Title: Observational Evidence for Dark Matter

Date: Aug 09, 2007 04:00 PM

URL: http://pirsa.org/07080013

Abstract:

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Observational Evidence for Dark Matter

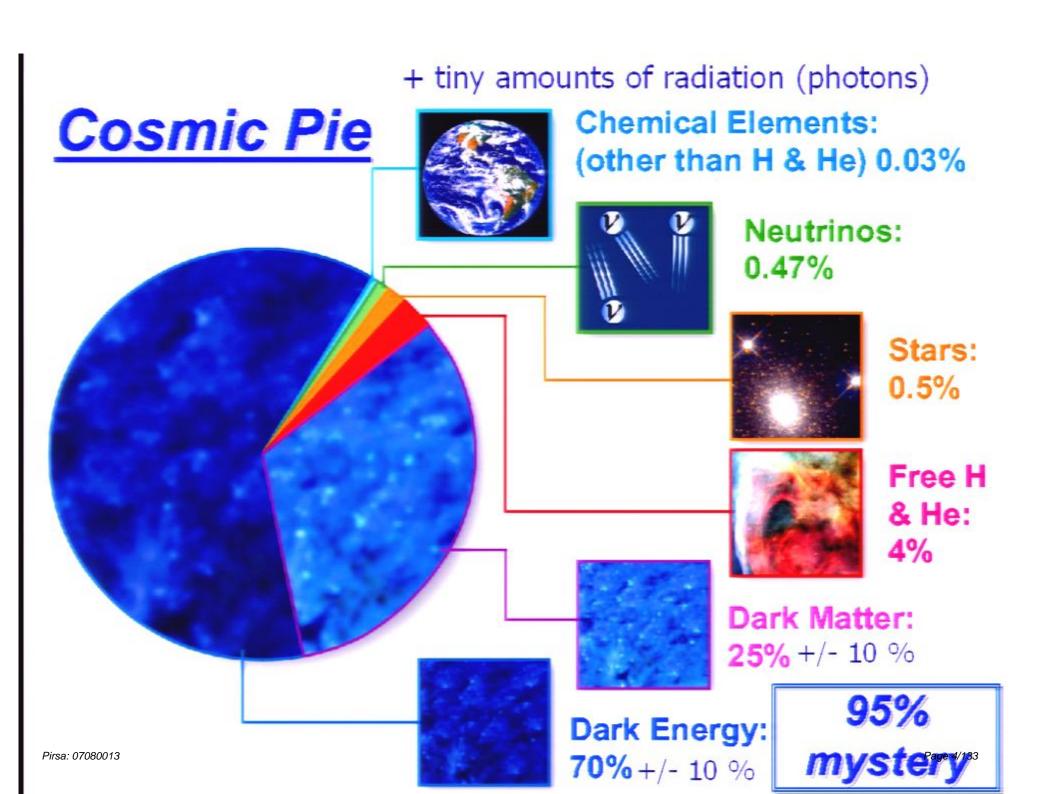
Mike Hudson
U. Waterloo

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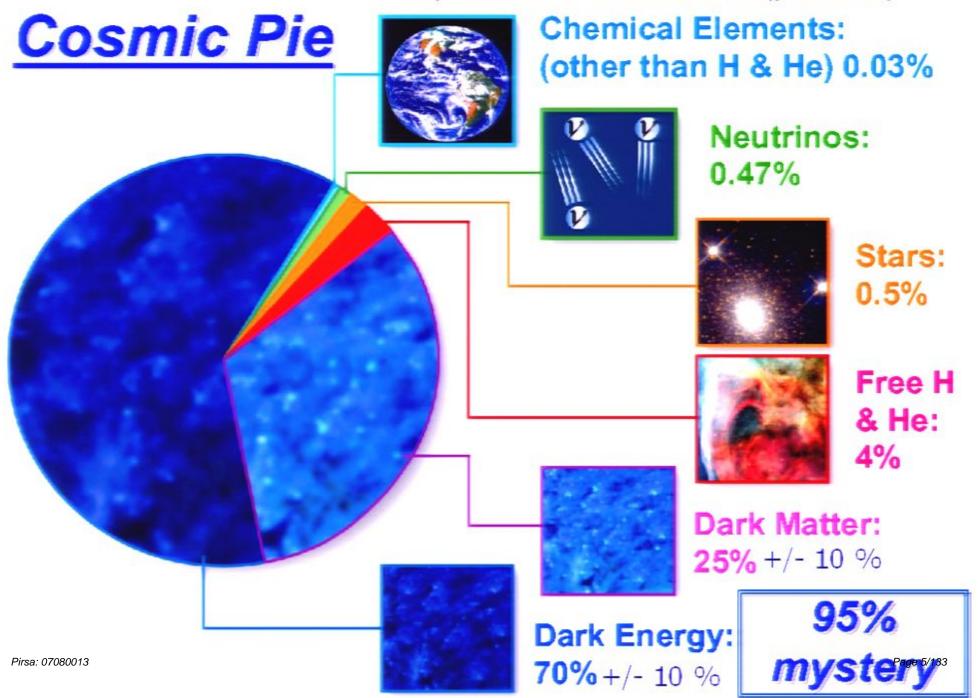
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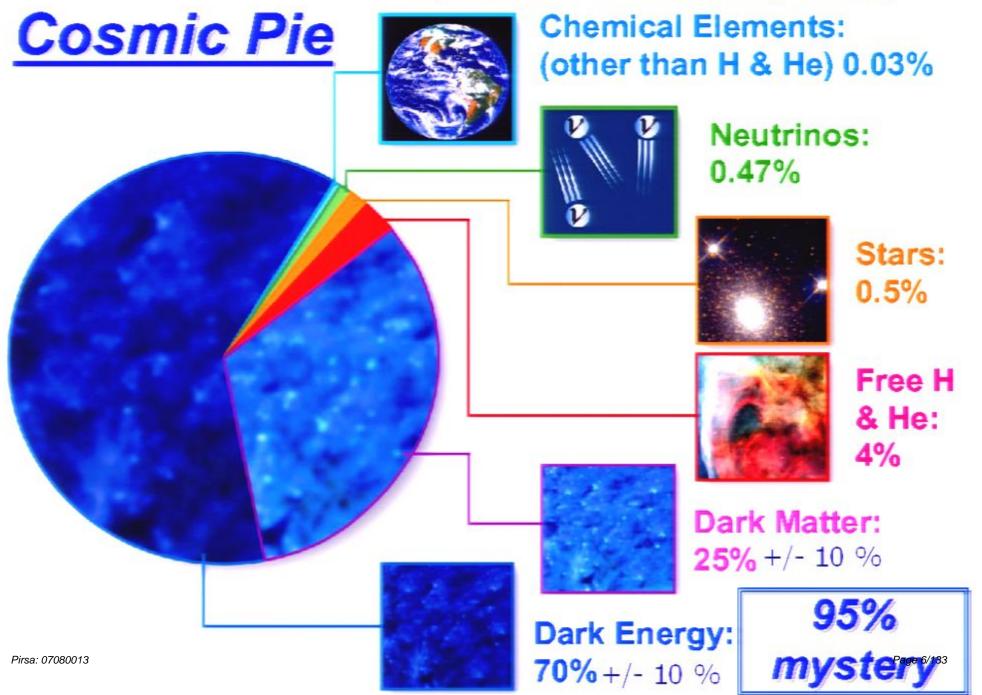
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+ tiny amounts of radiation (photons)



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 Ω = density of matter or energy divided by critical density

 $\Omega_{\rm b}$ = density of baryons

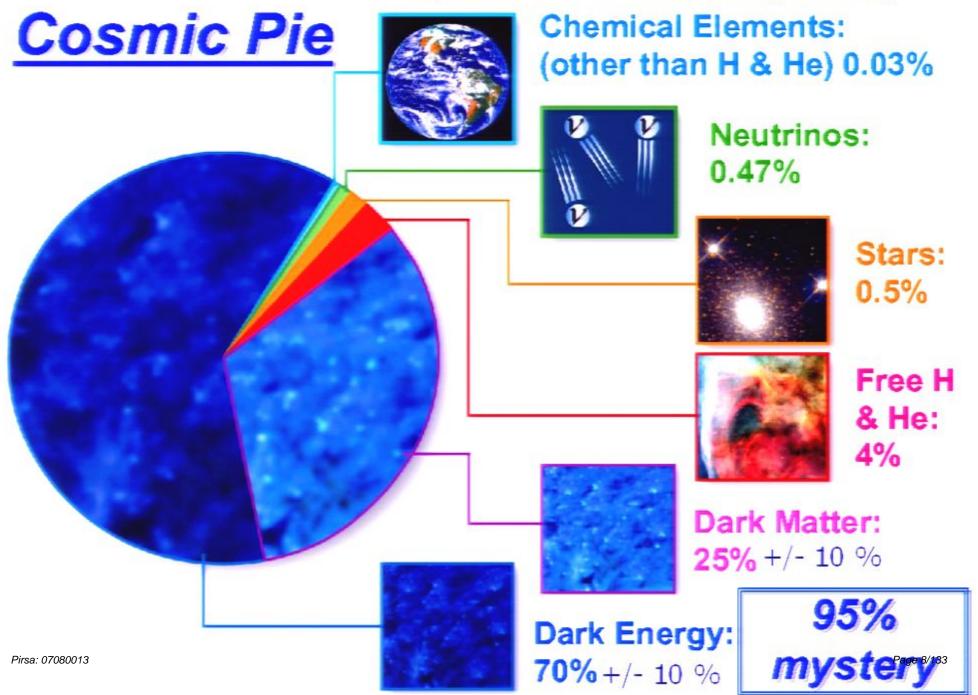
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Assumption: GR is valid

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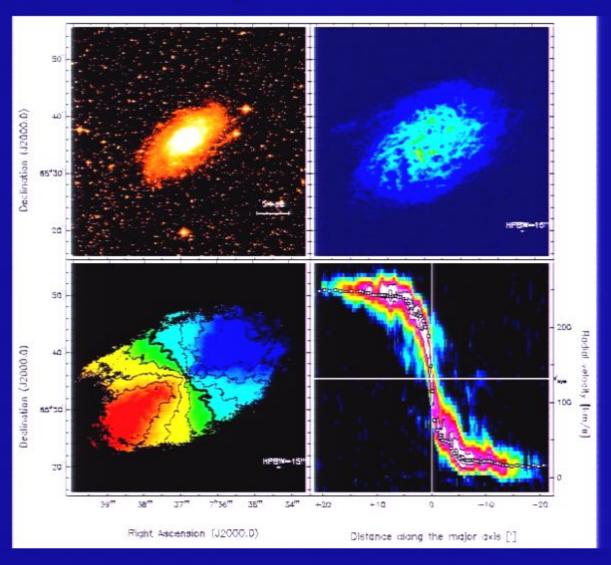
Pirea: 07080013

Outline

- Model-independent evidence for dark matter
 - Spiral galaxy rotation curves
 - Clusters of galaxies
 - Gravitational Lensing
 - Peculiar Velocities
- Model-dependent evidence
 - Cosmic Microwave background and large-scale structure

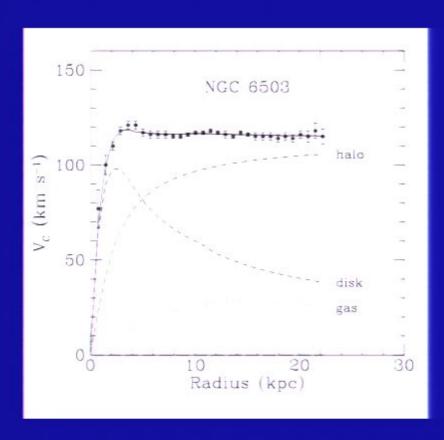
Pirsa: 07080013 Page 10/133

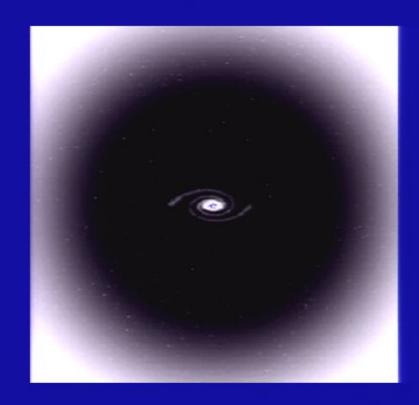
Spiral Galaxy Rotation Curves



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Dark Matter Halo



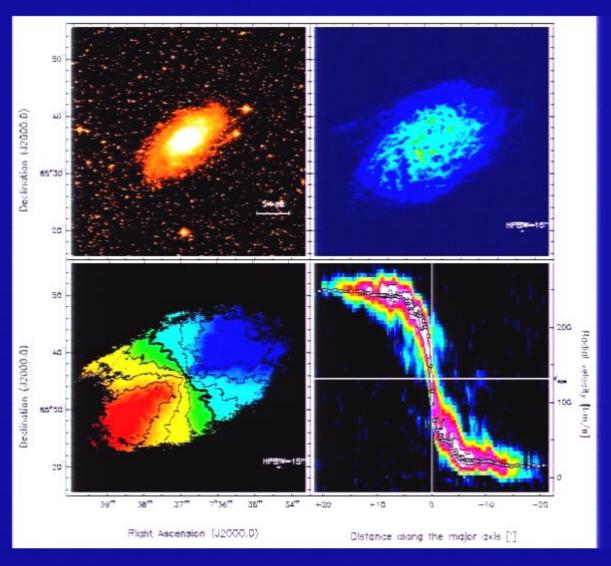


$$v^{2} = \frac{GM(\langle R)}{R} \text{ so if } v = const$$

$$\text{Nirsh: d7060013}R) \propto R$$

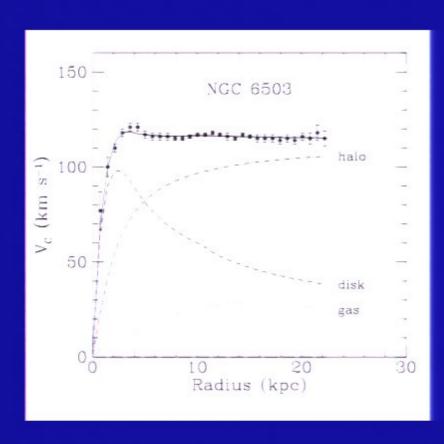
...lower limit on total mass

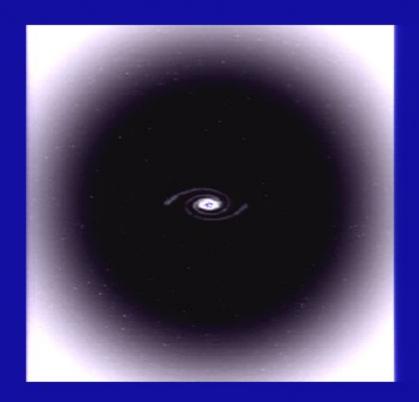
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Dark Matter Halo



