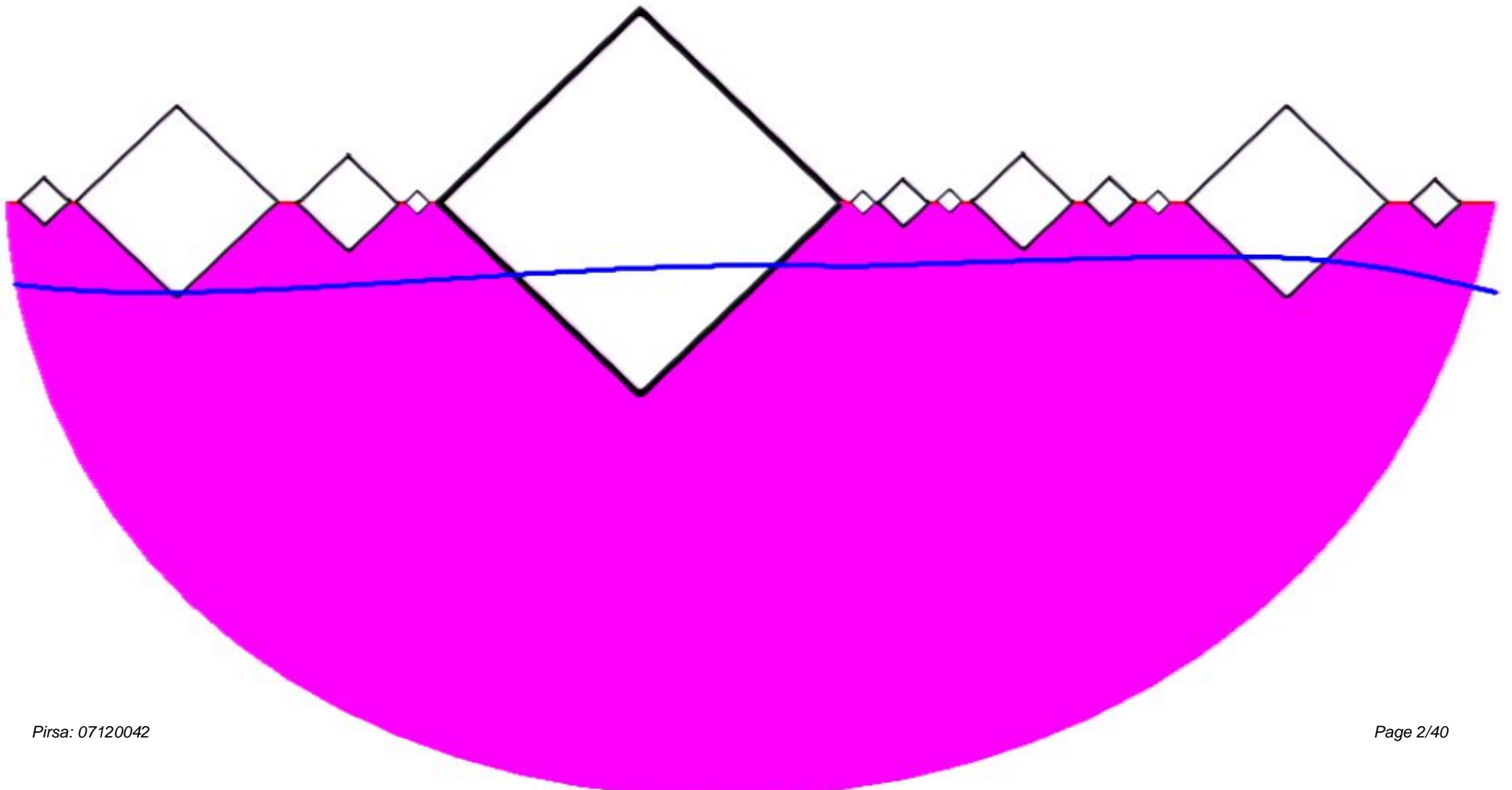


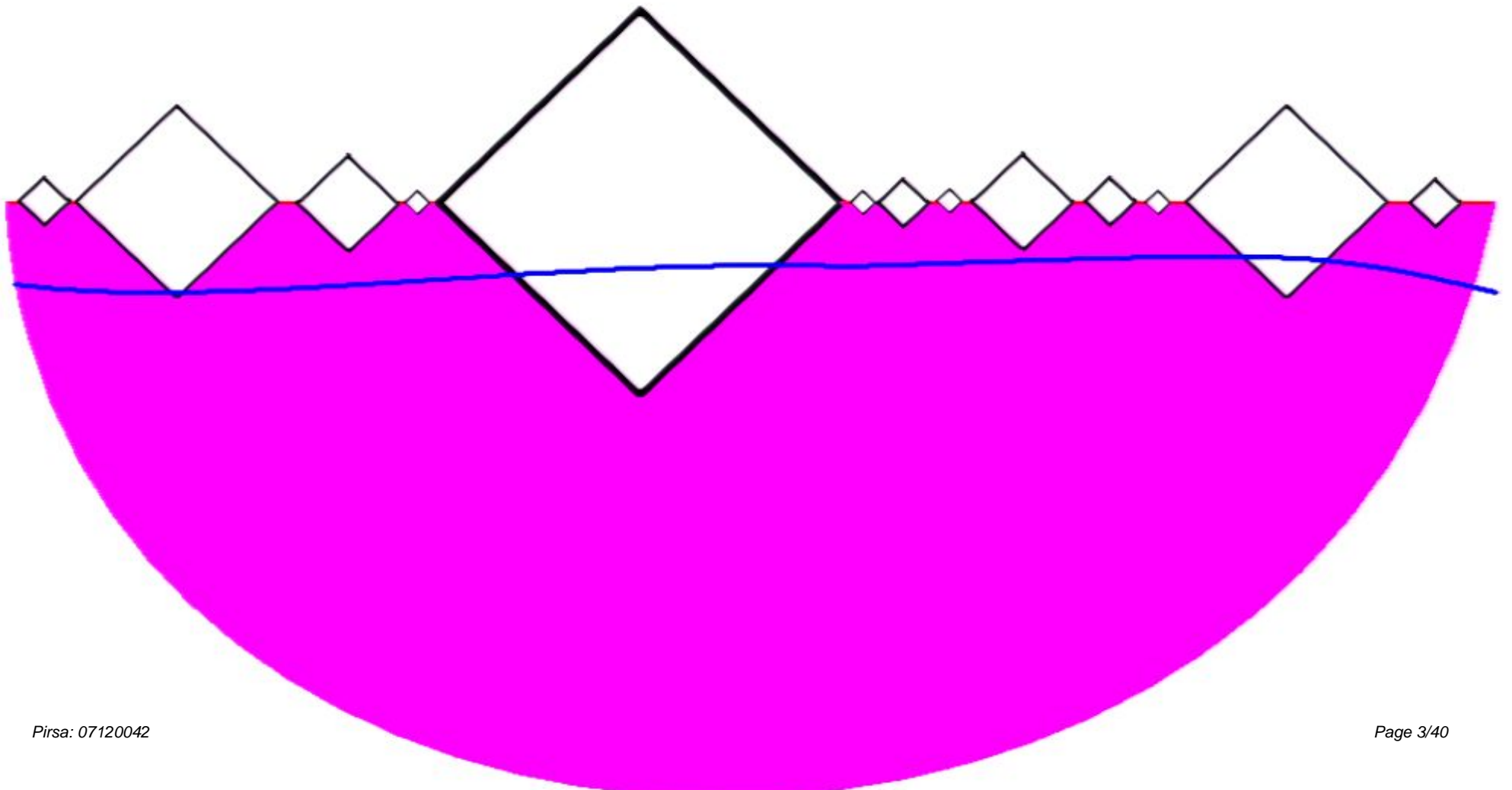
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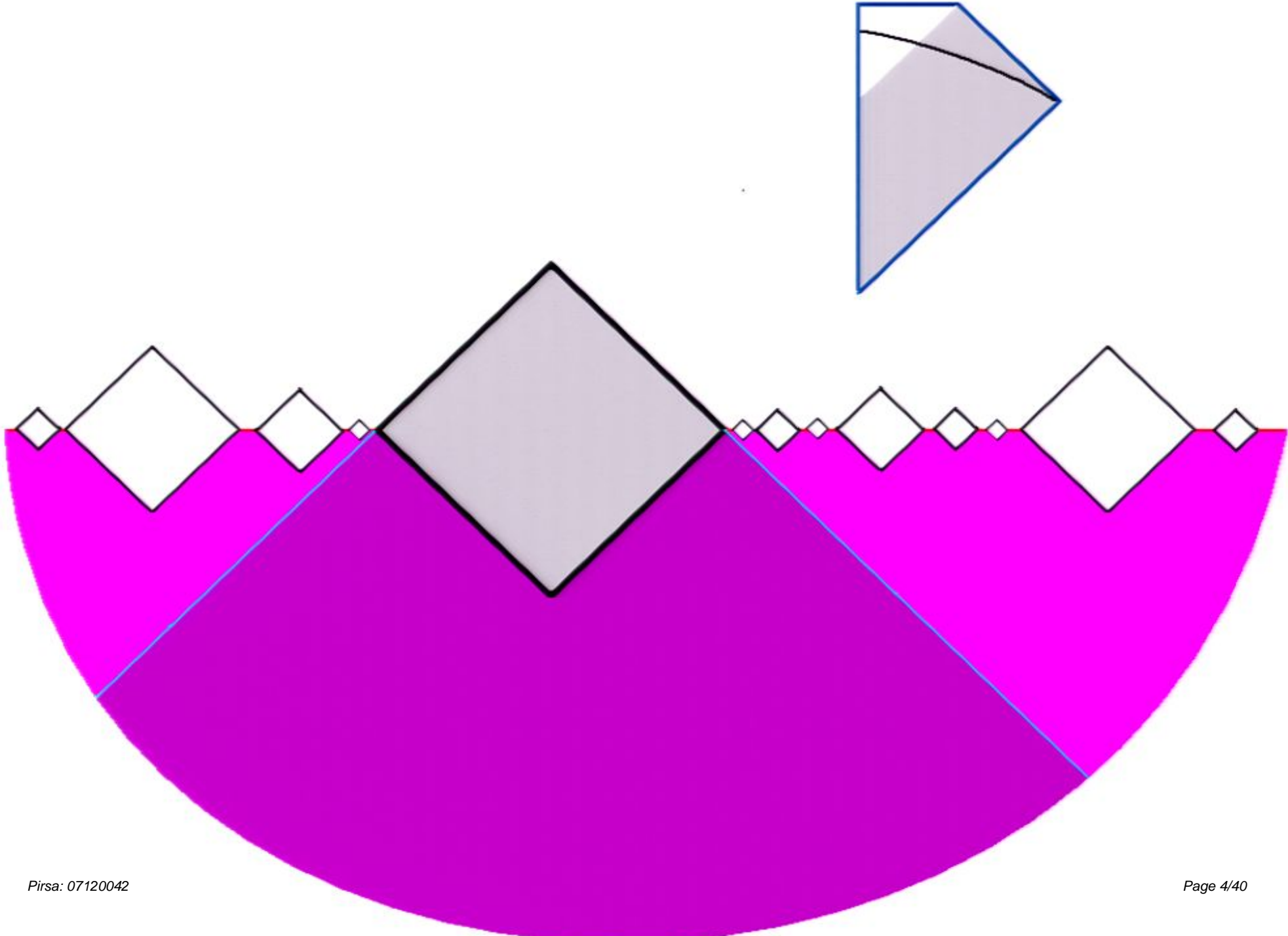
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