

Title: Intro to Supersymmetry 5

Date: Oct 02, 2007 12:30 PM

URL: <http://pirsa.org/07100015>

Abstract:

QM of spin $\frac{1}{2}$ particle.

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (\omega')^2 - \frac{1}{2} \hbar \omega^3 \omega''$$

QM of spin $\frac{1}{2}$ particle.

$$H = \frac{1}{2}\pi^2 + \frac{1}{2}(\omega')^2 - \frac{1}{2}\frac{1}{5}\sigma^3\omega''$$

\Rightarrow solve non-perturbatively.

QM of spin 1/2 particle:

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (\omega')^2 - \frac{1}{2} \hbar \sigma^3 \omega''$$

→ solve non-perturbatively.

(found a ground state wavefunction.

$$\mathcal{L} = \begin{pmatrix} \hat{\omega}_+ \\ 0 \end{pmatrix} \quad \text{or} \quad \mathcal{L} = \begin{pmatrix} 0 \\ \hat{\omega}_- \end{pmatrix}$$

QM of spin 1/2 particle:

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (\psi')^2 - \frac{1}{2} \epsilon \sigma^3 \psi''$$

⇒ solve non-perturbatively. For any spherically potential $W(r)$
(found a ground state wavefunction.

$$\mathcal{U} = \begin{pmatrix} \hat{\psi}_+ \\ 0 \end{pmatrix} \quad \text{or} \quad \mathcal{U} = \begin{pmatrix} 0 \\ \hat{\psi}_- \end{pmatrix}$$

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QM of spin $1/2$ particle.

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (\psi')^2 - \frac{1}{2} \psi \sigma^3 \psi''$$

→ solve non-perturbatively. For any superpotential $W(\psi)$
(found a ground state wavefunction.

$$\mathcal{L} = \begin{pmatrix} \hat{\psi}_+(\psi) \\ 0 \end{pmatrix} \quad \text{or} \quad \mathcal{L} = \begin{pmatrix} 0 \\ \hat{\psi}_-(\psi) \end{pmatrix}$$

fermionic bosonic

⇒ perturbatively.

∃ always a ground state at $w'(p) = 0 \Leftrightarrow q = q_0$
 $w'(q_0) = 0.$

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$$w''(p_0)$$

⇒ perturbatively.

∃ always a ground state at $w'(p) = 0 \Leftrightarrow q = q_0$
 $w'(q_0) = 0.$

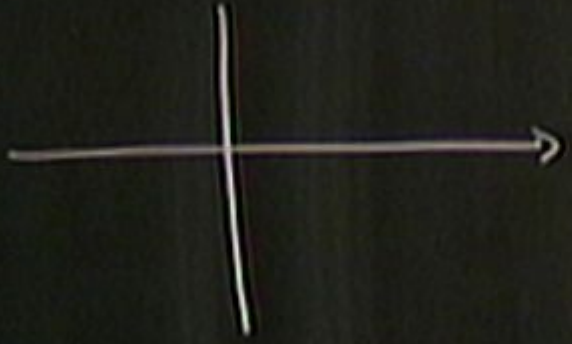
$$\lambda - w''(q_0) > 0$$

the ground state is fermionic

$$\lambda < 0$$

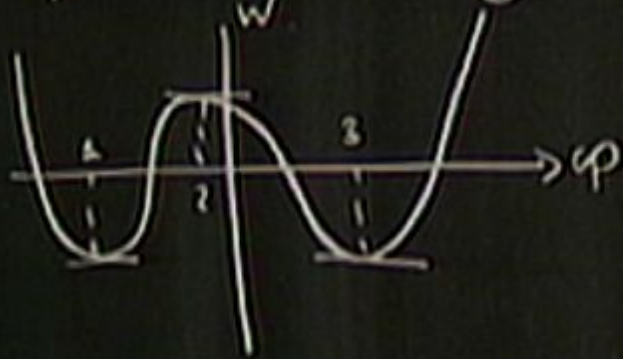
the ground state is bosonic

$W = q^4 +$ subleading terms.



$$W' = \underbrace{4q^3 + \dots}_{\text{cubic equation}} = 0$$

$W = \varphi^4 +$ subleading terms.

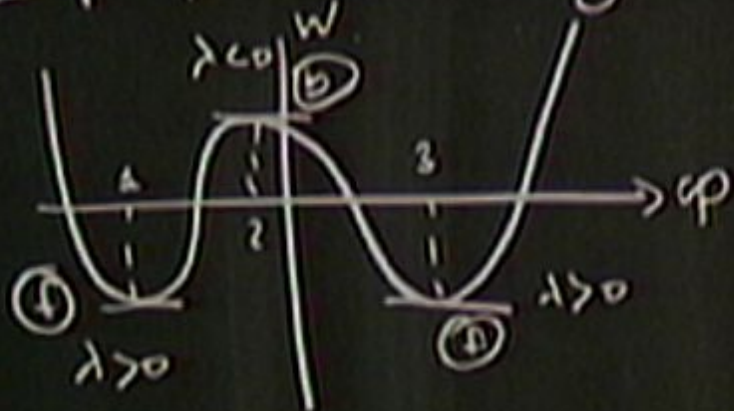


$$W' = 4\varphi^3 + \dots = 0$$

underbrace{4\varphi^3 + \dots} cubic equation



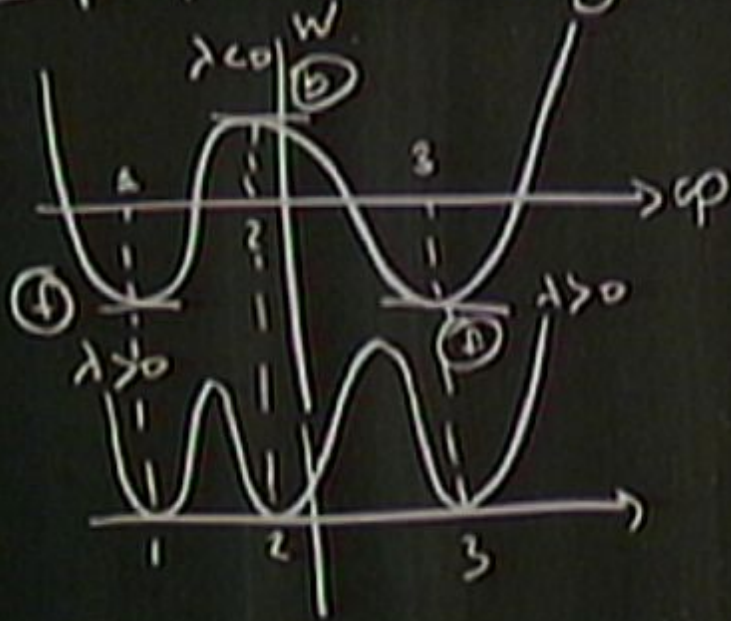
$W = \varphi^4 + \text{subleading terms.}$



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cubic equation

$W = \varphi^4 + \text{subleading terms.}$



$$W' = 4\varphi^3 + \dots = 0$$

cubic equation

$$V \propto (W')^2$$

QM of spin 1/2 particle.

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (\dot{w})^2 - \frac{1}{2} \epsilon_0^3 w''$$

→ solve non-perturbatively. For any superpotential $w(\varphi)$
 (found a ground state wavefunction.

$$\mathcal{Q} = \begin{pmatrix} \hat{w}_+(\varphi) \\ 0 \end{pmatrix} \quad \text{or} \quad \mathcal{Q} = \begin{pmatrix} 0 \\ \hat{w}_-(\varphi) \end{pmatrix}$$

fermionic $\hat{w}_+(\varphi) \rightarrow \infty$ $-w$ bosonic

QM of spin $\frac{1}{2}$ particle.

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→ solve non-perturbatively. For any superpotential $w(\phi)$
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$$\mathcal{L} = \begin{pmatrix} \hat{w}_+(\phi) \\ 0 \end{pmatrix} \quad \text{or} \quad \mathcal{L} = \begin{pmatrix} 0 \\ \hat{w}_-(\phi) \end{pmatrix}$$

fermionic $\hat{w}_+(\phi) \sim e^{-w/\hbar}$ $-w/\hbar$ bosonic

$$\hat{w}_L(\pi) = e^{+w/\hbar}$$

QM of spin 1/2 particle.

$$H = \frac{1}{2} p^2 + \frac{1}{2} (W')^2 - \frac{1}{2} \sigma^3 W''$$

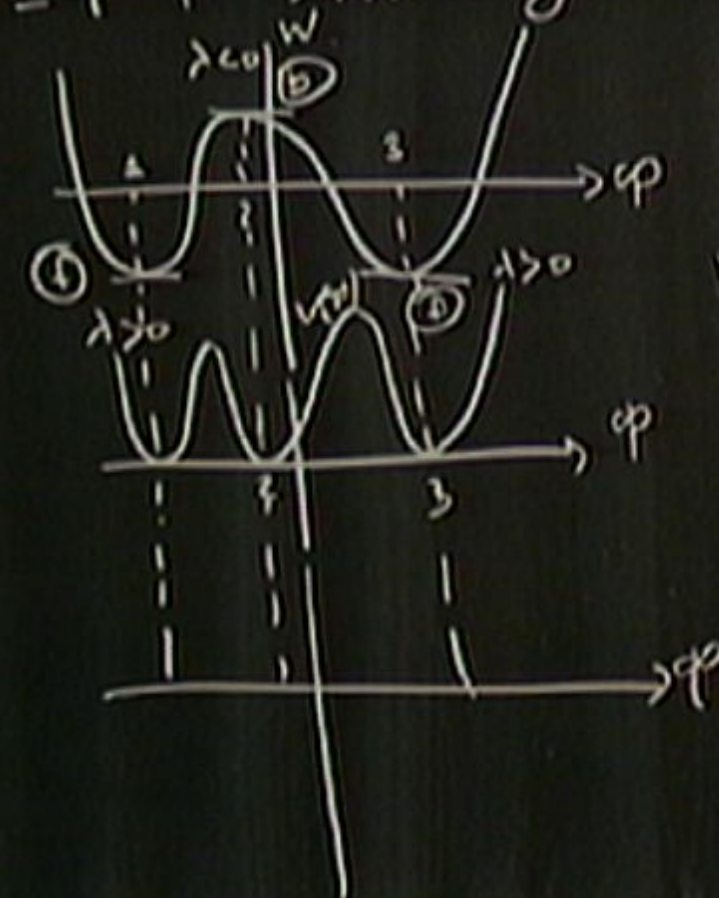
→ solve non-perturbatively. For any spherically potential $W(r)$
 (found a ground state wavefunction.

normalizable → $\mathcal{Q} = \begin{pmatrix} \hat{\psi}_+(r) \\ 0 \end{pmatrix}$ or $\mathcal{Q} = \begin{pmatrix} 0 \\ \hat{\psi}_-(r) \end{pmatrix}$ $\hat{\psi}_\pm(r) = e^{\pm W/r}$

fermionic $\hat{\psi}_+(r) \in \mathbb{C}$ - W/er bosonic.

$W = \varphi^4 + \text{subleading terms.}$

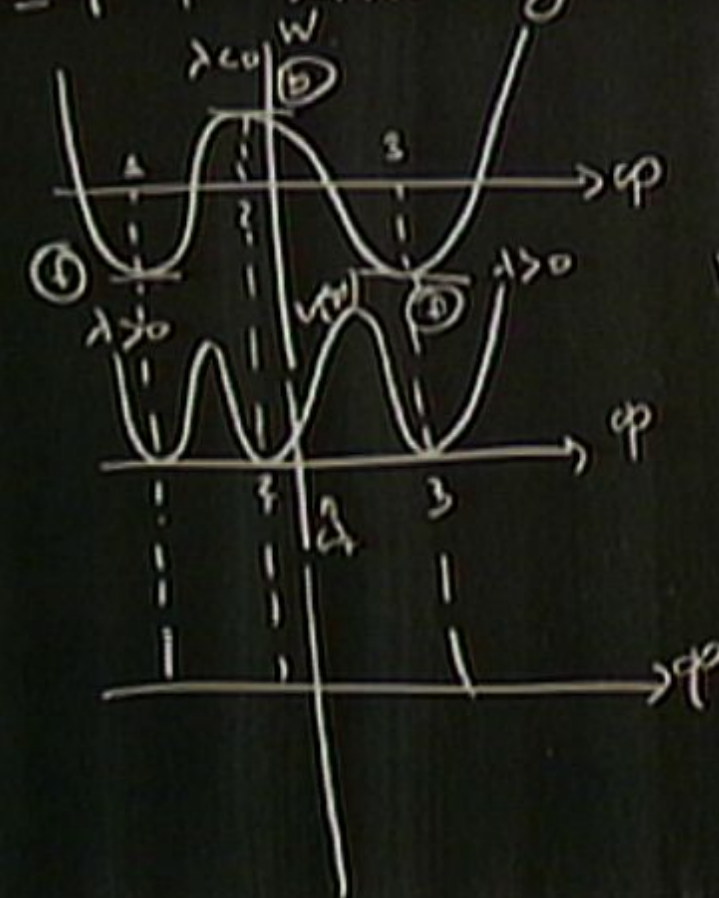
$W' = 4\varphi^3 + \dots = 0$
 cubic equation.



