

Title: Foundations of Quantum Mechanics #2

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Abstract: Interferometry, measurement and interpretation. Beyond the quanta.

# Measurement and Interpretation



*"It would seem that the theory is exclusively concerned with the 'results of measurement' and has nothing to say about anything else. When the 'system' in question is the whole world where is the 'measurer' to be found? Inside, rather than outside, presumably. What exactly qualifies some subsystems to play this role? Was the world wave function waiting to jump for thousands of millions of years until a single-celled living creature appeared? Or did it have to wait a little longer for some more highly qualified measurer - with a PhD?"*

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- Interpretation and Scientific Realism
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- Some solutions to the measurement problem

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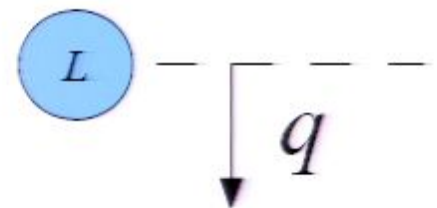




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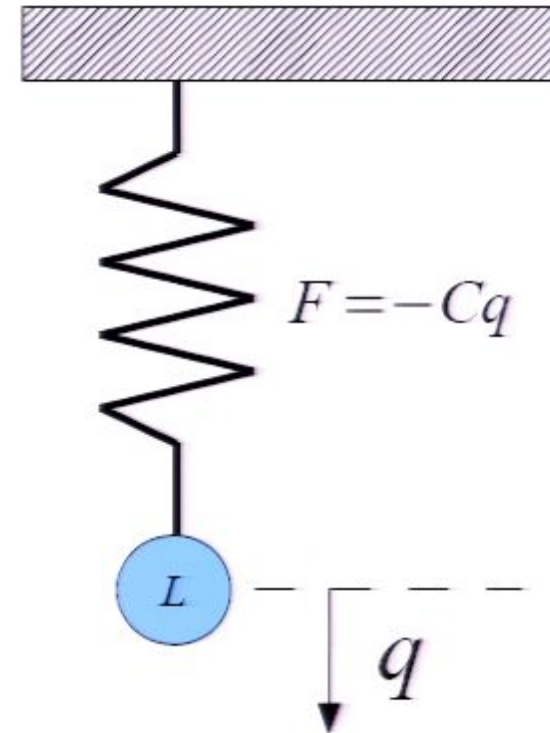
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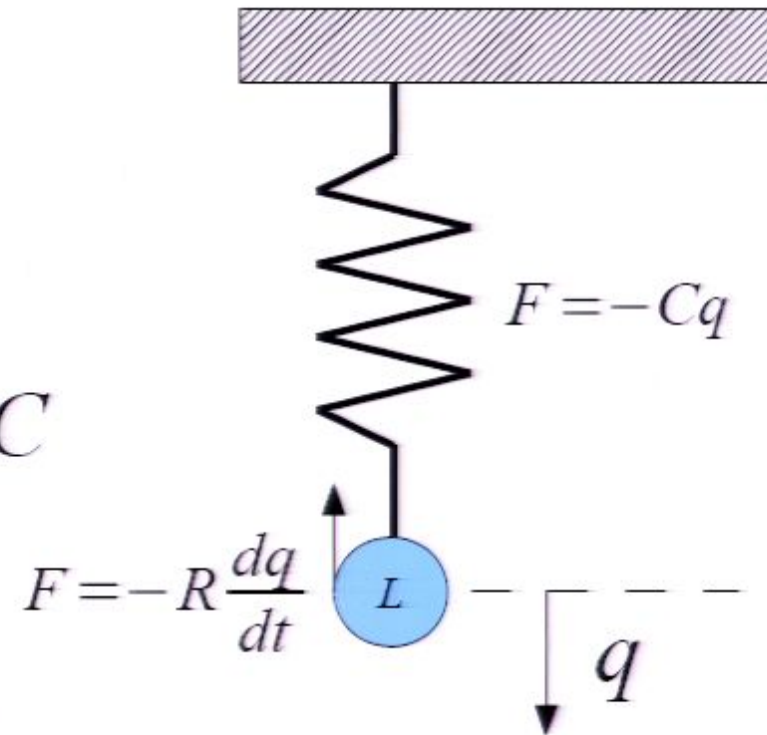


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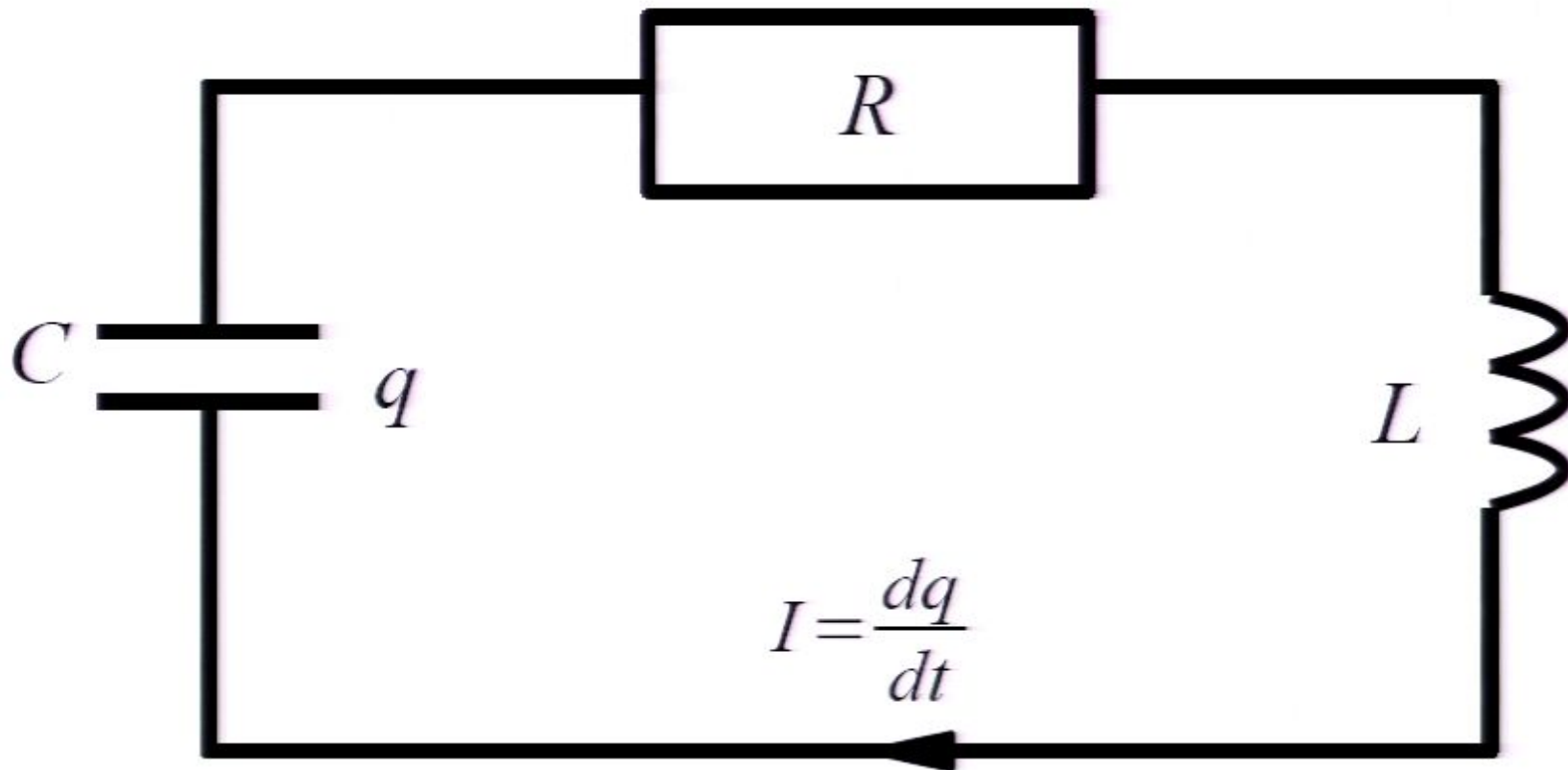
$q$  is the displacement of a mass of  $L$  kg

connected to a spring with Hooke's constant  $C$

and in a viscous medium with resistance  $R$



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# Interpretation and physics



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- At the absolute minimum, one must interpret to make predictions at all
  - Experiments make lights flash, things go click, pointers to point at numbers on a dial, printers to squirt ink on papers.
  - Something in the the mathematics of the theory has got to be identified as telling you which lights will or will not flash, when or how often things go click, what numbers get pointed to, what pretty patterns get ejected from the printer.

