

Title: Can We Detect Dynamics in Dark Energy?

Date: Dec 03, 2007 03:15 PM

URL: <http://pirsa.org/07120018>

Abstract: We highlight the unexpected impact of nucleosynthesis on the detectability of tracking quintessence dynamics at late times, showing that dynamics may be invisible until Stage-IV dark energy experiments (DUNE, JDEM, LSST, SKA). Nucleosynthesis forces  $|w\dot{w}| < 0.2$  for the models we consider and strongly limits potential deviations from  $\Lambda$ CDM.

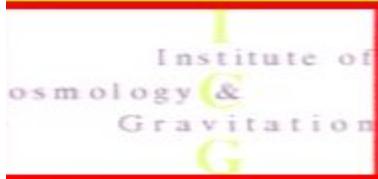
Surprisingly, the standard CPL parametrisation,  $w(z) = w_0 + w_a z / (1+z)$ , cannot match the nucleosynthesis bound for minimally coupled tracking scalar fields. Given that such models are arguably the best-motivated alternatives to a cosmological constant these results may significantly impact future cosmological survey design and imply that dark energy may be dynamical even if we do not detect any dynamics in the next decade.

# Can we detect dynamics in Dark Energy?

Marina Cortês  
University of Sussex

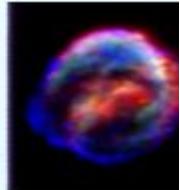
arxiv:0709.0526

Bruce Bassett, Mike Brownstone, Antonio Cardoso, Yabeba Fantaye, Renée Hlozek, Jacques Kotze Patrice Okouma



# 1998: ???

*supernovae 1a*

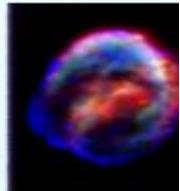


3

Expansion is **speeding up**  
not  
**slowing down!**

# 1998: ???

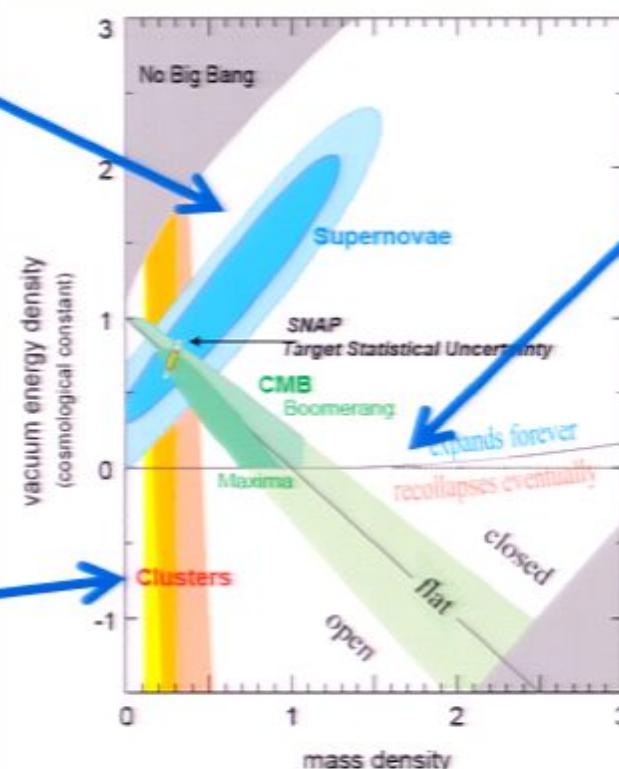
supernovae 1a



Expansion is speeding up  
not  
**slowing down!**

**SN1a:**  
brightness is same  
dimmer  
 are farther away

**Clusters**  
• x-ray fraction is constant  
• measured fraction depends on distance



**CMB:** power spectrum  

- baryons and photons pulled by gravity
- information from peak position + amplitude

When we don't know what it is we put "dark" in front of it...

Makes it easier to get funding!"  
*phd comics*

# DARK ENERGY

$\Lambda$

- why so small?
- why now?
- 120...

## Dynamics

- motivate from theory
- plenty of possibilities
- plenty of imagination..

all observations  
consistent with  
 $w = -1$

only  
covariant  
description



## MOST PLAUSIBLE MOST PUZZLING

- zero point energy
- no prediction →  $\rho_{\text{vac}} \propto k^4$
- energy scales phase transitions early universe



$$\rho_{\text{vac}}^{(\text{obs})} \sim 10^{-120} \rho_{\text{vac}}^{(\text{guess})}$$

**It is (also) a good rule  
not to put too much  
faith in observations  
until they are  
confirmed by theory...**

Sir Arthur Eddington

$$\omega = P / \rho$$



$$\omega = \frac{p}{P}$$

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# It's what we're looking for...

**ESSENCE**: deviations from  $\Lambda$  at  $z \sim 0.5$

*Wood-Vasey et al*

**HST**: bound  $w'$  across  $0.2 < z < 1.3$

*Riess et al*

**DETF**: consistency with Lambda?  
time evolution?

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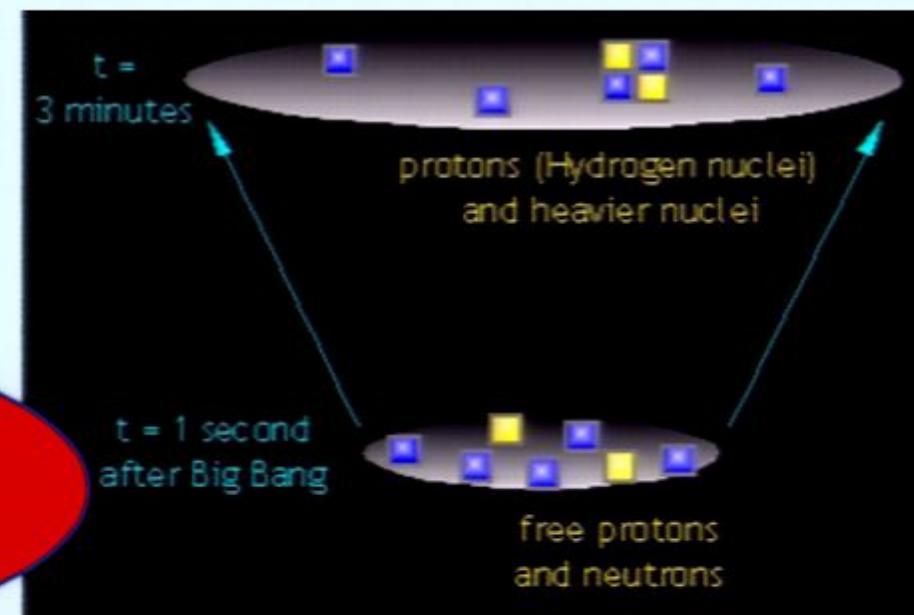
# BIG BANG NUCLEOSYNTHESIS

