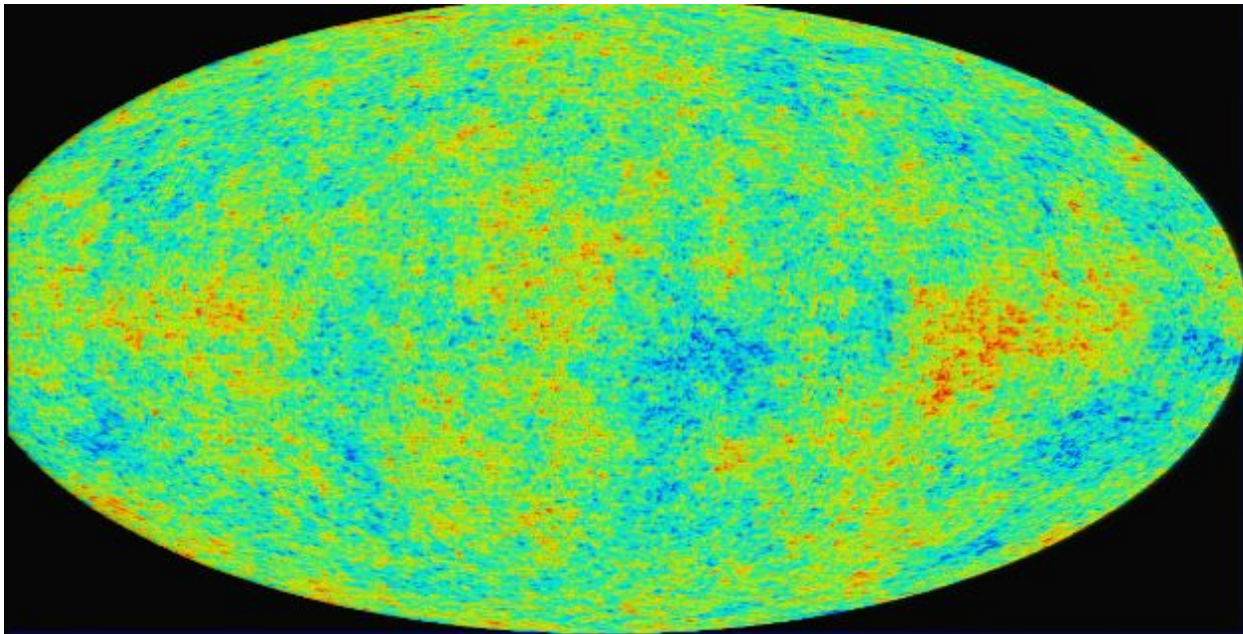


Title: Primordial Non-Gaussianity: A New Frontier

Date: Mar 08, 2008 02:10 PM

URL: <http://pirsa.org/08030052>

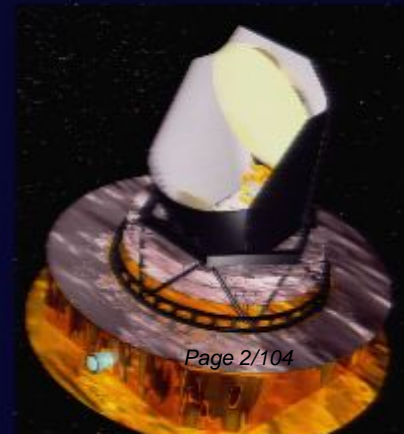
Abstract:



Primordial non- Gaussianity - a new frontier

Benjamin D. Wandelt
Amit P. Yadav

UIUC Physics/Astronomy



Why are we interested in cosmology?

Why are we interested in cosmology?

The big questions are:

Why are we interested in cosmology?

The big questions are:

“What is the fundamental theory, valid at the highest energies?”

Why are we interested in cosmology?

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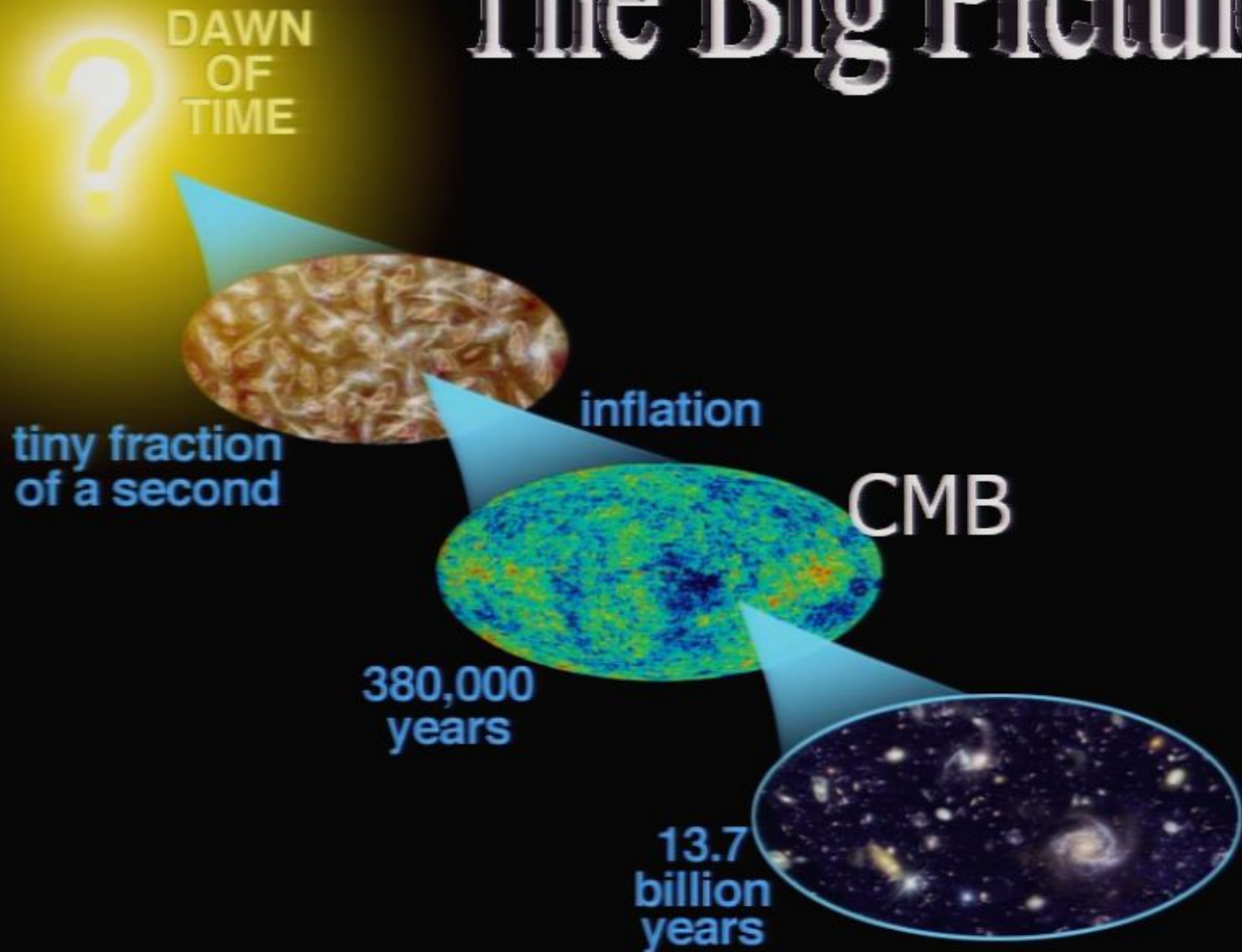
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“What is the fundamental theory, valid at the highest energies?”

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The Big Picture



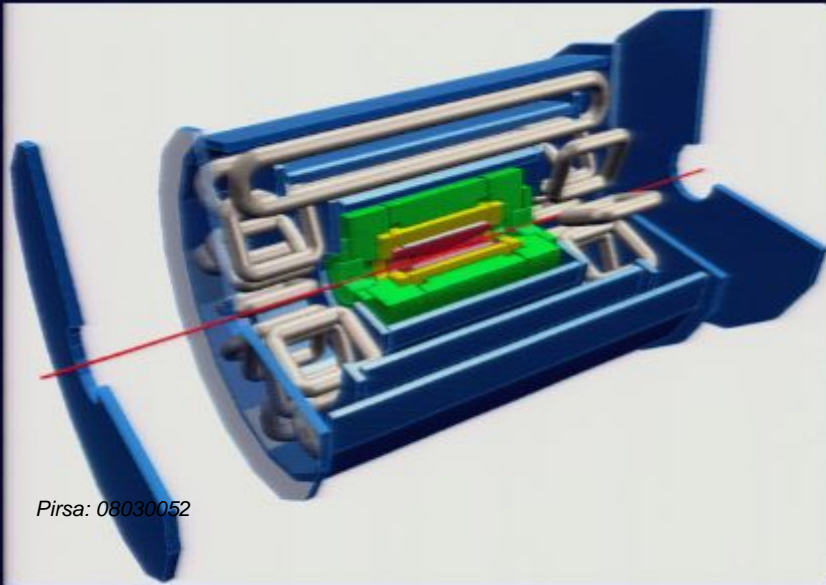
How do we study what happens at the highest energy scales and at the shortest time scales?

Showdown

WMAP, Planck

Showdown

LHC at CERN



Pirsa: 08030052

WMAP, Planck

Showdown

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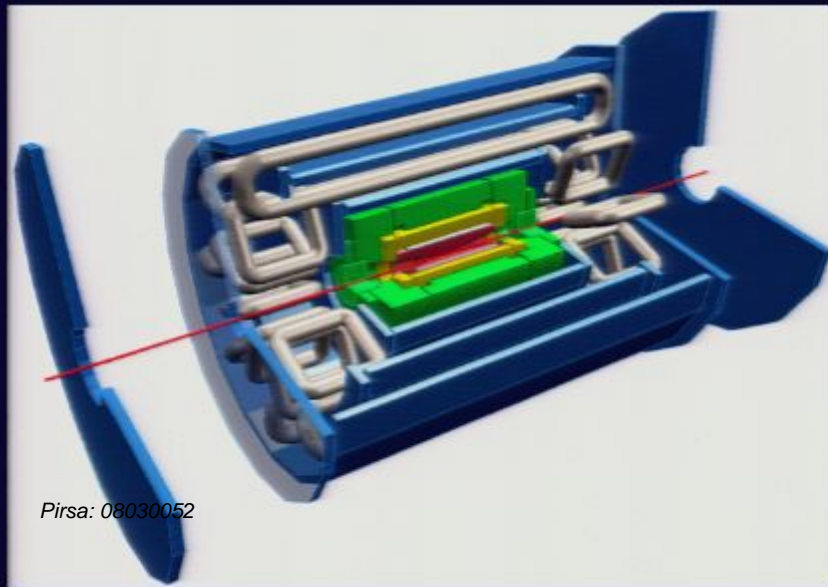
Hubble Ultra Deep Field

HST • ACS



NASA, ESA, S. Beckwith (STScI) and The HUDF Team

STScI-PRC04-07a



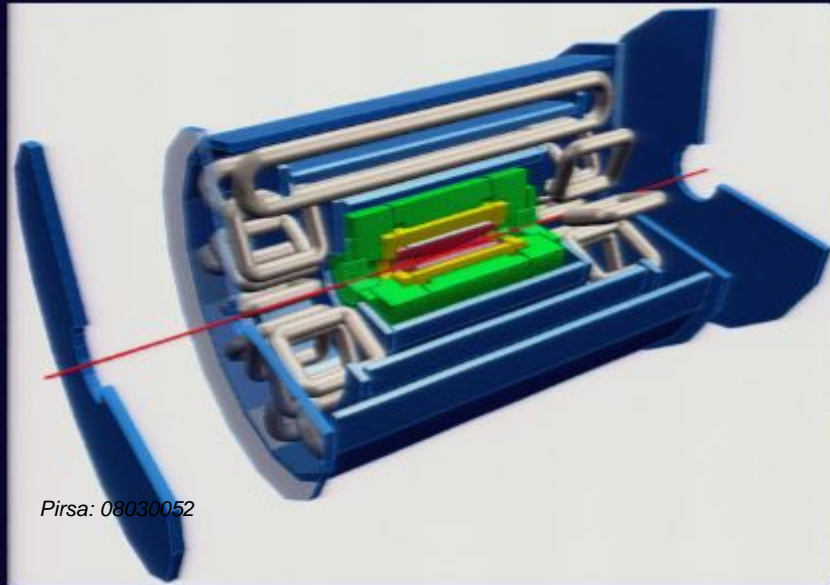
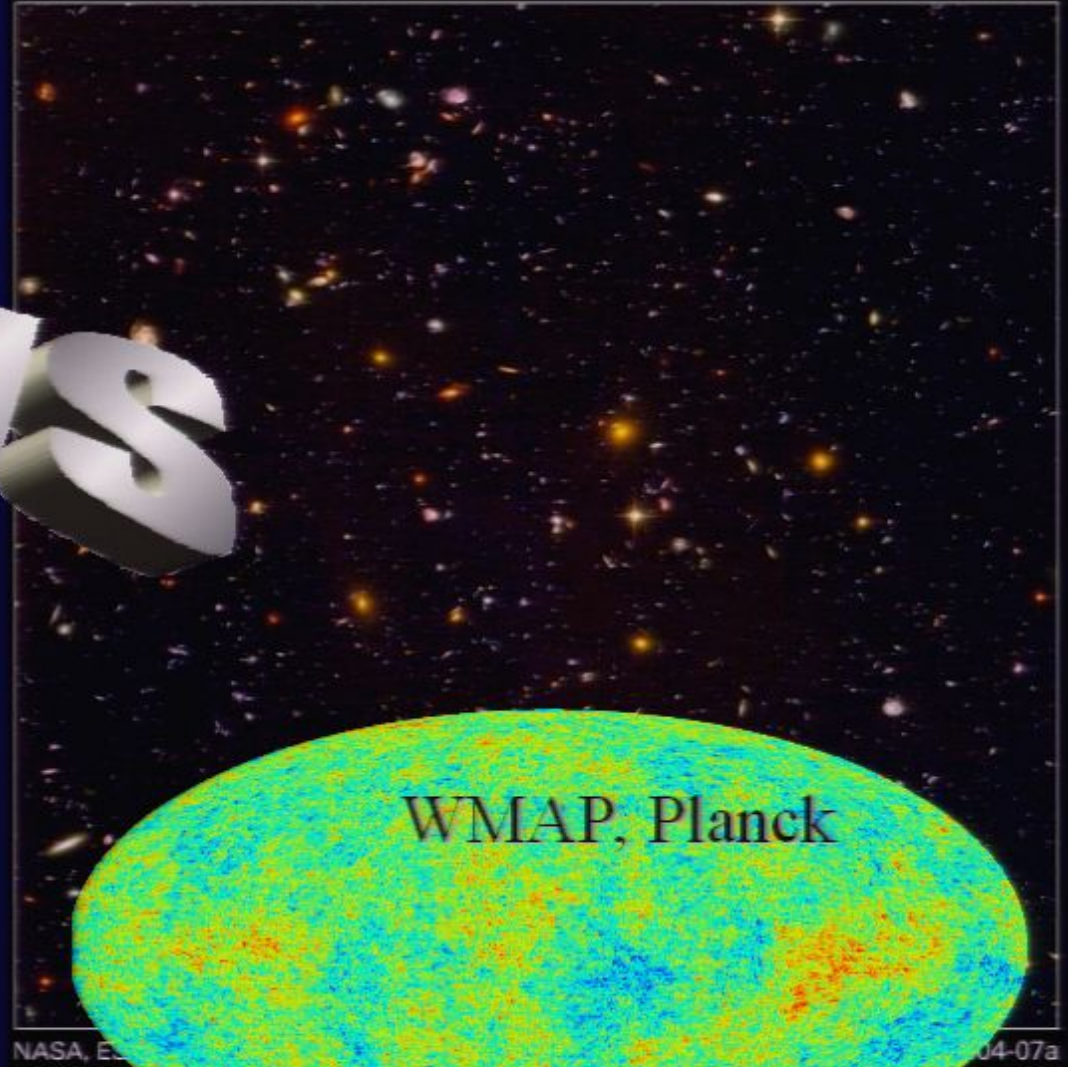
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Hubble Ultra Deep Field

HST • ACS



Will accelerators work?



Planck energy

Planck time 10^{-42} s

(Quantum
Gravity)

...

Unification of
forces

...

CERN

...

...

Everyday
energies

nanoseconds

Low energies

seconds



Will accelerators work?



Planck energy

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Everyday energies

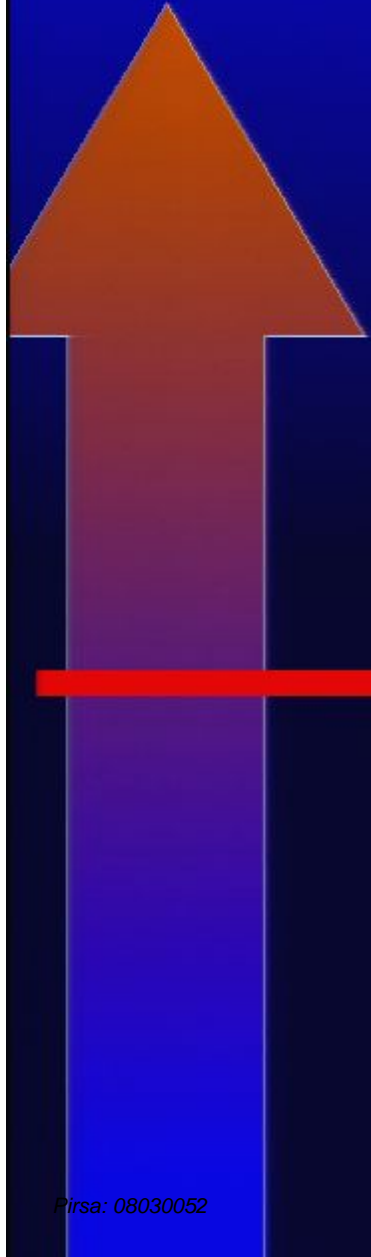
nanoseconds

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Will accelerators work?



Planck energy

Planck time $10^{-42}s$

(Quantum Gravity)

...

Unification of forces

Hard technological limit:

CERN

...

...

Everyday energies

nanoseconds

Low energies

seconds

Back to the Big Picture

(Big Bang ++)

Structure formation

- Some process, e.g. inflation, seeds **curvature perturbations** in a huge, smooth Universe at.
- Due to gravity these density fluctuations start to grow. Eventually, overdensities become so large that they collapse to form galaxies and clusters



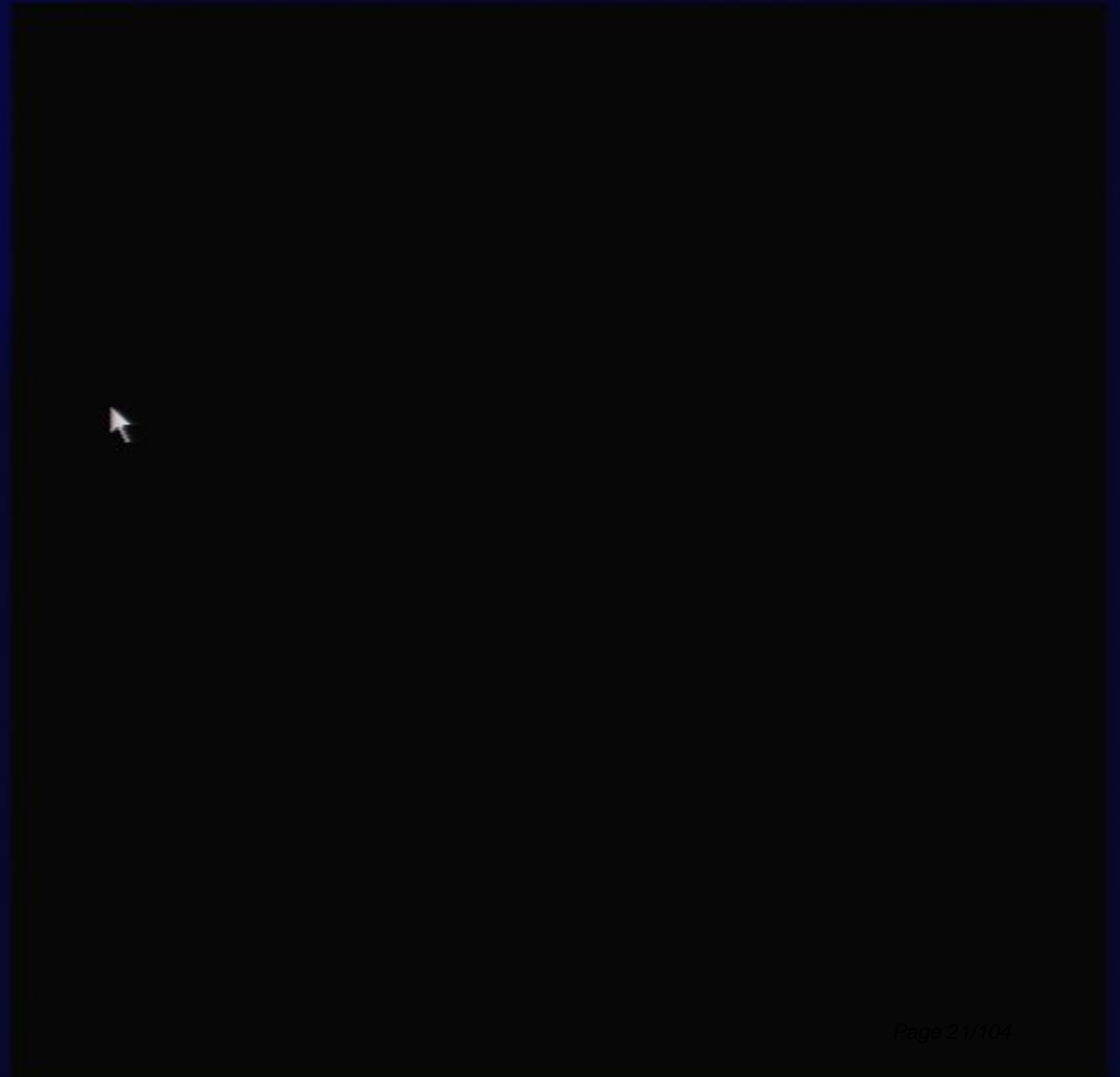
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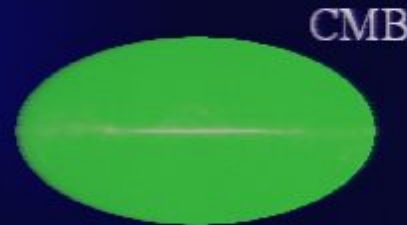
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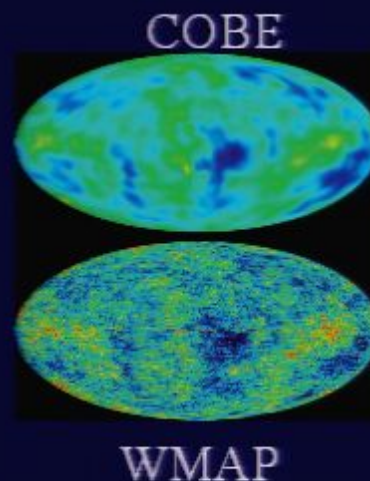
Data

- Homogeneity and Isotropy



- Flatness

- Seed perturbations



1978 Nobel Prize
in Physics



Robert Wilson and Arno Penzias



2006 Nobel Prize
in Physics



George Smoot John C. Mather

Testing Inflationary Paradigm

- Probes of inflation:
 - Inflation generates primordial fluctuations in space-time
 - Fluctuations in radiation
 - CMB T
 - CMB E-polarization
 - Fluctuations in matter
 - Dark matter distribution (Gravitational lensing etc.)
 - Galaxy and gas distribution (Redshift surveys, Lyman-alpha clouds, cosmological 21-cm radiation, etc)
 - Fluctuations in space time itself
 - Primordial Gravitational Waves (eg. Primordial B-modes of CMB)

Testing Inflationary Paradigm

- 0th Order Tests:
 - Is observable universe flat ?
 - Are fluctuations nearly Gaussian ?
 - Are fluctuation nearly scale independent ?
 - Are fluctuation adiabatic ?

