

Title: Small scale gadgets for large scale processing

Date: Jun 15, 2007 05:15 PM

URL: <http://pirsa.org/07060058>

Abstract:

# Small quantum gadgets for large-scale processing

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Jake Taylor (MIT)



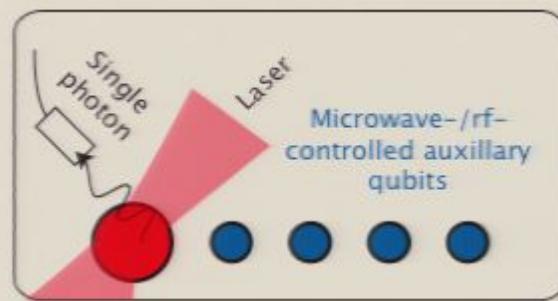
Massachusetts  
Institute of  
Technology



# Focus of this talk

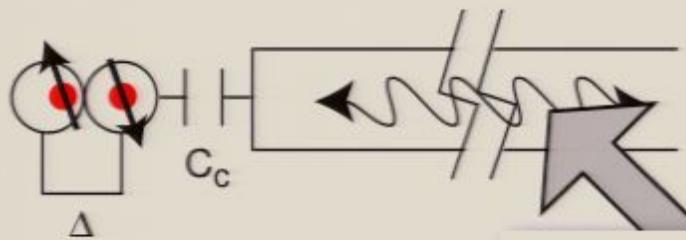
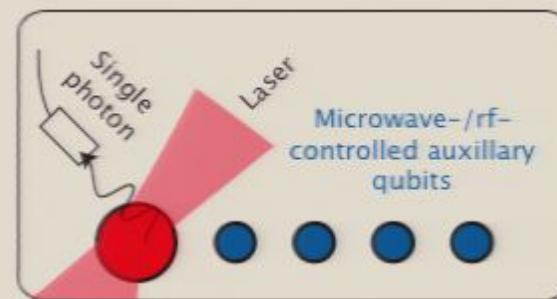
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Quantum registers for distributed computation

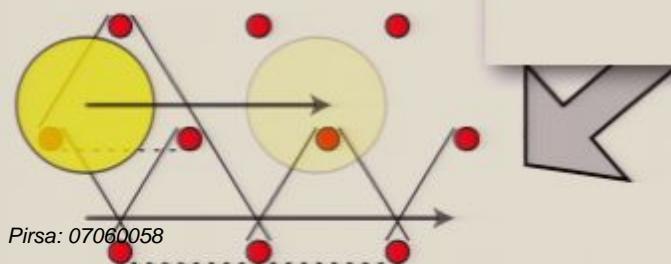


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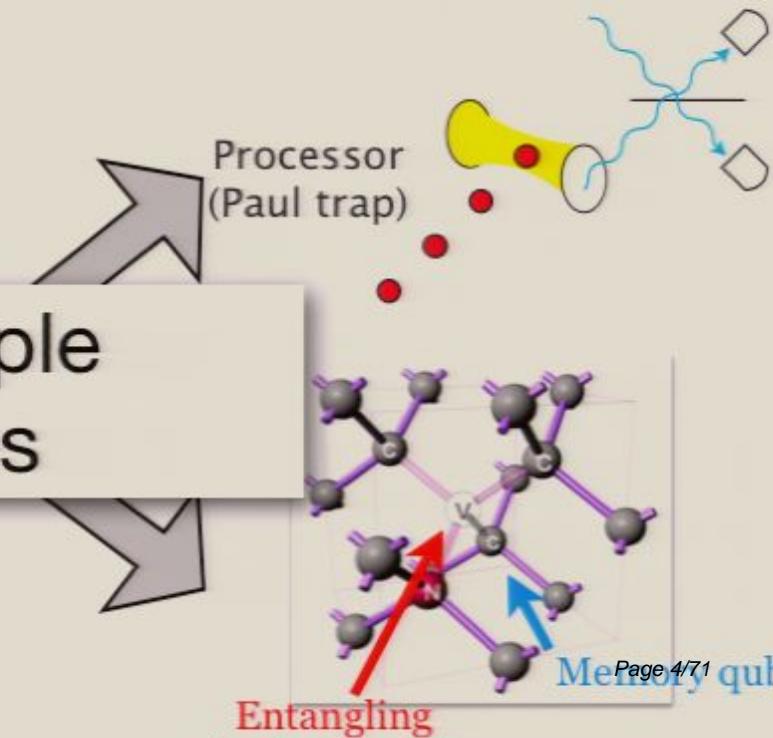
Quantum registers for distributed computation



Some example approaches



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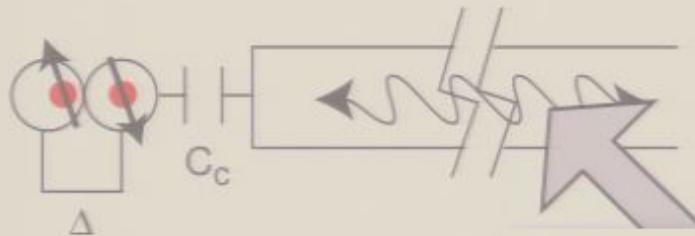
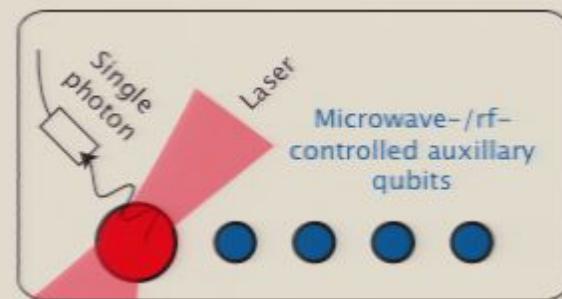


Entangling

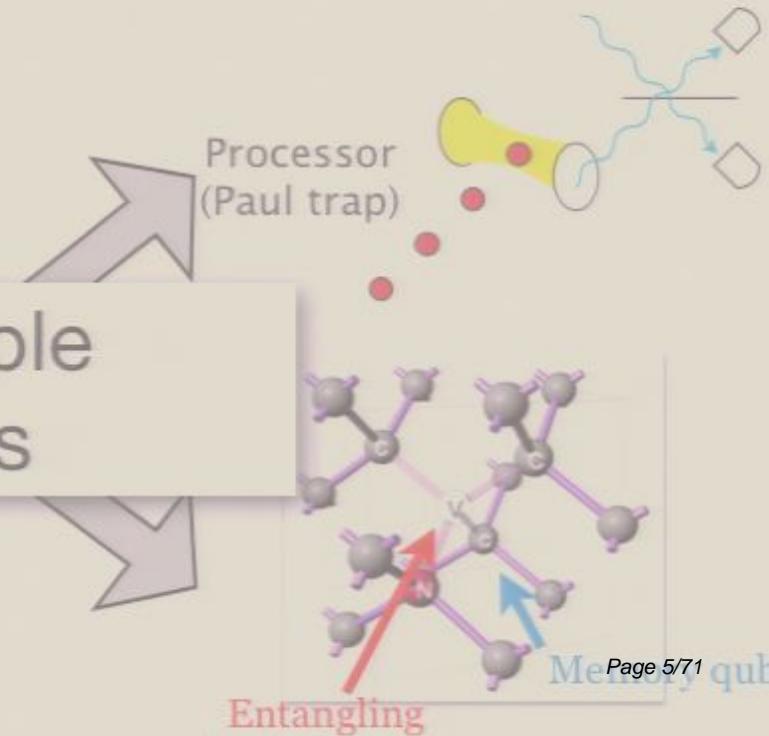
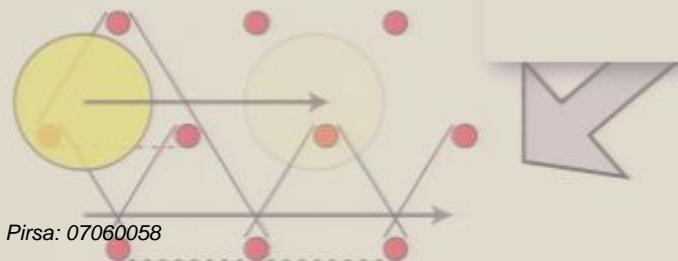
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# Focus of this talk

Quantum registers for distributed computation



Some example approaches



# Distributed quantum computation

- Problem: apparatus for many qubits?
  - limited coupling strengths in a NMR molecule (frequency selectivity)
  - quantum control in a dilution refrigerator



[image from Janis.com]

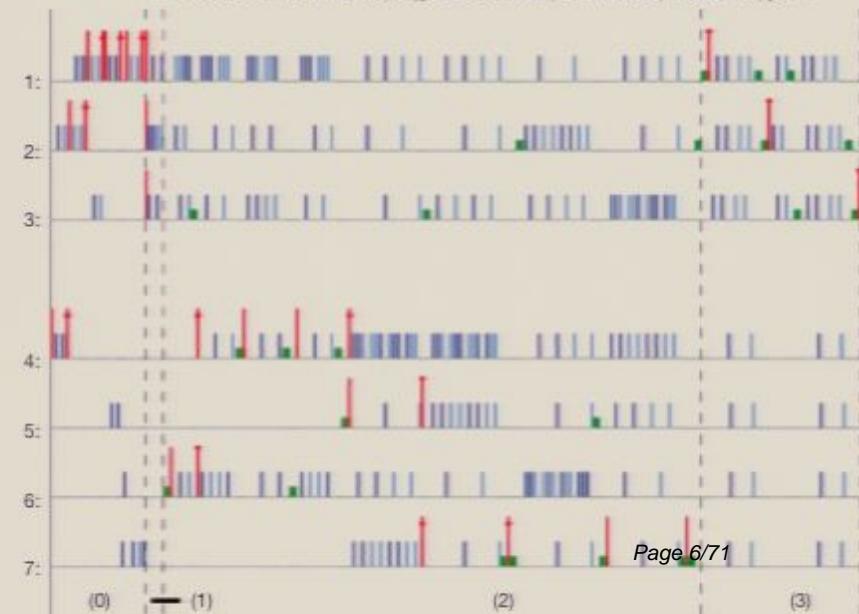
## Experimental realization of Shor's quantum factoring algorithm using nuclear magnetic resonance

Lieven M. K. Vandersypen<sup>\*†</sup>, Matthias Steffen<sup>\*†</sup>, Gregory Breyta<sup>\*</sup>, Costantino S. Yannoni<sup>\*</sup>, Mark H. Sherwood<sup>\*</sup> & Isaac L. Chuang<sup>†‡</sup>

<sup>\*</sup> IBM Almaden Research Center, San Jose, California 95120, USA

<sup>†</sup>Solid State and Photonics Laboratory, Stanford University, Stanford, California 94305-4075, USA

The number of steps any classical computer requires in order to find the prime factors of an  $l$ -digit integer  $N$  increases exponentially with  $l$ , at least using algorithms known at present<sup>1</sup>. Factoring large integers is therefore conjectured to be intractable classically, an observation underlying the security of widely used crypto-



# Distributed quantum computation

- Problem: apparatus for many qubits?
  - limited coupling strengths in a NMR molecule (frequency selection)
  - quantum control



Approach: build a  
**Quantum Register**

Use quantum communication  
between registers

- noisy, failure prone, still OK

Have good local operation of  
a given register

**Use many local operations  
to improve (faulty) inter-  
register operations**

Experimental realization of Shor's  
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using nuclear magnetic resonance

Andersen†, Matthias Steffen†, Gregory Breyta‡,  
John A. C. McDonnell‡, Mark H. Sherwood‡ & Isaac L. Chuang†

†Research Center, San Jose, California 95120, USA  
‡Physics Laboratory, Stanford University, Stanford,  
CA 94301, USA

number of steps any classical computer requires in order to factor a number into its prime factors of an  $l$ -digit integer  $N$  increases exponentially with  $l$ . Factoring is therefore conjectured to be intractable classically, thus underlining the security of widely used cryptographic protocols.

# Early ideas (monolithic architecture)

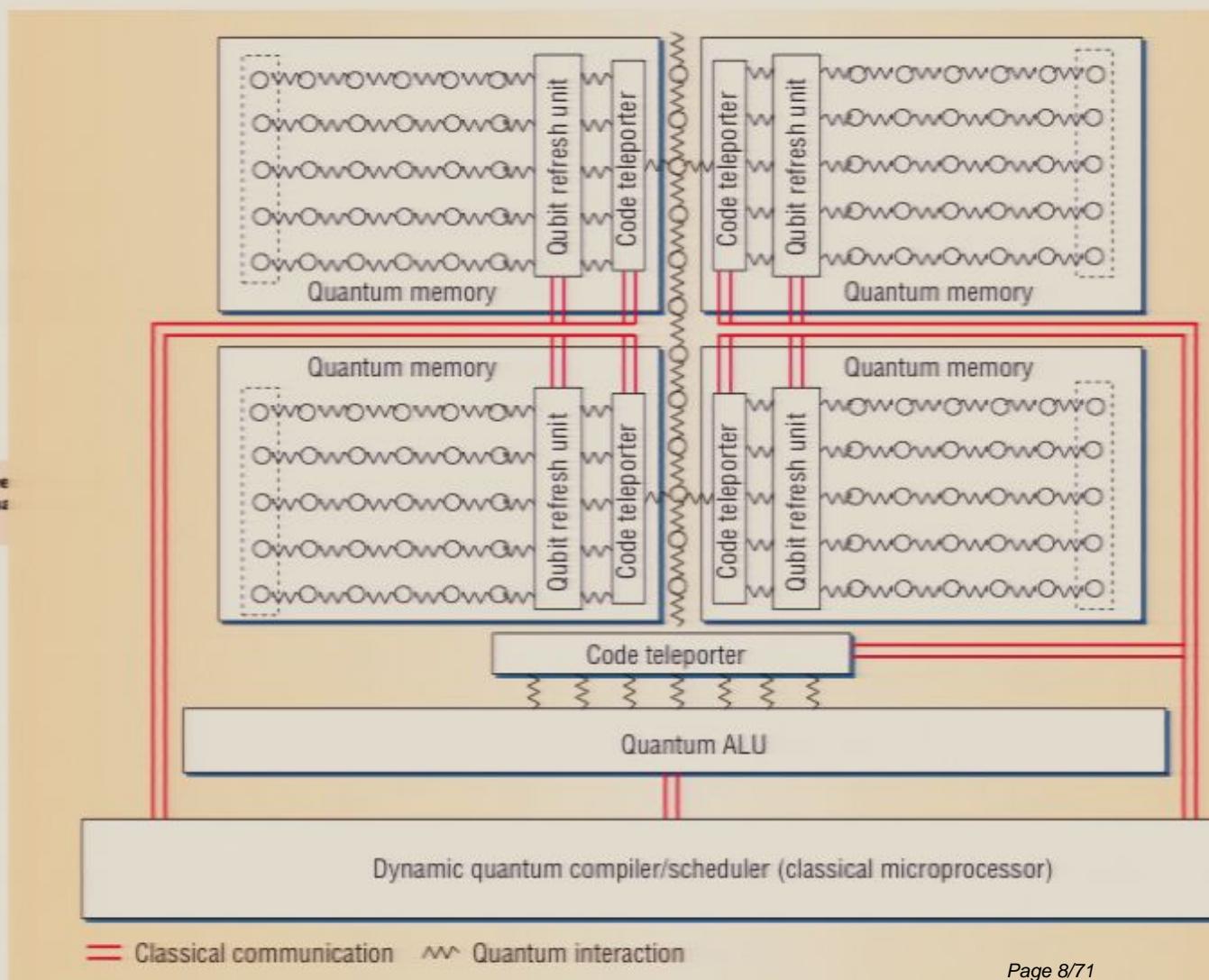
## A Practical Architecture for Reliable Quantum Computers

Quantum computation has advanced to the point where solutions can help close the gap between emerging quantum and real-world computing requirements.

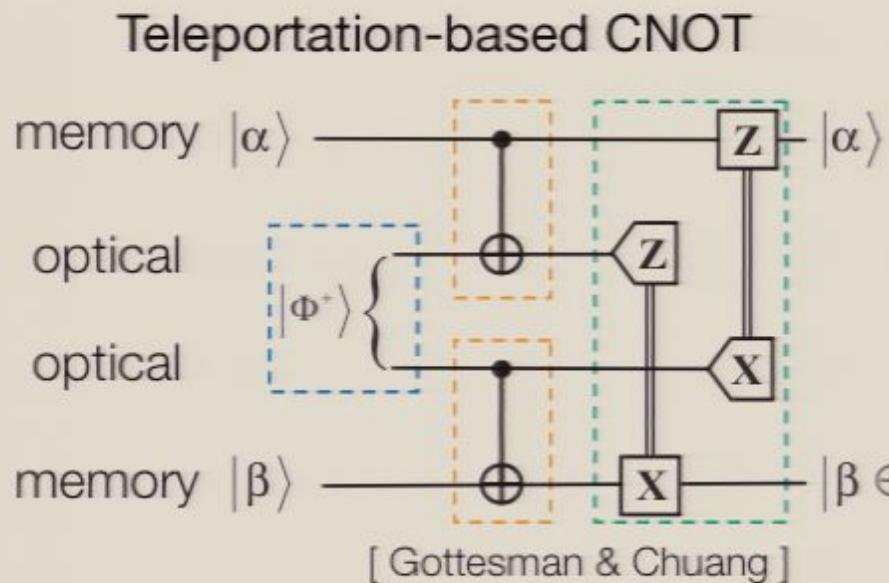
Mark Oskin  
University of Washington

Frederic T. Chong  
University of California, Davis

Isaac L. Chuang  
Massachusetts Institute of Technology

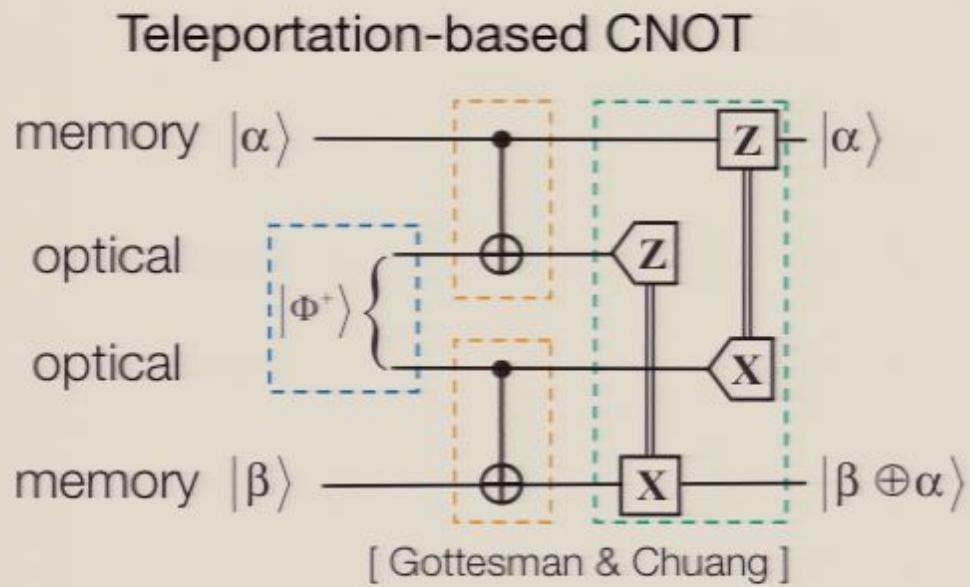


# Teleportation, gates, and bandwidth



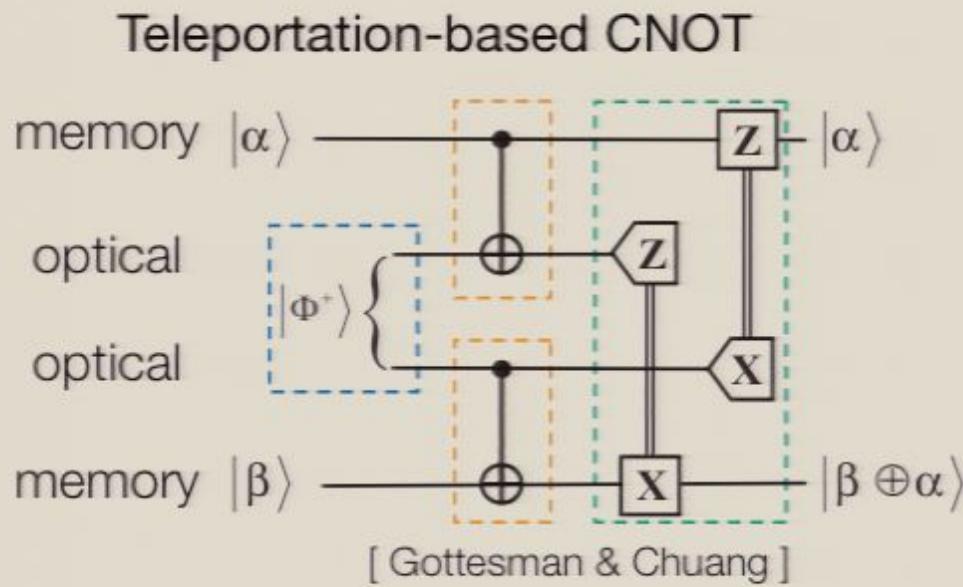
Entanglement +  
Local operations +  
Classical communication =