$$T \sim 1 \text{ MeV}$$

→ key difference between lambda and dynamics: **DE present at earlier times**

$$\frac{n}{p} \sim \exp\left(-\frac{m_n - m_p}{T}\right)$$

*exponentially  
sensitive to  
expansion rate*



freeze out: ratio fixed



determine expansion rate

we know expansion



we know amount of Dark Energy

# Constraints on Dark Energy...

## BBN

Bean, Hansen, Melchiorri (2001)

$$\Omega_{DE}(T \sim 1MeV) < 0.045 \quad \text{at} \quad 2\sigma$$

## CMB

Doran et al (2005)

$$\Omega_{DE}(T \sim 1eV) < 0.04$$

# Linking BBN to today... Scaling Fields!

10

## Definition

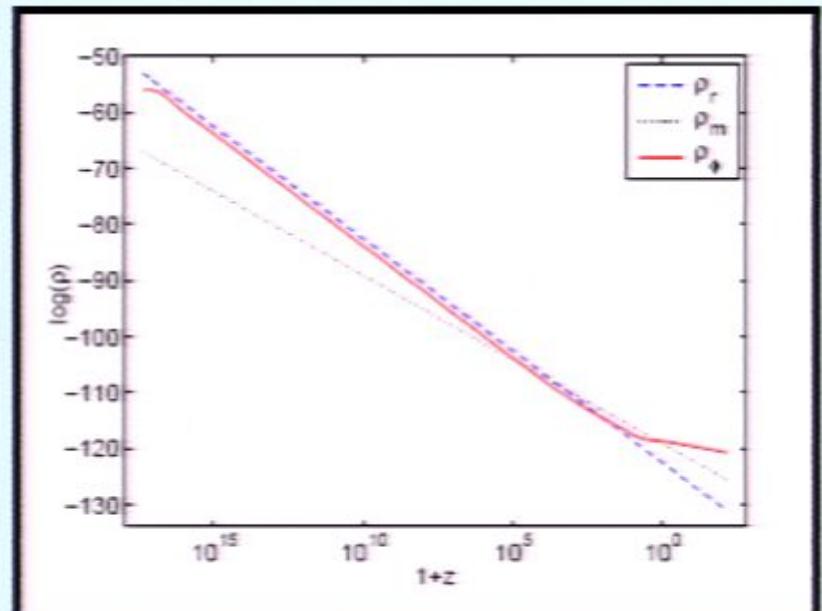
$$\Omega_\phi = \frac{\rho_\phi}{\rho_b} = const$$

Ratra and Peebles 199

Wetterich 199

Copeland Liddle Wands 199

- Field energy density **mimics** background
- Less dependence on **initial conditions** scaling regime from wide range i.c's
- Using Nucleosynthesis:



