

Title: Monodromy in the CMB: Gravity Waves and String Inflation

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Abstract: The sensitivity of inflationary models to Planck-suppressed operators motivates modeling inflation in string theory. The case of high-scale inflation is particularly interesting both theoretically and observationally. Observationally it yields a gravity wave (B mode polarization) signature, and theoretically it requires a large field excursion which is particularly sensitive to UV physics. I'll present a simple mechanism derived recently in collaboration with A. Westphal for obtaining large-field inflation, and hence a gravitational wave signature, from string theory. The simplest version of this mechanism, arising on twisted torus compactifications of string theory, yields an observationally distinctive version of chaotic inflation with a potential proportional to the $2/3$ power of the inflaton, falsifiable on the basis of upcoming CMB measurements. This mechanism for extending the field range arises widely in string compactifications, though in all cases it requires sufficient symmetry to control the corrections to the slow-roll parameters. I will finish by describing further developments in this direction.

Monodromy in the CMB:



Gravity waves and String Inflation

with A. Westphal 0803.3085 [hep-th]

- Works in progress with
 - Aharony; McAllister, AW
(A. Westphal talk)
 - Green, Horn, Senatore

Inflation

Guth '81
Linde '82
AS '82

$$ds^2 = -dt^2 + a^2(t) d\vec{x}^2 + \dots$$

$$H = \frac{\dot{a}}{a} = \text{const}$$

provides a solution

to standard cosmological problems
within effective field theory,
diluting high-scale relics, but
it is nonetheless UV-sensitive:

$$\epsilon \equiv -\frac{\dot{H}}{H^2}, \quad \tilde{\eta} \equiv \frac{\dot{\epsilon}}{\epsilon H}, \quad s = \frac{\dot{c}_s}{c_s H}$$

must be $\leq 10^{-2}$ to inflate, but
get $\mathcal{O}(1)$ contributions from

dimension 6 Planck-suppressed
operators: In slow-roll inflation,

$$\eta = M_p^2 \frac{V''}{V} \sim 1 \quad \text{from} \quad V(\phi) \frac{(\phi - \phi_0)^2}{M_p^2}$$

⇒ Useful to formulate inflation
in UV-complete theory of gravity

This UV-sensitivity is especially strong
in any inflation model with observable
tensor modes in the power spectrum:

Lyth: observable tensor modes ⇒ $\Delta\mathcal{Q} > M_p$ during inflation

Brief review of perturbations

$$ds^2 = -N^2 dt^2 + h_{ij} (dx^i + N^i dt)(dx^j + N^j dt)$$

$$h_{ij} = a^2(t) [e^{2\mathcal{S}} \delta_{ij} + \gamma_{ij}]$$

$a^2(t)$
 $e^{2\mathcal{S}}$

scalar perturbation
 ($\delta\mathcal{Q} = 0$ gauge)

$\partial_i \gamma_{ij} = 0 = \gamma_{ii}$
 tensor perturbations

Scalar perturbation :

e.g. Slow-roll inflation :

- Start in gauge $\delta\phi \neq 0, \delta = 0$
- Action for $\delta\phi$ is that of
 \approx massless field in dS

• solutions:

$$\begin{cases} u(t) \\ u^*(t) \end{cases} = \frac{H}{\sqrt{2k^3}} \left(1 \mp \frac{ik}{H} e^{-Ht} \right) e^{\pm \frac{k}{H} e^{-Ht}}$$

$\rightarrow \frac{H}{\sqrt{2k^3}}$ once $\frac{k}{a} < H$

$$\delta\phi = a u(t) + a^\dagger u^*(t)$$

- $\Rightarrow \langle \delta\phi_k \delta\phi_{k'} \rangle \rightarrow (2\pi)^3 \delta^{(3)}(\vec{k} + \vec{k}') \frac{H^2}{2k^3}$
- similarly $\langle \gamma_{\vec{k}}^s \gamma_{\vec{k}'}^{s'} \rangle \rightarrow (2\pi)^3 \delta^{(3)}(\vec{k} + \vec{k}') \delta_{ss'} \frac{2H^2/m_p^2}{2k^3}$

...

$$\bullet \Rightarrow \langle \delta \mathcal{Q}_k \delta \mathcal{Q}_{k'} \rangle \rightarrow (2\pi)^3 \delta^{(3)}(\vec{k} + \vec{k}') \frac{H^2}{2k^3}$$

$$\bullet \text{ similarly } \langle \gamma_{\vec{k}}^s \gamma_{\vec{k}'}^{s'} \rangle \rightarrow (2\pi)^3 \delta^{(3)}(\vec{k} + \vec{k}') \delta_{ss'} \frac{2H^2/M_{\text{pl}}^2}{2k^3}$$

In the case of the scalar, change to gauge $\mathcal{S} \neq 0, \delta \mathcal{Q} = 0$ ($h_{ij} = a^2(t) [e^{2\mathcal{S}} \delta_{ij} + \gamma_{ij}]$)

Bardeen et al, Mukhanov et al:

\mathcal{S} constant outside horizon

$$\mathcal{S} = \frac{H}{\dot{\mathcal{Q}}} \delta \mathcal{Q} \Rightarrow \left\{ \begin{array}{l} P_{\mathcal{S}} = \frac{H^4}{12\pi^2 \dot{\mathcal{Q}}^2} \\ P_{\gamma} = \frac{2H^2}{\pi^2 M_{\text{pl}}^2} \end{array} \right.$$

$$r \equiv \frac{P_{\gamma}}{P_{\mathcal{S}}} = \frac{24\dot{\mathcal{Q}}^2}{H^2 M_{\text{pl}}^2}$$

* Lyth '97: $r \leftrightarrow \frac{\Delta \mathcal{Q}}{M_{pl}}$

$$N_e = \int \frac{da}{a} = \int \frac{\dot{a}}{a} dt = \int H dt = \int \frac{H}{\dot{\mathcal{Q}}} d\mathcal{Q}$$

$$= \int \left(\frac{H M_{pl}}{\sqrt{24} \dot{\mathcal{Q}}} \right) \left(\frac{d\mathcal{Q}}{M_{pl}} \sqrt{24} \right)$$

vary slowly during inflation

$$\Rightarrow N_e \simeq \sqrt{24} \frac{\Delta \mathcal{Q}}{M_{pl}} \frac{1}{r^{\frac{1}{2}}}$$

$$\Rightarrow \boxed{\frac{\Delta \mathcal{Q}}{M_{pl}} \simeq r^{\frac{1}{2}} \frac{N_e}{\sqrt{24}}}$$

$$\Rightarrow \text{for observable } r \gtrsim 0.01,$$

$$\boxed{\Delta \mathcal{Q} \gtrsim M_{pl}} \quad \text{(also true in } G < 1 \text{ case)}$$

In slow-roll inflation, $V = 3M_p^2 H^2$

$$\ddot{\phi}_0 + 3H\dot{\phi}_0 + V'(\phi_0) \equiv 0$$

$$\delta\ddot{\phi}_k - \frac{k^2}{a^2}\delta\phi_k + 3H\delta\dot{\phi}_k + \frac{1}{2}V''(\phi_0)\delta\phi \equiv 0$$

$$\epsilon \equiv \frac{1}{2}M_p^2\left(\frac{V'}{V}\right)^2 \lesssim 10^{-2}, \quad \eta = M_p^2\frac{V''}{V} \lesssim 10^{-2}$$

$$\Rightarrow \left(r = \frac{24\dot{\phi}^2}{H^2 M_p^2} = 24M_p^2\left(\frac{V'}{V}\right)^2 = 16\epsilon \right)$$

\Rightarrow Must ensure $\epsilon \ll 1, \eta \ll 1$

over range $\Delta\phi \gg M_p$ in

any model with observable inflationary
gravity waves.

