

Title: Planck Meets Hubble and Boltzmann: Holographic Quantum Foam and Cosmology

Date: Nov 05, 2007 11:15 AM

URL: <http://pirsa.org/07110038>

Abstract: Quantum fluctuations of spacetime give rise to quantum foam, and black hole physics dictates that the foam is of holographic type. One way to detect quantum foam is to exploit the fact that an electromagnetic wavefront will acquire uncertainties in direction as well as phase as it propagates through spacetime. These uncertainties can show up in interferometric observations of distant quasars as a decreased fringe visibility. The Very Large Telescope interferometer may be on the verge of probing spacetime fluctuations which, we argue, have repercussions for cosmology, requiring the existence of dark energy/matter, critical cosmic energy density, and accelerating cosmic expansion in the present era. We speculate that, in the framework of holographic quantum foam, the dark energy is composed of an enormous number of inert ``particles\' of extremely long wavelength. These ``particles\' necessarily obey infinite statistics (quantum Boltzmann statistics) in which all representations of the particle permutation group can occur. For every boson or fermion in the present observable universe there could be $\sim 10^{31}$ such ``particles\'.

CONTENTS

Quantum fluctuations of spacetime

- gedanken expt; holographic principle; ... *skip*
- [loop quantum gravity (Gambini & Pullin)]
- mapping the geometry of spacetime \Leftarrow
- cumulative effects

Probing spacetime foam with

- Gamma ray bursts? *skip?* Laser-based interferometry? *skip*
- VLT interferometers
- [Bose-Einstein condensate (Gambini & Pullin)] *skip*

STF \Rightarrow Holographic Foam Cosmology

- Existence of dark energy/matter
- DE/DM and infinite statistics
- [DE, ∞ stat. & M-theory (Jejjala, Kavic, Minic)]

Summary and speculations

Notation: subscript P = Planck units

Planck length: $l_P \equiv \sqrt{\frac{\hbar G}{c^3}} \sim 10^{-33}$ cm etc

CONTENTS

Quantum fluctuations of spacetime

- gedanken expt; holographic principle; ... *skip*
- [loop quantum gravity (Gambini & Pullin)]
- mapping the geometry of spacetime \Leftarrow
- cumulative effects

Probing spacetime foam with

- Gamma ray bursts? *skip?* Laser-based interferometry? *skip*
- VLT interferometers
- [Bose-Einstein condensate (Gambini & Pullin)] *skip*

STF \Rightarrow Holographic Foam Cosmology

- Existence of dark energy/matter
- DE/DM and infinite statistics
- [DE, ∞ stat. & M-theory (Jejjala, Kavic, Minic)]

Summary and speculations

Notation: subscript P = Planck units

Planck length: $l_P \equiv \sqrt{\frac{\hbar G}{c^3}} \sim 10^{-33}$ cm etc

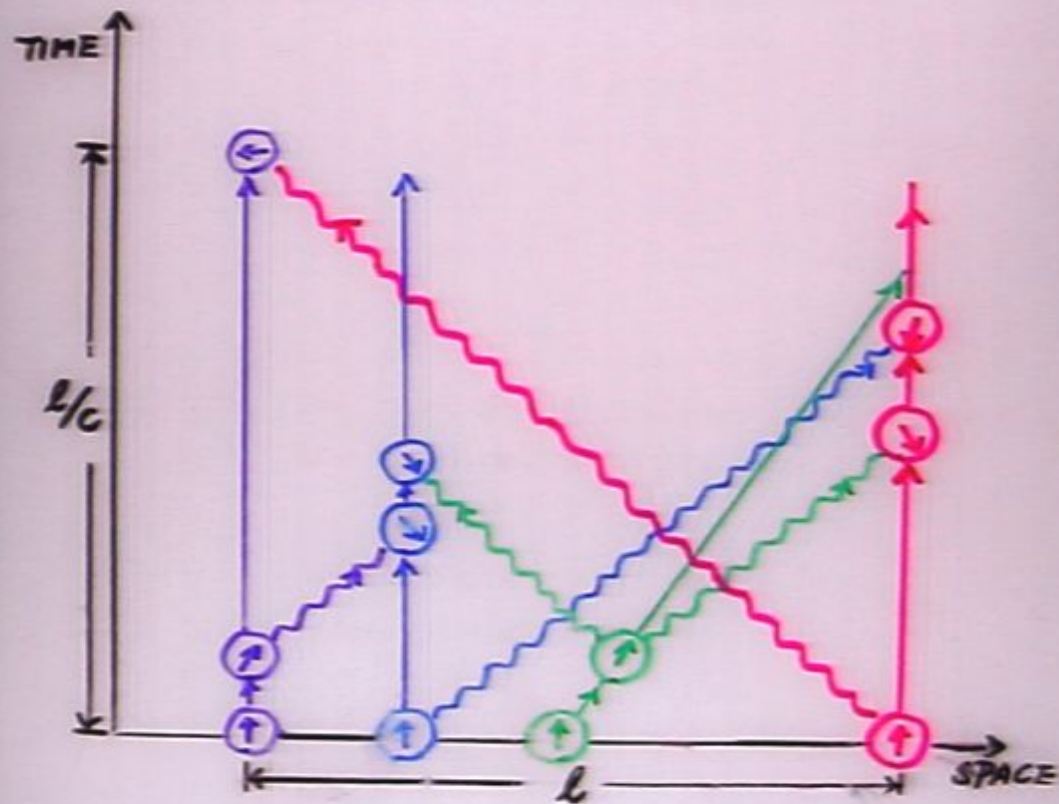
Method 2: Mapping the geometry of spacetime

(using a global positioning system)

[Giovannetti et al.] '04
[Lloyd & Ng]

Fill space with a swarm of clocks, exchanging signals with the other clocks and measuring the signals' time of arrival

How accurately can these clocks (of mass M) map out a volume of space-time with radius l over time l/c ?



Ticks & clicks of clocks in spacetime volume l^4/c

The process of mapping the geometry of spacetime is a kind of computational operation

- Margolus-Levitin theorem (rate of operations $\leq E/\hbar$; essentially energy-time Heisenberg uncertainty)

$$\Rightarrow \# \text{ operations} < (E/\hbar) \times \text{time} = \frac{Mc^2 l}{\hbar c}$$

- To prevent black-hole formation $\Rightarrow M \lesssim \frac{lc^2}{G}$ ($\rho \lesssim \frac{1}{l_p^2}$)

\Downarrow

$$\# \text{ ops or events (i.e., \# spacetime "cells")} < l^2 \frac{c^3}{\hbar G} = \frac{l^2}{l_p^2}$$

For max. spatial resolution, each clock ticks only ONCE

$$\Rightarrow \text{Each "cell" occupies spatial vol. } \frac{l^3}{l^2/l_p^2} = ll_p^2$$

$$\Rightarrow \text{Average spatial separation of "cells"} \simeq l^{1/3} l_p^{2/3}$$

- Consistent with the holographic principle
- Interpretation: $\delta l \gtrsim l^{1/3} l_p^{2/3}$, holographic model

[Károlyházy;
Ng + van Dam]

Maximum spatial resolution

- requires max. energy density $\rho \sim (ll_p)^{-2}$
- yields $\# \text{ bits} \sim l^2/l_p^2$

