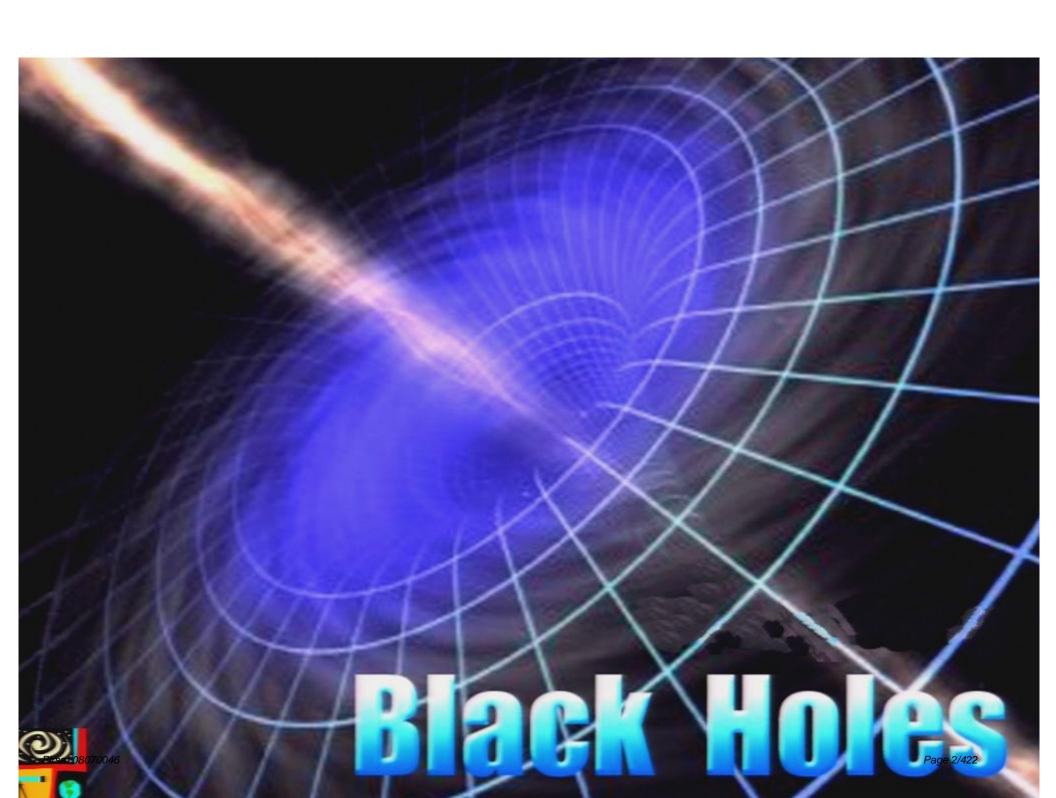
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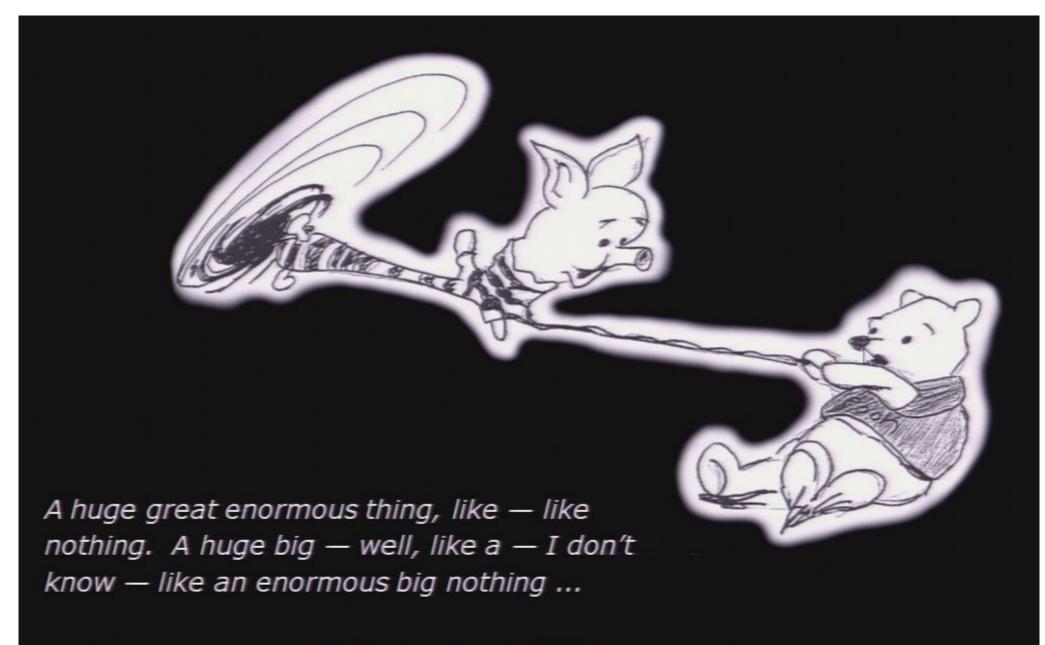
Date: Jul 30, 2008 02:00 PM

URL: http://pirsa.org/08070046

Abstract:

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Piglet describes the Heffalump, in Winnie the Pooh by A.A. Milne

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Dark stars

Rev. John Michell (1783)

A British born "natural philosopher" dared to combine the corpuscular description of light with Newton's gravitation laws to predict what large compact stars should look like.

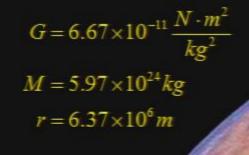
- He showed that a star, that has the same density of the sun, but 500 time as big, would have such a gravity, that "All light emitted from such a body would be made to return towards it". He said we wouldn't be able to see such a body, but we sure will feel it's gravitational pull.
- We could fly close to this "Dark star" and look around and describe the features of the object.
- A novelty, world lost interest when light was shown to be waves in 1803 by Thomas Young.

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$$\frac{1}{2}mv^2 = \frac{GMm}{r}$$

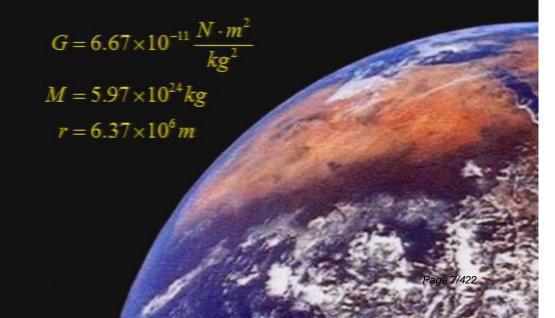


$$\frac{1}{2}mv^2 = \frac{GMm}{r}$$



Calculate Escape Velocity

$$\frac{1}{2}mv^2 = \frac{GMm}{r}$$

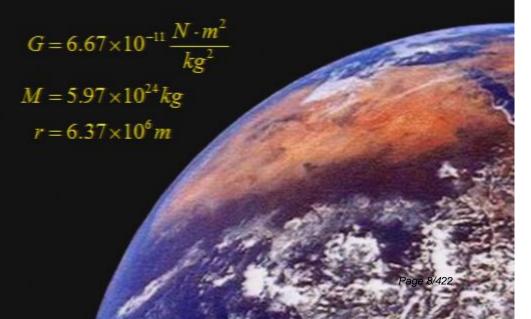


$$\frac{1}{2}mv^2 = \frac{GMm}{r}$$

$$\frac{1}{2}v^2 = \frac{GM}{r}$$

$$v = \sqrt{2 \frac{\left(6.67 \times 10^{-11}\right) \left(5.97 \times 10^{24}\right)}{6.37 \times 10^{6}}}$$

veldsim :



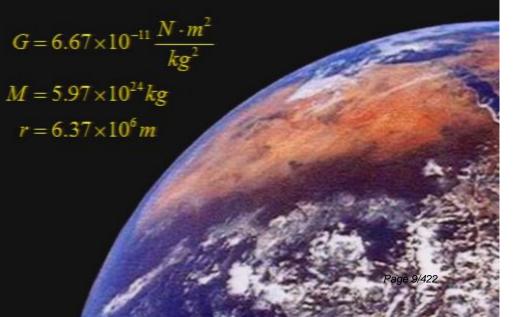
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$$v \approx 11181 m/s$$

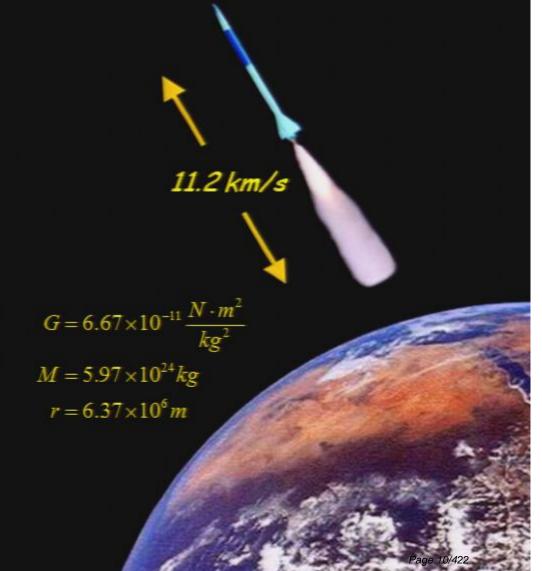
11.2 km/s



$$\frac{1}{2}mv^2 = \frac{GMm}{r}$$
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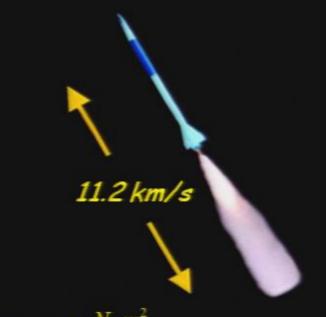
What is Earth's r when escape velocity is $3x10^8$ m/s

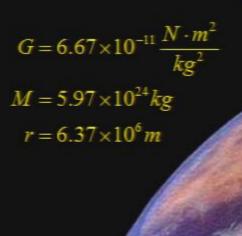
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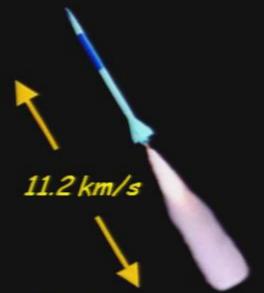
~8.9 mm

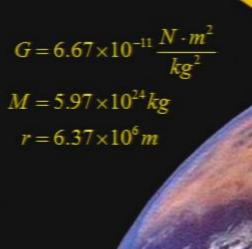
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Einstein's Equivalence Principle

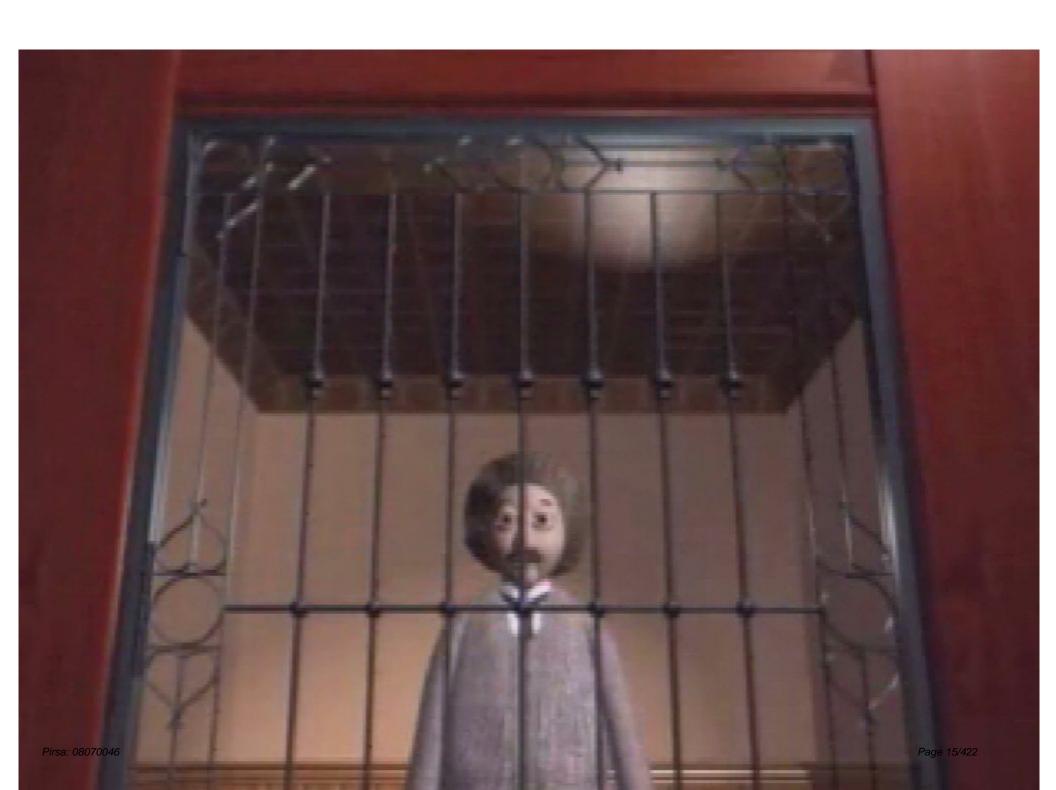
 There is no experiment that you can perform that will distinguish these two diagrams

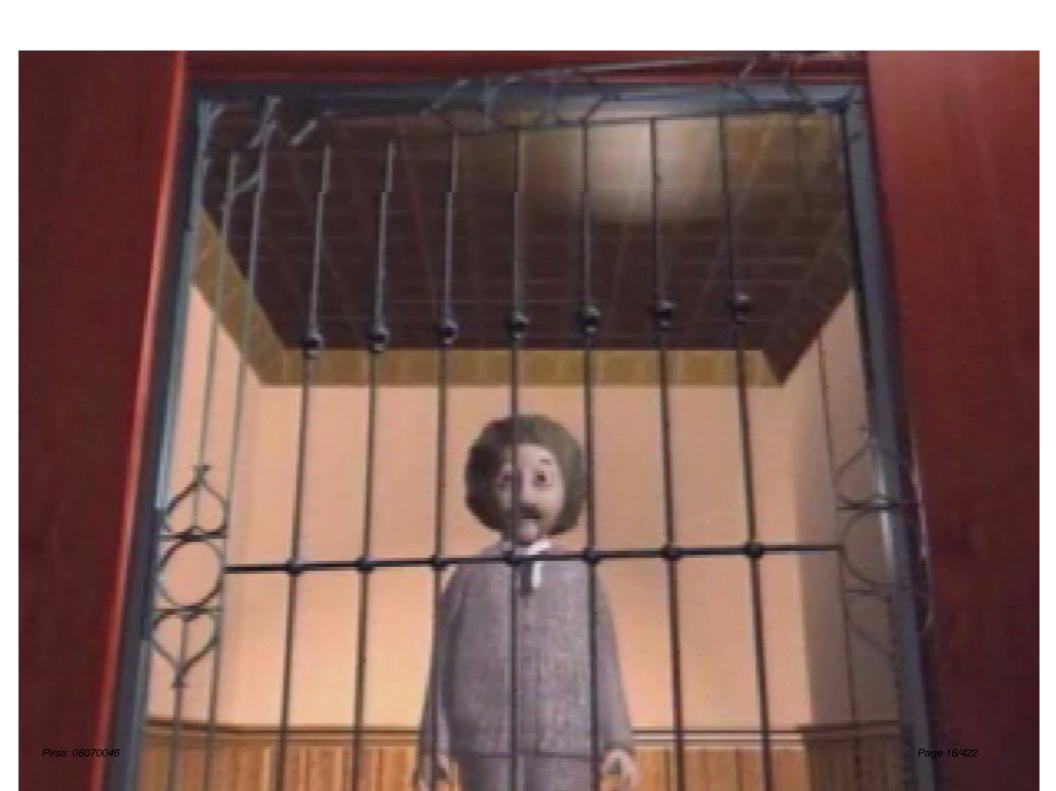


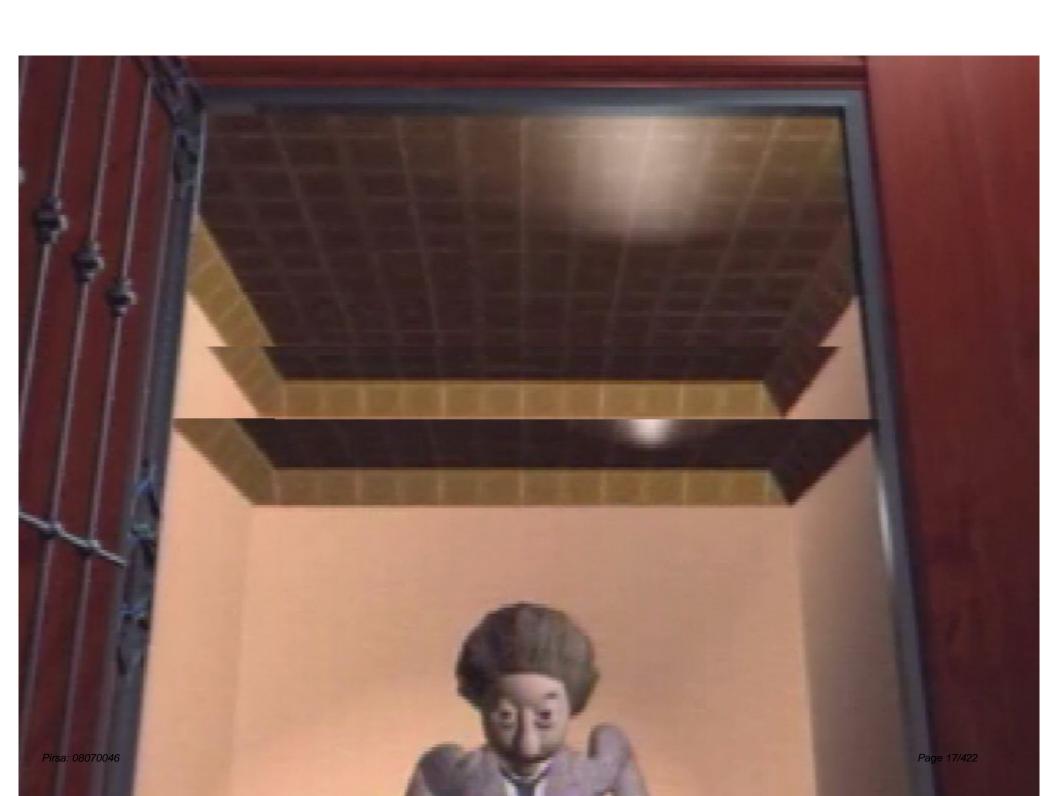


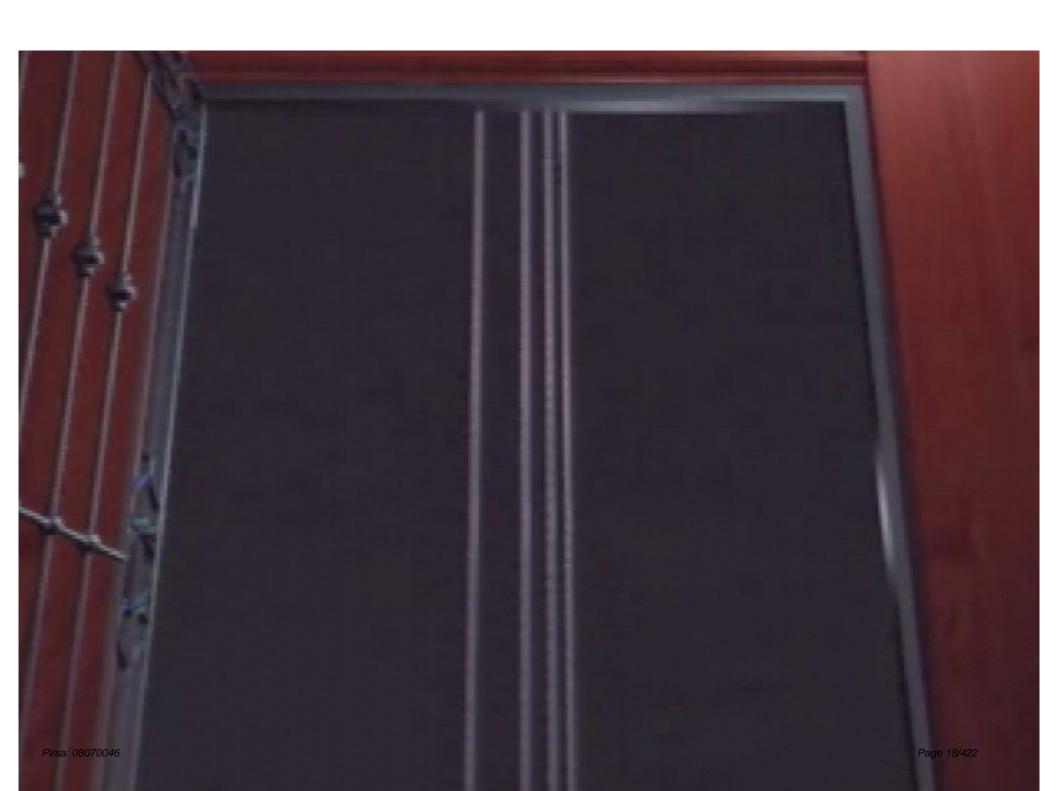
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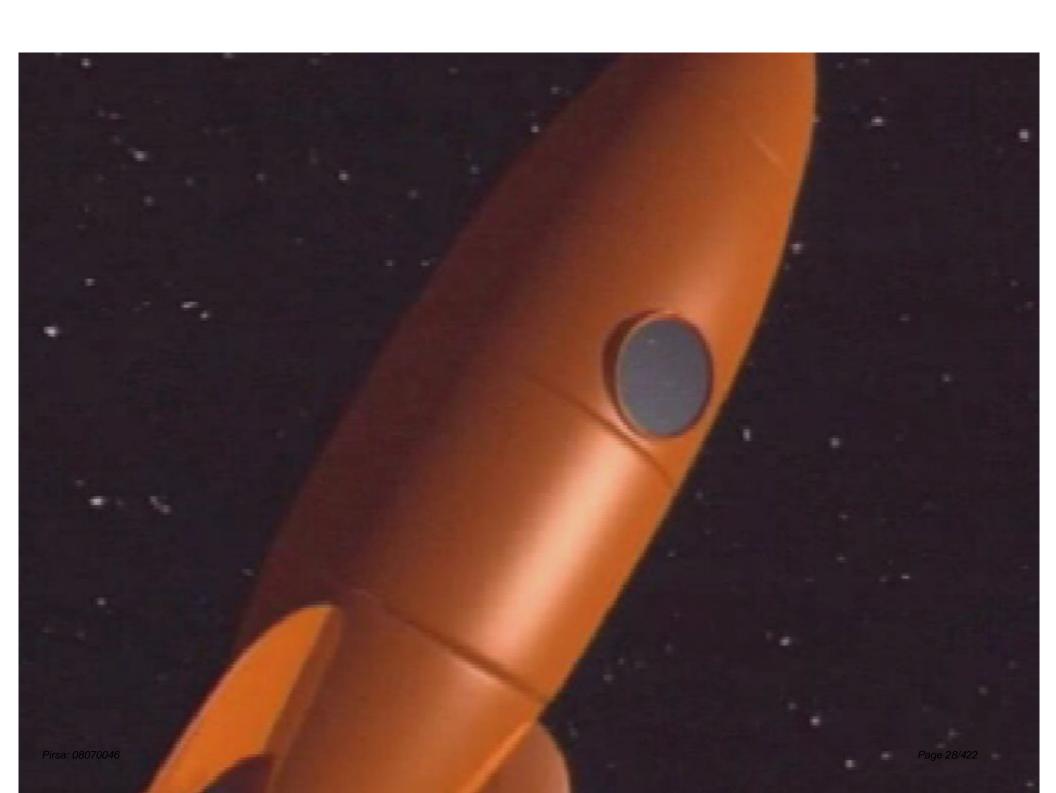


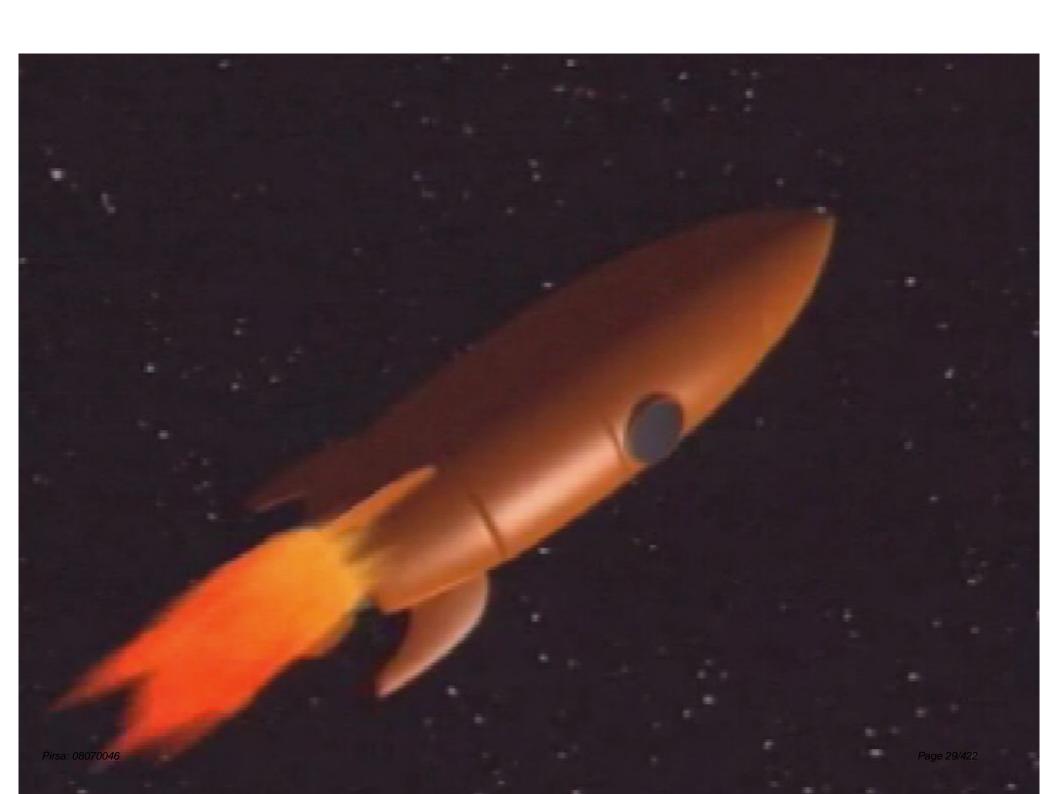




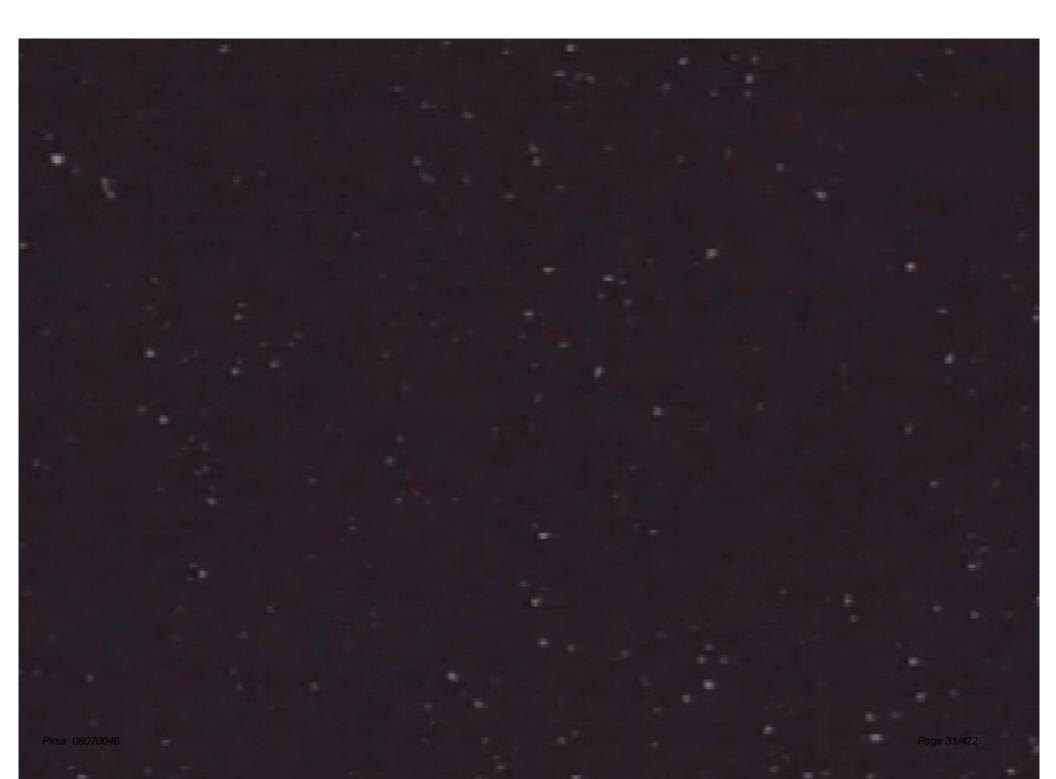


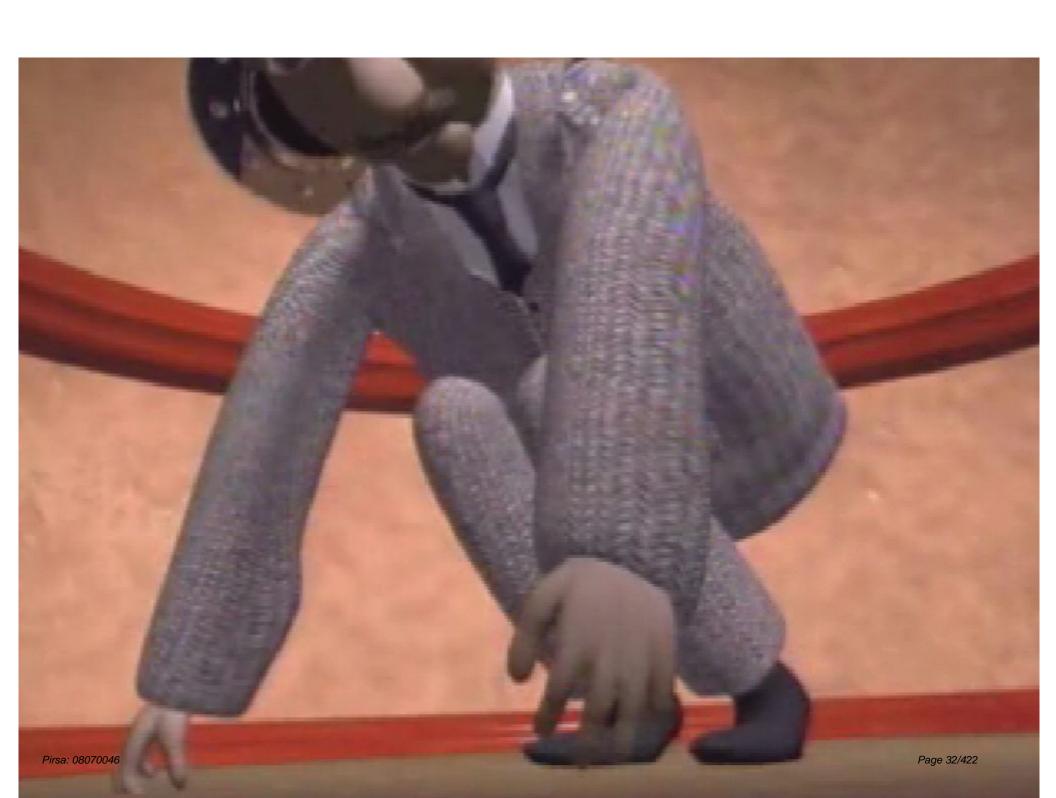




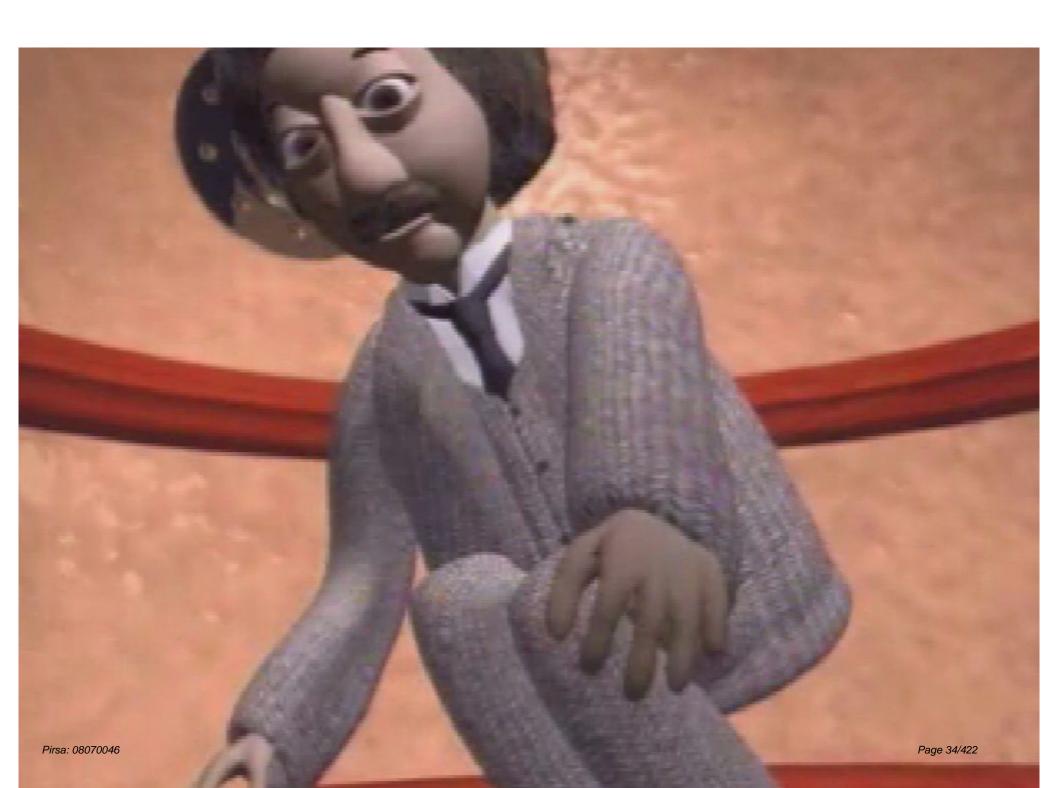


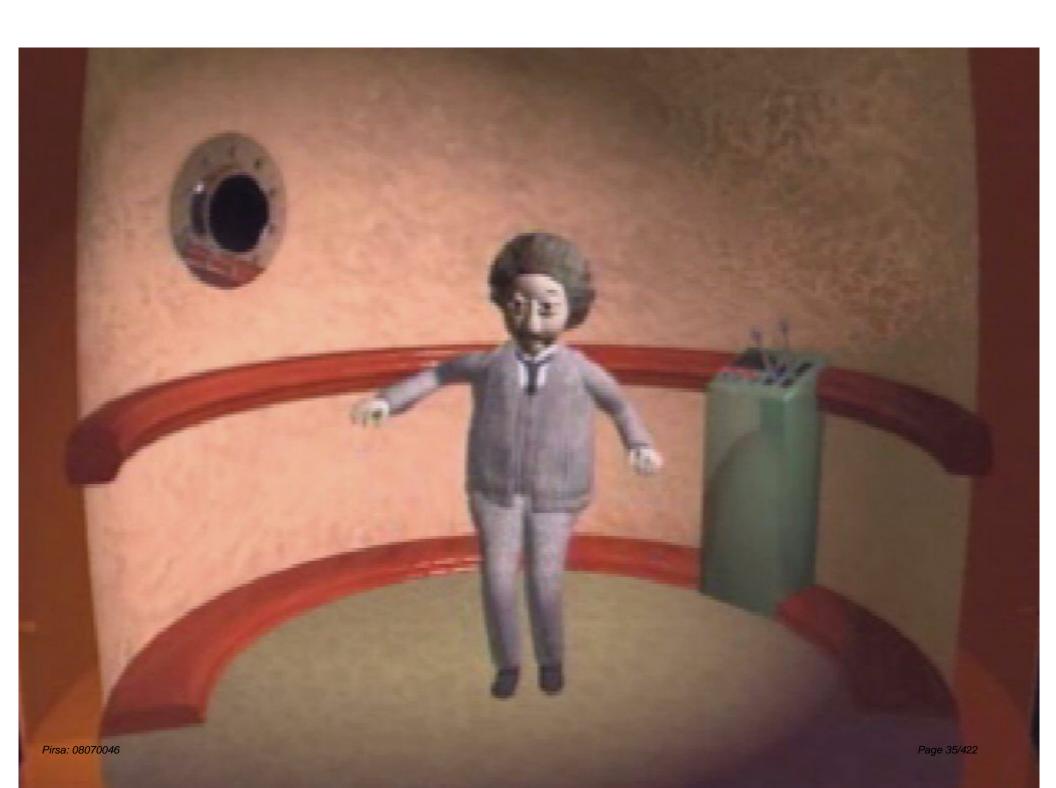


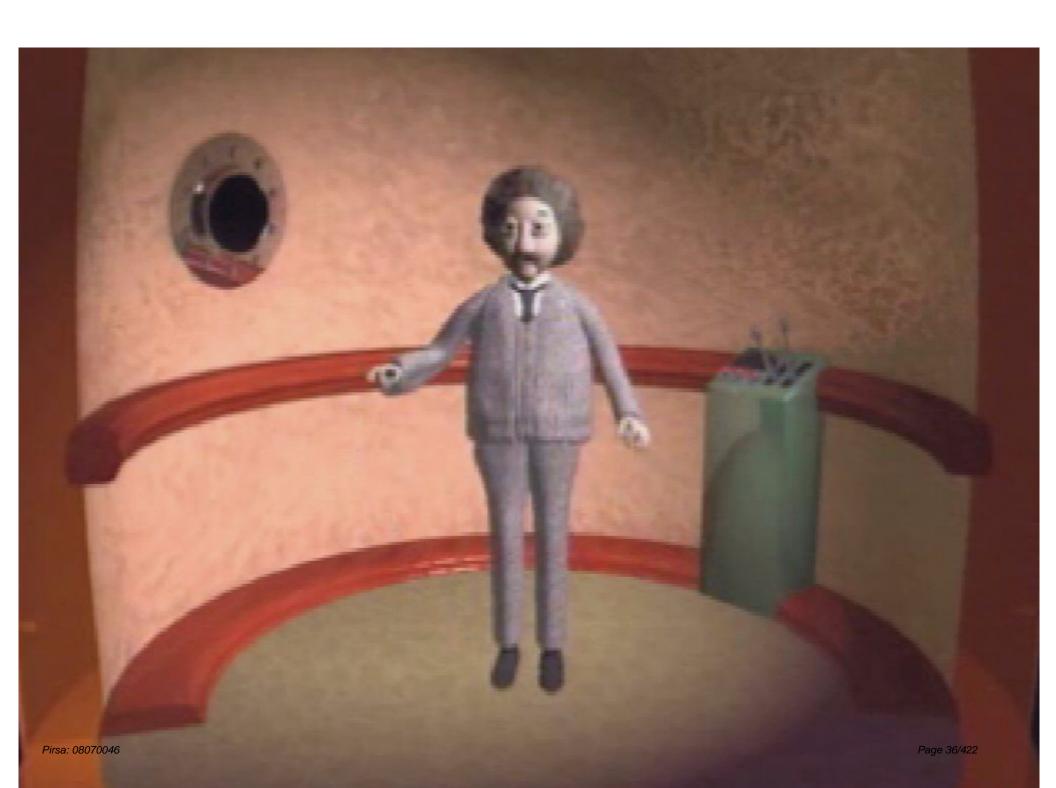


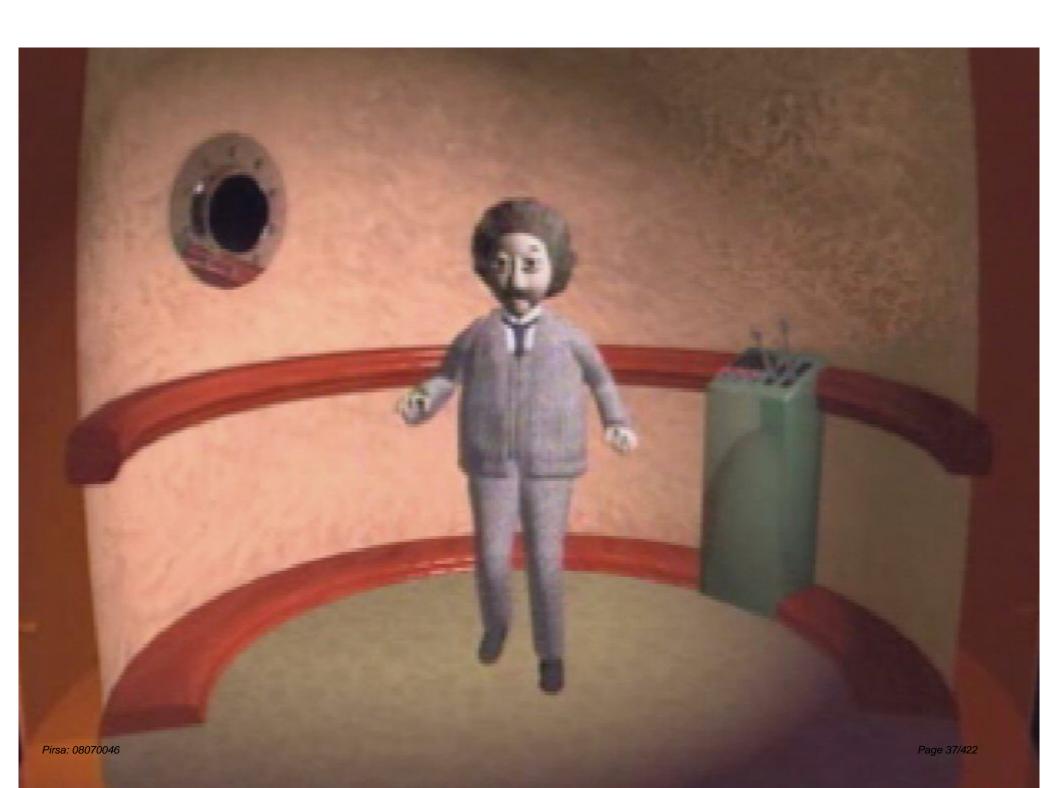


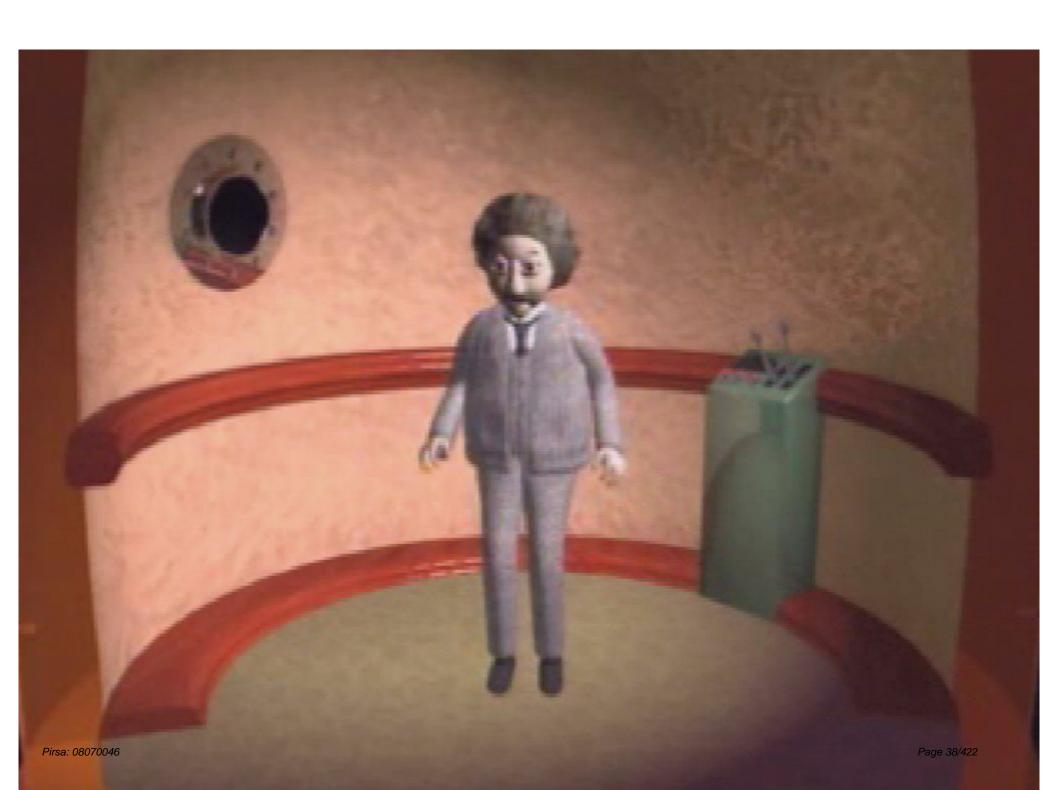




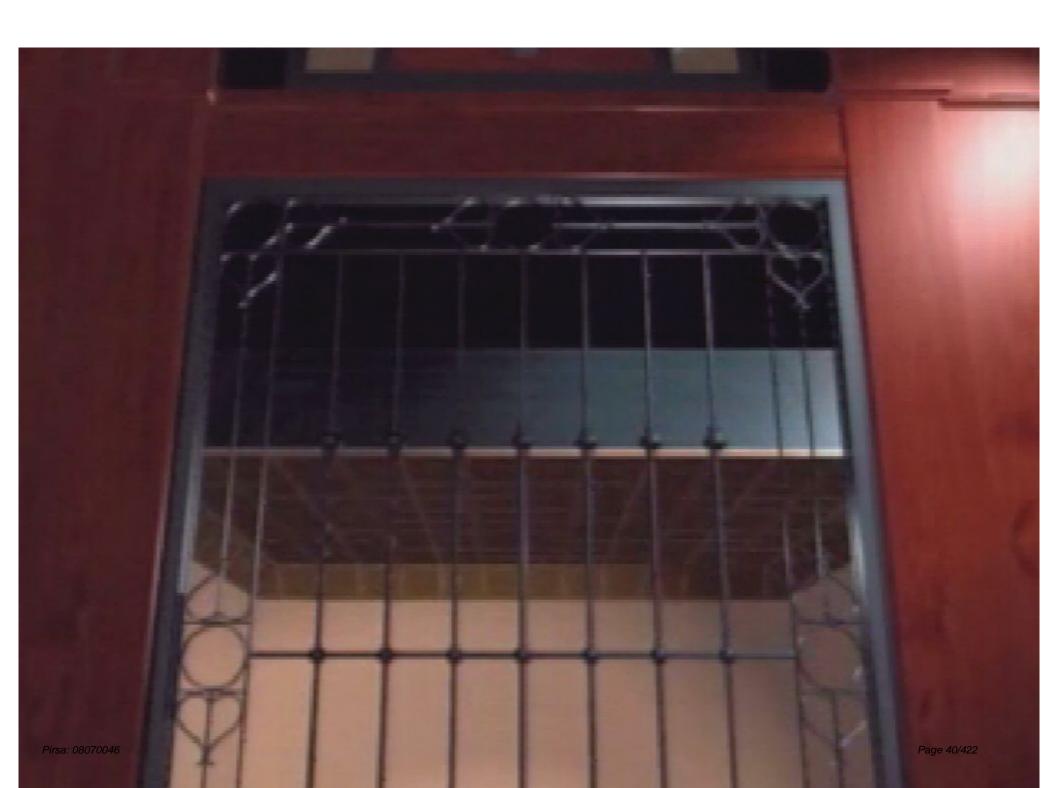


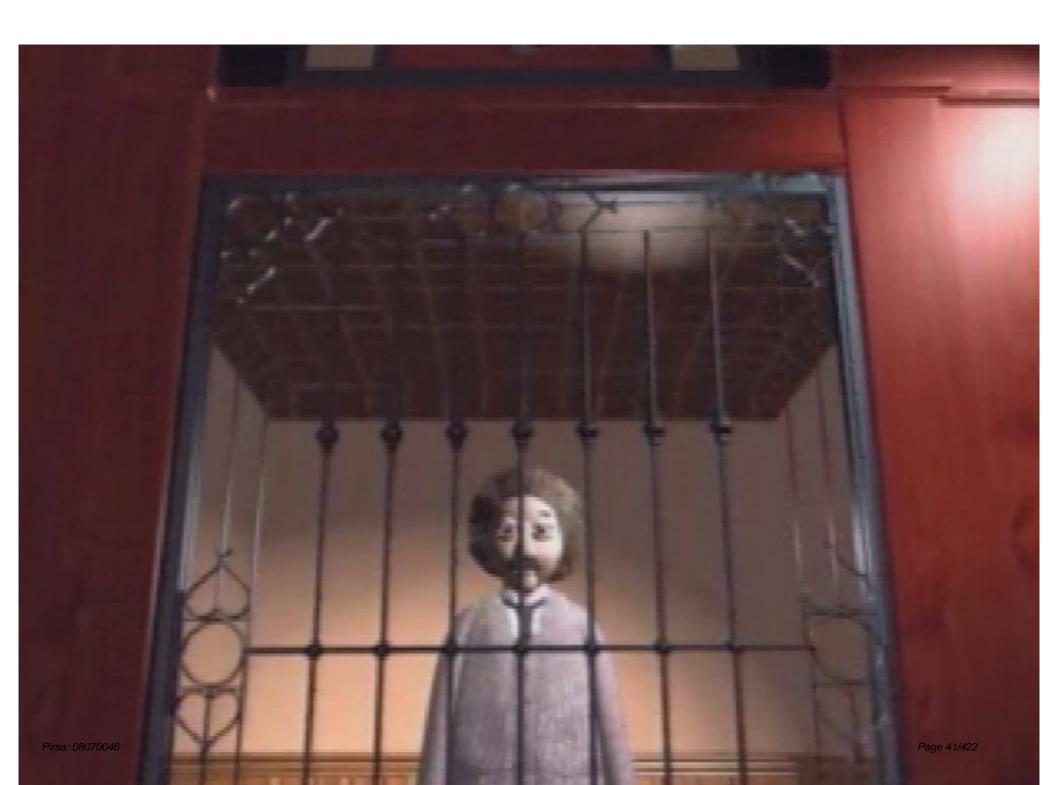


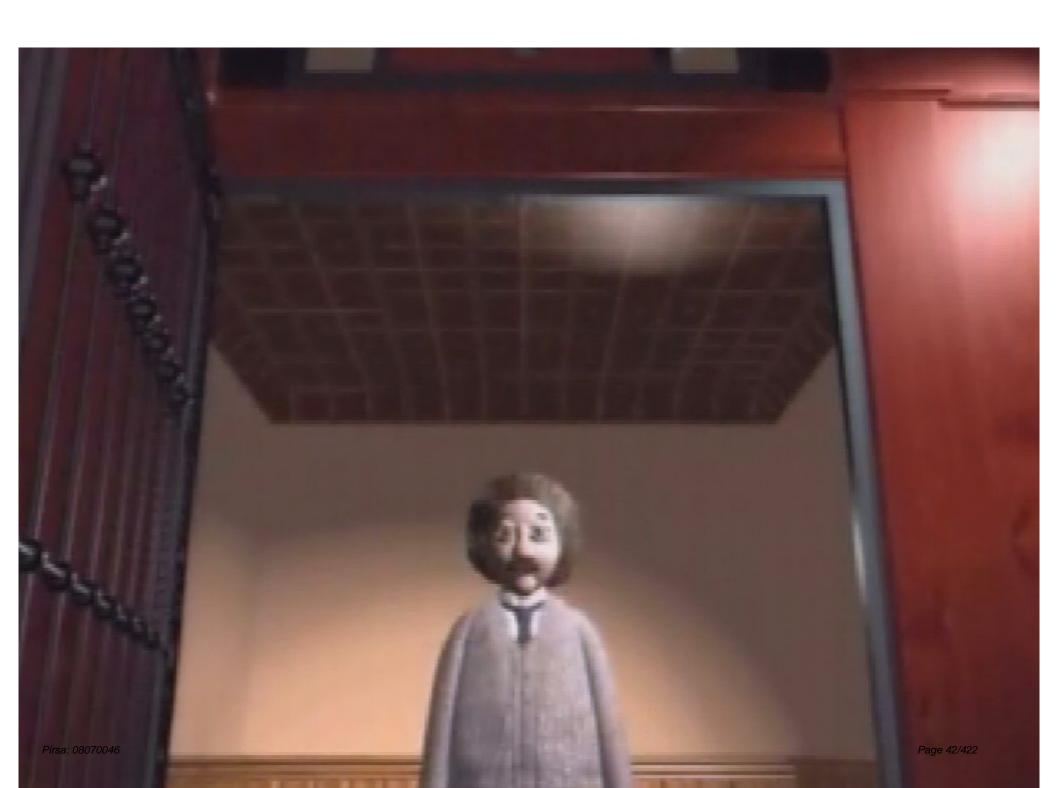




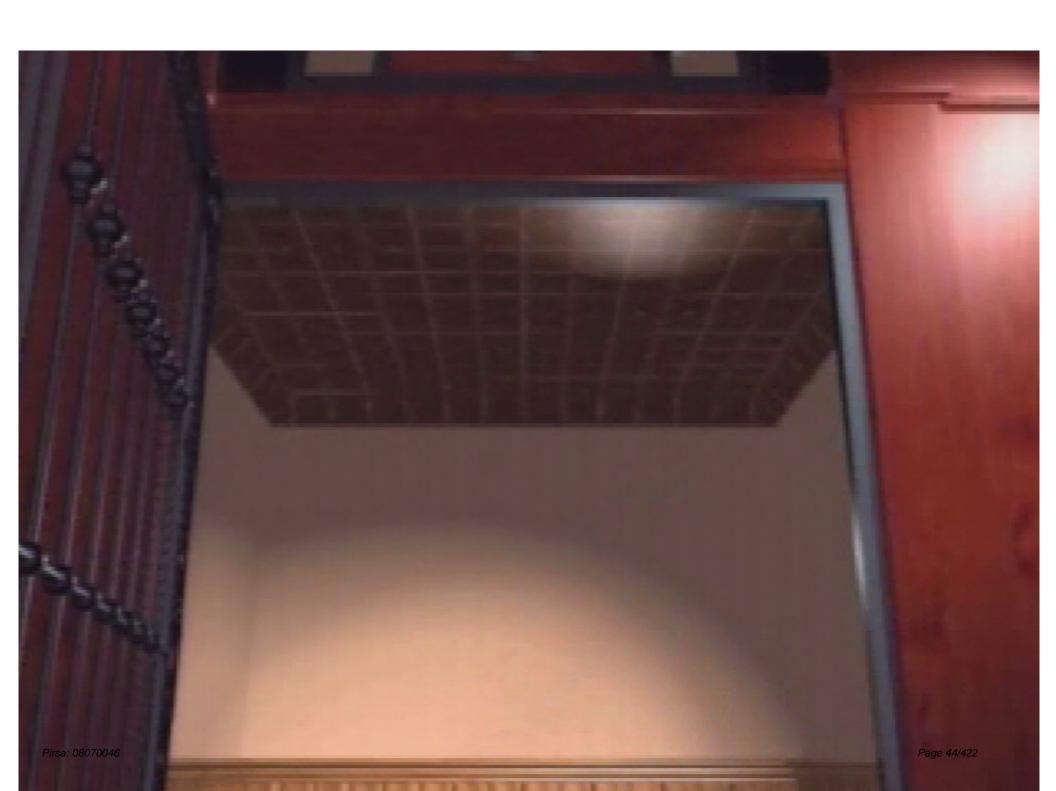










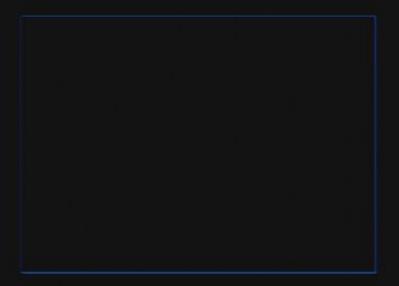


Pirsa: 08070046 Page 45/42:

Einstein's Equivalence Principle

 There is no experiment that you can perform that will distinguish these two diagrams

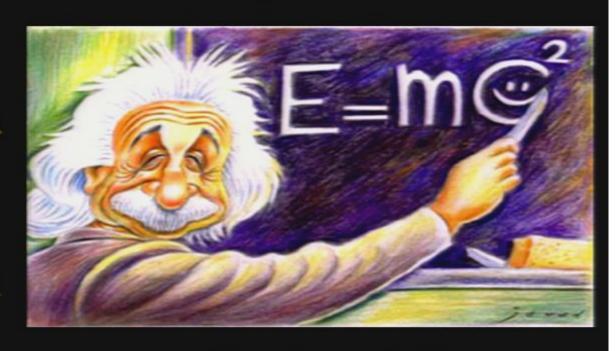




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The early 1900's changed he way gravity is looked at. Einstein didn't think of gravity as a force between objects, but as a curving of straight lines" due to mass. Light always follows these straight lines.

ime also slows down near nasses (space and time are different parts of spacetime", which is what gets bent).

