

Title: Inflation in String Theory

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Abstract: TBA



# Microscopic Aspects of Inflation in String Theory

Daniel Baumann

Princeton University

Perimeter Institute, March 2008

# Inflation

A period of accelerated expansion

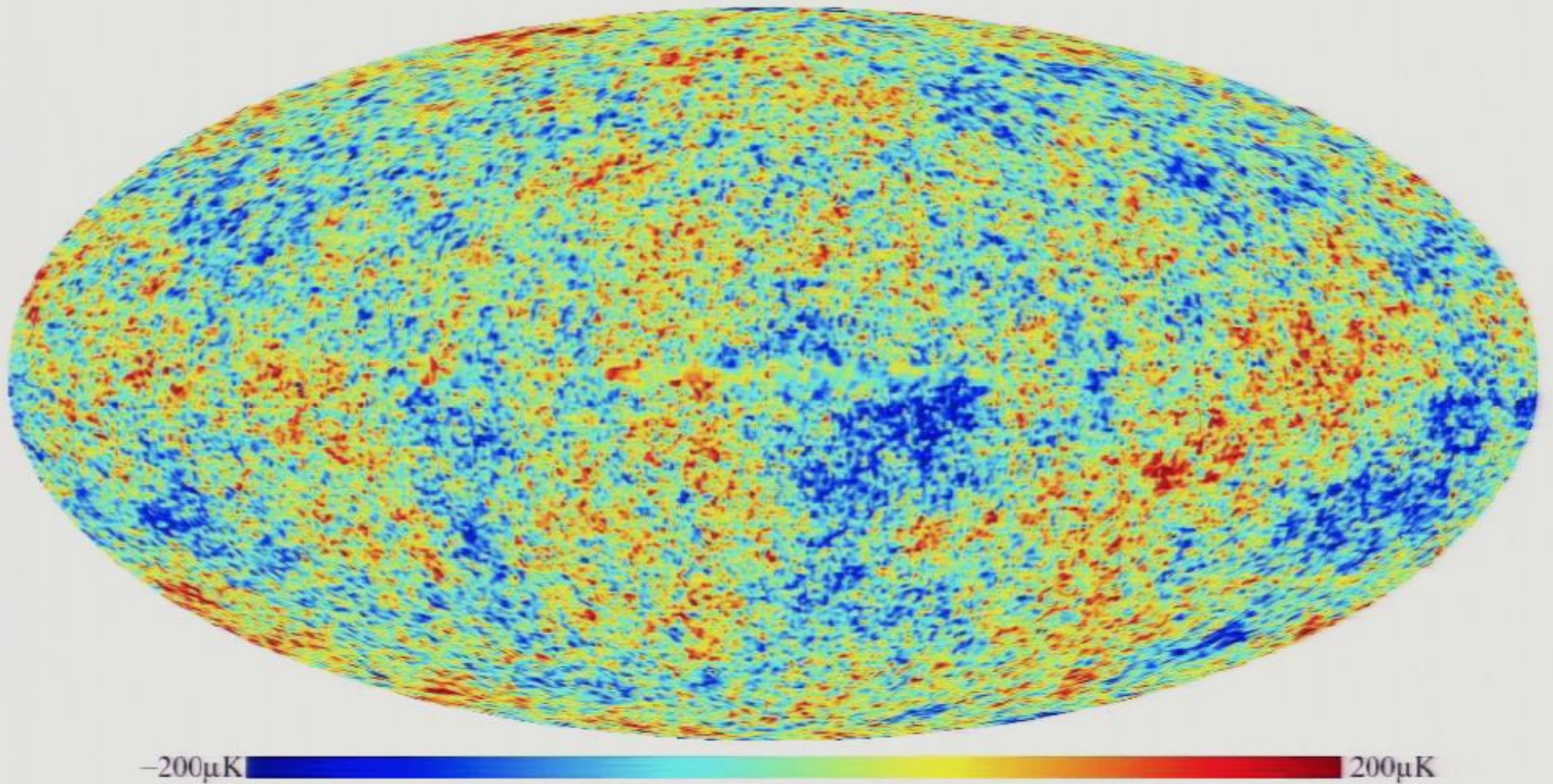
Guth; Linde; Albrecht & Steinhardt.

$$ds^2 = -dt^2 + e^{2Ht} d\mathbf{x}^2 \quad H \approx \text{const.}$$

- ▶ Solves horizon, flatness and monopole problems, *i.e.* explains why the universe is so large, so flat and so empty.
- ▶ Predicts **scalar** fluctuations in CMB temperature:
  - ▶ approximately, but not exactly, **scale-invariant**
  - ▶ approximately **Gaussian**
- ▶ Predicts primordial **tensor** fluctuations  
= **gravitational waves**



# The Golden Age of Cosmology



# Standard Model of Cosmology

## Observations:

### ► Homogeneous Background

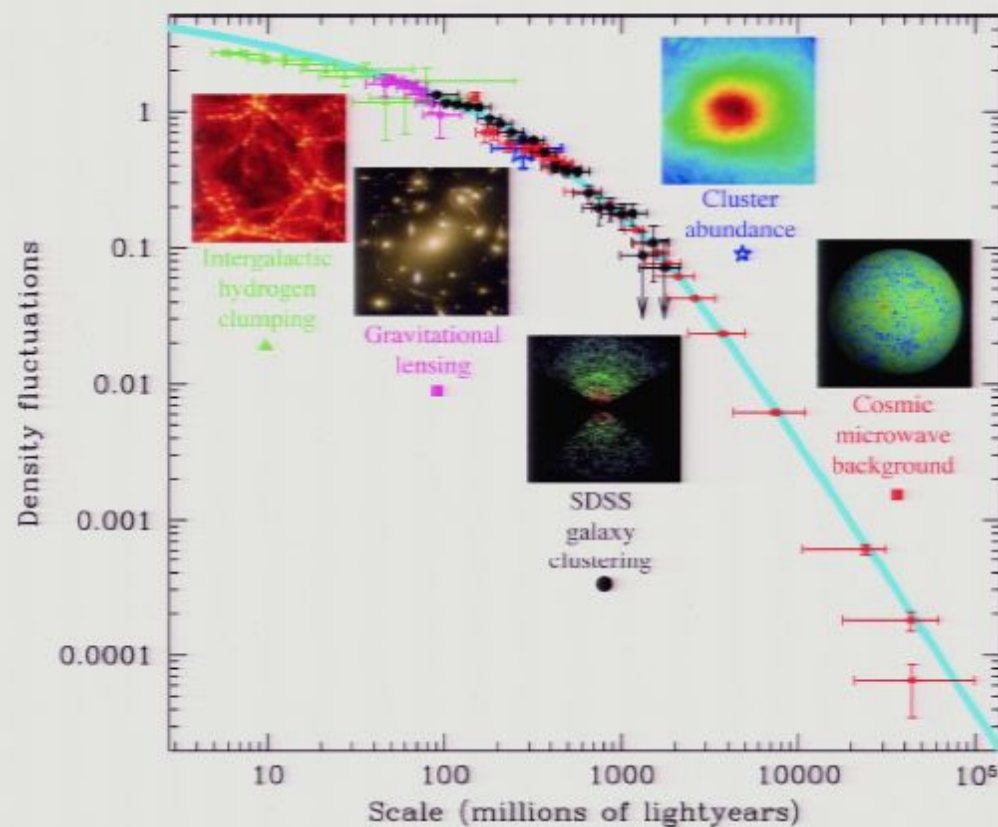
$$\Omega_b, \Omega_{dm}, \Omega_\Lambda, h, \tau$$

- Atoms 4%
- Dark Matter 23%
- Dark Energy 72%

### ► Fluctuations

$$A_s, n_s, r, f_{NL}$$

- (nearly) scale-invariant
- adiabatic
- Gaussian (?)





# Standard Model of Cosmology

## Theory:

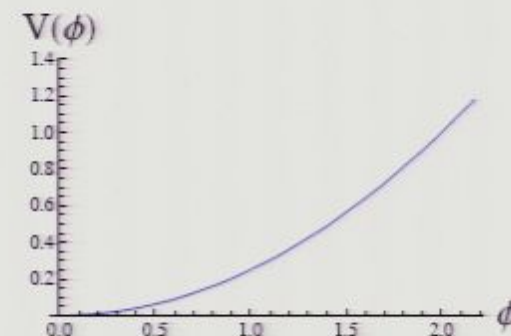
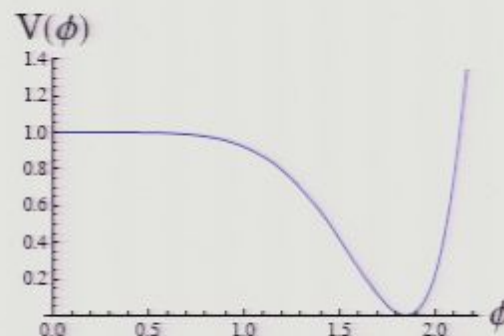
### ▶ $\Lambda$ CDM

- ▶ Dark matter?
- ▶ Dark energy?

### ▶ Inflation

What is the physics of inflation?

#### ▶ Potential $V(\phi)$ ?



#### ▶ Tensors $r$ ?

$r$  will be strongly constrained in the near future. Models which produce an observable signal require a **proper UV understanding**.

# Today's Talk

- ▶ Focus on a specific, concrete model of string inflation:  
warped D-brane inflation.

- ▶ Understand the predictions for

$$V(\phi) \quad \text{and} \quad r$$

as fully and explicitly as possible.

# Outline

1. Primordial Gravitational Waves and the Lyth Bound
2. Inflation in String Theory
3. A Microscopic Limit on Tensors in D-brane Inflation
4. Towards the First Explicit Model of D-brane Inflation
5. Conclusions




## Based on

- ▶ D.B., McAllister,  
A Microscopic Limit on Gravitational Waves from D-brane Inflation
- ▶ D.B., Dymarsky, Klebanov, McAllister,  
Towards an Explicit Model of D-brane Inflation
- ▶ D.B., Dymarsky, Klebanov, McAllister, Steinhardt,  
A Delicate Universe: Compactification Obstacles to D-brane Inflation
- ▶ D.B., Dymarsky, Klebanov, Maldacena, McAllister, Murugan,  
On D3-brane Potentials in Compactifications with Fluxes and Wrapped D-branes
- ▶ D.B., Dymarsky, Kachru, Klebanov, McAllister,  
*work in progress*
- ▶ D.B.,  
Aspects of Inflation in String Theory (PhD thesis)

# PART I

## Primordial Gravitational Waves and the Planck Distance

The Dumbbell Nebula — M27  HUBBLESITE.org

# Quantum Fluctuations in de Sitter

tensors ( $\delta g_{ij}$ )

$$P_t \propto \frac{H^2}{M_{\text{pl}}^2}$$

tensor-to-scalar ratio

$$r \equiv \frac{P_t}{P_s} = 8 \left( \frac{1}{M_{\text{pl}}} \frac{d\phi}{dN_e} \right)^2$$

scalars ( $\delta\rho$ )

$$P_s \propto H^2 \left( \frac{H}{\dot{\phi}} \right)^2$$

$$\delta\phi \times (\delta\phi \rightarrow \delta\rho)$$

where

$$dN_e \equiv d \ln a = H dt = \left( \frac{H}{\dot{\phi}} \right) d\phi$$



# The Lyth Bound

$$r = 8 \left( \frac{1}{M_{\text{pl}}} \frac{d\phi}{dN_e} \right)^2$$

$$\frac{\Delta\phi}{M_{\text{pl}}} = \int_{\phi_{\text{end}}}^{\phi_{\star}} dN_e \sqrt{\frac{1}{8} r(N_e)}$$

Let  $r_{\star}$  be the value of  $r$  on observable scales ( $N_e(\phi_{\star}) \sim 60$ ) and the **Lyth bound** follows

$$\frac{r_{\star}}{0.01} < \frac{8}{9} \left( \frac{\Delta\phi}{M_{\text{pl}}} \right)^2$$

- ▶ This is a useful constraint if we can compute  $\left( \frac{\Delta\phi}{M_{\text{pl}}} \right)_{\text{max}}$  from a microscopic theory.

$$P(x|\phi)$$

$$X = \frac{1}{2} \dot{\phi}^2$$

$$C_S P_{,X}$$

10/47

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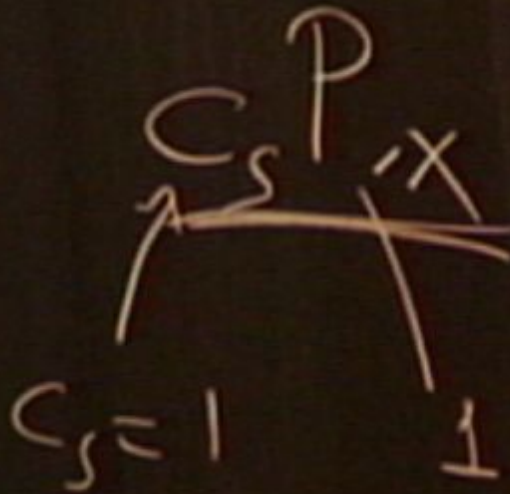
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## What if we see tensors?

Current constraint on tensors:  $r_{\star} \lesssim 0.4$ .

Realistically observable:  $r_{\star} \gtrsim 0.01$ .

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## 1. Energy-scale of Inflation

The measured amplitude of scalar perturbations  $P_s \sim \left(\frac{\delta\rho}{\rho}\right)^2 \sim 10^{-10}$   
(and  $H^2 \approx \frac{1}{3M_{\text{pl}}^2}V$ ) implies:

$$V^{1/4} \sim \left(\frac{r_{\star}}{0.01}\right)^{1/4} 10^{16} \text{ GeV}$$

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## 2. Super-Planckian Field Variation

Observable gravitational waves require  $\Delta\phi > M_{\text{pl}}$  during inflation:

$$\frac{\Delta\phi}{M_{\text{pl}}} > \mathcal{O}(1) \left(\frac{r_{\star}}{0.01}\right)^{1/2}$$

e.g.  $V(\phi) = \frac{1}{2}m^2\phi^2$  requires  $\Delta\phi \sim 15M_{\text{pl}}$ .

# The Microphysics of Observable Tensors

- ▶ Observable tensors ( $r_{\star} > 0.01$ ) require

$\Delta\phi > M_{\text{pl}}$  and **controllably flat potentials:**

Is this realizable in a **consistent microscopic theory** like string theory?



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- ▶ *Controversial Effective Field Theory Arguments:* (cut-off  $\Lambda \leq M_{\text{pl}}$ )
  - ▶  $V(\phi)$  can be reliably computed only over  $\Delta\phi < M_{\text{pl}}$
  - ▶ Flat potential and inflation only likely over  $\Delta\phi < M_{\text{pl}}$

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Arguments are controversial/UV-sensitive.

- ▶ Need UV-complete theory (e.g. string theory) to resolve the argument.

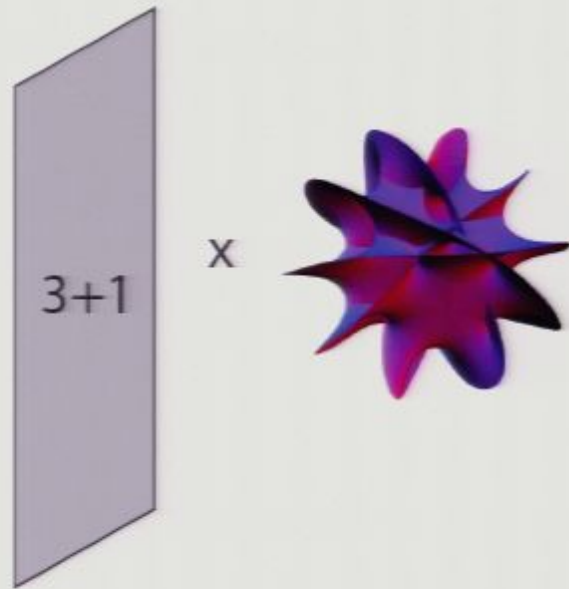
# Part II

## Review of String Inflation

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# Moduli Fields: "Blessing and Curse"



## ▶ **Moduli:**

Scalar fields in the effective 4d theory:

- ▶ dilaton
- ▶ complex structure moduli
- ▶ Kähler moduli
- ▶ D-brane positions

## ▶ "Blessing":

Dynamics of moduli may be a natural way to explain inflation.

## ▶ "Curse":

Unfixed moduli are "bad news".

**Moduli stabilization** in string theory was a major breakthrough.

## KKLT:

Kachru, Kallosh, Linde and Trivedi

Moduli are stabilized by **fluxes** (complex structure) and **non-perturbative (quantum) effects** on **wrapped branes** (Kähler).

# Models of Inflation in String Theory

**Moduli dynamics** can lead to inflation:

"Dynamics *OF* or *IN* the extra dimensions is reflected in a change in the inflationary energy in the 4d spacetime"

## ▶ Closed string models

Role of the inflaton is played by moduli fields which control "size and shape" of the compact space.

- ▶ Racetrack
- ▶ Kähler moduli
- ▶ Roulette
- ▶ N-flation
- ▶ ...

