

Title: Gravitational Bursts from Unstable Cosmic Strings

Date: Jun 06, 2008 09:30 AM

URL: <http://pirsa.org/08060168>

Abstract: We compute the GW signature of a meta-stable cosmic string network. Such networks arise in a large class of brane inflation models.

The Bursts and The Beads

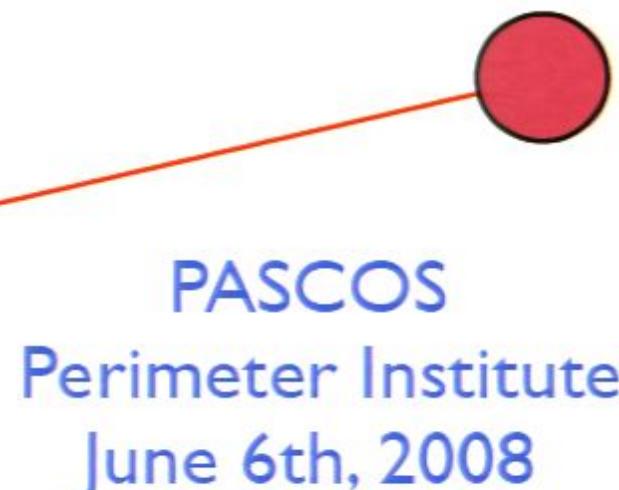
(gravitational bursts from monopoles on strings)

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Based on:

ArXiv:0806.xxxx (with Louis Leblond and Xavier Siemens)



PASCOS
Perimeter Institute
June 6th, 2008

Outline

- Motivation for Cosmic Strings
 - Brane Inflation
 - Detectable!
- Generic Instability
 - Motivation
 - Effects
- Cosmological Evolution
 - Boltzmann Eq. and Scaling
 - World Sheet Picture
- GW Signature
 - Bursts
 - Stochastic

Why Cosmic Strings?

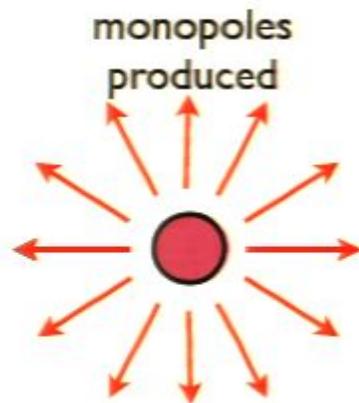
- Many (not all) Brane Inflationary scenarios predict their existence, e.g. KKLMMT
- Detectability
 - High tension: lensing, Kaiser-Stebbins
 - Low tension: LIGO/LISA (Stochastic GW, Cusp-GW bursts) B-Mode CMB
 - Extra low tension: LIGO/LISA(Monopole-GW Bursts), Pulsar Timing (perhaps)

Why monopoles?

Copeland, Myers, Polchinski, Martin, Guth, Vilenkin

- Generic instability of cosmic superstrings
- Pattern of Symmetry Breaking: Monopoles, then Strings.

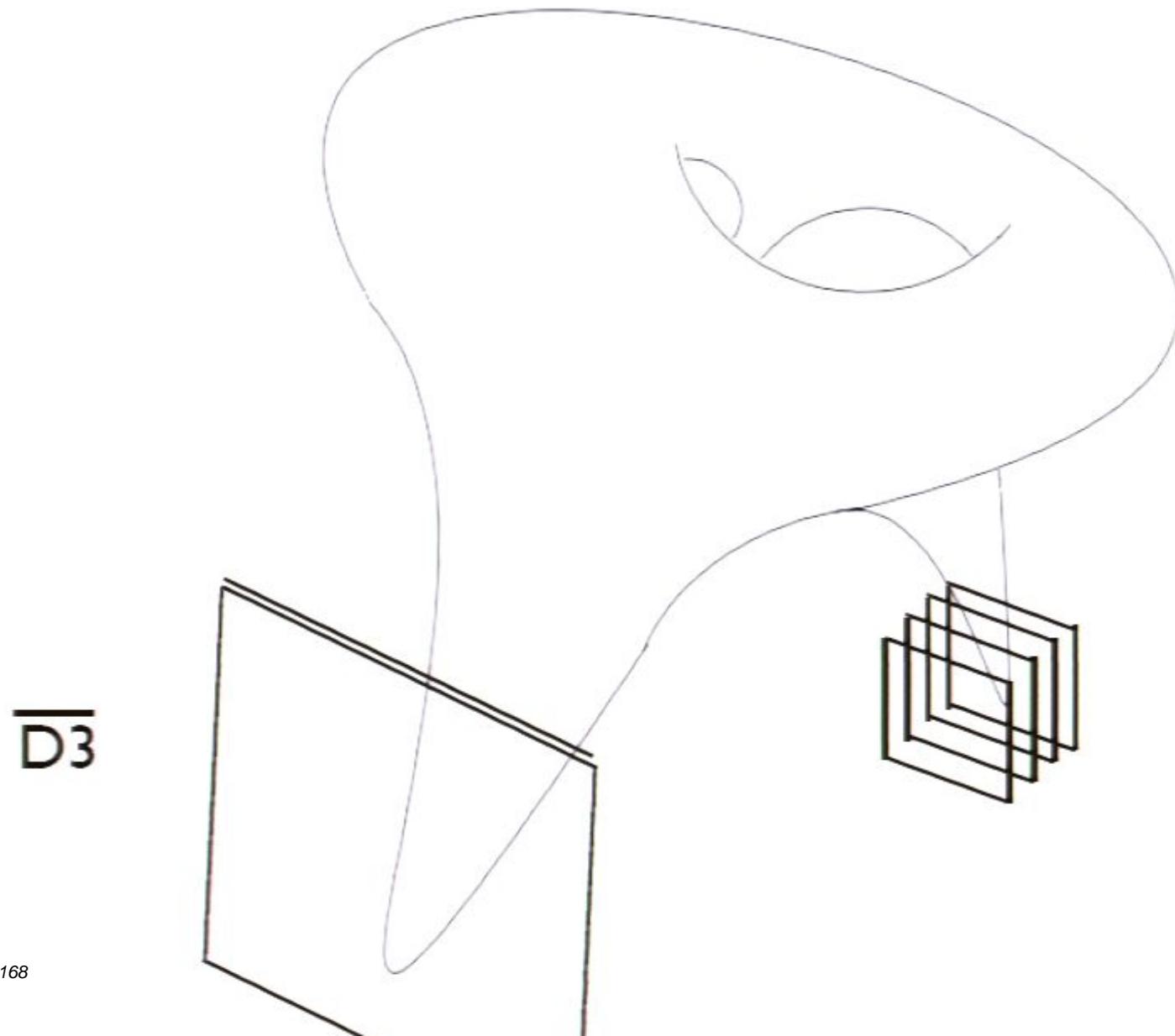
$$G \rightarrow H \times U(1) \rightarrow H$$