# Teleportation, gates, and bandwidth



Entanglement +  
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*Deterministic gates*  
from probabilistic  
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(quantum) bandwidth *in advance*

# Using photons to build entanglement

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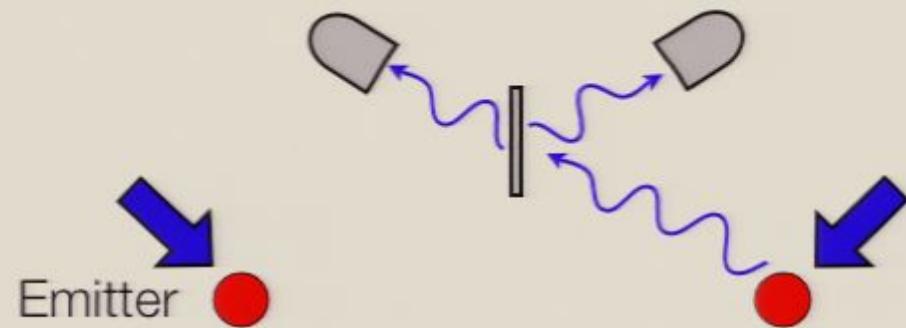
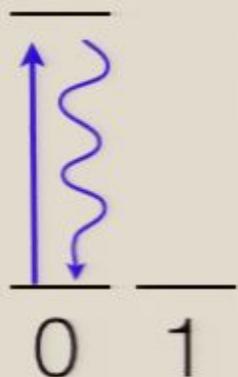
State-selective  
transition  
(atom, ion, etc.)



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0 1

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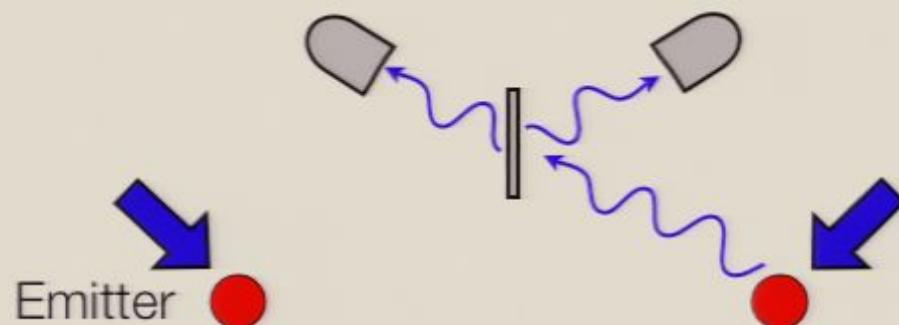
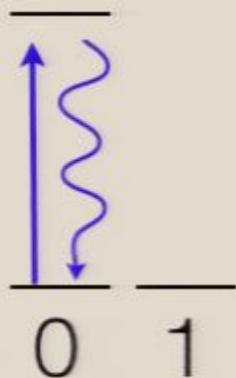
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$$(\sqrt{p}|0\rangle + |1\rangle) \otimes (\sqrt{p}|0\rangle + |1\rangle) \rightarrow \sqrt{p}(|0\rangle|1\rangle + |1\rangle|0\rangle) + \mathcal{O}(p)$$

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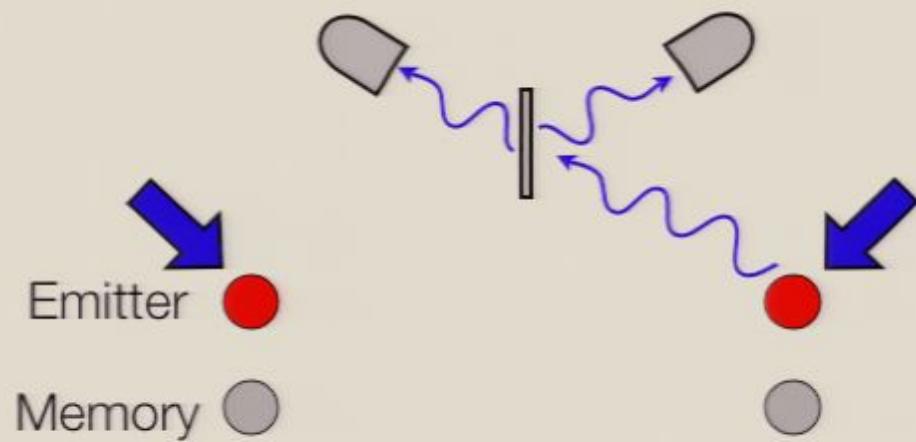
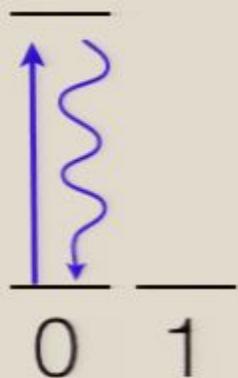


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- Single “click” with no which-path information
- Need good memory

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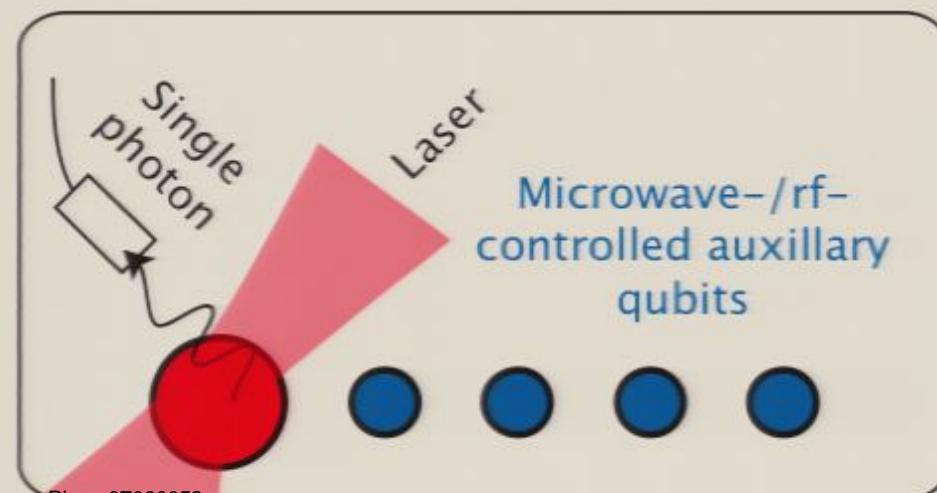
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# A minimal register

Minimum requirements:

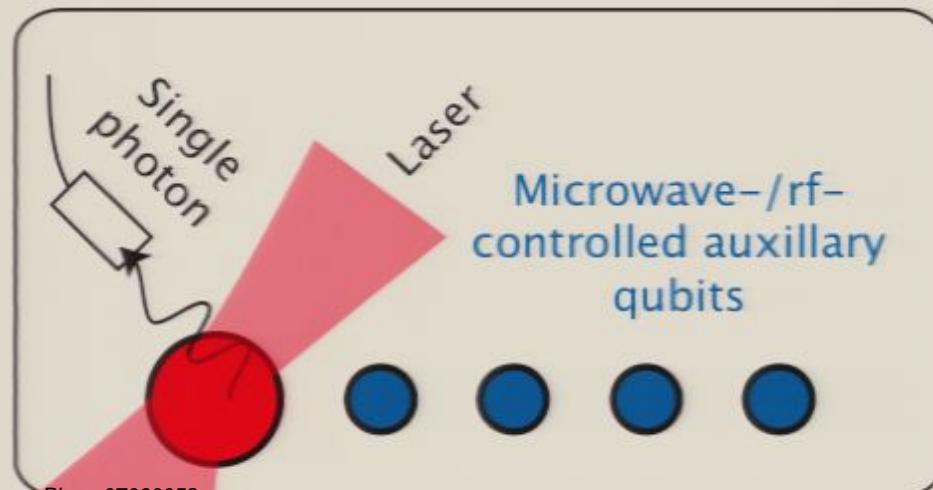
- “optical” qubit
  - entanglement generation
  - measurement / initialization
- “memory” qubit
- very good local control
- reasonable optical interface



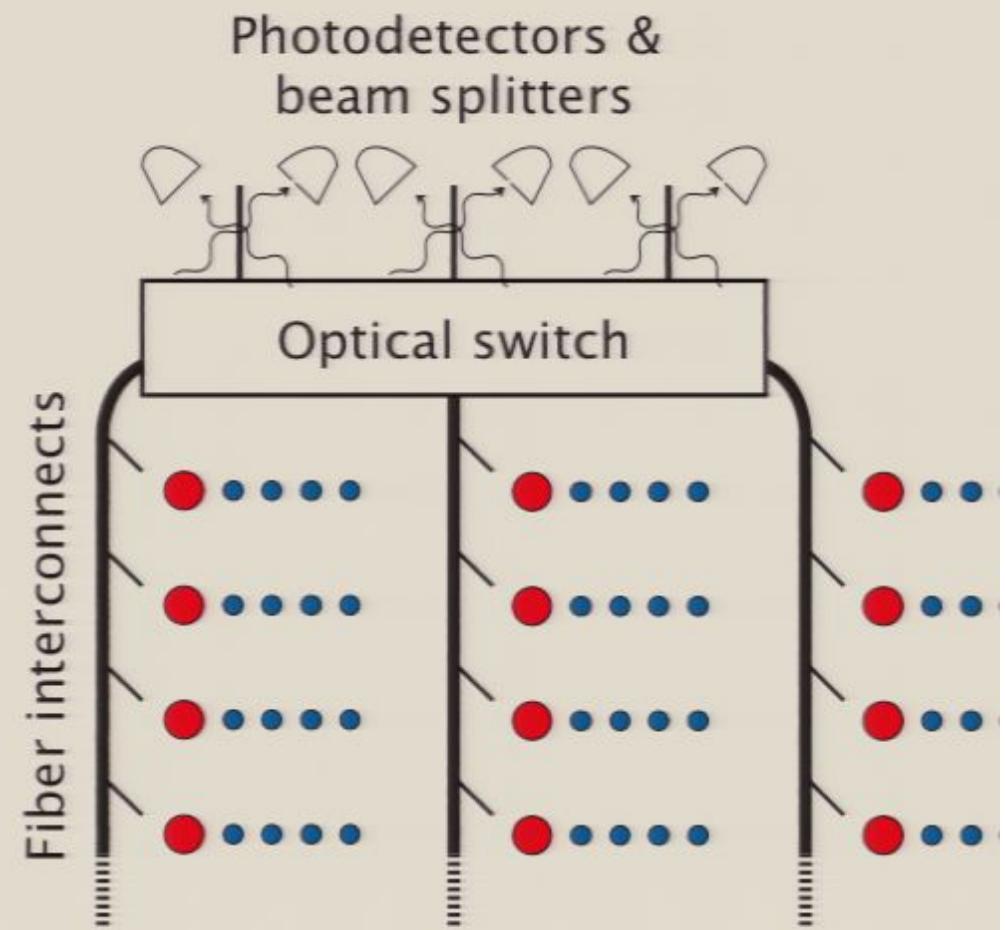
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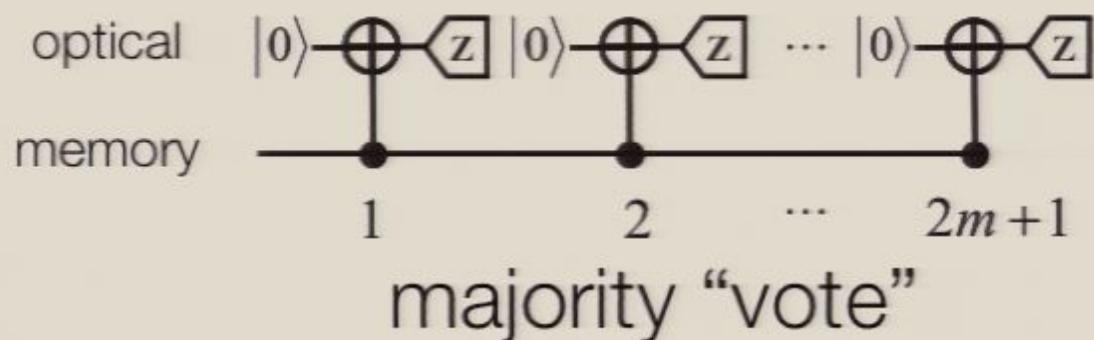
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# Dealing with imperfections

Robust measurement:

bit verification

- Trade measurement errors for local errors and time
- Phase errors in C irrelevant
- Also initializes memory bit



Robust entanglement generation

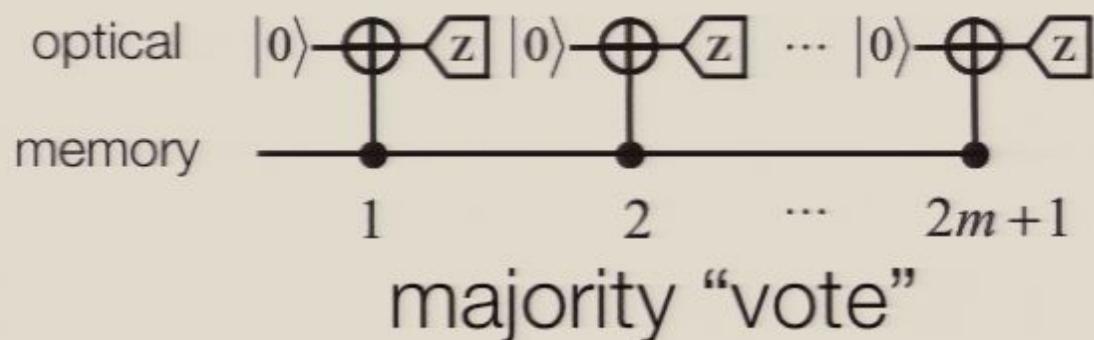
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- bit and phase corrections
- Dramatic improvement of final fidelity of entangled pair F
- Three extra qubits required  
(robust meas., bit, phase purification)



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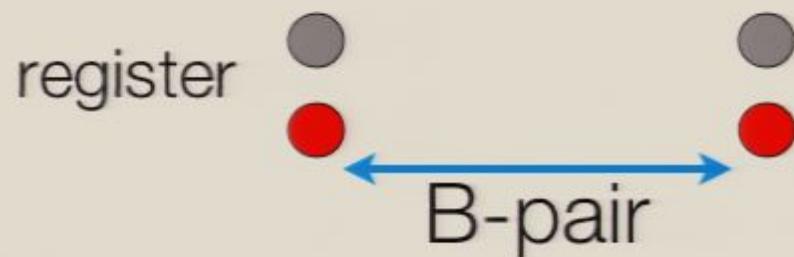
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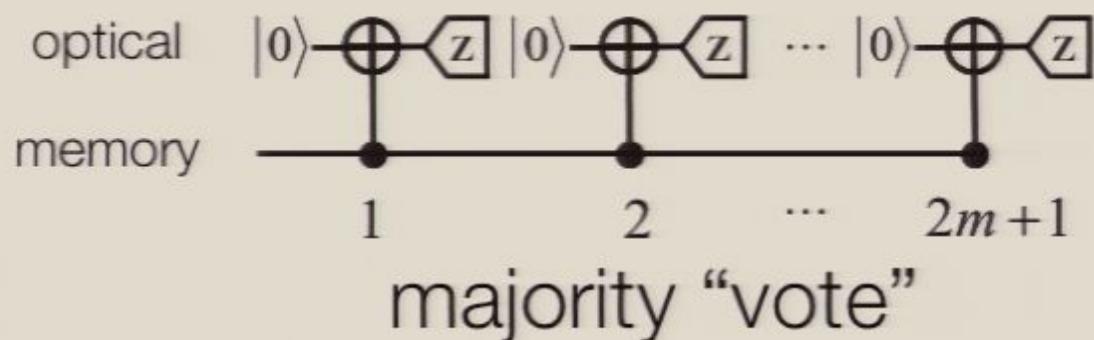