Holography in spherically symmetric loop quantum gravity

Rodolfo Gambini¹, Jorge Pullin²

1. Instituto de Física, Facultad de Ciencias, Igua 4225, esq. Mataojo, Montevideo, Uruguay.

2. Department of Physics and Astronomy, Louisiana State University, Baton Rouge, LA 70803-4001

We show that holography arises naturally in the context of spherically symmetric loop quantum gravity. The result is not dependent on detailed assumptions about the dynamics of the theory being considered. It ties strongly the amount of information contained in a region of space to the tight mathematical underpinnings of loop quantum geometry, at least in this particular context.

arXiv: 0708.0250

Physical principles usually represent facts partially collected by observation that end up guiding the development of physical theories. When the underlying theories are completely understood in detail, the principles can be explained as consequences of the theory they guided to create. The holographic principle has guided the construction of some of the leading physical theories of space time in the last few years. In a nutshell, holography establishes a limit to the amount of information contained in a space-time region [1]. In its simplest form, for spherical symmetry and weak gravity the principle establishes that the entropy of a region of space is limited by the area surrounding it and was first formulated by 't Hooft and Susskind [2]. Any successful theory of quantum gravity that incorporates holography should be able to derive it as a consequence of its framework. We would like to argue that holography does indeed follow from the framework of loop quantum gravity in spherical symmetry and that the result is robust: it does not depend on the details of the dynamics of the theory nor the type of matter included but rather on its kinematical structure and elementary dynamical considerations independent of the details of the Hamiltonian or its potential quantization ambiguities. In a nutshell, holography follows from the dependence of the volume operator in spherical loop quantum gravity on the radial distance, yielding an uncertainty in the determination of volumes that grows logarithmically. Such a dependence for the uncertainty of spatial measurements had already been postulated in heuristic arguments relating limitations of space-time measurements to holography by Ng [3] and with alternative reasonings by Susskind and Lloyd [4]. In this article we show that such a dependence can be derived from the kinematical structure of spherical loop quantum gravity. That holography in its simple and straightforward *spatial* form is materialized in the spherical case is appropriate, since it is known that in non-spherical cases more care is needed (in particular involving non-temporal regions) in its definition in order not to run into counterexamples (see [1] for details). Loop quantum gravity is emerging as a viable candidate for a theory of quantum gravity. Recent general discussions of the approach can be found in [5]. The kinematical setting for loop quantum gravity in spherically symmetric situations is well established and was discussed in detail by Bojowald and Swiderski [6]. There is only one non-trivial spatial direction (the radial) which we call x since it is not necessarily parameterized by the usual radial

But IF (not arguing that is the case)

Spread spacetime "cells" uniformly in both space and time:

temporal resolution \sim spatial resolution (here use $c = 1$)

Av. spatial separation of "cells" $\sim \left(\frac{l^4}{(l/l_P)^2} \right)^{1/4} = (ll_P)^{1/2}$

time sep. of successive ticks of each clock is $(ll_P)^{1/2}$

- Interpretation: $\delta l \gtrsim l^{1/2} l_P^{1/2}$, random-walk model
[Amelino-Camelia]

Time bet. ticks = time to communicate w. neighboring cells

Random Walk model

- predicts a coarser spatial resolution (larger fluctuations) than HM

- yields smaller bound on information content:

$$\frac{(l/l_P)^2}{(l/l_P)^{1/2}} = (l/l_P)^{3/2} = (l^2/l_P^2)^{3/4}$$

- does NOT require maximum energy density

But IF (not arguing that is the case)

Spread spacetime "cells" uniformly in both space and time:

temporal resolution \sim spatial resolution (here use $c = 1$)

Av. spatial separation of "cells" $\sim \left(\frac{l^4}{(l/l_P)^2} \right)^{1/4} = (ll_P)^{1/2}$

time sep. of successive ticks of each clock is $(ll_P)^{1/2}$

- Interpretation: $\delta l \gtrsim l^{1/2} l_P^{1/2}$, random-walk model
[Amelino-Camelia.]

Time bet. ticks = time to communicate w. neighboring cells

Random Walk model

- predicts a coarser spatial resolution (larger fluctuations) than HM
- yields smaller bound on information content:

$$\frac{(l/l_P)^2}{(l/l_P)^{1/2}} = (l/l_P)^{3/2} = (l^2/l_P^2)^{3/4}$$

- does NOT require maximum energy density

But IF (not arguing that is the case)

Spread spacetime "cells" uniformly in both space and time:

temporal resolution \sim spatial resolution (here use $c = 1$)

Av. spatial separation of "cells" $\sim \left(\frac{l^4}{(l/l_P)^2} \right)^{1/4} = (ll_P)^{1/2}$

time sep. of successive ticks of each clock is $(ll_P)^{1/2}$

- Interpretation: $\delta l \gtrsim l^{1/2} l_P^{1/2}$, random-walk model
[Amelino-Camelia]

Time bet. ticks = time to communicate w. neighboring cells

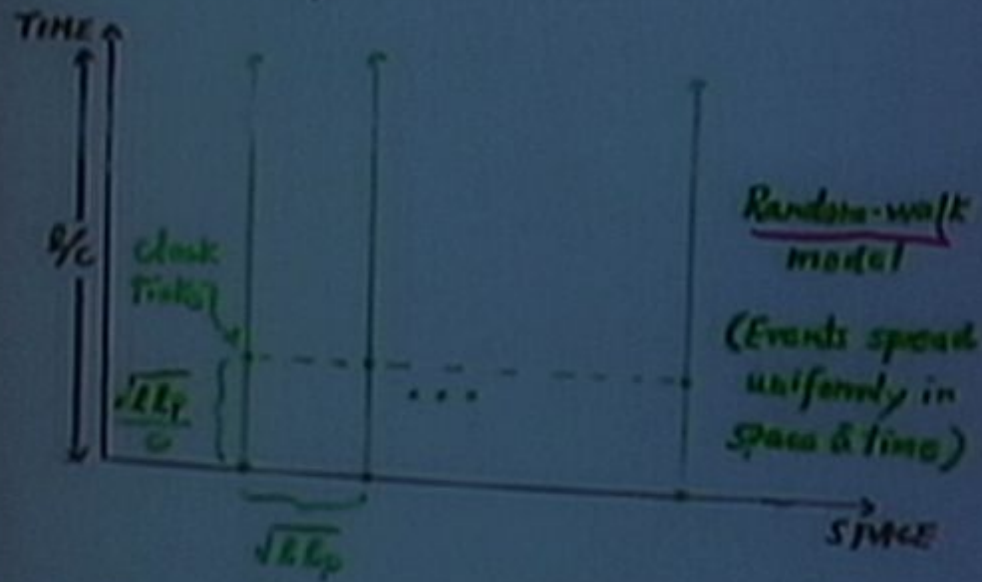
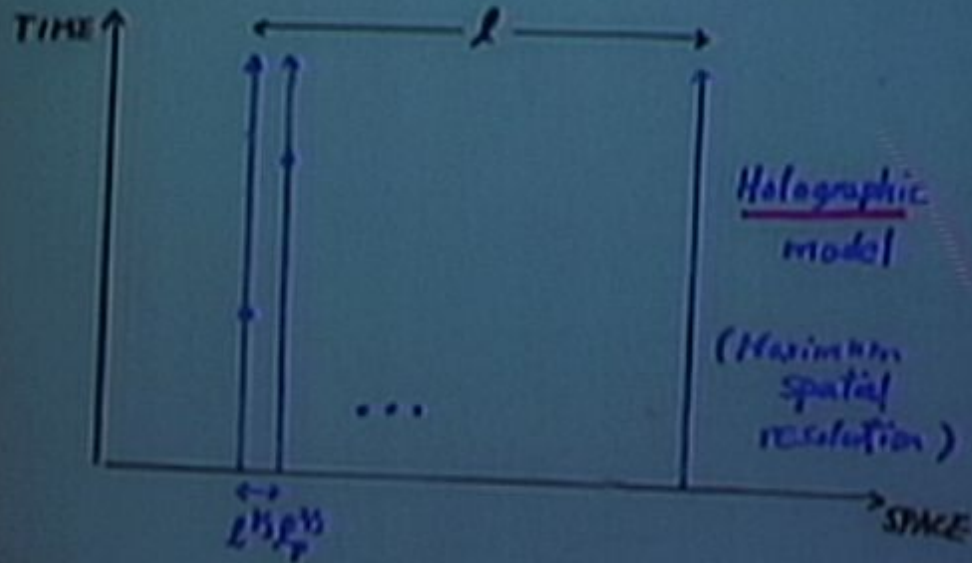
Random Walk model

