Title: Detecting Cosmic Strings in the CMB

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URL: http://pirsa.org/08060116

Abstract: We further advance the application of the Canny algorithm for detecting cosmic strings in CMB maps.

Detecting Cosmic Strings in the CMB

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McGill University

Collaborator: Robert Brandenberger

Starting point: Amsel, Berger, and Brandenberger (2007)

June 3, 2008 PASCOS

Cosmic Strings

RJD

Outline

Introduction to Cosmic Strings

Signatures

Numerical Studies

Conclusions

1 Introduction to Cosmic Strings

- What are cosmic strings? How are they formed?
- Why might cosmic strings be present?
- What are the current bounds on cosmic strings?
- Why are current bounds not optimal?

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1. **Introduction to Cosmic Strings**
   - What are cosmic strings? How are they formed?
   - Why might cosmic strings be present?
   - What are the current bounds on cosmic strings?
   - Why are current bounds not optimal?
2. **Cosmic String Signatures**
   - Cosmic String Gravity
   - Cosmic String Signatures
   - Why is the Canny algorithm ideal to detect cosmic strings?

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2 Cosmic String Signatures

- Cosmic String Gravity
- Cosmic String Signatures
- Why is the Canny algorithm ideal to detect cosmic strings?

3 Numerical Studies

- Overview
- Simulators
- Canny Algorithm
- Test Results

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   - Cosmic String Gravity
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   - Why is the Canny algorithm ideal to detect cosmic strings?
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   - Overview
   - Simulators
   - Canny Algorithm
   - Test Results
4. **Conclusions**

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Introduction to Cosmic Strings

What are cosmic strings?

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Introduction to Cosmic Strings

What are cosmic strings?

- One-dimensional topological defects

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Introduction to Cosmic Strings

What are cosmic strings?

- One-dimensional topological defects
- Very massive
- Very thin,

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Introduction to Cosmic Strings

What are cosmic strings?

- One-dimensional topological defects
- Very massive
- Very thin, Very long (infinite) or Loops

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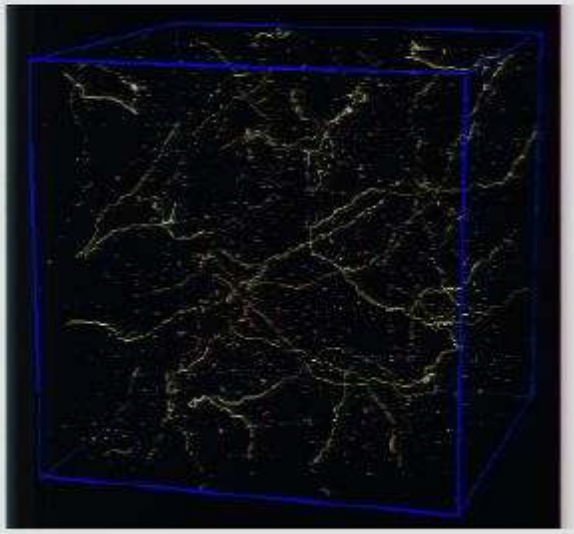
What are cosmic strings?

- One-dimensional topological defects
- Very massive
- Very thin, Very long (infinite) or Loops

C. Martins & E. P. Shellard: Initial cosmic string network simulation



B. Allen & E. P. Shellard: Late time simulation of cosmic strings

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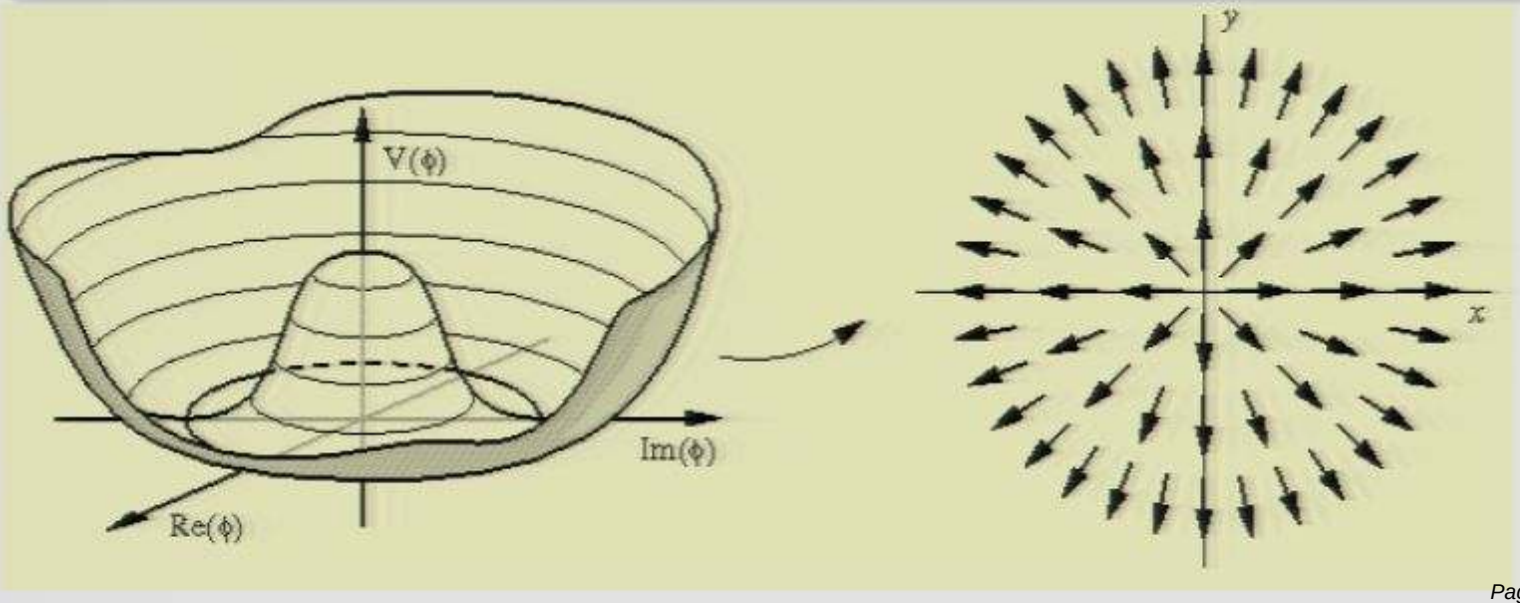
How are cosmic strings formed?

