

Title: Special Topics in Physics - Lecture 14B

Date: Apr 23, 2008 08:00 PM

URL: <http://pirsa.org/08040064>

Abstract: The Problem of Time in Quantum Gravity and Cosmology

Causets

discreteness: cwe ∞ 's, "explains metric" $(- + + +)$

order + number = geometry

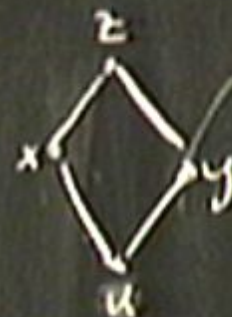
def causet

elt's x, y, \dots

$x < y$ x precedes y
 x ancestor of y



$x < z$
 $y < z$



transitive $x < y < z \Rightarrow x < z$

acyclic $\Leftrightarrow x \not< x$

part-finite each x has finite # of ancestors

$D(A, B)$

\uparrow geometry
 \uparrow causal set

① Recover time (from space) in CQG

② Conceptual problems from diff

What are the "observables" ("beables") ("variables")
covariant meaningful

③ Technical problems from diff (e.g. $\text{vol}(\text{D.C.}) = 0$)

④ Absence of natural Wick rotation?

⑤ Problem of "becoming" (Do things happen?) (no unique slicing)
arrow of time (can QG help?)

What are the "observables" ("beables") ("variables")
covariant meaningful

(3) Technical problems from diff (e.g. $\text{Vol}(D, \mathcal{P}) = 0$)

(4) Absence of natural Wick rotation?

(5) Problem of "becoming" (Do things happen?) (no unique slicing)

(6) Arrow of time (can QG help?)

① Recover time (from space) in CQG

② Conceptual problems from diffeo

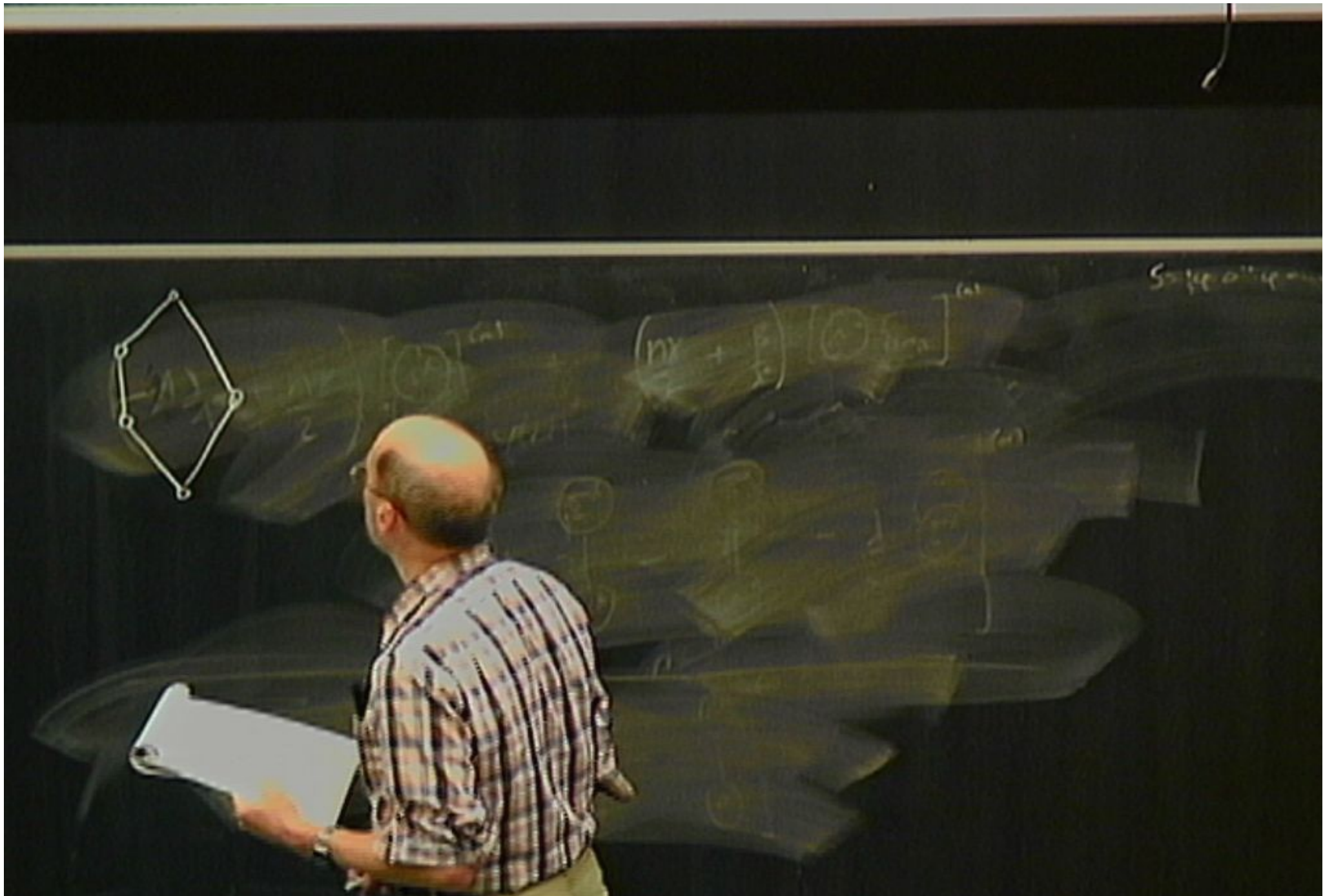
What are the "observables" ("beables") ("Variables")
Covariant meaningful

③ Technical problems from diff (e.g. $\text{vol}(D, \mathcal{R}) = 0$)

④ Absence of natural Wick rotation?

⑤ Problem of "becoming" (Do things happen?) (no unique slicing)

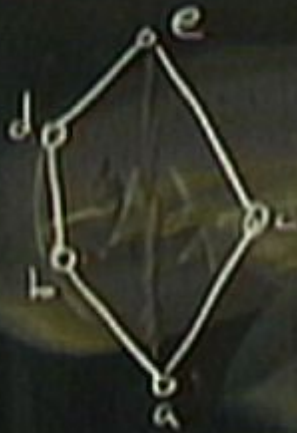
⑥ Arrow of time (can QG help?)



Separating

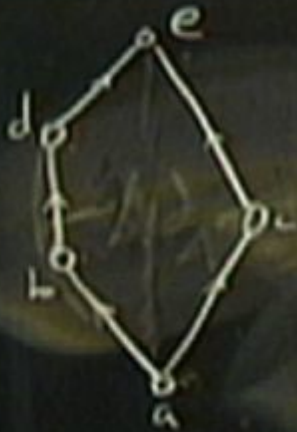


$$\left(\frac{nx}{2} + \frac{E}{2} \right) \left[\frac{2}{n} \sum_{i=1}^n \frac{1}{d_i} \right]$$



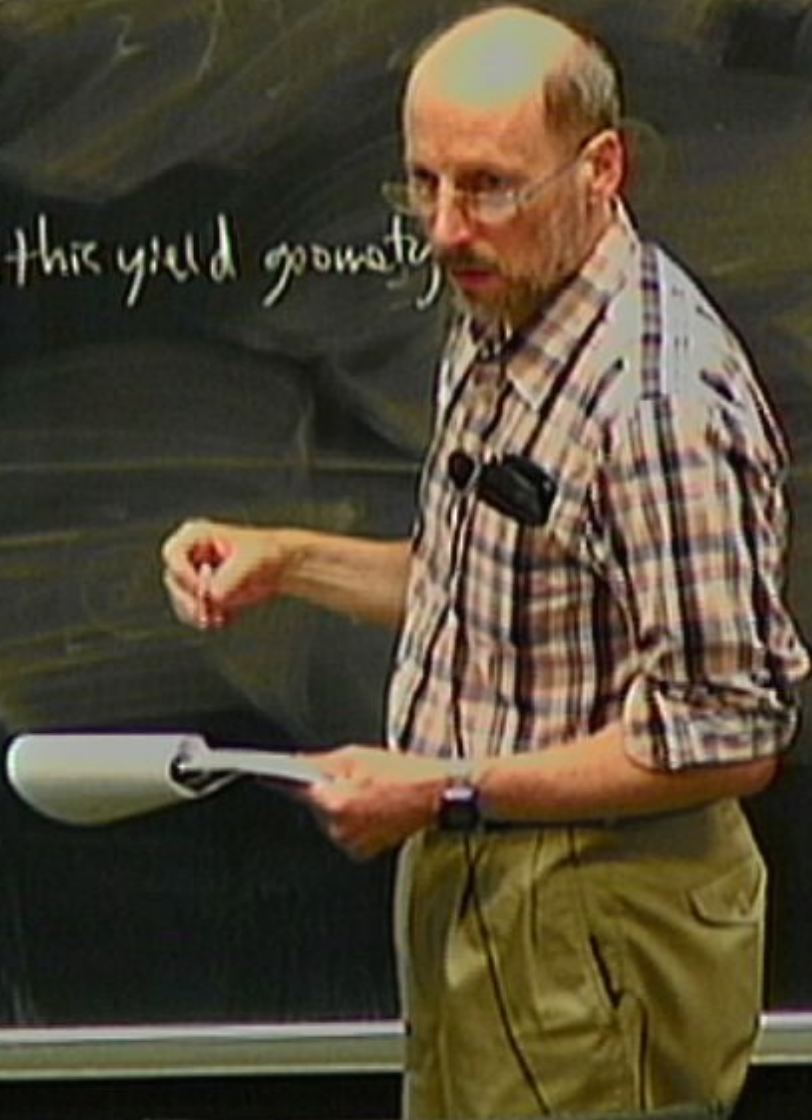
$a < b$ $c < e$
 $a < e$





$$\begin{aligned} a < b & \quad c < e \\ a < e & \end{aligned}$$

How can this yield geometry?





