

Title: Non-Metallic Resistivity in Strongly Correlated Metals

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Abstract: There are a few examples in the literature of metals that, in the  $T \rightarrow 0$  K limit, show a resistivity that rises with decreasing temperature without any sign of either saturation or a gap. Well known cases include underdoped cuprates in high magnetic fields and some doped uranium heavy fermion compounds. I will review these and some less-well-known cases, before describing the behaviour of FeCrAs [1], in which we find a continuously rising resistivity from 900 K down to below 50 mK, with a brief interruption due to an antiferromagnetic transition at about 100 K. Down to at least 50 mK the resistivity is nearly linear in temperature, but with a negative coefficient. We speculate that this behaviour may be connected to fluctuations of frustrated iron  $\mu$ -trimers that do not order magnetically. 1. W. Wu, A. McCollam, P.M.C. Rourke, D. Rancourt, I. Swainson and S.R. Julian, in preparation.

# Non-metallic resistivity in strongly correlated electron systems

*Stephen Julian*  
*University of Toronto*

- Non-fermi-liquid behaviour in
  - $\text{YUPd}_3$ ,  $\text{UCu}_{5-x}\text{Pd}_x$ , and other heavy fermions
  - Frustrated spin system  $\text{PrIr}_2\text{O}_7$
- Non-metallic resistivity and other properties of FeCrAs
  - Underscreened Kondo model?

## Non-Fermi-liquid transport

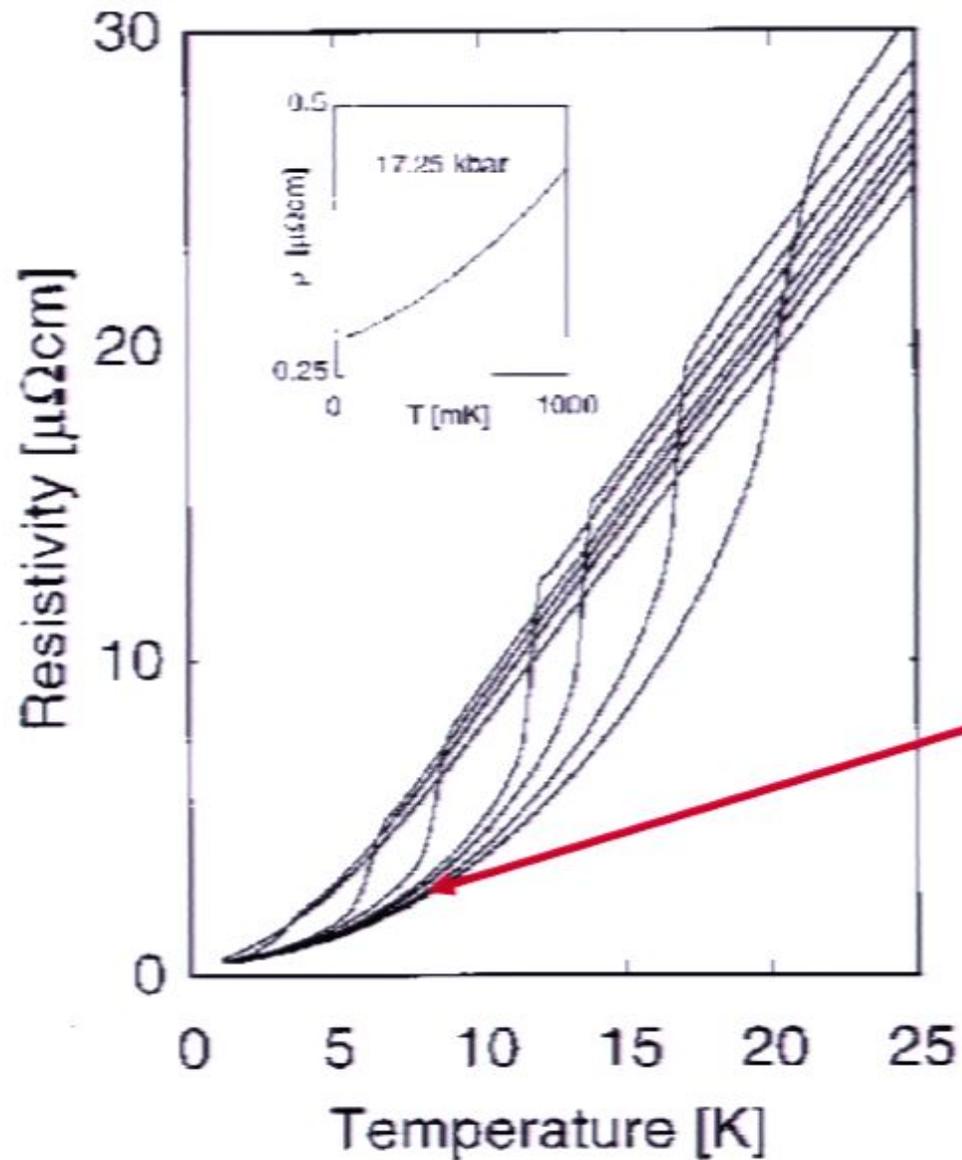
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$$\alpha < 2$$

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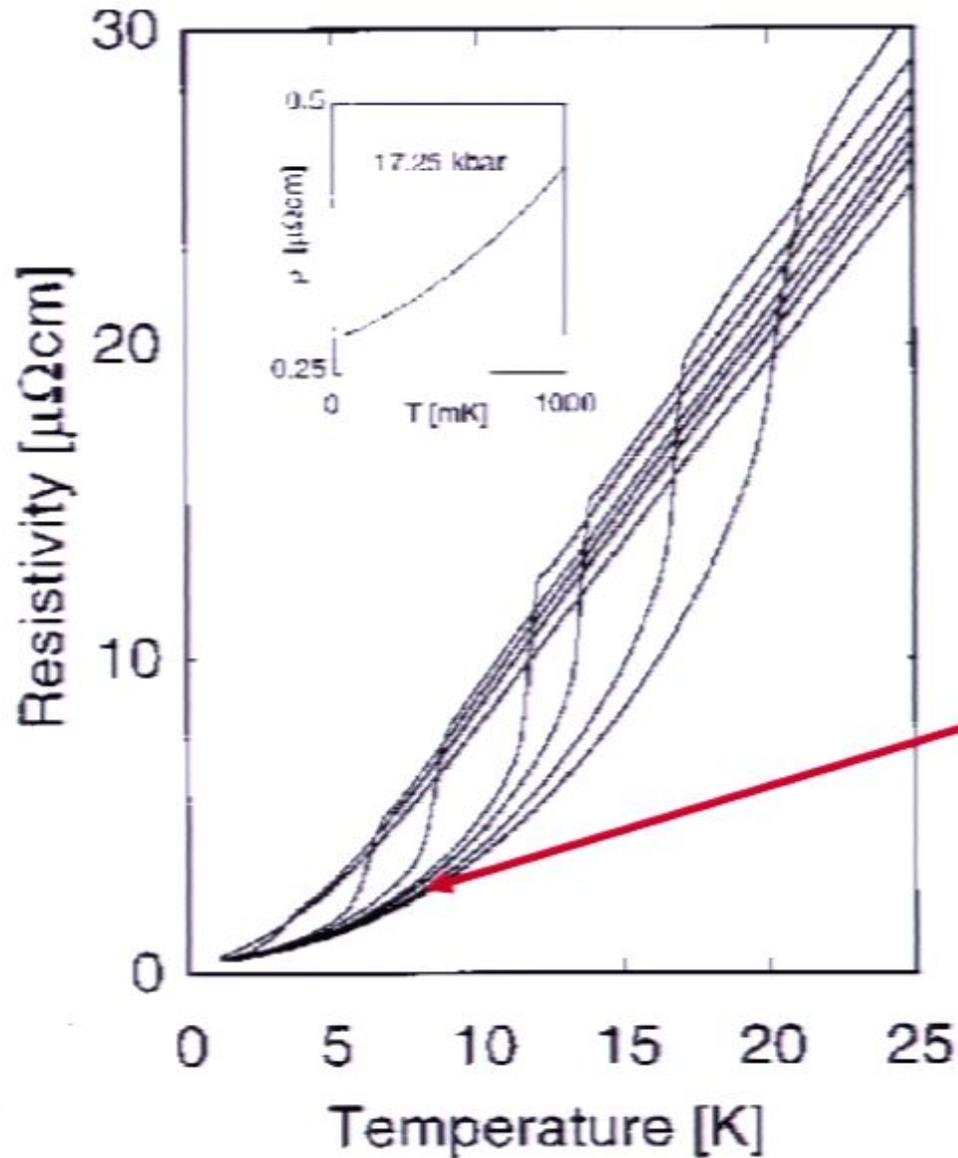
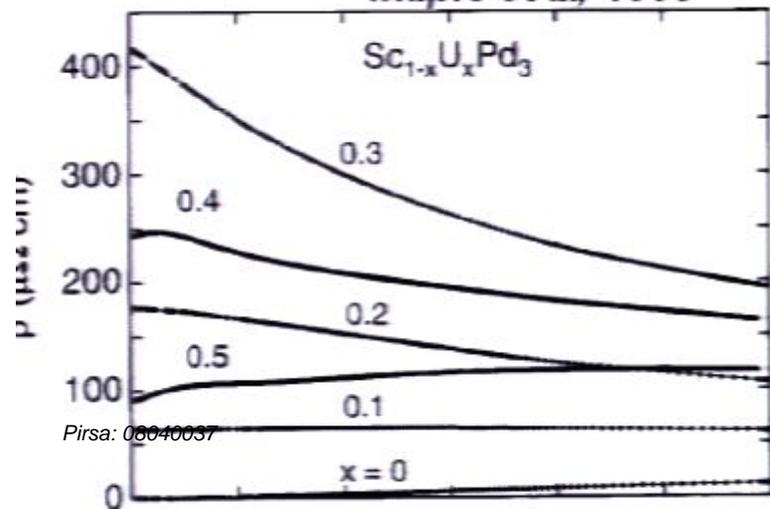
# Non-Fermi-liquid transport

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$$\alpha < 2$$

$$A < 0$$

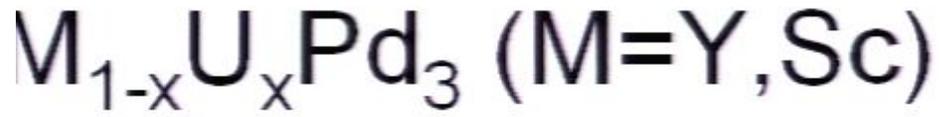
Maple et al, 1995



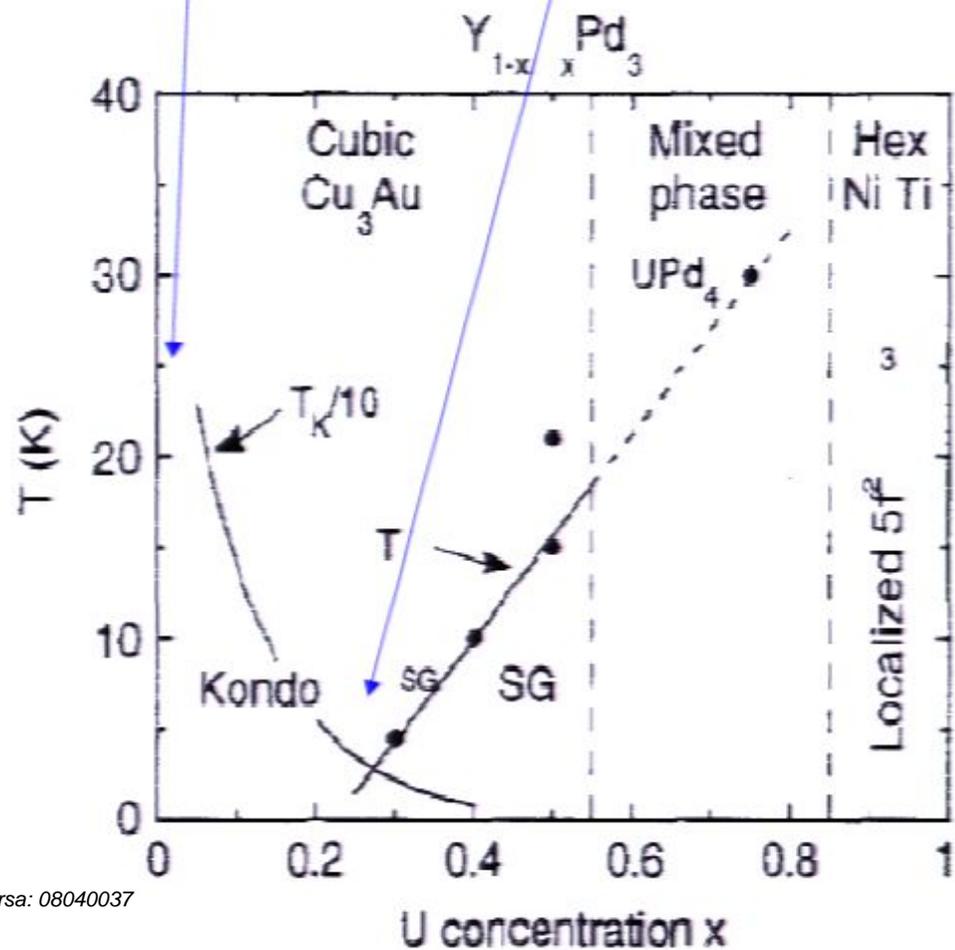
$T^2$

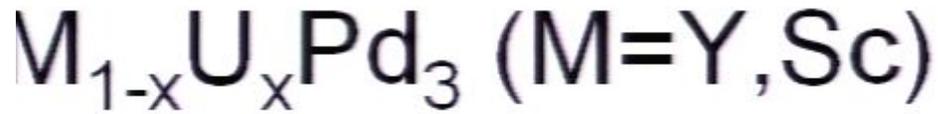
# non-Fermi-liquid systems with $d\rho/dT < 0$ in the $T \rightarrow 0\text{K}$ limit

- There are not many
- Roughly they can be divided into concentrated and dilute impurity limit systems.

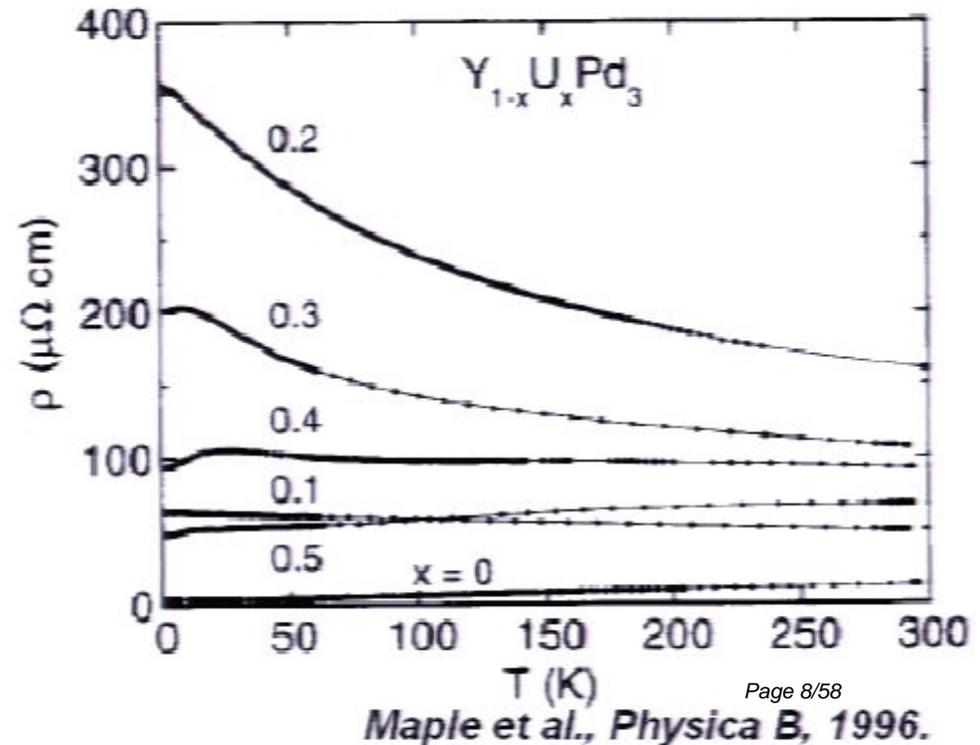
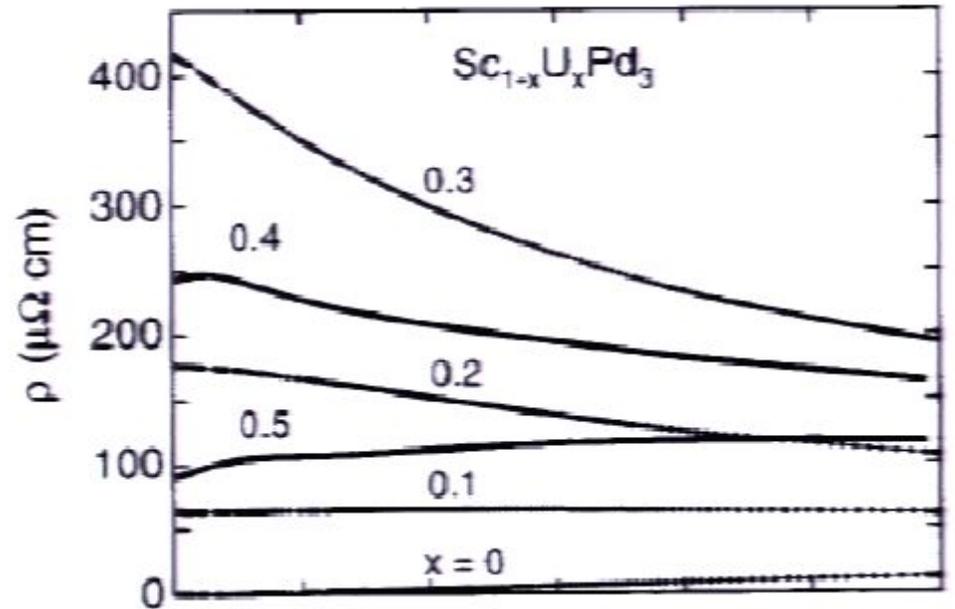
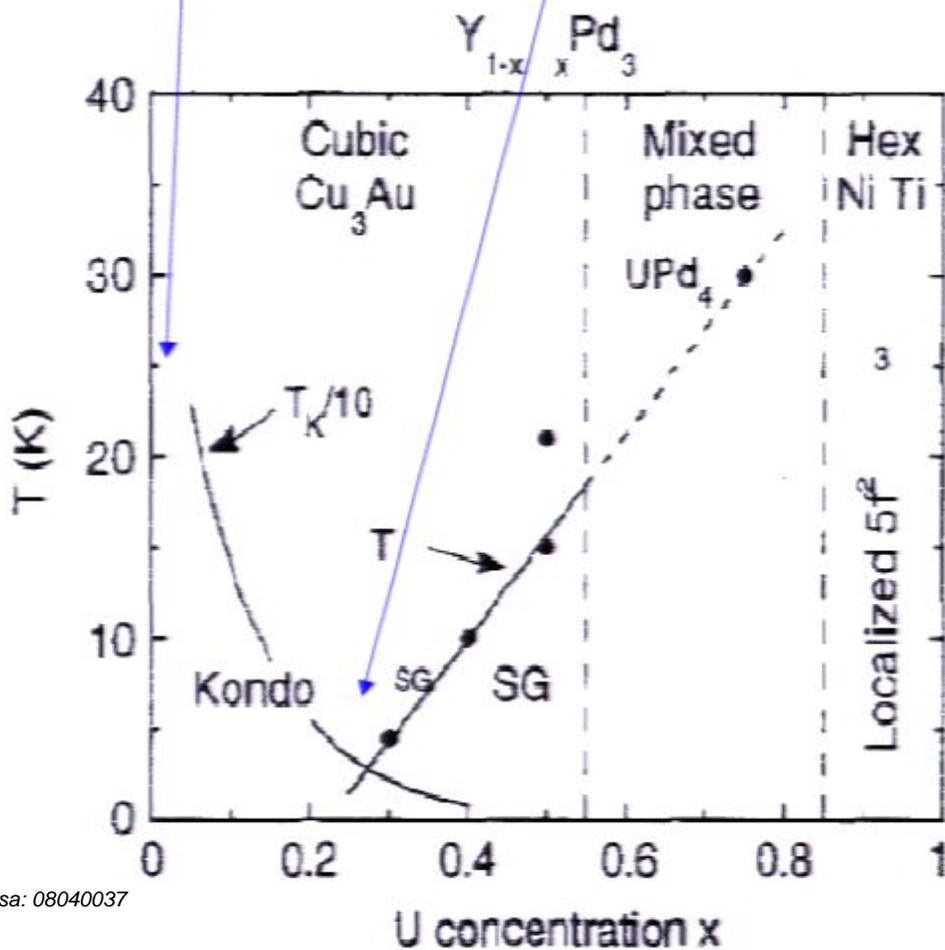


