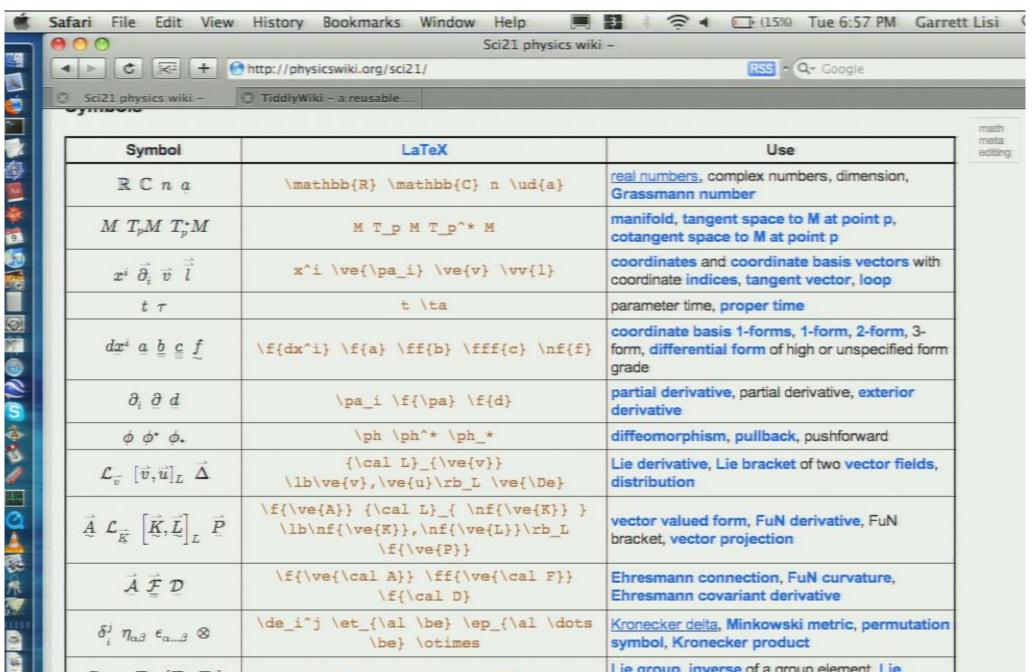
\de i^j \et {\al \be} \ep {\al \dots

\be} \otimes

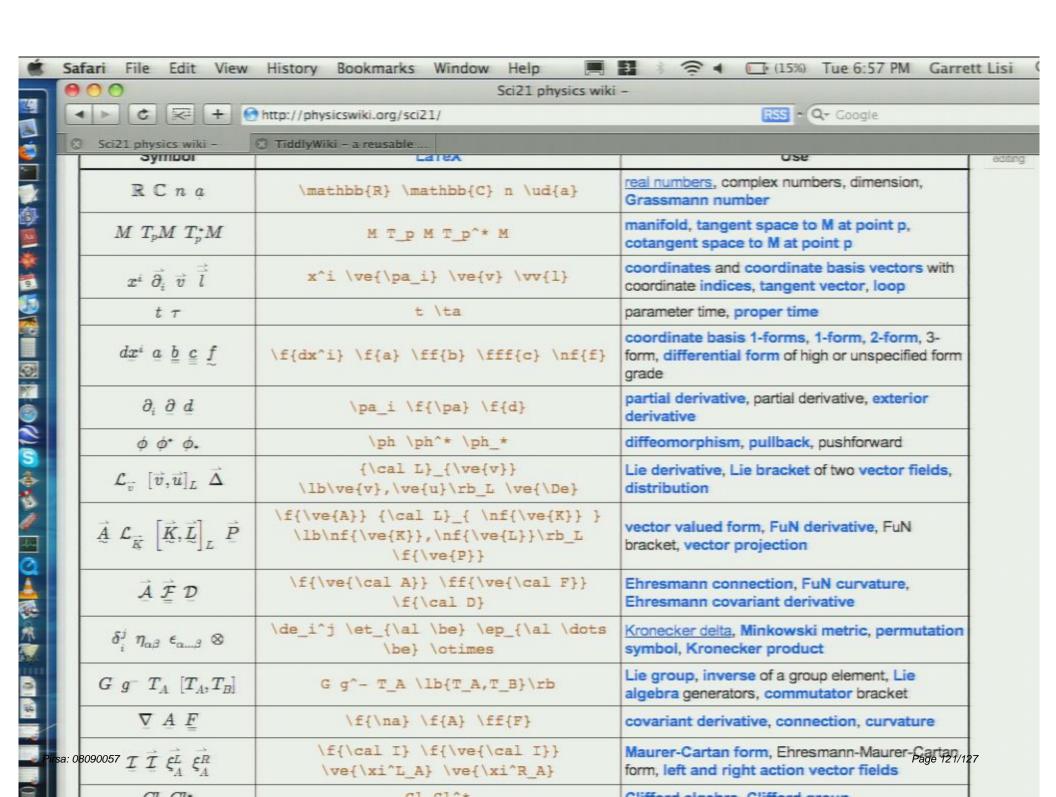
G q^- T A \lb{T A, T B}\rb