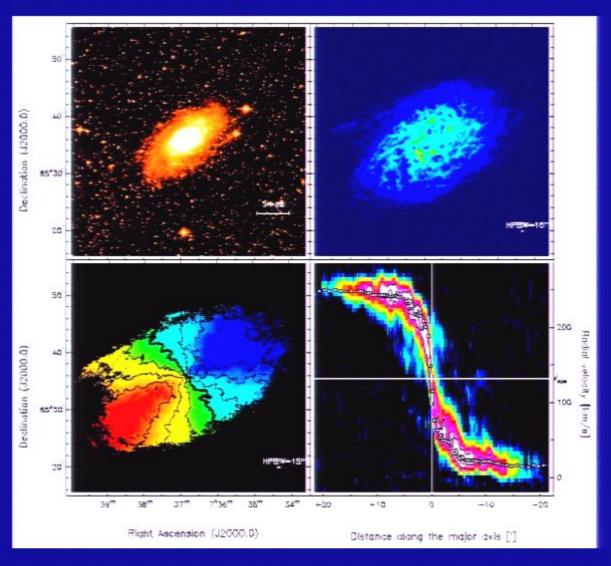


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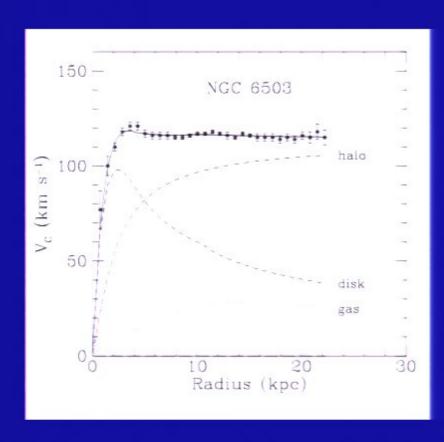
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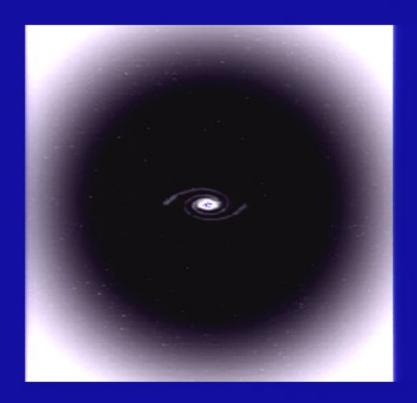
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Dark Matter Halo



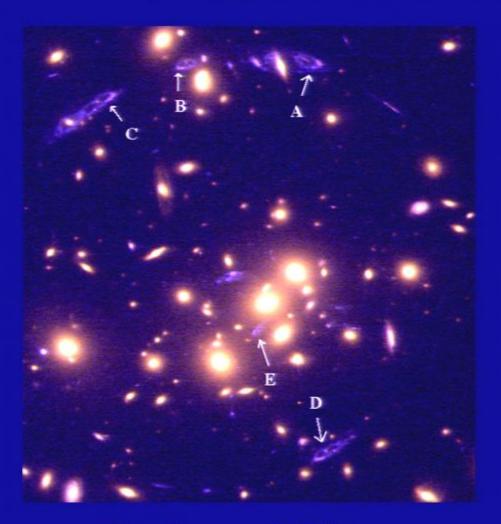


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Clusters of Galaxies



The largest virialized objects in the Universe

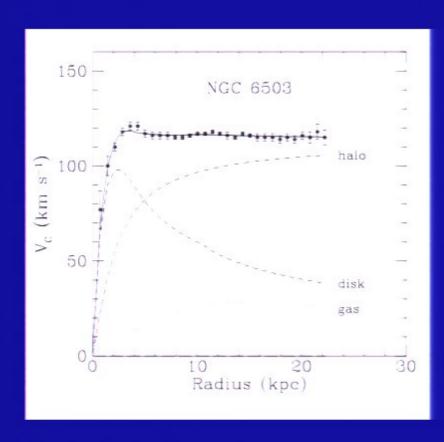
Masses can be obtained by three methods

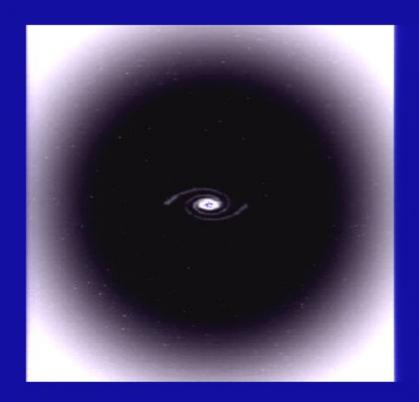
- Dynamics of galaxies (virial theorem)
- X-ray emitting gas (hydrostatic equilibrium)
- Gravitational Lensing

Scale: ~1 Mpc

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Dark Matter Halo



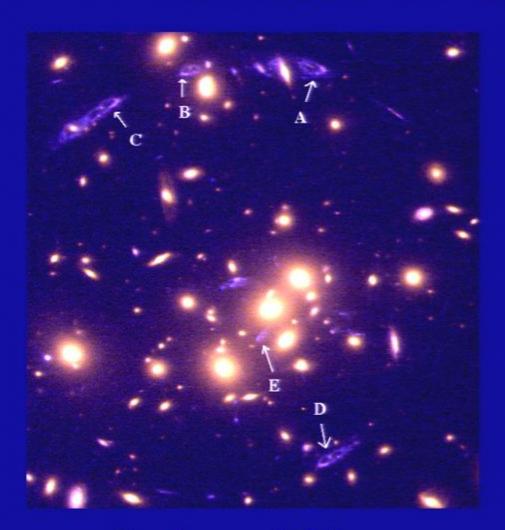


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Cluster Dynamics

 Virial theorem or Jean's equations applied to motions of galaxies with respect to cluster center yield cluster masses.

First noted by Zwicky 1937.

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$$M > 9 \times 10^{49} \text{gr}$$
. (35)

The Coma cluster contains about one thousand nebulae. The average mass of one of these nebulae is therefore

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$$\overline{M} > 0 \times 10^{41} \, \text{gr} = 4.5 \times 10^{10} \, M_{\odot}$$
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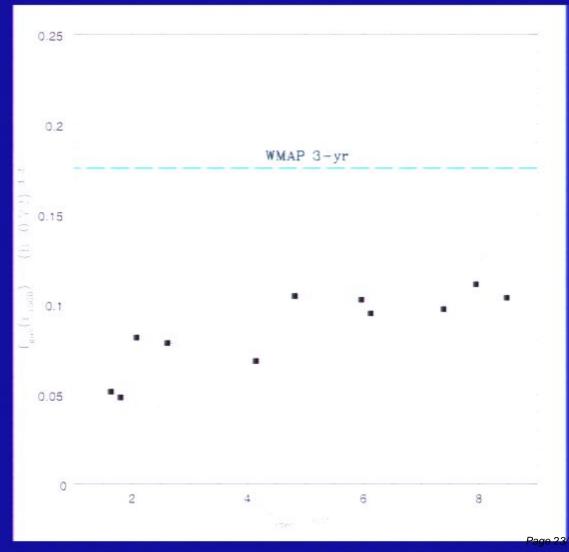
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We inquire first what happens if the cluster considered is not st-a

Clusters masses from X-ray data

Ratio of gas mass to total (gas plus dark matter) mass ~ 0.12

(stars are negligible)

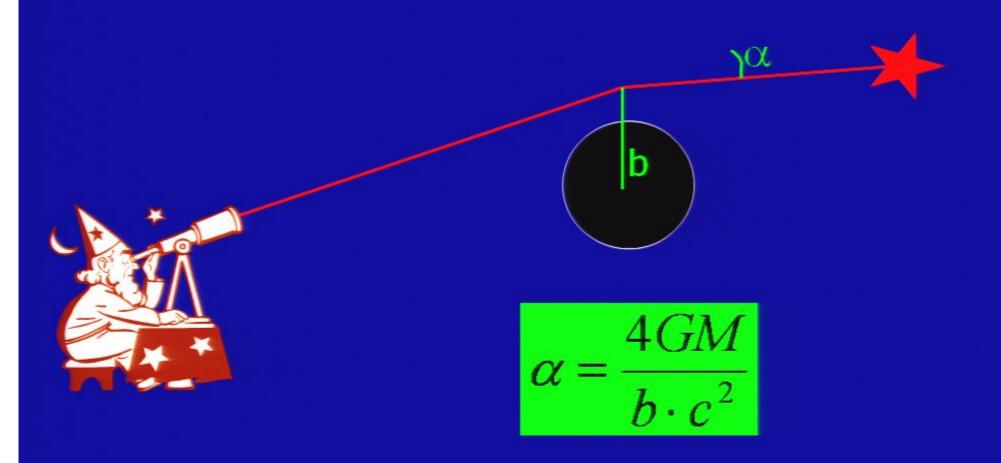






$$\alpha = \frac{4GM}{b \cdot c^2}$$

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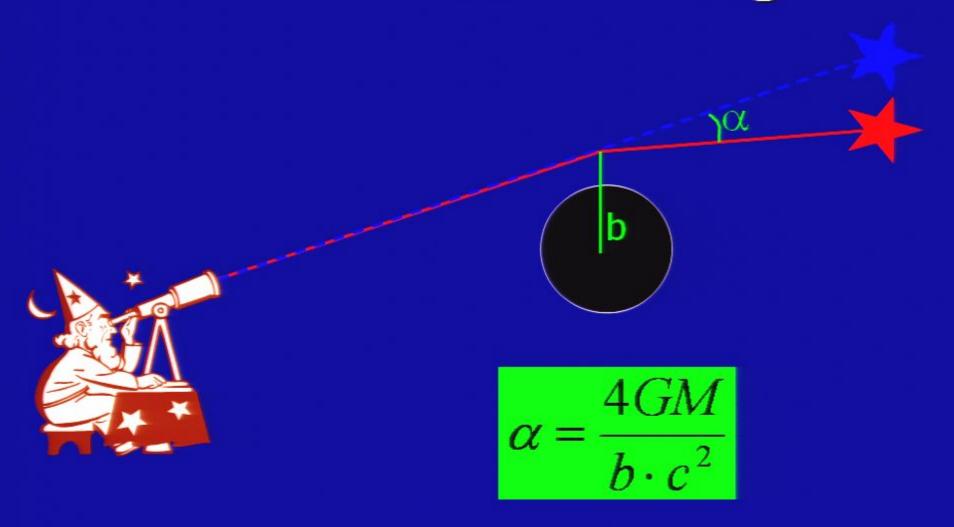
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Lensing in Cosmology

 Since the strength of the lensing effect depends on mass, use it to measure mass

 But the deflection is not directly observable, so use distortion and magnification

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Pirsa: 07080013

Lensing in Cosmology

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Gravitational lensing magnifies and distorts

Strong lensing (multiple imaging) in the center

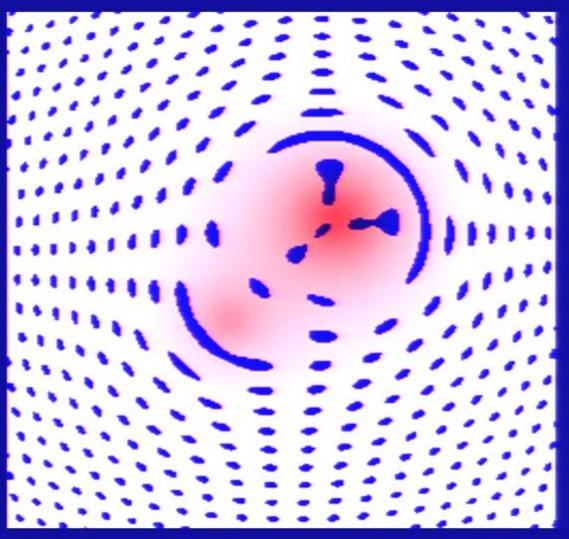
Weak lensing at edges

Pirsa: 07080013 Page 29/133

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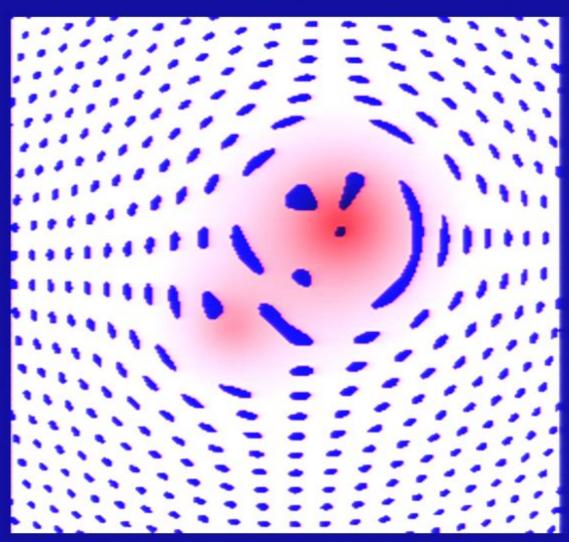
Weak lensing at edges



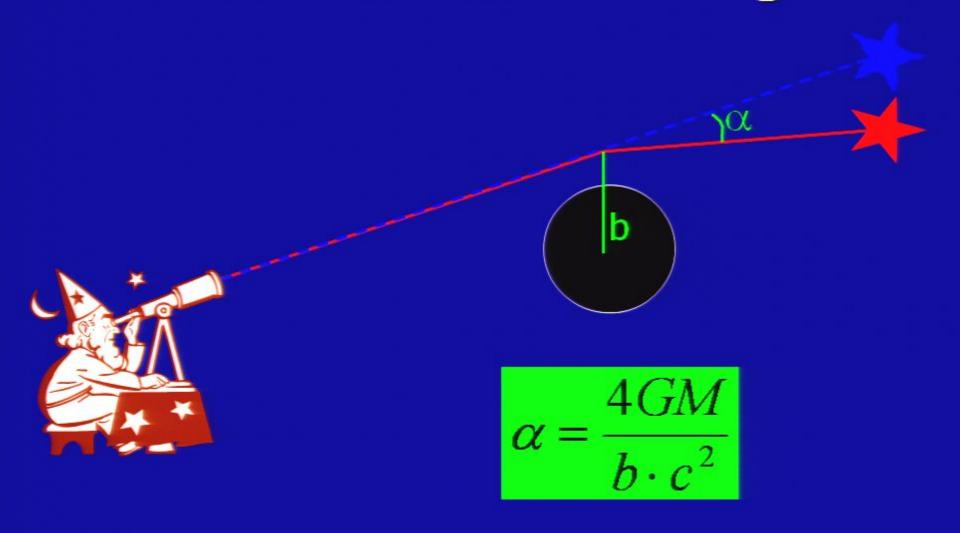
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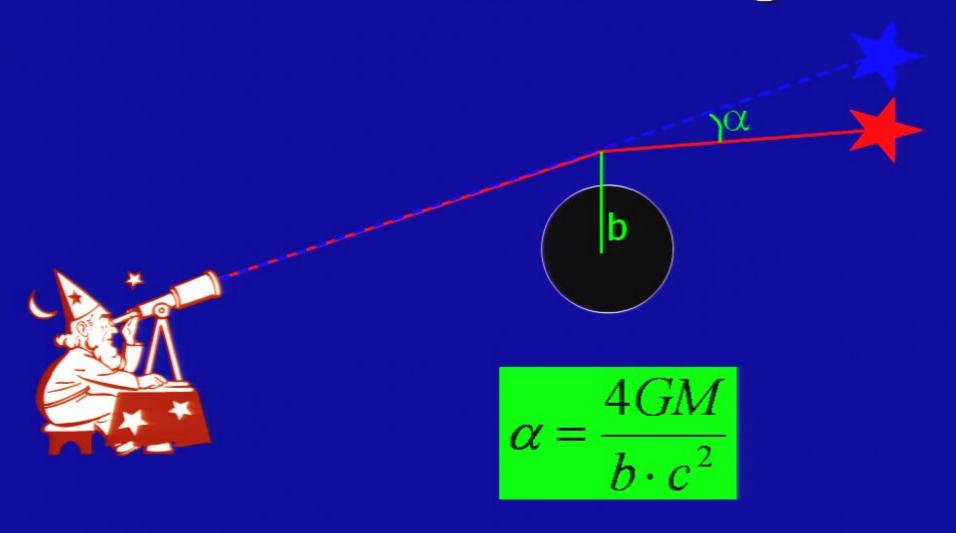
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Pirsa: 07080013 Page 31/13.