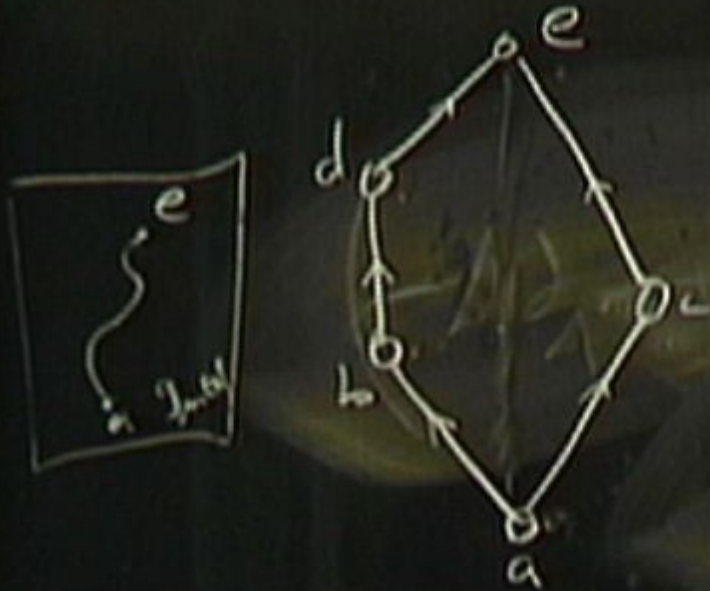
$$\begin{aligned} a < b & \quad c < e \\ a < e \end{aligned}$$

Some other...

$$\left[\frac{ny}{x} + \frac{p}{z} \right] \text{ (unclear)}$$

How can this yield geometry
proper for \leftrightarrow ?

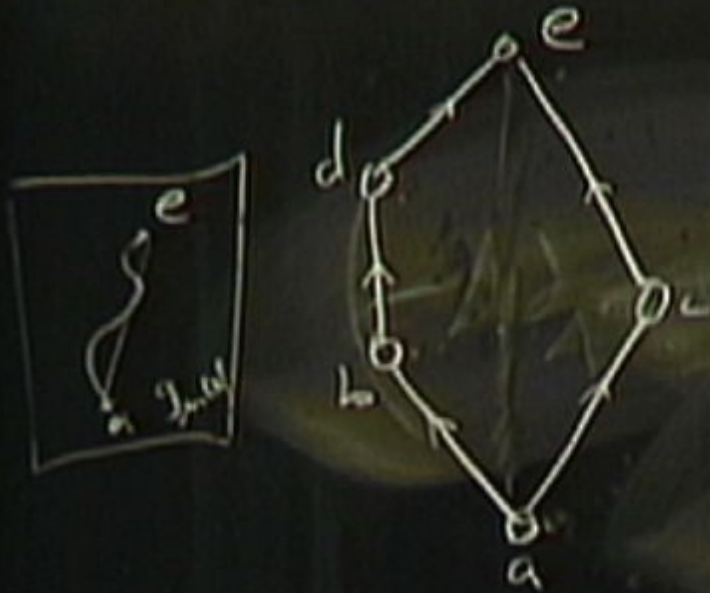




$a < b$ $c < e$
 $a < e$

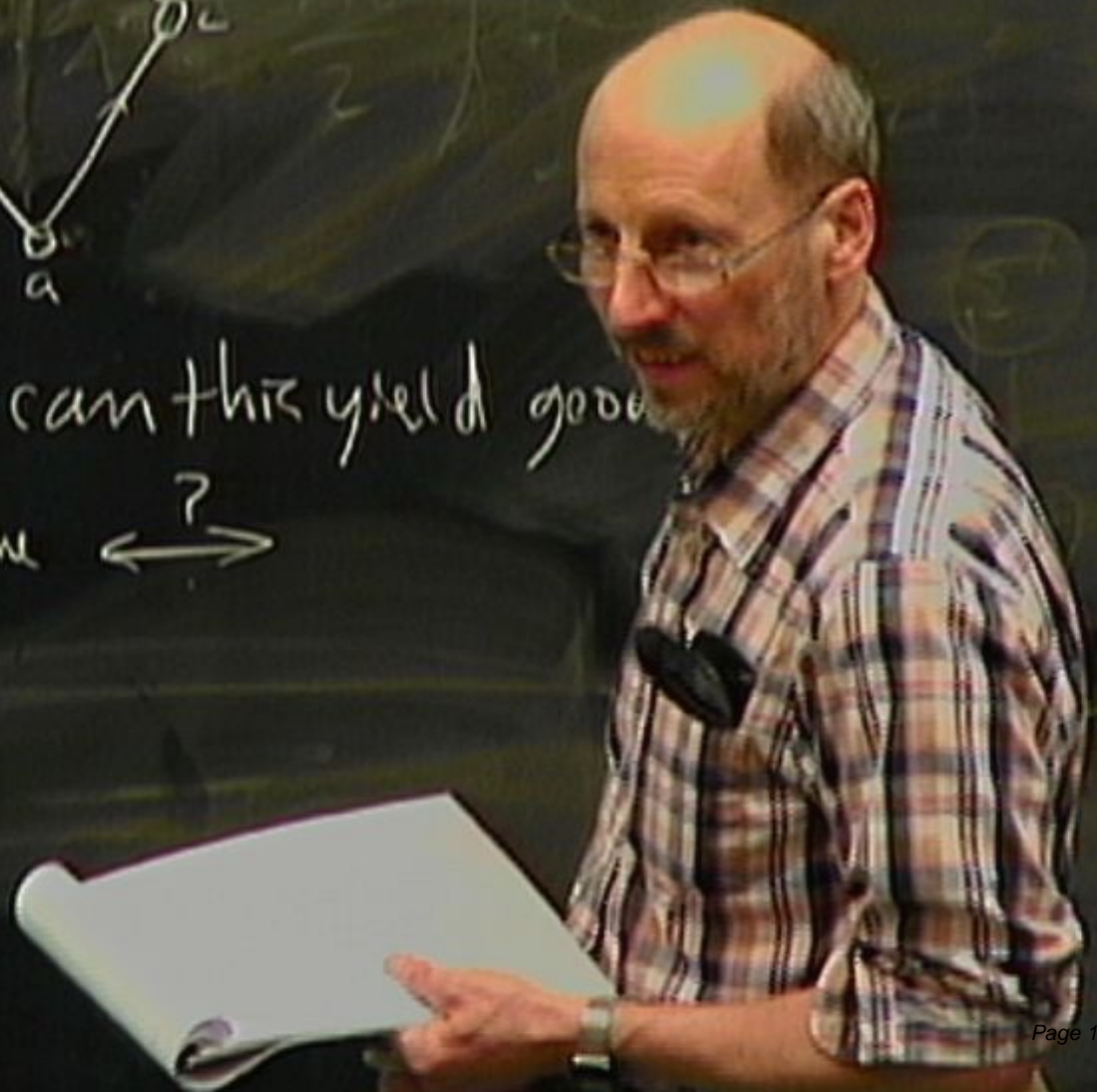
How can this be a total order?

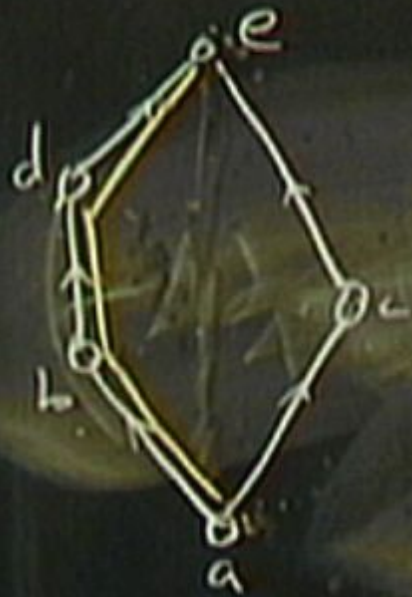
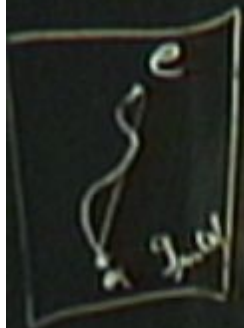
proper time \longleftrightarrow ?



$a < b$ $c < e$
 $a < e$

How can this yield good
 proper time \longleftrightarrow ?



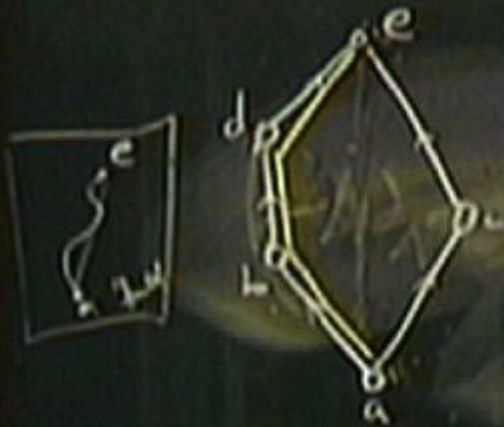


$a < b$ $c < e$
 $a < e$
 10^{240}



How can this yield geometry?

proper time \longleftrightarrow ?



$$(a < b) \quad c < e$$

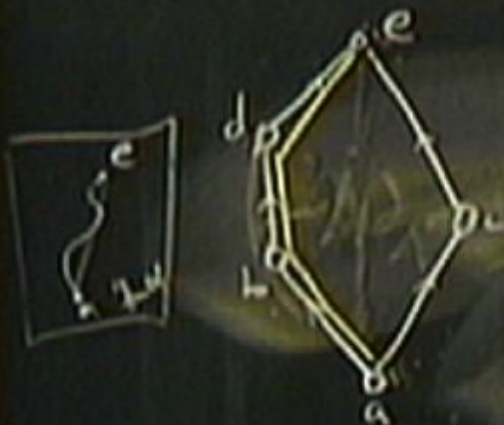
$$a < e$$

$$\approx 10^{240}$$



How can this yield geometry?
 proper time \longleftrightarrow ?





