

Title: Gravitino Dark Matter and Implications for Phenomenology at the LHC

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Abstract: Considering gravitino dark matter scenarios, cosmological constraints on the sparticle masses and on the reheating temperature of inflation will be discussed. These constraints are relevant for prospects of phenomenology at the LHC and for our understanding of inflation and the baryon asymmetry of the Universe.

Gravitino Dark Matter and Implications for Phenomenology at the LHC



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June 6th, 2008

PASCOS 2008 @ Perimeter Institute

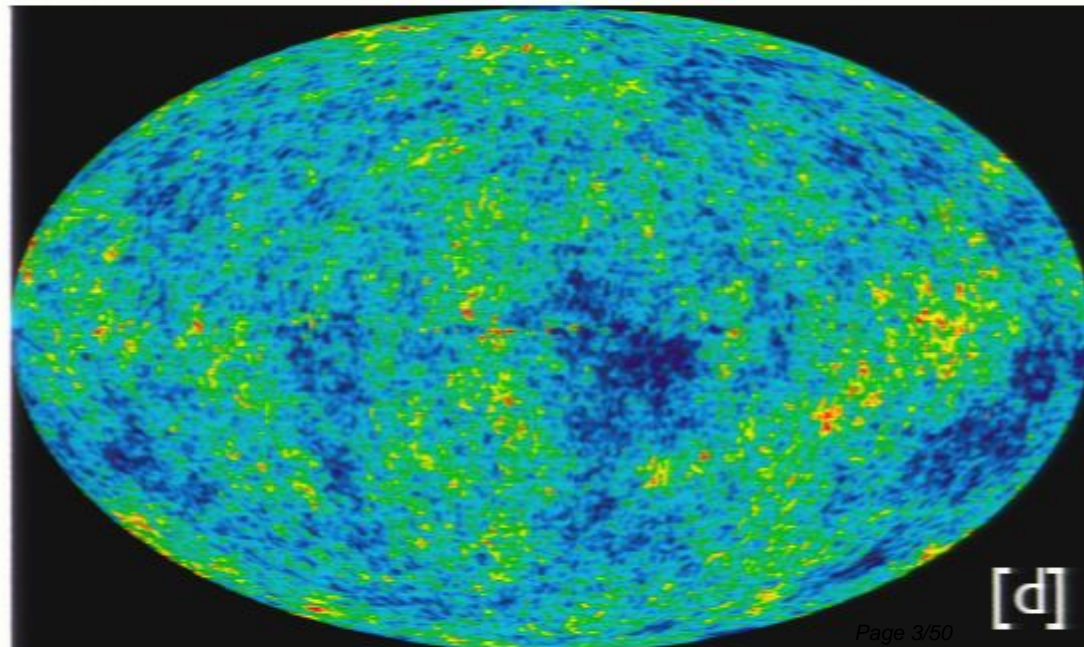
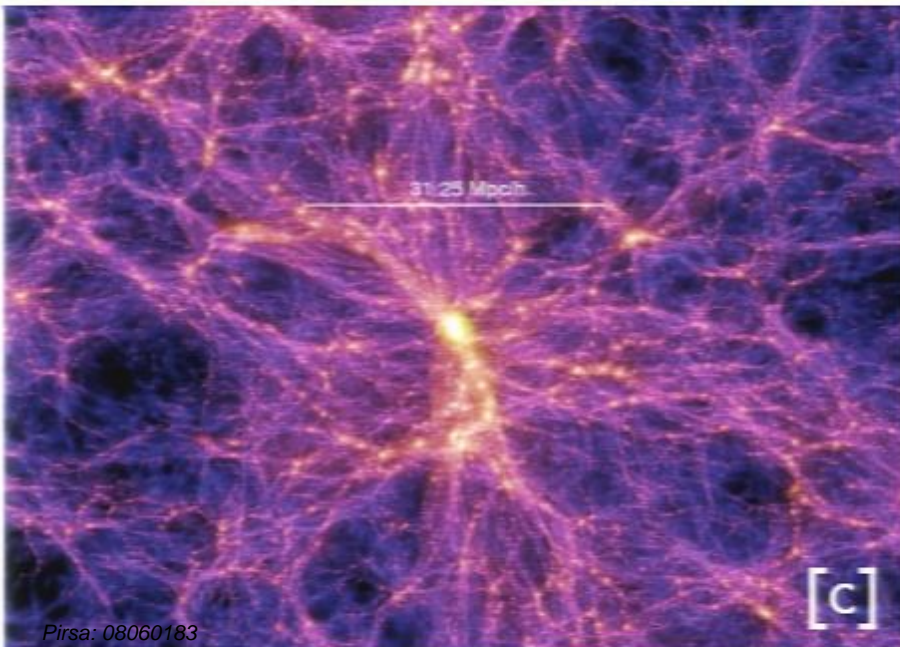
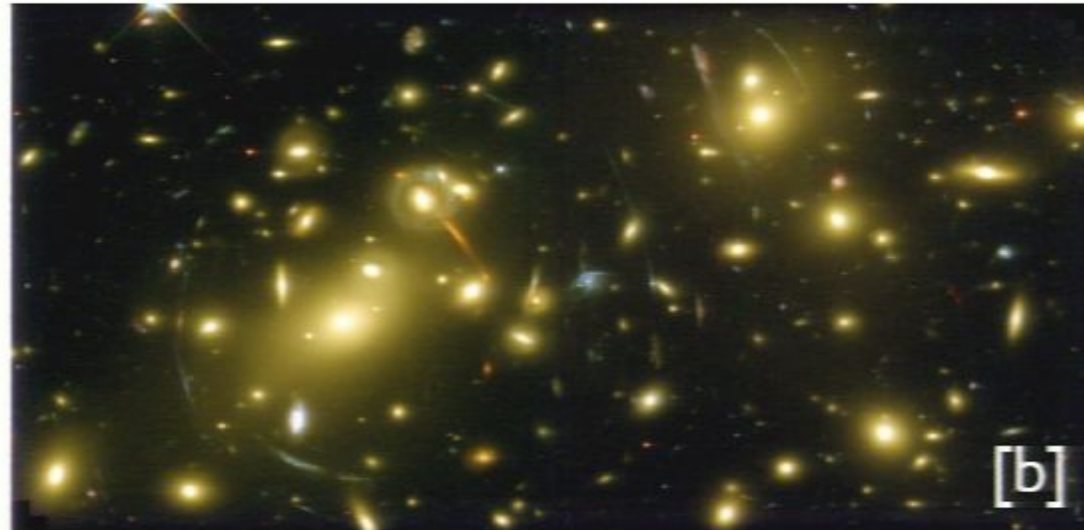


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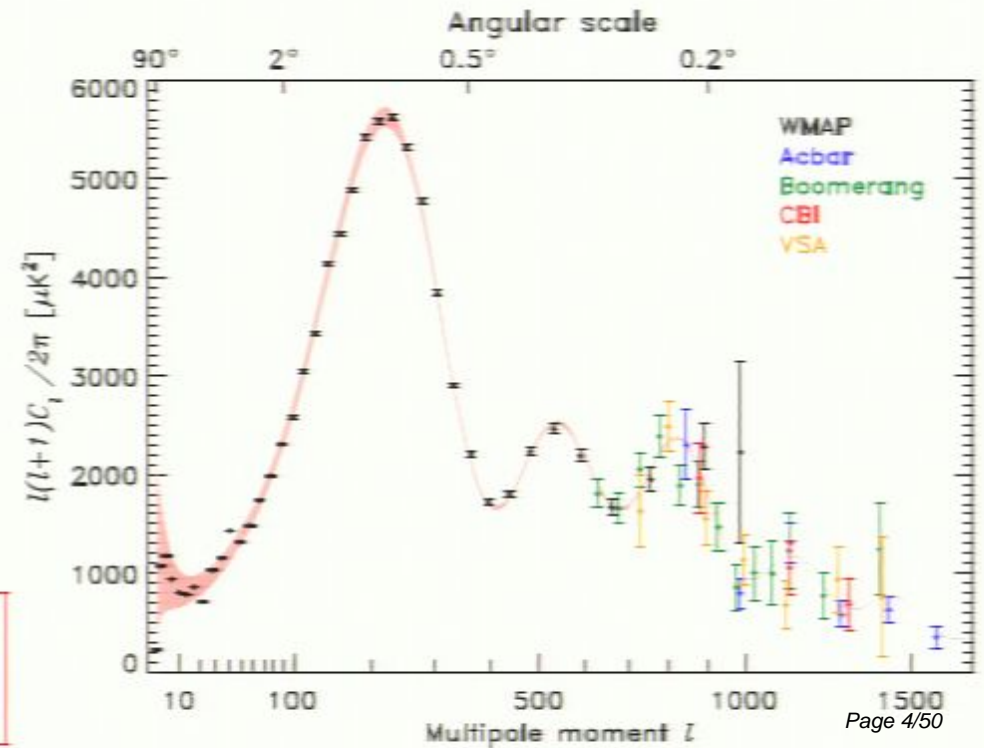
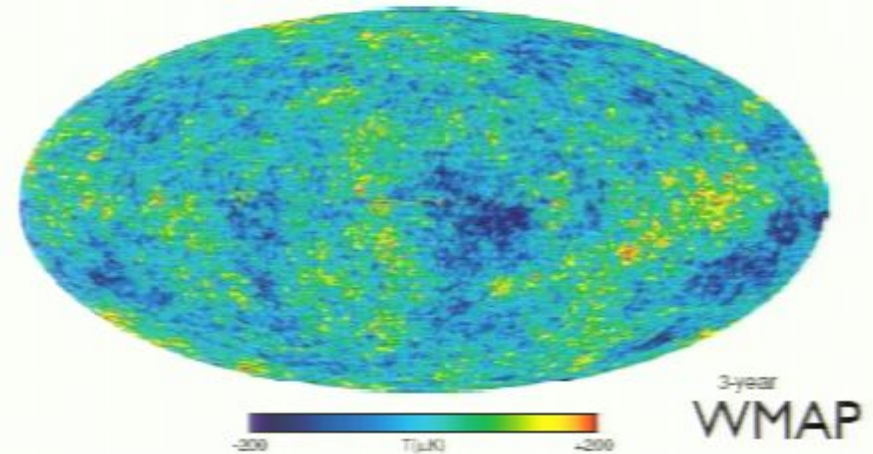
Evidence for Dark Matter in the Universe



Evidence for Dark Matter in the Universe

- Spiral Galaxies
 - * Rotation Curves
- (Super-) Clusters of Galaxies
 - * Galaxy Velocities — X-Rays
 - * Weak Gravitational Lensing
 - * Strong Gravitational Lensing
- Large Scale Structure
 - * Structure Formation
- CMB Anisotropy: WMAP. ...
 - * $\Omega_{\text{tot}} = 100\%$
 - * $\Omega_{\text{M}} = 27\%$
 - * $\Omega_{\text{B}} = 5\%$

$$\Omega_{\text{DM}} \simeq 22\%$$



What is the identity of Dark Matter ?

Supersymmetric Dark Matter Candidates

	LSP	ID	spin	mass	interaction
lightest neutralino ∈ MSSM	$\tilde{\chi}_1^0$	$\tilde{B}, \tilde{W}, \tilde{H}_u^0, \tilde{H}_d^0$ mixture	$\frac{1}{2}$	$\mathcal{O}(100 \text{ GeV})$ $M_1, M_2, \mu, \tan \beta$	g, g' weak
gravitino * gravity	\tilde{G}	superpartner of the graviton	$\frac{3}{2}$	eV – TeV SUSY breaking	$\left(\frac{p}{M_{\text{Pl}}}\right)^n$ extremely weak

$$m_{\tilde{G}} \sim \sum_I \frac{\langle F_I \rangle}{M_{\text{Pl}}} + \sum_A \frac{\langle D_A \rangle}{M_{\text{Pl}}} \sim \frac{M_{\text{SUSY}}^2}{M_{\text{Pl}}}$$

gauge-MSB	gravity-MSB gaugino-MSB	anomaly-MSB mirage-MSB
light gravitino 1 eV-1 GeV	weak-scale gravitino 0.01-1 TeV	heavy gravitino 1-100 TeV

The Supergravity Lagrangian (N=1, d=4)

$$\begin{aligned}
 \frac{1}{e} \mathcal{L} = & -\frac{M_{\text{P}}^2}{2} R + g_{ij}^* D_\mu \phi^i D^\mu \phi^{*j} - \frac{1}{2} g^2 \left[(\text{Re}f)^{-1} \right]^{ab} D_a D_b \\
 & + i g_{ij}^* \bar{\chi}_L^j \gamma^\mu D_\mu \chi_L^i + \varepsilon^{\mu\nu\rho\sigma} \bar{\psi}_{L\mu} \gamma_\nu D_\rho \psi_{L\sigma} \\
 & - \frac{1}{4} \text{Re}f_{ab} F_{\mu\nu}^a F^{b,\mu\nu} + \frac{1}{8} \varepsilon^{\mu\nu\rho\sigma} \text{Im}f_{ab} F_{\mu\nu}^a F_{\rho\sigma}^b \\
 & + \frac{i}{2} \text{Re}f_{ab} \bar{\lambda}^a \gamma^\mu D_\mu \lambda^b - e^{-1} \frac{1}{2} \text{Im}f_{ab} D_\mu \left[e \bar{\lambda}_R^a \gamma^\mu \lambda_R^b \right] \\
 & + \left[-\sqrt{2} g \partial_i D_a \bar{\lambda}^a \chi_L^i + \frac{1}{4} \sqrt{2} g \left[(\text{Re}f)^{-1} \right]^{ab} \partial_i f_{bc} D_a \bar{\lambda}^c \chi_L^i \right. \\
 & + \frac{i}{16} \sqrt{2} \partial_i f_{ab} \bar{\lambda}^a [\gamma^\mu, \gamma^\nu] \chi_L^i F_{\mu\nu}^b - \frac{1}{2M_{\text{P}}} g D_a \bar{\lambda}_R^a \gamma^\mu \psi_\mu \\
 & \left. - \frac{i}{2M_{\text{P}}} \sqrt{2} g_{ij}^* D_\mu \phi^{*j} \bar{\psi}_\nu \gamma^\mu \gamma^\nu \chi_L^i + \text{h.c.} \right] \\
 & - \frac{i}{M_{\text{P}}} \text{Re}f_{ab} \bar{\psi}_\mu \gamma^m, \gamma^n [\gamma^\mu \lambda^a F_{mn}^a] \\
 & - e^{K/2M_{\text{P}}^2} \left[\frac{1}{4M_{\text{P}}^2} W^* \bar{\psi}_{R\mu} [\gamma^\mu, \gamma^\nu] \psi_{L\nu} + \frac{1}{2M_{\text{P}}} \sqrt{2} D_i W \bar{\psi}_\mu \gamma^\mu \chi_L^i \right. \\
 & \left. + \frac{1}{2} D_i D_j W \bar{\chi}_L^i \chi_L^j + \frac{1}{4} g^{ij}^* D_j^* W^* \partial_i f_{ab} \bar{\lambda}_R^a \lambda_L^b + \text{h.c.} \right] \\
 & - e^{K/M_{\text{P}}^2} \left[g^{ij}^* (D_i W) (D_j^* W^*) - 3 \frac{|W|^2}{M_{\text{P}}^2} \right] + \mathcal{O}(M_{\text{P}}^{-2}) .
 \end{aligned}$$

Planck scale

gravitino

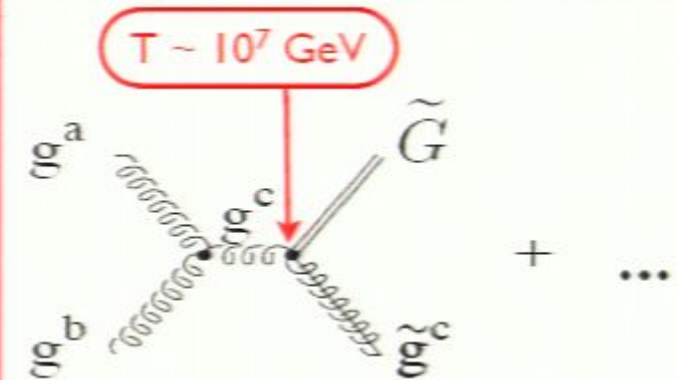
gauge boson

gaugino

Thermal Gravitino Production

LSP	interaction	production	constraints
\tilde{G}	$\left(\frac{P}{M_{\text{Pl}}}\right)^n$ extremely weak	therm. prod. NLSP decays	← cold ← warm
	$M_{\text{Pl}} = 2.44 \times 10^{18} \text{ GeV}$...	

Very Hot Early Universe



gauge-invariant treatment
(hard thermal loop resummation)
[Ellis, Nanopoulos, Olive, Rey, '96]

SUSY QCD
[Bolz, Brandenburg, Buchmüller, '01]
+ electroweak contributions
[Pradler, FDS, '06 & '07]