Pirsa: 07080013



Pirea: 07080013

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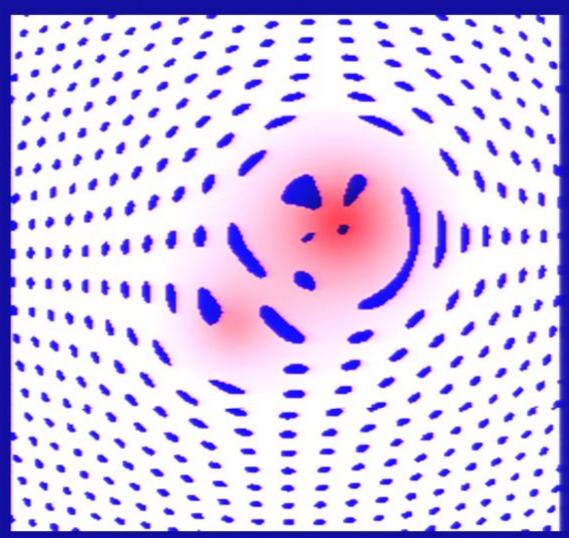
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Pirsa: 07080013 Page 34/133

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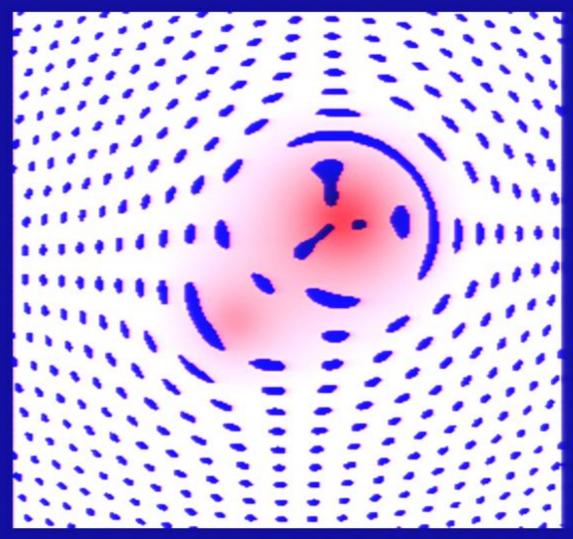


Pirsa: 07080013 Page 35/13.

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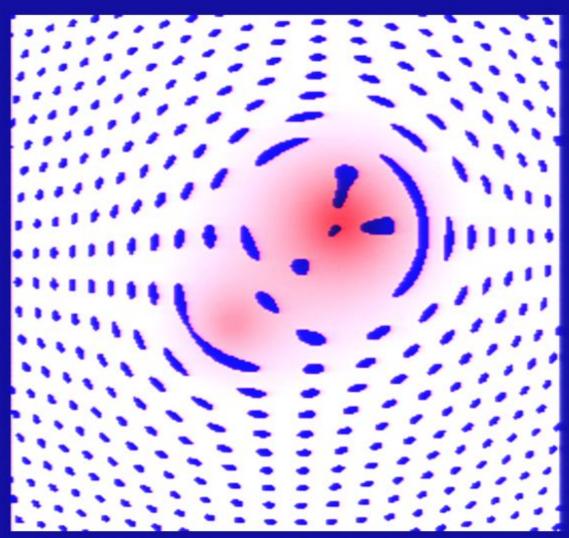
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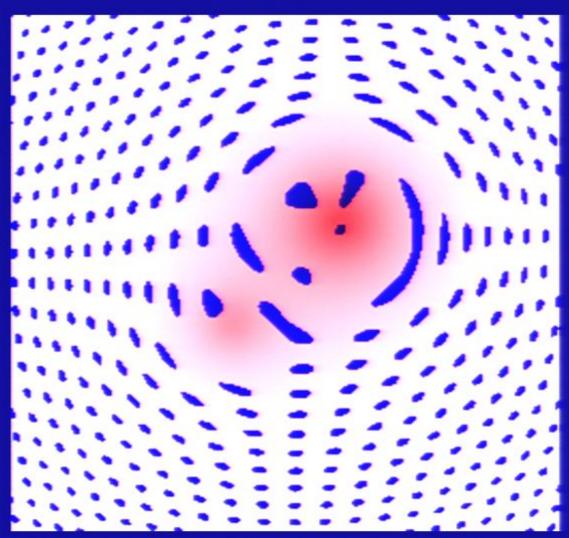


Pirsa: 07080013 Page 37/13.

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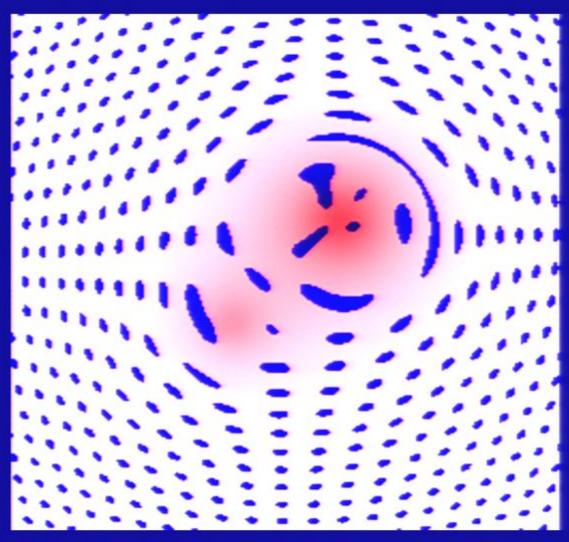


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Zwicky, Science, 1937

"The discovery of images of nebulae Would be of considerable interest for three reasons:

- It would furnish and additional test for the general theory of relativity.
- It would enable us to see nebulae at distances greater than those ordinarily reached by even the greatest telescopes
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Pirsa: 07080013 Page 40/133

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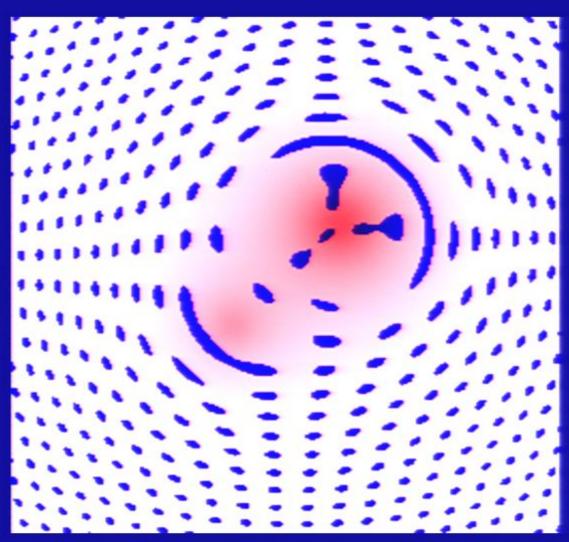
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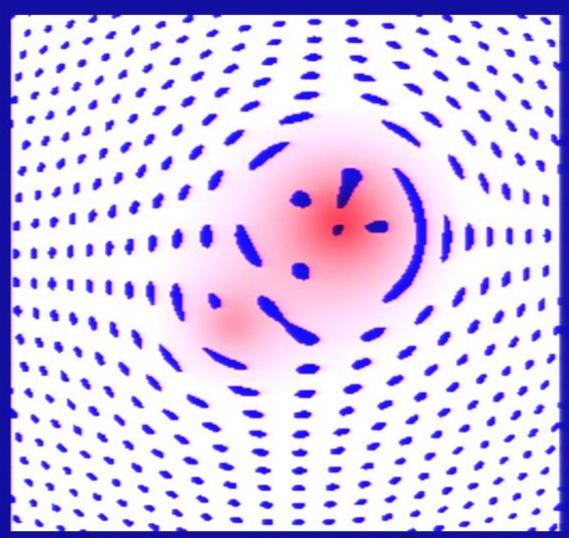


Pirsa: 07080013 Page 42/133

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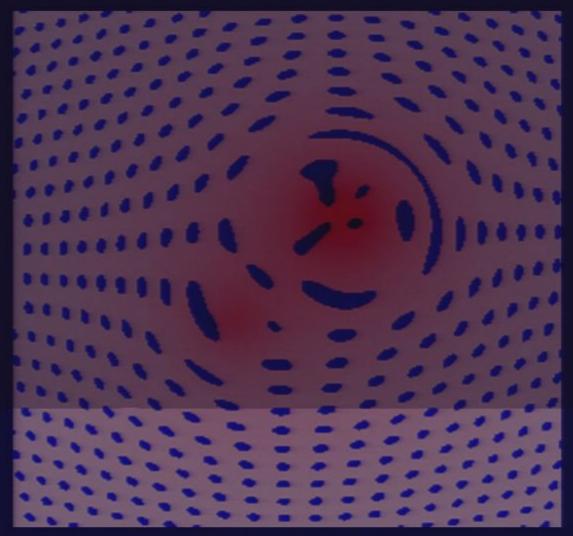


Pirsa: 07080013 Page 43/13.

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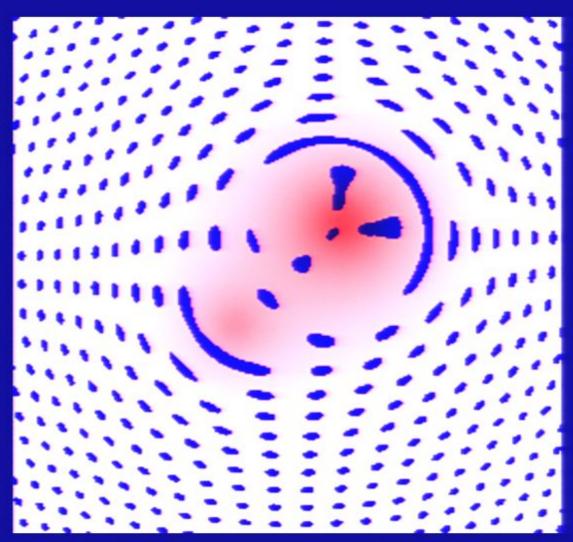


Pirsa: 07080013 Page 44/13

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Pirsa: 07080013 Page 45/133

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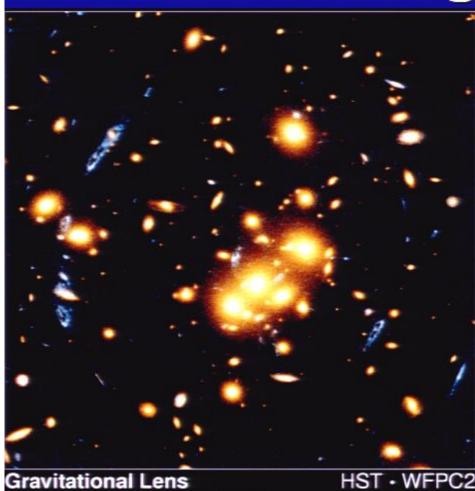
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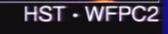
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Strong lensing



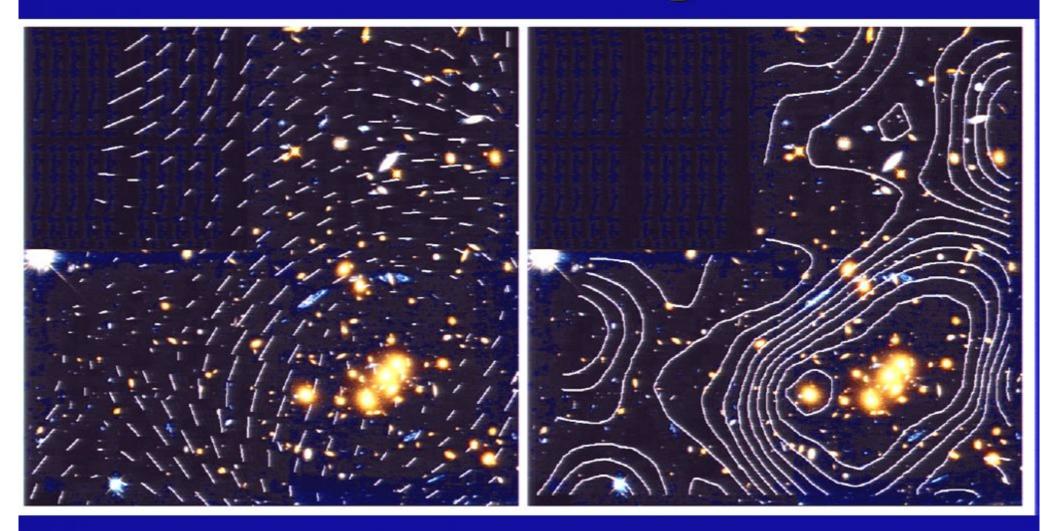


Galaxy Cluster 0024+1654 PRC96-10 · ST Scl OPO · April 24, 1996

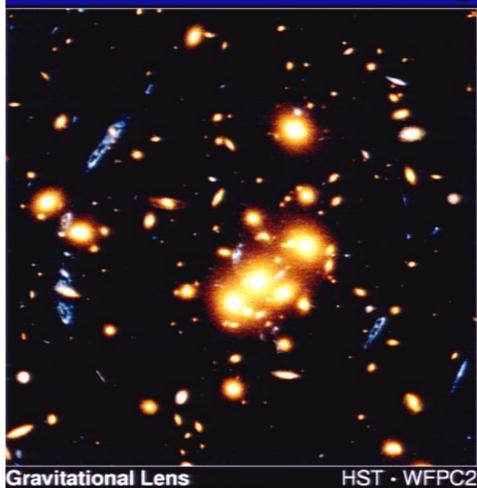
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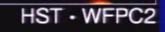
Lensed images and model (cluster at z=0.4, lensed source at z = 0.7)