Testing Inflationary Paradigm

(i) Flat, homogeneous and isotropic ✓

Eg: WMAP 08
+HST

(ii) Seed perturbations: *canonical models predict*

- Nearly adiabatic:

$$\frac{\delta \rho_i}{\dot{\rho}_i} = \frac{\delta \rho}{\dot{\rho}}$$



- Close to Gaussian

$$\langle \Phi(\vec{k}) \Phi(\vec{k}') \rangle = P_\Phi(k) \delta^3(\vec{k} - \vec{k}') \quad ?$$

- Nearly Scale Invariant

$$k^3 P_\Phi(k) = A k^{n_s - 1}$$

Eg: WMAP 08

Testing Inflationary Paradigm

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$$k^3 P_\Phi(k) = A k^{n_s - 1}$$

Eg: WMAP 08

Do we expect primordial perturbations to be absolutely positively Gaussian ?

- NO!
- Different inflationary models predict different amounts of NG so detection of NG helps distinguishing them.
- Even the 2nd order GR perturbations produce some NG ($f_{NL} \sim 1$)



Amplitude of non-Gaussianity. $f_{NL}=0$ for Gaussian perturbations and the larger the value the larger the non-Gaussianity

Are primordial perturbations really Gaussian ?

Non-Gaussianity from the Early Universe

$f_{NL} \sim 0.05$ canonical inflation (single field, couple of derivatives) (Maldacena 2003, Acquaviva et al 2003)

$f_{NL} \sim 0.1-100$ higher order derivatives

DBI inflation (Alishahiha et. al 2004)

UV cutoff (Creminelli 2003)

$f_{NL} > 10$ curvaton models (Lyth et. al 2003)

$f_{NL} \sim 100$ ghost inflation (Arkani-Hamed et al., 2004)

$f_{NL} \sim 20-100$ New Ekpyrotic models (Creminelli and Senatore 2007, Buchbinder et. al 2007, Koyama et. al 2007)

$f_{NL} \sim -50-200$ Ekpyrotic models (Lehners and Steinhardt 2008)

Non-Gaussianity – a new frontier

- Other than the information to be gained from 2-point correlations, Non-Gaussianity opens a new window on the Physics of the Beginning.
- What is the program?
 - The reliable theoretical prediction of non-Gaussianity from models of the early Universe
 - The characterization of non-Gaussianity from secondary anisotropies, foregrounds, etc.
 - The development of efficient and practical statistical methods to draw inferences about non-Gaussianity from the data.

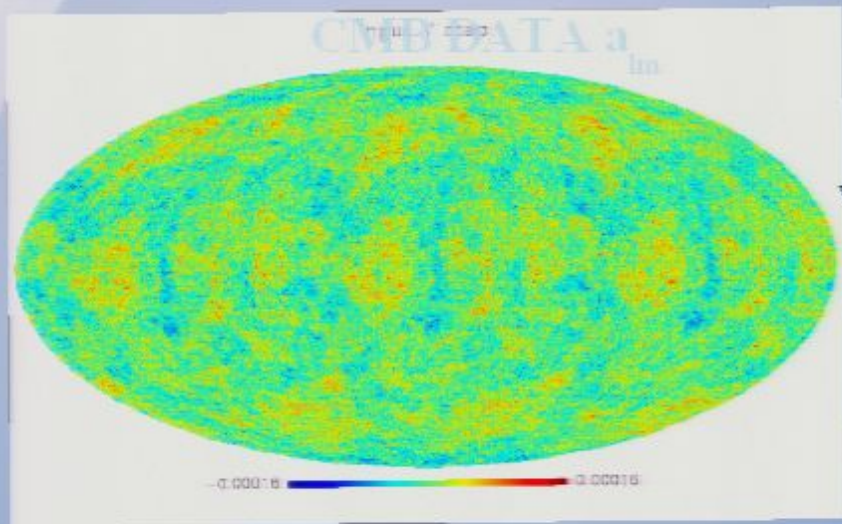
Our push at the frontier

- How to search for primordial non-Gaussianity
- How to search for f_{NL}
- What we find
- How to interpret our result
- Lessons for Planck
- Future prospects

How to search for (weak) primordial non-

- Reconstruct curvature perturbation from data
- Test for non-Gaussian features
- Compute error bars using Gaussian Monte Carlo realizations of the data

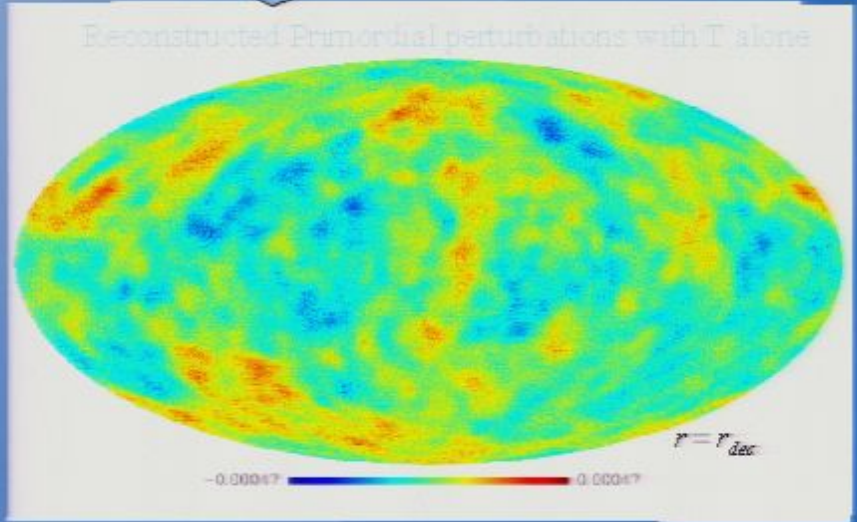
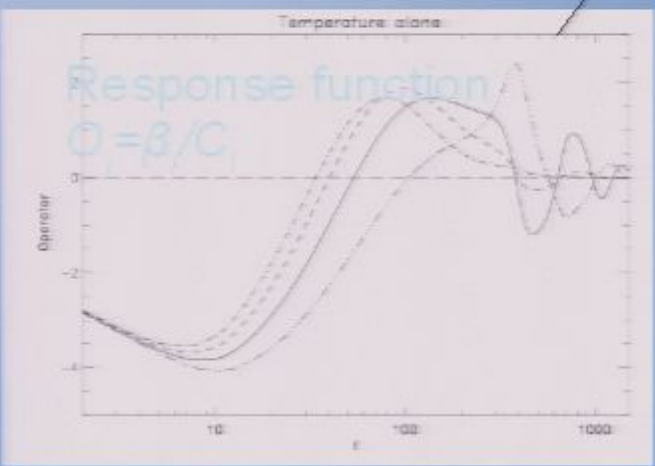
Reconstructed Primordial Perturbations



$$\phi_{lm} = \frac{\delta T}{T} a_{lm}$$

SW limit

$$\frac{\delta \phi}{\phi} = \frac{-1}{3} \frac{\delta T}{T}$$

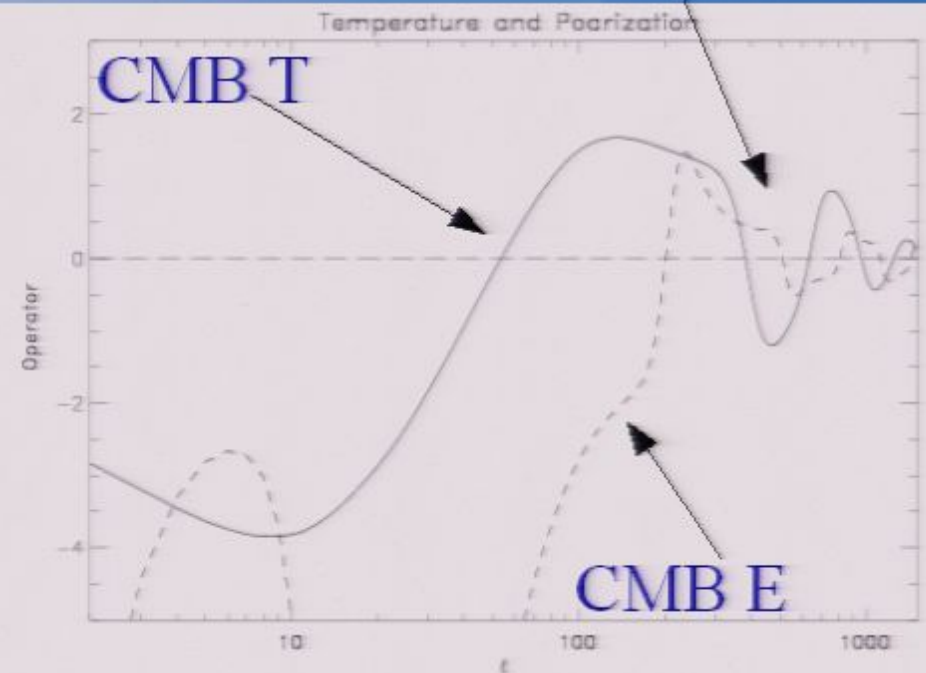
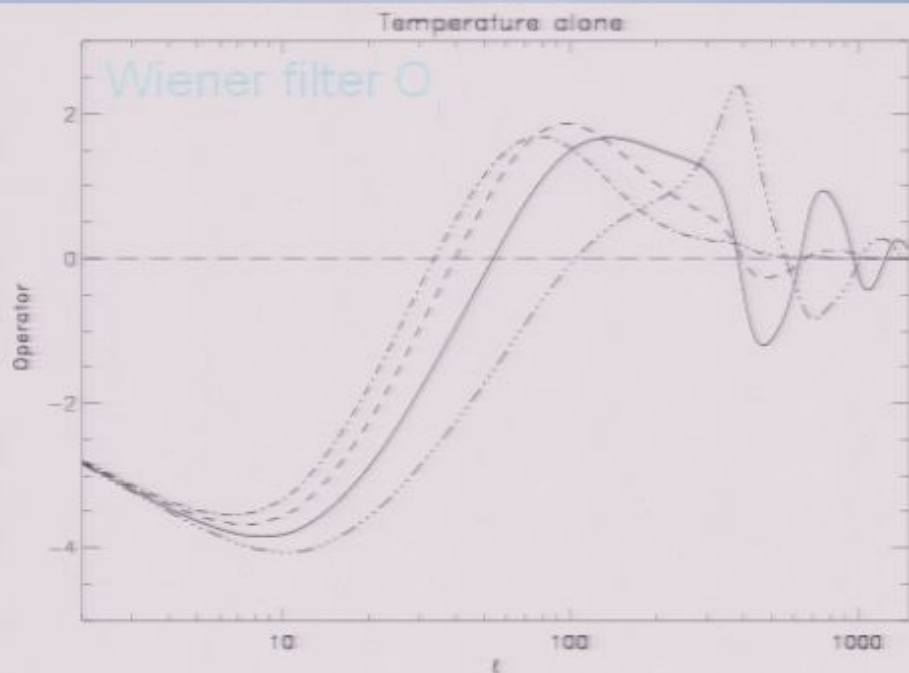


$$\beta_{\ell}^i(r) = \frac{2b_{\ell}^i}{\pi} \int k^2 dk P_{\phi}(k) g_{\ell}^i(k) j_{\ell}(kr)$$

The curvature perturbation leaves a *unique signature* in T & E

- Note negative response on large scales

T and E are out of phase



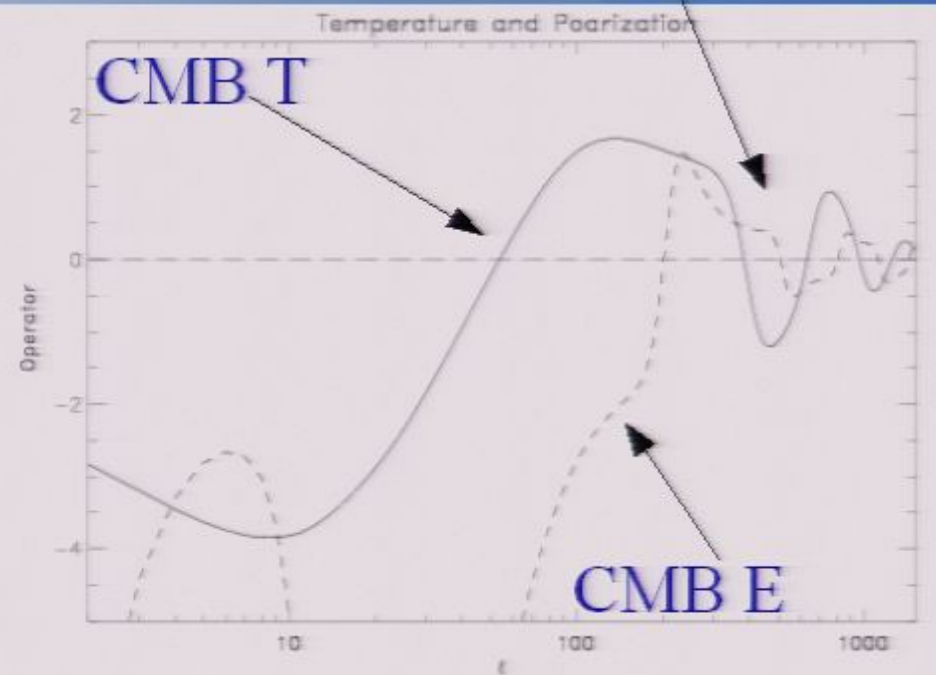
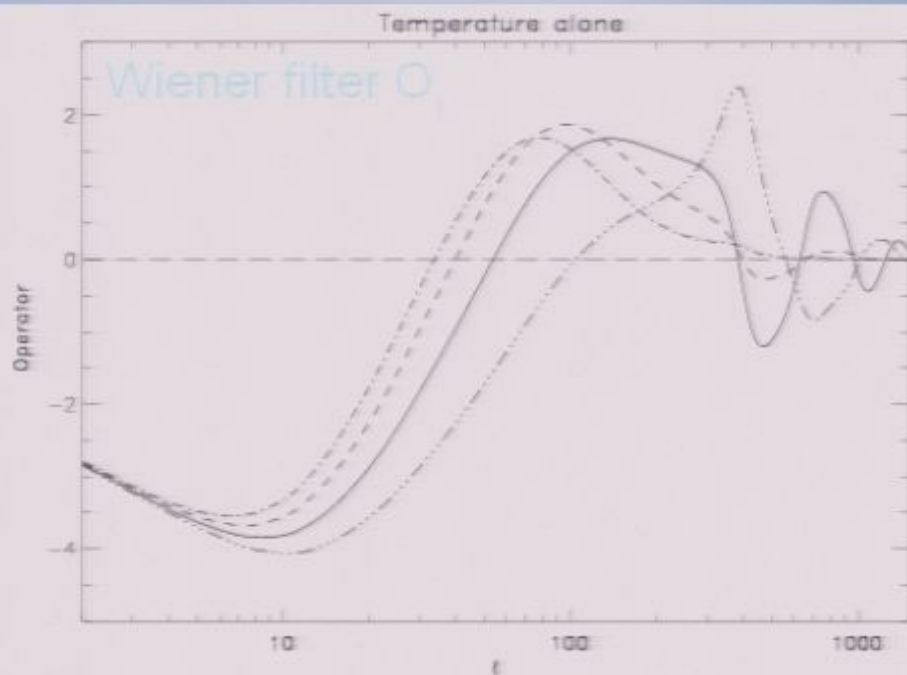
Yadav, and Wandelt, PRD (2005)

No Signal

VGA-1

The curvature perturbation leaves a *unique signature* in T & E

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Yadav, and Wandelt, PRD (2005)



Slides

- Primalordial non-Gaussianity - a new frontier
Benjamin D. Wandelt
Amit P. Yadav
The Cosmic Micr...
- Why are we interested in cosmology?
The big questions are:
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"What happened at $t = 0$?"
Why are we inte...
- The Big Micro:
Slide 3
- How do we study what happens at the highest energy scales and at the shortest time scales?
Click to add text.

Normal Outline Notes Handout Slide Sorter

Primordial non-Gaussianity
-
a new frontier

Benjamin D. Wandelt
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UIUC Physics/Astronomy

Physics Illinois

ASTRONOMY
UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

Tasks View

- Master Pages
- Layouts
- Custom Animation
- Slide Transition





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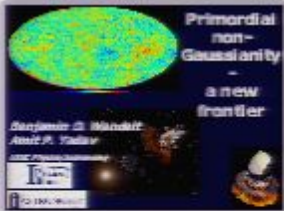
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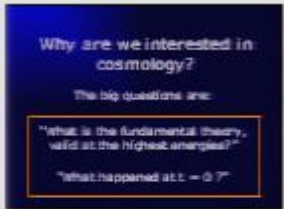
Physics Illinois
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Tasks View X

- Master Pages
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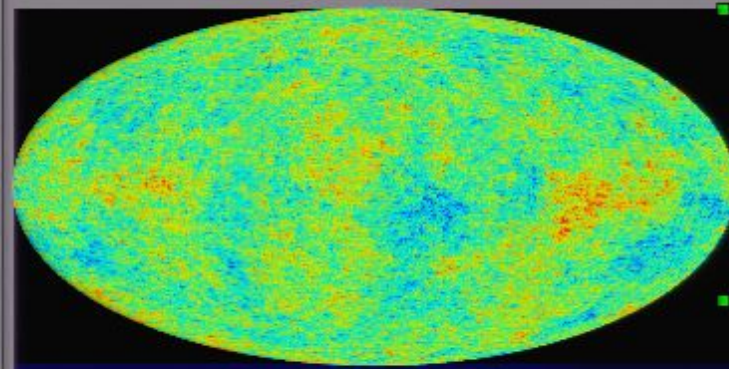
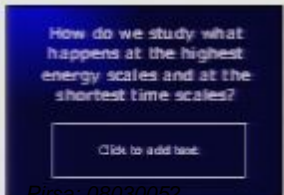
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Slide 3



Primordial non-Gaussianity - a new frontier

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UIUC Physics/Astronomy

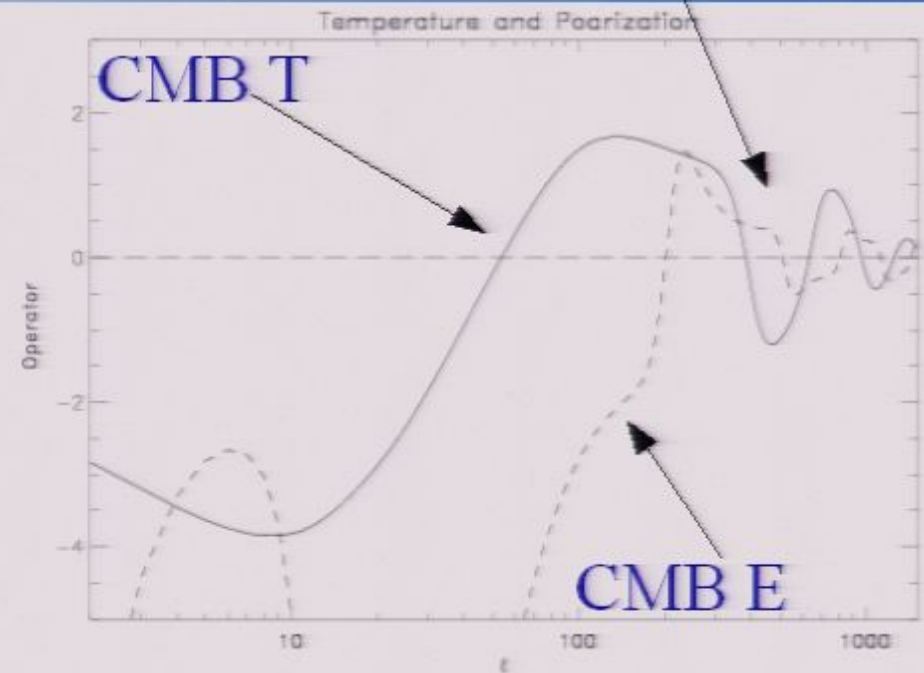
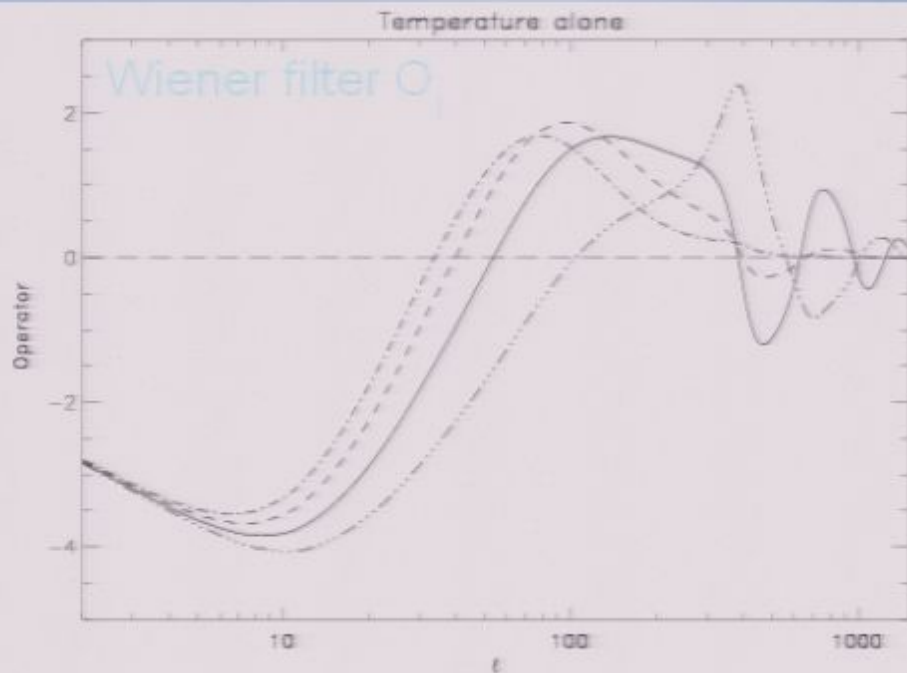


