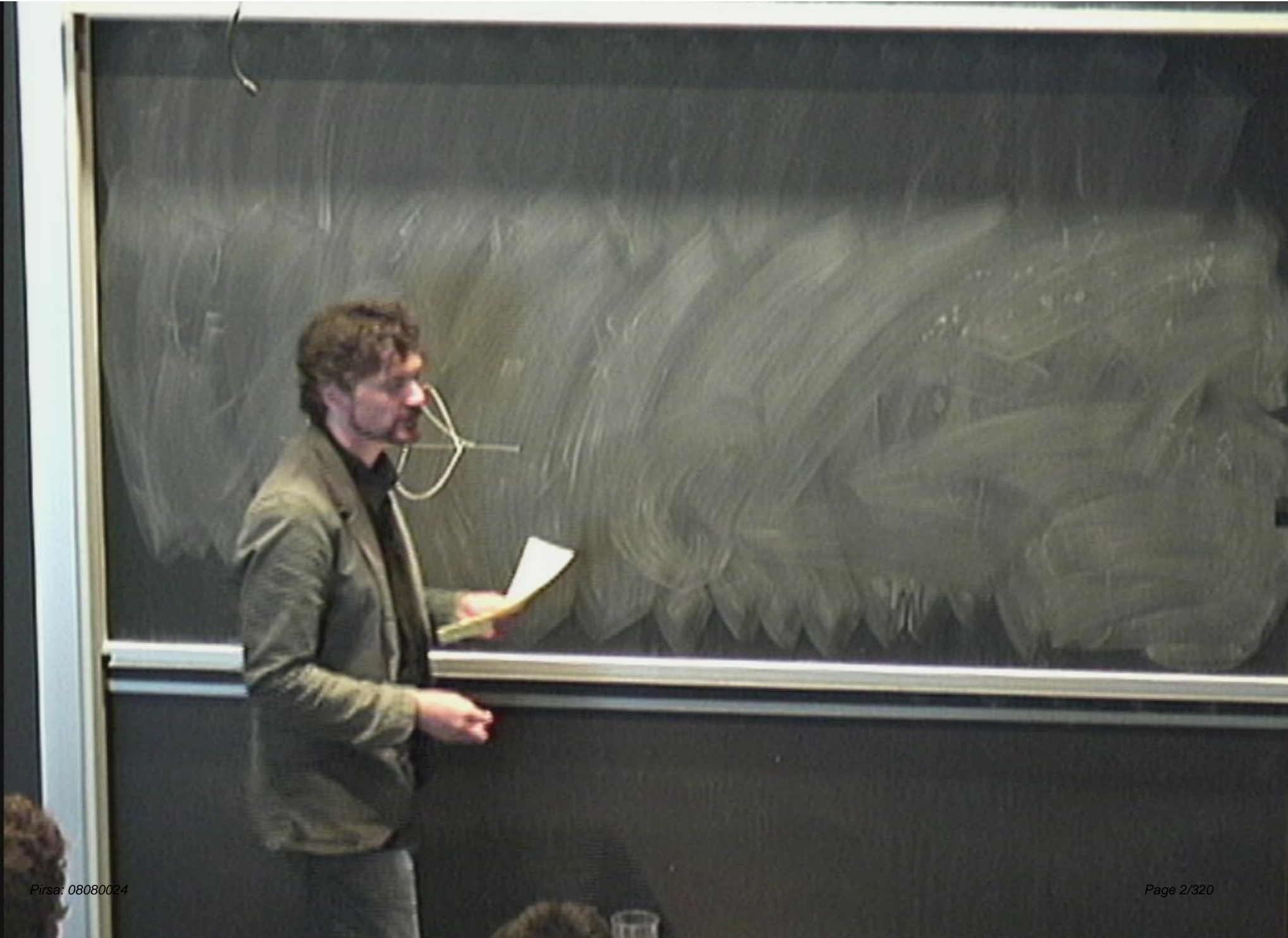


Title: Quantum 6

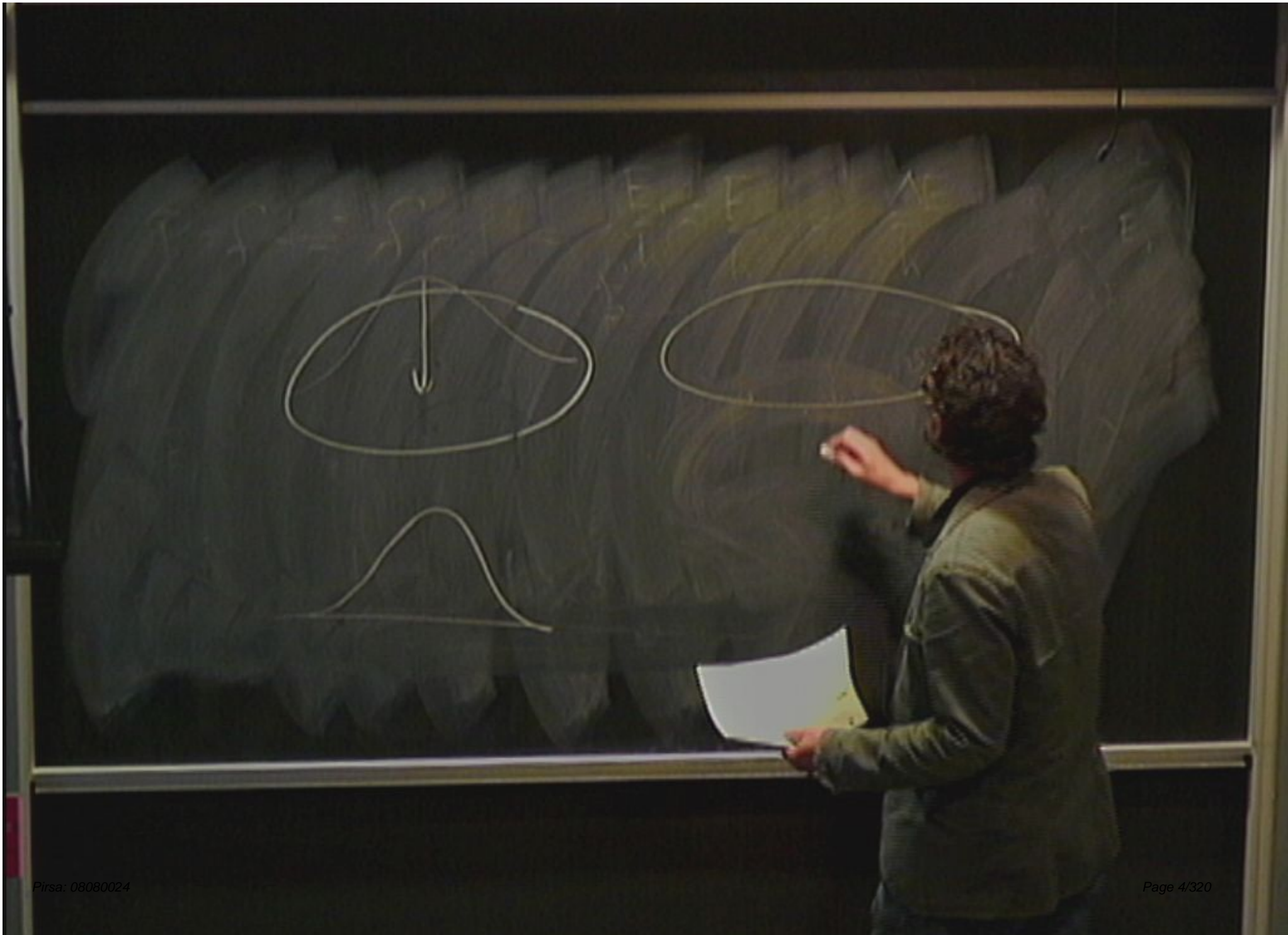
Date: Aug 16, 2008 03:30 PM

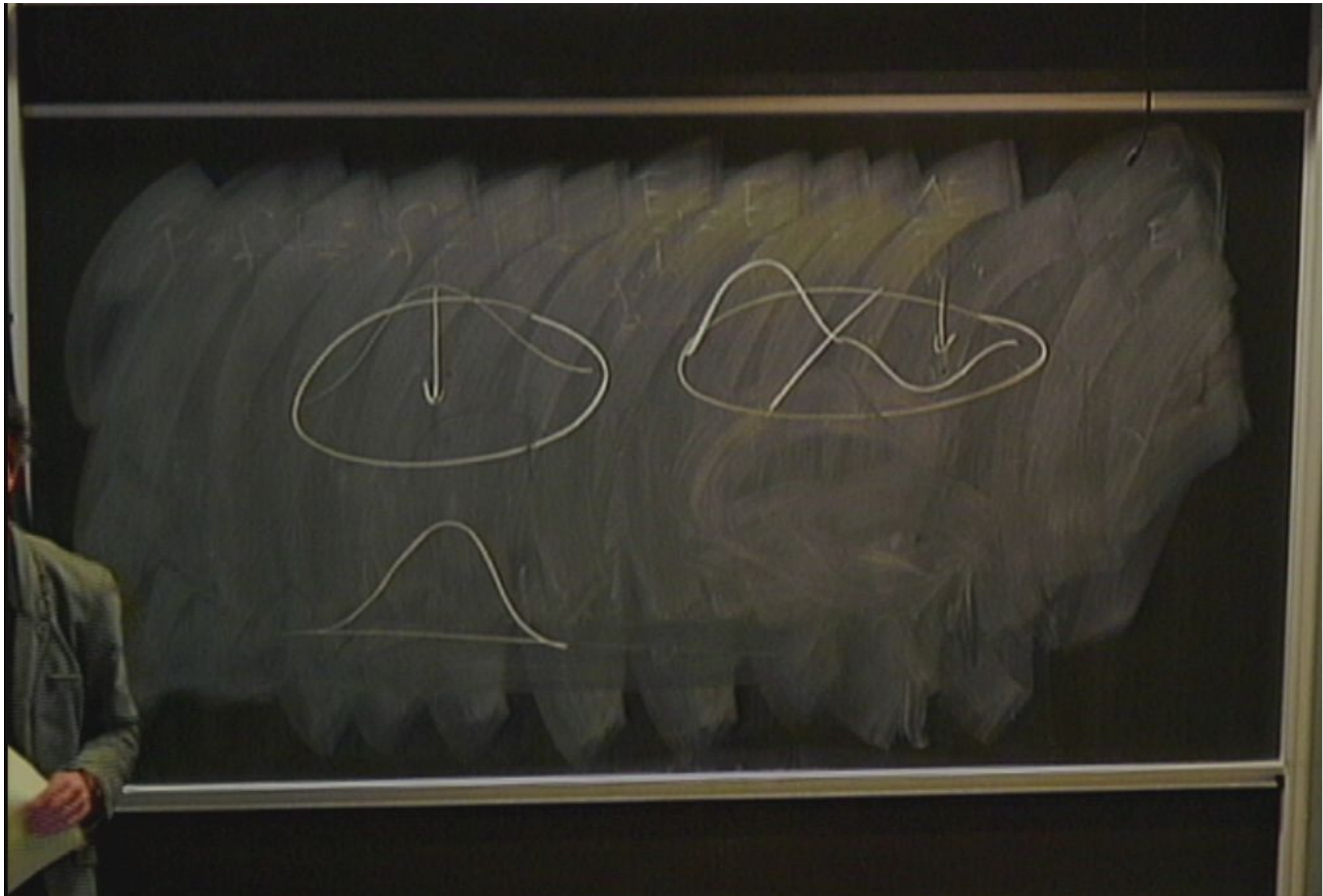
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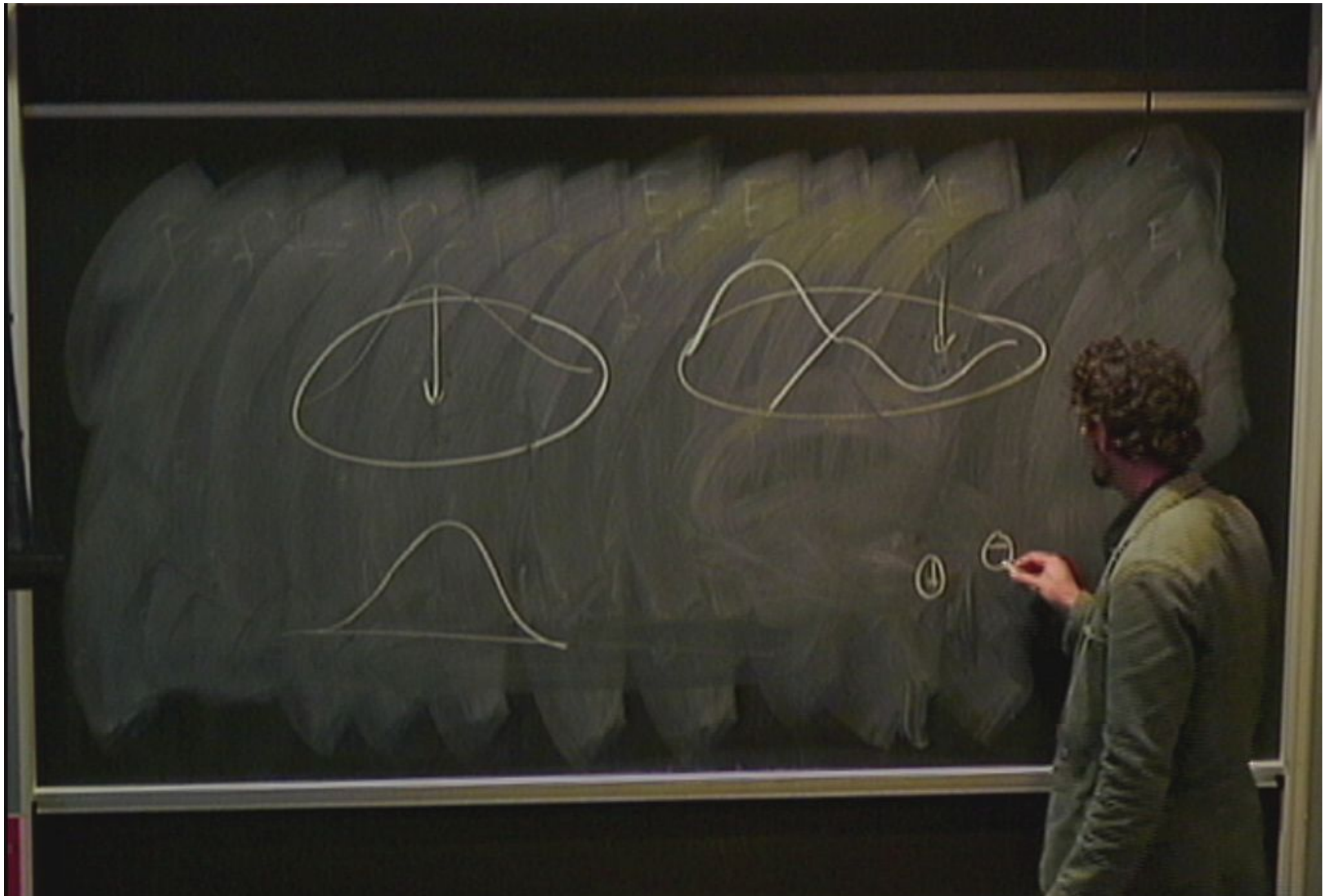
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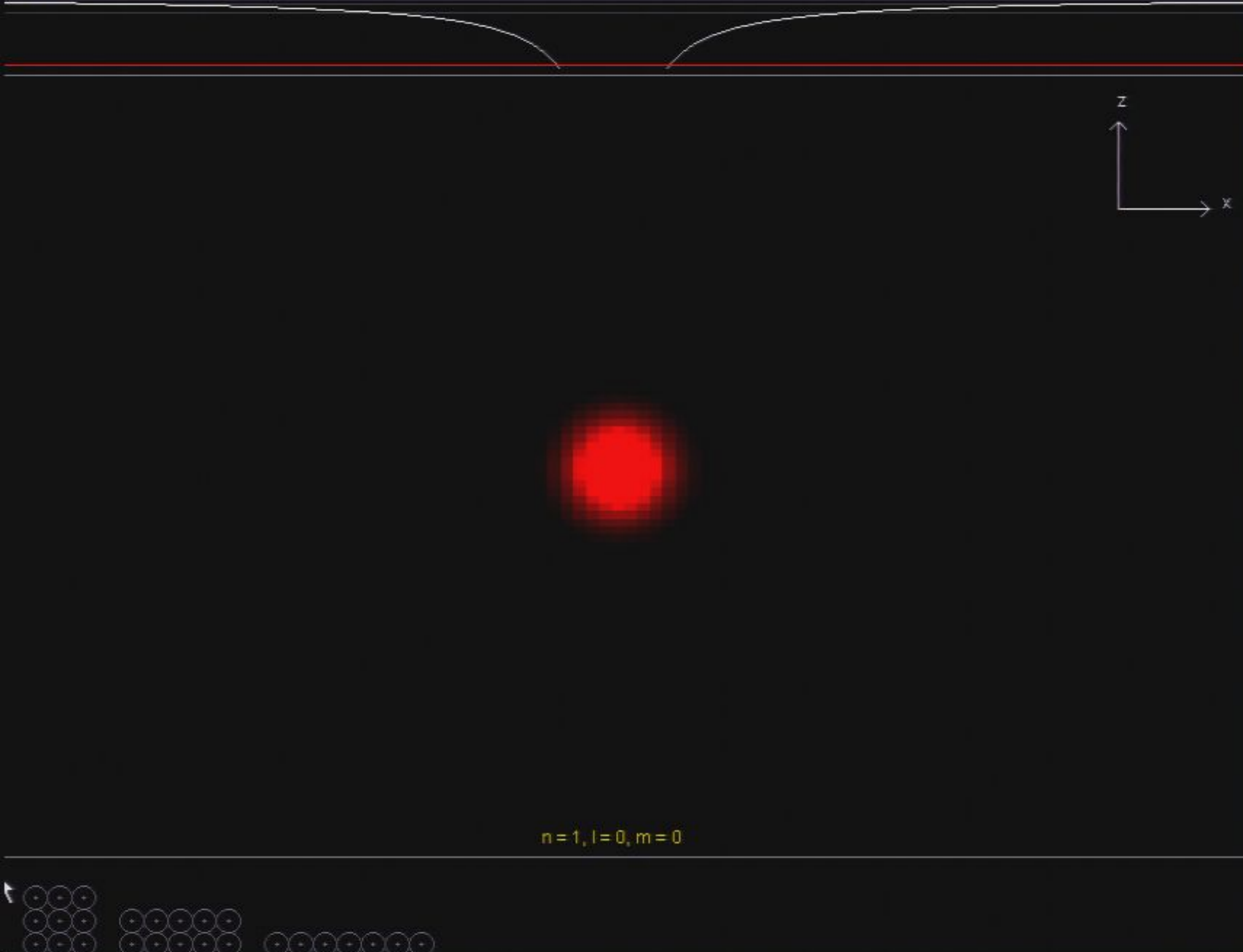






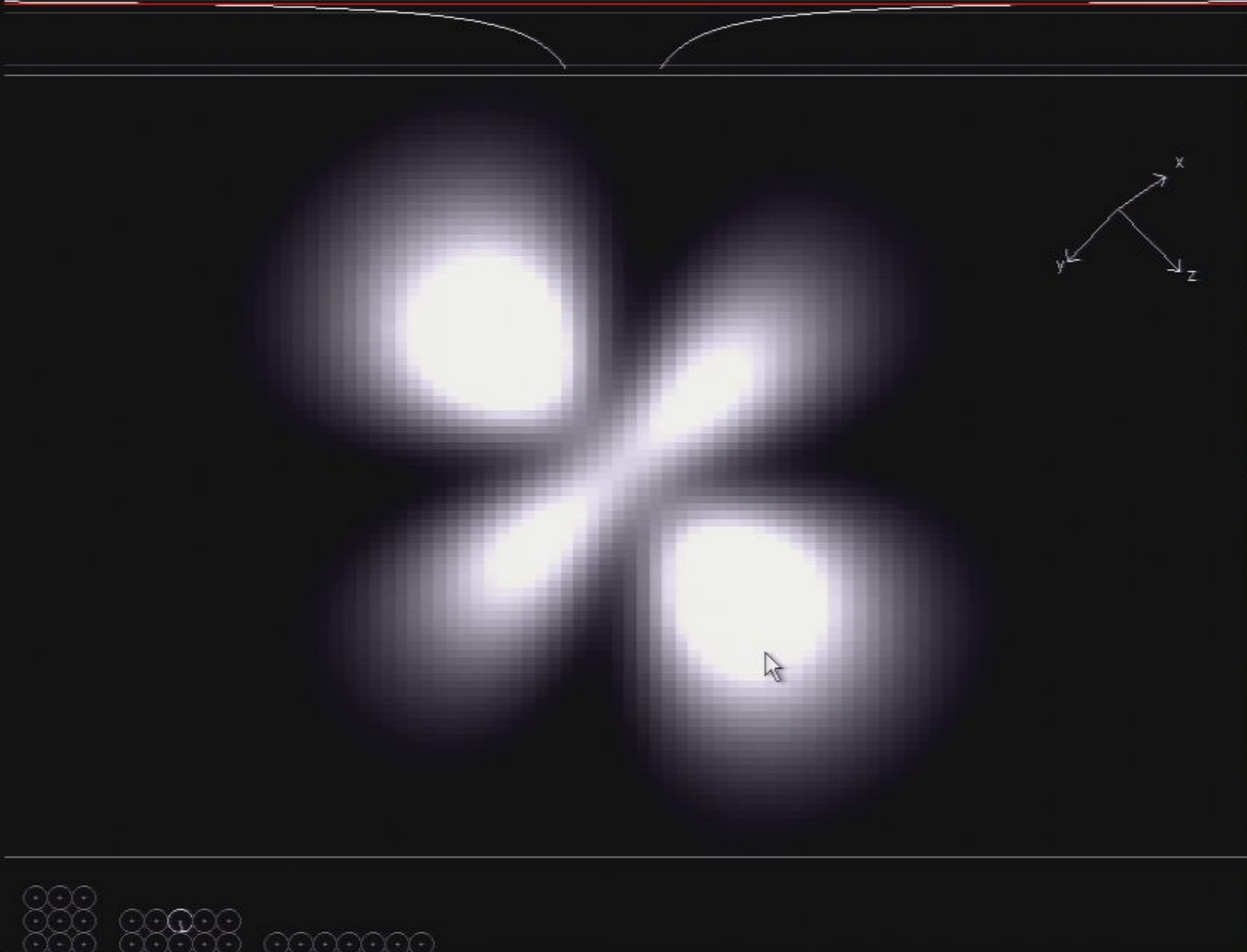






Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

Simulation Speed
Brightness
Image Resolution
Scale
<http://www.falstad.com>



Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

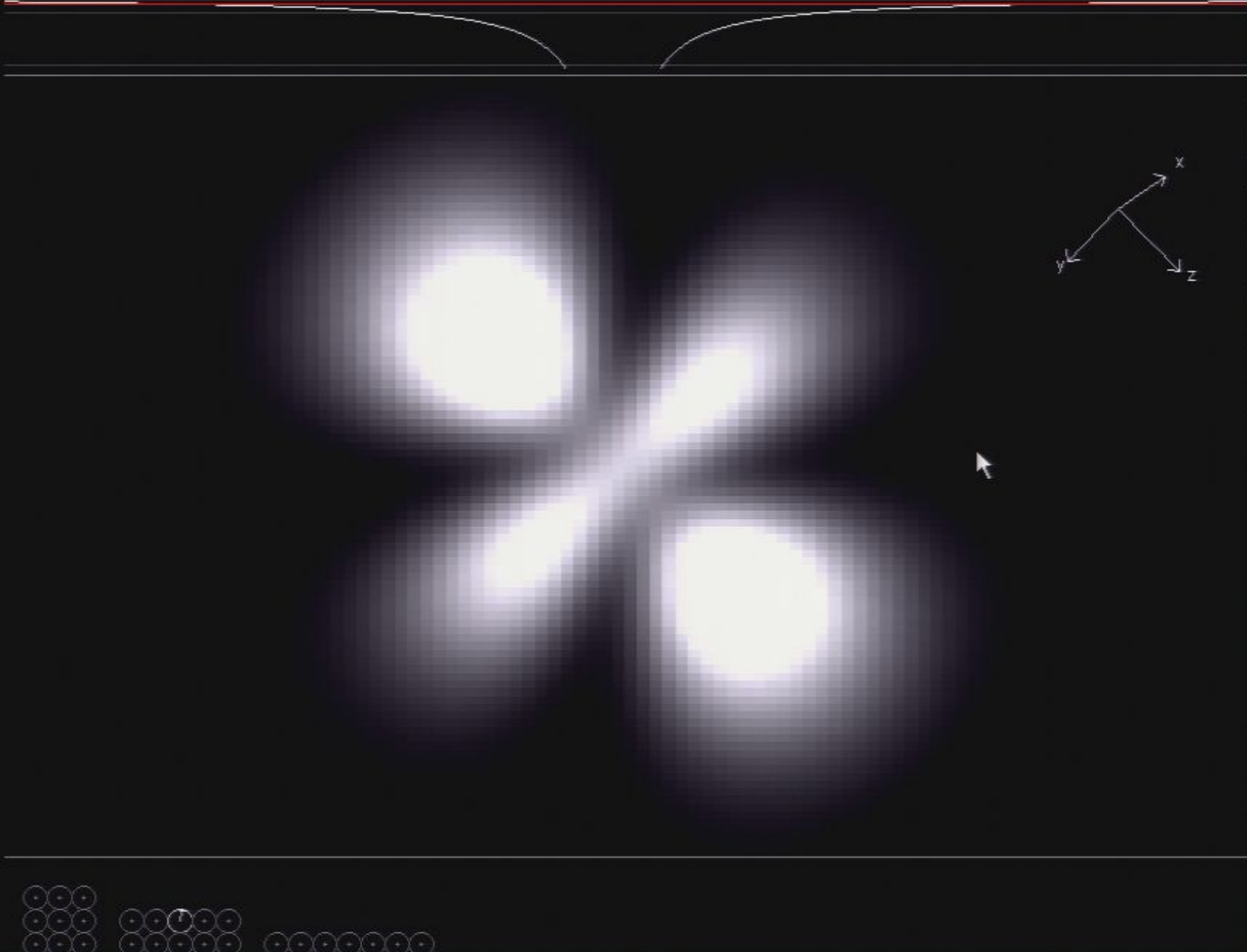
Simulation Speed

Brightness

Image Resolution

Scale

<http://www.falstad.com>



Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

Simulation Speed

Brightness

Image Resolution

Scale

<http://www.falstad.com>



Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

Simulation Speed

Brightness

Image Resolution

Scale

<http://www.falstad.com>





Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

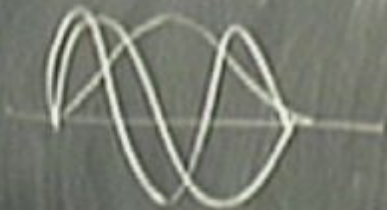
Simulation Speed

Brightness

Image Resolution

Scale

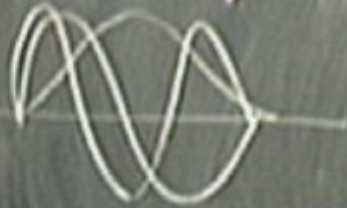
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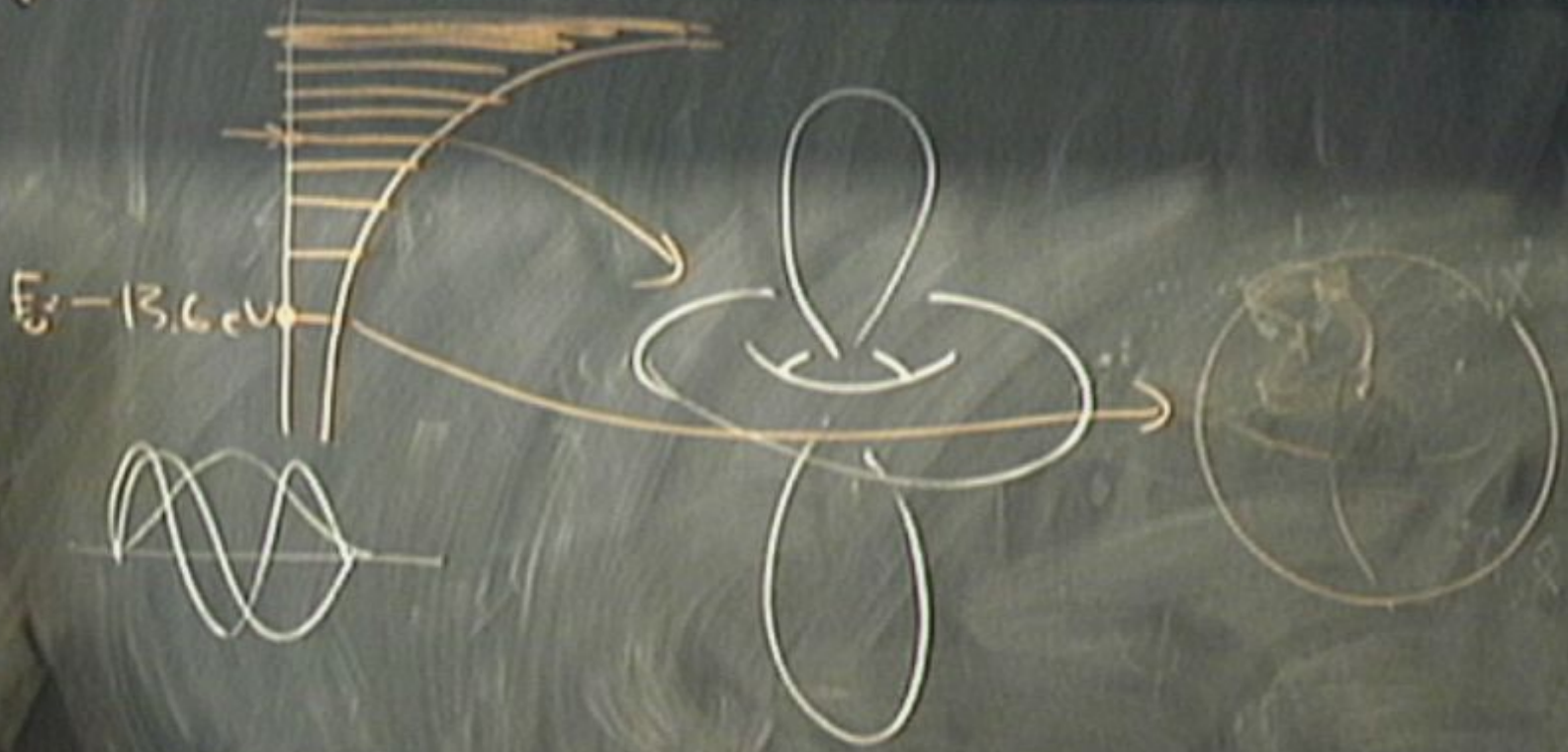


$$E_2 = 13.6 \text{ eV}$$

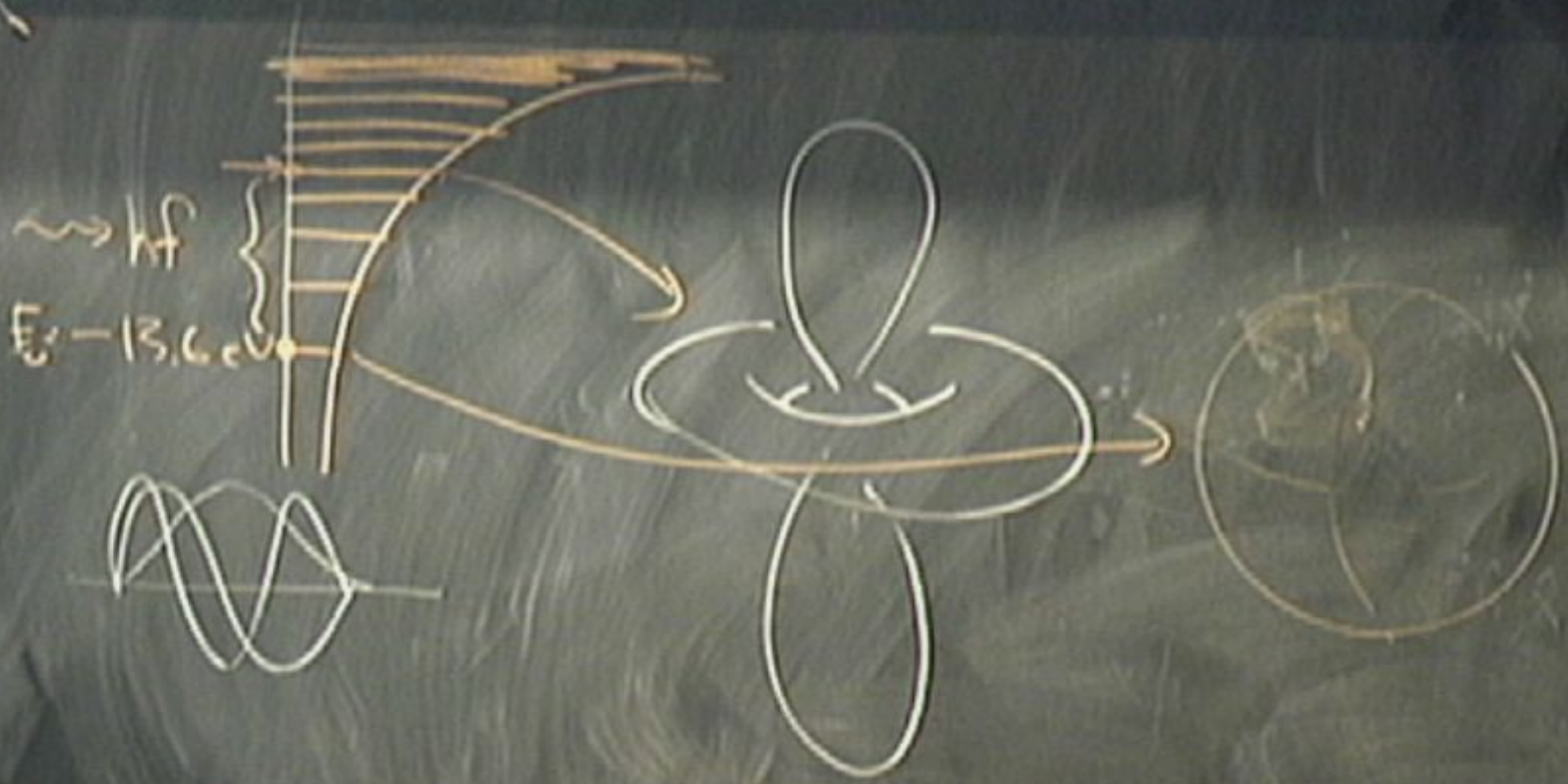


$$E_2 = 13.6 \text{ eV}$$



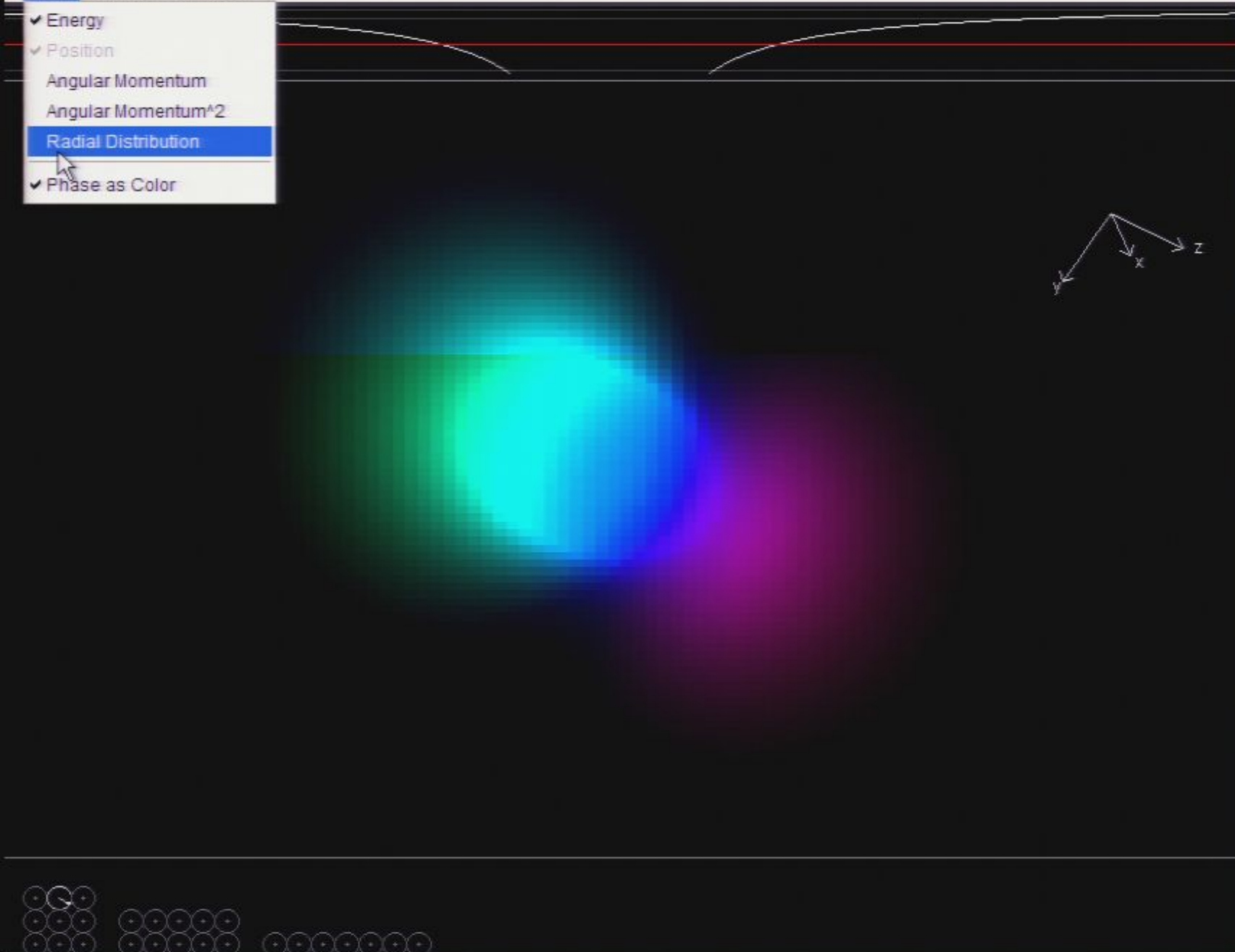








- ✓ Energy
- ✓ Position
- Angular Momentum
- Angular Momentum²
- Radial Distribution
- ✓ Phase as Color



Complex Combos (n=1-4)

No Slicing

Mouse = Adjust View

Stopped

Clear

Normalize

Maximize

Simulation Speed

Brightness

Image Resolution

Scale

<http://www.falstad.com>



Complex Combos (n=1-4)