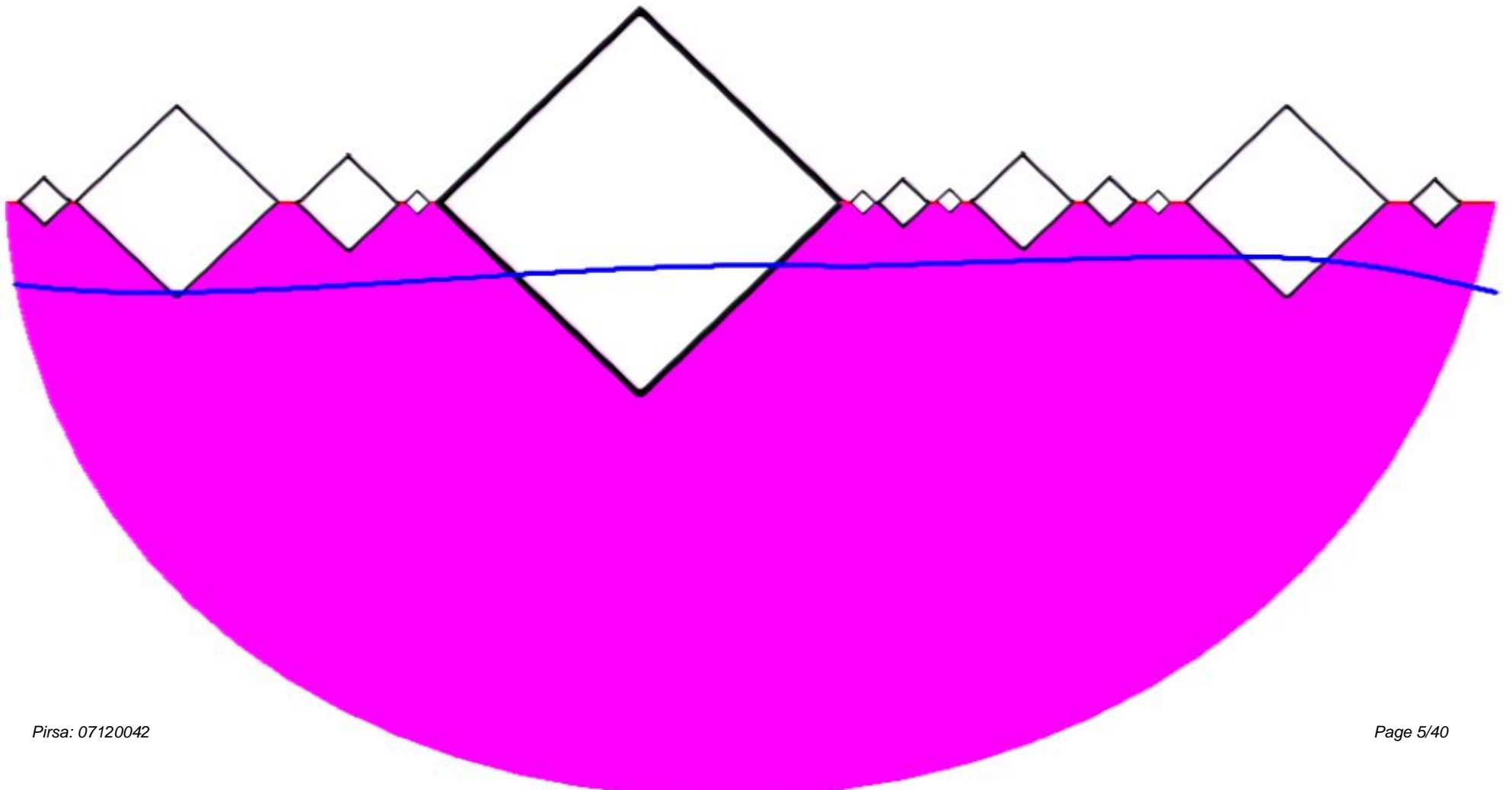
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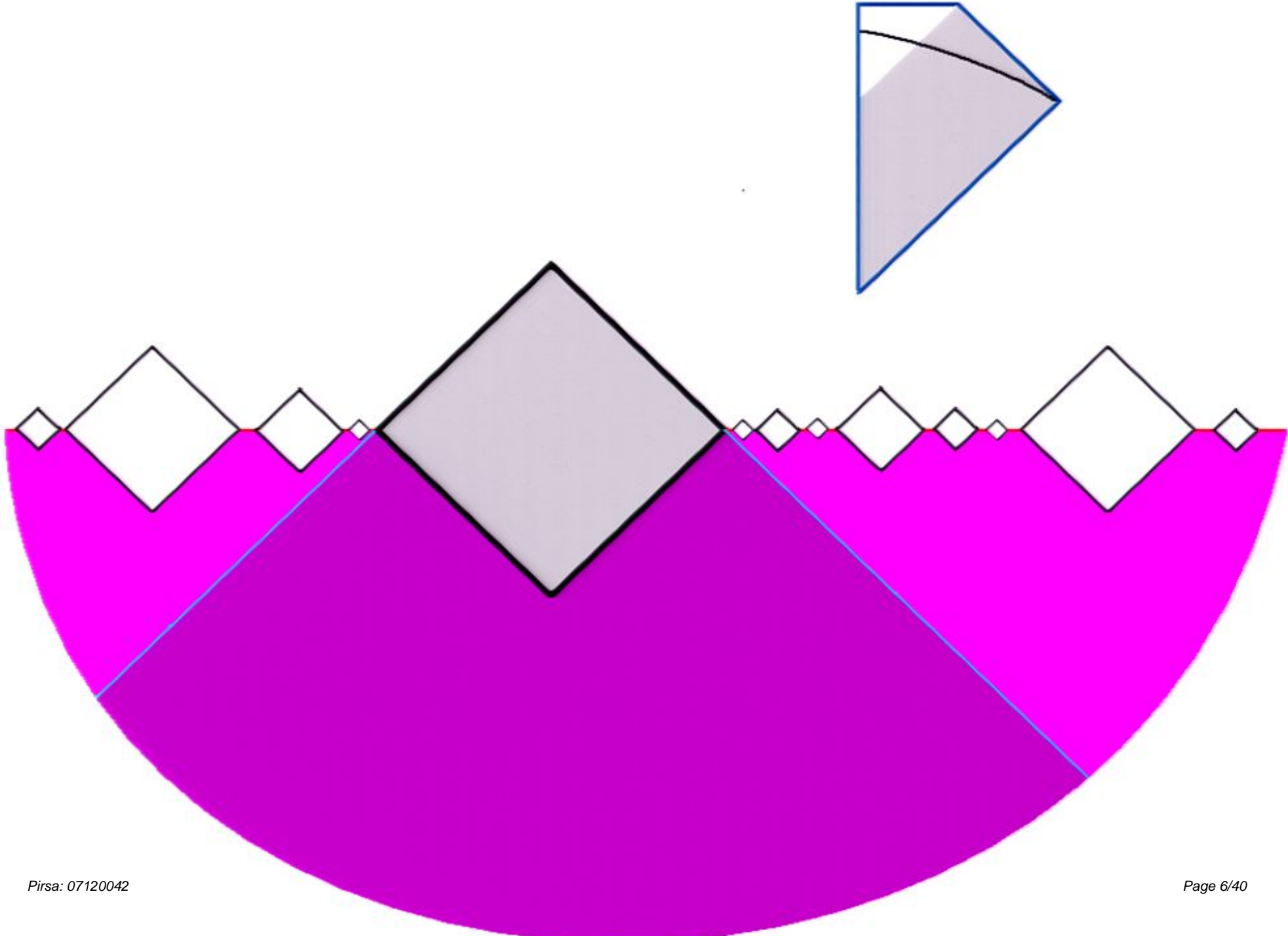
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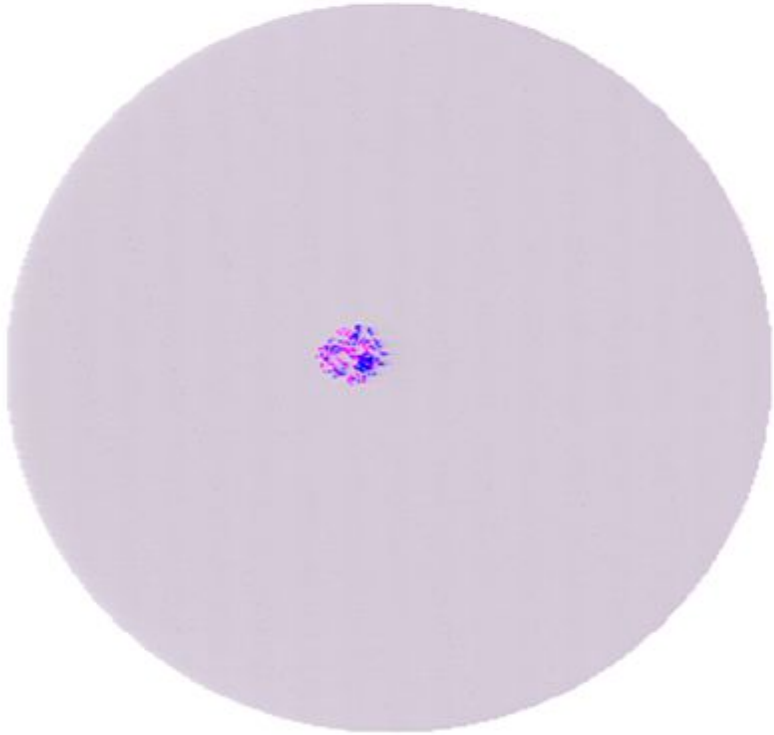