$$\Omega_\phi(BBN) = 0.045 \longrightarrow \Omega_\phi(z_t) = 0.045$$

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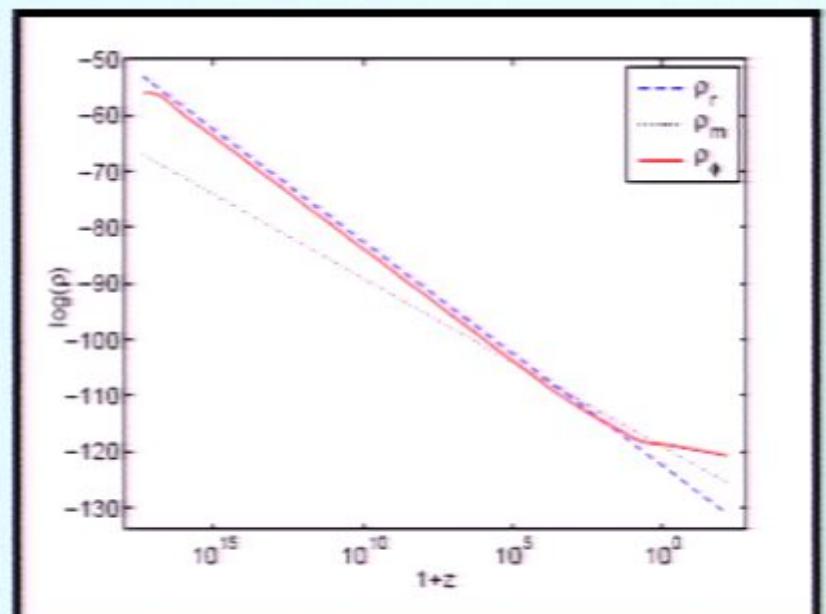
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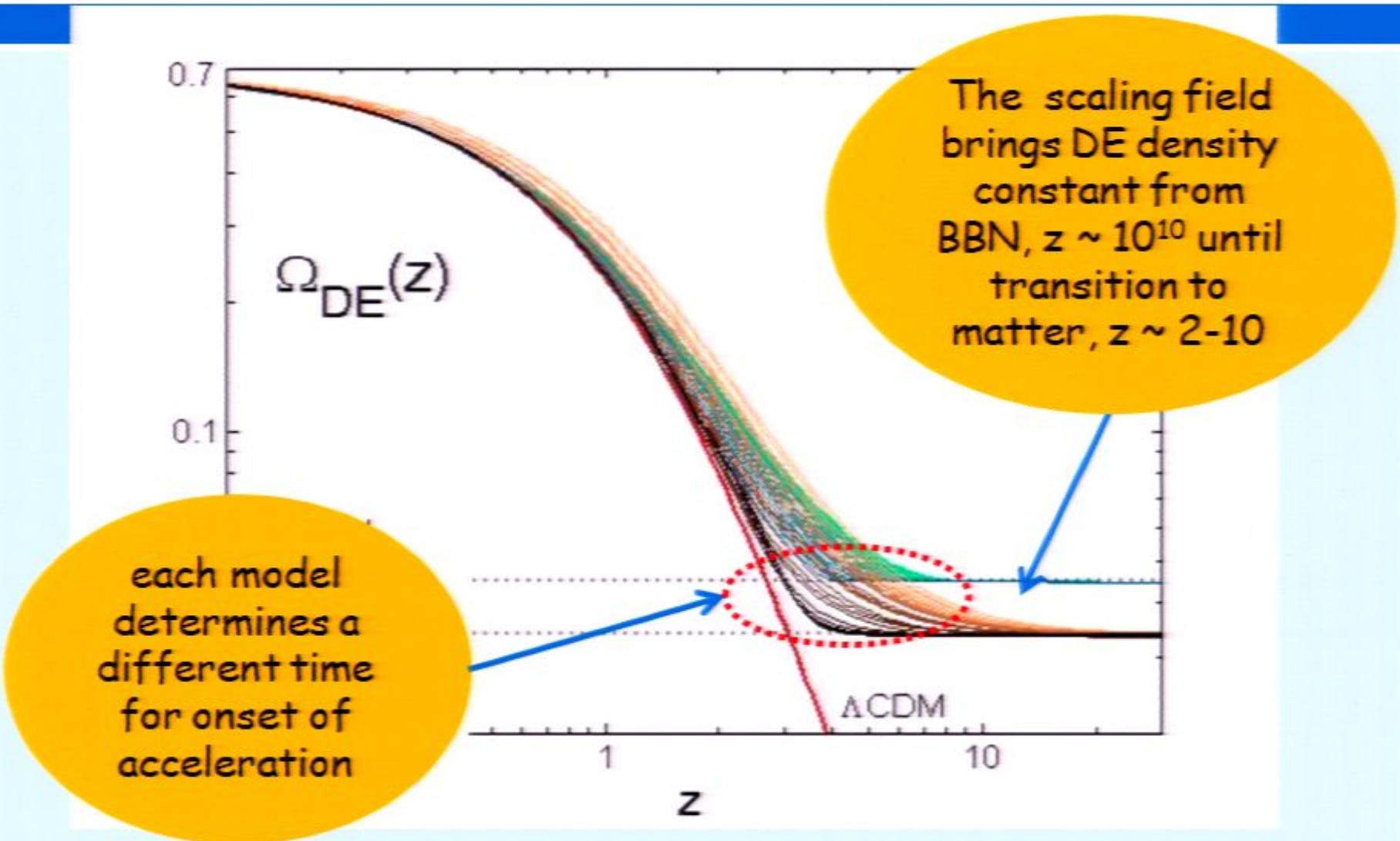
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# BBN+ scaling:



# So we take:

12

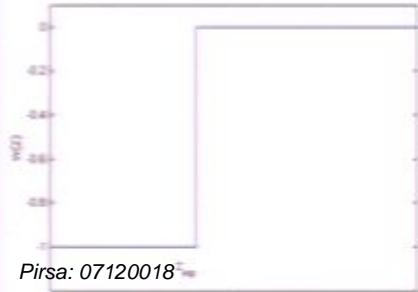
- ✓ Constraint at BBN
- ✓ Field **scales** until transition to matter



1. TOY MODEL:  
step function for  
transition

2. SCALAR FIELD:  
leaves scaling to  
dominate energy  
density

3. PHENOMENOLOGICAL  
after transition  
look for famous  $w(z)$ 's...



$$V(\phi) = M_1^4 e^{-\lambda \kappa \phi} + M_2^4 e^{-\mu \kappa \phi}$$



# BBN+ scaling:

13

The diagram illustrates the calculation of the dark energy density parameter  $\Omega_{DE}(z_t)$  at a specific transition point. It consists of three main components:

- A central yellow box contains the equation:
$$\Omega_{DE}(z_t) = \frac{\Omega_{DE}^{(0)} f(z_t)}{\Omega_{DE}^{(0)} f(z_t) + \Omega_m^{(0)} (1+z_t)^3} = 0.045$$
- An orange oval labeled "at transition" points to the term  $f(z_t)$  in the equation.
- An orange oval labeled "choose  $w(z)$  and invert" points to the term  $\Omega_{DE}^{(0)}$ .
- An orange oval labeled "saturate limit" points to the denominator term  $(1+z_t)^3$ , indicating it represents a saturation limit.
- A blue arrow points from the "choose  $w(z)$  and invert" oval to the "at transition" oval.
- A blue arrow points from the "saturate limit" oval to the central equation.

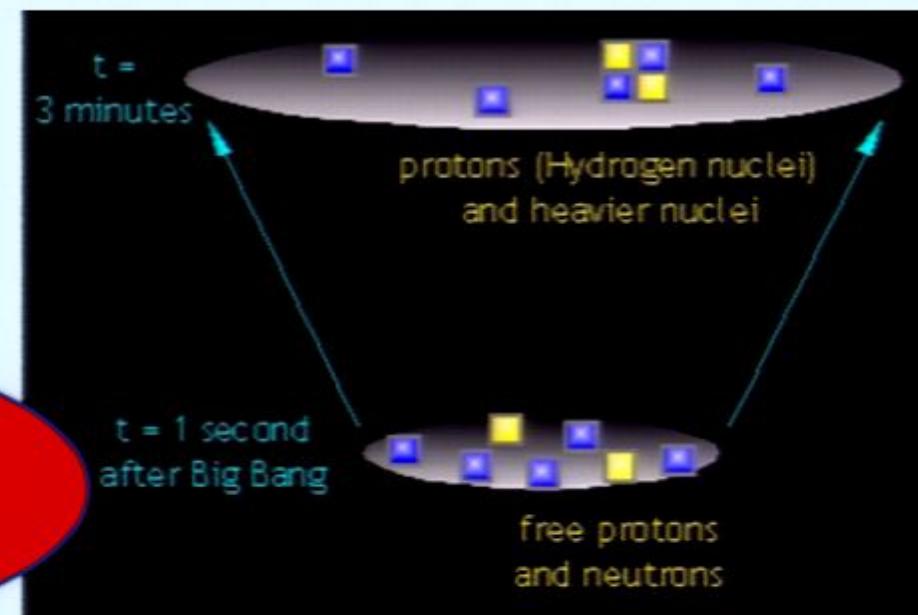
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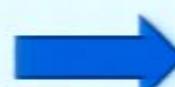


