

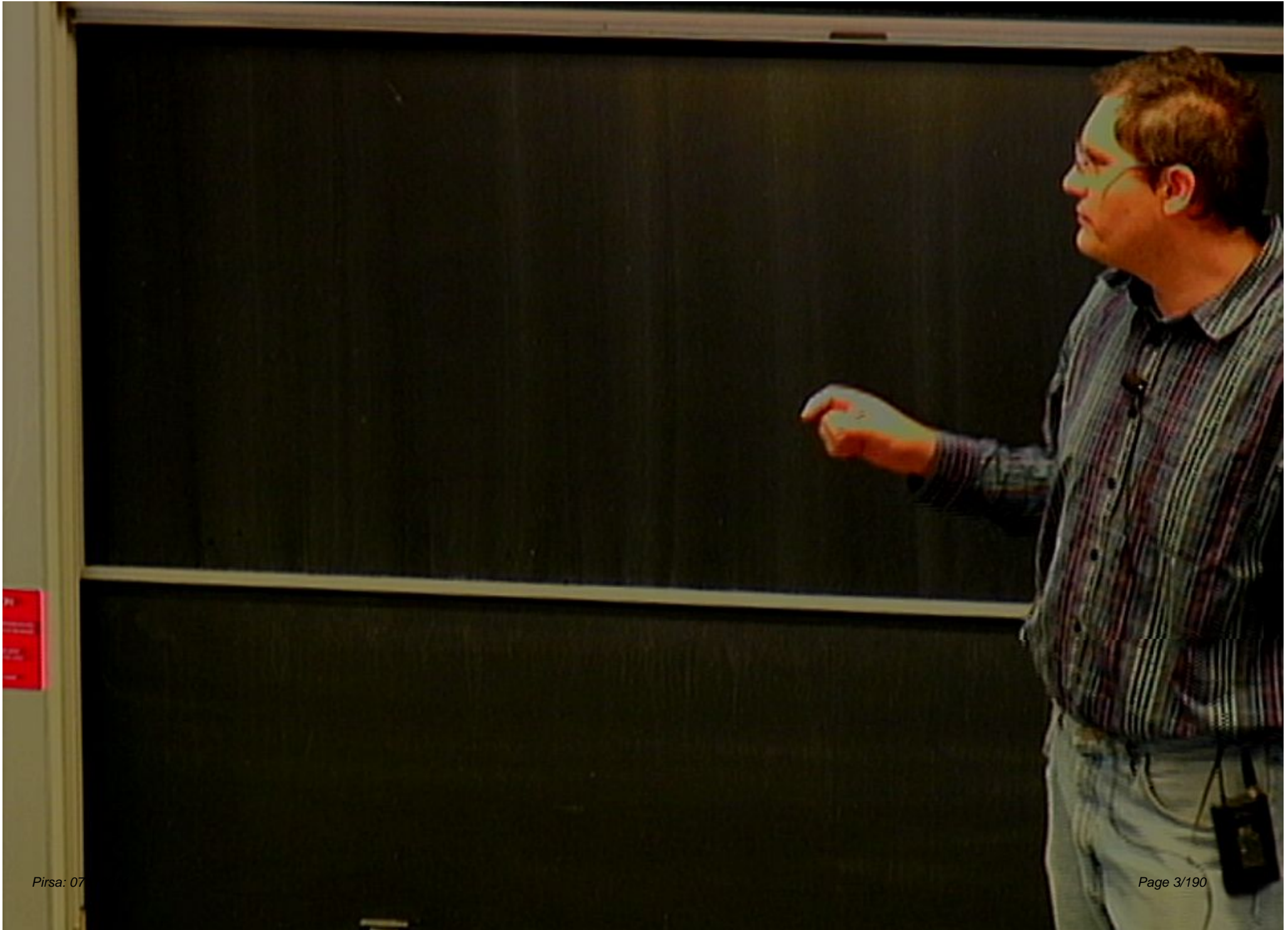
Title: Intro to Supersymmetry 15

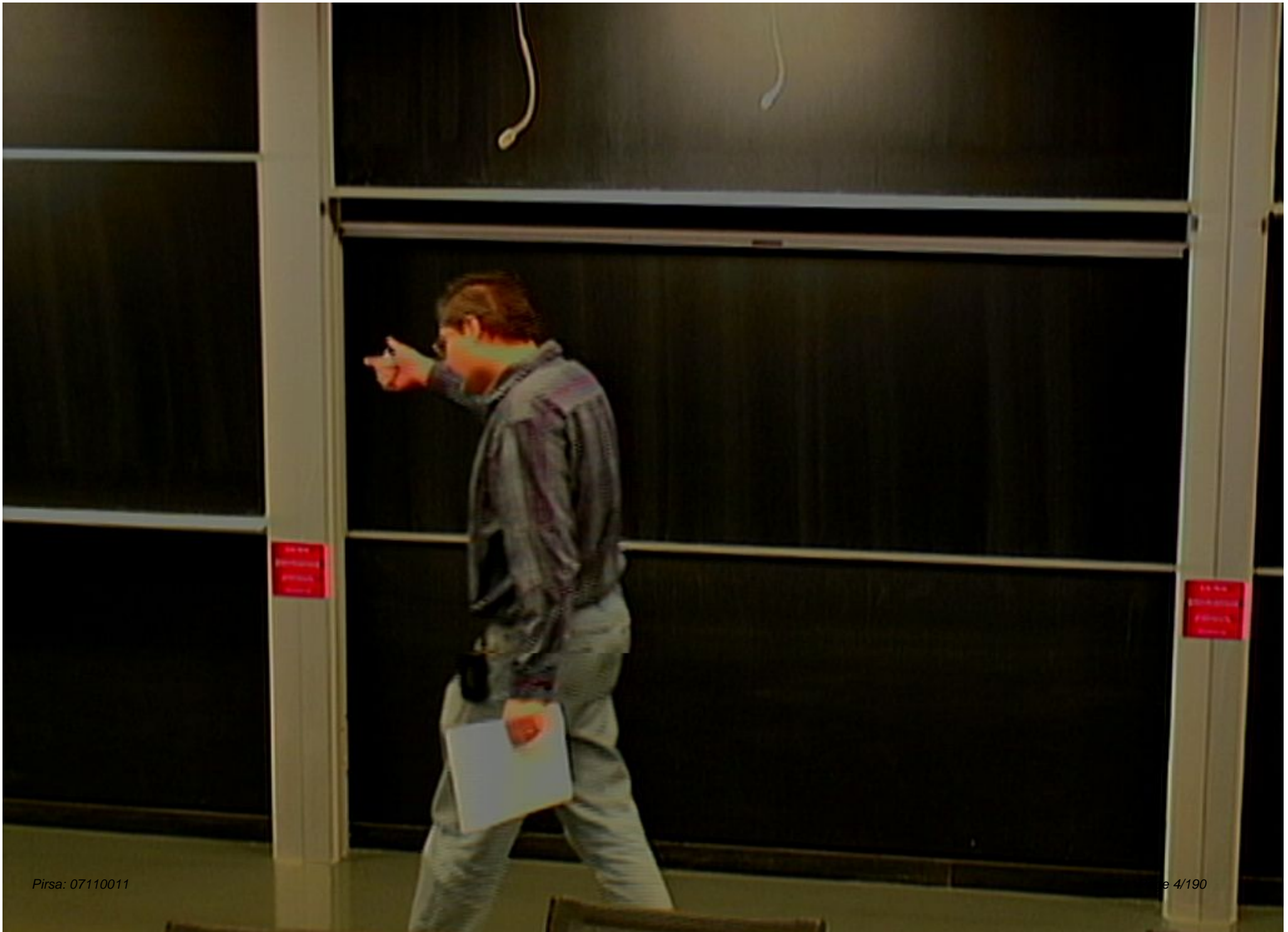
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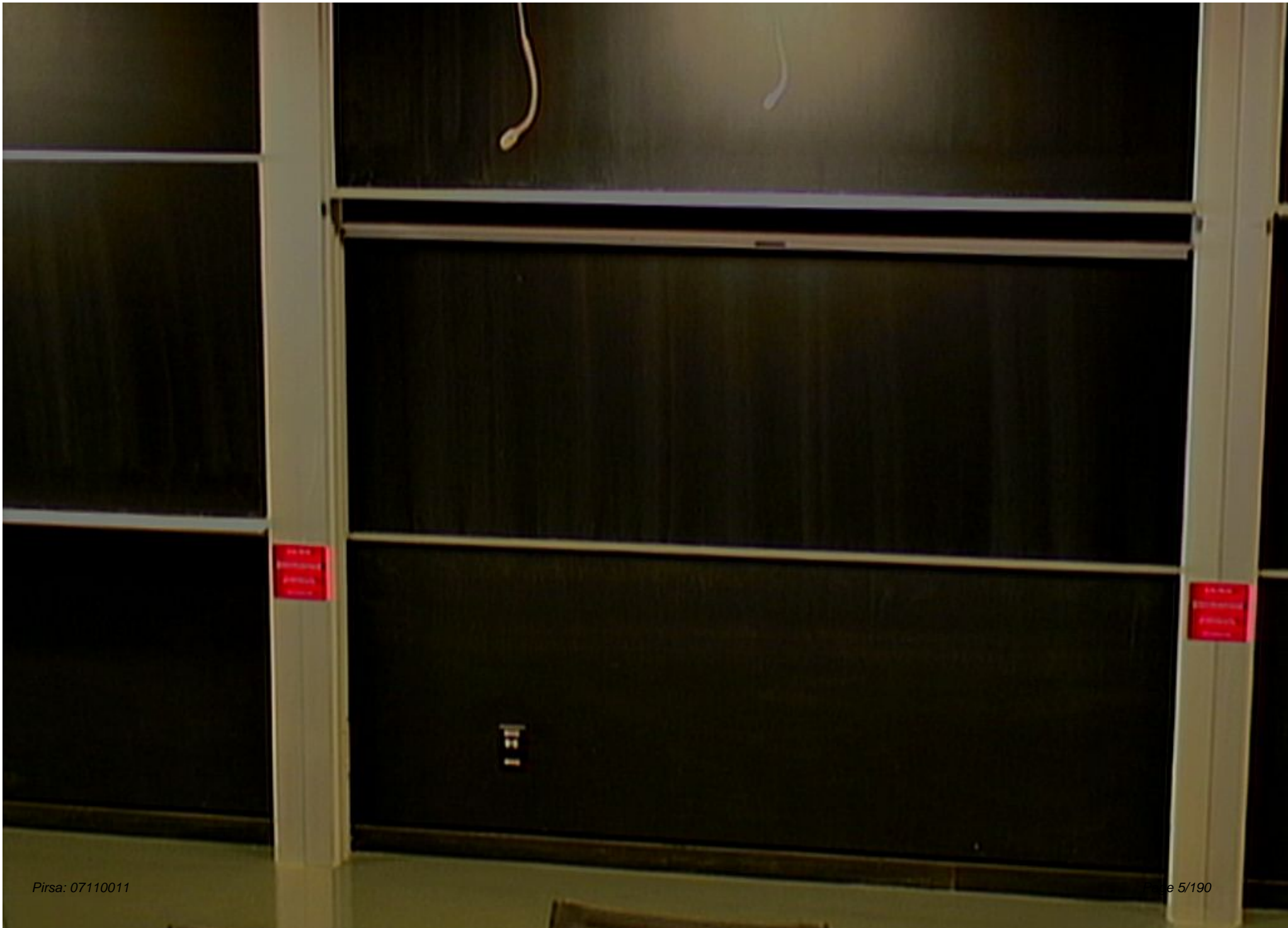
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Abstract:









"kinetic" scaling



"kinetic" scaling

w_k

"kinetic" scaling



are n

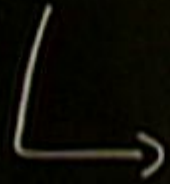
"kinetic" scaling



w/ renormalization

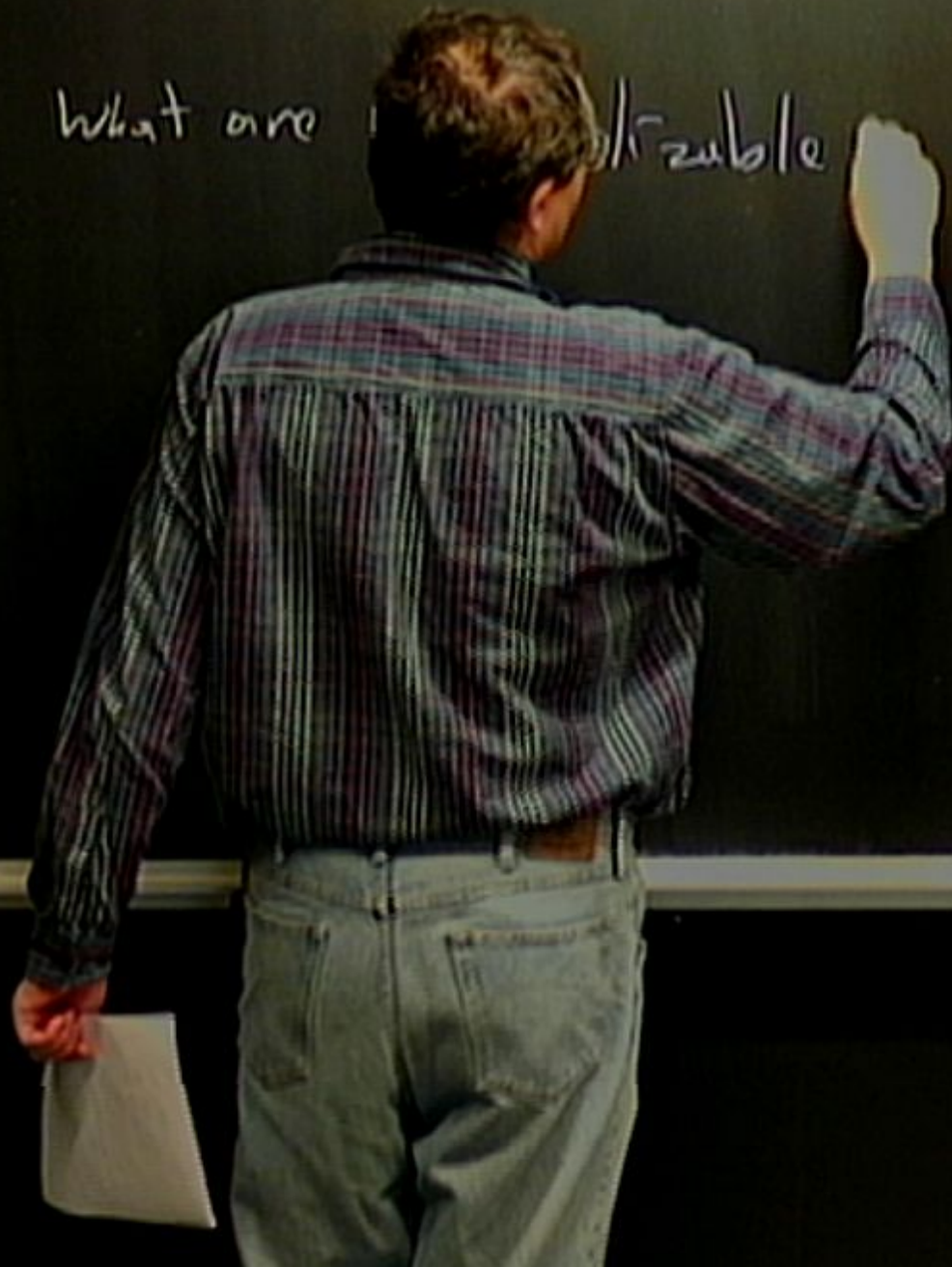


"kinetic" scaling



What are

self-similar



"kinetic" scaling



What are renormal interactions?

