Title: Special Relativity 14 - The Curved Geometry of a Rotating Space

Date: Jul 27, 2008 09:00 AM

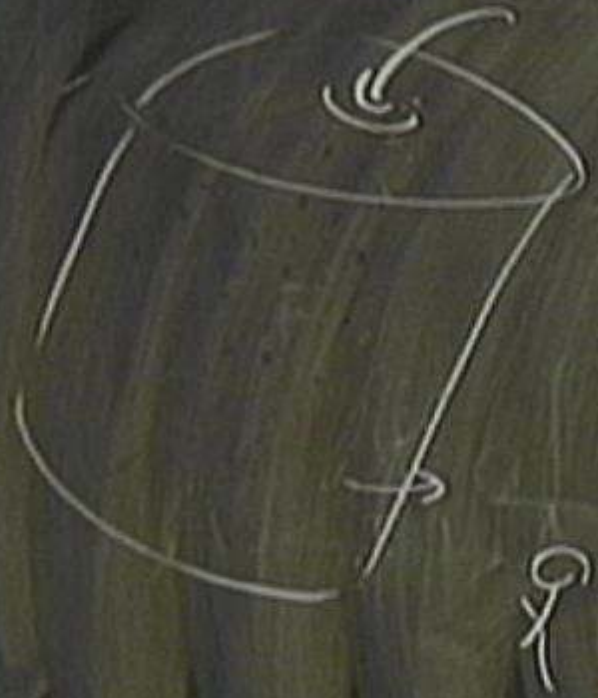
URL: http://pirsa.org/08070052

Abstract: The spacetime diagram of a rotating Bob is analyzed, leading us to conclude that his spatial geometry is curved.
 Learning Outcomes:
 â€¢ Understanding the physical effects of the rotation on the rotating observers, metal panels of the cylinder and so forth.
â€¢ Understanding the properties of a rotating cylinder using a spacetime diagram.
â€¢ Understanding curved spaces: The negatively curved space of a rotating observer and the positively curved space representing the real gravitational field of the Sun.

L = proper width of Bob. (same Alice)

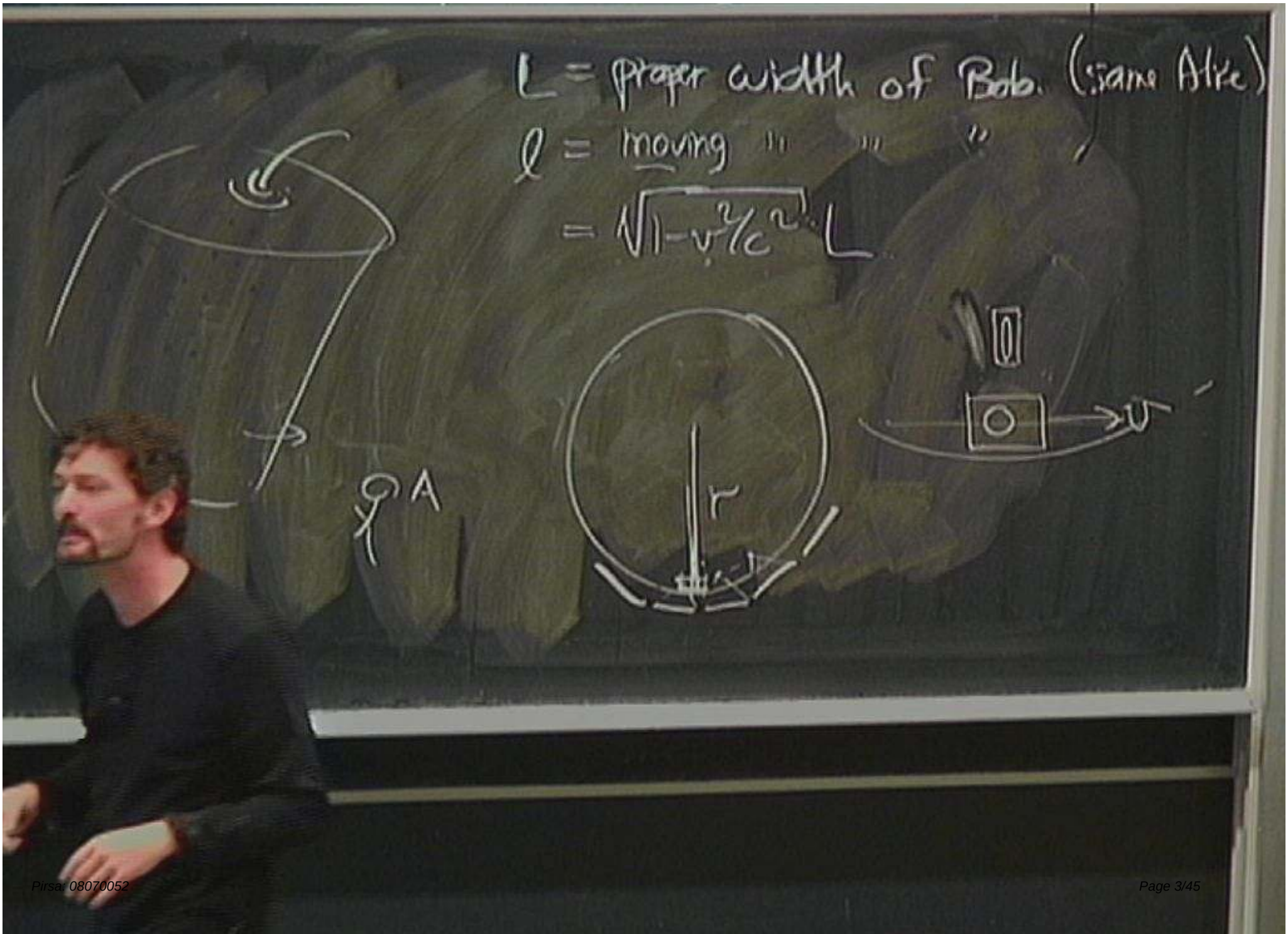
ℓ = moving " " "

$= \sqrt{1 - v^2/c^2} \cdot L$



A

B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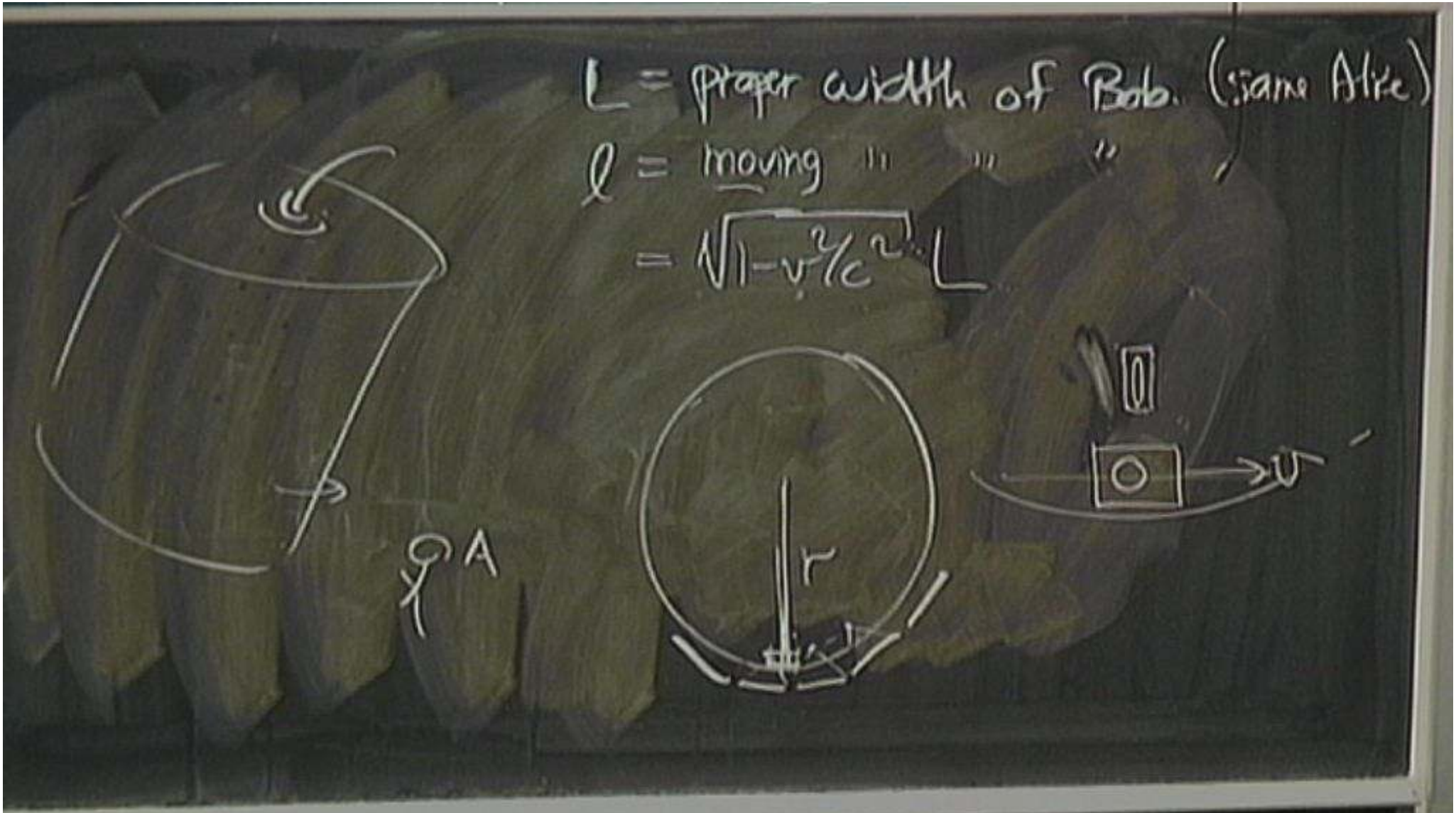
A
B
v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B
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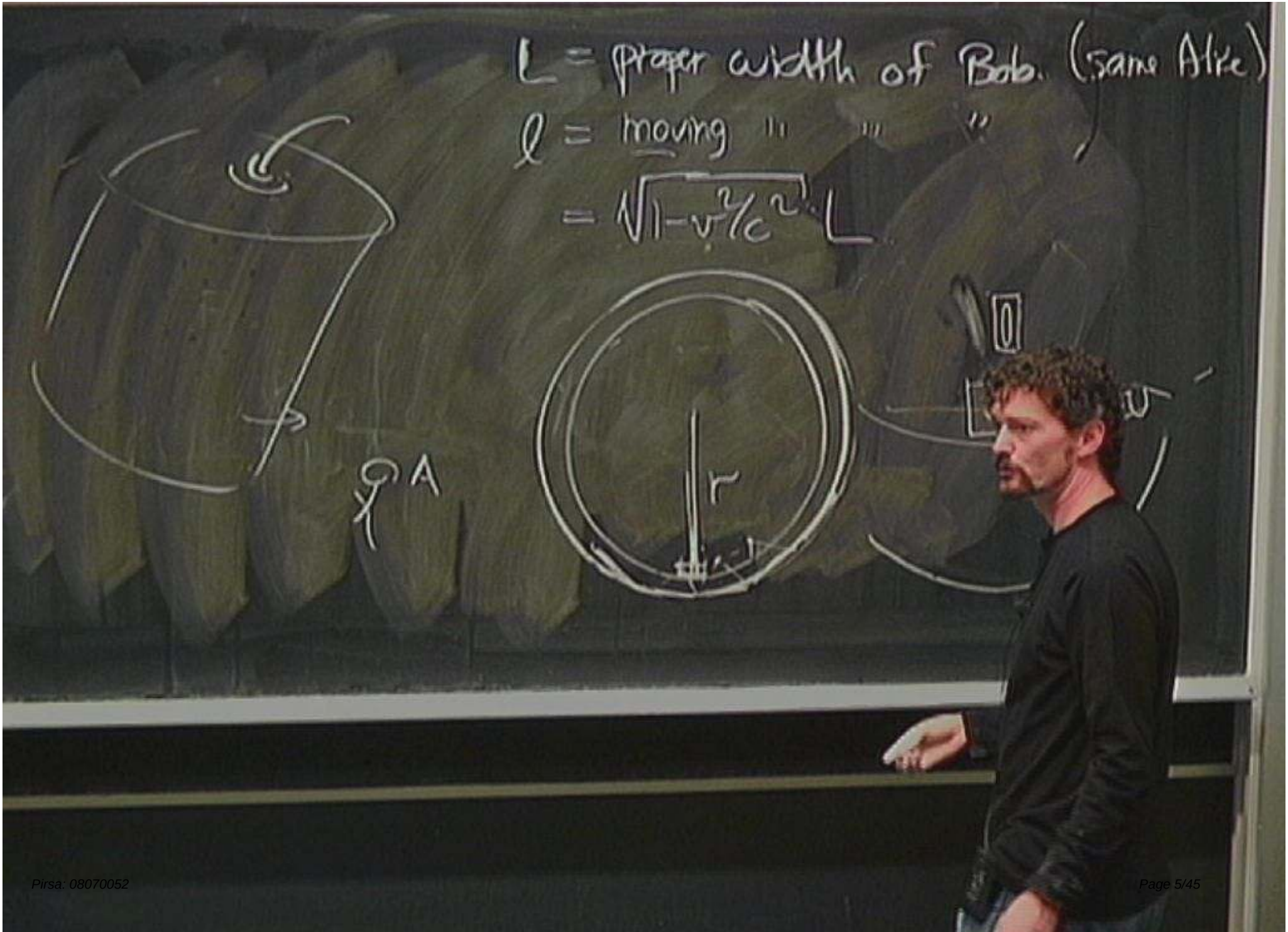
v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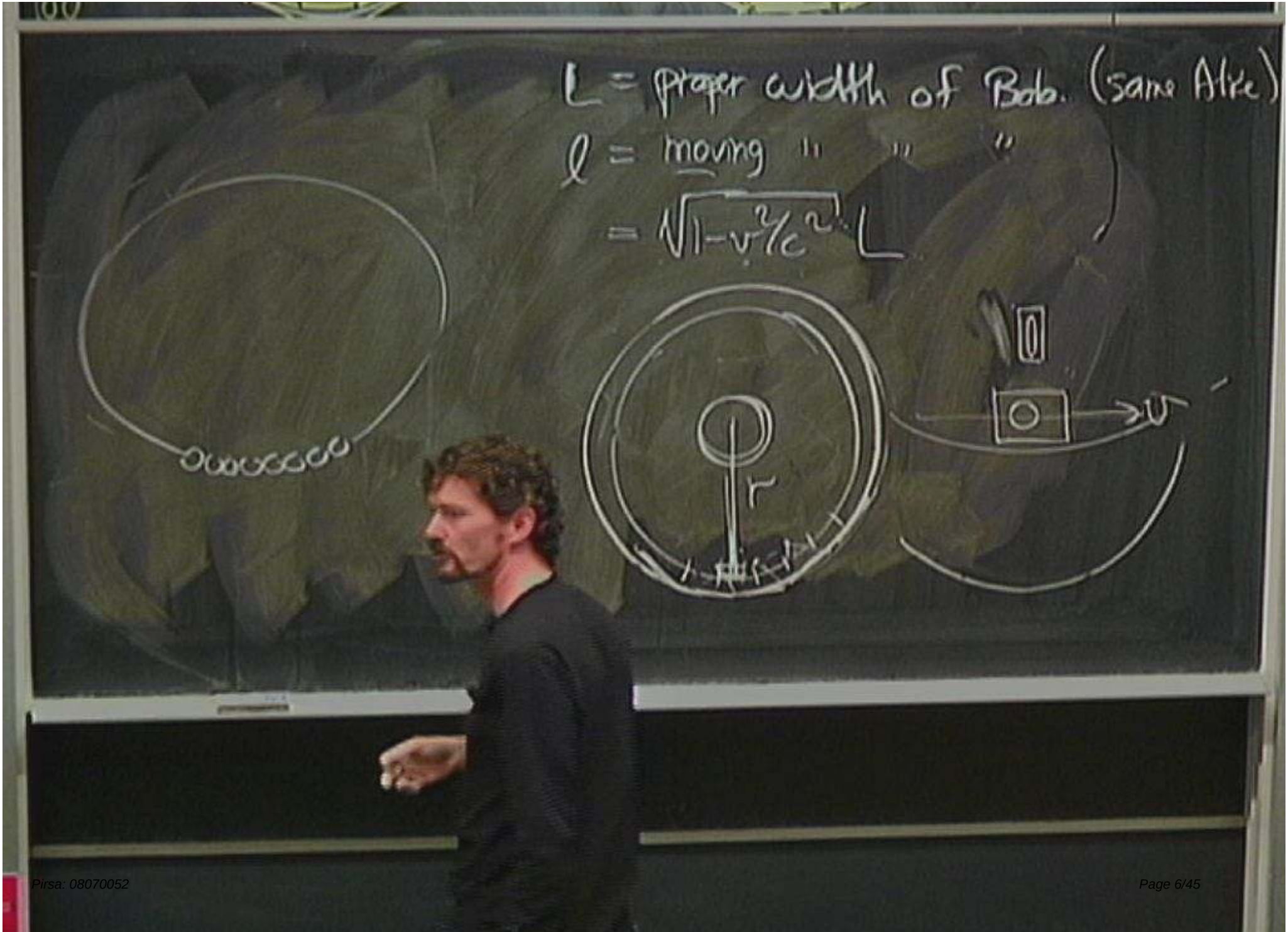
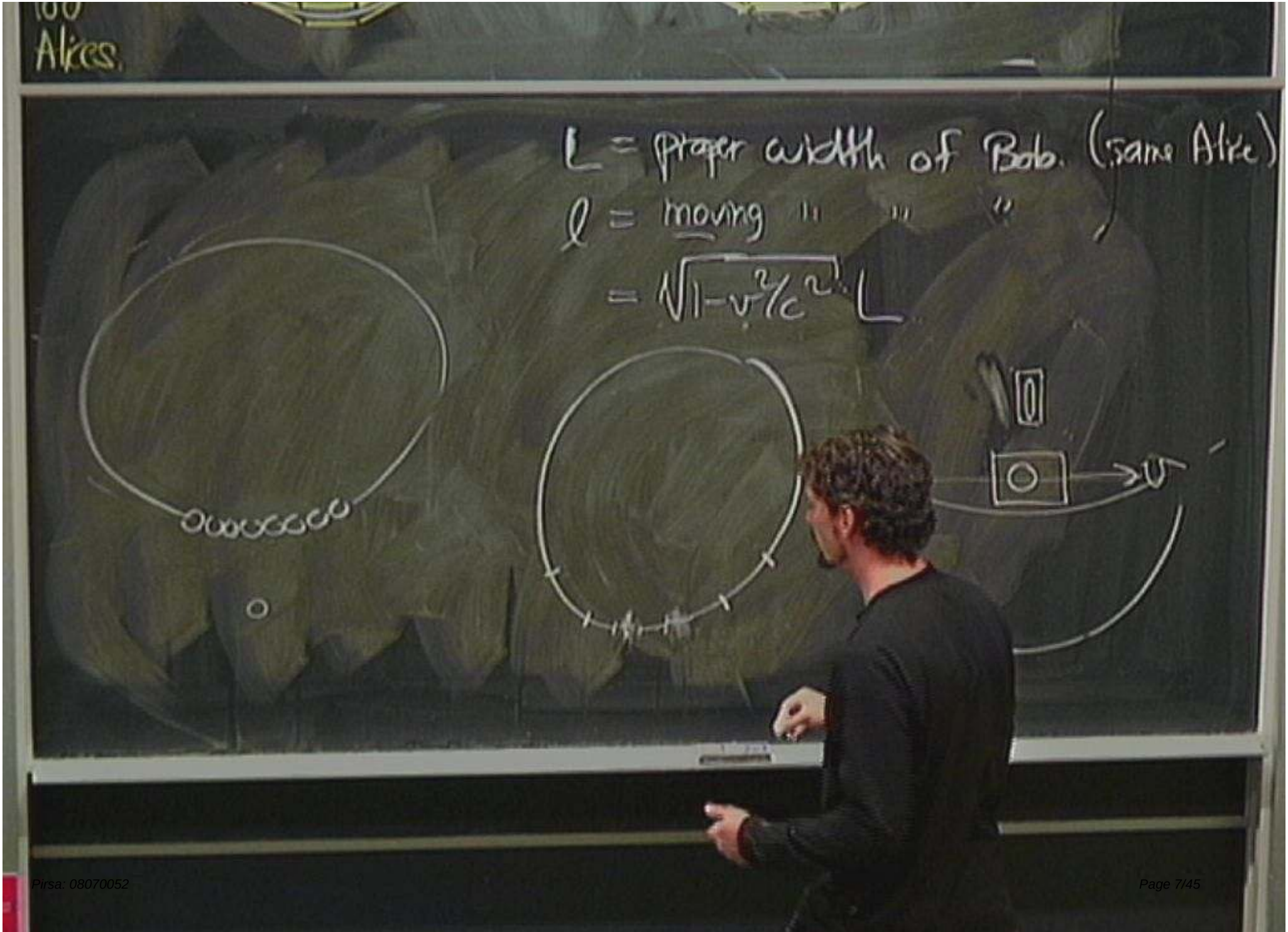

