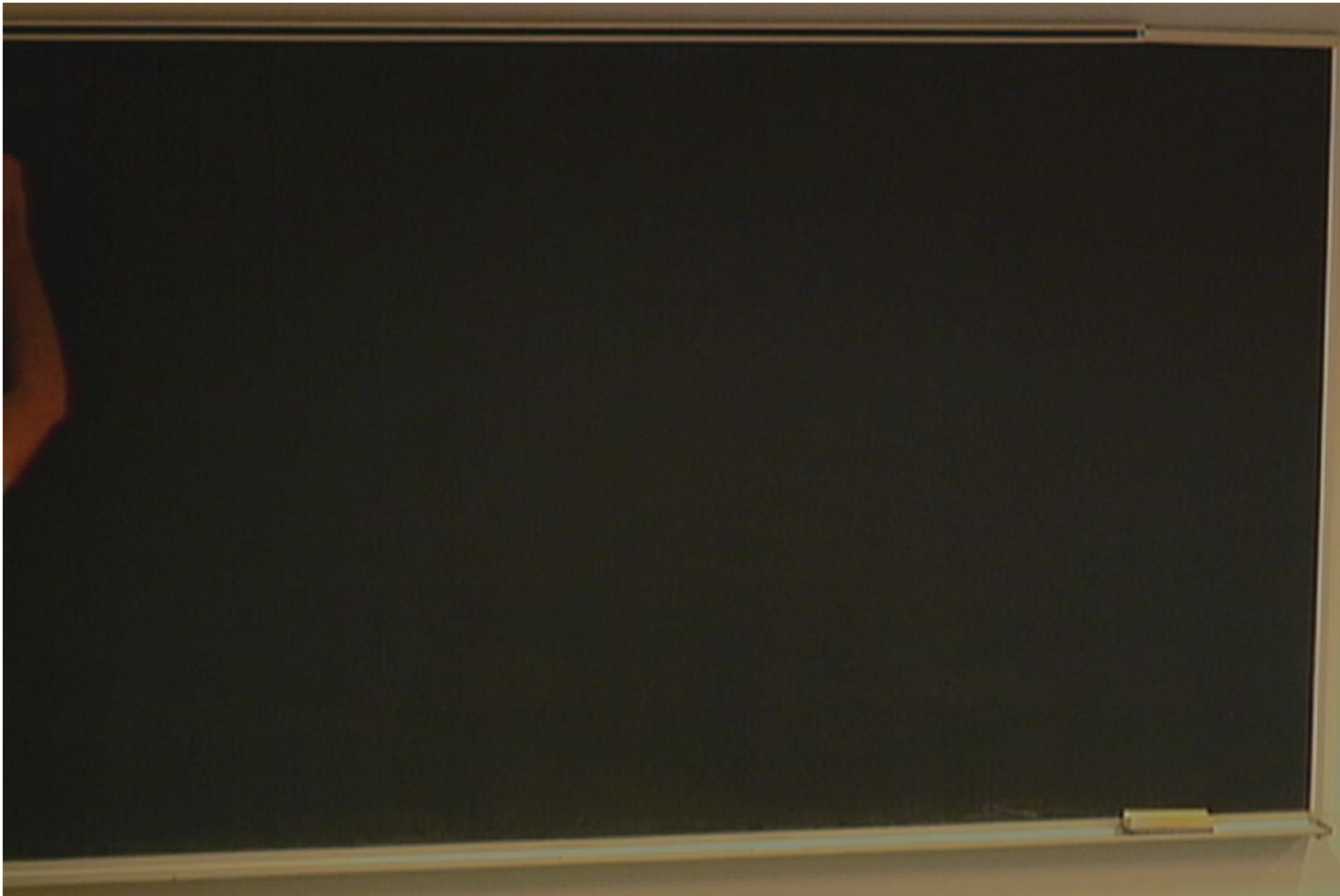


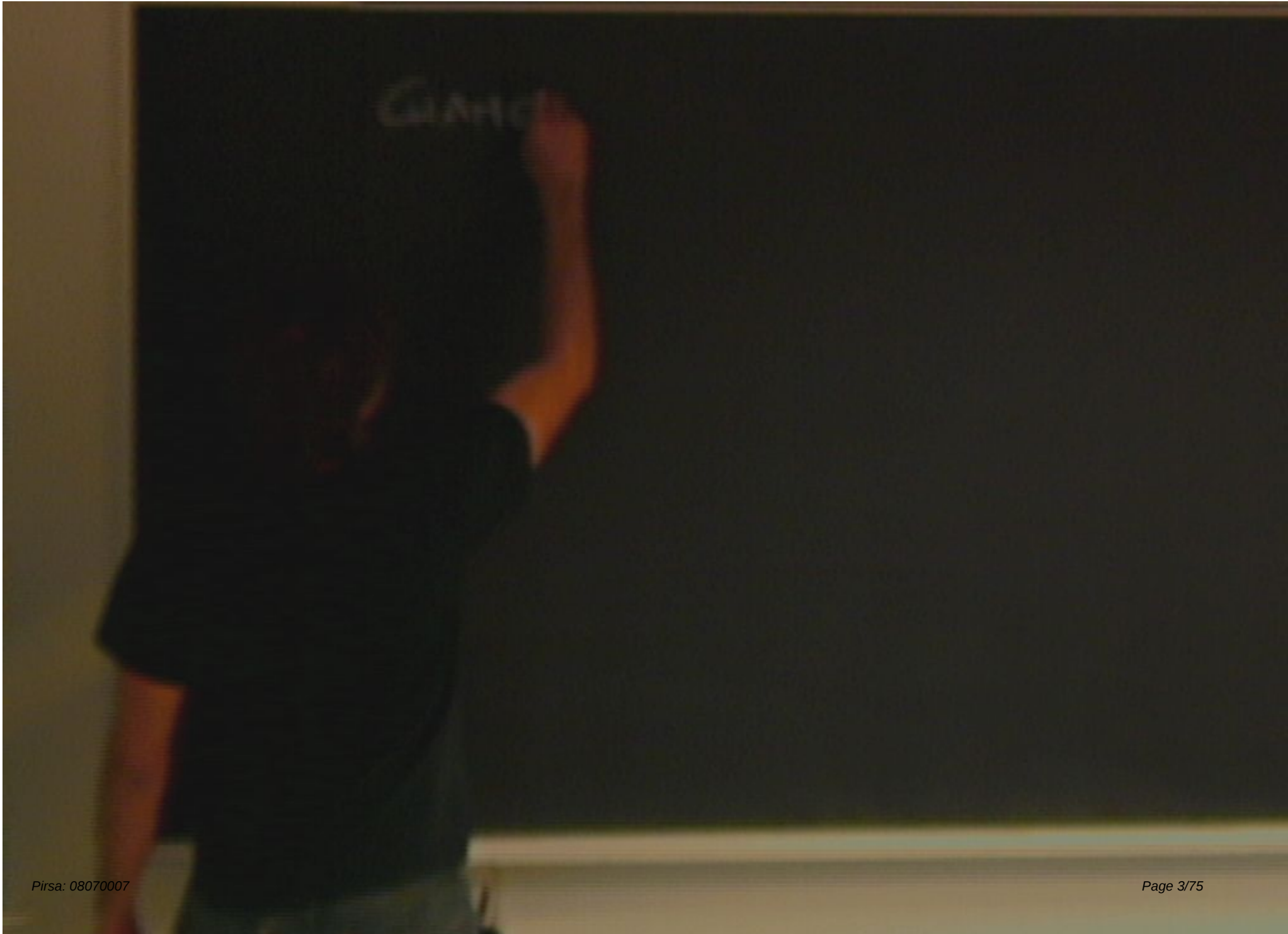
Title: Chameleon Theories

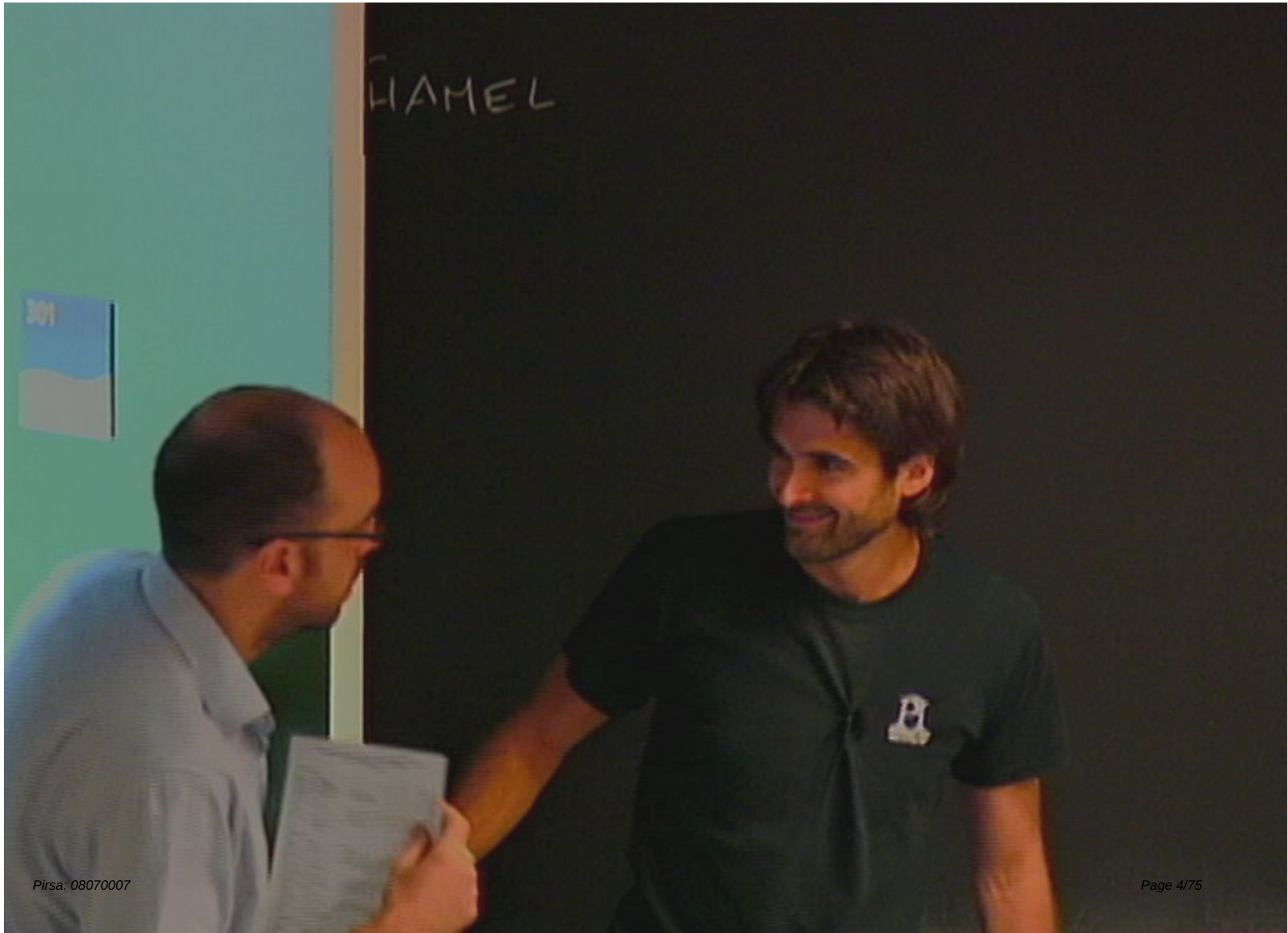
Date: Jul 14, 2008 12:00 PM

URL: <http://pirsa.org/08070007>

Abstract:







CHAMEL



CHAMELEON FIELD THEORIES



CHAMELEON FIELD THEORIES



GAUGE/FIELD THEORIES

4. A. HELLMAN, PRL
PRD (2004)

S. GUBSER

A. UPMANU

LOCAL

CHAMELEON FIELD THEORIES

W. A. HELTHAN, PRL
PRD (2001)

S. GUBSER

A. UPADHYE

LOCAL $\leftrightarrow$ COSMO.

0.05

CHAMELEON FIELD THEORIES

W. A. HELTHAN, PRL
PRD (2001)

S. GUBSER

A. UPADHYE

LOCAL $\leftrightarrow$ COSMO.

o.g. $w_{\text{eff}} \neq -1$

CHAMELEON FIELD THEORIES

W. A. HELTHAN, PRL
PRD (2001)

S. GUBSER

A. UPADHYE

LOCAL $\leftrightarrow$ COSMO.

o.g. $w_{de} \neq -1$

CHAMELEON FIELD THEORIES

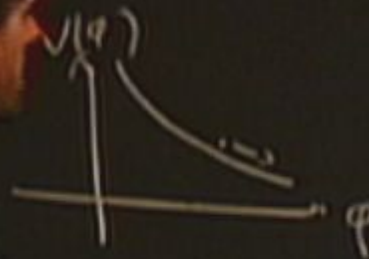
by A. HELLMAN, PRL
PRD (2004)

S. GUBSER

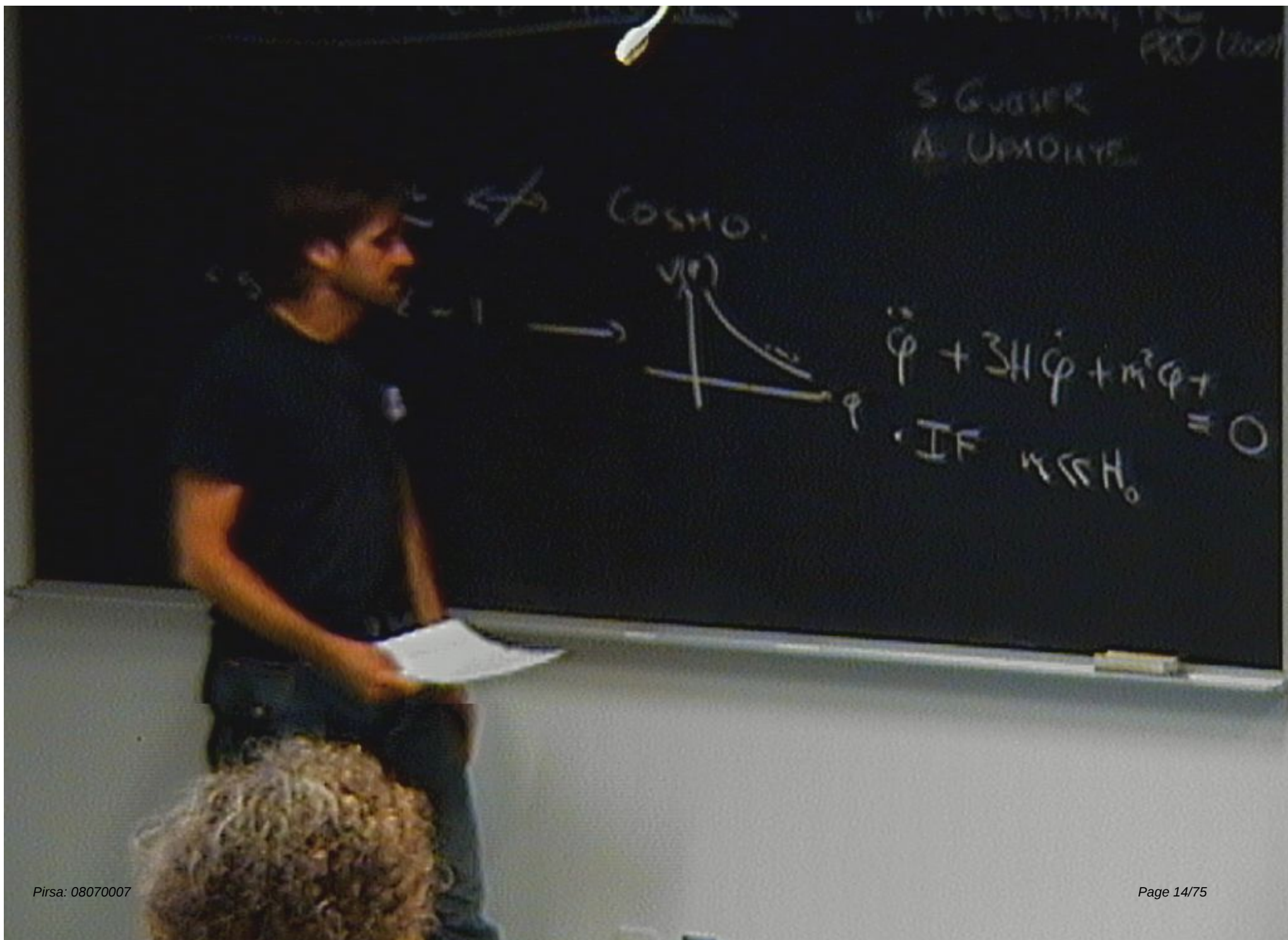
A. UPADHYE

LOCAL $\leftarrow$ SMO.

o.g. $w_{DE} \neq -1$



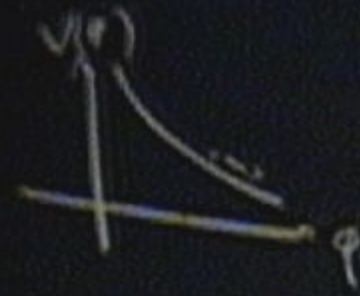
$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$



S. GUTSER
A. UPMOLITSKY

cosmo.