- predicts a coarser spatial resolution (larger fluctuations) than HM

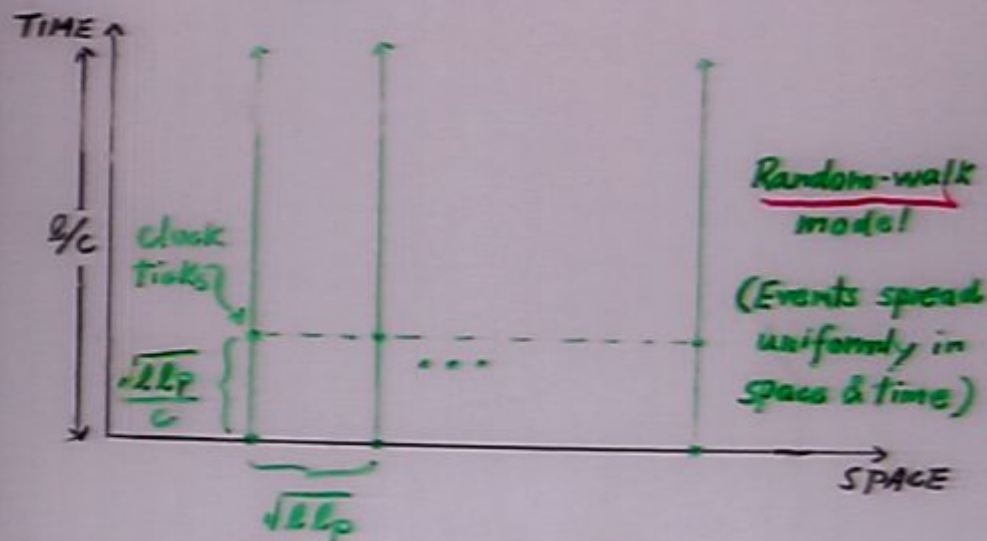
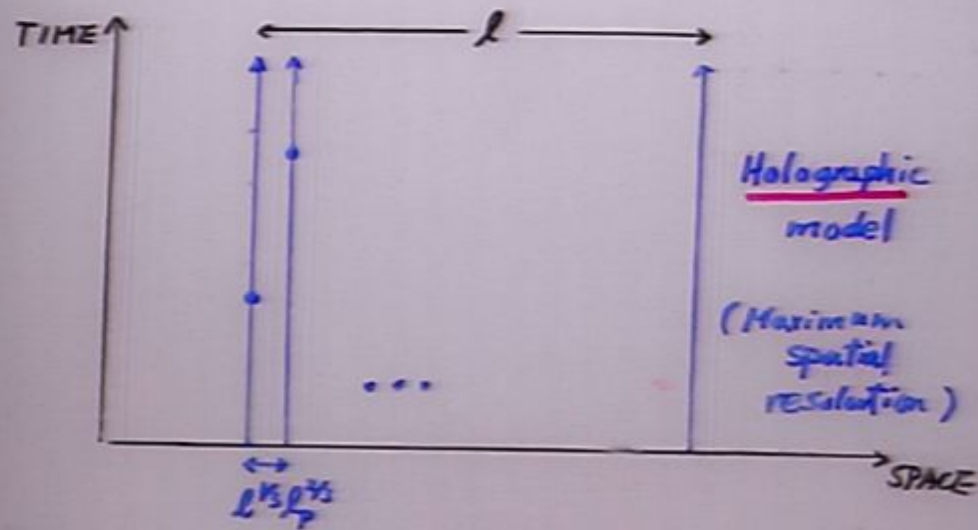
- yields smaller bound on information content:

$$\frac{(l/l_P)^2}{(l/l_P)^{3/2}} = (l/l_P)^{3/2} = (l^2/l_P^2)^{3/4}$$

- does NOT require maximum energy density



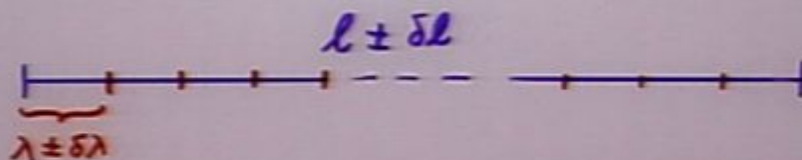
For $L \sim 10^{28}$ cm $\sim R_H$, $\frac{\sqrt{L/c}}{c} \sim 10^{-19}$ sec
 (clock ticks \rightarrow bit flips) $\sqrt{L/c} \sim 10^3$ cm



For $l \sim 10^{28} \text{ cm} \sim R_H$, $\frac{\sqrt{l \rho_p}}{c} \sim 10^{-14} \text{ sec}$
 (clock ticks \rightarrow bit flips) $\sqrt{l \rho_p} \sim 10^{-3} \text{ cm}$

Cumulative effects of spacetime fluctuations

Divide distance l into l/λ equal parts each of length λ (for any $l_p \leq \lambda \leq l$)



Question: Starting with $\delta\lambda$ from each part, how do the l/λ parts add up to δl for the whole distance l ?

I.e., find the cumulative factor C in $\delta l = C \delta \lambda$

$$\delta l \sim l^{1/3} l_p^{2/3}; \quad \delta \lambda \sim \lambda^{1/3} l_p^{2/3}$$

\Downarrow

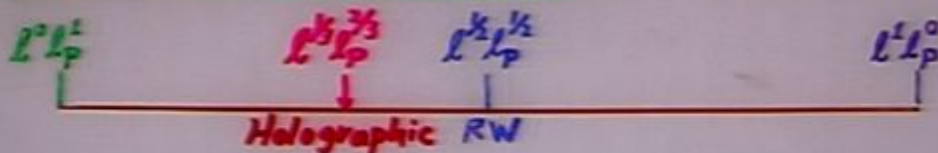
$$C = \left(\frac{l}{\lambda}\right)^{1/3}$$

Cumulative Factor = $(\#intervals)^{1/3}$

(\sim Brownian motion with self-similarity parameter 1/3)