L = proper width of Bob. (same Alice)
l = moving " " "
= √(1 − v²/c²) · L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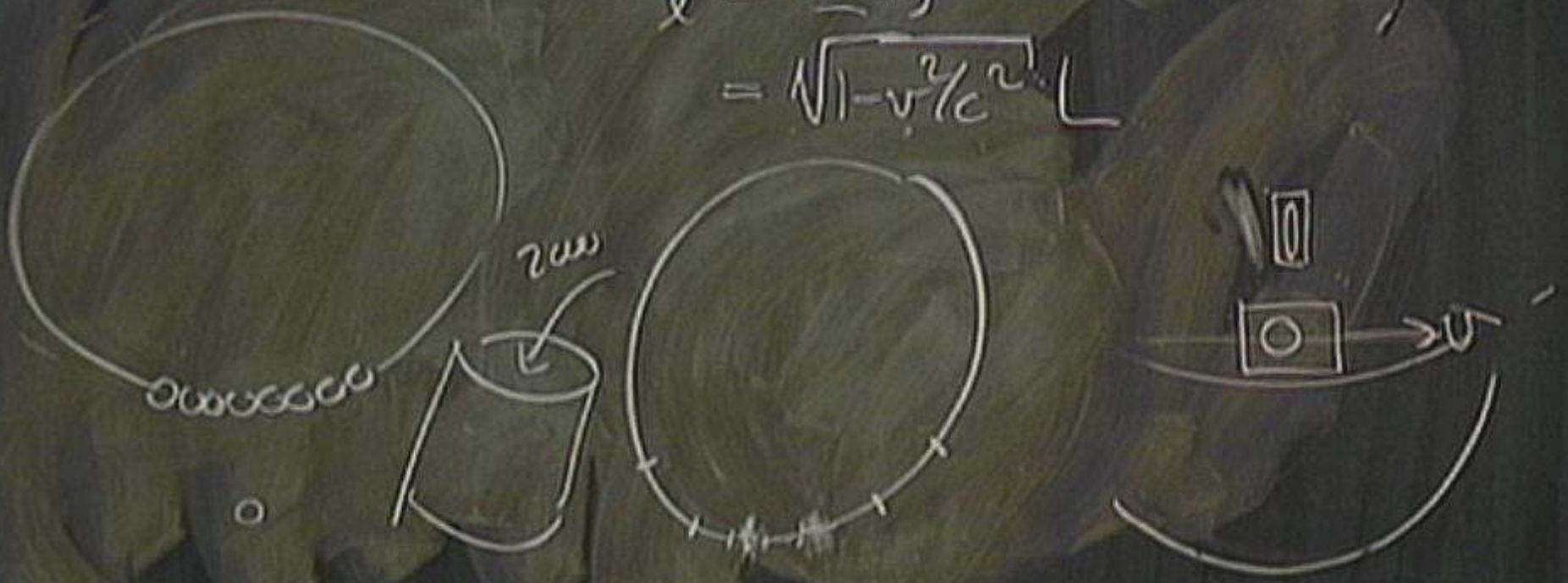
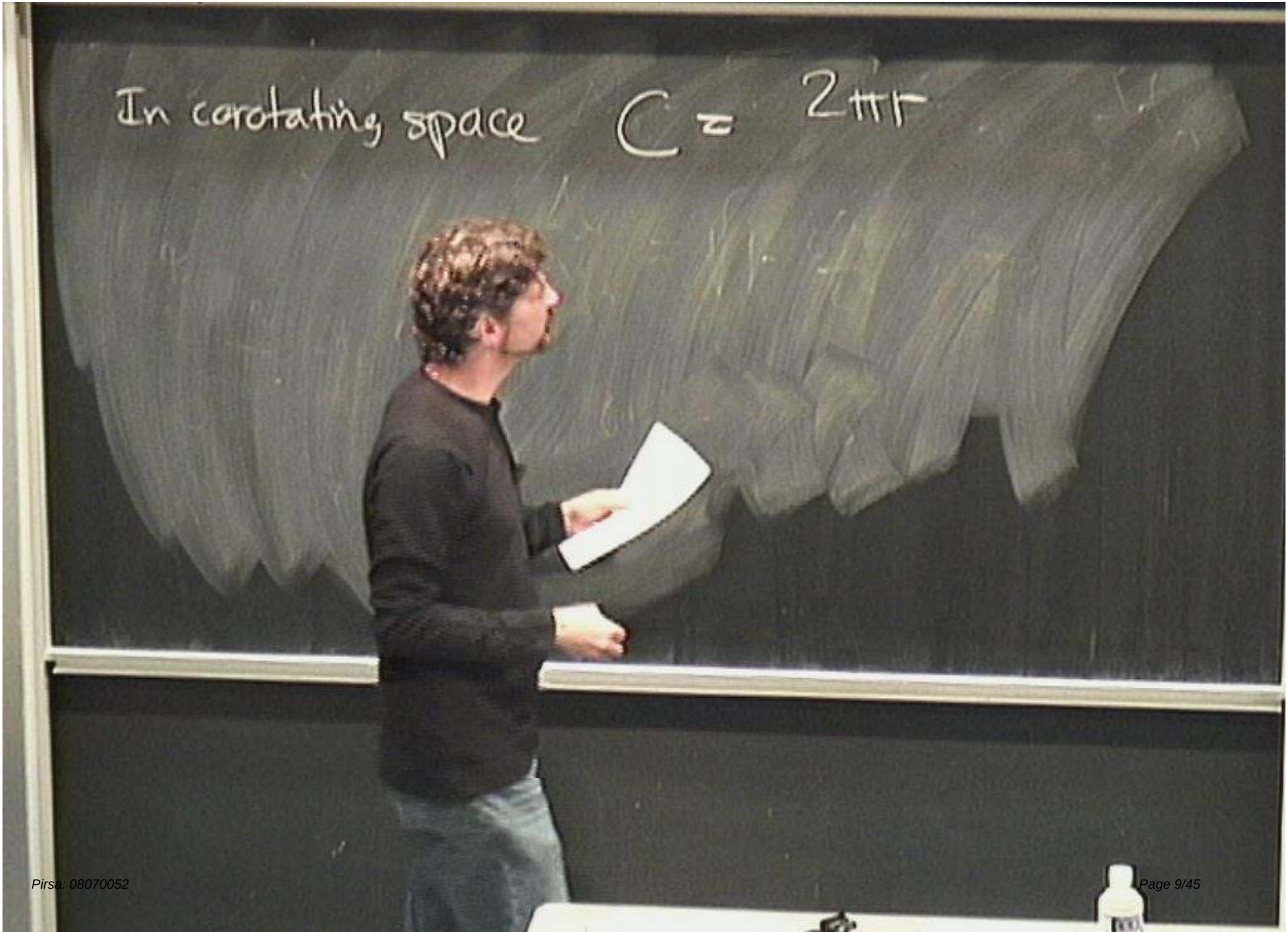
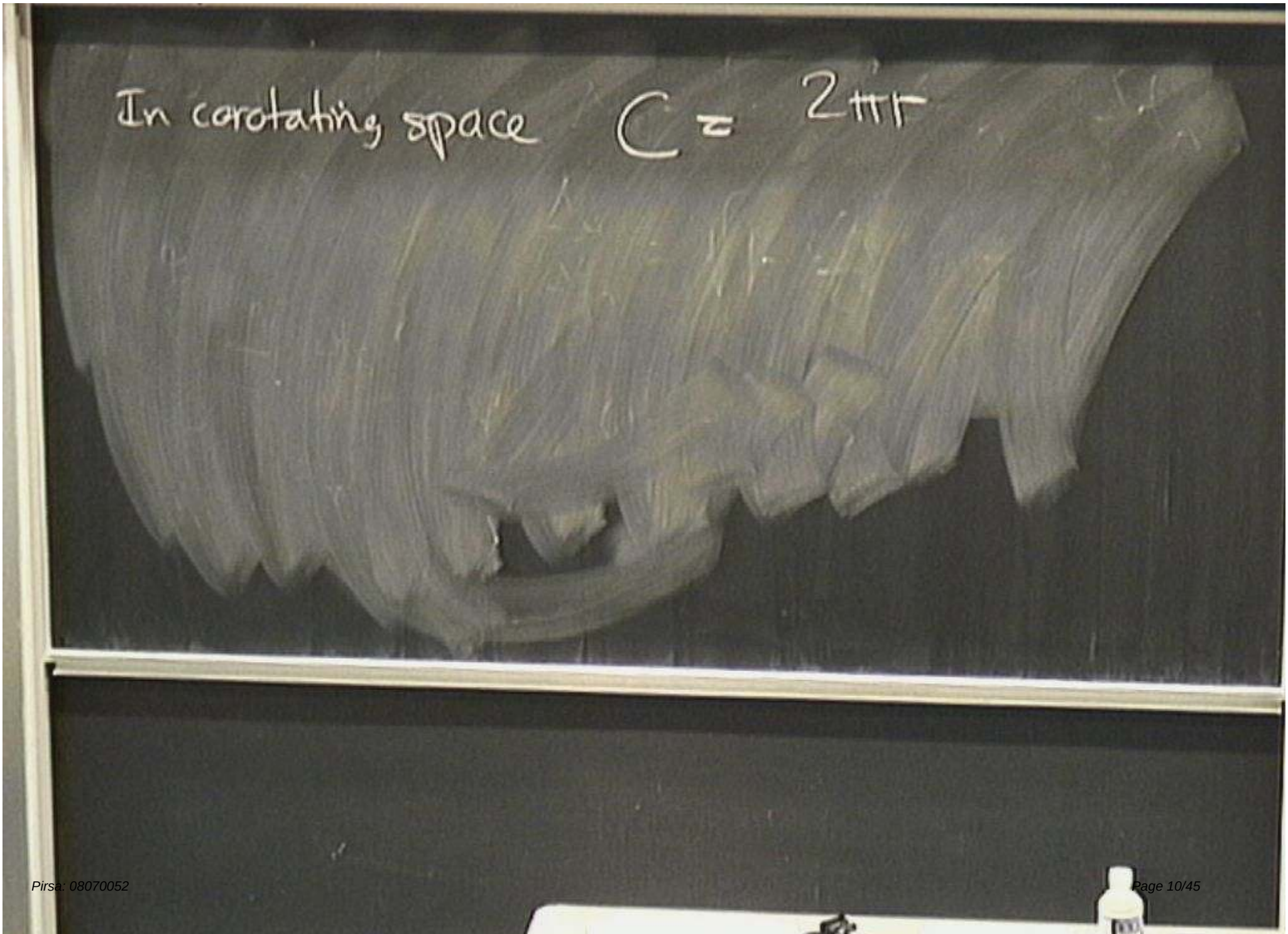



In corotating space $C = 2\pi r$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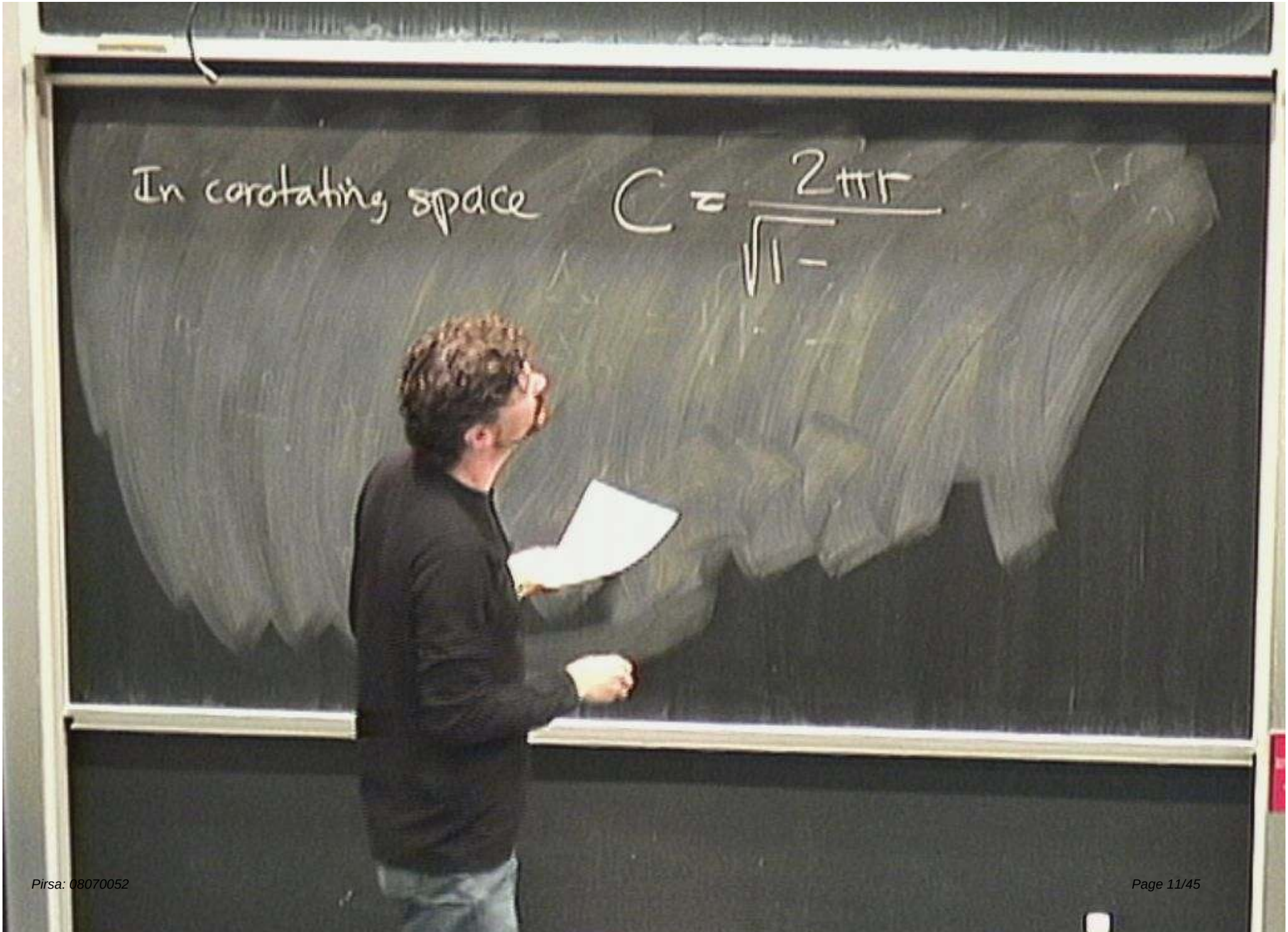
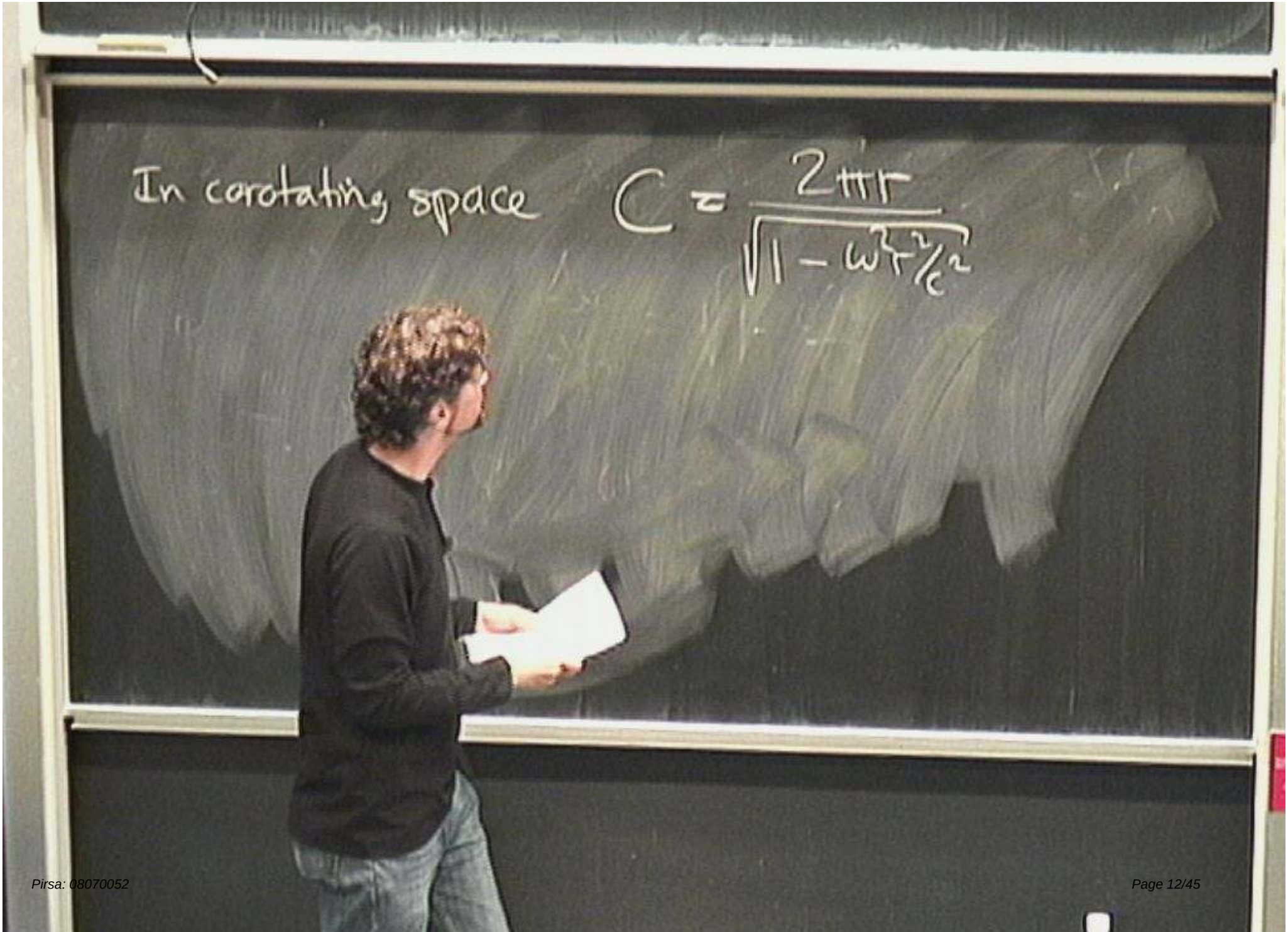
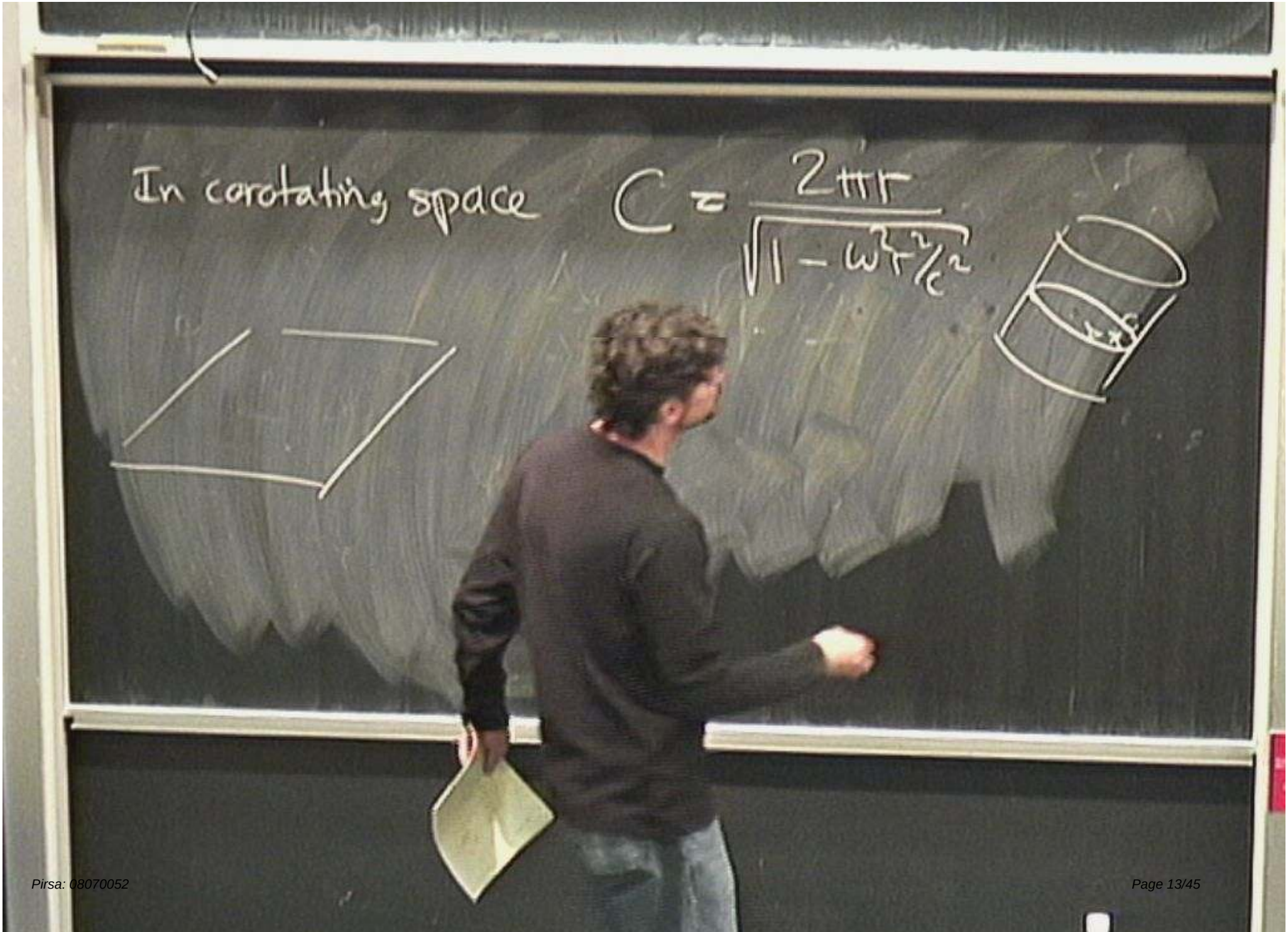