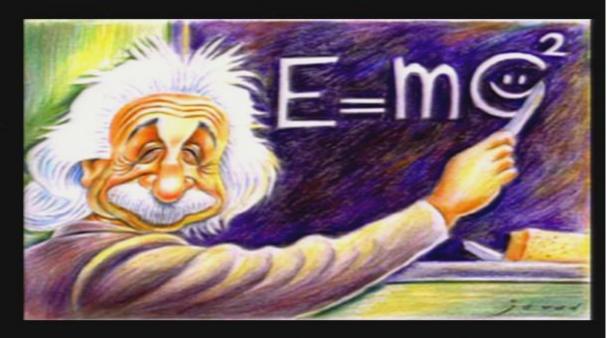


$$G_{uv} + \Lambda g_{uv} = 8\pi T_{uv}$$

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$$G_{uv} + \Lambda g_{uv} = 8\pi T_{uv}$$

$$f$$

$$Encodes$$

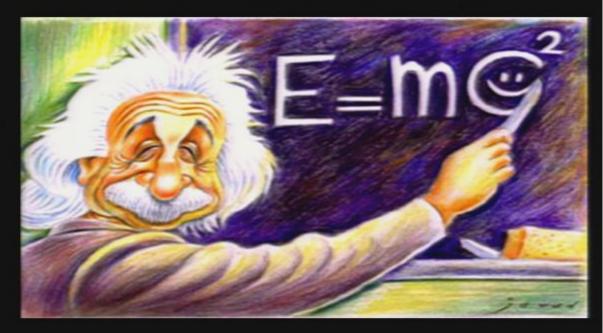
$$geometry$$

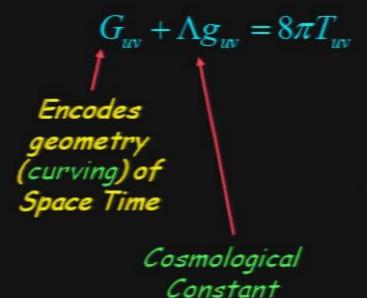
$$(curving) of$$

$$Space Time$$

The early 1900's changed he way gravity is looked at. Einstein didn't think of gravity as a force between objects, but as a curving of straight lines" due to mass. Light always follows these straight lines.

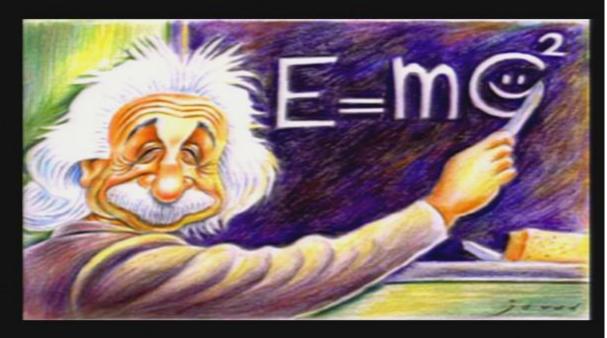
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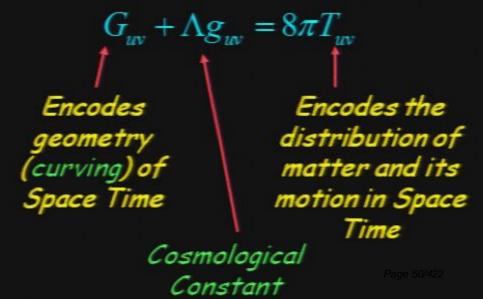




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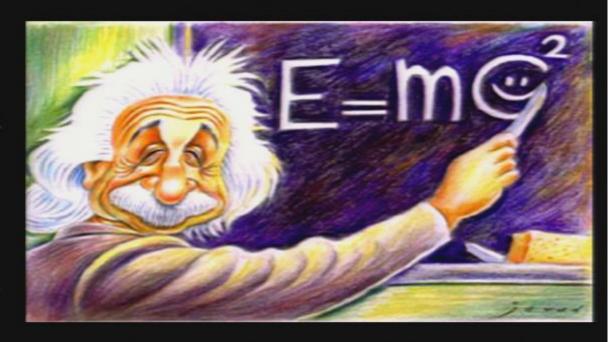
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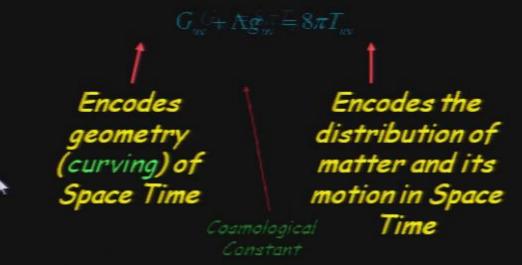




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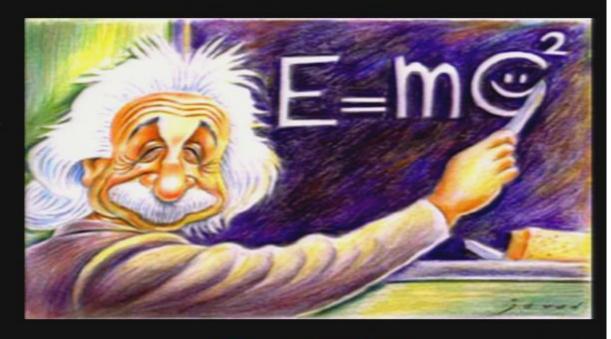




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 $G_{uv} = 8\pi T_{uv}$ Encodes
geometry
(curving) of
Space Time EncodesEncodes the
distribution of
matter and its
motion in Space
Time

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Generally speaking, Einstein field equation: 6_{μν} = 8πT_{μν}

is coupled elliptic-hyperbolic nonlinear partial differential equations for the metric components.

· Just so that we are clear on definitions:

Pirsa: 08070046 Page 53/422

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Pirsa: 08070046 Page 54/422

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Pirsa: 08070046 Page 55/422

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"nonlinear" - dependent on nonlinear function of metric components

Pirsa: 08070046 Page 56/422

• Generally speaking, Einstein field equation: $G_{\mu\nu} = 8\pi T_{\mu\nu}$

is coupled elliptic-hyperbolic nonlinear partial differential equations for the metric components.

- · Just so that we are clear on definitions:
- "coupled" each differential equation contains multiple terms; equations cannot be solved individually.
- "elliptic-hyperbolic" determinants of sub-matrices of the system of equations matrix are either positive or negative; never zero.
- "nonlinear" dependent on nonlinear function of metric components
- "partial differential equation" an equation containing partial derivatives of functions, for example $\partial^2 f(x,y,z)/\partial x \partial y$

Pirea: 08070046

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- "nonlinear" dependent on nonlinear function of metric components
- "partial differential equation" an equation containing partial derivatives of functions, for example $\partial^2 f(x,y,z)/\partial x \partial y$
- "metric components" components of the metric tensor $g_{\mu\nu}$

Let's Review

54723M3

-

Let's Review



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Let's Review



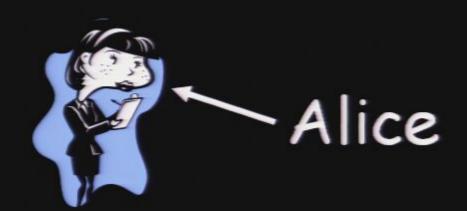
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Space Diagram Bob

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Alice's twin sister, Alice



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 $d_A = 10$ metres



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 $d_A = 10$ metres



$$t_{A} = 0$$





 $d_A = 10$ metres



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 $d_A = 10 \text{ metres}$



$$t_A = 5 sec$$

$$t_A = 5 sec$$





 $d_A = 10$ metres



$$t_A = 5 sec$$

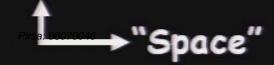
$$t_A = 5 sec$$

Question: How much time has elapsed for Bob? 2007022

Draw a "Spacetime Diagram"



Draw a "Spacetime Diagram"

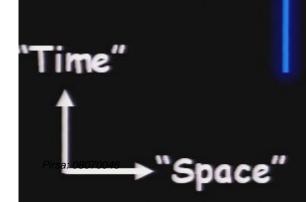


A ("at rest")



A ("at rest")

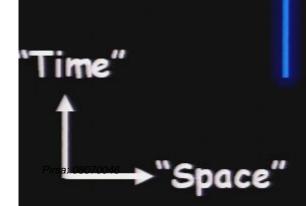
A' (at rest relative to A)



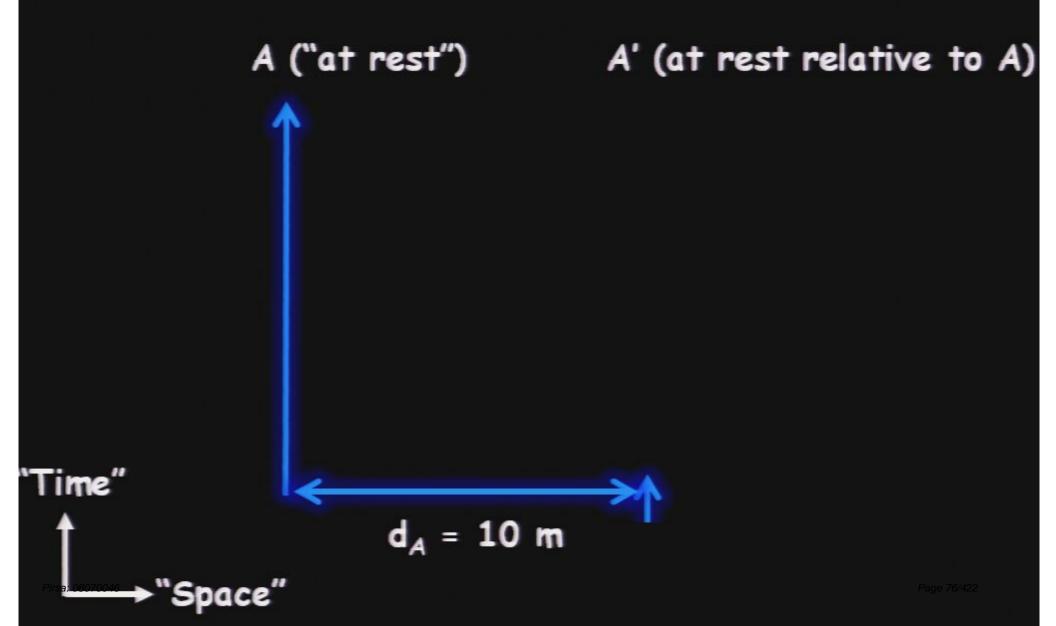
 $d_A = 10 \text{ m}$

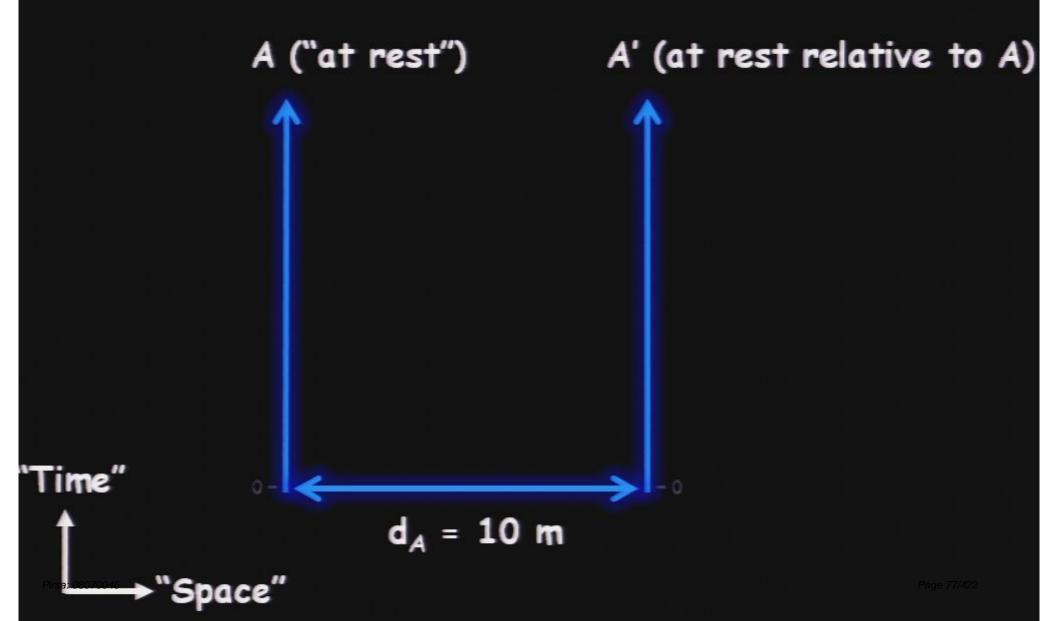
A ("at rest")

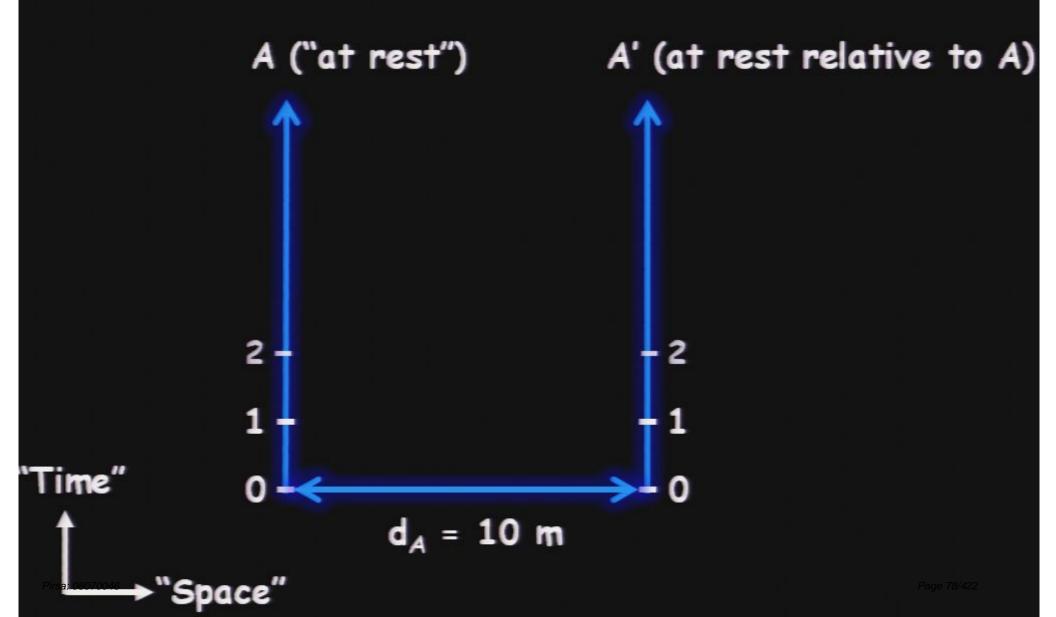
A' (at rest relative to A)

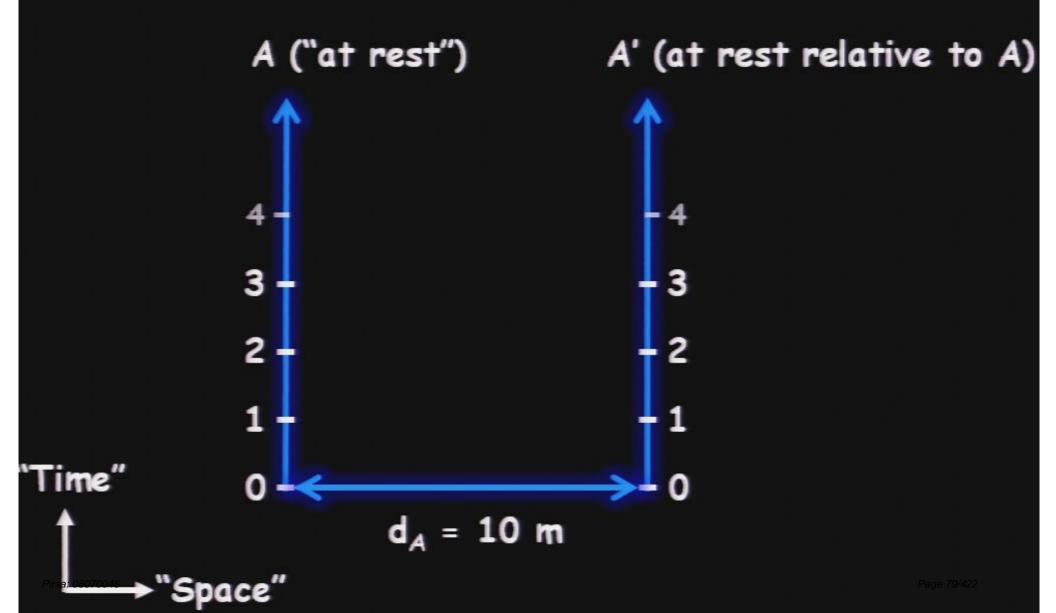


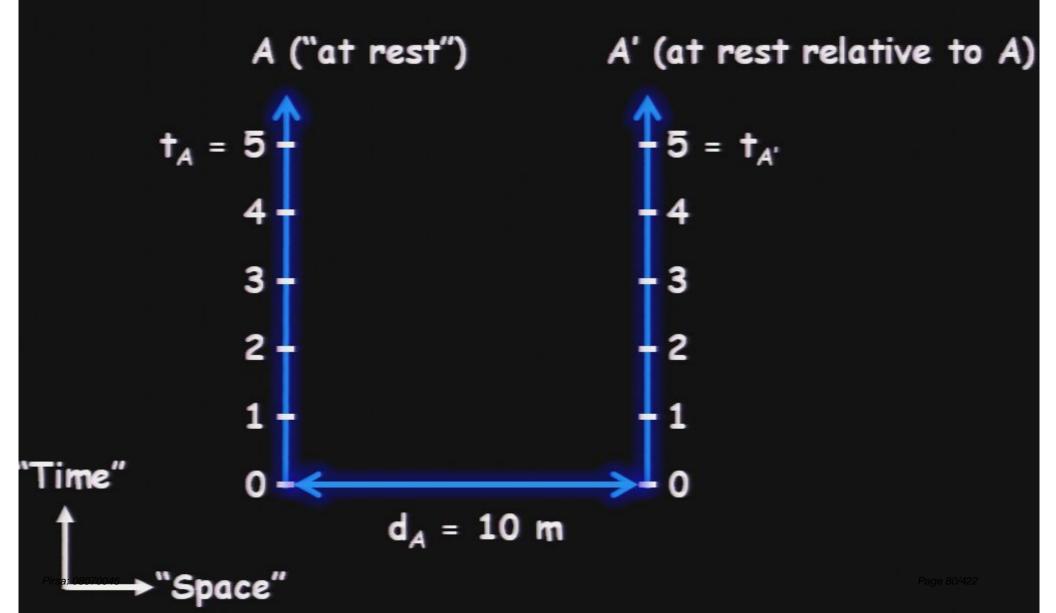
$$d_A = 10 \text{ m}$$

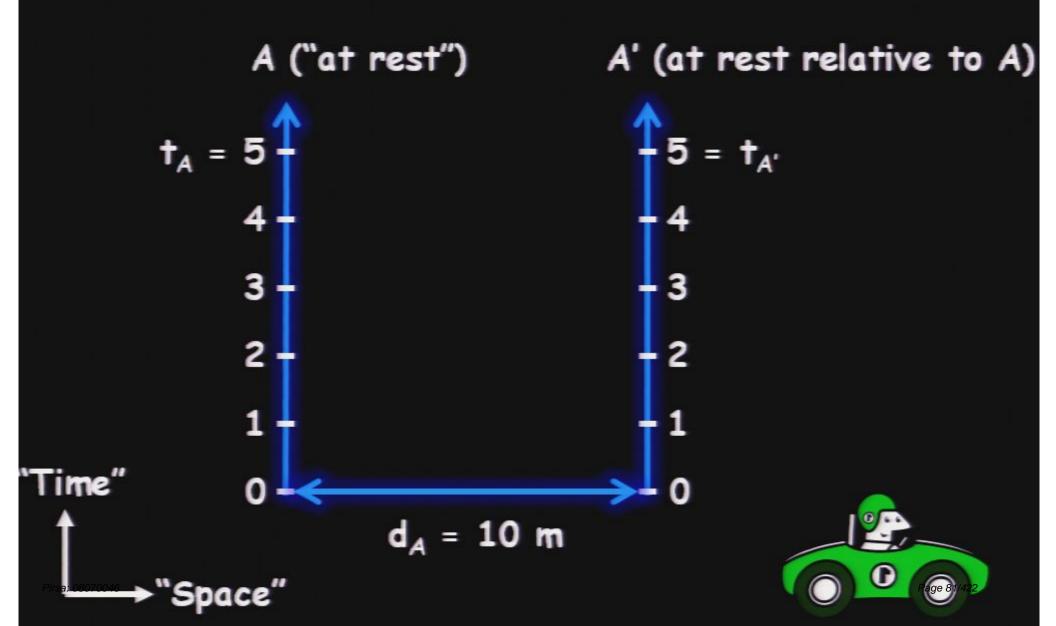


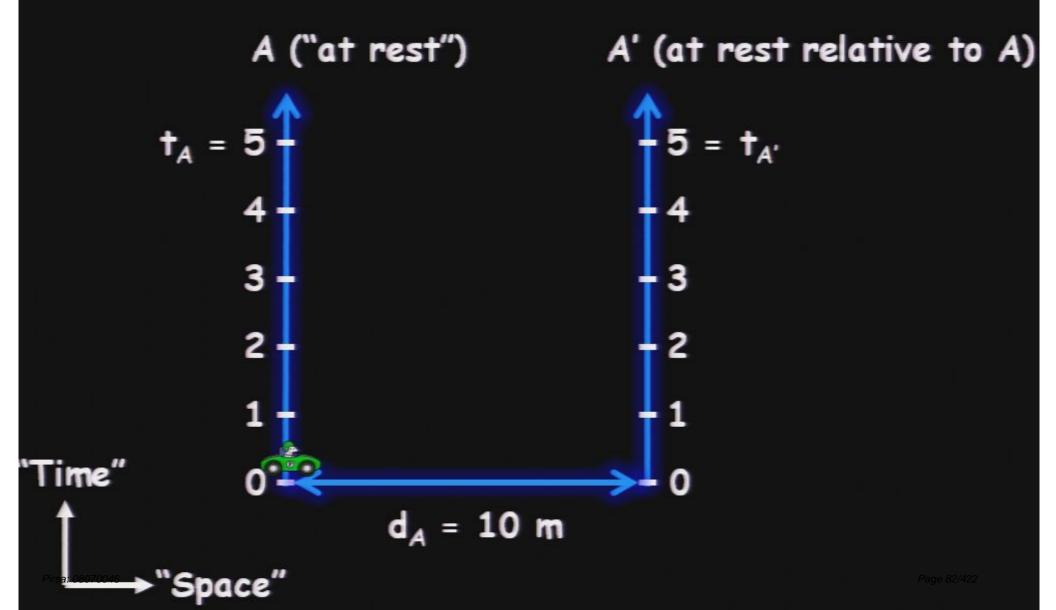


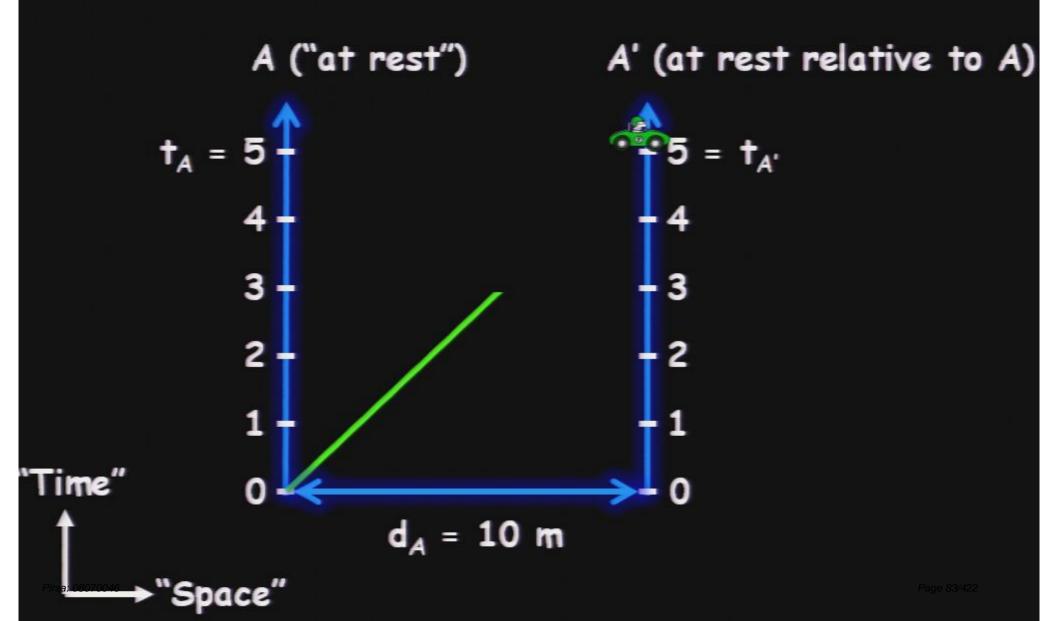


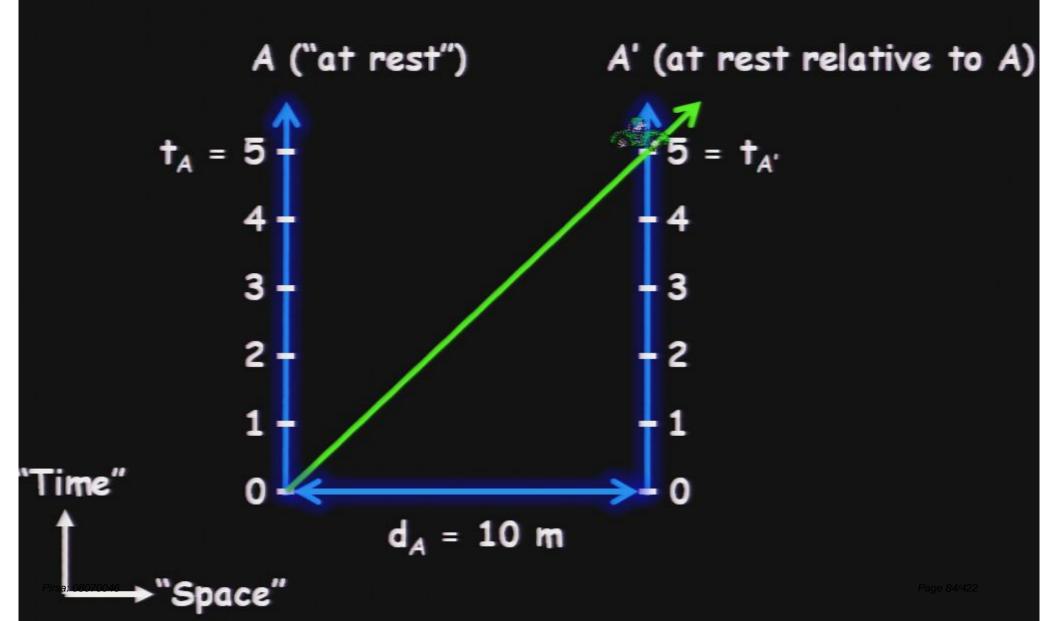


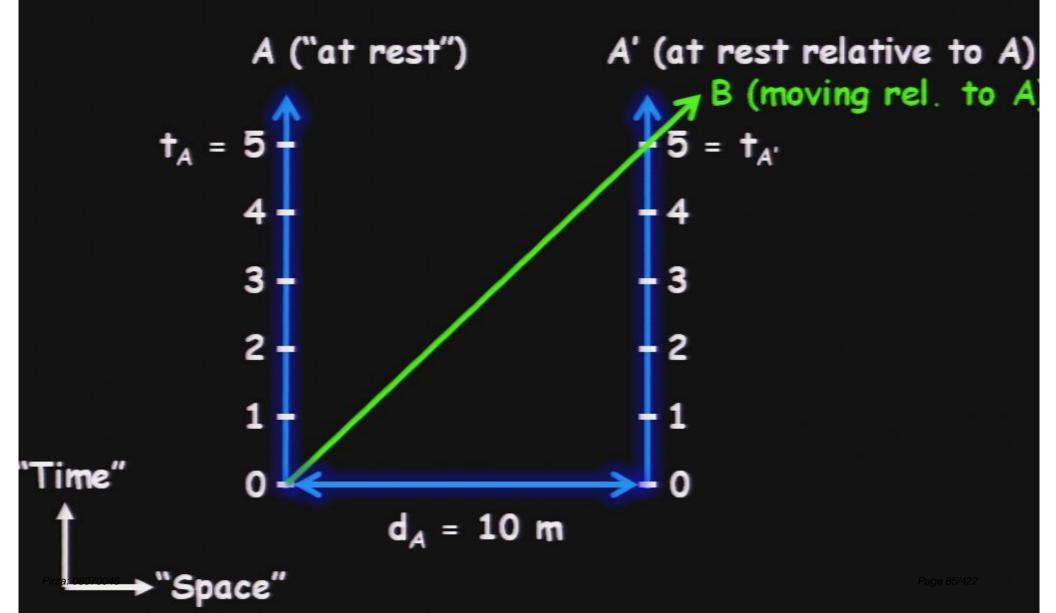


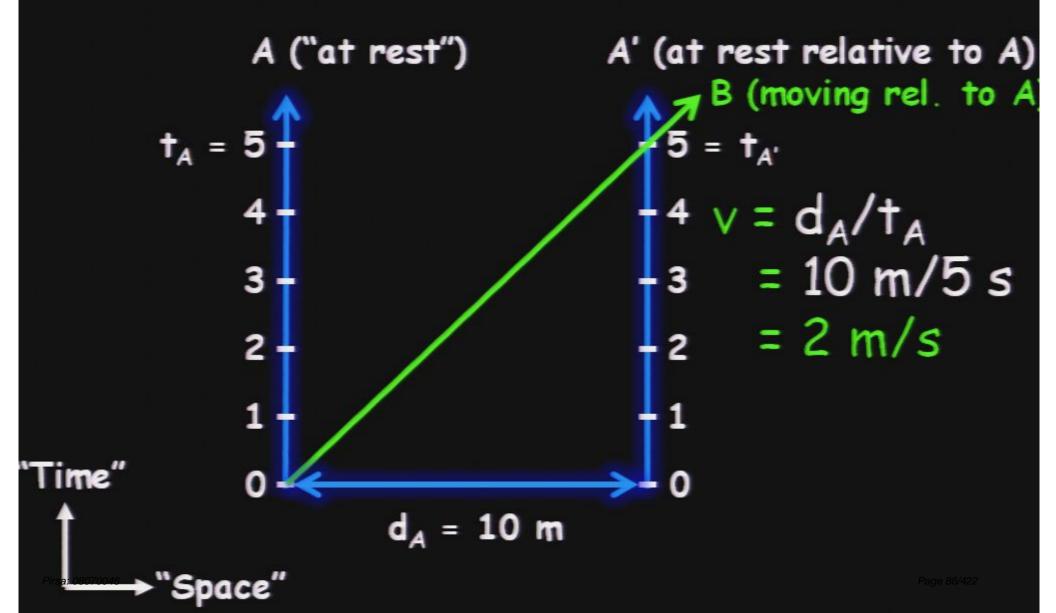












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Let's Have Spacetime Fun!

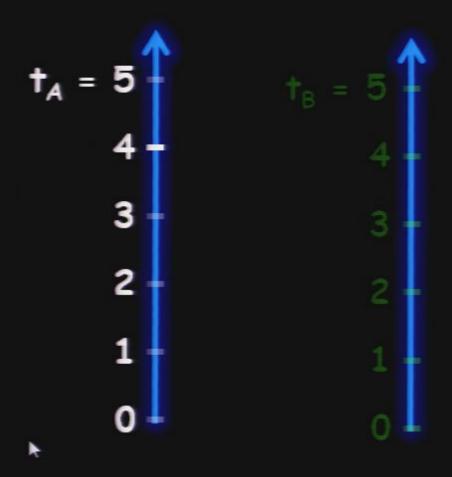
Sketch spacetime diagrams for each:

- 1: Bob at rest relative to Alice
- 2: Alice tossing a baseball up
- 3: Bob moving Fast
- 4: Bob moving Slow
- 5: The Earth orbiting about the Sun

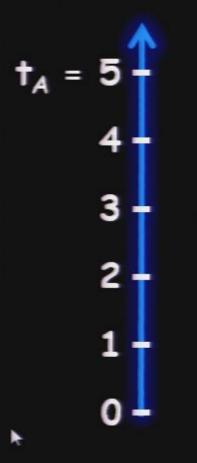
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Bob at rest relative to Alice



Bob at rest relative to Alice

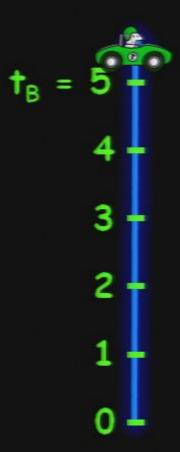


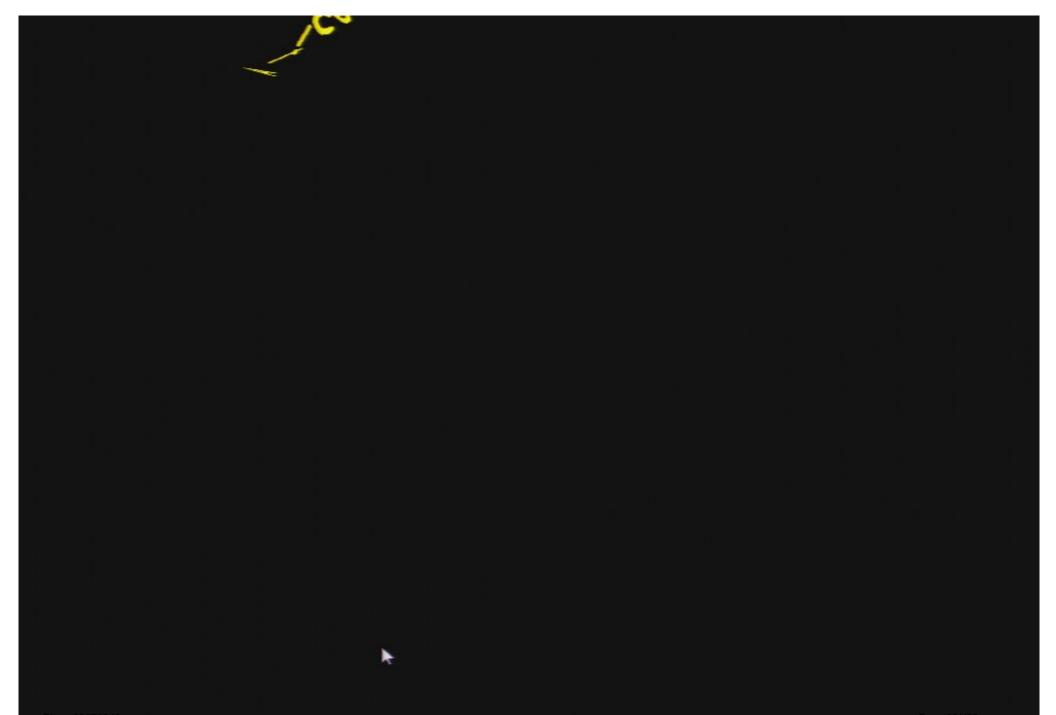


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Bob at rest relative to Alice









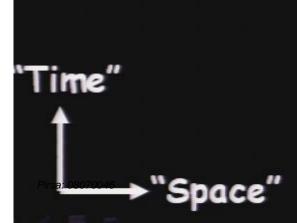


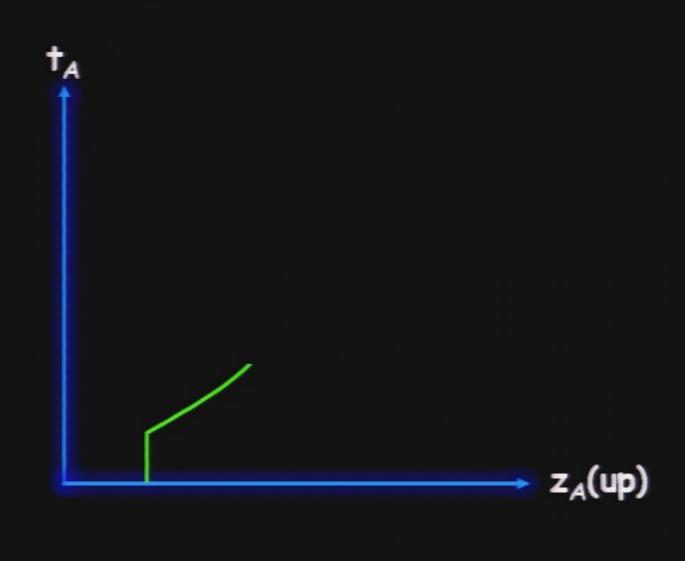


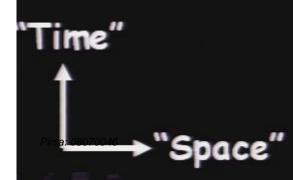


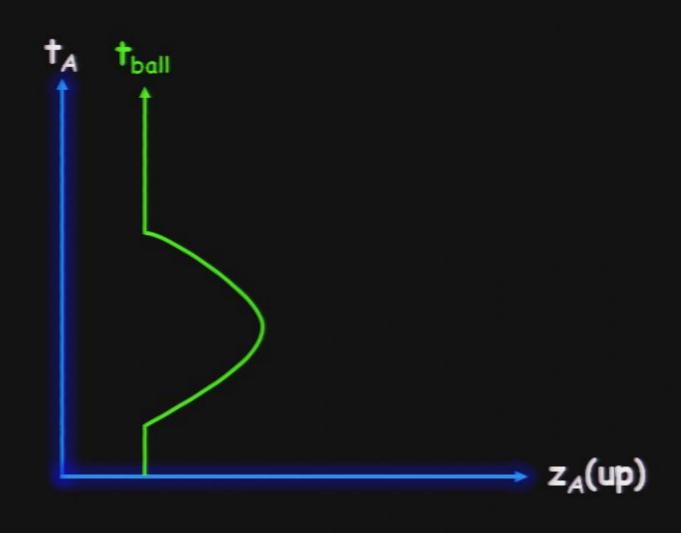


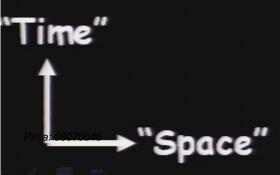


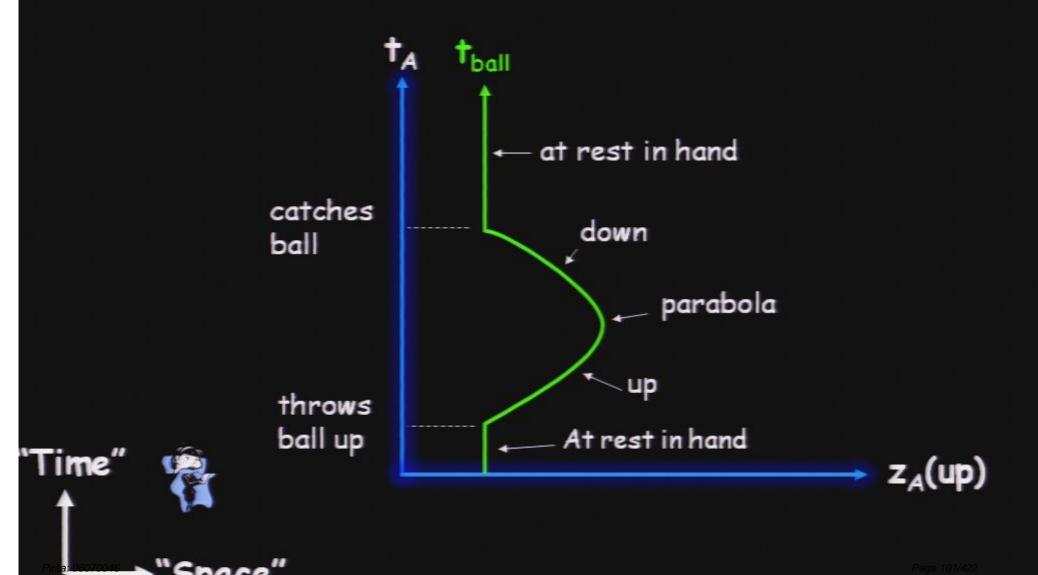


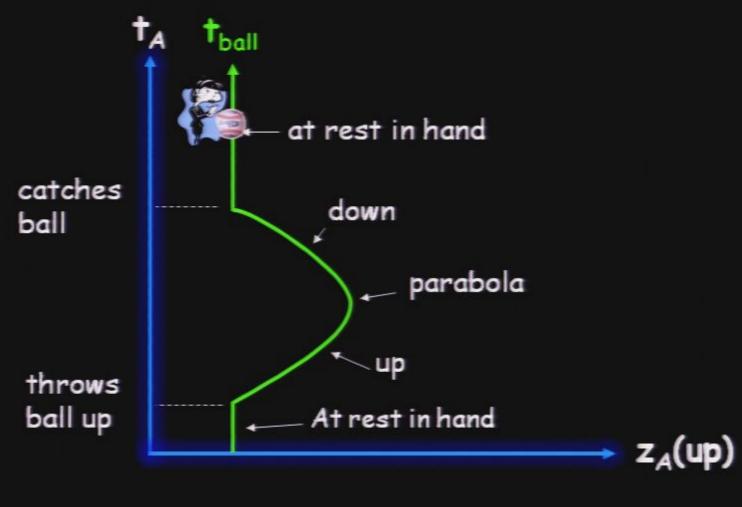






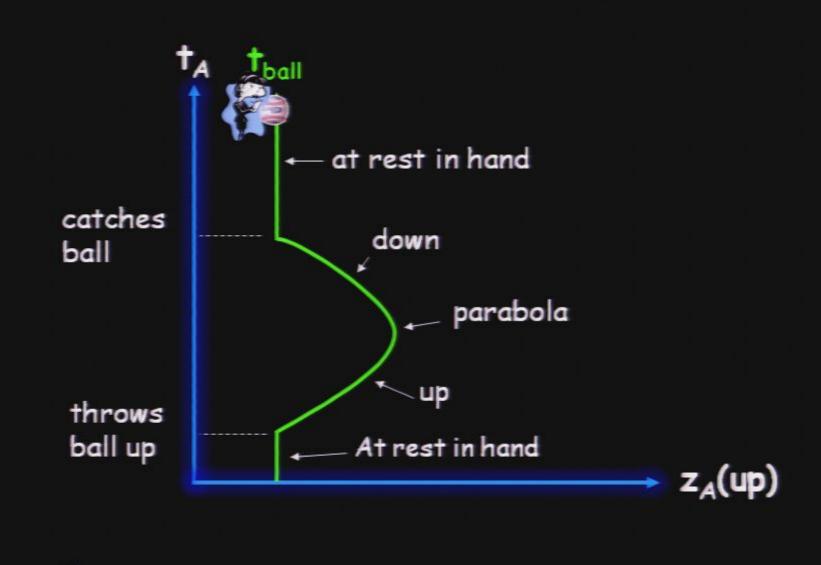






Time"