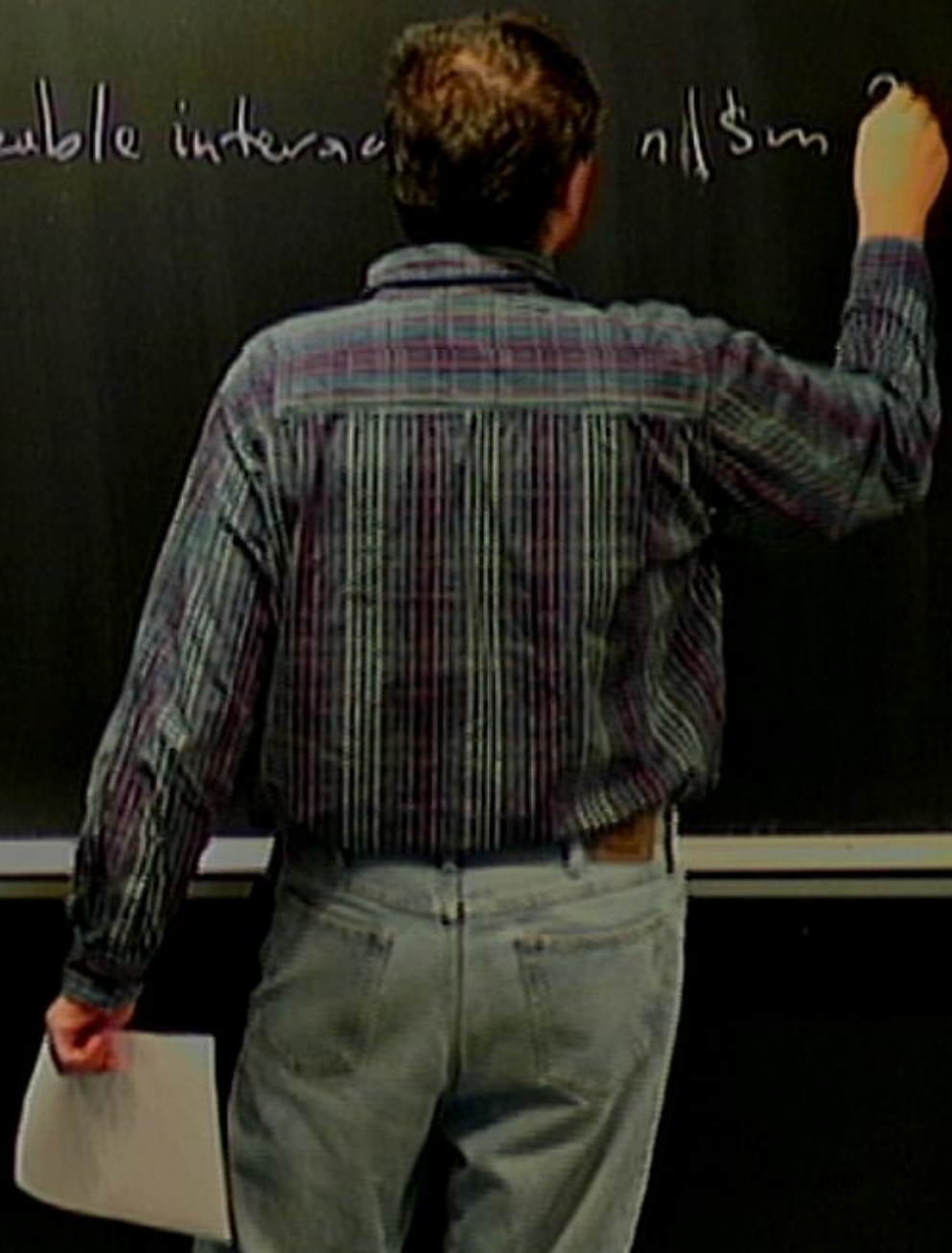


"kinetic" scaling

↳ what are renormalizable interactions in ns

"kinetic" scaling

↳ what are renormalizable interactions n/d sum?



"kinetic" scaling



are renormalizable interaction in n/d dim?



"kinetic" scaling

↳ what are renormalizable interaction in $n=4$ dim?

⇒ WZ

"kinetic" scaling

↳ what are renormalizable interaction in n/dim?

⇒ WZ

⇒ n/dim scaling

Σ $g_i \varphi^i$

"kinetic" scaling

↳ what are renormalizable interaction in n/dim?

⇒ WZ

⇒ n/dim scaling?

$$W(\varphi) = \sum_i g_i \varphi^i$$

infinite # of term

⇒ nonrenorm interact

hism \rightarrow must be an effective field theory.

hism \rightarrow must be an effective field theory.
 \rightarrow vacuum properties.



$h_{\text{sm}} \rightarrow$ must be an effective field theory,
 \rightarrow vacuum properties.

\Rightarrow



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\Rightarrow kinetic terms should no matter

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hls m \rightarrow must be an effective field theory,

\rightarrow vacuum properties.

\Rightarrow kinetic terms should no matter

\cdot $[\rho] = 0$



nlsm \rightarrow must be an effective field theory.

\rightarrow vacuum properties.

\Rightarrow kinetic terms should matter

• $[\varphi] = 0$

\uparrow dimensionless assignment

$$\Rightarrow I_n W \Rightarrow [g_i] = 3$$

$\Rightarrow \Gamma_n W \Rightarrow [\gamma_i] = 3$
(all couplings are equally important)

\Rightarrow In $W \Rightarrow [\gamma_i] = 3$
(all couplings are equally important)

$\Rightarrow \Rightarrow$ all term have scaling dim $+2$

$\Rightarrow \text{In } W \Rightarrow [g_i] = 3$
 $[w] = 3$ (all couplings are equally important)

$\Rightarrow \text{In } K \Rightarrow$ all terms have scaling dim + 2

$$[k] = 2$$

Example

$$\mathcal{L} = \frac{1}{2} m \dot{\varphi}^2 - V(\varphi)$$

Example

$$\mathcal{L} = -\frac{1}{2} \partial^\mu \varphi \partial_\mu \varphi - V(\varphi)$$

$$V(\varphi) = -\frac{m^2}{2} \varphi^2 + \lambda \varphi^8 \quad \begin{array}{l} m^2 > 0 \\ \lambda > 0 \end{array}$$

Example

$$\mathcal{L} = -\frac{1}{2} \partial^\mu \varphi \partial_\mu \varphi - V(\varphi)$$

$$V(\varphi) = -\frac{m^2}{2} \varphi^2 + \lambda \varphi^8$$

$$m^2 > 0$$

$$\lambda > 0$$

\Rightarrow If we are to use kinetic scaling

$$[\varphi] = 1$$

$$[\lambda] = -4$$

$$[\lambda] = 4$$

⇒ Kinetic terms should be wa

• $[\mathcal{P}] = 0$

↑ dimensionless assignment
(vacuum scaling)

1 dimensionless assignment
(vacuum scaling)

In vacuum scaling



1 dimensionless assignment
(vacuum scaling)

In vacuum scaling

$$\hat{p} = \frac{p}{\Lambda}$$

1 dimensionless assignment
(vacuum scaling)

In vacuum scaling

$$\hat{\phi} = \frac{\phi}{\Lambda} \rightarrow \text{out of scale of eff. field theory.}$$

1 dimensionless assignment
(vacuum scaling)

In vacuum scaling

$$[\varphi] = 0$$

$$\hat{\varphi} = \frac{\varphi}{\Lambda} \rightarrow \text{out of scale of efr. field theory.}$$

1 dimensionless assignment
(vacuum scaling)

In vacuum scaling

$$[\hat{\varphi}] = 0$$

$\hat{\varphi} = \frac{\varphi}{\Lambda}$ → out of scale of eff. field theory.

$$\mathcal{L} = -\frac{\Lambda^2}{2} \partial_\mu \hat{\varphi} \partial^\mu \hat{\varphi} + \frac{m^2 \Lambda^2}{2} \hat{\varphi}^2 - \lambda \Lambda^8 (\hat{\varphi})^8$$

$\Rightarrow \Gamma_n W \Rightarrow [\Gamma_n] = 3$
 $[\Gamma_n] = 3$
(all couplings are equally important)

$\Rightarrow \Gamma_n K \Rightarrow$ all term have $1 + ?$

$$[\Gamma_n] = 2$$

vacuum scaling

$$[\hat{\varphi}] = 0$$

$\sim \frac{\varphi}{\Lambda}$ \rightarrow out of scale of eff. field theory.

$$\mathcal{L} = -\frac{\Lambda^2}{2} \partial_\mu \hat{\varphi} \partial^\mu \hat{\varphi} + \underbrace{\frac{m^2 \Lambda^2}{2} \hat{\varphi}^2}_{[\text{m}^2 \Lambda^2] = +4} - \underbrace{\lambda \Lambda^8 (\hat{\varphi})^8}_{[\lambda \Lambda^8] = -4 + 8 = +4}$$

In vacuum scaling

$$[\hat{\phi}] = 0$$

$\hat{\phi} = \frac{\varphi}{\Lambda}$ → out of scale of eff. field theory.

$$\mathcal{L} = -\frac{\Lambda^2}{2} \partial_\mu \hat{\phi} \partial^\mu \hat{\phi} + \underbrace{\frac{m^2 \Lambda^2}{2} \hat{\phi}^2}_{[m^2 \Lambda^2] = +4} - \underbrace{\lambda \Lambda^8 (\hat{\phi})^8}_{[\lambda \Lambda^8] = -4 + 8 = 4}$$

$$\partial_\mu \langle \vec{\phi} \rangle = 0$$

In vacuum $\vec{\phi} = \text{const}$

$$\partial_{\mu} \langle \hat{\varphi} \rangle = 0$$

In vacuum $\hat{\varphi} = \text{const}$

$$\hat{\varphi} \propto \int_{\mathcal{D}_0} e^{i\omega t - i\vec{k}\vec{x}}$$

$$\int \langle \hat{\phi} \rangle = 0$$

In vacuum $\hat{\phi} = \text{const}$

$$\hat{\phi} \propto \int_{\mathcal{D}_0} e^{i\omega t - i\vec{k}\vec{x}} \quad \left(\begin{array}{l} k^2 \text{ is small} \\ k^2 = -\omega^2 + |\vec{k}|^2 \\ k^2 \ll \Lambda^2 \end{array} \right)$$

$$\int_k \langle \hat{\varphi} \rangle = 0$$

In vacuum $\hat{\varphi} = \text{const}$

$$\hat{\varphi} \propto \int_0 \cdot e^{i\omega t - i\vec{k}\vec{x}}$$

$$\omega^2 + |\vec{k}|^2 \approx \omega^2$$

is small

$$\omega \approx \Lambda^2 k^2 + m^2 \Lambda^2$$

$$\int_k \langle \hat{\phi} \rangle = 0$$

In vacuum $\hat{\phi} = \text{const}$

$$\hat{\phi} \propto \int_0 \cdot e^{i\omega t - i\vec{k}\vec{x}} \quad (k^2 \text{ is small})$$

$$k^2 = -\omega^2 + |\vec{k}|^2$$

$$\mathcal{L} \propto \Lambda^2 k^2 + m^2 \Lambda^2 + \lambda \Lambda^4$$

$$k^2 \ll \Lambda^2$$

$$\text{In the limit } \frac{|\vec{k}|^2}{\Lambda^2} \rightarrow 0 \quad \frac{|\vec{k}|^4}{m^2} \rightarrow 0$$

$$\langle \hat{p} \rangle = 0$$

In vacuum $\hat{\phi} = \text{const}$

$$\hat{\phi} \propto \int_0^{\infty} e^{i\omega t - i\vec{k}\vec{x}} \quad (k^2 \text{ is small})$$

$$k^2 = -\omega^2 + |\vec{k}|^2$$

$$k^2 \ll \Lambda^2$$

$$\omega \propto \cancel{\Lambda k^2} + m^2 \Lambda^2 + \lambda \Lambda^4$$

In the limit $\frac{|\vec{k}|^2}{\Lambda^2} \rightarrow 0 \quad \frac{|\vec{k}|^4}{m^2} \rightarrow 0$

$$\int_{\psi} \langle \psi | \psi \rangle = 0$$

In vacuum $\phi = \text{const}$

$$\hat{\phi} \propto \int_{\mathcal{D}_0} e^{i\omega t - i\vec{k}\vec{x}} \quad (k^2 \text{ is small})$$

$$k^2 = -\omega^2 + |\vec{k}|^2$$

$$k^2 \ll \Lambda^2$$

$$\mathcal{L} \propto \cancel{\Lambda^2 k^2} + m^2 \Lambda^2 + \lambda \Lambda^4$$

In the limit $\frac{|\vec{k}|^2}{\Lambda^2} \rightarrow 0$ $\frac{|\vec{k}|^4}{m^2} \rightarrow 0$ (low energy)

"kinetic" scaling implies that $\langle \rho \rangle \sim 0$

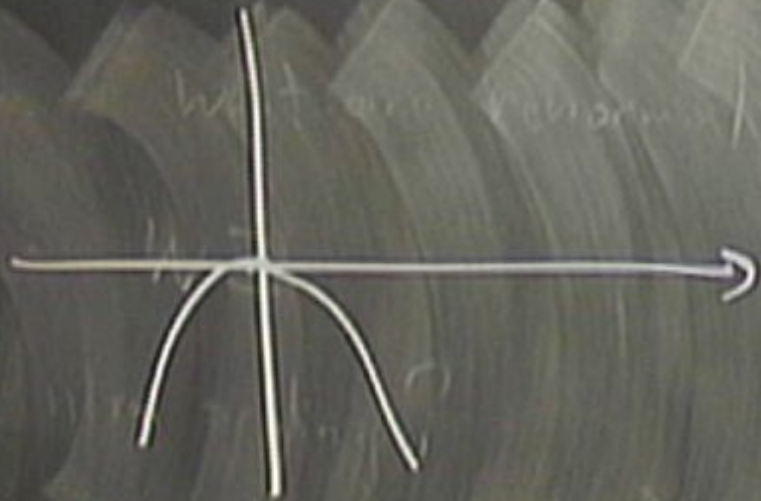
What are the relevant interactions in $1/\beta \ln Z$?