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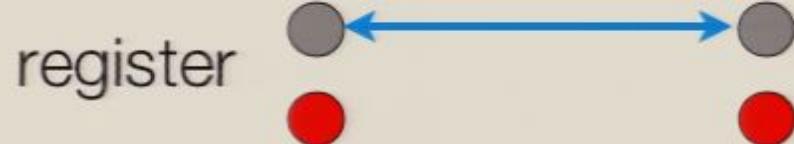
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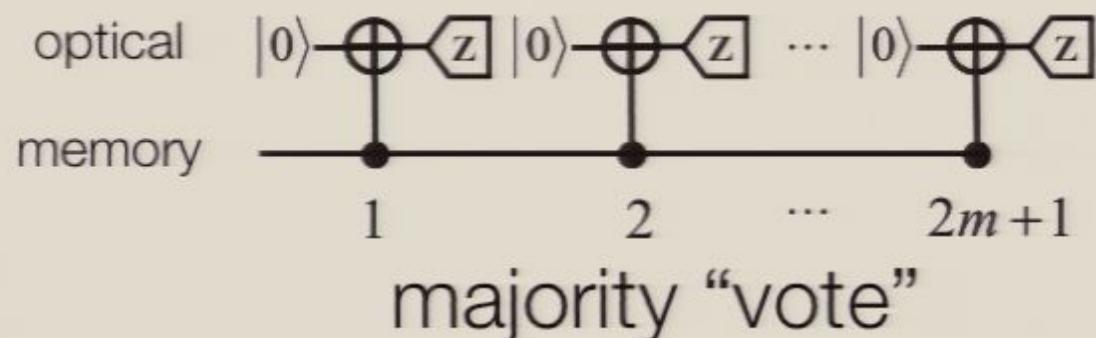


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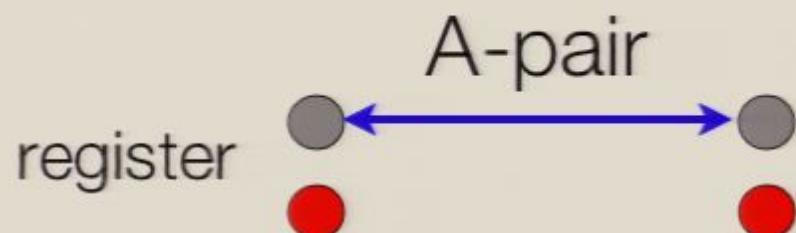
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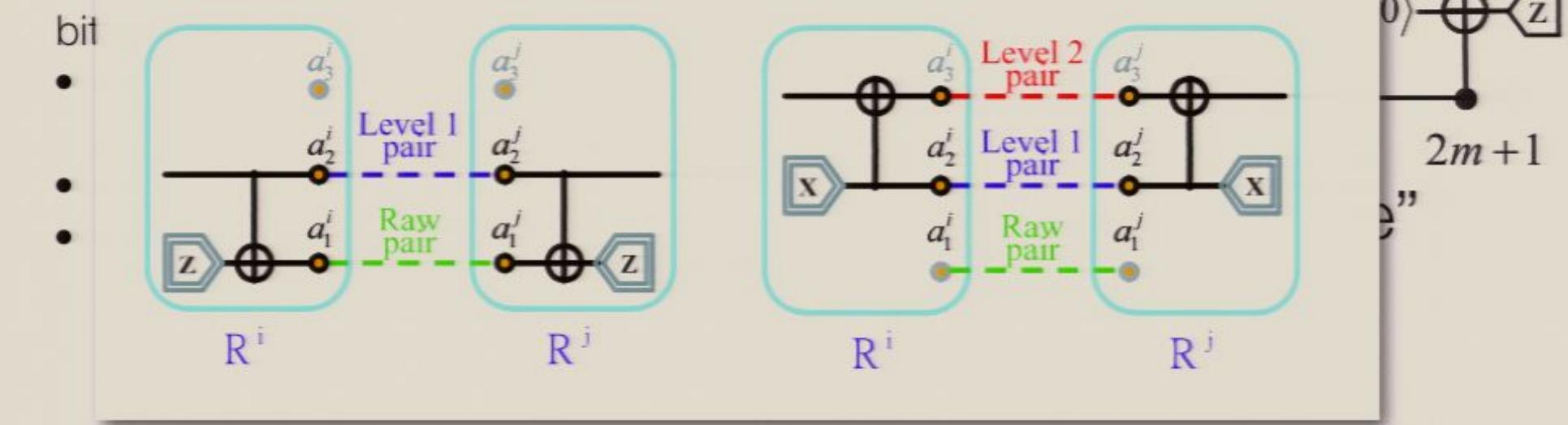
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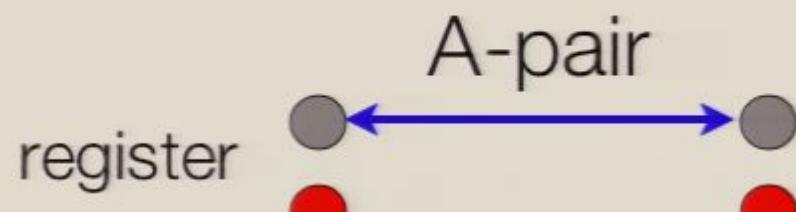
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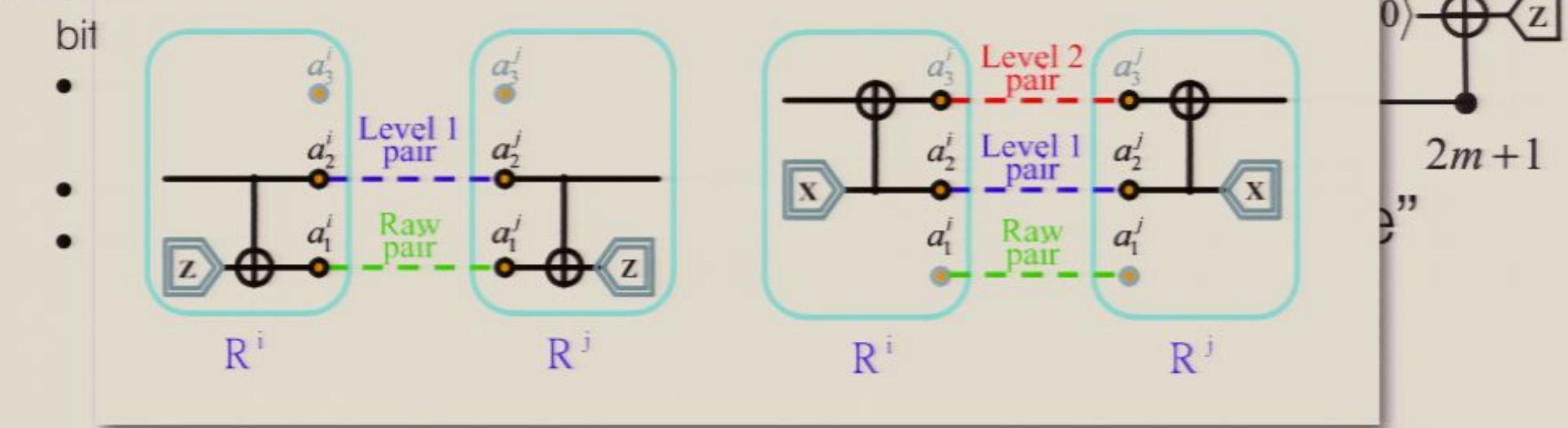
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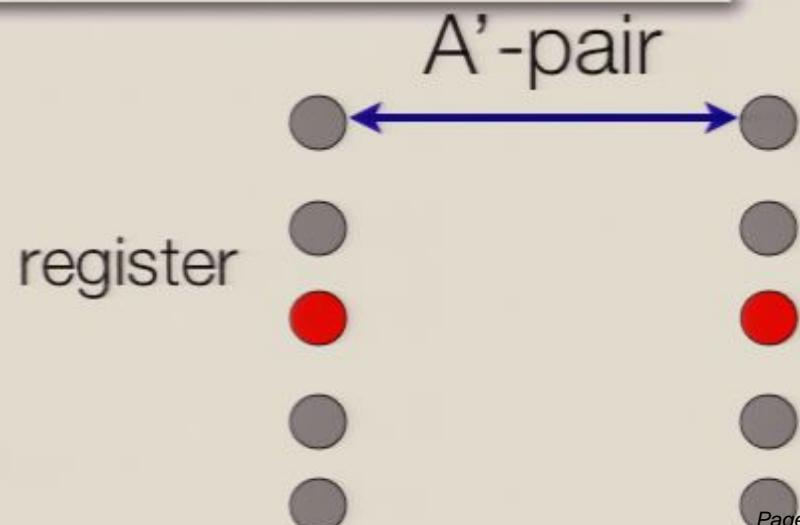
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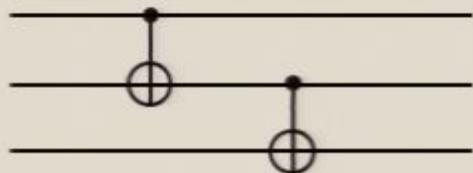
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# Deterministic distributed computation

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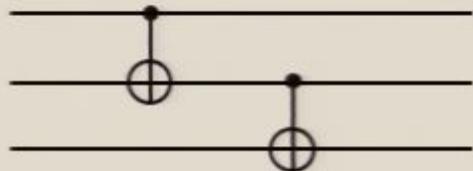
desired (logical) circuit



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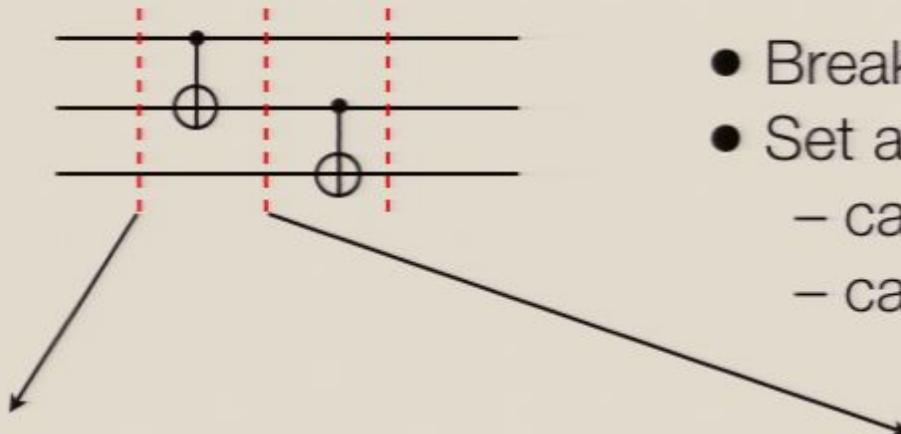


Idea:

- Break into pairwise gates
- Set a “clock cycle” time
  - can have “did not succeed” errors
  - can have logical errors

# Deterministic distributed computation

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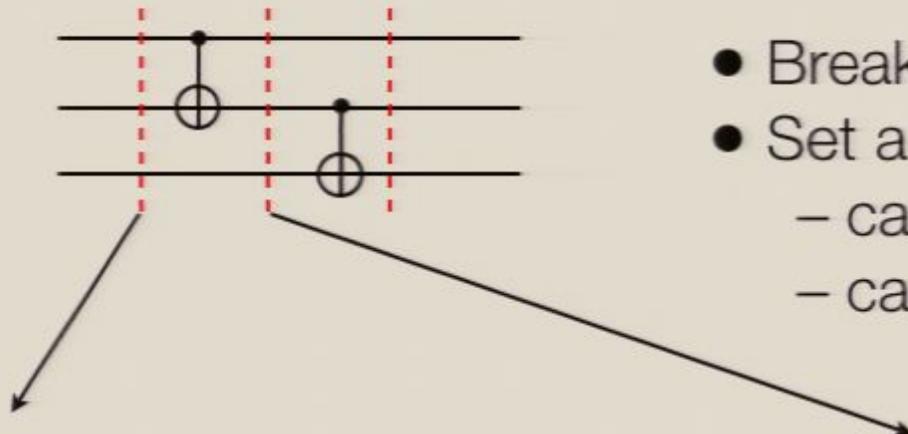
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memory  
optical

optical  
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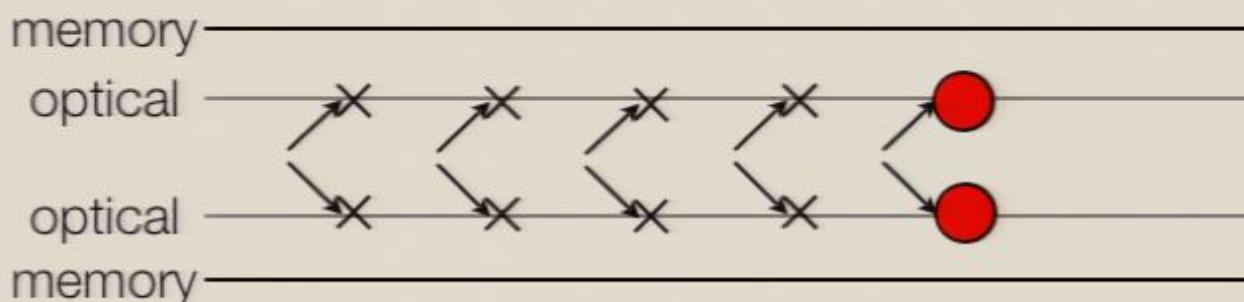
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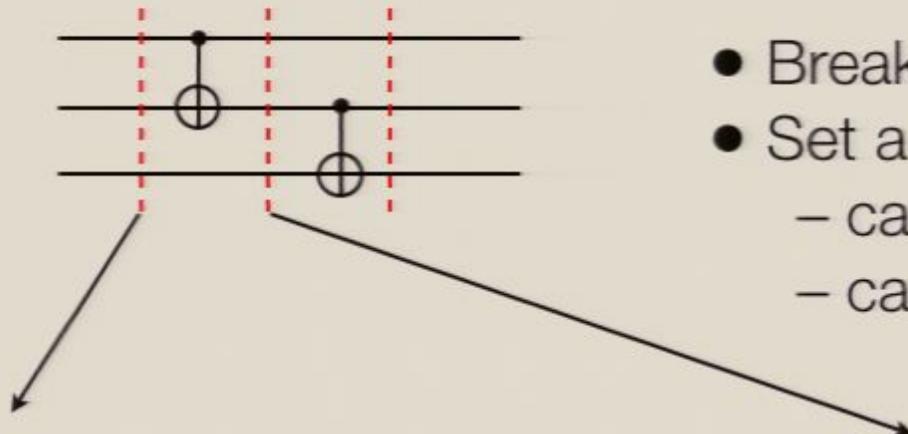
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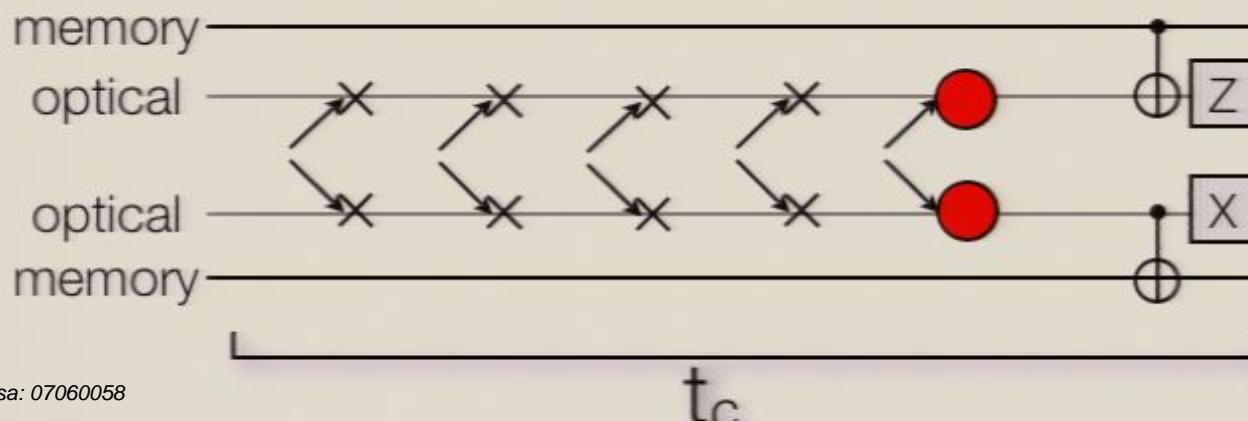
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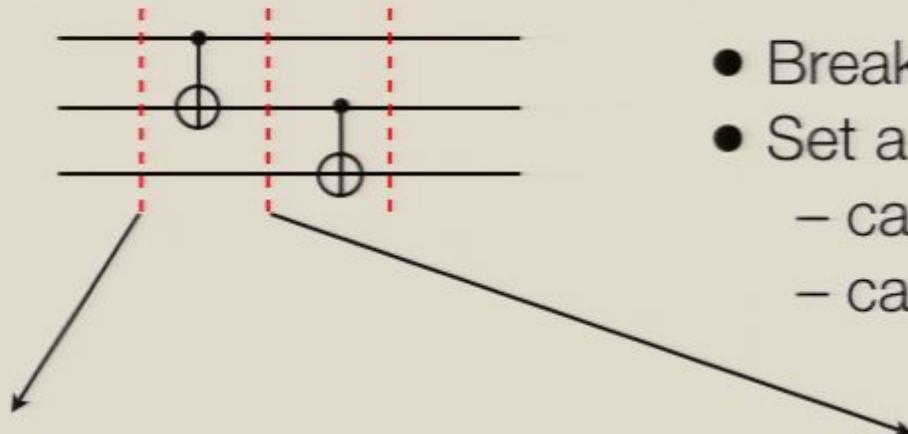
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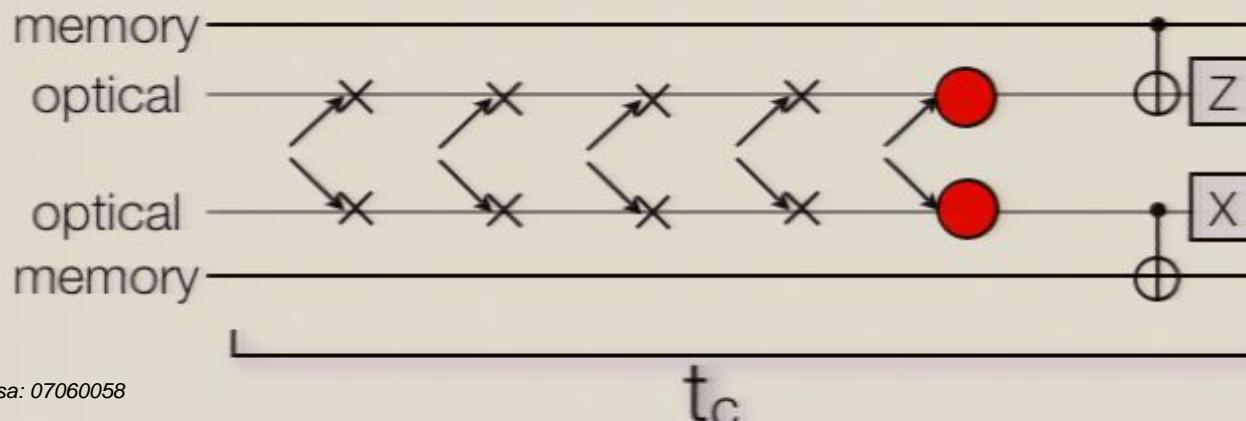
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$$\begin{aligned} \text{time/gate} &= t_c \\ \text{error/gate} &= N_{\text{eff}} p_L \end{aligned}$$