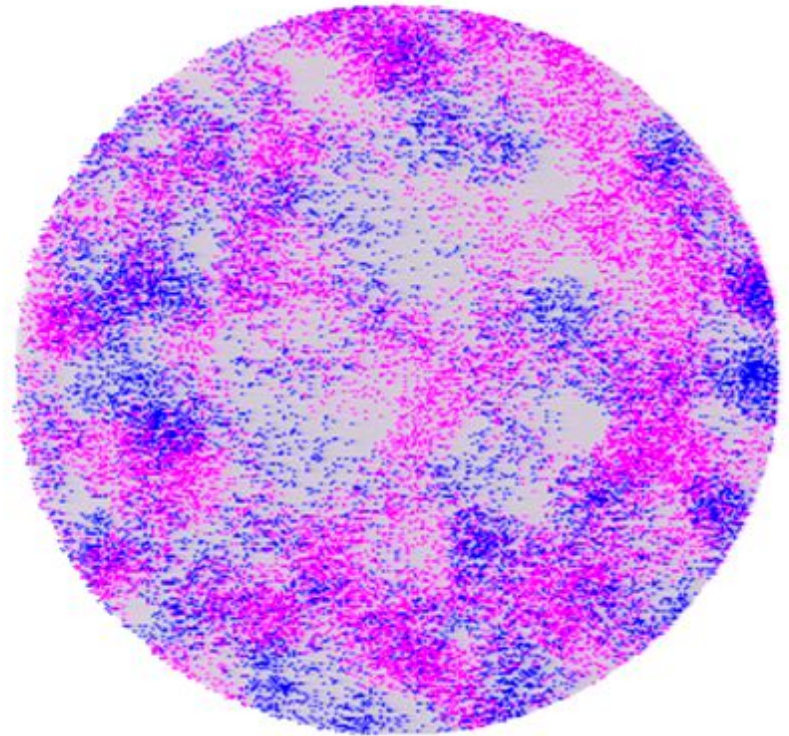






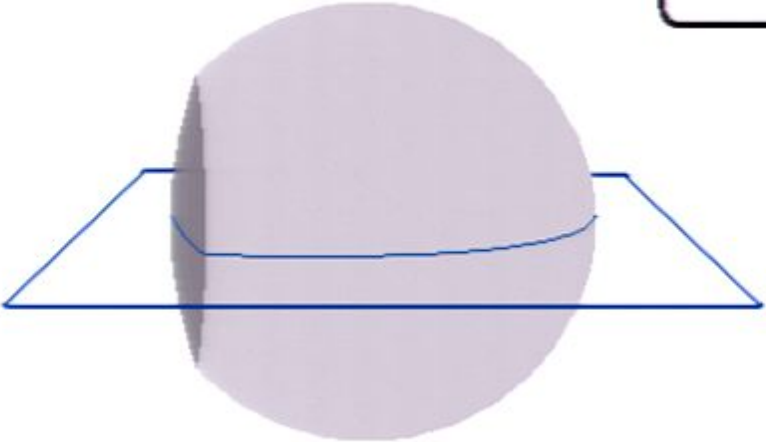


Asymptotically Cold
Flat, ADS

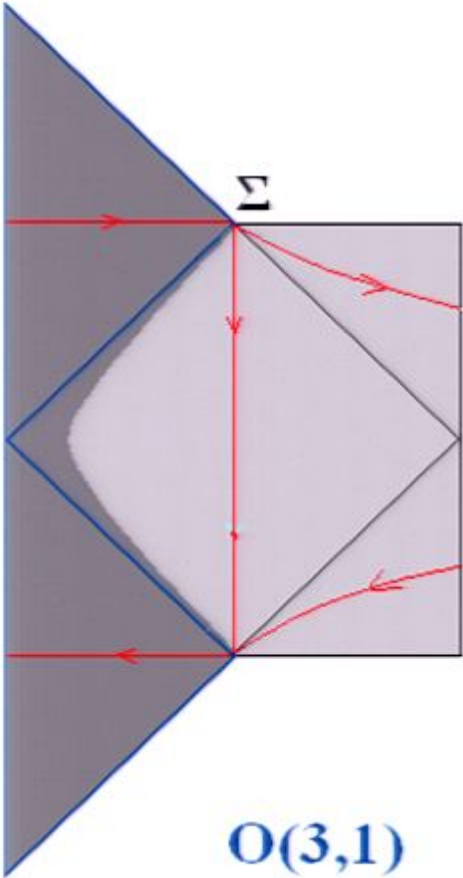


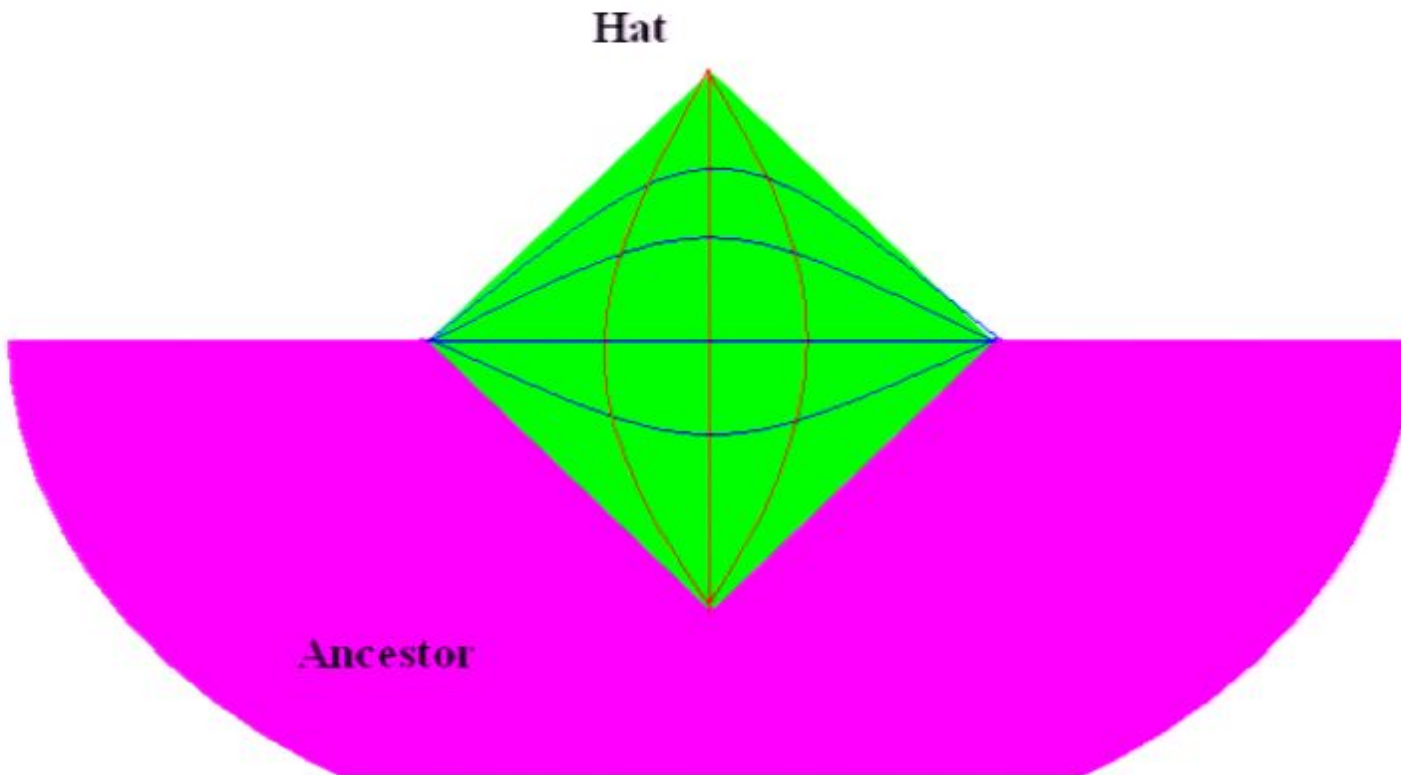
Asymptotically Warm
Open FRW

$$\Lambda_{\text{final}} = 0$$



O(4) symmetry





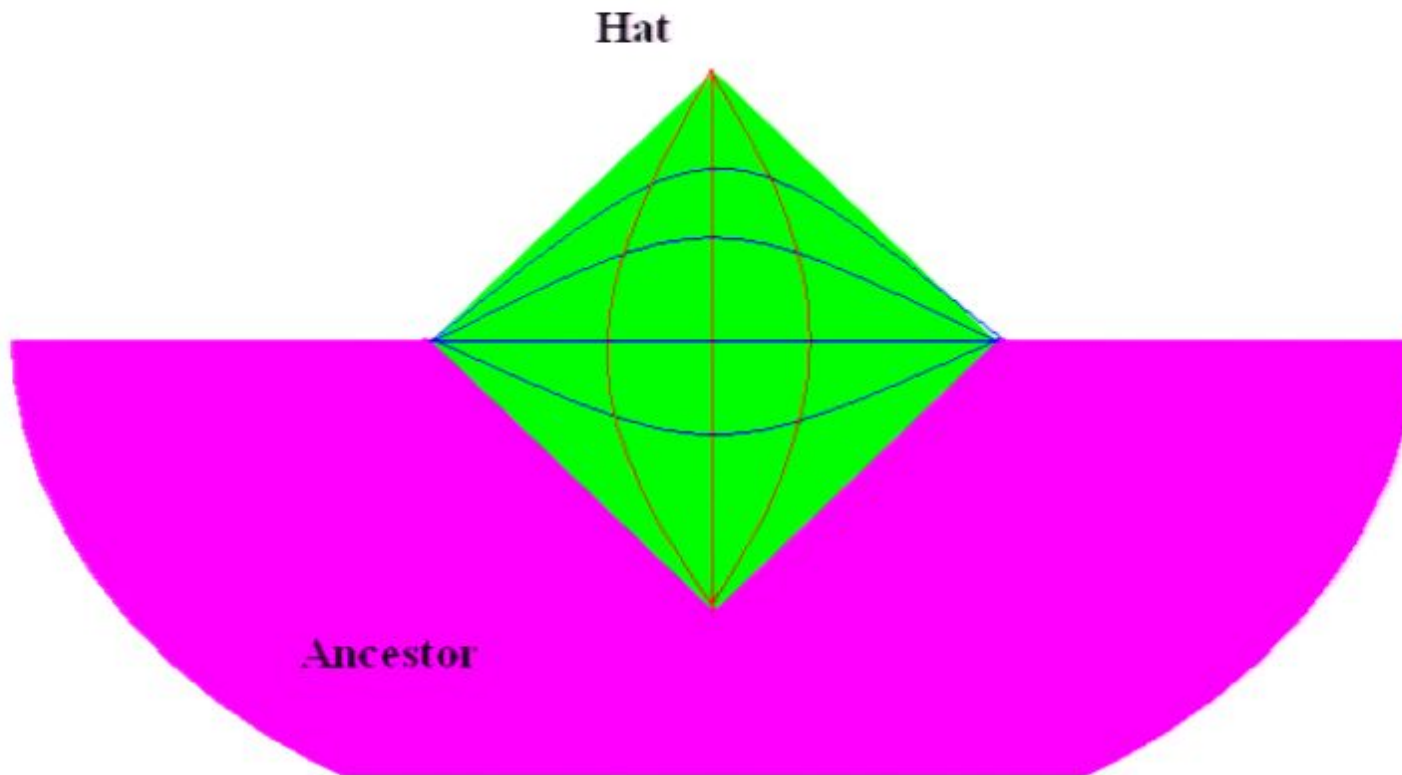
$$\begin{aligned}
 ds^2 &= - dt^2 + a(t)^2 \{ dR^2 + \sinh^2 R d\Omega_2^2 \} \\
 &= a(T)^2 \{ - dT^2 + dR^2 + \sinh^2 R d\Omega_2^2 \} \\
 &= a(T)^2 \{ - dT^+ dT^- + \sinh^2 R d\Omega_2^2 \}
 \end{aligned}$$

At early and late times the universe is curvature dominated.

$$a(t) \sim t$$

$$a(T) \sim \exp(T)$$

$$ds^2 \rightarrow - e^{2T} dT^+ dT^- + e^{2T^+} d\Omega_2^2$$



$$\begin{aligned}
 ds^2 &= - dt^2 + a(t)^2 \{dR^2 + \sinh^2 R \, d\Omega_2^2\} \\
 &= a(T)^2 \{- dT^2 + dR^2 + \sinh^2 R \, d\Omega_2^2\} \\
 &= a(T)^2 \{- dT^+ dT^- + \sinh^2 R \, d\Omega_2^2\}
 \end{aligned}$$

At early and late times the universe is curvature dominated.