*dilute impurity limit*  
*concentrated limit*

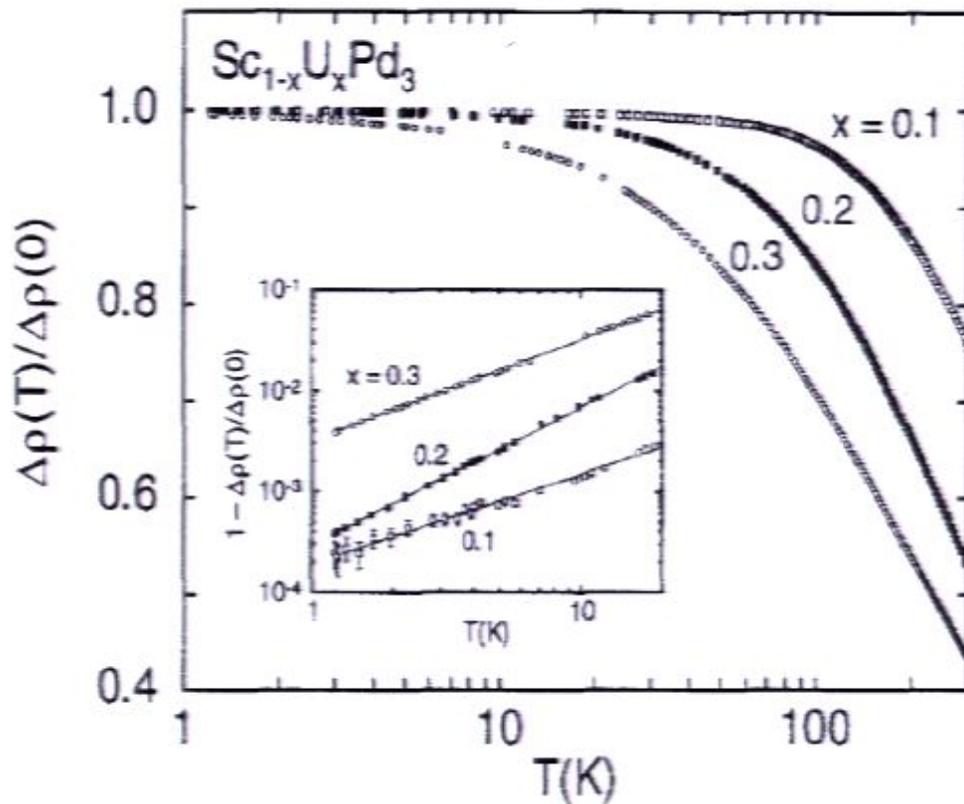




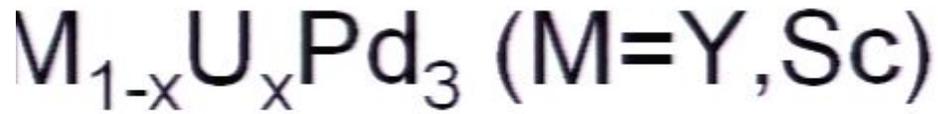
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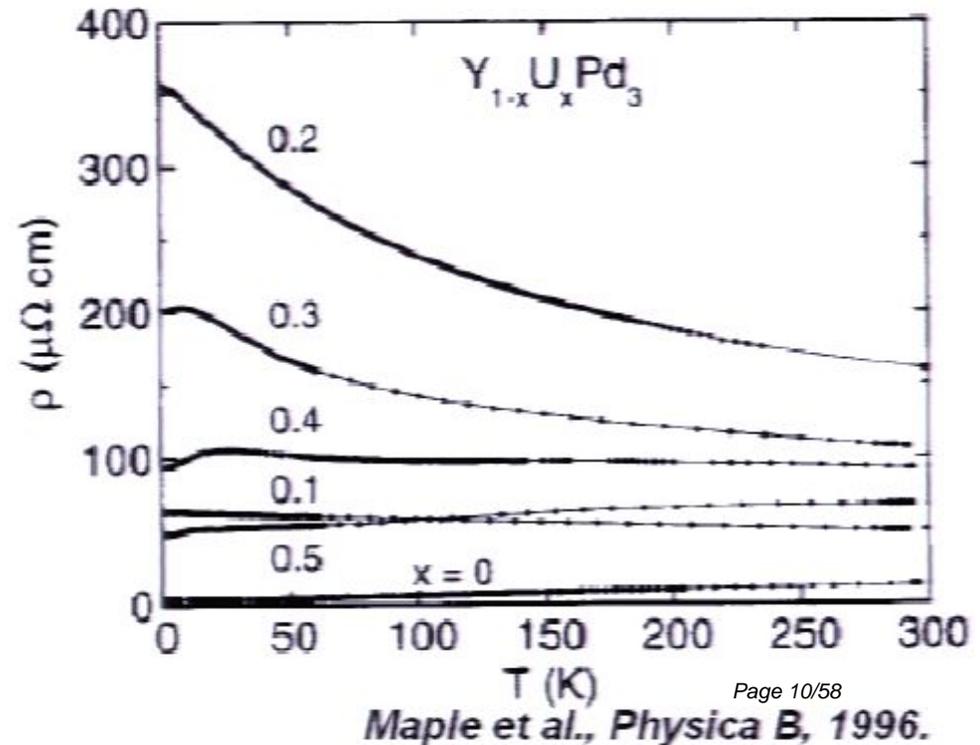
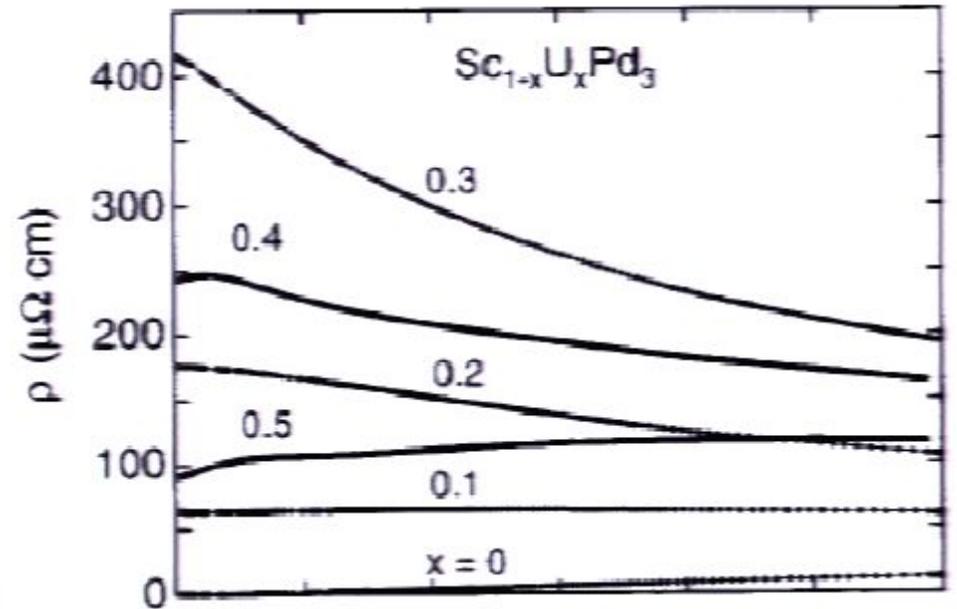
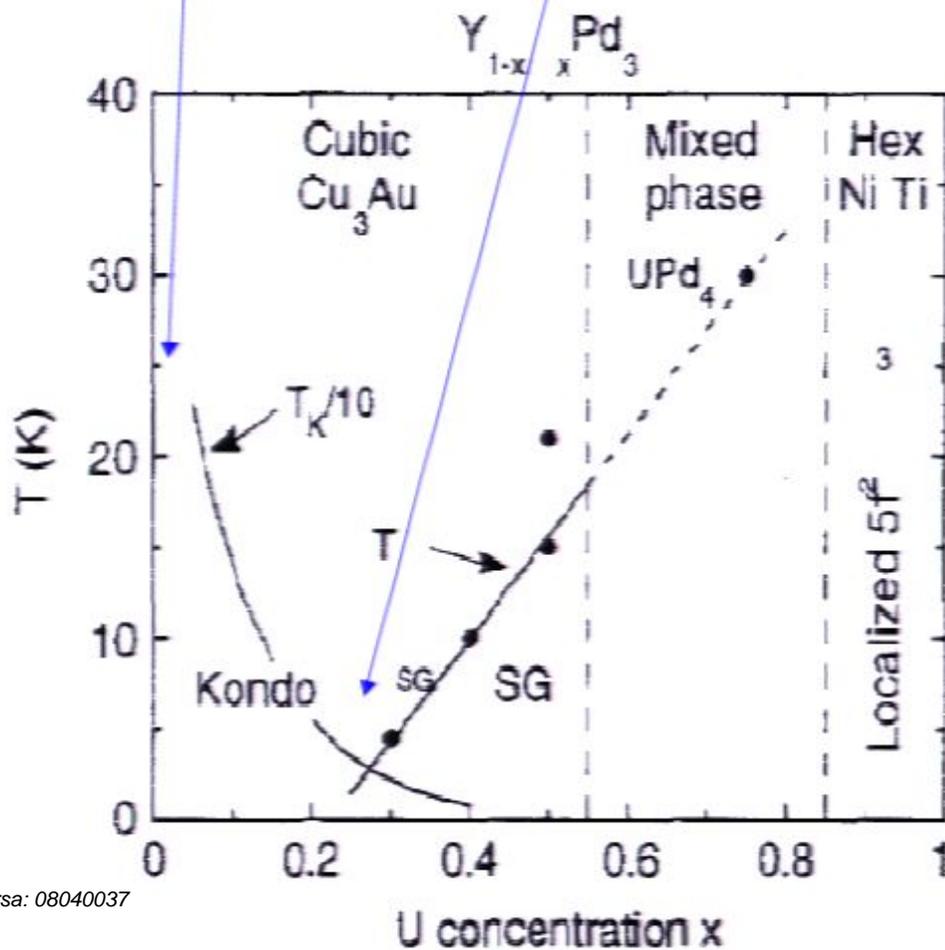
# Evidence of Kondo and non-Fermi-liquid physics:



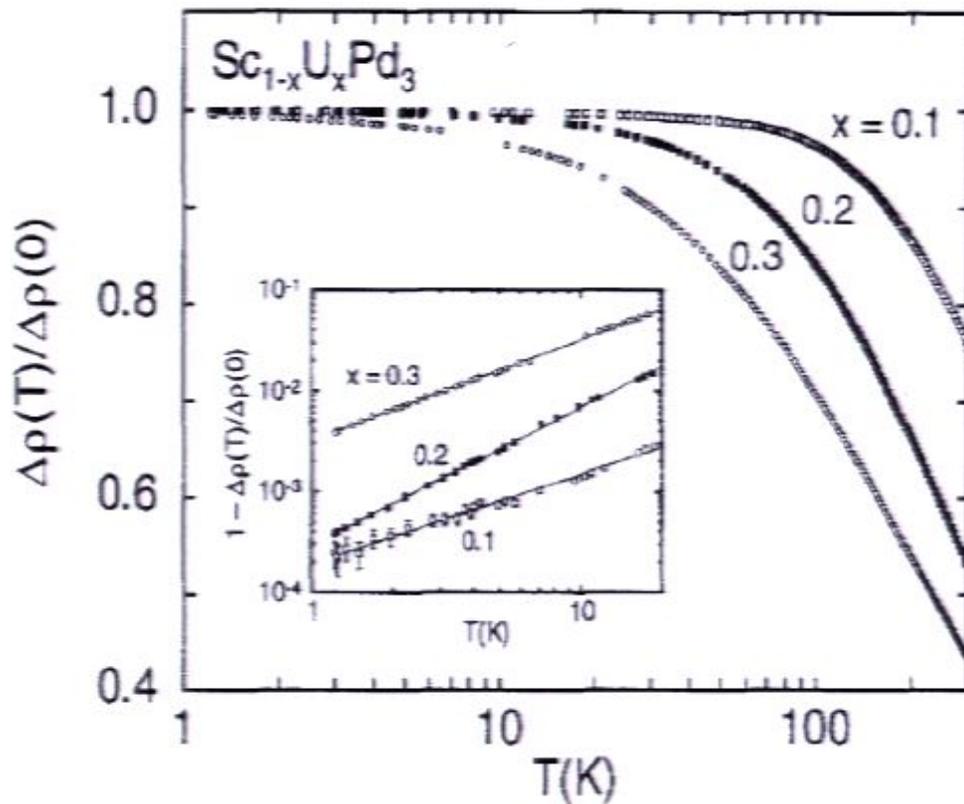
- **$\text{Log}(T/T_0)$  resistivity at high  $T$**
- **Linear resistivity at low  $T$**



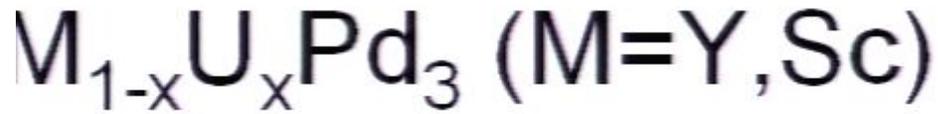
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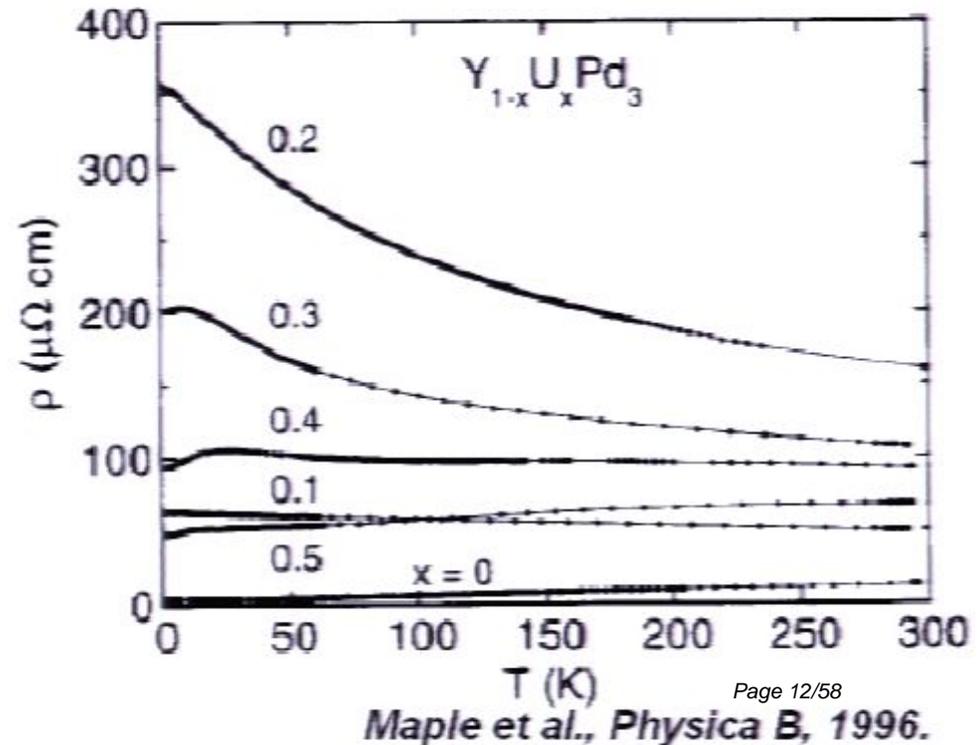
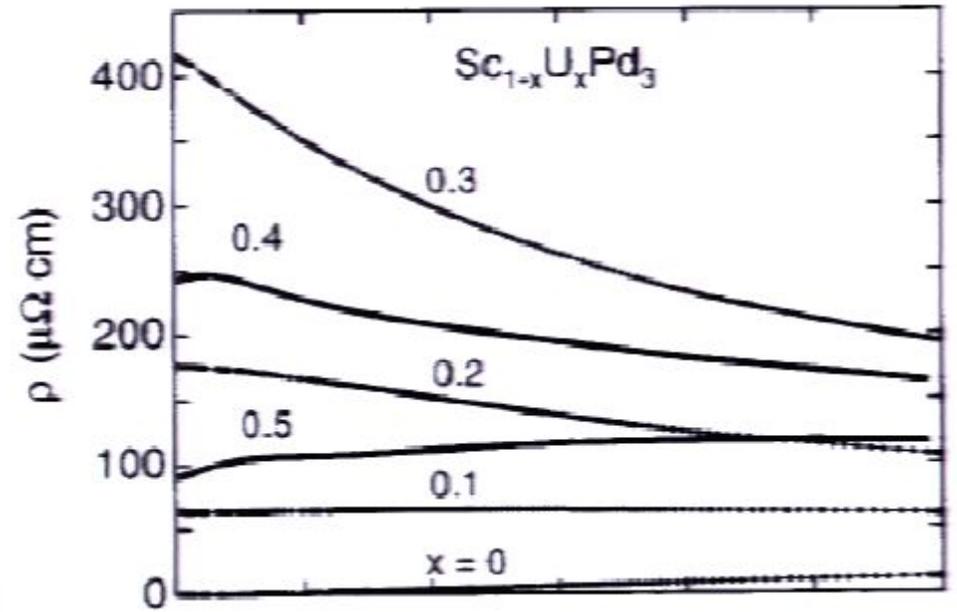
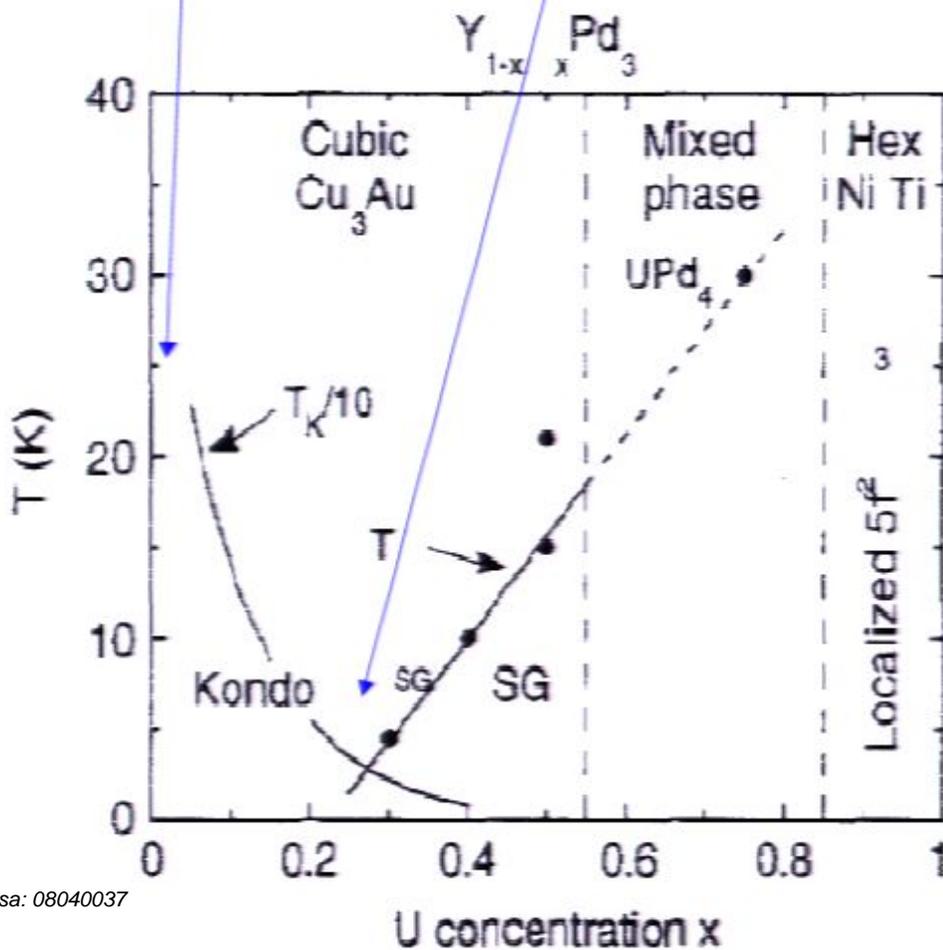
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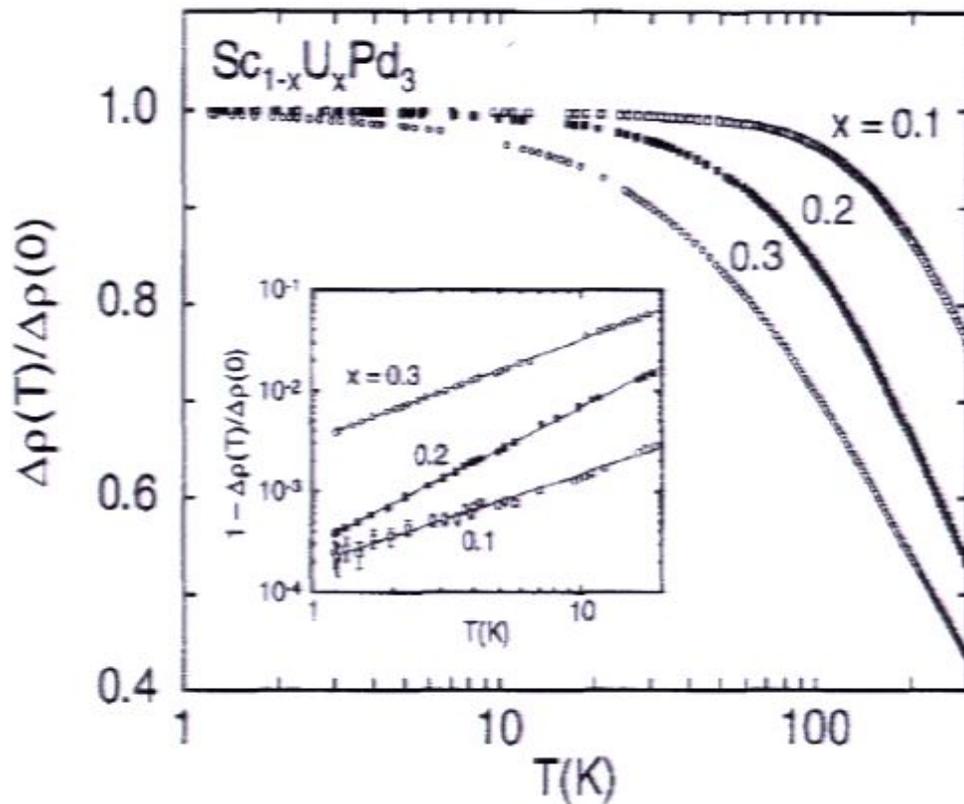
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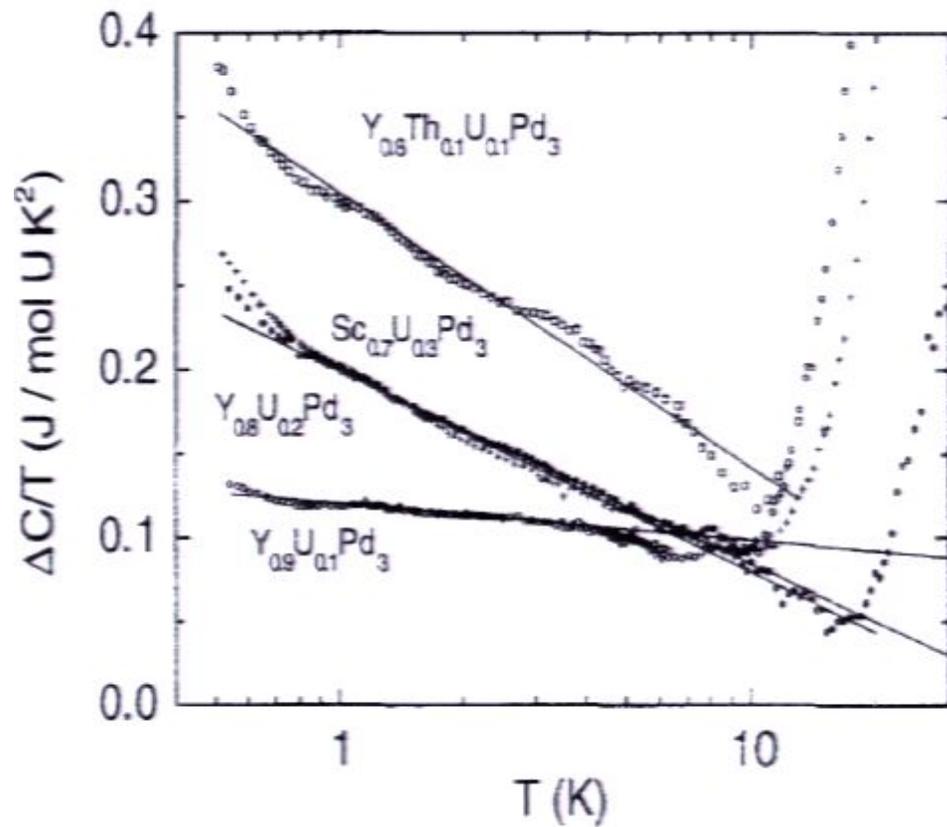


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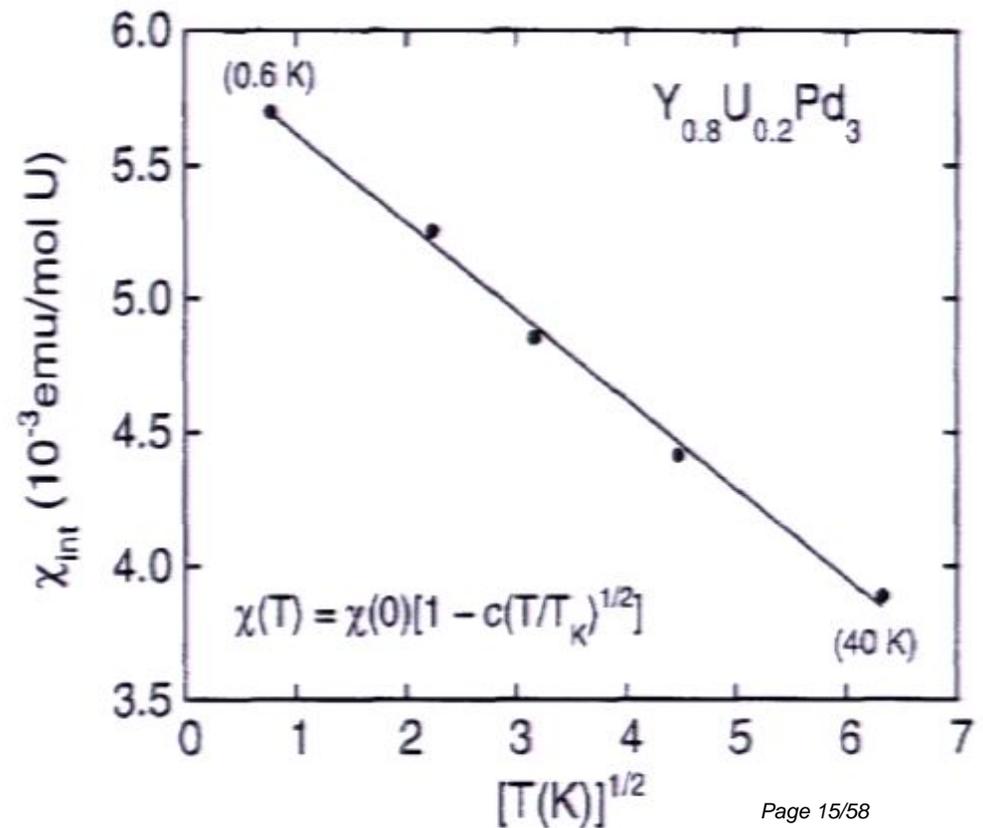
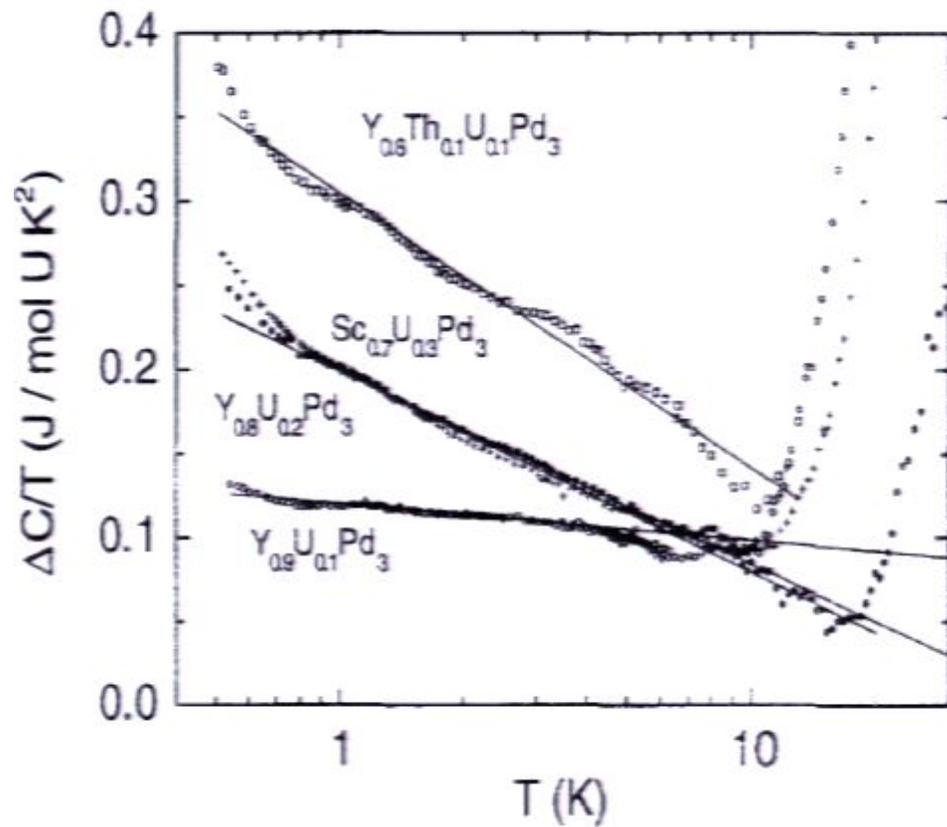