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determine expansion rate

we know expansion



we know amount of Dark Energy

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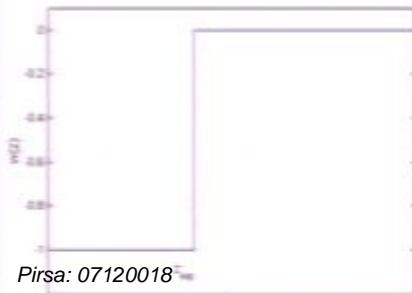
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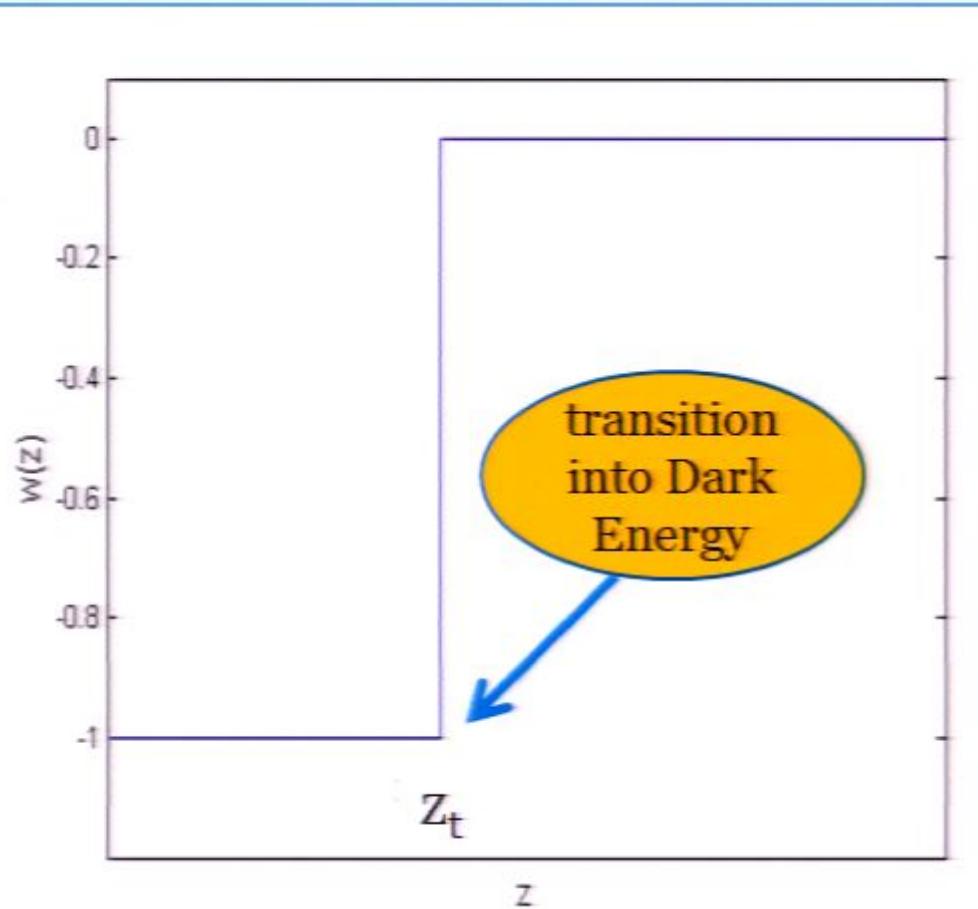


$$V(\phi) = M_1^4 e^{-\lambda \kappa \phi} + M_2^4 e^{-\mu \kappa \phi}$$



# 1.Toy Model: Step Function

14



BBN + scaling +

$$\begin{cases} w(z_t) = 0 \\ w(0) = -1 \end{cases}$$

$z_t > 2.6$

transition doesn't happen within  
reach of most DE probes...!