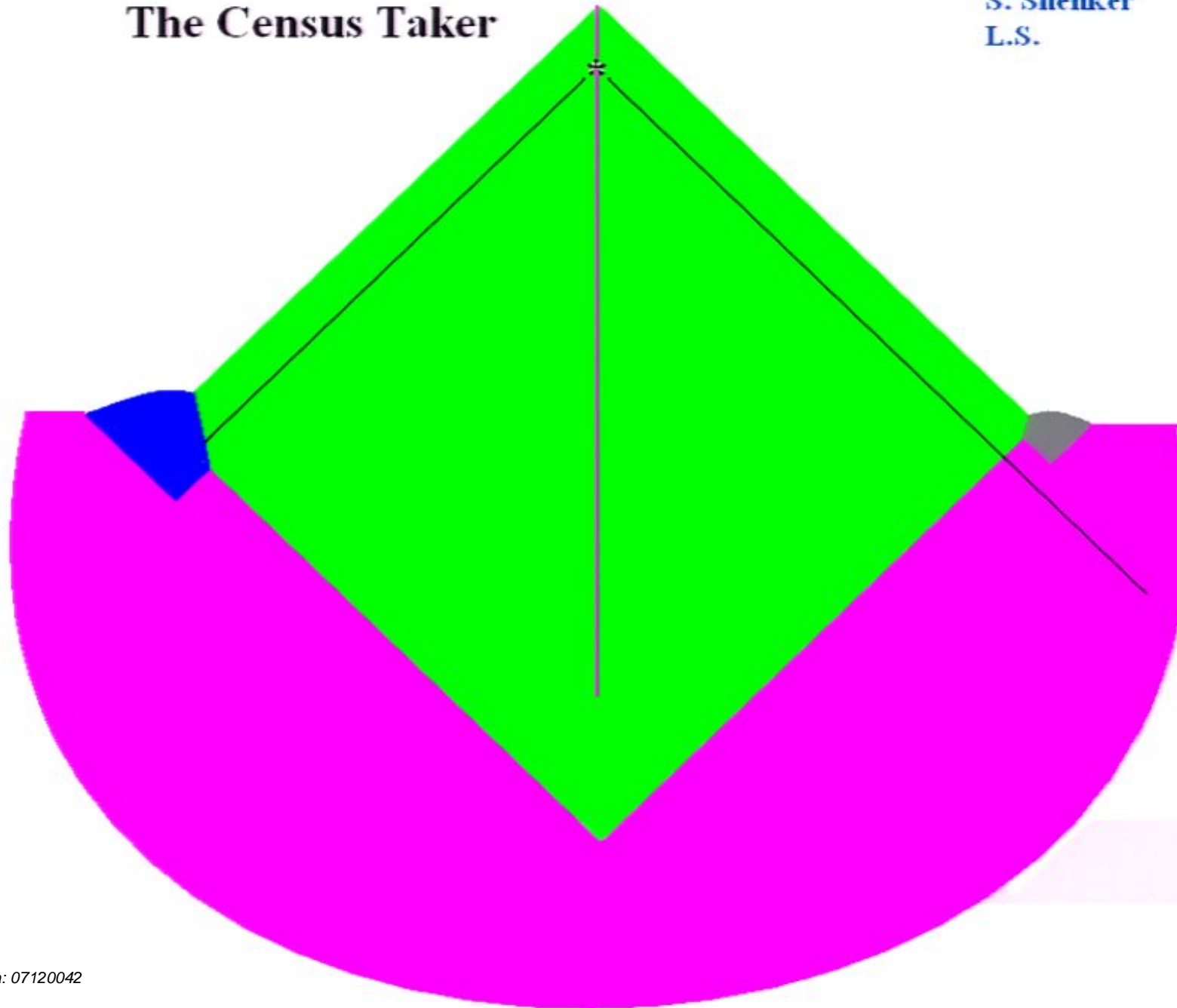
$$a(t) \sim t$$

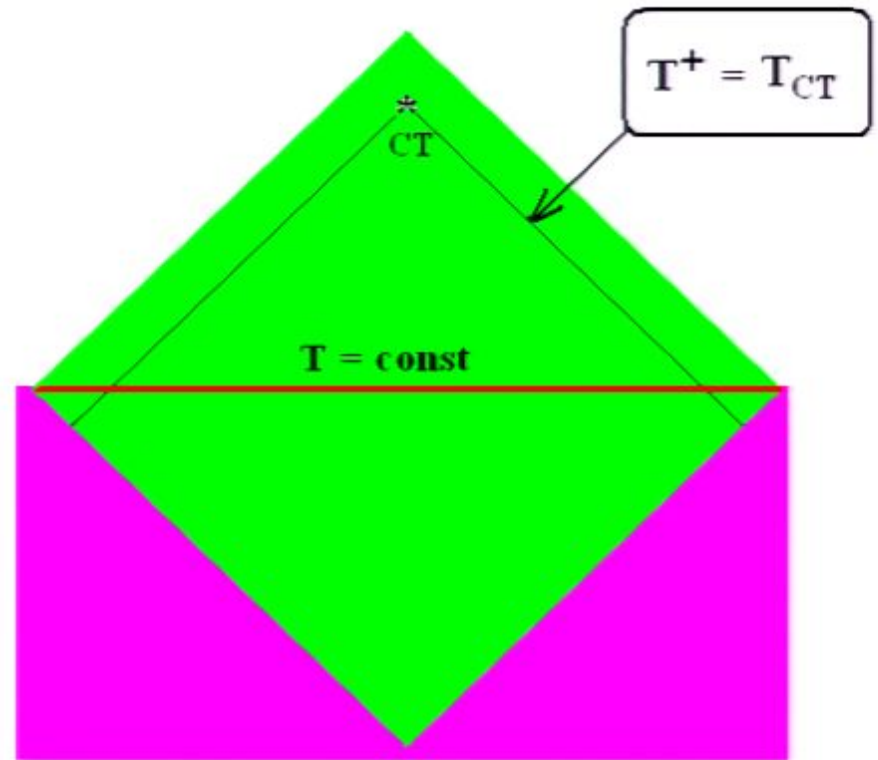
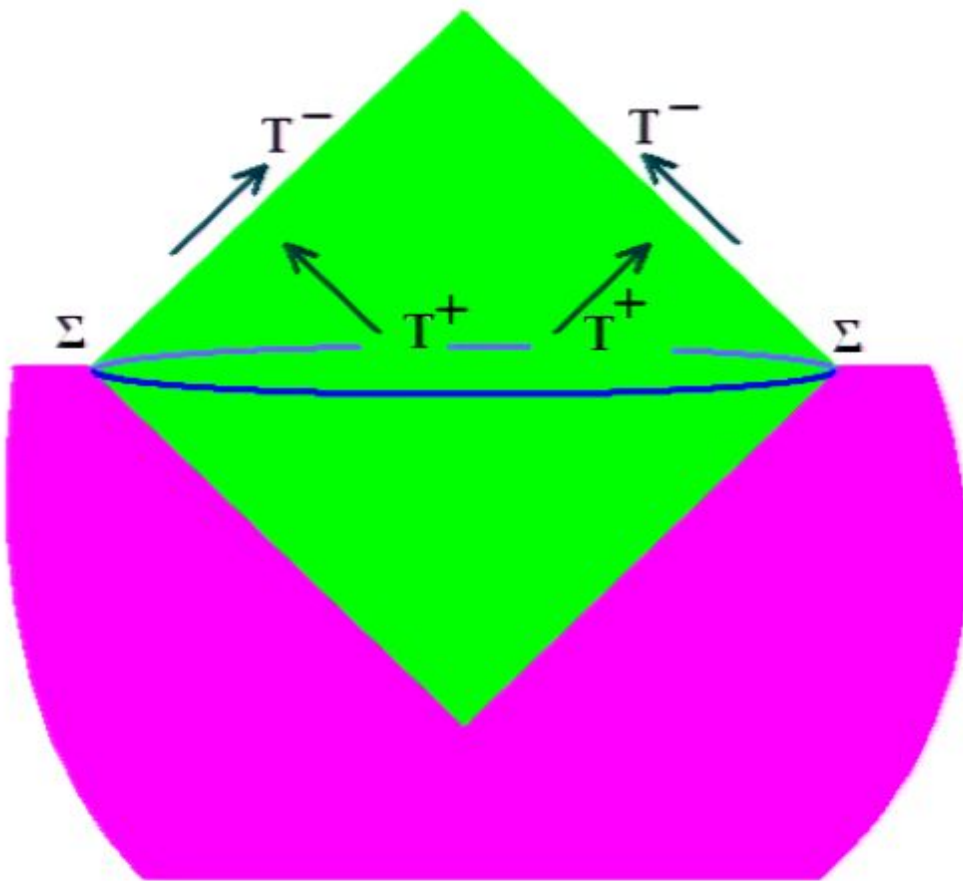
$$a(T) \sim \exp(T)$$

$$ds^2 \rightarrow - e^{2T} dT^+ dT^- + e^{2T^+} d\Omega_2^2$$

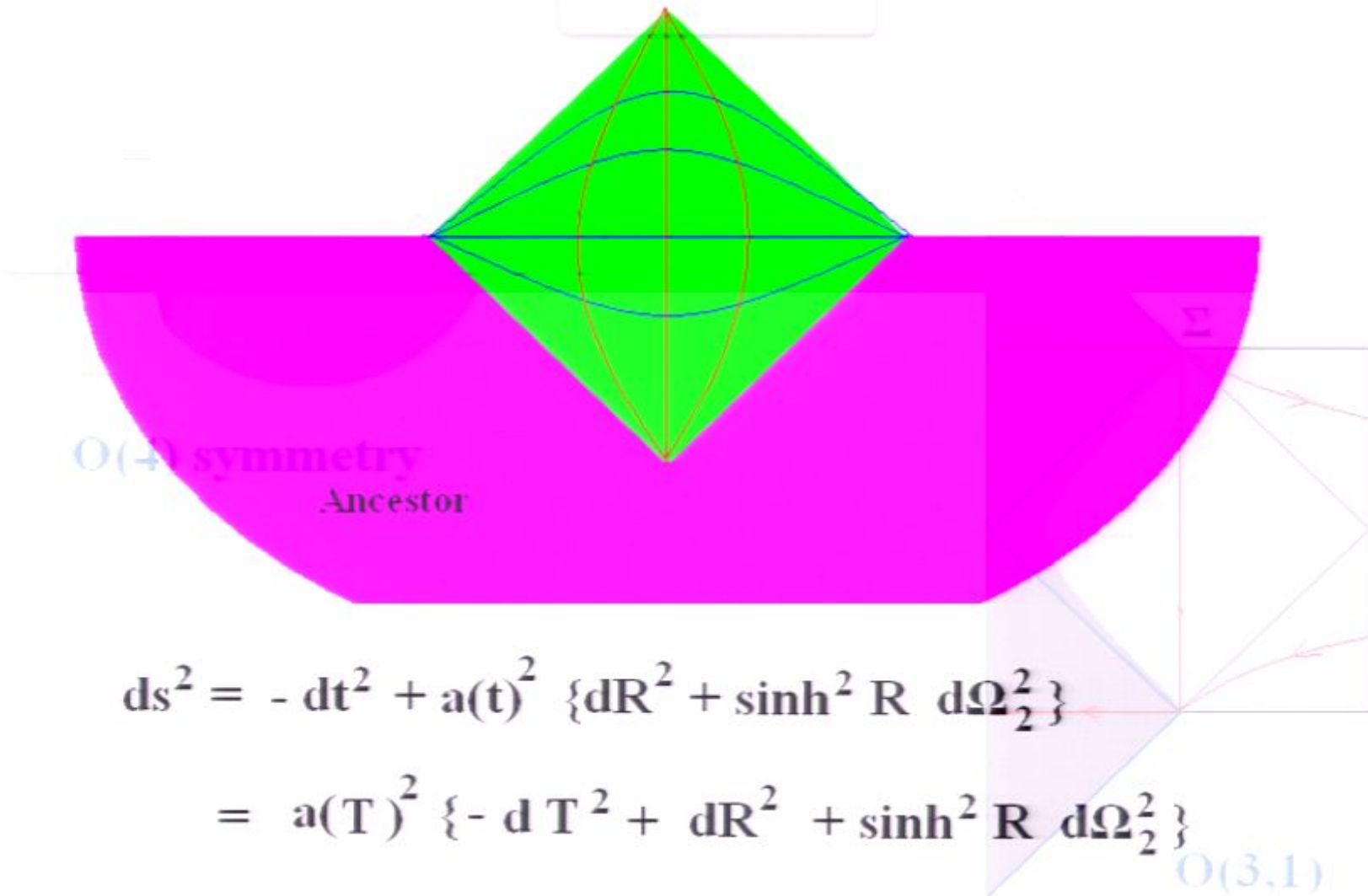
The Census Taker

A. Maloney
S. Shenker
L.S.



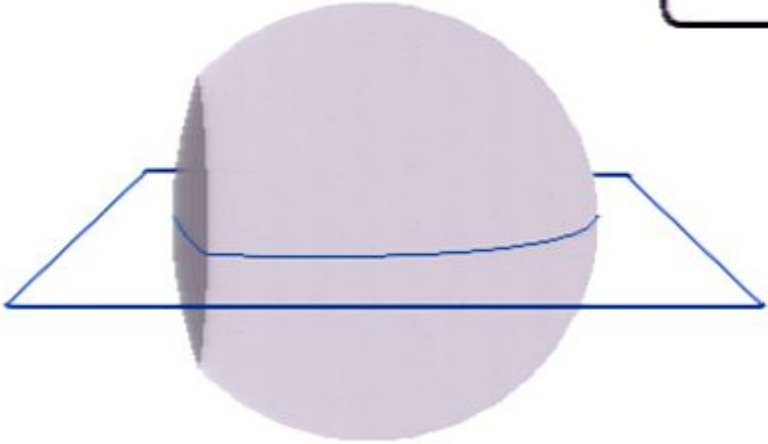


Hat $\equiv \parallel$

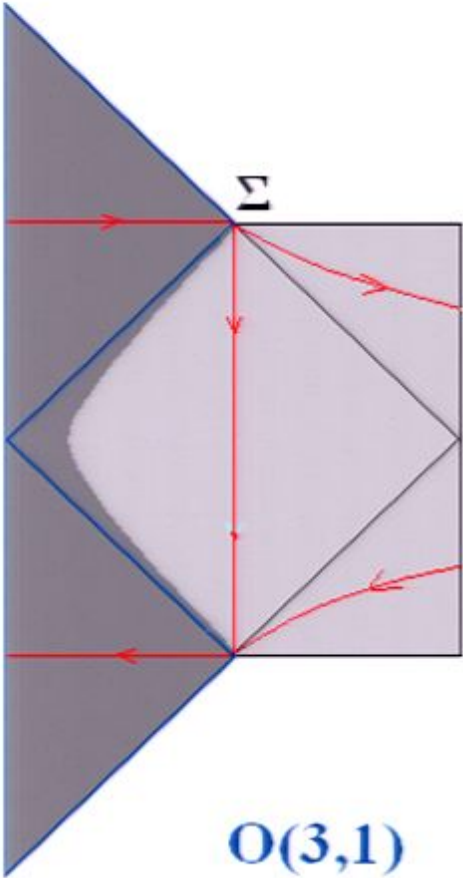


$$\begin{aligned}
 ds^2 &= - dt^2 + a(t)^2 \{ dR^2 + \sinh^2 R \, d\Omega_2^2 \} \\
 &= a(T)^2 \{ - dT^2 + dR^2 + \sinh^2 R \, d\Omega_2^2 \} \\
 &= a(T)^2 \{ - dT^+ dT^- + \sinh^2 R \, d\Omega_2^2 \}
 \end{aligned}$$

