

Title: Structure Formation in Dark and Luminous Matter

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Abstract:

# Outline

## I: Mapping Structure on Large Scales

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[III: Understanding the Dynamics of Non-linear Structure Formation]

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IV: CDM versus Modified Gravity

# I: Mapping Structure on Large Scales: The Quest for Precision

# Gravitational Lensing

For 2-D distribution of mass, deflection of ray from object at (2-D vector) position  $\eta$  should be at  $\beta$ , instead seen at  $\theta$ :

$$\theta = \alpha(\theta) + \beta$$

where deflection angle  $\alpha$  is given

by:

$$\hat{\alpha}(\xi) = \frac{4G}{c^2} \int d^2\xi' \Sigma(\xi') \frac{\xi - \xi'}{|\xi - \xi'|^2}$$

or:

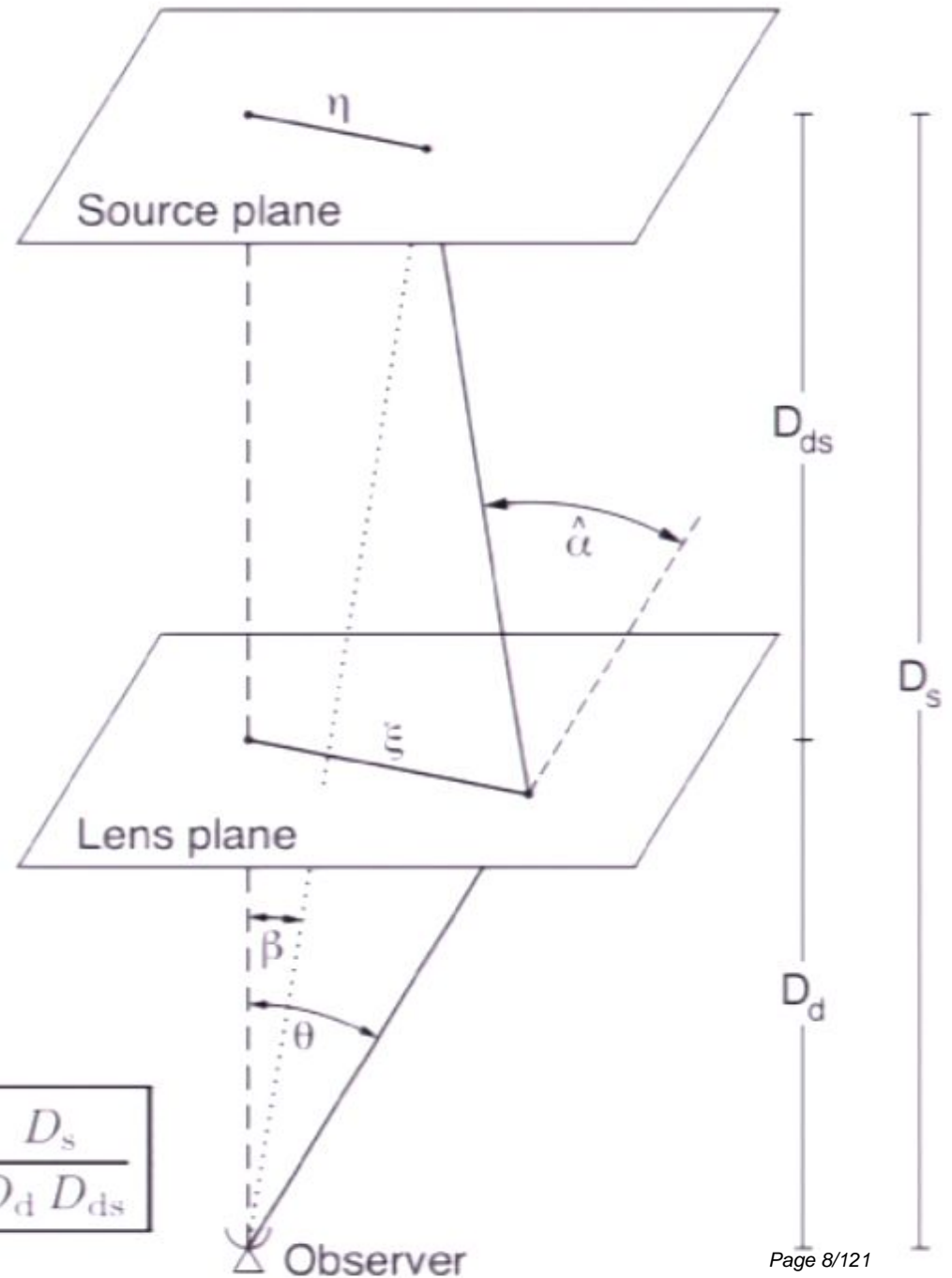
$$\alpha(\theta) = \frac{1}{\pi} \int_{\mathbb{R}^2} d^2\theta' \kappa(\theta') \frac{\theta - \theta'}{|\theta - \theta'|^2}$$

with convergence:

$$\kappa(\theta) := \frac{\Sigma(D_d \theta)}{\Sigma_{cr}}$$

with

$$\Sigma_{cr} = \frac{c^2}{4\pi G} \frac{D_s}{D_d D_{ds}}$$





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(systematic)



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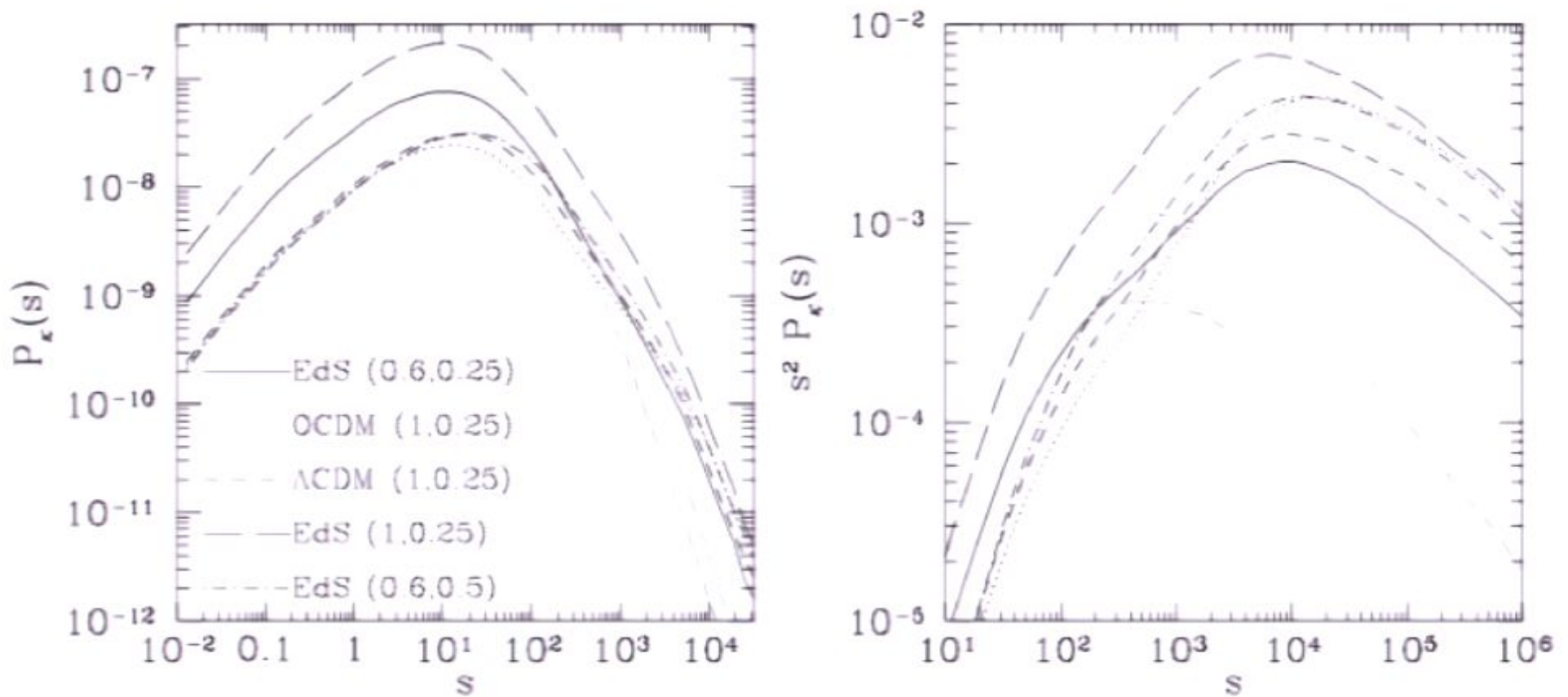
Redshift dependence of effect is very slow, producing a very broad kernel in redshift space:

$$\frac{4\pi G}{c^2} \int \frac{D_L D_{LS}}{D_S} \rho dl$$

# Simple-minded Example of an Application:

## Projected (Convergence/Surface Density) Power Spectrum

In principle, calculate kappa at each point, take Fourier transform and there you are:



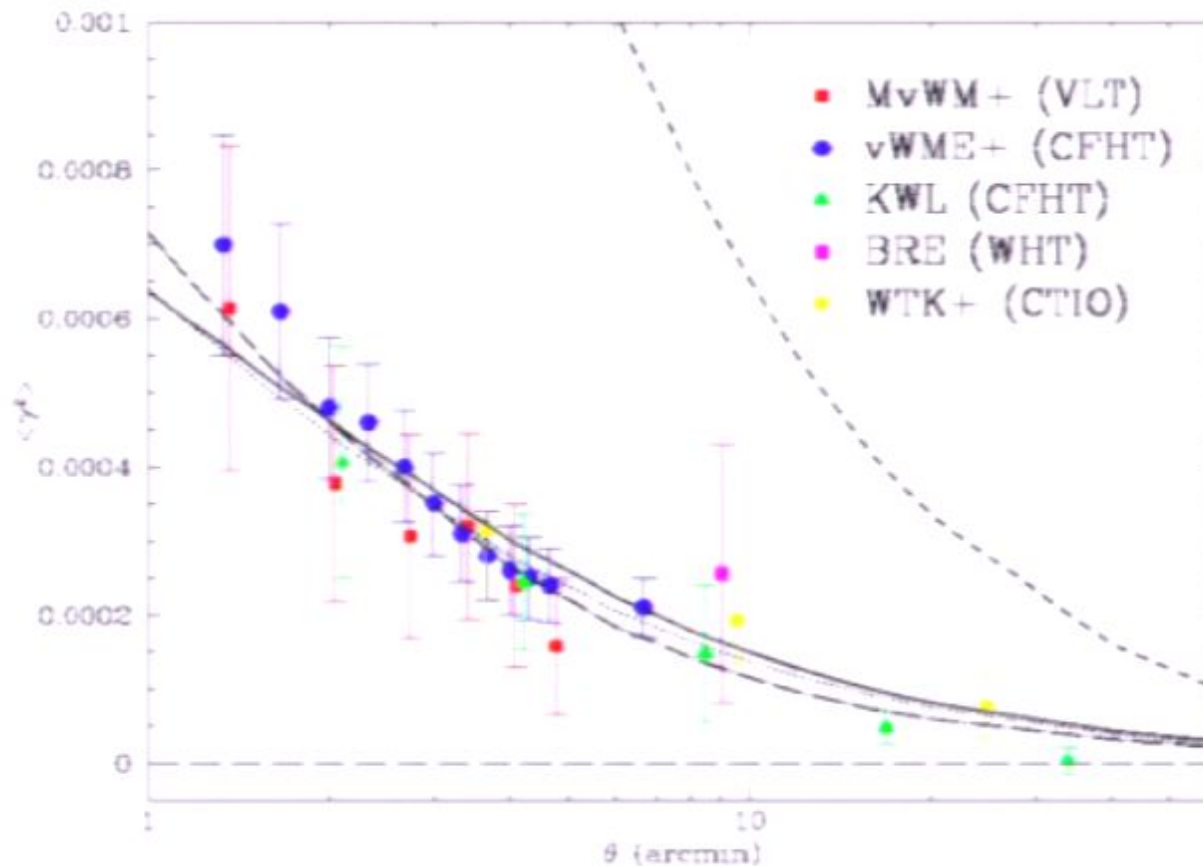


## More Sophisticated Examples:

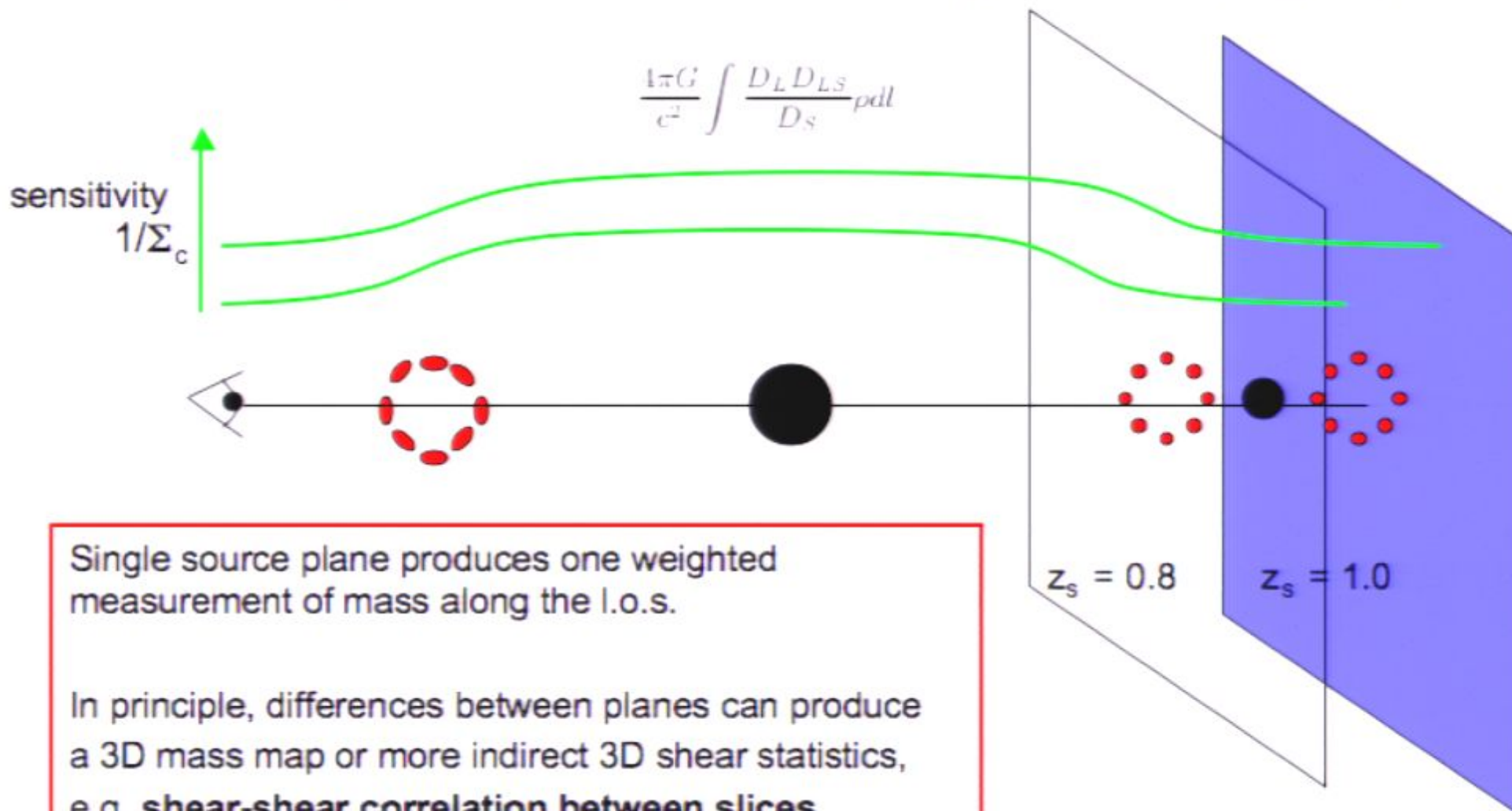
In practice, several other more practical measurements, e.g.

- 2-point shear correlation function
- mean shear dispersion
- aperture mass dispersion

which can be easier to measure and provide better sampling of the power spectrum



# Measuring Growth: 3D Lensing Tomography



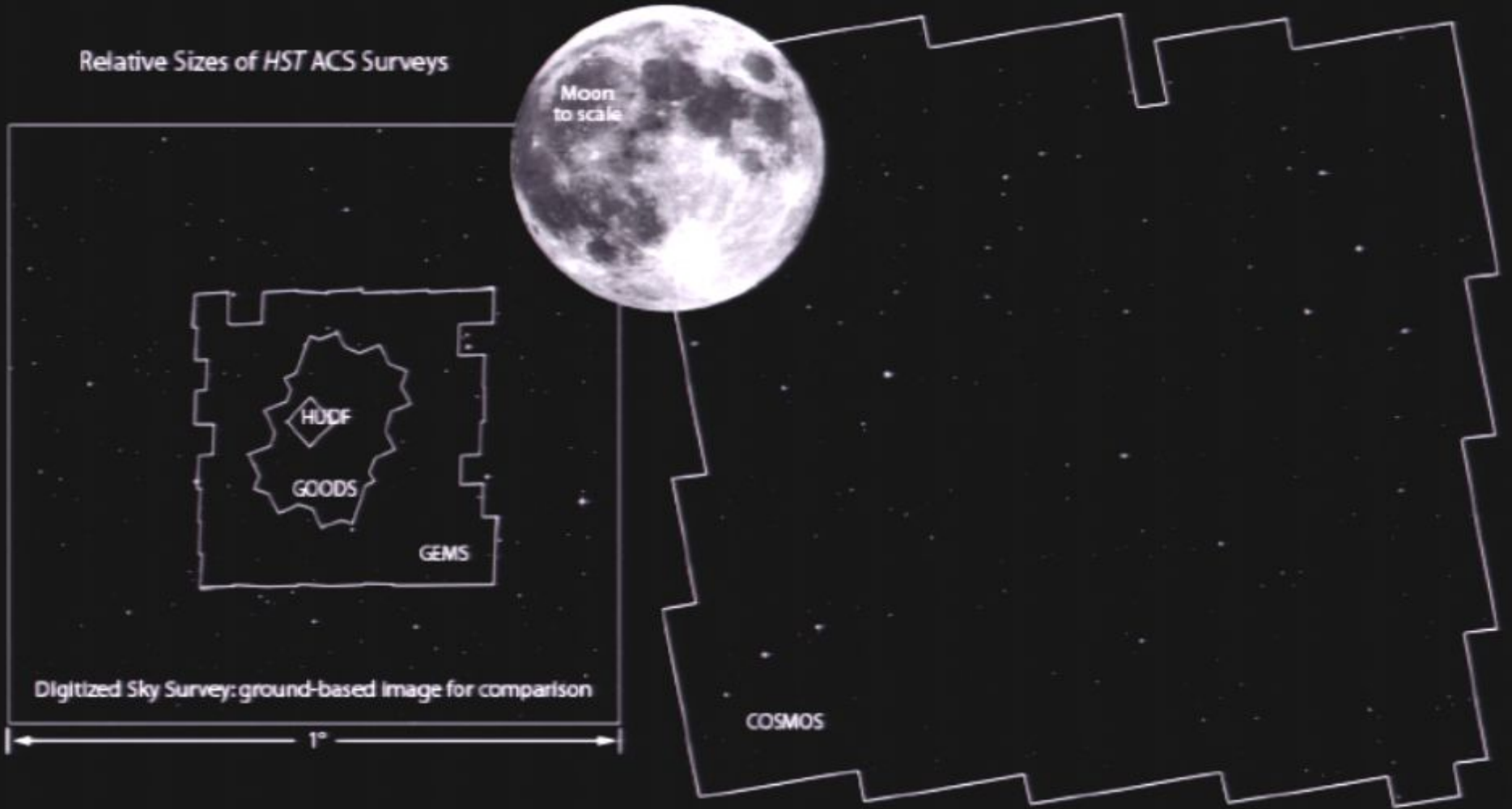
Single source plane produces one weighted measurement of mass along the l.o.s.

In principle, differences between planes can produce a 3D mass map or more indirect 3D shear statistics, e.g. **shear-shear correlation between slices**

Problems include extent of redshift kernel, inaccuracies in photo-zs

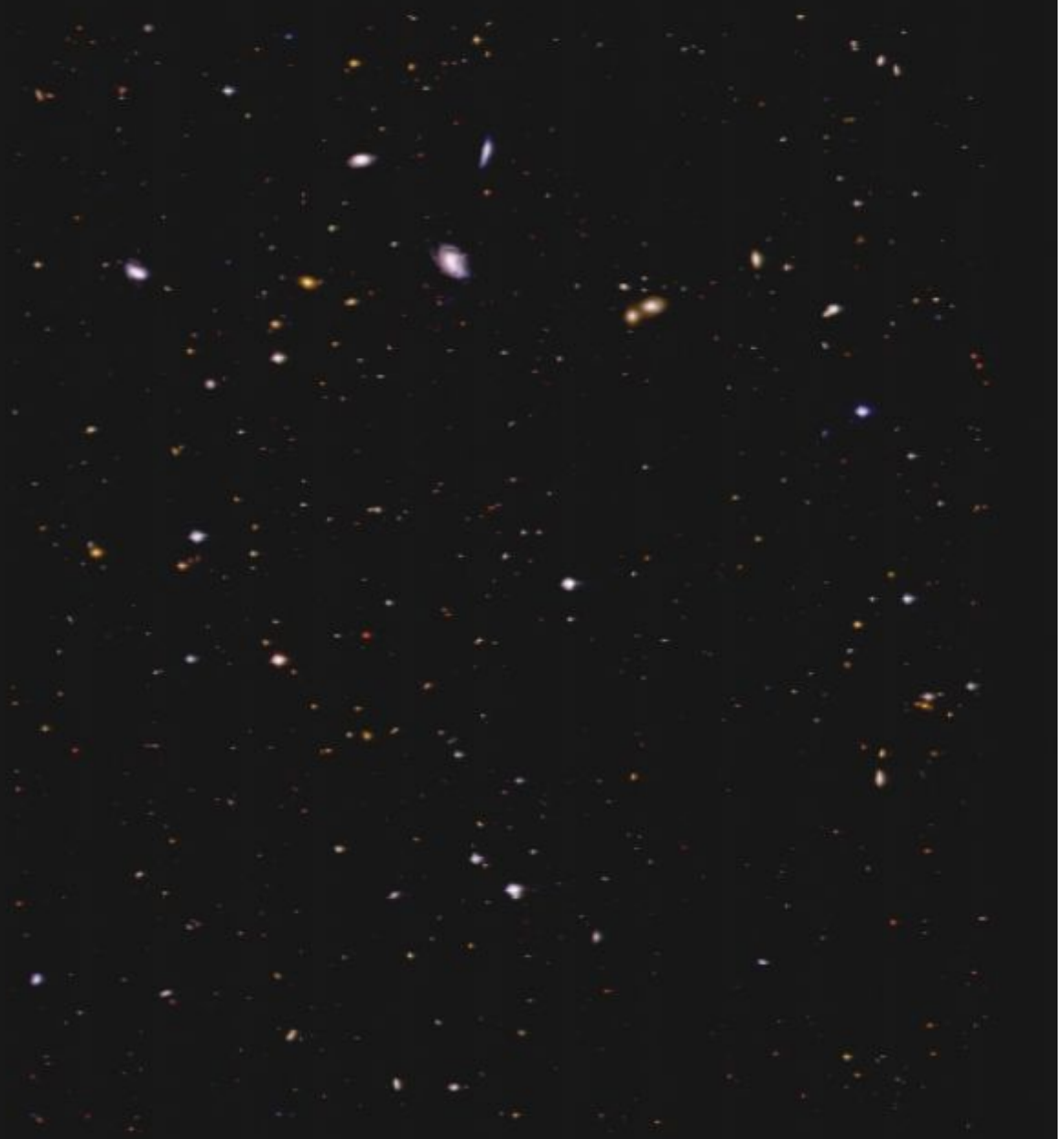
# The COSMOS Survey P.I. Nick Scoville

Relative Sizes of *HST* ACS Surveys



# The COSMOS Survey

- 2 square degree ACS mosaic
- current lensing results from 1.64 square degrees
- 2-3 million galaxies down to  $F814W_{AB} = 26.6$
- 15-band photometry, photo-zs with  $dz \sim 0.03(1+z)$  to  $z = 1.4$  and  $I_{F814W} = 24$
- follow-up in X-ray, radio, IR, UV



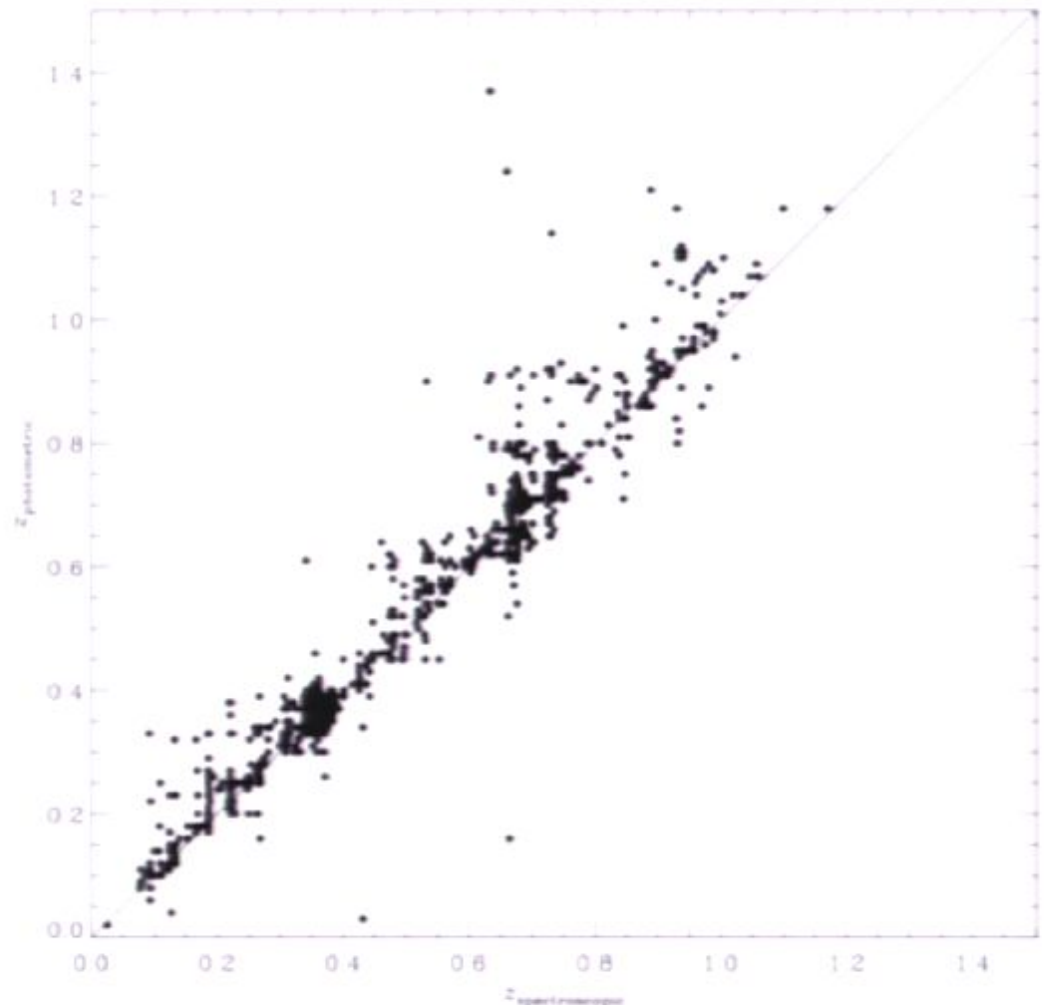
## Getting the 3rd dimension

Spectra ~1000x more expensive than images

Get approximate spectrum with  
multi-band photometry  
(COSMOS now up to 18 bands)

Can get redshift errors down to  
 $dz/(1+z) \sim 0.02$

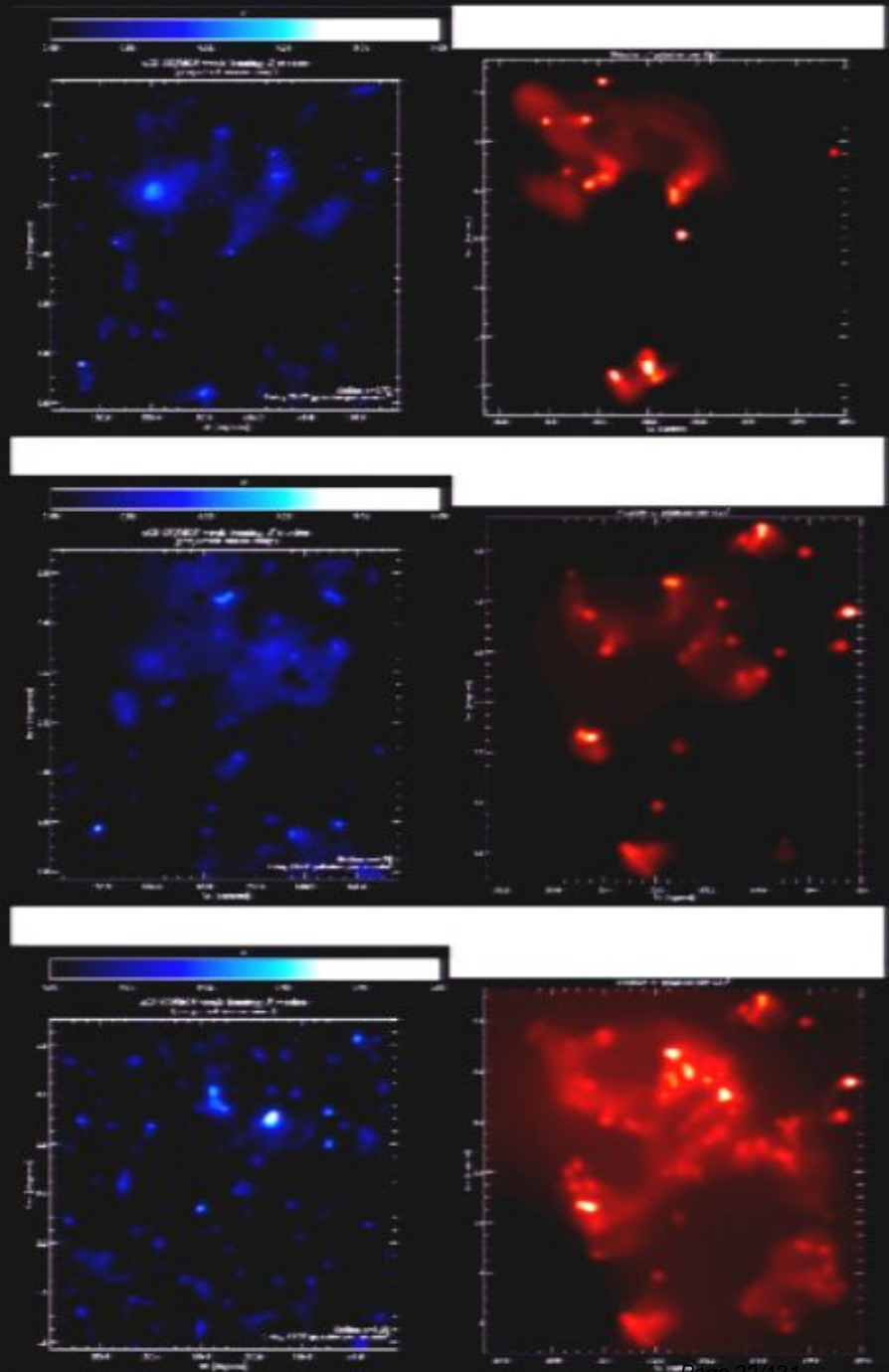
Lasting concern:  
catastrophic errors



# WL Convergence Maps

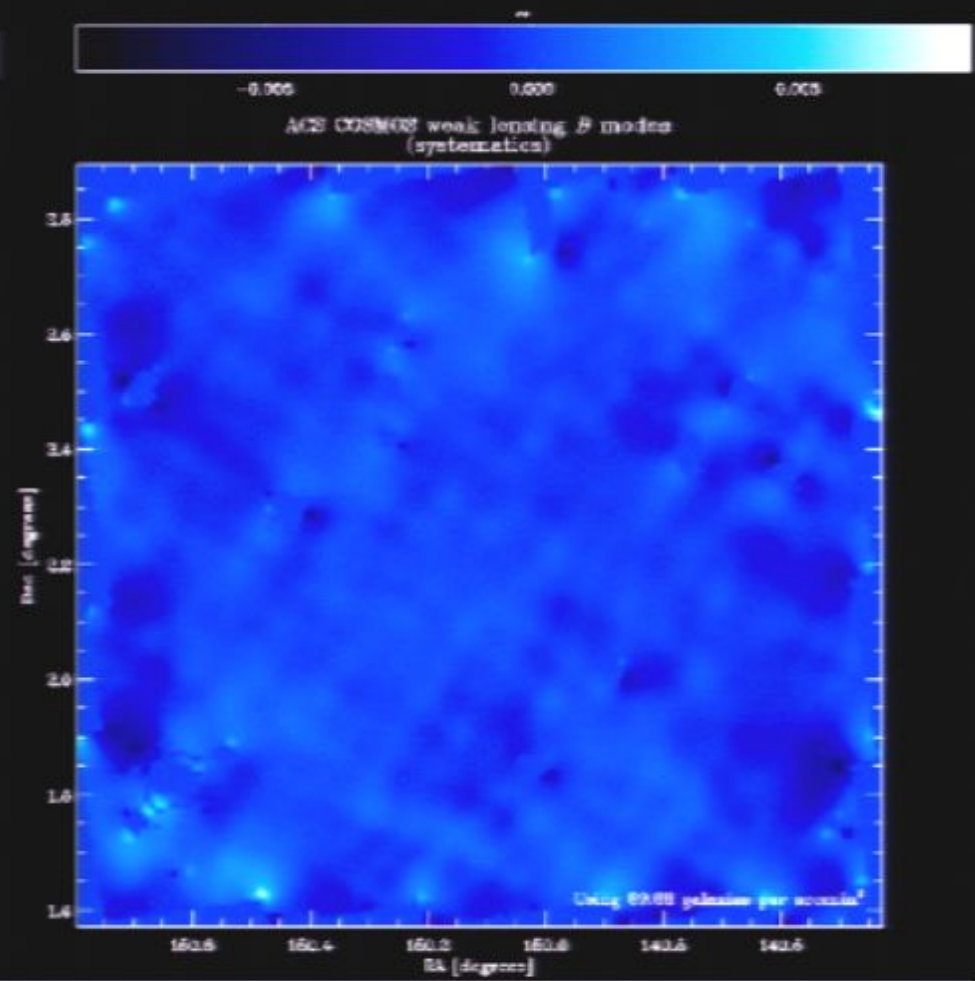
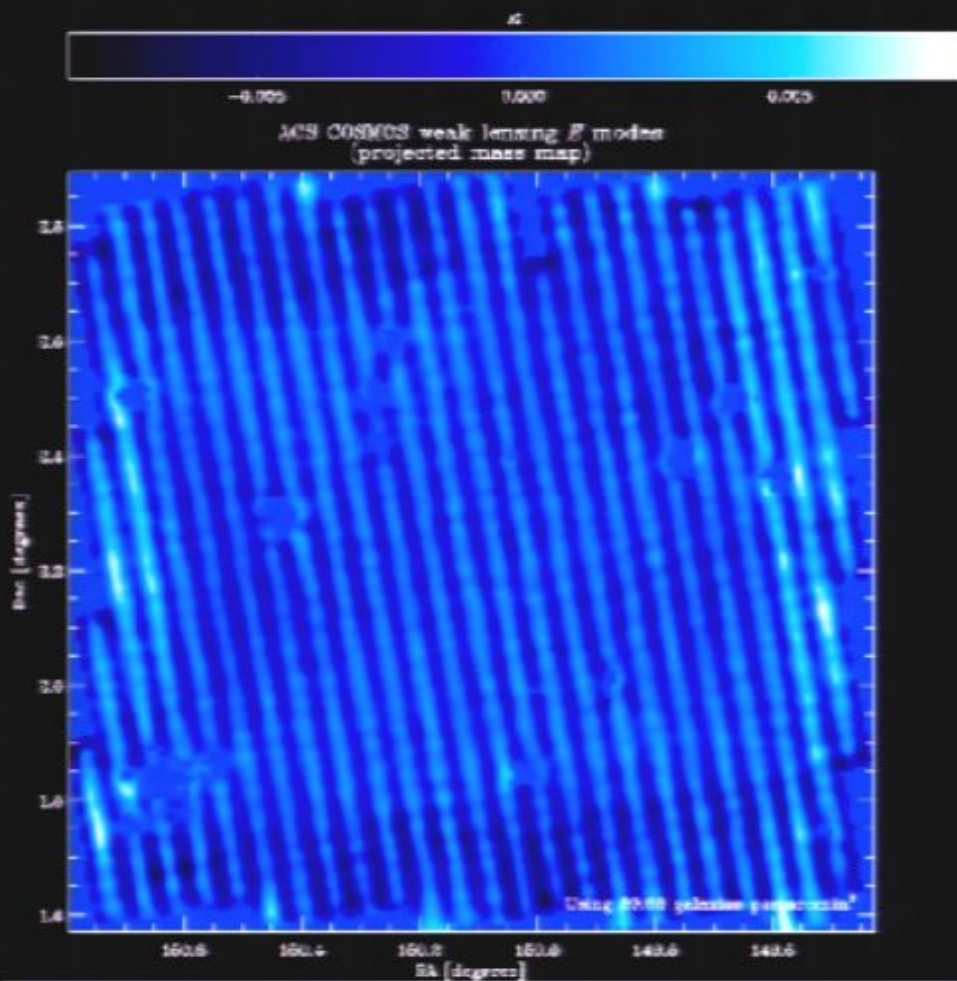
Massey, Rhodes, Leauthaud  
Capak, Koekemoer, Scoville, Refregier