$a < b$ $c < e$
 $a < e$
 10^{240}



$d=1$



$d=2$



How can this yield geometry?
 proper time \leftrightarrow ?



$a < b$ $c < e$
 $a < e$
 10^{240}



$d=1$



$d=2$

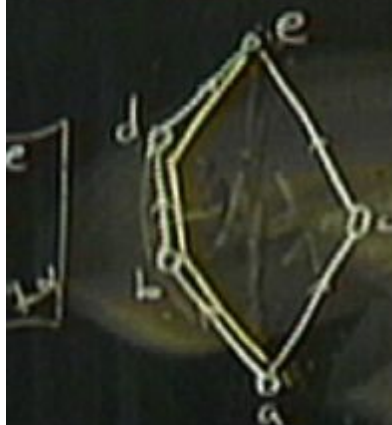


$d=3$

How can this yield geometry?

proper time \longleftrightarrow ?





$a < b$ $c < e$
 $a < e$
 10^{240}



$d=1$



$d=2$



$d=3$

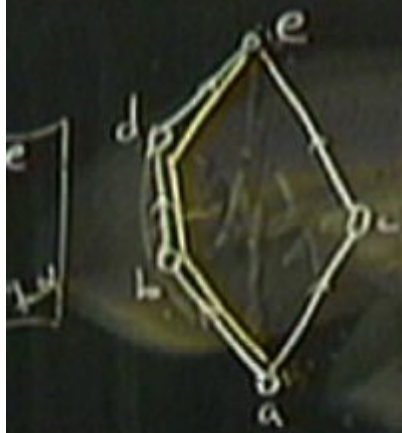
How can this yield geometry?

proper time \longleftrightarrow ?

\mathbb{Z}^2

x'

y'



$a < b$ $c < e$
 $a < e$
 10^{240}



$d=1$



$d=2$



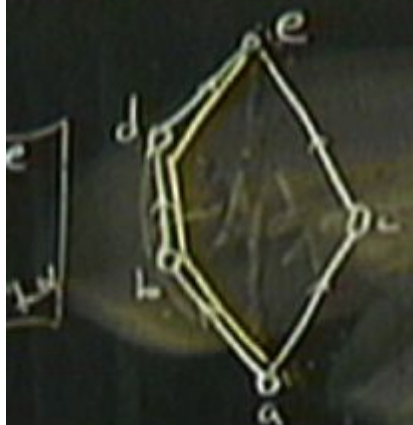
$d=3$



\mathbb{Z}_2

How can this yield geometry?

proper time \longleftrightarrow ?



$a < b$ $c < e$
 $a < e$
 10^{240}



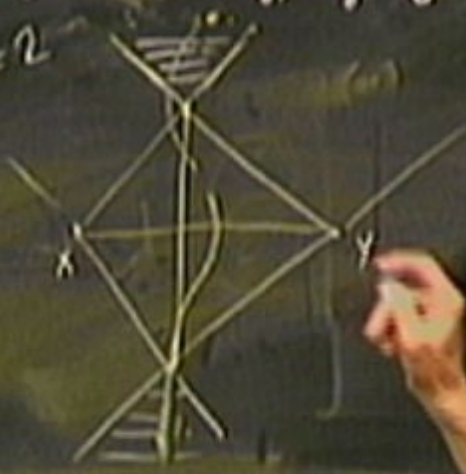
$d=1$



$d=2$



$d=3$

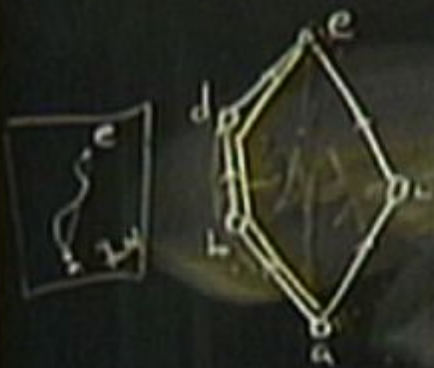


3^2

How can this yield geometry?

proper time \longleftrightarrow ?





$a < b$ $c < e$
 $a < e$
 $10^{24} 0$



$d=1$



$d=2$



$d=3$



proposed
 not

How can this yield geometry?
 proper time \leftrightarrow ?



How can this yield geometry?
propose \leftrightarrow ?

M^2



prop
works in M^2

M^2



How can this yield geometry?
proper flow \leftrightarrow ?

M^2



prop
works in M^2

Rohb (2/19/15)

Melanut

$g(x)$

$\Gamma \rightarrow \Gamma_n$



How can this yield geometry?
propose \leftrightarrow ?

M^2



Prop
works in M^2

Rohy (2/19/15)

Malament

$g(x)$

Continuum

$\Gamma \leftrightarrow \mathbb{R}^n$

order alone \Rightarrow conf. order



How can this yield geometry?
proper flow \leftrightarrow ?

M^2



prob
works in M^2

Rohy (2/19/15)

Malament

Continuum

$g(x)$

$\Gamma \leftrightarrow \nabla_a$

order alone \Rightarrow continuous

$\frac{g(x)}{|dx|}$

$|dx|$



How can this yield geometry?
 prop. due \leftrightarrow ?

M^2



Prop. marks in M^2

Rohly (2-1915)

Malament

Continuum

$g_0(x)$

$\Gamma \leftarrow \nabla_n$

order alone \Rightarrow ...

(H) $\int \sqrt{-g} dy$

How can this yield geometry?
 prop. due \leftrightarrow ?

M^2



prop. roots in M^2

Rohly (2-1915)

Malamut

Continuum

$g_0(x)$

$\Gamma \leftarrow \nabla_n$

order alone \Rightarrow contour order

$$\left(\frac{1}{4}\right) \int \sqrt{-g} d^4y \quad \frac{g_0(x)}{|det g|^{1/4}}$$

9/10

Causets

discreteness: cwe ∞ 's, "explains metric" (- + + +)

order + number = geometry

def causet

elts x, y, \dots

$x < y$ x precedes y
 $x < y$ x ancestor



transitive $x < y < z \Rightarrow x < z$
 acyclic $\Leftarrow x \nlessgtr x$
part-finite

$x < z$
 $y < z$



$D(A, B)$
 ↑
 4-geometry
 2-atom set

ancestors

How can this yield geometry?

time \leftrightarrow ?

10^{-10}

M^2

$d=2$



proposed
works in M^2

Rohly (2/19/15)

Malament

Continuum

$g_0(x)$

$\Gamma \rightarrow \Gamma$

order alone \Rightarrow conform

$\int \sqrt{-g} d^d y$
9/10

$\frac{g_0(x)}{|\det g|}$

10^{24}

M^2

$d=2$

proper
nets in M^2

How can this yield geometry?

proper time \leftrightarrow ?

Rohr (1915)
Malament
Continuum

$g_0(x)$

$\Gamma \leftarrow \mathbb{P}_n$

order one \Rightarrow conformal metric

$\frac{1}{4}$

$d^4y \frac{g_0(x)}{\det g^{1/4}}$

$10^{24} 10$

M^2

$d=2$

propose
works in M^2

How can this yield geometry?

proper time \leftrightarrow ?

Rohy (21915)
Malament

Continuum

$g_0(x)$

$\Gamma \leftarrow \nabla_n$

order above \Rightarrow conformal metric

$\int g d^4 y$

$\frac{g_0(x)}{|det g|^{1/4}}$

10

10^{24}

M^2

$d=2$

propor
ranks in M^2

How can this yield geometry?

propor time \leftrightarrow ?

Continuum

Rohy (21915)
Malament

$g_0(x)$

$\Gamma \leftarrow \nabla_n$

order alone \Rightarrow conformal metric

$$\frac{1}{4} \int \sqrt{-g} d^4y \quad \frac{g_0(x)}{|det g|^{1/4}}$$

9/10

$10^{24} 10$

M^2

propor
ratio in M^2

How can this yield geometry?

propor line \leftrightarrow ?

Rohr (1915)
Malament
Continuum

$g_{\alpha\beta}(x)$
 $\Gamma \leftarrow \nabla_{\alpha}$

order alone \Rightarrow continuum

$N \rightarrow 2 \frac{N^2}{\dots}$

$\left(\frac{1}{4}\right) \int \sqrt{-g} d^4y \frac{g_{\alpha\beta}(x)}{|det g|^{1/4}}$
9/10

$10^{24} 10$

M^2

$d=2$

propor
ranks in M^2

How can this yield geometry?

propor line \leftrightarrow ?