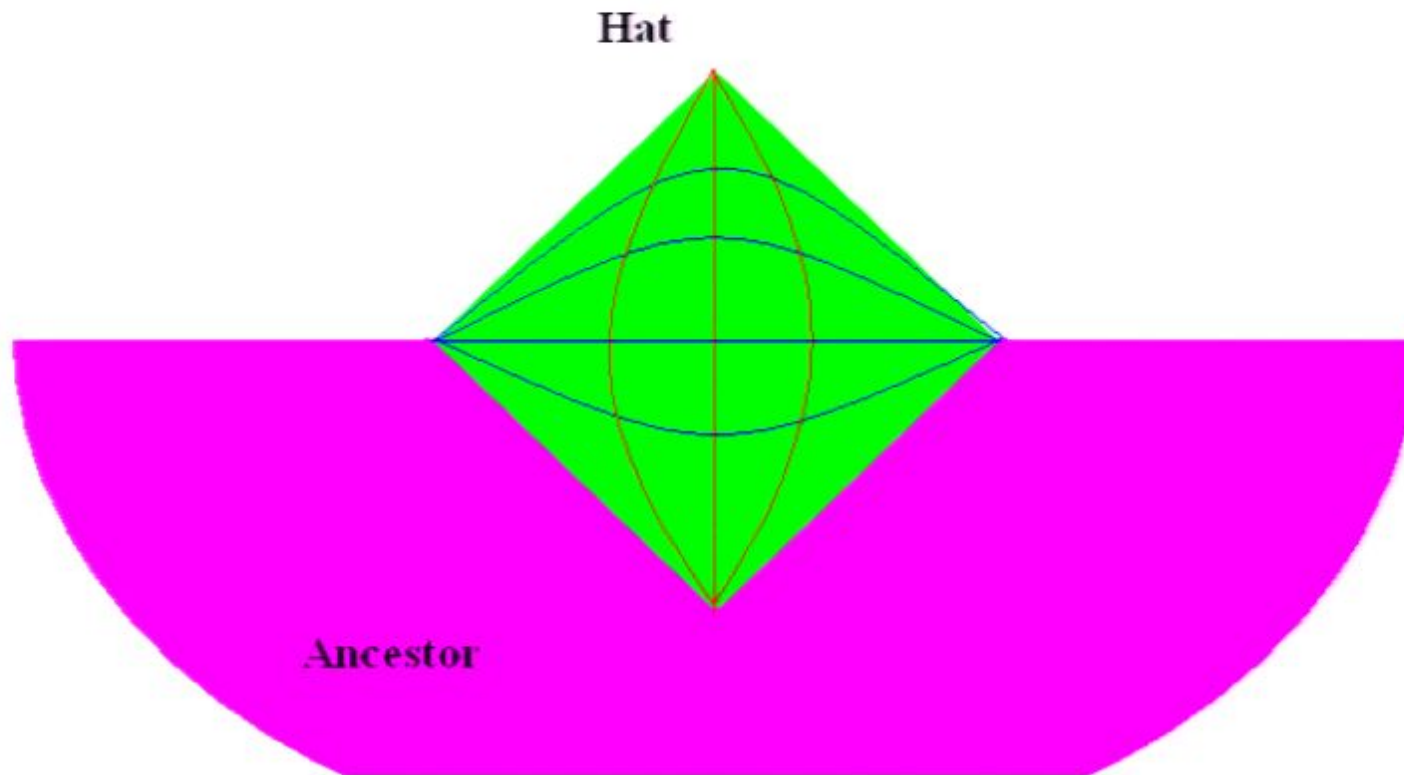
$$\Lambda_{\text{final}} = 0$$



O(4) symmetry



O(3,1)



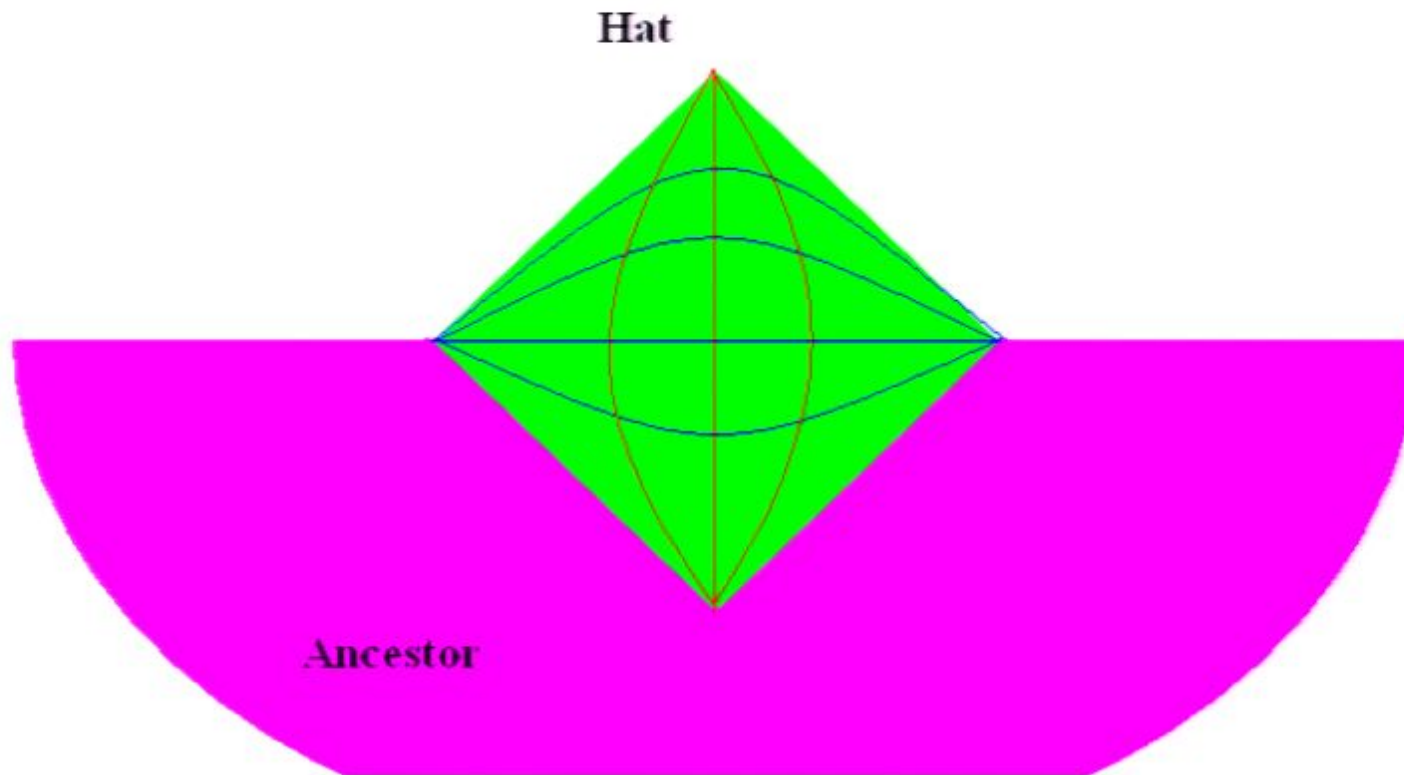
$$\begin{aligned}
 ds^2 &= - dt^2 + a(t)^2 \{ dR^2 + \sinh^2 R d\Omega_2^2 \} \\
 &= a(T)^2 \{ - dT^2 + dR^2 + \sinh^2 R d\Omega_2^2 \} \\
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$$\begin{aligned}
 ds^2 &= - dt^2 + a(t)^2 \{dR^2 + \sinh^2 R \, d\Omega_2^2\} \\
 &= a(T)^2 \{- d T^2 + dR^2 + \sinh^2 R \, d\Omega_2^2\} \\
 &= a(T)^2 \{- d T^+ d T^- + \sinh^2 R \, d\Omega_2^2\}
 \end{aligned}$$

At early and late times the universe is curvature dominated.

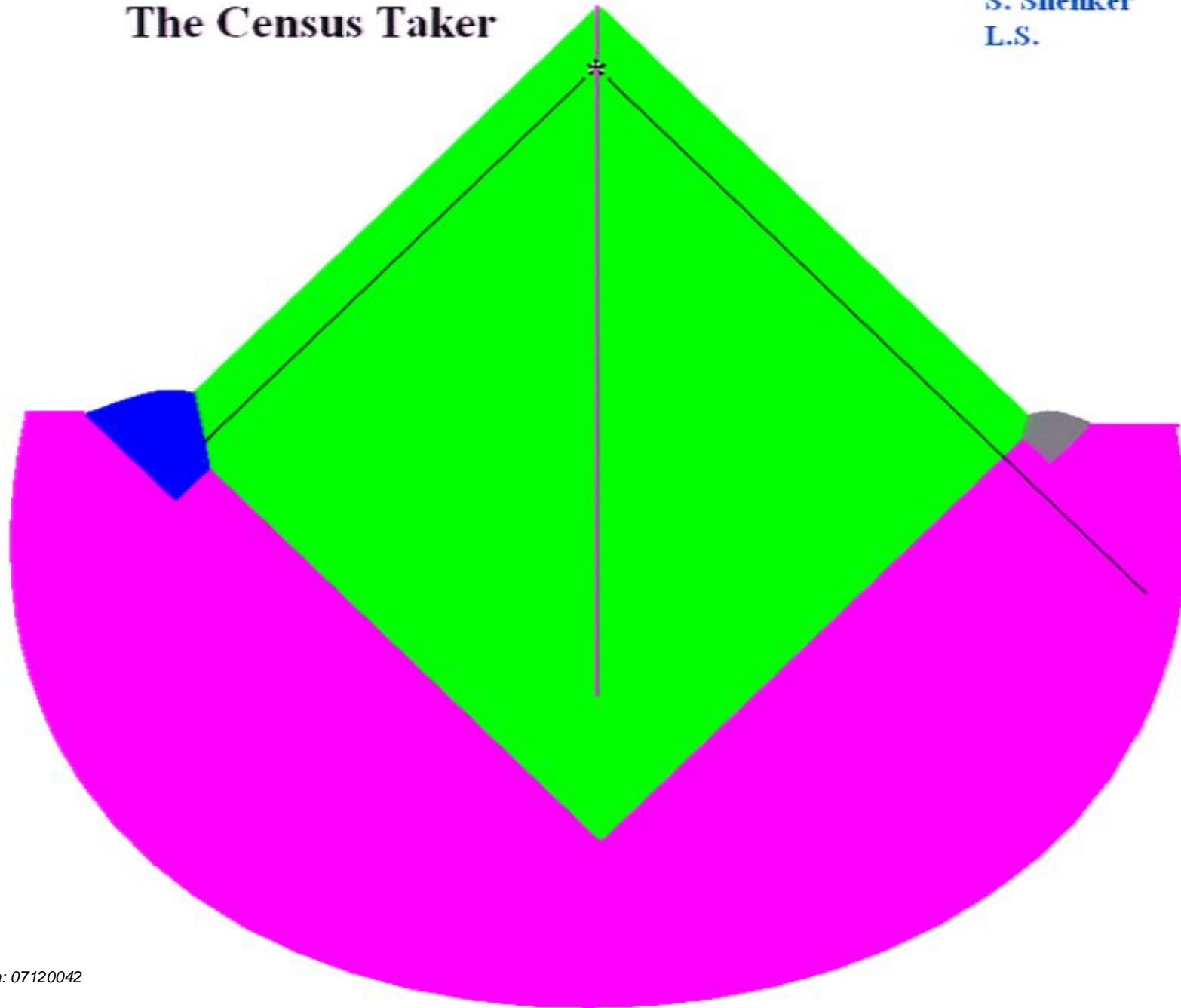
$$a(t) \sim t$$

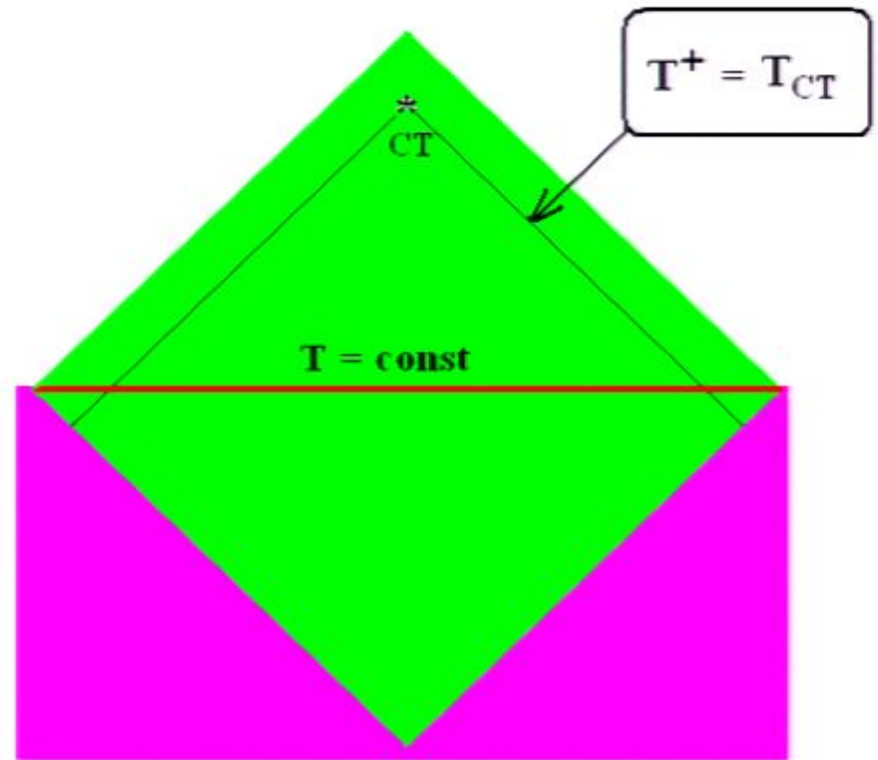
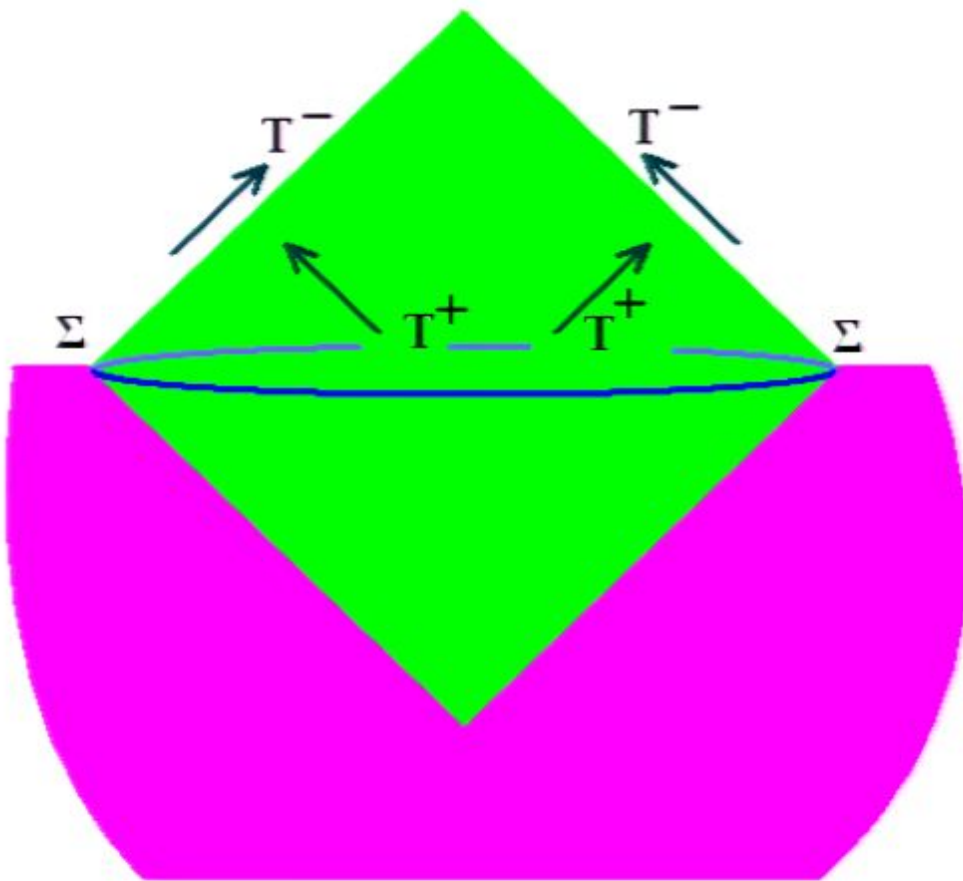
$$a(T) \sim \exp(T)$$