## ▶ Open string models

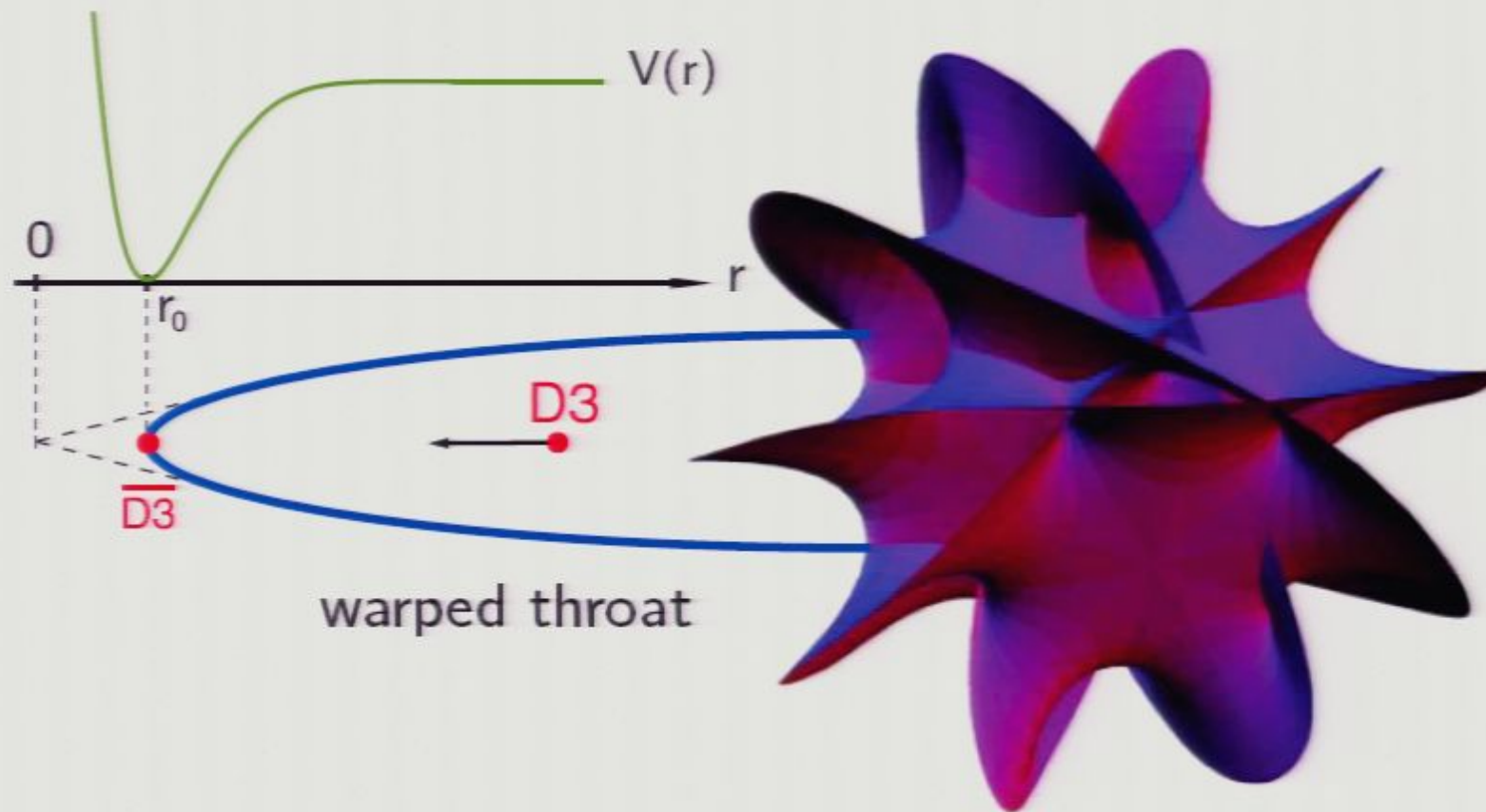
Role of the inflaton is played by **D-brane positions** or orientations.

- ▶ Brane-antibrane
- ▶ Branes at angles
- ▶ D3-D7
- ▶ **Warped brane-antibrane**
- ▶ M5-brane
- ▶ DBI
- ▶ ...

# Warped D-Brane Inflation

## KKLMMT Scenario

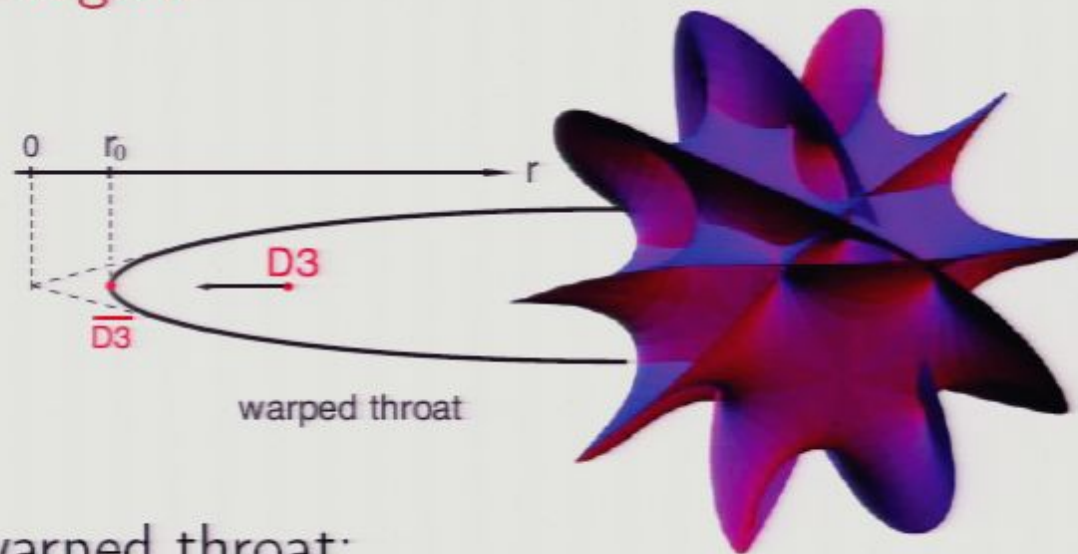
Kachru, Kallosh, Linde, Maldacena, McAllister, Trivedi





# Warped D-Brane Inflation

Fluxes backreact on the Calabi-Yau metric to produce a "warped throat region"



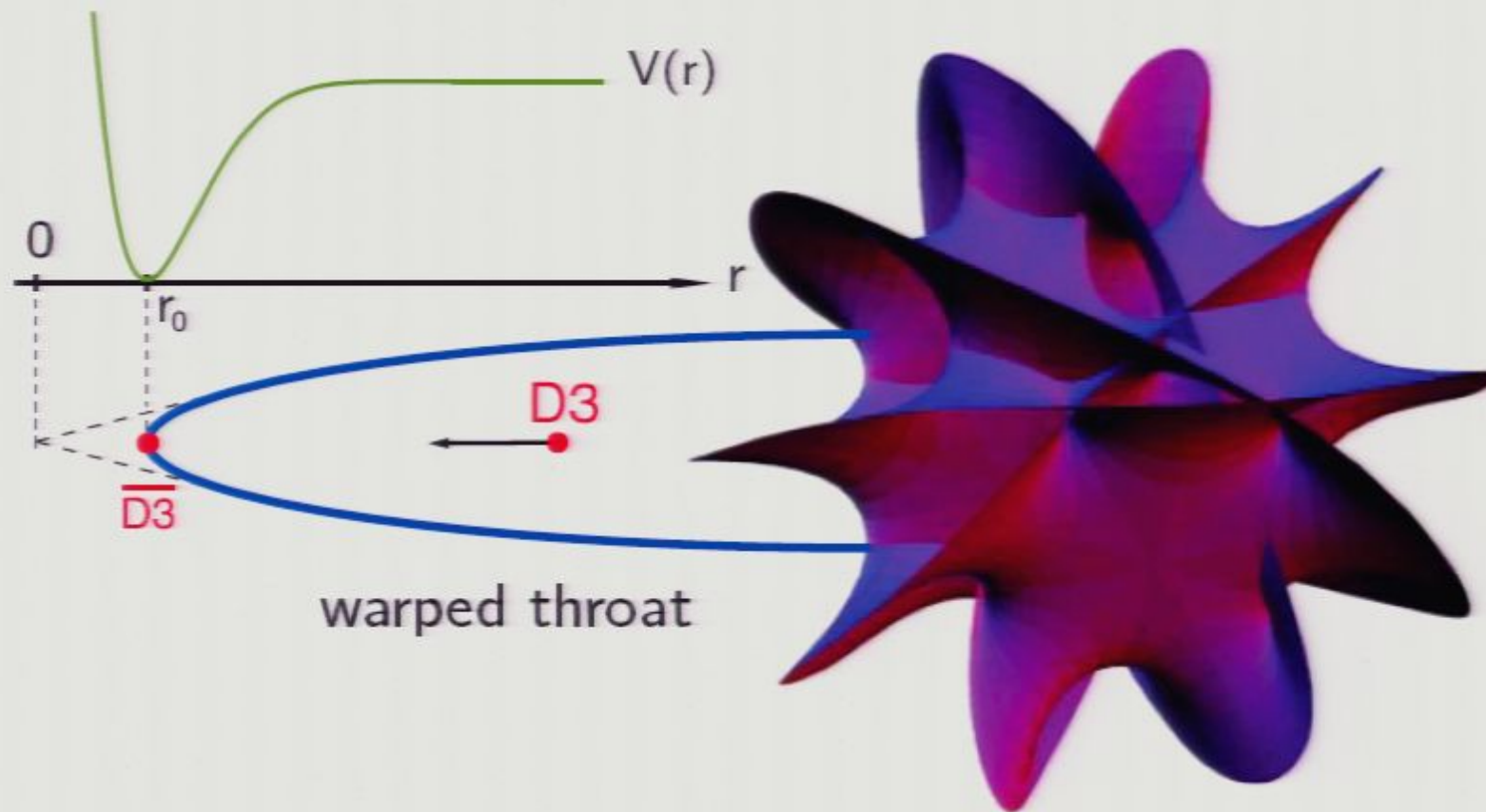
Advantages of warped throat:

- ▶ Warping suppresses the force between the branes. Coulomb potential is exponentially flat.
- ▶ Stringy realization of Randall-Sundrum scenario; Hierarchy of scales.
- ▶ Local model  $\Rightarrow$  explicit metrics  $\Rightarrow$  **computable**  
cf. general Calabi-Yau metrics are not known.

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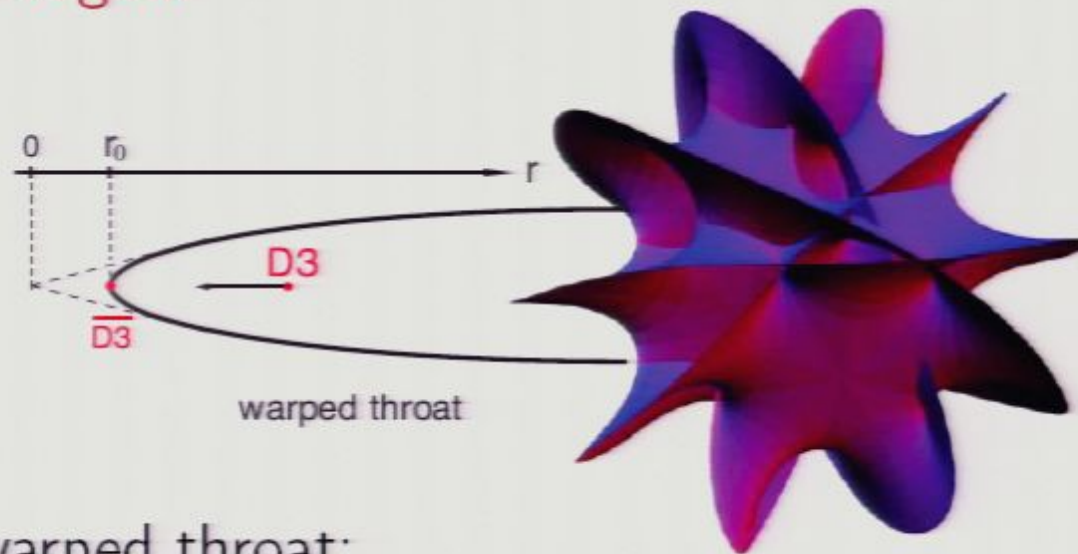
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# Part III

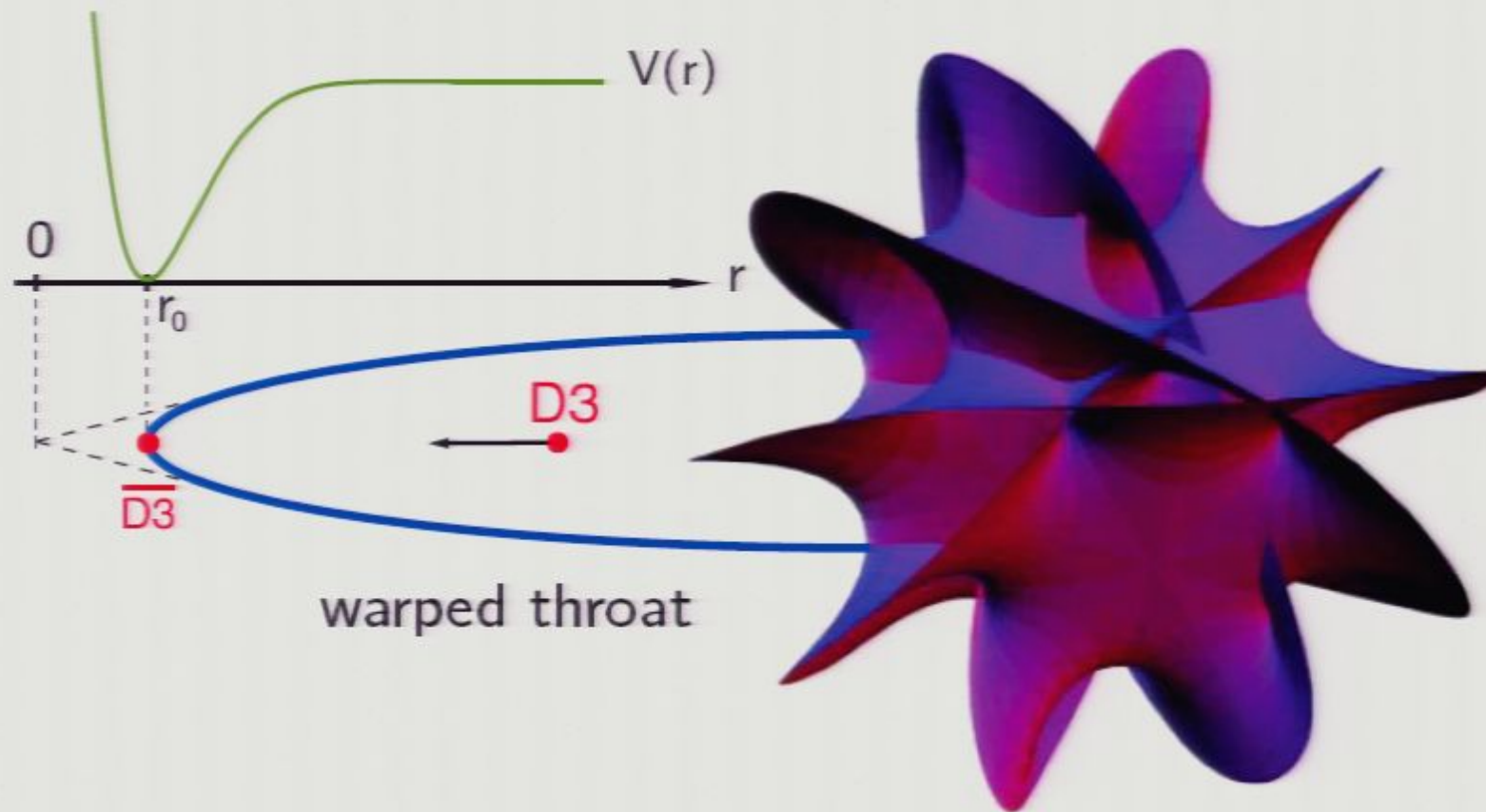
## The Field Range Bound

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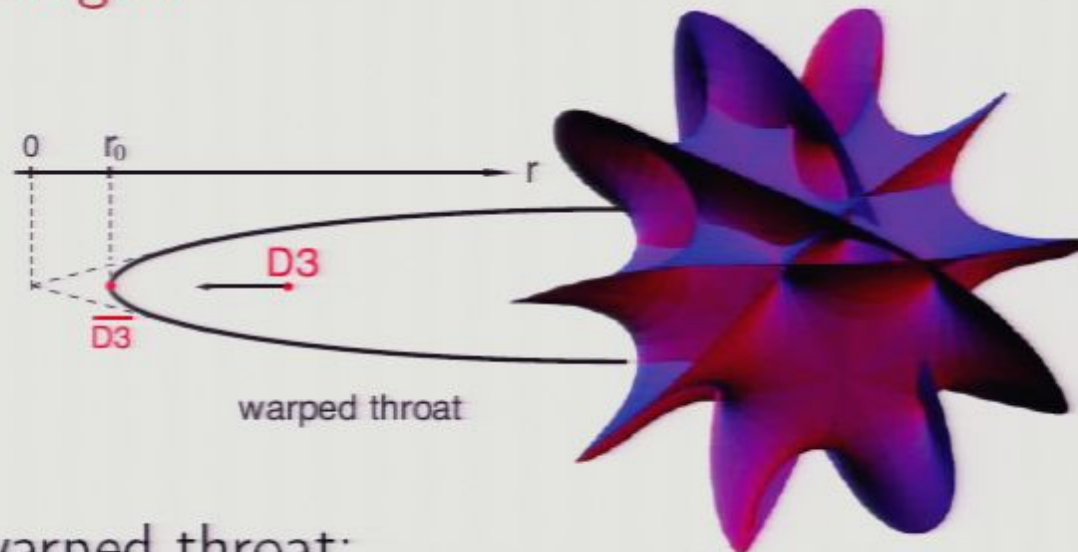
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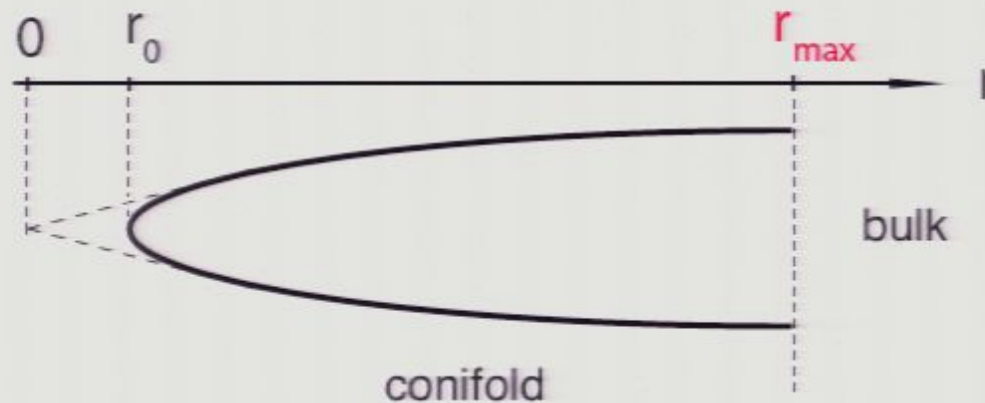