EM

infinite # of terms
→ however, irrelevant

$$W(\phi) = \sum_i \phi_i^2$$

"kinetic" scaling implies that $\langle \rho \rangle \sim 0$

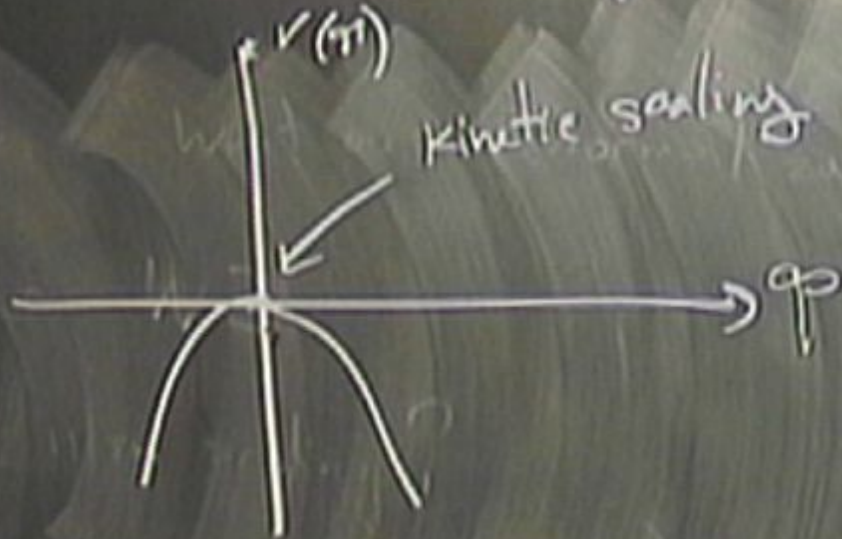


What are relevant/irrelevant interactions in $1/S$ expansion?

$$W(\mathbf{r}) = \sum_i g_i \psi_i$$

Infinite K of fermions
→ hierarchical interactions

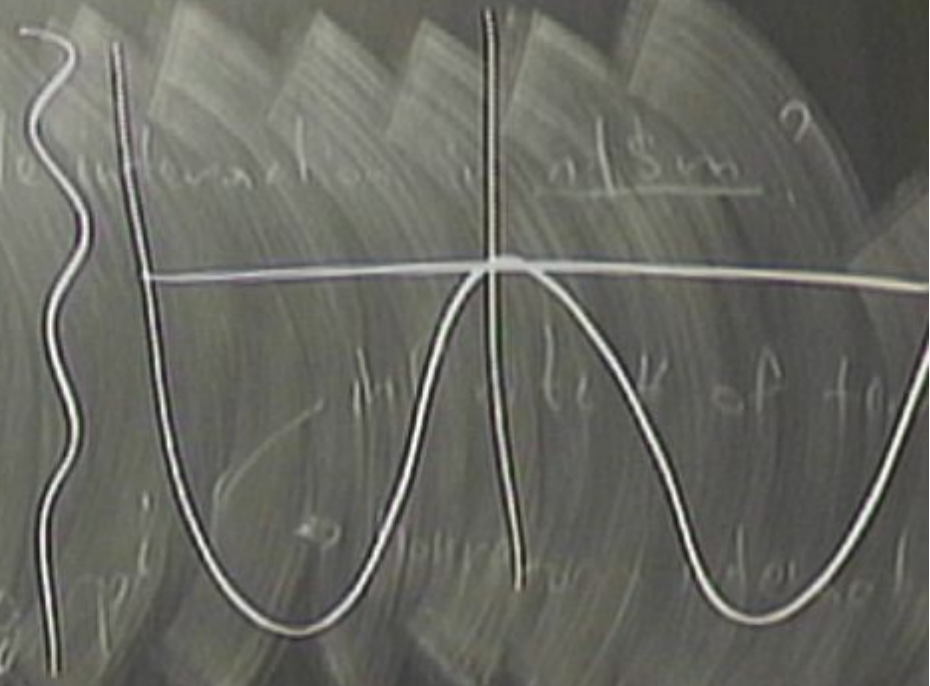
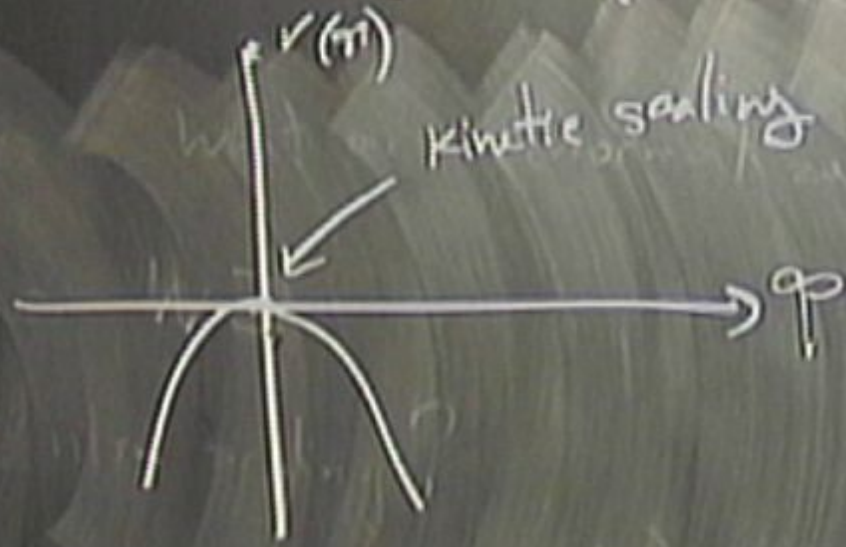
"kinetic" scaling implies that $\langle \rho \rangle \sim 0$



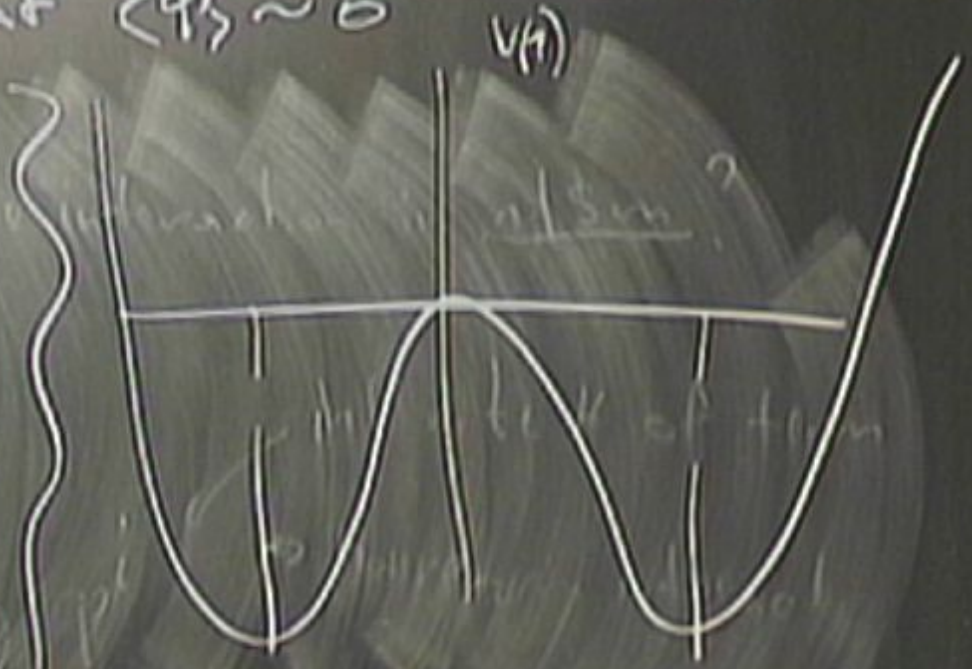
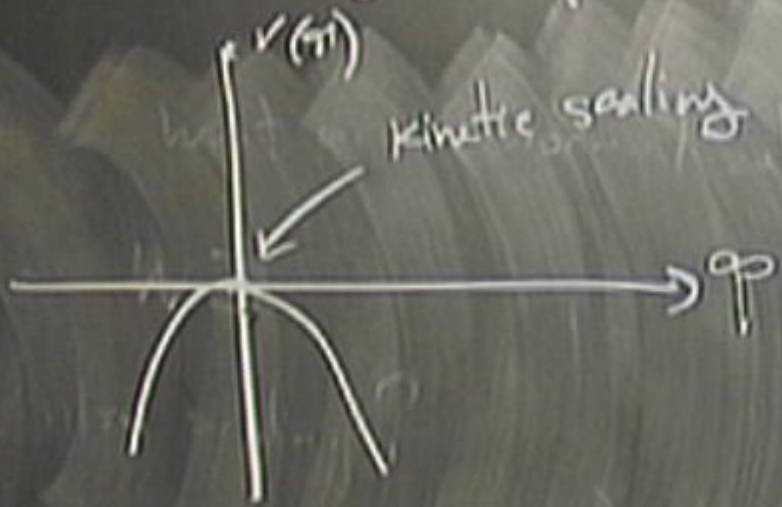
kinetic scaling



kinetic scaling implies that $\langle \eta \rangle \sim 0$



"kinetic" scaling implies that $\langle \rho \rangle \sim 0$



$$v'(r) \Big|_{r=r_v} = 0$$

$$-m^2 r_v + 8 \lambda r_v^7 = 0$$

$$v'(r) \Big|_{r=r_v} = 0$$

$$-m^2 \rho_v + 8 \lambda \rho_v^7 = 0$$

$$\rho_v = \pm \left(\frac{m^2}{8\lambda} \right)^{1/6}$$

$$v'(\varphi) \Big|_{\varphi = \varphi_v} = 0$$

$$-m^2 \varphi_v + 8 \lambda \varphi_v^7 = 0$$

$$\varphi_v = \pm \left(\frac{m^2}{8\lambda} \right)^{1/6}$$

$\varphi \leftrightarrow -\varphi$ is spontaneously broken

$$\varphi = \varphi_v + h(x)$$



$$\varphi = \varphi_v + \underbrace{h(x)}_{\text{kinetic scaling}}$$

$$\varphi = \varphi_v + \underbrace{h(x)}_{\text{kinetic scaling}}$$

V_{eff}



$$\varphi = \varphi_v + \underbrace{h(x)}$$

kinetic scaling

$$V_{\text{eff}}(h) = -\frac{3}{8}m^2\varphi_v^2 + \underbrace{3m^2h^2}_{\text{positive}}$$

$$\varphi = \varphi_v + \underbrace{h(x)}$$

kinetic scaling

$$V_{\text{eff}}(h) = -\frac{3}{8} m^2 \varphi_v^2 + \underbrace{3 m^2 h^2}_{\text{positive}} + 56 \lambda \varphi_v^5 h^3 + 70 \lambda \varphi_v^4 h^4 + O(h^5)$$

$$\varphi = \varphi_v + \underbrace{h(x)}$$

kinetic scaling

$$V_{\text{eff}}(h) = \left(-\frac{3}{8} m^2 \varphi_v^2 + \underbrace{3 m^2 h^2}_{\text{positive}} + 56 \lambda \varphi_v^5 h^3 + 70 \lambda \varphi_v^4 h^4 + O(h^5) \right)$$

$$\varphi = \varphi_v + \underbrace{h(x)}$$

$$|h| \ll |\varphi_v|$$

kinetic scaling

$$V_{\text{eff}}(h) = \left(-\frac{3}{8} m^2 \varphi_v^2 + \underbrace{3 m^2 h^2}_{\text{positive}} + 56 \lambda \varphi_v^5 h^3 + 70 \lambda \varphi_v^4 h^4 + O(h^5) \right)$$

In nlsm \Rightarrow the only important thing is w



in $hls_m \Rightarrow$ the only important thing is w

\Rightarrow

In $h_{1,2}$ \Rightarrow the only important thing is w

\Rightarrow we can use classical Kähler potential.

In hlsu \Rightarrow the only important thing is W

\Rightarrow we can use classical Kähler potential.

\Rightarrow In SUSY QFT W does not receive ~~quantum~~ quantum correction.

11/10 IF SUSY in unbroken field theory.

→ vacuum expectation

→ $\langle \phi \rangle = v$

$\langle F \rangle = 0$

$\langle D \rangle = 0$

$\langle \lambda \rangle = 0$

nlsm If SUSY in unbroken ^{field} dimensional vacua
survive quantum corrections.

Selection rules and nonren. terms

nlsm

nlsm If SUSY is unbroken, ^{theoretical} ^{classical} vacua survive quantum corrections.

Selection rules and nonren. theory

⇒ nlsm might have some global symmetries.

nlsm If SUSY in unbroken ^{field} ^{theoretical} vacua
survive quantum corrections.

Selection rules and no- θ theorem

\Rightarrow nlsm might have some global symmetries.

\Rightarrow Global sym must commute

nlsm If SUSY in unbroken ^{field} classical vacua
survive quantum corrections.

Selection rules and no-~~non~~ theorem

\Rightarrow nlsm might have some global symmetries.

\Rightarrow Global sym must commute with Poincare symm.

SUSY generators G_i are the charged under $U(1)_R$

(all couplings are equally important)

$$[G_i] = 3$$

K have vanishing dim $+2$

$$[K] = 2$$

In the limit $\frac{|\mathbf{k}|}{m} \rightarrow 0$ $\frac{|\mathbf{k}|}{m^2} \rightarrow 0$ (low energy)

SUSY generators are charged under $U(1)_R$ symmetry. (all couplings are equally important)

$U(1)_R$



ex

dim + 2

In the limit $\frac{g^2}{m^2} \rightarrow 0$ $\frac{g^2}{m^2} \rightarrow 0$ (low energy)

SUSY generators ~~can~~ be charged under $U(1)_R$ R-symmetry.

$U(1)_R$

(all supercharges are equally important)
In extended SUSY model R-symmetry
can become non-abelian?

$N=2 \Rightarrow SU(2)_R$

$N=4 \Rightarrow SU(4)_R \sim$

$AdS_5 \times S^5 \times SO(6)$



In the limit $\frac{|k|}{m} \rightarrow 0$ $\frac{|k|}{m^2} \rightarrow 0$ (low energy)

SUSY generators ~~are~~ be charged under $U(1)_R$ R-symmetry.

$U(1)_R$

(all supercharges are equally important)
in extended SUSY model R-symmetry
can become non-abelian?

$N=2 \Rightarrow SU(2)_R$

$N=4 \Rightarrow SU(4)_R \sim SO(6)_R$

$AdS_5 \times S^5$ $SO(6)$

$$\text{AdS}_5 \times (\text{S}^3) \text{SO}(6)$$

$$\{Q_a, Q_i\} = 2P_{a,i} = 2\sqrt{\alpha'} P_{a,i}$$

$$\mathbb{R}^3 \times \mathbb{S}^3$$

In the limit $\frac{R^2}{\alpha'^2} \rightarrow 0$ $\frac{R^2}{\alpha'^2} \rightarrow 0$

$$\text{Ad}S_5 \times (S^3) \text{SO}(6)$$

$$\{Q_+, Q_-\} = 2I_{d,d} = 2\sigma_{d,d} P_{in}$$

$$R[P_{in}] = 0$$

$$R[Q_+] = -1$$

conventional normal

In the limit $\frac{h^*}{h} \rightarrow 0$ $\frac{h^*}{h^2} \rightarrow 0$

$$\text{AdS}_5 \times (S^3) \text{SO}(6)$$

$$\{Q_+, Q_-\} = 2P_{\text{d.i.}} = 25 \text{ d.i. } P_{\text{in}}$$

$$R[P_{\text{in}}] = 0$$

$$R[Q_+] = -1$$

conventional normalization of $U(1)_R$

In the limit $\frac{R^2}{l_p^2} \rightarrow 0$

$$\frac{R^2}{l_p^2} \rightarrow 0$$

$$\text{AdS}_5 \times (S^3) \text{SO}(6)$$

$$\{Q_+, Q_-\} = 2P_{d,i} = 2\sqrt{5} \alpha_{d,i} P_{in}$$

$$\rightarrow R[P_{in}] = 0$$

$$R[Q_+] = -1$$

$$R[\bar{Q}_+] = +1$$

conventional normalization of $U(1)_R$

kinetic Show implies that $\langle \mathcal{P} \rangle = 0$

$$[R, Q_2] = -Q_2$$

$$[R, \bar{Q}_2] = +\bar{Q}_2$$

Selection rule and more stuff

- \Rightarrow nlsm might have some global symmetries.
- \Rightarrow Global sym must commute with Poincare symm
- \Rightarrow Global sym are not required to commute with SU(2)

$$[\psi] = \lambda$$

Show implies that $\langle \psi, \psi \rangle = 0$

$$[R, Q_\alpha] = -Q_\alpha$$

$$[R, \bar{Q}_\alpha] = +\bar{Q}_\alpha$$

$$[R, P_\alpha] = 0 \quad (\text{Coleman-Mandula theorem})$$

$[R, Q] |n\rangle$

... interaction ...