Reheating after Inflation - Definition of T_R

$$\Gamma_\phi = \xi H_{\text{rad}}(T_R)$$

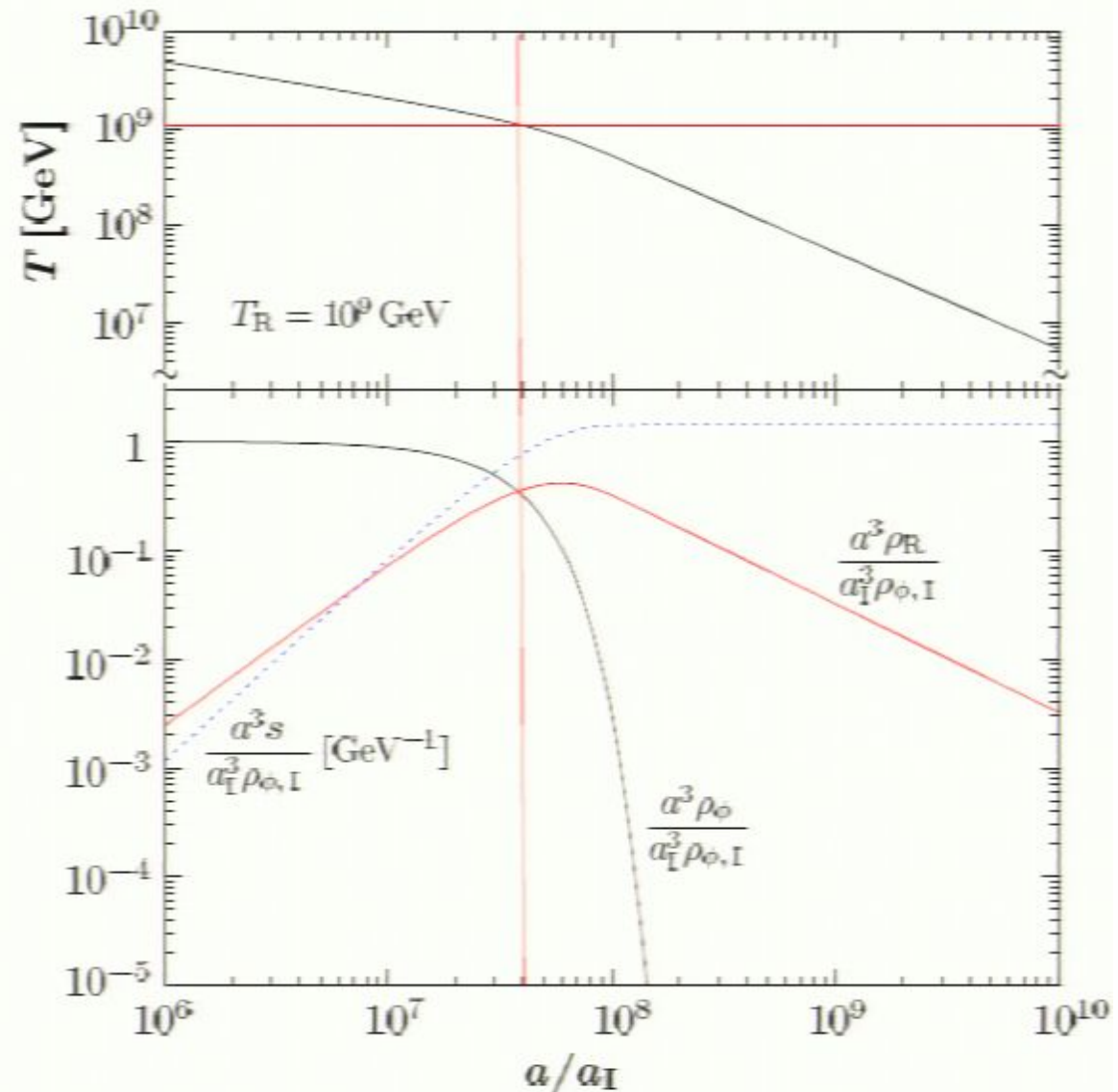
$$T_R^\xi \equiv \left[\frac{90}{g_*(T_R)\pi^2} \right]^{1/4} \sqrt{\frac{\Gamma_\phi M_{\text{P}}}{\xi}}$$

$$\frac{d\rho_{\text{rad}}}{dt} + 4H\rho_{\text{rad}} = \Gamma_\phi \rho_\phi,$$

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = -\Gamma_\phi \rho_\phi,$$

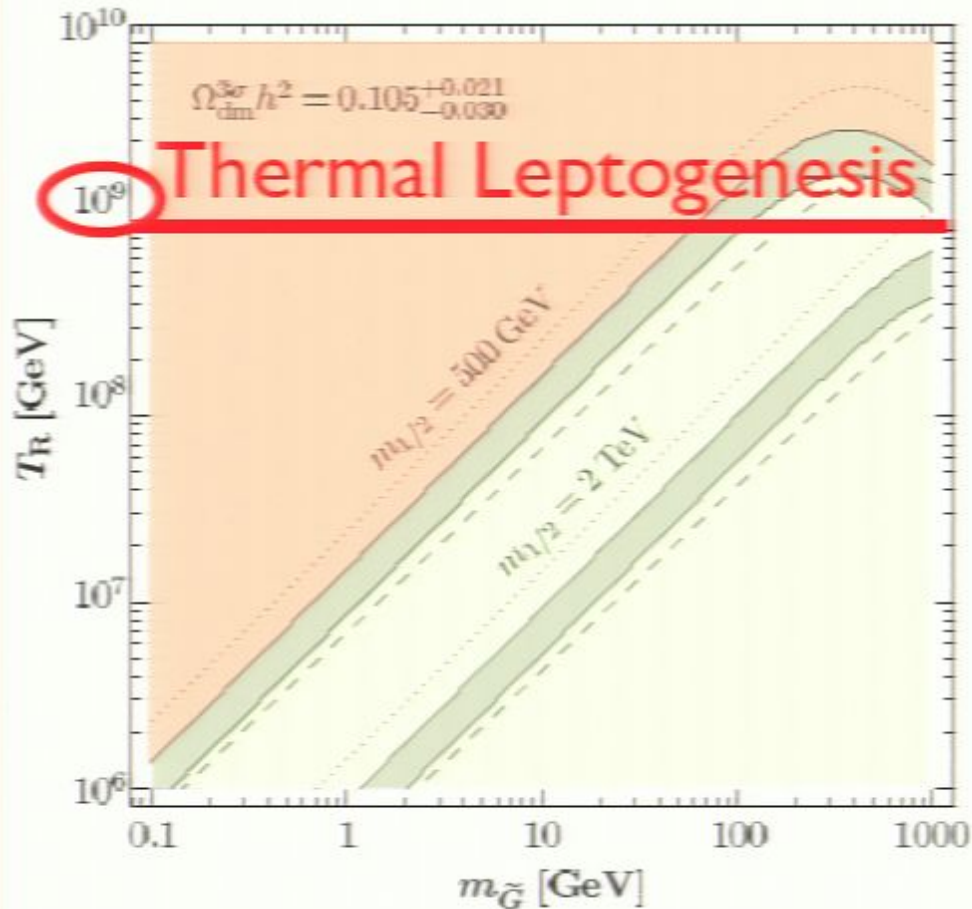
$$\frac{dn_{\tilde{G}}}{dt} + 3Hn_{\tilde{G}} = C_{\tilde{G}},$$

$$C_{\tilde{G}} = \sum_{i=1}^3 \frac{3\zeta(3)T^6}{16\pi^3 M_{\text{P}}^2} \left(1 + \frac{M_i^2}{3m_{\tilde{G}}^2} \right) c_i g_i^2 \ln\left(\frac{k_i}{g_i}\right),$$



[Pradler, FDS, '07]

Thermal \tilde{G} Production



[Pradler, FDS, '07]

see also [Moroi, Murayama, Yamaguchi, '93,
Asaka, Hamaguchi, Suzuki, '00, Roszkowski et al., '05,
Pirsa: 08060183
Cerdeno et al., '06, FDS '06, Rychkov, Strumia, '07]

Gravitino Dark Matter from Thermal Production

□ Boltzmann Equation

$$\frac{dn_{\tilde{G}}}{dt} + 3Hn_{\tilde{G}} = C_{\tilde{G}}$$

□ Collision Term

$$C_{\tilde{G}} = \sum_{i=1}^3 \frac{3\zeta(3)T^6}{16\pi^3 M_{\text{Pl}}^2} \left(1 + \frac{M_i^2}{3m_{\tilde{G}}^2}\right) c_i g_i^2 \ln\left(\frac{k_i}{g_i}\right)$$

□ Gravitino Density

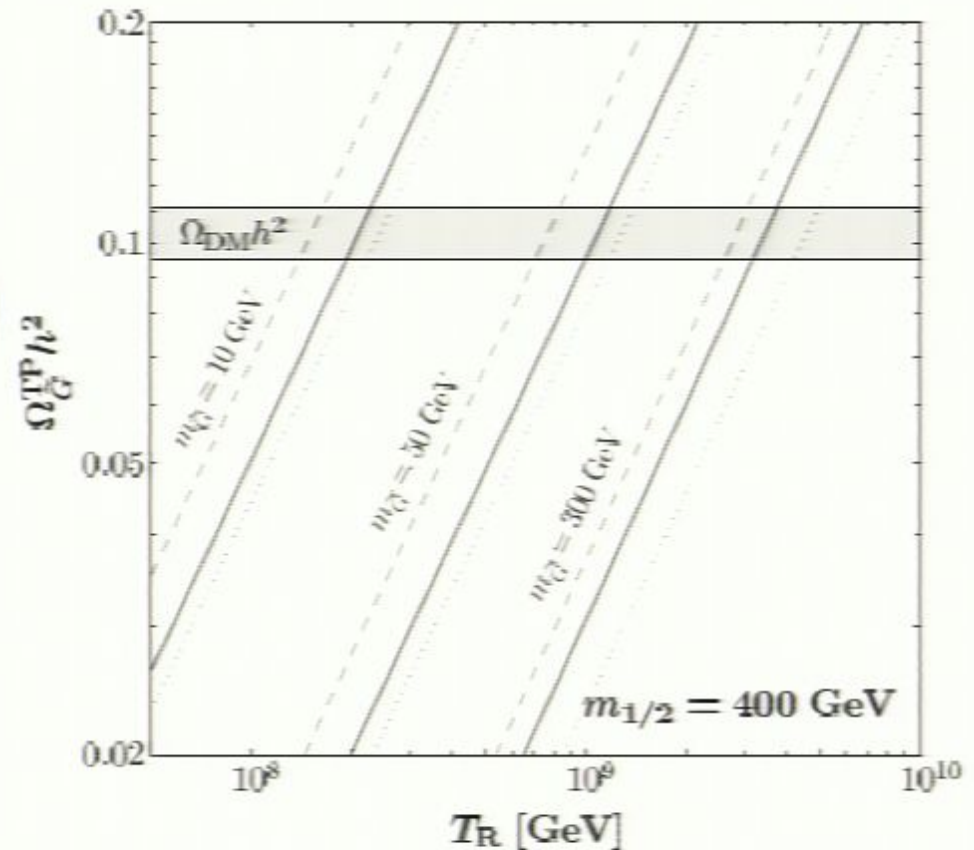
$$\Omega_{\tilde{G}}^{\text{TP}} h^2 = \sum_{i=1}^3 \omega_i g_i^2 \left(1 + \frac{M_i^2}{3m_{\tilde{G}}^2}\right) \ln\left(\frac{k_i}{g_i}\right) \times \left(\frac{m_{\tilde{G}}}{100 \text{ GeV}}\right) \left(\frac{T_{\text{R}}}{10^{10} \text{ GeV}}\right)$$

□ $U(1)_Y \times SU(2)_L \times SU(3)_c$

$$c_i = (11, 27, 72)$$

$$k_i = (1.266, 1.312, 1.271)$$

$$\omega_i = (0.018, 0.044, 0.117)$$

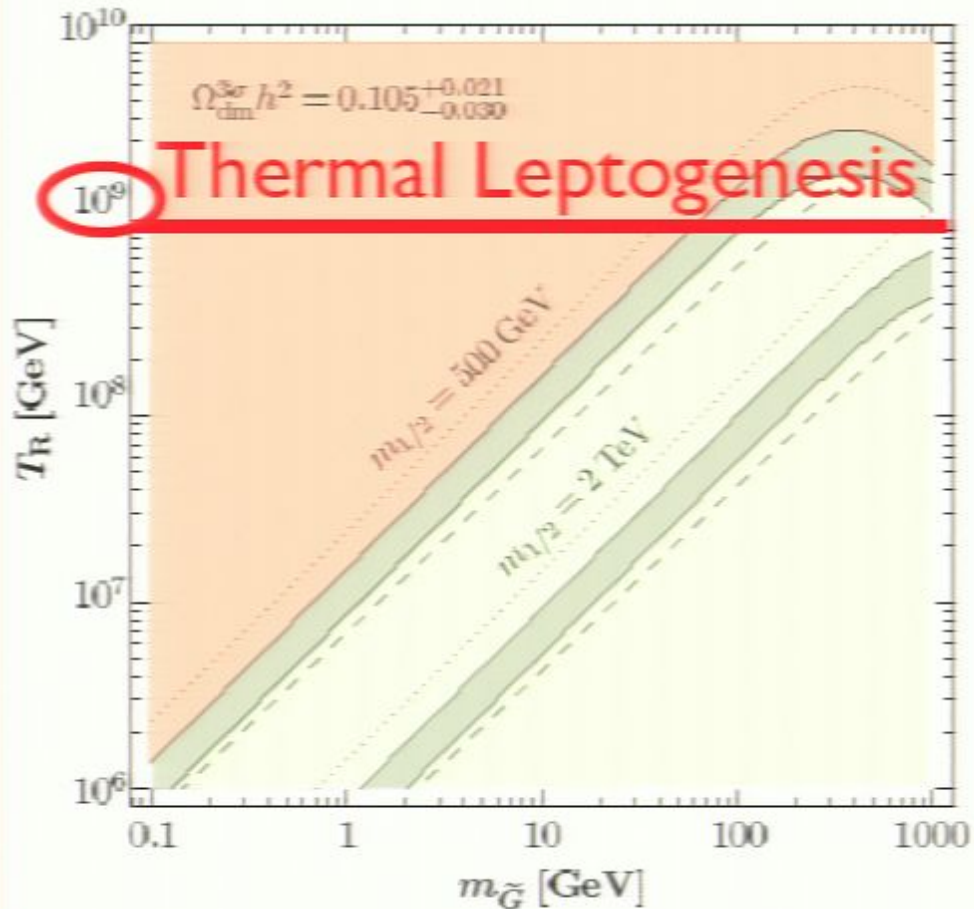


solid: $M_{1,2,3} = m_{1/2}$

dashed: $0.5 M_{1,2} = M_3 = m_{1/2}$

dotted: $M_3 = m_{1/2}$

Thermal \tilde{G} Production

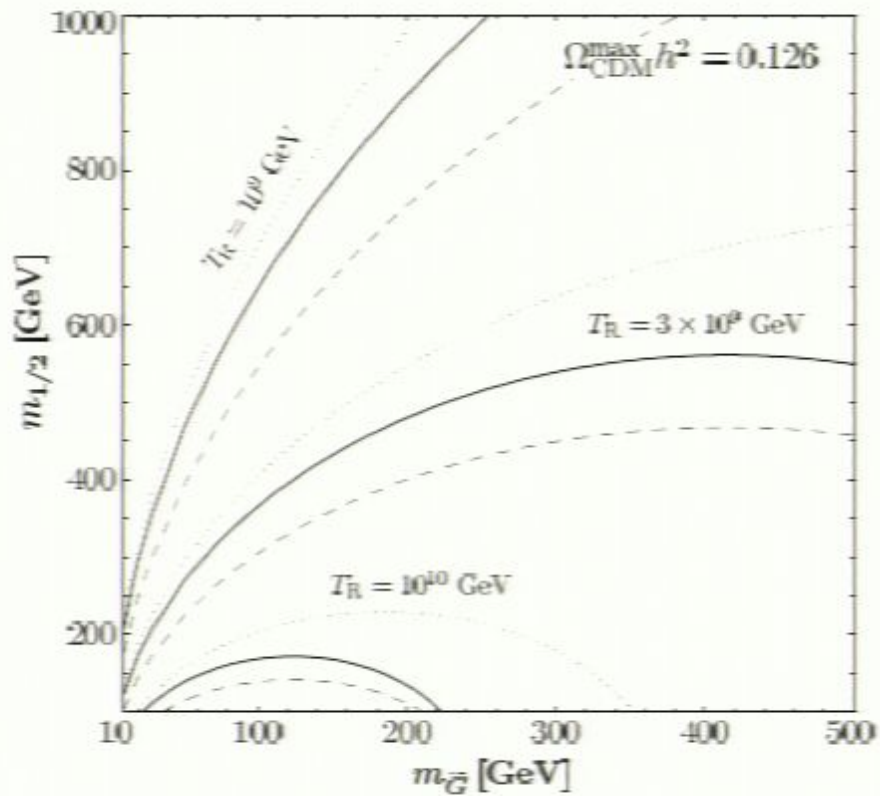


[Pradler, FDS, '07]

see also [Moroi, Murayama, Yamaguchi, '93,
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Pirsa: 08060183
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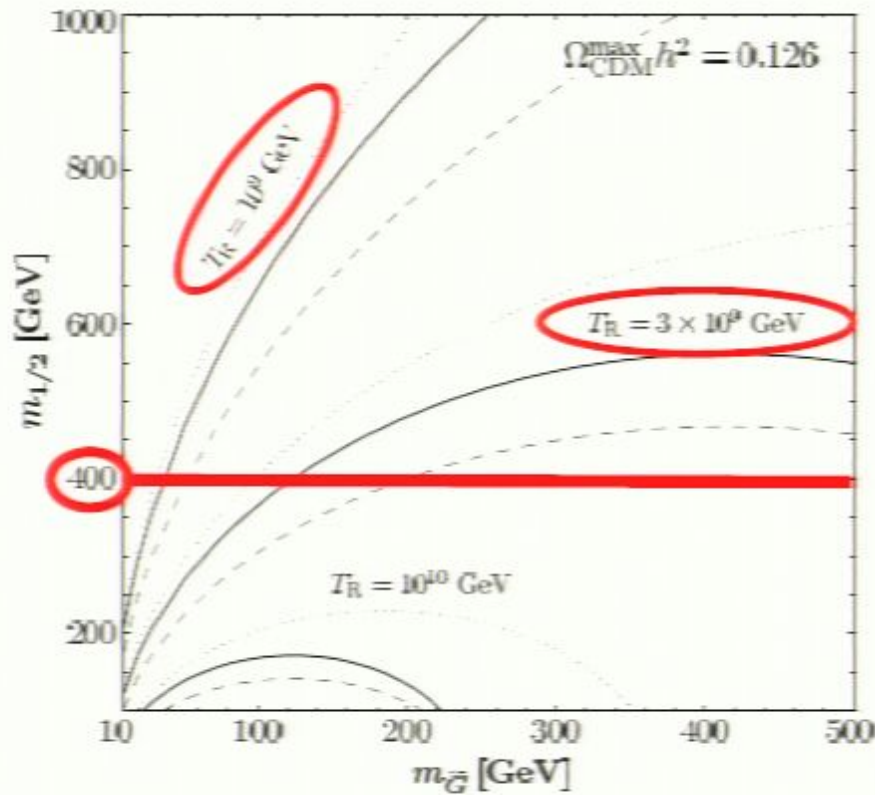
[Pradler, FDS, '06]

Probing T_R at Colliders in Gravitino DM Scenarios



[Pradler, FDS, '06]

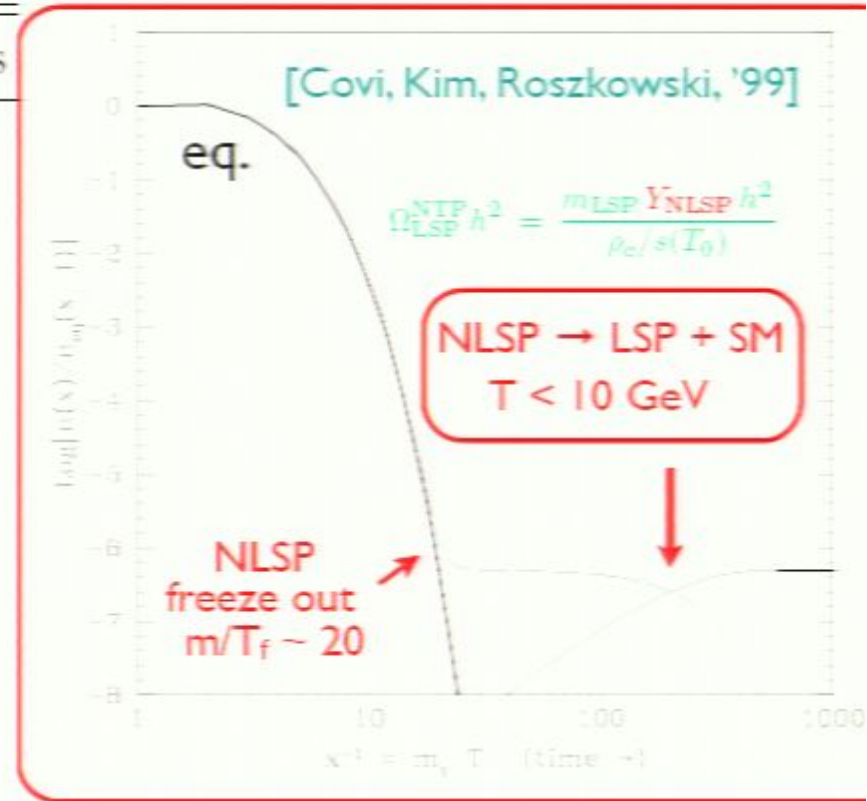
Probing T_R at Colliders in Gravitino DM Scenarios



