

Title: Detecting Cosmic Strings in the CMB

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URL: <http://pirsa.org/08060116>

Abstract: We further advance the application of the Canny algorithm for detecting cosmic strings in CMB maps.

# Detecting Cosmic Strings in the CMB

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McGill University

Collaborator: Robert Brandenberger

Starting point: Amsel, Berger, and Brandenberger (2007)

June 3, 2008 PASCOS

- 1 **Introduction to Cosmic Strings**
  - What are cosmic strings? How are they formed?
  - Why might cosmic strings be present?
  - What are the current bounds on cosmic strings?
  - Why are current bounds not optimal?

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  - Cosmic String Gravity
  - Cosmic String Signatures
  - Why is the Canny algorithm ideal to detect cosmic strings?

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  - Overview
  - Simulators
  - Canny Algorithm
  - Test Results

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- 4 Conclusions**

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# Introduction to Cosmic Strings

## What are cosmic strings?

# Introduction to Cosmic Strings

## What are cosmic strings?

- One-dimensional topological defects



# Introduction to Cosmic Strings

## What are cosmic strings?

- One-dimensional topological defects
- Very massive
- Very thin,

# Introduction to Cosmic Strings

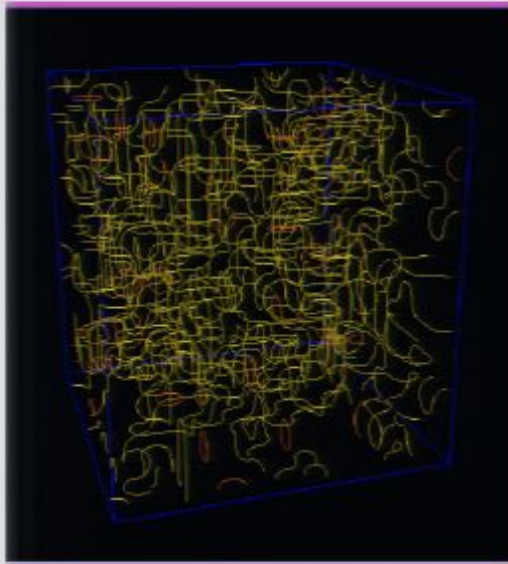
## What are cosmic strings?

- One-dimensional topological defects
- Very massive
- Very thin, Very long (infinite) or Loops

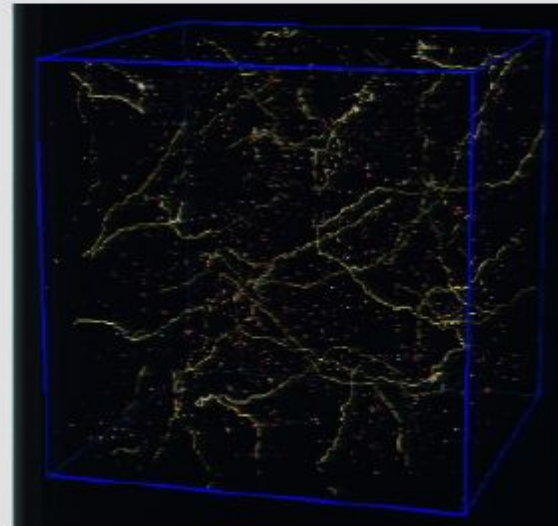
# Introduction to Cosmic Strings

## What are cosmic strings?

- One-dimensional topological defects
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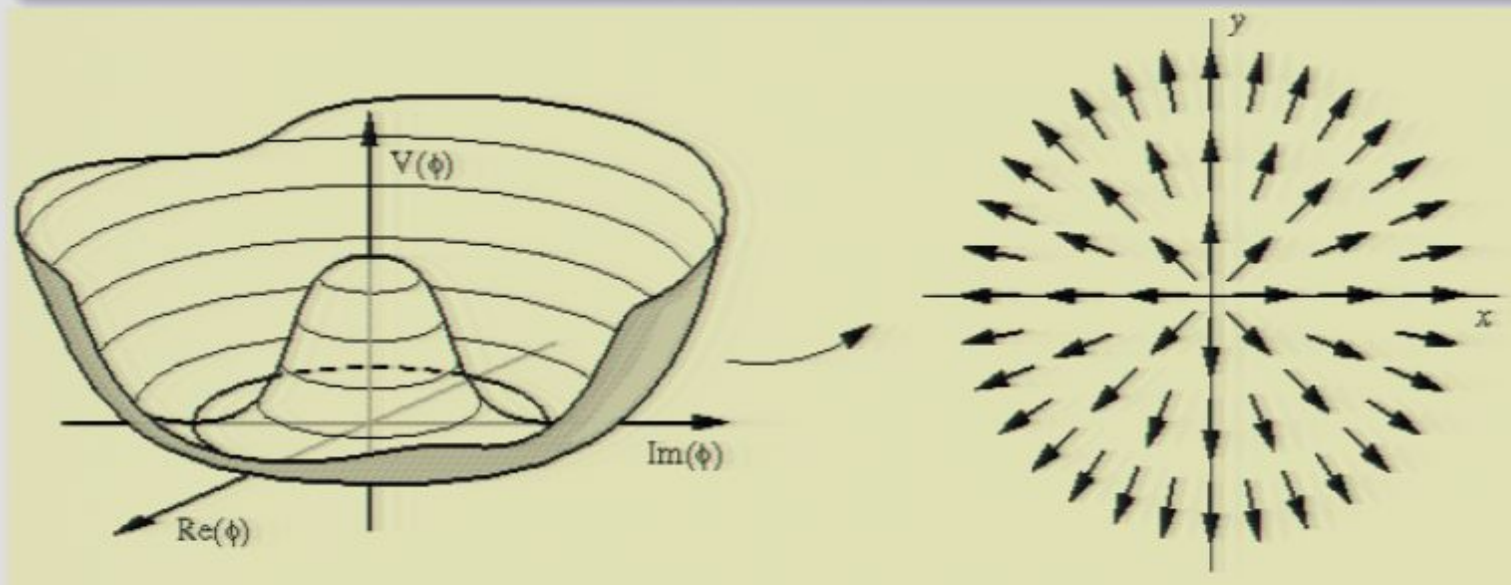
C. Martins & E. P. Shellard: Initial cosmic string network simulation