# Performance for 5-qubit registers

---

Robust measurement

- imperfect initialization, measurement ( $p_I, p_M \sim 5\%$ )
- near-perfect local operation ( $p_L \sim 0.01\%$ )

$$\tilde{\varepsilon}_M \approx \binom{2m+1}{m+1} (p_I + p_M)^{m+1} + (2m+1) p_L$$

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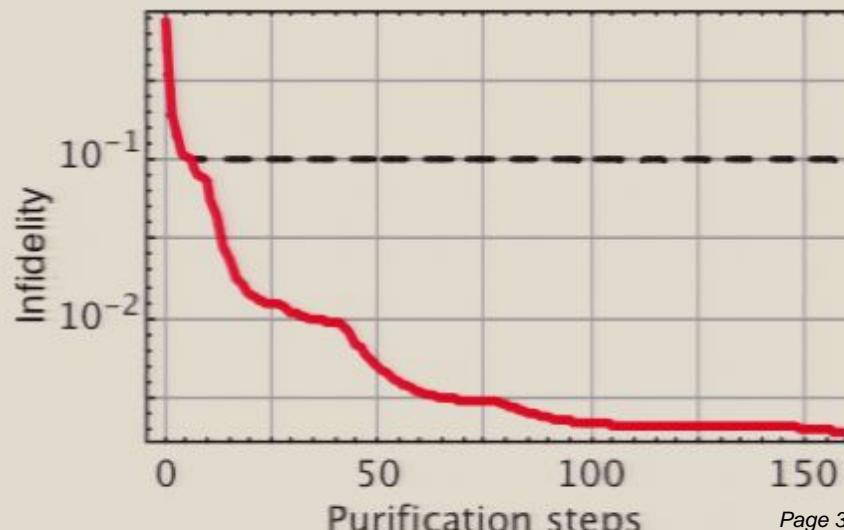
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Robust entanglement generation

- Large time overhead ( $t_C \sim 100-1000 t_L$ )
- Initial  $F=0.9$  gives final  $F>0.995$  ( $N_{\text{eff}} \sim 20$ )
- Good quantum memory *critical*



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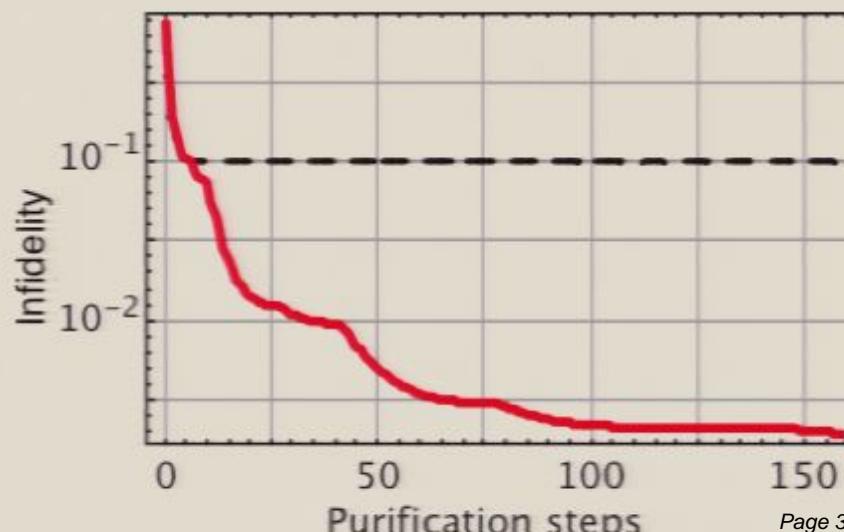
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Further improvements:  
better collection efficiency via  
optical cavities (Purcell effect)  
— improves both speed and fidelity

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# Approaches towards commodity gadgets

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- Commodity good: cheap, interchangeable, ubiquitous
- Finite size control problem *per register*.
  - GRAPE pulses [ Khaneja et al. ], feedback & filtering, composite pulses, etc.
- Optical or other “distributed qubit” interconnect system can be faulty (<50% errors after post-selection sufficient; for <10%, only 5 qubits needed)
- Implementations:
  - NEED: few coupled, controllable qubits with fantastic quantum memory; optical (or phononic, or qubit-bus) interconnection possible
  - Ion traps, NV centers, Quantum dots, neutral atoms(?)
- FUTURE: better use of post-selected computing; better purification protocols (c.f. n-bit purification approaches); direct, multi-qubit entanglement protocols

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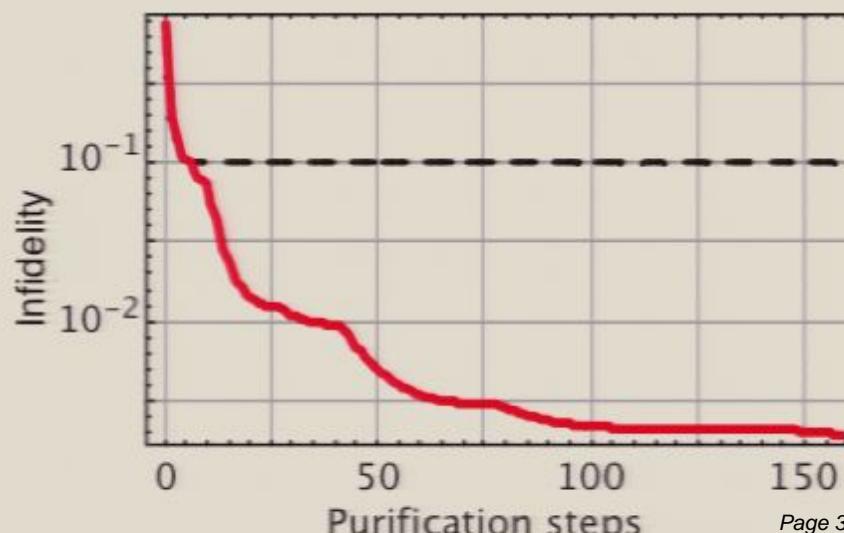
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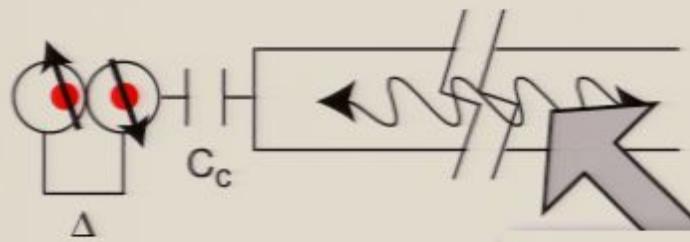
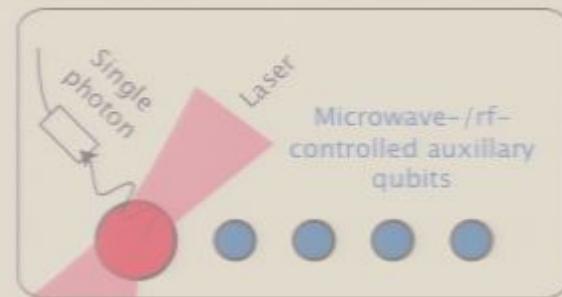
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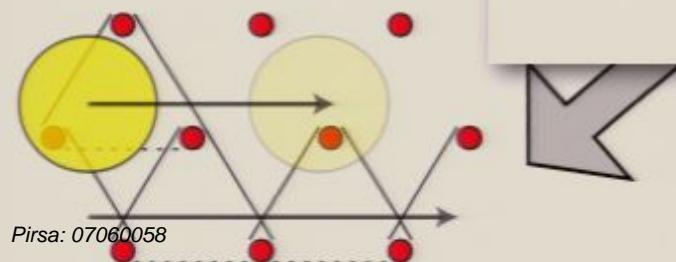
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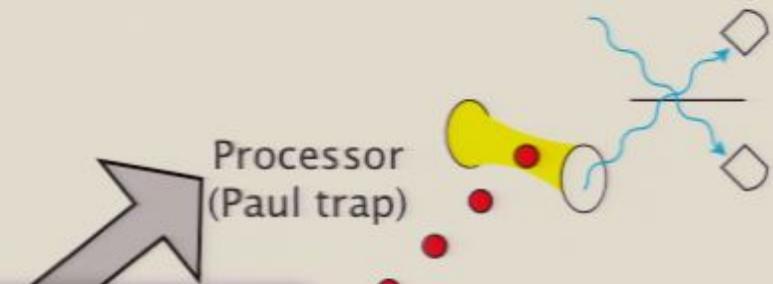
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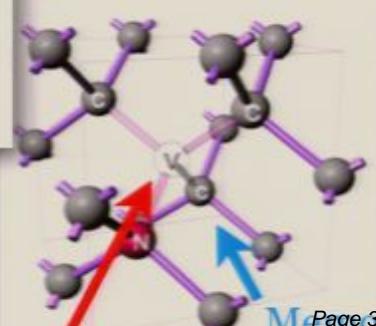


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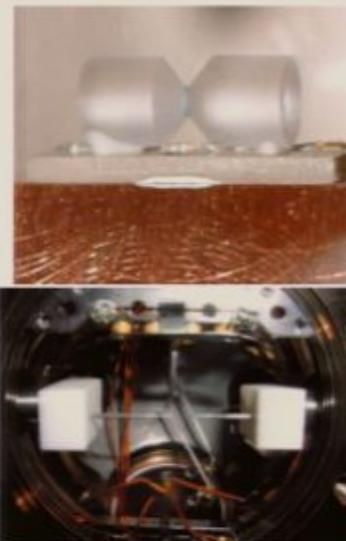
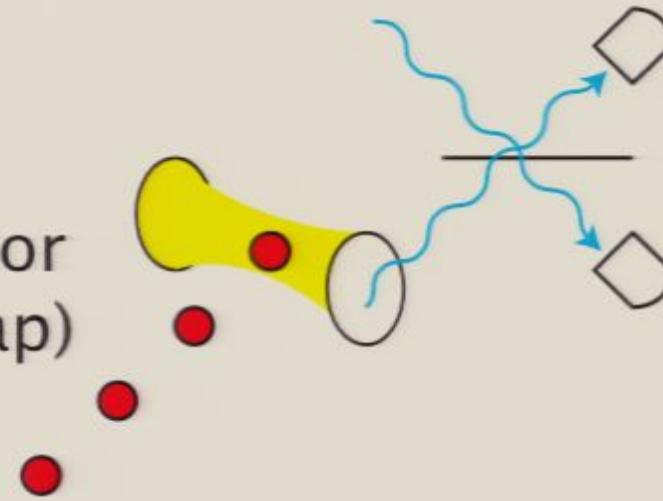
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Memory qubit

# Linear paul traps + cavity

Processor  
(Paul trap)



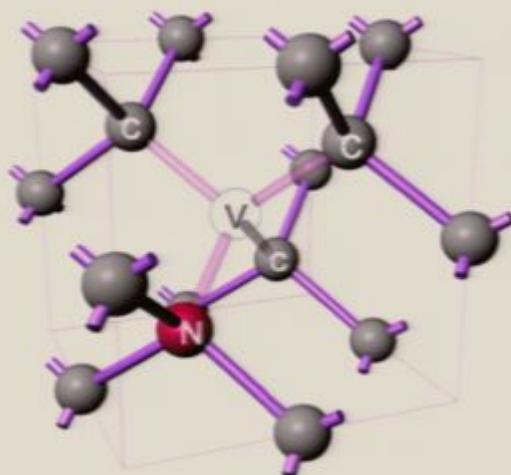
Innsbruck



Sussex

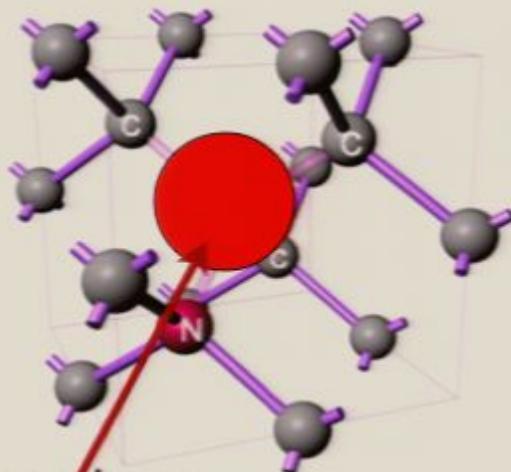
# Nitrogen-vacancy color center in diamond

Color centers as qubits  
(NV centers in diamond)



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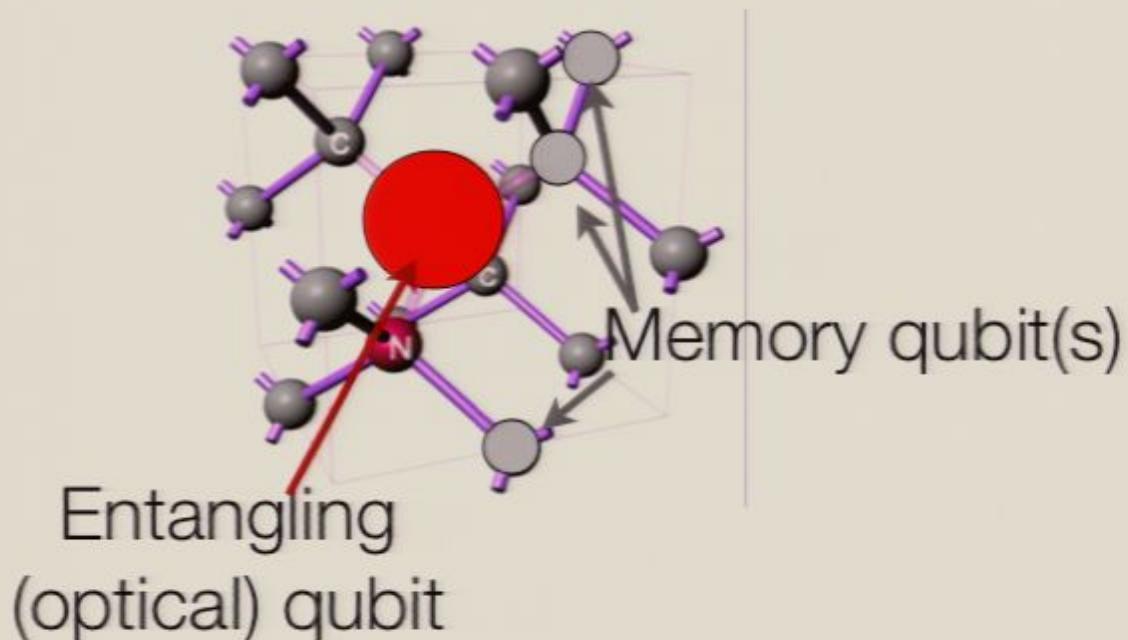
Color centers as qubits  
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Entangling  
(optical) qubit

# Nitrogen-vacancy color center in diamond

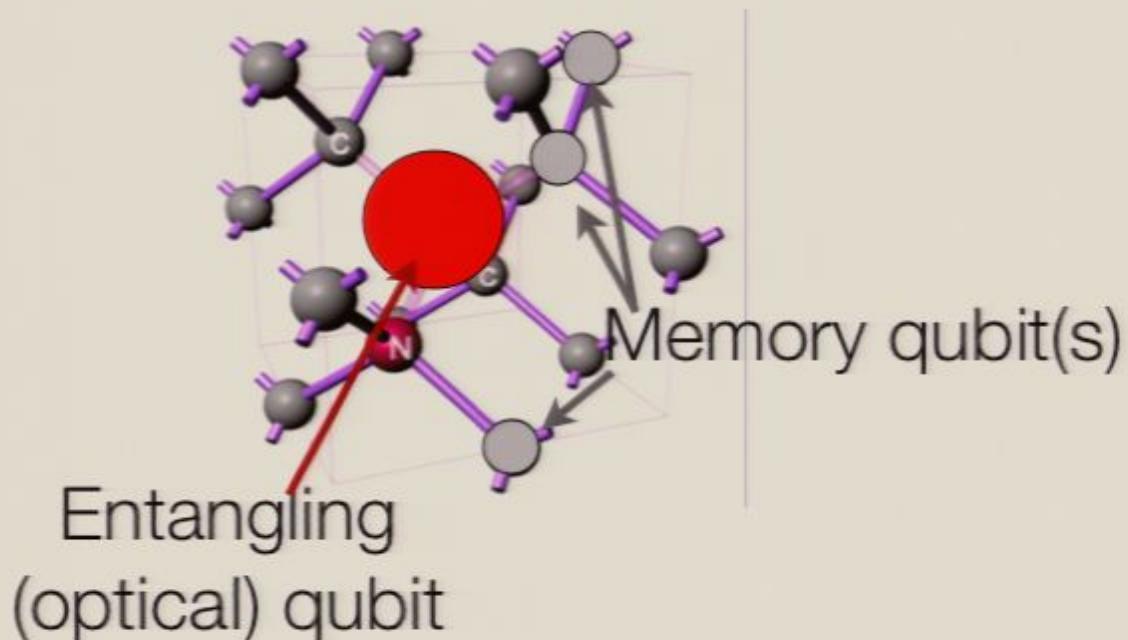
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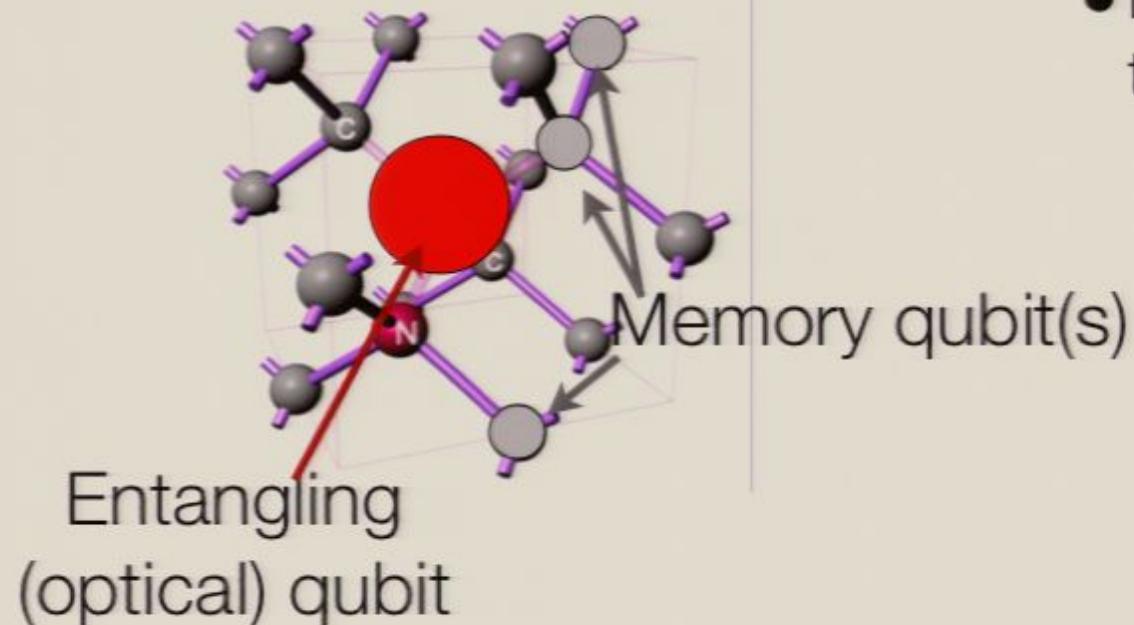
Color centers as qubits  
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- $^{13}\text{C}$  provides NMR-based memory