Roth (21915)
Malament

$g_4(x)$

$\Gamma \leftarrow \mathbb{P}_n$

Continuum

order alone \Rightarrow conformal metric

$N \rightarrow 2 \frac{N^2}{\dots}$

$$\left(\frac{1}{4} \right) \int \sqrt{-g} d^4y \quad \frac{g_4(x)}{|det g|^{1/4}}$$

9/10



Classical Sequential Growth models



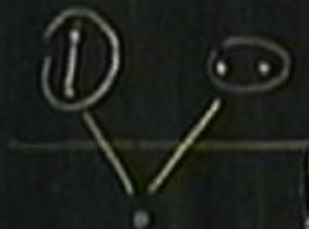
Classical Sequential Growth models (percolation)



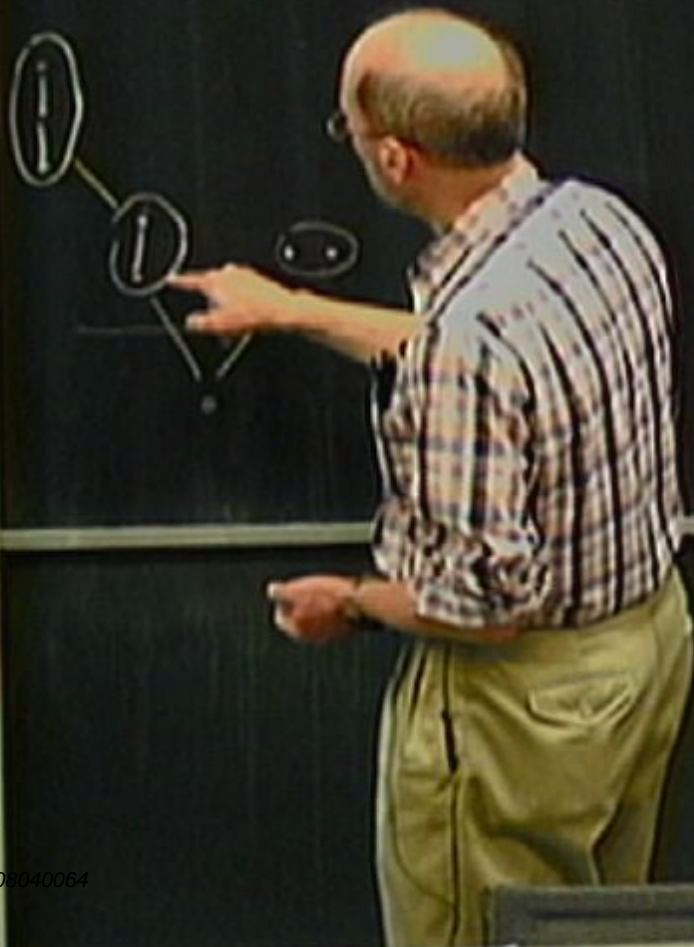
Classical Sequential Growth models (percolation)



Classical Sequential Growth models (percolation)

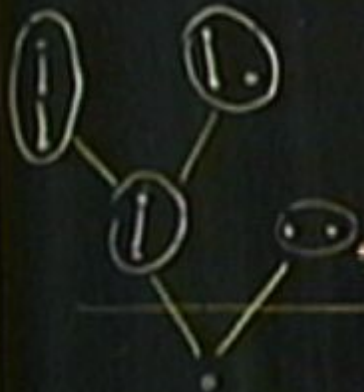


Classical Sequential Growth models (percolation)



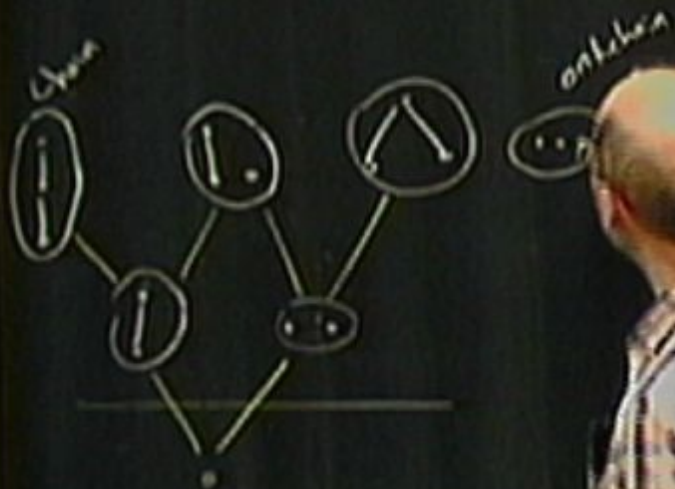
Classical Sequential Growth models

(percolation)



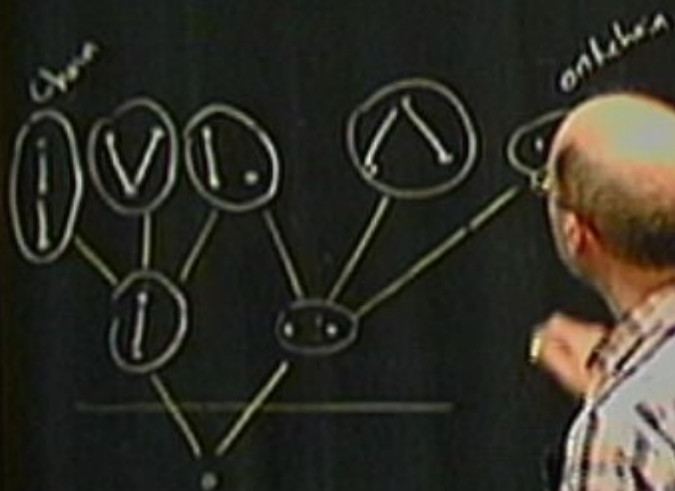
Classical Sequential Growth models

(percolation)



Classical Sequential Growth models

(percolation)



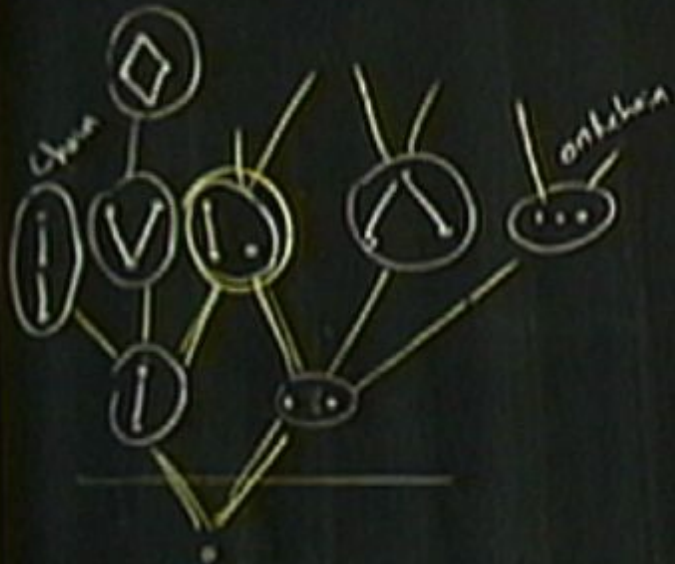
Classical Sequential Growth models (percolation)



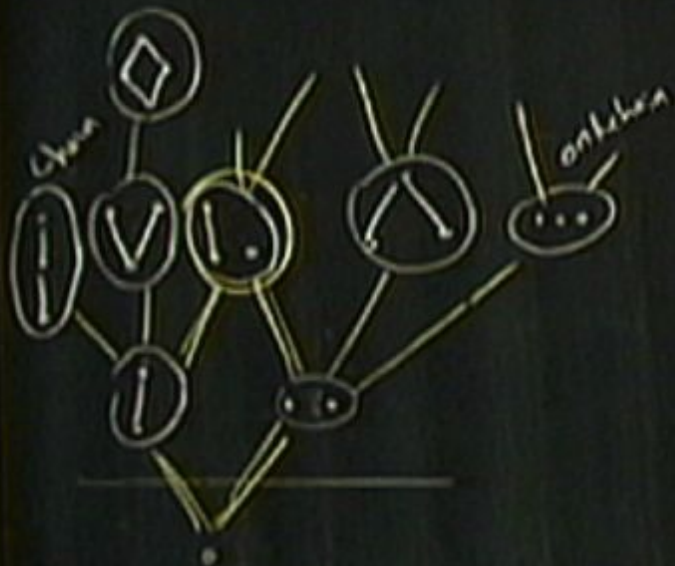
Classical Sequential Growth models (percolation)



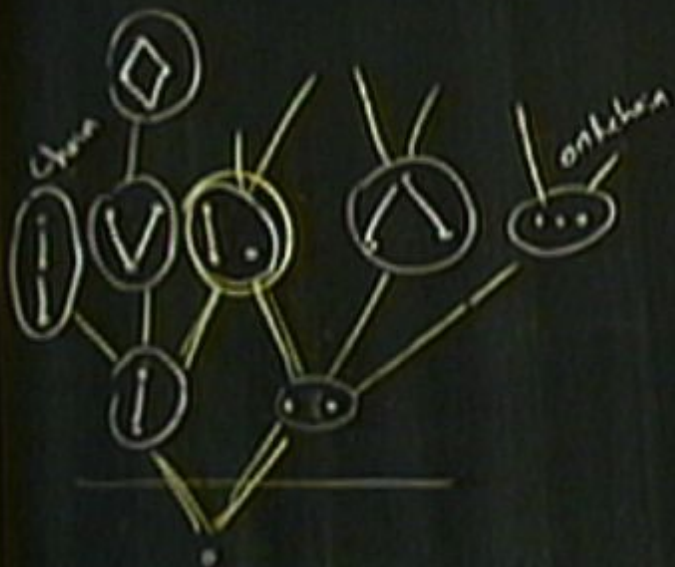
Classical Sequential Growth models (percolation)



Classical Sequential Growth models (percolation)