Space

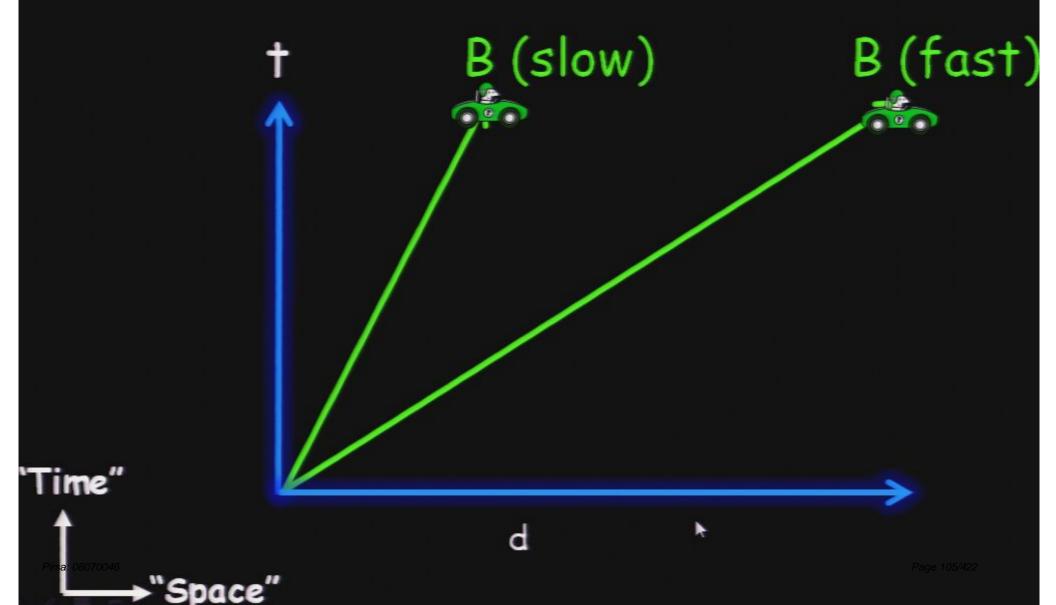


Bob Moving Fast and Slow



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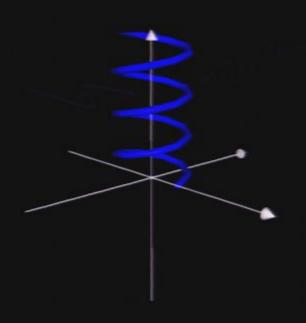
Bob Moving Fast and Slow



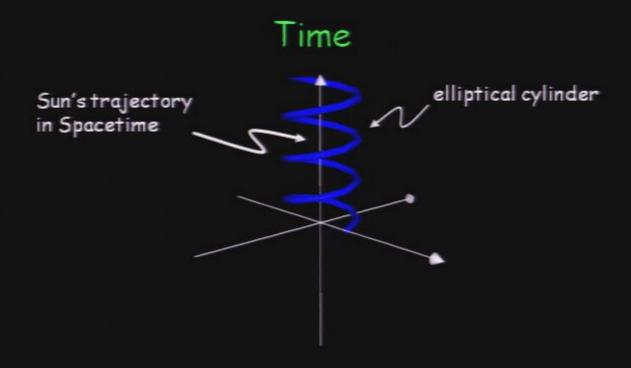
Earth Orbiting the Sun

irsa: 08070046 Page 106/422

Earth Orbiting the Sun



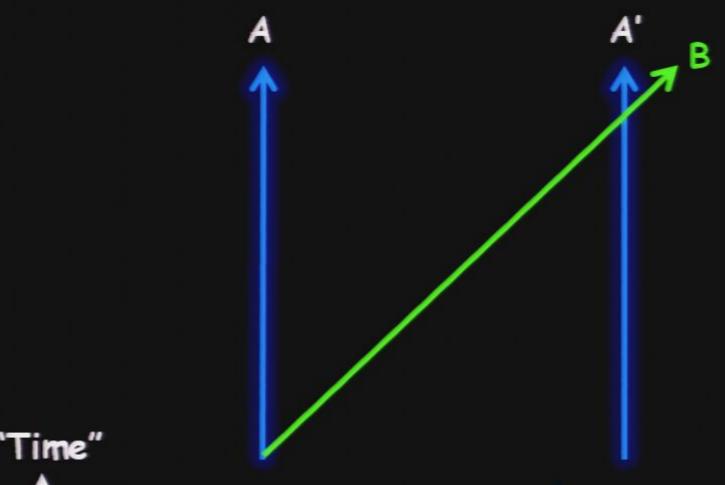
Earth Orbiting the Sun



Earth's Trajectory

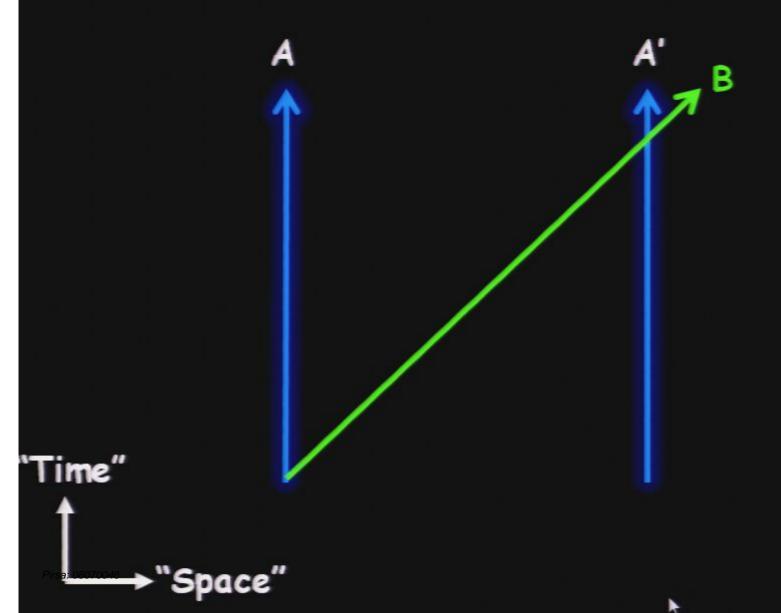
Back to Bob and Alice

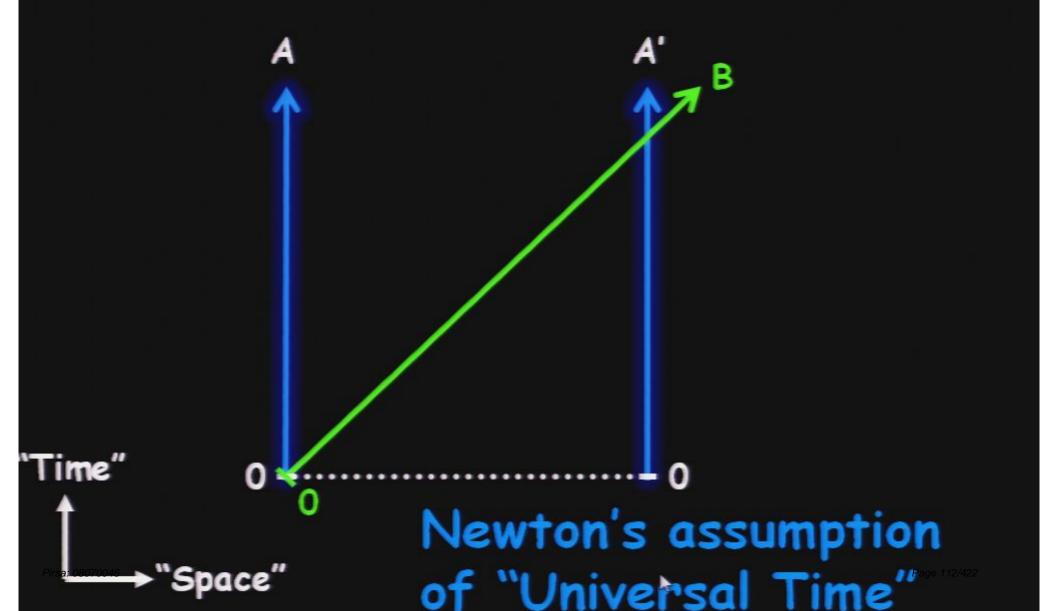
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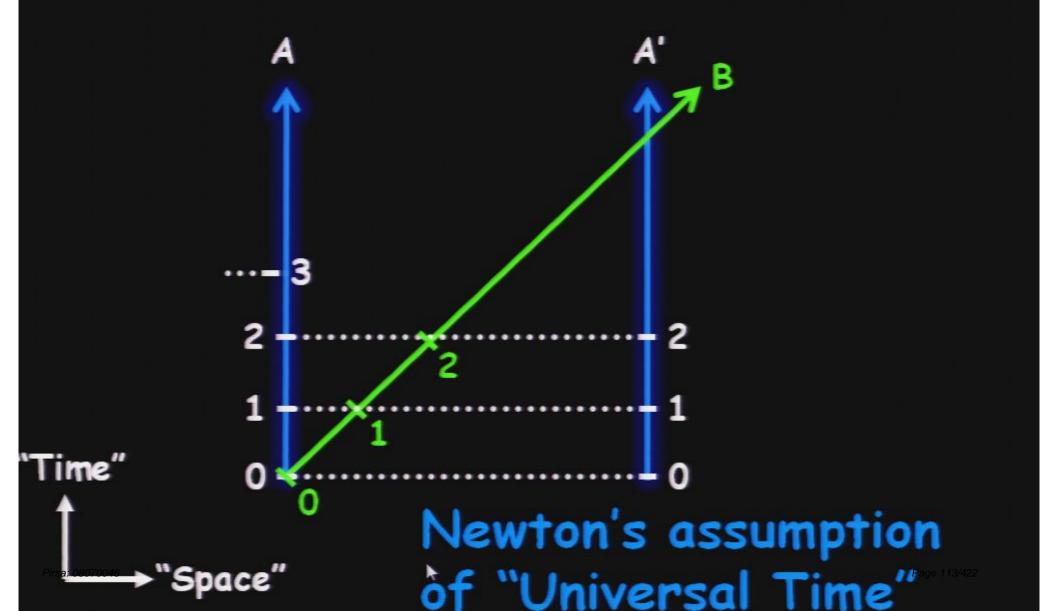


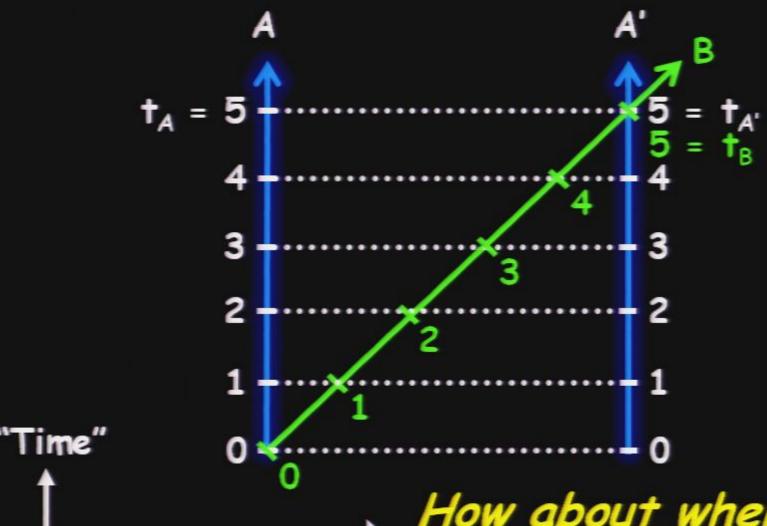
Space

How do we indicate the ticking of B's clock?



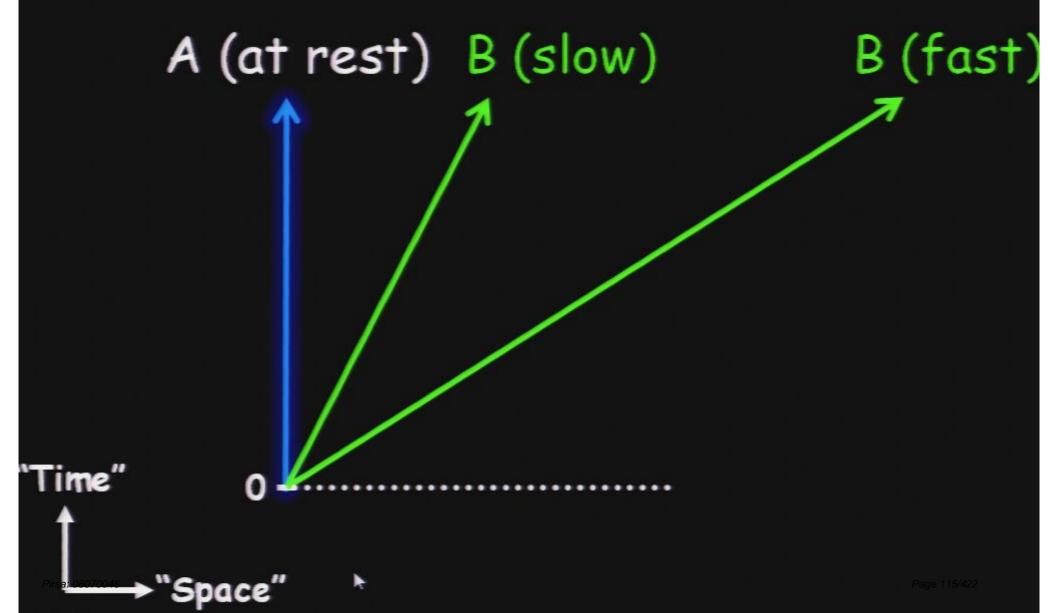


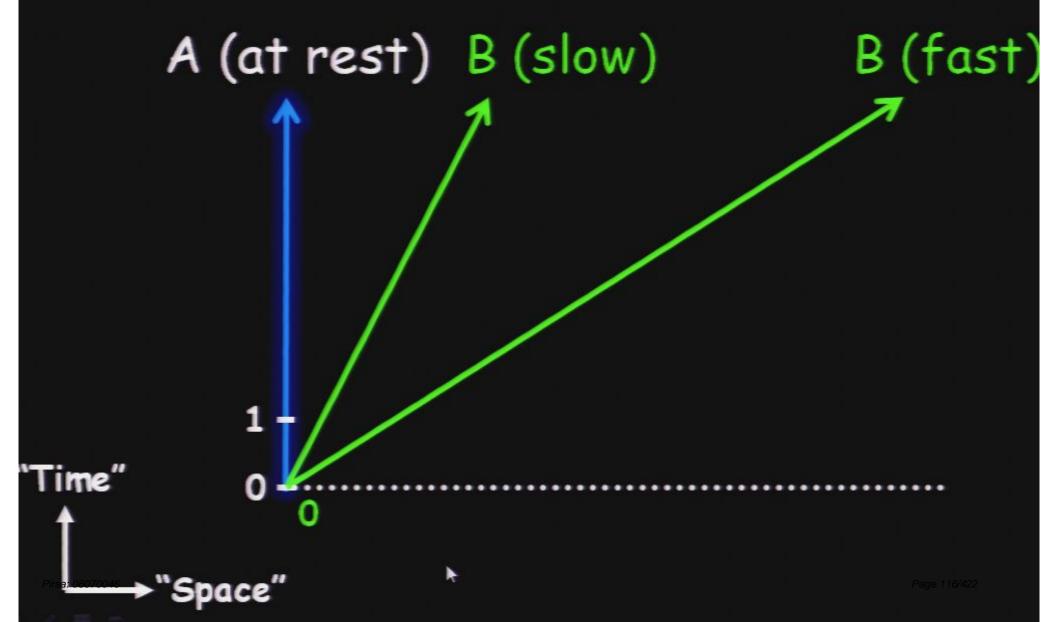


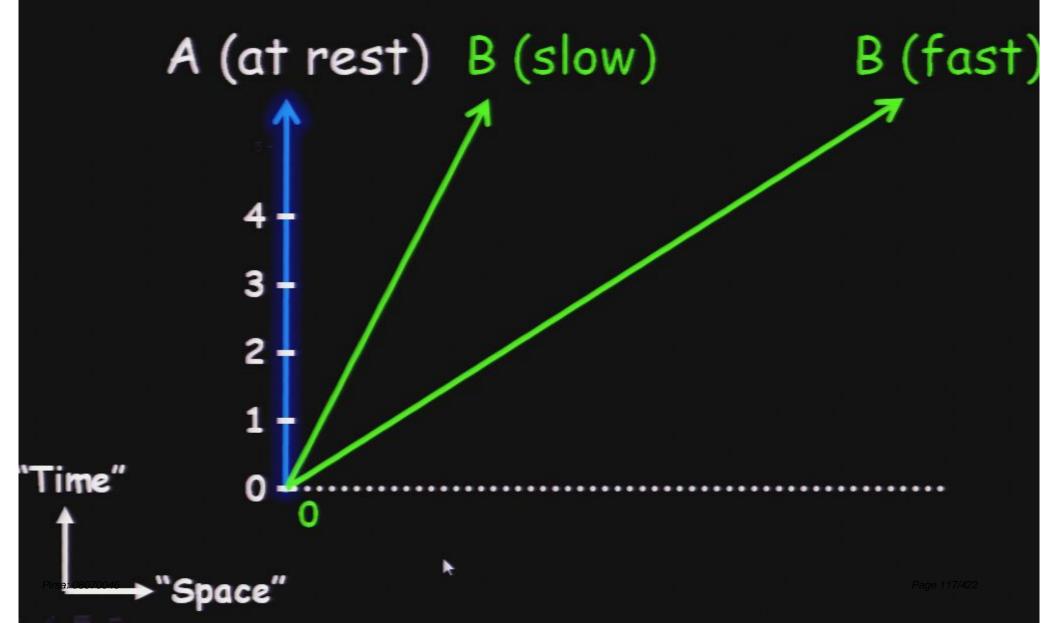


Space

, How about when Bob is travelling at different speeds

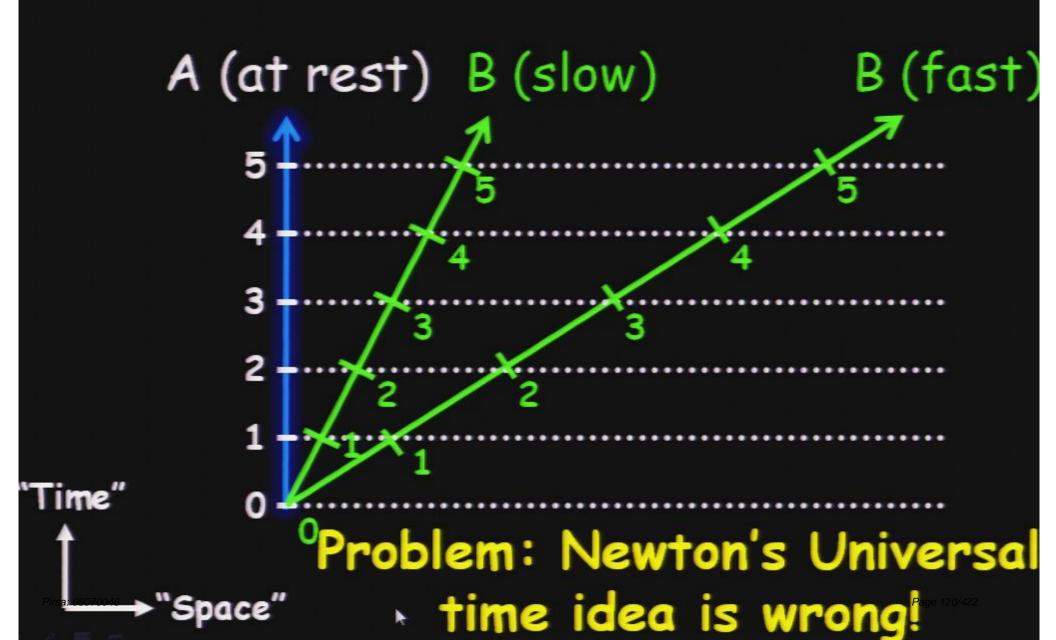


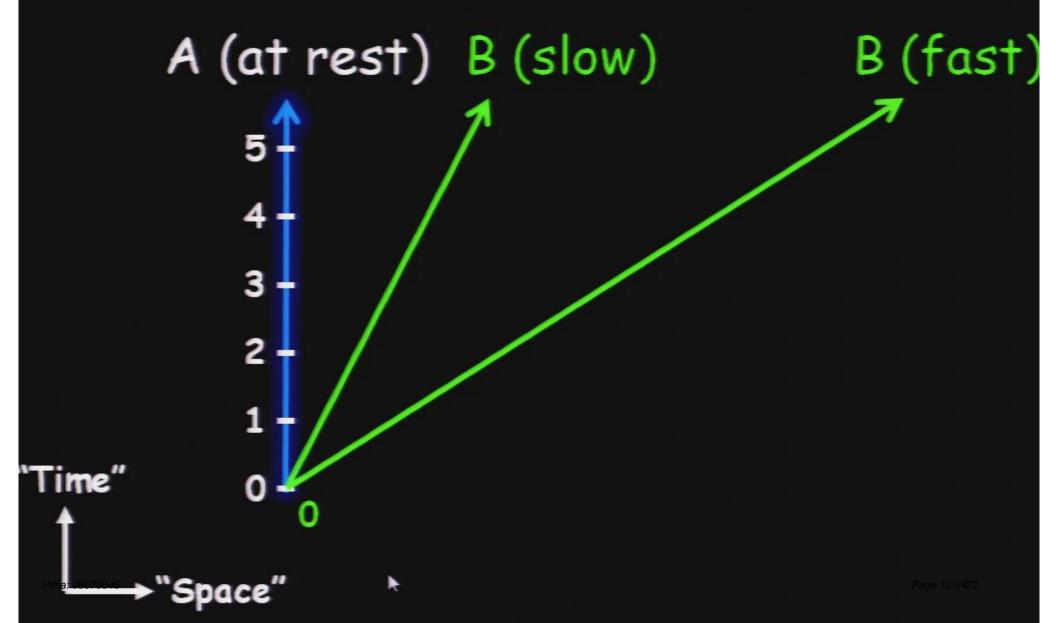


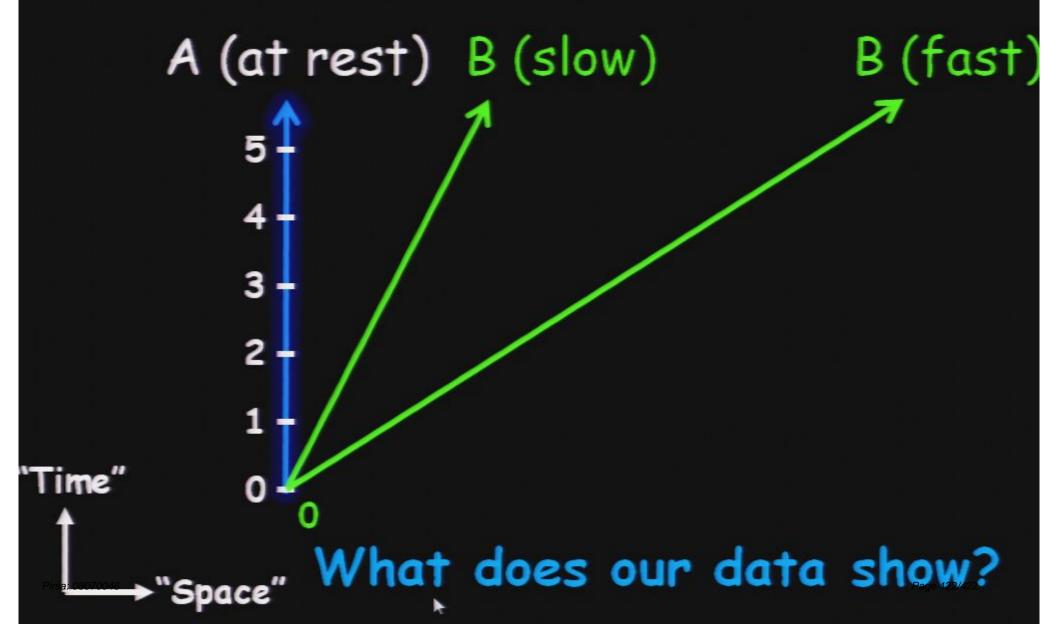


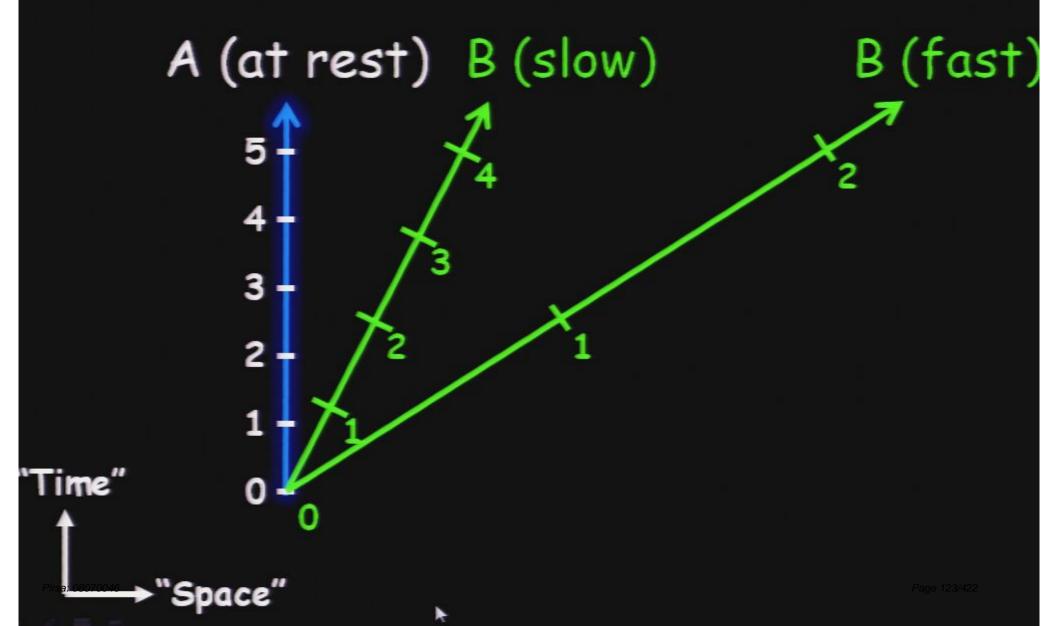


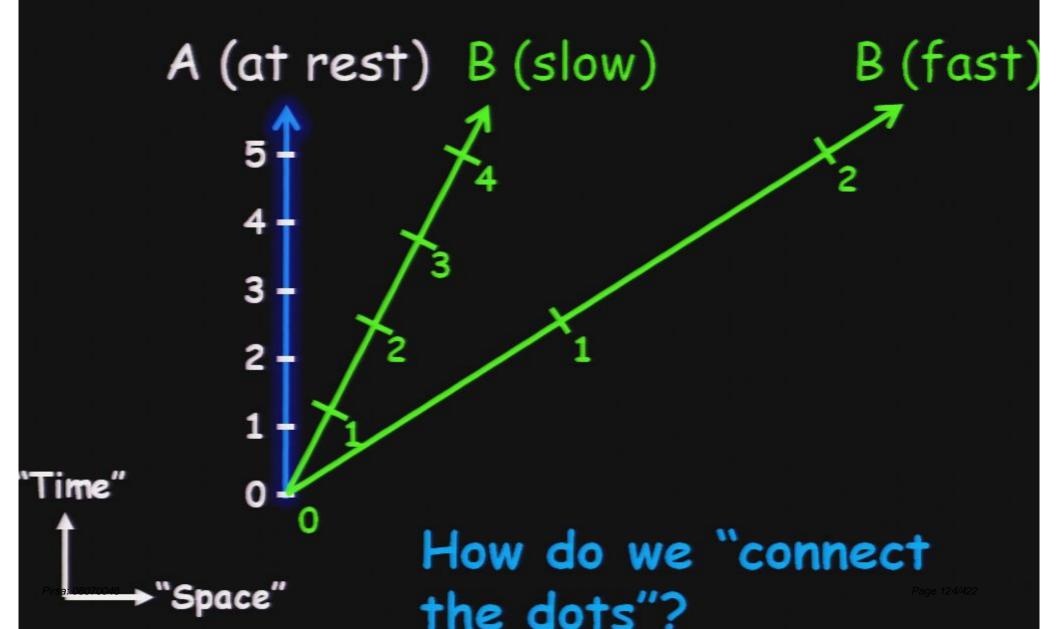


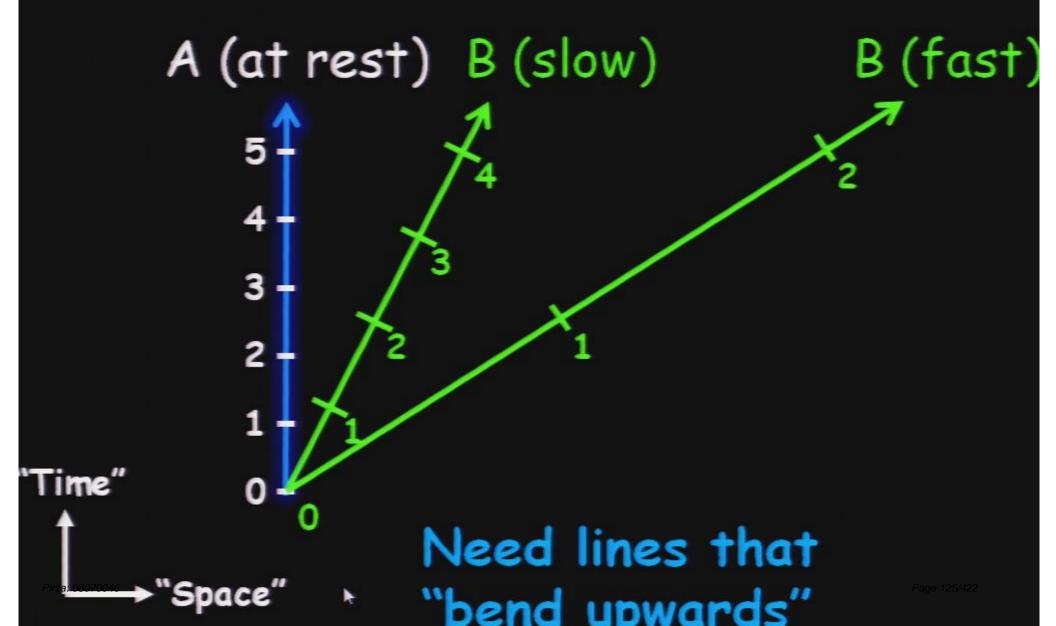


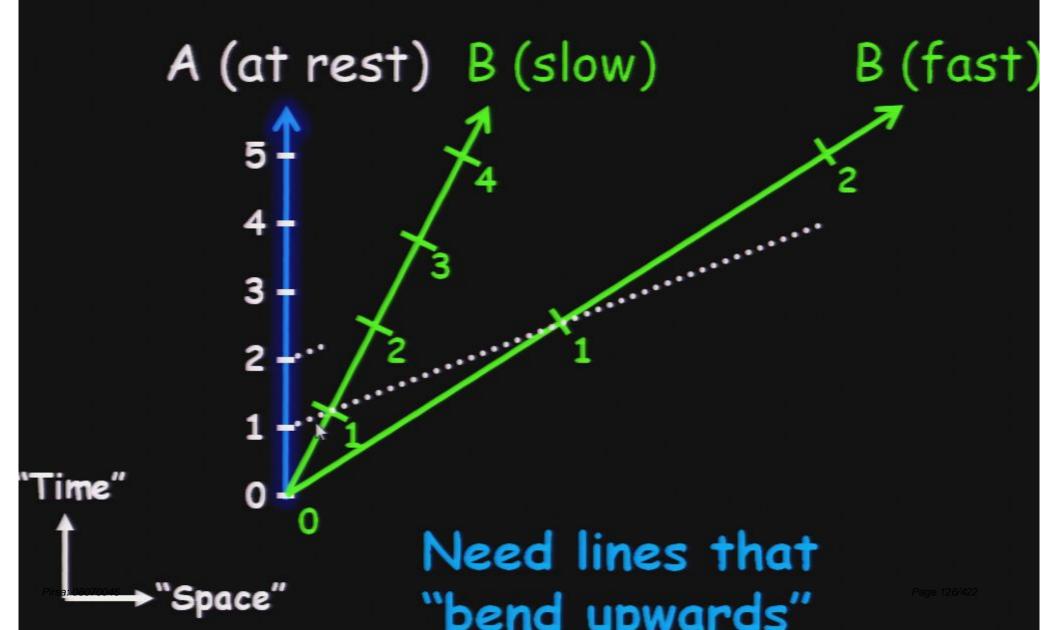


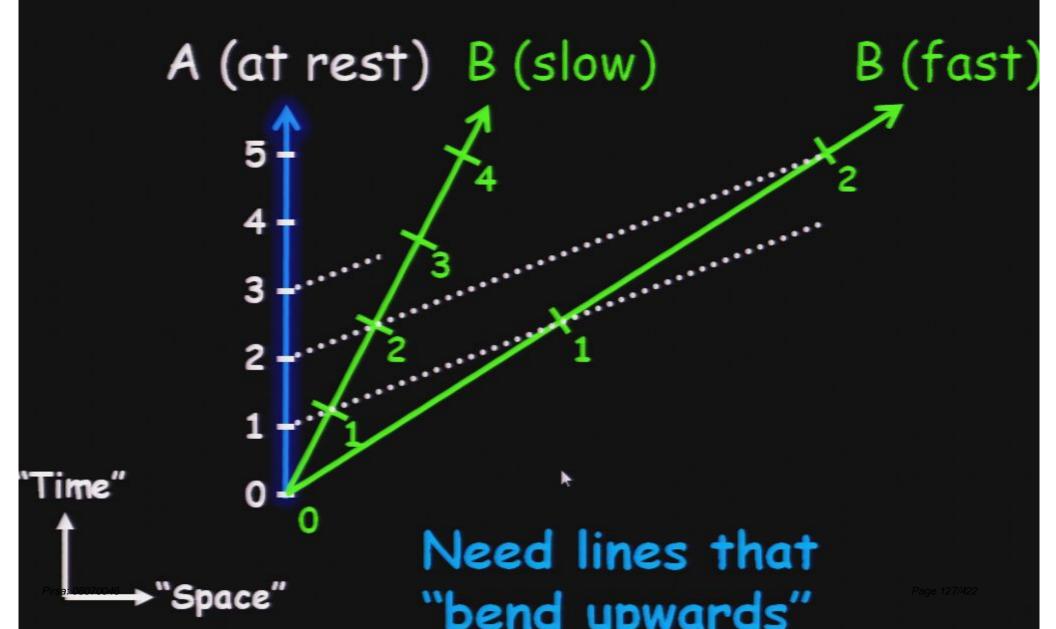


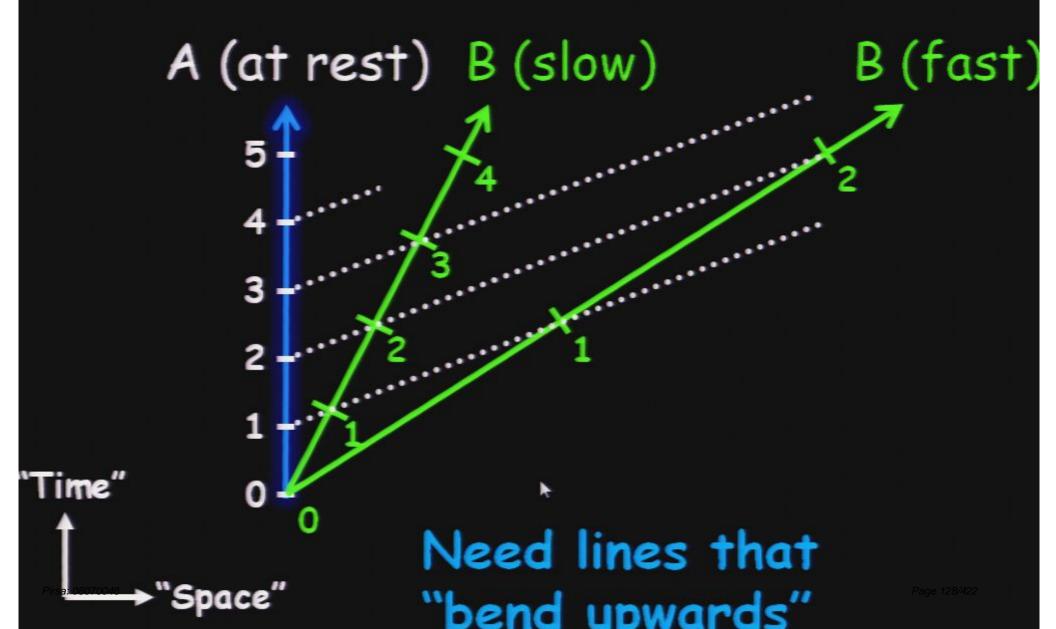


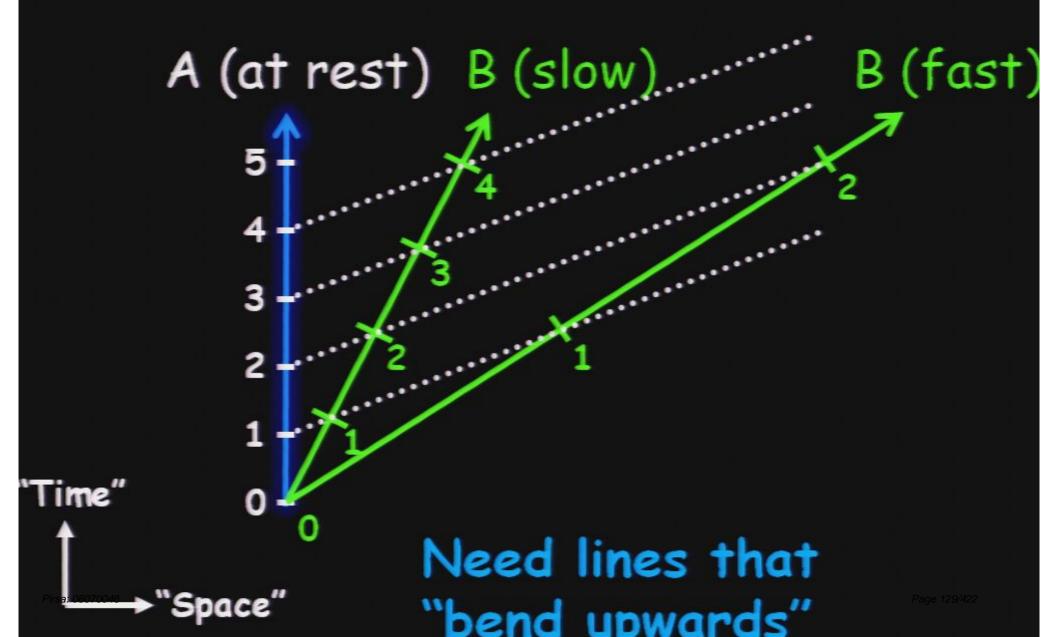


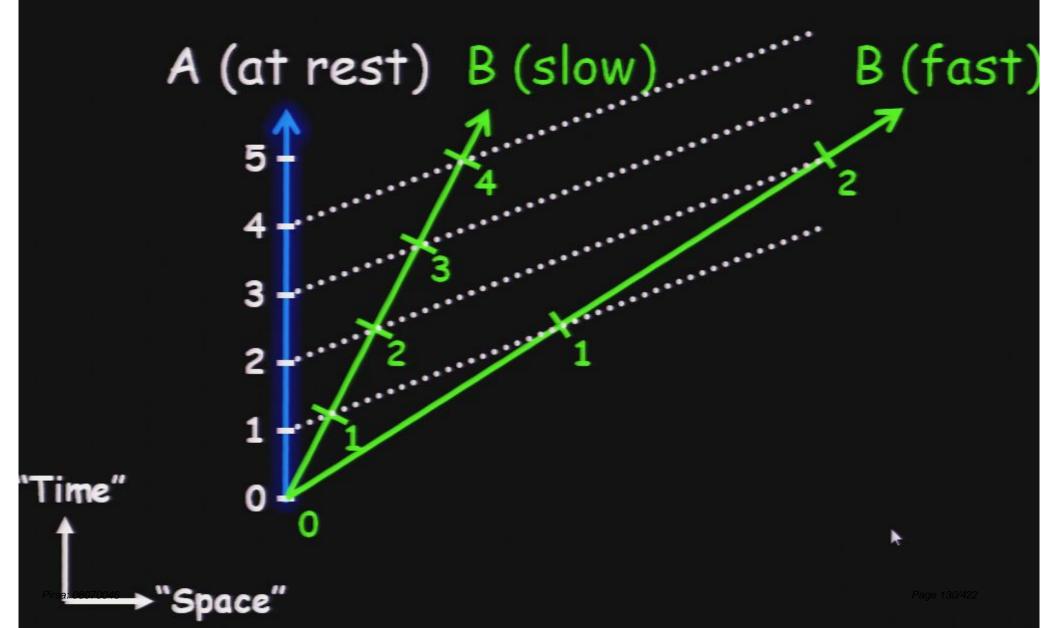


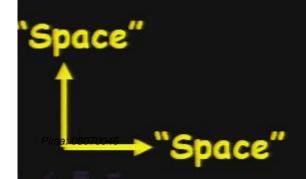






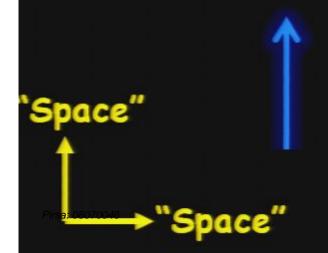






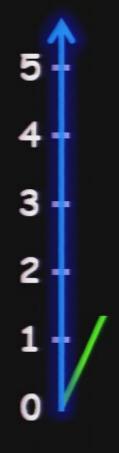


A (walking N)





A (walking N)

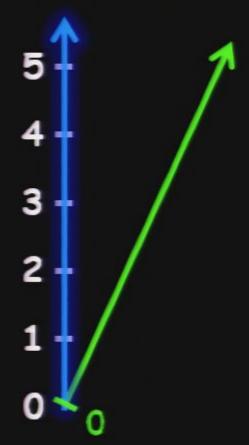


'Space"

B (walking NE)



A (walking N)



B (walking NE)

How do we transfer A's tick marks?



A (walking N)



B (walking NE)

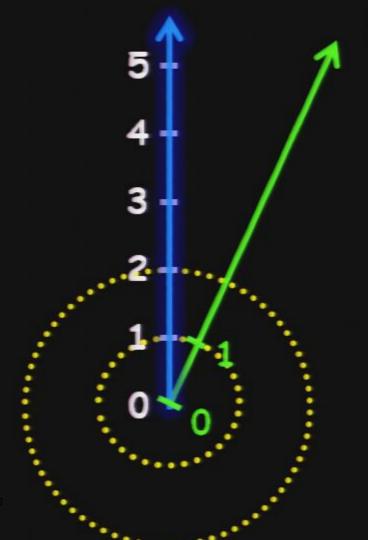
How do we transfer A's tick marks?

Let's Try CIRCLES



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A (walking N)

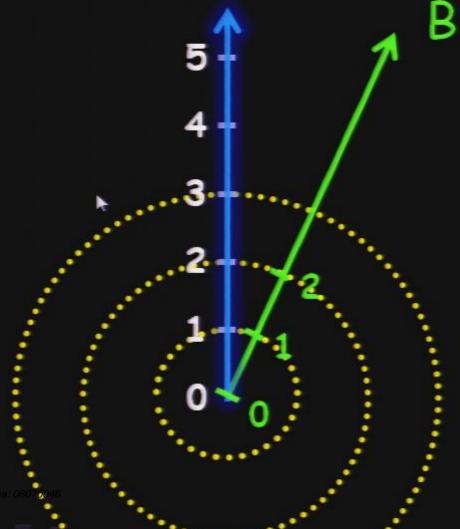


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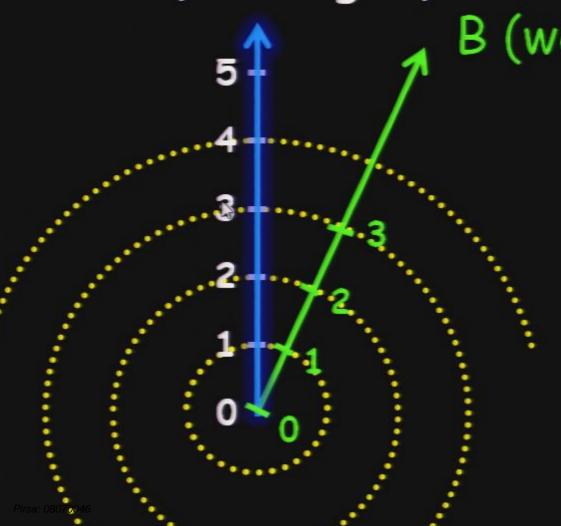


B (walking NE)

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A (walking N)

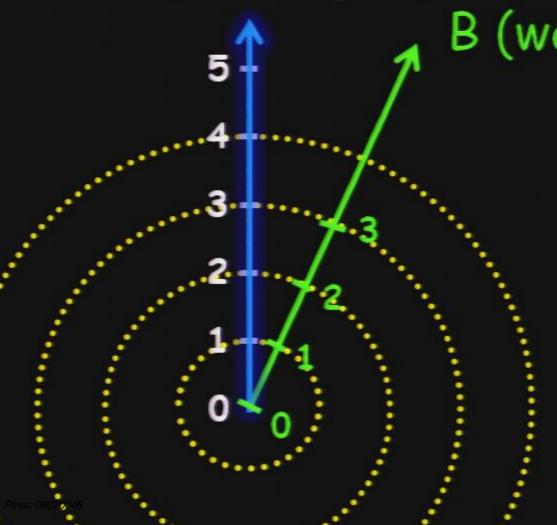


B (walking NE)

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A (walking N)

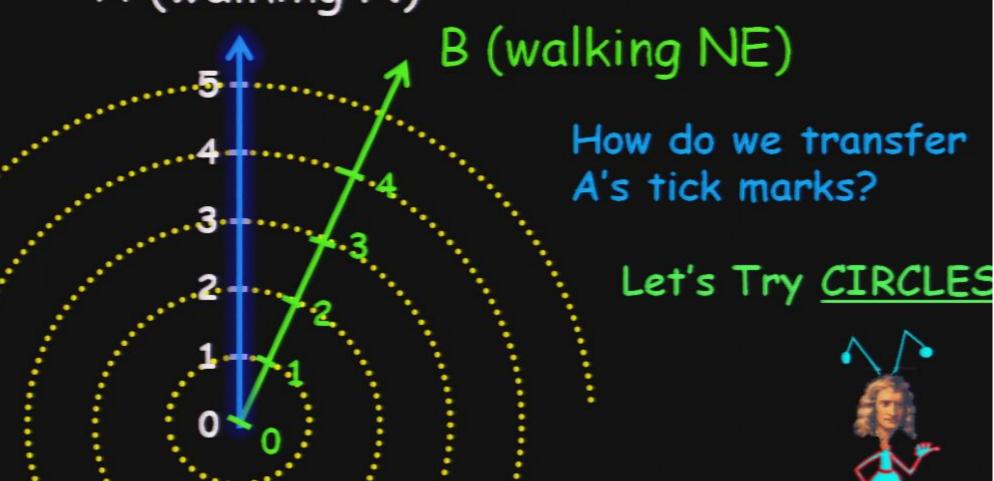


B (walking NE)

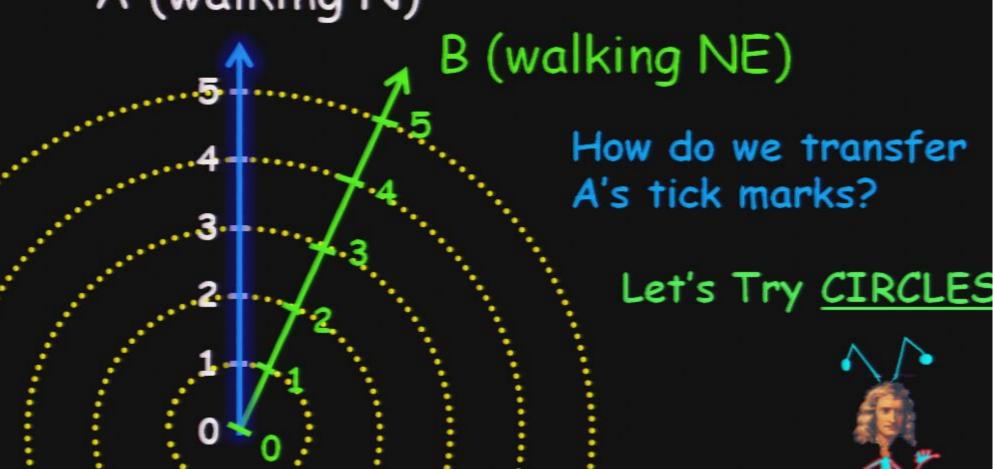
How do we transfer A's tick marks?