In corotating space
C =
2πr


In corotating space $C = \frac{2\pi r}{\sqrt{1-\omega^2 r^2/c^2}}$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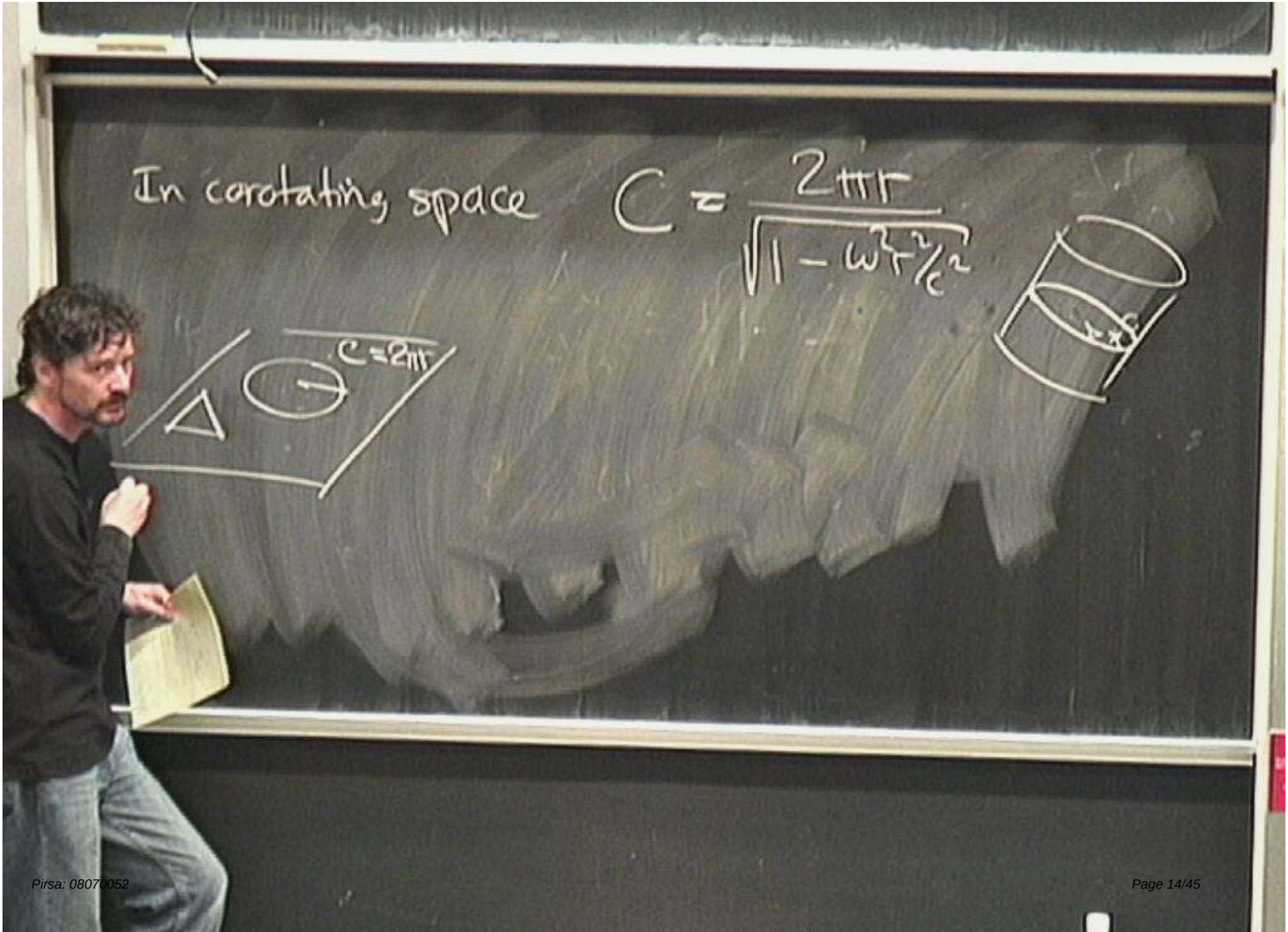
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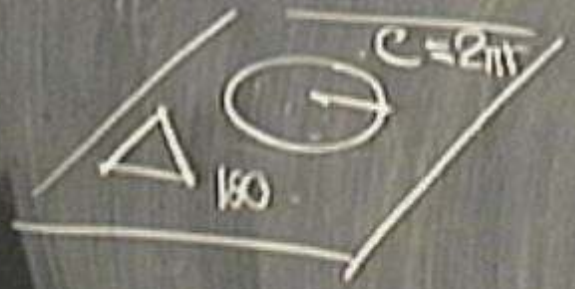
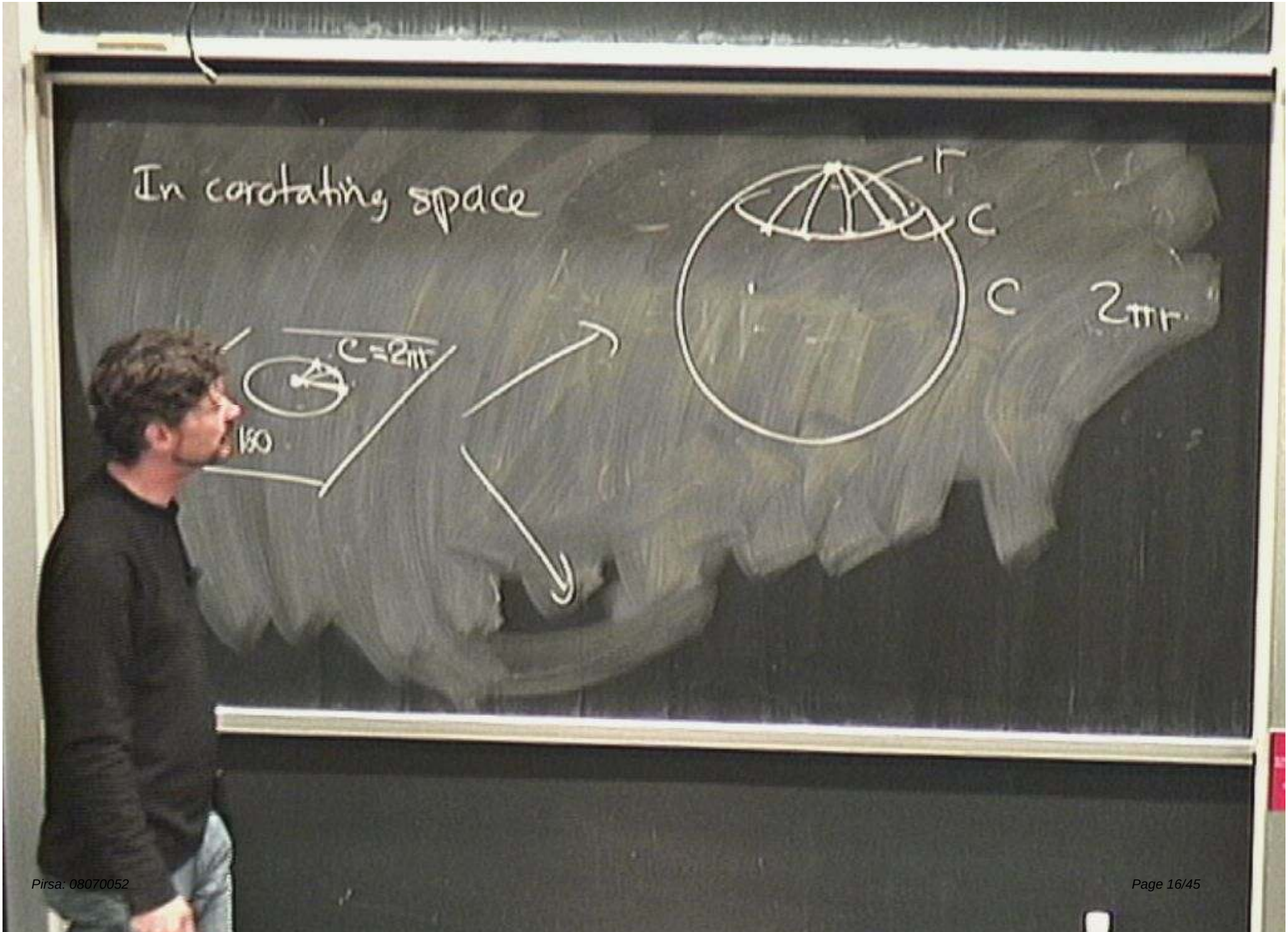
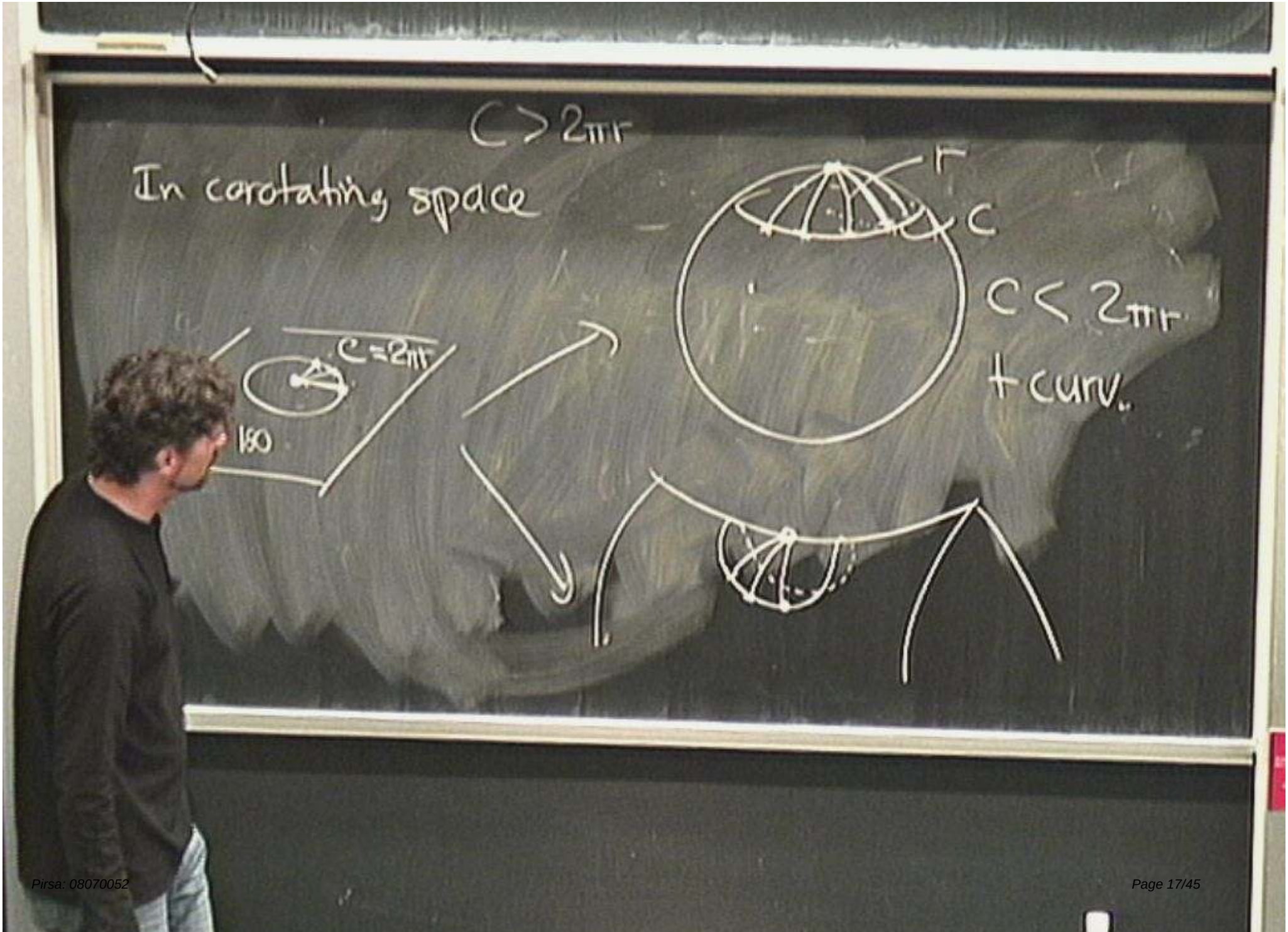
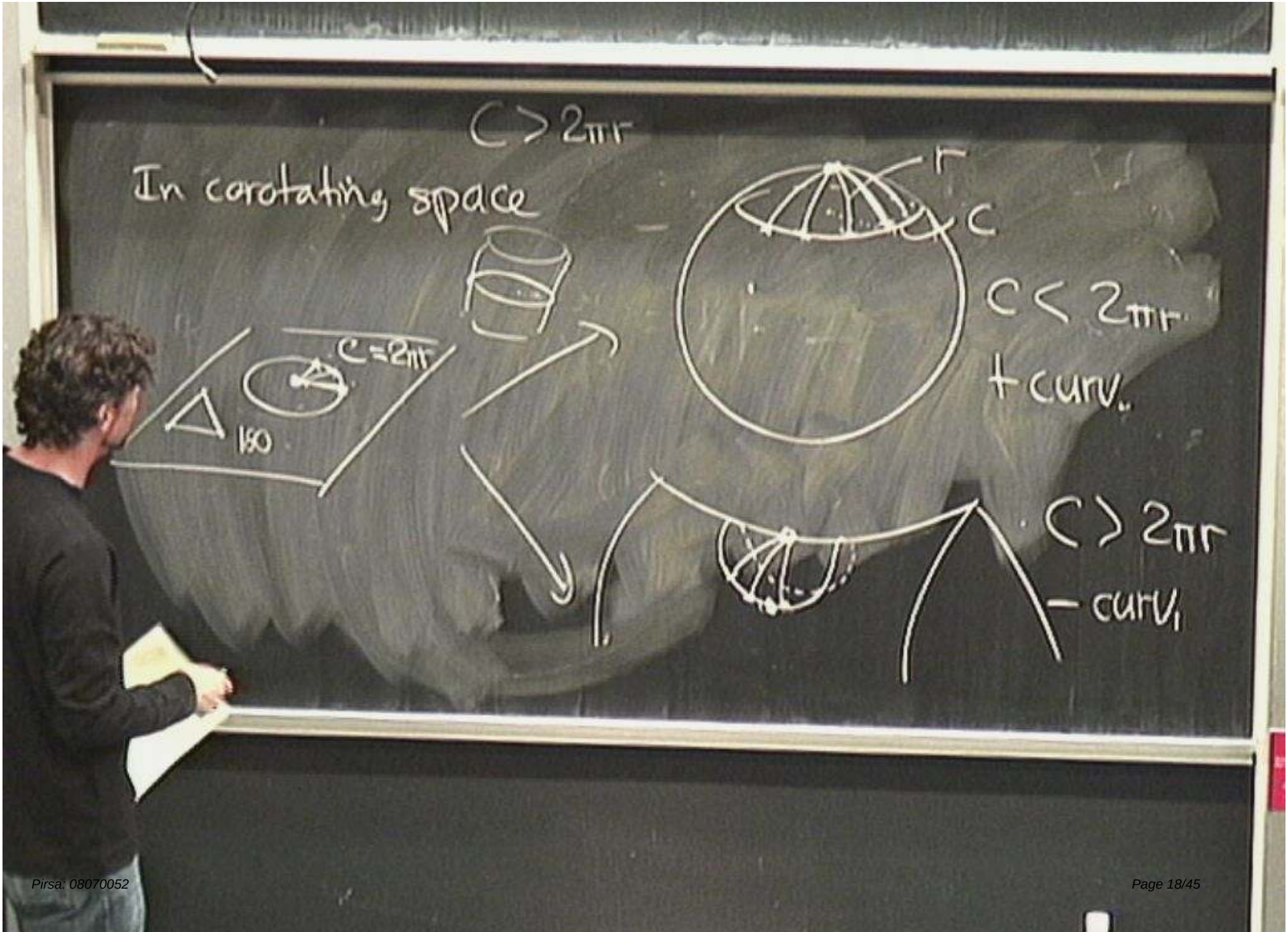
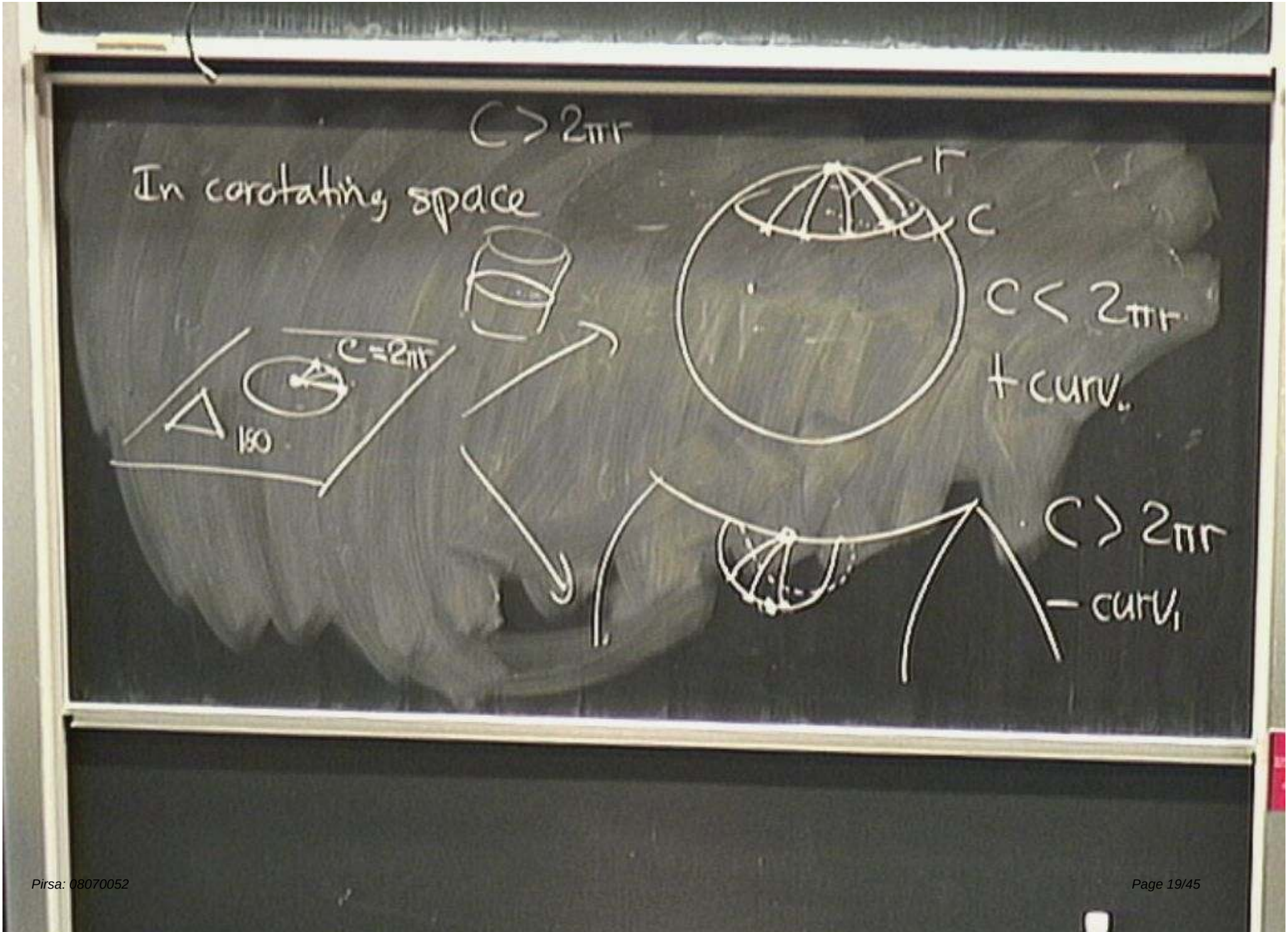
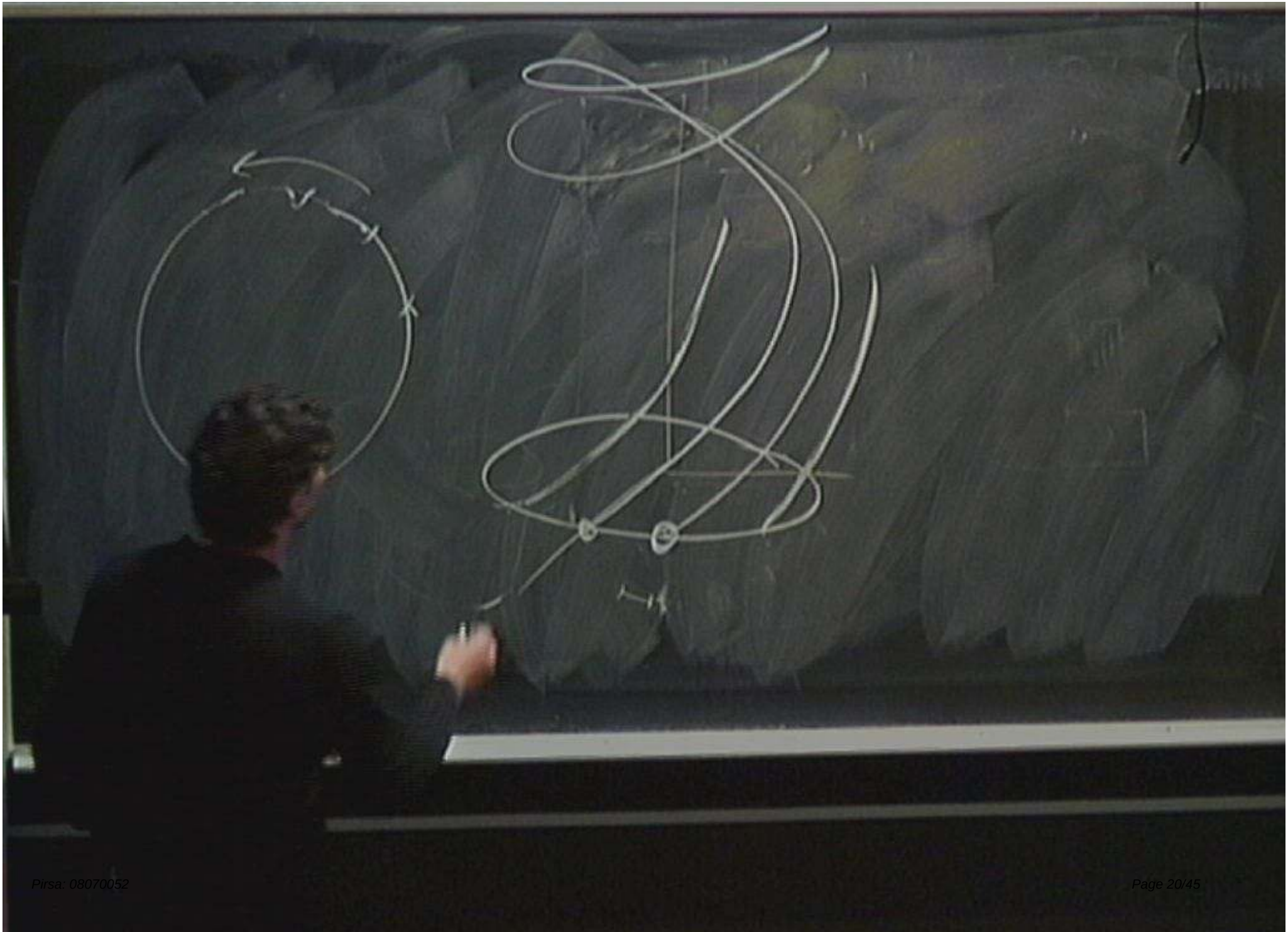