UV Sensitivity of Inflation

① Terms of order

$$V \cdot \frac{(\mathcal{Q} - \mathcal{Q}_0)^2}{M_p^2} \quad (\text{dimension 6})$$

in the effective action can ruin inflation

② $\frac{\Delta \mathcal{Q}}{M_p} \simeq r^{\frac{1}{2}} \frac{N_e}{\sqrt{24}} \quad (\text{Lyth})$

GUT-scale inflation (with observable tensor modes) $\Leftrightarrow \Delta \mathcal{Q} > M_p$

③ General Single-field inflation involves higher derivative terms which affect solution & perturbations
cf Non-Gaussianity Creminelli, DBI, ...

From a different point of view,
large-field "chaotic" inflation

A. Linde '83 seems very simple.
cf symmetries

- We find a mechanism for large-field inflation using monodromy, and realize it in a specific model \rightarrow

$$V(\varphi) \Big|_{\varphi \gg M_p} \approx \mu^{\frac{10}{3}} \varphi^{\frac{2}{3}}, \quad \Delta\varphi \sim 9 M_p, \quad n_s \approx 0.98, \quad r \approx 0.04$$

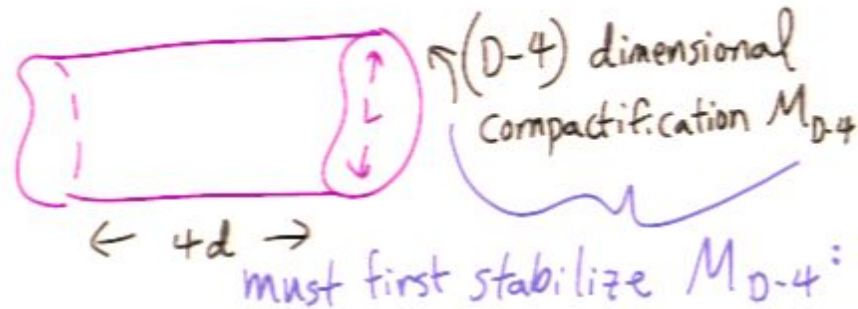
in a basic class of string compactifications

- Work in progress on other examples (e.g. Calabi-Yau models, with $V \propto \varphi$)

other interesting recent approaches include

N-flation Dimitrios Kastrup, McGreevy, Wacker wrapped brane inflation, Becker, LeBlond, Susskind

Modeling inflation in string theory is a laborious process:

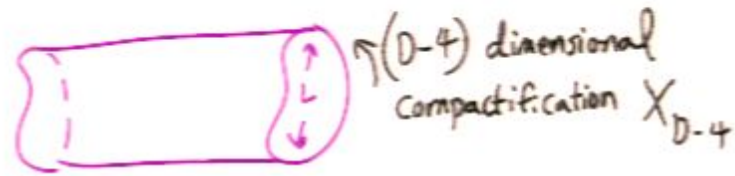



many scalar field "moduli" with generically steep potential $U_{\text{mod}}(L, g, \dots)$ depending on discrete quantum #'s (BP, FMSW)

2001-2003: moduli stabilized in corners
 $D > 10$ ES, MSS '01 '02 ; II B GKP '01 DOF Calabi/Yau/querredo '03 D3-D7
 KKLTT '03

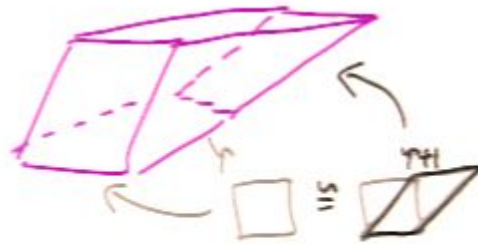
→ promising $\Delta\phi \ll M_p$ models KKLMMT, Racetrack
 → Novel mechanism(s) DBI ST, AST Roulette, Accidental
 → observational opportunities cosmic strings CMP non-Gaussianity DBI

2005-2007: • IIA on CY → AdS DGKT... KSS... HKTT.
 • IIA on Nil manifold → dS ES '07
 Bianchi II, -, Schenk-Schwartz, Kallosh/Myers, ...



The simplest compactification
is a torus 
(periodic boundary conditions)

The next simplest* is a "twisted
torus"



cf also

$$K3 \times T^2 / \mathbb{Z}_2$$

Haack, Kallosh, Krause,
Linde, Lust, Zagerman

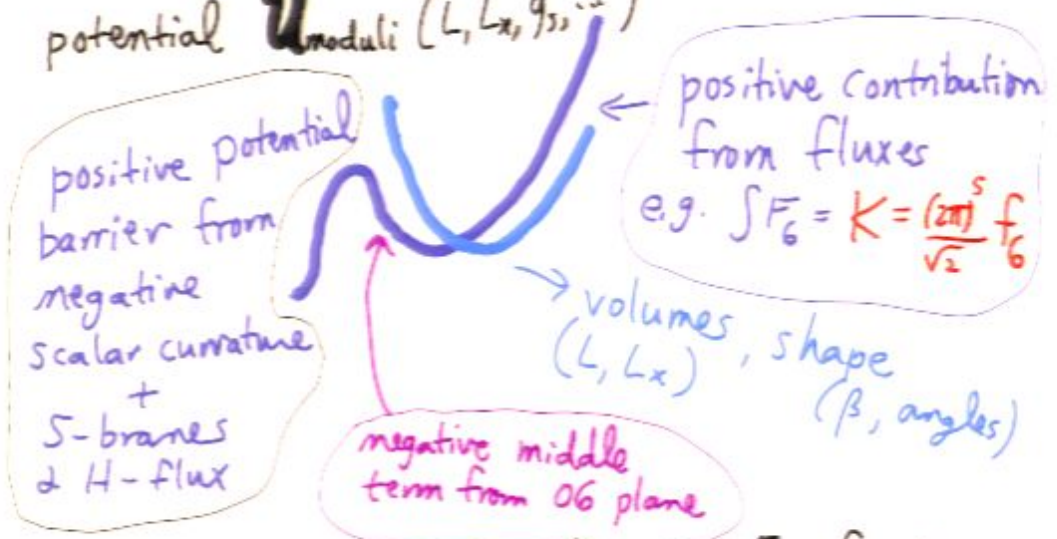
Executive summary of IIA dS

construction:



$$ds^2 = L_a^2 \left(\frac{du_i^2}{\beta} + \beta du_i^2 \right) + L_x^2 (dx' + M u_i du_i)^2 \quad \text{over } \mathbb{R}^3$$

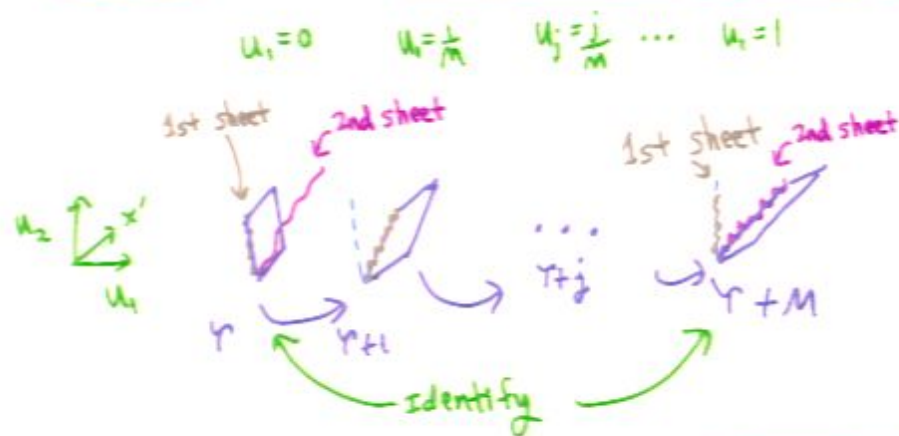
potential $\mathcal{U}_{\text{moduli}}(L, L_x, g_{SS}, \dots)$



- Simplest version: $\frac{M}{K} \sim 10^{-5}$, $f_6 \sim 100$,
 α' & loop corrections small (local 10d susy)
 subtlety: $m_{KK}/m_{\text{mod}} \text{ not parametrically } \gg 1$
- Elaborate version: separate all scales parametrically with additional ingredients

Nil manifold (Twisted Torus):

$$ds^2 = L_u^2 \left(\frac{du_1^2}{\beta} + \beta du_2^2 \right) + L_x^2 (dx' + M u_1 du_2)^2$$



D4 brane wrapped on u_2 direction:
 Scalar fields arise from transverse motion.