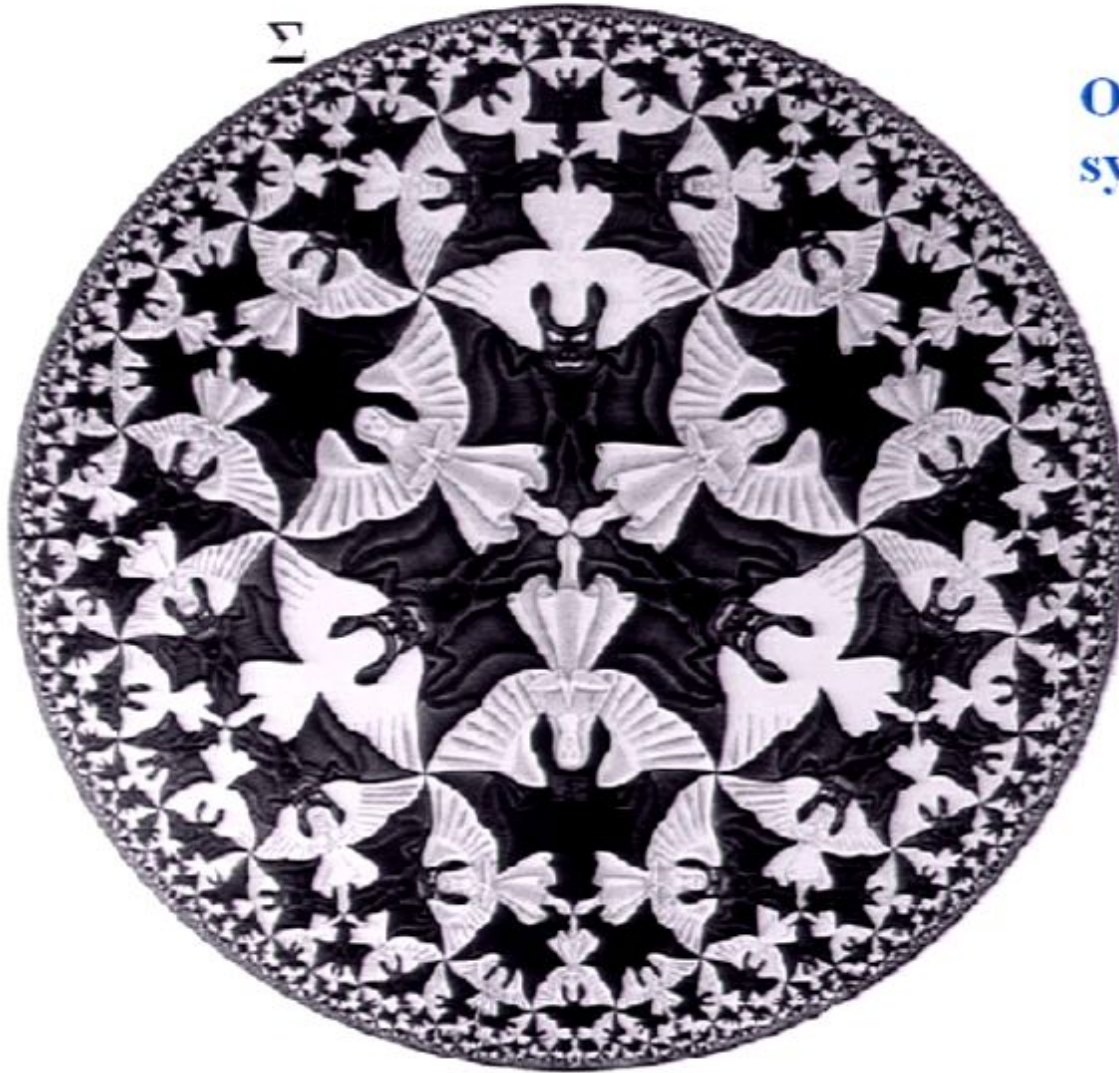
$$ds^2 \rightarrow - e^{2T} dT^+ dT^- + e^{2T^+} d\Omega_2^2$$

The Census Taker

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S. Shenker
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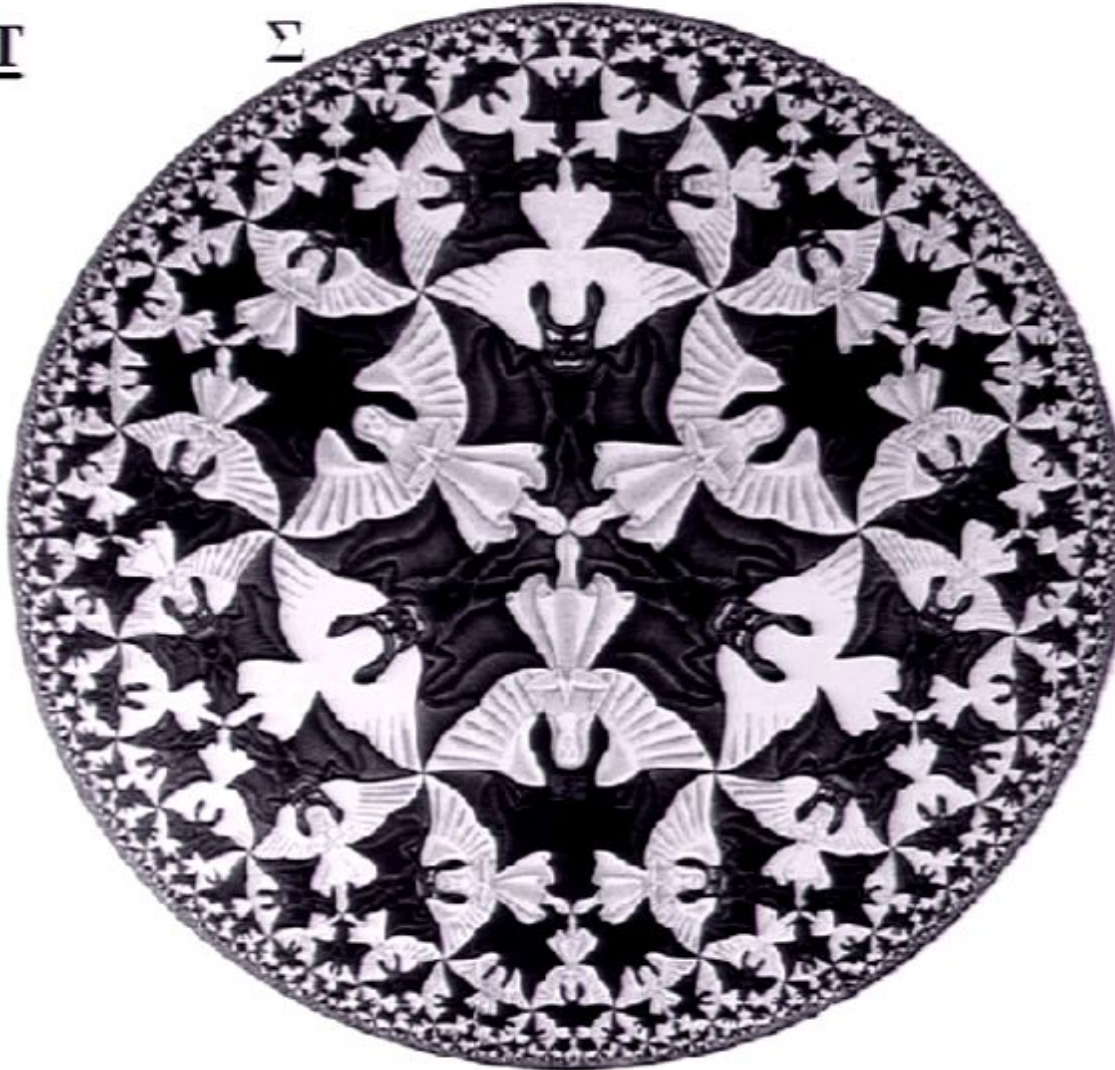




