

Title: Inflation and its Cosmic Probes, Now and Then

Date: Sep 14, 2007 11:30 AM

URL: <http://pirsa.org/07090050>

Abstract:

CBI pol to Apr'05 @Chile

Acbar to Jan'06, 07f @SP

Bicep @SP

QUaD @SP

CBI2 to Dec'07

Quiet2

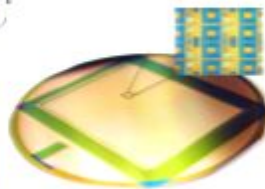
(1000 HEMTs)

Quiet1 @Chile

SZA

(Interferometer)
@Cal

APEX
(~400 bolometers)
@Chile



SCUBA2

(12000 bolometers)

JCMT @Hawaii



Spider

2312
bolometer
@LDB

ACT

(3000 bolometers)

@Chile EBEX@LDB

Clover
@Chile

Boom03@LDB

LMT@Mexico

2003

2005

2007

2017

2004

2006

2008

WMAP @L2 to 2009-2013?

SPT

(1000 bolometers)

@South Pole

Bpol@L2

DASI @SP

CAPMAP

AMI

Polarbear

(300 bolometers)

@Cal

ALMA

(Interferometer)

@Chile

Planck08.6

(84 bolometers)

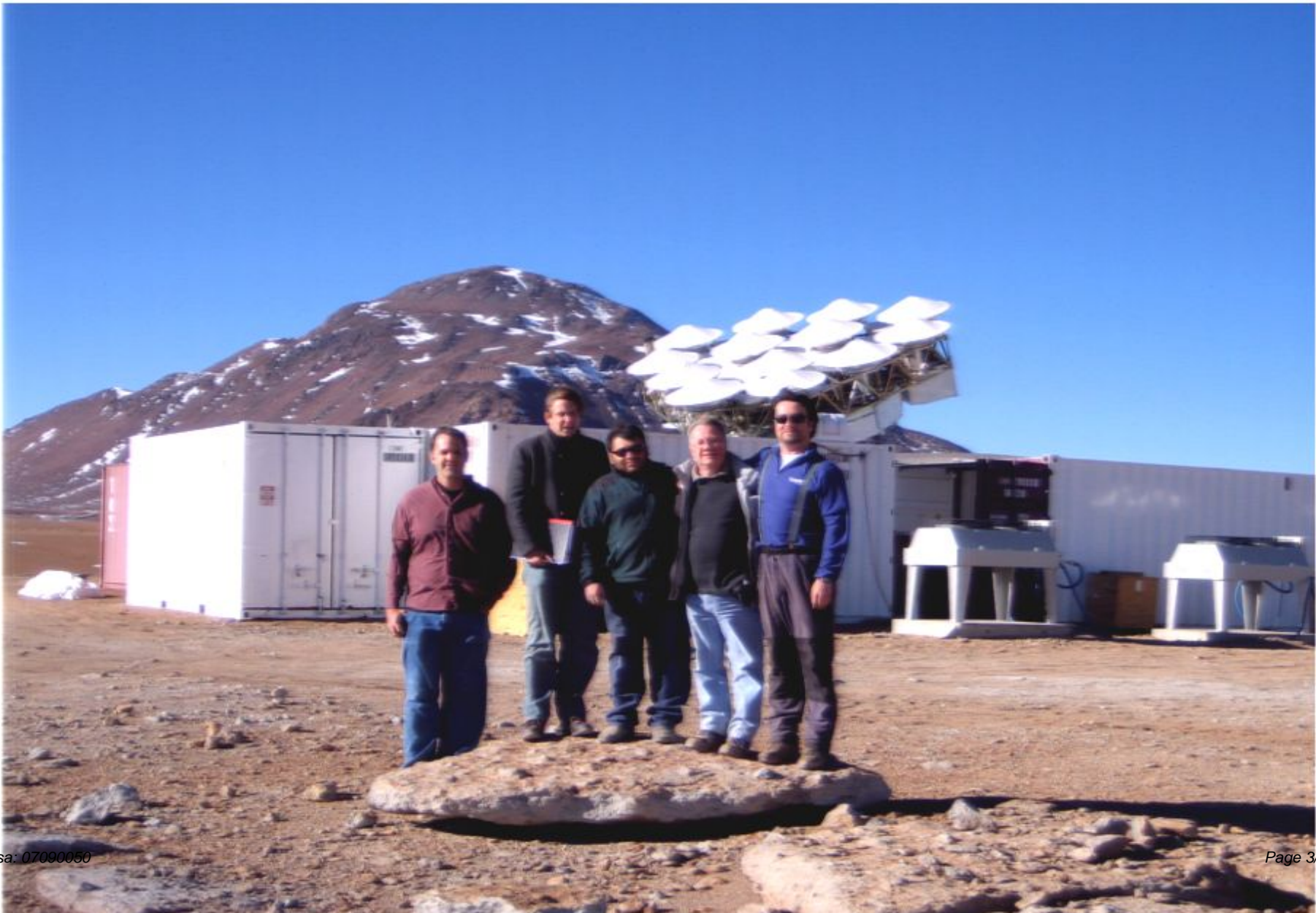
HEMTs @L2



GBT

CBI2@5040m

why Atacama? driest desert in the world. thus: cbi, toco, apex, asti, act, alma, quiet, clover



ACT@5170m



Inflation & its Cosmic Probes, now & then

Cosmic Probes **CMB, CMBpol (E,B modes of polarization)**

B from tensor: **Bicep, Planck, Spider, Spud, Ebex, Quiet, Pappa, Clover, ..., Bpol**

CFHTLS SN(192), WL(Apr07), JDEM/DUNE BAO, LSS, Ly α

Inflation Then $\varepsilon(k) = (1+q)(a) \sim r/16 \quad 0 < \varepsilon < 1$

= multi-parameter expansion in ($\ln H a \sim \ln k$)

Dynamics ~ Resolution ~ 10 good e-folds ($\sim 10^{-4} \text{Mpc}^{-1}$ to $\sim 1 \text{Mpc}^{-1}$ LSS)
-10+ parameters? Bond, Contaldi, Kofman, Vaudrevange 07

(k_p) i.e. $\varepsilon(k)$ is prior dependent now, not then. Large (uniform ε), Small uniform $\ln \varepsilon$). Tiny (roulette inflation of moduli; almost all string-inspired models)

Eisa, 10/09/06 **(KLMMT etc. Quevedo et al. Bond, Kofman, Prokushkin, Vaudrevange 07, Kallosh and Linde 07** Page 5/96

Inflation & its Cosmic Probes, **now** & then

Inflation Now $1+w(a) = \epsilon_s f(a/a_{\Lambda\text{eq}}, a_s/a_{\Lambda\text{eq}}, \zeta_s)$

goes to $\epsilon(a)_{\text{NS}} \approx 3/2 = 3(1+q)/2 \sim 1$ good e-fold. only ~ 2 params

Zhiqi Huang, Bond & Kofman 07 $\epsilon_s = 0.0 \pm 0.25$ now, to ± 0.08 Planck+JDEM SN, weak a_s

Cosmic Probes Now CFHTLS SN(192), WL(Apr07), CMB, BAO, LSS, Ly α

THEN

Standard Parameters of Cosmic Structure Formation

$$\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$$

$r < 0.6$ or < 0.28 95% CL

$$\Omega_k$$

$$\Omega_b h^2$$

$$\Omega_{dm} h^2$$

$$\Omega_\Lambda$$

$$\tau_c$$

$$n_s$$

$$n_t$$

$$\ln A_s \sim \ln \sigma_8$$

$$r = A_t / A_s$$

Standard Parameters of Cosmic Structure Formation

$$\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$$

Period of inflationary expansion,
quantum noise \rightarrow metric perturbations

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Scalar Amplitude

Standard Parameters of Cosmic Structure Formation

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$$\ln \mathcal{P}_t(k)$$

$$\ln \mathcal{P}_s(k)$$

Ω_k

New Parameters of Cosmic Structure Formation

$\Omega_b h^2$

$\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$

$\ln \mathcal{P}_t(k)$

$\Omega_{dm} h^2$

$\ln \mathcal{P}_s(k)$

τ_c

scalar spectrum
use order N Chebyshev
expansion in $\ln k$,
N-1 parameters
amplitude(1), tilt(2),
running(3), ...
(or N-1 nodal point k-
localized values)

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$$\ln \mathcal{P}_s(k)$$

$$\ln \mathcal{P}_t(k)$$

tensor (GW) spectrum
use order M Chebyshev
expansion in $\ln k$,
M-1 parameters
amplitude(1), tilt(2), running(3),...

scalar spectrum
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Dual Chebyshev expansion in $\ln k$:

Standard 6 is Cheb=2

Standard 7 is Cheb=2, Cheb=1

Run is Cheb=3

Run & tensor is Cheb=3, Cheb=1

Low order N,M power law but high order Chebyshev is Fourier like

New Parameters of Cosmic Structure Formation

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$$\epsilon(k), \quad k \approx Ha$$

$$\ln H(k_p)$$

$$H(k_p)$$

Ω_k

New Parameters of Cosmic Structure Formation

 $\Omega_b h^2$ $\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$ $\ln H(k_p)$ $\Omega_{dm} h^2$ $\epsilon(k), k \approx Ha$ $H(k_p)$ τ_c

**=1+q, the deceleration
parameter history**

$$\mathcal{P}_s(\mathbf{k}) \propto H^2/\epsilon, \mathcal{P}_t(\mathbf{k}) \propto H^2$$

**order N Chebyshev
expansion, N-1 parameters
(e.g. nodal point values)**

Ω_k

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$\ln H(k_p)$

$H(k_p)$

Hubble parameter at inflation at a pivot pt

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(e.g. nodal point values)**

**Hubble parameter at
inflation at a pivot pt
– $\epsilon = d \ln H / d \ln a$**

Ω_k

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$$\frac{-\epsilon}{1-\epsilon} = \frac{d \ln H}{d \ln k}$$

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$$\frac{-\epsilon}{1-\epsilon} = \frac{d \ln H}{d \ln k}$$

$$\mathcal{P}_s(\mathbf{k}) \propto H^2 / \epsilon, \quad \mathcal{P}_t(\mathbf{k}) \propto H^2$$

order N Chebyshev expansion, N-1 parameters (e.g. nodal point values)

Fluctuations are from stochastic kicks $\sim H/2\pi$ superposed on the downward drift at $\Delta \ln k = 1$.

Potential trajectory from HJ (SB 90,91):

$$V \propto H^2 \left(1 - \frac{\epsilon}{3}\right); \quad \frac{d\psi_{\text{inf}}}{d \ln k} = \frac{\pm \sqrt{V}}{1-\epsilon}$$

$$\epsilon = \left(\frac{d \ln H}{d \ln k} \right)^2$$

The Parameters of Cosmic Structure Formation

Cosmic Numerology: [astroph/0611198](#) – our Acbar paper on the basic 7+

WMAP3modified+B03+CBIcombined+Acbar06+LSS (SDSS+2dF) + DAS1
(incl polarization and CMB weak lensing and tSZ)

$$n_s = .958 \pm .015$$

$$\Omega_b h^2 = .0226 \pm .0006$$

$$.93 \pm .03 @0.05/\text{Mpc run\&tensor}$$

$$\Omega_c h^2 = .114 \pm .005$$

$$r = A_t / A_s < 0.28 \text{ 95\% CL}$$

$$\Omega_\Lambda = .73 +.02 - .03$$

$$<.36 \text{ CMB+LSS run\&tensor}$$

$$h = .707 \pm .021$$

$$dn_s / d \ln k = -.060 \pm .022$$

$$\Omega_m = .27 + .03 - .02$$

$$.038 \pm .024 \text{ CMB+LSS run\&tensor}$$

$$z_{\text{reh}} = 11.4 \pm 2.5$$

$$A_s = 22 \pm 2 \times 10^{-10}$$

E and B polarization mode patterns

Blue = +

Red = -

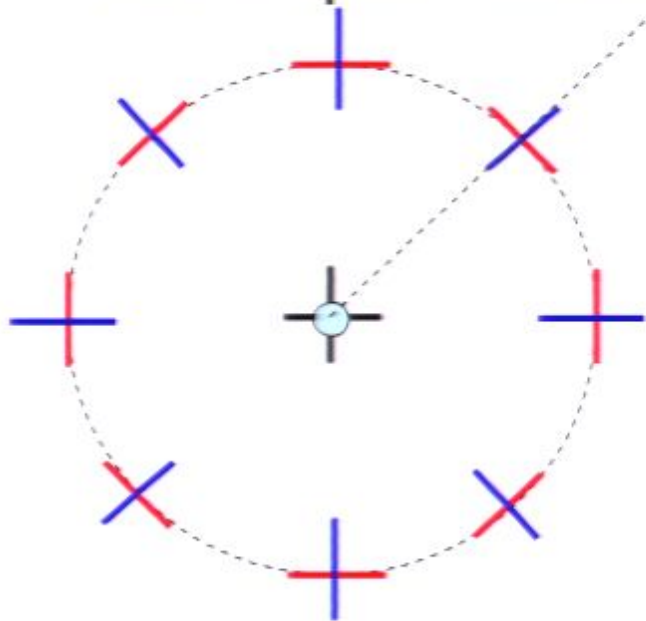
E="local" Q in 2D
Fourier space basis

B="local" U in 2D
Fourier space basis

Scalar

+

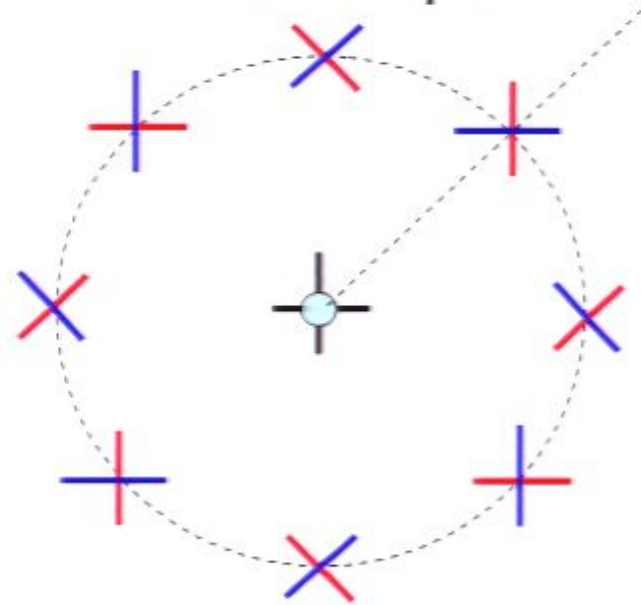
Tensor
(GW)



Tensor
(GW)

+

lensed
scalar

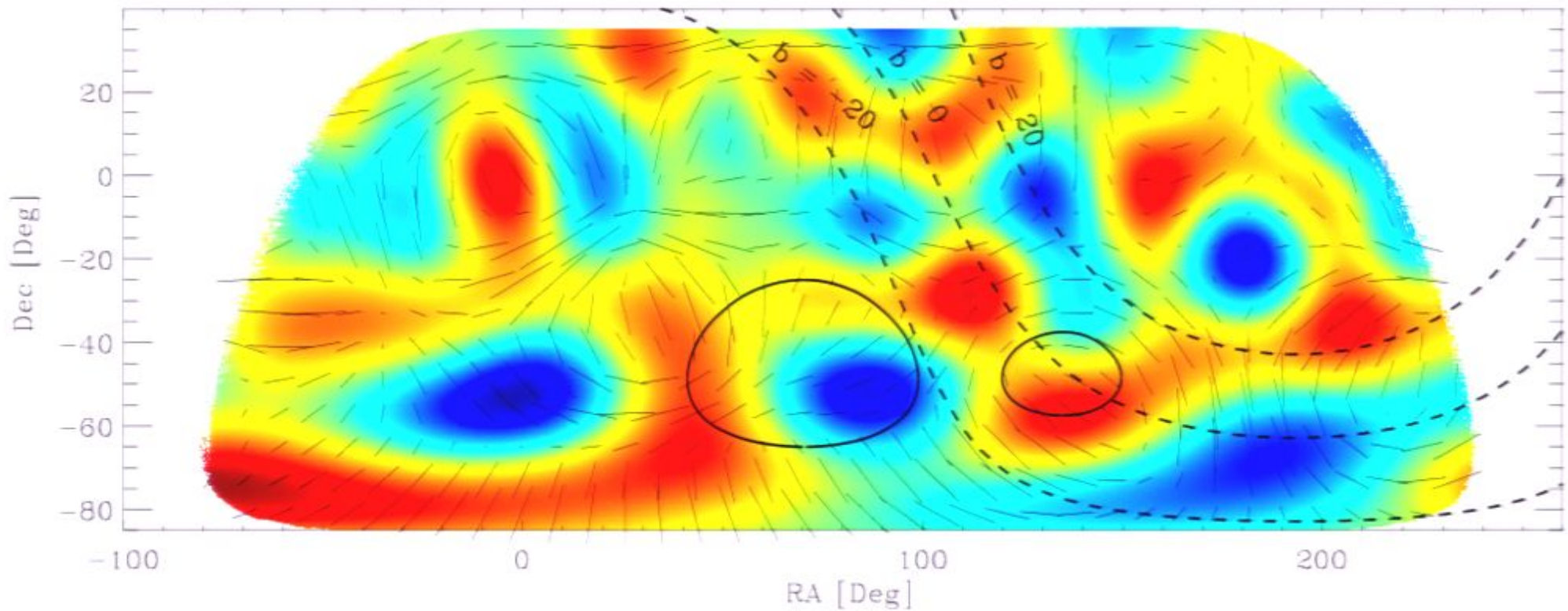


SPIDER Tensor Signal

- Simulation of large scale polarization signal

$$\frac{A_T}{A_S} = 0.1$$

No Tensor

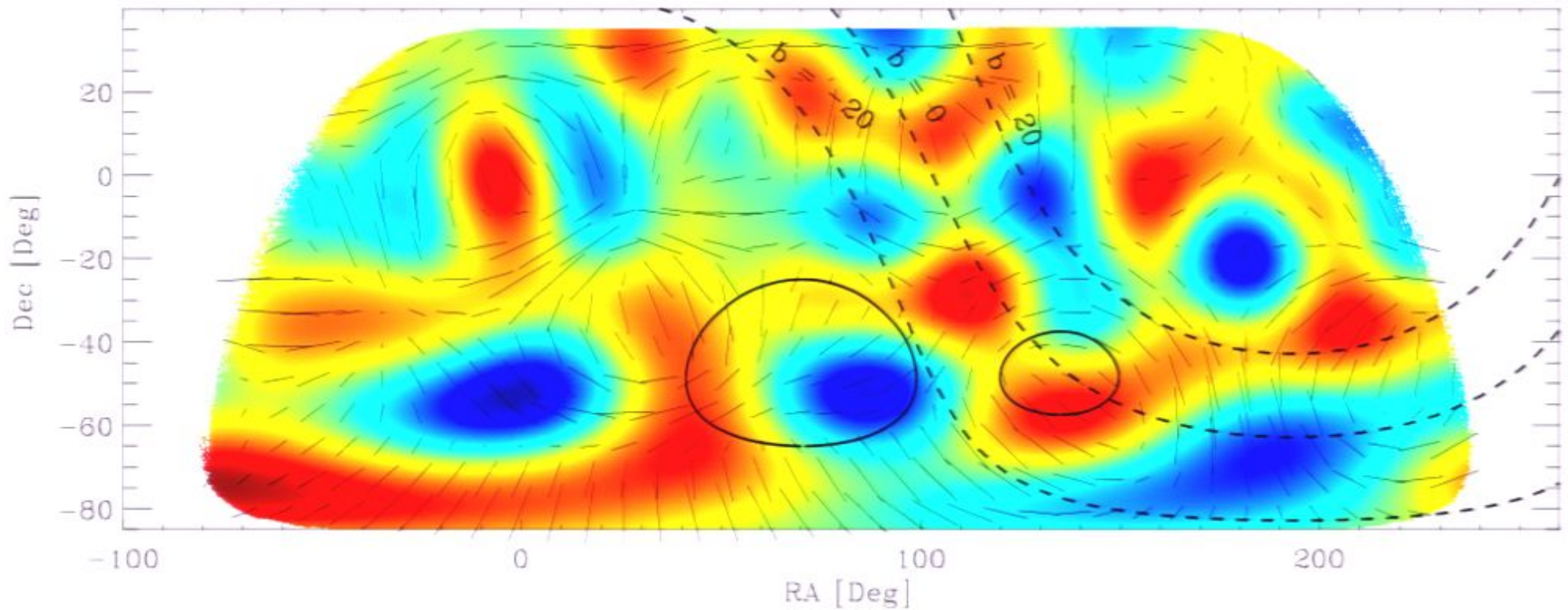


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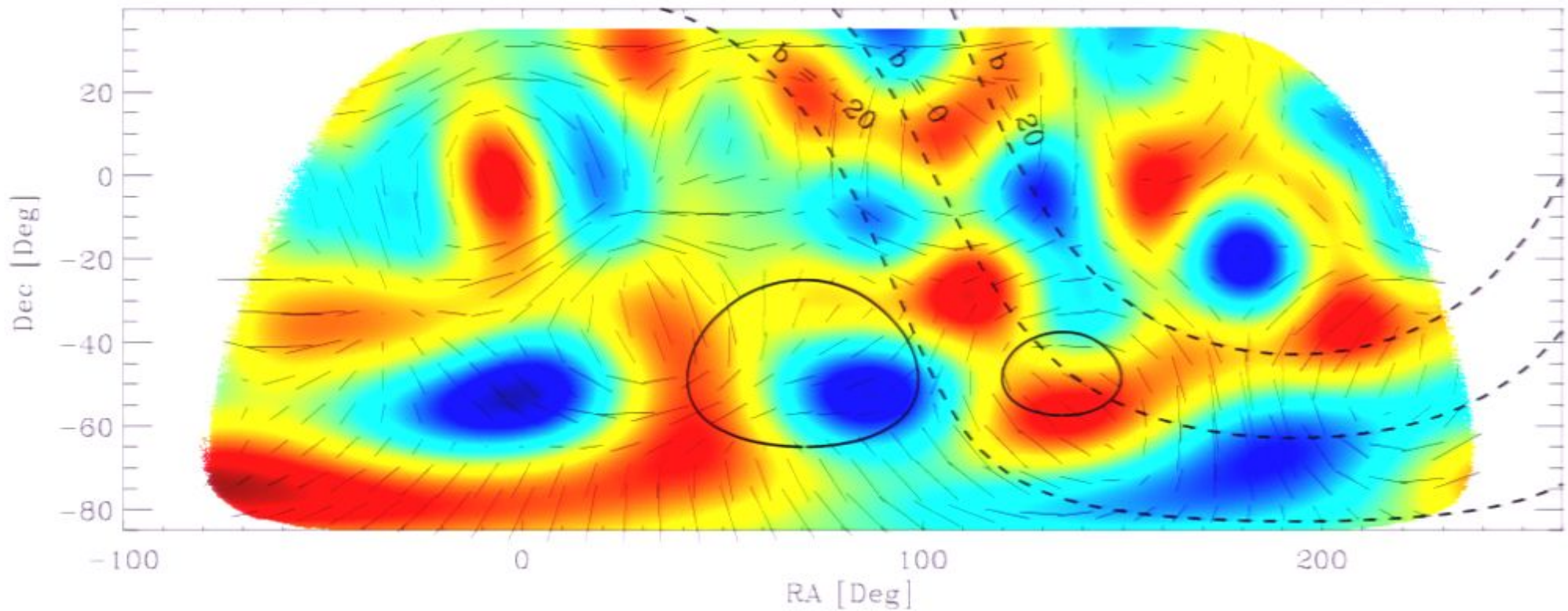


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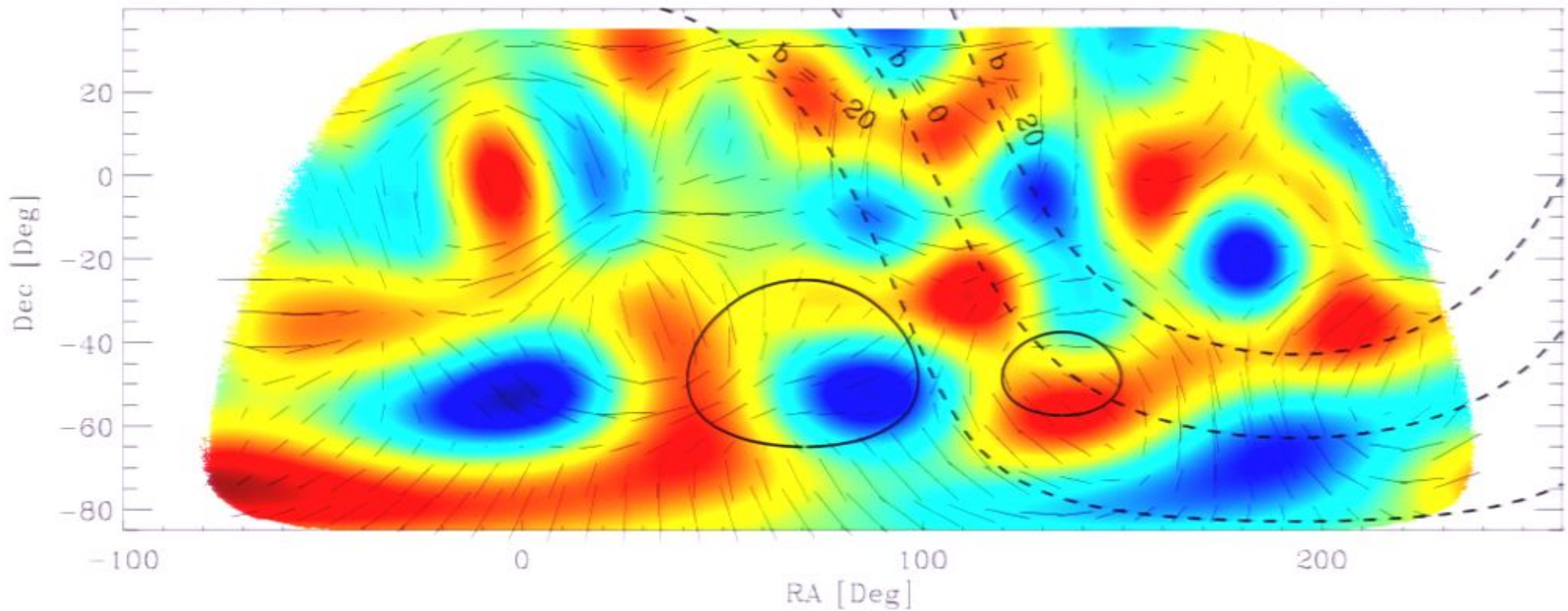


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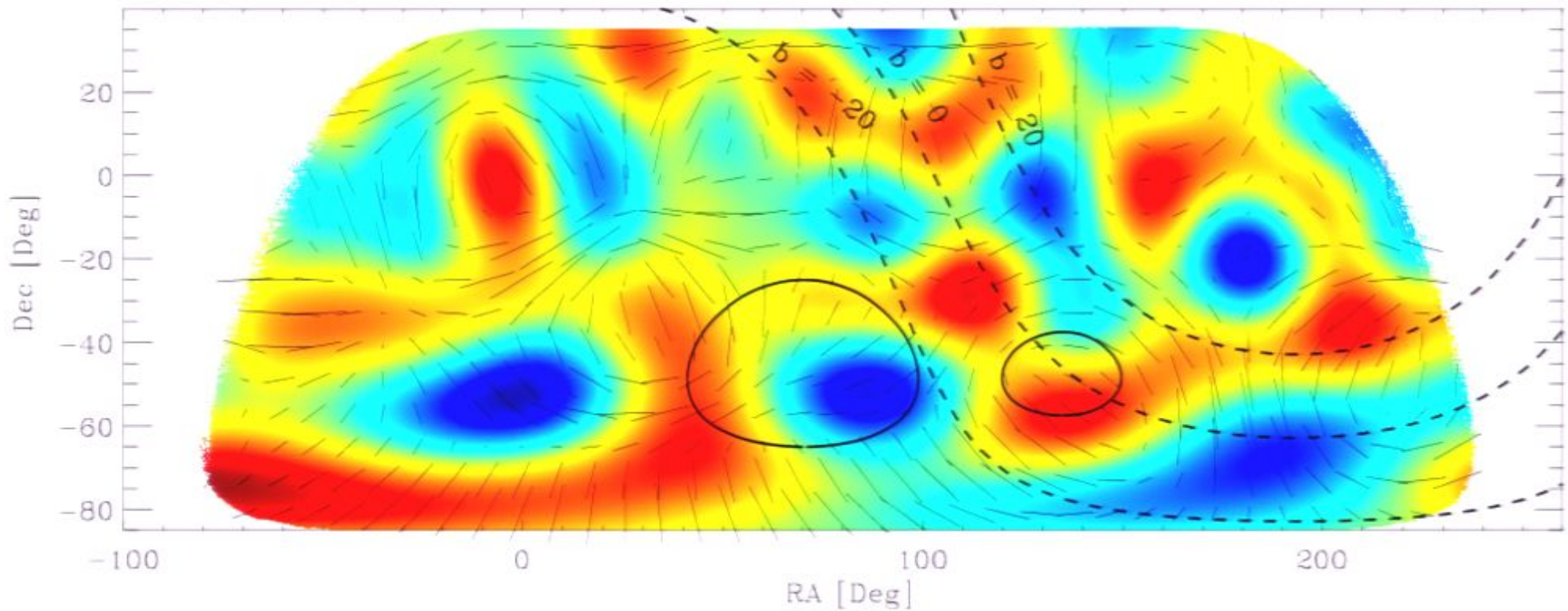


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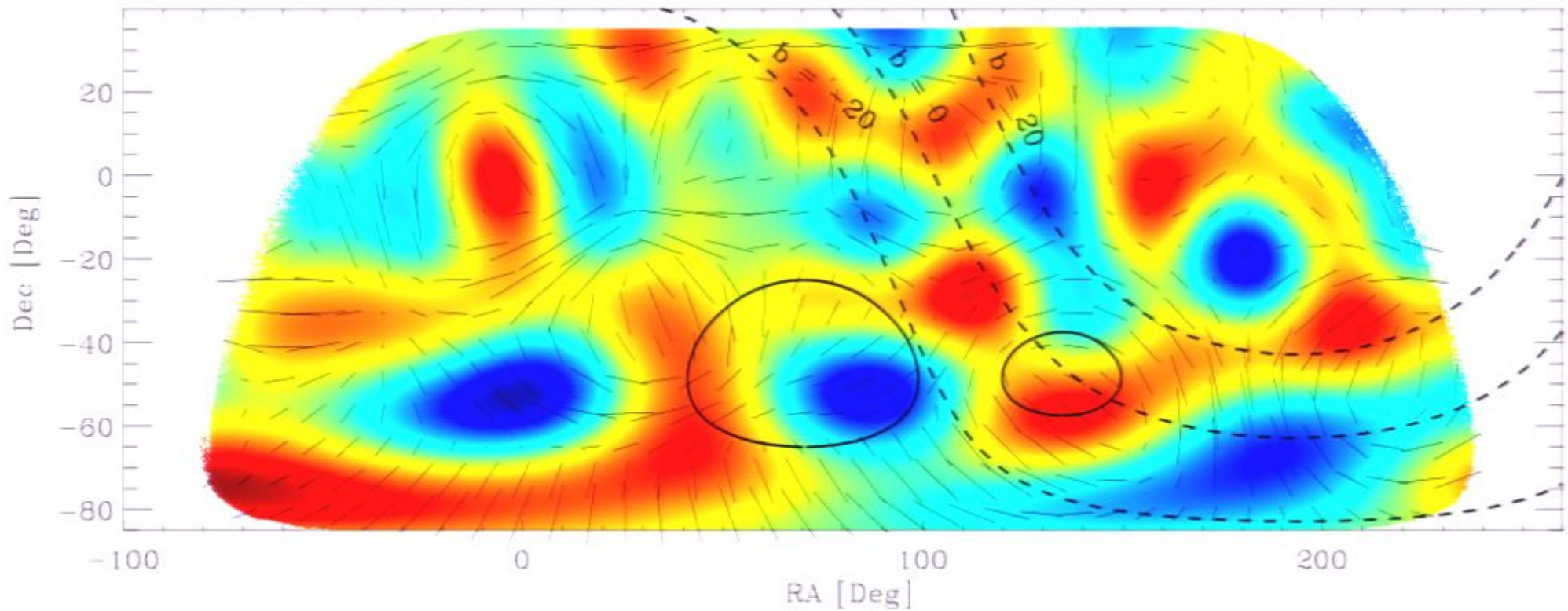


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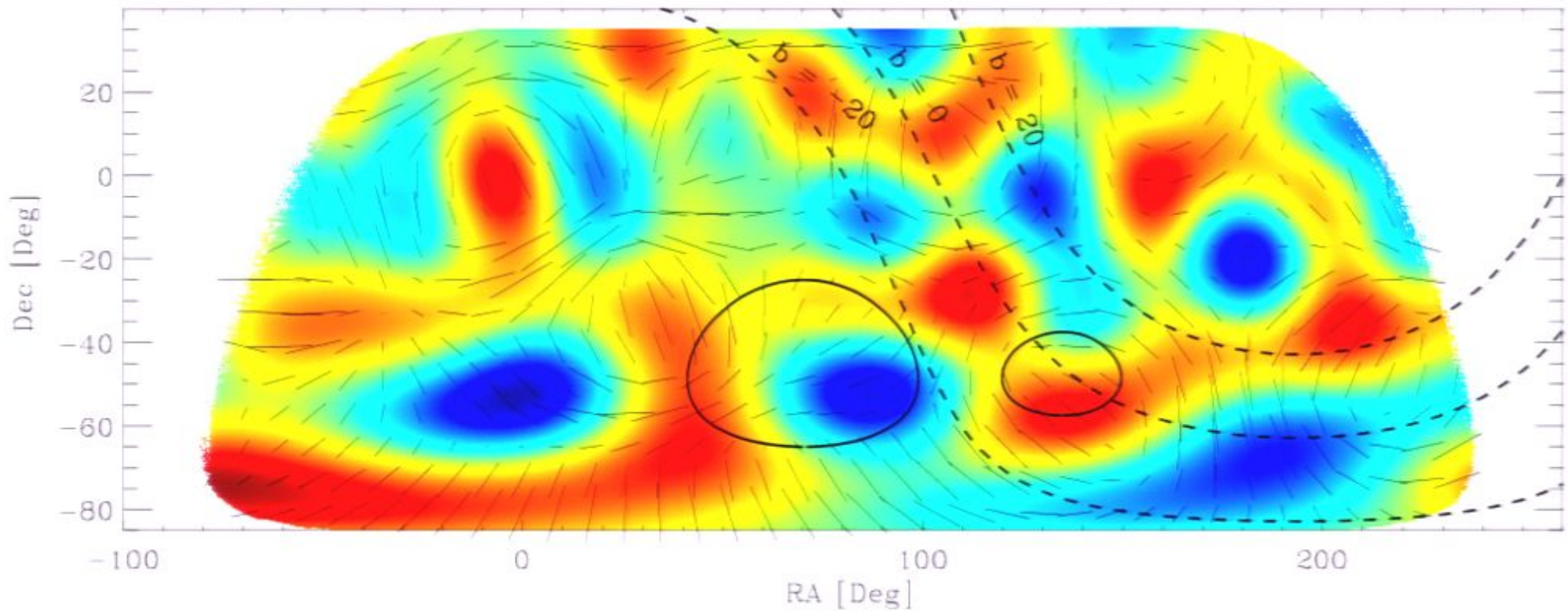