- As move in u_1 direction away from $u_1=0$, the brane wraps a larger cycle \Rightarrow heavier
- As move around u_1 circle, the D4 does not come back to itself: Monodromy
 \Rightarrow Scalar field range is unbounded geometrically (at fixed $M_p^2 \sim \text{Vol}/g_s^2$)

Monodromy occurs frequently
in string compactifications

e.g. • CYs (Candelas et al, ...
(work in progress)

- fluxes, non-geometrical fluxes,
monodromies


Schenk-Schwarz, Kaloper-Myers, Hellerman, McGreevy, Williams
Kachru et al, Hull et al, Lawrence-Schulz-Wecht, ...

⇒ The mechanism we study here
may arise far more generally

cf Westphal talk: monodromy in axion
directions in closed string moduli space
in the presence of wrapped branes



This geometrically unbounded field range contrasts with the (special) case of D3-branes:



$$M_p^2 = \frac{L^6}{(2\pi\alpha')^2 g_s^2}$$

also bounded by L

yields bound $\frac{\Delta Q}{M_p} \ll 1$

Baumann/McAllister

Becker LeBlond Shandera, Kobayashi et al, Lidsey, Huston, ^{ward}...

Wrapped branes, or large numbers of branes, yield larger field range geometrically, but in previously studied cases they led to potentially destabilizing back reaction. \rightarrow Check dynamics and back reaction in our case:

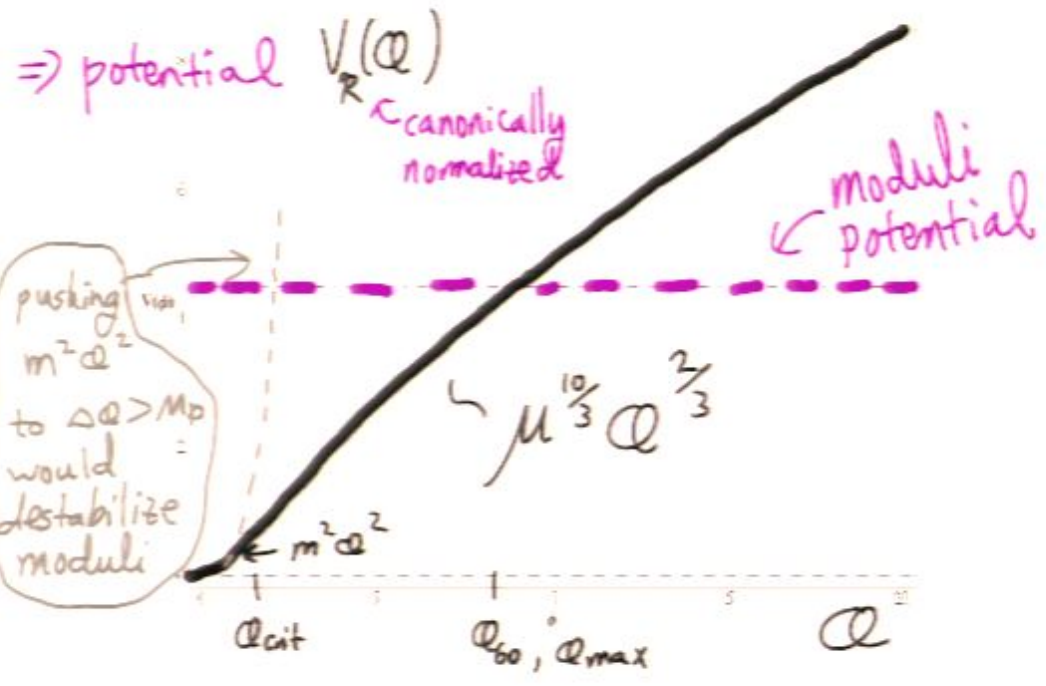
The D4 effective action is

$$S_{D4} = -\frac{1}{(2\pi)^4 \alpha'^2} \int d^5 \xi \sqrt{\det G_{MN} \partial_\alpha X^M \partial_\beta X^N} + S_{CS} + \alpha' \cdot \text{h.d.} + \text{loops}$$

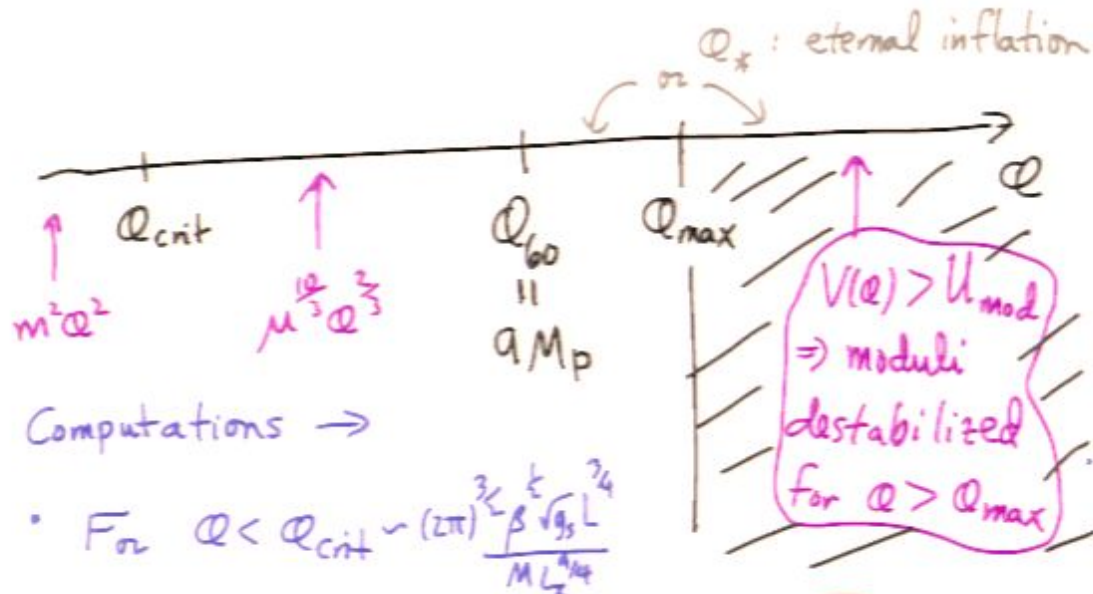
\leftarrow compactification geometry + local sources

$$S_{D4, R} = \frac{1}{(2\pi)^4 \alpha'^2 g_s} \int d^4 x \sqrt{-g} \left\{ \frac{L u^2 (U_1^2)}{\beta (2)} \sqrt{\beta L u^2 + M^2 L_x^2 u_1^2} - \sqrt{\beta L u^2 + M^2 L_x^2 u_1^2 + \dots} \right\}$$