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  - Before and after coin flipped?
  - Before and after result seen?

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  - At the minimum a theory must tell us

$$P(K|I, J)$$

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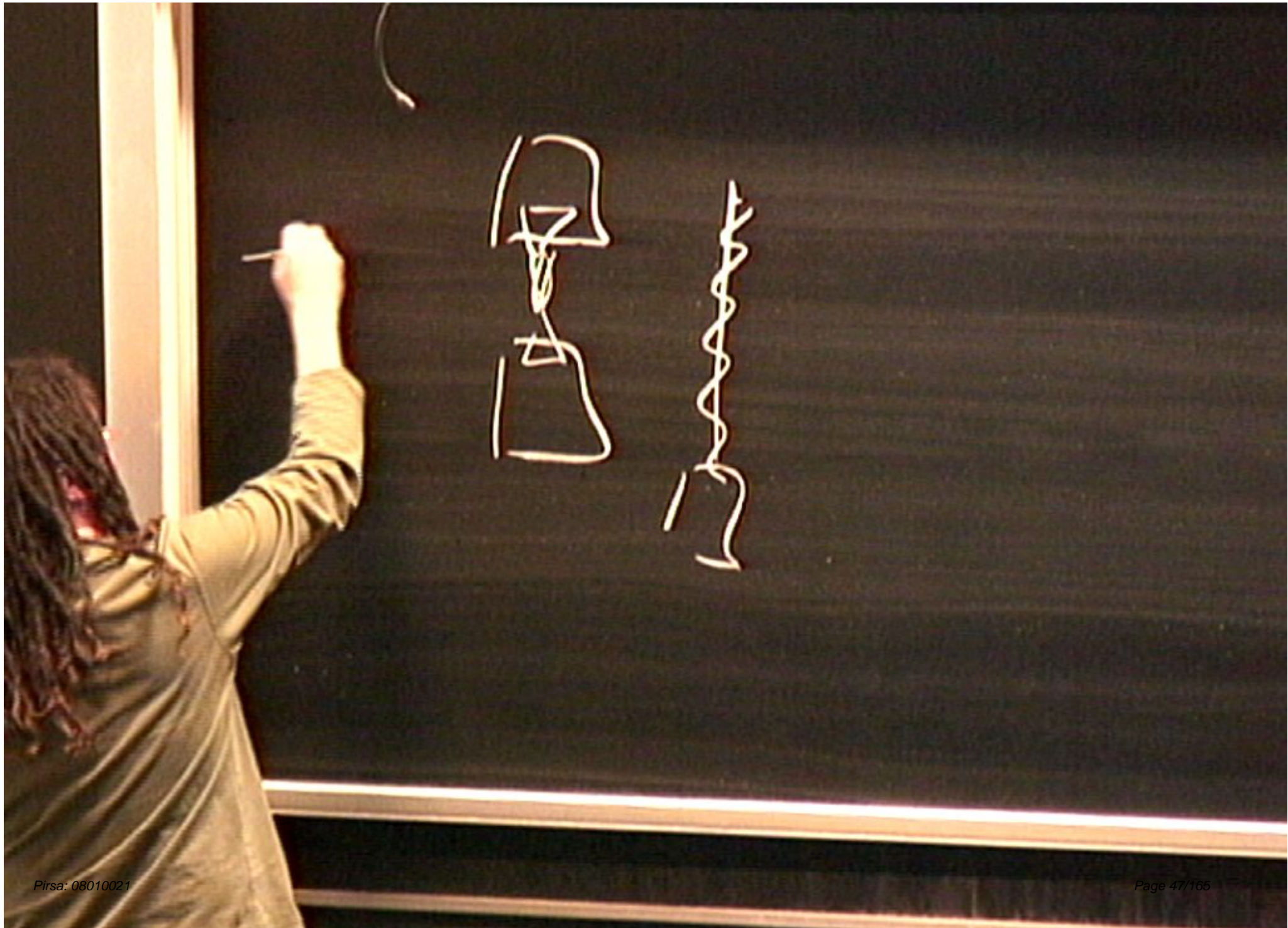
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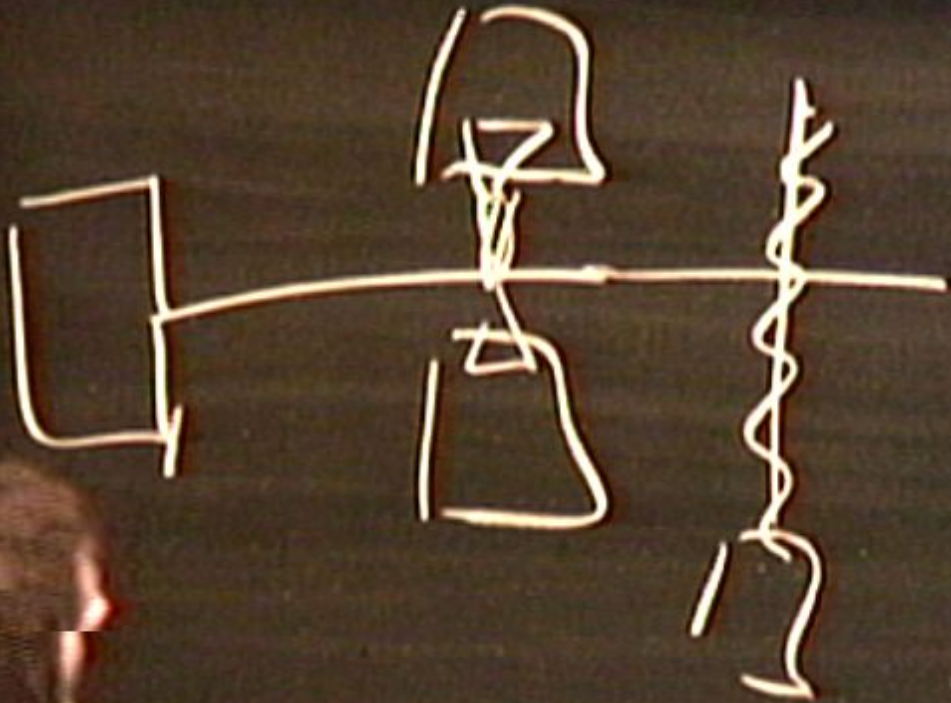
$$\text{If } \begin{array}{l} \psi_1 \rightarrow \psi'_1 \\ \psi_2 \rightarrow \psi'_2 \end{array} \text{ then } \alpha \psi_1 + \beta \psi_2 \rightarrow \alpha \psi'_1 + \beta \psi'_2$$