No Slicing

Mouse = Adjust View

Stopped

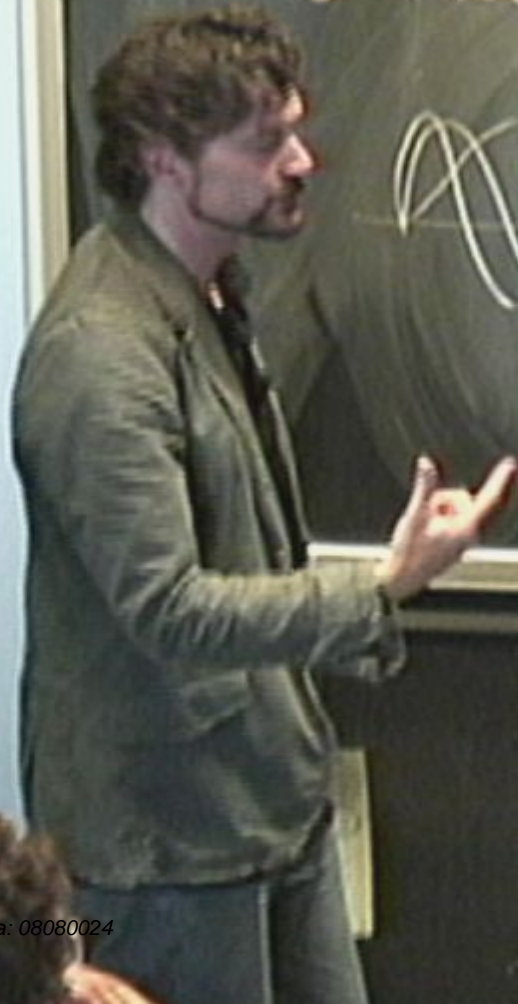
Simulation Speed

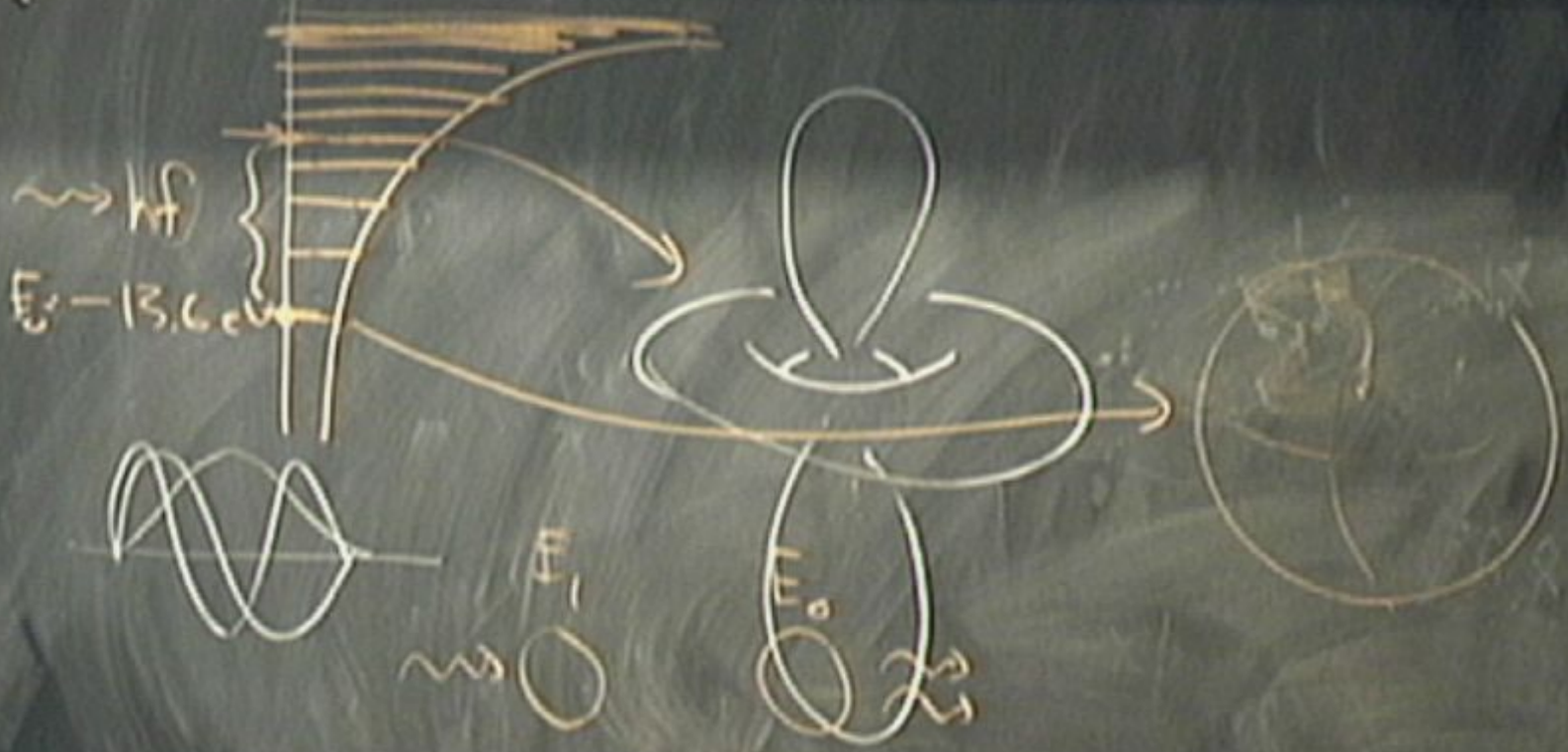
Brightness

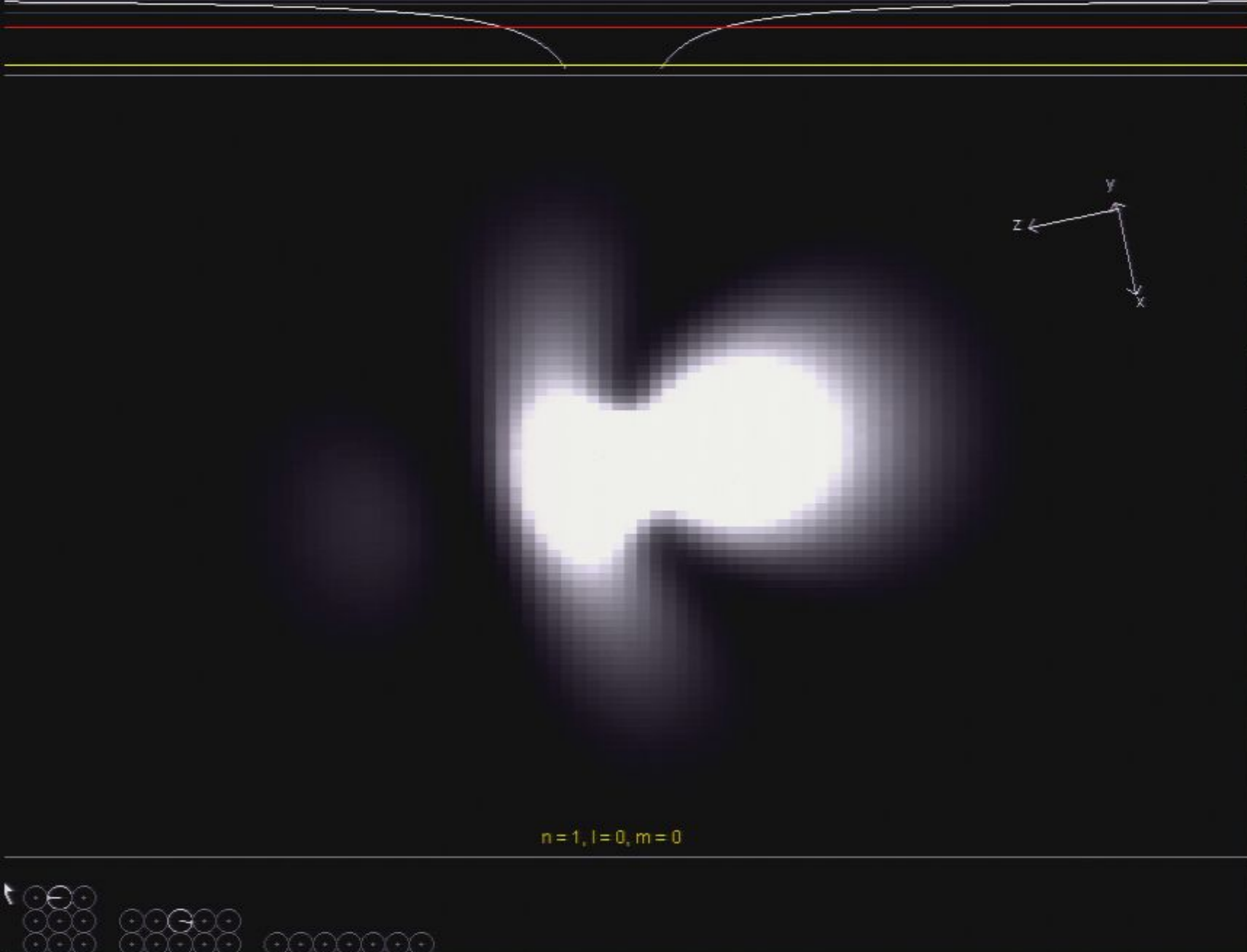
Image Resolution

Scale

<http://www.falstad.com>







Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

Simulation Speed

Brightness

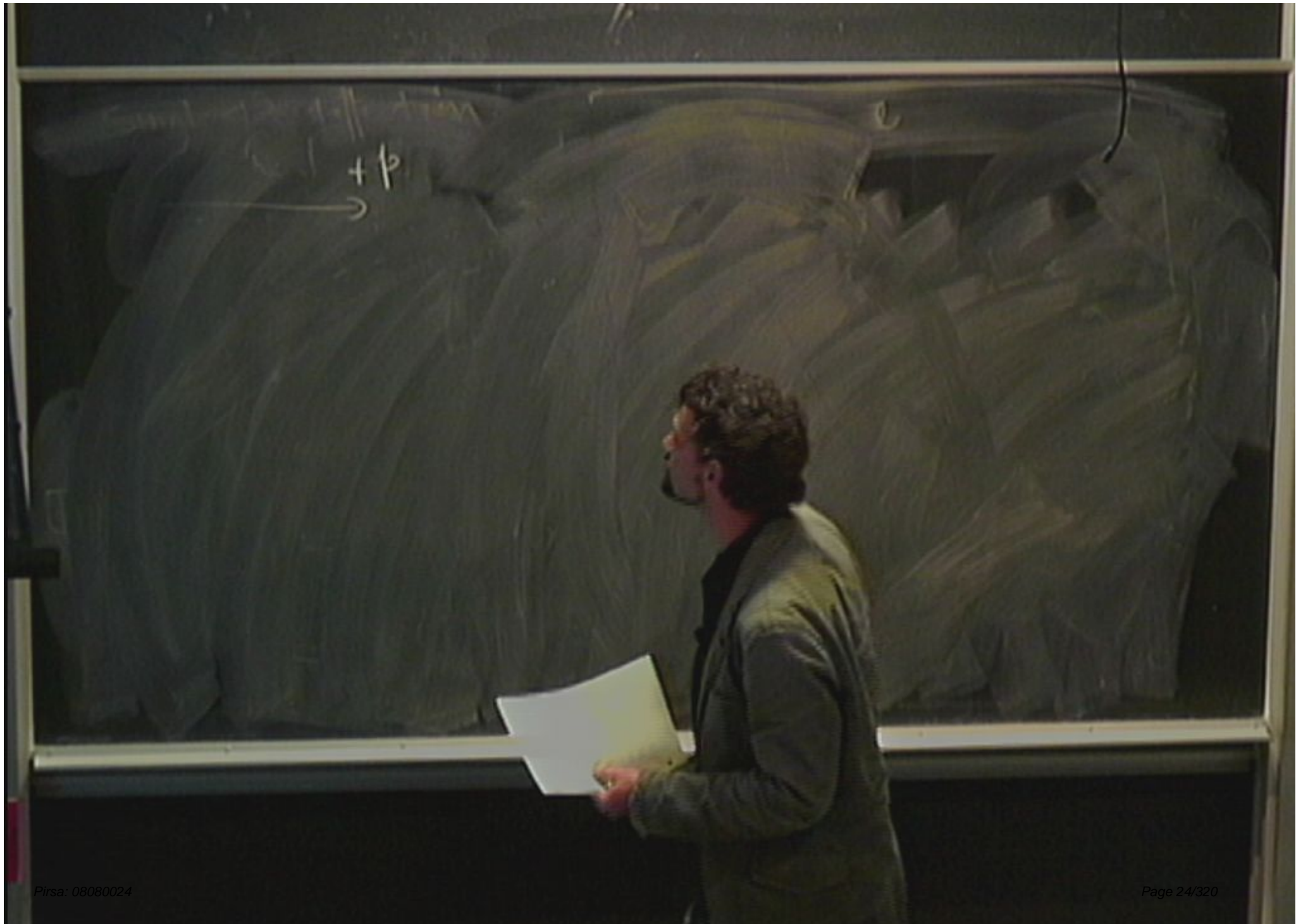
Image Resolution

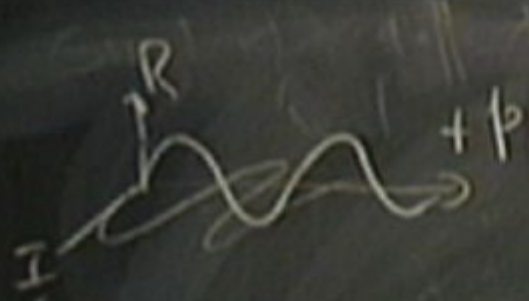
Scale

<http://www.falstad.com>

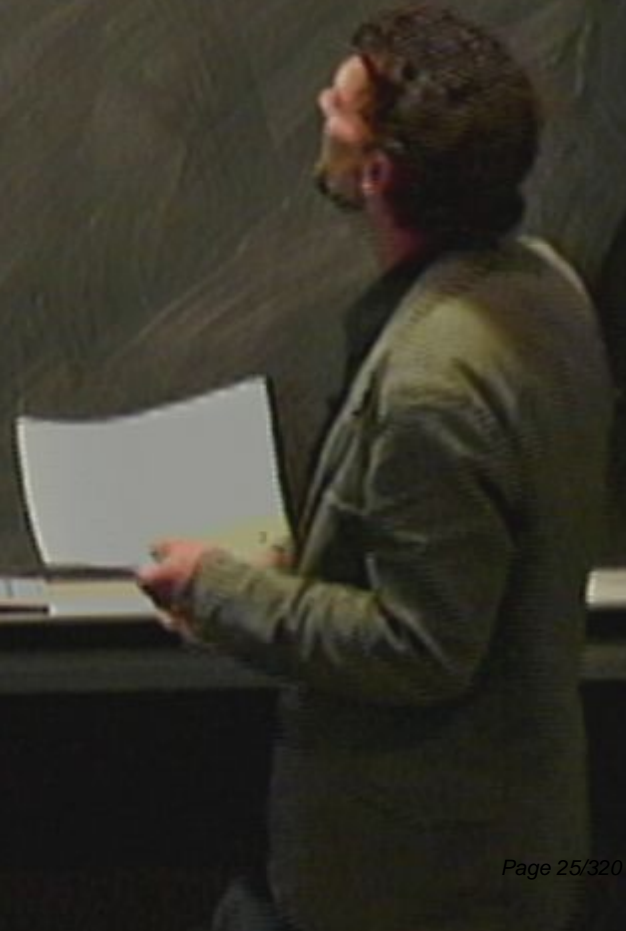
$n = 1, l = 0, m = 0$

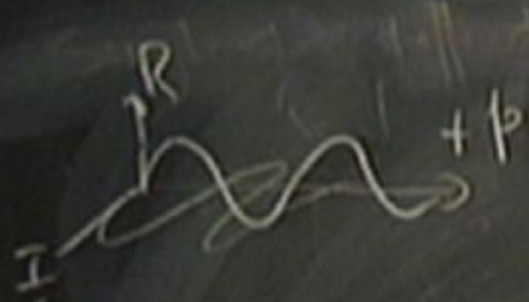




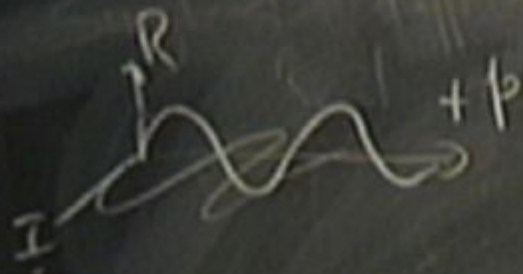


$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$



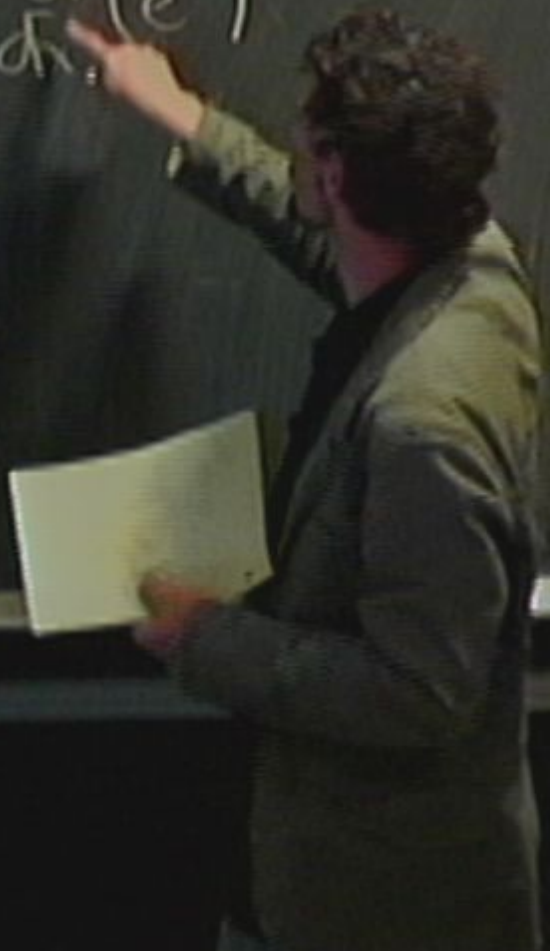


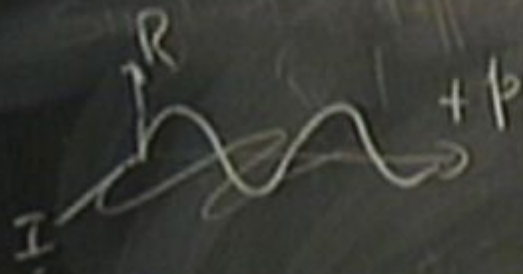
$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

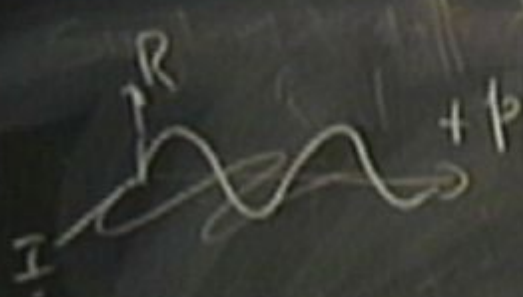
$$\frac{d}{dx}(e^x)$$





$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

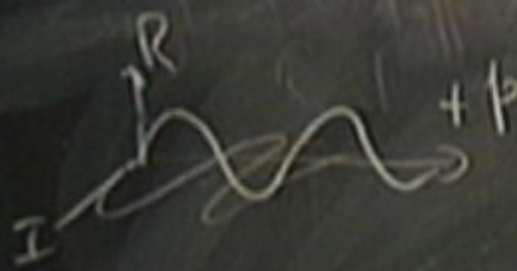
$$\frac{d}{dx}(e^x)$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

$$\frac{d}{dx}(x^n) =$$





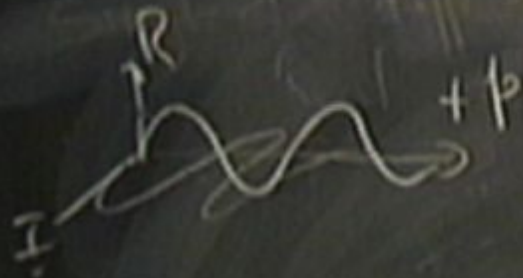
$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(e^{\alpha x})$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

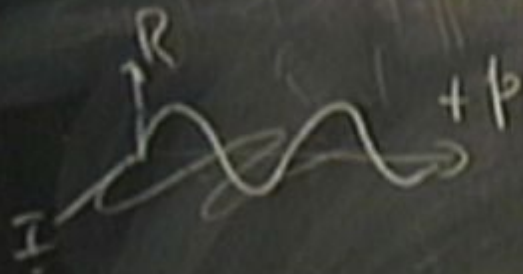
$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\alpha \frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\alpha \frac{d}{dy}(e^y) = \alpha e^y$$





$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dy}(e^y) = e^y$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\textcircled{\alpha} \frac{d}{dy}(e^y) = \alpha e^y$$

$$\frac{d}{dx}(\quad)$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

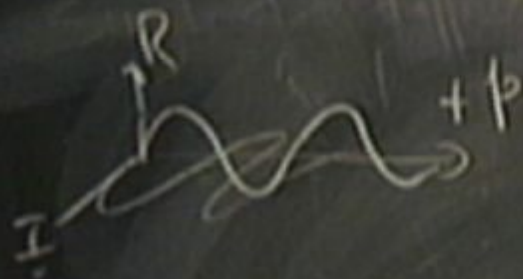
$$\frac{d}{dt}$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dt}$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dt} \psi =$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\alpha \frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\alpha \frac{d}{dy}(e^y) = \alpha e^y$$

$$\frac{d}{dx}(\dots)$$

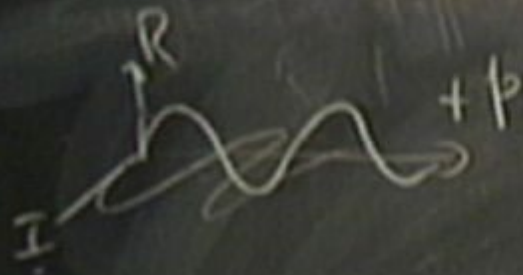


$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\psi =$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dt} \psi =$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

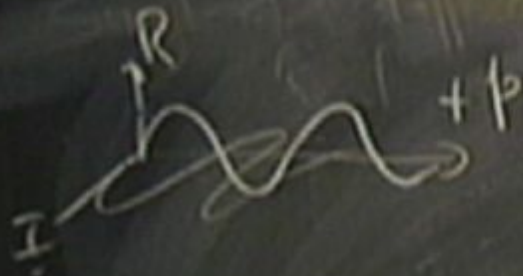
$$\alpha \frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\alpha \frac{d}{dy}(e^y) = \alpha e^y$$

$$\frac{d}{dx}(\quad)$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} \psi =$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\frac{i}{\hbar}px}$$

$$e^a e^b = e^{a+b}$$
$$\alpha \frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

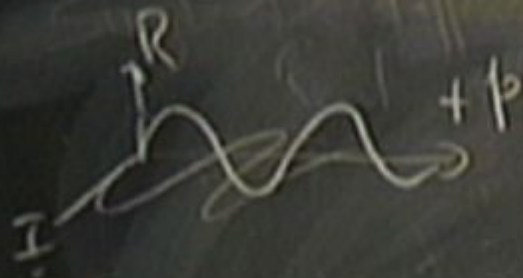
$$\alpha \frac{d}{dy} (e^y)$$

$$\frac{d}{dx} ($$

$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\left(\frac{i}{\hbar}px\right)} e^{-\frac{i}{\hbar}Et}$$

$e^a e^b = e^{a+b}$

$$\alpha \frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$

$$\alpha \frac{d}{dy} (e^y) = \alpha e^y$$

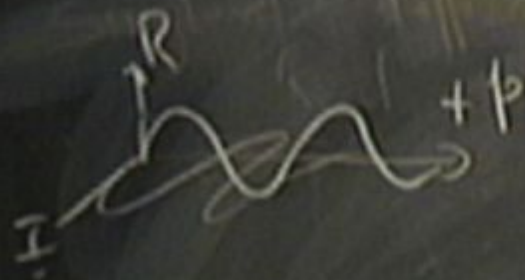
$$\frac{d}{dx} ($$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

=

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} \psi = i p \psi$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\left(\frac{i}{\hbar}px\right)} e^{-\frac{i}{\hbar}Et}$$

$$e^a e^b = e^{a+b}$$

$$\alpha \frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$

$$\alpha \frac{d}{dy} (e^y) = \alpha e^y$$

$$\frac{d}{dx} ($$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} \psi = i p \psi$$

$$\psi = \frac{d}{dx} \left(\frac{d}{dx} \psi \right)$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} \psi = i p \psi$$

$$\frac{d^2}{dx^2} \psi = \frac{d}{dx} \left(\frac{d}{dx} \psi \right) = \frac{d}{dx} (i p \psi) =$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

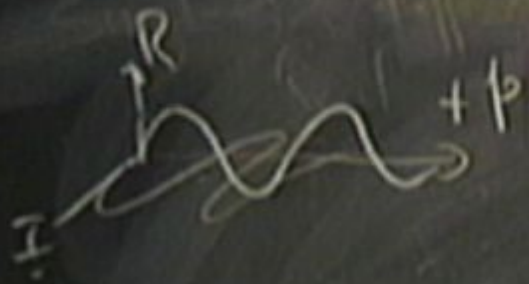
$$\psi' = \frac{i\hbar p}{\hbar} \psi$$

$$\psi'' = \frac{d}{dx} \left(\frac{d}{dx} \psi \right) = \frac{d}{dx} \left(\frac{i\hbar p}{\hbar} \psi \right) = \left(\frac{i\hbar p}{\hbar} \right)^2 \psi =$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} \psi = \frac{i}{\hbar} p \psi$$

$$\frac{d^2}{dx^2} \psi = \frac{d}{dx} \left(\frac{d}{dx} \psi \right) = \frac{d}{dx} \left(\frac{i}{\hbar} p \psi \right) = \left(\frac{i}{\hbar} p \right)^2 \psi = -\frac{p^2}{\hbar^2} \psi$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\left(\frac{i}{\hbar}px\right)} e^{-\frac{i}{\hbar}Et}$$

$$e^a e^b = e^{a+b}$$

$$\alpha \frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

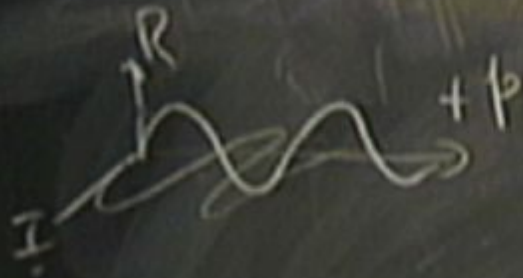
$$\alpha \frac{d}{dy} (e^y) = \alpha e^y$$

$$\frac{d}{dx} ($$

$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\left(\frac{i}{\hbar}px\right)} e^{\left(-\frac{i}{\hbar}Et\right)}$$

$$e^a e^b = e^{a+b}$$

$$\alpha \frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\alpha \frac{d}{dy} (e^y) = \alpha e^y$$

$$\frac{d}{dx} ($$

$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} \psi = \frac{i}{\hbar} p \psi$$

$$\frac{d^2}{dx^2} \psi = \frac{d}{dx} \left(\frac{d}{dx} \psi \right) = \frac{d}{dx} \left(\frac{i}{\hbar} p \psi \right) = \left(\frac{i}{\hbar} p \right)^2 \psi = -\frac{p^2}{\hbar^2} \psi$$

$$\frac{d}{dt} \psi = -\frac{i}{\hbar} E \psi$$

$$-i\hbar \frac{d}{dt} \psi =$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi =$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{p^2}{2m} \psi$$

$$E = KE + PE$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{p^2}{2m} \psi$$

$$E = KE + PE =$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{\hbar^2}{2m} \psi$$

$$E = KE + PE = \frac{\hbar^2}{2m}$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi + V \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{\hbar^2}{2m} \psi$$

$$V(x) = +PE = \frac{\hbar^2}{2m}$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{p^2}{2m} \psi$$

$$E = KE + \underbrace{PE}_{V(x)} = \frac{p^2}{2m}$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi + V \psi$$



Complex Combos (n=1-4)

No Slicing

Mouse = Adjust View

Stopped

Simulation Speed

Brightness

Image Resolution

Scale

<http://www.falstad.com>

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{p^2}{2m} \psi$$

$$E = KE + PE = \frac{p^2}{2m} + V(x)$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi + V \psi$$

$\psi(x, y, z, t)$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{p^2}{2m} \psi$$

$$E = KE + \frac{V(x)}{0} = \frac{p^2}{2m}$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi + V \psi$$

$\psi(x, y, z, t)$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$+i\hbar \frac{d}{dt} \psi = +E \psi$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi = +\frac{p^2}{2m} \psi$$

$$= KE + \cancel{PE} = \frac{p^2}{2m}$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi + V \psi$$

$$\psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$i\hbar \frac{d}{dt} \psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi + V \psi$$

$$\psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$

$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2c^4 + c^2p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$

$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$

$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$

$$\Psi \rightarrow \begin{pmatrix} \Psi_1 \\ \Psi_2 \\ \Psi_3 \\ \Psi_4 \end{pmatrix}$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = \dots + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$

$$\Psi \rightarrow \begin{pmatrix} \psi_1 \\ \psi_2 \\ \psi_3 \\ \psi_4 \end{pmatrix}$$

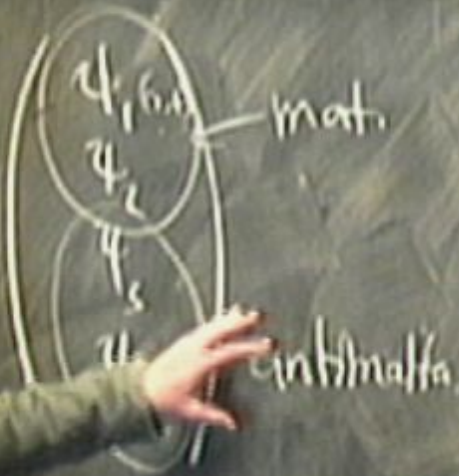
$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \nabla^2 \Psi + V\Psi$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$

$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$

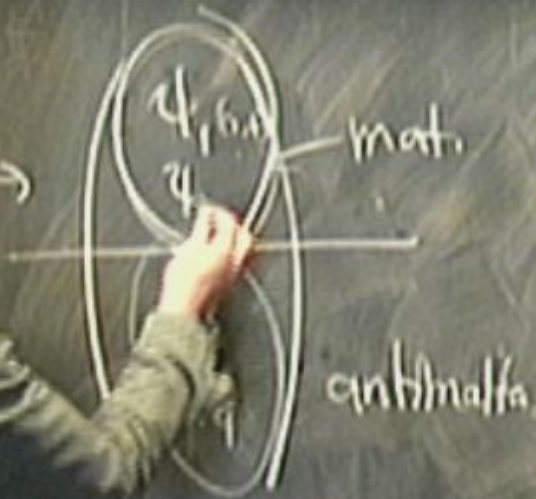


$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i \Psi_I$$

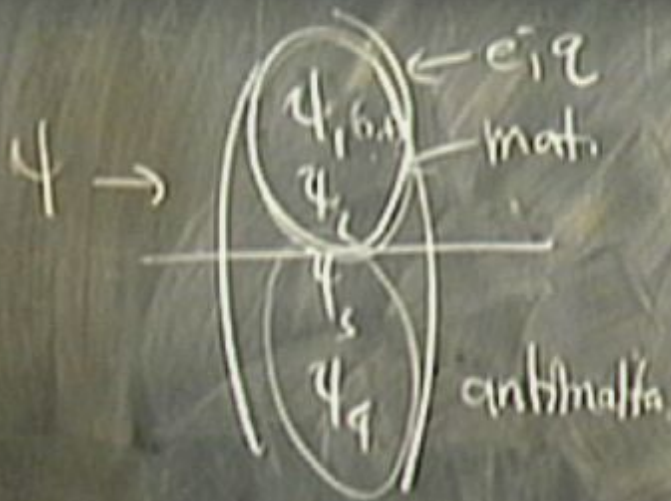
$$i \hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V \Psi$$



$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i \Psi_I$$



$$i \hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V \Psi$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$



$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\left(\frac{ipx}{\hbar}\right)} e^{\left(-\frac{iEt}{\hbar}\right)}$$

$$e^a e^b = e^{a+b}$$

$$\frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

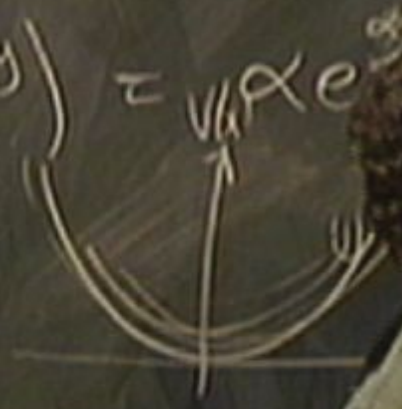
$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$

$$\frac{d}{dy} (e^y) = e^y$$

$$\frac{d}{dx} ($$





$$\psi = e^{ik(x - vt)} = e^{ikx} e^{-i\omega t}$$

$$e^a e^b = e^{a+b}$$

$$\frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

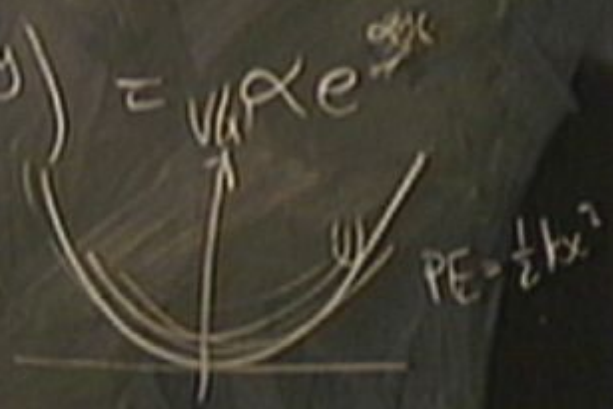
$$\frac{d}{dx} (x^n) = nx^{n-1}$$

$$\frac{d}{dx} (e^x) = e^x$$

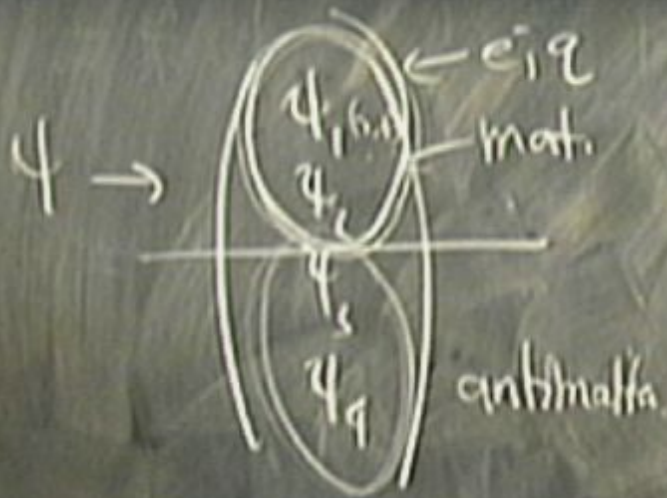
$$\frac{d}{dx} (\sin x) = \cos x$$

$$\frac{d}{dy} (e^y) = e^y$$

$$\frac{d}{dx} ($$



$$\Psi \rightarrow \Psi_R + i\Psi_I$$



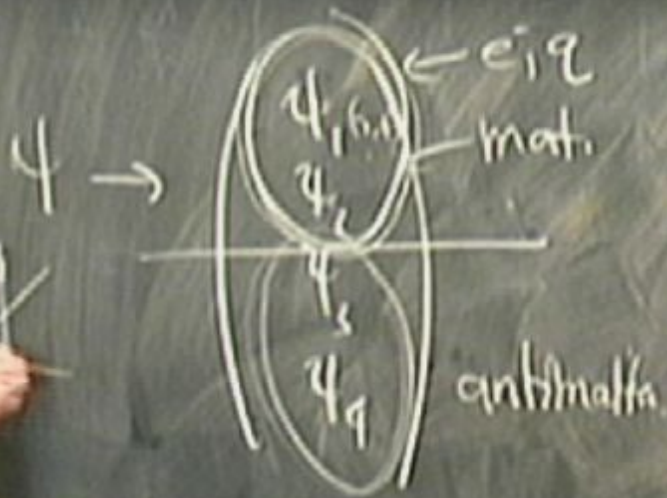
$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$

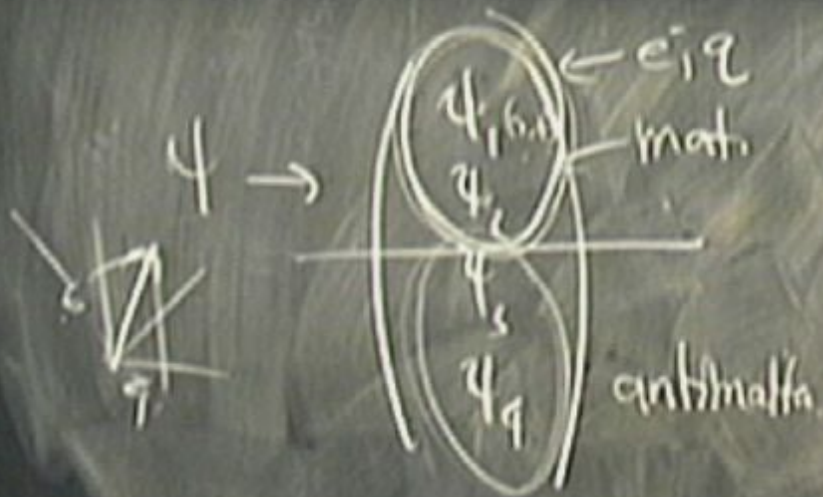
$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$



$$\Psi(x, y, z, t) \quad E \approx \frac{\hbar^2 k^2}{2m} + mc^2$$

$$E^2 = m^2 c^4 + c^2 p^2$$

$$\Psi \rightarrow \Psi_R + i\Psi_I$$



$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$

$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

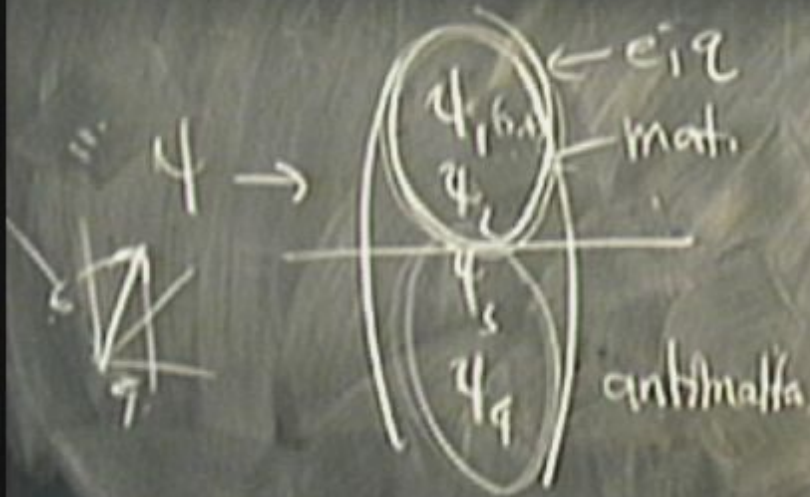
$$E^2 = m^2 c^4 + c^2 p^2$$

$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{dx^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} = \nabla^2$$

↑
lapla

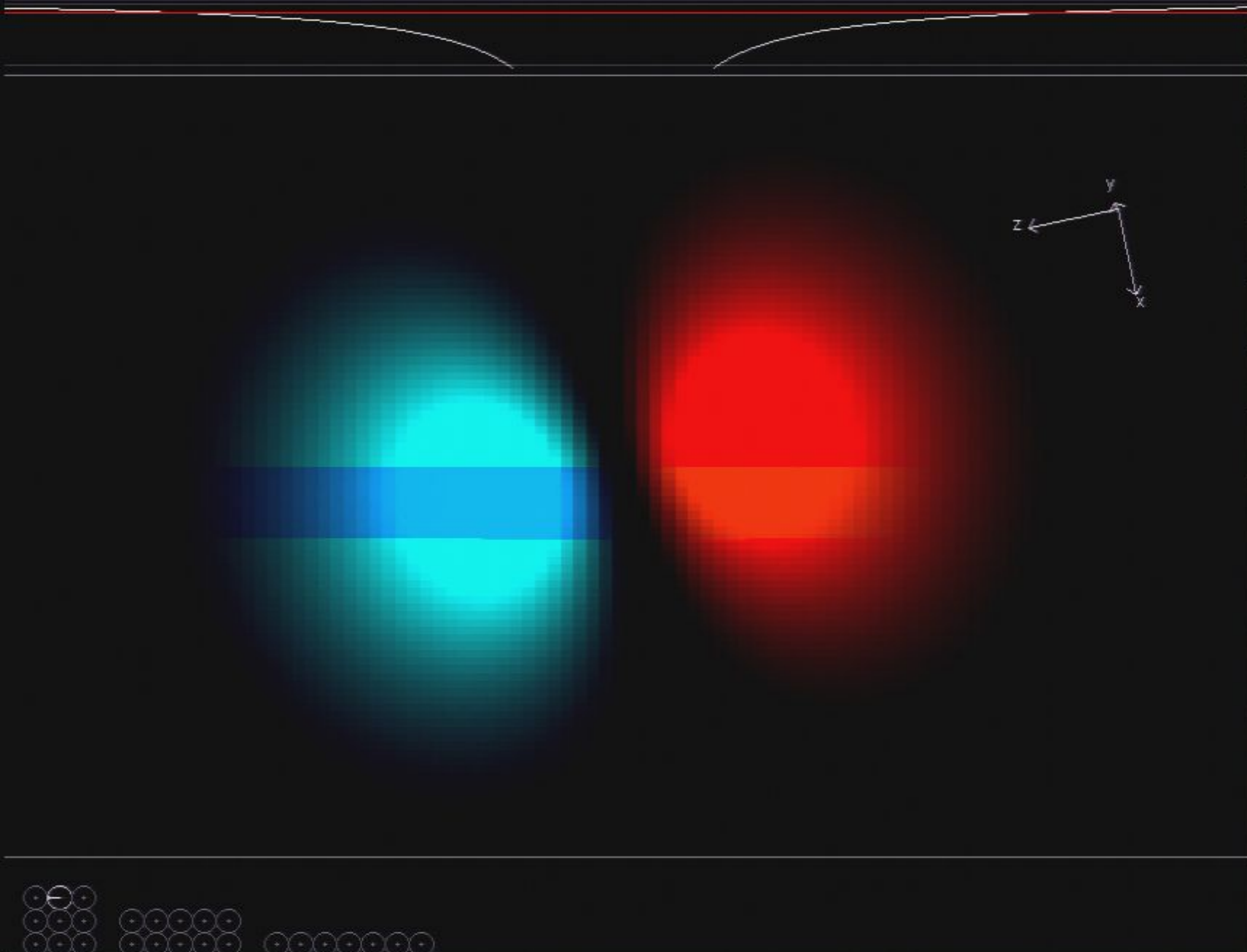
$$\Psi \rightarrow \Psi_R + i\Psi_I$$

$$i\hbar \frac{d}{dt} \Psi = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \Psi + V\Psi$$



$$\Psi(x, y, z, t) \quad E \approx \frac{p^2}{2m} + mc^2$$

$$E^2 = mc^2 + c^2 p^2$$



Complex Combos (n=1-4)
No Slicing
Mouse = Adjust View
 Stopped

Simulation Speed
Brightness
Image Resolution
Scale
<http://www.falstad.com>





$$\psi = e^{i k x} = e^{i k x} e^{i k x}$$

$$e^a e^b = e^{a+b}$$

$$\frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} (x^n) = n x^{n-1}$$

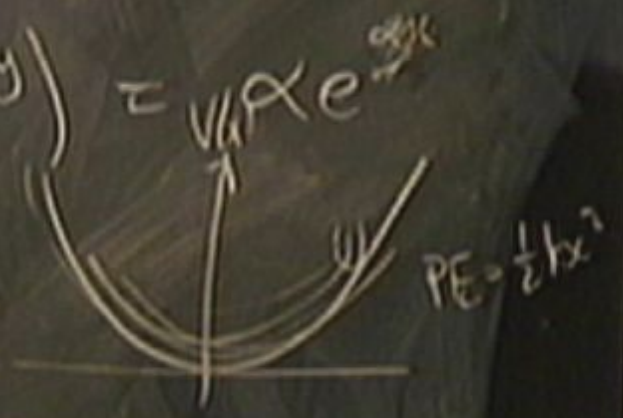
$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$



$$\frac{d}{dy} (e^y) = e^y$$

$$\frac{d}{dx} ($$





$$\psi = e^{\frac{i}{\hbar}(px - Et)} = e^{\left(\frac{c\hbar}{\hbar}kx\right)} e^{-\left(\frac{c}{\hbar}Et\right)}$$

$$e^a e^b = e^{a+b}$$

$$\frac{d}{dx} (e^{\alpha x}) = \alpha e^{\alpha x}$$

$$\frac{d}{dx} (x^n) = nx^{n-1}$$

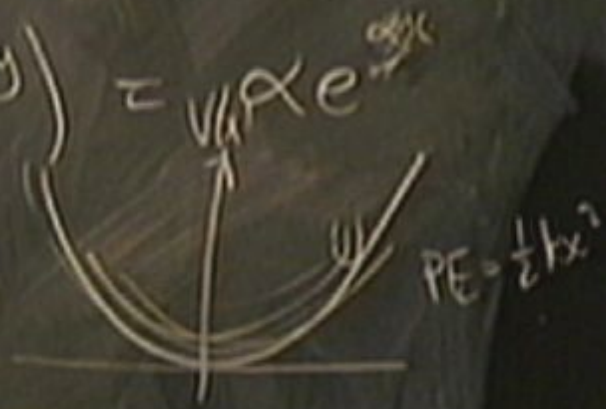
$$\frac{d}{dx} (e^x) = e^x$$

$$\frac{d}{dx} (\sin x) = \cos x$$

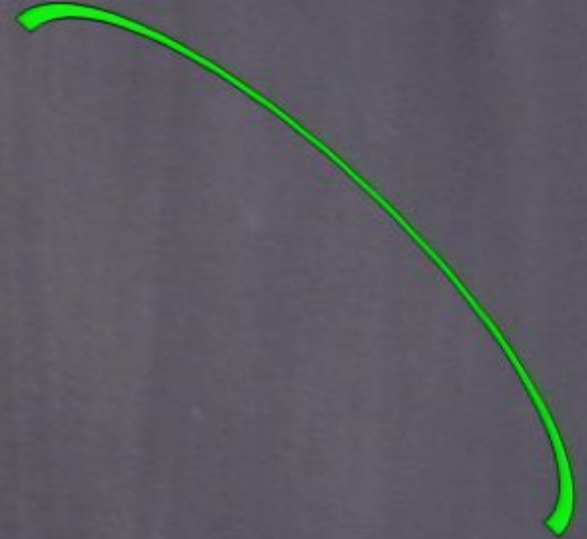


$$\frac{d}{dy} (e^y) = e^y$$

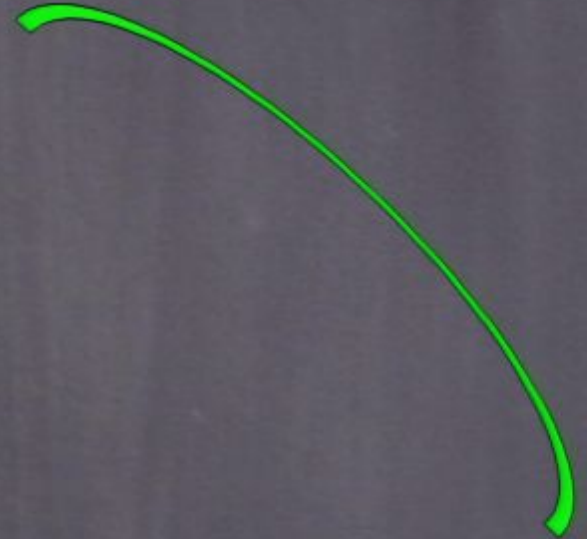
$$\frac{d}{dx} ($$



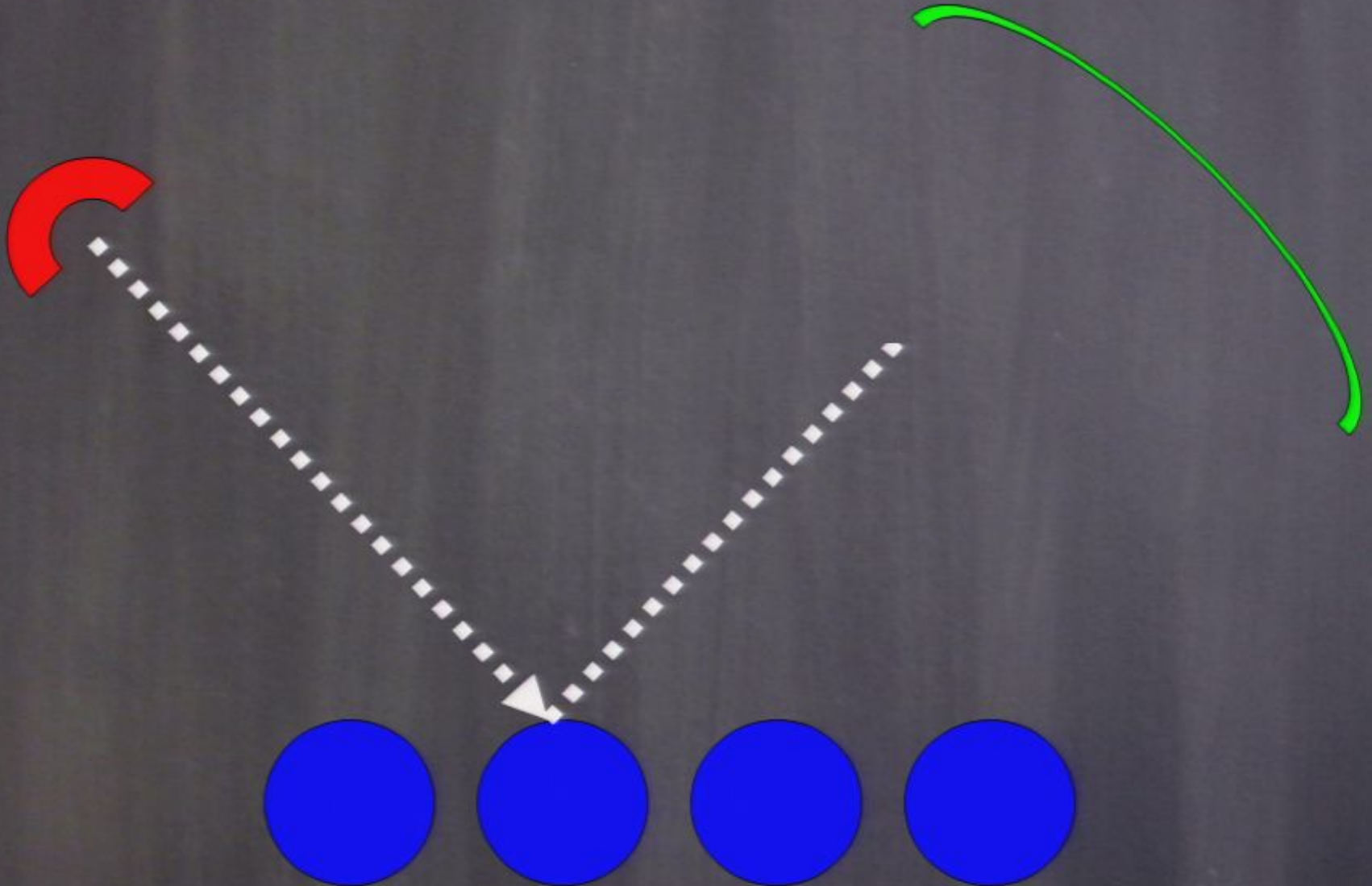
What's Inside the Tube?