$\underbrace{\hspace{10em}}_{\text{Nil geometry}}$



Important crossover scales :



$V(\phi) \xrightarrow{\mathcal{R}} \frac{1}{2} m^2 \phi^2$ and $\frac{1}{2} m^2 \phi^2 \sim \left(\frac{\phi}{M_p}\right)^2 U_{mod, \mathcal{R}}$

$\Rightarrow \frac{1}{2} m^2 \phi^2$ not viable in this setup

(It would destabilize the moduli to push ϕ_{crit} to the $15 M_p$ required for $m^2 \phi^2$ chaotic inflation.) cf Kallosh & Linde

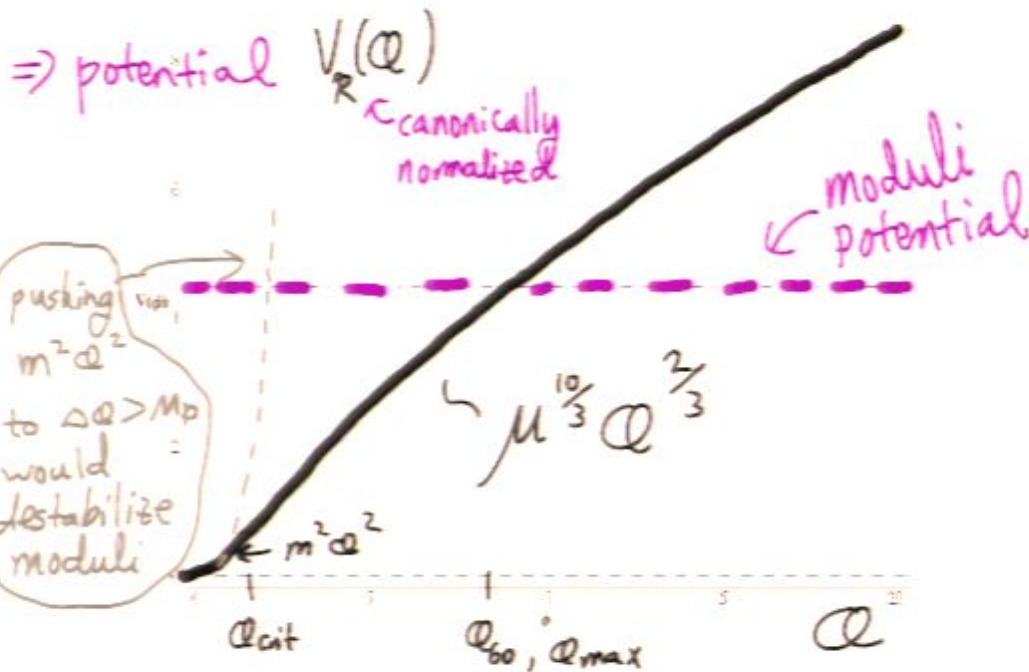
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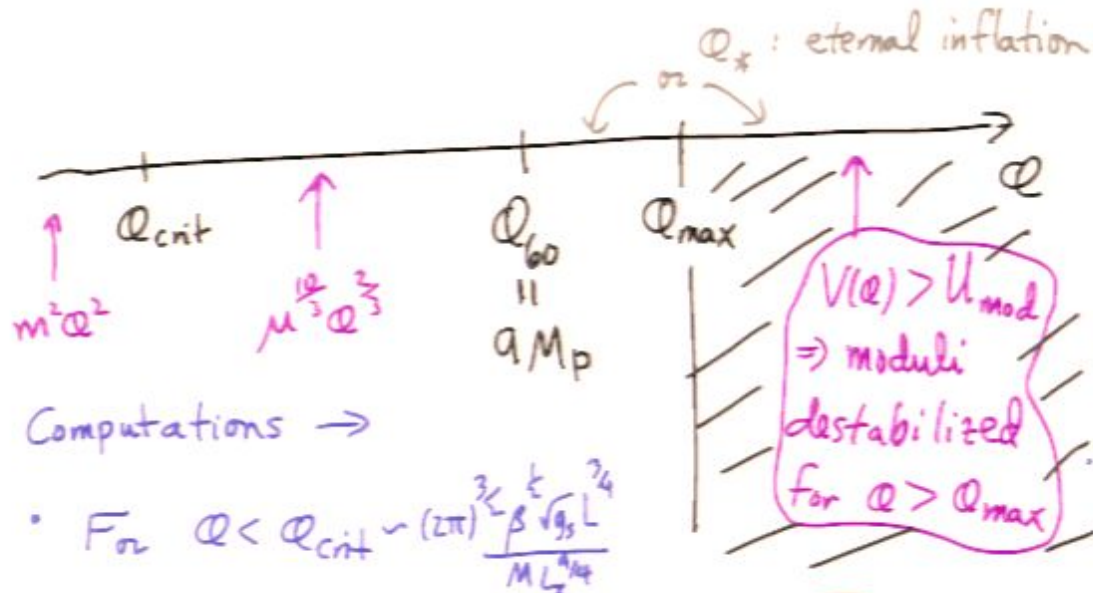
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(It would destabilize the moduli to push Q_{crit} to the $15 M_p$ required for $m^2 \phi^2$ chaotic inflation.) cf Kallosh Linde

... Computations \rightarrow

- $V(\mathcal{Q}) = \mu^{\frac{2\mathcal{Q}}{3}} \mathcal{Q}^{\frac{2}{3}}$ pertains

for $\mathcal{Q}_{\text{crit}} \ll \mathcal{Q} \ll \mathcal{Q}_{\text{max}}$

$$\left(\frac{2\pi}{\tilde{\gamma}}\right)^{\frac{2}{3}} \tilde{\gamma}^{-\frac{1}{2}} \quad \frac{\tilde{\gamma}}{(2\pi)^3} \cdot (\text{const})$$

where $\tilde{\gamma} = \frac{1}{\beta^{\frac{1}{2}}} \left(\frac{K}{M}\right)^{\frac{1}{2}} \gg 1$ in dS construction

- $N_e = 60 \Rightarrow \Delta\mathcal{Q} = 9M_p \leq \mathcal{Q}_{\text{max}}$
 $\Rightarrow \tilde{\gamma} \gtrsim 190$

- $\left(\frac{\delta\rho}{\rho}\right)^2 - P_s \sim 10^{-10} \sim \left(\frac{2\pi}{\tilde{\gamma}}\right)^{\frac{2}{3}} N_e^{\frac{2}{3}} \frac{1}{\tilde{\gamma}^{\frac{1}{2}}} \frac{1}{K^{\frac{3}{2}}} \cdot \text{const}$
 $\Rightarrow K \leq 10^6 \Leftrightarrow f_6 \leq 310 \Rightarrow \beta M^{\frac{1}{2}} \leq 0.04$

\Rightarrow Altogether modest parameters
e.g. $\beta \sim 0.04$ $M \sim 1$, $f_6 \sim 300$, $\Delta\mathcal{M}_1 \sim 20$
fits in simplest version of IIA dS