Thermal
Leptogenesis

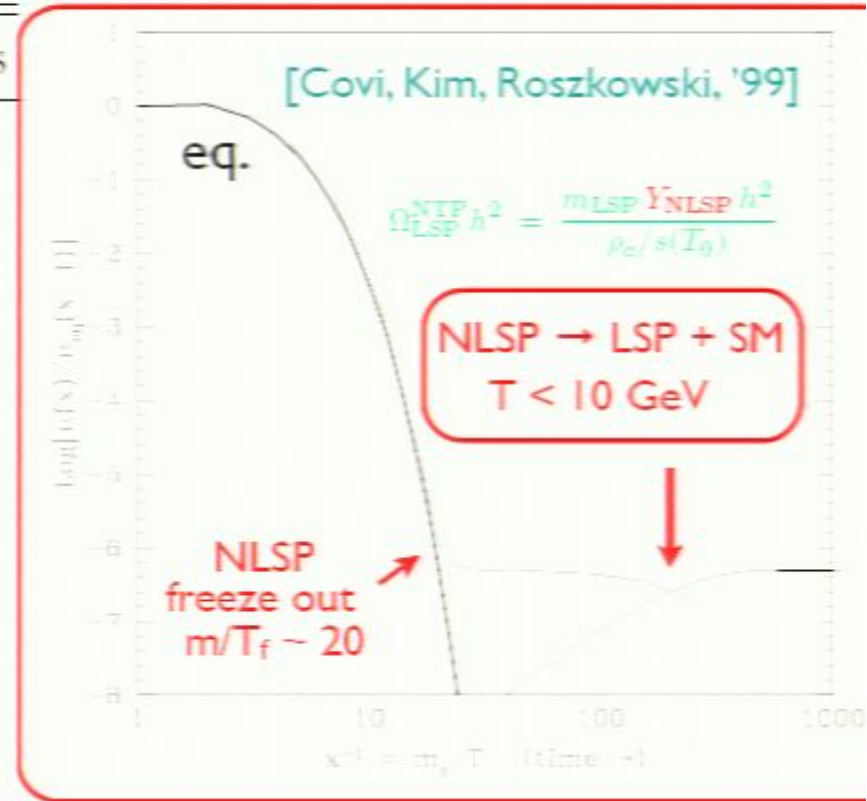
Non-Thermal Gravitino Production

LSP	interaction	production	constraints
\tilde{G}	$\left(\frac{p}{M_{\text{Pl}}}\right)^n$ extremely weak	therm. prod. NLSP decays	← cold ← warm
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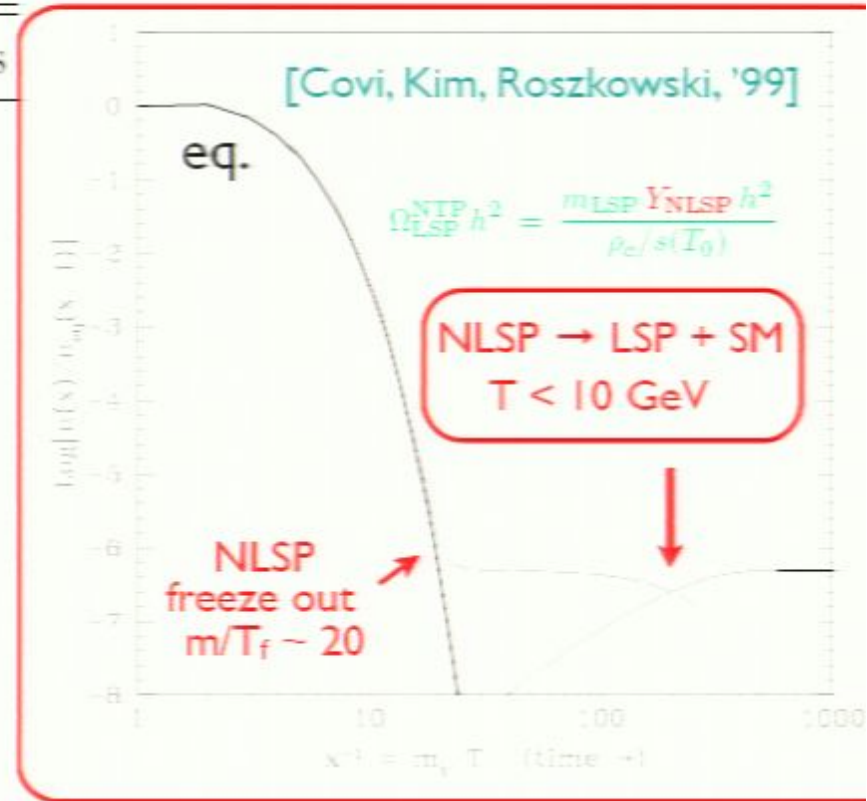


NLSP Candidates

- lightest neutralino
- lighter stau
- lighter stop
- lightest sneutrino

Non-Thermal Gravitino Production

LSP	interaction	production	constraints
\tilde{G}	$\left(\frac{p}{M_{\text{Pl}}}\right)^n$ extremely weak $M_{\text{Pl}} = 2.44 \times 10^{18} \text{ GeV}$	therm. prod. NLSP decays ...	← cold ← warm



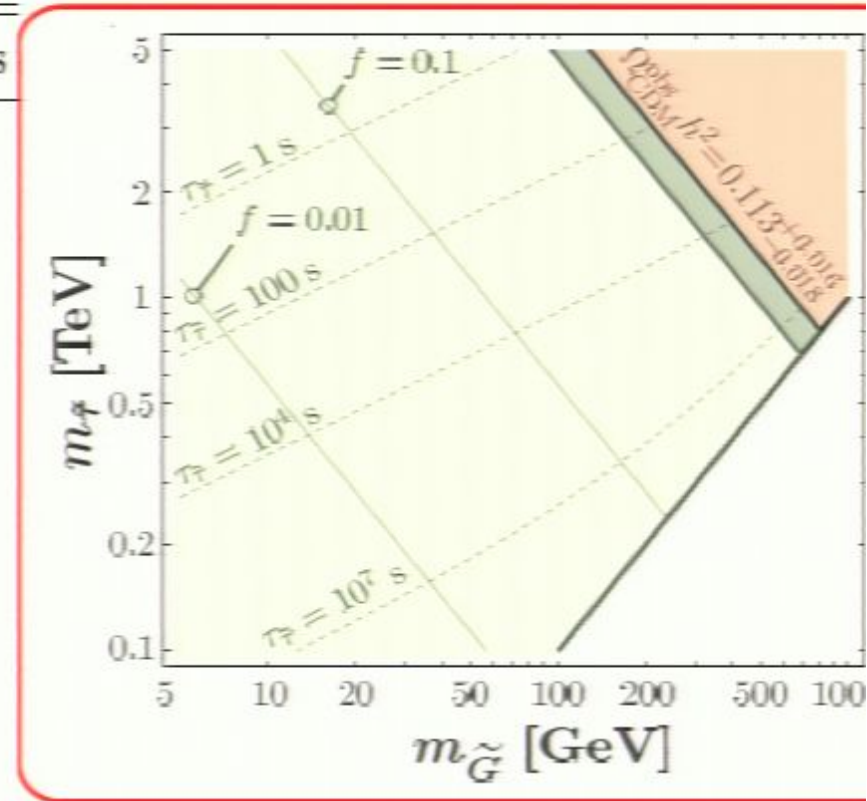
NLSP Candidates

electrically charged \rightarrow

- lightest neutralino
- **lighter stau**
- lighter stop
- lightest sneutrino

Non-Thermal Gravitino Production

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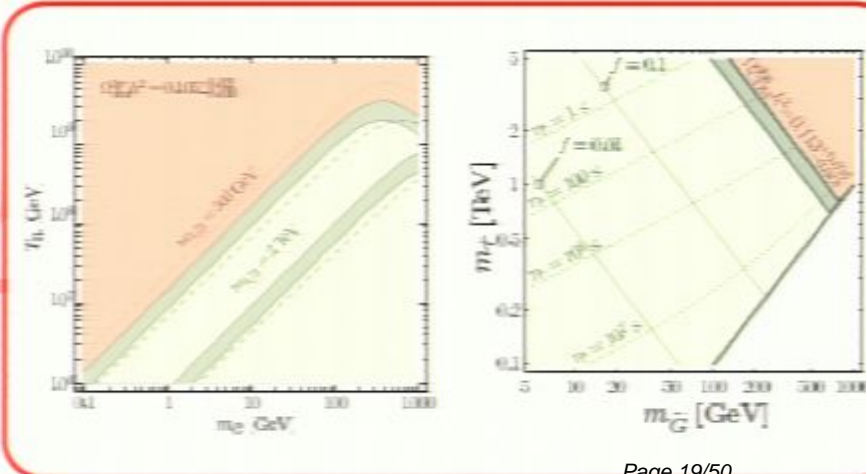
LSP Dark Matter: Production, Constraints, Experiments

LSP	interaction	production	constraints	experiments
$\tilde{\chi}_1^0$	g, g' weak	WIMP freeze out	← cold	indirect detection (EGRET, GLAST, ...) direct detection (CRESST, EDELWEISS, ...) prod.@colliders (Tevatron, LHC, ILC, ...)
	$M_W \sim 100 \text{ GeV}$			

\tilde{G} $\left(\frac{p}{M_{\text{Pl}}}\right)^n$
 extremely weak
 $M_{\text{Pl}} = 2.44 \times 10^{18} \text{ GeV}$

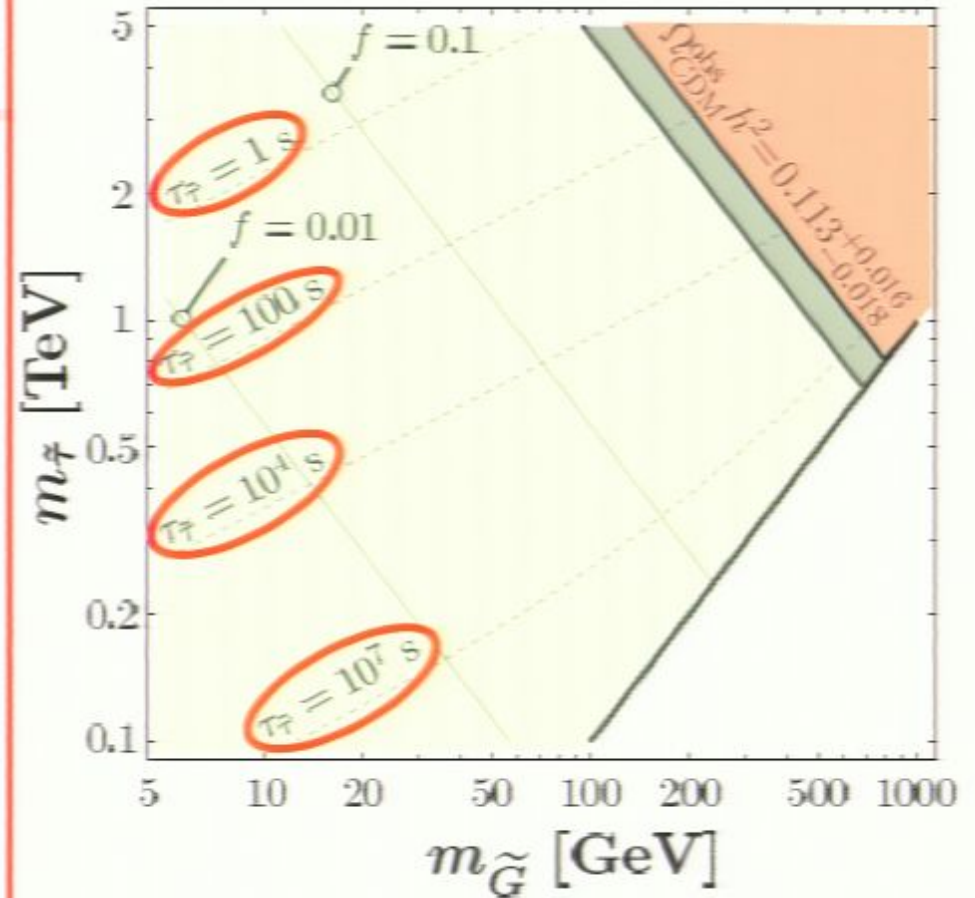
therm. prod. ← cold
 NLSP decays ← warm
 ...

$\Omega_{\tilde{G}} = \Omega_{\text{DM}}$
 is possible!!!



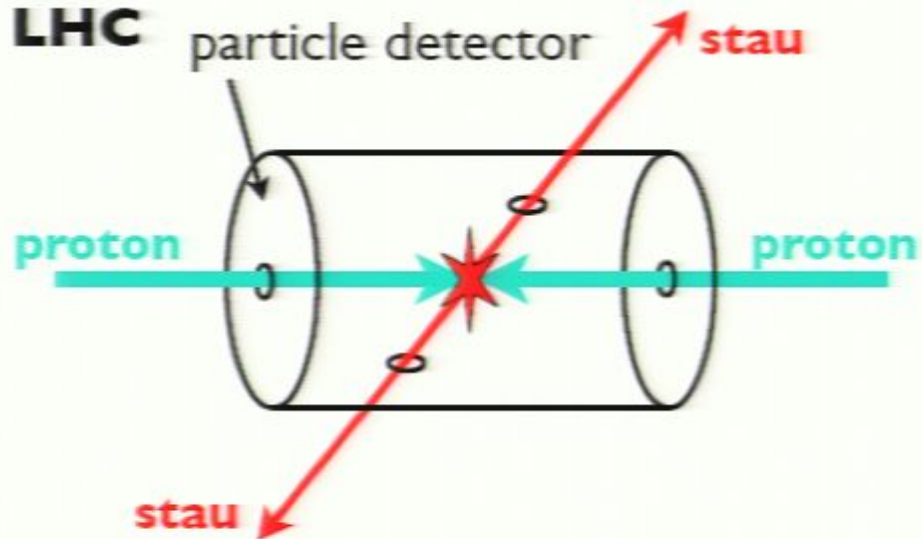
long-lived NLSP

$$\tilde{\tau} \text{ NLSP} \rightarrow \tilde{G} + \tau$$



Gravitino DM @ LHC ← Stau NLSP

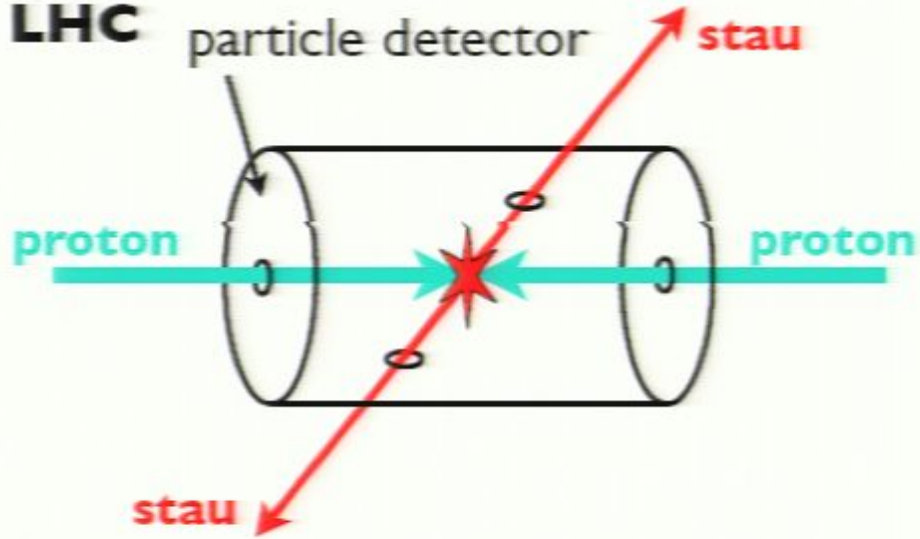
2009
LHC



The signal:
jets + leptons
+ 2 “stable”
charged particles

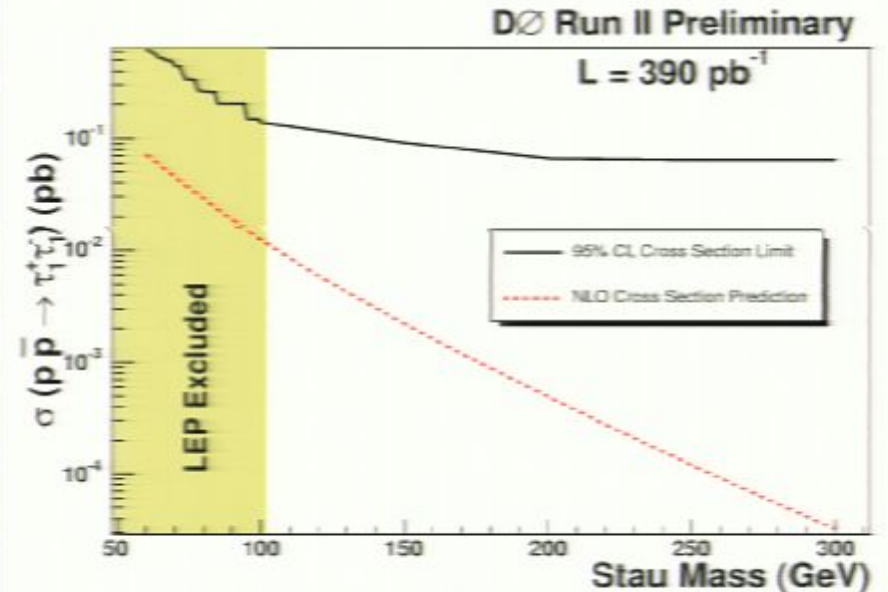
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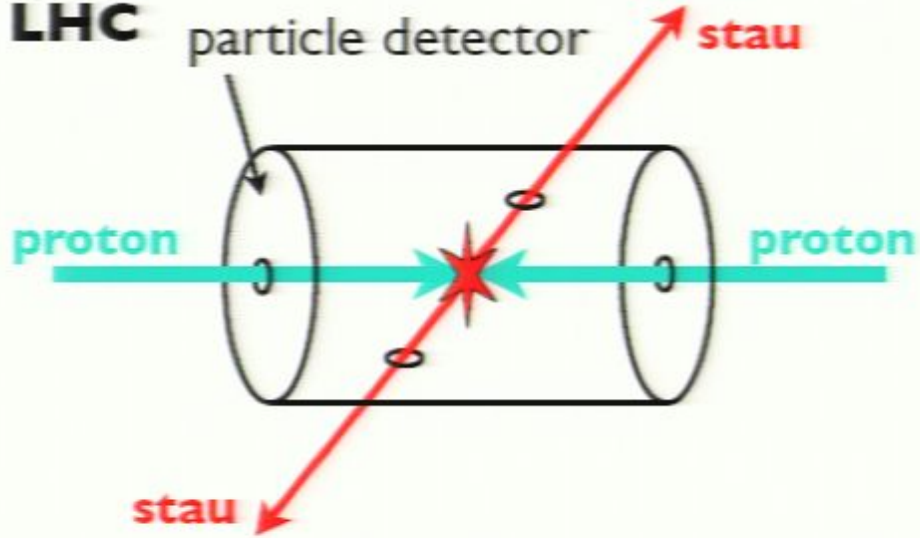
Tevatron



[from Gershtein's Talk, SUSY2007]