$\epsilon = 1 \rightarrow$



$$\ddot{\varphi} + 3H\dot{\varphi} + m^2\varphi = 0$$

• IF $\kappa < H_0$

S. GUBSER

A. UPADHYAY

← COSMO.



$$\ddot{\varphi} + 3H\dot{\varphi} + m^2\varphi = 0$$

• IF $m \ll H_0 \Rightarrow w \approx -1$

S. GUBSER

A. UPADHYE

COSMO.



$$\ddot{\varphi} + 3H\dot{\varphi} + m^2\varphi = 0$$

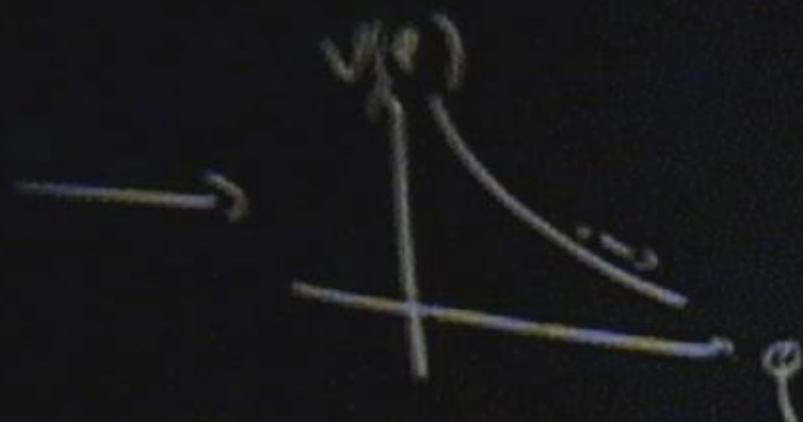
• IF

• "

$$w \ll H_0 \Rightarrow w \approx -1$$

$$w \gg H_0$$

* Cosmo.



$$\ddot{\varphi} + 3H\dot{\varphi} + m^2\varphi = 0$$

• IF

• "

$$m \ll H_0 \Rightarrow \omega \approx -1$$

$$m \gg H_0$$

$$\omega \approx -1 \rightarrow \boxed{m \approx H_0}$$

CHAMELEON FIELD THEORIES

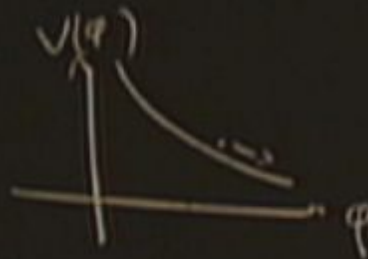
by A. HELTHAN, PRL
PRD (2001)

S. GUBSER

A. UPADHYE

LOCAL $\leftrightarrow$ COSMO.

$$w_{\text{eff}} \neq -1 \longrightarrow$$



$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

• IF $m \ll H_0 \Rightarrow w_{\text{eff}} = -1$

• " $m \gg H_0$

$$w_{\text{eff}} \neq -1 \longrightarrow \boxed{m \sim H_0}$$

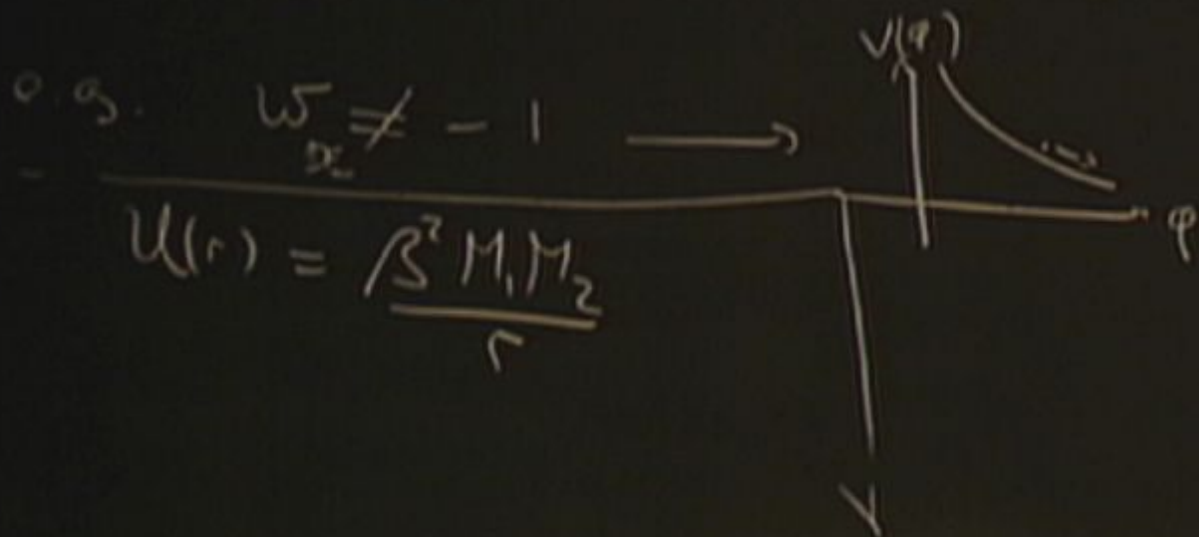
CHAMELEON FIELD THEORIES

W. A. HELTHAN, PRL
PRD (200)

S. GUBSER

A. UPADHYE

LOCAL $\leftrightarrow$ COSMO.



$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

• IF $w < H_0 \Rightarrow w_{av} = -1$

• " $w > H_0$

$$w \neq -1 \rightarrow \boxed{w \sim H!}$$

CHAMELEON FIELD THEORIES

W. A. HELTHAN, PRL
PRD (200)

S. GUBSER

A. UPADHYE

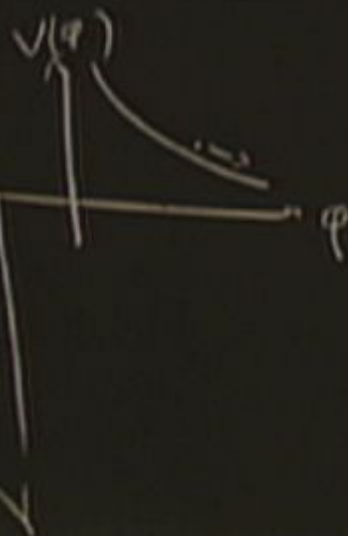
LOCAL $\leftrightarrow$ COSMO.

$$w_{\text{eff}} \neq -1 \longrightarrow$$

$$U(r) = \frac{\beta^2 M_1 M_2}{r}$$

$$\bullet \beta < 10^{-5}$$

$$\bullet < 10^{-4}$$



$$\ddot{\varphi} + 3H\dot{\varphi} + m^2\varphi = 0$$

$$\bullet \text{ IF } w < H_0 \Rightarrow w_{\text{eff}} = -1$$

$$\bullet \text{ " } w > H_0$$

$$w_{\text{eff}} \neq -1 \longrightarrow \boxed{m \sim H_0}$$

CHAMELEON FIELD THEORIES

by A. HELTHAN, PRL
PRD (2001)

S. GUBSER

A. UPADHYE

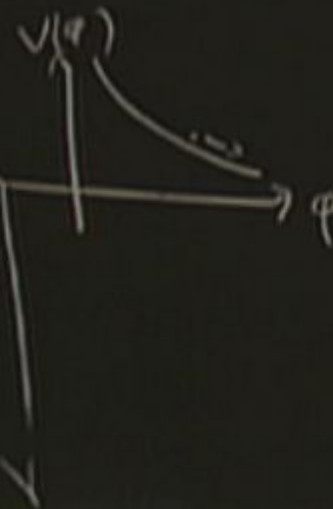
LOCAL $\leftrightarrow$ COSMO.

$$w_x \neq -1 \rightarrow$$

$$U(r) = \frac{\beta^2 M_1 M_2}{r}$$

$$\bullet \beta < 10^{-5}$$

$$\bullet < 10^{-4}$$

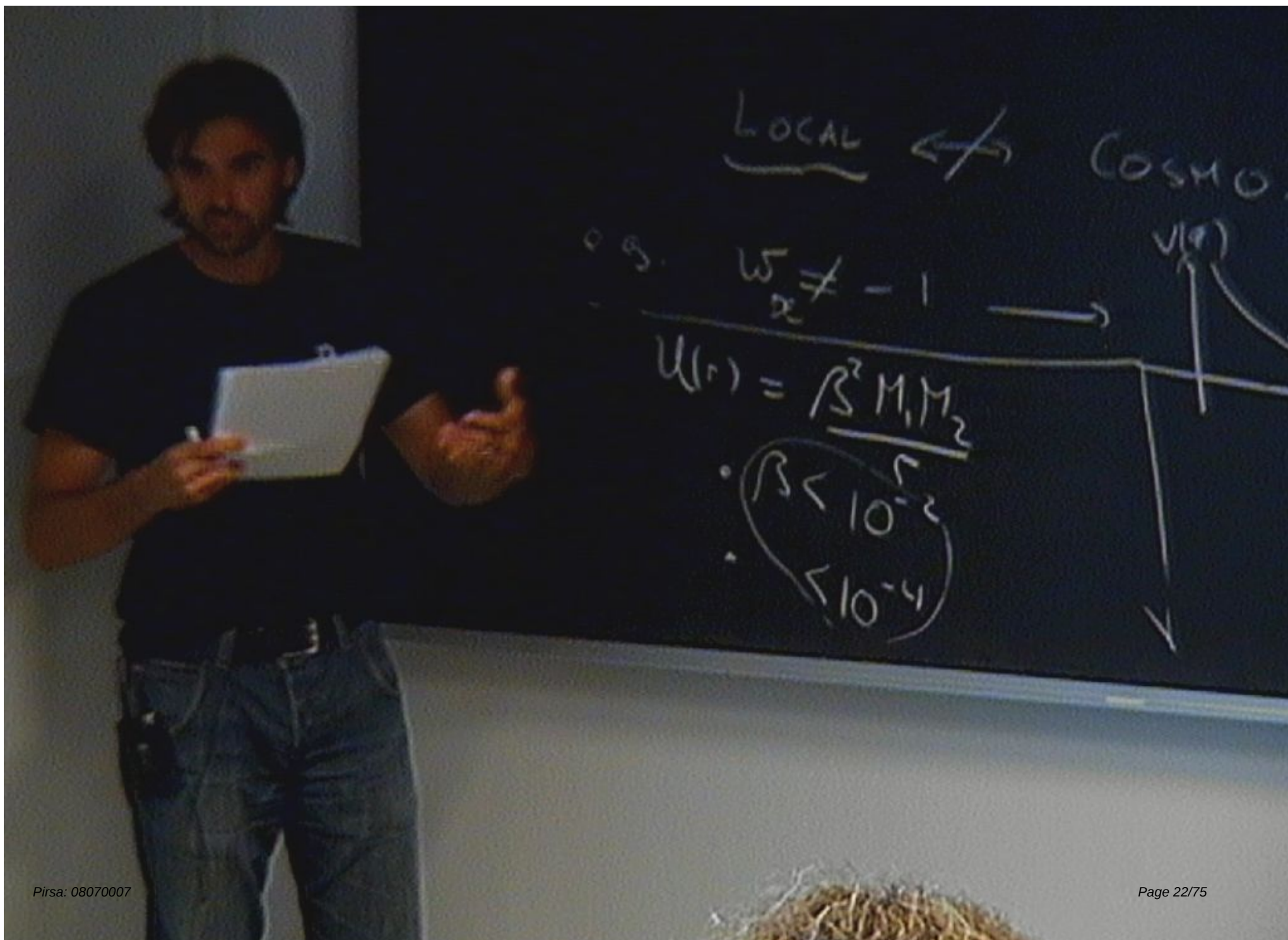


$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

$$\bullet \text{ IF } w < H_0 \Rightarrow w \rightarrow -1$$

$$\bullet \text{ " } w > H_0$$

$$w \neq -1 \rightarrow \boxed{w \sim H_0}$$

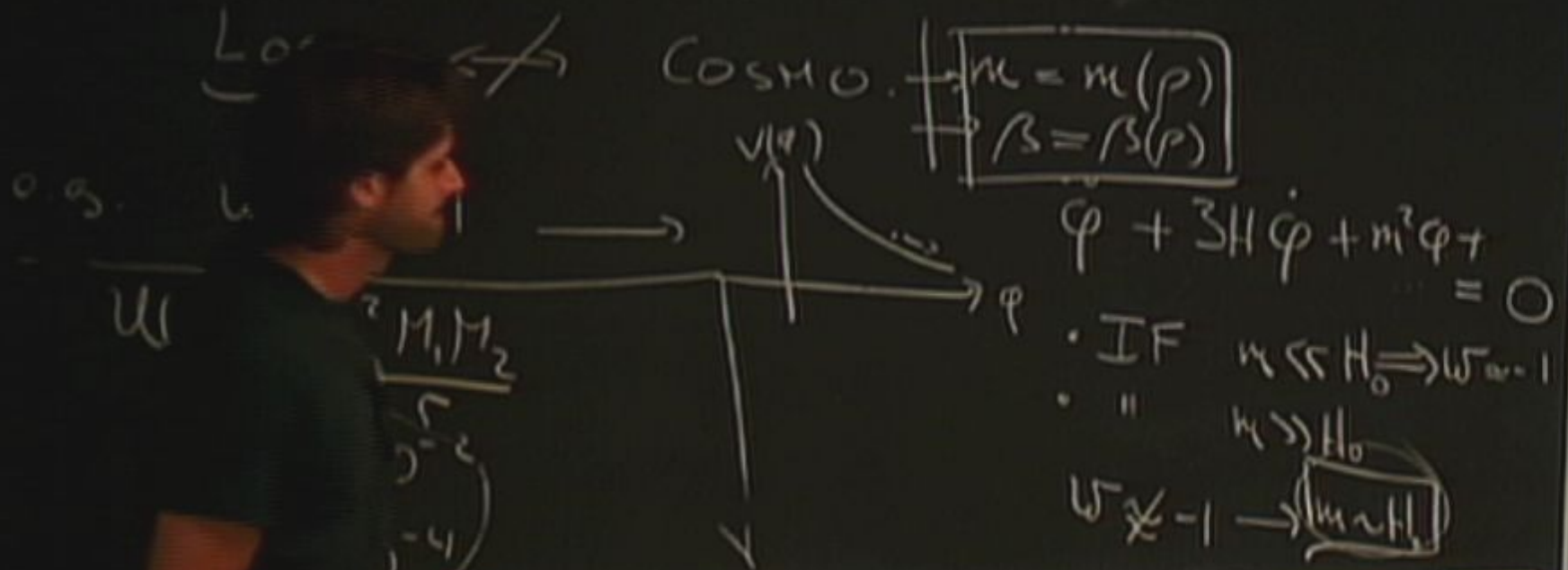


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A. UPADHYE



CHAMELEON FIELD THEORIES

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PRD (2001)

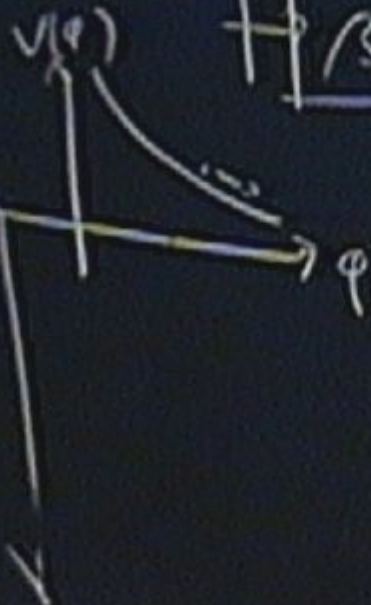
S. GUBSER
A. UPADHYE

LOCAL $\leftrightarrow$ COSMO. $\left\{ \begin{array}{l} m = m(\rho) \\ \beta = \beta(\rho) \end{array} \right.$

e.g. $w \neq -1$

$$U(\rho) = \beta^2 M_1 M_2$$

• $\beta < 10^{-2}$
• $< 10^{-4}$



$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

• IF $m \ll H_0 \Rightarrow w \approx -1$
• " $m \gg H_0$

$w \neq -1 \rightarrow m \sim H_0$

MECHANISM.

$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\chi)^2 - V(\chi) \right\} - \int d^4x \sqrt{-g} \ln(\chi^2 g^{\mu\nu})$$

MECHANISM:

$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\chi')^2 - V(\varphi) \right\} - \int d^4x \sqrt{-g} \mathcal{L}_m(\psi, g^{\mu\nu})$$

$$g_{\mu\nu}^{(i)} = e^{2\beta_i \varphi / M_{Pl}} g_{\mu\nu}$$

MECHANISM:

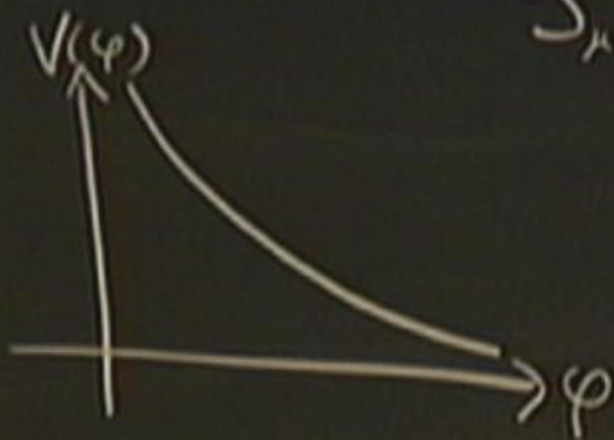
$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) \right\} - \int d^4x \sqrt{-g} \mathcal{L}_m(\psi, g^{\mu\nu})$$

$$g_{\mu\nu}^{(i)} = e^{2\beta_s \phi / M_{Pl}} g_{\mu\nu} \approx \left(1 + \frac{2\beta_s \phi}{M_{Pl}} \right) g_{\mu\nu}$$

MECHANISM:

$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\dot{\varphi})^2 - V(\varphi) \right\} - \int d^4x \sqrt{-g} \mathcal{L}_m(\psi, g^{\mu\nu})$$

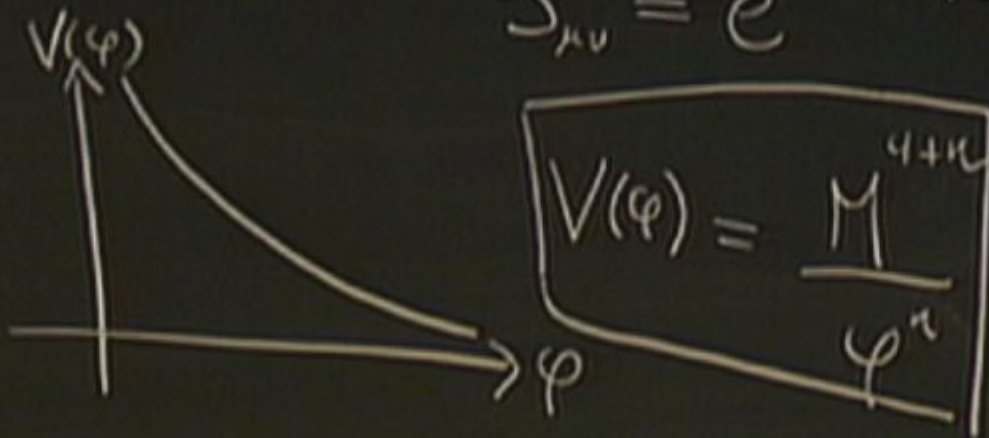
$$g_{\mu\nu}^{(i)} = e^{2\beta_i \varphi / M_{Pl}} g_{\mu\nu} \approx \left(1 + \frac{2\beta_i \varphi}{M_{Pl}} \right) g_{\mu\nu}$$