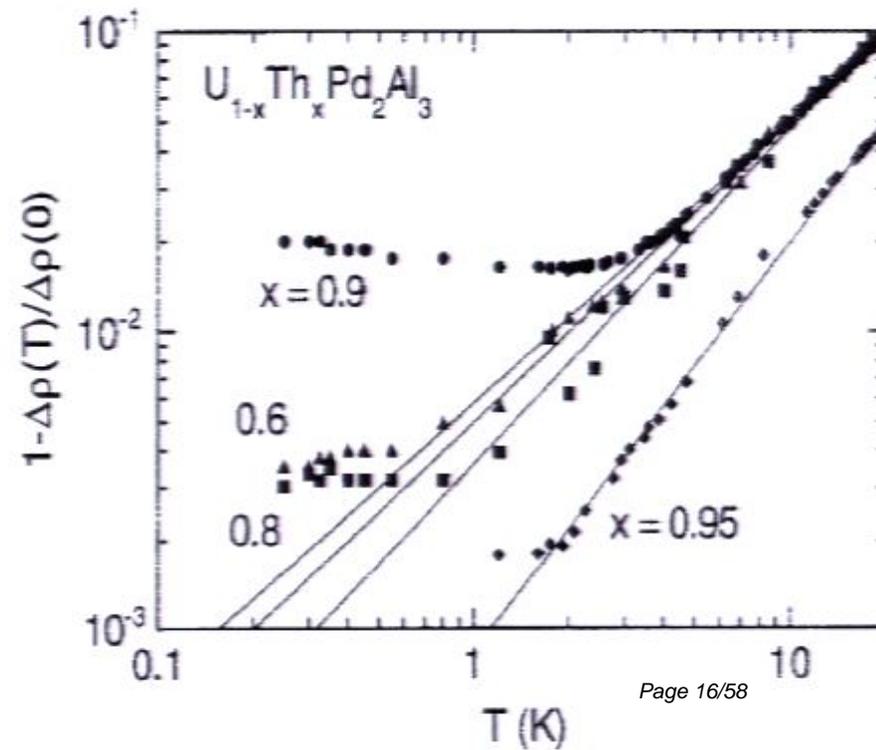
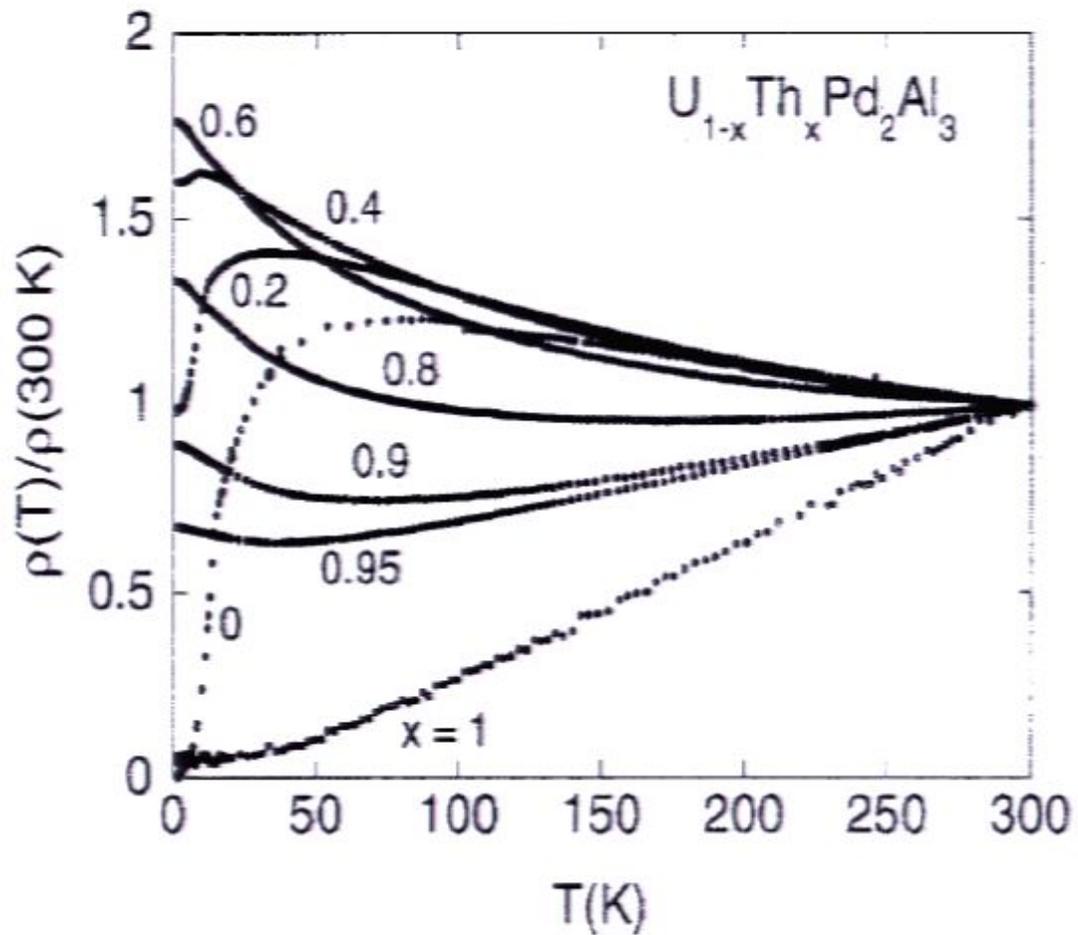
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# Non-Fermi-liquid thermodynamic properties

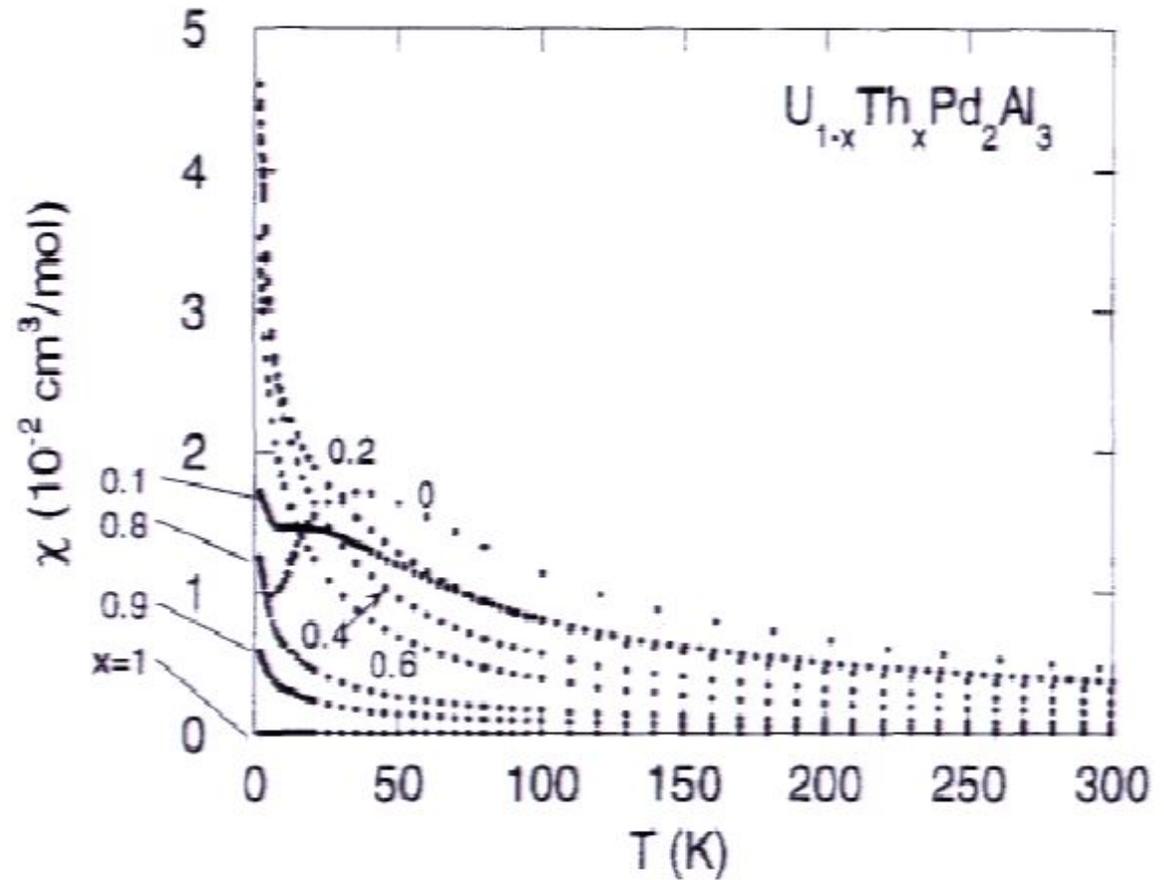
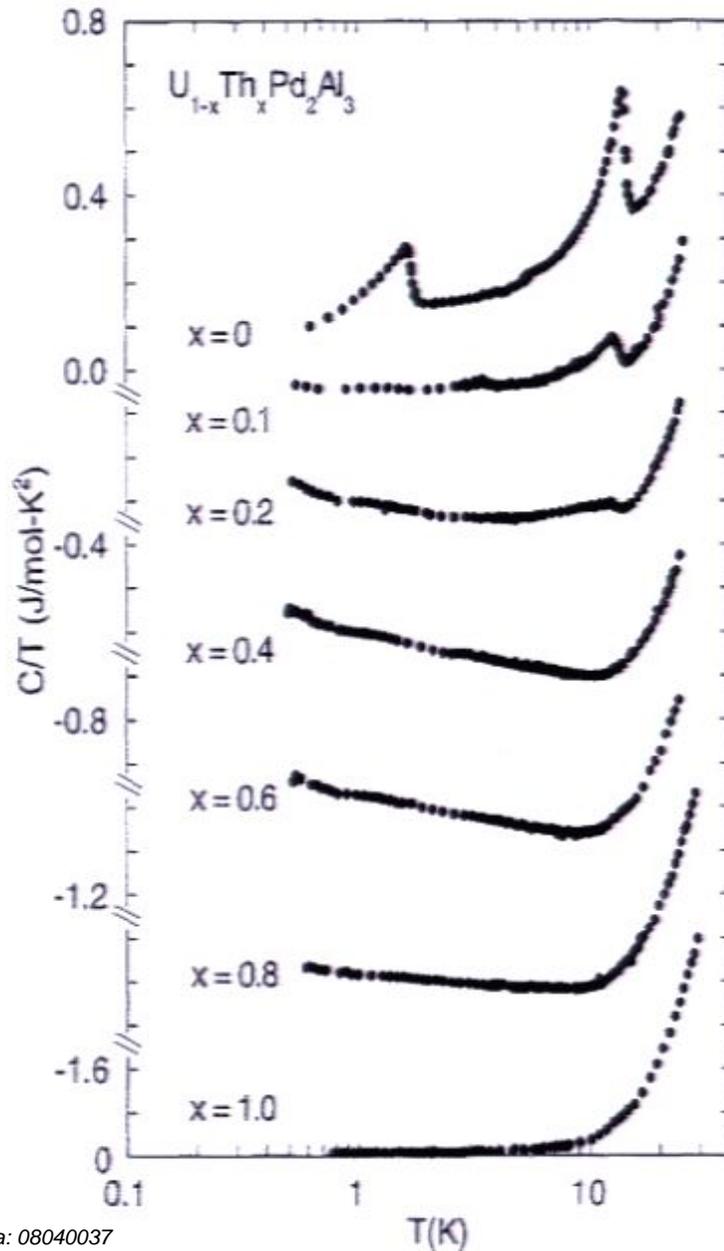


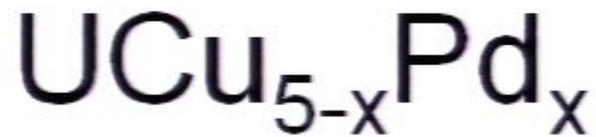
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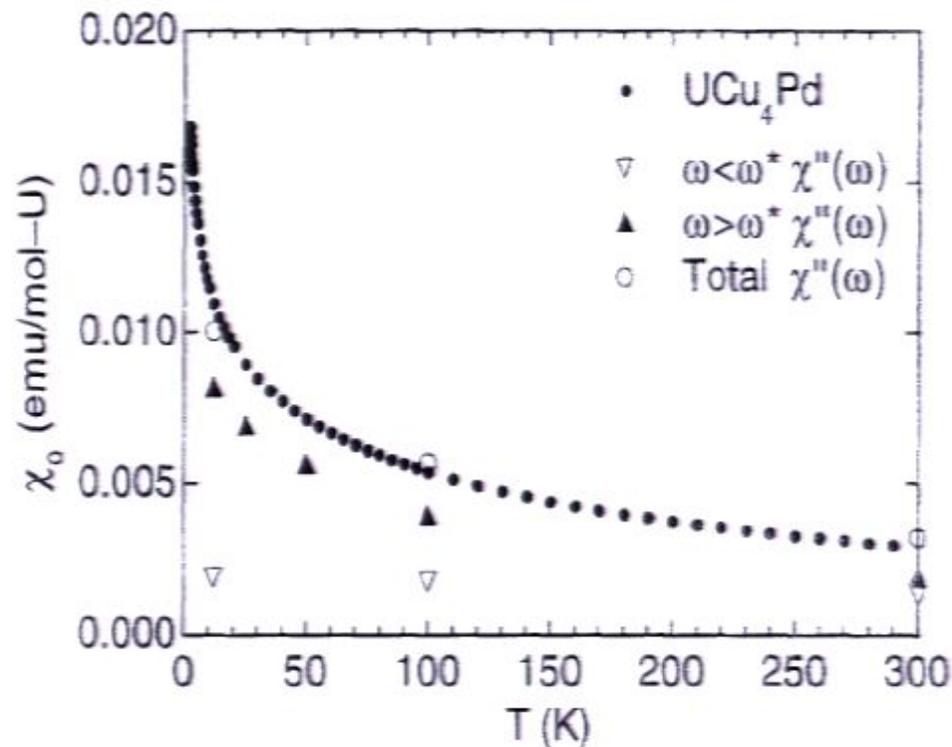


# NFL thermodynamic properties





- UCu<sub>5</sub> has  $T_N = 15$  K,  $T_K = 100$  K
- UCu<sub>3.5</sub>Pd<sub>1.5</sub> and UCu<sub>4</sub>Pd have no long range order, and show the same NFL behaviour as Y<sub>1-x</sub>U<sub>x</sub>Pd<sub>3</sub>



# Overview of NFL properties

Table 2. Examples of f-electron systems which exhibit characteristic non Fermi liquid behavior in the low temperature electrical resistivity  $\rho(T) \sim 1 - aT/T_0$ , specific heat  $C(T)/T \sim (-1/T_0) \ln(T/bT_0)$ , and magnetic susceptibility  $\chi(T) \sim 1 - c(T/T_0)^{1/2}$ .

System	$\rho$	$C/T$	$\chi$	$T_0^*$ (K)
$\text{La}_{0.9}\text{Ce}_{0.1}\text{Cu}_2\text{Si}_2$	yes	yes	—	9
$\text{M}_{1-x}\text{U}_x\text{Pd}_3$ (M = Sc, Y)	yes	yes	yes	40-220
$\text{UCu}_{3.5}\text{Pd}_{1.5}$	yes	yes	yes	28
$\text{U}_{1-x}\text{Th}_x\text{Pd}_2\text{Al}_3$	yes	yes	yes	20
$\text{M}_{0.1}\text{U}_{0.9}\text{Ni}_2\text{Al}_3$ (M = Pr, Th)	—	yes	yes	200
$\text{Ce}_{1-x}\text{Th}_x\text{RhSb}$	—	yes	—	33
$\text{Th}_{1-x}\text{U}_x\text{Ru}_2\text{Si}_2$	( $a < 0$ )	yes	$-\ln(T/bT_K)$	11
$\text{U}_{0.9}\text{Th}_{0.1}\text{Be}_{13}$	( $a < 0$ )	yes	yes	8
$\text{CeCu}_{5.9}\text{Au}_{0.1}$	( $a < 0$ )	yes	yes	3.5

\*Deduced from the slope  $A = d(C/T)/d \ln T$  of the logarithmic divergence in the specific heat:  $T_0 = -0.251 R/A$

# Summary:

- These doped systems, both dilute and concentrated show:

$$\rho(T) = \rho_0 - AT^1$$

$$\chi(T) = \chi_0 (1 - c\sqrt{T/T_K})$$

$$C(T)/T = -\ln(T/T_K)$$

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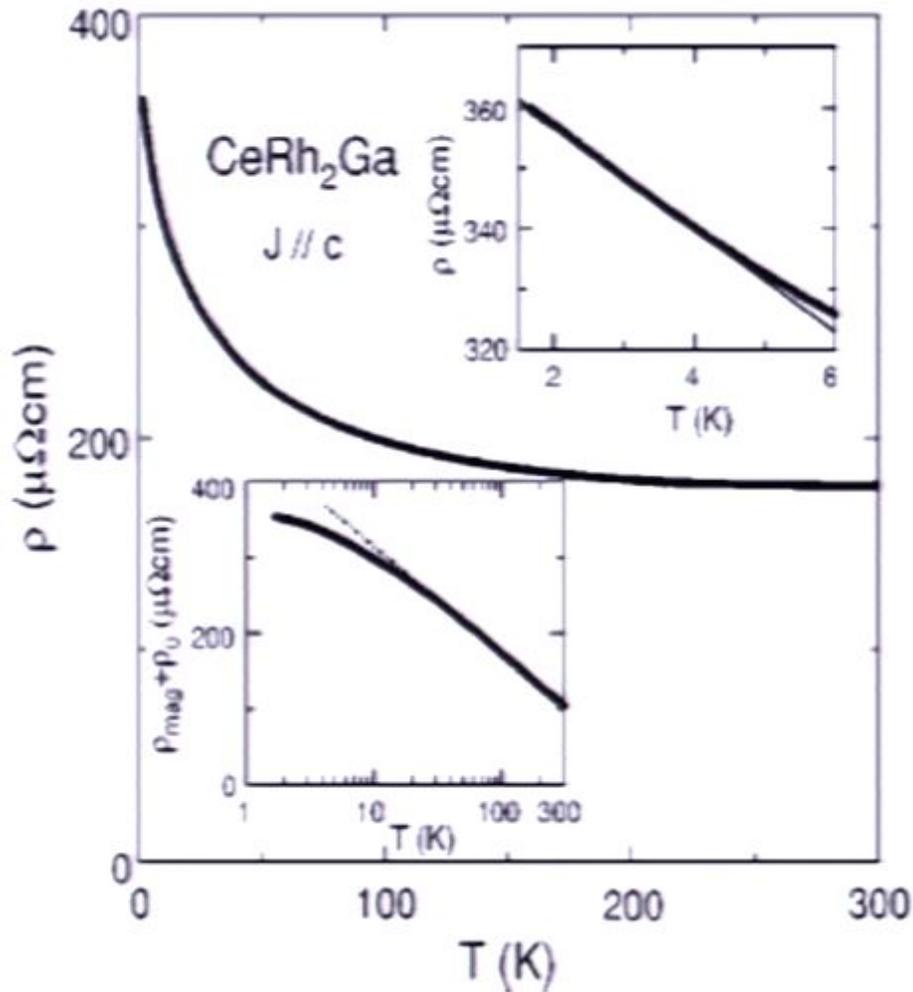
$$C(T)/T = -\ln(T/T_K)$$

***(note that it is difficult to establish these asymptotic behaviours very precisely)***

# Role of disorder in concentrated systems?

- Until recently, all of the concentrated NFL “non-metallic” systems had high levels of disorder (this may still be true)
- A long-standing model has been Griffiths phase physics (Castro-Neto; Sachdev; Millis, Morr and Schmalian)
- Even stoichiometric materials are interpreted this way:

# CeRh<sub>2</sub>Ge

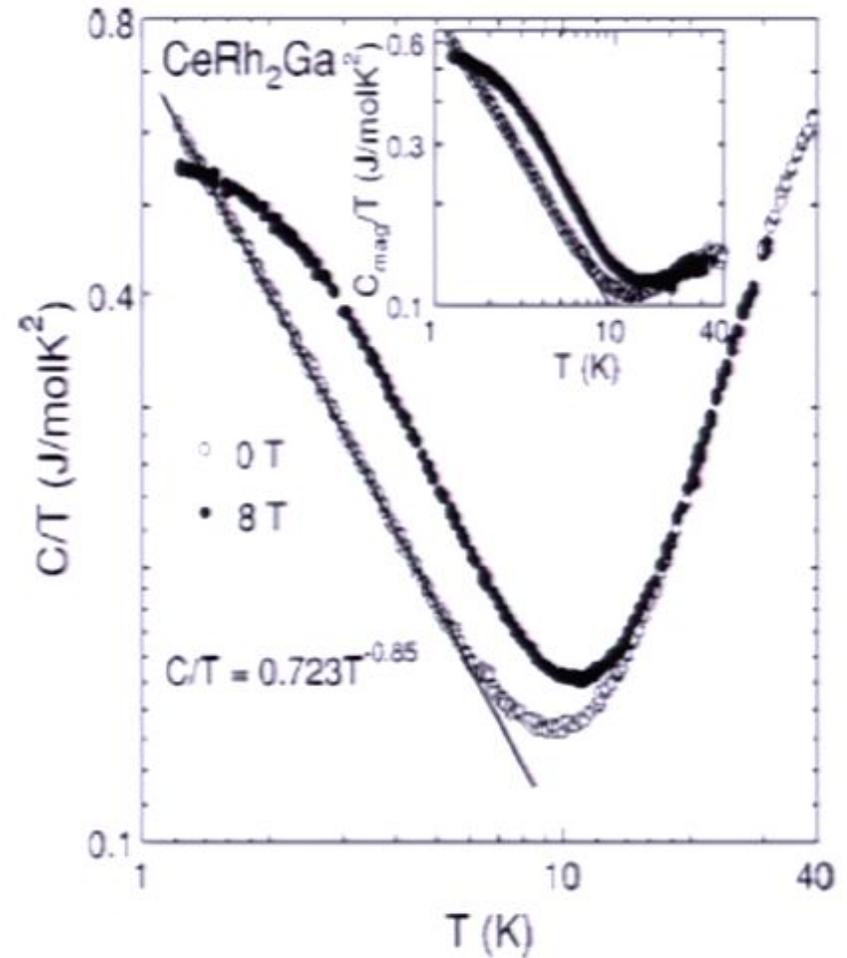
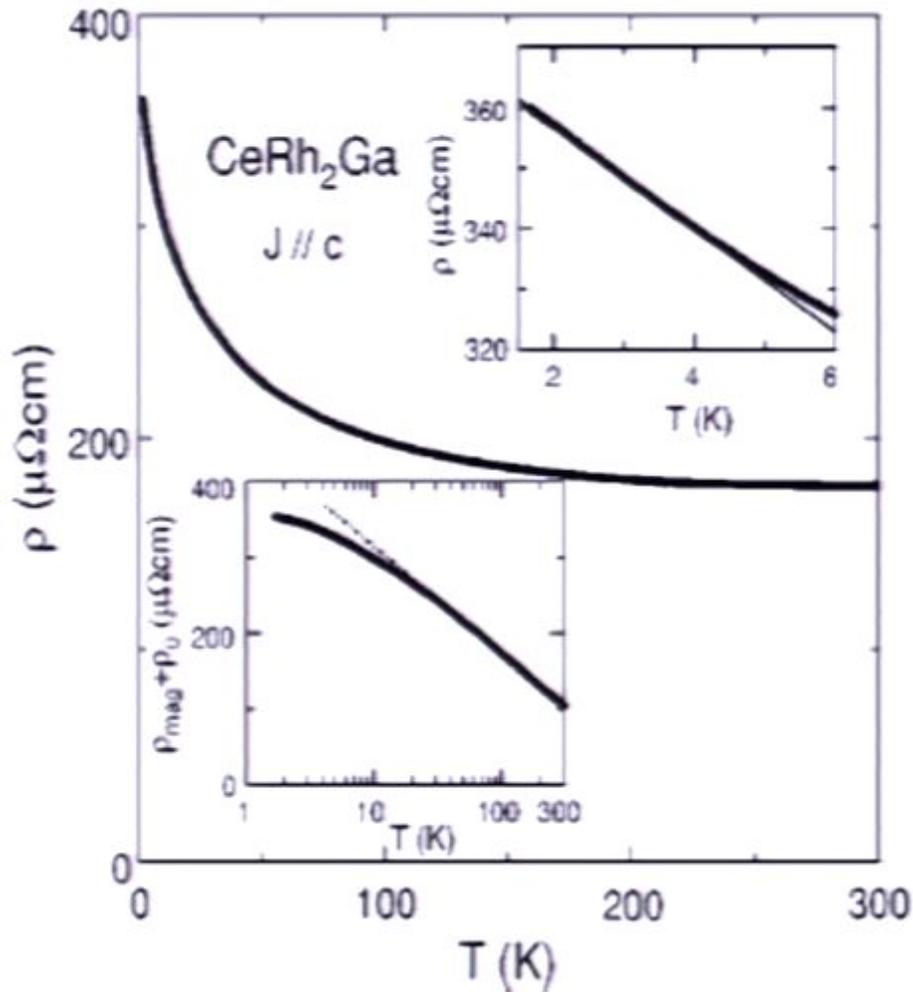


**Hexagonal crystal structure.**  
**Considerable site disorder.**

Figure 10.04.037

**Chen et al., PRB 2004.**

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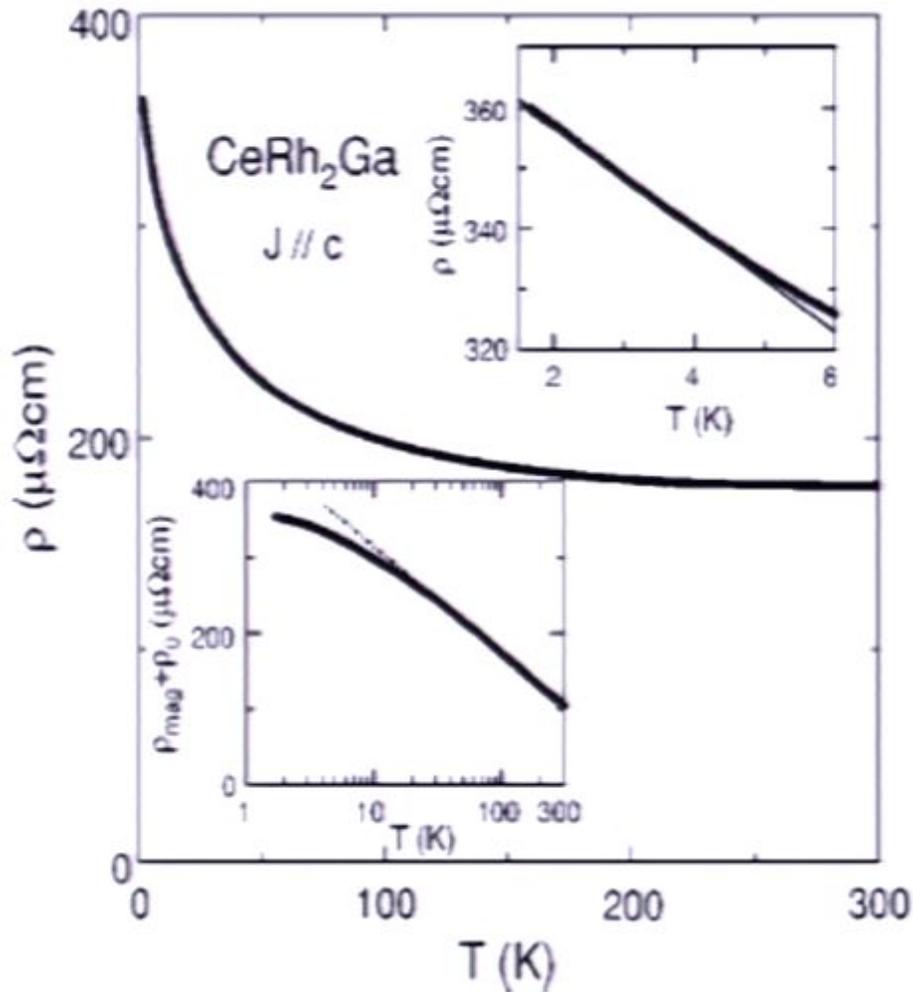


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Figure 10 of 1037

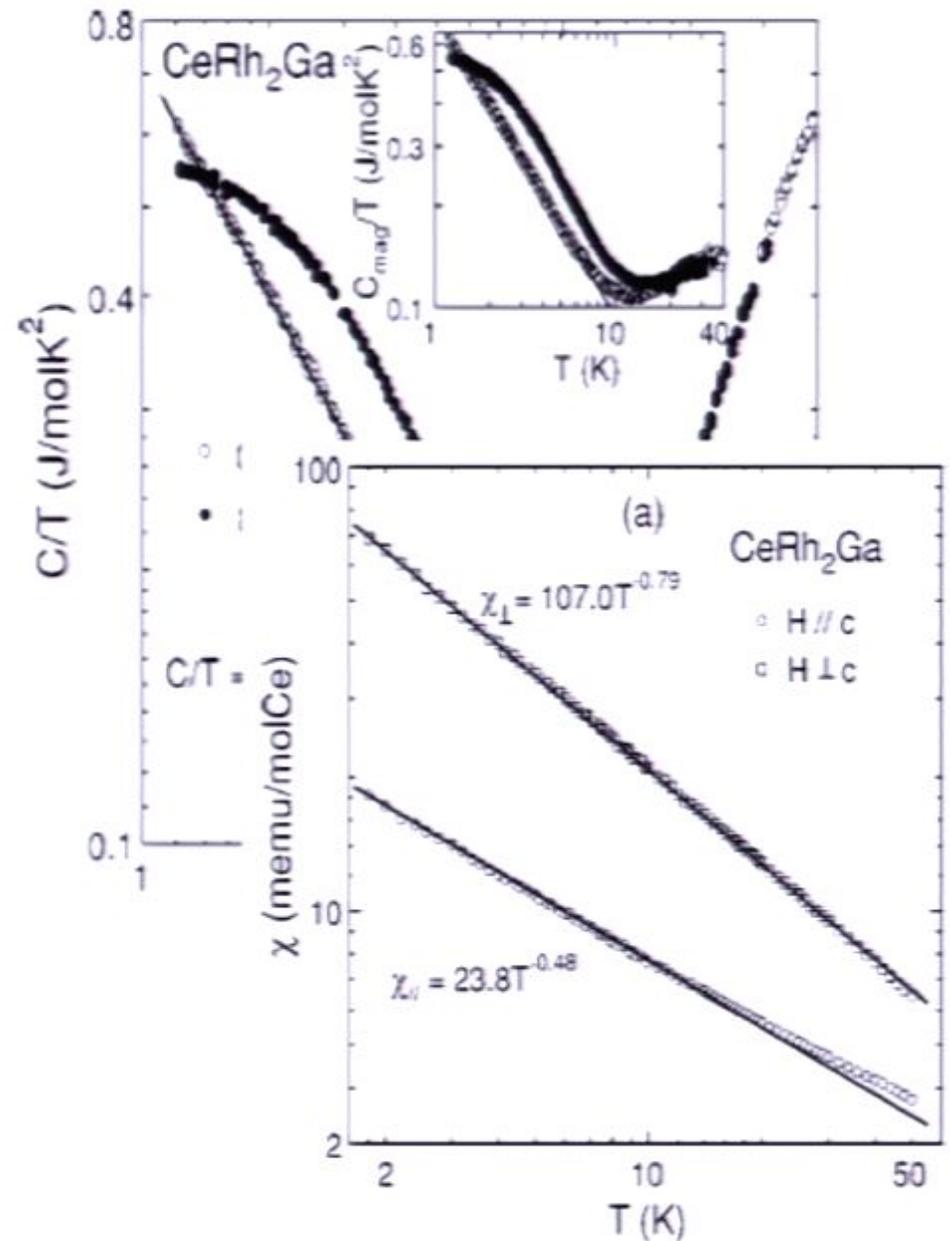
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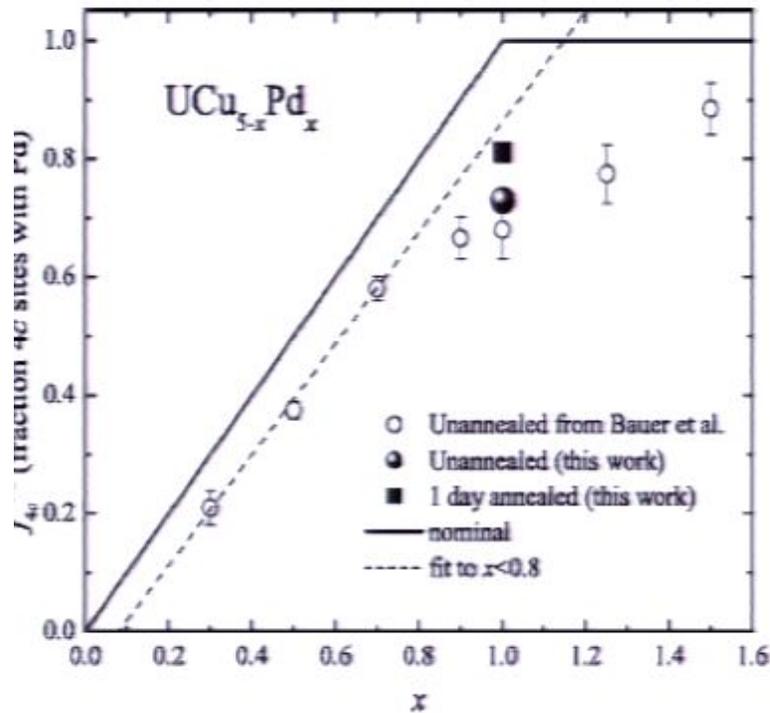
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Physica 260 (2003) 37

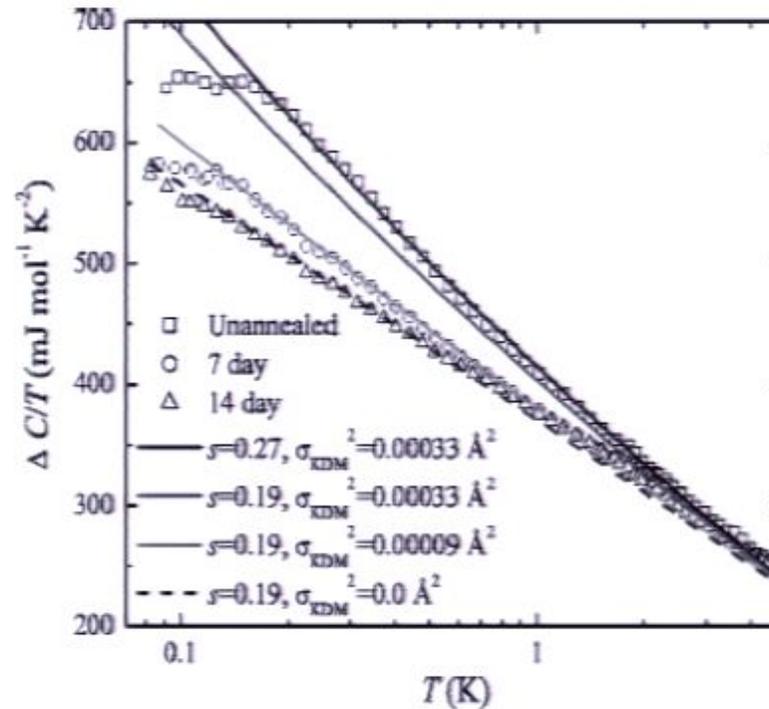


Chen et al., PRB 2004.

# Disorder effects in concentrated systems



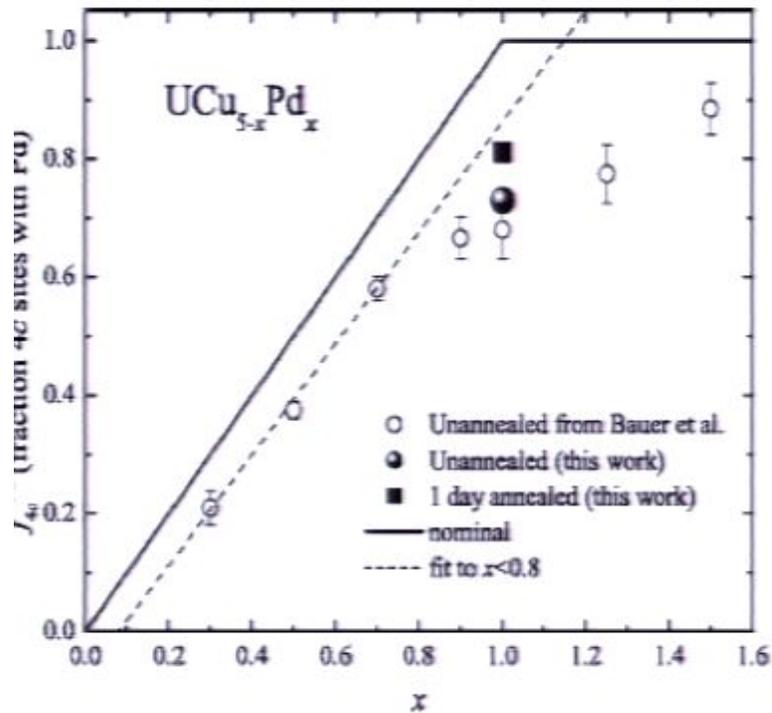
**Booth et al, PRB 2002.**



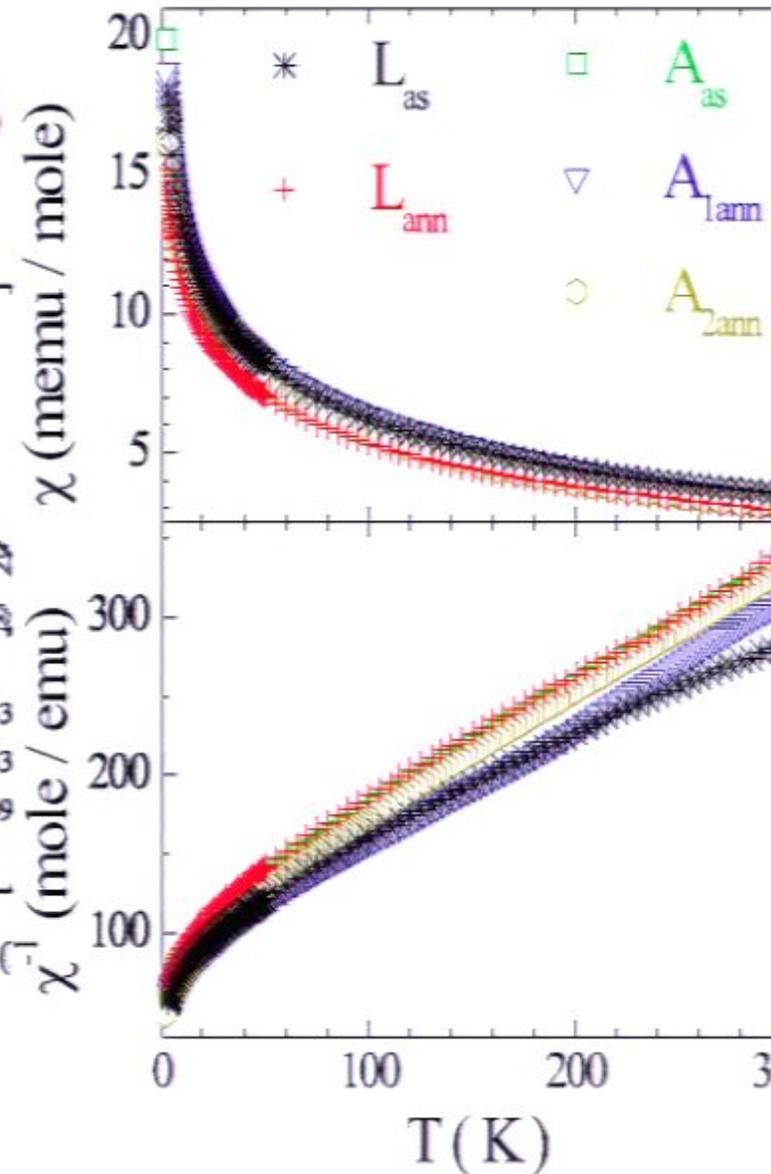
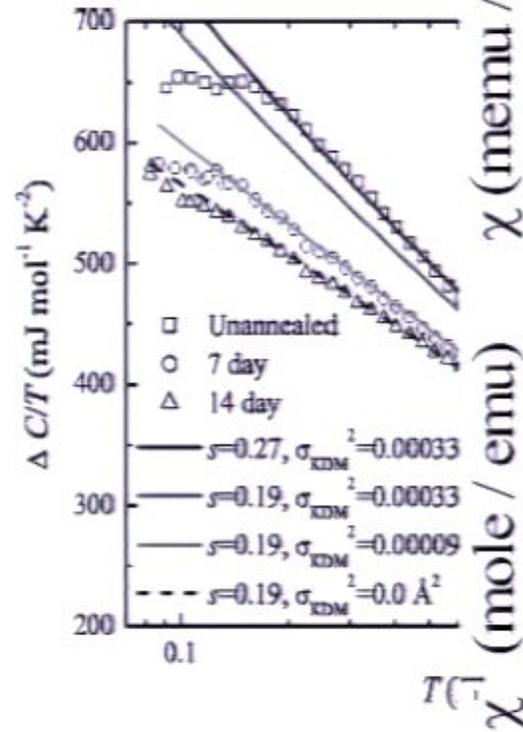
**Otop et al, PRB 2008.**

## Effect of annealing on $UCu_4Pd$ .

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Booth et al, PRB 2002.