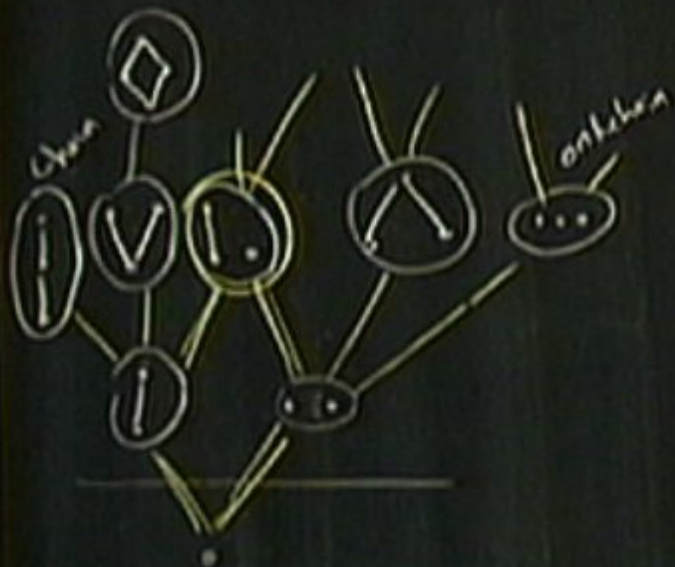
Classical Sequential Growth models (percolation)



label invariance



Classical Sequential Growth models (percolation)



label invariance \leftrightarrow Gen cover



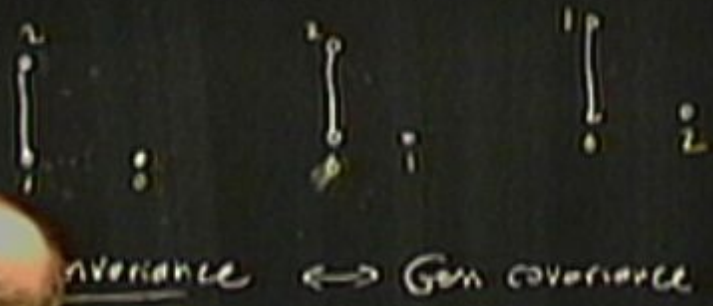
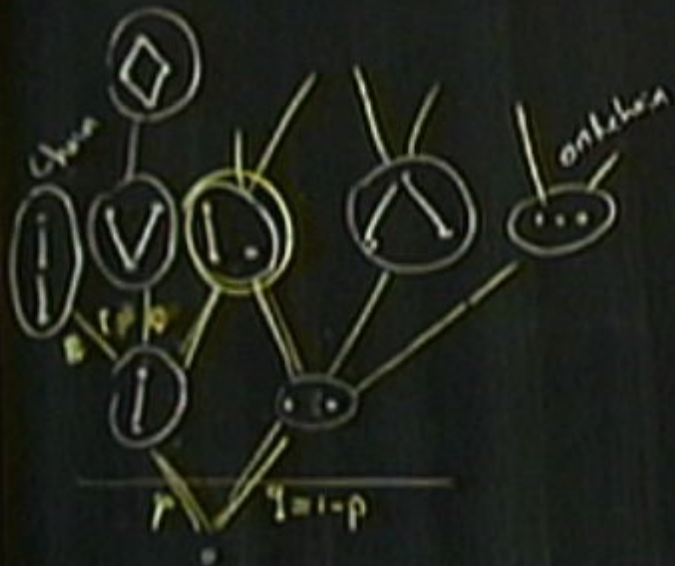
Classical Sequential Growth models

(percolation)

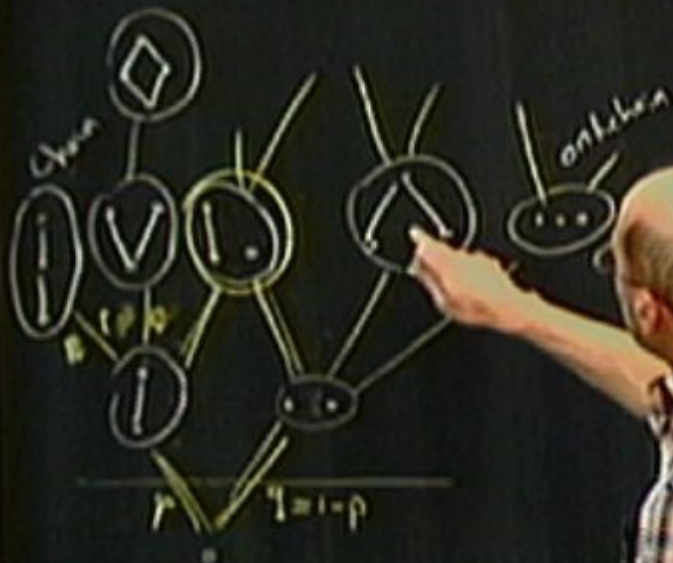


label invariance \leftrightarrow Gen covariance

Classical Sequential Growth models (percolation)

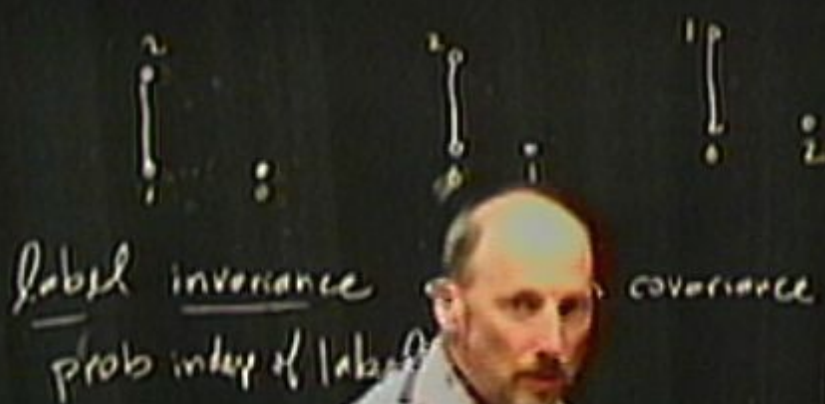
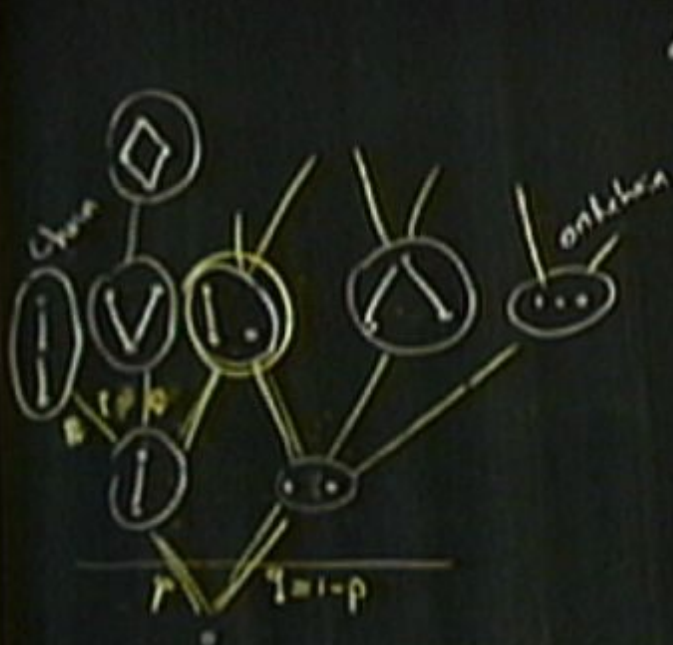


Classical Sequential Growth models (percolation)

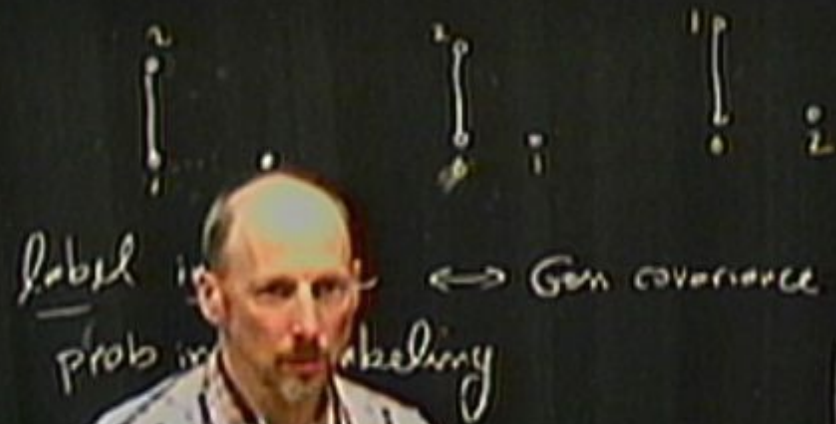
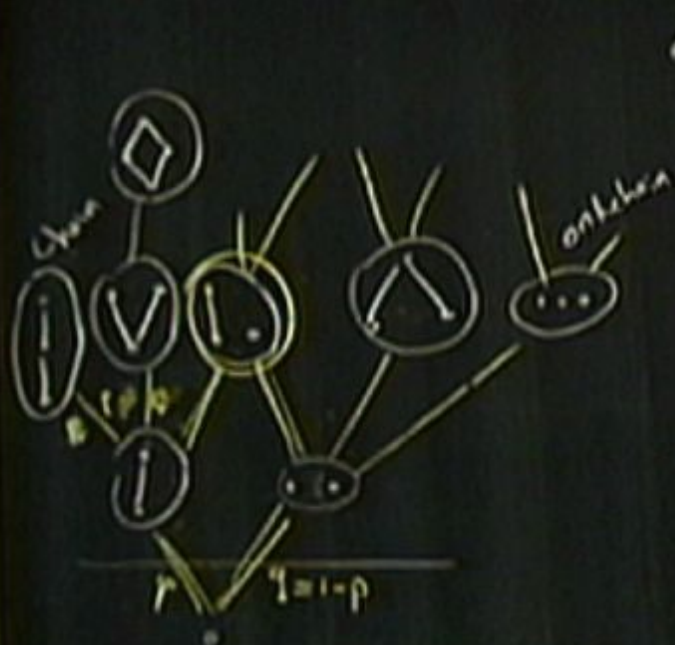


label invariance \leftrightarrow Gem covariance
 prob indep of labeling

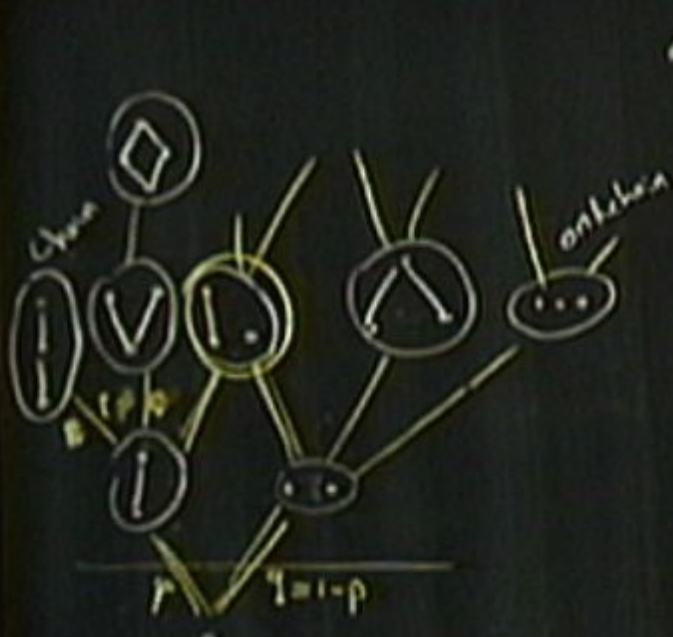
Classical Sequential Growth models (percolation)