Weak lensing



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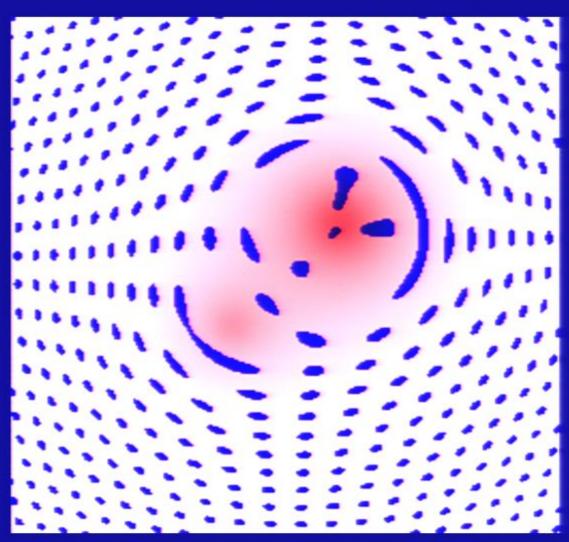
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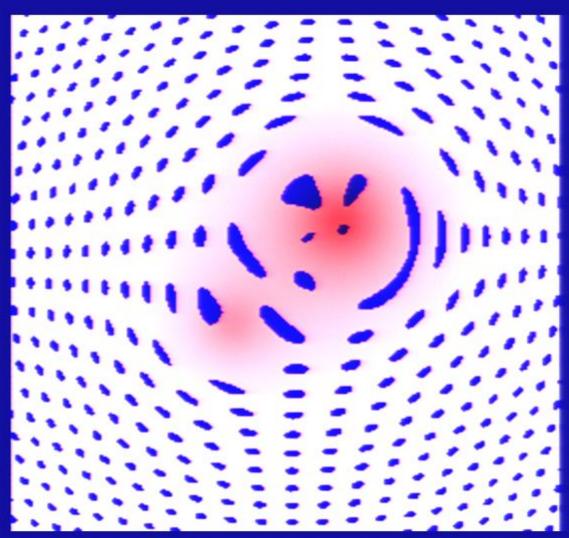


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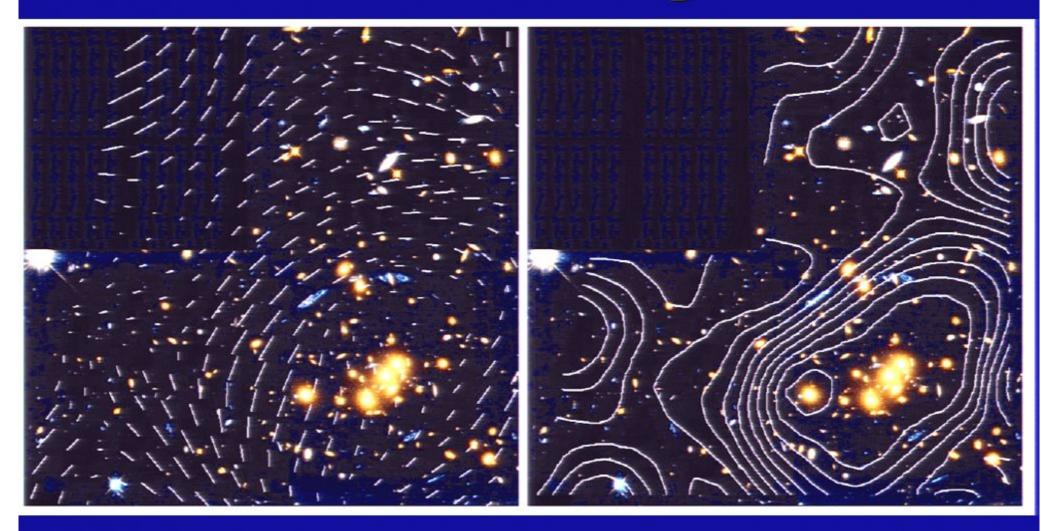
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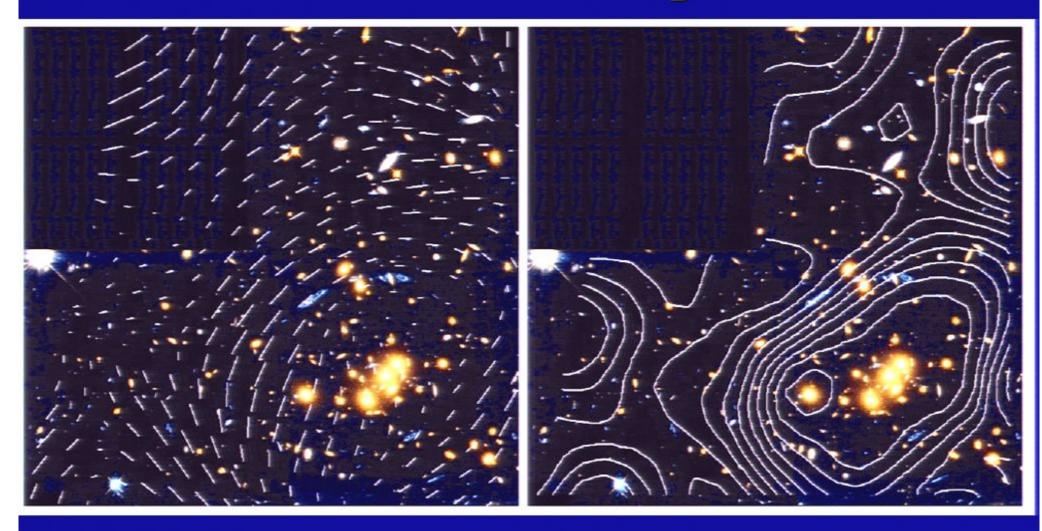


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Weak lensing



Weak lensing



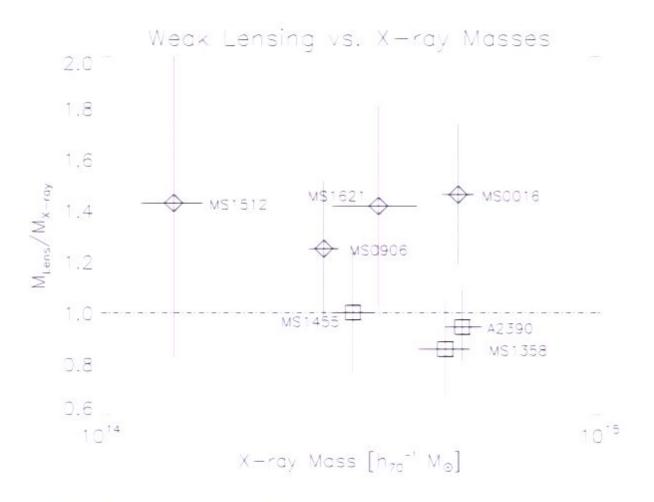
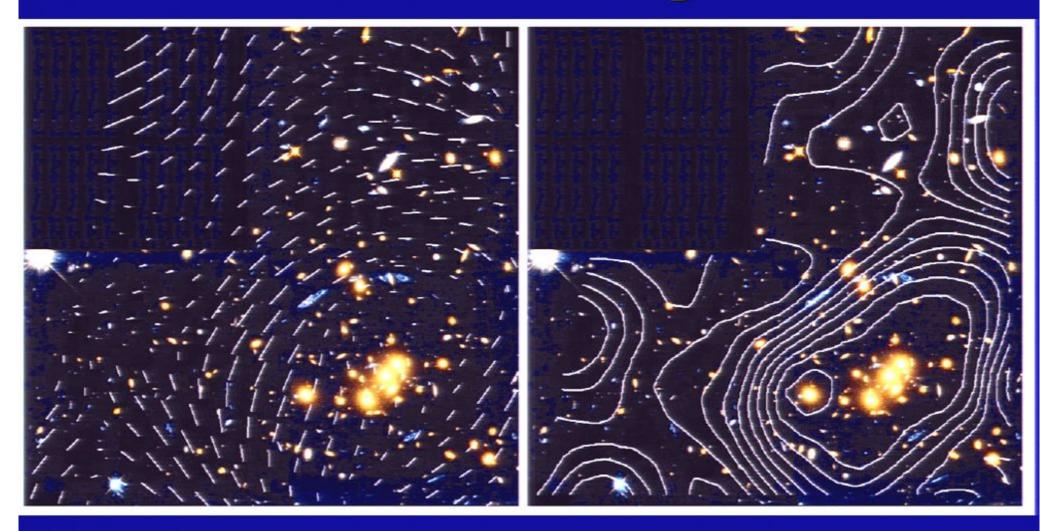
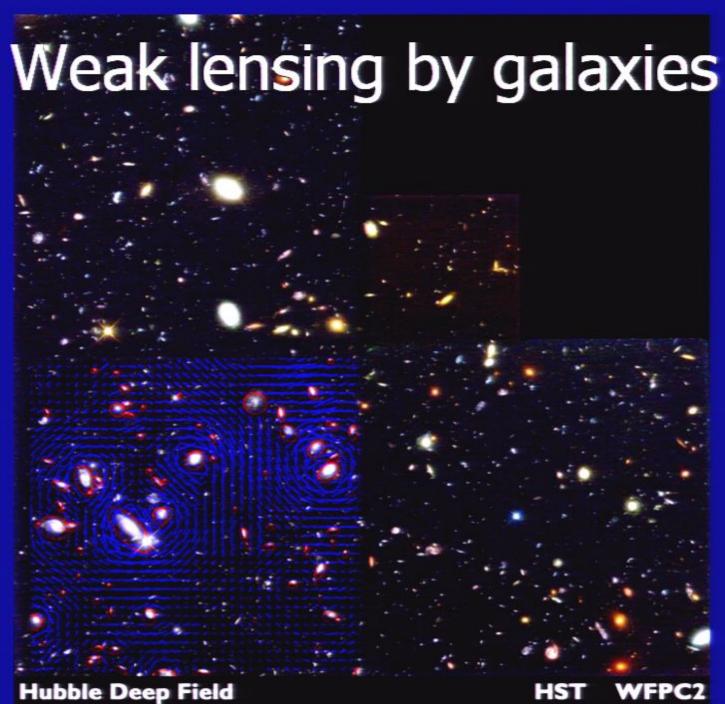


Fig. 6.— Weak Lensing vs. X-ray Masses. X-ray mass estimates are plotted against the ratio M_{Lens}, M_{X-ray}. The dot-dash line represents a mass ratio of 1.0. Squares indicate cooling core clusters, and error bars denote 68% confidence limits. Though the distribution appears assymmetric, it is not statistically significant.

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Weak lensing





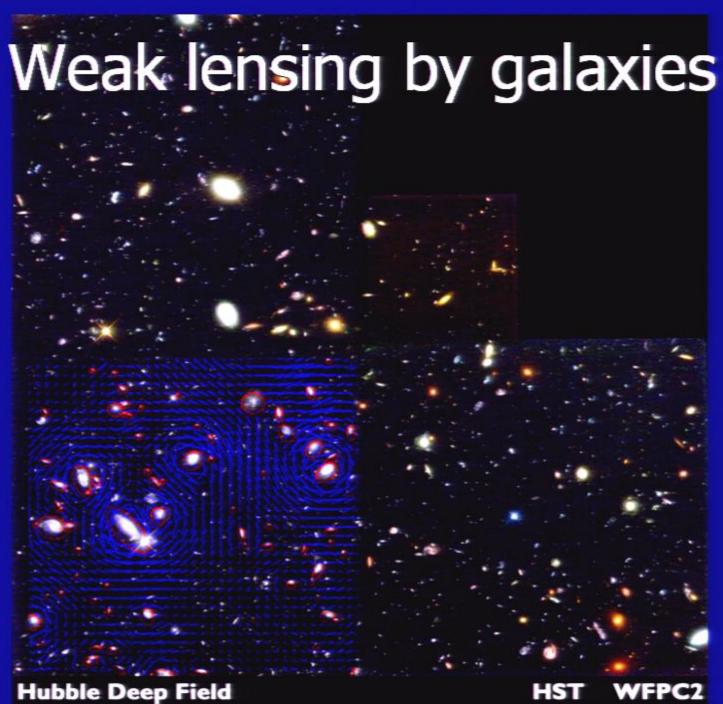
Peculiar velocities

 Peculiar velocities are deviations from the uniform expansion of the Universe

 Caused by extra matter retards the expansion of the Universe locally

 In principle by measuring the former, one can deduce the latter.

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Peculiar velocities

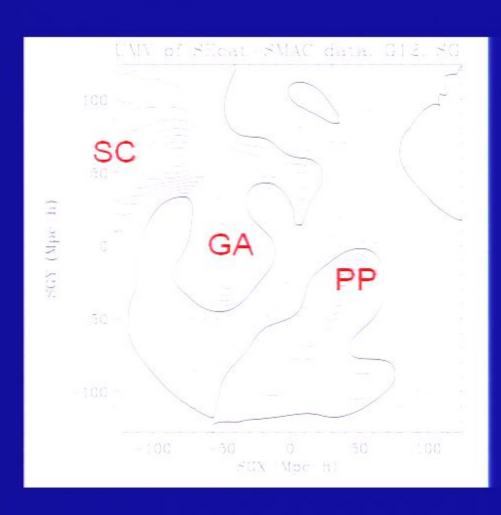
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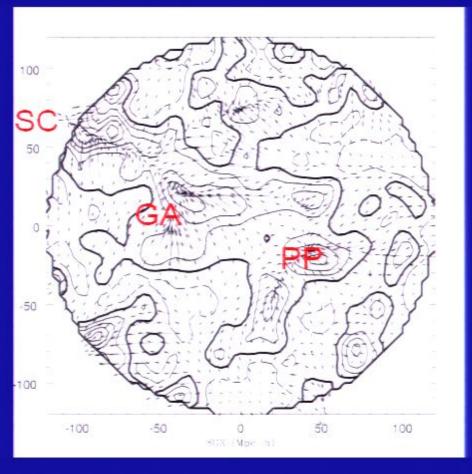
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Mass vs Light





Mass from peculiar velocities

(Zaroubi inversion)

Light in Galaxies

(Branchini)

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 For consistency between peculiar velocties and light, we require

$$\square$$
 $\Omega_{\rm m} \sim 0.3$

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Large-scale structure

The spectrum of mass fluctuations on large-scales and the angular spectrum of CMB fluctuations depends on the cosmological parameters.