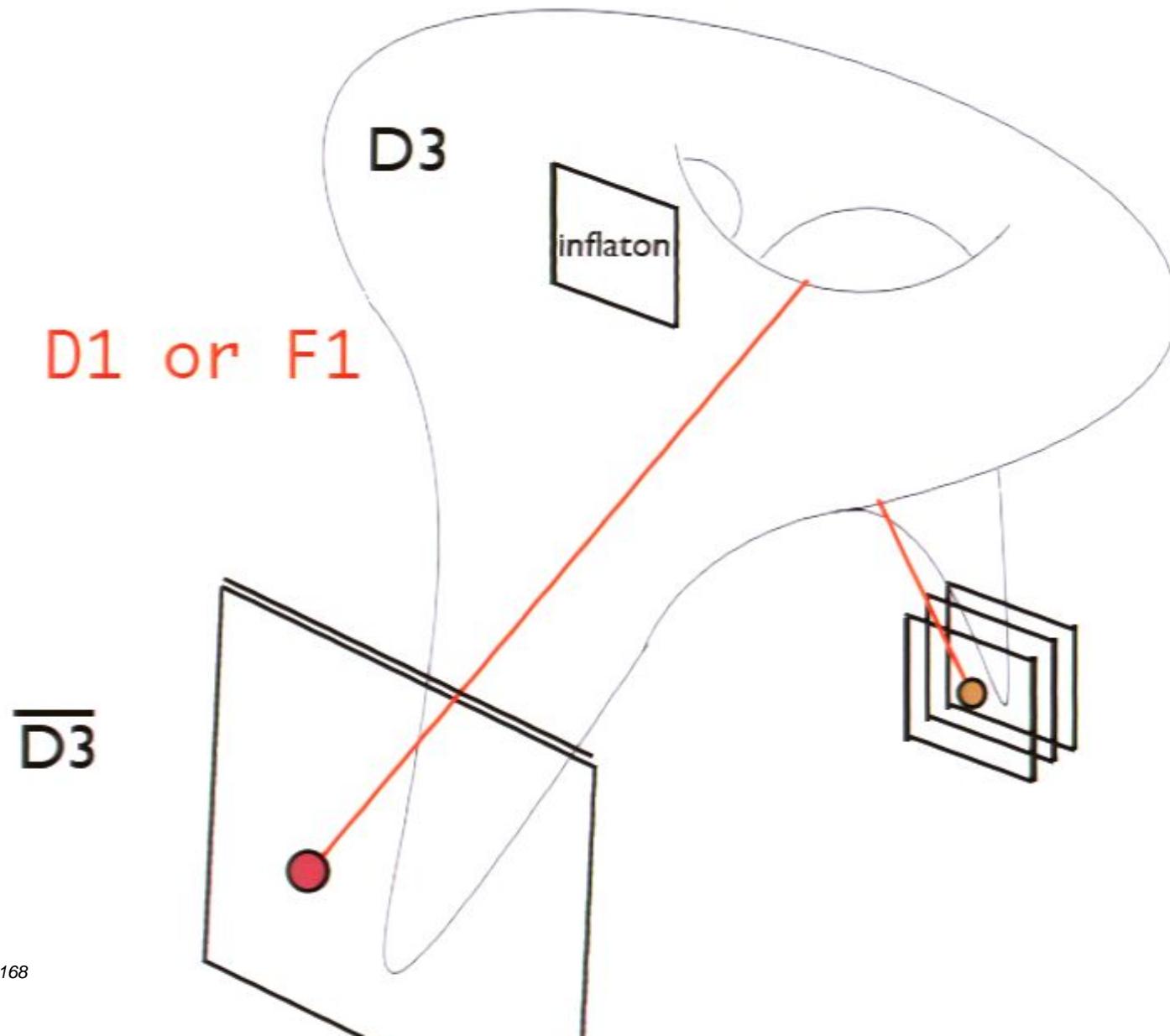
monopoles' flux
is confined
into a string