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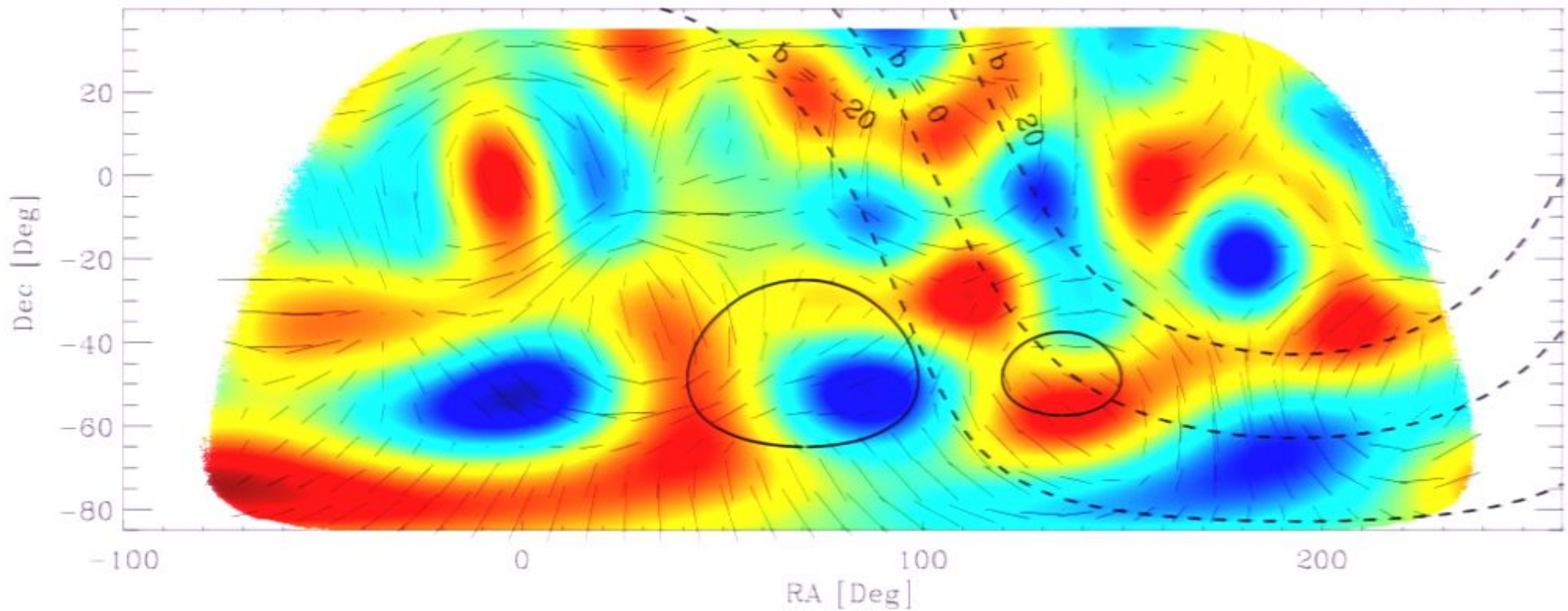


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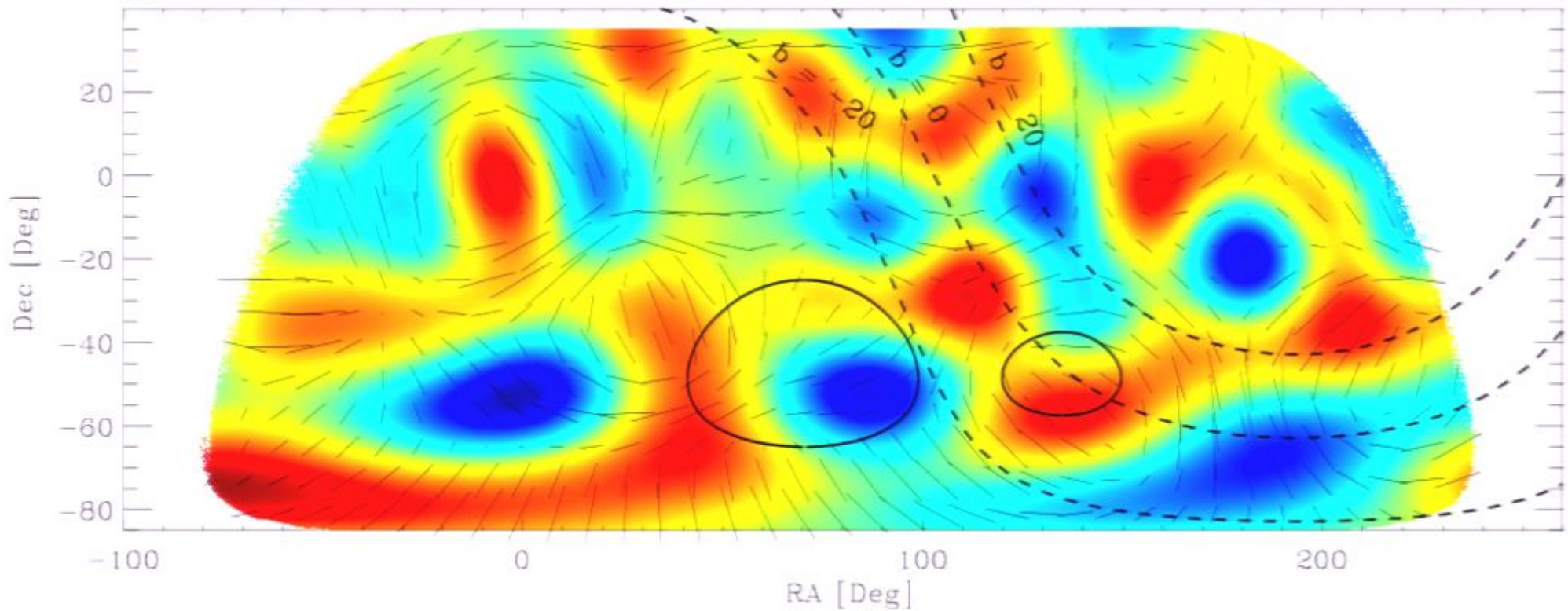


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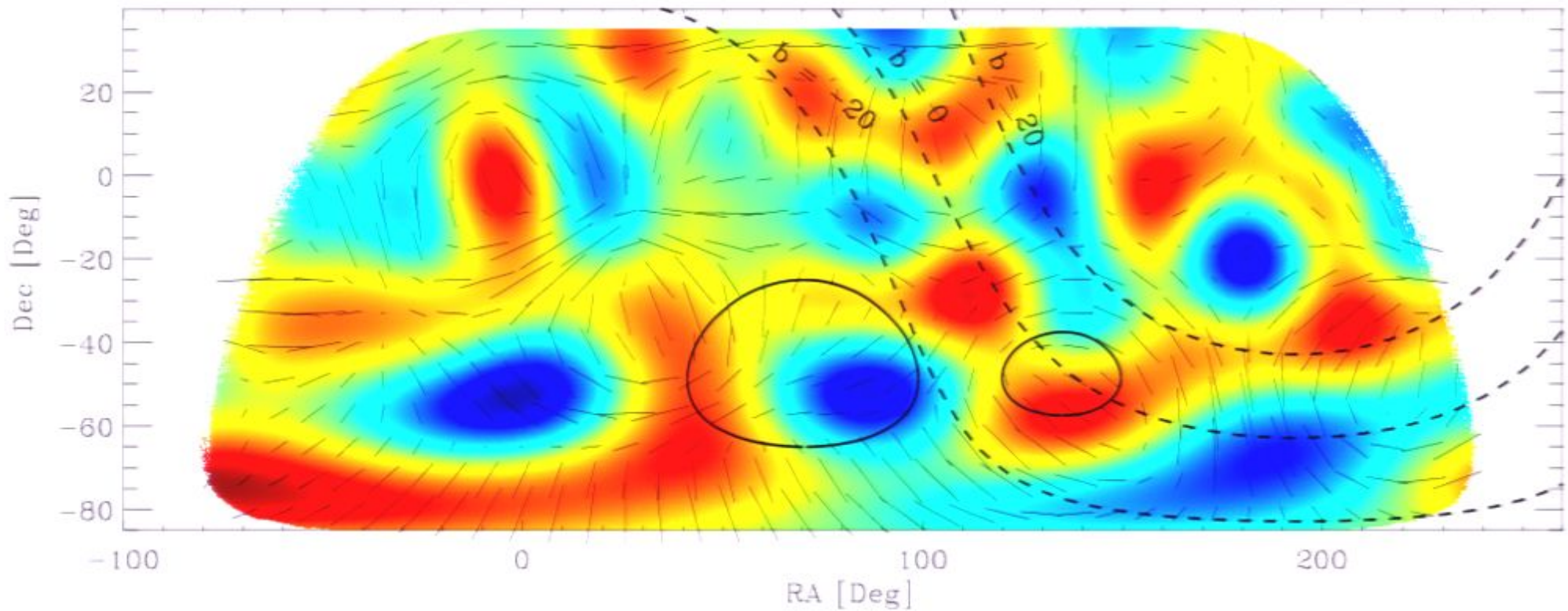


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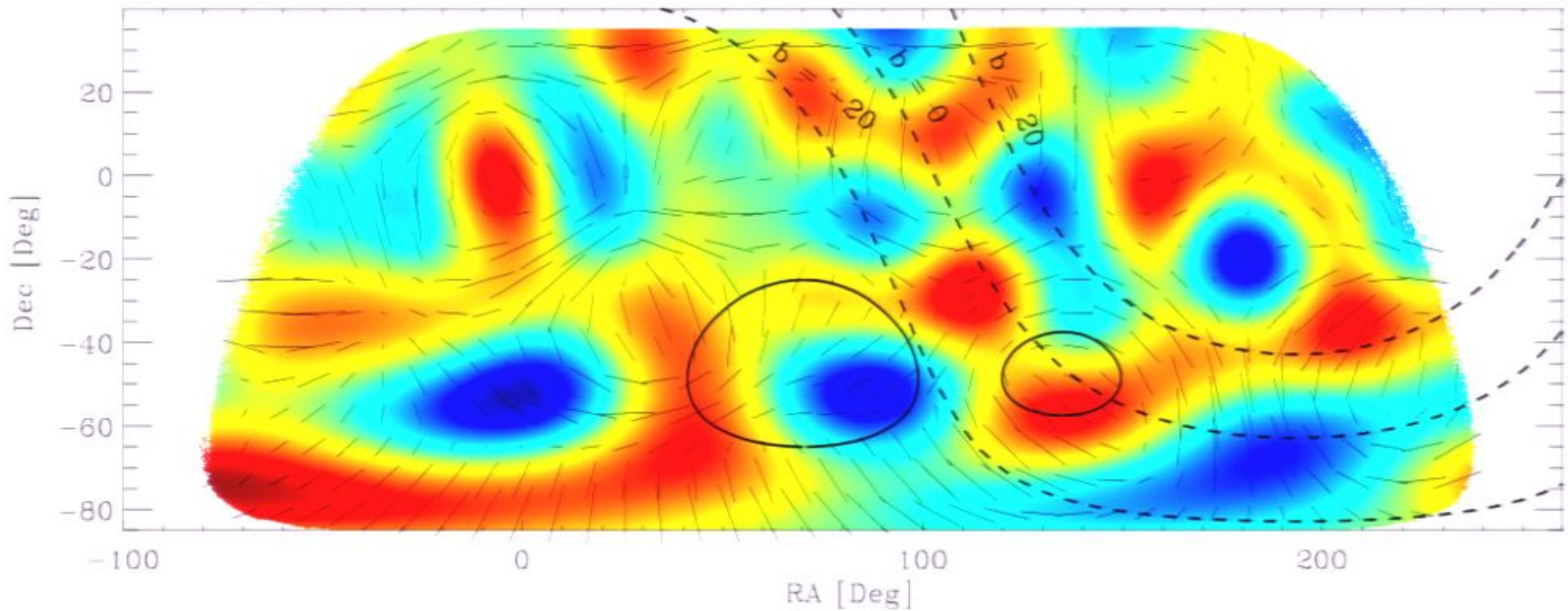


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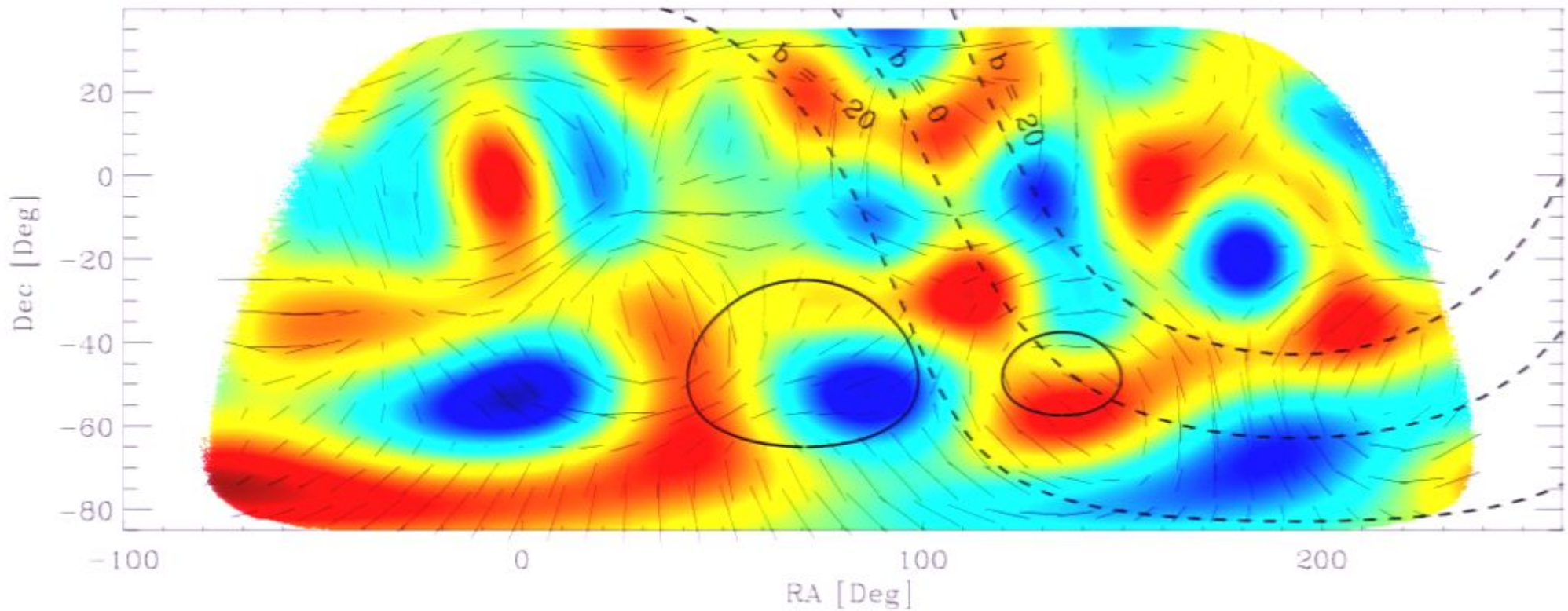


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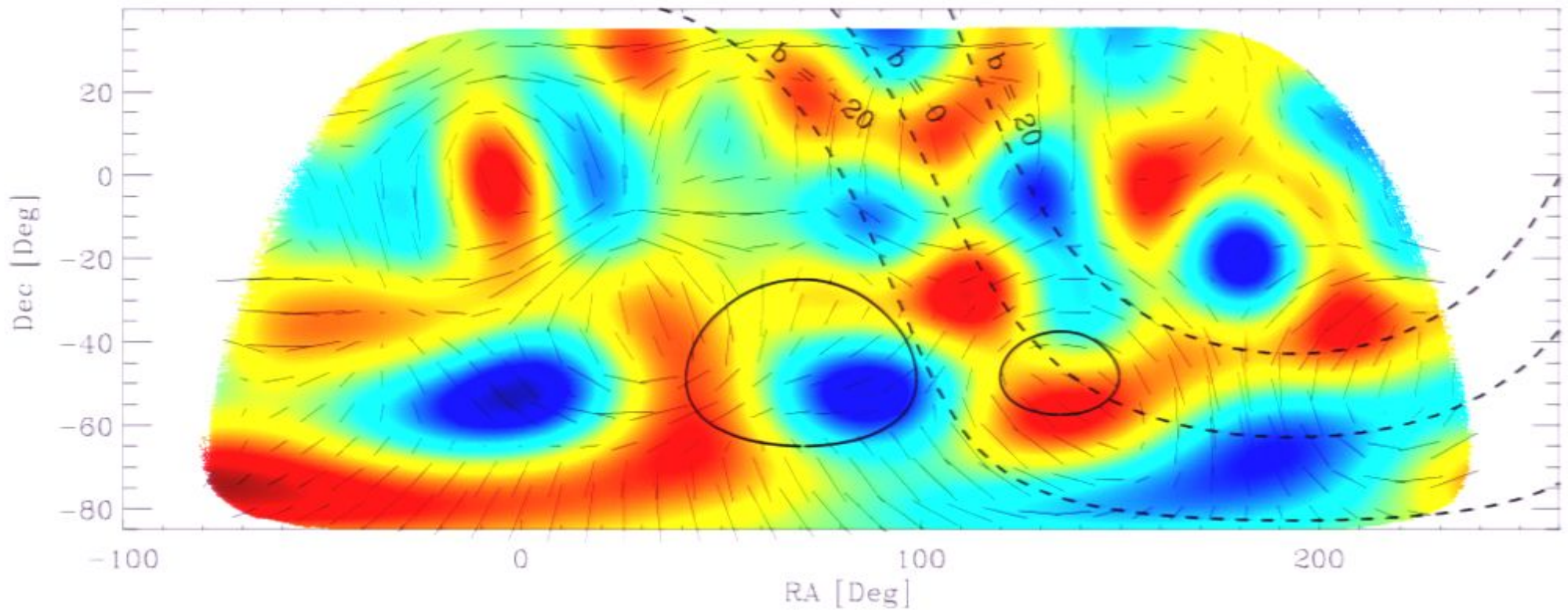


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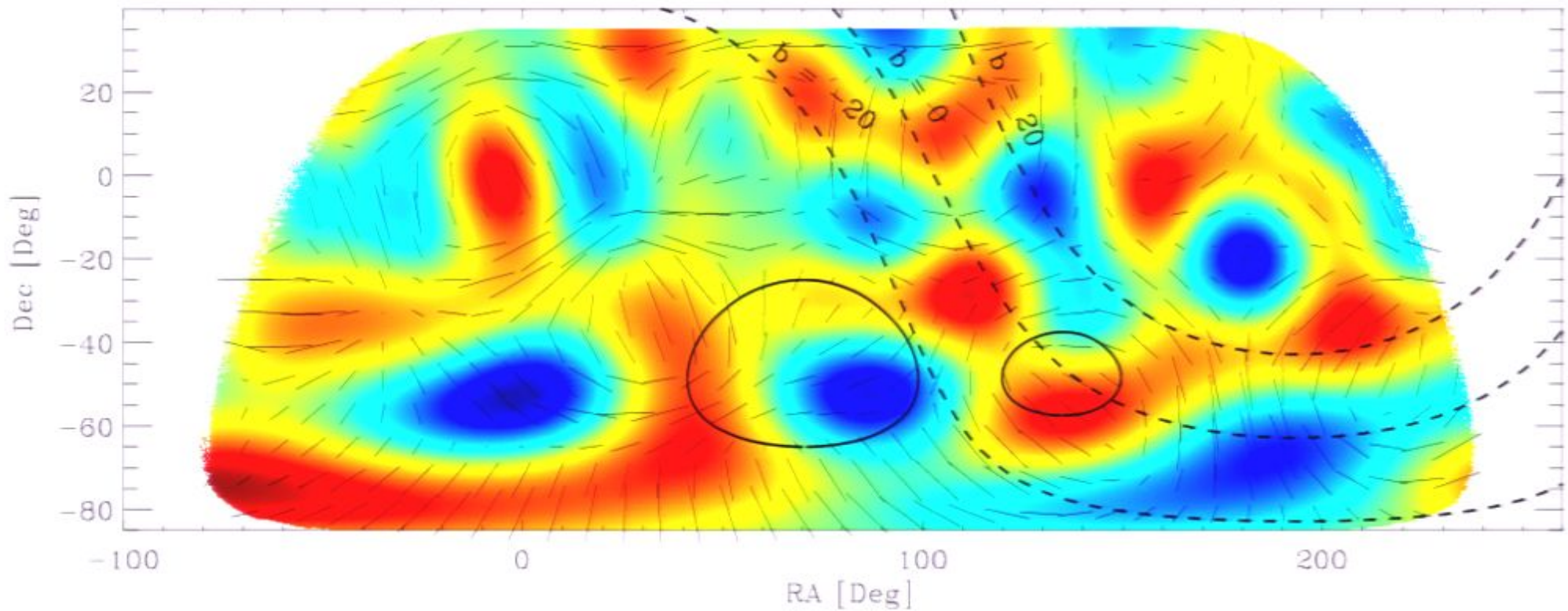


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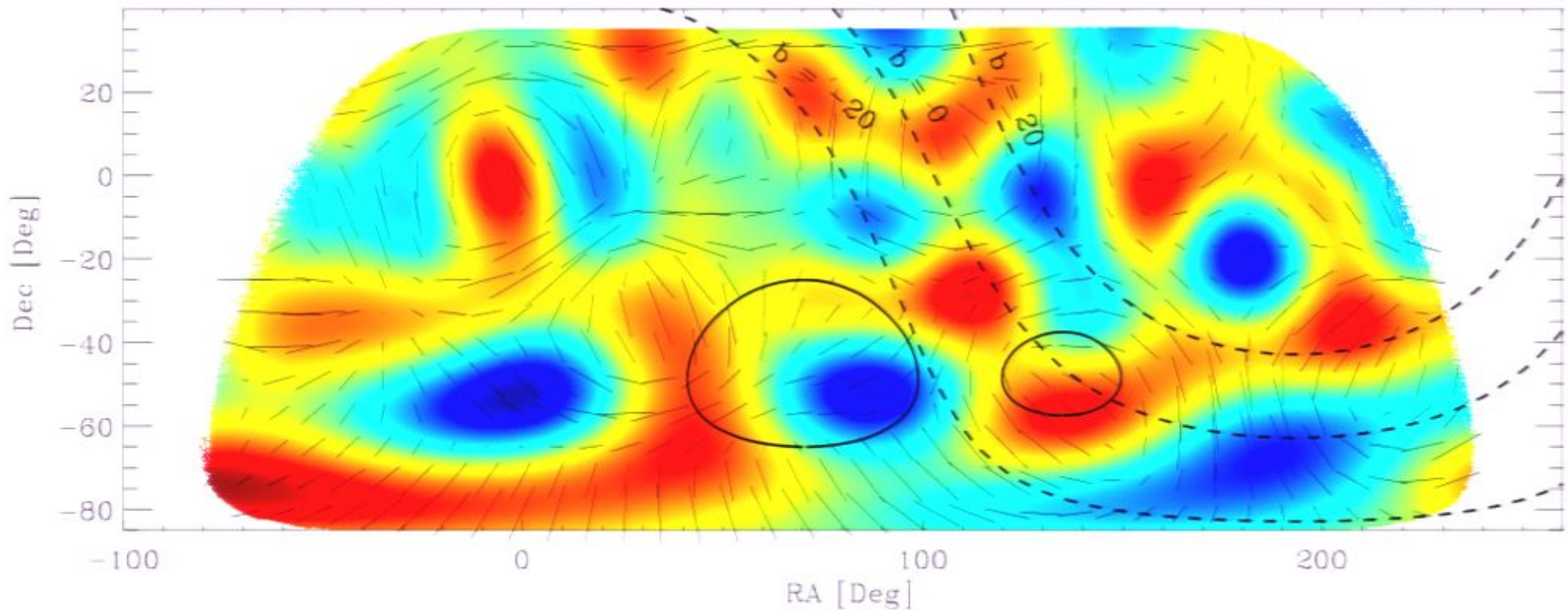


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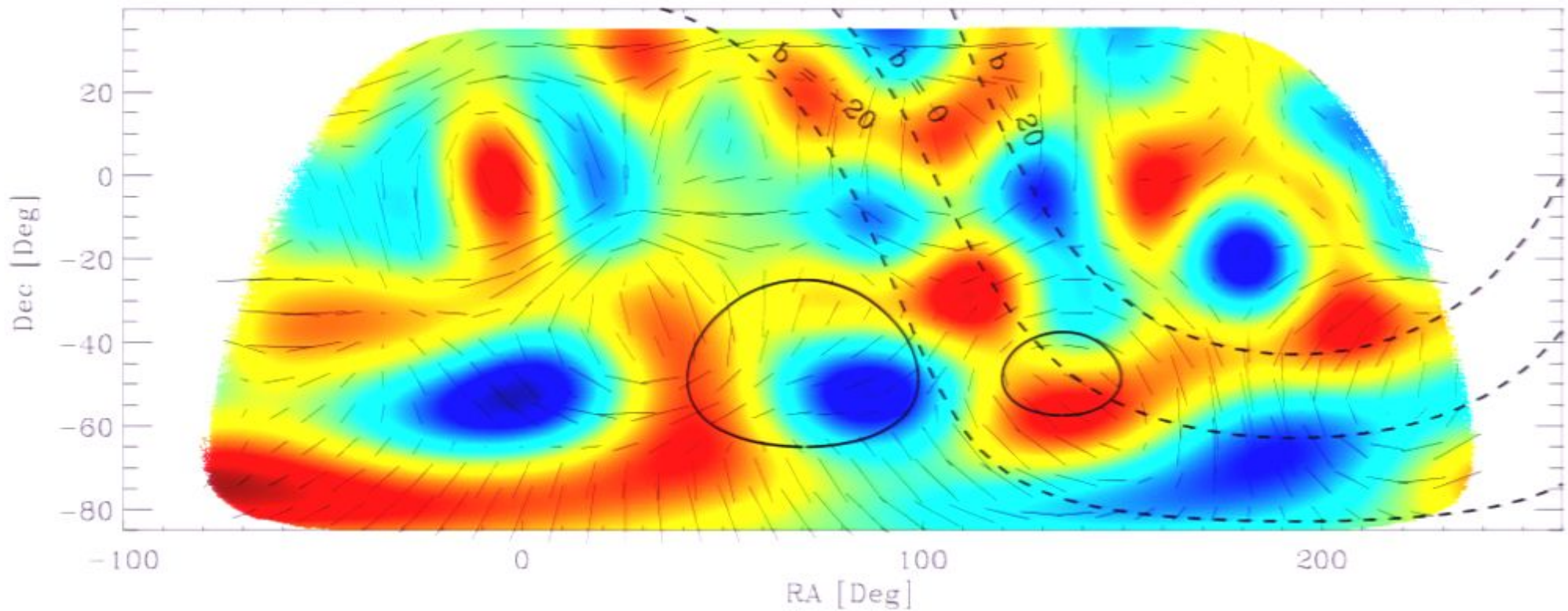


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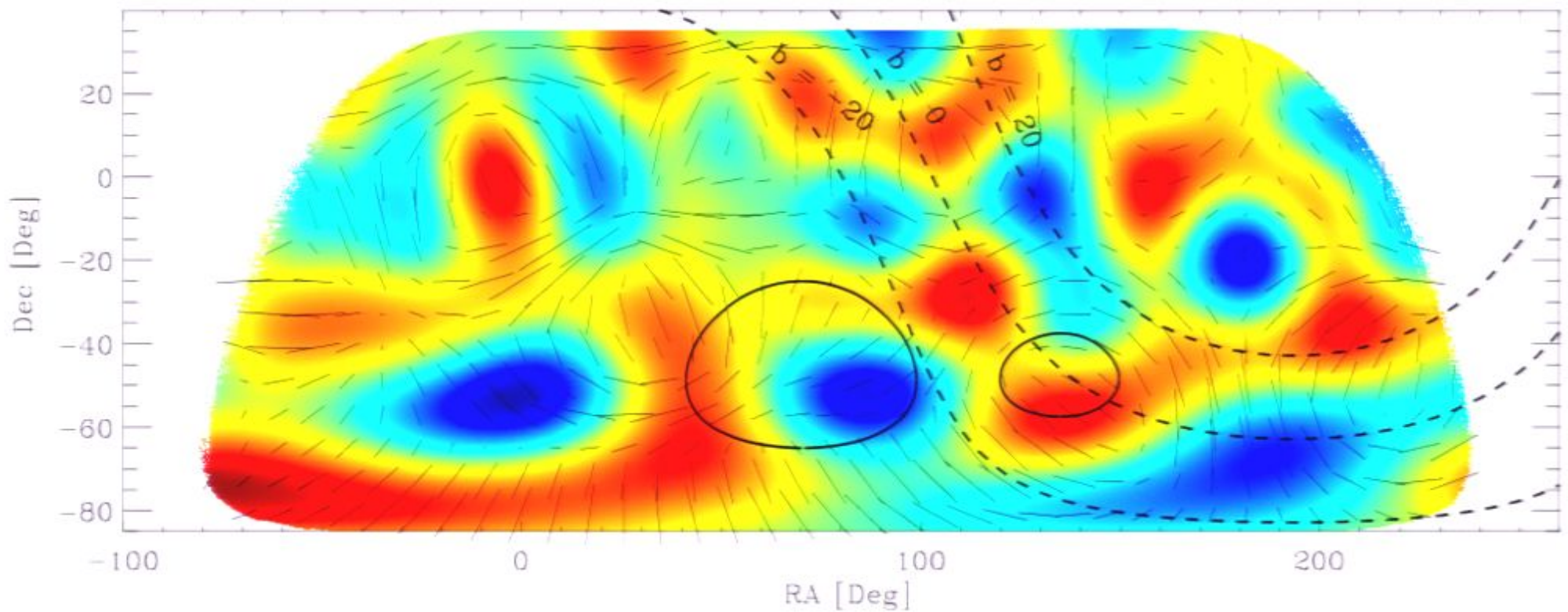


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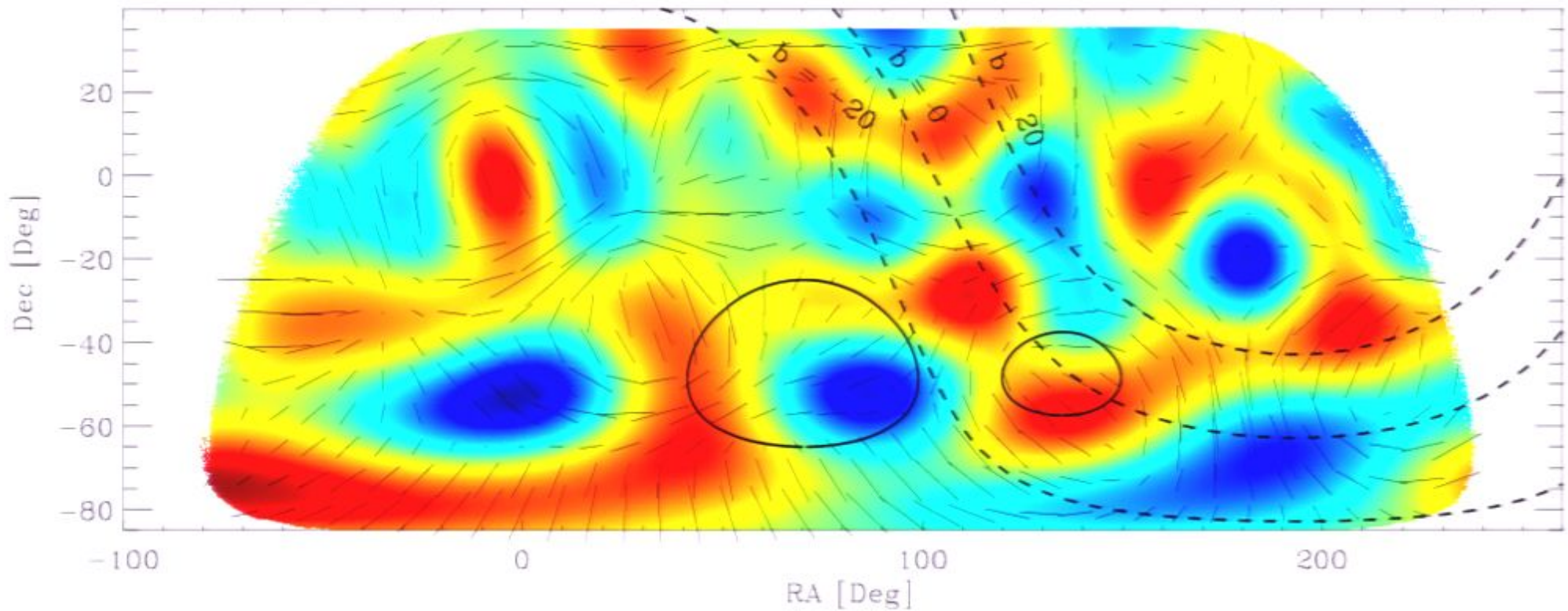


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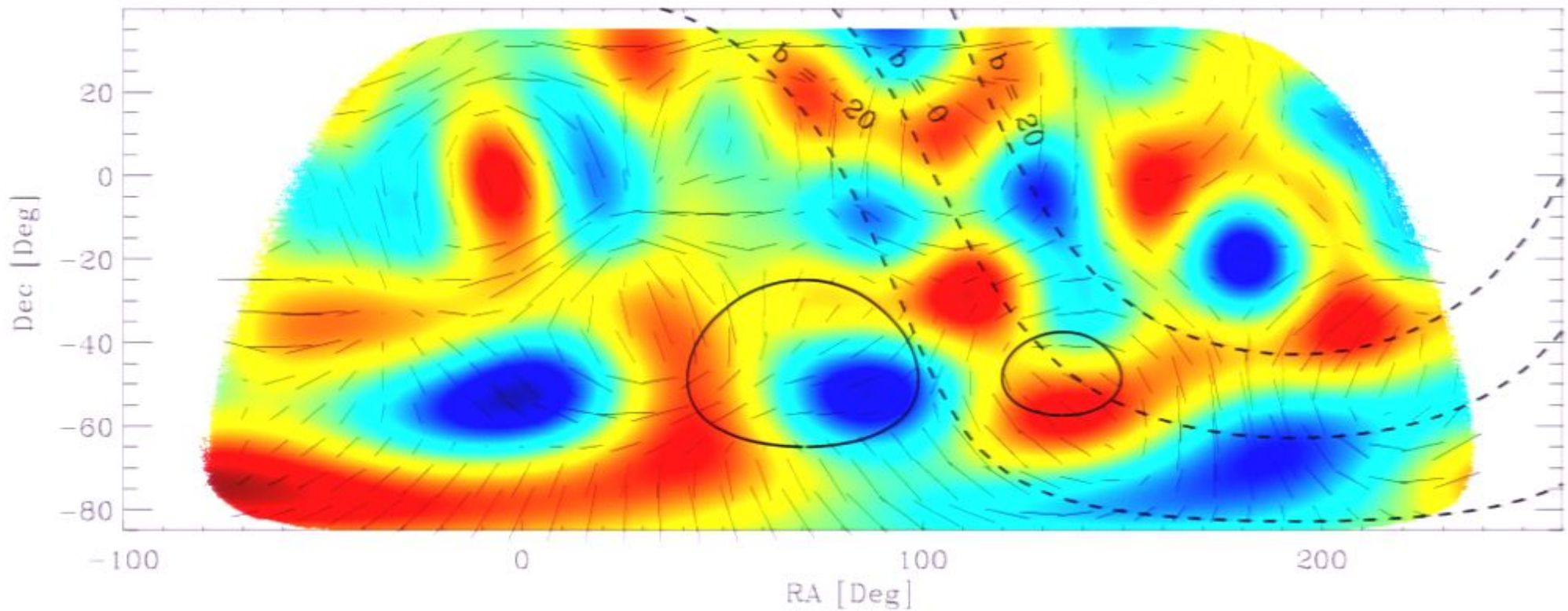