# Is Quantum theory a fundamental theory?

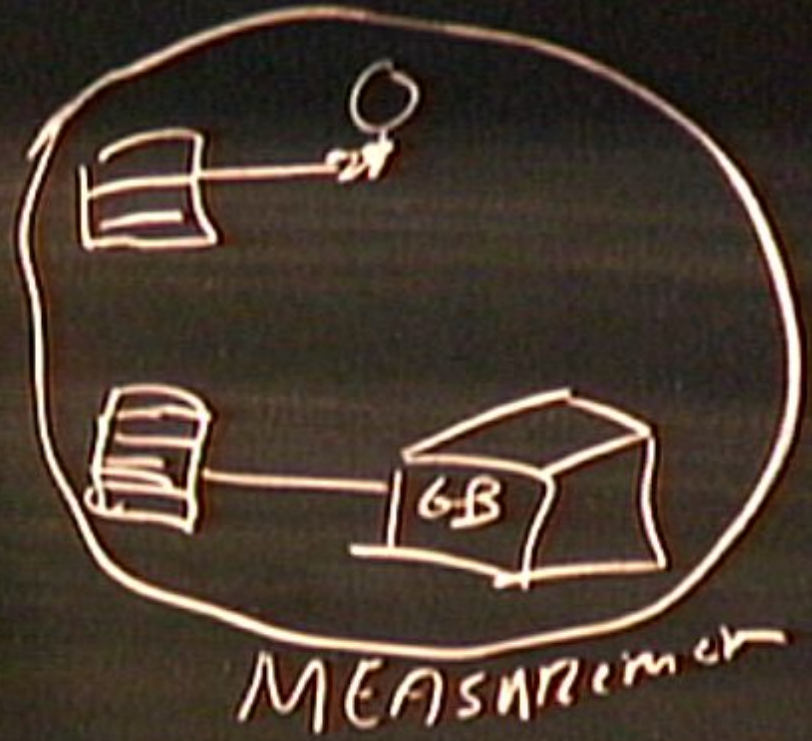
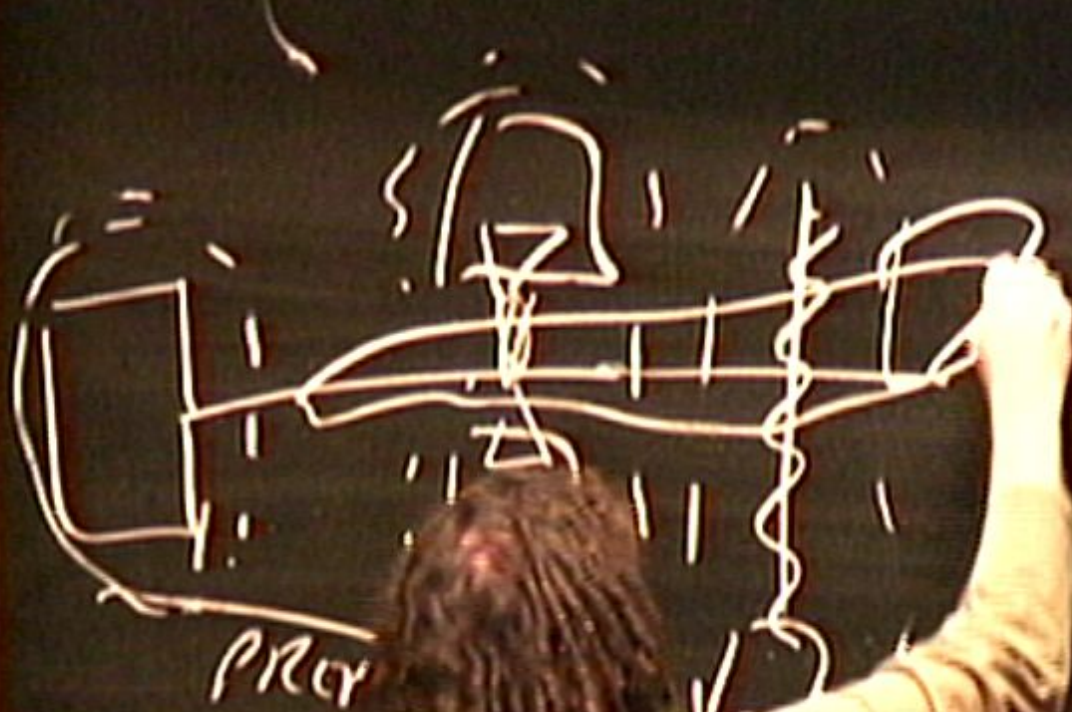


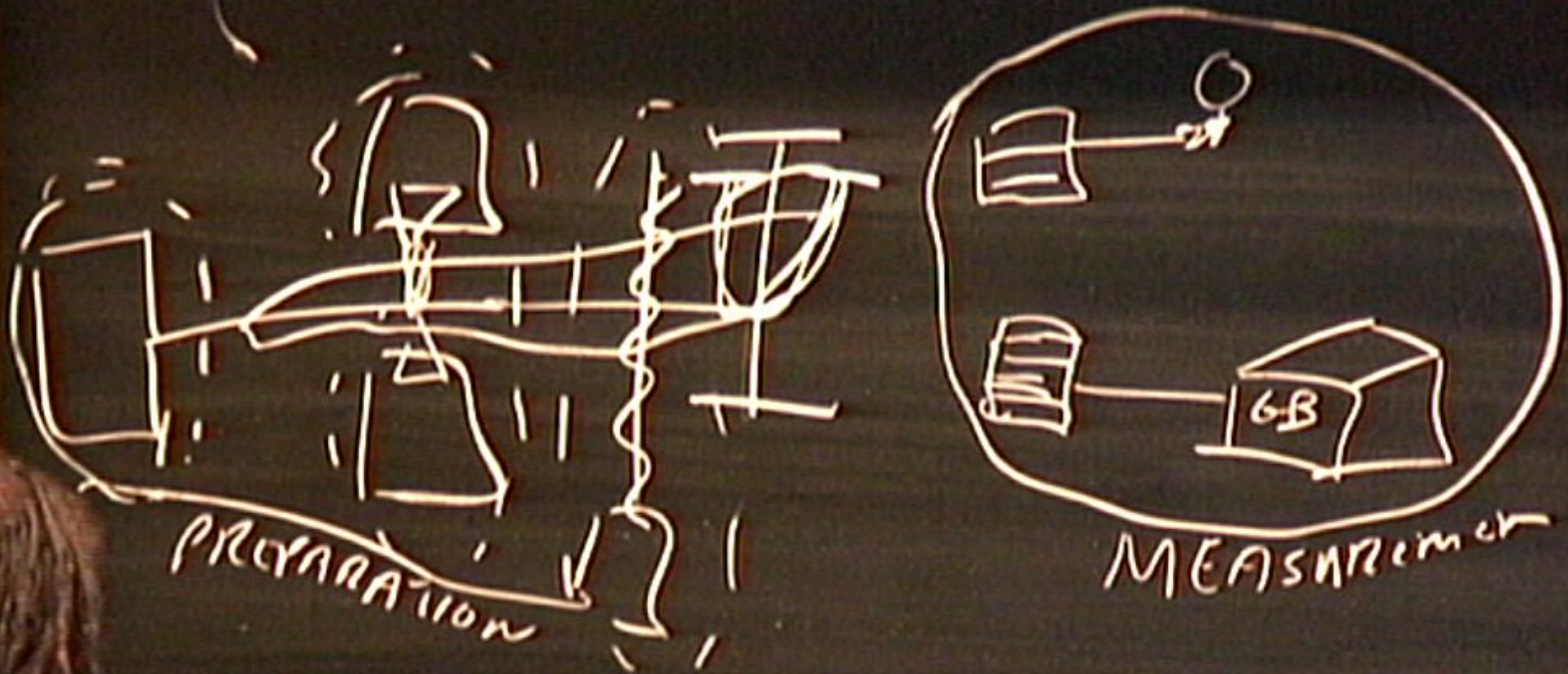
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  - Does quantum mechanics enable us to describe apparatus, equipment, chairs etc?
  - Is the process of measurement itself described by quantum theory?
  - In short, is quantum theory a universal theory or not?



# The Measurement Problem!



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We also want it to interact with a different state:  
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**MARKS**

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and interacts so that

$$\psi_u \Phi_0 E_0 \rightarrow \psi_u \Phi_u E_u$$

so that the measuring device state corresponds to something like a big pointer pointing at the letter "U"

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We also want it to interact with a different state:

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*Recent work has suggested a resolution, but it is still controversial.*