B. Allen & E. P. Shellard: Late time simulation of cosmic strings

## How are cosmic strings formed?

- Spontaneous Symmetry breaking:  $\langle 0|\phi|0\rangle \neq 0$
- Phase transitions  $\rightarrow$  topological defects
- Grand Unification Transition:  $t = 10^{-43} \rightarrow 10^{-35}$ s at  $T = 10^{15}$  GeV  $\Rightarrow$  Kibble Mechanism
- Causality  $\Rightarrow$  Strings exist at all times on super-Hubble scales (given symmetry breaking)
- $\pi_1(\mathcal{M}) \neq 0$



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# Scaling Solution for String Network

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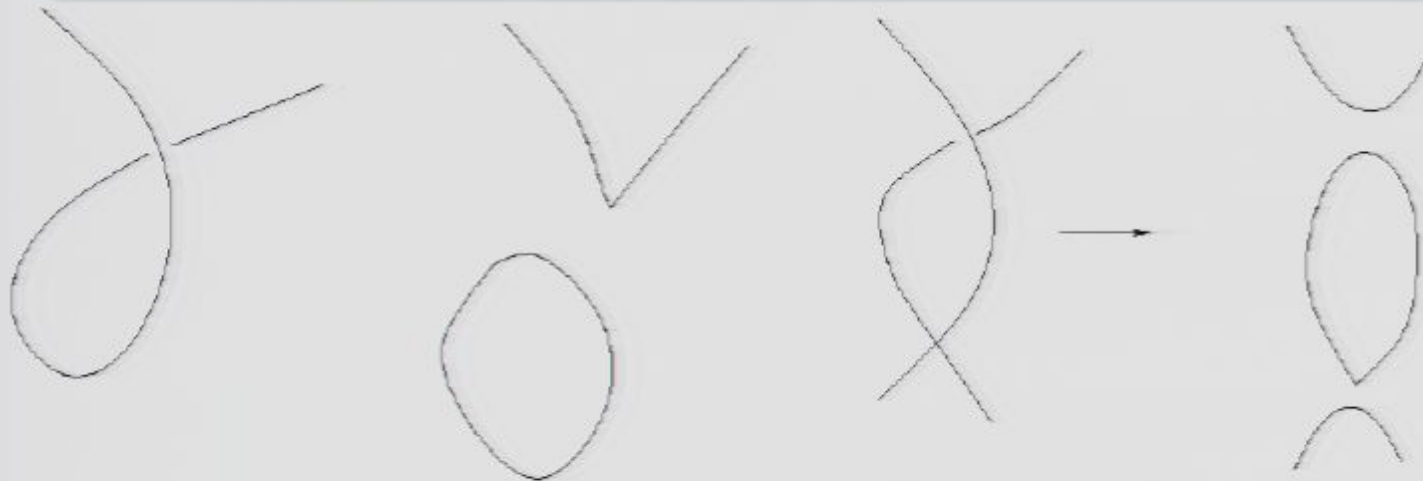
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## Scaling Solution for String Network

- Order of 1 infinite string segment per Hubble volume

## Scaling Solution for String Network

- Order of 1 infinite string segment per Hubble volume
- Loops from interactions/collisions