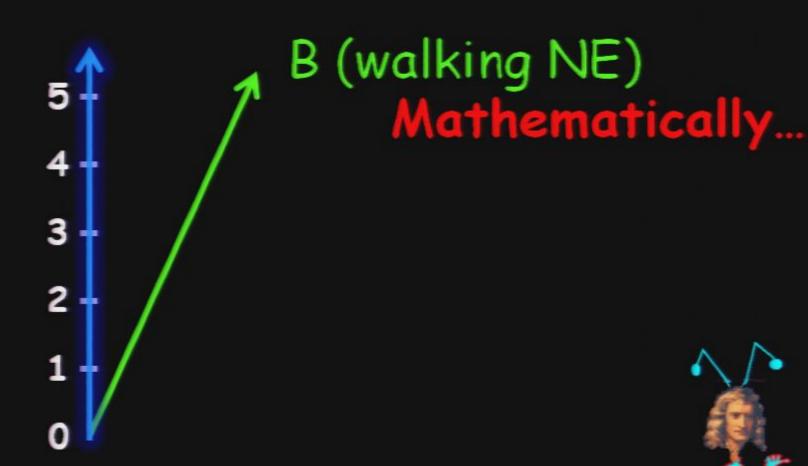




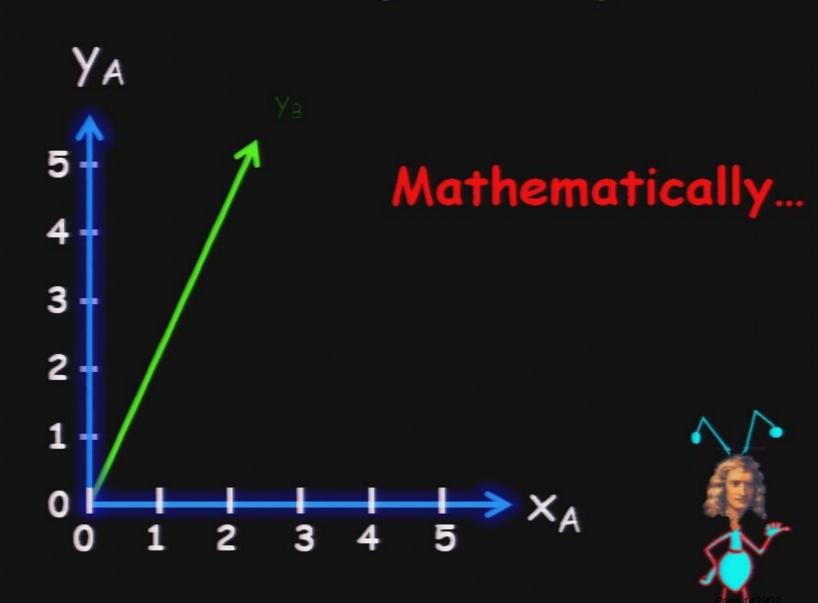


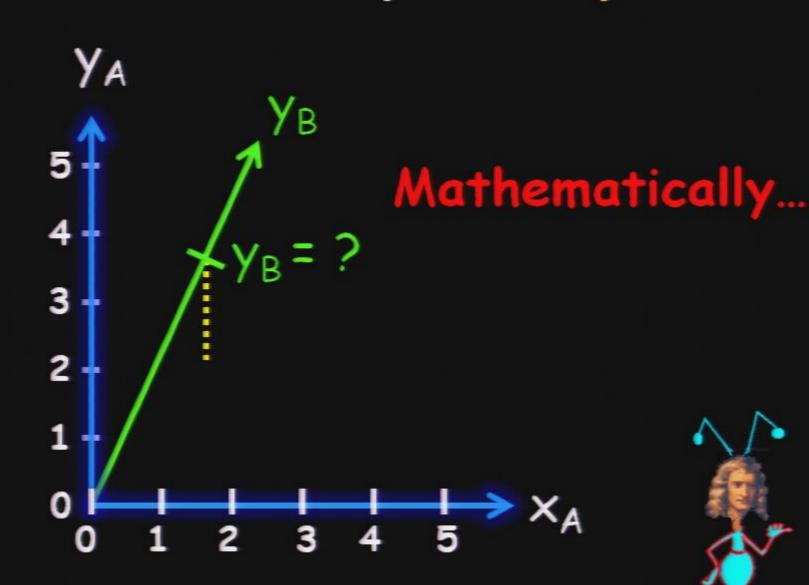


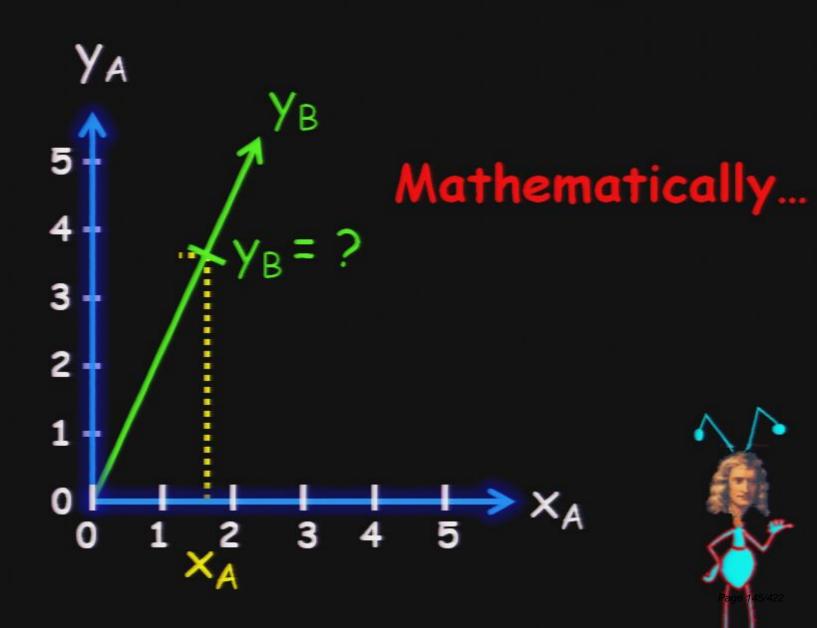


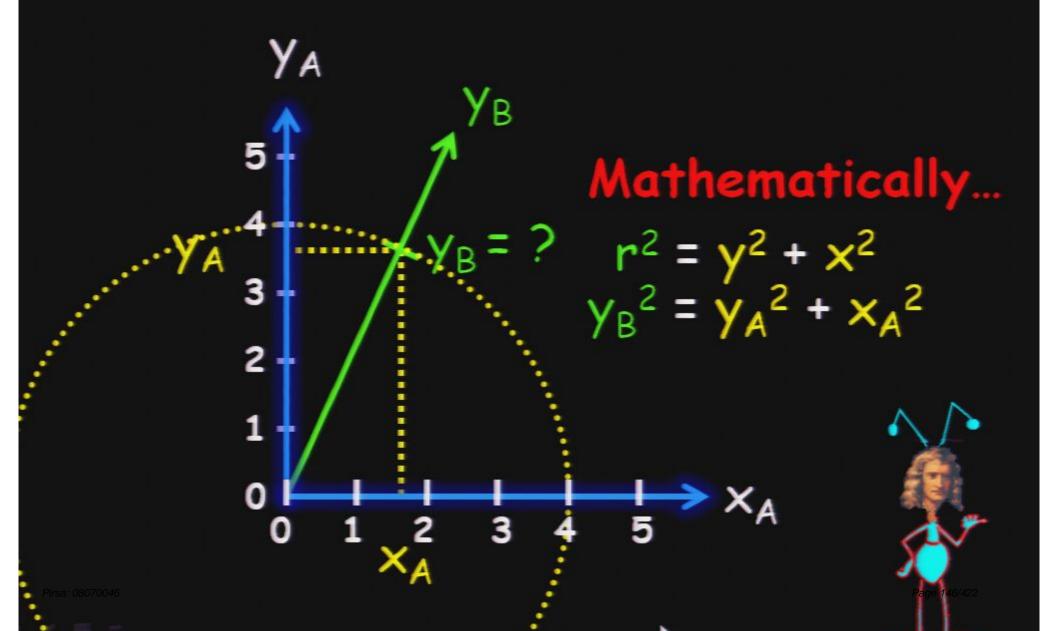


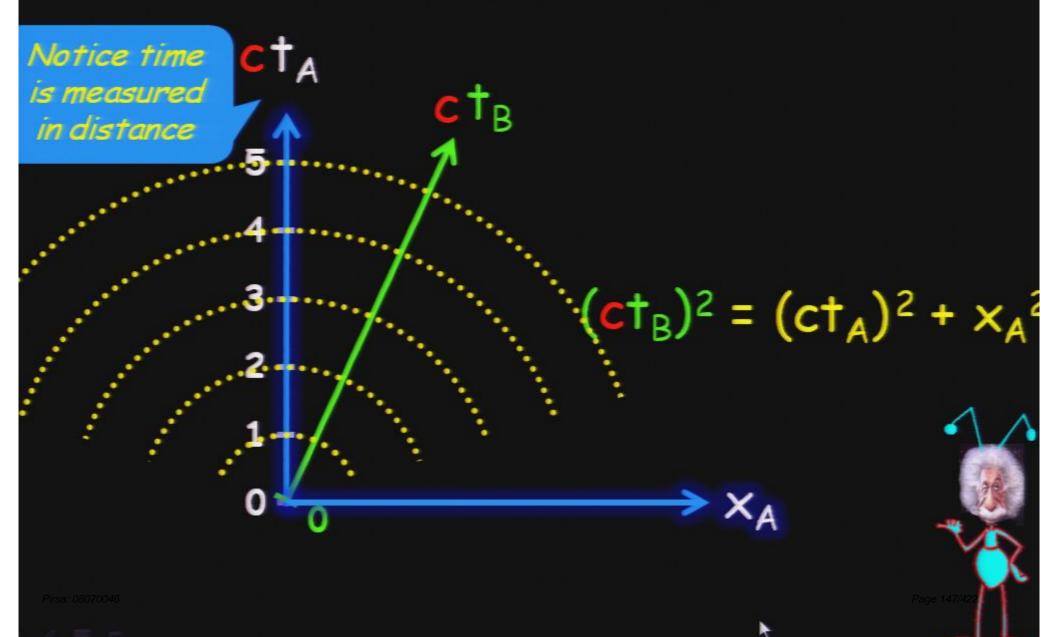


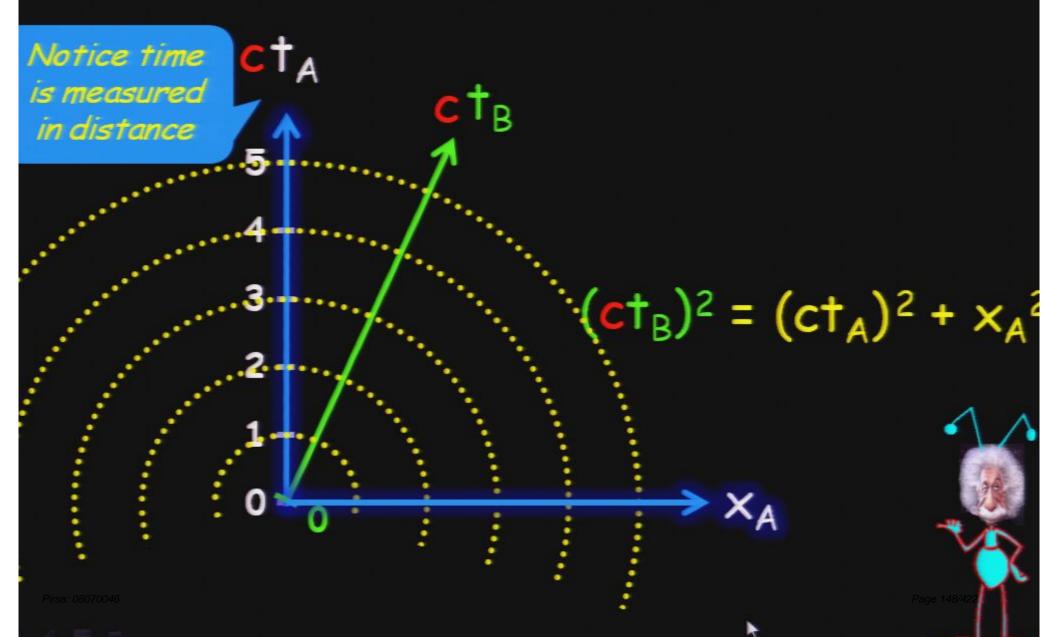


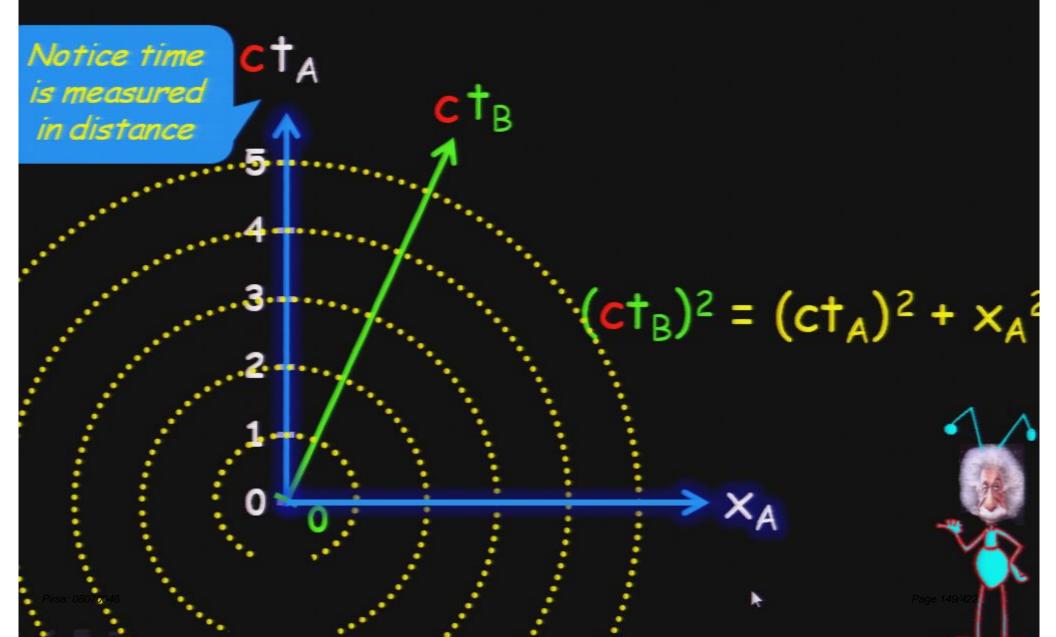


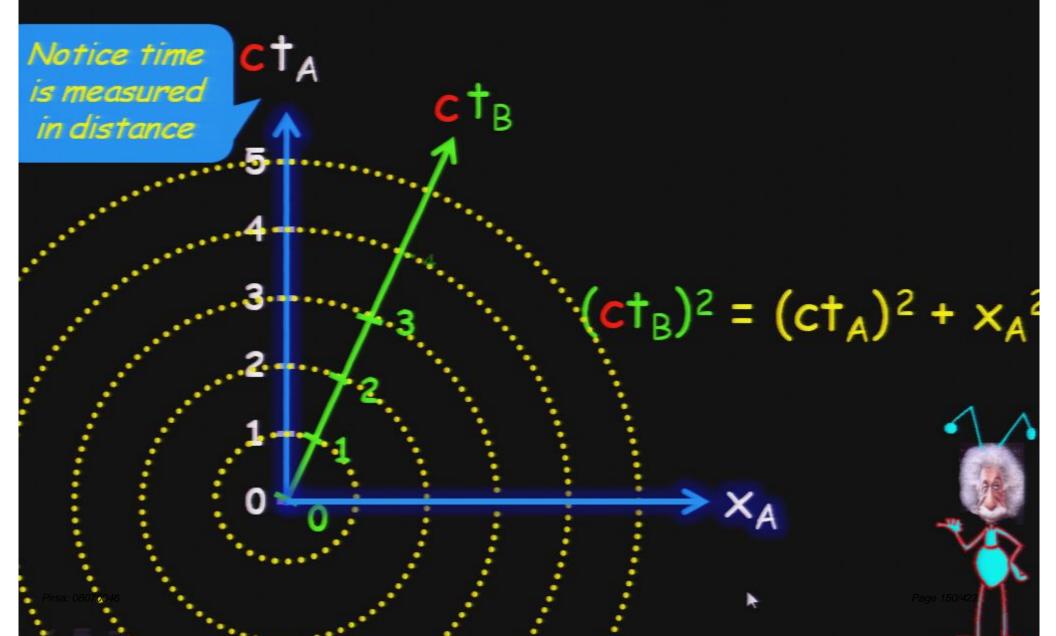


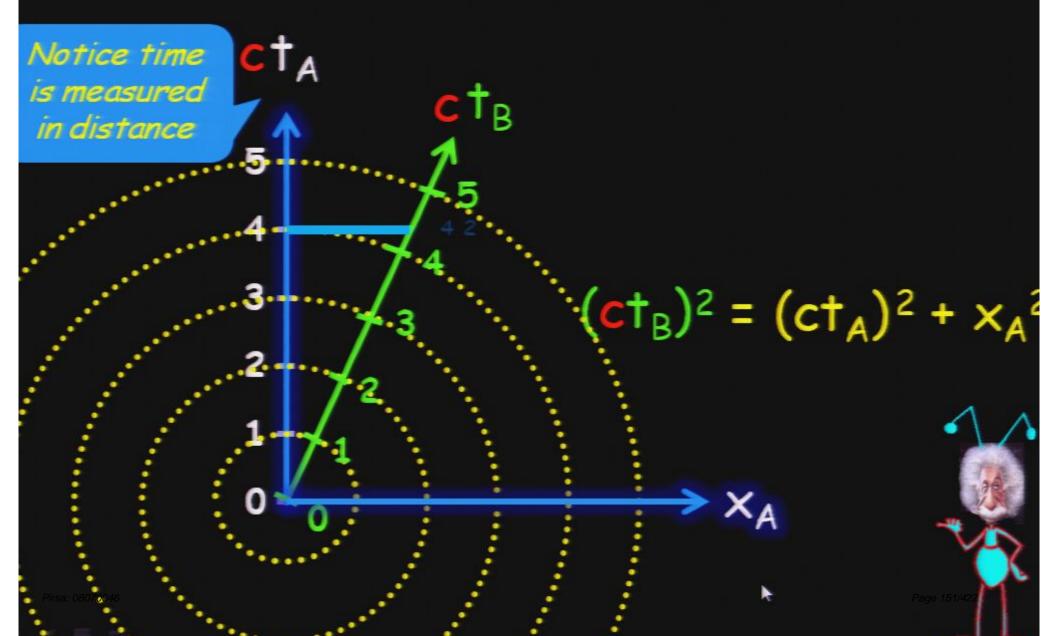


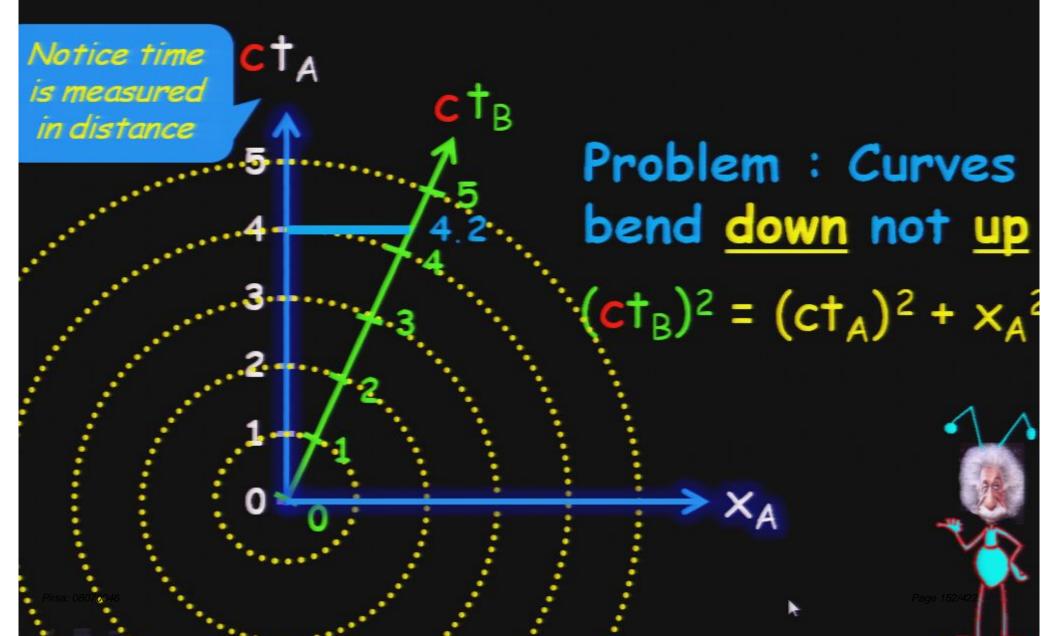




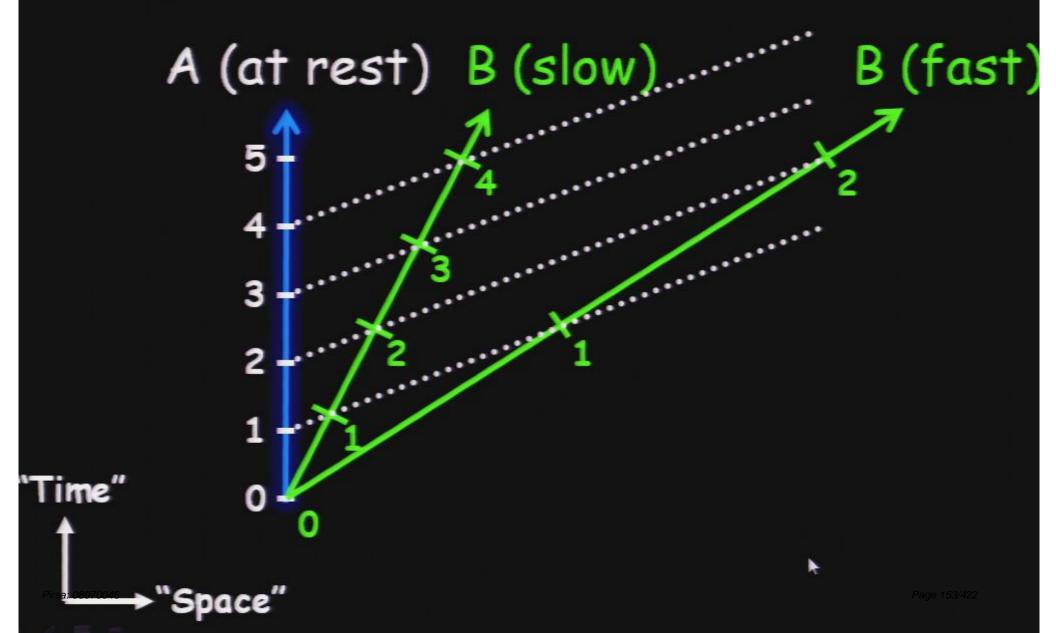


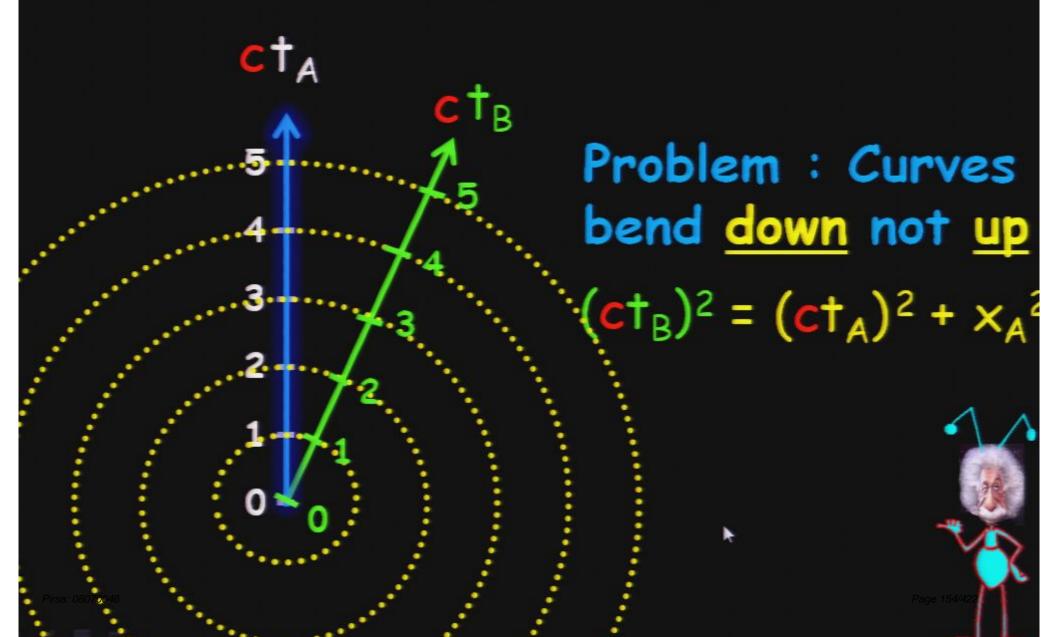






Experimental Data:







Problem : Curves bend down not up

$$(ct_B)^2 = (ct_A)^2 + x_A^2$$



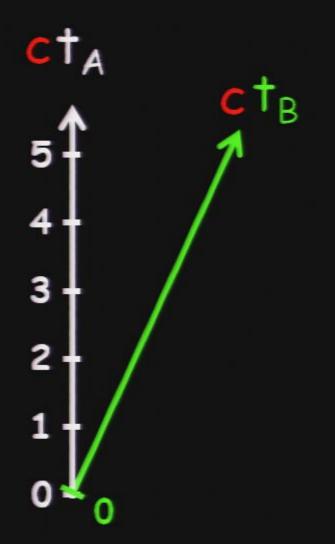
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$$(ct_B)^2 = (ct_A)^2 + x_A^2$$



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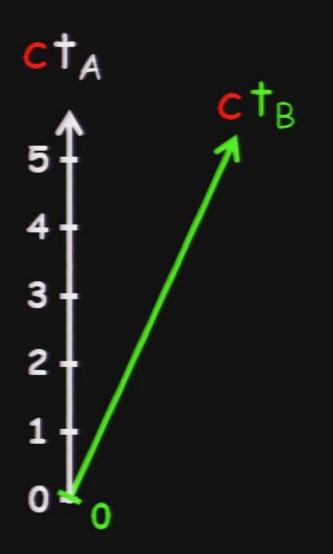


Try <u>hyperbolas</u> instead of circles:

$$(ct_B)^2 = (ct_A)^2 + x_A^2$$



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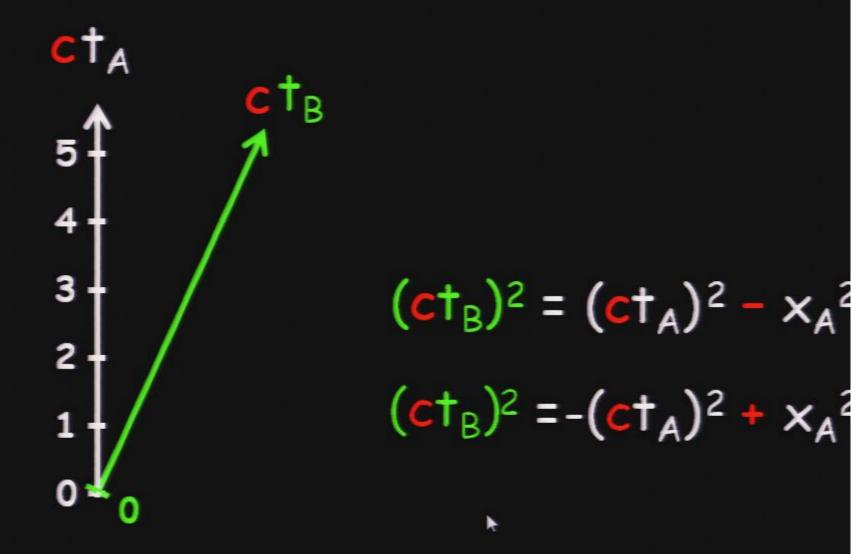


Try <u>hyperbolas</u> instead of circles:

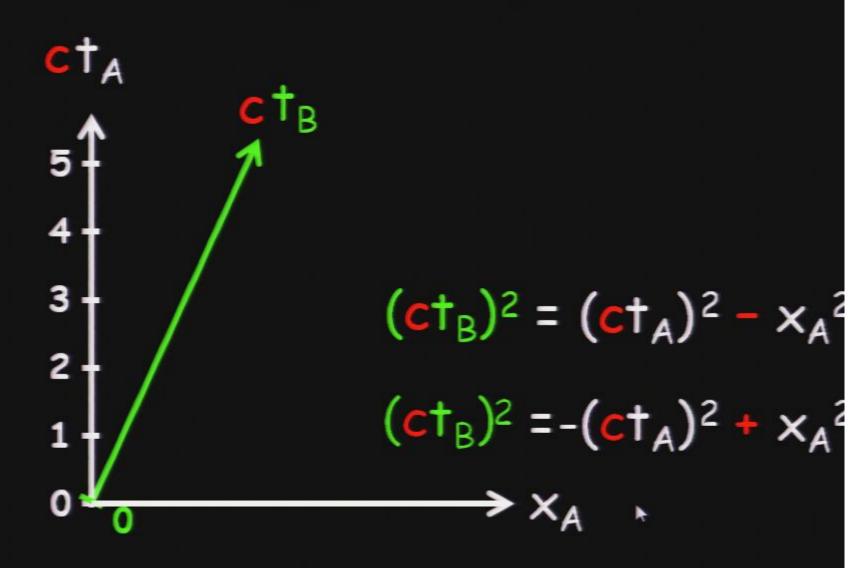
$$(ct_B)^2 = (ct_A)^2 - x_A^2$$

Minus sign

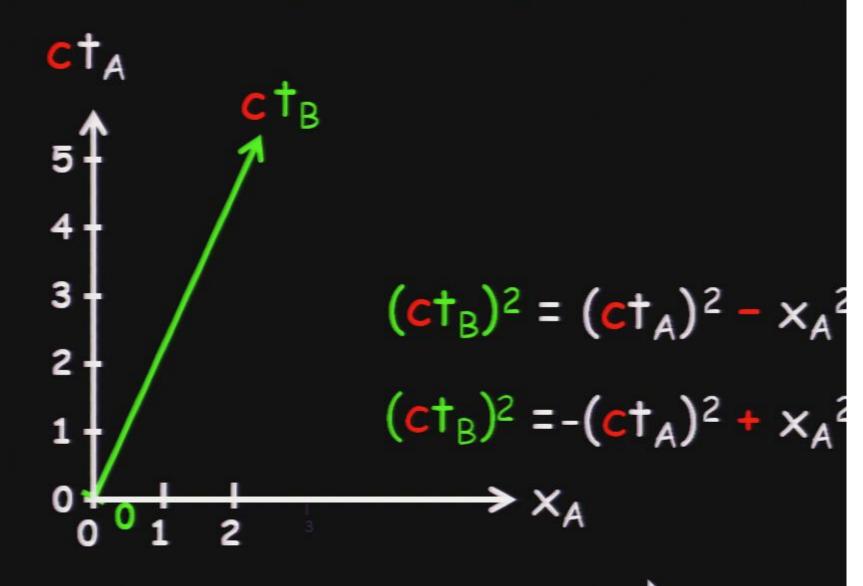




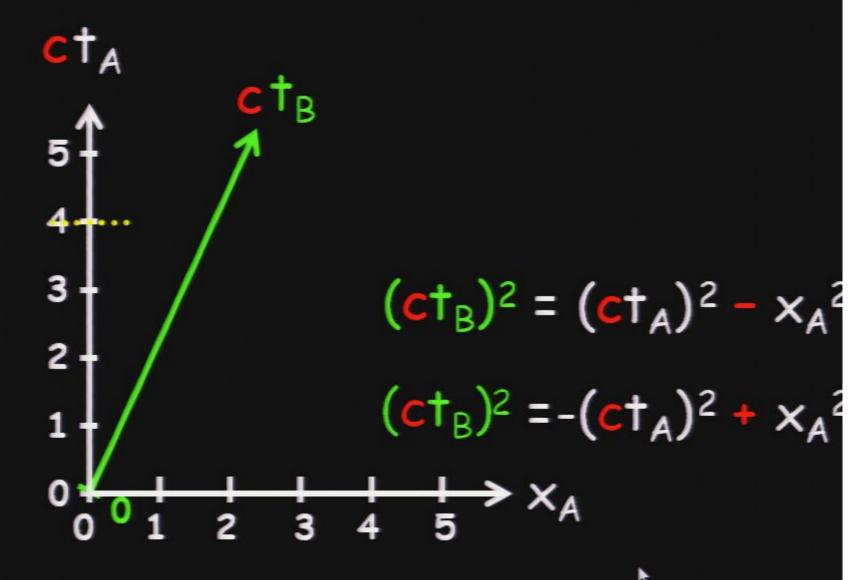
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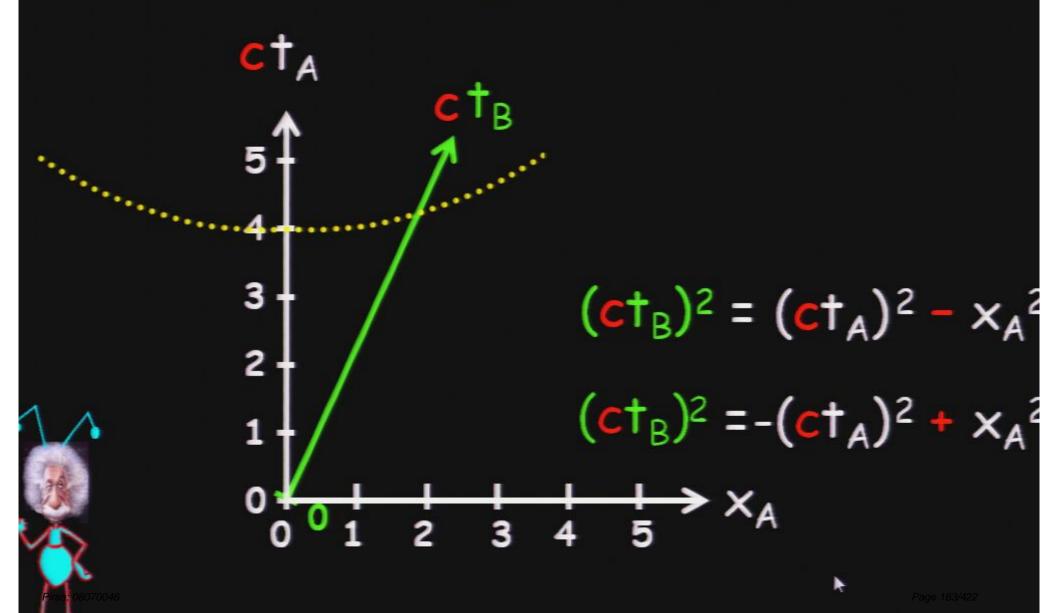