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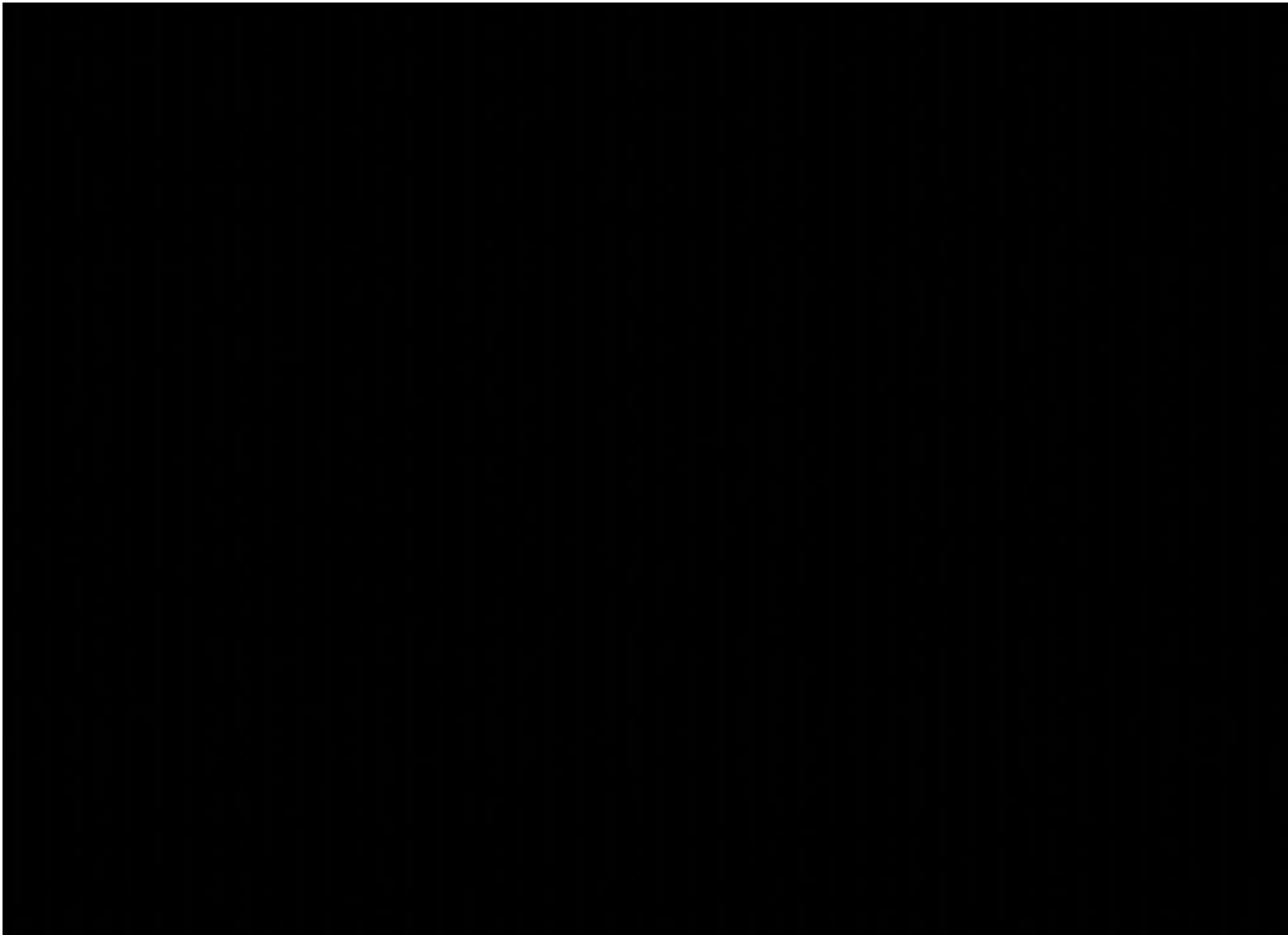
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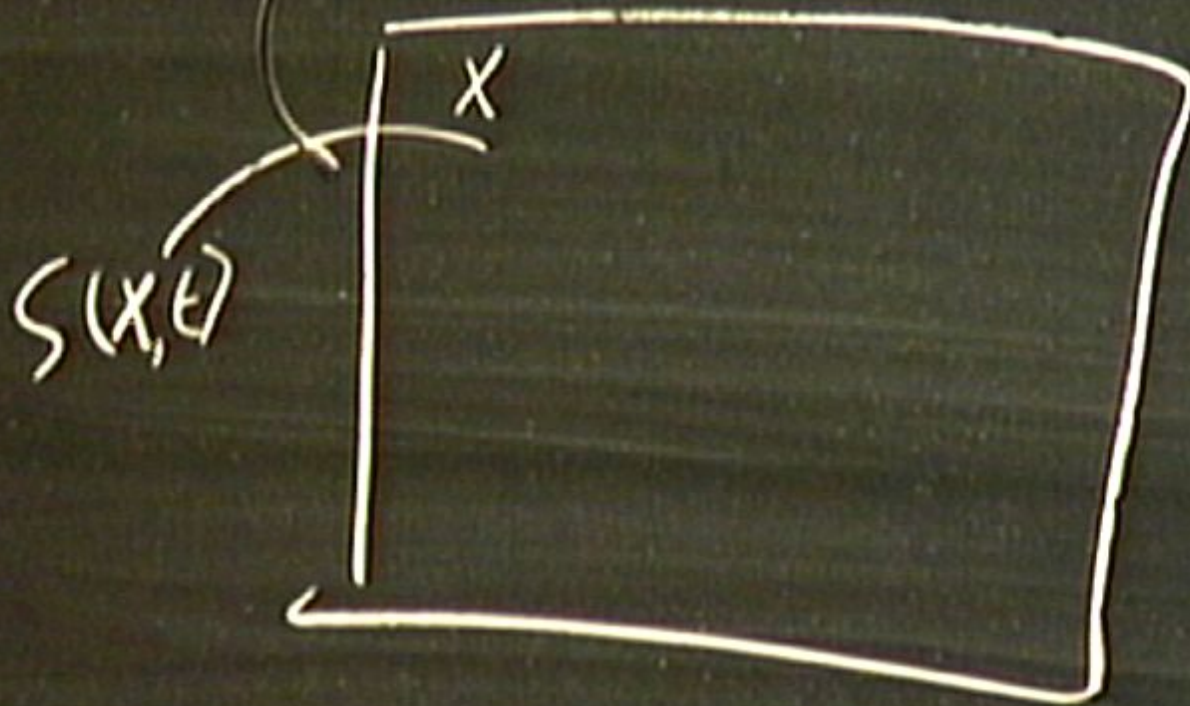
$$J(x, t) = \frac{\psi^*(x, t) \hbar \nabla \psi(x, t) - \psi(x, t) \hbar \nabla \psi^*(x, t)}{2im} = \frac{P(x, t) \hbar \nabla S(x, t)}{m} = P(x, t) \dot{x}$$