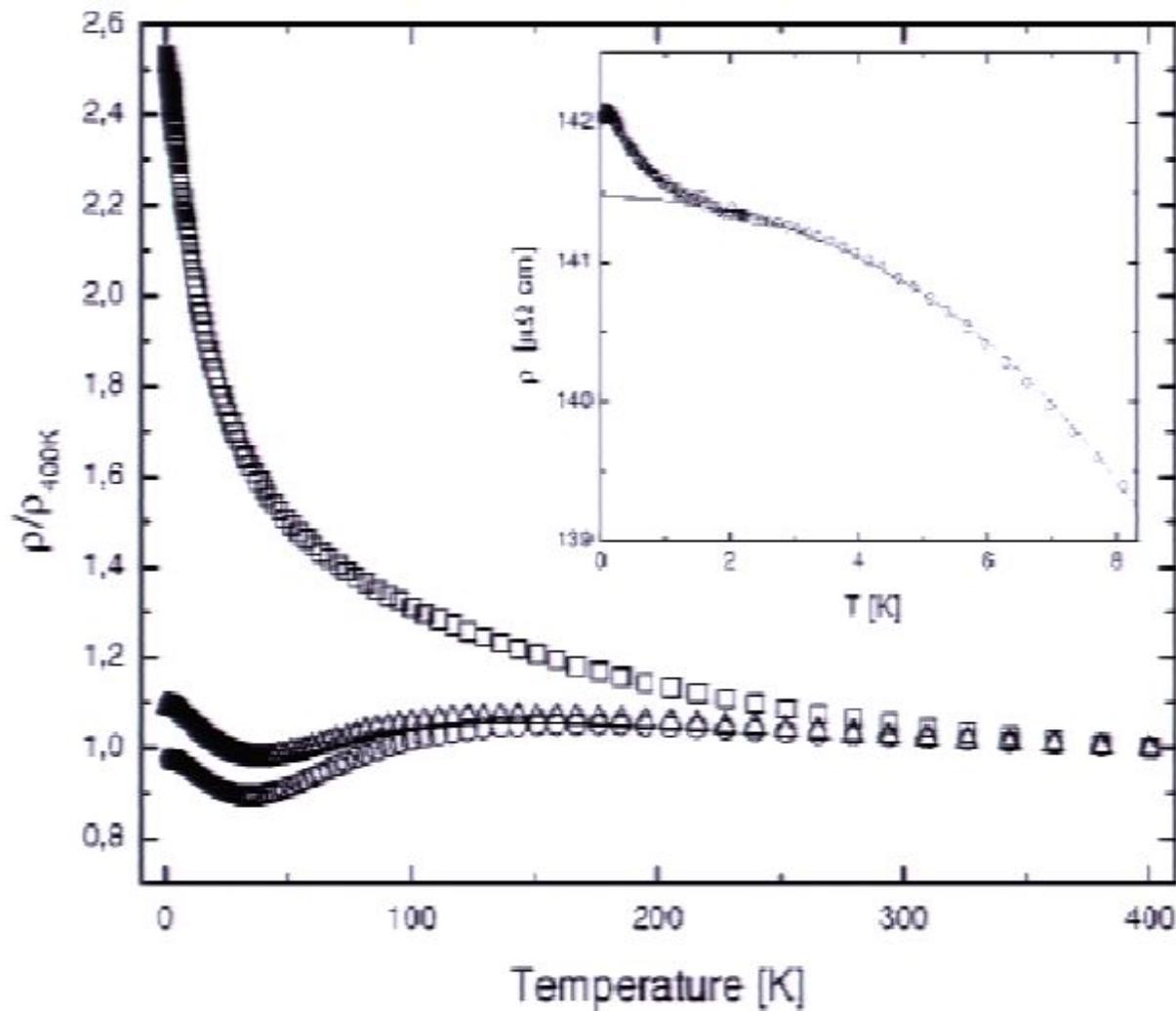
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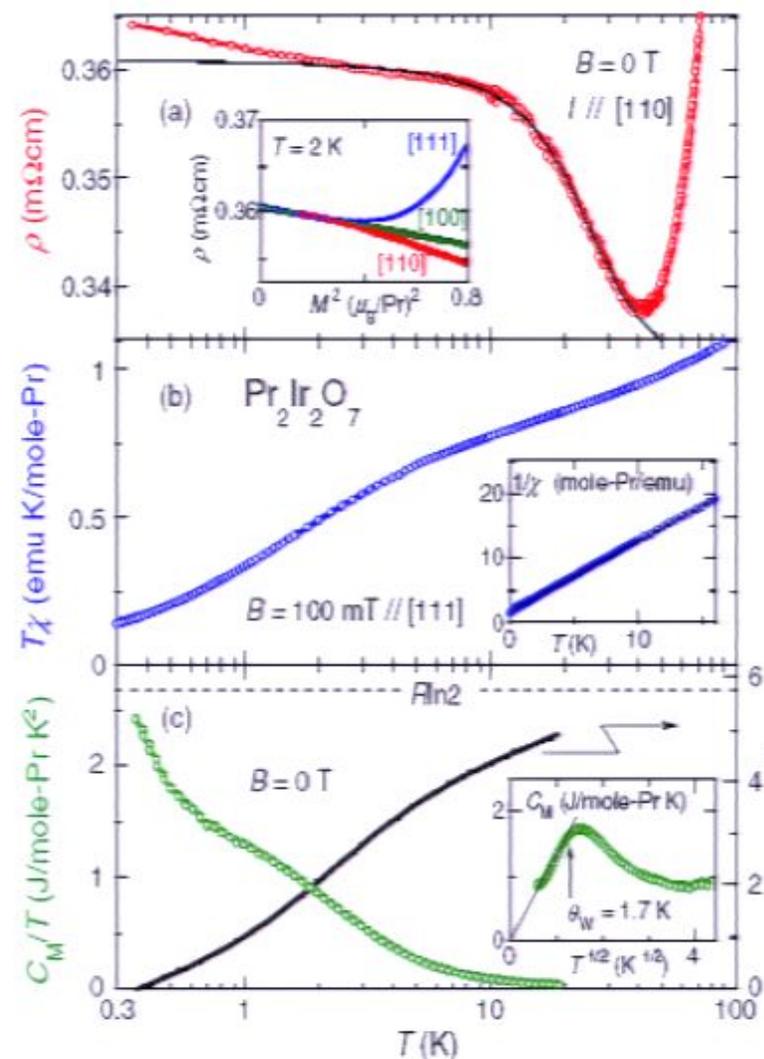
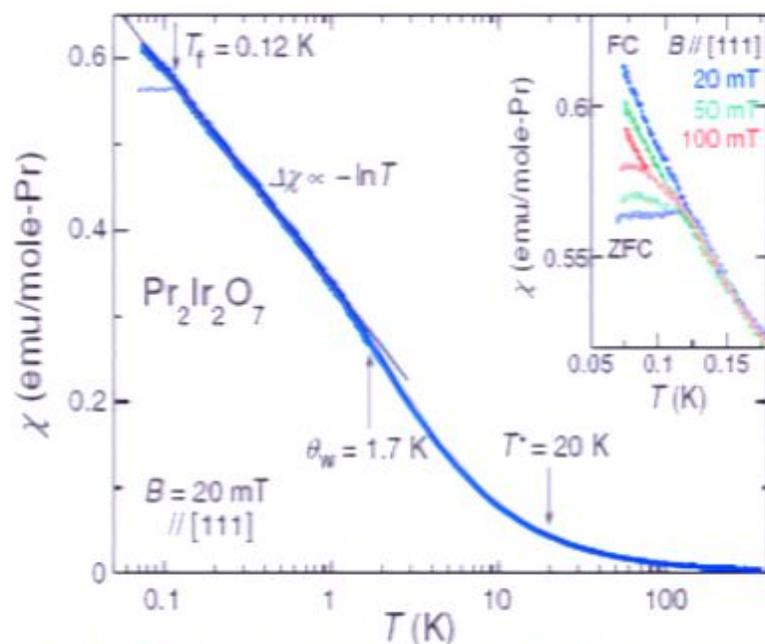
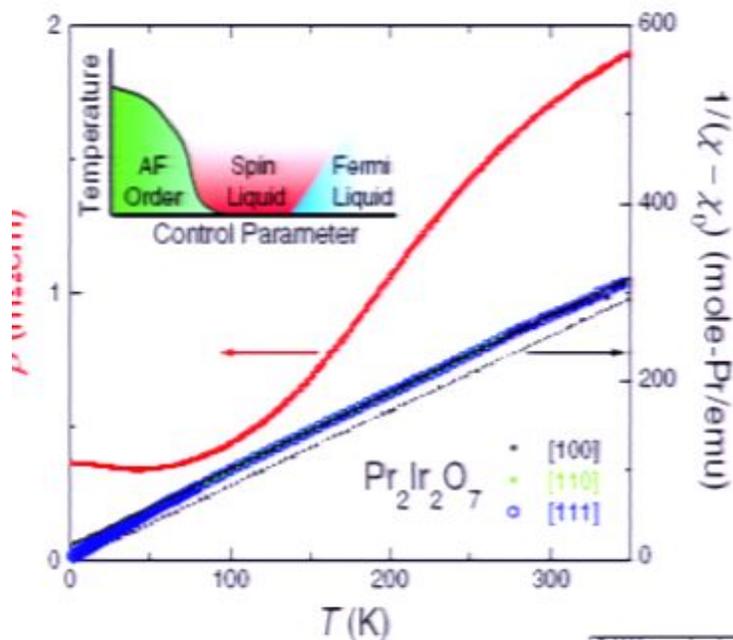
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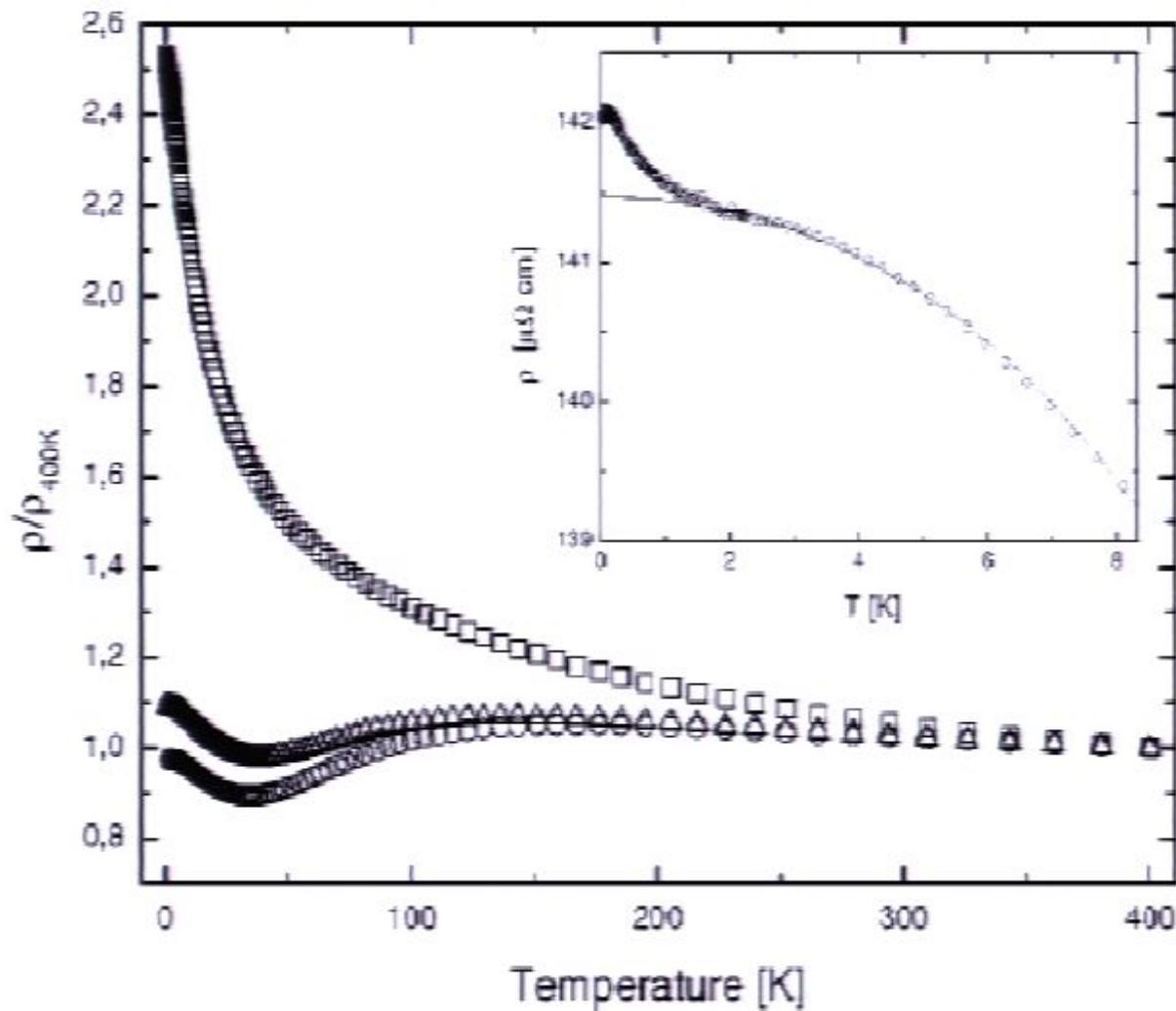
# UCu<sub>4</sub>Pd: effect of annealing on $\rho$ vs T



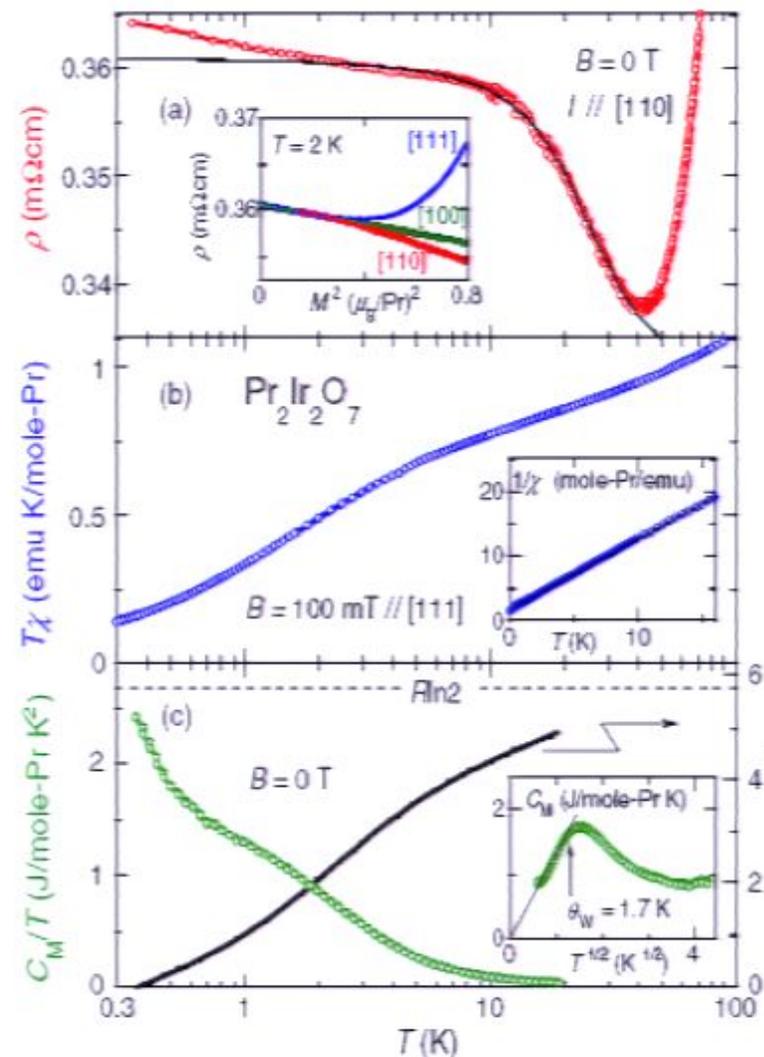
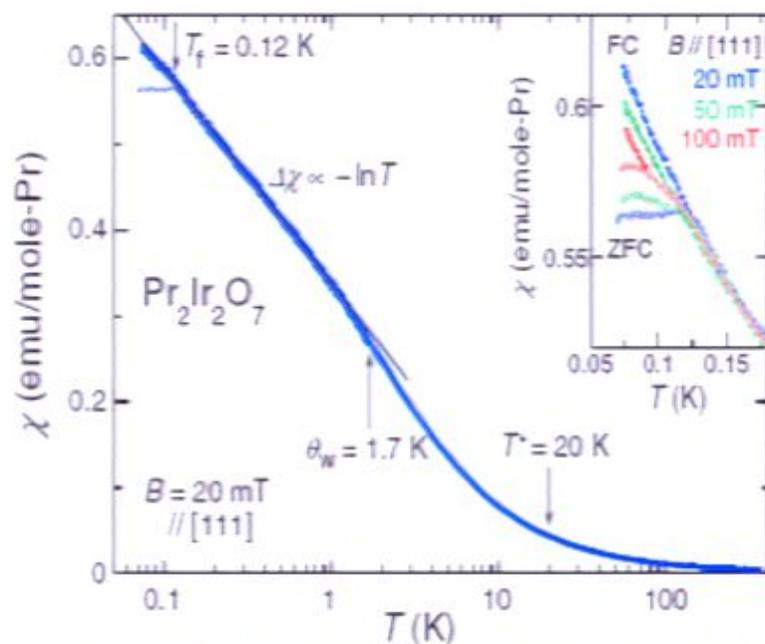
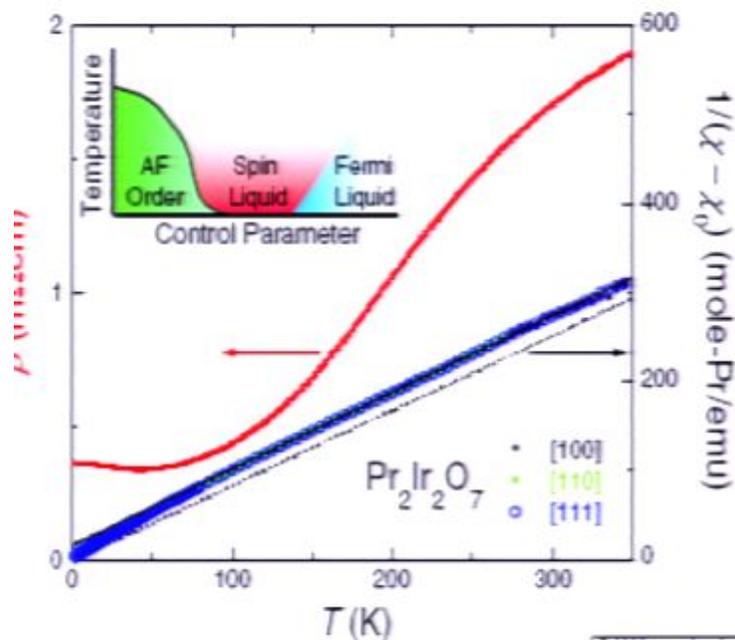
# A highly pure concentrated system: $\text{PrIr}_2\text{O}_7$



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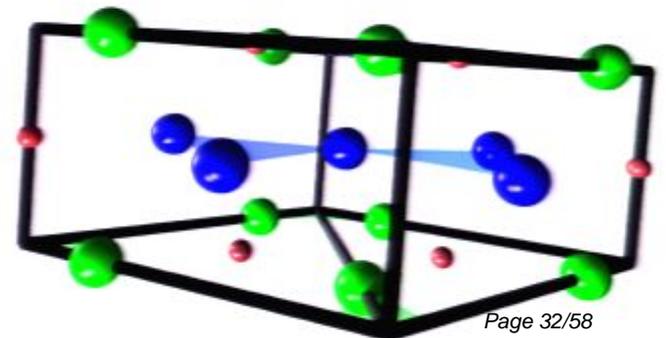
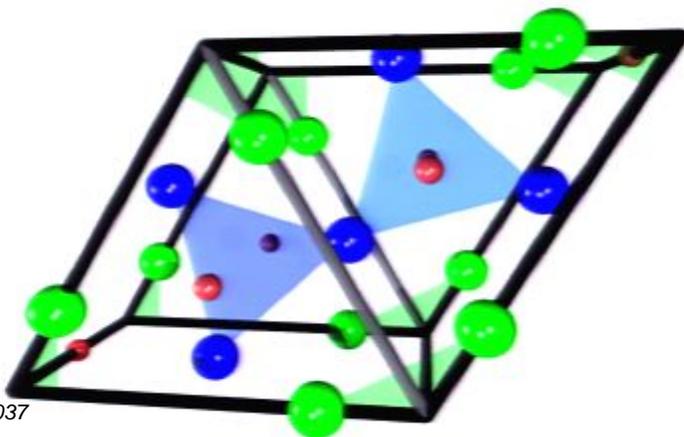


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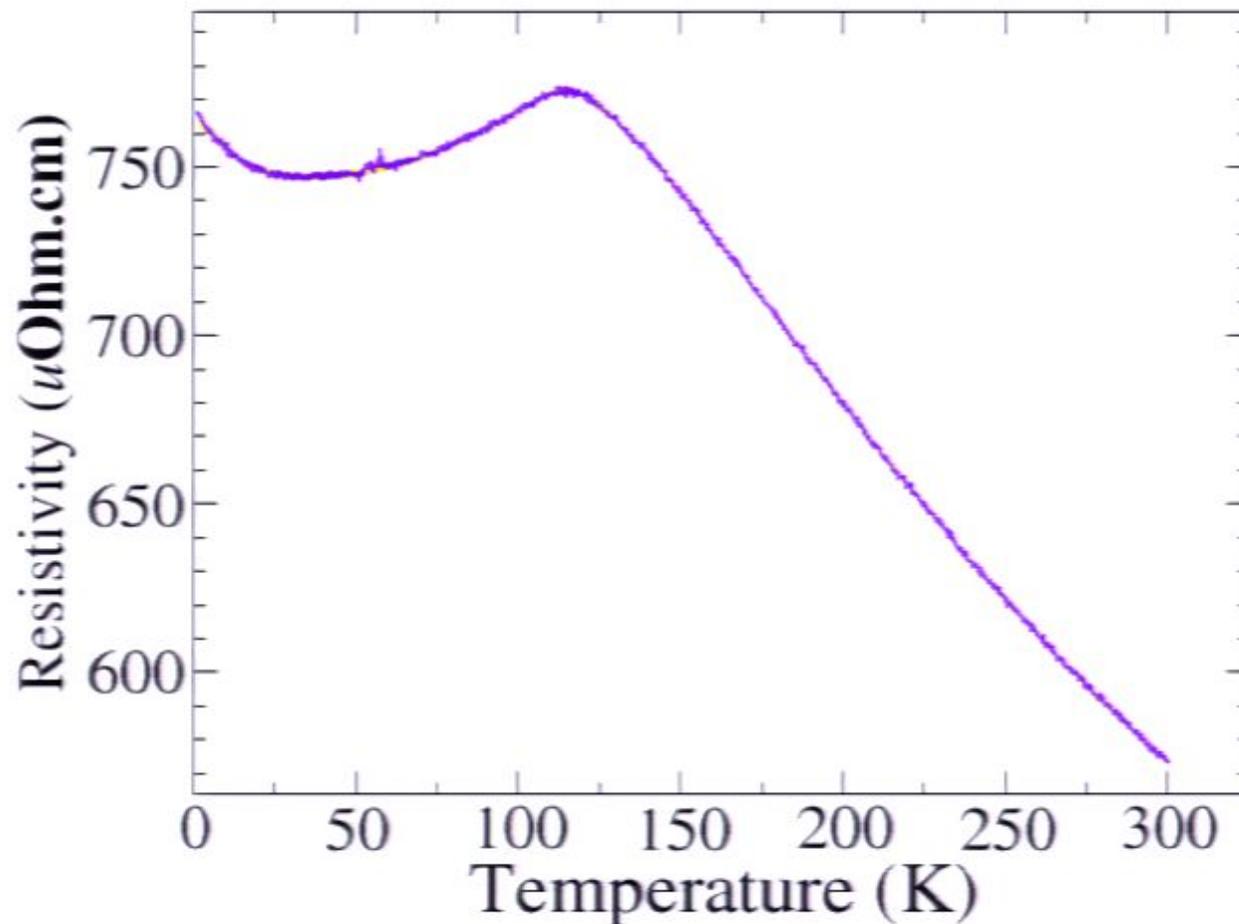


# FeCrAs: background

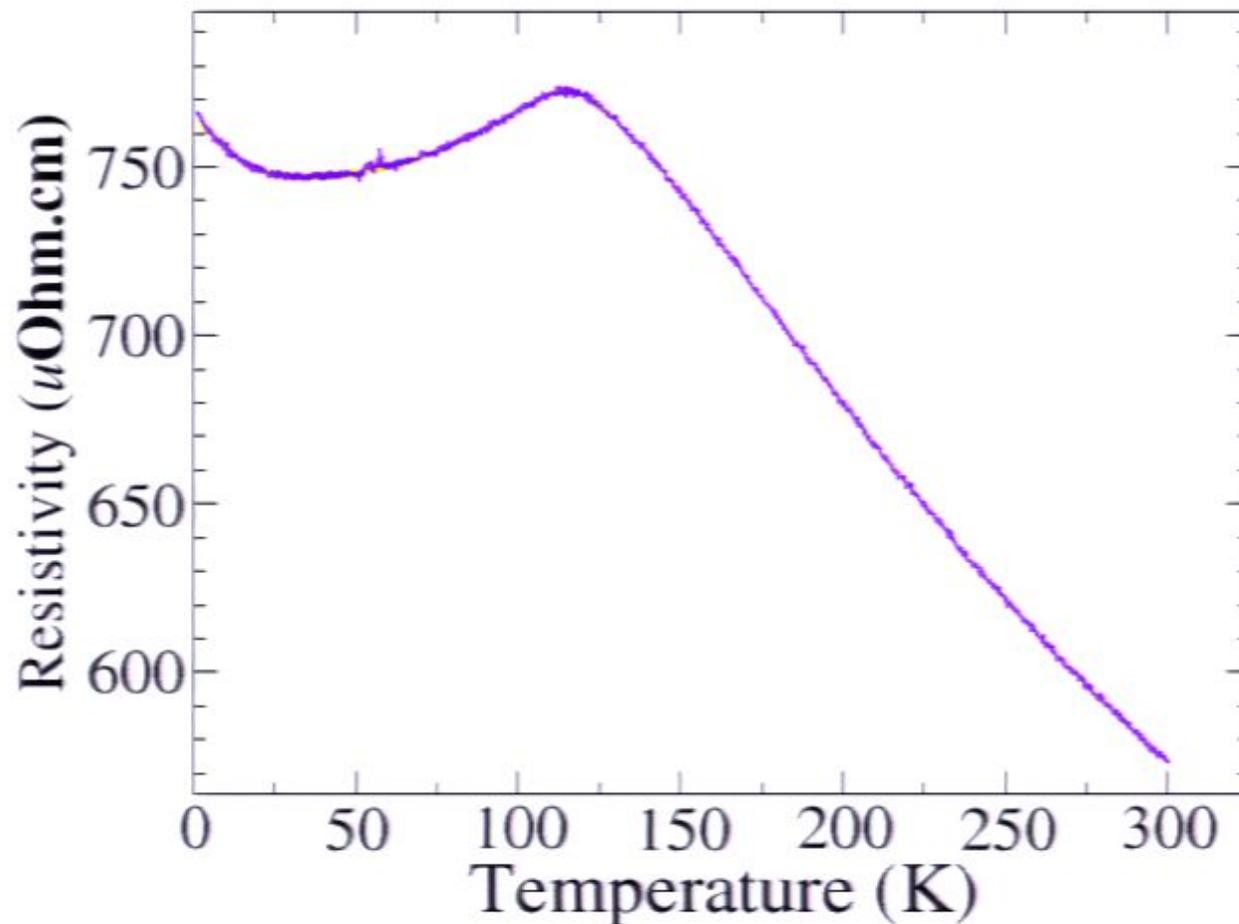
- FeCrAs is a hexagonal ( $\text{Fe}_2\text{P}$ ) member of a large ternary monopnictide family
- Most members are tetragonal, and order antiferromagnetically above room temperature
- Early (unpublished) Mossbauer work suggested no magnetic order down to 4.2K in FeCrAs