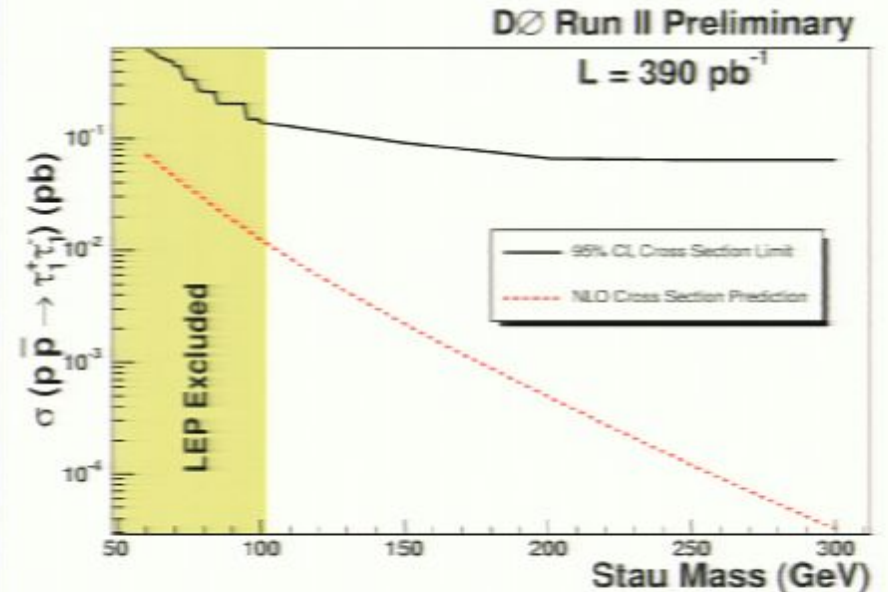
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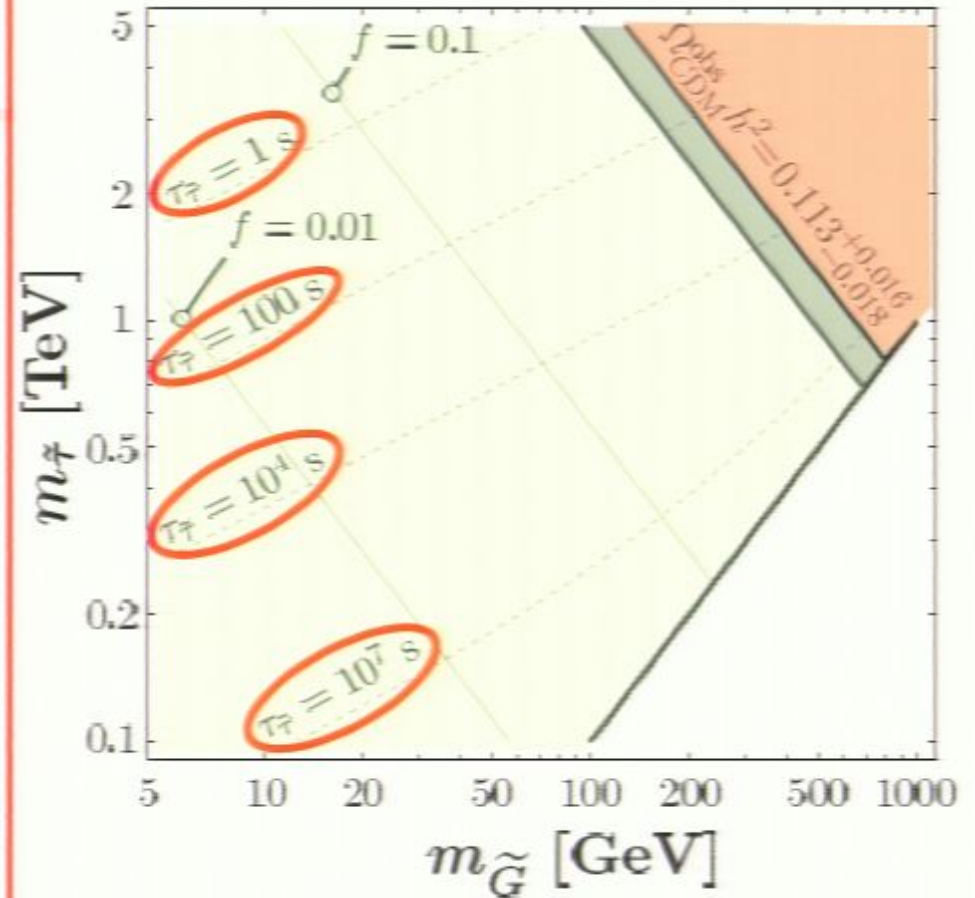


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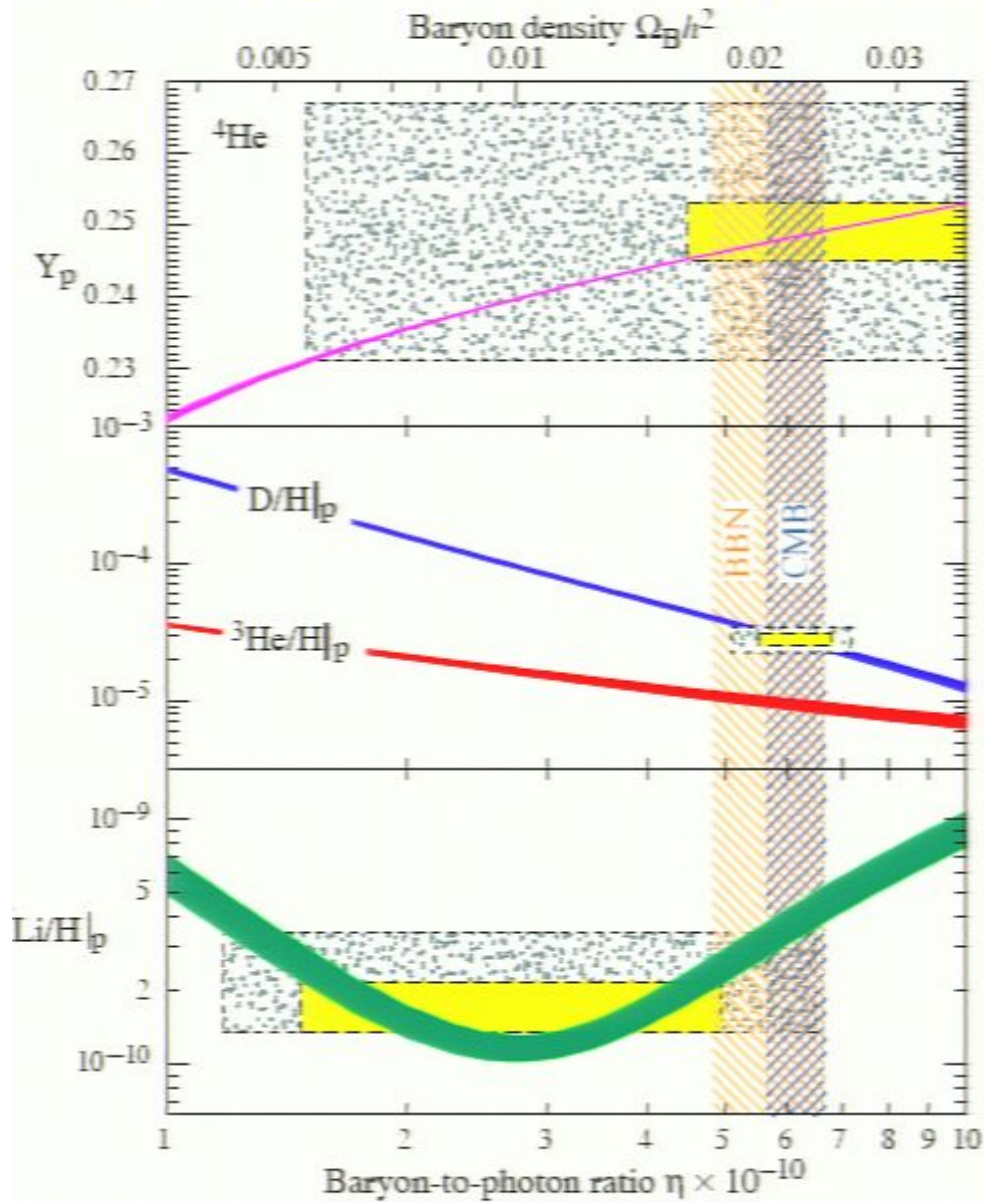
[Drees, Tata, '88, Nisati, Petrarca, Salvini, '97, Ambrosanio, Kribs, Martin, '97, Feng, Moroi, '98, Martin, Wells, '99, Ambrosanio et al., '01, ...]

long-lived NLSP

$$\tilde{\tau} \text{ NLSP} \rightarrow \tilde{G} + \tau$$

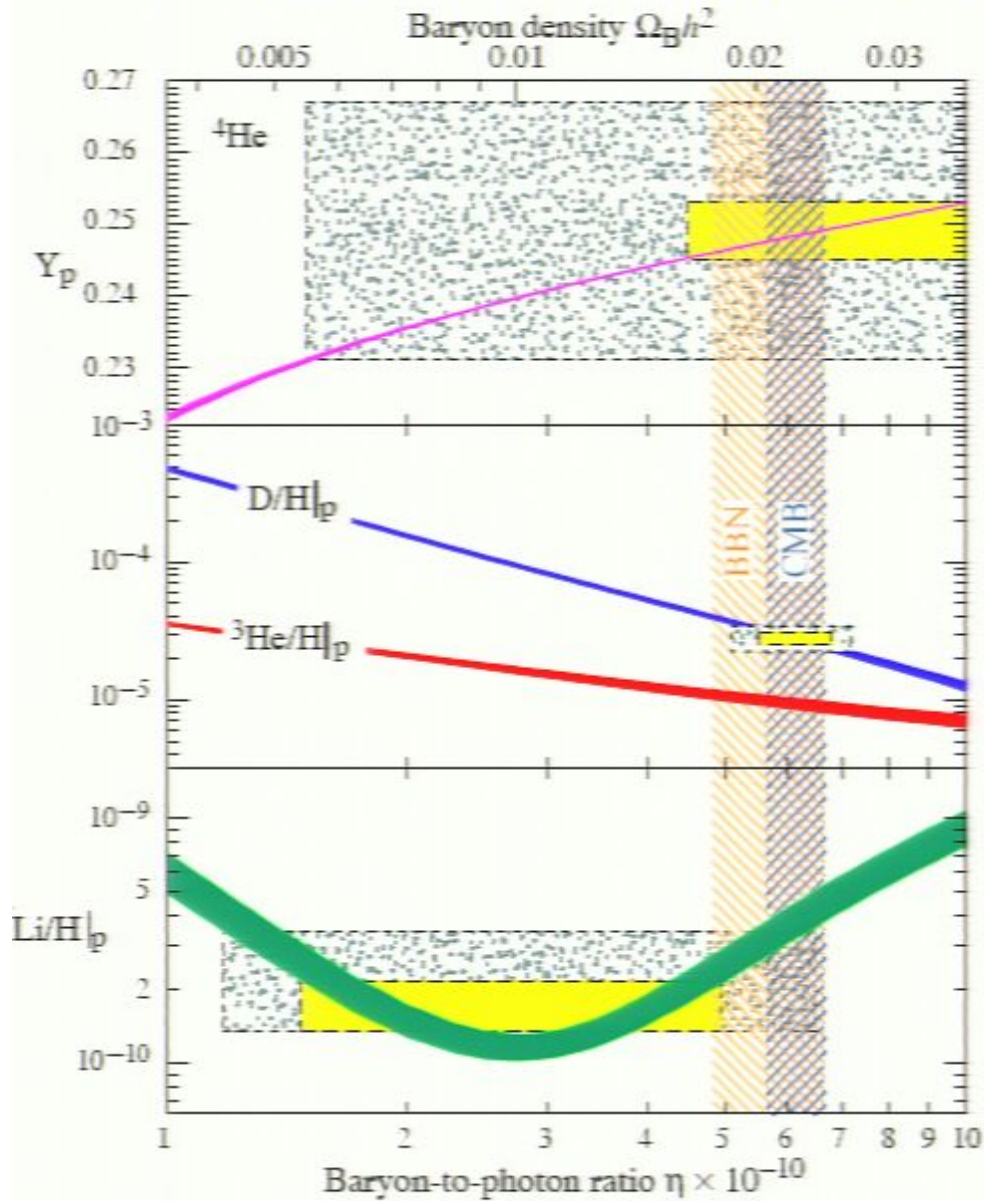


Big-Bang Nucleosynthesis



[Particle Data Book 2006]

Big-Bang Nucleosynthesis

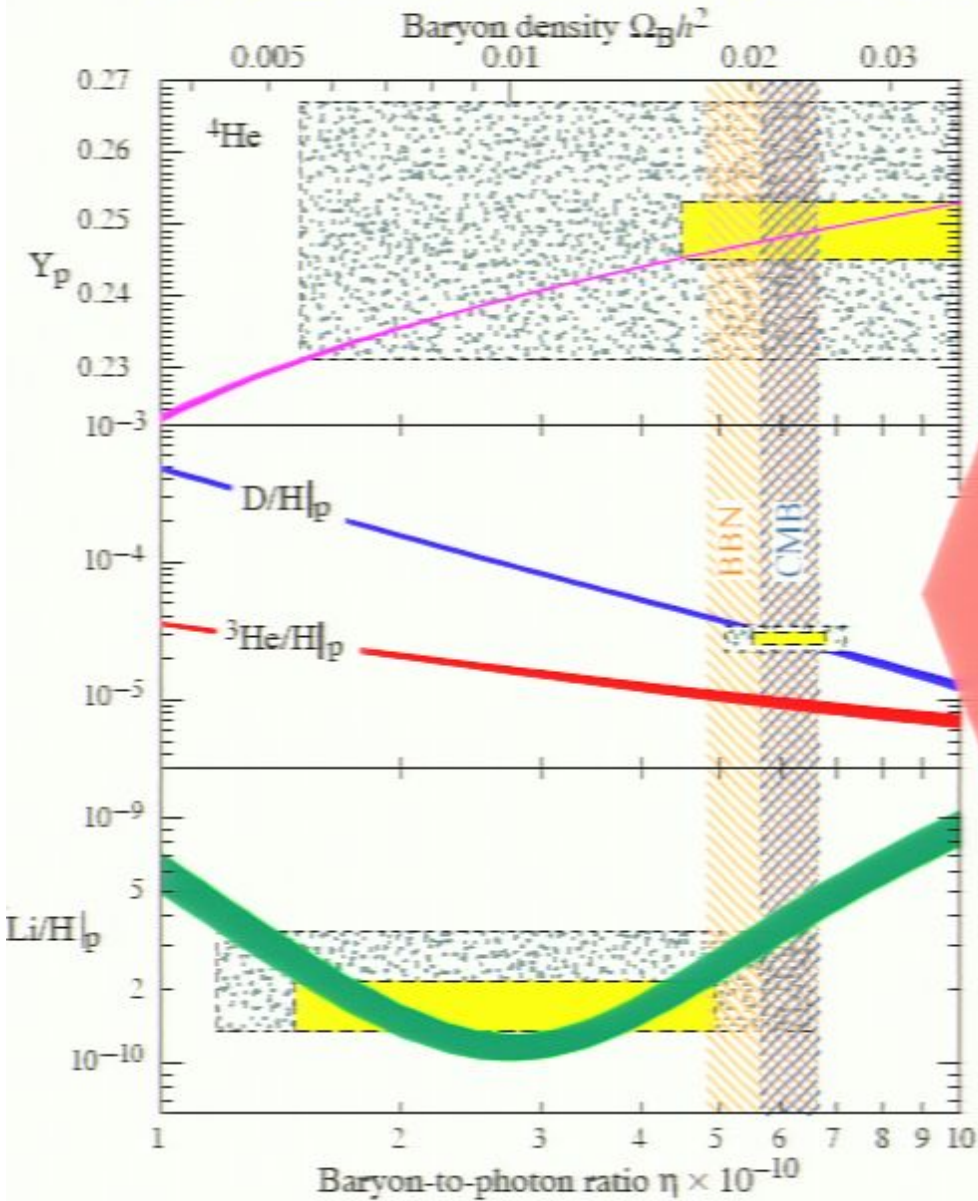


[Particle Data Book 2006]

Big Bang Nucleosynthesis and
Particle Physics

Workshop @ Perimeter Institute

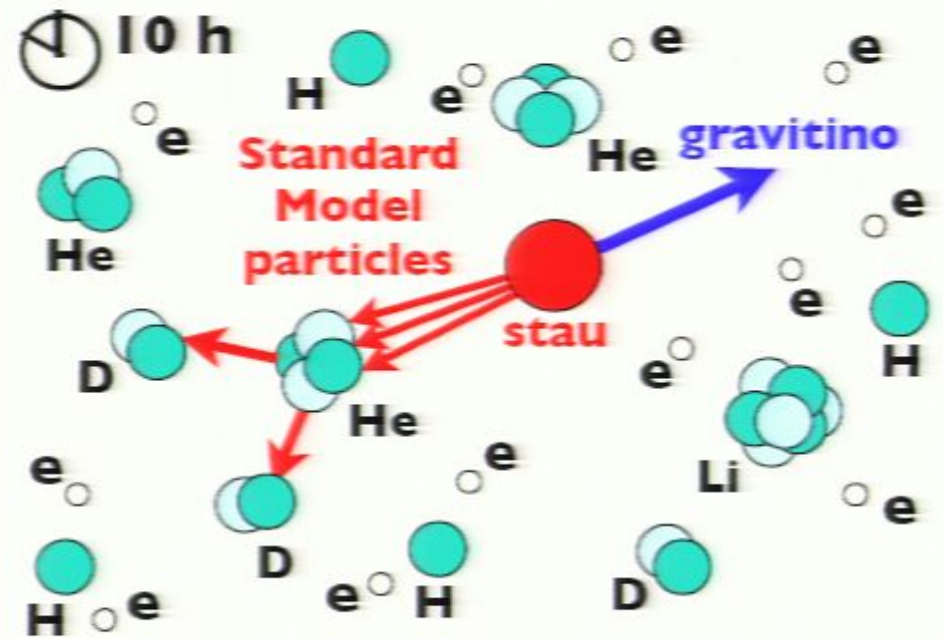
Big-Bang Nucleosynthesis



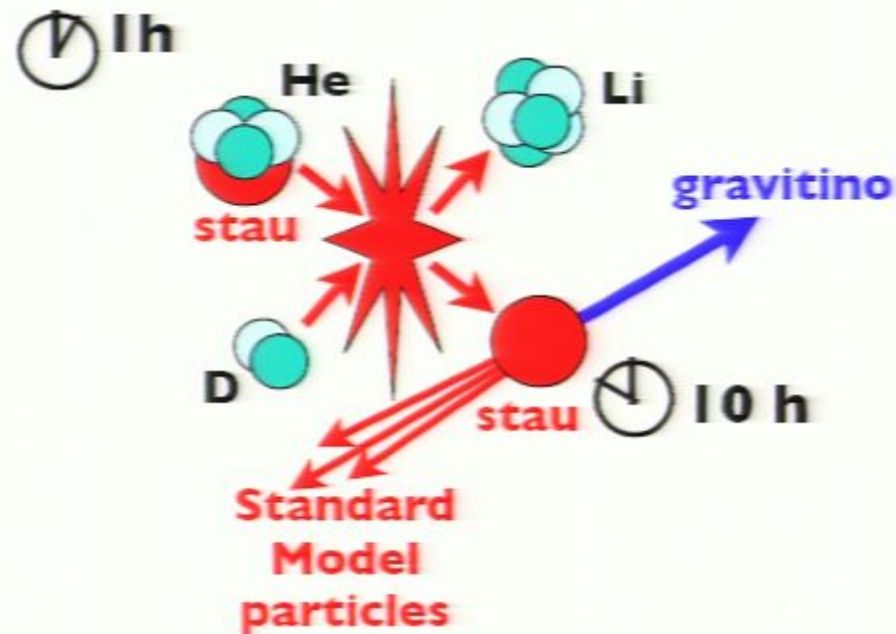
[Particle Data Book 2006]