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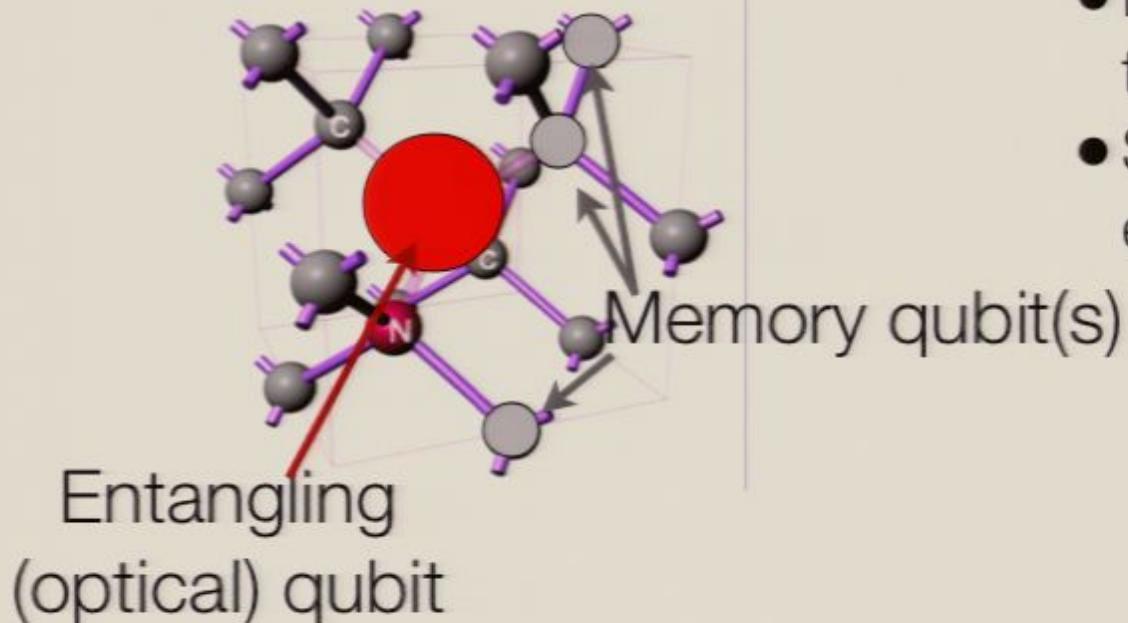
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- Dipolar/hyperfine coupling to electron spin

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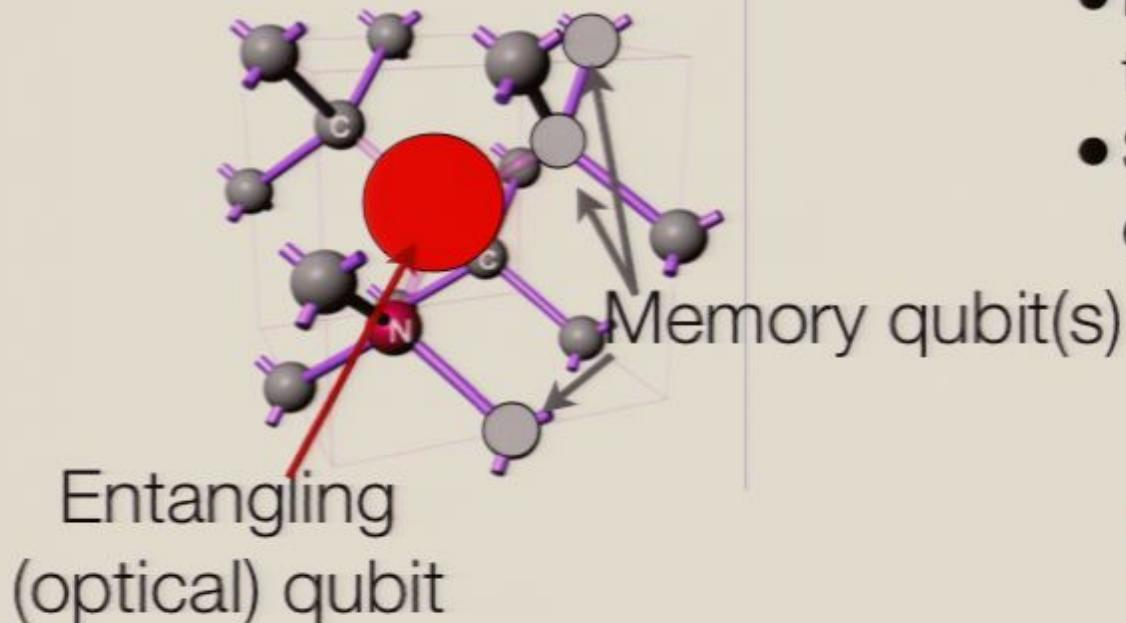
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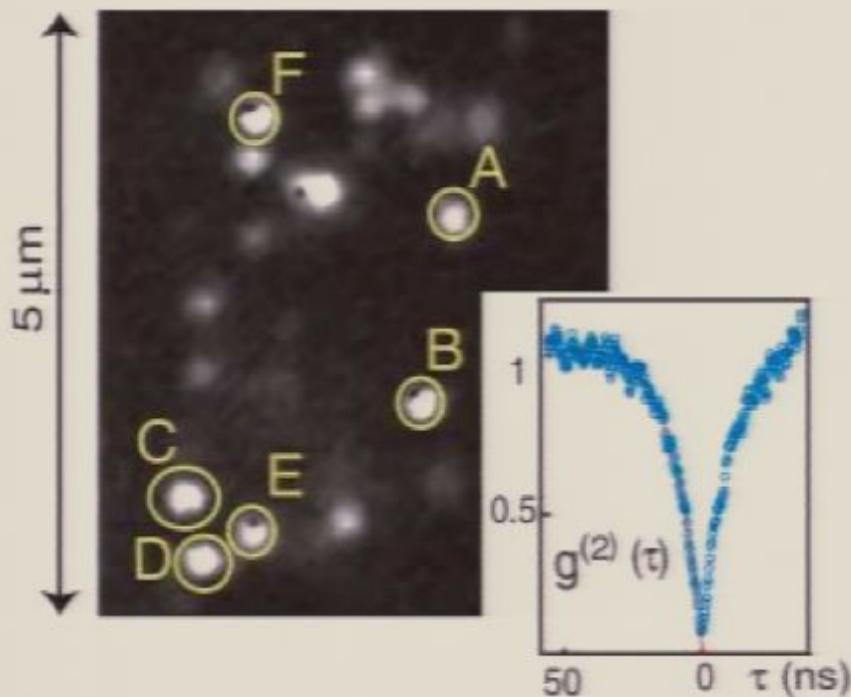
- $^{13}\text{C}$  provides NMR-based memory
- Dipolar/hyperfine coupling to electron spin
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**NMR molecule  
in a lattice**

# State-selective fluorescence

[ Lenef & Rand; Kennedy; Jelezko; Grangier; ... ]

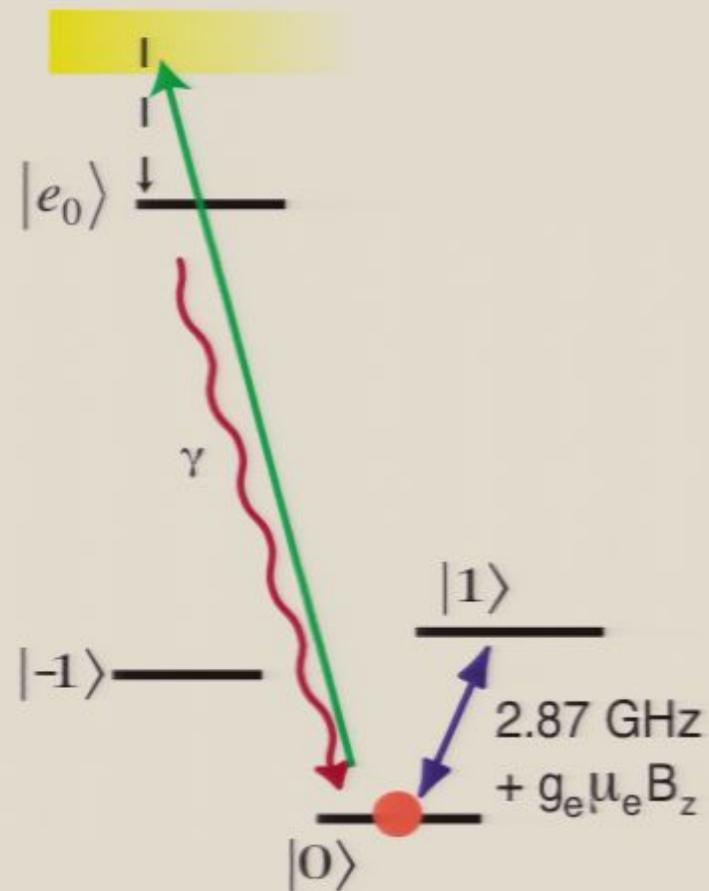
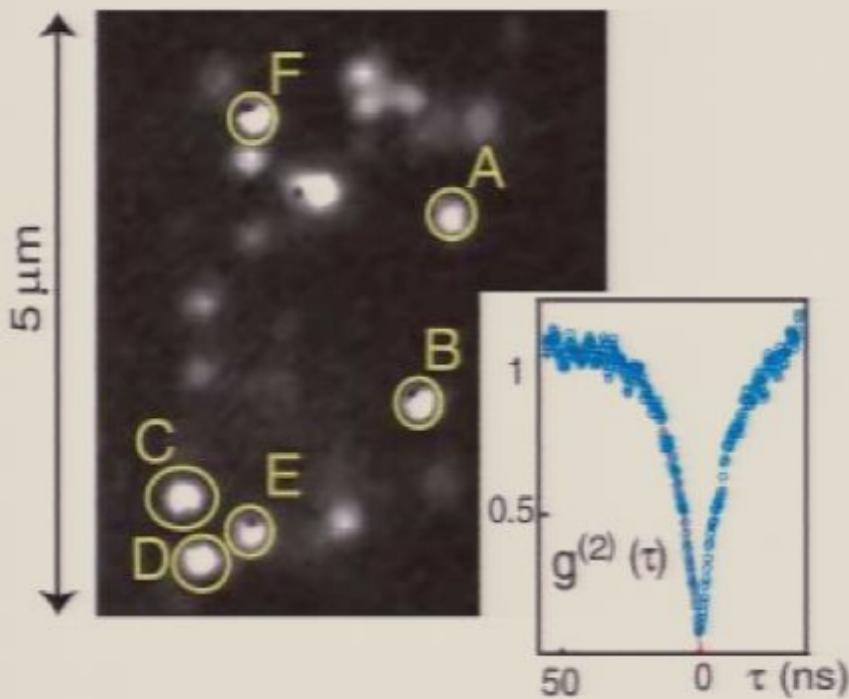
Confocal microscope  
image and  $g^{(2)}$



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[ Lenef & Rand; Kennedy; Jelezko; Grangier; ... ]

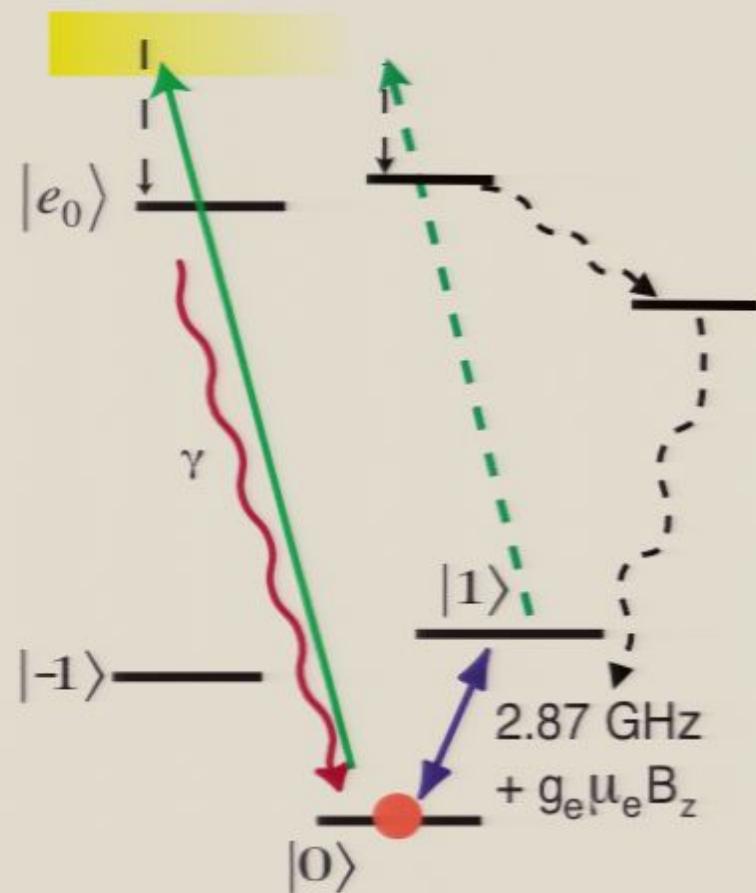
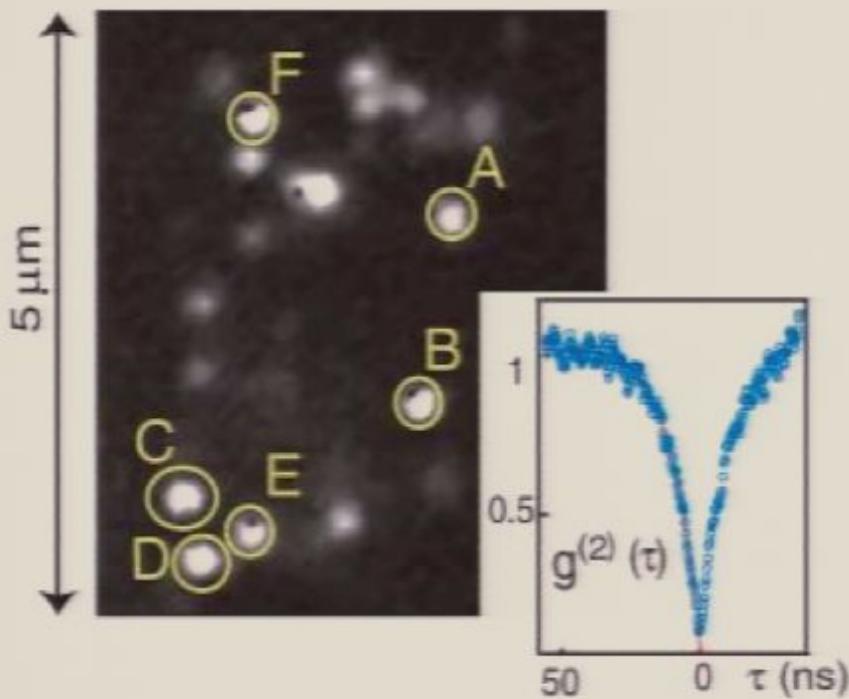
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[ Lenef & Rand; Kennedy; Jelezko; Grangier; ... ]