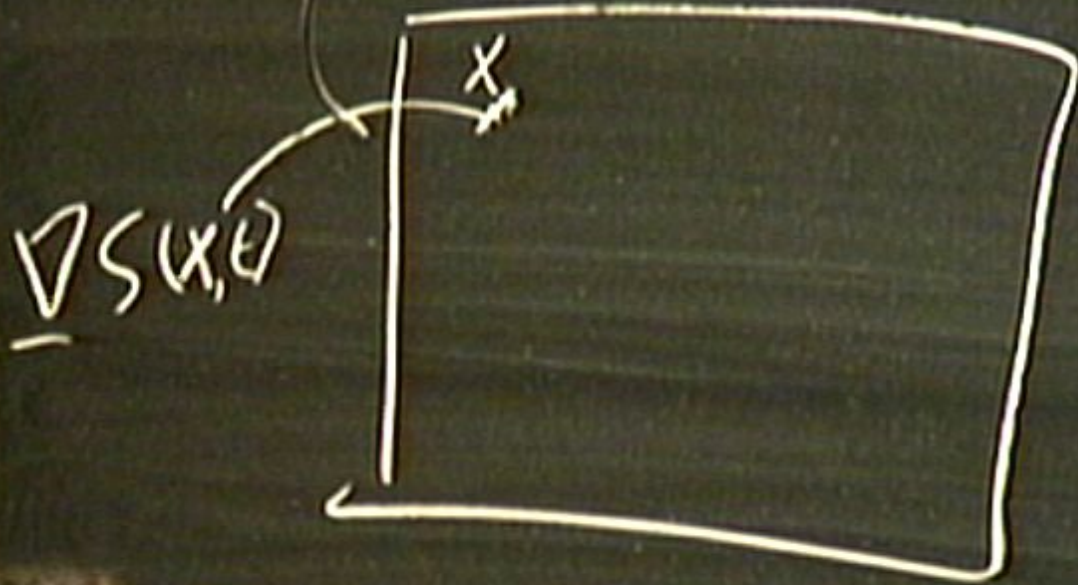
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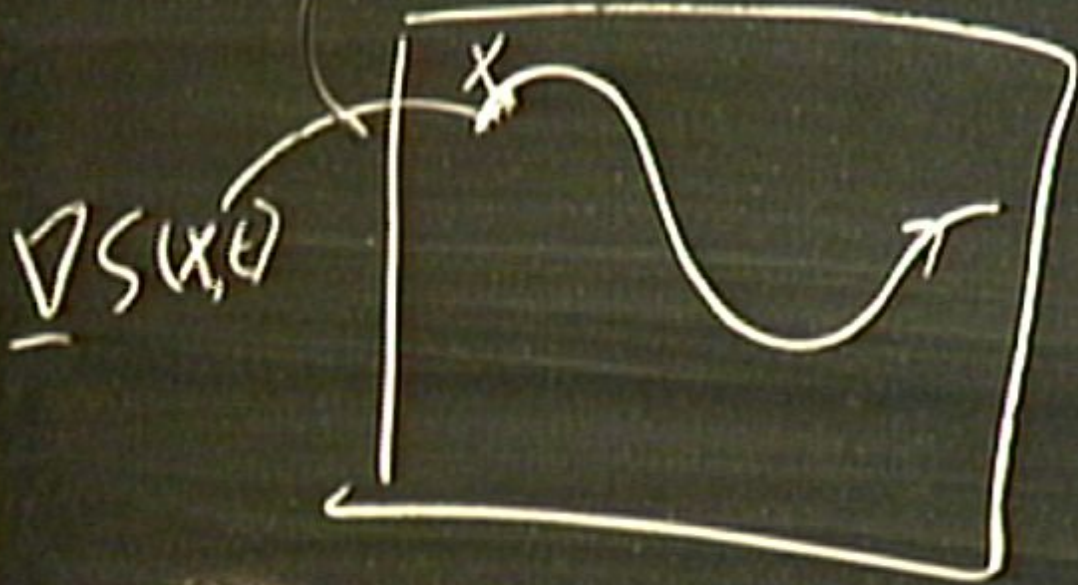
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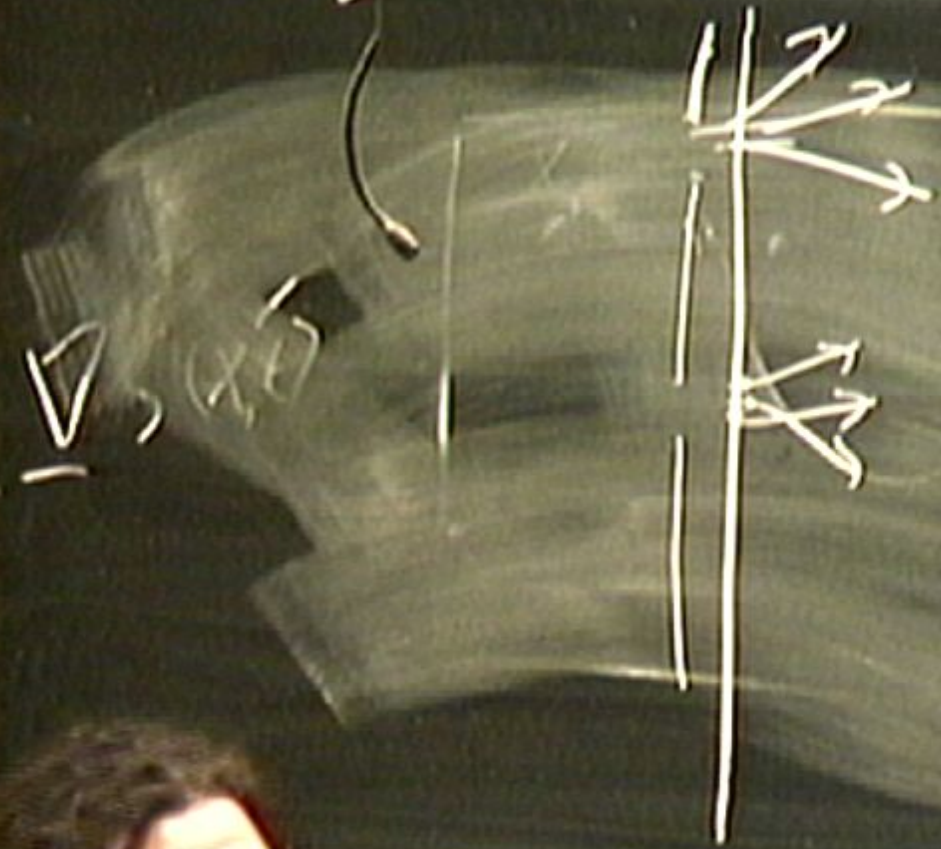
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