Tasks View X

- Master Pages
- Layouts
 - Blank slide
 - Slide with title and content
 - Slide with title and two columns of content
 - Slide with title and image
 - Slide with title and table
 - Slide with title and bar chart
 - Slide with title and pie chart
 - Slide with title and list
 - Slide with title and image
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The curvature perturbation leaves a *unique signature* in T & E

- Note negative response on large scales
- T and E are out of phase

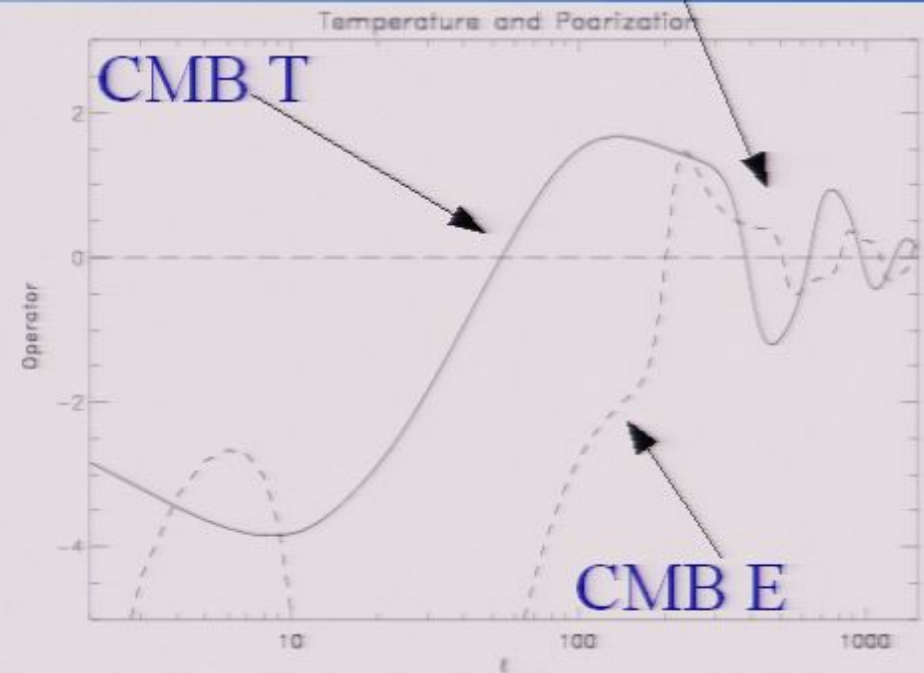
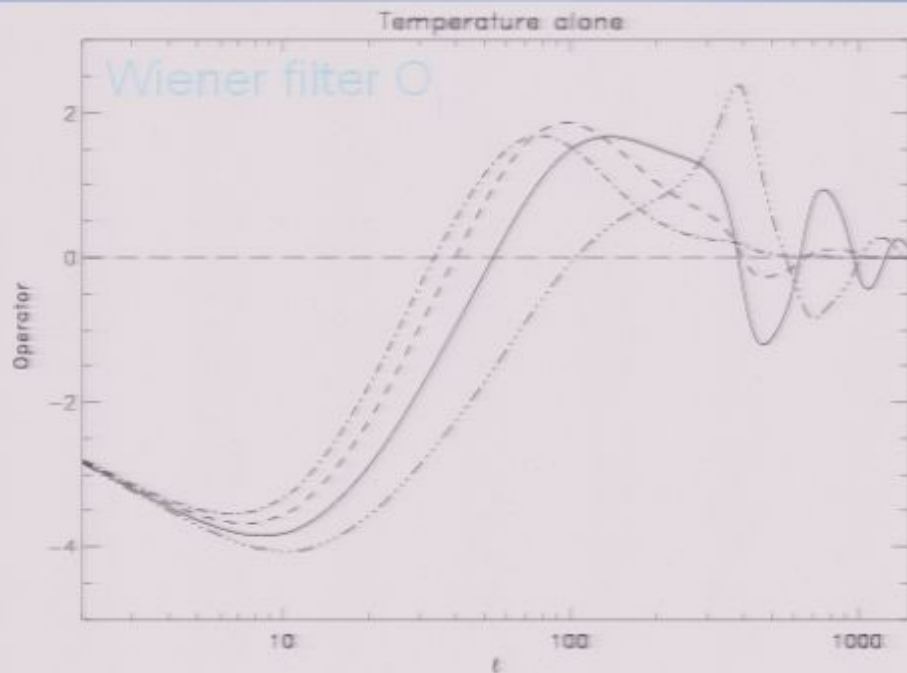


Yadav, and Wandelt, PRD (2005)

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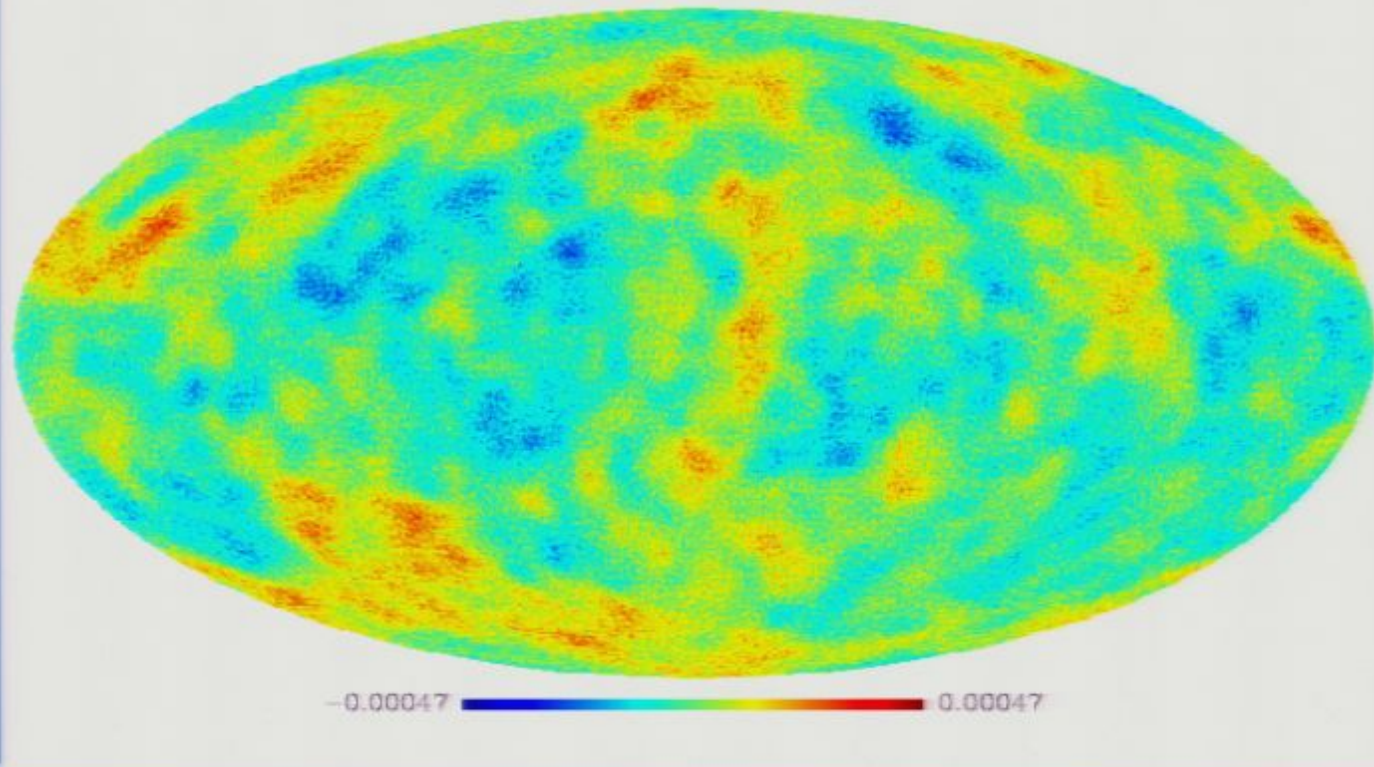
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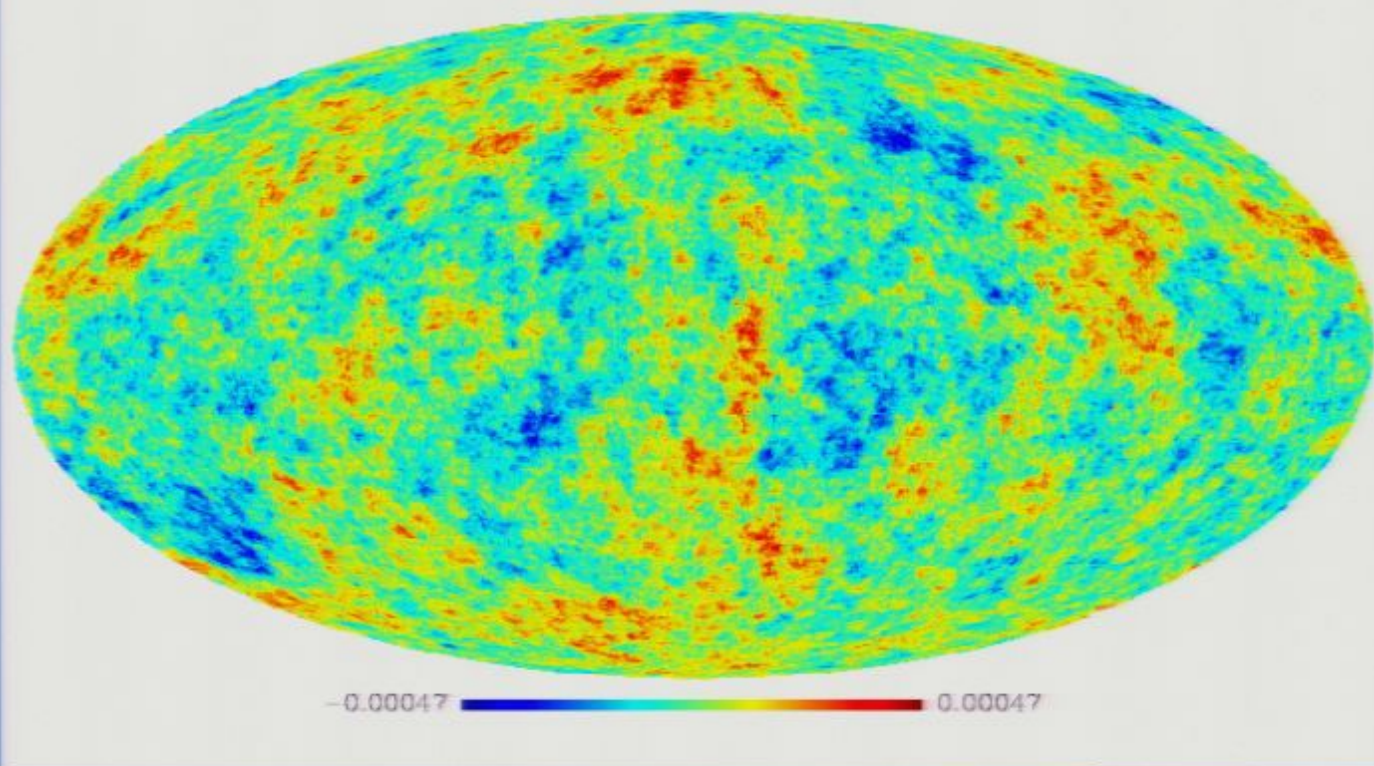


Yadav, and Wandelt, PRD (2005)

primordial map, using T alone

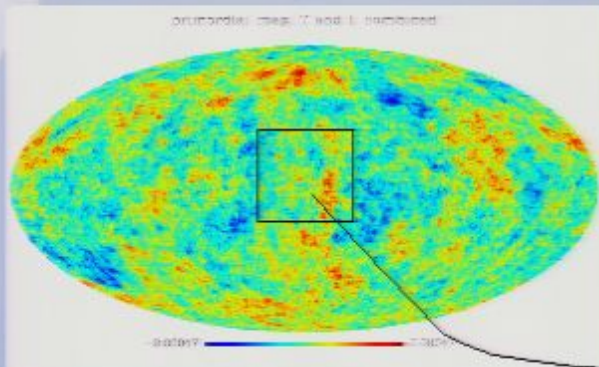


primordial map, T and E combined

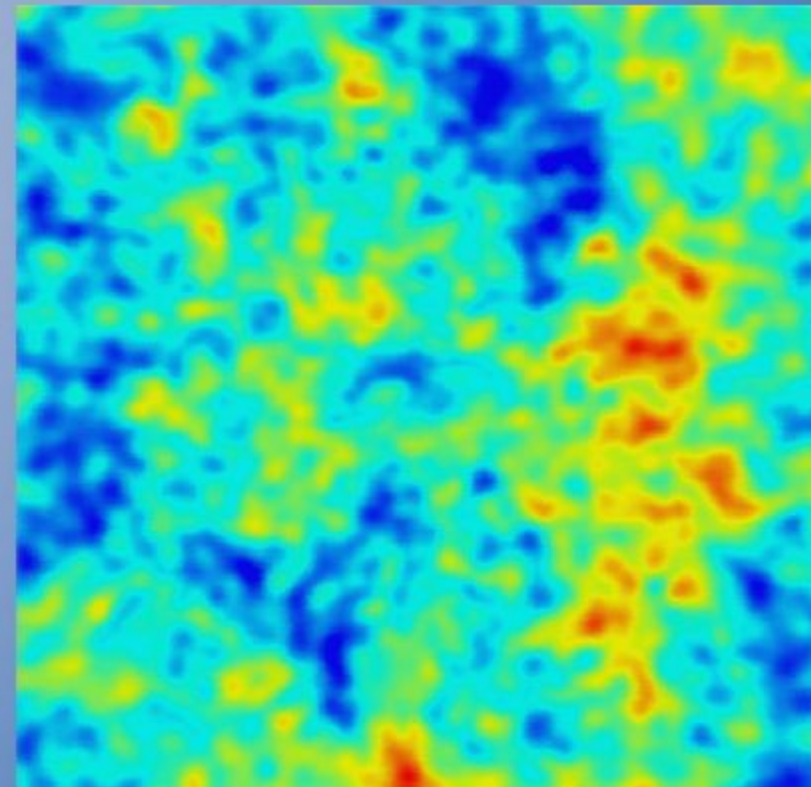


-0.00047 0.00047

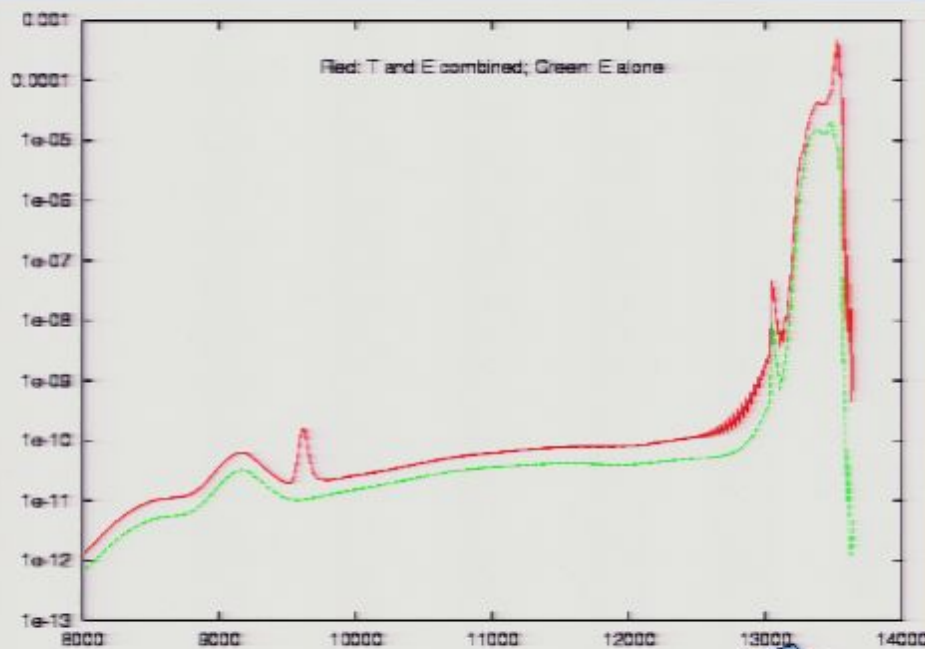
Reconstructed perturbations at different radii



Curvature fluctuations



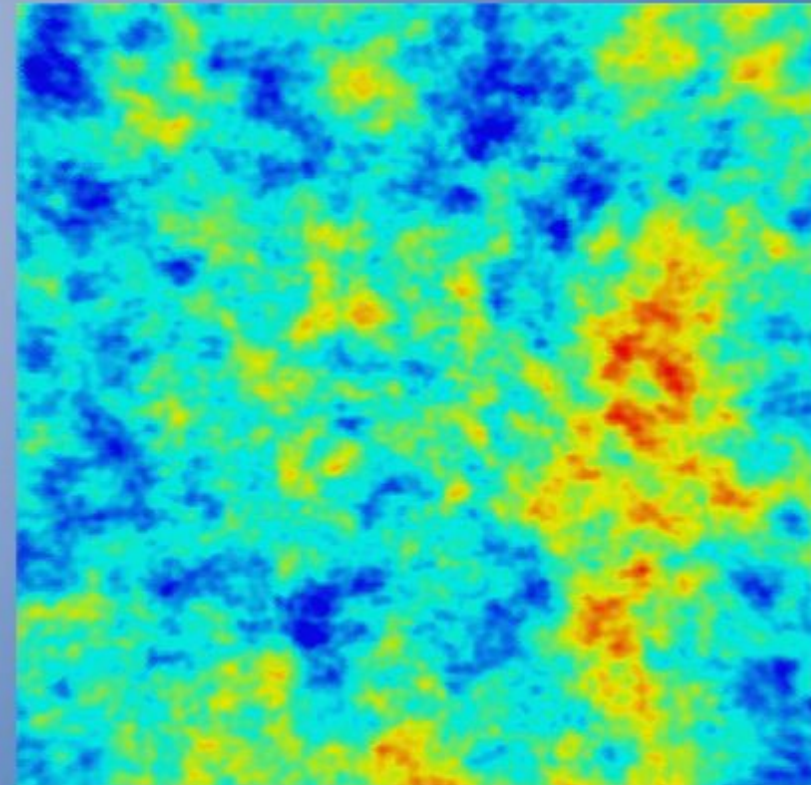
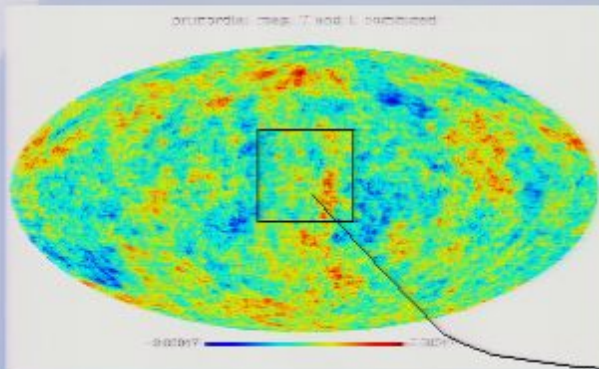
-0.00035 0.00052
(0.0, 0.0) Galactic



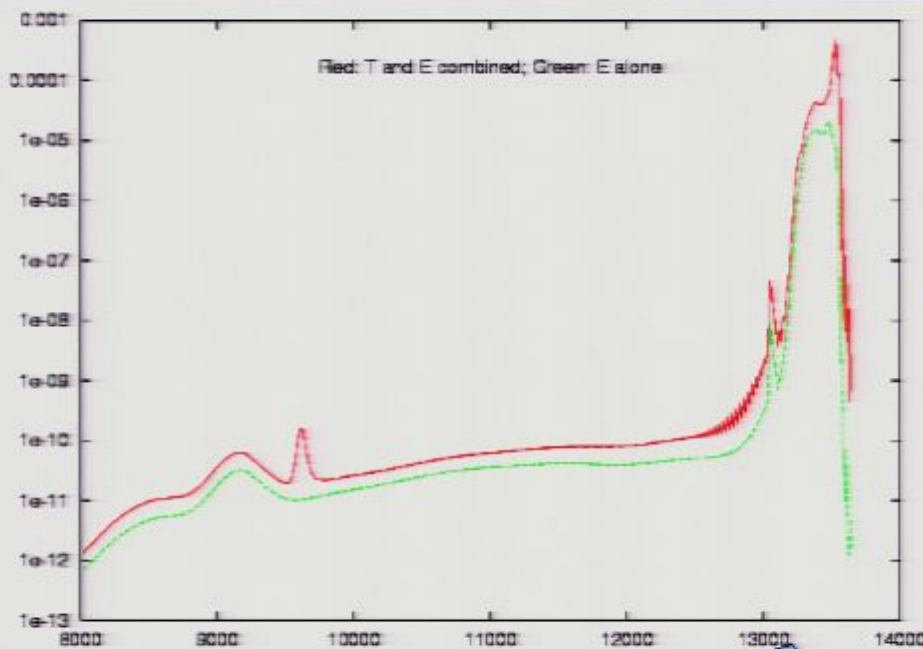
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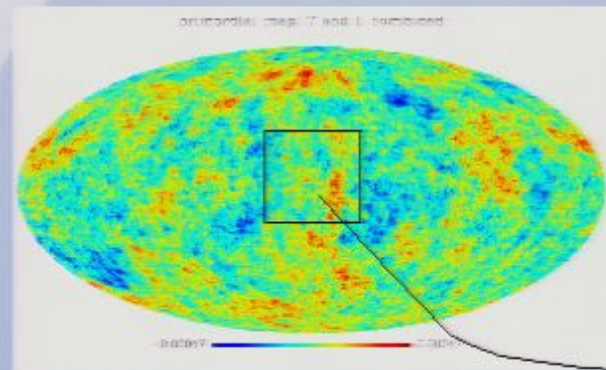