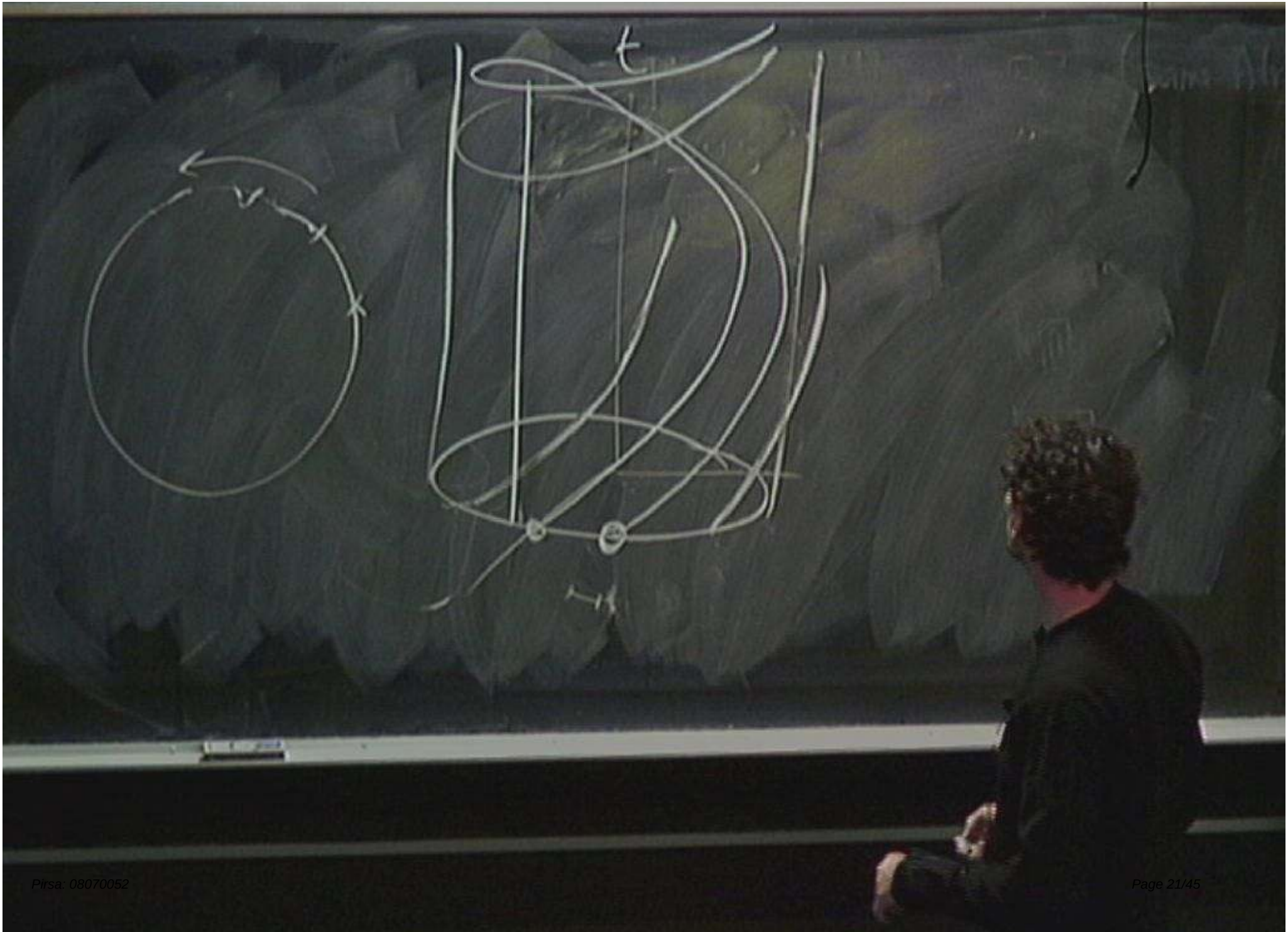

In corotating space
r
C
C
2πr
C=2πr
180


C > 2πr
In corotating space
r
C
C < 2πr
+ curv.
C = 2πr
180


C > 2πr
In corotating space
r
C
C < 2πr
+ curv.
C = 2πr
180
C > 2πr
- curv.


C > 2πr
In corotating space
r
C
C < 2πr
+ curv.
C = 2πr
Δ
180
C > 2πr
− curv.

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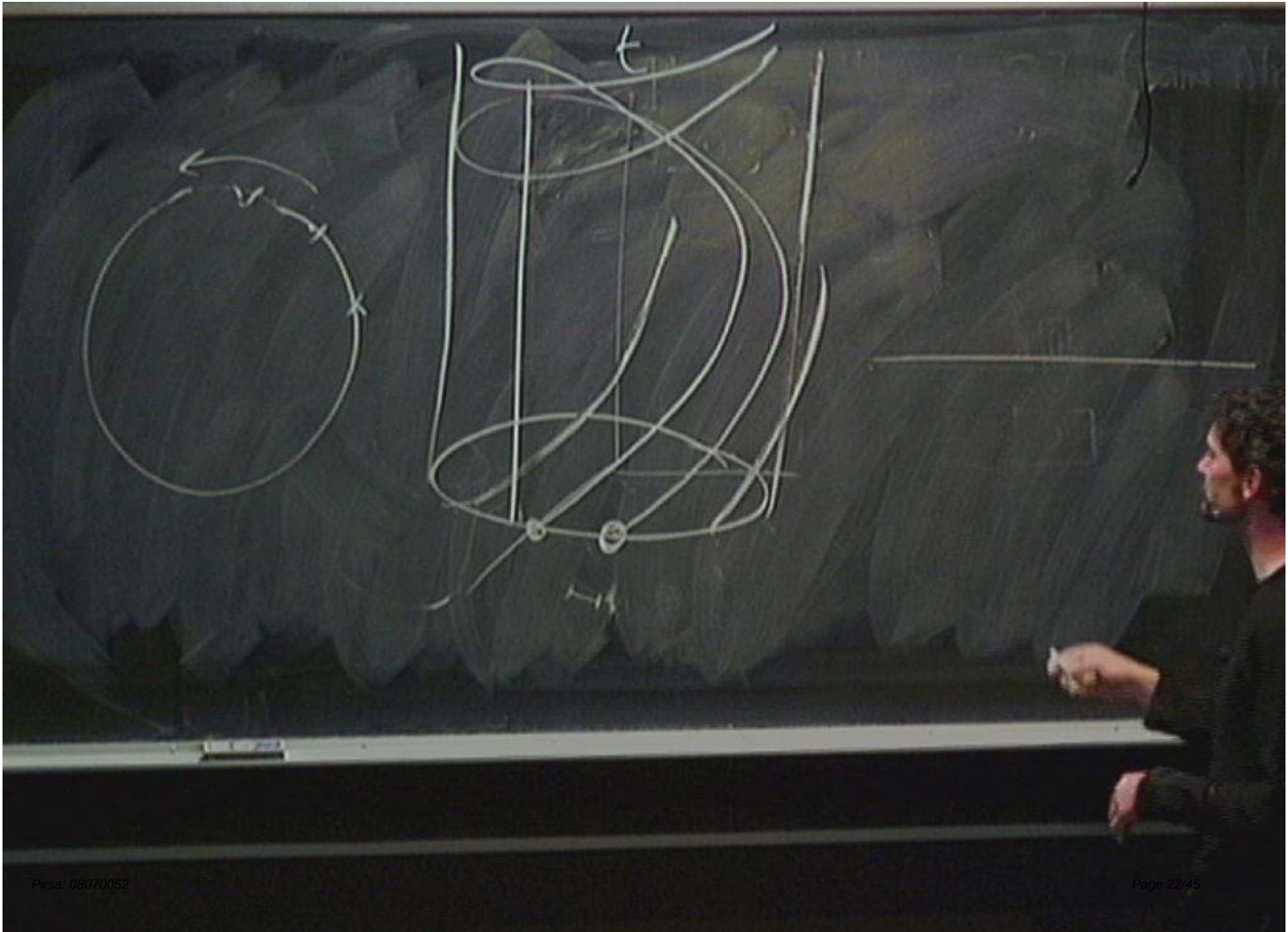
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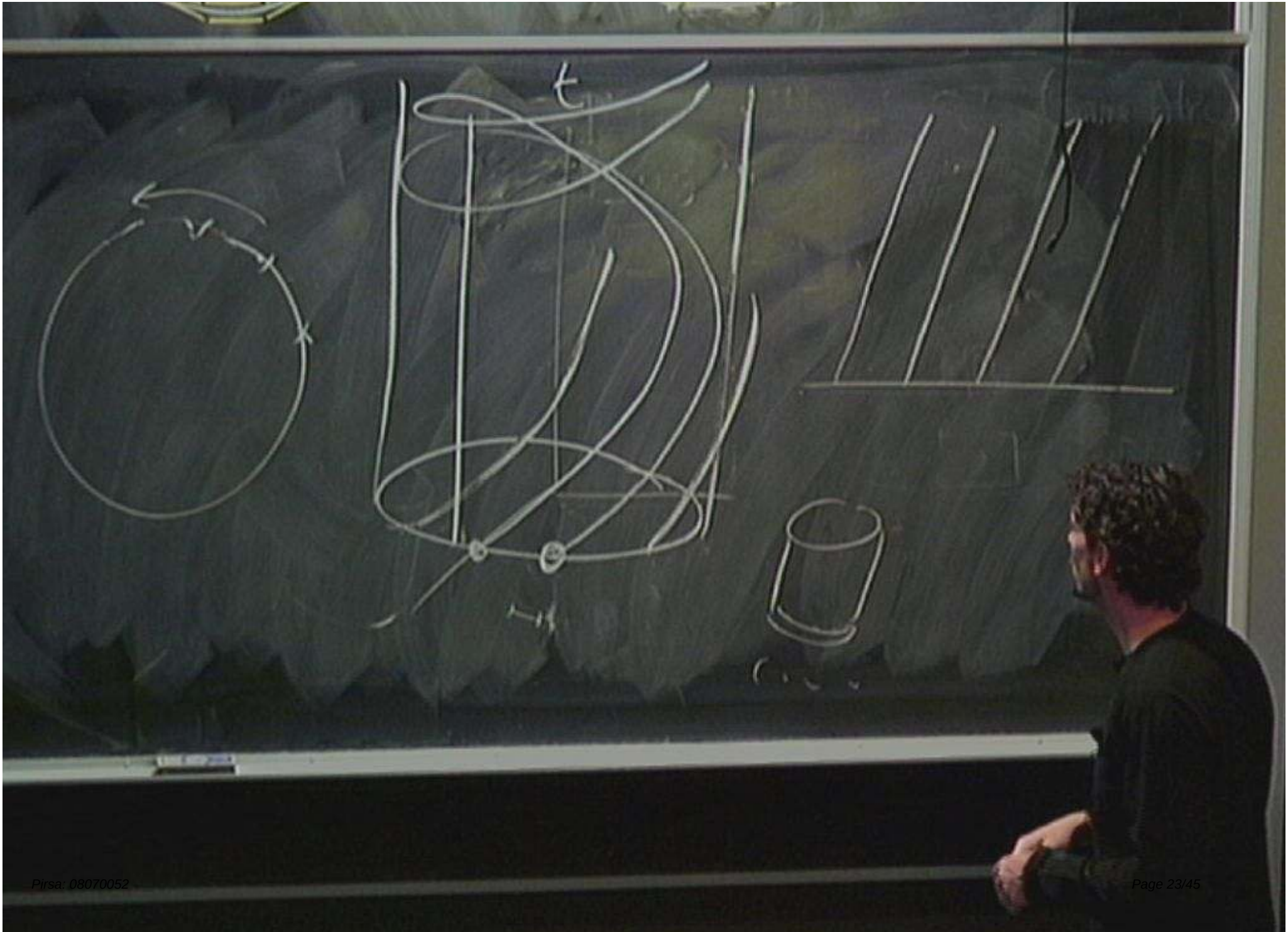
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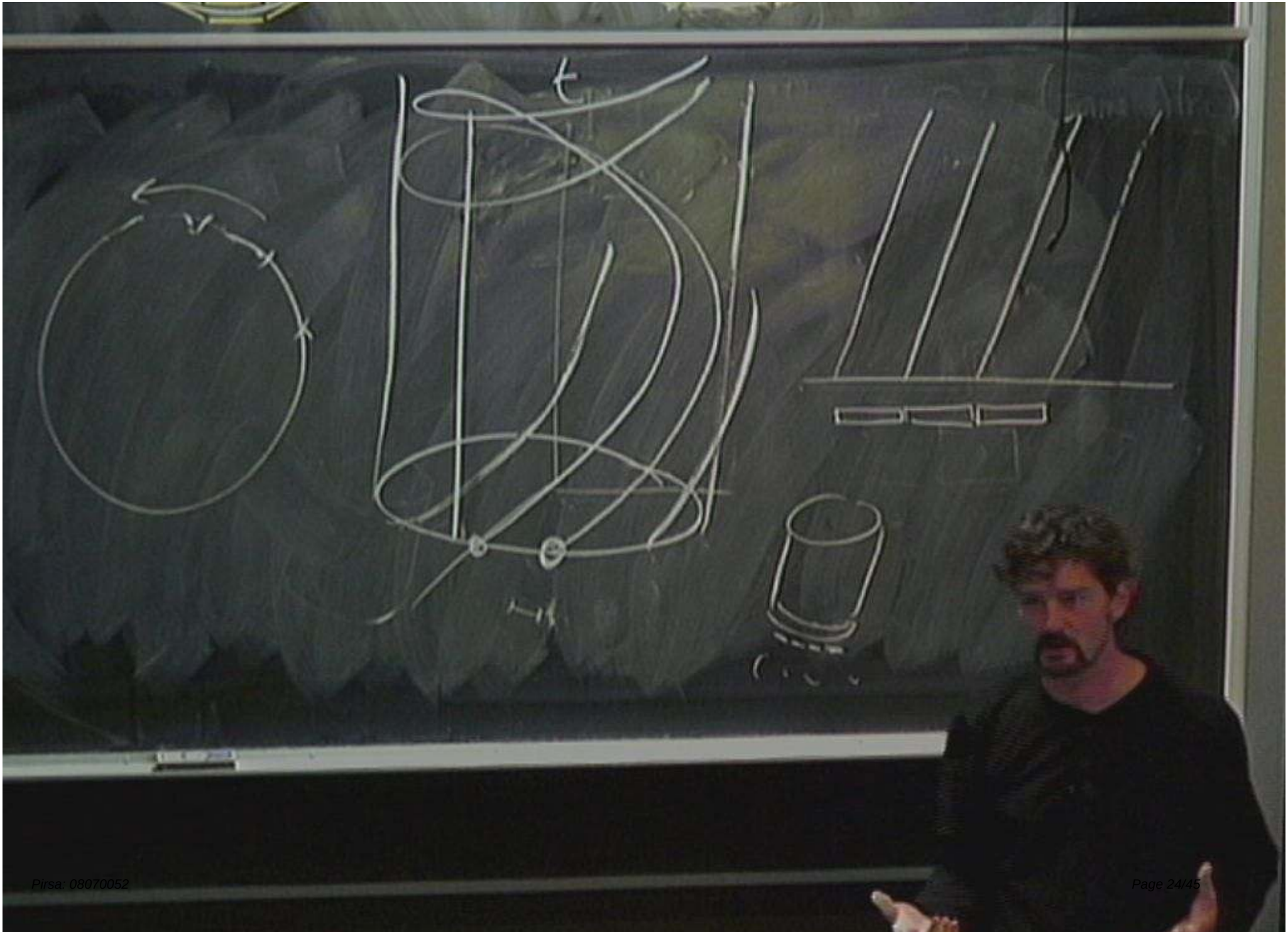
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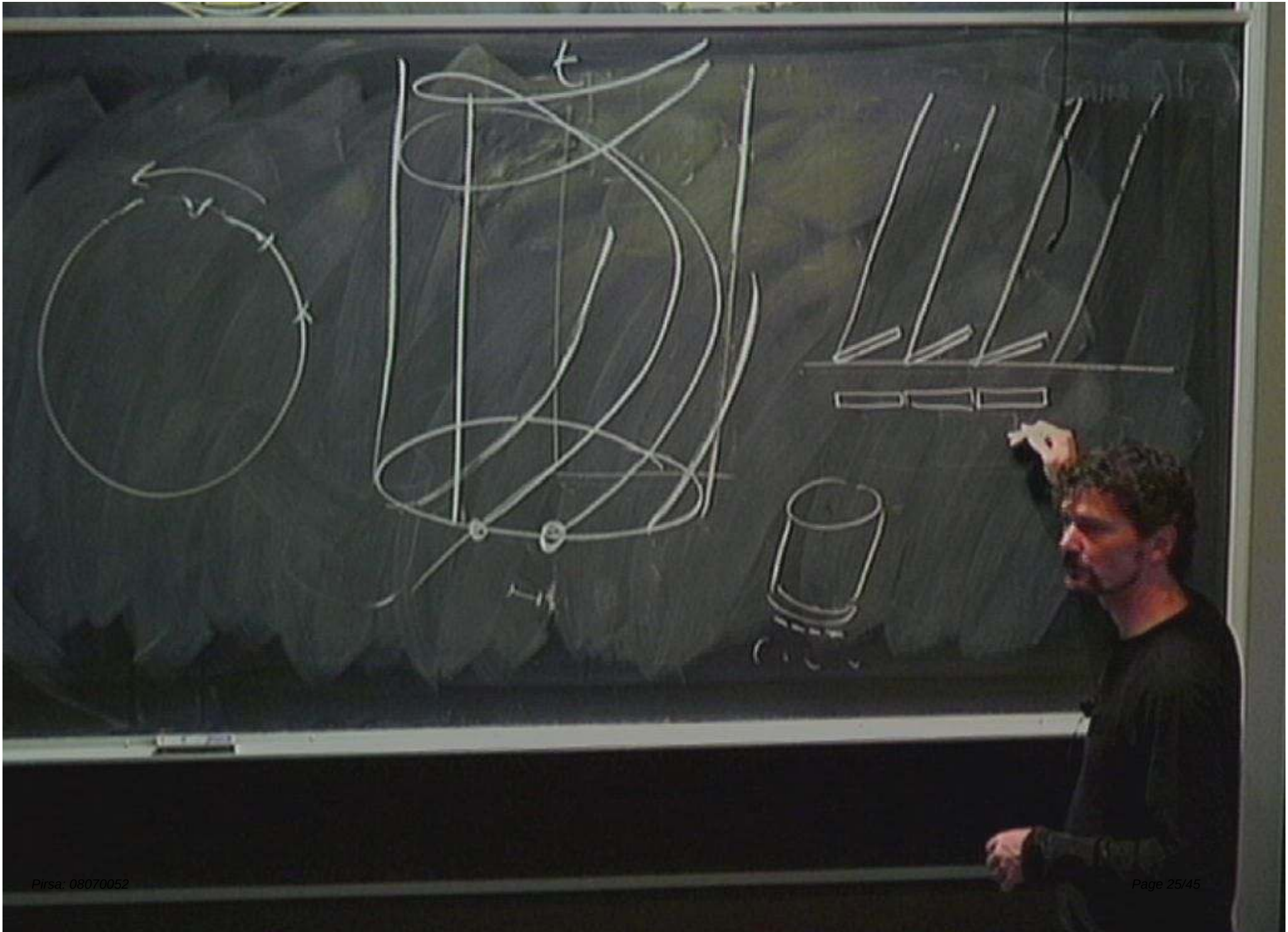
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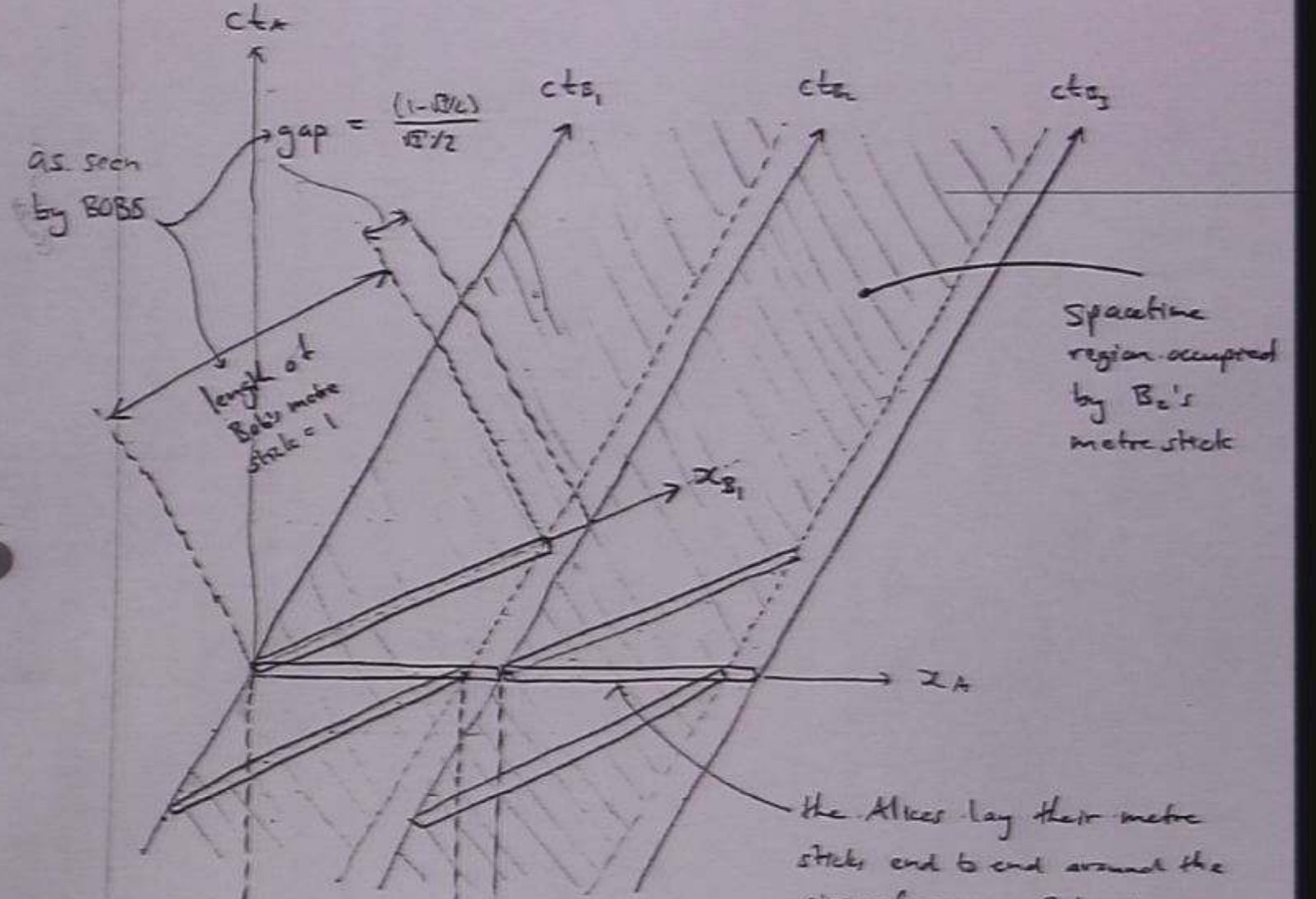
let all Alices & Bobs have identical metre sticks.