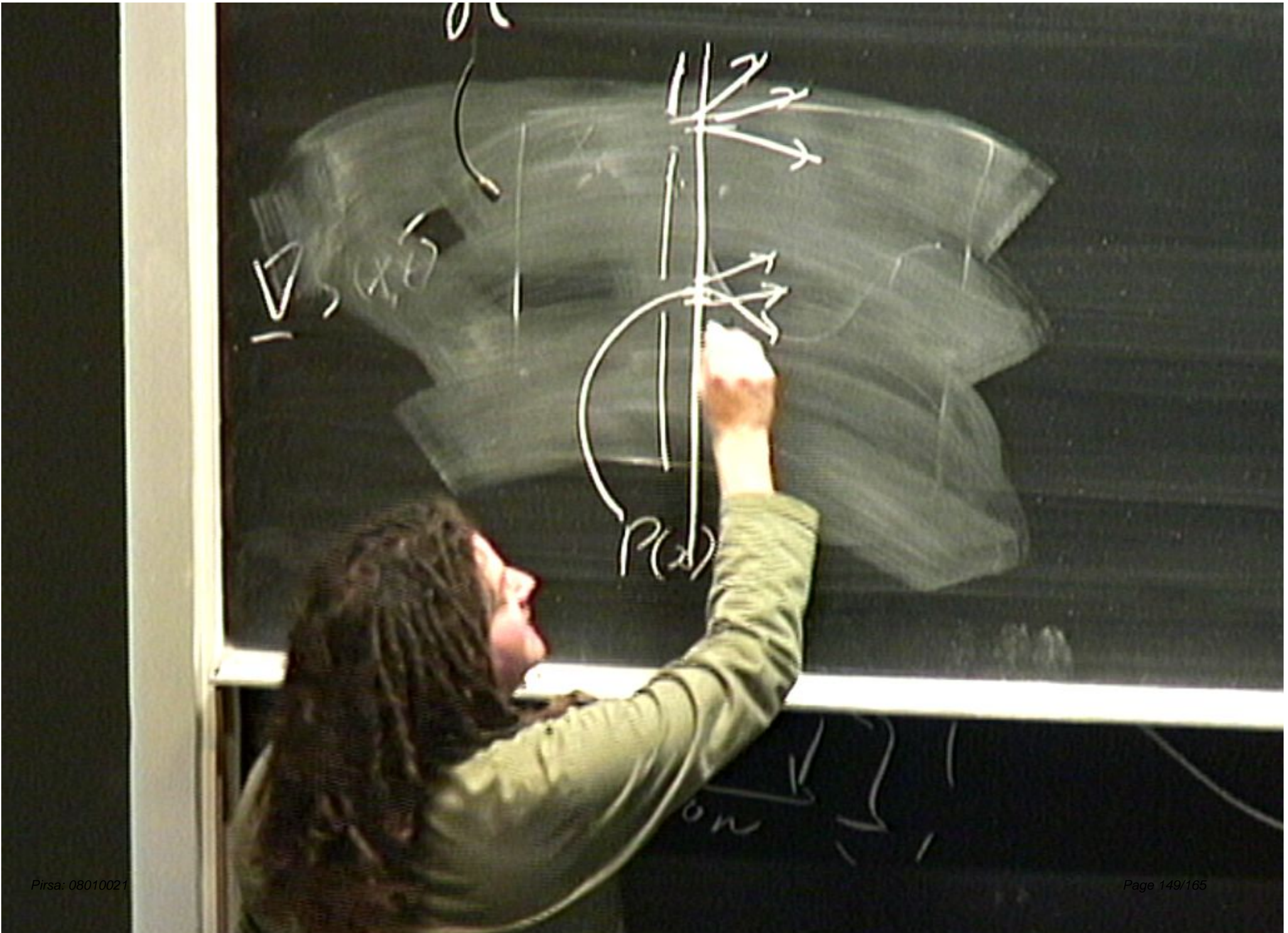
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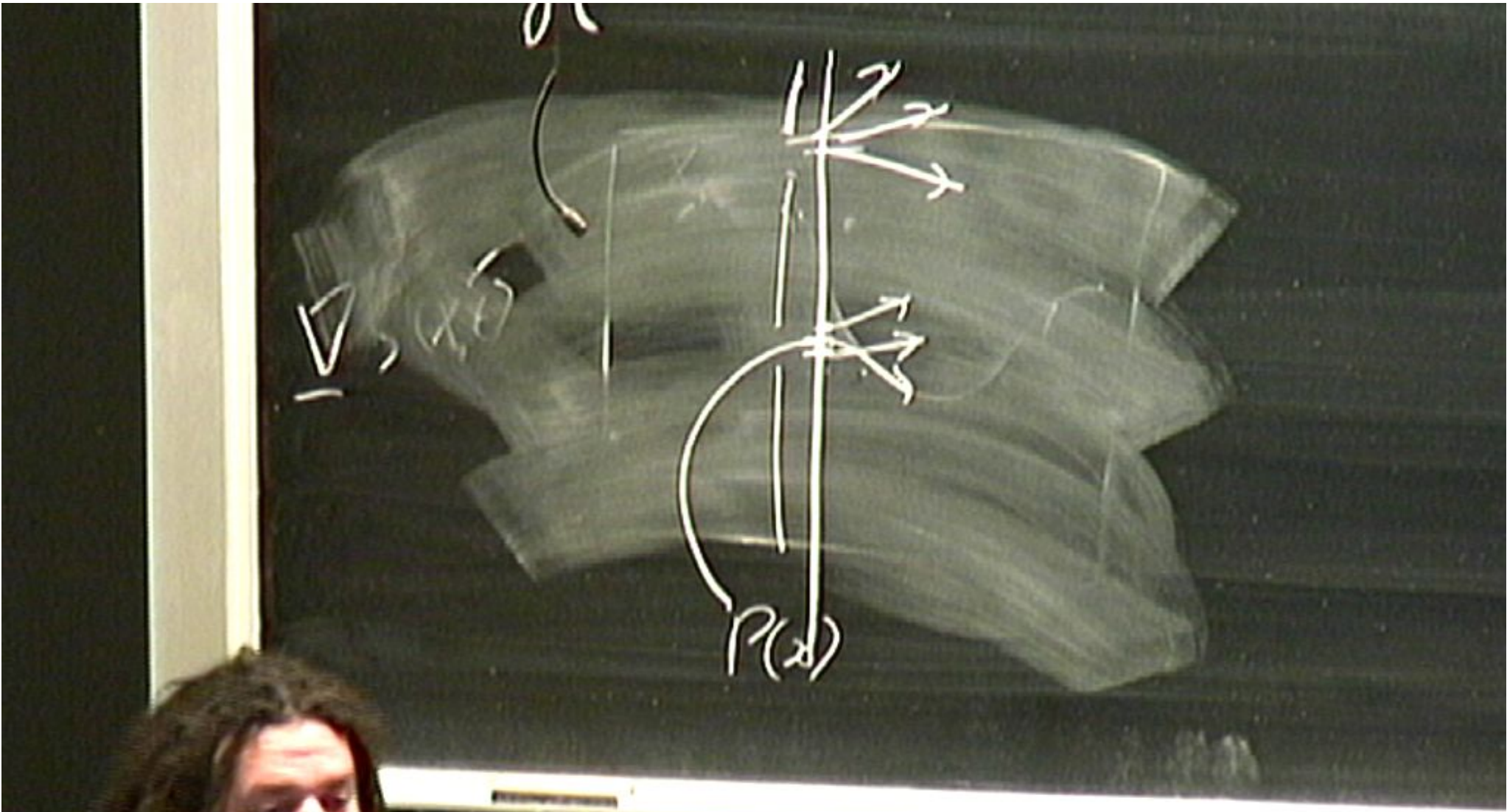
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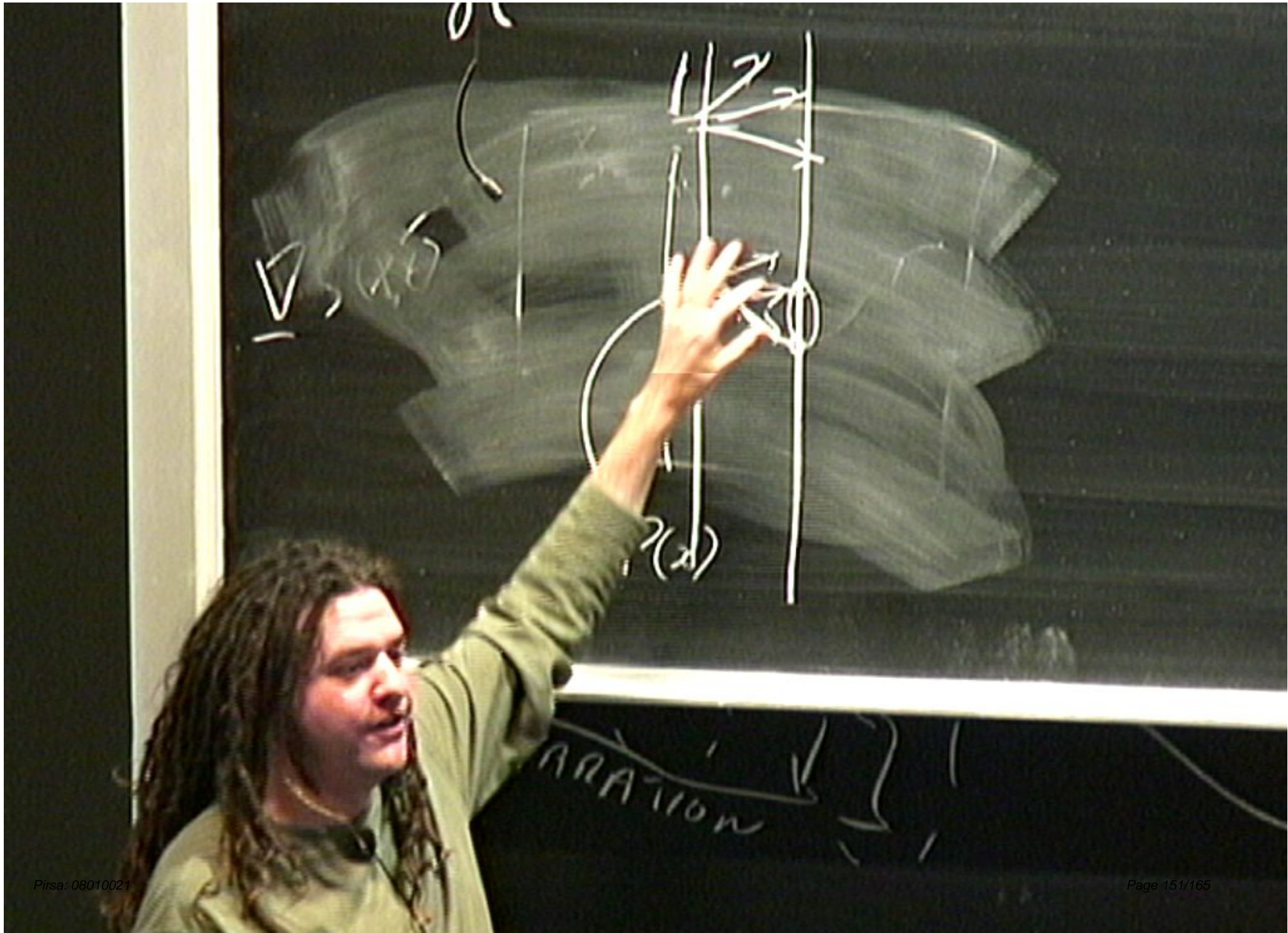
$$\frac{d}{dt} (P + V(P, V)) = 0$$