Pirsa: 07080013 Page 63/133

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Pirsa: 07080013 Page 64/133

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Pirsa: 07080013 Page 65/133

Peculiar velocities

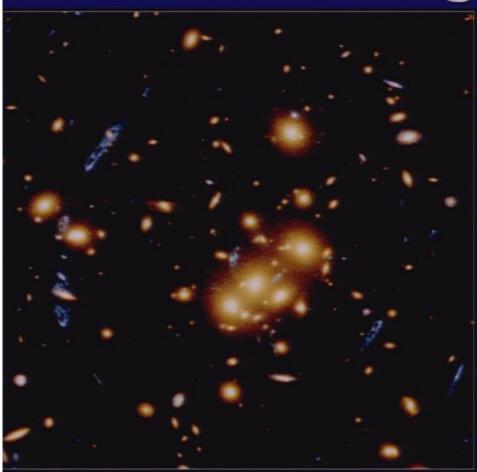
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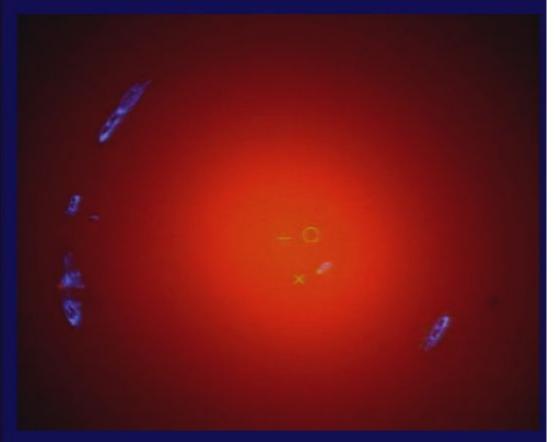
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Strong lensing





Gravitational Lens Galaxy Cluster 0024+1654 HST - WFPC2

PRC96-10 · ST Scl OPO · April 24, 1996

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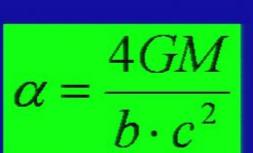
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Weak lensing at edges

Pirsa: 07080013 Page 68/133









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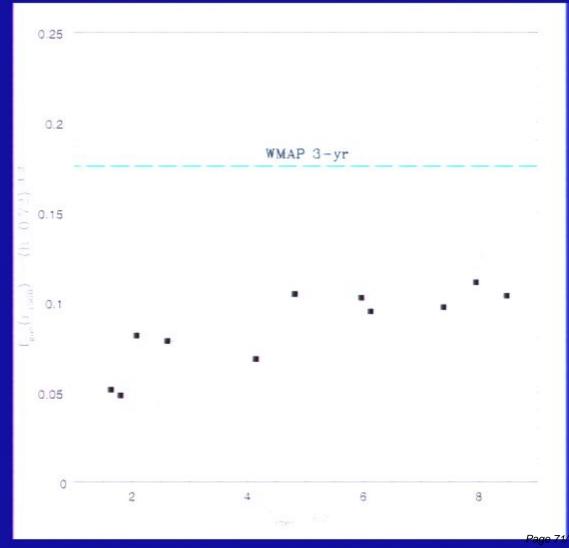
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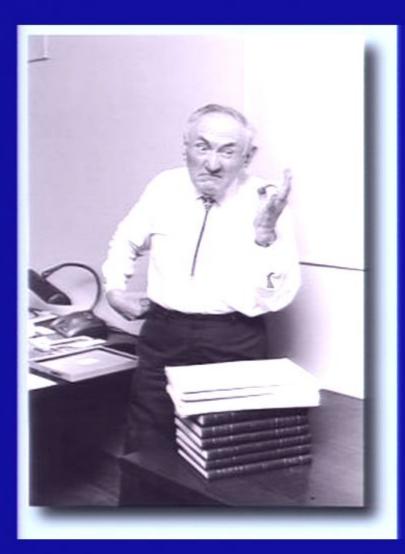




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Fritz Zwicky

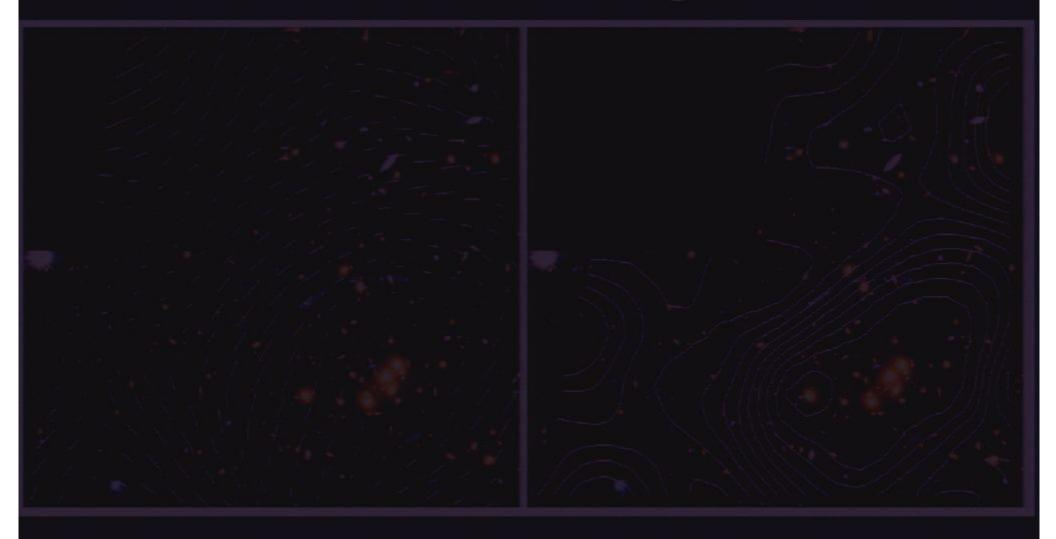


 Zwicky had a difficult personality:

He was fond of calling people "spherical bastards", because they were bastards every way he looked at them.

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Weak lensing



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Daikumaite mass.

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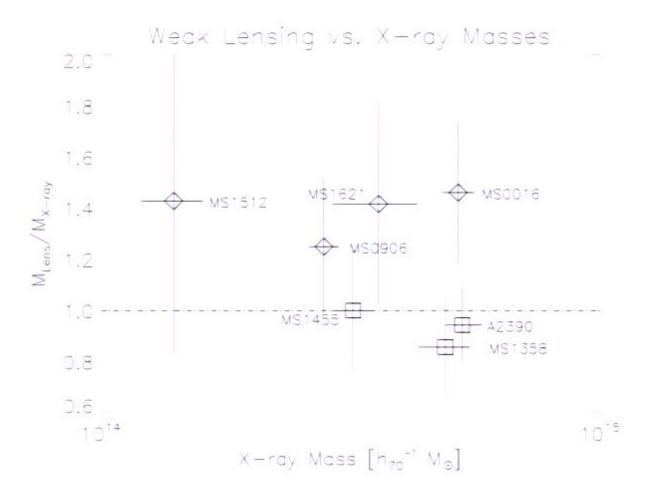
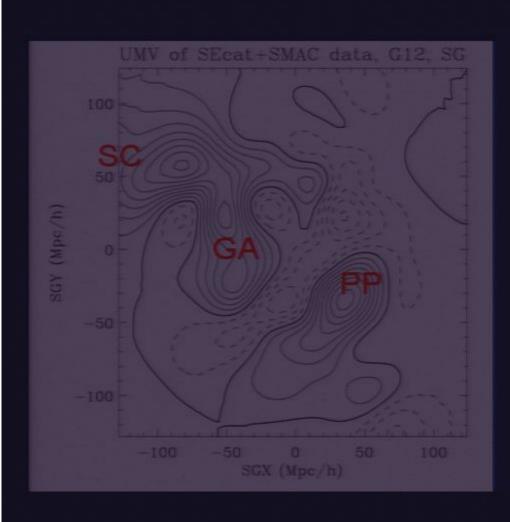
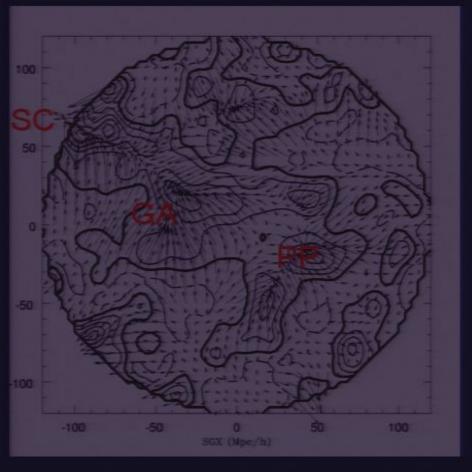


Fig. 6.— Weak Lensing vs. X-ray Masses. X-ray mass estimates are plotted against the ratio M_{Lens} M_{X-ray}. The dot-dash line represents a mass ratio of 1.0. Squares indicate cooling core clusters, and error bars denote 68% confidence limits. Though the distribution appears assymmetric, it is not statistically significant.

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Mass vs Light





Mass from peculiar velocities

(Zaroubi inversion)

Light in Galaxies

(Branchini)

Page 76/13:

 For consistency between peculiar velocties and light, we require

$$\square$$
 $\Omega_{\rm m} \sim 0.3$

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Large-scale structure

The spectrum of mass fluctuations on large-scales and the angular spectrum of CMB fluctuations depends on the cosmological parameters.

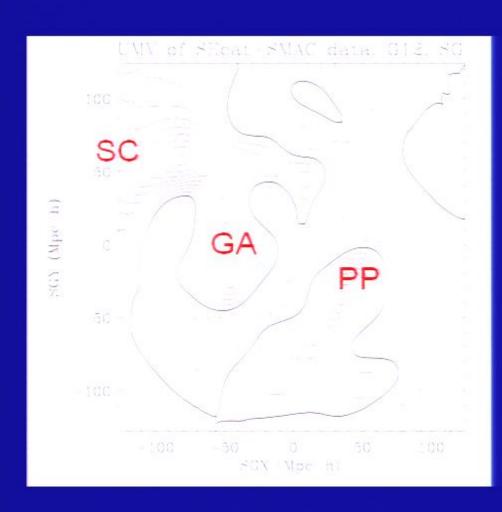
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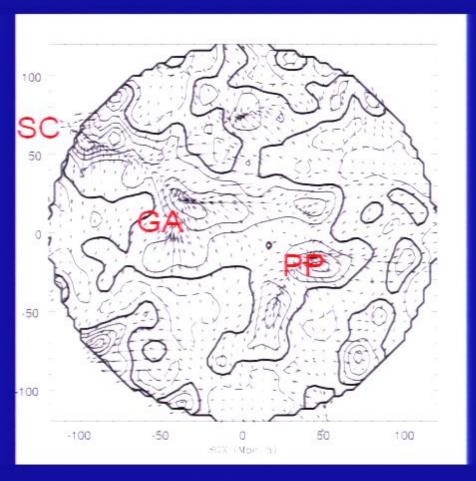
 For consistency between peculiar velocties and light, we require

$$\square$$
 $\Omega_{\rm m} \sim 0.3$

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Mass vs Light





Mass from peculiar velocities

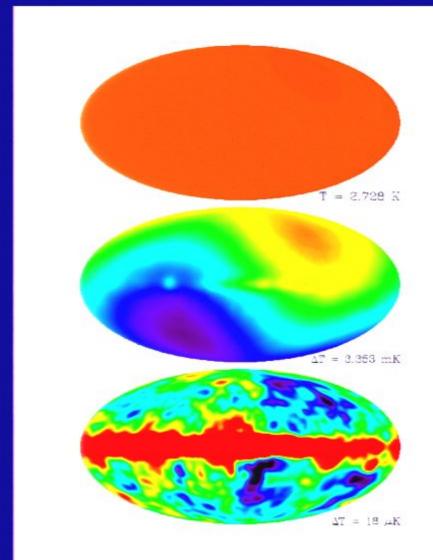
(Zaroubi inversion)

Light in Galaxies

(Branchini)

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Cosmic Microwave Background

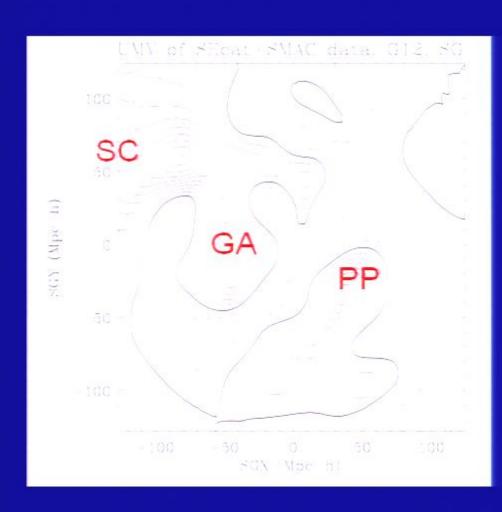


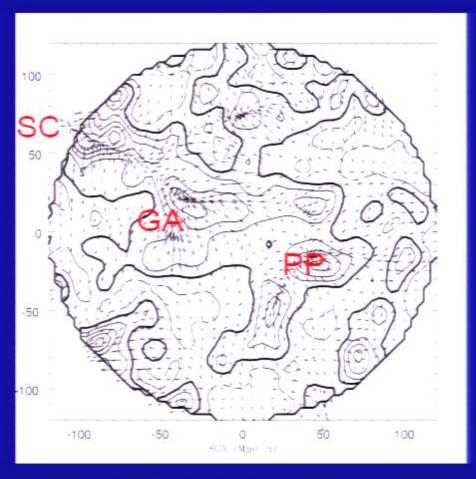
The primeval "fog" left over from when the Universe became transparent to radiation.

The micro-K ripples are due to redshifting from gravitational wells at z ~ 1000.

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Mass vs Light





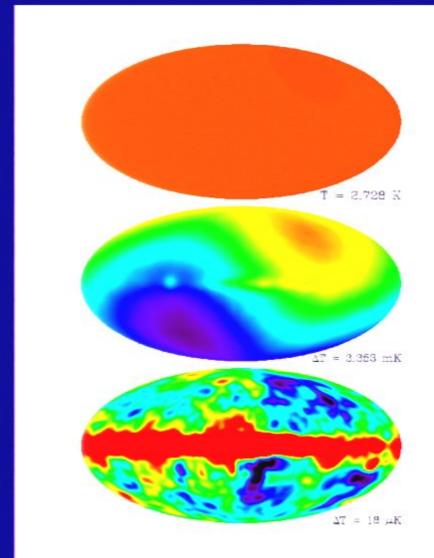
Mass from peculiar velocities

(Zaroubi inversion)

Light in Galaxies

(Branchini)

Cosmic Microwave Background

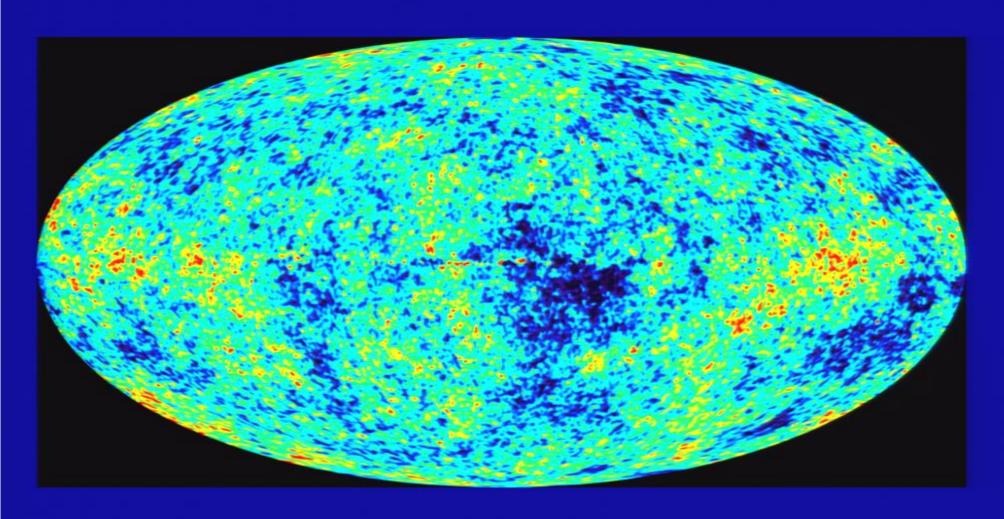


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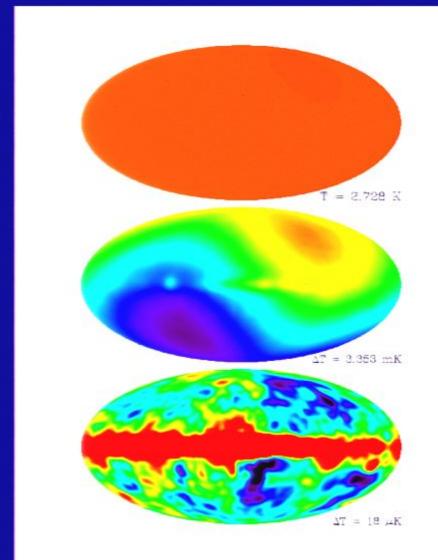
a: 07080013 Page 83/133