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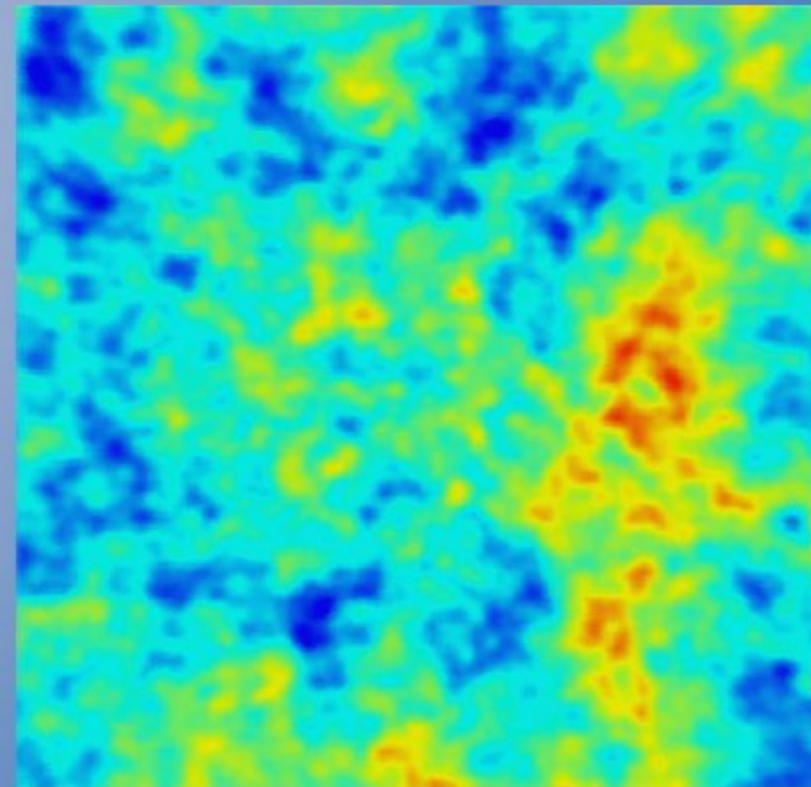


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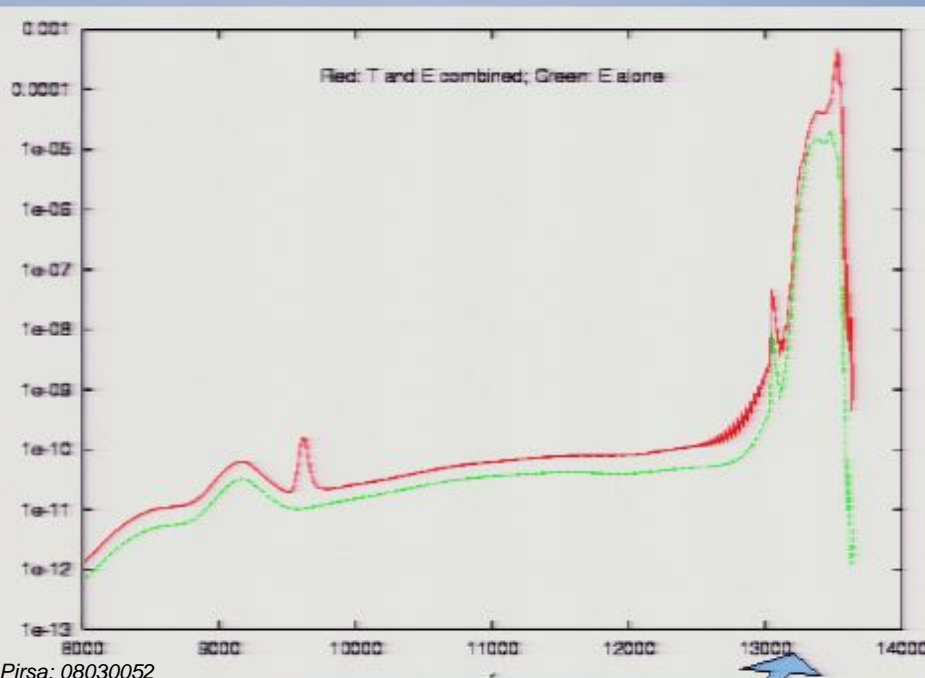
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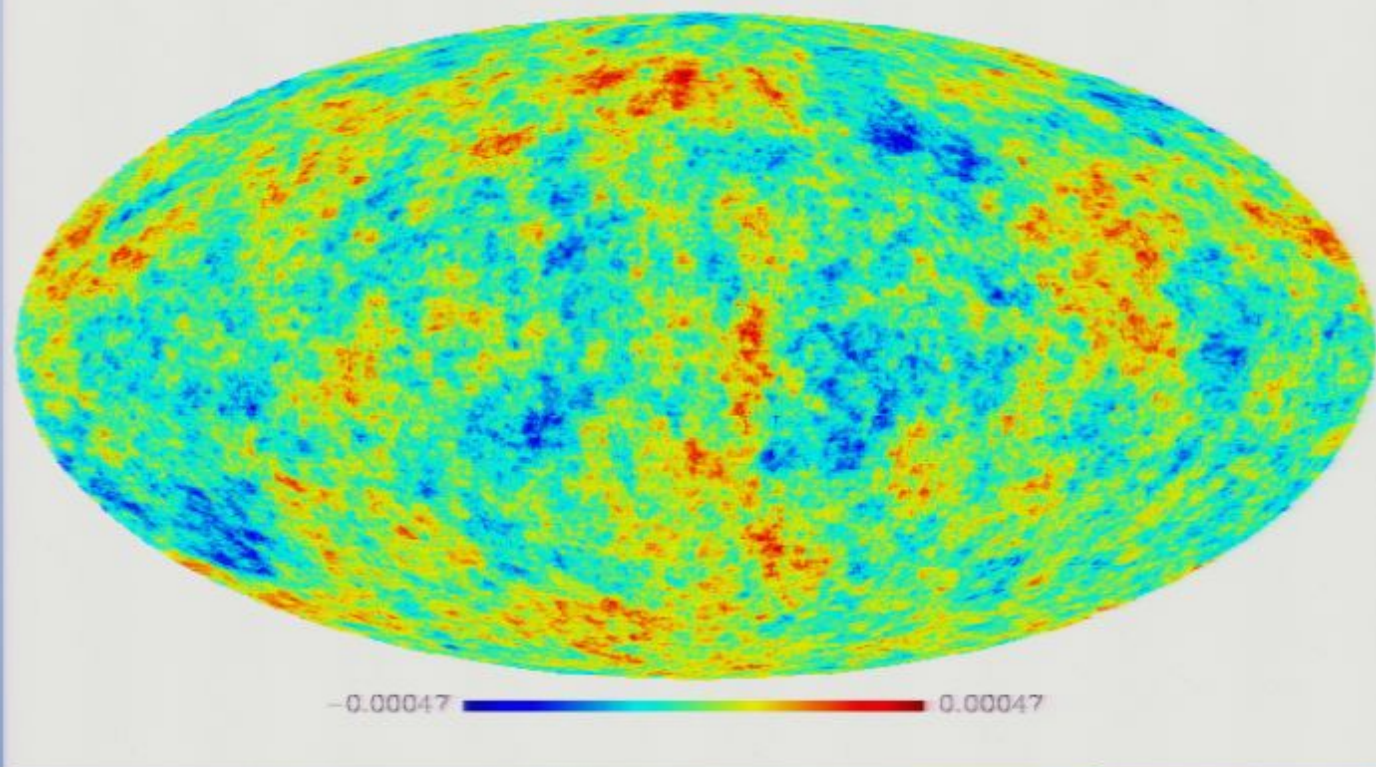


-0.00015 0.00015
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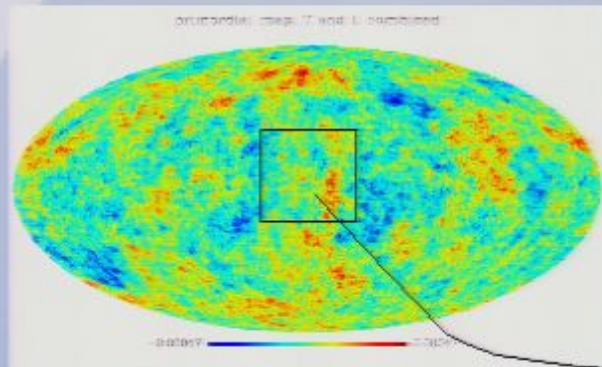


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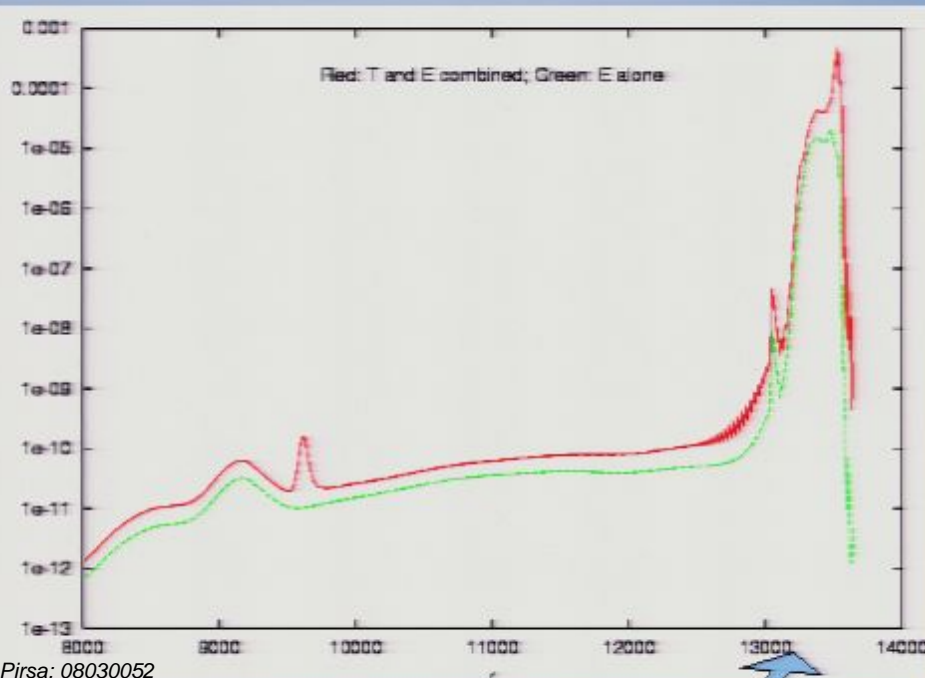
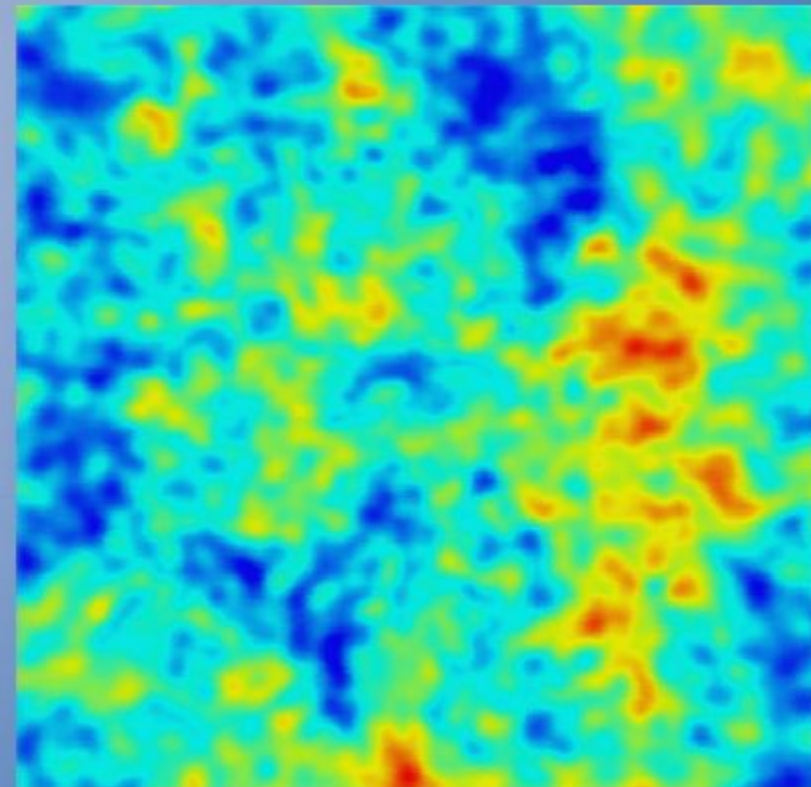
primordial map, T and E combined



Reconstructed perturbations at different radii



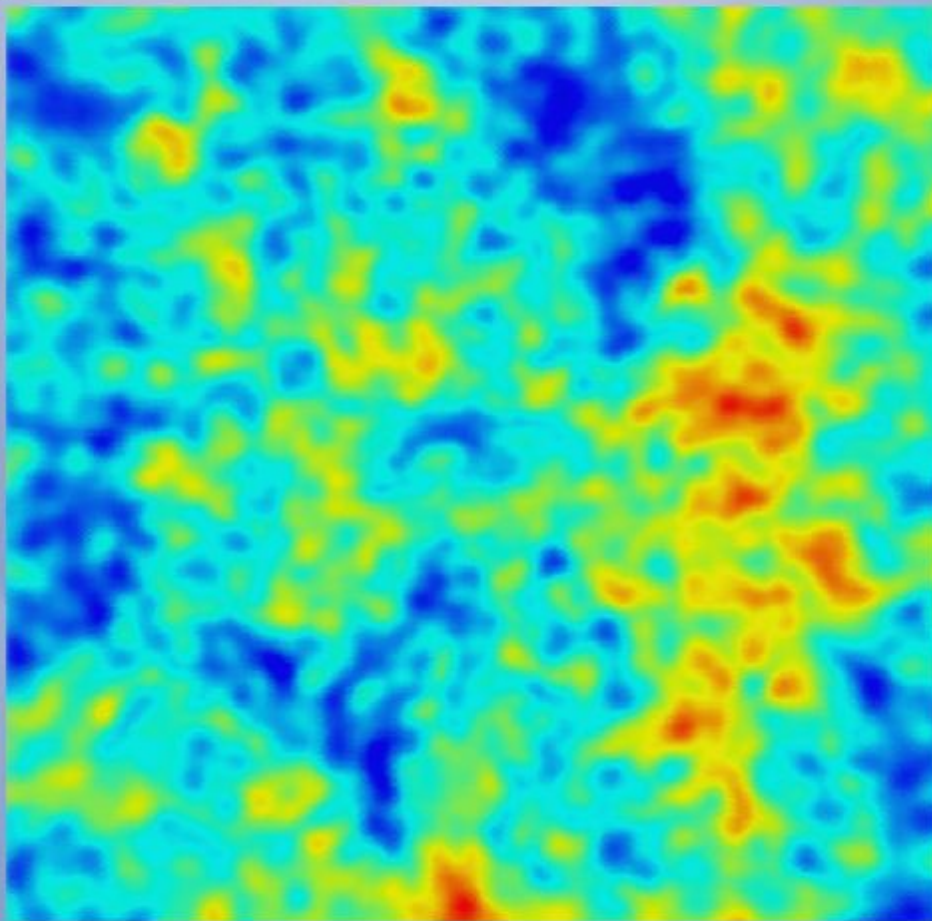
Curvature fluctuations



Yadav, and Wandelt, PRD (2005)

Tomographic reconstruction of inflationary scalar curvature

Curvature fluctuations



-0.00035 0.00035

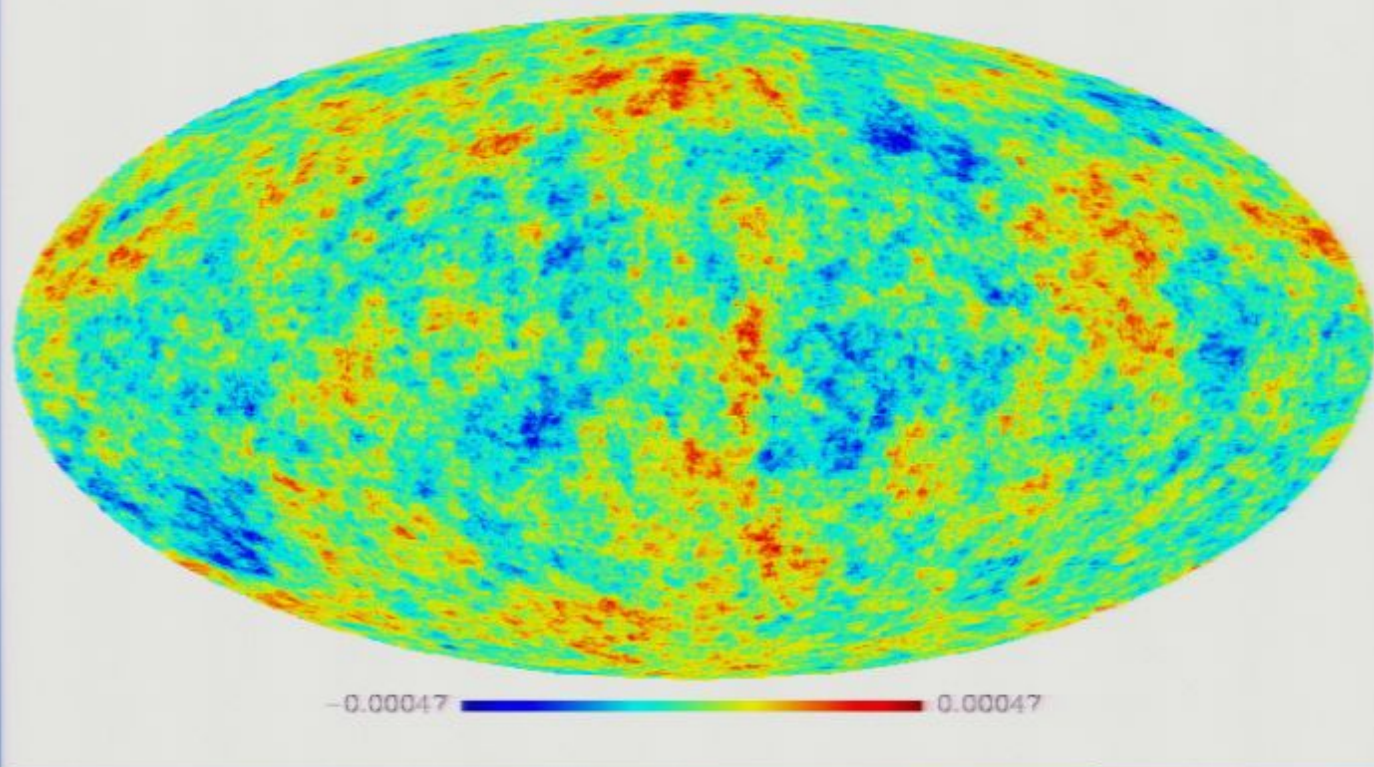
We construct filters that invert linear radiative transport.

Generates a single scalar that contains all the information from T&E.

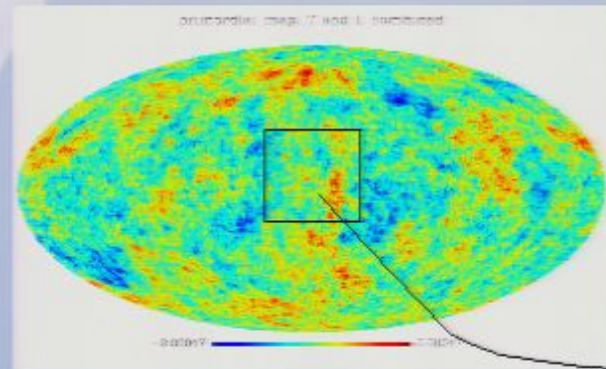
Anyone intending to test primordial non-Gaussianity (and anisotropy!) in T and/or E data should do so using curvature perturbations obtained with our filters.

Yadav and Wandelt 2006

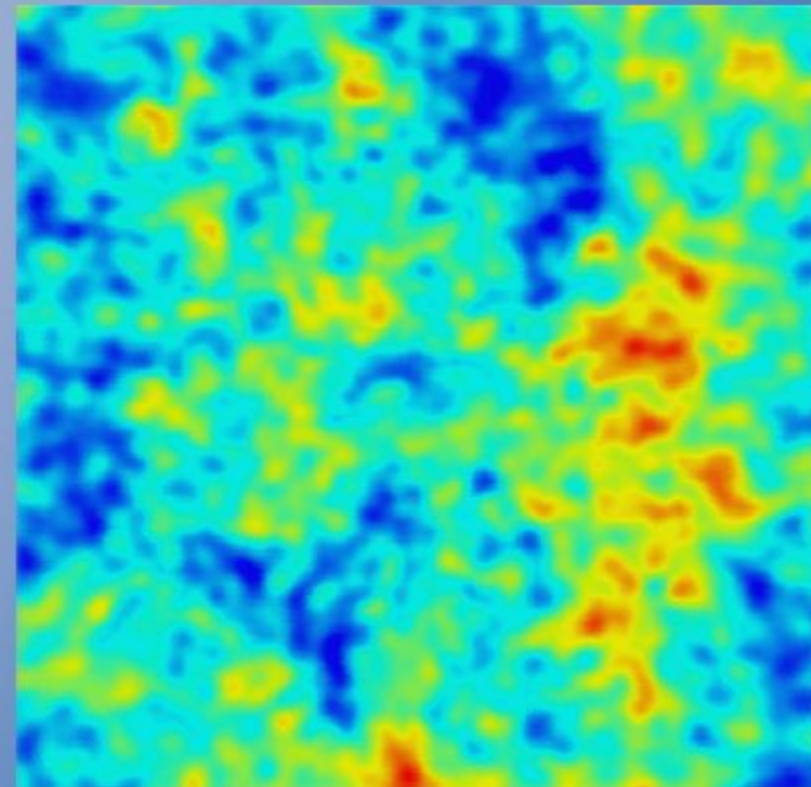
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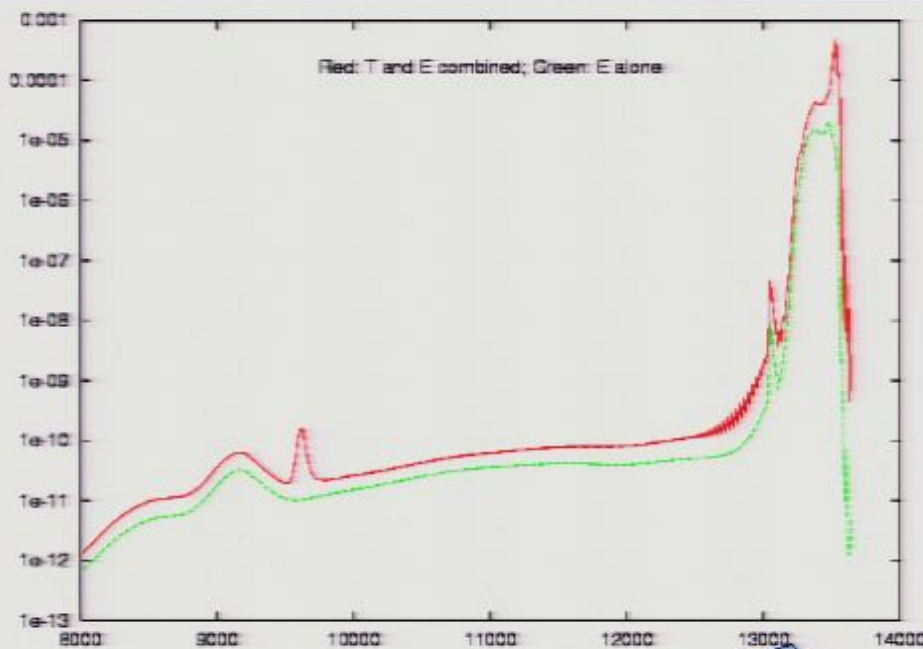
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Curvature fluctuations