$V \propto (W')^2$

$W = \varphi^4 + \text{subleading terms.}$

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 cubic equation

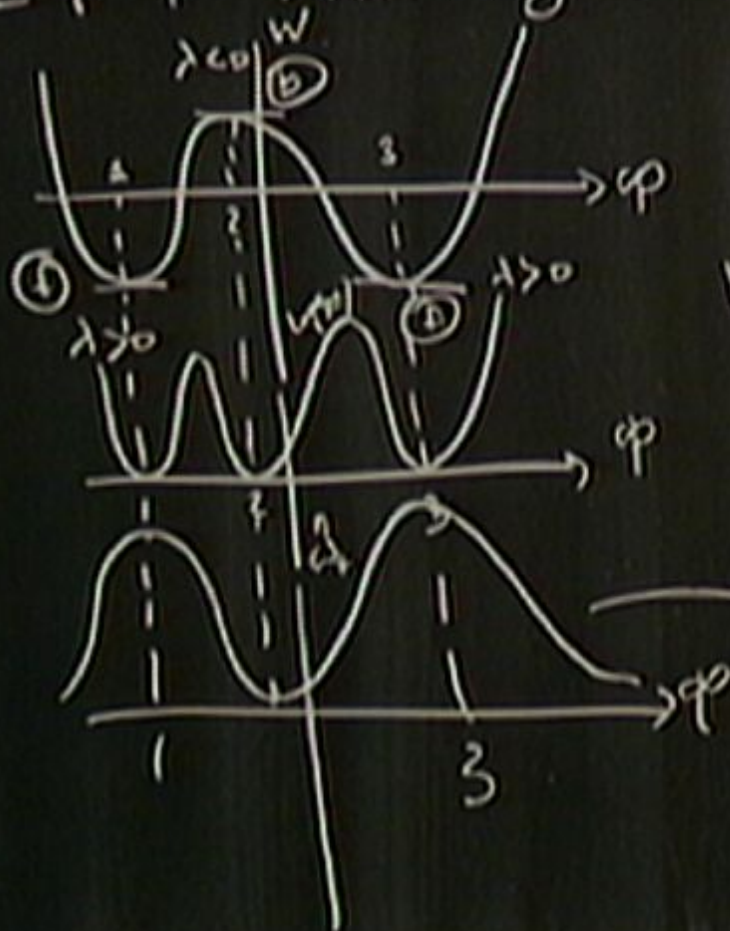


$V \propto (w')^2$

$\omega_+ \propto e^{-W/\hbar}$

$W = \varphi^4 + \text{subleading terms.}$

$W' = 4\varphi^3 + \dots = 0$
 cubic equation



$V \propto (W')^2$

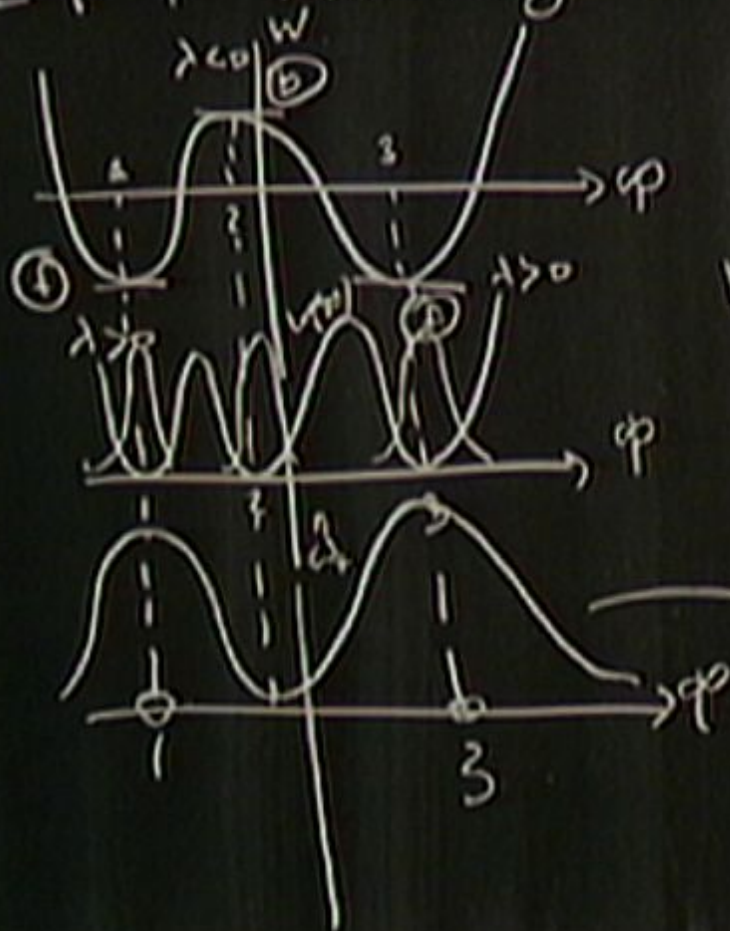
$\psi_+ \propto e^{-W/\hbar}$

exact wave function

$W = \varphi^4 + \text{subleading terms.}$

$$W' = 4\varphi^3 + \dots = 0$$

⏟
cubic equation



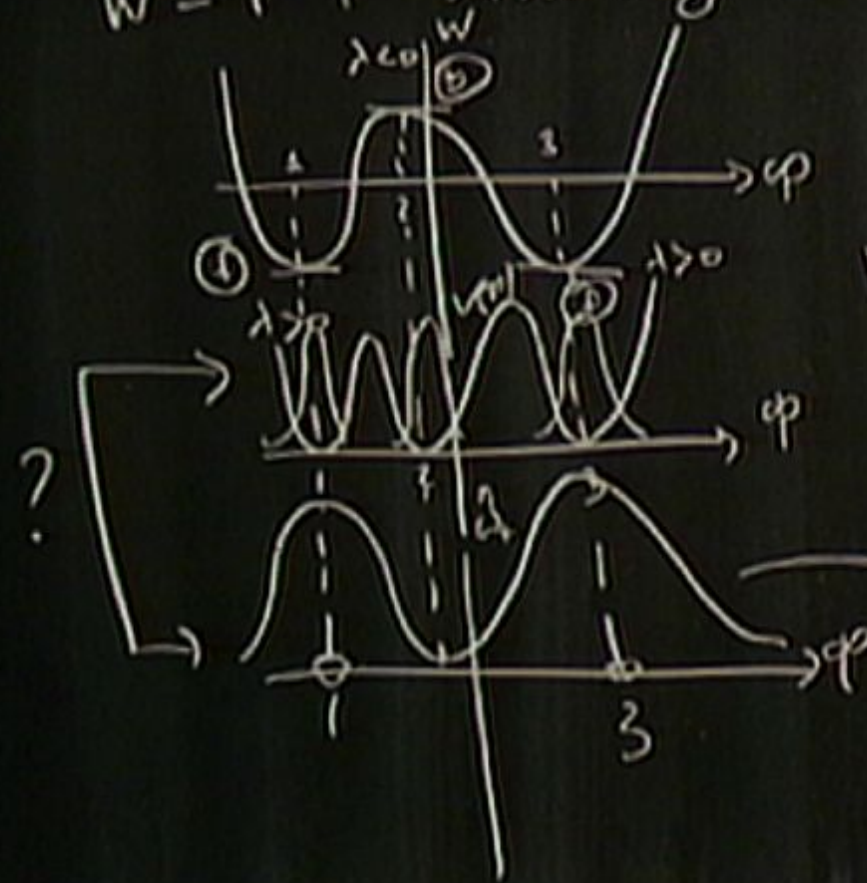
$$V \propto (W')^2$$

$$\psi_{\pm} \propto e^{-W/\hbar}$$

exact wave function.

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 cubic equation.



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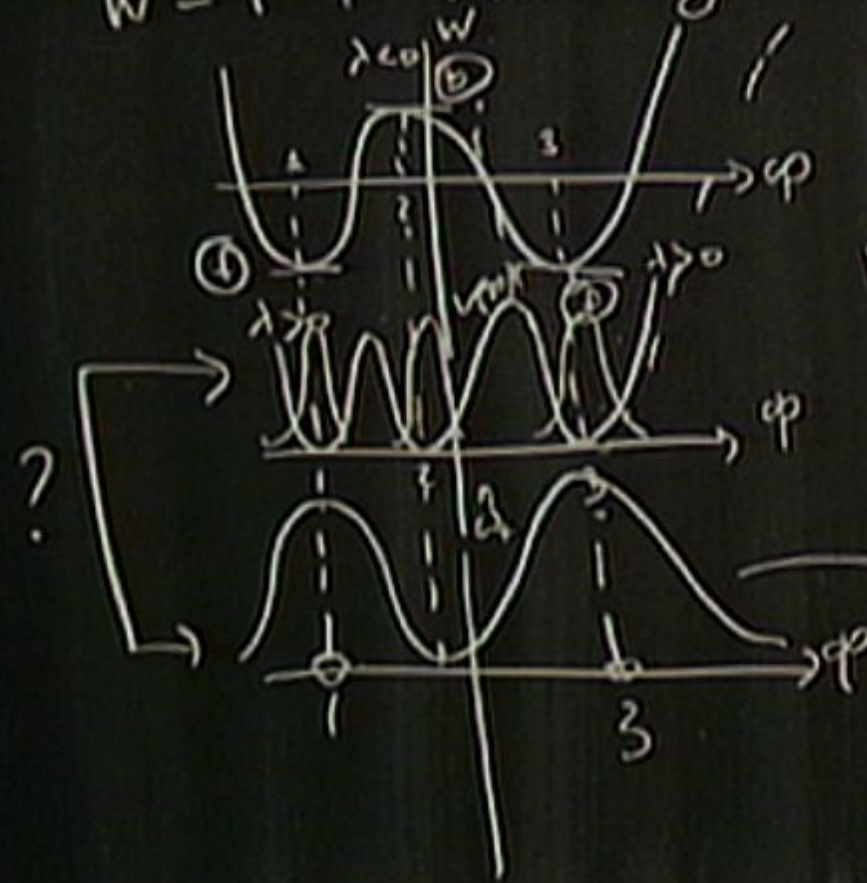
$\hat{\omega}_+ \propto e^{-W/\hbar}$

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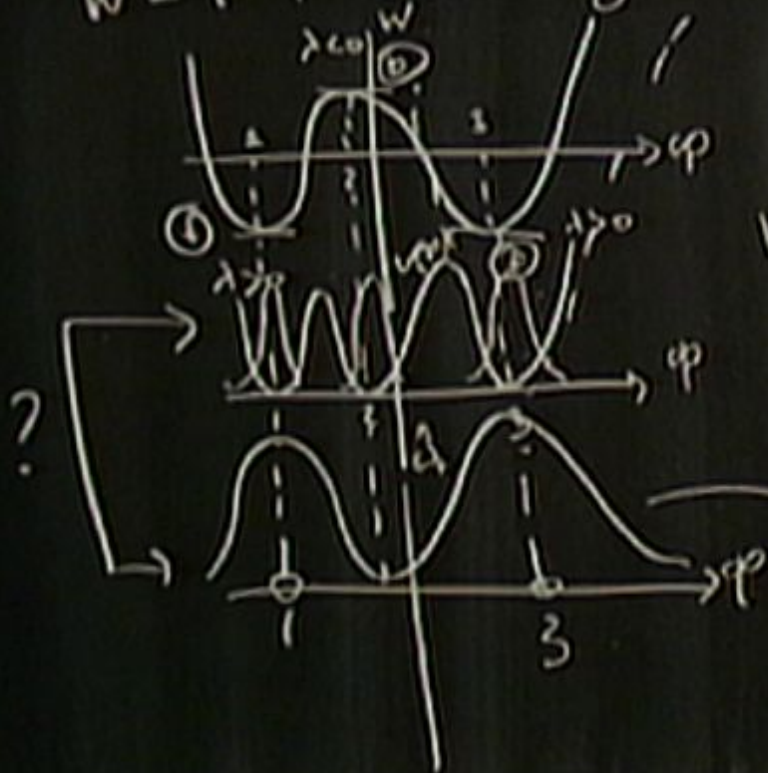
- $\psi_1 - a$
- $\psi_2 - b$
- $\psi_3 - c$

$\hat{\omega}_+ \propto e^{-W/\hbar}$

exact wave function.

$W = \varphi^4 + \text{subleading terms.}$

$W' = 4\varphi^3 + \dots = 0$
 cubic equation



$V \propto (W')^2$

- $\psi_1 - p$
- $\psi_2 - b$
- $\psi_3 - p$

$\omega_+ \propto e^{-W/\hbar}$

exact wave function.