vacuum

current

manipulation

S_{cl}

rule

and some

S_{cl}

... some global symmetries

... must be consistent with physical symmetries

... must be consistent with physical symmetries

$$[R, Q] |n\rangle = RQ |n\rangle - (Q+R) |n\rangle$$

$$R(|n\rangle) = r$$

$$[R, Q] |n\rangle = RQ |n\rangle - QR |n\rangle$$

$$R(|n\rangle) = r$$

$$R(Q|n) = -1 + r$$

$$[R, Q_+]|n\rangle = RQ_+|n\rangle - Q_+R|n\rangle$$

$$R(Q_+|n\rangle) = r = (-1 + \Gamma)Q_+|n\rangle$$

$$R(Q_+|n\rangle) = -1 + \Gamma$$

$$[R, Q_k] |n\rangle = RQ_k |n\rangle - Q_k R |n\rangle$$

$$R(-1 + \Gamma) |n\rangle = Q_k r |n\rangle$$

$$R(-1 + \Gamma) = -Q_k |n\rangle$$

$$[R, Q_\alpha] |n\rangle = RQ_\alpha |n\rangle = Q_\alpha R |n\rangle$$

$$R(|n\rangle) = r = (-1 + \Gamma) Q_\alpha |n\rangle = Q_\alpha r |n\rangle$$

$$R(Q_\alpha |n\rangle) = -1 + \Gamma = -Q_\alpha |n\rangle$$

Recall

$$[R, Q_x] |n\rangle = RQ_x |n\rangle - Q_x R |n\rangle$$

$$R(|n\rangle) = r = (-1 + \Gamma) Q_x |n\rangle + Q_x r |n\rangle$$

$$R(Q_x |n\rangle) = -1 + \Gamma = -Q_x |n\rangle$$

Recall

$$R(|0\rangle) = 0$$

$$[R, Q_x] |n\rangle = RQ_x |n\rangle - Q_x R |n\rangle$$

$$R(|n\rangle) = r = (-1 + \Gamma) Q_x |n\rangle + Q_x r |n\rangle$$

$$R(Q_x |n\rangle) = -1 + \Gamma = -Q_x |n\rangle$$

Recall

$$R(|0\rangle) = 0$$

$$\hat{N} |0\rangle = |0\rangle$$

$Q_x |N\rangle$

$$[R, Q_x] |n\rangle = RQ_x |n\rangle - Q_x R |n\rangle$$

$$R(|n\rangle) = r = (-1 + \Gamma) Q_x |n\rangle + Q_x r |n\rangle$$

$$R(Q_x |n\rangle) = -1 + \Gamma = -Q_x |n\rangle$$

Recall

$$R(|0\rangle) = 0$$

$$\hat{N} |0\rangle = |0\rangle$$

$$Q_x \hat{N}$$

$$R(\hat{N}) = r$$

$$R(Q_x) = -1$$

$$R \begin{pmatrix} N \\ Q_2 \end{pmatrix} = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \text{ sus}$$

$$R(Q_2) = -1$$

$$Q_2 = \frac{\partial}{\partial \theta^{\alpha}} - i \sigma_{\alpha i} \bar{\theta}^i \partial_{\mu} \gamma_{\mu}$$

$\mathbb{R}^4 \rightarrow \mathbb{P}^3$ is spontaneously broken

$$P \begin{pmatrix} \mathbf{z} \\ \mathbf{a}_2 \end{pmatrix} = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad \text{sys}$$

$$R(\mathbf{Q}_2) = -1$$

$$\mathbf{Q}_2 = \begin{pmatrix} \frac{\partial}{\partial \theta^2} & -i \sigma_{\alpha\beta} \bar{\theta}_2^{\beta} \end{pmatrix} \mathbf{z}_\mu$$

\mathbf{P} is spontaneously broken

$$R(\hat{a}_2) = -1$$

$$R(\hat{a}_2) = -1$$

$$\hat{a}_2 = \left(\frac{\partial}{\partial \theta^2} \right) - i \sigma_{\alpha\beta} \hat{\theta}_2^{\alpha\beta} \gamma_{\mu}^{\alpha\beta}$$

$$R[\hat{\theta}^{\alpha\beta}] = +1$$

$$R(\hat{Q}_2) = -1$$

$$Q_2 = \left(\frac{\partial}{\partial \theta^*} \right) - i \sigma_{\alpha\beta} \bar{\theta}^{\beta} \gamma_{\mu} \partial_{\mu}$$

$$R[\theta^*] = +1$$

$$R\left(\frac{\partial}{\partial x^i}\right) = -1$$

$$R(Q_2) = -1$$

$$Q_2 = \left(\frac{\partial}{\partial \theta^2}\right) - i \sigma_{21} \bar{\theta}^2 \partial_{\bar{\theta}^2}$$

$$R(\theta^2) = +1$$

$$R(\bar{\theta}^2) = -1$$

$$d = \int d\theta^{\nu} k + \int d^2\theta W + \text{L.c.}$$

$U(1)$

$U(1)$

$N=1$

$SU(2)$

$U(1)$



$$d = \int_{\mathcal{M}} \Theta^k + \int_{\mathcal{R}} \Theta^W + \text{L.C.}$$

$U(1)$

$U(1)$

$U(1)$

$U(1)$

$SO(N)$

$$d = \int_{\mathcal{M}} \Theta \cdot k + \int_{\mathcal{R}} \Theta \cdot W + \text{L.C.}$$

$$R[\alpha] = 0$$

$$d = \int_{\mathcal{M}^d} k + \int_{\mathcal{R}^d} \Theta W + \text{L.C.}$$

$$R[\alpha] = 0$$

$$d = \int_{\mathbb{S}^2} \mathcal{M} \vec{k} + \int_{\mathbb{R}^2} \Theta W + \text{L.C.}$$

$$R[\alpha] = 0$$

$$d\theta = \frac{2}{\partial\theta}$$

(Faint, mostly illegible handwritten notes and scribbles on the chalkboard)

$$d = \int_{\mathcal{M}^v} k$$

$$+ \int_{\mathcal{R}^n} \Theta W + \text{L.C.}$$

$$R[\alpha] = 0$$

$$\frac{d}{d\theta} \rightarrow R[\theta]$$

$$d = \int_{\mathcal{M}^d} k + \int_{\mathcal{R}^d} \Theta W + \text{L.C.}$$

$$R[\alpha] = 0$$

$$\frac{d\theta}{d\theta} = \frac{2}{\theta^2}$$

$$R[d\theta] = -1$$

$$d = \int_{\mathcal{M}^0} k + \int_{\mathcal{R}^0} W + \text{L.C.}$$

$$R[d] = 0$$

$$\frac{d}{d\theta} = \frac{\partial}{\partial \theta}$$

$$R[d\theta] = -1$$

$$R[d^2\theta] = -2$$

$$R[W] = +2$$

$$R(\Phi) = \Gamma$$

$$\Phi(y, \theta)$$

$$y = x + \theta \delta \theta$$

$$R(\Phi) = \Gamma$$

$$\Phi(y, \theta) \rightarrow \mu + \theta^2 \Gamma$$

$$y = x + \theta \sigma \theta$$

$$R(\Phi) = \gamma$$

$$\Phi(y, \theta) = \mu + \sqrt{2} \theta \psi + \theta^2 \Gamma$$

$$y = x + \theta \delta \theta$$

$$R(\Phi) = \Gamma$$

$$\Phi(y, \theta) \rightarrow \beta + \sqrt{2} \theta \psi + \theta^2 \Gamma$$

$$y = x + \theta \delta \theta$$

$$K(\Phi) = \mathbb{R}$$

$$\Phi(y, \theta) \rightarrow \beta = \Theta + \sqrt{2} \theta \Psi + \theta^2 \Gamma$$

$$y = x + \theta \delta \theta$$

$$K(\beta) = r$$

$$K(\Psi) = r - 1$$

$$K(\Gamma) = r - 2$$

Can we always find R-symmetry? $v(\pi)$

$$(K, \partial_K) = \dots$$

$$(K, \partial_K) = \dots$$



Can we always find R-symmetry? $\psi(\pi)$

$$\{K, \mathcal{Q}_K\} = -\mathcal{Q}_K$$

$$\{K, \mathcal{P}_K\} = +\mathcal{P}_K$$

$$P^T = 0$$

also \mathcal{P}_K

(also \mathcal{M})

Can we always find R -symmetry? $v(n)$

- no
- yes

Can we always find R-symmetry? $V(\pi)$

- no
- yes

$\left(\begin{array}{c} \text{F in coupling} \\ = + \end{array} \right)$

$= 0$

Can we always find R-symmetry? $v(\pi)$

• no

• yes

$$\left(\begin{array}{l} \neq \text{coupling} \\ R(\delta_i) = 0 \end{array} \right)$$

Can we always find R-symmetry? $V(\pi)$

• no

• yes

$$\left(\begin{array}{l} F \neq \text{coupling} \\ R(\delta_1) = 0 \end{array} \right)$$

Can we always find R-symmetry? $V(\pi)$

• no

• yes

$(F \neq \text{coupling} \Rightarrow R(\delta\phi) = 0)$

Can we always find R-symmetry? $v(\pi)$

• no

• yes

(If \neq coupling $R(y_i) = 0$)

(If supling $R(y_i) \neq 0$)

$$V = -\lambda$$

$$[J] = -4$$

Can we always find R-symmetry? $V(\pi)$

• no

• yes

$$\left(\begin{array}{l} \text{I} \neq \text{coupling} \\ \text{II} \neq \text{coupling} \end{array} \Rightarrow R(y_i) = 0 \right)$$

$$\left(\begin{array}{l} \text{I} \neq \text{coupling} \\ \text{II} \neq \text{coupling} \end{array} \Rightarrow R(y_i) \neq 0 \right)$$

$\chi^2 = 1$

$[J] = -4$

Can we always find R-symmetry? $v(\eta)$

• no

• yes

(\neq coupling $\Rightarrow R(y_i) = 0$)

(\neq coupling $\Rightarrow R(y_i) \neq 0$)

$$W = m\varrho^2 + \lambda\varrho^3$$

$R(\varrho)$

Regul

$$W = m\varphi^2 + \lambda\varphi^3$$

φ is xsp

n n
1 no

$R(\varphi)$

Boyll



$$W = m\varphi^2 + \lambda\varphi^3$$

φ is xsf

"no"

$$R(W) = +2$$

$R(\varphi)$

form

$$W = m\varphi^2 + \lambda\varphi^3$$

φ is xsp

"no"

$$R(W) = +2$$

$R(L_n)$

$$R(m) = 0$$

form

$$R(\lambda) = 0$$

$$W = (mq^2) + \lambda q^3$$

q is xsf

$$R(mq^2) = R(n) + 2R(\tau)$$

"no"

$$R(W) = +2$$

$R(q)$

$$R(m) = 0$$

freq

$$R(\lambda) = 0$$

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

$$R(m\varphi^2) = R(m) + 2R(\varphi)$$

$$\Rightarrow R(\varphi) = +1$$

"no"

$$R(W) = \underline{\underline{+2}}$$

R(m)

$$R(m) = 0$$

R(\lambda)

$$R(\lambda) = 0$$

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

$$R(m\varphi^2) = R(m) + 2R(\varphi)$$

$$\Rightarrow R(\varphi) = +1$$

"no"

$$R(W) = +2$$

$$R(m) = 0$$

$$R(\lambda\varphi^3) = +2$$

$$R(\lambda) = 0$$

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

$$R(m\varphi^2) = R(m) + 2R(\varphi)$$

$$\Rightarrow R(\varphi) = +1$$

"no"

$$R(W) = +2$$

$$R(m) = 0$$

$$R(\lambda\varphi^3) = +2$$

$$\underline{R(\lambda) = 0}$$

R(m)

feyll

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

$$R(m\varphi^2) = R(m) + 2R(\varphi)$$

$$\Rightarrow R(\varphi) = +1$$

"no"

$$R(W) = \underline{\underline{+2}}$$

$$R(m) = 0$$

$$R(\lambda\varphi^3) = +2 \Rightarrow R(\varphi) =$$

$$\underline{\underline{R(\lambda) = 0}}$$

$$W = (mq^2) + \lambda q^3$$

q is xsf

$$R(mq^2) = R(m) + 2R(q)$$

$$\Rightarrow R(q) = (+1)$$

"no"

$$R(W) = +2$$

$$R(m) = 0$$

$$R(\lambda q^3) = +2 \Rightarrow R(q) =$$

$$\underline{R(\lambda) = 0}$$

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

"no"

$$R(W) = \underline{\underline{+2}}$$

$$R(m) = 0$$

$$\underline{R(\lambda) = 0}$$

$$R(m\varphi^2) = R(m) + 2R(\varphi) = 2$$

$$\Rightarrow R(\varphi) = \textcircled{+1}$$

$$R(\lambda\varphi^3) = +2 \Rightarrow R(\varphi) = \textcircled{+\frac{2}{3}}$$

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

$$R(m\varphi^2) = R(m) + 2R(\varphi) = 2$$

$$\Rightarrow R(\varphi) = \boxed{+1}$$

"no"

$$R(W) = \underline{\underline{+2}}$$

$$R(m) = 0$$

$$\underline{R(\lambda) = 0}$$

$$R(\lambda\varphi^3) = +2 \Rightarrow R(\varphi) = \boxed{+\frac{2}{3}}$$

$$W = (m\varphi^2) + \lambda\varphi^3$$

φ is xsf

$$R(m\varphi^2) = R(m) + 2R(\varphi) = 2$$

$$\Rightarrow R(\varphi) = \boxed{+1}$$

"no"

$$R(W) = \underline{\underline{+2}}$$

$$R(m) = 0$$

$$\underline{R(\lambda) = 0}$$

$$R(\lambda\varphi^3) = +2 \Rightarrow R(\varphi) = \boxed{+\frac{2}{3}}$$

• "Yes"

$$R(\lambda) = -1$$

$$R(\psi) = 0$$

$$R(\bar{\psi}) = \rightarrow$$

co-charge assignment

• "Yes"

$$R(\lambda) = -1$$

$$R(m) = 0$$

$$R(\bar{\Phi}) = +1$$

consistent with charge assignment

⇒ Assum

• "Yes"

$$R(\lambda) = -1$$

$$R(m) = 0$$

$$R(\infty) = +1$$

consistent RR - charge assignment

→ Assum

is an effective superpotential

• Yes

$$R(\lambda) = -1$$

$$R(m) = 0$$

$$R(\bar{\Phi}) = +1$$

consistent with charge assignment

\Rightarrow Assume \mathcal{W} is an effective superpotential

• "Yes"

$$R(\lambda) = -1$$

$$R(m) = 0$$

$$R(\bar{\Phi}) = +1$$

consistent with charge assignment

⇒ Assume W is

effective superpotential

$$W_{\text{eff}} = m \Phi^2$$

• "Yes"

$$R(\lambda) = -1$$

$$R(m) = 0$$

$$R(\bar{\Phi}) = +1$$

consistent with charge assignment

⇒ Assume W is an effective superpotential

$$W_{\text{eff}} = m\varphi^2 + \lambda\varphi^3$$

• "Yes"

$$\left. \begin{aligned} R(\lambda) &= -1 \\ R(m) &= 0 \\ R(\Phi) &= +1 \end{aligned} \right\}$$

consistent with charge assignment

⇒ Assume W is an effective superpotential

$$W_{\text{eff}} = m\phi^2 + \lambda\phi^3 \iff W_{\text{uni}} = m\phi^2 + \lambda\phi^3$$