CMB by WMAP 2003



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Cosmic Microwave Background

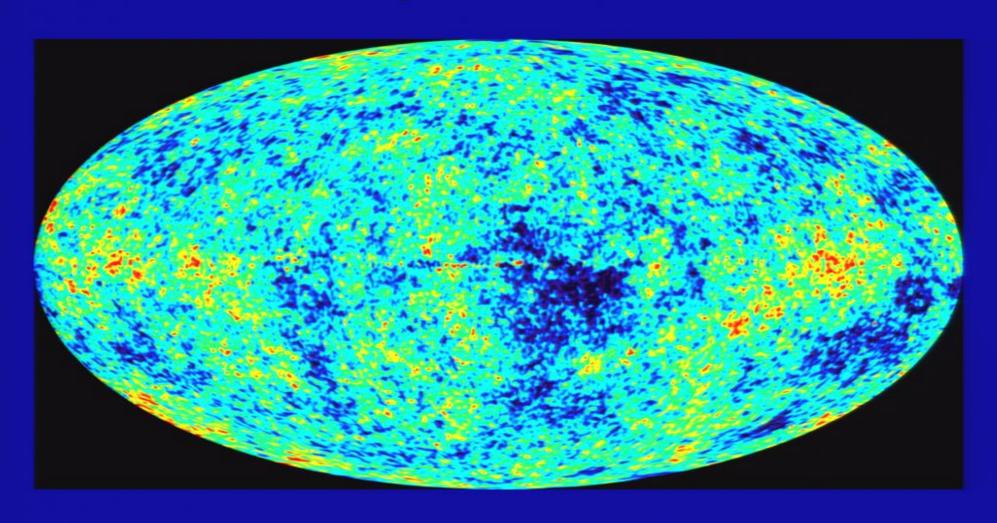


The primeval "fog" left over from when the Universe became transparent to radiation.

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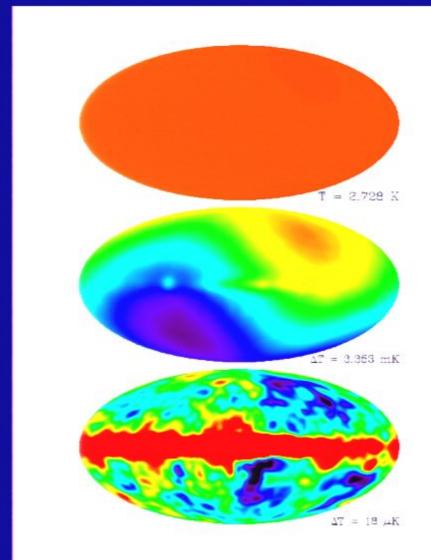
a: 07080013 Page 85/133

CMB by WMAP 2003



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Cosmic Microwave Background

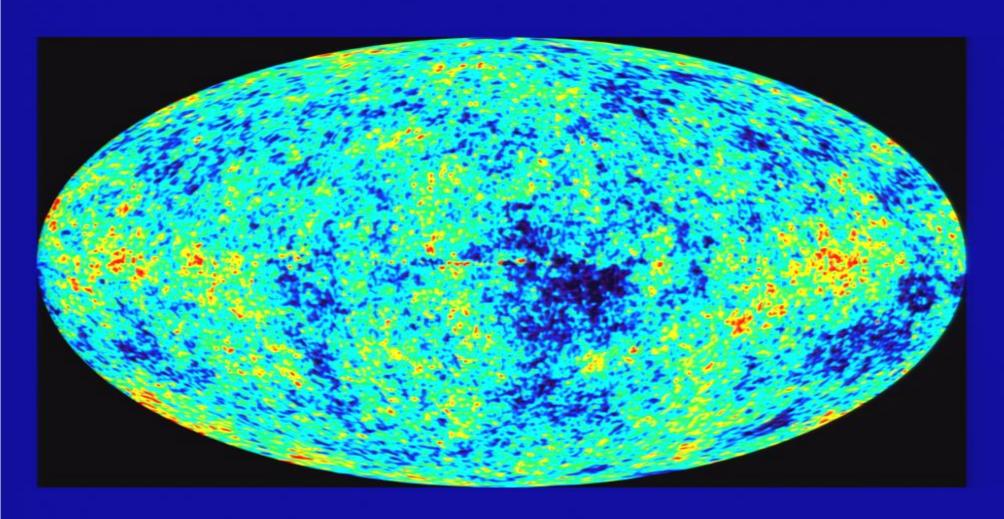


The primeval "fog" left over from when the Universe became transparent to radiation.

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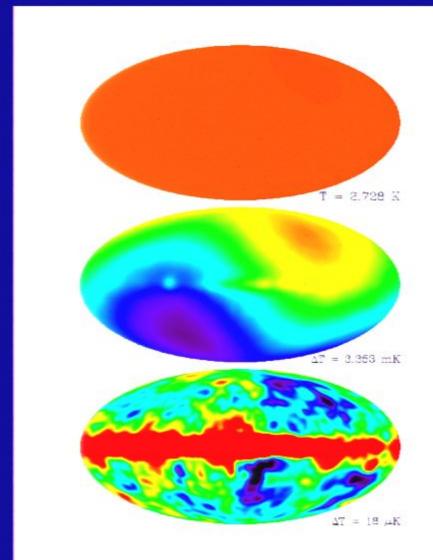
sa: 07080013 Page 87/133

CMB by WMAP 2003



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Cosmic Microwave Background

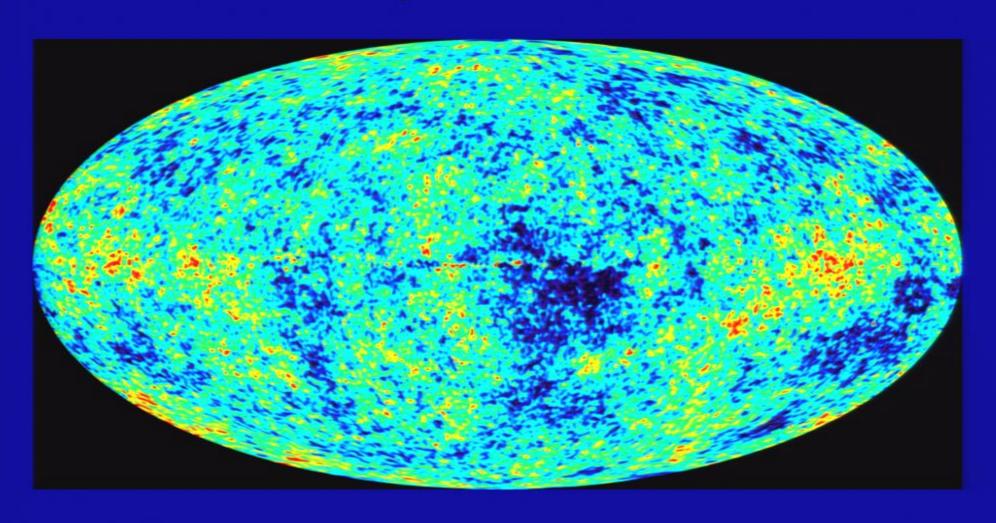


The primeval "fog" left over from when the Universe became transparent to radiation.

The micro-K ripples are due to redshifting from gravitational wells at z ~ 1000.

sa: 07080013 Page 89/133

CMB by WMAP 2003



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Very Large-scale Structure

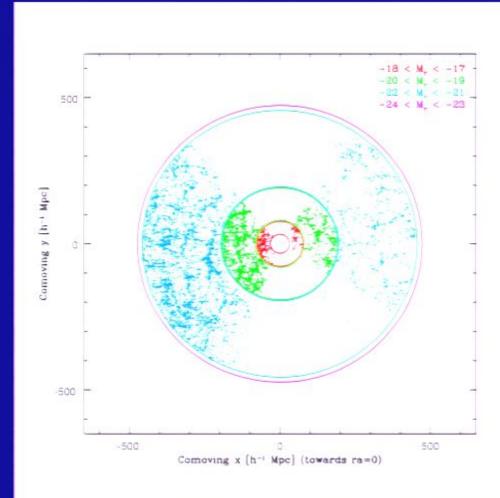
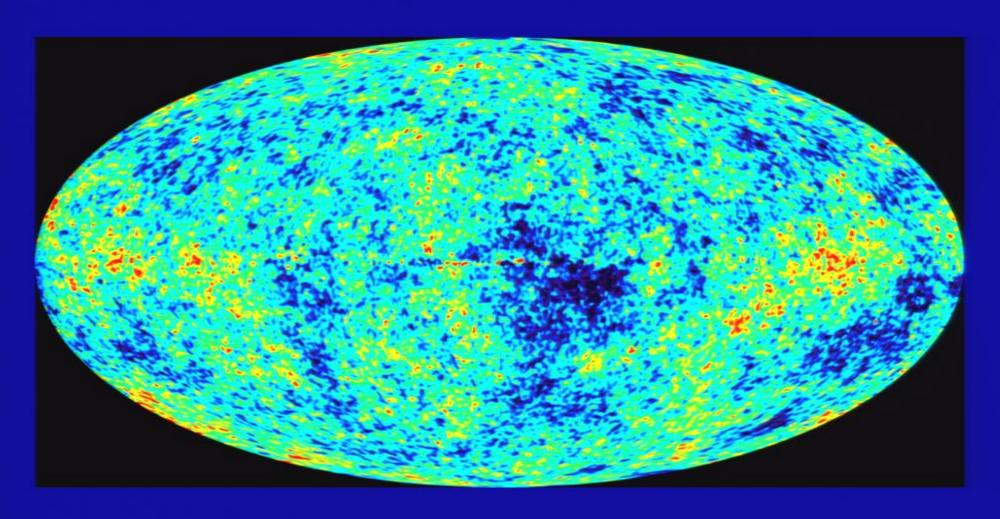


Fig. 5.— The distribution of galaxies within 5—of the equatorial plane is shown for the volume-limited subsamples L1, L3, L5 and L7 from Table 1.

Gradual transition to homogeneous Universe.

The structure that is visible on scales of 150 Mpc is the descendent of the 1 deg spots in the CMB!

CMB by WMAP 2003



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Very Large-scale Structure

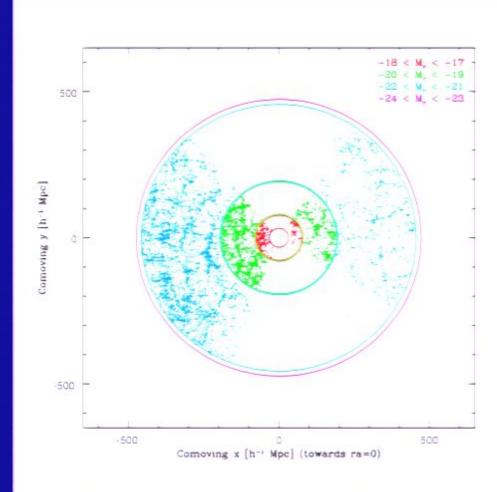
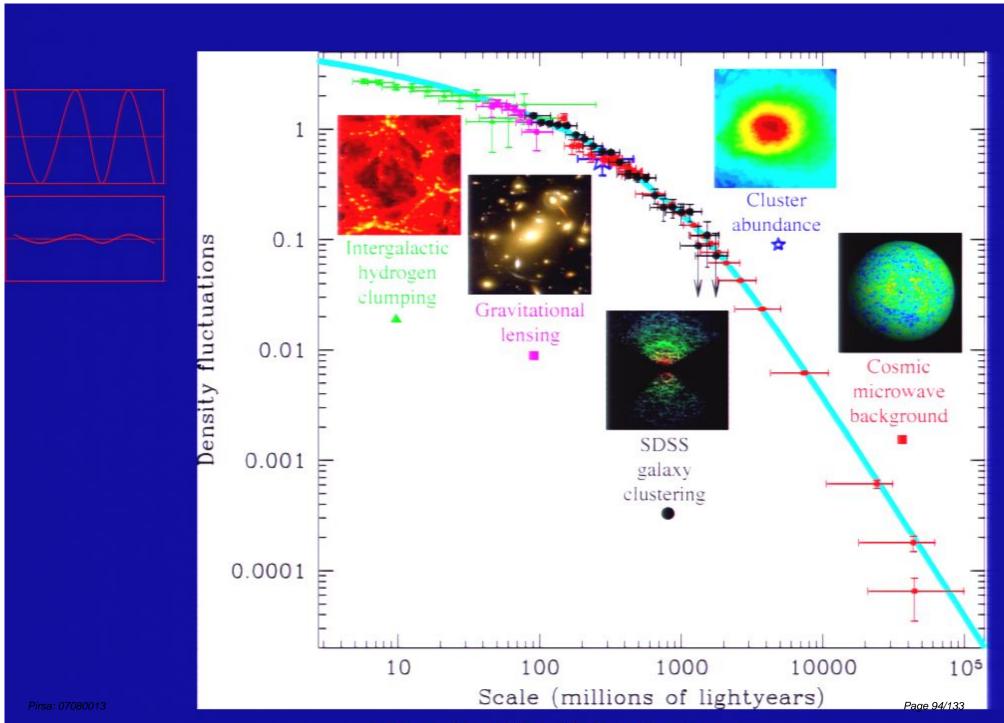