Perturbatively:

ψ_1

ψ_2

ψ_3

\Rightarrow

$\psi_1 + \psi_2$

ψ_2

$\psi_1 - \psi_3$

Perturbatively:

ψ_1

ψ_2

ψ_3

\Rightarrow

$\psi_1 + \psi_3 \quad - \quad P$

$\psi_2 \quad - \quad b$

$\psi_1 - \psi_3 \quad - \quad P$

Perturbatively:

$$\psi_1 \quad \psi_1 + \psi_3 - a = E = 0.$$

$\psi_2 \Rightarrow$

$$\psi_2 - b$$

ψ_3

$$\psi_1 - \psi_3 - c$$

} just the correct multipl. c. f. for

Perturbatively:

$$\psi_1 \quad \psi_1 + \psi_3 - a = E = 0.$$

$\psi_2 \Rightarrow$

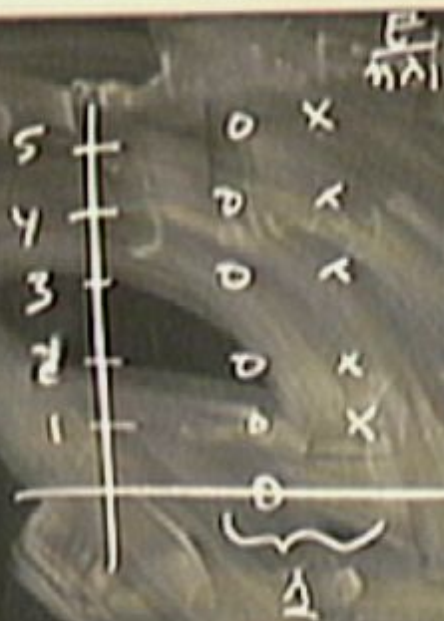
$$\psi_2 - b$$

ψ_3

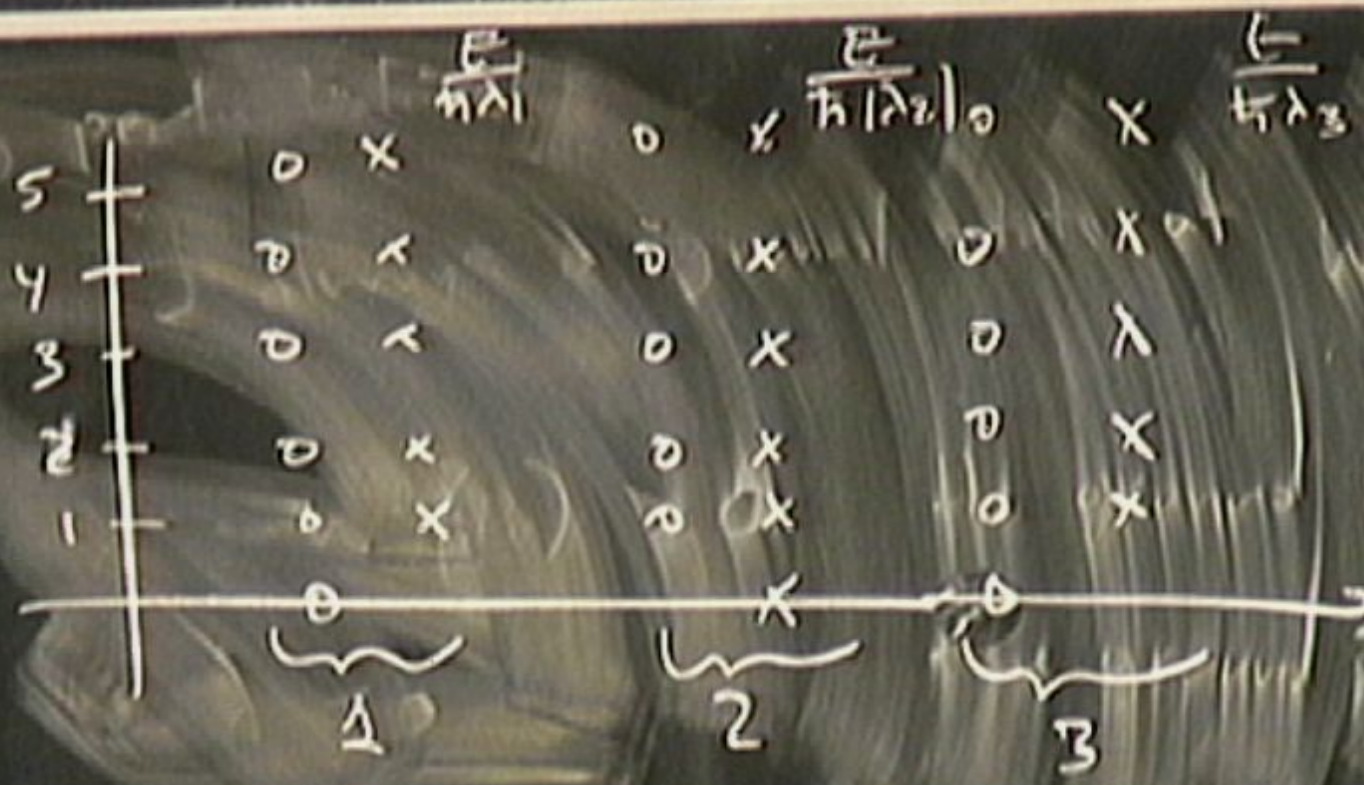
$$\psi_1 - \psi_3 - c$$

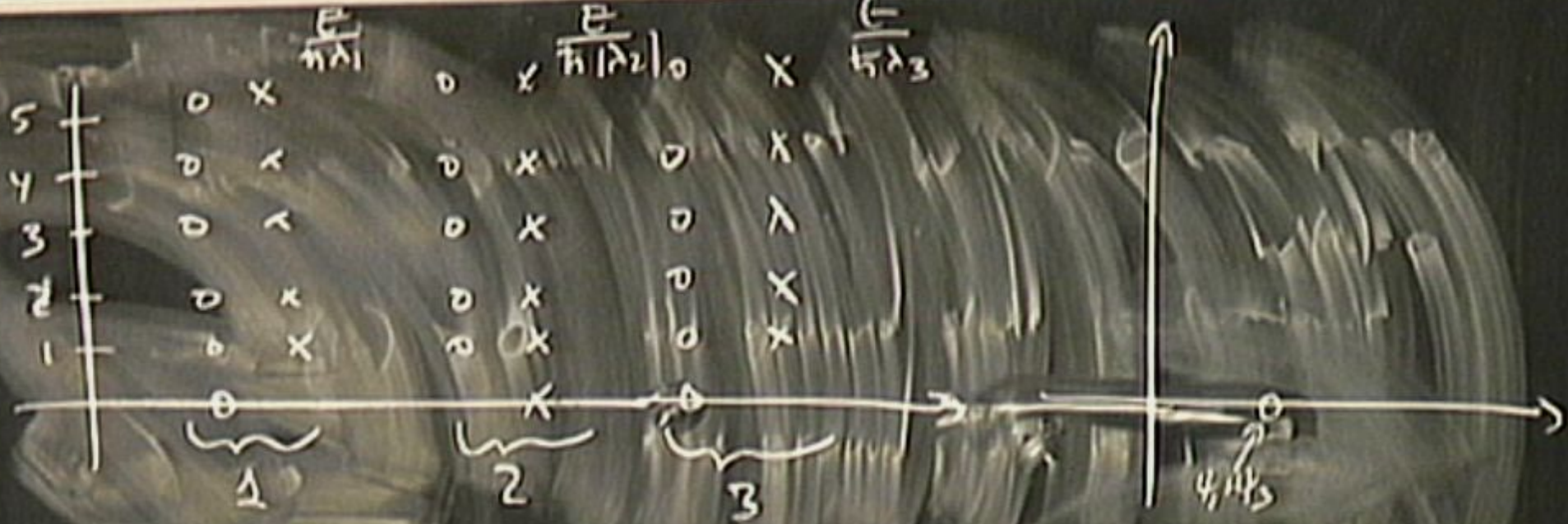
} just the correct multiplicities
for "nonperturbative"
effect (tunnelling)
to lift $\psi_2, \psi_1 - \psi_3$
to a massive susy
multiplet

