

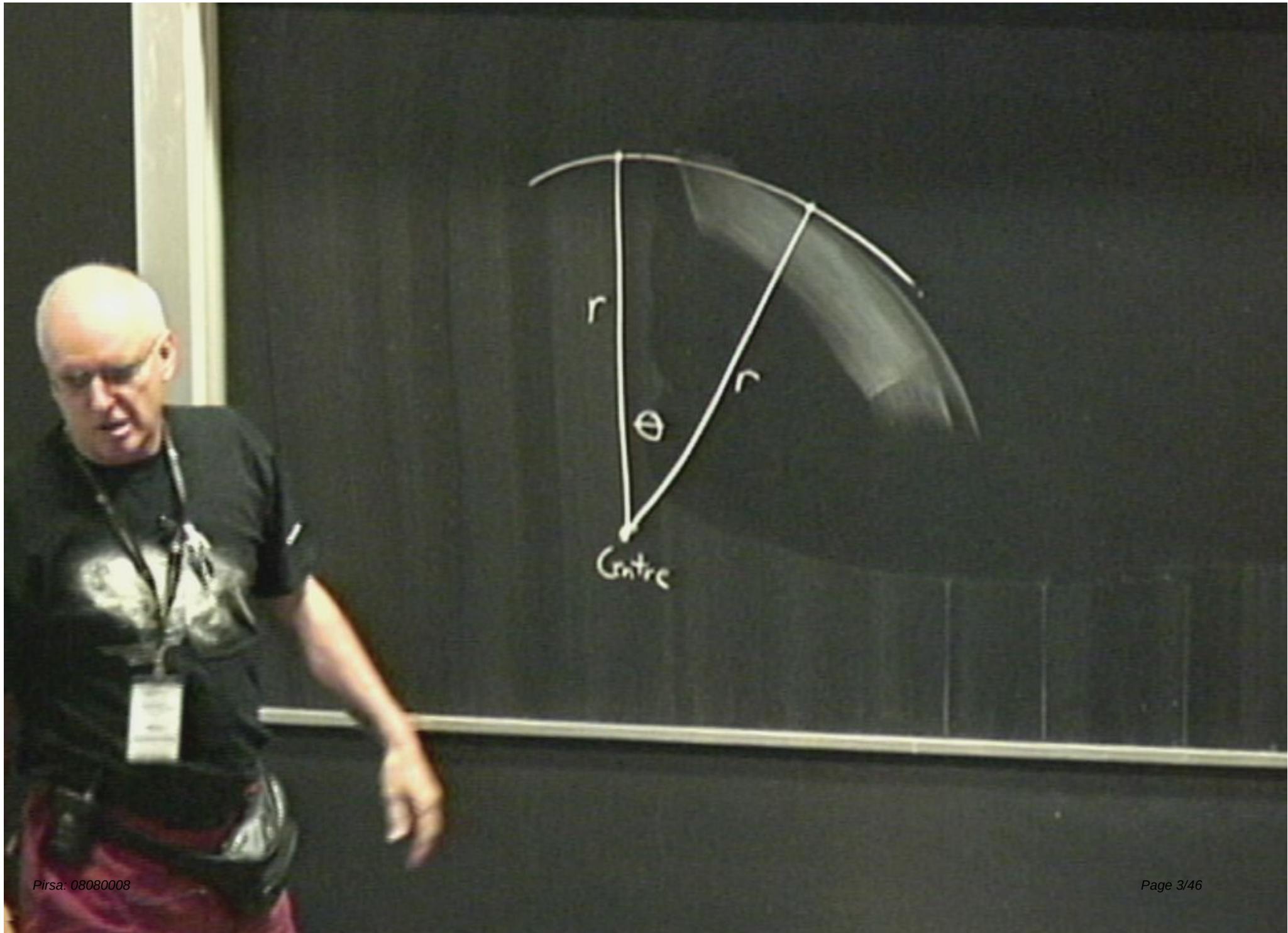
Title: Dark Matter

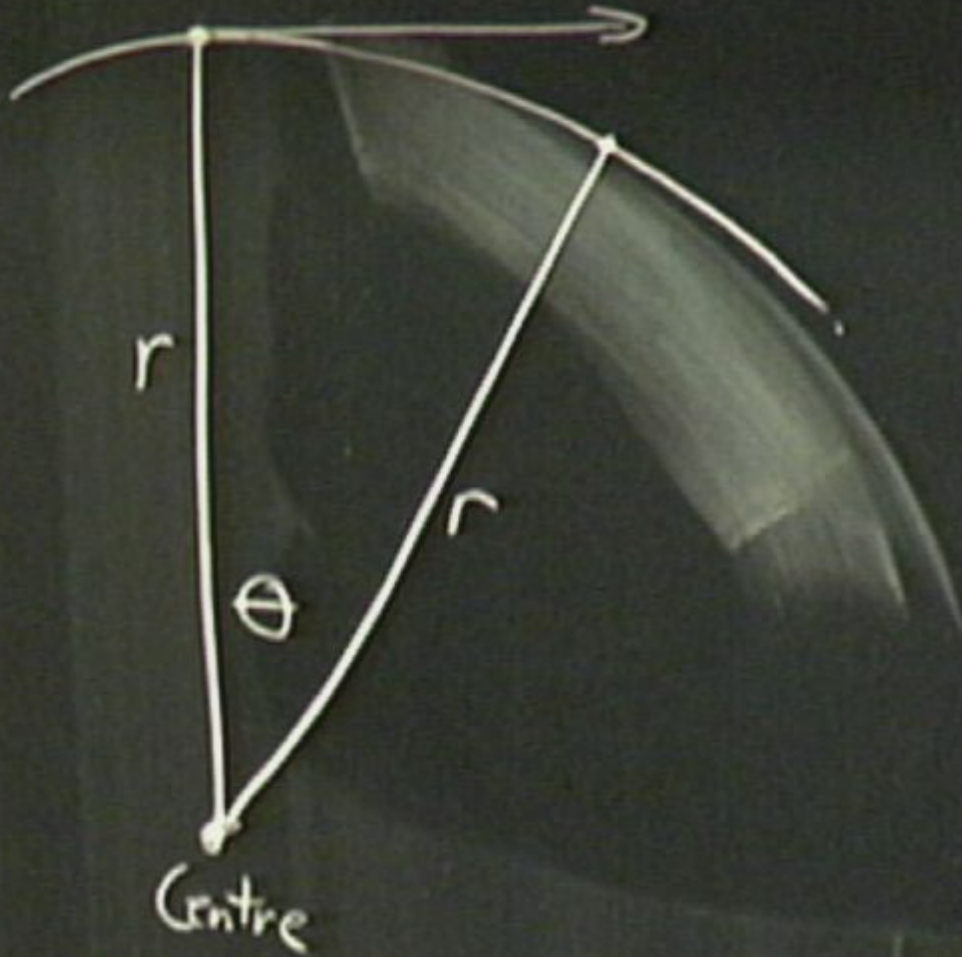
Date: Aug 02, 2008 09:00 AM

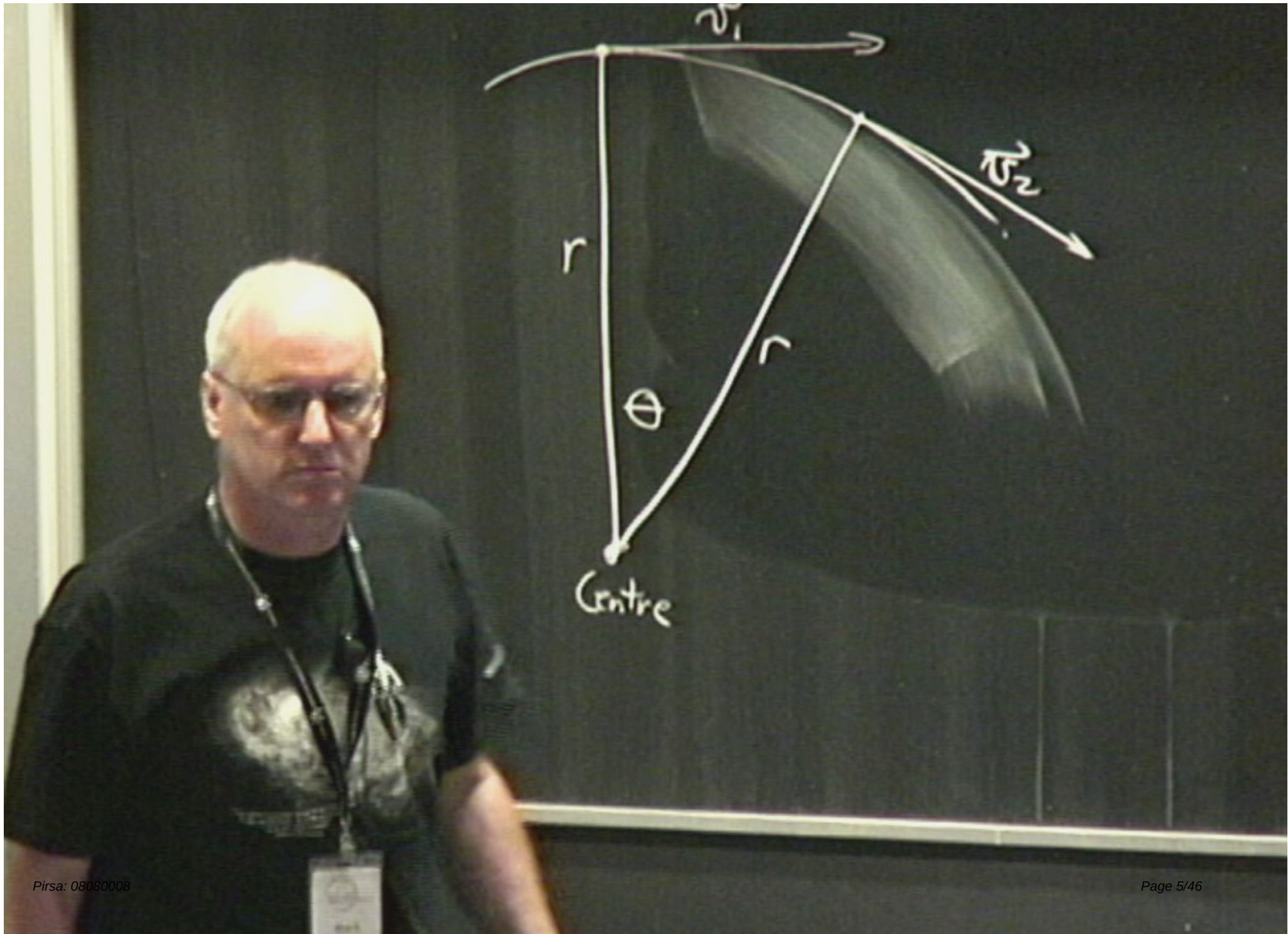
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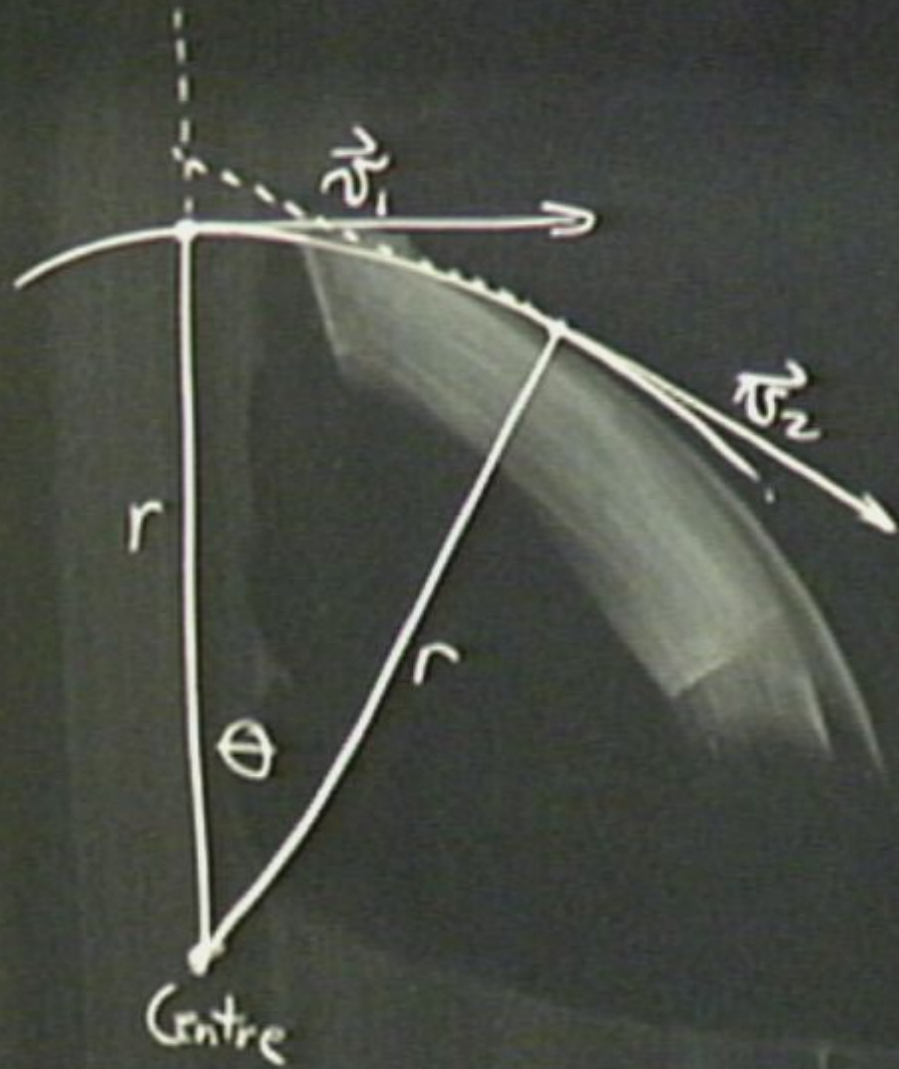
Abstract:







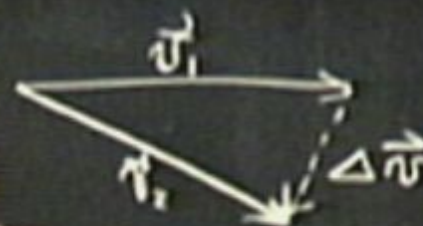




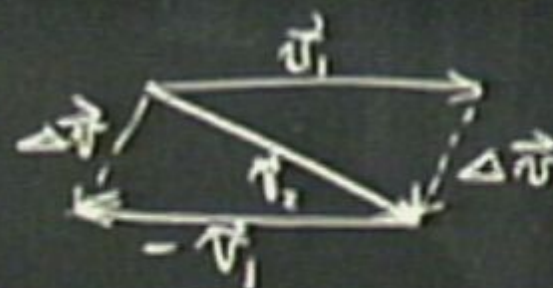
$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$



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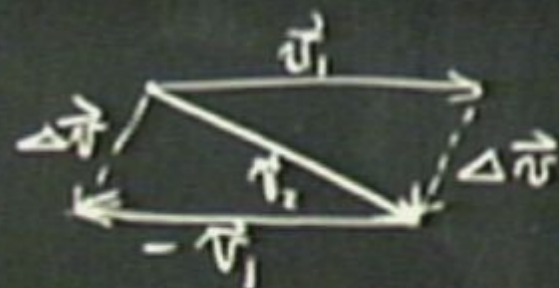
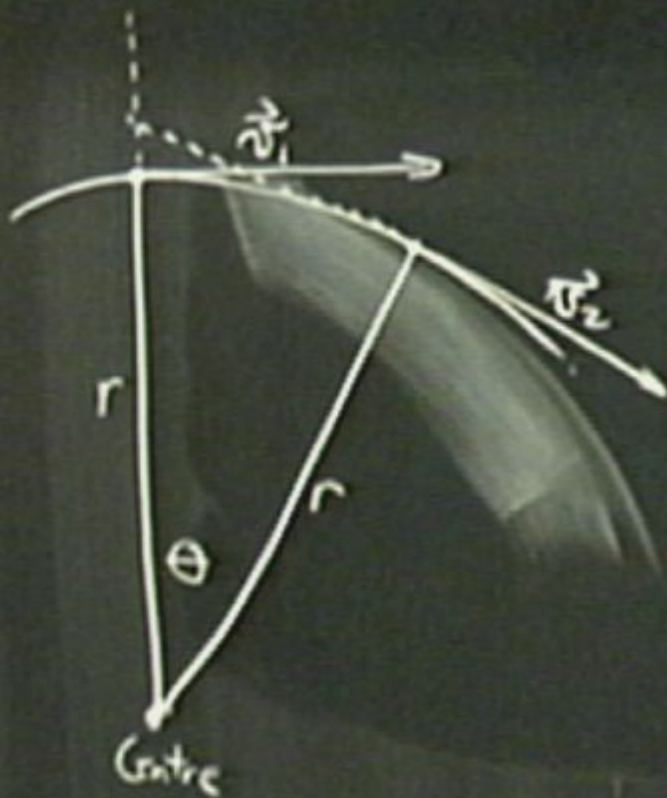


$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$



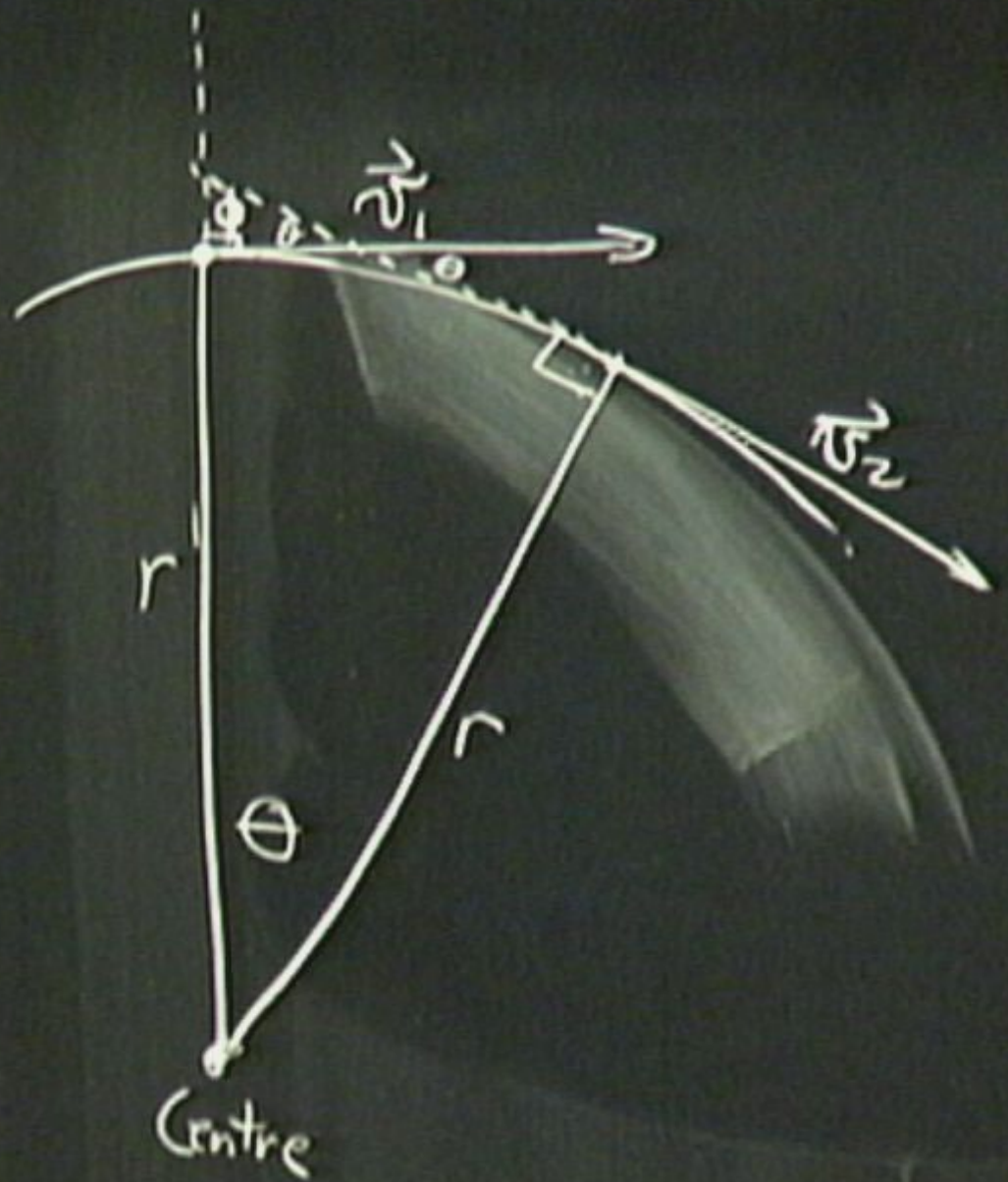
$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

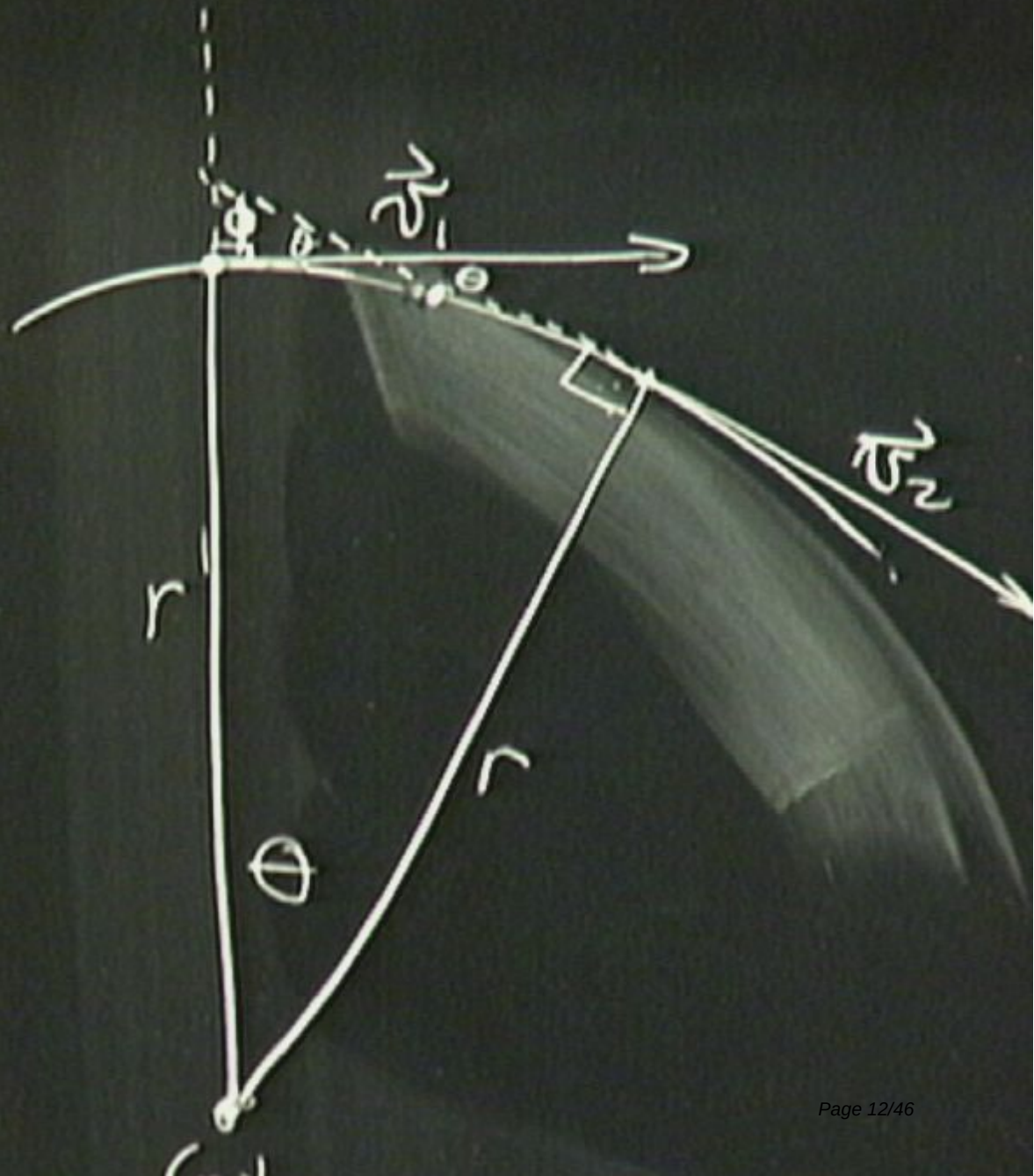


$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$

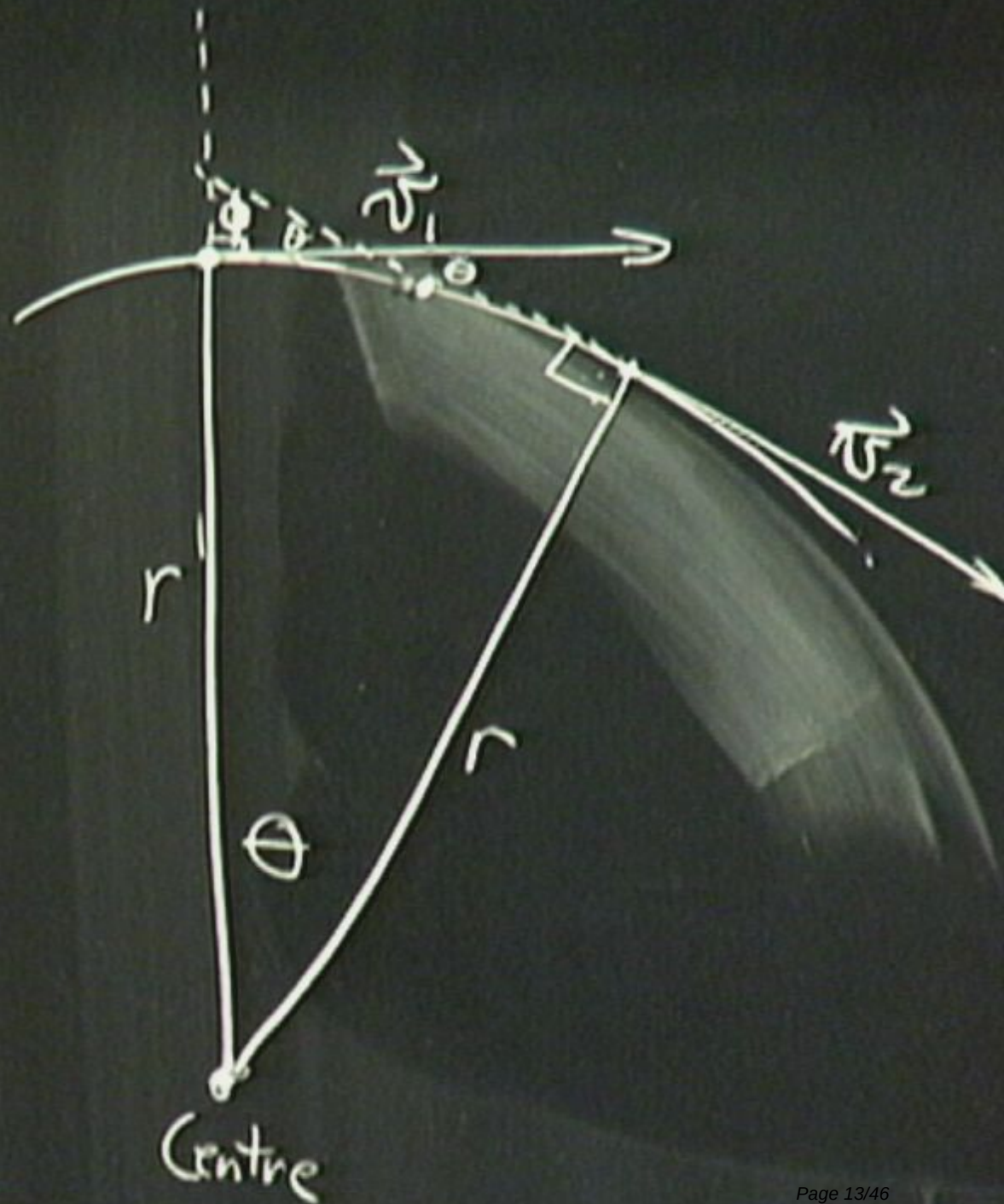
$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