- cut catalogue down to 40 galaxies/arcmin<sup>2</sup> to remove bad zs
- correct for PSF variations, CTE
- Get lensing maps, low-resolution 3D maps, various measures of power in 2D and restricted 3D
- results compare well with baryonic distributions (e.g. galaxy distribution)

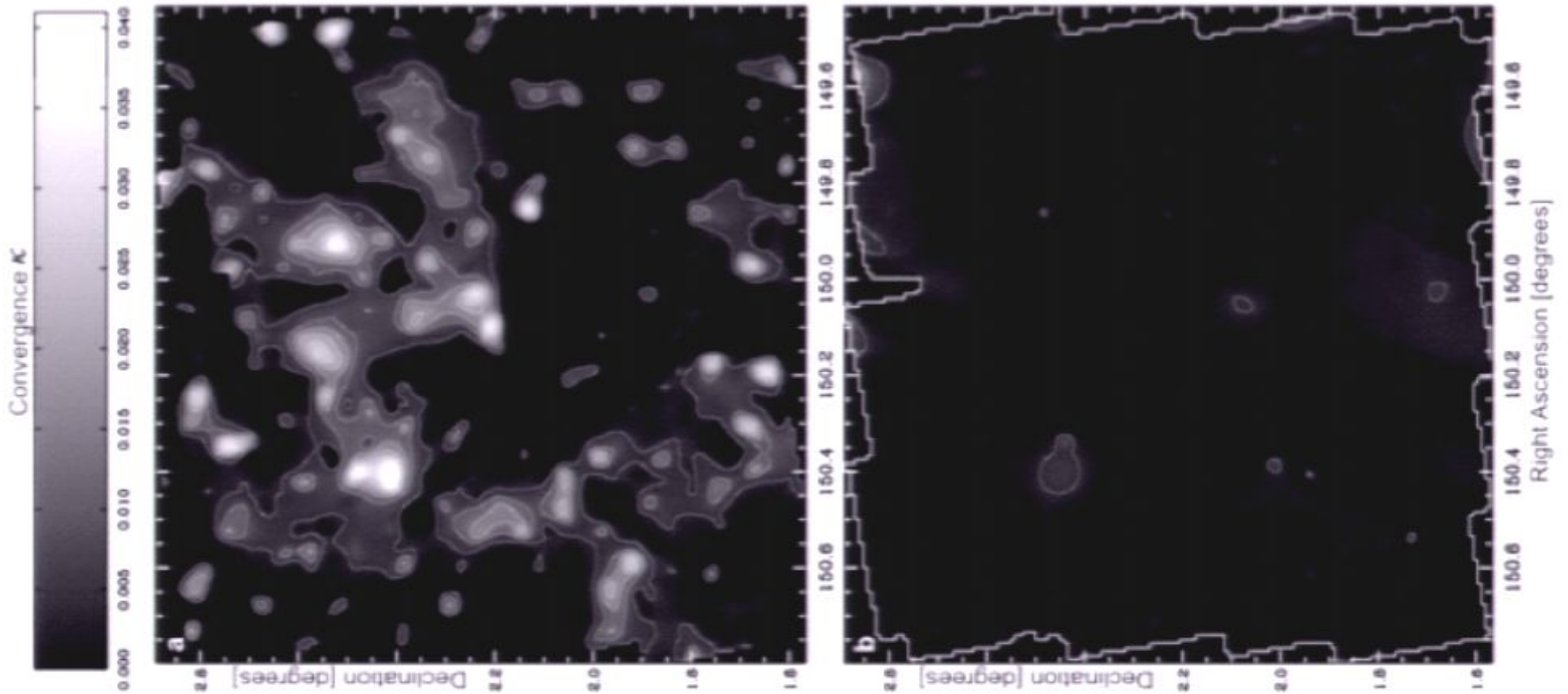


# Systematics

instrumental systematics a major and unanticipated headache  
(PSF variations, CTE)



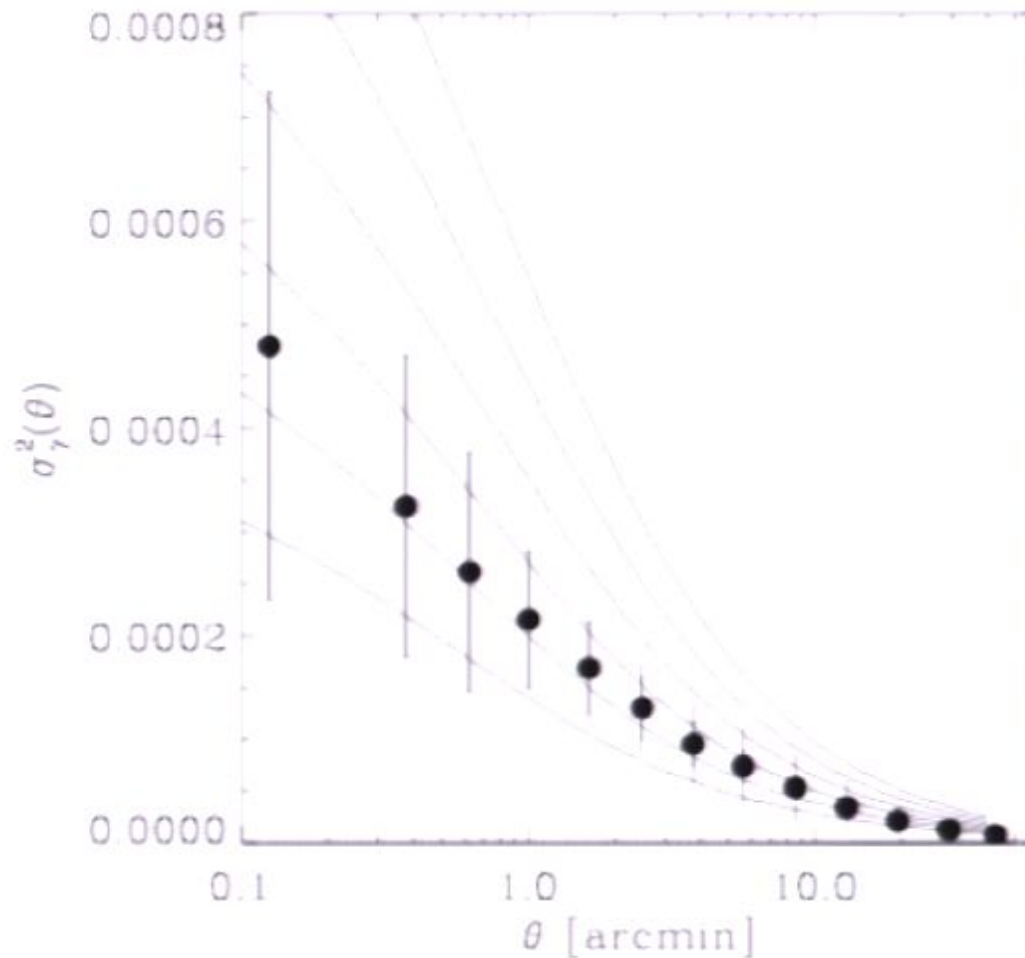
# The Final Result



E-modes (left) versus B-modes (right)



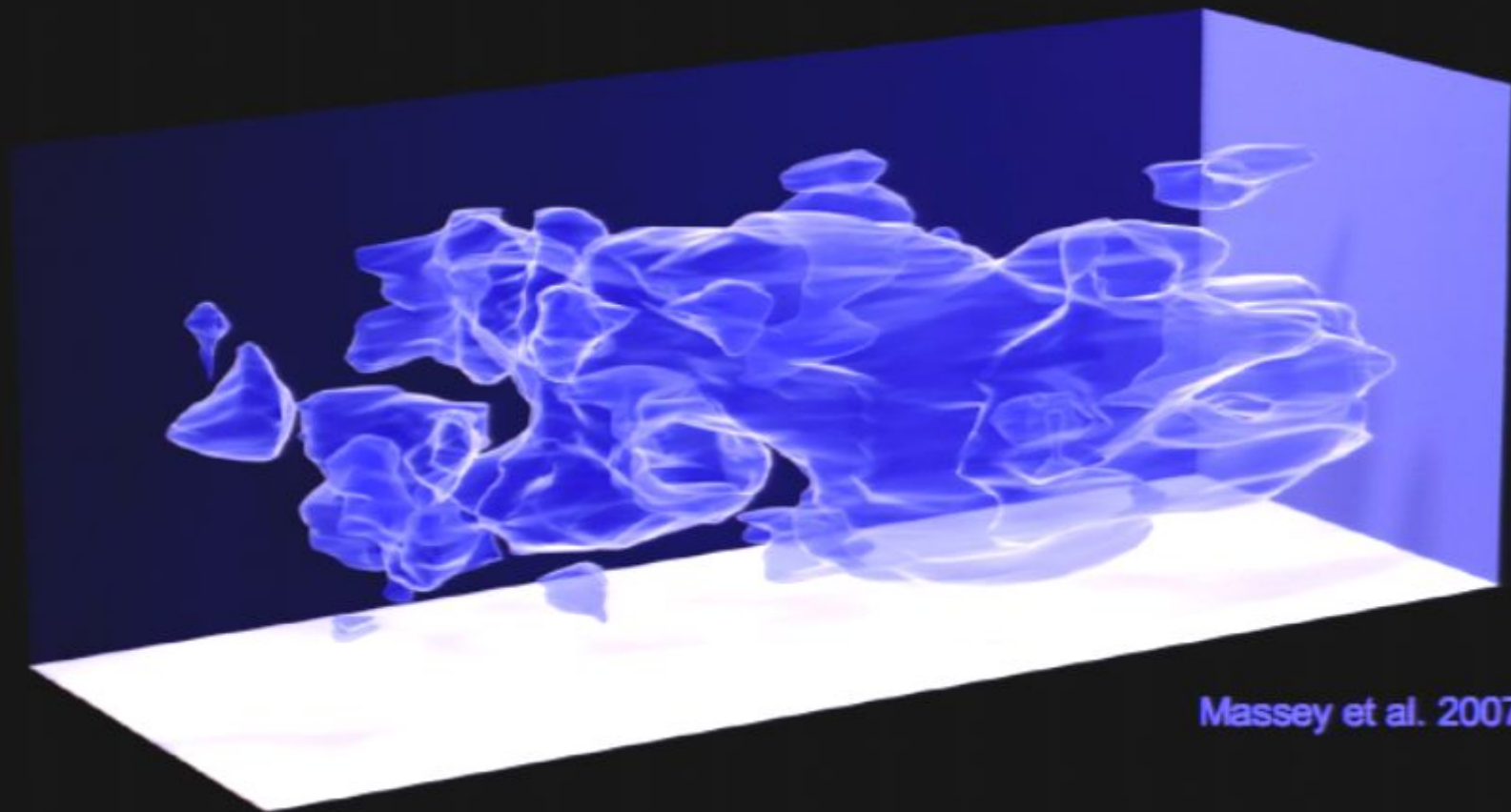
# The Final Result: Nice 2D signal



Shear variance in cells as a function of angular size.  
Curves indicate prediction for  $\sigma_8 = 0.7, 0.8, 0.9, 1.0, 1.1, 1.2$

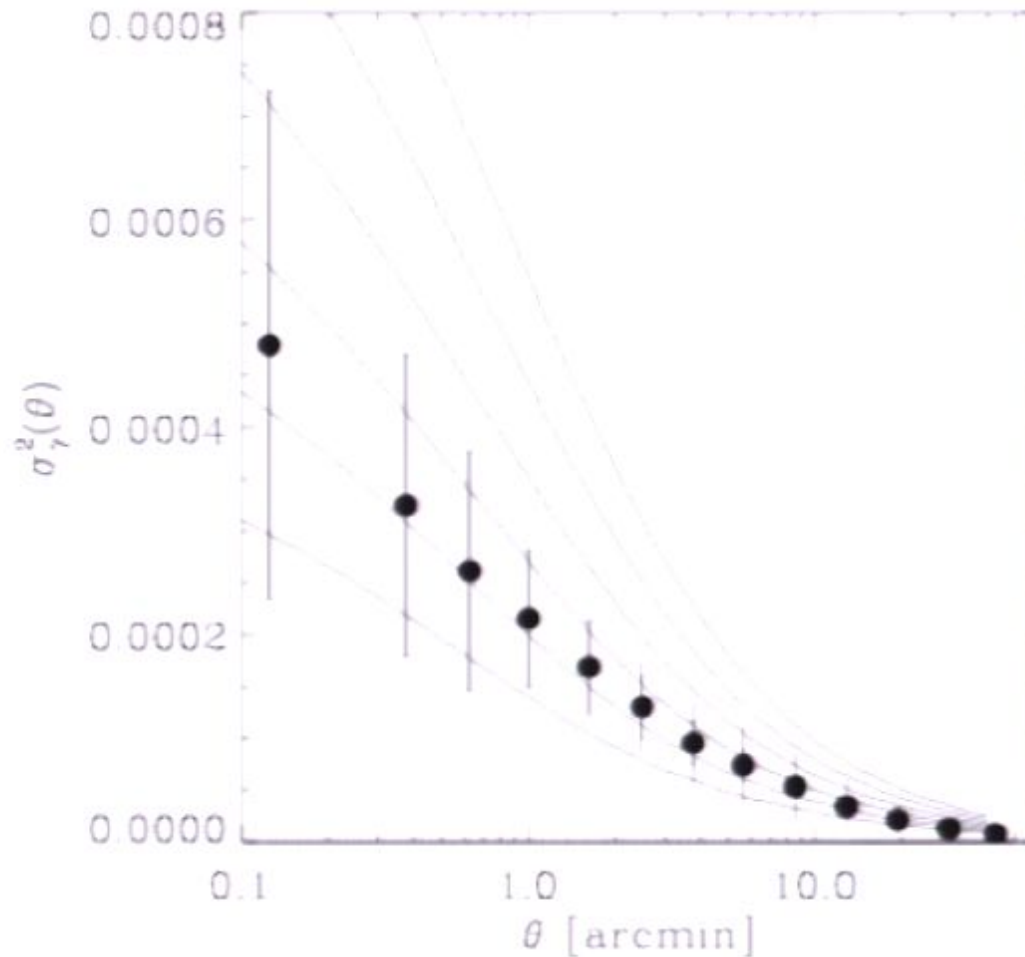
## 3D Mass Distribution

Final result: first 3D map of the mass (or potential) distribution in a large volume. Note this is only 1.6 square degrees on the sky.



Massey et al. 2007a

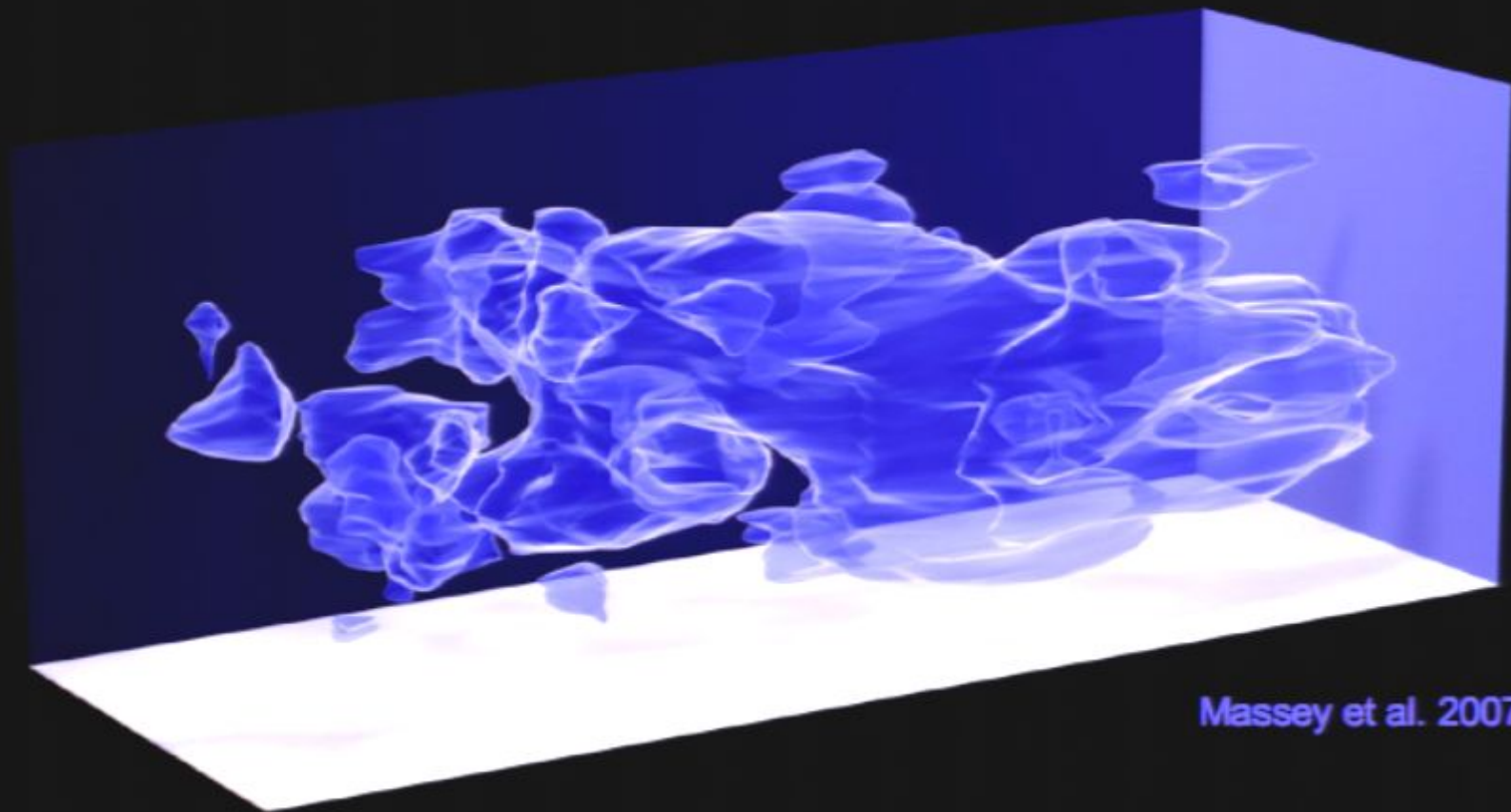
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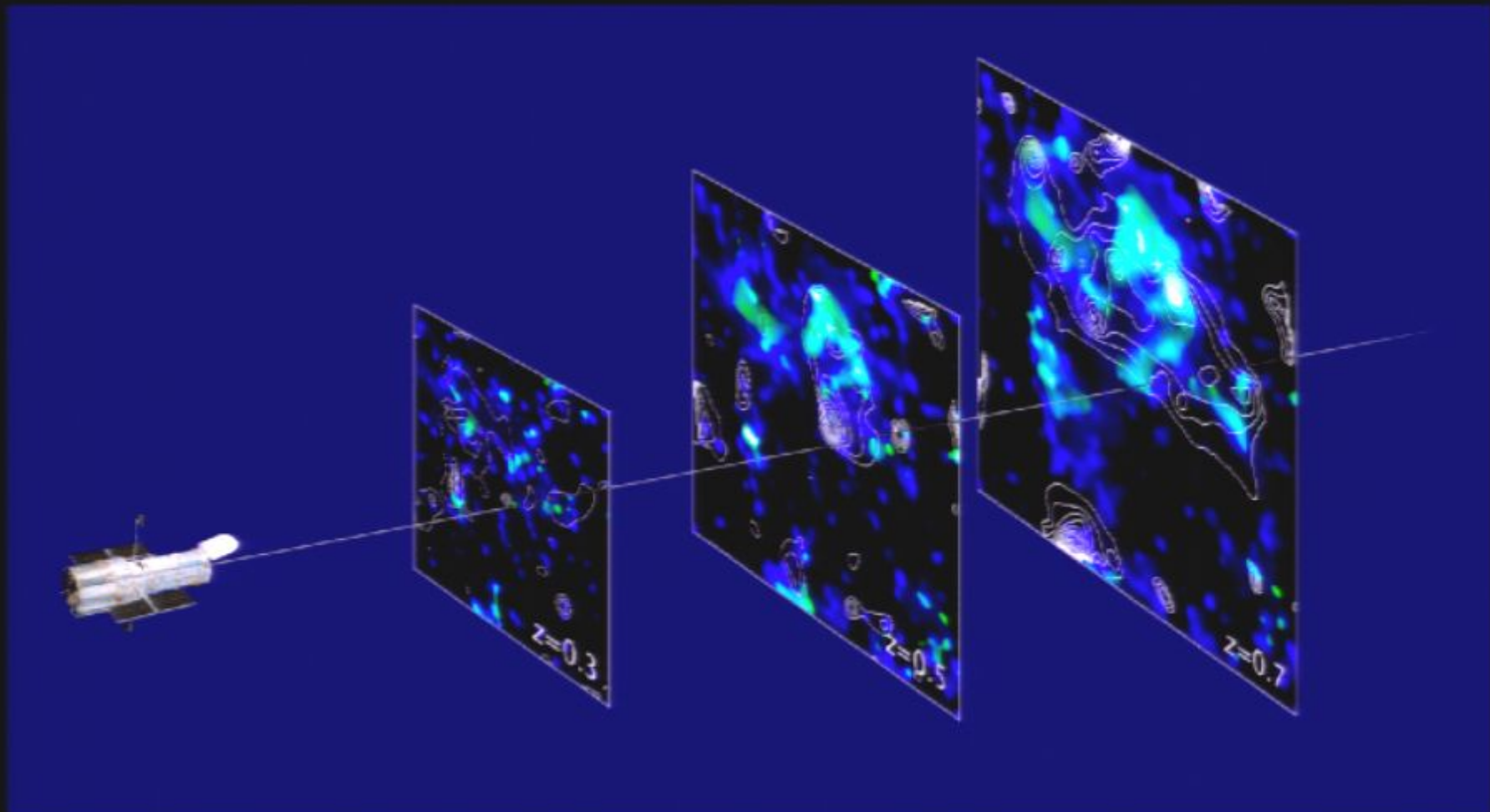
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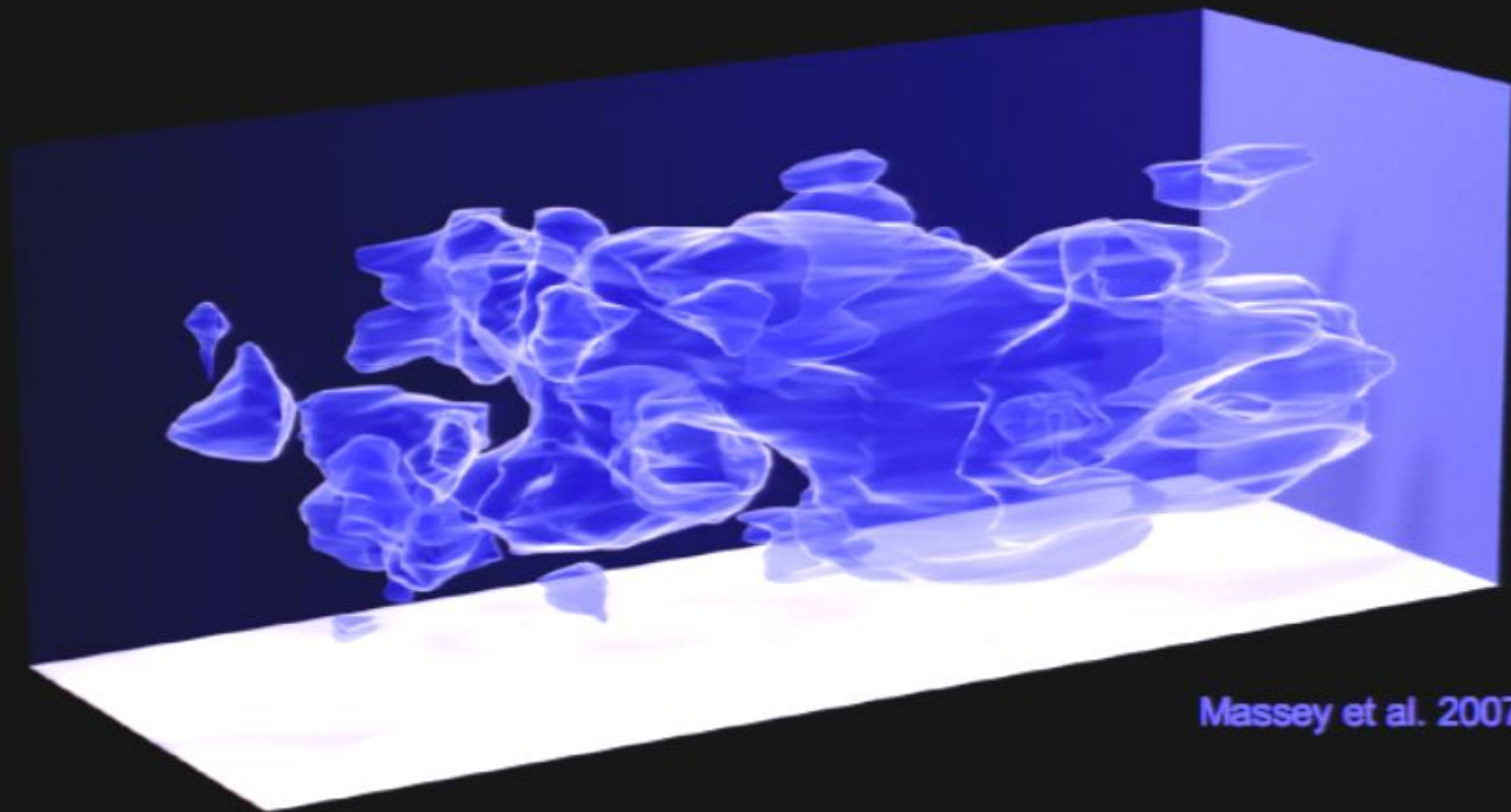
# Seeing the Growth of Structure Directly