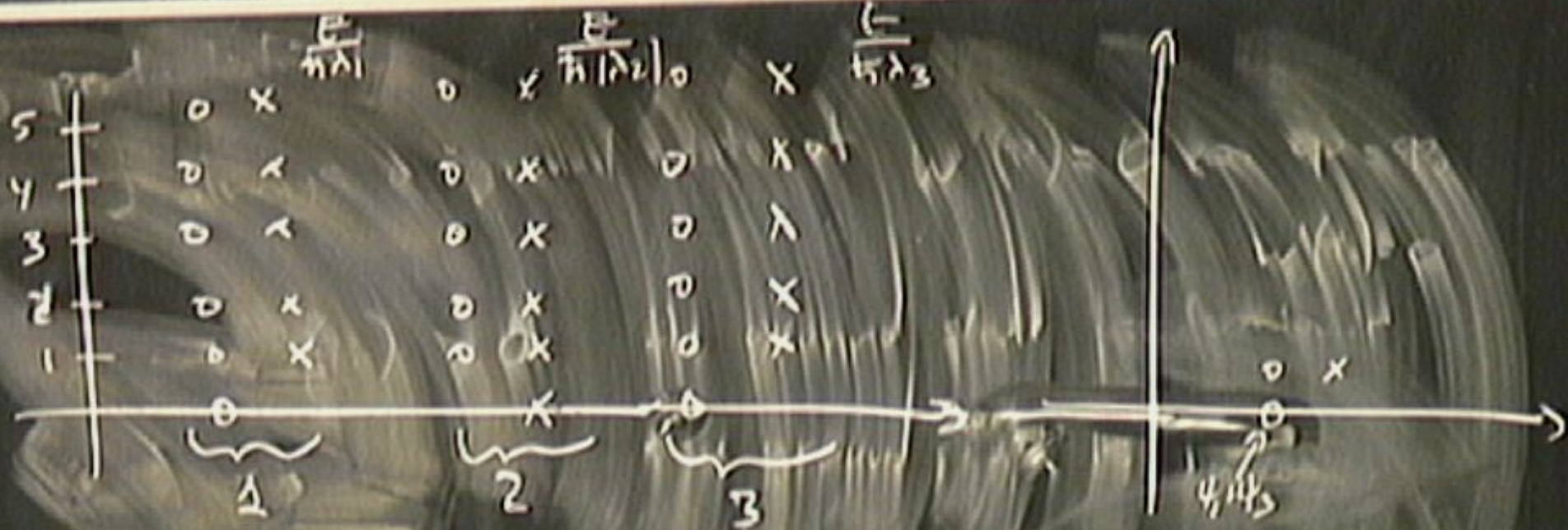
3
2
1

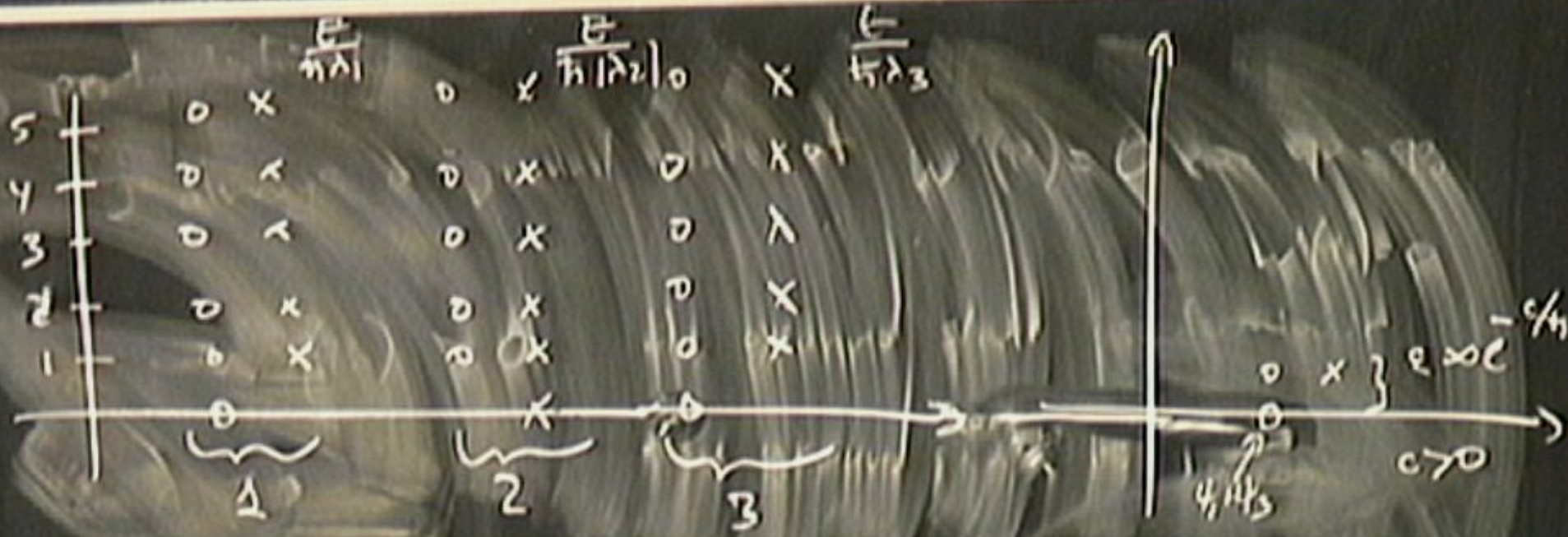


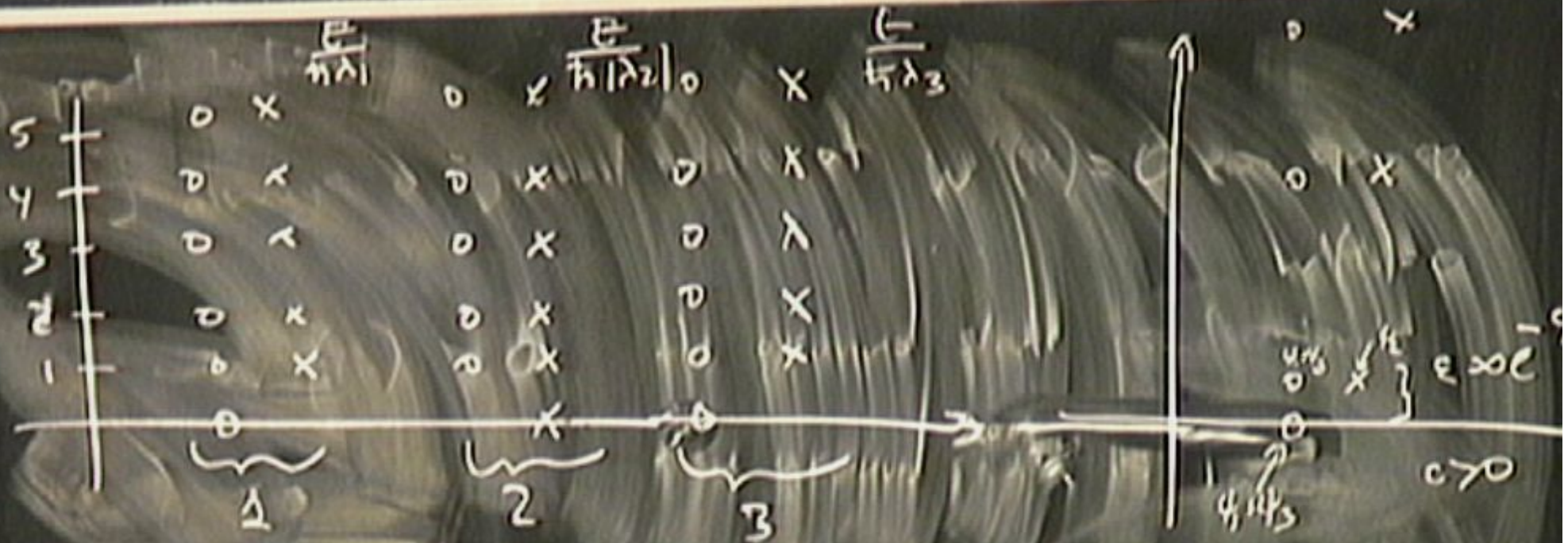
CAUTION
DISPLACEMENT
DANGER

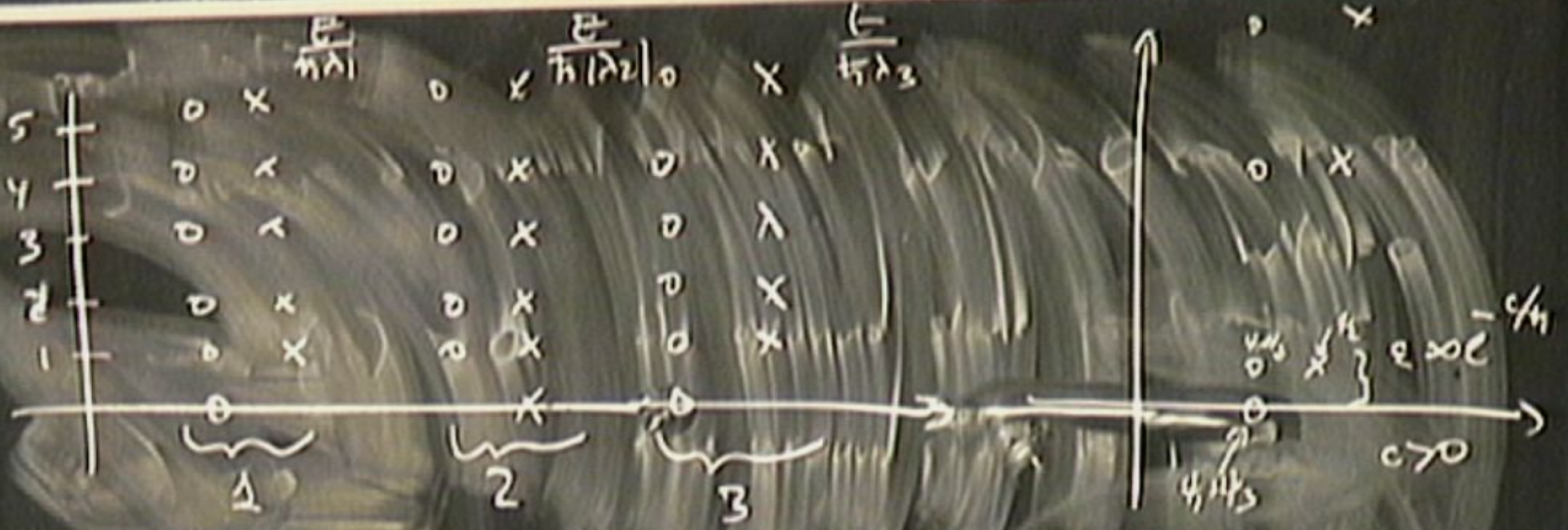


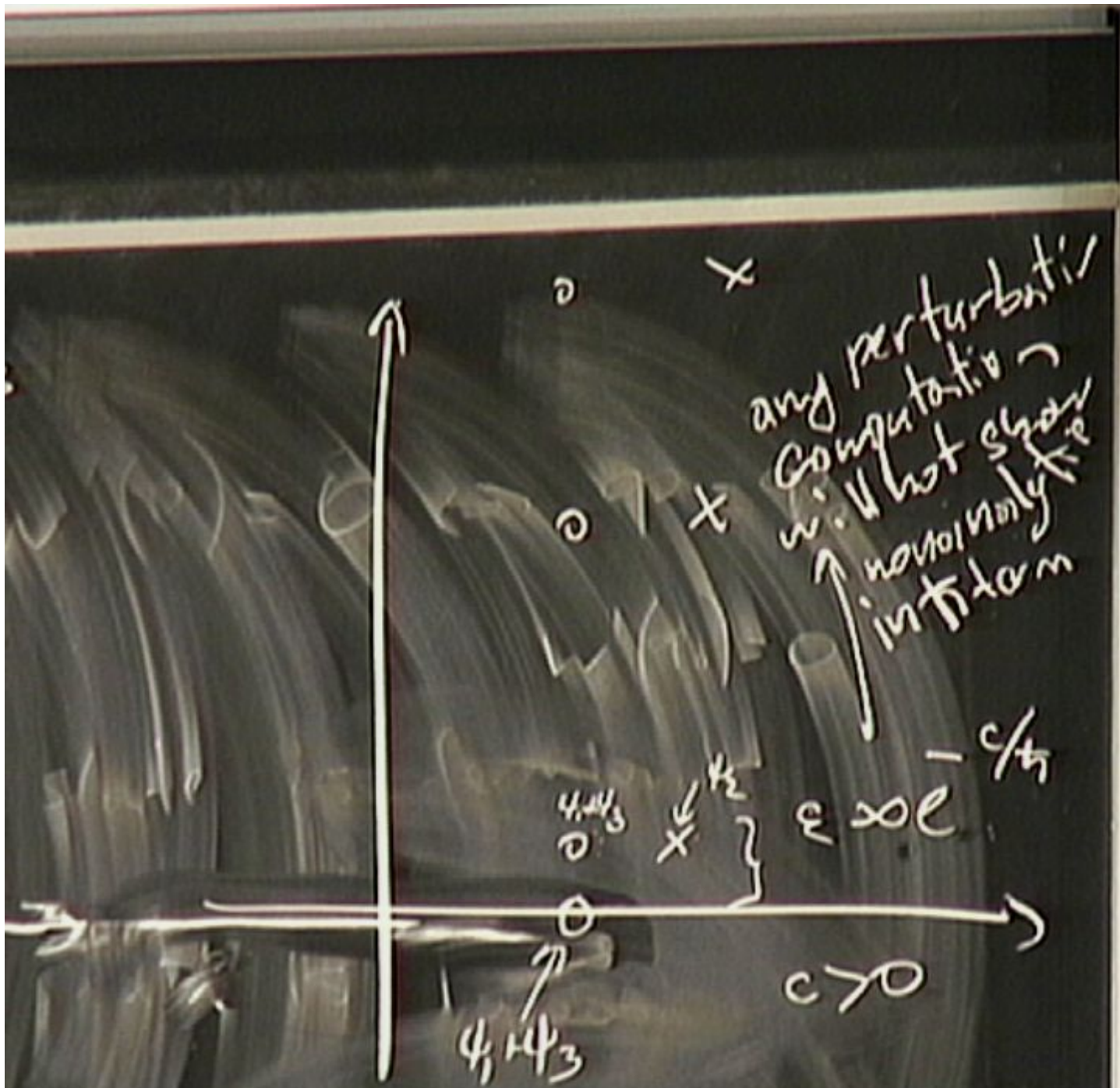




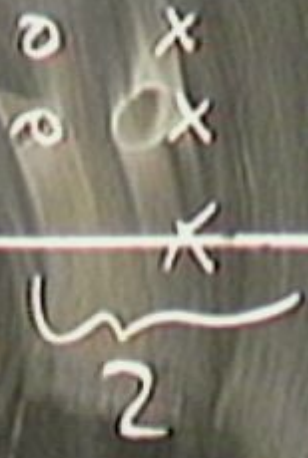




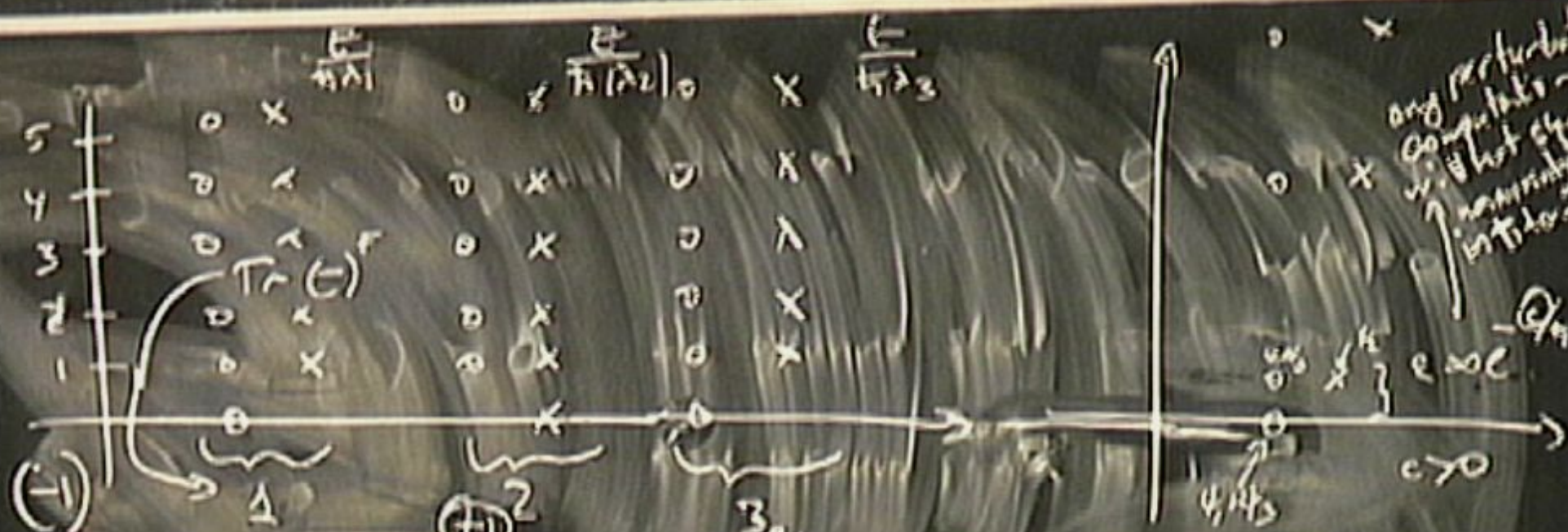




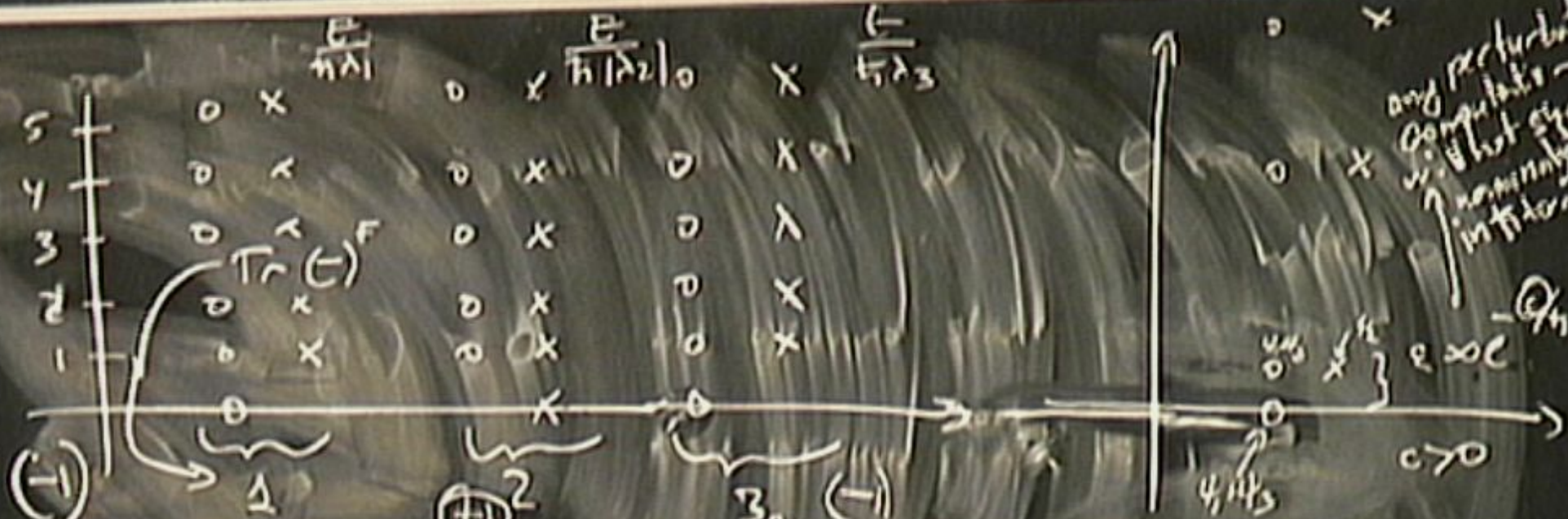
?