- Spontaneous Symmetry breaking: $\langle 0|\phi|0\rangle \neq 0$
- Phase transitions $\rightarrow$ topological defects
- Grand Unification Transition: $t = 10^{-43} \rightarrow 10^{-35}$s at $T = 10^{15} GeV \Rightarrow$ Kibble Mechanism
- Causality $\Rightarrow$ Strings exist at all times on super-Hubble scales (given symmetry breaking)
- $\pi_1(\mathcal{M}) \neq 0$



(DAMTP's webpage)

Scaling Solution for String Network

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Scaling Solution for String Network

- Order of 1 infinite string segment per Hubble volume

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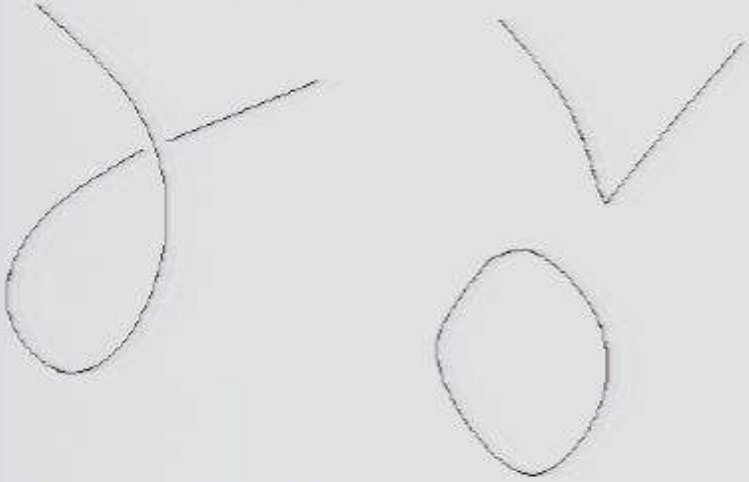
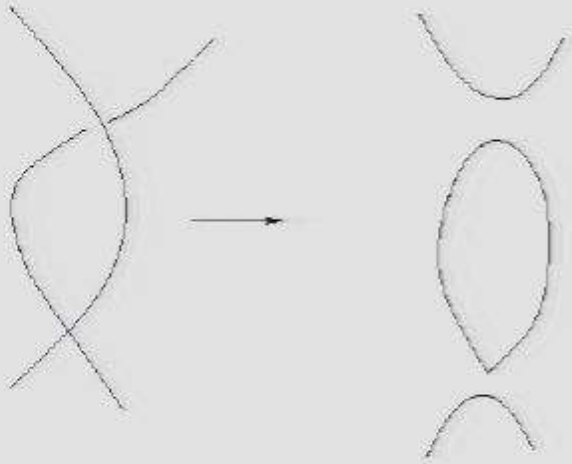
Scaling Solution for String Network

- Order of 1 infinite string segment per Hubble volume
- Loops from interactions/collisions



A string self-intersecting



A string collision

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- Order of 1 infinite string segment per Hubble volume
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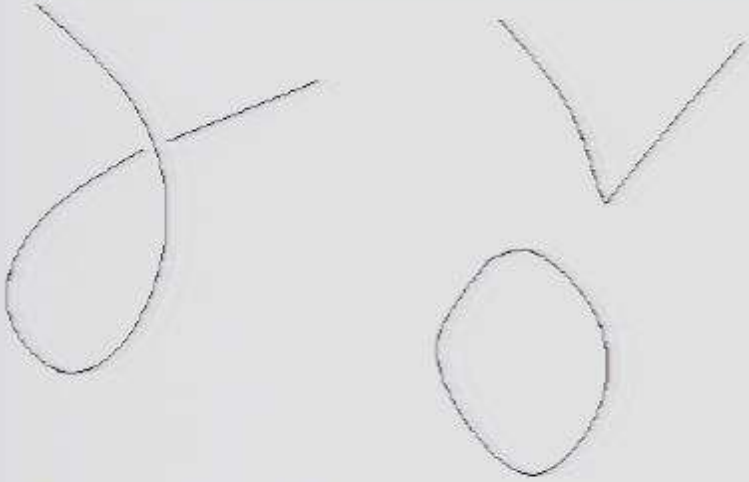