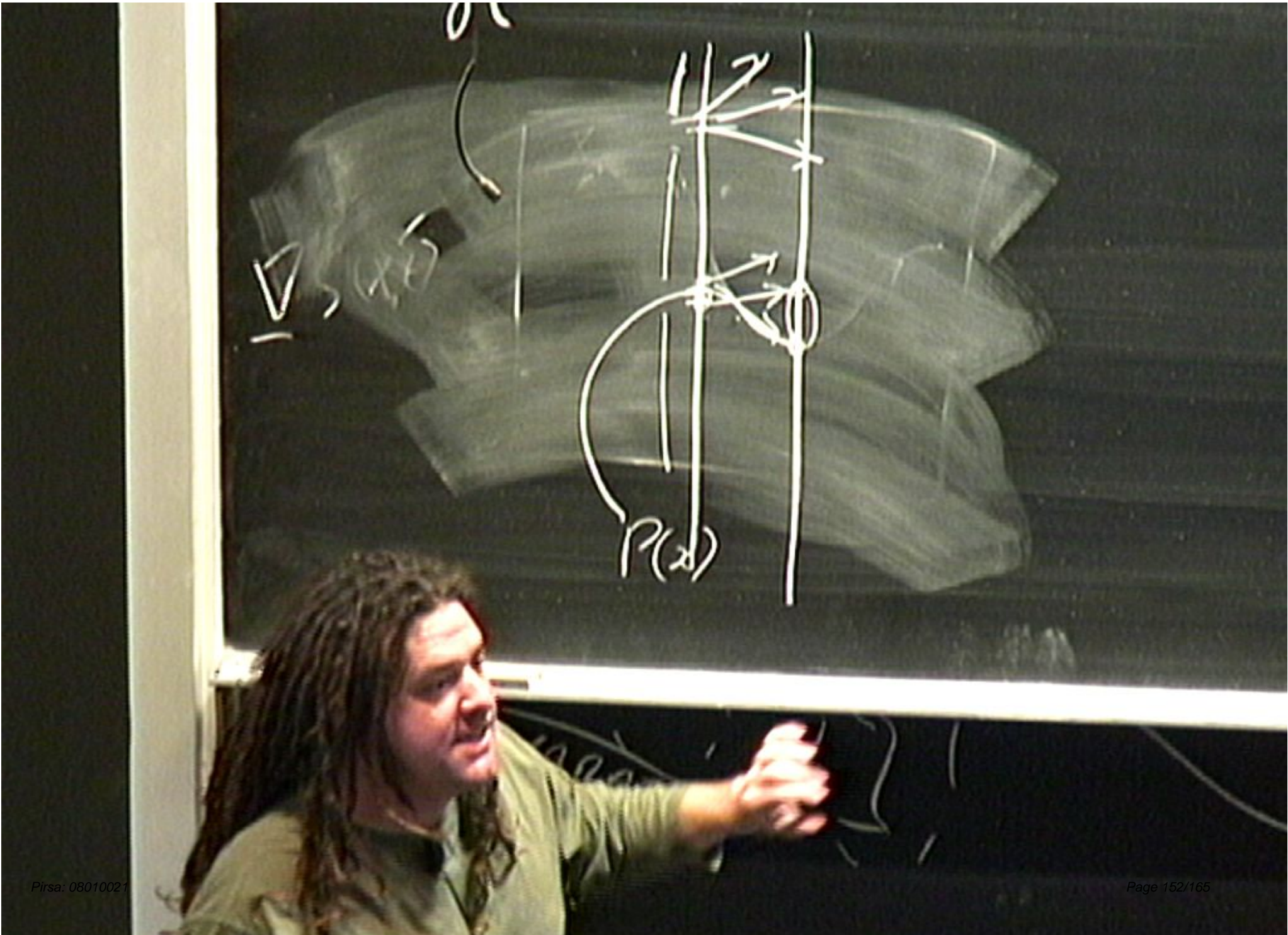






PREPARATION







(2)

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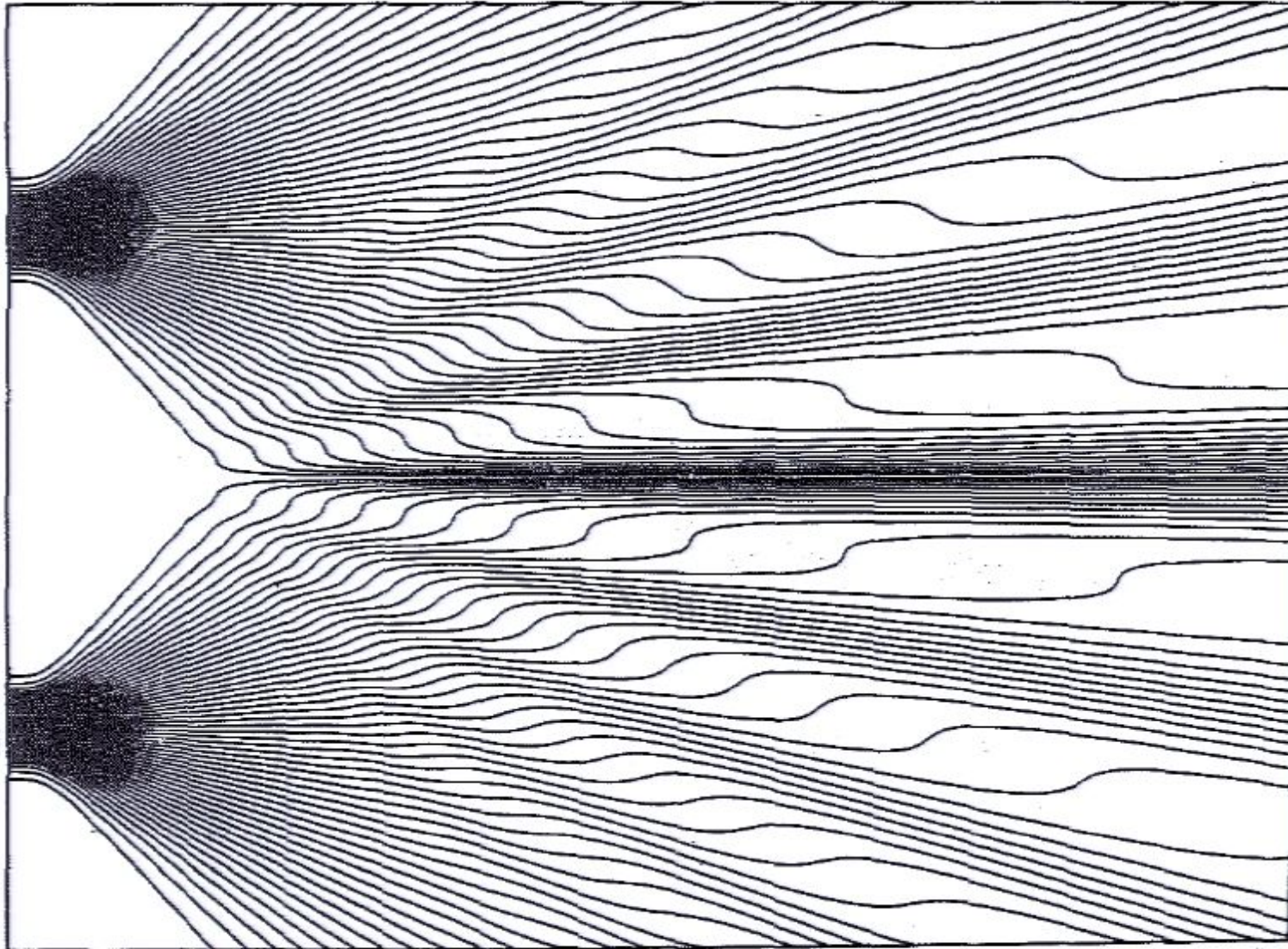
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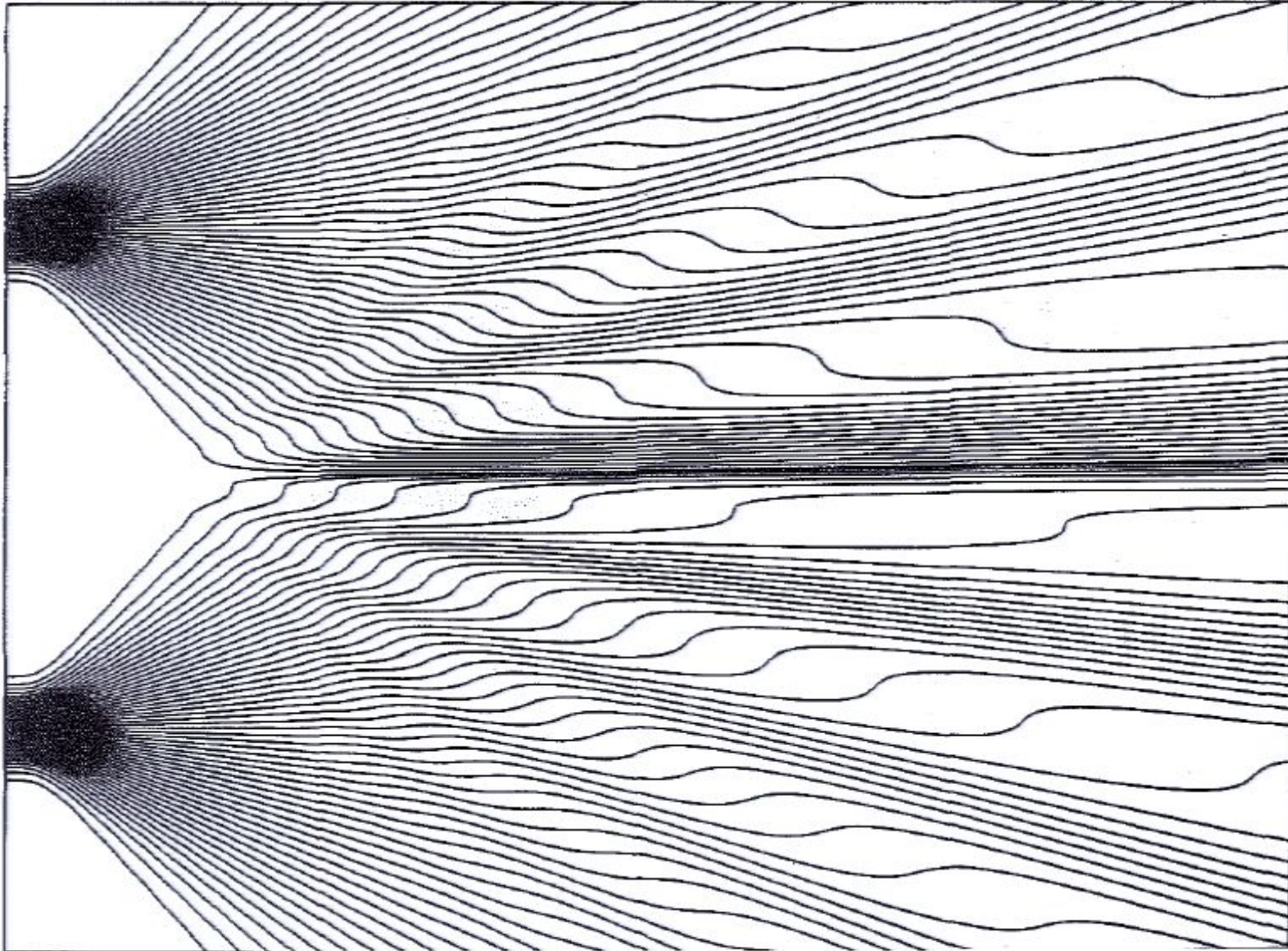
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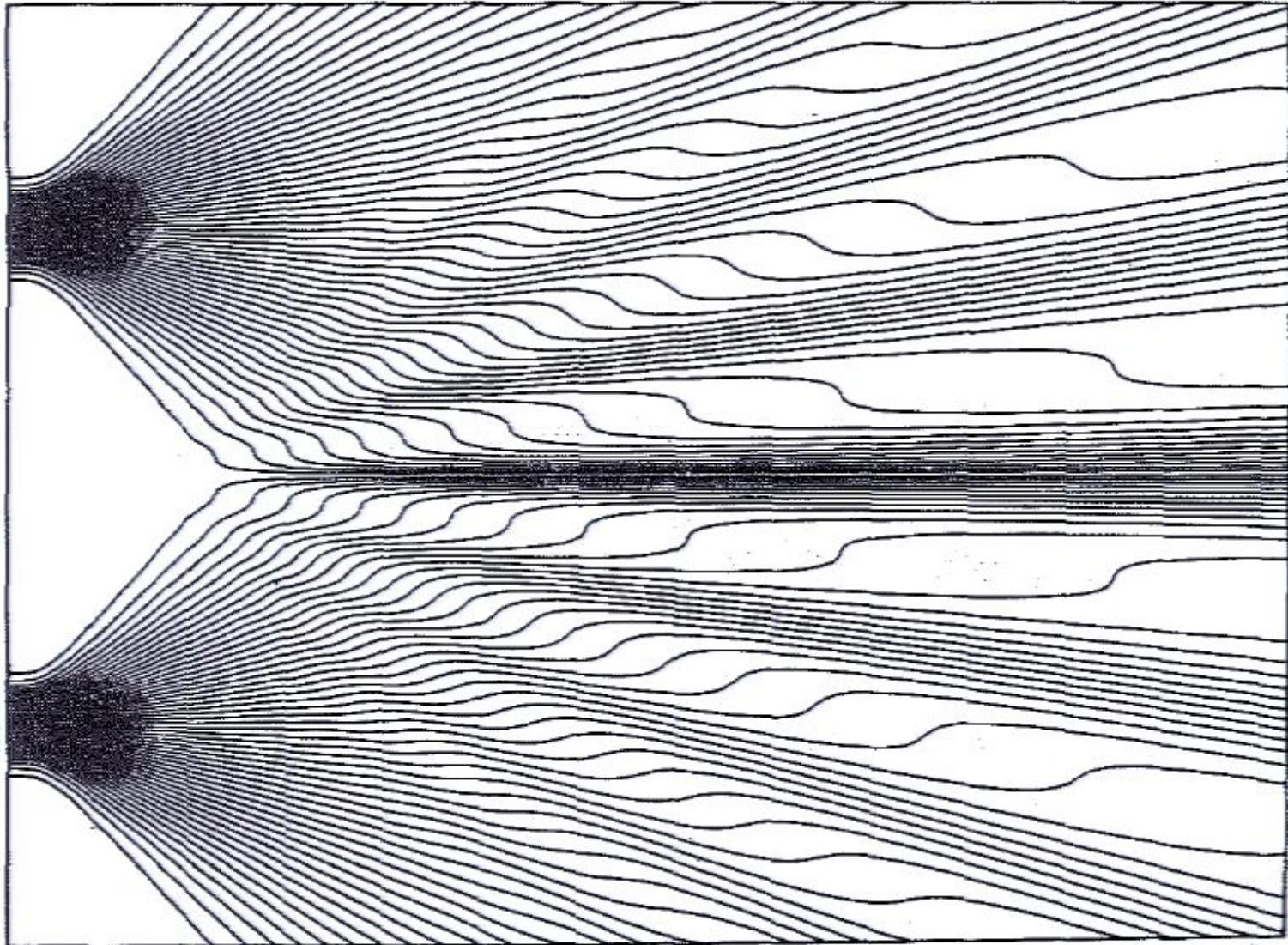