Salomonson and van Hoffen.

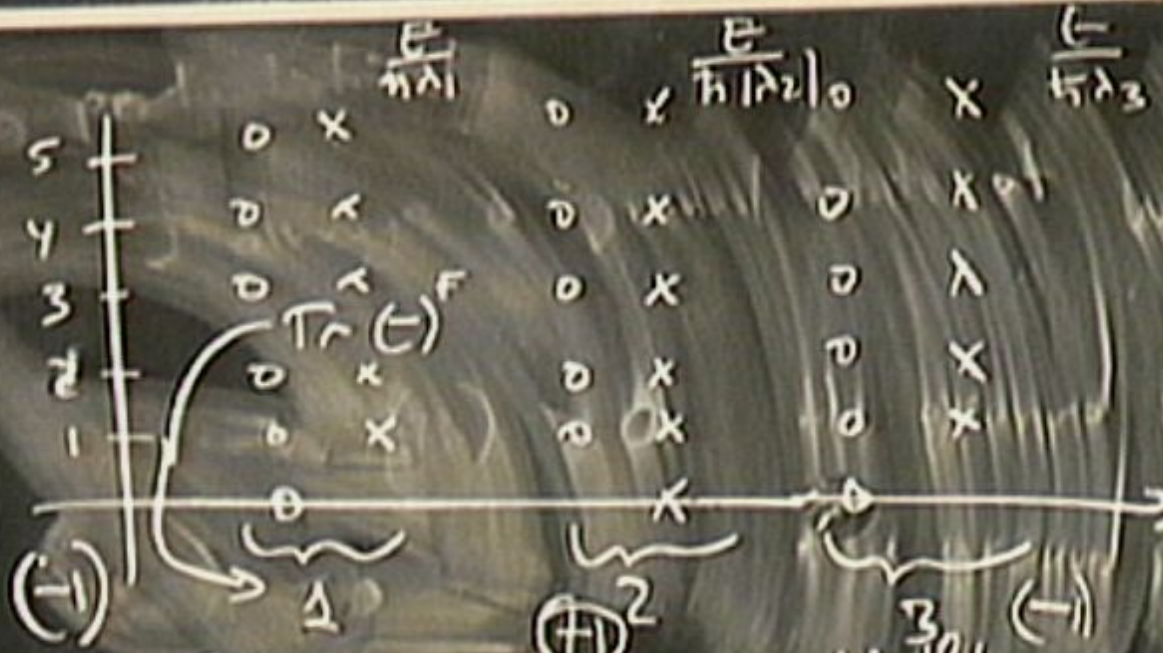


Salomonson and van Hoften.



Salomonson and van Hotten.

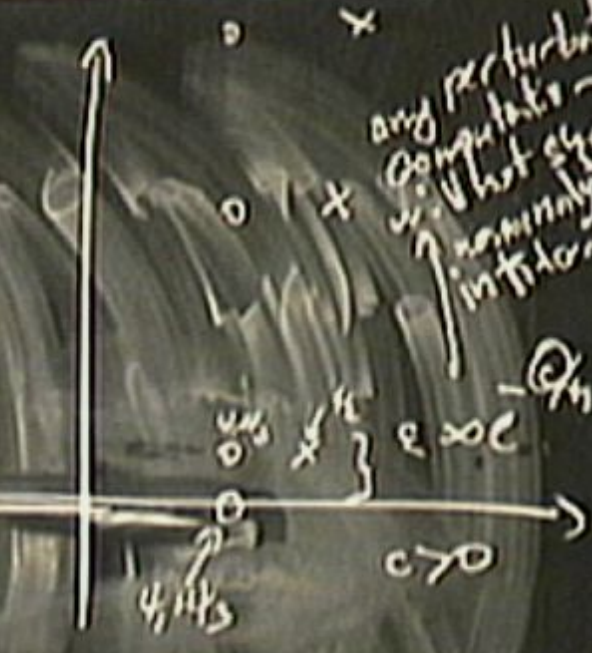
$$T_{\text{perturb}}(-)^F = -1 + 1 - 1 = -1$$



(-)

Salomonson and van Holten.

$$Tr_{pert}(-)^F = -1 + 1 - 1 = -1$$



$$Tr_{pert}(-)^F = -1$$



$$T_{\text{eff}} = 0 = \sum_{n \neq 0} \langle n | \hat{O} | n \rangle$$

... ..

(... ..) α ground state

... ..

$$\mathcal{U} = \begin{pmatrix} \hat{\omega}_+(\varphi) \\ 0 \end{pmatrix}$$

fermionic

$$\hat{\omega}_+(\varphi) = \infty c$$

$$\text{Tr} \rho = 1 = \sum_{n \in \text{basis}} \langle n | \rho | n \rangle$$

$$\lim_{\beta \rightarrow \infty} \text{Tr} (-)^F e^{-\beta H}$$

(odd) π ground states

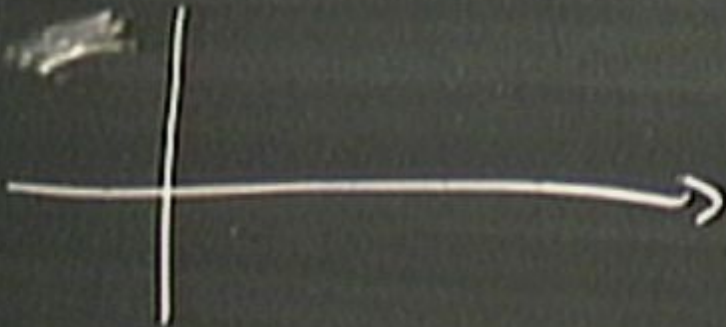
$$\mathcal{U} = \begin{pmatrix} \hat{\omega}_+(\varphi) \\ 0 \end{pmatrix}$$

fermionic

$$\hat{\omega}_+(\varphi) \rightarrow c$$

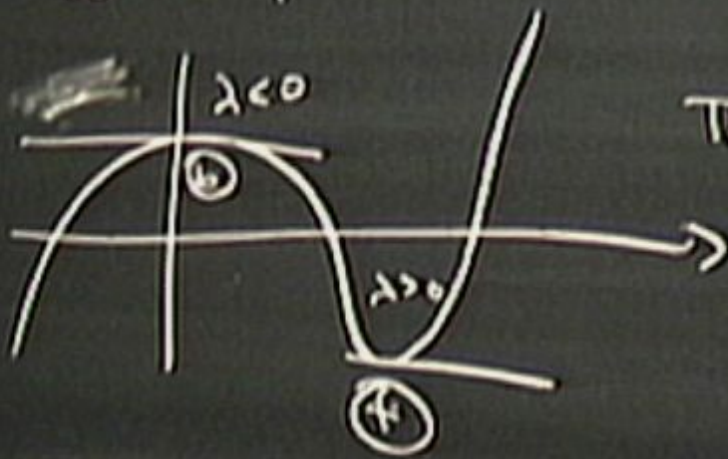
Example 2

$$W = q^3 + \text{subleading terms.}$$



Example 2

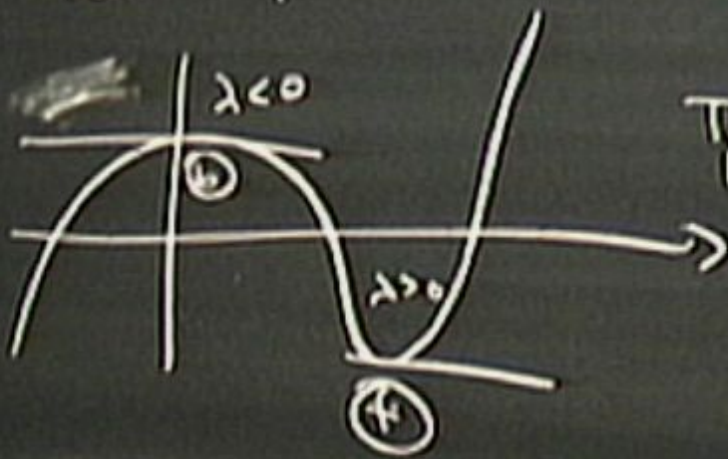
$w = \varphi^3 + \text{subleading terms.}$



$$\text{Tr}(-)^F = -1 + 1 = 0$$

Example 2

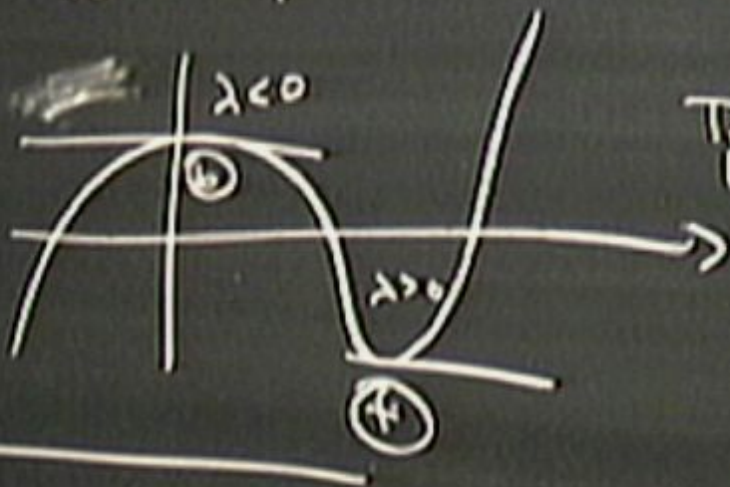
$w = q^3 + \text{subleading terms.}$



$$T_{\text{perturbative}}(\epsilon)^F = -1 + 1 = 0$$

Example 2

$w = q^3 + \text{subleading terms.}$

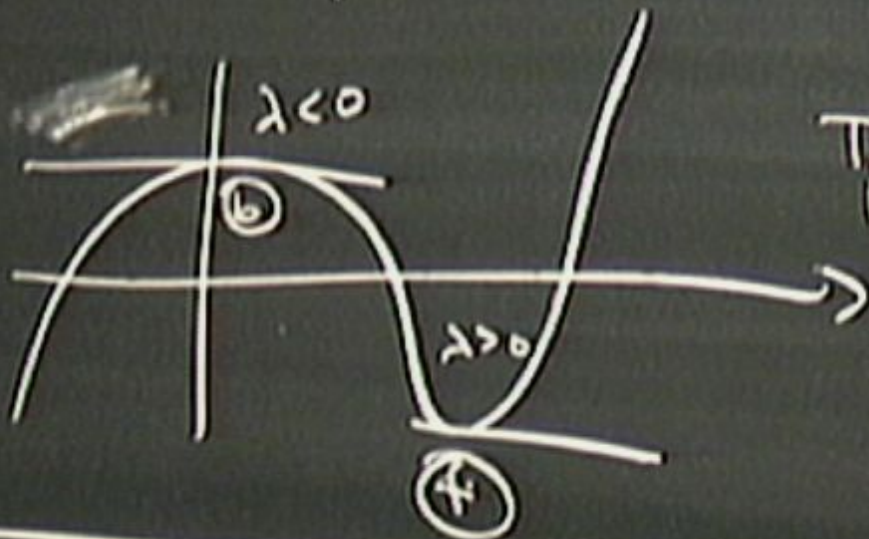


$$T_{\text{perturbative}}(\Theta)^F = -1 + 1 = 0$$

multifid

Example 2

$$W = \varphi^3 + \text{subleading terms.}$$



$$T_{\text{perturbative}}^{(-)F} = -1 + 1 = \underline{0}$$

$$\hat{\omega}_+ \propto e^{-W/\hbar}$$

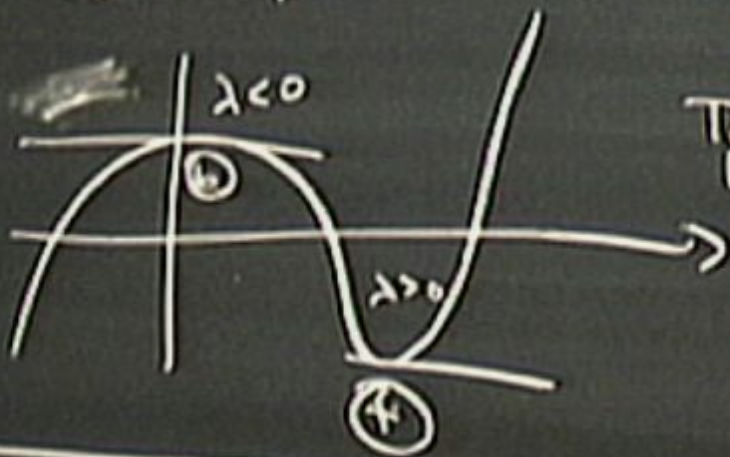
$$\hat{\omega}_- \propto e^{+W/\hbar}$$

exact:
→ no ground state

$$T_{\text{exact}}^{(-)F} = \underline{0}$$

Example 2

$$W = \varphi^3 + \text{subleading terms.}$$



$$T_{\text{perturbative}}(\Theta)^F = -1 + 1 = \underline{0}$$

$$\hat{\omega}_+ \sim e^{-W/\hbar} \quad \hat{\omega}_- \sim e^{+W/\hbar}$$

exactly
 \Rightarrow no ground state

$$T_{\text{exact}}^{(-)F} = \underline{0}$$

Example 3

\Rightarrow tune subleading terms in \mathcal{F}_n^2 in a special manner

$$W = \varphi^3 + \varphi$$

Example 3

⇒ tune subalgebra terms in \mathbb{F}_2 in a special manner.