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Tensor



forecast
Planck2.5

100&143

Spider10d

95&150

$Q_p / (\mu K^2)$

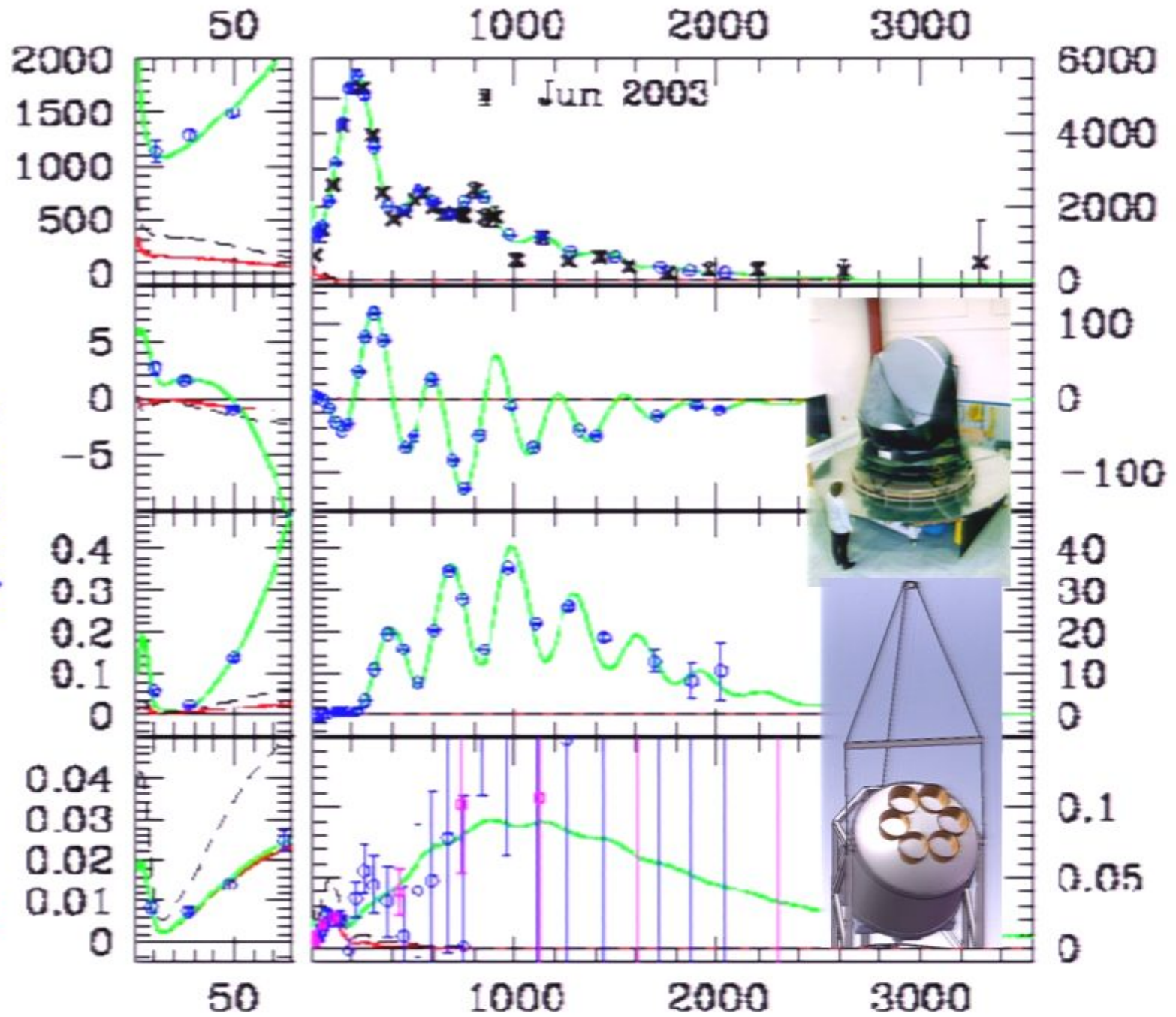
Synchrotron pol'n

Dust pol'n

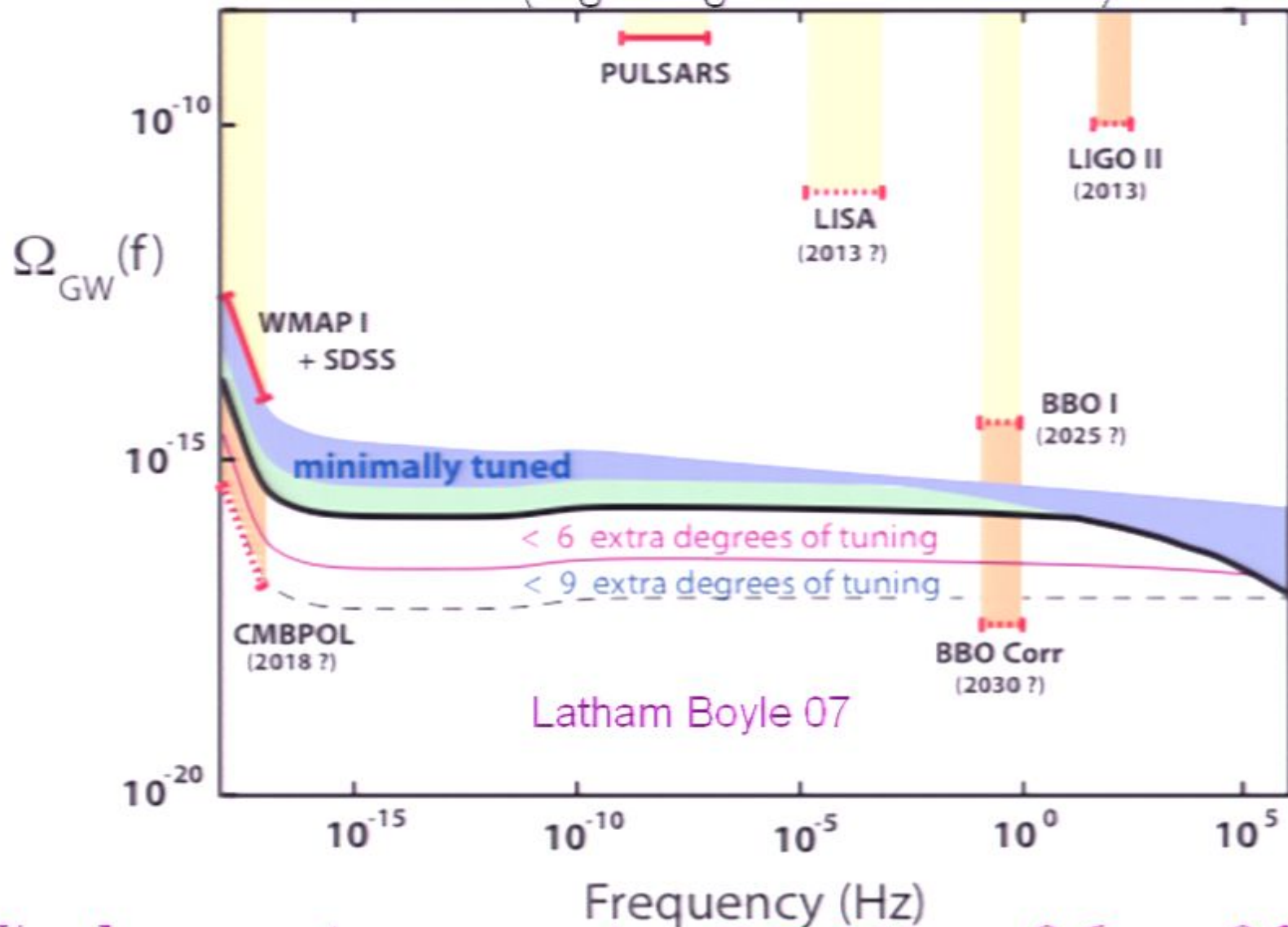
are higher in B

Foreground
template removals
from multi-
frequency data

is crucial



Very very difficult to get at with direct gravity wave detectors – even in our dreams (Big Bang Observer ~ 2030)



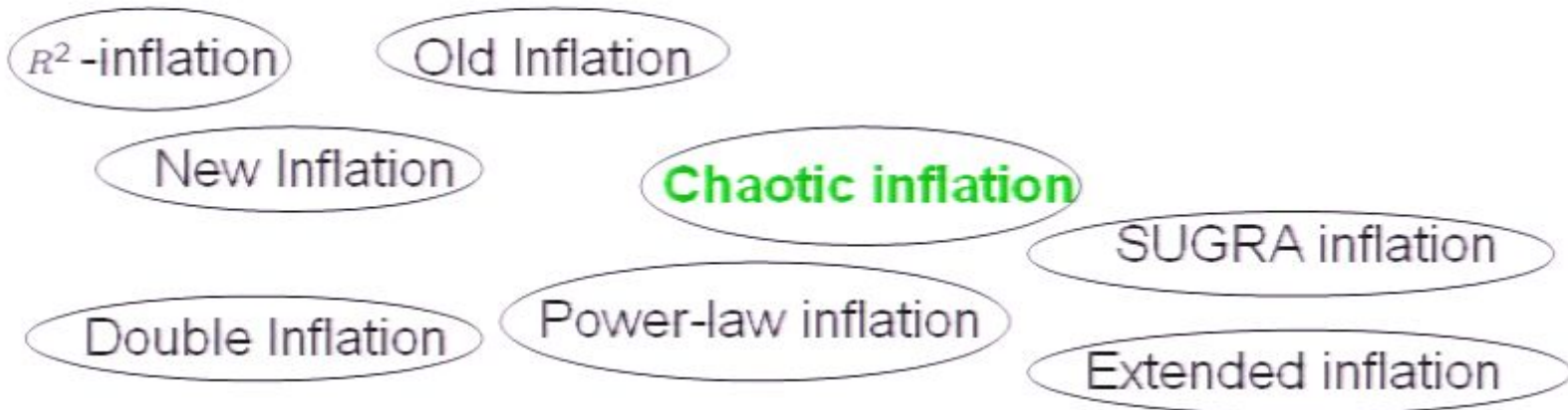
GW/scalar curvature: current from CMB+LSS: $r < 0.6$ or < 0.25 (.28) 95%;

good shot at **0.02** 95% CL with **BB polarization** (+- .02 PL2.5+Spider), **.01 target**

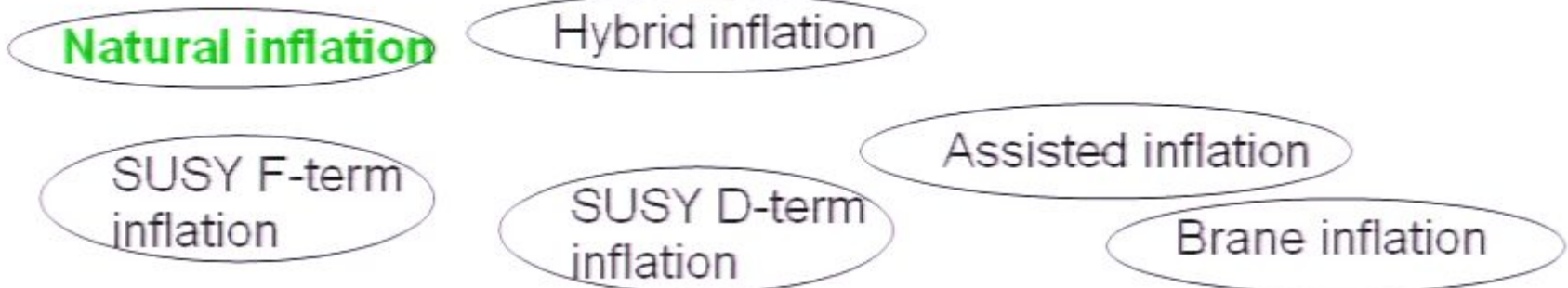
BUT foregrounds/systematics?? But r-spectrum. But low energy inflation

Inflation in the context of ever changing fundamental theory

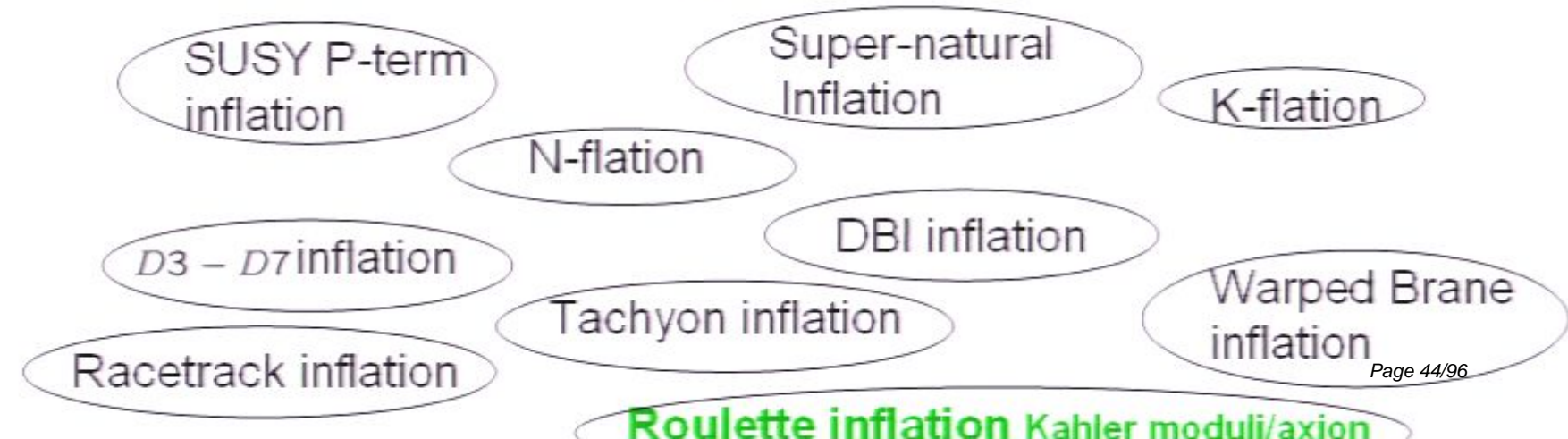
1980



1990



2000



Power law (chaotic) potentials

$$V/M_{\text{P}}^4 \sim \lambda \psi^{2\nu}, \quad \psi = \phi/M_{\text{P}} \quad 2^{-1/2}$$

$$\varepsilon = (\nu/\psi)^2, \quad \varepsilon = (\nu/2) / (\mathbf{N}_{\text{I}}(\mathbf{k}) + \nu/3),$$

$$\mathbf{n}_s - 1 = -(\nu + 1) / (\mathbf{N}_{\text{I}}(\mathbf{k}) - \nu/6),$$

$$\mathbf{n}_t = -\nu / (\mathbf{N}_{\text{I}}(\mathbf{k}) - \nu/6),$$

$$\nu=1, \mathbf{N}_{\text{I}} \sim 60, \quad r = 0.13, \quad \mathbf{n}_s = .967, \quad \mathbf{n}_t = -.017$$

$$\nu=2, \mathbf{N}_{\text{I}} \sim 60, \quad r = 0.26, \quad \mathbf{n}_s = .950, \quad \mathbf{n}_t = -.034$$

PNGB: $V/M_P^4 \sim \Lambda_{\text{red}}^4 \sin^2(\psi/f_{\text{red}}^{2^{-1/2}})$

ABFFO93

$$n_s \sim 1 - f_{\text{red}}^{-2},$$

$$\epsilon = (1 - n_s)/2 / (\exp[(1 - n_s) N_I(k)] (1 + (1 - n_s)/6) - 1),$$

exponentially suppressed; higher r if lower N_I & $1 - n_s$

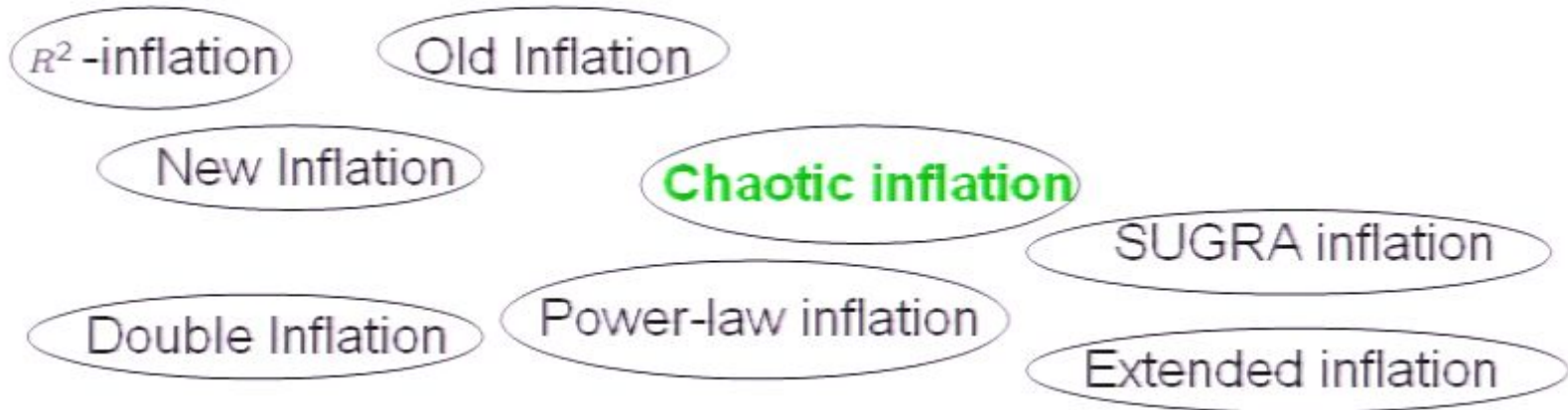
to match $n_s = .96$, $f_{\text{red}} \sim 5$, $r \sim 0.032$

to match $n_s = .97$, $f_{\text{red}} \sim 5.8$, $r \sim 0.048$

cf. $v=1$, $r = 0.13$, $n_s = .967$, $n_t = -.017$

Inflation in the context of ever changing fundamental theory

1980



1990



$$\mathbf{n}_t = -v / (\mathbf{N}_I(\mathbf{k}) - v/6),$$

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ABFFO93

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to match $n_s = .96$, $f_{\text{red}} \sim 5$, $r \sim 0.032$

to match $n_s = .97$, $f_{\text{red}} \sim 5.8$, $r \sim 0.048$

cf. $v=1$, $r = 0.13$, $n_s = .967$, $n_t = -.017$

Moduli/brane distance limitation in stringy inflation. Normalized canonical inflaton

$\Delta\psi < 1$ over $\Delta N \sim 50$, e.g. $2/n_{\text{brane}}^{1/2}$ BM06

$\epsilon = (d\psi / d \ln a)^2$ so $r = 16\epsilon < .007$, $\ll ?$

roulette inflation examples $r \sim 10^{-10}$ & $\Delta\psi < .002$

possible way out with many fields assisting: N-flation

$n_s = .97$, $f_{\text{red}} \sim 5.8$, $r \sim 0.048$, $\Delta\psi \sim 13$

cf. $v=1$, $r = 0.13$, $n_s = .967$, $\Delta\psi \sim 10$

energy scale of inflation & r

$$V/M_{\text{P}}^4 \sim P_s r (1-\epsilon/3)^{3/2}$$

$$V \sim (10^{16} \text{ GeV})^4 r/0.1 (1-\epsilon/3)$$

roulette inflation examples $V \sim (\text{few} \times 10^{13} \text{ GeV})^4$

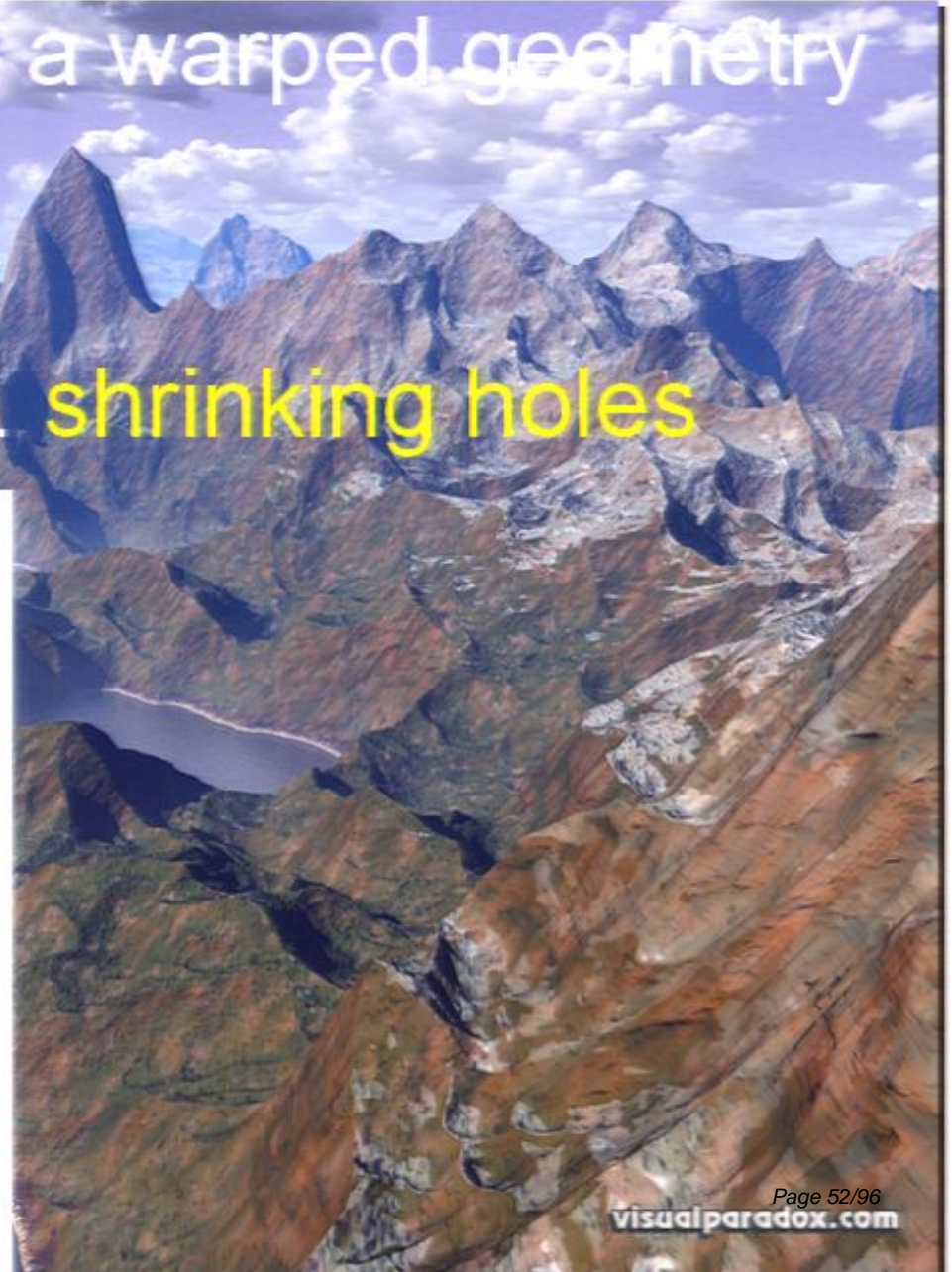
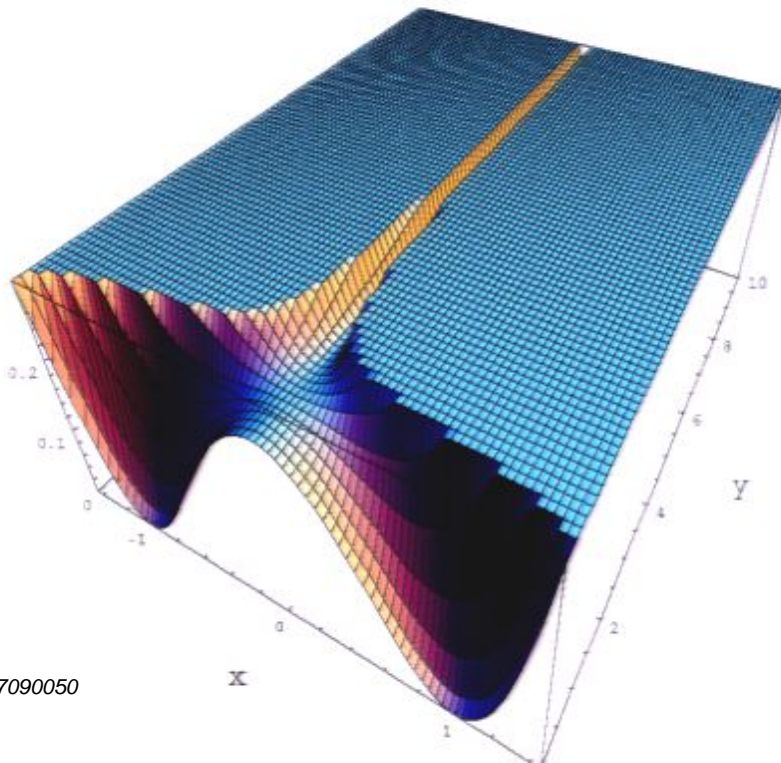
$$H/M_{\text{P}} \sim 10^{-5} (r/.1)^{1/2}$$

inflation energy scale cf. the gravitino mass (Kallosh & Linde 07) if a KKL_T/large V_{CY} -like generation mechanism

$$10^{13} \text{ GeV} (r/.01)^{1/2} \sim H < m_{3/2} \text{ cf. } \sim \text{Tev}$$

String Theory Landscape & Inflation++ Phenomenology for CMB+LSS

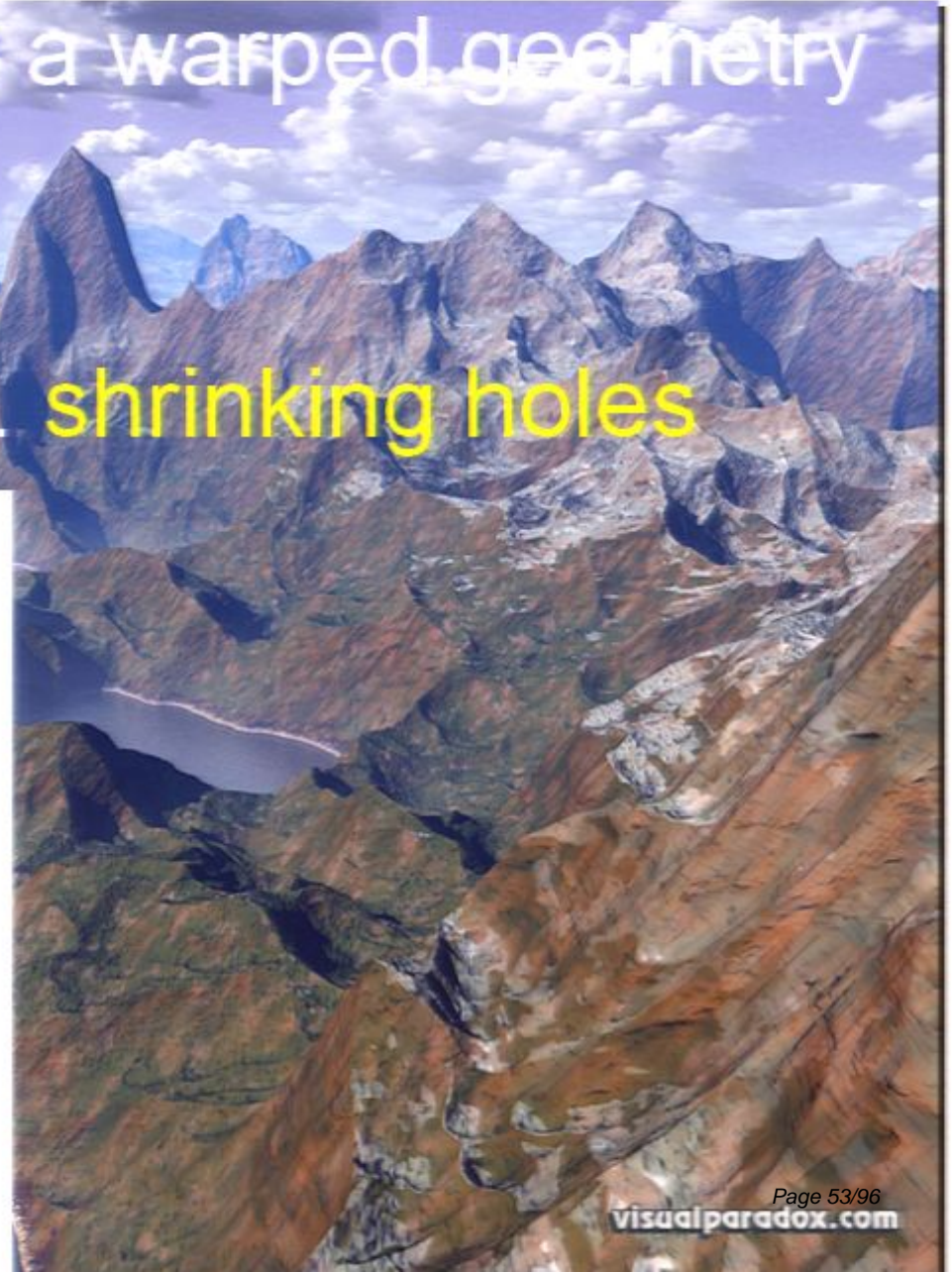
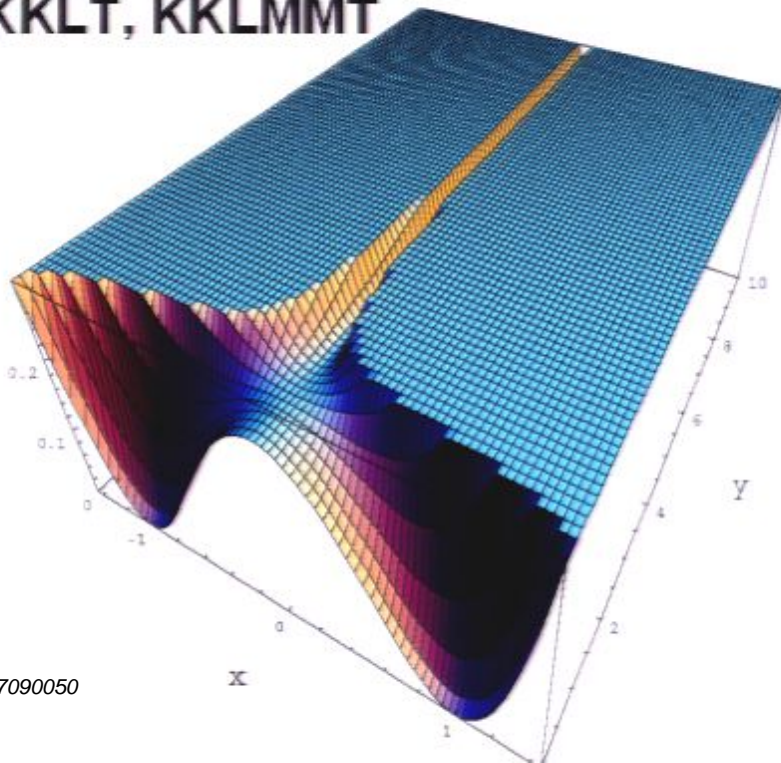
- D3/anti-D3 branes in a warped geometry
- D3/D7 branes
- axion/moduli fields ... **shrinking holes**



String Theory Landscape & Inflation++ Phenomenology for CMB+LSS

- D3/anti-D3 branes in a warped geometry
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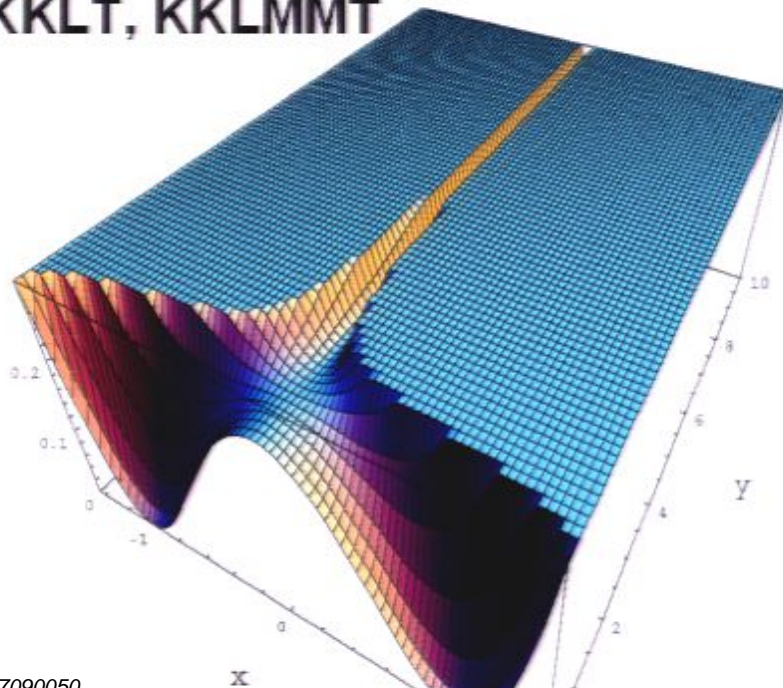
KKLT, KKLMNT



String Theory Landscape & Inflation++ Phenomenology for CMB+LSS

- D3/anti-D3 branes in a warped geometry
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KKLT, KKLMNT

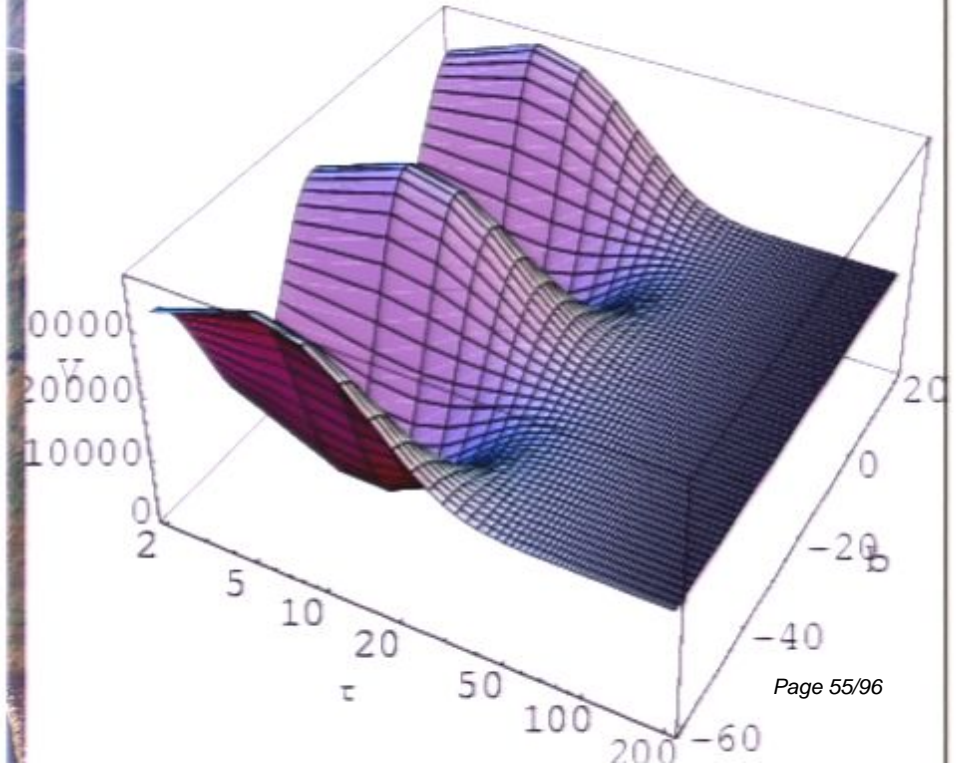
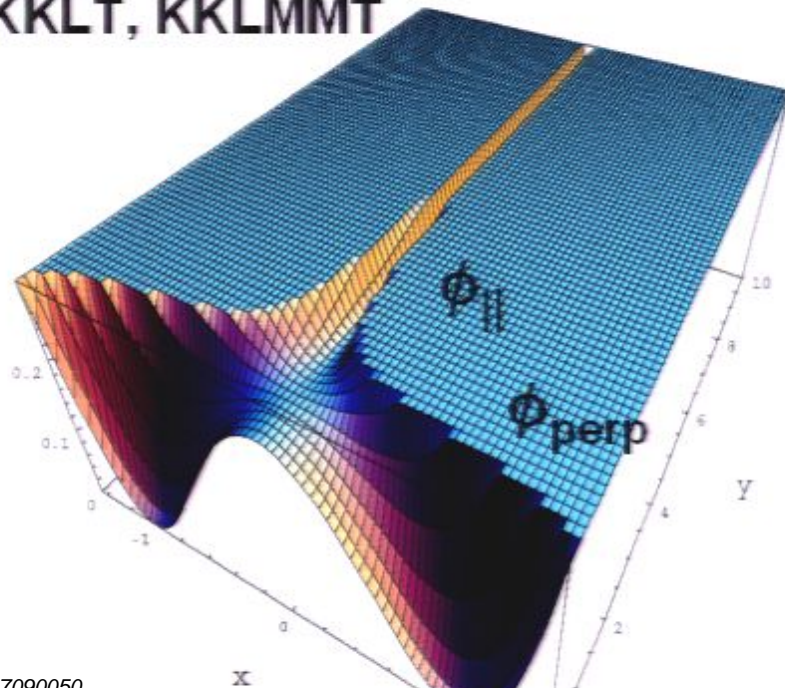