Big Bang Nucleosynthesis and Particle Physics

Workshop @ Perimeter Institute



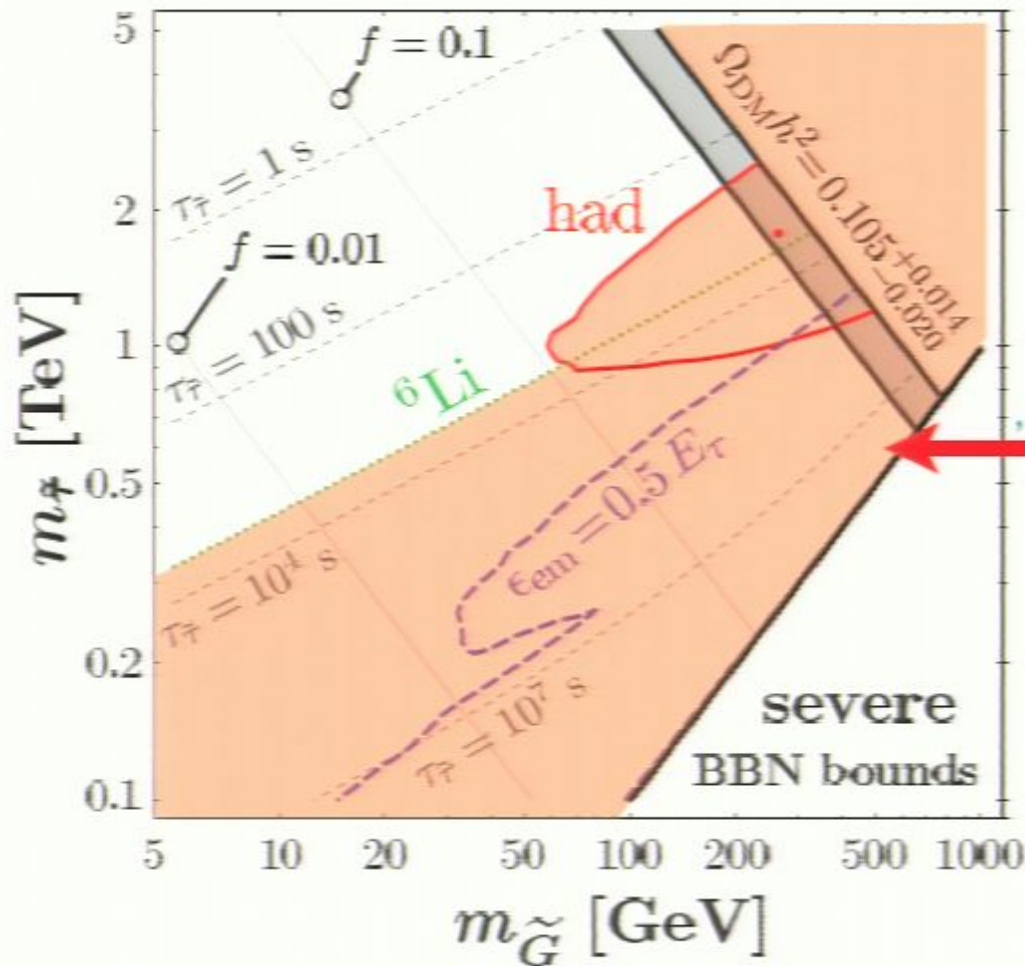
Catalyzed BBN [Pospelov, '06]



Recent Result: [Hamaguchi et al., '07]

[Cyburt et al., '06; FDS, '06; Pradler, FDS, '07;
Kawasaki, Kohri, Moroi, '07; Takayama, '07; Jedamzik, '07;
Pradler, FDS, arXiv:0710.2213 & arXiv:0710.4548; ...]

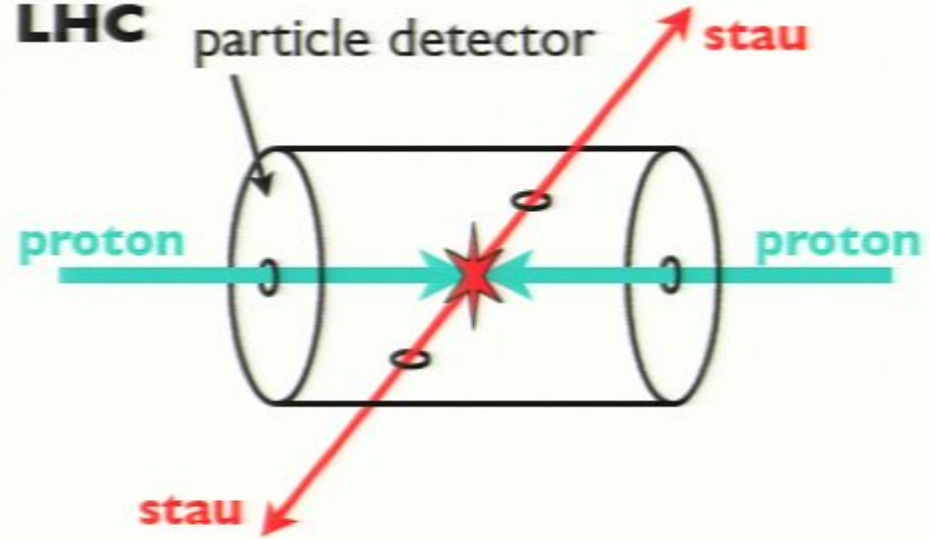
Cosmological Constraints — Ω_{DM} & BBN



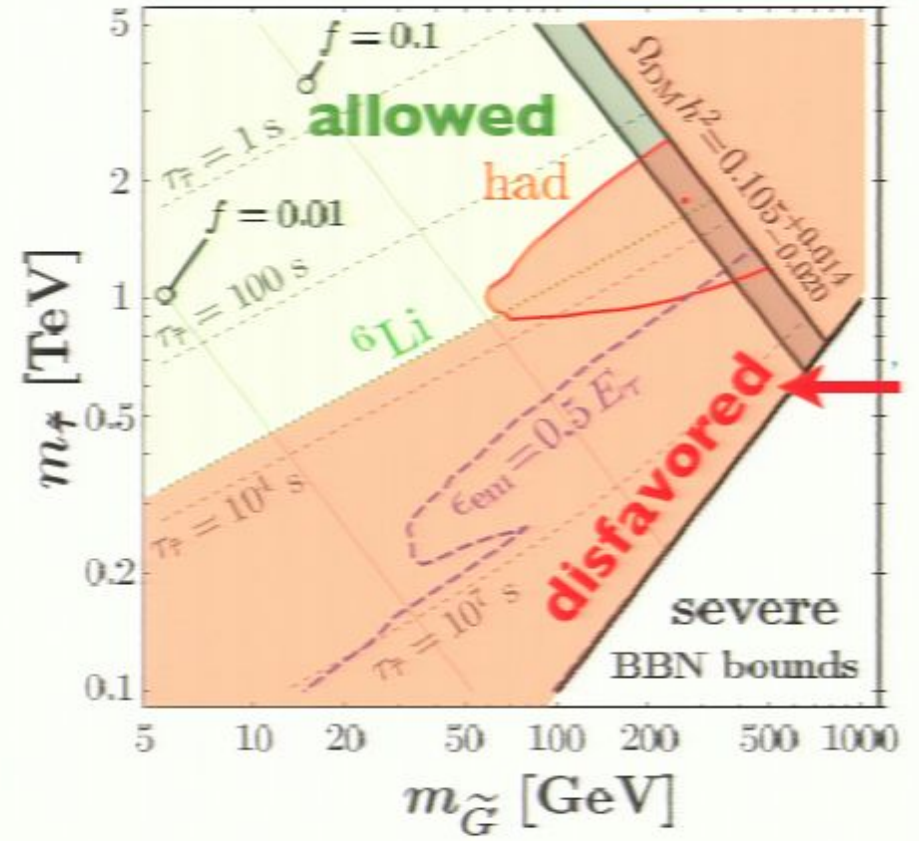
**disfavored
by
cosmological
constraints**

Gravitino DM @ LHC ← Stau NLSP

2009
LHC



The signal:
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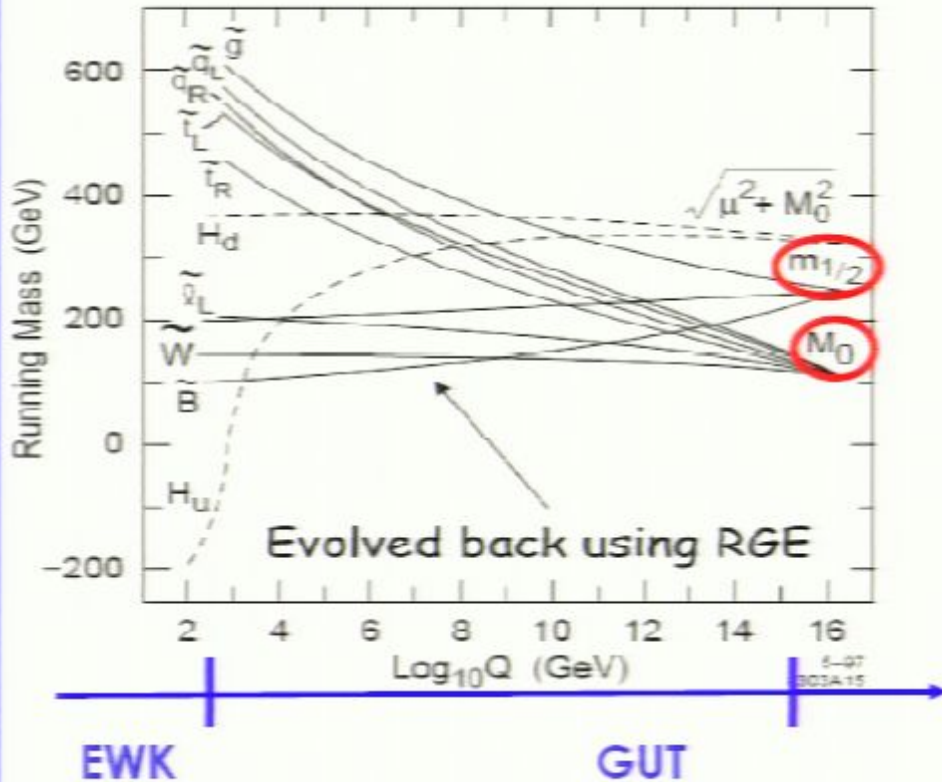


Cosmological Constraints

[FDS, hep-ph/0611027 & arXiv:0711.1240,
 Kawasaki, Kohri, Moroi, hep-ph/0703122, ...]

CMSSM with Gravitino DM

mSUGRA / CMSSM

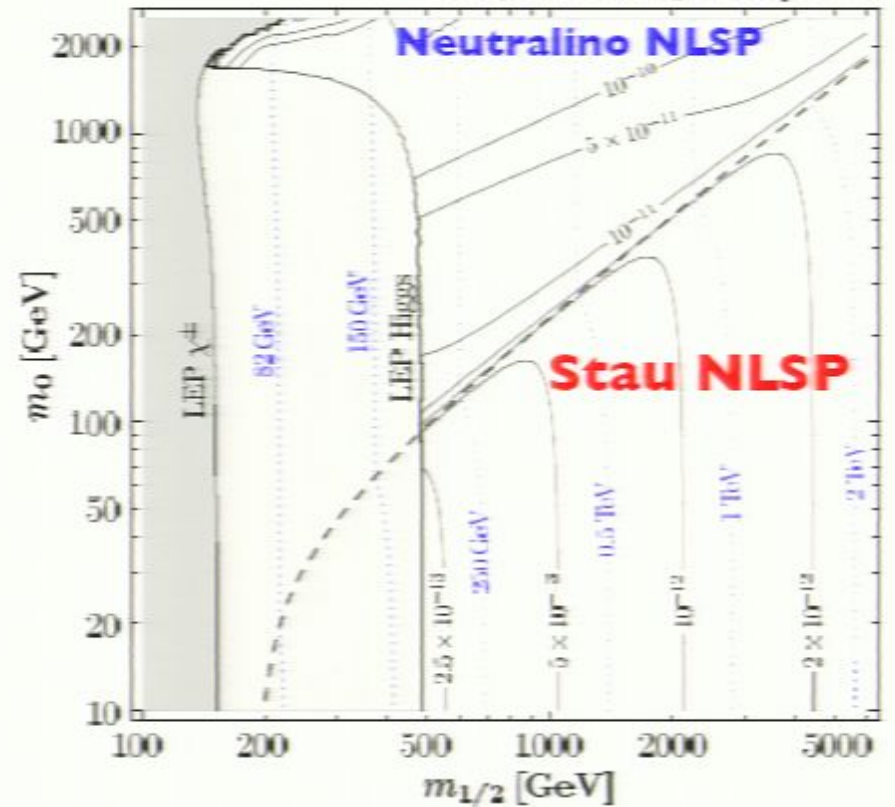


1. Unified gaugino mass $m_{1/2}$
2. Unified scalar mass m_0
3. Ratio of H_1, H_2 vevs $\tan\beta$
4. Trilinear coupling A_0
5. Higgs mass term $\text{sgn}(\mu)$

CMSSM Scan $m_{\text{LOSP}} & Y_{\text{LOSP}}$

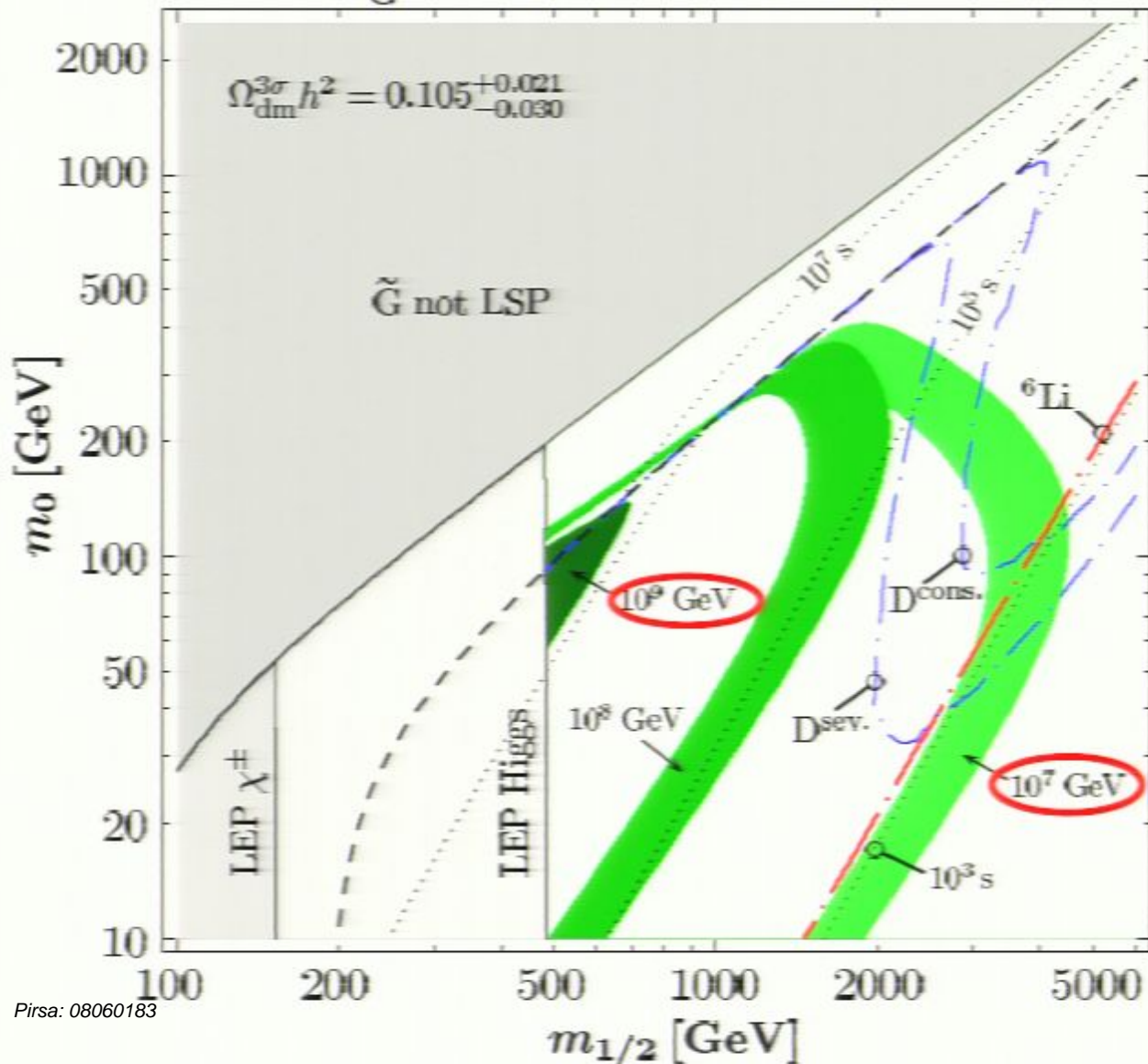
[Pradler, FDS, arXiv:0710.4548]