$$W = \textcircled{\mathbb{F}^3} + \mathbb{F}$$

Example 3

\Rightarrow tune subleading terms in \mathcal{F}_2 in a special manner.

$$W = \textcircled{\varphi^2} + \varphi$$

\Rightarrow perturbatively.

$$W' = 3\varphi^2 + 1 = 0$$

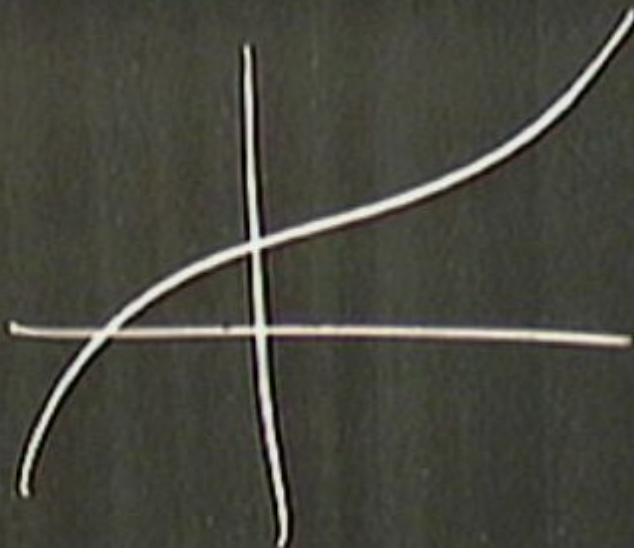
Example 3

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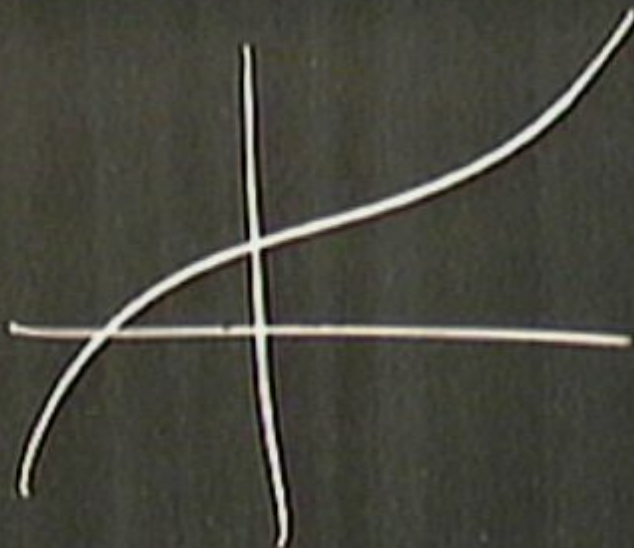
Example 3

⇒ tune subleading terms in Eq 2 in a special manner.

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Example 3

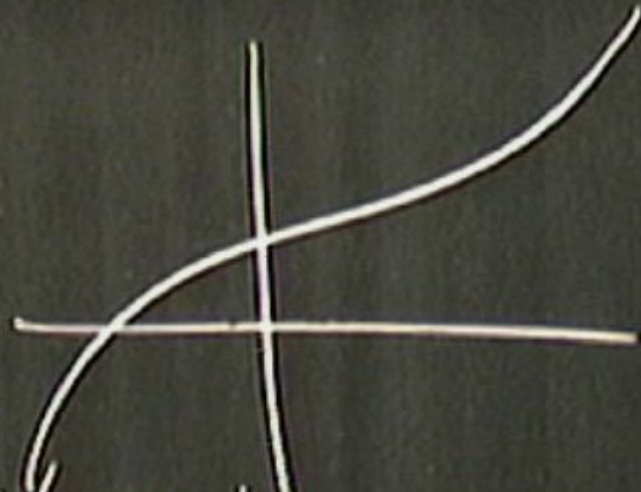
⇒ tune subleading terms in Eq 2 in a special manner

$$W = \textcircled{\varphi^3} + \varphi$$

⇒ perturbatively.

$$W' = 3\varphi^2 + 1 \neq 0$$

SUSY is broken classically



$$W = \varphi^3 + \lambda \varphi^2 + \dots$$

↑
is a parameter as we vary.

$$W = \varphi^3 + \lambda \varphi^2 + \dots$$

is a parameter as we vary.

$$V = \left(3\varphi^2 + 2\lambda\varphi + \dots \right)^2$$

$$W = \varphi^3 + \lambda \varphi^2 + \dots$$

is a parameter as we vary.

$$V = \left(3\varphi^2 + 2\lambda\varphi + \dots \right)^2$$

$$\Rightarrow E_i(\lambda)$$

$$W = \varphi^3 + \lambda \varphi^2 + \dots$$

↑
is a parameter as we vary.

$$V = \left(3\varphi^2 + 2\lambda\varphi + \dots \right)^2$$

$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} \langle \psi_n^{(s)} | \psi_n^{(s)} \rangle \lambda^n$$

$$W = \rho^3 + \lambda \rho^2 + \dots$$

is a parameter as we vary.

$$V = \left(3\rho^2 + 2\lambda\rho + \dots \right)^2$$

$$\Rightarrow E(\lambda) = \sum_{n=0}^{\infty} \frac{8}{5} \frac{\lambda^n}{(3)^n} \rho^n$$

what is the radius of convergence?

$$W = p^3 + \lambda p^2 + \dots$$

is a parameter as we vary.

$$V = \left(3p^2 + 2\lambda p + \dots \right)^2$$

$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} F_i^{(n)} \lambda^n$$

\Rightarrow usually in QFT perturb. expansions are asymptotic

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$$W = p^3 + \lambda p^2 + \dots$$

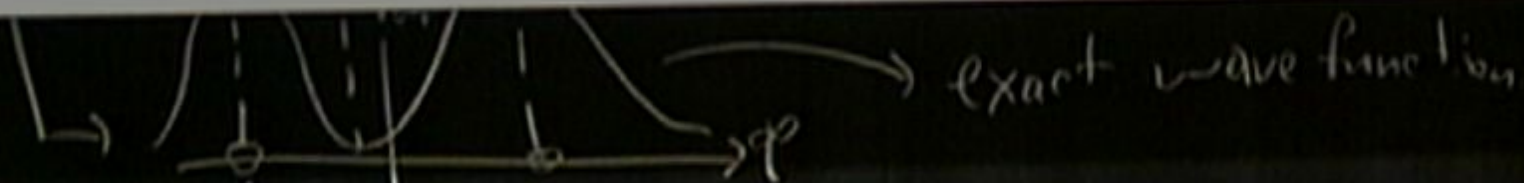
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$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} F_i^{(n)} \lambda^n$$

what is the radius of convergence?

\Rightarrow usually in QFT perturb. expansions are asymptotic
 \Rightarrow so, because there corrections nonanalytic in λ .



$$W = \varphi^3 + \lambda \varphi^2 + \dots$$

is a parameter as we vary.

$$V = \left(3\varphi^2 + 2\lambda\varphi + \dots \right)^2$$

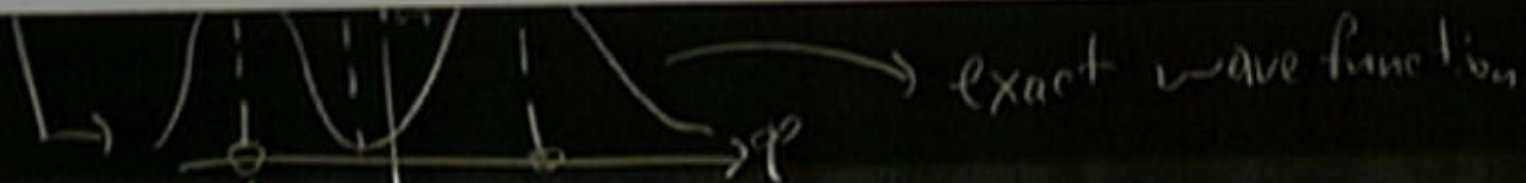
$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} E_i^{(n)} \lambda^n$$

what is the radius of convergence?

\Rightarrow usually in QFT perturb. expansions are asymptotic

\Rightarrow so, because there corrections nonanalytic in λ .

$$\lambda \varphi^4 \gg 0$$



$$W = \varphi^3 + \lambda \cdot \varphi^2 + \dots$$

is a parameter as we vary.

$$V = \left(3\varphi^2 + 2\lambda\varphi + \dots \right)^2$$

what is the radius of convergence?

$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} E_i^{(n)} \lambda^n$$

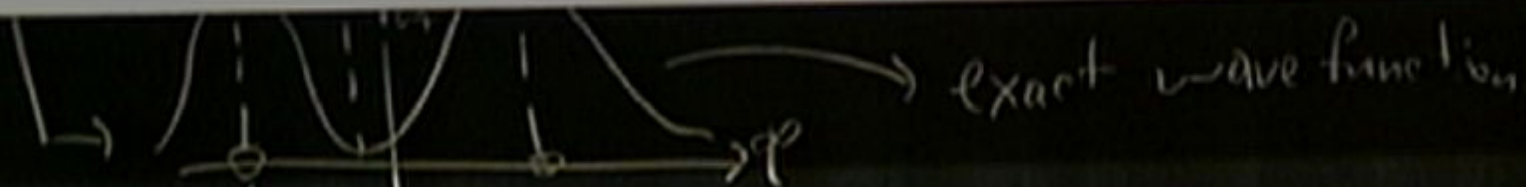
\Rightarrow usually in QFT perturb. expansions are asymptotic

\Rightarrow so, because there corrections nonanalytic in λ .

$$\lambda \varphi^4 \gg 0$$

$$e^{-1/\lambda}$$

Taylor expansion (in λ)



$$W = \varphi^3 + \lambda \cdot \varphi^2 + \dots$$

is a parameter as we vary.

$$V = \left(3\varphi^2 + 2\lambda\varphi + \dots \right)^2$$

$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} E_i^{(n)} \lambda^n$$

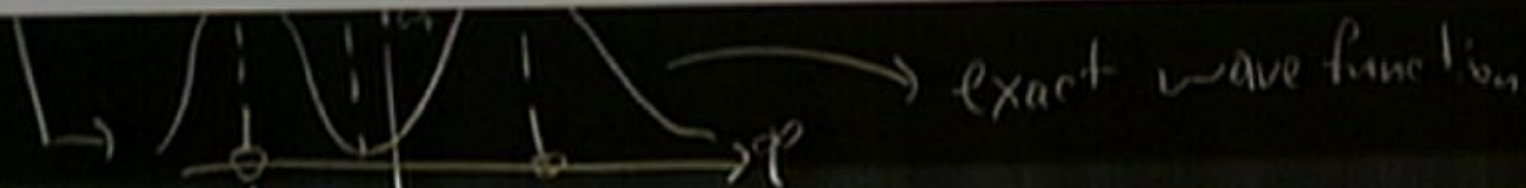
what is the radius of convergence?

\Rightarrow usually in QFT perturb. expansions are asymptotic

\Rightarrow so, because $\lambda \varphi^4 \gg 0$ these corrections nonanalytic in λ .

$e^{-1/\lambda} = \text{Taylor expansion for } 0$

$0 + 0 \cdot \lambda + 0 \cdot \lambda^2 + 0 \cdot \lambda^3 + \dots$



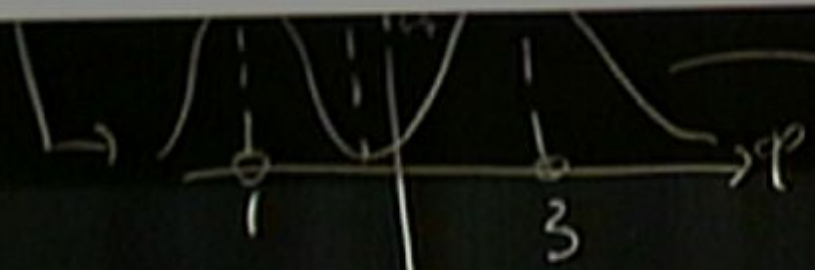
$= \varphi^3 + \lambda \cdot \varphi^2 + \dots$
 is a parameter as we vary.