MECHANISM:

$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\chi')^2 - V(\varphi) \right\} - \int d^4x \sqrt{-g} \mathcal{L}_m(\psi, g^{\mu\nu})$$

$$g_{\mu\nu}^{(i)} = e^{2\beta_i \varphi / M_{Pl}} g_{\mu\nu} \approx \left(1 + \frac{2\beta_i \varphi}{M_{Pl}} \right) g_{\mu\nu}$$



$$\Delta\varphi = \frac{dV}{d\varphi} - \sum_i$$

$$U(r) = \beta^2 V$$

- $\beta < 10$
- < 10

- IF $w \ll$
- " $w \gg$
- $w \ll 1 \rightarrow$

FROM THE THEORIES

$$\Delta\varphi = \frac{dV}{d\varphi} = \sum_i \frac{4\beta_i}{M_{Pl}} e^{4\beta_i\varphi/M_{Pl}} T^{(i)}$$

$$U(r) = \beta^2 M_1 M_2$$

• $\beta < 10^{-5}$
 • $< 10^{-4}$

- IF $m \ll H_0$
- " $m \gg H_0$
- $\omega \neq -1 \rightarrow$

$$\Delta\varphi = \underbrace{\frac{dV}{d\varphi} - \sum_i \frac{4\beta_i}{M_{Pl}} e^{4\beta_i\varphi/M_{Pl}} T^{(i)}}_{\text{SERRADIV}} \quad \text{SER} \quad \text{ADIV}$$

$$V(r) = \beta^2 M_1 M_2$$

$$\bullet \beta < 10^{-2}$$

$$\bullet < 10^{-4}$$

• IF $m \ll H_0 \Rightarrow$

• " $m \gg H_0$

$\sqrt{-1} \rightarrow \boxed{m \sim H_0}$

$$\Delta\varphi = \frac{dV}{d\varphi} - \sum_i \frac{4\beta_i}{M_{Pl}} e$$

$\frac{4\beta_i c\hbar}{M_{Pl}} T^{(i)}$

$$\frac{dV_{eff}}{d\varphi}$$

$$U(r) = \beta^2 M_1 M_2$$

- $\beta < 10^{-2}$
- $< 10^{-4}$

- IF $m < H_0$
- " $m > H_0$
- $\sqrt{x} - 1 \rightarrow \ln x$

LEPTON FIELDS THEORIES

$$\Delta\varphi = \frac{dV}{d\varphi} - \sum_i \frac{4\beta_i}{M_{Pl}} e^{4\beta_i\varphi/M_{Pl}} \left(T^{(i)} \right)$$

$$T^{(i)} = -\rho_{(i)}$$

$$\frac{dV_{eff}}{d\varphi}$$

$$+ 3H^2\varphi + m^2\varphi$$

$$\bullet \beta < 10^{-5}$$

$$\bullet < 10^{-4}$$

$$\bullet \text{ IF } w \ll H_0 \Rightarrow w \approx$$

$$\bullet \text{ " } w \gg H_0$$

$$w \approx -1 \rightarrow \boxed{w \sim H_0}$$

$$\Delta\varphi = \underbrace{\frac{dV}{d\varphi} - \sum_i \frac{4\beta_i}{M_{Pl}} e^{\frac{4\beta_i \varphi}{M_{Pl}}} T^{(i)}}_{\frac{dV_{eff}}{d\varphi}} = -\rho_{tot}$$

$$V_{eff}(\varphi) = V(\varphi) + \sum_i e^{\frac{4\beta_i \varphi}{M_{Pl}}} \left(\rho_{tot} + 3H\dot{\varphi} + m^2\varphi^2 \right)$$

$$\begin{aligned} &< 10^{-2} \\ &< 10^{-4} \end{aligned}$$

$$\begin{aligned} w < H_0 &\Rightarrow w_{eff} \\ w > H_0 &\Rightarrow w_{eff} \\ w_{eff} < -1 &\Rightarrow \boxed{w \sim -1} \end{aligned}$$

$$\Delta\varphi = \frac{dV}{d\varphi} - \sum_i \frac{4\beta_i}{M_{Pl}} e^{\frac{4\beta_i\varphi}{M_{Pl}}} T^{(i)} = -\rho_{tot}$$

$$\frac{dV_{eff}}{d\varphi}$$

$$V_{eff}(\varphi) = V(\varphi) + \sum_i e^{\frac{4\beta_i\varphi}{M_{Pl}}} \rho_{(i)}$$

$$\beta < 10^{-2}$$

$$< 10^{-4}$$

$$w < H_0 \Rightarrow w < -1$$

$$w > H_0$$

$$w \neq -1 \rightarrow (w \sim -1)$$



$$S = \int d^4x \sqrt{-g} \left(\frac{1}{2} R - \frac{1}{2} (\partial \phi)^2 - V(\phi) \right)$$

$g_{\mu\nu} = e^{2\beta(\phi)/4}$

$V(\phi) = \frac{M^4}{\phi^2}$

$V(\phi)$

ϕ

$$\Delta\varphi = \underbrace{\frac{dV}{d\varphi} - \sum_i \frac{4\beta_i}{M_{Pl}} e^{4\beta_i\varphi/M_{Pl}} T^{(i)}}_{\frac{dV_{eff}}{d\varphi}} = -\beta_{tot}$$