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Wavelength of fluctuation

Very Large-scale Structure

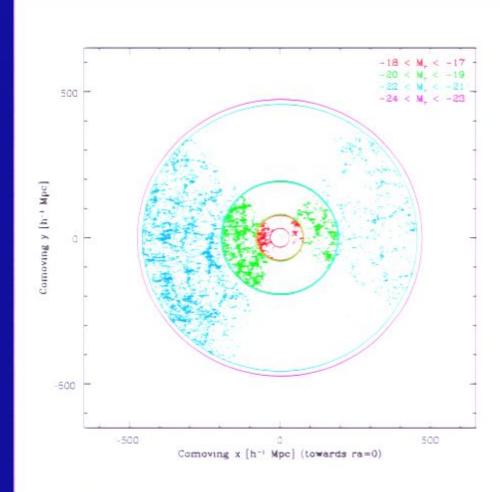
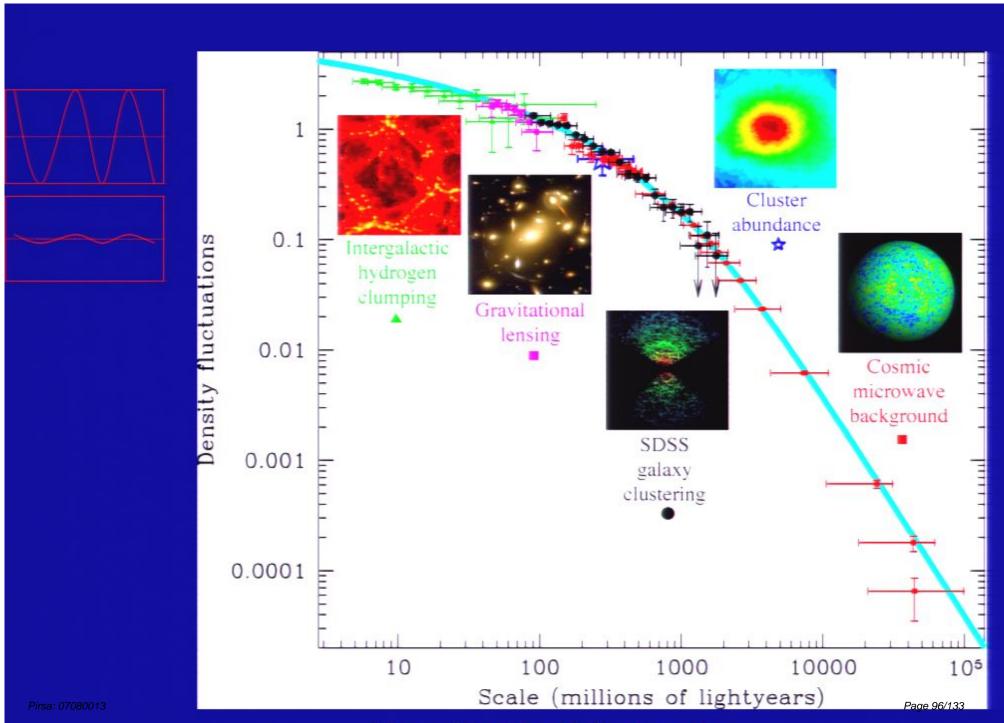


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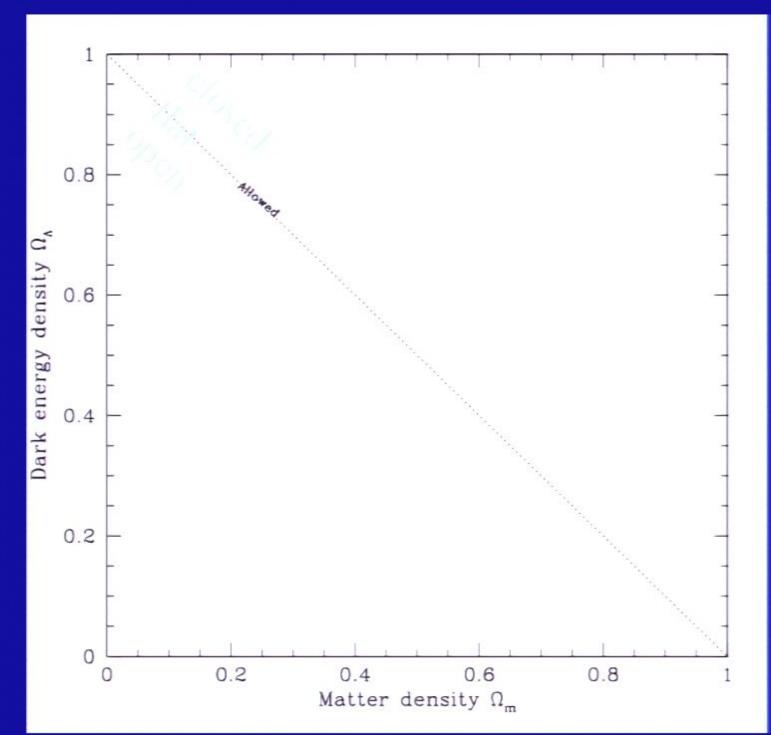
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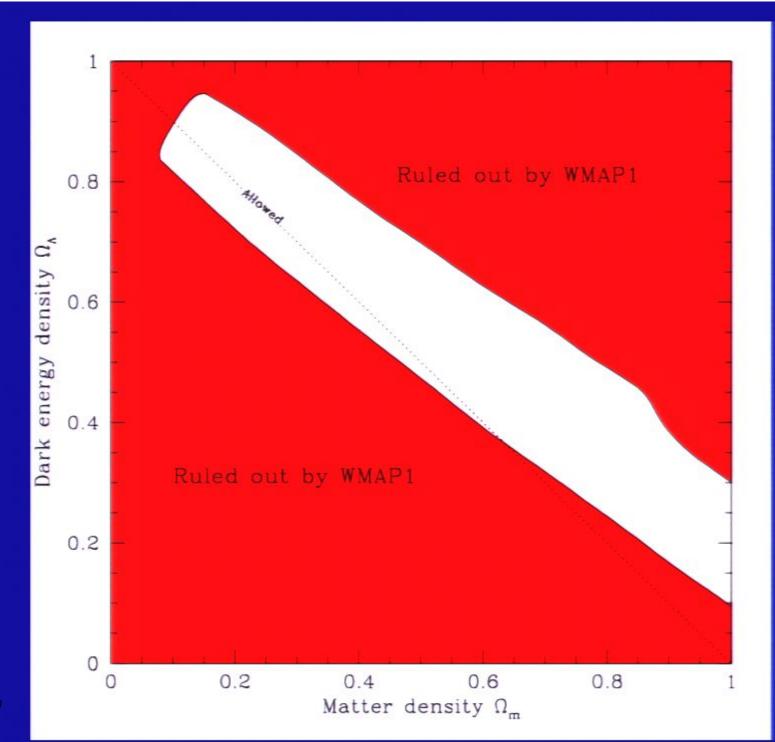


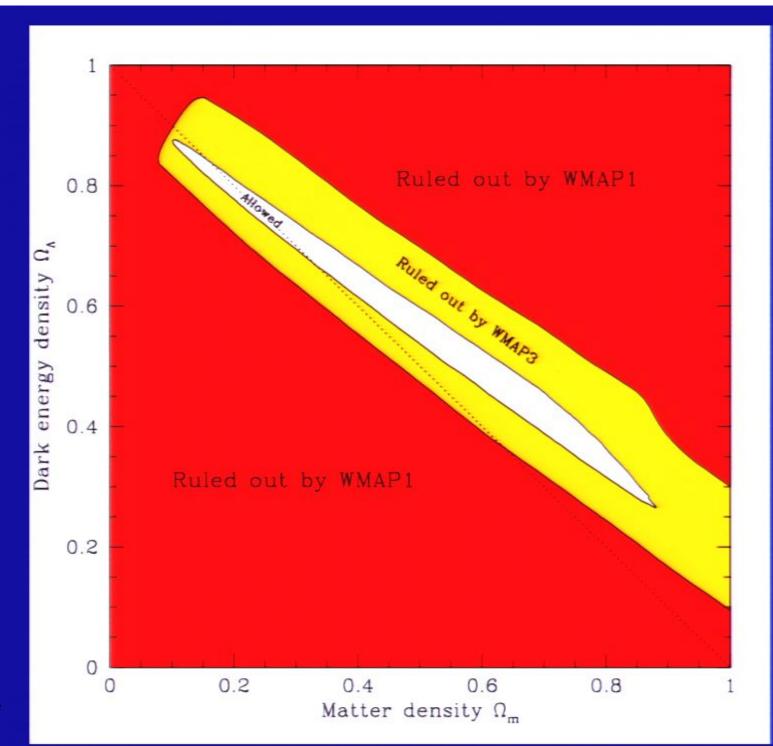
Wavelength of fluctuation

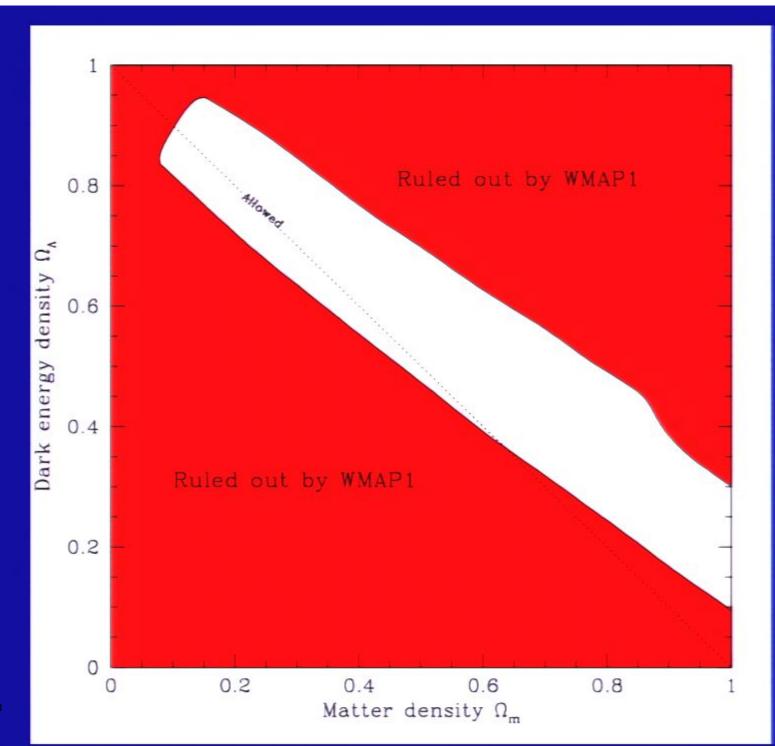
.... Skip hundreds of man-years of theoretical and observational work

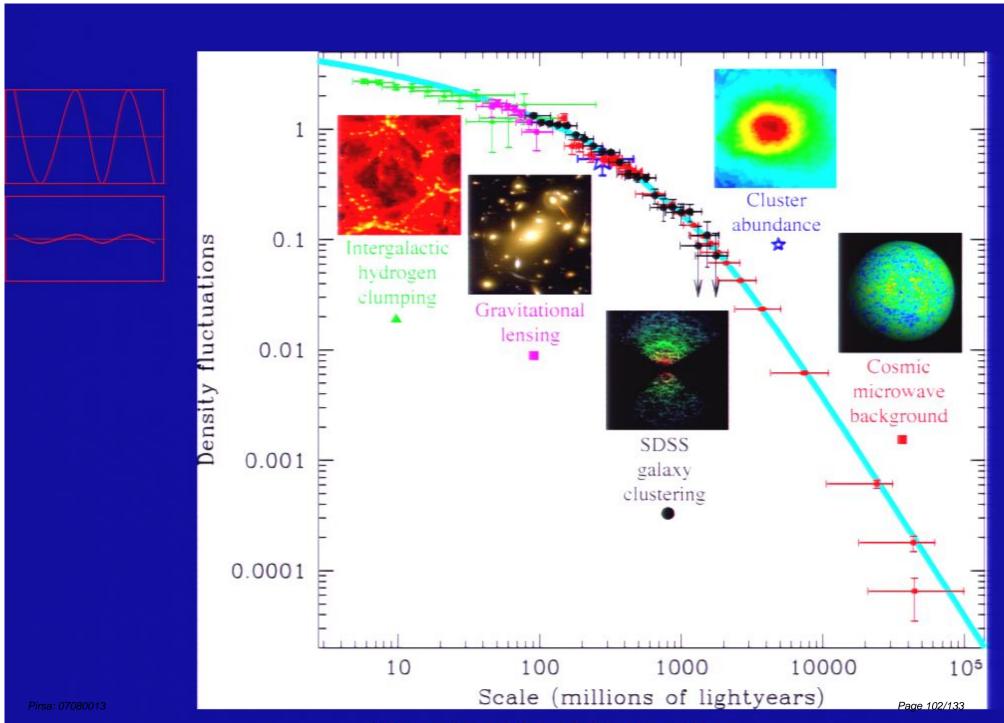
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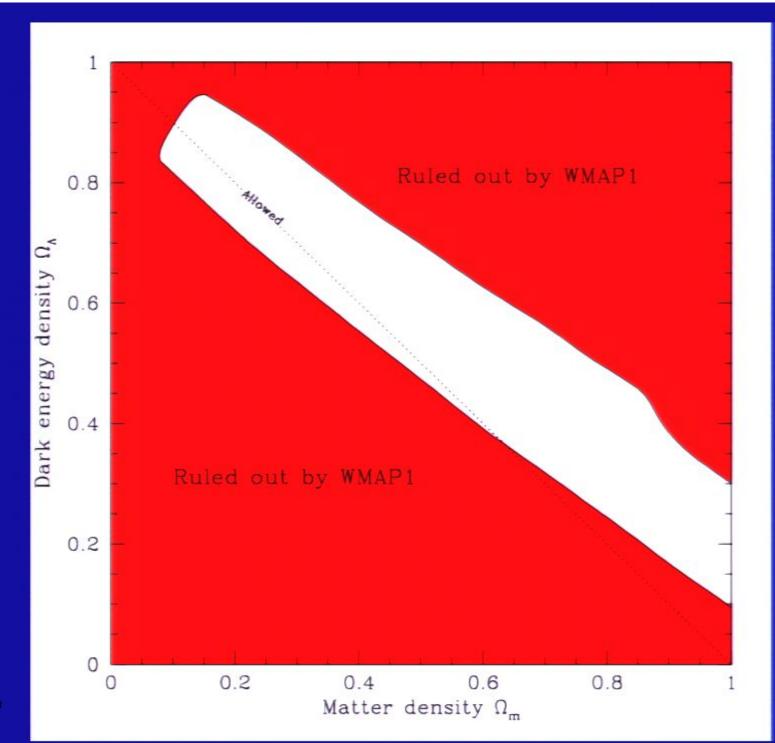