$O(3,1)$
symmetry

ADS/CFT

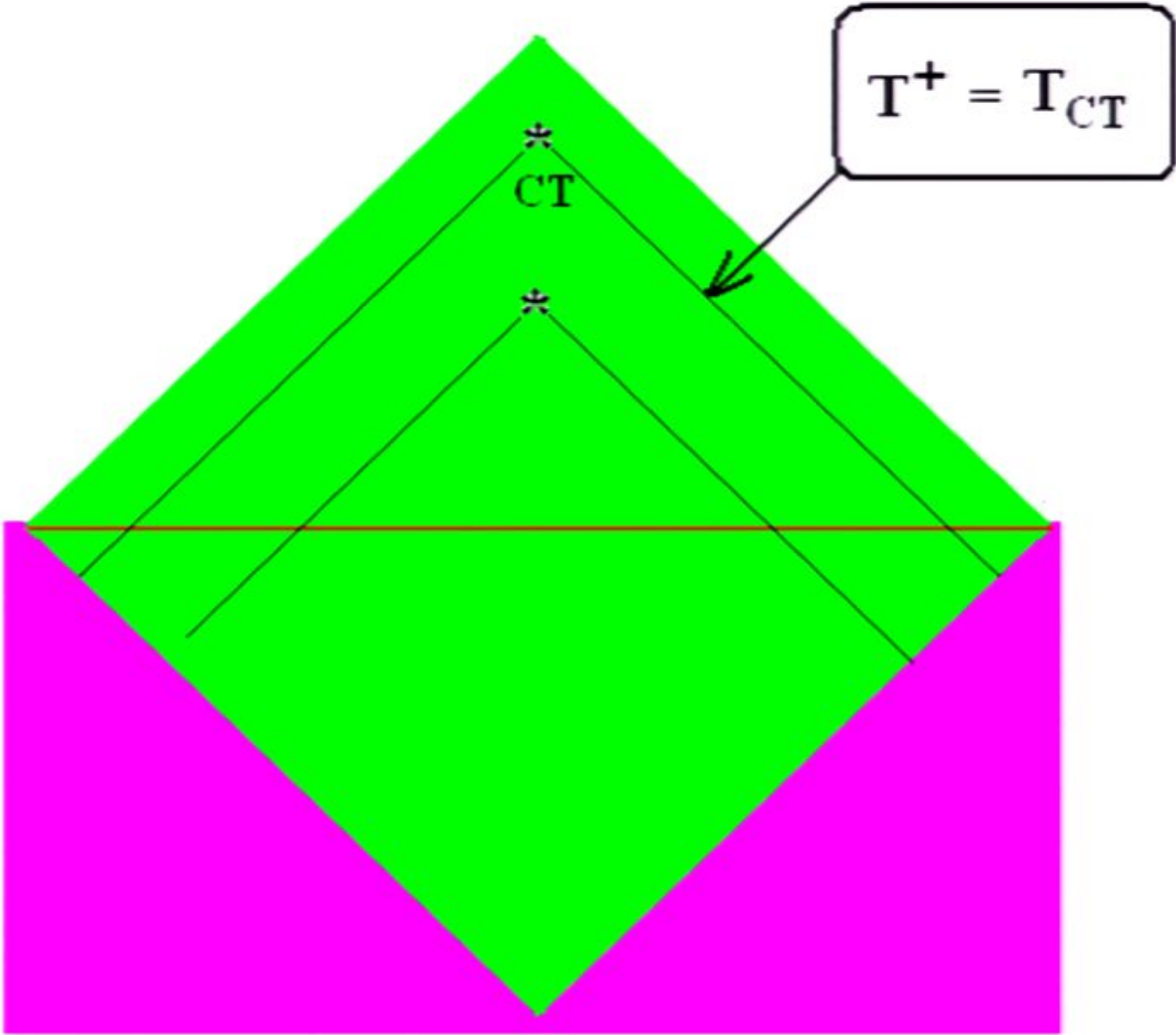
Σ

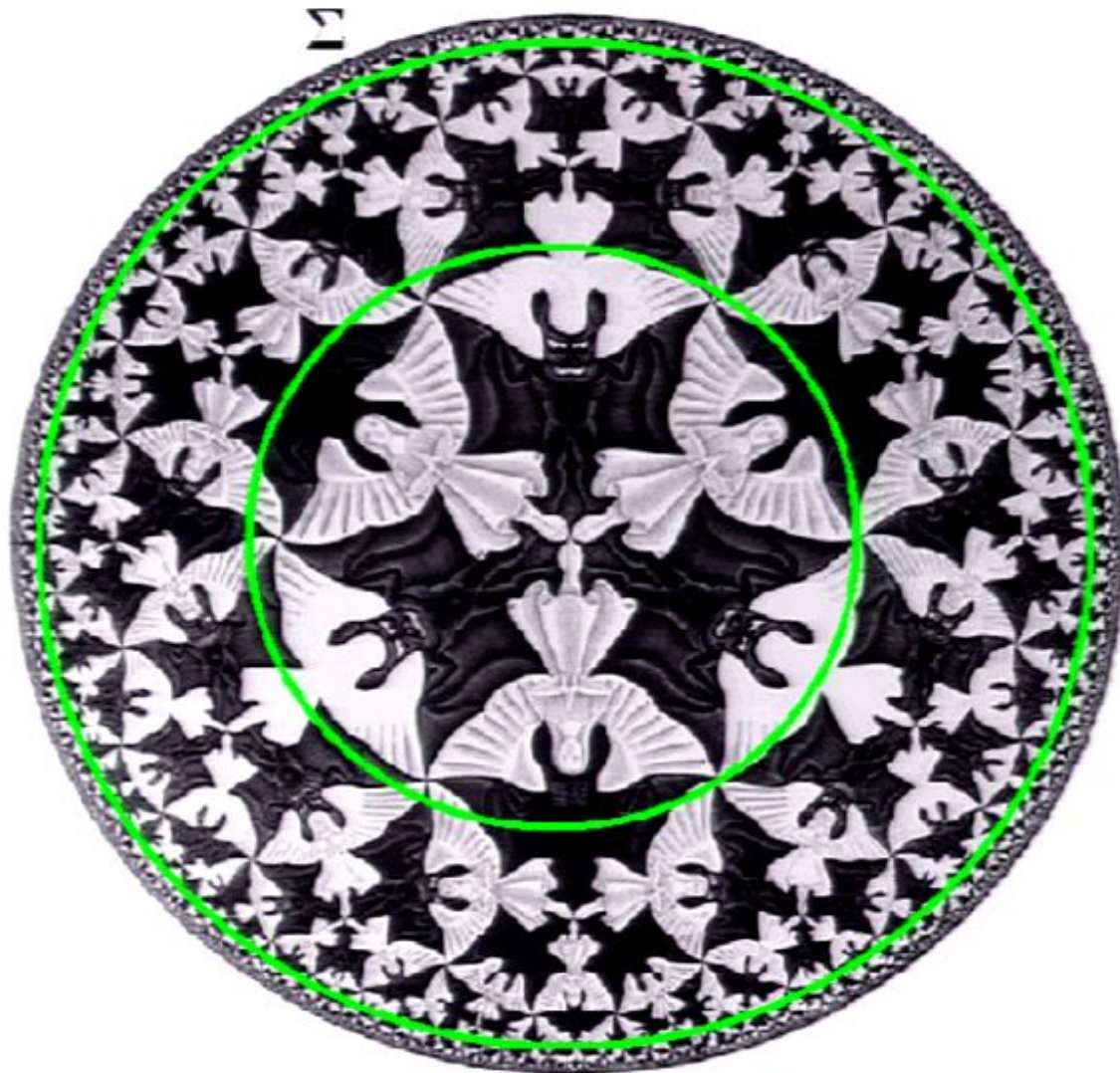


The radial
direction =
RG flow.

$$R = \log \kappa$$

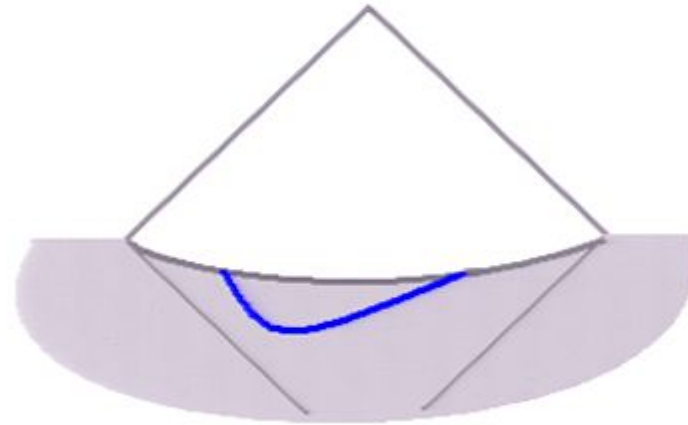
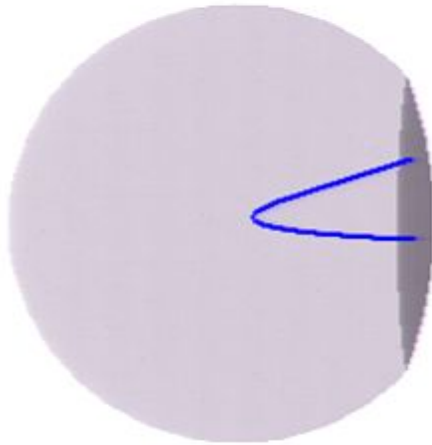
$$\langle \Phi_{\Delta} \Phi_{\Delta} \rangle = \kappa^{-\Delta} \kappa^{-\Delta} (1 - \cos \alpha)^{-\Delta}$$





Open FRW

Census
taker time
defines an
RG flow.



Correlations on Σ are covariant under $O(3,1)$.
This means CONFORMAL symmetry.

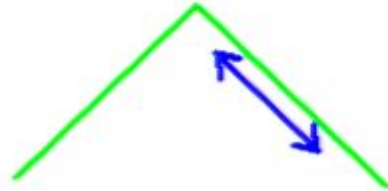
**Is there a dual Euclidean 2D CFT
on Σ ?**

Ben Freivogel
Yasuhiro Sekino
L.S
Chen Pin Yeh

FSSY: Tensor and scalar

RG covariant Proactive

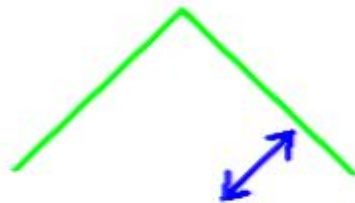
$$\mathbf{G}_1 = e^{-(\mathbf{T}_1^+ + \mathbf{T}_2^+)} \sum_{\Delta=2} \mathbf{G}_\Delta e^{(\Delta-1)(\mathbf{T}_1^- + \mathbf{T}_2^-)} (1 - \cos \alpha)^{-\Delta}$$



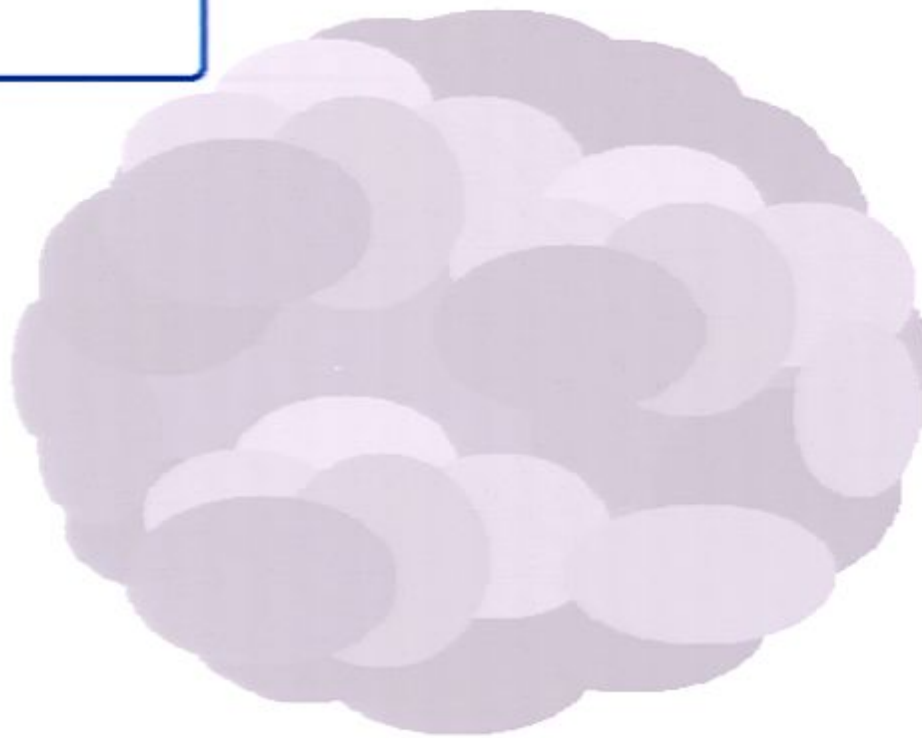
$\Delta = 2$ term is exactly T_{ij}

RG invariant Reactive

$$\mathbf{G}_2 = \mathbf{T}_1^+ + \mathbf{T}_2^+ + \log(1 - \cos \alpha) \quad \text{Liouville}$$
$$+ \sum_{\Delta} \mathbf{G}_\Delta e^{-\Delta(\mathbf{T}_1^+ + \mathbf{T}_2^+)} (1 - \cos \alpha)^{-\Delta}$$



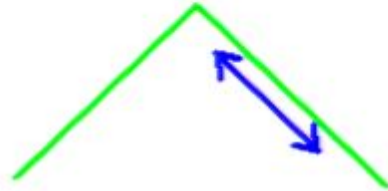
**Gravitational
fluctuations do not
go to zero at
space-like
infinity.**



FSSY: Tensor and scalar

RG covariant Proactive

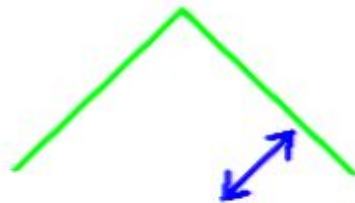
$$\mathbf{G}_1 = e^{-(\mathbf{T}_1^+ + \mathbf{T}_2^+)} \sum_{\Delta=2} \mathbf{G}_\Delta e^{(\Delta-1)(\mathbf{T}_1^- + \mathbf{T}_2^-)} (1 - \cos \alpha)^{-\Delta}$$