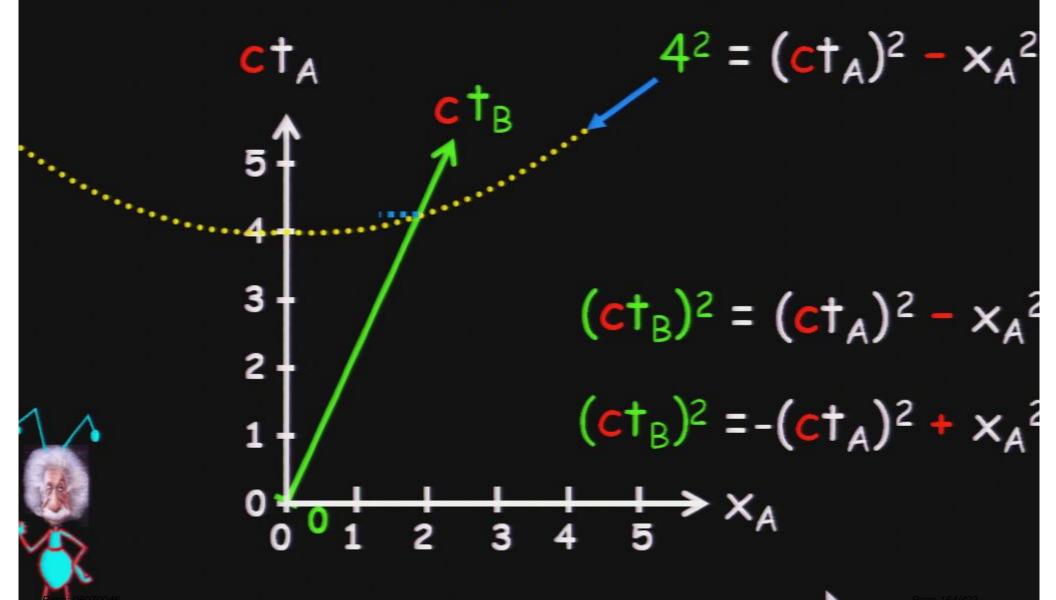


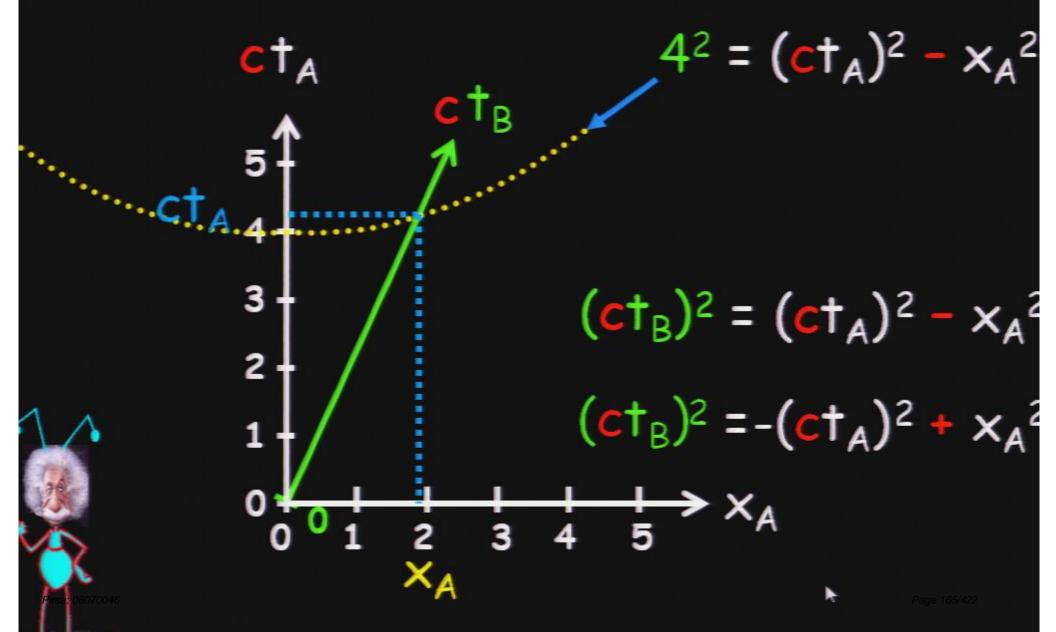


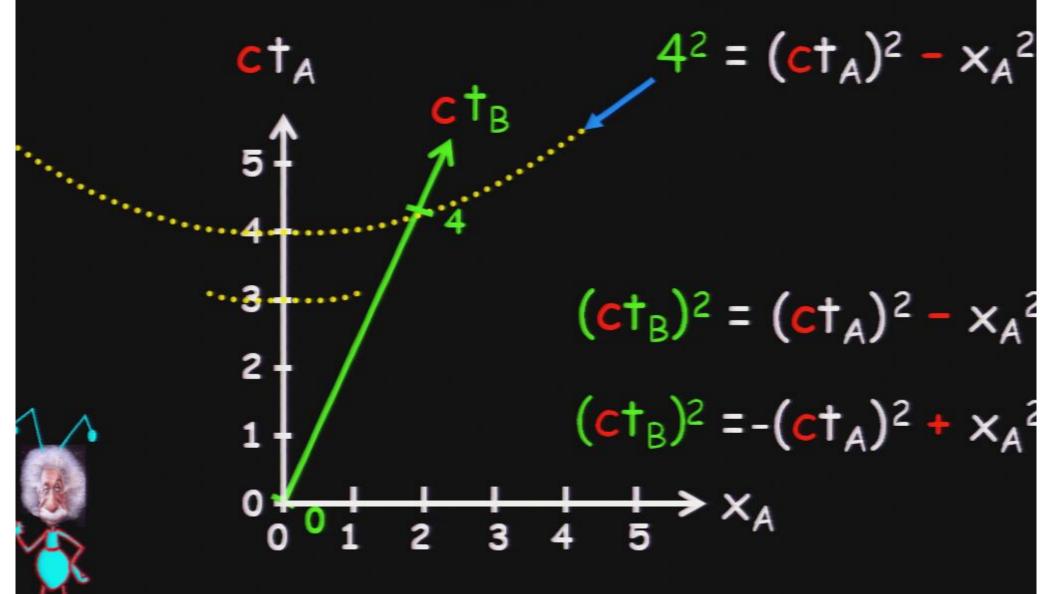


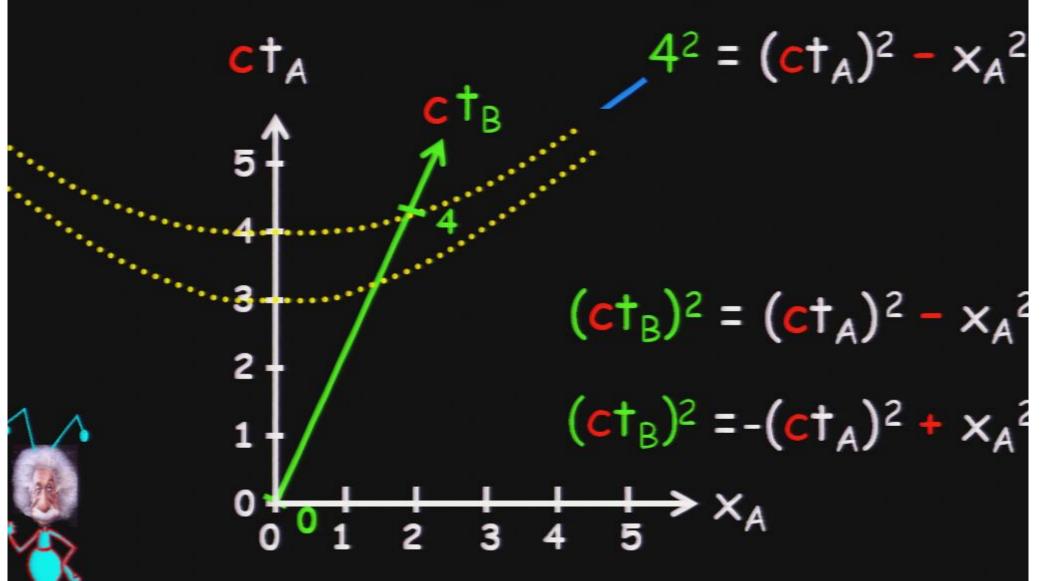


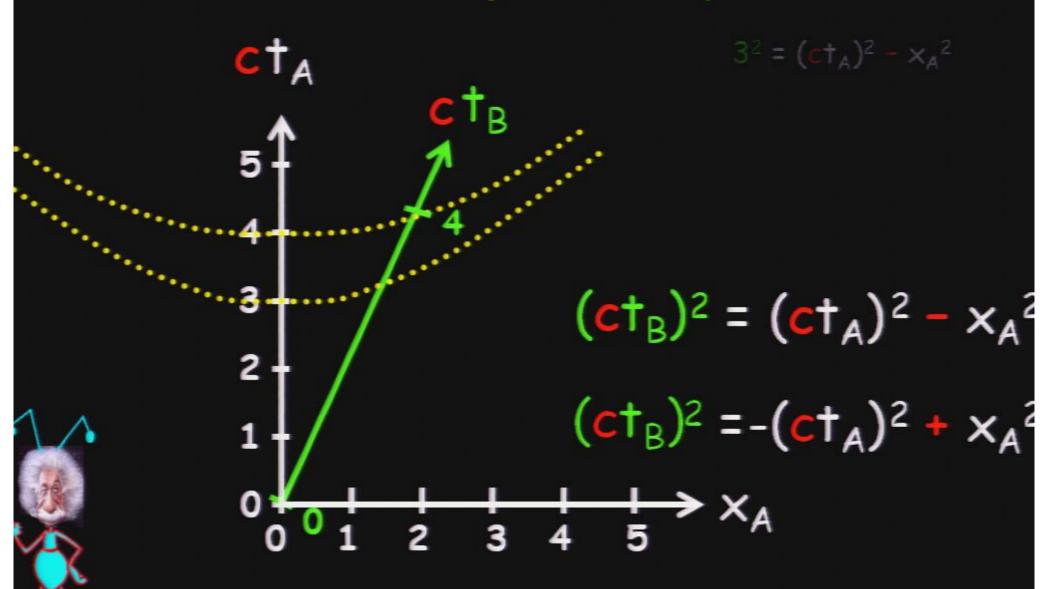


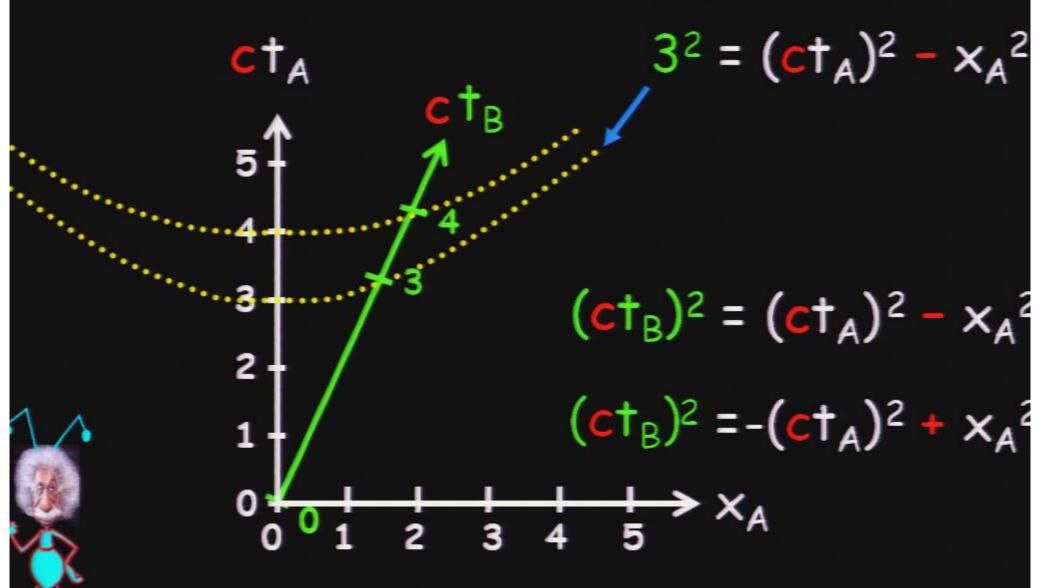


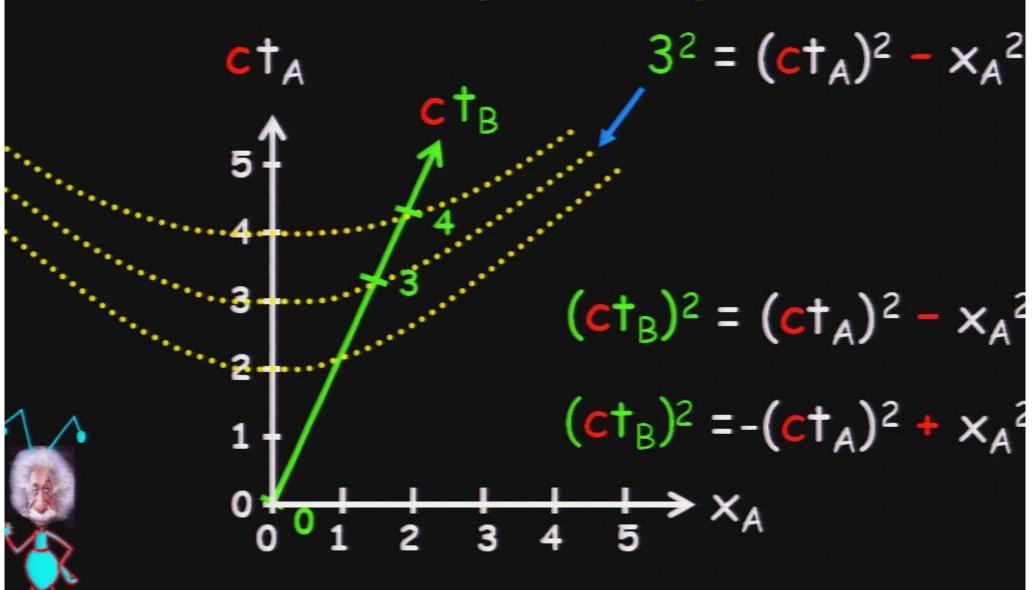


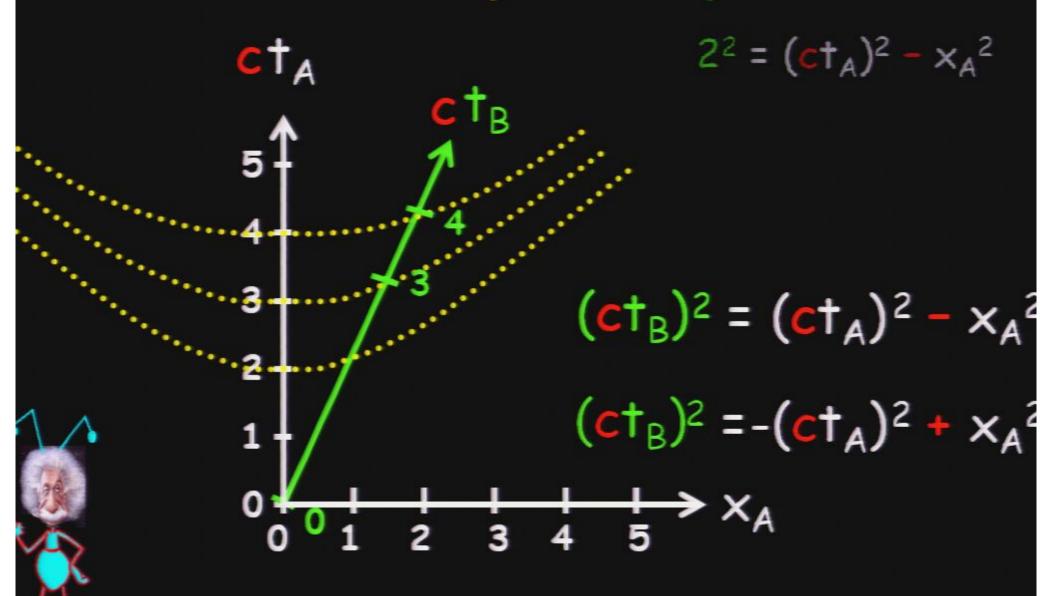


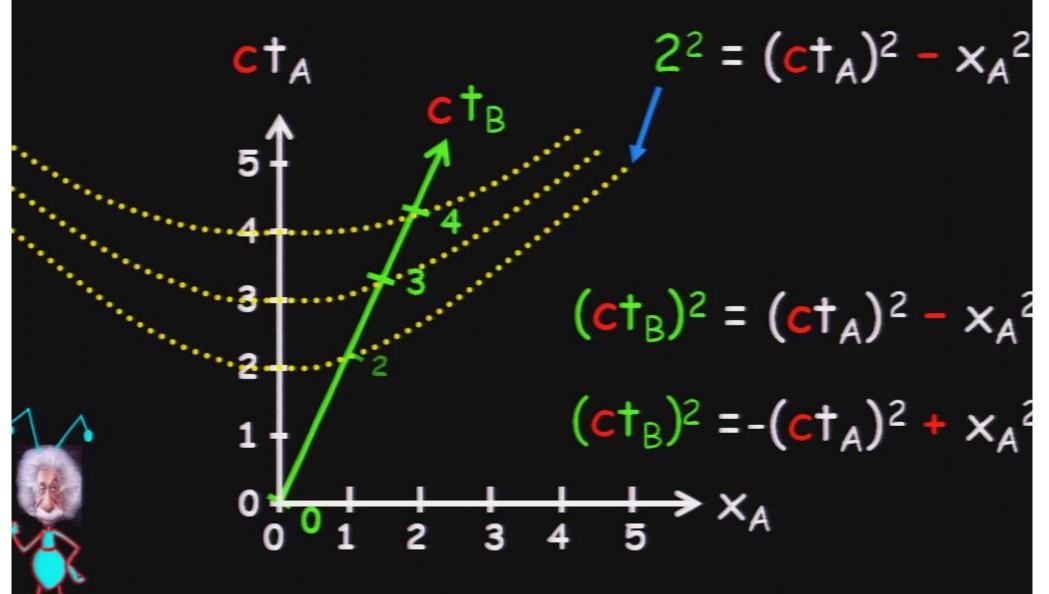


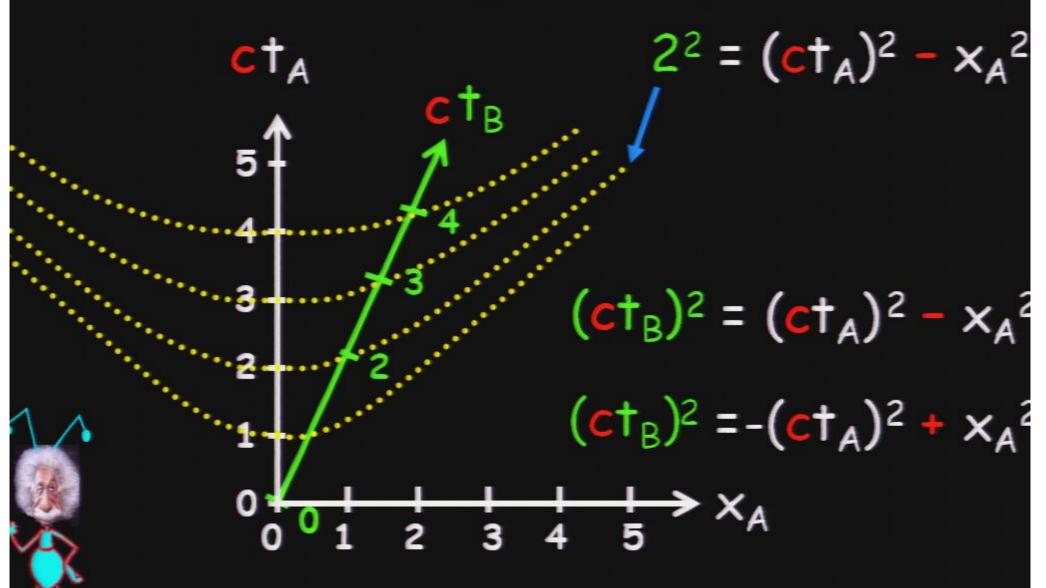


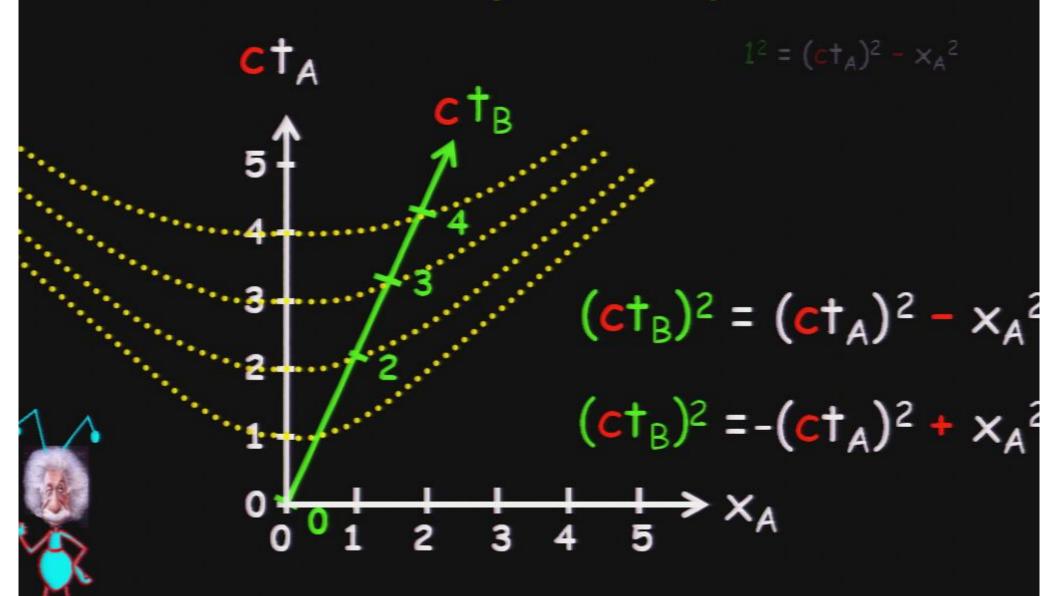


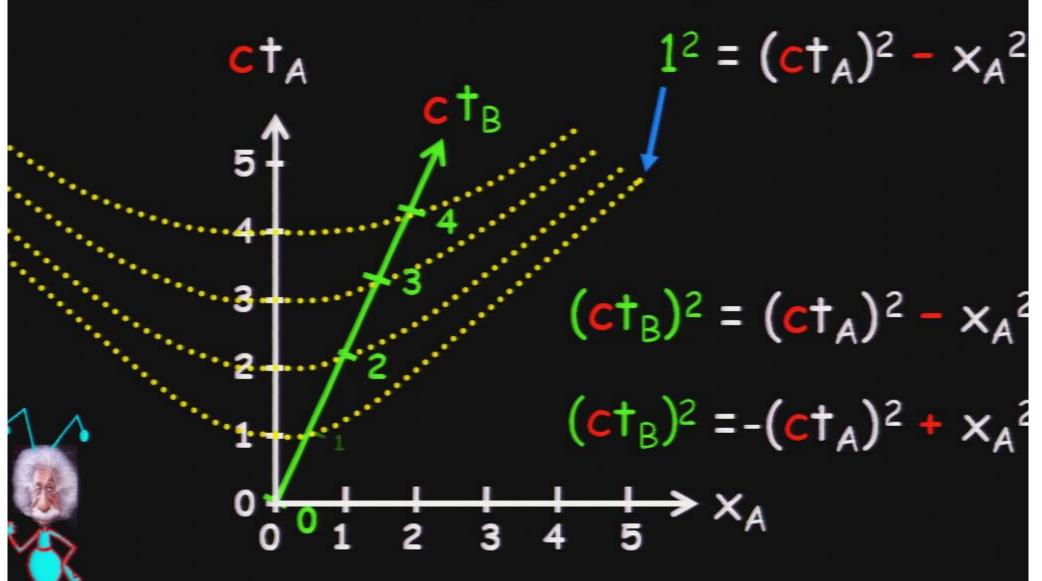


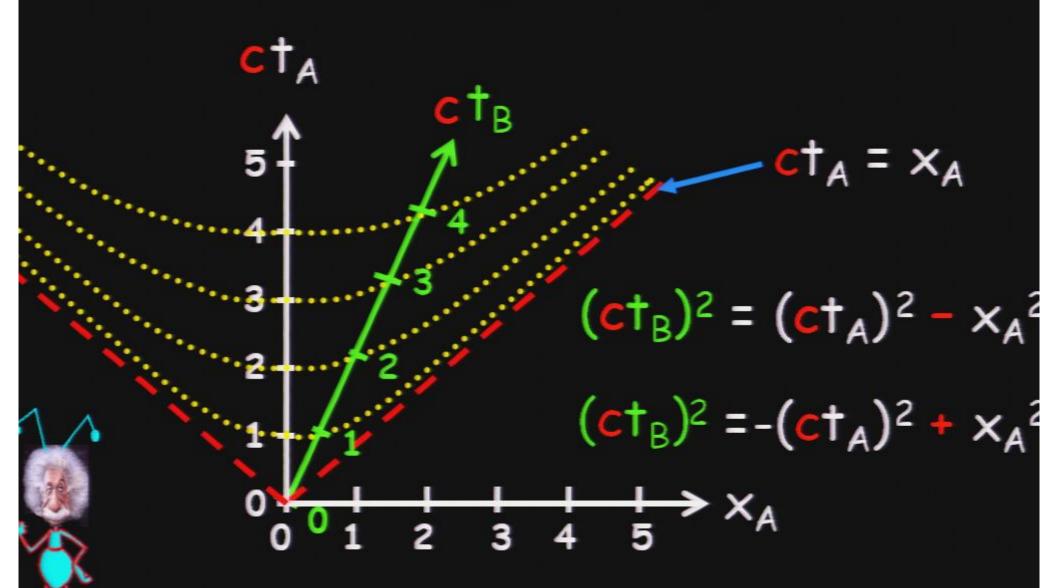








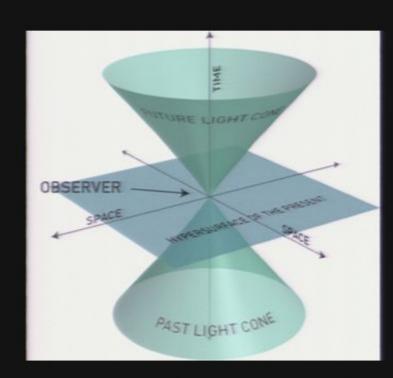




Spacelike, Null, Timelike

Special relativity implies that all matter must move at less than or equal to the speed of light.





Einstein's Spacetime

· Define a mathematical tool that handles both Space and Time P(t, x, y, z)

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Einstein's Spacetime

- Define a mathematical tool that handles both Space and Time P(t,x,y,z)
- · Example two dimensional Euclidean Space

$$\left(\Delta s\right)^2 = \left(\Delta x\right)^2 + \left(\Delta y\right)^2$$
 Cartesian coordinates $\left(\Delta s\right)^2 = \left(\Delta r\right)^2 + r^2\left(\Delta\phi\right)^2$ Polar coordinates

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Einstein's Spacetime

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· Example of two dimensional Minkowski Space

$$\left(\Delta s\right)^2 = -\left(\Delta t\right)^2 + \left(\Delta x\right)^2$$
 Usual representation $\left(\Delta s\right)^2 = -\left(\Delta t\right)^2 + t^2\left(\Delta\phi\right)^2$ Milne representation

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 Einstein needed to modify Newton's First Law and he did it like like this...

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... A body will move along the curve of shortest distance in SPACETIME unless a force acts on it.



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 Einstein needed to modify Newton's First Law and he did it like like this...

... A body will move along the curve of shortest distance in SPACETIME unless a force acts on it.



... The shortest distance between two points in general space isn't generally a straight line.

Curves of shortest distance are known in relativistic jargon as geodesics.



The pilot does not need to turn the plane to fly from Toronto to Rome



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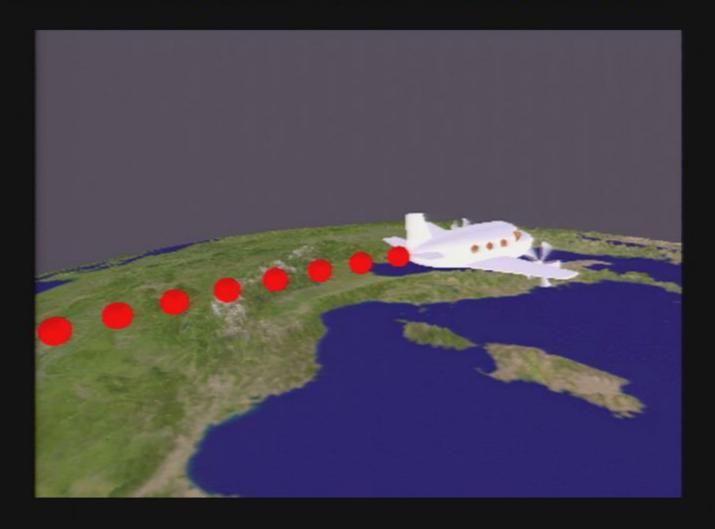
The pilot does not need to turn the plane to fly from Toronto to Rome



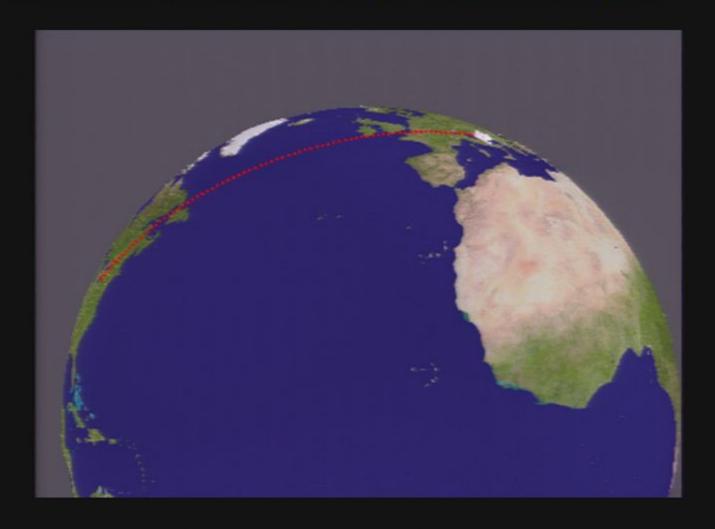
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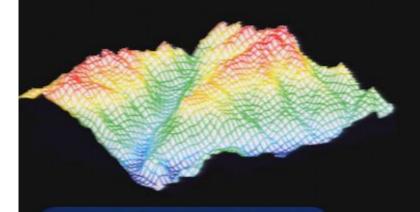
The pilot does not need to turn the plane to fly from Toronto to Rome



The pilot does not need to turn the plane to fly from Toronto to Rome

Geodesics are very difficult to calculate in general, Imagine surveying a complex landscape with hills and valleys. How is one to calculate the shortest distance

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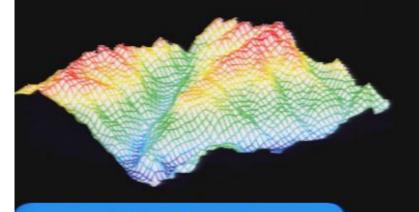


...and I had to do it in four dimensions!, Yep, that time thing.

Geodesics are very difficult to calculate in general. Imagine surveying a complex landscape with hills and valleys. How is one to calculate the shortest distance over this terrain?



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...and I had to do it in four dimensions!, Yep, that time thing.

Geodesics are very difficult to calculate in general. Imagine surveying a complex landscape with hills and valleys. How is one to calculate the shortest distance over this terrain?

It would by very easy to do this is we looked at the landscape from above. Then I could use ds²=dx²+dy²



...but I needed the distance in SPACETIME, so I used a mathematical quantity which converts the flat map distances into actual distances on our curved space. This is the METRIC of the space. Denoted by "g".

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The idea of a metric is very common to us. It is a way of converting universal distance (the distance on a flat space) to distances on curved spaces.

Pirsa: 08070046 Page 203/42:

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It's like a taxi meter which converts fixed amounts of time and distance into a cost for the passenger





Page 204/422

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It may cost you more at night than it does in daytime to go the same distance



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The idea of a metric is very common to us. It is a way of converting universal distance (the distance on a flat space) to distances on curved spaces.

It's like a taxi meter which converts fixed amounts of time and distance into a cost for the passenger



It may cost you more at night than it does in daytime to go the same distance



It may cost you more to take a taxi in New York than it does in Waterloo to travel the same distance.

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The idea of a metric is very common to us. It is a way of converting universal distance (the distance on a flat space) to distances on curved spaces.

It's like a taxi meter which converts fixed amounts of time and distance into a cost for the passenger

The "taxi metric" can depend on time, it can depend on location.



It may cost you more at night than it does in day time to go the same distance



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The Metric, g

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The Metric, g

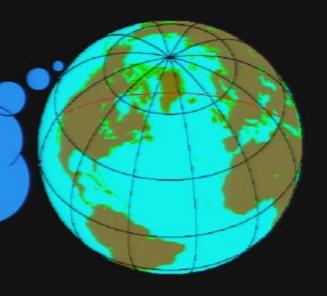
The Metric, g





The Metric, g

I curve in two directions (north-south, and east-west)



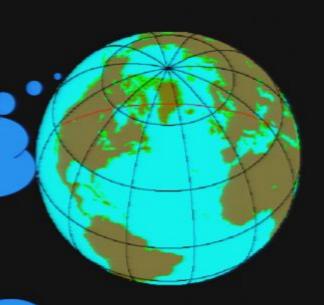
Me, I only bend in east -west.





The Metric, g

My mama calls me an intrinsic curvature



My mama calls
me my little
extrinsic
curvature

So, for these geometries we need 2 numbers to uniquely specify the curvature of the surface



What about g, in Four Dimensions?

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What about g, in Four Dimensions?

We will designate two numbers representing the metric, g_{xx} and g_{yy} , to show that they are associated with curvature in the x and y direction.

In four dimensions, it works out that we need 10

I needed another mathematical tool to help me keep the numbers straight, and yet allow me to do calculations.

The Tensor (in Spacetime)

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The Tensor (in Spacetime)



Tensors are mathematical objects that are simply organized groups of numbers. They have an index that indicate there size (how many numbers they hold)



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O-tensor is a single number: for example "5"

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0-tensor is a single number: for example "5"
1-tensor is a string of 4 numbers: for example A;=(1, 0, -3.14, 2)



Tensors are mathematical objects that are simply organized groups of numbers. They have an index that indicate there size (how many numbers they hold)



1-tensor is a string of 4 numbers: for example A_j =(1, 0, -3.14, 2)

2- tensor is a matrix of 4x4=16 numbers

$$B_{ij} = \begin{pmatrix} 3 & -1 & 17 & 2 \\ 7 & 99 & 0 & 34 \\ 1000 & 3 & 0 & -1 \\ 4 & -2.5 & 7 & -12.3 \end{pmatrix}$$



With these tools, I can finally write down how the Geometry of Space Time is affected by mass or is it how mass is affected by the geometry of Space Time



O-tensor is a single number: for example "5"

1-tensor is a string of 4 numbers: for example A_j =(1, 0, -3.14, 2)

2- tensor is a matrix of 4x4=16 numbers

$$B_{ij} = \begin{pmatrix} 3 & -1 & 17 & 2 \\ 7 & 99 & 0 & 34 \\ 1000 & 3 & 0 & -1 \\ 4 & -2.5 & 7 & -12.3 \end{pmatrix}$$

The Einstein field equation (EFE) is usually written in the form

$$G_{ij} = 8\pi T_{ij} + \Lambda g_{ij}$$

Einstein's Tensor

Stress-Energy Tensor Metric Tensor

$$\begin{pmatrix} G_{11} & G_{12} & G_{13} & G_{14} \\ G_{21} & G_{22} & G_{23} & G_{24} \\ G_{31} & G_{32} & G_{33} & G_{34} \\ G_{41} & G_{42} & G_{43} & G_{44} \end{pmatrix} = 8\pi \begin{pmatrix} T_{11} & T_{12} & T_{13} & T_{14} \\ T_{21} & T_{22} & T_{23} & T_{24} \\ T_{31} & T_{32} & T_{33} & T_{34} \\ T_{41} & T_{42} & T_{43} & T_{44} \end{pmatrix} + \Lambda \begin{pmatrix} g_{11} & g_{12} & g_{13} & g_{14} \\ g_{21} & g_{22} & g_{23} & g_{24} \\ g_{31} & g_{32} & g_{33} & g_{34} \\ g_{41} & g_{42} & g_{43} & g_{44} \end{pmatrix}$$

$$G_{ij} = R_{ij} - \frac{1}{2} g_{ij} R$$

Curvature of Space Time describes the density and flux of energy and momentum in spacetime

The EFE is a tensor equation relating a set of symmetric 4 x 4 tensors. Einstein's equations are actually 16 equations in the form: $G_{11} = 8\pi T_{11} + \Lambda g_{11}$

If you sit down and write down the Ricci tensor for a general case of a 2-dimensional space with axial symmetry, you would get something like this:

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$$R_{qq} = -\frac{2a^{2}\frac{\partial\phi}{\partial\theta}\cot\theta}{\frac{\partial\phi}{\partial\theta}\cot\theta} + \frac{2ac\frac{\partial\phi}{\partial\eta}\cot\theta}{\frac{\partial\phi}{\partial\eta}\cot\theta} + \frac{a\frac{\partial\phi}{\partial\eta}\cot\theta}{\frac{\partial\phi}{\partial\eta}\cos\theta} + \frac{a\frac{\partial\phi}{\partial\eta}$$

... and just a little bit more.

$$R_{qq} = \frac{2a^{2}\frac{\partial \phi}{\partial \theta}\cot\theta}{\delta \psi} + \frac{2ac\frac{\partial \phi}{\partial \phi}\cot\theta}{a\frac{\partial \phi}{\partial \phi}} + \frac{a\frac{\partial \phi}{\partial \phi}\cot\theta}{a\frac{\partial \phi}{\partial \phi}} + \frac{a\frac{\partial \phi}{\partial \phi}\cos\theta}{a\frac{\partial \phi}{\partial \phi}}$$

... and just a little bit more.

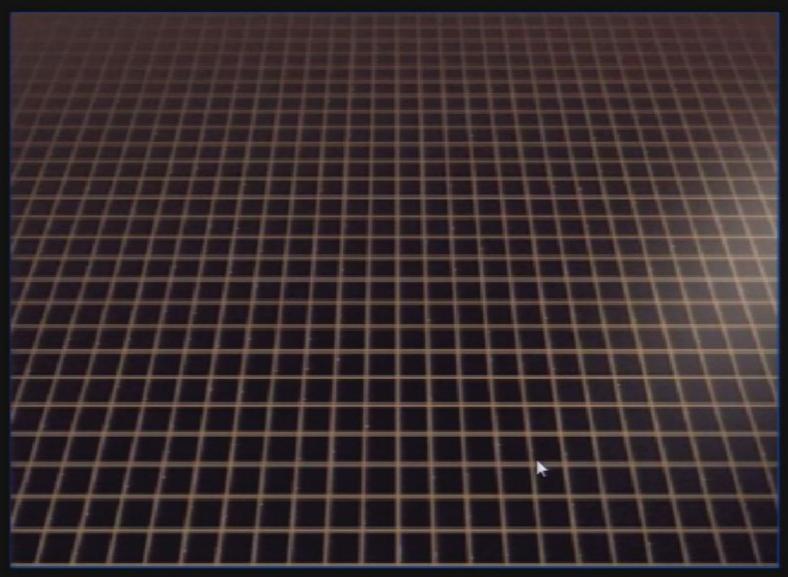
$$R_{qq} = -\frac{2a^{2}\frac{\partial \phi}{\partial \phi} \cot \theta}{\delta \psi} + \frac{2ac\frac{\partial \phi}{\partial \phi} \cot \theta}{\delta \psi} + \frac{a\frac{\partial c}{\partial \phi} \cot \theta}{\delta \psi} + \frac{$$

This is a general expression for Ricci tensor R_{mn} in only <u>two</u> <u>dimensions</u>, with <u>axial symmetry</u>.

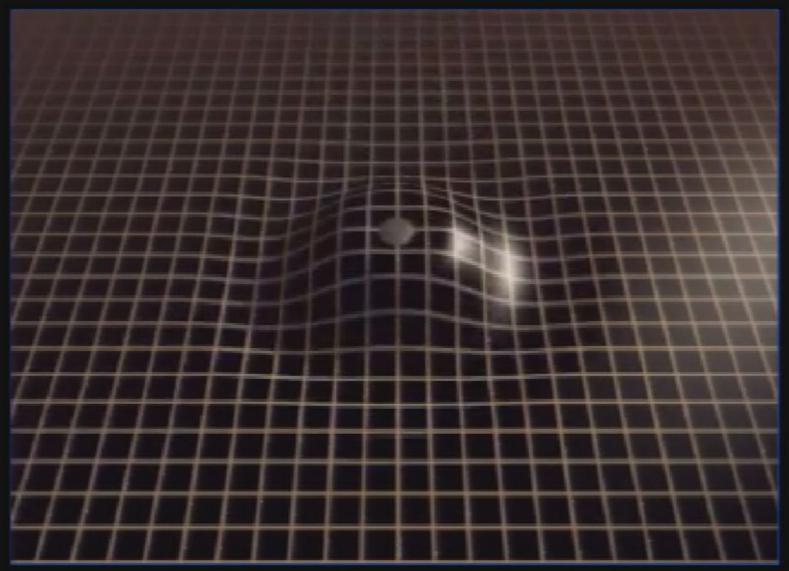
Just try to imagine all of three dimensions of space plus one of time!

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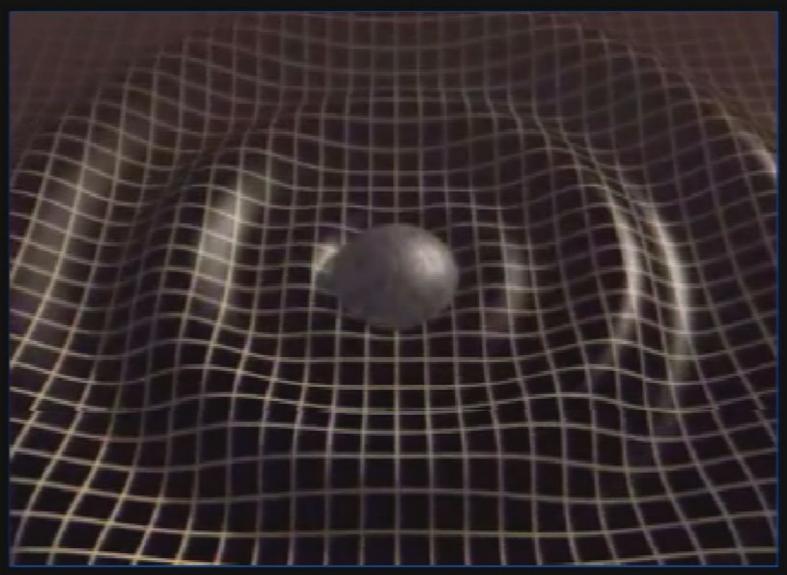
What does all this say?



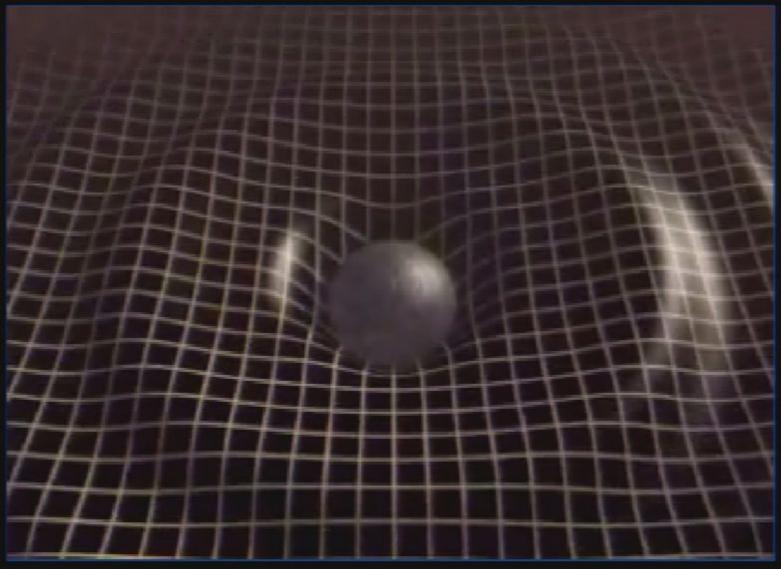
Pirsa: 08070046 Page 230/422



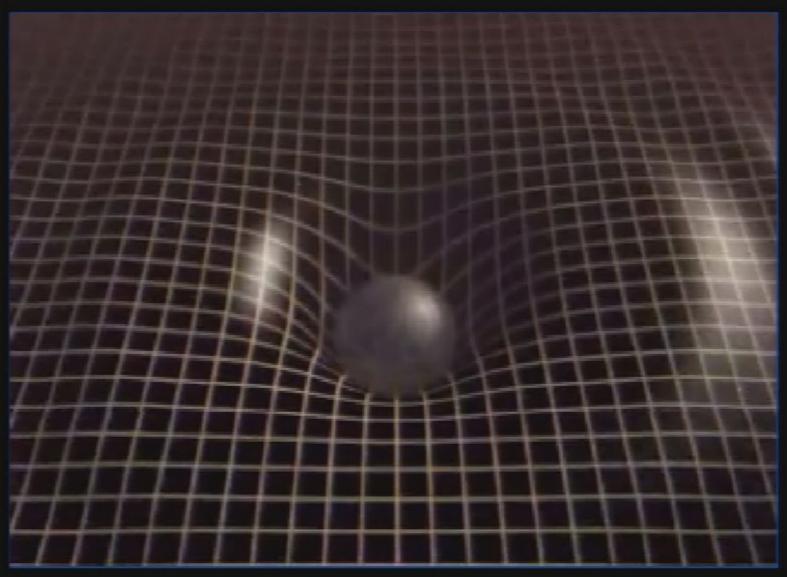
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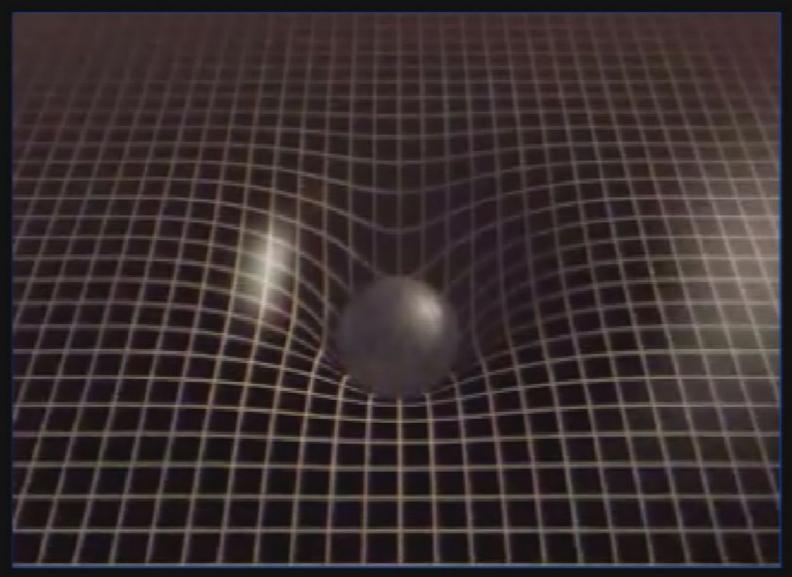
Pirsa: 08070046 Page 232/422



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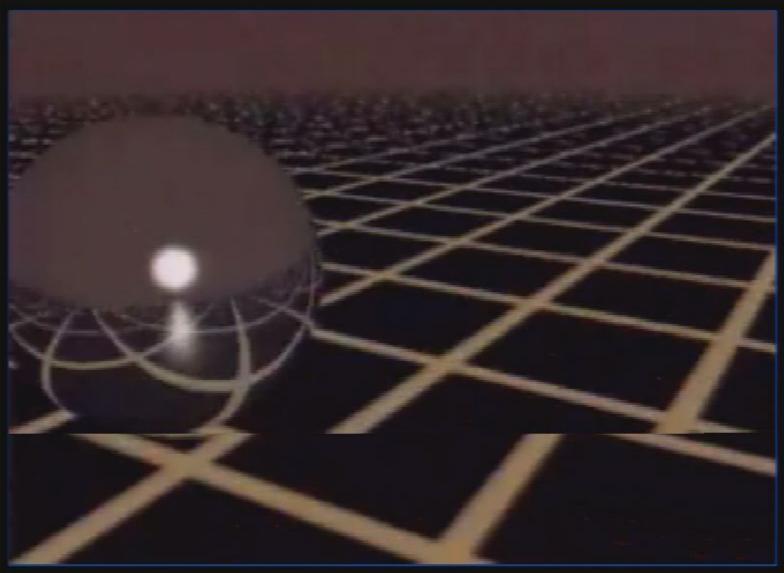
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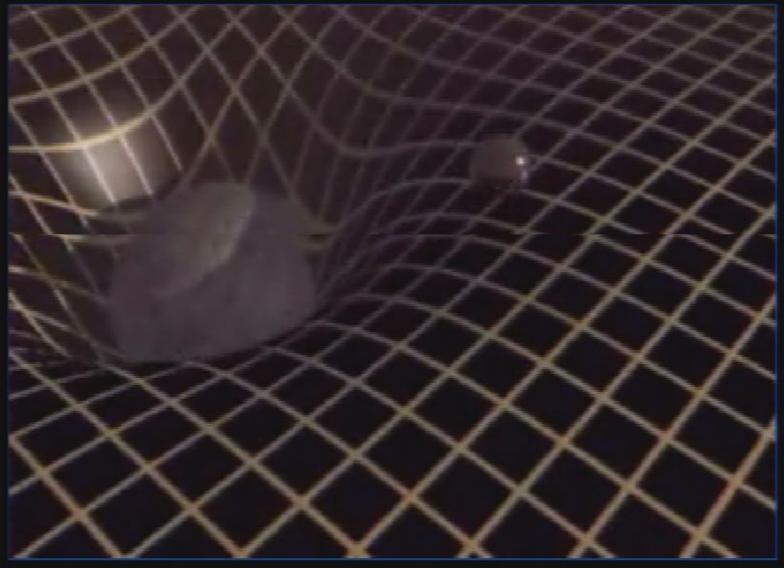
Pirsa: 08070046 Page 235/422



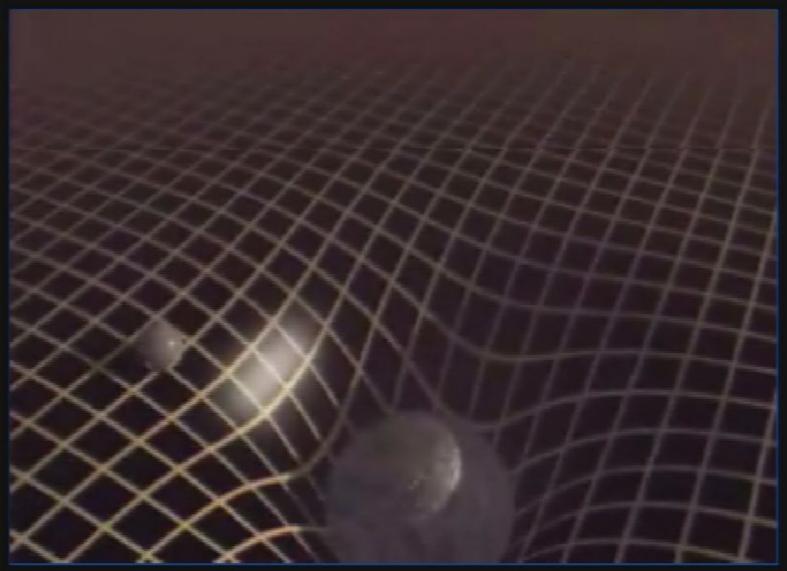
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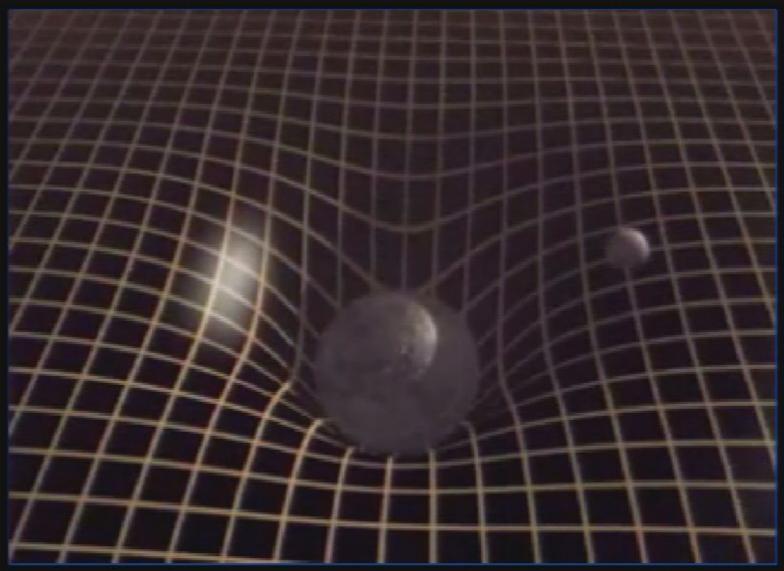
Pirsa: 08070046 Page 237/422



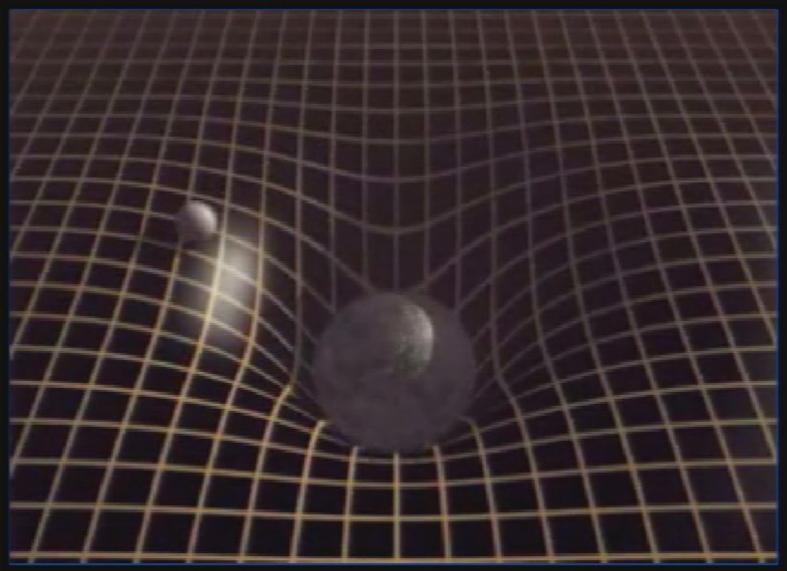
Pirsa: 08070046 Page 238/422



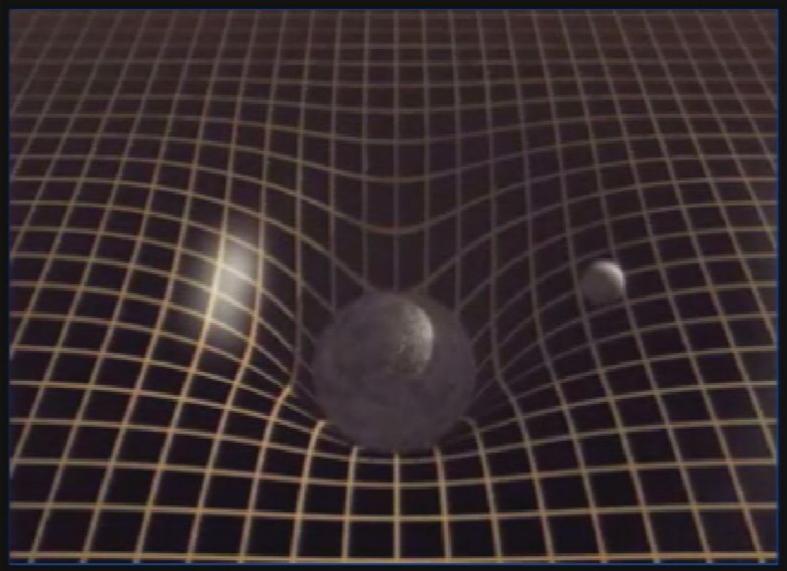
Pirsa: 08070046 Page 239/422



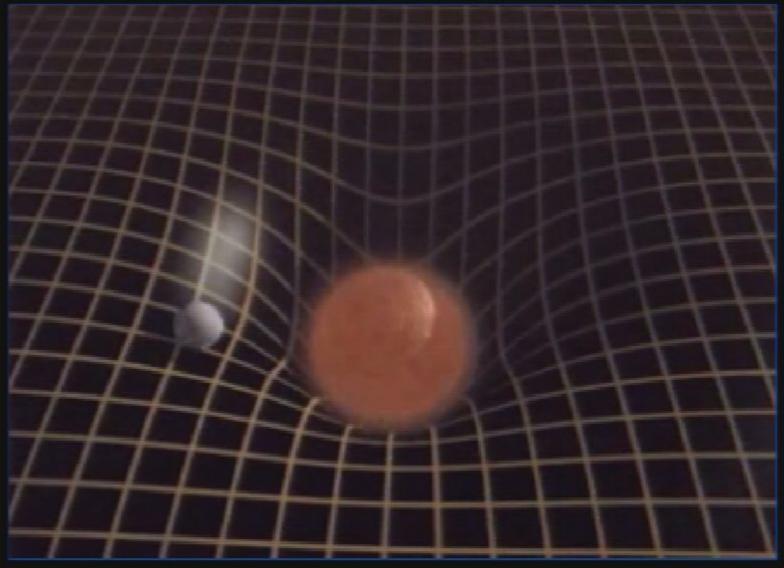
Pirsa: 08070046 Page 240/422



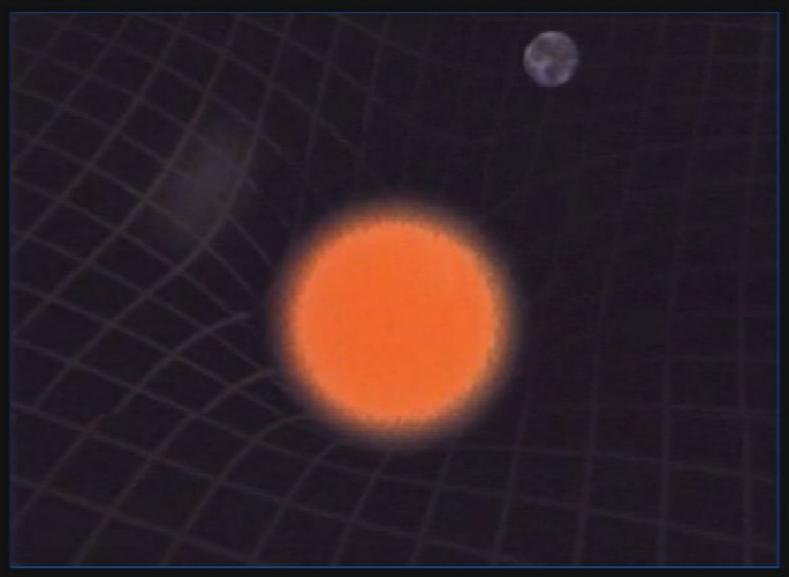
Pirsa: 08070046 Page 241/422



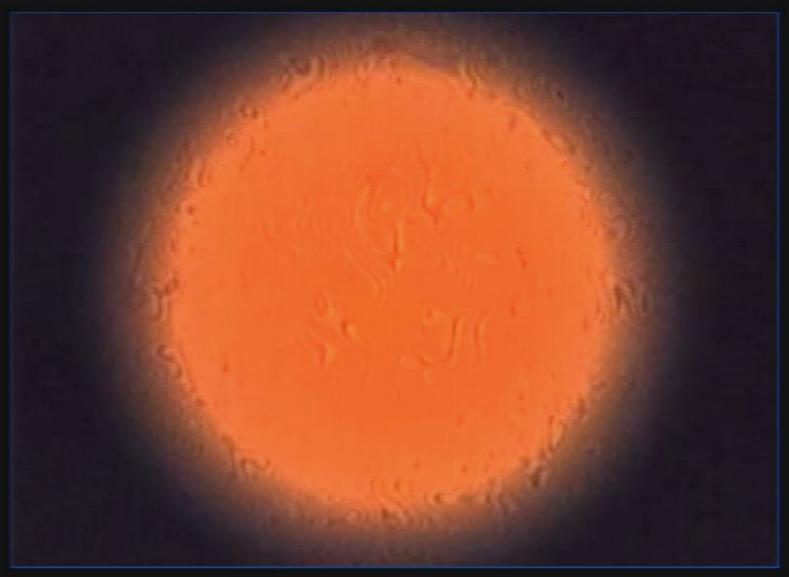
Pirsa: 08070046 Page 242/422

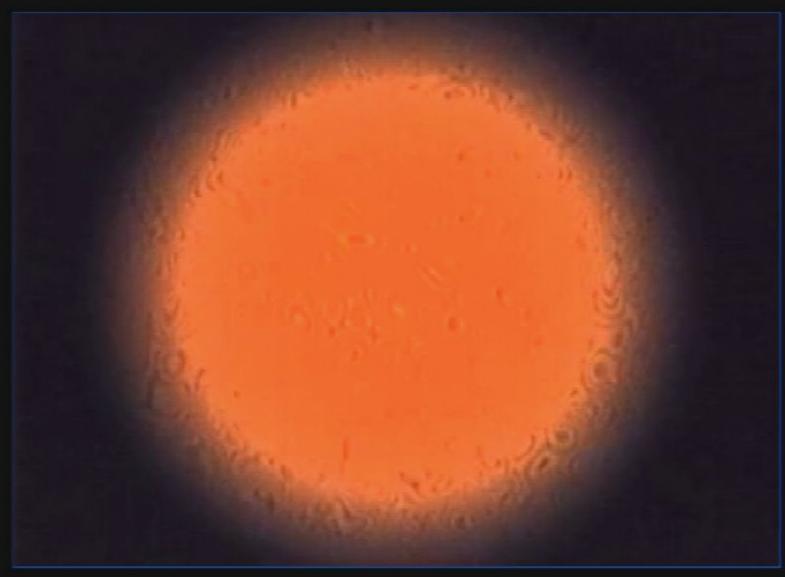


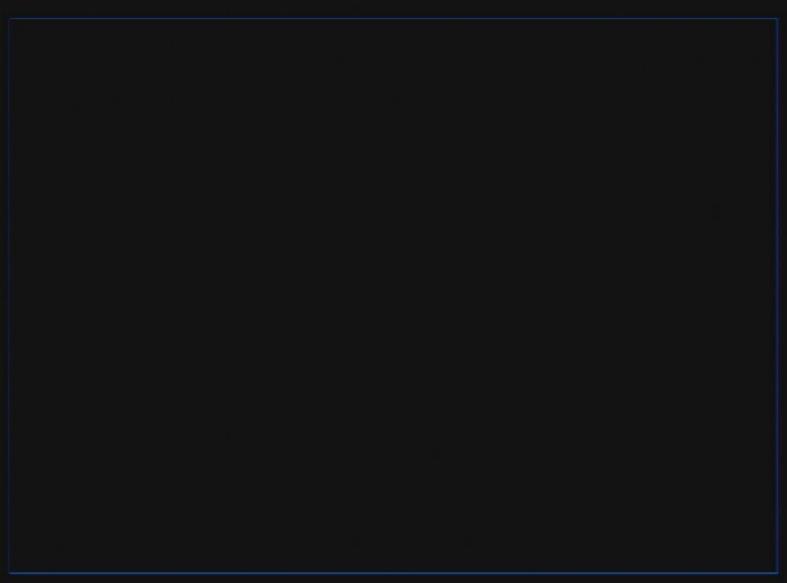
Pirsa: 08070046 Page 243/422



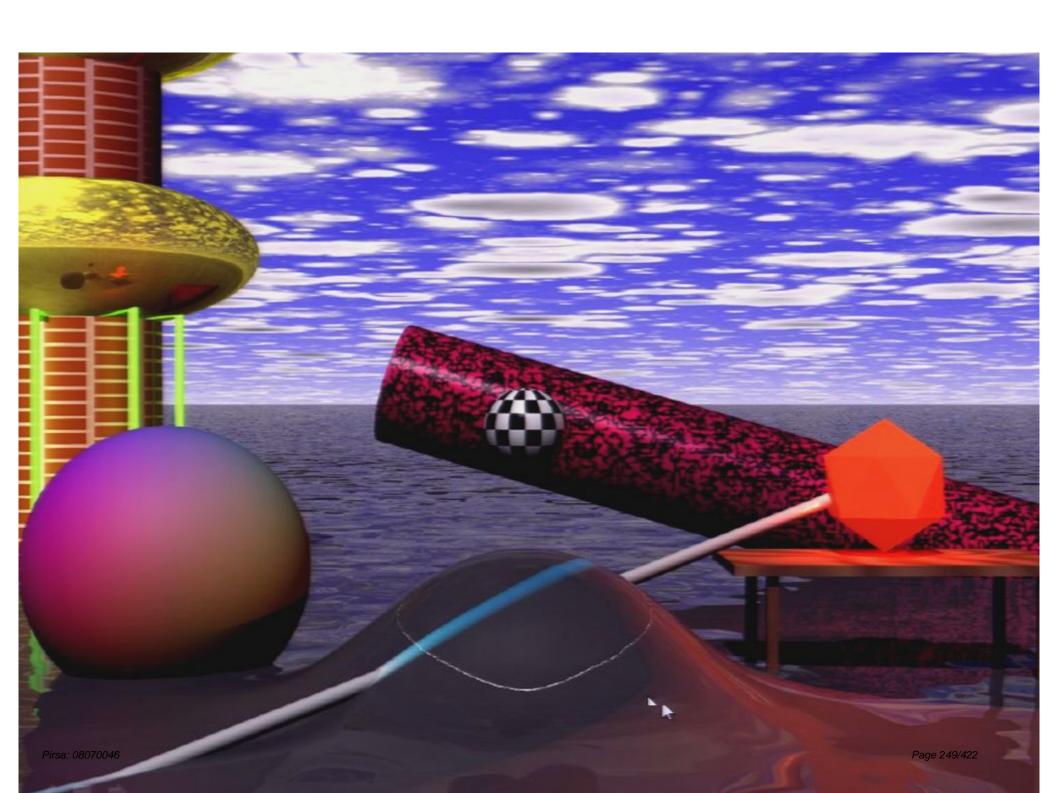


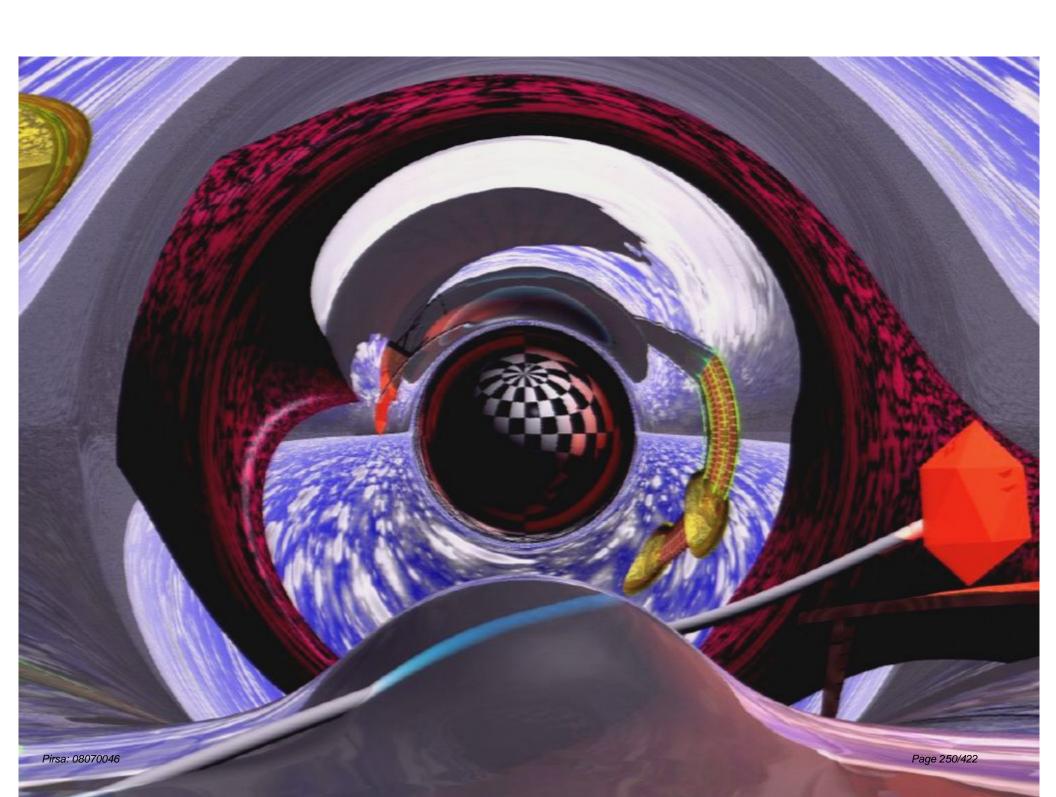




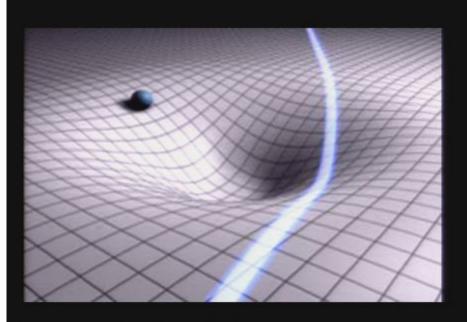


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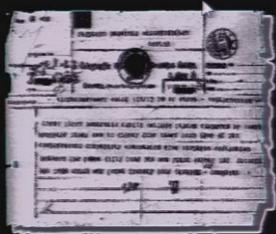
1919 Verification







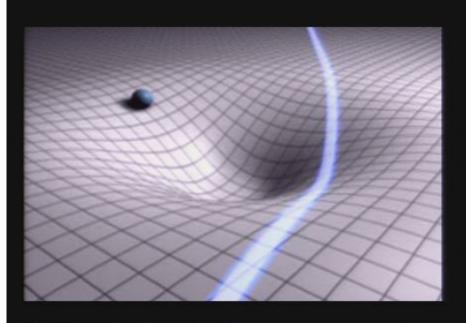




The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

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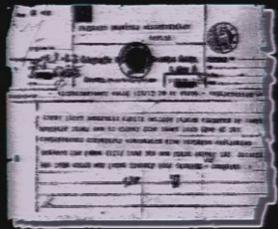
1919 Verification





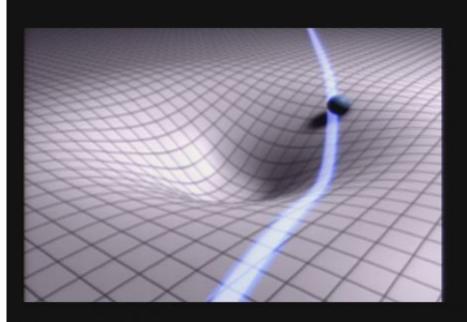


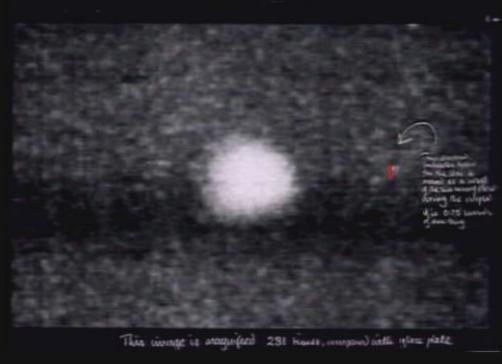




The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

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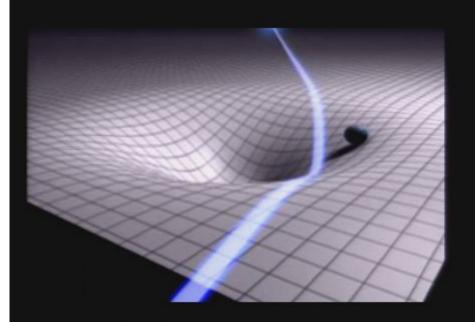








The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.