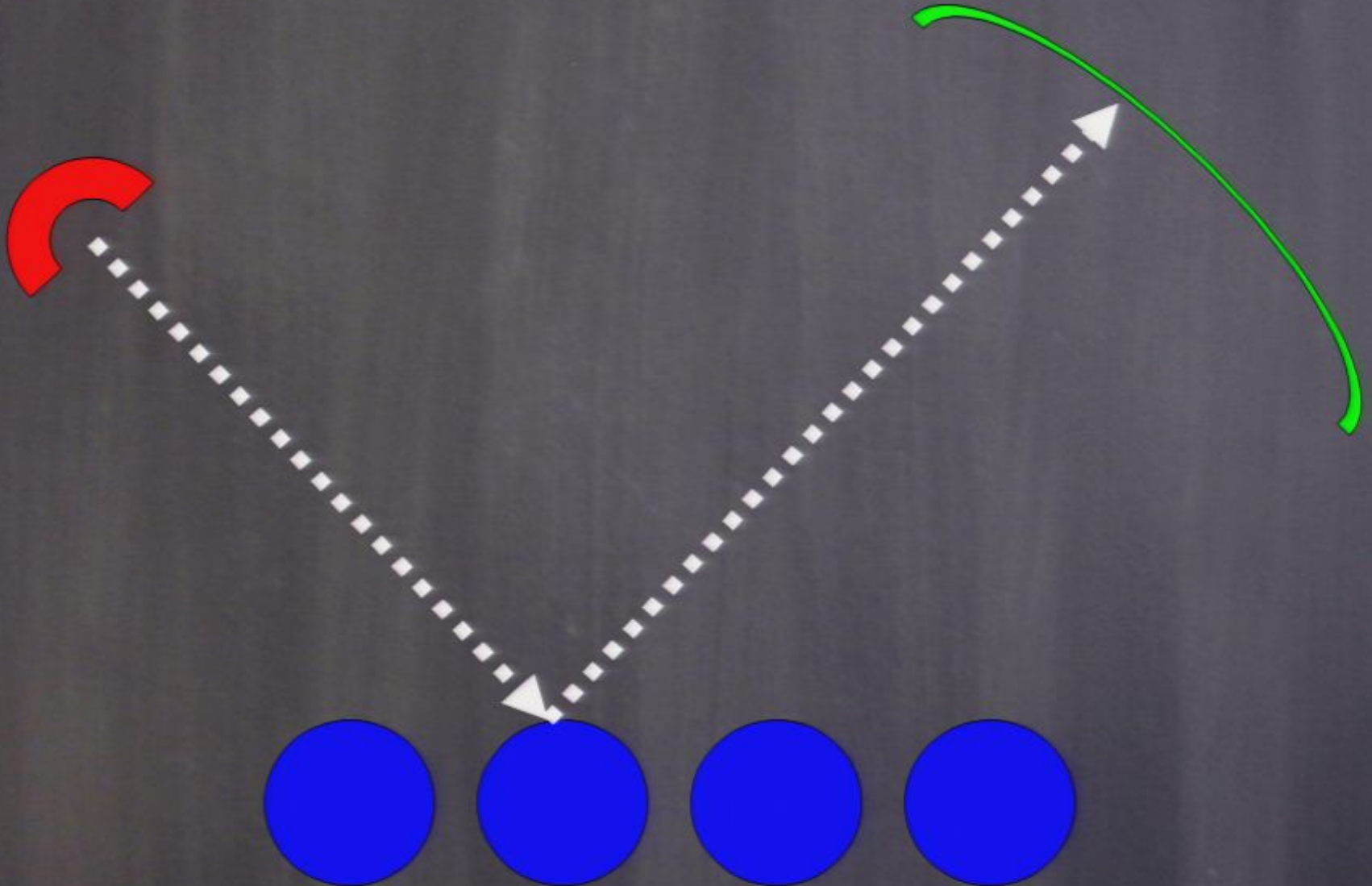
What's Inside the Tube?



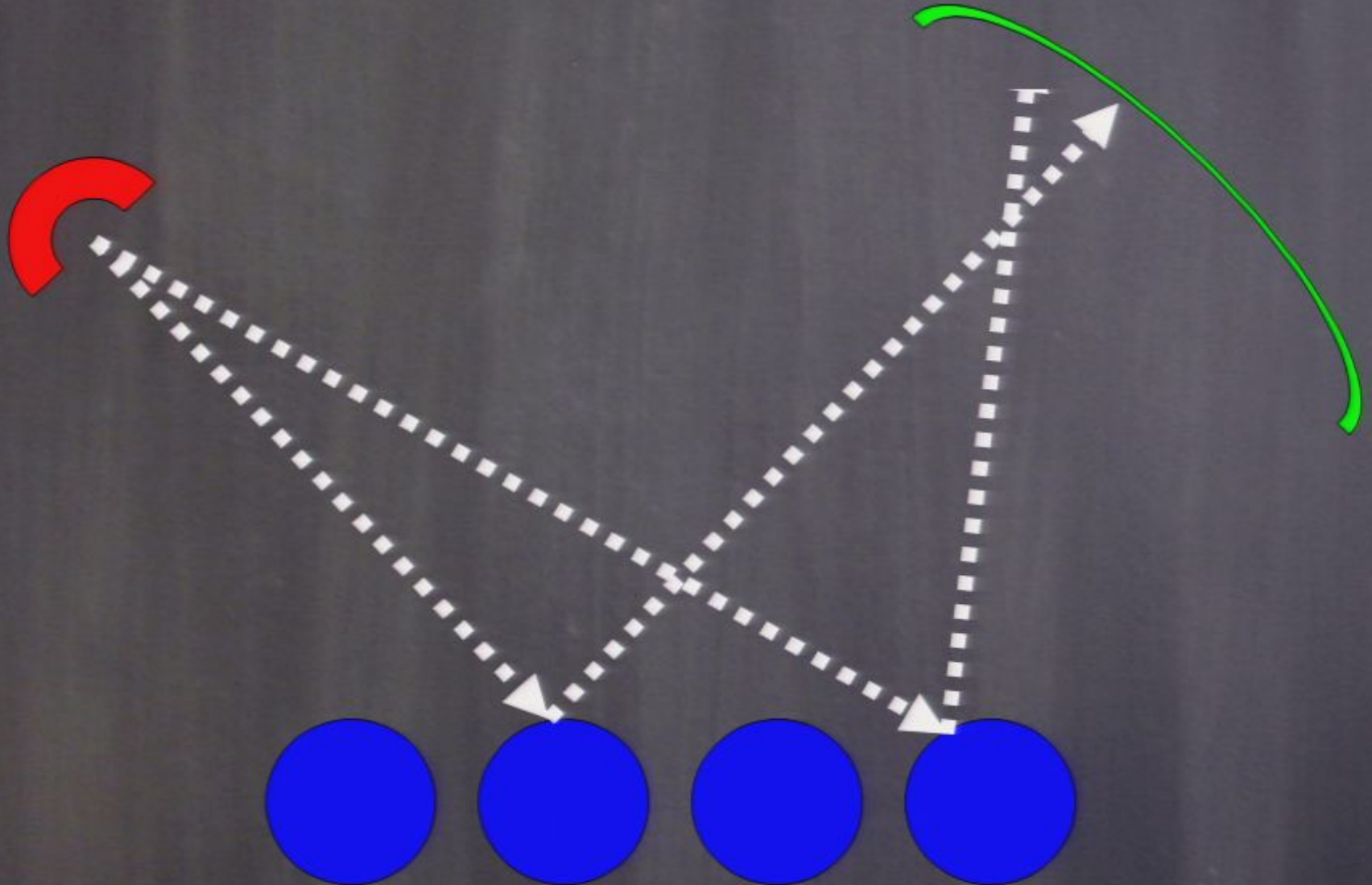
What's Inside the Tube?



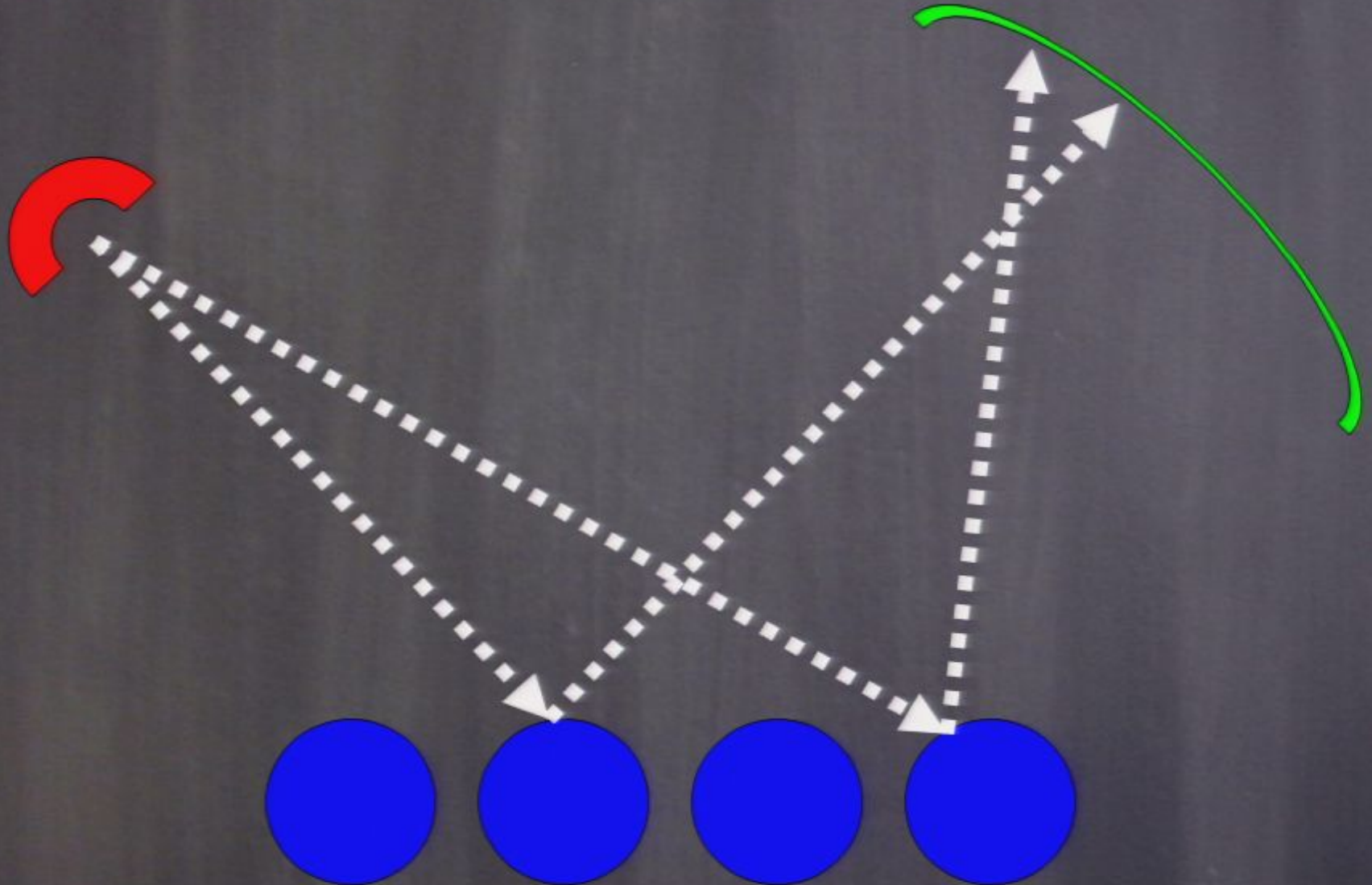
What's Inside the Tube?



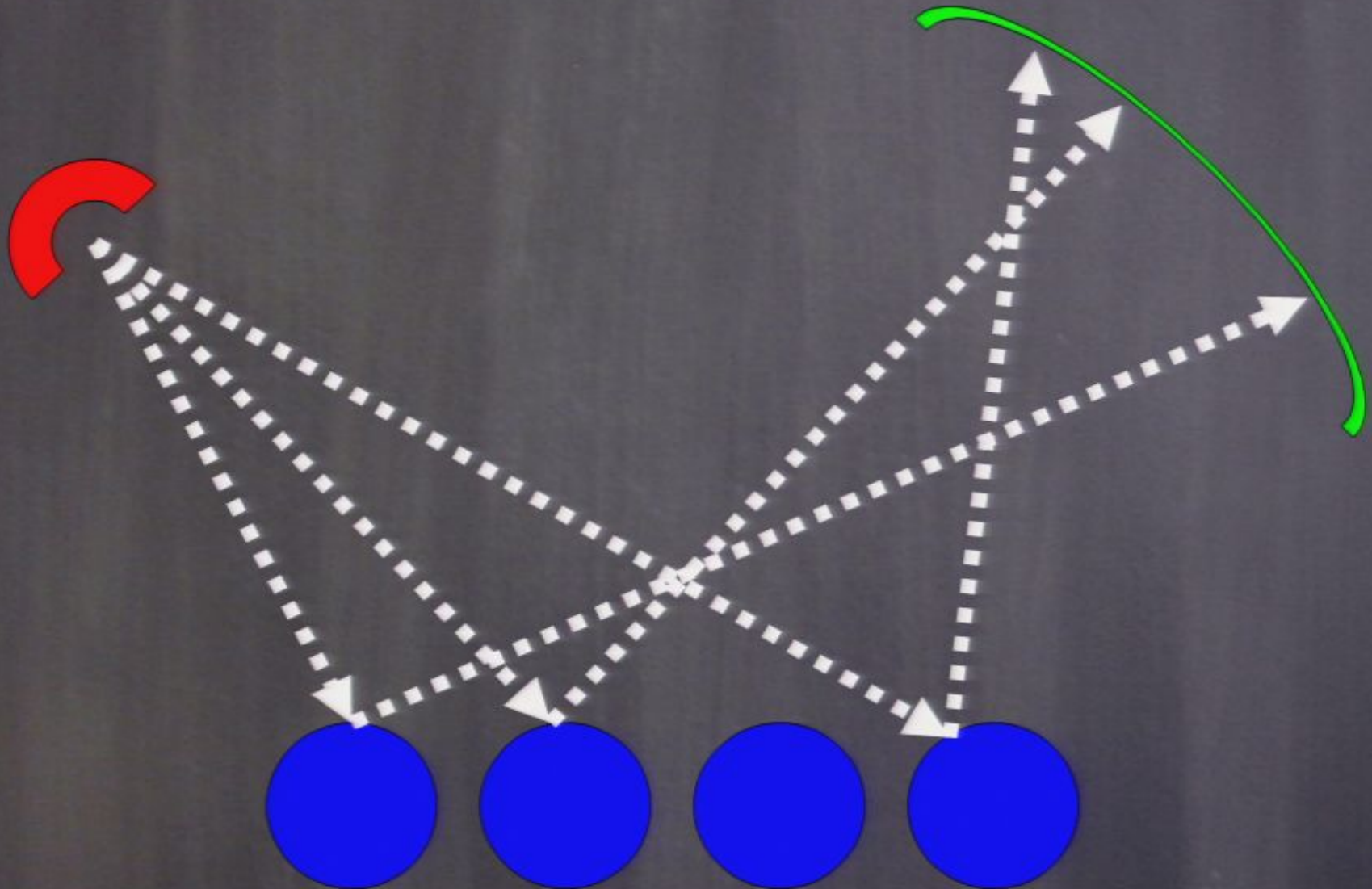
What's Inside the Tube?



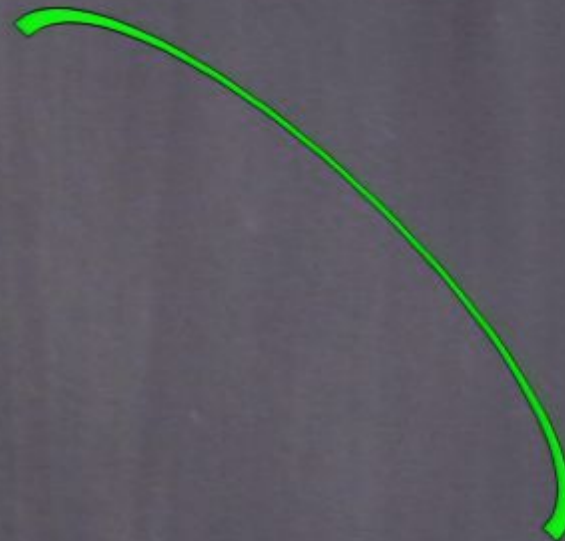
What's Inside the Tube?



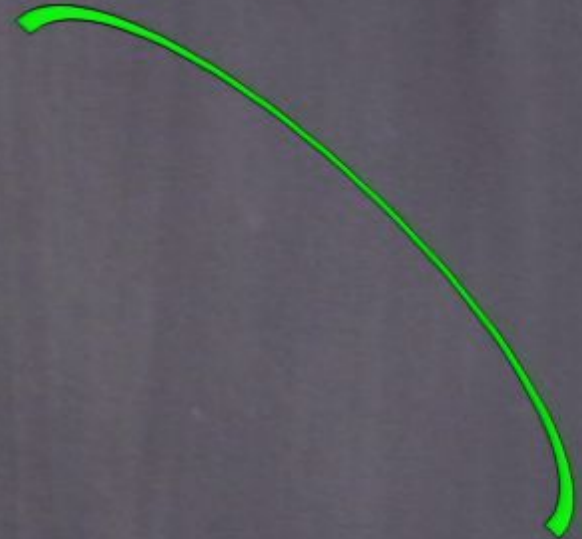
What's Inside the Tube?