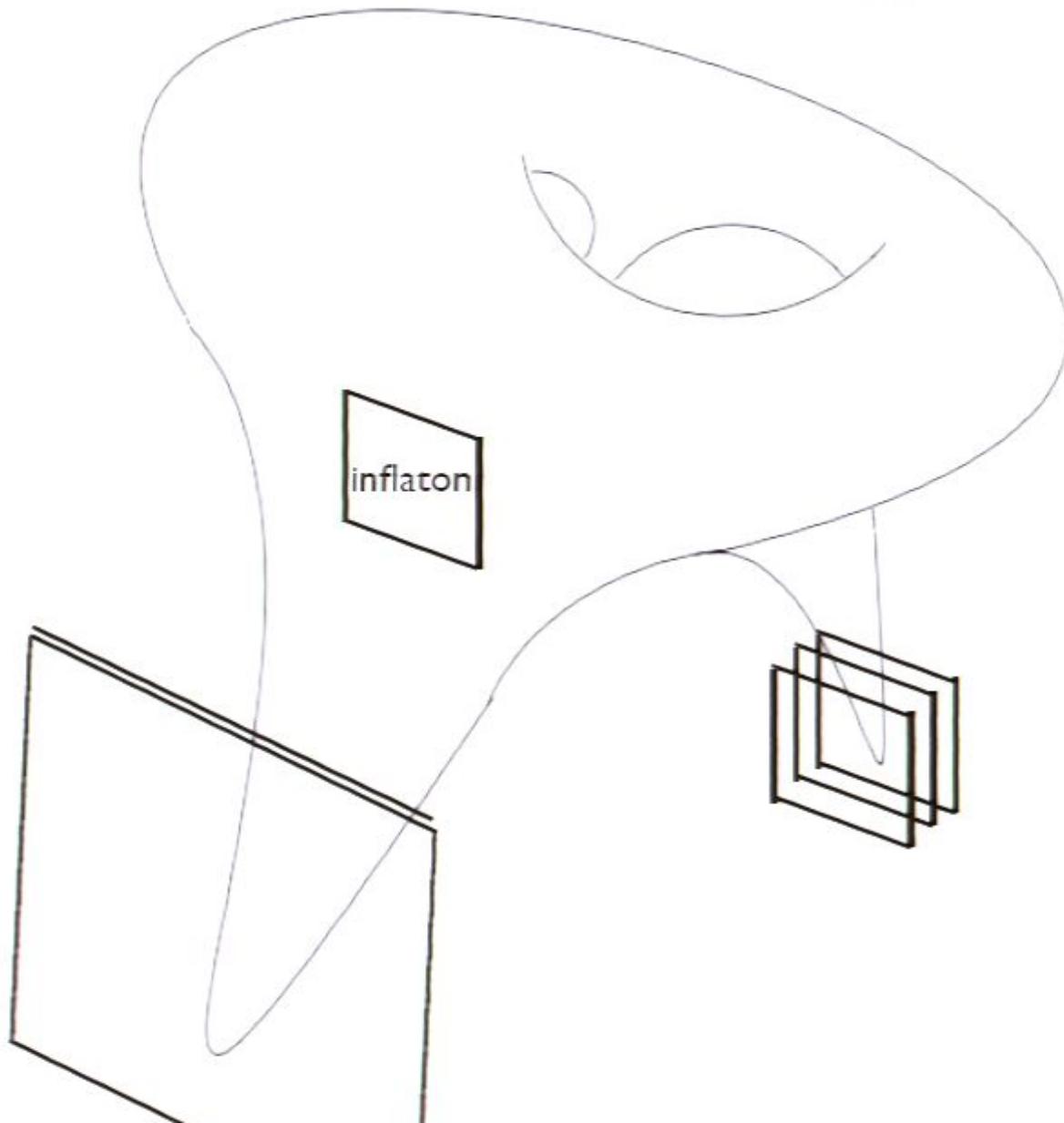
IIB Flux Compactification w/ $\overline{\text{D}3}$



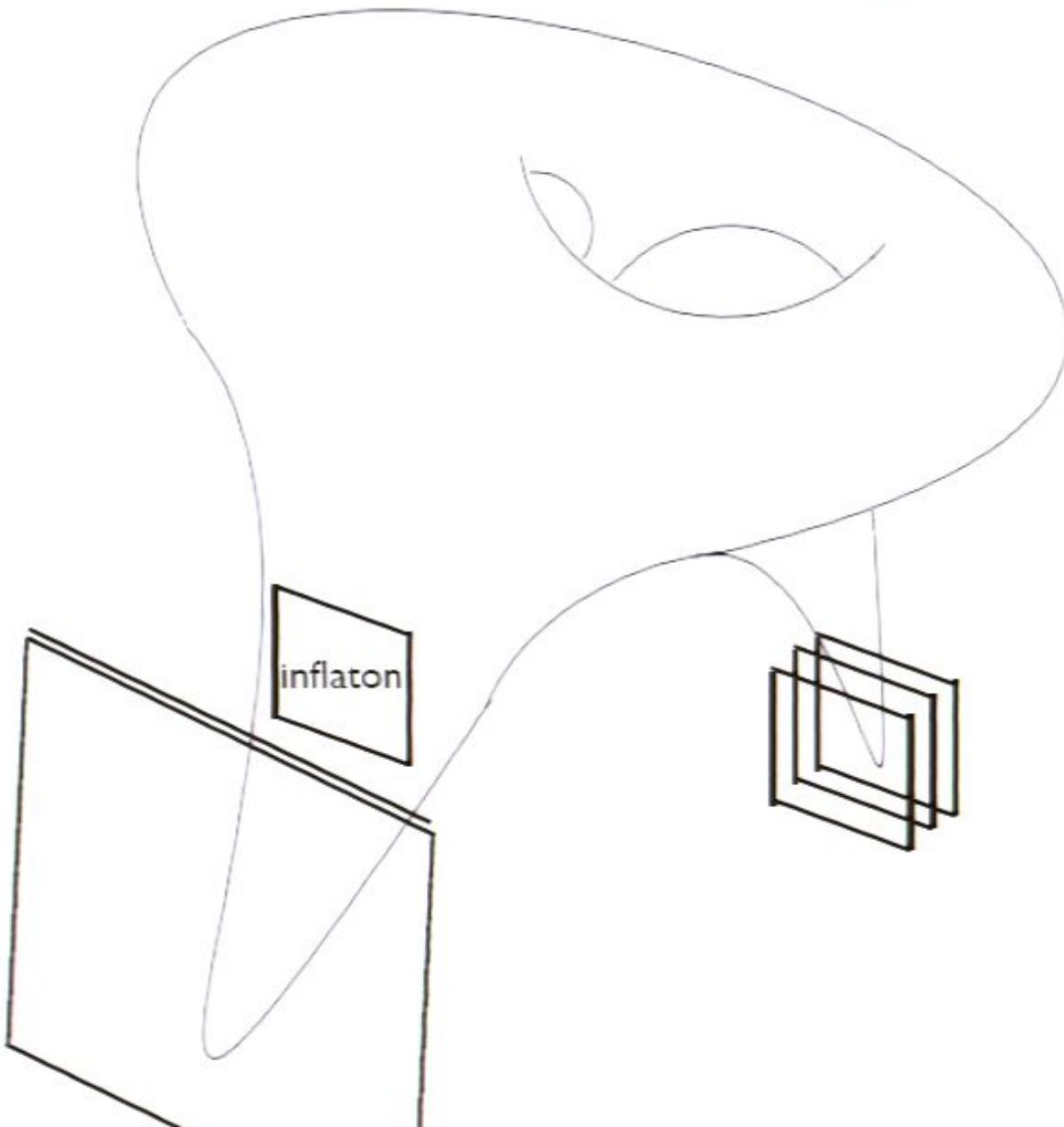
Spectrum contains monopoles
(but they're inflated away)