\Rightarrow So far, good candidate for model realizing our monodromy mechanism

⇒ So far, good candidate for model
realizing our monodromy mechanism

Now must check self-consistency

- back reaction

- effects of moduli-stabilizing
ingredients on ϵ & n_s
cf KKLMMT

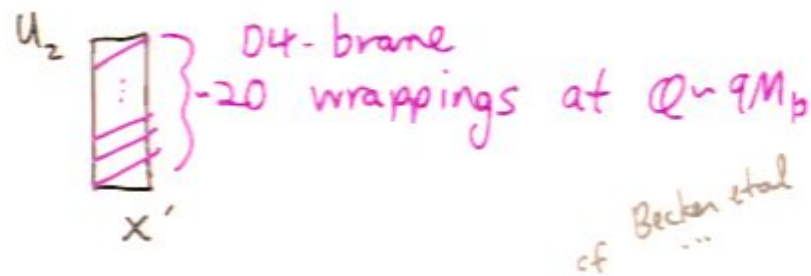
Δn of order 1 or 0.1 would ruin inflation
 Δn of order 0.01 affects n_s prediction
tilt

- generic α' & loop corrections

Back reaction:

$$ds^2 = L_u^2 \left(\frac{du_i^2}{\beta} + \beta du_i^2 \right) + L_x^2 (dx' + M u_i du_i)^2$$

$\Delta Q = 9M_p$ means $\Delta U_i \sim 20 M_{\text{pl}}^2$
in our model \Rightarrow



\rightarrow Negligible back reaction, and
negligible correction to G_N
from multiple species cf N-flation

Moduli shifts and $V_R(\mathcal{Q})$:

Inflaton potential $V_R(\mathcal{Q}; L e^{\frac{\sigma}{M_p}}, \dots)$
depends on moduli $\frac{\sigma}{M_p}$ as well as \mathcal{Q}

← canonically normalized

\Rightarrow \mathcal{Q} -dependent shifts of

moduli : $\frac{\sigma}{M_p} \sim \frac{\partial_\sigma V_R}{\partial_\sigma^2 (U_{\text{mod}} + V_R)} \sim \frac{V_R}{U_{\text{mod}}}$

\Rightarrow correction to \mathcal{Q} -dependence of full scalar potential $U + V$

$$U_{\text{tot}} \sim U_{\text{mod}}(L) + V_R(\mathcal{Q}, L) + c_{\text{ca}} \frac{V_R(\mathcal{Q}, L)^2}{U_{\text{mod}}(L)}$$

$$\Rightarrow \Delta \eta \sim \eta \frac{V_R}{U_{\text{mod}}} \leq \mathcal{O}(\eta) \checkmark$$

Must control total $\Sigma = \left(\frac{M_p^2 V'}{V} \right)^2$ and
 $\eta = M_p^2 \frac{V''}{V}$ over full range $\Delta\mathcal{Q} = 9M_p$



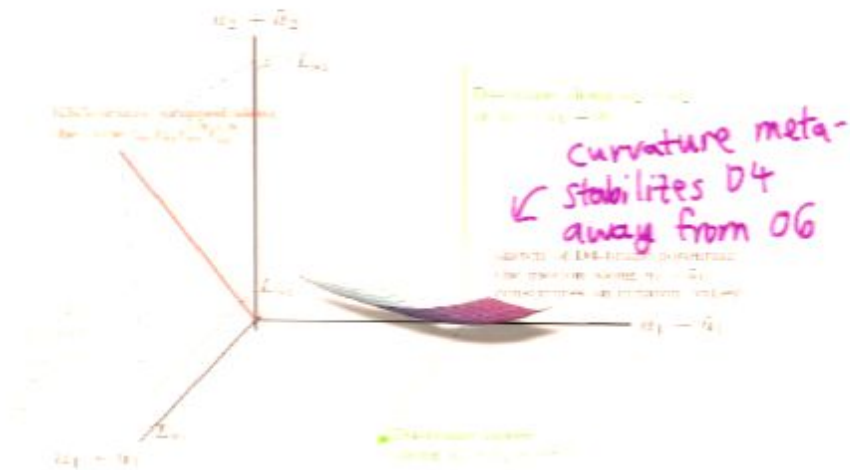
cf KKLMNT... Kachru
McAllister
Sundrum

$\Delta\eta \sim 1$ generic

This is somewhat easier than it sounds here, because of the monodromy ...

Since the D4-brane executes ≥ 20 circuits of the compactification during inflation, the methods for controlling Σ & η may be similar in each sub-Planckian interval $\Delta u_i = 1$

... and because of the symmetries and the extended nature of moduli-stabilizing ingredients in IIA dS construction:



The KK5-branes and O6-plane involved in moduli stabilization are extensive along $\mathcal{Q} \Rightarrow$

As in QFT formulation of chaotic inflation, symmetry prevents large corrections to $V(\mathcal{Q})$.

- $\alpha' \mathcal{R}$ + loop corrections
→ small corrections to \mathcal{E} & \mathcal{H}

- Parametric limit (arbitrarily small corrections) would entail additional ingredients (e.g. NS5 branes) as in IIA dS construction.

- Standard Model + Reheating not yet explicitly included
(Work in progress)

e.g. potential curvature corrections
are small and of a simple form:

$$S_{D4} \rightarrow \frac{1}{(2\pi)^4 (\alpha')^2} \int d^4x e^{-\frac{\sigma}{\alpha'}} \sqrt{\det(G_{mn} + \alpha' c R_{mn})} \partial_\alpha X^M \partial_\beta X^N$$

$$\cdot (1 + \check{c} \alpha' R + \dots)$$

(Putting all covariant possibilities in)

$$\text{Now } R_{u_1 u_1} = -\frac{L_x^2 M^2}{2L_u^2} \quad R_{u_2 u_2} = -\frac{L_x^2 M^2}{2L_u^4} (L_u^2 - L_x^2 M^2 u_1^2)$$

$$\text{and } R = \frac{L_x^2 M^2}{L_u^4} \rightarrow \ll 1$$

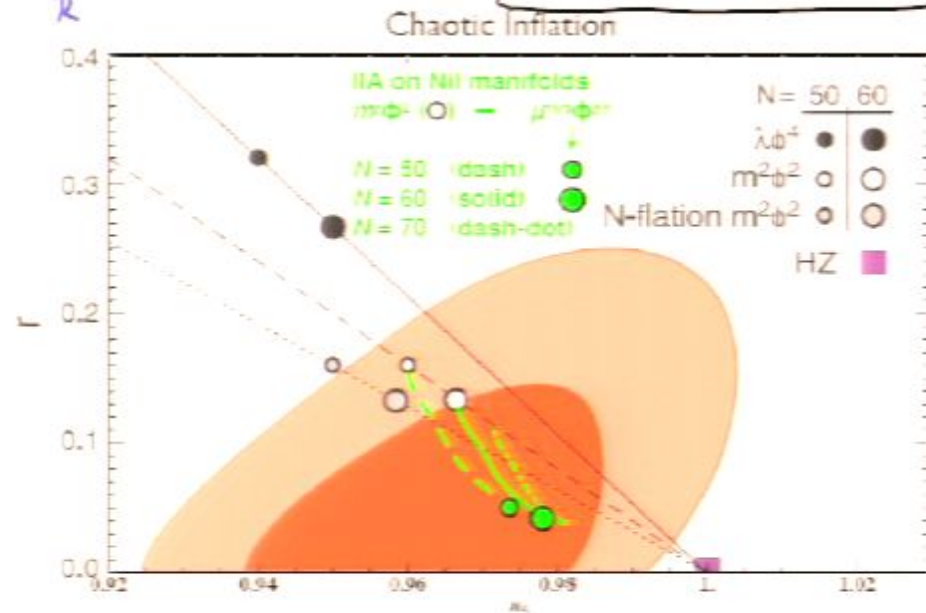
$$\text{while } G_{u_1 u_1} = L_u^2, \quad G_{u_2 u_2} = L_u^2 + L_x^2 M^2 u_1^2$$

\Rightarrow same shape $\mu^{1/3} \mathcal{Q}^{2/3}$, with
small $\Delta\mu$ from these corrections...