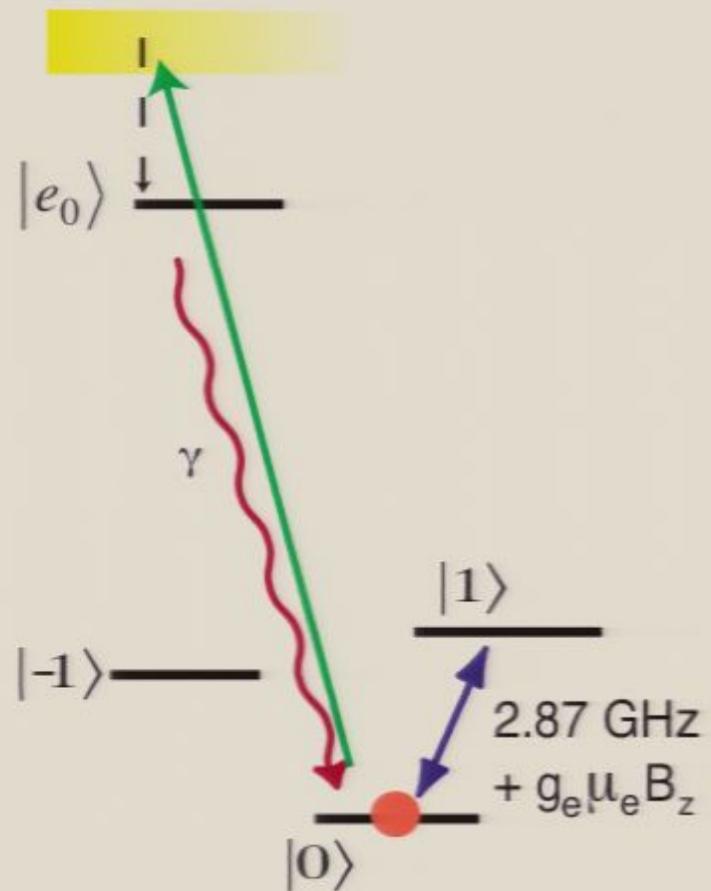
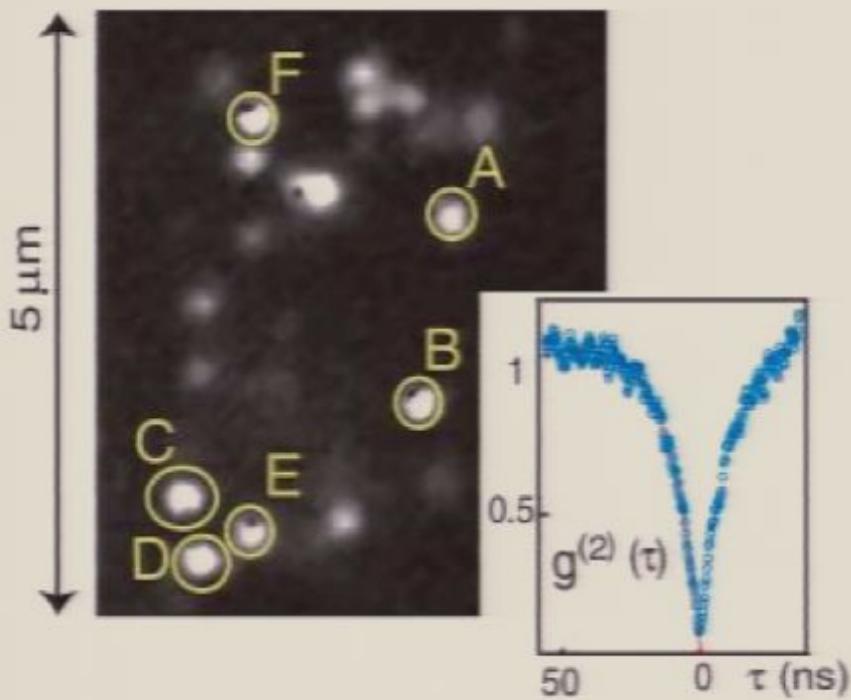
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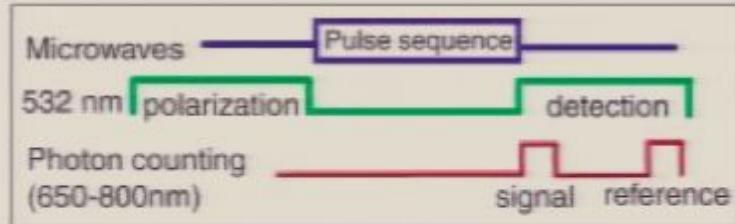
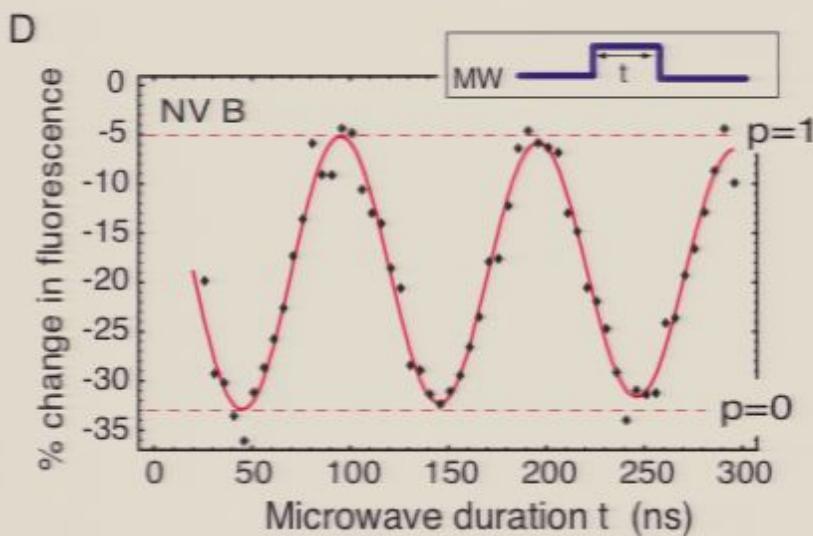
[ Lenef & Rand; Kennedy; Jelezko; Grangier; ... ]

Confocal microscope  
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# Optically detected single-center ESR

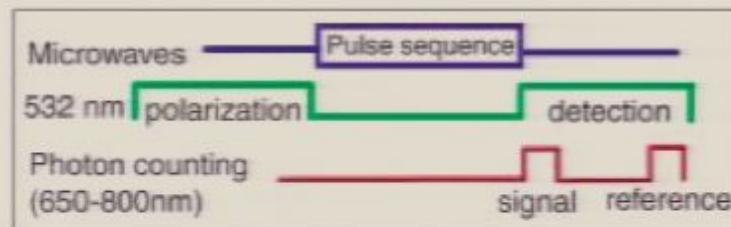
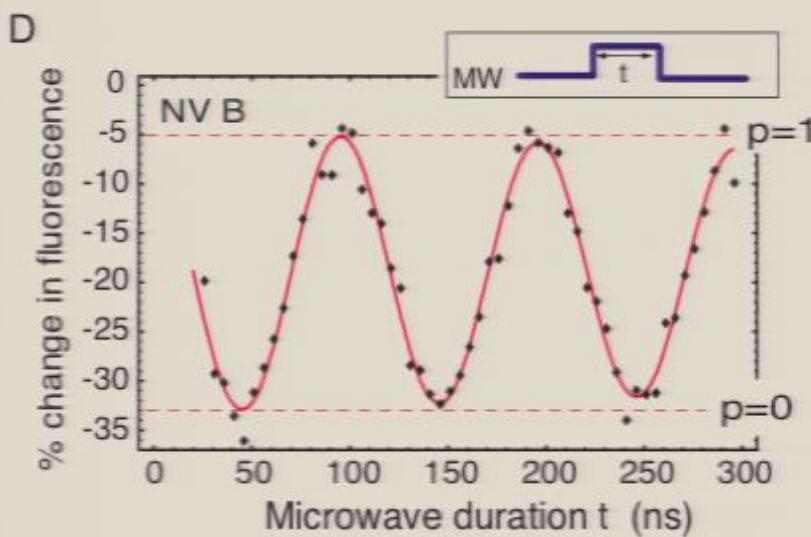
[ Childress et al. Science (2006) ]



- Driven oscillations (Rabi)

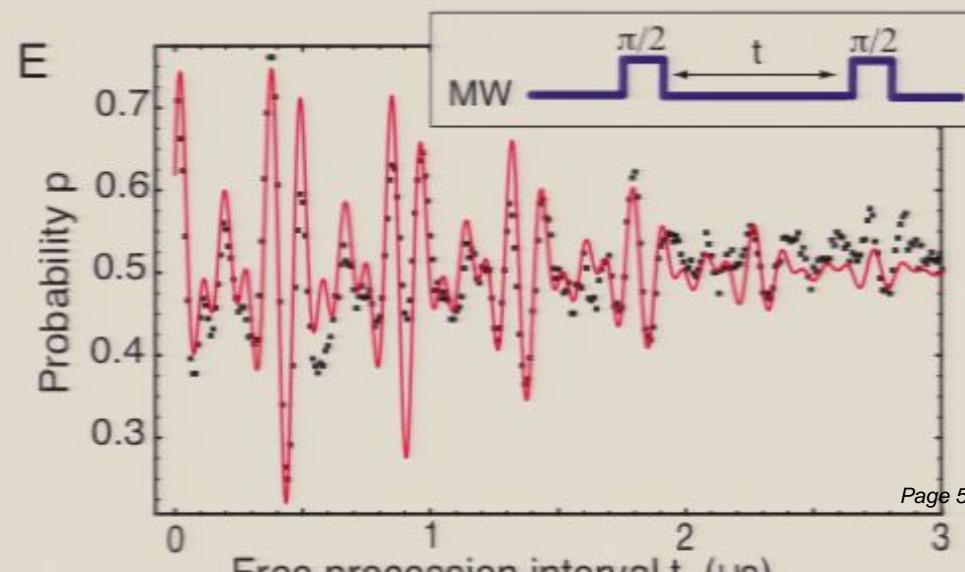
# Optically detected single-center ESR

[ Childress et al. Science (2006) ]



- Driven oscillations (Rabi)

- Free precession (Ramsey)



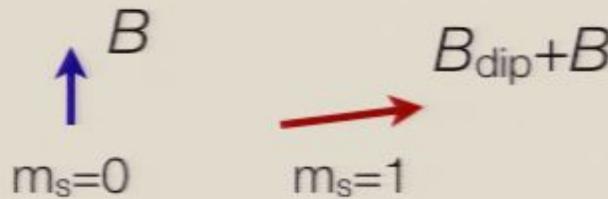
# Electron spin echo

- Electron spin–nuclear spin dipole-dipole interaction

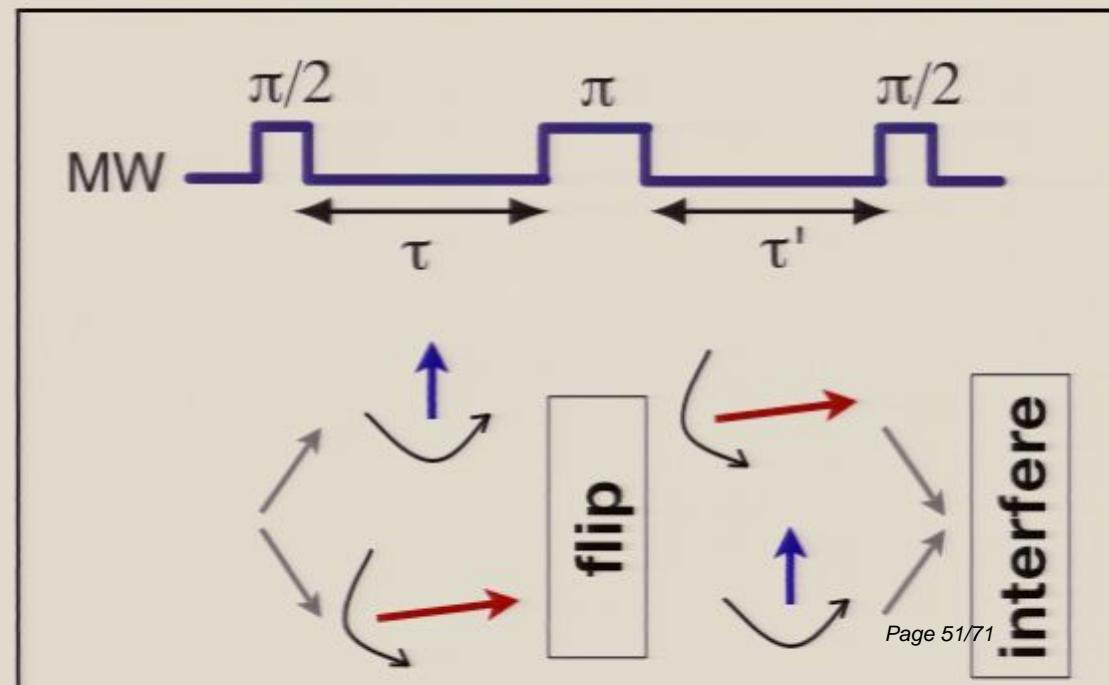
$$\hat{H} = \Delta \hat{S}_z^2 - B_z \hat{S}_z + \hat{S}_z \sum_k \alpha_{z\nu}^k \hat{I}_\nu^k + \gamma_{\text{nuc}} \sum_k \vec{B} \cdot \hat{\vec{I}}^k$$

- For nuclear spin  $j$

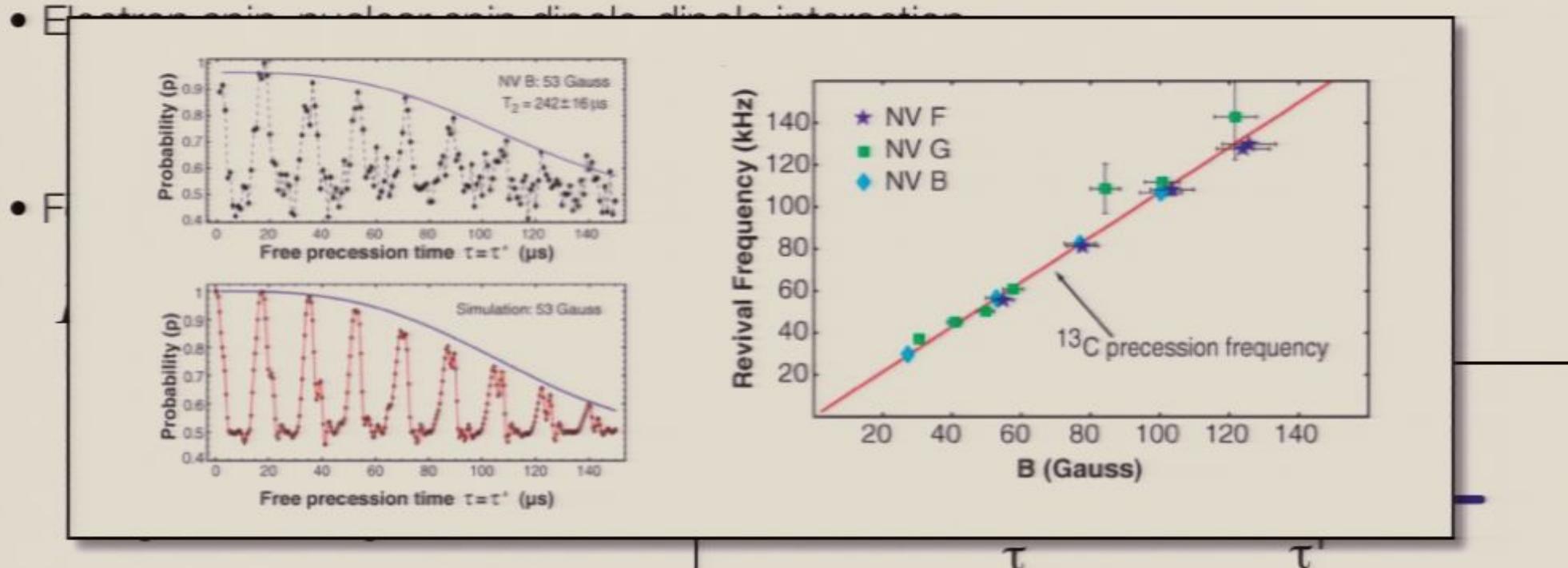
$$\hat{H}^j = \hat{S}_z \vec{B}_{\text{dip}}^j \cdot \hat{\vec{I}}^j + \gamma_{\text{nuc}} \vec{B} \cdot \hat{\vec{I}}^j$$



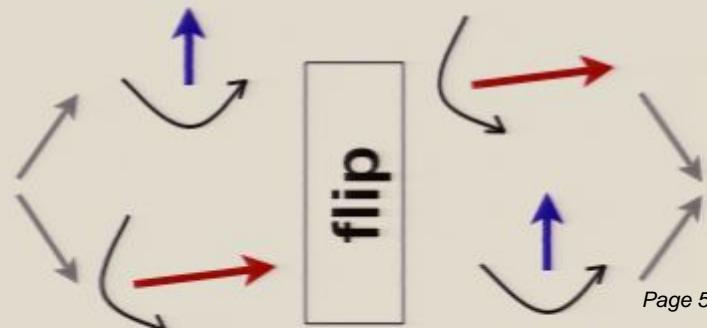
- Coupling leads to echo decay  
[ Mims 1977, van Oort et al. 1989,  
Childress et al. Science (2006) ]



# Electron spin echo



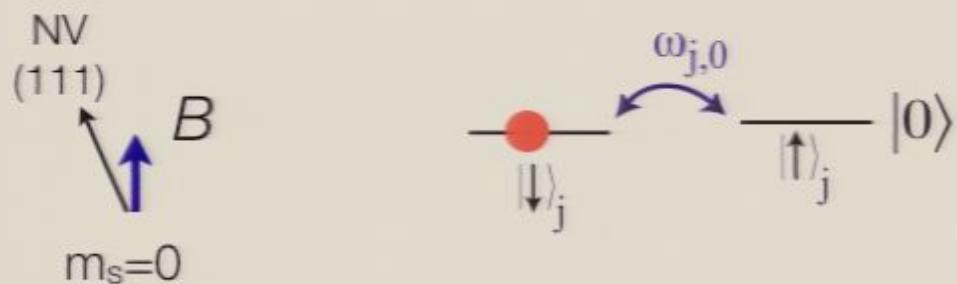
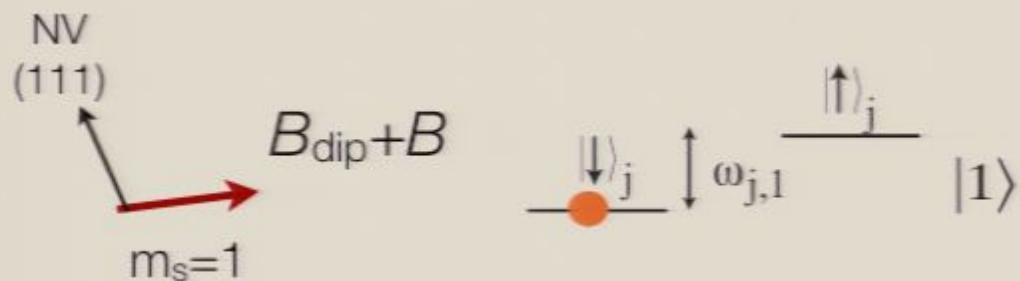
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# Local addressing of Carbon-13

Recall: large 0–1 splitting (RWA)