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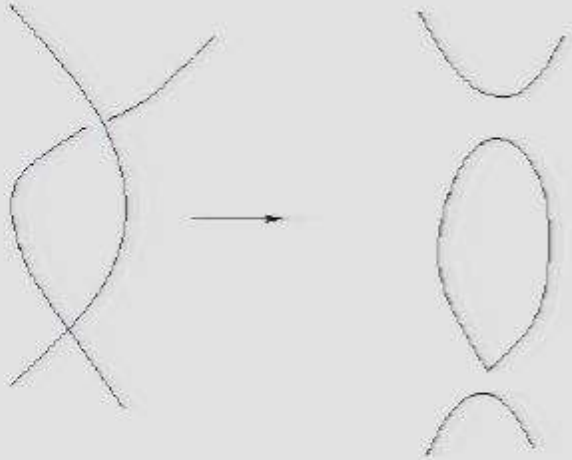

A string collision

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Why might cosmic strings be present?

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Why might cosmic strings be present?

Predictions of strings:

- Brane inflation models

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Why might cosmic strings be present?

Predictions of strings:

- Brane inflation models
- Many supergravity inflation models

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Why might cosmic strings be present?

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Some References

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Why might cosmic strings be present?

Predictions of strings:

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Some References

- Viability of Cosmic F- and D- Strings
  - Polchinski, hep-th/0412244
  - Copeland, Myers, Polchinski, hep-th/031206

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Why might cosmic strings be present?

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  - Cline, hep-th/0501179
  - Sarangi and Tye, hep-th/0204074

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Why might cosmic strings be present?

Predictions of strings:

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- Supergravity inflation models
  - Jeannerot hep-ph/9509365

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What are the current bounds on cosmic strings?

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What are the current bounds on cosmic strings?

$G\mu < 10^{-5}$

- WMAP: Matched filtering method

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What are the current bounds on cosmic strings?

$G\mu < 10^{-5}$

- WMAP: Matched filtering method

$G\mu < 10^{-6}$

- WMAP: New statistics
  - Decomposition of temperature map

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What are the current bounds on cosmic strings?

$G\mu < 10^{-5}$

- WMAP: Matched filtering method

$G\mu < 10^{-6}$

- WMAP: New statistics
  - Decomposition of temperature map

$G\mu < 10^{-7}$

- Acoustic peak structure observations

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What are the current bounds on cosmic strings?

$G\mu < 10^{-5}$

- WMAP: Matched filtering method

$G\mu < 10^{-6}$

- WMAP: New statistics
  - Decomposition of temperature map

$G\mu < 10^{-7}$

- Acoustic peak structure observations

$G\mu < 10^{-8}$ and $G\mu < 10^{-5.5}$

- Pulsar timing measurements
  (Dependent on arguable assumptions of properties of cosmic string loop distributions$\Rightarrow$ Not robust)

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Why are current bounds not optimal?

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Why are current bounds not optimal?

Current bounds:

- Not based on string-specific signatures.

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Why are current bounds not optimal?

Current bounds:

- Not based on string-specific signatures.
- Based on quantities such as CMB power spectrum

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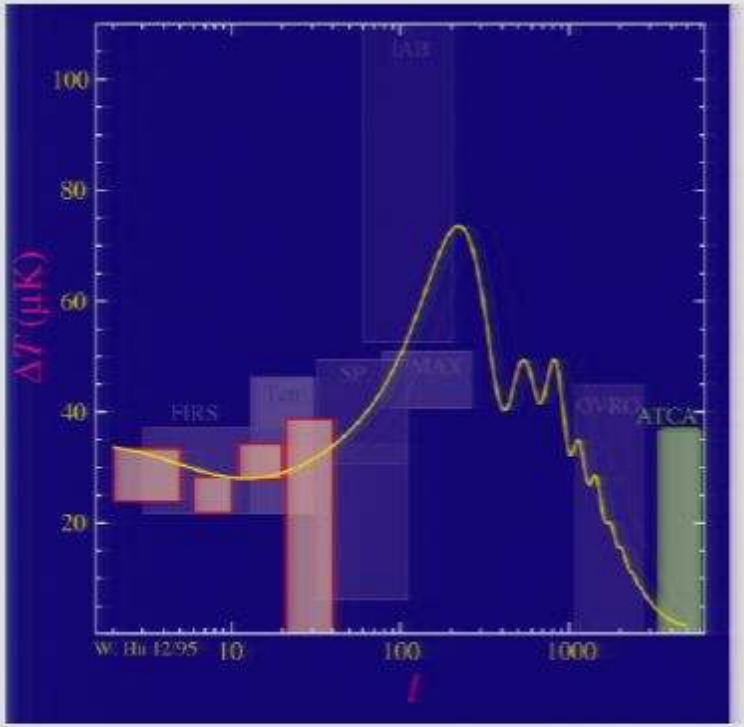
Why are current bounds not optimal?