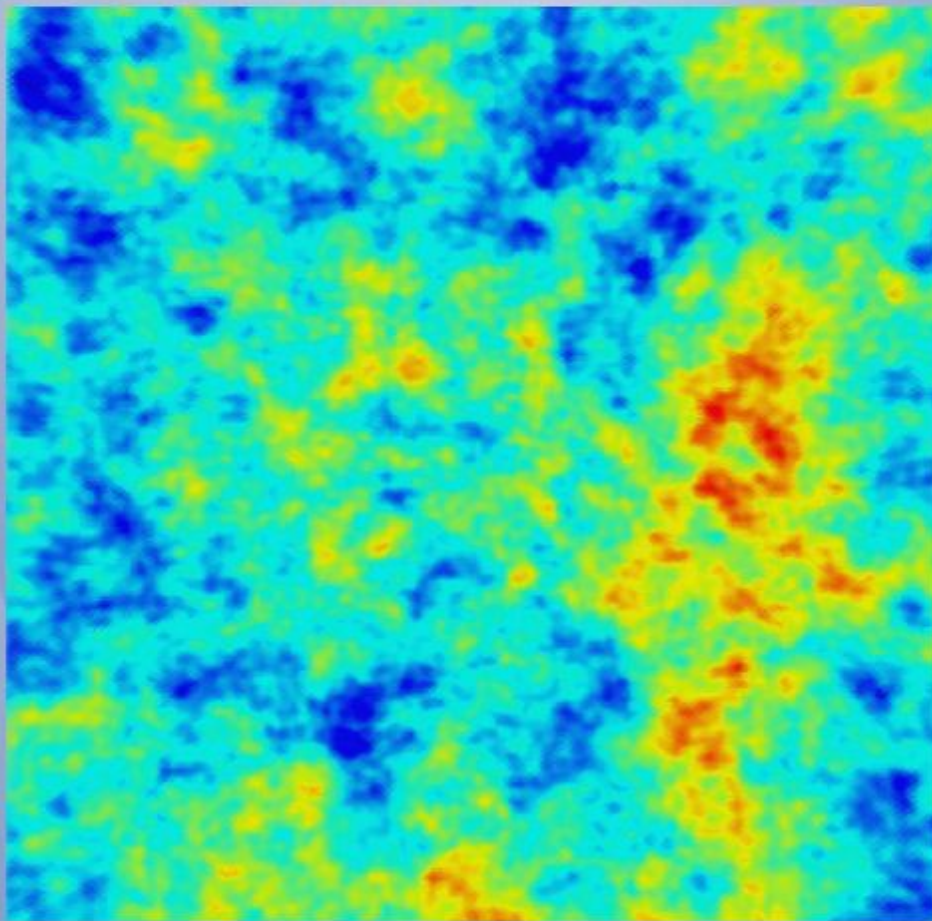
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Yadav, and Wandelt, PRD (2005)

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Curvature fluctuations



-0.00035 0.00050

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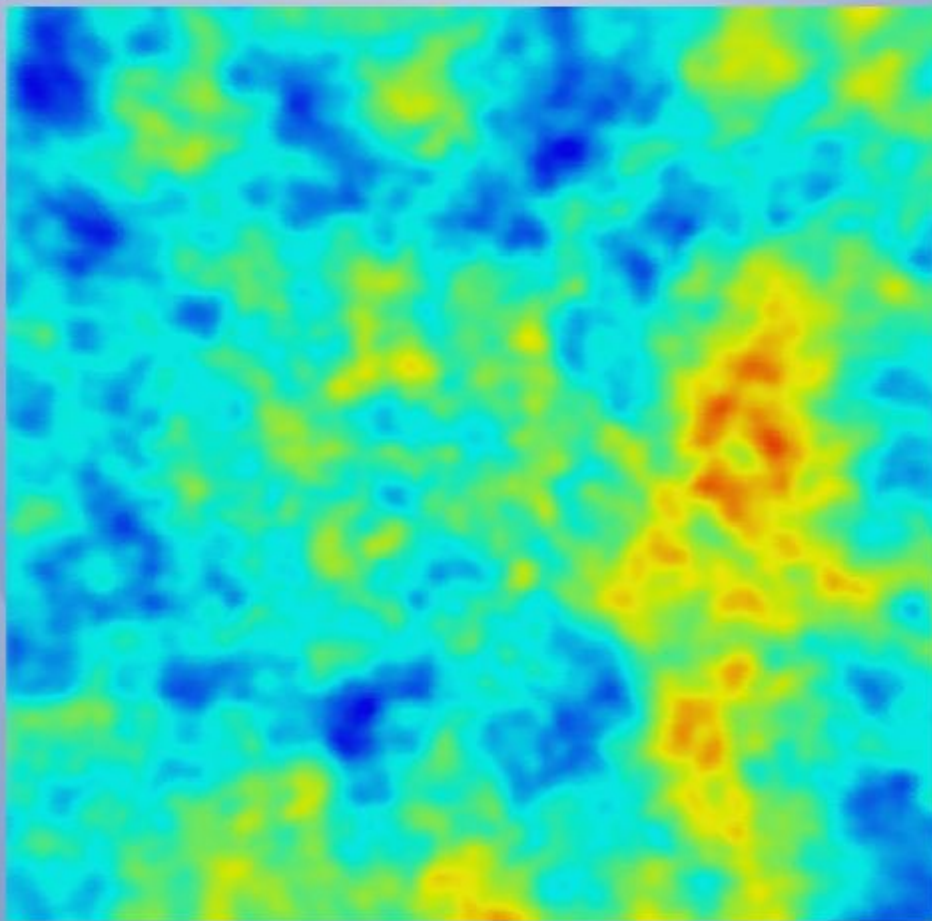
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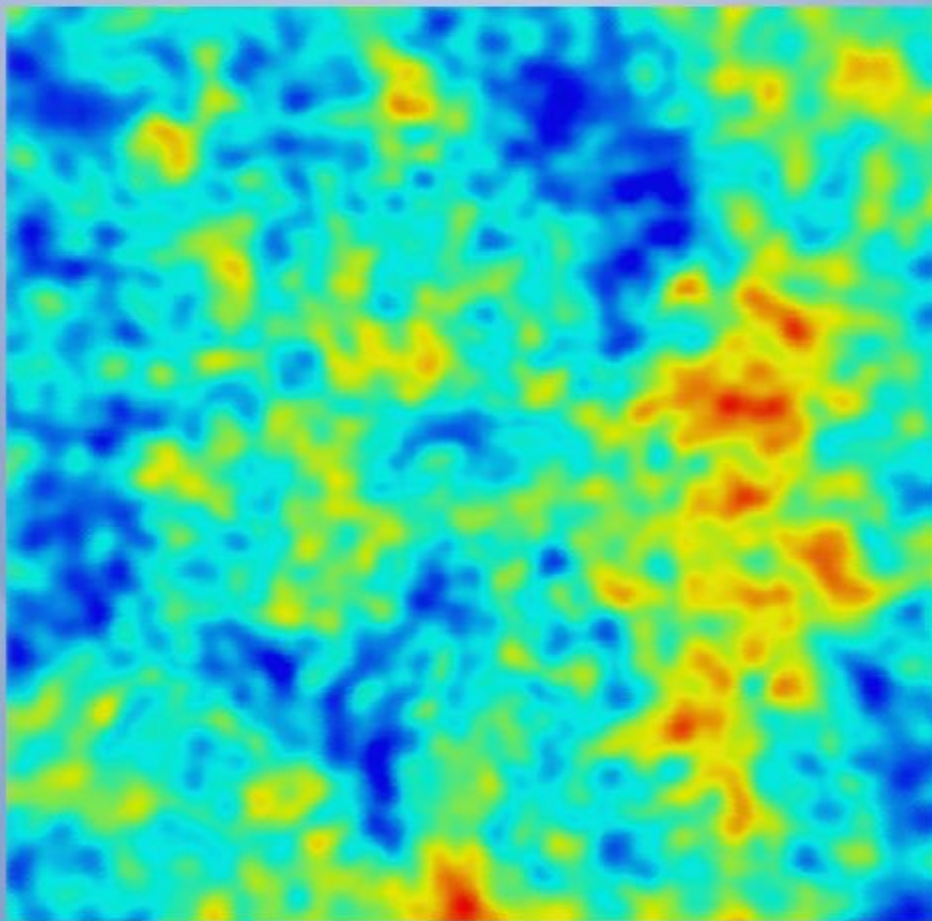
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Yadav and Wandelt 2006

How to search for f_{NL} – a specific parameterization of non-Gaussianity

$$\Phi(x) = \Phi_G(x) + f_{NL} \Phi_G^2(x)$$

Salopek & Bond 1990
Komatsu & Spergel 2001

Non-Gaussianity from Inflation

$f_{NL} \sim 0.05$ canonical inflation (single field, couple of derivatives) (Maldacena 2003, Acquaviva et al 2003)

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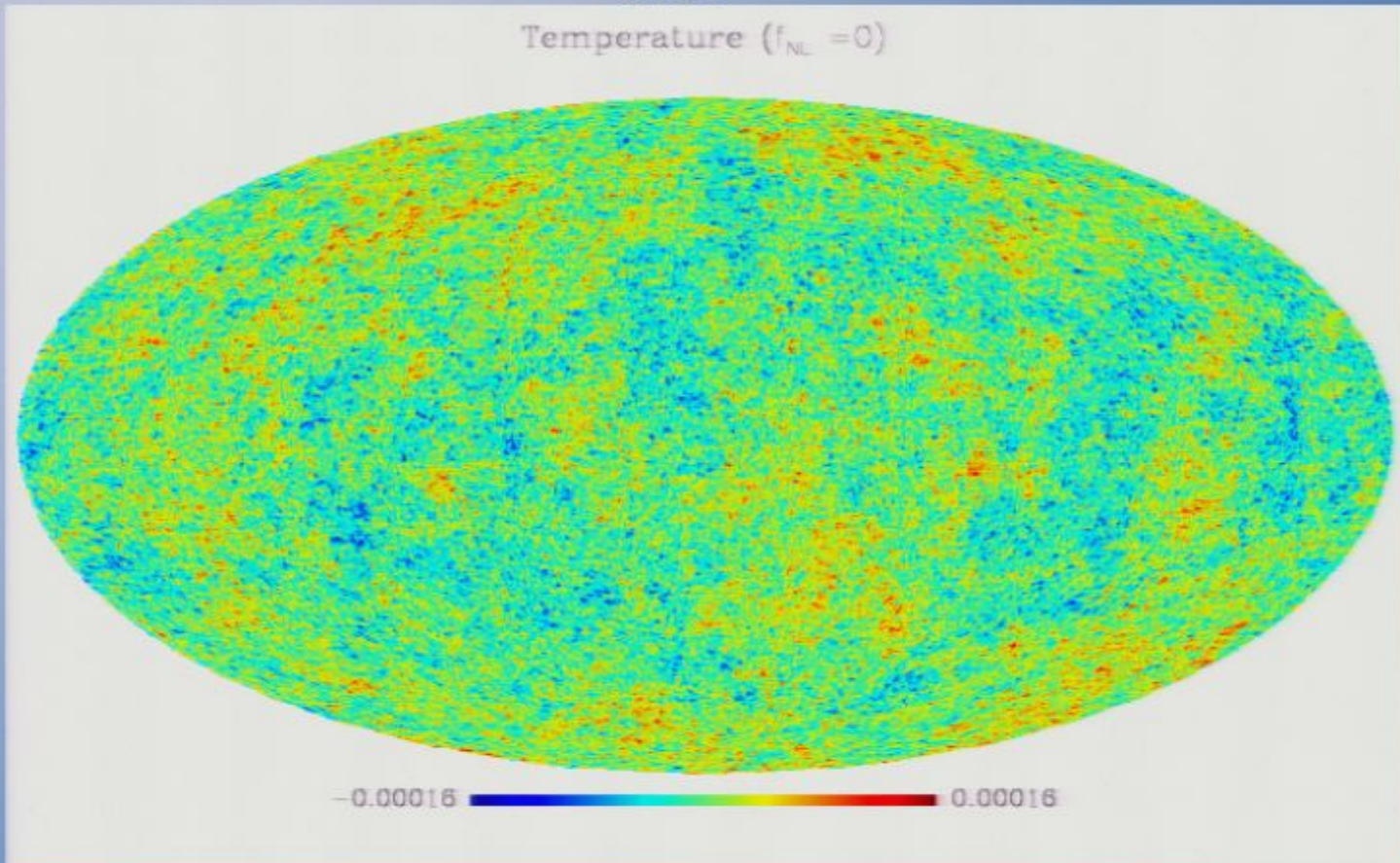
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$f_{NL} > 10$ curvaton models (Lyth, Ungarelli and Wands, 2003)

$f_{NL} \sim 100$ ghost inflation (Arkani-Hamed et al., Cosmol, 2004)

$$f_{NL} = 0$$

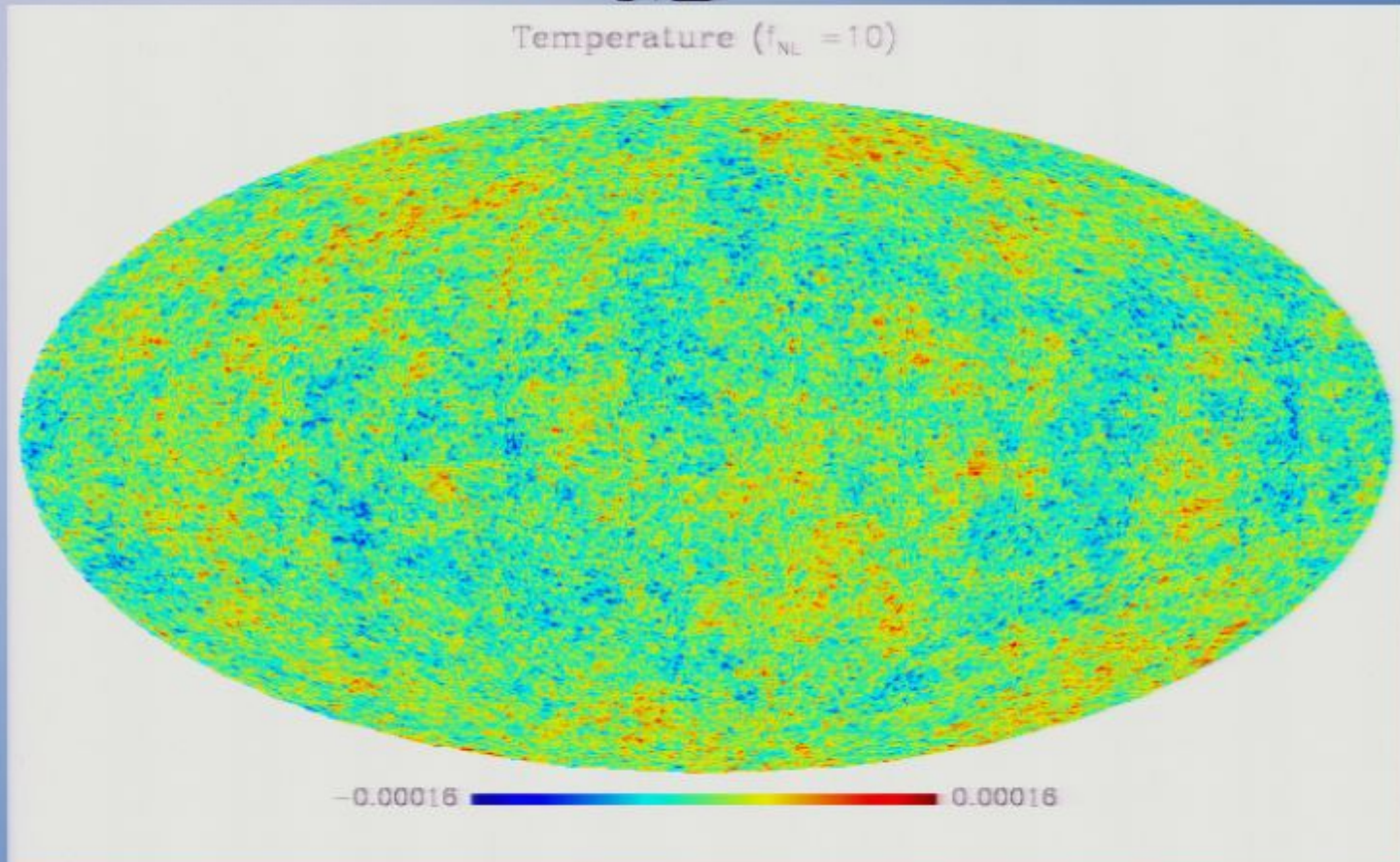
Temperature ($f_{NL} = 0$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^1$$

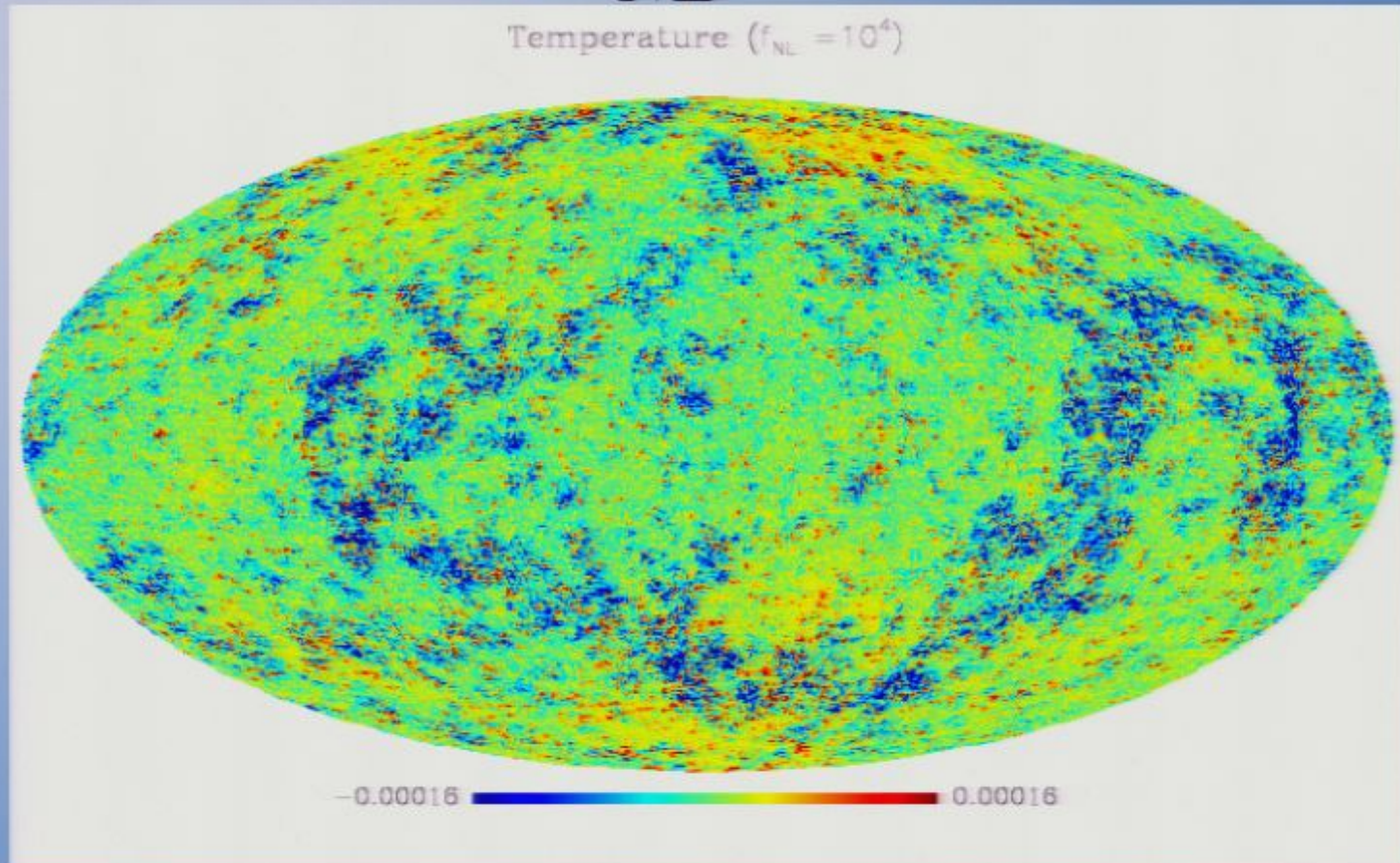
Temperature ($f_{NL} = 10$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^4$$

Temperature ($f_{NL} = 10^4$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

Why use the bispectrum?

$$B_{\text{non-Gaussian}} = 0 + f_{\text{NL}} b^2$$

$$T_{\text{non-Gaussian}} = T_{\text{Gaussian}} + f_{\text{NL}}^2 \delta T$$

For weak non-Gaussianity any even moment has a much larger contribution from Gaussian perturbations. This makes measuring the non-Gaussian component difficult.