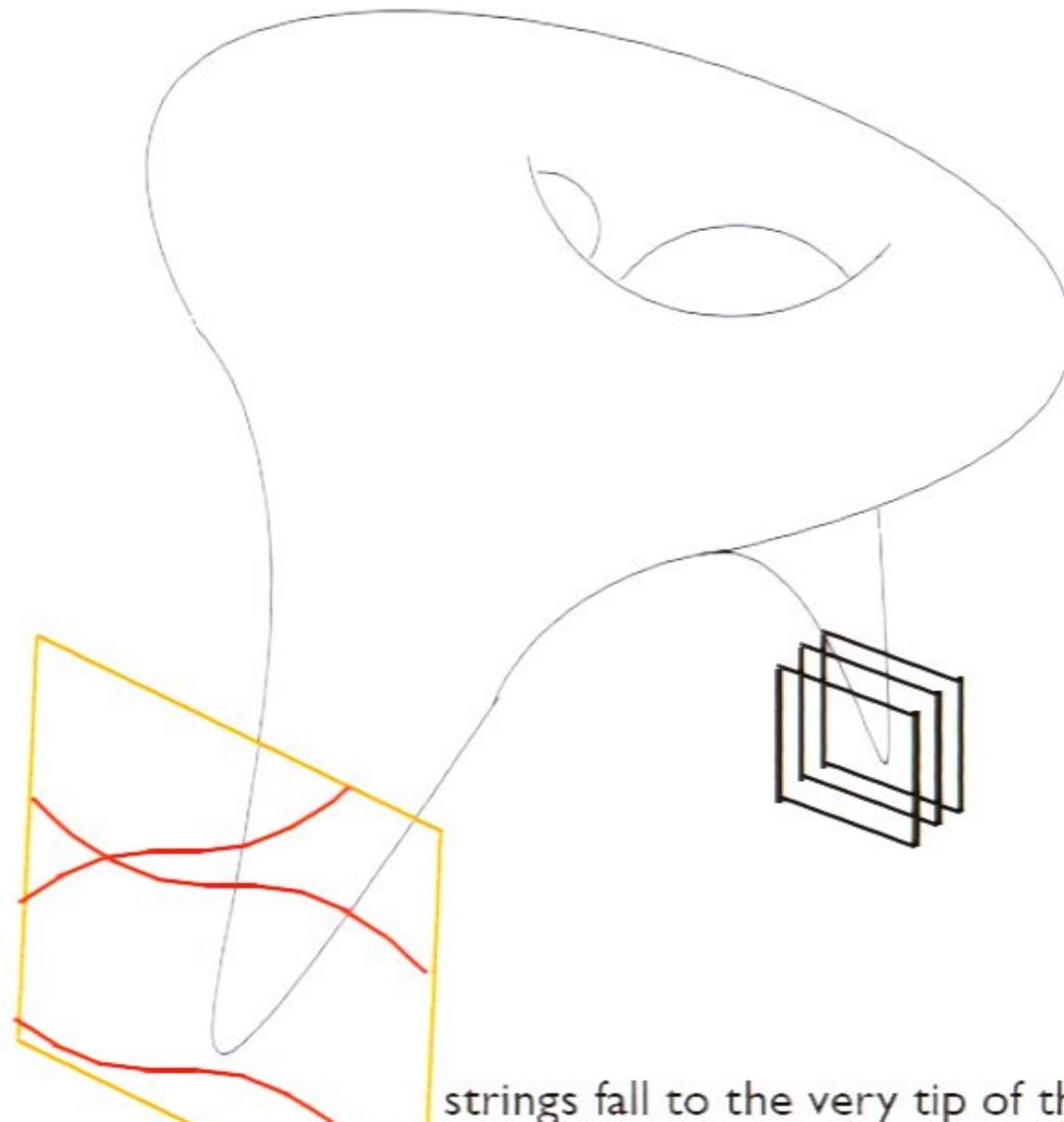
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Cosmic Strings are Produced via Kibble Mechanism