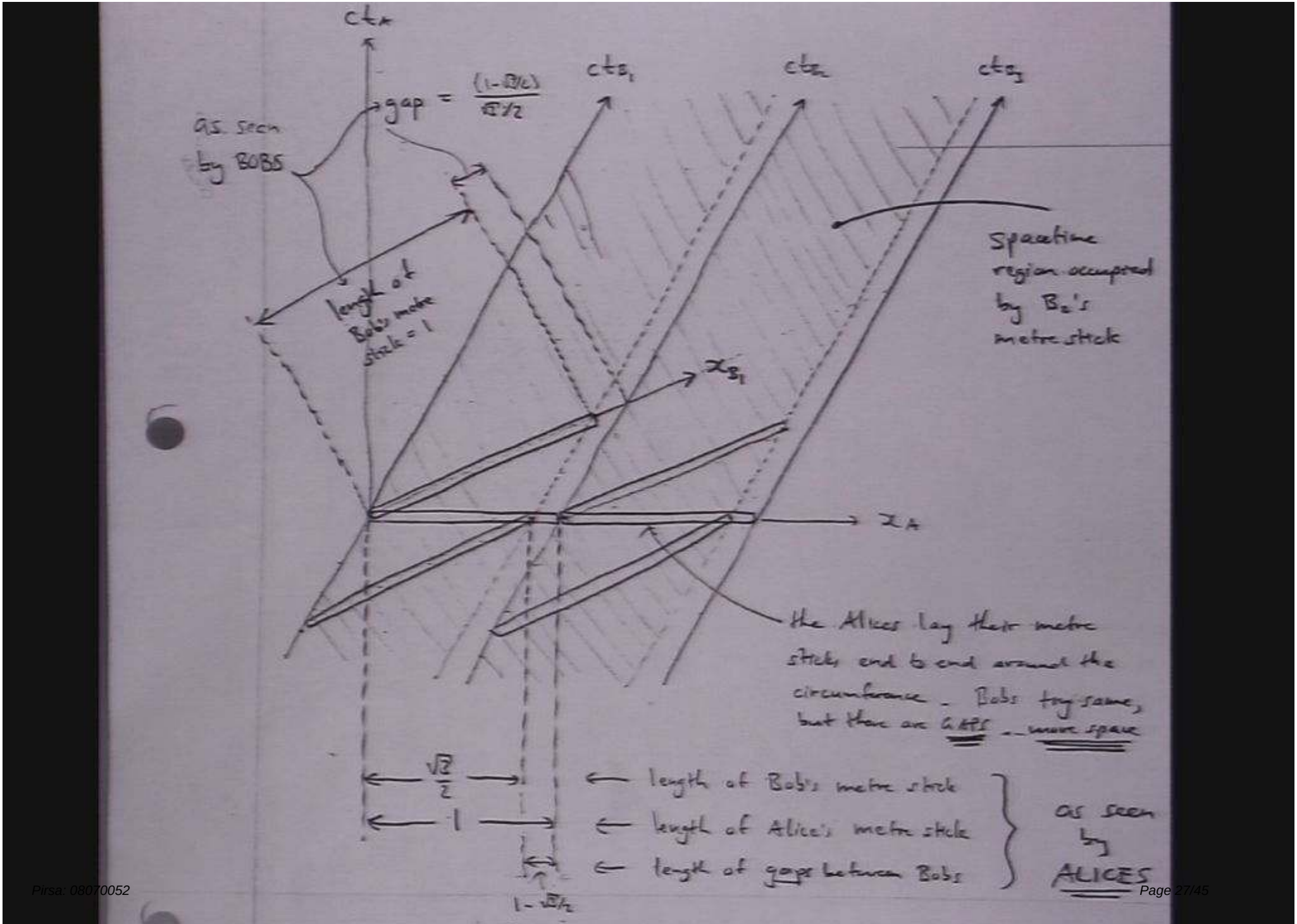


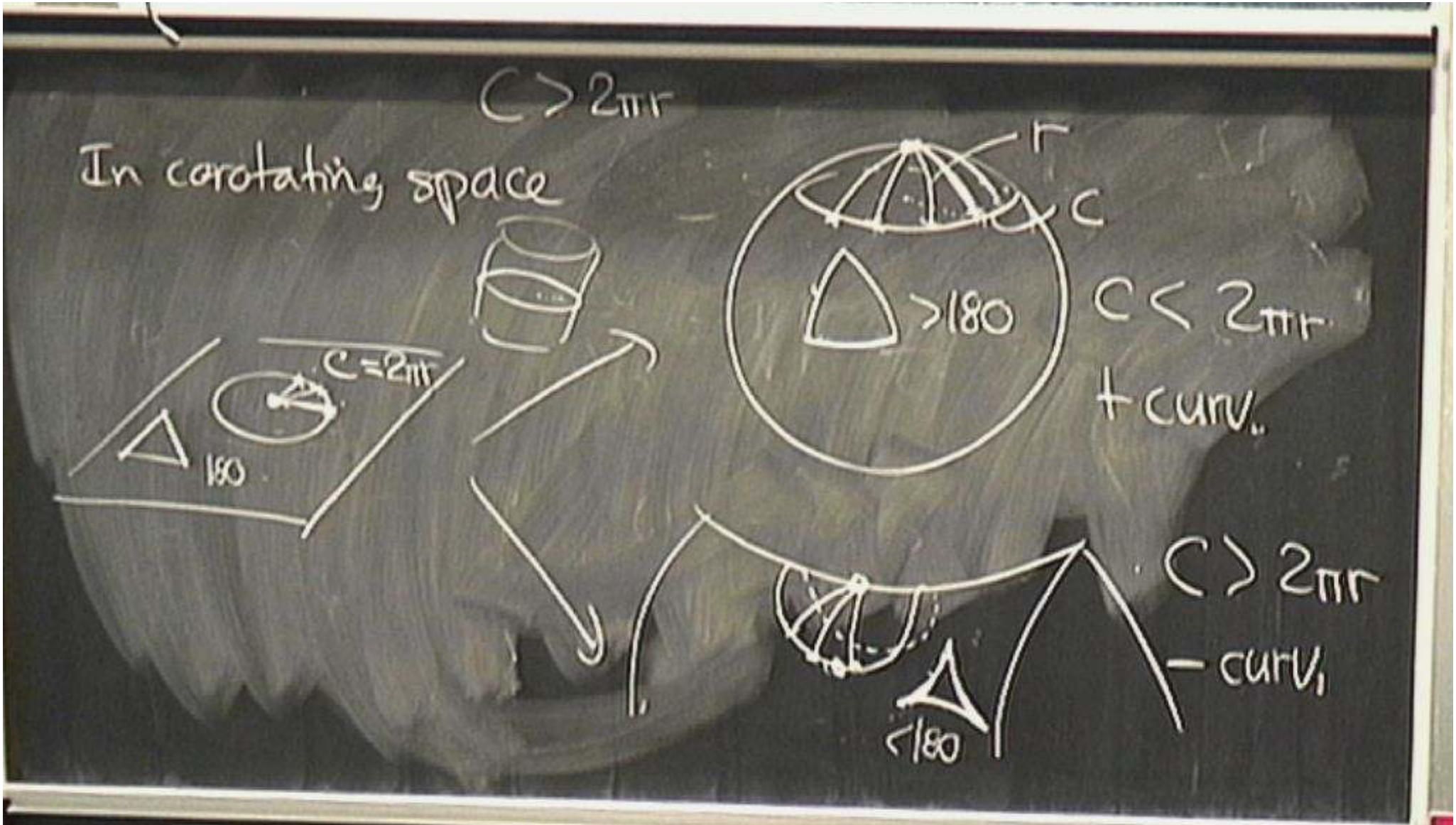
$\frac{\sqrt{2}}{2}$ ← length of Bob's metre stick