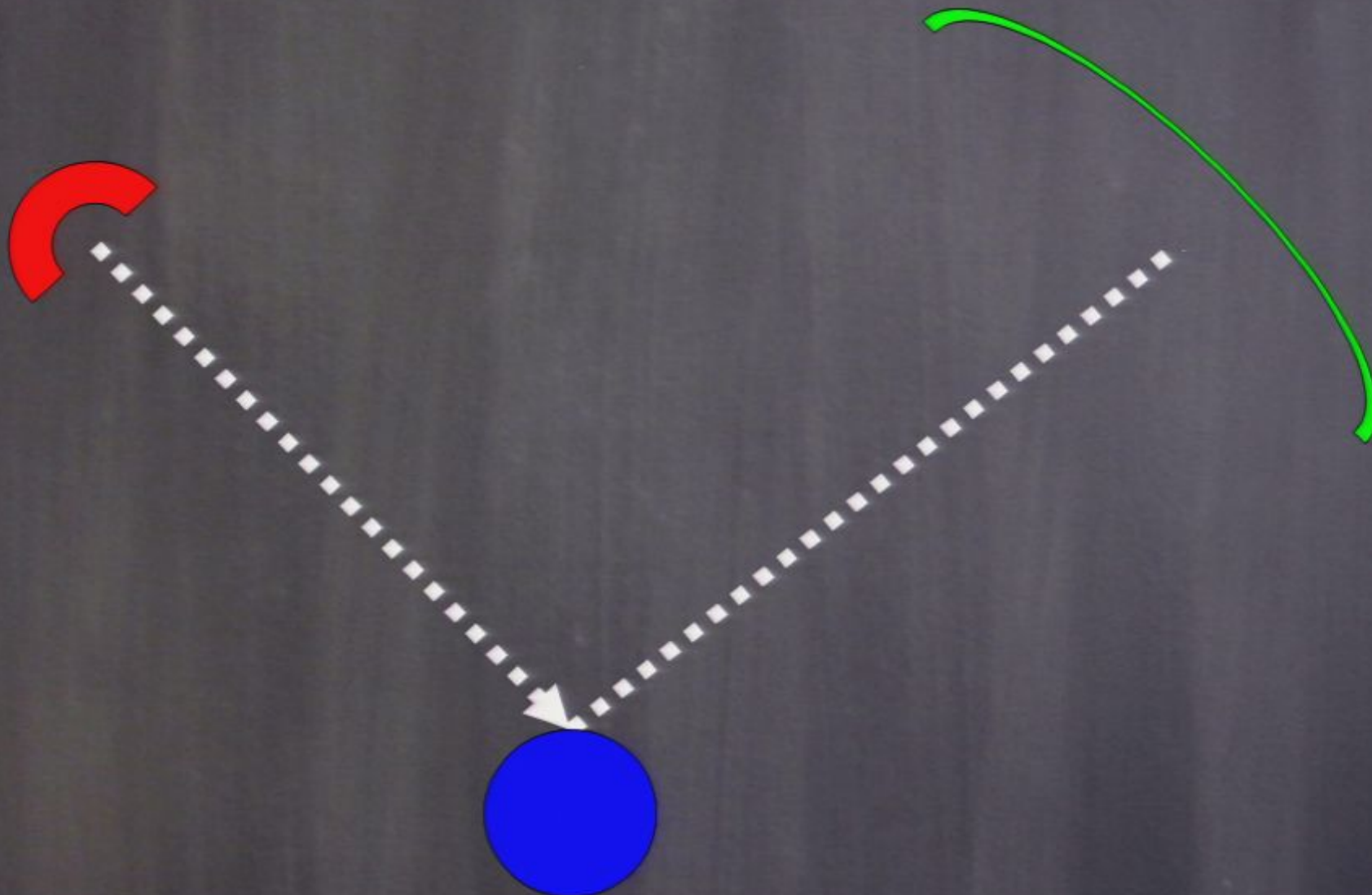
Simplify: Only **ONE** Atom



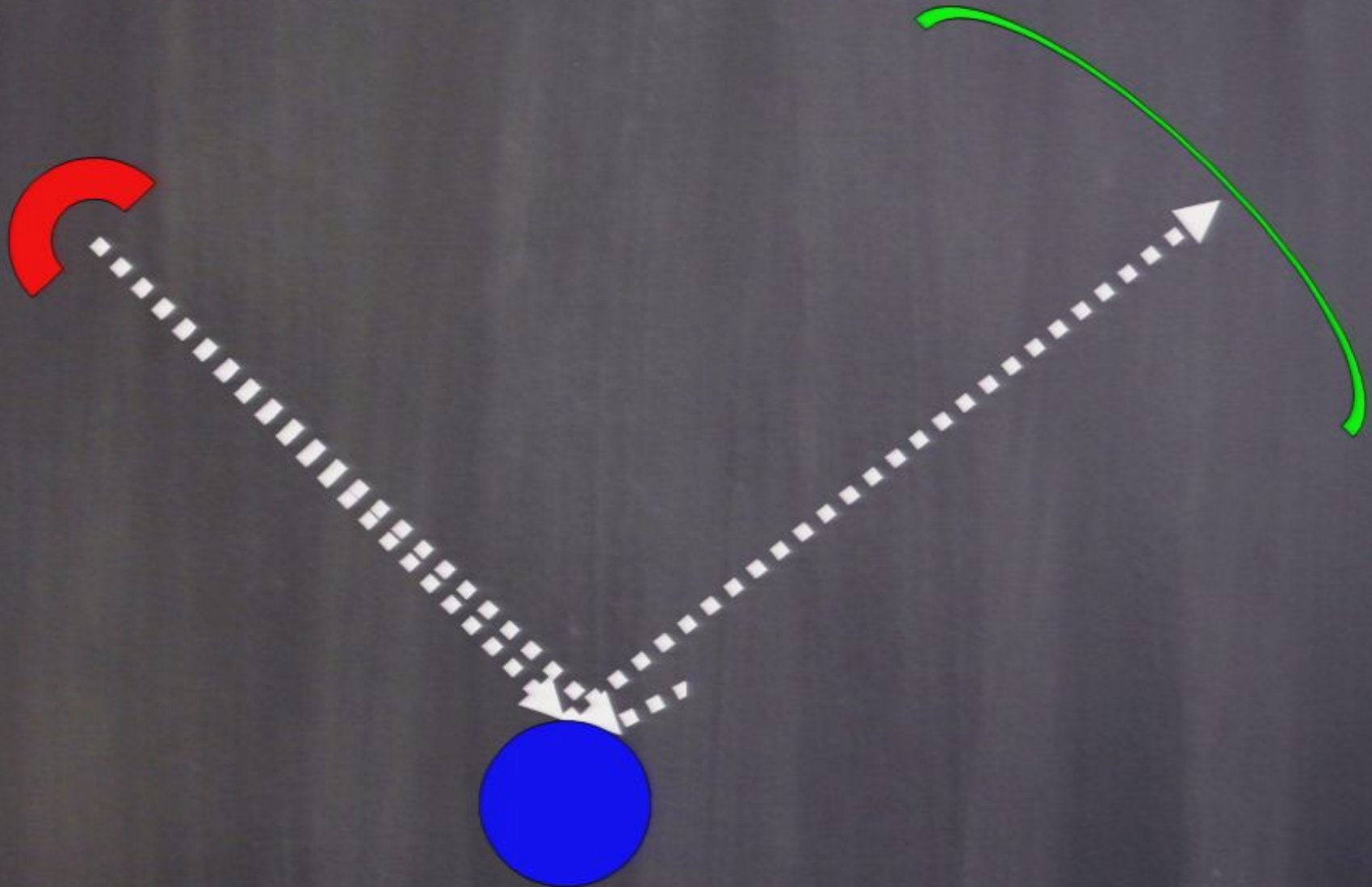
Simplify: Only **ONE** Atom



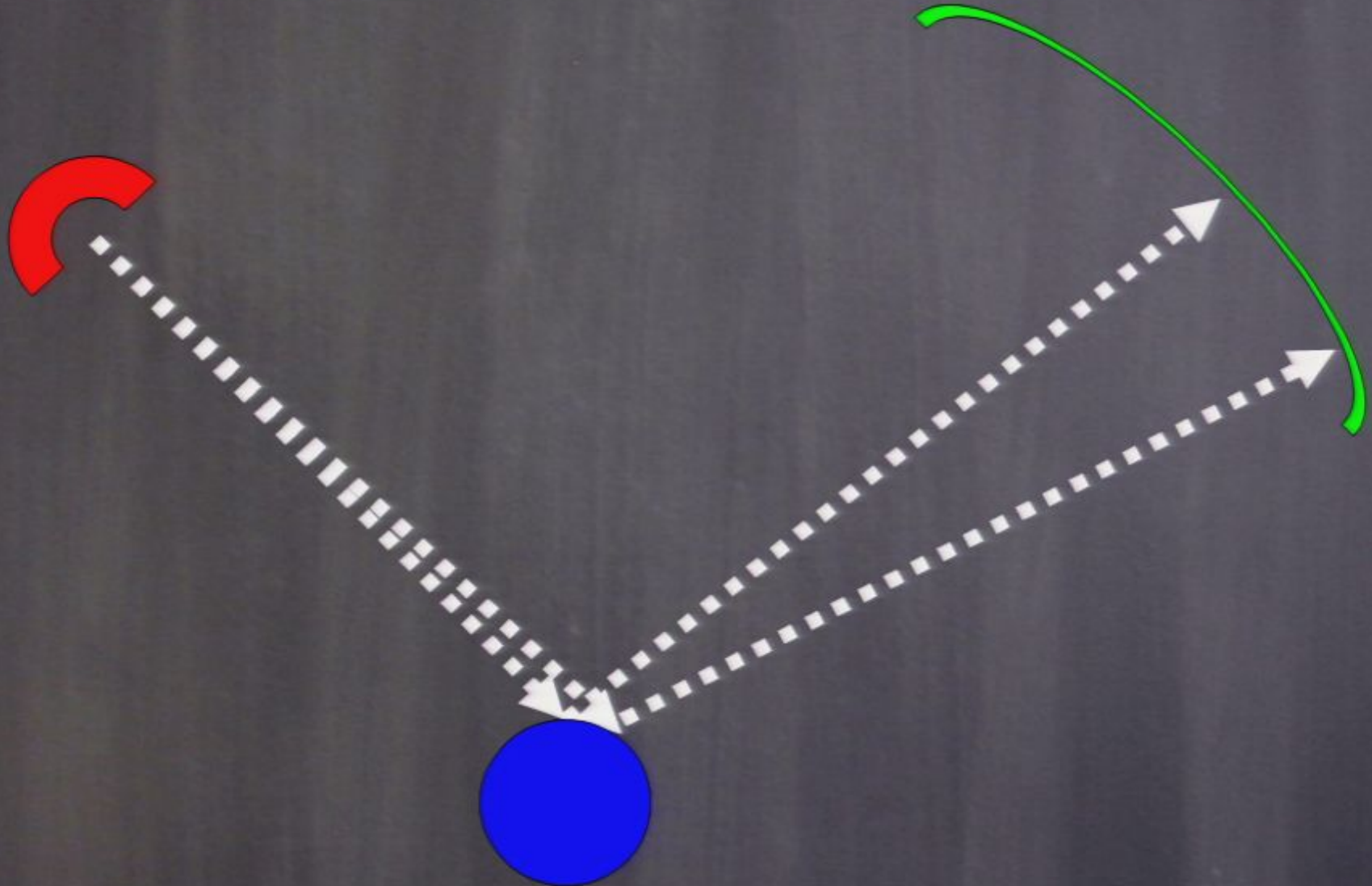
Simplify: Only **ONE** Atom



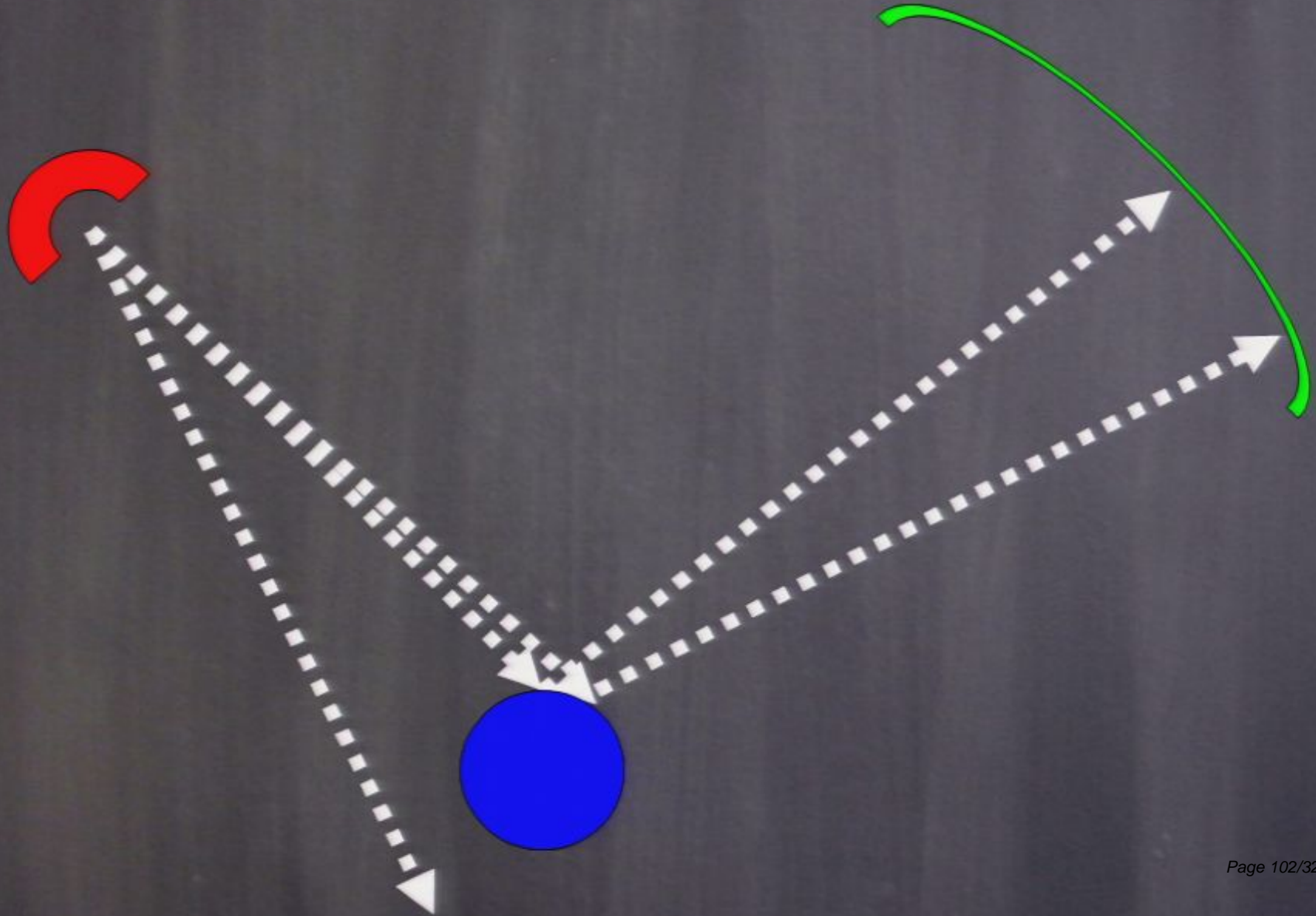
Simplify: Only **ONE** Atom



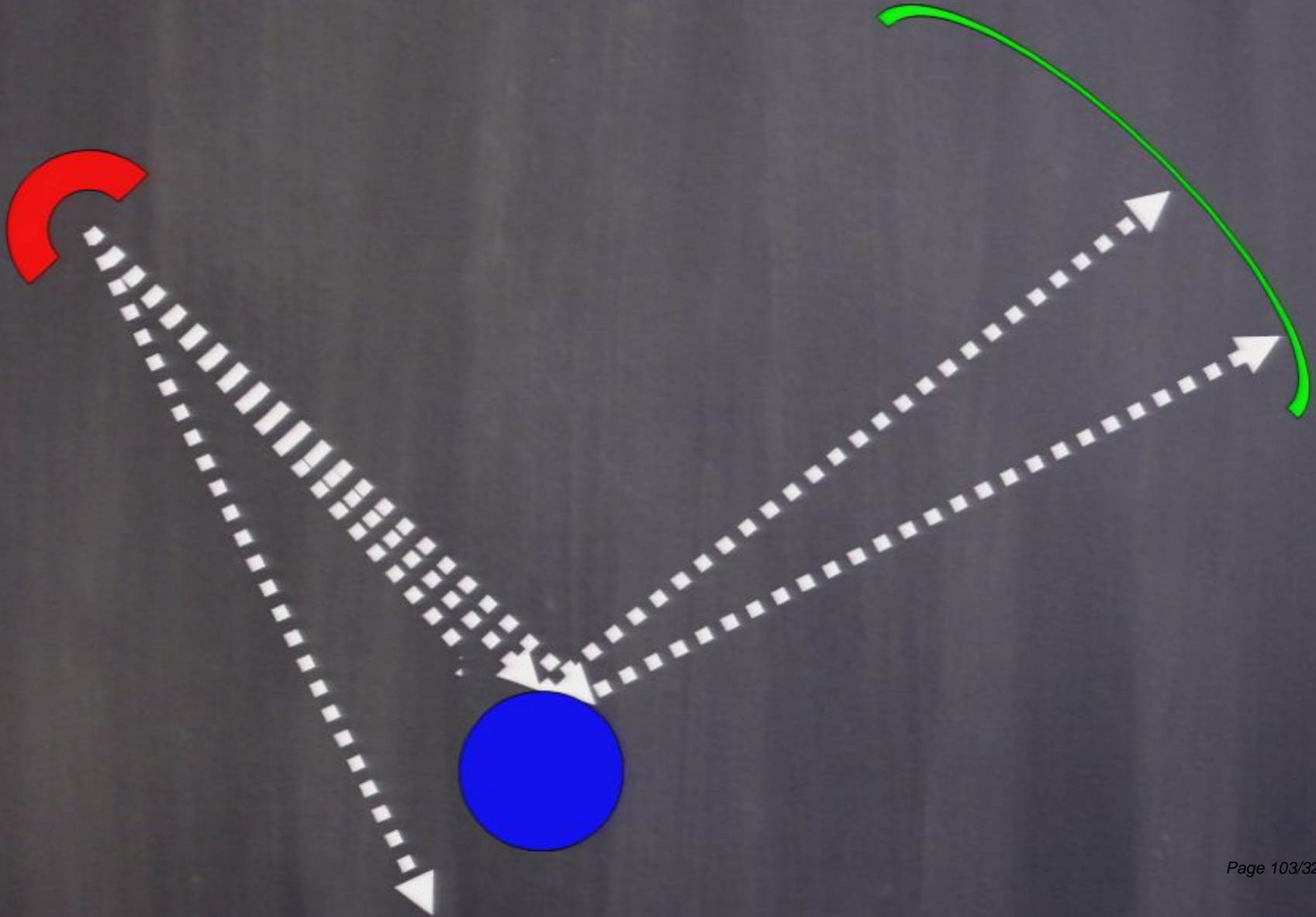
Simplify: Only **ONE** Atom



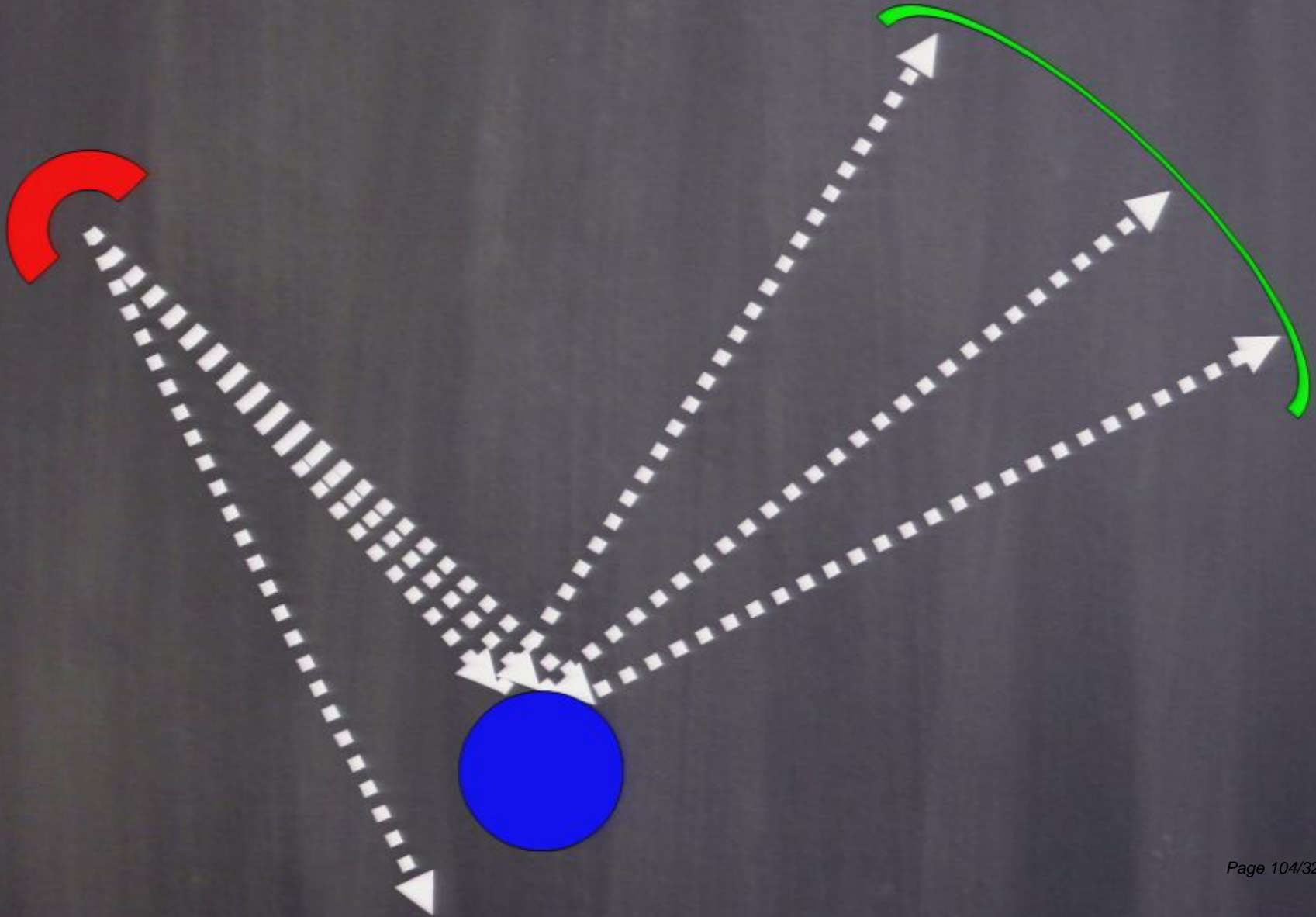
Simplify: Only **ONE** Atom



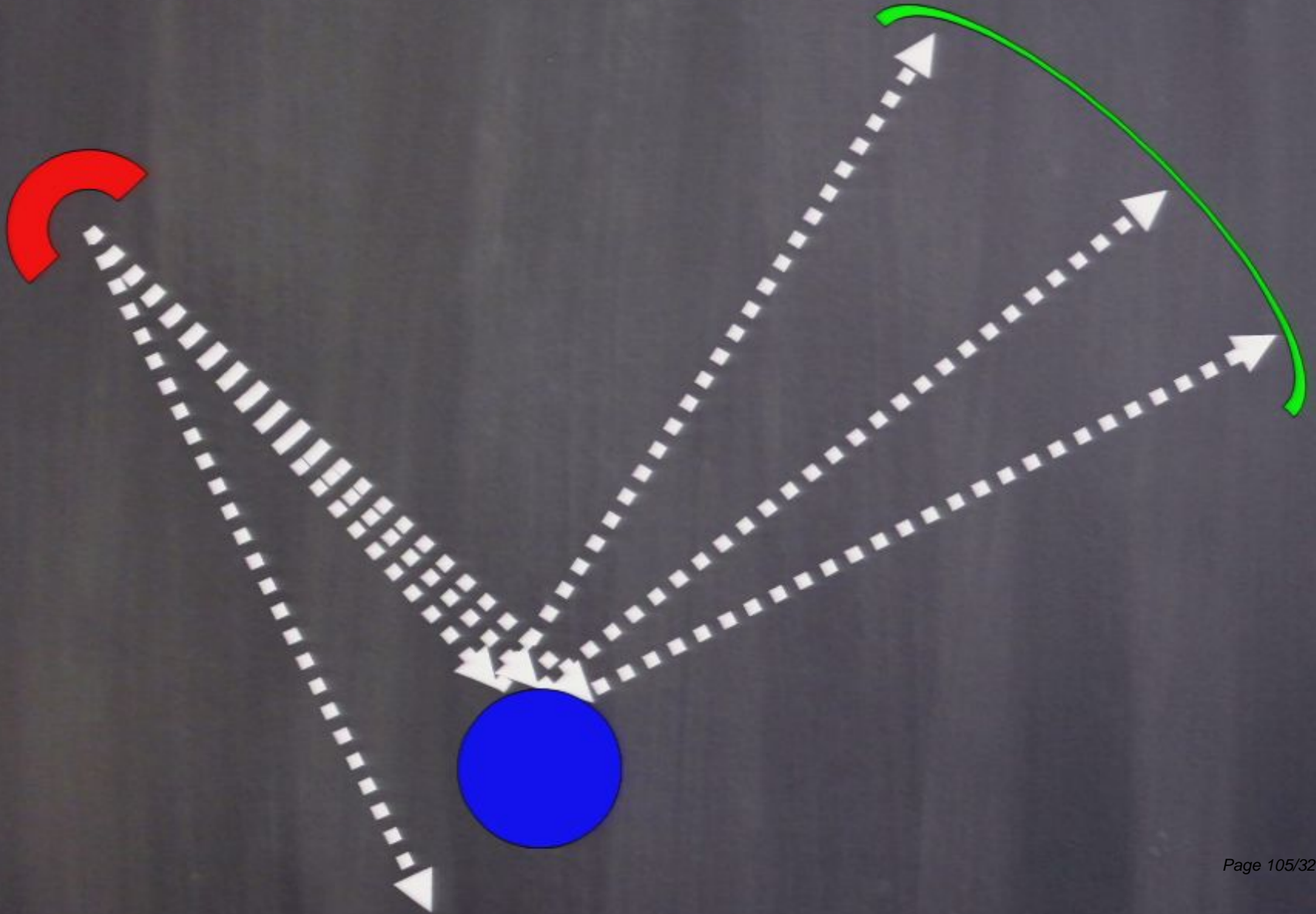
Simplify: Only **ONE** Atom



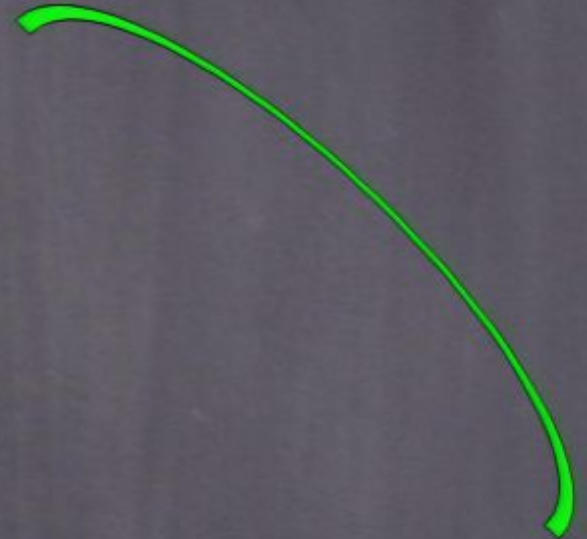
Simplify: Only **ONE** Atom



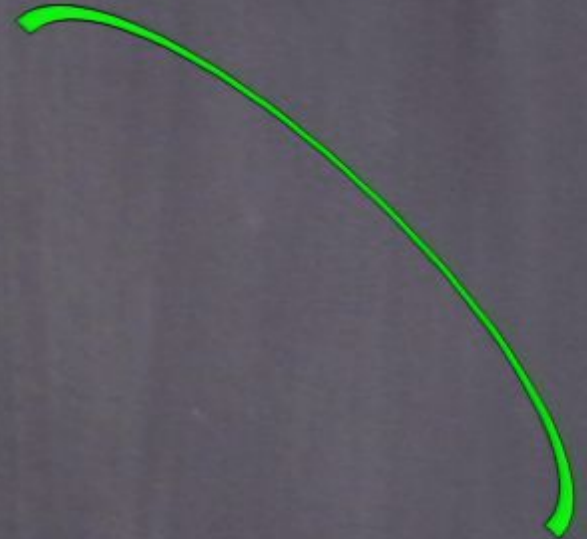
Expect?



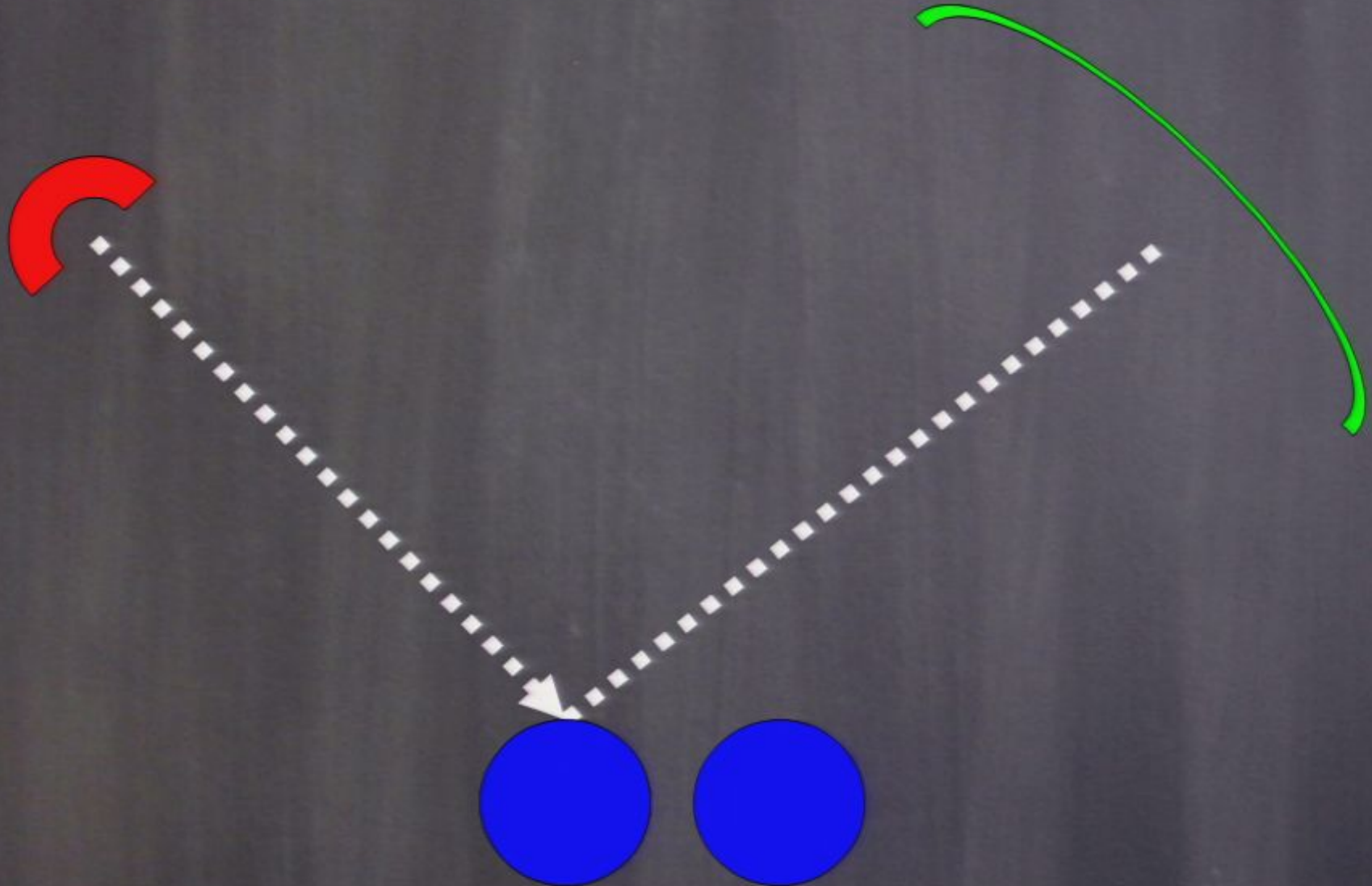
Bring in a **SECOND** Atom



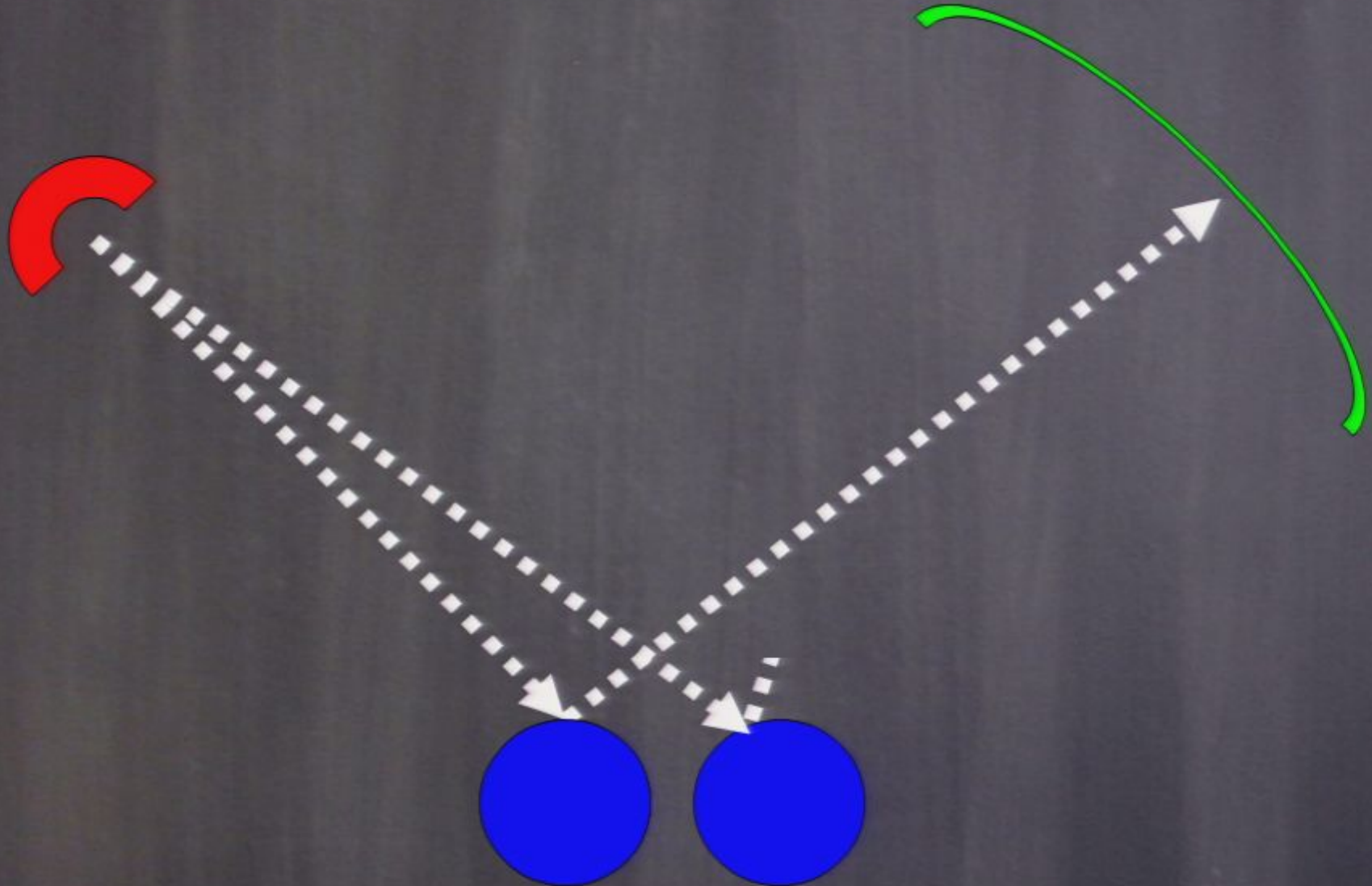
Bring in a **SECOND** Atom



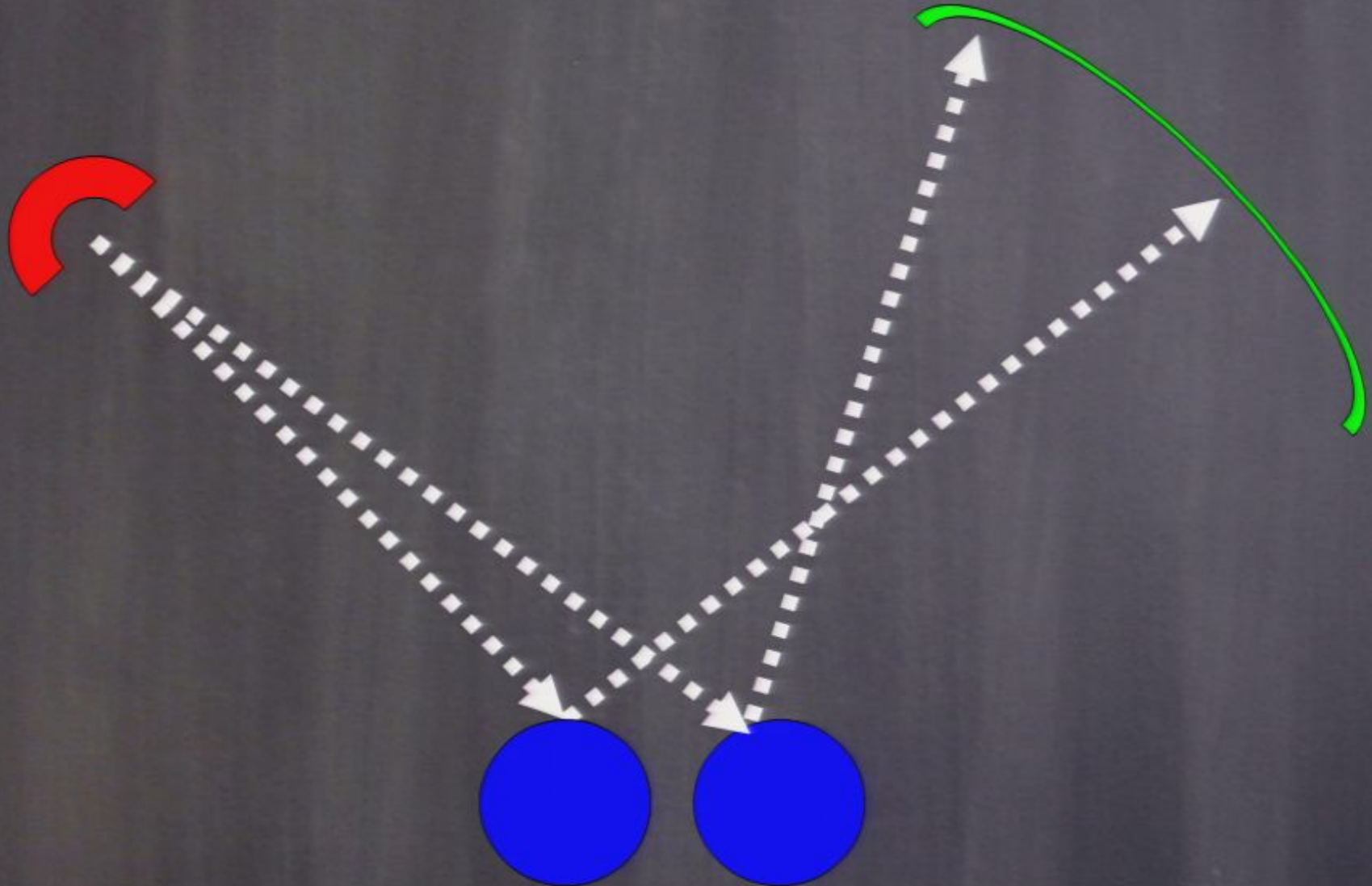
Bring in a **SECOND** Atom



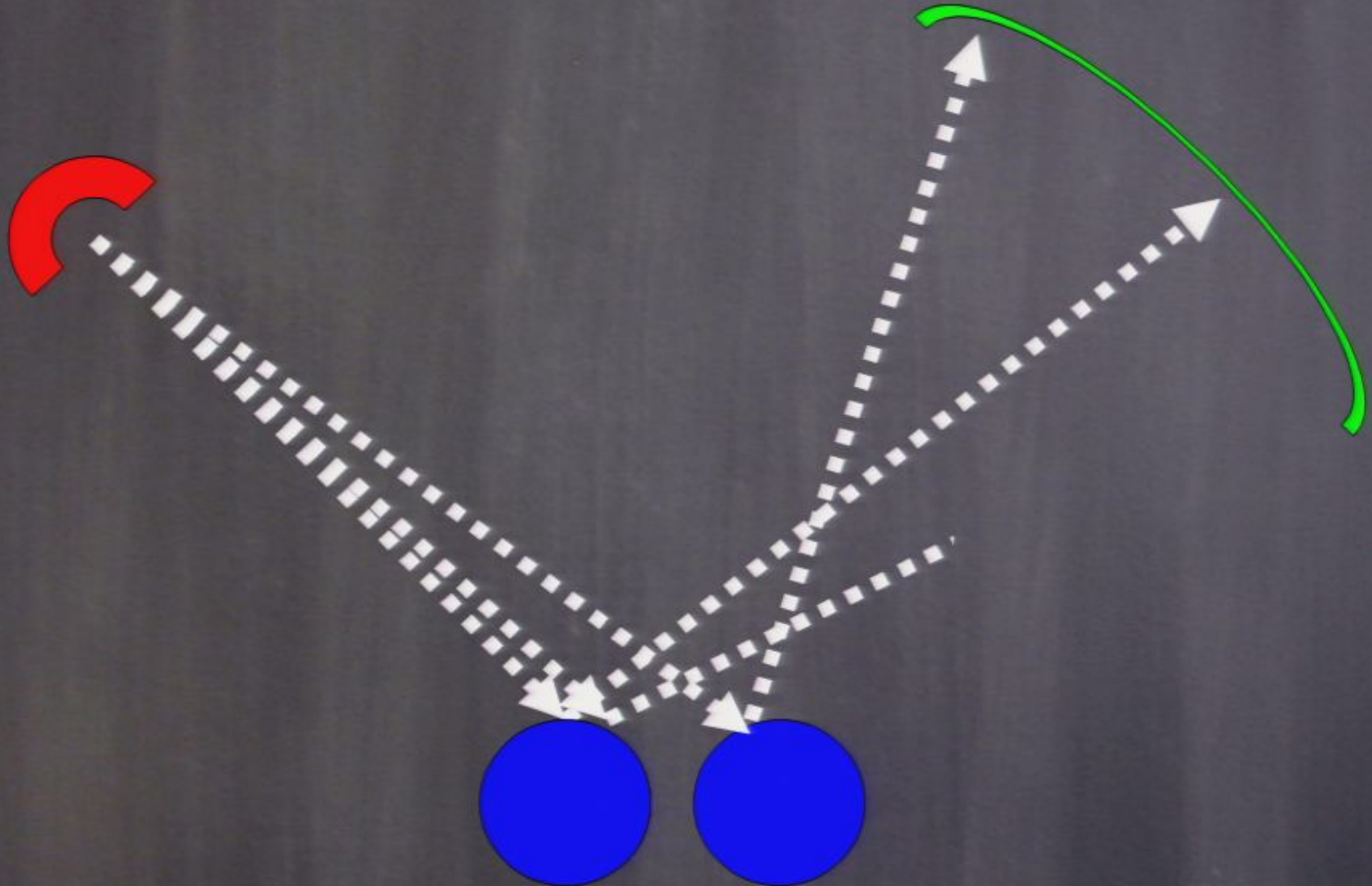
Bring in a **SECOND** Atom



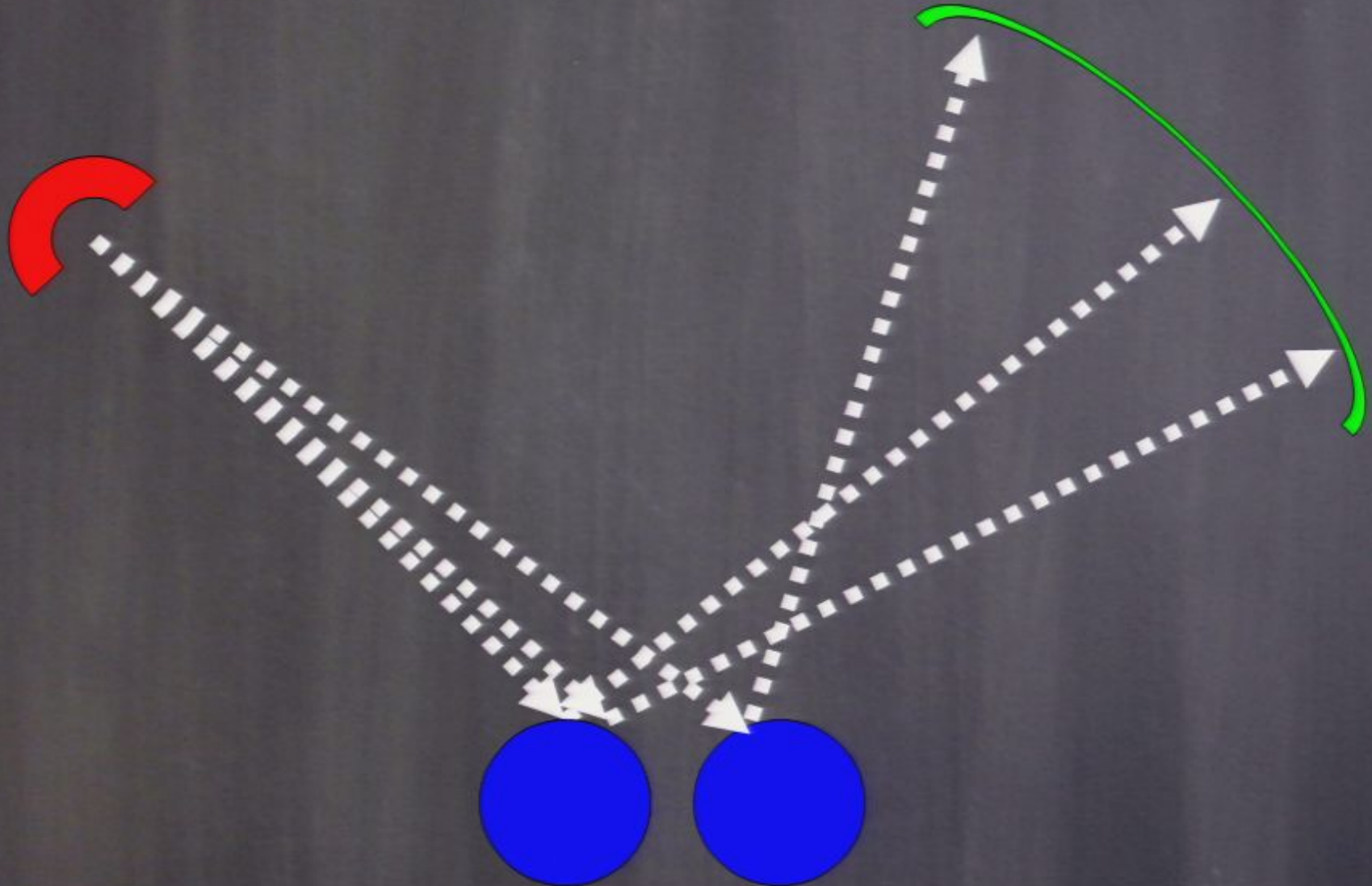
Bring in a **SECOND** Atom



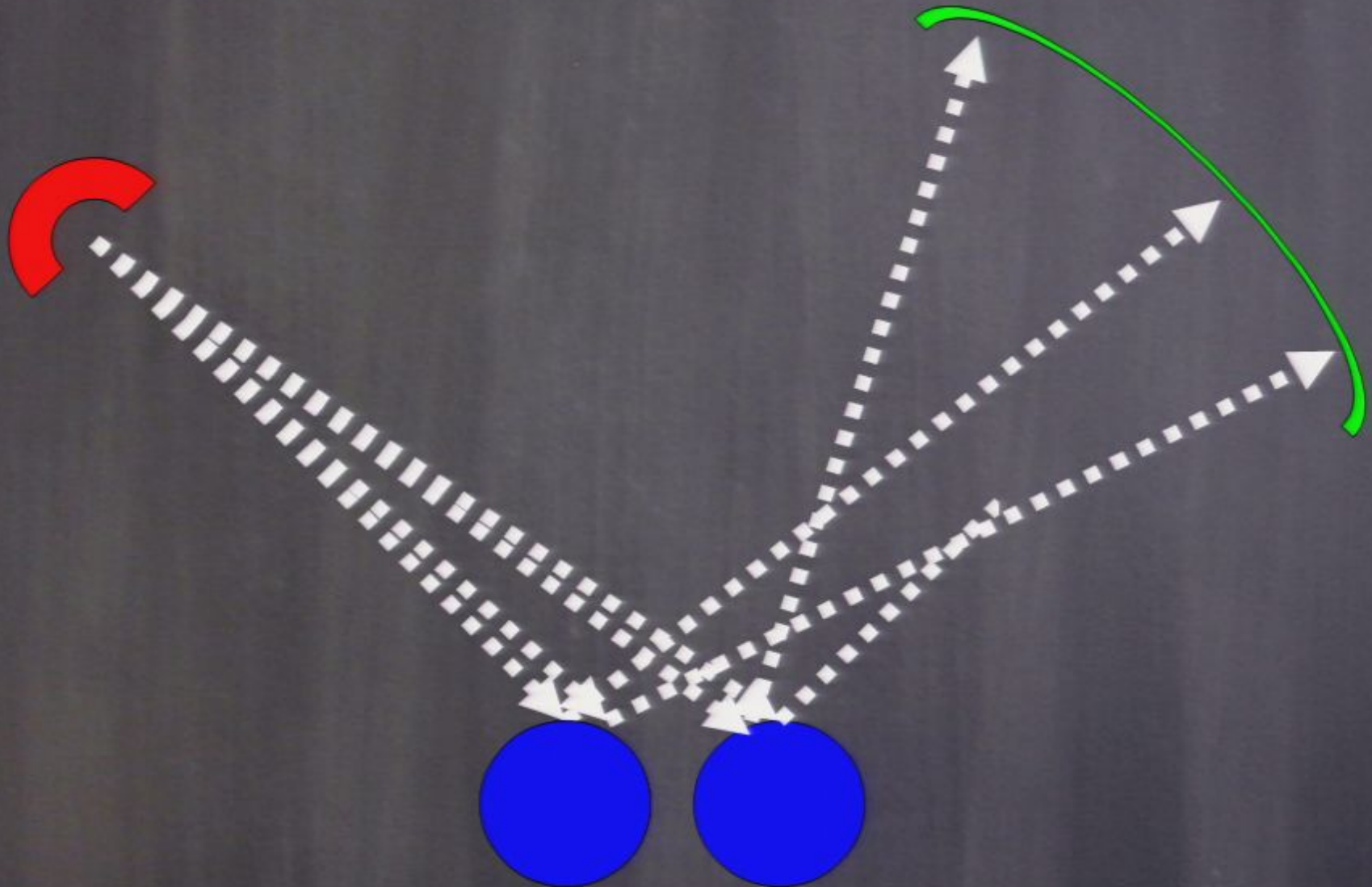
Bring in a **SECOND** Atom



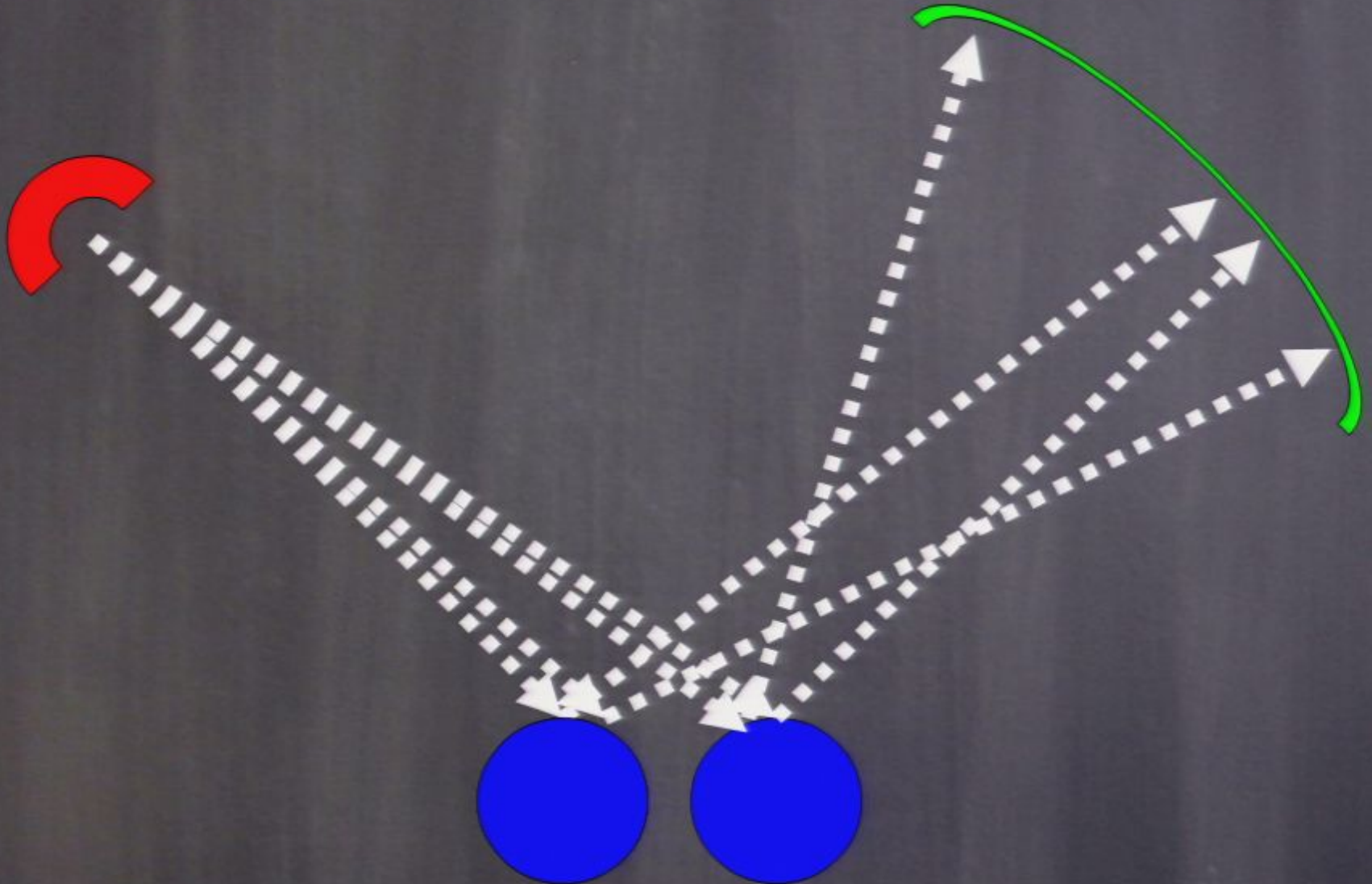
Bring in a **SECOND** Atom



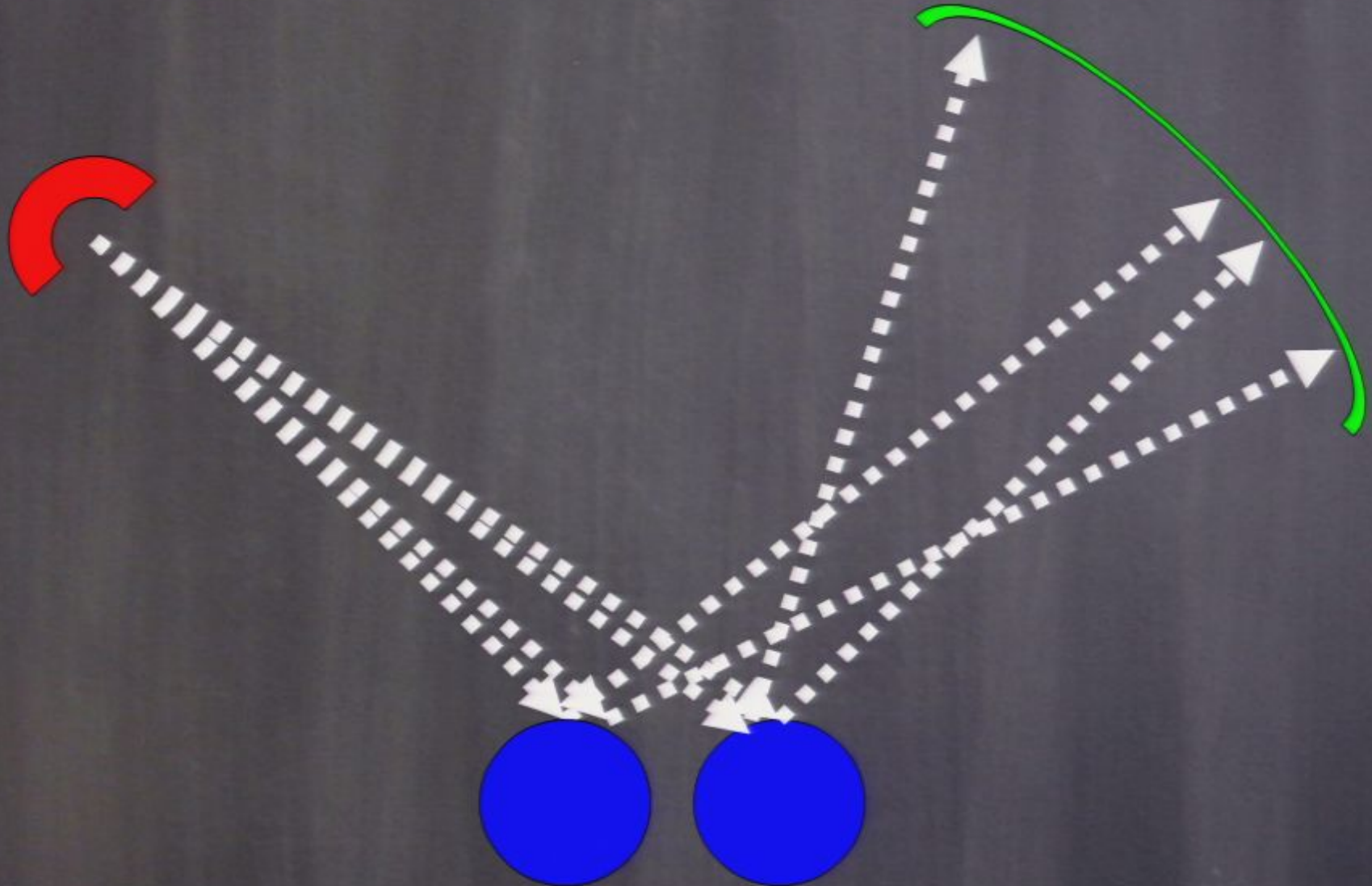
Bring in a **SECOND** Atom



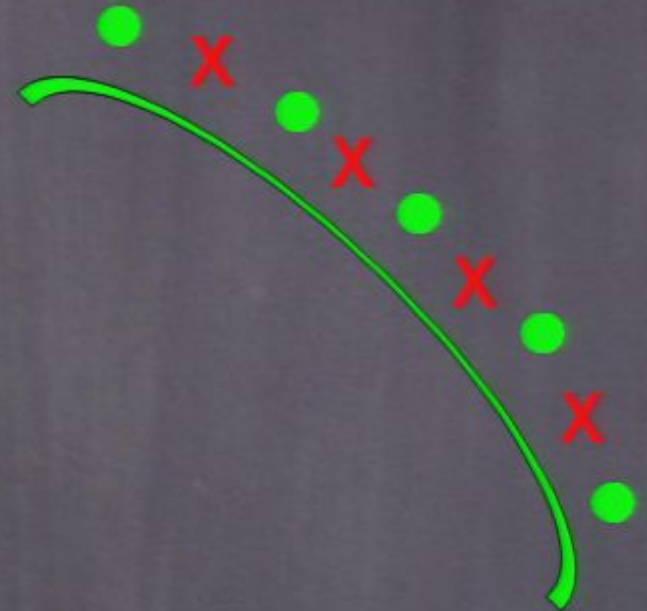
Expect?



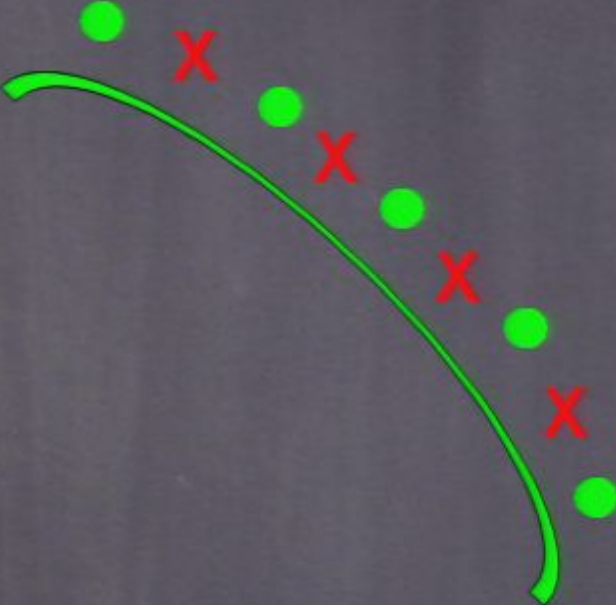
Actual: Pattern of Hits!



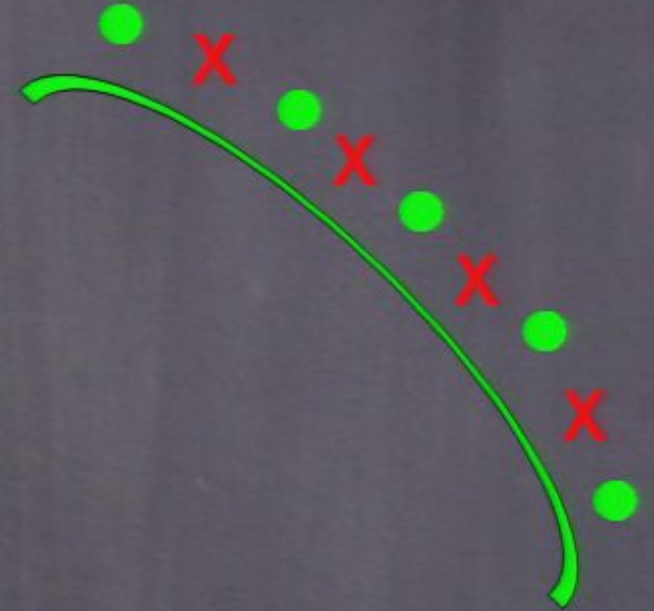
Actual: Pattern of Hits!



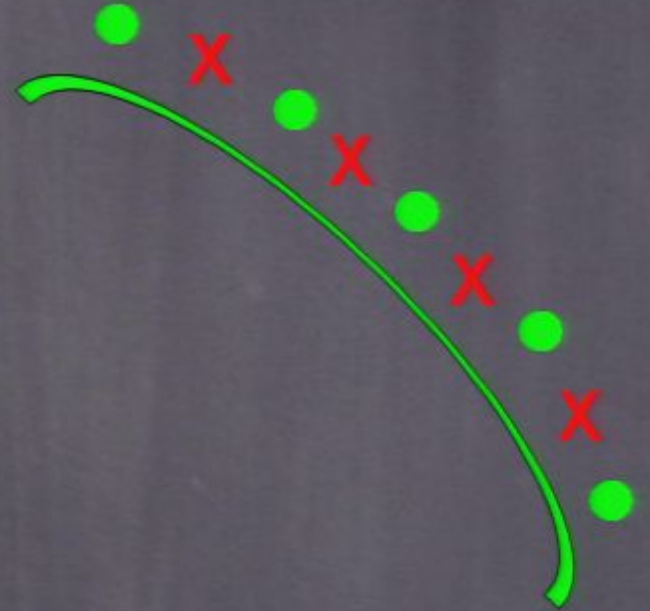
How is this POSSIBLE?