$z_t \sim 1$

needs

$w = -1.88$

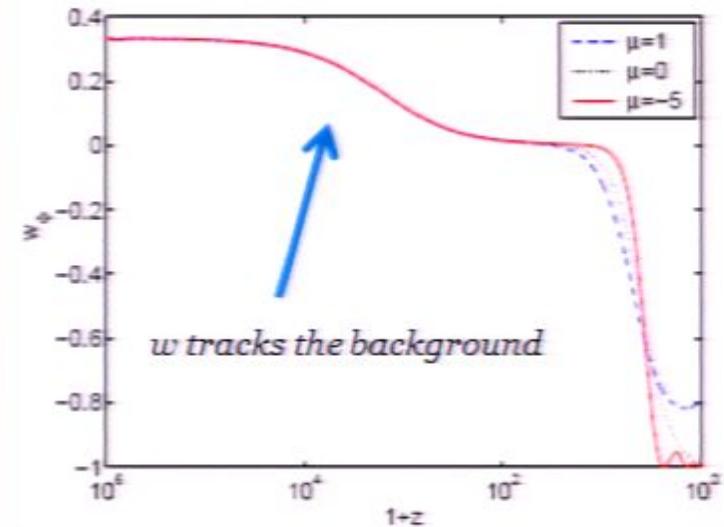
## 2. Double Exponential Potential

45

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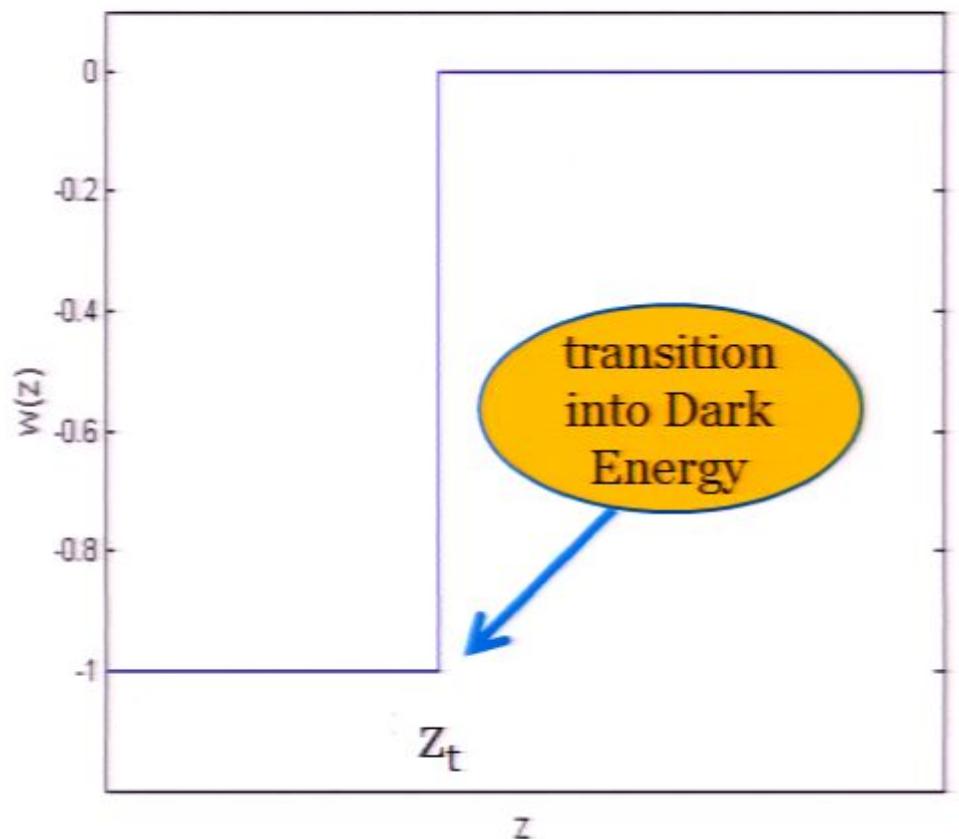
BBN +  $\Omega_\phi \sim 0.7$   
 $\Omega_m \sim 0.3$  sets  $\lambda, M_2, \mu^2 < 2$

➤ saturate BBN bound  $\mu=1$   
to maximize deviations from LAMBDA...  
...examine detectability