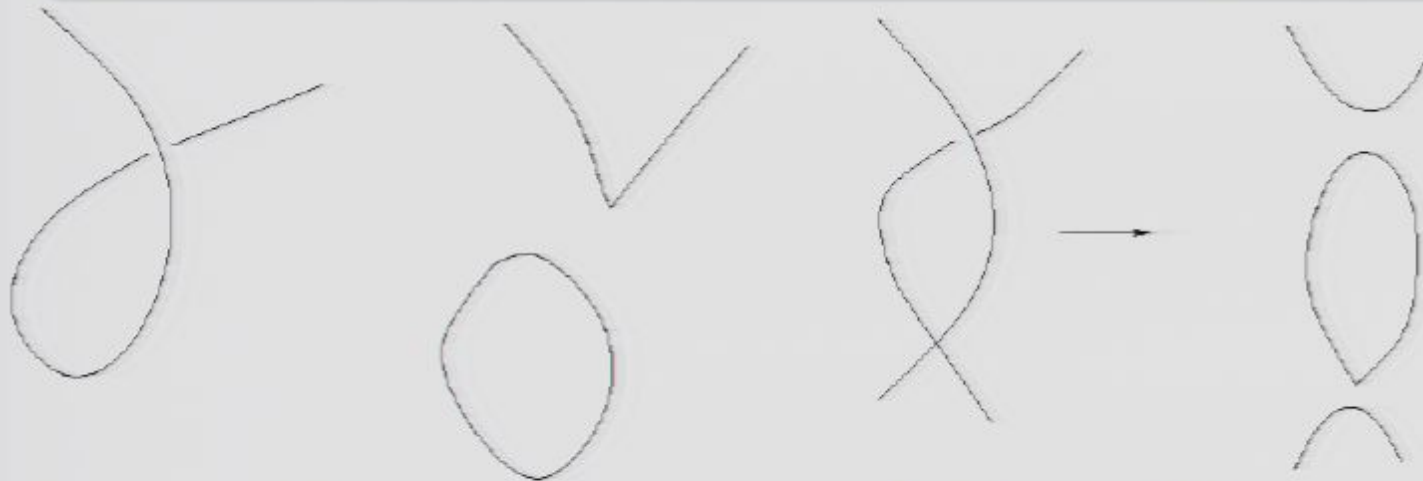


A string self-intersecting

A string collision

## Scaling Solution for String Network

- Order of 1 infinite string segment per Hubble volume
- Loops from interactions/collisions



A string self-intersecting

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# Why might cosmic strings be present?

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## Why might cosmic strings be present?

Predictions of strings:

- Brane inflation models

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## Why might cosmic strings be present?

Predictions of strings:

- Brane inflation models
- Many supergravity inflation models

## Why might cosmic strings be present?

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## Some References

## Why might cosmic strings be present?

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## Some References

- Viability of Cosmic F- and D- Strings
  - Polchinski, hep-th/0412244
  - Copeland, Myers, Polchinski, hep-th/031206

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# What are the current bounds on cosmic strings?



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# What are the current bounds on cosmic strings?

$$G\mu < 10^{-5}$$

- WMAP: Matched filtering method

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- WMAP: New statistics
  - Decomposition of temperature map

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- Acoustic peak structure observations

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$$G\mu < 10^{-5}$$

- WMAP: Matched filtering method

$$G\mu < 10^{-6}$$

- WMAP: New statistics
  - Decomposition of temperature map

$$G\mu < 10^{-7}$$

- Acoustic peak structure observations

$$G\mu < 10^{-8} \text{ and } G\mu < 10^{-5.5}$$

- Pulsar timing measurements  
(Dependent on arguable assumptions of properties of cosmic string loop distributions  $\Rightarrow$  Not robust)

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# Why are current bounds not optimal?

## Why are current bounds not optimal?

Current bounds:

- Not based on string-specific signatures.

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## Why are current bounds not optimal?

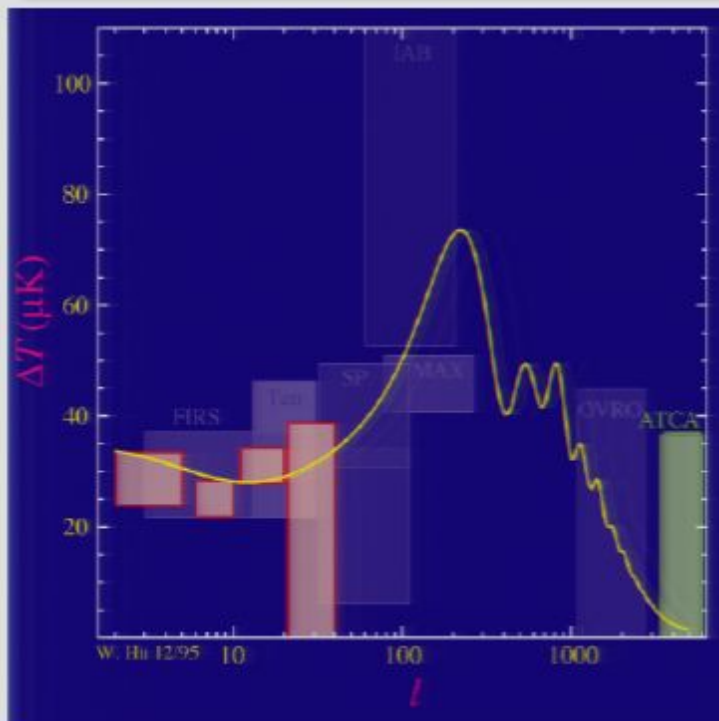
Current bounds:

- Not based on string-specific signatures.
- Based on quantities such as CMB power spectrum

## Why are current bounds not optimal?

Current bounds:

- Not based on string-specific signatures.
- Based on quantities such as CMB power spectrum
  - $\Rightarrow$  string specific features are smeared out



(MAP Year 1: Wayne Hu's webpage)