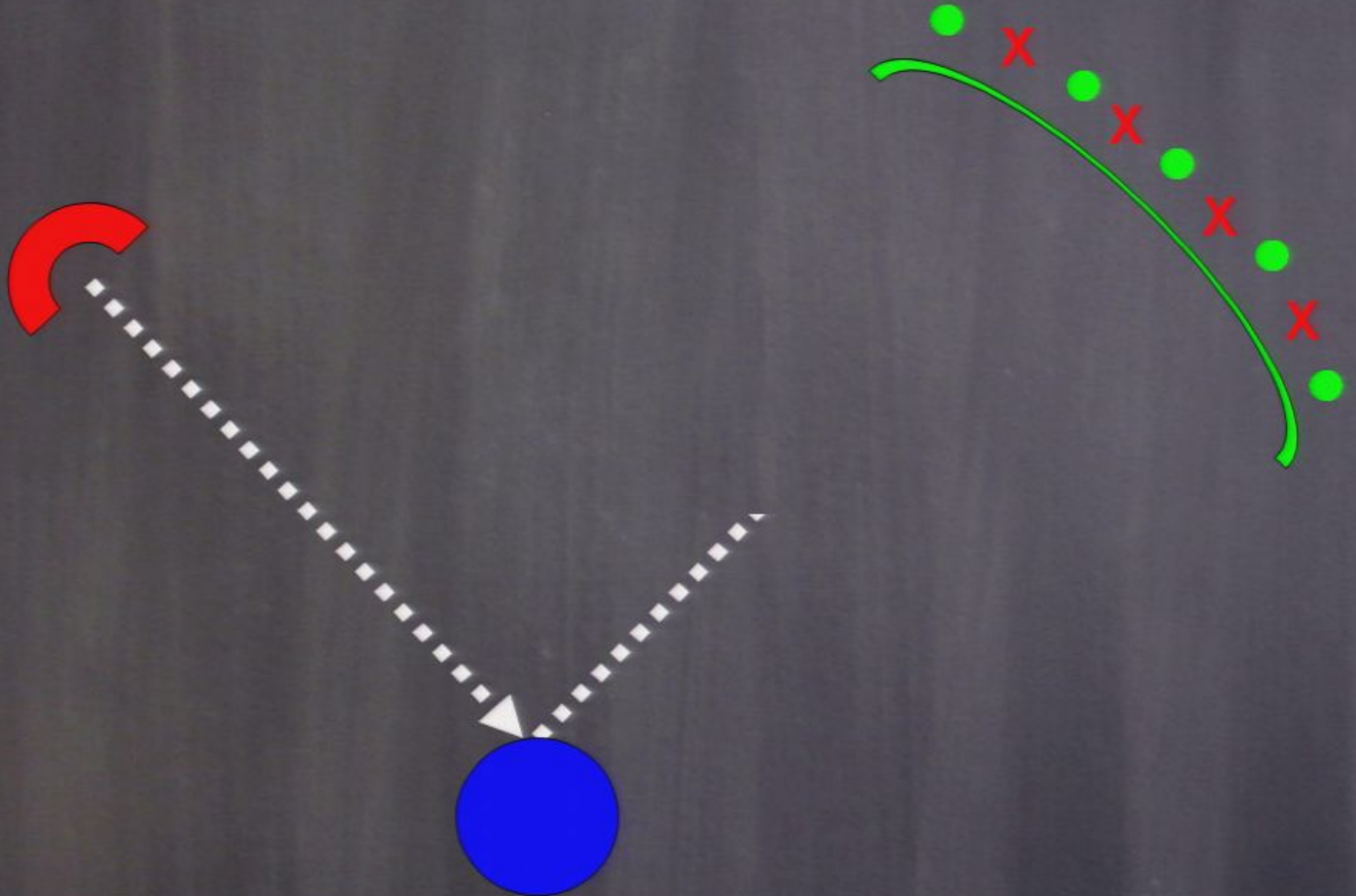
How is this POSSIBLE?



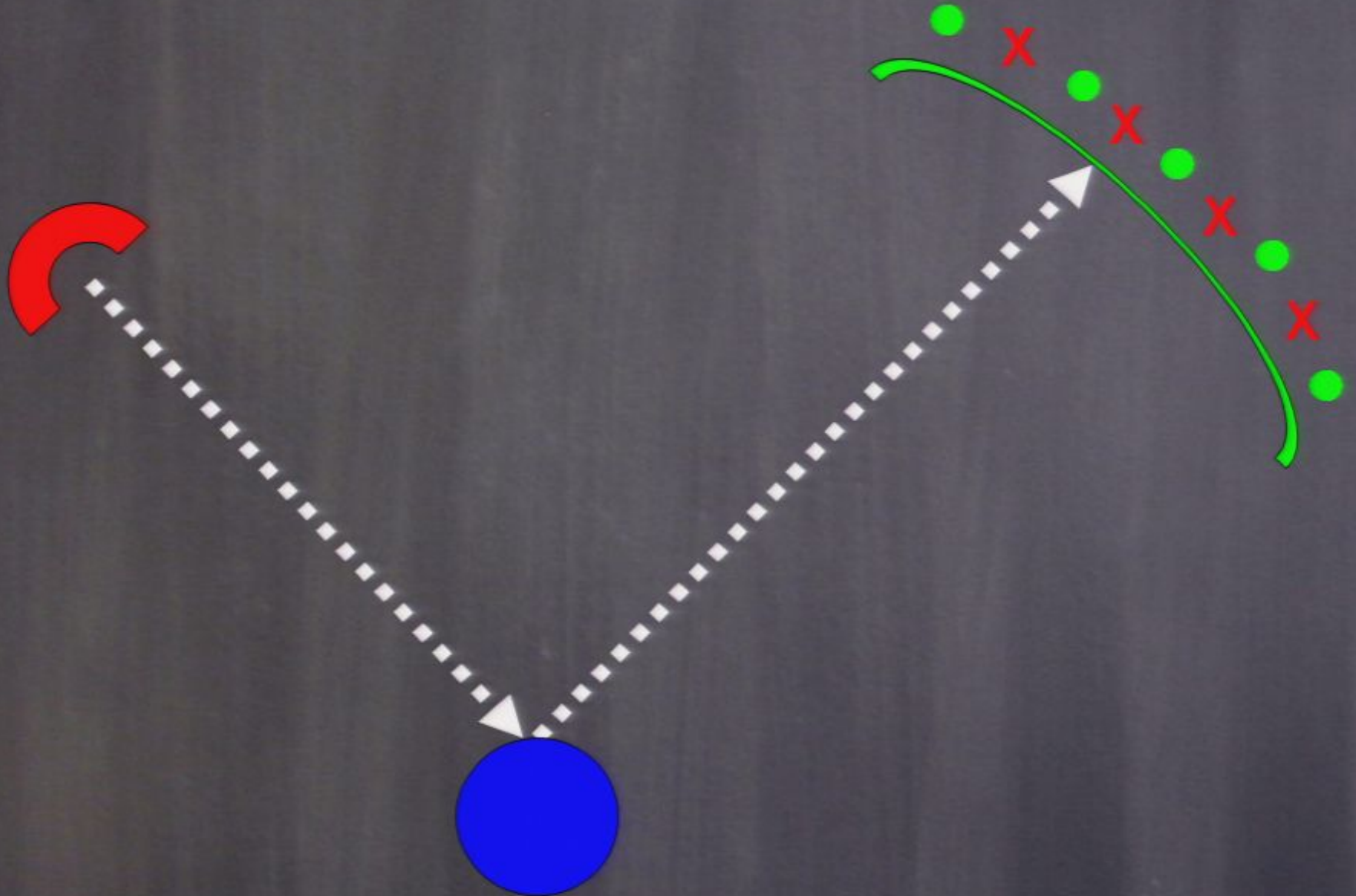
How is this POSSIBLE?



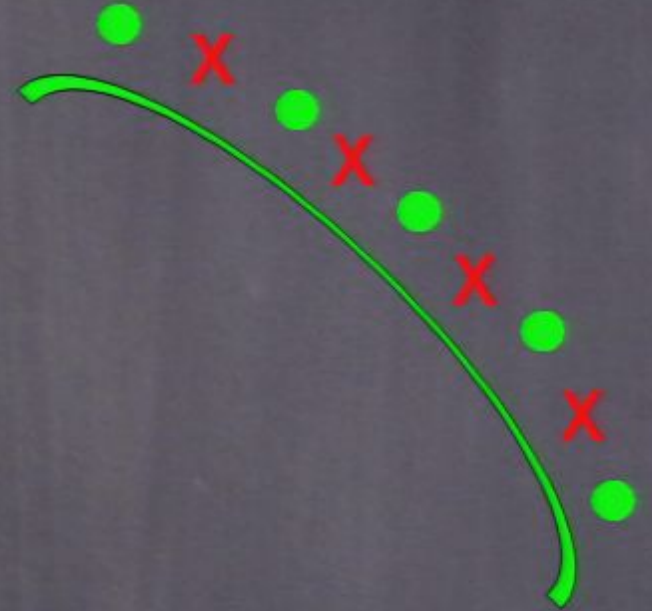
How is this **POSSIBLE?**



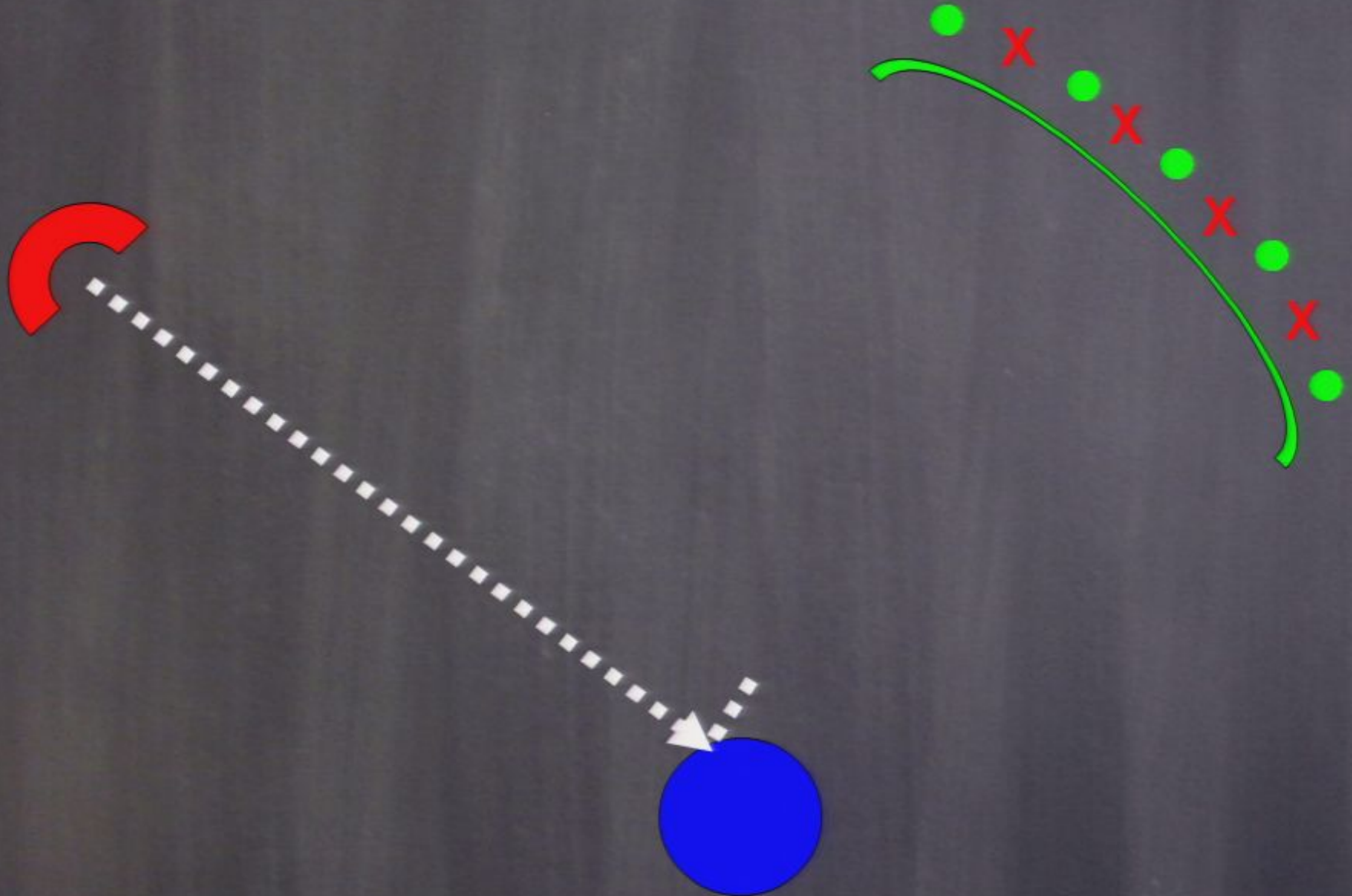
How is this POSSIBLE?



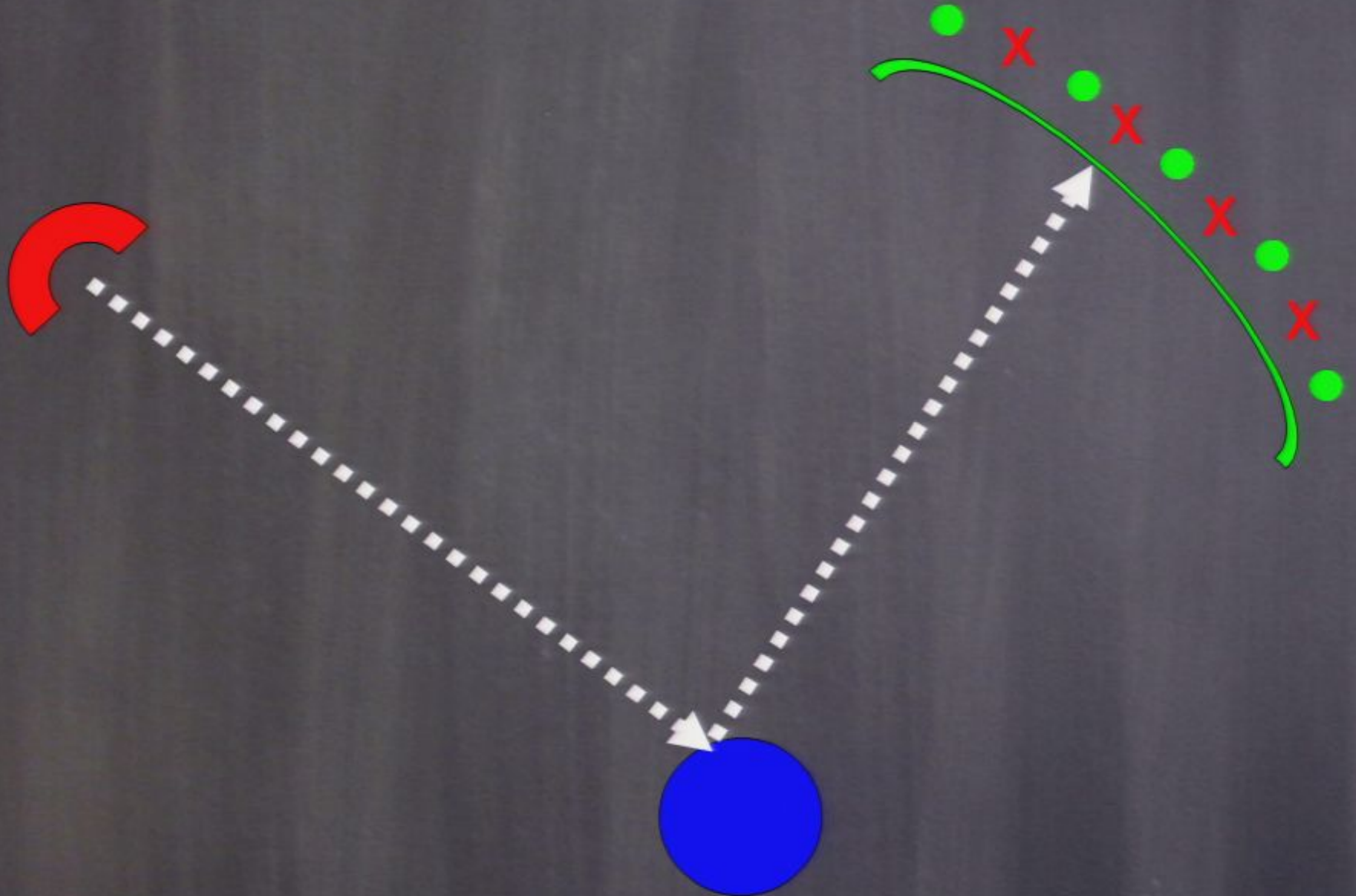
How is this POSSIBLE?



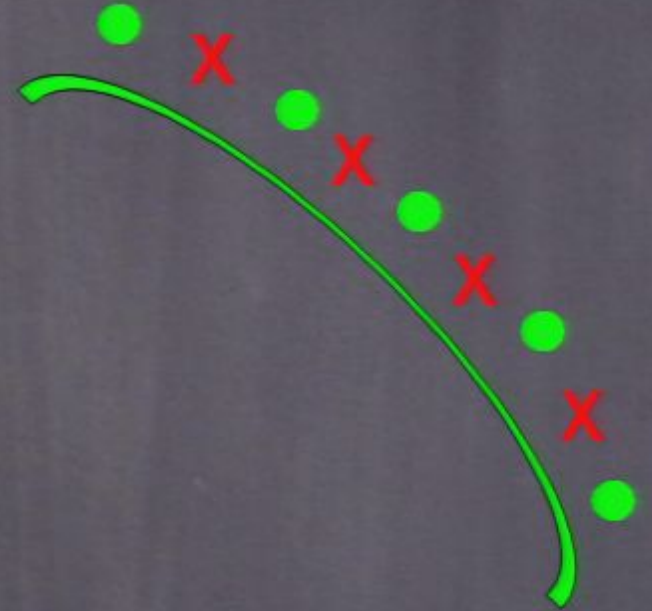
How is this POSSIBLE?



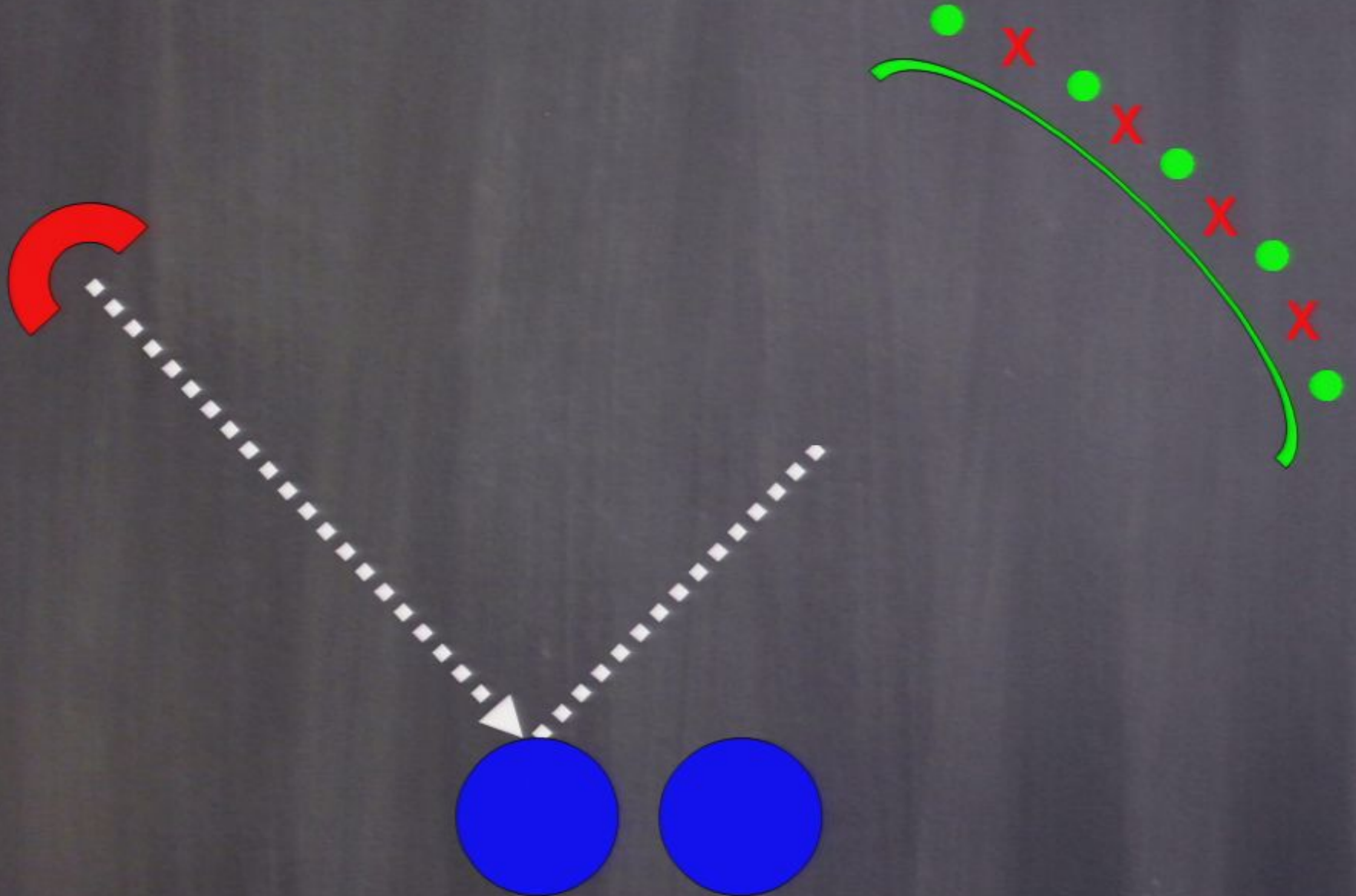
How is this POSSIBLE?



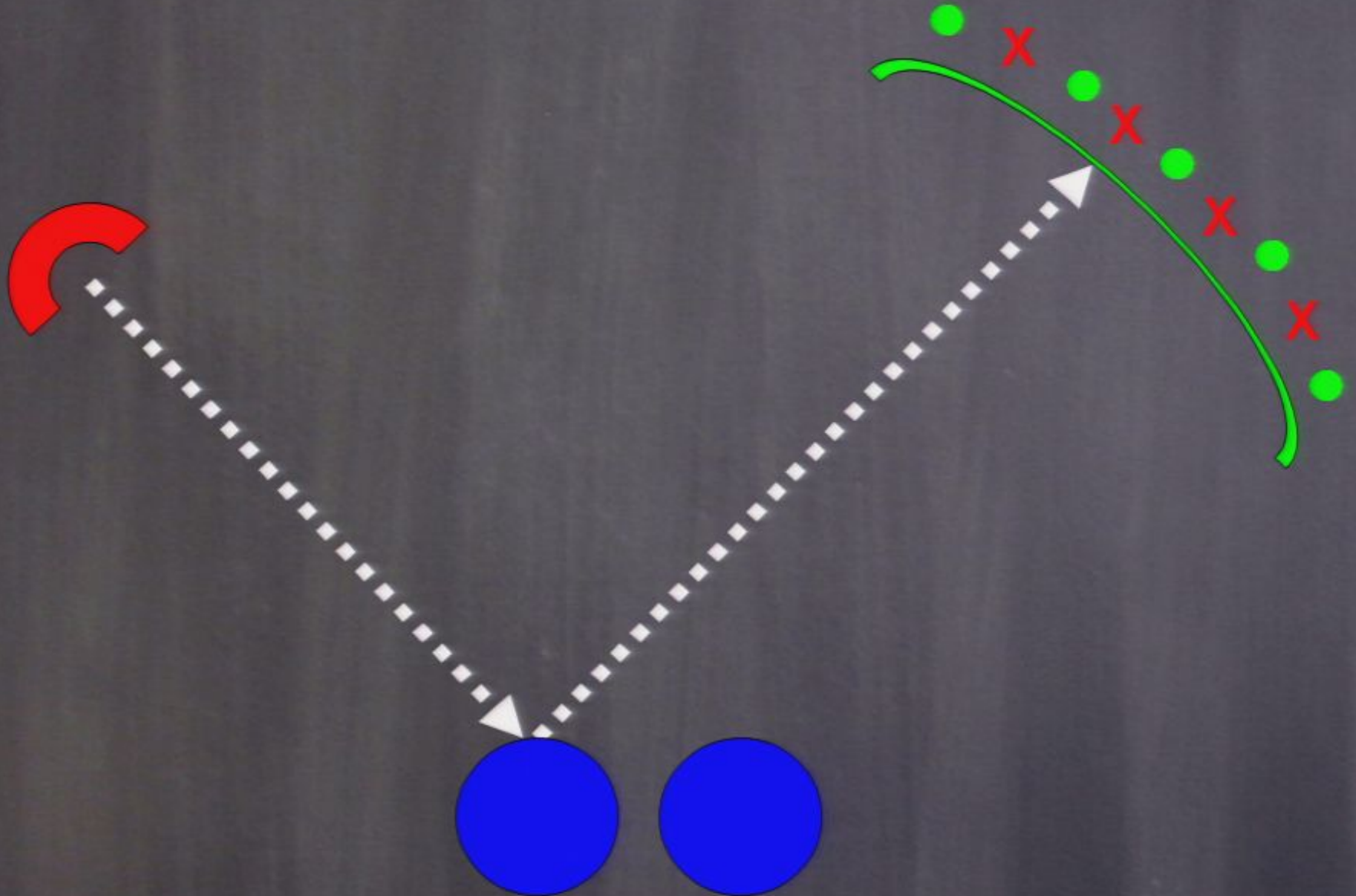
How is this POSSIBLE?



How is this **POSSIBLE?**

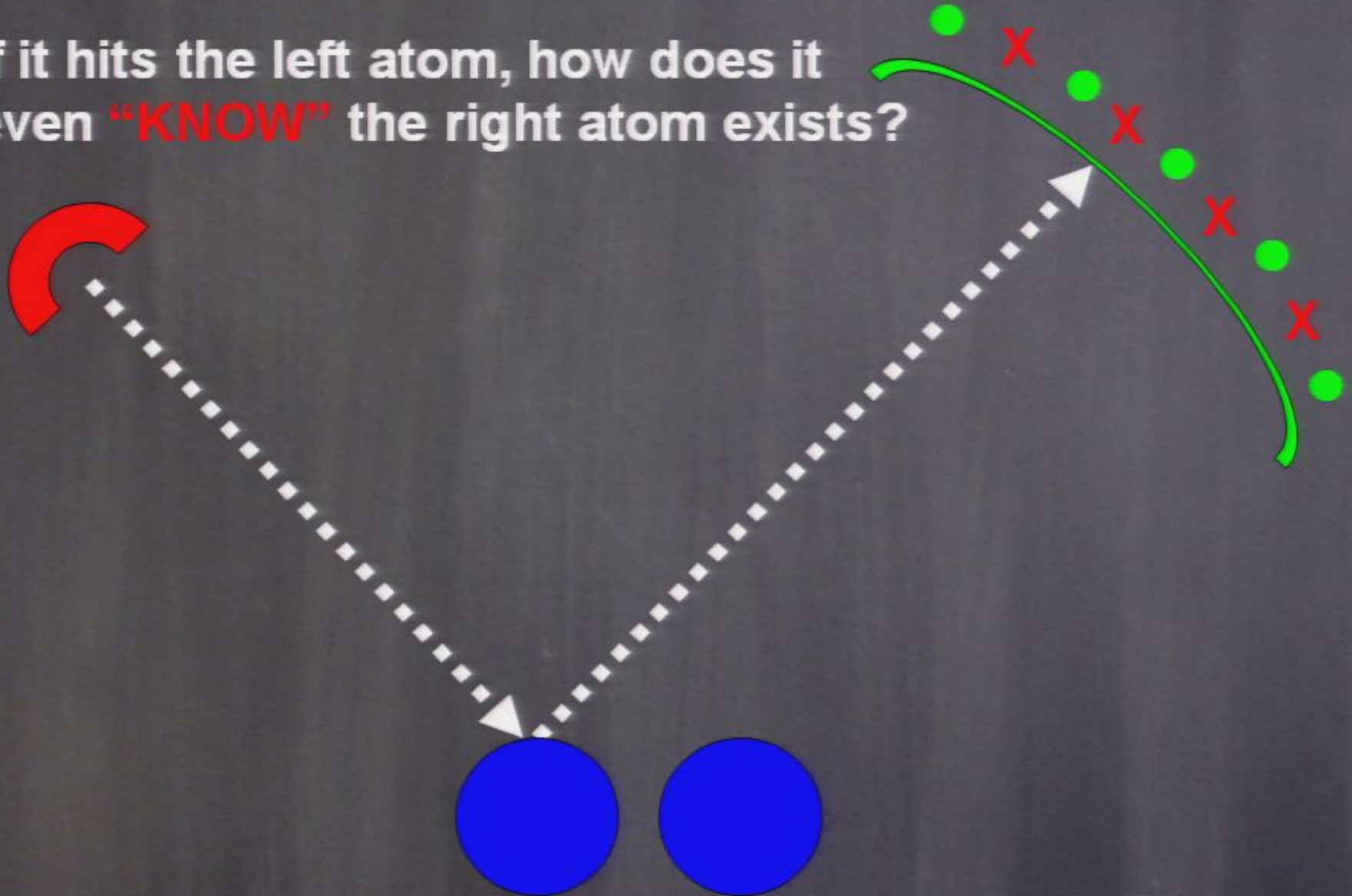


How is this **POSSIBLE?**



How is this **POSSIBLE**?

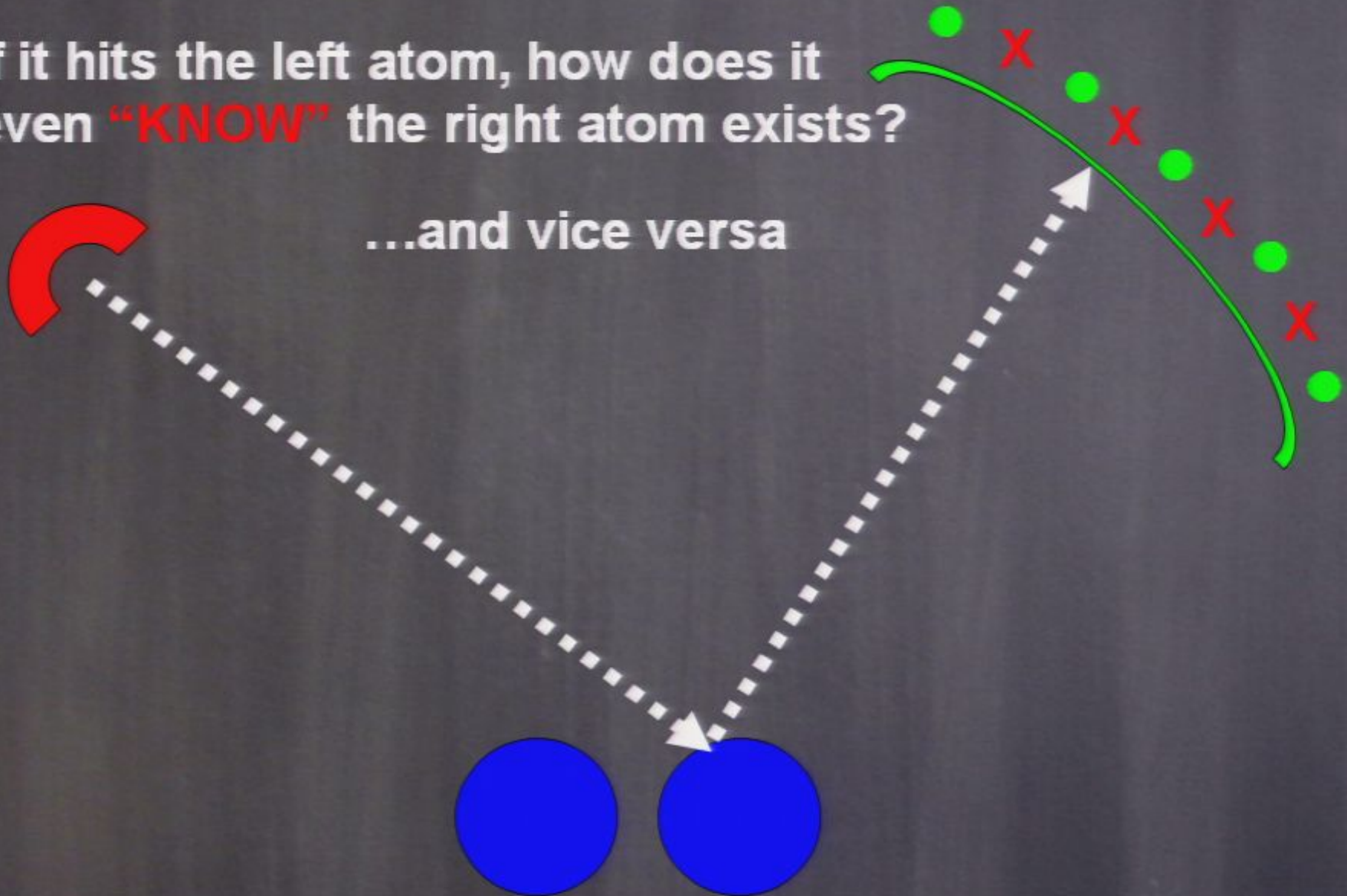
If it hits the left atom, how does it even **“KNOW”** the right atom exists?



How is this **POSSIBLE**?

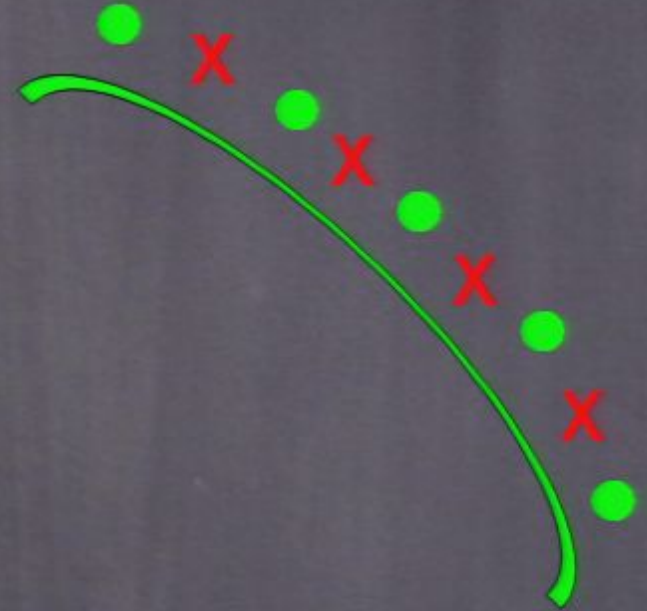
If it hits the left atom, how does it even **“KNOW”** the right atom exists?

...and vice versa



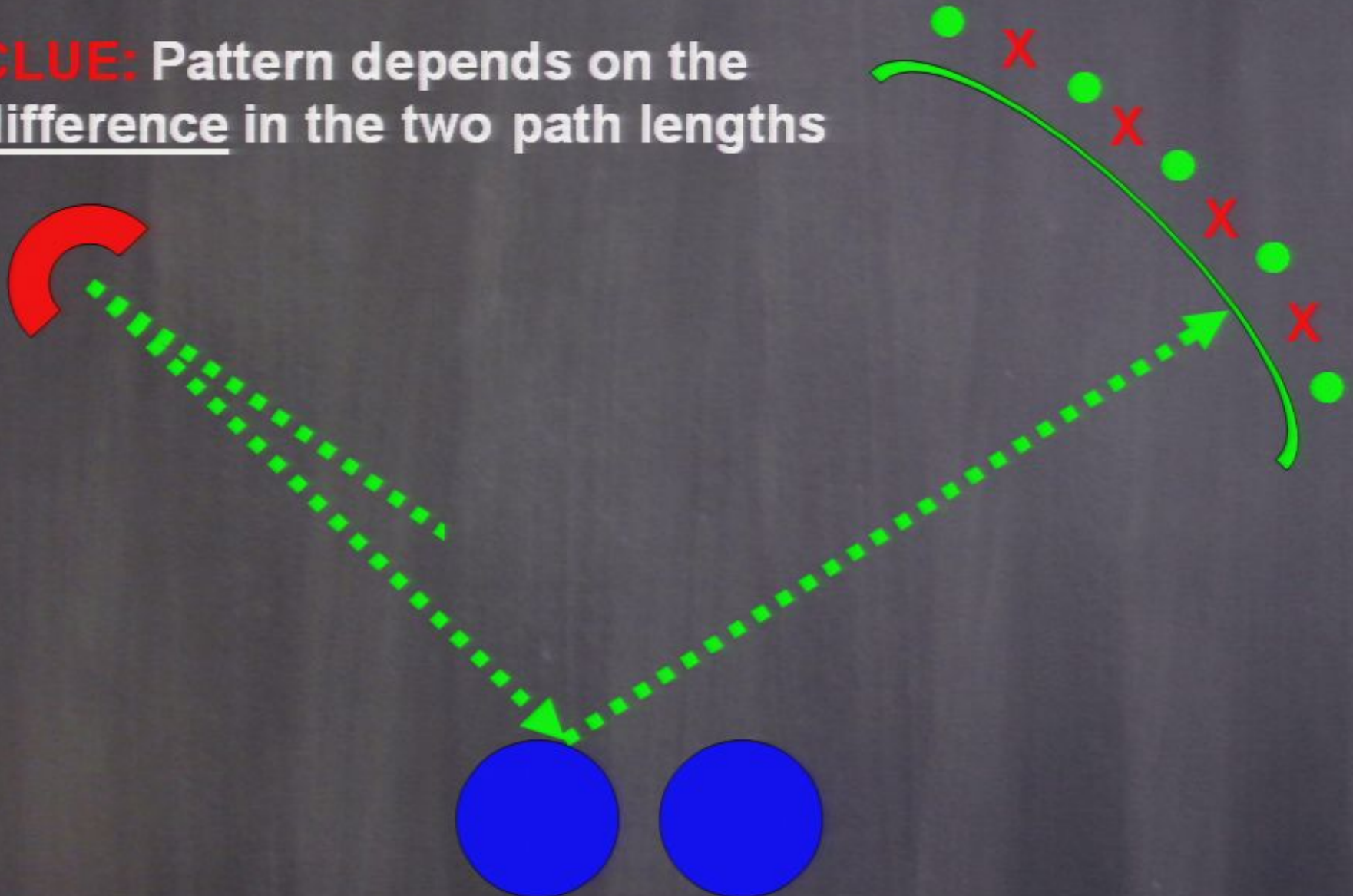
How is this POSSIBLE?