actually quite complicated to show the growth of structure going forward in time



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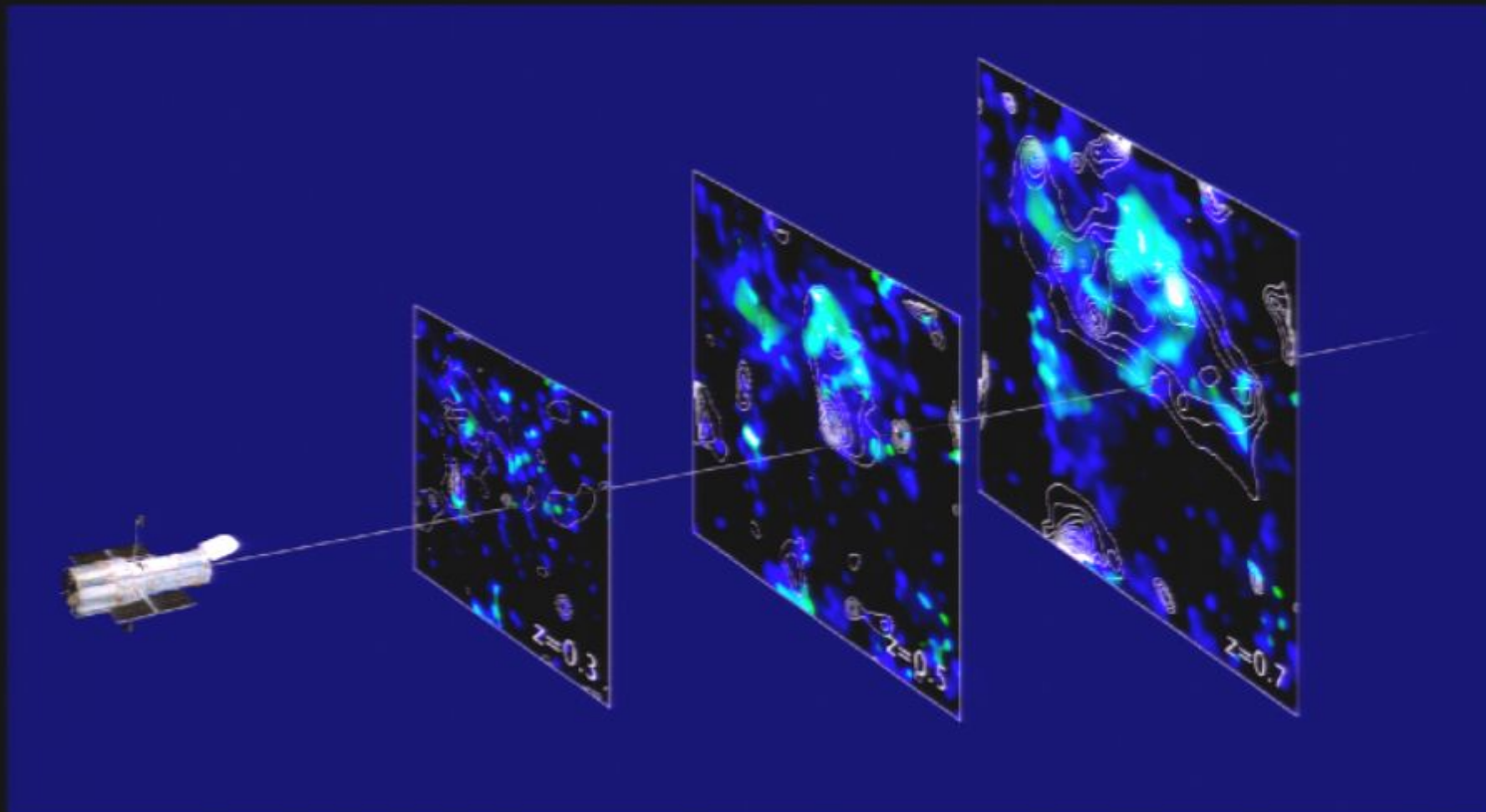
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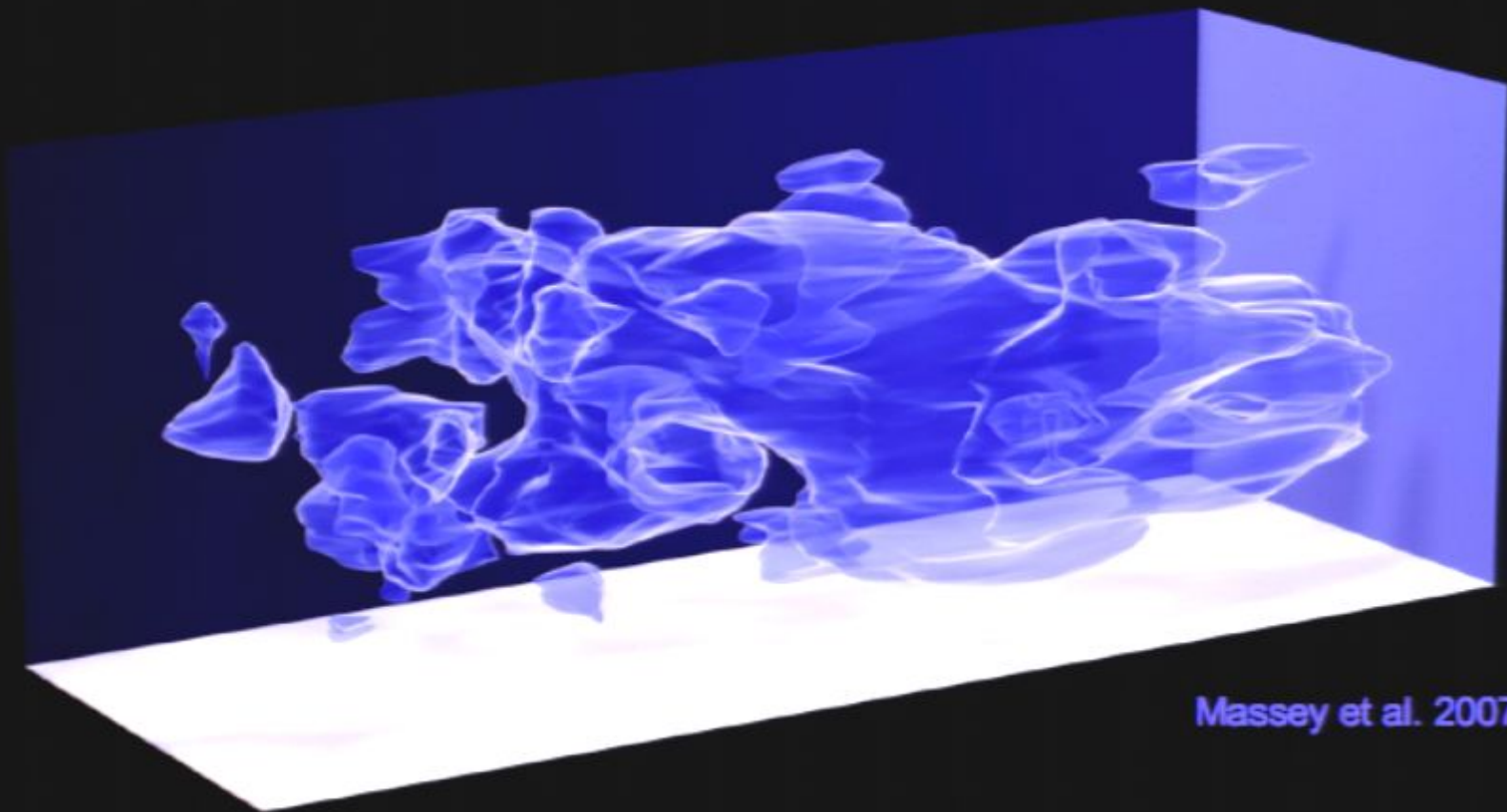
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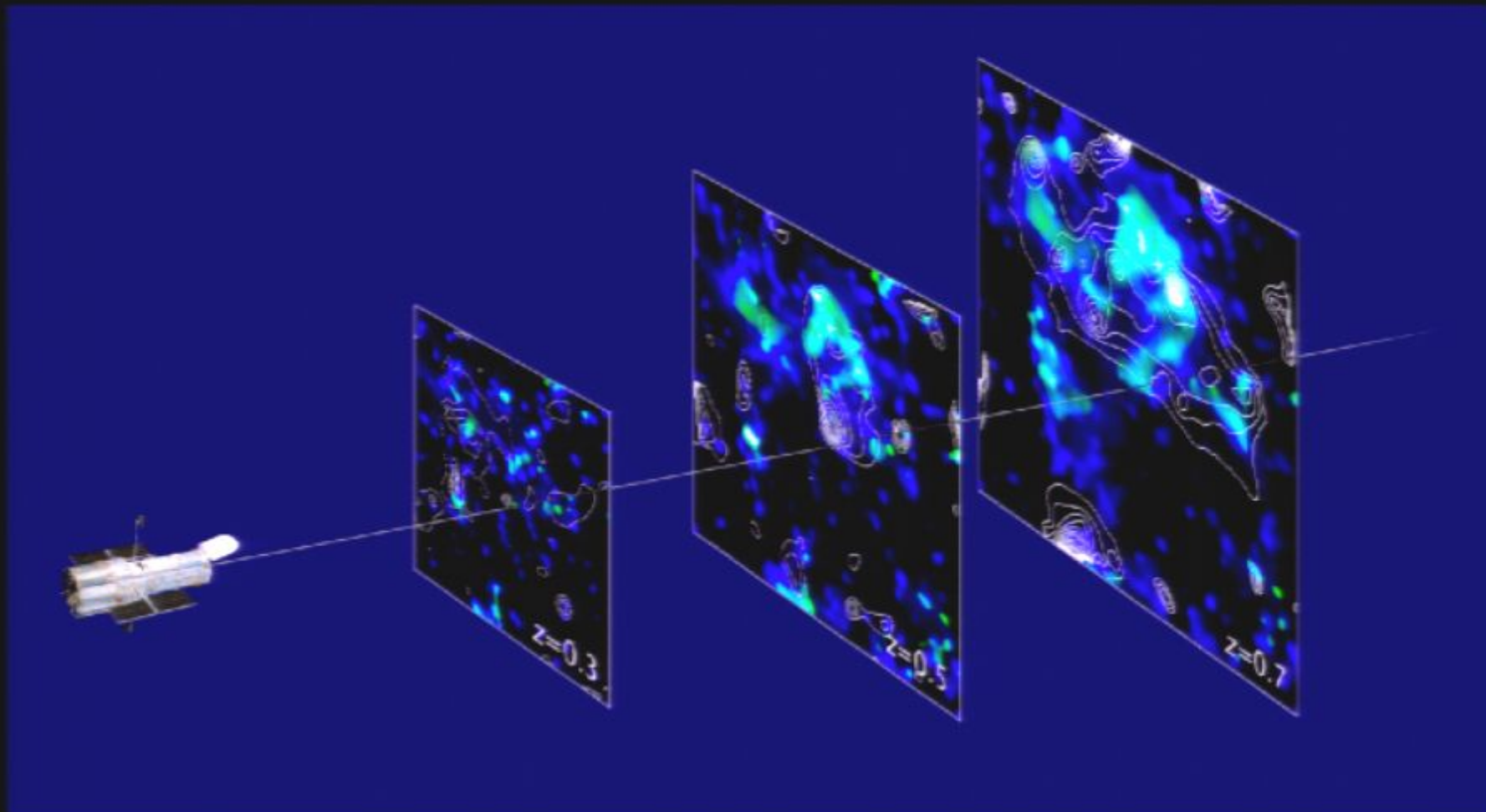


Massey et al. 2007a



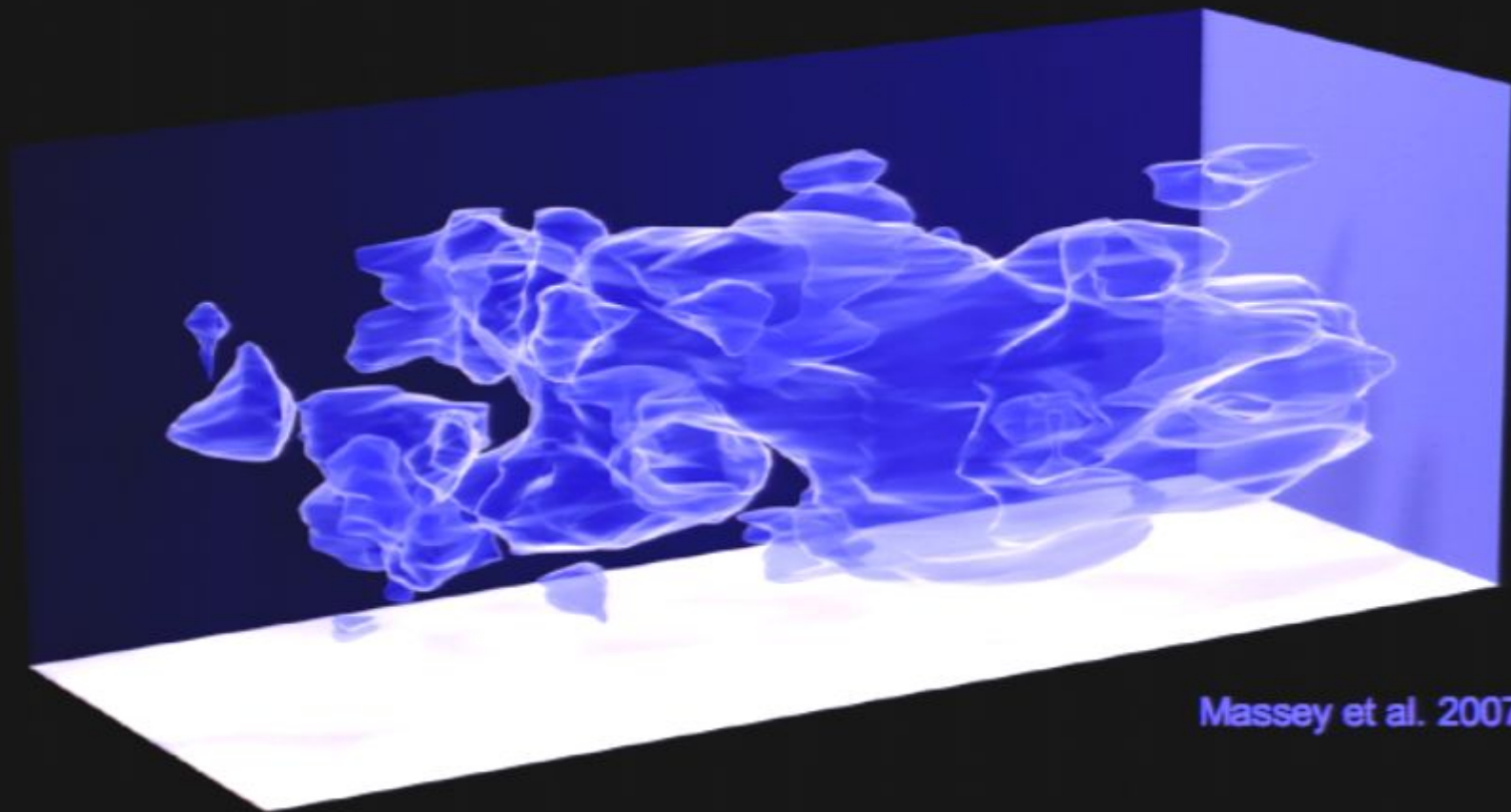
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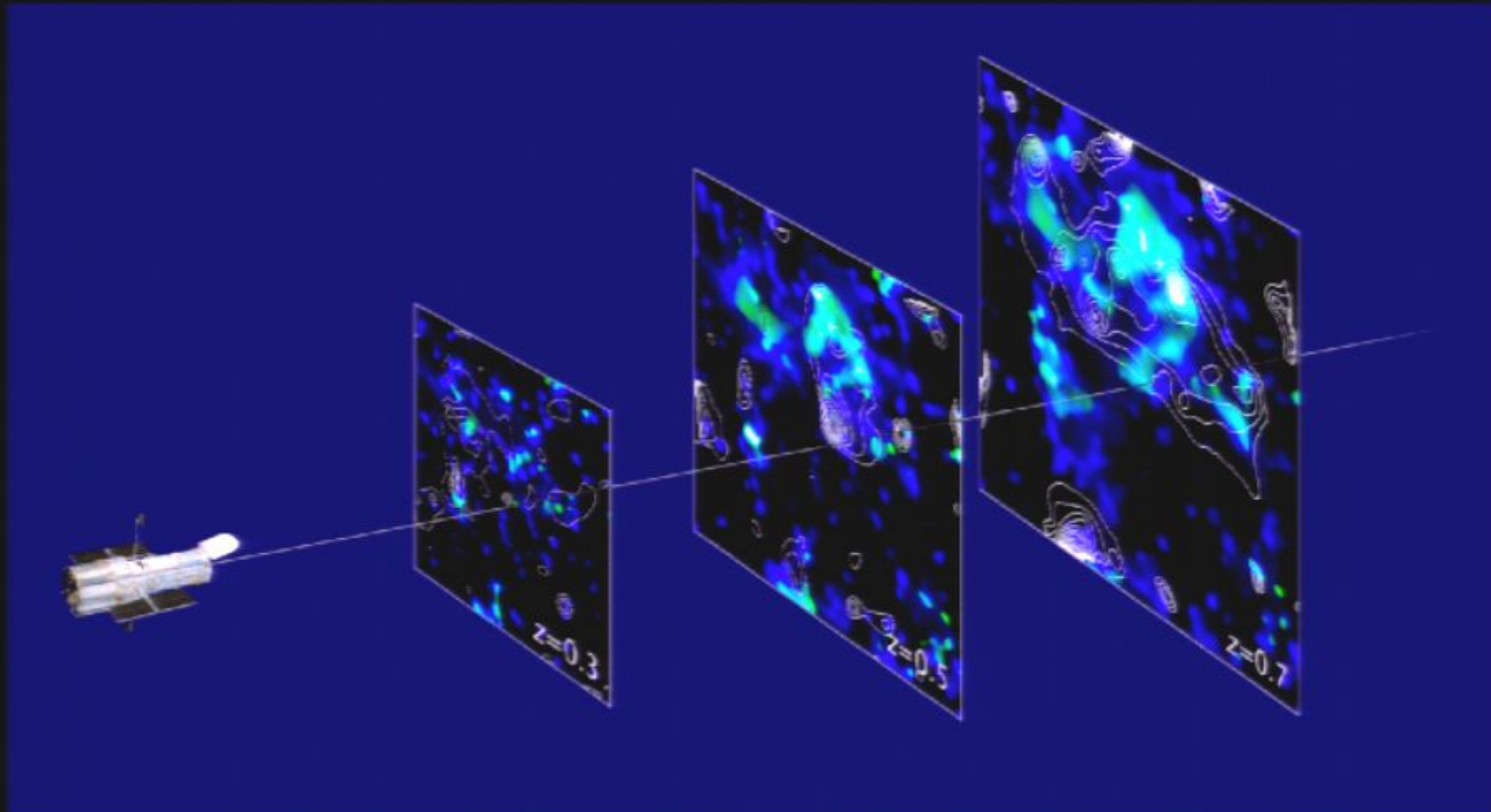
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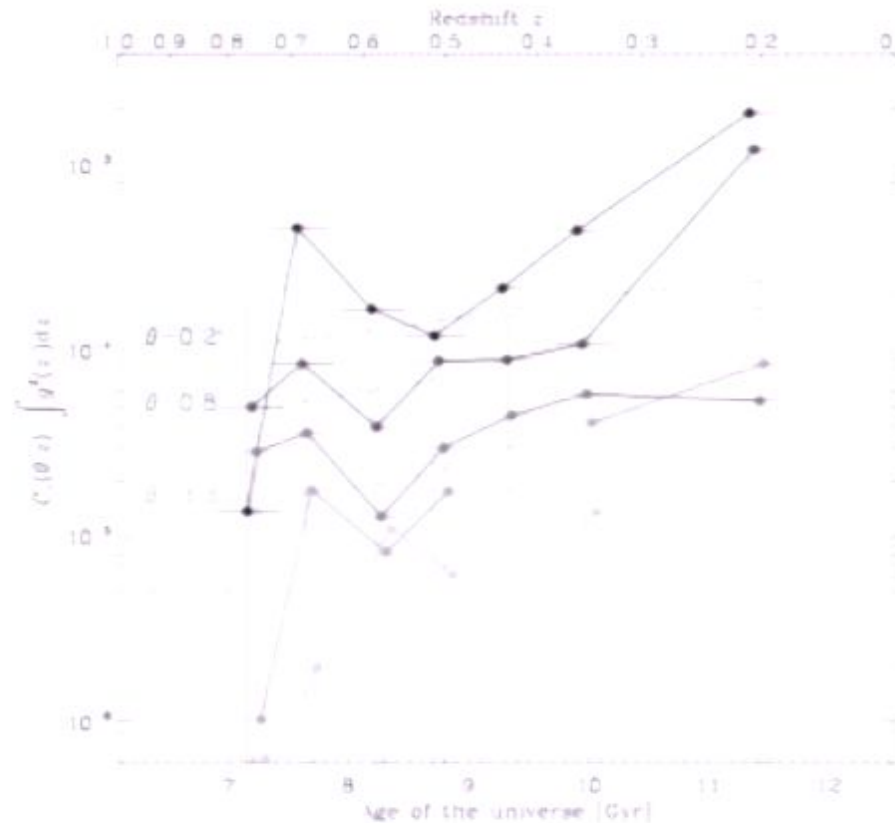
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# Measuring the Growth of Structure

Calculate the shear correlation function divided by the integrated lensing sensitivity to a given slice, and rescale to a fixed physical scale, assuming the signal is coming from the redshift of peak sensitivity.

Get (rather noisy) measure of the growth of structure:



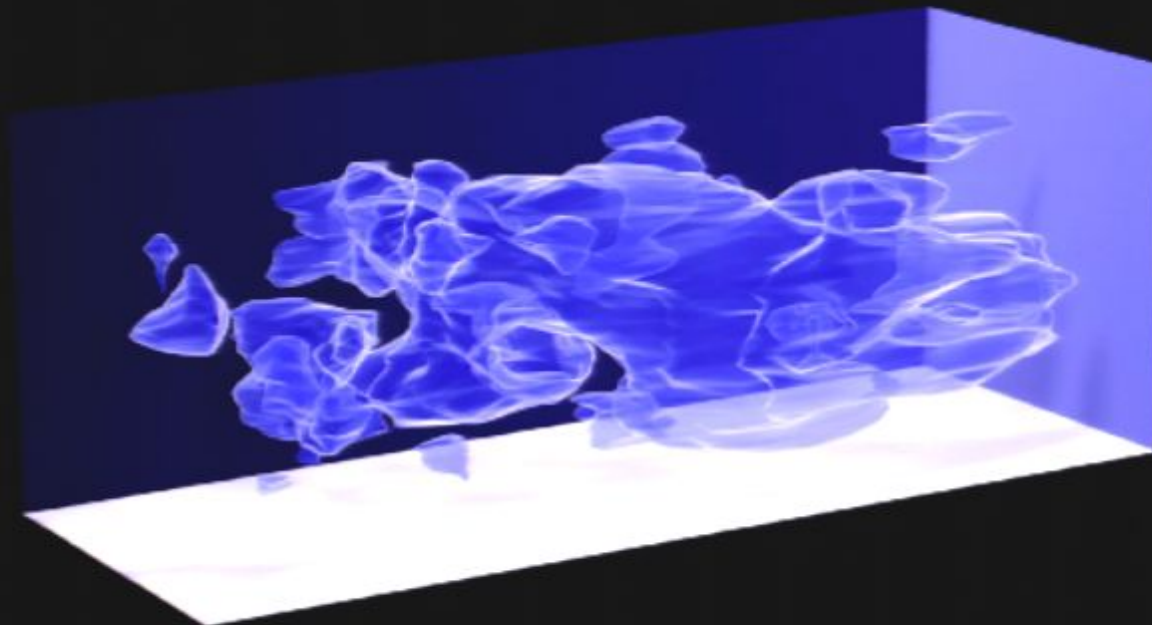
Massey et al. 2007b

# The value of redshift information

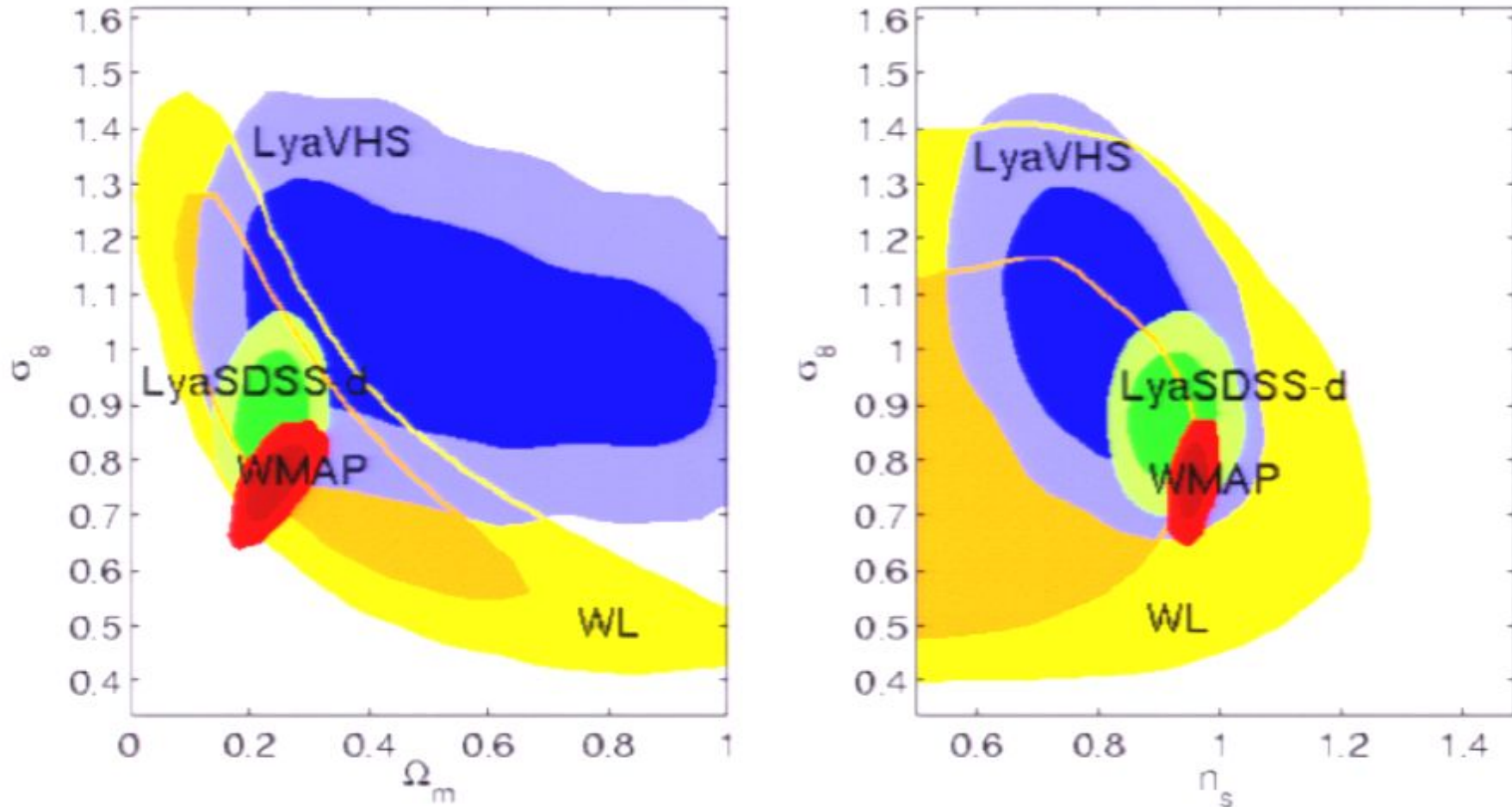
Even limited 3D information breaks some degeneracy, gives much tighter constraints (error bars 3x smaller)

$$2D \quad \sigma_8 \left( \frac{\Omega_m}{0.3} \right)^{0.48} = 0.81 \pm 0.17$$

$$3D \quad \sigma_8 \left( \frac{\Omega_m}{0.3} \right)^{0.44} = 0.866^{+0.085}_{-0.068}$$



## Combined constraints on power spectrum and cosmology

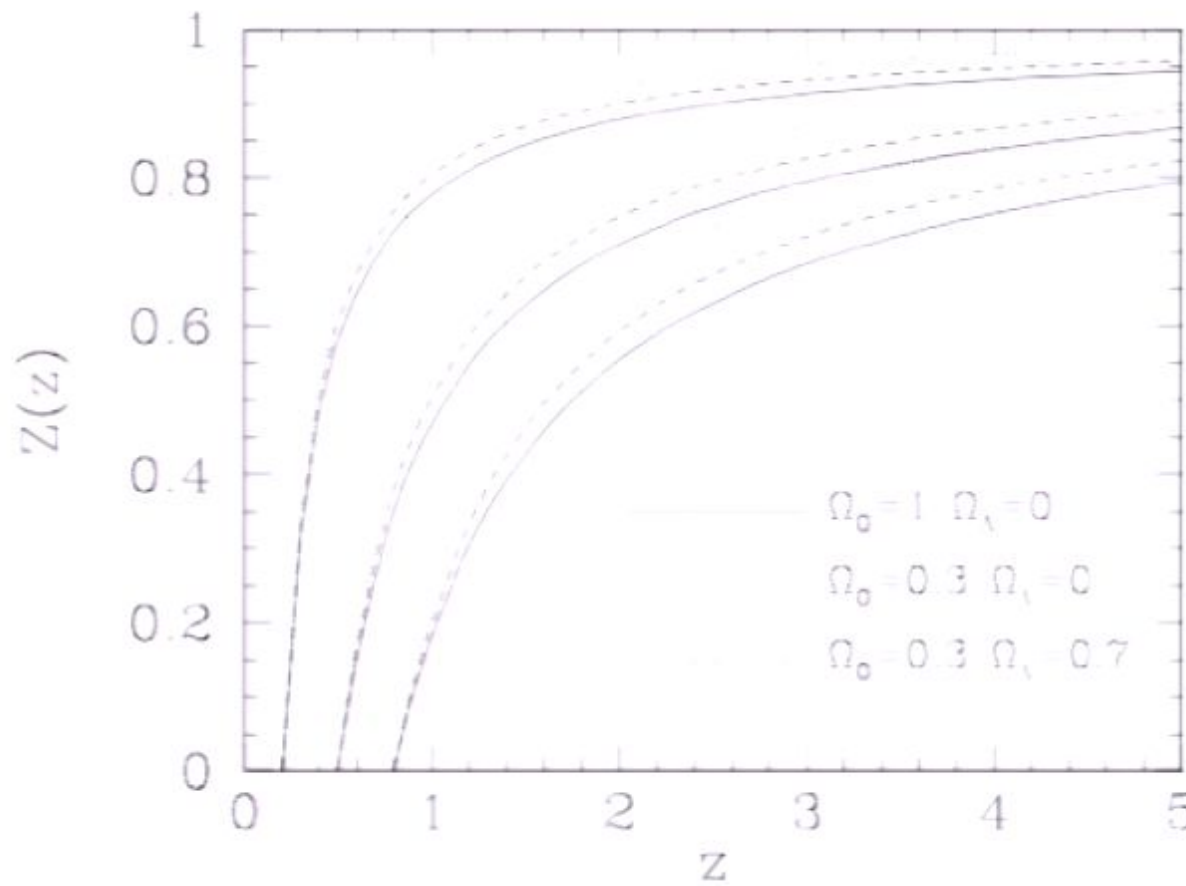


Lesgourgues et al. 2007: Lensing+ Lyman alpha results pull  $\sigma_8$  higher (0.87 +/- 0.05); combining with CMB get very tight constraint:  $\sigma_8 = 0.8 \pm 0.02$

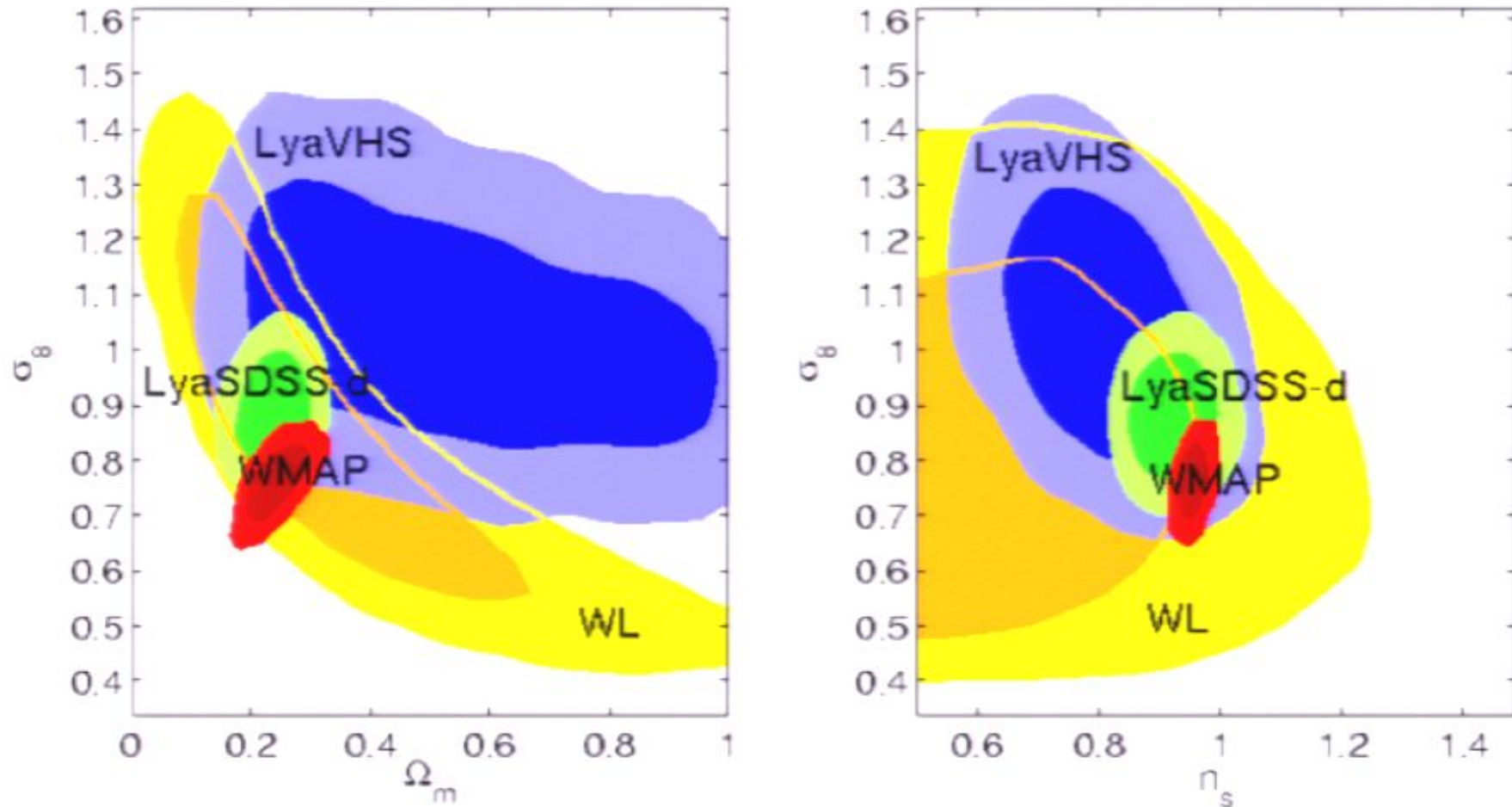
# Measuring Geometry: The Shear Ratio Test

(Jain & Taylor 2003, Bernstein & Jain 2004, Taylor et al. 2007)

- ☺ Take ratio of shear of objects **behind** a particular mass, as a function of redshift
- ☺ Details of mass distribution, overall calibration cancel => clean geometric test
- ☺ Can extend this to continuous result by fitting to all redshifts  $Z(z) \propto D_{LS}/D_S$



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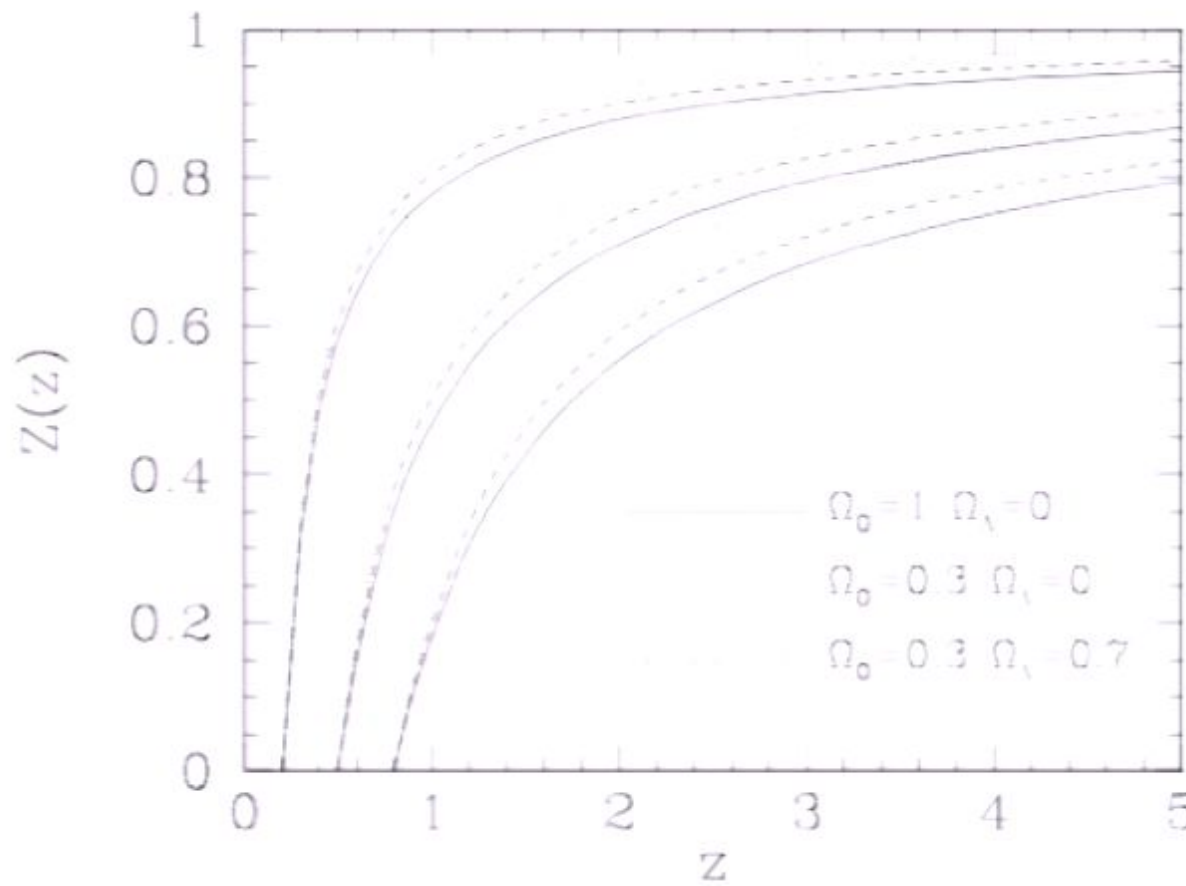
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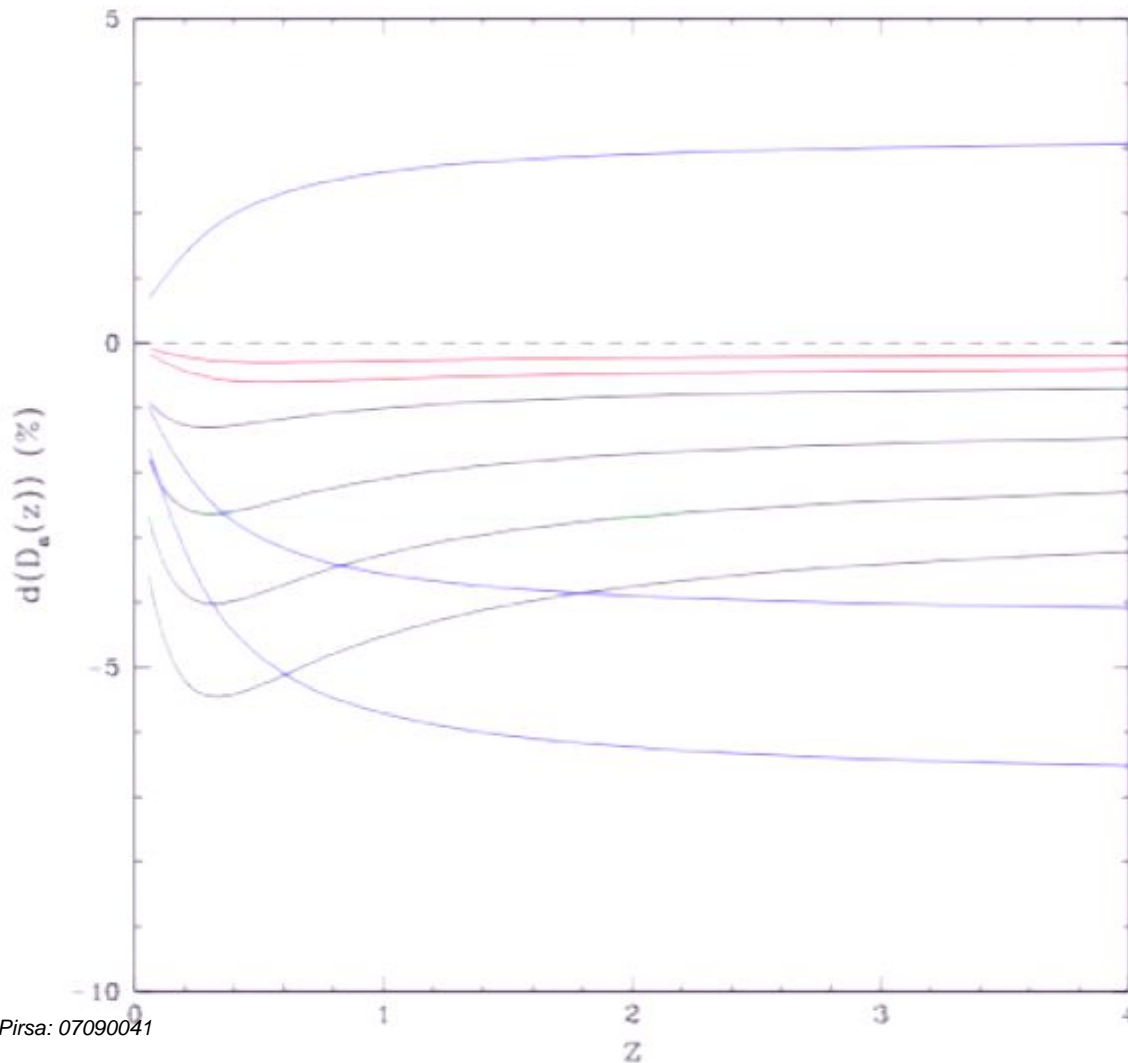
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# Lensing Behind Clusters