→ This appears to provide a viable model realizing monodromy mechanism

⇒ Observational predictions

$$V(\phi) = \mu \frac{10}{3} \phi^{\frac{2}{3}} \Rightarrow r \approx 0.04, n_s \approx 0.98$$



- For single-field version, $f_{NL}^{\text{squeezed}} \sim 0.01$, $f_{NL}^{\text{equilateral}} \approx 0 \Rightarrow$ distinct from $C_s \ll 1$ case
multifield extension required for f_{NL}^{squeezed}

The tensor signal is detectable
via CMB experiments sensitive to
polarization :



gravity wave \Rightarrow locally
anisotropic propagation of
CMB photons. Scattering
of CMB off e^- 's present during
re-ionization & recombination
 \rightarrow polarization

The observational situation is very
healthy. ("instant" gratification...)

Bock et al ("Weiss report")

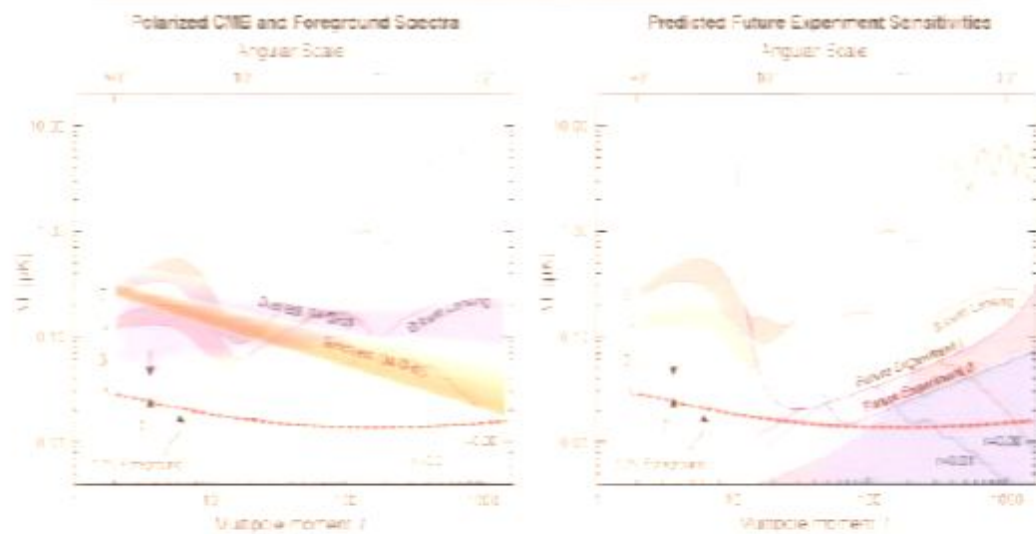


Figure 2.2: CMB Polarization Power Spectra, Backgrounds and Estimated Sensitivity of Future Experiments. Thin, wiggly curves in the two panels show the predictions for the angular power spectrum of the CMB polarization signal (E modes and B modes) in the standard cosmological model (as of 2005). The E signal is reasonably well predicted, but the B signal depends linearly on the gravitational wave amplitude, as measured by the tensor-to-scalar ratio, r . The B curves shown are for $r=0.3$ (red) and $r=0.01$ (blue). For $l < 20$, the thickness of the theory curves reflects the current degree of uncertainty about the epoch of reionization. The predicted B-mode signal due to the distortion of E modes by weak gravitational lensing is shown in green (see §3).

Left: Current estimates of the polarized Galactic foreground signals and their uncertainty, due to synchrotron emission from cosmic ray electrons and thermal emission from interstellar dust grains, as described in §4. The red dashed curve is an estimate for the residual foreground contamination after modeling using multi-frequency observations described in §4.

Right: Estimated instrumental sensitivities for a space mission of the type called for in our roadmap (grey shading) and two sample ground-based experiments (solid lines), based on the assumptions listed in §10.

- CLOVER, QUIET, BICEP/SPUD SPIDER (ground)
- POLARBEAR, EBEX, BRAIN, ... $\Delta r \sim 0.01!$
- CMBPOL? (satellite)

Observational Status :

Planck : $\Delta n_s \sim 0.01$
 $\Delta f_{NL} \sim 5-10$
or ~ 0.1

Ground-based Polarization expts:

$$\Delta r \sim 0.01$$

\Rightarrow Will distinguish wildly different mechanisms for inflation

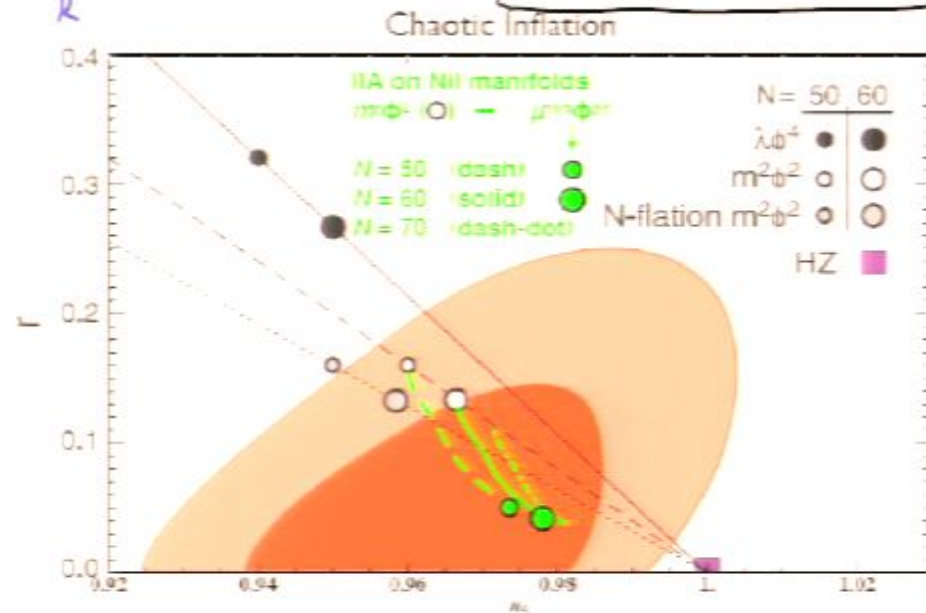
- small field cf KKLMAT, talks here
- large field monodromy (v-station)
- $c_s \ll 1$ (DBI)
- multiple fld

The combination of UV sensitivity & observational accessibility strongly motivates research in this direction.