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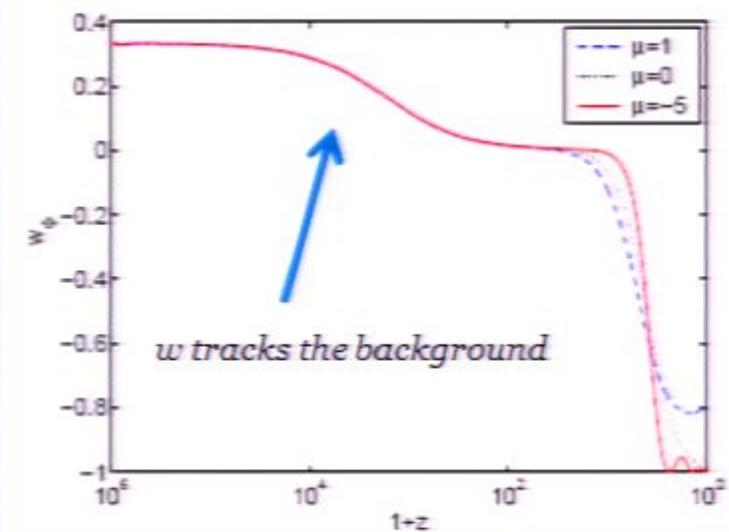
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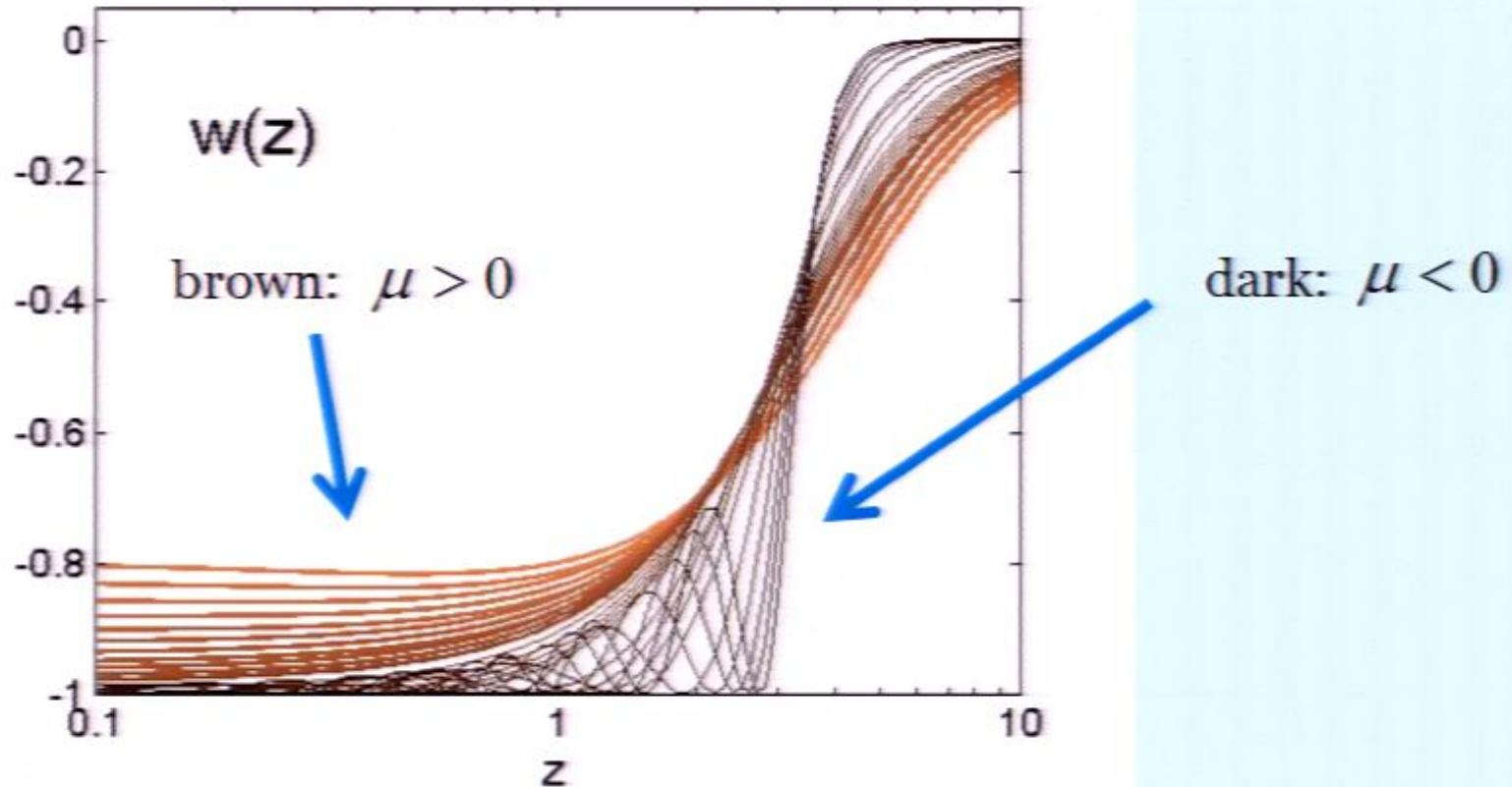
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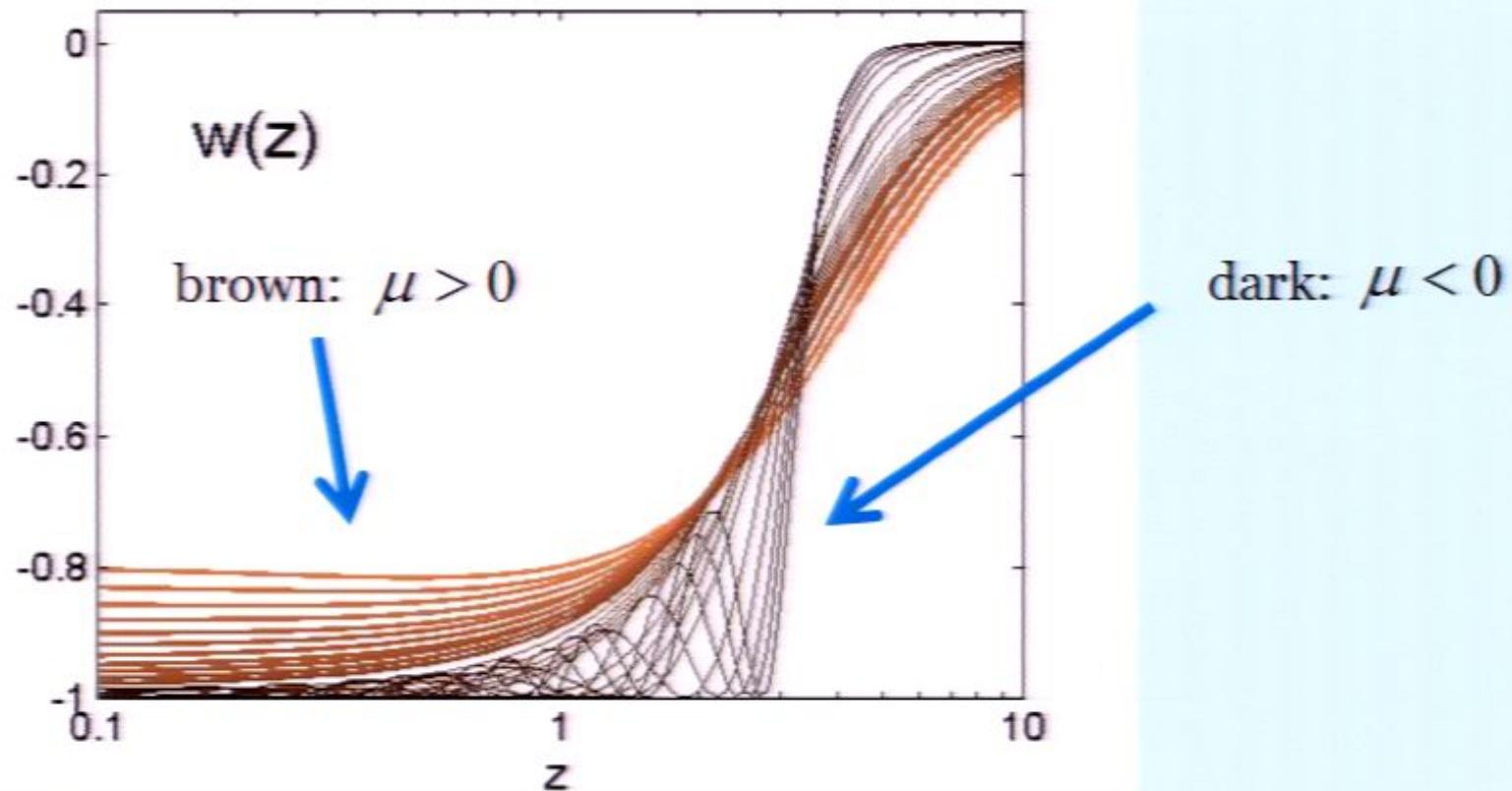
16



- if  $w$  today close to  $2\sigma$  boundary ( $\mu = 1$ )  
detectability is within reach of Stage IV experiments

# Double Exponential Potential

16



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detectability is within reach of Stage IV experiments