↑
additional

no

↓

+

$$R(\psi) = r - 1 \quad R(\chi)$$

"Yes"

$$\left. \begin{aligned} R(\lambda) &= -1 \\ R(m) &= 0 \\ R(\bar{\phi}) &= +1 \end{aligned} \right\}$$

consistent with charge assignment

⇒ Assume W is an effective superpotential

$$W_{\text{eff}} = m\phi^2 + \lambda\phi^3 \iff W_{\text{tree}} = m\phi^2 + \lambda\phi^3$$

additional

no $\bar{\phi}$

• "Yes"

$$\left. \begin{aligned} R(\lambda) &= -1 \\ R(m) &= 0 \\ R(\Phi) &= +1 \end{aligned} \right\}$$

consistent with charge assignment

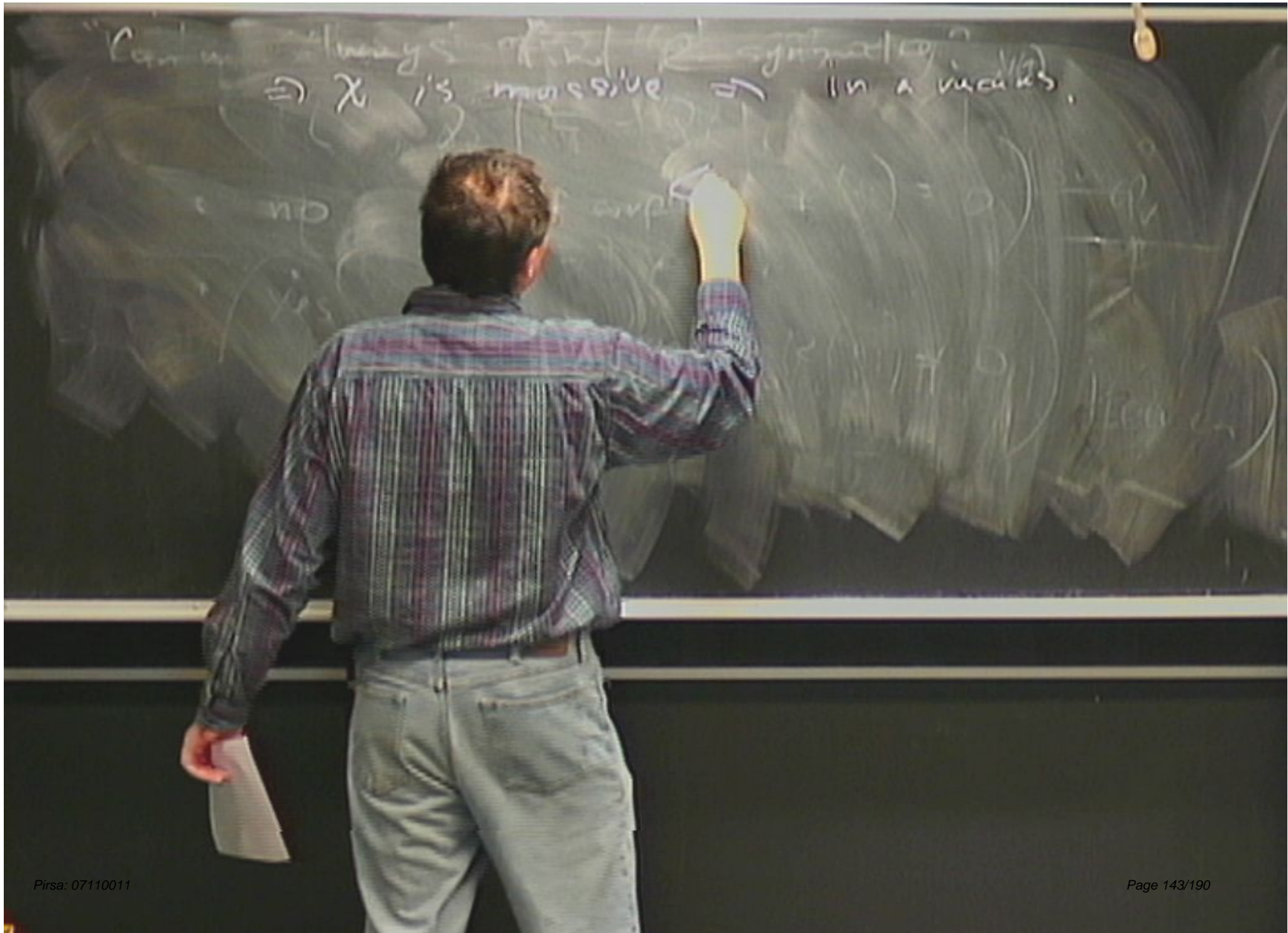
no $\bar{\Phi}$

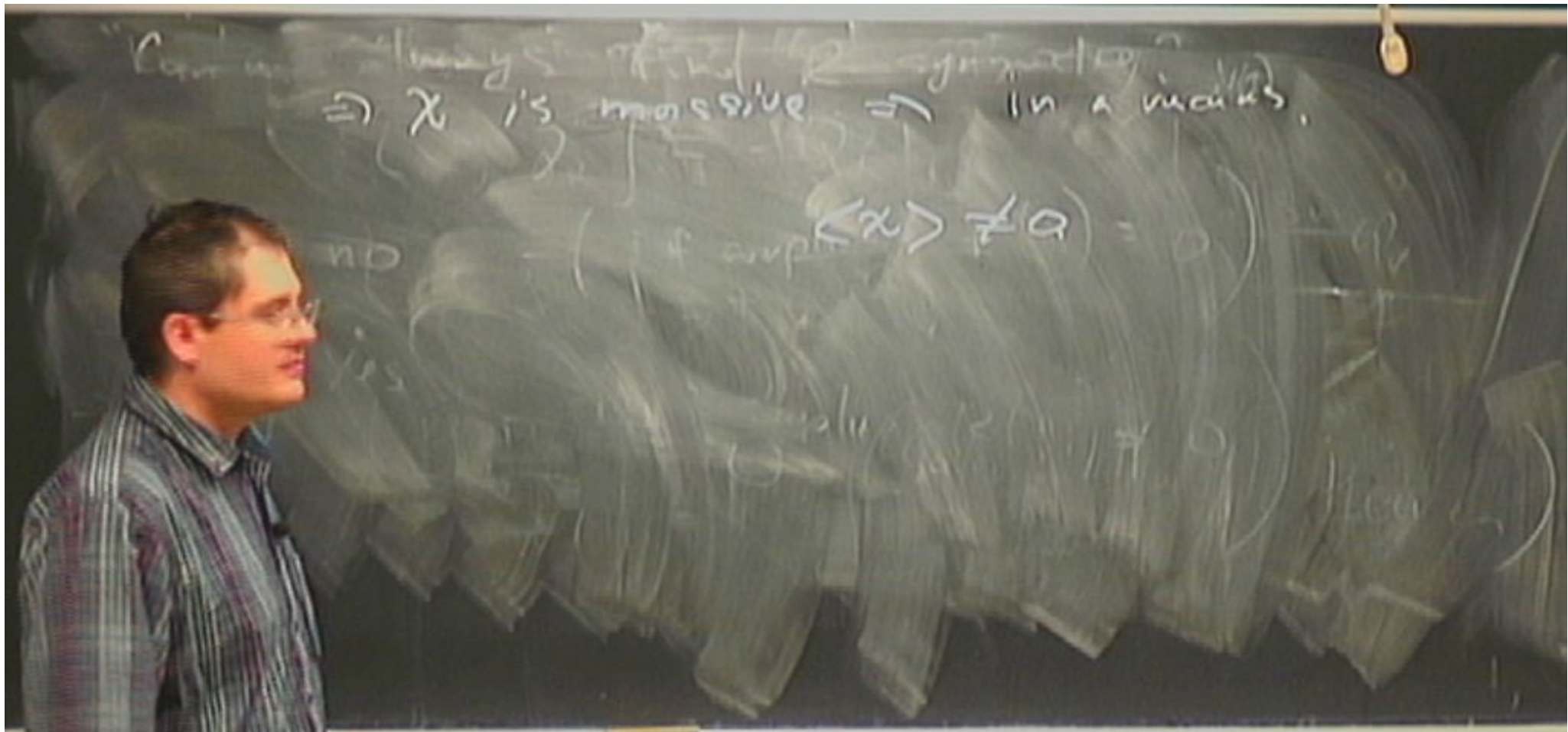
⇒ Assume W is an effective superpotential

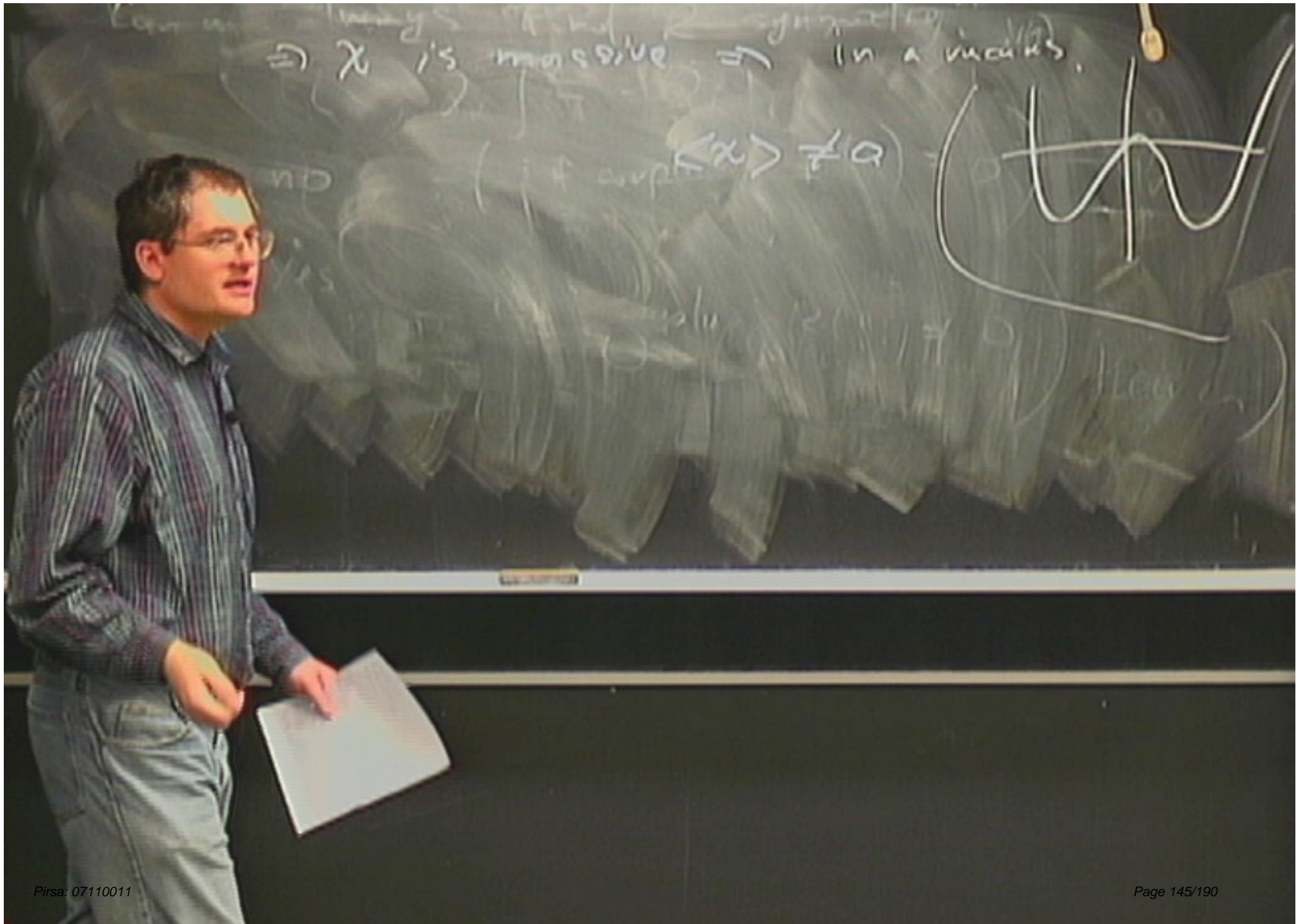
$$\underline{W_{\text{eff}}} = m\phi^2 + \lambda\phi^3 \iff W = \underbrace{m\phi^2}_{\text{microscopic}} + \underbrace{\lambda\phi^3}_{\text{additional}}$$

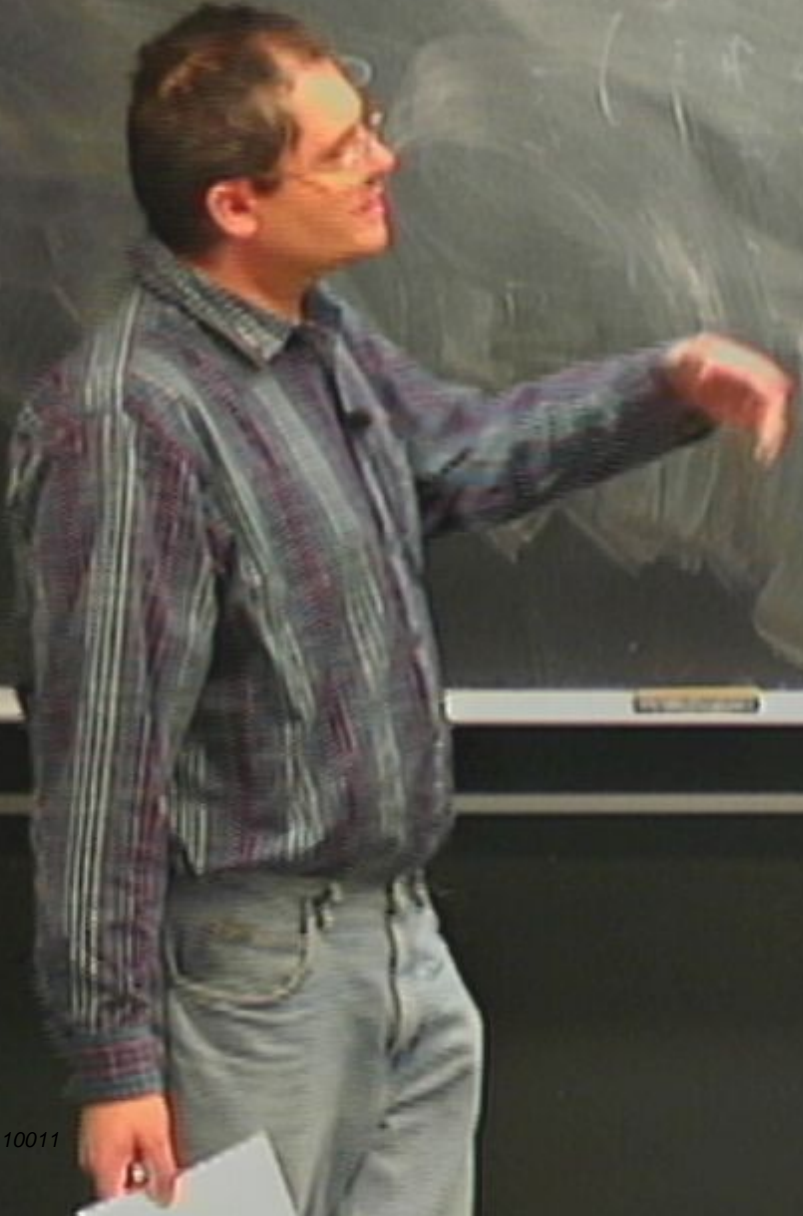
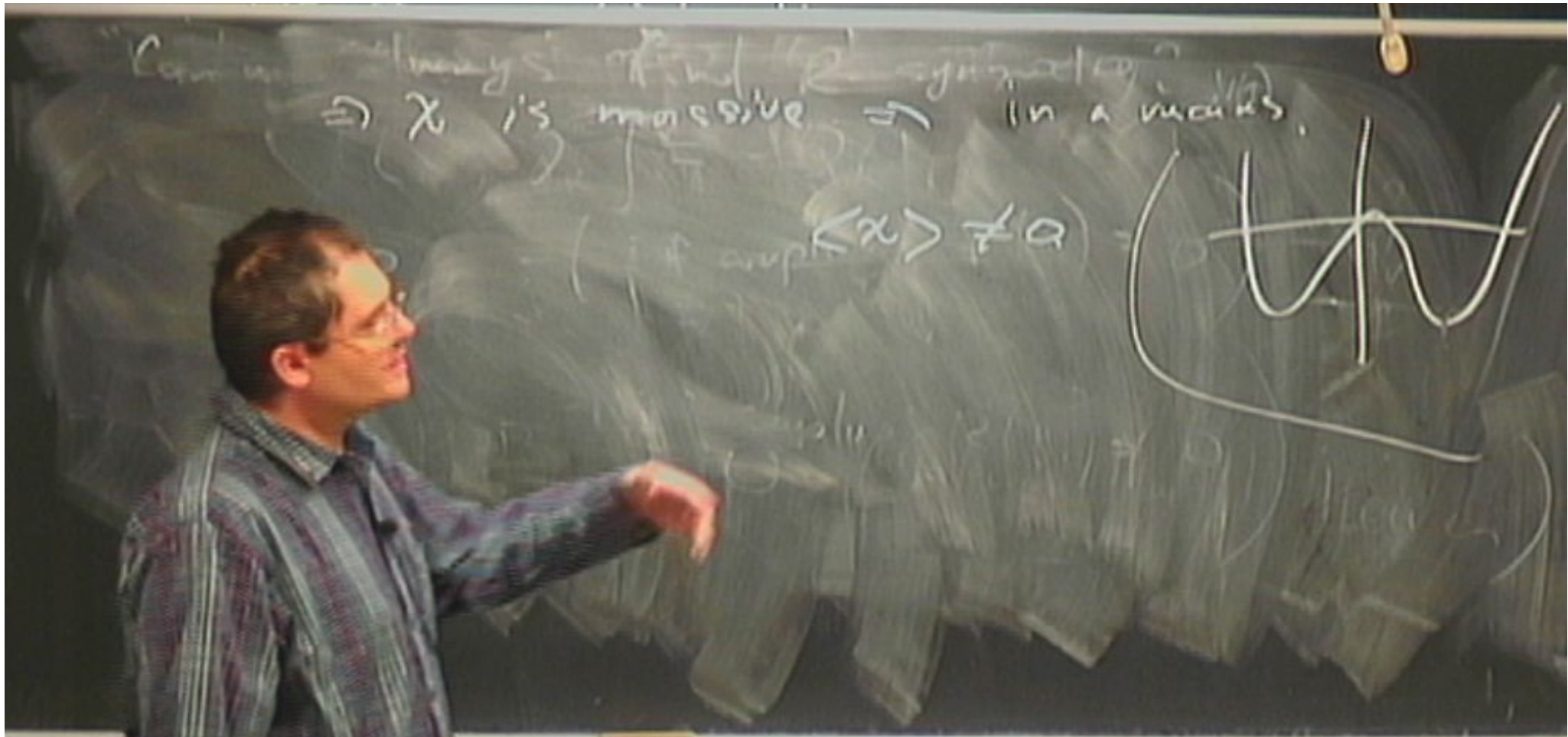