$$V(\varphi) = V(\varphi) + \sum_i e^{4\beta_i\varphi/M_{Pl}} P_{(i)}$$

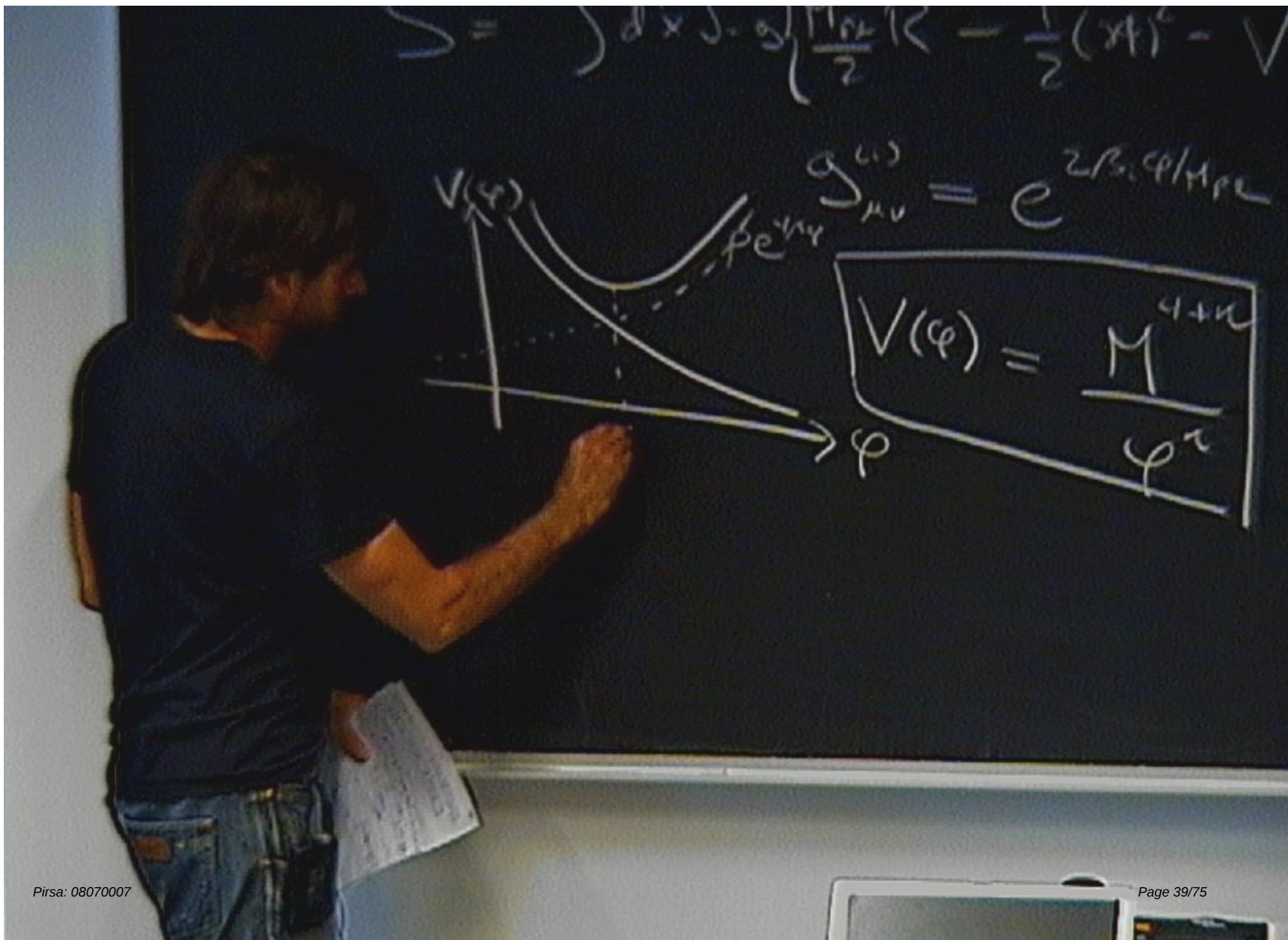
$$\beta < 10^{-5}$$

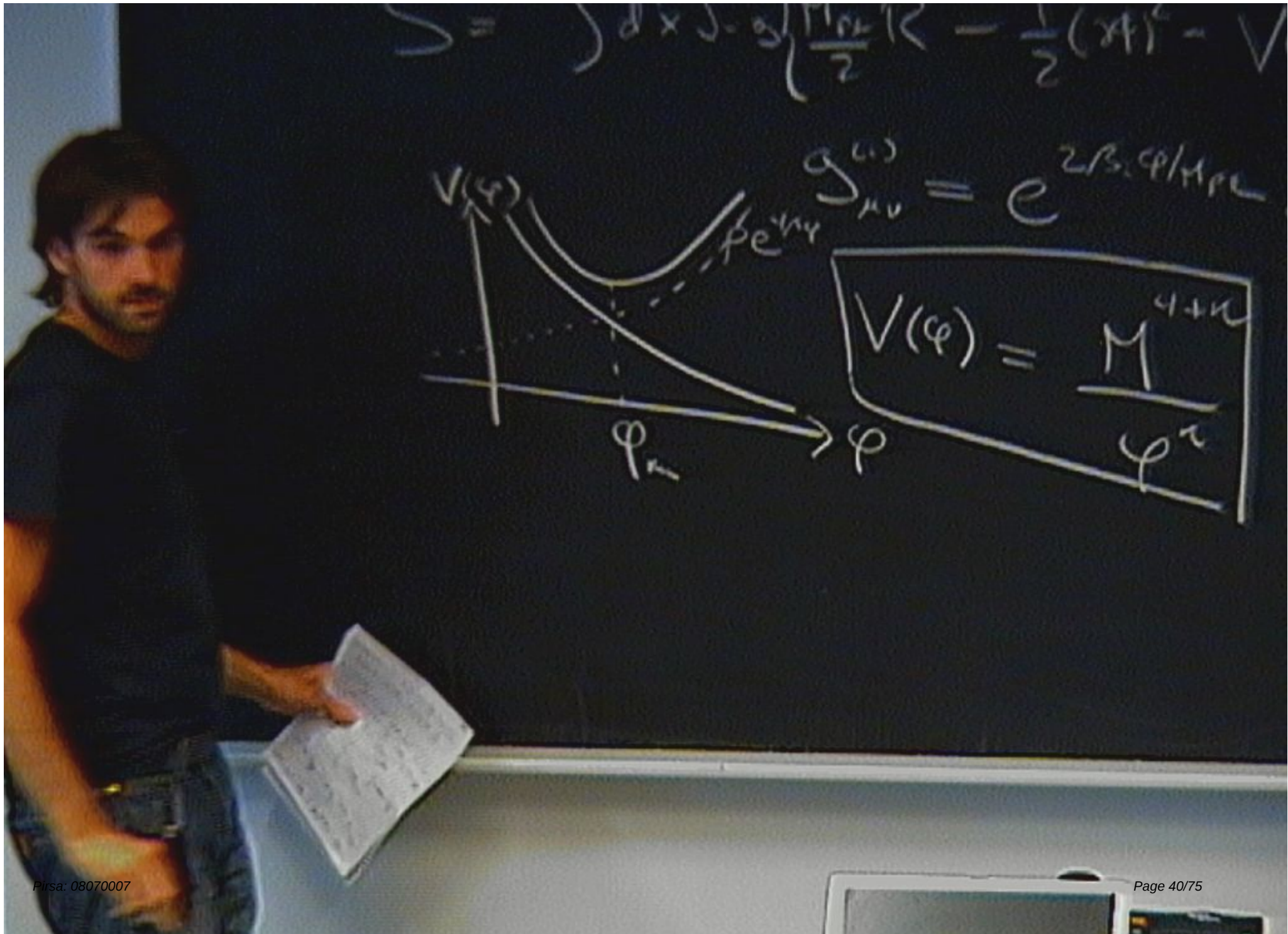
$$< 10^{-4}$$

$$w \ll H_0 \Rightarrow w \approx -1$$

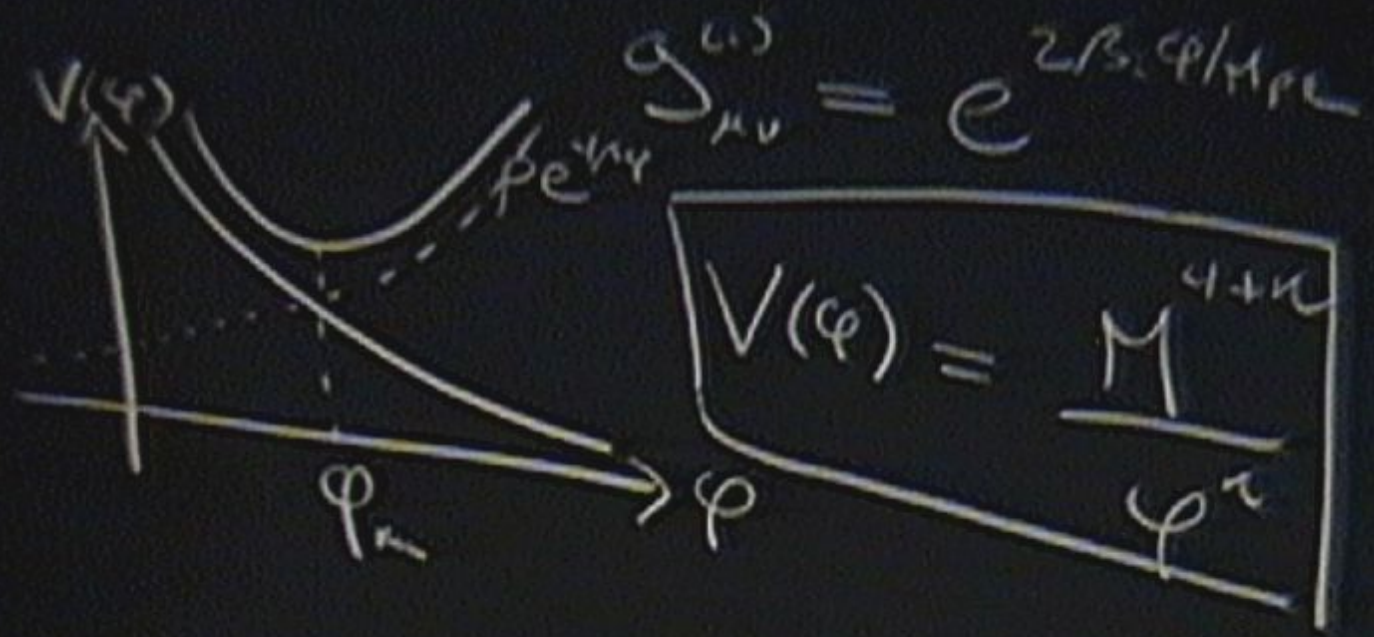
$$w \gg H_0$$

$$w \approx -1 \rightarrow (w \sim -1)$$

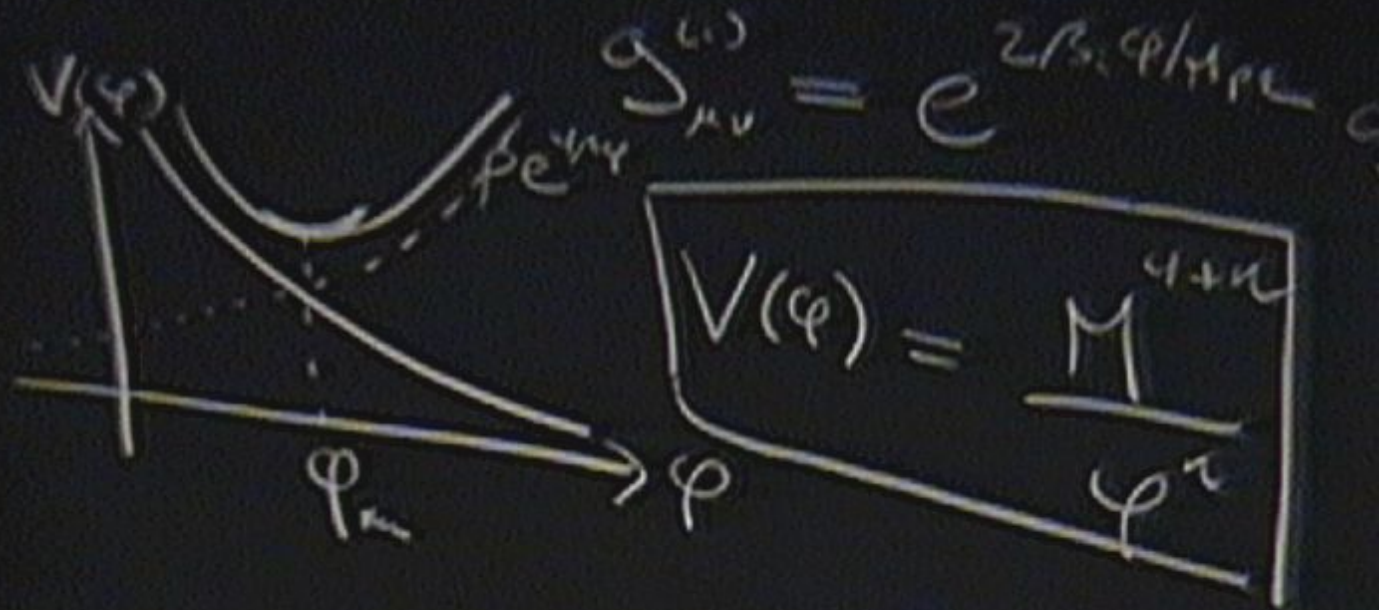




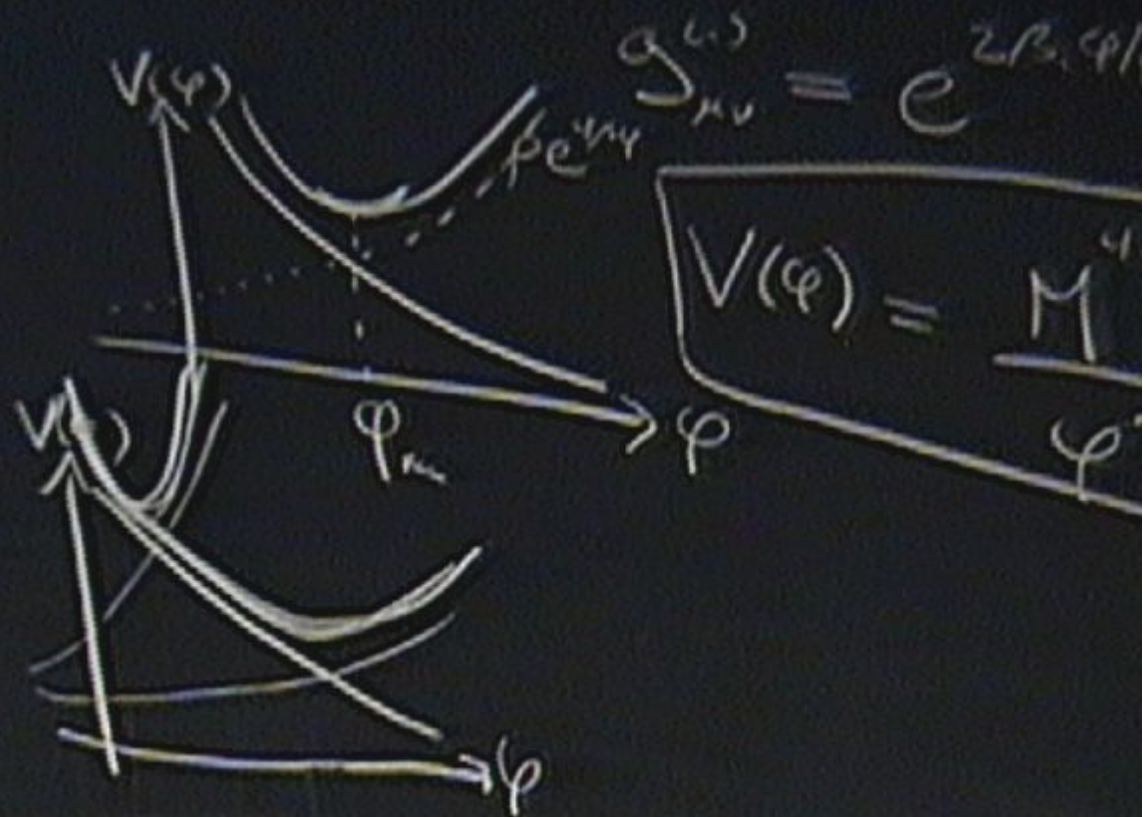
$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\partial\varphi)^2 - V \right\}$$



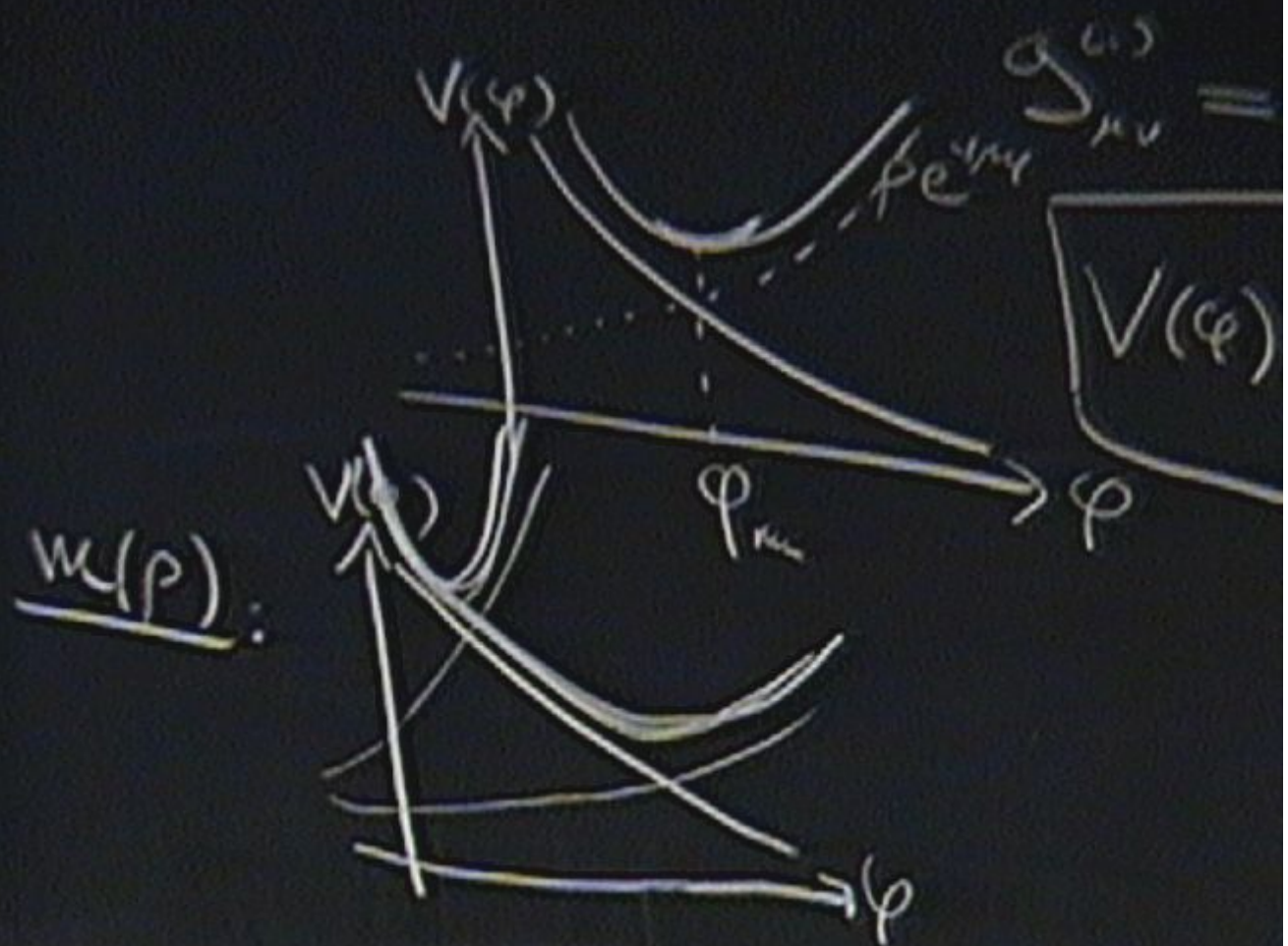
$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) \right\}$$

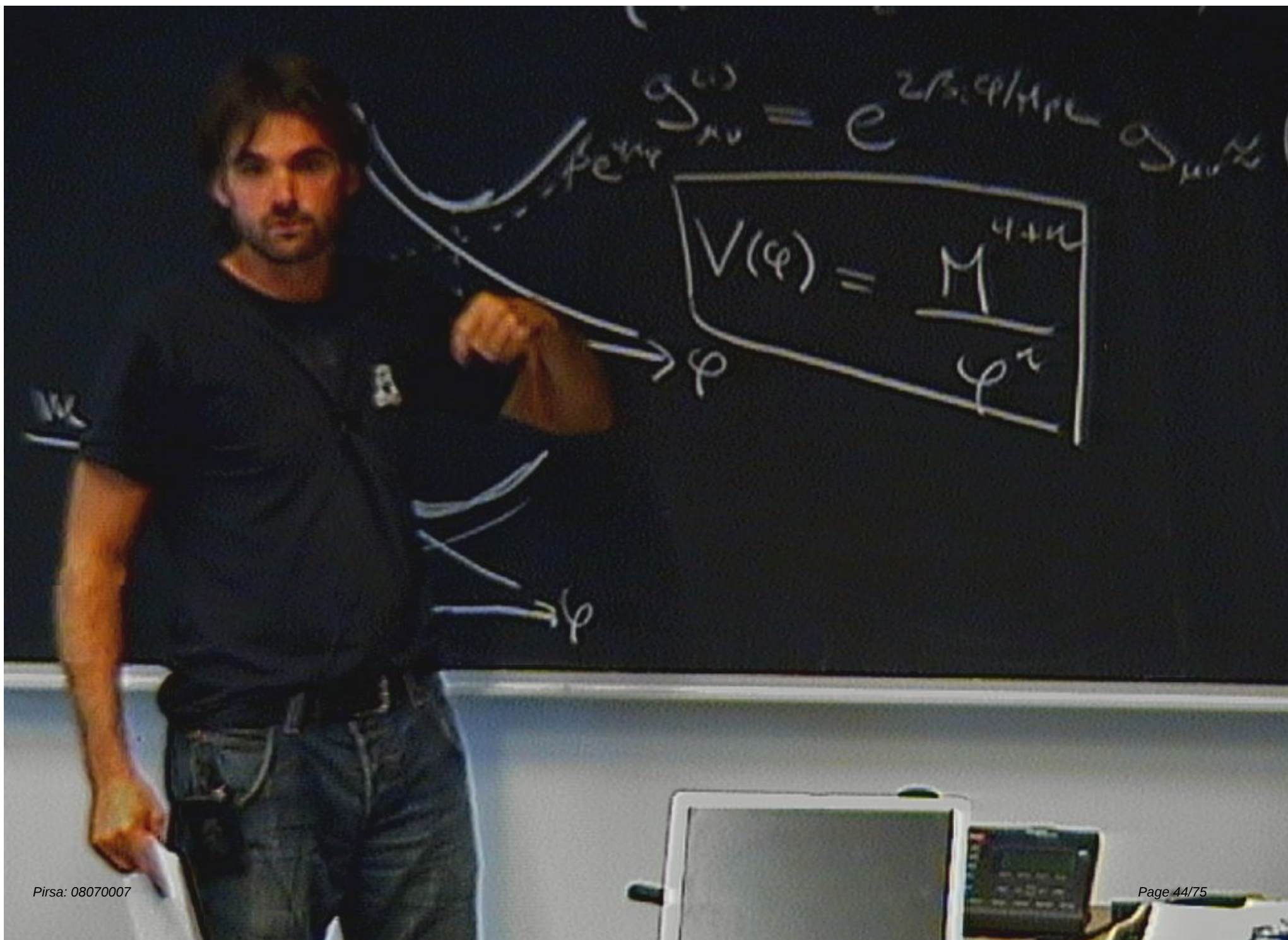


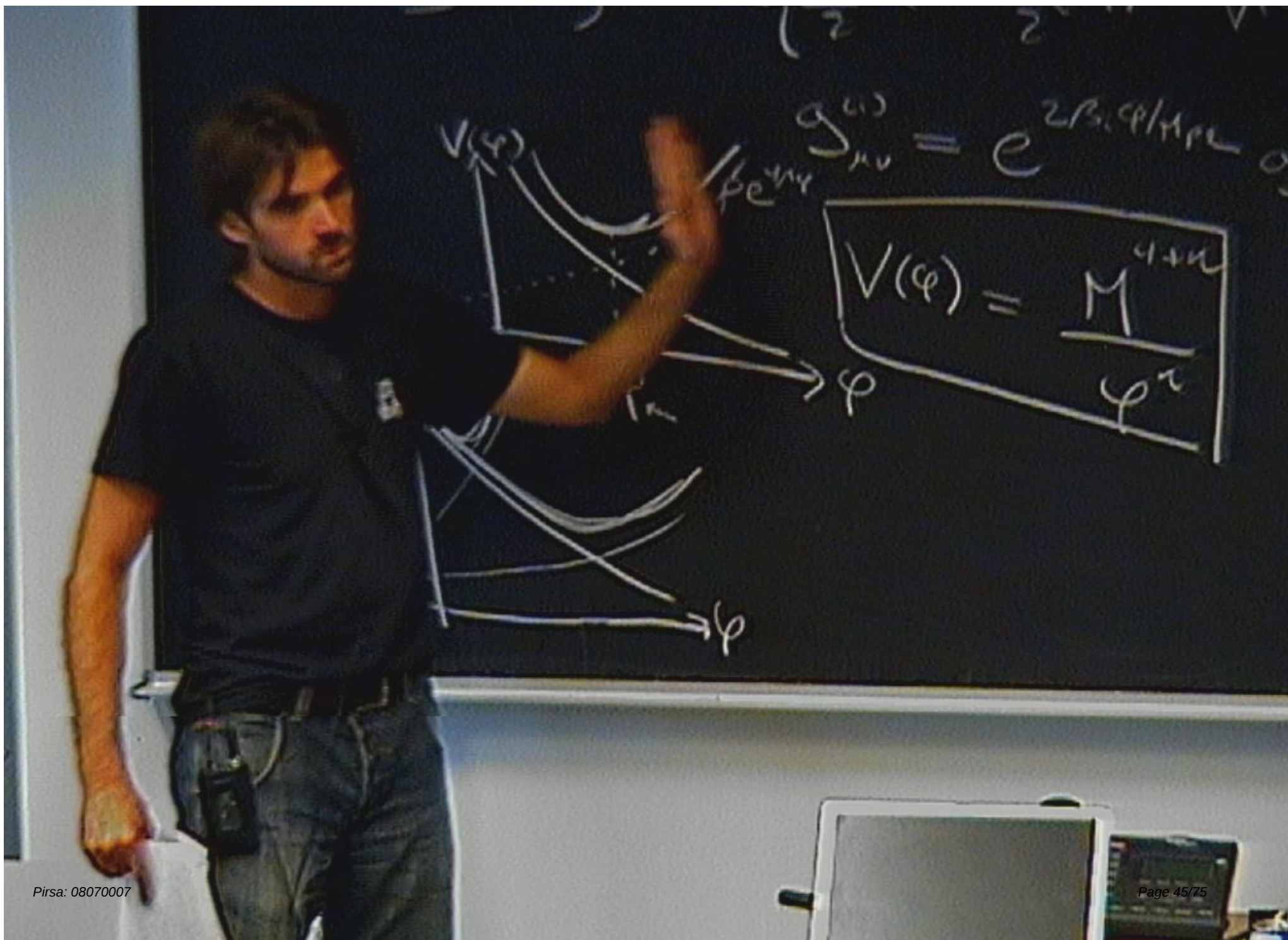
$$S = \int d^4x \sqrt{-g} \left\{ \frac{M_{Pl}^2}{2} R - \frac{1}{2} (\partial\mu)^2 \right.$$

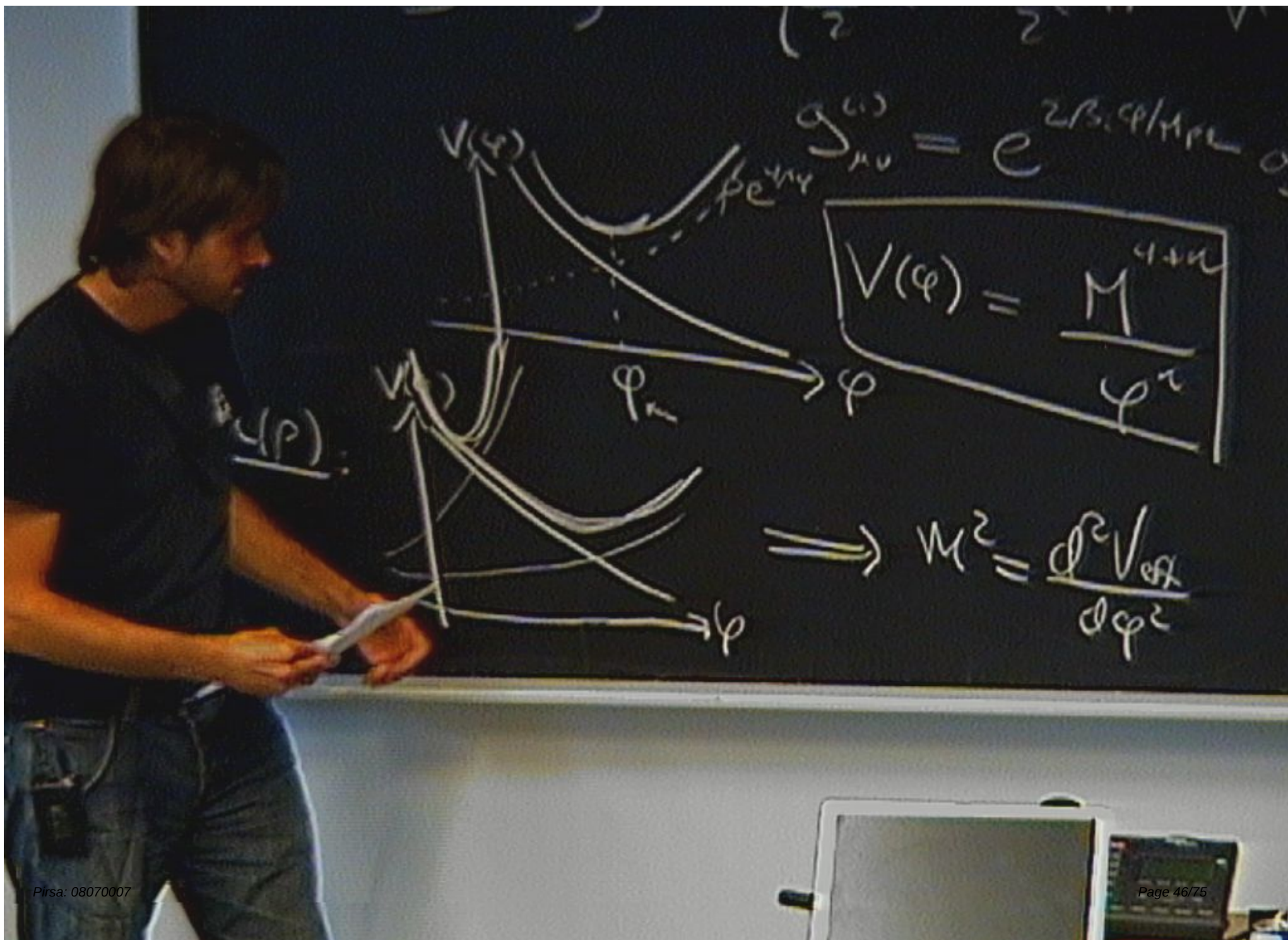


$W(\varphi)$:

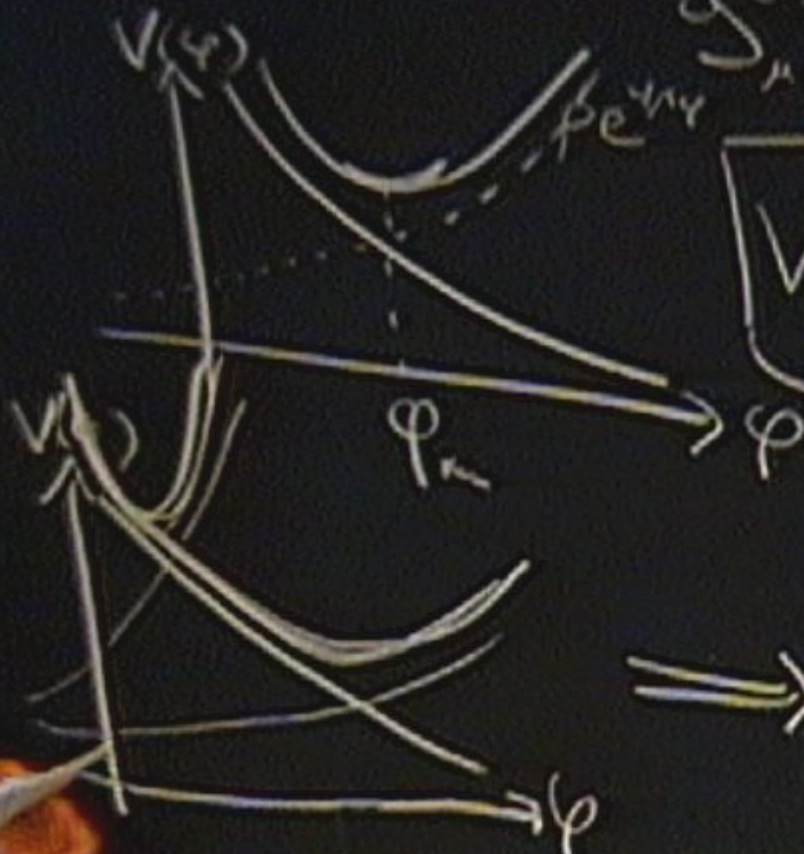






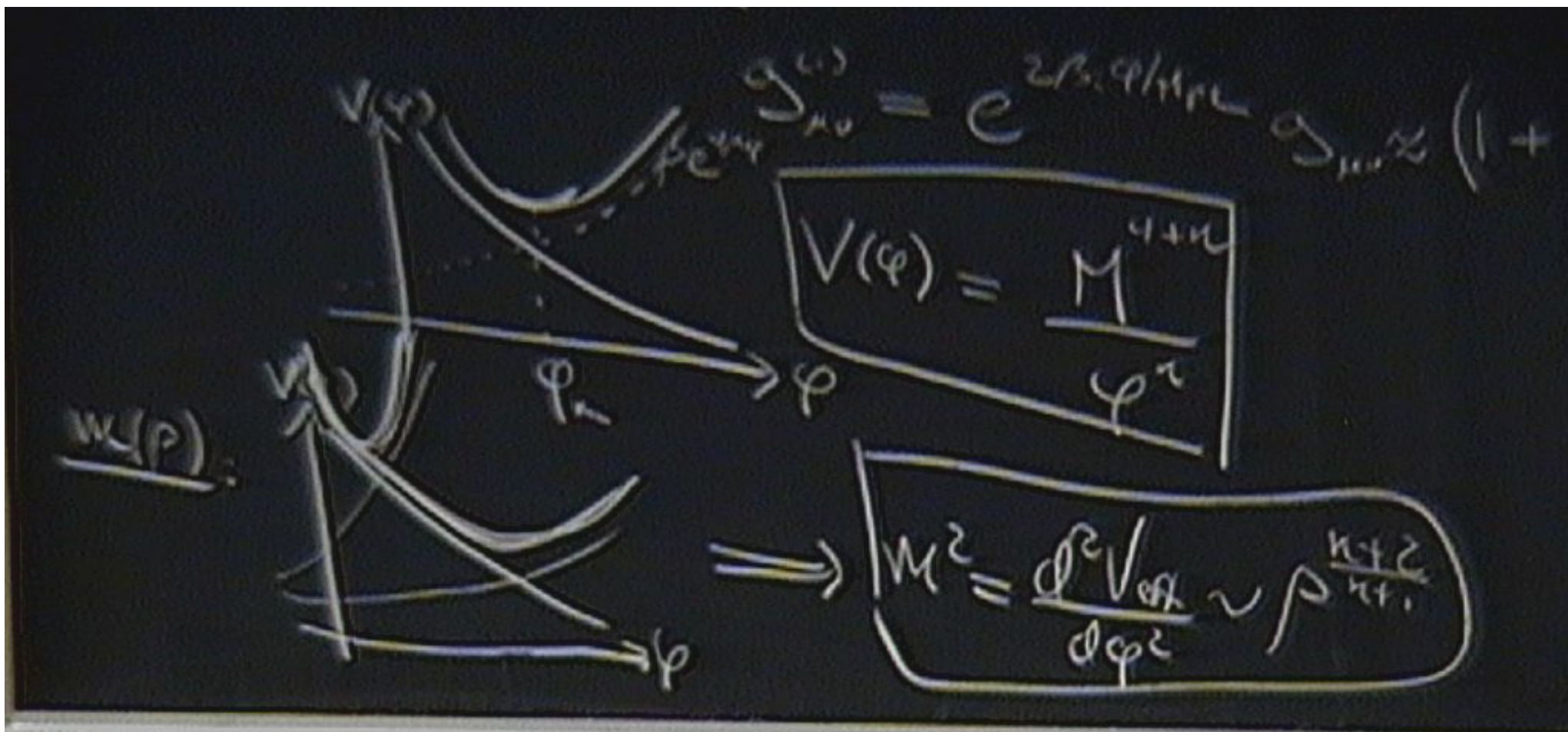


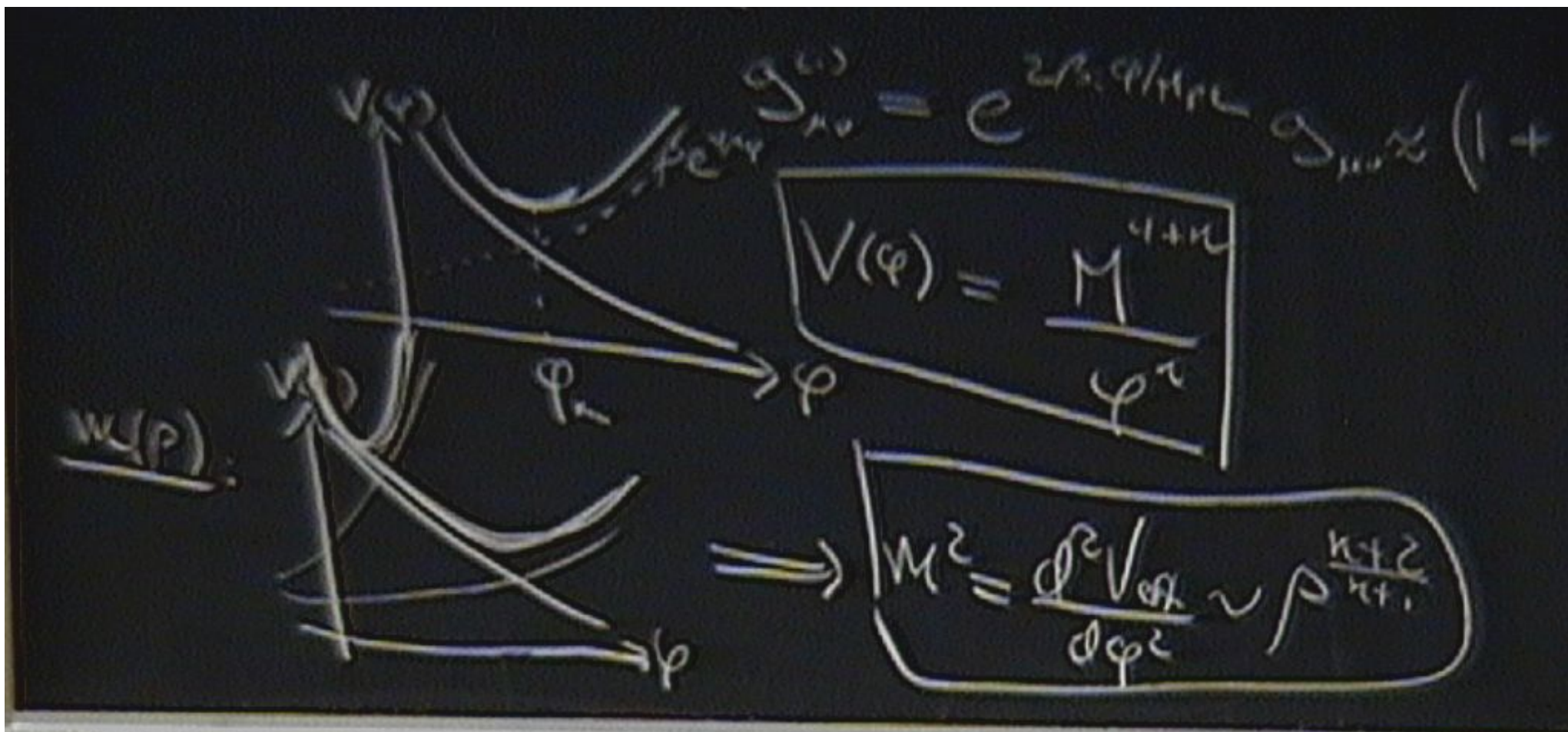
$$g_{\mu\nu}^{(0)} = e^{2\beta_0 \phi / M_{\text{Pl}}} g_{\mu\nu}^{\text{EH}}$$

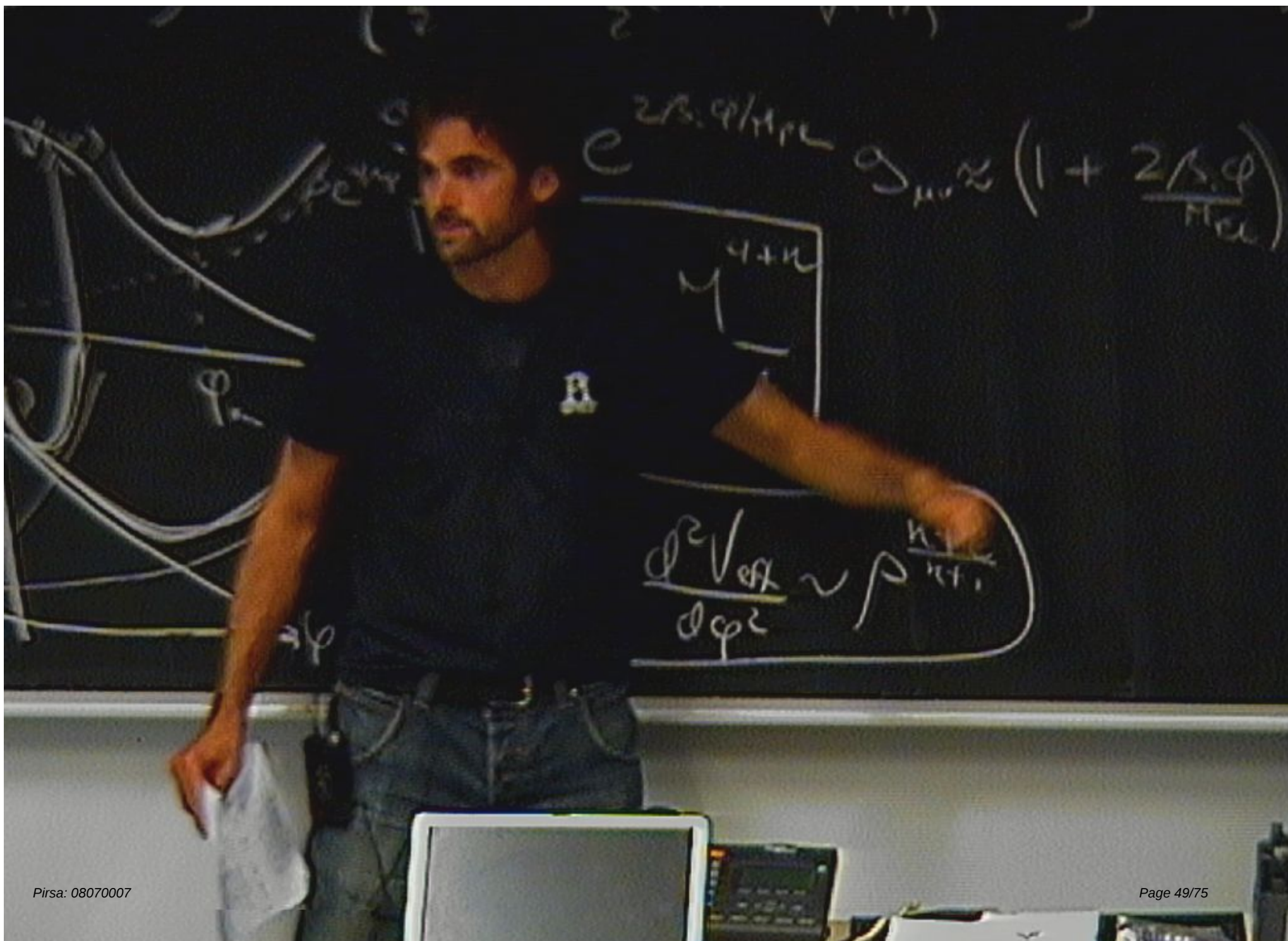


$$V(\phi) = \frac{M^{4+n}}{\phi^2}$$

$$\Rightarrow m^2 = \frac{d^2 V}{d\phi^2}$$







$$\underline{\beta_i^{\text{est}} = \beta_i^{\text{eff}}(p)}$$

IF THE THEORIES

$$\frac{dV}{d\beta} = \dots$$

$$\dots$$

$$= \dots$$

$$V_s(\omega) = \dots$$

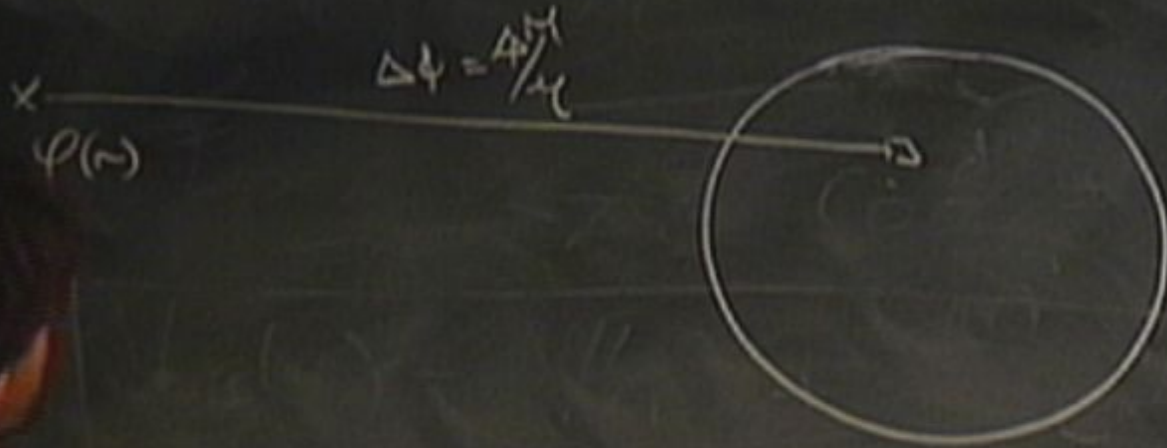
$$1, 1, 1, 2$$

$\beta_i^{\text{est}} = \beta_i^{\text{eff}}(\rho)$: THIN-SHELL EFFECT

$$\underline{\beta_c^{est} = \beta_c^{est}(p)} : \text{THIN-SHELL EFFECT}$$

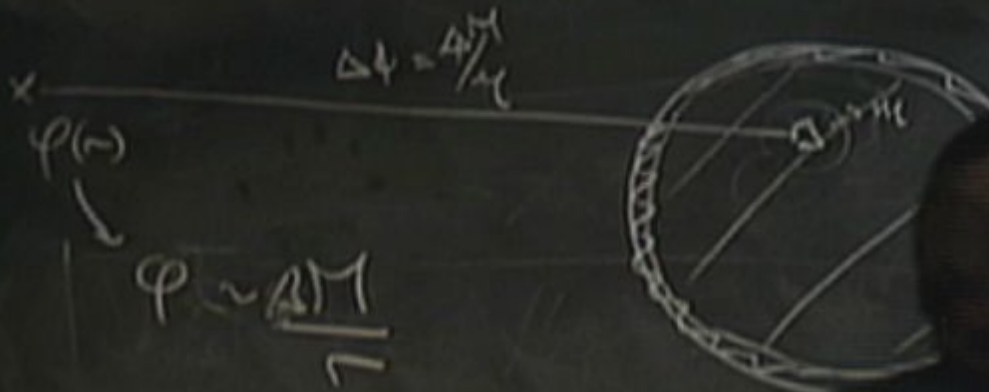


$$\underline{\beta_i^{\text{est}} = \beta_i^{\text{est}}(\rho)} : \text{THIN-SHELL EFFECT}$$