Classical Sequential Growth models (percolation)



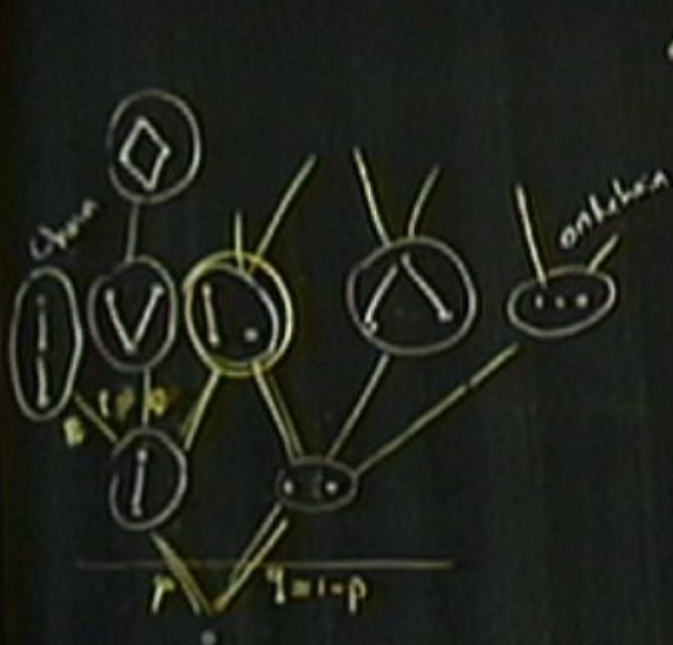
Classical Sequential Growth models (percolation)



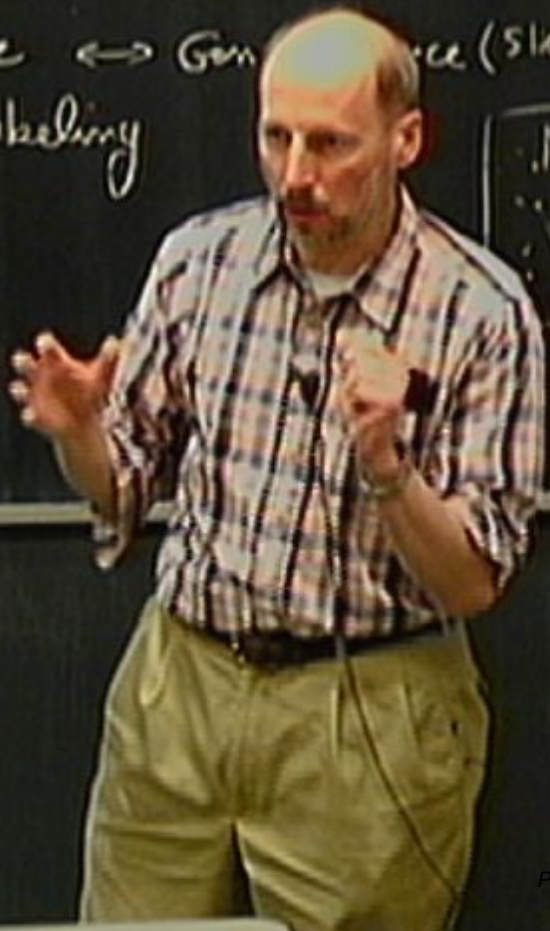
label invariance \leftrightarrow Gen. rel. (string invariance)
 prob indep of labeling



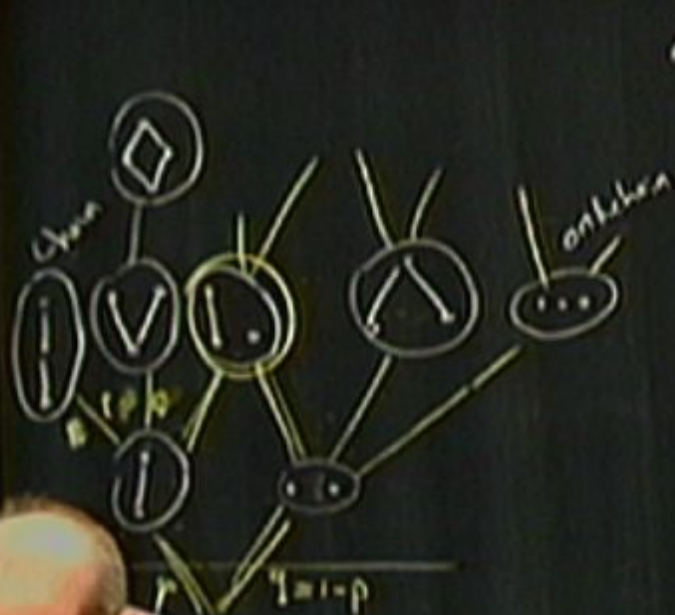
Classical Sequential Growth models (percolation)



label invariance \leftrightarrow Gen. Invariance (Slice invariance)
 prob indep of labeling



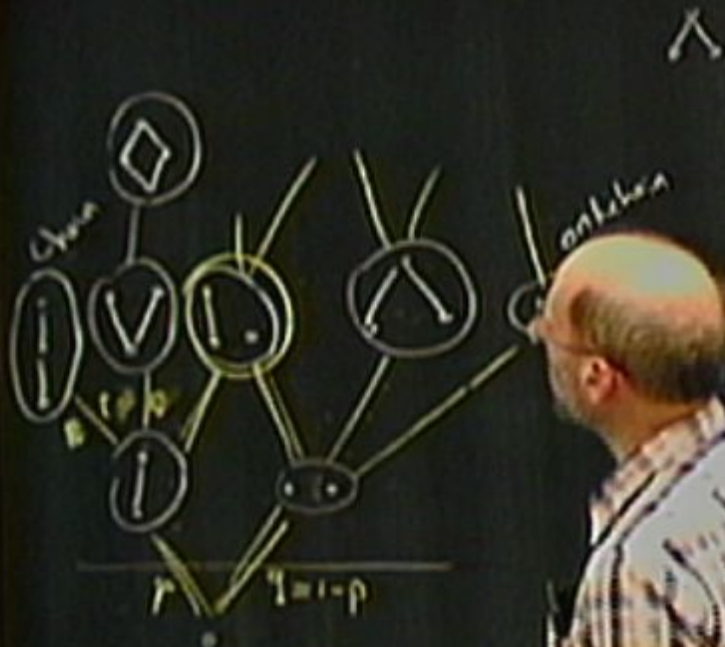
Classical Sequential Growth models (percolation)



label invariance \leftrightarrow Gem covariance (Slicing invariance)
 prob indep of labeling



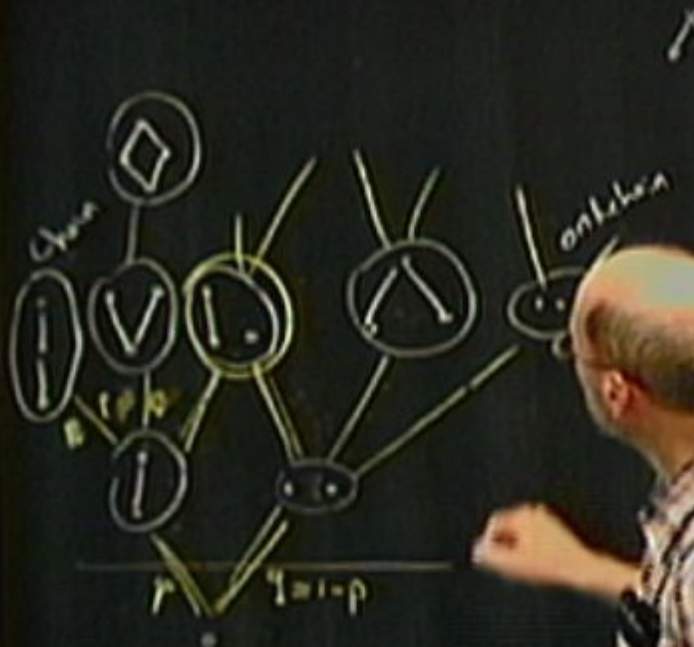
Classical Sequential Growth models (percolation)



label invariance \leftrightarrow Gen covariance (Slicing invariance)
 prob indep of labeling



Classical Sequential Growth models (percolation)

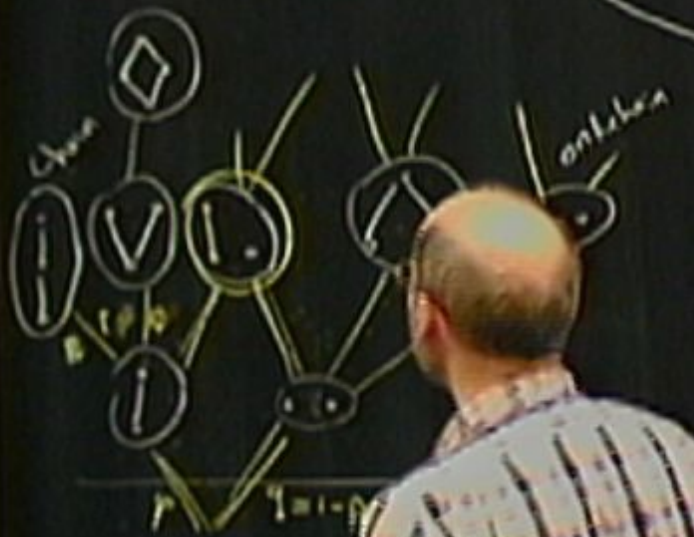


label invariance \leftrightarrow prob indep of labeling
Bell causality

Gen covariance (Slicing invariance)