# Detectability: Hubble rate

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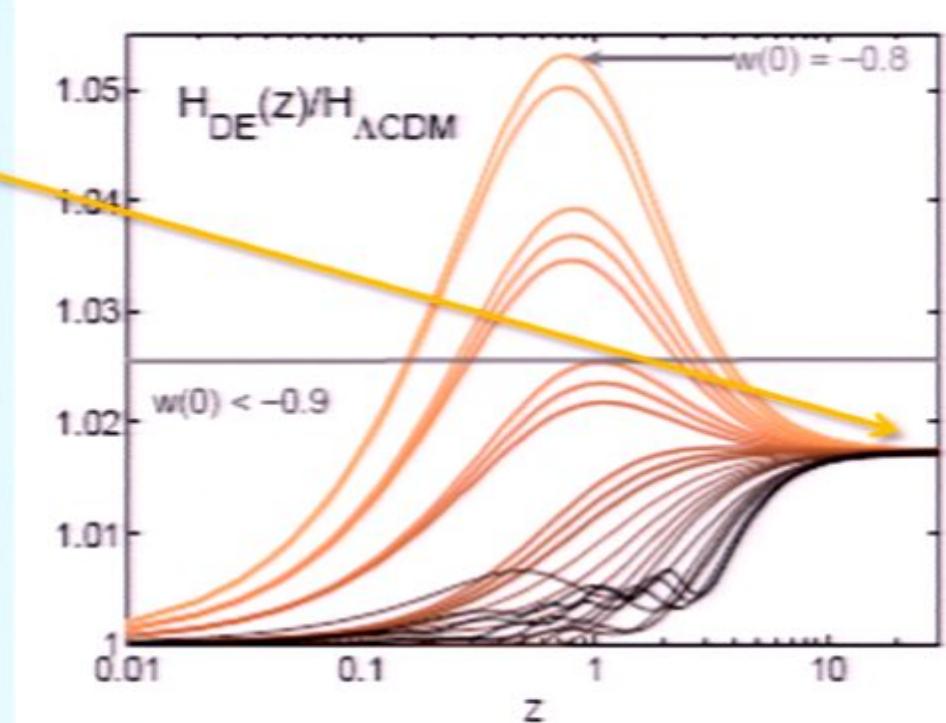
$$\begin{aligned}\frac{H_{DE}}{H_\Lambda}(z \geq z_t) &= \sqrt{\frac{(1+zt)^3}{(1-\epsilon)(1+z_t)^3 + r}} \\ &\leq \sqrt{\frac{1}{1-\epsilon}} \\ &= 1.017 \text{ for } \epsilon = \frac{3}{4} 0.045\end{aligned}$$

$w(0) < 0.9$



Deviations of  $H(z)$  from LCDM <  
**2.7%**

Largest deviation at  $z \sim 1$



# Distance Modulus

## □ Distance modulus

$$\Delta\mu = 5 \log \left( \frac{d_{L,DE}(z)}{d_{L,\Lambda}(z)} \right)$$

where (assuming flatness)

$$d_L = \frac{c}{H_0} (1+z) \int_0^z \frac{dz'}{E(z')}$$
$$\text{and } E(z) = \frac{H(z)}{H_0}$$

If

$$\frac{H_{DE}(z)}{H_\Lambda(z)} < 1 + \alpha^2$$
$$\rightarrow \frac{d_{L,DE}(z)}{d_{L,\Lambda}(z)} \propto \frac{H_\Lambda}{H_{DE}} > \frac{1}{1 + \alpha^2}$$

plots of distance modulus see paper

### 3. Standard Parametrization... CPL

20

$$w(z) = w_0 + w_a(1-a) = w_0 + w_a \frac{z}{1+z}$$

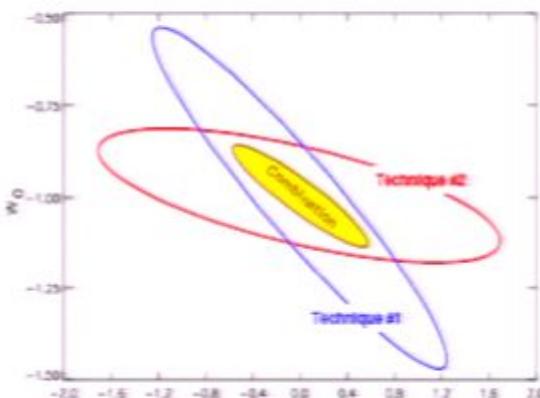
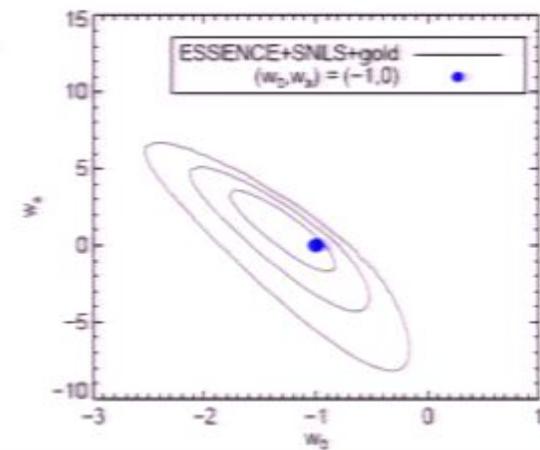
Chevallier Polarski (2001)  
Linder (2003)