Use strength of signal behind cluster as a function of redshift to measure  $D_A(z)$ :



## Base:

$h = 0.73, \Omega_m = 0.27$   
( $\Lambda$  or  $X = 1 - \Omega_m$ )

## Variants:

$\Omega_m = 0.25, 0.30, 0.32$

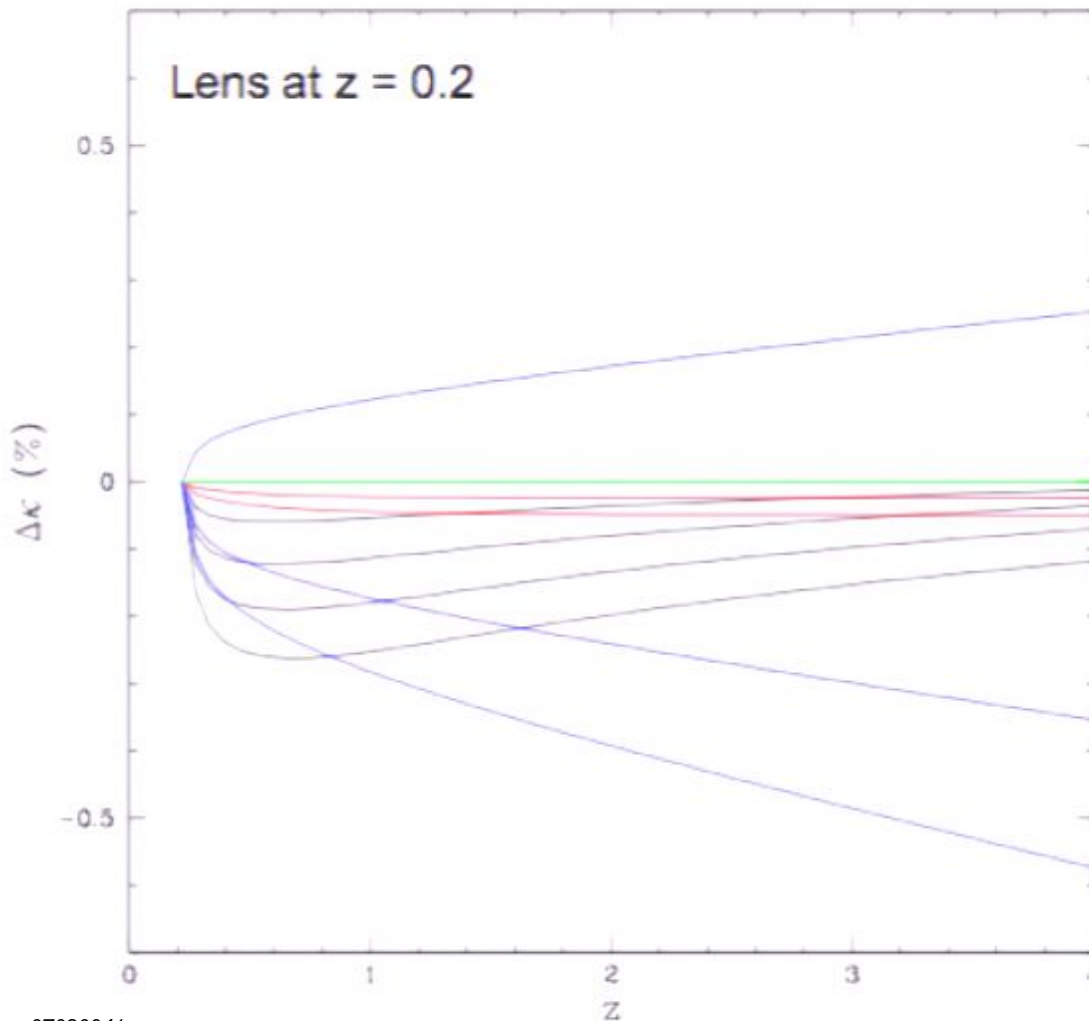
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$w(z) = w_0 + w_a(1-a)$

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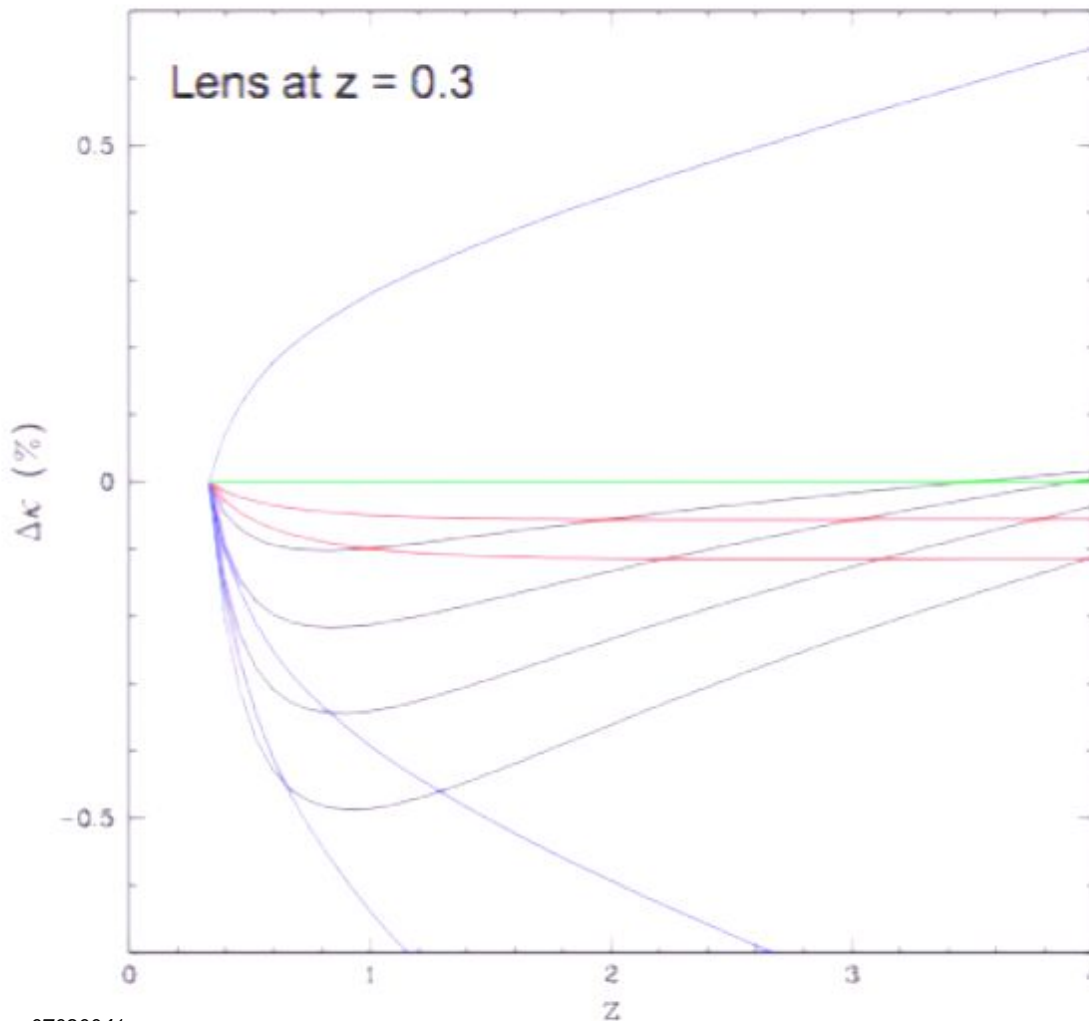
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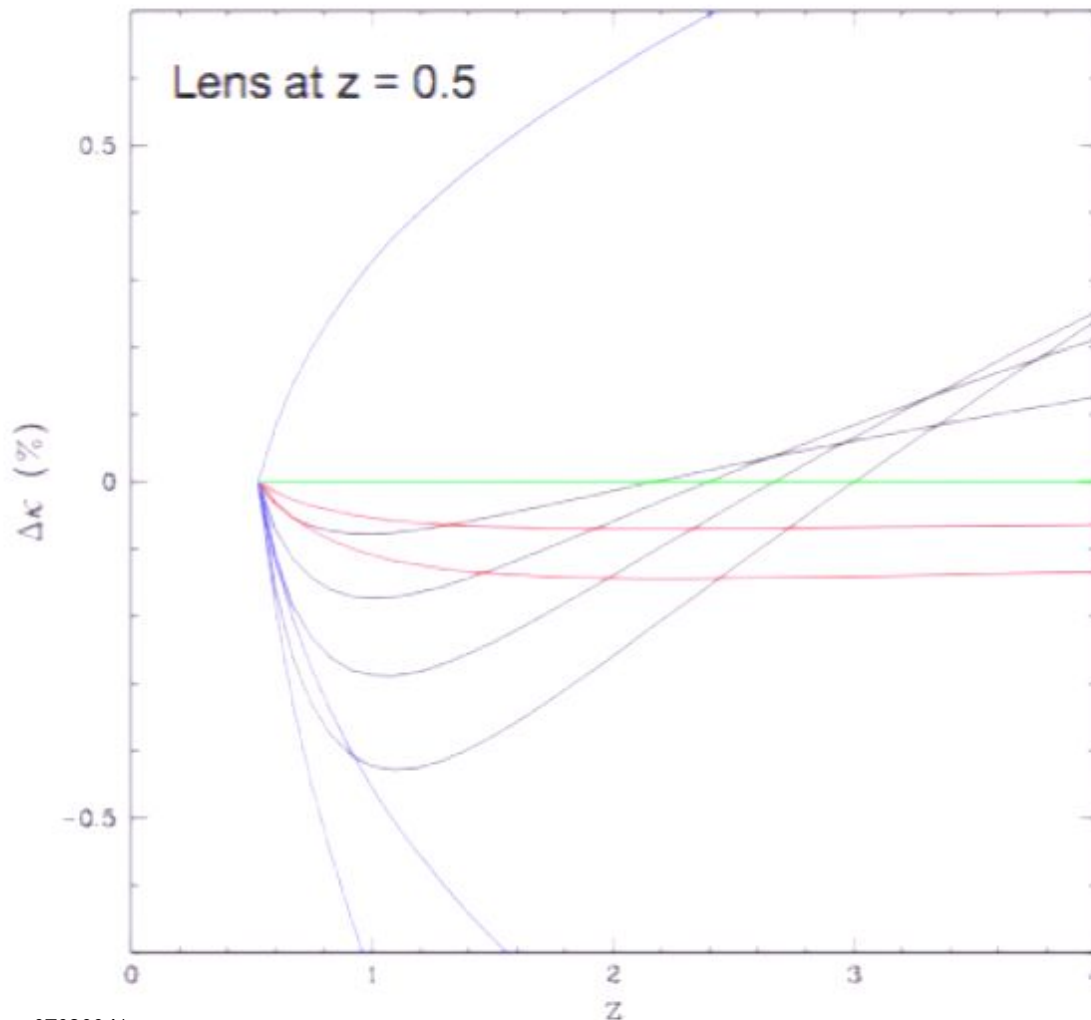
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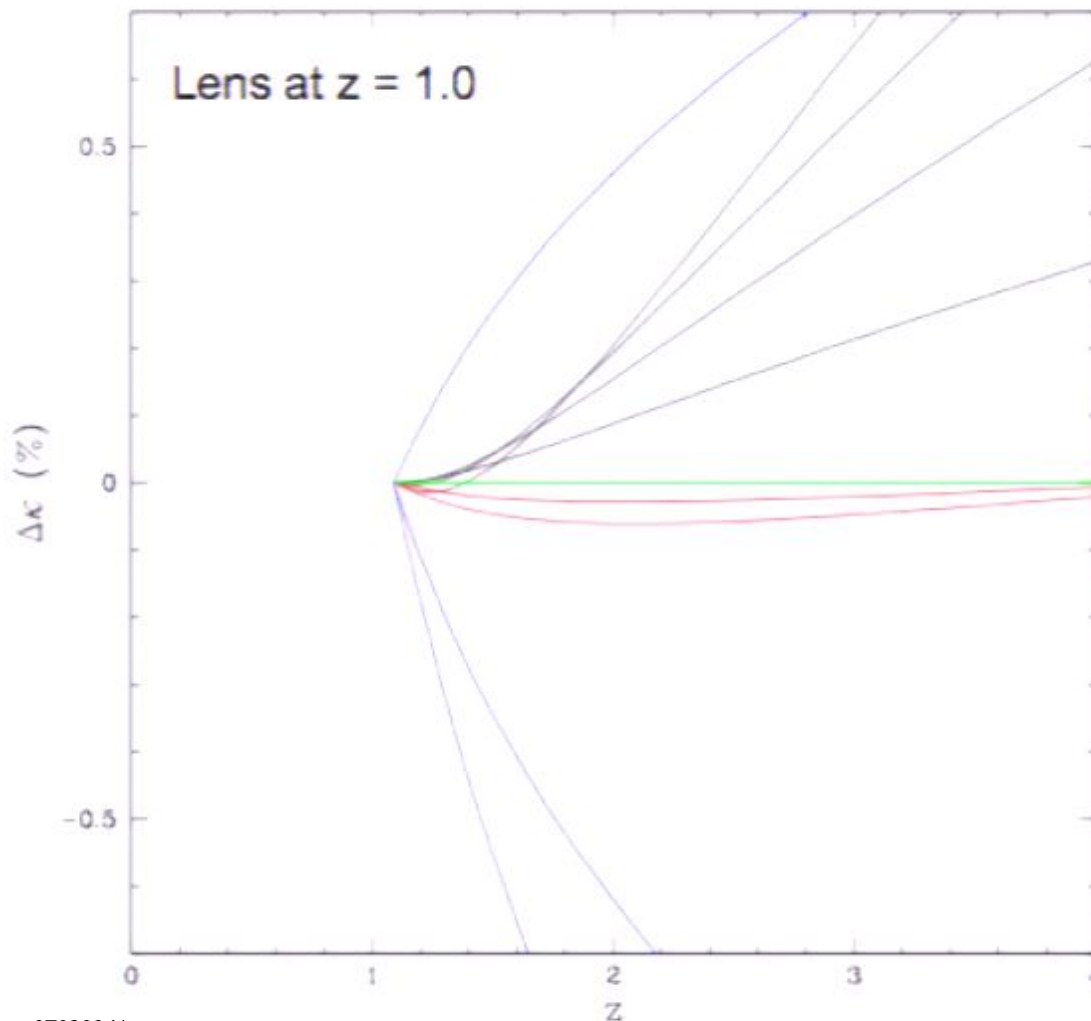
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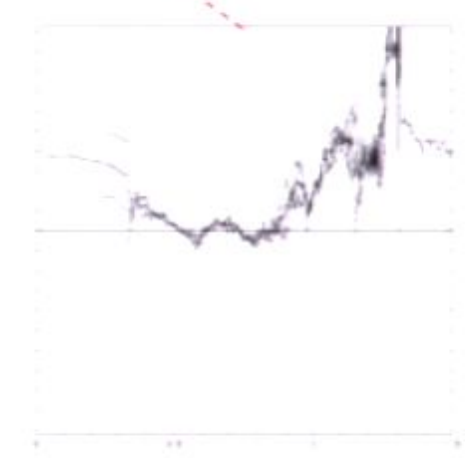
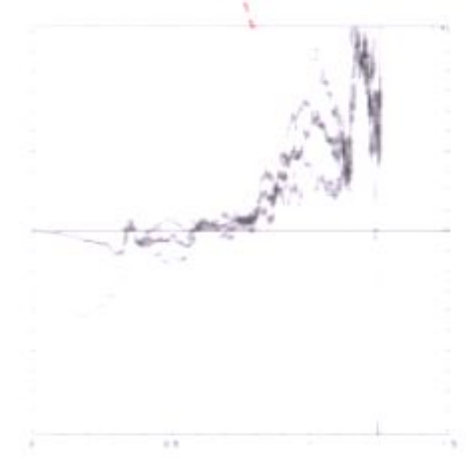
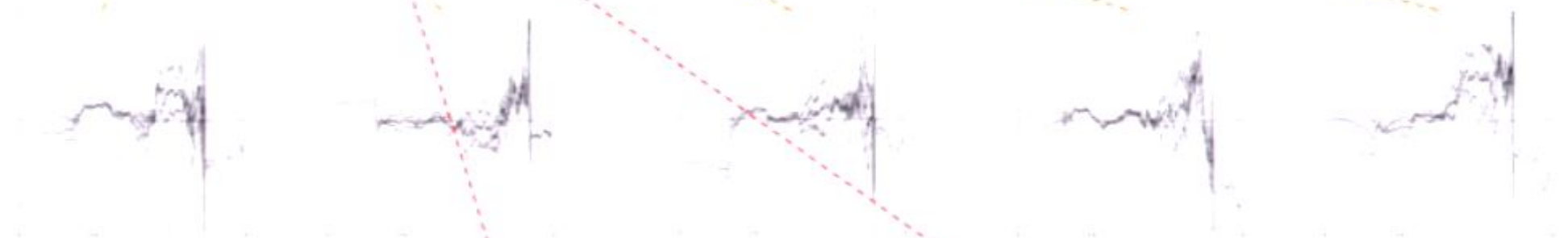
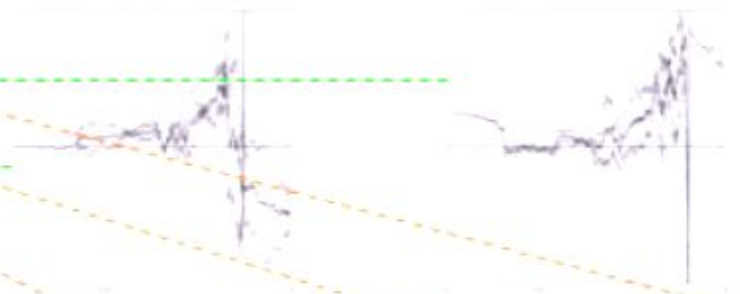
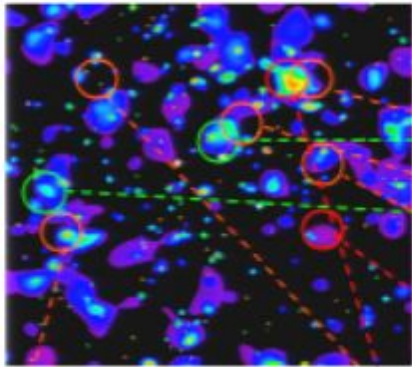
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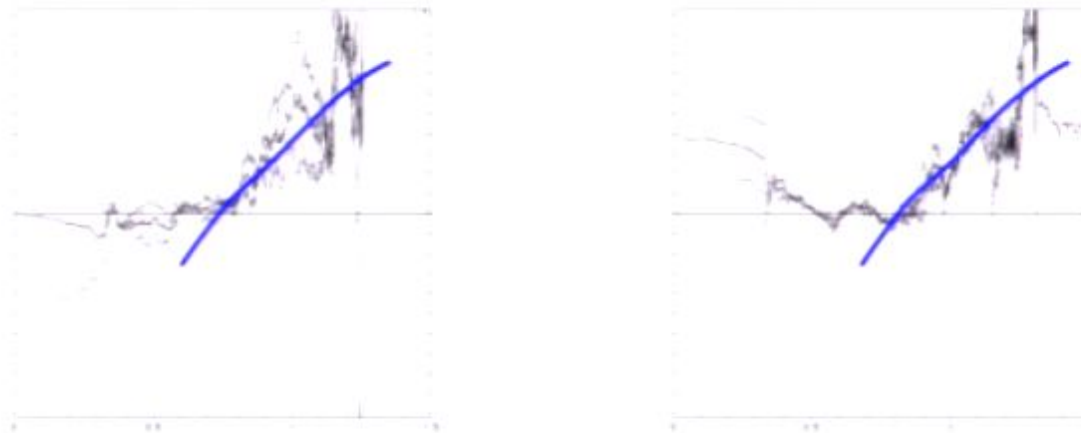
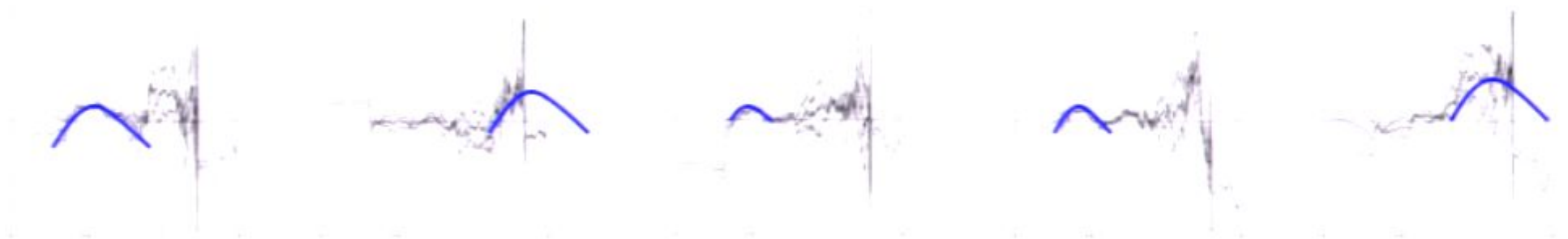
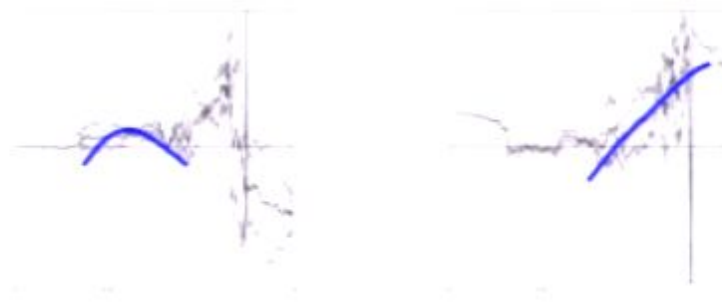
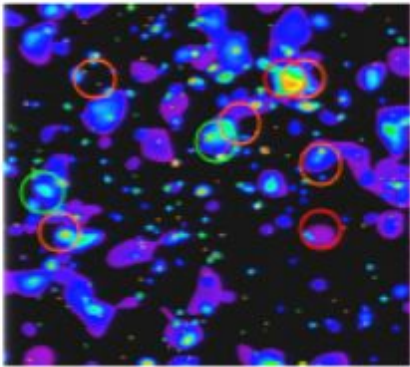
Signal weak but distinctive

# Shear vs. photo-z around peaks, along promising lines of sight



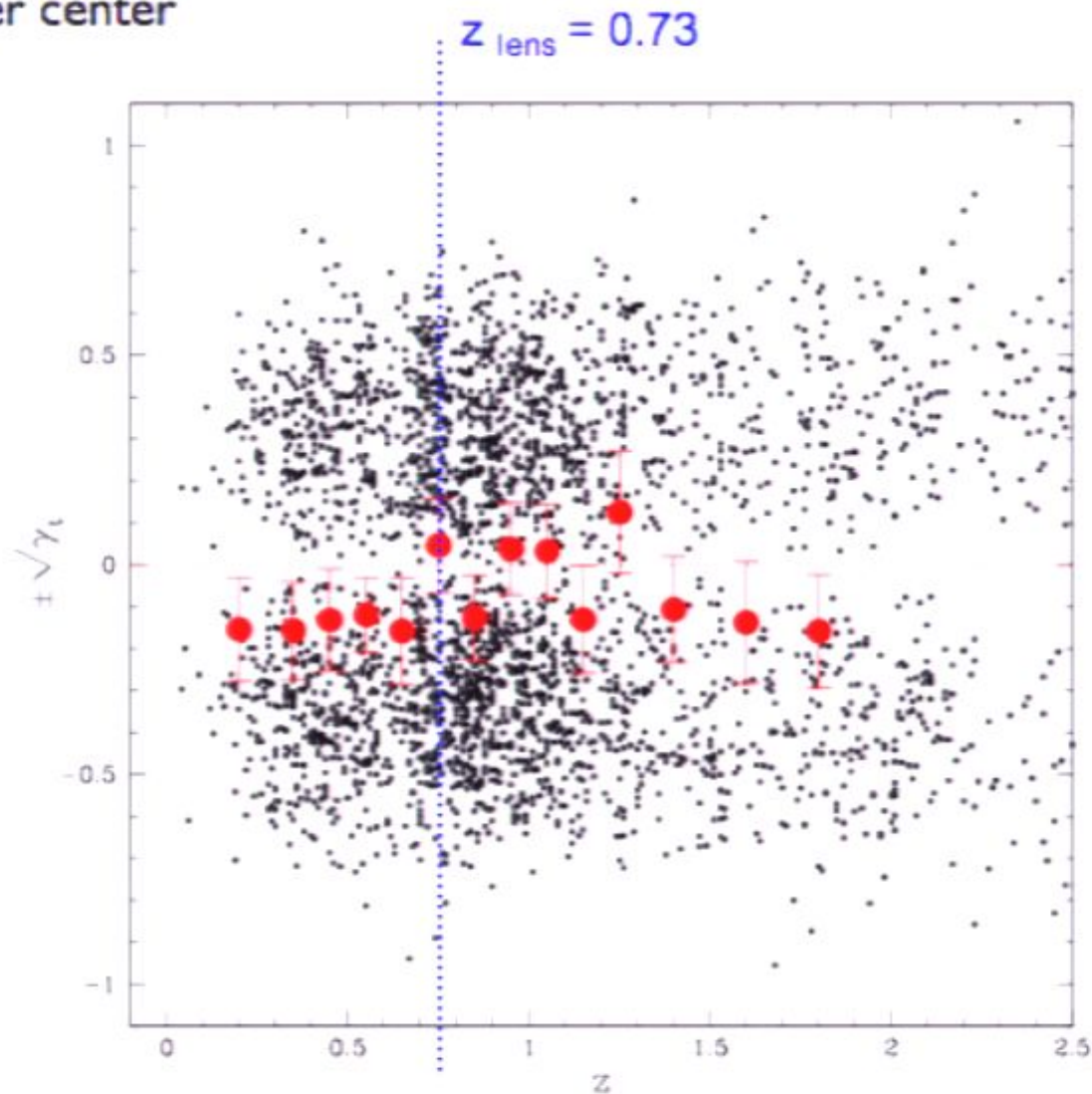


# Shear vs. photo-z around peaks, along promising lines of sight



## Preliminary Results

Signal detected in positive mean tangential shear within a given aperture behind cluster center

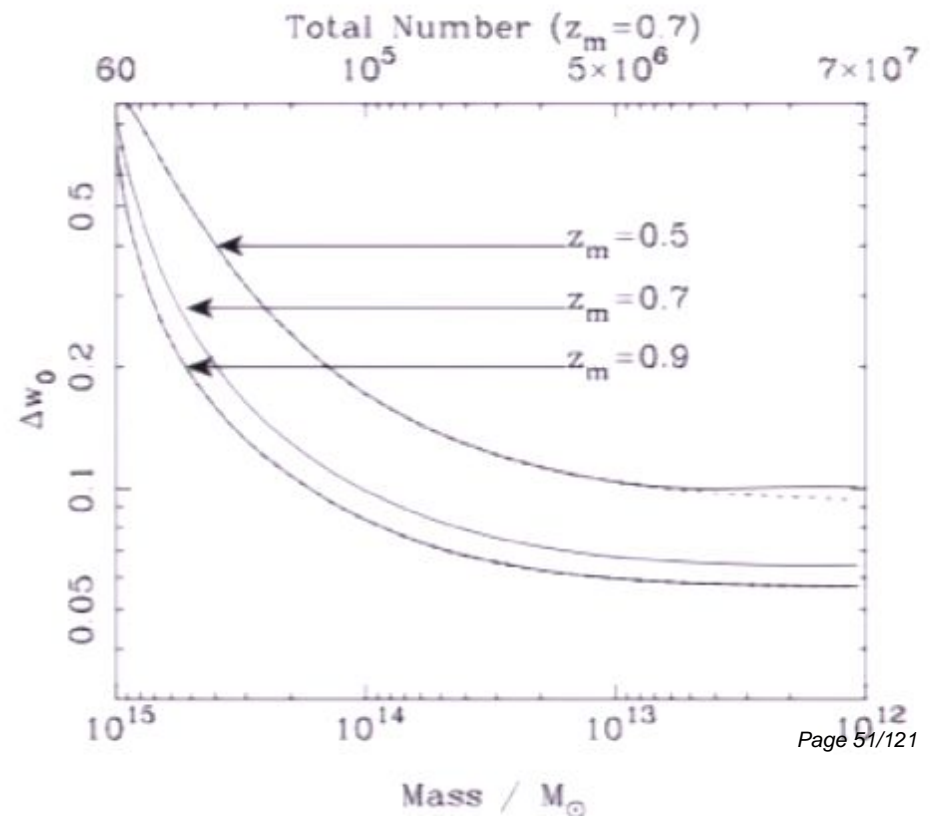


## Preliminary Results

- ¶ Signal detected behind 6-7 clusters
- ¶ Still studying noise versus cylinder radius, catalogue cuts, path weighting
- ¶ Results consistent with  $w_0 \sim -1.0 \pm 1.0$ , but based on only a few objects
- ¶ Future predictions for large surveys + CMB + BAO (Taylor et al. 2007):

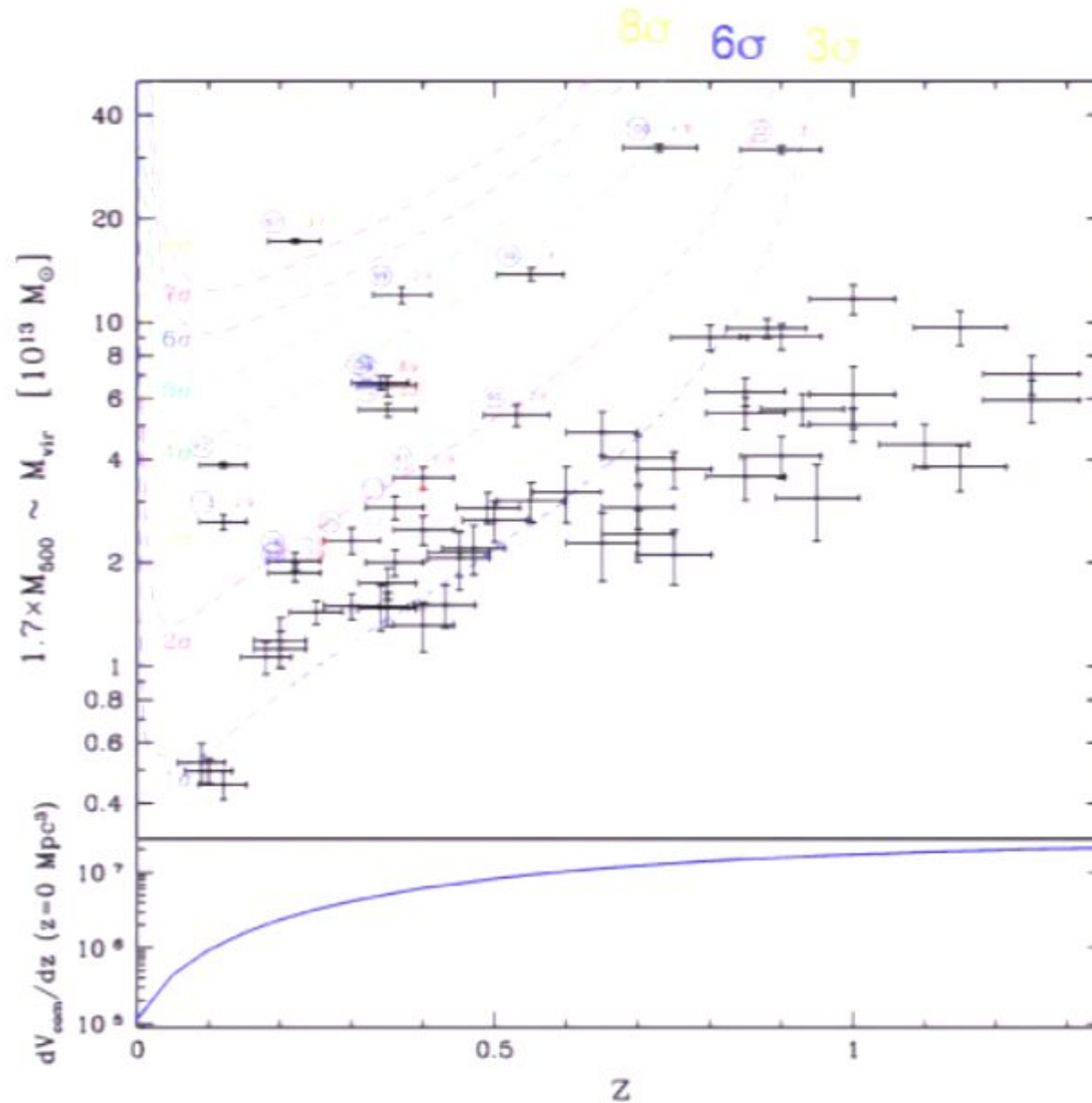
$\Delta w_0 = 0.047$ ,  $\Delta w_a = 0.1111$  and 2%  
measurement of dark energy at  
 $z \sim 0.6$

error forecasts from 20,000 deg<sup>2</sup>  
survey (Taylor et al. 2007)



# COSMOS Peaks: Xray-lensing comparison

(Finoguenov et al. 2006, Taylor et al in prep.)