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# Cosmic String Signatures

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# Cosmic String Signatures

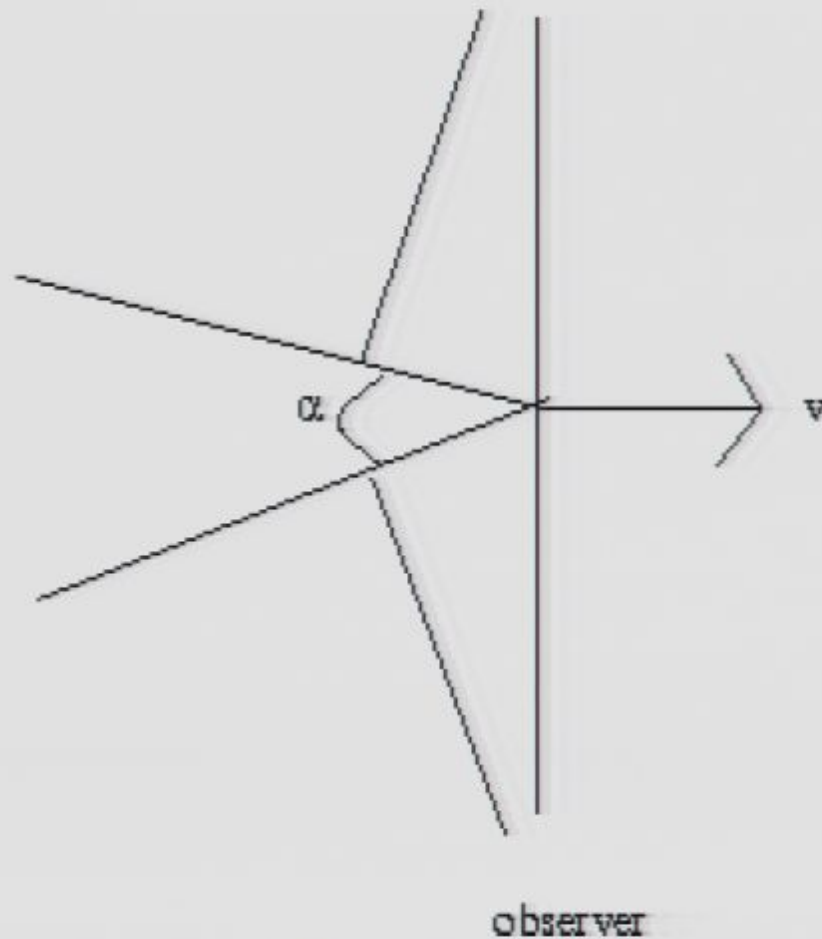
## Cosmic String Gravity

# Cosmic String Signatures

## Cosmic String Gravity

### Gravitational Lensing & Doppler Shift

photon paths



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# Kaiser Stebbins Effect:

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# Kaiser Stebbins Effect: Gravitational Lensing & Doppler Effect:

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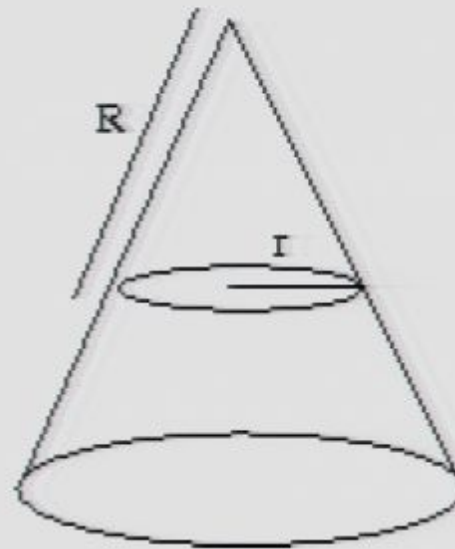
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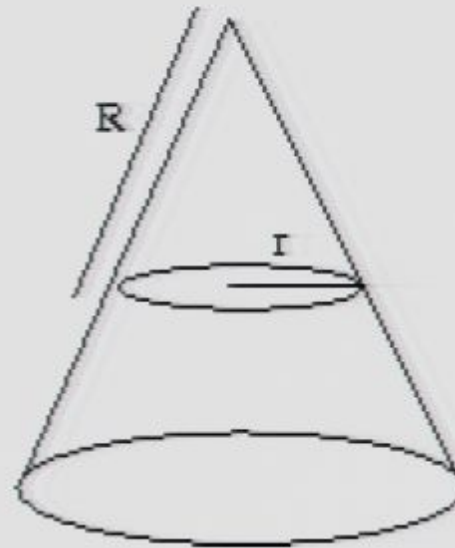
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# Kaiser Stebbins Effect: Gravitational Lensing & Doppler Effect:

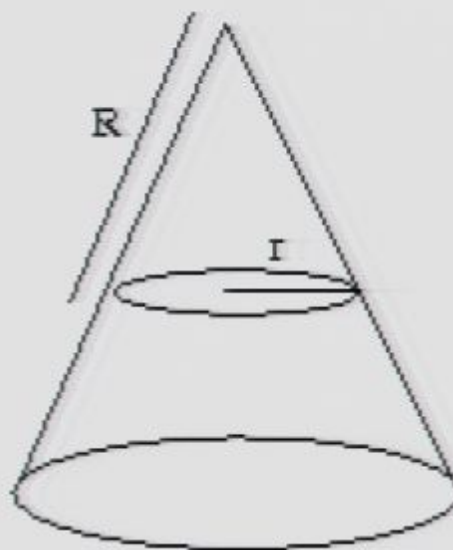


# Kaiser Stebbins Effect: Gravitational Lensing & Doppler Effect:



- Deficit angle:  $\alpha = \frac{2\pi R - 2\pi r}{R} = 8\pi G\mu$

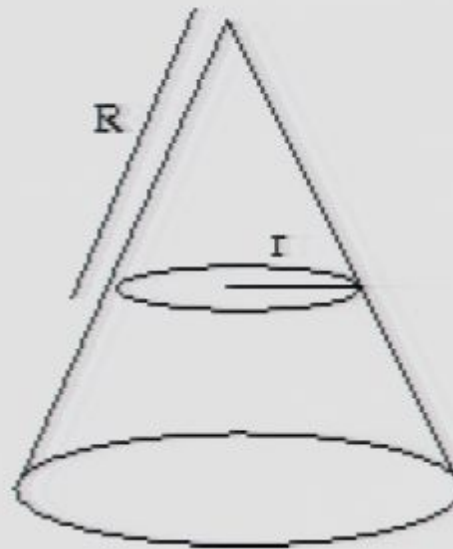
# Kaiser Stebbins Effect: Gravitational Lensing & Doppler Effect:



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- Deficit angle:  $\alpha = \frac{2\pi R - 2\pi r}{R} = 8\pi G\mu$
- Doppler shift:  $\frac{\delta T}{T} = 8\pi\gamma(v)vG\mu$
- Scale invariant spectrum of cosmological perturbations

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# What is the Canny algorithm?

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## What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map

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## What is the Canny algorithm?

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## Why is the Canny algorithm ideal to detect cosmic strings?

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- Method developed in 1986 to map edges in an image map
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## Why is the Canny algorithm ideal to detect cosmic strings?

- Canny algorithm finds line discontinuities and produces a map of the edges.

## What is the Canny algorithm?

- Method developed in 1986 to map edges in an image map
- Maximum gradient perpendicular to edge

## Why is the Canny algorithm ideal to detect cosmic strings?

- Canny algorithm finds line discontinuities and produces a map of the edges.
- Because of the Kaiser-Stebbins effect, strings produce line discontinuities.

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# Numerical Studies



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## Overview

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## Overview

- Simulate a Gaussian Temperature Map using CAMB

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# Numerical Studies

## Overview

- Simulate a Gaussian Temperature Map using CAMB
- Simulate cosmic strings as straight line segments

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# Numerical Studies

## Overview

- Simulate a Gaussian Temperature Map using CAMB
- Simulate cosmic strings as straight line segments
- Edge search: Find segments of maximum gradients in simulated maps

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# Numerical Studies

## Overview

- Simulate a Gaussian Temperature Map using CAMB
- Simulate cosmic strings as straight line segments
- Edge search: Find segments of maximum gradients in simulated maps
- Compare edge lengths in simulated maps

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# Simulators

# Simulators

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## Gaussian Map Simulator

Assumption: Flat Sky Approximation

$$\frac{\Delta T}{T} = \sum_{l,m} a_{lm} Y_{lm}$$

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## Gaussian Map Simulator

Assumption: Flat Sky Approximation

$$\frac{\Delta T}{T} = \sum_{l,m} a_{lm} Y_{lm}$$

$$\frac{\Delta T}{T} = \sum_{\mathbf{k}} T(\mathbf{k}) e^{i\mathbf{k}\cdot\mathbf{x}}$$

$$\langle T(\mathbf{k})^2 \rangle = \langle a_{lm}^2 \rangle = C_{l(k)}$$



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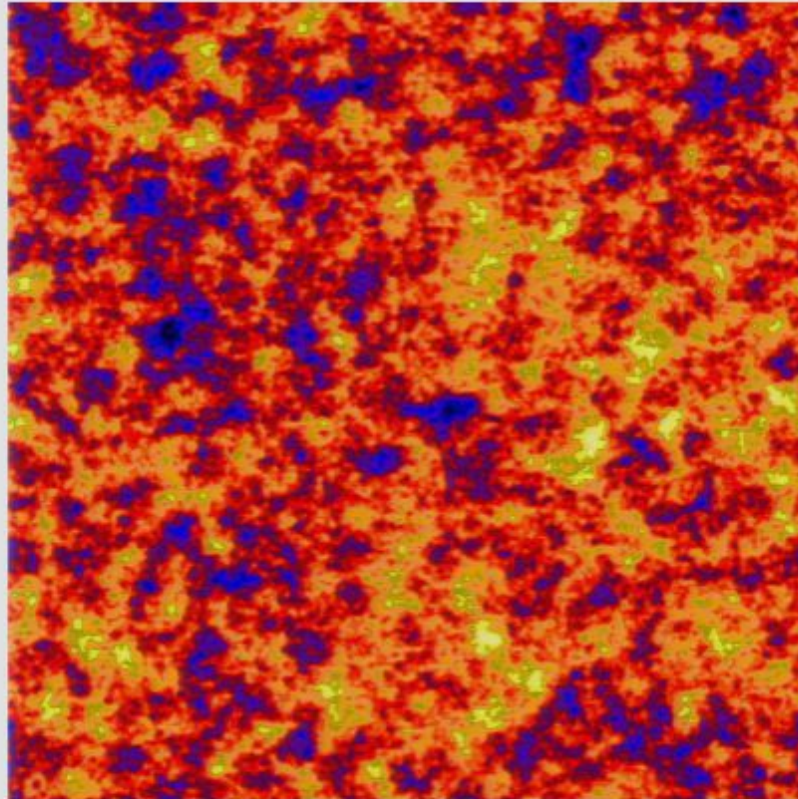
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# Gaussian Temperature Map Simulation