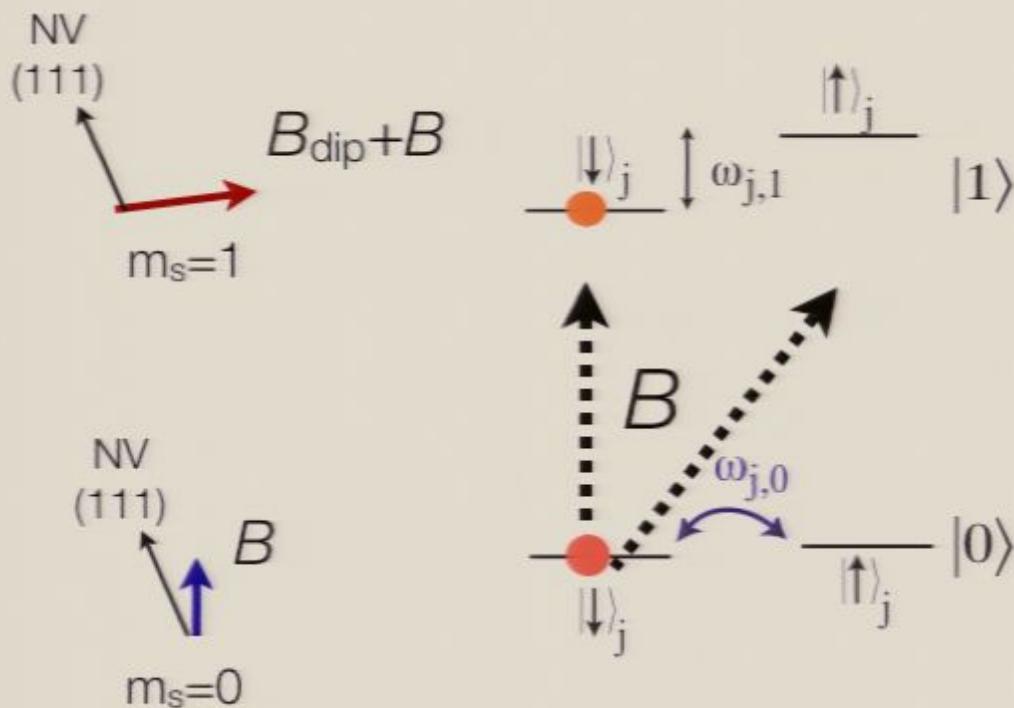
- First correction  $\sim B_{xy}$



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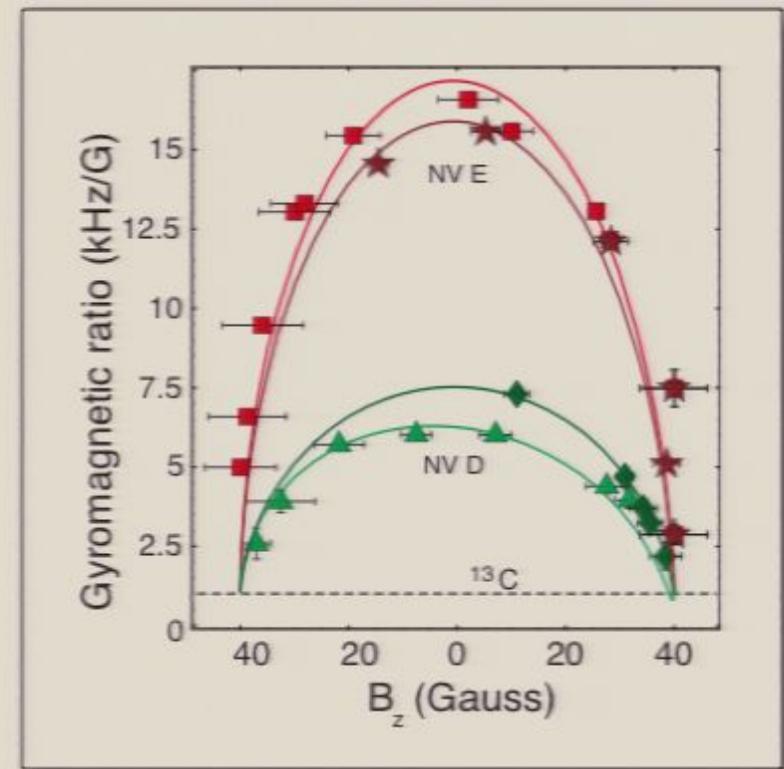
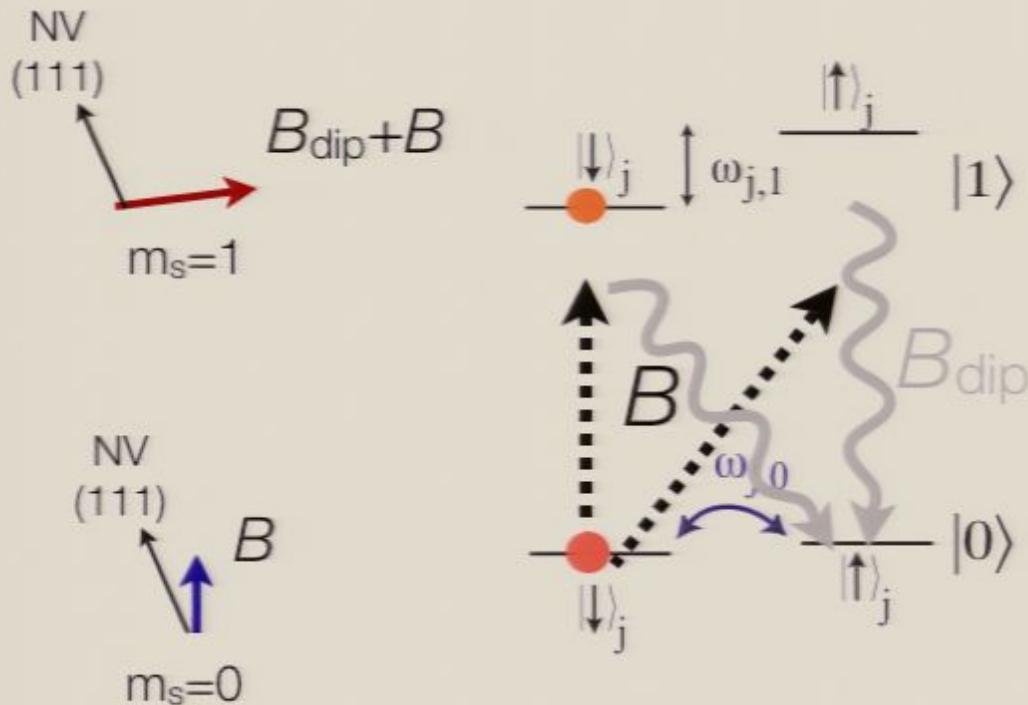
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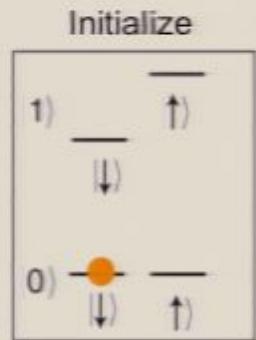
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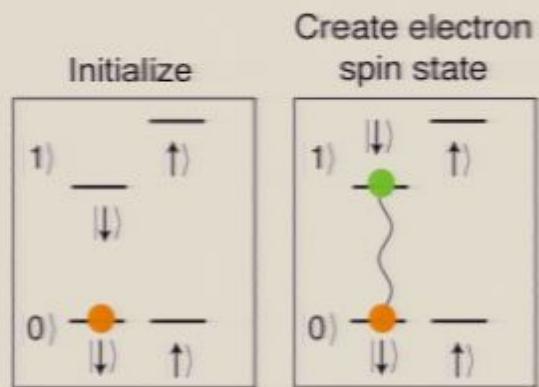
# A $^{13}\text{C}$ quantum memory

[ Dutt et al., Science (2007) ]



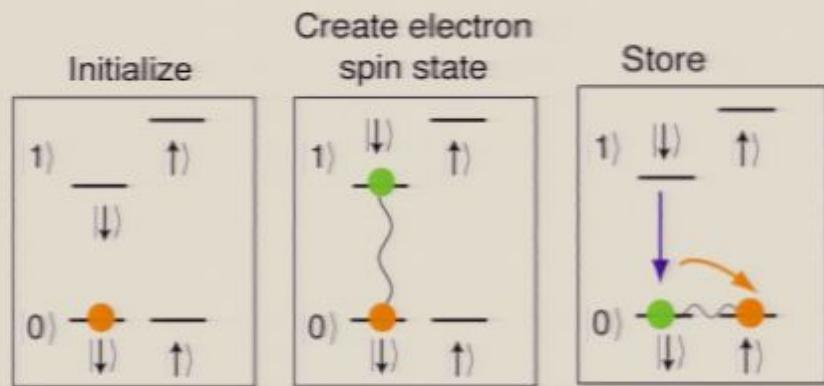
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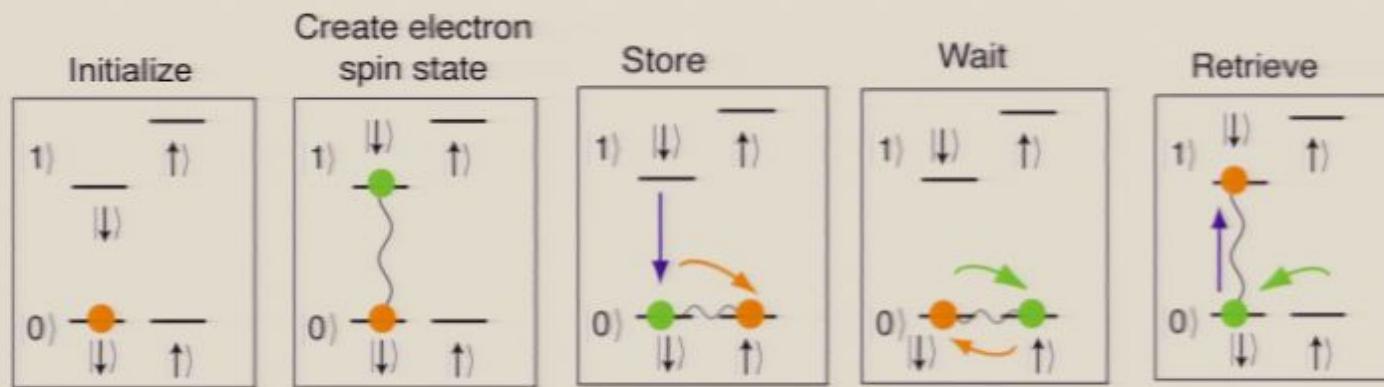
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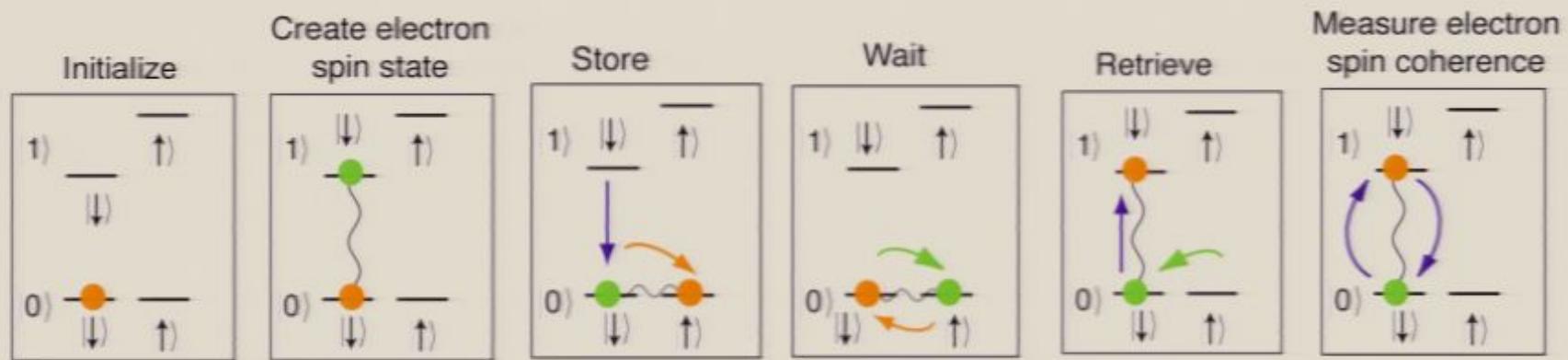
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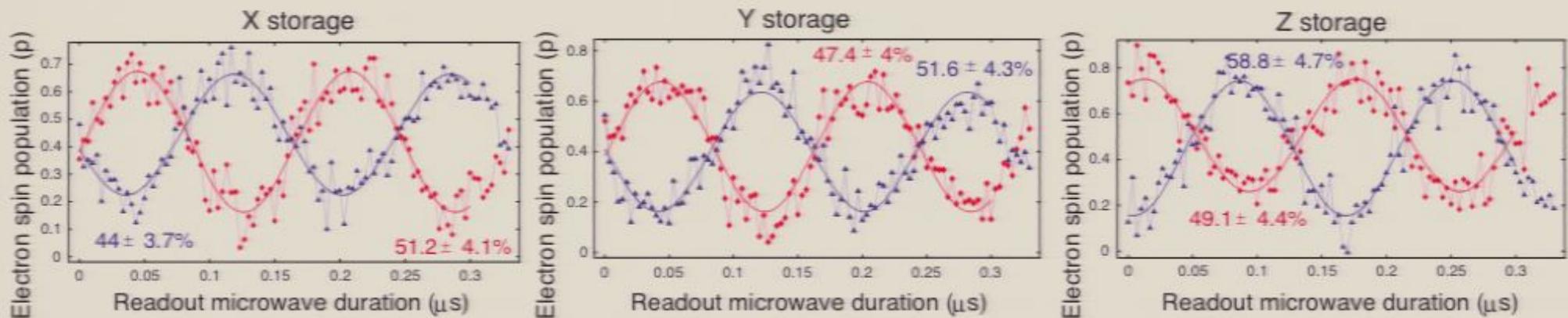
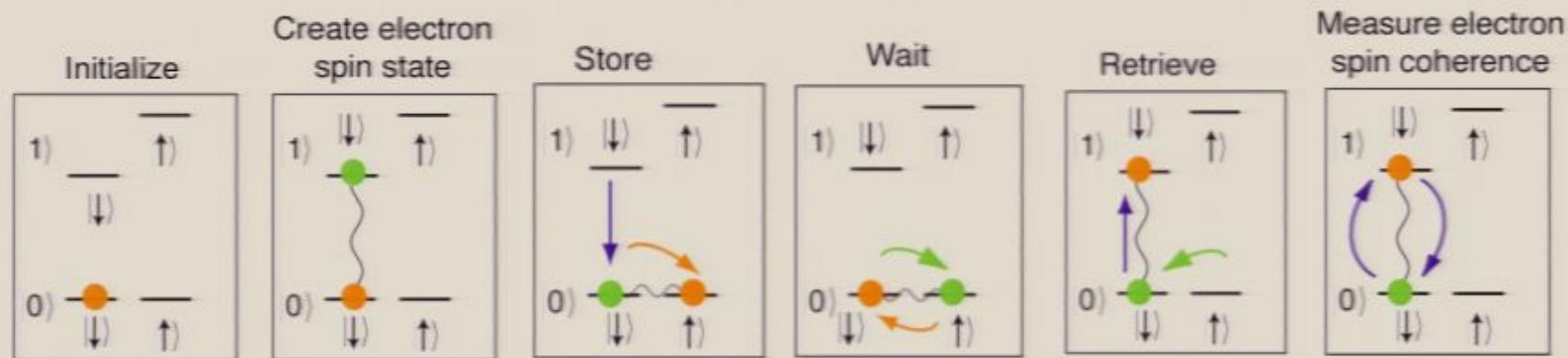
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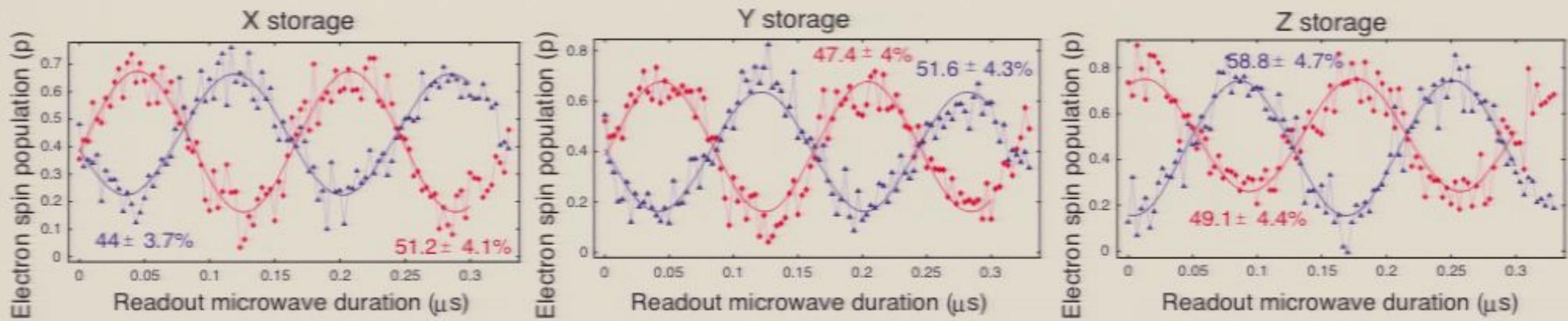
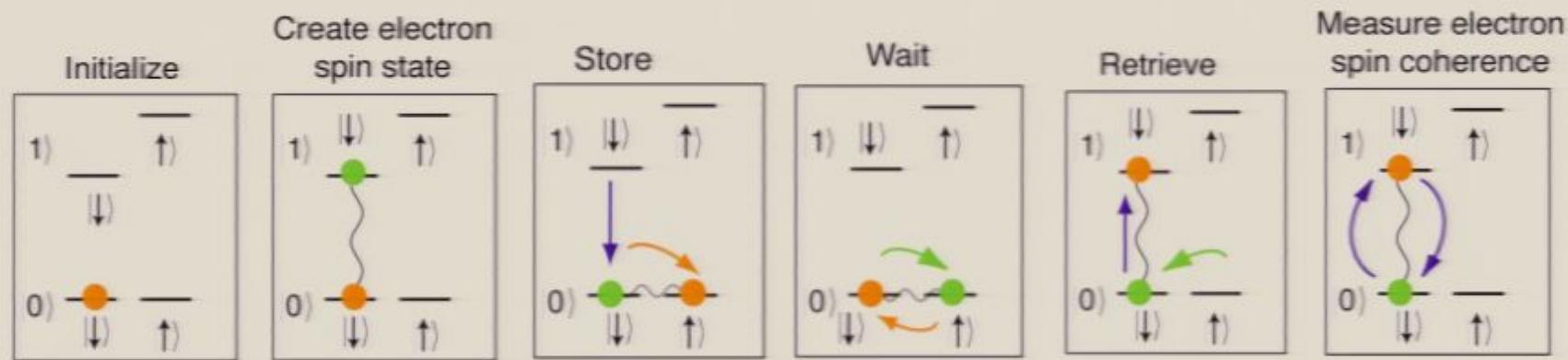
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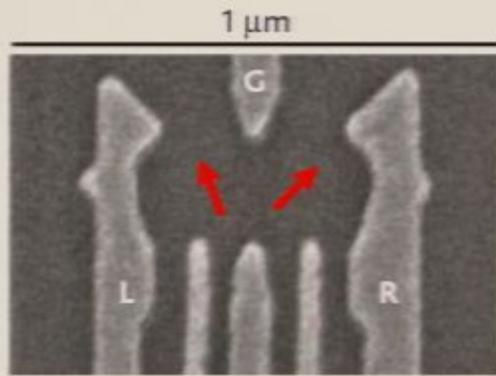
# A $^{13}\text{C}$ quantum memory