Hybrid D3/D7 Potential

String Theory Landscape & Inflation++ Phenomenology for CMB+LSS

- D3/anti-D3 branes in a warped geometry
- D3/D7 branes
- axion/moduli fields ... **shrinking holes**

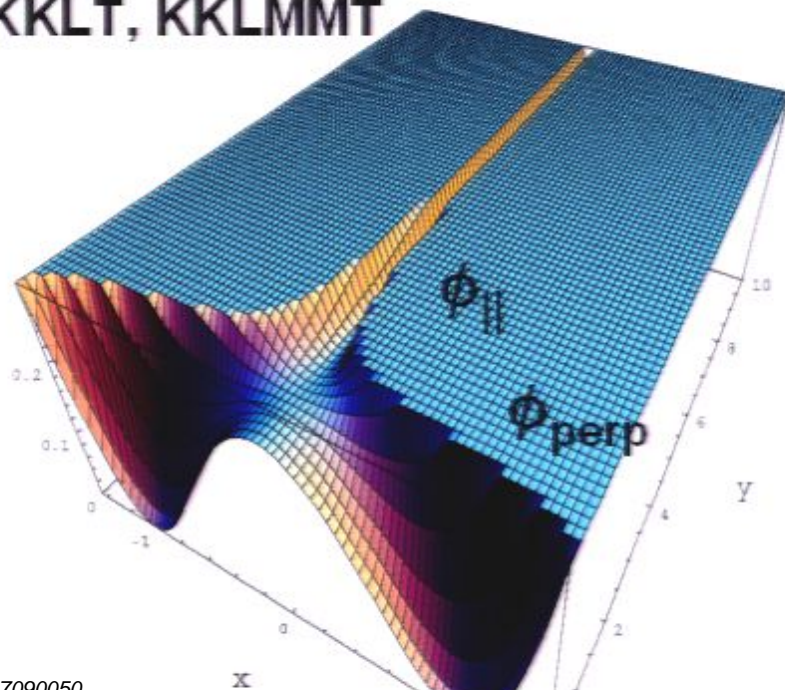
KKLT, KKLMNT



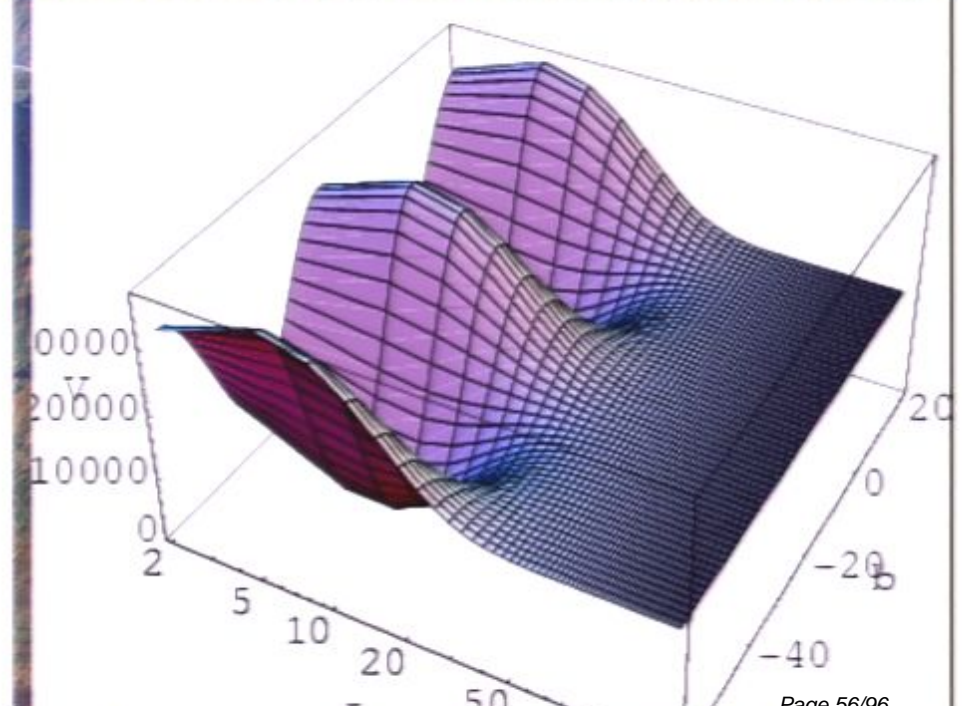
String Theory Landscape & Inflation++ Phenomenology for CMB+LSS

- D3/anti-D3 branes in a warped geometry
- D3/D7 branes
- axion/moduli fields ... **shrinking holes**

KKLT, KKLMNT



Hybrid D3/D7 Potential

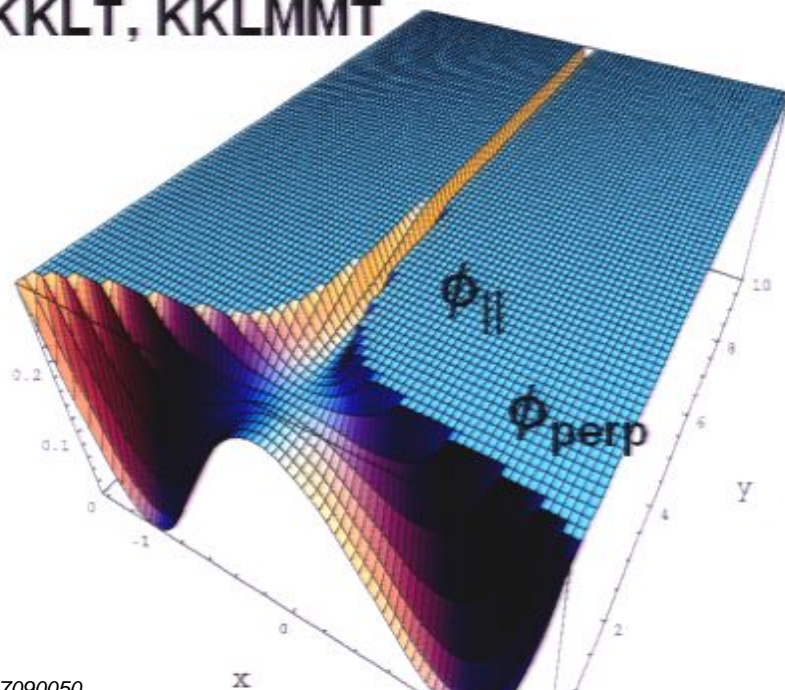


large volume 6D ect Calabi Yau

String Theory Landscape & Inflation++ Phenomenology for CMB+LSS

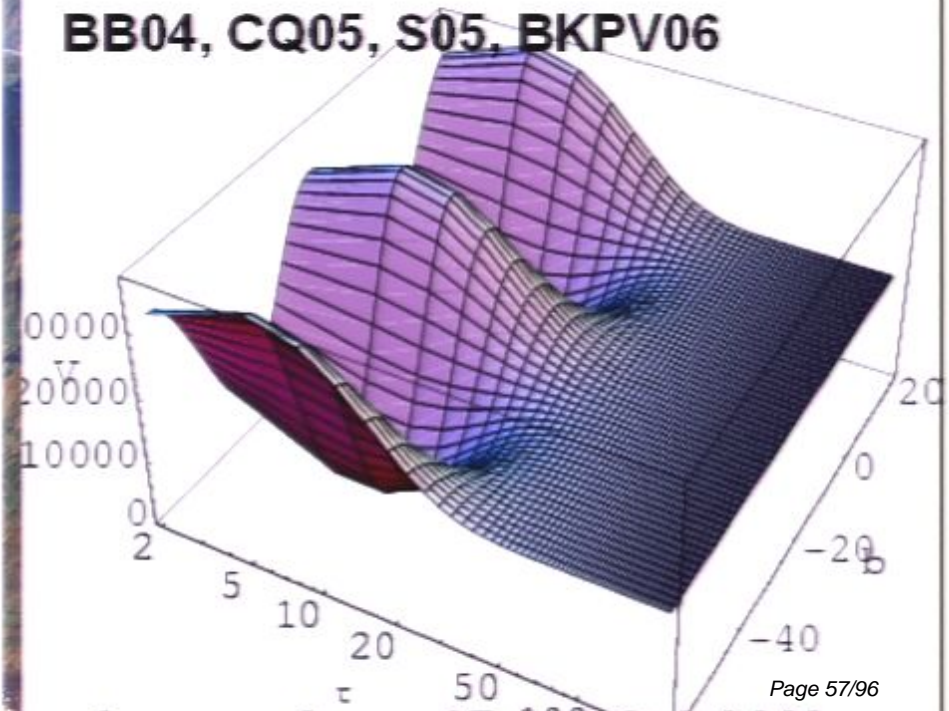
- D3/anti-D3 branes in a warped geometry
- D3/D7 branes
- axion/moduli fields ... **shrinking holes**

KKLT, KKLMMT



Hybrid D3/D7 Potential

BB04, CQ05, S05, BKPV06



large volume 6D ect Calabi Yau

Constraining Inflaton Acceleration Trajectories

Bond, Contaldi, Kofman & Vaudrevange 07

“path integral” over probability landscape of theory and data, with mode-function expansions of the paths truncated by an imposed smoothness (Chebyshev-filter) criterion **[data cannot constrain high $\ln k$ frequencies]**

$$P(\text{trajectory}|\text{data}, \text{th}) \sim P(\ln H_{p,\epsilon_k}|\text{data}, \text{th})$$

$$\sim P(\text{data}|\ln H_{p,\epsilon_k}) P(\ln H_{p,\epsilon_k}|\text{th}) \quad / \quad P(\text{data}|\text{th})$$

Likelihood

theory prior

/ evidence

Data:

Theory prior

CMBall

uniform in $\ln H_{p,\epsilon_k}$

(WMAP3,B03,CBI, ACBAR,

(equal a-prior probability hypothesis)

DASI,VSA,MAXIMA)

Nodal points cf. Chebyshev coefficients
(linear combinations)

+

LSS (2dF, SDSS, σ_8 [lens])

uniform in / log in / monotonic in ϵ_k

The theory prior matters a lot for current data. Not quite as much for a Bpol future.

We have tried many theory priors

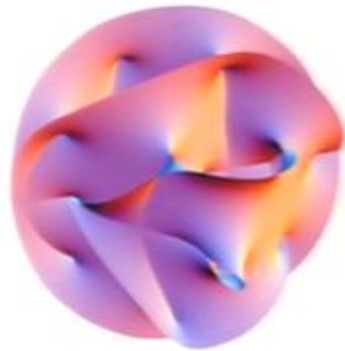
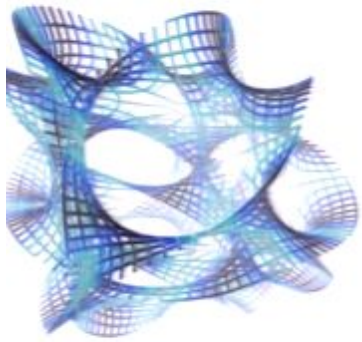
Old view: Theory prior = delta function of THE correct one and only theory

New view: Theory prior = probability distribution on an energy landscape whose features are at best only glimpsed, huge number of potential minima, inflation the late stage flow in the low energy structure toward these minima. Critical role of collective geometrical coordinates (moduli fields) and of brane and antibrane “moduli” (D3,D7).

Roulette Inflation: Ensemble of Kahler Moduli/Axion Inflations Bond, Kofman, Prokushkin & Vaudrevange 06

A Theory prior in a class of inflation theories that seem to work

Low energy landscape dominated by the last few (complex) moduli fields $T_1 T_2 T_3 \dots$
 $U_1 U_2 U_3 \dots$ associated with the settling down of the compactification of extra dims



CY are compact Ricci-flat Kahler mfd

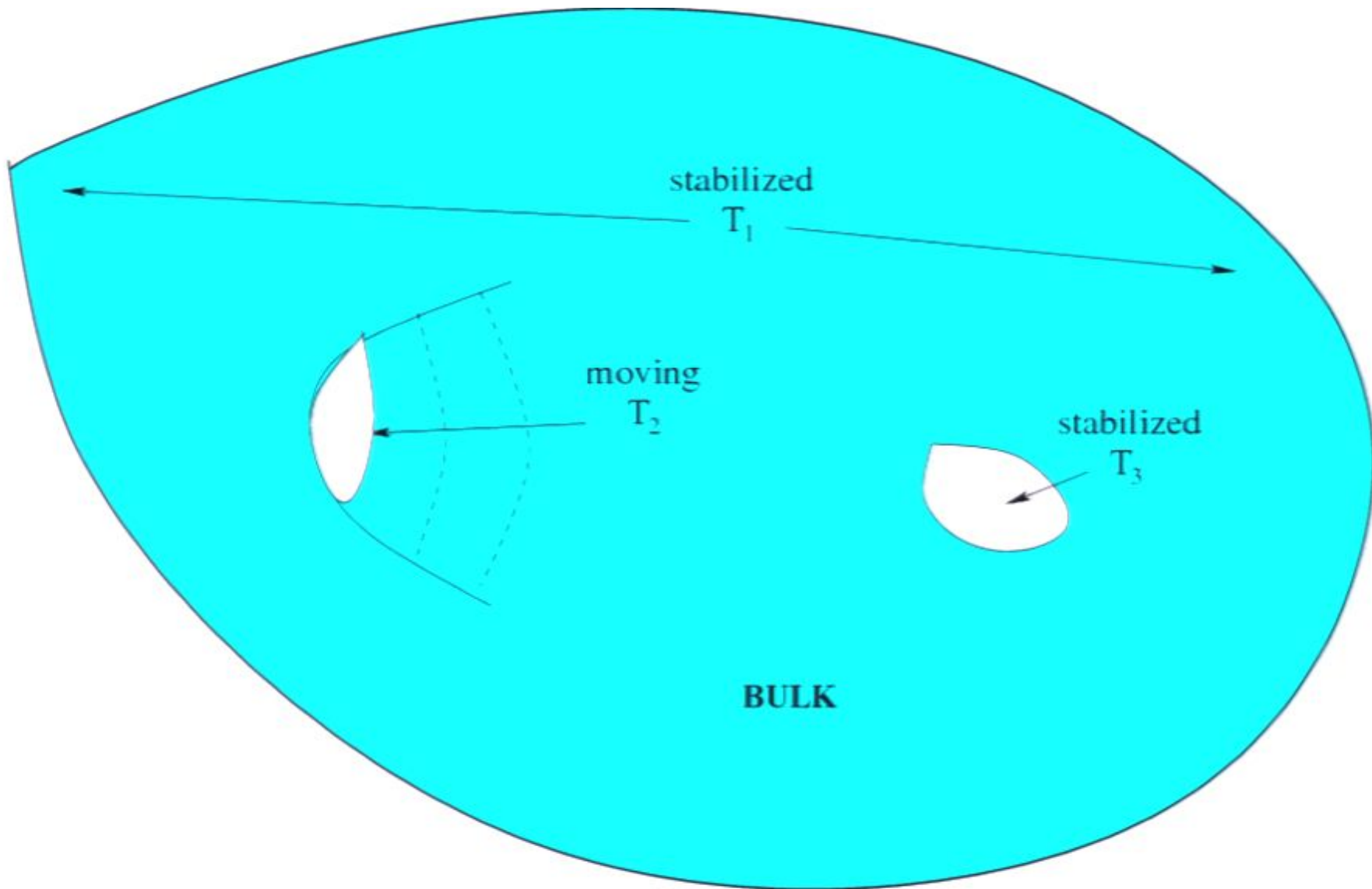
Kahler are Complex mfd with a hermitian metric & 2-form associated with the metric is closed (2nd derivative of a Kahler potential)

(complex) Kahler modulus associated with a 4-cycle volume in 6 dimensional Calabi Yau compactifications in Type IIB string theory. Real & imaginary parts are both important.

Builds on the influential KKLT, KKLMNT moduli-stabilization ideas for stringy inflation and the focus on 4-cycle Kahler moduli in large volume limit of IIB flux compactifications. Balasubramanian, Berglund 2004, + Conlon, Quevedo 2005, + Suruliz 2005 As

motivated as any stringy inflation model. Many possibilities:

Theory prior ~ **probability of trajectories given potential parameters of the collective coordinates X** probability of the potential parameters X **probability of initial conditions**



Stabilization from 3rd ... n^{th} field $T_3 \dots T_n$
 \Rightarrow uniform (?) distribution of initial values of (τ, θ)

P. Conlon, C. H. Kom, K. Suruliz, B. C. Allanach, F. Quevedo

arXiv:0704.3403v1 [hep-ph] 25 Apr 2007

Sparticle Spectra and LHC Signatures for Large Volume String Compactifications

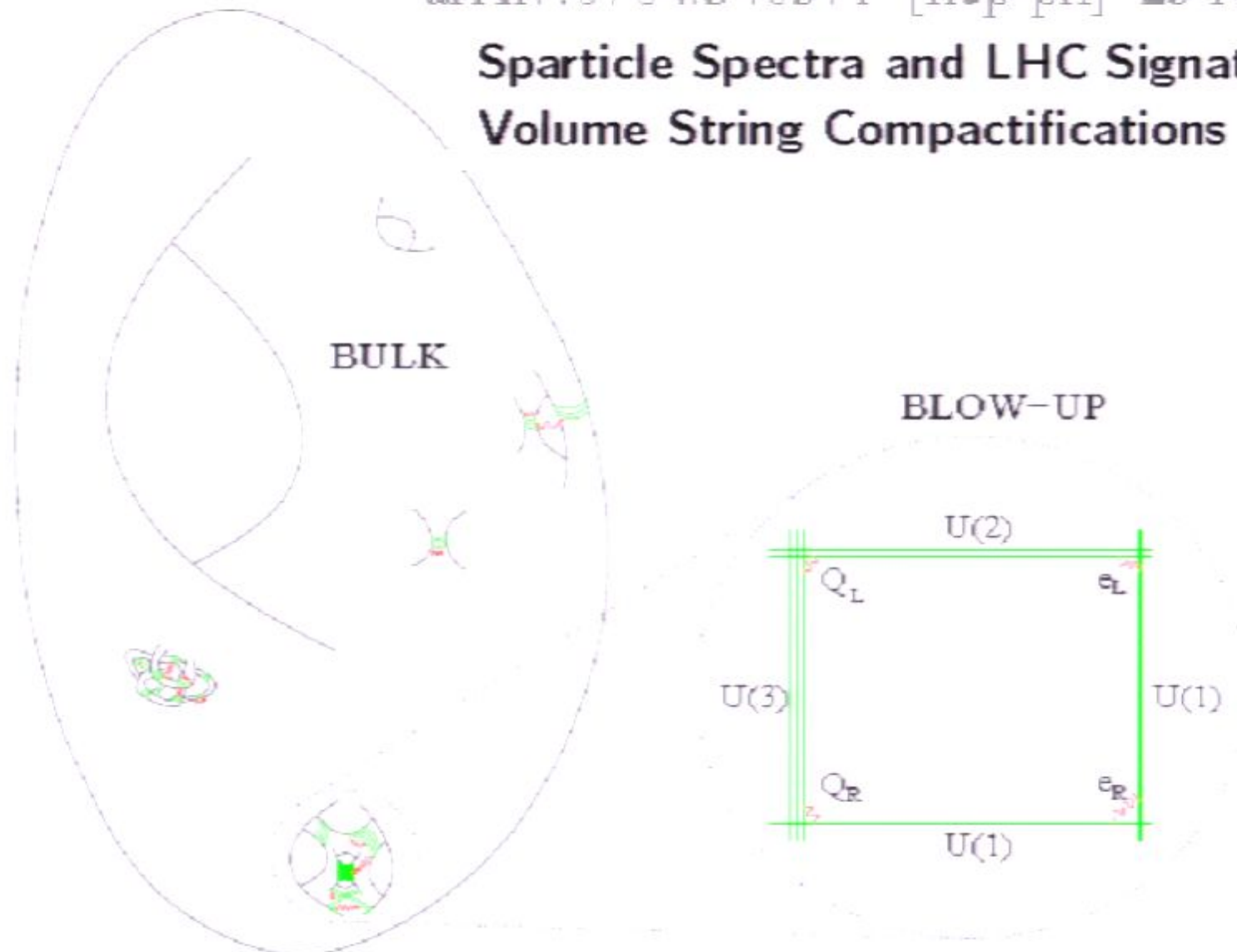
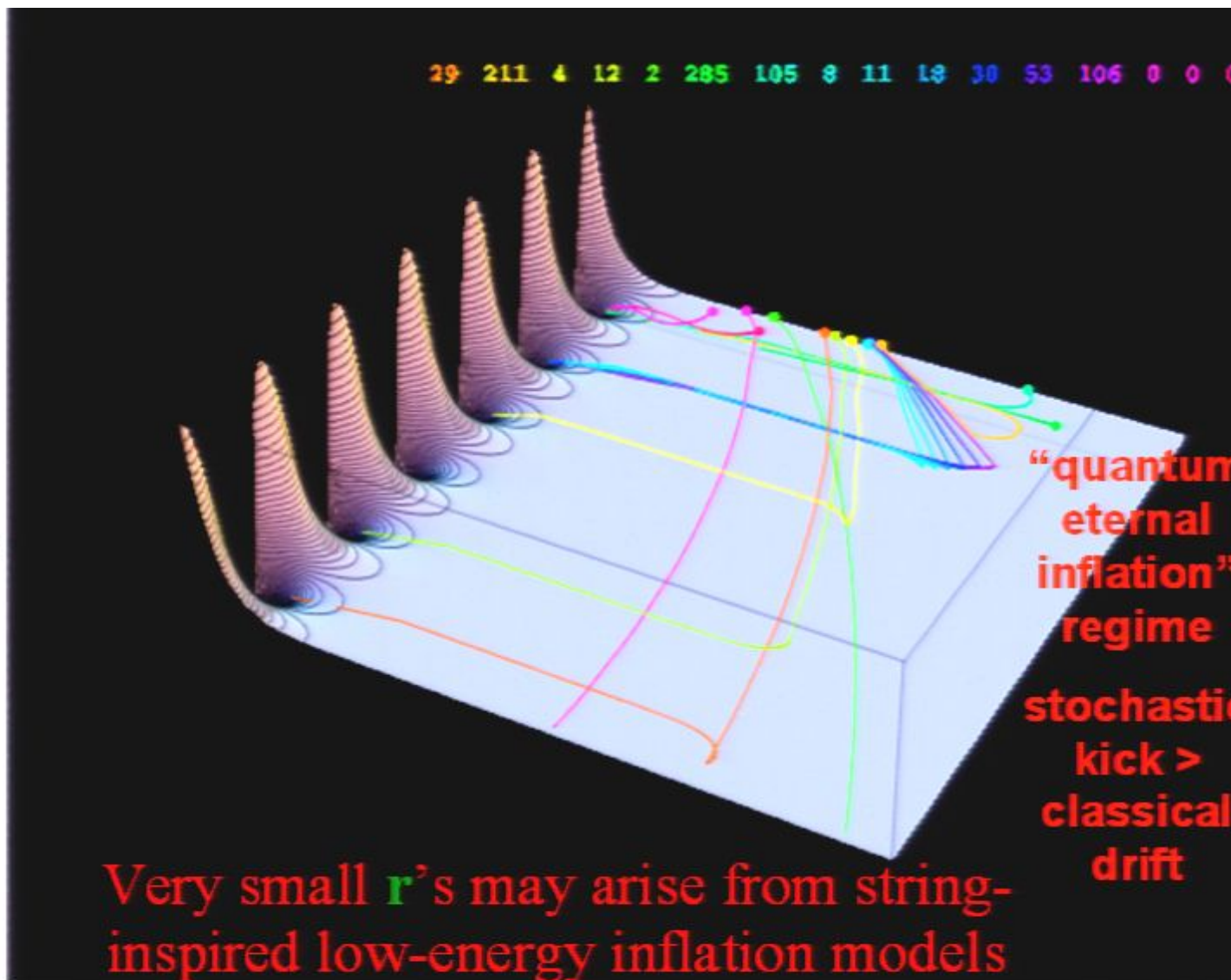


Figure 1: The physical picture: Standard Model matter is supported on a small blow-up cycle located within the bulk of a very large Calabi-Yau. The volume of the Calabi-Yau sets the gravitino mass and is responsible for the weak/Planck hierarchy

Roulette:

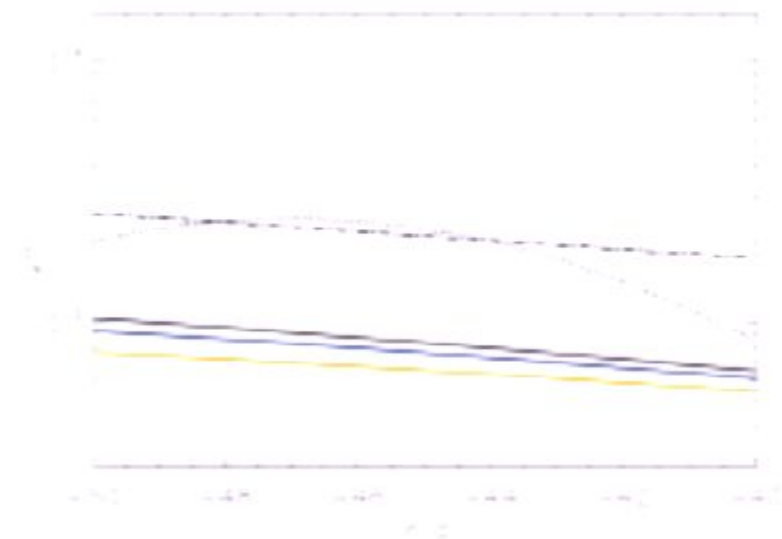
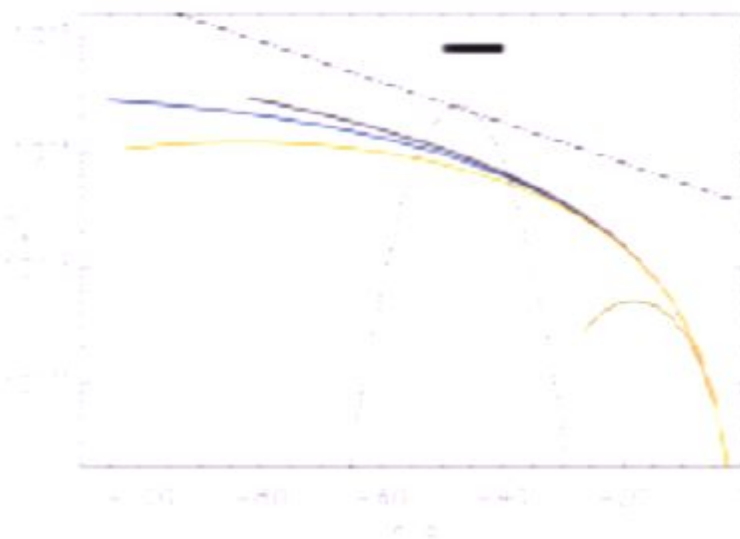
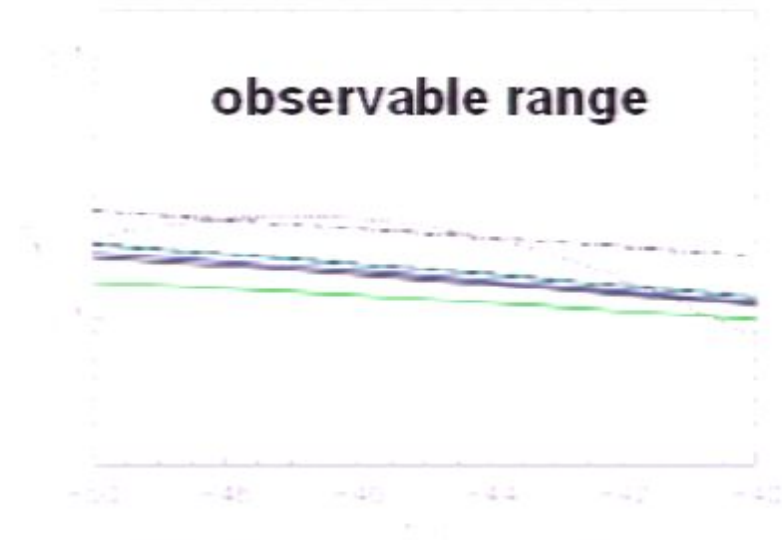
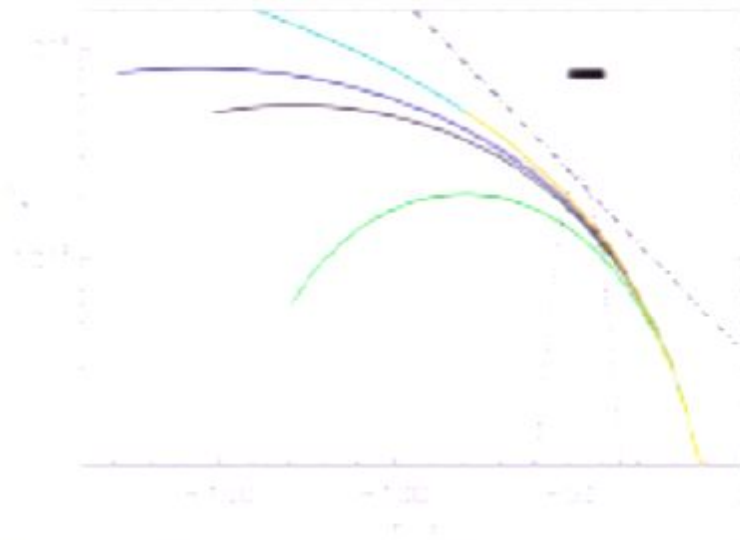
which minimum for the rolling ball depends upon the throw; but which roulette wheel we play is chance too.