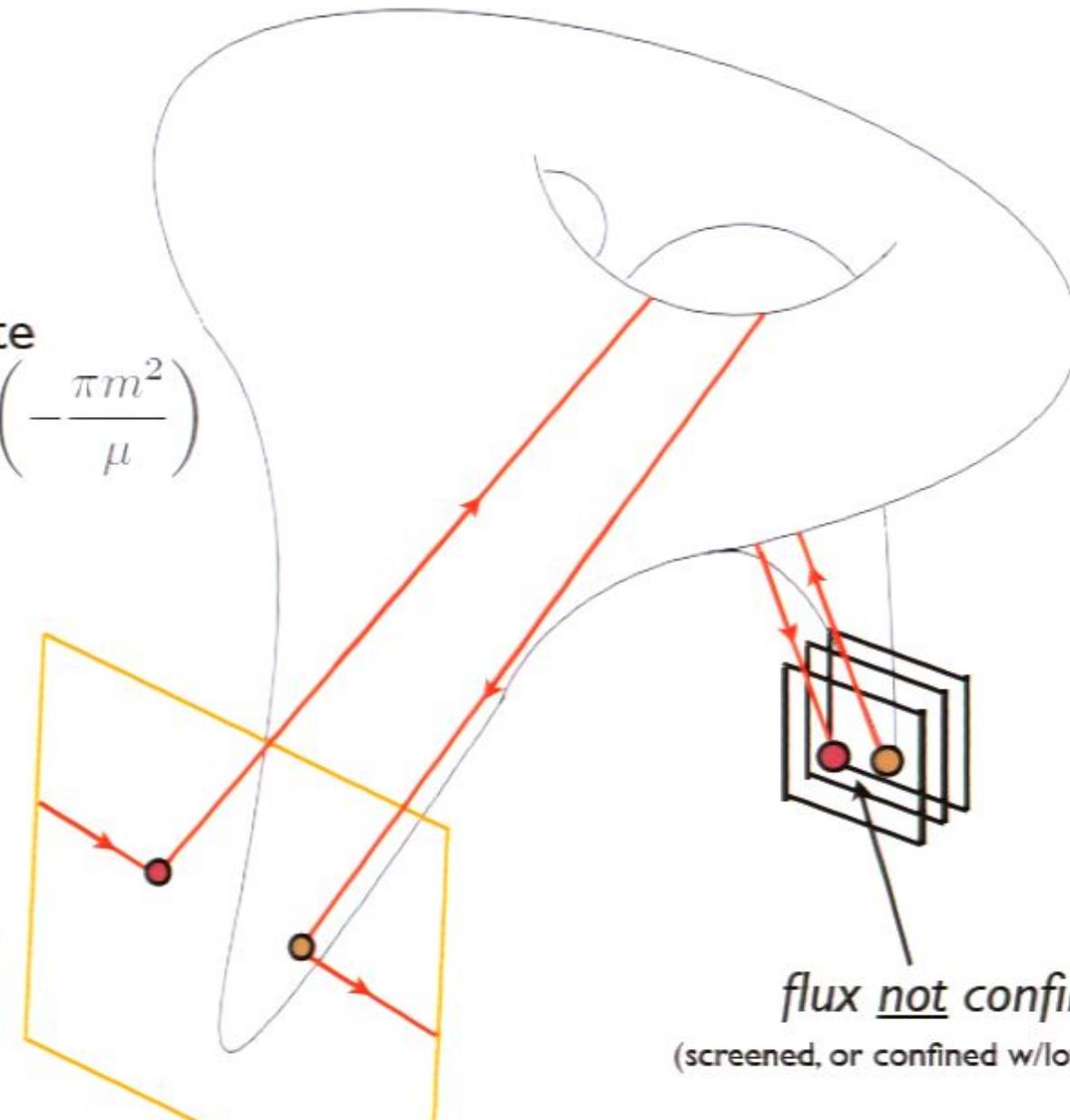


Cosmic Strings Break via Monopole Pair Production

Breakage Rate

$$\Gamma_2 = \frac{\mu}{2\pi} \exp\left(-\frac{\pi m^2}{\mu}\right)$$

monopoles
neutral under
all light fields



(screened, or confined w/lower tension)

GW Radiation

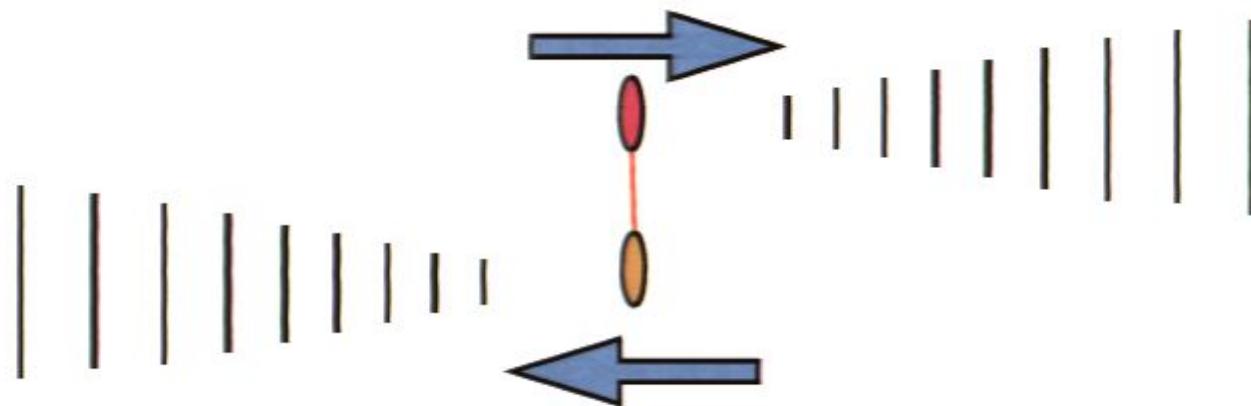
monopoles are accelerated over extremely long distances



Also contributes to stochastic GW background

Highly focused GW Burst

monopoles are *ultra ultra* relativistic !!!
with a changing acceleration



$$\gamma = 1/\sqrt{1-v^2} \lesssim \mu/Hm$$

γ can be Hubble length in string units!