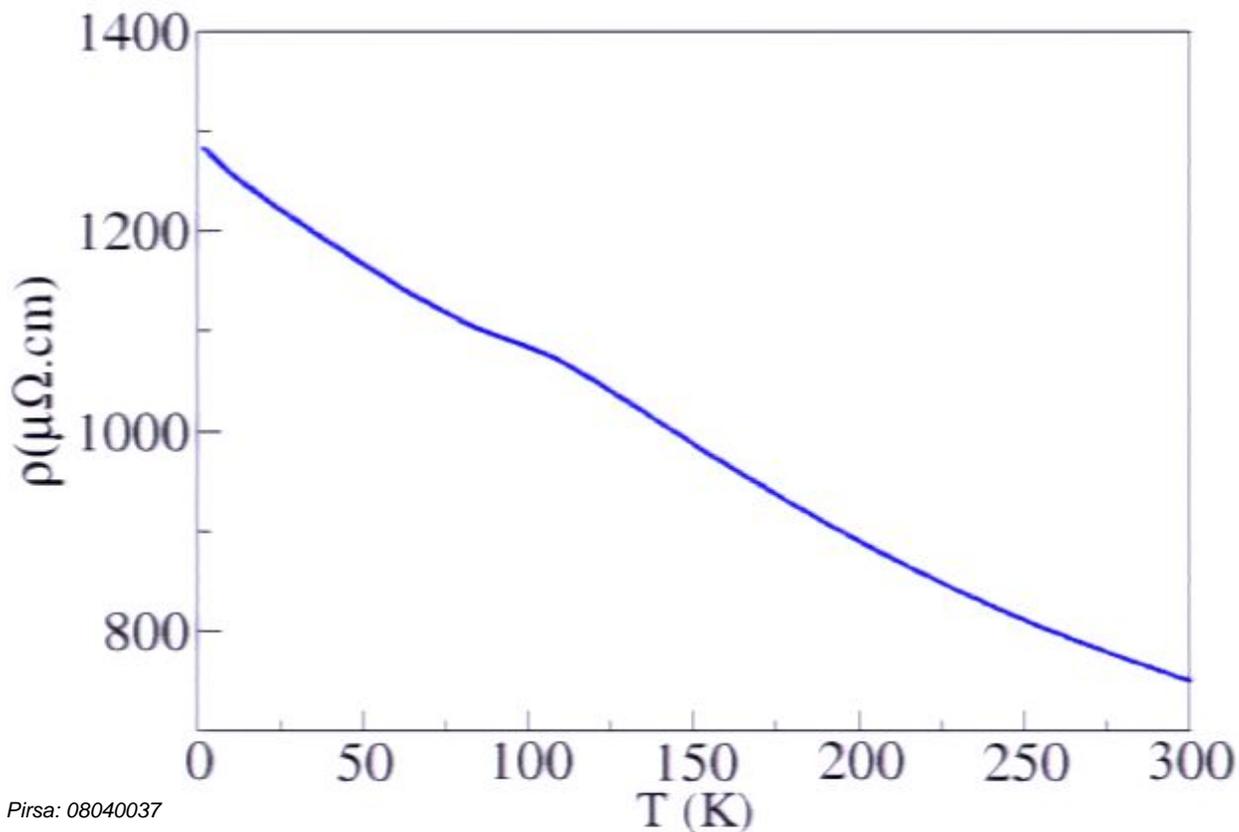
# Resistivity of polycrystalline FeCrAs (magnetic sample)



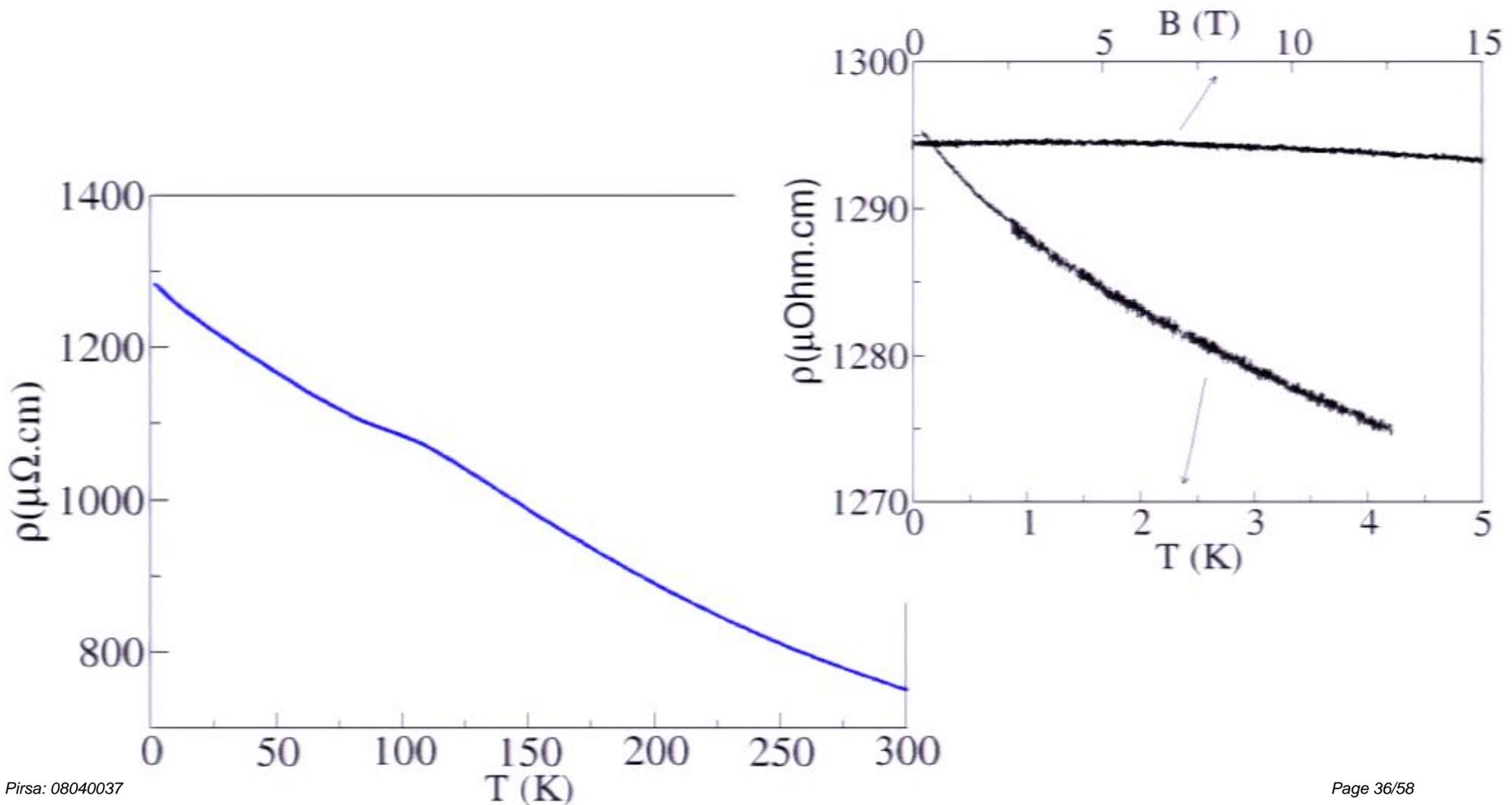
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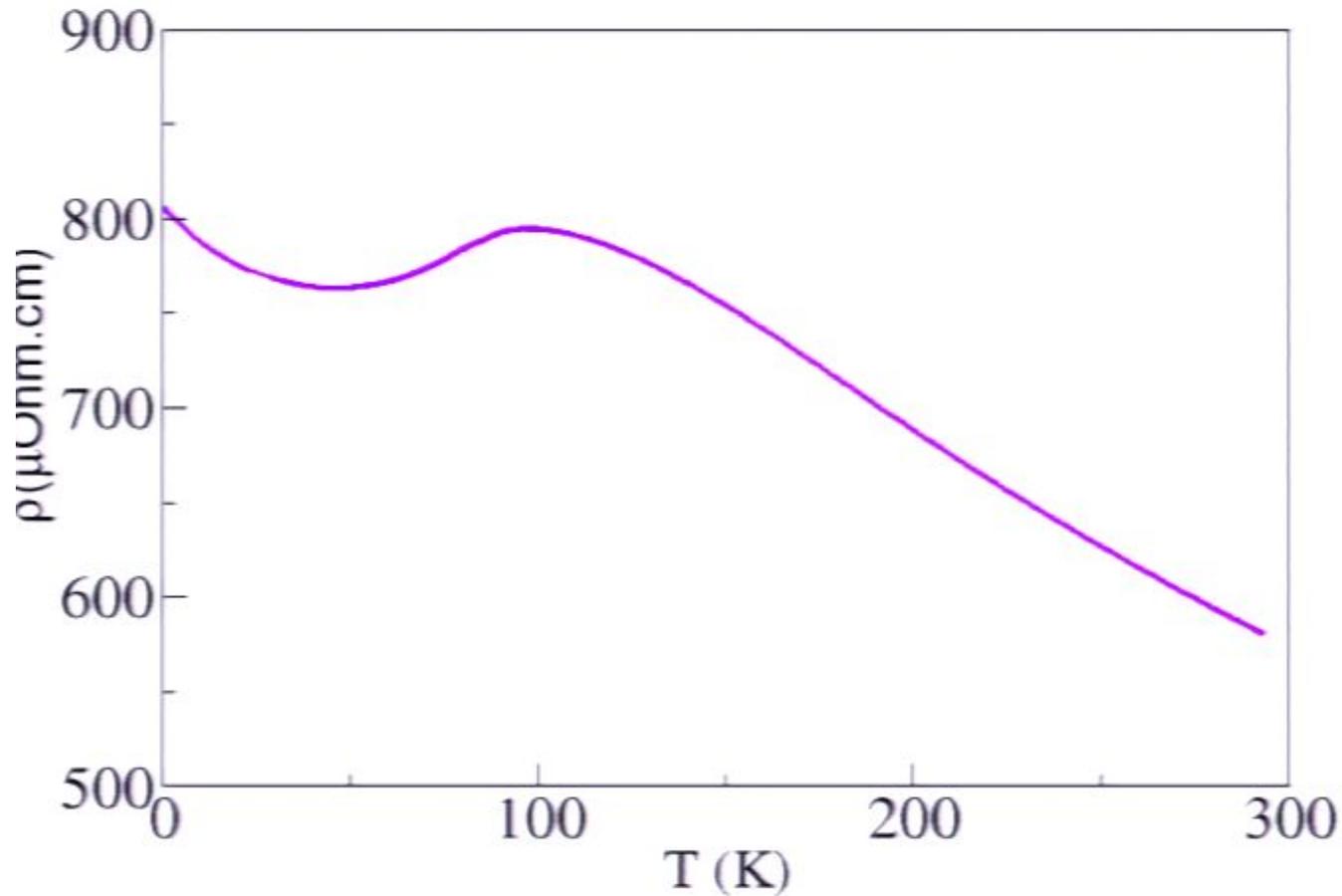
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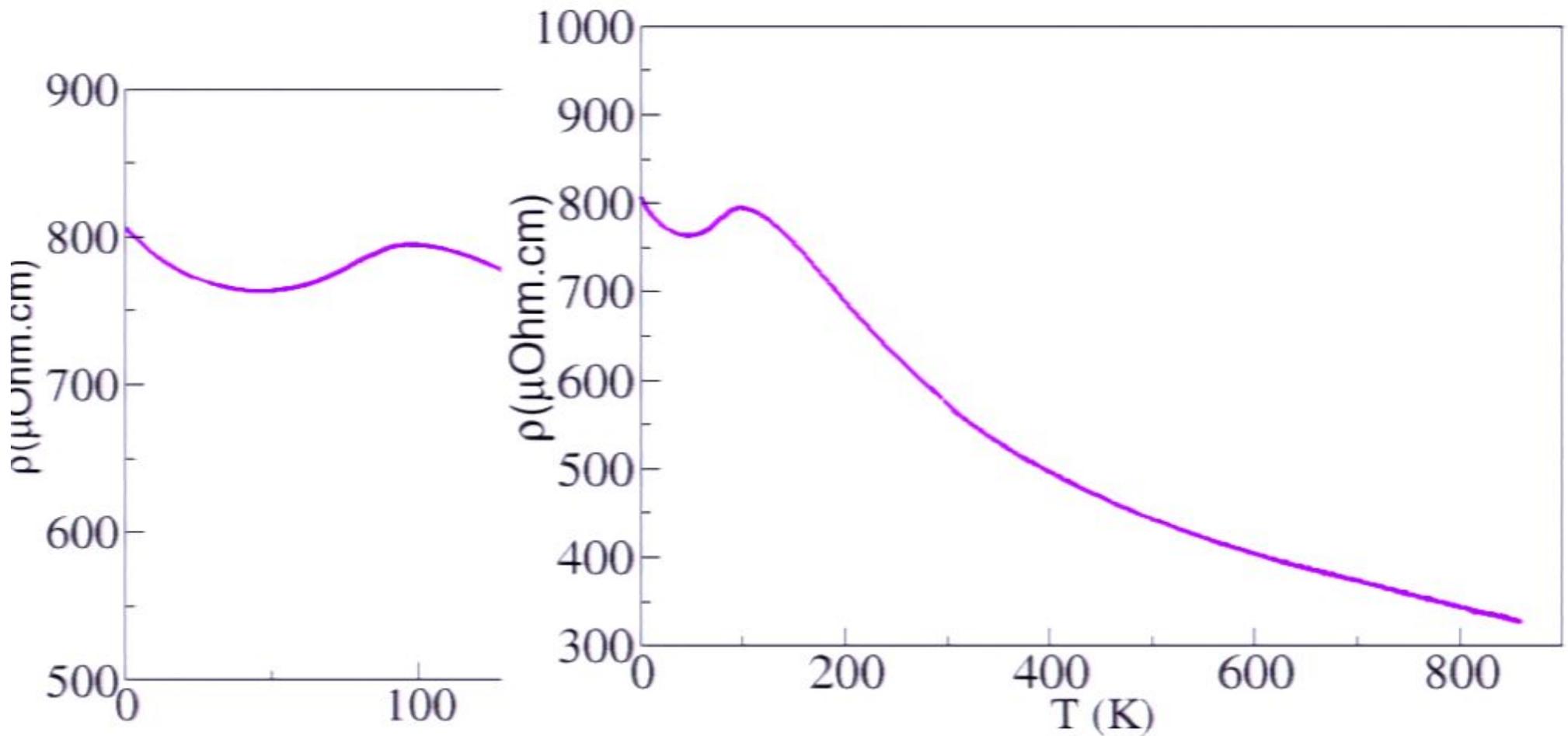
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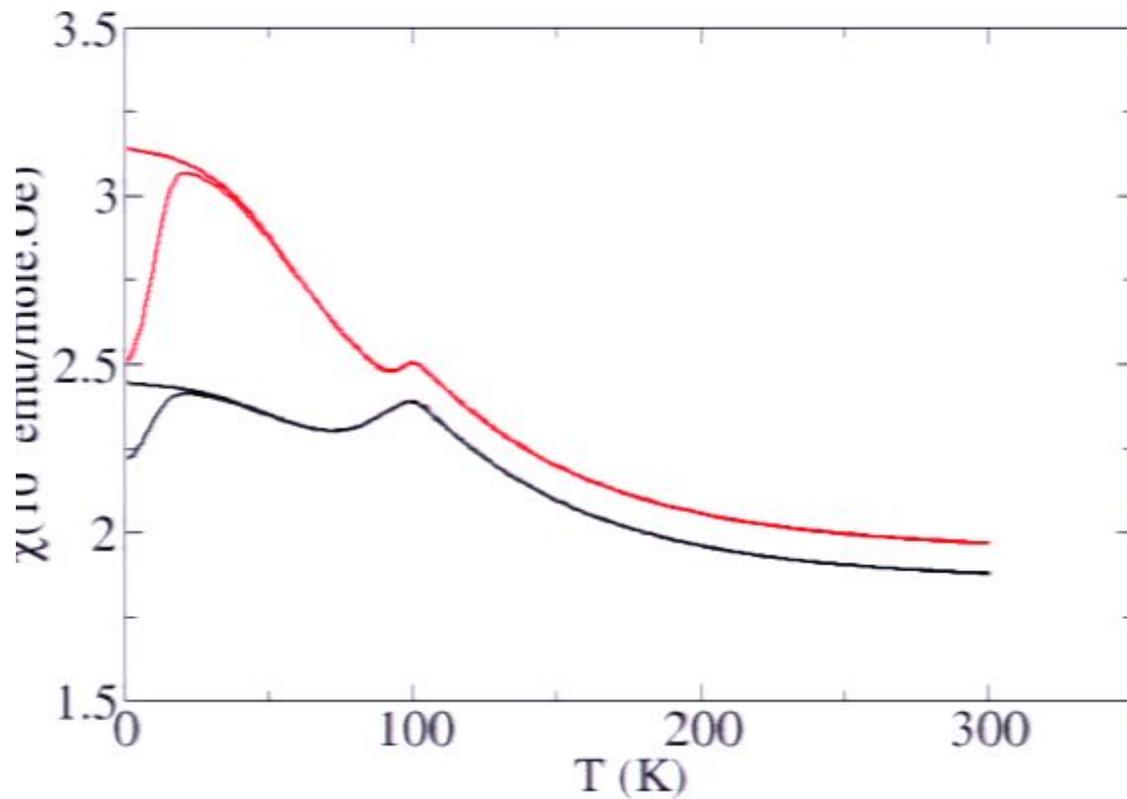
# Out-of-plane non-magnetic single crystal



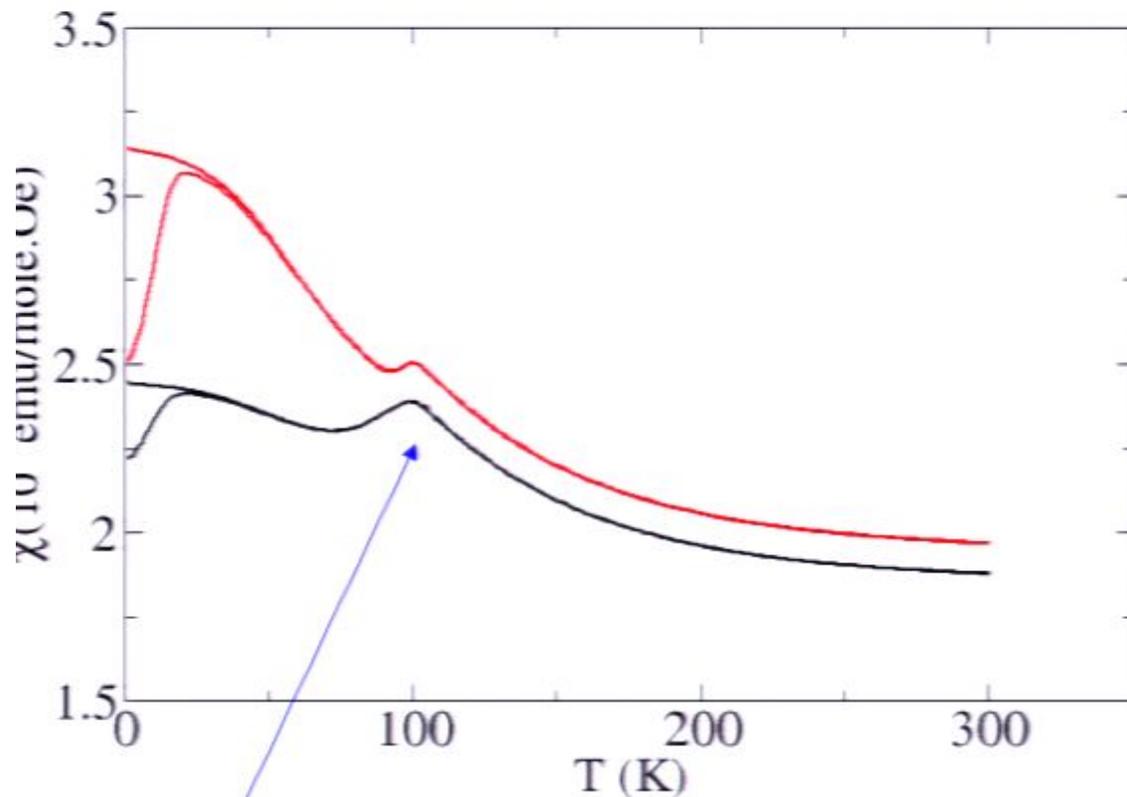
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# Magnetic susceptibility: non-magnetic sample