The 'house' does not just play dice with the world.



$$V(\tau, \theta) = \frac{8(a_2 A_2)^2 \sqrt{\tau} e^{-2a_2 \tau}}{3\alpha \lambda_2 \mathcal{V}_5} + \frac{4W_0 a_2 A_2 \tau e^{-a_2 \tau} \cos(a_2 \theta)}{\mathcal{V}_5^2} + \frac{3W_0^2 \xi}{4\mathcal{V}_5^3} + V_{\text{uplift}}$$

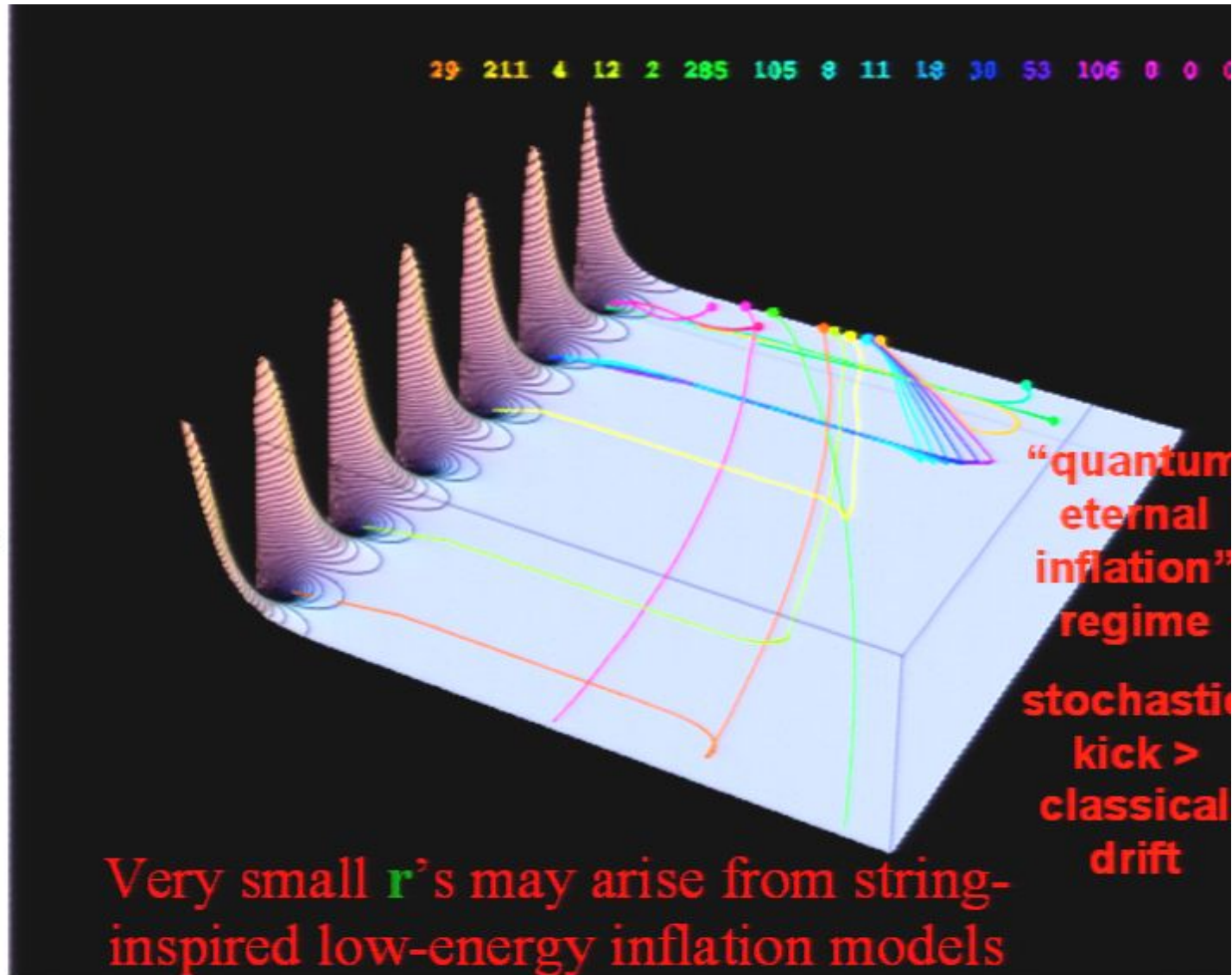
P_S (ln Ha) Kahler trajectories



Roulette:

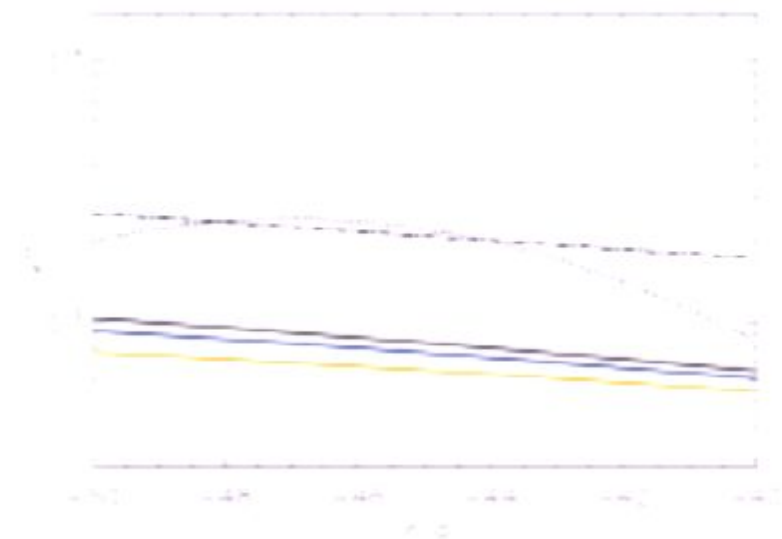
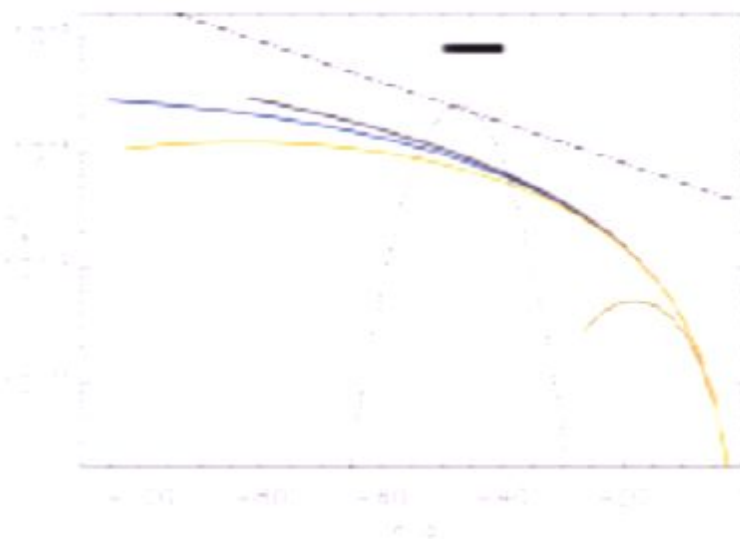
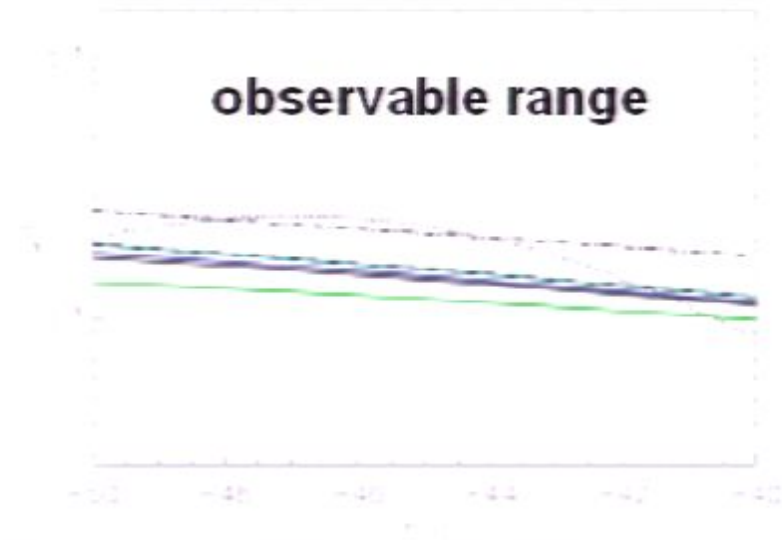
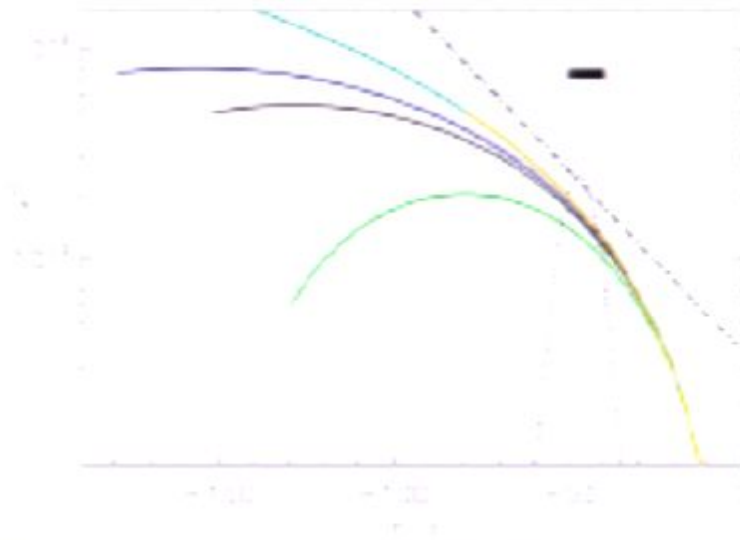
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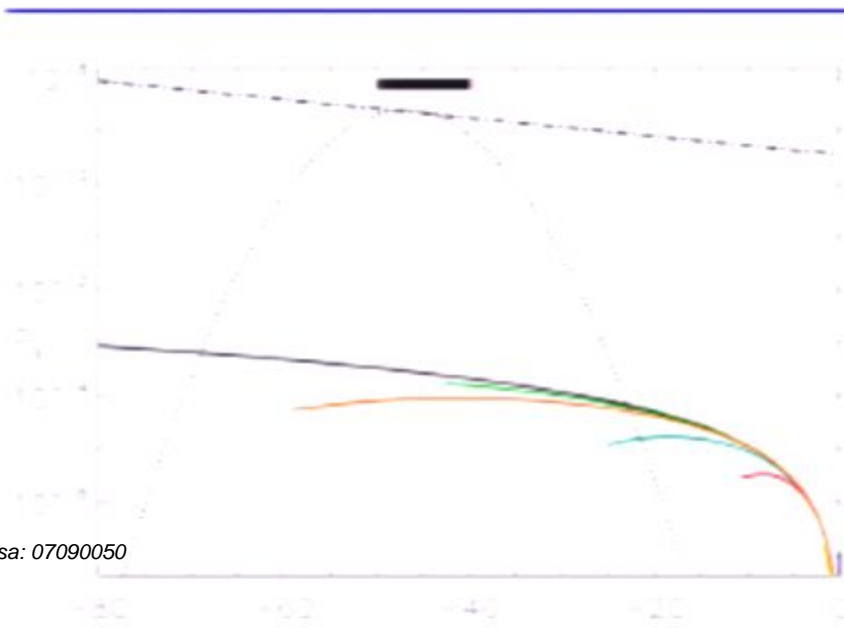
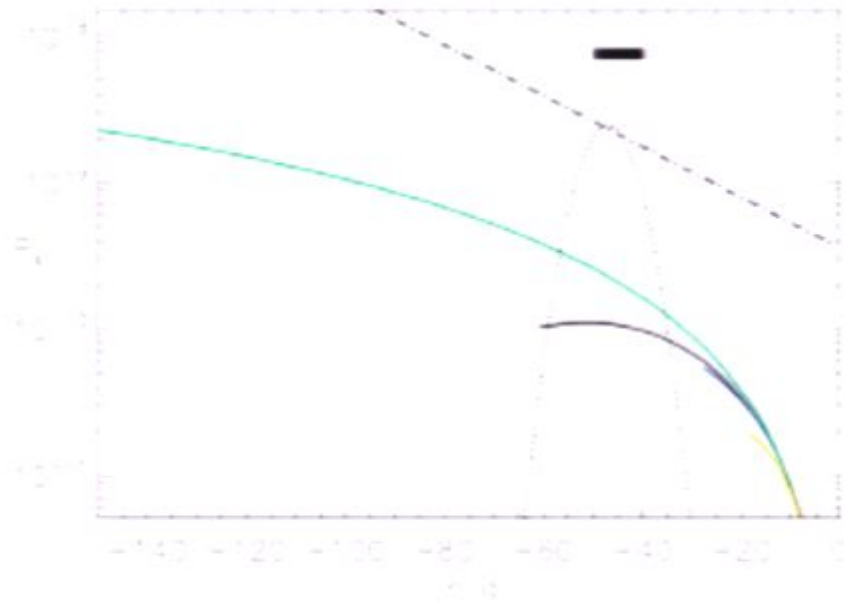
$$V(\tau, \theta) = \frac{8(a_2 A_2)^2 \sqrt{\tau} e^{-2a_2 \tau}}{3\alpha \lambda_2 V_5} + \frac{4W_0 a_2 A_2 \tau e^{-a_2 \tau} \cos(a_2 \theta)}{V_5^2} + \frac{3W_0^2 \xi}{4V_5^3} + V_{\text{uplift}}$$

P_S (ln Ha) Kahler trajectories

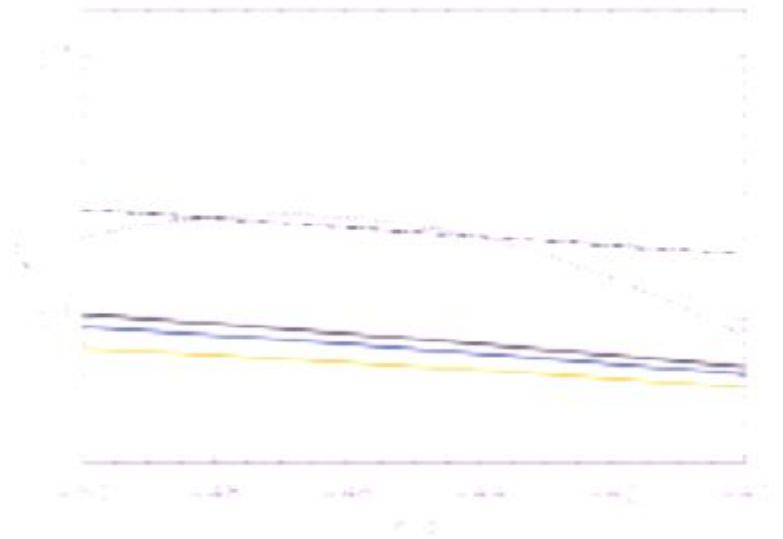
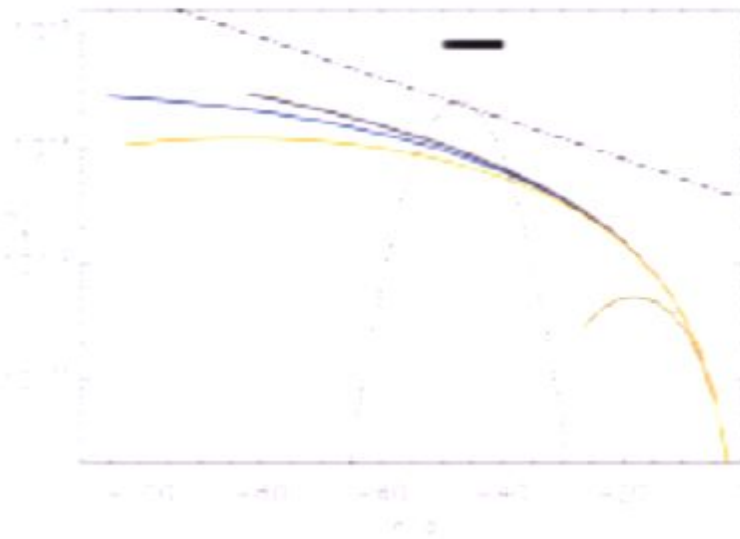
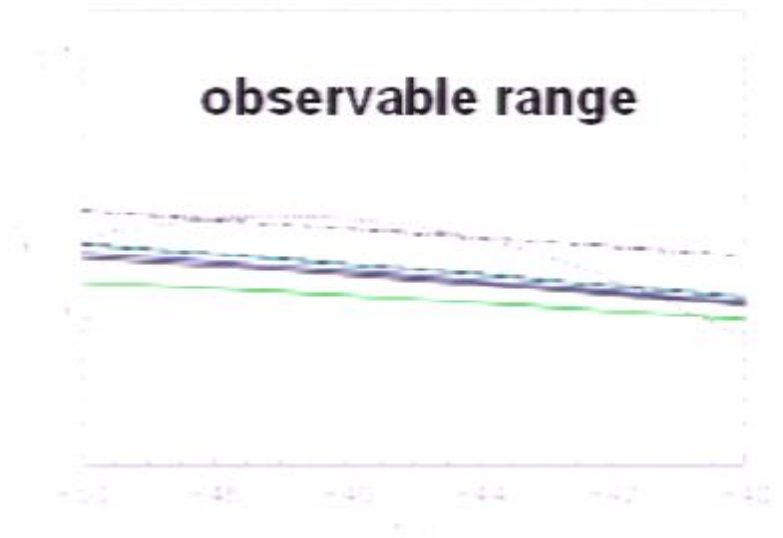
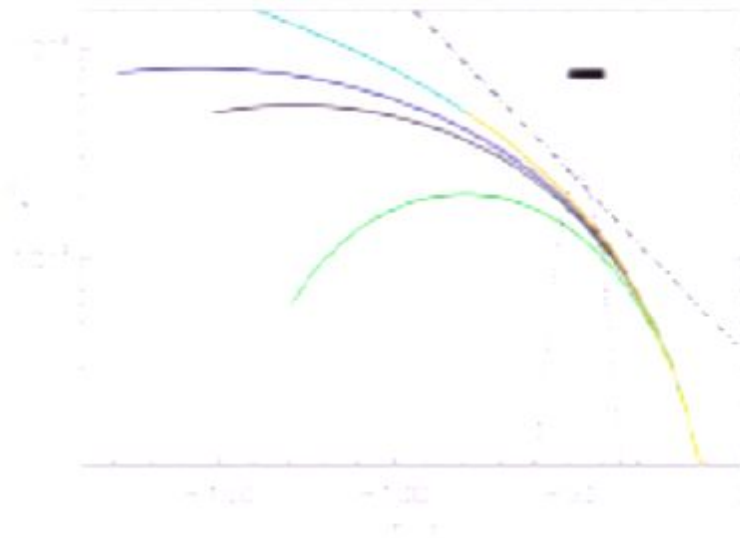


Ps (In Ha) Kahler trajectories

It is much easier to get models which do not agree with observations. Here the amplitude is off.



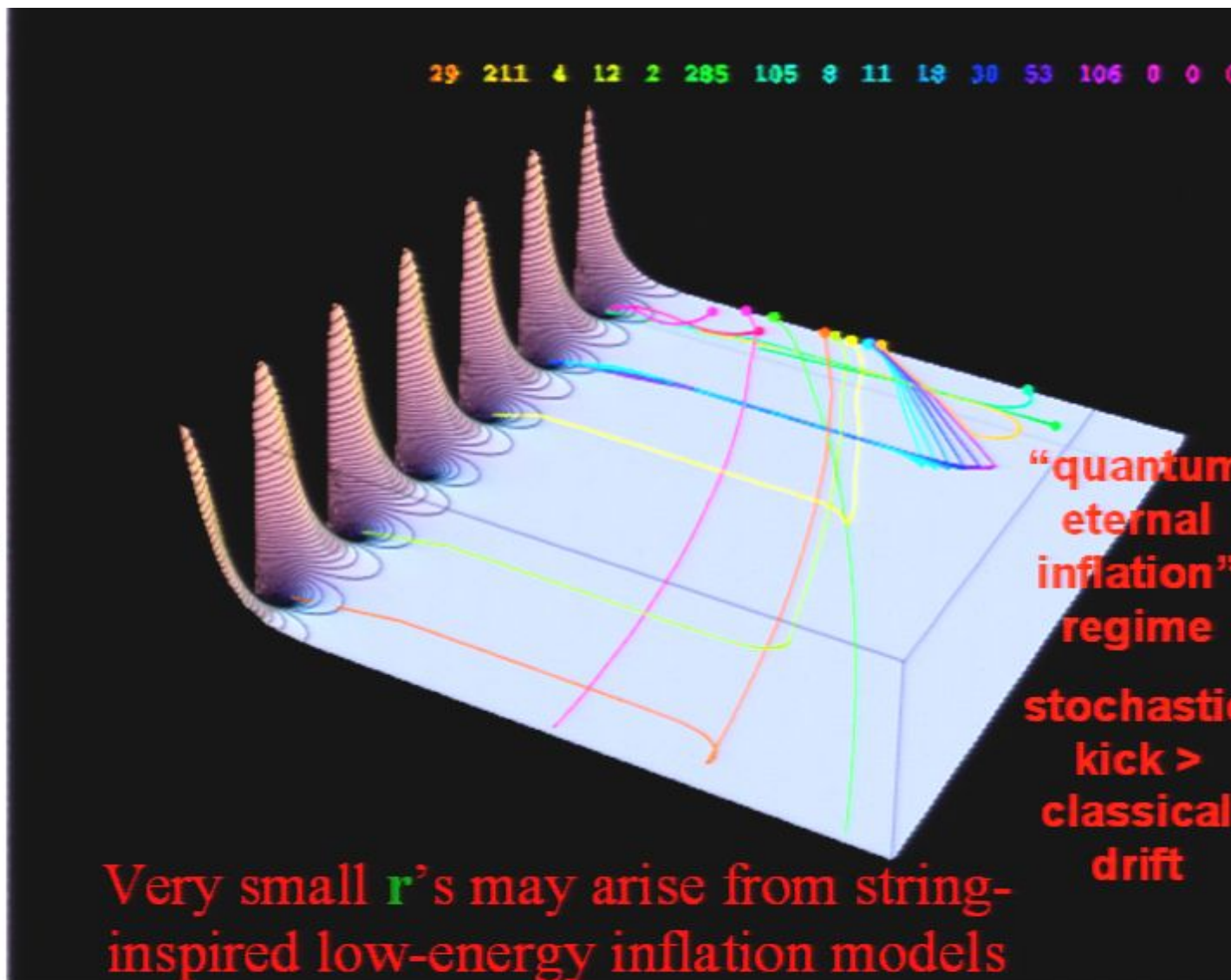
P_s (ln Ha) Kahler trajectories



Roulette:

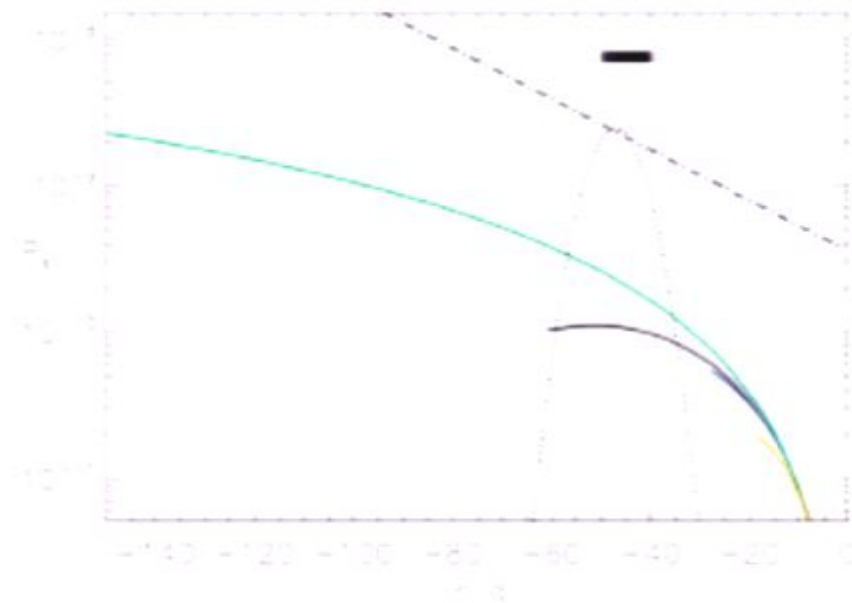
which minimum for the rolling ball depends upon the throw; but which roulette wheel we play is chance too.

The 'house' does not just play dice with the world.

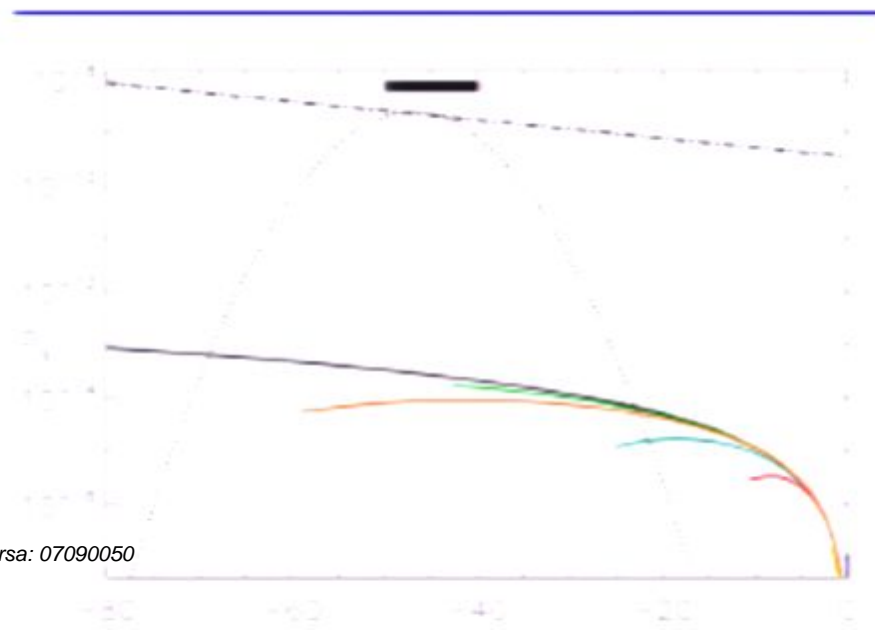


$$V(\tau, \theta) = \frac{8(a_2 A_2)^2 \sqrt{\tau} e^{-2a_2 \tau}}{3\alpha \lambda_2 V_5} + \frac{4W_0 a_2 A_2 \tau e^{-a_2 \tau} \cos(a_2 \theta)}{V_5^2} + \frac{3W_0^2 \xi}{4V_5^3} + V_{\text{uplift}}$$

Ps (In Ha) Kahler trajectories



It is much easier to get models which do not agree with observations. Here the amplitude is off.



New Parameters of Cosmic Structure Formation

$$\Omega_k$$

$$\Omega_b h^2$$

$$\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$$

$$\ln \mathcal{P}_t(k)$$

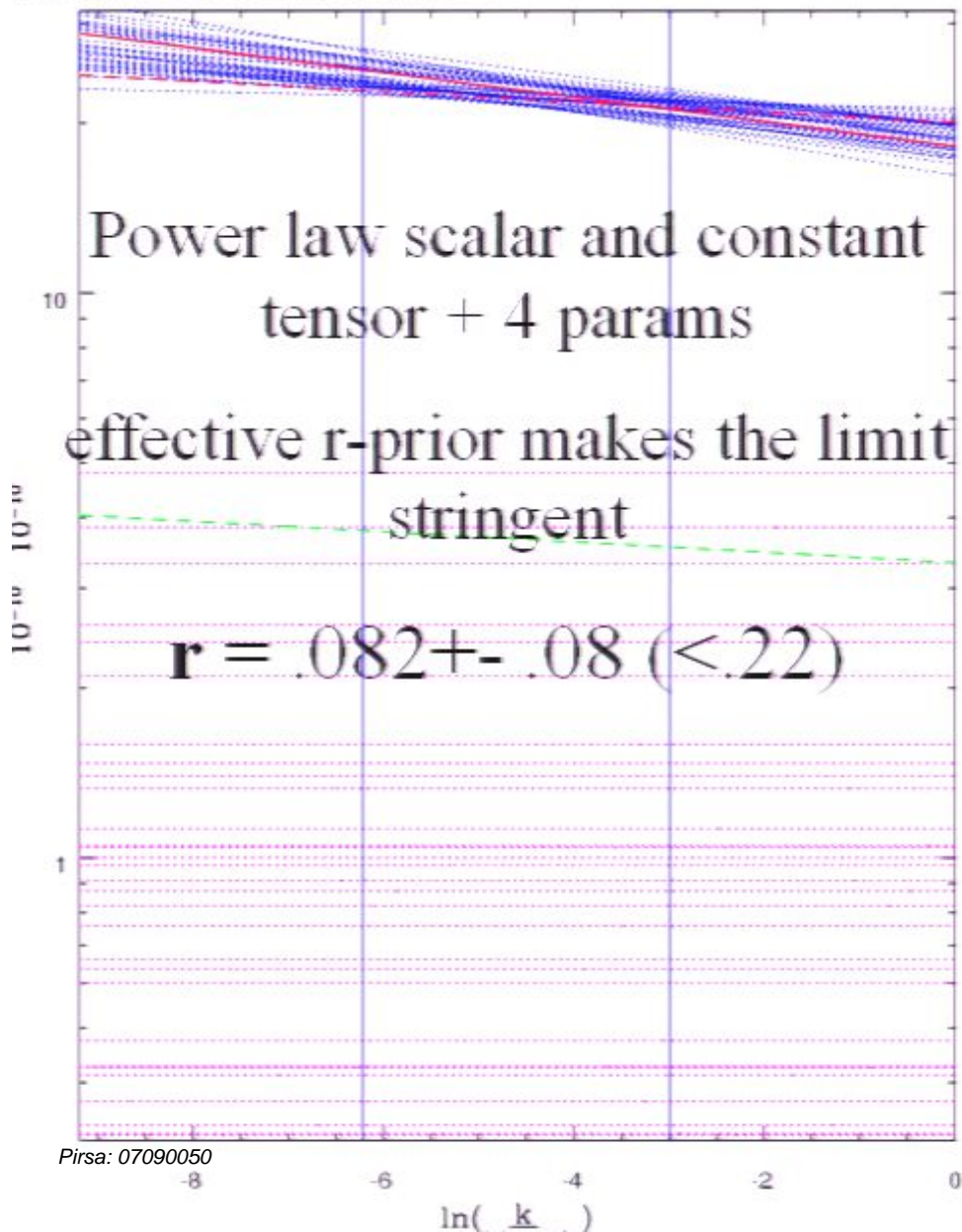
$$\Omega_{dm} h^2$$

$$\ln \mathcal{P}_s(k)$$

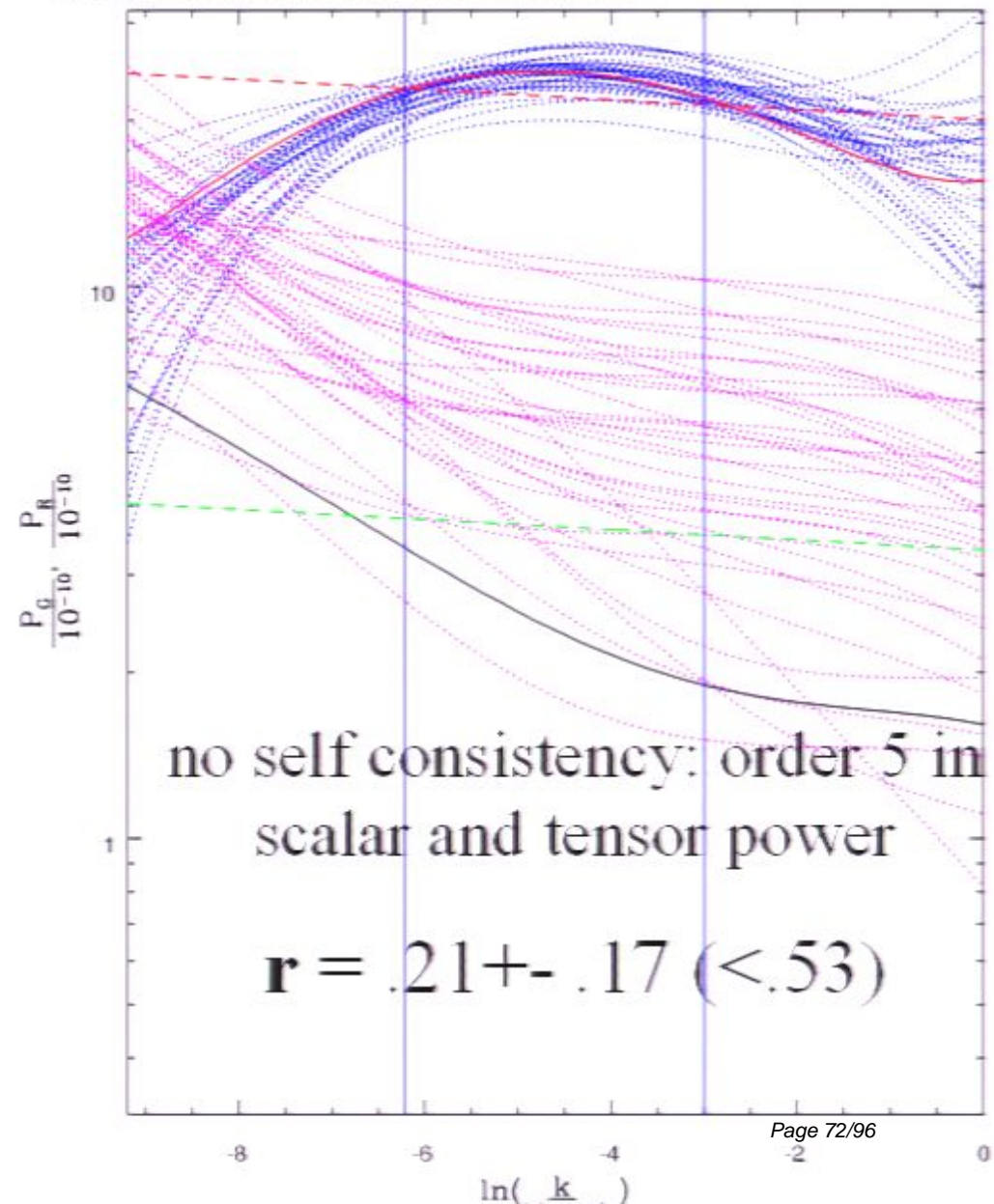
$$\tau_c$$

$\ln P_s P_t$ (nodal 2 and 1) + 4 params of $P_s P_t$ (nodal 5 and 5) + 4 params
reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC

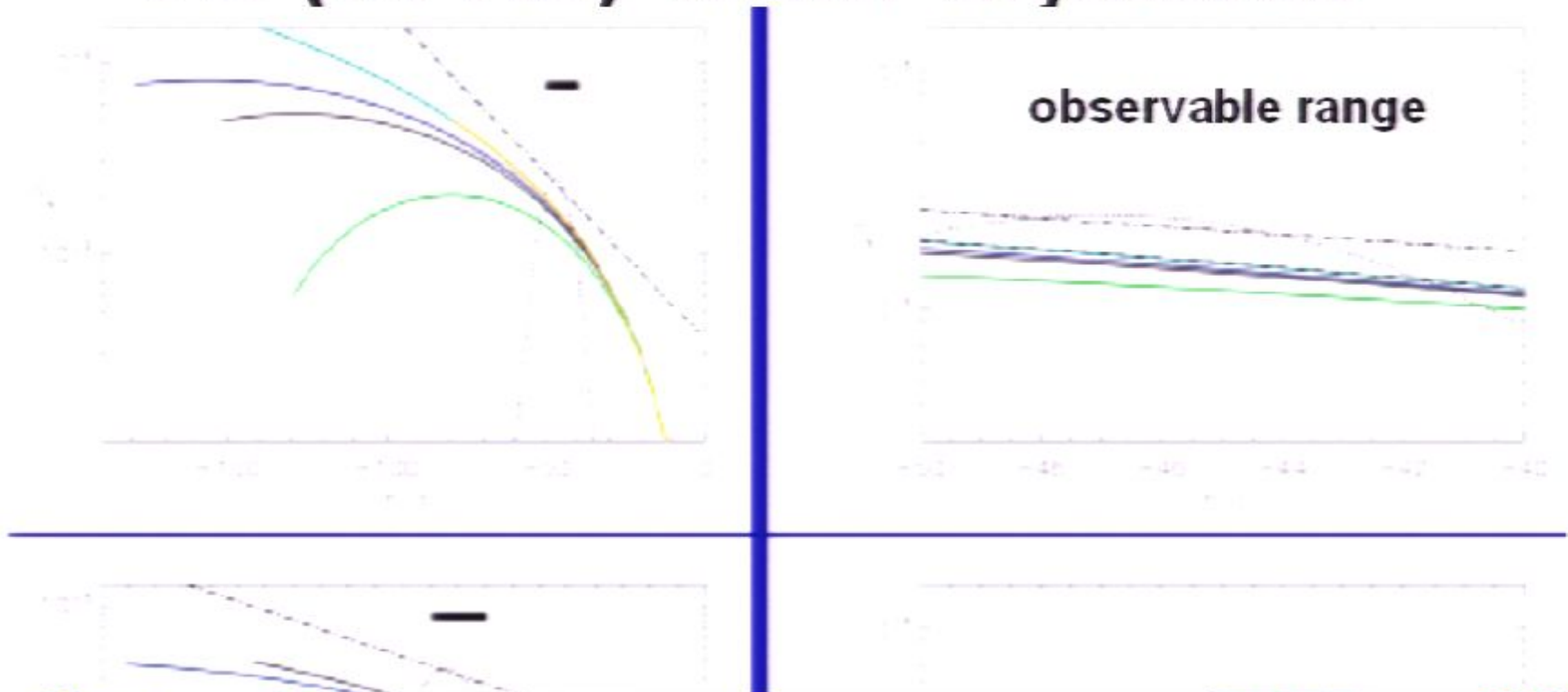
PR2_1_all_paramsb.powerspectrum.likestats



PR_nodal5_5_all_params_cont.powerspectrum.likestats



P_s (In Ha) Kahler trajectories



play dice with
the world.