Log(volume)

## Caveat: Peak Height Systematics (e.g. Hamana et al. 2004)

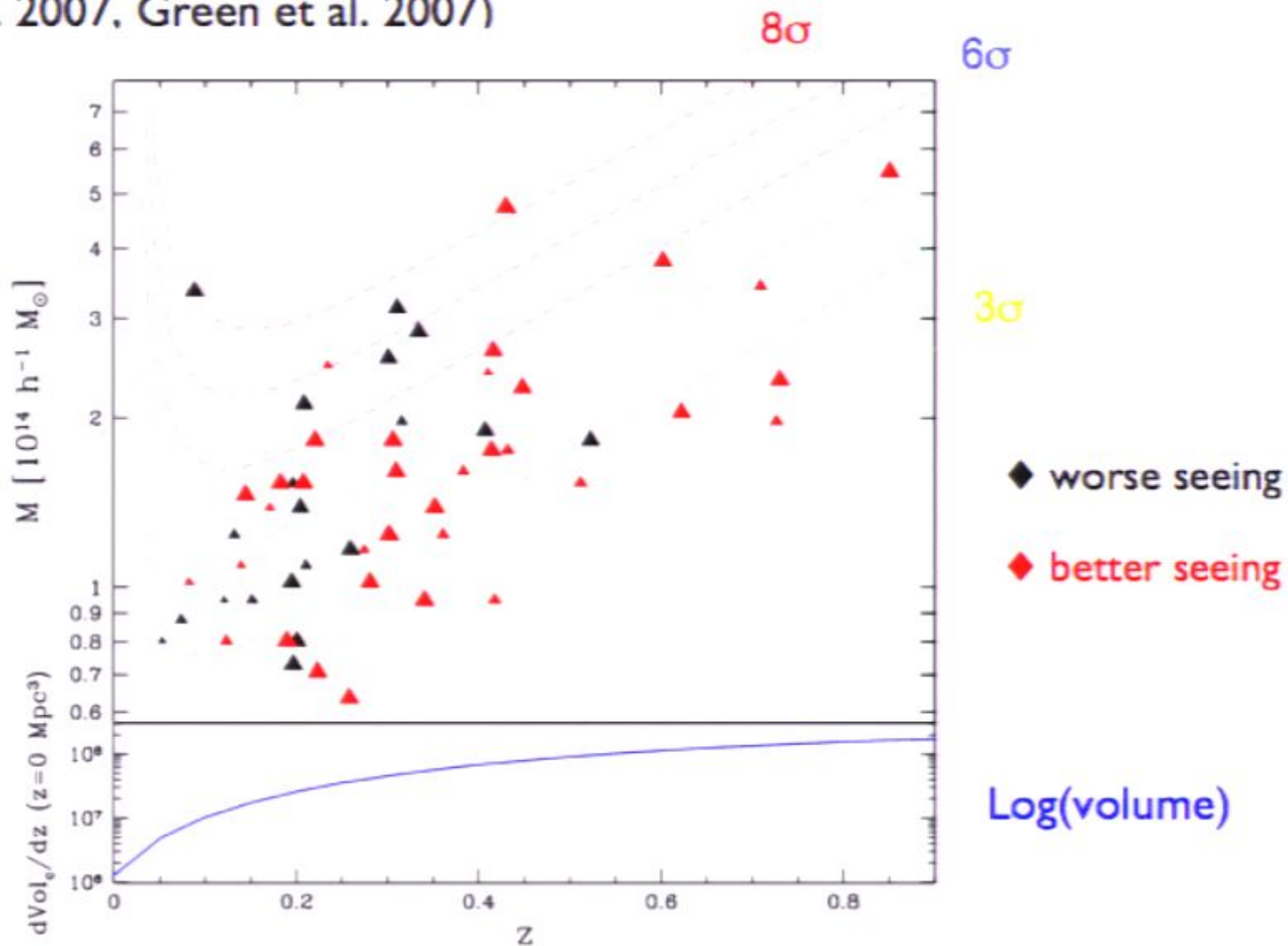
With respect to shape noise, moderately massive clusters can be detected in ground based data at  $4\text{-}\sigma$  significance at a rate of  $\sim 5/\text{degree}^2$  or more (e.g. GaBoDs survey, Suprime survey)

Problem: many  $0.3\text{-}1\sigma$  systematics, including:

- ☹ halo elongation
- ☹ halo concentration
- ☹ halo substructure
  
- ☹ chance projection
- ☹ correlated mass (i.e. non-chance projection)
  
- ☹ background source density fluctuations
- ☹ background mean- $z_s$  fluctuations
  
- ☹ **seeing**
- ☹ other observational problems (field edges, stars, etc.)

# Recent Subaru Suprime22 Survey Results

(Miyazaki et al. 2007, Green et al. 2007)



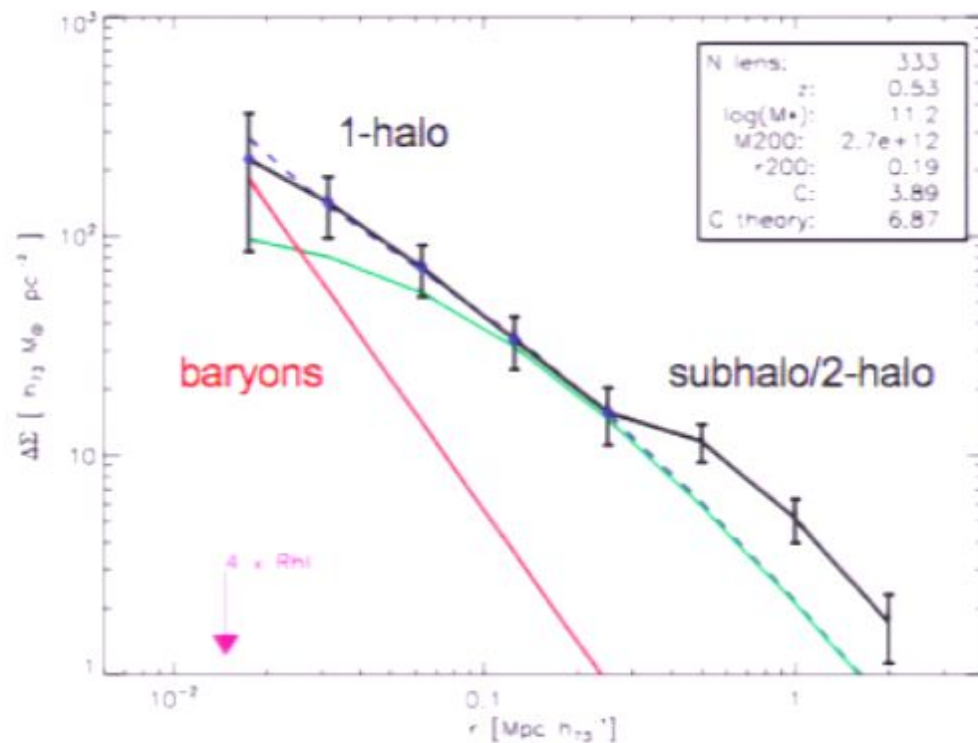
## Other Lensing Results

### Galaxy-galaxy lensing:

Stack lensing signal around groups and galaxies to get significant detection  
(have to decide how to bin galaxies)

Result: lensing detected at high significance over a range of radii

Future possibilities in this field include 1-halo/2-halo/baryonic decomposition of profile, concentration measurements, evolution etc.



Leauthaud et al. 2007

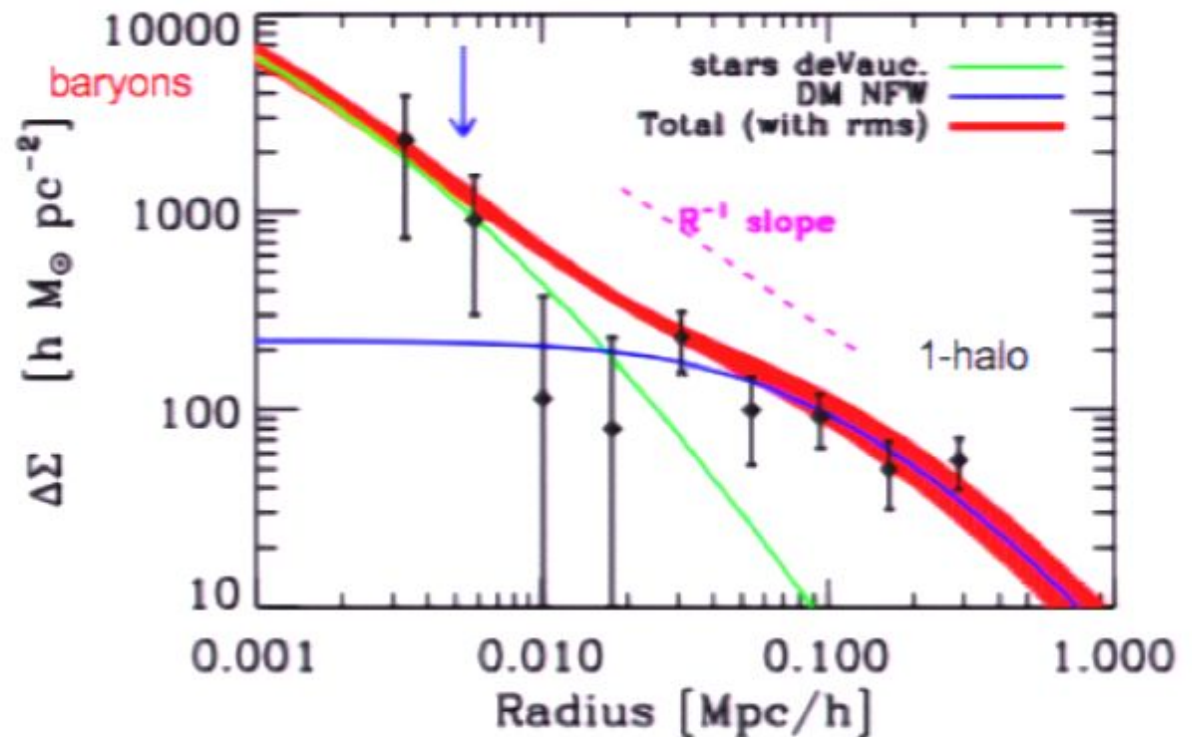
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### Galaxy-galaxy lensing:

Stack lensing signal around groups and galaxies to get significant detection  
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Result: lensing detected at high significance over a range of radii

Future possibilities in this field include 1-halo/2-halo/baryonic decomposition of profile, concentration measurements, evolution etc.





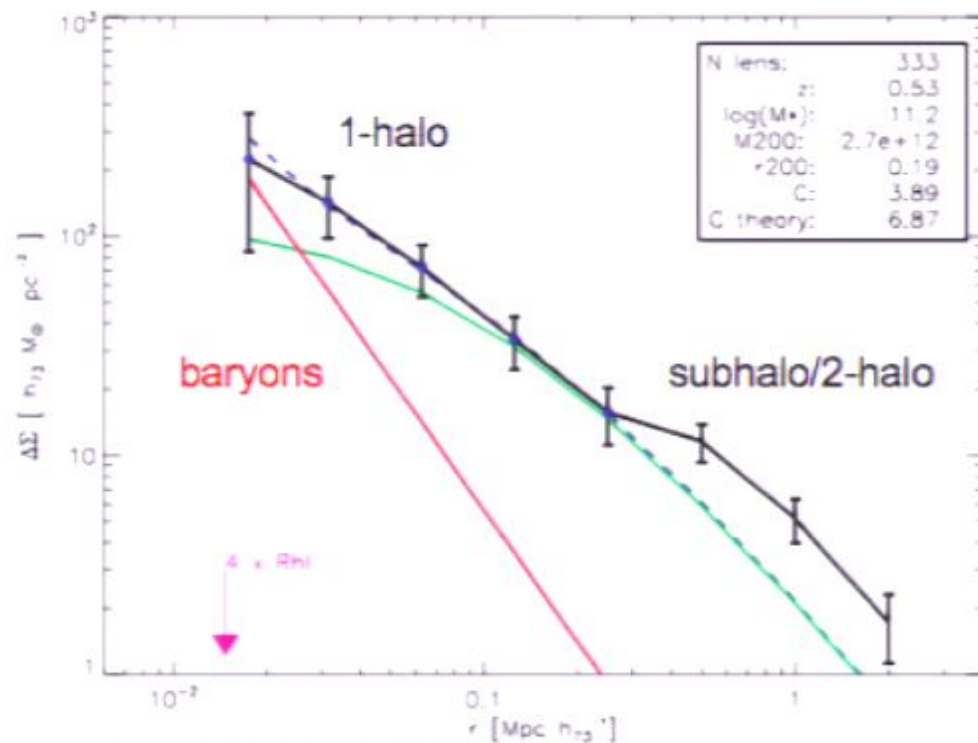
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Leauthaud et al. 2007

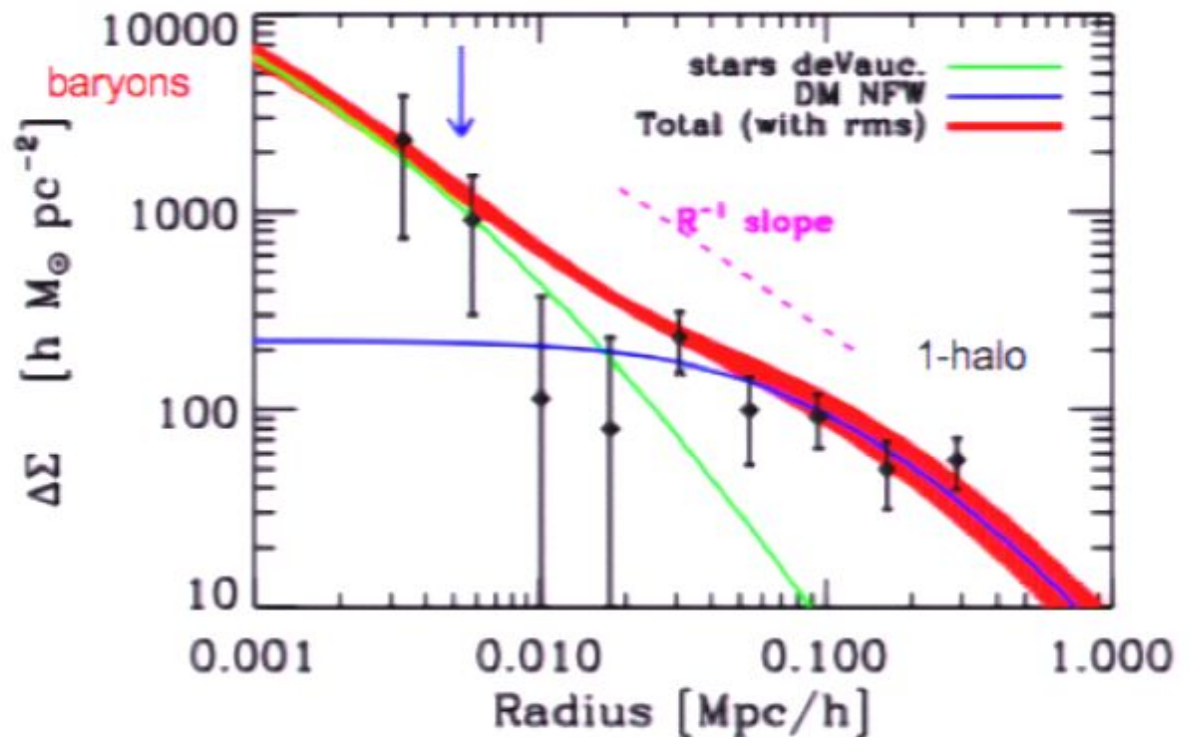
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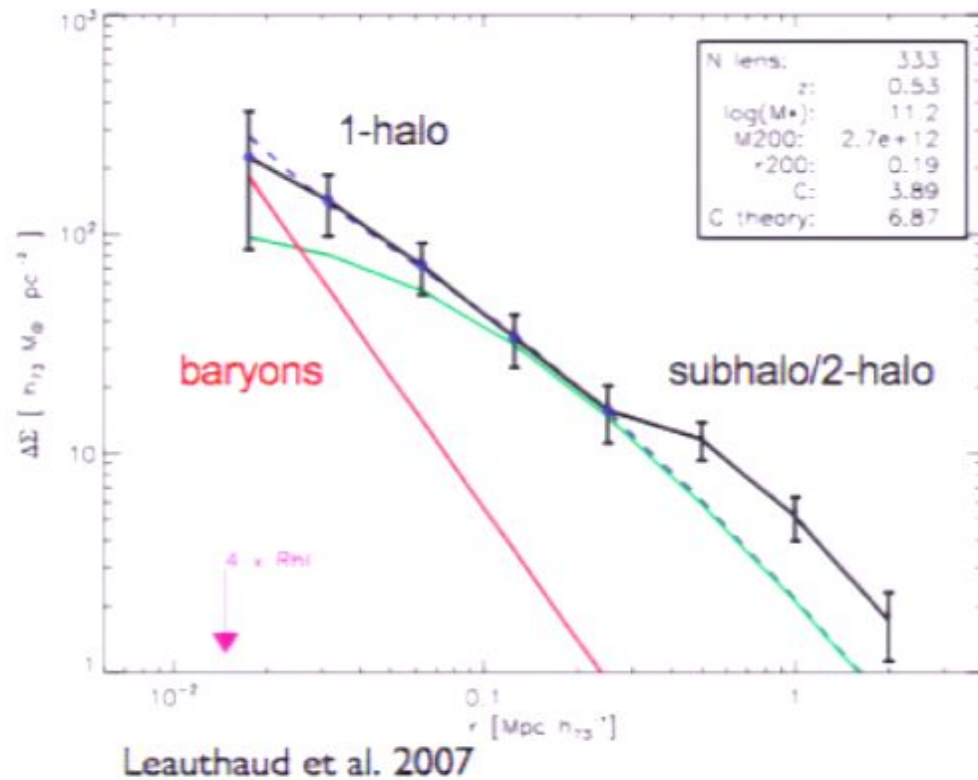
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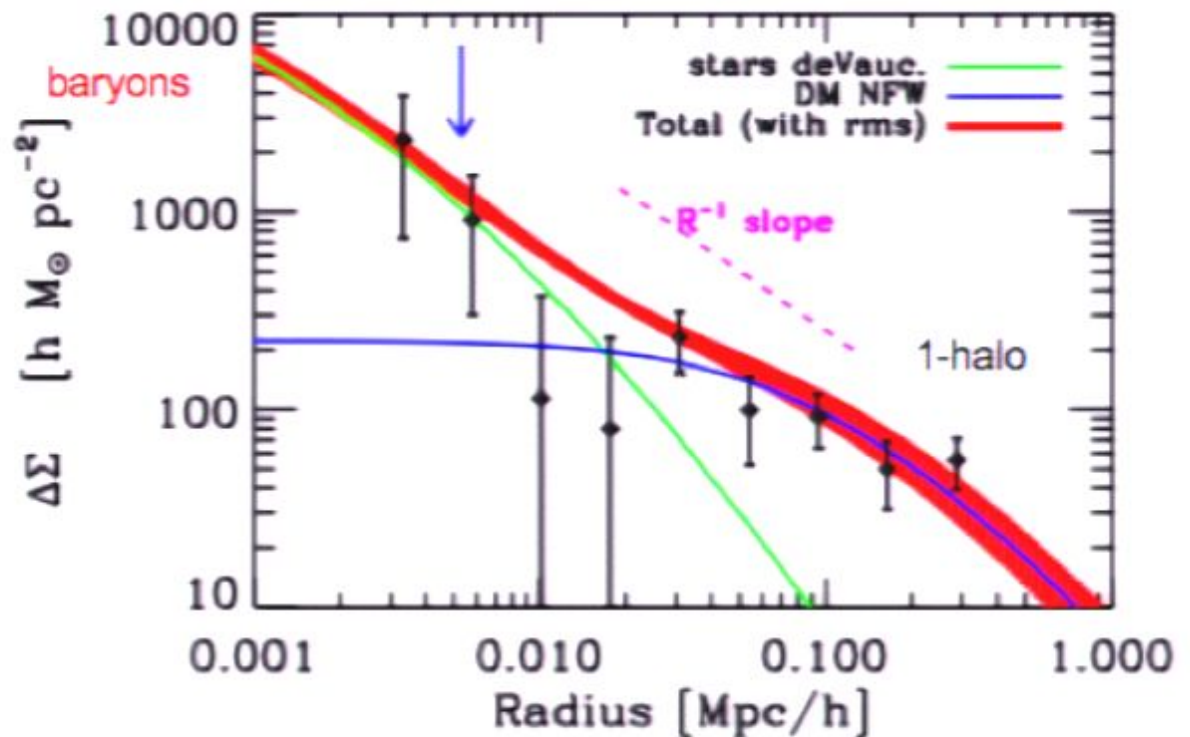
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## II: Detecting Structure on Small Scales

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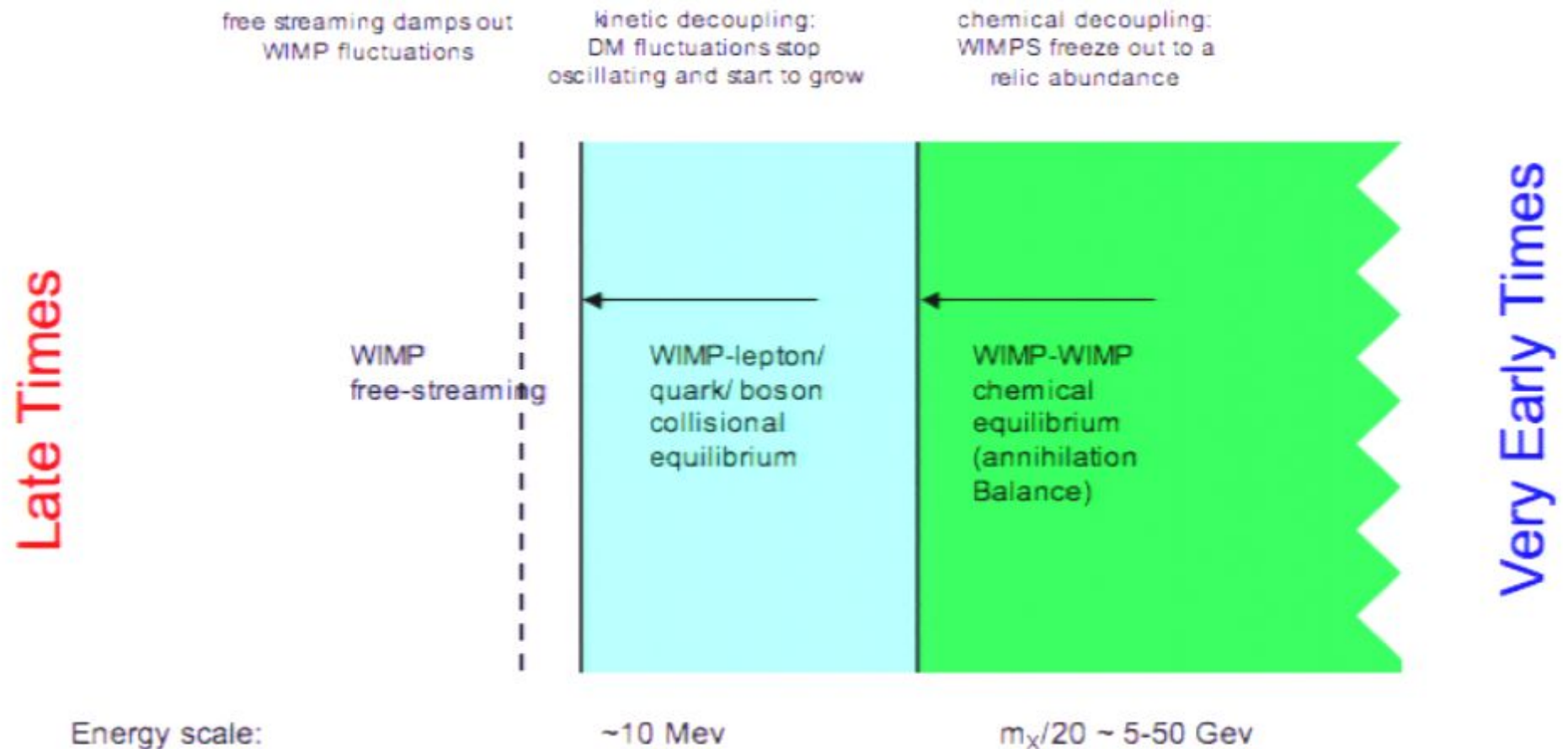
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## II: Detecting Structure on Small Scales

# What are the initial conditions for structure formation?

Consider specific example: supersymmetric WIMP



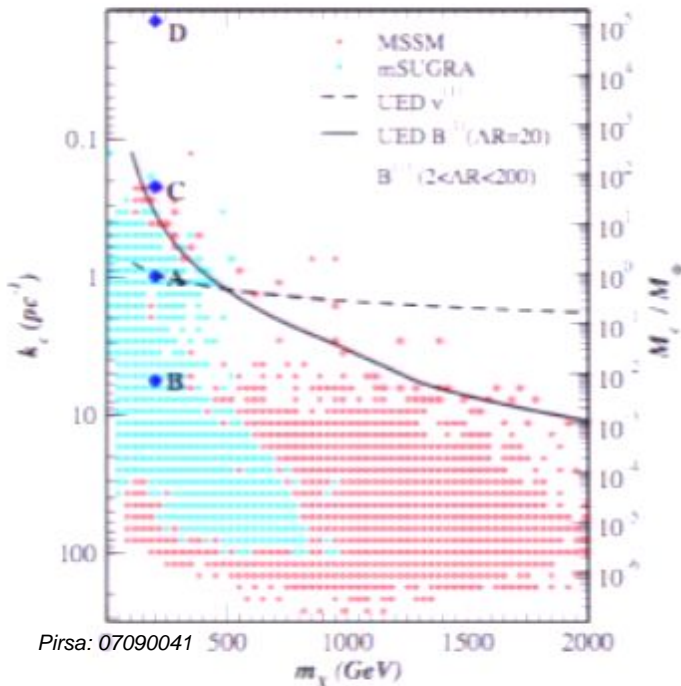
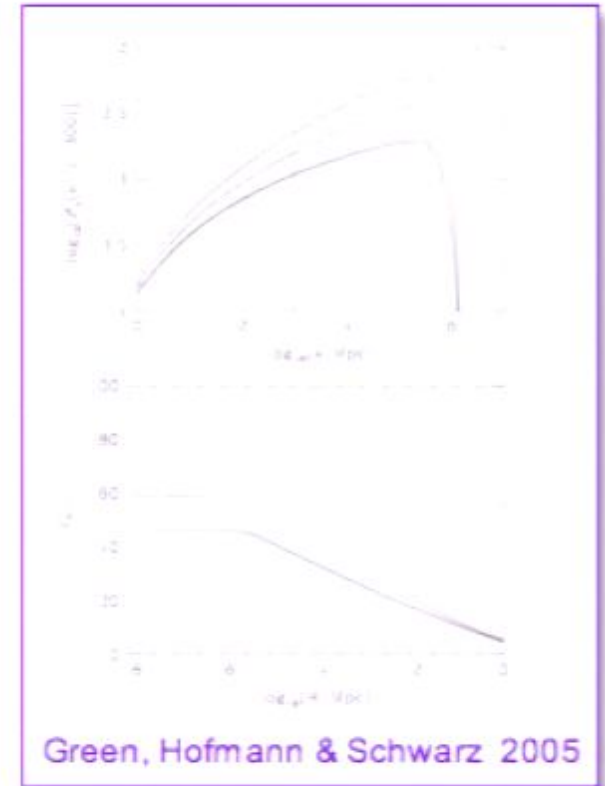
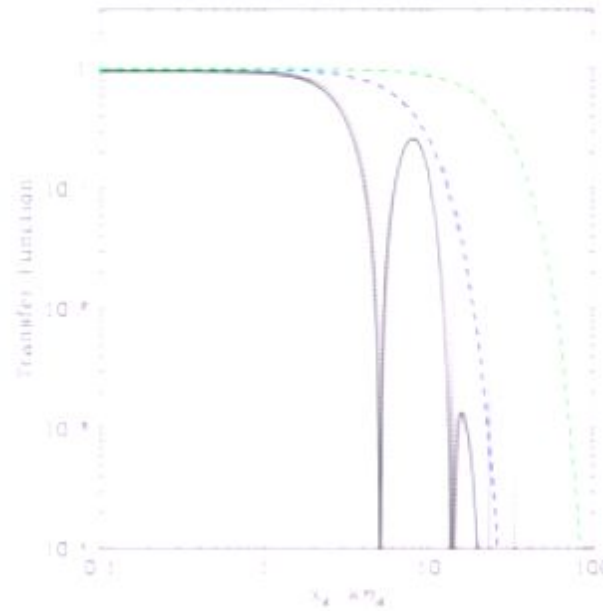
Basic answer: free streaming suppresses fluctuations below some scale, but acoustic oscillations also contribute  $\Rightarrow$  minimum halo mass  $M_c$

e.g. Loeb & Zaldarriaga (2005):

approximate calculation of transfer function due to collisional damping

dominates over free streaming in case considered (100GeV WIMP w.  $T_d = 10\text{MeV}$ )

gives cutoff mass  $M_c = 10^{-4} - 10^{-5} M_\odot$



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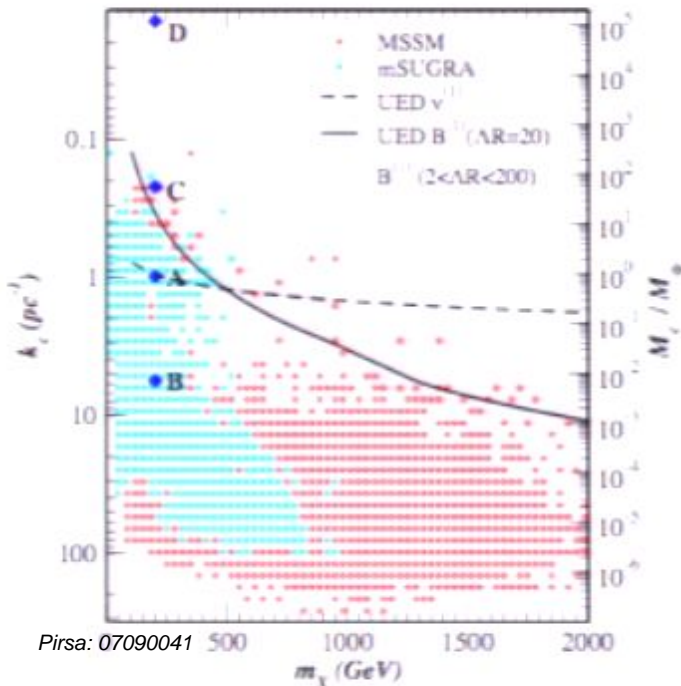
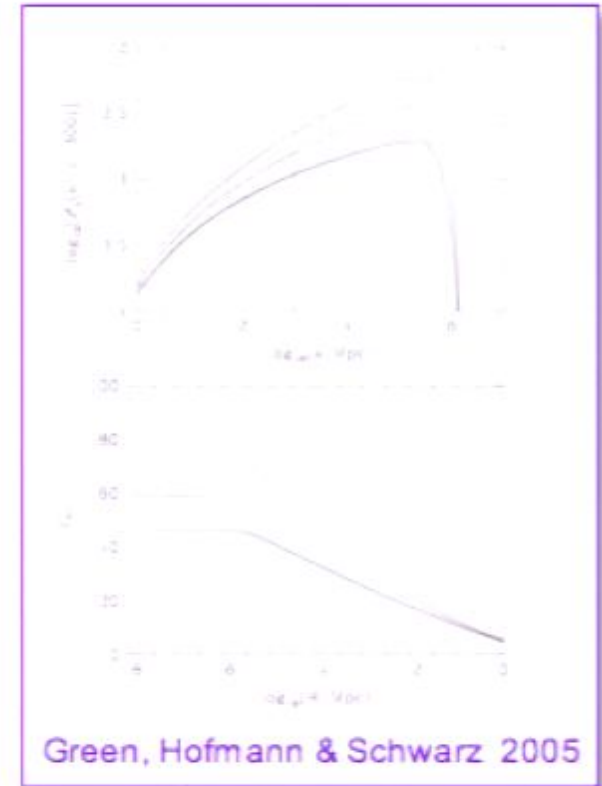
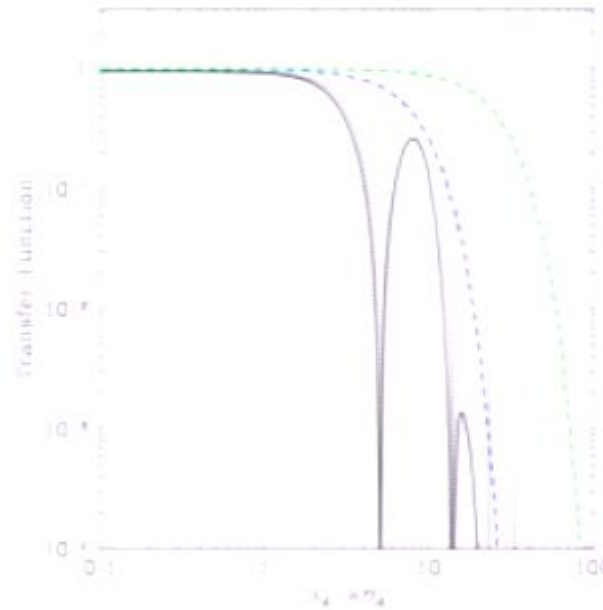
So smallest scale dark matter structure encapsulates DM particle properties (via  $M_c$ ) and possibly also inflaton properties (via  $\rho$  or  $z_f$ ) (e.g. Zentner & Bullock 2002, 2003)