Random walk model ($\delta l \sim l^{1/2} l_p^{1/2}$): $C = (l/\lambda)^{1/2}$

Completely anti-correlation model ($\delta l \sim l_p$): $C = 1$

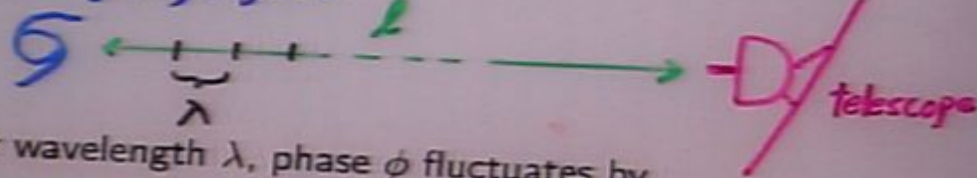


δl (anti-correlation \Leftarrow ; correlation \Rightarrow)

Phase incoherence of γ s from distant galaxies

Idea: Spacetime fluctuations can **cumulatively** lead to loss of phase coherence for radiation from far enough galaxies

distant galaxy/quasar



Over wavelength λ , phase ϕ fluctuates by

$$\delta\phi = 2\pi \frac{\delta\lambda}{\lambda} \sim \pm 2\pi (\lambda^{1/3} l_P^{2/3}) / \lambda = \pm 2\pi \left(\frac{l_P}{\lambda}\right)^{2/3}$$

Intuitively, over distance l , the cumulative phase dispersion is

$$\Delta\phi = \delta\phi \times \frac{l}{\lambda} \quad [\text{Lieu \& Hillman; Ragazzoni et al.}]$$

Factor $\frac{l}{\lambda}$ is enormously huge so that $\Delta\phi \gg 2\pi$
 \Rightarrow Distant compact radiation sources should not produce normal interference patterns. But ... **Wrong!**

$\delta\phi$'s fluctuate \pm "randomly", do not add coherently

Cumulative factor is $\left(\frac{l}{\lambda}\right)^{1/3} \ll \frac{l}{\lambda}$:

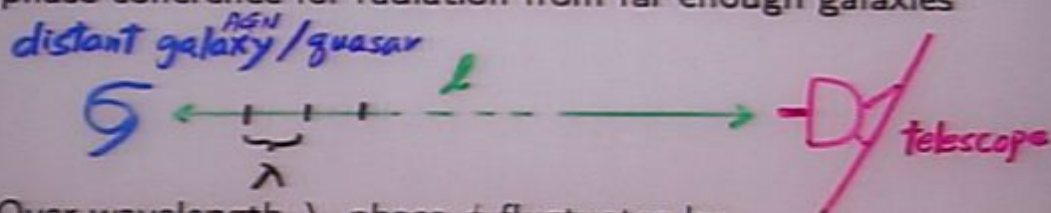
$$\Delta\phi \sim 2\pi \left(\frac{l_P}{\lambda}\right)^{2/3} \left(\frac{l}{\lambda}\right)^{1/3} = 2\pi \frac{l_P^{2/3} l^{1/3}}{\lambda}$$

For PKS1413+135, $\Delta\phi \sim 10^{-9} \times 2\pi \ll 2\pi$ for holographic model
 [Ng, Christiansen, & van Dam]

- $\Delta\phi \sim 10 \times 2\pi$ for random walk model, ruled out (?)

Phase incoherence of γ s from distant galaxies

Idea: Spacetime fluctuations can **cumulatively** lead to loss of phase coherence for radiation from far enough galaxies



Over wavelength λ , phase ϕ fluctuates by

$$\delta\phi = 2\pi \frac{\delta\lambda}{\lambda} \sim \pm 2\pi (\lambda^{1/3} l^{2/3}) / \lambda = \pm 2\pi \left(\frac{l_P}{\lambda}\right)^{2/3}$$

Intuitively, over distance l , the cumulative phase dispersion is

$$\Delta\phi = \delta\phi \times \frac{l}{\lambda} \quad \text{[Lieu & Hillman; Ragazzoni et al.]}$$

Factor $\frac{l}{\lambda}$ is enormously huge so that $\Delta\phi \gg 2\pi$

\Rightarrow Distant compact radiation sources should not produce normal interference patterns. But ... **Wrong!**

$\delta\phi$'s fluctuate \pm "randomly", do not add coherently

Cumulative factor is $\left(\frac{l}{\lambda}\right)^{1/3} \ll \frac{l}{\lambda}$:

$$\Delta\phi \sim 2\pi \left(\frac{l_P}{\lambda}\right)^{2/3} \left(\frac{l}{\lambda}\right)^{1/3} = 2\pi \frac{l_P^{2/3} l^{1/3}}{\lambda}$$

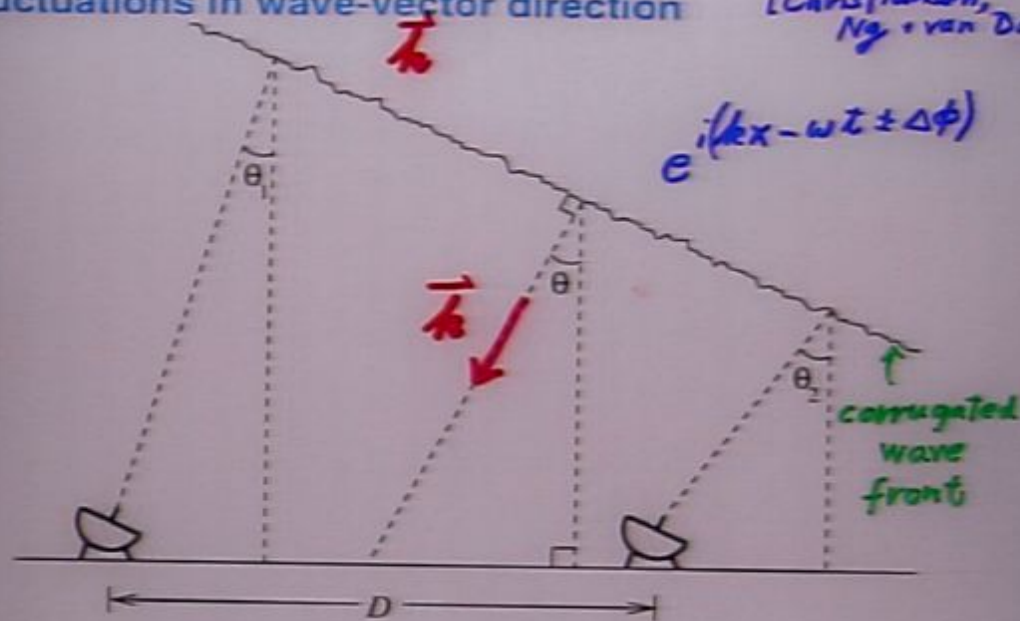
For PKS1413+135, $\Delta\phi \sim 10^{-9} \times 2\pi \ll 2\pi$ *for holographic model*

[Ng, Christiansen, & van Dam]

- $\Delta\phi \sim 10 \times 2\pi$ for **random walk model**, ruled out (?)