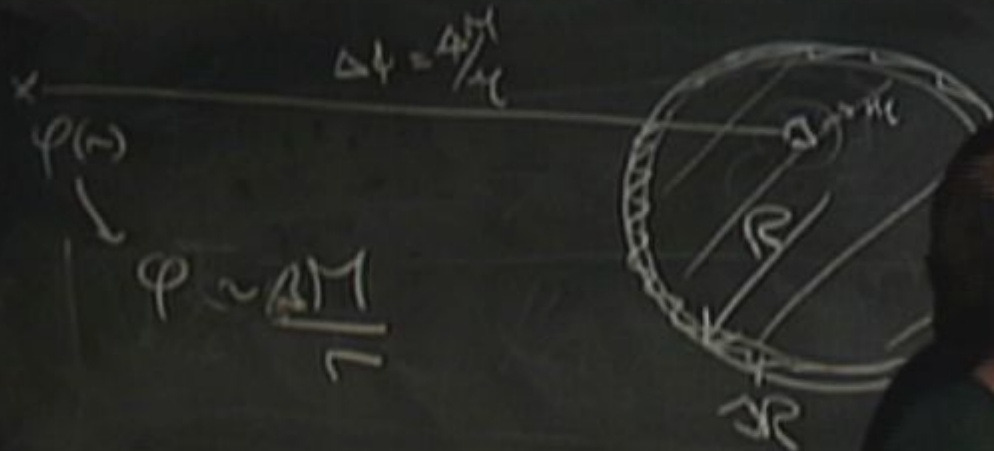
$$\underline{\beta_c^{eff} = \beta_c^{eff}(p)} : \text{THIN-SHELL EFFECT}$$

$$\varphi(r) = \frac{\beta M}{r} e^{-mr} \frac{\Delta R}{R}$$



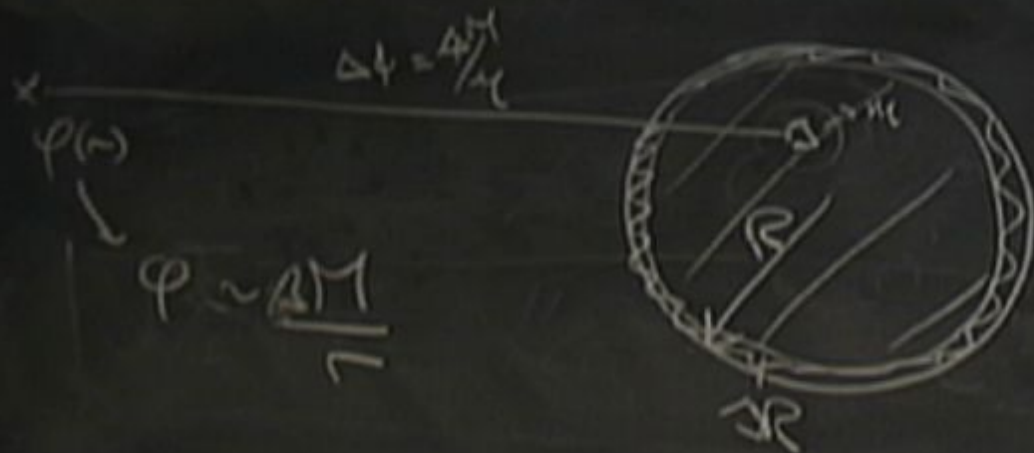
$$\underline{\beta_0^{est} = \beta_0^{est}(p)} : \text{THIN-SHELL EFFECT}$$

$$\varphi(r) = \frac{\beta M}{r} e^{-mr} \frac{\Delta R}{R}$$



$$\varphi \sim \frac{\beta M}{r}$$

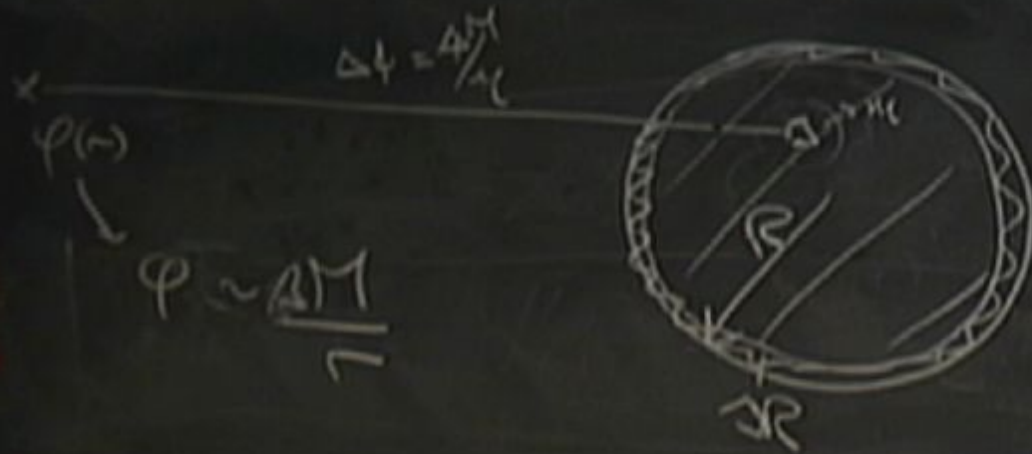
$$\underline{\beta_{est} = \beta_{est}(p)} : \text{THIN-SHELL EFFECT}$$



$$\phi(r) = \frac{\beta M e^{-mr}}{r} \frac{\Delta R}{R}$$

$$\frac{\Delta R}{R} \rightarrow \frac{1}{6\beta} \frac{\phi_{at} - \phi_{in}}{\Phi_{at} - \Phi_{in}}$$

$$\underline{\beta_{est} = \beta_{est}(p)} : \text{THIN-SHELL EFFECT}$$

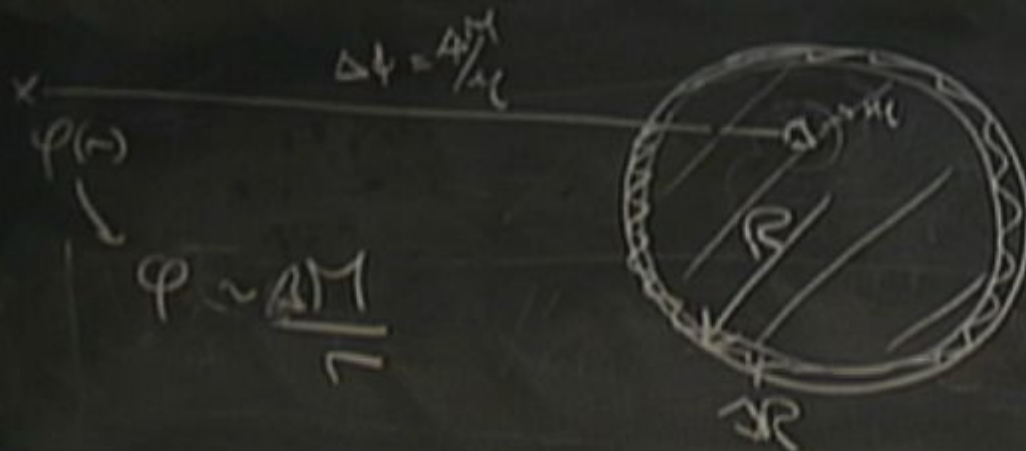


$$\phi(r) = \frac{\beta M}{r} e^{-mr} \frac{\Delta R}{R}$$

$$\frac{\Delta R}{R} \rightarrow \frac{1}{6\beta} \frac{\phi_{at} - \phi_{in}}{\Phi_{at} - \Phi_{in}}$$

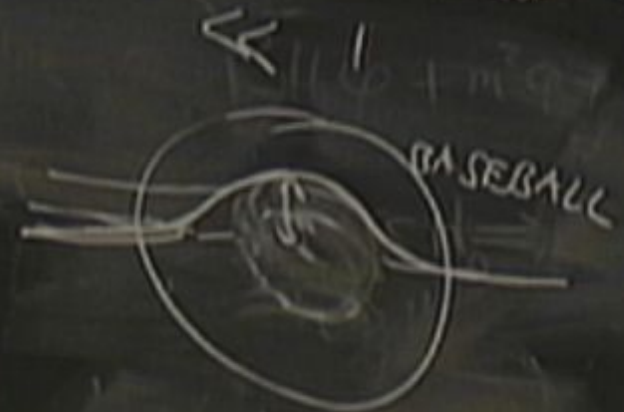
$$\Delta\phi = \frac{4M}{\lambda c}$$

$$\underline{\beta_c^{est} = \beta_c^{est}(p)} : \text{THIN-SHELL EFFECT}$$



$$\phi(r) = \frac{\beta M e^{-mr}}{r} \frac{\Delta R}{R}$$

$$\frac{\Delta R}{R} \rightarrow \frac{1}{6/\beta} \frac{(\phi_{at} - \phi_{in})}{\Phi_{at} - \Phi_{in}}$$



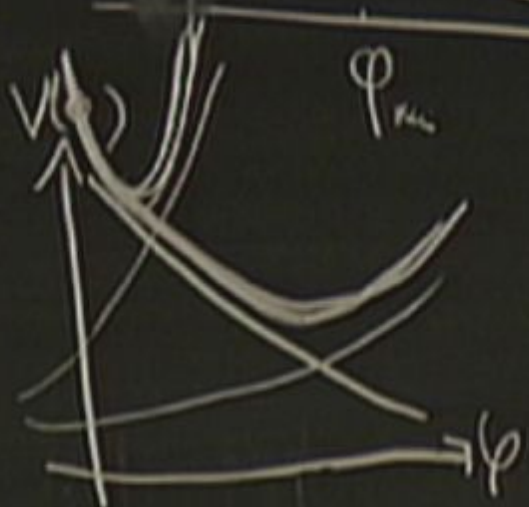
MECHANISM:



LAB: $F_{\varphi} = \frac{\beta^2 M_1 M_2}{r^2} \left(\frac{\Delta R}{R} \right)^2$

SPACE: $= \frac{\Delta^2}{r^2} M_1 M_2$

$w(\rho)$:



$\Rightarrow w^2 = \frac{d^2 V_{eff}}{d\phi^2} \sim \rho^{\frac{n+2}{n+1}}$

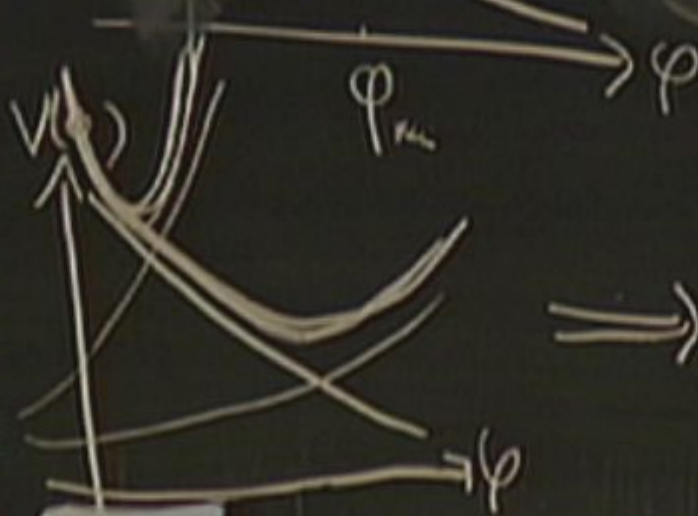
MECHANISM:



LAB: $F_{\varphi} = \frac{\beta^2 M_1 M_2}{r^2} \left(\frac{\Delta R}{R} \right)^2 e^{-m r}$

SPACE:

$$= \frac{\Delta^2}{r^2} M_1 M_2$$



$$\Rightarrow \left| M^2 = \frac{d^2 V_{\varphi}}{d\varphi^2} \sim \rho^{\frac{n+2}{n+1}} \right|$$

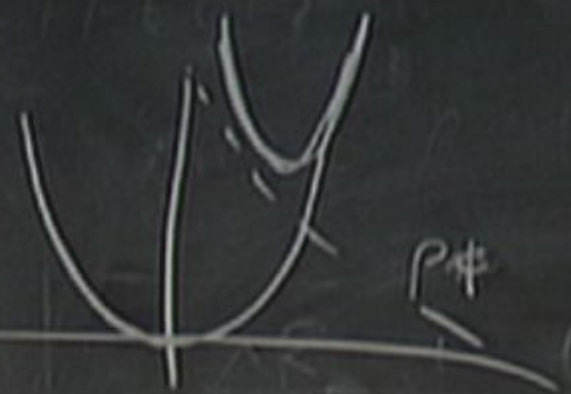
$$V(\phi) = \frac{\gamma \phi^4}{4!} - \frac{\beta \phi}{4! \epsilon}$$

THIN SHELL EFFECT?



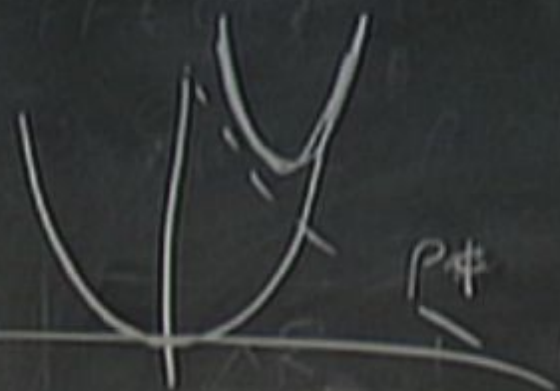
$$V(\phi) = \frac{\gamma \phi^4}{4!} - \frac{\beta \rho}{M_{\text{Pl}}}$$

$$n \sim \gamma^{-1/6} \beta^{-1/3} \rho^{-1/3}$$



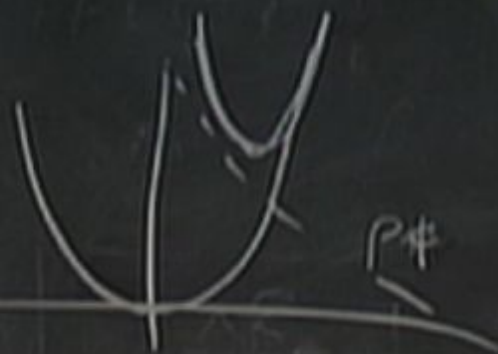
$$V(\phi) = \frac{\gamma \phi^4}{4!} - \frac{\beta \rho}{M_{\text{pl}}}$$

$$m_{\text{eff}}^{-1} \propto \gamma^{-1/6} \beta^{-1/3} \rho^{-1/3}$$



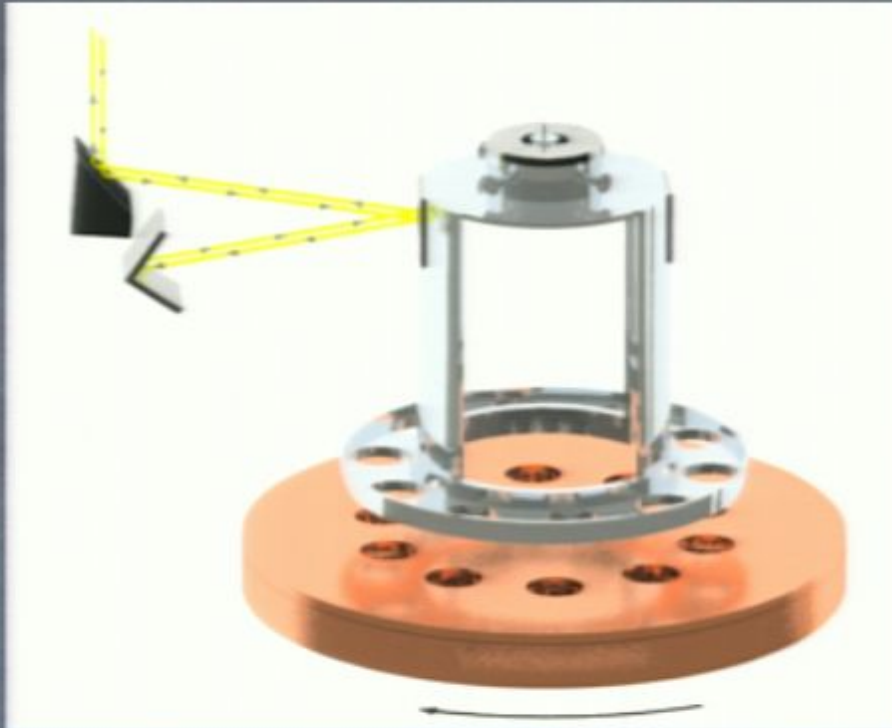
$$V(\phi) = \frac{\gamma \phi^4}{4!} - \frac{\beta \rho}{M_{\text{Pl}}}$$

$$m_{\text{eff}}^{-1} \sim \gamma^{-1/6} \beta^{-1/3} \rho^{-1/3}$$

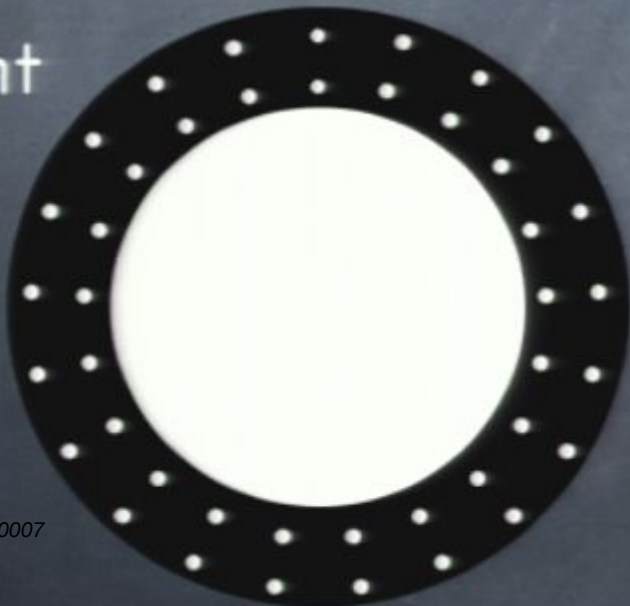


$$\gamma, \beta \sim \mathcal{O}(1) \quad \& \quad \rho \sim 10^3 / \text{cm}^3 \implies m_{\text{eff}}^{-1} \sim 0.1 \text{ mm}$$