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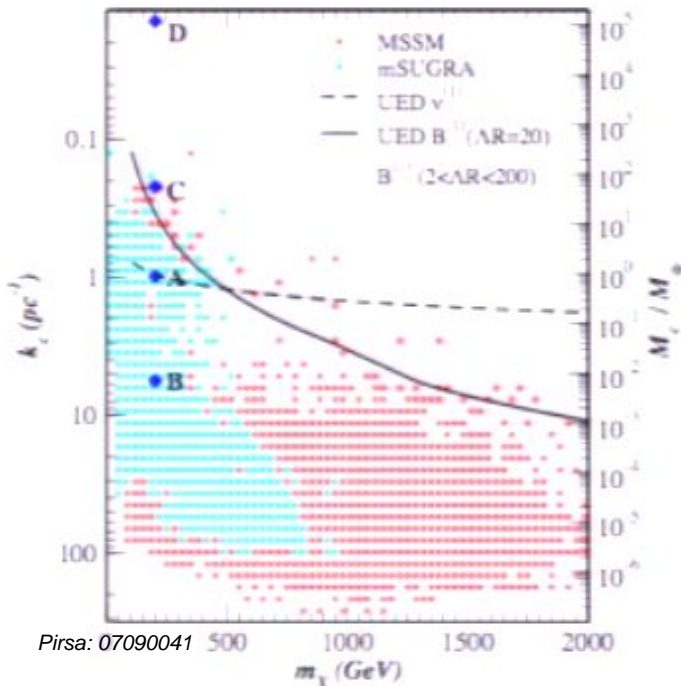
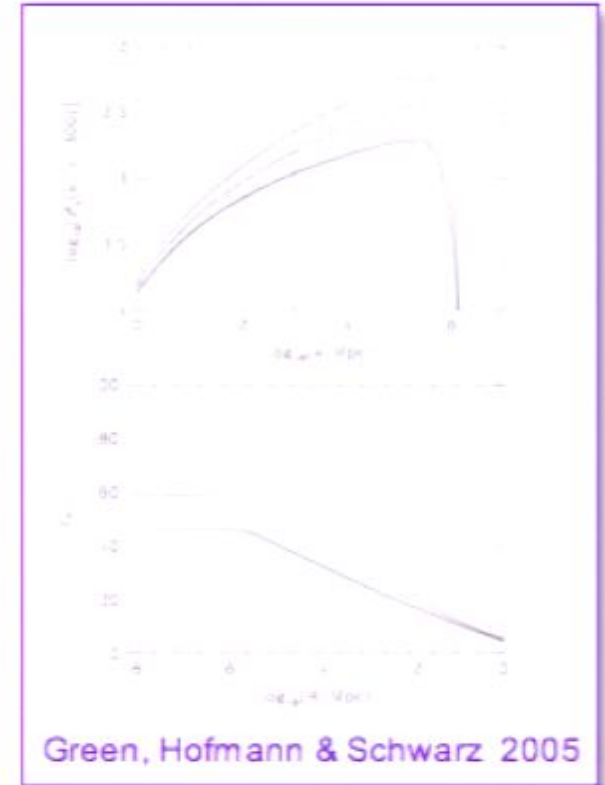
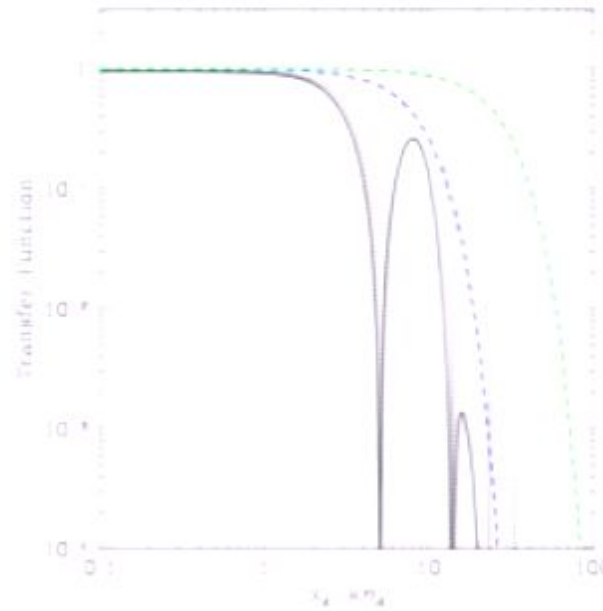
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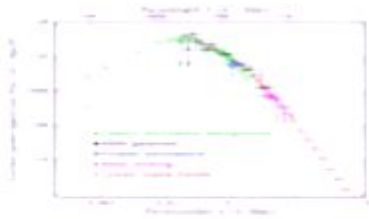
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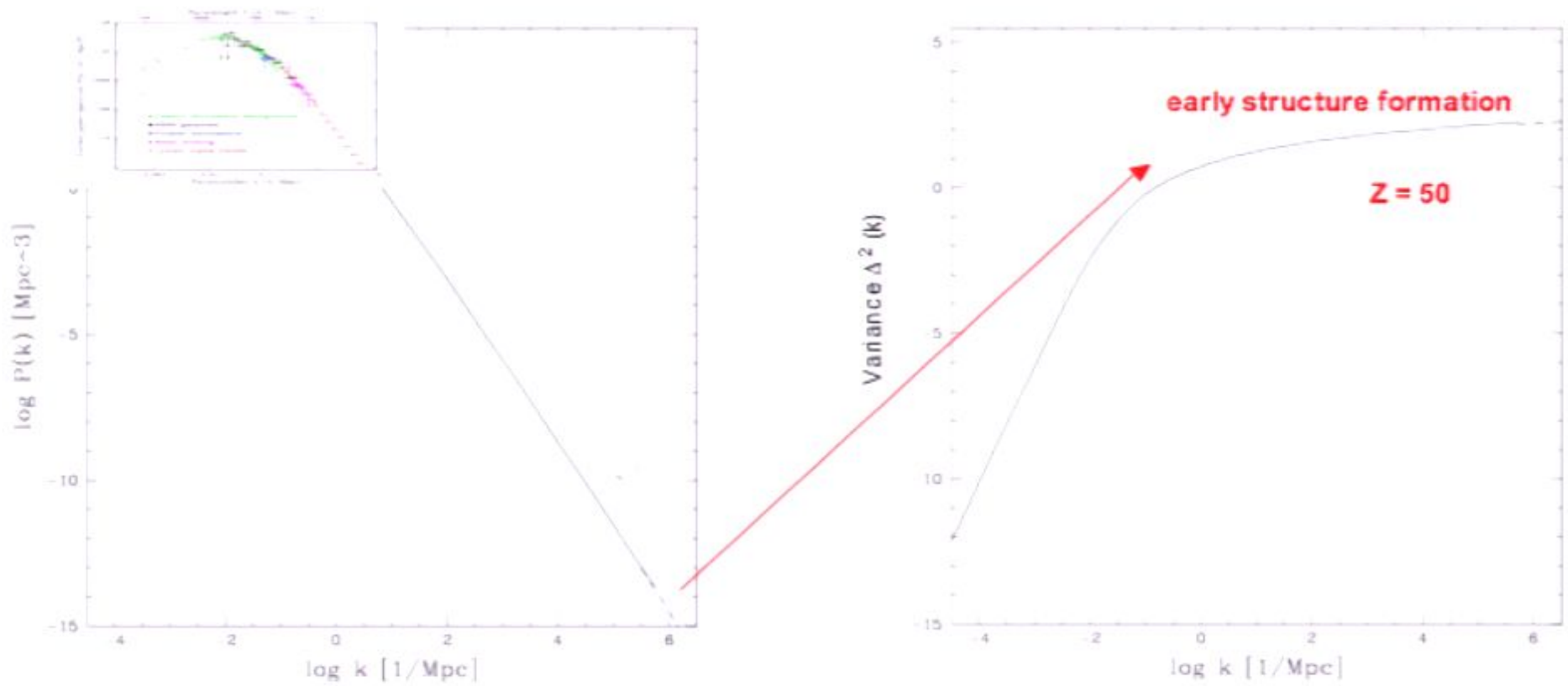
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# The Resulting Non-linear Power: Theoretical Expectations

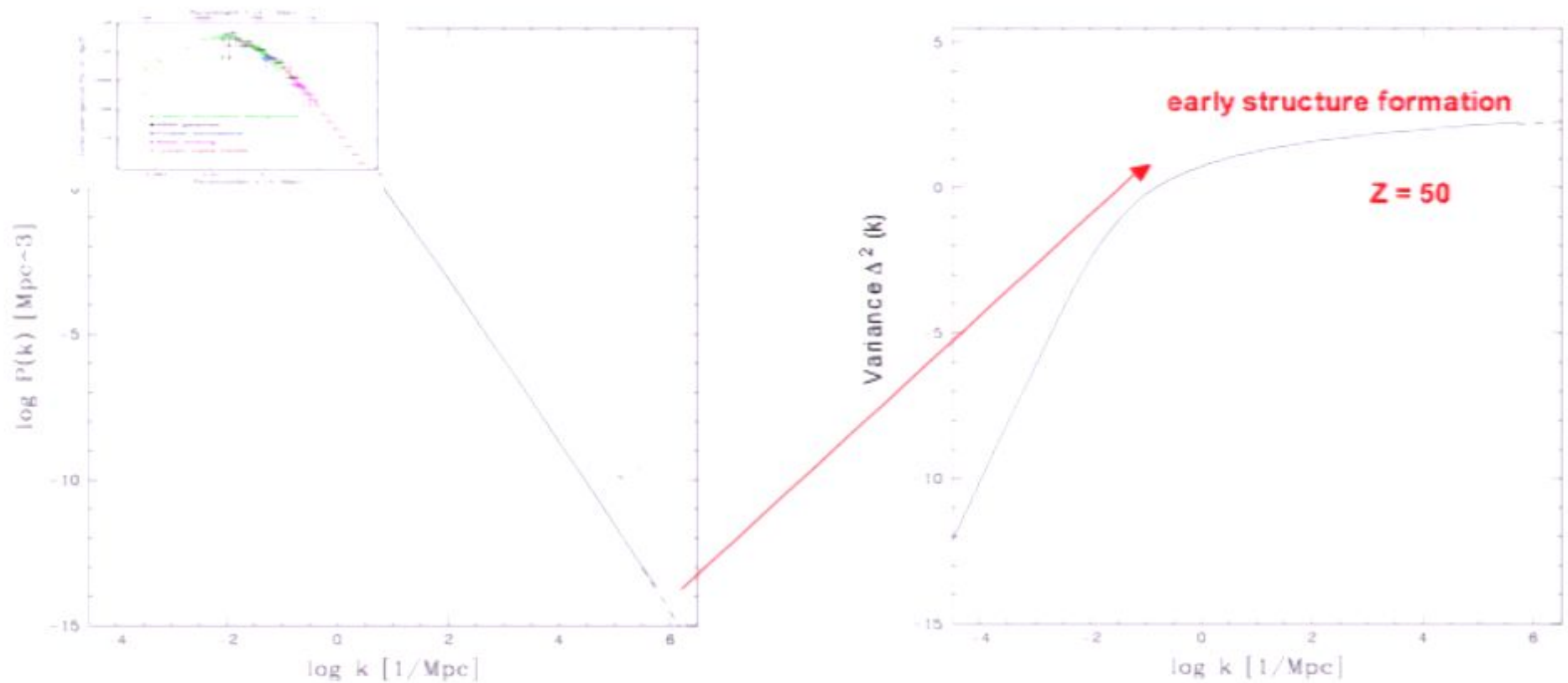




# The Resulting Non-linear Power: Theoretical Expectations



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From linear power spectrum and subsequent growth history, expect **scale invariance** over  $\sim 20$  orders of magnitude in mass

But effect of flattening of variance vs. mass?

Diemand et al. (2005): first numerical attempt w. small box, stopping at high z

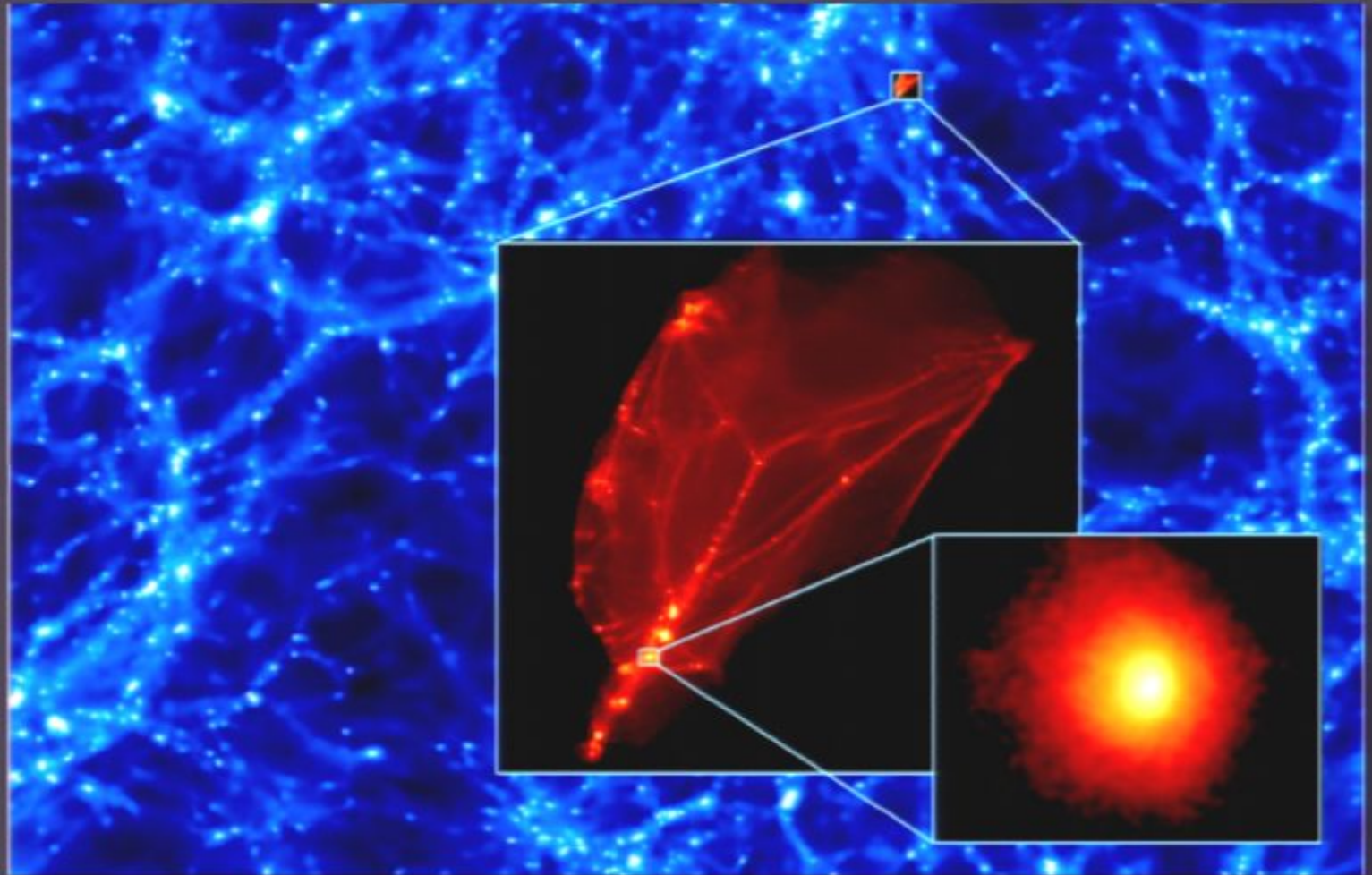
Consider linear power spectrum with  $M_c = 10^{-6} M_\odot$

Start at  $z=350$

Zoom in:

Simulate  $[3 \text{ kpc}]^3$  box,  $[60 \text{ pc}]^3$  sub-box and  $[0.024 \text{ pc}]^3$  sub-sub-box with  $6 \times 10^7$  particles of mass  $10^{-10} M_\odot$  each

Find  $10^{-6} M_\odot$  'first' halo  
With  $M \sim M_c$



Profile, density as expected from theory

(Diemand et al. 2005)

Halo profile  $\sim$  universal;  
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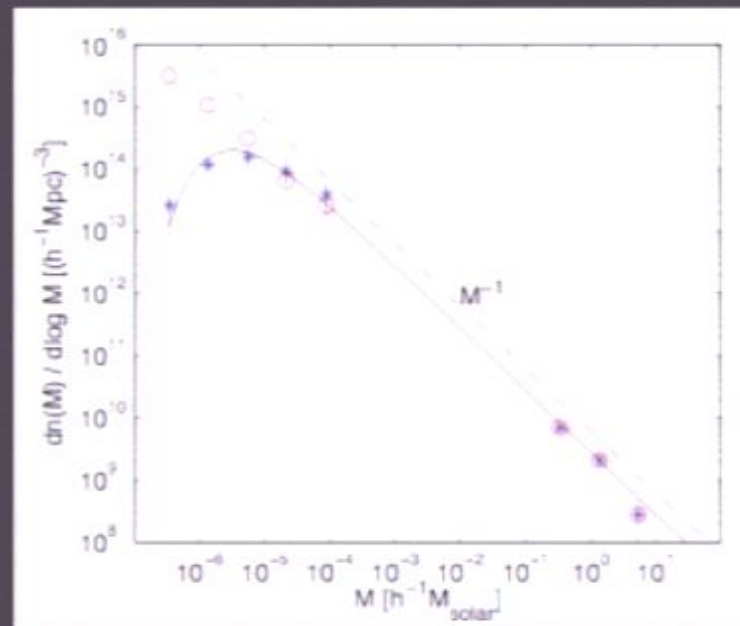
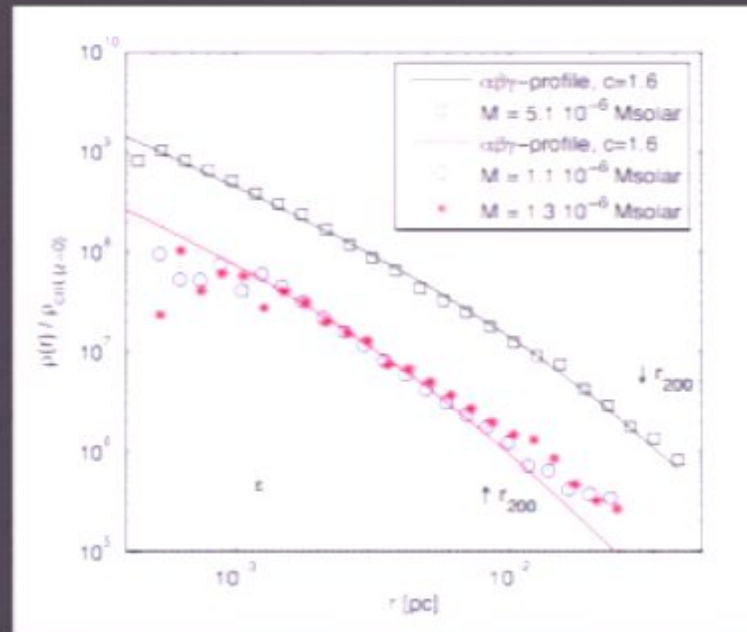
Also abundance matches  
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**Implication:** following scaling  
for more massive substructure,  
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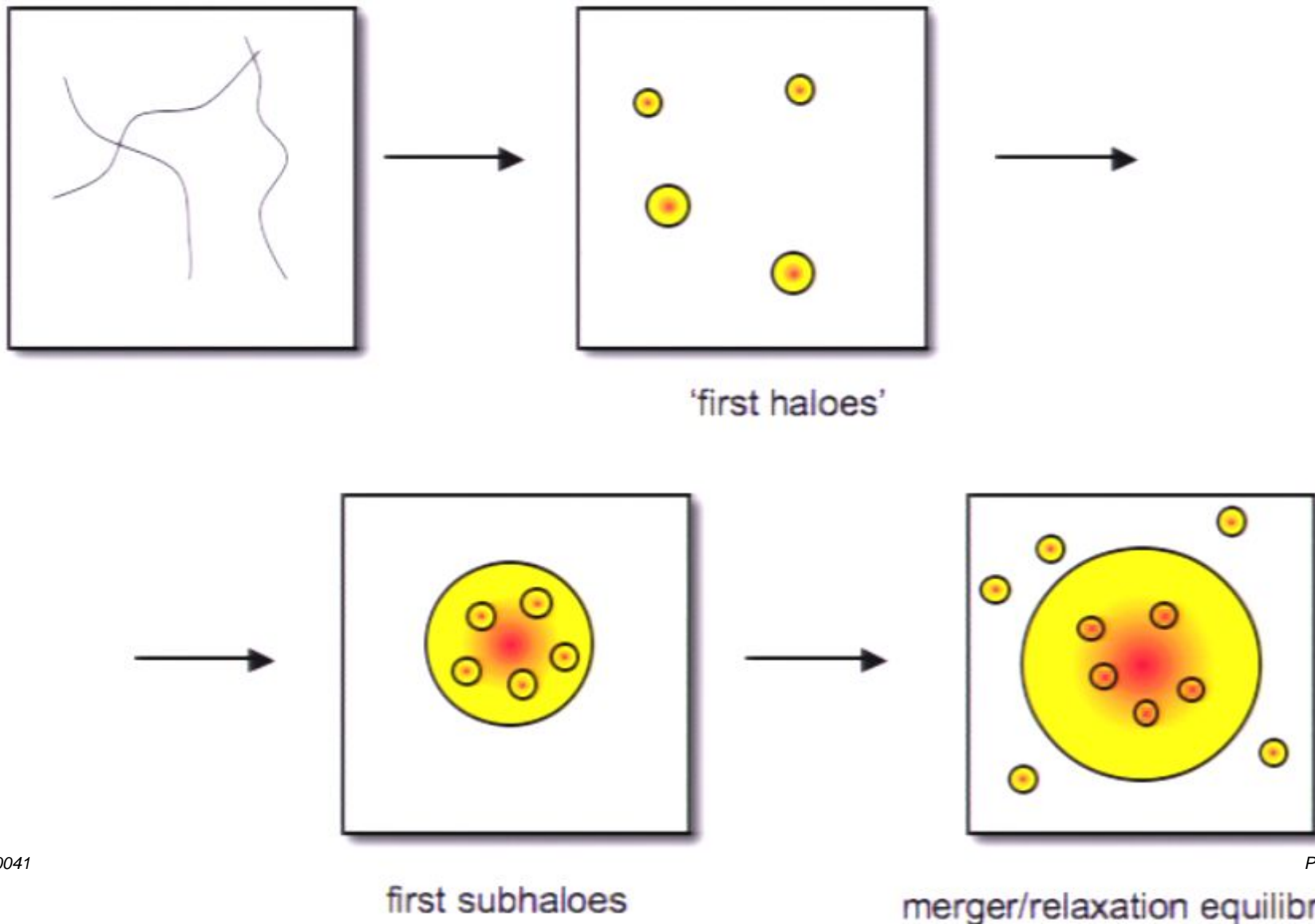
Further implications for direct and  
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These objects move through solar  
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Motion on sky  $\sim 1$  arcmin/yr



Given an initial spectrum, how does small-scale structure evolve subsequently?



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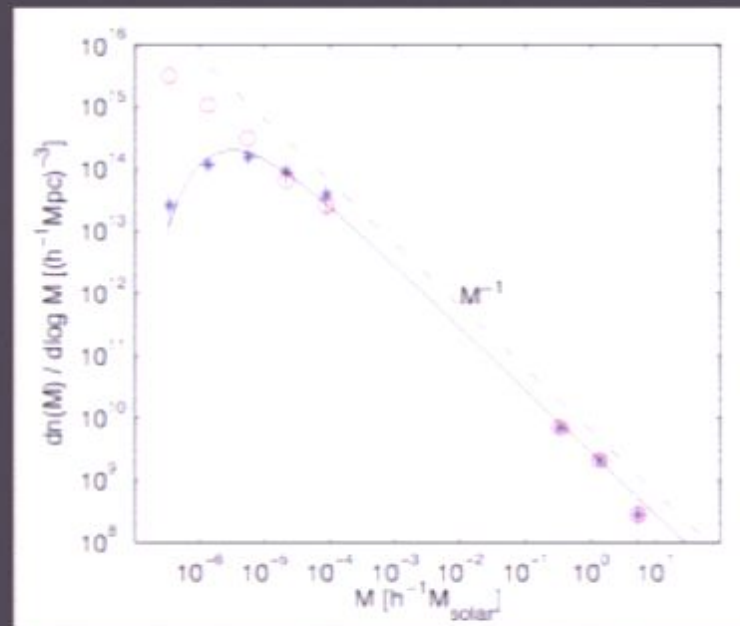
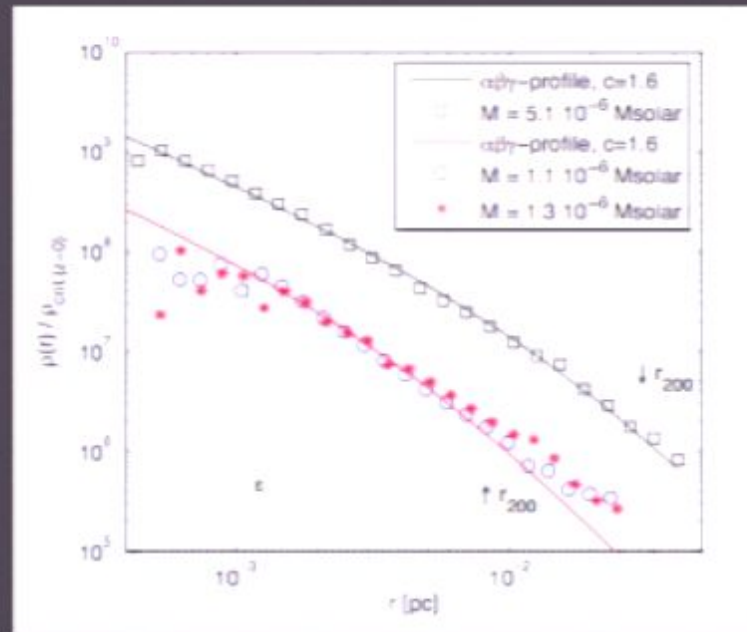
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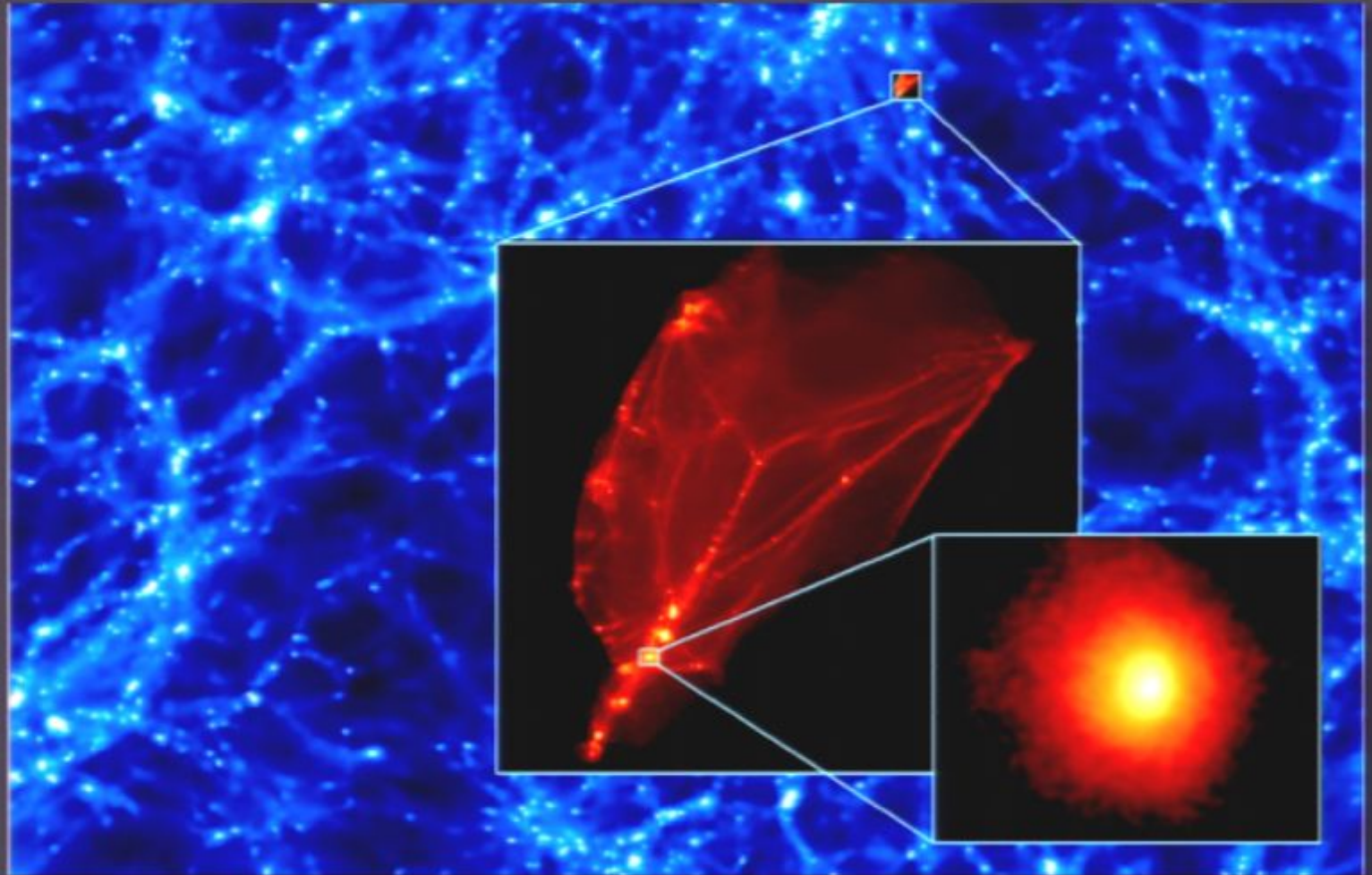
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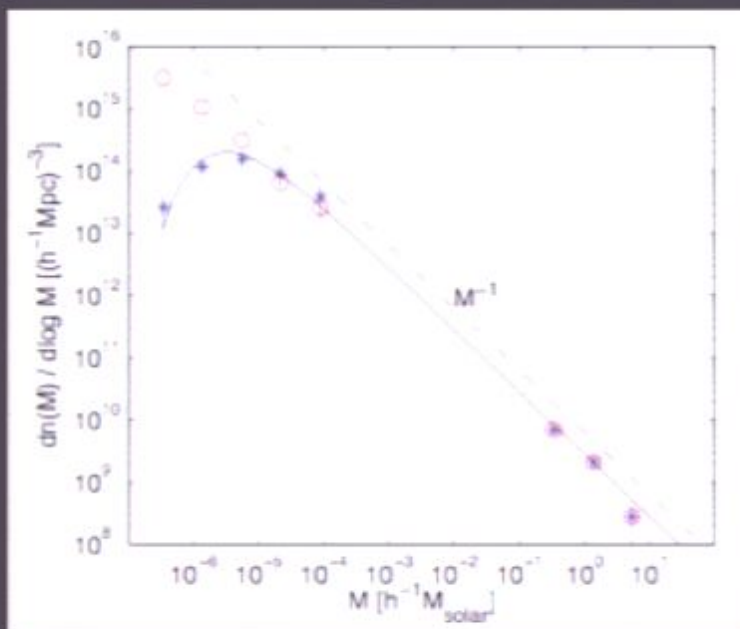
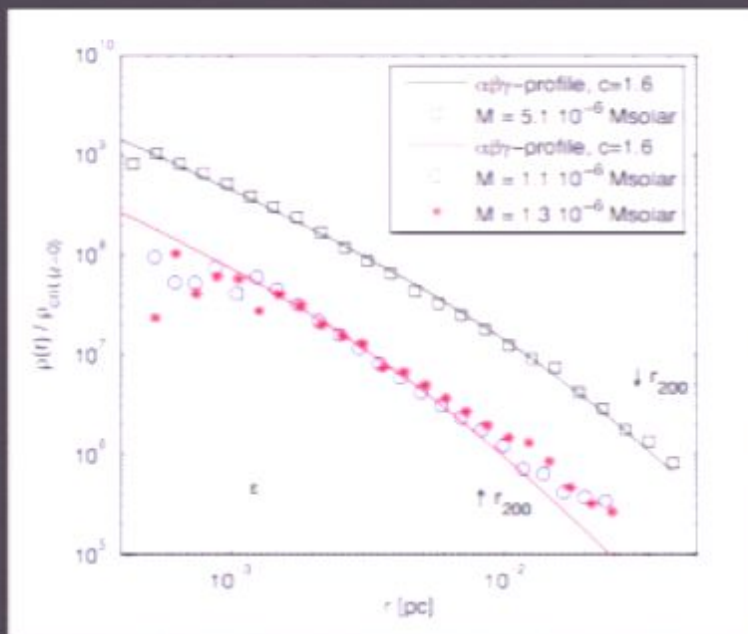
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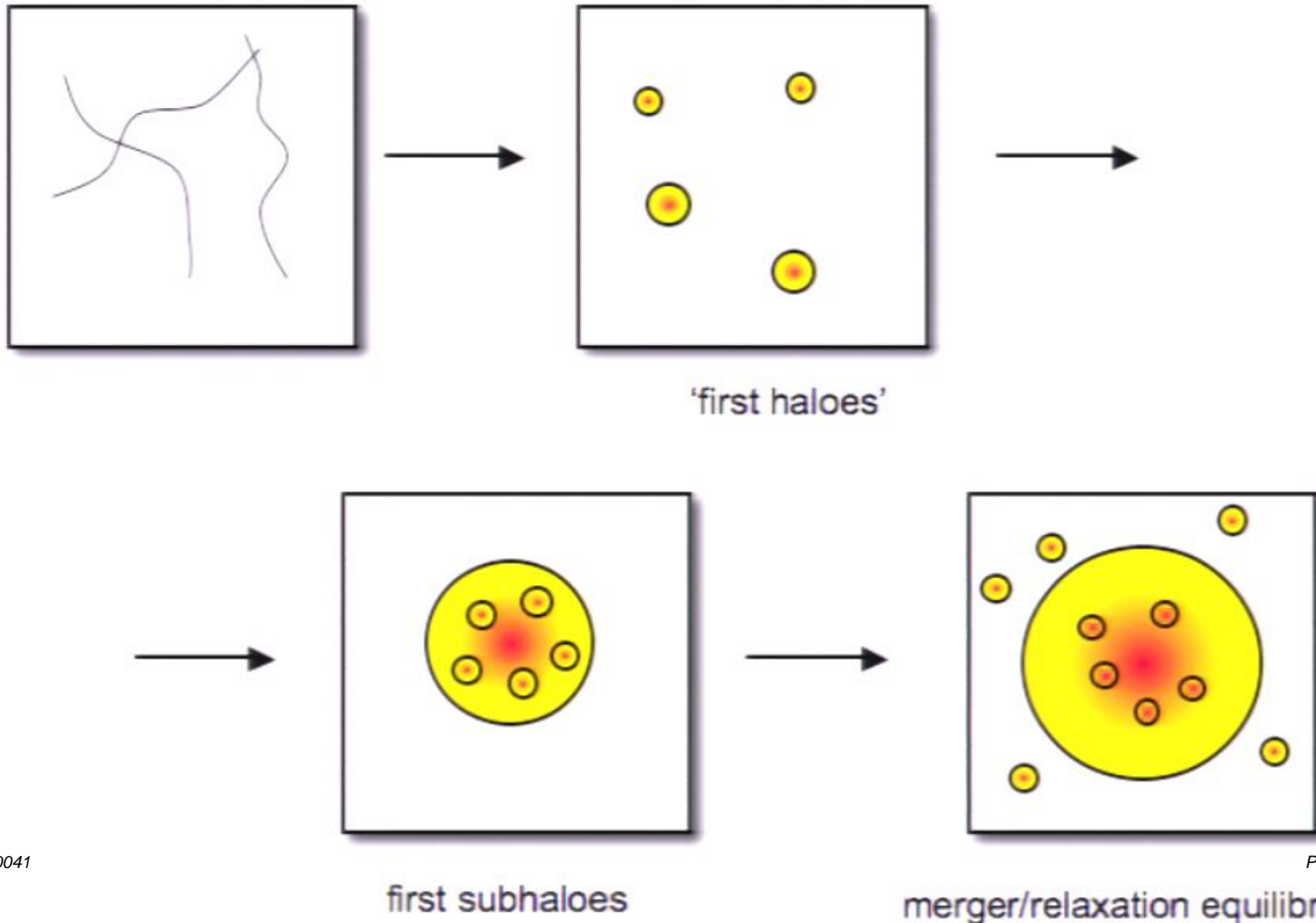
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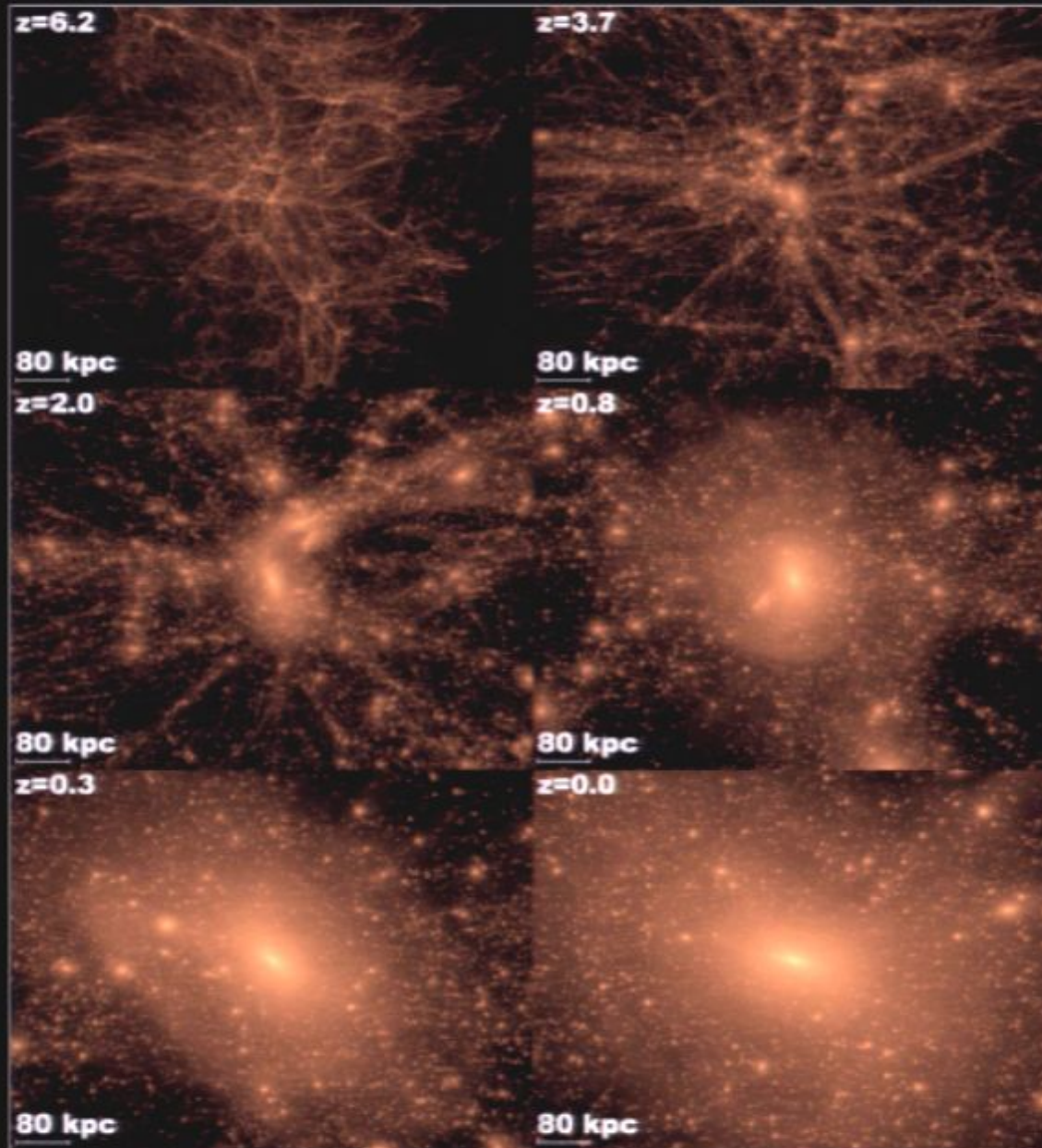