Current bounds:

- Not based on string-specific signatures.
- Based on quantities such as CMB power spectrum
  - $\Rightarrow$ string specific features are smeared out



(MAP Year 1: Wayne Hu's webpage)

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Cosmic String Signatures

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Cosmic String Signatures

Cosmic String Gravity

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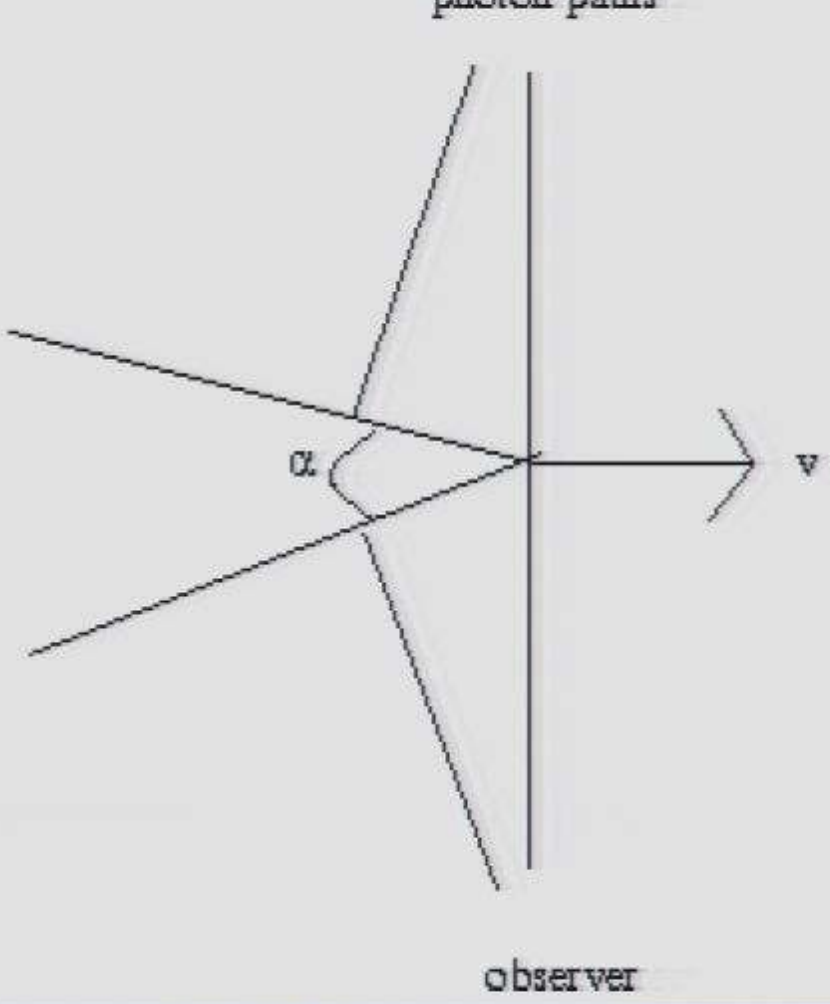
Cosmic String Signatures

Cosmic String Gravity

Gravitational Lensing & Doppler Shift



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Kaiser Stebbins Effect:

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Kaiser Stebbins Effect:
Gravitational Lensing & Doppler Effect:

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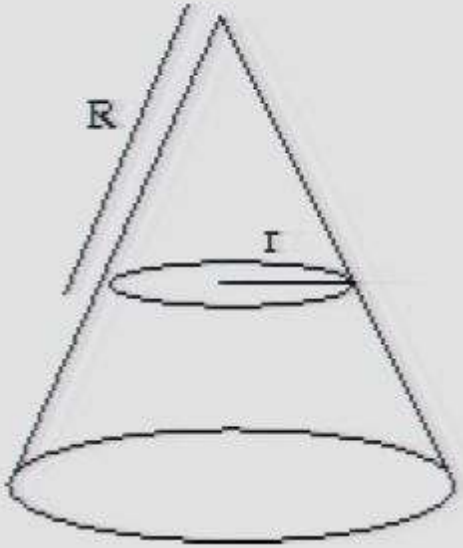
Kaiser Stebbins Effect:
Gravitational Lensing & Doppler Effect:



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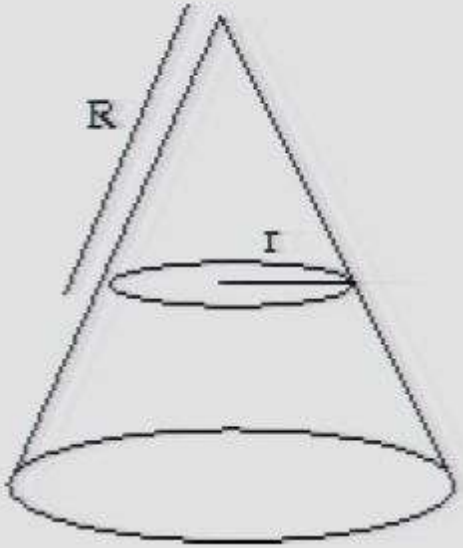
Kaiser Stebbins Effect:
Gravitational Lensing & Doppler Effect:



- Deficit angle: $\alpha = \frac{2\pi R - 2\pi r}{R} = 8\pi G\mu$

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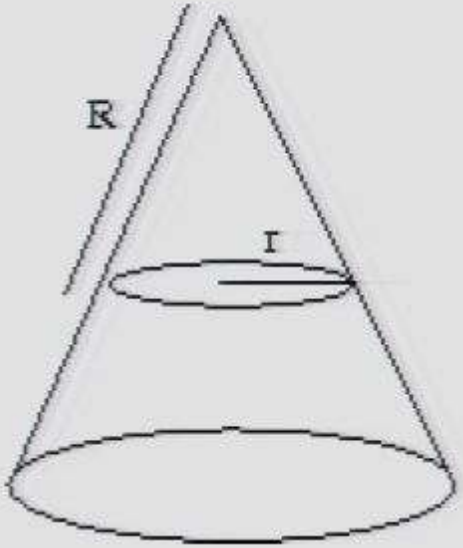
Kaiser Stebbins Effect:

Gravitational Lensing & Doppler Effect:



- Deficit angle: $\alpha = \frac{2\pi R - 2\pi r}{R} = 8\pi G\mu$
- Doppler shift: $\frac{\delta T}{T} = 8\pi\gamma(v)vG\mu$

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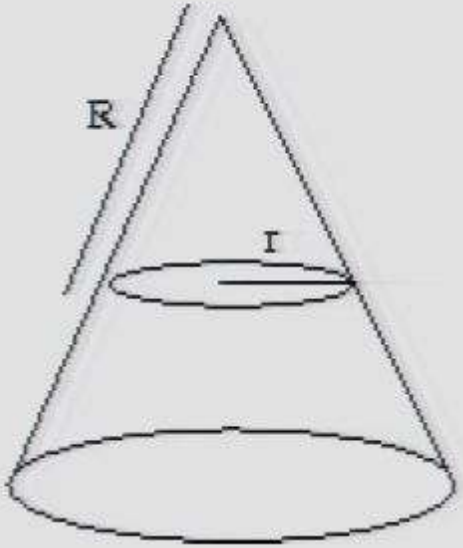
Kaiser Stebbins Effect:

Gravitational Lensing & Doppler Effect:



- Deficit angle: $\alpha = \frac{2\pi R - 2\pi r}{R} = 8\pi G\mu$
- Doppler shift: $\frac{\delta T}{T} = 8\pi\gamma(v)vG\mu$
- Scale invariant spectrum of cosmological perturbations

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What is the Canny algorithm?

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What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map

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What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map
- Maximum gradient perpendicular to edge

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What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map
- Maximum gradient perpendicular to edge

Why is the Canny algorithm ideal to detect cosmic strings?

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What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map
- Maximum gradient perpendicular to edge

Why is the Canny algorithm ideal to detect cosmic strings?

- Canny algorithm finds line discontinuities and produces a map of the edges.

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What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map
- Maximum gradient perpendicular to edge

Why is the Canny algorithm ideal to detect cosmic strings?

- Canny algorithm finds line discontinuities and produces a map of the edges.
- Because of the Kaiser-Stebbins effect, strings produce line discontinuities.

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Overview

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Overview

- Simulate a Gaussian Temperature Map using CAMB

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Overview

- Simulate a Gaussian Temperature Map using CAMB
- Simulate cosmic strings as straight line segments

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Overview

- Simulate a Gaussian Temperature Map using CAMB
- Simulate cosmic strings as straight line segments
- Edge search: Find segments of maximum gradients in simulated maps

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Overview

- Simulate a Gaussian Temperature Map using CAMB
- Simulate cosmic strings as straight line segments
- Edge search: Find segments of maximum gradients in simulated maps
- Compare edge lengths in simulated maps

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Simulators

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Simulators

Gaussian Map Simulator

Assumption: Flat Sky Approximation

$$\frac{\Delta T}{T} = \sum_{l,m} a_{lm} Y_{lm}$$

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Simulators

Gaussian Map Simulator

Assumption: Flat Sky Approximation

$$\frac{\Delta T}{T} = \sum_{l,m} a_{lm} Y_{lm}$$

$$\frac{\Delta T}{T} = \sum_{k} T(\boldsymbol{k}) e^{i\boldsymbol{k}\cdot\boldsymbol{x}}$$