CLUE: Pattern depends on the difference in the two path lengths



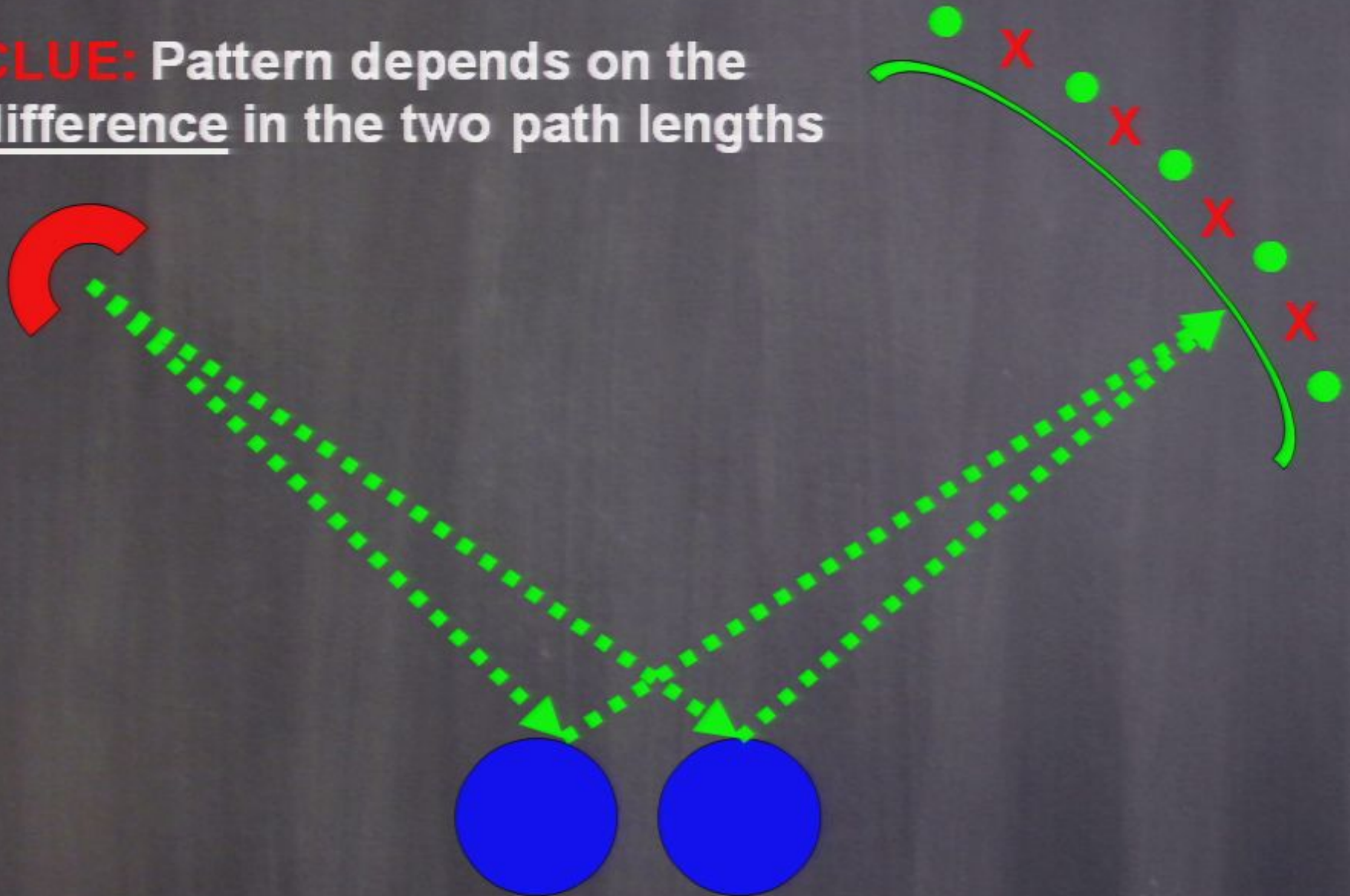
How is this **POSSIBLE?**

CLUE: Pattern depends on the difference in the two path lengths



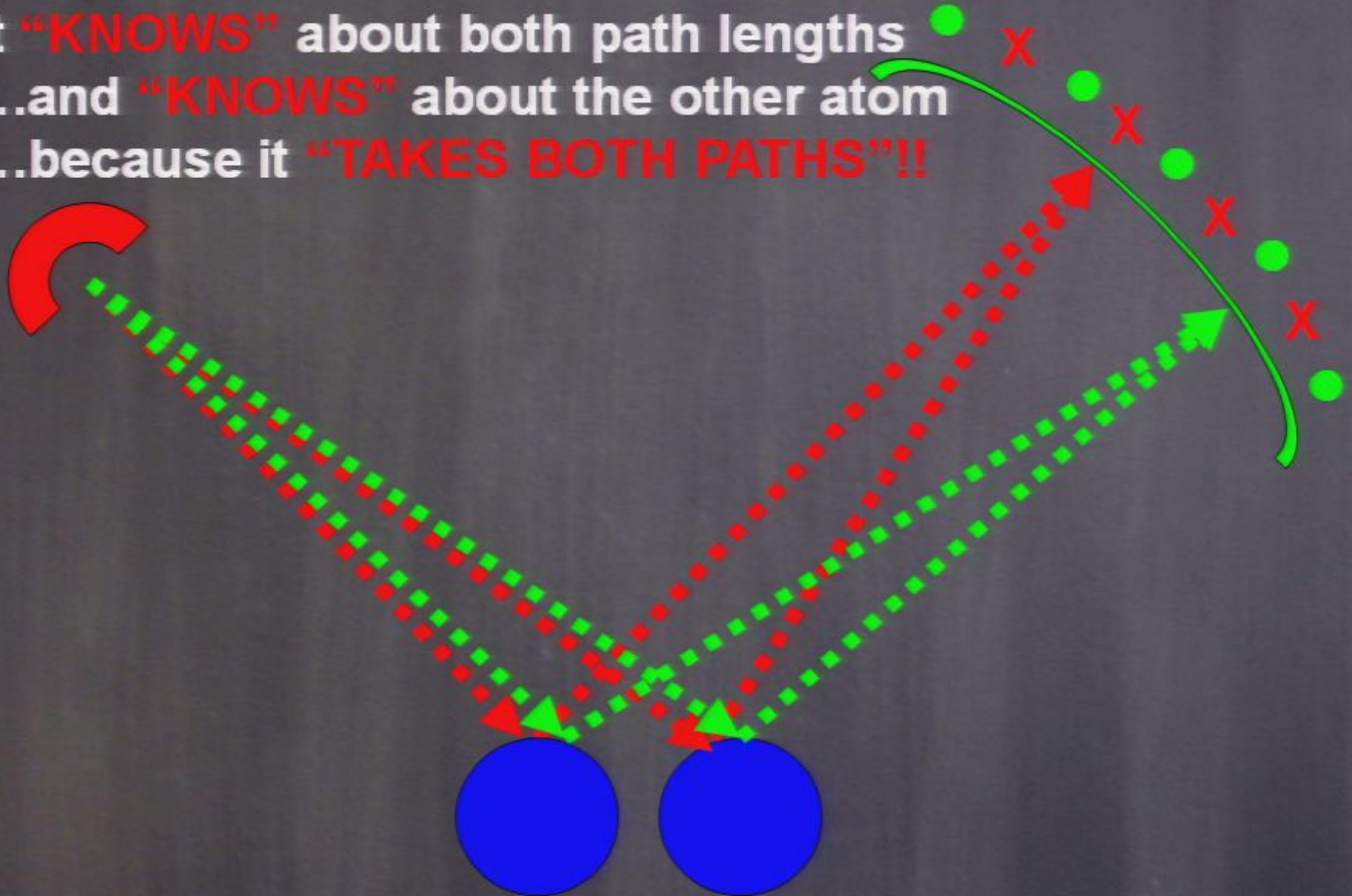
How is this **POSSIBLE?**

CLUE: Pattern depends on the difference in the two path lengths



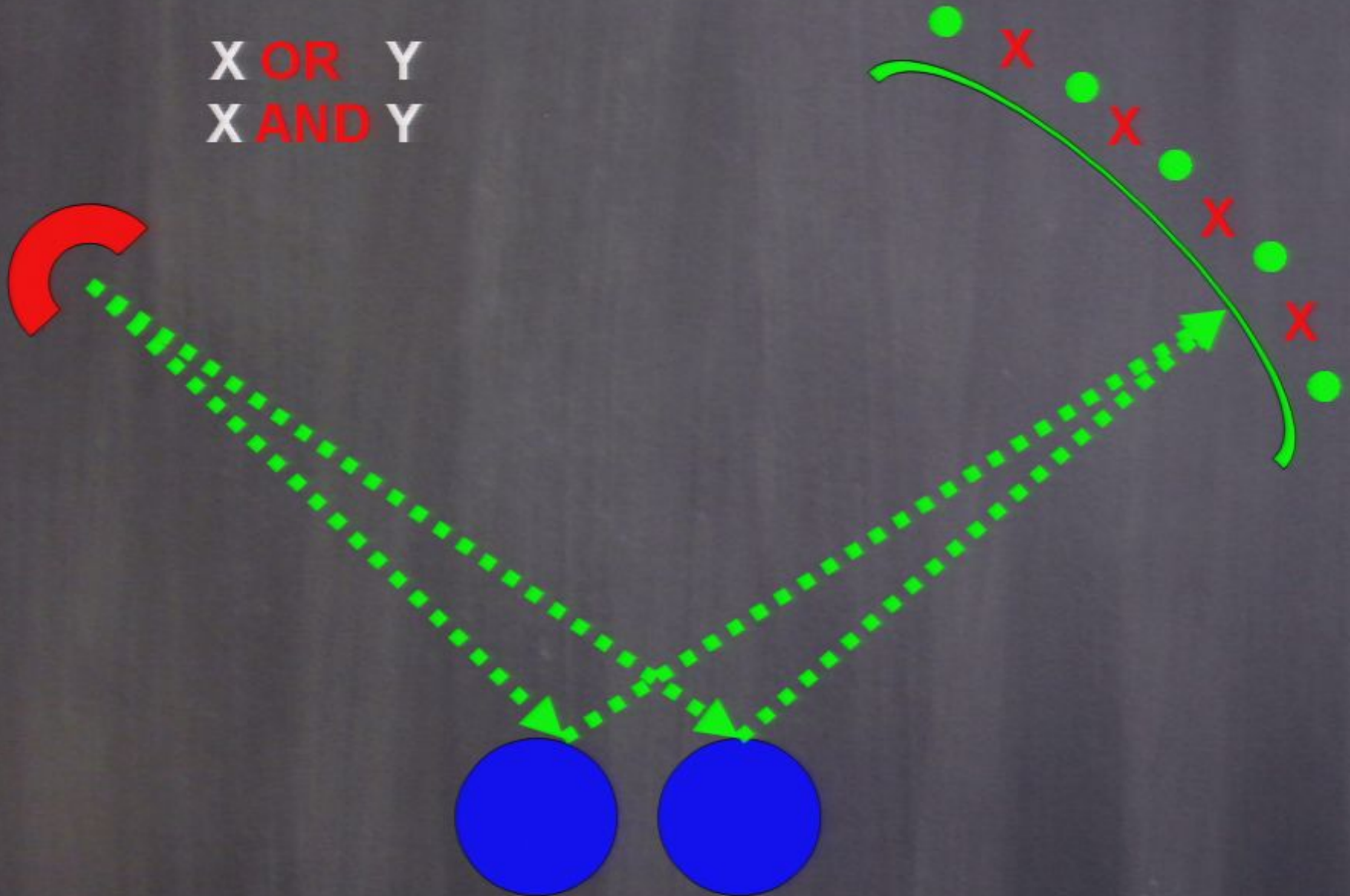
How is this **POSSIBLE?**

It **"KNOWS"** about both path lengths
...and **"KNOWS"** about the other atom
...because it **"TAKES BOTH PATHS"!!**



How is this POSSIBLE?

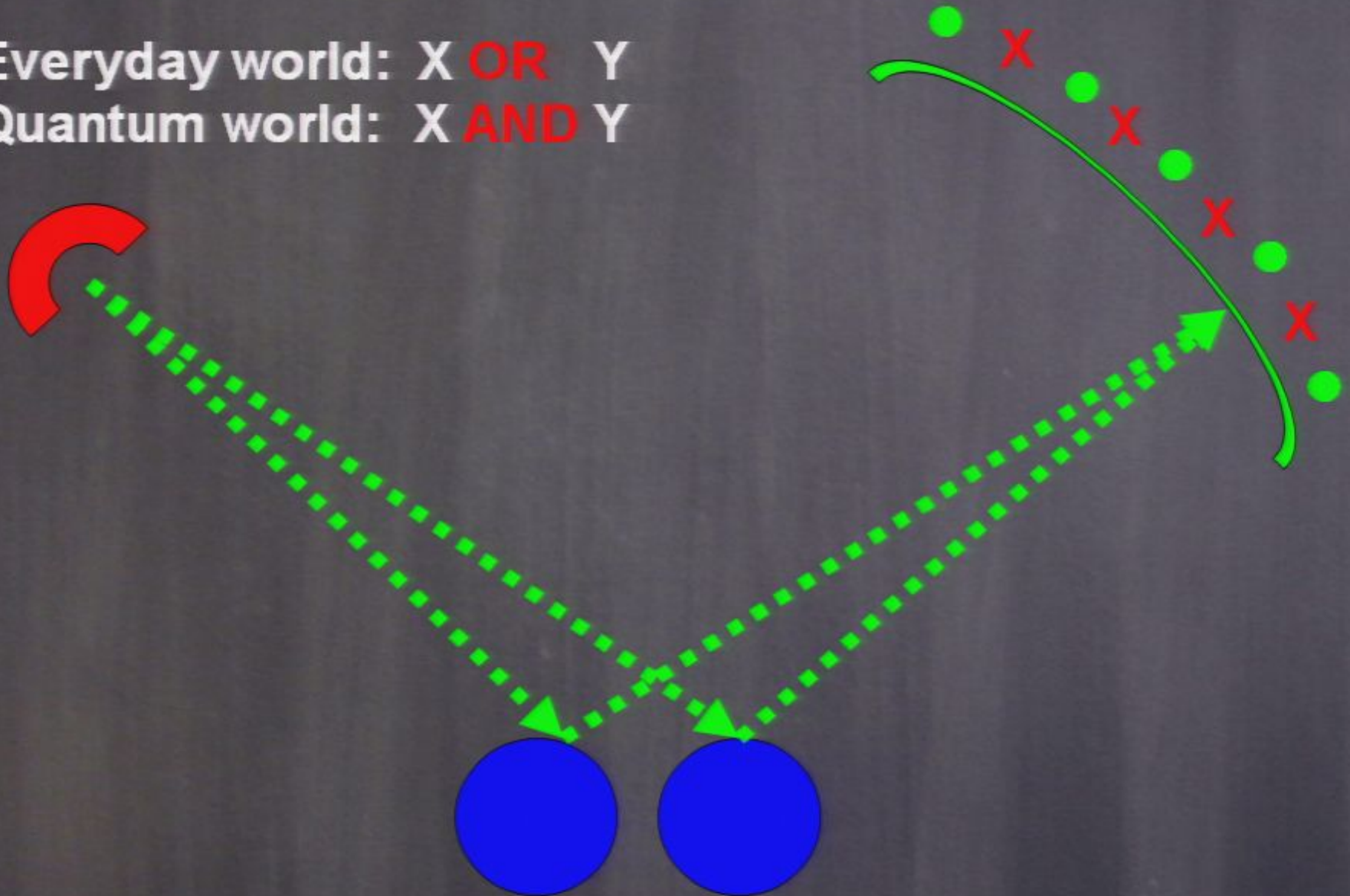
X OR Y
X AND Y



How is this POSSIBLE?

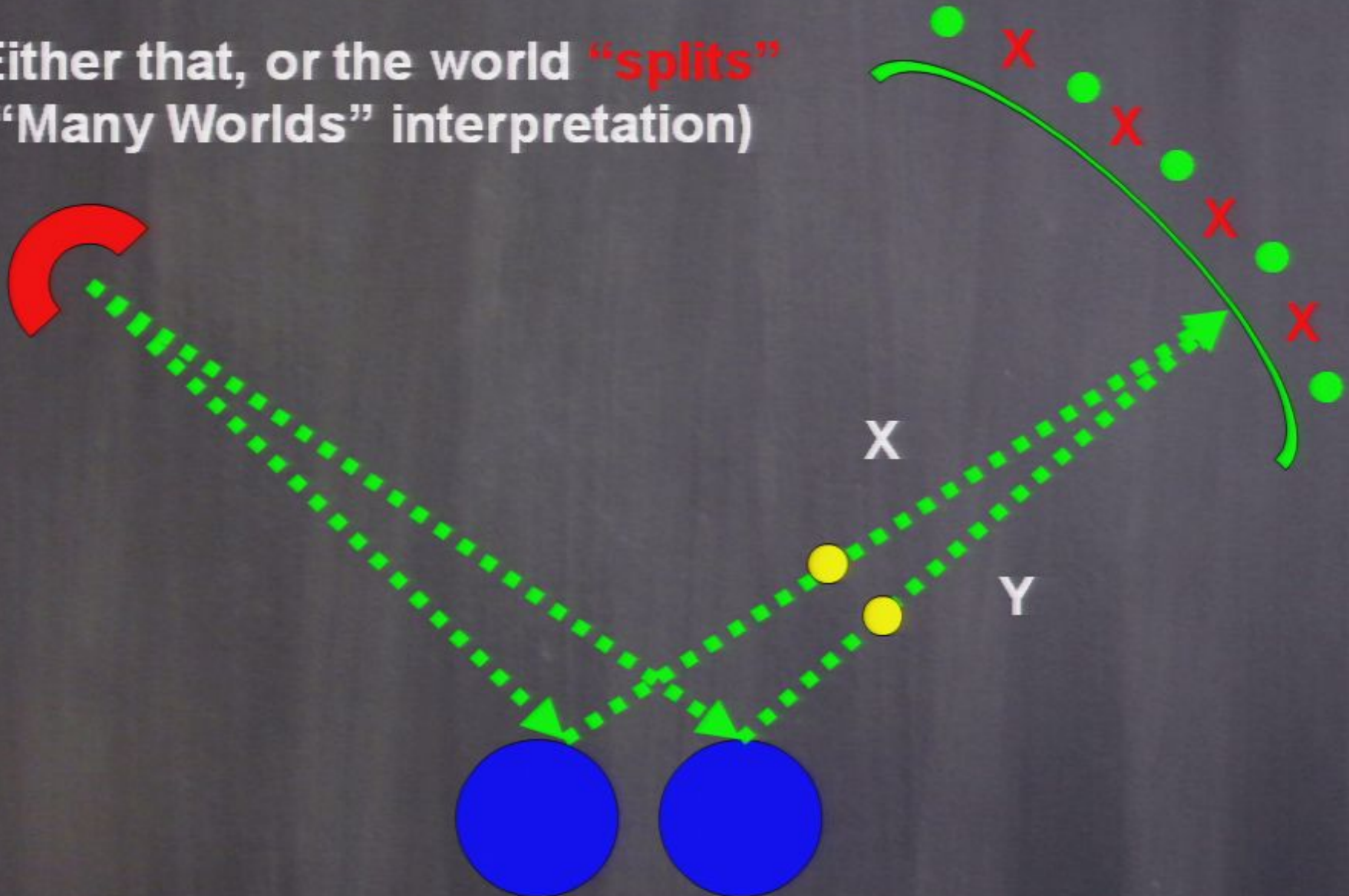
Everyday world: X **OR** Y

Quantum world: X **AND** Y

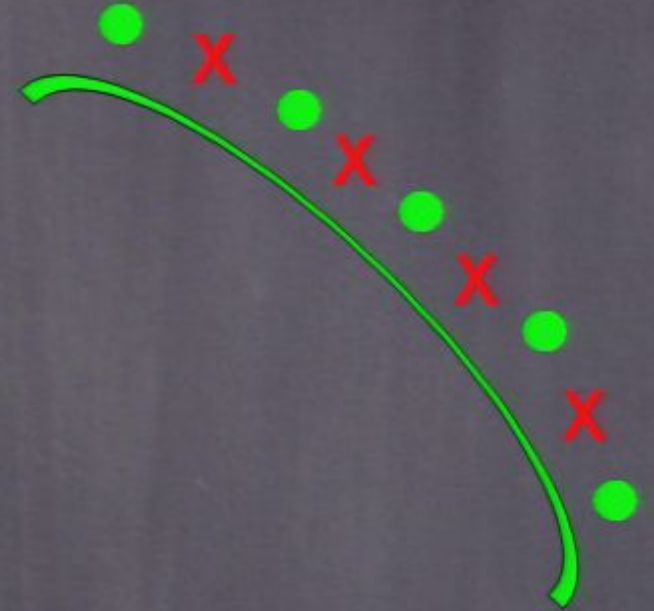


How is this POSSIBLE?

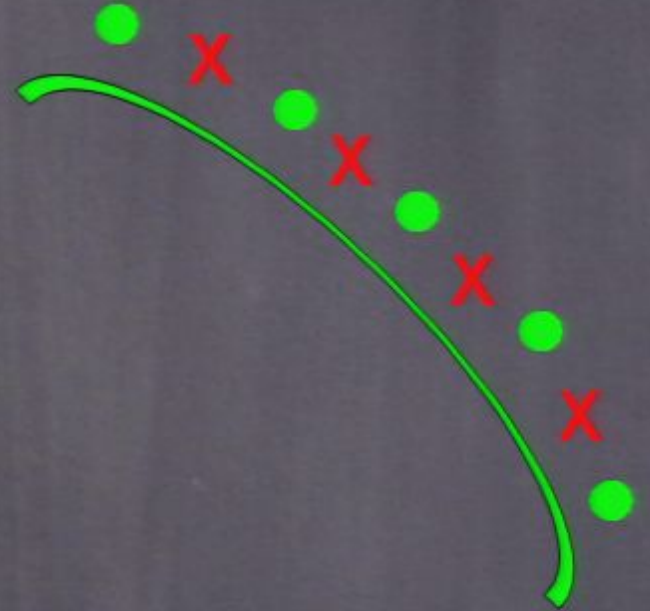
Either that, or the world “splits”
 (“Many Worlds” interpretation)



Consider **ALL** the Atoms

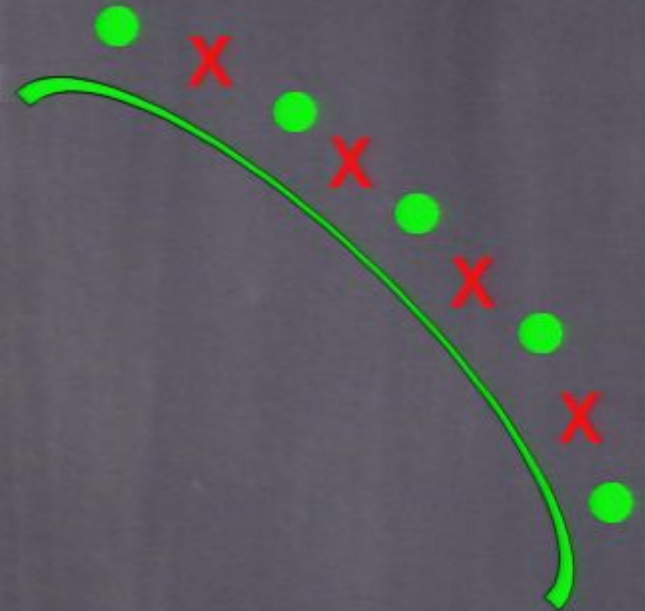


Consider **ALL** the Atoms



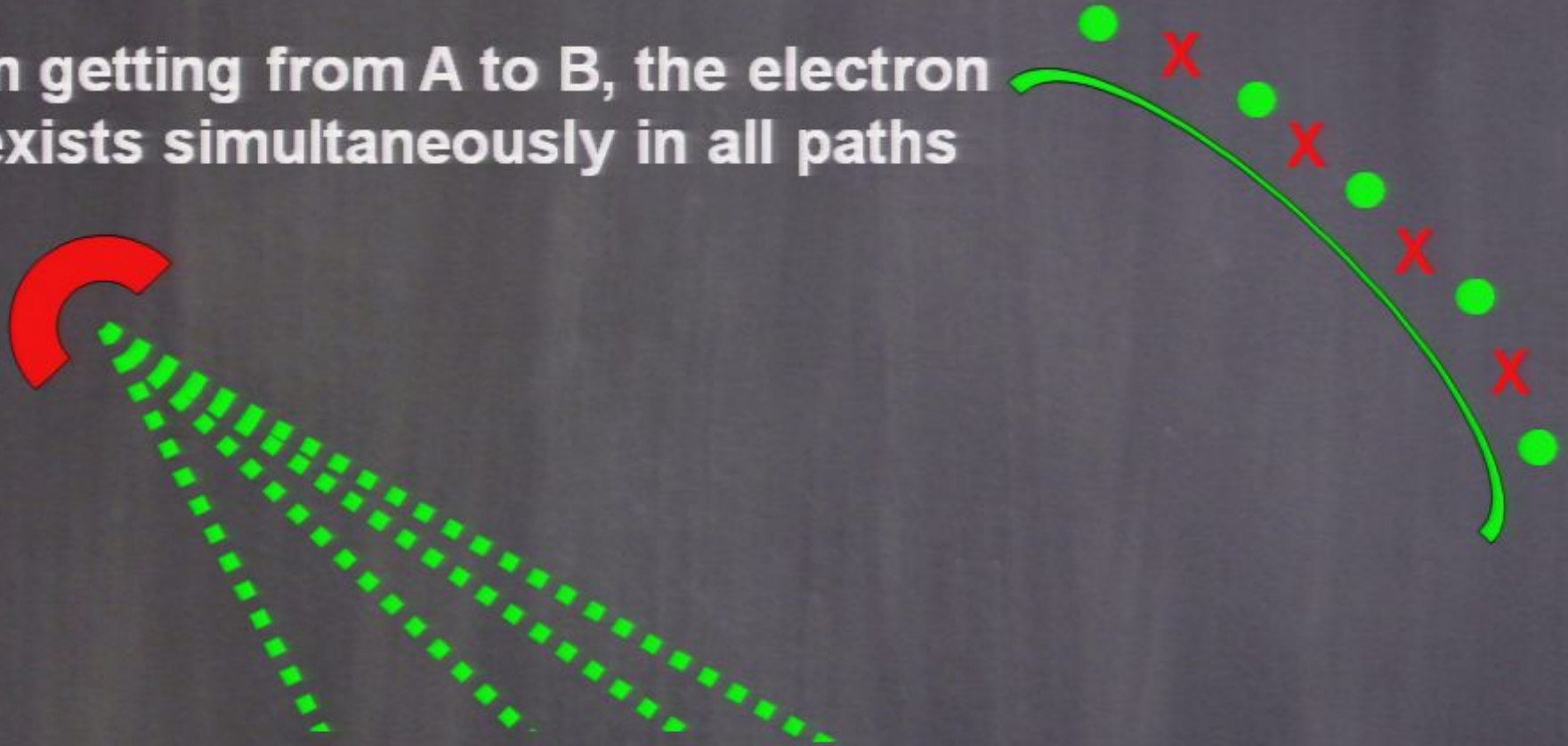
Consider **ALL** the Atoms

In getting from A to B, the electron exists simultaneously in all paths



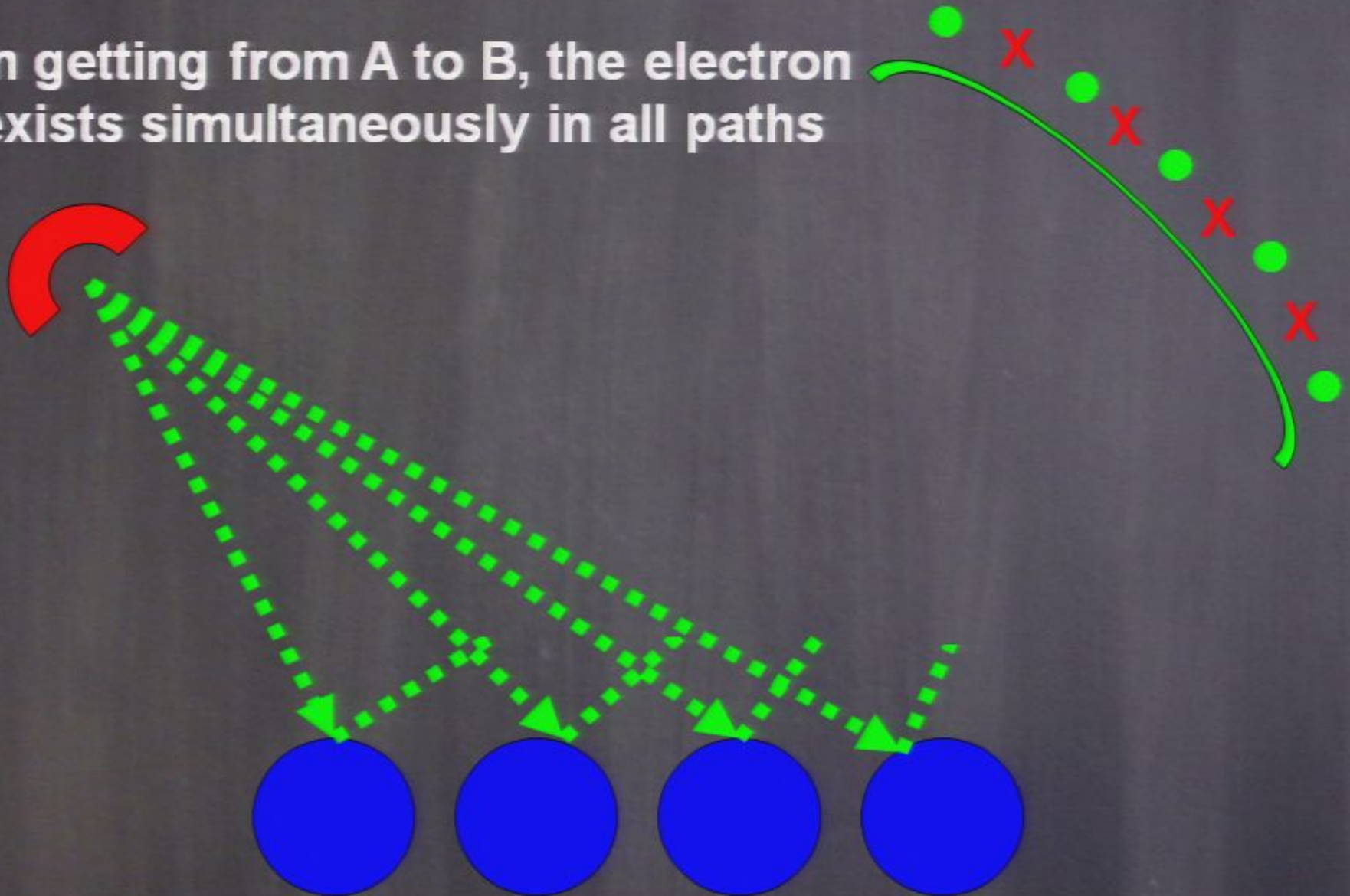
Consider **ALL** the Atoms

In getting from A to B, the electron exists simultaneously in all paths



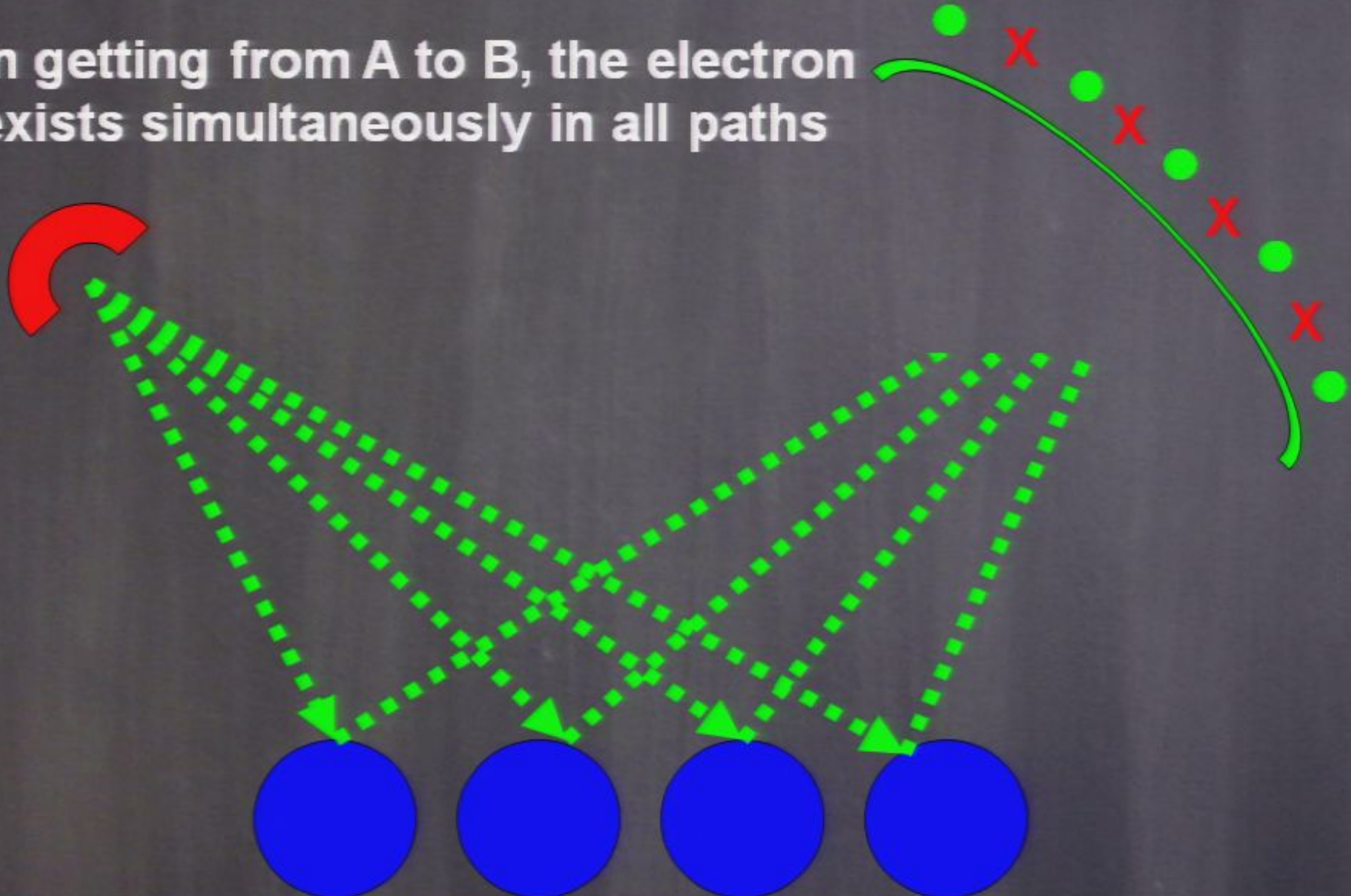
Consider **ALL** the Atoms

In getting from A to B, the electron exists simultaneously in all paths



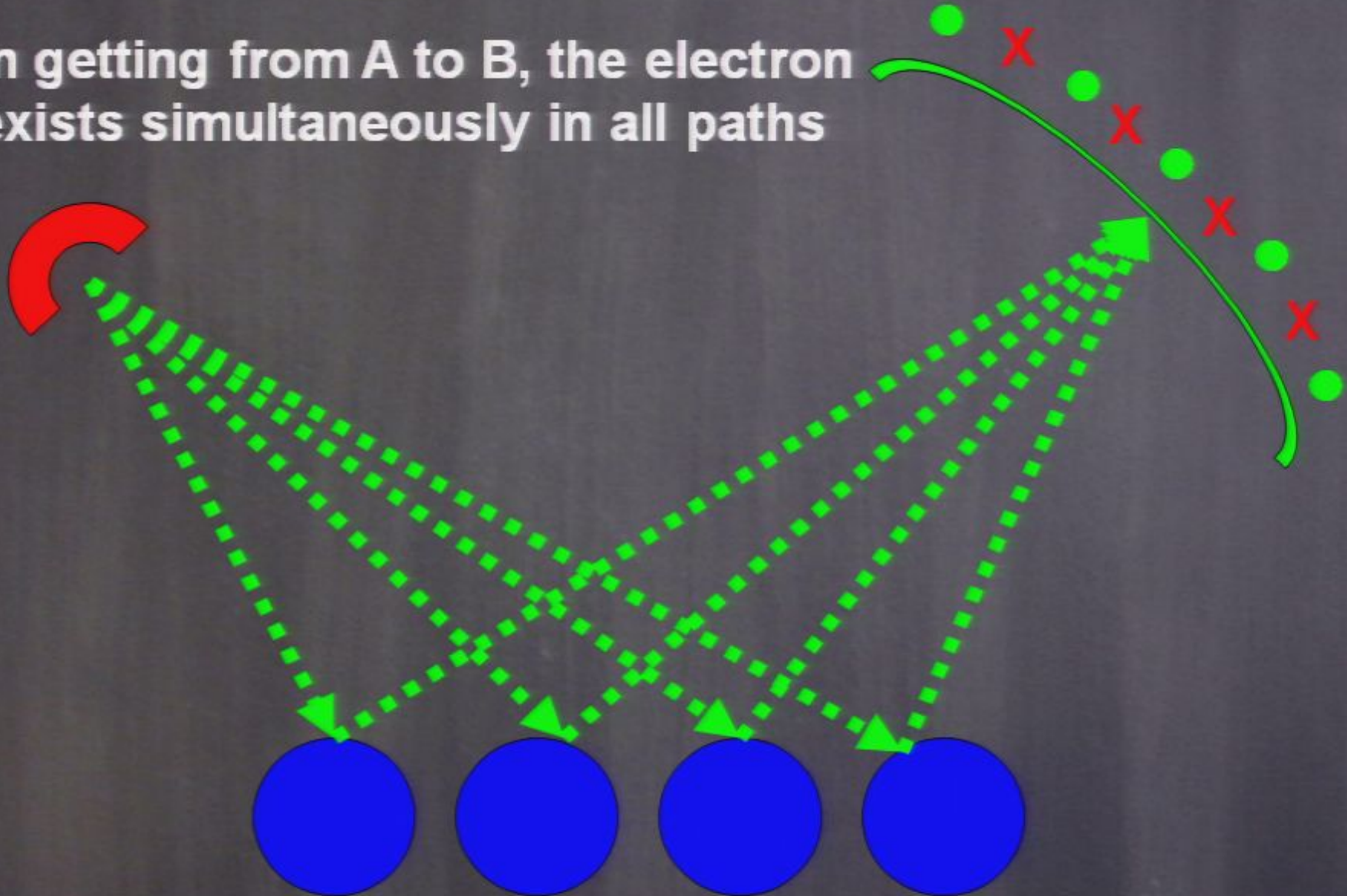
Consider **ALL** the Atoms

In getting from A to B, the electron exists simultaneously in all paths

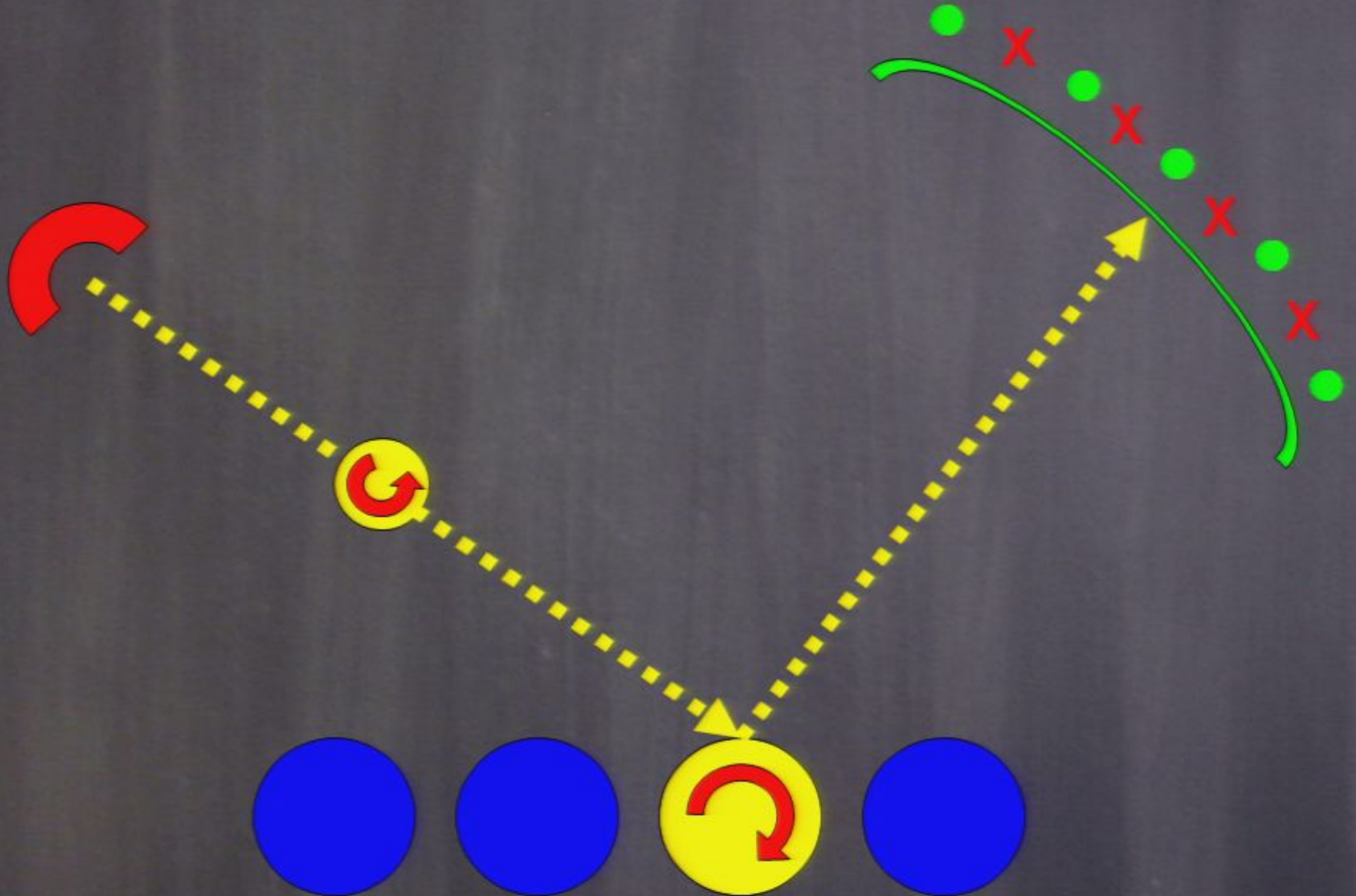


Consider **ALL** the Atoms

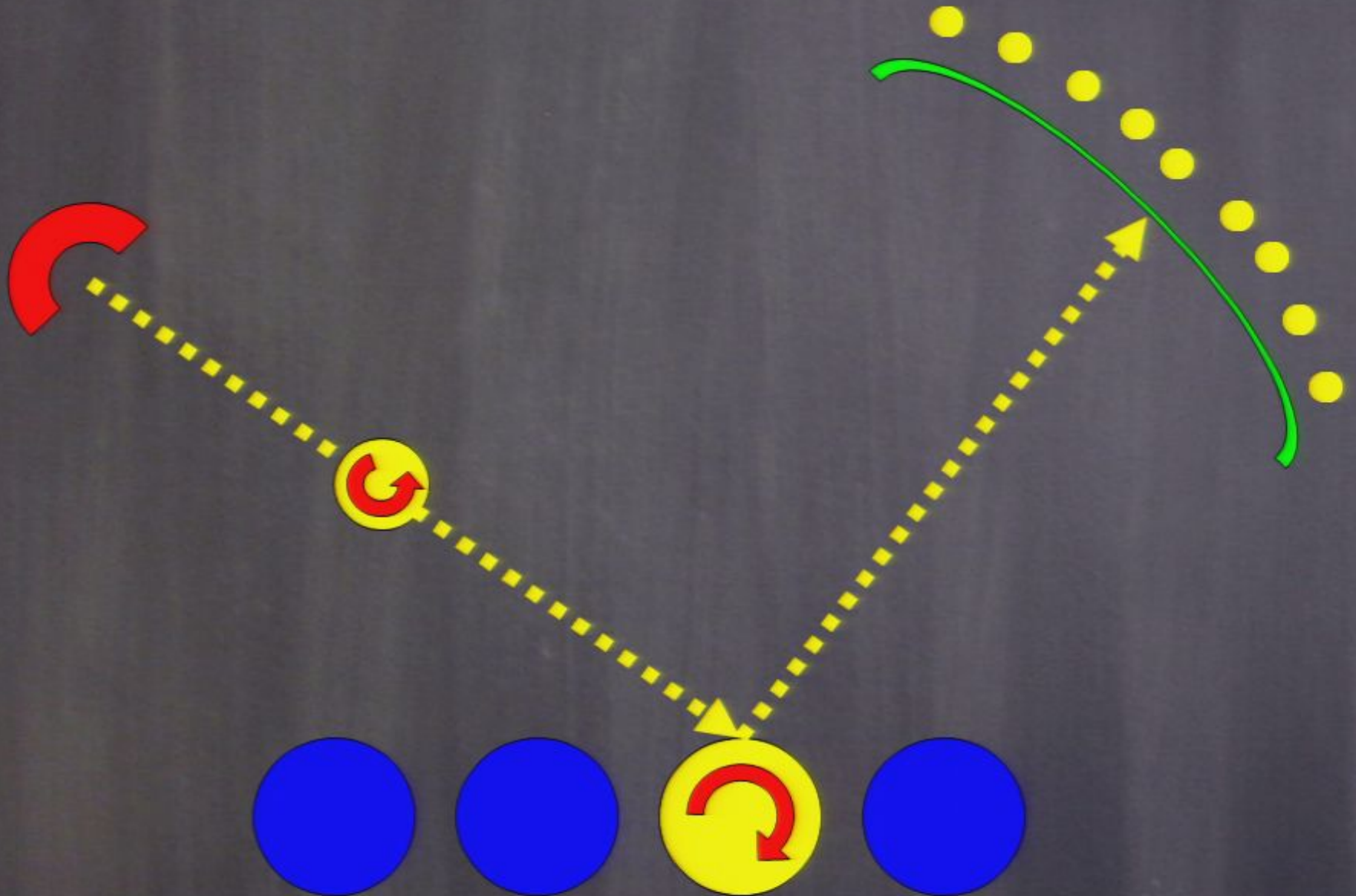
In getting from A to B, the electron exists simultaneously in all paths



Give the Electron a "SPIN"



Give the Electron a "SPIN"





Quantum 5 and 6 Lectures

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Address C:\Documents and Settings\repp\Desktop\Quantum 5 and 6 Lectures

Name	Size	Type	Date Modified
1 The Physics and Mathematics of Spin.ppt	1,734 KB	Microsoft Office Po...	7/29/2008 8:20 PM
2 Electron Diffraction Apparatus.ppt	786 KB	Microsoft Office Po...	7/29/2008 6:51 PM
3 Quantum Entanglement - Brief.ppt	289 KB	Microsoft Office Po...	7/29/2008 6:58 PM
4 Quantum Teleportation Love Story.ppt	2,759 KB	Microsoft Office Po...	7/29/2008 6:53 PM
Details of Quantum Teleportation.doc	419 KB	Microsoft Office Wo...	8/1/2008 12:26 PM