$V = (3\varphi^2 + 2\lambda\varphi + \dots)^2$
 $\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} E_i^{(n)} \lambda^n$

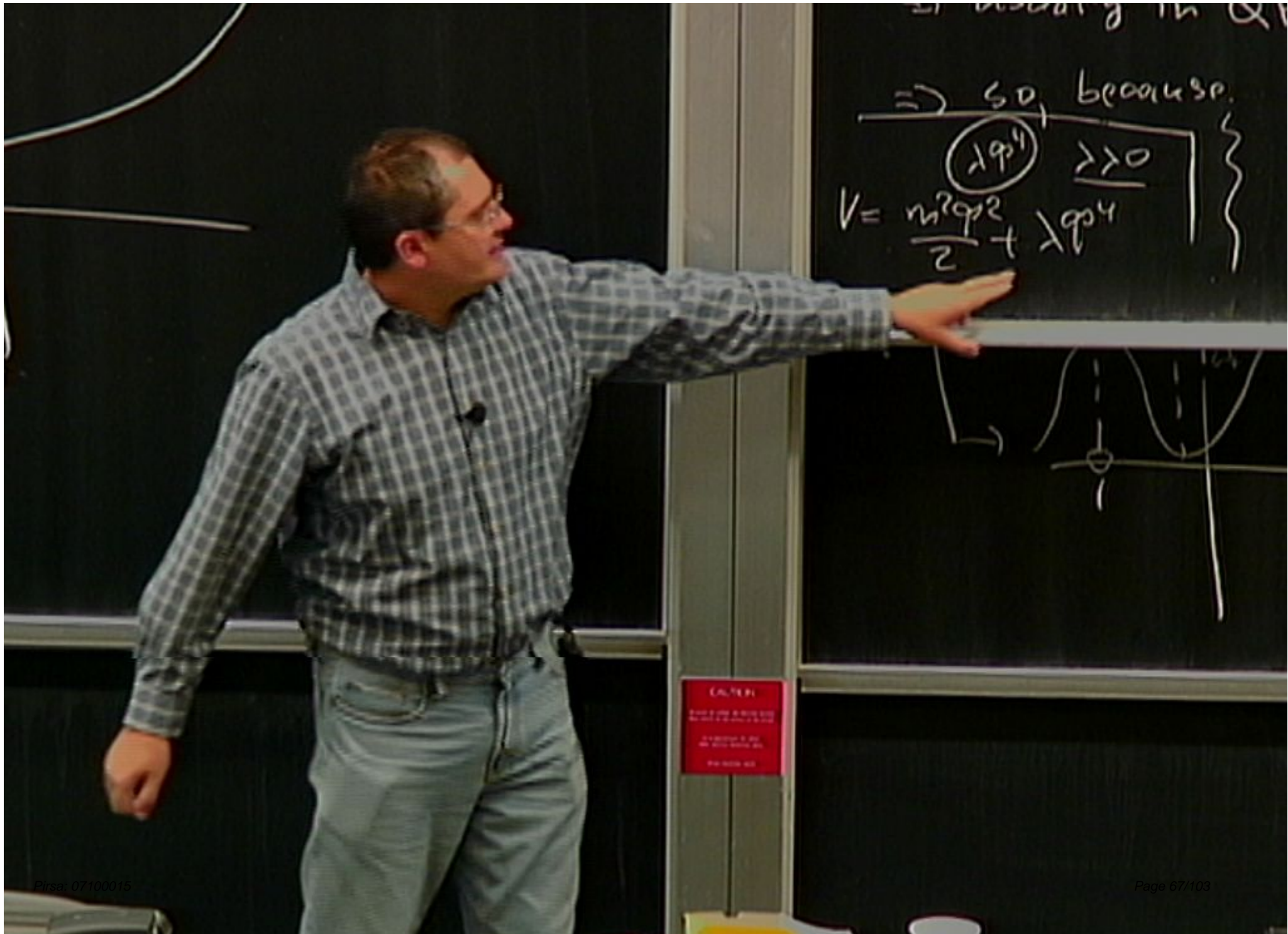
what is the radius of convergence?

\Rightarrow usually in QFT perturb. expansions are asymptotics

\Rightarrow so, because $\lambda \gg 0$ there corrections nonanalytic in λ .
 $e^{-1/\lambda} = 0 + 0 \cdot \lambda + 0 \cdot \lambda^2 + 0 \cdot \lambda^3 + \dots$
 $e^{-1/\lambda} = \lambda \rightarrow 0^- + \infty$
Taylor expansion for 0!



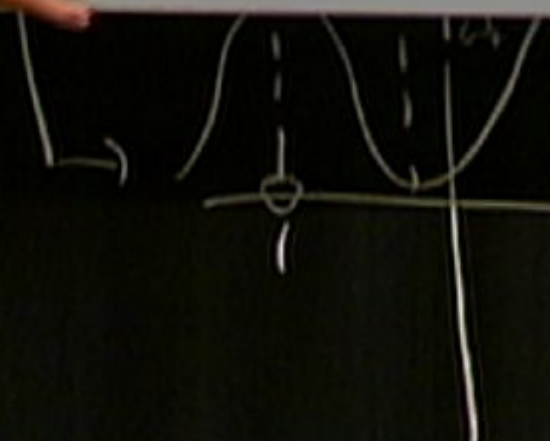
exact wave function



\Rightarrow so, because.

λq^4 $\lambda > 0$

$V = \frac{m^2 q^2}{2} + \lambda q^4$



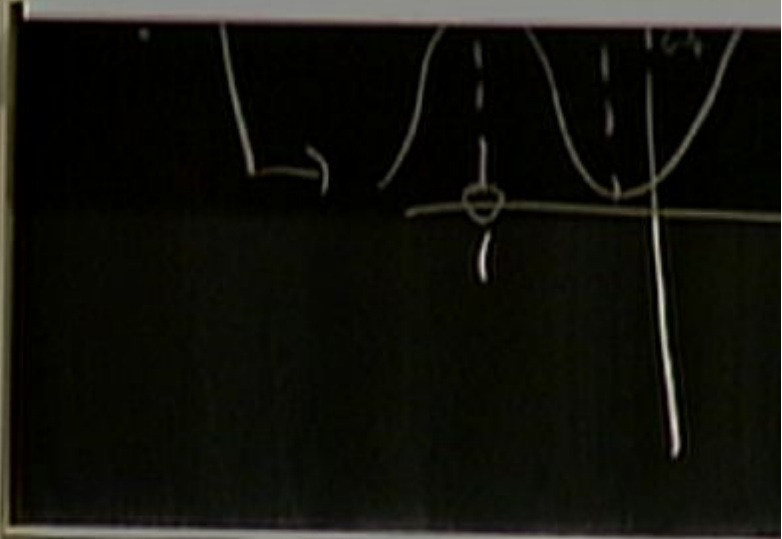
CAUTION
DO NOT TOUCH THE BOARD
OR THE EQUIPMENT
OR THE WALLS



\Rightarrow so, because.

$$V = \frac{m^2 \phi^2}{2} \mp \lambda \phi^4$$

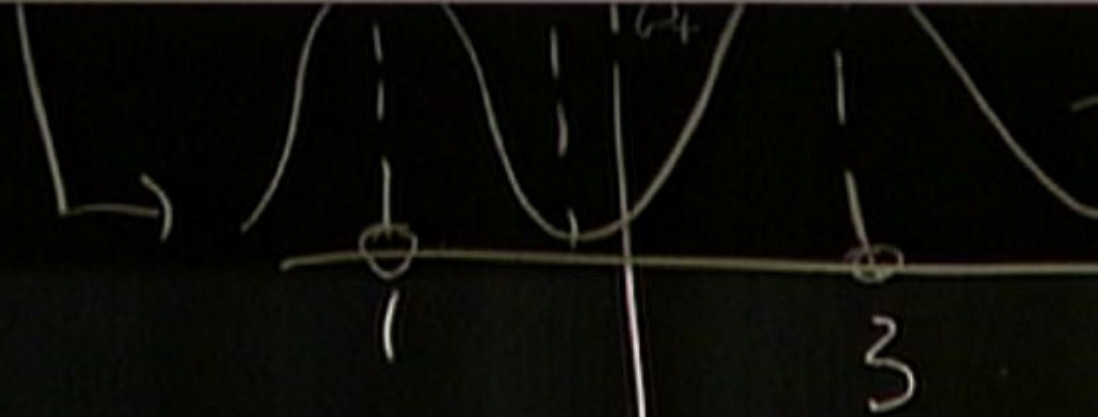
$\lambda > 0$



CAUTION
DO NOT TOUCH THE BOARD
OR THE EQUIPMENT

⇒ usually in QFT p

⇒ so, because. there e^{-iHt}
 e^{-iHt}
 $V = \frac{m^2 \phi^2}{2} + \lambda \phi^4$
 $\lambda > 0$
 $\lambda \rightarrow -\lambda$



What is the radius of convergence?

$$\int_{-\infty}^{+\infty} dx e^{-x^2 + \lambda x^4}$$

Expansions are asymptotics

nonanalytic in λ .

$$0 + 0 \cdot \lambda + 0 \cdot \lambda^2 + 0 \cdot \lambda^3 + \dots$$

$$+\infty$$

for
expansion
around
 0^-

what is the radius of convergence?

$$\int_{-\infty}^{+\infty} dx e^{-x^2 + \lambda x^4} = \sum_{n=0}^{\infty} \frac{\lambda^n}{n!} \int_{-\infty}^{+\infty} dx x^{4n} e^{-x^2}$$

expansions are asymptotic, nonanalytic in λ .

$$0 + 0 \cdot \lambda + 0 \cdot \lambda^2 + 0 \cdot \lambda^3 + \dots$$

what is the radius of convergence?

$$\int_{-\infty}^{+\infty} dx e^{-x^2 + \lambda x^4} = \sum_{n=0}^{\infty} \frac{\lambda^n}{n!} \int_{-\infty}^{+\infty} dx (-x^4)^n e^{-x^2}$$

expansions are asymptotic
nonanalytic in λ .

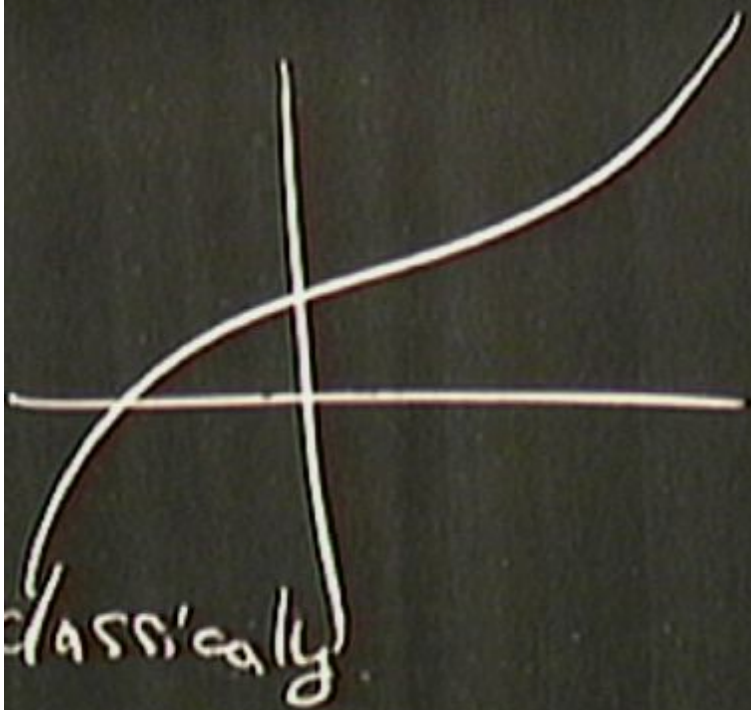
$$0 + 0 \cdot \lambda + 0 \cdot \lambda^2 + 0 \cdot \lambda^3 + \dots$$

Convergence!

$$\int_{-\infty}^{+\infty} dx e^{-x^2 + \lambda x^4}$$
$$= \sum_{n=0}^{\infty} \frac{\lambda^n}{n!} \int_{-\infty}^{+\infty} dx (-x^2)^n e^{-x^2}$$

Signs are asymptotic,
analytic in λ .

in $E \wedge 2$ in a special manner.



QED

$$e^2 \rightarrow -e^2$$

$$V = (3\varphi)$$

$$\Rightarrow E:$$

$$\Rightarrow \text{USL}$$

$$\Rightarrow \frac{50}{+}$$

$$\textcircled{\lambda \varphi^4}$$

$$V = \frac{m^2 \varphi^2}{2} + \frac{\lambda}{4} \varphi^4$$

$$W = \varphi^3 + \lambda \varphi^4 + \dots$$

is a parameter as we vary.

$$V = \left(3\varphi^2 + \lambda \varphi^3 + \dots \right)^2$$

what is the radius of
convergence?

$$\Rightarrow E_i(\lambda) = \sum_{n=0}^{\infty} F_i^{(n)} \lambda^n$$

If the deformation is subleading \Rightarrow we expect the
perturbative expansion to converge

Perturbative

$$V(\phi) = m^2 \phi^2 + \lambda \phi^4$$

$$f(x) = x^2 + \lambda x^4$$

⇒ If vary subleading parameter in a model.