Fluctuations in wave-vector direction

[Christianson, Ng, & van Dam]



Spacetime foam-induced fluctuations in wave-vector direction $\sim \Delta\phi/2\pi$

Correlated electric field $|E| \sim \left| \cos \left(\frac{\pi}{2} [2\theta - \Delta\phi/2\pi] \frac{D}{\lambda} \right) \right|$

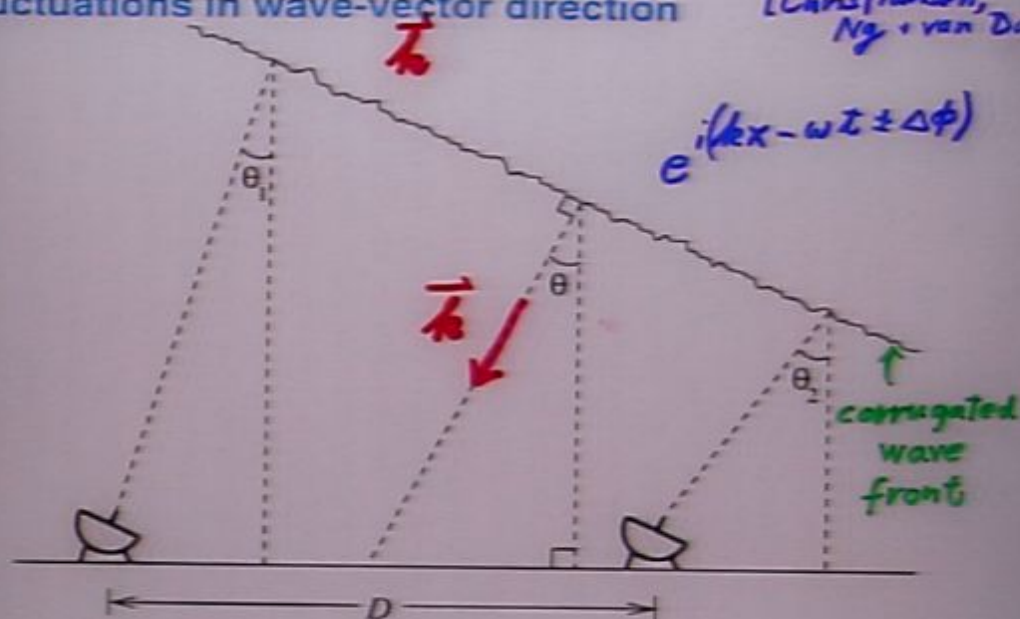
- For $\Delta\phi = 0$, 1st null at $2\theta = \lambda/D$
- For $\Delta\phi \neq 0$, 1st null for halo at $2\theta - \Delta\phi/2\pi \sim \lambda/D$
 \Rightarrow halo appearance w. half-width $\sim \Delta\phi/2\pi$.

In effect, spacetime foam creates a "seeing disk" whose angular diameter is $\sim \Delta\phi/2\pi$.

Shows up in interferometer fringe pattern as decreasing fringe visibility as soon as $\Delta\phi \sim 2\pi \lambda/D$.

Fluctuations in wave-vector direction

[Christianson, Ng, & van Dam]



Spacetime foam-induced fluctuations in wave-vector direction $\sim \Delta\phi/2\pi$

Correlated electric field $|E| \sim \left| \cos\left(\frac{\pi}{2}[2\theta - \Delta\phi/2\pi]\frac{D}{\lambda}\right) \right|$

- For $\Delta\phi = 0$, 1st null at $2\theta = \lambda/D$
- For $\Delta\phi \neq 0$, 1st null for halo at $2\theta - \Delta\phi/2\pi \sim \lambda/D$
 \Rightarrow halo appearance w. half-width $\sim \Delta\phi/2\pi$.

In effect, spacetime foam creates a "seeing disk" whose angular diameter is $\sim \Delta\phi/2\pi$.

Shows up in interferometer fringe pattern as decreasing fringe visibility as soon as $\Delta\phi \sim 2\pi\lambda/D \ll 1$

For the PKS1413+135 image at HST (with $D \simeq 2.4\text{m}$), expect halos at $\Delta\phi \sim 10^{-6} \times 2\pi$.

- Absence of halo rules out convincingly random-walk model ($\Delta\phi \sim 10 \times 2\pi$).
- Fails to test the holographic model ($\Delta\phi \sim 10^{-9} \times 2\pi$) only by 3 orders of magnitude.

Exciting news: the full Very Large Telescope interferometer (comprising four 8.2 m telescopes with baselines up to ~ 200 m) can reach an angular resolution of 1 - 2 milliarcsec ($\sim 5 - 10 \times 10^{-9}$ radians) w. sensitivity ~ 50 mJy in near IR \implies Can potentially detect spacetime foam(!?)

- No need for extra telescope time; can use archived data!
- Next generation of more powerful telescopes: ELT, OWL...
- Alternatives to IR Interometry?

Very Long Baseline Array would require a resolution ~ 4 orders of magnitude finer at radio wavelengths.

Chandra X-ray Observatory, at $\lambda \sim 10^{-8}\text{cm}$, might make up for lack of angular resolution (~ 1 arcsec)?

For the PKS1413+135 image at HST (with $D \simeq 2.4\text{m}$), expect halos at $\Delta\phi \sim 10^{-6} \times 2\pi$.

- Absence of halo rules out convincingly random-walk model ($\Delta\phi \sim 10 \times 2\pi$).
- Fails to test the holographic model ($\Delta\phi \sim 10^{-9} \times 2\pi$) only by 3 orders of magnitude.

Exciting news: the full Very Large Telescope interferometer (comprising four 8.2 m telescopes with baselines up to ~ 200 m) can reach an angular resolution of 1 - 2 milliarcsec ($\sim 5 - 10 \times 10^{-9}$ radians) w. sensitivity ~ 50 mJy in near IR \Rightarrow Can potentially detect spacetime foam(!?)

- No need for extra telescope time; can use archived data!
- Next generation of more powerful telescopes: ELT, OWL...
- Alternatives to IR Interometry?

Very Long Baseline Array would require a resolution ~ 4 orders of magnitude finer at radio wavelengths.

Chandra X-ray Observatory, at $\lambda \sim 10^{-8}\text{cm}$, might make up for lack of angular resolution (~ 1 arcsec)?

From spacetime foam to cosmology

Universe as a computer: (R_H =Hubble radius; T =temp.)

- Known $R_H \Rightarrow$ # operations $\lesssim (R_H/l_P)^2 \sim 10^{123}$
- Stat. mech.: Energy density $\sim T^4$, entropy density $\sim T^3$
 \Rightarrow # bits I (on conventional matter) $\sim (\#op)^{3/4} \lesssim 10^{92}$
- Known I & $R_H \Rightarrow$ distance between neighboring bits $\sim 10^{-3}$ cm and so takes $\sim 10^{-14}$ sec to communicate
- Known density & R_H , via ML, \Rightarrow Op rate $\lesssim 10^{106}$ /sec
- Known I & op rate \Rightarrow bit flips once every 10^{-14} sec