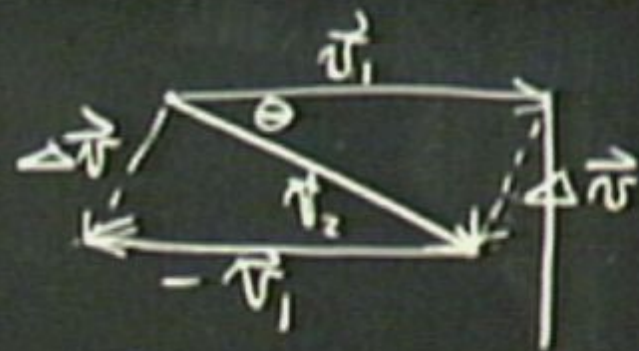


$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

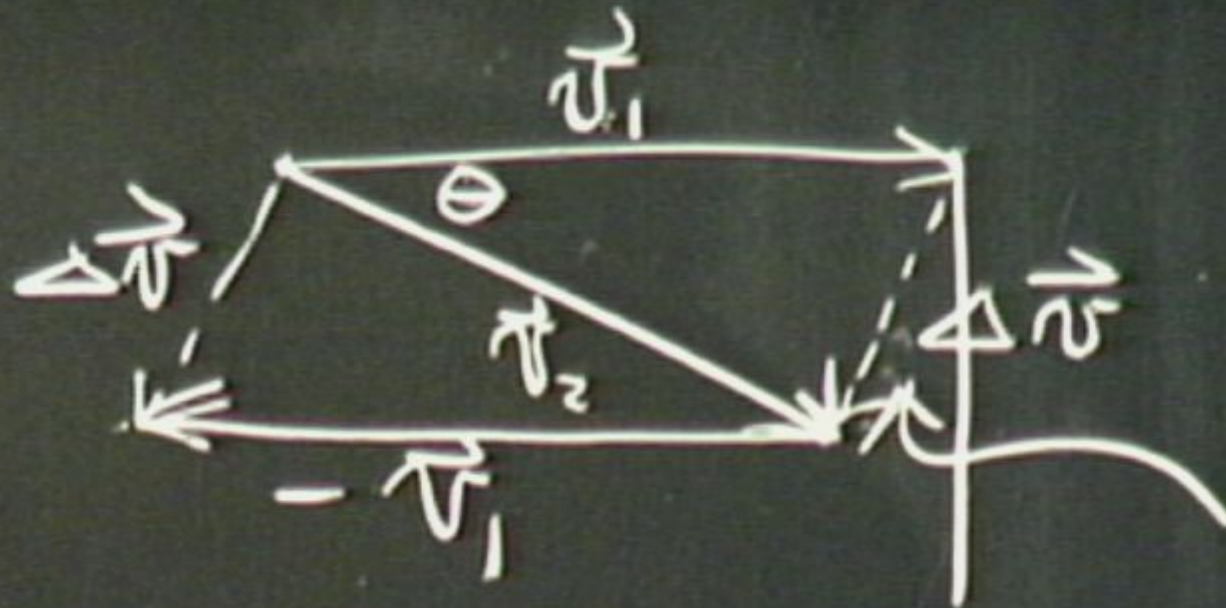


$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

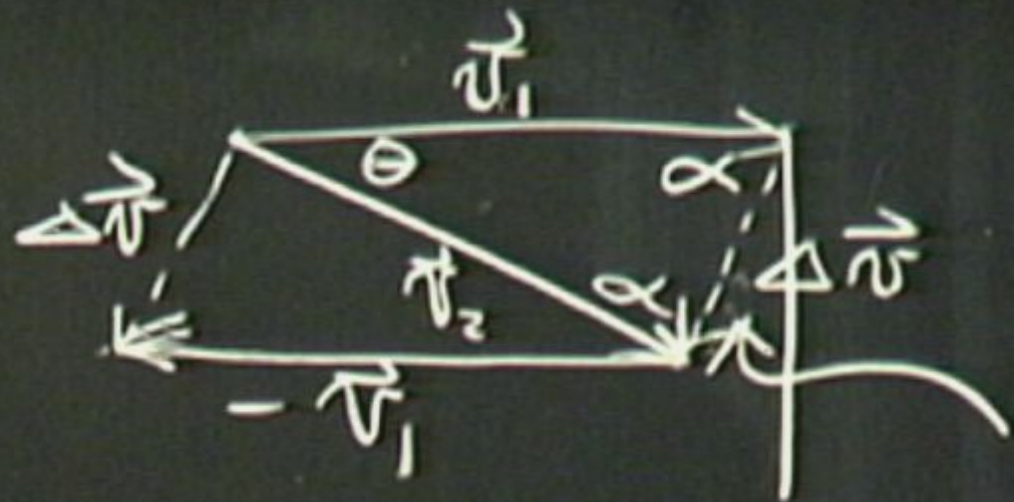
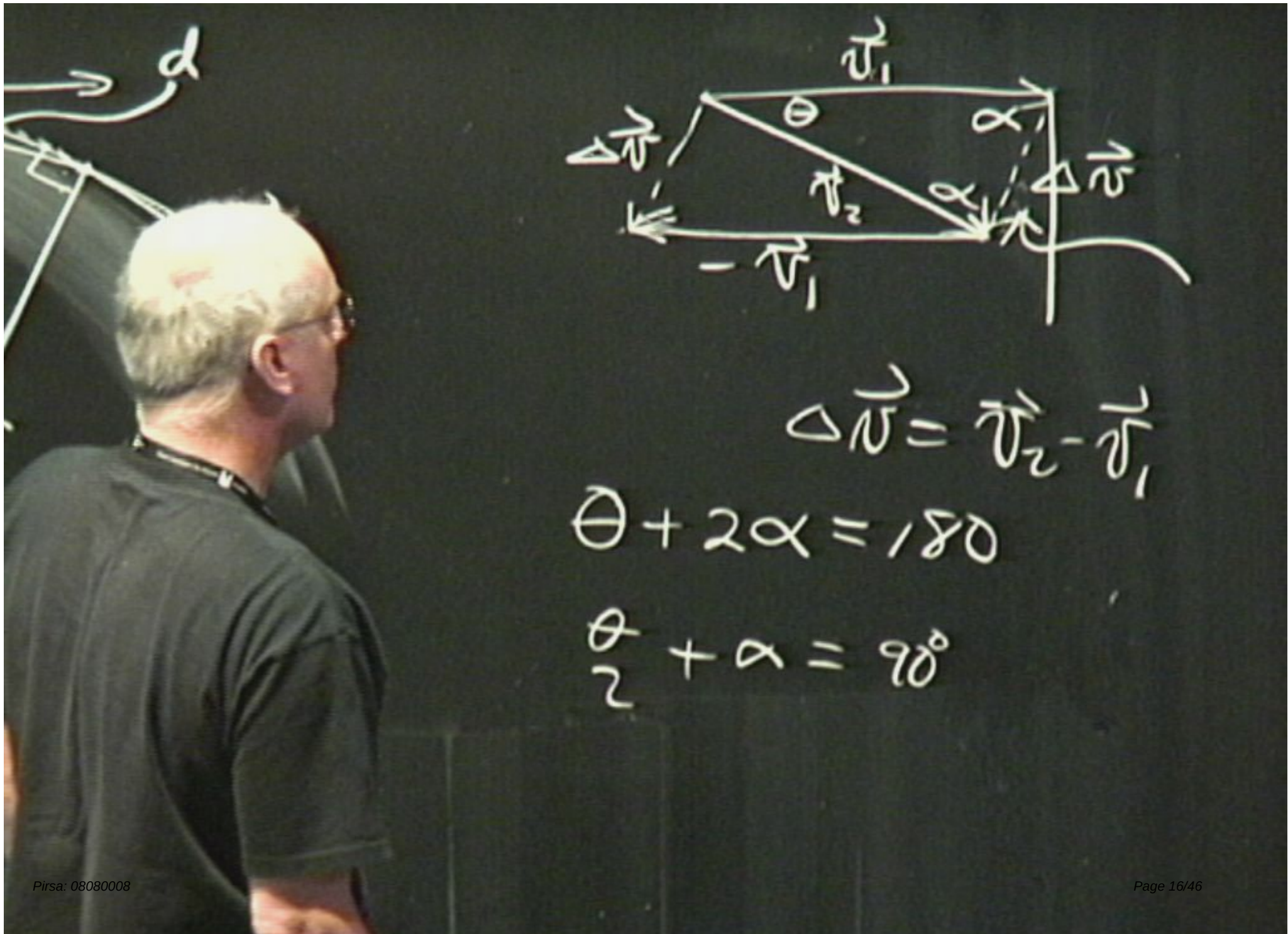




$$\Delta\vec{v} = \vec{v}_2 - \vec{v}_1$$



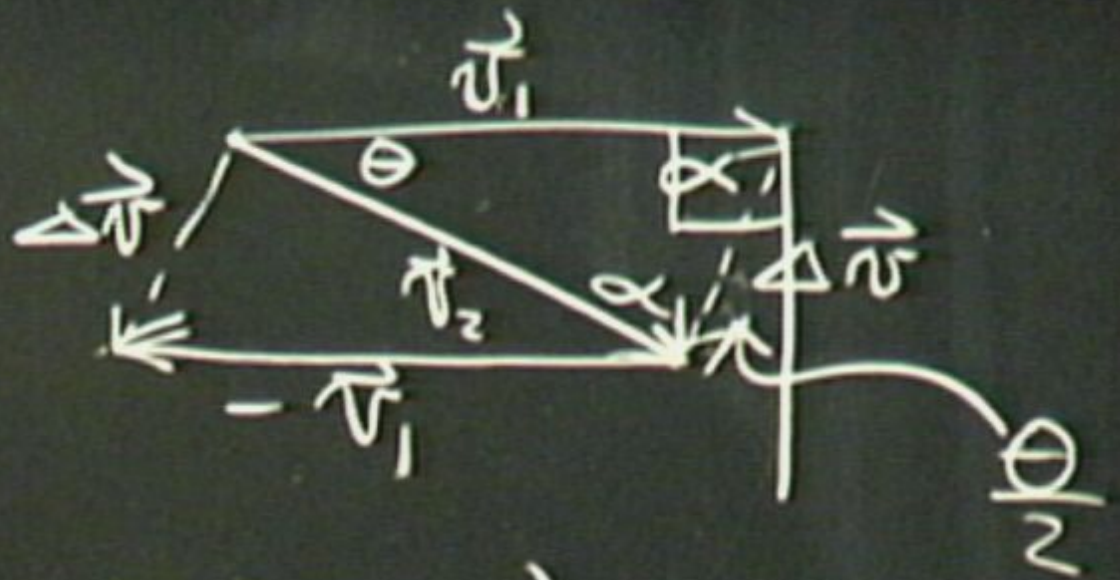
$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$