Cosmological Evolution of Cosmic Strings

$$\rho_{cs} \sim 1/a^2$$

inert strings

$$\rho_{cs} \sim 1/t^2$$

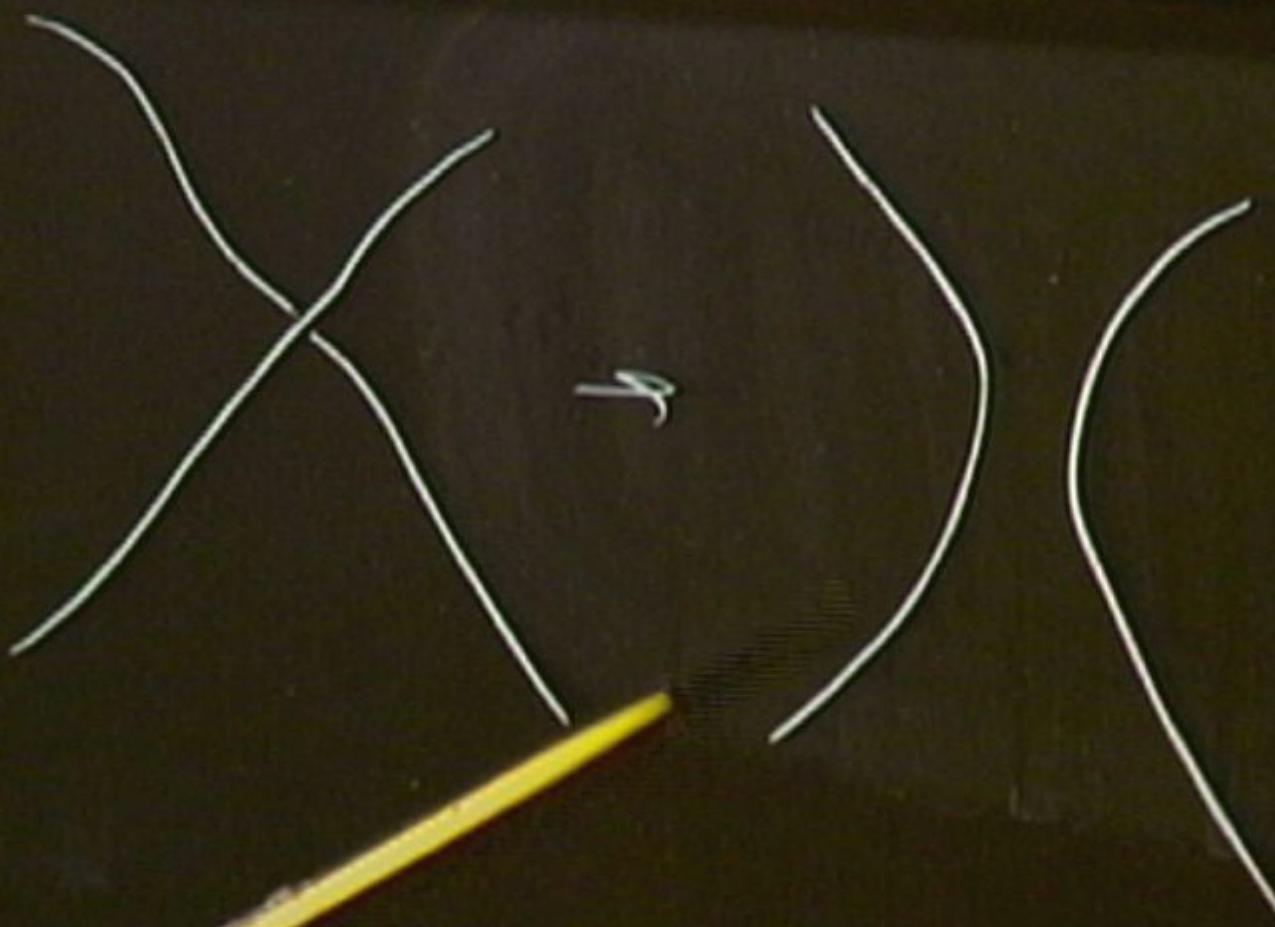
actual strings

$$\Rightarrow \rho_{cs} \sim \begin{cases} 1/a^4 & \text{radiation era} \\ 1/a^3 & \text{matter era} \end{cases}$$

Mechanism: String collisions (intercommutation)
generates small scale wiggles on the strings.
These cause the strings to quickly lose energy via
production of small loops.

wiggles \Rightarrow loops

more string \Rightarrow more collisions \Rightarrow more loop production.
 \Rightarrow Stable Scaling Solution



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Cosmological Evolution of String Segments

number density
(per unit length)

$$\frac{\partial n(l, t)}{\partial t} = -\frac{\partial}{\partial l} (\ln(l, t)) - 3 \frac{\dot{a}}{a} n(l, t) + g$$

$$l := E/\mu$$

$$g = g_{loop} + g_{ic} + g_{break}$$

$$g_{break} dl = \Gamma_2 \left(2 \int_l^\infty n(l', t) dl' - \ln(l, t) \right) dl$$