→ This appears to provide a viable model realizing monodromy mechanism

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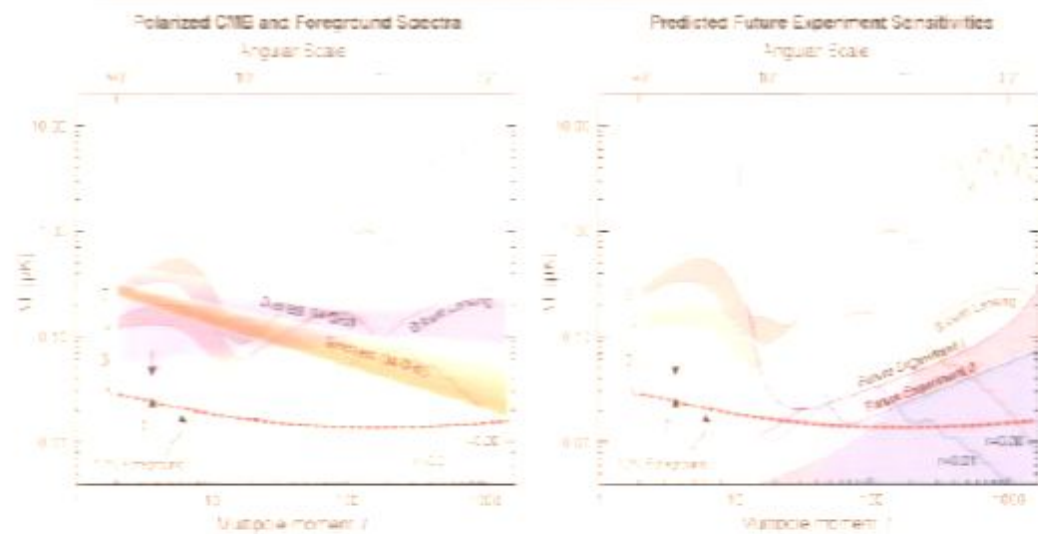


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$\Delta f_{NL} \sim 5-10$

or ~ 0.1

Ground-based Polarization expts:

$\Delta r \sim 0.01$

\Rightarrow Will distinguish wildly different mechanisms for inflation

- small field cf KKLMAT, talks here
- large field monodromy (v-station)
- $c_s \ll 1$ (DBI)
- multiple fld

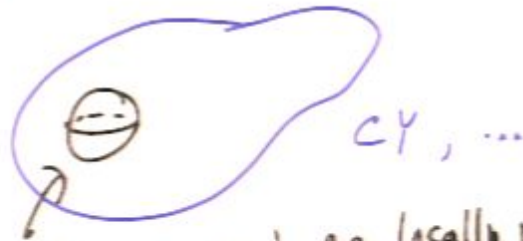
The combination of UV sensitivity & observational accessibility strongly motivates research in this direction.

Monodromy in closed string moduli spaces

L. McAllister, E.S., AW

- Monodromies were central in formal work on SUSY gauge theories and string compactification (e.g. Calabi-Yau's)

Consider e.g.



CY, ...

2-cycle Σ (size $L_2 \sqrt{\alpha'}$) e.g. locally preserve $N=4$ SUSY

Axions from $B_2^{(NS)}$ & $C_2^{(RR)}$ on Σ_2 :

wrapped D5: potential

$$V \sim \frac{1}{g_s} \sqrt{L_2^4 + b^2} \left(\frac{1}{\alpha'^2} \right)$$

$\Rightarrow V \propto b$ large b
monodromy

Wrapped NS5 :

potential

$V \propto C$ large C
monodromy

Again we must require dynamical consistency with moduli stabilization

(here { Kallosh-Linde
or
GKP + KKLT
or
Saltman, ES } + 03/07 version of Grimm/Louis)

In the 2 cases: warp down Σ_2 + brane

wrapped D5: potential

$$V \sim \frac{1}{g_s} \sqrt{L_2^4 + b^2} \left(\frac{1}{\alpha'^2}\right)$$

$\Rightarrow V \propto b$ large b
monodromy

⊖ Generic η problem if fix moduli with KKLT non-perturbative effects:

$$e^{-T} \quad T = \frac{L_2^4}{g_s} + b^2$$

Wrapped NS5:

potential

$$V \propto C \text{ large } C$$

monodromy

✓ Moduli-stabilizing effects, + D-instantons, give suppressed C_2 dependence cf Grimm

Bock et al ("Weiss report")

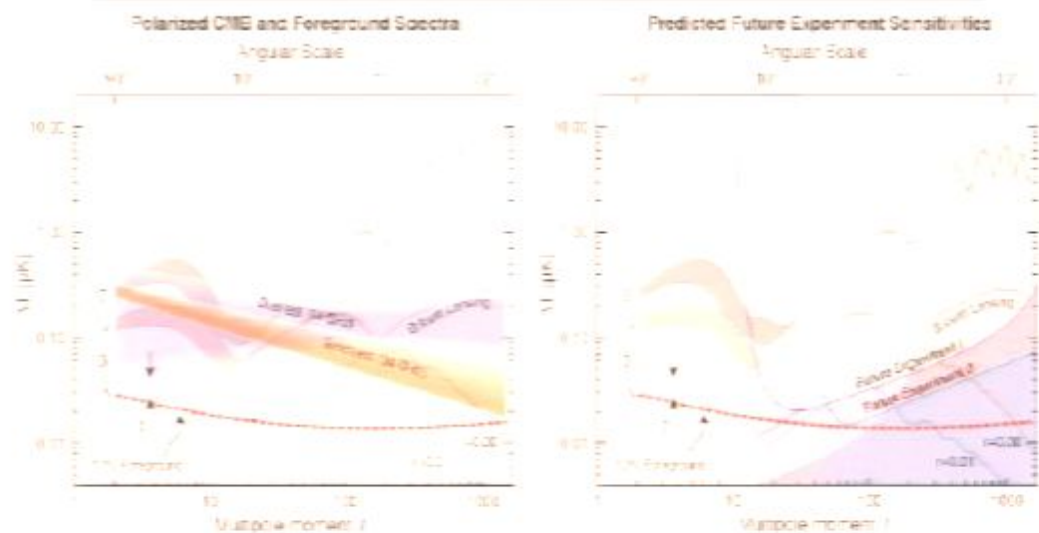


Figure 2.2: CMB Polarization Power Spectra, Backgrounds and Estimated Sensitivity of Future Experiments. Thin, wiggly curves in the two panels show the predictions for the angular power spectrum of the CMB polarization signal (E modes and B modes) in the standard cosmological model (as of 2005). The E signal is reasonably well predicted, but the B signal depends linearly on the gravitational wave amplitude, as measured by the tensor-to-scalar ratio, r . The B curves shown are for $r=0.3$ (red) and $r=0.01$ (blue). For $l < 20$, the thickness of the theory curves reflects the current degree of uncertainty about the epoch of reionization. The predicted B-mode signal due to the distortion of E modes by weak gravitational lensing is shown in green (see §3).

Left: Current estimates of the polarized Galactic foreground signals and their uncertainty, due to synchrotron emission from cosmic ray electrons and thermal emission from interstellar dust grains, as described in §4. The red dashed curve is an estimate for the residual foreground contamination after modeling using multi-frequency observations described in §4.

Right: Estimated instrumental sensitivities for a space mission of the type called for in our roadmap (grey shading) and two sample ground-based experiments (solid lines), based on the assumptions listed in §10.