The spectrum is analytic under such variations.



If $E_{\text{vacuum}}(\lambda) \neq 0$

Consider potential $w(\phi)$

Wavefunction

$$\Psi = \begin{pmatrix} \psi_1 \\ \psi_2 \\ \vdots \end{pmatrix}$$

$$\partial_L \Psi = \dots$$

⇒ If vary subleading parameter in a model.

The spectrum is analytic under such variations.



If $E_{\text{vacuum}}(\lambda) \neq 0$ (generically)



⇒ If vary subleading parameter in a model.

The spectrum is analytic under such variations.



If $E_{\text{vacuum}}(\lambda) \neq 0$ (generically) →

~~Susy~~ (0)

* If $E_{\text{vacuum}}(\lambda) = 0$ (generically) (P)

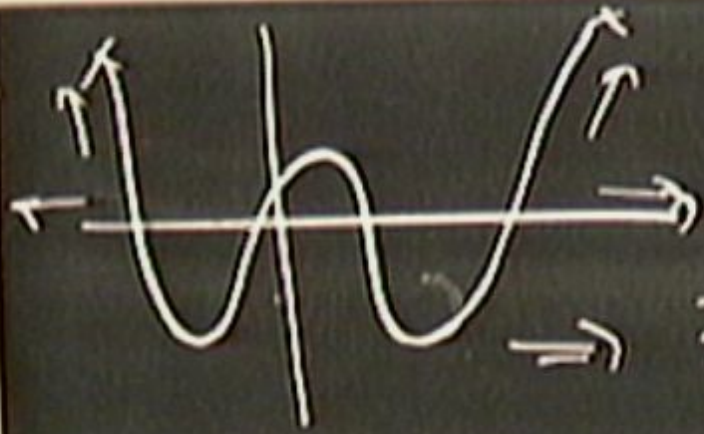
⇒ If vary subleading parameter in a model.

The spectrum is analytic under such variations



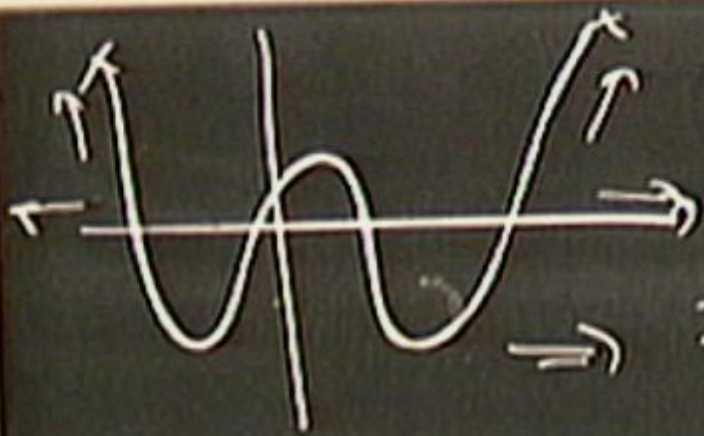
* If $E_{\text{vacuum}}(\lambda) \neq 0$ (generically) \rightarrow ~~SUSY~~

If $E_{\text{vacuum}}(\lambda) = 0$ (generically) \rightarrow SUSY



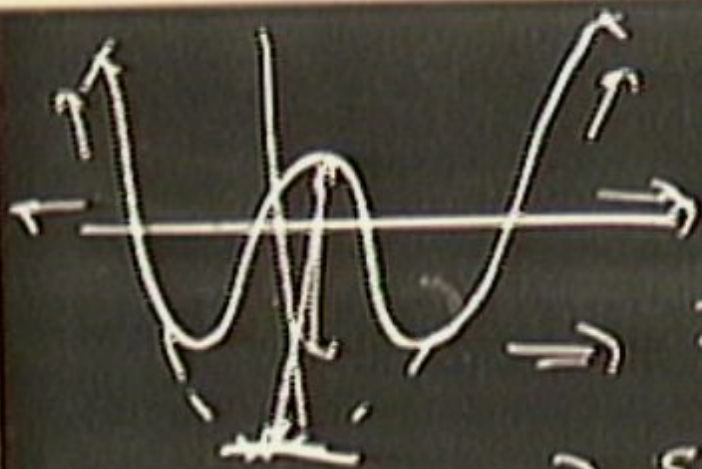
$\Rightarrow \exists$ at least one

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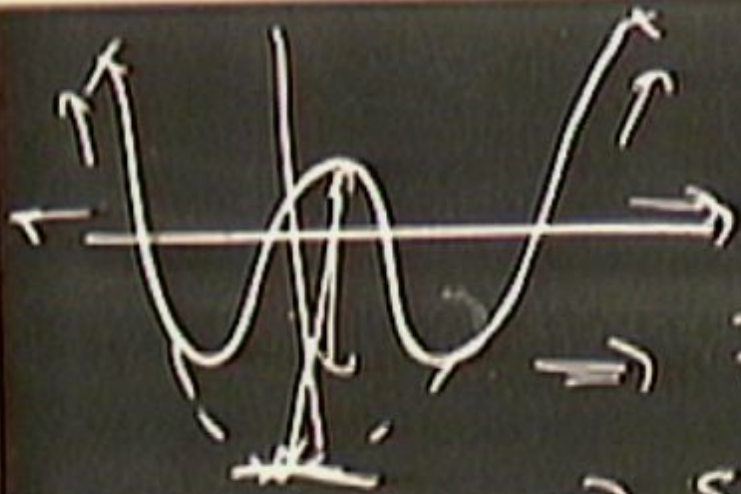
$\Rightarrow \exists$ at least one extremum.

\Rightarrow SUSY must be preserved.



$\Rightarrow \exists$ at least one extremum.

\Rightarrow SUSY must be preserved.



$\Rightarrow \exists$ at least one extremum.

\Rightarrow SUSY must be preserved.

\Rightarrow under smooth variation $\mathcal{T}(-)^F$ is unchanged.

~~1/1~~ \Rightarrow SUSY ~~must~~ be preserved.

Under smooth variation $T(-)^F$ is unchanged

Witten index paper:

NPB 202, 1982, 253

$$\text{Perf}_n = -1 + 1 - 1 = -1$$

Susy

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (W')^2 - \frac{1}{2} \hbar \sigma^3 W'' \rightarrow \text{SQM}$$

$\langle \psi | H | \psi \rangle = 0$ (generally) \rightarrow susy

Susy

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (W')^2 - 3\frac{1}{2} g^2 W''' \rightarrow \text{SQM}$$



Susy

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (W')^2 - 3t_5^3 W''' \rightarrow \text{SQM}$$

\Rightarrow superspace + superfield formalism

$(D \neq 0)$ (generally) \rightarrow susy

Sub.

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (w')^2 - 3t \delta^3 w''' \rightarrow \text{SQM}$$

⇒ superspace + superfield formalism

⇒ we need to recast SQM really as a QFT

$$\Rightarrow \int = \int dt \mathcal{L}(\text{some fields})$$

Subj.

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (w')^2 - 3t \vec{\sigma} \cdot w''' \rightarrow \text{SQM}$$

→ superspace + superfield formalism

→ we need to recast SQM really as off-shell QFT

$$\Rightarrow \int = \int dt \mathcal{L}[\text{some fields}] \Rightarrow H = \dots$$

Smb.

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (w')^2 - \frac{1}{2} \hbar \vec{\sigma} \cdot w'' \rightarrow \text{SQM}$$

→ superspace + superfield formalism

→ we need to recast SQM really as a $\hbar \rightarrow 0$ limit of QFT

$$\Rightarrow \int = \int dt \mathcal{L}[\text{some fields}] \Rightarrow H = \dots$$

Smb

$$H = \frac{1}{2} \pi^2 + \frac{1}{2} (W')^2 - \frac{1}{2} \psi \sigma^3 W'' \rightarrow \text{SQM}$$

⇒ superspace + superfield formalism

⇒ we need to recast SQM really as path integral $\int \mathcal{D}Q$

$$\Rightarrow \int = \int dt \mathcal{L}(\text{some fields}) \Rightarrow H = \dots$$

Def:

$$\psi = \sqrt{\hbar} \sigma^-$$

$$\psi^+ = \sqrt{\hbar} \sigma^+$$

$$Q = \sigma^- [f'(p) + i\pi]$$

$$\{Q, Q^+\} = 2\hbar$$

$$Q^+ = \sigma^+ [f'(p) - i\pi]$$

Def: $\psi = \sqrt{\hbar} \sigma^-$ $\psi^+ = \sqrt{\hbar} \sigma^+$

$Q = \sigma^- [f'(p) + i\pi]$ $\{Q, Q^+\} = 2\hbar$

$Q^+ = \sigma^+ [f'(p) - i\pi]$ $\{Q, Q\} = \{Q^+, Q^+\} = 0$

$\{Q^+, Q\} = \hbar$

2021/982, 253

Def. $\psi = \sqrt{h} \sigma^-$ $\psi^\dagger = \sqrt{h} \sigma^+$

$Q = \sigma^- [f'(\tau) + i\pi]$ $\{Q, Q^\dagger\} = 2H$

$Q^\dagger = \sigma^+ [f'(\tau) - i\pi]$ $\{Q, Q\} = \{Q^\dagger, Q^\dagger\} = 0$

$\{\psi^\dagger, \psi\} = h$ $\{\psi^\dagger, \psi^\dagger\} = 0, \quad \{\psi, \psi\} = 0.$

2021, 1982, 253

Def. $\psi = \sqrt{\hbar} \phi$ $\phi^+ = \sqrt{\hbar} \phi^+$ as operators is S. picture

$$Q = \sigma^- [f'(p) + i\pi]$$

$$\{Q, Q^+\} = 2\hbar$$

$$Q^+ = \sigma^+ [f'(p) - i\pi]$$

$$\{Q, Q\} = \{Q^+, Q^+\} = 0$$

$$\{\psi^+, \psi\} = \hbar$$

$$\{\psi^+, \psi^+\} = 0, \quad \{\psi, \psi\} = 0.$$

Def.

$$\psi = \sqrt{\hbar} \sigma^-$$

$$\psi^+ = \sqrt{\hbar} \sigma^+$$

as operators is S. picture

↓

Heisenber pic

$\psi \rightarrow \psi(t)$

$$Q = \sigma^- [f'(p) + i\pi]$$

$$\{Q, Q^+\} = 2\hbar$$

$$Q^+ = \sigma^+ [f'(p) - i\pi]$$

$$\{Q, Q\} = \{Q^+, Q^+\} = 0$$

$$\{\psi^+, \psi\} = \hbar$$

$$\{\psi^+, \psi^+\} = 0,$$

$$\{\psi, \psi\} = 0.$$

202, 1982, 253

Def:

$$\psi = \sqrt{\hbar} \sigma^- \quad \phi^+ = \sqrt{\hbar} \sigma^+$$

as operators in S. picture

↓

Heisenberg picture

$$\psi \rightarrow \psi(t)$$

$$Q = \sigma^- [f(p) + i\pi]$$

$$\{Q, Q^+\} = 2\hbar$$

$$Q^+ = \sigma^+ [f(p) - i\pi]$$

$$\{Q, Q\} = \{Q^+, Q^+\} = 0$$

$$\{\psi^+, \psi\} = \hbar$$

$$\{\psi^+, \psi^+\} = 0,$$

$$\{\psi, \psi\} = 0.$$

2007, 1982, 253

$$H = \frac{1}{2} \dot{\varphi}^2 + \frac{1}{2} (\varphi')^2 - \frac{1}{2} [\psi^\dagger, \psi] \varphi''$$

for mass we vary.

→ Hermiticity of commutator

$$H = \frac{1}{2} \dot{\varphi}^2 + \frac{1}{2} (\varphi')^2 - \frac{1}{2} [\psi^\dagger, \psi] \varphi'' \rightarrow \text{SQM.}$$



$$H = \frac{1}{2} \dot{\phi}^2 + \frac{1}{2} (\phi'')^2 - \frac{1}{2} [\psi^\dagger, \psi] \phi'' \rightarrow \text{SQM.}$$

$$\rightarrow S[\phi, \psi, \psi^\dagger] =$$

$$H = \frac{1}{2} \dot{\varphi}^2 + \frac{1}{2} (f')^2 - \frac{1}{2} [\psi^\dagger, \psi] f'' \rightarrow \text{SQM.}$$

$$\hookrightarrow S[\varphi, \psi, \psi^\dagger] = \int dt \left\{ \frac{1}{2} \dot{\varphi}^2 + i \psi^\dagger \dot{\psi} - \frac{1}{2} (f')^2 + \frac{1}{2} f [\psi^\dagger, \psi] \right\}$$

$$H = \frac{1}{2}\dot{\varphi}^2 + \frac{1}{2}(f')^2 - \frac{1}{2}[\psi^\dagger, \psi] f'' \rightarrow \text{SQM.}$$

$$\hookrightarrow S[\varphi, \psi, \psi^\dagger] = \int dt \left\{ \frac{1}{2}\dot{\varphi}^2 + i\psi^\dagger\dot{\psi} - \frac{1}{2}(f')^2 + \frac{1}{2}f[\psi^\dagger, \psi] \right\}$$