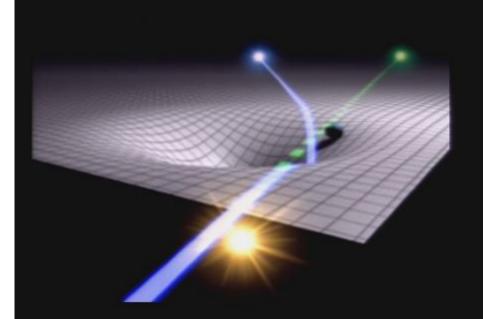








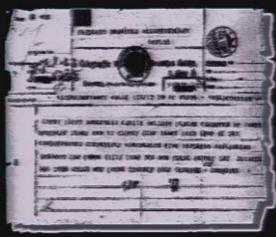
The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.





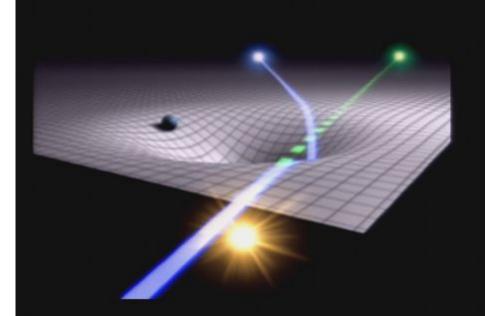


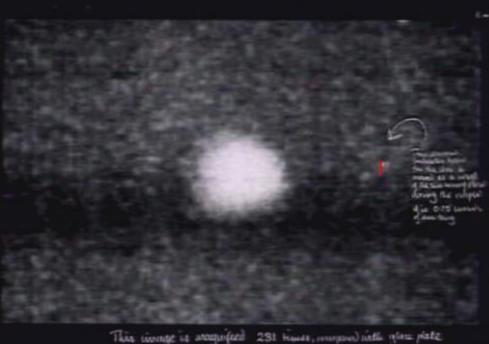




The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

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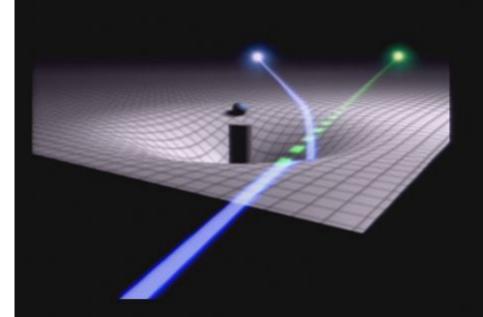








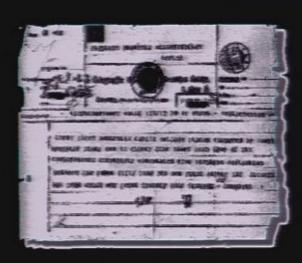
The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.



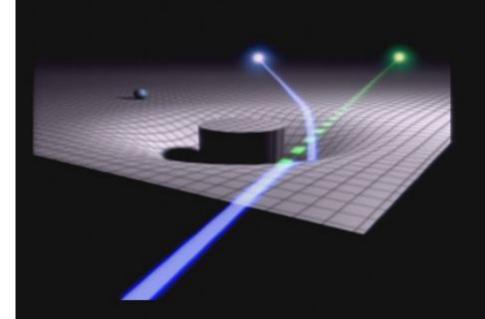








The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.





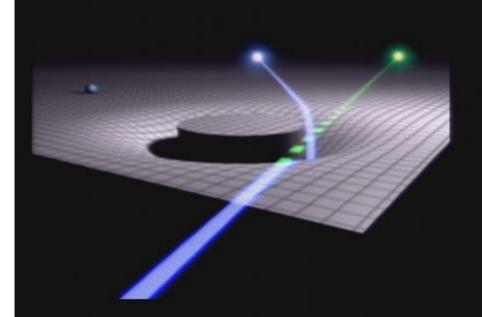






The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

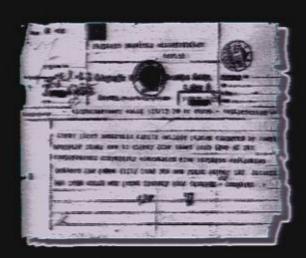
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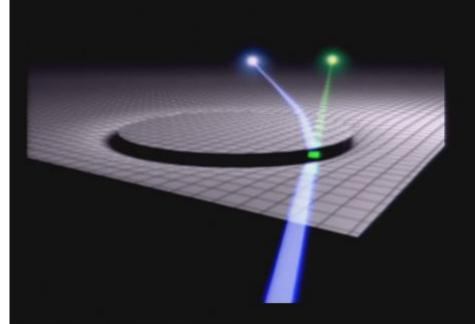








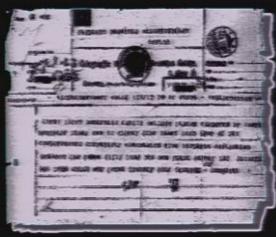
The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.





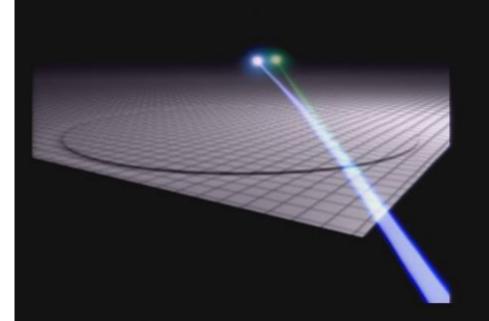






The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

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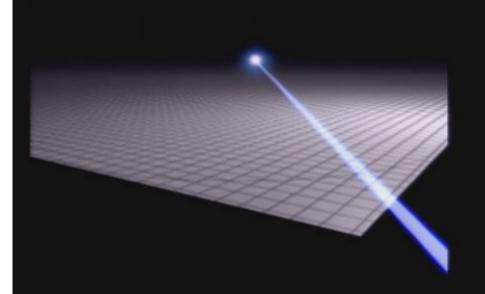


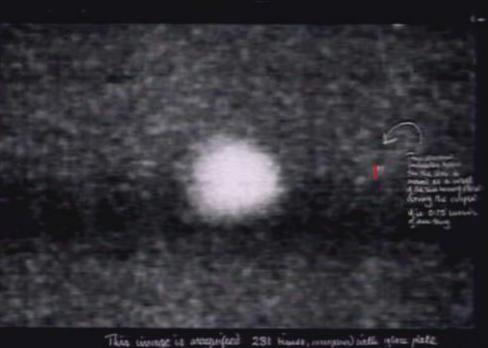




The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

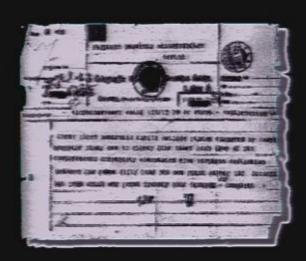
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The final proof: the small red line shows how far the position of the star has been shifted by the Sun's gravity.

65 Excess Time Delay, Microseconds





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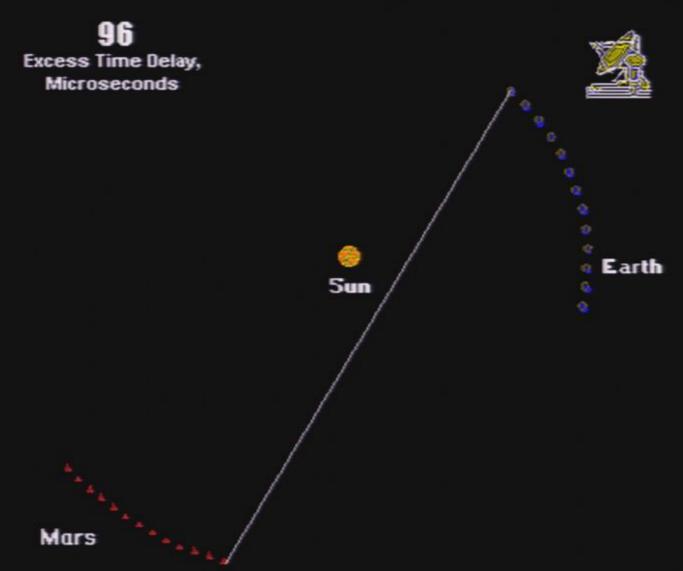
Excess Time Delay, Microseconds



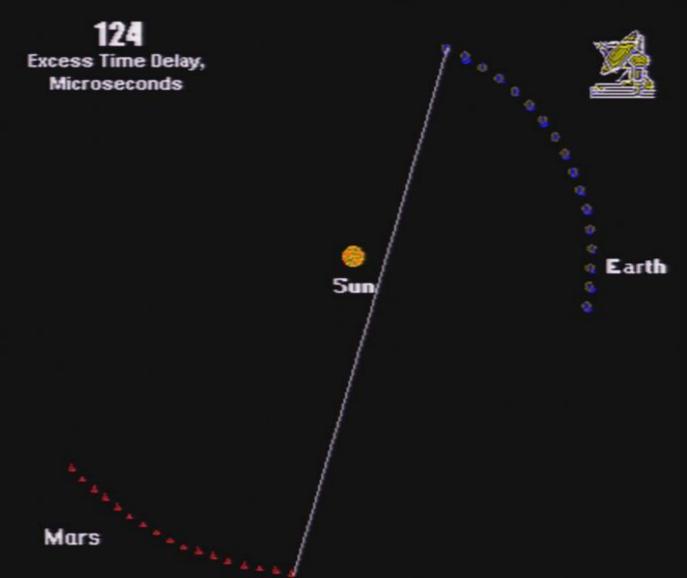


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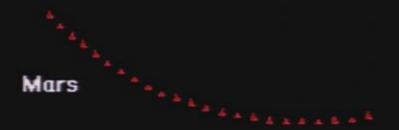
irsa: 08070046 Page 265/42:

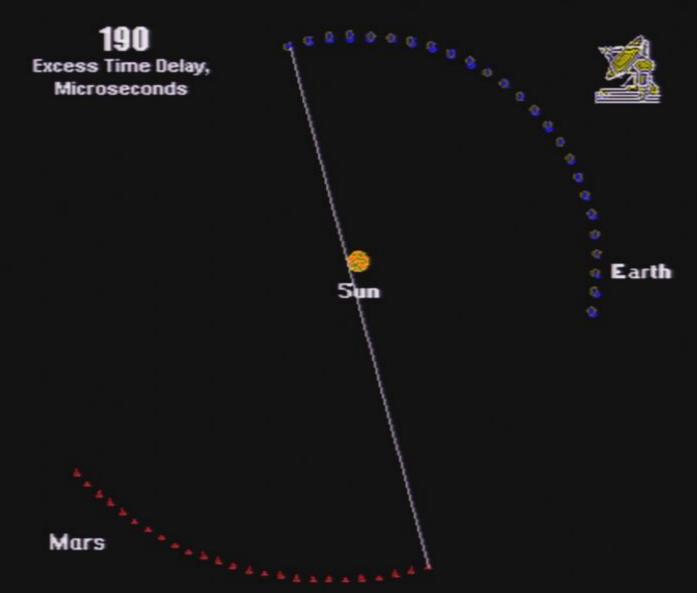


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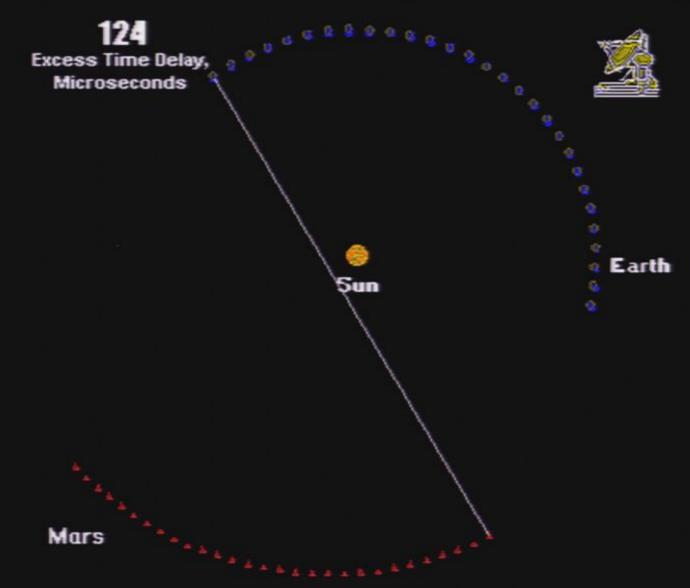
190 Excess Time Delay, Microseconds

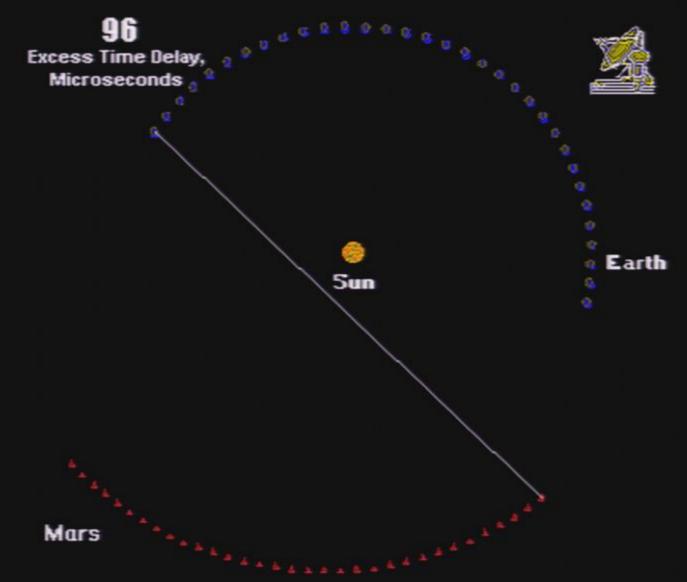




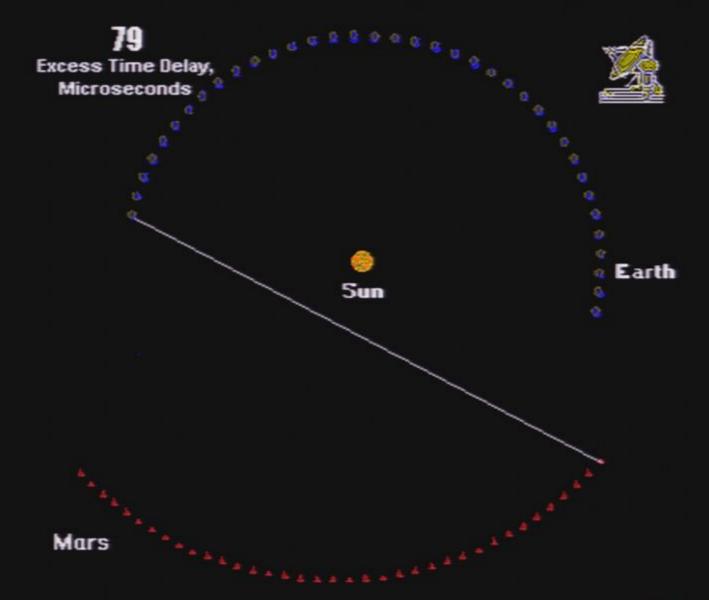


Dietance 37 km

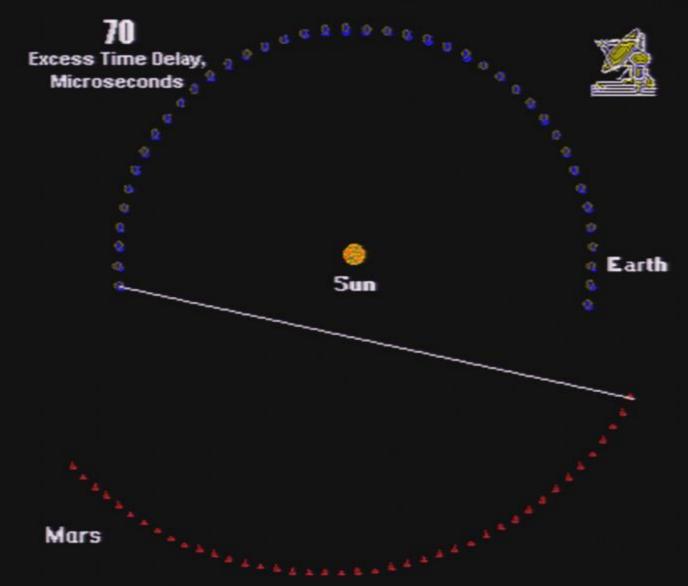




Distance 37 km



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60 Excess Time Delay, Microseconds

Mars





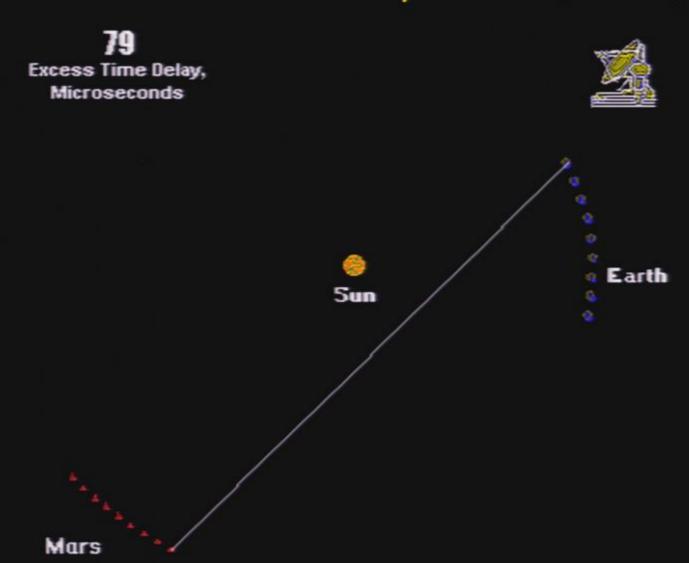
sa: 08070046 Page 273/422

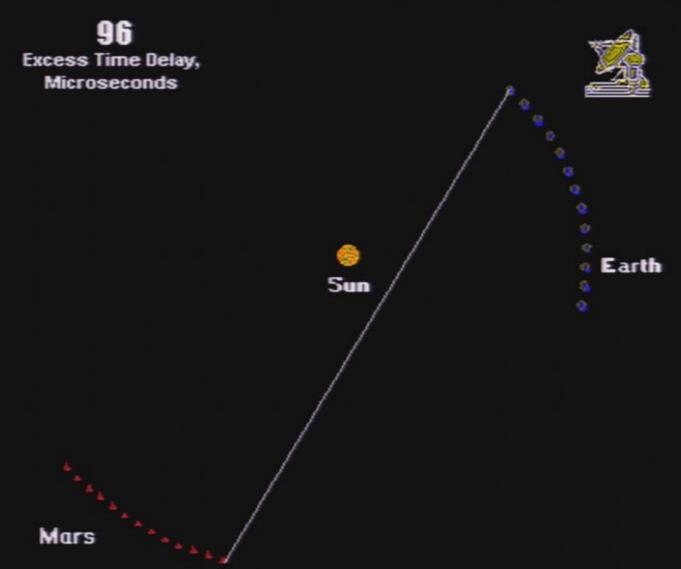
65 Excess Time Delay, Microseconds





Distance 37 km





rsa: 08070046 Page 276/42

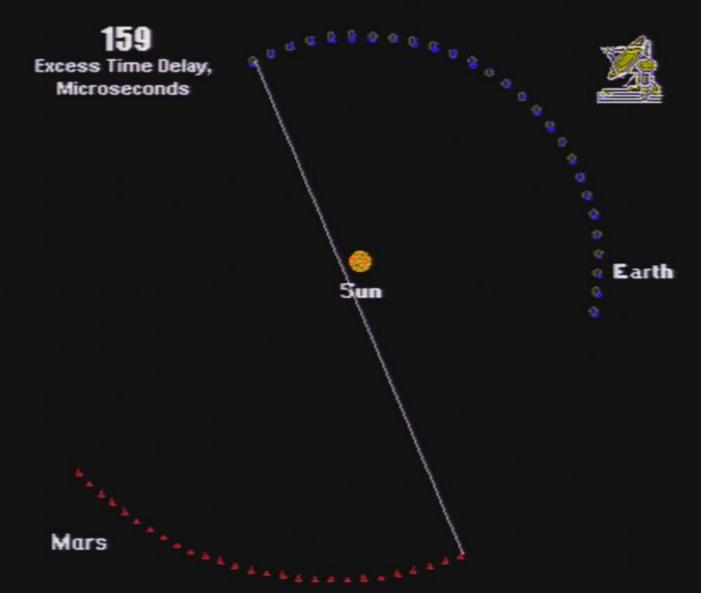


Excess Time Delay, Microseconds

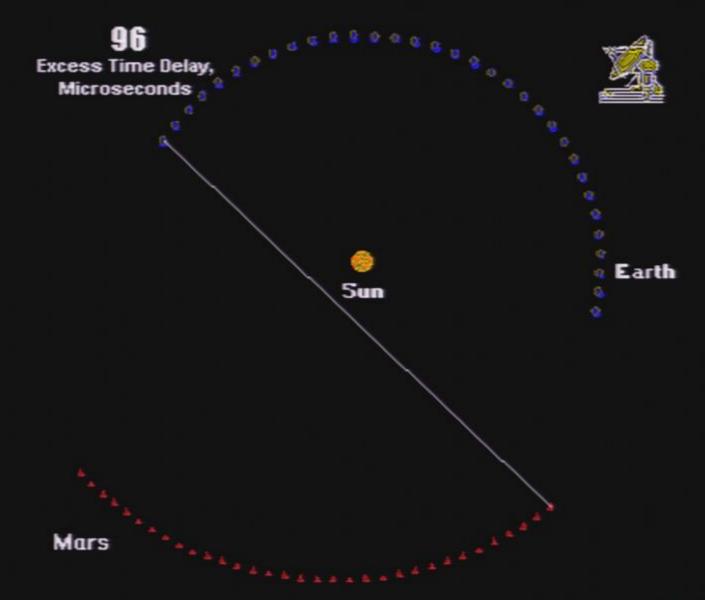




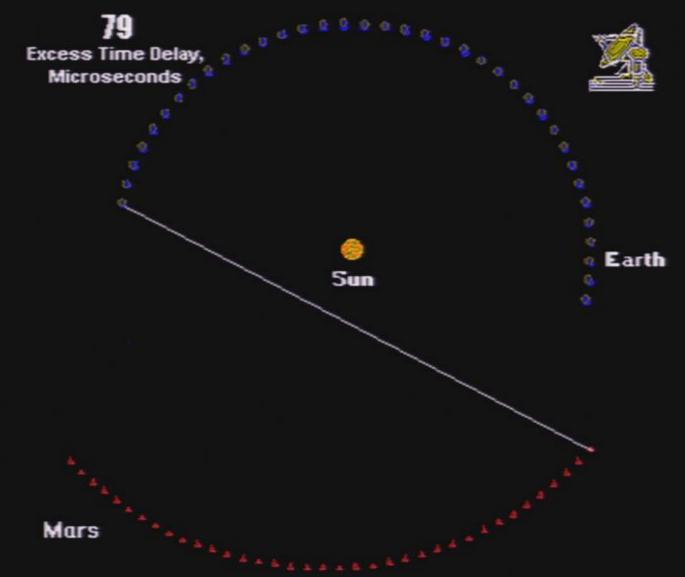
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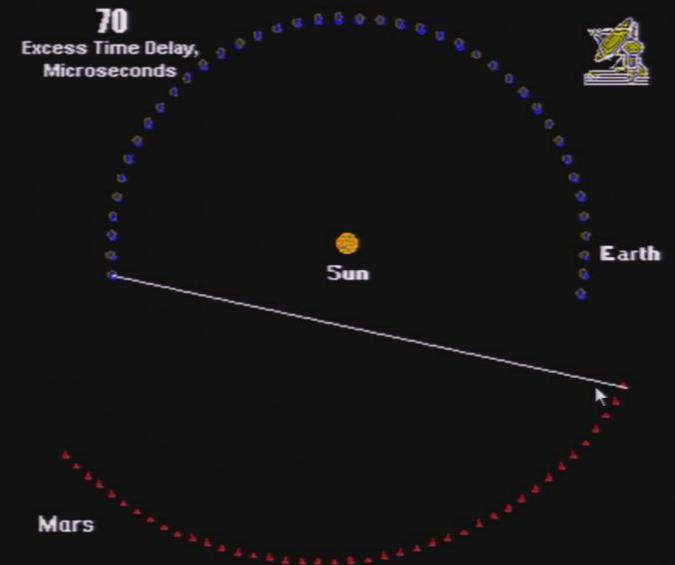
Dietance 37 km



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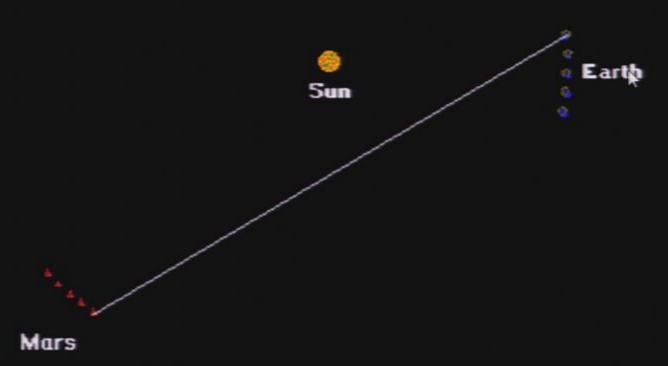




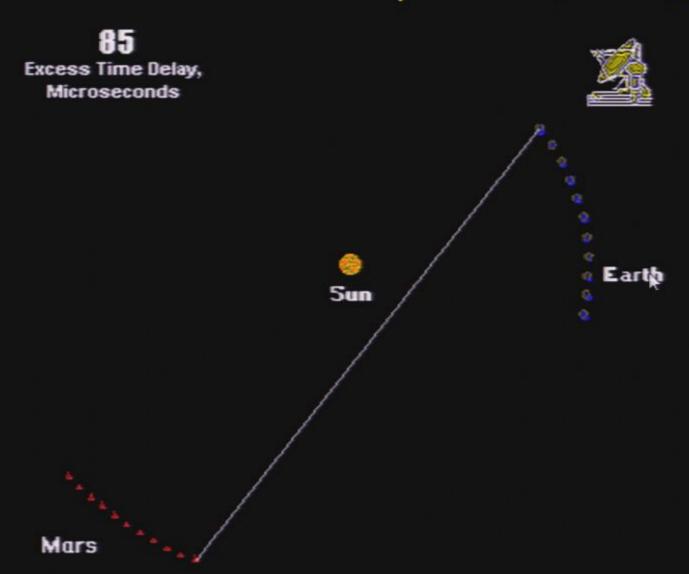
Mars

70 Excess Time Delay, Microseconds

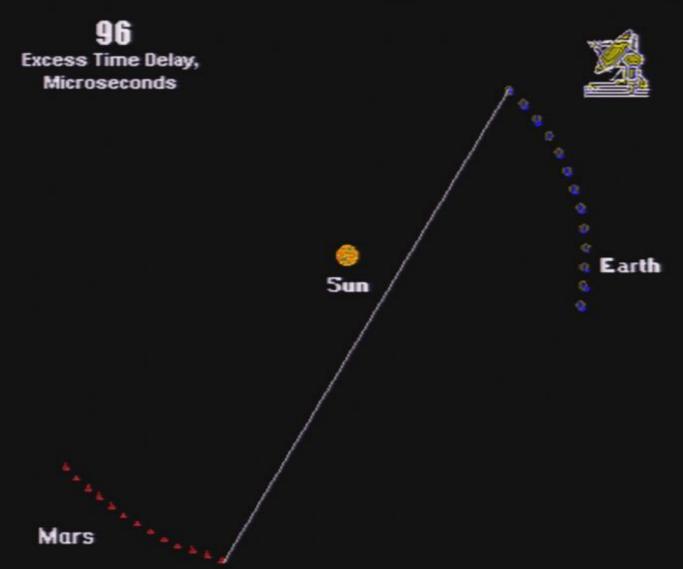




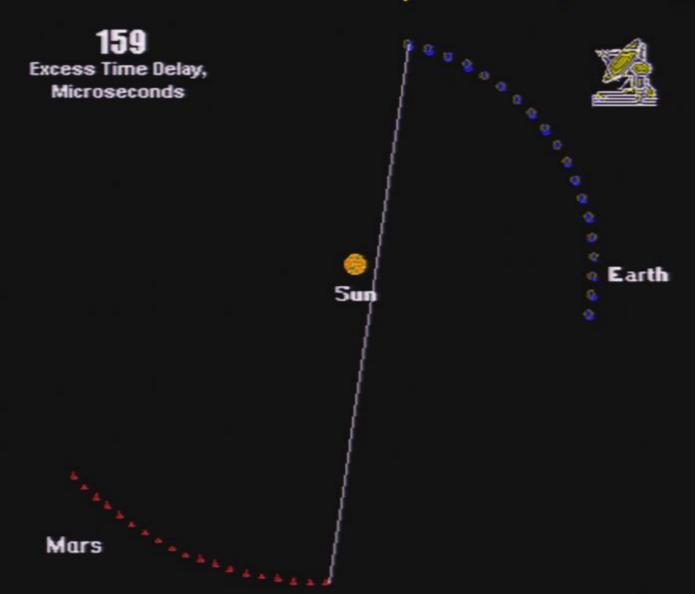
a: 08070046 Page 284/422



raye 200/422



rsa: 08070046 Page 286/42:

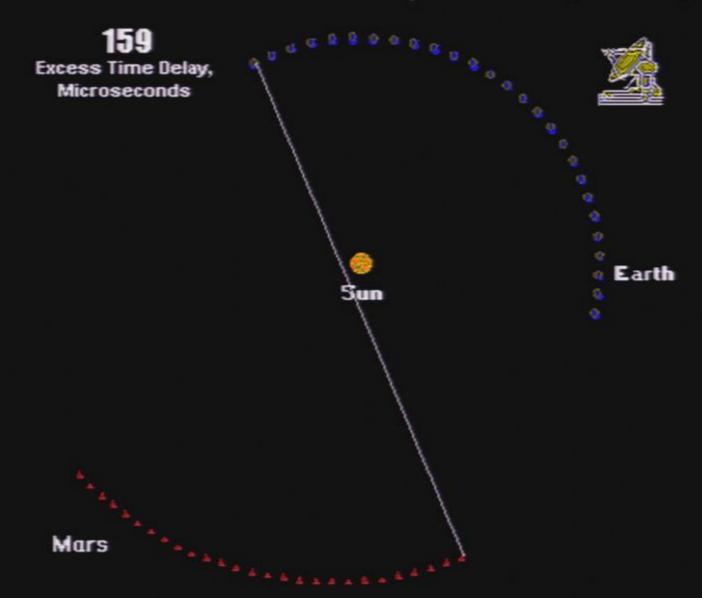


Excess Time Delay, Microseconds

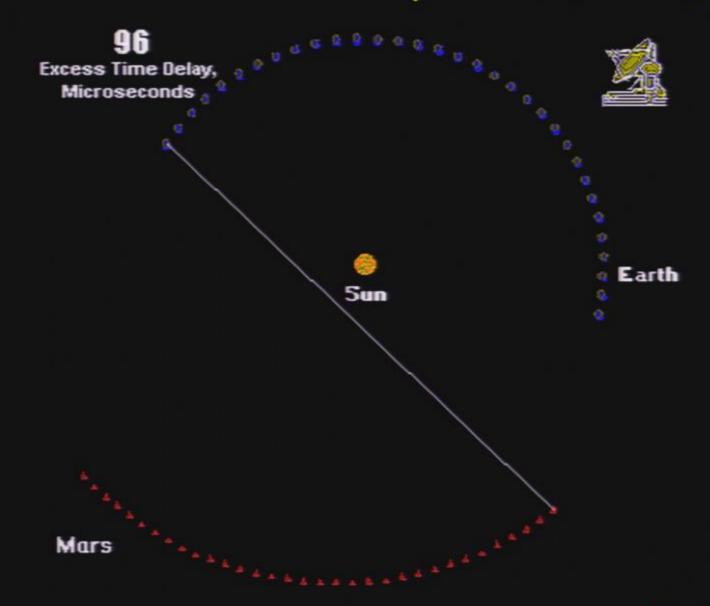




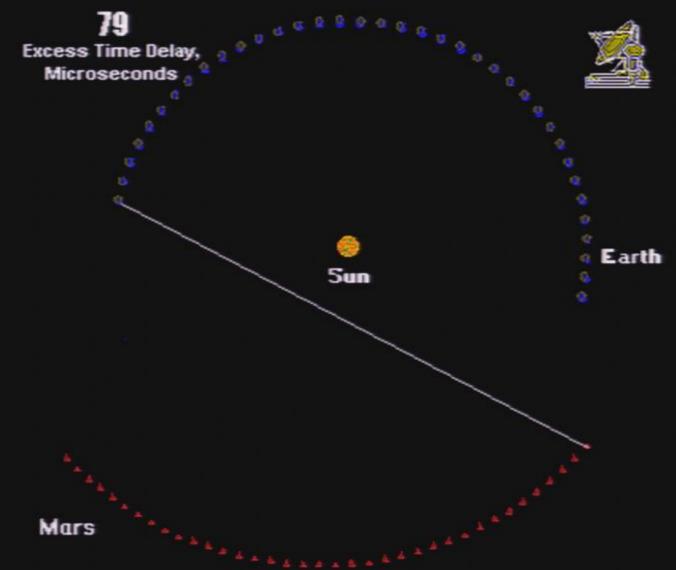
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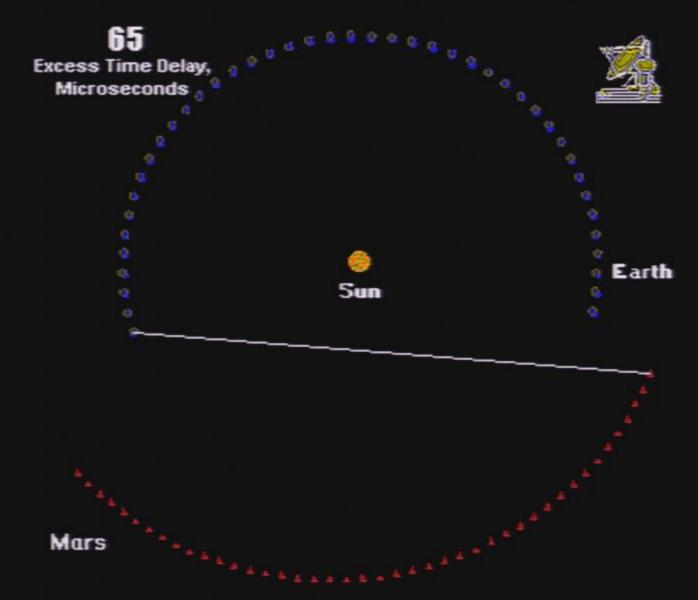
age 289/422



raye 290/422



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60 Excess Time Delay, Microseconds





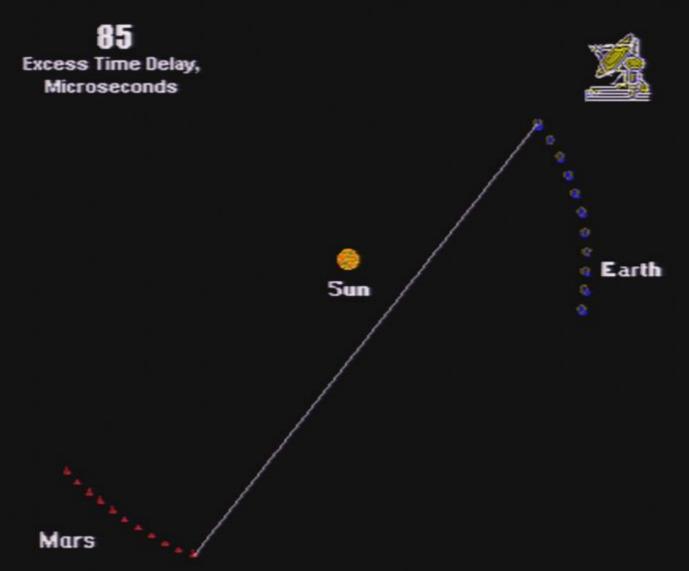
rsa: 08070046 Page 293/422

74 Excess Time Delay, Microseconds

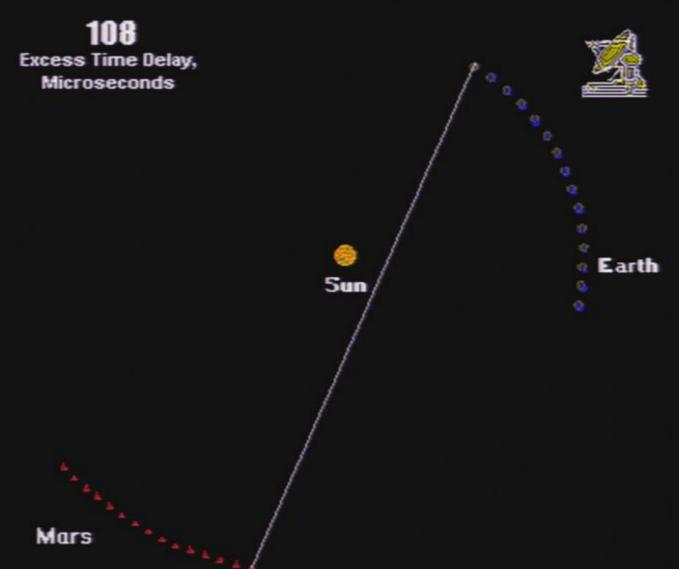




rsa: 08070046 Page 294/422



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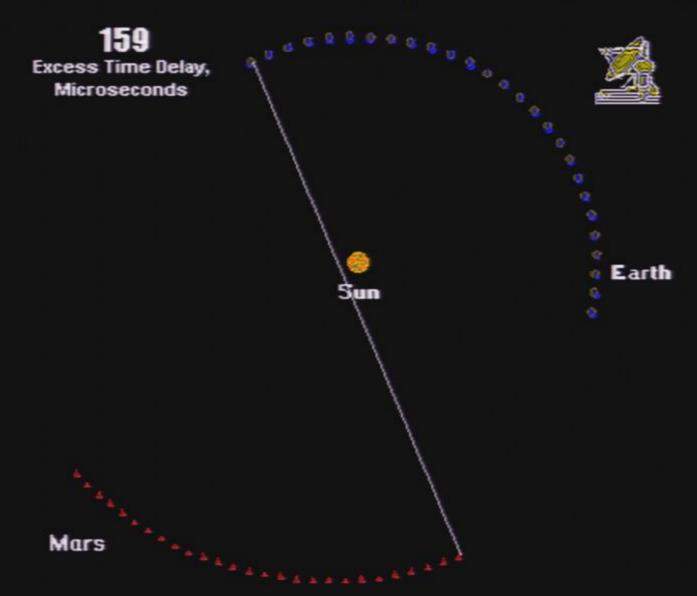


Excess Time Delay, Microseconds

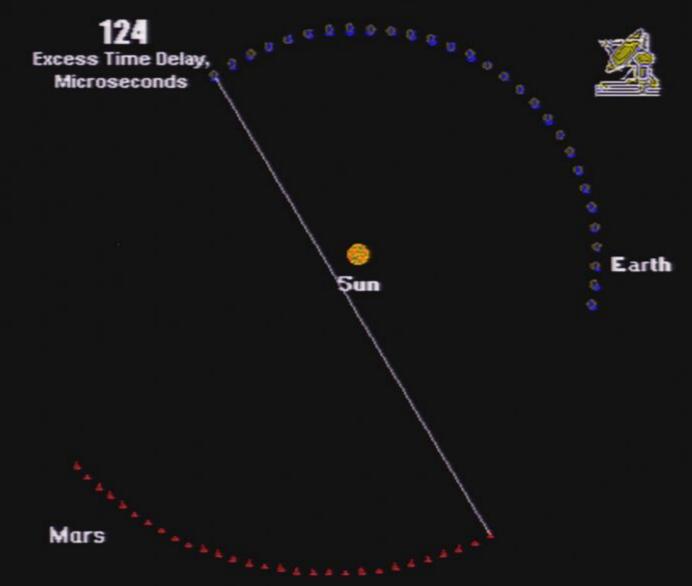


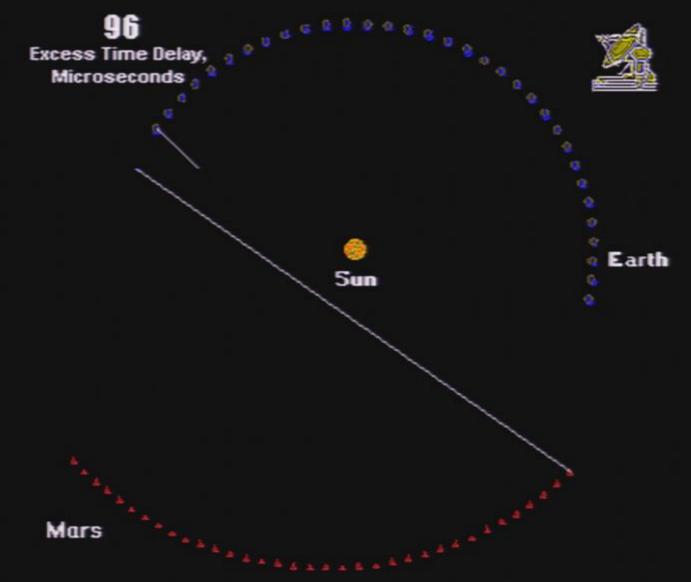


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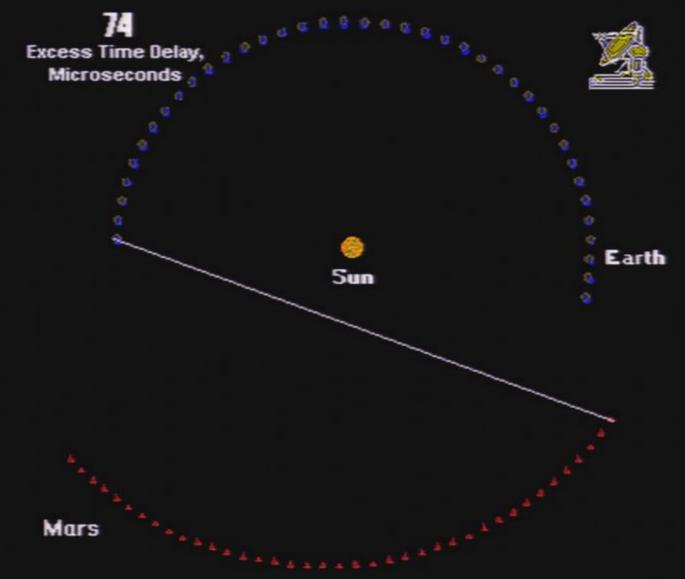