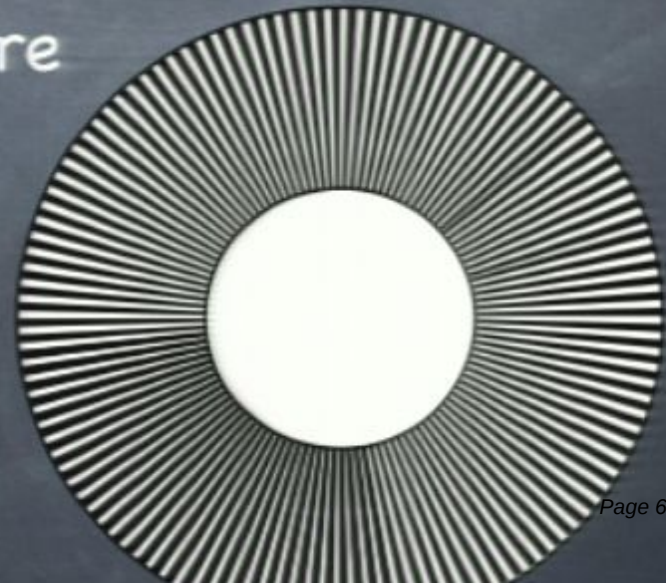
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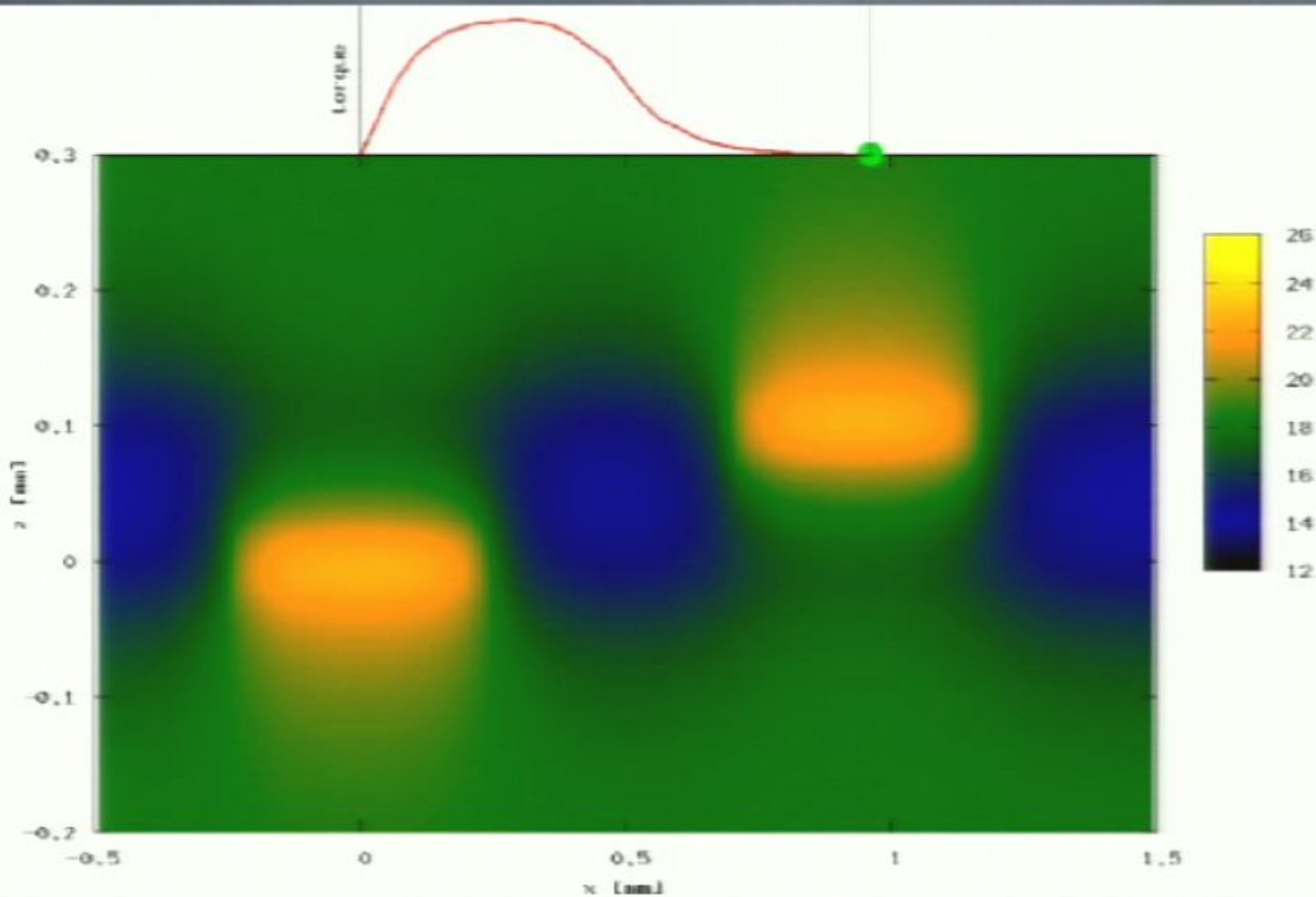


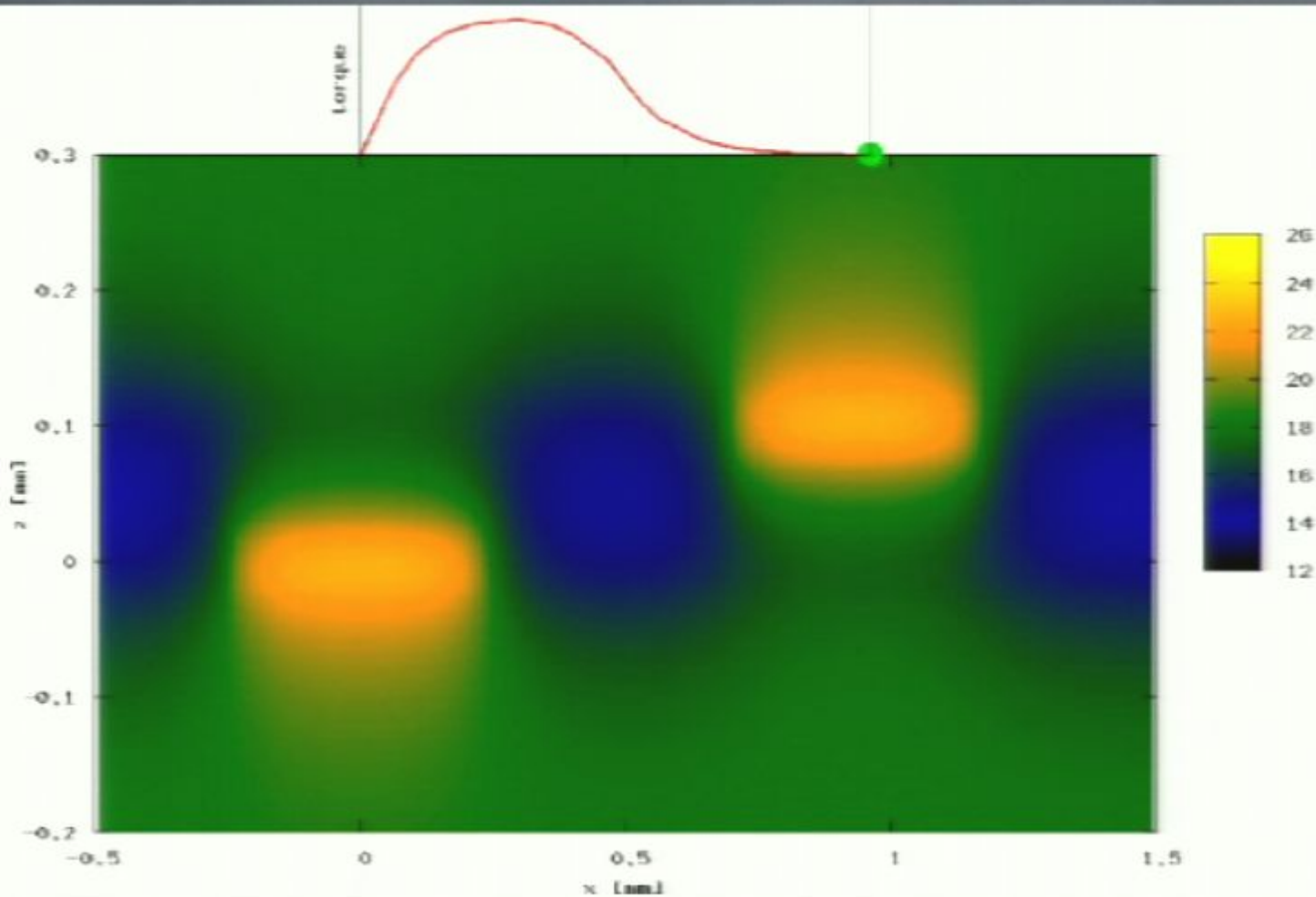
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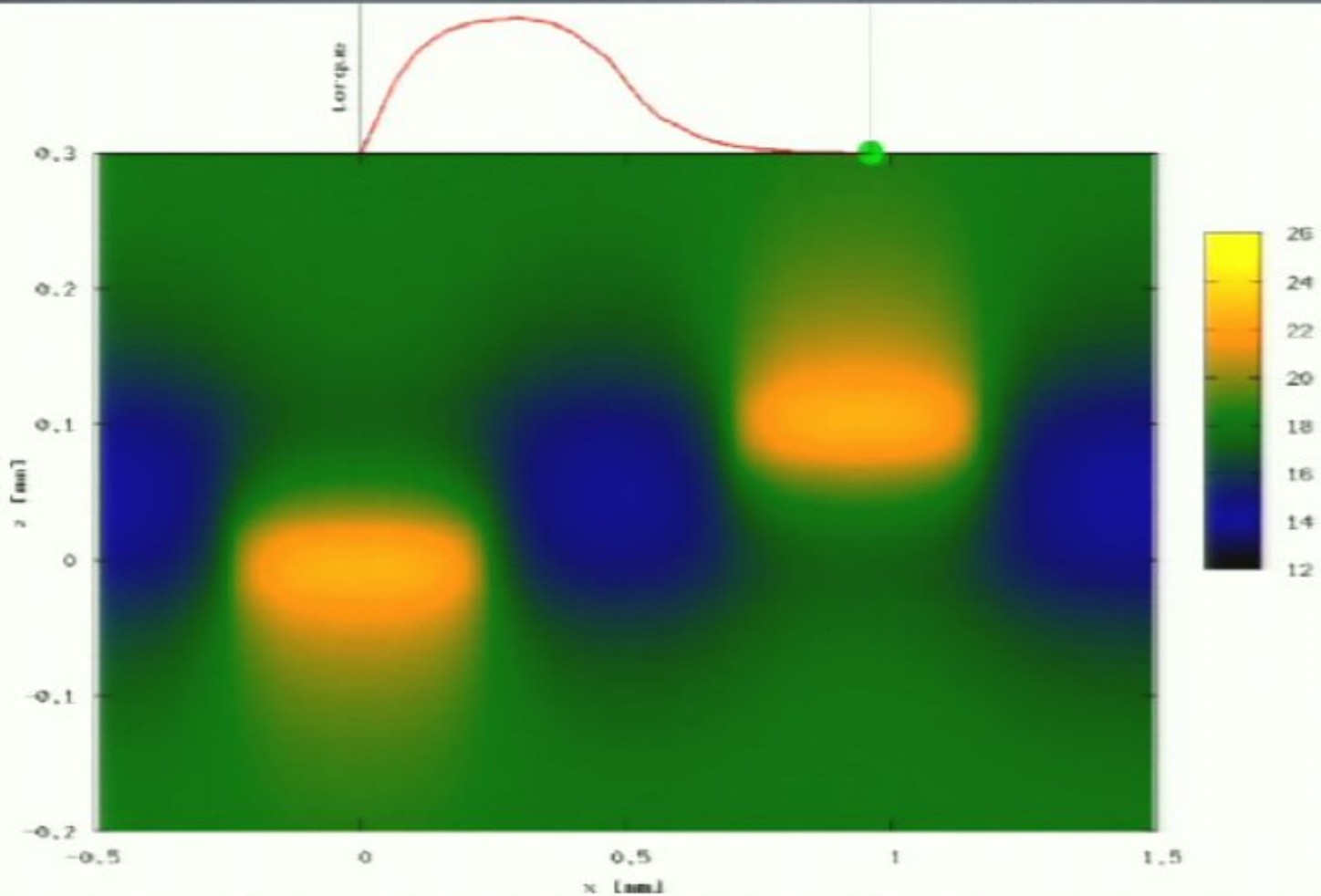