Babich (2005): bispectrum contains nearly all the information about f_{NL} . Kogo&Komatsu: Trispectrum contains complementary information

Unfortunately evaluating all $B_{l_1 l_2 l_3}$ is too expensive.

f_{NL} phenomenology from the bispectrum

- Komatsu & Spergel 2001 – CMB bispectrum from f_{NL}
- Komatsu, Wandelt, Spergel, Banday, Gorski 2001 – f_{NL} from COBE
- Komatsu Spergel & Wandelt 2003 – fast f_{NL} estimator
- Komatsu et al (WMAP team) 2003 – WMAP1 analysis using KSW
- Babich and Zaldarriaga 2004 – temperature + polarization
- Creminelli, Nicolis, Senatore, Tegmark, Zaldarriaga 2006 – introduce linear term to improve KSW estimator
- Spergel et al (WMAP team) 2006 – WMAP3 analysis using KSW
- Creminelli, Senatore, Tegmark, Zaldarriaga 2006 – apply cubic + linear term to WMAP3 data
- Yadav & Wandelt 2005 – tomography of the curvature perturbations
- Yadav Komatsu & Wandelt 2007 – KSW generalized to T+P
- Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007 – calibrate YKW estimator against non-Gaussian simulations
- Yadav, Komatsu, Wandelt, Liguori, Hansen, Matarrese 2007 – Creminelli et al. corrected and generalized to T+P
- Yadav & Wandelt 2007 – application of YKWLHM07 to WMAP3`

Fast, bispectrum based estimator of local f_{NL}

Cubic Statistic:

$$\hat{S}_{prim} = \frac{1}{f_{sky}} \int r^2 dr \int d^2\hat{n} B(\hat{n}, r) B(\hat{n}, r) A(\hat{n}, r)$$

Komatsu, Spergel and Wandelt 2005

$$B(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{\ell m}^i \beta_{\ell}^p(r) Y_{\ell m}(\hat{n})$$

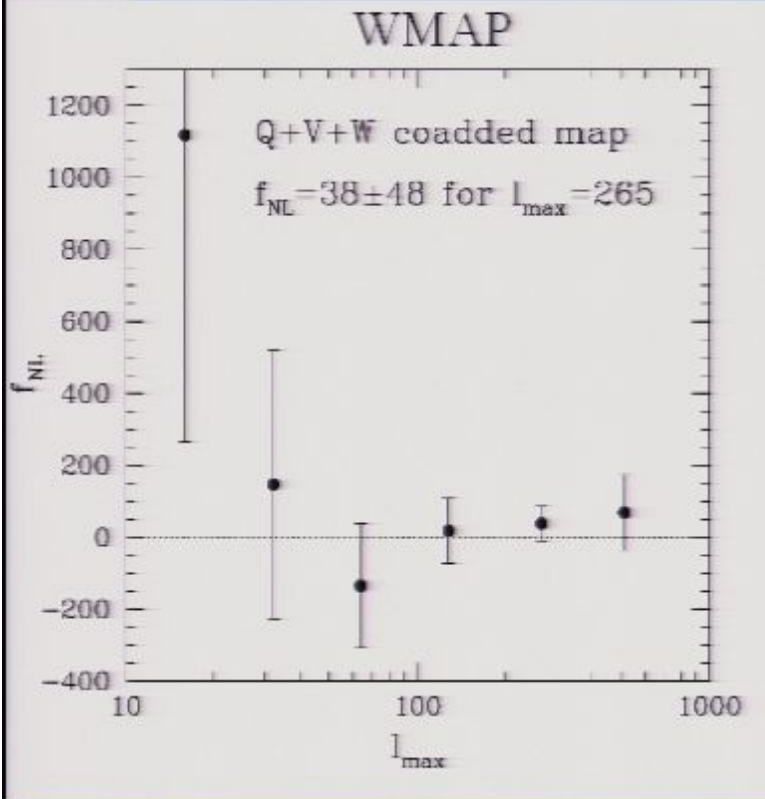
primordial perturbations

$$A(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{\ell m}^i \alpha_{\ell}^p(r) Y_{\ell m}(\hat{n})$$

configurations of the bispectrum

Abstract: All configurations of the bispectrum such that it is most sensitive to “local” primordial non-Gaussianity i.e f_{NL} .

Status before December 2007



$$-58 < f_{NL} < 137 \text{ (95\%)}$$

WMAP 1yr

$$-54 < f_{NL} < 114 \text{ (95\%)}$$

WMAP 3yr

$$-36 < f_{NL} < 100 \text{ (95\%)}$$

Creminelli et. al. 2006
using WMAP 3yr data

$$2\Delta f_{NL} \sim 70$$

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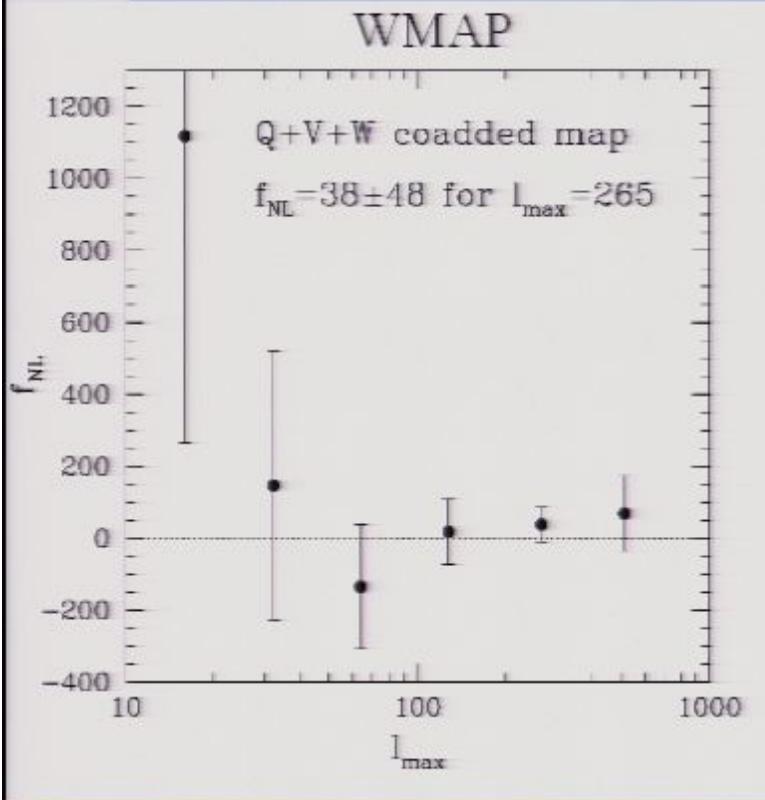
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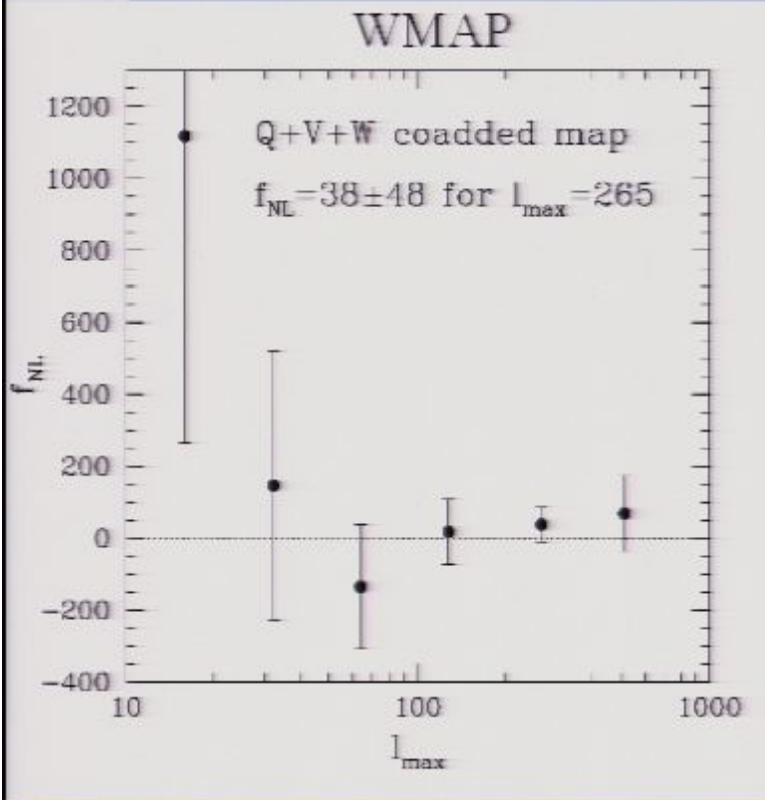
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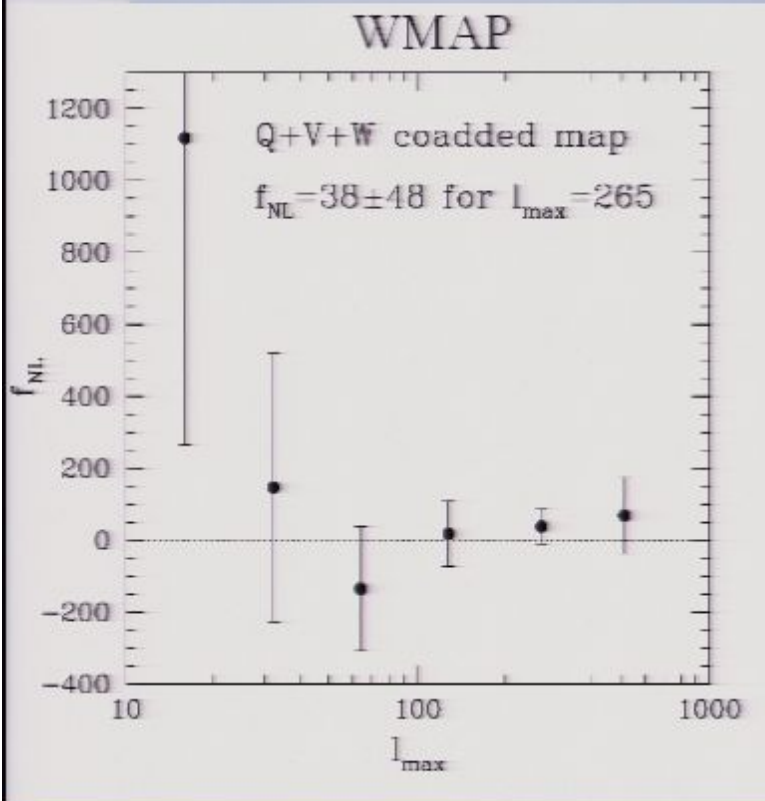
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using WMAP 3yr data

Non-Gaussianity from Inflation

$f_{NL} \sim 0.05$ canonical inflation (single field, couple of derivatives) (Maldacena 2003, Acquaviva et al 2003)

$f_{NL} \sim 0.1-100$ higher order derivatives

DBI inflation (Alishahiha, Silverstein and Tong 2004)

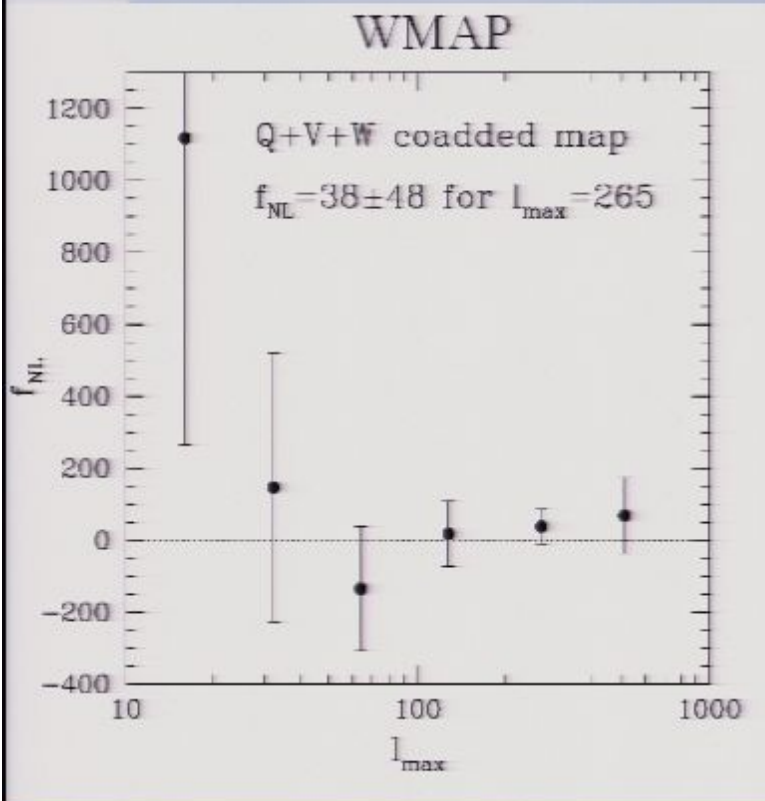
UV cutoff (Creminelli and Cosmol, 2003)

$f_{NL} > 10$ curvaton models (Lyth, Ungarelli and Wands, 2003)

$f_{NL} \sim 100$ ghost inflation (Arkani-Hamed et al., Cosmol, 2004)

$$2\Delta f_{NL} \sim 70$$

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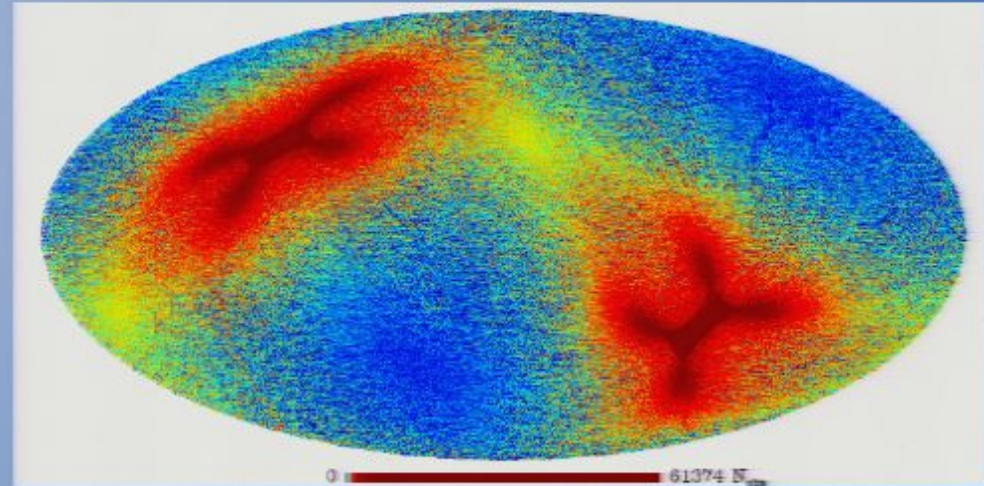
$$2\Delta f_{NL} \sim 70$$

We are far from $\Delta f_{NL} \sim 1$ but can already start putting constraints on some

models like DBI inflation, ghost inflation etc

Anisotropic sky coverage

- The KSW and YKWLHM estimators are optimal only for uniform sky coverage and noise distribution. Anisotropic noise distribution couples different l and produces excess variance.



- For non-uniform noise the addition of a linear term to the variance of the estimator (Creminelli et al. 2005)

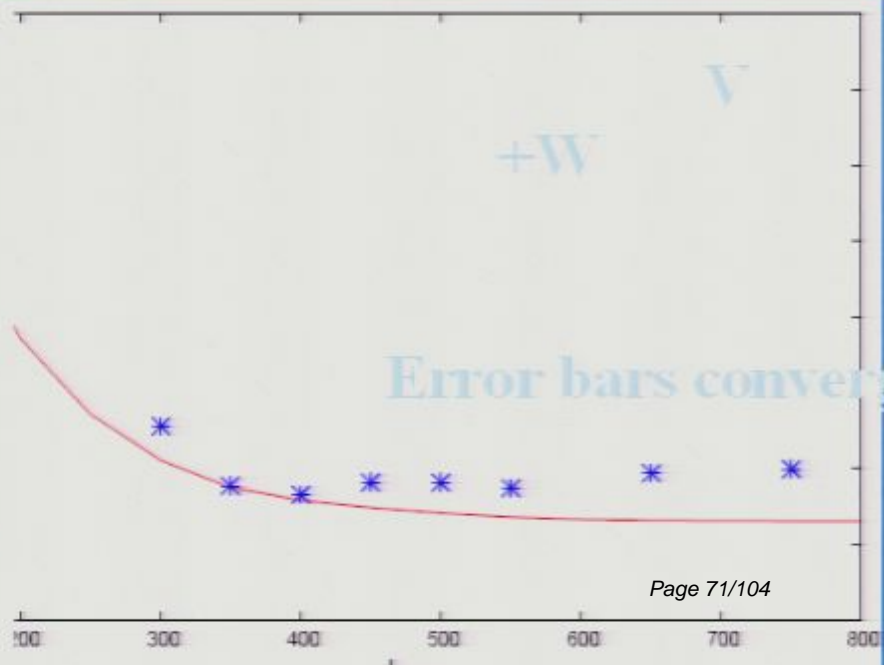
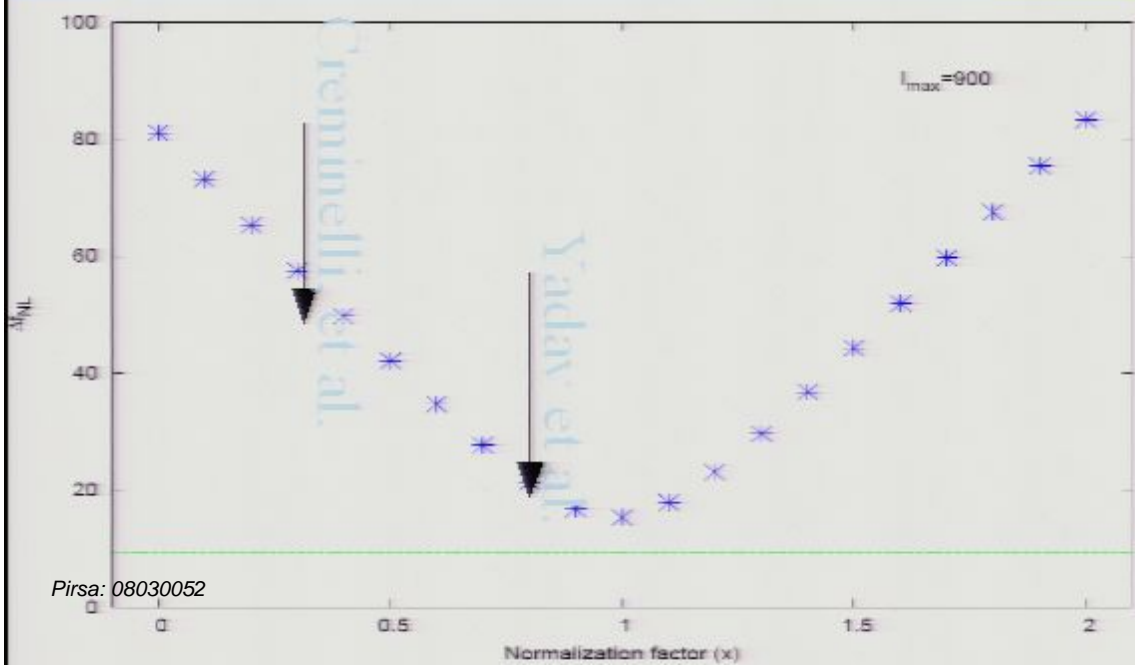
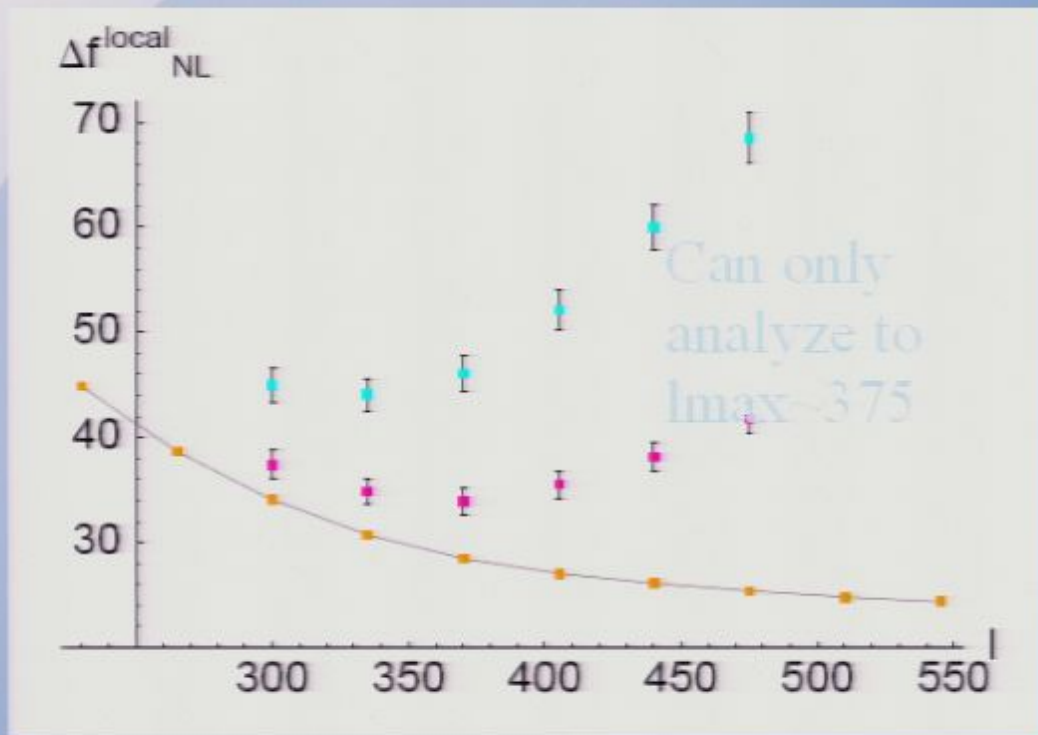
$$\hat{S}_{prim}^{linear} = \frac{-3}{f_{sky}} \int r^2 dr \int d^2\hat{n} \{B(\hat{n}, r)S_{AB}(\hat{n}, r) + S_{BB}(\hat{n}, r)A(\hat{n}, r)\}$$

- We (Yadav, Komatsu, Wandelt, et al. arxiv:0711.4933) generalized this estimator to include polarization; and discovered and corrected an error in the linear term.