 $\delta^{j} \eta_{\alpha\beta} \epsilon_{\alpha\beta} \otimes$

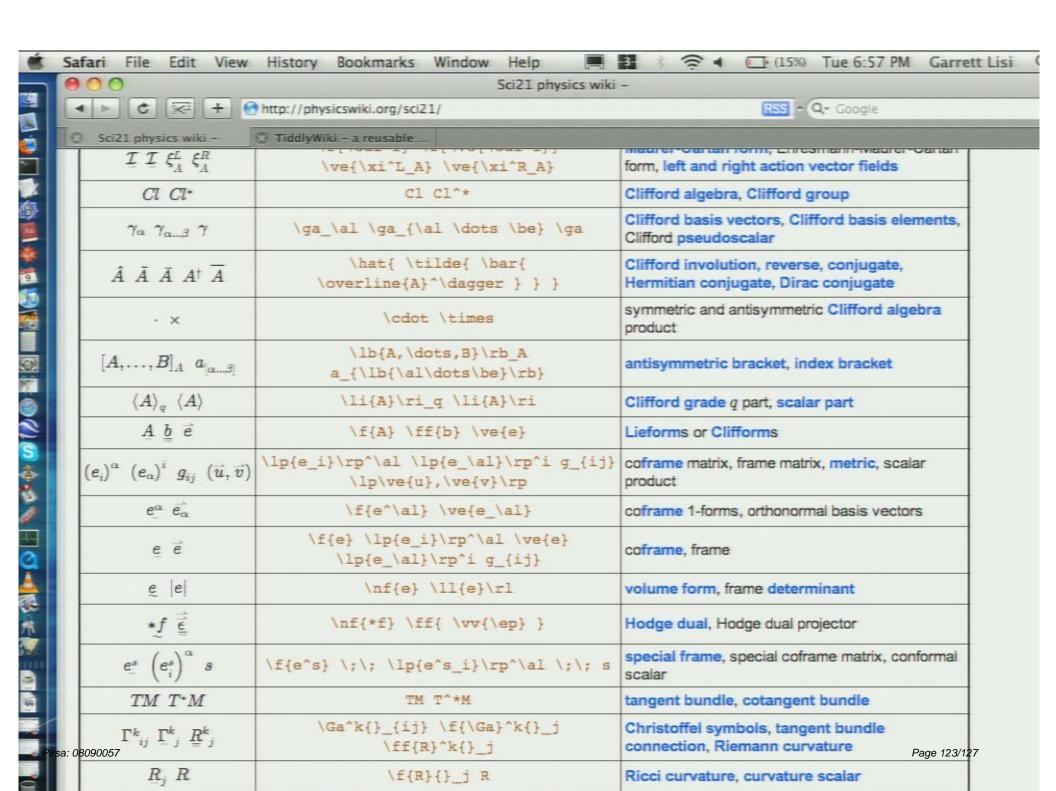
sa: 08090057 $g^ T_A$ $\left[T_A,T_B
ight]$