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# Warped Geometry



A warped cone over the base  $X_5$  has the following metric:

$$ds^2 = h^{-1/2}(r)g_{\mu\nu}dx^\mu dx^\nu + h^{1/2}(r)(dr^2 + r^2 ds_{X_5}),$$


where the warp factor follows from supergravity

$$h^{-1} = \left(\frac{r}{R}\right)^4, \quad T_3 R^4 = \frac{\pi}{2} \frac{N}{\text{Vol}(X_5)}.$$

The supergravity approximation requires large value of the flux integer  $N \gg 1$ .

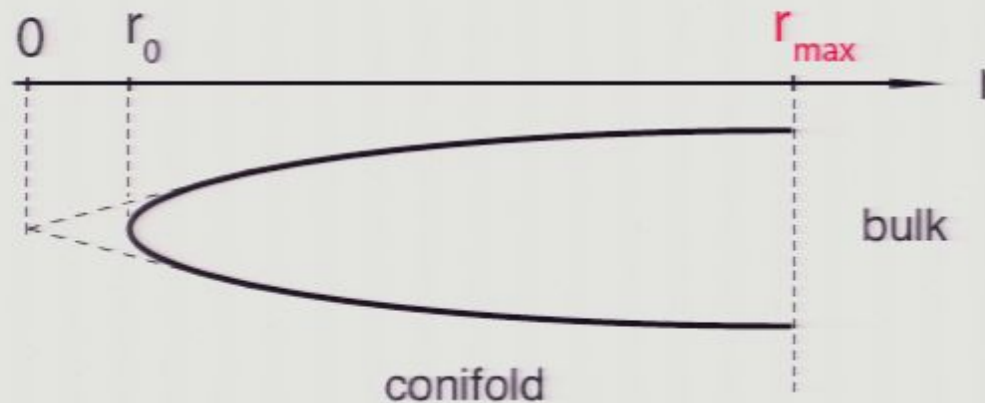
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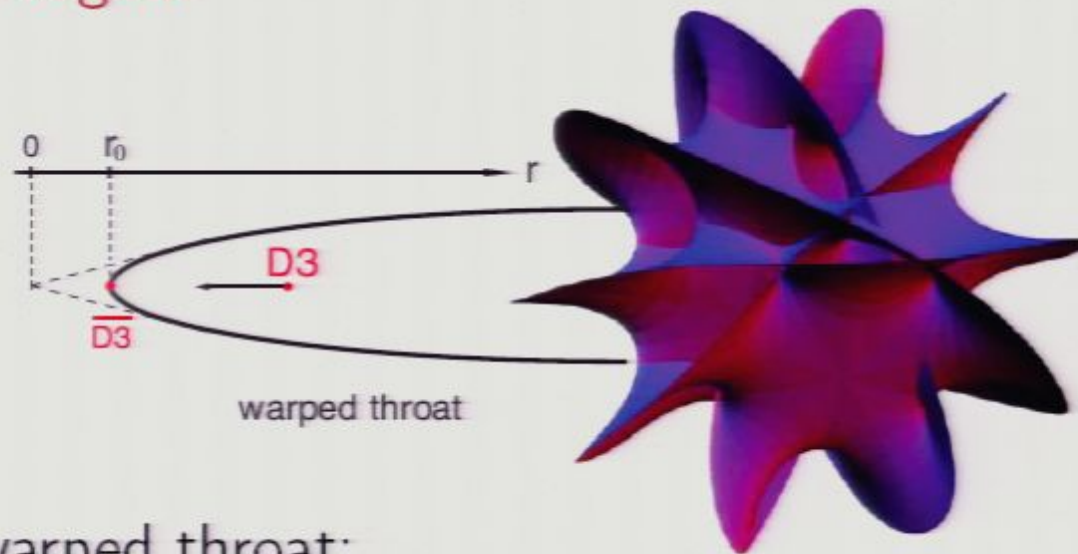
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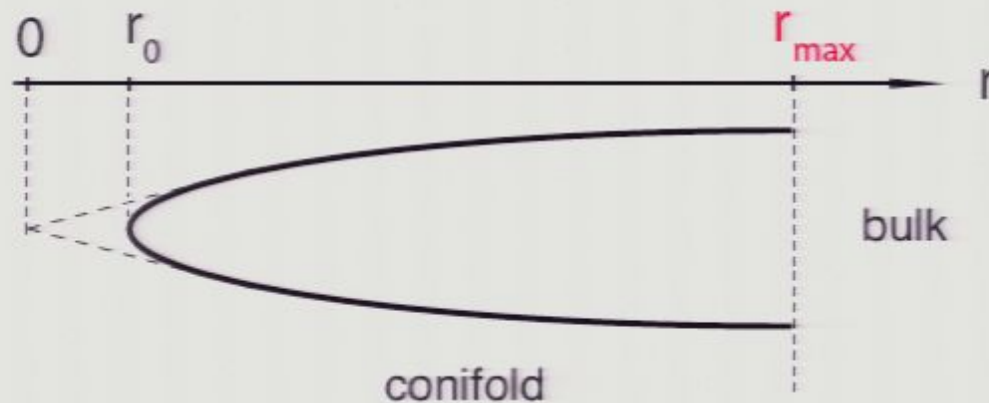


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# Compactification Volume and 4d Planck Mass

## Dimensional reduction

$$M_{\text{pl}}^2 = M_{10}^8 V_6^w$$

where  $M_{10}^8 \equiv \frac{2}{(2\pi)^7 g_s^2 (\alpha')^4} = \frac{1}{\pi} (T_3)^2$  and

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Get **conservative constraint** by ignoring the (unknown) bulk volume and computing the **warped throat volume**

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$$M_{\text{pl}}^2 > T_3 r_{\text{max}}^2 \frac{N}{4}$$



# Compactification Constraint on the Field Variation

4d-Planck Mass

$$M_{\text{pl}}^2 > T_3 r_{\text{max}}^2 \frac{N}{4}$$

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$$\frac{\Delta\phi}{M_{\text{pl}}} < \frac{2}{\sqrt{N}}$$

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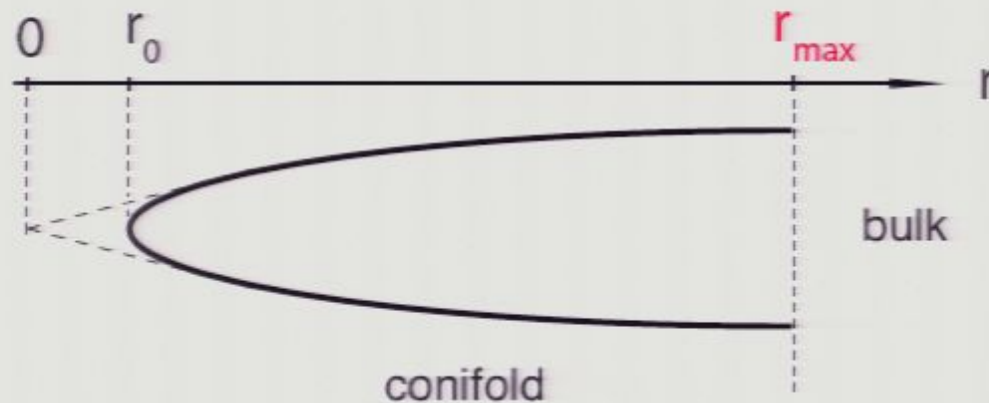
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# Primordial Tensors?

Consistency requires

$$\frac{\Delta\phi}{M_{\text{pl}}} < \frac{2}{\sqrt{N}}$$

$$N \gg 1$$

i.e.

$$\Delta\phi \ll M_{\text{pl}}$$

**NO** observable tensors from brane inflation!



Notice that our field range bound

*did not require use of any genericity argument like:*

*"it would be very fine tuned to have such a flat potential over such a large distance in the throat"*

The bound follows from *pure geometry*.

Also notice that *longer throats have shorter canonical field range in 4d Planck units!*

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# Dramatic Constraint on DBI Inflation

Silverstein and Tong

Relativistic limit of brane motion:

- ▶ DBI action allows inflation even for steep potentials.
- ▶ Non-gaussianity is large.

# Dramatic Constraint on DBI Inflation

Observations ( $f_{\text{NL}} < 100$ ) require super-Planckian field variation

$$\phi > M_{\text{pl}}$$

This is inconsistent with our microscopic constraint!

D.B., McAllister

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# Summary

Implications of the field range bound:

1. Detectable tensors **impossible in slow roll of D3-branes**.
2. **Rules out DBI inflation** from D3-branes on Calabi-Yau cones.  
(D.B., McAllister; see also: Lidsey, Huston; Bean et al.; Peiris, D.B., Friedman, Cooray)



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+

$$\frac{\Delta\phi}{M_{\text{pl}}} < \frac{2}{\sqrt{N}}$$

*Canonical* Inflaton Field

$$\phi^2 = T_3 r^2 < T_3 r_{\text{max}}^2$$

D.B., McAllister

A Microscopic Limit on Gravitational Waves from D-brane Inflation

# Dramatic Constraint on DBI Inflation

Observations ( $f_{\text{NL}} < 100$ ) require super-Planckian field variation

$$\phi > M_{\text{pl}}$$

This is inconsistent with our microscopic constraint!

D.B., McAllister

A Microscopic Limit on Gravitational Waves from D-brane Inflation



# Summary

## Implications of the field range bound:

1. Detectable tensors **impossible in slow roll of D3-branes.**
2. **Rules out DBI inflation** from D3-branes on Calabi-Yau cones.  
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Question:

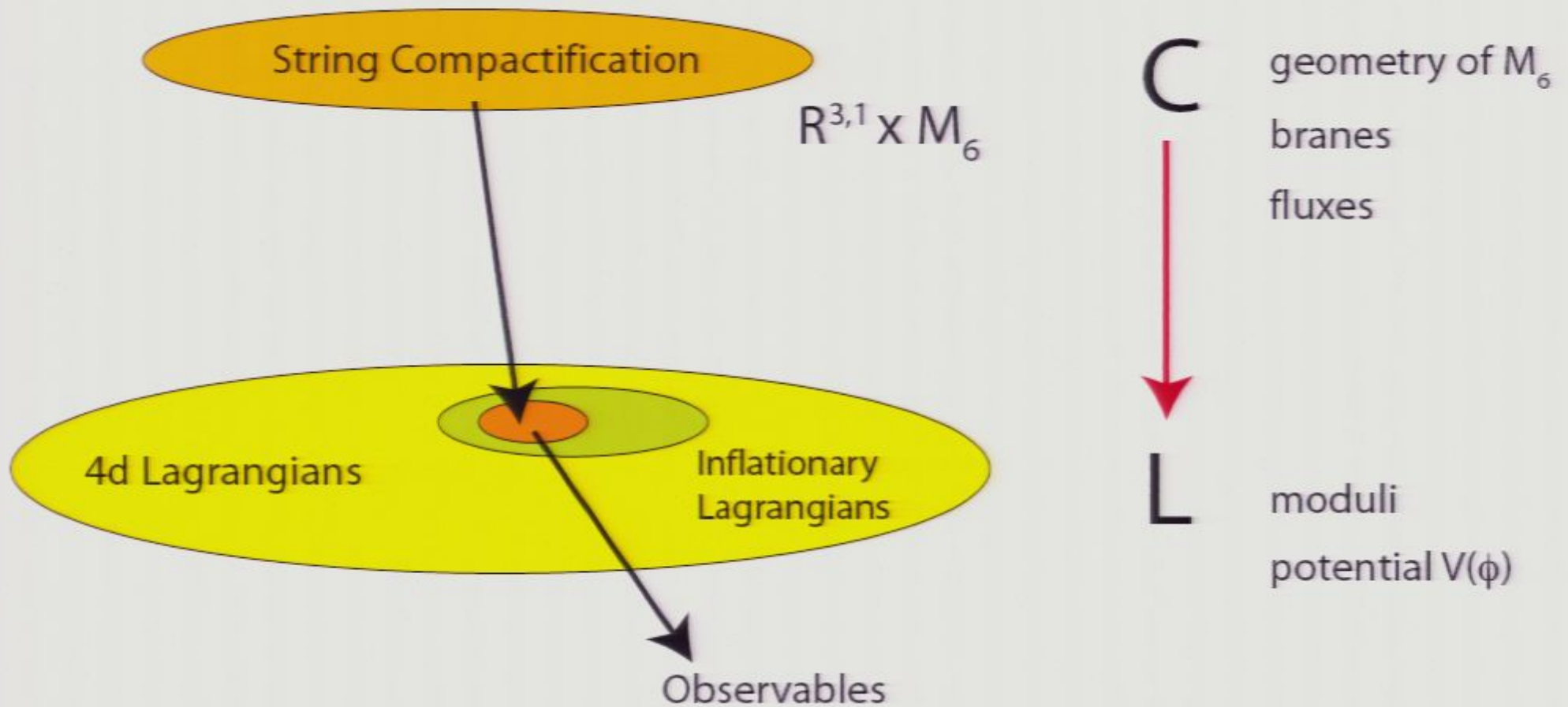
Can large-field inflation be realized in a consistent string compactification?