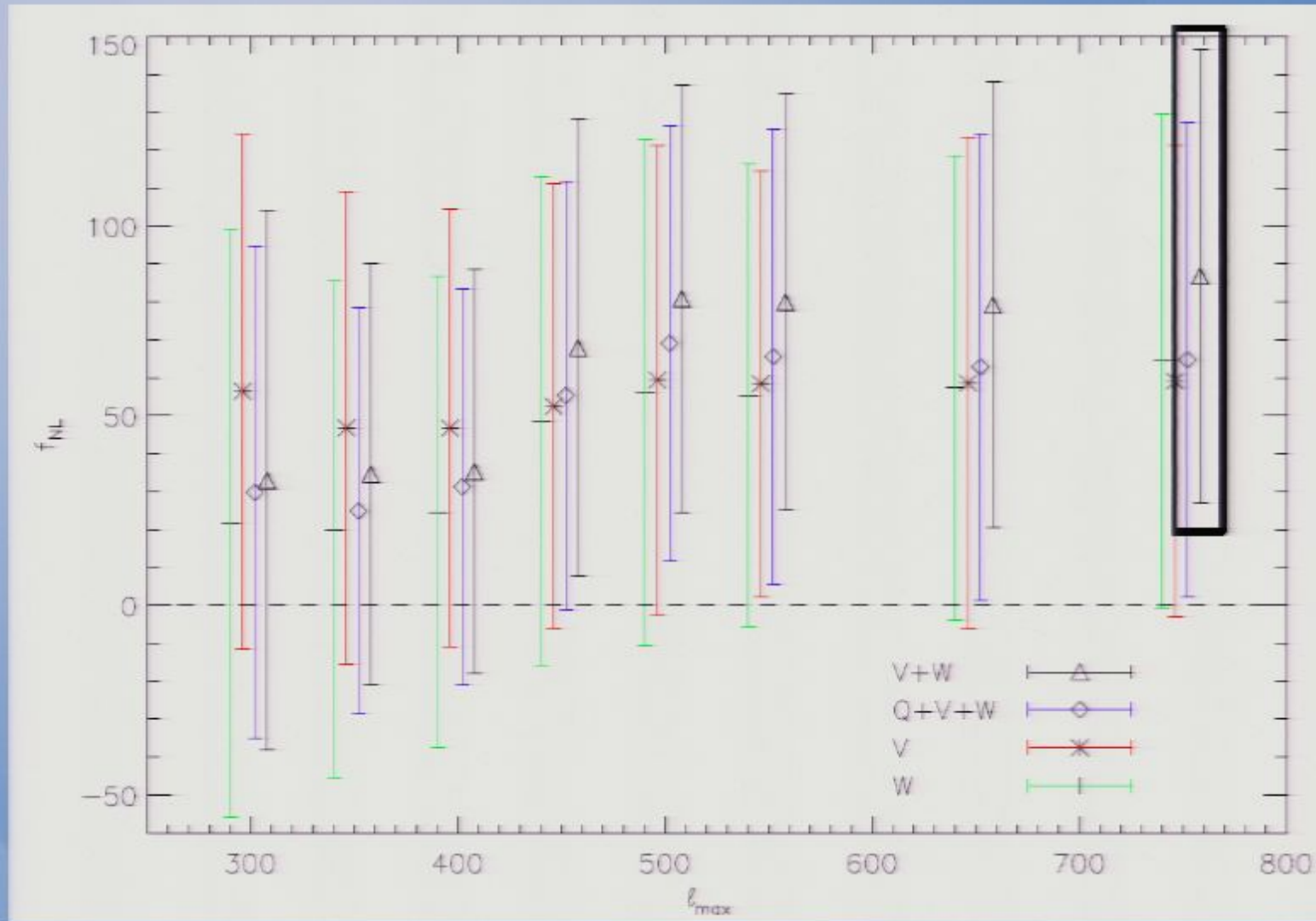
$$A(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{lm}^i \alpha_\ell^p(r) Y_{lm}(\hat{n})$$

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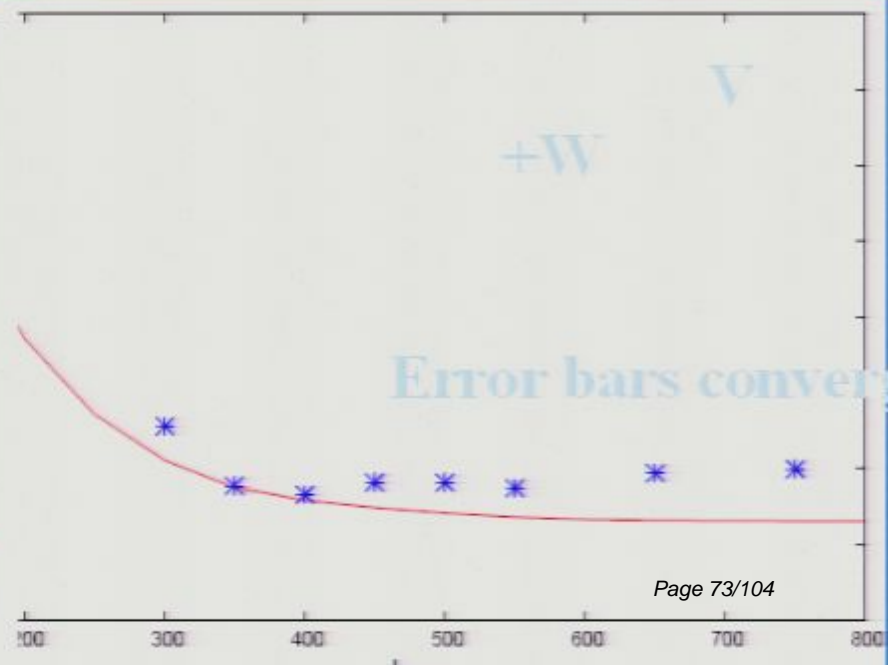
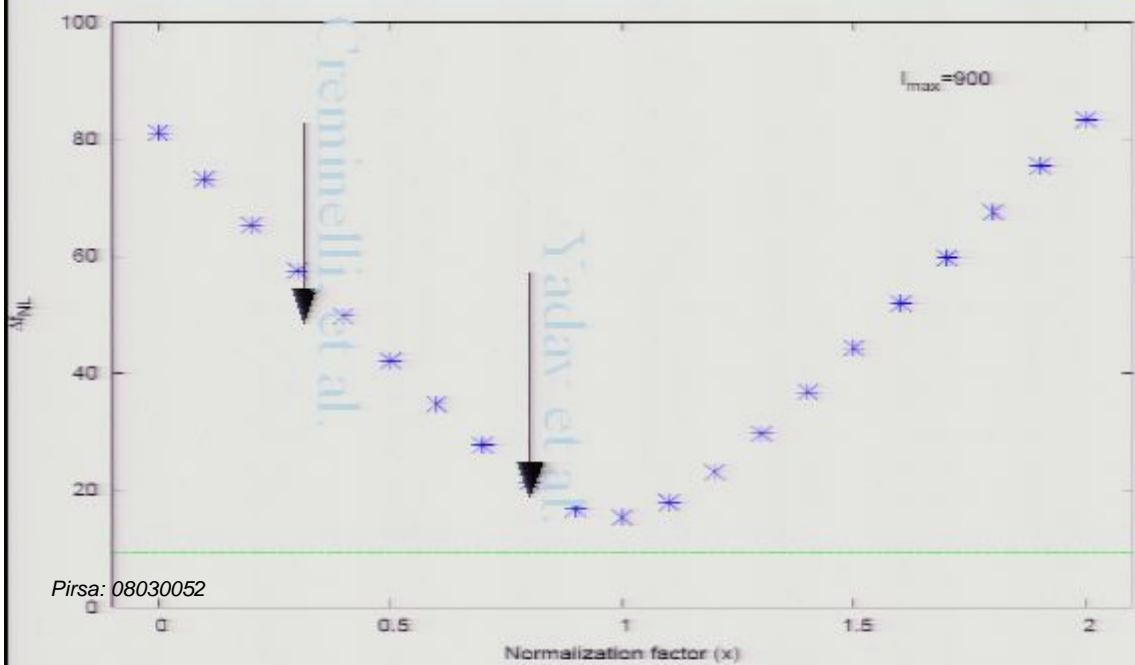
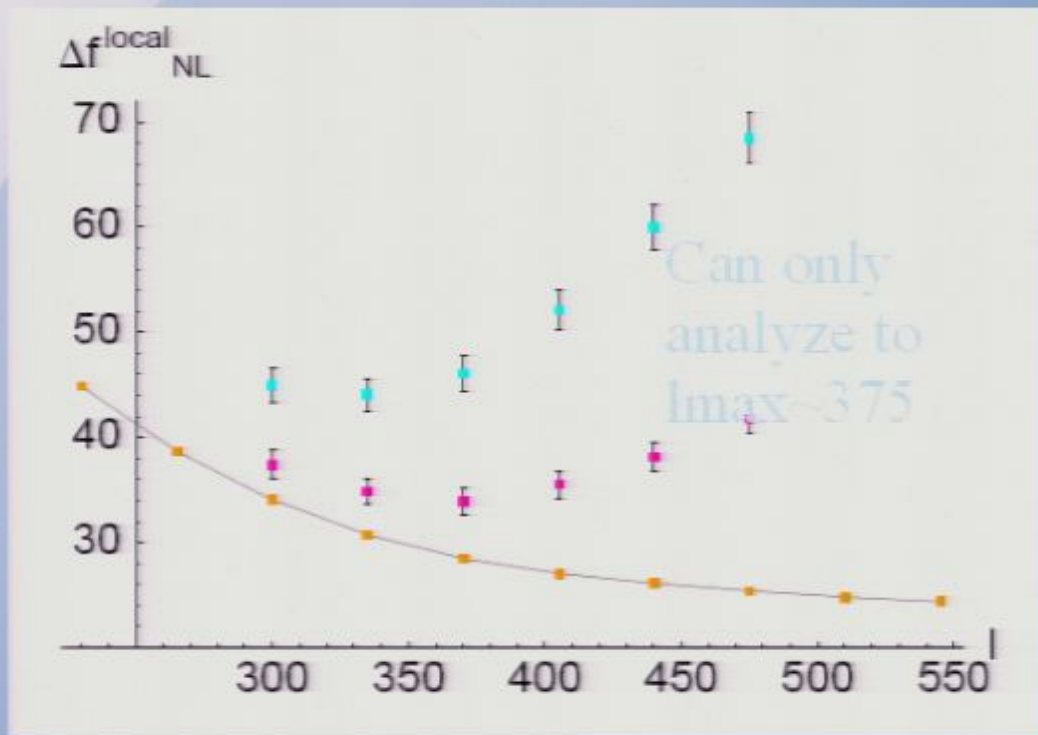
What is new in Yadav & Wandelt 2008?



Our result:



What is new in Yadav & Wandelt 2008?





Slides

- Primalordial non-Gaussianity - a new frontier
Benjamin D. Wandelt
Amit P. Yadav
- The Cosmic Micr...
- Why are we interested in cosmology?
The big questions are:
"What is the fundamental theory, valid at the highest energies?"
"What happened at $t = 0$?"
- Why are we inte...
- The Big Micr...
- Slide 3
- How do we study what happens at the highest energy scales and at the shortest time scales?
Click to add text.

Normal Outline Notes Handout Slide Sorter

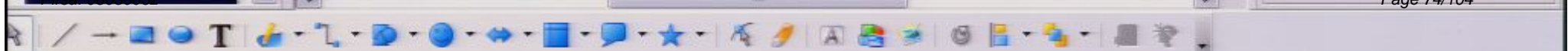
Primordial non-Gaussianity
-
a new frontier

Benjamin D. Wandelt
Amit P. Yadav
UIUC Physics/Astronomy

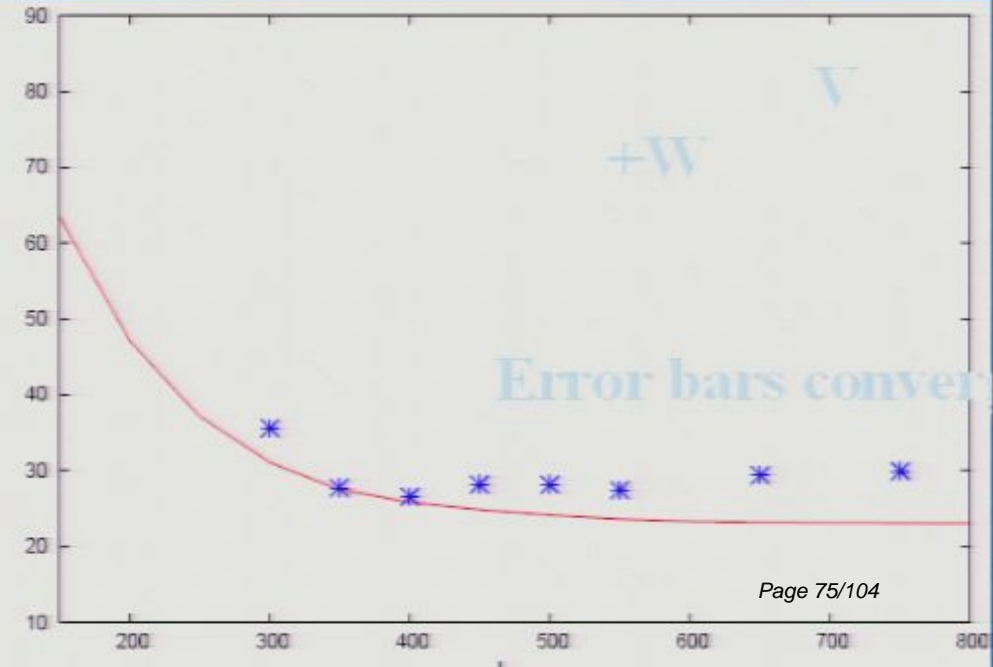
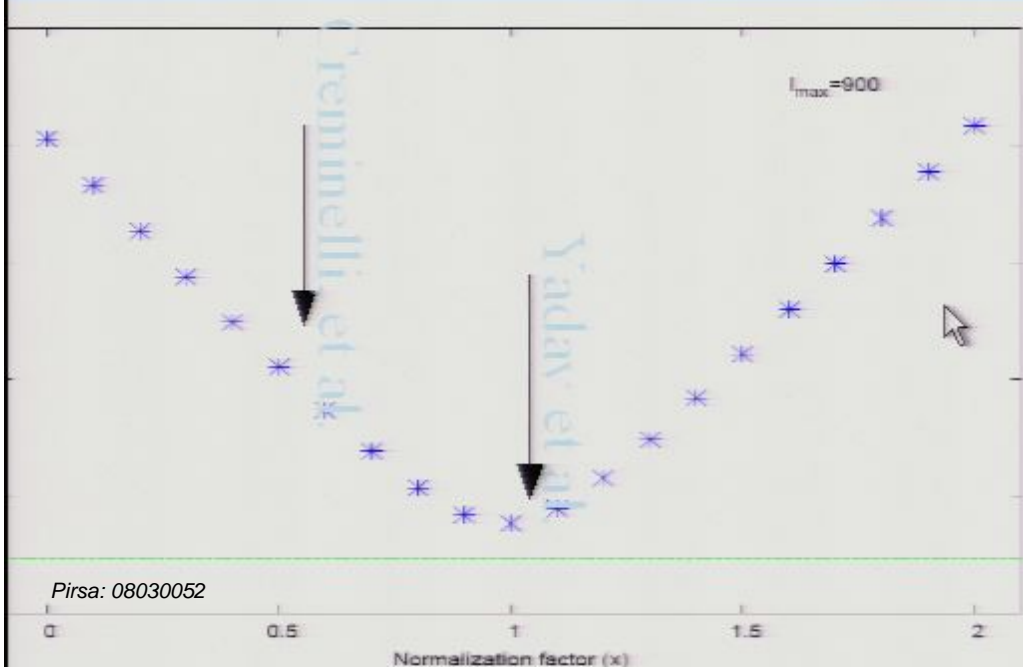
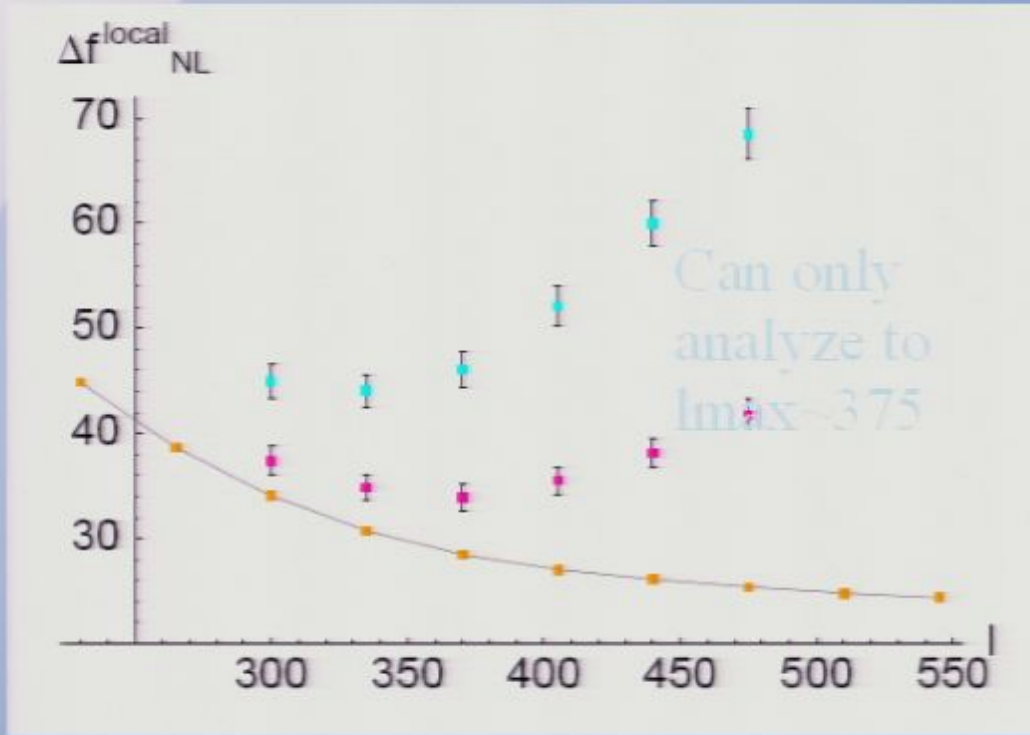
Physics Illinois
ASTRONOMY
UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

Tasks View X

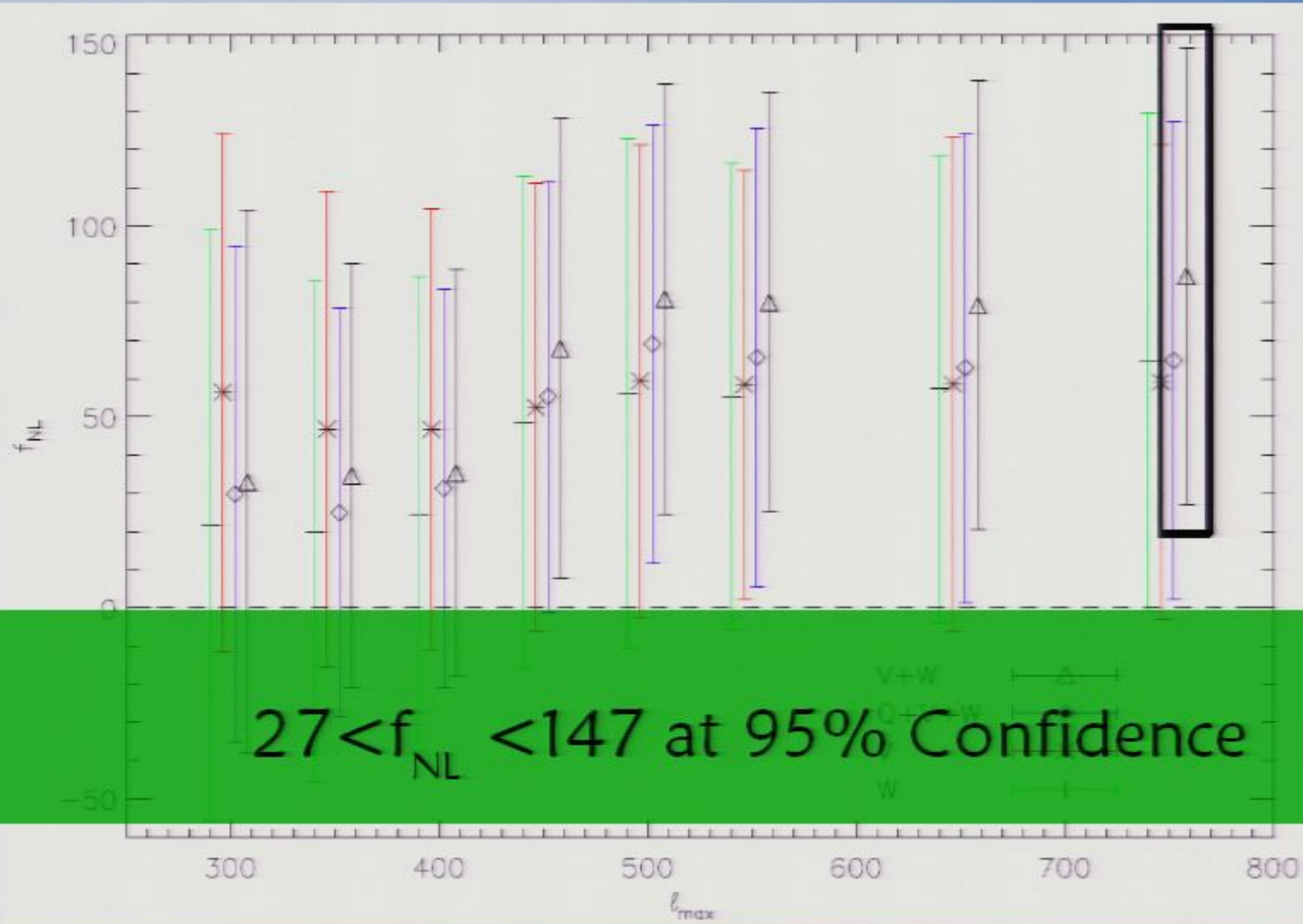
- Master Pages
- Layouts
- Custom Animation
- Slide Transition



What is new in Yadav & Wandelt 2008?