$$\langle T(\boldsymbol{k})^2 \rangle = \langle a_{lm}^2 \rangle = C_{l(k)}$$

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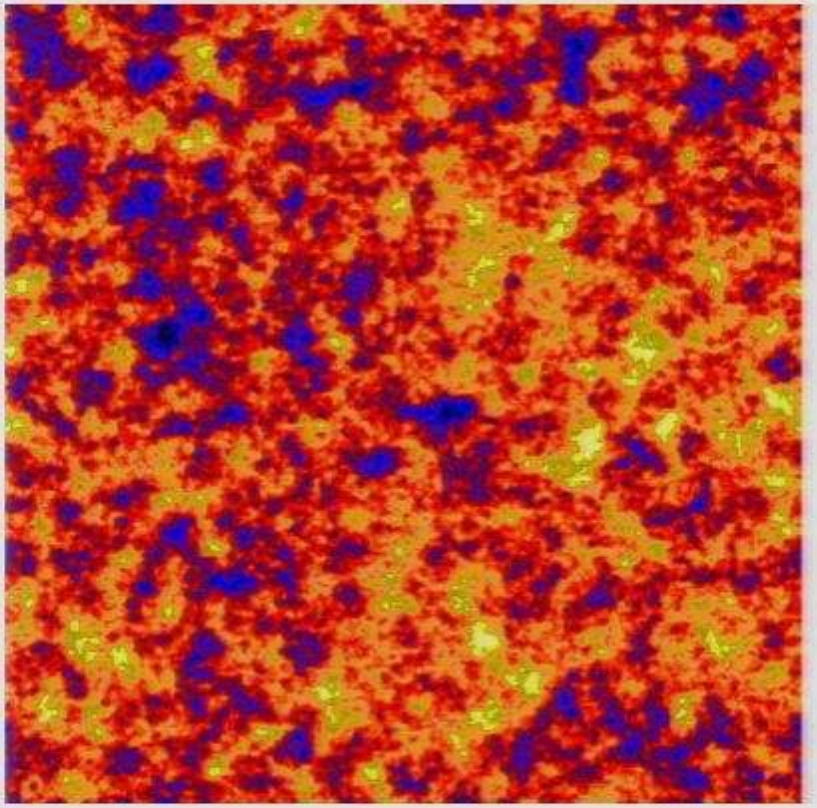
Gaussian Temperature Map Simulation



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Cosmic String Simulator

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Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)

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Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB

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Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB
- Consider time intervals from $t_{rec} \rightarrow t_0$

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Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB
- Consider time intervals from $t_{rec} \rightarrow t_0$
- Project all strings in one Hubble time to the center of one time step's Hubble time

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Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB
- Consider time intervals from $t_{rec} \rightarrow t_0$
- Project all strings in one Hubble time to the center of one time step's Hubble time
- Simulate strings via KS effect on surface of each time interval

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Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB
- Consider time intervals from $t_{rec} \rightarrow t_0$
- Project all strings in one Hubble time to the center of one time step's Hubble time
- Simulate strings via KS effect on surface of each time interval
- Superimpose simulated surfaces

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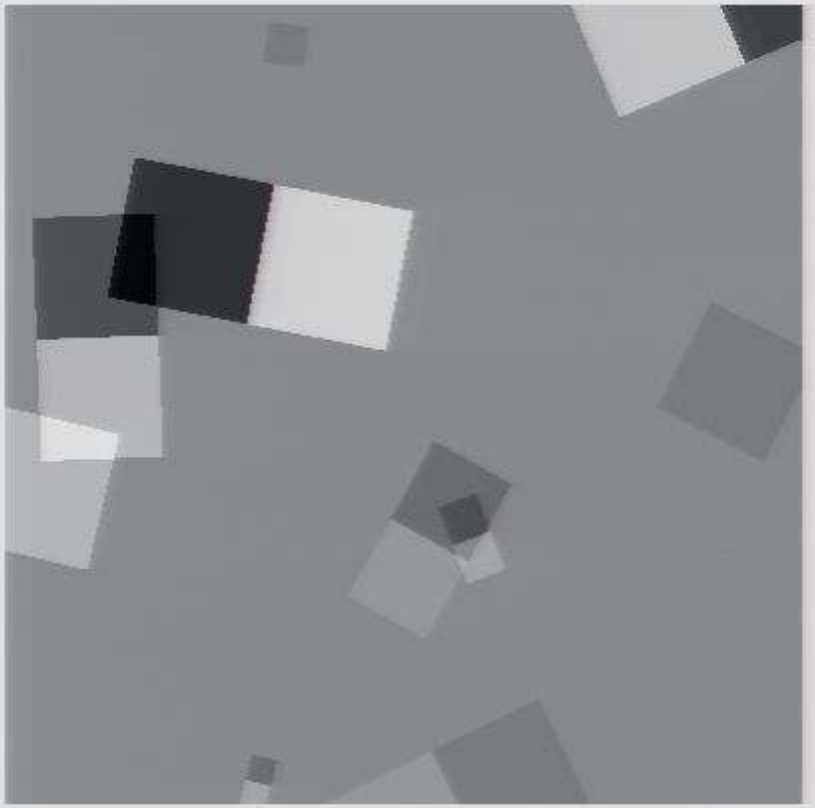
A Few Strings