# PART IV

## Towards *Explicit* D-brane Inflation

The Dumbbell Nebula — M27  HUBBLESITE.org


# From String Compactification to Low Energy Lagrangian





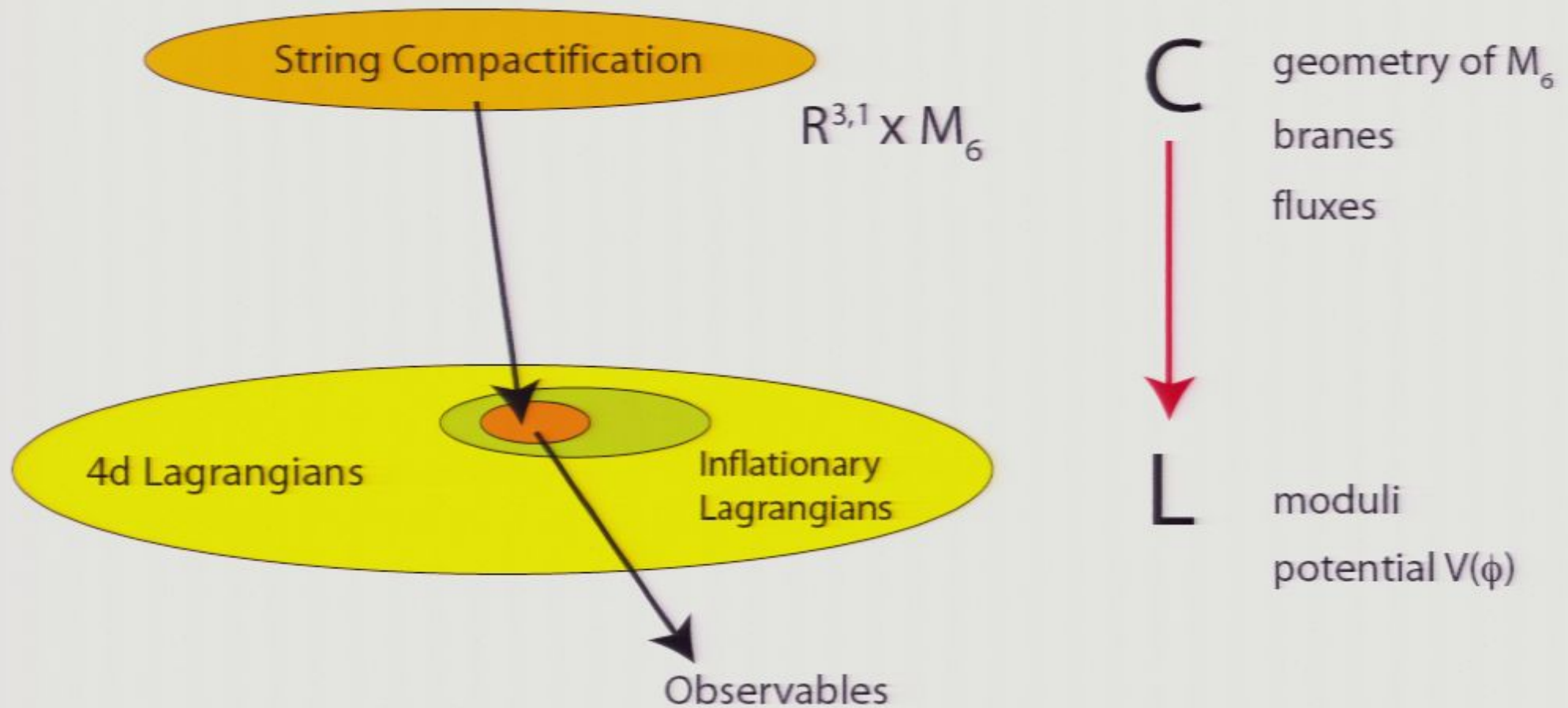
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# From String Compactification to Low Energy Lagrangian



# String Theory and Inflationary Cosmology

## 1. Short-Term Goal

Existence Proof of Inflation in String Theory

## 2. Mid-Term Goal

Classification of Possible Inflationary Models in String Theory

e.g. large field vs. small field

Understand Microscopic Constraints

Understand Naturalness

## 3. Long-Term Goal

Compute Observational Signatures

# What is required for an Existence Proof?

"The hard part is not to find a flat potential, but to show that it is *THE* potential."

# What is required for an Existence Proof?

Consider an inflation model with some  $V(\phi)$ .

A robust model requires understanding gravity corrections up to dimension 6

$$\delta V \sim \frac{V}{M_{\text{pl}}^2} \phi^2.$$

These can induce order Hubble corrections to the inflaton mass,

$$\Delta\eta \sim \mathcal{O}(1).$$

i.e. for a controllable model one needs to demonstrate explicitly that these dangerous terms are *absent*, *suppressed* or *cancel*.

This requires some knowledge of Planck scale physics or quantum gravity.



## e.g. $V(\phi)$ for Brane Inflation

- ▶ **Before** moduli stabilization:

Brane-antibrane Coulomb potential is exponentially flat.

- ▶ **After** moduli stabilization:

Moduli stabilization induces  $\Delta\eta = \mathcal{O}(1)$  terms and spoils flatness of the inflaton potential!

- ▶ Obligated to

compute corrected potential in **stabilized vacuum**.

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# $V(\phi)$ and Moduli Stabilization

## KKLT compactification: Effects on mobile D3-branes?

### 1. FLUXES

Type IIB on  $CY_3$  orientifold with  $G_3 \equiv F_3 - \tau H_3$  flux.

- ▶ GKP compactification: eom enforces ISD flux:

$$\star_6 G_3 = i G_3$$

- ▶ Graña:  
scalars governing motion of a spacetime-filling D3-brane couple **only** to IASD flux

$$(\star_6 - i)G_3$$

**NO force on D3-branes from ISD fluxes.**

- ▶ systematic study of IASD effects from UV perturbations:  
D.B., Dymarsky, Kachru, Klebanov, McAllister, *work in progress*



# $V(\phi)$ and Moduli Stabilization

**KKLT** compactification: **Effects on mobile D3-branes?**

2. **Non-perturbative effects** on wrapped branes induce dangerous  $\Delta\eta \sim \mathcal{O}(1)$  corrections to the inflaton potential.

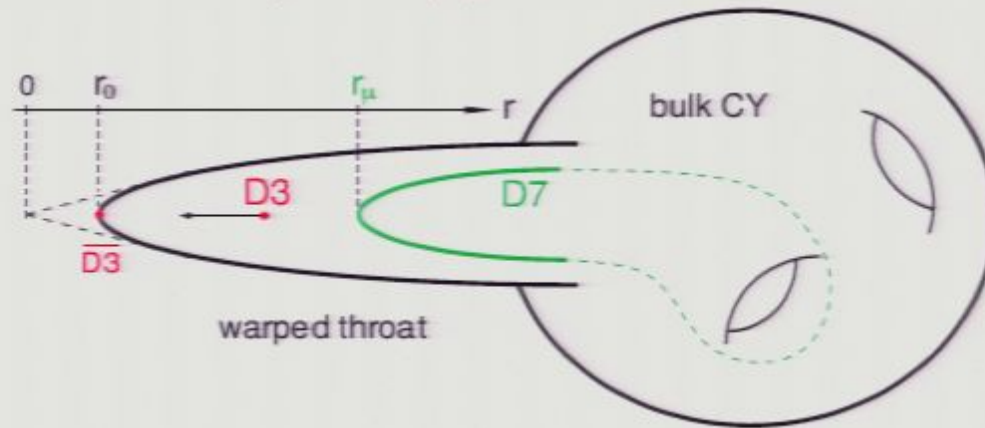
$$W_{\text{np}} = \underline{\underline{A(\phi)}} e^{-a\rho}$$

# The Physics of the Brane Inflation Potential

Two physical effects lead to  $\Delta\eta \sim \mathcal{O}(1)$  corrections to the Coulomb potential:

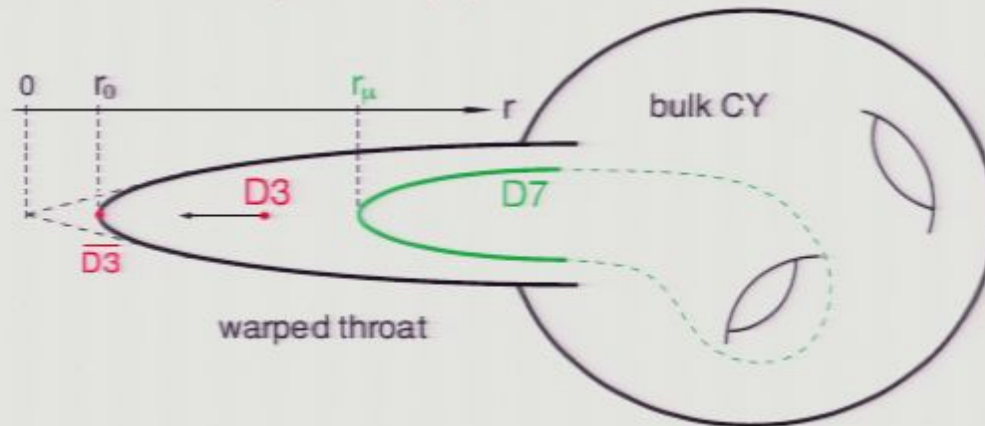
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## 1. D3-brane backreaction on the compactification volume

The physical volume of the compact space depends on the position of the D3-brane,  $\mathcal{V}(\phi)$ .

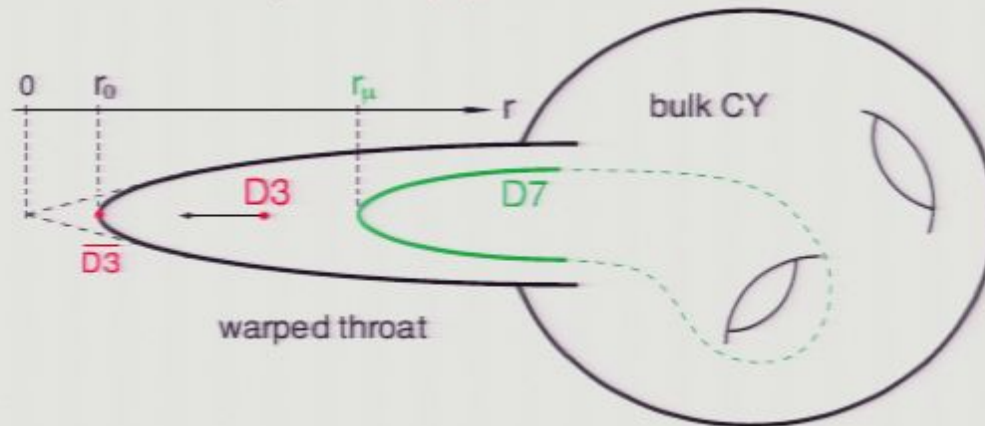
$$\mathcal{L}_{\text{Einstein}} \sim \frac{1}{\mathcal{V}(\phi)^{\#}} \mathcal{L}_{\text{String}} \Rightarrow \delta V(\phi).$$

First computed by KKLMMT.



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## 2. D3/D7 interaction

The presence of the D3-brane changes the *warped* volume of the 4-cycle wrapped by the D7-branes,  $\mathcal{V}_4^w(\phi) \equiv \int d^4y \sqrt{g} h(\phi)$ .

$$\frac{1}{g^2} \propto \mathcal{V}_4^w(\phi) \quad \Rightarrow \quad W_{\text{np}} \propto e^{-c\mathcal{V}_4^w(\phi)} \equiv A(\phi)e^{-a\rho} \quad \Rightarrow \quad \delta V(\phi).$$

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(see also: Ganor; Berg, Haack and Körs; Giddings & Maharana)

# Eta-Problem from Compactification Effects

Both the **D3-backreaction on the volume** and the **D3/D7 interaction** give large contributions to the inflaton mass:

$$\eta = \frac{V''}{V} = \frac{2}{3} + \eta_{3/7}(\phi)$$

Can  $\eta$  ever be small?

## Recap of the Situation

- ▶ The potential in the KKLM model is **not** naturally flat enough for inflation, despite initial hopes.
- ▶ Depending on the function  $\eta_{3/7}(\phi)$ , it may sometimes, or never, be flat enough.
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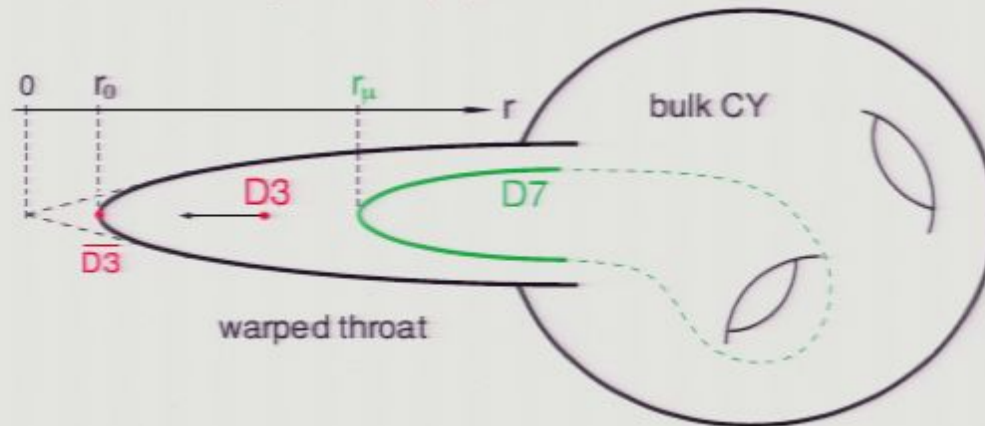
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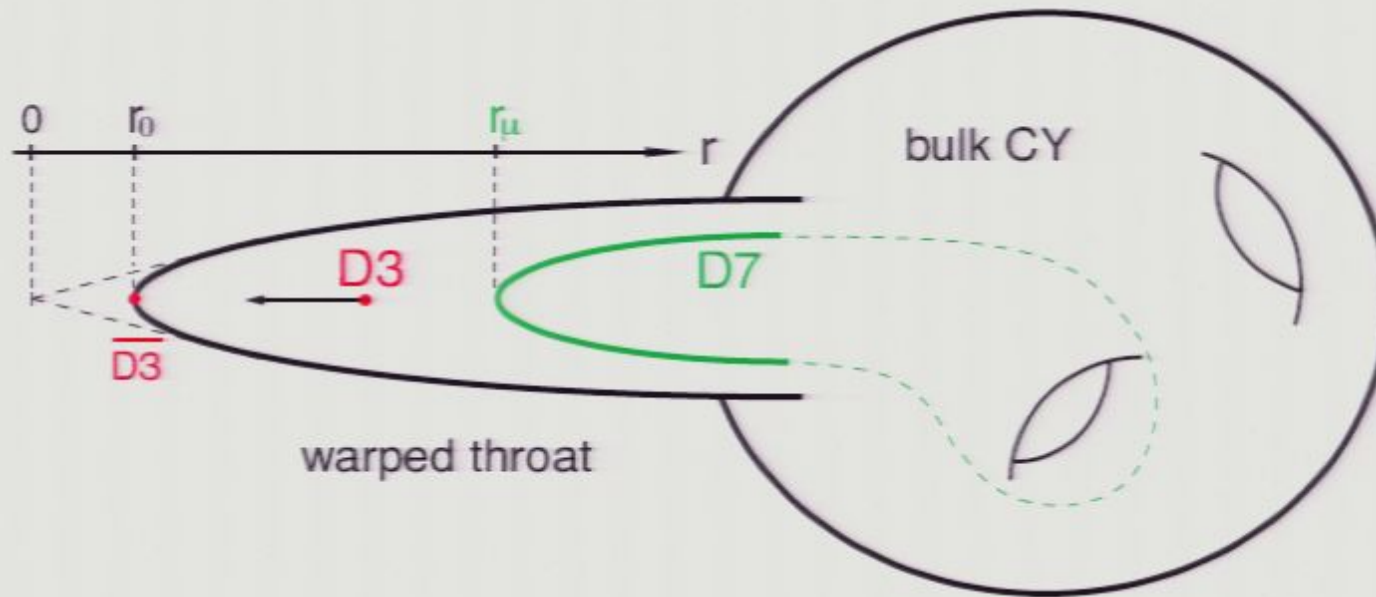
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# D3/D7-Interaction

## Setup



$$\delta\mathcal{V}_4^w \equiv \int d^4y \sqrt{g} \delta h, \quad \nabla^2 \delta h = \mathcal{C} \delta(r - r')$$

$\Rightarrow$  D3/D7 interaction:

D.B., Dymarsky, Klebanov, Maldacena, McAllister, Murugan,  
On D3-brane Potentials in Compactifications with Fluxes and Wrapped Branes.

JHEP 0611 (2006) 031

see also: [Ganor](#)



# Effective Single Field Potential

- ▶ Potential depends on 8 real fields.

Integrating out the angles and the compactification volume gives the **effective single field potential** for radial motion.