$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$

$$\theta + 2\alpha = 180$$

$$\frac{\theta}{2} + \alpha = 90^\circ$$

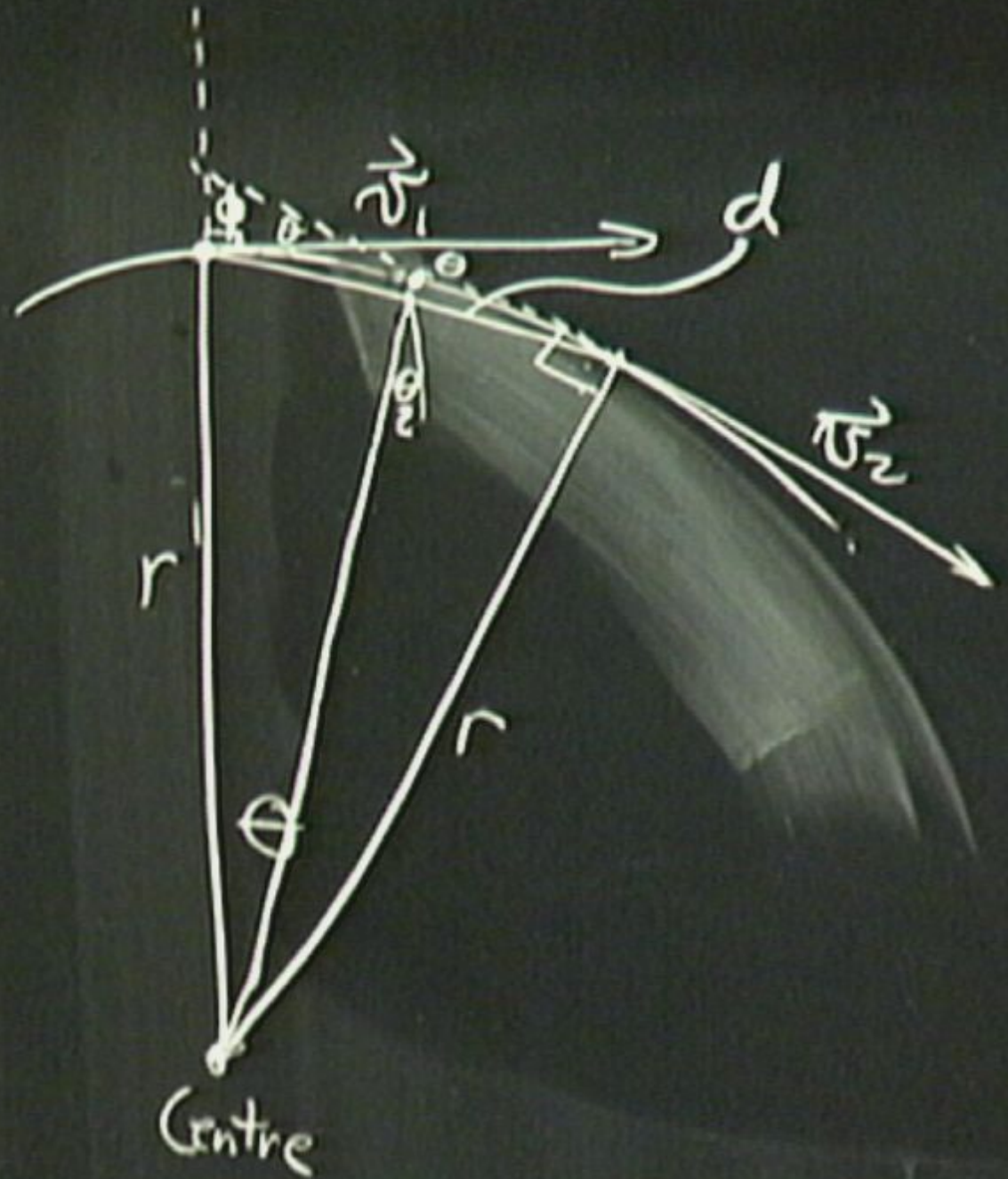


$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$

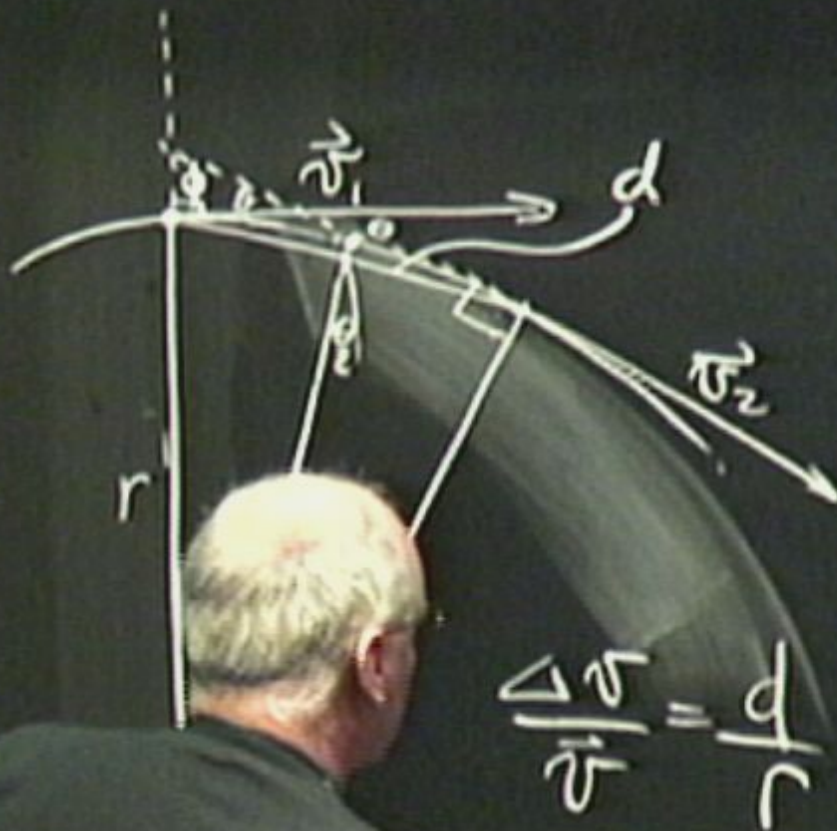
$$\theta + 2\alpha = 180$$

$$\frac{\theta}{2} + \alpha = 90^\circ$$

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$



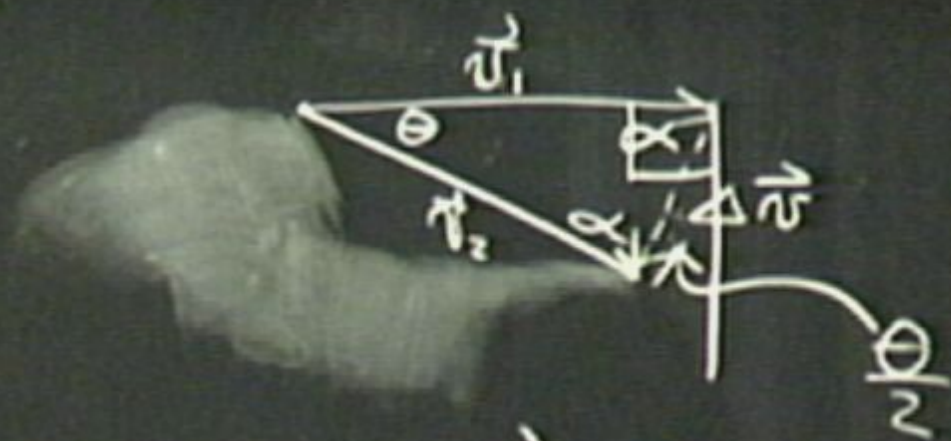
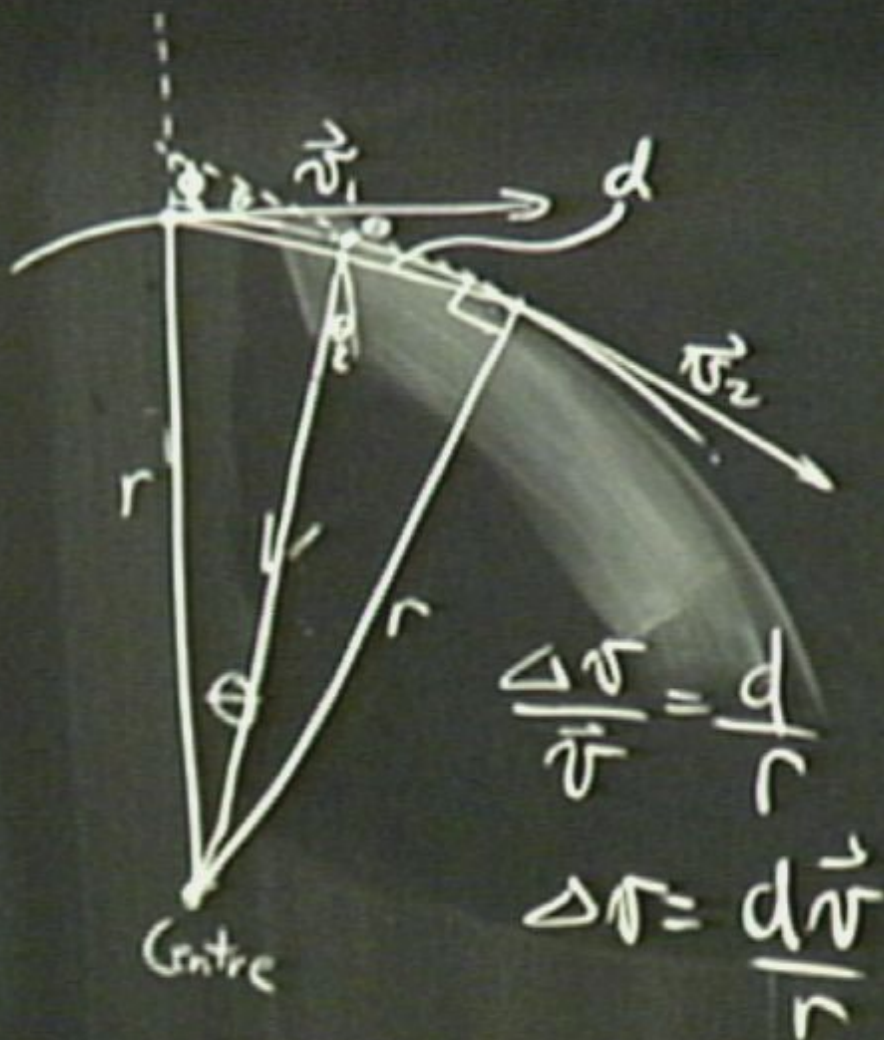
$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$