Dietance \ 37 km

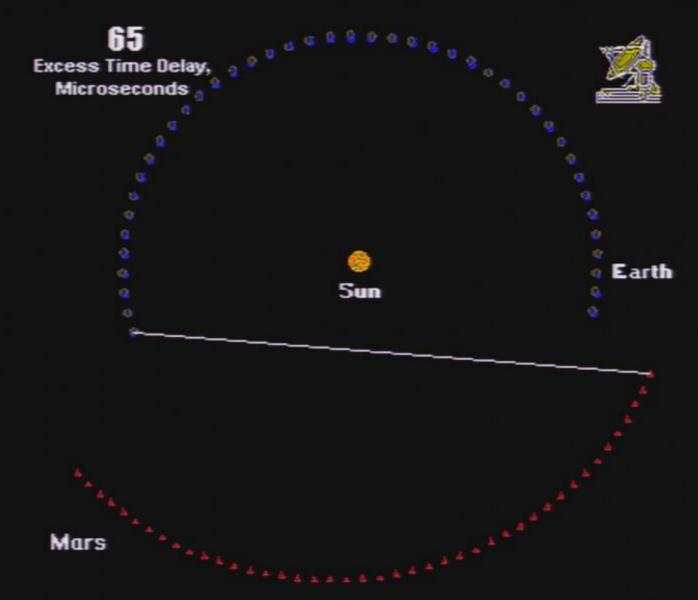




Dietance 37 km



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60 Excess Time Delay, Microseconds

Mars





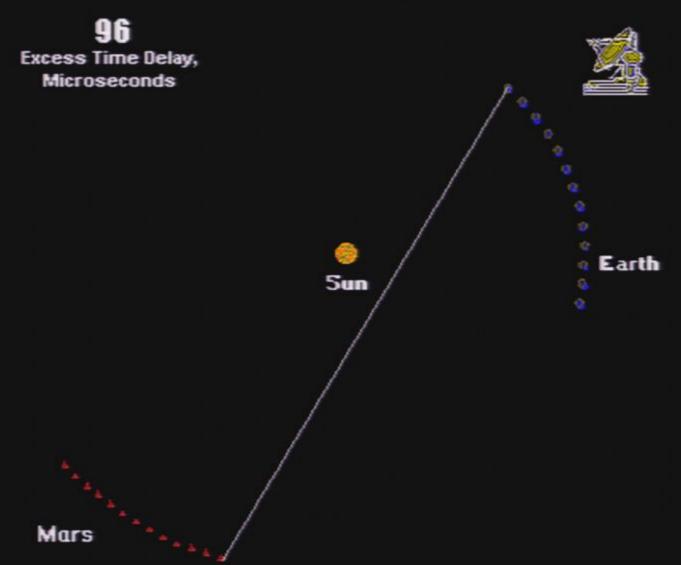
sa: 08070046 Page 304/422

74 Excess Time Delay, Microseconds

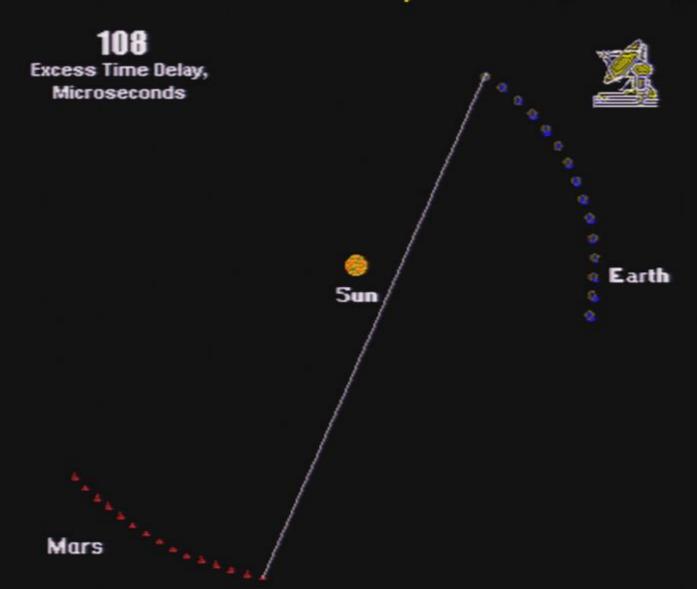




Pirsa: 08070046 Page 305/422

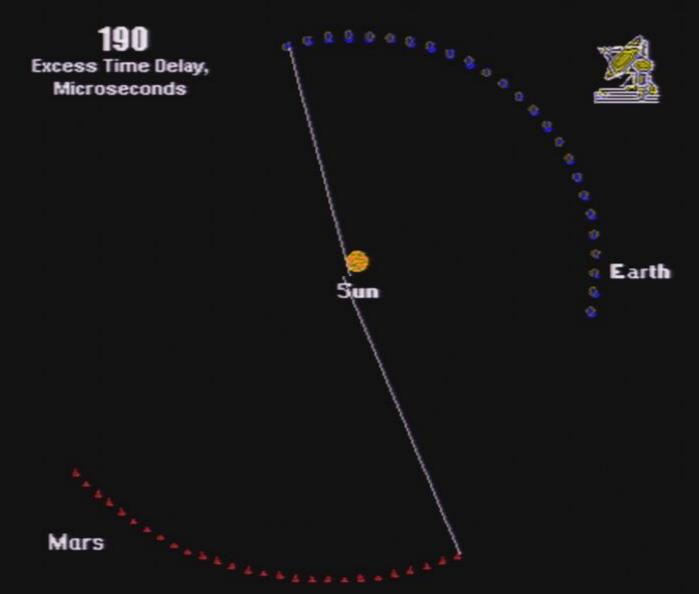


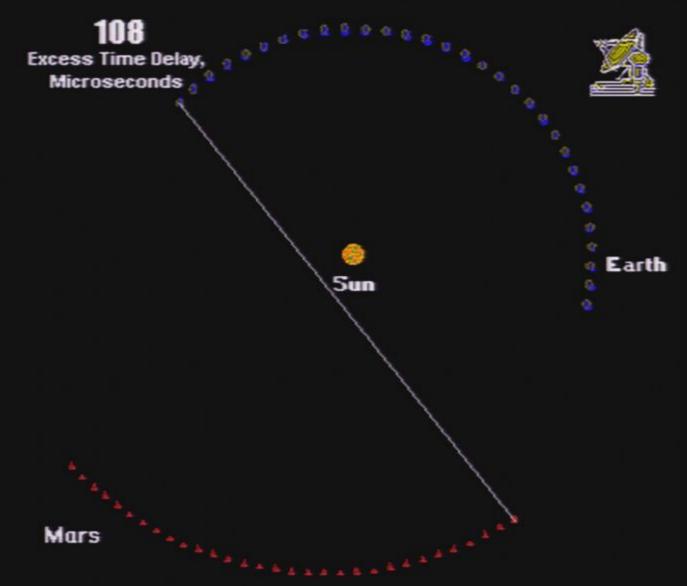
irsa: 08070046 Page 306/422



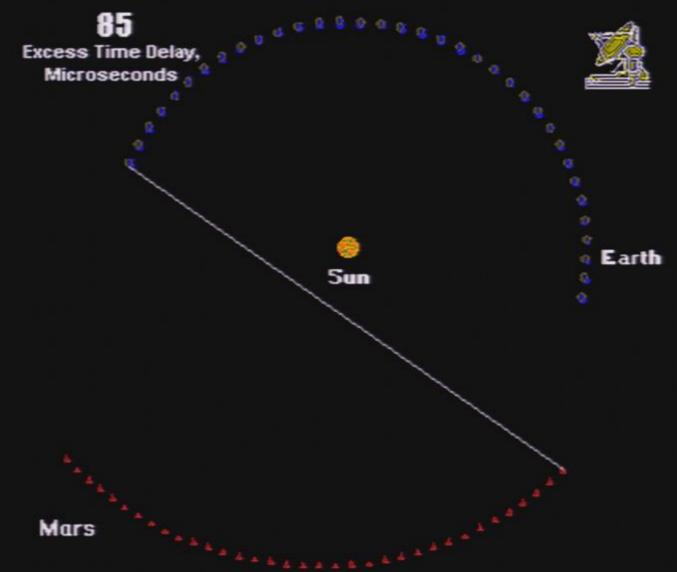
1 ago 301/422

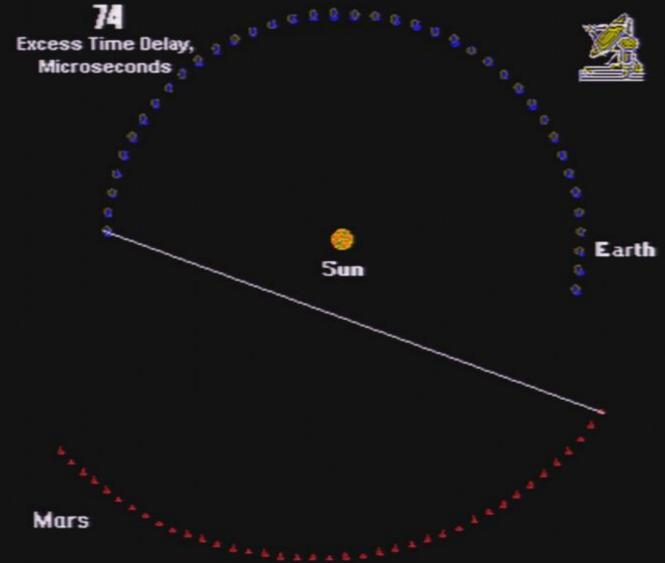


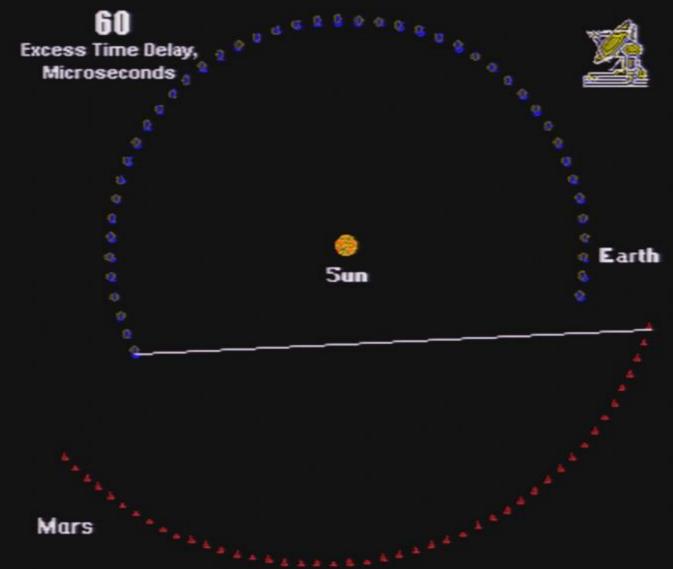




Dietance 37 km







1 age 513-422

60 Excess Time Delay, Microseconds

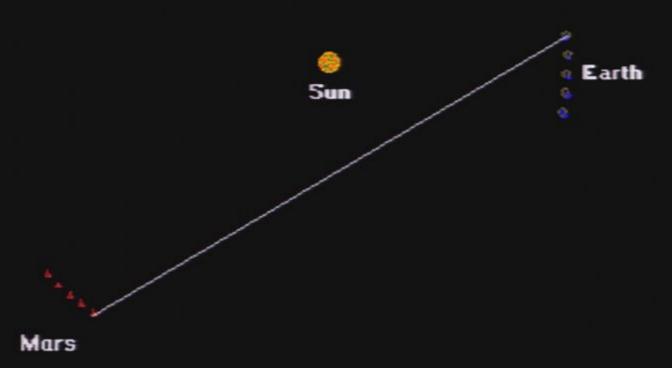




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70 Excess Time Delay, Microseconds





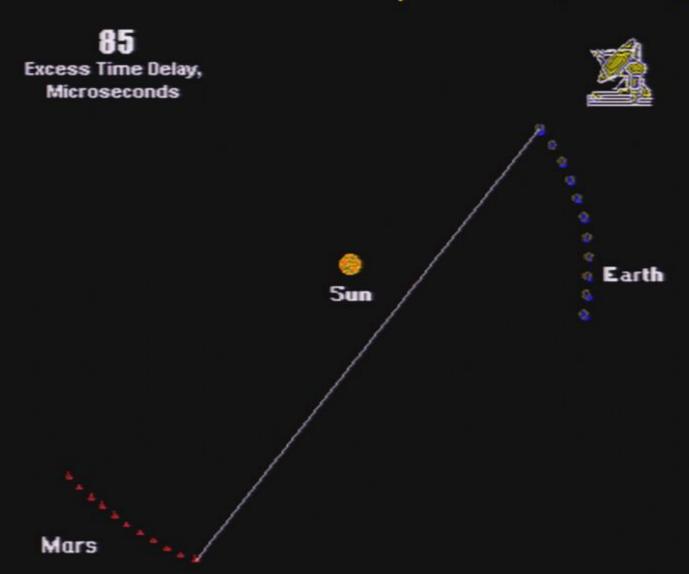
rsa: 08070046 Page 315/422

74 Excess Time Delay, Microseconds

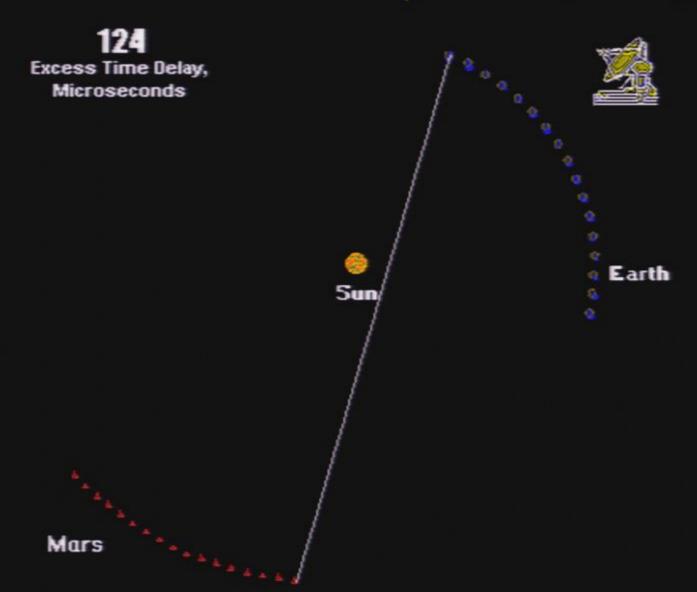




rsa: 08070046 Page 316/422

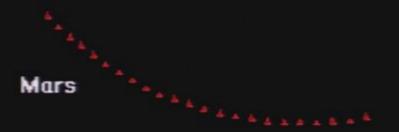


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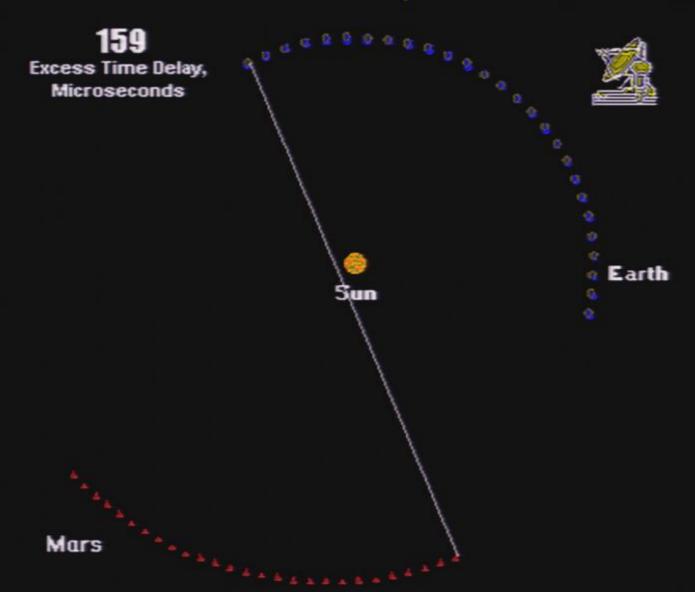


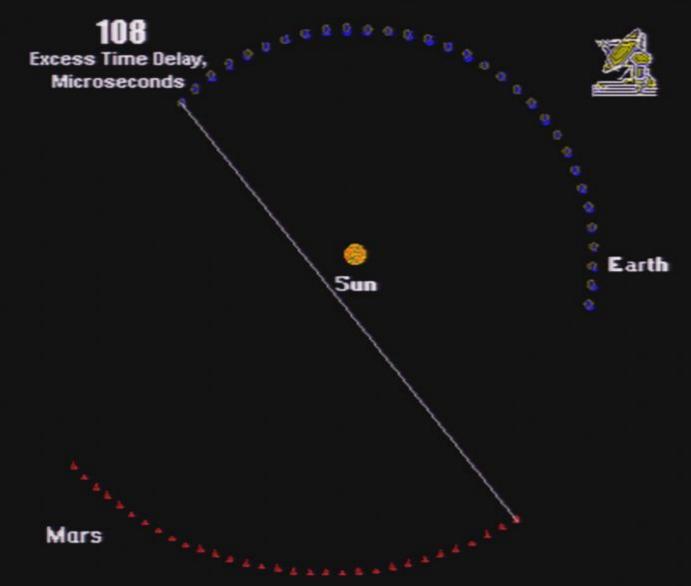
Excess Time Delay, Microseconds



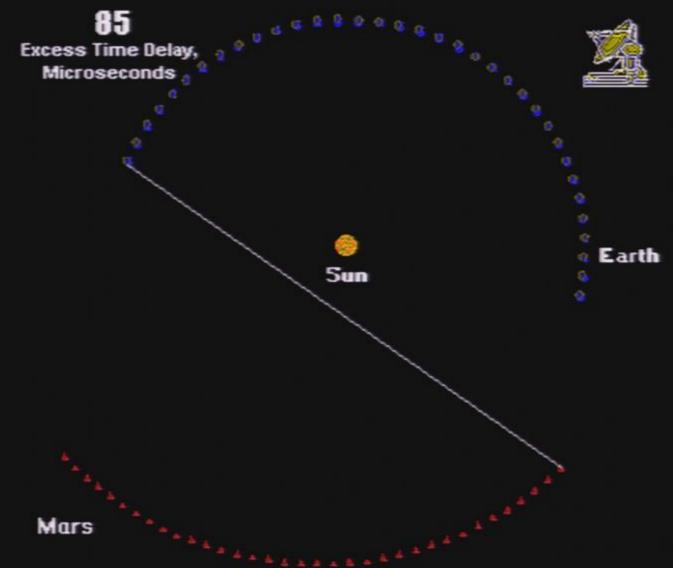


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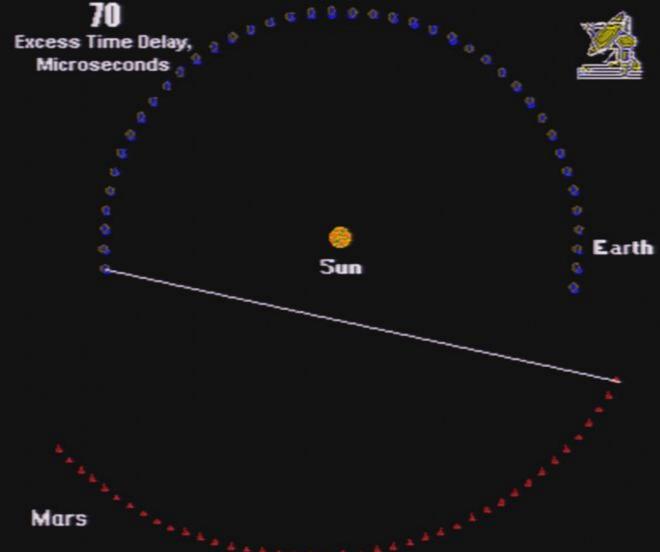




Dietance 37 km



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60 Excess Time Delay, Microseconds

Mars



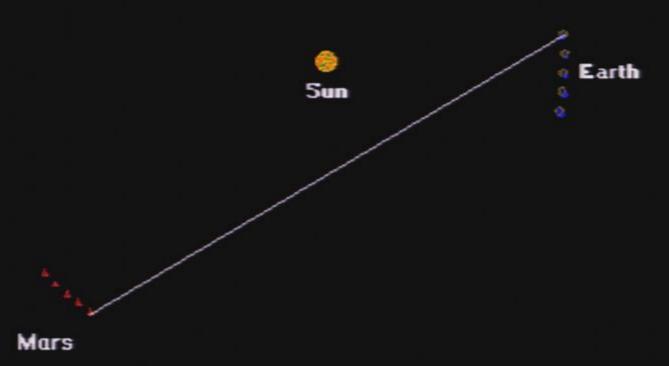


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General Relativity Test (1976)

70 Excess Time Delay, Microseconds





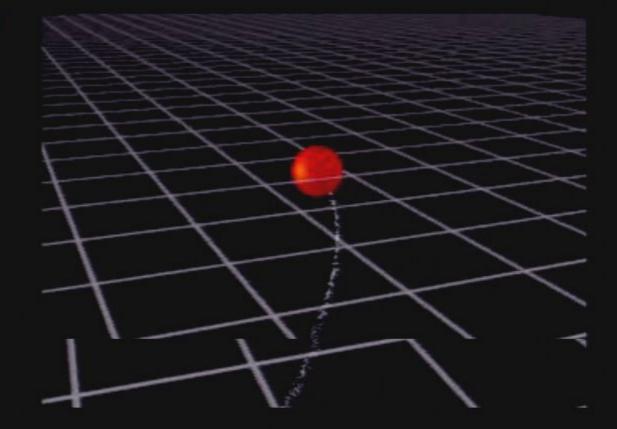
rsa: 08070046 Page 325/422

- Mercury's precession did not agree with Newton's Laws
- Out by 43 arc seconds per century.
- Einstein's Theory accounted for this 43 arc seconds



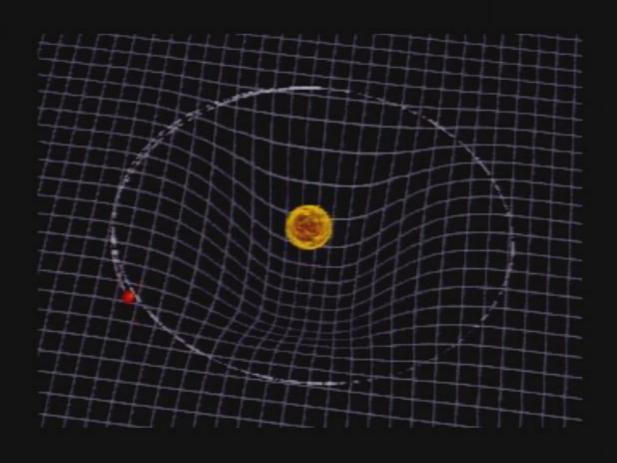
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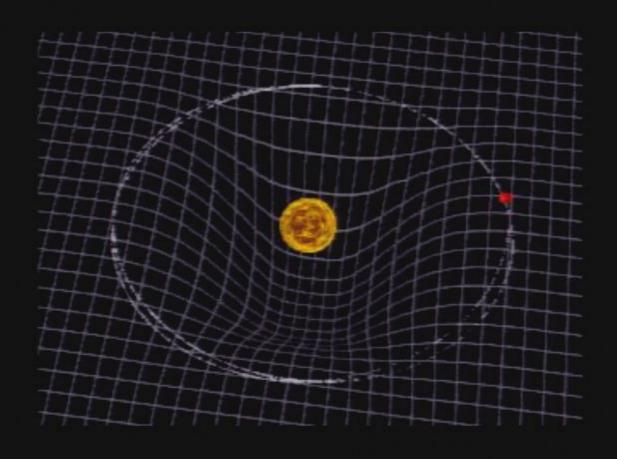
Pirsa: 08070046 Page 327/422

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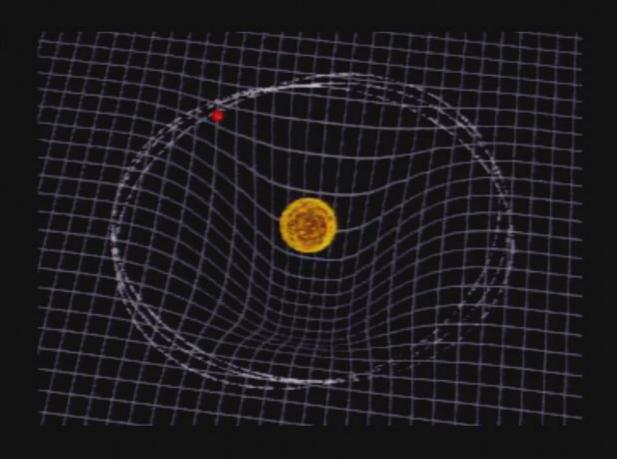
Pirsa: 08070046 Page 328/422

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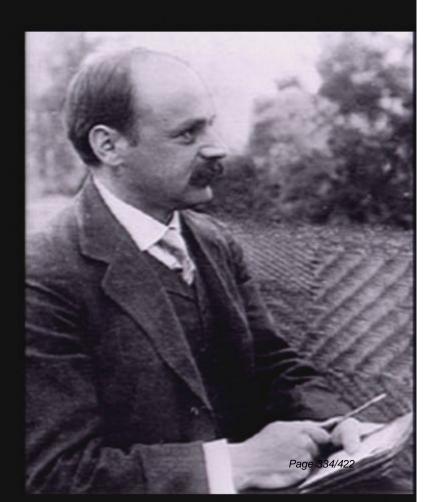
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What to do with the Field Equations

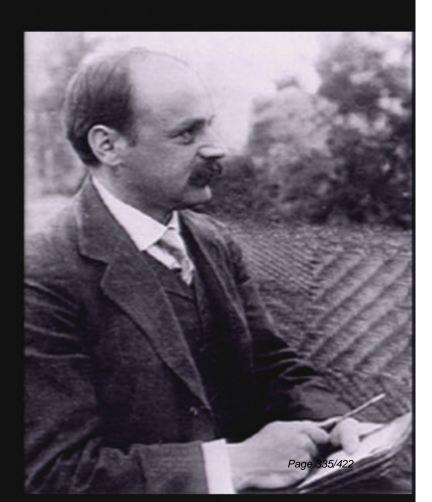
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Pirsa: 08070046 Page 333/422

In 1916 Karl Schwarzschild discovers a olution of the Einstein field equation, which describes a nonspinning, incharged spherical body.

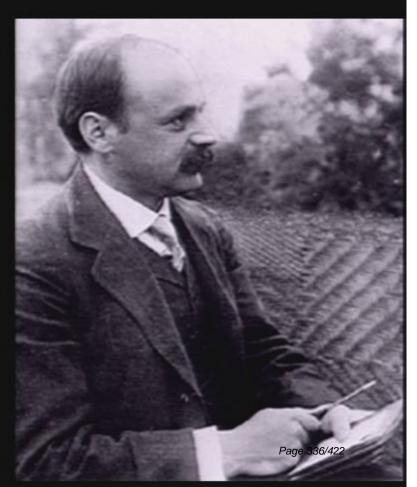


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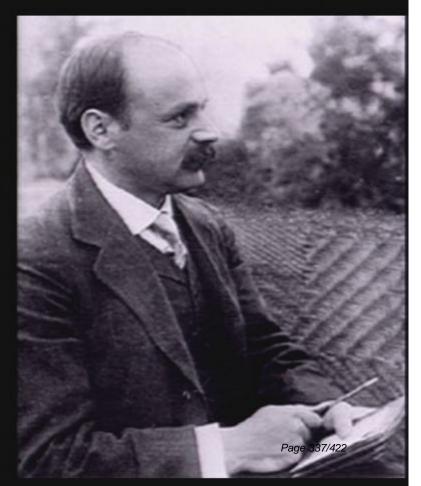
Did this when serving in the German Army on the Russian front of World War I



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Only required a few days to solve equation and describe spacetime curvature.

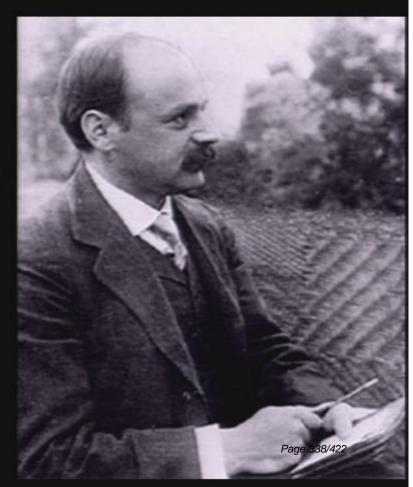


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Einstein presented solution on behalf of Schwarzschild to the Academy of Sciences.



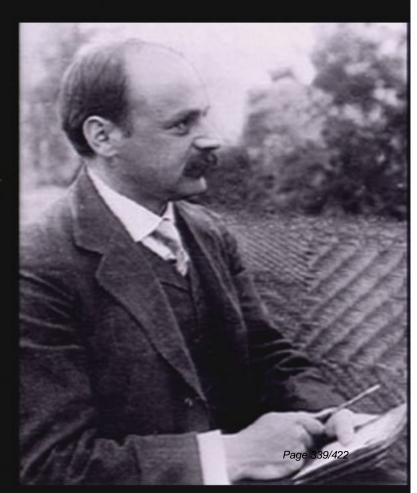
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Schwarzschild died on the front 4 nonths later.



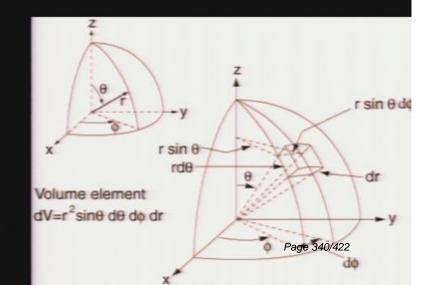
The Schwarzschild Radius

$$d\sigma^2 = -\left(1 - \frac{r_s}{r}\right)c^2dt^2 + \frac{dr^2}{\left(1 - \frac{r_s}{r}\right)} + r^2\left(d\theta^2 + \sin^2(\theta)d\phi^2\right)$$

Curvature factor

$$r_s = \frac{2GM}{c^2}$$

 r, θ, ϕ are the polar coordinates



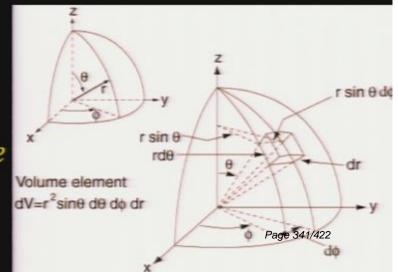
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Pirsa: 08070046

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Pirsa: 08070046 Page 346/422

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Pirsa: 08070046 Page 347/422

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is the Schwarzschild radius

tr = r = Space time Metric



$$\tau^2 = t^2 - s^2$$
 Timelike Spacetime Metric

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$$d\tau^2 = dt^2 - dx^2 - dy^2$$
 2D flat Spacetime in Cartesian

It is the square of the wristwatch time between two events as marked by x, y, t

ŀ

$$d\tau)^2 = (dt)^2 - (dr)^2 - (rd\phi)^2$$
 2D flat Spacetime in Polar

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$$(d\tau)^2 = (dt)^2 - (dr)^2 - (rd\phi)^2$$

2D flat Spacetime in Polar

$$d\tau^{2} = \left(1 - \frac{r_{s}}{r}\right)c^{2}dt^{2} - \frac{dr^{2}}{\left(1 - \frac{r_{s}}{r}\right)} - r^{2}d\phi^{2}$$

Curvature added, now Schwarzschild timelike Spacetime Metric

$$r_s = \frac{2GM}{c^2}$$

$$d\sigma^{2} = -\left(1 - \frac{2M}{r}\right)dt^{2} + \frac{dr^{2}}{\left(1 - \frac{2M}{r}\right)} + r^{2}d\phi^{2}$$

The metric describes the shape of spacetime outside of matter. Once you hit matter, be it some gas, a star, a planet, or a rock, this metric no longer applies.

You can see that, if r = 2M, dt term would be zero. That is to say that at the event horizon there would be no change in time. Makes sense; you can look at the event horizon as being the place where time "stops". The dr factor deals with "how close to something you are. You'll notice that it "blows up" when r = 2M? ""

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Spacelike Form

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Timelike Form

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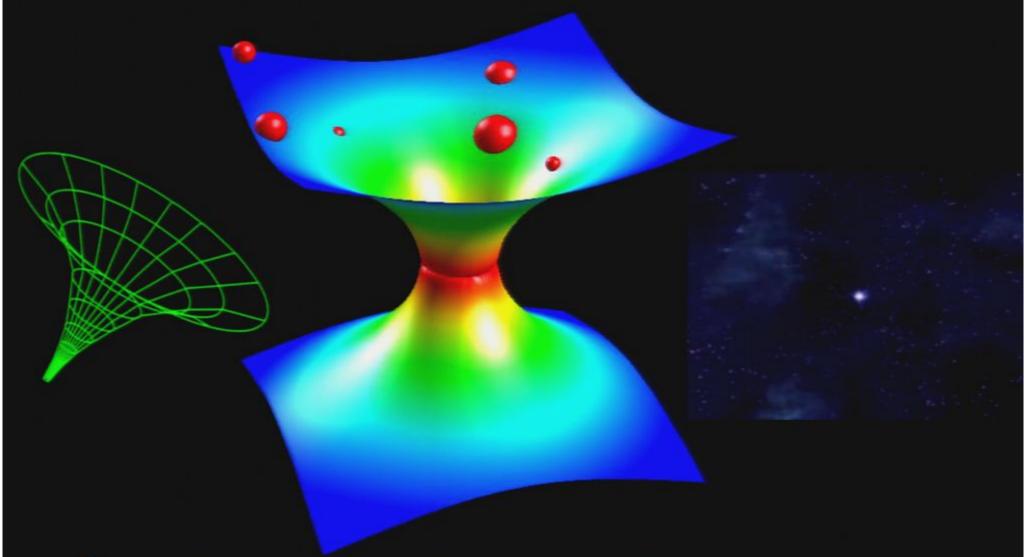
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Schwarzchild radii for different objects

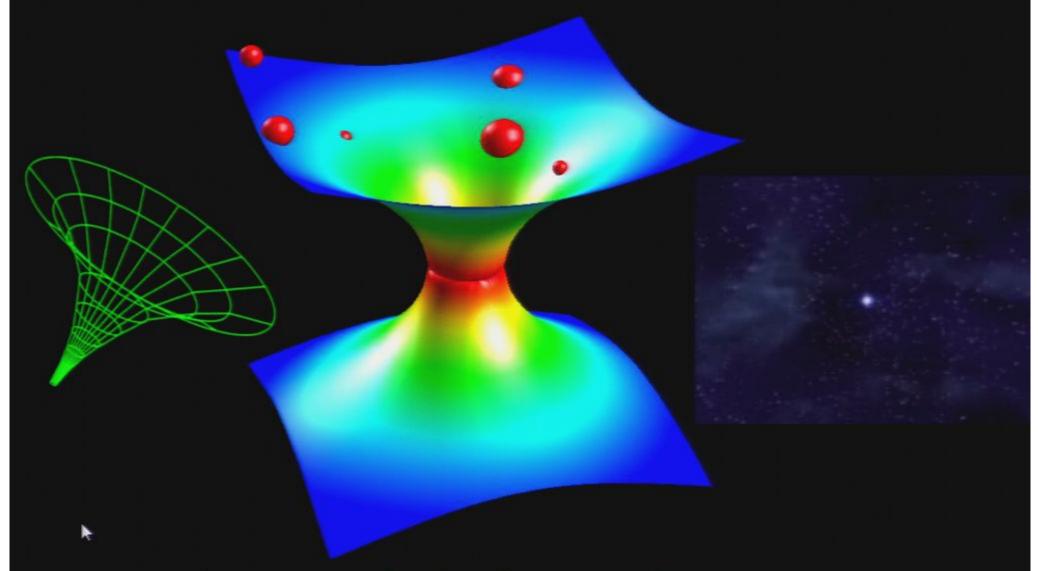
Object	Mass	R_{S}
Atom	10^{-26} kg	10^{-51} cm
Human Being	70 kg	10^{-23} cm
Earth	$6.0\times10^{24}~\mathrm{kg}$	$0.89~\mathrm{cm}$
Sun	$2.0\times10^{30}~\mathrm{kg}$	$3.0~\mathrm{km}$
Galaxy	$10^{11} \ M_{\rm S}$	10^{-2} l.y.
Universe (if closed)	$10^{23} \ M_{ m S}$	10 ¹⁰ l.y.

$$r_{s} = \frac{2GM}{c^{2}}$$

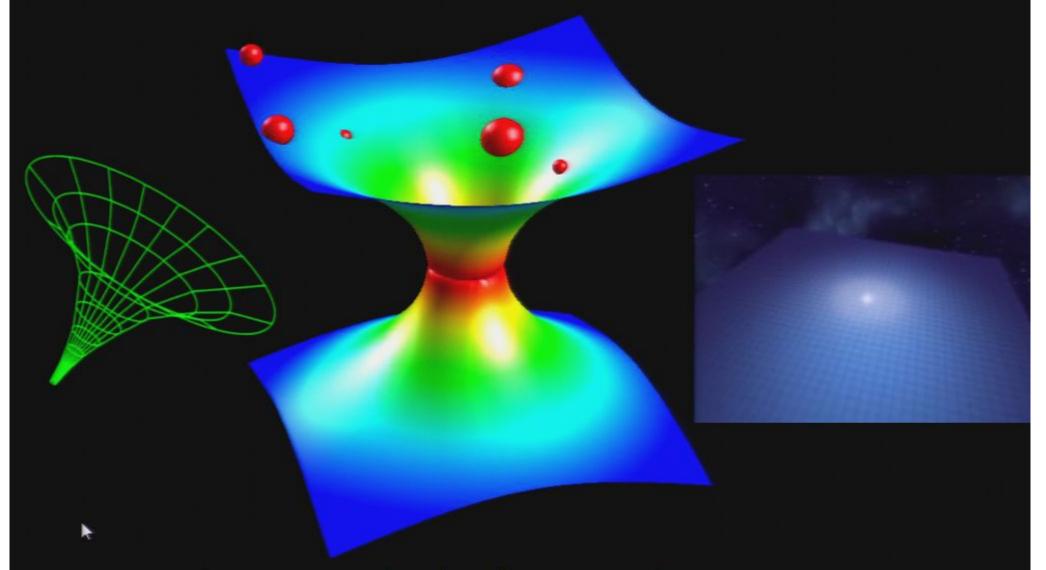




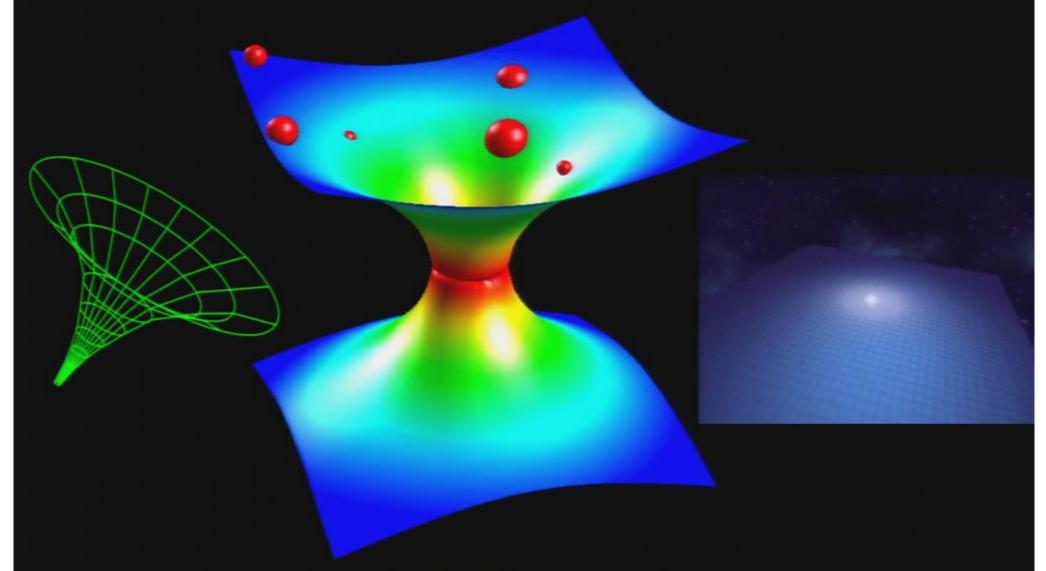


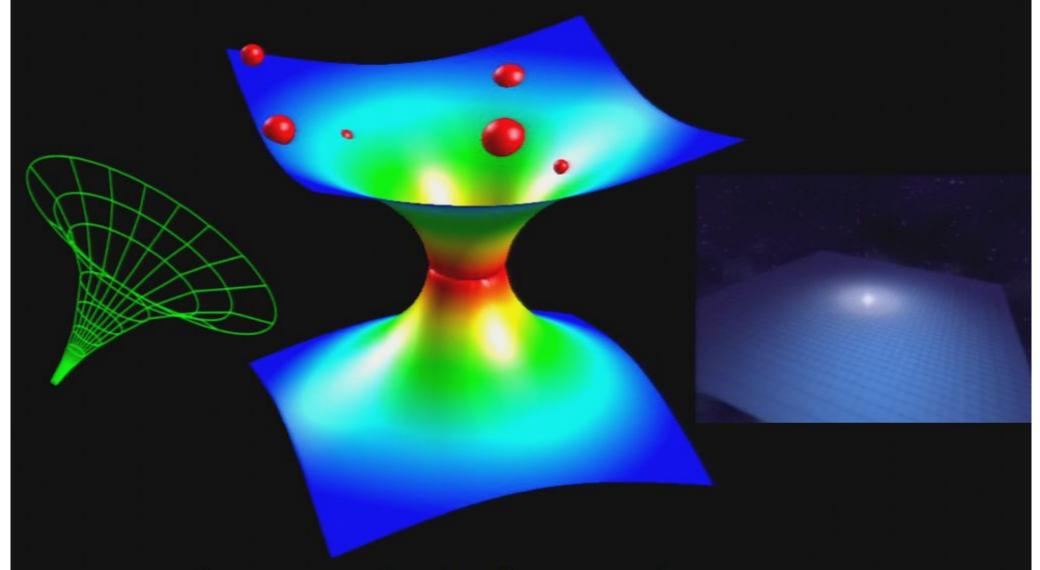


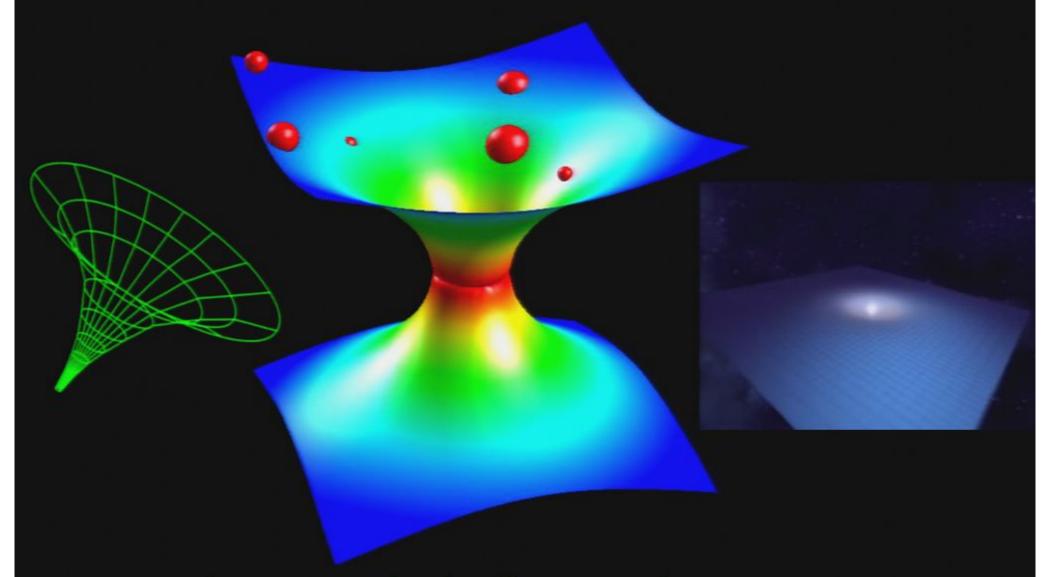
Emphasis on Spatial rather than temporal interpretations

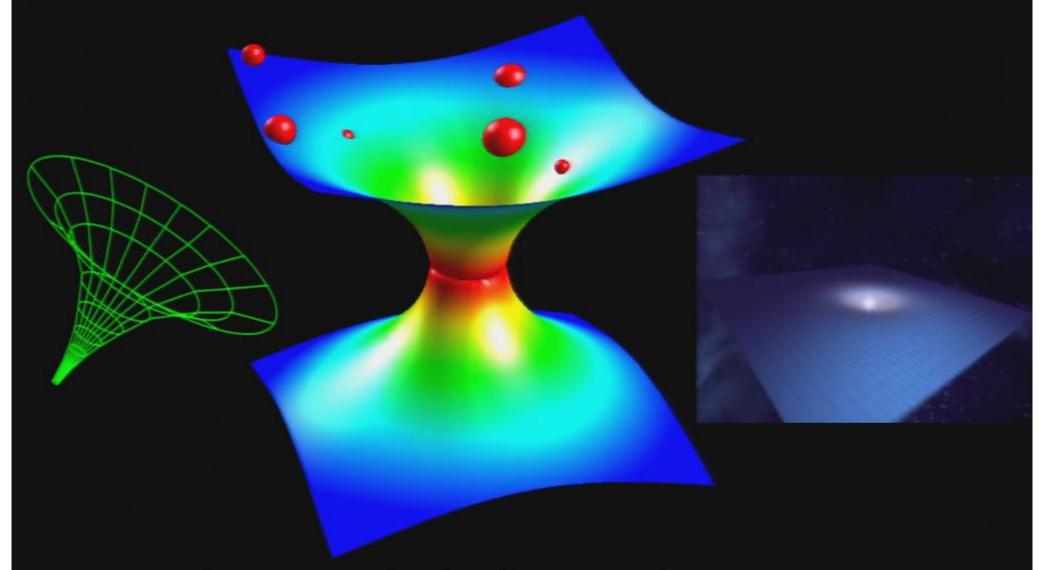


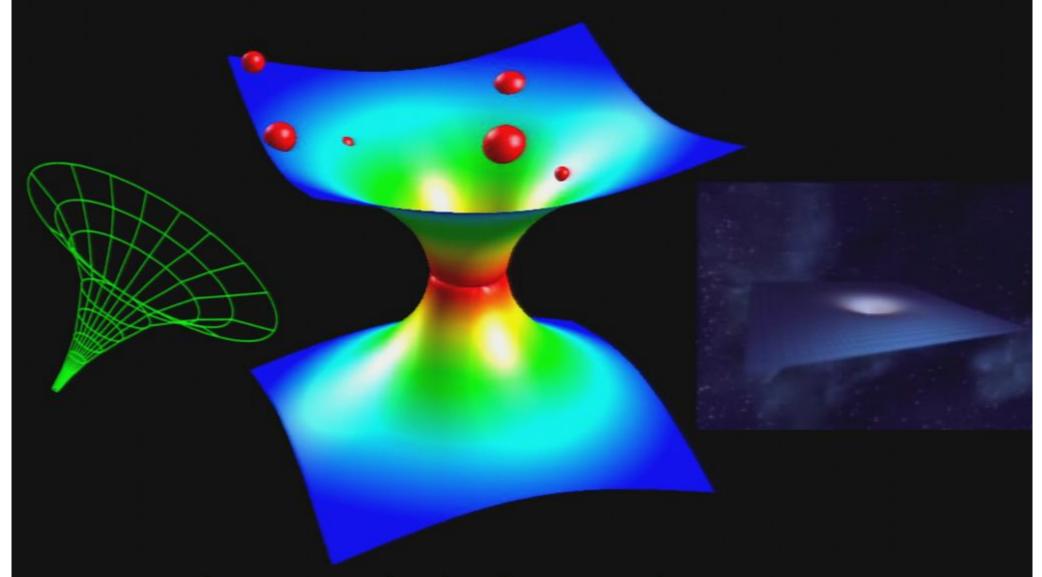
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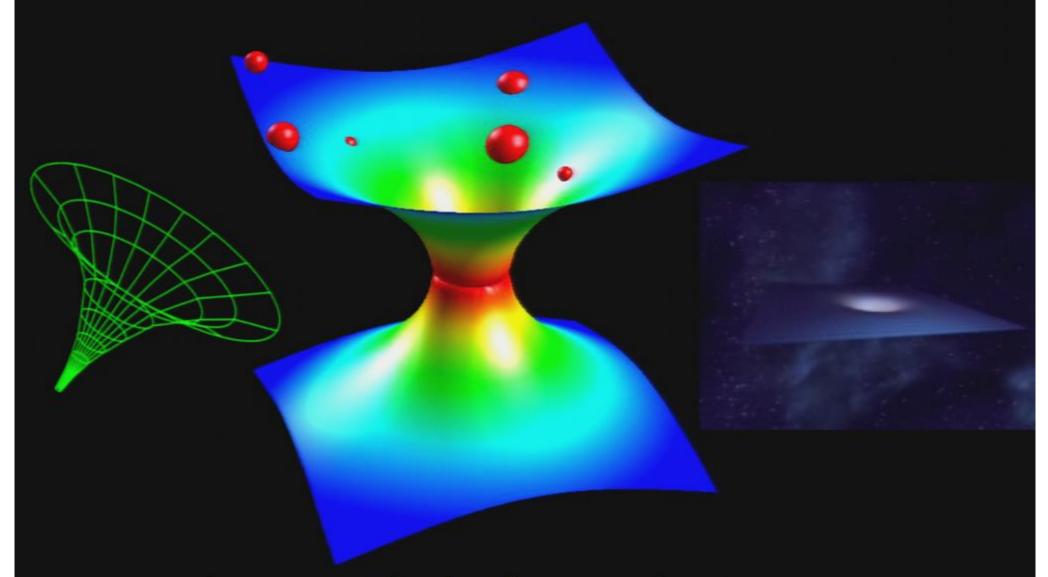