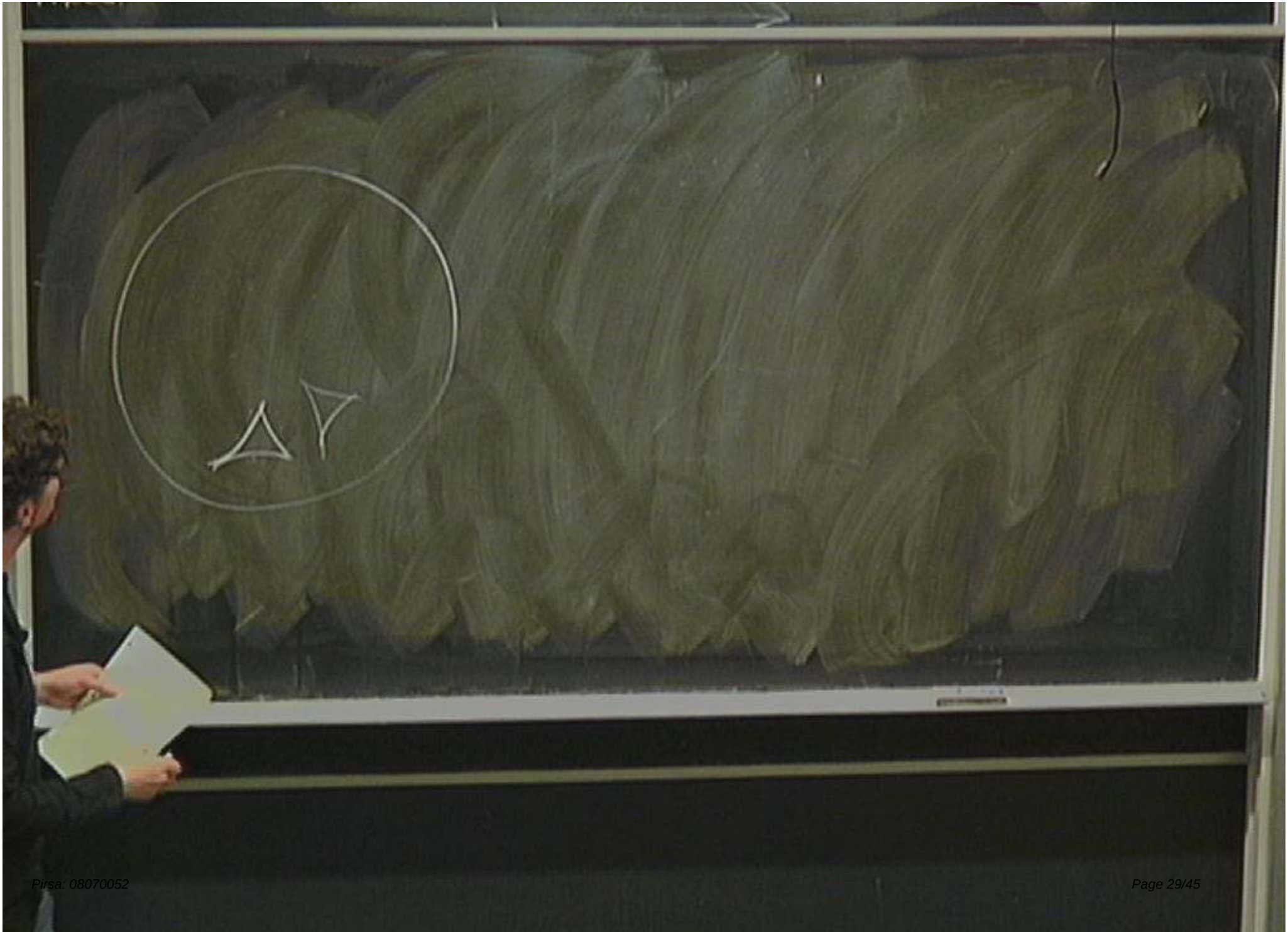
1 ← length of Alice's metre stick

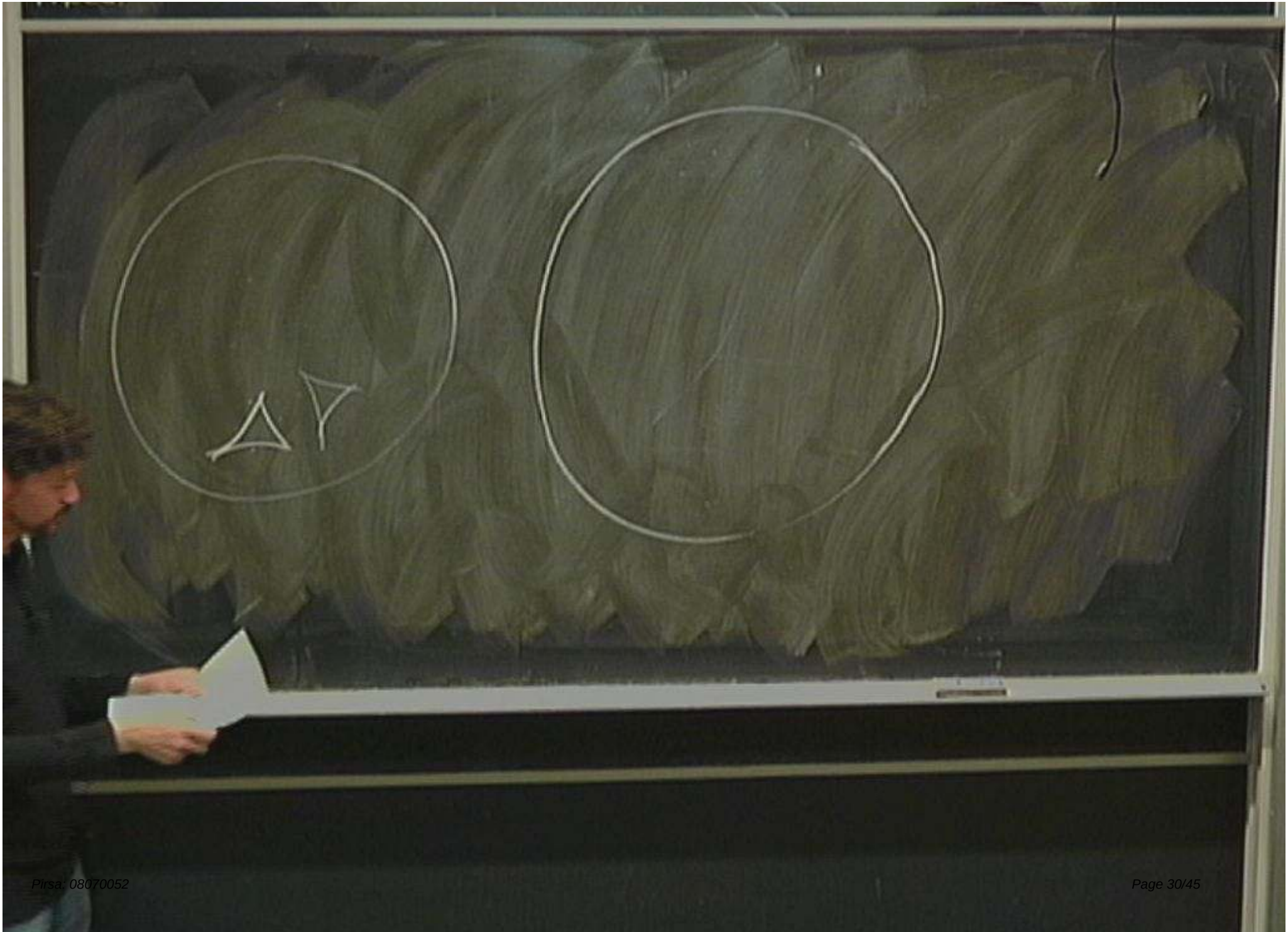
← length of gap between B_1

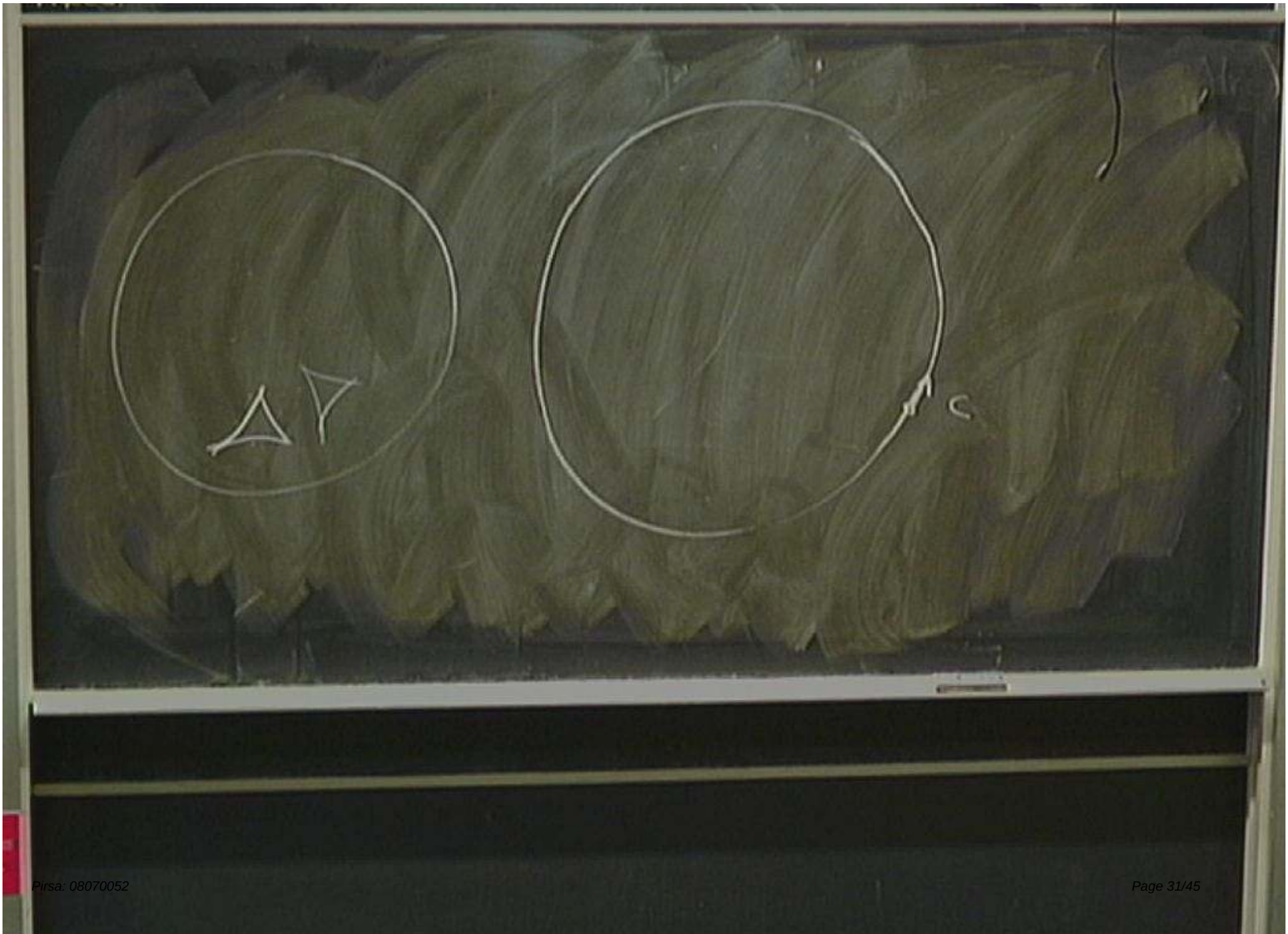
} as seen by Alices

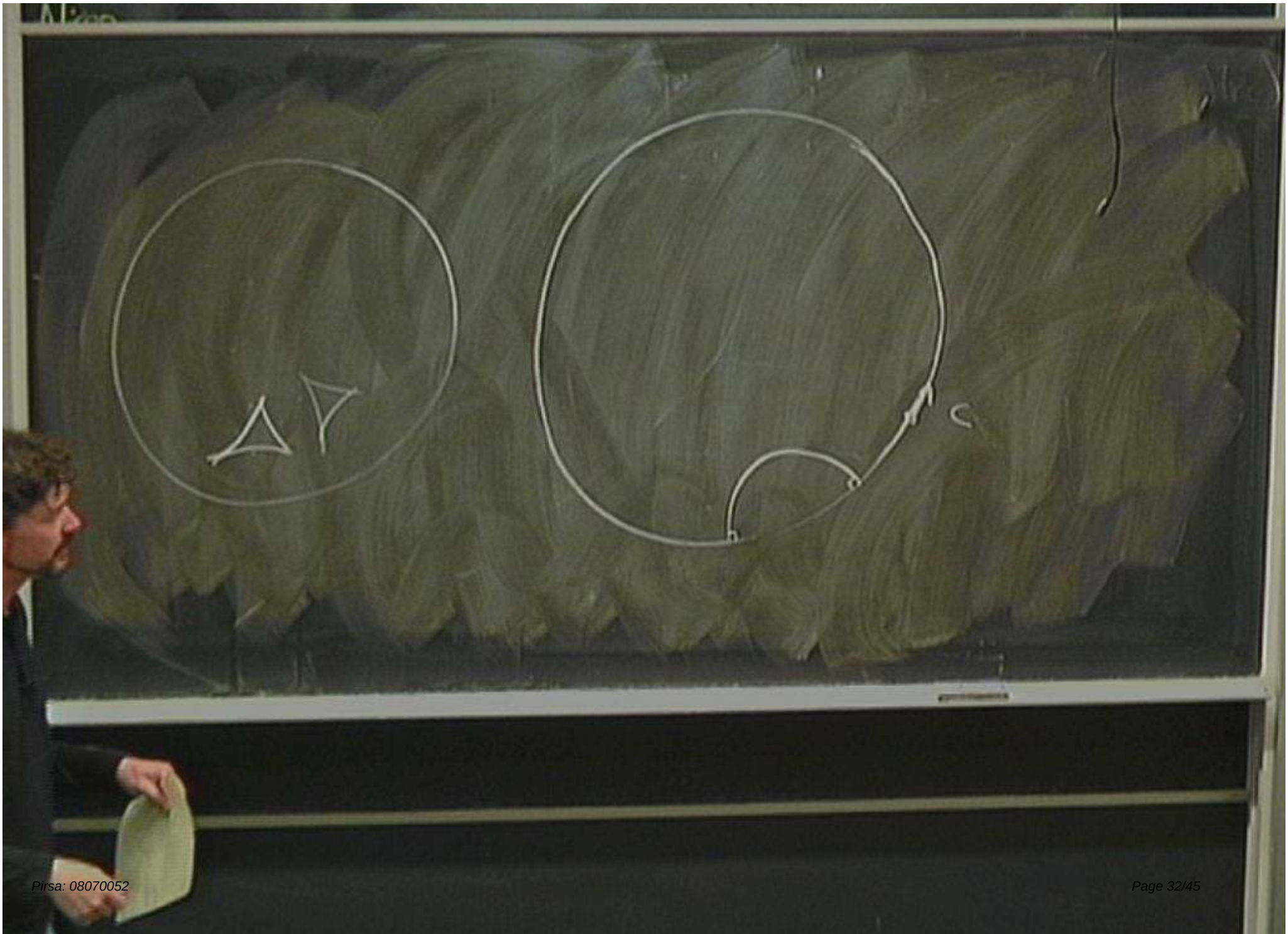

ct_A
ct_{B_1}
ct_{B_2}
ct_{B_3}
gap = $\frac{(1-\sqrt{2}/2)}{\sqrt{2}/2}$
as seen by BOBS
length of Bob's metre stick = 1
x_{B_1}
x_A
Spacetime region occupied by B_2's metre stick
the Alices lay their metre sticks end to end around the circumference. Bobs toy same, but there are GAPS ... more space
$\frac{\sqrt{2}}{2}$
1
$1-\sqrt{2}/2$
← length of Bob's metre stick
← length of Alice's metre stick
← length of gaps between Bobs
as seen by ALICES

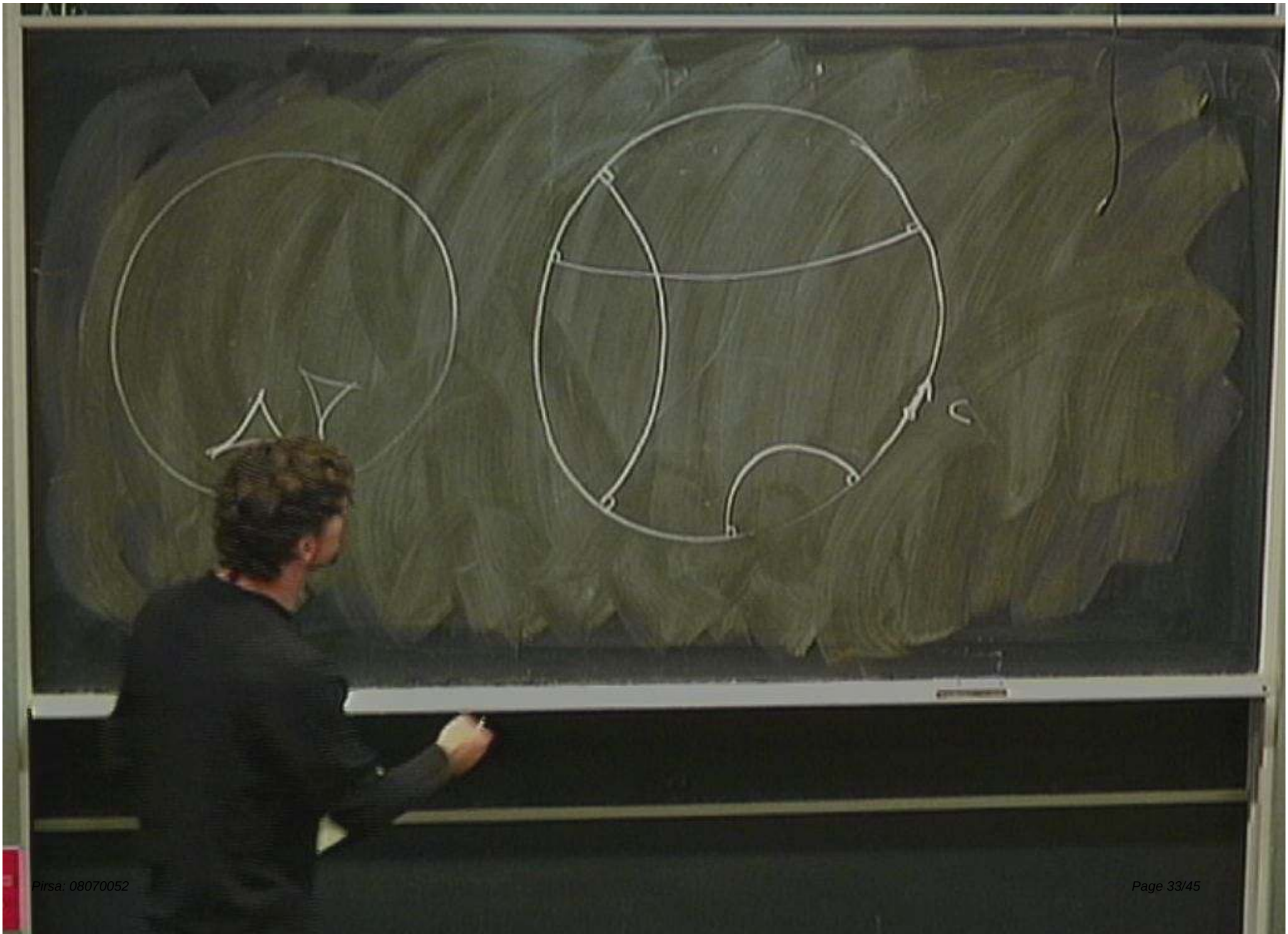

C > 2πr
In corotating space
r
C
>180
C < 2πr
+ curv.
C=2πr
Δ
180
C > 2πr
- curv.
<180