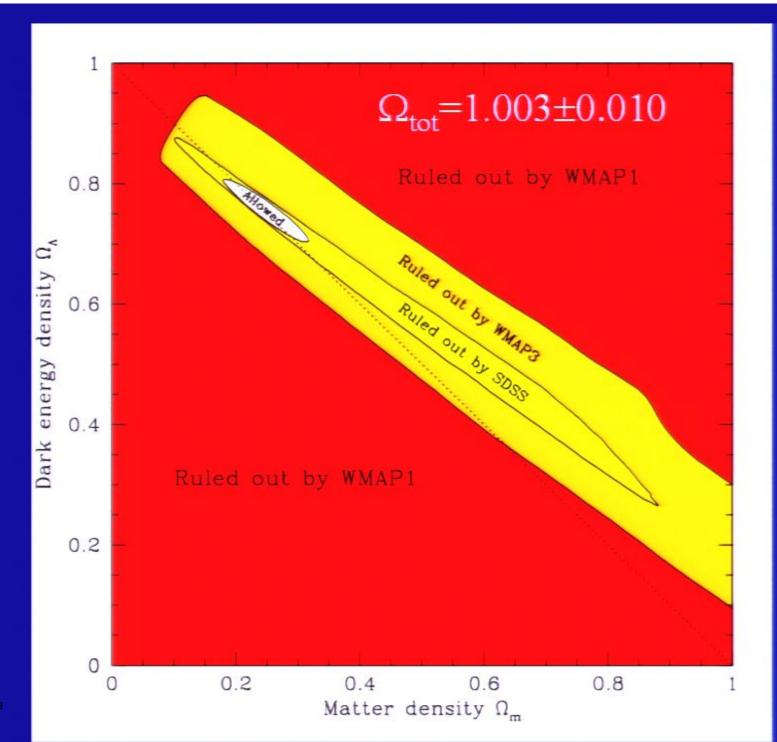






Wavelength of fluctuation



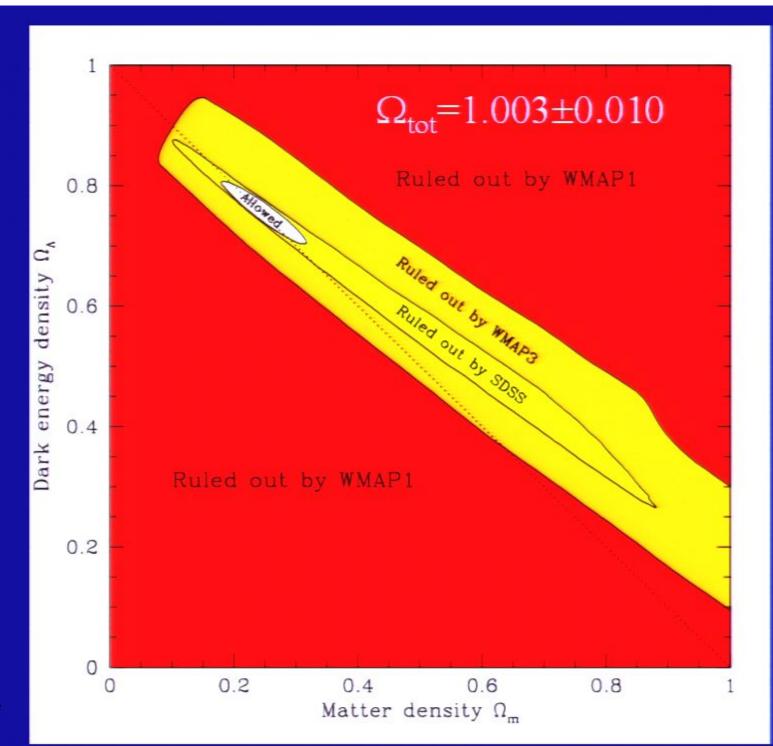


Consistency

- Clusters
 - Agreement amongst methods
 - All require 6-7x more matter than can be accounted for in gas and stars
- Peculiar velocities
- Large-scale structure and the CMB

Require dark matter (20-25%) and dark energy (70-75%) in addition to baryonic matter (~4%)

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Consistency

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FAQ

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- Q: Can't the Dark Matter be made of baryons
 - Black Holes
 - Jupiters
 - Bricks

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- Q: Can't the Dark Matter be made of baryons
 - Black Holes
 - Jupiters
 - Bricks
- A: No
 - Omega_m = 0.25
 - But big bang nucleosynthesis and CMB data limit the density of baryonic material to only 0.05

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Pirsa: 07080013 Page 111/133

• Q: What's the particle's mass?

Pirsa: 07080013 Page 112/133

Pirsa: 07080013 Page 113/133

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Pirsa: 07080013 Page 114/133

Pirsa: 07080013 Page 115/133

• Q: What's the particle's mass?

Pirsa: 07080013 Page 116/133

Q: What's the particle's mass?

A: >roughly a keV.
 Otherwise it would affect the spectrum of fluctutations.

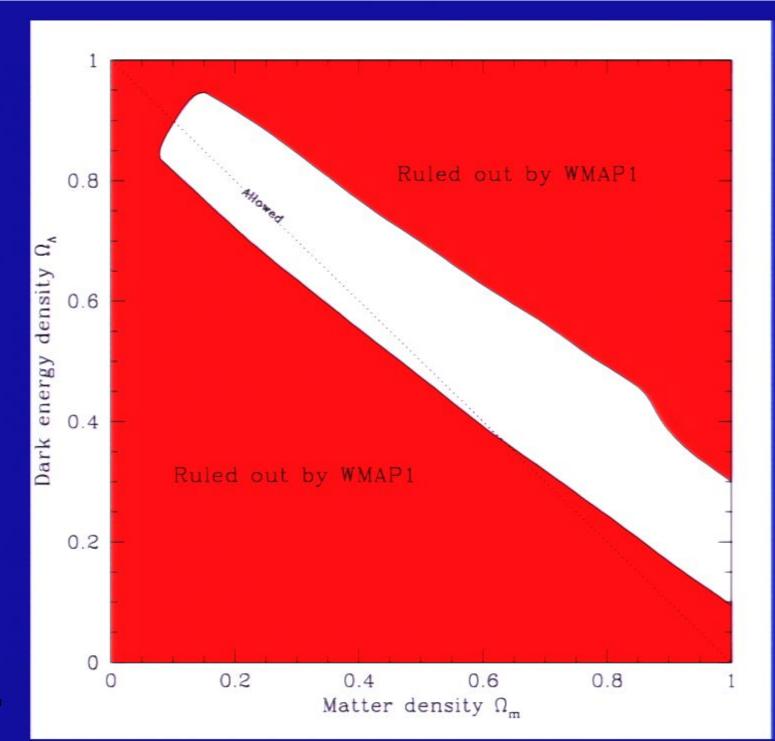
Pirsa: 07080013 Page 117/133

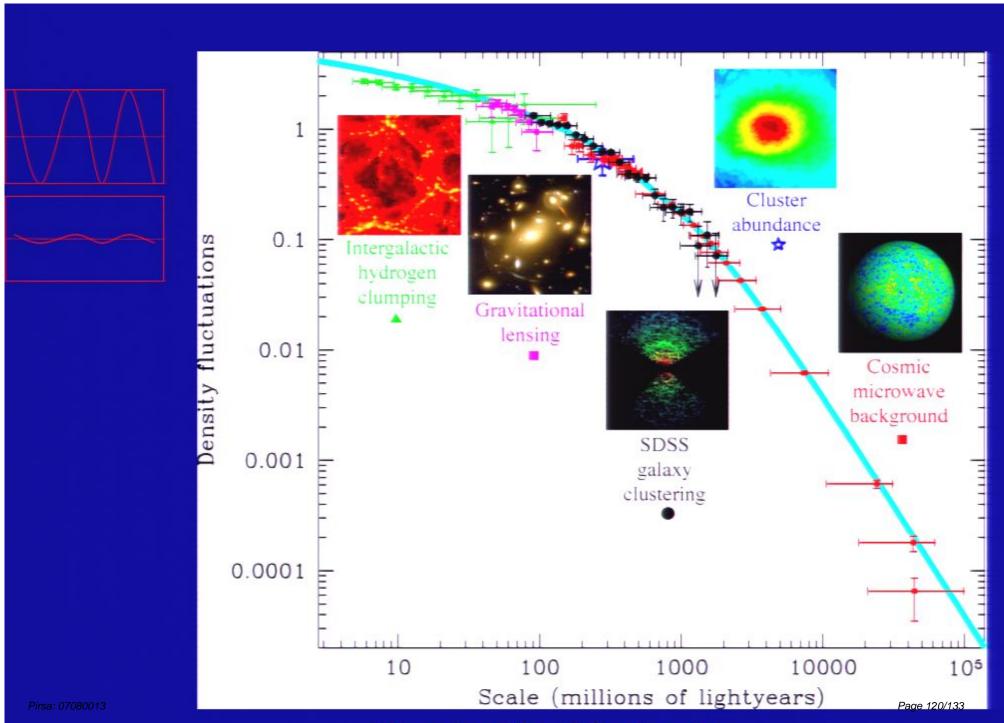
Consistency

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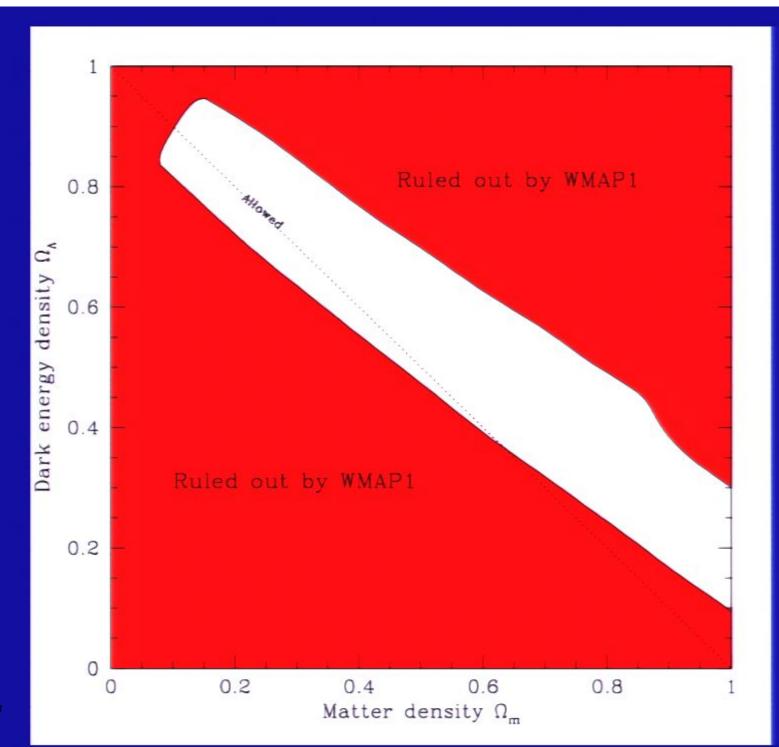
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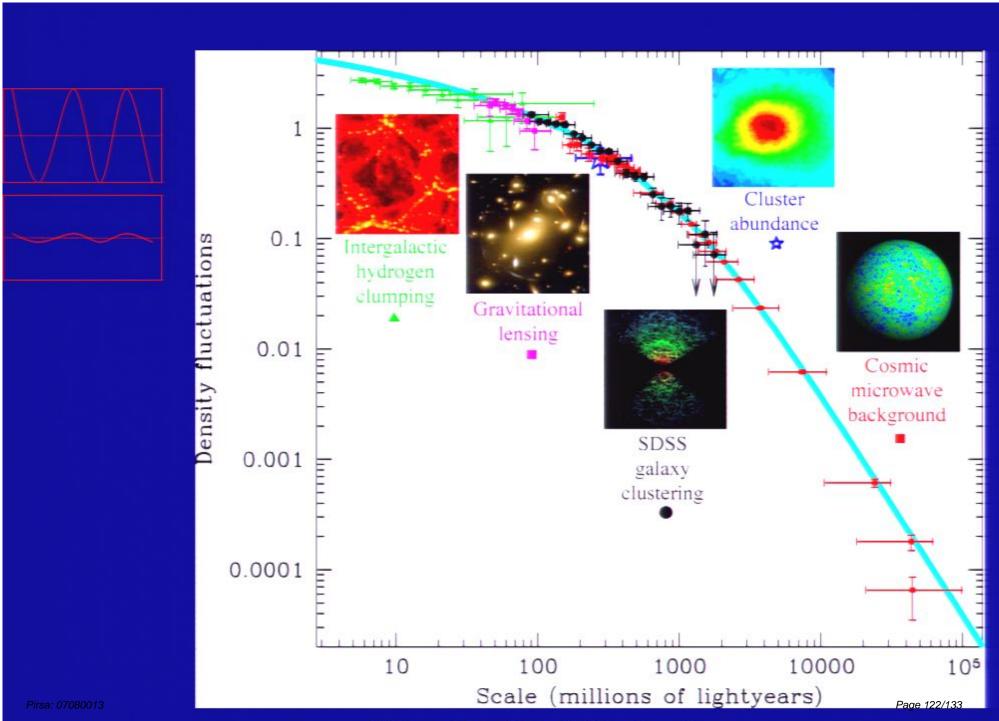
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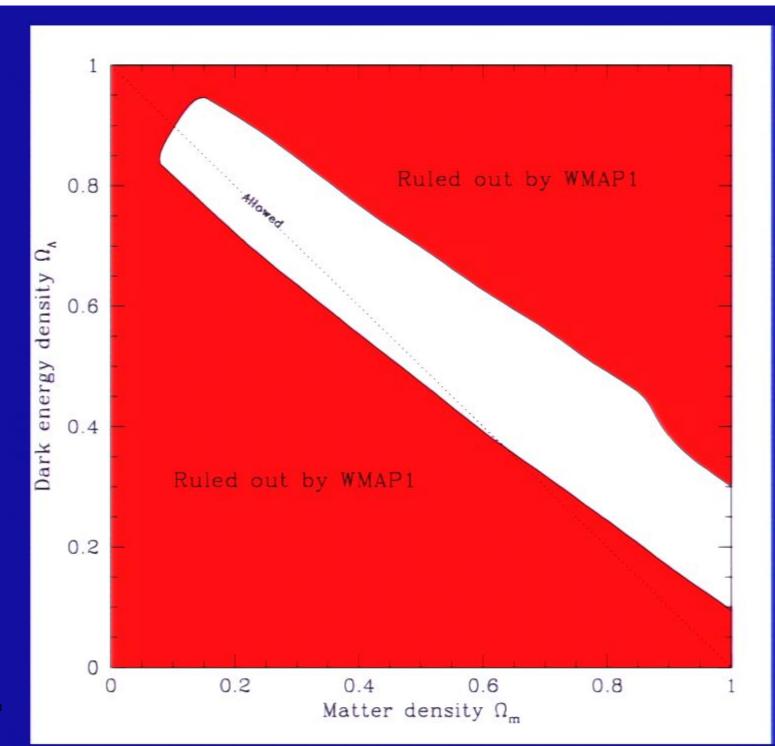


Wavelength of fluctuation





Wavelength of fluctuation



Consistency

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Pirsa: 07080013 Page 125/133

- Q: Can't the Dark Matter be made of baryons
 - Black Holes
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Pirsa: 07080013 Page 126/133

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Pirsa: 07080013 Page 127/133

Pirsa: 07080013 Page 128/133

• Q: What's the particle's mass?

Pirsa: 07080013 Page 129/133

Q: What's the particle's mass?

A: >roughly a keV.
 Otherwise it would affect the spectrum of fluctutations.

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- Q: What about modified gravity acting on baryons?
- A1: It is in general possible to modify gravity
 - MOND
 - TeVeS
 - etc

to explain individual spherical systems (e.g. galaxy rotation curves) by adjusting one or two parameters.

It is difficult to explain systems (clusters, large-scale structure) with very different masses using the *same* parameters.

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A2: "Bullet" Cluster

collisionless

dark matter
(blue) (from
weak
gravitational
lensing)

gas (pink) (from X-ray emission)

collisionless stars (yellow)



• The End

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