$$\frac{\Delta \vec{v}}{\Delta t} = \frac{d}{r/c}$$

$$\theta + 2$$

$$\frac{\theta}{2} + \theta$$



$$\Delta \vec{v} = \vec{v}_2 - \vec{v}_1$$

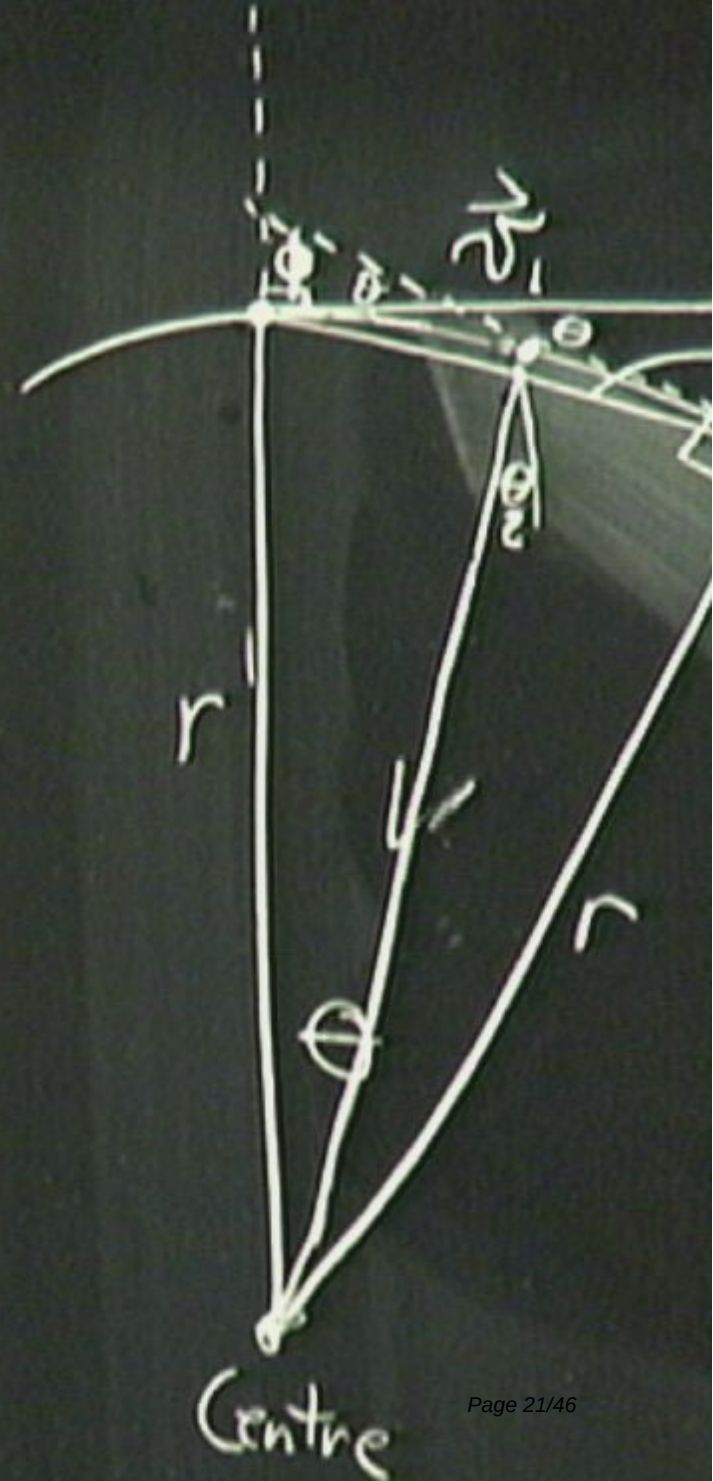
$$\theta + 2\alpha = 180$$

$$\frac{\theta}{2} + \alpha = 90^\circ$$

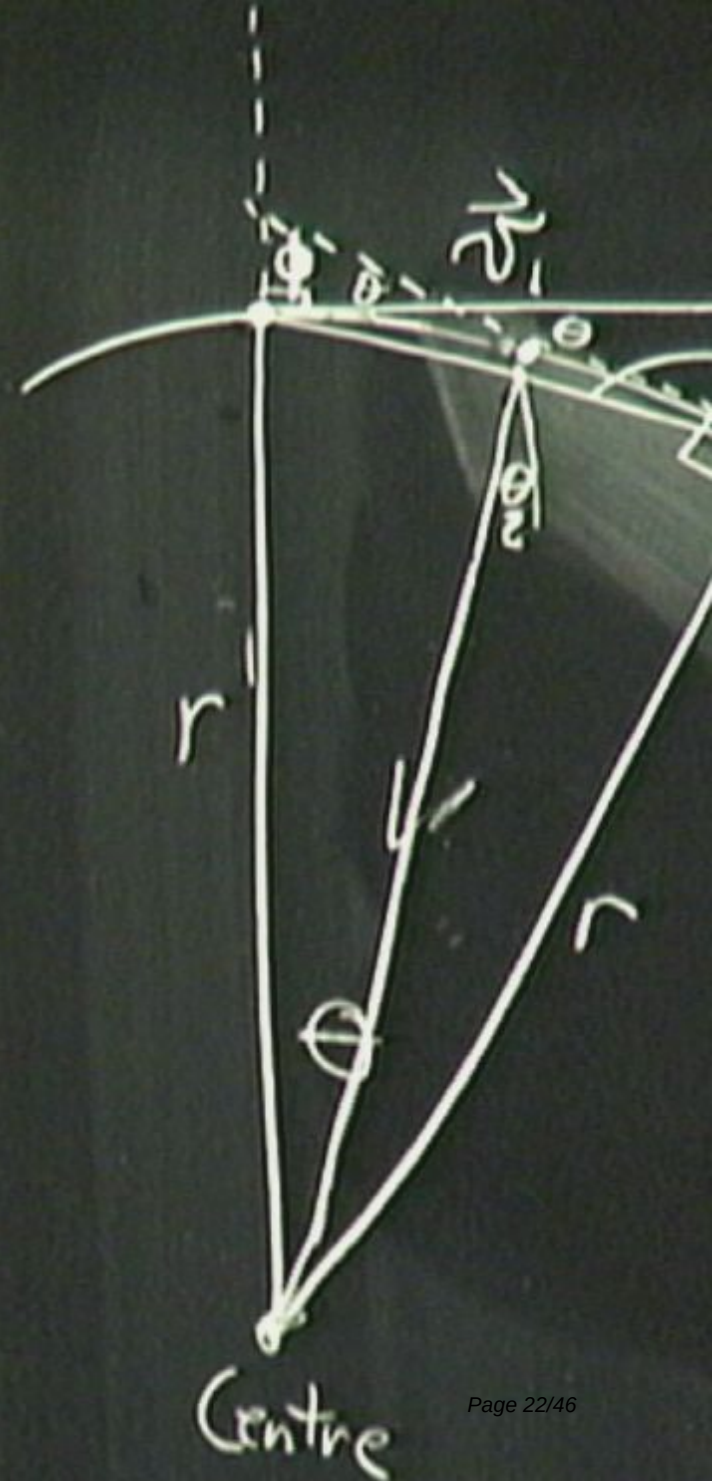
$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$= \frac{d\vec{v}}{dt}$$

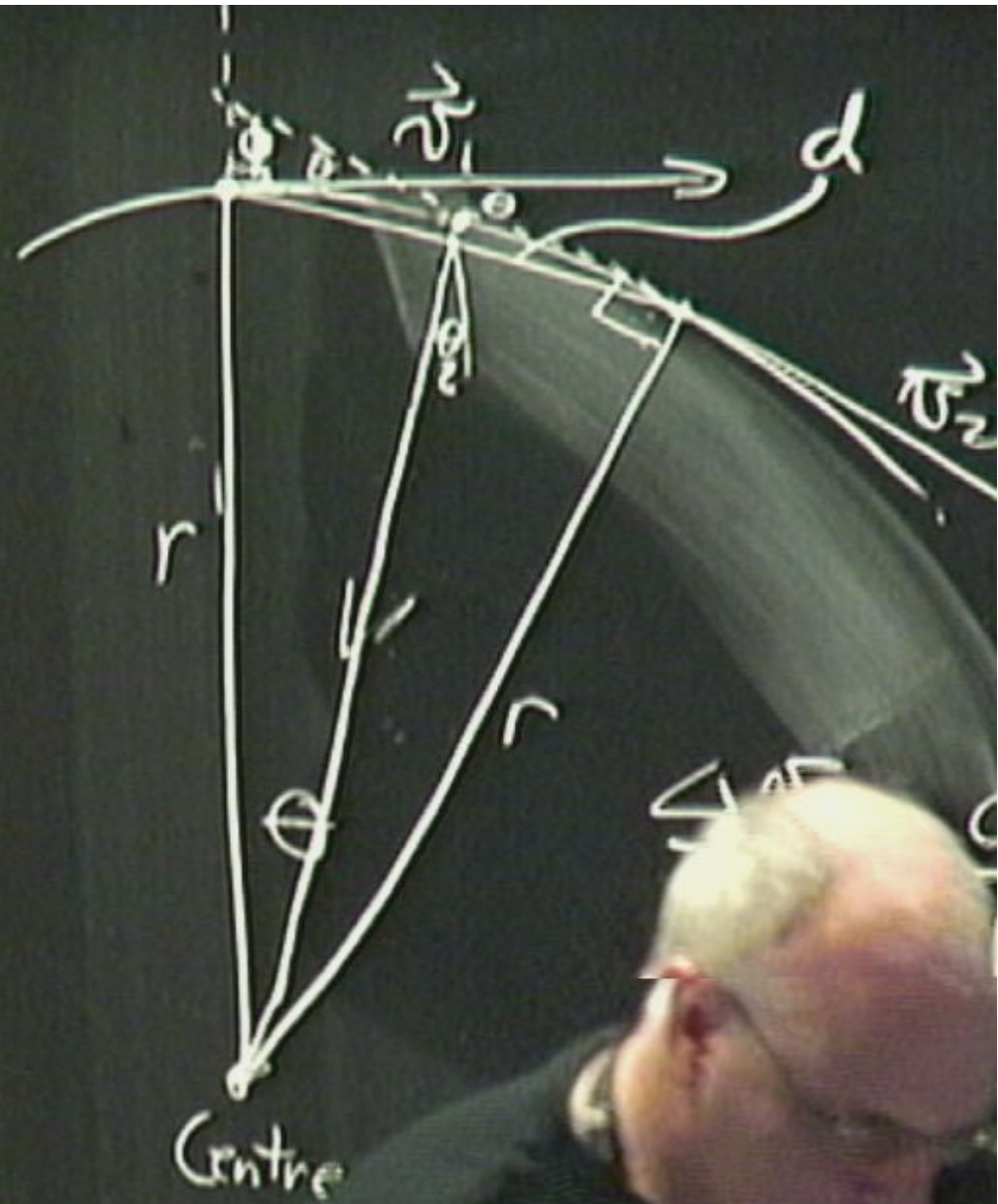
$$= \frac{d}{dt} \frac{z}{r}$$



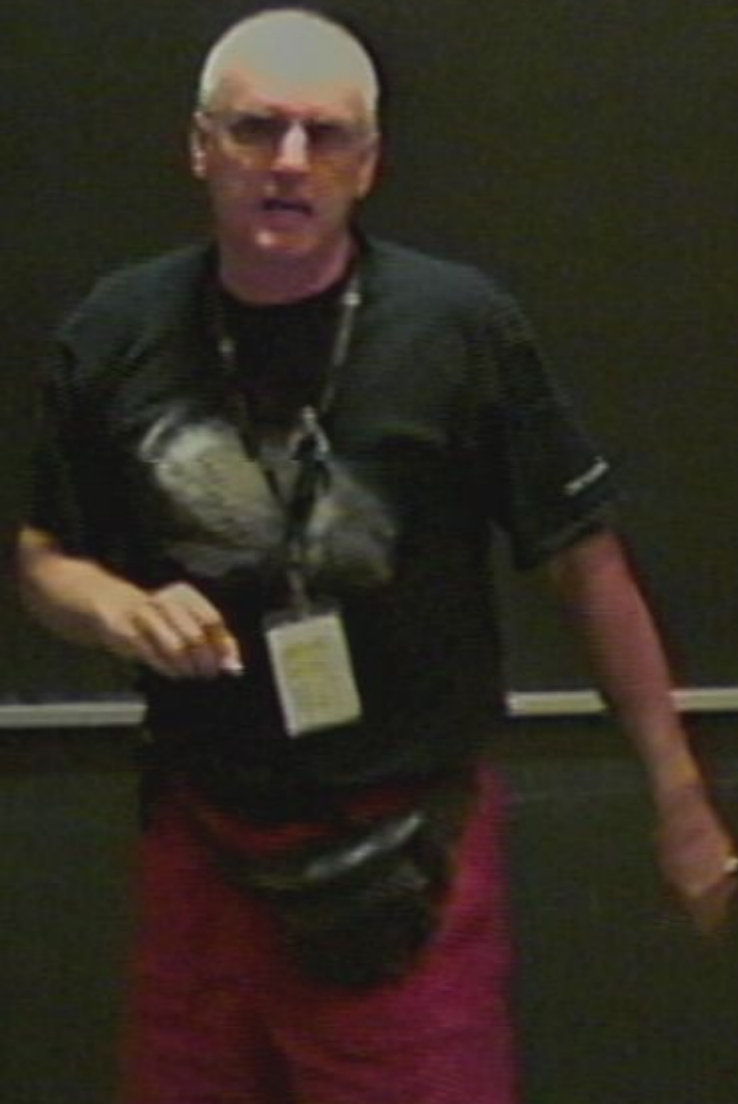
$$\begin{aligned}
 \vec{a} &= \frac{\Delta \vec{v}}{\Delta t} \\
 &= \frac{d\vec{v}}{r dt} \\
 &= \frac{d}{dt} \frac{\vec{v}}{r}
 \end{aligned}$$



$$\begin{aligned}
 \vec{a} &= \frac{\Delta \vec{v}}{\Delta t} \\
 &= \frac{d\vec{v}}{r dt} \\
 &= \frac{d}{dt} \frac{\vec{v}}{r} \\
 &= \frac{v}{r} \frac{d\vec{v}}{v} \\
 &= \frac{v}{r} \frac{d\theta}{dt} \hat{e}_\theta
 \end{aligned}$$



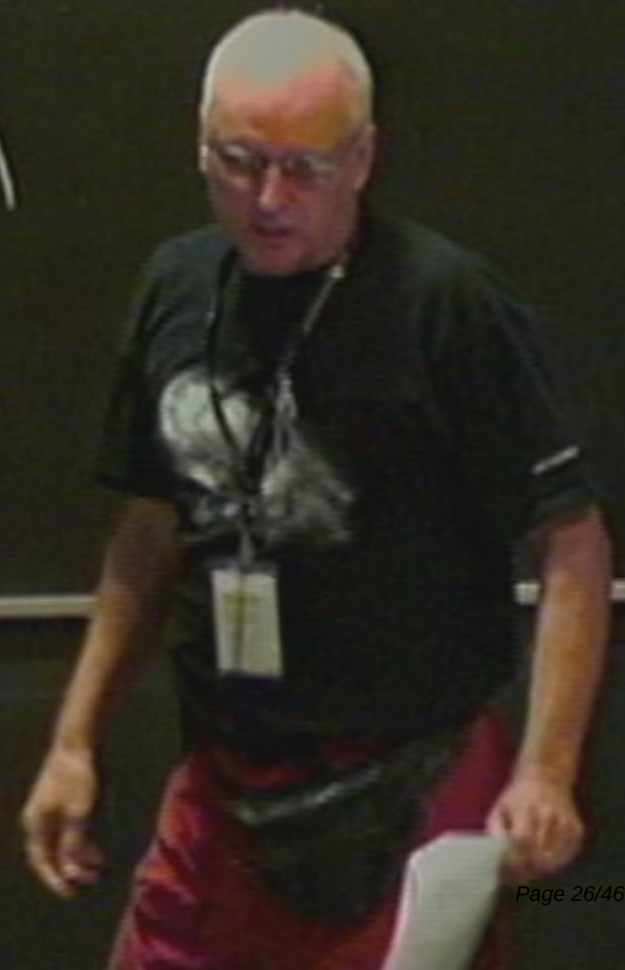
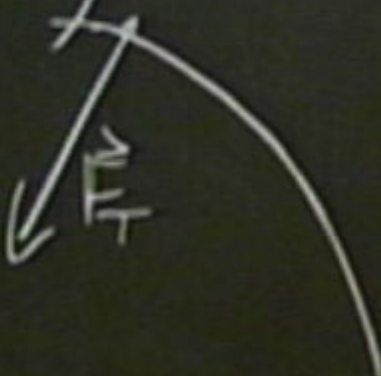
$\vec{F}_{un}$ ($\vec{F}_{net}$)
unbalanced force