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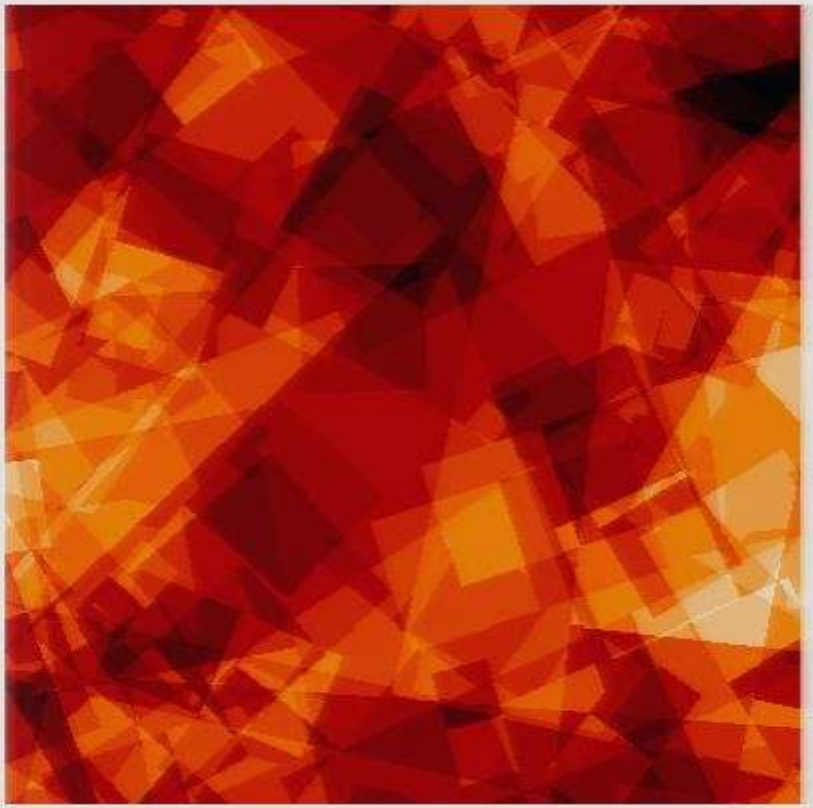
Full simulation for N=1



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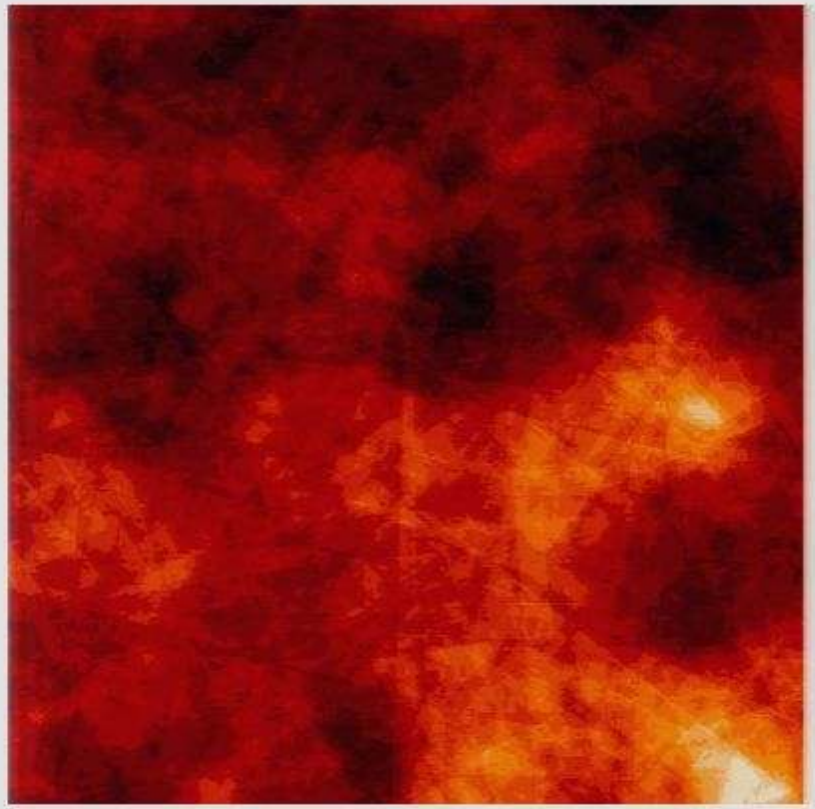
Full simulation for N=10



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Canny algorithm

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Canny algorithm

- Smooth Map: Eliminate point source noise

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Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient

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Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients

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Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima

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Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima
- Assign grid points:
  - Greater than an upper threshold as 1

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Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima
- Assign grid points:
  - Greater than an upper threshold as 1
  - Between lower and the upper thresholds 1/2

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Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima
- Assign grid points:
  - Greater than an upper threshold as 1
  - Between lower and the upper thresholds 1/2
- Turn grid points marked as 1/2 into 1 if criteria are met

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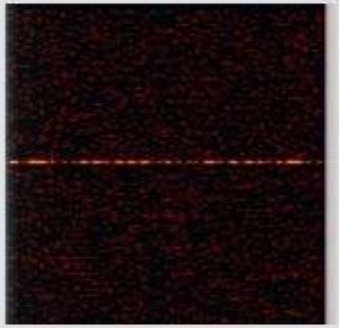
Test Results