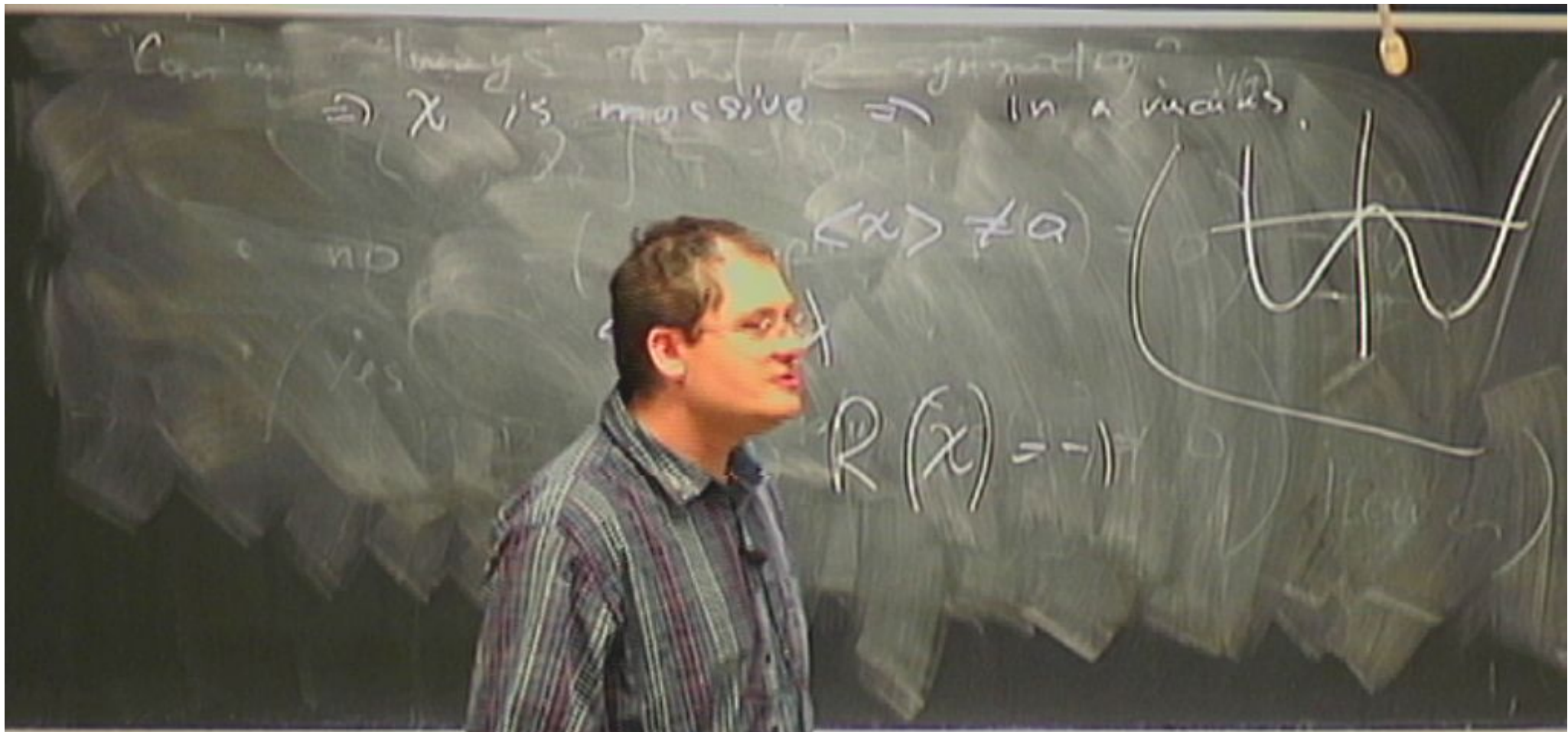
$$R(\psi) = r-1 \quad R(\chi) = r$$











Common property of functions $f: \mathbb{R} \rightarrow \mathbb{R}$ is that f is continuous \Leftrightarrow x is massive \Rightarrow in a vicinity,

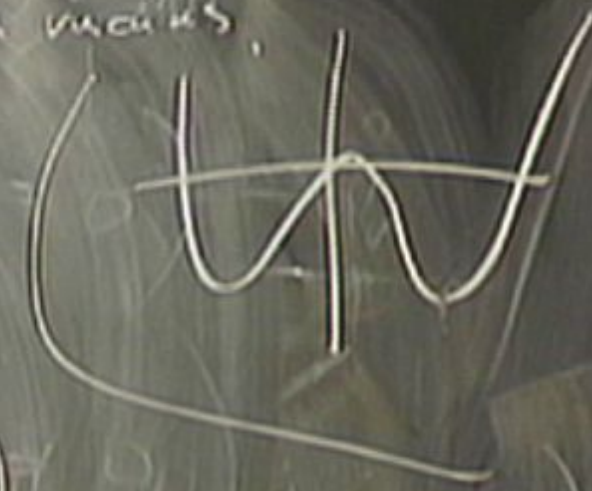
no

yes

$$\langle x \rangle \neq a$$

$$\langle x \rangle = x$$

$$R(x) = -1$$



"Yes"

$$R(\lambda) = -1$$

$$R(m) = 0$$

$$R(\bar{\phi}) = +1$$

consistent with R-charge assignment

⇒ Assume W is an effective superpotential

$$W_{\text{eff}} = m\phi^2 + \lambda\phi^3$$

$$m\phi^2 + \lambda\phi^3$$

←
anomalous
? additional

$$W_{\text{classical}} = m\dot{q}^2 + \lambda q^2$$

$$W_{\text{quantum}} = m\dot{q}^2 + \lambda q^3$$

↑ includes
all perturbative
and nonperturbative
corrections.

$$W_{\text{quant}} = W_1(\varphi)$$

$$W_{\text{quant}} = W_1(\varphi)$$



$$W_{\text{quant}} = W_1 (\hat{\phi})$$



$$W_{\text{quant}} = W_1(\varphi, \lambda, m)$$

$$W_{\text{quant}} = W_1(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

\Rightarrow global symmetries are not anomalous

\rightarrow

$$W_{\text{quant}} = W_1(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

\Rightarrow global symmetries are not anomalous

\rightarrow

$$W_{\text{quant}} = W_{\text{cl}}(\varphi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous

\rightarrow

$$W_{\text{quant}} = W_{\text{cl}}(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous.

$$\rightarrow \chi = \langle \chi \rangle$$

$$W_{\text{quant}} = W_{\text{cl}}(\varphi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous.

$$\rightarrow \lambda = \langle \lambda \rangle$$

$$\bar{\lambda} = \bar{\lambda}$$

$$W_{\text{quant}} = W_1(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous

$$\rightarrow \chi = \langle \chi \rangle$$

$$\bar{\chi} = \langle \bar{\chi} \rangle$$

$$W_{\text{quant}} = W_1(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous
 W can depend only on $\text{tr} F^2$

$$\rightarrow \lambda = \langle \lambda \rangle \Rightarrow$$

$$\bar{\lambda} = \langle \bar{\lambda} \rangle$$

$$W_{\text{quant}} = W_1(\varphi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous
 W can depend only on RST

$$\begin{aligned} \lambda &= \langle \lambda \rangle \\ \bar{\lambda} &= \langle \bar{\lambda} \rangle \end{aligned} \Rightarrow$$

$$\frac{\partial W}{\partial \lambda} = 0$$

$$W_{\text{quant}} = W_1(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous
 W can depend only on \mathcal{R}^2

$$\begin{aligned} \lambda &= \langle \lambda \rangle \\ \bar{\lambda} &= \langle \bar{\lambda} \rangle \end{aligned} \Rightarrow$$

$$\left[\frac{\partial W_1}{\partial \lambda} = 0 \right]$$

$$W_{\text{quant}} = W_1(\phi, \lambda, m)$$

\Rightarrow SUSY is unbroken

$U(1)_R$

\Rightarrow global symmetries are not anomalous.
 W can depend only on \mathcal{R}^2

$$\begin{aligned} \lambda &= \langle \chi \rangle \\ \bar{\lambda} &= \langle \bar{\chi} \rangle \end{aligned} \Rightarrow$$

$$\left[\frac{\partial W_1}{\partial \lambda} = 0 \right]$$

(a) couplings in W are complex

(b) W is holomorphic in these couplings

$$\frac{\partial W}{\partial g}$$

(a) couplings in W are complex

(b) W is holomorphic in these couplings,

$$\frac{\partial W}{\partial g} = 0 \quad \frac{\partial W}{\partial \theta} = 0$$

$$W_{\text{classical}} = \underline{m\phi^2} \rightarrow \left| \frac{pW}{\hbar T} \right|^2 = \underline{m}^2$$

$$W_{\text{quantum}} = \underline{m\phi^2} + \underline{d\phi^3}$$

↑ includes
all perturbative
and nonperturbative
corrections.

$$\langle \bar{\chi} \chi \rangle = \frac{M}{e} \chi$$

$$W_{\text{classical}} = \underline{m \dot{\varphi}^2} \rightarrow \left| \frac{p \dot{\varphi}}{\hbar} \right|^2 = \underline{m \dot{\varphi}^2}$$

$$W_{\text{quantum}} = \underline{m \dot{\varphi}^2} + \underline{\lambda \varphi^3}$$

↑ includes
all perturbative
and nonperturbative
corrections.

$$\int \underline{d^2 \theta} W$$

$$\bar{\lambda} = \langle \bar{\lambda} \rangle$$

$$W_{\text{classical}} = \int \mathcal{L} dt = \int \left(\frac{1}{2} m \dot{\phi}^2 - V(\phi) \right) dt \approx \int \frac{1}{2} m \dot{\phi}^2 dt = \frac{1}{2} m \int \dot{\phi}^2 dt$$

$$W_{\text{quantum}} = \int \mathcal{L} dt + \text{higher order terms}$$

↑ includes
all perturbative
and nonperturbative
corrections.