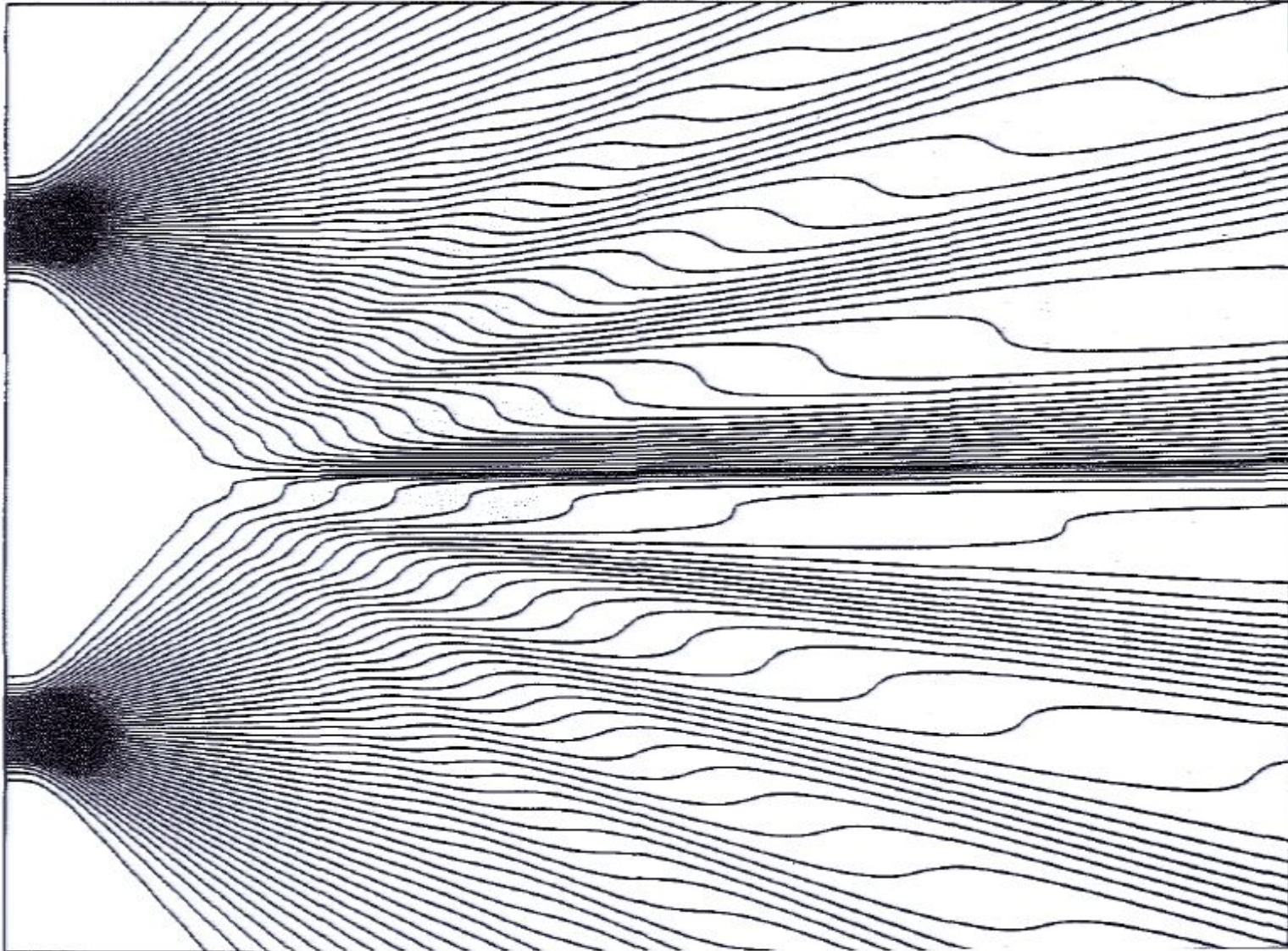
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With two degrees of freedom:

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