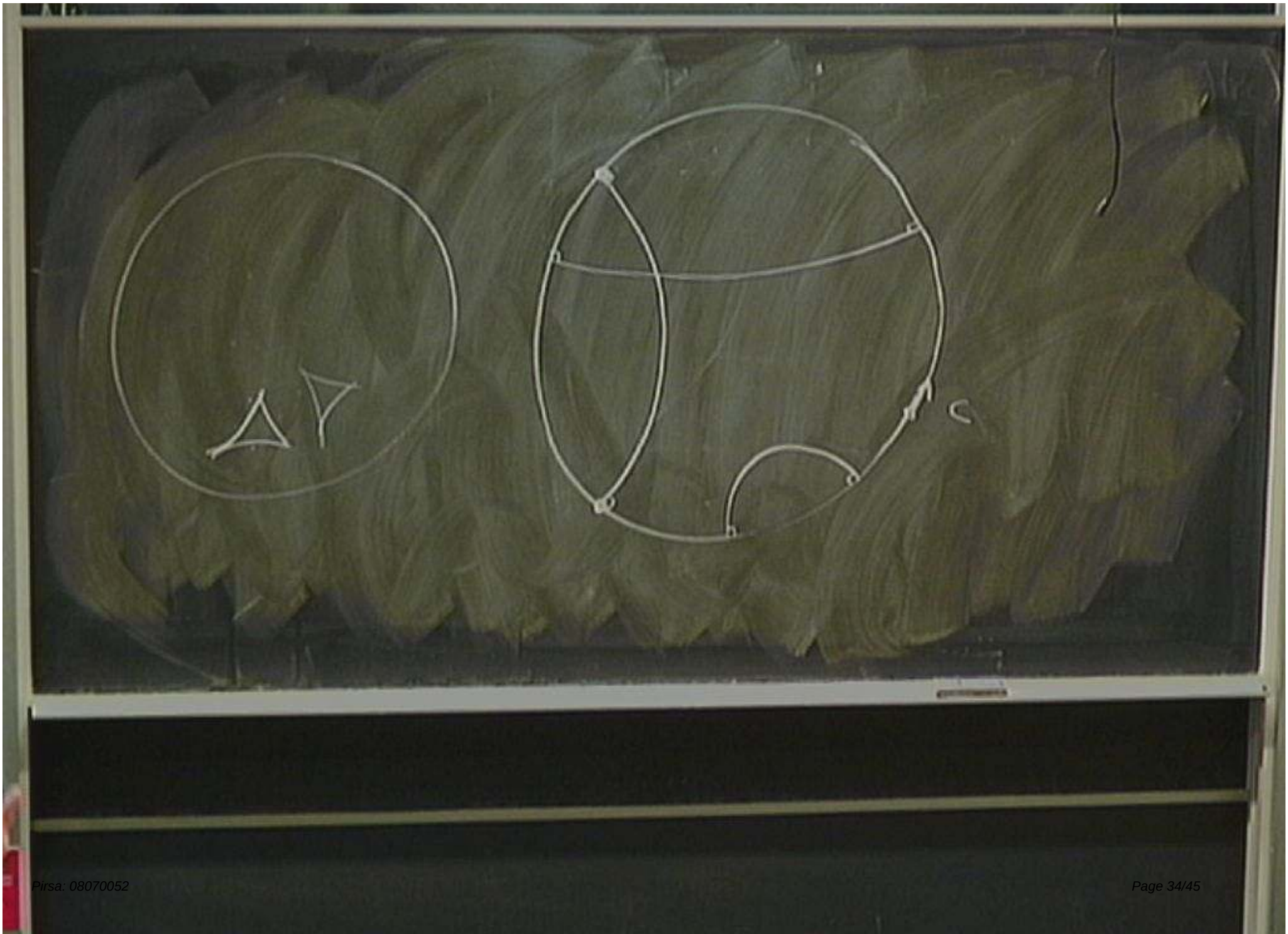





C



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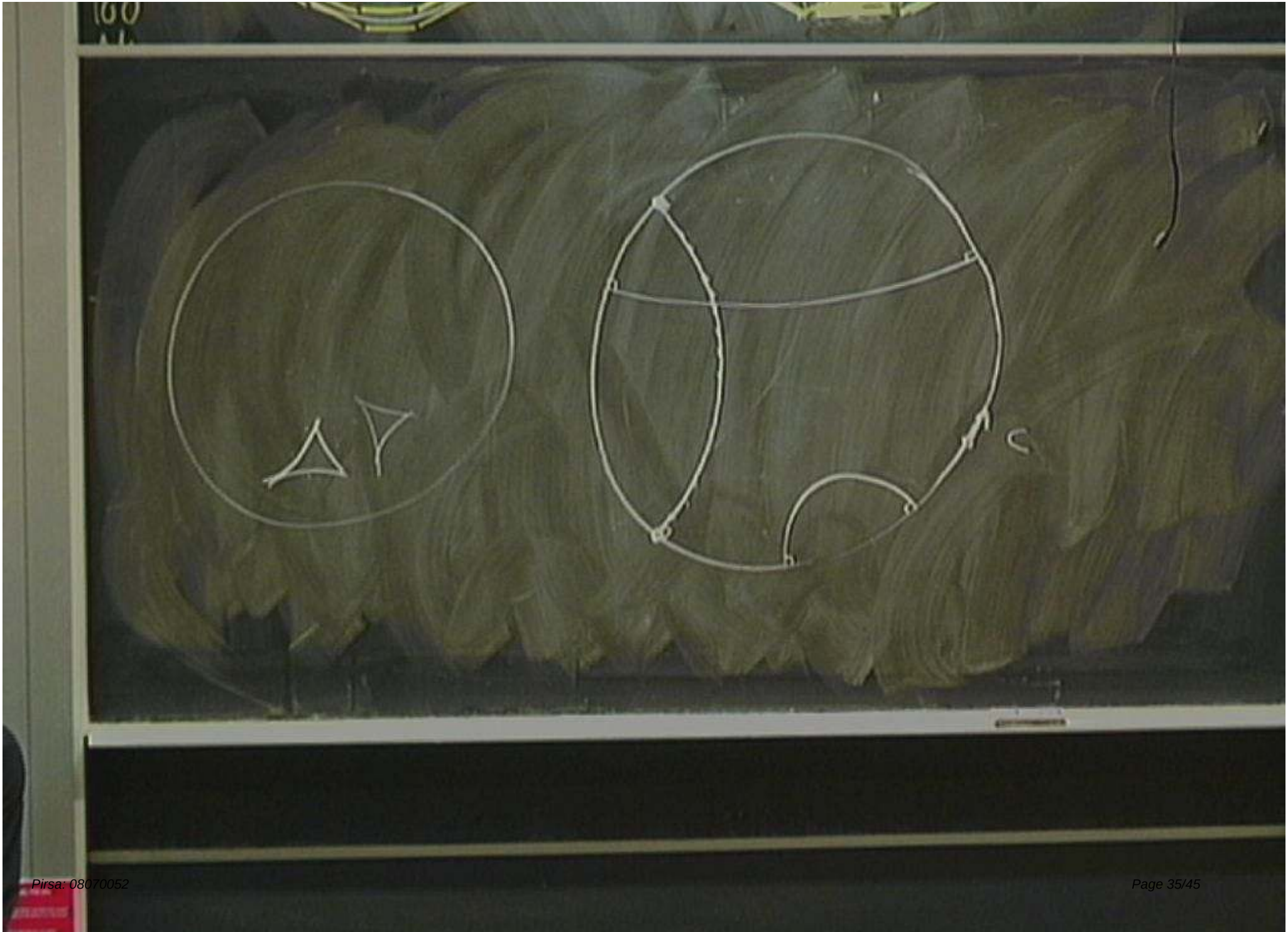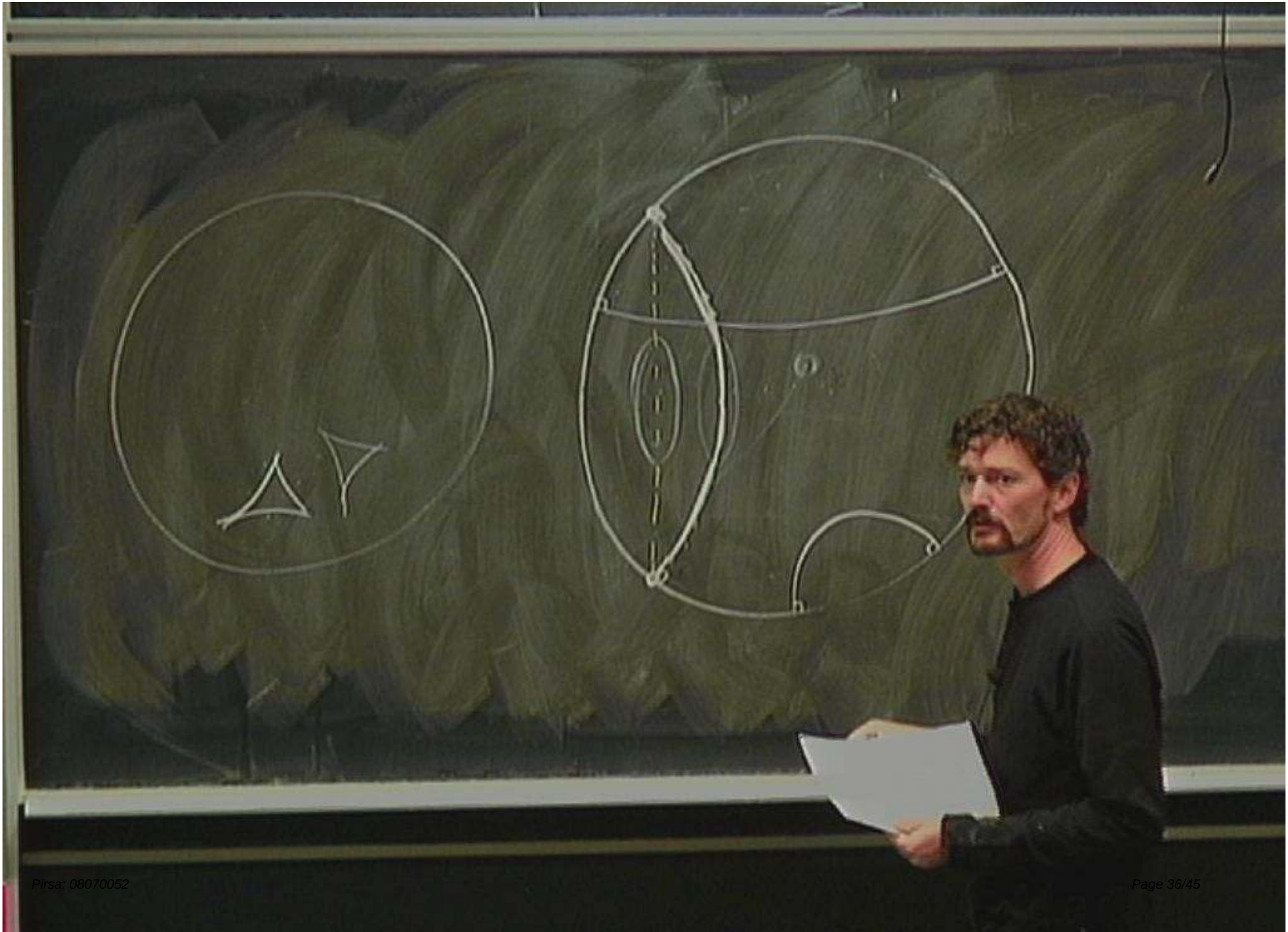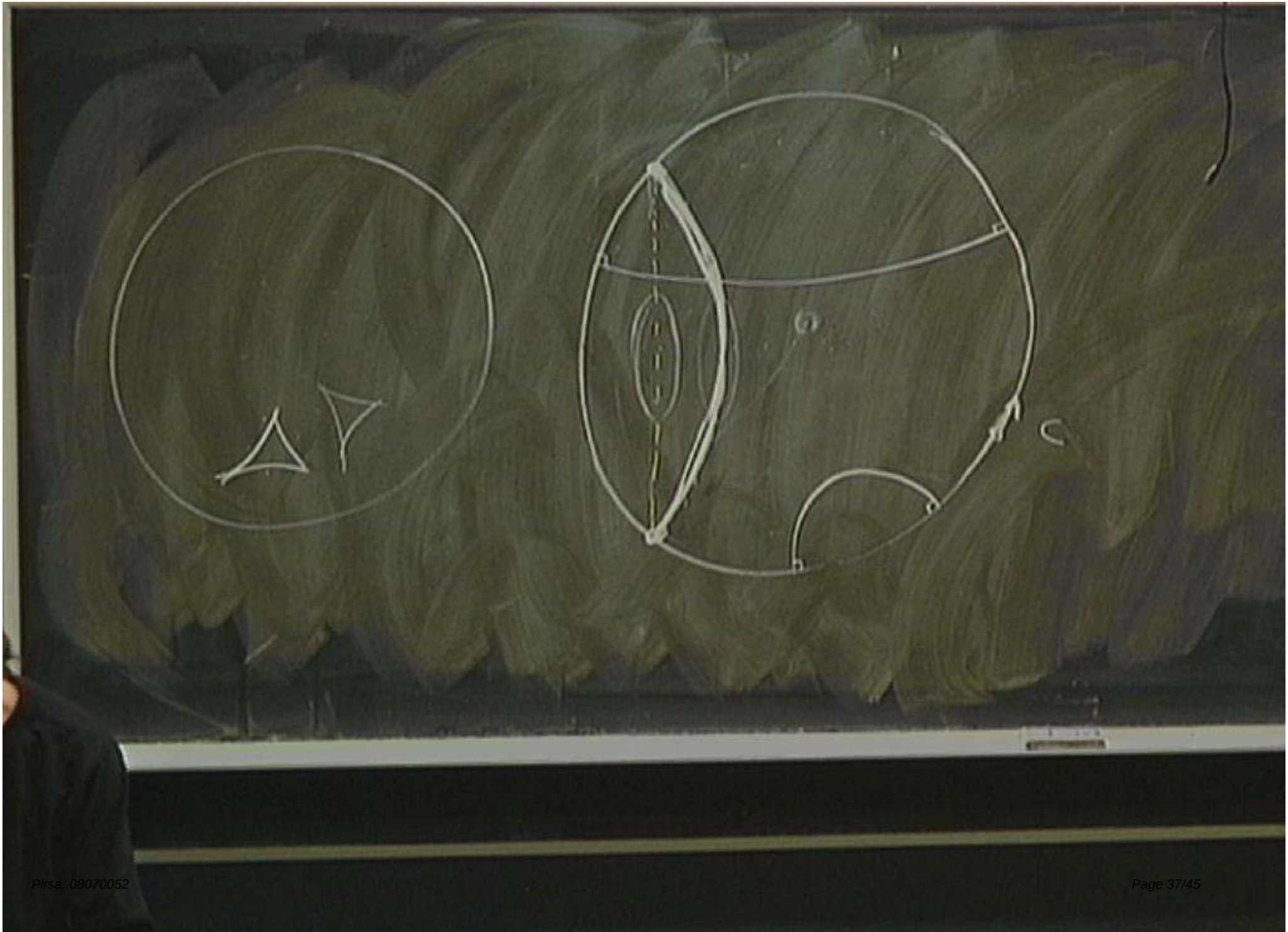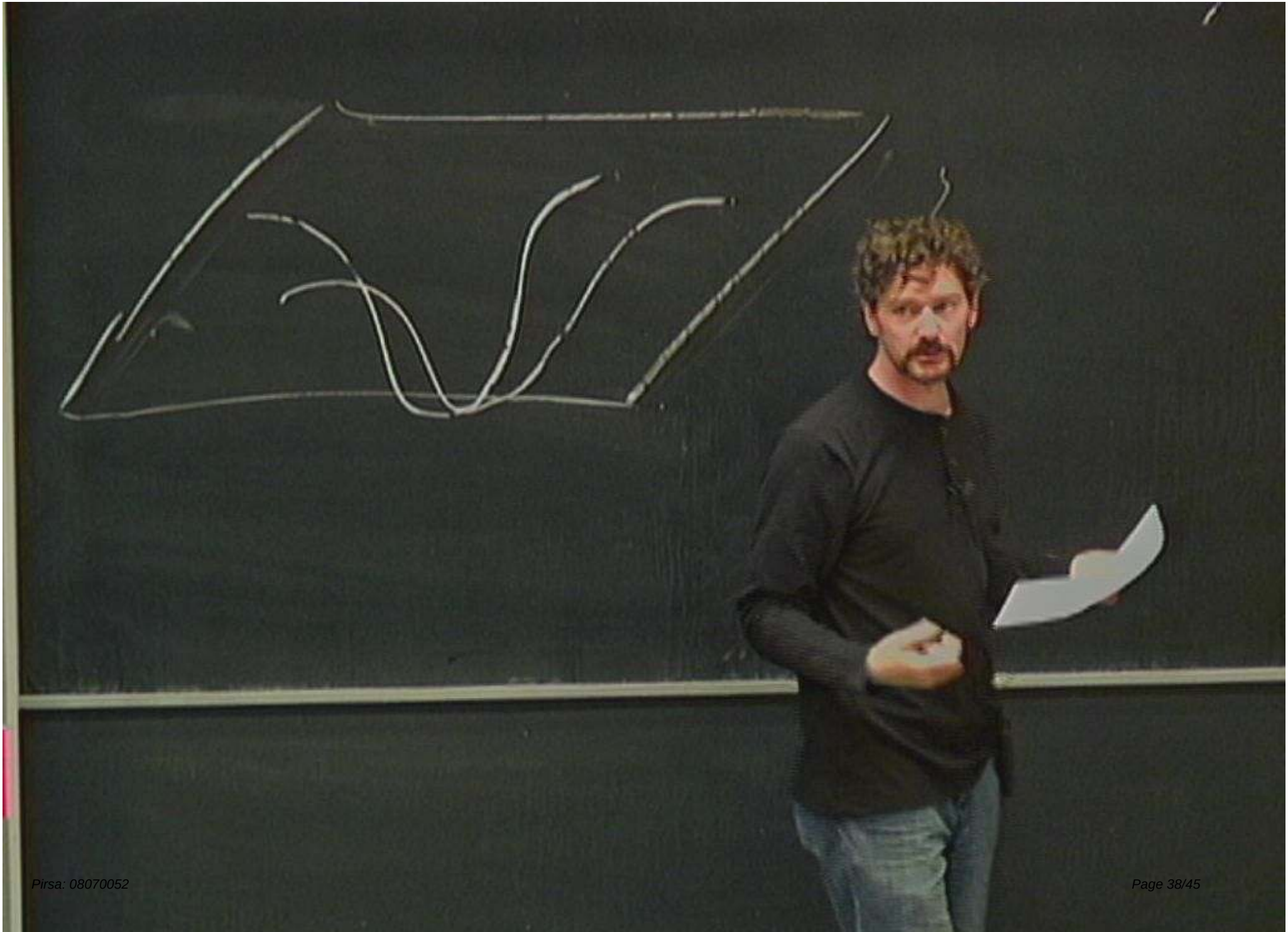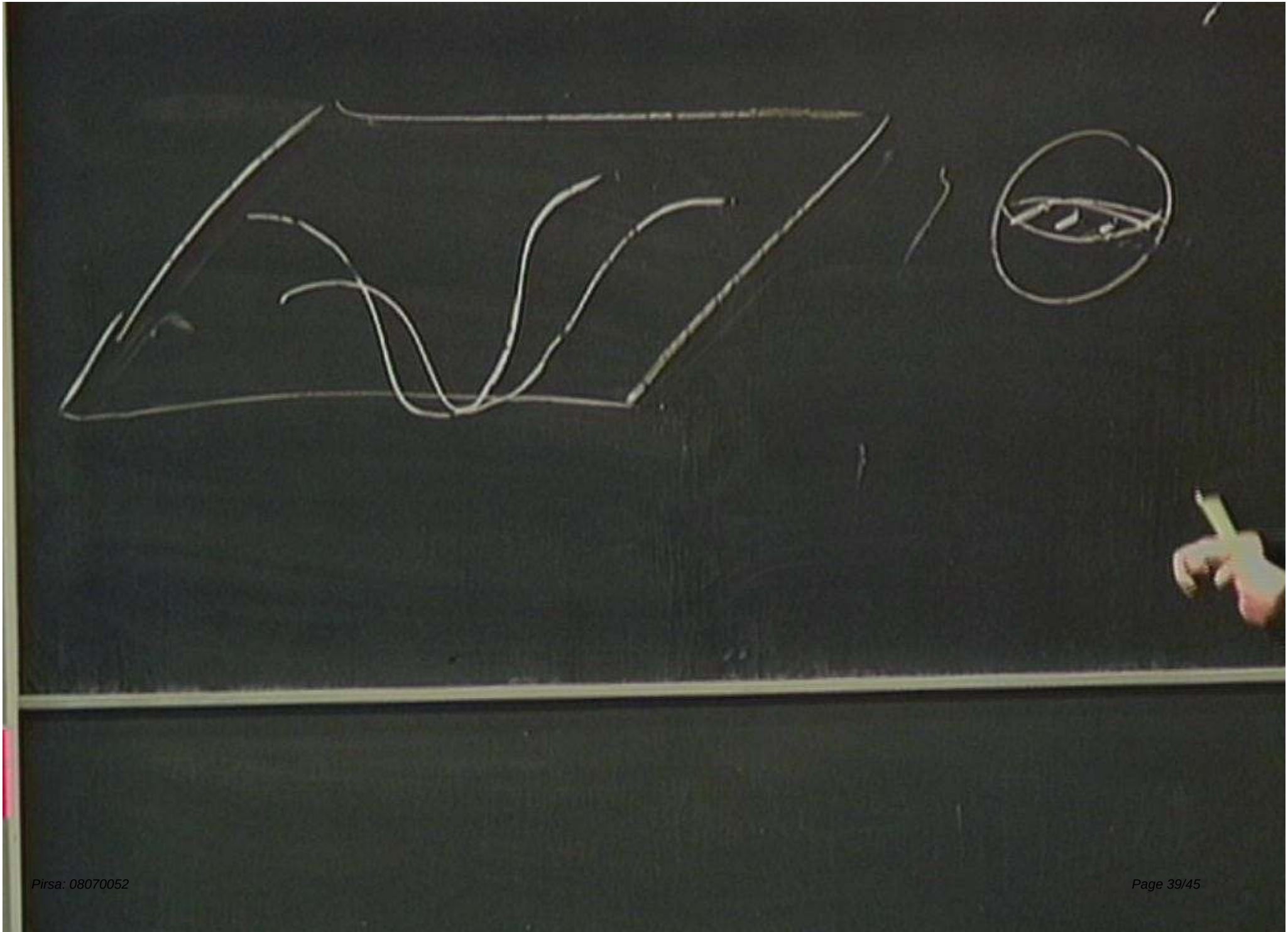