Classical Sequential Growth models (percolation)

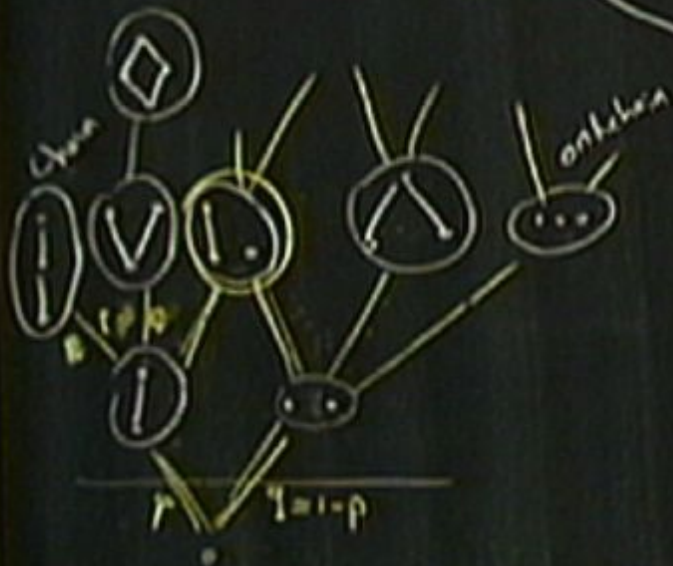


label invariance
 prob indep of labeling
 Bell causality

Gen covariance (Slicing invariance)



Classical Sequential Growth models (percolation)



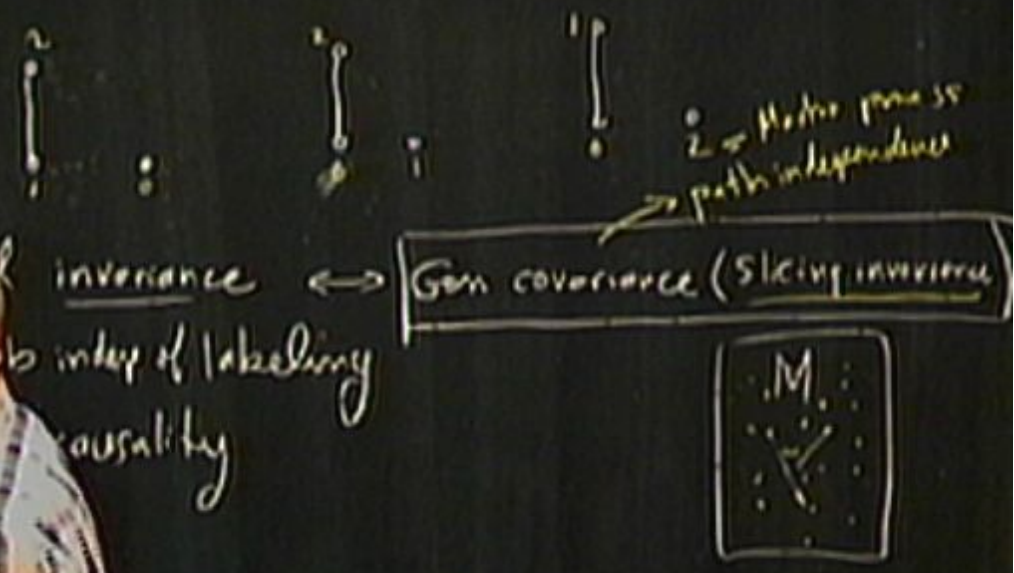
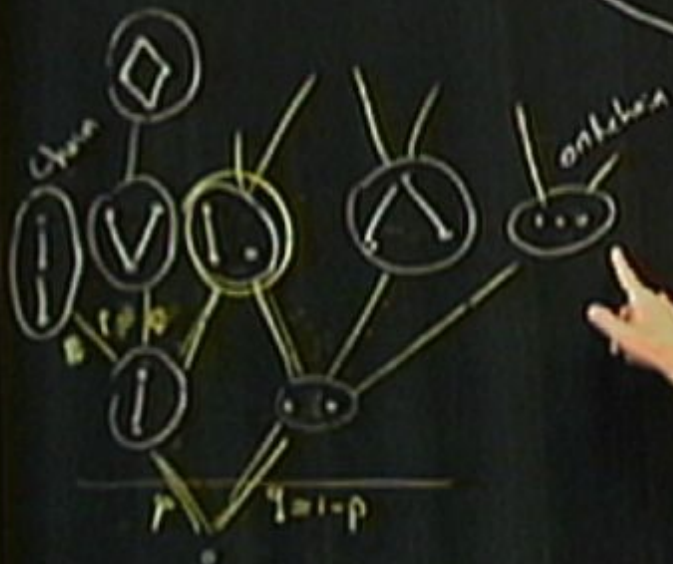
$Z \rightarrow$ Markov process
path independent

label invariance \leftrightarrow Gen
prob indep of labeling
Bell causality

(Slicing invariance)



Classical Sequential Growth models (percolation)



① Recover time (from space) in CQG

② Conceptual problems from diff

What are the "observables" ("beables") ("variables")
covariant meaningful

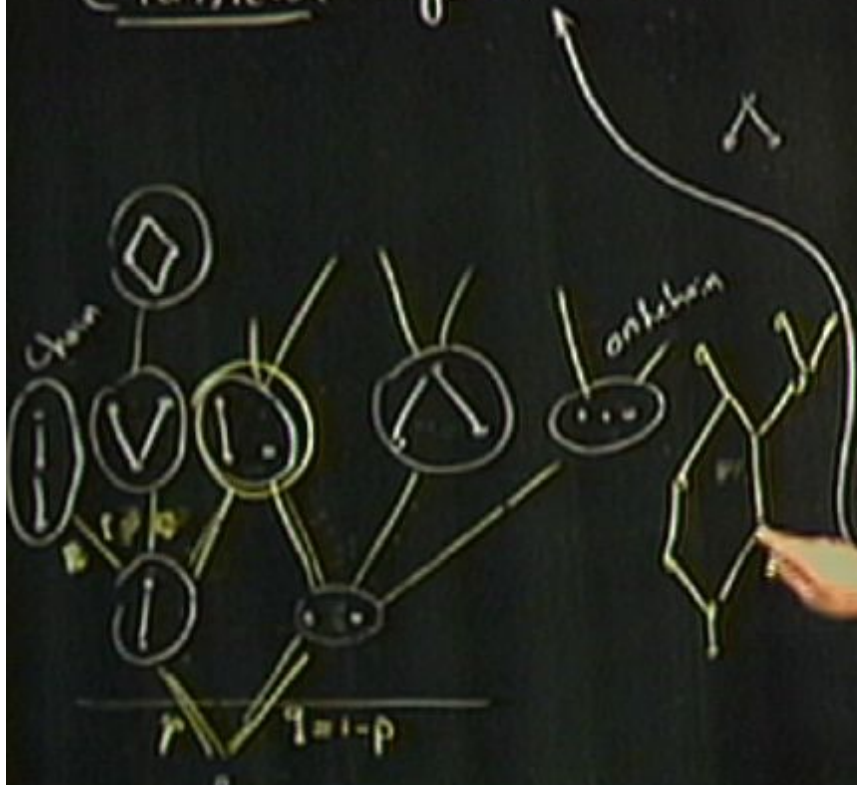
③ Technical problems from diff (e.g. $\text{vol}(D.R) = 0$)

④ Absence of natural Wick rotation?

⑤ Problem of 'becoming' (Do things happen?) (no unique slicing)

⑥ Arrow (can QG help?)

Classical Sequential Growth models (percolation)



label
prob
Bell cov

Gen covariance (Slicing inversion)

$z \rightarrow$ Markov process
path independence



① Recover time (from space) in CQG

② Conceptual problems from diff

What are the "observables" ("beables") ("Variables")
Covariant meaningful

③ Technical problems from diff (e.g. $\text{Vol}(\mathcal{D}, \mathcal{R}) = 0$) $\mathcal{S} \rightarrow \Sigma$

④ Absence of natural Wick rotation?

⑤ Problem of "becoming" (things happen?) (no unique slicing)

⑥ Arrow of time (conformal?)

① Recover time (from space) in CQG

② Conceptual problems from diffeo

What are the "observables" ("beables") ("variables")
Covariant meaningful

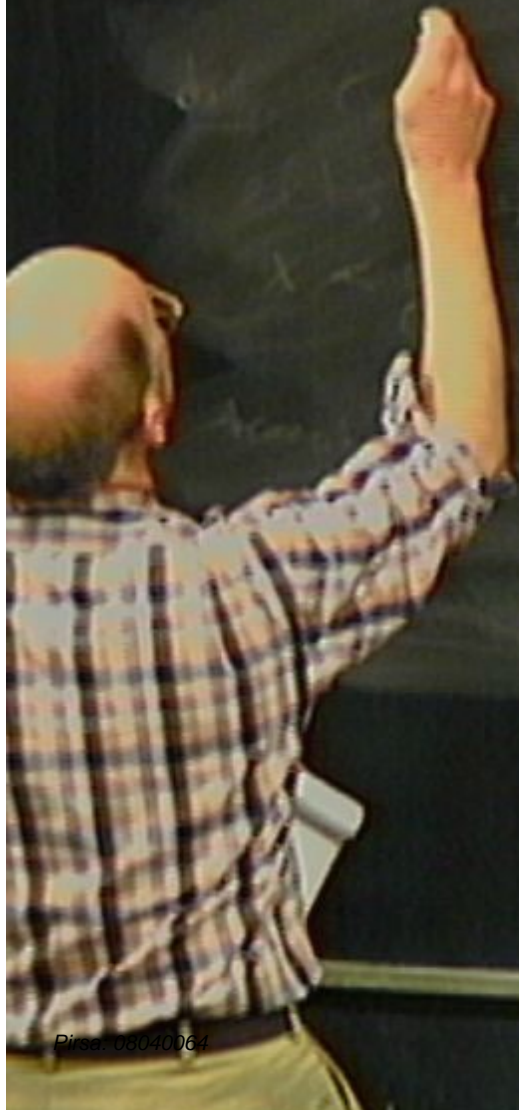
③ Technical problems from diff (e.g. $\text{vol}(D, \mathcal{P}) = 0$) $\mathcal{S} \rightarrow \Sigma$

④ Absence of natural Wick rotation?