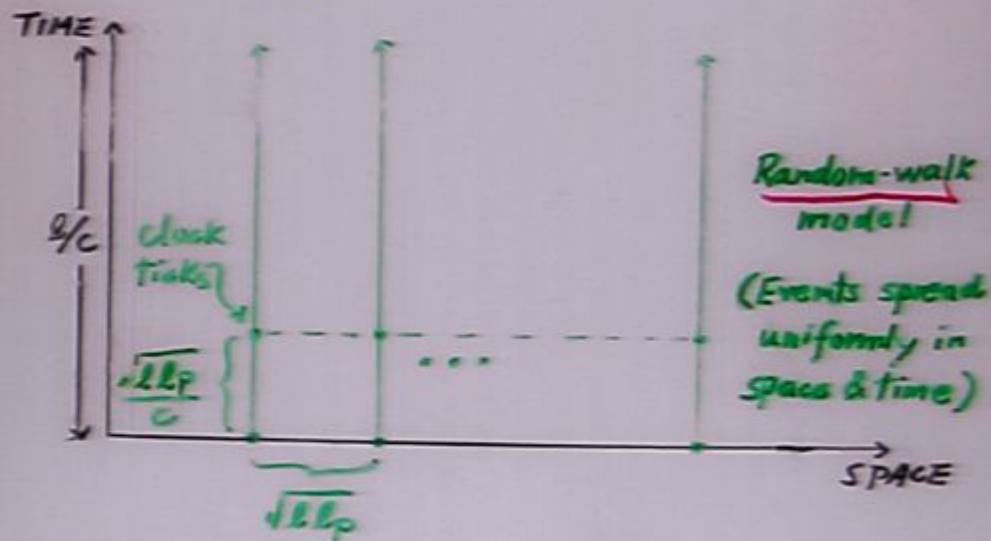
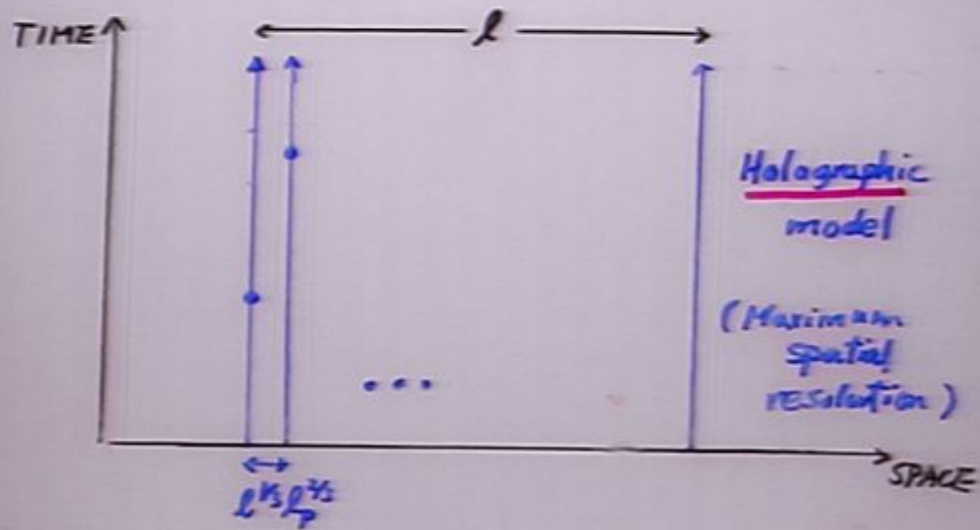
\Rightarrow Storing bits in ordinary matter corresponds to a distribution of events in which each bit flips in the same amount of time it takes to communicate w. a neighboring bit

\Rightarrow The accuracy to which ordinary matter maps out spacetime corresponds to the case of events spread out uniformly in spacetime, i.e., to random-walk model

Random-walk model is ruled out \Rightarrow ST can be mapped to a finer accuracy than that provided by using ordinary matter

$\Rightarrow \exists$ unconventional (read dark) matter/energy with which the universe can map out its own spacetime geometry

- Observed critical cosmic ρ supports holographic model (?)



For $l \sim 10^{28} \text{ cm} \sim R_H$, $\frac{\sqrt{l} l_p}{c} \sim 10^{-14} \text{ sec}$
 (clock ticks \rightarrow bit flips) $\sqrt{l} l_p \sim 10^{-3} \text{ cm}$

From spacetime foam to cosmology

Universe as a computer: (R_H =Hubble radius; T =temp.)

- Known $R_H \Rightarrow$ # operations $\lesssim (R_H/l_P)^2 \sim 10^{123}$
- Stat. mech.: Energy density $\sim T^4$, entropy density $\sim T^3$
 \Rightarrow # bits I (on conventional matter) $\sim (\#op)^{3/4} \lesssim 10^{92}$
- Known I & $R_H \Rightarrow$ distance between neighboring bits
 $\sim 10^{-3}$ cm and so takes $\sim 10^{-14}$ sec to communicate
- Known density & R_H , via ML, \Rightarrow Op rate $\lesssim 10^{106}$ /sec
- Known I & op rate \Rightarrow bit flips once every 10^{-14} sec

\Rightarrow Storing bits in ordinary matter corresponds to a distribution of events in which each bit flips in the same amount of time it takes to communicate w. a neighboring bit

\Rightarrow The accuracy to which ordinary matter maps out spacetime corresponds to the case of events spread out uniformly in spacetime, i.e., to random-walk model

Random-walk model is ruled out \Rightarrow ST can be mapped to a finer accuracy than that provided by using ordinary matter

$\Rightarrow \exists$ **unconventional (read dark) matter/energy** with which the universe can map out its own spacetime geometry

- **Observed critical cosmic ρ supports holographic model (?)**

STF \Rightarrow HOLOGRAPHIC FOAM COSMOLOGY

2 main features: (H, R_H = Hubble parameter, radius)

- critical cosmic energy $\rho \sim (H/l_P)^2 \sim (R_H l_P)^{-2}$
- Universe contains $I = (R_H/l_P)^2$ bits of info

Average energy carried by each bit is $\rho R_H^3 / I \sim R_H^{-1}$

Such long-wavelength bits carry negligible kinetic energy

$KE \sim 0 \Rightarrow P \sim -\rho \Rightarrow$ acceleration, like quintessence?

For $\rho \sim H^2/G$, Friedmann Eq. yields ($a(t)$ = scale factor)

$$H \propto 1/a, a \propto t, \text{ and } P = -\rho/3$$

Whether expansion accel or decel depends on interactions between DE and DM (can accommodate both) [Zimdahl]

Each unconventional bit flips once in time $I/\nu \sim R_H$: inert

With $\lambda \sim R_H$, unconventional bits sit on top of one another

\Rightarrow uniform distribution of energy density

\Rightarrow effective cosmological "constant" $\Lambda \sim R_H^{-2}$ (for $P \sim -\rho$)

A LOGICAL SPECULATION

Assume DE is composed of long wavelength "particles"

How different are these "particles"?

Consider $N \sim (R_H/l_P)^2$ such "particles" obeying Boltzmann statistics in volume $V \sim R_H^3$ at $T \sim R_H^{-1}$

The partition function $Z_N = (N!)^{-1}(V/\lambda^3)^N \Rightarrow$ Entropy of the system is $S = N[\ln(V/N\lambda^3) + 5/2]$ with $\lambda \sim T^{-1}$

But $V \sim \lambda^3$, so S becomes **negative** unless $N \sim 1$ which is equally **nonsensical**

Solution: The N inside the log in S , i.e. the Gibbs factor $(N!)^{-1}$ in Z_N , must be absent \Rightarrow the N "particles" are **distinguishable!**

Then $S = N[\ln(V/\lambda^3) + 3/2]$, +ve $S \sim N$

The only known consistent statistics in greater than 2 space dimensions without the Gibbs factor is the **quantum Boltzmann statistics**, aka **infinite statistics**

A logical speculation: The "particles" constituting dark energy obey infinite statistics, rather than the familiar Fermi or Bose statistics. This is the overriding difference between DE and conventional matter.

In the framework of M-theory, $V_{int} \sim M_{pl}^{-3} \sim M_{pl}^{-3}$

A LOGICAL SPECULATION

Assume DE is composed of long wavelength "particles"

How different are these "particles"?