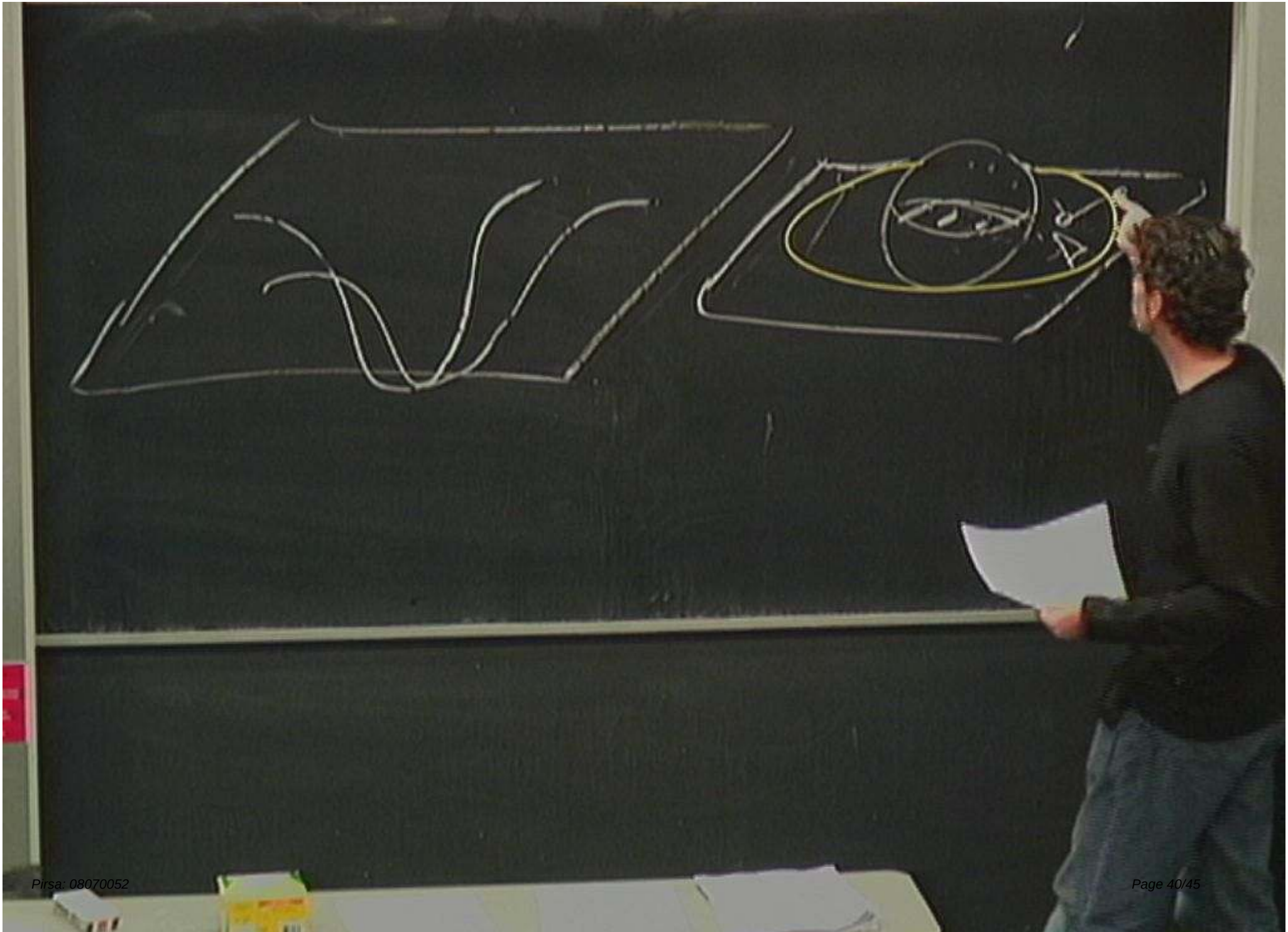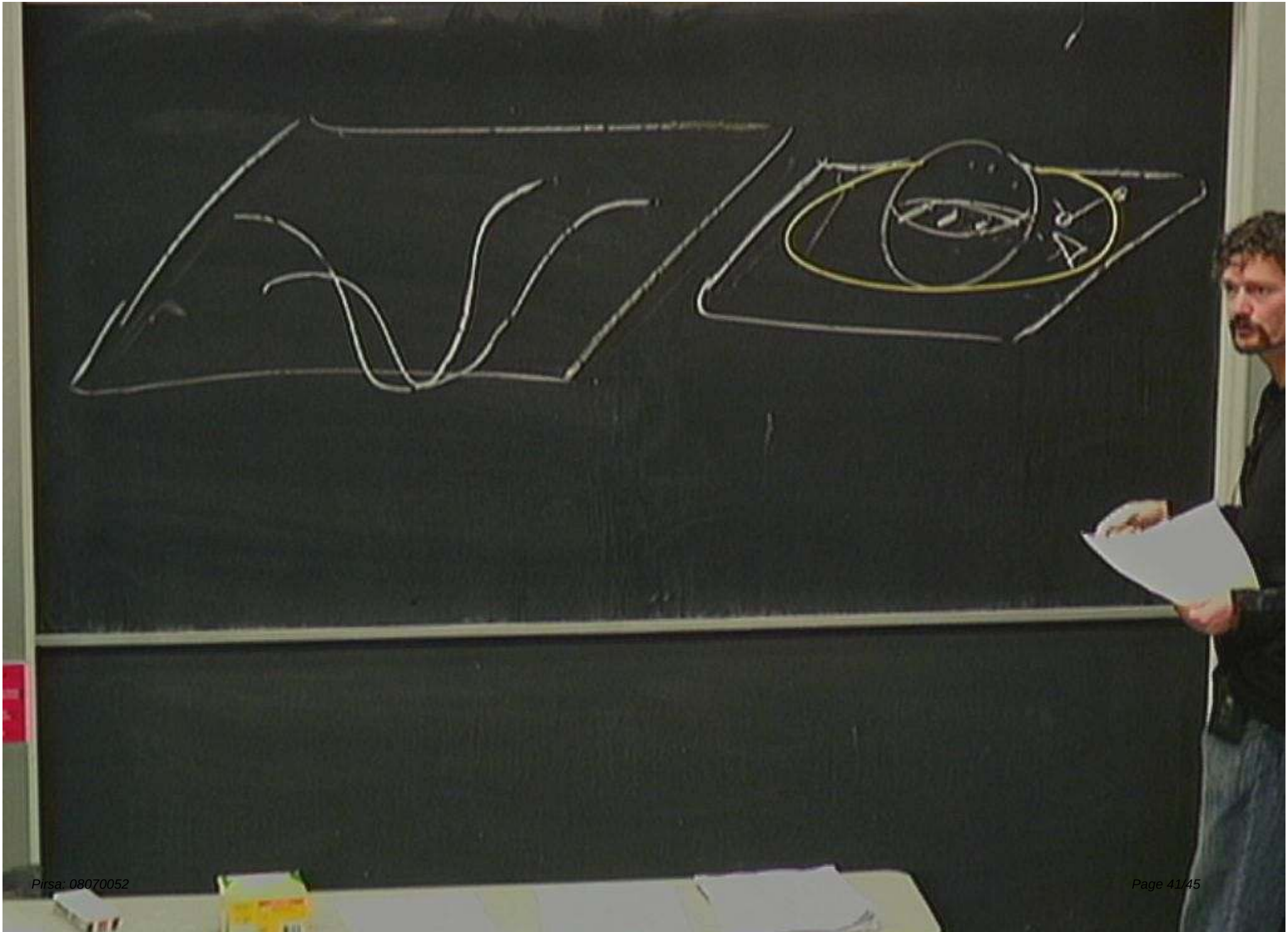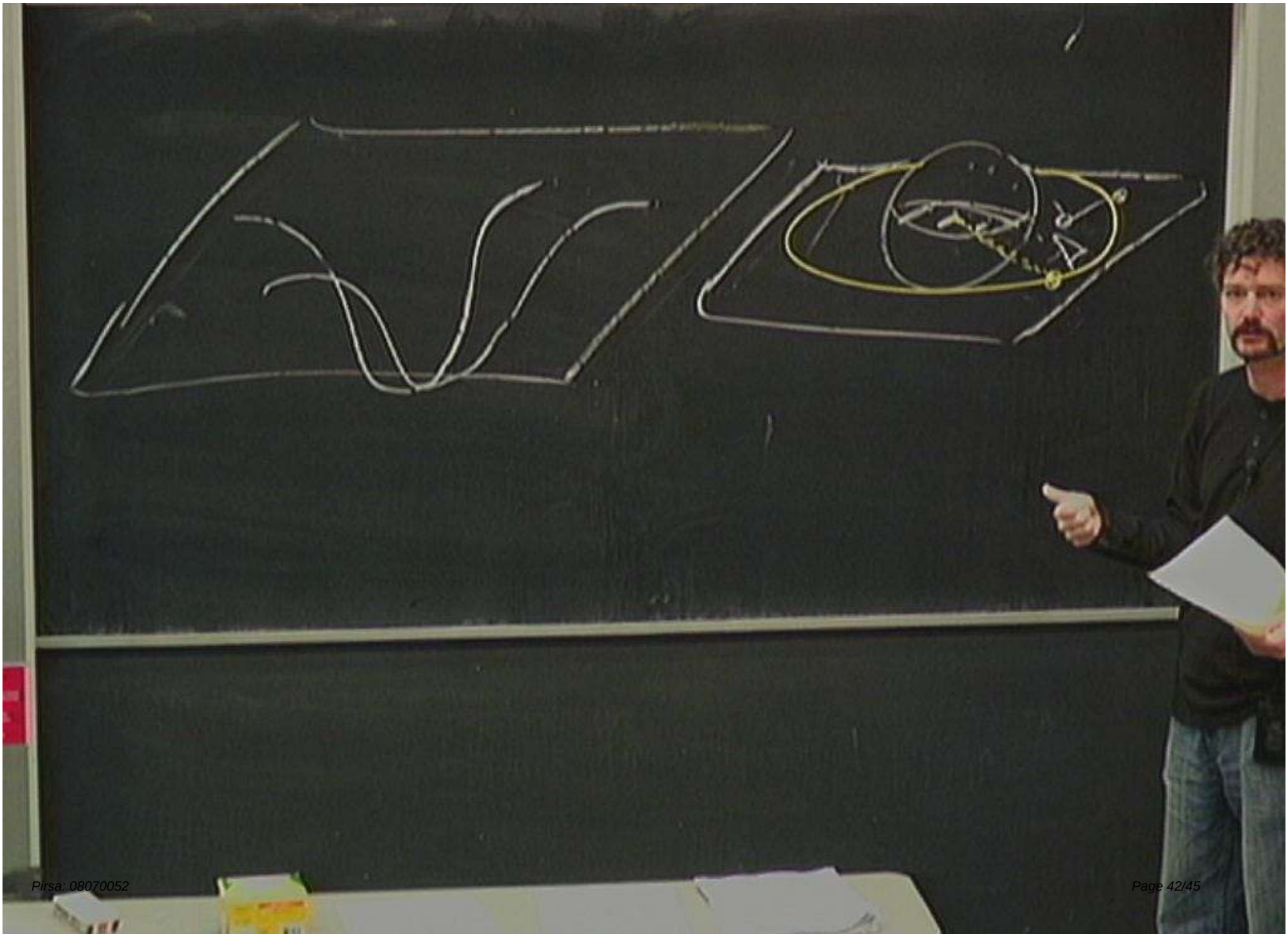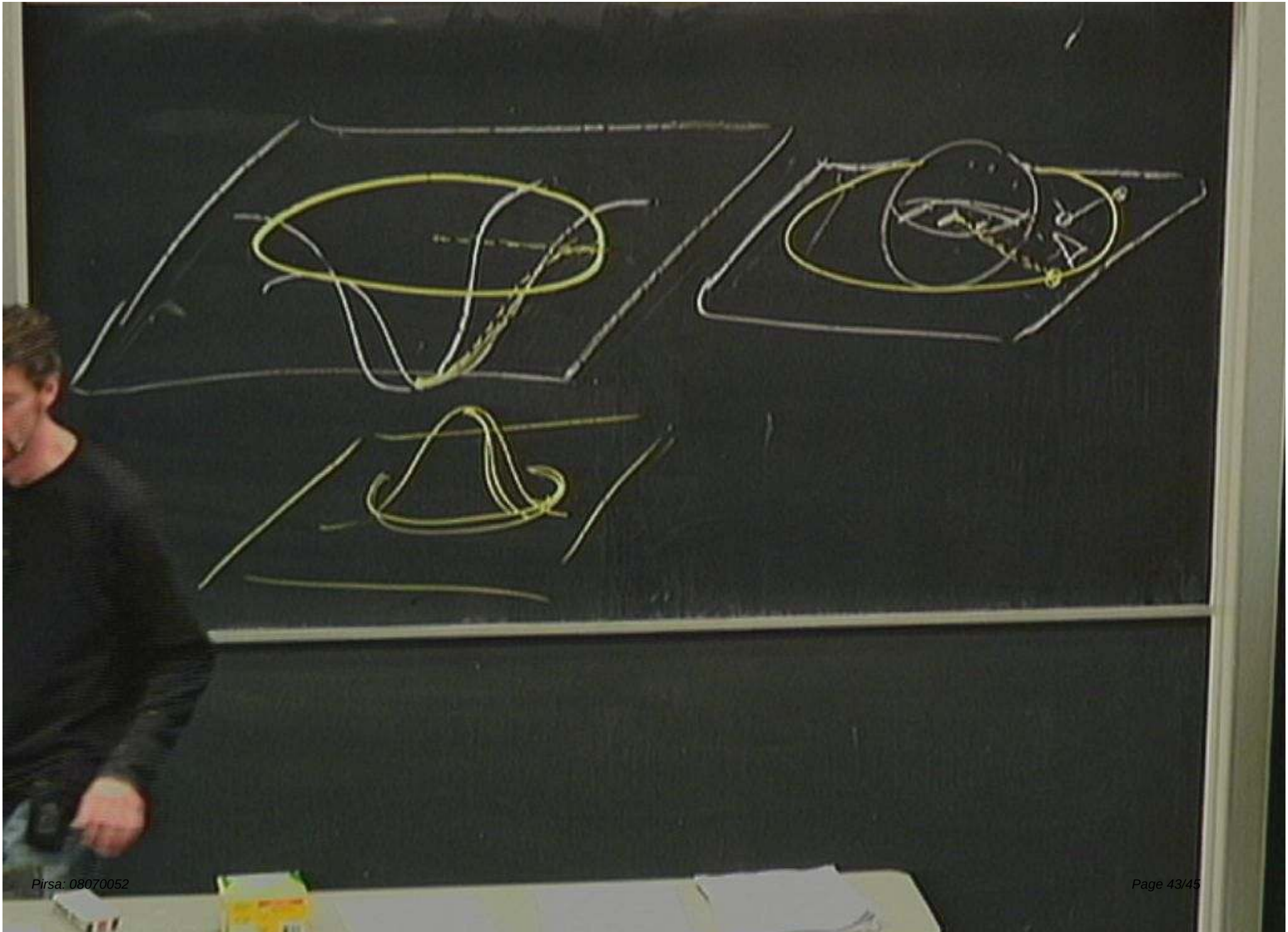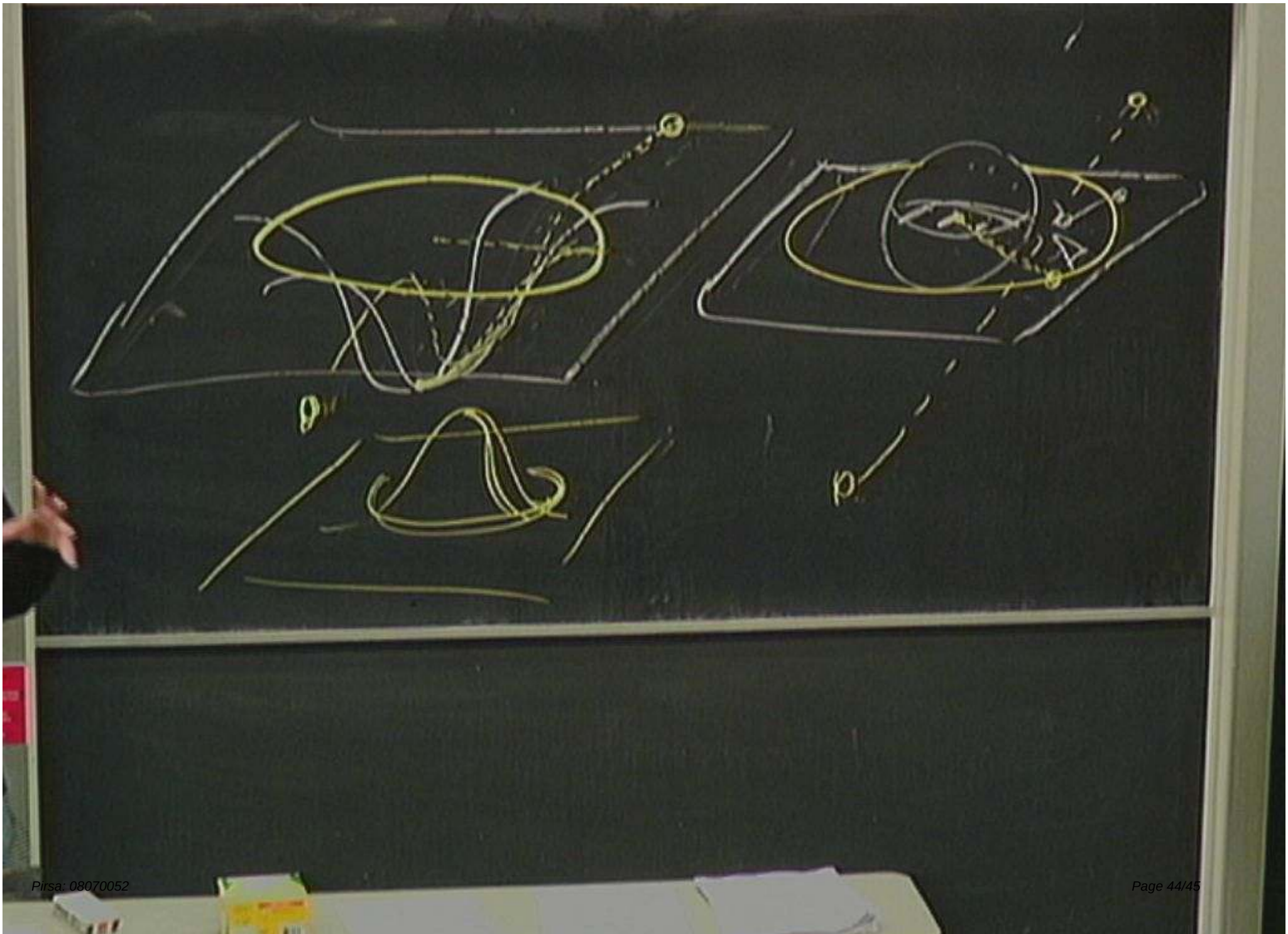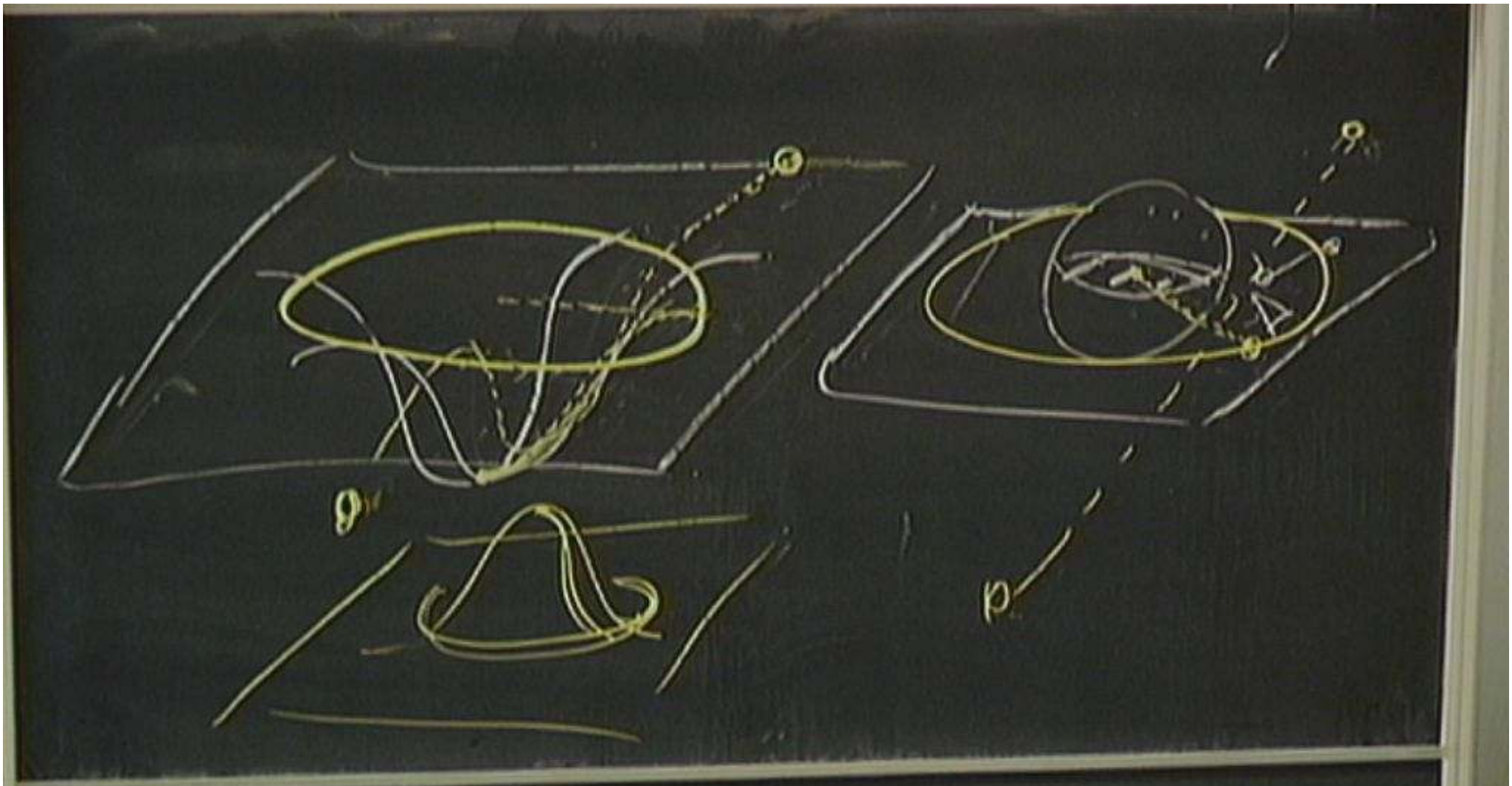
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