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## Cosmic String Simulator

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## Cosmic String Simulator

- **Simplicity:** Consider straight segments (curvature radius)

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## Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB

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## Cosmic String Simulator

- Simplicity: Consider straight segments (curvature radius)
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- Consider time intervals from  $t_{rec} \rightarrow t_0$

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**Cosmic String Simulator**

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB
- Consider time intervals from  $t_{rec} \rightarrow t_0$
- Project all strings in one Hubble time to the center of one time step's Hubble time

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**Cosmic String Simulator**

- Simplicity: Consider straight segments (curvature radius)
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- Consider time intervals from  $t_{rec} \rightarrow t_0$
- Project all strings in one Hubble time to the center of one time step's Hubble time
- Simulate strings via KS effect on surface of each time interval

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**Cosmic String Simulator**

- Simplicity: Consider straight segments (curvature radius)
- Consider the past light cone of CMB
- Consider time intervals from  $t_{rec} \rightarrow t_0$
- Project all strings in one Hubble time to the center of one time step's Hubble time
- Simulate strings via KS effect on surface of each time interval
- Superimpose simulated surfaces



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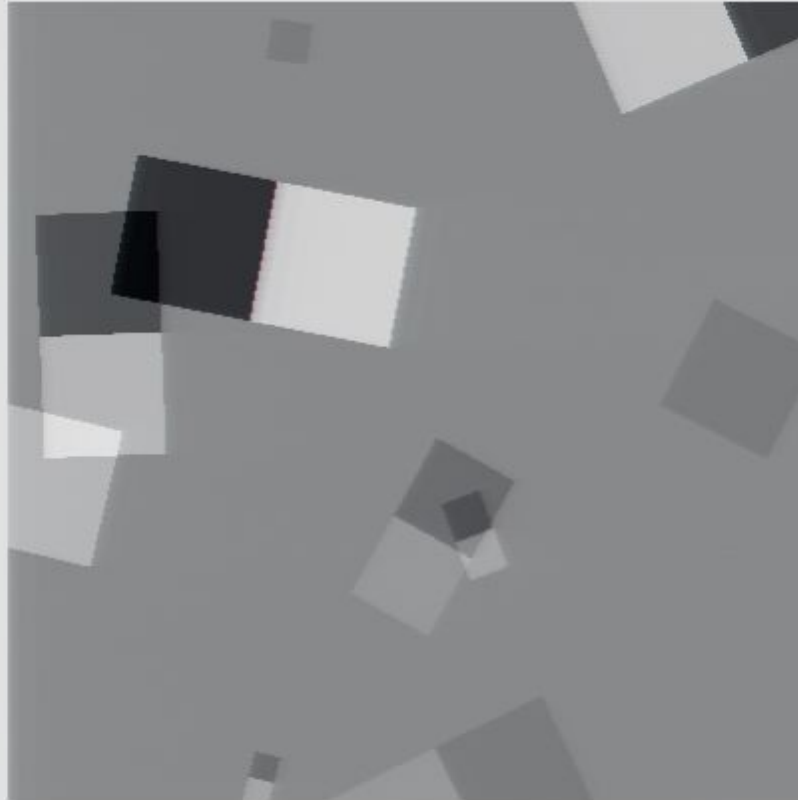
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# A Few Strings



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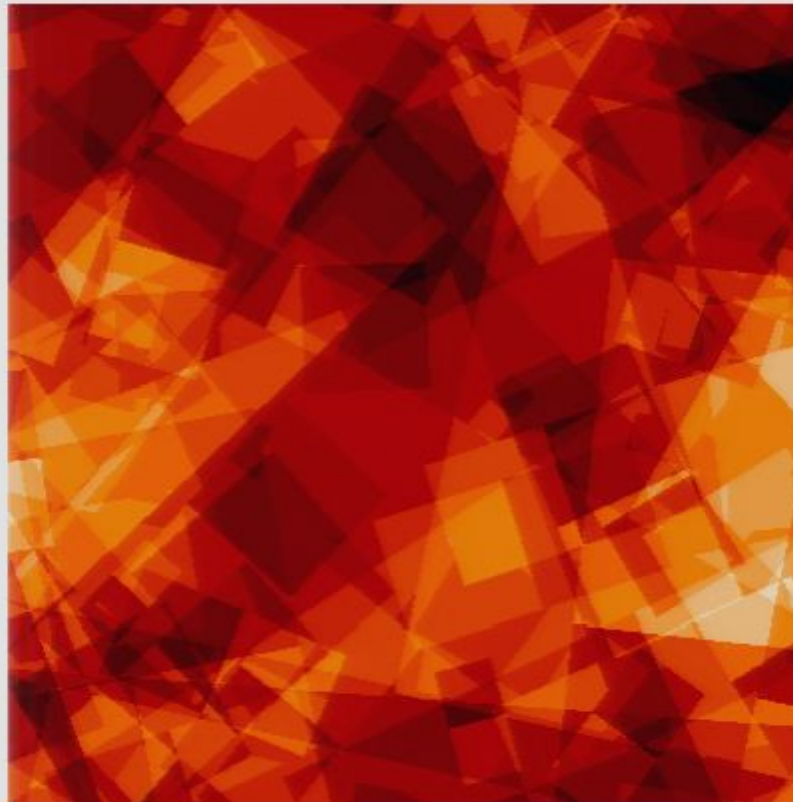
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## Full simulation for $N=1$