D.B., Dymarsky, Klebanov, McAllister

Towards an Explicit Model of D-brane Inflation.

see also: **Burgess et al., Krause & Pajer**

$$\left. \frac{\partial V}{\partial \rho} \right|_{\rho=\rho_*(\phi)} = \left. \frac{\partial V}{\partial \Psi} \right|_{\Psi=\Psi_*(\phi)} \equiv 0 \quad \Rightarrow \quad \mathbf{V}(\phi) \equiv V(\phi, \rho_*(\phi), \Psi_*(\phi))$$

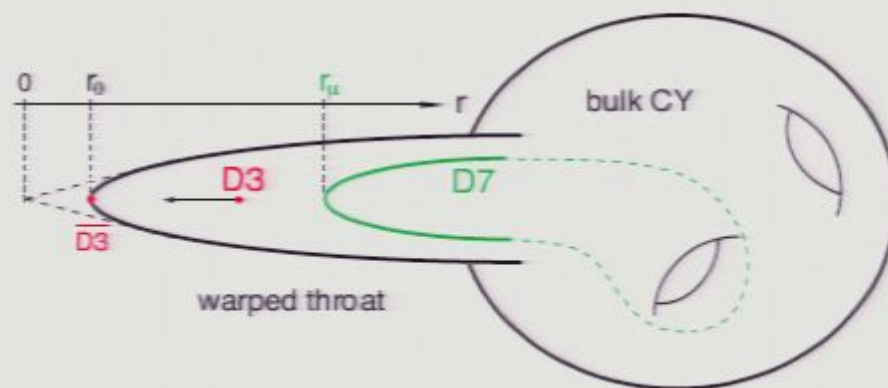
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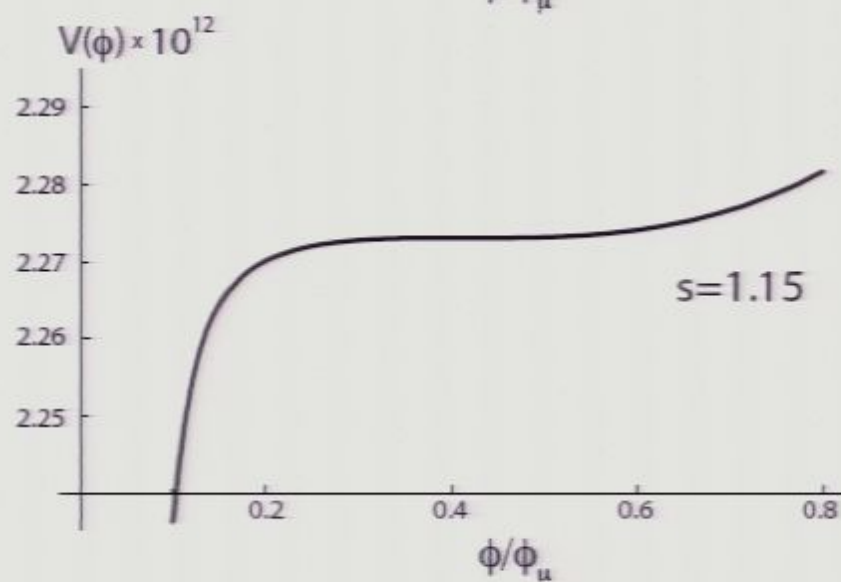
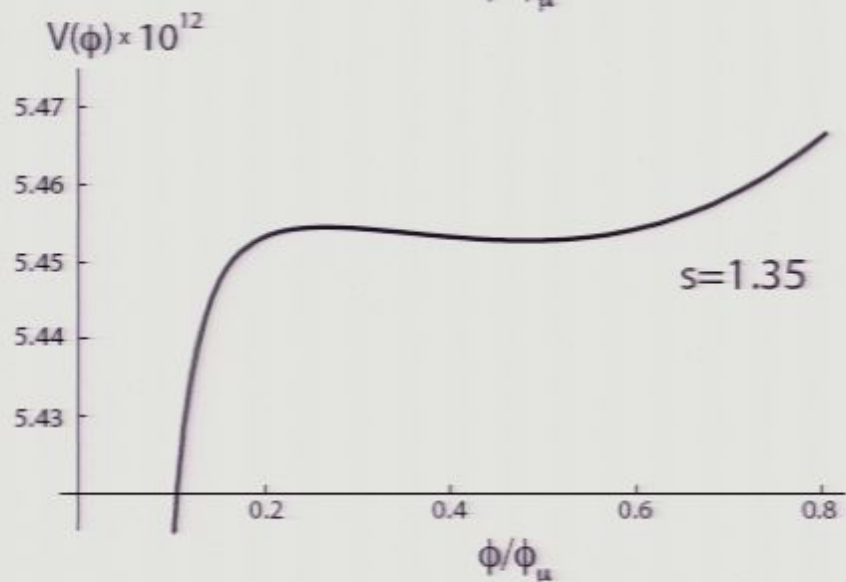
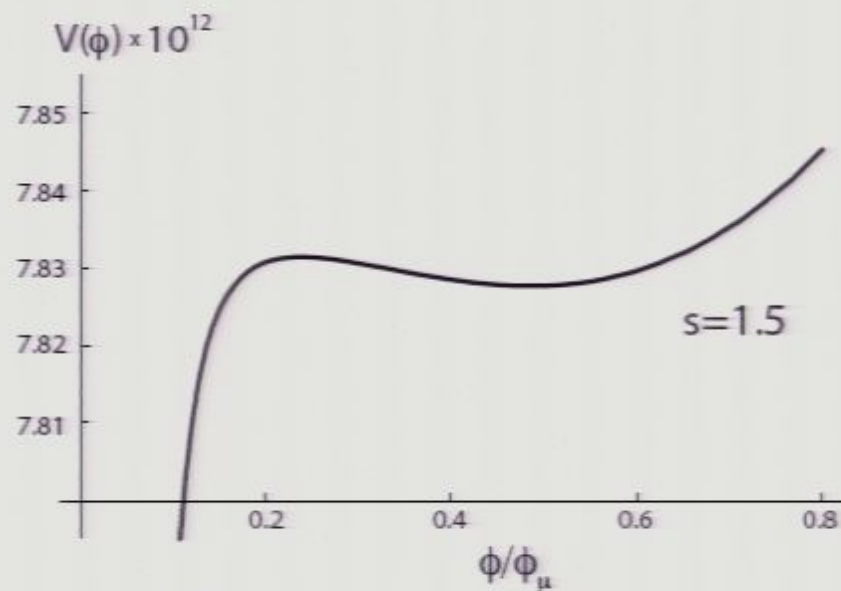
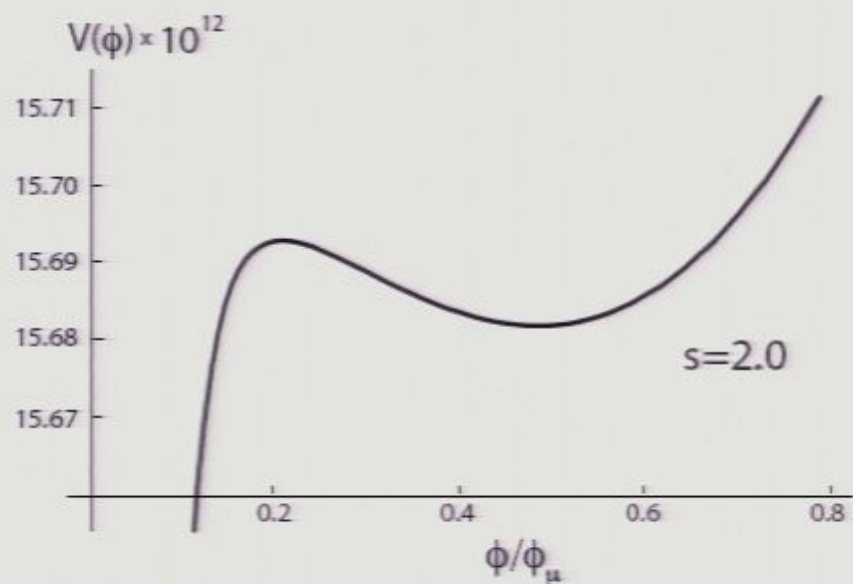
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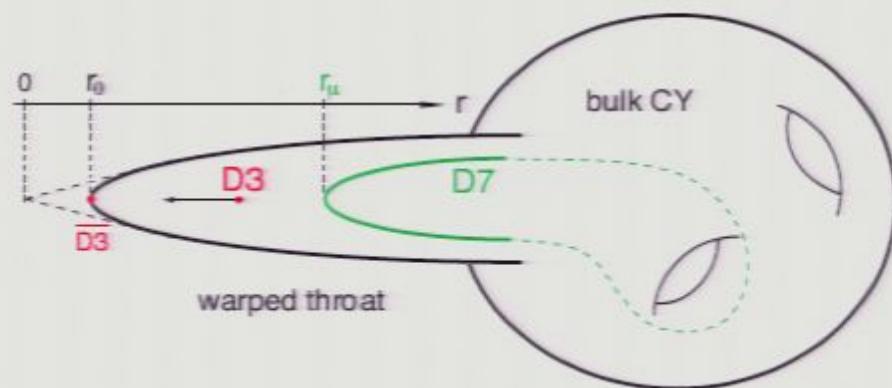
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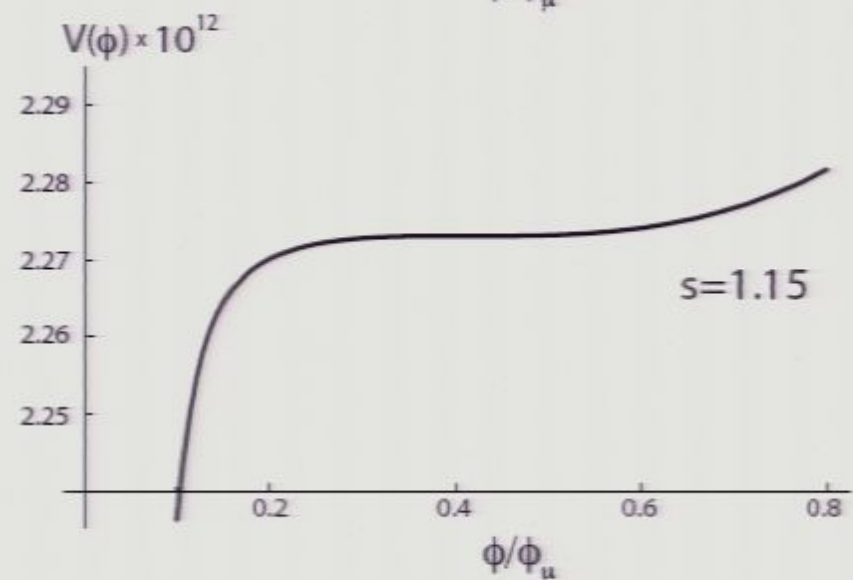
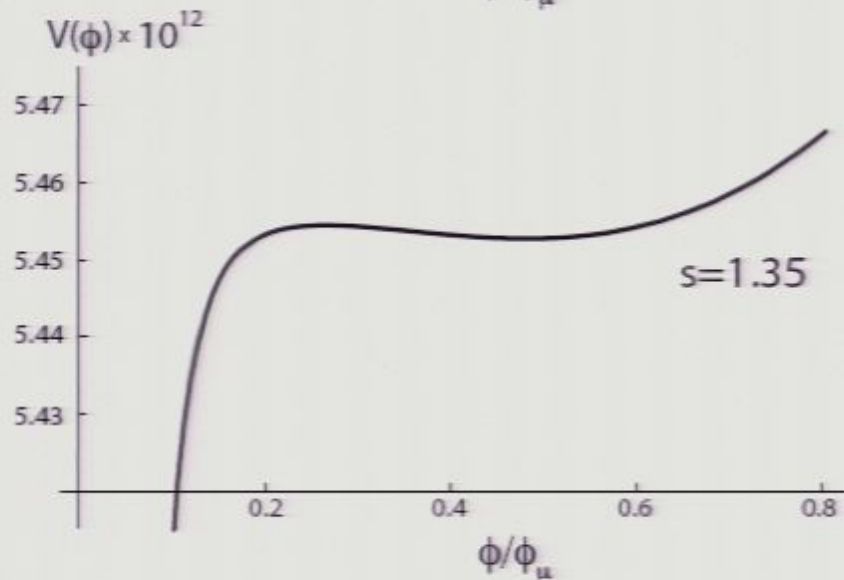