$\tan\beta = 10, A_0 = 0, \mu > 0$

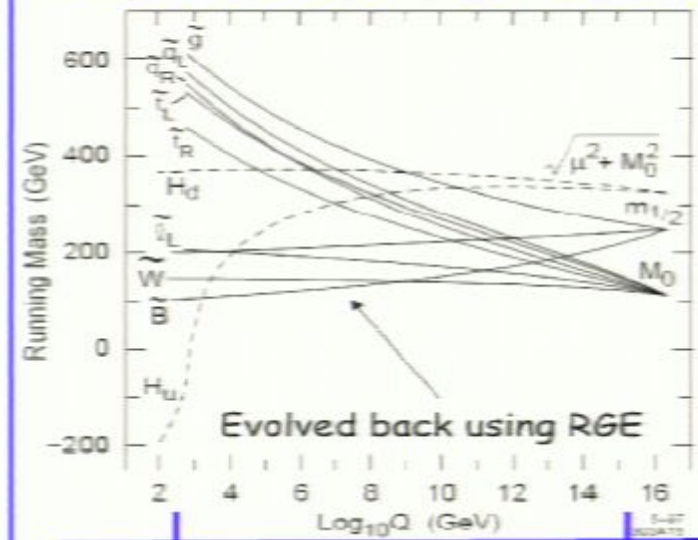


TP + NTP of Gravitino DM within the CMSSM

$$m_{\tilde{G}} = m_0, \tan\beta = 10, A_0 = 0, \mu > 0$$



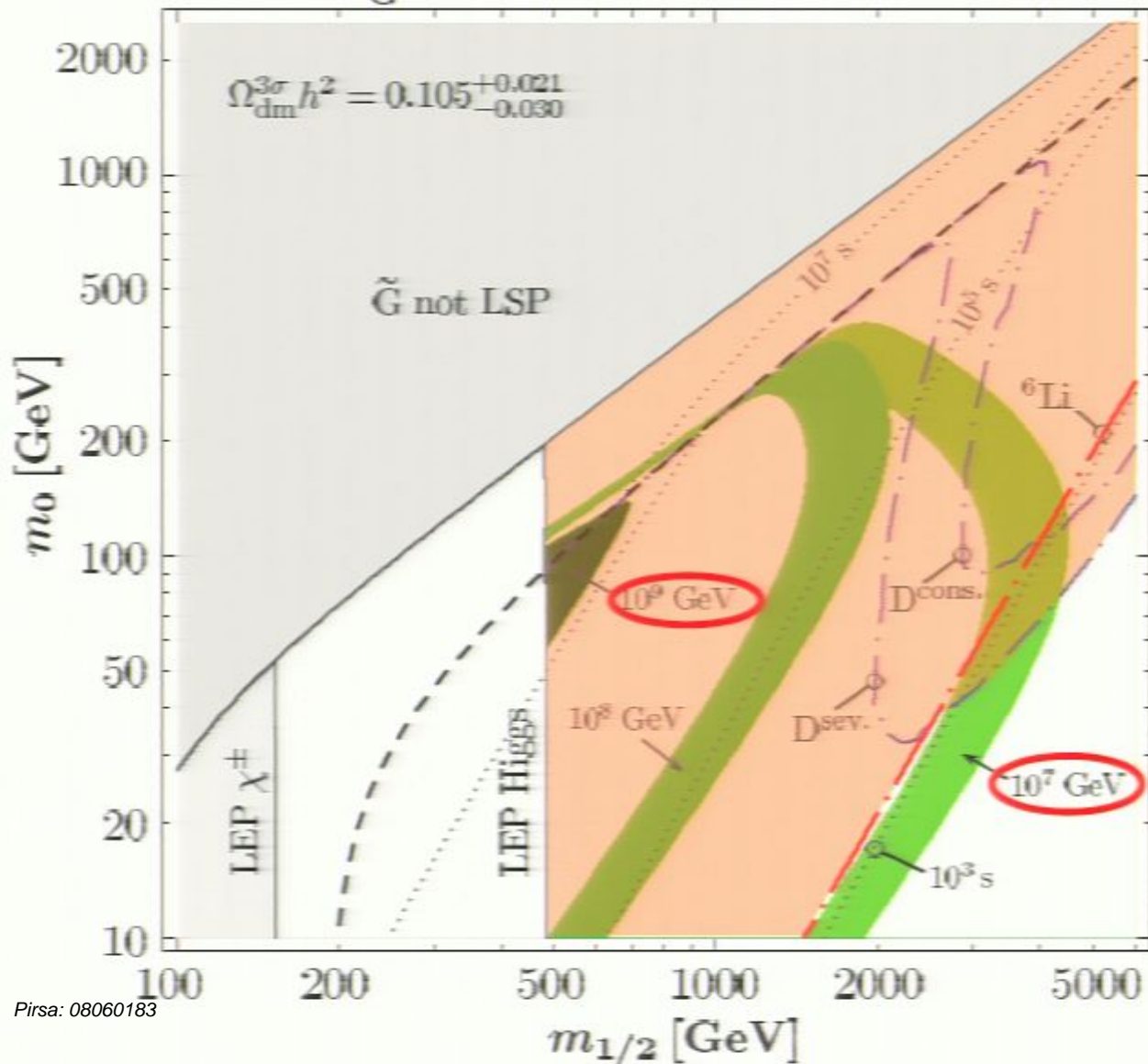
mSUGRA / CMSSM



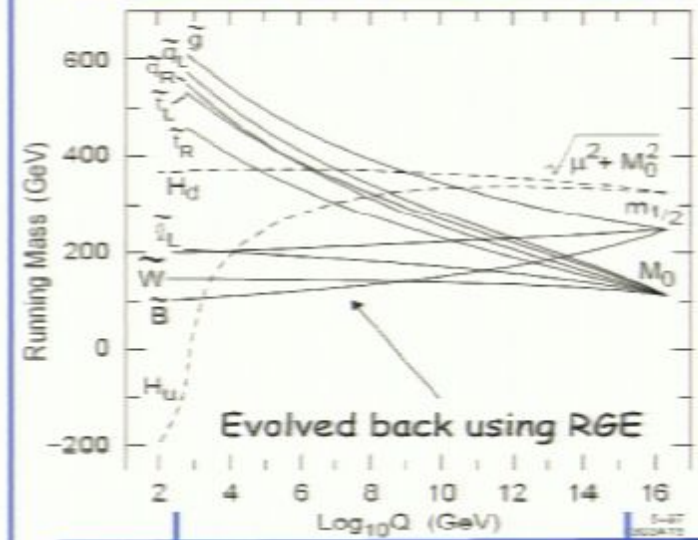
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Upper Bounds on T_R in the CMSSM with \tilde{G} Dark Matter

$$m_{\tilde{G}} = m_0, \tan\beta = 10, A_0 = 0, \mu > 0$$



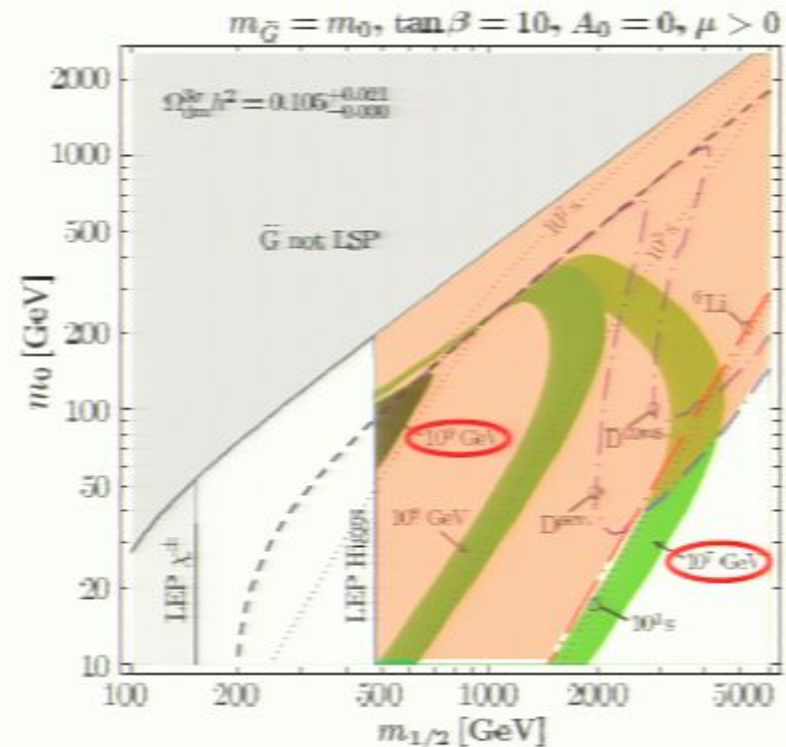
mSUGRA / CMSSM



- EWK | GUT
1. Unified gaugino mass $m_{1/2}$
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Upper Bounds on T_R in the CMSSM with \tilde{G} Dark Matter

Implications for inflation and the origin of the baryon asymmetry



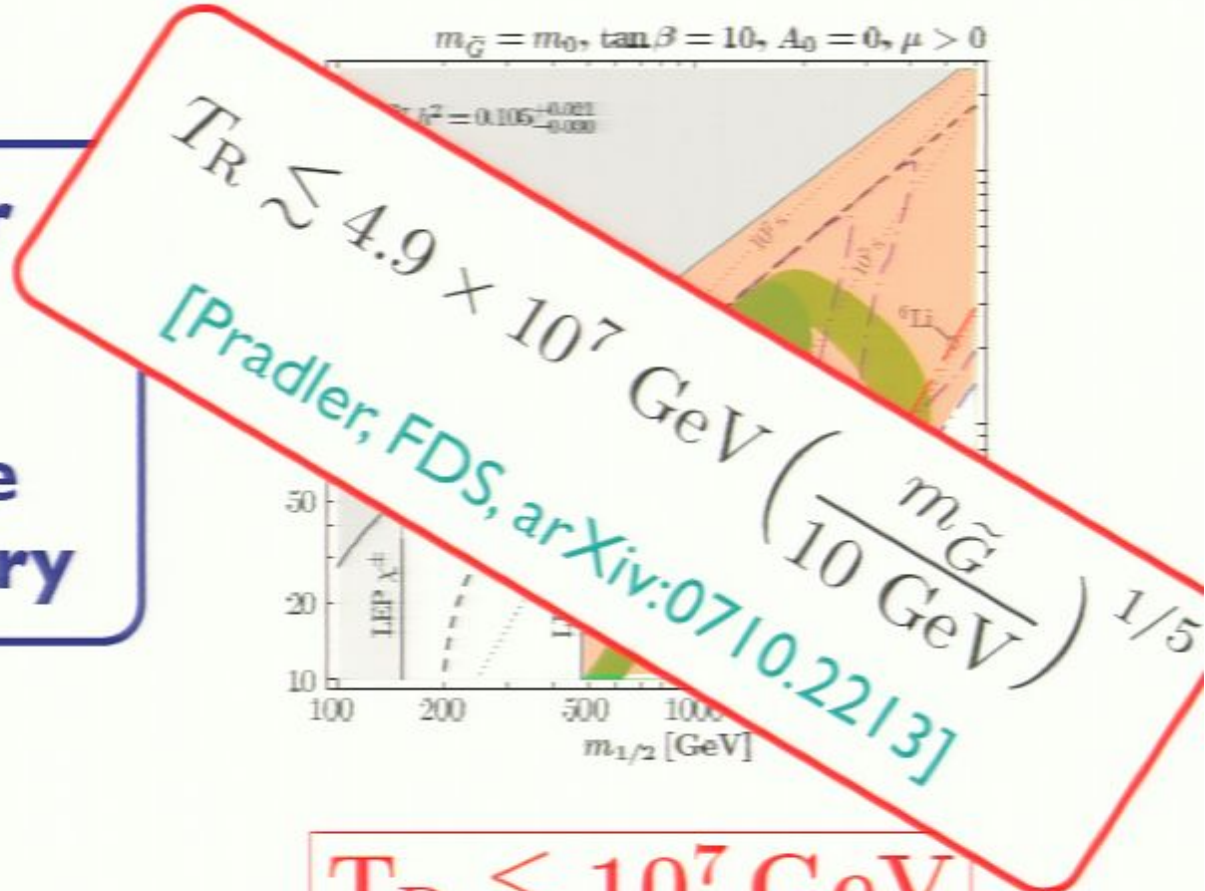
$$T_R \lesssim 10^7 \text{ GeV}$$



Thermal Leptogenesis requires $T > 10^9 \text{ GeV}$

Upper Bounds on T_R in the CMSSM with \tilde{G} Dark Matter

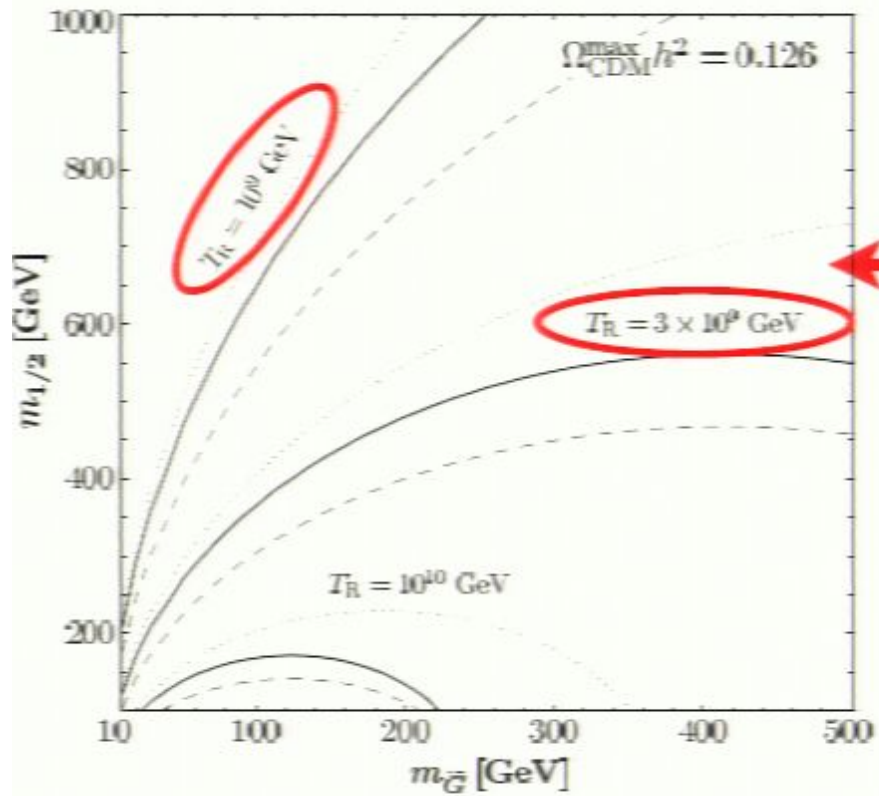
Implications for inflation and the origin of the baryon asymmetry



$$T_R \lesssim 10^7 \text{ GeV}$$

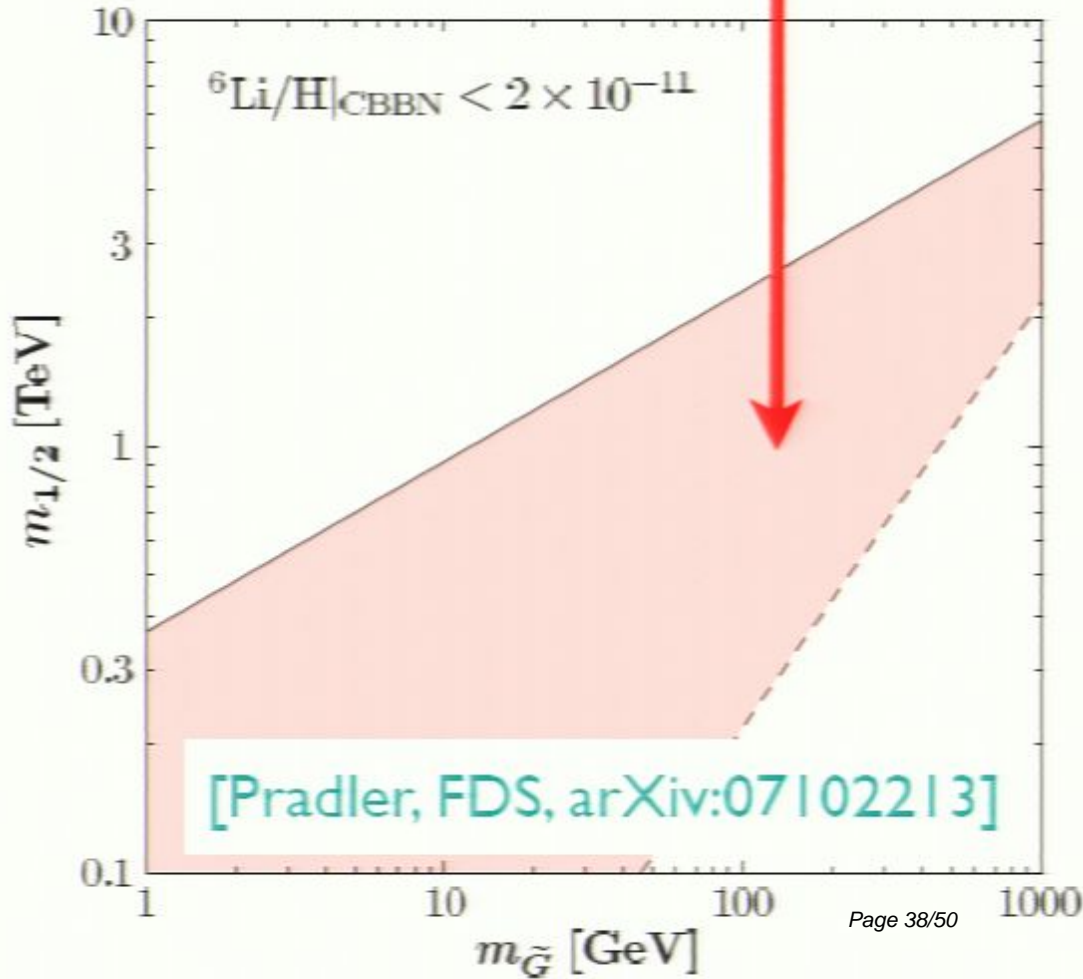


Thermal Leptogenesis requires $T > 10^9 \text{ GeV}$

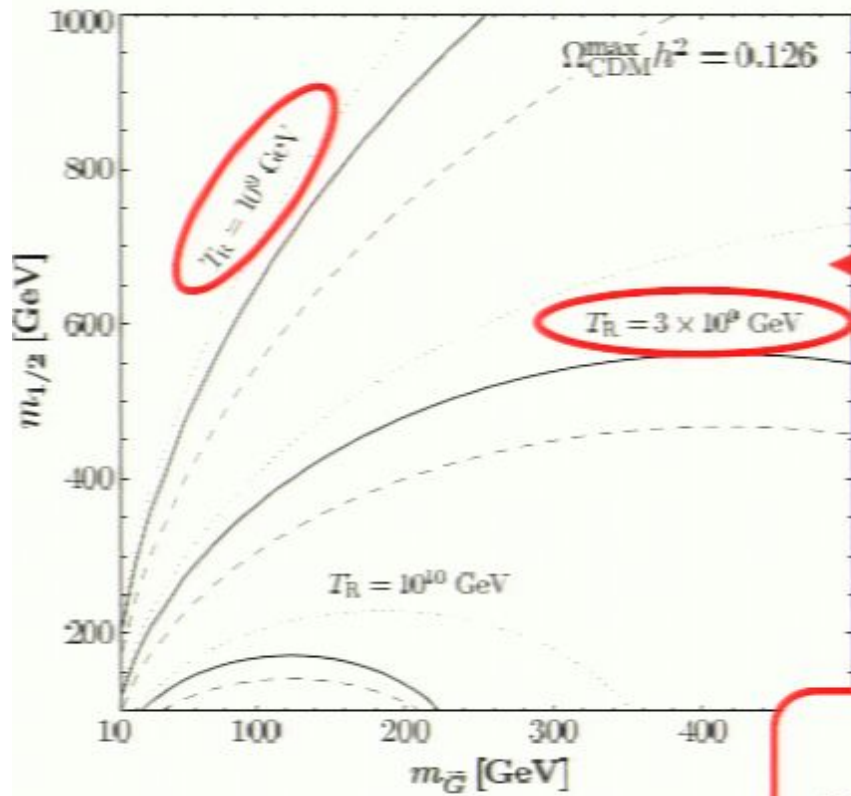


[Pradler, FDS, '06]

**disfavored
by
cosmological
constraints**

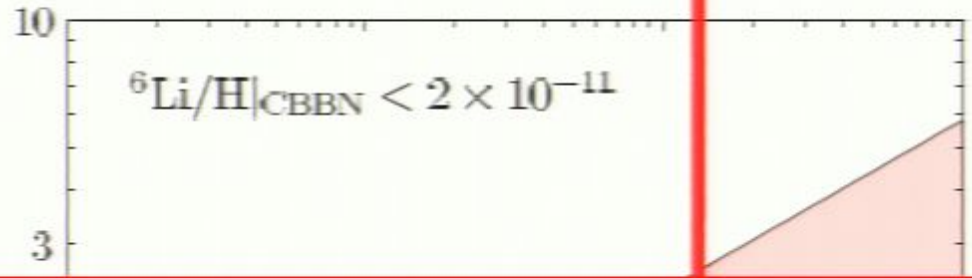


[Pradler, FDS, arXiv:07102213]



[Pradler, FDS, '06]

**disfavored
by
cosmological
constraints**



$$m_{1/2} \geq 0.9 \text{ TeV} \left(\frac{m_{\tilde{G}}}{10 \text{ GeV}} \right)^{2/5}$$