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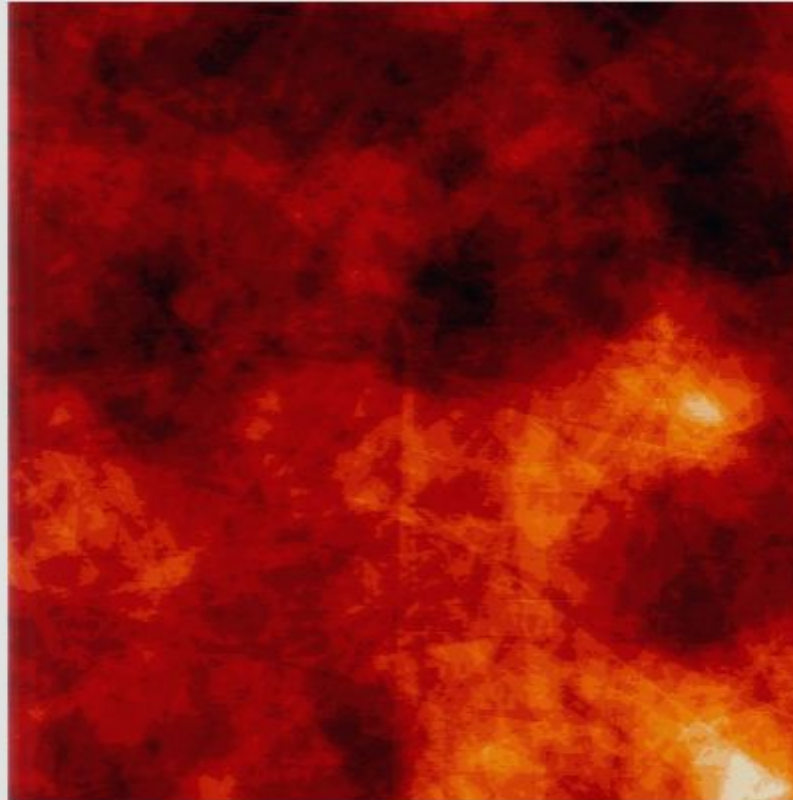
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## Full simulation for $N=10$



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# Canny algorithm

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## Canny algorithm

- Smooth Map: Eliminate point source noise

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## Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient

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## Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients

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## Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima



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## Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima
- Assign grid points:
  - Greater than an upper threshold as 1

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## Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
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- Assign grid points:
  - Greater than an upper threshold as 1
  - Between lower and the upper thresholds  $1/2$

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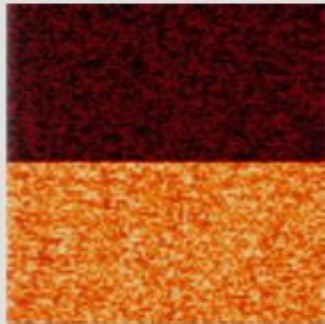
## Canny algorithm

- Smooth Map: Eliminate point source noise
- Find the smoothed map's gradient
- Find local maxima in the gradients
- Sort through local maxima
- Assign grid points:
  - Greater than an upper threshold as 1
  - Between lower and the upper thresholds  $1/2$
- Turn grid points marked as  $1/2$  into 1 if criteria are met