[ Dutt et al., Science (2007) ]



- Storage fidelity  $F \sim 0.75$
- NMR echo lifetime  $>> 2 \text{ ms}$

# Other directions? Spins in quantum dots



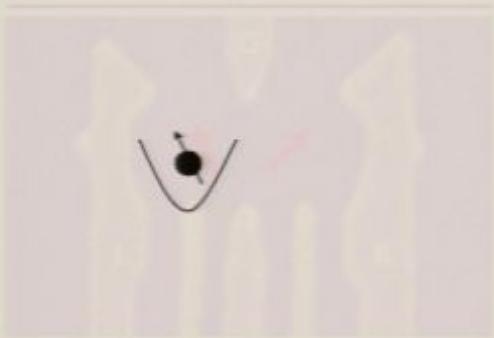
Local confinement in a semiconductor

- Trap single electrons in controlled potentials
- Electron spin provides a quantum bit

[ Loss & DiVincenzo 1998 ]

$$|“0”\rangle = |\uparrow\rangle, |“1”\rangle = |\downarrow\rangle$$

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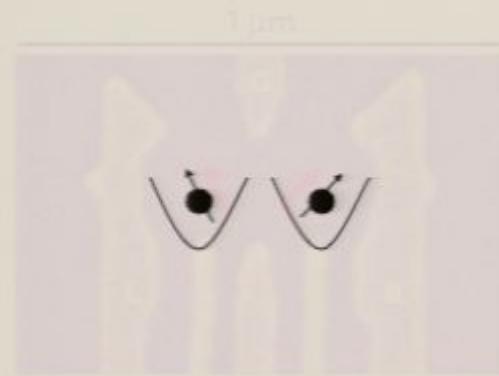
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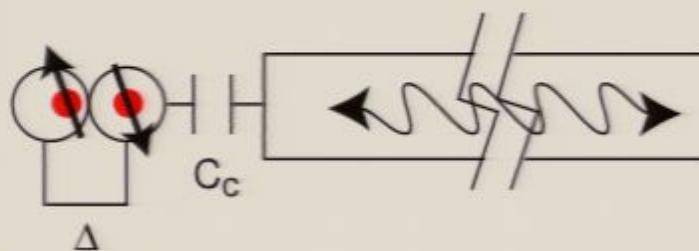
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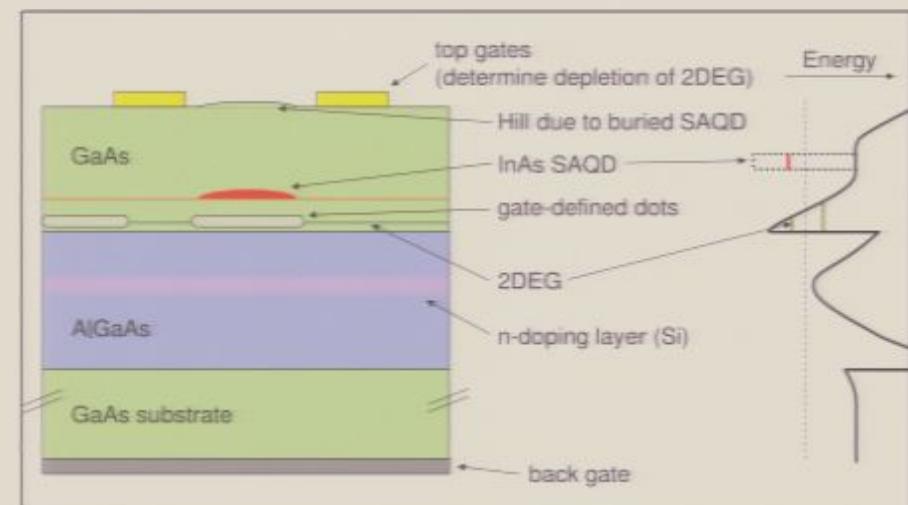
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Couple to photons or phonons

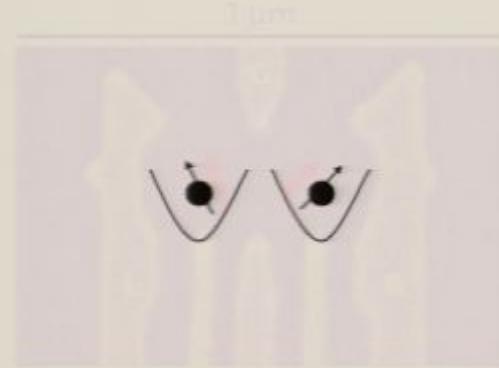


[ Burkard & Imamoglu, PRB (2006),  
Taylor & Lukin, cond-mat/0605144 ]



[ Engel et al., cond-mat/0612700 ]

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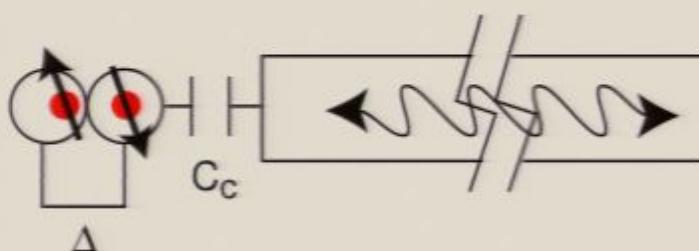
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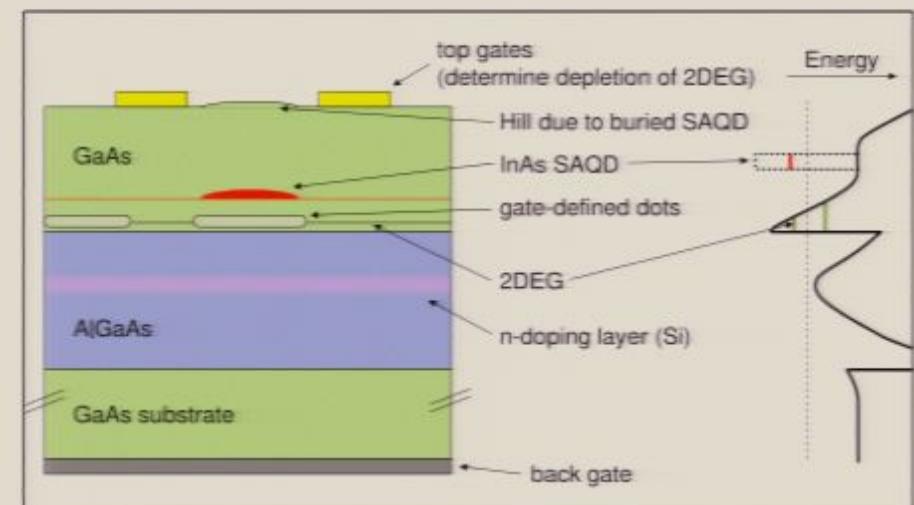
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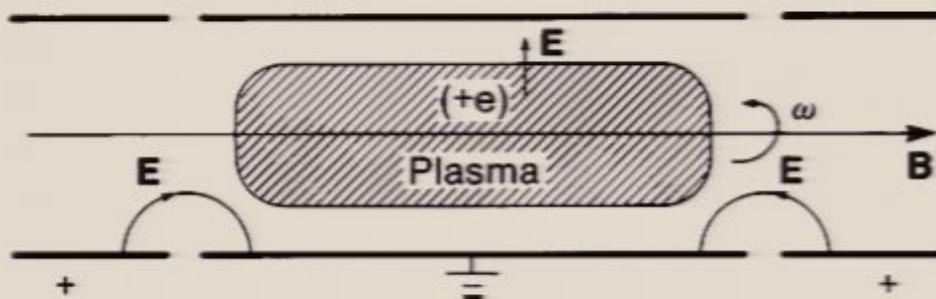


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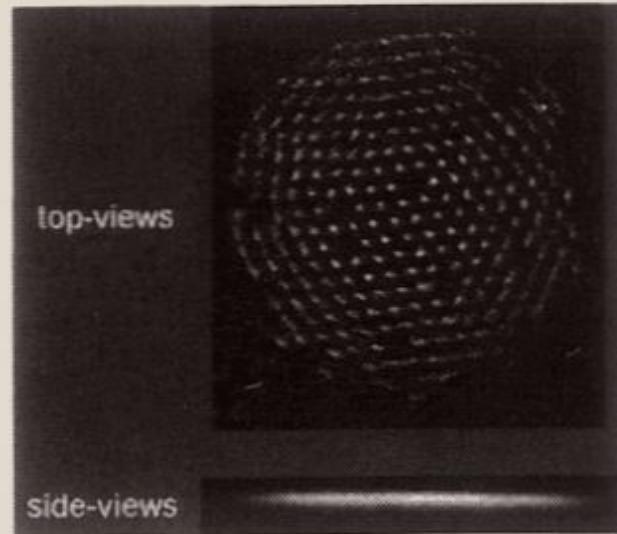
# Other directions? Wigner crystals of ions



[ Dubin & O'Neil, RMP (1999) ]

Progress toward making spin squeezed states with ions in a  
Penning-Malmberg trap.

N. Shiga, W.M. Itano and J.J. Bollinger  
*National Institute of Standard and Technology,  
325 Broadway, Boulder, CO 80305, USA*  
e-mail: shiga@boulder.nist.gov



[OCMC 2006]

## Advantages:

- many ions (good memory)
- self-organized, stable
- optically resolved sites

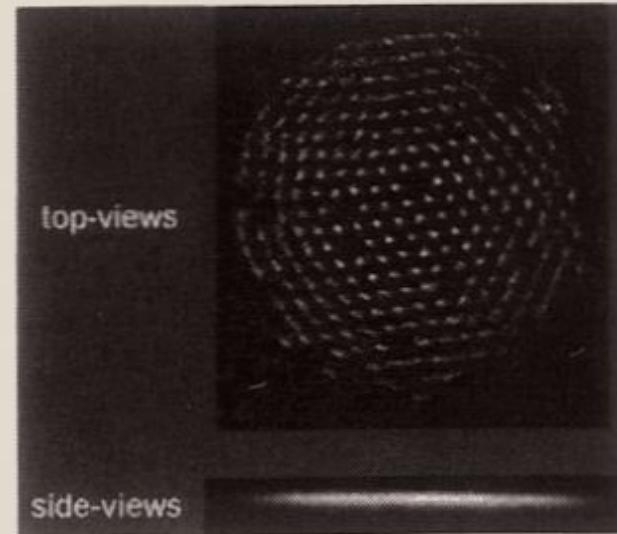
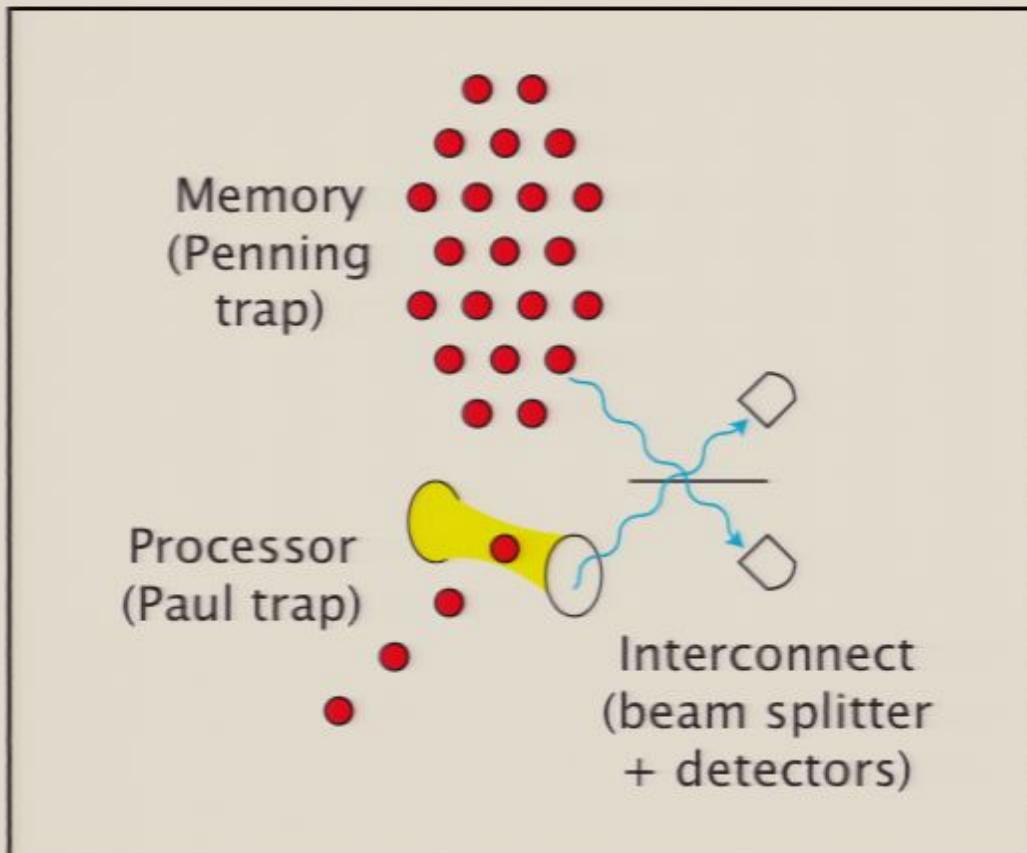
## Problems:

- high temperature
- finite size
- low collection efficiency

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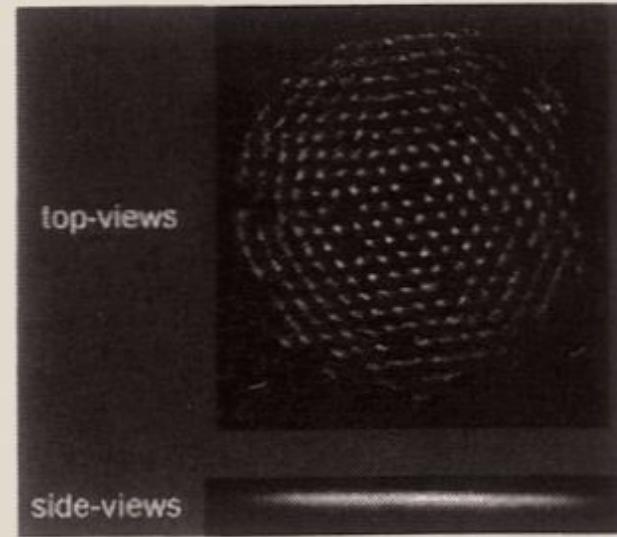
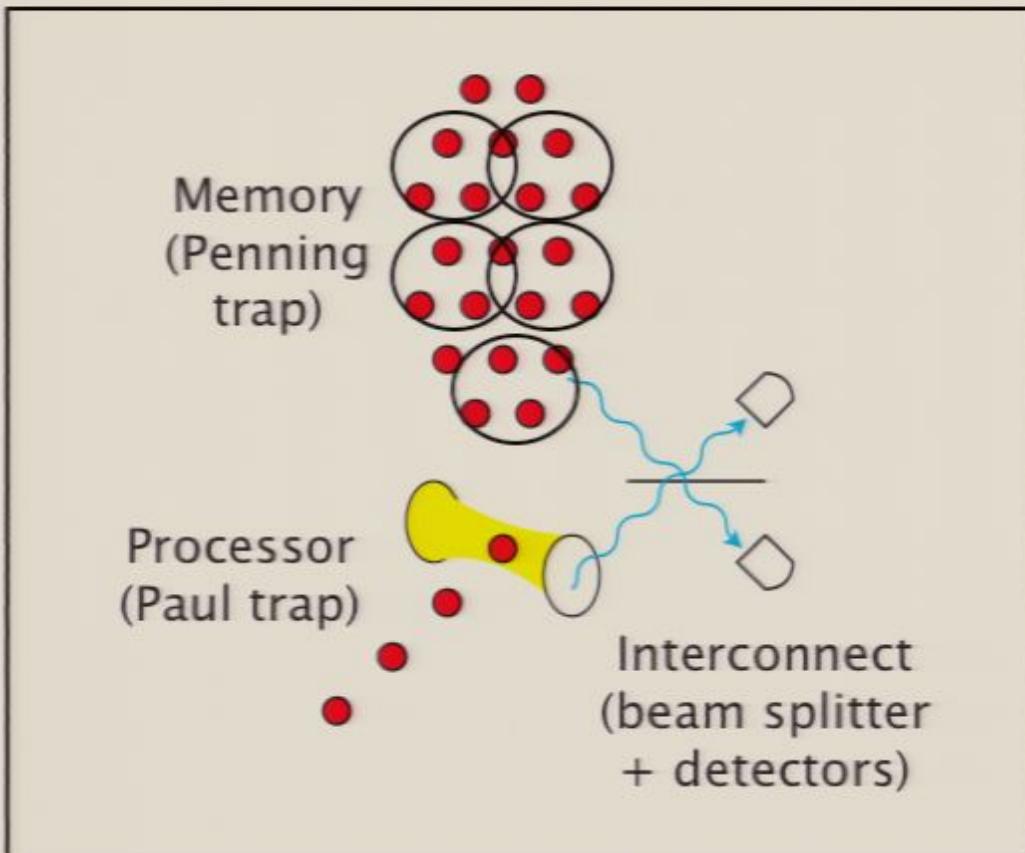
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## Problems:

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- finite size
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# Outlook

---

- Few qubit register sufficient for computation

Use remote CNOTs,  
purification =>  
*high fidelity,*  
*deterministic CNOT*  
*possible*

*Application in:*  
ion-based computation  
(linear Paul traps + cavities)  
NV centers  
Quantum dots  
Neutral atoms?  
Superconducting qubits??  
???

- Progress in implementations

Long memory times, some local operations demonstrated

*but, still need atom-atom entanglement generation,*  
*more qubits per node*

# Collaborators

Harvard:

T. Calarco

J. R. Petta (->Princeton)

D. Reilly

A. C. Johnson

E. A. Laird

A. Yacoby (<- Weizmann)

C. M. Marcus

H.-A. Engel

L. Jiang

L. I. Childress

M. G. Dutt

A. S. Zibrov

M. D. Lukin

\$\$\$: Pappalardo, ARO,  
DARPA-QIST, NSF, ...

Elsewhere:

W. Dür

P. Zoller (Innsbruck)

A. Imamoglu (ETH Zürich)

C. Flindt

A. Sørensen (NBI Copenhagen)

F. Jelezko

J. Wrachtrup (Stuttgart)

P. R. Hemmer (Texas A&M)

M. P. Hanson

A. C. Gossard (UCSB)