$$\int d^2\theta W$$

$$\langle \bar{\chi} \chi \rangle = \langle \bar{\chi} \chi \rangle$$

$$Q = \frac{M}{\rho} \frac{K}{e}$$

(a) couplings in W are complex

(b) W is holomorphic in these couplings

$$\frac{\partial W_g}{\partial M^2} = 0$$

$$0 = \frac{\partial W_g}{\partial \tilde{g}} = 0$$

chiral \Leftrightarrow holomorphic

antichiral \Leftrightarrow anti-holomorphic

$$R(A) = -1$$

$$R(\lambda) = -1$$

$$W_3(\rho, \lambda, \bar{\lambda}, m, \bar{m})$$

$$R(\lambda) = -1$$

$$W_3(p, \lambda, \bar{\lambda}, m, \frac{1}{m}) = \dots + - \mathcal{O}_{10}$$

$$R(\lambda) = -1$$

$$W_p(\rho, \lambda, \bar{\lambda}, m, \bar{m}) =$$

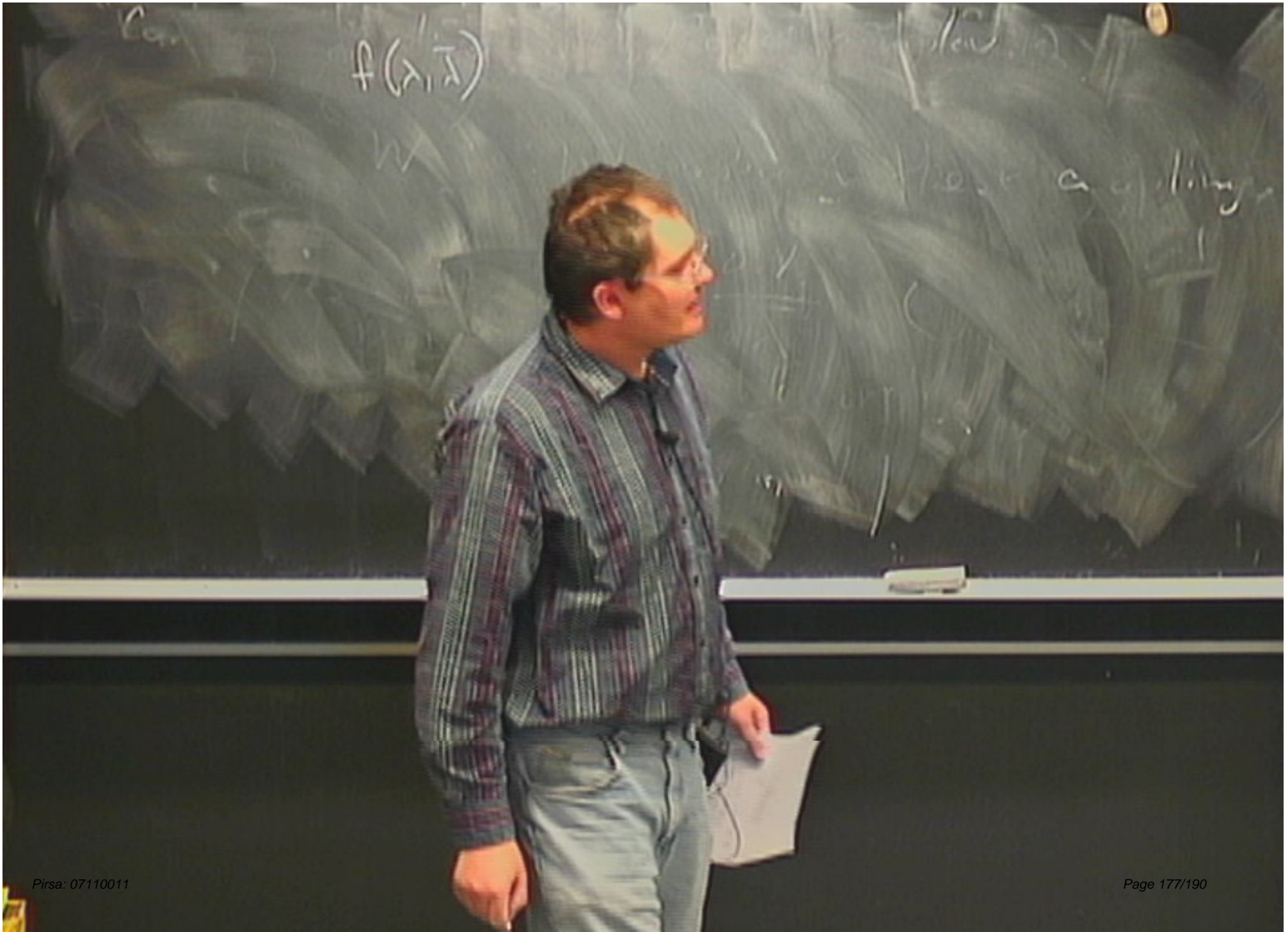
$$R(0_0) = +10$$

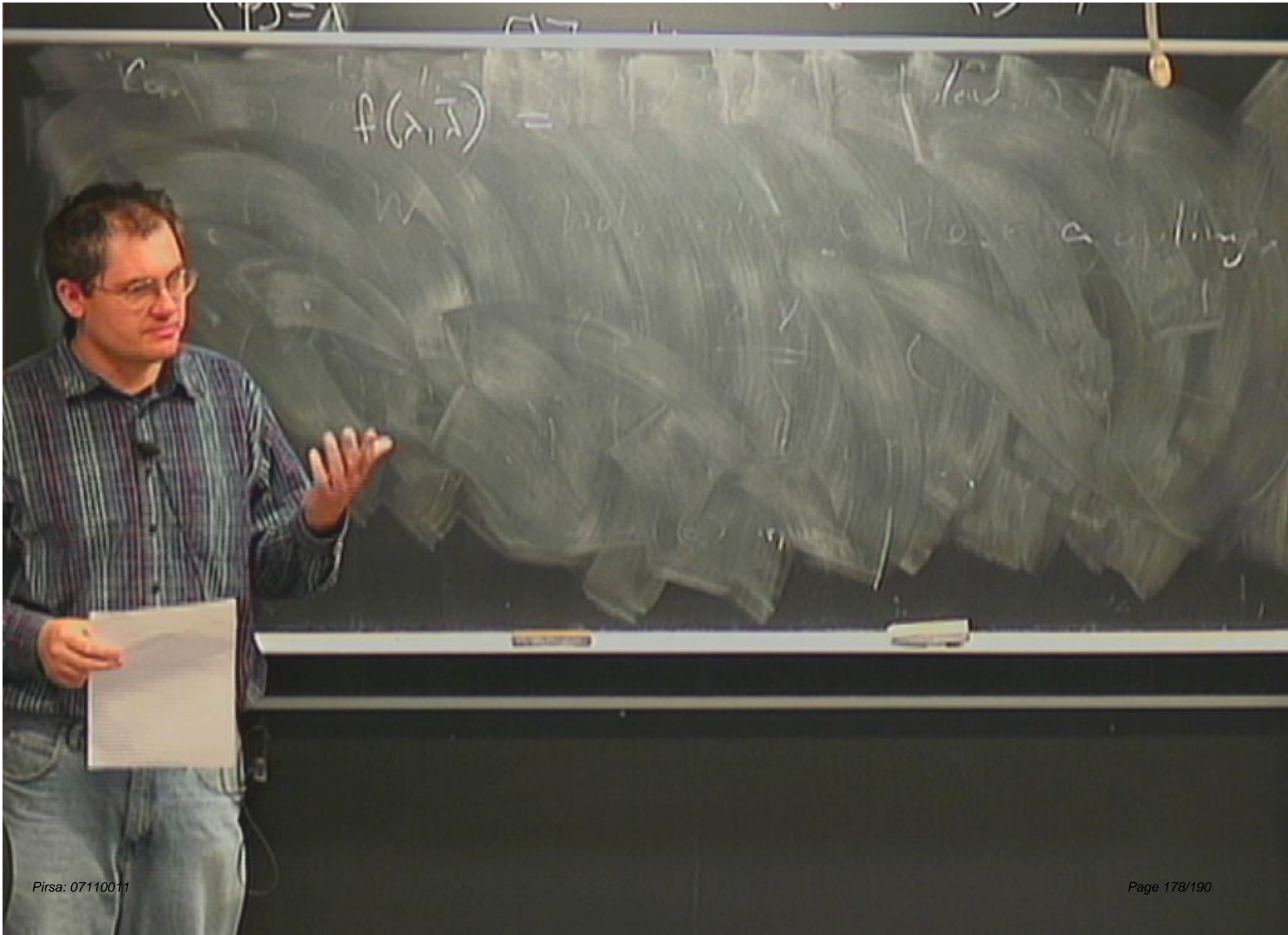
$$R(\lambda) = -1$$

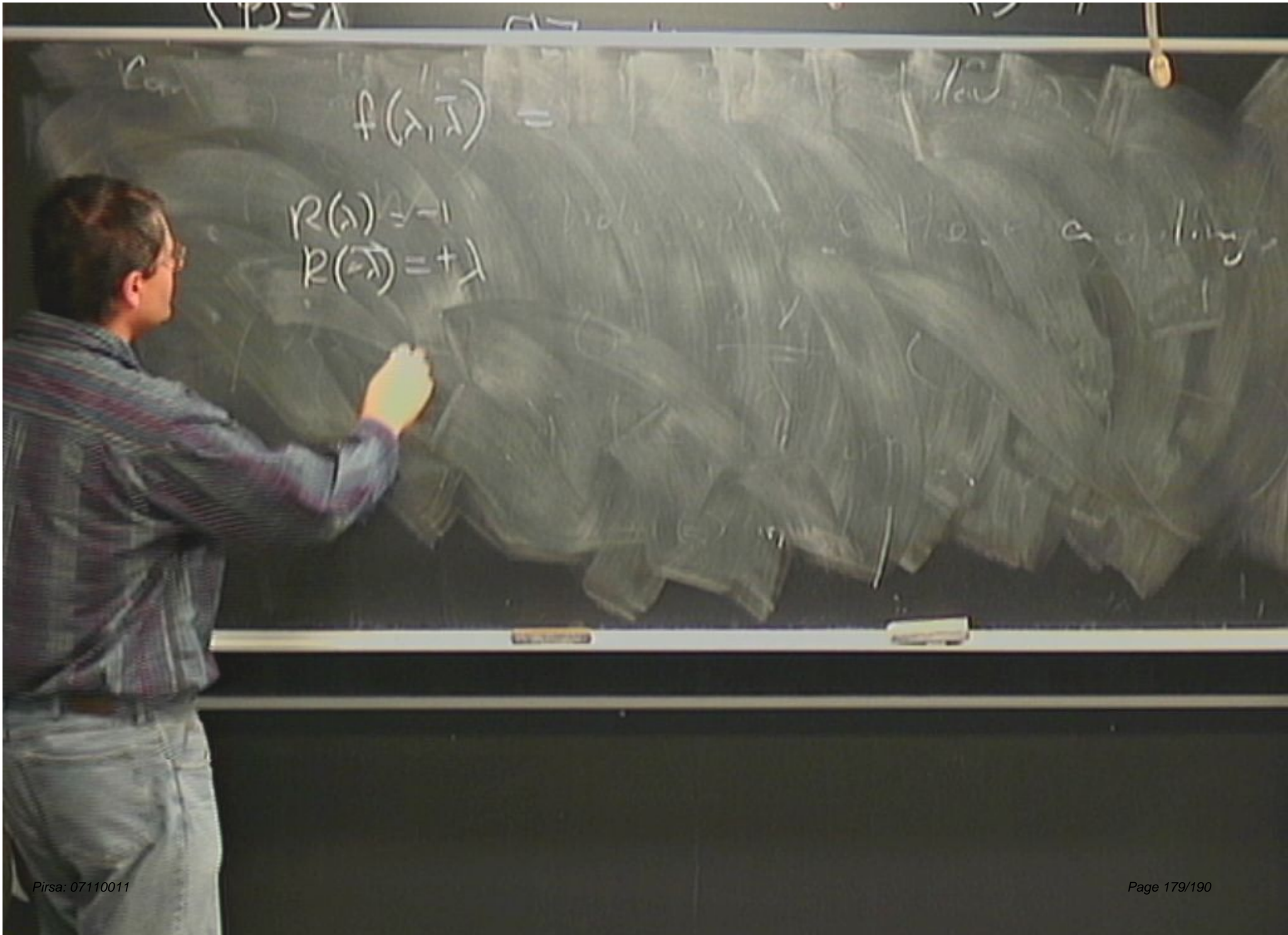
$$W_p(p, \lambda, \bar{\lambda}, m, \bar{m}) = \dots + \underbrace{O_{10} f(\lambda, \bar{\lambda})}_{+2! \dots}$$