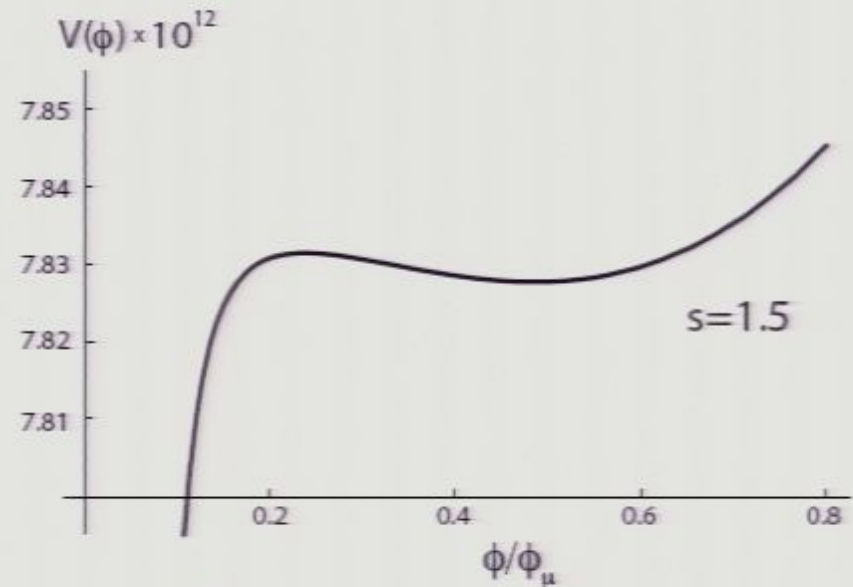
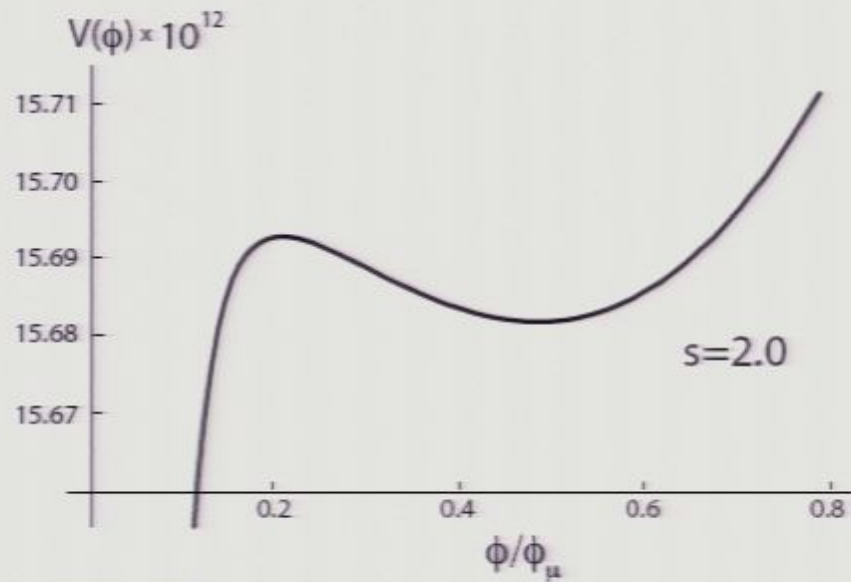
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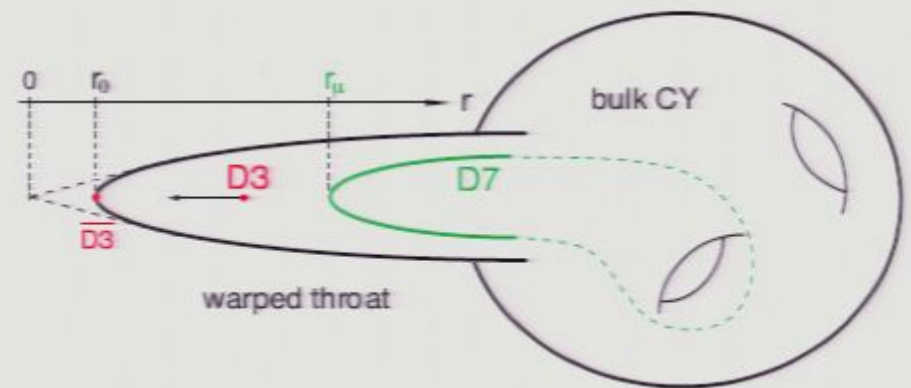
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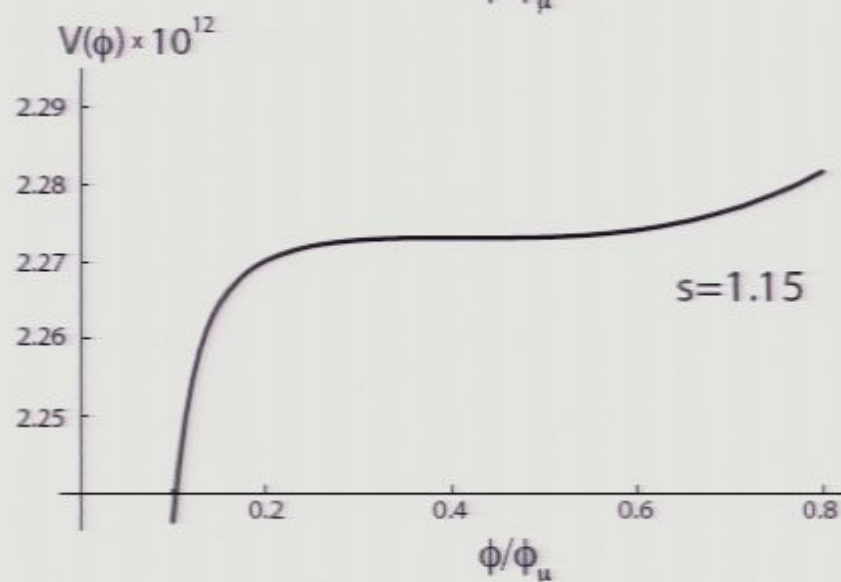
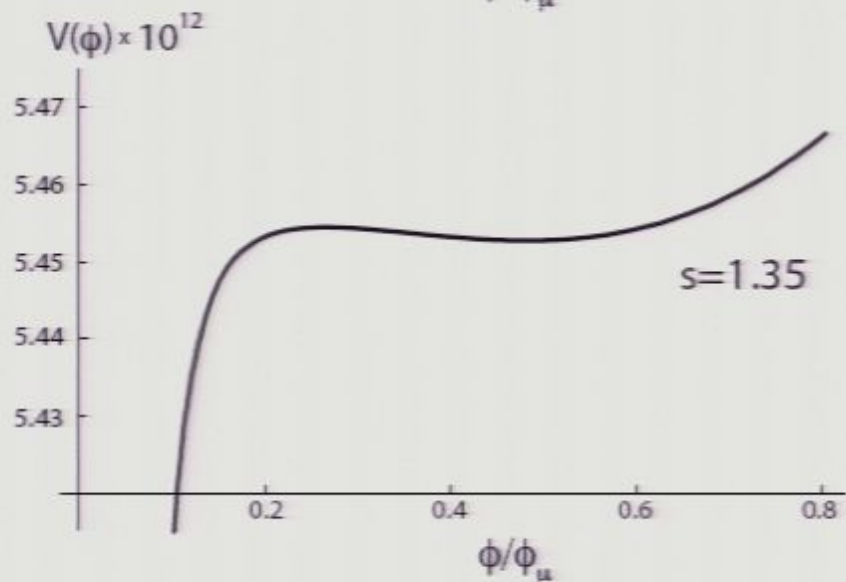
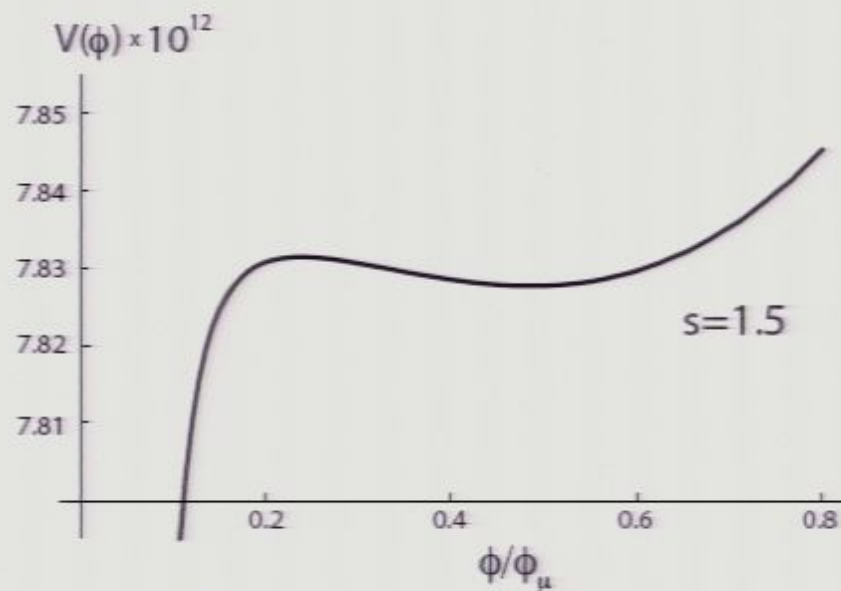
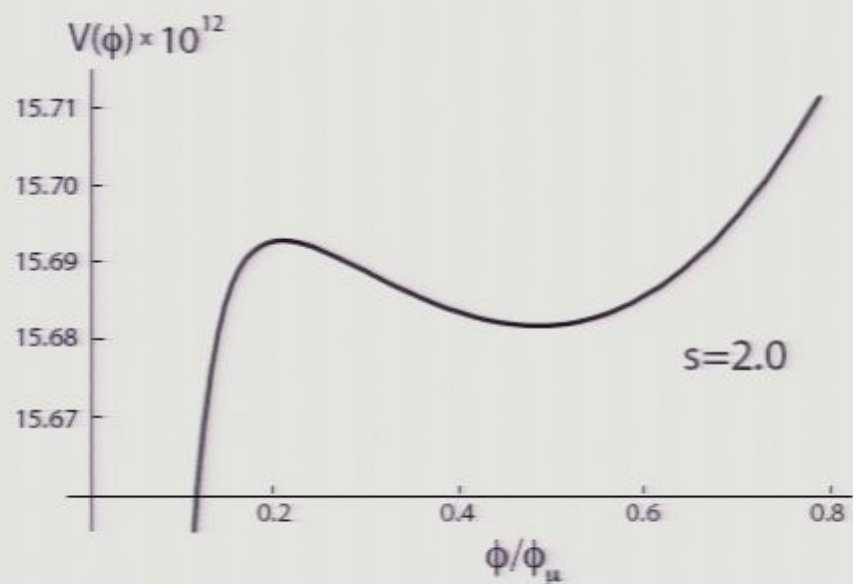
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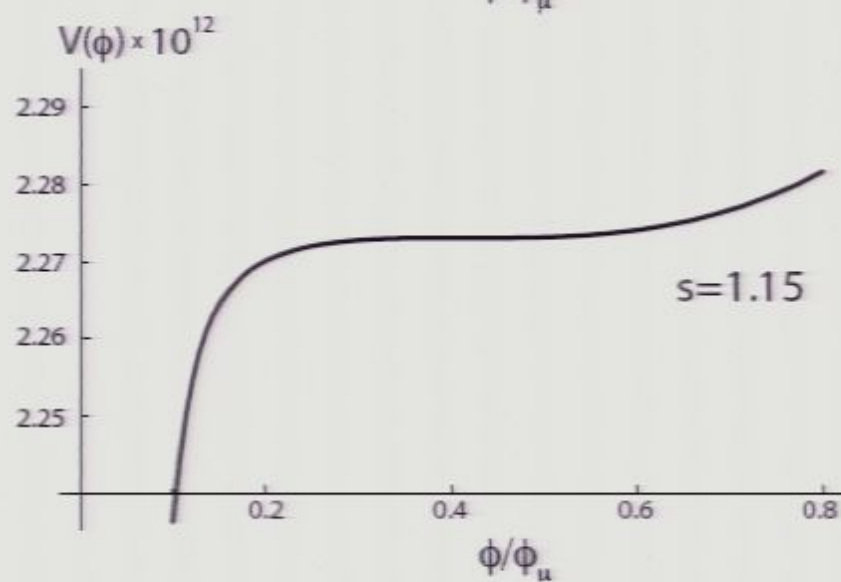
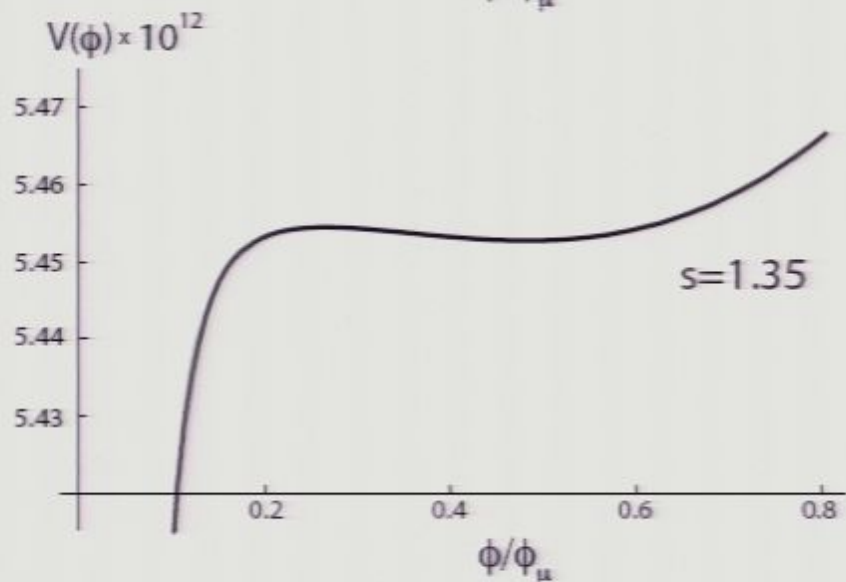
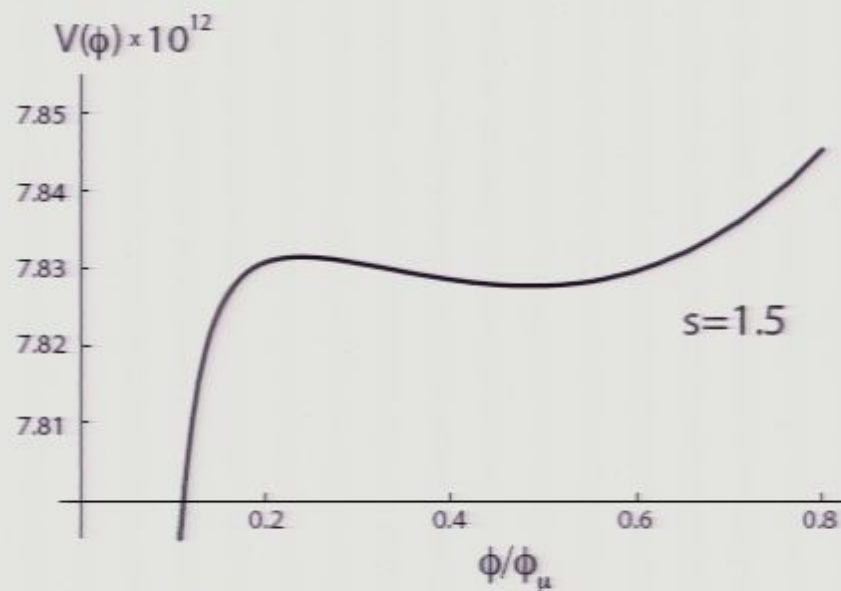
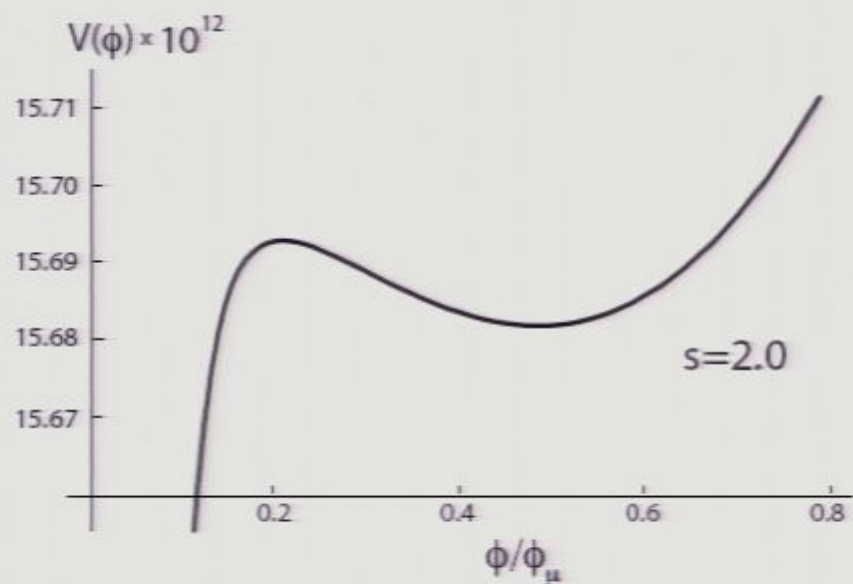
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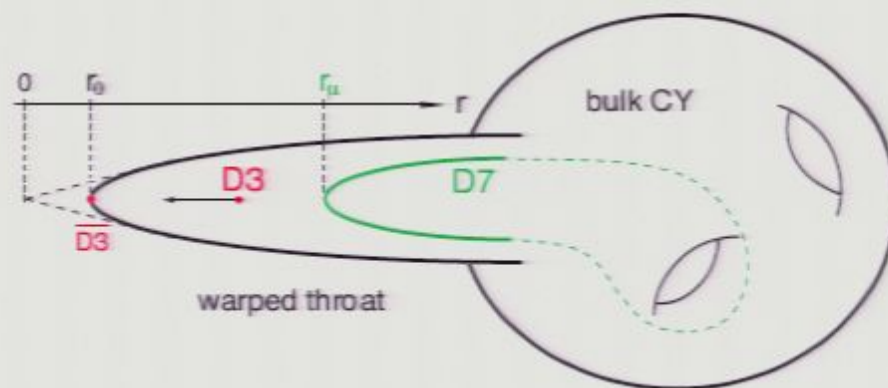
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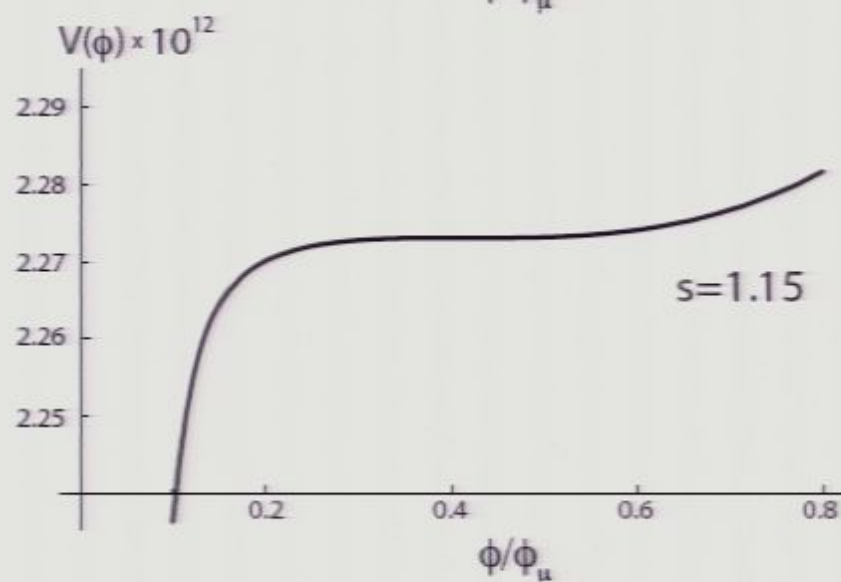
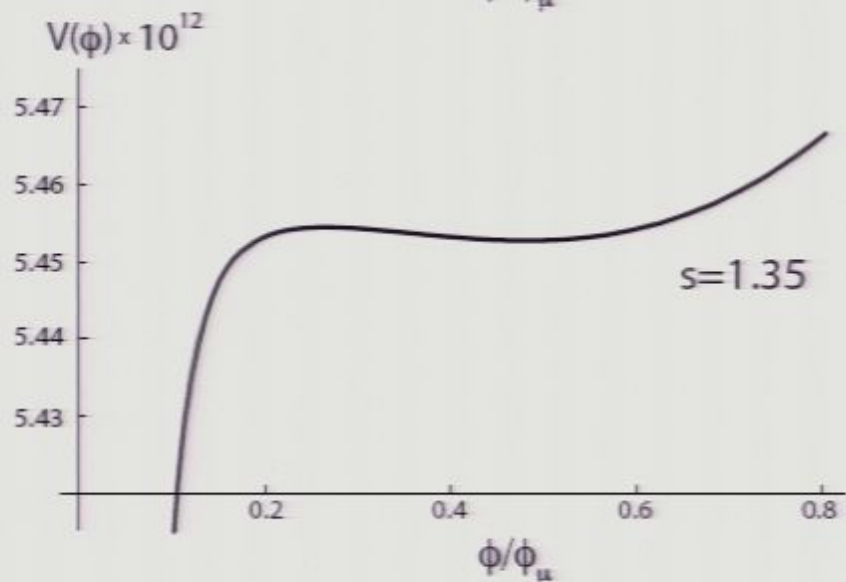