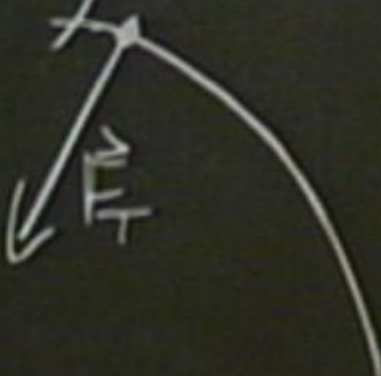
$$\vec{F}_{un} = (\vec{F}_{net})(\Sigma F).$$

unbalanced force

$\vec{F}_{un}$ ($\vec{F}_{net}$) ($\Sigma \vec{F}$)
unbalanced force

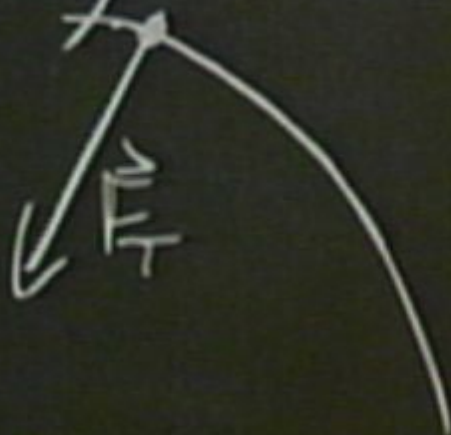


$\vec{F}_{un}$ ($\vec{F}_{net}$) ($\Sigma \vec{F}$)
unbalanced force



$$\vec{F}_{un} = \vec{F}_T$$

$\vec{F}_{un}$ ($\vec{F}_{net}$) ($\Sigma \vec{F}$)
 unbalanced force



$$\begin{aligned}
 \vec{F}_{un} &= \vec{F}_T \\
 m\vec{a} &= \vec{F}_T \\
 \left(\frac{mv^2}{r} \right) &= \vec{F}_T
 \end{aligned}$$

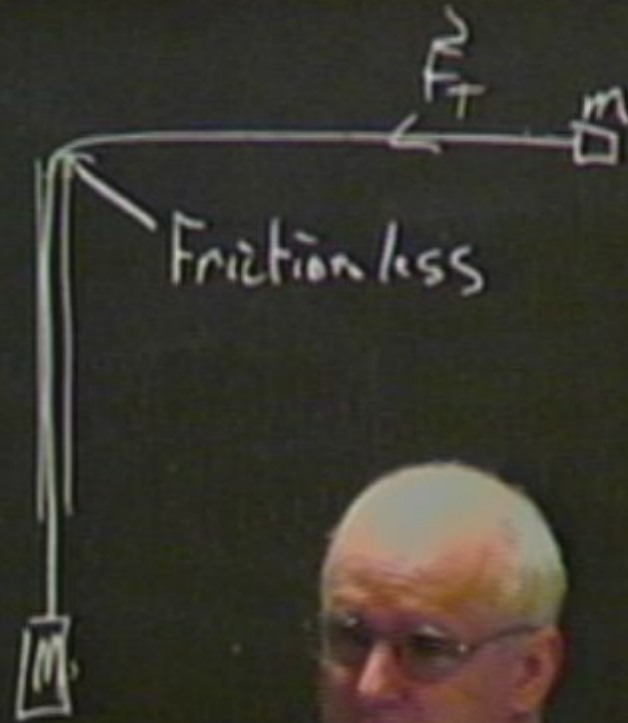
centripetal force



$$\vec{F}_{\text{net}} = \vec{F}_g + \vec{F}_T$$

$$\vec{F}_T = -\vec{F}_g$$

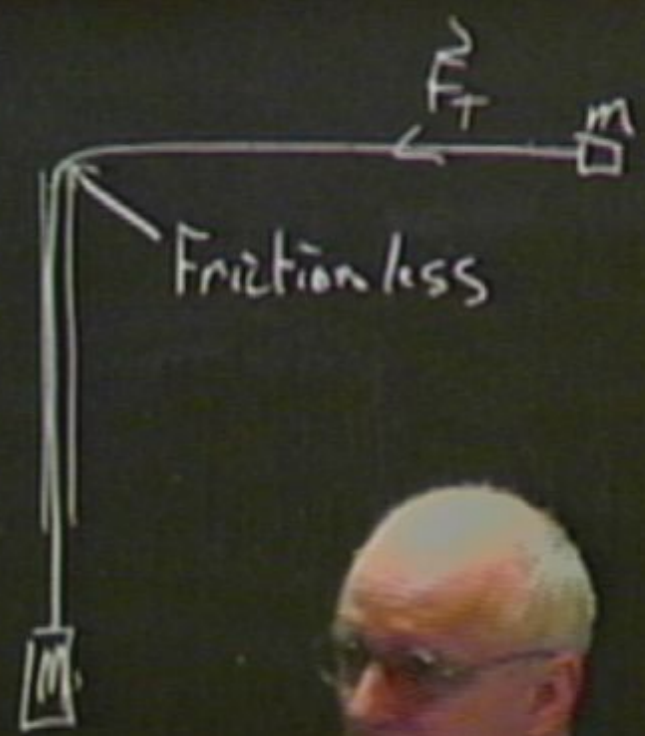
$$= -Mg$$

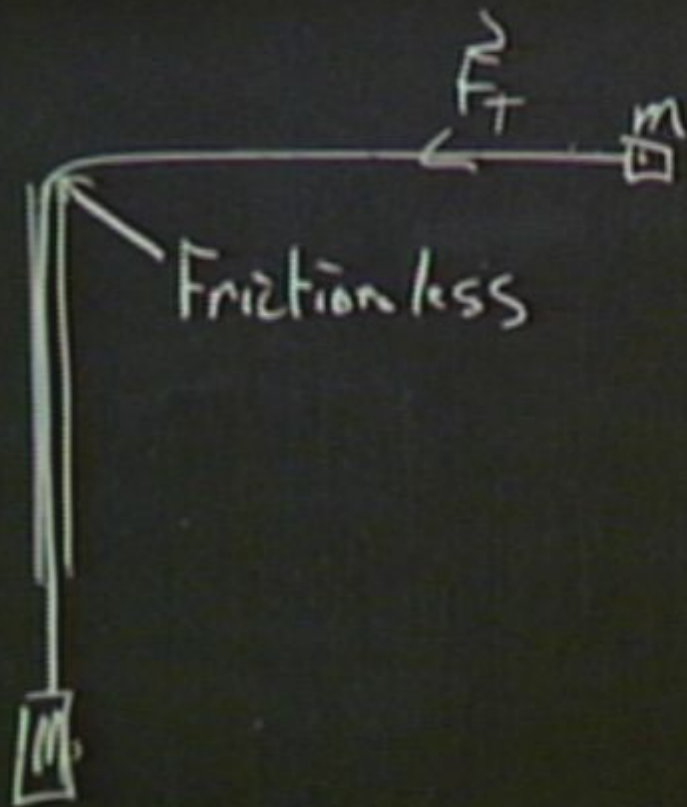


$$\vec{F}_{\text{sum}} = \vec{F}_g + \vec{F}_T$$

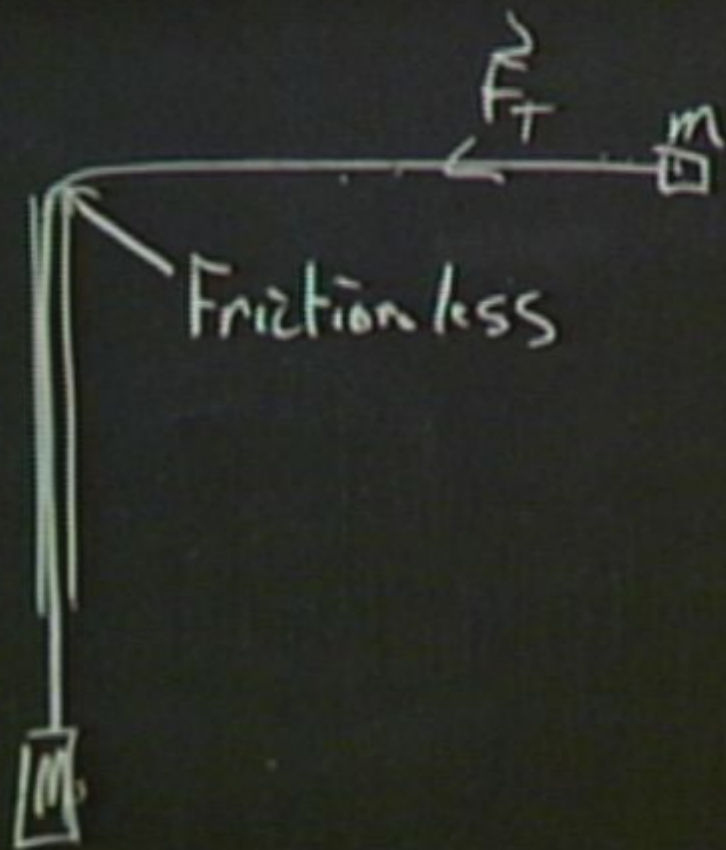
$$\vec{F}_T = -\vec{F}_g$$

$$= -Mg$$





$$F_{un} = F_T$$



$$F_{\text{un}} = F_T$$

$$ma_c = F_T$$

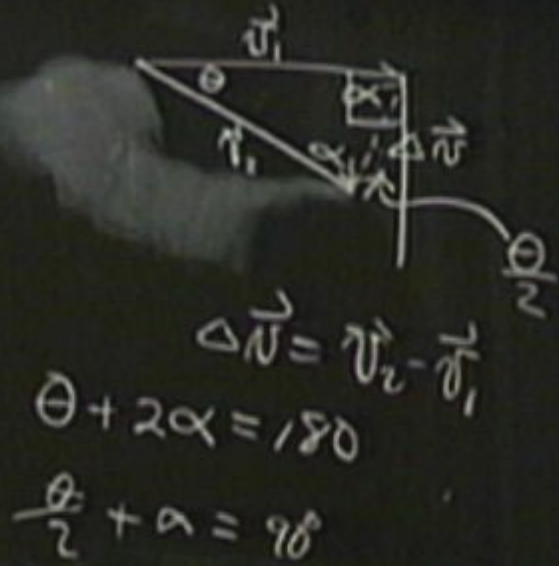
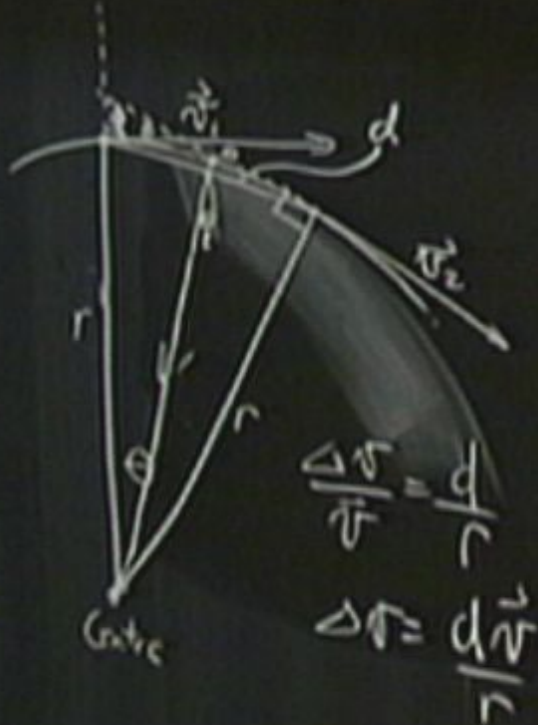
$$\frac{mv^2}{r} = Mg$$