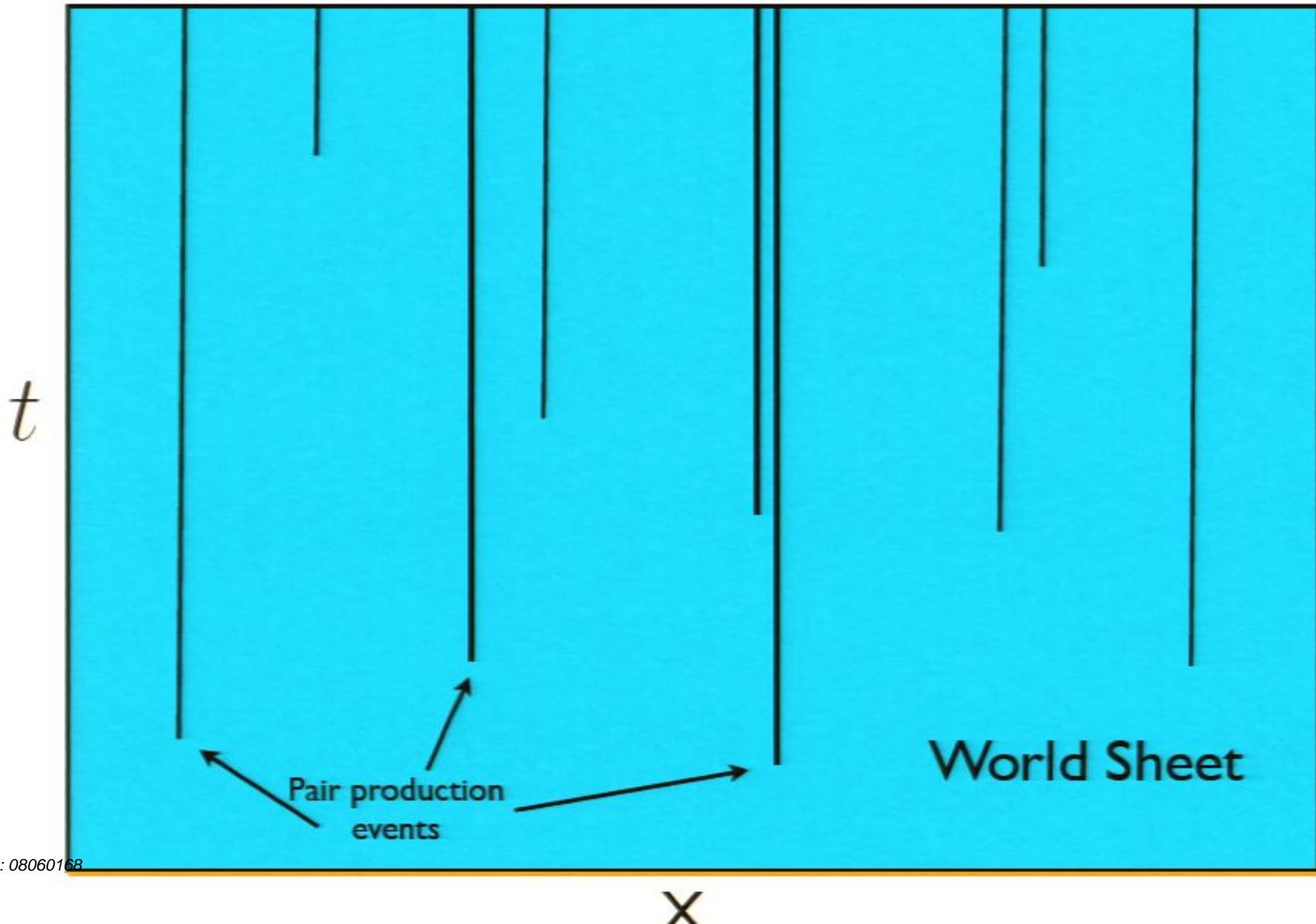
related

$$g_{ic} dl = \Gamma_2^{ic} \left(\frac{1}{2} \int_{l/2}^\infty n(l', t) dl' - \ln(l, t) \right) dl$$
$$g_{loop} = (\text{difficult})$$

But we can use scaling!
 $\subseteq \dot{l}$

number density: easy derivation of $n(l, t)$

$$P_k(A) = \frac{(A\Gamma_2)^k e^{-A\Gamma_2}}{k!} \quad \Rightarrow \quad P(l, t) = e^{-\Gamma_2 lt} \Gamma_2 t dl$$



number density (per unit length)

$$P_k(A) = \frac{(A\Gamma_2)^k e^{-A\Gamma_2}}{k!} \quad \rho_{cs}(t) \sim \mu/t^2$$

$$\Rightarrow n(l, t) \sim \Gamma_2^2 e^{-\Gamma_2 l t}$$

Boltzmann Equation Solution:

$$n(l, t) = 4\Gamma_2^2 e^{-2\Gamma_2 l t}$$

worldsheet method not
too bad...

Gravitational Wave Signature

- Because monopoles are ultra relativistic, bursts are extremely intense. Thus strings with no measurable kink/cusp bursts can still yield a strong burst signature
- The scaling solution of cosmic strings remains robust, and allows for a tremendous signal over certain parameter ranges.

Damour, Vilenkin, Hogan, Siemens,
Creighton, Maor, Majumder, Cannon, Reed

details

$$h(f, \gamma, r) \approx \frac{G\mu}{r} \frac{\gamma^2}{f^2}$$

Strain (+ polarization)

$$\theta \approx 1/\gamma$$

Beam width

$$n(l, t)$$

Number density

⇒ LIGO detection event rate

results (preliminary)

$m^2 \lesssim 50\mu$ \Rightarrow LIGO off the chart!

Strong constraints on m
even for extremely light strings!

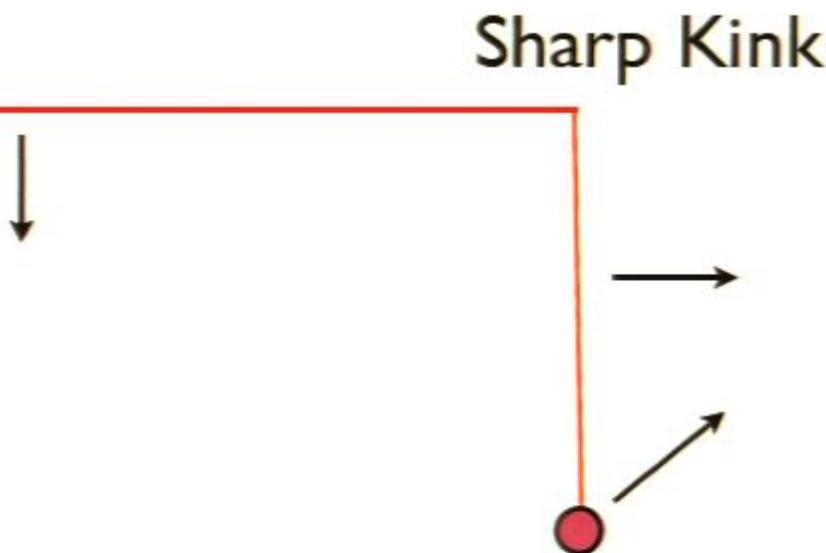
Bottom Line: Many models
(even those with extremely light strings)
are ruled out.