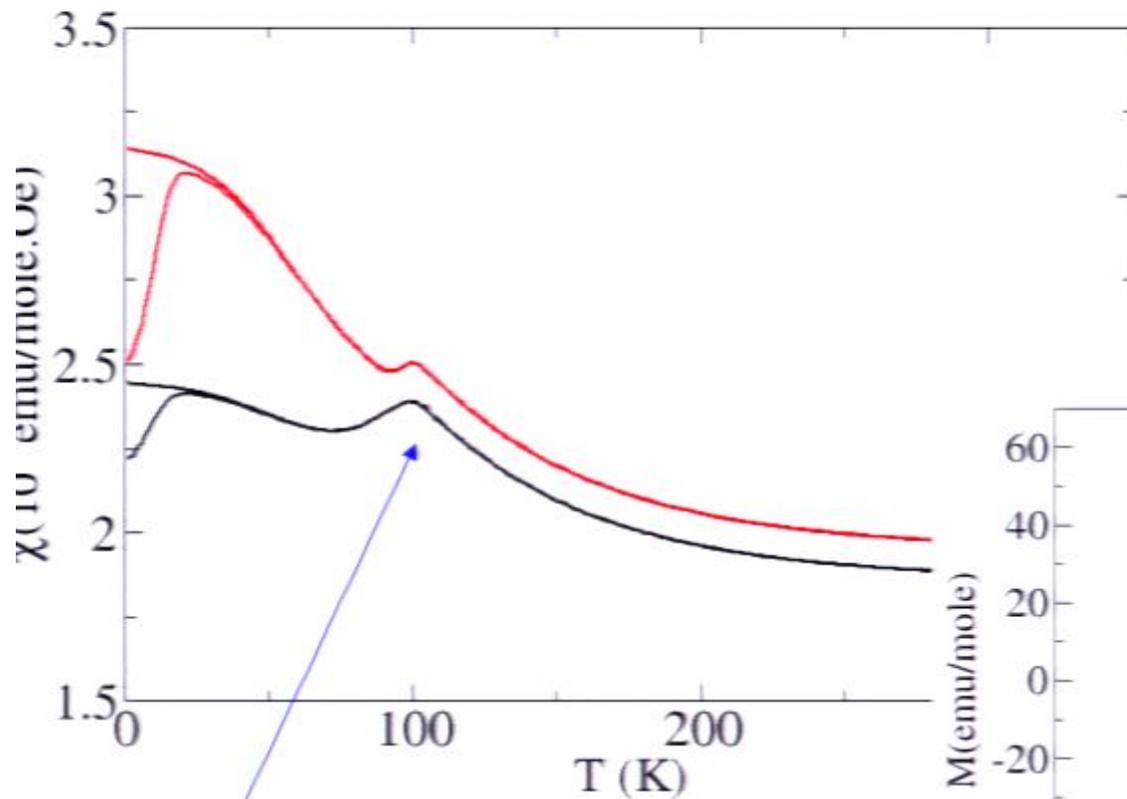


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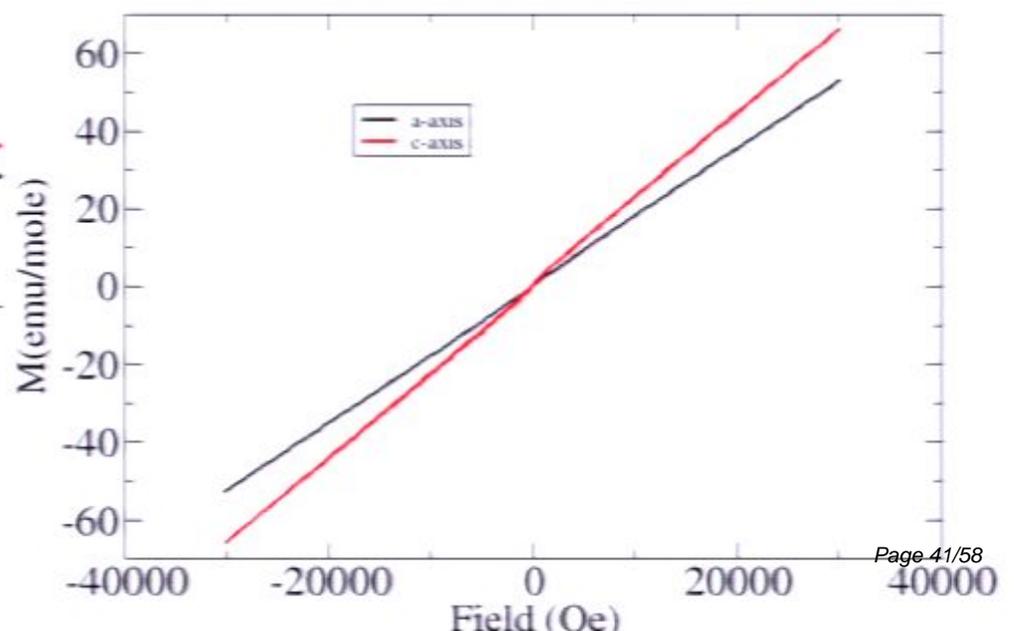
***Powder neutron diffraction  
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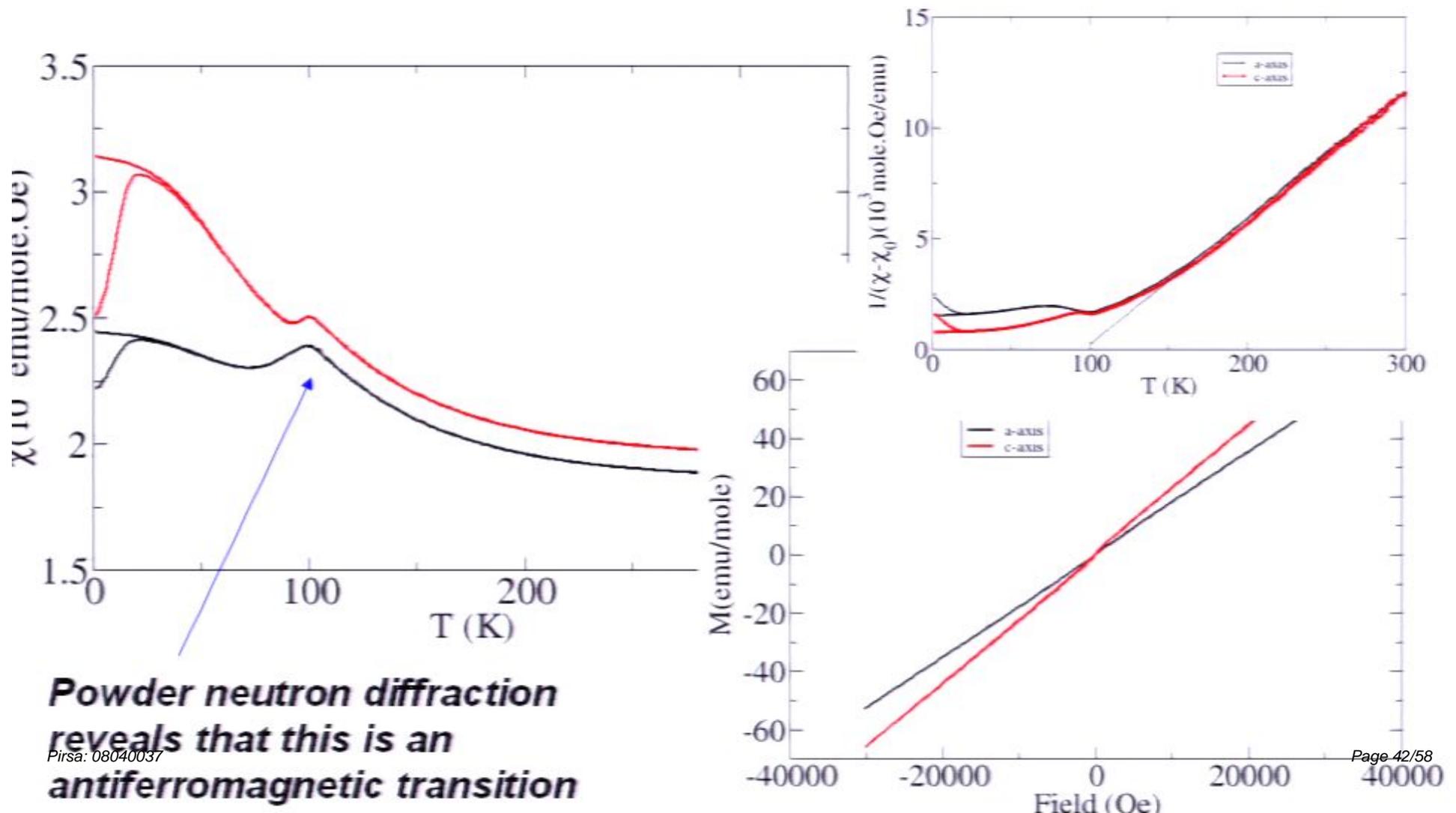
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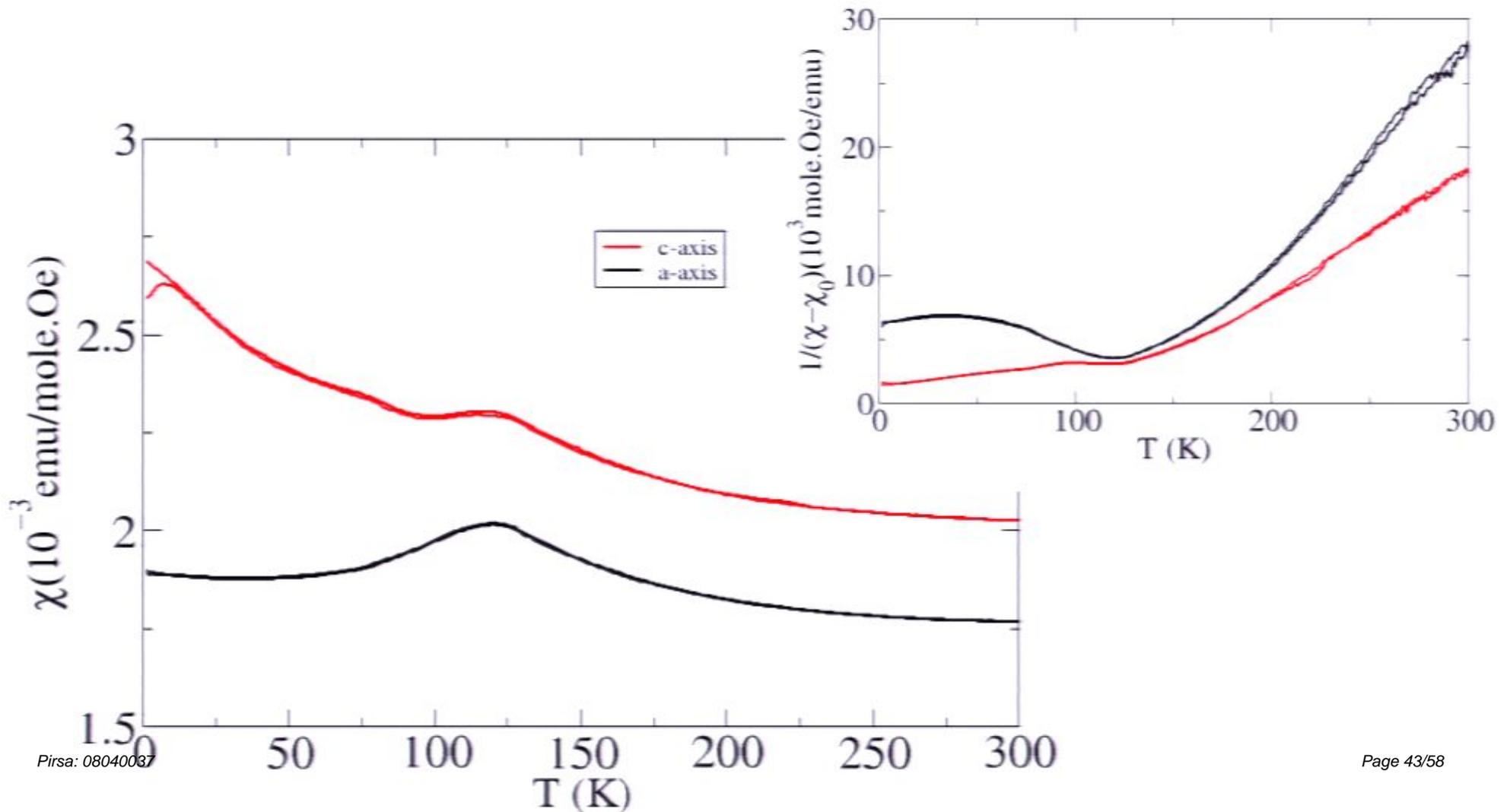
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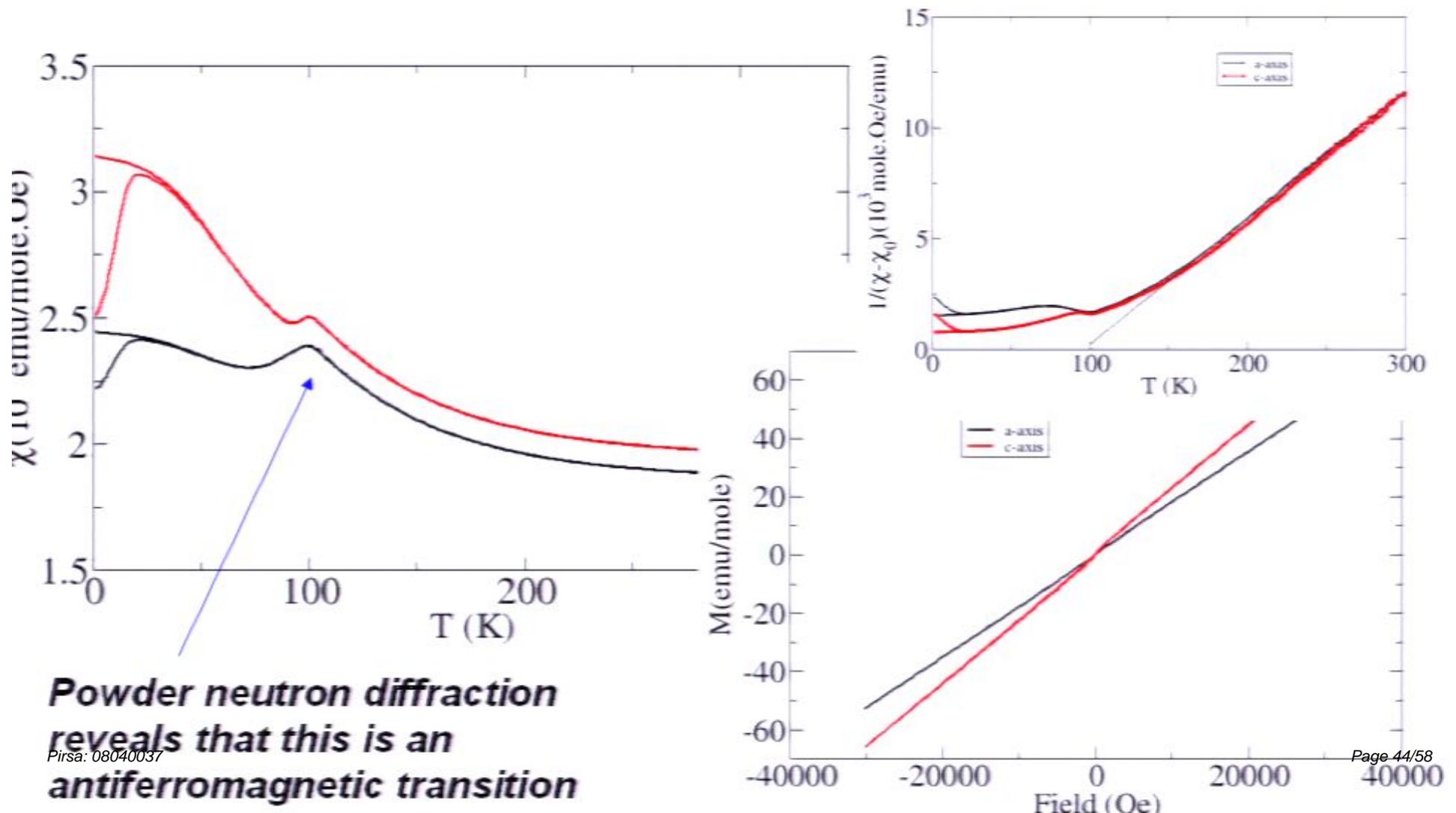


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# Non-magnetic annealed sample

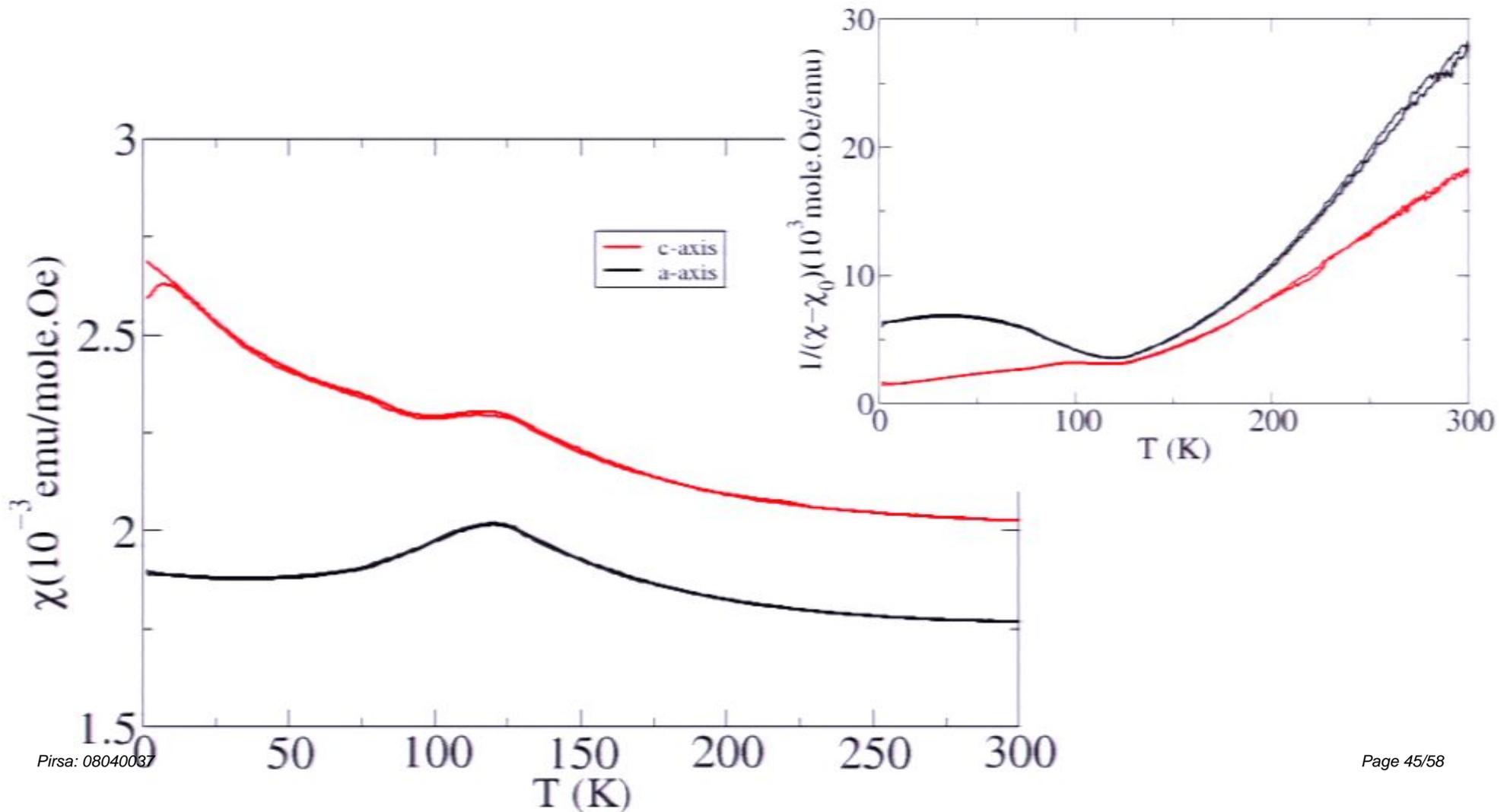


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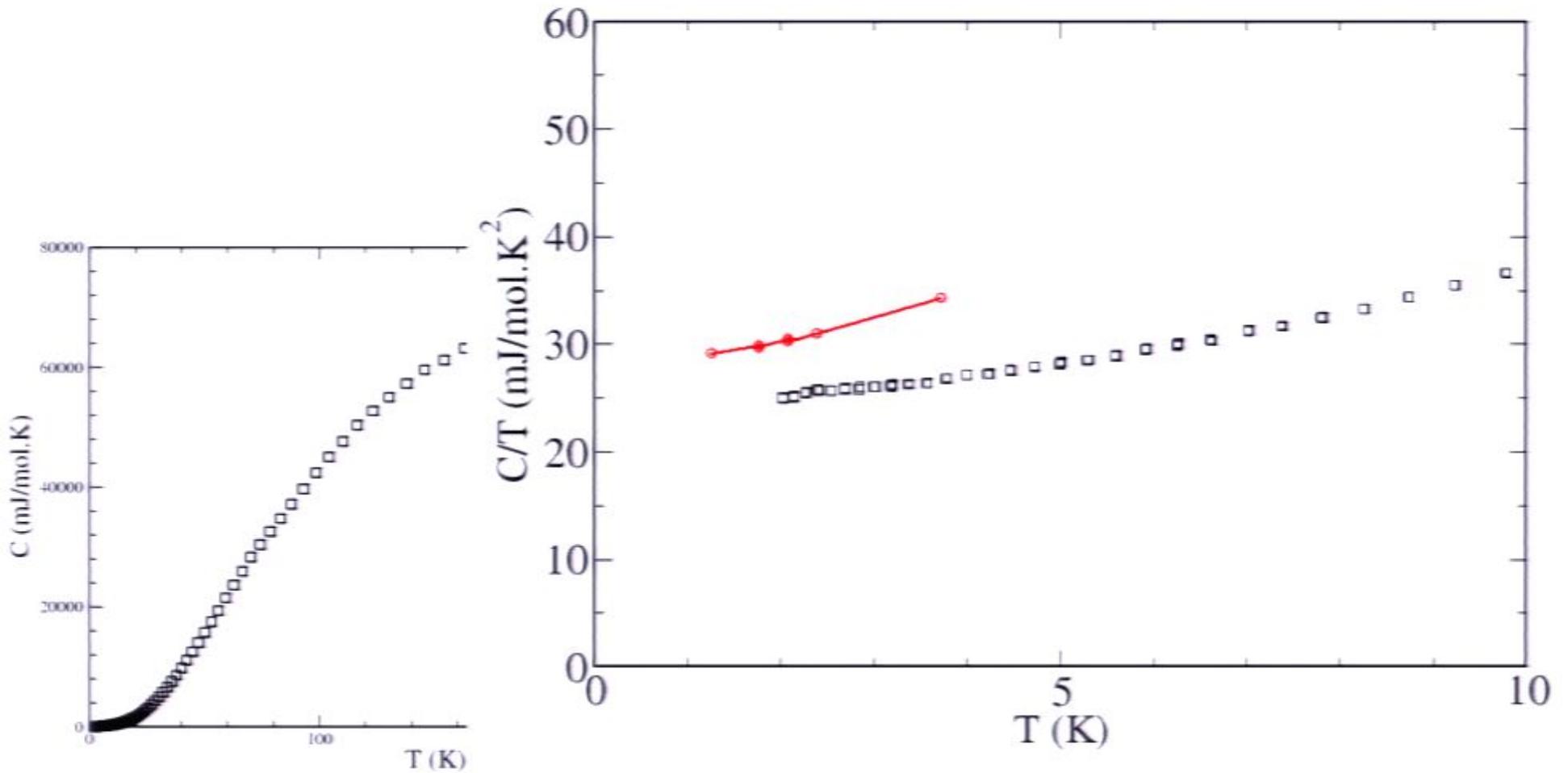


**Powder neutron diffraction  
reveals that this is an  
antiferromagnetic transition**

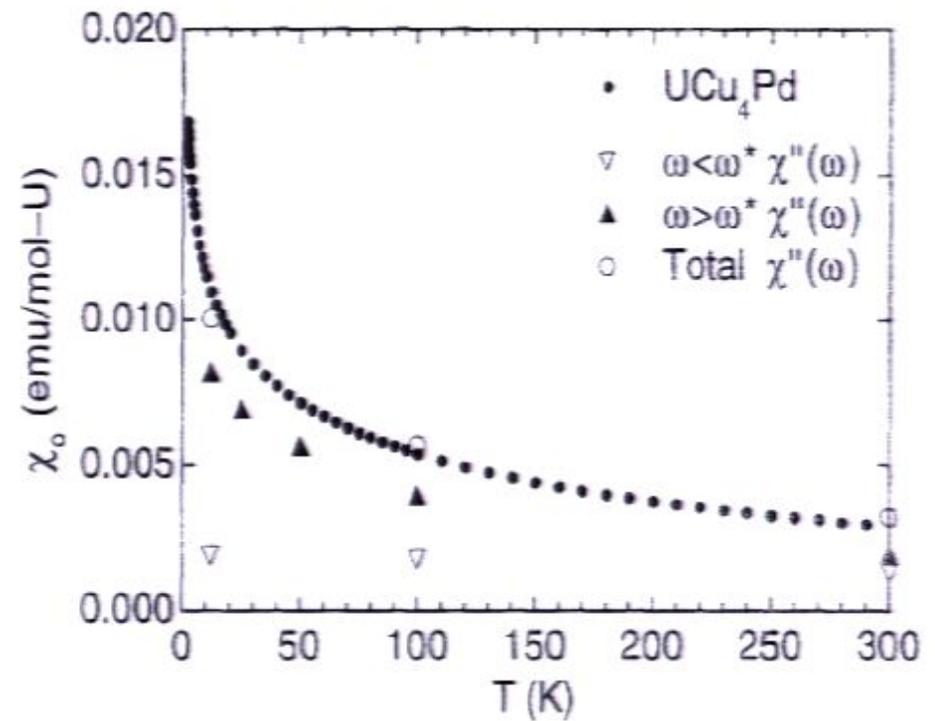
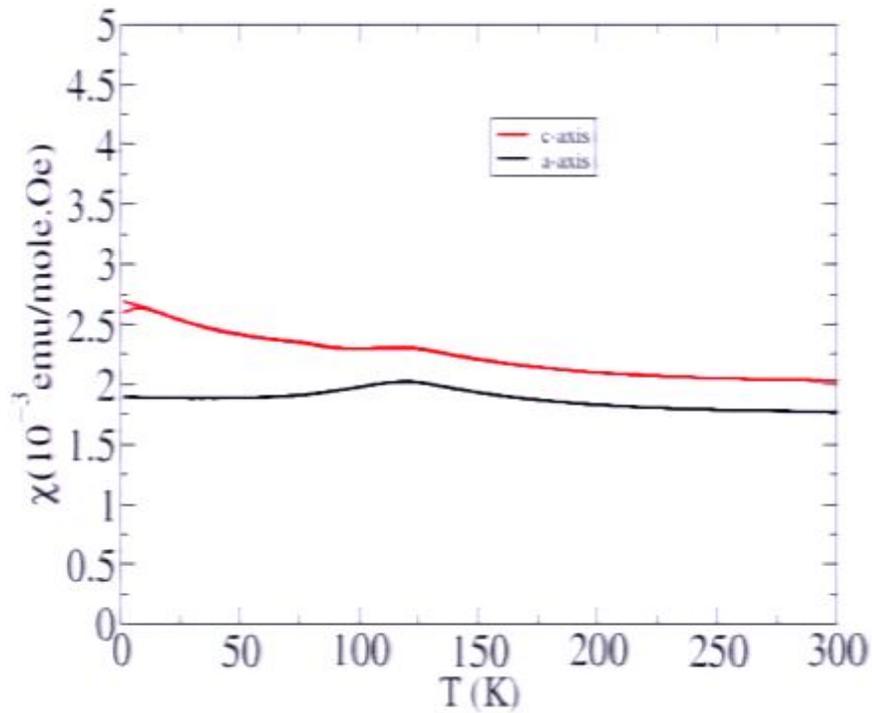
# Non-magnetic annealed sample