$$R(0_{10}) = +10$$

$$R(f(\lambda, \bar{\lambda})) = -8$$







$$f(\lambda, \bar{\lambda}) = \lambda^{\infty}$$

$$R(\lambda) = -1$$

$$R(-\lambda) = +\lambda$$

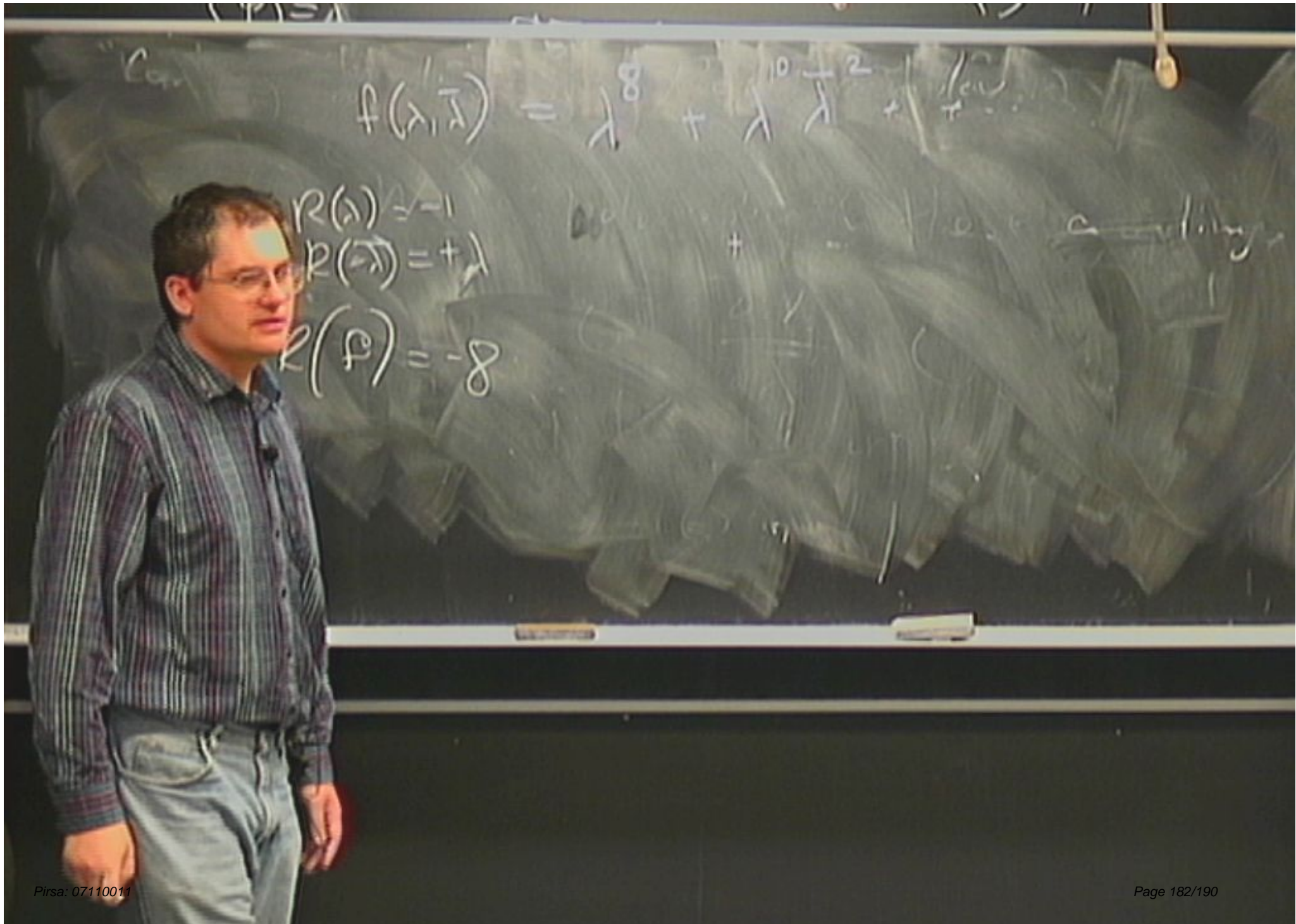
$$R(\rho) = -8$$

$$f(\lambda, \bar{\lambda}) = \lambda^8 + \lambda^{10}$$

$$R(\lambda) = -1$$

$$r(\lambda) = +\lambda$$

$$f(p) = -8$$



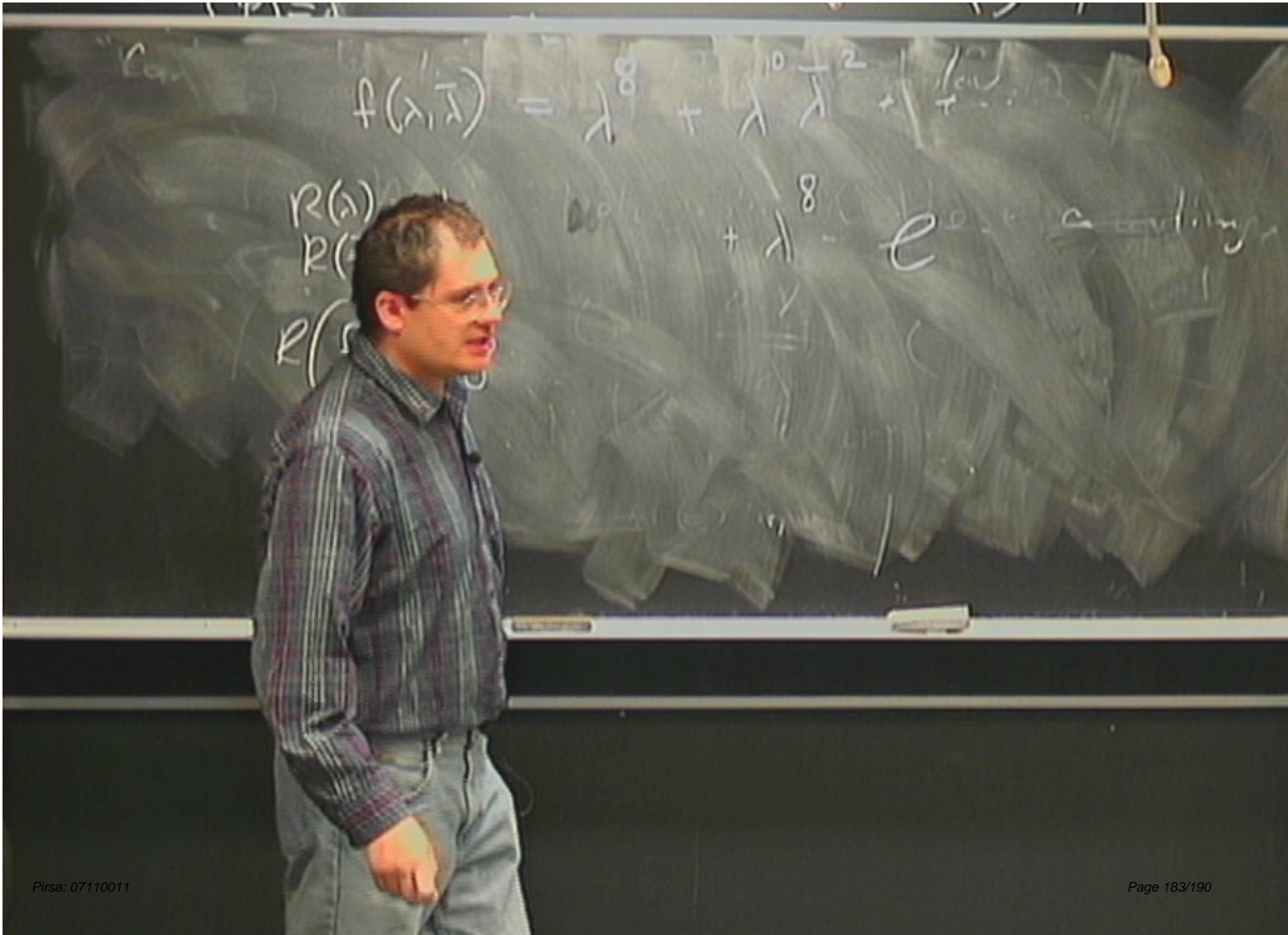
$$f(\lambda, \lambda) = \lambda^8 + \lambda^{10} + \lambda^2 + \dots$$

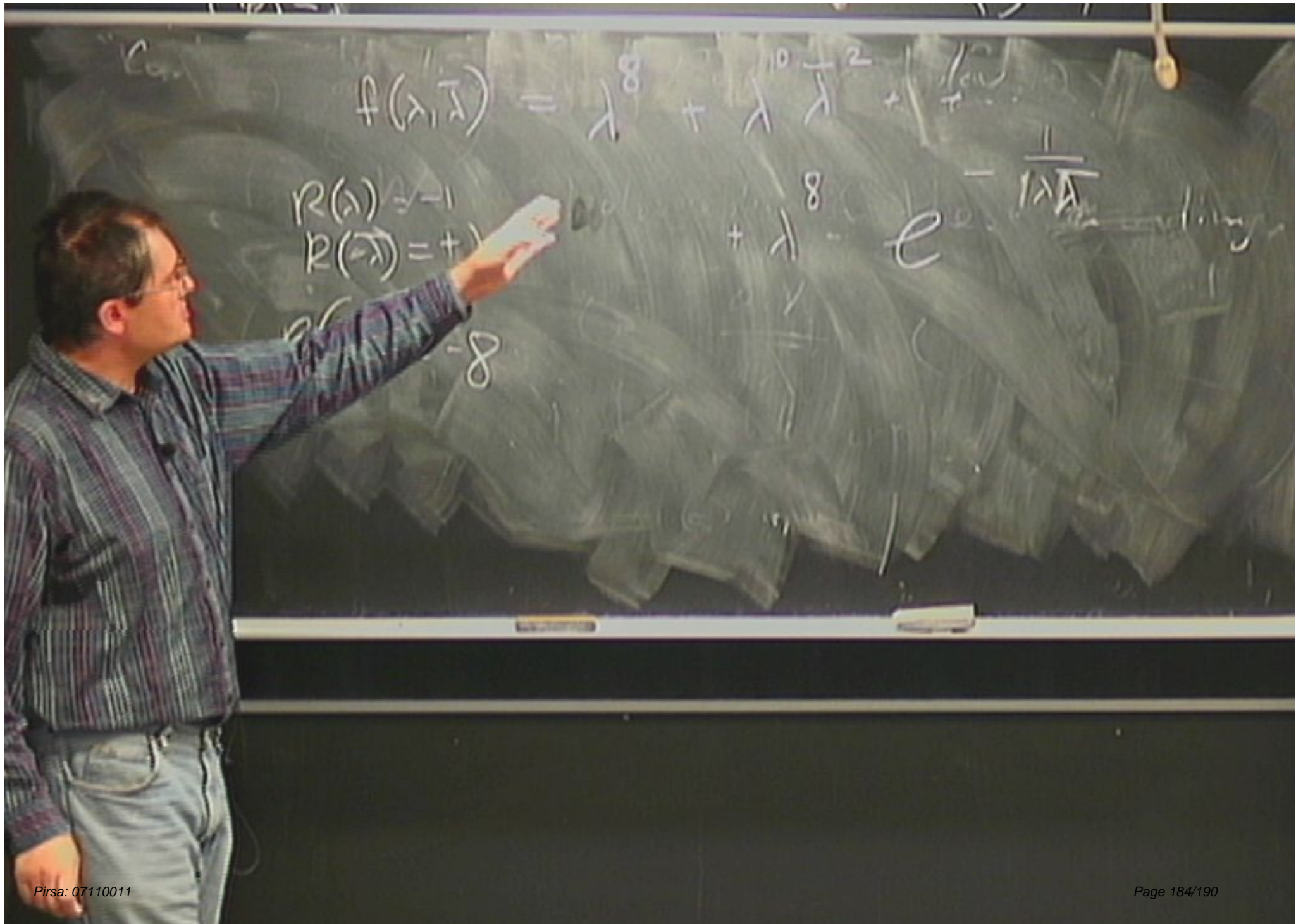
$$R(\lambda) = -1$$

$$R(-\lambda) = +\lambda$$

$$R(P) = -8$$

... something





$$f(\lambda, \bar{\lambda}) = \lambda^8 + \lambda^{10} \lambda^{-2} + \frac{1}{\lambda}$$

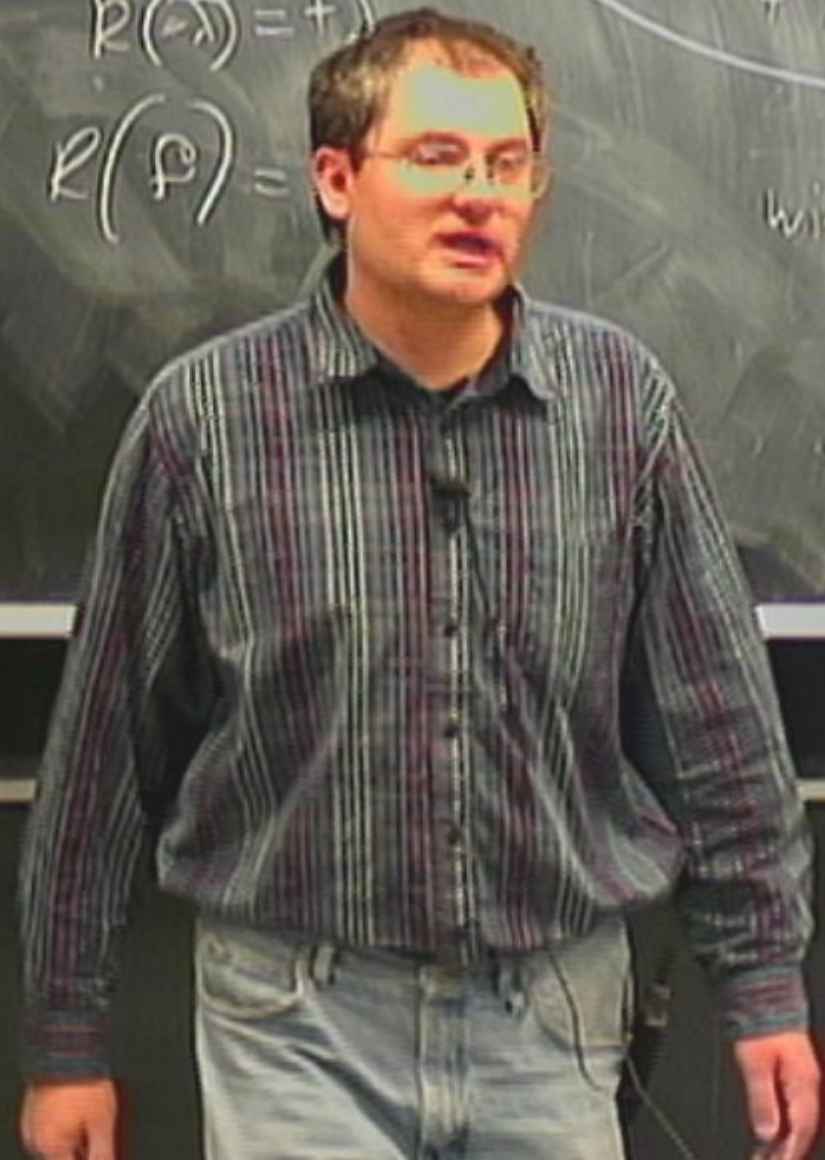
$$R(\lambda) = -1$$

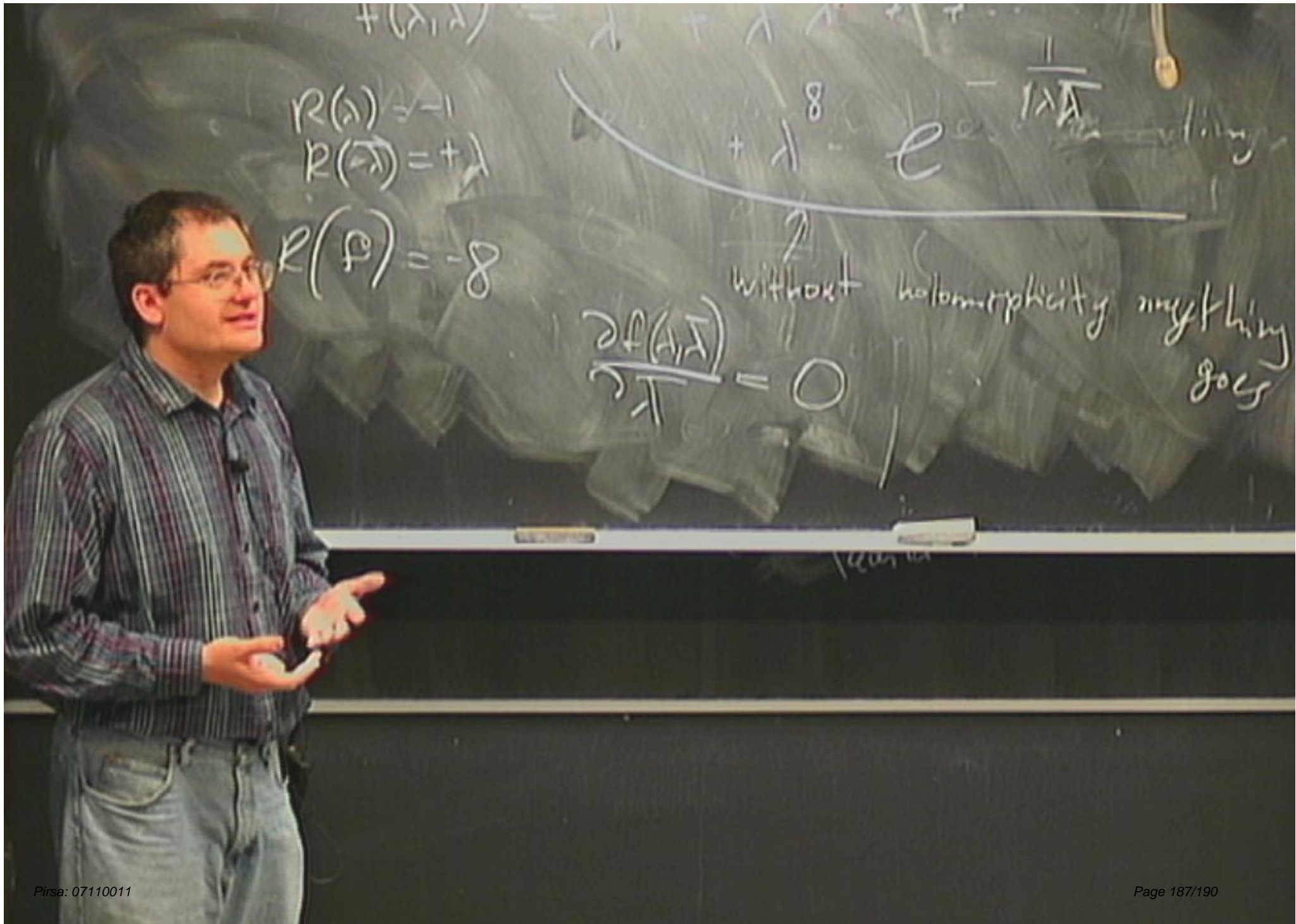
$$R(-\lambda) = +\lambda$$

$$R(P) = -8$$

$$+ \lambda^8 e^{-\frac{1}{\lambda \bar{\lambda}}}$$

$f(\lambda, \bar{\lambda}) = \lambda^8 + \lambda \bar{\lambda}^2 + \frac{1}{\lambda \bar{\lambda}}$
 $R(\lambda) = -1$
 $R(\bar{\lambda}) = +1$
 $R(\rho) =$
 $+ \lambda^8 e^{-\frac{1}{\lambda \bar{\lambda}}}$
 without holomorphicity, anything goes





$$\sqrt{13} = \lambda$$

$$\sqrt{13} = \lambda$$

$$f(\lambda, \bar{\lambda}) = \lambda^8 + \frac{10}{\lambda} + \frac{1}{\lambda^2}$$

$$R(\lambda) = -1$$
$$R(\bar{\lambda}) = +\lambda$$

$$R(P) = -8$$

$$+ \frac{1}{\lambda^8} e^{-\frac{1}{\lambda \bar{\lambda}}}$$

without holomorphicity anything goes

$$\frac{\partial f(\lambda, \bar{\lambda})}{\partial \bar{\lambda}} = 0$$

$$R(\lambda) = -1$$

$$R(-\lambda) = +1$$

$$\rho(\lambda) = -8$$

$$0_{10} \cdot 8$$

$$\frac{\partial f(A, \bar{A})}{\partial \bar{A}} = 0$$

without holomorphicity, everything goes

receive quantum correction.

$$R(\pi) = -1$$

$$R(\pi) = +1$$

$$R(\pi) = -8$$

$$\Rightarrow \begin{matrix} 0 & 8 \\ 0 & 0 \end{matrix}$$

$$0 = \frac{R(\pi)}{R(\pi)} = 0$$

without holomorphicity anything goes

\Rightarrow

π does not receive quantum correction.