Very small r 's may arise from string-
inspired low-energy inflation models

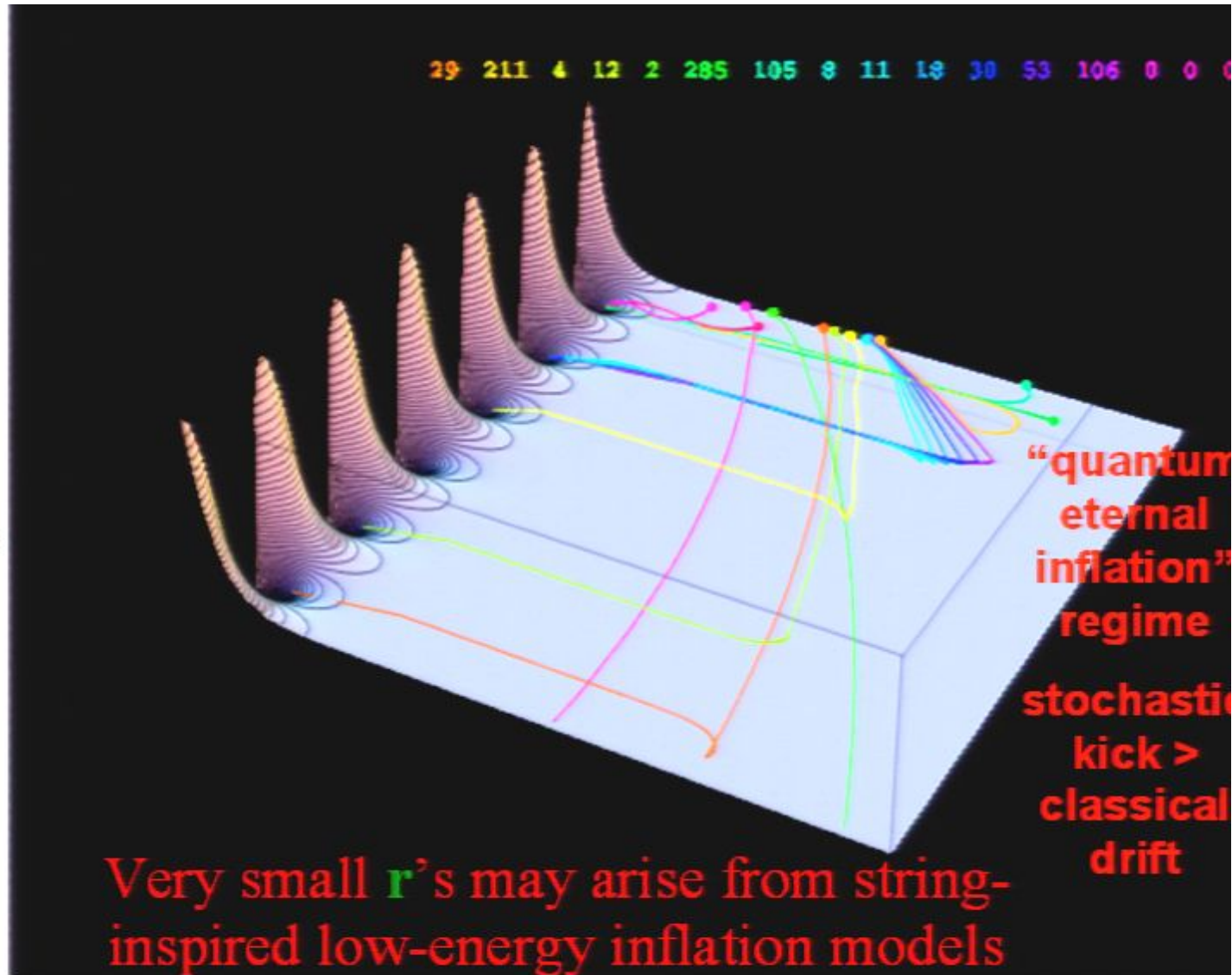
classical
drift

$$V(\tau, \theta) = \frac{8(a_2 A_2)^2 \sqrt{\tau} e^{-2a_2 \tau}}{3\alpha \lambda_2 \mathcal{V}_5} + \frac{4W_0 a_2 A_2 \tau e^{-a_2 \tau} \cos(a_2 \theta)}{\mathcal{V}_5^2} + \frac{3W_0^2 \xi}{4\mathcal{V}_5^3} + V_{\text{uplift}}$$

Roulette:

which minimum for the rolling ball depends upon the throw; but which roulette wheel we play is chance too.

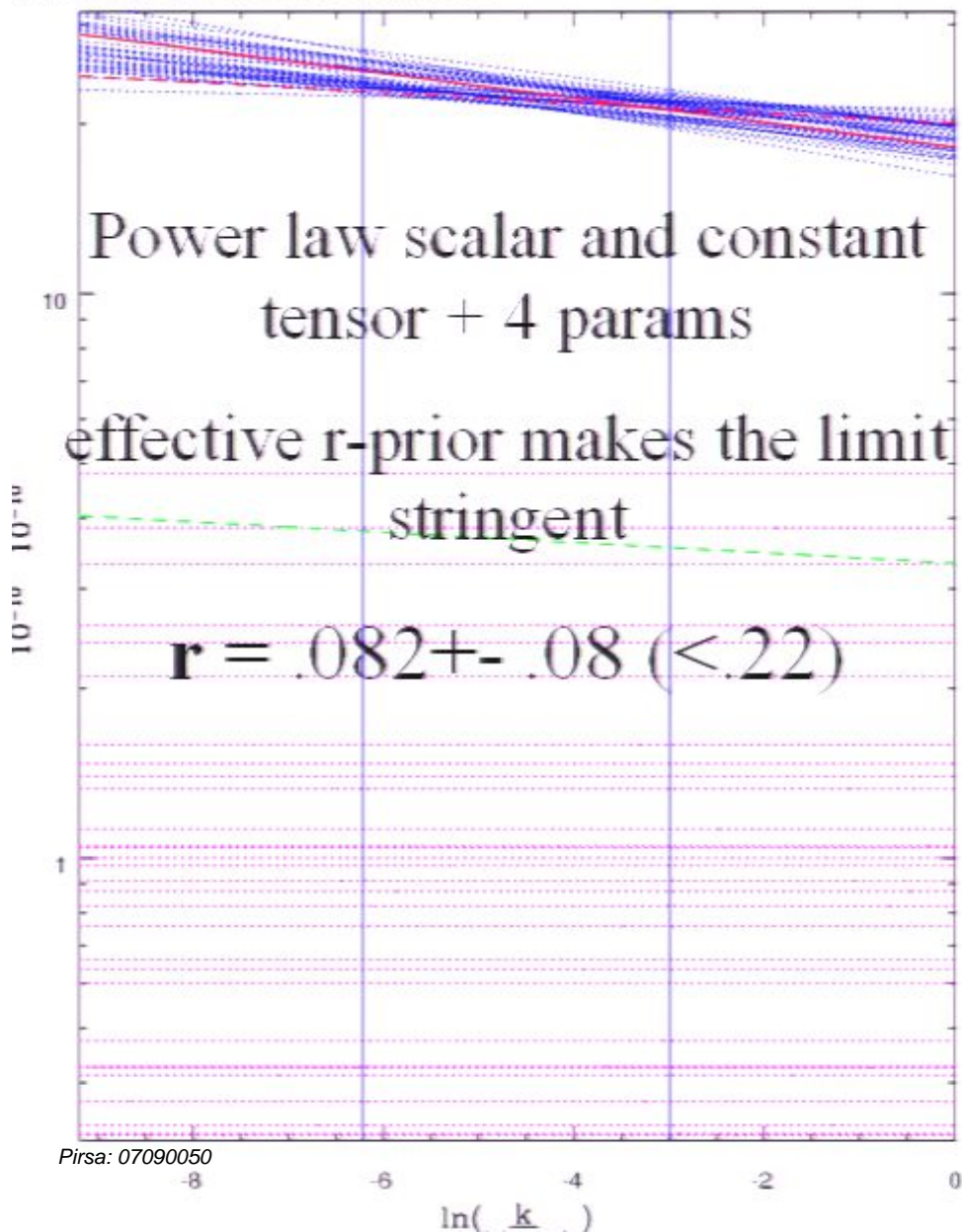
The 'house' does not just play dice with the world.



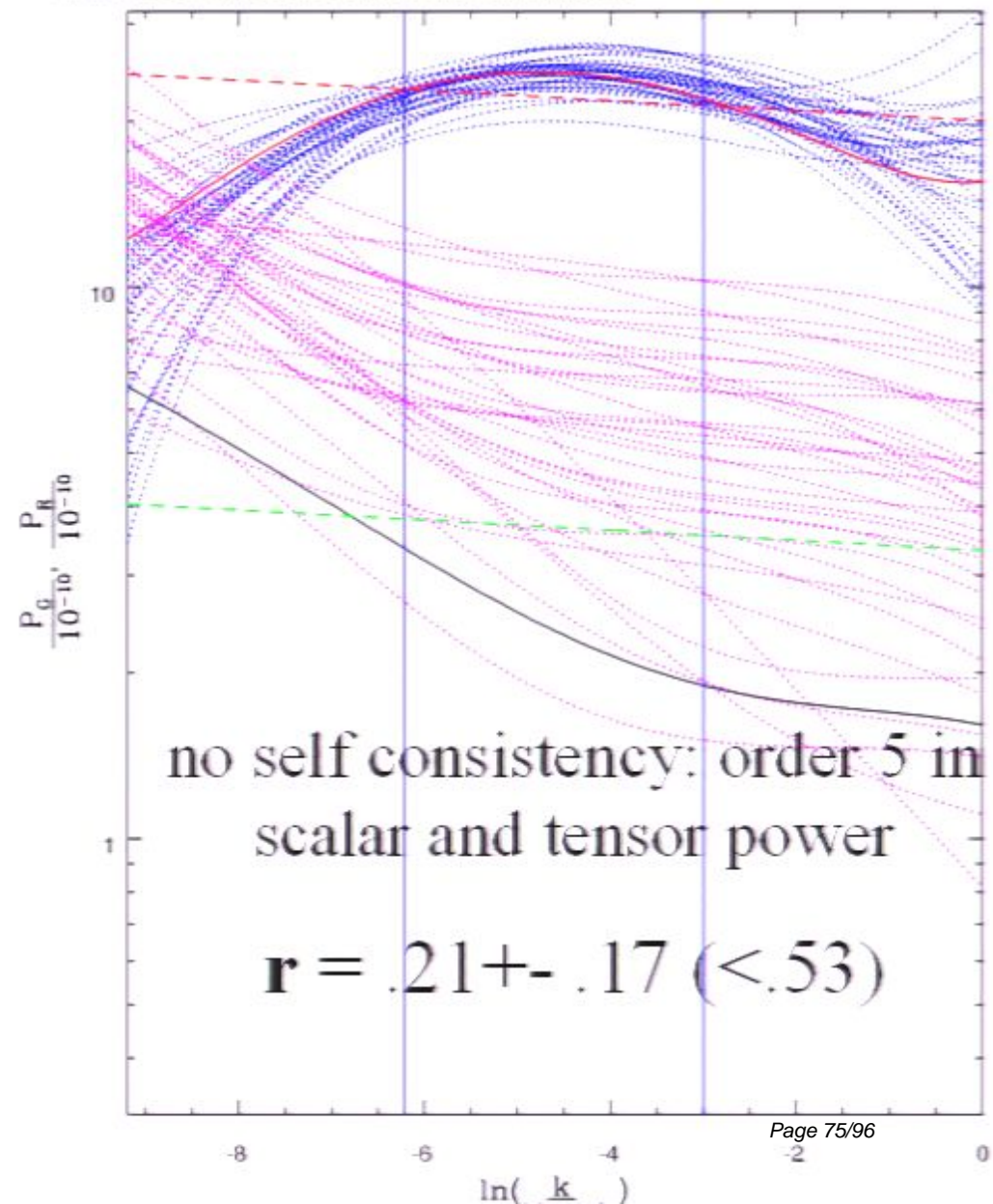
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$\ln P_s P_t$ (nodal 2 and 1) + 4 params of $P_s P_t$ (nodal 5 and 5) + 4 params
 reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC

PR2_1_all_paramsb.powerspectrum.likestats

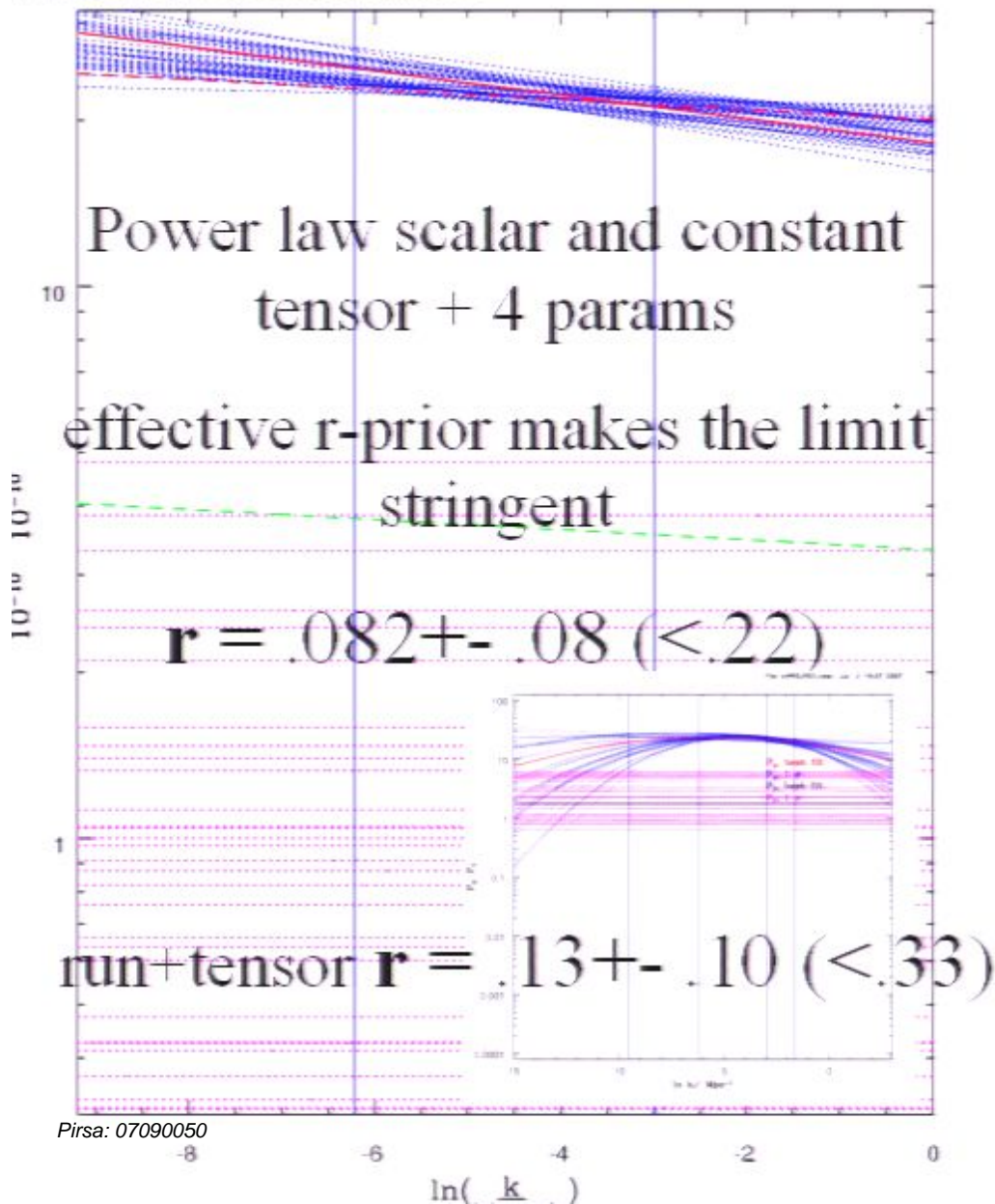


PR_nodal5_5_all_params_cont.powerspectrum.likestats

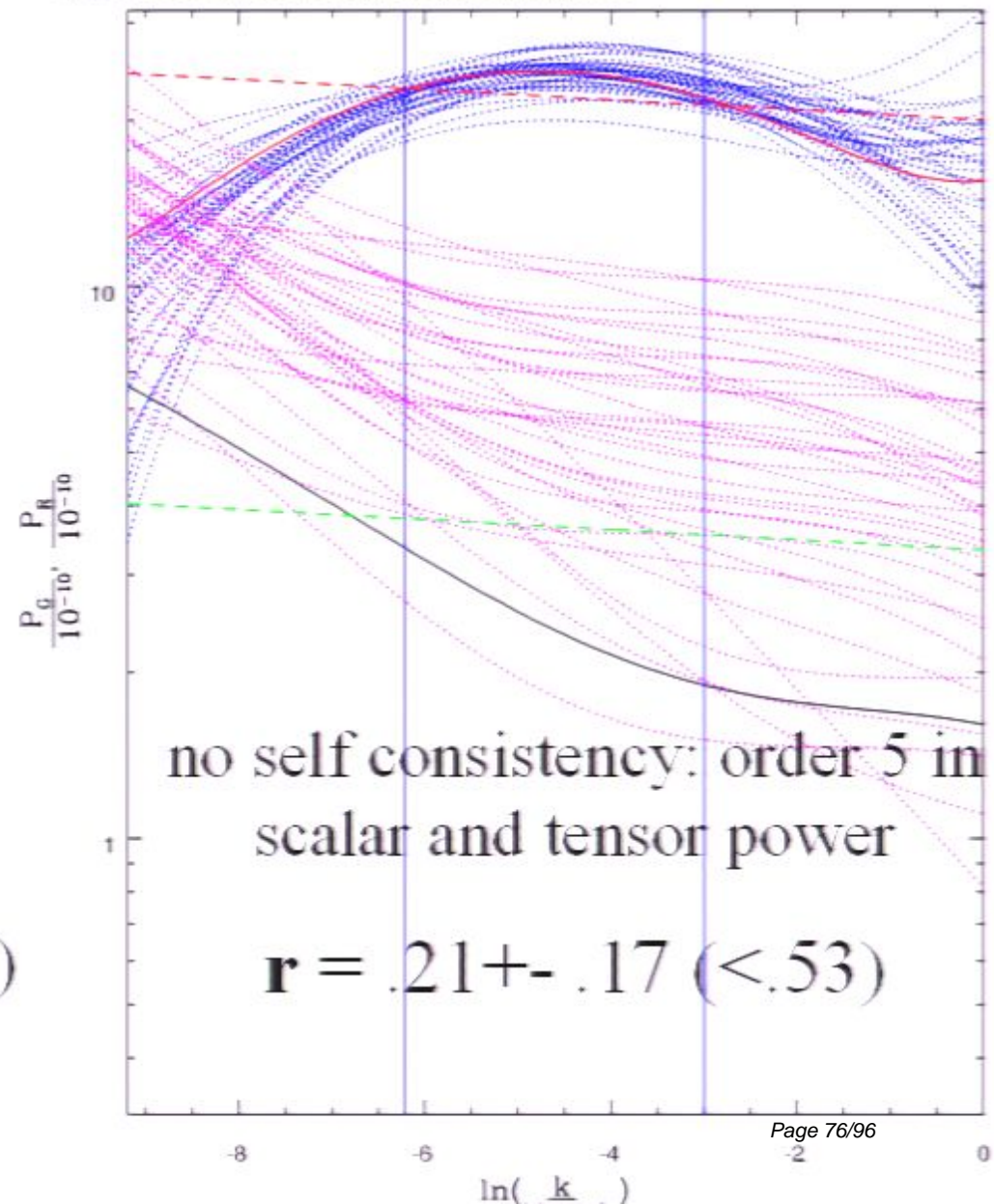


$\ln P_s P_t$ (nodal 2 and 1) + 4 params of $P_s P_t$ (nodal 5 and 5) + 4 params
 reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC

PR2_1_all_paramsb.powerspectrum.likestats



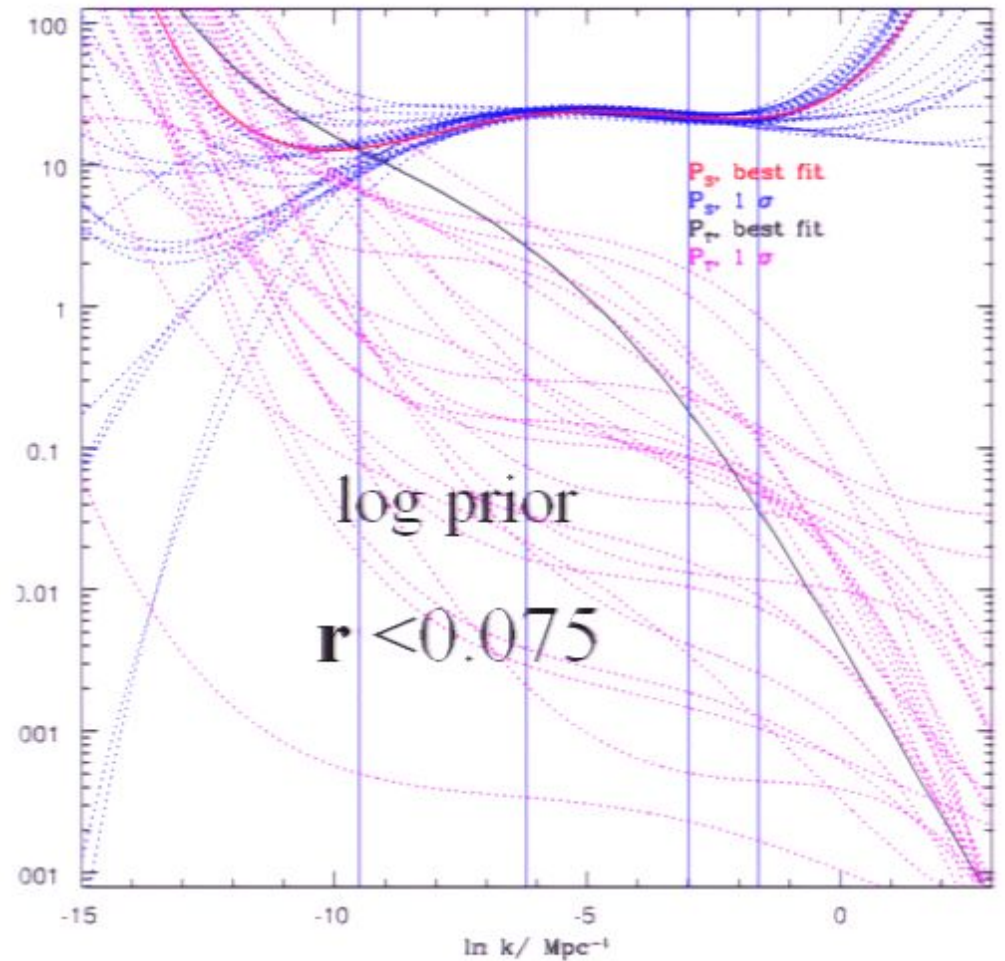
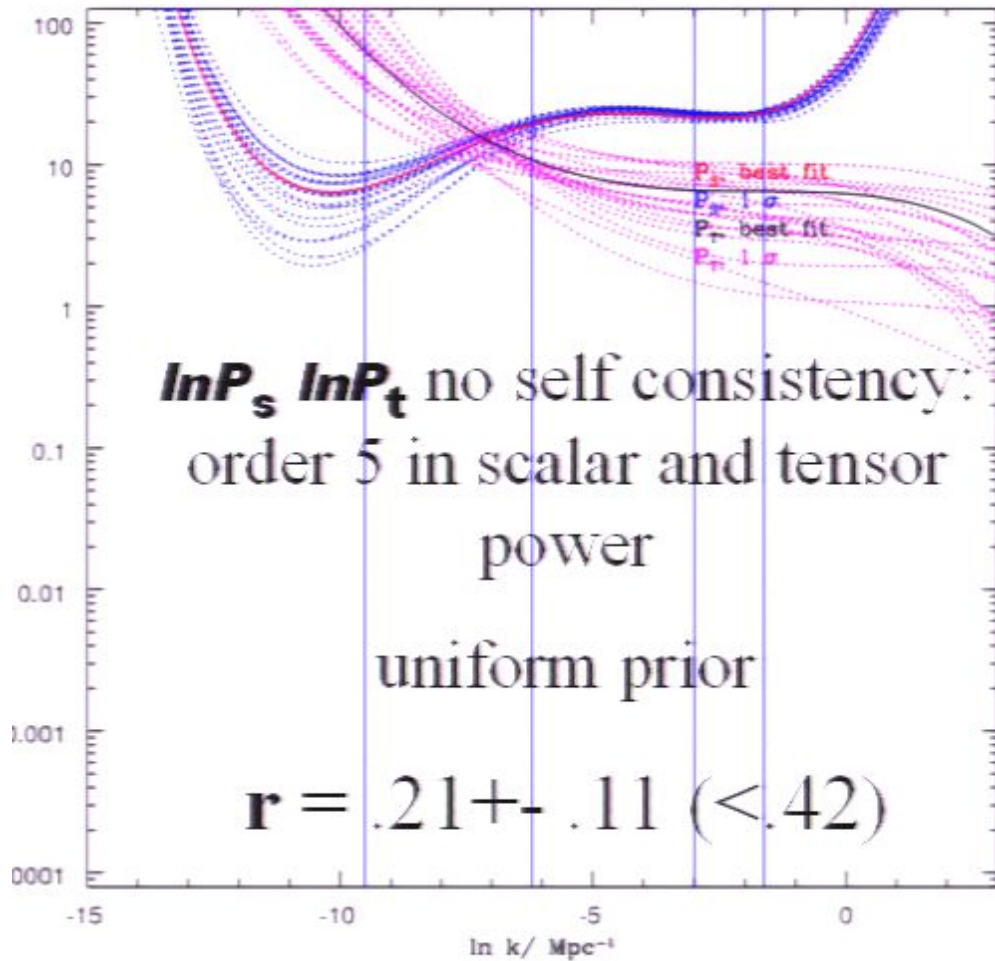
PR_nodal5_5_all_params_cont.powerspectrum.likestats



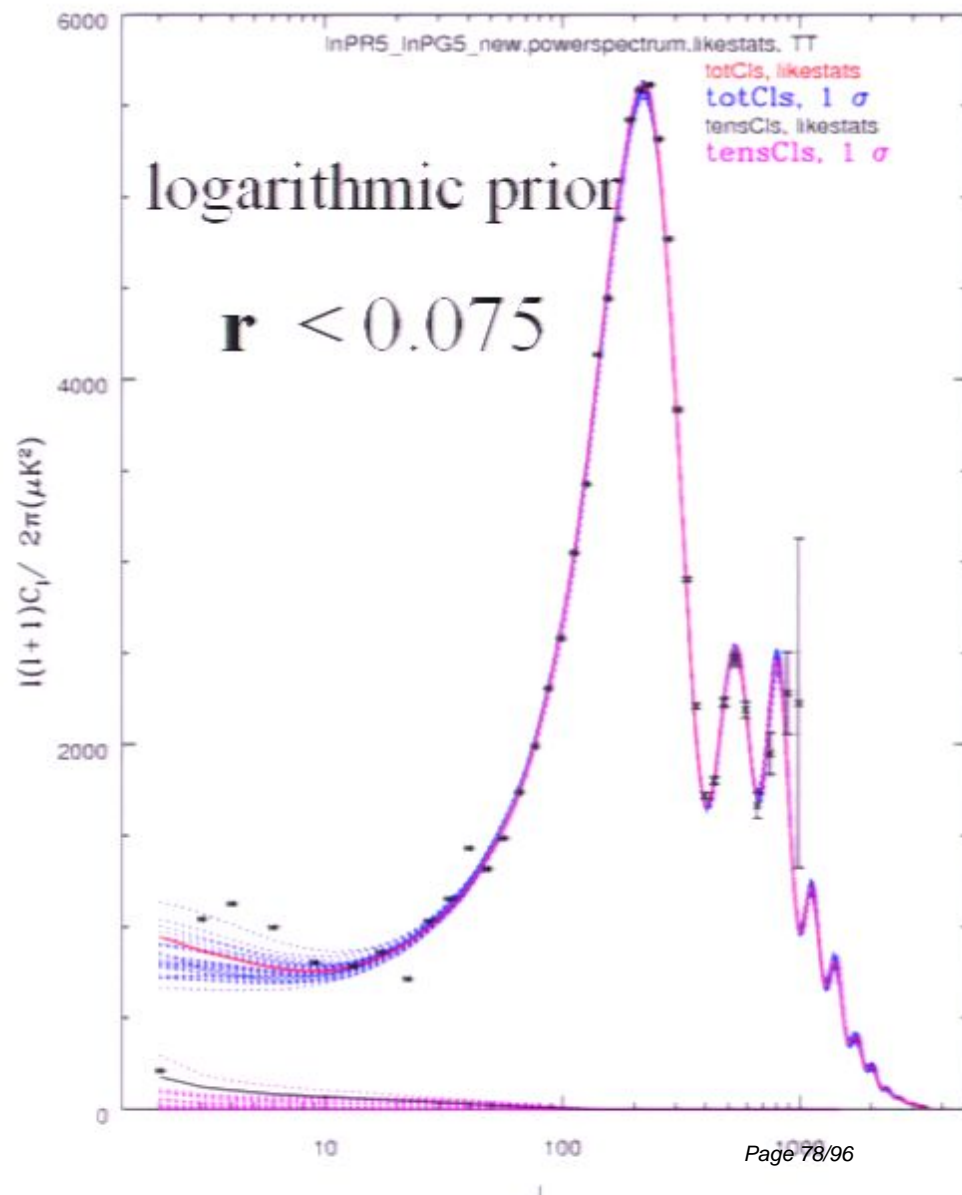
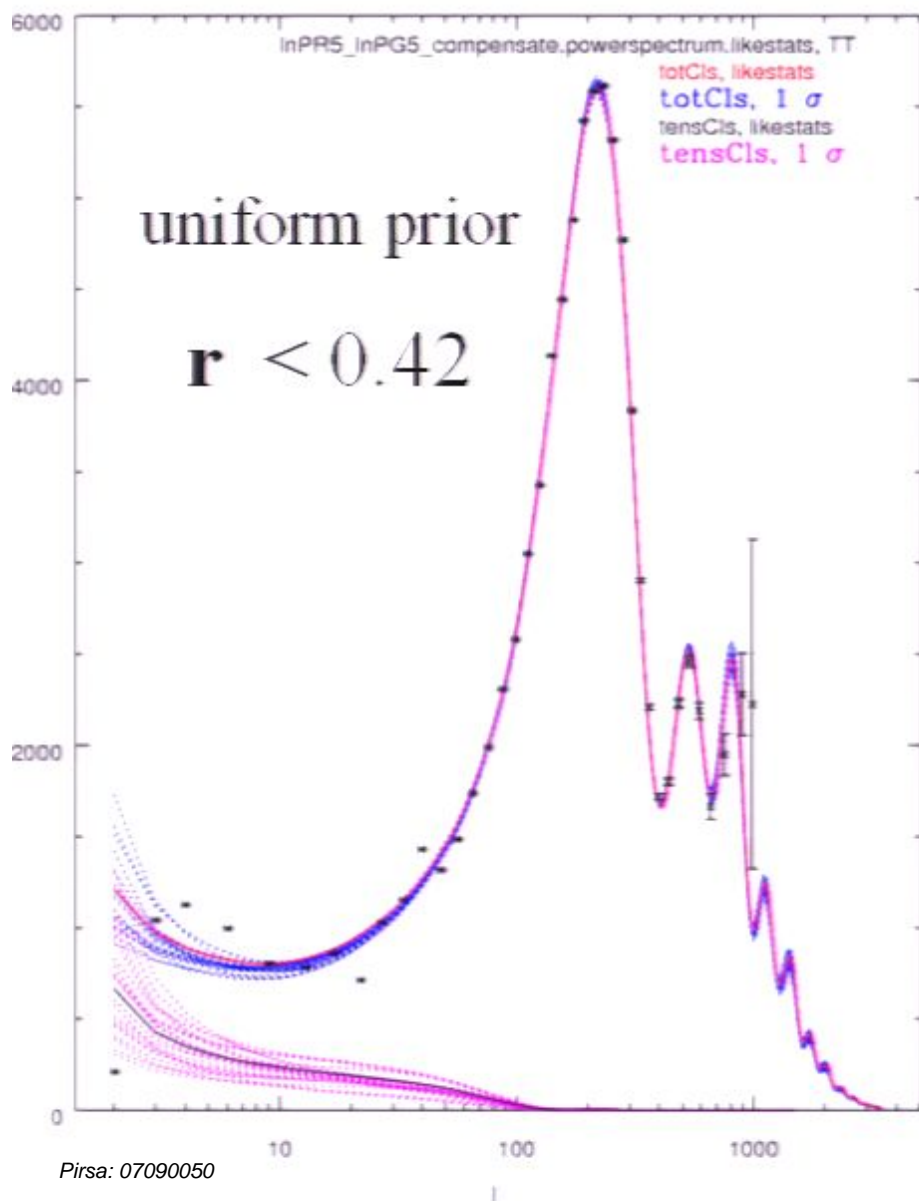
$\ln P_s \ln P_t$ (nodal 5 and 5) + 4 params. Uniform in $\exp(\text{nodal bandpowers})$ cf. uniform in nodal bandpowers reconstructed from April07 CMB+LSS data using Chebyshev nodal point expansion & MCMC: shows prior dependence with current data

File: lnPR5_lnPG5_compensate : Jul 2 19:38 2007

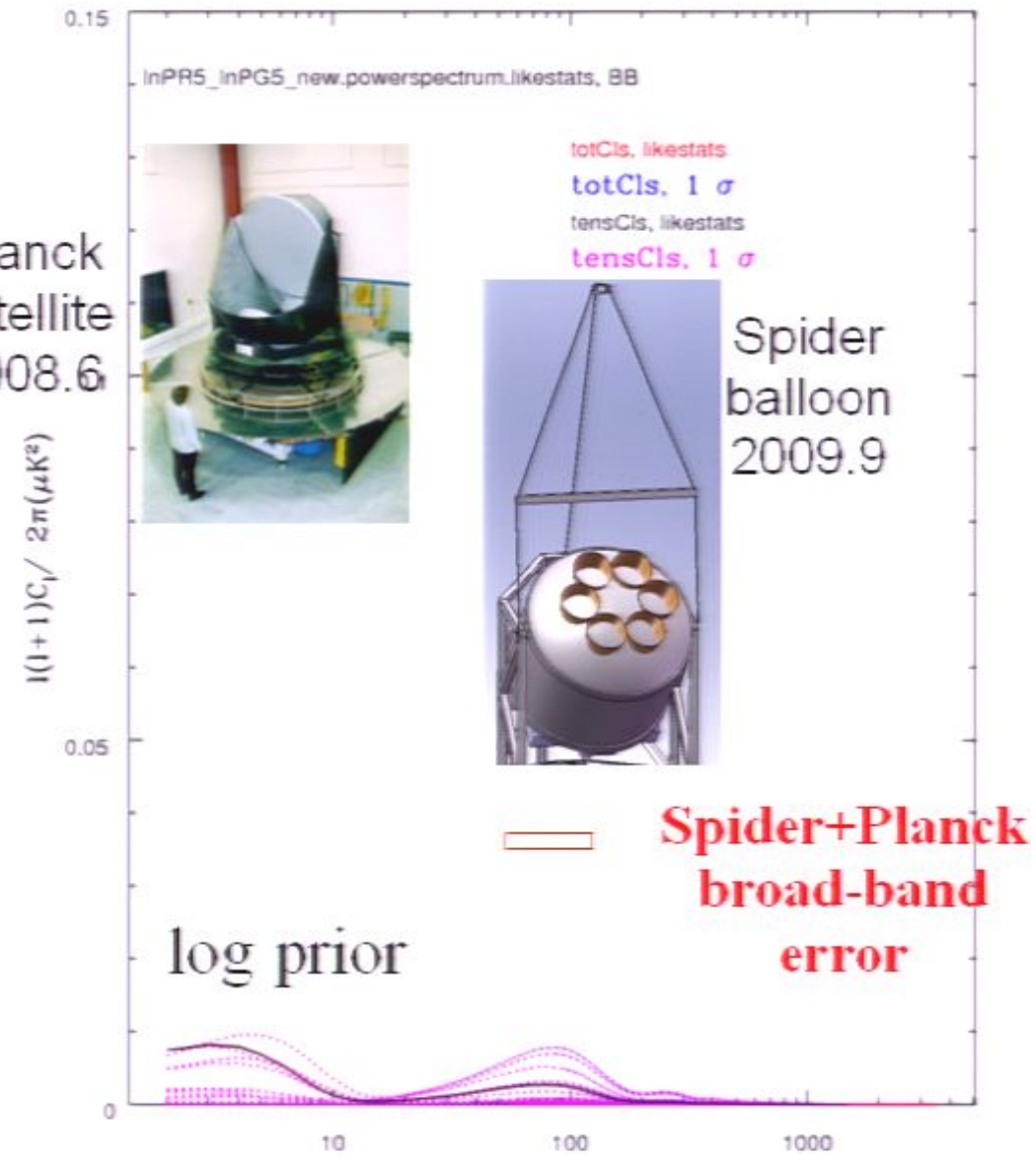
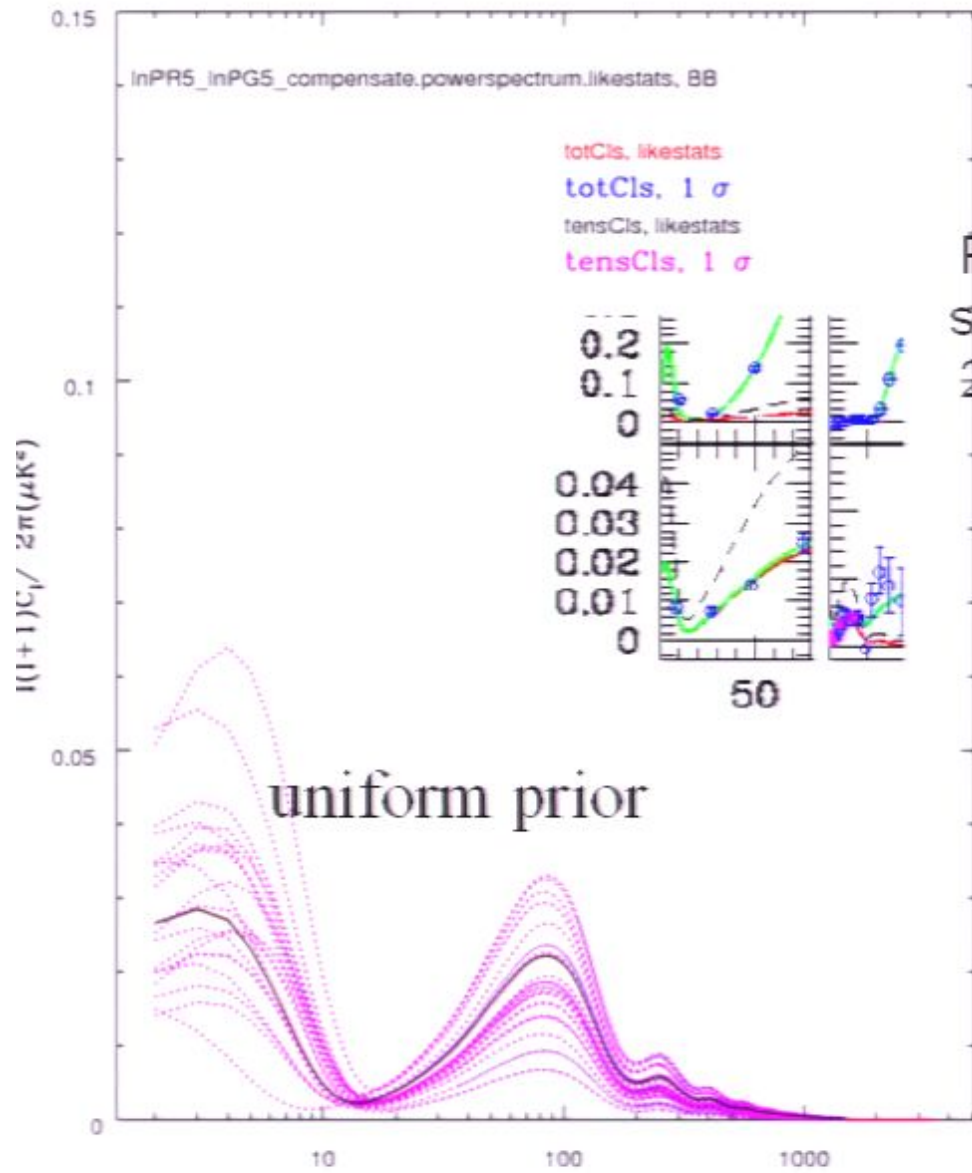
File: lnPR5_lnPG5_new : Jul 2 19:39 2007