File and Folder Tasks

- Rename this file
- Move this file
- Copy this file
- Publish this file to the Web
- E-mail this file
- Print this file
- Delete this file

Other Places

- Desktop
- My Documents
- My Computer
- My Network Places

Details

Computer black_hole_... From Rohan's Memory Stick

INSTALL Recyc

erVideo inDVD Shortc repp on

e Acrobat Standard OpenVF

inEdt RealP

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Tunes iTunesC

nvias 11 Buy C Onli

ellaneous Dark Matter From Memory Stick + SCIENTIFIC PI vs UW.docx To Do.docx OUTREACH

Picture of Samantha

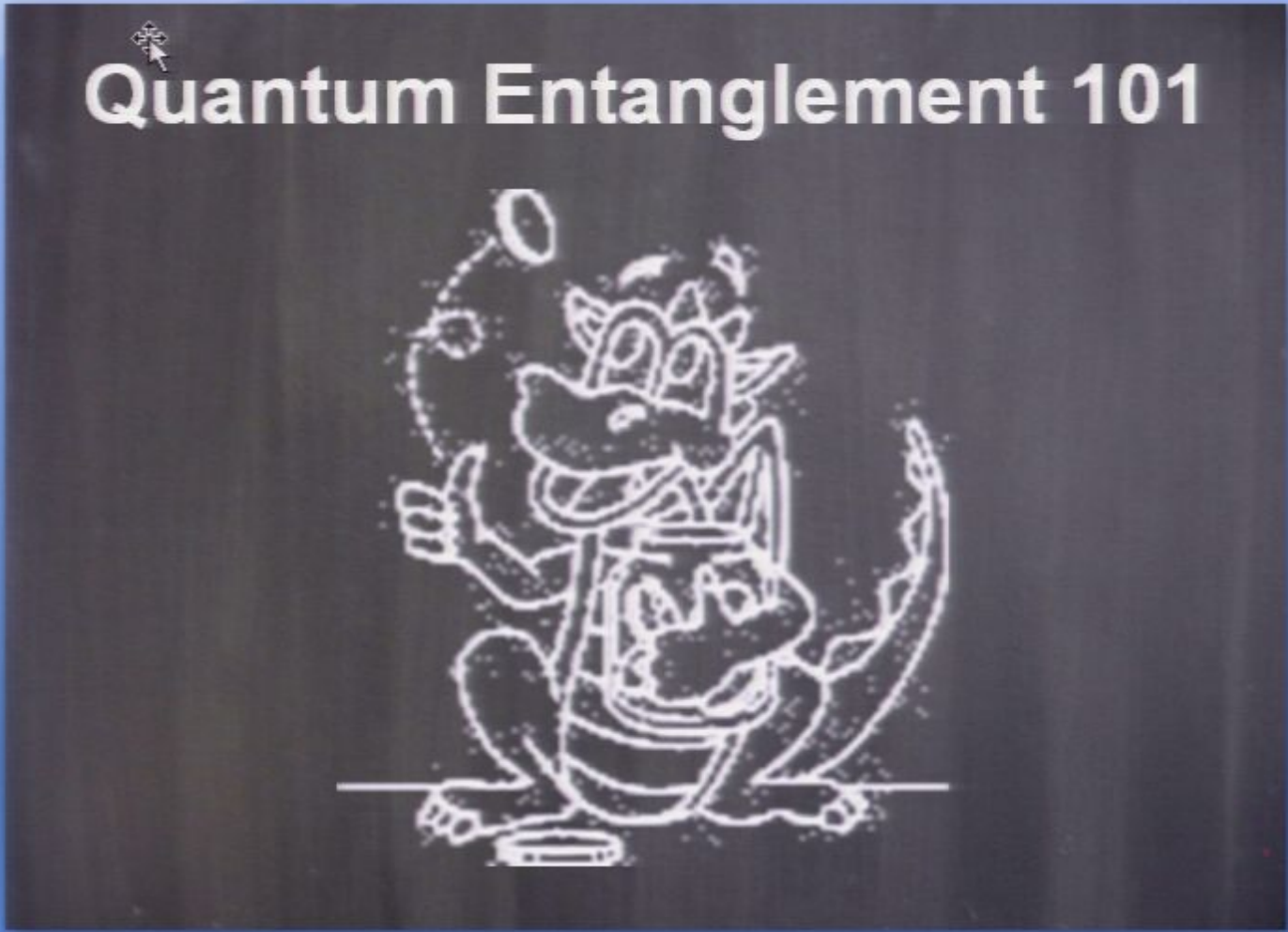


Font Paragraph Drawing Editing

Layout, Reset, Delete, New Slide, Slides, Font (B, I, U, S, Aa, A), Paragraph (bullets, indent, line and paragraph spacing), Drawing (Shape Fill, Shape Outline, Shape Effects), Editing (Find, Replace, Select)

Outline

- Quantum Entanglement 101
- Quantum Entanglement 101 (with diagram)



Click to add notes

Quantum Entanglement 101

Quantum Entanglement 101



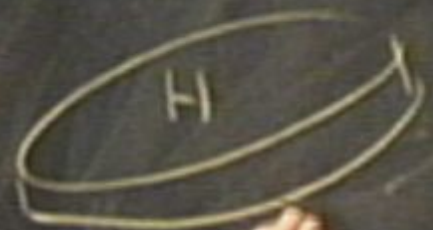








$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} =$$



$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} = \nabla^2$$

↑
habla





Alice



Bob



Alice



Bob



Alice



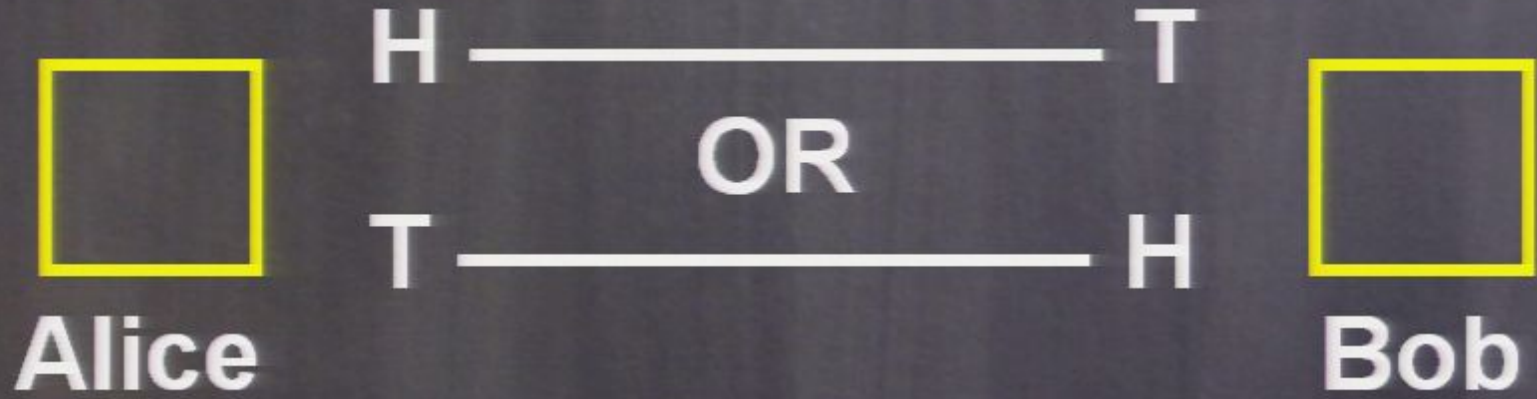
Bob



Alice

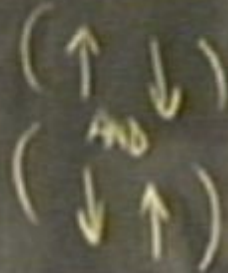
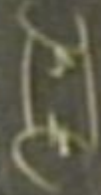
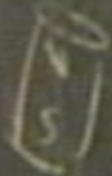


Bob



$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} = \nabla^2$$

↑
habla







Alice

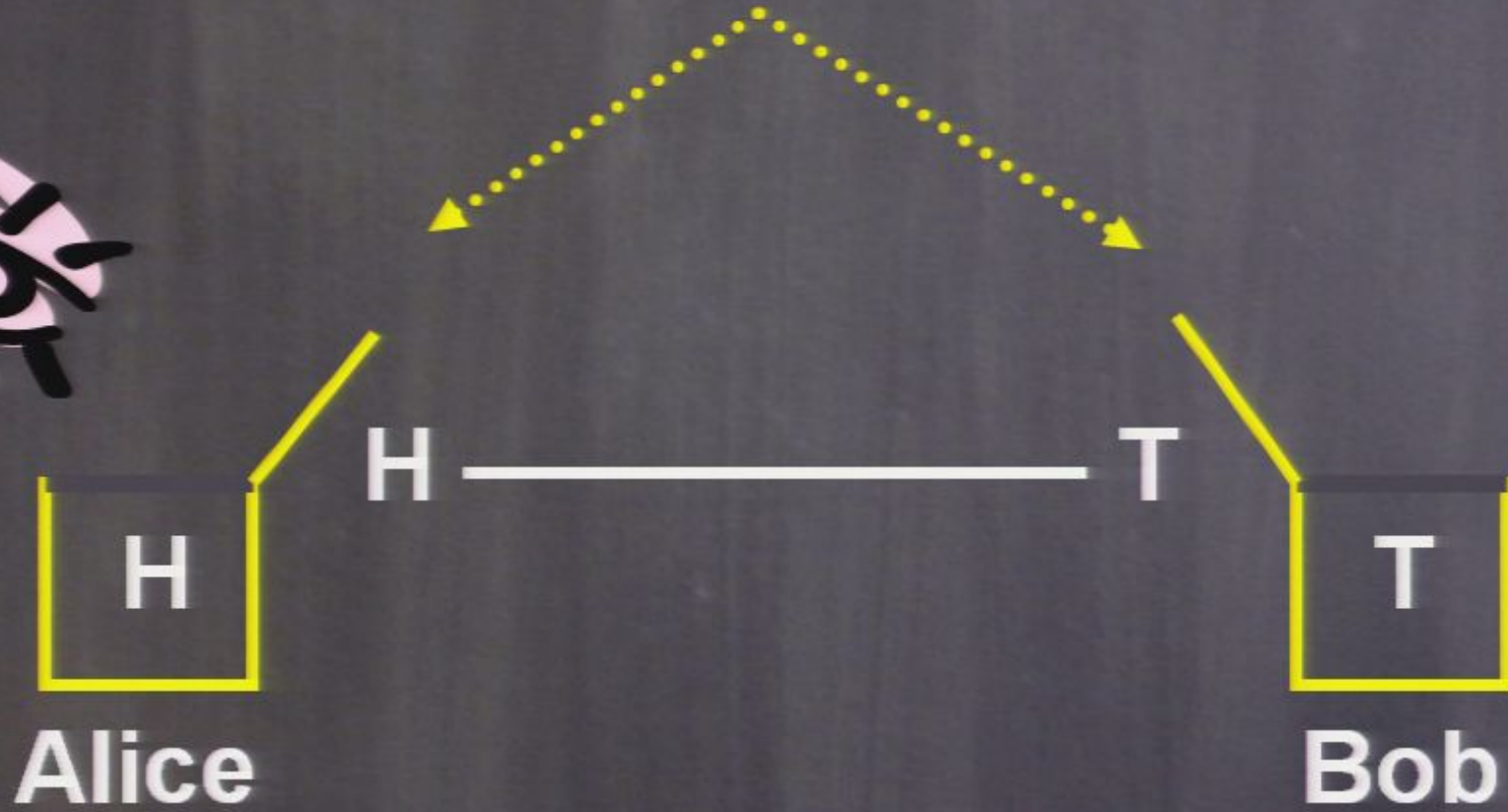
H



T



Bob





H

Alice

H



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Bob



Alice

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Bob





Alice

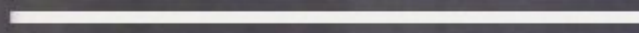


Bob



Alice

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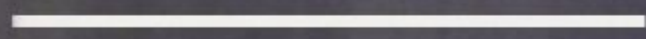


Bob



Alice

T

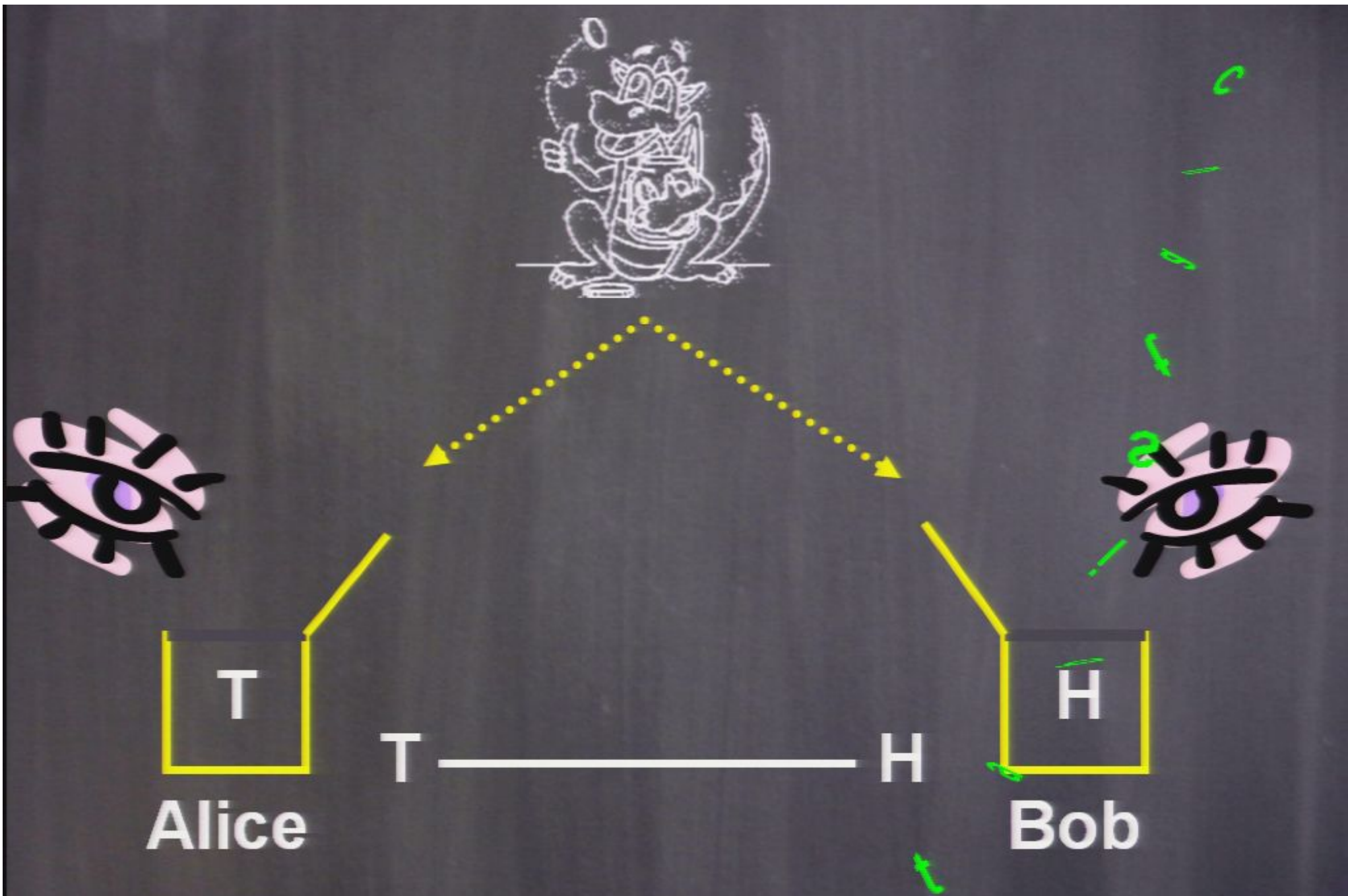


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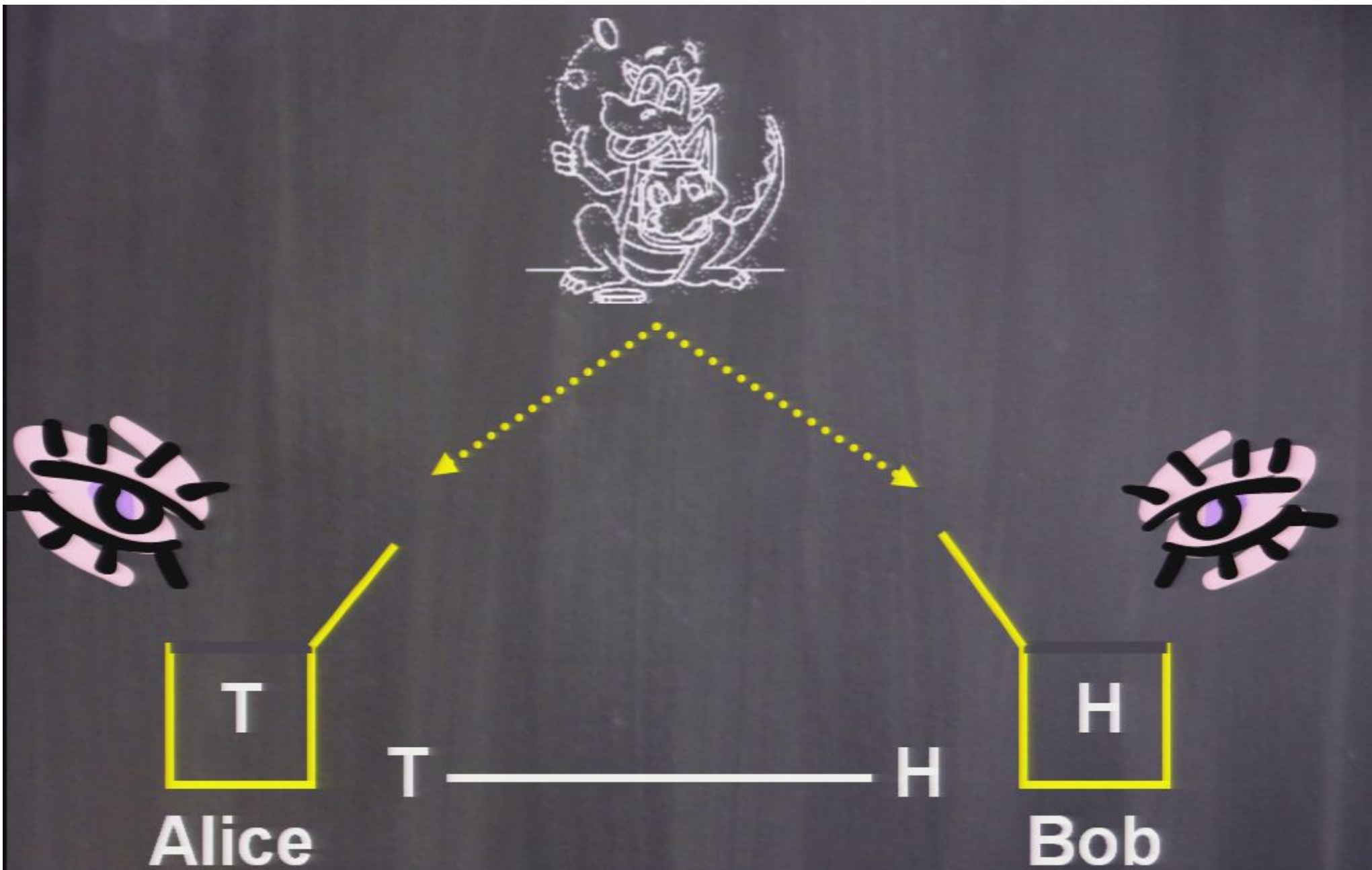


Bob



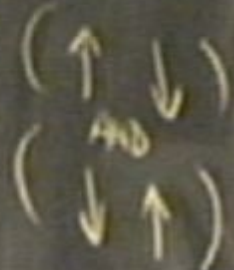


Einstein: "Spooky action a



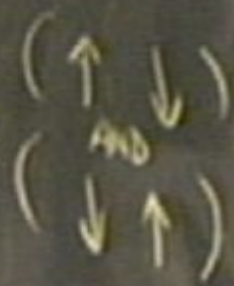
$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{dz^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} =$$

∇^2
habla



$$\frac{d^2}{dx^2} \rightarrow d^2 + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} =$$

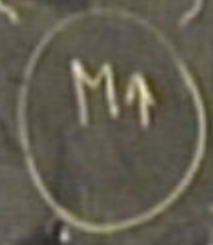
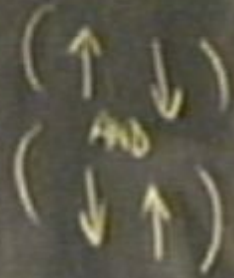
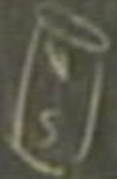
∇^2
habla

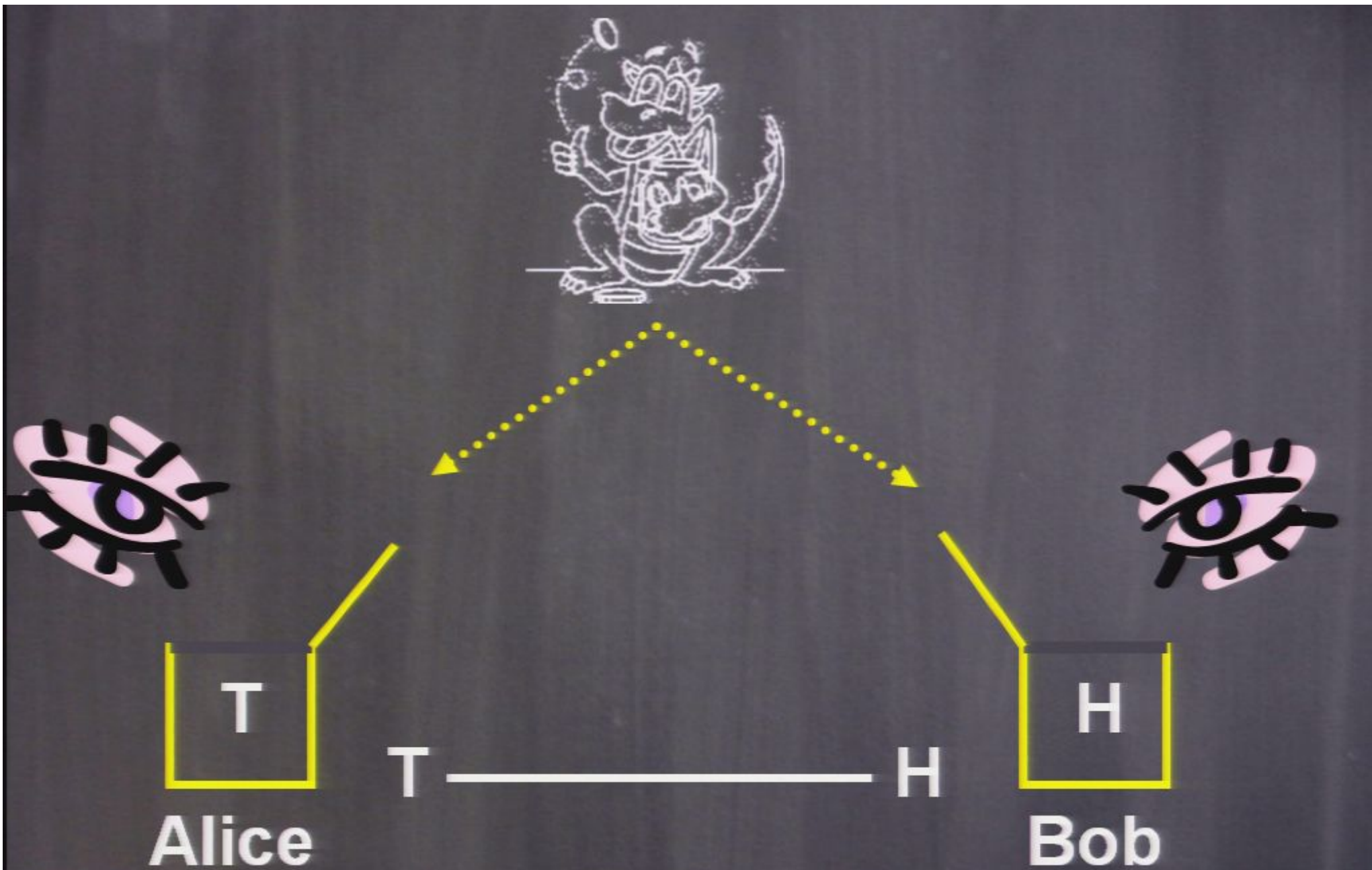


$\{s\}$

$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} =$$

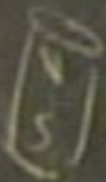
∇^2
lapla





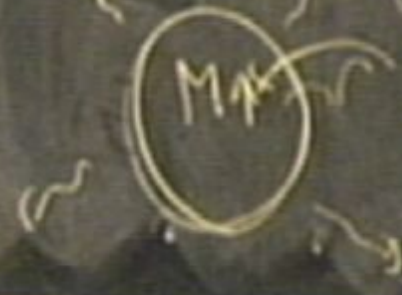
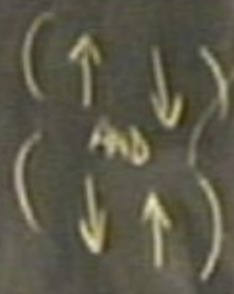
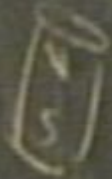
$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + d^2 + d^2 = \nabla^2$$

habla



$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} = \nabla^2$$

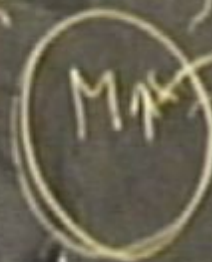
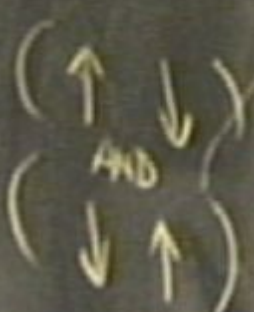
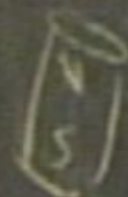
↑
habla

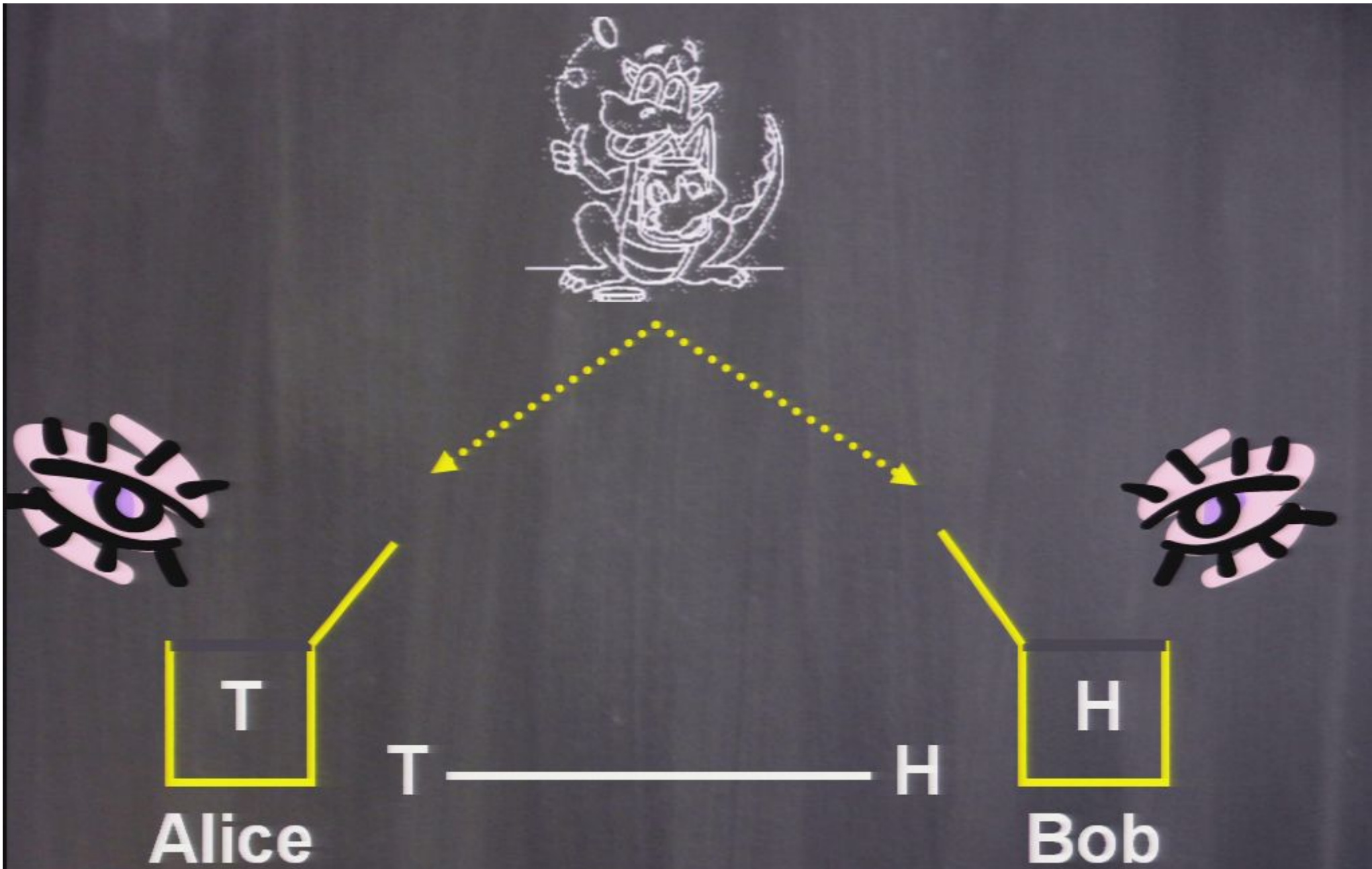


$$\frac{d^2}{dx^2} \rightarrow \frac{d^2}{ds^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} = \Delta^2$$

$$T \sim (10^{66} M_{\oplus}^3)$$

habla





Q UANTUM

Quantum Teleportation

Quantum Teleportation

...A Love Story





Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat



Schrödinger's Cat

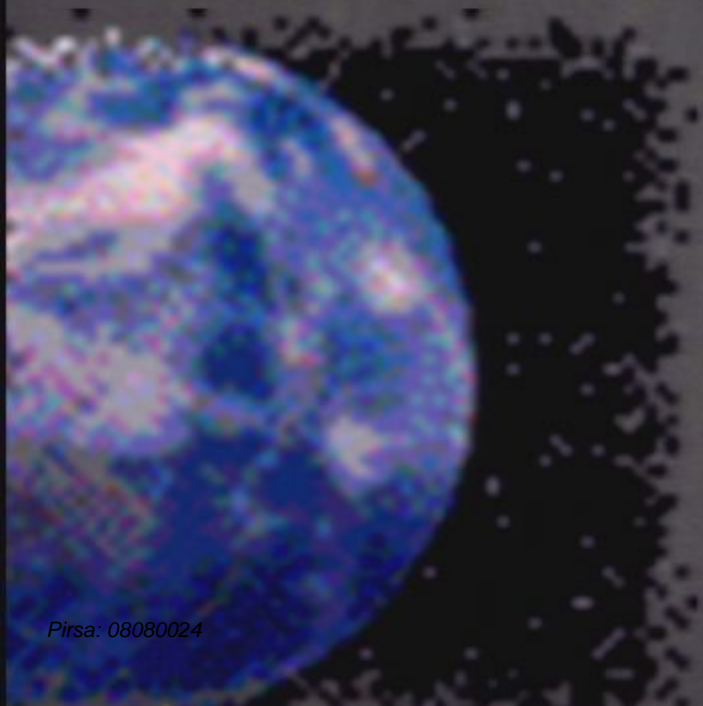


Schrödinger's Cat

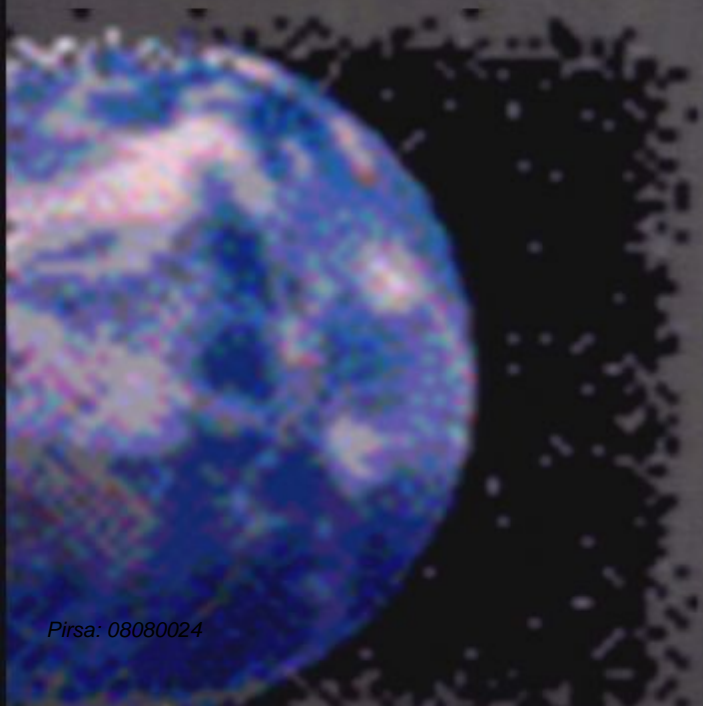


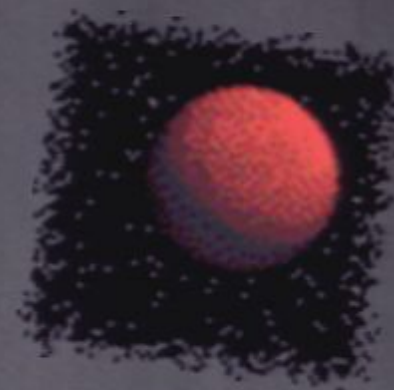
Schrödinger's Cat

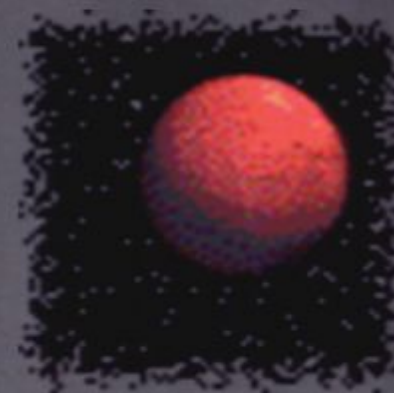
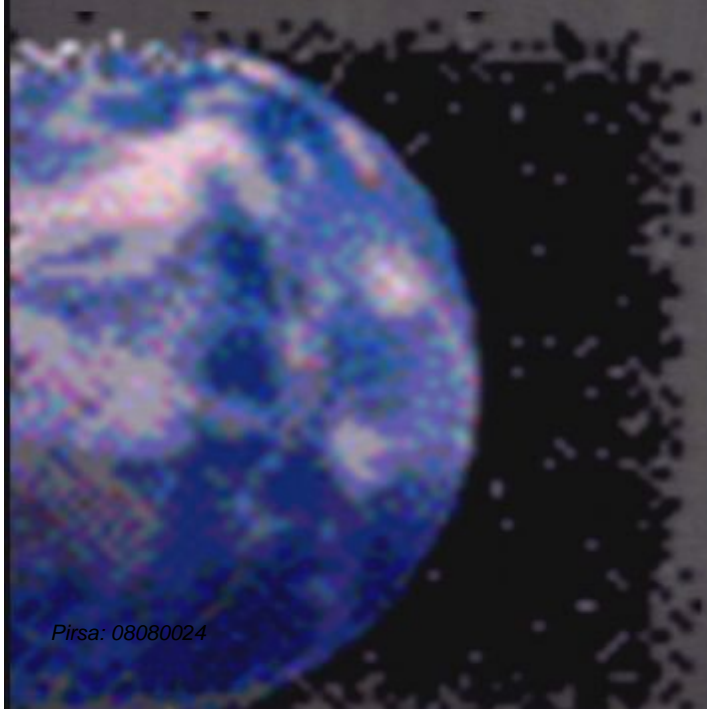


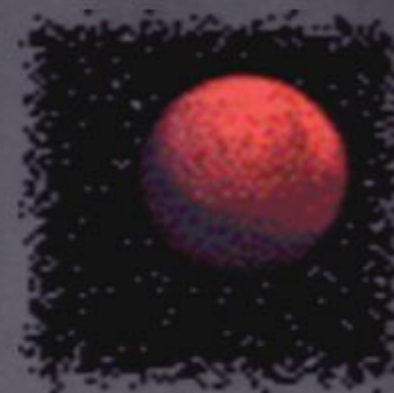


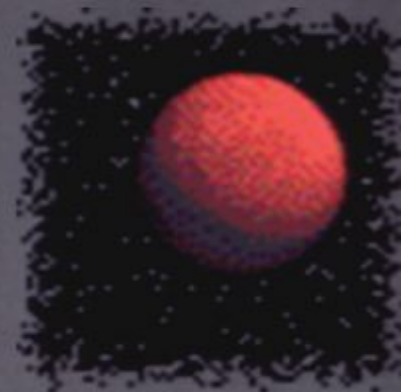
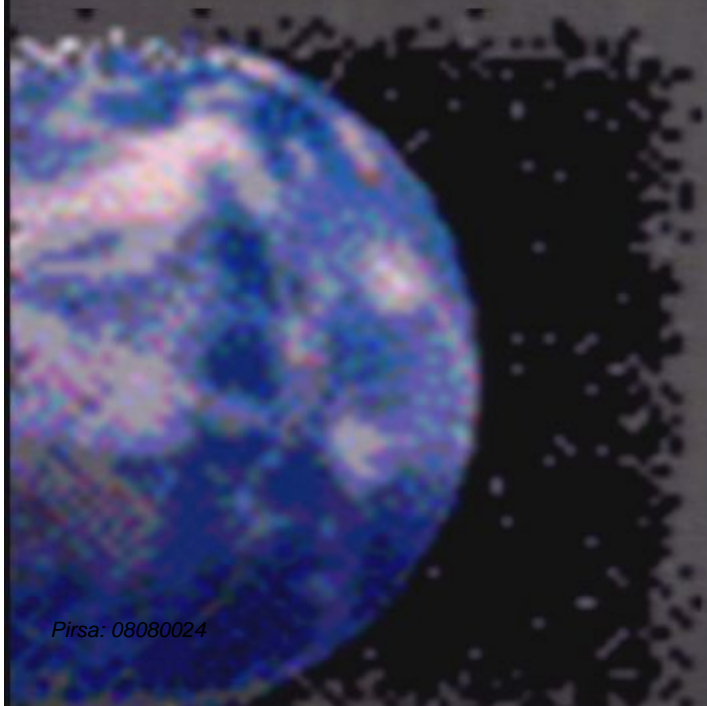


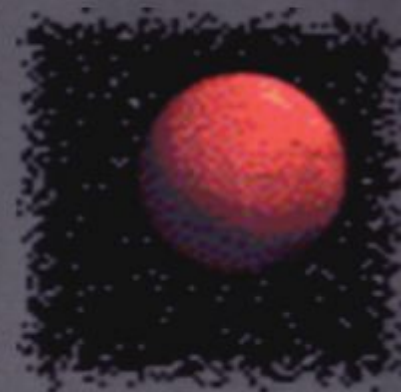


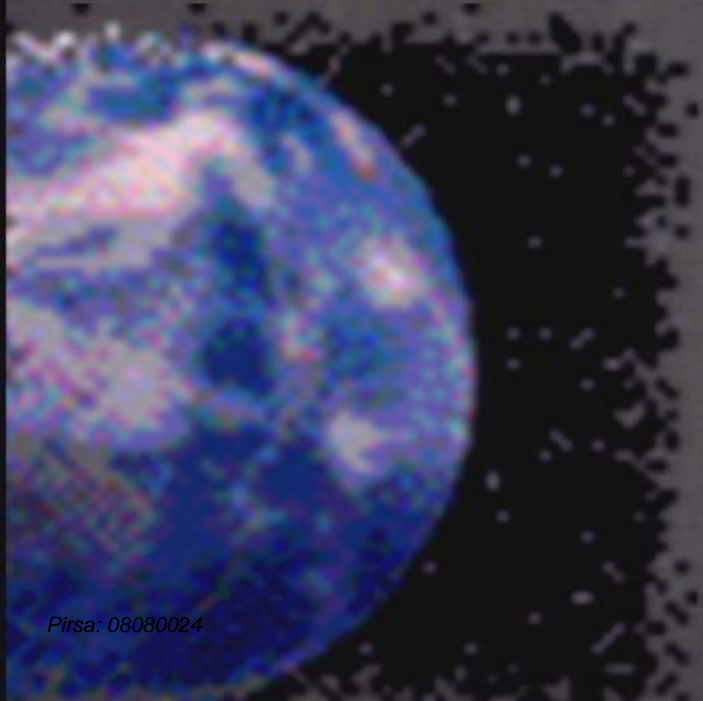
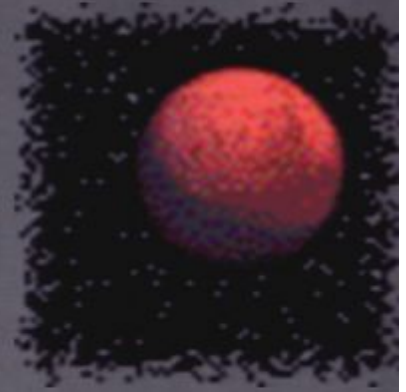


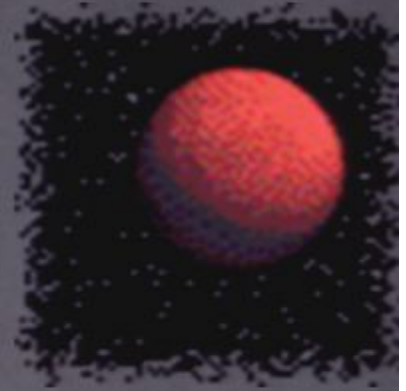
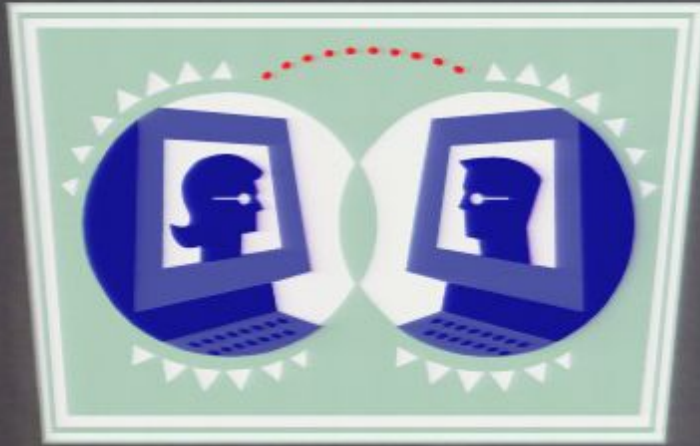