- CLOVER, QUIET, BICEP/SPUD SPIDER (ground)
- POLARBEAR, EBEX, BRAINE, ... $\Delta r \sim 0.01!$
- CMBPOL? (satellite)

The tensor signal is detectable
via CMB experiments sensitive to
polarization :



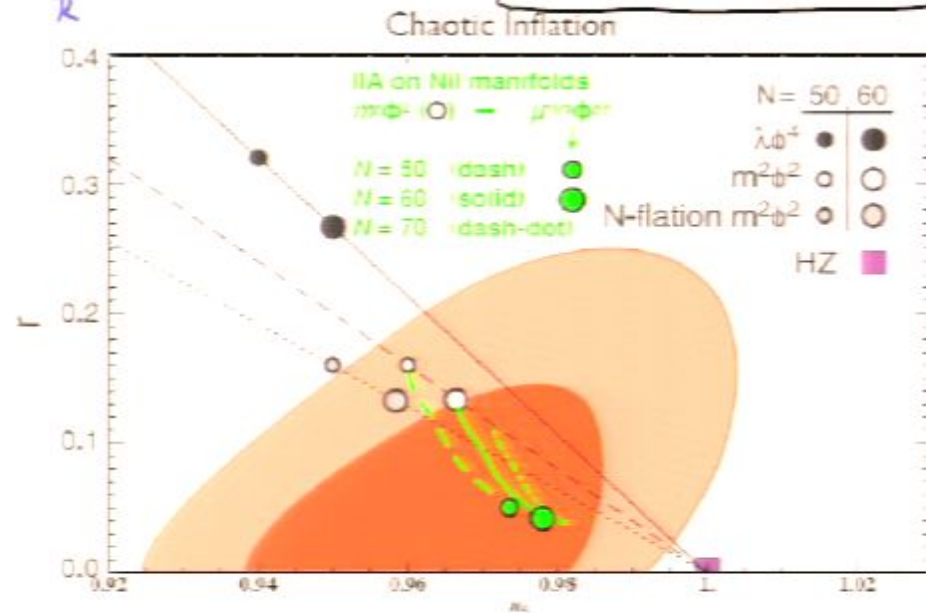
gravity wave \Rightarrow locally
anisotropic propagation of
CMB photons. Scattering
of CMB off e^- 's present during
re-ionization & recombination
 \rightarrow polarization

The observational situation is very
healthy. ("instant" gratification...)

→ This appears to provide a viable model realizing monodromy mechanism

⇒ Observational predictions

$$V(\phi) = \mu \frac{10}{3} \phi^{\frac{2}{3}} \Rightarrow r \approx 0.04, n_s \approx 0.98$$



- For single-field version, $f_{NL}^{\text{squeezed}} \sim 0.01$, $f_{NL}^{\text{equilateral}} \approx 0 \Rightarrow$ distinct from $G_2 \ll 1$ case
multifield extension required for f_{NL}^{squeezed}

Again we must require dynamical consistency with moduli stabilization

(here { Kallosh-Linde
or
GKP + KKLT
or
Saltman, ES } + 03/07 version of Grimm/Louis)

In the 2 cases: warp down Σ_2 + brane

wrapped D5: potential

$$V \sim \frac{1}{g_s} \sqrt{L_2^4 + b^2} \left(\frac{1}{\alpha'^3}\right)$$

$\Rightarrow V \propto b$ large b
monodromy

... n problem

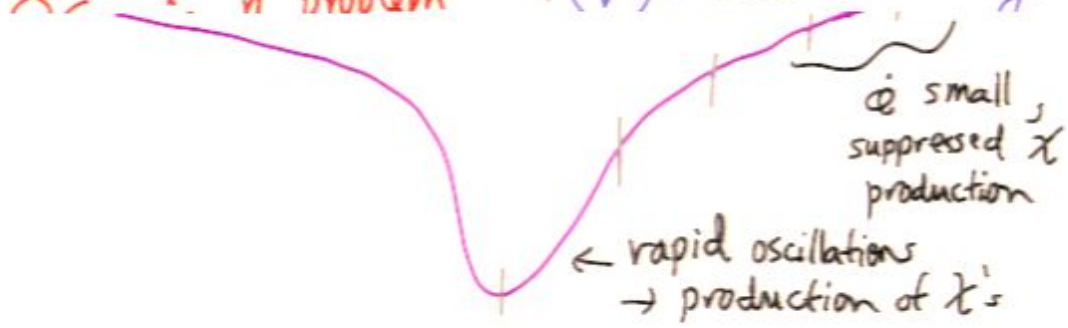
Wrapped NS5:

potential

$$V \propto C \text{ large } C$$

monodromy

(✓) Moduli-stabilizing



Reheating

In ordinary chaotic inflation, the inflaton must couple to other degrees of freedom in order to reheat

Small couplings $g \leq 10^{-3}$ prevent destabilization of $V(\phi)$

$g^2 \chi^2 \phi^2 \rightarrow$ production of χ 's KLS, ...

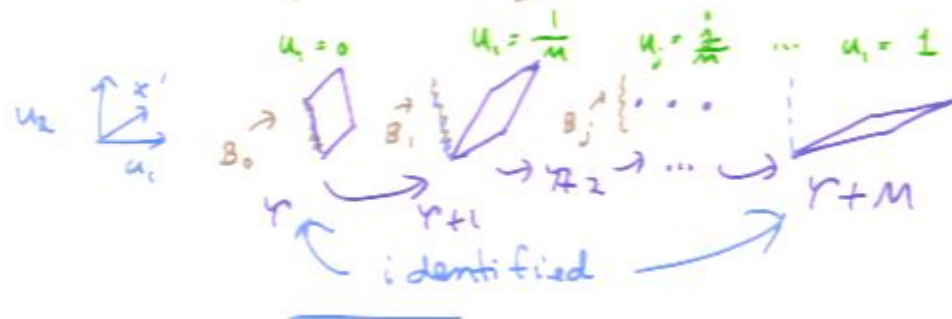
\hookrightarrow periodic in our case: $g^2 \chi^2 f(\phi)$



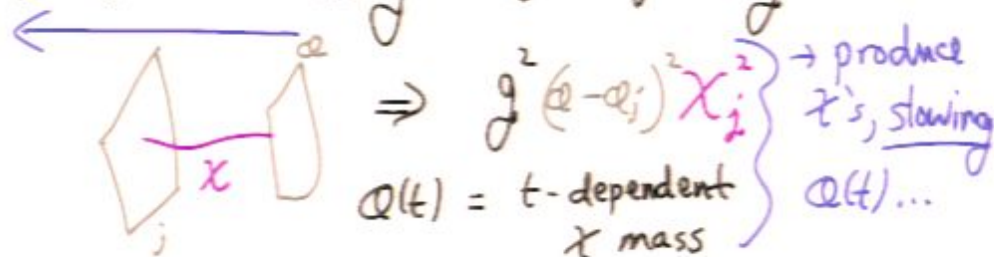
Trapped Inflation

c.f. Kofman Linde Starobinski; Tong ES
 Kofman Linde Liu McAllister
 Maloney E.S.

B. Horn, D. Green, T. Rube, L. Senatore, ES
 (in progress)



There are stable positions for other
 D4-branes along the trajectory



So far ...

- Relatively simple class of compactification geometries \rightarrow $\left\{ \begin{array}{l} \text{monodromy} \Rightarrow \text{large } \Delta\mathcal{Q} \\ \text{homogeneity} \Rightarrow \text{easier to control } \Delta V \end{array} \right.$

Candidate e.g.'s $V(\mathcal{Q}) \propto \mathcal{Q}^{\frac{2}{3}} \rightarrow r = 0.04$
 $n_s = 0.98$

in progress $\left\{ \begin{array}{l} V(\mathcal{Q}) \propto \mathcal{Q} \quad \text{B, C monodromies} \\ V(\mathcal{Q}) \propto \mathcal{Q}^{\frac{2k}{k+2}} \quad \text{higher-dimensional} \\ \quad \text{(Aharony)} \quad \text{SO}(d,d,2) \text{ monodromies} \end{array} \right.$

\rightarrow distinctive signatures; falsifiable on the basis of the tensor signal

- Reasonably explicit small-field models also arise in string theory
cf other talks here

\Rightarrow No general prediction about detectable r from string theory at the level of model building.

Initial conditions?

- small-field inflation requires landing on a tiny $\Delta\mathcal{Q}$, with somewhat smooth initial patch of size H^{-1}

Genericity?

- Both types of models use common ingredients
- More symmetry required for chaotic inflation?
 - But monodromy reduces this to a small-field problem
 - Tuneability of ϵ, η not automatic in small-field models (cf IACV no-go)