Consider $N \sim (R_H/l_P)^2$ such "particles" obeying Boltzmann statistics in volume $V \sim R_H^3$ at $T \sim R_H^{-1}$

The partition function $Z_N = (N!)^{-1} (V/\lambda^3)^N \Rightarrow$ Entropy of the system is $S = N[\ln(V/N\lambda^3) + 5/2]$ with $\lambda \sim T^{-1}$

But $V \sim \lambda^3$, so S becomes negative unless $N \sim 1$ which is equally nonsensical

Solution: The N inside the log in S , i.e. the Gibbs factor $(N!)^{-1}$ in Z_N , must be absent \Rightarrow the N "particles" are distinguishable!

Then $S = N[\ln(V/\lambda^3) + 3/2]$, +ve $S \sim N$

The only known consistent statistics in greater than 2 space dimensions without the Gibbs factor is the quantum Boltzmann statistics, aka infinite statistics

A logical speculation: The "particles" constituting dark energy obey infinite statistics, rather than the familiar Fermi or Bose statistics. This is the overriding difference between DE and conventional matter.

In the framework of M-theory, V. Jejjala, M. Kavcic and D. Minic [hep-th:0705.4581] have made a similar suggestion

Fine Structure of Dark Energy and New Physics

Vishnu Jejjala,^{1*} Michael Kavic,^{2†} and Djordje Minic^{2‡}

¹*Department of Mathematical Sciences,
Durham University,
South Road, Durham DH1 3LE, U.K.*

²*Institute for Particle, Nuclear, and Astronomical Sciences,
Department of Physics, Virginia Tech,
Blacksburg, VA 24061, U.S.A.*

Abstract

Following our recent work on the cosmological constant problem, in this letter we make a specific proposal regarding the fine structure (*i.e.*, the spectrum) of dark energy. The proposal is motivated by a deep analogy between the blackbody radiation problem, which led to the development of quantum theory, and the cosmological constant problem, which we have recently argued calls for a conceptual extension of the quantum theory. We argue that the fine structure of dark energy is governed by a Wien distribution, indicating its dual quantum and classical nature. We discuss observational consequences of such a picture of dark energy and constrain the distribution function.

Fine Structure of Dark Energy and New Physics

Vishnu Jejjala,^{1*} Michael Kavic,^{2†} and Djordje Minic^{2‡}

¹*Department of Mathematical Sciences,
Durham University,
South Road, Durham DH1 3LE, U.K.*

²*Institute for Particle, Nuclear, and Astronomical Sciences,
Department of Physics, Virginia Tech,
Blacksburg, VA 24061, U.S.A.*

Abstract

Following our recent work on the cosmological constant problem, in this letter we make a specific proposal regarding the fine structure (i.e., the spectrum) of dark energy. The proposal is motivated by a deep analogy between the blackbody radiation problem, which led to the development of quantum theory, and the cosmological constant problem, which we have recently argued calls for a conceptual extension of the quantum theory. We argue that the fine structure of dark energy is governed by a Wien distribution, indicating its dual quantum and classical nature. We discuss observational consequences of such a picture of dark energy and constrain the distribution function.

$$N_i = a_i^\dagger a_i + \sum_m a_m^\dagger a_i^\dagger a_i a_m + \sum_{m_1, m_2} a_{m_1}^\dagger a_{m_2}^\dagger a_i^\dagger a_i a_{m_2} a_{m_1} + \dots$$

... does not affect the formulation of a consistent non-relativistic theory. Cluster the CPT theorem, and a version of Wick's theorem are still valid, and the theorem implies that particles obeying infinite statistics can be of any spin. theory with infinite statistics remains unitary. However, there does not exist a and quantized local field theory. The presence of non-locality while appearing to may in fact be a virtue. Because there is not a well-defined local field theory, theory arguments will miss the possibility that dark energy is associated with infinite statistics.

[21] a holographic model of spacetime foam was considered. It was argued that spacetime foam implies the existence of a type of dark energy quanta obeying infinite statistics. This is intriguing as this was conjectured using a different formalism from the usual.

... the various instances in which infinite statistics play a role (i.e., black hole theory, holographic spacetime foam, as well as our formulation of a background matrix theory), we note a common feature. In each of these the holographic central. Holographic theories possess a manifestly non-local quality in that the degrees of freedom must know something about the boundary. Thus the non-locality of infinite statistics and the non-locality present in holographic theories (This was also argued in [21].) Perhaps the presence of infinite statistics in relational systems is indicative of a holographic view of spacetime.

... point of this letter is that *the spectral distribution of dark energy that follows infinite statistics is the familiar Wien distribution.* First recall that in the context of the

$$N_i = a_i^\dagger a_i + \sum_m a_m^\dagger a_i^\dagger a_i a_m + \sum_{m_1, m_2} a_{m_1}^\dagger a_{m_2}^\dagger a_i a_i a_{m_2} a_{m_1} + \dots$$

This non-locality does not affect the formulation of a consistent non-relativistic theory. The decomposition, the CPT theorem, and a version of Wick's theorem are still valid. The spin statistics theorem implies that particles obeying infinite statistics can be consistently quantized. A quantum theory with infinite statistics remains unitary. However, there does not seem to be a consistent second quantized local field theory. The presence of non-locality while quantizing a theory that would otherwise be a liability may in fact be a virtue. Because there is not a well-defined local effective field theory, arguments will miss the possibility that dark energy is associated with quanta of infinite statistics.

Recently in [21] a holographic model of spacetime foam was considered. It was argued that this type of spacetime foam implies the existence of a type of dark energy quanta with infinite statistics. This is intriguing as this was conjectured using a different formulation of the current proposal.

If we consider the various instances in which infinite statistics play a role (i.e., Matrix theory, holographic spacetime foam, as well as our formulation of a consistent independent Matrix theory), we note a common feature. In each of these theories, the principle [22] is central. Holographic theories possess a manifestly non-local quality. The internal degrees of freedom must know something about the boundary. Thus the non-locality present in systems obeying infinite statistics and the non-locality present in holographic theories may be related. (This was also argued in [21].) Perhaps the presence of infinite statistics in quantum gravitational systems is indicative of a holographic view of spacetime.

The central point of this letter is that *the spectral distribution of dark energy quanta from infinite statistics is the familiar Wien distribution*. First recall that in the context of a black body, the spectral distribution may be expressed as

INFINITE STATISTICS

[Doplicher, Haag, & Roberts; Govorkov; Greenberg]

- q -deformation of the Heisenberg algebra ($-1 \leq q \leq 1$)

$$a_k a_l^\dagger - q a_l^\dagger a_k = \delta_{kl}; \quad a_k |0\rangle = 0$$

($q = \pm 1$ corresponds to bosons/fermions)

- Inner product of two N -particle states is

$$\langle 0 | a_{i_1} \dots a_{i_2} a_{j_2}^\dagger \dots a_{j_N}^\dagger | 0 \rangle = \delta_{i_1 j_1} \dots \delta_{i_N j_N}$$

2 states obtained from acting with the same a and a^\dagger in a different order are mutually orthogonal: the states may be in any representation of the permutation group

- The partition function is

$$Z = \sum e^{-\beta H}, \text{ NO Gibbs factor}$$

- \sim statistics of identical particles with an ∞ of internal degrees of freedom [$SU(\infty)$] \iff statistics of nonidentical particles (distinguishable by their internal states)