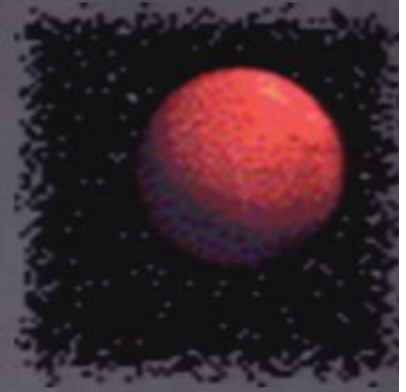
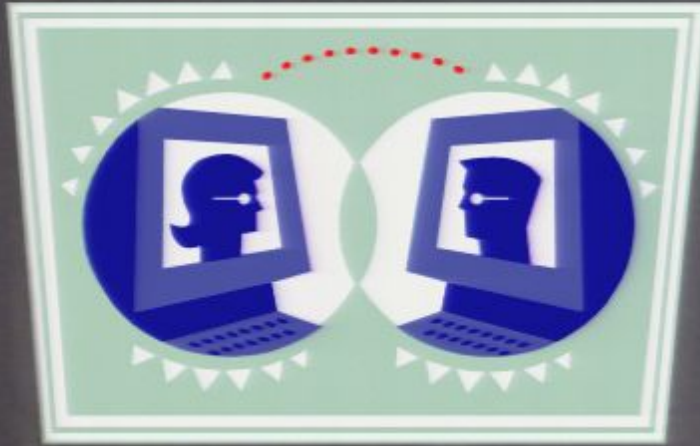


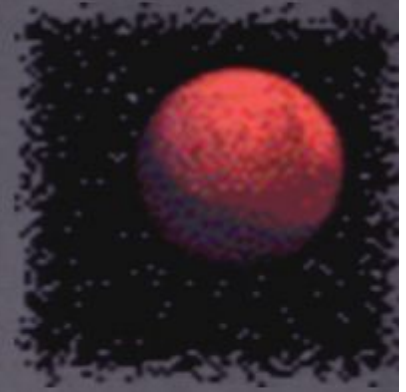
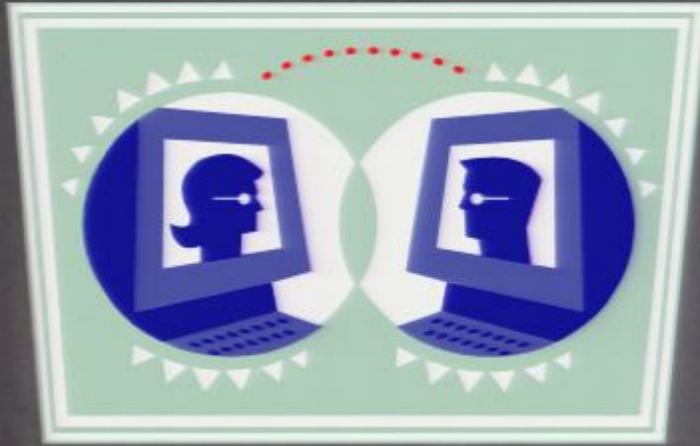


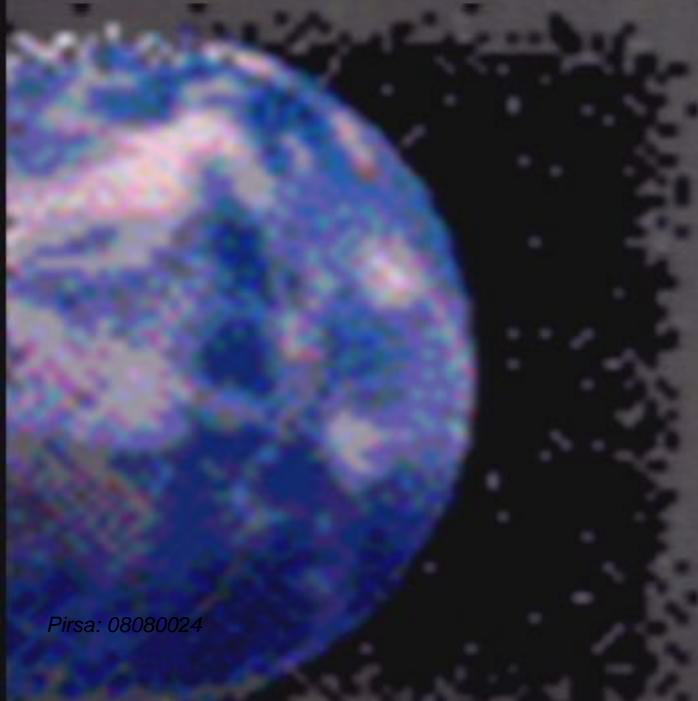
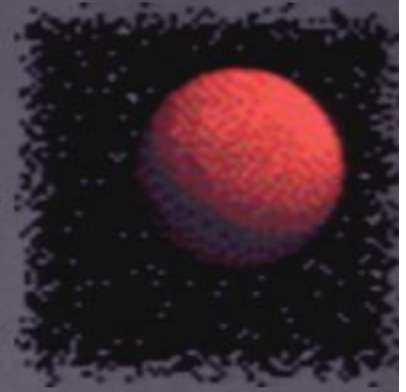
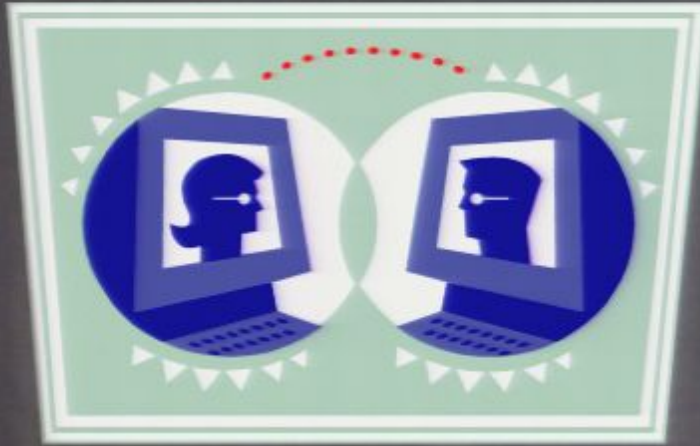


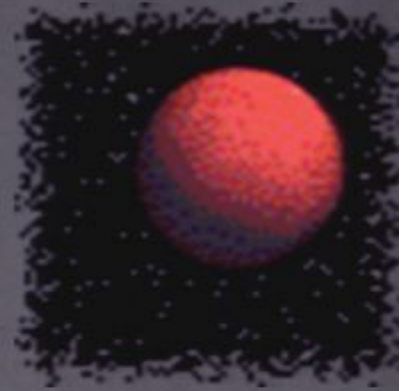
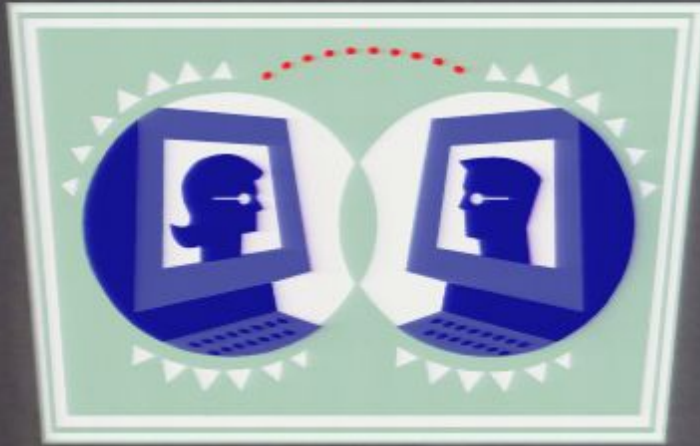


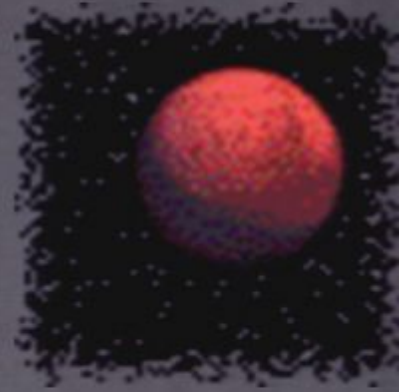
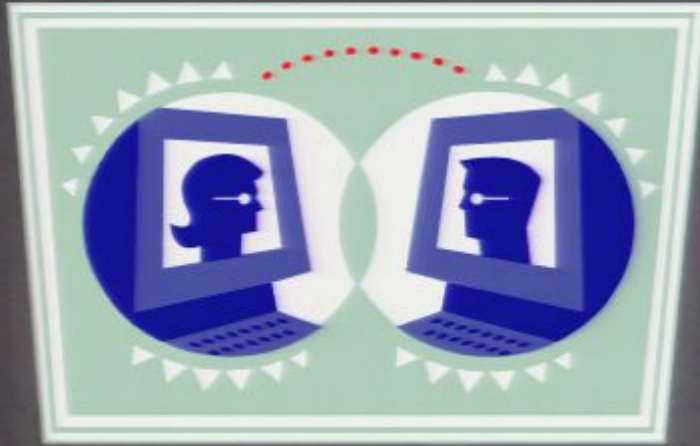


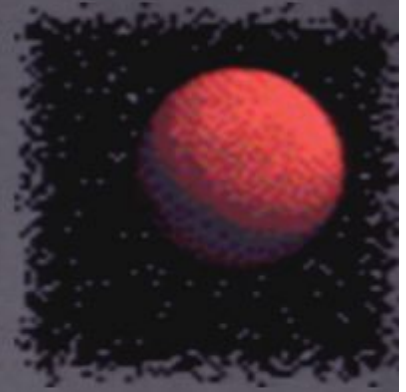
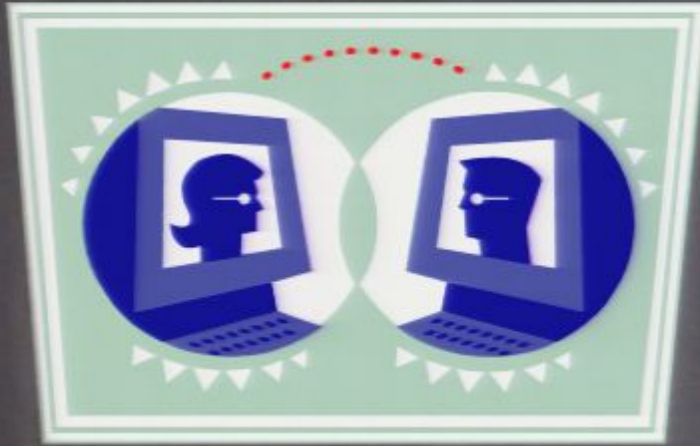


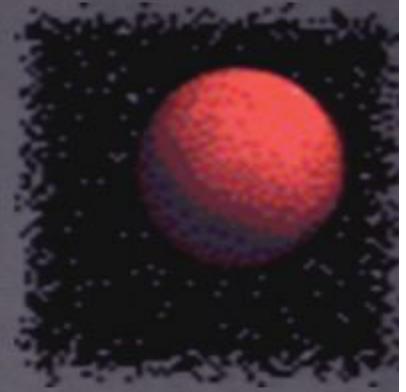
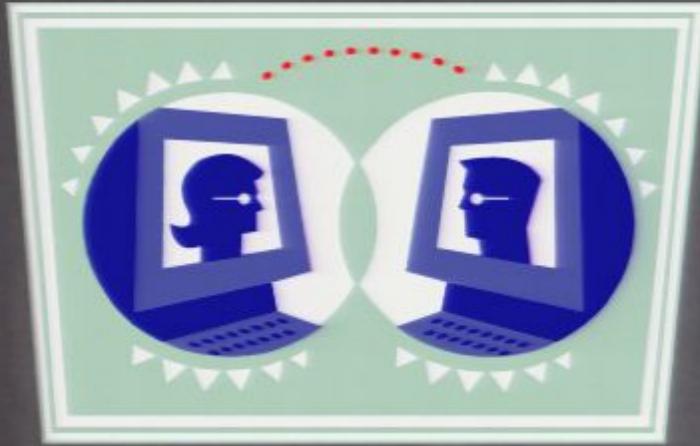


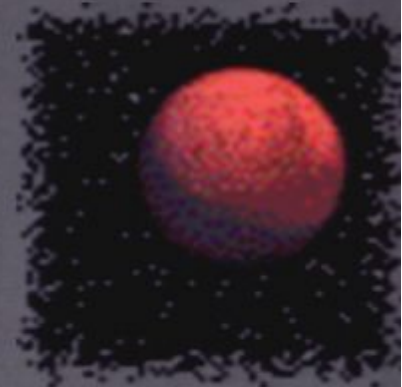
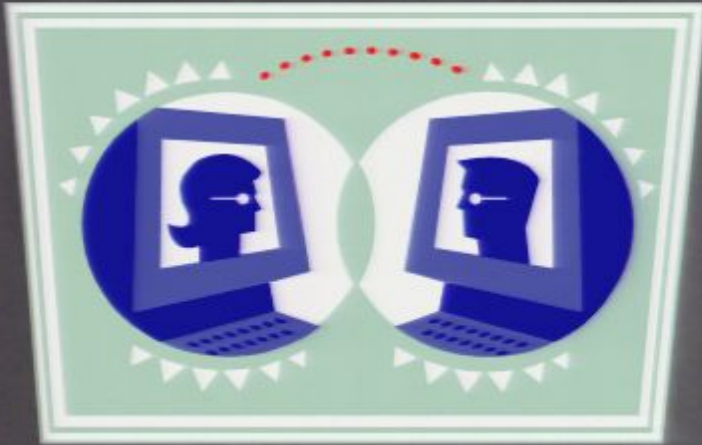


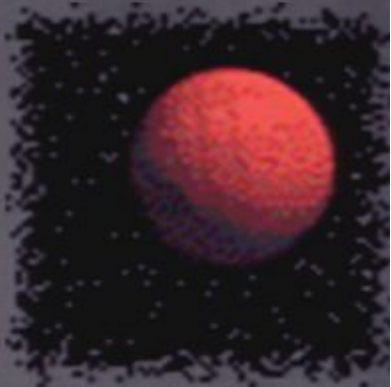


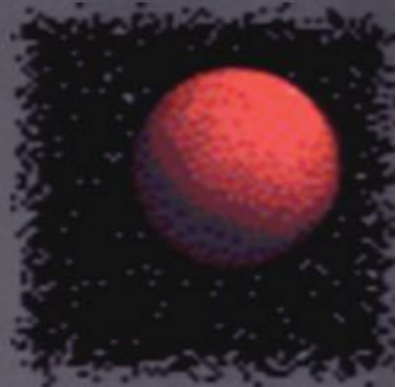


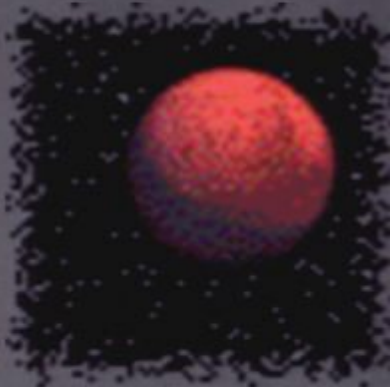


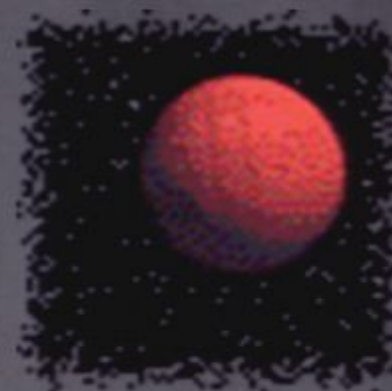


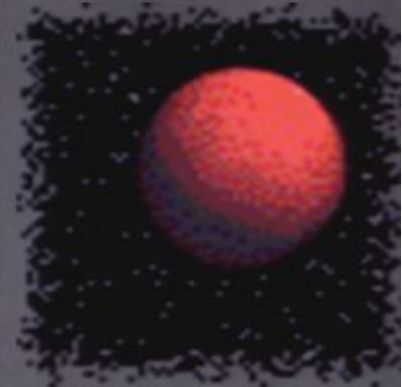


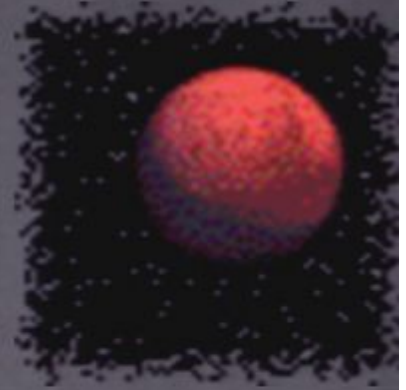


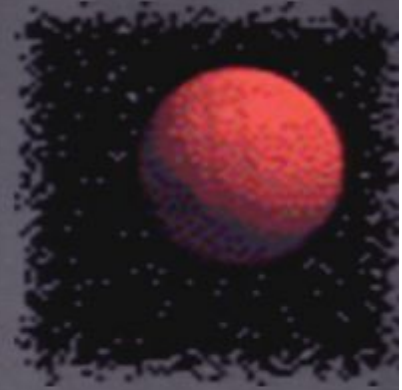


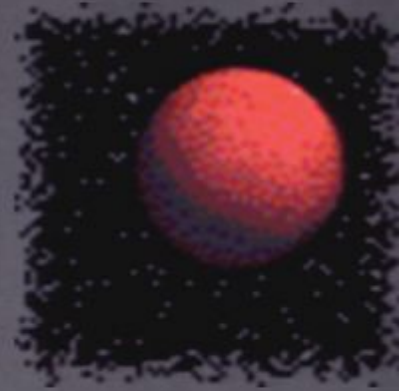


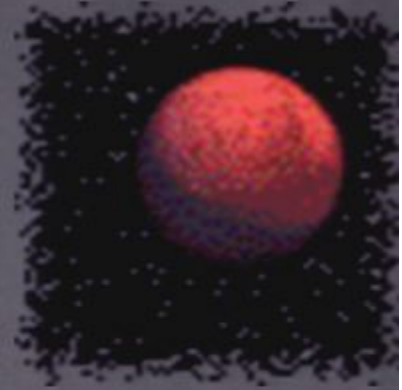


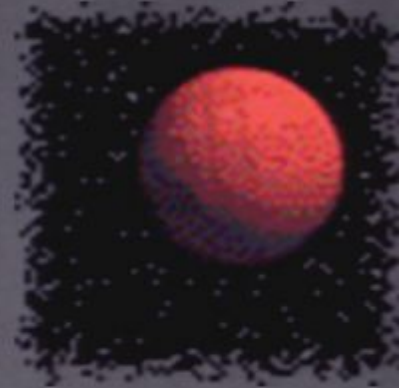


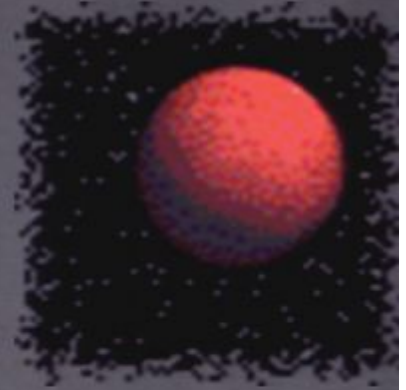


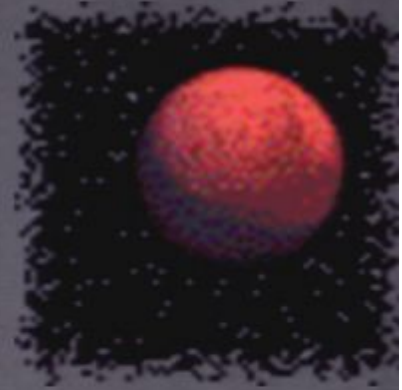


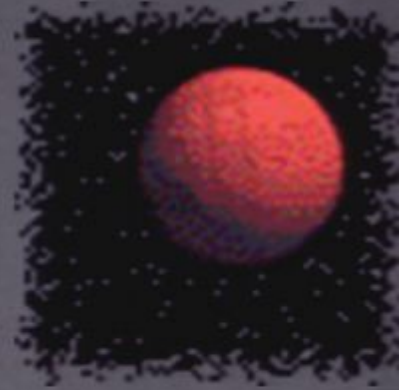


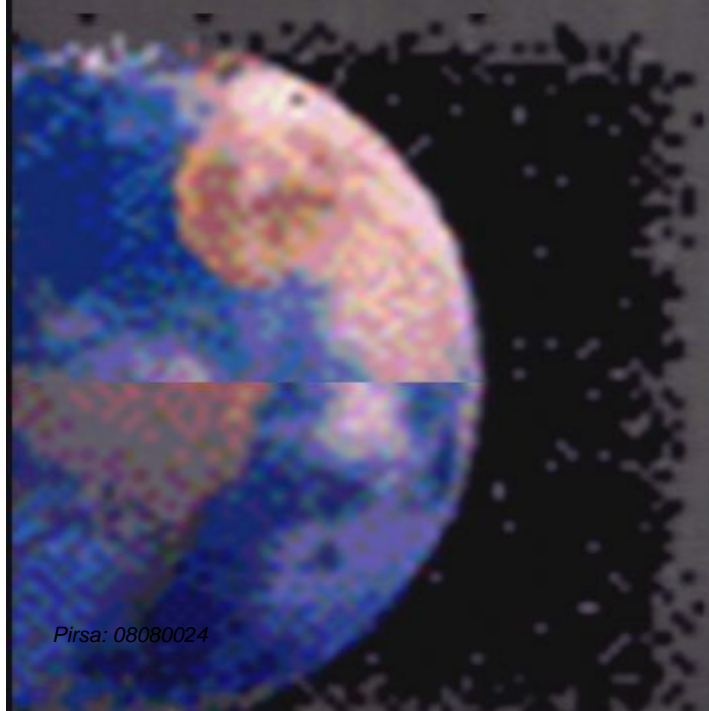
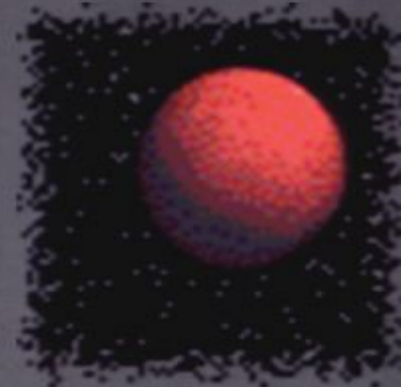




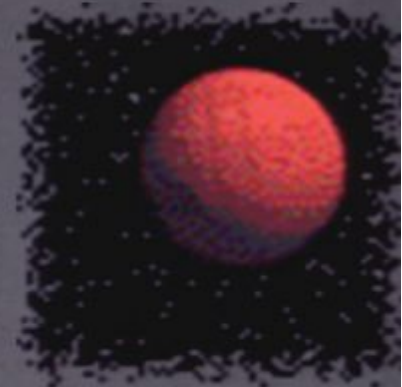


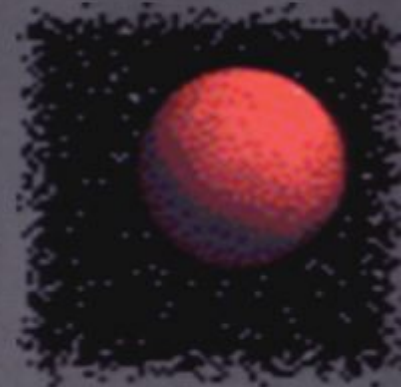


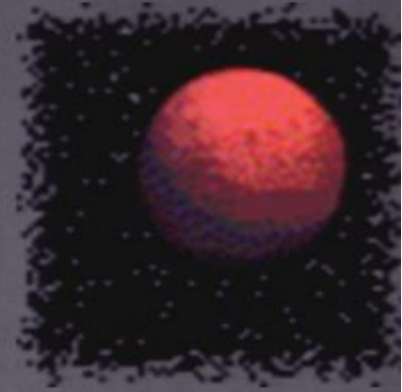


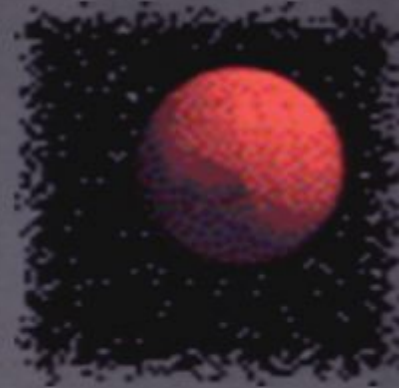


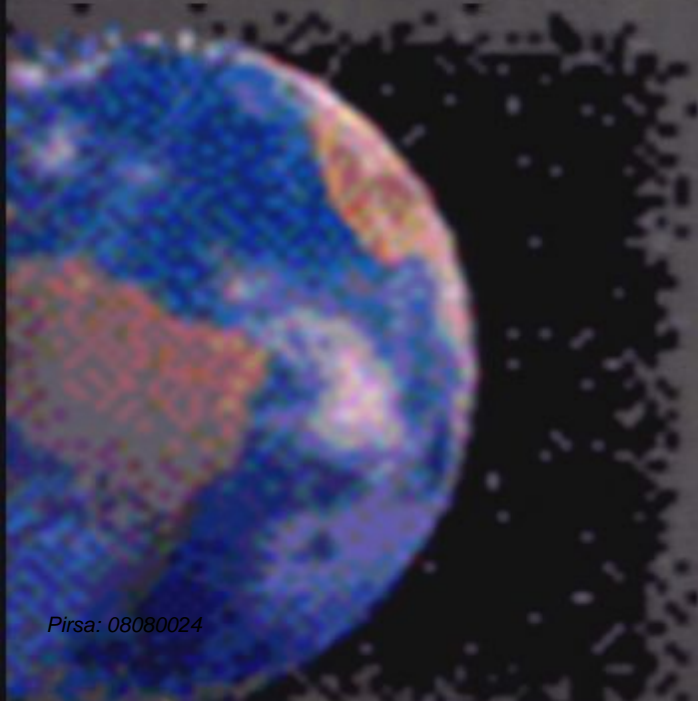
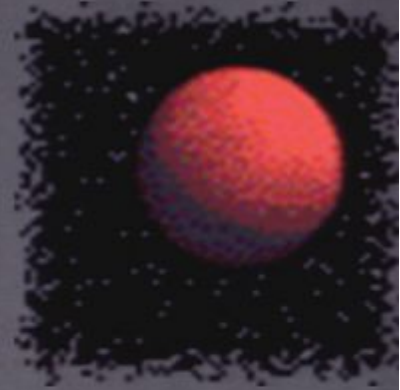


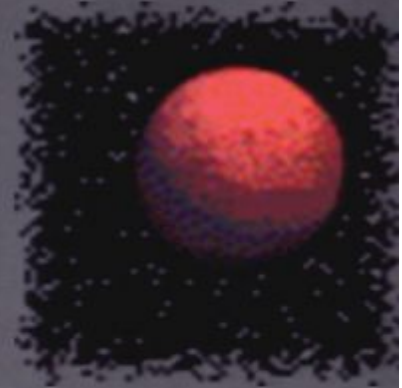


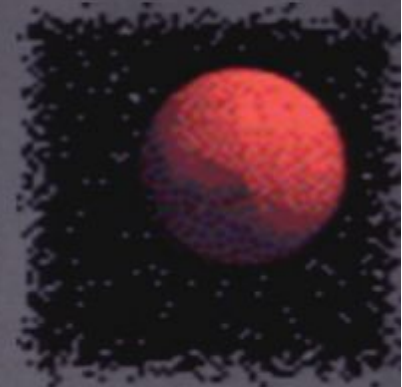


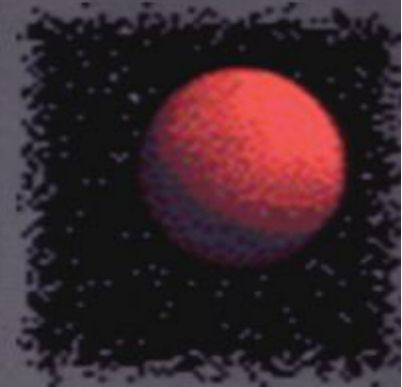


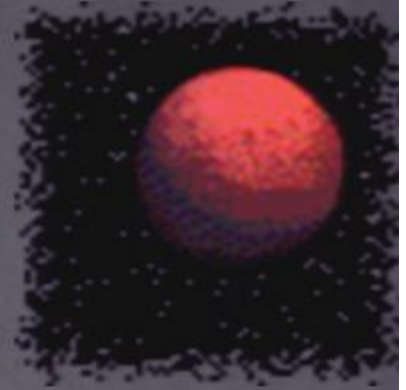


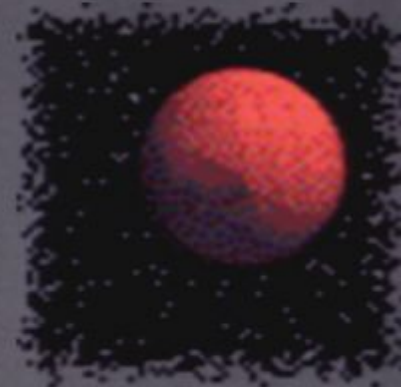


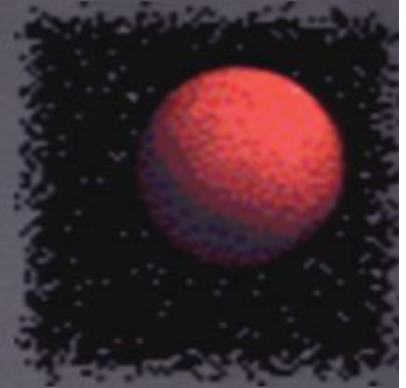


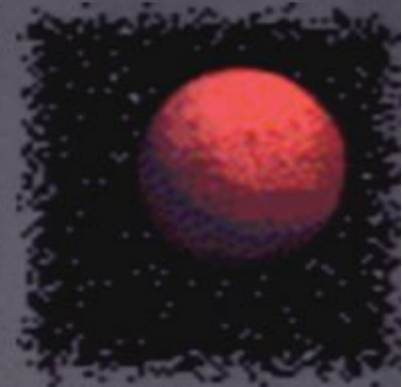












What do we mean by "teleportation"?

What do we mean by "teleportation"?



What do we mean by "teleportation"?



What do we mean by "teleportation"?



Disappear Here

What do we mean by "teleportation"?



What do we mean by "teleportation"?



Reappear There

What do we mean by "teleportation"?



- ✓ Must be a time delay ($<$ speed of light)

What do we mean by "teleportation"?



✓ Must be a time delay ($<$ speed of light)



What do we mean by "teleportation"?



✓ Must be a time delay ($<$ speed of light)



Disassemble into
individual atoms...

What do we mean by "teleportation"?



✓ Must be a time delay ($<$ speed of light)



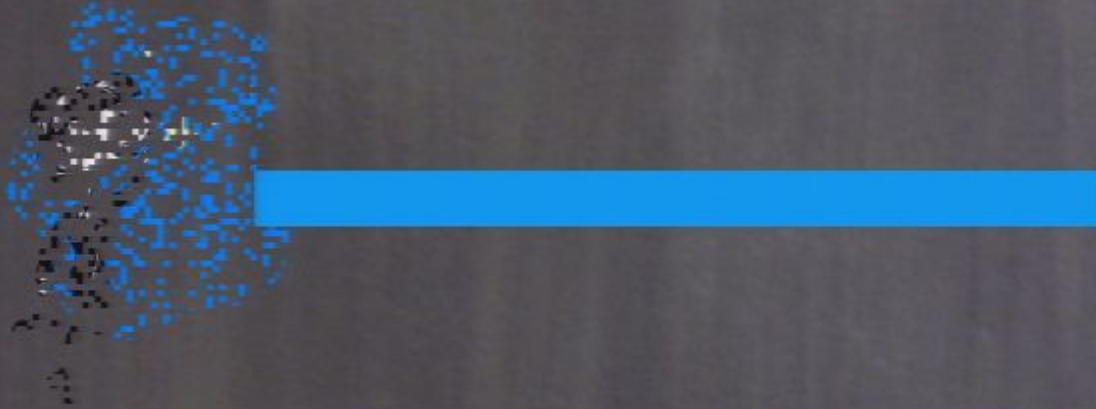
Disassemble into
individual atoms...

...beam the
physical atoms

What do we mean by "teleportation"?



✓ Must be a time delay ($<$ speed of light)



Disassemble into individual atoms...

...beam the physical atoms

What do we mean by "teleportation"?



✓ Must be a time delay ($<$ speed of light)



Disassemble into
individual atoms...

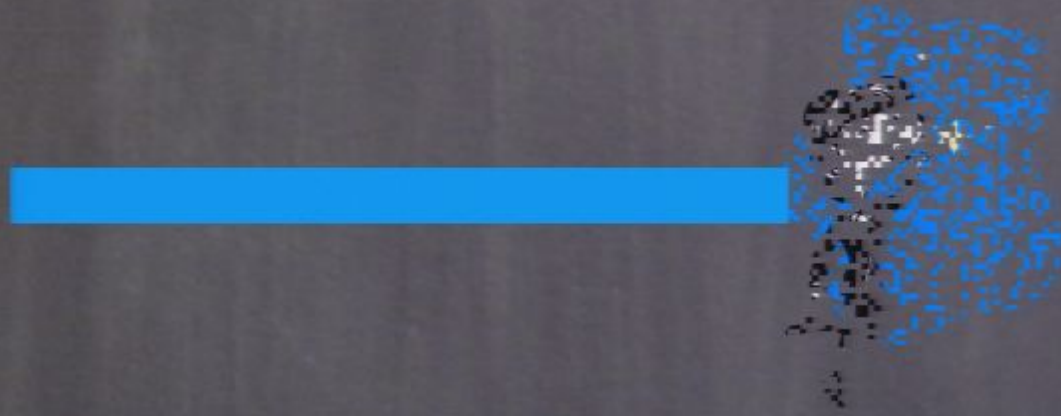
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Unnecessarily complicated!

Quantum Fact: All atoms of same type are truly identical

Need only send the information, not the atoms

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11101011101010101100100110



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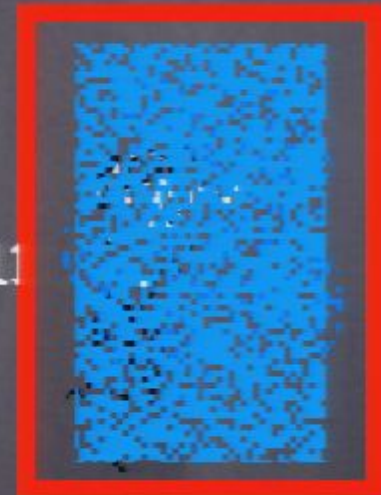


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10010



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Quantum teleportation *must* destroy the original Alice

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There can be only one Alice \rightarrow



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Question: How do we measure the "quantum information" in Alice's atoms?

Answer: We can't!

Quantum Facts: *Heisenberg Uncertainty limits the amount of information that can be extracted*
Worse: Certain quantum information cannot be measured at all!

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we can't even measure the information we wish to send,
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NO: In 1993 Charles Bennett *et al* discovered that quantum entanglement could be used to send the information without actually measuring it!

What do we mean by "teleportation"?



- ✓ Must be a time delay (speed of light)
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- ✓ The original Alice is destroyed (teleporting, not copying)
- ✓ Quantum teleportation is possible using entanglement

Quantum Teleportation

here's how it works:

Quantum Teleportation

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Warning: The Following is *Science Fiction*

Quantum Teleportation

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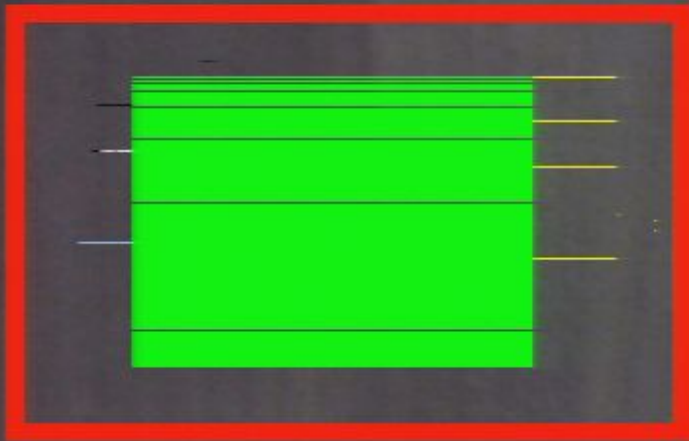
here's how it works:



```
101101101
001101110
101101101
```

Quantum Teleportation

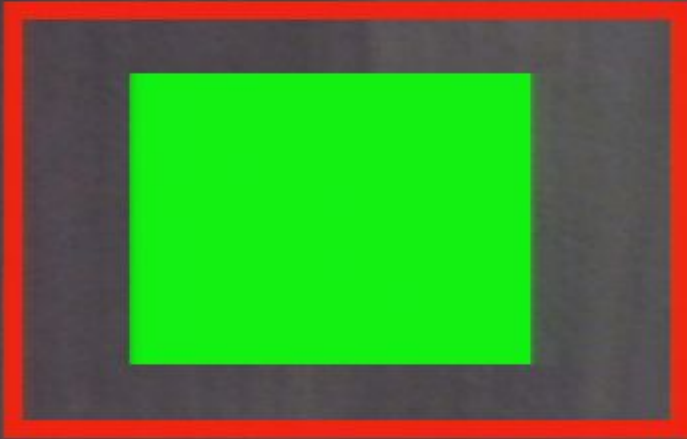
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```
101101010  
010111010  
011011011  
101101101  
001101110  
101101101
```

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```
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```

$$\frac{d}{dx}(e^{\alpha x}) = \alpha e^{\alpha x}$$

(?)

| (?)

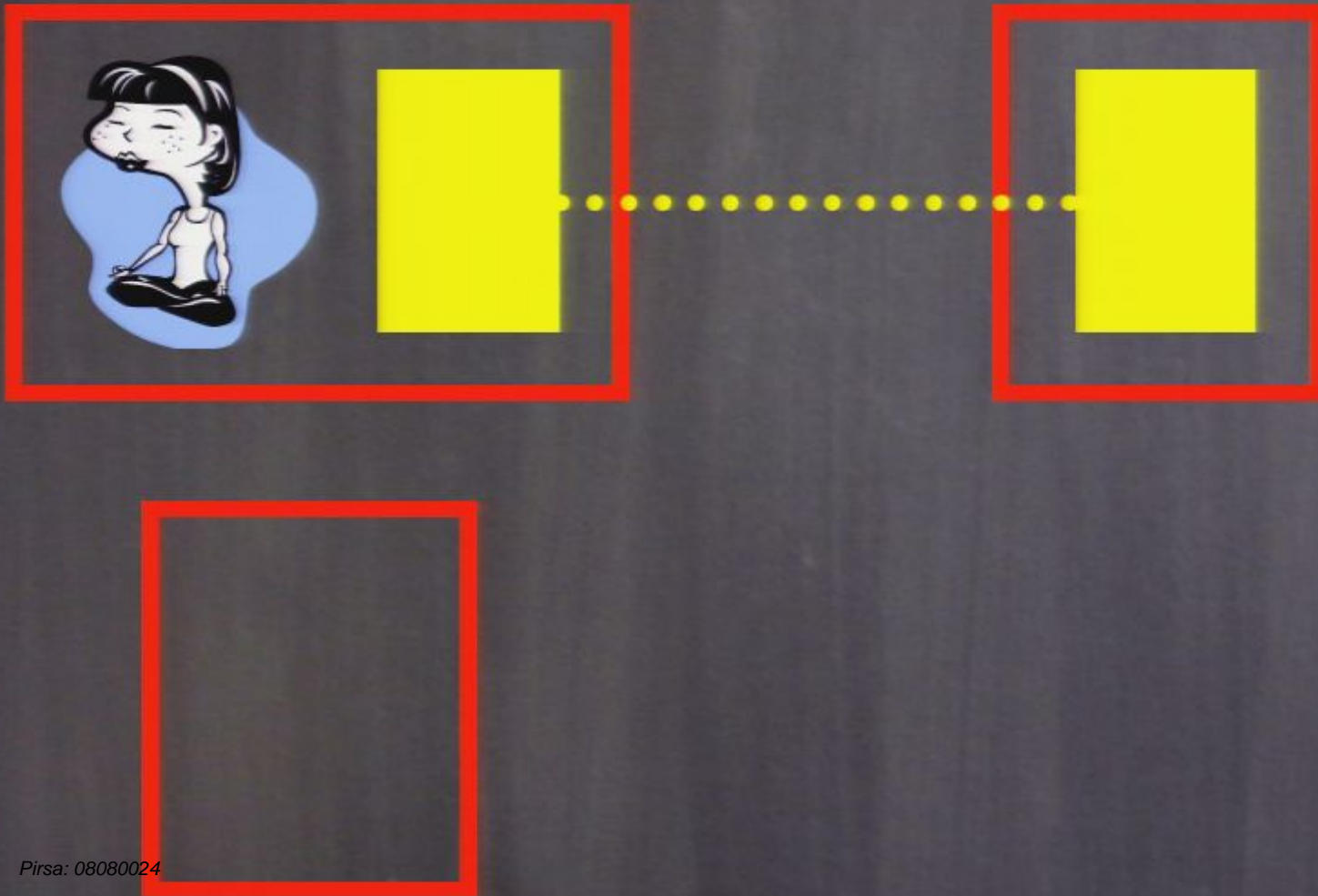
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A

B

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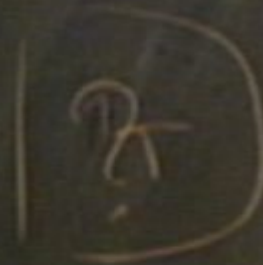
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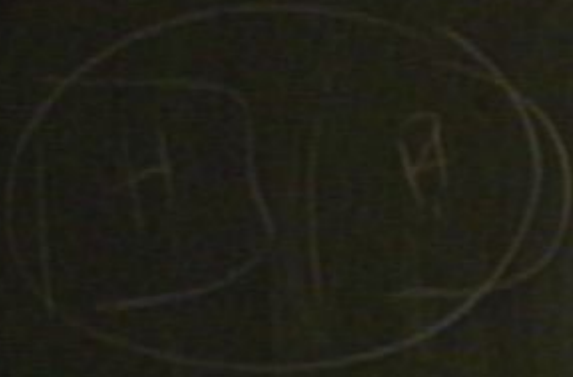


101101010
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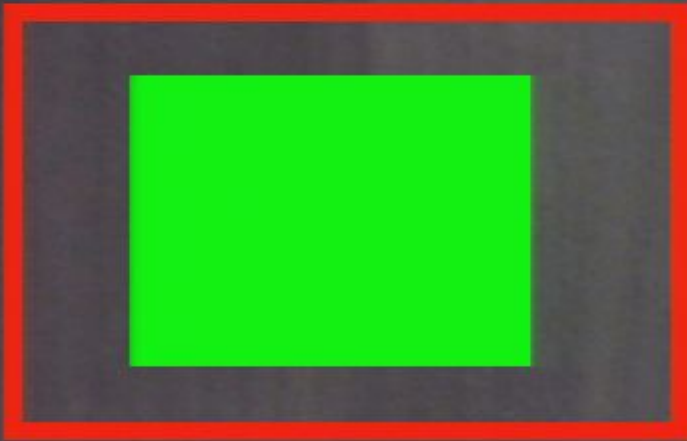
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Quantum Teleportation

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Quantum Teleportation

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A quantum identical version of Alice on Mars!