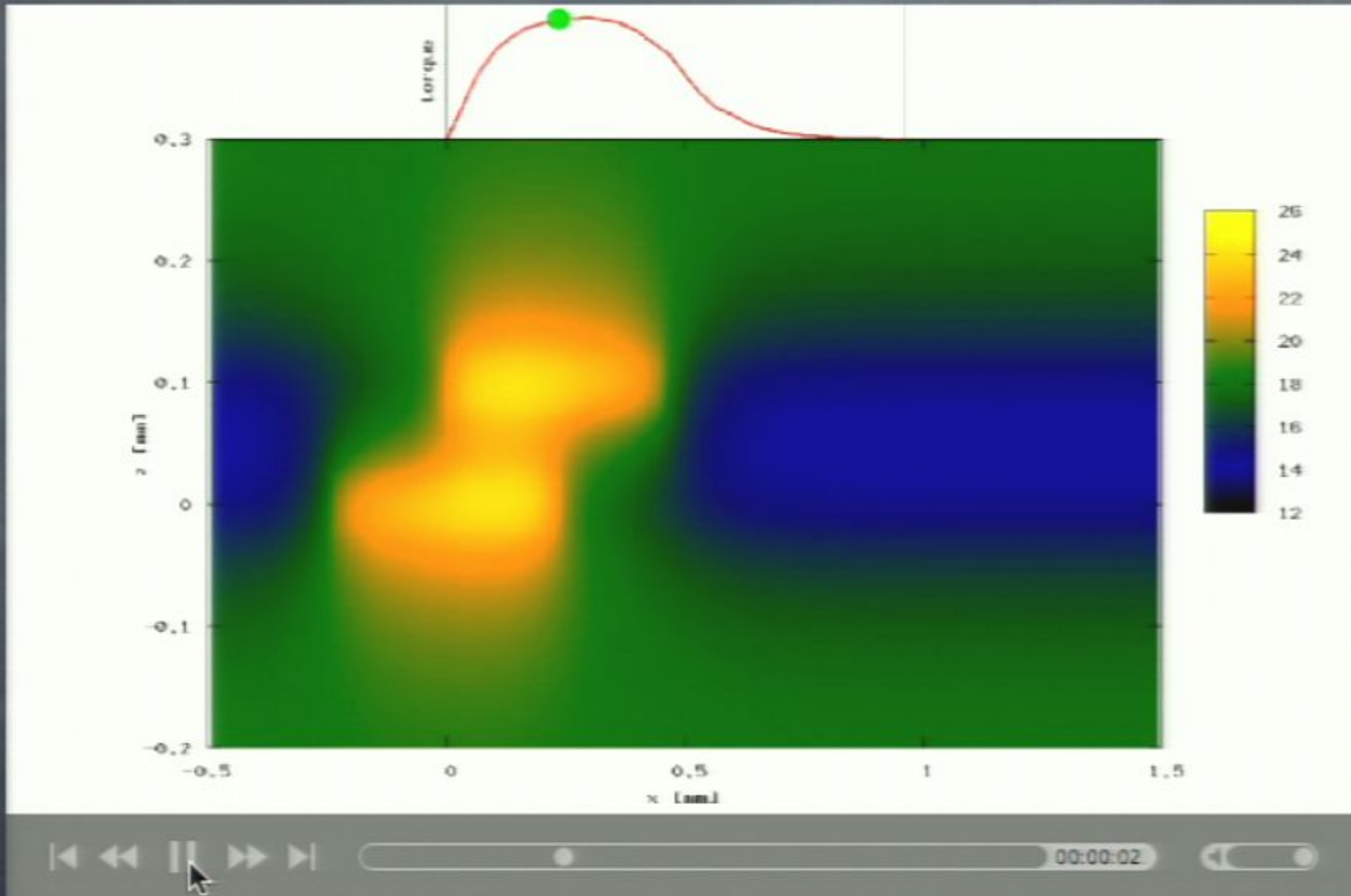
Future

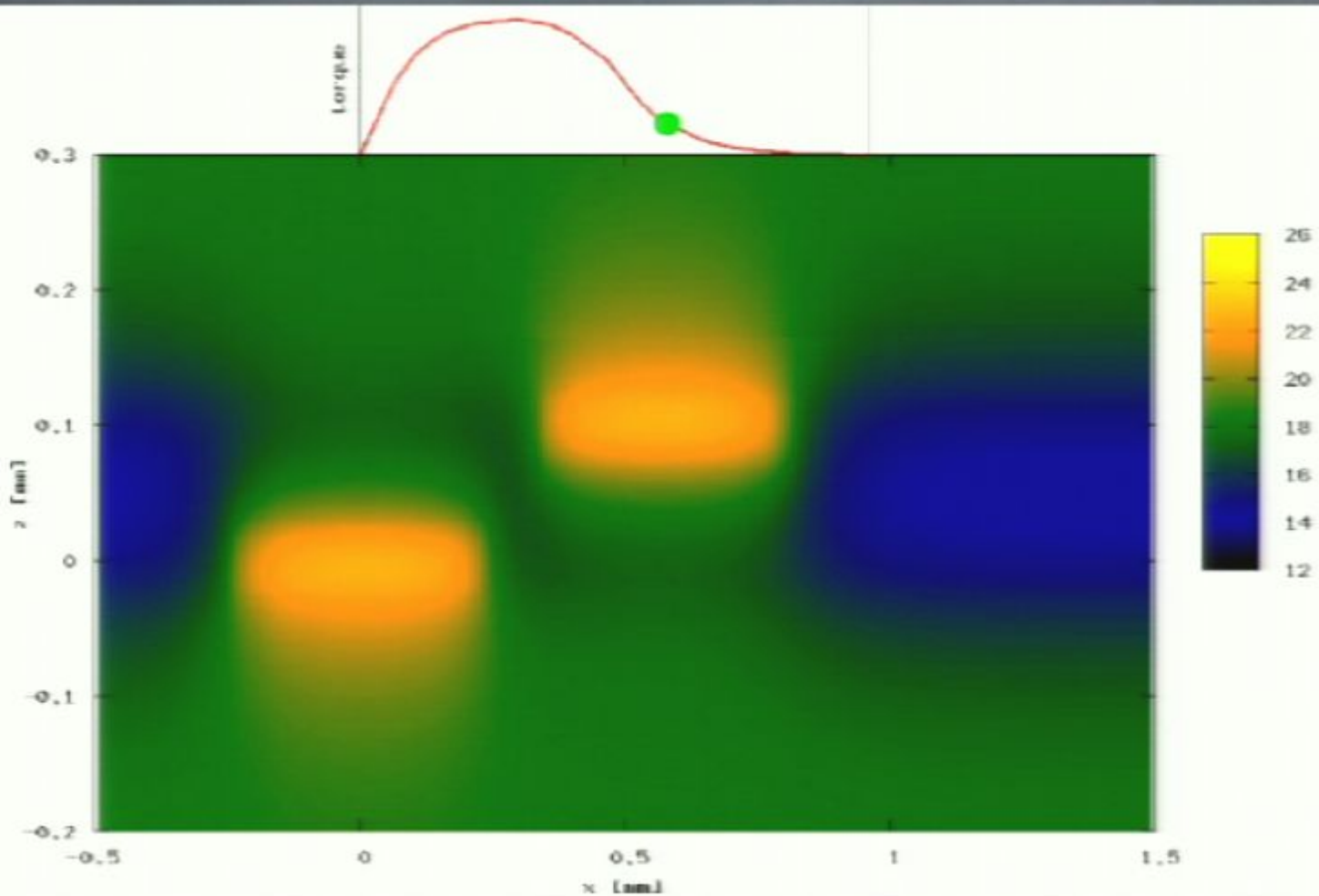


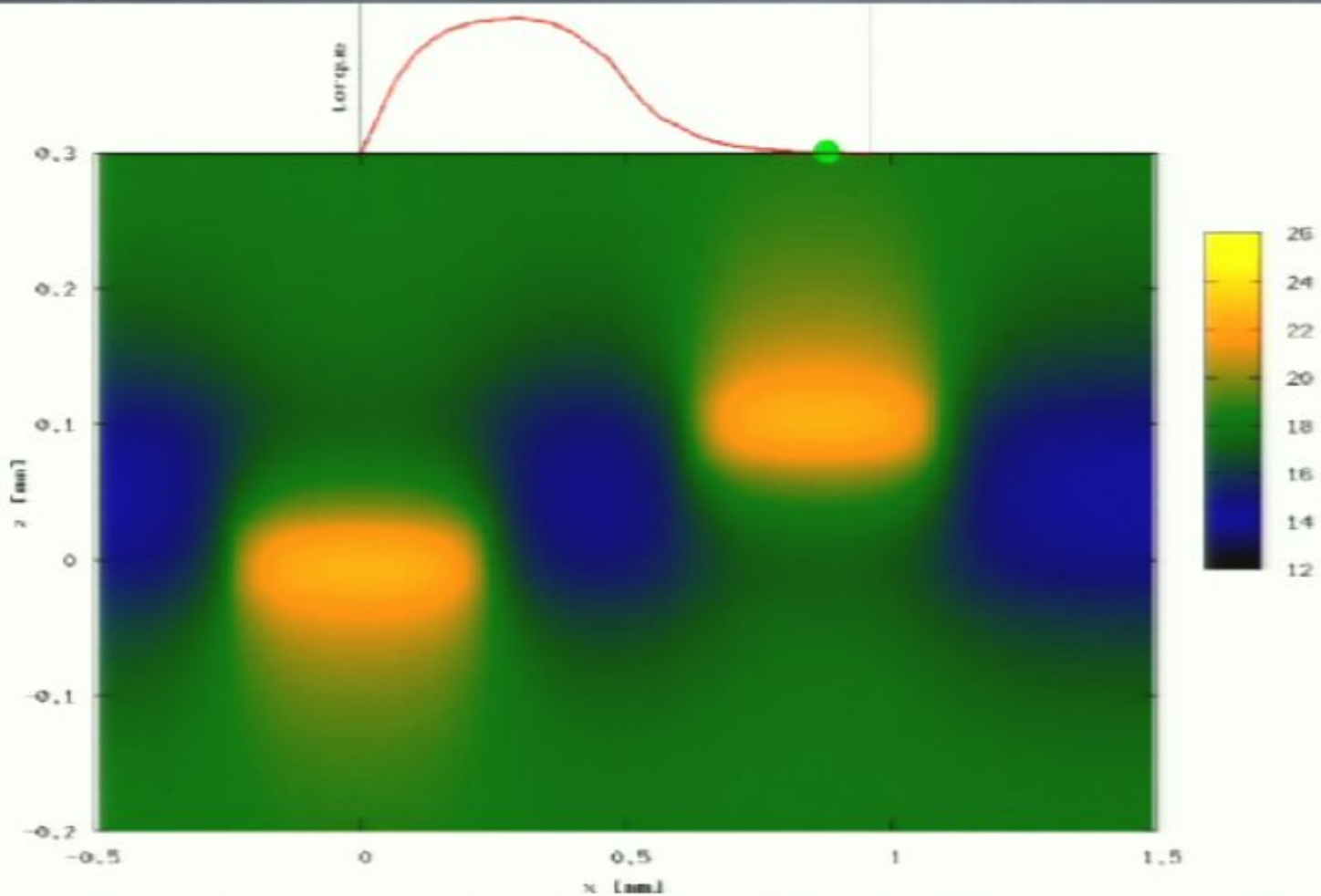


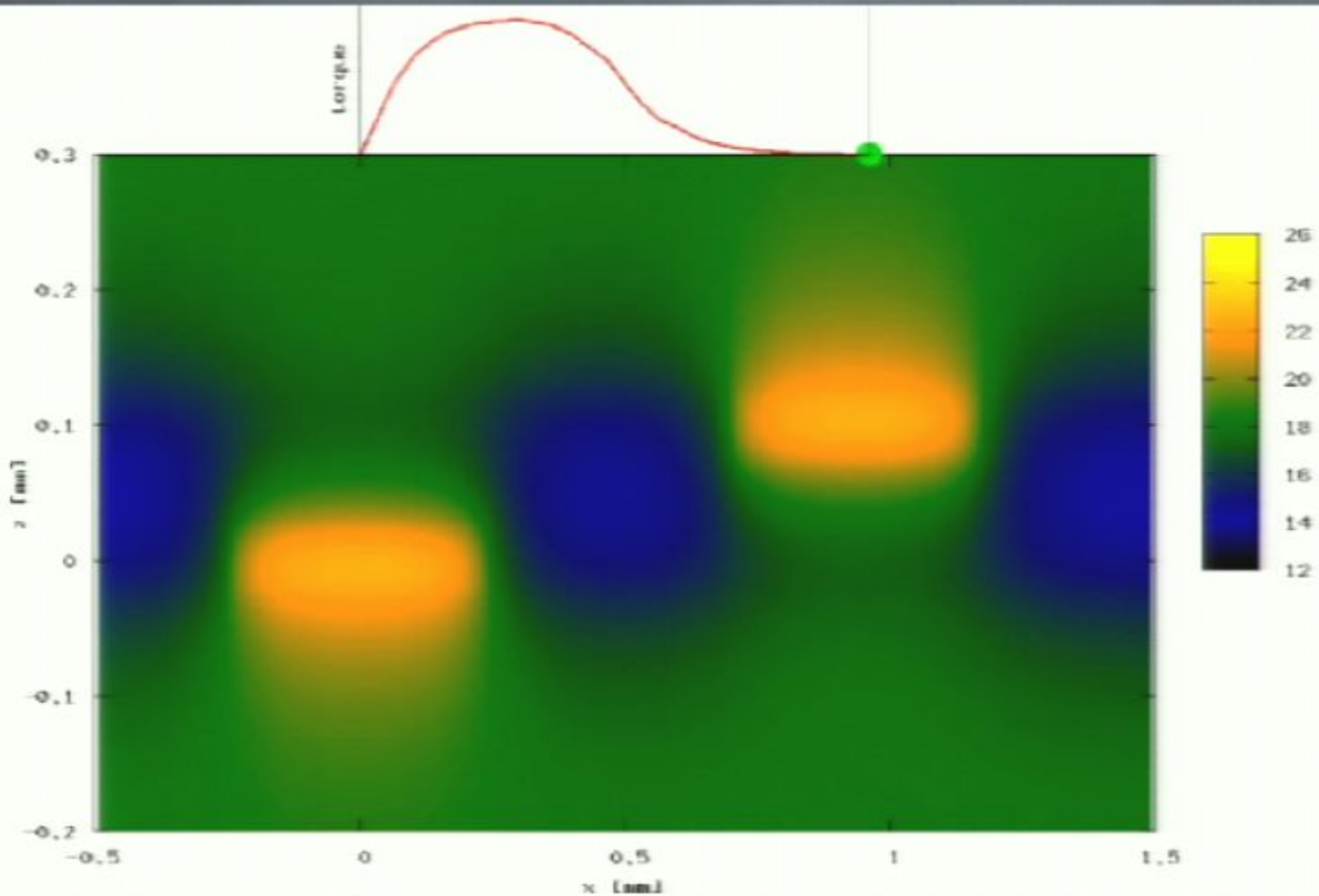


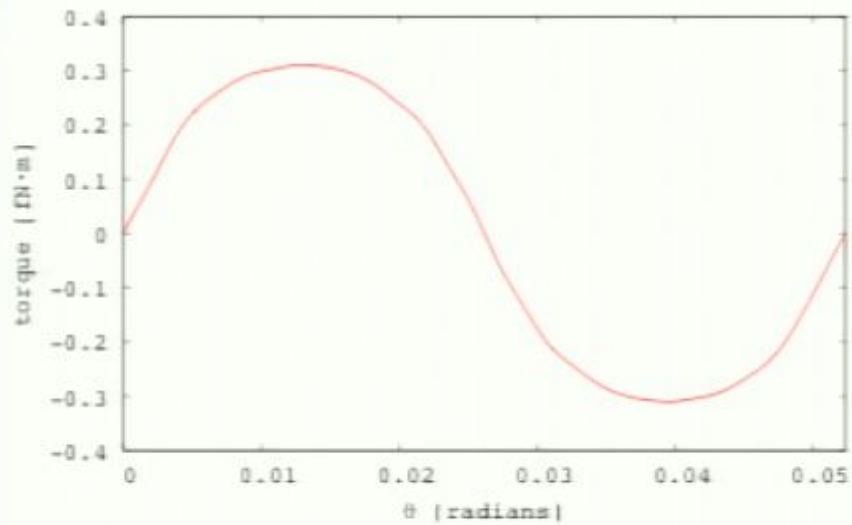
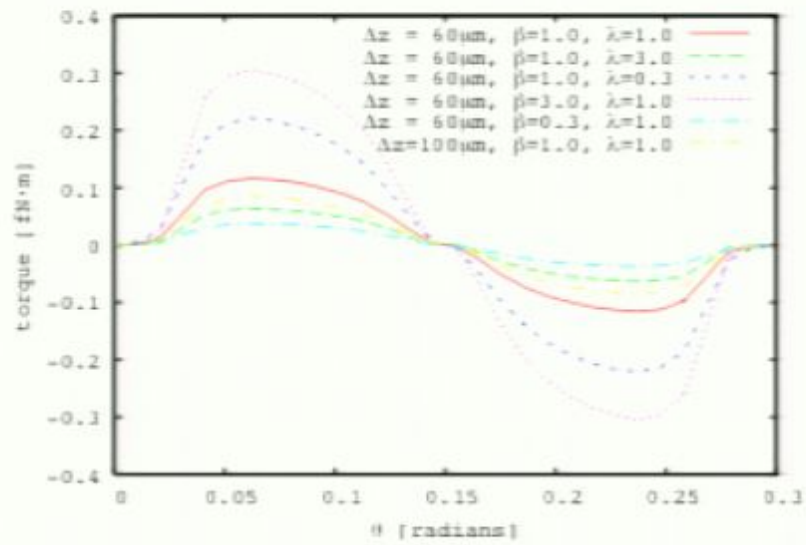
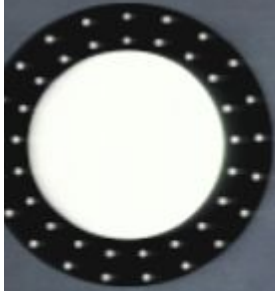








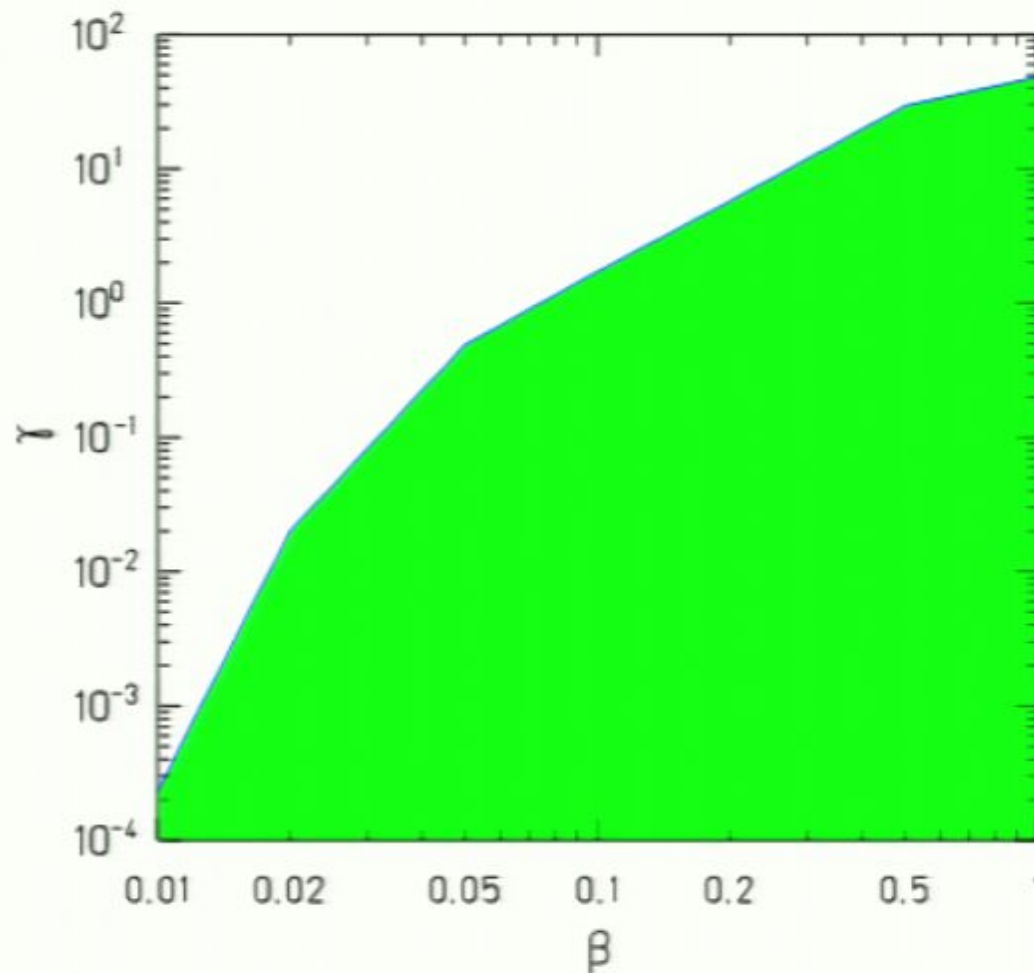




Chameleon Constraints

Adelberger et al., PRL (2007)

$$V_{\text{eff}}(\phi, \vec{x}) = \frac{\gamma}{4!} \phi^4 - \frac{\beta}{M_{\text{Pl}}} \rho(\vec{x}) \phi$$



gammeV expt (FNAL)

Brax et al. (2007)

GammeV collaboration, to appear

$$e^{\beta\phi/M_{\text{Pl}}} F_{\mu\nu} F^{\mu\nu}$$

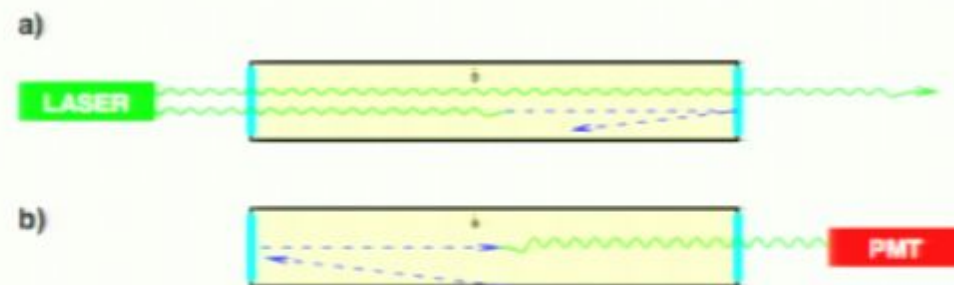


Figure 2: Schematic of the GammeV apparatus. a) Chameleon production phase: photons propagating through a region of magnetic field oscillate into chameleons. Photons travel through the glass endcaps whereas chameleons see the glass as a wall and are trapped. b) Afterglow phase: chameleons in the chamber gradually decay back into photons and are detected by a photomultiplier tube.

from A. Weltman (2008)