⑤ Problem of "becoming" (Do things happen?) (no unique slicing)

⑥ Arrow of time (can QG help?) ✓

The meaningful questions



Can we explain π (with π)

number = geometry

representing

number

The meaningful questions are "stem-questions"

$S(F) =$ "Does C contain F as stem?"

F a finite causal set

C be " " of interest

The meaningful questions are "stem-questions"

$S(F) =$ "Does C contain F as stem?"

F a finite causal set

C be " " of interest

↑
subset that
contains all
ancestors

The meaningful questions are "stem-questions"

$S(F) =$ "Does C contain F as stem?"

F a finite causal set

C be " " of interest

↑
subset that
contains all
ancestors



The meaningful questions are "stem-questions"

$S(F) = \text{"Does } C \text{ contain } F \text{ as stem?"}$

F a finite causal set

C be " " of interest

↑ subset that
contains all
ancestors
(down set)
(past set)



The meaningful questions are "stem-questions"

$S(F) = \text{"Does } C \text{ contain } F \text{ as stem?"}$

F a finite causal set

C be " " of interest

↑ subset that contains all ancestors
(down set)
(past set)



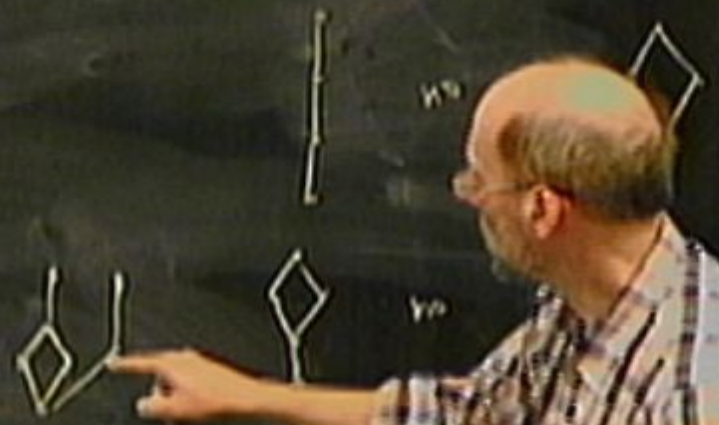
The meaningful questions are "stem-questions"

$S(F) =$ "Does C contain F as stem?"

F a fork causal set

C be " " of interest

↑ subset that contains all ancestors
(down set)
(past set)



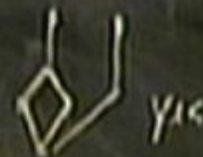
The meaningful questions are "stem-questions"

$S(F) = \text{"Does } C \text{ contain } F \text{ as stem?"}$

F a fork causal set

C be " " of interest

↑ subset that contains all ancestors
(down set)
(past set)



The meaningful questions are "stem-questions"

$S(F) = \text{"Does } C \text{ contain } F \text{ as stem?"}$

F a fork causal set

C be " " of interest

↑ subset that contains all ancestors



The meaningful questions are "stem-questions"

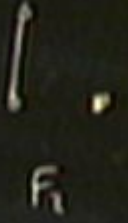
$S(F) =$ "Does C contain F as stem?"

F a finite causal set

C be " " of interest

Every question can be expressed
in terms of stem-questions
using and or not

↑ subset that
contains all
ancestors
(down set)
(past set)



yes



no

The meaningful questions are "stem-questions"

$S(F) = \text{"Does } C \text{ contain } F \text{ as stem?"}$

F a fork causal set

C be " " of interest

↑ subset that contains all ancestors (down set) (past set)

Every question can be expressed in terms of stem-questions using and or not

(up to sets of axioms etc)



① Recover time (from space) in CQG

② Conceptual problems from diff

What are the "observables" ("beables") ("variables")
covariant meaningful

③ Technical problems from diff (e.g. $\text{vol}(\text{D.f.f.}) = 0$) $\mathcal{S} \rightarrow \Sigma$

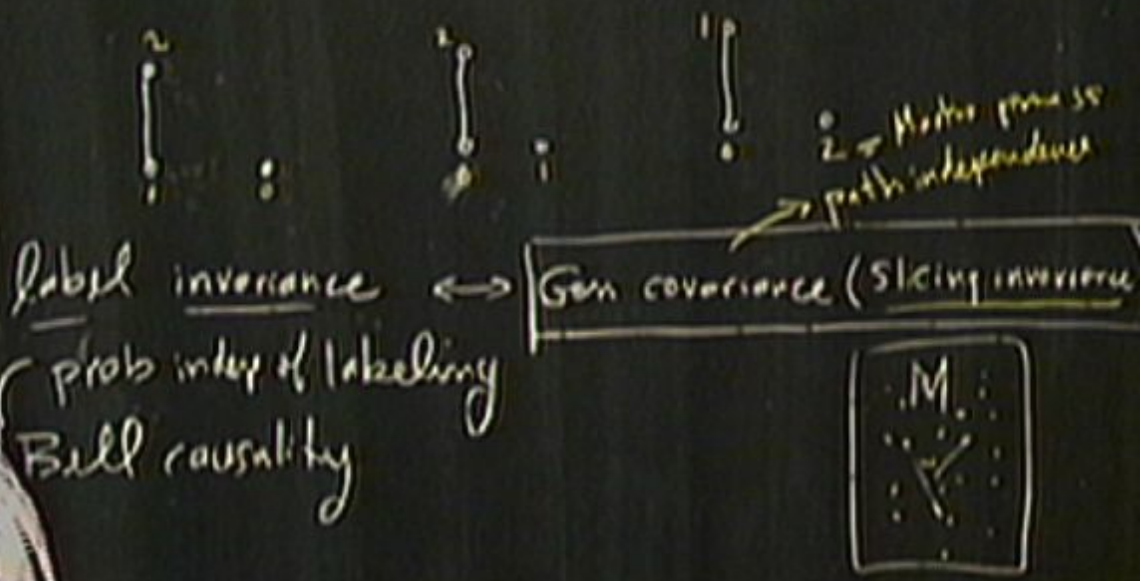
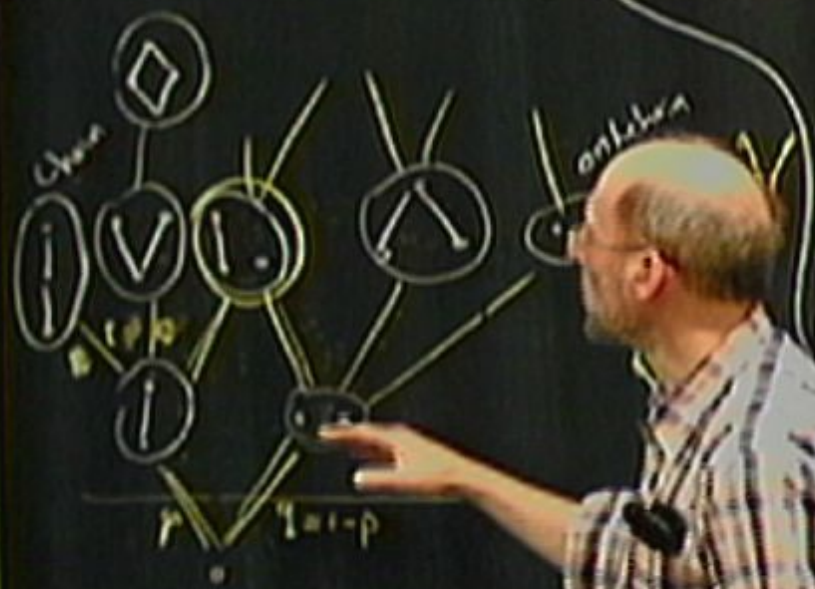
④ Absence of natural Wick rotation?

problem of "becoming" (Do things happen?) (no unique slicing)
(arrow of time) (can QG help?) ✓



9/10

Classical Sequential Growth models (percolation)



① Recover time (from space) in CQG

② Conceptual problems from diff

What are the "observables" ("beables") ("variables")
covariant meaningful

③ Technical problems from diff (e.g. $\text{vol}(D, \mathcal{M}) = 0$) $\mathcal{S} \rightarrow \Sigma$

④ Absence of natural Wick rotation?

Problem of "becoming" (Do things happen?) (no unique slicing)

Arrow of time (can QG help?) ✓



What are the "observables" ("beables") ("Variables")

Covariant meaningful

Technical problems from diff (e.g. $\text{Vol}(\mathcal{D}, \mathcal{M}) = 0$) $\mathcal{S} \rightarrow \Sigma$

existence of natural Wick rotation?

Problem of 'becoming' (Do things happen?) (no unique 'ing')

Arrow of time (can QG help?) ✓

'asynchronous becoming'



① Recover time (from space) in CQG

② Conceptual problems from diff

What are the "observables" ("beables") ("variables")
Covariant meaningful

③ Technical problems from diff (e.g. w/ (D.R) = 0) $\mathcal{S} \rightarrow \Sigma$

④ Absence of natural Wick rotation?

⑤ Problem of 'becoming' (Do things happen?) (no unique slicing)

⑥ Arrow of time (can QG help?) ✓

'asynchronous becoming'