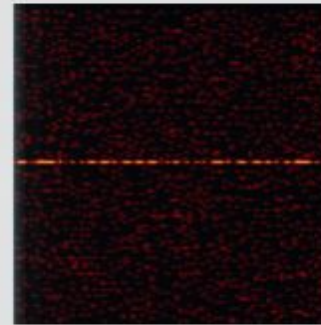
# Test Results

Tests on a single string

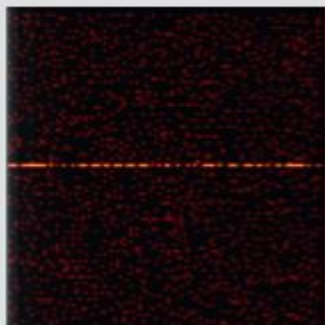
Temp. Map



Points marked as 1 and 1/2



New pts marked as 1



Edge map



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## Gaussian Map

Point Marked as 1

Edges



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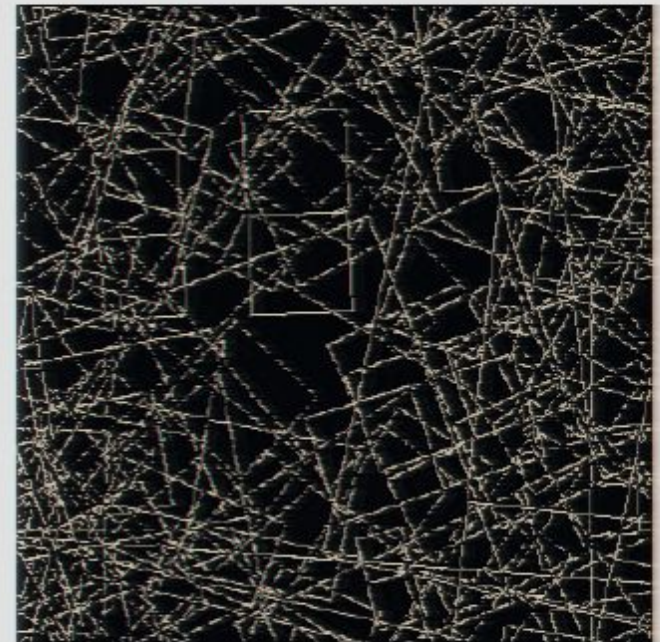
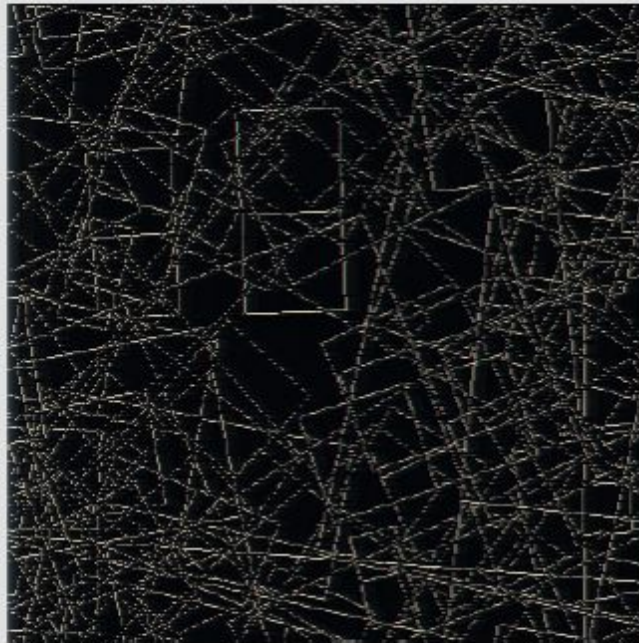
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## String Simulated Map $N=1$

Points Marked as 1

Edges

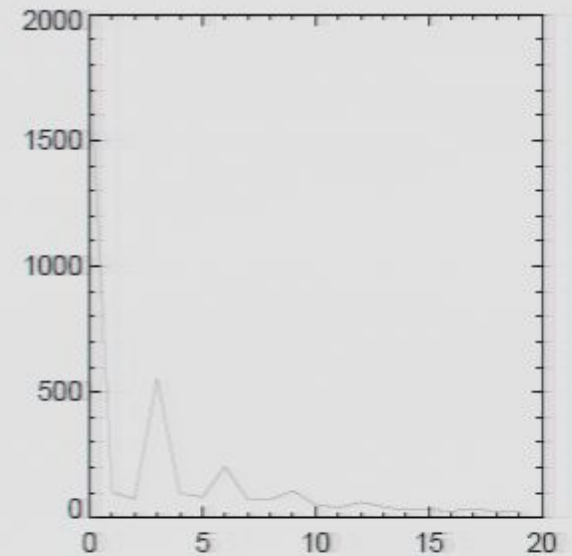
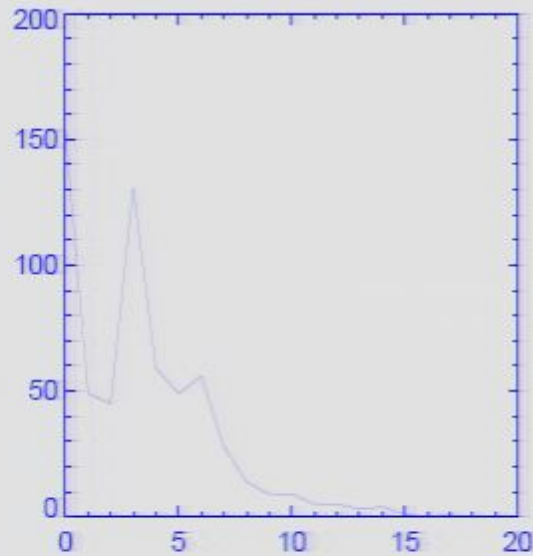


# Edge Length Histograms

Number of edges versus edgelen

Gaussian Edge Lengths

String Simulated Map Edge Lengths



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- Cosmic strings produce discontinuities, edges, in CMB

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## Conclusions

- Cosmic strings produce discontinuities, edges, in CMB
- Canny algorithm finds longer edges for cosmic strings than the purely inflationary perturbation temperature map