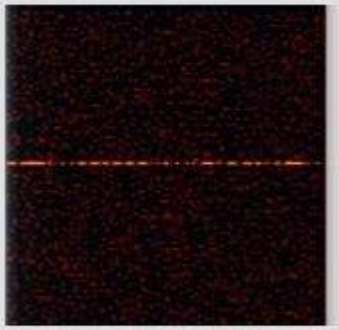
Tests on a single string

Temp. Map

Points marked as 1 and 1/2



New pts marked as 1



Edge map

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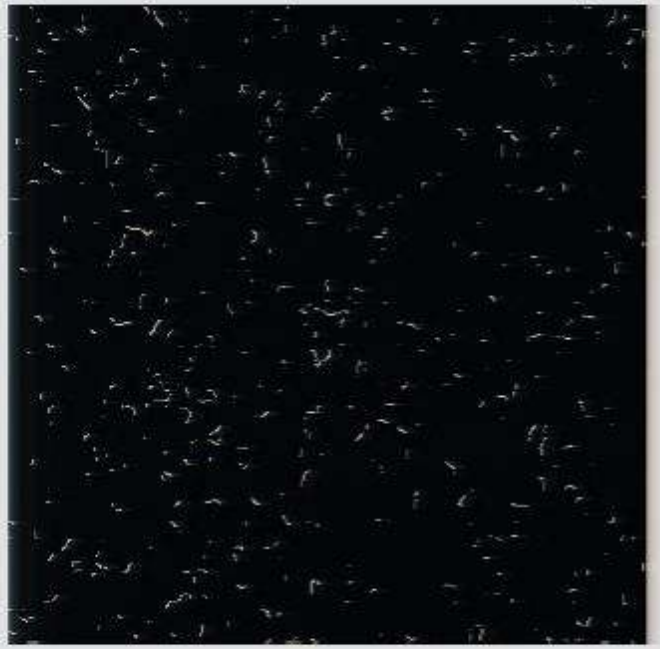
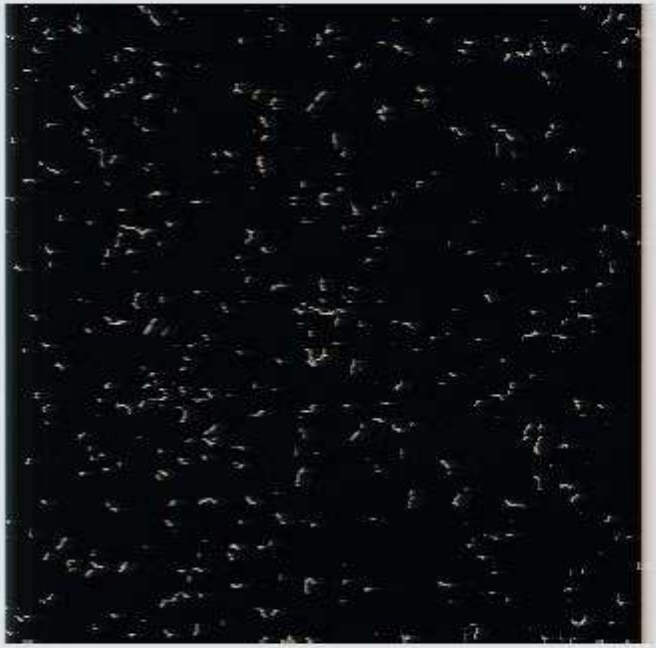
Gaussian Map

Point Marked as 1



Edges



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String Simulated Map N=1

Points Marked as 1

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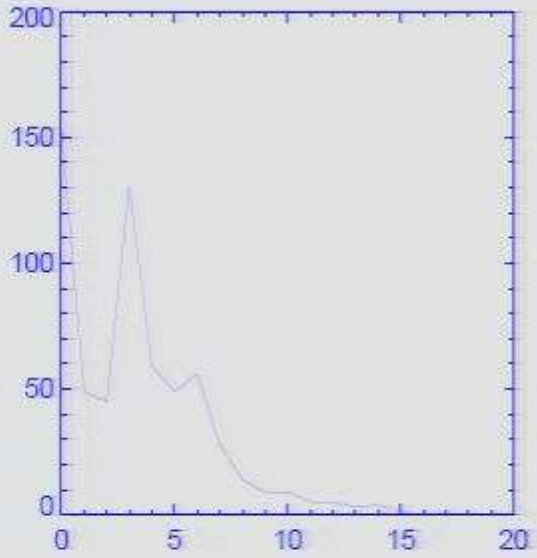
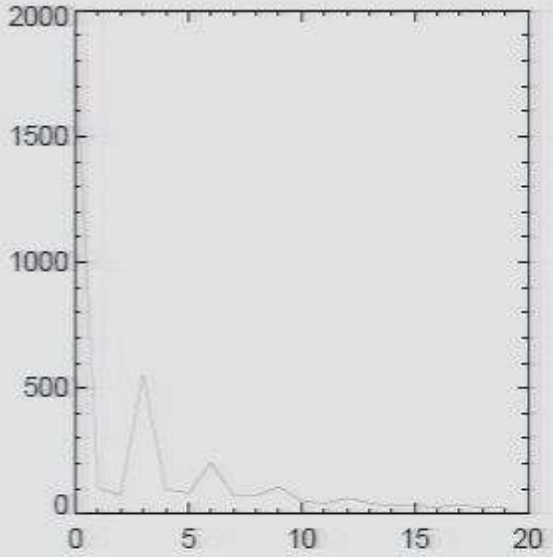
Edge Length Histograms

Number of edges versus edgelength

Gaussian Edge Lengths



String Simulated Map Edge Lengths



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- Cosmic strings produce discontinuities, edges, in CMB

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Conclusions

- Cosmic strings produce discontinuities, edges, in CMB
- Canny algorithm finds longer edges for cosmic strings than the purely inflationary perturbation temperature map