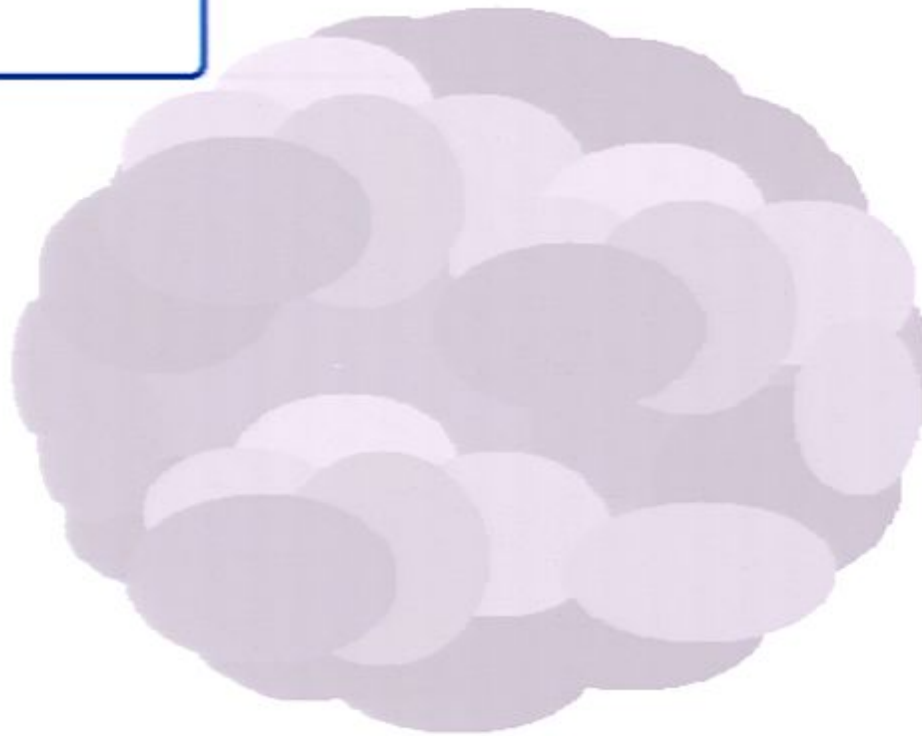
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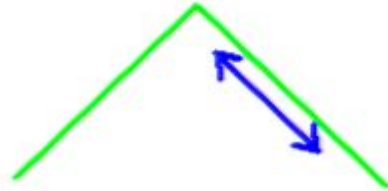
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FSSY: Tensor and scalar

RG covariant Proactive

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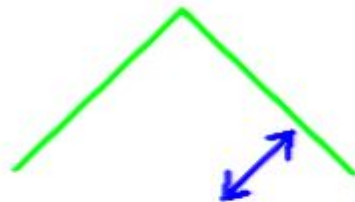


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**Gravitational
fluctuations do not
go to zero at
space-like
infinity.**





$$ds^2 = a(T)^2 \sinh^2 R \, d\Omega_2^2$$

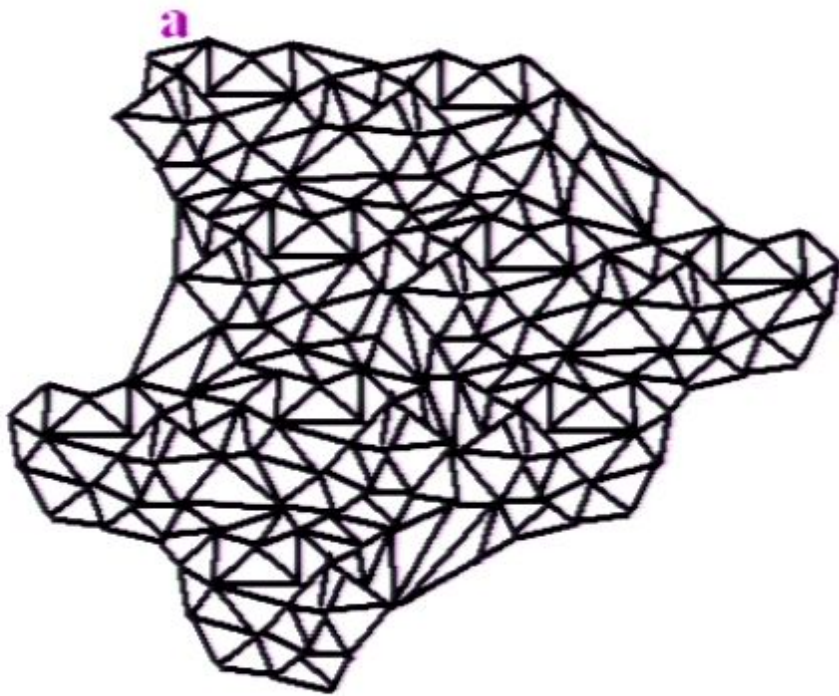
$$\approx a(T)^2 \{e^{2R} d\Omega_2^2\} \leftarrow \text{reference metric}$$

$$T \longrightarrow T + f(\Omega_2)$$

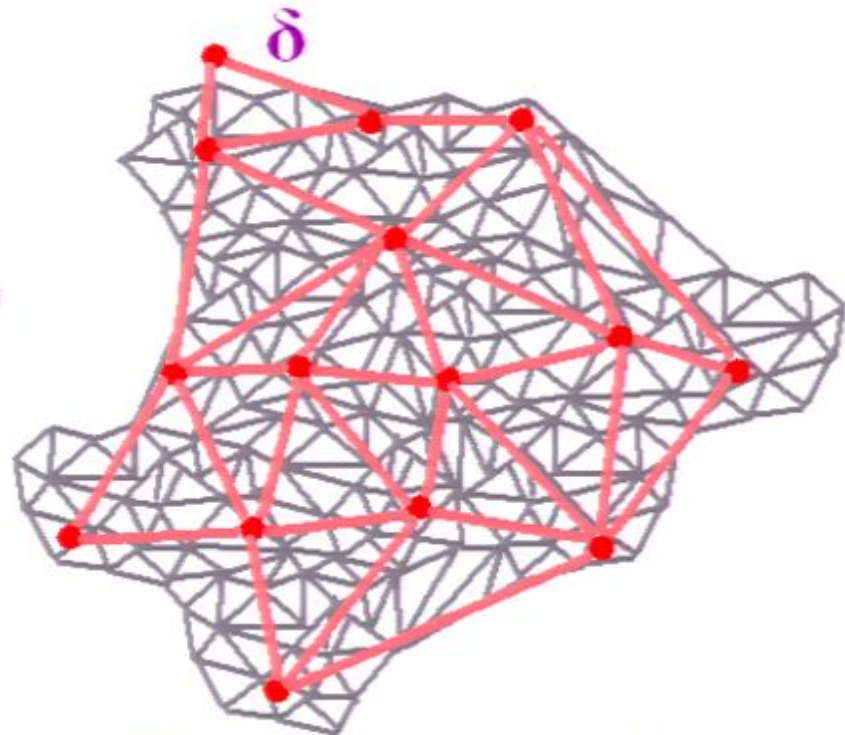
$$ds = e^{U(\Omega_2)} ds_R$$

U is a (time-like) Liouville field.

$$C_L = -C_M$$



True metric ds



Reference metric ds_R

$$ds = e^U ds_R$$



$$ds^2 = a(T)^2 \sinh^2 R \, d\Omega_2^2$$

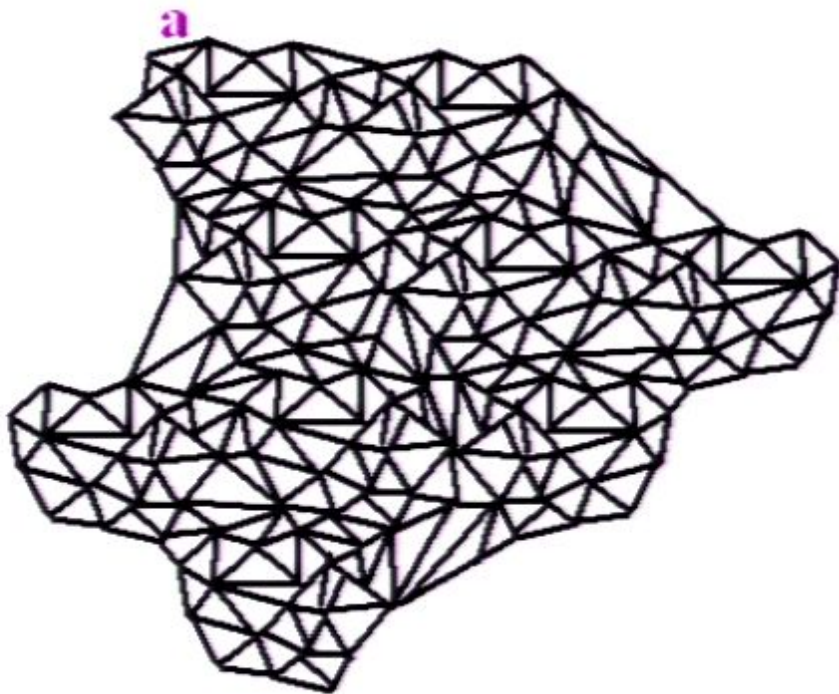
$$\approx a(T)^2 \{e^{2R} d\Omega_2^2\} \leftarrow \text{reference metric}$$

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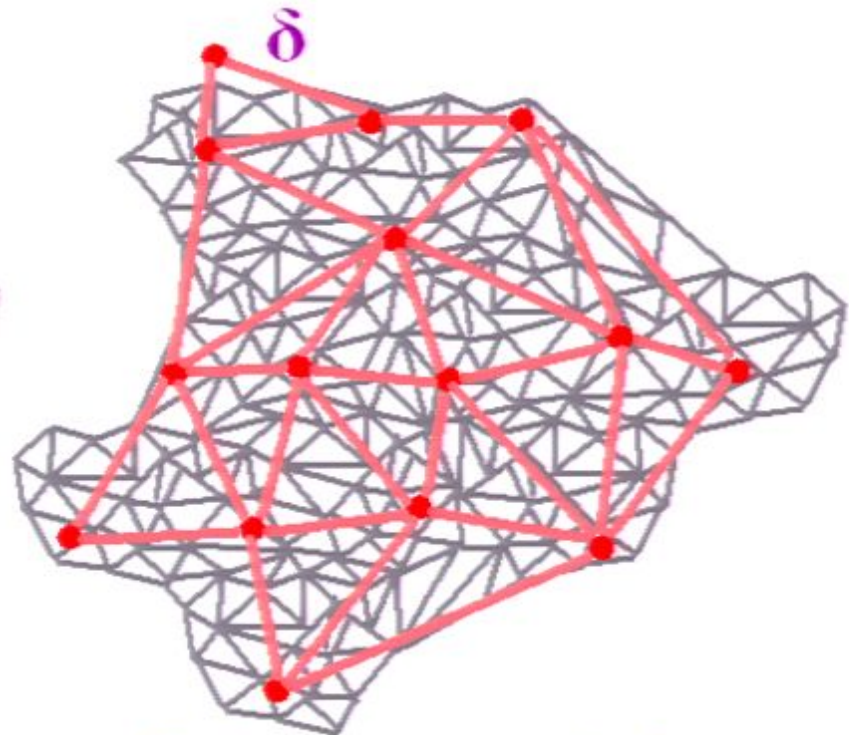
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True metric ds



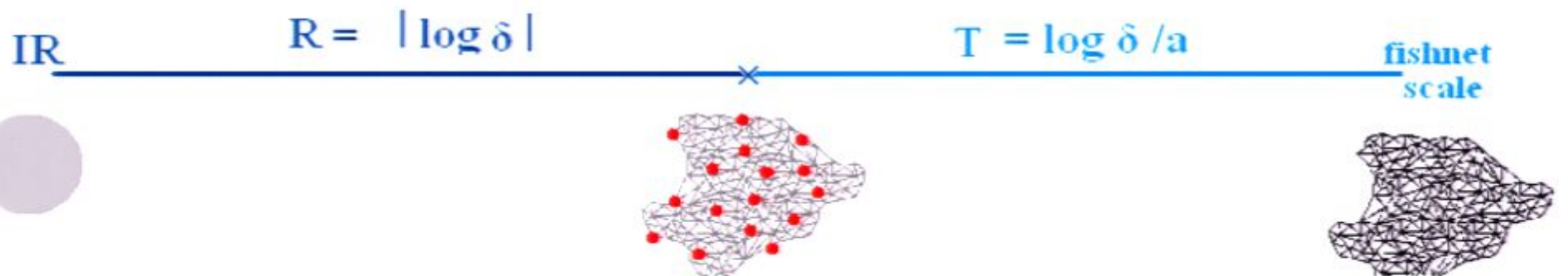
Reference metric ds_R

$$ds = e^U ds_R$$



Wilson Line

$L(R) = \text{effective action}$



$L(R, T) = \text{effective action}$

RG Flow: RG covariant and RG invariant Quantities

covariant: effective action, energy momentum tensor

$$\mathbf{L} = \sum_{\Delta} \mathbf{g}_{\Delta} \mathbf{O}_{\Delta}$$

$$\hat{\mathbf{g}}_{\Delta} = \mathbf{g}_{\Delta} \delta^{(2-\Delta)}$$

$$\frac{d\hat{\mathbf{g}}_{\Delta}}{\log \delta} = \beta(\hat{\mathbf{g}}) = 0 \quad (\text{fixed pt})$$

$$\mathbf{g}_{\Delta}(\delta) = \mathbf{g}_{\Delta}(\mathbf{a}) \left\{ \frac{\delta}{\mathbf{a}} \right\}^{(\Delta-2)}$$

$$\mathbf{L}(\delta) = \sum_{\Delta} \mathbf{O}_{\Delta} \left\{ \frac{\delta}{\mathbf{a}} \right\}^{(\Delta-2)}$$