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# How to model small scales

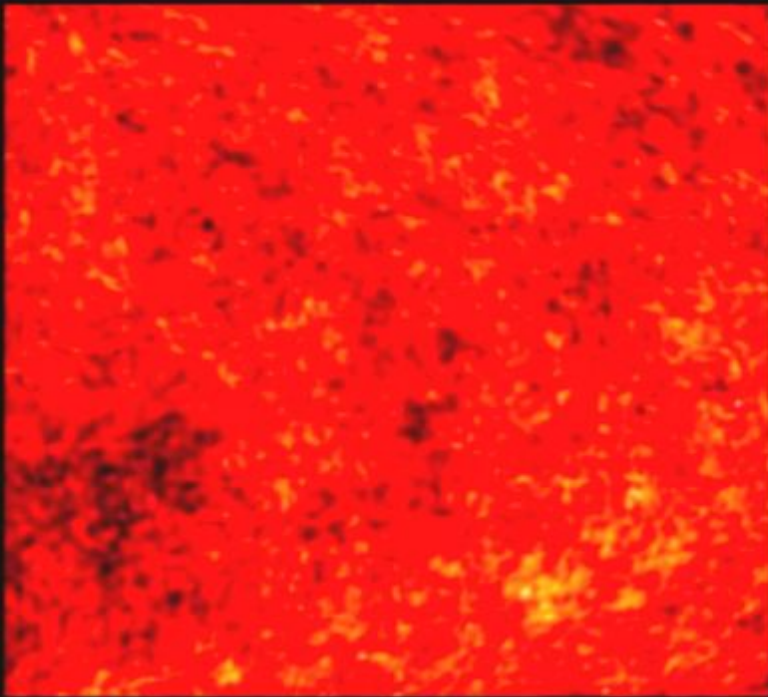


Fundamental  
resolution  
limit  
← mixing

## A statistical approach to the non-linear regime

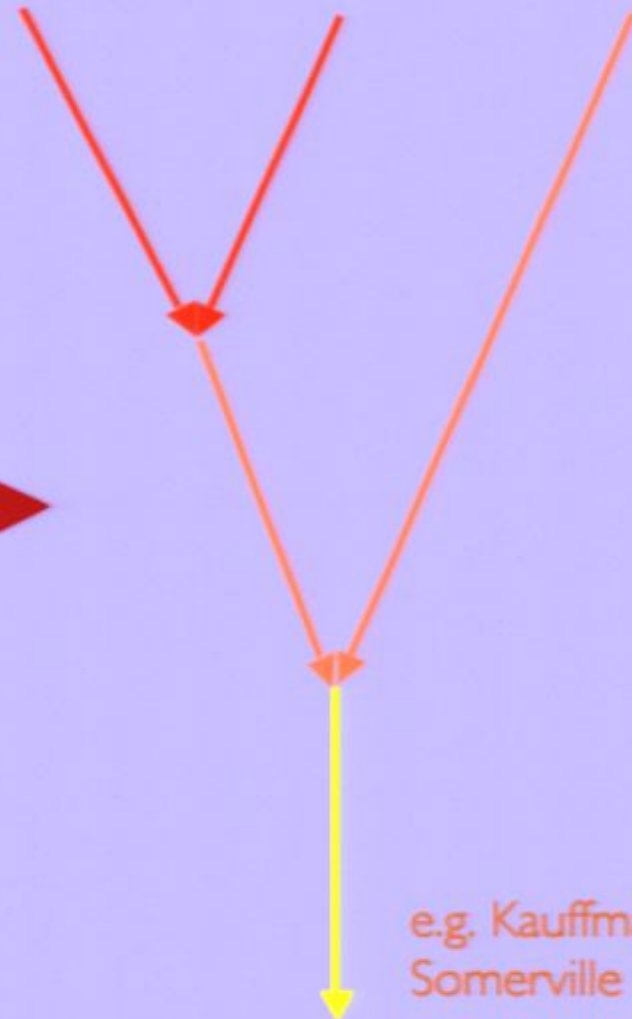
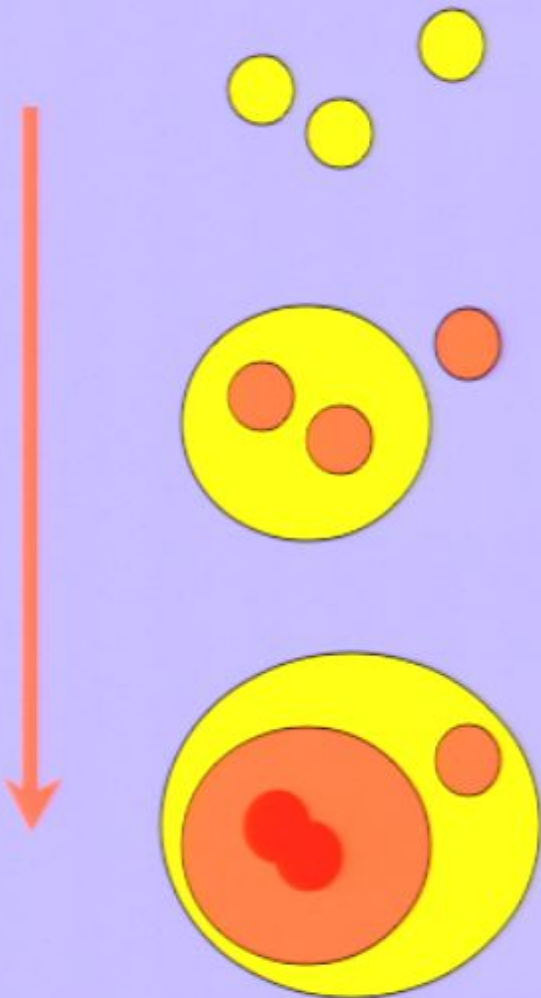
Can't calculate full evolution of non-linear regime without N-body simulations, but can make statistical estimate of its extent: Press-Schechter theory

=> retain some of the power of linear theory to constrain parameters



# Representing hierarchical non-linear growth: semi-analytic merger trees

Iterated Press-Schechter calculations give  
Mass Accretion Histories and merger statistics



e.g. Kauffmann et al.  
Somerville & Kolatt

## Alternate Merger Tree Approach (w. Abel & Turk):

Basic resolution problem with trees:

Number of branches grows as  $\sim N \log(N)$ , where  $N = M/M_{\text{res}}$

Number of distinct redshift steps grows as  $N^2$  or faster

So rather than following every branch, choose some preferentially,  
e.g. with declining probability at low mass

e.g. branching probability = 1 for  $M > M_1$

=  $M/M_1$  for  $M_2 > M > M_1$

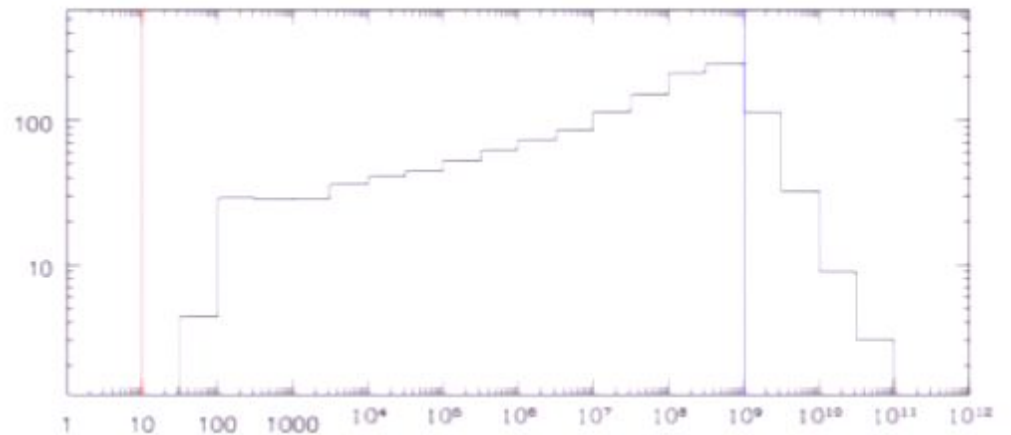
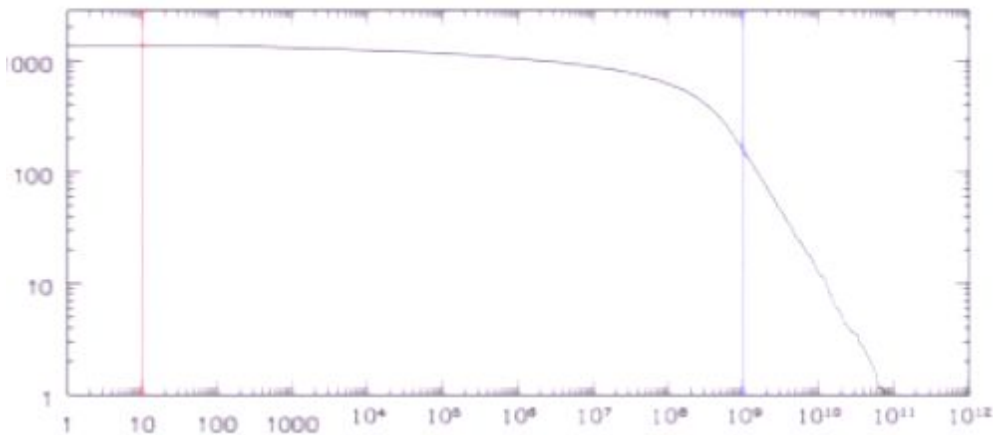
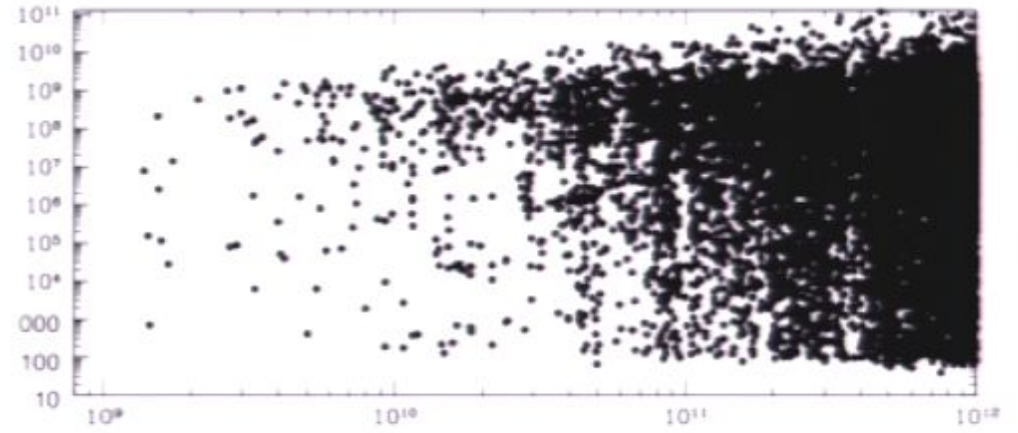
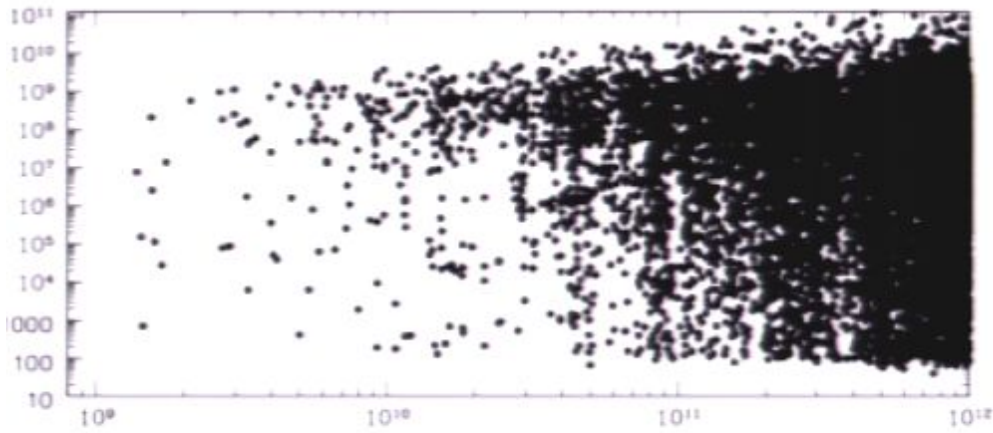
= 0 for  $M < M_2$

Get fast trees for  $M_f/M_1 \sim 10^3$ ,  $M_1/M_2 \sim 10^8$

Use this as input to semi-analytic model of halo mergers and substructure evolution



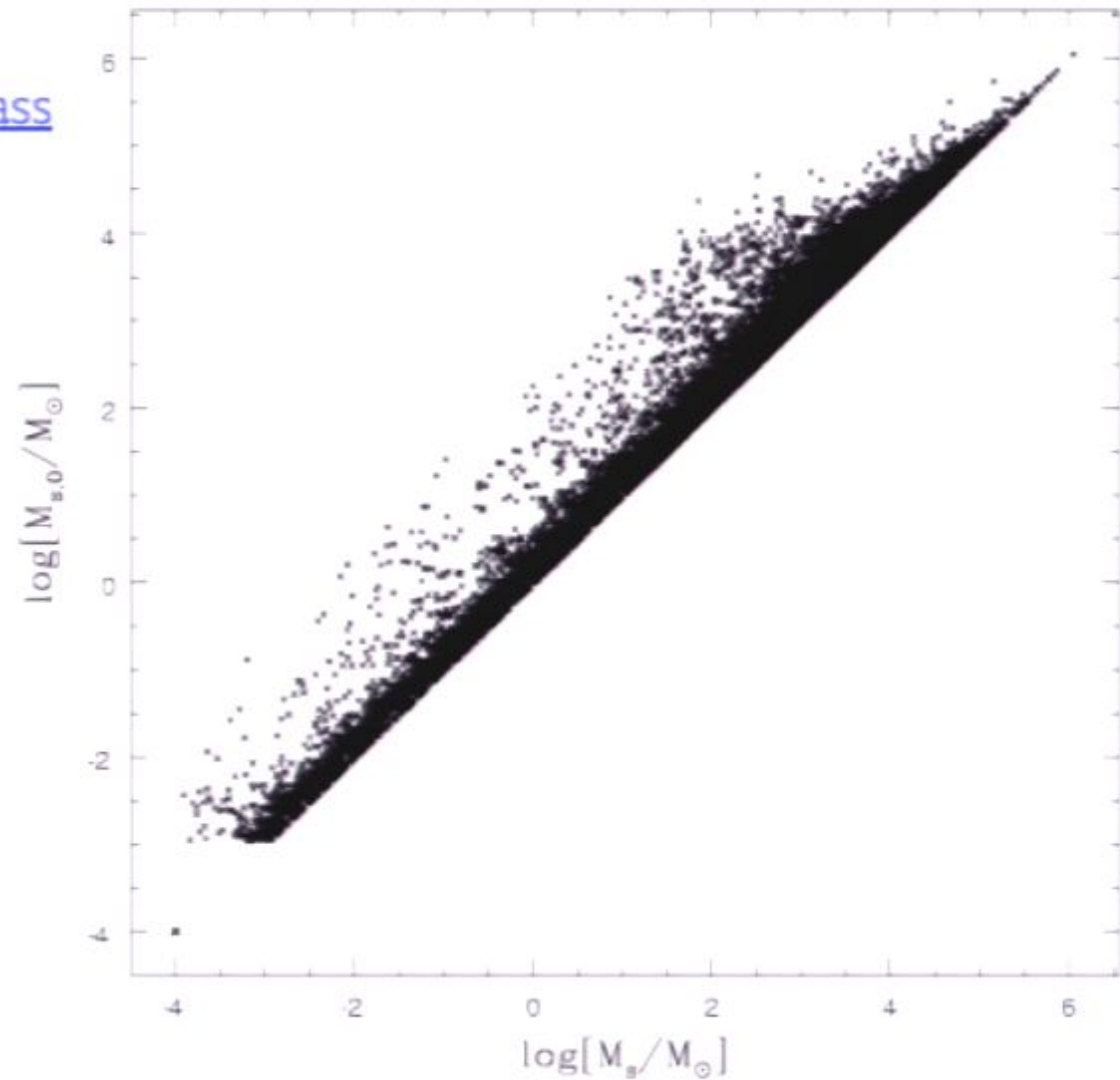
## Sparsely-sampled Trees:



## Some Results from Small Scales ( $\sim R < R_{\text{Sun}}$ )

1: Final mass versus initial mass

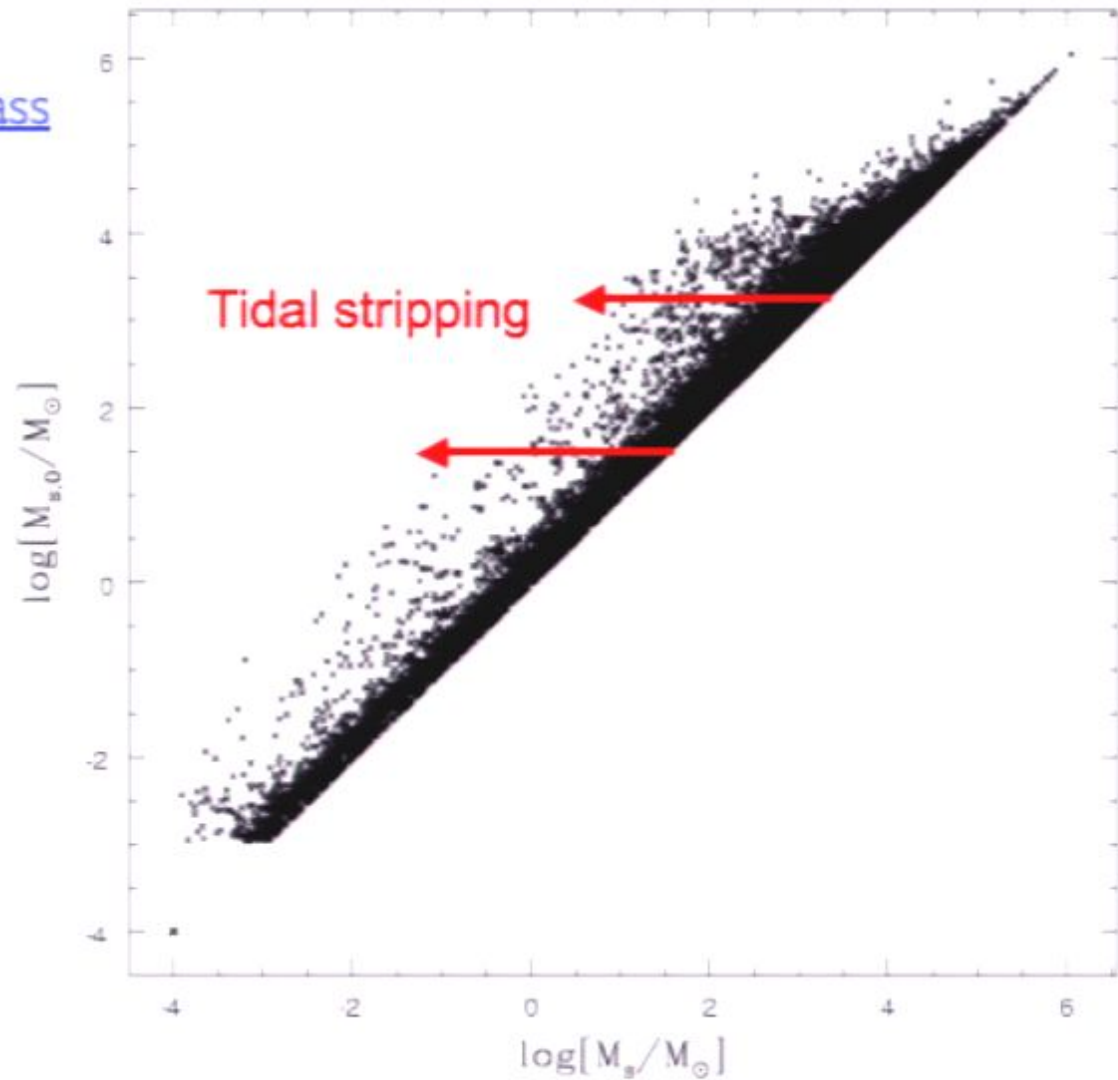
$\Rightarrow$  two orders of magnitude  
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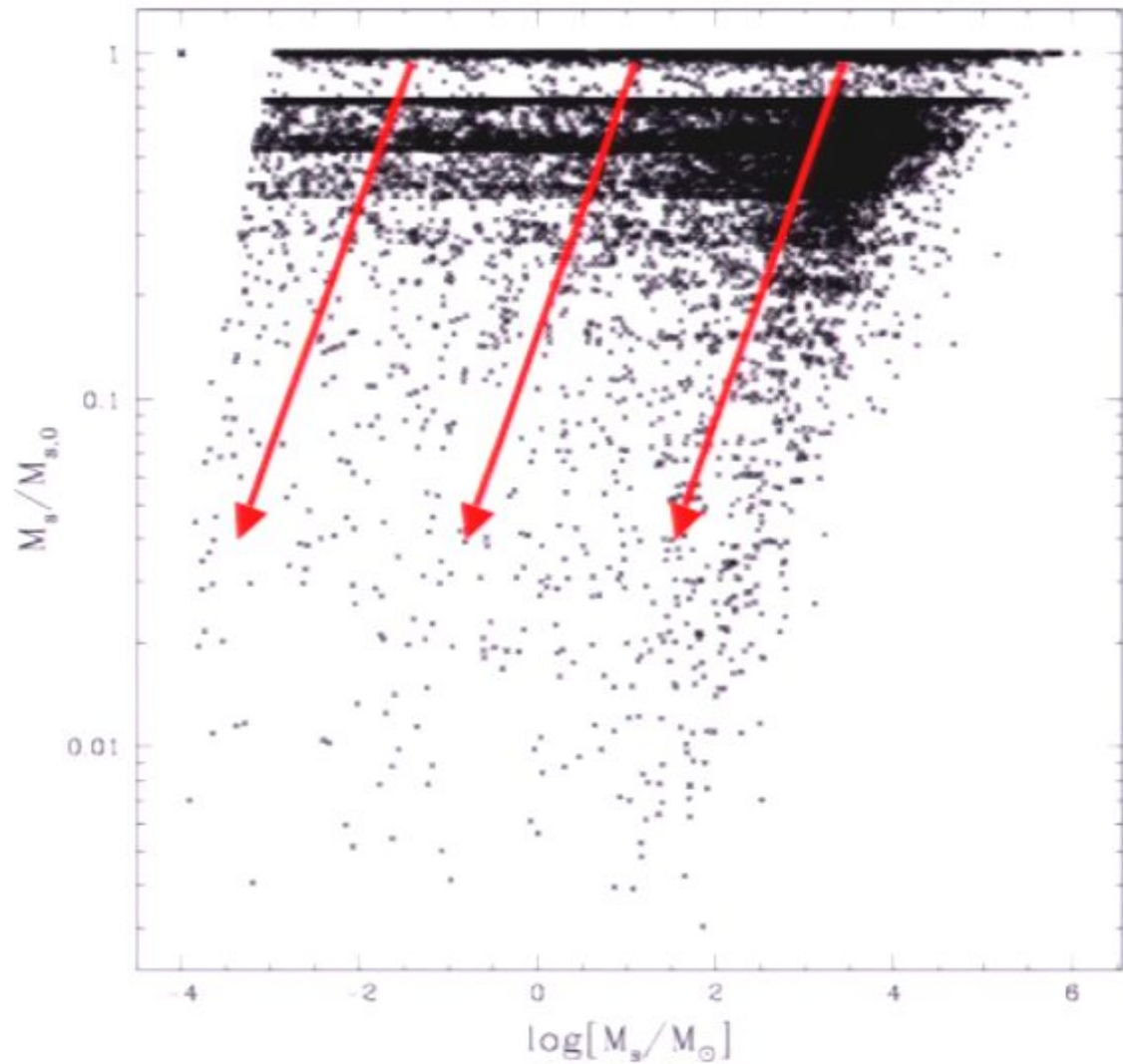


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### 2: Mass loss vs. final mass

$\Rightarrow$  no major trend with mass

$\Rightarrow$  incompleteness in  
merger tree

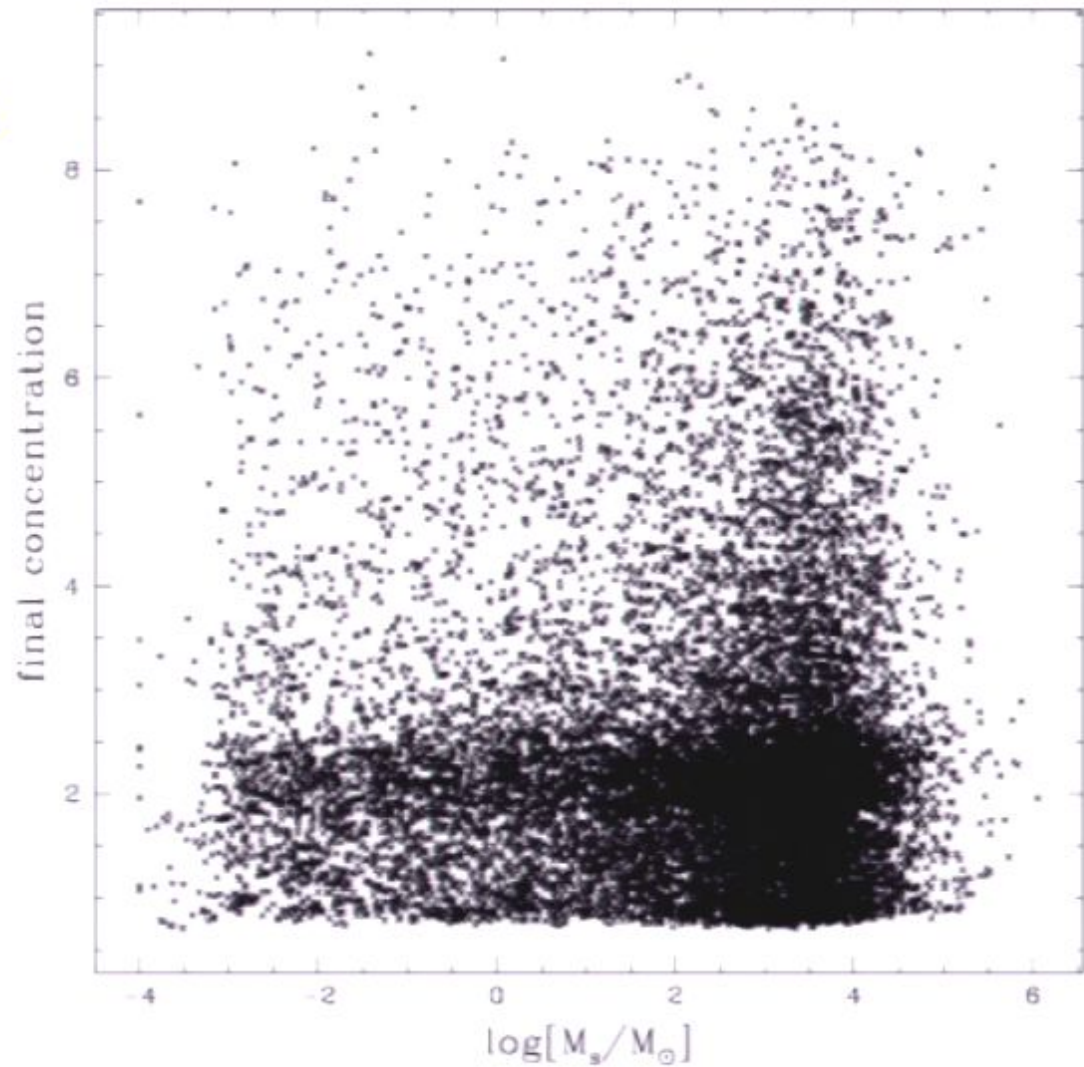


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### 3: concentration vs. final mass