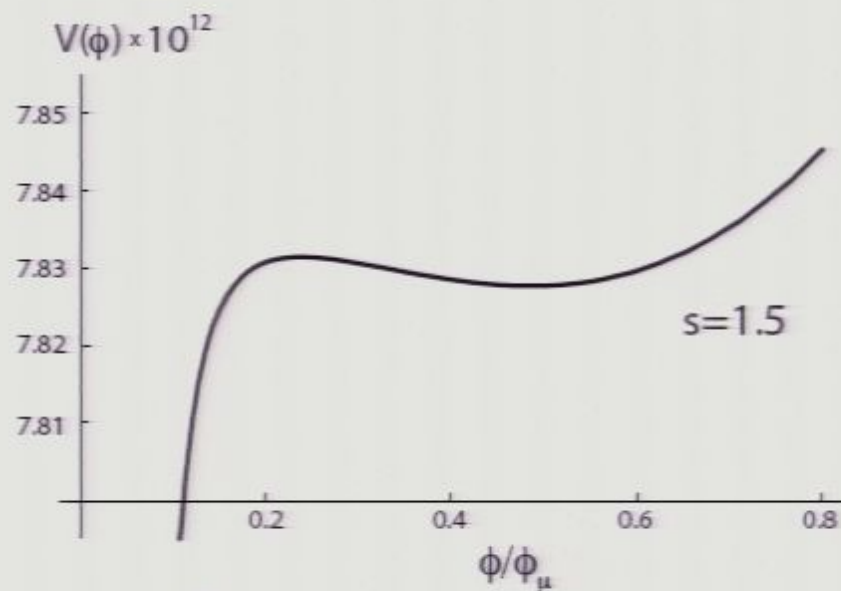
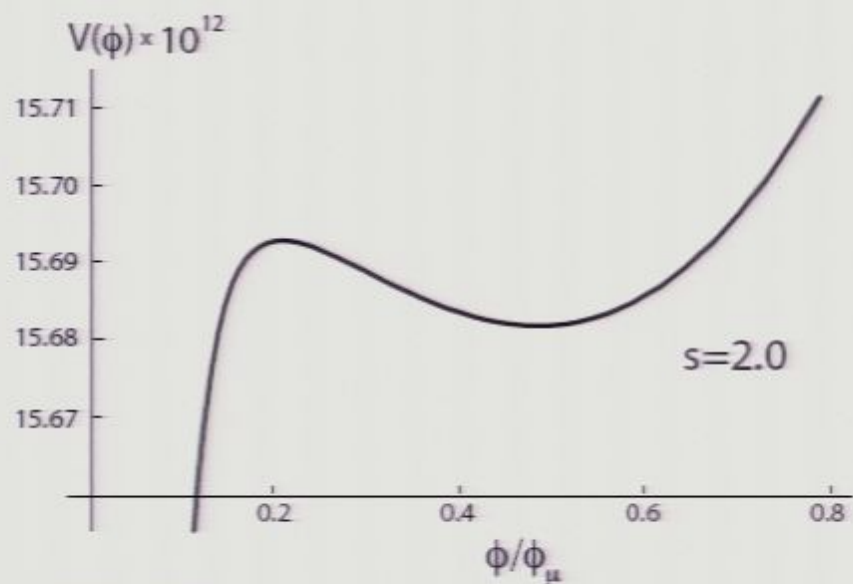
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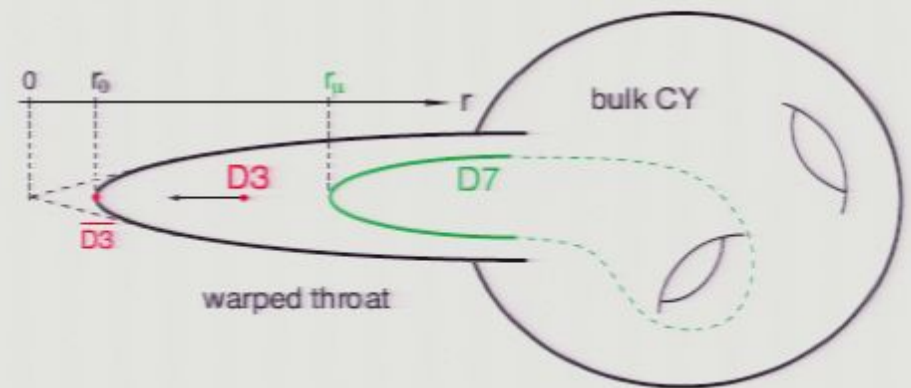
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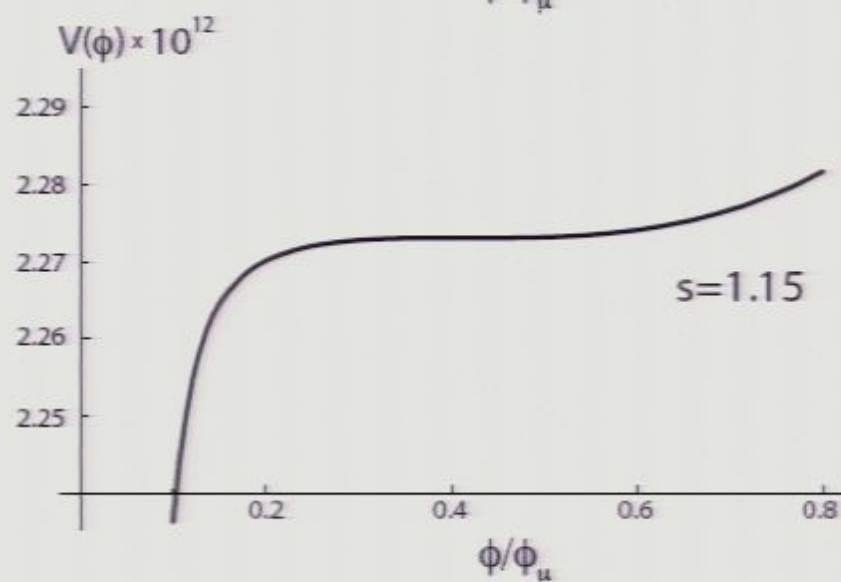
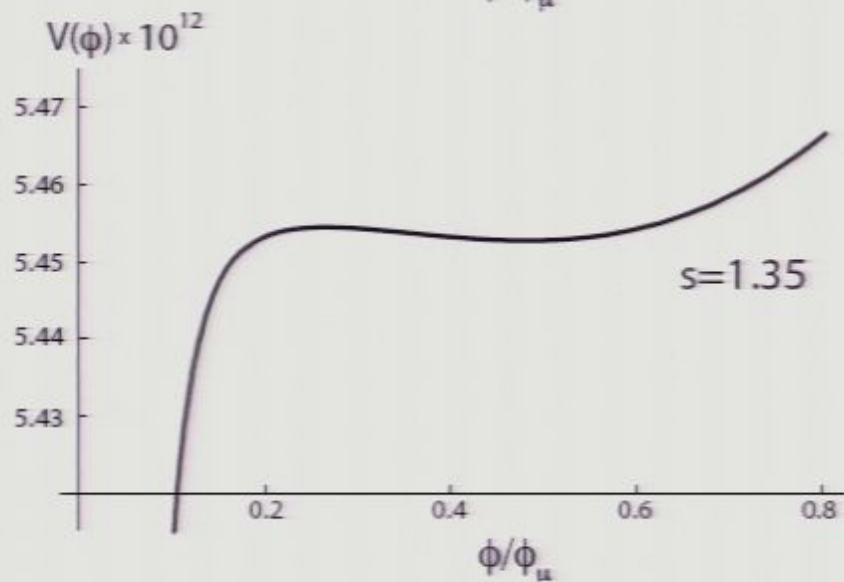
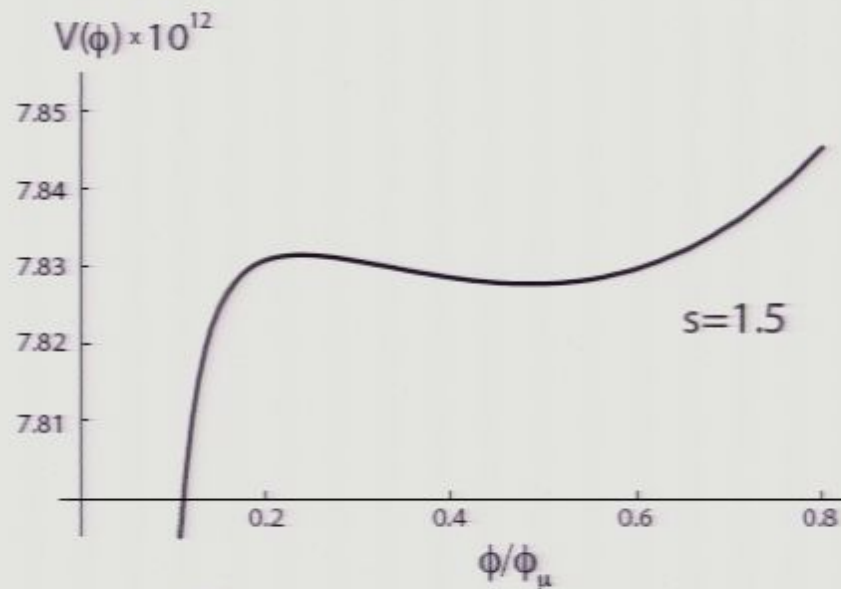
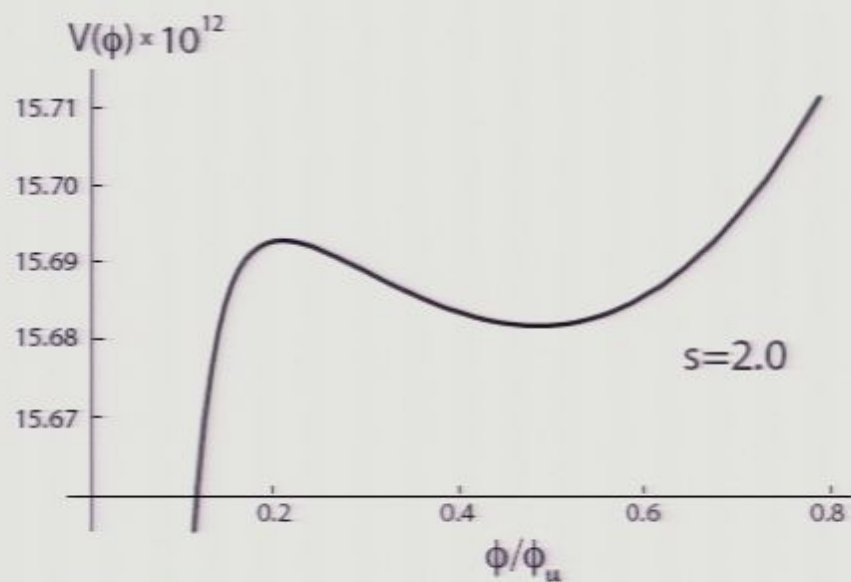
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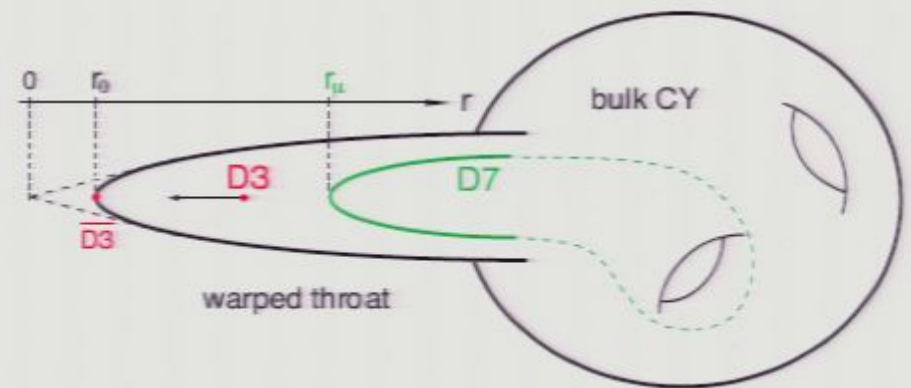
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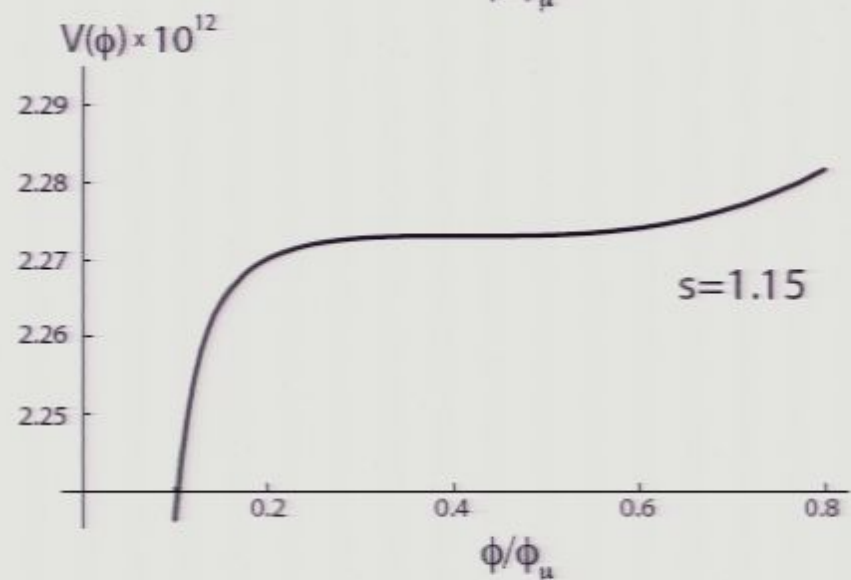
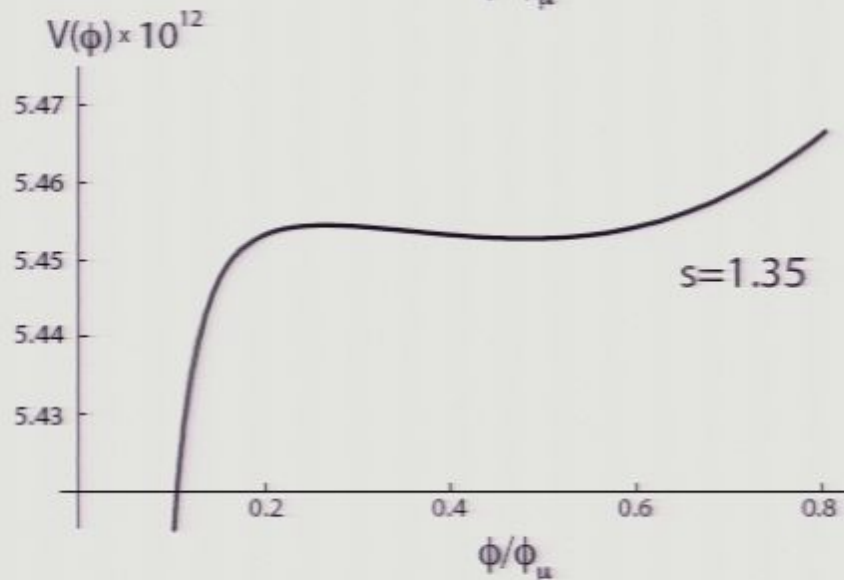
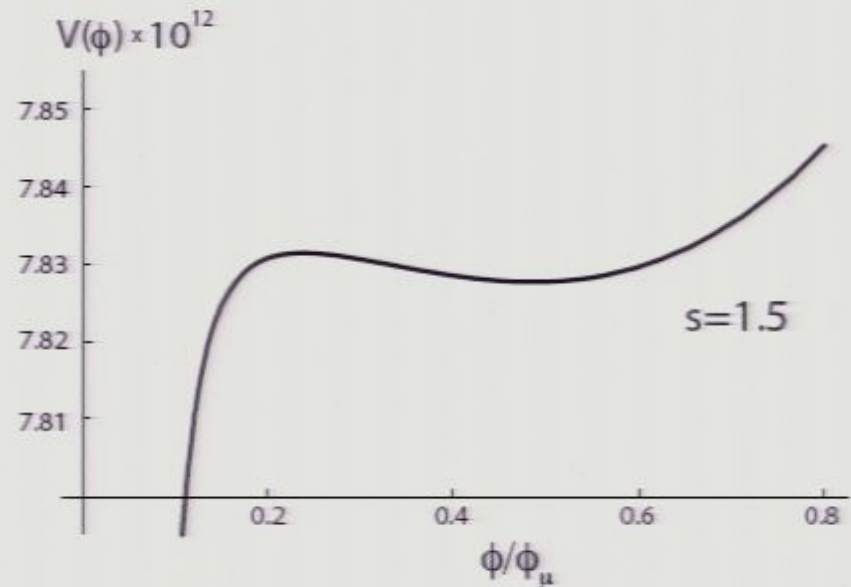
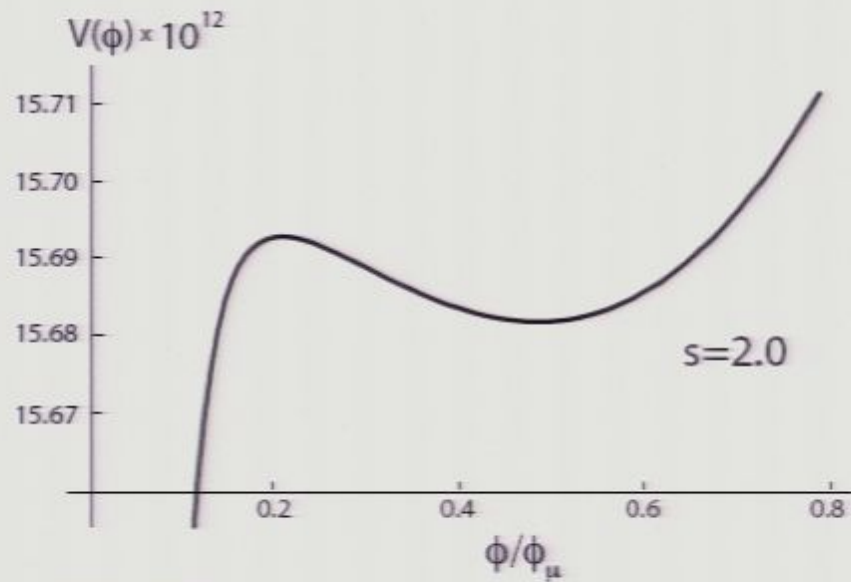
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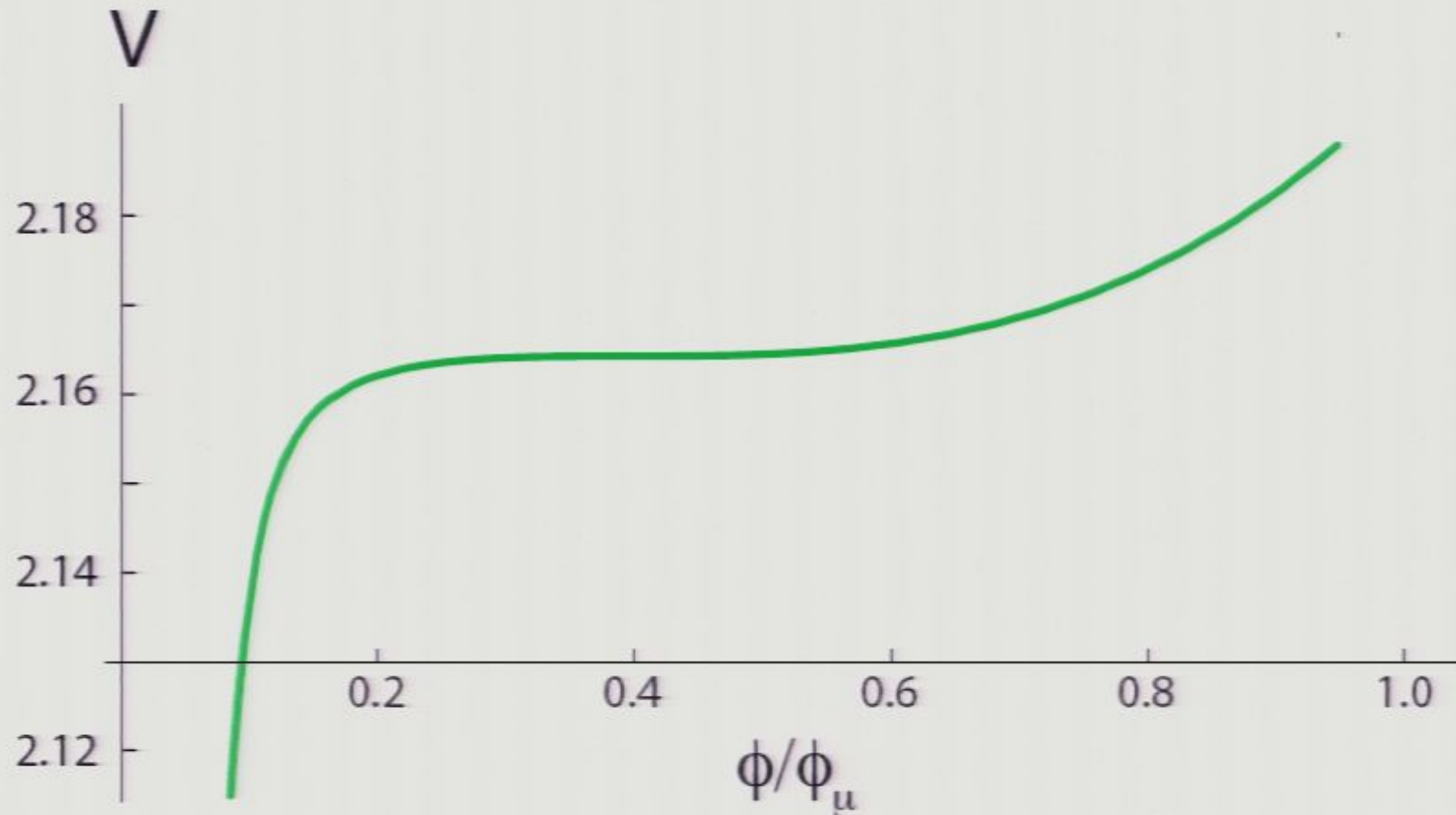
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 $n \ll N$ .