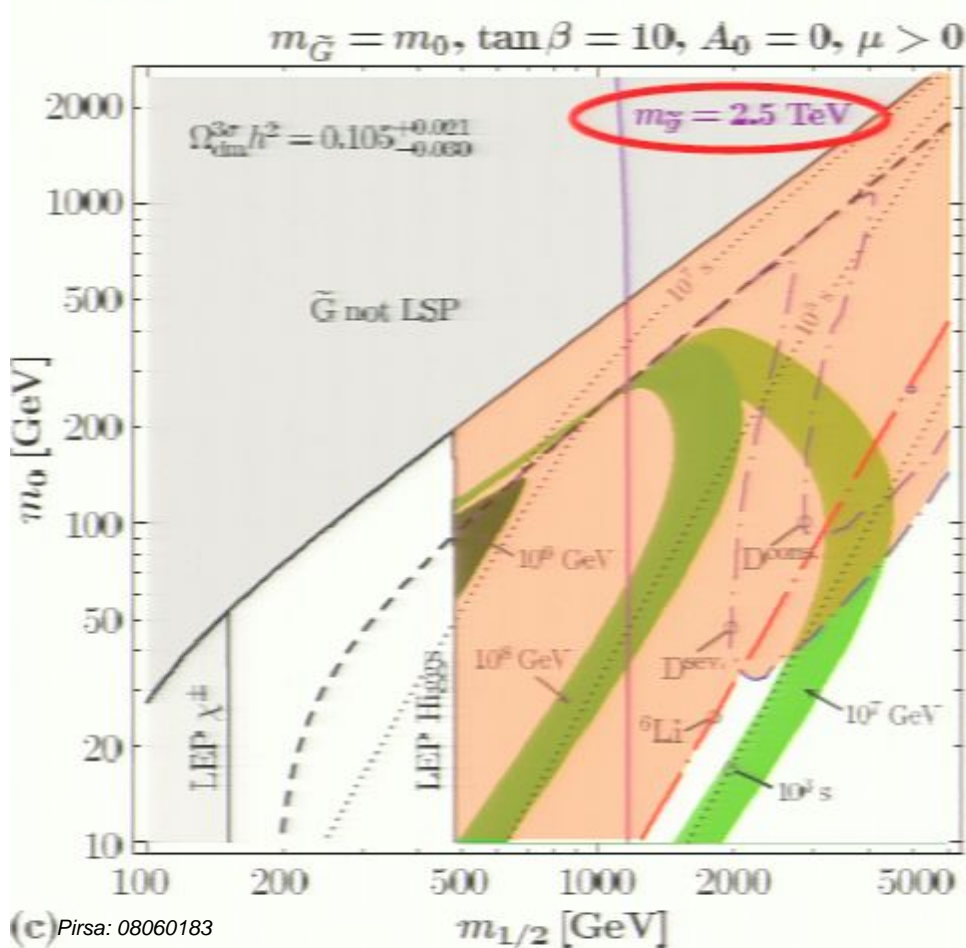
$$T_R \lesssim 4.9 \times 10^7 \text{ GeV} \left(\frac{m_{\tilde{G}}}{10 \text{ GeV}} \right)^{1/5}$$

[Pradler, FDS, arXiv:0710.2213]

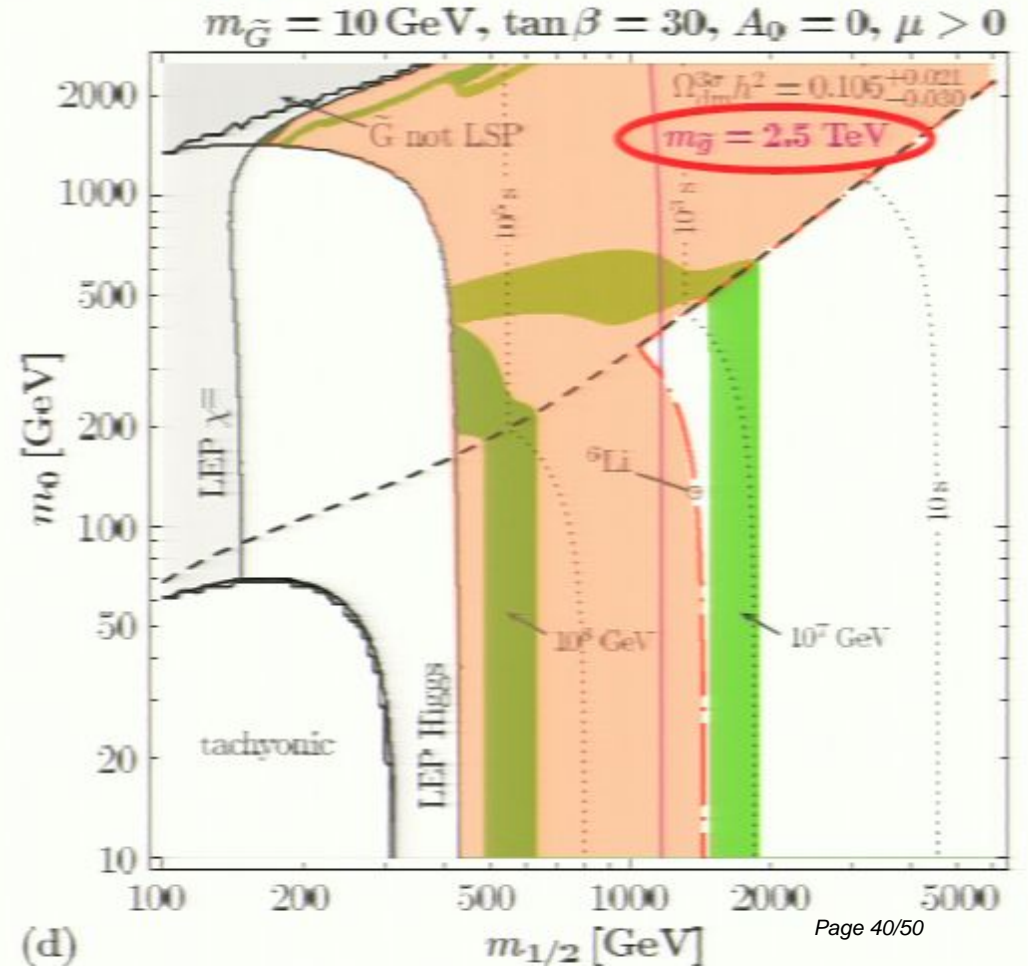


Gravitino DM with a GeV scale mass (as obtained in gravity med. SUSY breaking) could be very difficult to probe at the LHC

[Cyburt et al., astro-ph/0608562, Pradler, FDS, hep-ph/0612291 & arXiv:0710.4548]



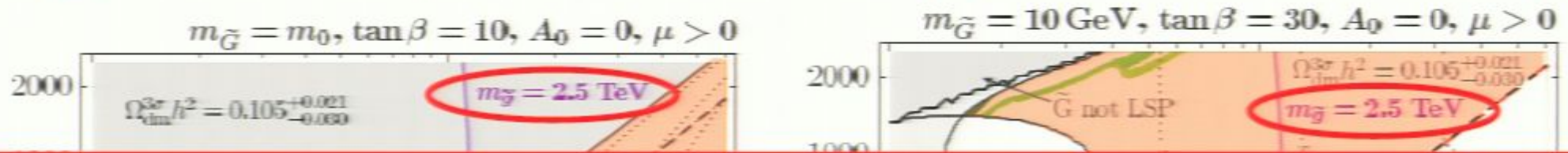
(c) Pirs: 08060183



(d)

Gravitino DM with a GeV scale mass (as obtained in gravity med. SUSY breaking) could be very difficult to probe at the LHC

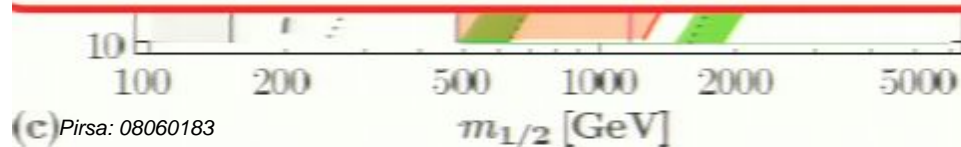
[Cyburt et al., astro-ph/0608562, Pradler, FDS, hep-ph/0612291 & arXiv:0710.4548]



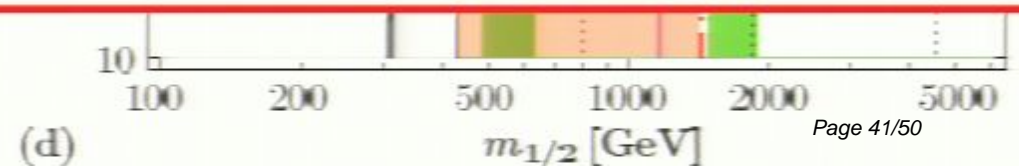
Gravitino DM with a mass $< 1 \text{ GeV}$

(as obtained in gauge mediated SUSY breaking)

could still be accessible at the LHC



(c) Pirs: 08060183



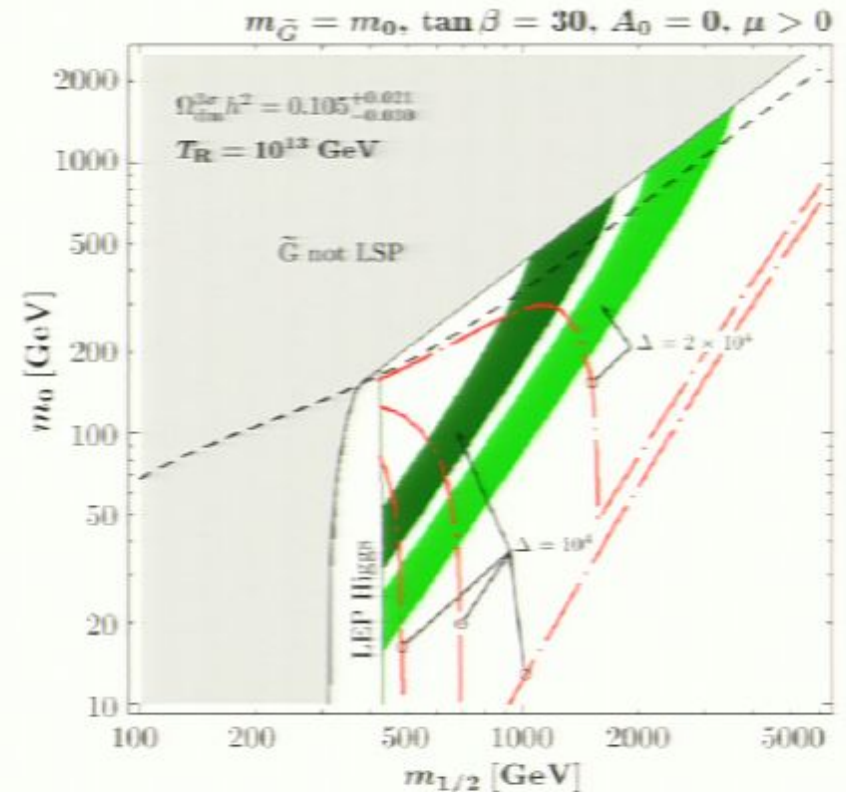
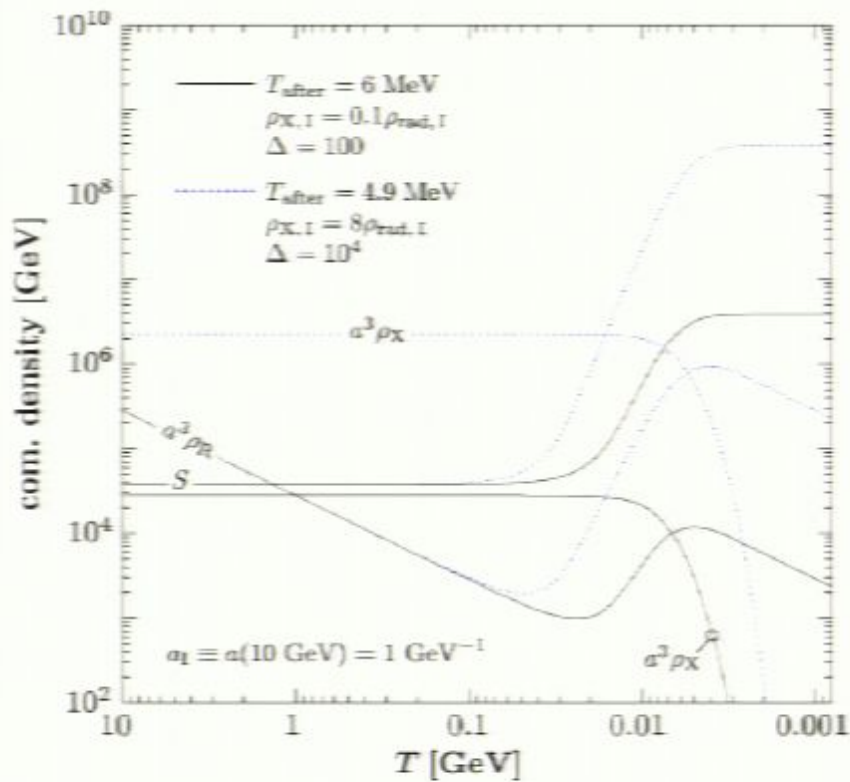
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Warning: Standard Cosmological History

Late-Time Entropy Production

[Pradler, FDS, '07]

Rescuing Thermal Leptogenesis



$$\frac{d\rho_{\text{rad}}}{dt} + 4H\rho_{\text{rad}} = \Gamma_{\phi}\rho_{\phi},$$

$$\frac{d\rho_{\phi}}{dt} + 3H\rho_{\phi} = -\Gamma_{\phi}\rho_{\phi},$$

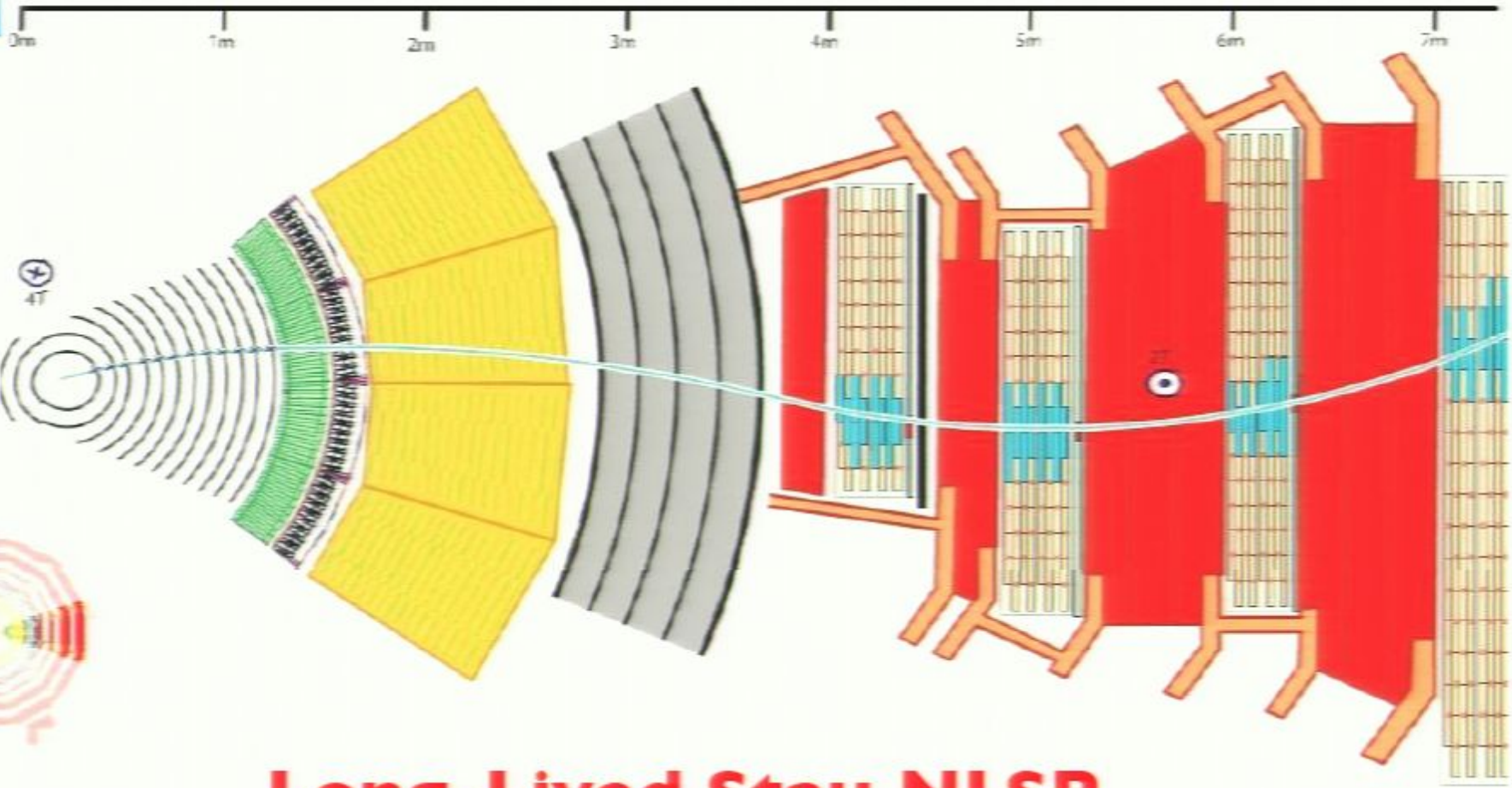
$$\frac{dS}{dt} = \frac{\Gamma_X \rho_X a^3}{T} = \left(\frac{2\pi^2}{45} g_{*}\right)^{1/3} \Gamma_X \rho_X a^4 S^{-1/3}$$

$$Y_{\tilde{G}}^{\text{TP}}(T_0) = \frac{1}{\Delta} Y_{\tilde{G}}^{\text{TP}}(T_{\text{low}}),$$

$$Y_{\text{NLSP}}(T_0) = \frac{1}{\Delta} Y_{\text{NLSP}}(T_{\text{low}})$$

$$\eta(T_{\text{after}}) = \frac{1}{\Delta} \eta(T_{\text{before}}).$$

“Stable” Charged Massive Particle @ LHC

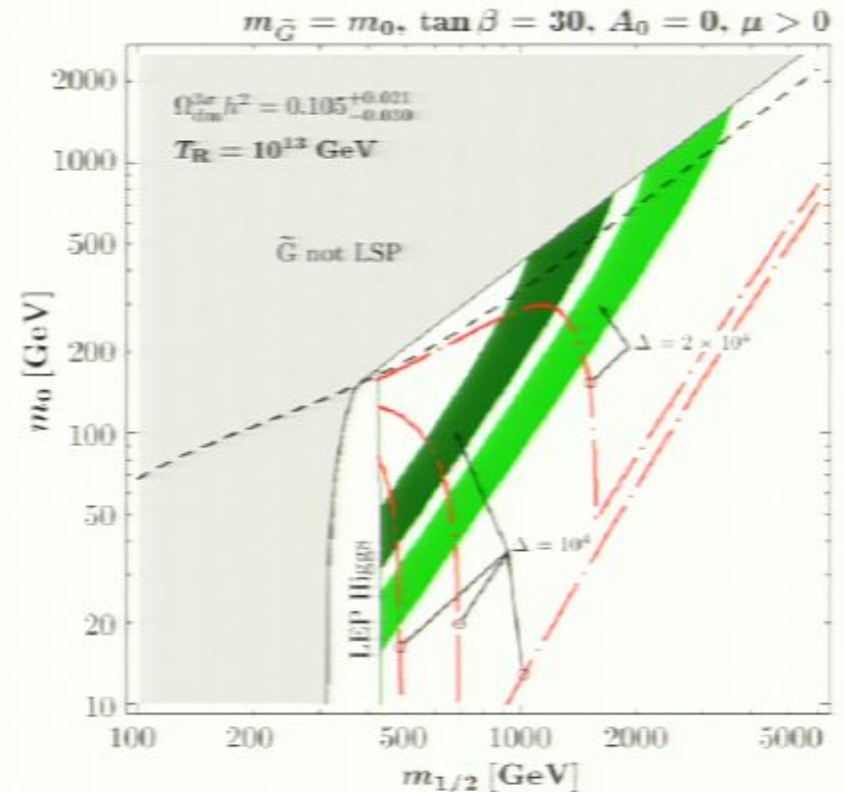
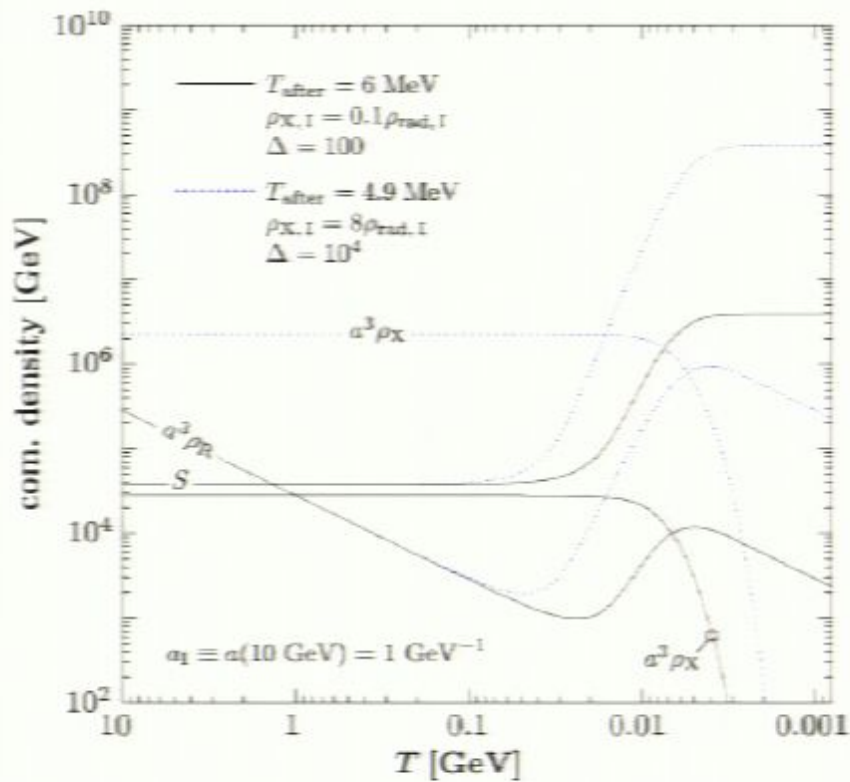