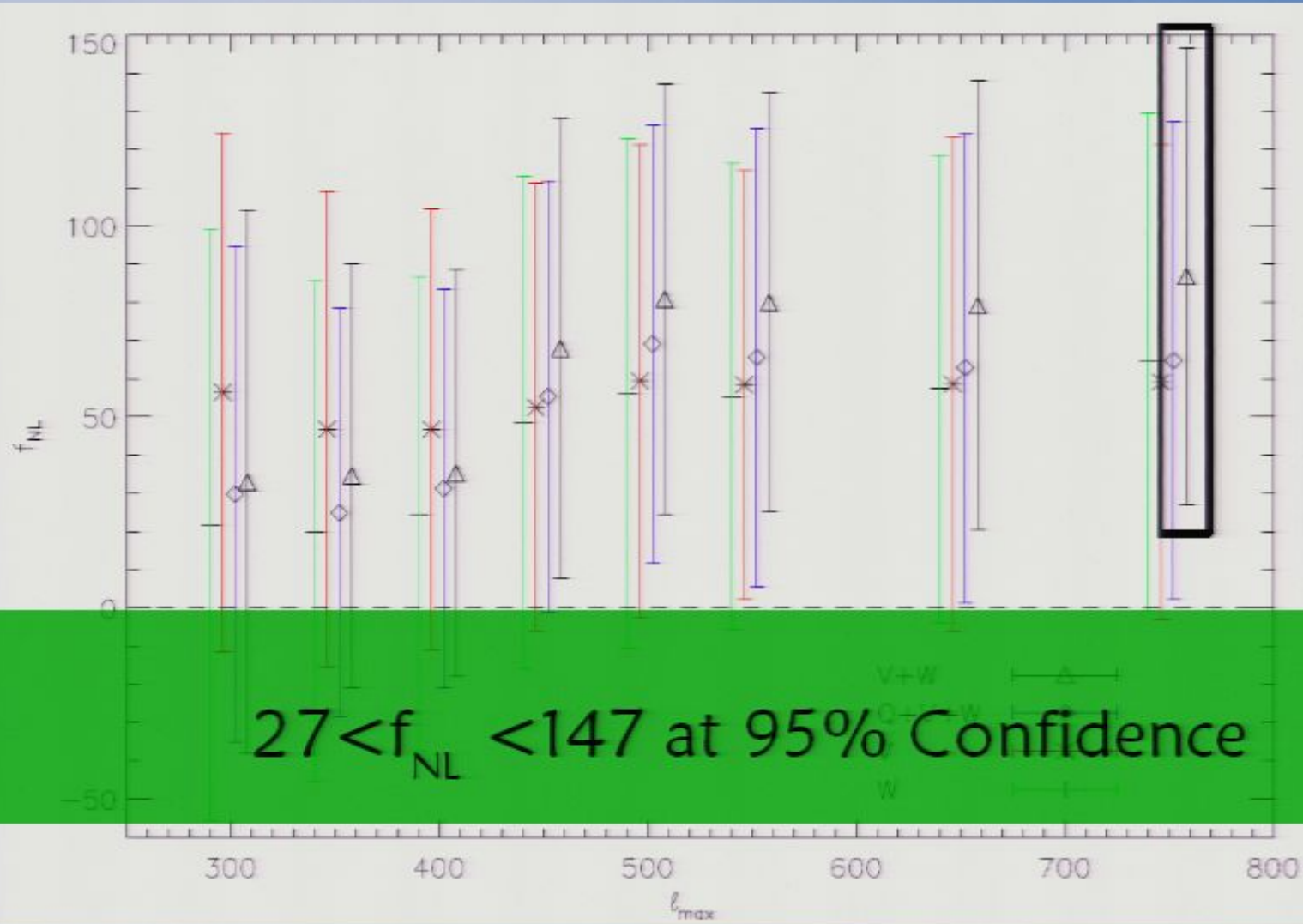


Our result:



$27 < f_{NL} < 147$ at 95% Confidence

Our result:

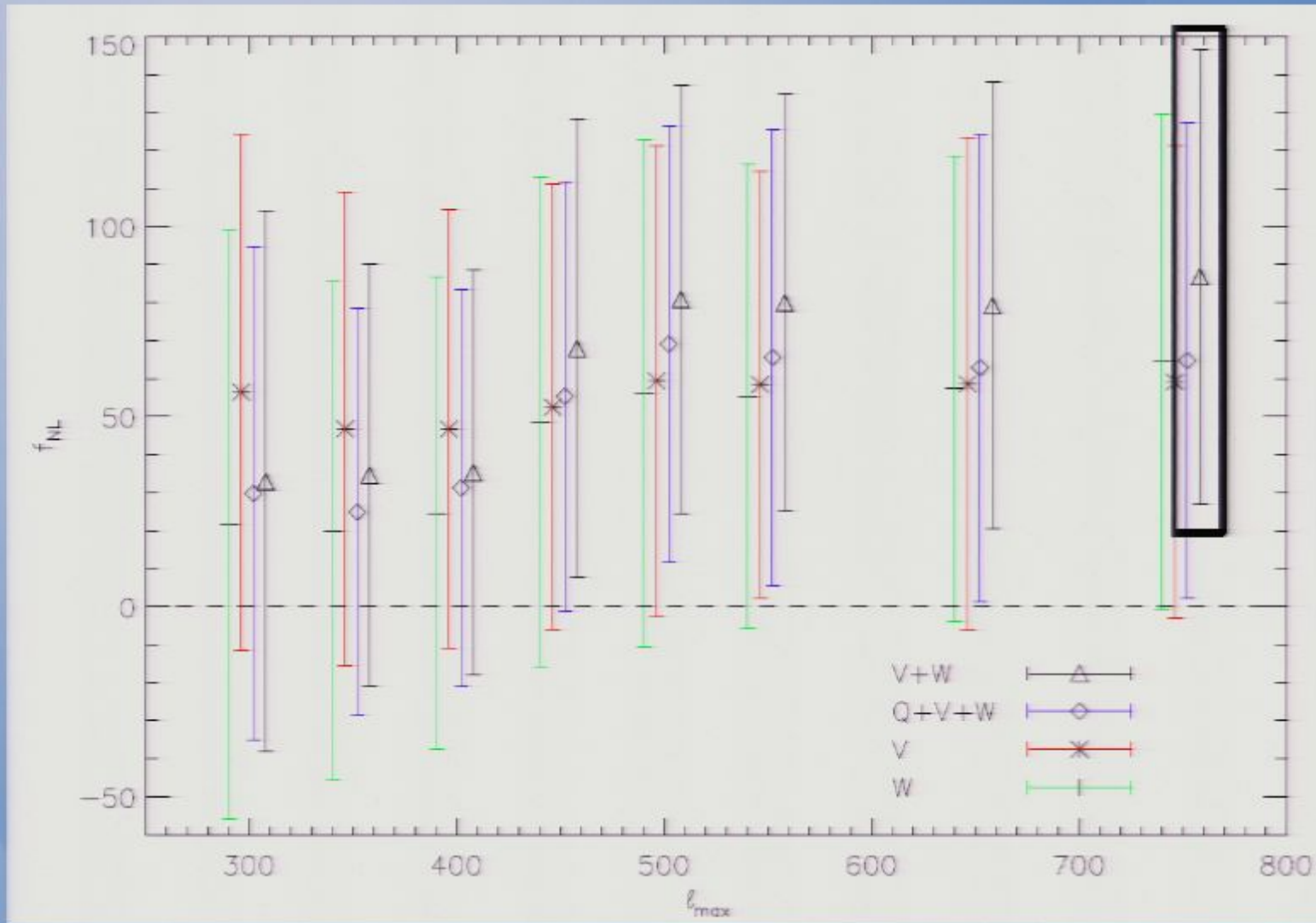


Questions you might ask

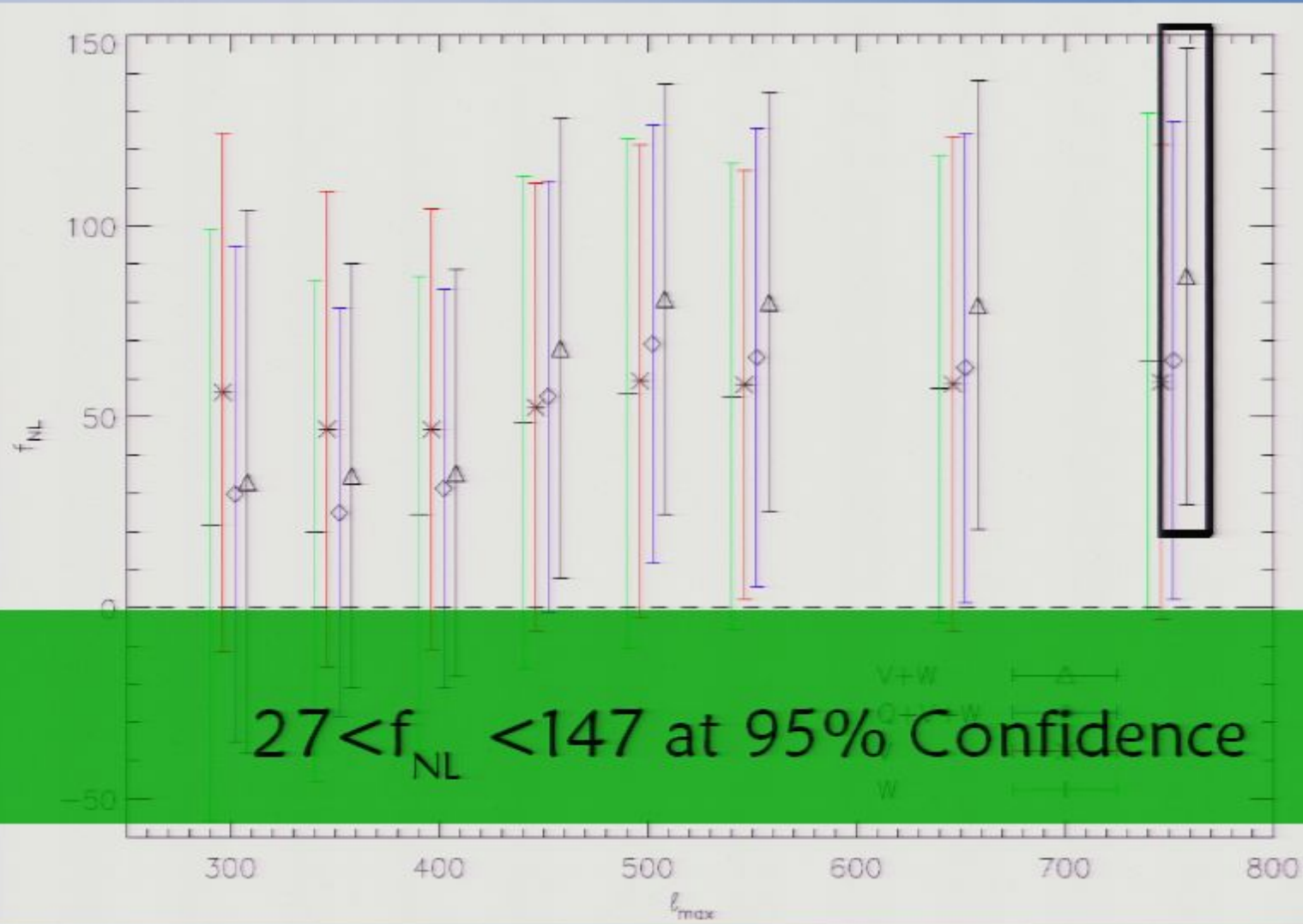
Might his result be due to...

- Instrument systematics?
- Foregrounds?
- Secondary anisotropies?
- Just rediscovery of other non-Gaussian signals?
- Noise fluctuation?

Our result:



Our result:



Questions you might ask

Might his result be due to...

- Instrument systematics?
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Instrument systematics?

1) Beam asymmetries

- If the CMB is Gaussian, no asymmetry of the main beam can produce non-vanishing bispectrum.
- If there are large side-lobes that spread foreground around the sky they will produce large scale features – unlikely to affect the high l regime. Further, we do not see evidence for frequency dependence.

Instrument systematics? II: WMAP Noise

- Noise correlations (striping)

- As long as noise is Gaussian, **no** noise correlations will produce a bispectrum.

- Non-Gaussian noise?

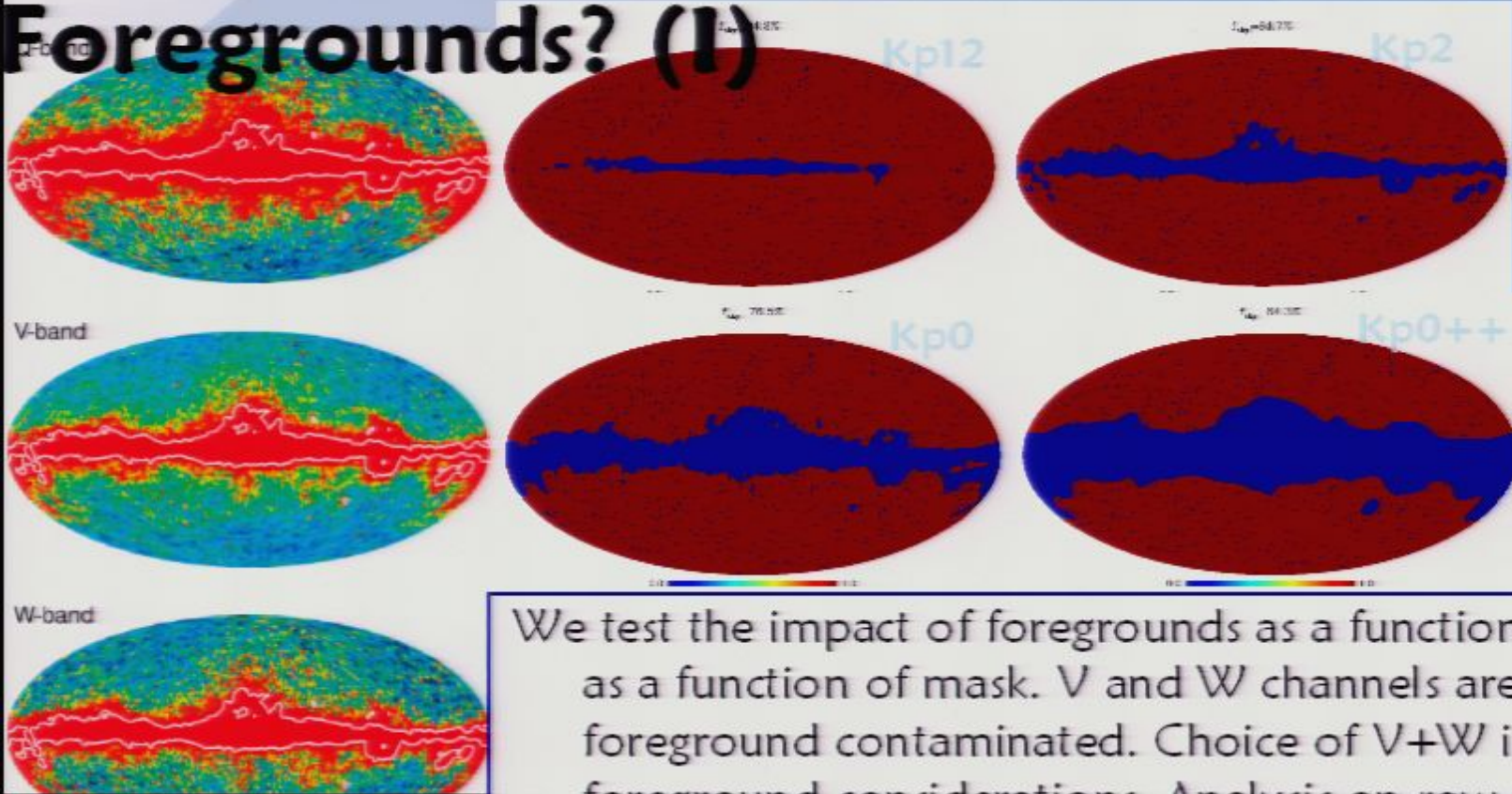
Analyzed differences of WMAP yearly maps

- year1-year2 $f_{NL}=1.1$ (+/- ~60 at 95% C.L.)
- year2-year3 $f_{NL}=1.8$
- year1-year3 $f_{NL}=-3.4$

- **So to explain our results an instrumental systematic has to be 1) non-Gaussian, 2) the same in individual years and 3) mimic the specific**

bispectrum signature of f_{NL} .

Foregrounds? (I)



We test the impact of foregrounds as a function of frequency and as a function of mask. V and W channels are the least foreground contaminated. Choice of V+W is driven by foreground considerations. Analysis on raw maps to avoid FG oversubtraction.

max	$f_{\text{sky}} = 94.2\%$	$f_{\text{sky}} = 84.7\%$		
	Kp12	Kp2	Kp0	
50	-3145.22	-26.68	34.62	19.24
50	-1425.06	-15.63	67.94	64.69
50	-1509.92	-13.09	79.99	83.53
50	-1559.91	-22.43		
50	-1575.11	-22.81	86.81	86.52

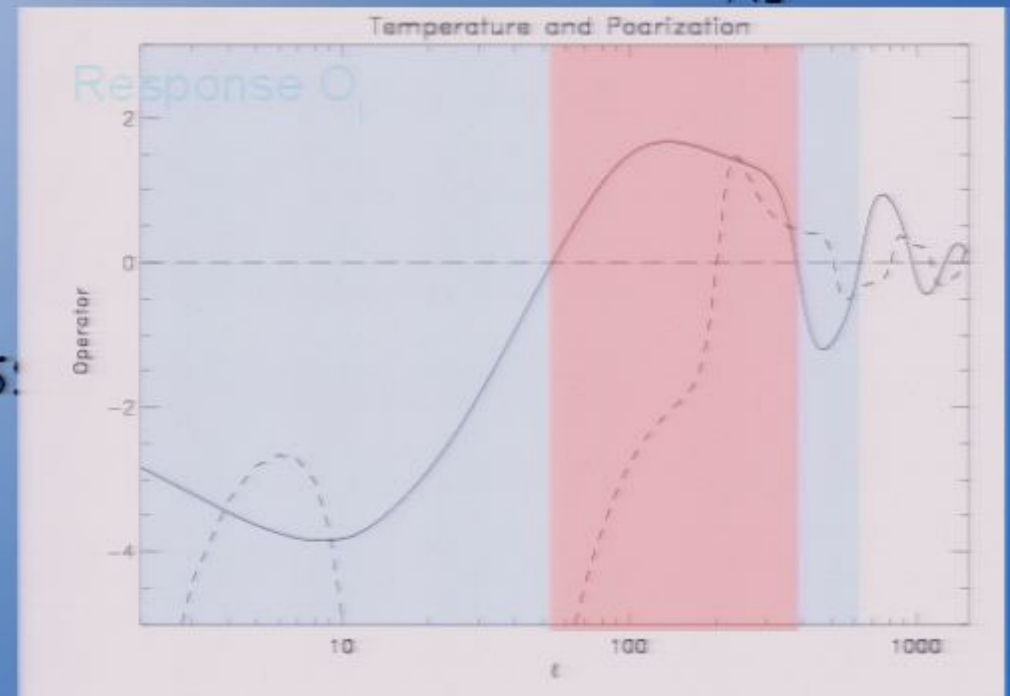
stable beyond kp0



Foregrounds? (II)

- Remember – large scale skewness in the Temperature map corresponds to *negative* f_{NL} .

- The added l modes at $400 < l < 550$ correspond to modes where positive skewness also gives *negative* contributions.



- At intermediate scales positive skewness gives *positive* f_{NL} .

Foregrounds? (III)

- WMAP Raw maps vs WMAP foreground subtracted maps
 - Foreground subtracted maps do not show negative f_{NL} behavior
 - Same level of f_{NL} , slightly higher for FG subtracted maps
- Gaussian CMB + Foregrounds + WMAP Noise

ℓ_{max}	f_{NL}			
	Kp12	Kp2	Kp0	kp0++
750	-1105	-41.7	-5.8	-0.3

- negative for smaller masks
- goes to zero by the time you reach Kp0 mask
- is consistent with zero for masks greater than kp0

Secondary Anisotropies?

- Point sources, including SZ
 - Orthogonal overlap with primordial bispectrum. Bias of $|f_{NL}| < 1$. SZ and point sources have opposite signs.
- Serra and Cooray (arxiv:0801.3276)
 - dominant secondary confusion level to WMAP bispectrum arises from
 - ISW-lensing bispectrum (positive bias)
 - SZ-lensing bispectrum (negative bias)
 - **If $f_{NL} = 20$** effective bias around 10%. **Negligible** for $f_{NL} > 20$, because effects add in quadrature.

Re-discovery of another non-Gaussian signal?

- Larson/Wandelt (hot and cold spots not hot or cold enough):
 - at smaller angular scales **X**
 - symmetric-> no odd correlation. Probably noise model.
- The Cold Spot (Vielva et al. 2004) is localized in the map and covers a particular range in scale. **X**
Preliminary result: **$f_{NL} = 94 \pm 60$ (95% C.L.)**
- Large Scale anomaly? Can check by removing large scale signal. Preliminary result: **X**

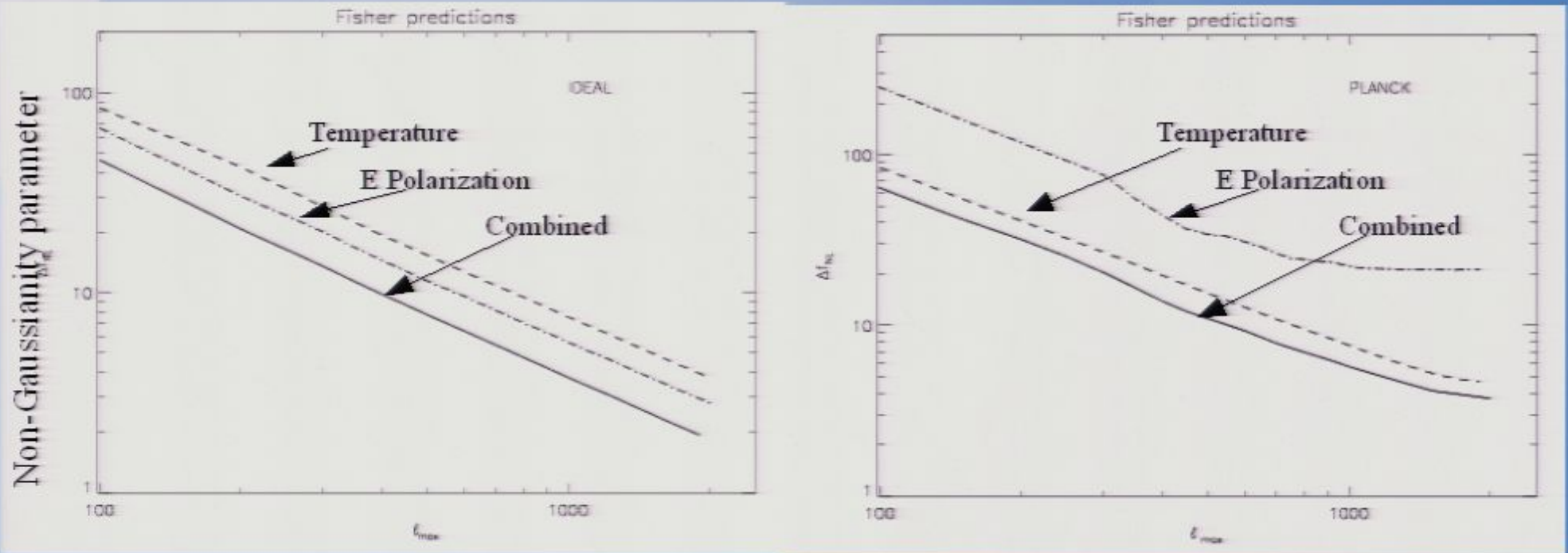
Noise fluctuation?

- Possible.
- It's a 2.5-3 sigma result. $P \leq 0.01$

2.5 sigma for conservative increase of error bar for possible systematics

The most aggressive interpretation of the data would be a 3.3 sigma effect (correcting for negative foreground bias and using best fit WMAP parameters)

Non-Gaussianity post WMAP



Smaller scales →

For an Ideal CMB experiment and using both temperature and polarization we can get down to $\Delta f_{NL} \sim 1$

For Planck the Cramer Rao limit is $\Delta f_{NL} \sim 3$.

Summary and Conclusions

- $\Delta f_{NL} \sim 30$ for all of WMAP 3 using YKWLHM07 and WMAP best fit parameters (statistical)
- First bispectrum-based analysis of the full WMAP3 data
- First significant departure of f_{NL} from 0 at $>99\%$ C.L.
- Estimators tested against Gaussian and non-Gaussian simulations with and without inhomogeneous noise
- If any bias, it is likely to be negative. Guess of systematic error bar: $-0/+5$

Our detailed tests back up the analysis and arguments in Yadav & Wandelt 2007.

Conclusions and Outlook

- **“If our result holds up to scrutiny and the statistical weight of future data [...] we conclude that single field slow roll inflation is disfavored by the WMAP data.”**

Outlook

- New data to come soon! Forecasts:
 - WMAP 5 year: $\Delta f_{NL} \sim 25$ (See Eiichiro's talk!)
 - WMAP 8 year: $\Delta f_{NL} \sim 21$
- $\Delta f_{NL} \sim 5$ from Planck T and E polarization (in <5 yrs!)
- Cross-checks using temperature and polarization
- f_{NL} is complementary to tensor modes as a way to distinguish between classes of models that give similar predictions for the two-point correlations
- Great news for very early Universe cosmology!

No Signal

VGA-1

No Signal

VGA-1

No Signal

VGA-1

No Signal

VGA-1

No Signal

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No Signal

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No Signal

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No Signal
VGA-1

WMAP 5-Year Results: Measurement of f_{NL}

Eiichiro Komatsu

University of Texas at Austin

“Origins and Observations of Primordial Non-Gaussianity”

Perimeter Institute, March 8, 2008