⇒ no major trend with mass

⇒ most systems heavily  
stripped



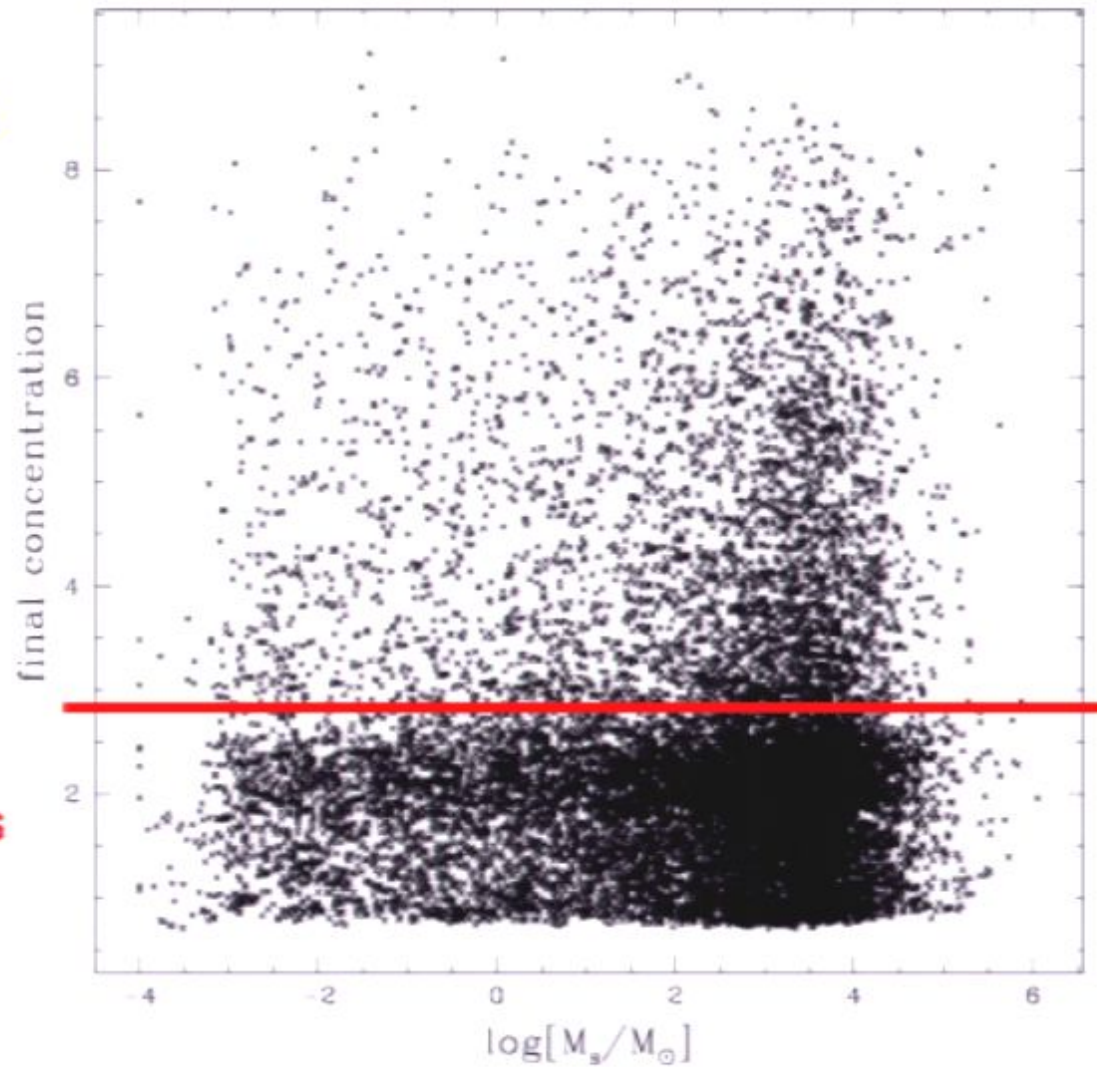
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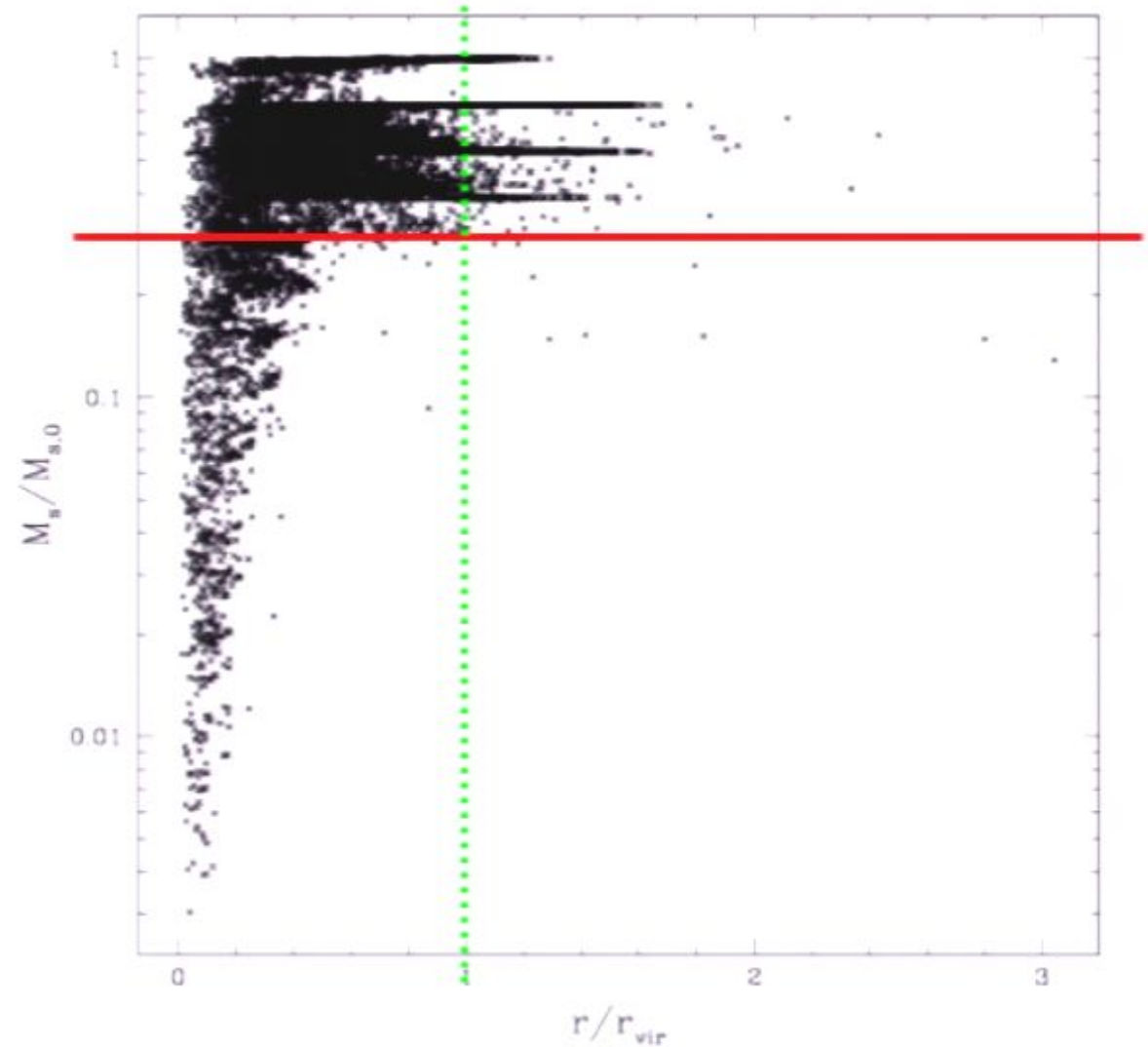
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### 4: mass loss vs. location

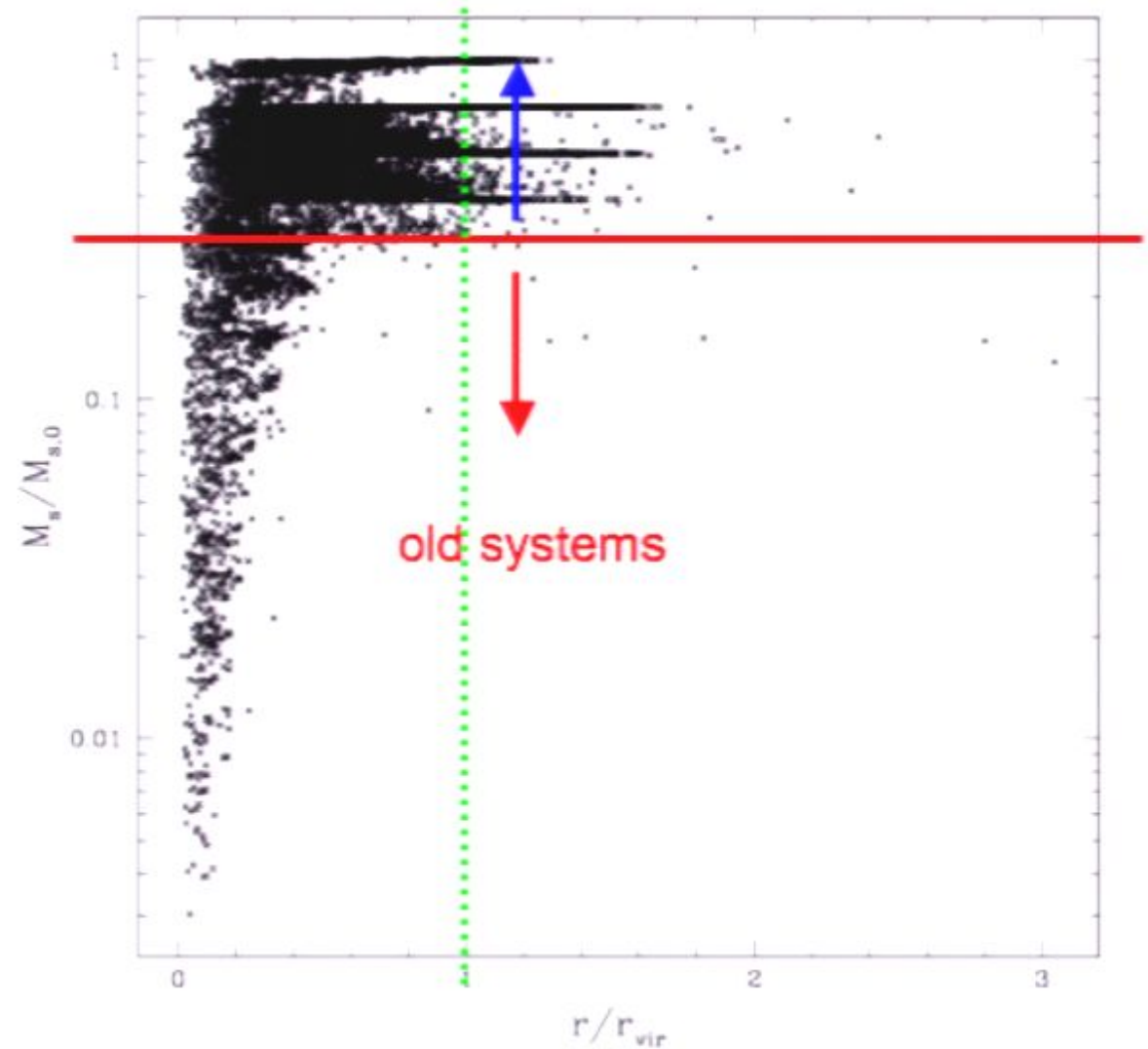
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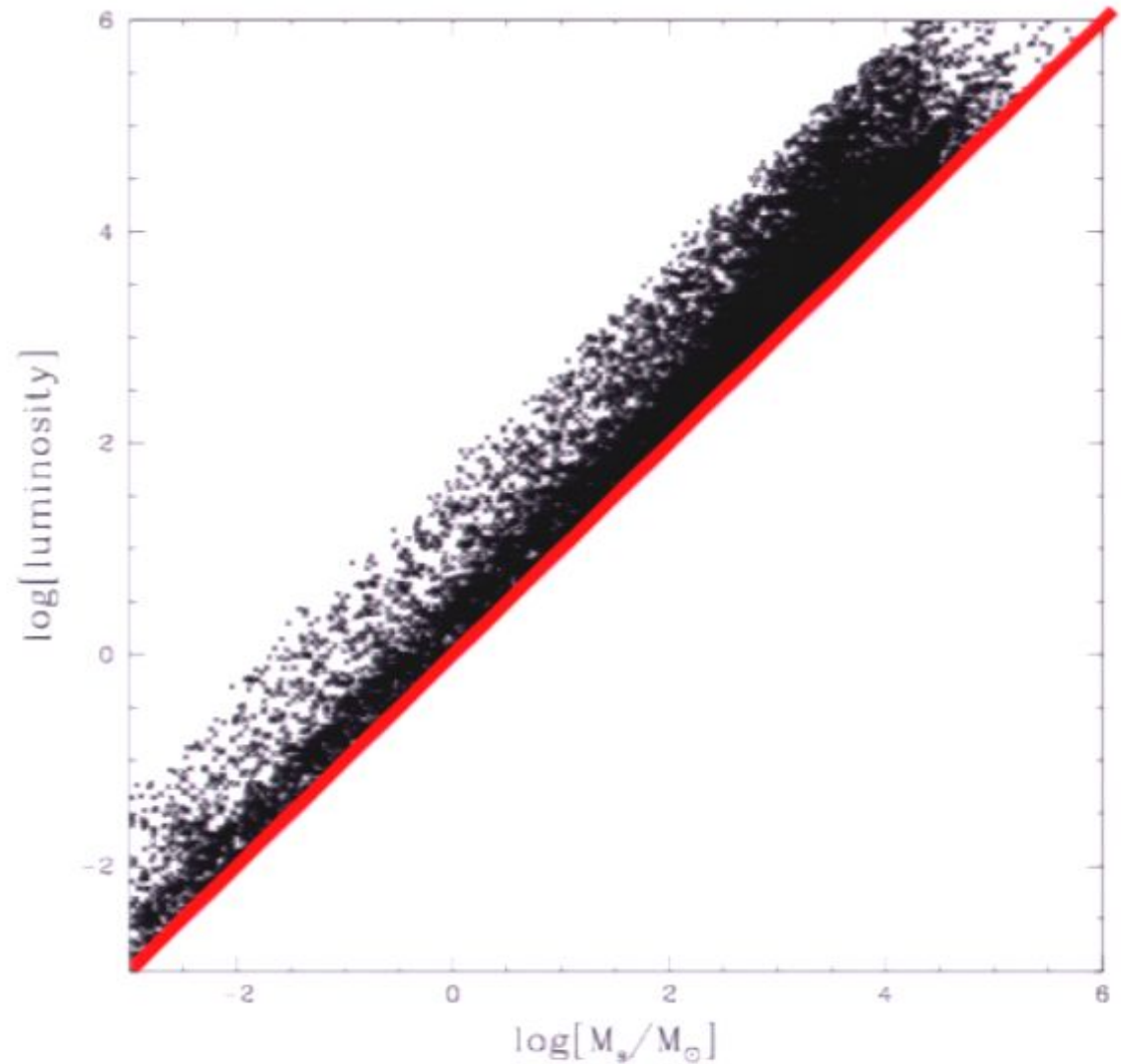


## Some Results from Smaller Scales ( $\sim R < R_{\text{Sun}}$ )

### 5: luminosity vs. mass

$\Rightarrow$  large scatter at fixed mass  
 $\Rightarrow$  massive systems dominate  
however

(N.b. distance  $\propto n^{-1/3}$   
so apparent luminosity  $\propto n^{2/3}$ )



# Small-scale Structure Summary

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- In hard-core CDM, expect structure well below galaxy scale
- Ultimate scale depends on/encodes particle model; could be  $\sim$ planetary mass or smaller
- The first dark matter halos survive as debris in the local solar neighbourhood, but most of mass probably in streams
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# Observational Paths to New Physics

- line-of-sight distances, e.g.  $D_L(a)$  from SNe
- physical scales, e.g. the sound horizon from **Baryon Acoustic Oscillations**
- volumes, e.g. from **cluster number counts**?
- the growth of potential fluctuations (**ISW**)
- the growth of linear fluctuations (**cosmic shear**)
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- the **differential growth** of non-linear structure

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geometry

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geometry



growth of structure

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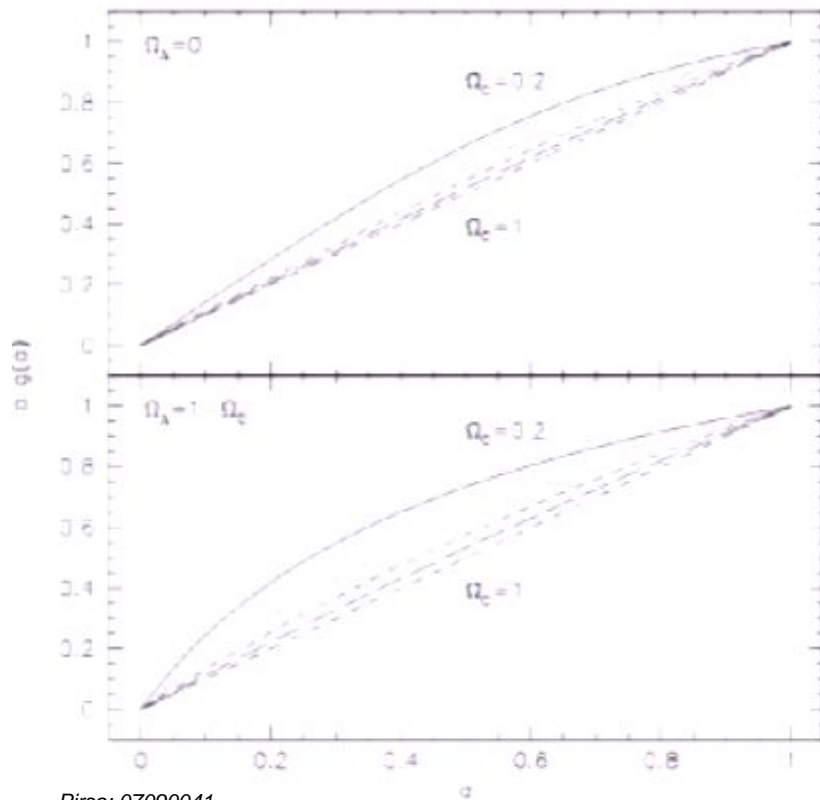
} growth of structure

Both ultimately measure  $H(a)$  or  $\Sigma\Omega_i(a)$ ,  
but with very different redshift weighting,  
+ different relation to standard GR gravity.

# The value of multiple constraints (cf. Linder 2005)

Can modify the Friedman equation  $H(a)$  either by changing the *equation of state of dark energy* or by *modifying gravity*; either could produce exactly the same expansion history.

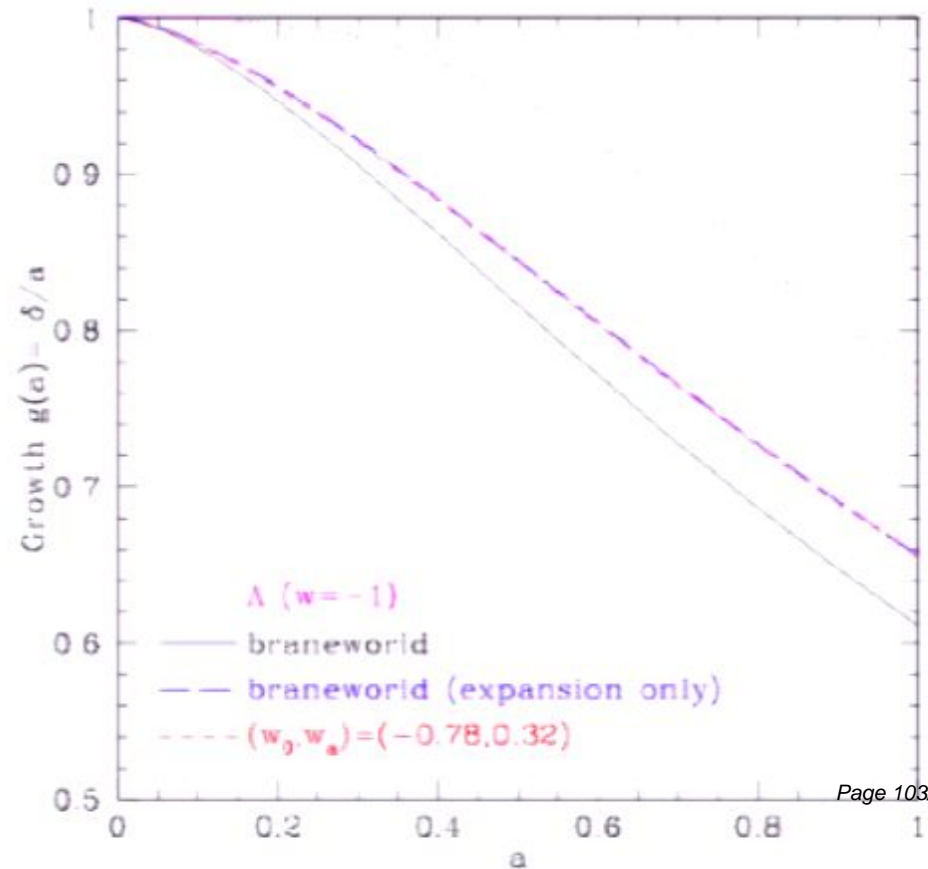
$$g \equiv \frac{D}{a} = \frac{5\Omega_m}{2} \frac{H(a)}{a} \int_0^a \frac{da'}{a'^3 H(a')^3}$$



Bartelmann & Schneider 1999

Linear growth factor describing the growth of perturbations can distinguish between the two (local vs. global effect)

e.g. DGP braneworld gravity



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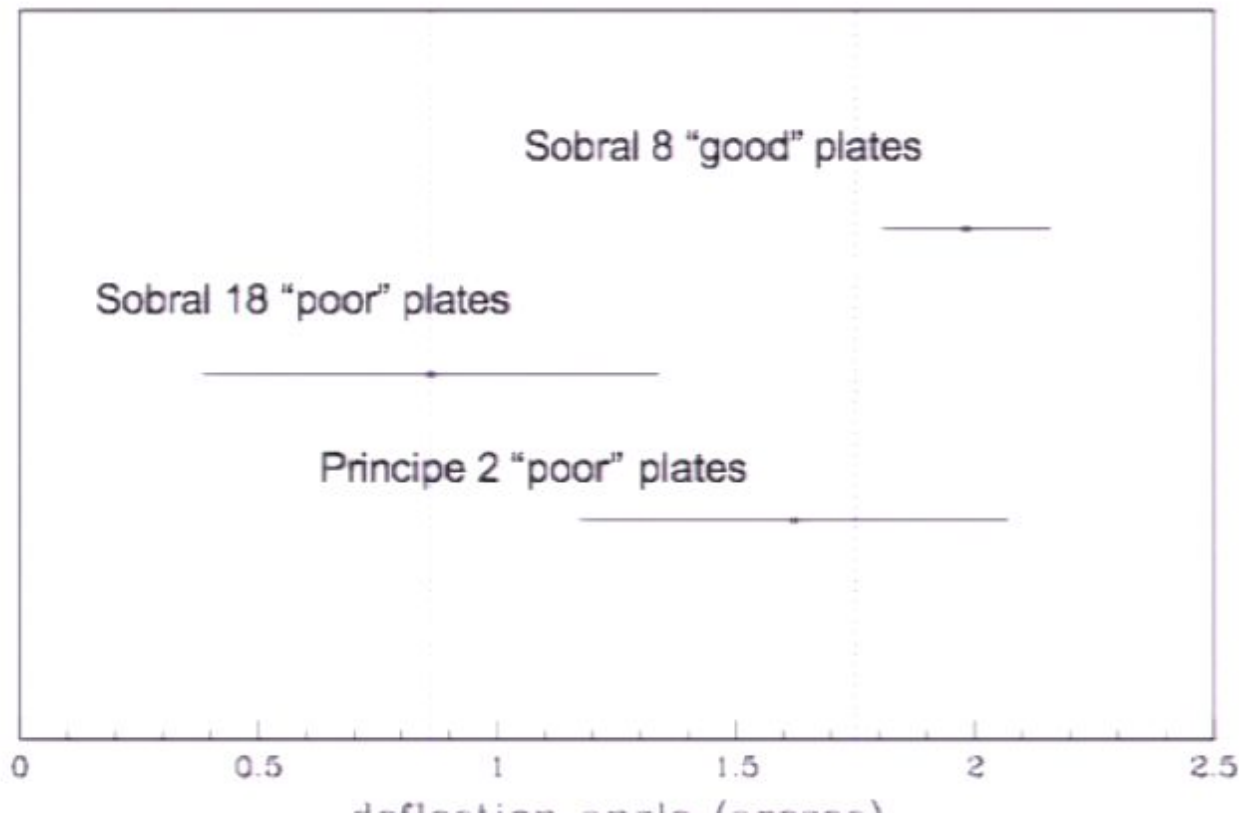
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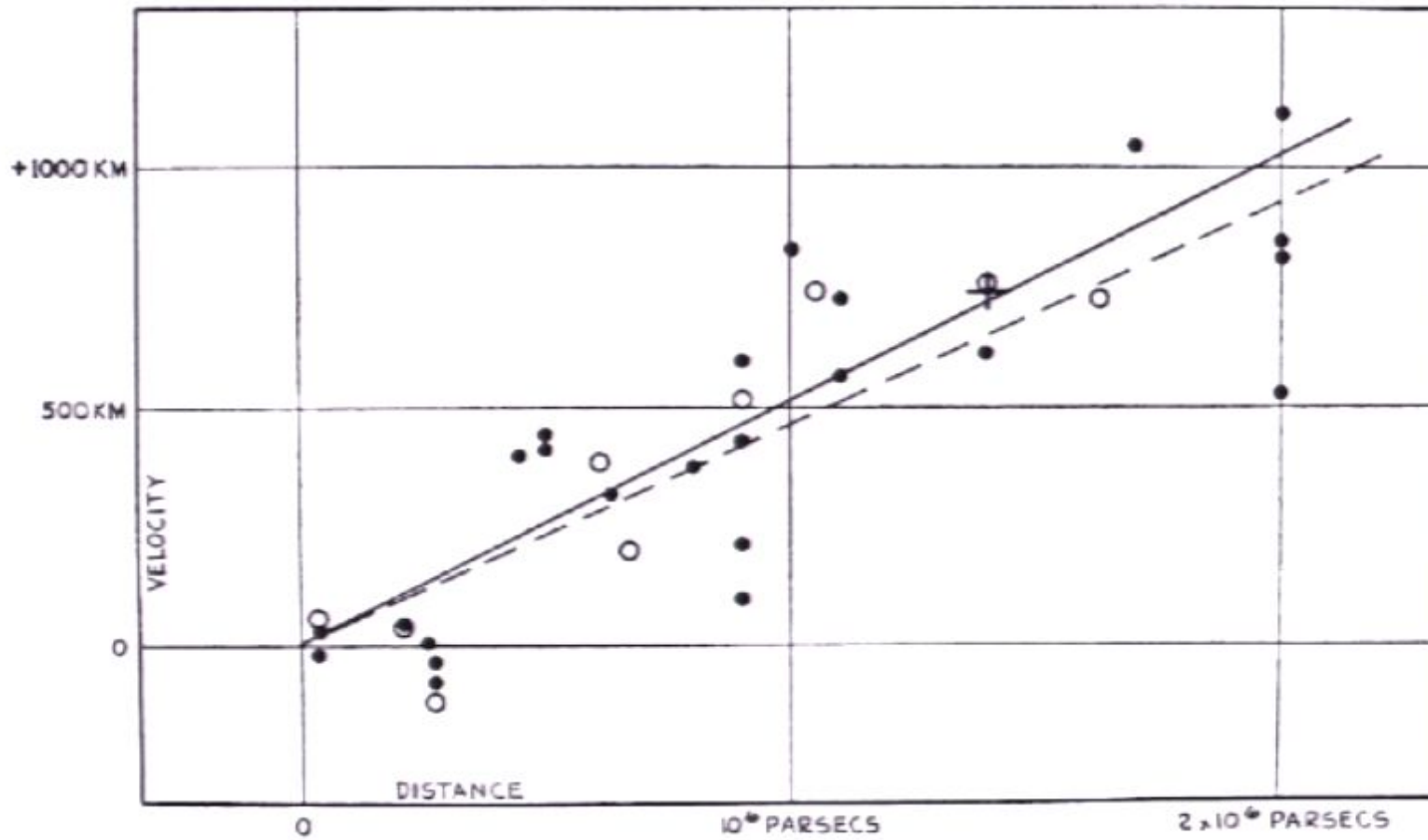
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N.B. The original Hubble Law:



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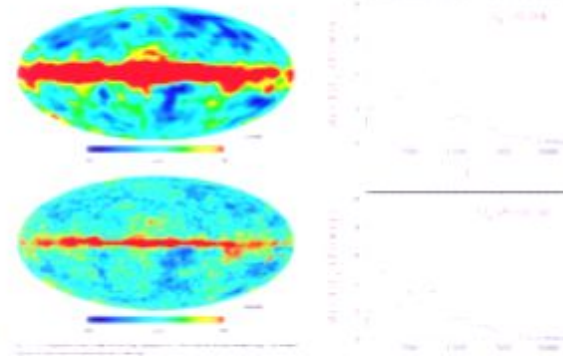
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From this point of view, small scale structure and complex non-linear dynamics are **attractive** features of CDM, not crises or problems.

Also from this perspective, modifications to gravity need to focus on showing **what else they can do**, not on how well they can reproduce existing observations.

# Homework for MOND/MOG etc.:

1: match CMB spectrum

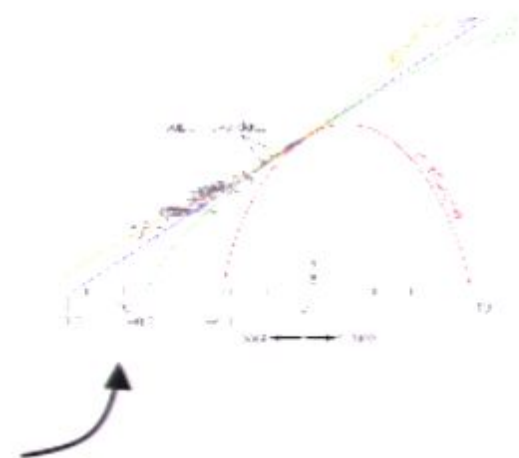
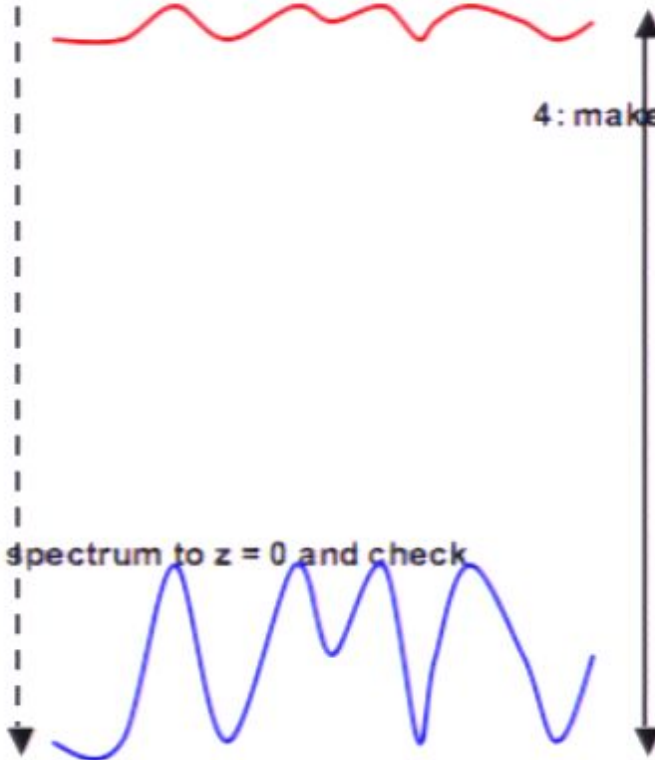
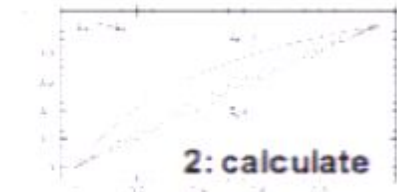


2: calculate linear growth

4: make sure smooth expansion history is consistent

3: evolve spectrum to  $z = 0$  and check

smooth expansion history is consistent



**Note that:**

- 1) none of these tests constitute a prediction
- 2) if it's too hard to figure out how to perform these tests properly that does not reflect well on the theory

## Real Homework for MOND/MOG/etc.:

Where are the missing baryons? (i.e. the 50-70% of all baryons)

Can we ever detect them?

When do the “first” galaxies form? How do they form?

What are the masses of the first galaxies? Where do AGN come in?

What sets present-day galaxy masses, sizes, spins?

How is the IGM enriched?

How are baryons processed through galaxies?

What are the masses of the first stars?

and finally...

is there a solid theoretical motivation for the theory? e.g. is it some sort of “attractor” in theory space?



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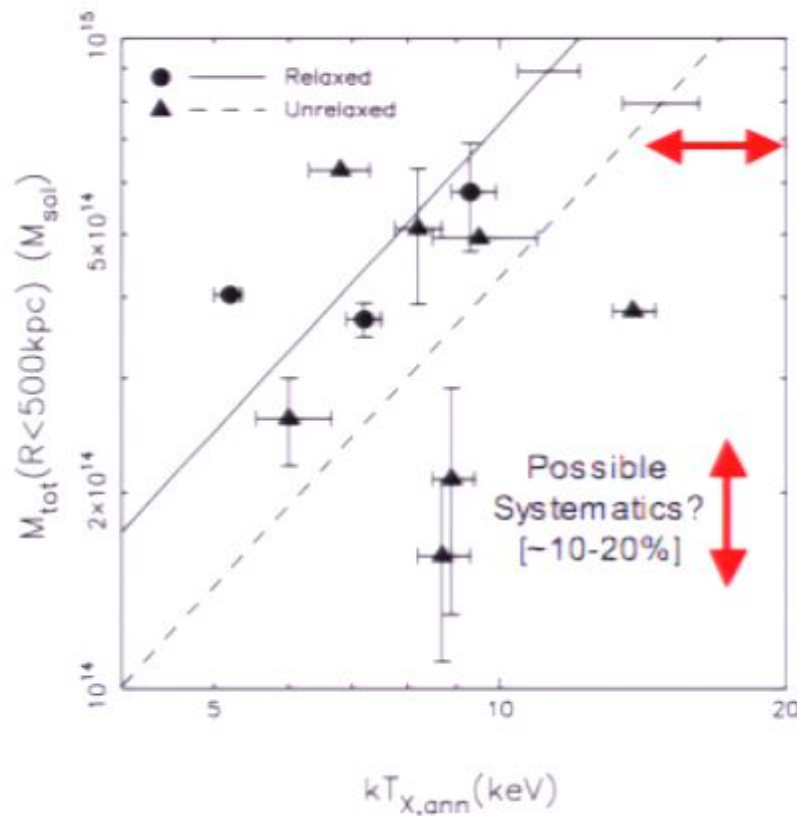
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# Structural segregation in the M-T relation?



Smith et al., 2005, MNRAS, 359, 417

- Mass measurement wrong for non-SL clusters?
- Core-related phenomena?
  - Pederson et al., 0603260
- Cluster-cluster mergers?
  - Ricker & Sarazin 2001, Randall et al. 2003
- What else?