➤ Widely used

➤ Surveys use it for constraints on dynamics



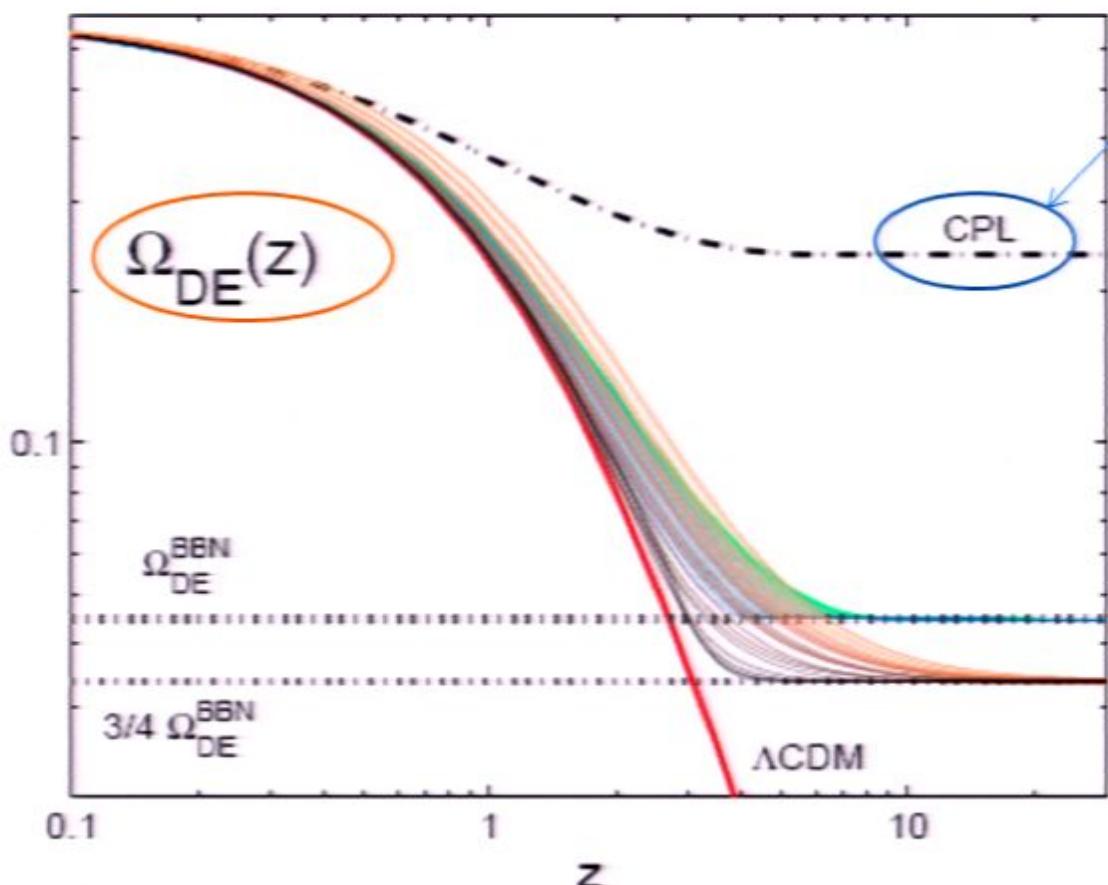
➤ Basis for DETF's Figure-of-Merit!  
(evaluates merit of ongoing and future DE studies)



# Failure of CPL...

*...to meet nucleosynthesis constraints with a scaling field*

21



$w_{CPL}$  cannot bring  $\Omega_{DE}$

from

$$\Omega_{DE}(z_t) = 0.045$$

to

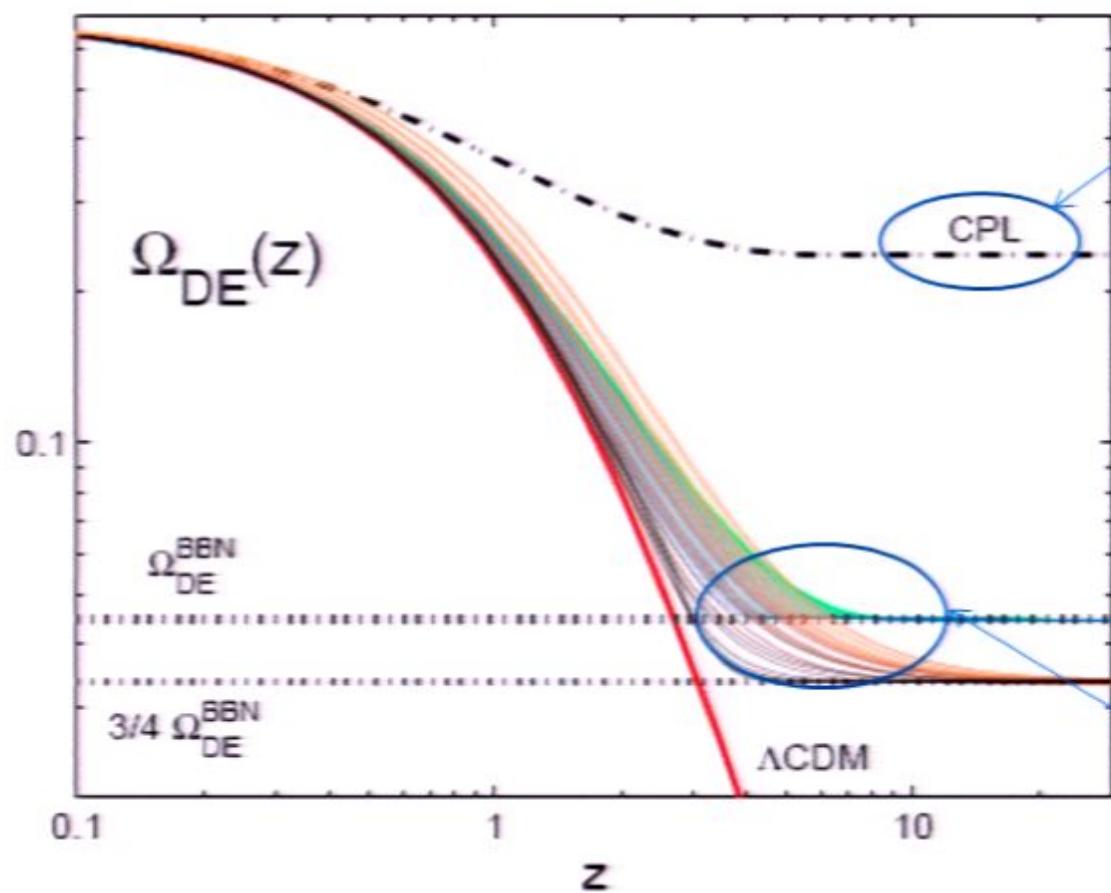
$$\Omega_{DE}(0) = 0.7$$

if

$$\begin{cases} w(0) = -1 \\ w(z_t) = w_m = 0 \end{cases}$$

# Failure of CPL...

*...to meet nucleosynthesis constraints with a scaling field*



- Maximum value of  $w_{CPL}$  is

$$w_{CPL} = w_0 + w_a$$

- asymptotically  $w = 0$  but never reaches

Double Exponential Potential

# CONCLUSIONS

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- Scaling fields among best alternatives to LAMBDA
- BBN constraints on  $\Omega_{DE}$  at  $T \sim 1\text{MeV}$  **strong limits** on dynamics
- Constraints Hubble rate **detectability** not guaranteed within next decade surveys
- if  $w$  today close to maximum we can detect dynamics with Stage IV
- Standard CPL parametrization fails to meet BBN with a scalar field
- Important because **figure-of-merit**
  - using this parametrization may systematically point away from quintessence scaling models