# From Metastable to Monotonic

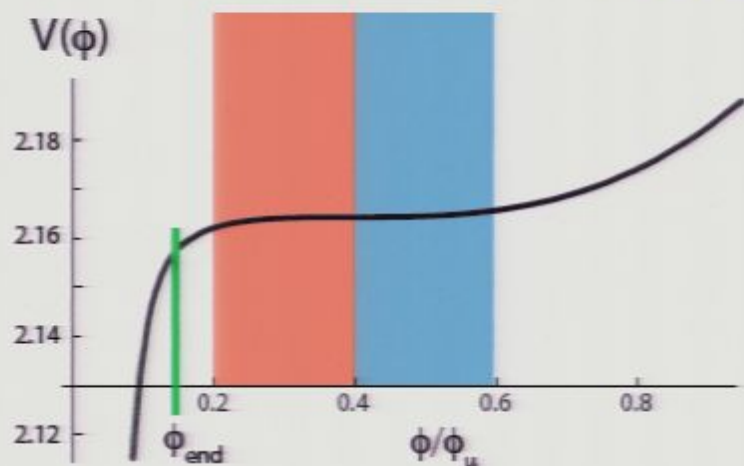


# Inflection Point Inflation



D.B., Dymarsky, Klebanov, McAllister, Steinhardt  
A Delicate Universe: Compactification Obstacles to D-brane Inflation  
PRL 99, 061601 (2007)

# Scalar Spectrum



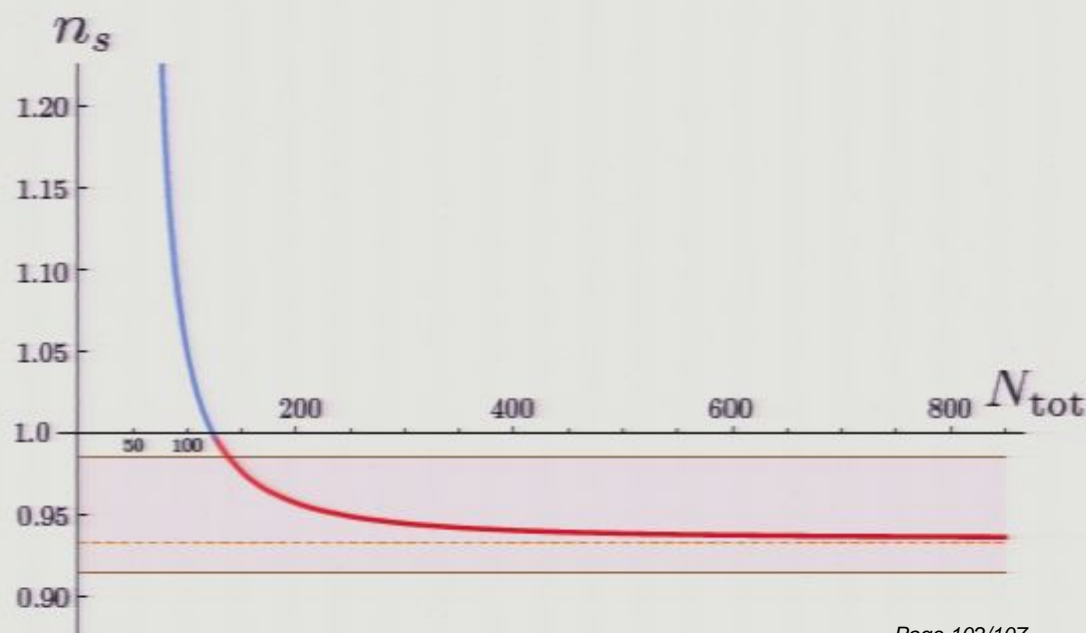
$$V(\phi) = V_0 + \lambda_1 \phi + \frac{1}{3!} \lambda_3 \phi^3$$

Total number of e-folds is finite:  $N_{\text{tot}} = \pi \sqrt{\frac{2V_0^2}{\lambda_1 \lambda_3}}$ .

$$n_s - 1 = -\frac{4\pi}{N_{\text{tot}}} \cot\left(\frac{\pi N_\star}{N_{\text{tot}}}\right)$$

- ▶  $n_s$  can be red or blue;
- ▶ lower limit on  $n_s$ :

$$n_s \geq 1 - \frac{4}{N_\star} \approx 0.9\bar{3}$$





# A Critical Assessment

- ▶ Brane-inflation is fine-tuned and delicate.
- ▶ Scale-invariant scalar spectrum requires extra tuning not required by a solution to the horizon problem.

- ▶ Initial conditions and overshoot problems.


But see: [Itzhaki & Kovetz](#)  
*Inflection Point Inflation*

[Underwood](#)  
*Brane Inflation is Attractive*

- ▶ Model lacks embedding into an honest compactification:  
⇒ parameterize with UV perturbations to KS geometry

[D.B., Dymarsky, Kachru, Klebanov, McAllister,](#)  
*work in progress*

# Conclusions

The Dumbbell Nebula — M27  HUBBLESITE.org

# Inflationary UV Challenges/Opportunities

Three problems in inflationary cosmology **scream out for a UV completion**:

- ▶  **$V(\phi)$  and the  $\eta$ -Problem**

Satisfactory theory must come with a sufficient degree of UV completeness to estimate corrections to the inflationary potential and prove absence of the  $\eta$ -problem.

- ▶ **Gravitational Waves**

$$\frac{\Delta\phi}{M_{\text{pl}}} \sim \mathcal{O}(1) \left( \frac{r}{0.01} \right)^{1/2}$$

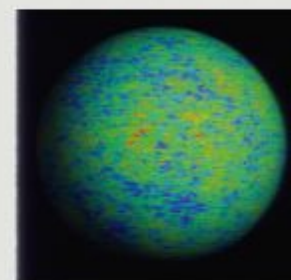
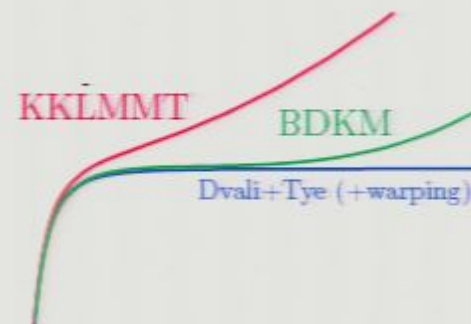
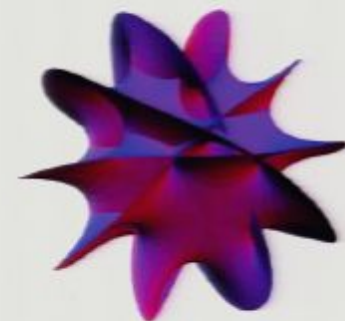
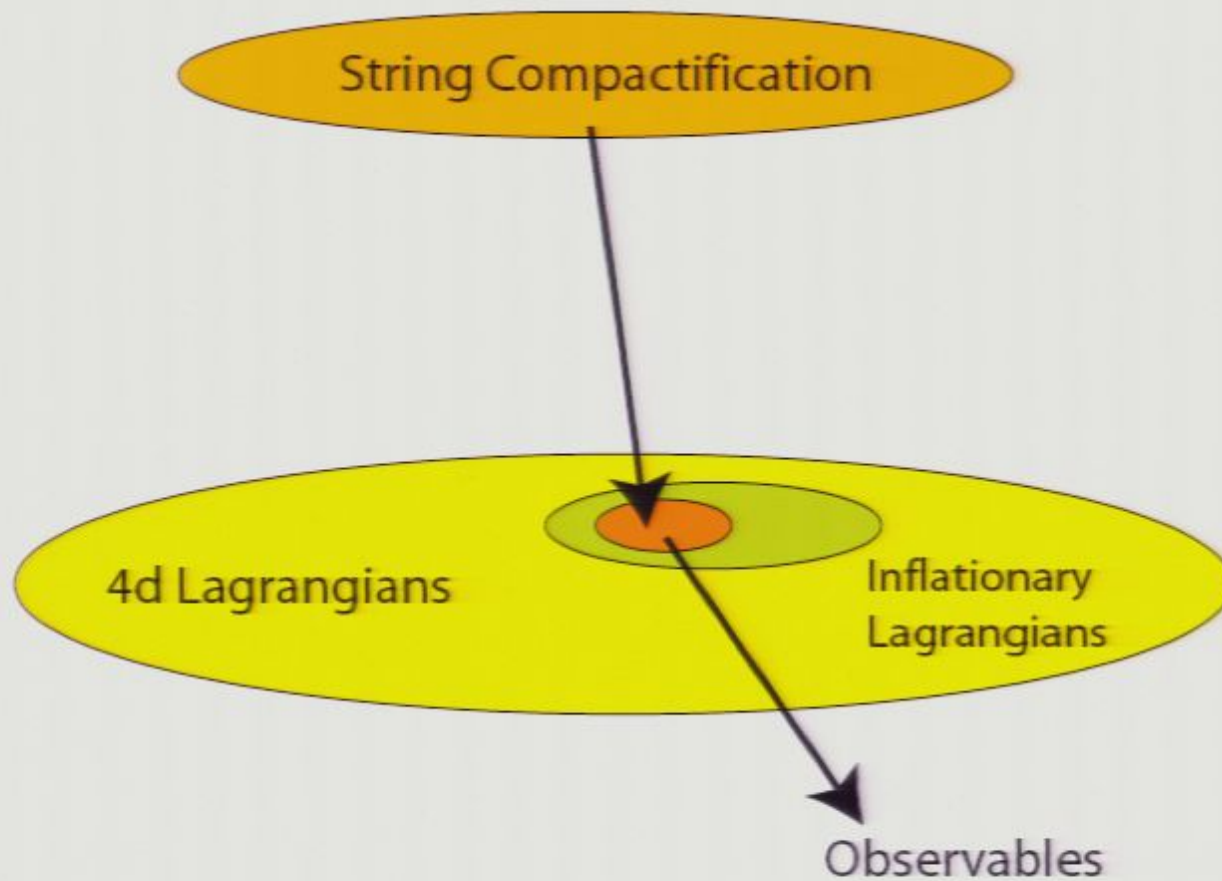
Detection of tensors implies super-Planckian field variation.

- ▶ **Non-Gaussianity**

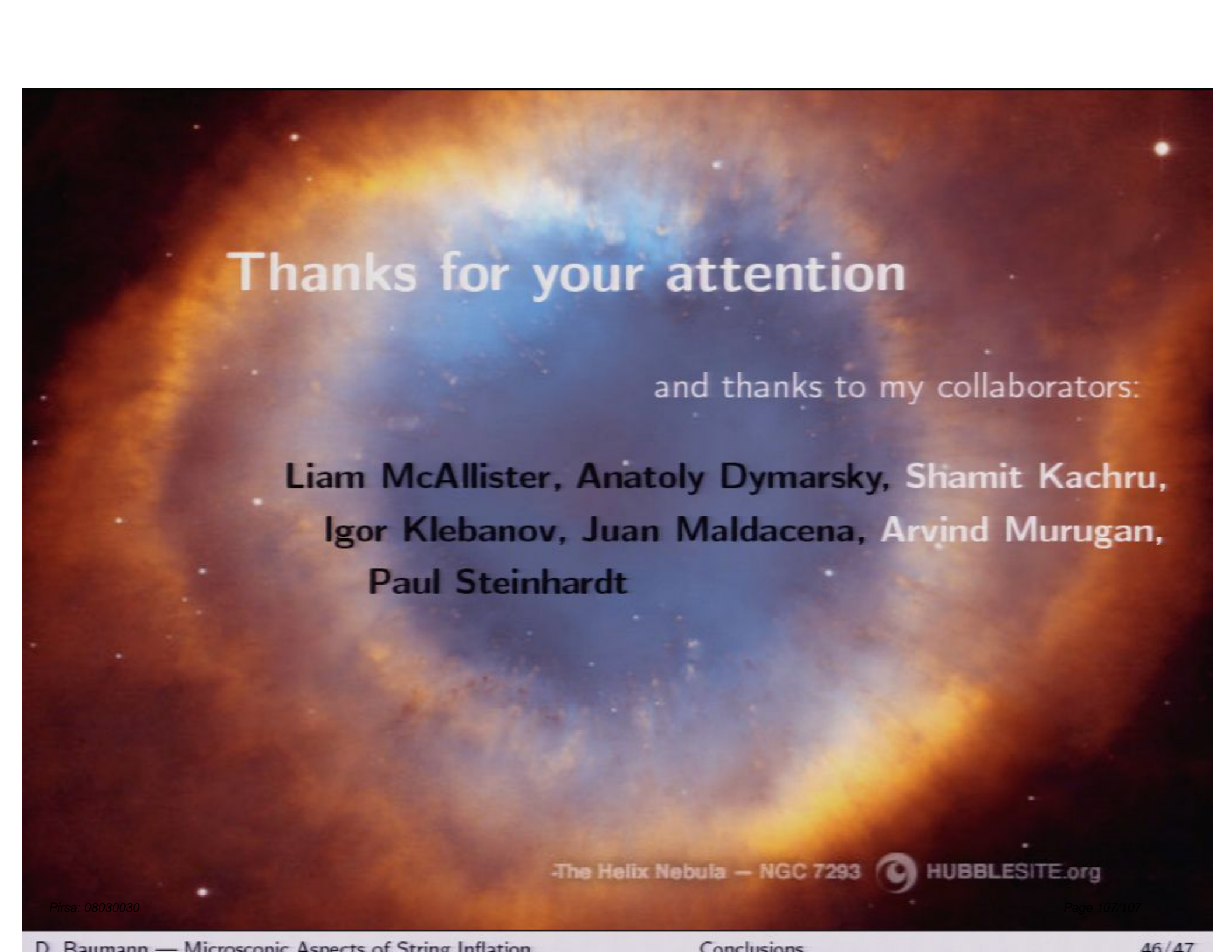
In single-field models non-Gaussianity can only be large if higher derivative terms,  $((\partial\phi)^2)^n$ , play a crucial role during inflation. Of course, this requires a plausible UV completion, e.g. DBI inflation.



# From Compactification Data to Low-Energy Lagrangian






The background of the slide is a vibrant image of the Helix Nebula, showing a complex structure of glowing gas clouds in shades of blue, orange, and red, with numerous bright stars scattered throughout.

**Thanks for your attention**

and thanks to my collaborators:

**Liam McAllister, Anatoly Dymarsky, Shamit Kachru,  
Igor Klebanov, Juan Maldacena, Arvind Murugan,  
Paul Steinhardt**

The Helix Nebula — NGC 7293  HUBBLESITE.org