$$v^2 = M$$

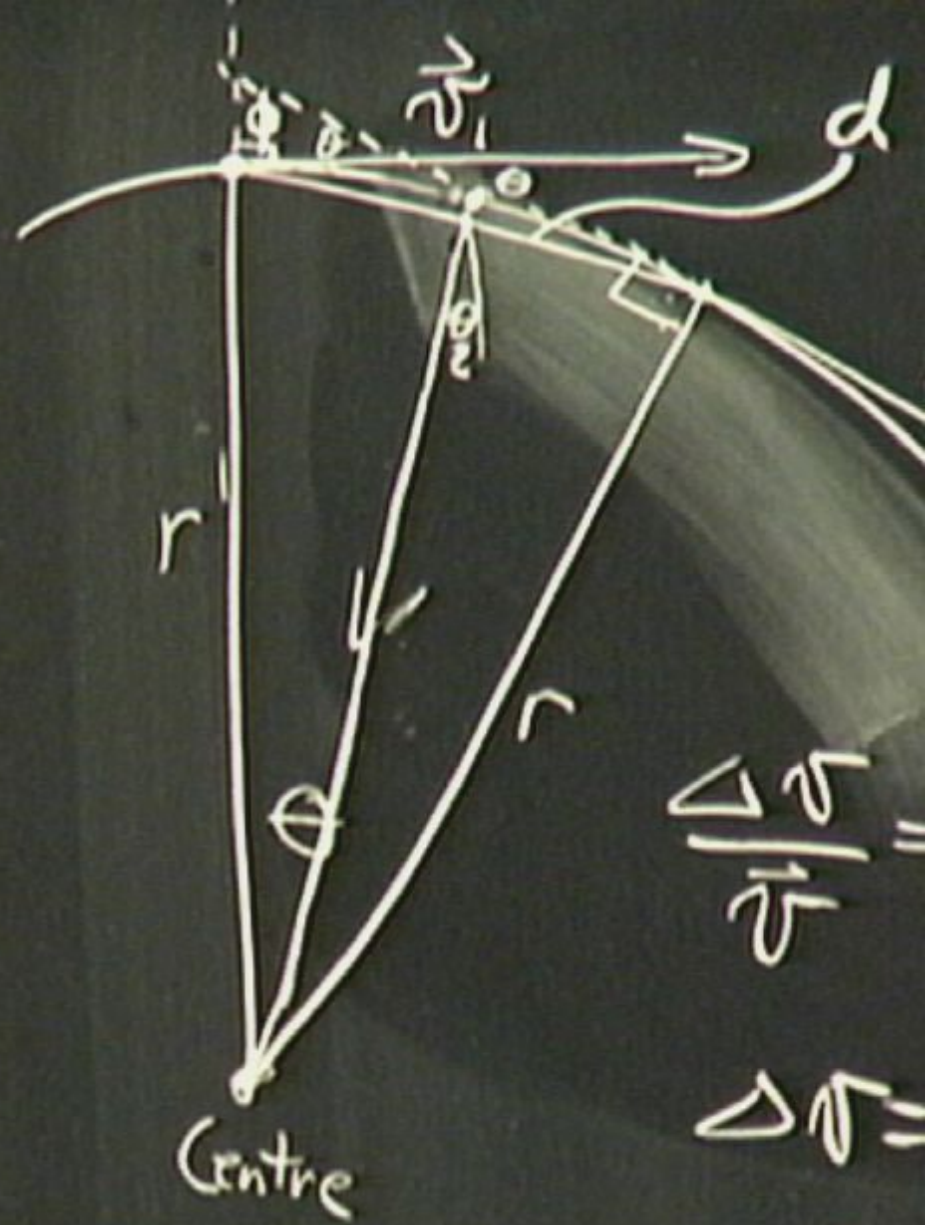
$$v = \sqrt{M}$$

$$\psi \propto r$$

$$\begin{aligned} \vec{a}_c &= \frac{\Delta \vec{v}}{\Delta t} \\ &= \frac{d\vec{v}}{dt} \\ &= \frac{d}{dt} \left(\frac{v}{r} \right) \\ &= \frac{dv}{dt} \frac{1}{r} \\ a_c &= \frac{dv}{dt} \frac{1}{r} \end{aligned}$$



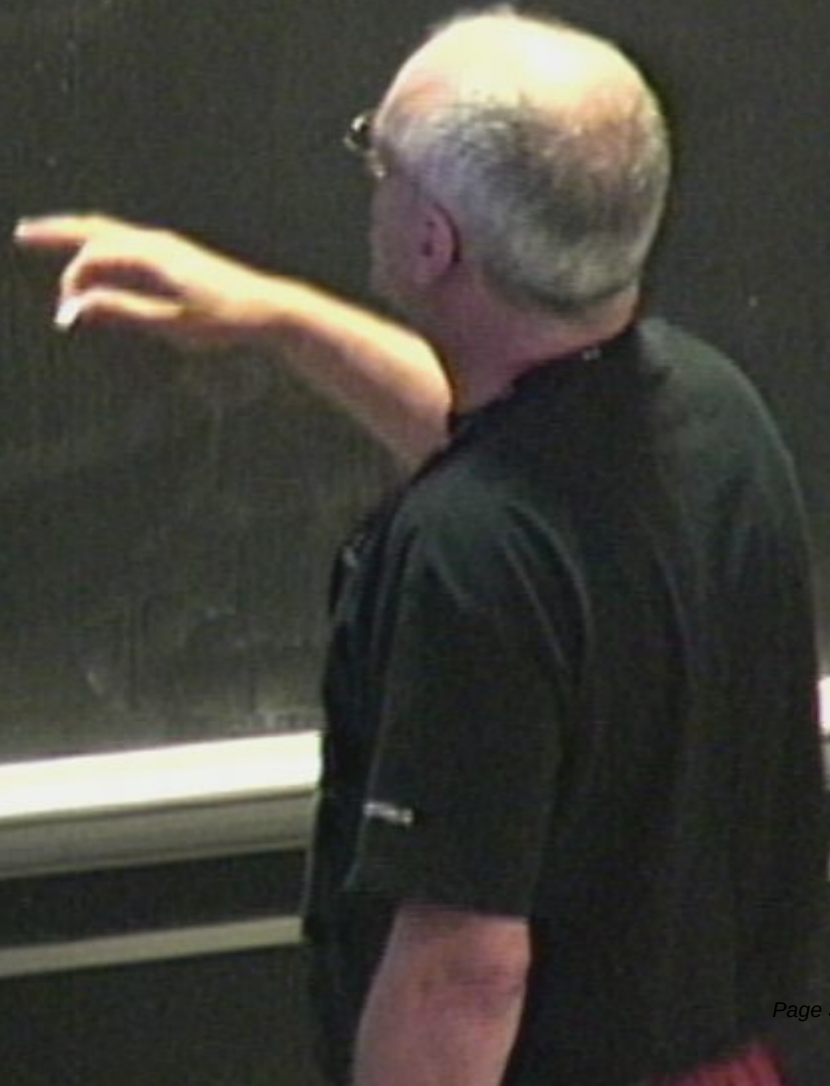
$$\begin{aligned}
 \vec{a}_c &= \frac{\Delta \vec{v}}{\Delta t} \\
 &= \frac{d\vec{v}}{r dt} \\
 &= \frac{d}{dt} \frac{\vec{v}}{r} \\
 &= \frac{v}{r} \frac{v}{r} \\
 a_c &= \frac{v^2}{r}
 \end{aligned}$$