Long-Lived Stau NLSP
[from P. Zalewski's Talk, SUSY 2007]

Late-Time Entropy Production

[Pradler, FDS, '07]

Rescuing Thermal Leptogenesis



$$\frac{d\rho_{\text{rad}}}{dt} + 4H\rho_{\text{rad}} = \Gamma_{\phi}\rho_{\phi},$$

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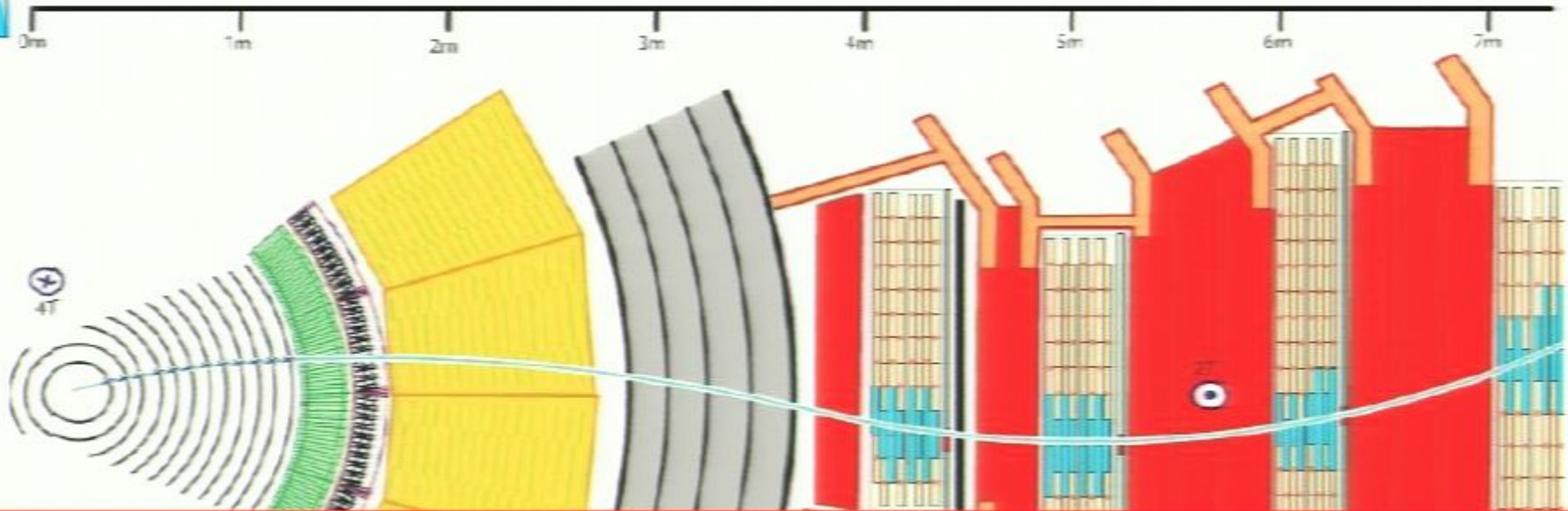
$$\frac{dS}{dt} = \frac{\Gamma_X \rho_X a^3}{T} = \left(\frac{2\pi^2}{45} g_{*}\right)^{1/3} \Gamma_X \rho_X a^4 S^{-1/3}$$

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$$Y_{\text{NLSP}}(T_0) = \frac{1}{\Delta} Y_{\text{NLSP}}(T_{\text{low}})$$

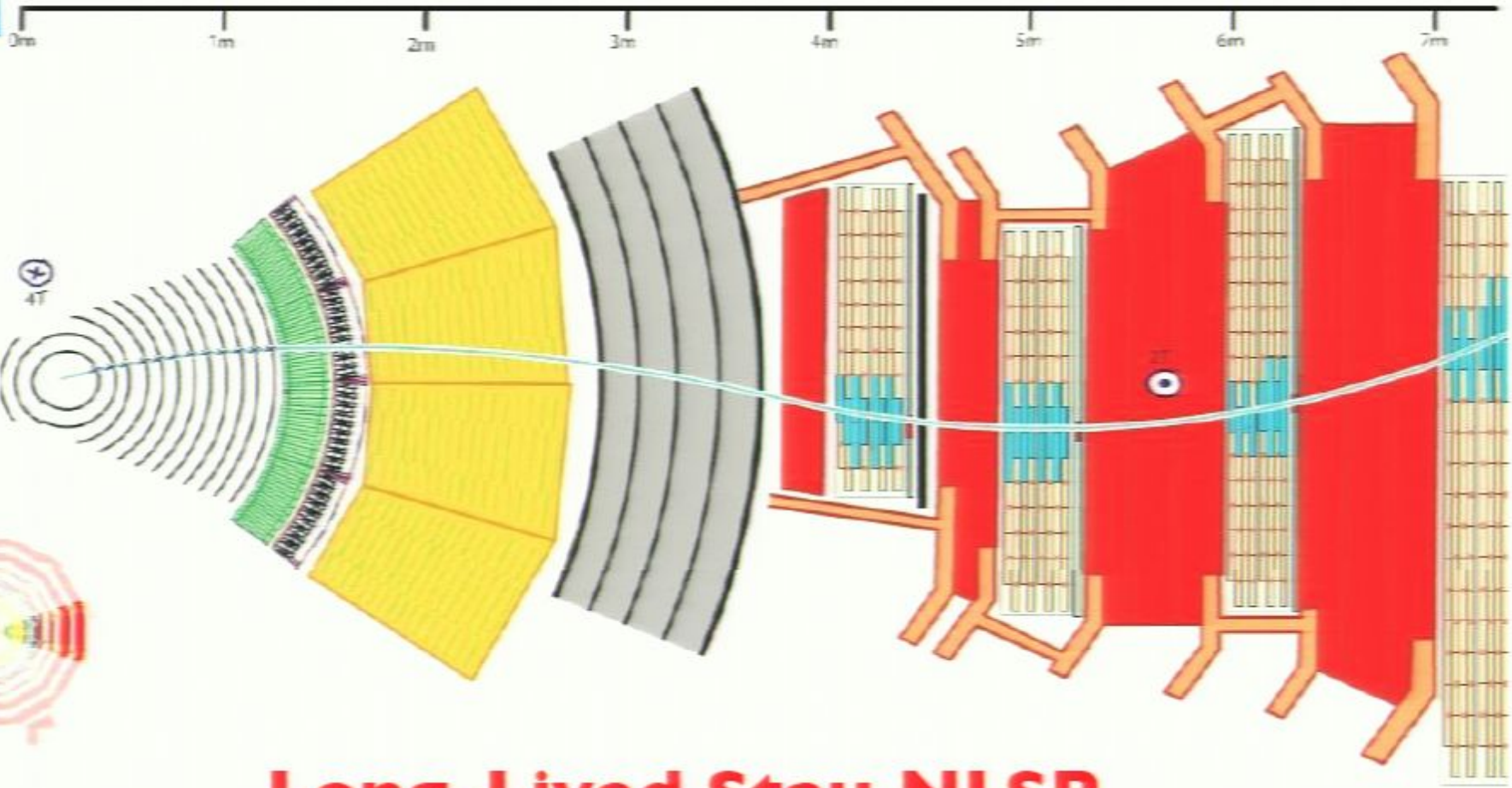
$$\eta(T_{\text{after}}) = \frac{1}{\Delta} \eta(T_{\text{before}}).$$

“Stable” Charged Massive Particle @ LHC



**The smoking gun for
Gravitino (or Axino) Dark Matter
at the LHC**

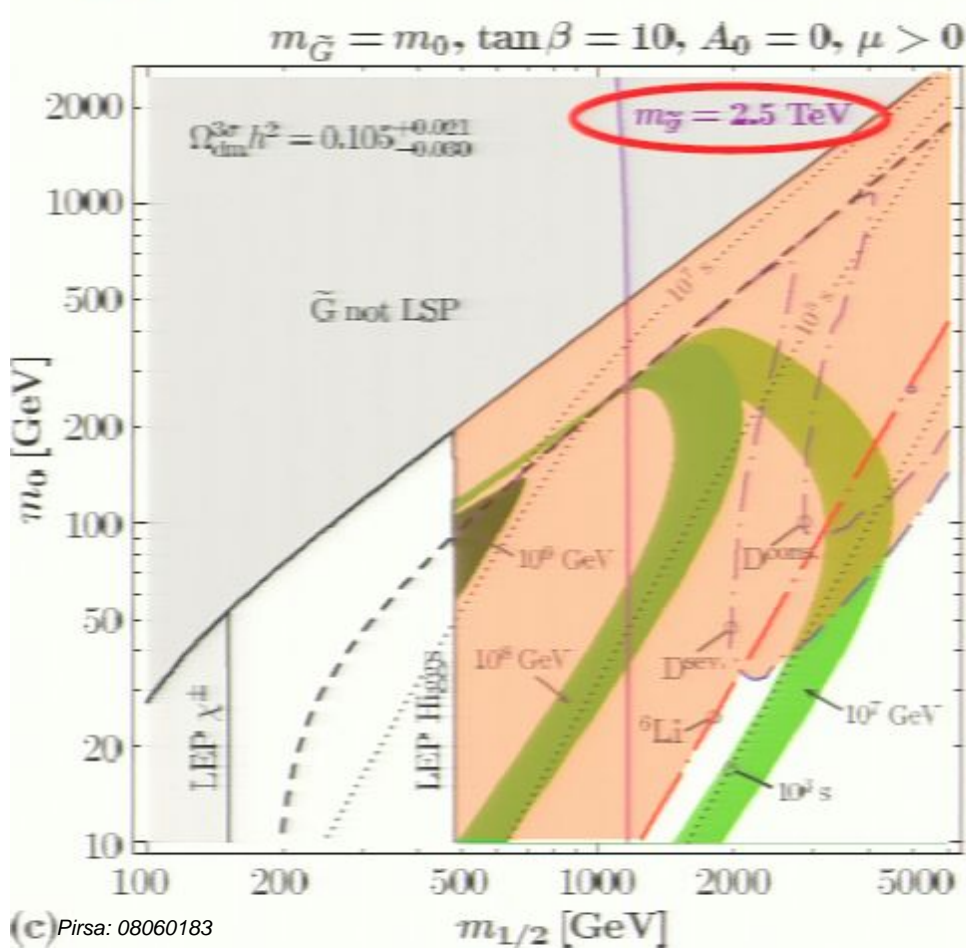
“Stable” Charged Massive Particle @ LHC



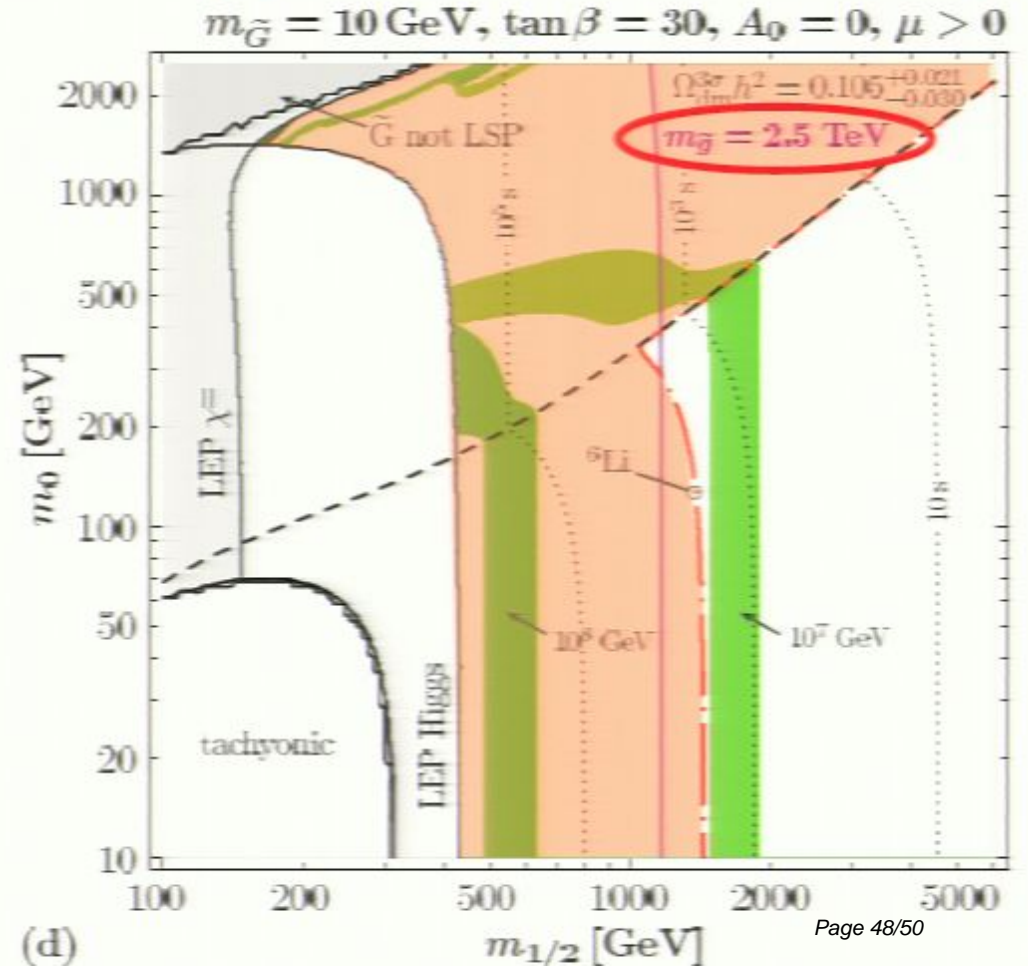
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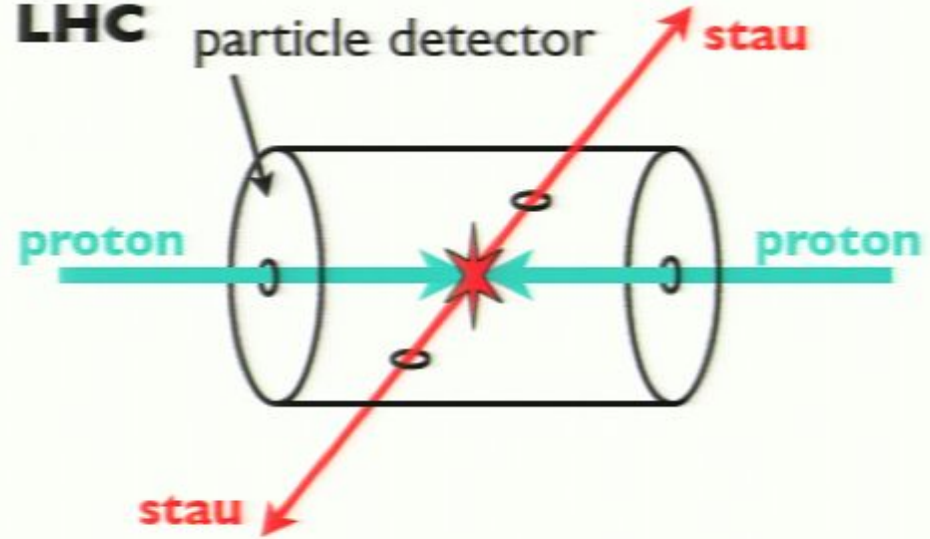
(c) Pirs: 08060183



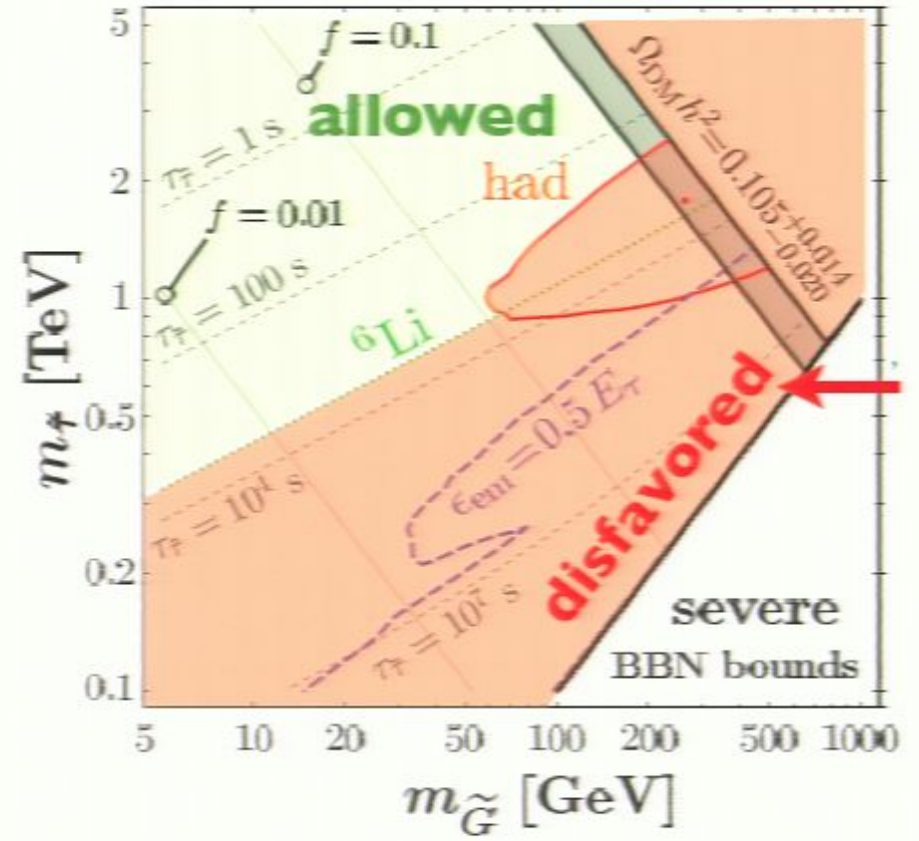
(d)

Gravitino DM @ LHC ← Stau NLSP

2009
LHC



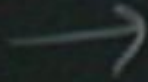
The signal:
jets + leptons
+ 2 “stable”
charged particles



Cosmological Constraints

[FDS, hep-ph/0611027 & arXiv:0711.1240, Kawasaki, Kohri, Moroi, hep-ph/0703122, ...]

$$(k_1 + k_2 + k_3)^3$$



$$-k_1 + k_2 + k_3$$

$\frac{1}{2}$