$\ln P_s \ln P_t$ (nodal 5 and 5) + 4 params. Uniform in $\exp(\text{nodal bandpowers})$ cf. uniform in nodal bandpowers reconstructed from April07 CMB+LSS data using Chebyshev nodal point expansion & MCMC: shows prior dependence with current data



C_L BB for $\ln P_s \ln P_t$ (nodal 5 and 5) + 4 params inflation trajectories reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC



New Parameters of Cosmic Structure Formation

Ω_k

$\Omega_b h^2$

$\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$

$\ln H(k_p)$

$\Omega_{dm} h^2$

$\epsilon(k), \quad k \approx Ha$

$H(k_p)$

τ_c

New Parameters of Cosmic Structure Formation

Ω_k

$\Omega_b h^2$

$\theta \sim \ell_s^{-1}, \text{ cf. } \Omega_\Lambda$

$\ln H(k_p)$

$\Omega_{dm} h^2$

τ_c

$\epsilon(k), \quad k \approx Ha$

$H(k_p)$

**=1+q, the deceleration
parameter history**

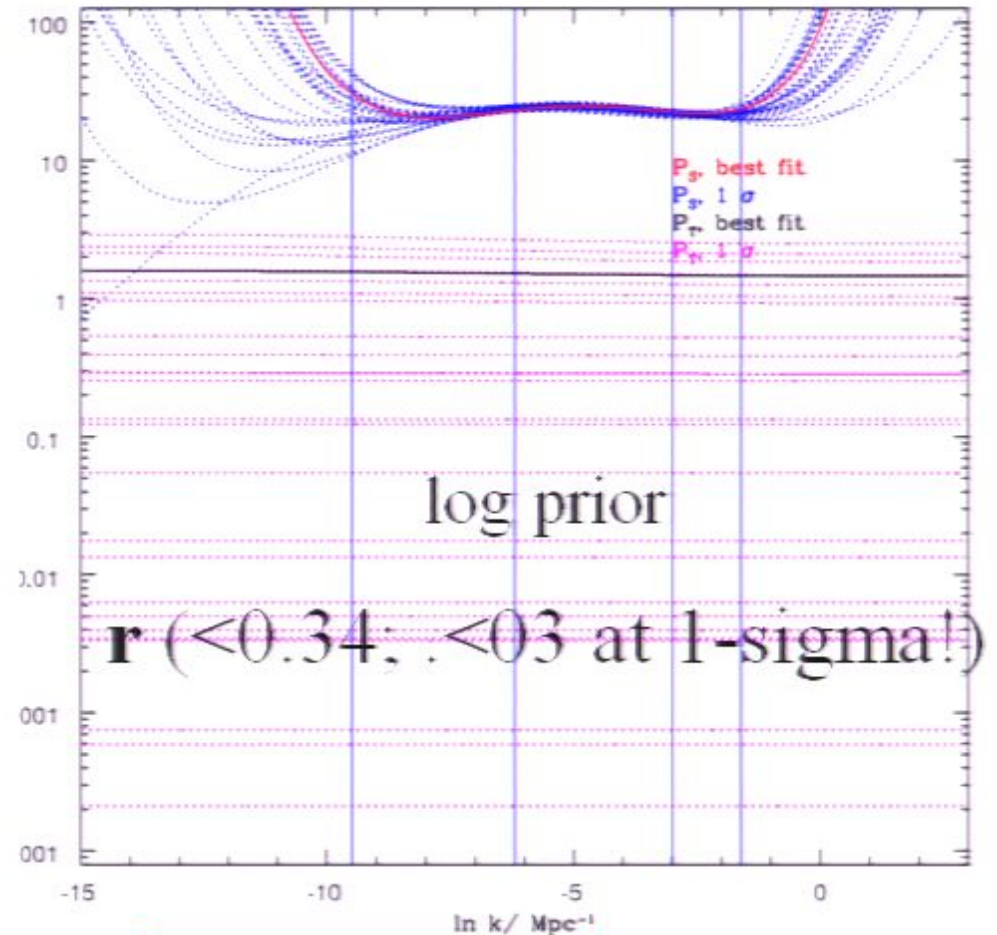
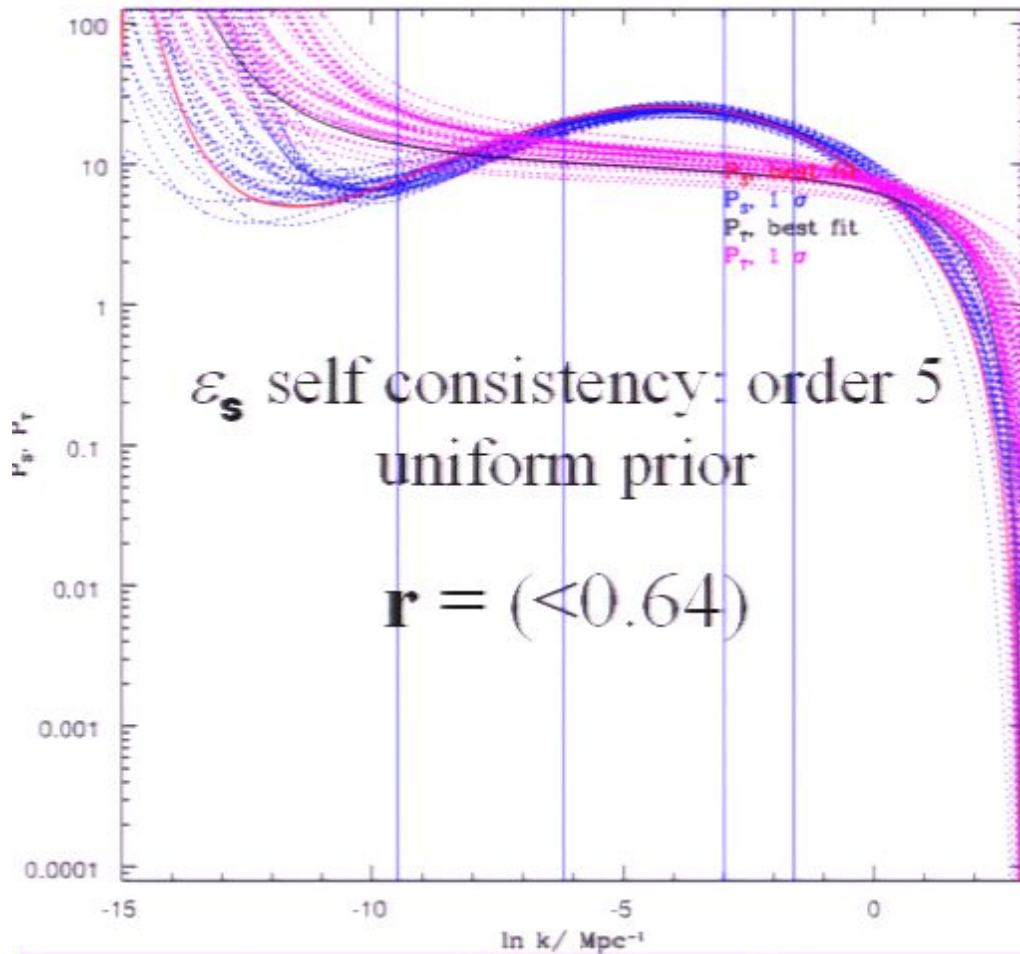
$$\mathcal{P}_s(\mathbf{k}) \propto H^2/\epsilon, \quad \mathcal{P}_t(\mathbf{k}) \propto H^2$$

**order N Chebyshev
expansion, N-1 parameters
(e.g. nodal point values)**

$\ln \mathcal{E}_s$ (nodal 5) + 4 params. **Uniform in exp(nodal bandpowers) cf. uniform in nodal bandpowers** reconstructed from April07 CMB+LSS data using Chebyshev nodal point expansion & MCMC: shows prior dependence with current data

File: lnepsilon5_compensate_minus : Jul 2 19:35 2007

File: lnepsilon5_cont2 : Jul 2 19:36 2007



$$\mathcal{P}_s(k) \propto H^2 / \epsilon, \mathcal{P}_t(k) \propto H^2$$

Pirsa: 07090050

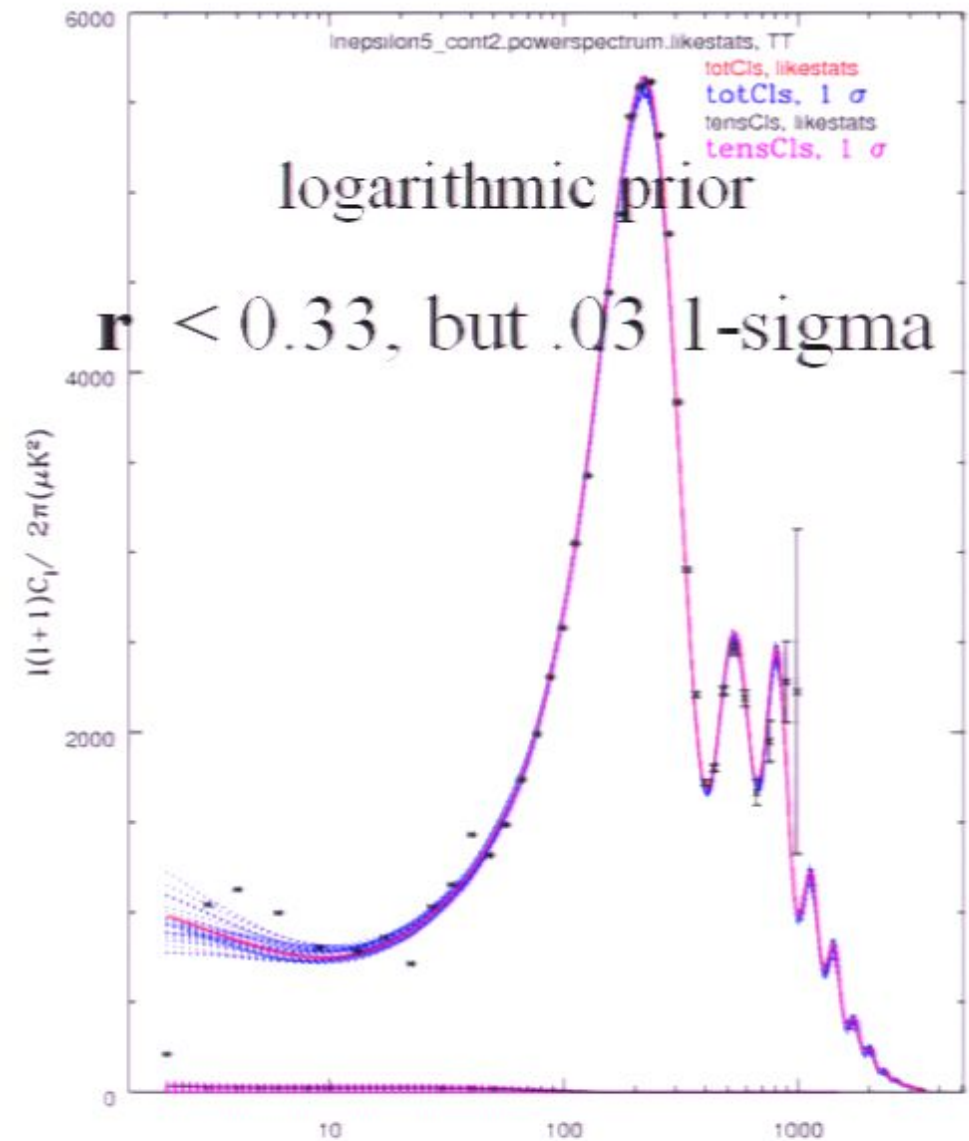
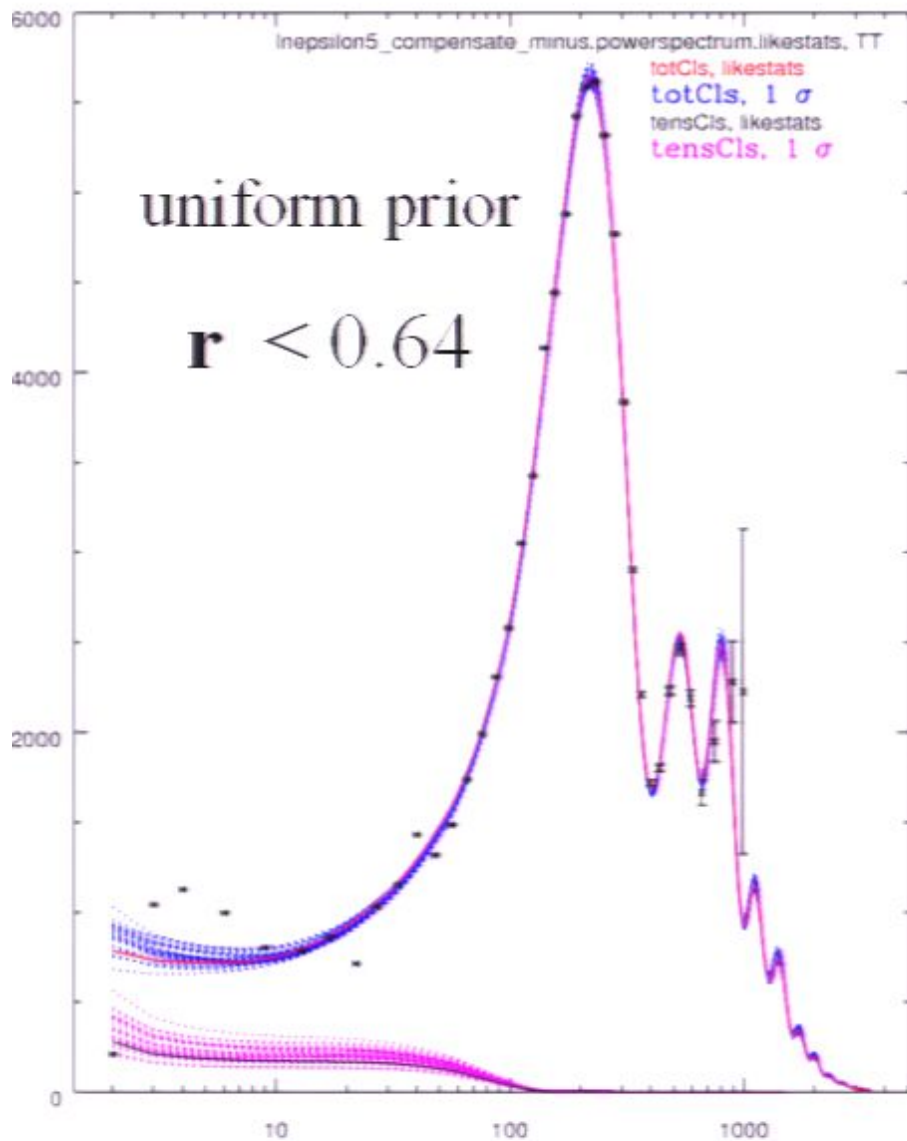
$$\frac{-\epsilon}{1-\epsilon} = \frac{d \ln H}{d \ln k}$$

$$\frac{dz_{inf}}{d \ln k} = \frac{\pm \sqrt{V}}{1}$$

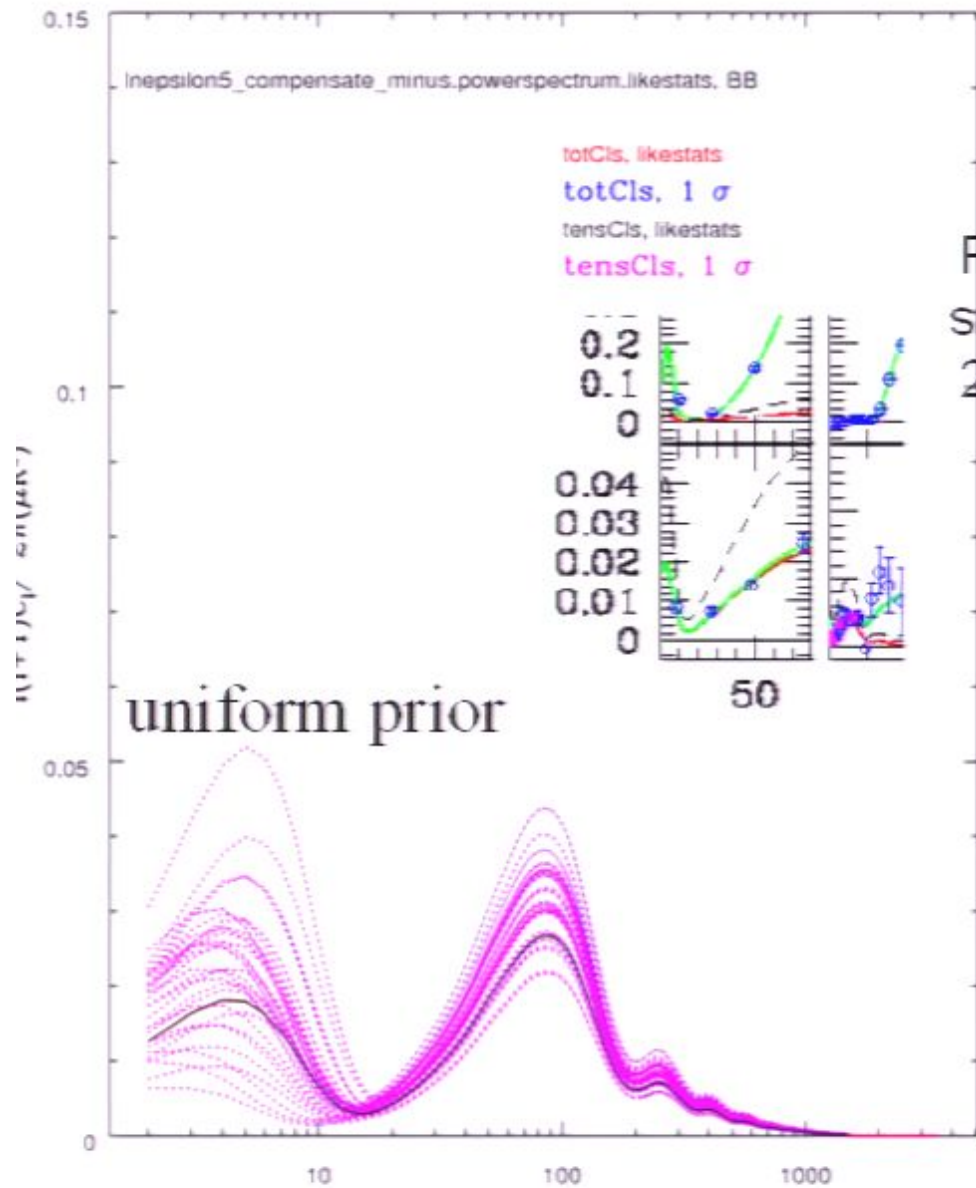
$$\epsilon = \left(\frac{d \ln H}{d \ln k} \right)^2$$

$$V \propto H^2 \left(1 - \frac{\epsilon}{2} \right)$$

$\ln \mathcal{E}_s$ (nodal 5) + 4 params. Uniform in $\exp(\text{nodal bandpowers})$ cf. uniform in nodal bandpowers reconstructed from April07 CMB+LSS data using Chebyshev nodal point expansion & MCMC: shows prior dependence with current data



C_L BB for $\ln \mathcal{E}_s$ (nodal 5) + 4 params inflation trajectories reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC

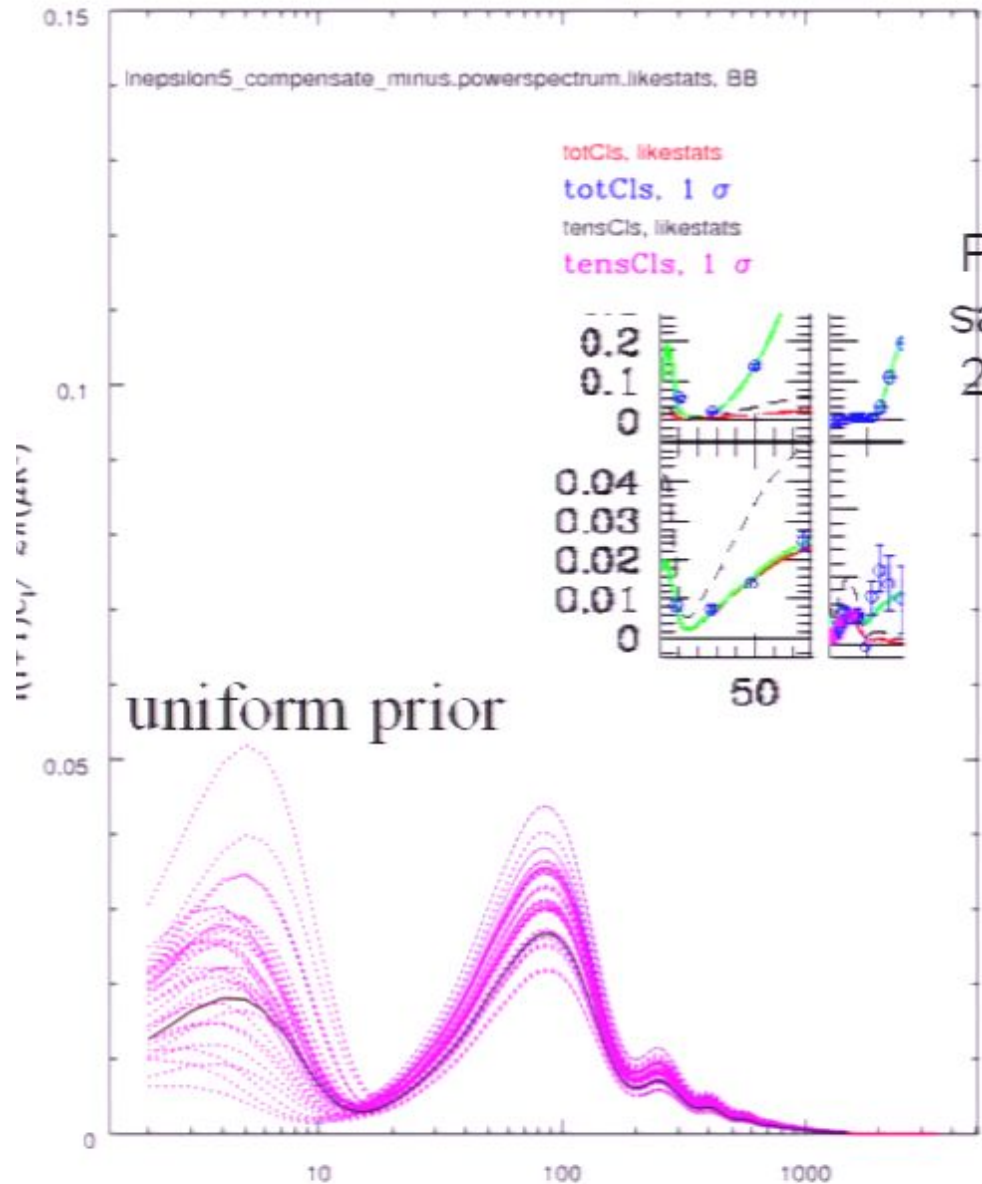


Planck satellite
2008.6

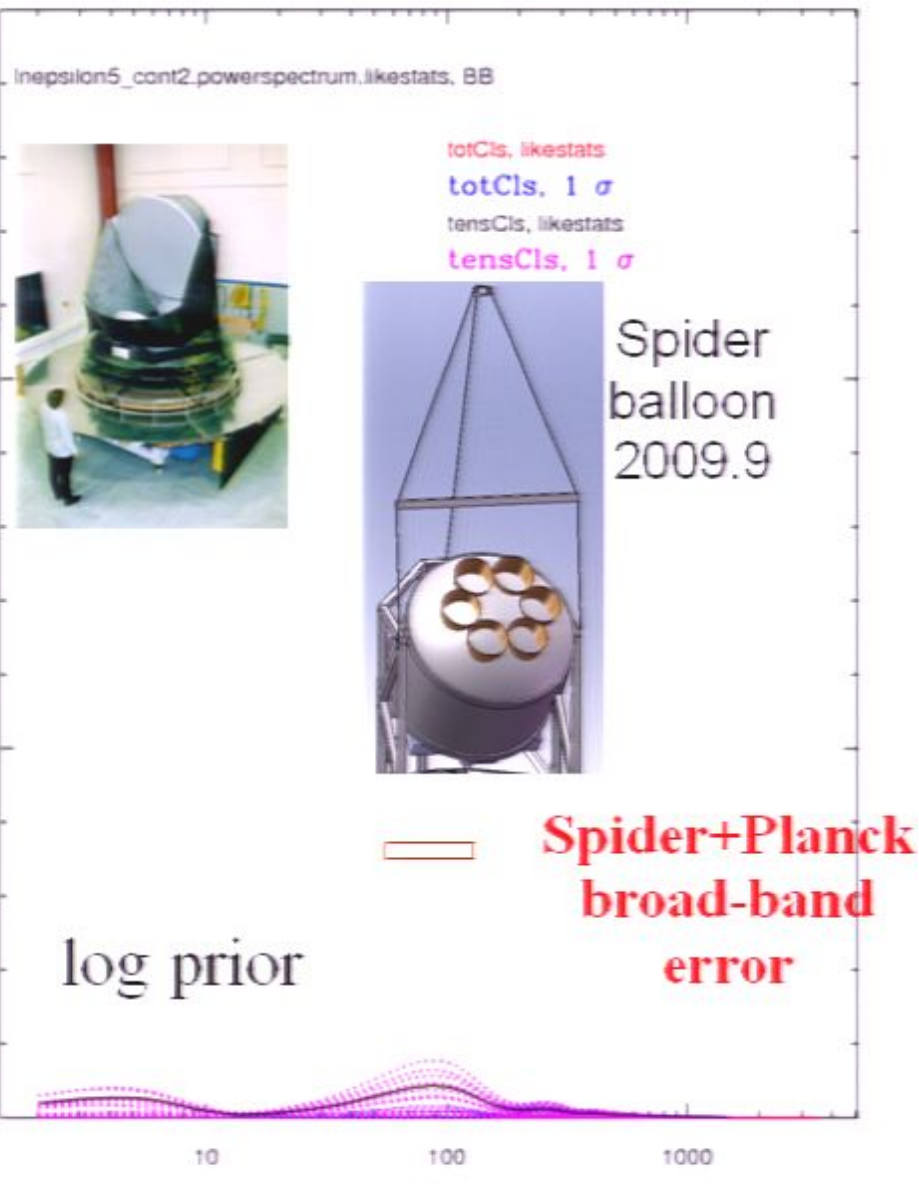
$l(l+1)C_l / 2\pi (\mu K^2)$



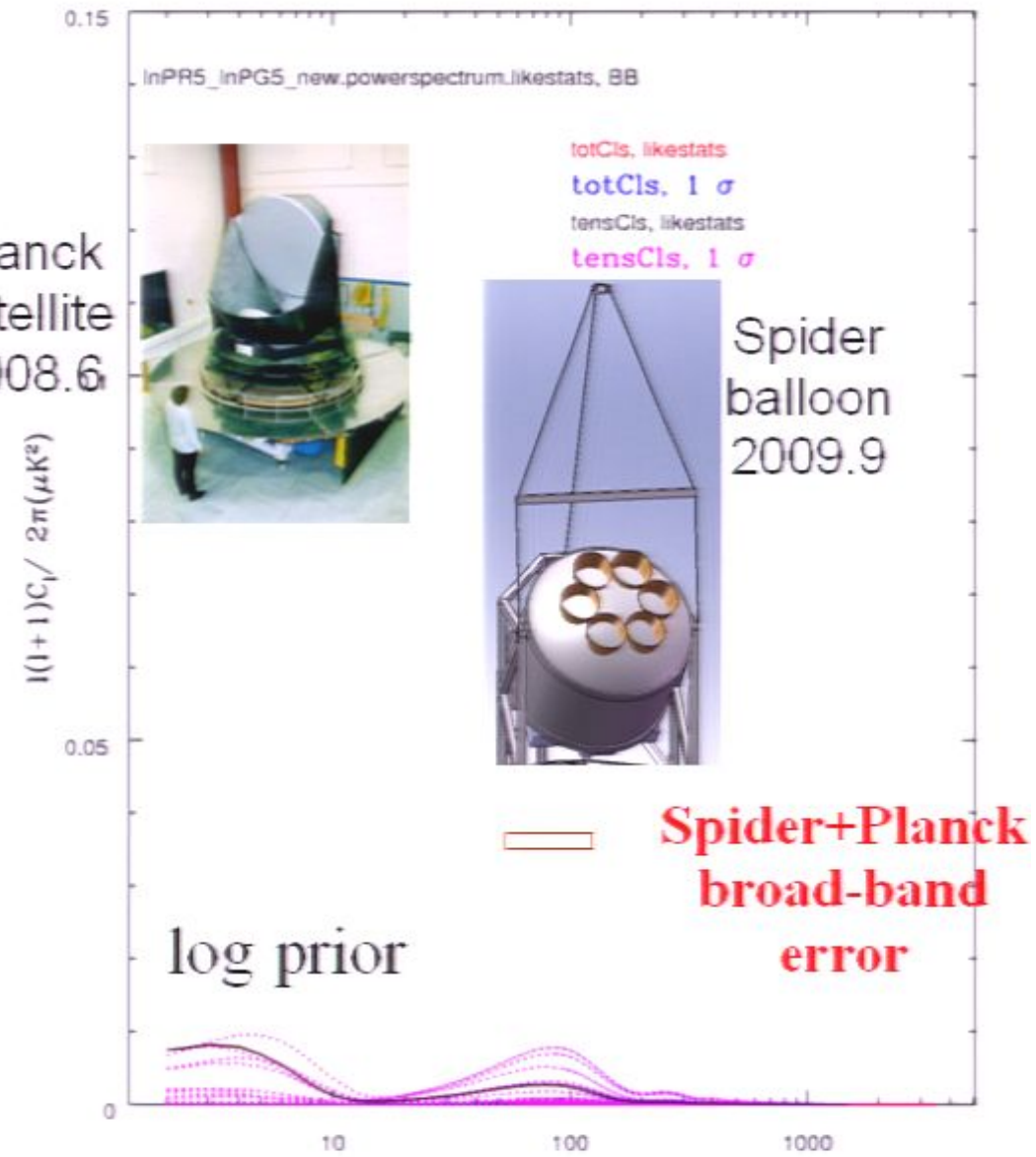
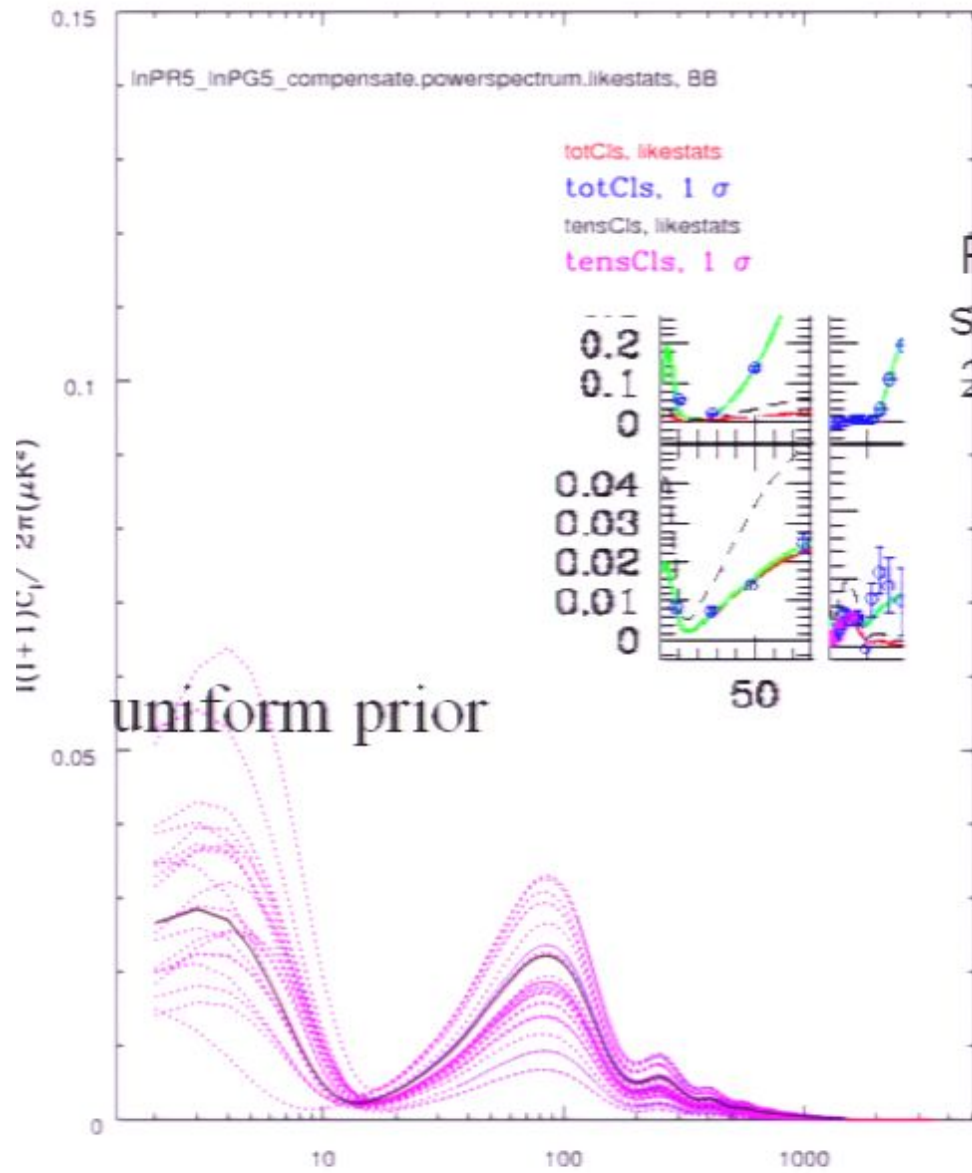
C_L BB for $\ln \mathcal{E}_s$ (nodal 5) + 4 params inflation trajectories reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC



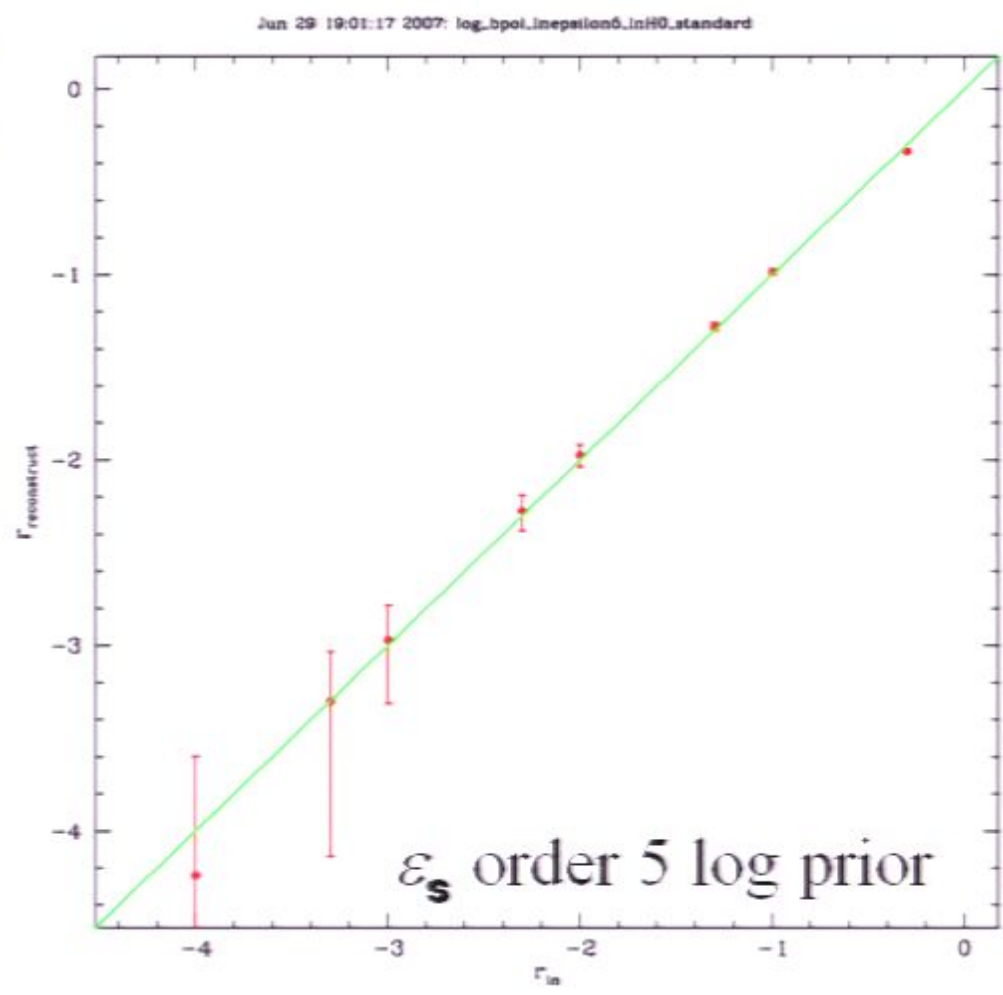
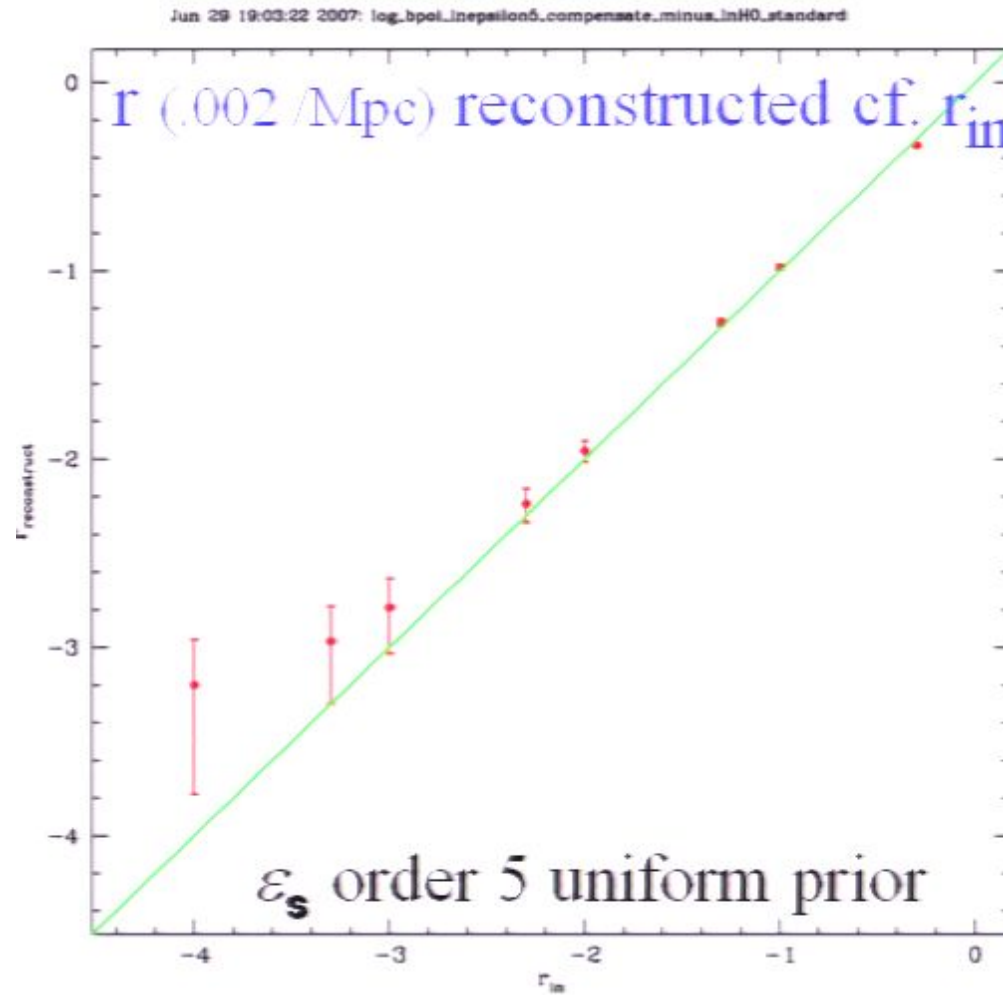
Planck satellite
2008.6



C_L BB for $\ln P_s \ln P_t$ (nodal 5 and 5) + 4 params inflation trajectories reconstructed from CMB+LSS data using Chebyshev nodal point expansion & MCMC



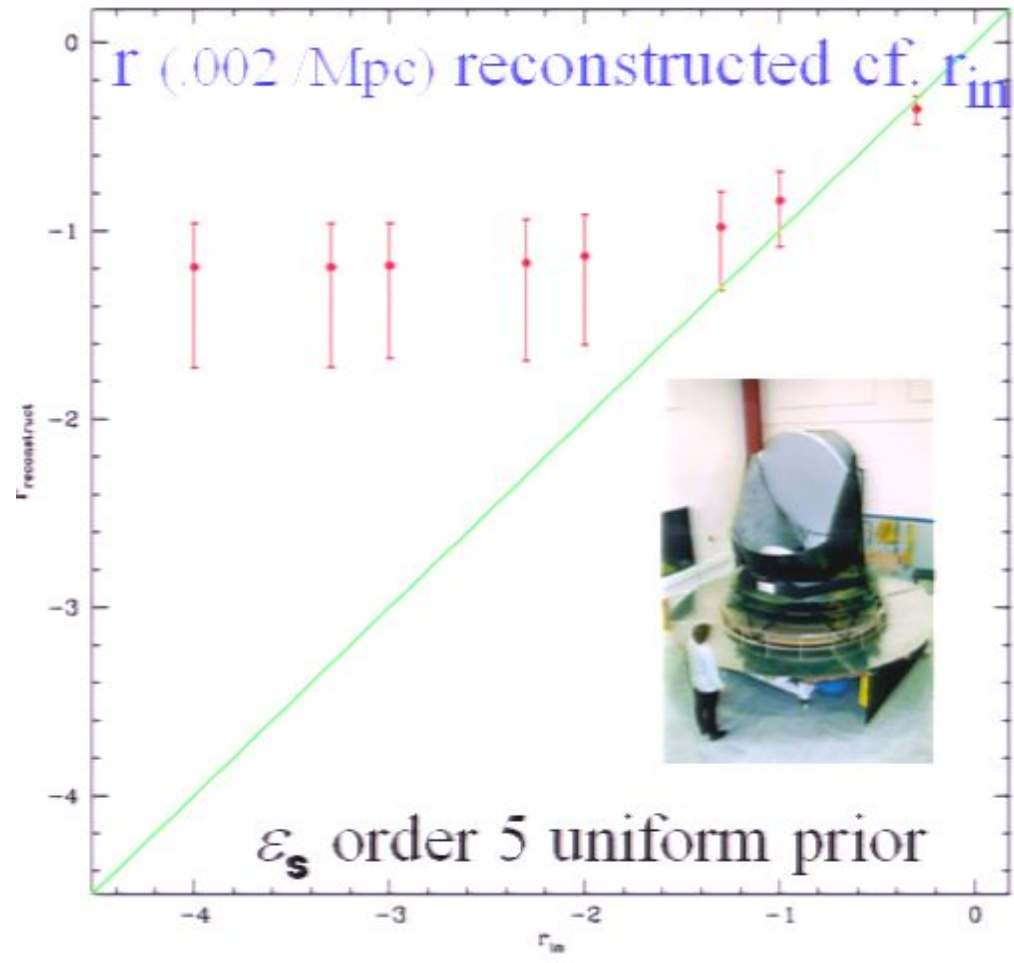
B-pol simulation: input LCDM (Acbar)+run+uniform tensor



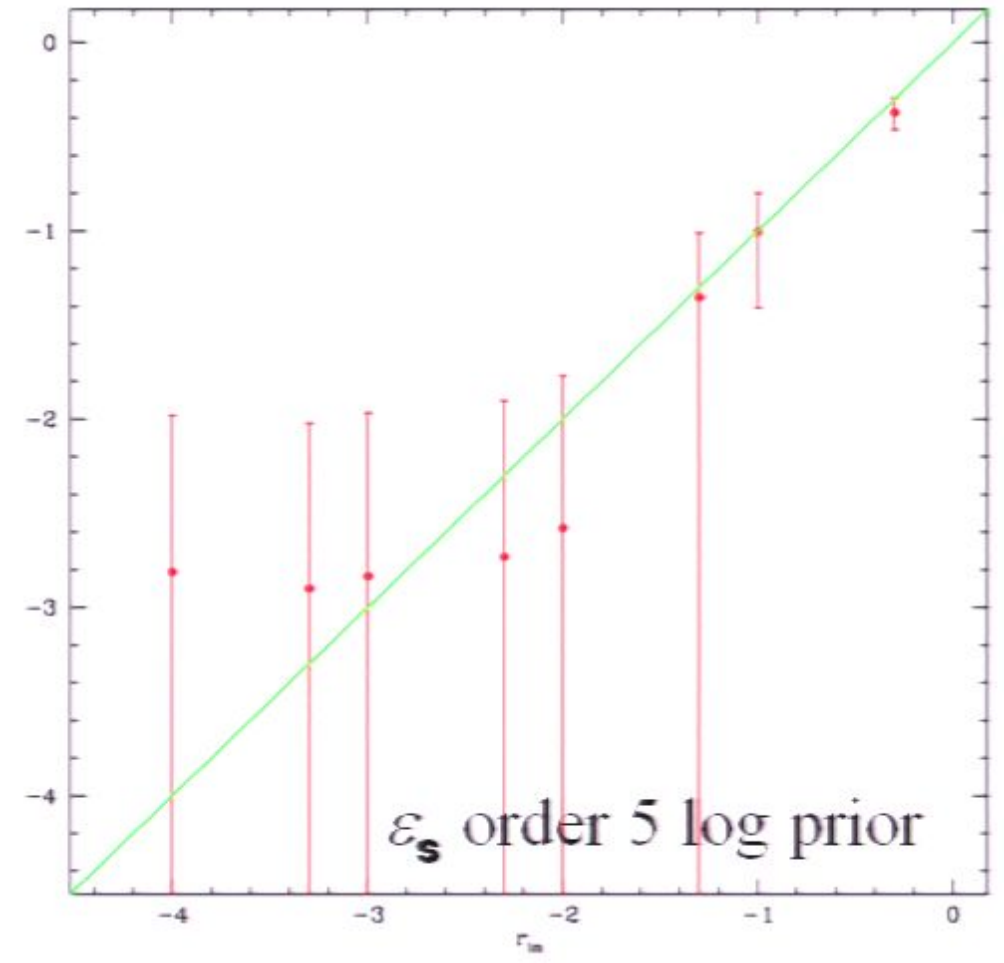
Pirsa: 07090050 a very stringent test of the ϵ -trajectory methods: A+

Planck 1 yr simulation: input LCDM (Acbar)+run+uniform tensor

Jun 29 19:03:06 2007: log_planck_inepsilon5_compensate_minus_inH0_standard



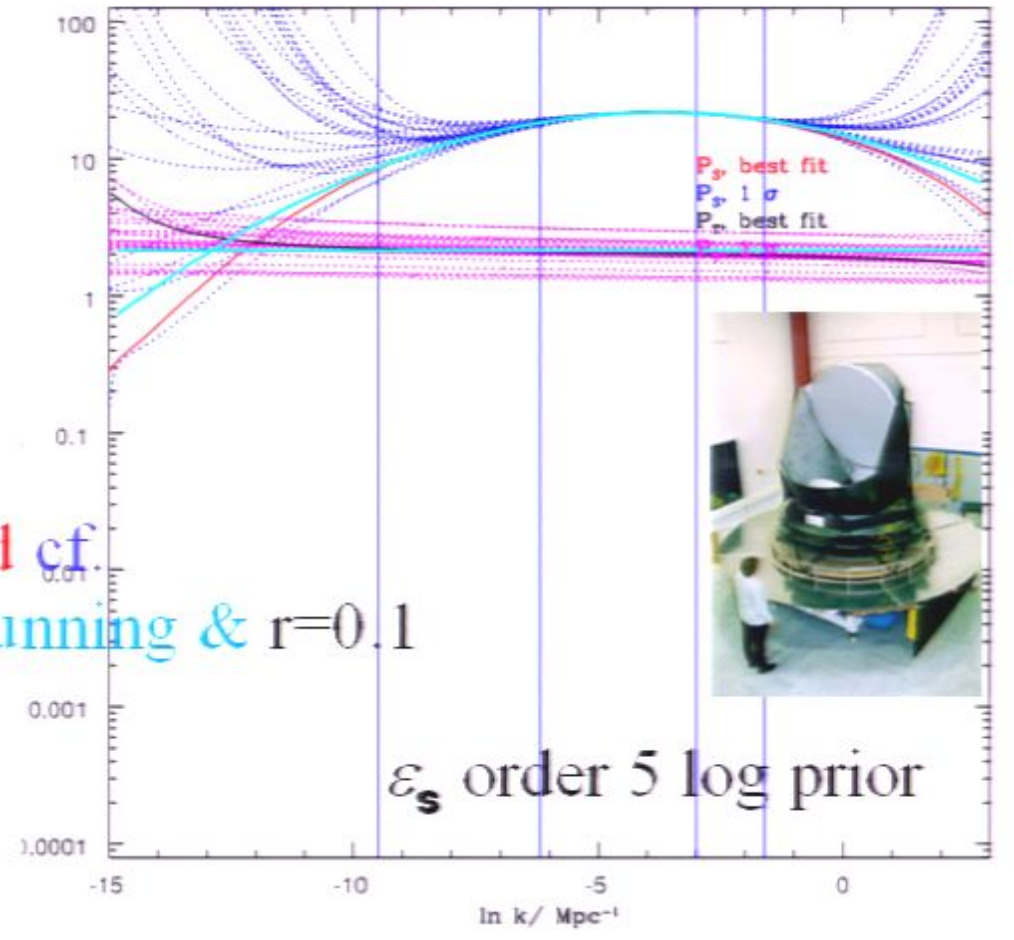
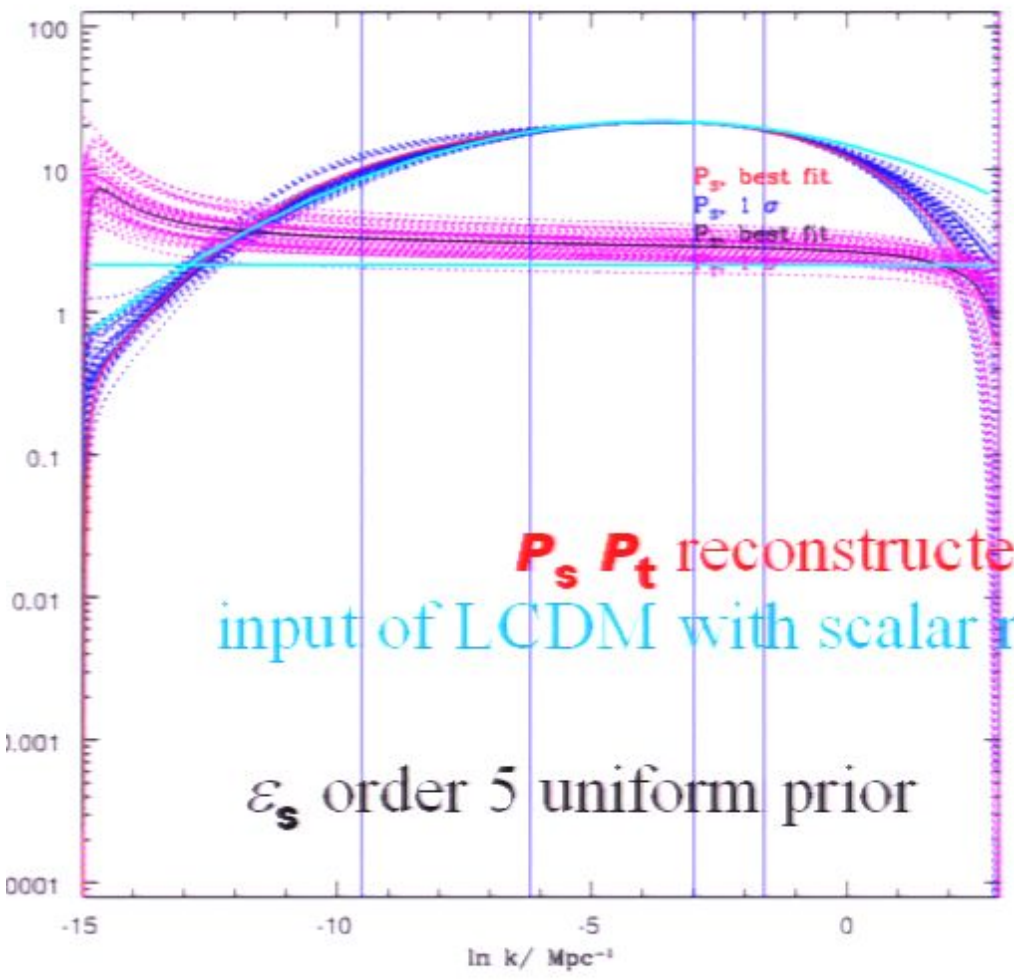
Jun 29 19:01:03 2007: log_planck_inepsilon5_inH0_standard



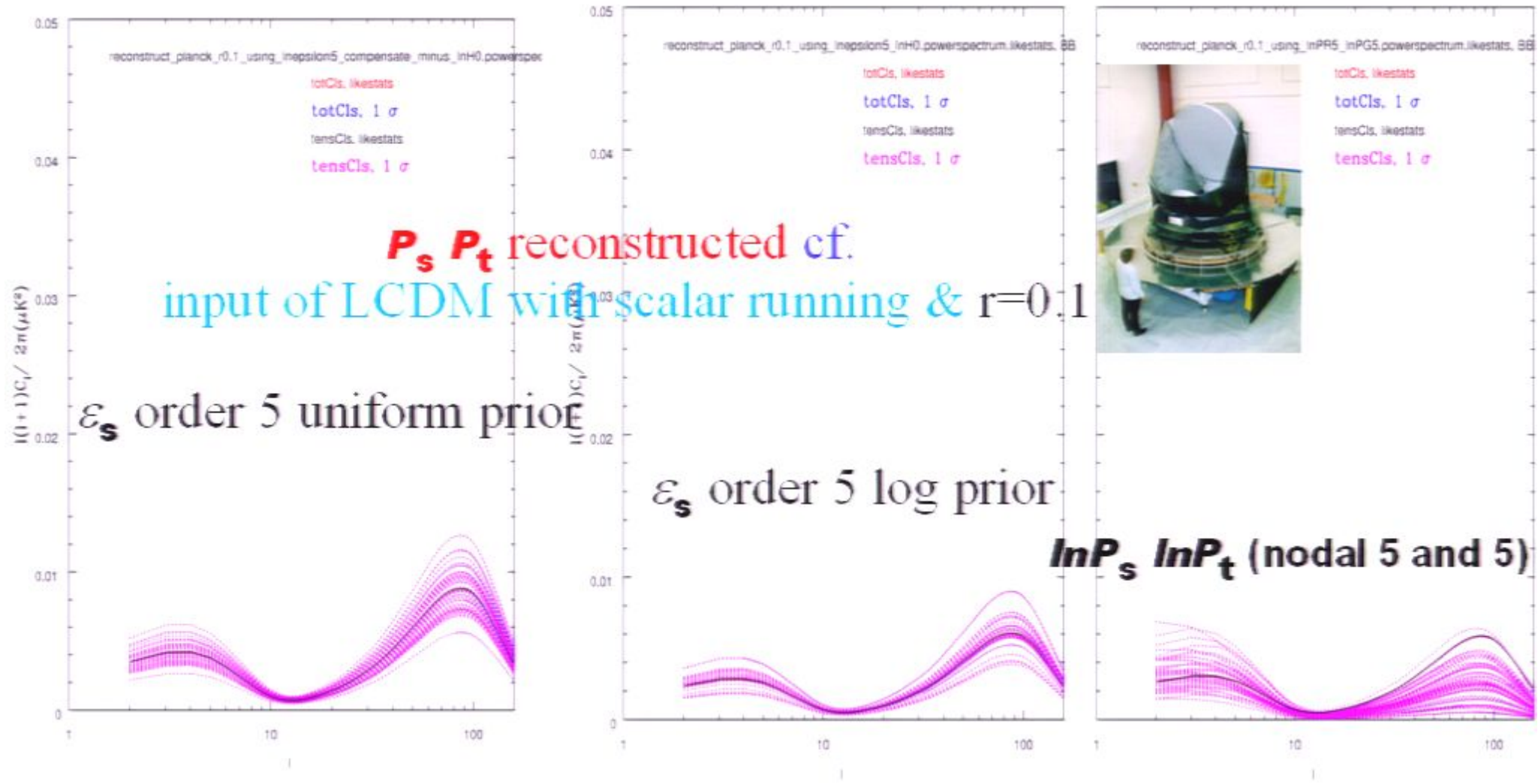
Planck1 simulation: input LCDM (Acbar)+run+uniform tensor

File: reconstruct_planckr0.1_using_ineps : Jul 2 19:07 2007

File: reconstruct_planckr0.1_using_ineps : Jul 2 19:01 2007



Planck1 simulation: input LCDM (Acbar)+run+uniform tensor



Inflation then summary

the basic 6 parameter model with no GW allowed fits all of the data OK

Usual GW limits come from adding r with a fixed GW spectrum and no consistency criterion (7 params). Adding minimal consistency does not make that much difference (7 params)

($<.28$ 95%) limit comes from relating high k region of σ_8 to low k region of GW C_L

Uniform priors in $\epsilon(k) \sim r(k)$: with current data, the scalar power downturns ($\epsilon(k)$ goes up) at low k if there is freedom in the mode expansion to do this. Adds GW to compensate, **breaks old r limit**. T/S (k) can cross unity. **But log prior in ϵ drives to low r . a B-pol could break this prior dependence, maybe Planck+Spider.**

Complexity of trajectories arises in many-moduli string models. Roulette example: 4-cycle complex Kahler moduli in large compact volume Type IIB string theory

TINY $r \sim 10^{-10}$ if the normalized inflaton $\psi < 1$ over ~ 50 e-folds then $r < .007$
 $\Delta\psi \sim 10$ for power law & PNOB inflaton potentials

Prior probabilities on the inflation trajectories are crucial and cannot be decided at this time. Philosophy: be as wide open and least prejudiced as possible

Even with low energy inflation, the prospects are good with Spider and even Planck to either detect the GW-induced B-mode of polarization or set a powerful upper limit against nearly uniform acceleration. Both have strong Cdn roles. CMBpol

NOW

3-parameter parameterization

$$\begin{aligned}
 w(a) = & -1 + \frac{2\epsilon_s}{3} \left\{ \frac{\left(\frac{a_s}{a}\right)^{3-3.6a_s|\epsilon_s|(1-\Omega_{m0})}}{\sqrt{1 + \frac{\epsilon_s}{3|\epsilon_s|} \left(\frac{a_s}{a}\right)^{6-7.2a_s|\epsilon_s|(1-\Omega_{m0})}}} \frac{1}{\sqrt{|\epsilon_s|}} \right. \\
 & + \left[\sqrt{1 + \left(\frac{a_{eq}}{a}\right)^3} - \left(\frac{a_{eq}}{a}\right)^3 \ln\left(\left(\frac{a}{a_{eq}}\right)^{\frac{3}{2}} + \sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3}\right) \right] (1 - \zeta_s) \\
 & + 0.36\epsilon_s(1 - \Omega_{m0}) \frac{\left(\frac{a}{a_{eq}}\right)^2}{1 + \left(\frac{a}{a_{eq}}\right)^4} \left[0.9 - 0.7\frac{a}{a_{eq}} - 0.045\left(\frac{a}{a_{eq}}\right)^2 \right] \\
 & \left. + \frac{2\zeta_s}{3} \left[\sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3} - 2\left(\frac{a_{eq}}{a}\right)^3 \left(\sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3} - 1 \right) \right] \right\}^2
 \end{aligned}$$

where

$$a_{eq} \equiv \left(\frac{\Omega_{m0}}{1 - \Omega_{m0}} \right)^{\frac{1}{3[1 - 0.36\epsilon_s(1 - \Omega_{m0})]}}$$

$$a_s \geq 0$$

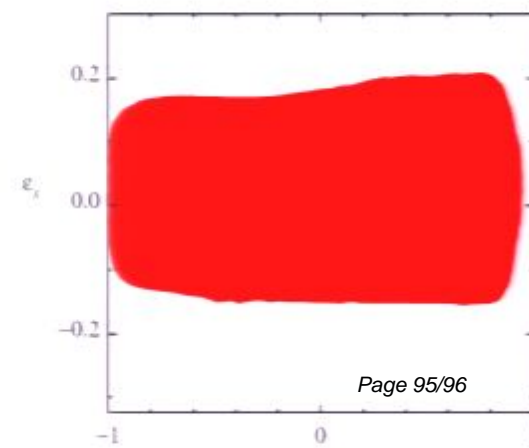
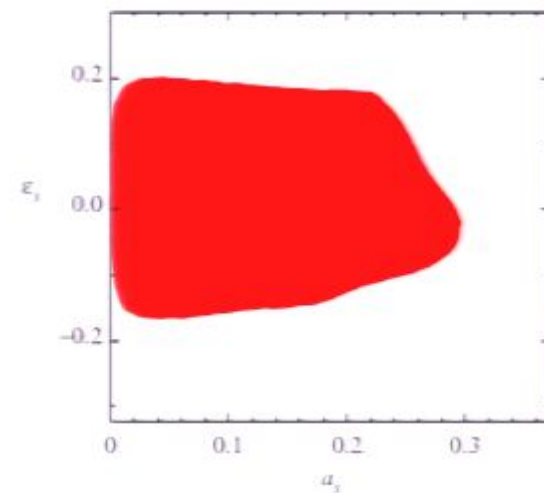
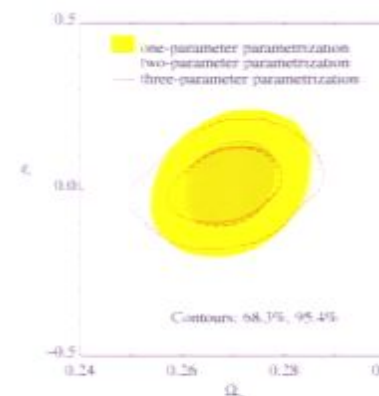
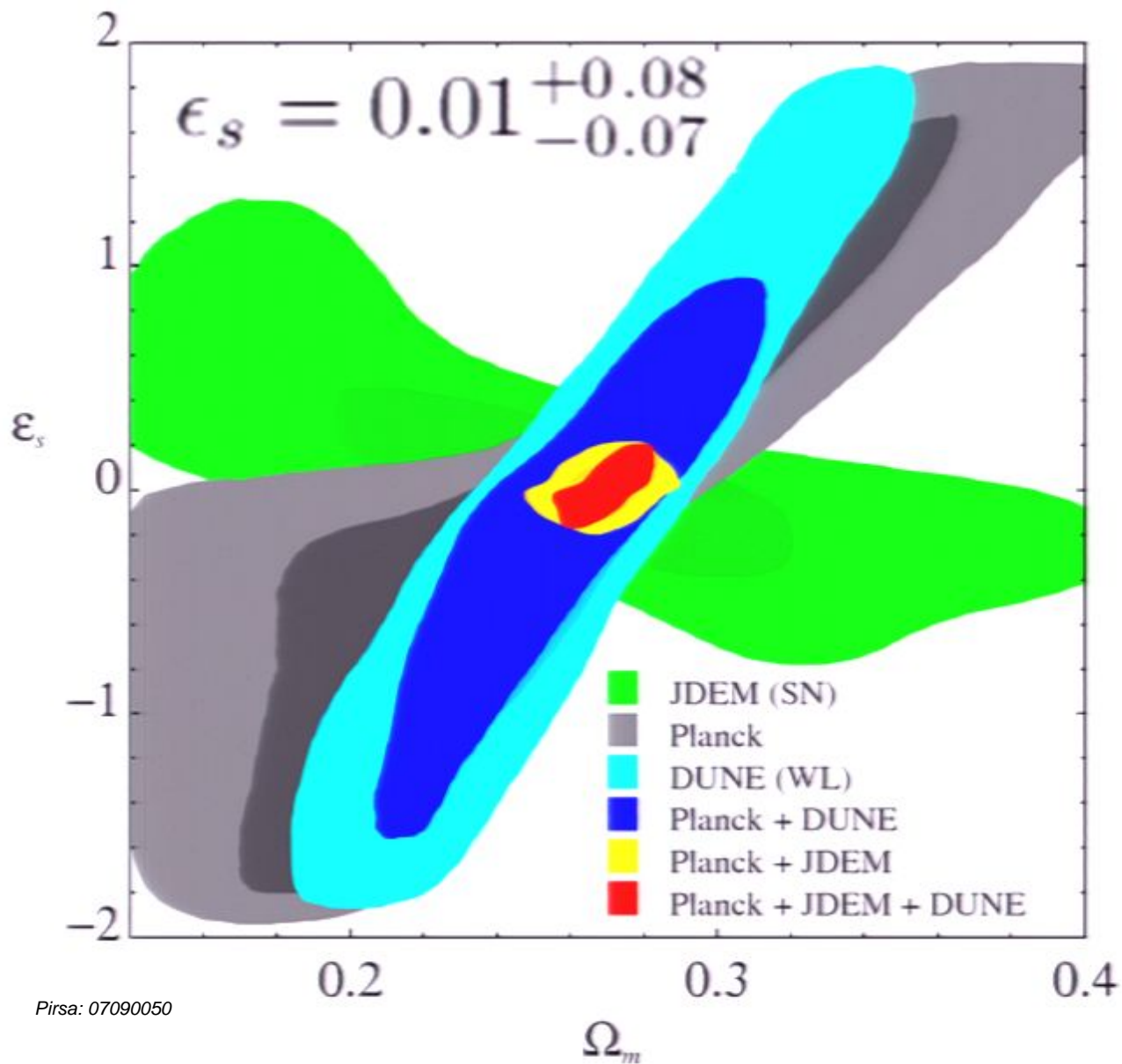
$$-1 < \zeta_s < 1$$

Beyond Einstein panel: LISA+JDEM

Forecast: **JDEM-SN** (2500 hi-z + 500 low-z)

+ **DUNE-WL** (50% sky, gals @z = 0.1-1.1, 35/min²) +

Planck1.4



Inflation now summary

the data cannot determine more than 2 w -parameters (+ c_{sound} ?). general higher order Chebyshev expansion in $1+w$ as for “inflation-then” $\varepsilon=(1+q)$ is not that useful. **Parameter eigenmodes** show what is probed

The $w(a)=w_0+w_a(1-a)$ phenomenology requires baroque potentials

Philosophy of HBK07: **backtrack from now ($z=0$) all w -trajectories arising from quintessence ($\varepsilon_s > 0$) and the phantom equivalent ($\varepsilon_s < 0$); use a 3-parameter model to well-approximate even rather baroque w -trajectories.** We ignore constraints on Q -density from photon-decoupling and BBN because further trajectory extrapolation is needed.

For **general slow-to-moderate rolling one needs 2 “dynamical parameters”** (a_s, ε_s) & Ω_Q to describe w to a few % for the not-too-baroque w -trajectories.

a_s is not well-determined by the current data: to ± 0.3 in Planck1yr-CMB+JDEM-SN+DUNE-WL future

In the early-exit scenario, the information stored in a_s is erased by Hubble friction over the observable range & w can be described by a single parameter ε_s .

a 3rd param $\zeta_s, (\sim d\varepsilon_s/d\ln a)$ is ill-determined now & in a Planck1yr-CMB+JDEM-SN+DUNE-WL future

To use: given V , compute trajectories, do a -averaged ε_s & test (or simpler ε_s -estimate)

for each given Q -potential, velocity, amp, shape parameters are needed to define a w -trajectory

current observations are well-centered around the cosmological constant $\varepsilon_s=0.0\pm 0.25$

in Planck1yr-CMB+JDEM-SN+DUNE-WL future ε_s to ± 0.08

but cannot reconstruct the quintessence potential, just the slope ε_s & hubble drag info

Aside: detailed results depend upon the SN data set used. Best available used here (192 SN), soon CFHT SNLS ~ 300 SN + ~ 100 non-CFHTLS. will put all on the same analysis/calibration footing – very important.

Newest CFHTLS Lensing data is important to narrow the range over just CMB and SN