$$v = \frac{2\pi r}{\Delta t}$$

$$= \frac{2\pi r}{T}$$

$$a_c \propto r$$



$$v = \frac{2\pi r}{\Delta t}$$

$$= \frac{2\pi r}{T}$$

$$a_c \propto r$$

$$a_c = \frac{v^2}{r}$$

$$= \frac{\left(\frac{2\pi r}{T}\right)^2}{r}$$

$$v = \frac{2\pi r}{\Delta t}$$

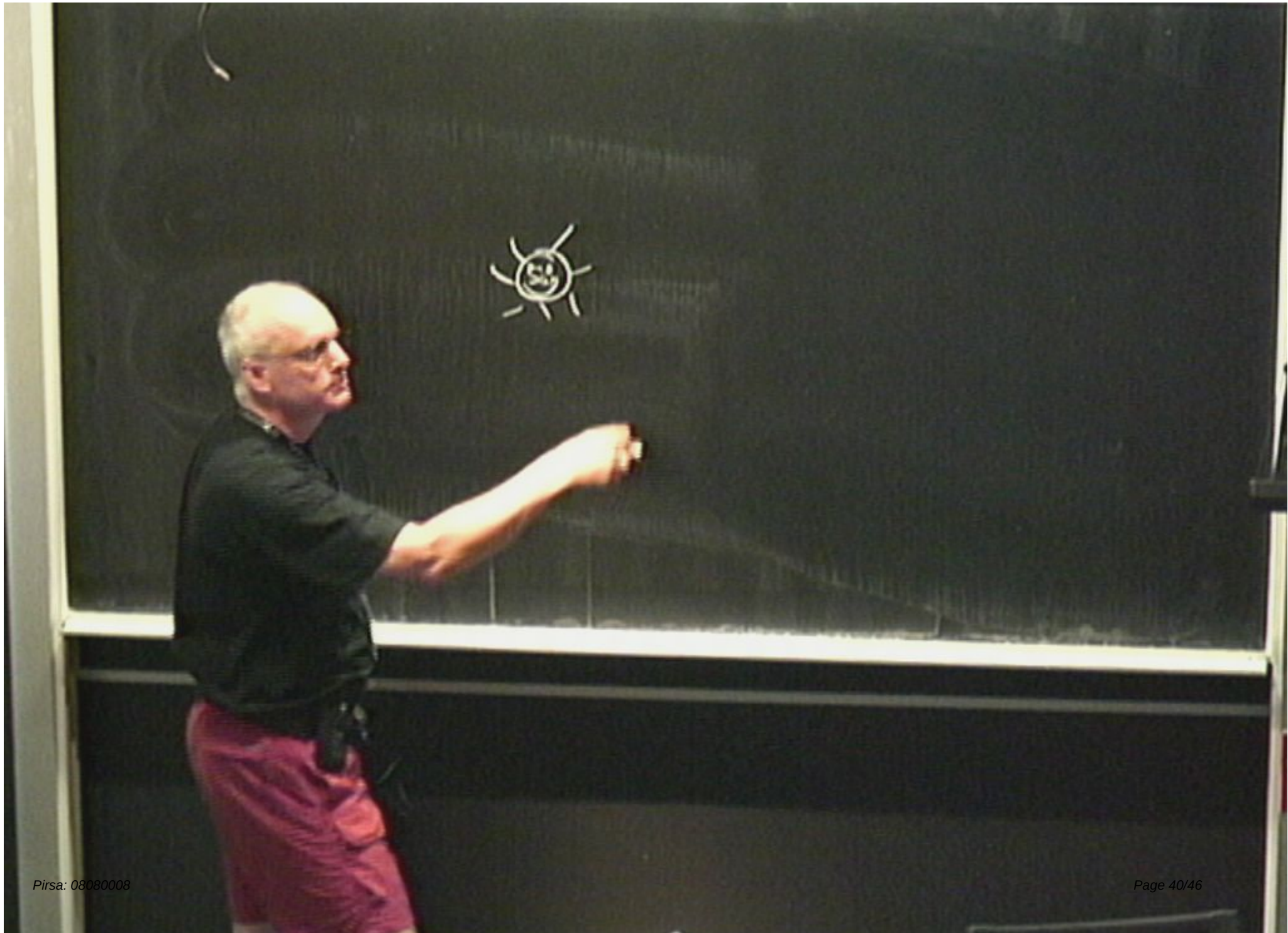
$$= \frac{2\pi r}{T}$$

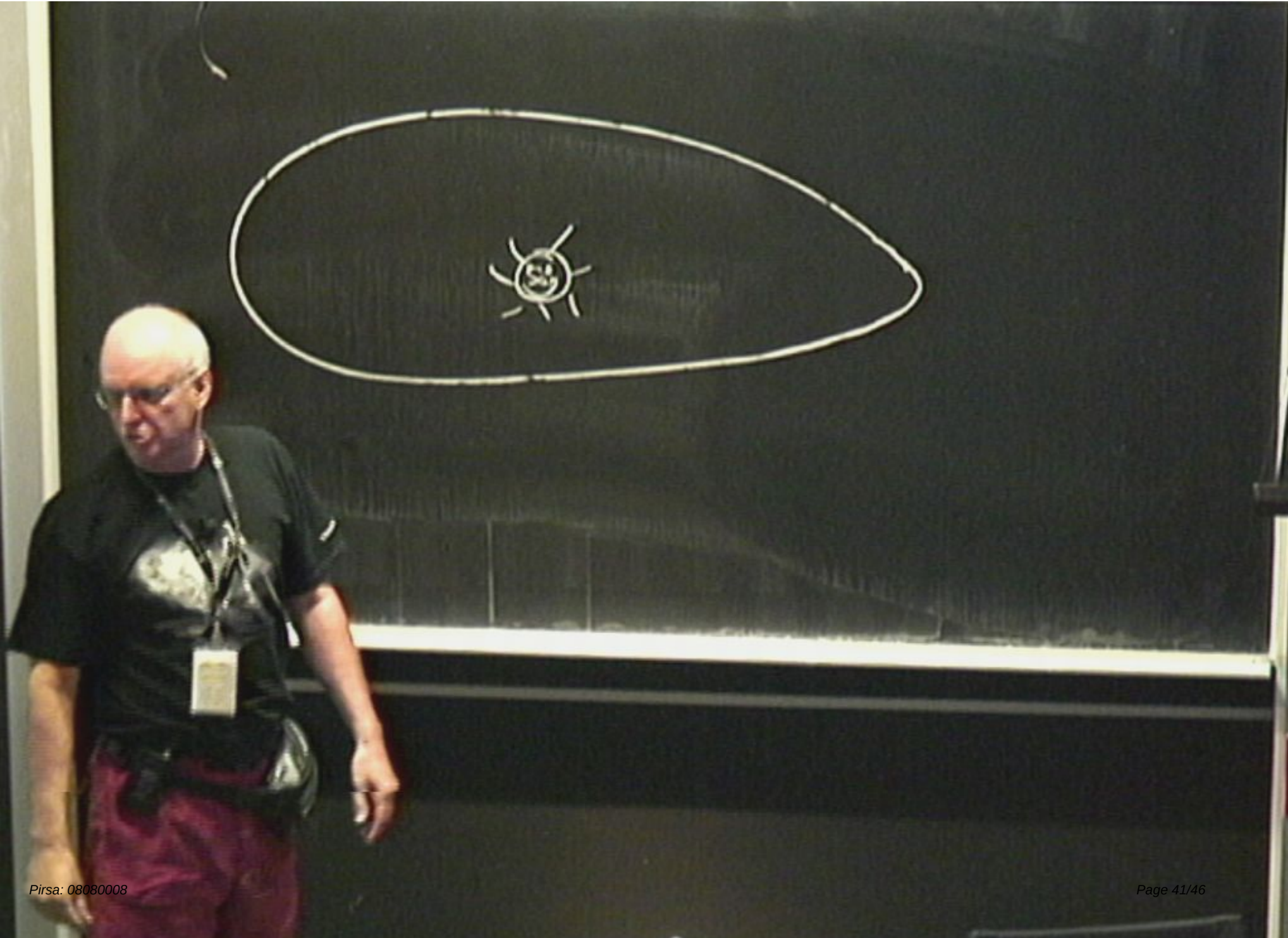
$$a_c \propto r$$

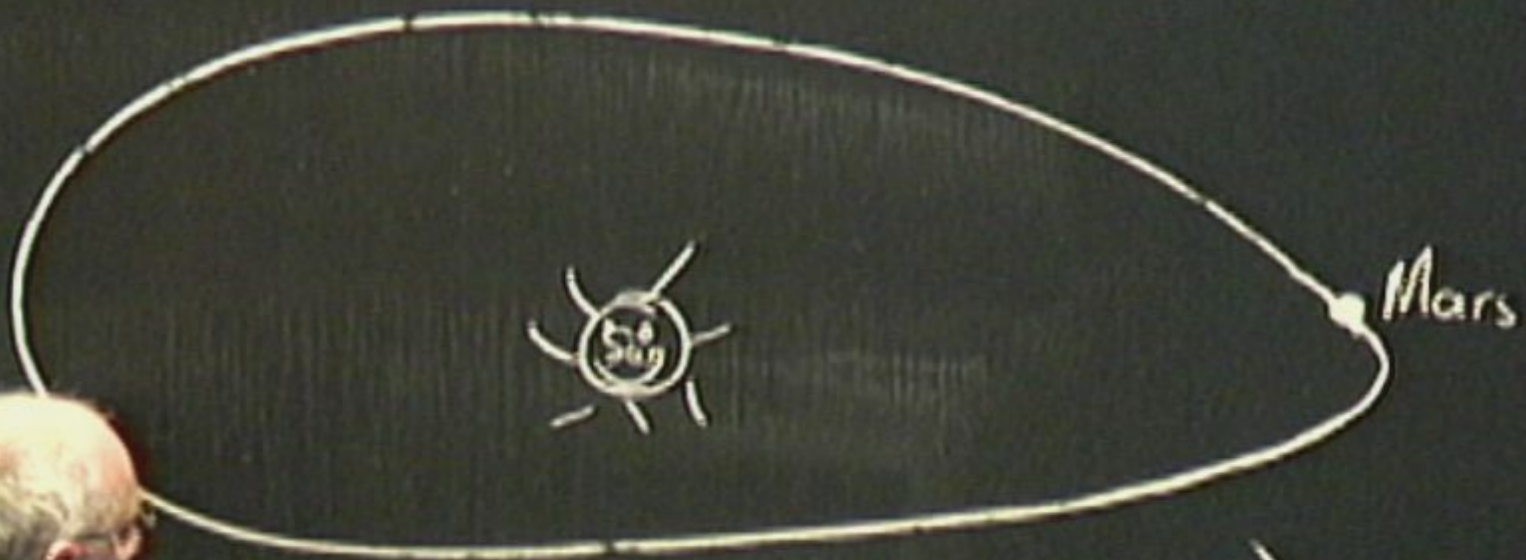
$$a_c = \frac{v^2}{r}$$

$$= \frac{\left(\frac{2\pi r}{T}\right)^2}{r}$$

$$a_c = \frac{4\pi^2 r}{T^2}$$

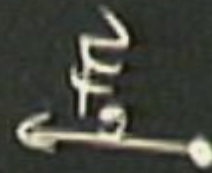


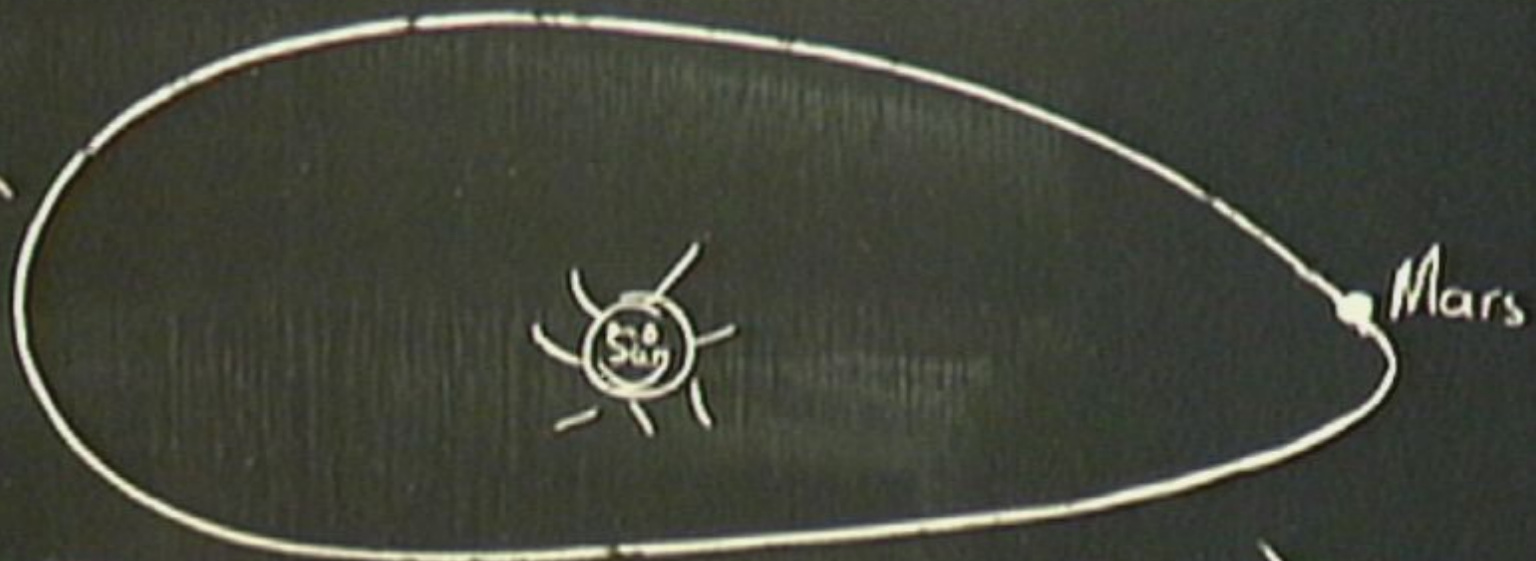




$$F_{\text{grav}} = F_g$$

re

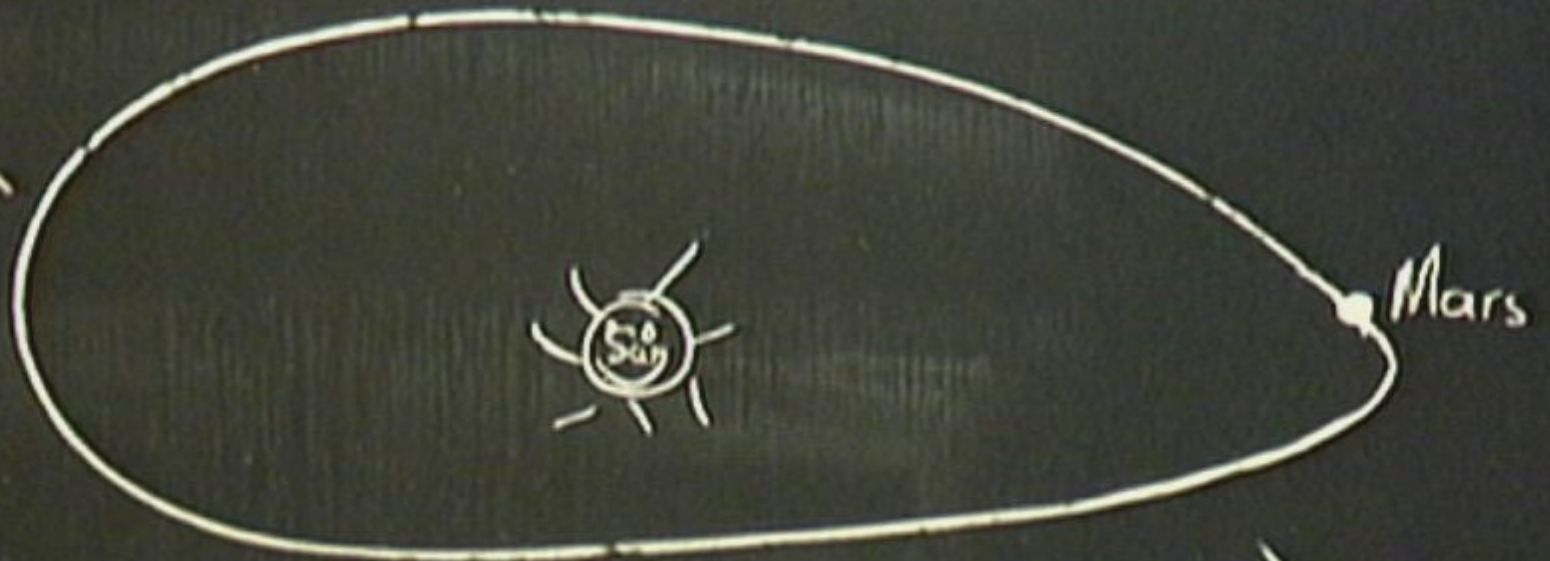




$$F_{\text{grav}} = F_g$$

$$\frac{mv^2}{r} = \frac{GmM}{r^2}$$



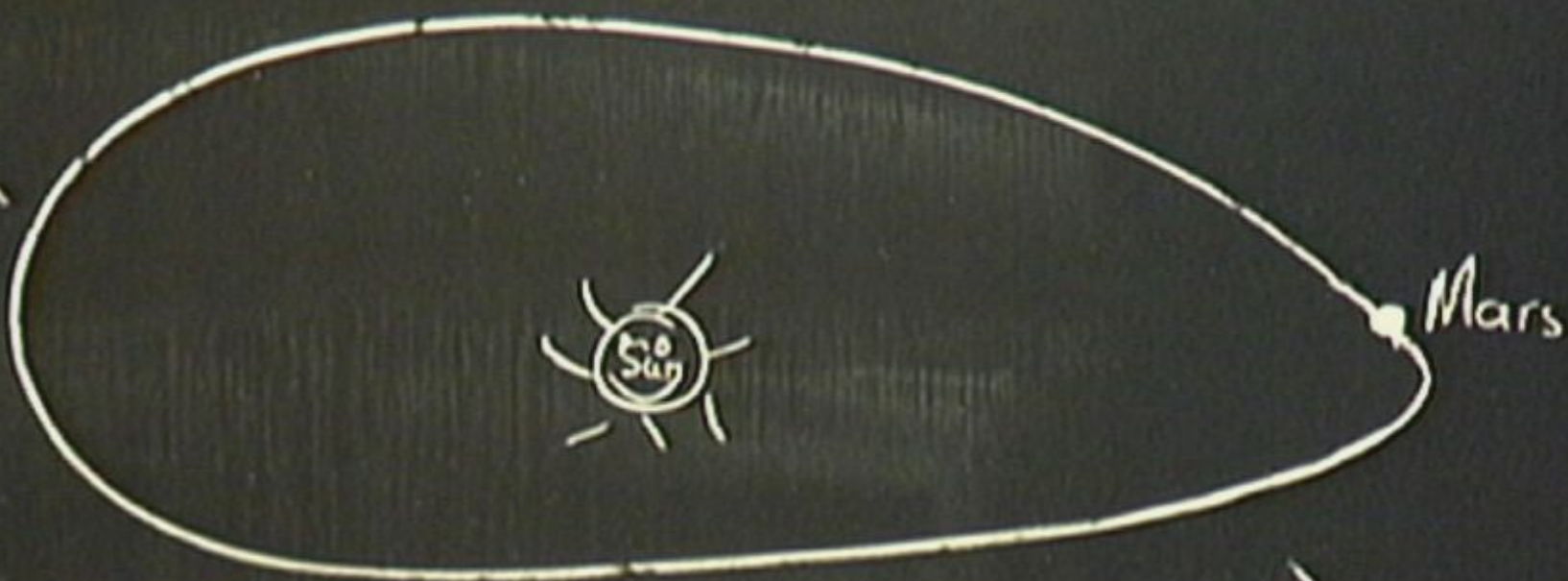


$$v^2 = \frac{GM}{r}$$

$$v = \sqrt{\frac{GM}{r}}$$

$$f_{\text{cent}} = f_g$$

$$\frac{mv^2}{r} = \frac{GmM}{r^2}$$



$$v^2 \propto \frac{1}{r}$$

$$v \propto \frac{1}{\sqrt{r}}$$

$$F_{\text{cent}} = F_g$$

$$\frac{mv^2}{r} = \frac{GmM}{r^2}$$