Interesting Possibilities

- Kinks and small scale wiggles lead to bursts, too (extreme gamma factor is robust)
- Oscillation smoothens strings, after rapid loop production
- String segments become dynamical upon Horizon Crossing
 - Coherence to Burst & Stochastic spectra!
 - Does any of this survive intercommutation of segments?

$$g_{ic} dl = \Gamma_2^{ic} \left(\frac{1}{2} \int_{l/2}^{\infty} n(l', t) dl' - l n(l, t) \right) dl$$

Kink-Monopole scattering



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Kink-Monopole scattering



Kink-Monopole scattering



Kink-Monopole scattering



Kink-Monopole scattering



Kink-Monopole scattering



Kink-Monopole scattering

Sharp Kink



Kink-Monopole scattering



Monopoles air-condition string segments

- Monopoles heat up the wiggles & Kinks when collapsing (like Compton scattering)
- String radiates more loops
- Monopoles cool string upon re-expansion

Conclusion

- Monopoles are a generic instability of a cosmic string network
- Ultra relativistic nature gives a strong signal even for light strings (i.e. constrains m^2/μ)
- Exponential sensitivity to monopole mass makes detectability highly model dependent
- Coherence and A/C effect make Monopole Burst Signature striking and unique

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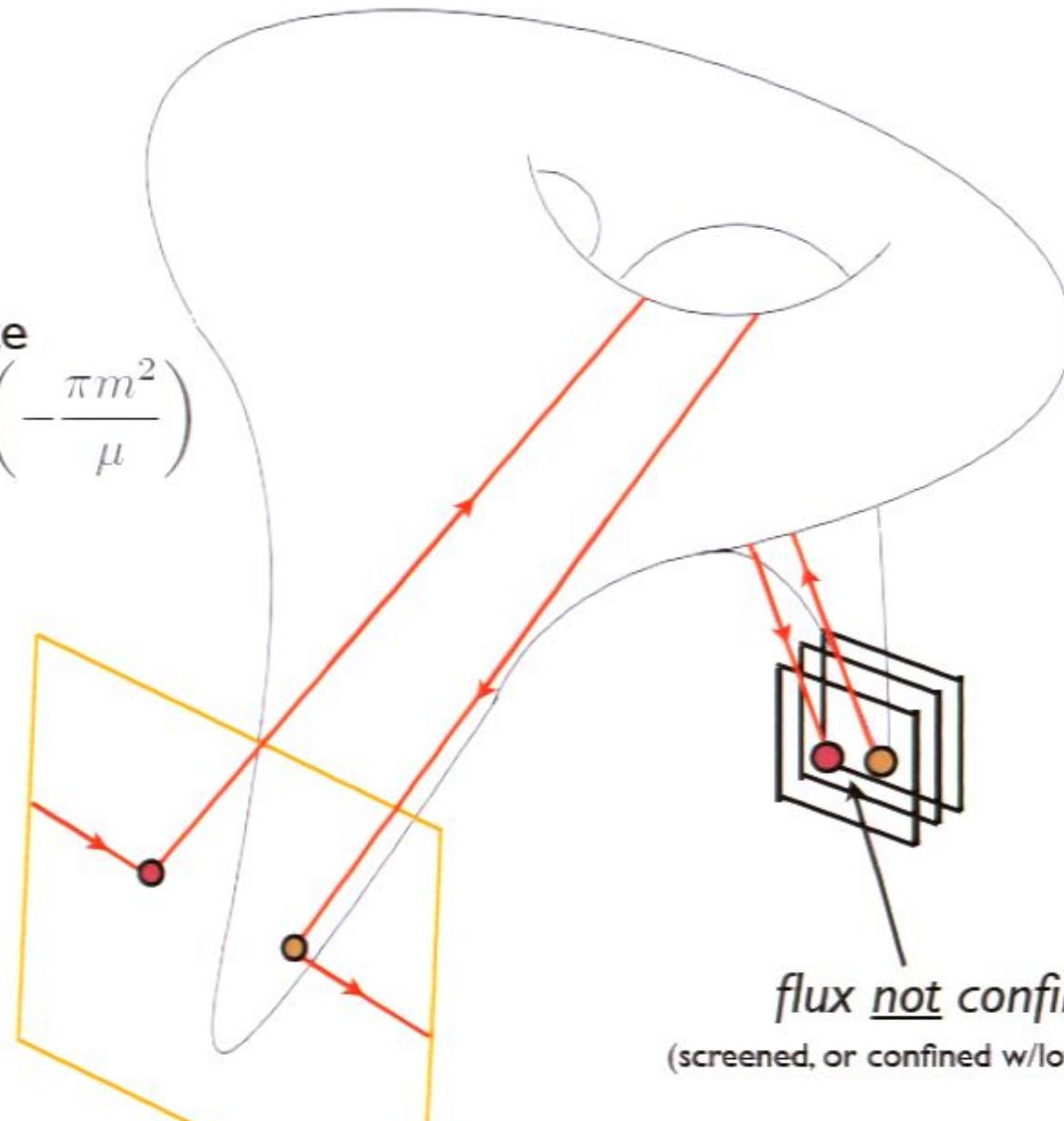
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No Signal
VGA-1