Symbol	LaTeX	Use
R C n a	\mathbb{R} \mathbb{C} n \ud{a}	real numbers, complex numbers, dimension, Grassmann number
$M T_p M T_p^* M$	M T_p M T_p^* M	manifold, tangent space to M at point p, cotangent space to M at point p
$x^i \; \overrightarrow{\partial_i} \; \overrightarrow{v} \; \overset{ ightharpoonup}{\overrightarrow{l}}$	x^i \ve{\pa_i} \ve{v} \vv{1}	coordinates and coordinate basis vectors with coordinate indices, tangent vector, loop
tτ	t \ta	parameter time, proper time
$dx^i \stackrel{a}{=} \stackrel{b}{=} \stackrel{c}{=} \stackrel{f}{=}$	\f{dx^i} \f{a} \fff{b} \fff{c} \nf{f}	coordinate basis 1-forms, 1-form, 2-form, 3- form, differential form of high or unspecified form grade
$\partial_i \ \underline{\partial} \ \underline{d}$	\pa_i \f{\pa} \f{d}	partial derivative, partial derivative, exterior derivative
φ φ* φ.	\ph \ph^* \ph_*	diffeomorphism, pullback, pushforward
$\mathcal{L}_{\overrightarrow{v}} \;\; [\overrightarrow{v}, \overrightarrow{u}]_L \;\; \overrightarrow{\Delta}$	{\cal L}_{\ve{v}} \lb\ve{v},\ve{u}\rb_L \ve{\De}	Lie derivative, Lie bracket of two vector fields, distribution
$\vec{A} \; \mathcal{L}_{\vec{K}} \; \left[\vec{K}, \vec{L} \right]_L \; \vec{P}$	\f{\ve{A}} {\cal L}_{ \nf{\ve{K}}} } \lb\nf{\ve{K}},\nf{\ve{L}}\rb_L \f{\ve{P}}	vector valued form, FuN derivative, FuN bracket, vector projection
À Ē D	\f{\ve{\cal A}} \ff{\ve{\cal F}} \f{\cal D}	Ehresmann connection, FuN curvature, Ehresmann covariant derivative
$\delta_i^j \; \eta_{lphaeta} \; \epsilon_{lphaeta} \; \otimes$	<pre>\de_i^j \et_{\al \be} \ep_{\al \dots \be} \otimes</pre>	Kronecker delta, Minkowski metric, permutation symbol, Kronecker product
G $g^ T_A$ $[T_A, T_B]$	G g^- T_A \lb{T_A,T_B}\rb	Lie group, inverse of a group element, Lie algebra generators, commutator bracket
8090057 ∇ A F	\f{\na} \f{A} \ff{F}	covariant derivative, connection, curvat@ge 120/1.
	\f{\cal I} \f{\ve{\cal I}}	Maurer-Cartan form, Ehresmann-Maurer-Cartan