INFINITE STATISTICS

[Doplicher, Haag, & Roberts; Govorkov; Greenberg]

- q -deformation of the Heisenberg algebra ($-1 \leq q \leq 1$)

$$a_k a_l^\dagger - q a_l^\dagger a_k = \delta_{kl}; \quad a_i |0\rangle = 0$$

($q = \pm 1$ corresponds to bosons/fermions)

- Inner product of two N -particle states is

$$\langle 0 | a_{i_1} \dots a_{i_N} a_{j_1}^\dagger \dots a_{j_N}^\dagger | 0 \rangle = \delta_{i_1 j_1} \dots \delta_{i_N j_N}$$

2 states obtained from acting with the same a and a^\dagger in a different order are mutually orthogonal: the states may be in any representation of the permutation group

- Inner product of two N-particle states is

$$\langle 0 | a_{i_1} \dots a_{i_s} a_{j_1}^\dagger \dots a_{j_N}^\dagger | 0 \rangle = \delta_{i_1 j_1} \dots \delta_{i_N j_N}$$

2 states obtained from acting with the same a and a^\dagger in a different order are mutually orthogonal: the states may be in any representation of the permutation group

- The partition function is

$$Z = \sum e^{-\beta H}, \text{ NO Gibbs factor}$$

- \sim statistics of identical particles with an ∞ of internal degrees of freedom $[SU(\infty)] \iff$ statistics of nonidentical particles (distinguishable by their internal states)

Theories of particles obeying ∞ statistics are non-local
 [Fredenhagen; Greenberg]

Number operator, Hamiltonian, etc., are both nonlocal and nonpolynomial in the field operators:

$$N_i = a_i^\dagger a_i + \sum_m a_m^\dagger a_i^\dagger a_i a_m + \sum_{m,n} a_m^\dagger a_n^\dagger a_i^\dagger a_i a_n a_m + \dots$$

- difficult to formulate a relativistic version of the theory, i.e., \nexists consistent 2nd quantized local field theory; but a non-relativistic theory can be developed.

Nonlocality in ∞ statistics can be a virtue

- may be related to nonlocality in holographic principle

Examples:

- charged extremal black holes [Strominger];
- holographic quantum foam; • M-theory

Holographic principle is a crucial ingredient of quantum gravity \implies QG and ∞ stat fit together nicely

- Conjecture: (non-perturbative) dynamics of gravity is unitary but nonlocal

[Giddings]

...

Nonlocality in ∞ statistics can be a virtue

- may be related to nonlocality in holographic principle

Examples:

- charged extremal black holes [Strominger];
- holographic quantum foam; • M-theory

Holographic principle is a crucial ingredient of quantum gravity \implies QG and ∞ stat fit together nicely

- Conjecture: (non-perturbative) dynamics of gravity is unitary but nonlocal

[Giddings]

...

SUMMARY

- Spacetime undergoes quantum fluctuations \Rightarrow uncertainties in spacetime measurements.
- Spacetime fluctuations scale as the **cube root** of distances. (Supported by an argument in loop QG approach)
- Discussion only depends on the quantum characteristics of spacetime measurements, and NOT on any particular theory.
- Detecting the tiny effects of spacetime fluctuations is difficult, but not impossible. May be within striking distance of detecting spacetime foam when the Very Large Telescope interferometer reaches its design performance. (Indirect detection: Use of Bose-Einstein condensates)
- Spacetime foam \Rightarrow cosmology: \exists Dark energy/matter
- **Holographic Foam Cosmology:**
critical cosmic energy density: flatness problem \checkmark
 $P \sim -p/3$: accelerating or decelerating expansion depends on interactions with matter (flexible?)
- Speculation: "particles" constituting DE obey ∞ statistics (Supported by an argument in M-theory approach)
QG and ∞ statistics appear to fit nicely together
Conjecture: QG is unitary but non-local
- Phenomenology of HFC yet to be studied ...

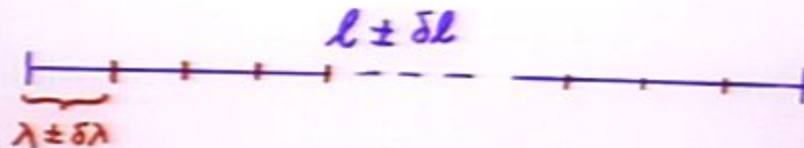
SUMMARY

- Spacetime undergoes quantum fluctuations \Rightarrow uncertainties in spacetime measurements.
- Spacetime fluctuations scale as the **cube root** of distances. (Supported by an argument in loop QG approach)
- Discussion only depends on the quantum characteristics of spacetime measurements, and NOT on any particular theory.
- Detecting the tiny effects of spacetime fluctuations is difficult, but not impossible. **May be within striking distance of detecting spacetime foam when the Very Large Telescope interferometer reaches its design performance.** (Indirect detection: Use of Bose-Einstein condensates)
- Spacetime foam \Rightarrow cosmology: \exists Dark energy/matter
- **Holographic Foam Cosmology:**
critical cosmic energy density: flatness problem \checkmark
 $P \sim -\rho/3$: accelerating or decelerating expansion depends on interactions with matter (flexible?)
- **Speculation: "particles" constituting DE obey ∞ statistics** (Supported by an argument in M-theory approach)
QG and ∞ statistics appear to fit nicely together
Conjecture: QG is unitary but non-local
- Phenomenology of HFC yet to be studied ...

- Spacetime undergoes quantum fluctuations \Rightarrow uncertainties in spacetime measurements.
- Spacetime fluctuations scale as the **cube root** of distances. (Supported by an argument in loop QG approach)
- Discussion only depends on the quantum characteristics of spacetime measurements, and NOT on any particular theory.
- Detecting the tiny effects of spacetime fluctuations is difficult, but not impossible. May be within striking distance of detecting spacetime foam when the Very Large Telescope interferometer reaches its design performance. (Indirect detection: Use of Bose-Einstein condensates)
- Spacetime foam \Rightarrow cosmology: \exists Dark energy/matter
- Holographic Foam Cosmology: **critical cosmic energy density**: flatness problem ✓
 $P \sim -\rho/3$: accelerating or decelerating expansion depends on interactions with matter (flexible?)
- Speculation: "particles" constituting DE obey ∞ statistics (Supported by an argument in M-theory approach)
 QG and ∞ statistics appear to fit nicely together
 Conjecture: QG is unitary but non-local
- Phenomenology of HFC yet to be studied ...

Cumulative effects of spacetime fluctuations

Divide distance l into l/λ equal parts each of length λ (for any $l_p \leq \lambda \leq l$)



Question: Starting with $\delta\lambda$ from each part, how do the l/λ parts add up to δl for the whole distance l ?

I.e., find the cumulative factor C in $\delta l = C \delta\lambda$

$$\delta l \sim l^{1/3} l_p^{2/3}; \quad \delta\lambda \sim \lambda^{1/3} l_p^{2/3}$$

\Downarrow

$$C = \left(\frac{l}{\lambda}\right)^{1/3}$$

Cumulative Factor = $(\# \text{intervals})^{1/3}$

(\sim Brownian motion with self-similarity parameter 1/3)

Random walk model ($\delta l \sim l^{1/2} l_p^{1/2}$): $C = (l/\lambda)^{1/2}$

Completely anti-correlation model ($\delta l \sim l_p$): $C = 1$



δl (anti-correlation \Leftarrow ; correlation \Rightarrow)