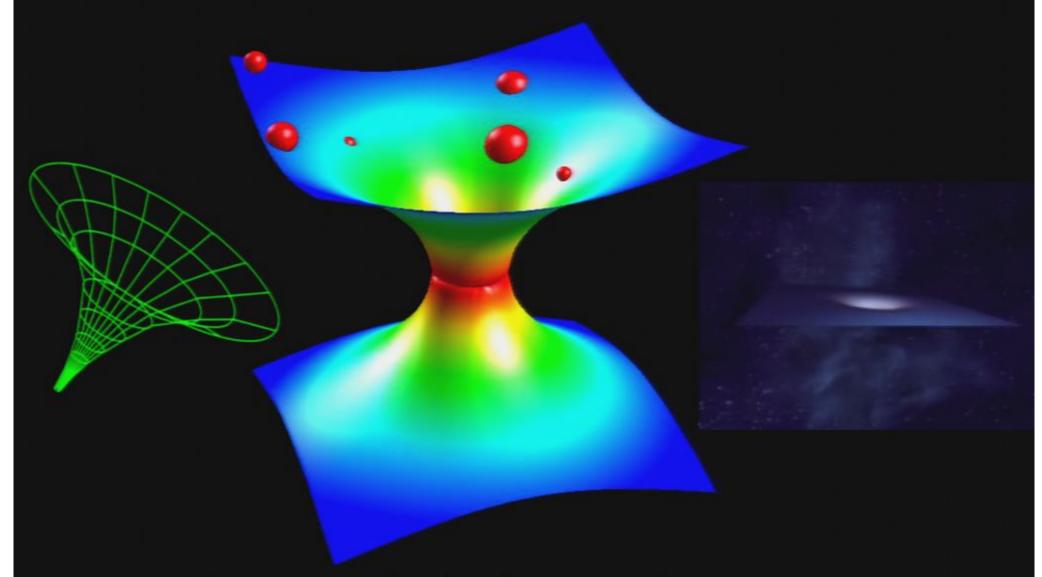


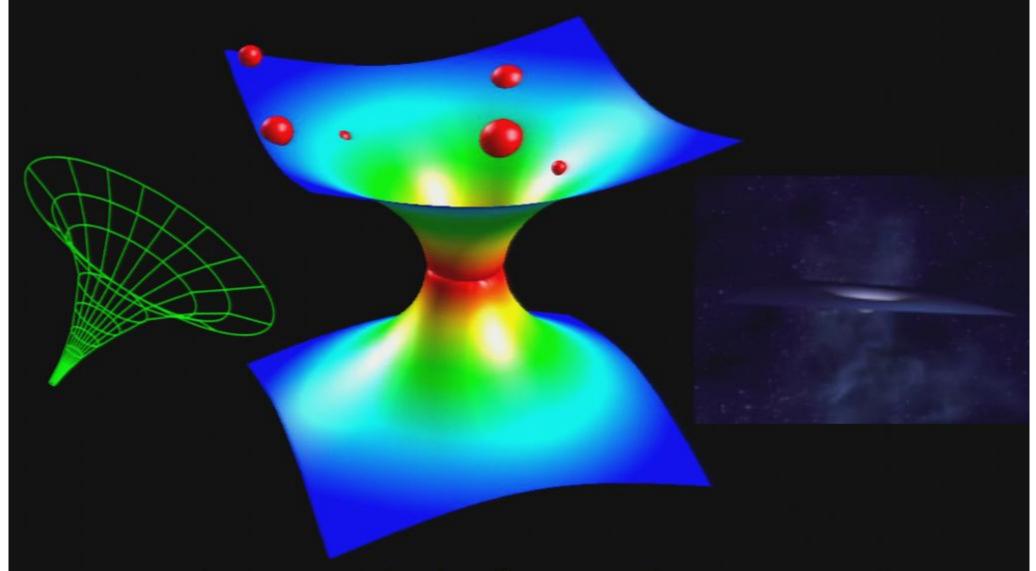


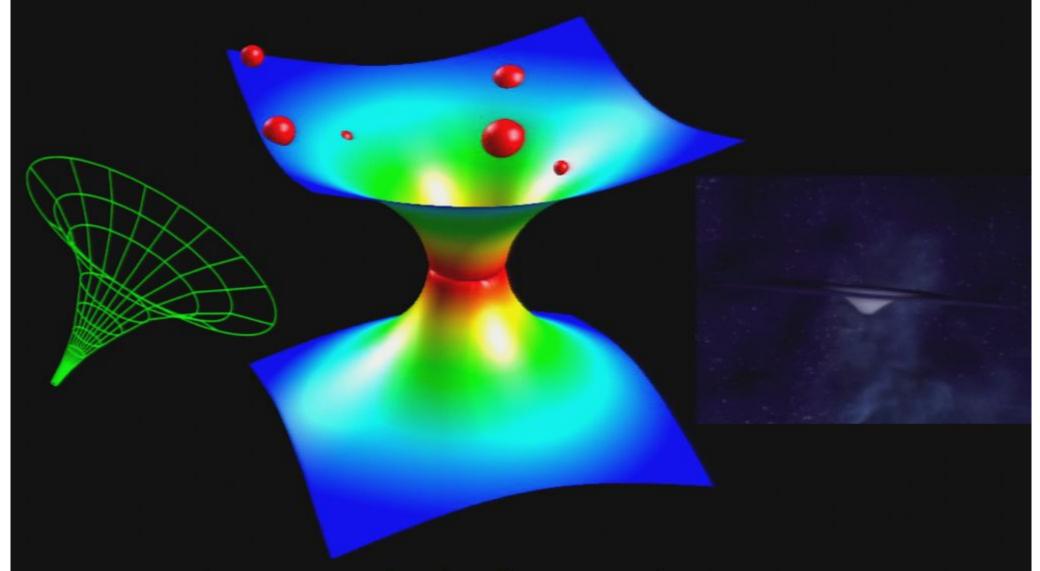


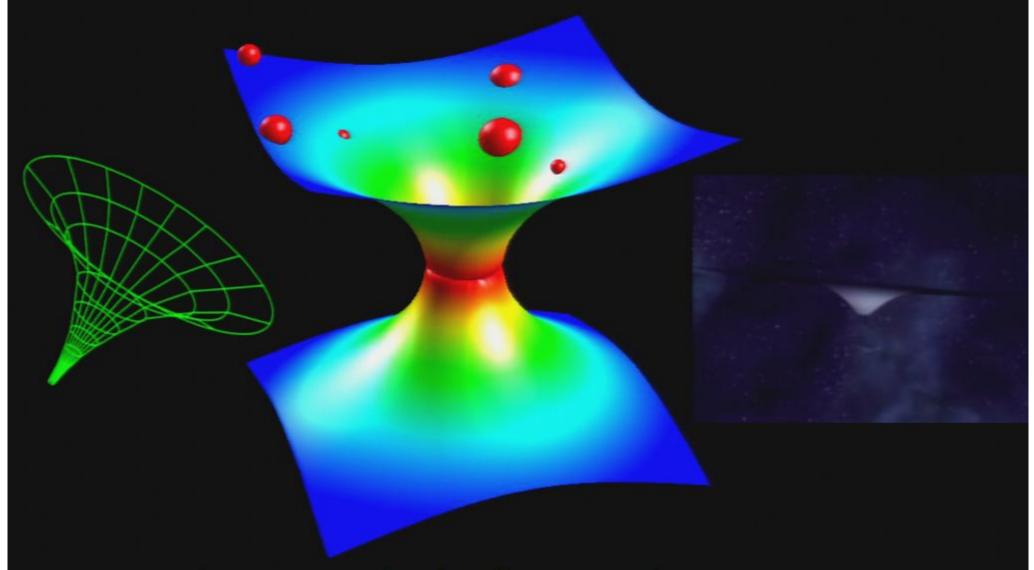


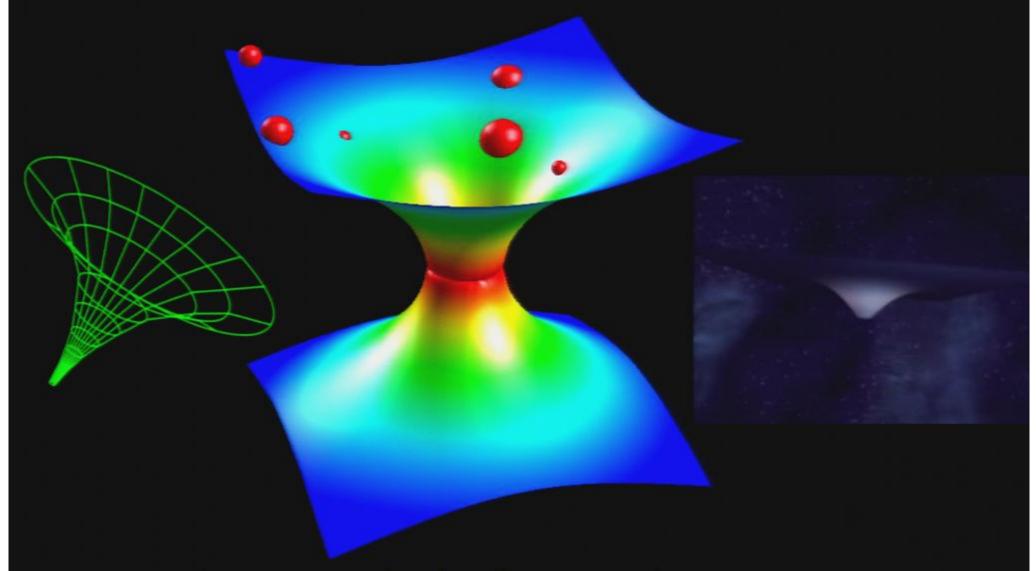


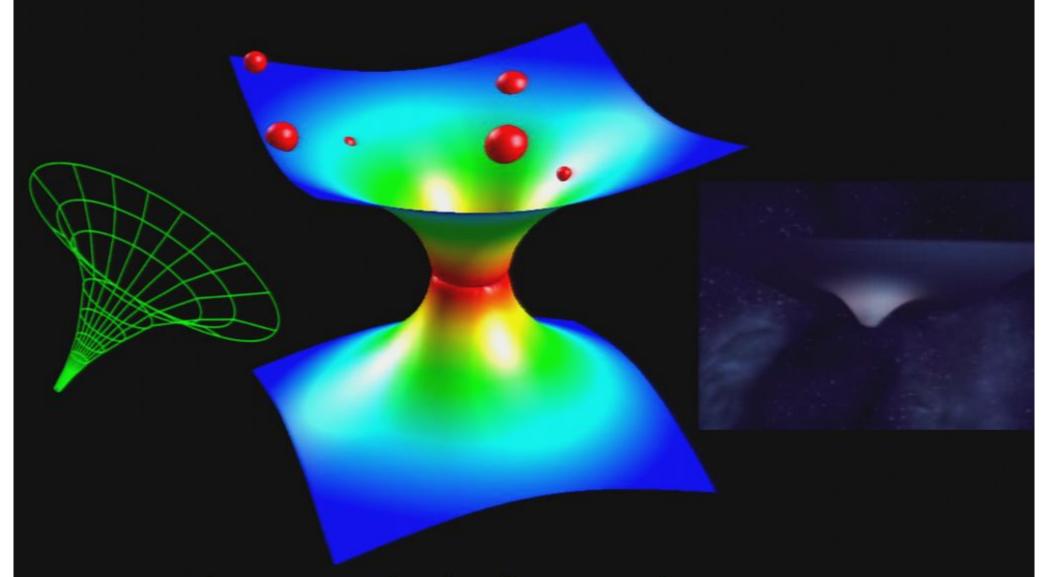


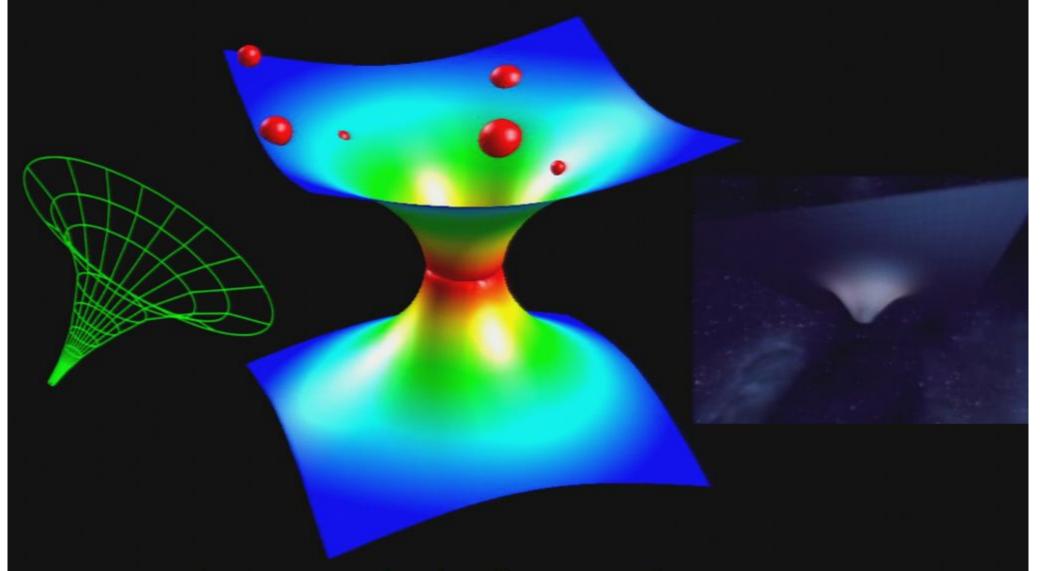


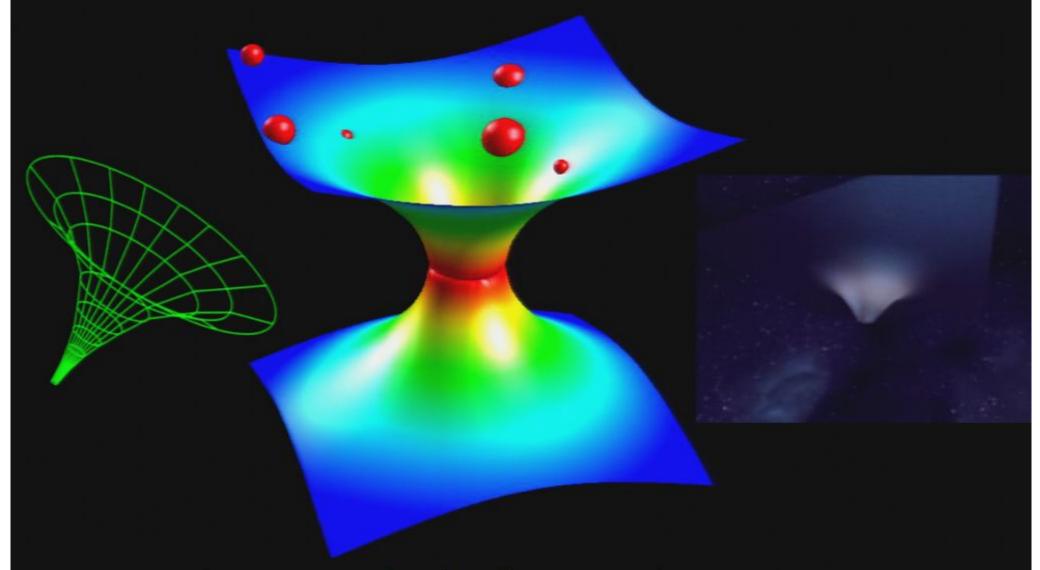


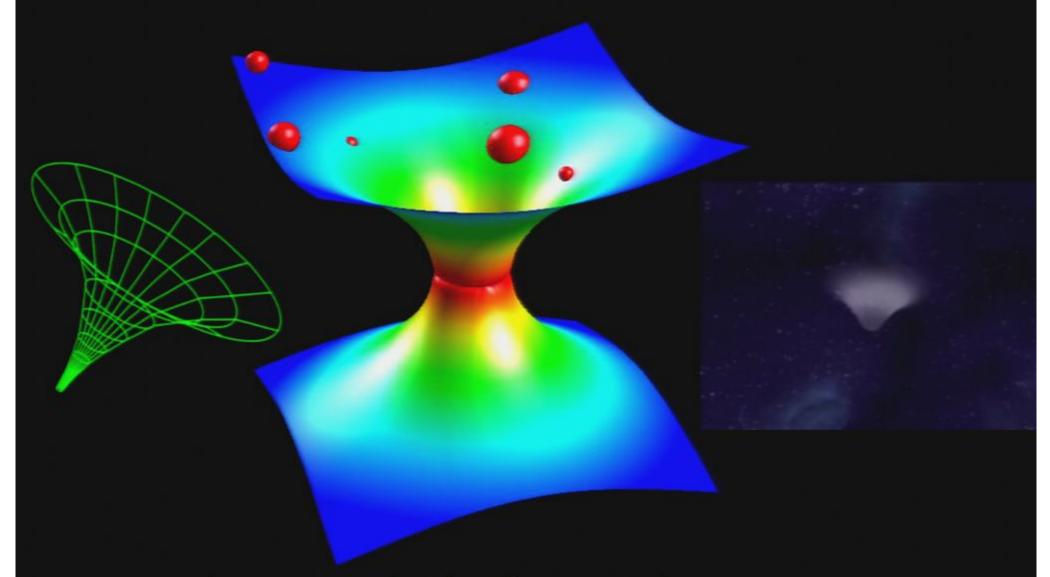




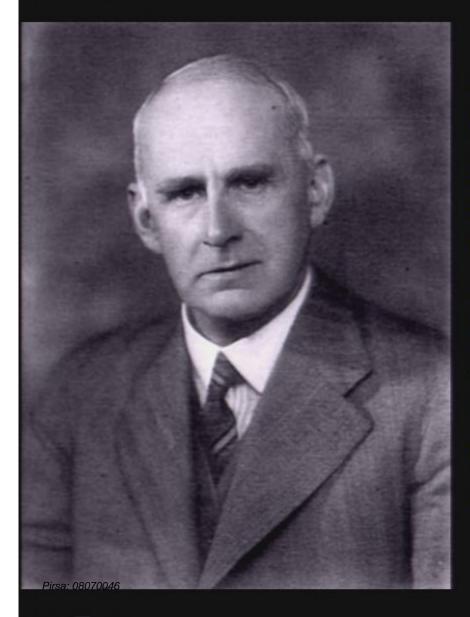






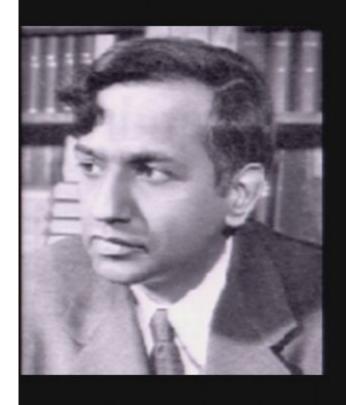


Sir Arthur Eddington



- ·1926 Book The internal constitution of the Stars
- ·Early proponent of Einstein's Theory of General Relativity (next to Einstein best expert on General Relativity)
- ·Poses the mystery of white dwarfs and attacks the reality of black holes predicted by Schwarzschild.
- · Believed White Dwarf was last state in a stars life (rock Star)
- · Paradox with White Dwarf

Subrahmanyan Chandrasekhar





- Idolized Eddington, resolved Eddington; s paradox
- •In 1930 he showed that there is a maximum mass for White Dwarfs
- •1935 Eddington attacks his work. "Chandra" left the field of Blackholes until 1970's
- ·Nobel Prize in Physics 1983



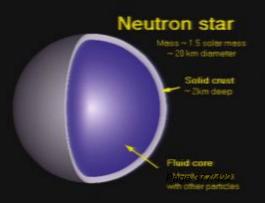
Walter Baade and Fritz Zwicky

Neutron star Mass ~ 1.5 solar mass ~ 29 km diameter Solid crust ~ 2km deep Fluid core Manny resitrons

- · Identifies the process of a supernovae, predicted that this collapse strips the atoms of their electrons, packing the nuclei together as a neutron star.
- ·Neutron stars would not be verified observably until 1968.
- Identified the galaxies associated with cosmic radio sources.
- · Still something was missing that took a star from fusion to supernovae.







Robert J. Oppenheimer

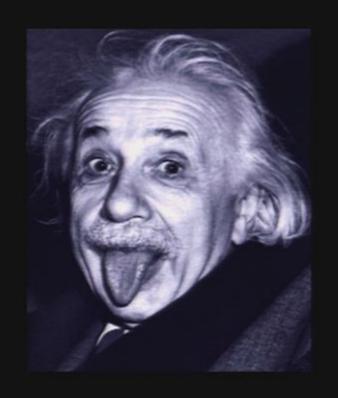
- · Showed that there is a maximum mass for a neutron star from 1.5 to about 3 solar masses (1938).
- ·In a highly idealized calculation, showed that an imploding star forms a black hole.
- ·Led the American atomic bomb project.
- · Which provided the opportunity to experimentally verify and test theories (too expensive for the universities) and the development of the atomic bombs which mimic the power source for the sun to come up with the mathematics and understanding of stellar mechanics
- · Major battle with Wheeler.



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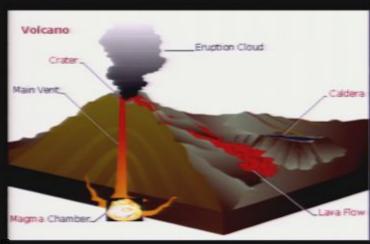
Robert J. Oppenheimer

In 1939 Einstein wrote a paper about his concerns about Oppenheimer's paper and the Schwarzschild radius and states "Schwarzschild singularities do not exist in physical reality". He demonstrated that a collapsing star is unstable when it reaches the Schwarzschild radius, which ended up being mute since that star collapses into a singularity there anyway.



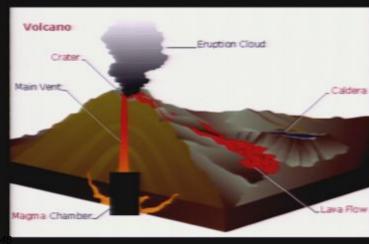
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- · Soviet counterpart to Oppenheimer.
- Developed the theory of nuclear chain reactions. (1939)
- · Lead theorist on USSR atomic bomb (1945)
- · Creates black hole research team (1962).
- Super massive black holes power Quasars (1960's).



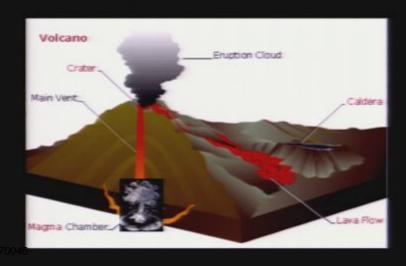


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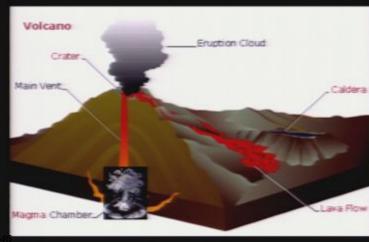


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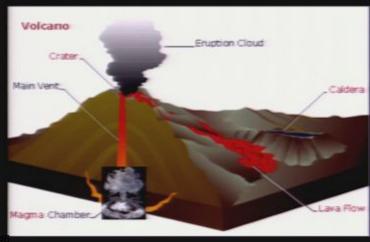


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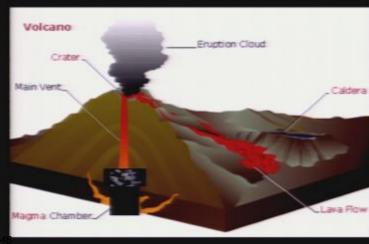


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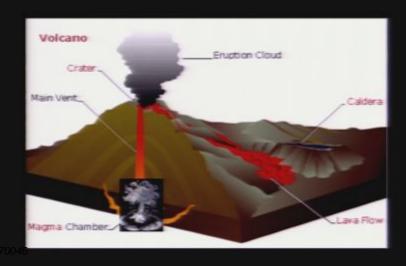


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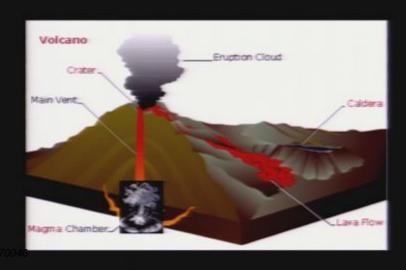


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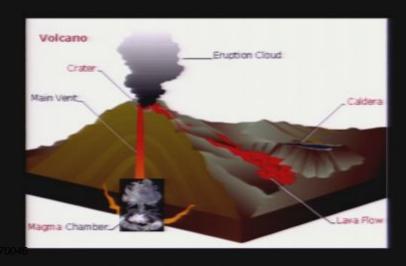


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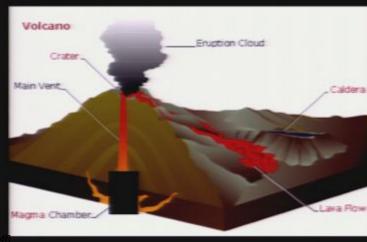


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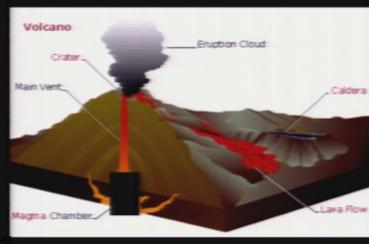


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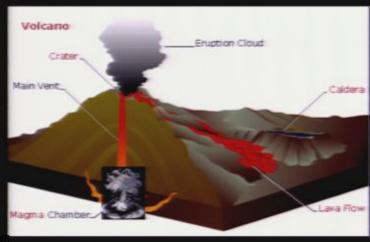


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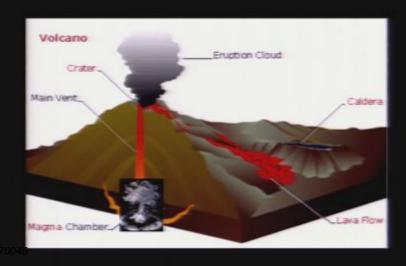


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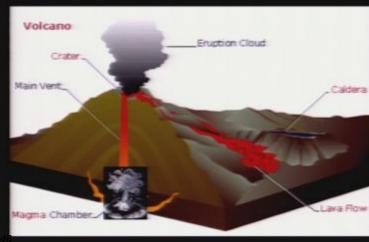


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- Developed the theory of nuclear chain reactions. (1939)
- · Lead theorist on USSR atomic bomb (1945)
- · Creates black hole research team (1962).
- Super massive black holes power Quasars (1960's).



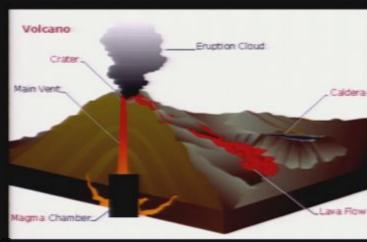


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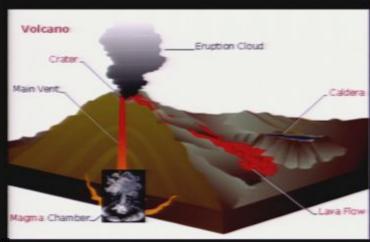


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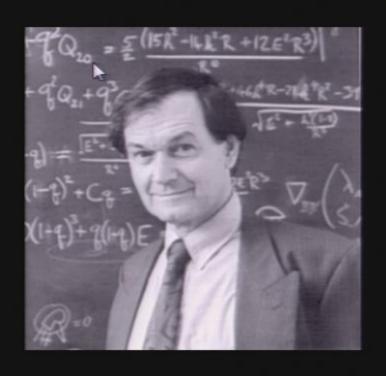


John Wheeler

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- With Bohr develops the theory of nuclear fission.
- Completes a catalog cold, dead stars firming up evidence of destiny of dead stars. (1957)
- ·Major battle with Oppenheimer about existence of black holes. (1957)
- Retracted argument and became the leading proponent of black hole. (1960)
- Coined the phrase "Black Hole".
- Coined the phrase "a Black Hole has no hair" (1968).



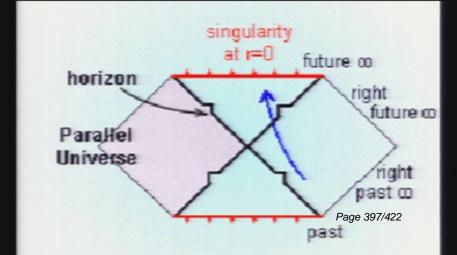


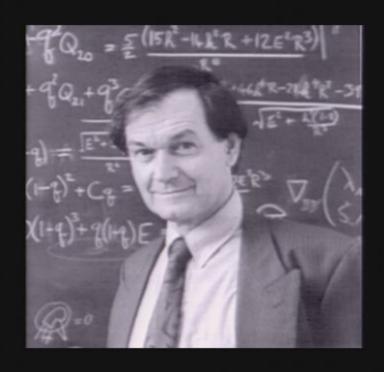
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• Proposed cosmic censorship conjecture

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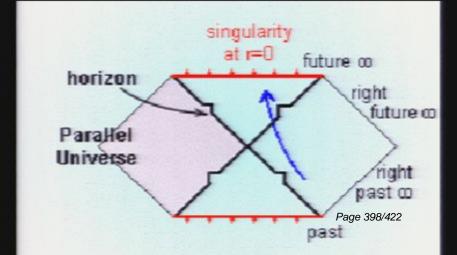
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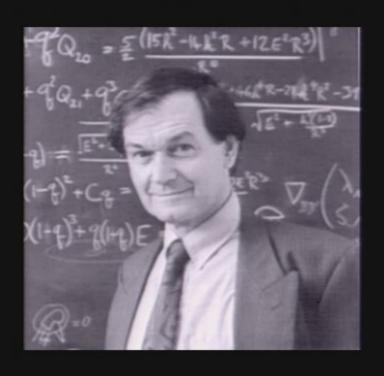
(1969).



Topology



Pirsa: 08070046

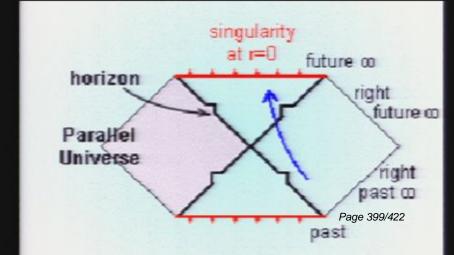


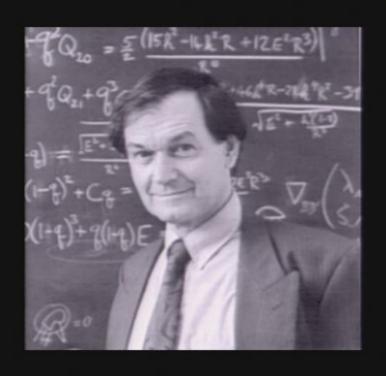
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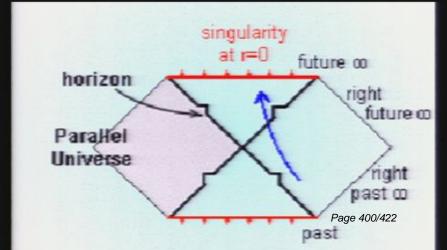


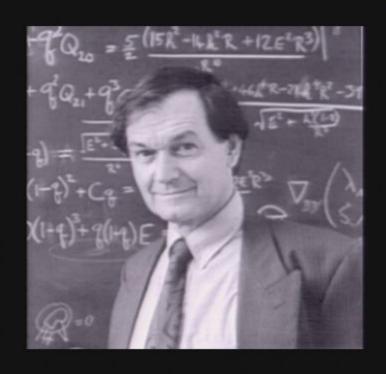
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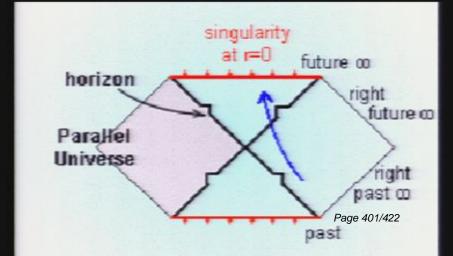
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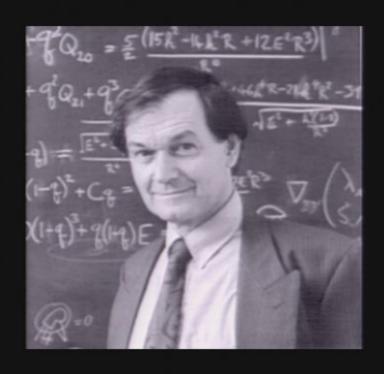
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Topology



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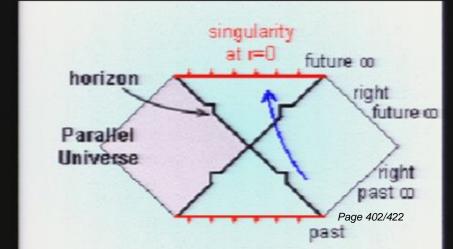


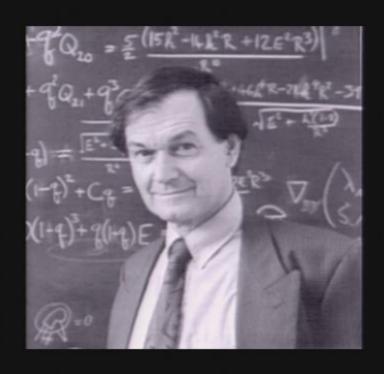
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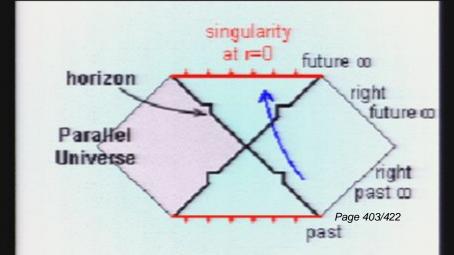


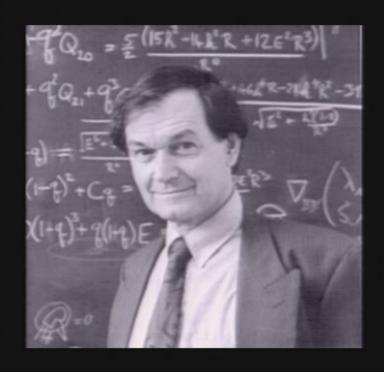
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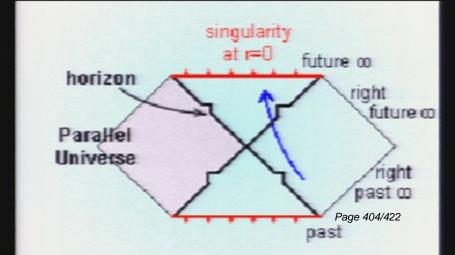
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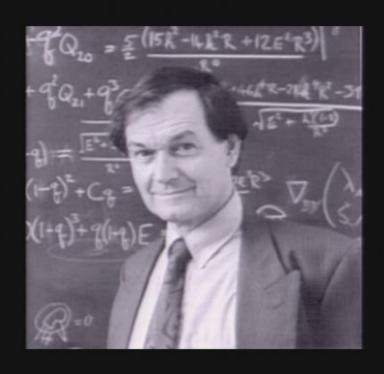
(1969).



Topology



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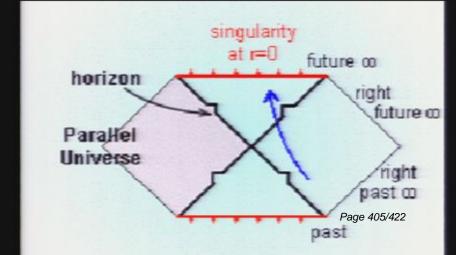


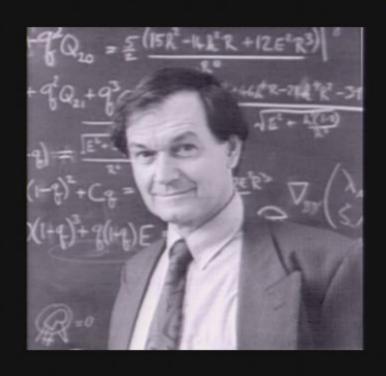
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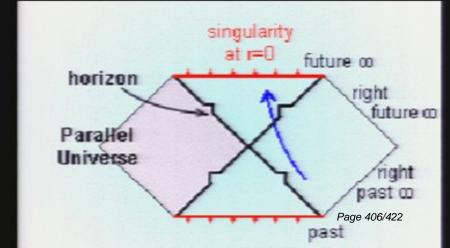


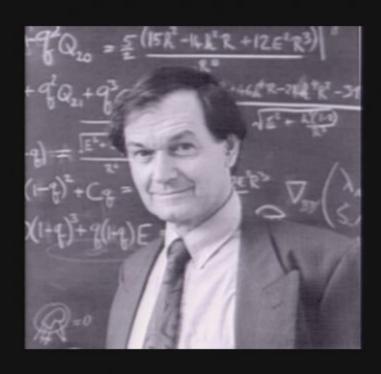


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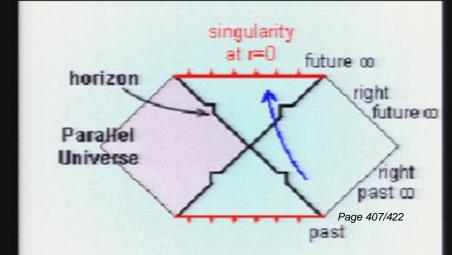


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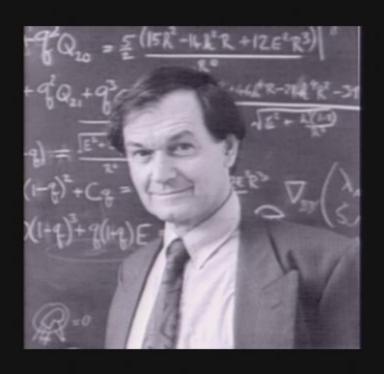
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Topology



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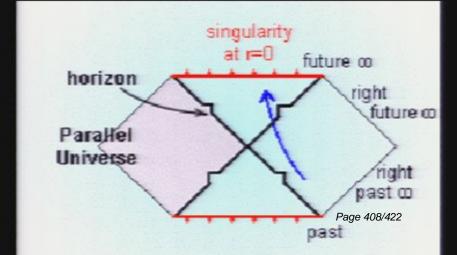


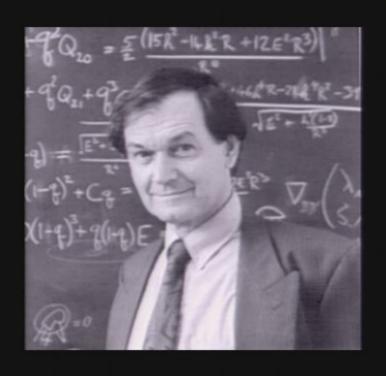
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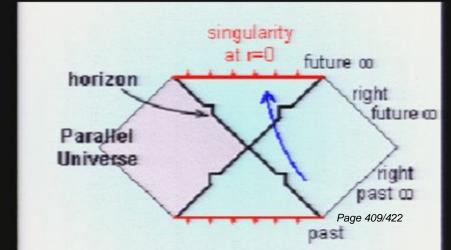


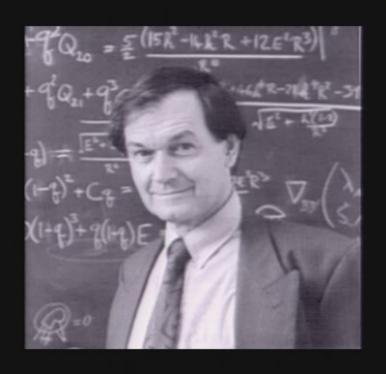
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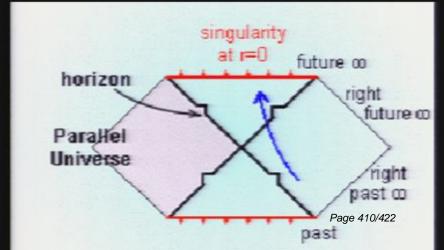


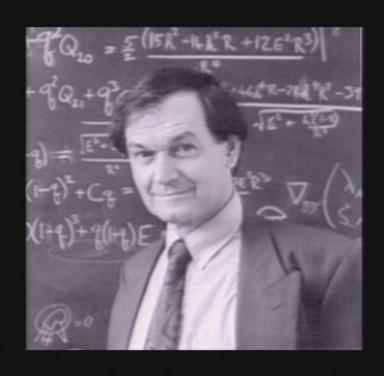
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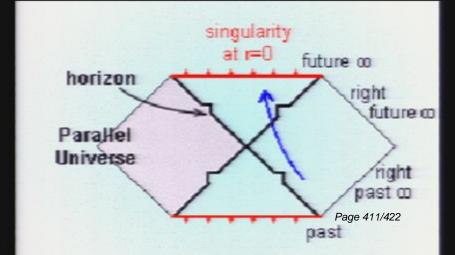


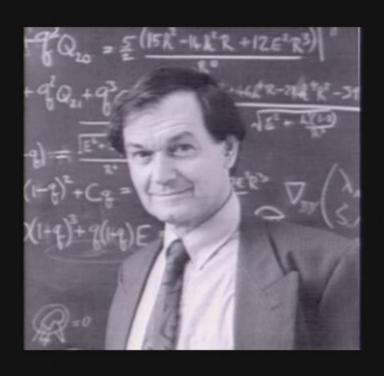
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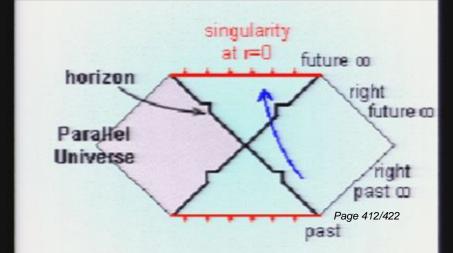


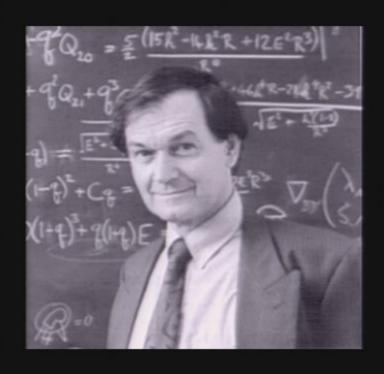
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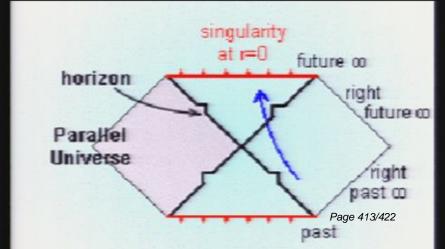


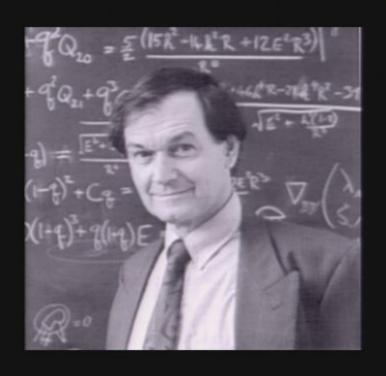
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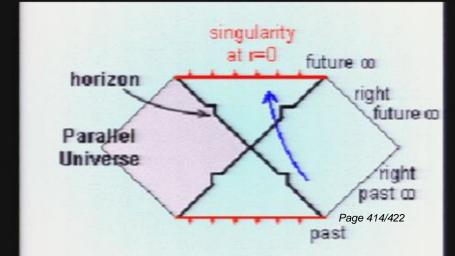


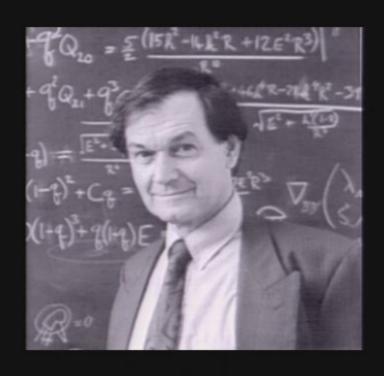
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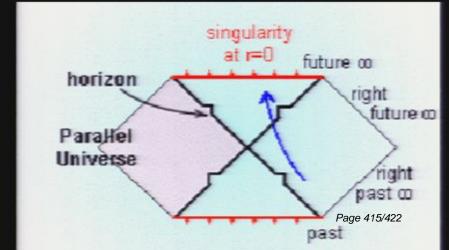


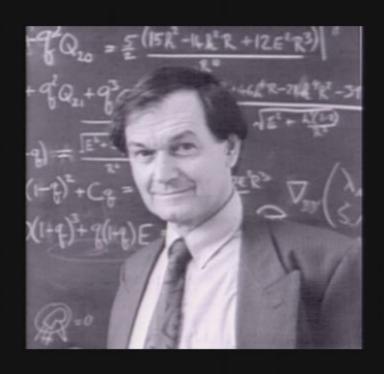
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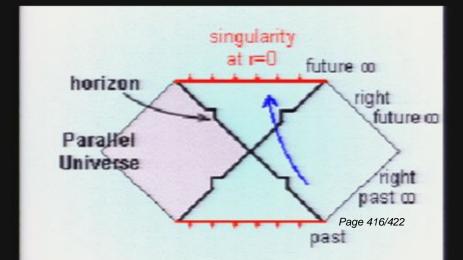


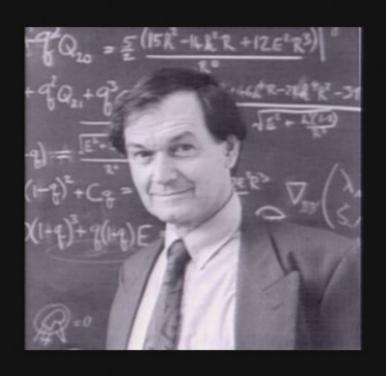
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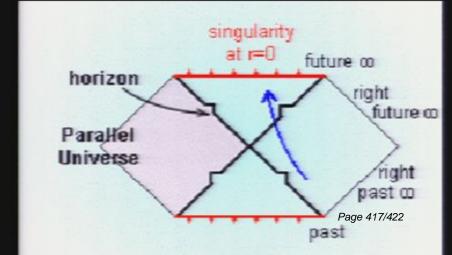


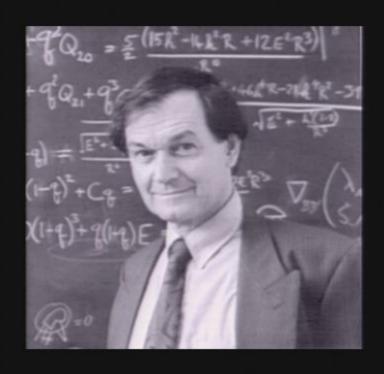


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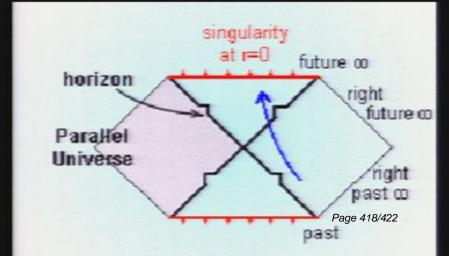
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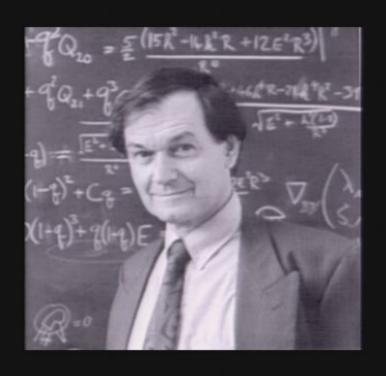
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Topology



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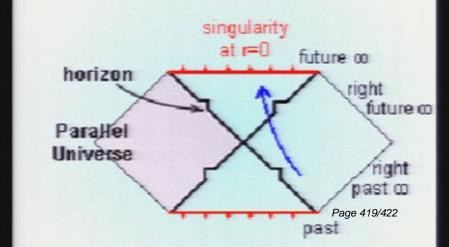


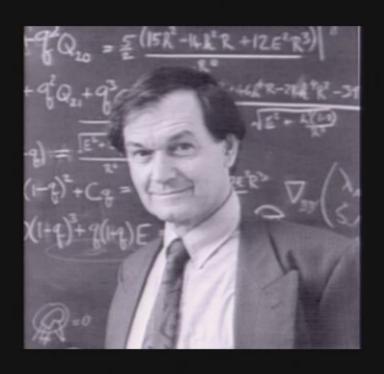
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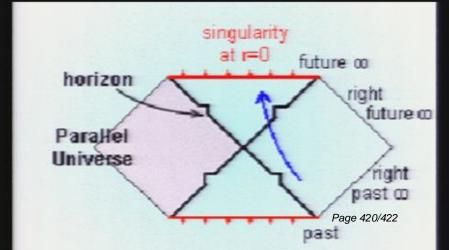


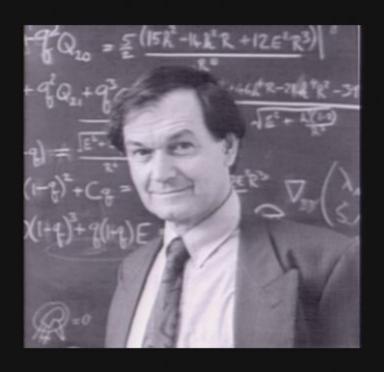
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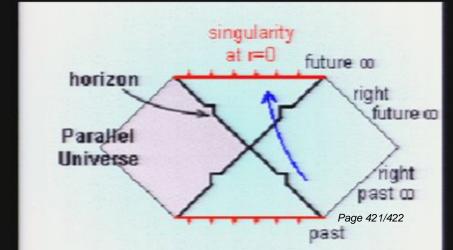


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The Blackhole Stars Today



Hawking







Thorne





Robert Wald