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4	· C ₹ + 0	http://physicswiki.org/sci21/	RSS - Q- Google
3	Sci21 physics wiki –	☑ TiddlyWiki - a reusable (I (UX I) (I (U) (III (U) (III (U) (III (I)	grade
	$\partial_i \ \partial \ \underline{d}$	\pa_i \f{\pa} \f{d}	partial derivative, partial derivative, exterior derivative
	φ φ* φ.	\ph \ph^* \ph_*	diffeomorphism, pullback, pushforward
	$\mathcal{L}_{ec{v}} \ \ [ec{v},ec{u}]_L \ \ ec{\Delta}$	{\cal L}_{\ve{v}} \lb\ve{v},\ve{u}\rb_L \ve{\De}	Lie derivative, Lie bracket of two vector fields, distribution
	$\vec{A} \ \mathcal{L}_{\vec{K}} \ \left[\vec{K}, \vec{L} \right]_L \ \vec{P}$	\f{\ve{A}} {\cal L}_{ \nf{\ve{K}}} } \lb\nf{\ve{K}},\nf{\ve{L}}\rb_L \f{\ve{P}}}	vector valued form, FuN derivative, FuN bracket, vector projection
	$\vec{\mathcal{A}} \ \vec{\underline{\mathcal{F}}} \ \mathcal{D}$	\f{\ve{\cal A}} \ff{\ve{\cal F}} \f{\cal D}	Ehresmann connection, FuN curvature, Ehresmann covariant derivative
	$\delta_i^j \; \eta_{\alpha\beta} \; \epsilon_{\alpha\beta} \; \otimes$	<pre>\de_i^j \et_{\al \be} \ep_{\al \dots \be} \otimes</pre>	Kronecker delta, Minkowski metric, permutation symbol, Kronecker product
	$G \ g^- \ T_A \ [T_A, T_B]$	G g^- T_A \lb{T_A,T_B}\rb	Lie group, inverse of a group element, Lie algebra generators, commutator bracket
	$\nabla A E$	\f{\na} \f{A} \ff{F}	covariant derivative, connection, curvature
	$\mathcal{I} \stackrel{ ightarrow}{\mathcal{I}} \stackrel{ ightarrow}{ec{\xi}_A^L} \stackrel{ ightarrow}{ec{\xi}_A^R}$	\f{\cal I} \f{\ve{\cal I}} \ve{\xi^L_A} \ve{\xi^R_A}	Maurer-Cartan form, Ehresmann-Maurer-Cartan form, left and right action vector fields
	Cl Cl-	Cl Cl^*	Clifford algebra, Clifford group
	γα γαβ γ	\ga_\al \ga_{\al \dots \be} \ga	Clifford basis vectors, Clifford basis elements, Clifford pseudoscalar
	\hat{A} \bar{A} \bar{A} A^{\dagger} \bar{A}	<pre>\hat{ \tilde{ \bar{ \overline{A}^\dagger } } }</pre>	Clifford involution, reverse, conjugate, Hermitian conjugate, Dirac conjugate
	· ×	\cdot \times	symmetric and antisymmetric Clifford algebra product
08	$[a_090057,\ldots,B]_A$ $a_{[lphaeta]}$	<pre>\lb{A,\dots,B}\rb_A a_{\lb{\al\dots\be}\rb}</pre>	antisymmetric bracket, index bracket Page 122/12



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(e_i) (e_a) g_{ij} (u,v)	\lp\ve{u},\ve{v}\rp	product
e^{α}_{-} e^{\rightarrow}_{α}	\f{e^\al} \ve{e_\al}	coframe 1-forms, orthonormal basis vectors
e è	<pre>\f{e} \lp{e_i}\rp^\al \ve{e} \lp{e_\al}\rp^i g_{ij}</pre>	coframe, frame
€ e	\nf{e} \ll{e}\rl	volume form, frame determinant
* <u>f</u>	\nf{*f} \ff{ \vv{\ep} }	Hodge dual, Hodge dual projector
$e^s \left(e^s_i\right)^\alpha s$	\f{e^s} \;\; \lp{e^s_i}\rp^\al \;\; s	special frame, special coframe matrix, conformal scalar
TM T⁺M	TM T^*M	tangent bundle, cotangent bundle
Γ^k_{ij} Γ^k_{j} R^k_{j}	\Ga^k{}_{ij} \f{\Ga}^k{}_j \ff{R}^k{}_j	Christoffel symbols, tangent bundle connection, Riemann curvature
R_j R	\f{R}{}_j R	Ricci curvature, curvature scalar
L^{eta}_{lpha}	<pre>L^_\al \f{w}^_\al \ff{F}^_\al</pre>	Lorentz rotation, tangent bundle spin connection, Riemann curvature
CIM Cl ¹ M	ClM Cl^1M	Clifford bundle, Clifford vector bundle
AωR	\f{A} \f{\om} \ff{R}	Clifford connection, spin connection, Clifford- Riemann curvature
R R	\f{R} R	Clifford-Ricci curvature, Clifford curvature scalar
Ţκ	\ff{T} \f{\ka}	torsion, contorsion
$C \not B \not A \not E$	$\ud{C} \inf{\od{B}} \udf{A} \udff{F}$	BRST ghost, anti-ghost, extended connection, extended curvature