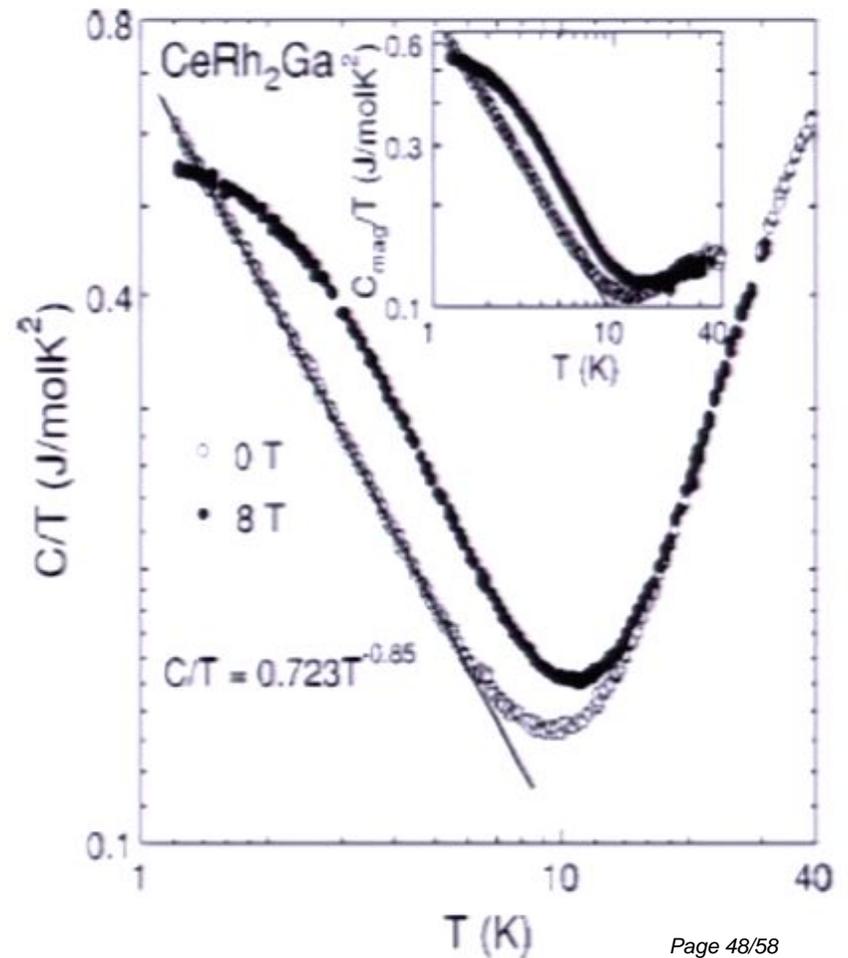
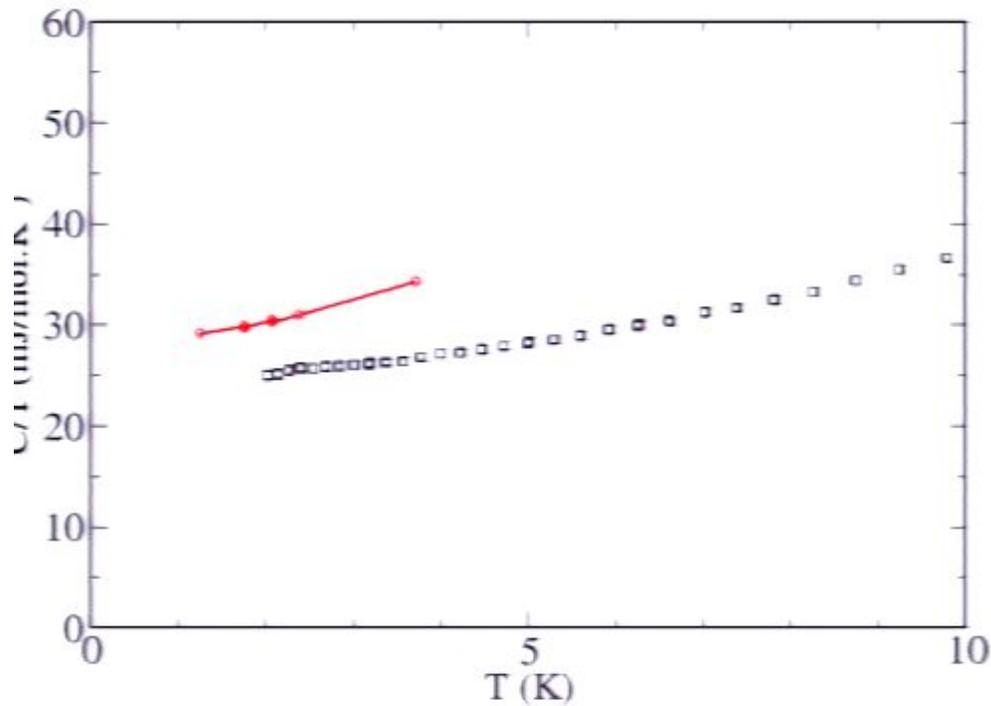
# Specific heat



# Comparison of susceptibility with doped systems:



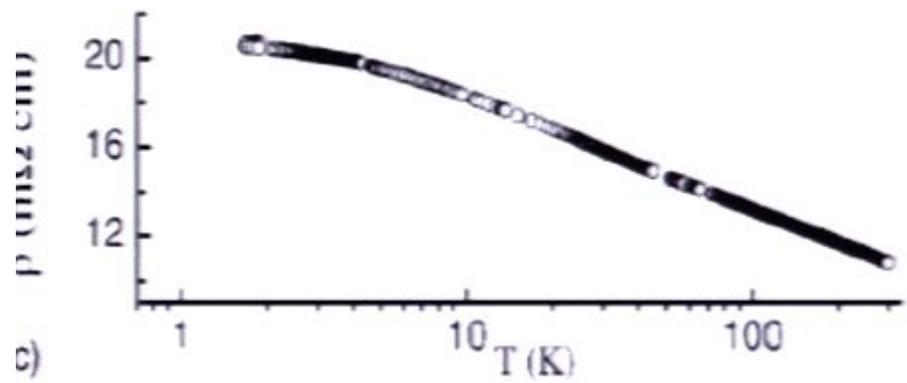
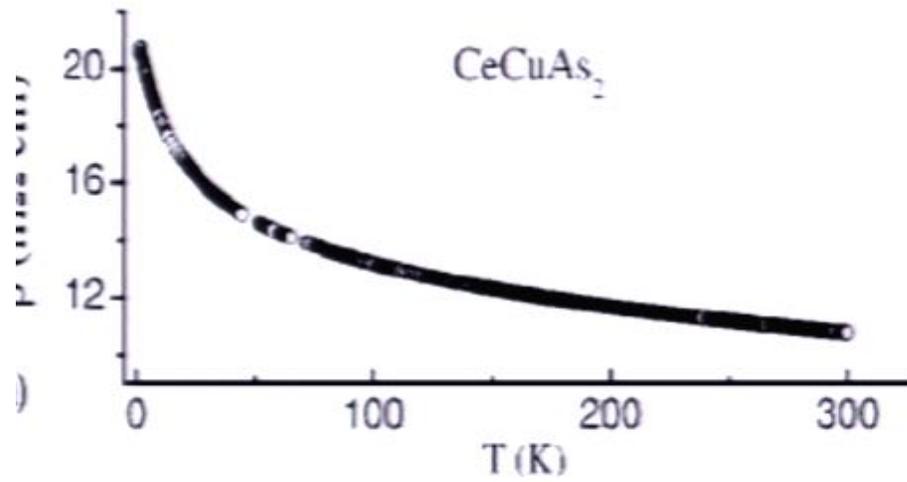
# Comparison of specific heat with doped systems:



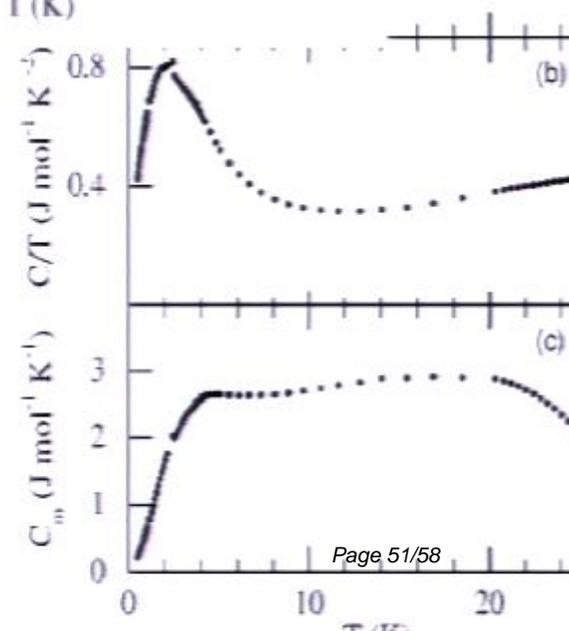
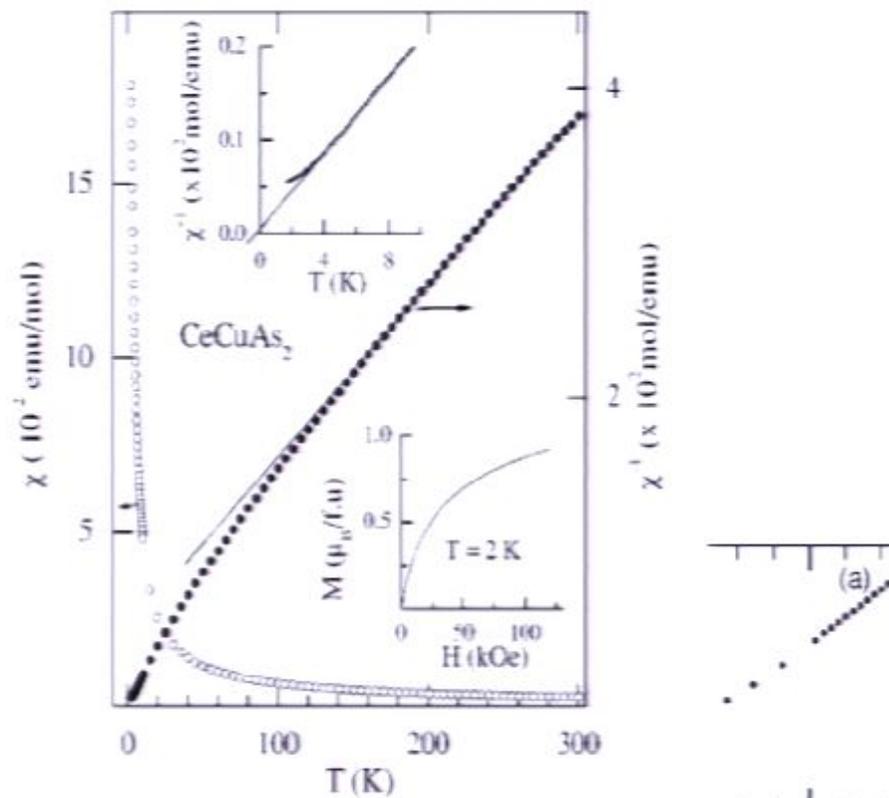
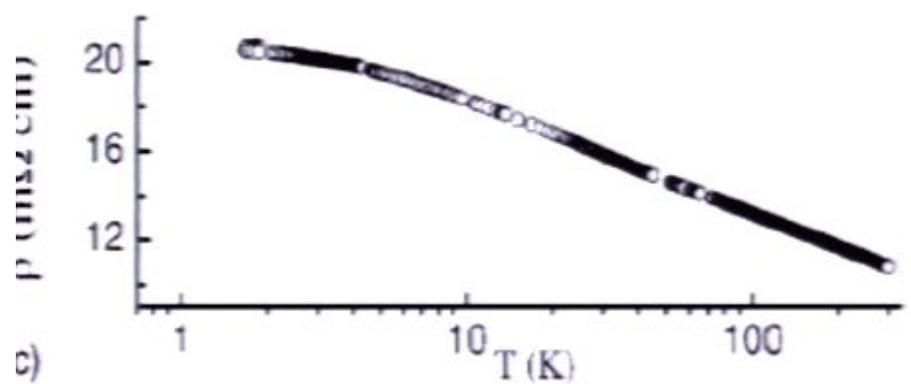
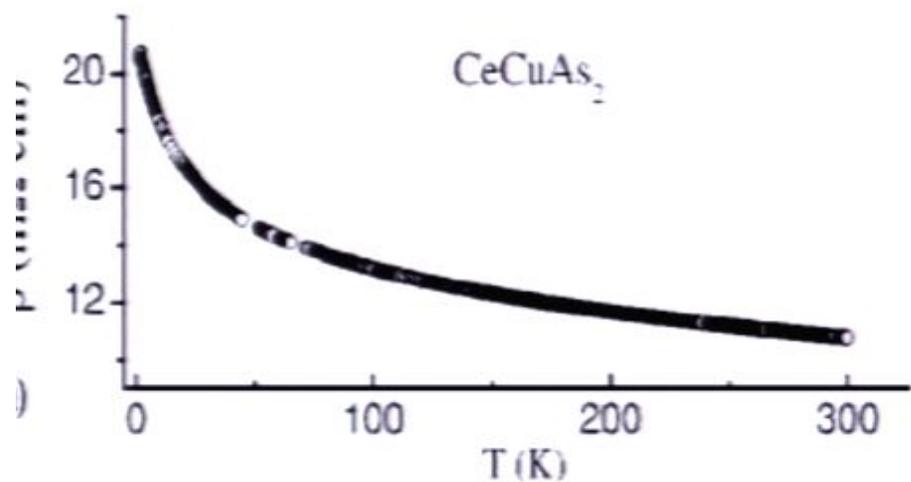
# Summary:

- Neutron scattering and magnetic susceptibility agree, there is an antiferromagnetic transition above 100K
- The ordered moment on the iron site is very small (from Mossbauer spectroscopy)
- The magnetic susceptibility is large, and not strongly dependent on temperature
- The anomalous behaviour of resistivity is field independent, and not strongly dependent on annealing or other treatment of the crystal
- The specific heat is roughly linear in  $T$  at low temperature, and not strongly enhanced.

# CeCuAs<sub>2</sub>



# CeCuAs<sub>2</sub>



- FeCrAs seems to show quite different thermodynamic behaviour from previously discovered “non-metallic strongly correlated electron systems”
  - Constant  $C(T)/T$  as opposed to  $\ln(T/T_0)$
  - Slowly rising  $\chi(T)$  as opposed to steep rise.

***Is the physics different?***

# A possible theoretical model: underscreened Kondo lattice

- Andrei and Orignac, PRB 2000: 1d chain electrons plus spin  $S > 1$ .
  - A chiral non-Fermi-liquid
  - (Generalized Wess-Zumino-Novikov-Witten model)
  - Strong tendency to antiferromagnetism.

$$\chi(T) = (2S - 1) / 2\pi\nu$$

$$C(T) / T = \text{const.}$$

# Details:

$$H_{\text{el}} = H_{\rho} + H_{\sigma}, \quad (2)$$

$$H_{\rho} = \int dx \frac{v_F}{2\pi} [(\pi\Pi_{\rho})^2 + (\partial_x\phi_{\rho})^2],$$

$$H_{\sigma} = \frac{2\pi v_F}{3} \int dx (\vec{J}_R \cdot \vec{J}_R + \vec{J}_L \cdot \vec{J}_L), \quad (3)$$

where the canonically conjugate fields  $\Pi_{\rho}, \phi_{\rho}$  describe the charge excitations, and the non-Abelian  $SU(2)_1$  currents  $\vec{J}_{R,L}$  describe the electron-spin excitations. The local moments are described in the low-energy regime by the Hamiltonian

$$H_{\text{mom}} = \frac{2\pi v_S}{2(1+S)} \int dx (\vec{S}_R \cdot \vec{S}_R + \vec{S}_L \cdot \vec{S}_L), \quad (4)$$

where  $\vec{S}_{R,L}$  are  $SU(2)_{2S}$  WZNW currents. The Kondo interaction  $\lambda_K$  at incommensurate filling becomes

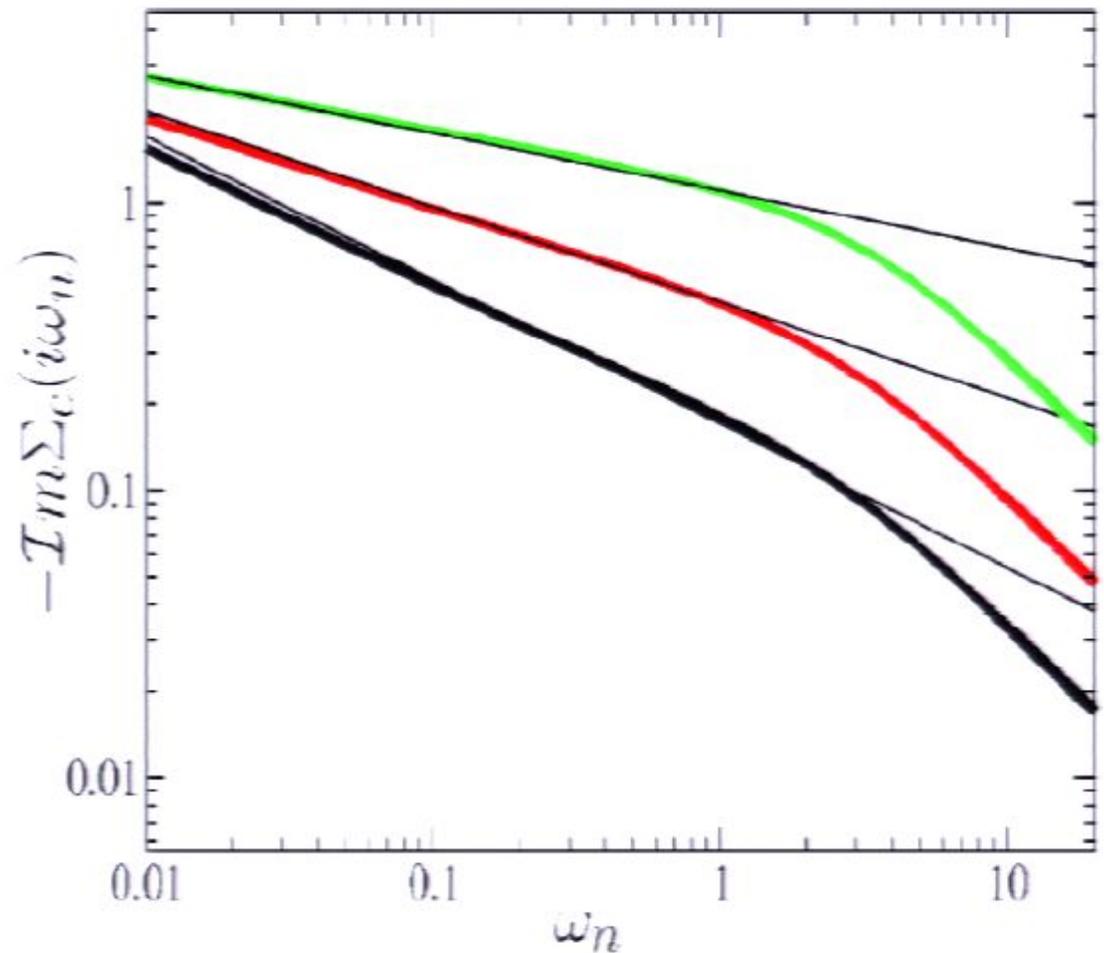
$$\lambda_K a \int dx (\vec{J}_R + \vec{J}_L) \cdot (\vec{S}_L + \vec{S}_R)(x) \quad (5)$$

# Underscreened Kondo Lattice: 1/N calculation

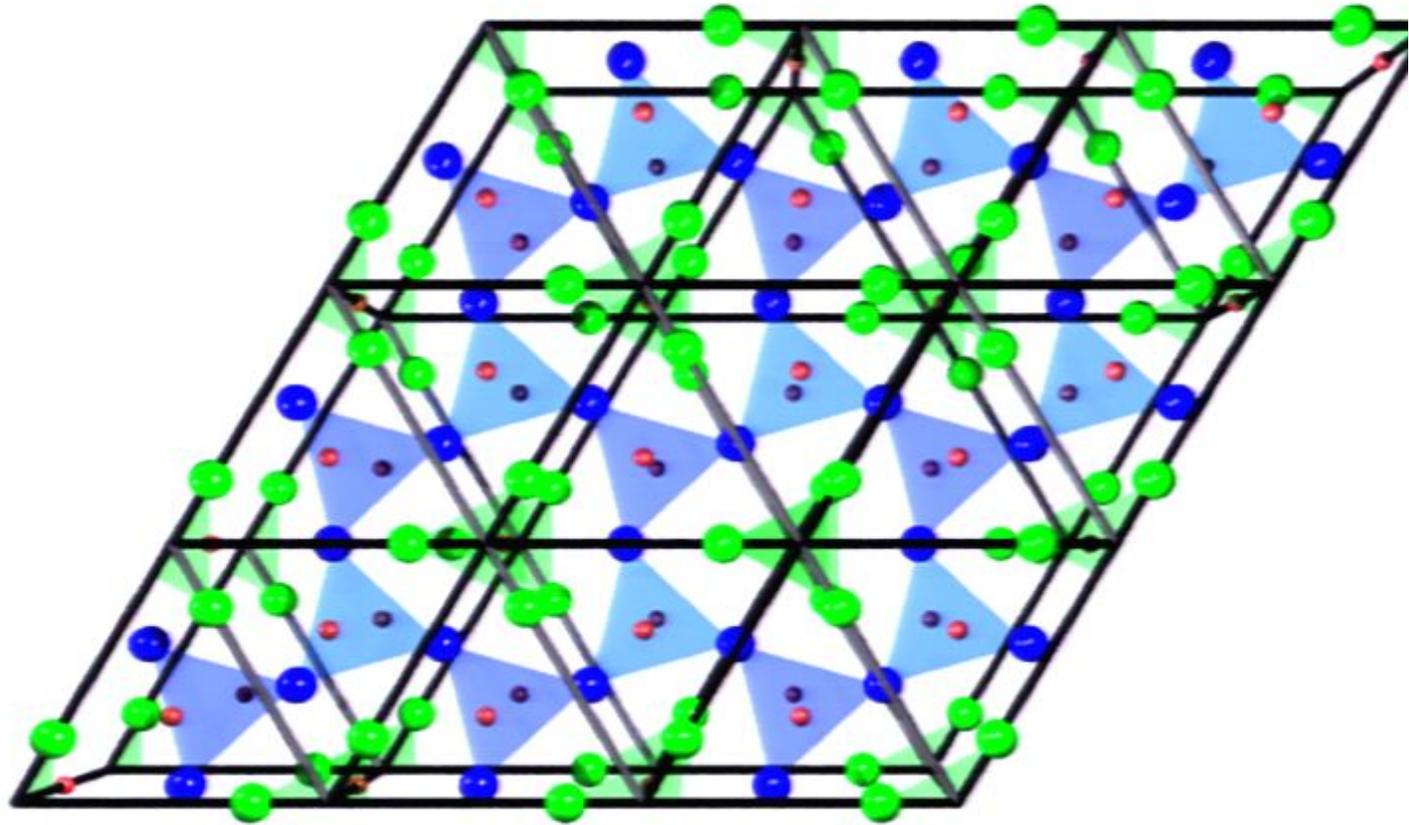
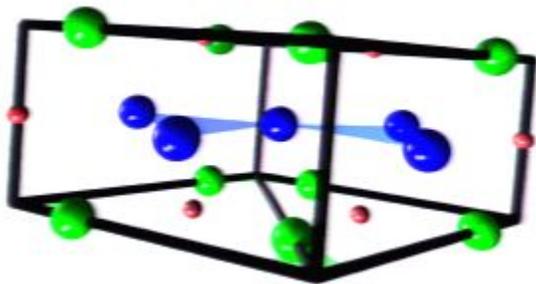
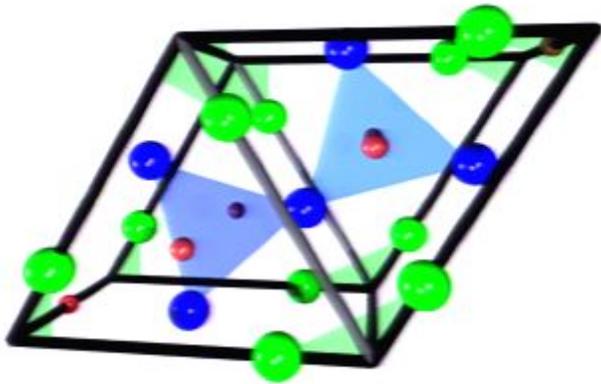
*Insulating pseudogap regime in place of usual renormalized metal, preventing the buildup of coherence over the lattice.*

*The underscreened Kondo lattice has a pseudogap density of states above the ordering temperature of the moments.*

*Predict power-law resistivity increasing with decreasing  $T$ .*



# Crystal structure FeCrAs



# Summary:

- FeCrAs shows a robust “non-metallic” low temperature resistivity
- Specific heat and magnetic susceptibility are enhanced, but not anomalous compared to previously discovered “non-metallic” concentrated Kondo systems
- Is this evidence of a new kind of behaviour?

# Crystal structure FeCrAs

